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**NOTE ON THE EFFECT OF MERIDIAN CURVATURE**

Supplement to  
**POTENTIAL FLOW THROUGH RADIAL FLOW TURBOMACHINE ROTORS**

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## Abstract

The effect of meridian curvature in a centrifugal impeller is estimated by assuming that the meridian streamlines may be replaced by "two-dimensional" surfaces of revolution. For the analysis, a shape was chosen that made the potential flow on this surface easy to solve. It is found that the slope of the streamline at the blade inlet is quite important for the determination of the flow-rate for shockless entry. If the solidity is somewhat greater than unity, the shockless condition is relatively independent of the exit inclination. The head, however, shows little dependence on the inlet, but is a function of the exit slope.

## Introduction

The theoretical operating characteristics of radial flow centrifugal pump impellers with small variations in breadth and vane angle have been worked out previously.<sup>1</sup> These calculations were intended primarily for straight radial meridian profiles although it was shown how they could be applied (in the case of small constant breadth) to conical shapes. It is well known that most impellers of the so-called Francis type have appreciable meridian curvatures in which the exit is more or less radial and the inlet may be nearly axial. This present note is a continuation of the work in Reference 1 and is intended to show the effect of this curvature on the characteristics of the impeller. For this purpose, the meridian flow is assumed to occur on a "two-dimensional" surface of revolution. Furthermore, two adjacent meridian streamlines are presumed to be a constant infinitesimal distance  $dh$  apart (Fig. 1), so that complex variable theory can be used.

If  $dh$  is not constant, the stream function will not satisfy Laplace's equation and the problem becomes much more difficult. However, in this event, further corrections can still be made as are indicated in (1). The impeller may be thought of as consisting of a number of such surfaces, so that a "psuedo-three-dimensional" solution could be constructed for any given design. In the development that follows, however, only one meridian stream surface will be considered.

### Formulation of the Problem

Consider the two-dimensional surface of revolution shown in Fig. 2 where the equation of the surface is

$$z = f(R) . \quad (1)$$

The flow on this surface is assumed to satisfy all of the requirements of a potential flow, i. e., it is frictionless, irrotational, and incompressible. Thus, if  $F$  is the potential of the flow, then it must satisfy Laplace's equation on the surface. In curvilinear coordinates  $x_1, x_2$ , this equation is<sup>2</sup>

$$\frac{\partial}{\partial x_1} \left( \frac{h_2}{h_1} \frac{\partial F}{\partial x_1} \right) + \frac{\partial}{\partial x_2} \left( \frac{h_1}{h_2} \frac{\partial F}{\partial x_2} \right) = 0 . \quad (2)$$

Let  $x_2 = \theta$  be the polar angle, and  $x_1 = s$ , the arc distance along a meridian ( $\theta = \text{constant}$ ). Since an element of distance is

$$dS^2 = ds^2 + R^2 d\theta^2$$

then

$$h_1 = 1 ; \quad h_2 = R .$$

Thus

$$R \frac{\partial}{\partial s} \left( R \frac{\partial F}{\partial s} \right) + \frac{\partial^2 F}{\partial \theta^2} = 0$$

where  $R = R(s)$  is the question to be solved. It is more convenient to map the  $(s, \theta)$  coordinates into polar coordinates  $(y, \theta)$ , where Eq. (2) assumes the form

$$y \frac{\partial}{\partial y} \left( y \frac{\partial F}{\partial y} \right) + \frac{\partial^2 F}{\partial \theta^2} = 0 . \quad (3)$$

The connection between  $s, R,$  and  $y$  is

$$\frac{dy}{y} = \frac{ds}{R} = \frac{dR}{R} \left[ 1 + \left( \frac{dz}{dR} \right)^2 \right]^{1/2}$$

or

$$\ln y = \int \frac{dR}{R} \left[ 1 + \left( \frac{dz}{dR} \right)^2 \right]^{1/2} \quad (4)$$

Also

$$s = \int dR \left[ 1 + \left( \frac{dz}{dR} \right)^2 \right]^{1/2} \quad (5)$$

The relation between the  $(s, \theta)$  and  $(y, \theta)$  planes is a conformal one so that an impeller blade of constant angle  $\gamma$  defined by

$$\tan \gamma = R d\theta/ds$$

is mapped into a logarithmic spiral in the  $(y, \theta)$  plane.

#### Boundary Conditions

In the  $(s, \theta)$  plane let  $V_{ns}$  be the normal velocity component and  $V_{ny}$  be the normal component in the  $(y, \theta)$  plane. Then

$$V_{ny} = V_{ns} \frac{\partial s}{\partial y} = V_{ns} \frac{\partial s}{\partial R} \frac{\partial R}{\partial y} \quad (6a)$$

or

$$V_{ny} = V_{ns} \frac{R}{y} \quad (6b)$$

For an impeller the total flow is composed of the through flow and the displacement flow. The through flow consists of the flow originating from a source vortex in the  $(y, \theta)$  plane and is mapped onto the physical plane by Eqs. (4), (5). The displacement flow arises from rotation of the vanes with no net discharge. At any point on the blade surface the normal velocity component must satisfy the condition (Fig. 2)

$$V_{ns} = R\omega \cos \gamma .$$

Thus,

$$V_{ny} = \frac{R^2}{y} \omega \cos \gamma \quad (7)$$

is the boundary condition imposed in the  $(y, \theta)$  plane. In this plane, the blade will appear as a logarithmic spiral for which suitable transformations are available.

## Applications

### A. Francis-type Impeller

In this type of impeller the exit is nearly radial and the inlet may vary anywhere from axial to near radial as seen in Fig. 1. From Eqs. (4) and (7) it is seen that rather difficult boundary conditions may occur in the  $(y, \theta)$  plane depending on the exact shape of the streamline contour. In this work the item of major interest is the axial inclination of the inlet ( $\delta_1$ ) and not the particular shape by which this slope is achieved. It is supposed for the present that the details of the profile shape are not of crucial importance, particularly for impellers of high solidity. Later, this contention will be supported by comparing the results of two different shapes.

In view of these remarks it seems reasonable to choose that contour which will give the simplest boundary condition in the  $(y, \theta)$  plane and still give a streamline shape that has a continuous smooth curvature from inlet to exit. A simple relation that still preserves the axial to radial transition is

$$y^2 = R^2 - R_i^2 \quad (8)$$

where  $R_i$  is a constant. Equation (7) gives

$$V_{ny} = \omega \cos \gamma \left[ \frac{R_i^2}{y} + y \right] \quad (9)$$

The first term is the boundary condition for an axial impeller (or cascade) of straight blades. The second term is the boundary condition for a strictly radial impeller.

The relation between  $z$  and  $R$  is given by Eq. (4), i. e.,

$$\frac{dy}{y} = \frac{dR}{R} \left[ 1 + f'^2 \right]^{1/2}$$

or with Eq. (8)

$$f'(R) = \frac{dz}{dR} = \left[ \frac{R^4}{(R^2 - R_i^2)^2} - 1 \right]^{1/2} \quad (10)$$

The integral of Eq. (10) is plotted in Fig. 3 and the angle  $\delta_1$  is given in Fig. 4 as a function of  $R/R_i$ . The constant,  $R_i$ , is the value of the radius for which the streamline becomes axial. Although the shape given in Fig. 3 has a much smaller radius ratio than is typical of pump designs, it will be seen that it is still useful for the determination of the effect of  $\delta_1$ .

#### 1. Displacement Flow

In order to present the results in dimensionless form, consider the new variable

$$r = \frac{y}{R_2} \left/ \left[ 1 - \left( \frac{R_i}{R_2} \right)^2 \right]^{1/2} \right. \quad (11)$$

Then

$$V_{nr} = \frac{V_{ny}}{R_2} \cdot \frac{d(y/R_2)}{dr} \quad (12)$$

or

$$V_{nr} = \cos \gamma \left\{ \frac{(R_i/R_2)^2}{r} + \left[ 1 - \left( \frac{R_i}{R_2} \right)^2 \right] r \right\} \quad (13)$$

With these substitutions  $r = 1$  when  $R/R_2 = 1$ , and all velocities are now expressed in terms of the tip speed  $R_2$  of the impeller.

The blades appear as logarithmic spirals in the  $(r, \theta)$  plane, and because of that fact this plane can be easily transformed into one in which the blade system appears as a circle. In this latter plane the solution to the boundary value problems given by Eq. (13) is relatively simple. As previously noted, the second term represents the conventional radial flow theory whereas the first term is the same as that due to a source flow at the origin. Both of these results are given in Ref. 1 in a form most useful for presentation here.

In this way the effect of meridian curvature can be obtained by "fairing together" two known solutions in the  $(r, \theta)$  plane by means of Eq. (13). The relation between the actual geometry and the transformed radial plane  $(r, \theta)$  is given by Eqs. (4), (5), and (11).

The solution of the second term is given by Eq. (11) in Ref. 2. If subscript (2) denotes the exit and (1) the inlet, then the tangential velocity in the circle plane due to this term is

$$\left. \begin{aligned} V_{d_2} &= - \frac{\left[ 1 - \left( \frac{R_i}{R_2} \right)^2 \right]}{N \rho_2} \left[ \frac{w_c}{w_o - 1} \right]^{\bar{q}} \left[ \frac{\bar{w}_o}{w_o - 1} \right]^q \left[ 2F_1 + \frac{N}{\cos \gamma} (\rho_2 - 2 \cos \gamma) F_2 \right] \cos \gamma \\ V_{d_1} &= \frac{\left[ 1 - \left( \frac{R_i}{R_2} \right)^2 \right]}{N \rho_1} \left[ \frac{w_c}{w_o - 1} \right]^{\bar{q}} \left[ \frac{\bar{w}_o}{w_o - 1} \right]^q \left[ 2F_1 - \frac{N}{\cos \gamma} (\rho_1 - 2 \cos \gamma) F_2 \right] \cos \gamma \end{aligned} \right\} (14)$$

where  $w_o, \rho$  are constants that occur in the transformation of the  $(r, \theta)$  into the circle plane. The constant  $q$  is a function of the number of blades  $N$

and the blade angle  $\gamma$  and  $F_1, F_2$  are hypergeometric functions given by Eqs. (10) in Ref. 1.

The tangential velocity of the first (or source flow) term is readily obtained in the circle plane by letting  $m = -2$  or  $N' = \infty$  in Eq. (35), Ref. 1, to obtain

$$v_{d_2}' = - \frac{2 \cos \gamma}{N \rho_2} \left[ \frac{R_i}{R_2} \right]^2 \quad (15)$$

$$v_{d_1}' = \frac{2 \cos \gamma}{N \rho_1} \left[ \frac{R_i}{R_2} \right]^2$$

The dashes refer to the first term of the displacement flow given in Eq. (13).

### 2. Through Flow

The through flow solution in the  $(r, \theta)$  plane is not altered. In particular, the flow-rate coefficient  $\phi = V_{r_2} / V_2$  remains unchanged in going from the physical plane to the  $(r, \theta)$  plane.<sup>2</sup> The appropriate solutions are then given by Eqs. (15), Ref. 1, i. e.,

$$v_{t_2} = - \frac{Q \cos \gamma}{\pi \rho_2} (\tan \gamma - \tan \alpha_1) \quad (16)$$

$$v_{t_1} = \frac{Q \cos \gamma}{\pi \rho_1} (\tan \gamma - \tan \alpha_1)$$

where  $Q$  is the flow-rate per passage per unit width.

### 3. Shockless Entry

All the essential information is now available to make calculations of head flow-rate performance in which the effect of meridian curvature is taken into account. The first and most important item is the flow-rate for which shockless or smooth entry occurs on the Francis-type impellers.

This operating point is determined by the condition that the velocity must be zero in the circle plane at the point corresponding to the inlet of the blade.

According to Ref. 1 this occurs when

$$(V_{t_1} - V_{t_2}) + (V_{d_1} - V_{d_2}) + (V_{d_1}^i - V_{d_2}^i) = 0. \quad (17)$$

After suitable manipulation of the equations quoted above, the flow-rate coefficient  $\phi_e$  for this condition may be expressed as

$$\phi_e = \phi_{e\infty} \left[ A + \left( \frac{R_i}{R_1} \right)^2 (1 - A) \right] \quad (18)$$

where  $\phi$  is defined by

$$\phi = \frac{V_{r_2}}{U_2} = \frac{\text{Flow-Rate}}{\text{Exit Area} \times \text{Tip Speed}} \quad (19)$$

The subscript ( $\infty$ ) denotes the value of this coefficient for an infinite number of vanes, i. e.,

$$\phi_{e\infty} = - \left[ \frac{R_1}{R_2} \right]^2 / (\tan \gamma - \tan \alpha_1).$$

The term  $A$  is the ratio  $\phi_e / \phi_{e\infty}$  for a purely radial impeller, and is given in Ref. 1 as

$$A = \left. \frac{\phi_e}{\phi_{e\infty}} \right|_{\delta=0} = \frac{1}{\psi_0} \left( 1 + \frac{4\pi^2 \cos^2 \gamma}{3N^2} \right) \quad (20)$$

subject to the restriction that the solidity be greater than about 1.2. The solidity for a Francis impeller is defined as

$$\sigma = \frac{N \ln r_2 / r_1}{2\pi \cos \gamma} \quad (21)$$

Equation (18) appears to be independent of  $R_1/R_2$ . Actually,  $A$  depends on

$\sigma$  (and thus  $R_1/R_2$ ) but if the solidity is subjected to the above restriction  $A$  becomes independent of  $\sigma$  and is a function of the vane angle and number of blades alone. In fact, Eq. (20) is only an approximation for the case  $\sigma = 1.2$ , and for smaller values a more complicated relation must be used (Ref. 1).

If a large value of  $R_2/R_1$  is chosen as the tip radius in Fig. 3, the angular inclination of the exit will be essentially radial. Suppose for the moment that the radius ratio  $R_1/R_2$  of the impeller is sufficiently small so that  $\sigma \geq 1.2$ . If now,  $R_1/R_2$  is decreased below this value, the inlet edge of the blade will become more axial. Since the impeller geometry already is presumed to be such that  $A$  does not change, the sole effect on the shockless flow-rate condition is that due to a change in the inlet meridian angle  $\delta_1$ . Values of  $(R_1/R_2)$  then may be substituted into Eq. (18) and the corresponding value of  $\delta_1$  determined from Fig. 4. (Actually, for these purposes, one may just as well take  $R_2/R_1$  as infinity.)

This result is independent of the exit meridian angle  $\delta_2$  if the solidity remains high. This fact may be seen in the following way: Let  $\sigma$  have a constant value so that  $r_1 = r_1/r_2$  is also constant. Since

$$\left[ \frac{R_0}{R_1} \right]^2 = \frac{1 - r_1^2 (R_2/R_1)^2}{1 - r_1^2}$$

the value of  $A$  will stay constant if  $r_1$  is kept constant and independent of the radius ratio  $R_1/R_2$  of the impeller. Thus, for a given  $r_1$  (and therefore constant  $A$ )  $R_1/R_1$  and  $R_2/R_1$  can both approach unity and  $\delta_2$  approach  $90^\circ$  without affecting the value of  $\phi_e/\phi_{e\infty}$  as computed by Eq. (18).

Equation (18) is plotted in Fig. 5 for the case of  $N=6$ ,  $\gamma = 70^\circ$  which is typical of many pump designs. It is evident that the inlet meridian inclination  $\delta_1$  has a large effect and must be taken in account in any actual design.

#### 4. Head Flow-Rate Performance

The head developed by the impeller is usually expressed by the coefficient

$$\psi = H/U_2^2/g$$

where  $H$  is the developed head, and  $U_2$  is the tip speed of the impeller. This coefficient may be shown to be equal to

$$\psi = -N (v_{d_2} + v_{t_2})$$

$\omega$  and  $r_2$  being unity. With the aid of Eqs. (14), (15), and (16), the head flow-rate relation becomes

$$\psi = \psi_o^* - C_H \phi (\tan \gamma - \tan \alpha_1) \quad (22)$$

for backward curved impellers where

$$\psi_o^* = \psi_o \left[ 1 - \left( \frac{R_i}{R_2} \right)^2 \right] + C_H \left[ \frac{R_i}{R_2} \right]^2 \quad (23)$$

is now the shut-off head coefficient. The coefficient  $C_H$  depends on the impeller solidity and the blade angle and is usually very near unity. The term  $\psi_o$  is the shut-off head coefficient for a straight radial configuration. Graphs of both of these coefficients are given in Ref. 1.

Equation (23) is plotted in Fig. 7 for  $N = 6$  and  $\gamma = 70^\circ$  with the assumption that  $\sigma = 1.2$ .

### B. Conical Impellers

The meridian picture now appears as a simple cone. Equations (1) and (4) give

$$f'(R) = \tan \delta$$

$$r = \left[ \frac{R}{R_2} \right]^{\frac{1}{\cos \gamma}} .$$

The boundary condition for the displacement flow is

$$v_{nr} = \omega \cos \gamma r^{2 \cos \delta - 1} . \quad (24)$$

The solution of this problem is given by a value of

$$m = 2 \cos \delta - 2$$

in Eq. (35), Ref. 1. It is seen that the equivalent number of vanes to be used in Eq. (38), Ref. 1, is

$$N' = \frac{2N}{m+2} = \frac{N}{\cos \delta} \quad (25)$$

Thus, the characteristics of the conical impeller are obtained by replacing the actual number of blades by the equivalent number given by Eq. (25). The shockless entry calculation gives then

$$\frac{\phi_e}{\phi_{e\infty}} = \frac{1}{\psi_o(N')} \left[ 1 + \frac{4\pi^2 \cos^2 \gamma}{3N'^2} \right] \quad (26)$$

These results were previously obtained in Ref. 1 by a different method and also by Prof. Wislicenus in an unpublished note.

Equation (26) is plotted on Fig. 5 for the case of  $N = 6$ ,  $\gamma = 70^\circ$ . It is seen that this curve is quite close to that of Eq. (18). This agreement shows that as far as shockless entry is concerned the exact details of the meridian streamline shape are relatively unimportant and that the influence of the exit angle  $\delta_2$  is small.

The shut-off head coefficient for a conical impeller is determined by the use of the equivalent number of blades as given by Eq. 24 and Fig. 6 of Ref. 1. The effect of the cone angle on this coefficient is shown in Fig. 6 for the case  $N = 6$ ,  $\gamma = 70^\circ$  and  $\sigma = 1.2$ . The two curves are seen to agree quite closely as is reasonable for impellers of high solidity.

### Conclusions

This analysis has shown that the flow-rate for shockless entry is strongly dependent upon the inlet meridional inclination of the blade and is

relatively independent of the shape of the meridional stream surface. The shut-off head coefficient shows a similar behavior with the exit slope.

These calculations were made for a particular profile that had a continuous axial to radial curvature, and for conical profiles. The agreement between the two was sufficiently close so that the effect of inlet and exit meridional slopes may just as well be approximated by the simpler conical shape. This result should hold true at least for shroud curvatures no sharper than the particular one studied.

#### References

1. Acosta, A. J., "Potential Flow through Radial Flow Turbomachine Rotors", California Institute of Technology, Hydrodynamics Laboratory Report No. E-19.4.
2. Smythe, W. R., "Static and Dynamic Electricity", 1st ed. McGraw-Hill, 1939, p. 241.

Notations

- A - The flow-rate ratio  $\phi_e / \phi_{e\infty}$  for a radial impeller
- $C_H$  - Flow-rate correction factor
- F - Velocity potential
- g - Gravitational constant
- H - Impeller head (ft.)
- N - Number of blades
- Q - Flow rate (ft<sup>3</sup>/sec)
- R - Radial coordinate in physical plane
- r - Radius in the transformed radial plane
- s - Arc distance along a meridian
- U - Circumferential velocity ( $R\omega$ )
- V - Absolute velocity
- y - Intermediate radial variable
- z - Axial coordinate in physical plane
- 
- $\alpha$  - Angle between absolute velocity and meridian (positive increasing counter-clockwise)
- $\gamma$  - Angle between blade tangent and meridian
- $\delta$  - Angle between radial line and tangent to meridian
- $\theta$  - Polar angle about axis of rotation
- $\sigma$  - Solidity -  $\frac{N \ln r_2/r_1}{2\pi \cos \gamma}$
- $\phi$  - Flow-rate coefficient,  $\frac{\text{Discharge}}{\text{Exit area} \times \text{tip speed}} = \frac{V}{U_2}$
- $\psi$  - Head coefficient,  $H/U_2^2/g$
- $\psi_0^*$  - Shut-off head coefficient
- $\psi_0$  - Shut-off head coefficient for a purely radial impeller
- $\omega$  - Angular speed

Subscripts

- d - Refers to displacement flow
- e - Denotes shockless or smooth entry
- n - Normal component of velocity
- m - Meridional component of velocity
- r - Refers to  $(r, \theta)$  plane
- s - Refers to  $(s, \theta)$  plane
- t - Refers to through flow
- 1 - Refers to vane inlet
- 2 - Refers to vane exit or tip
- $\infty$  - Denotes the infinite vane theory

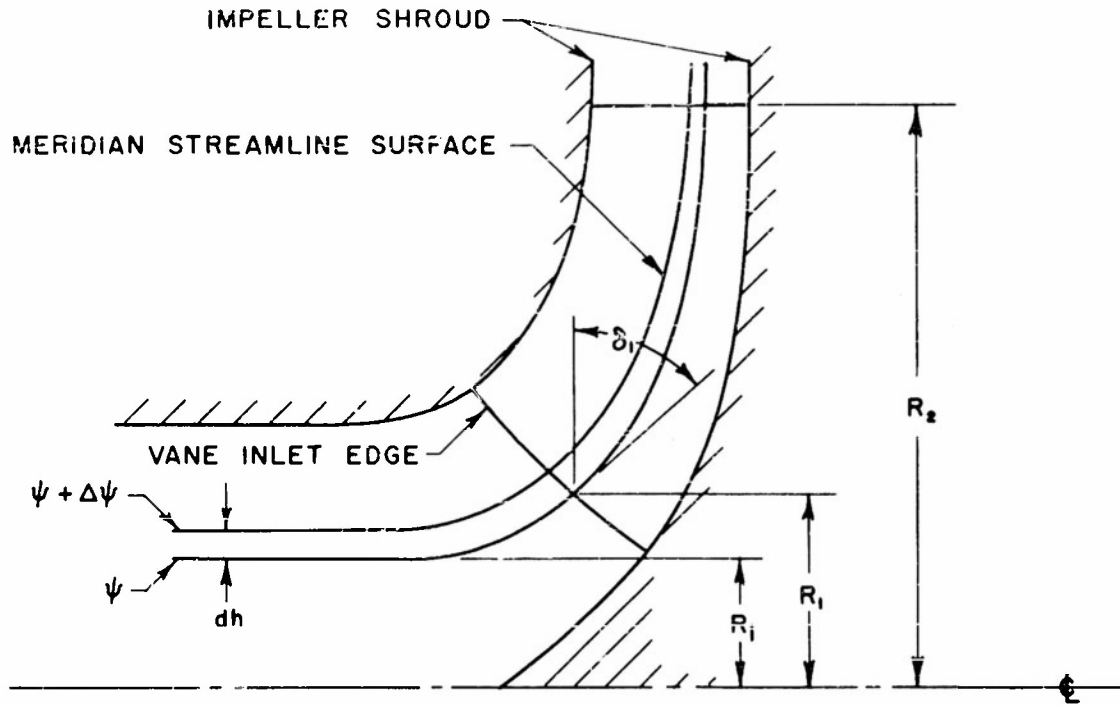


Fig. 1 - Meridian profile of a Francis type impeller.

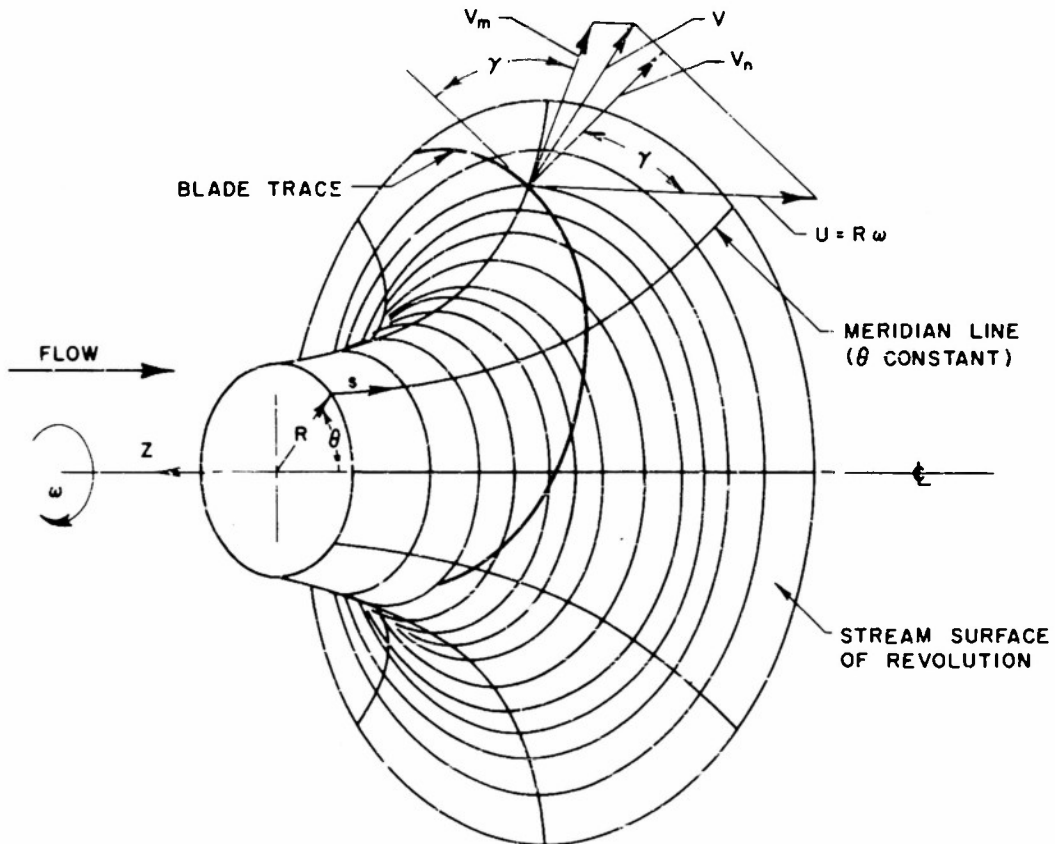


Fig. 2 - Oblique view of a typical stream surface of revolution showing the blade trace and coordinate system.

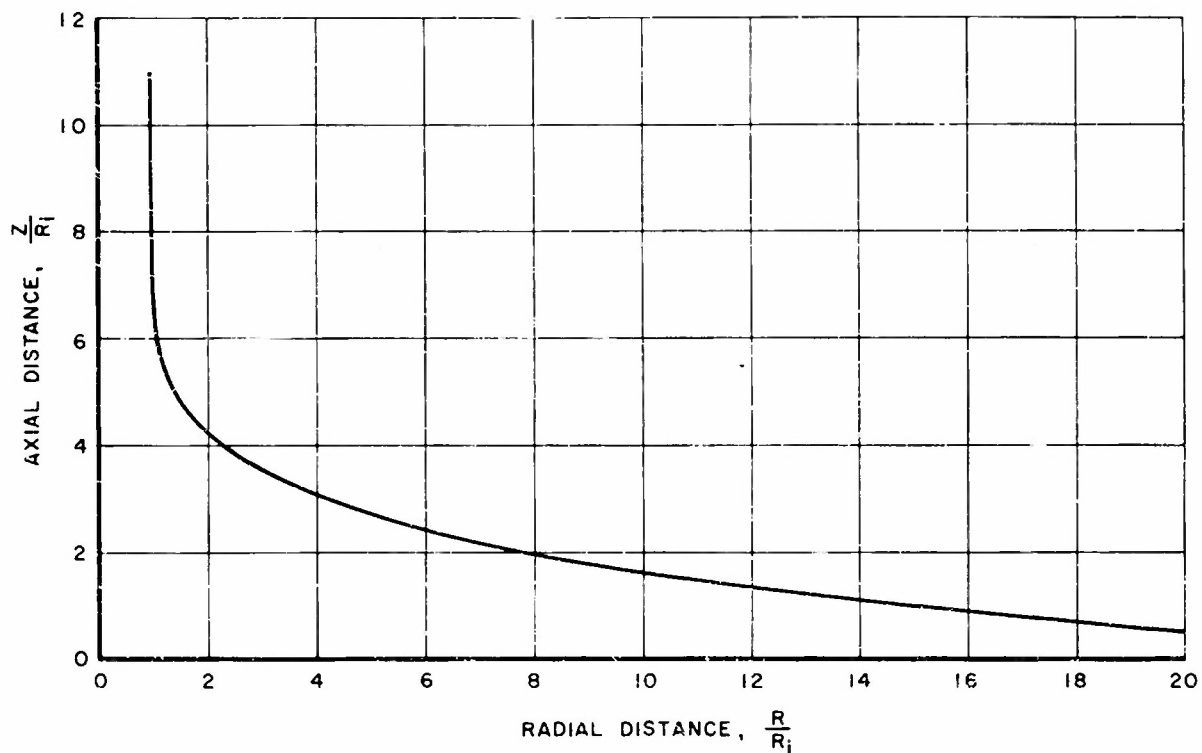


Fig. 3 - Plot of axial distance vs. radius for the special stream surface given by Eq. 10.

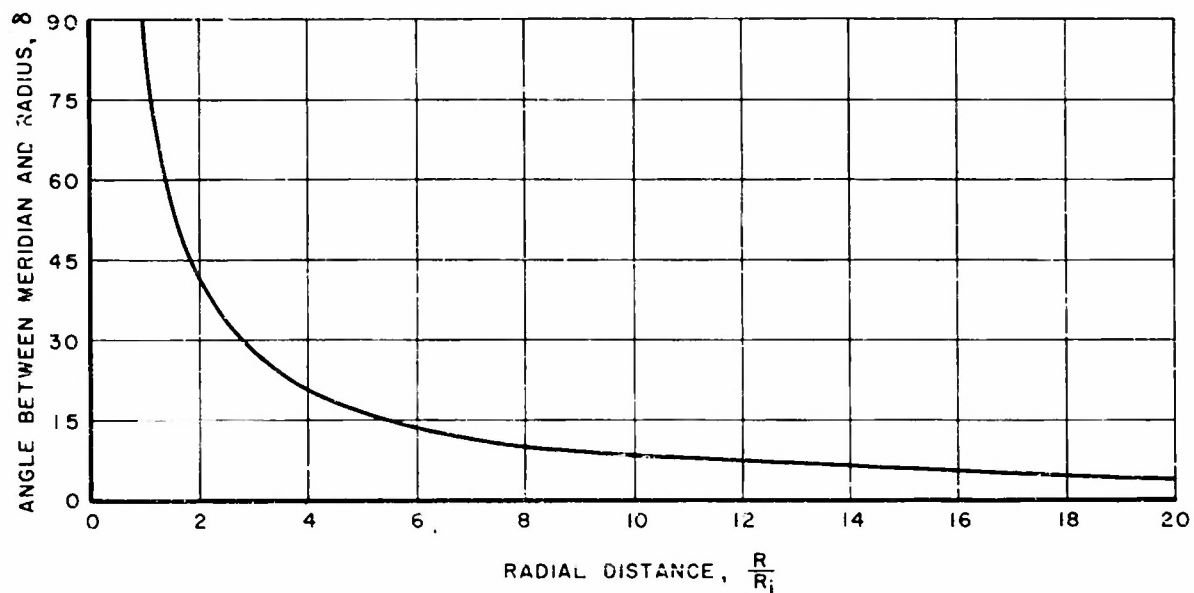


Fig. 4 - Meridian inclination  $\delta$  for the shape shown in Fig. 3.

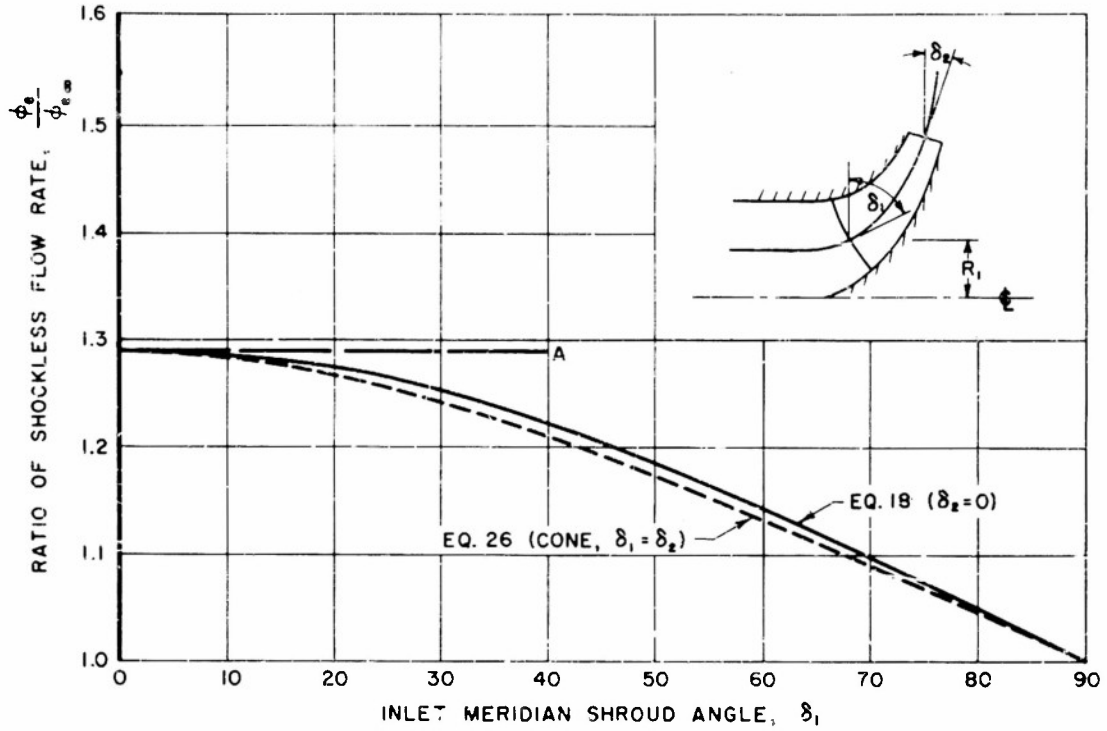


Fig. 5 - Ratio of shockless flow rates vs. inlet meridian shroud angle  $\delta_1$  for the case of 6 blades,  $\gamma = 70^\circ$  and solidity = 1.2.

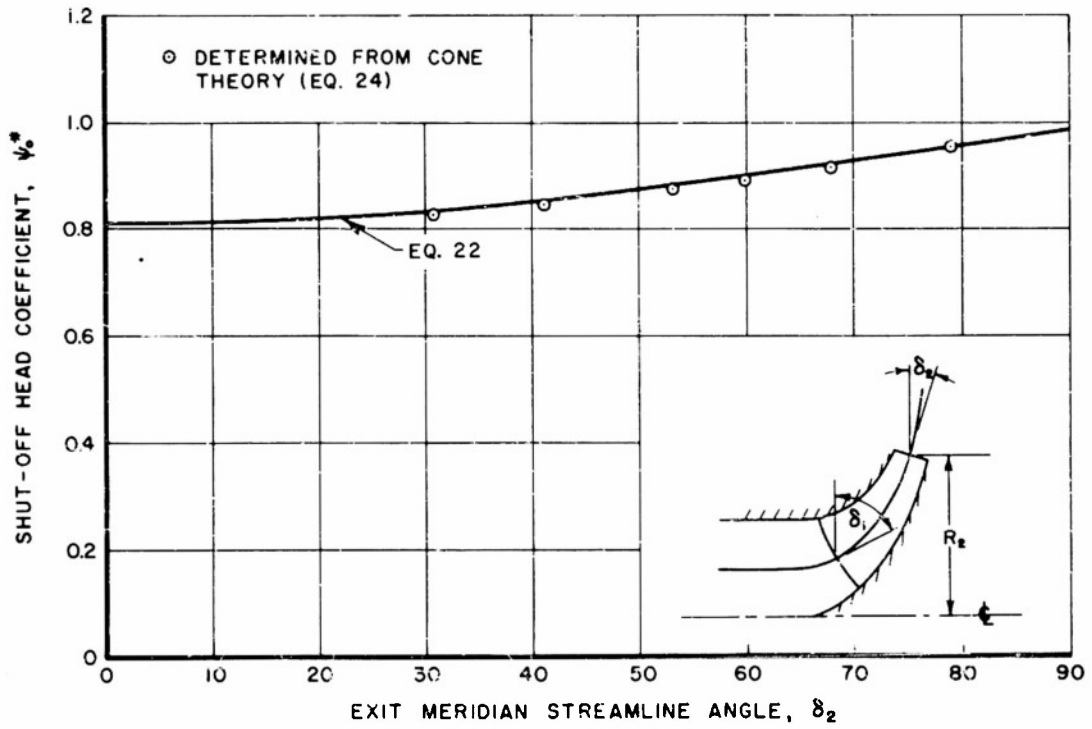


Fig. 6 - Shut-off head coefficient  $\psi_0^*$  vs. exit meridian shroud angle  $\delta_2$  for the case of 6 blades,  $\gamma = 70^\circ$  and solidity = 1.2.

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