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APPROXIMATE SOLUTIONS FOR NONEQUILIBRIUM
AIRFLOW IN HYPERSONIC NOZZLES

BY
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AUGUST 1960

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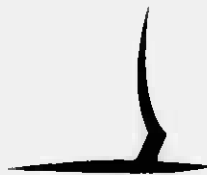
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Buffalo 21, New York

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AIR RESEARCH AND DEVELOPMENT COMMAND
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FOREWORD

This technical note was prepared as part of the Wave Superheater Hypersonic Tunnel project being constructed at Cornell Aeronautical Laboratory, Inc., Buffalo, New York.

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The authors are pleased to acknowledge the helpful discussions held with Dr. J. G. Hall of CAL throughout the course of this work.

ABSTRACT

A method has been described to estimate the effects of finite chemical reaction rates on the one-dimensional expansion of air in hypersonic nozzles. The calculations have considered stagnation temperatures from 4000 to 6000°K, stagnation pressures from 100 to 1000 atmospheres, and a range of wedge and axisymmetric nozzle shapes. Vibrational equilibrium is assumed.

A relaxation length criterion has been applied to a simplified kinetic model of air to determine the approximate location of freezing for flow with finite reaction rates in each nozzle configuration. Equilibrium composition profiles obtained by machine calculation were used for the calculation of the relaxation lengths. The resultant chemically frozen expansions have been calculated and are presented in tabular and graphical form. In all cases freezing occurs fairly early in the nozzle. Further, freezing in the nozzle is delayed by an increase in stagnation pressure, an increase in stagnation temperature, and by the use of gradually expanding nozzles. The effect of freezing is to reduce the pressure, velocity and temperature at a particular area ratio from the corresponding equilibrium values, and to increase the density and Mach number. The change in temperature and Mach number may be considerable whereas the density and flow velocity are relatively unaffected by freezing.

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NOTATION

Dimensional

- A' cross sectional area of nozzle
 D dissociation energy per mole
 ΔF_l° change in standard free energy for l th reaction
 h'_i enthalpy of i th species including energy of formation, cal/mole
 h Planck's constant
 H' enthalpy of mixture, cal/gm
 k_f dissociation rate coefficient, $\text{cm}^3/\text{mole sec}$
 k_R recombination rate coefficient, $\text{cm}^6/\text{mole}^2 \text{ sec}$
 K_e equilibrium constant = k_f / k_R , mole/cm^3
 K_{pl}, K_{xl} equilibrium constant referred to partial pressures and mole fractions respectively
 K Boltzmann constant
 l characteristic nozzle dimension L/a
 L characteristic throat dimension, cm
 m' mass flow $\rho' u' A'$
 p' fluid pressure
 r' local relaxation length, Equation (35)
 r'_∞ local relaxation length based on infinite-rate equilibrium, Equation (36)
 R_0 universal gas constant
 s'_0 entropy (per unit mass) at reservoir conditions
 $S_i^{\circ'}$ molar entropy of i th species at standard pressure
 T' local absolute temperature of gas

- u' local gas velocity
 x' distance from nozzle throat
 γ_i concentration of species i , moles/gm
 θ'_0 characteristic dissociation temperature D/R_0
 θ'_v characteristic vibrational temperature $h\nu/k$
 μ molecular weight of undissociated mixture
 $\bar{\mu}$ molecular weight of mixture
 ν characteristic frequency of molecule
 ρ' fluid density
 ψ parameter $\frac{2L\rho_0'^2}{\sqrt{\frac{R_0 T_0'}{\mu}}} k_{R_0}^{(2)}$

Dimensionless

- a tangent of nozzle semi-angle
 A_{jk} member of correction coefficient matrix in Newton-Raphson method
 A A'/A_*
 C number of linearly independent species
 F_j function used in Newton-Raphson method defined by Equations (A-2) and (A-3)
 h_i $h'_i/R_0 T_0'$
 h_k fractional correction to the k th independent variable in Newton-Raphson iteration
 H $H'/\frac{R_0 T_0'}{\mu}$
 m mass flow $\rho u A$

- m number of chemical elements present
 M Mach number
 M_i chemical formula of i th species
 n exponent in area relation $A = 1 + x^n$
 p p'/p_0'
 q_j mole fraction of j th component in a hypothetical system containing components only
 Q_k number of gram atoms of k th chemical element present
 r r'/ℓ
 r_∞ r'_∞/ℓ
 s number of species
 s_0 s_0'/R_0
 S_i° S_i°'/R_0
 T T'/T_0'
 u $u'/\sqrt{\frac{R_0 T_0'}{\mu}}$
 x x'/ℓ
 X_i mole fraction of i th species
 y_i formula vector of i th species
 α_{jk} atoms of k th chemical element per molecule of j th chemical species
 β_i $k_f^{(i)}/k_f^{(2)}$, Equation (32)
 δ_{jk} Kronecker delta
 ϵ_h maximum permissible fractional correction to mole fractions
 θ_D θ_D'/T_0'
 θ_V θ_V'/T_0'

ν_{ij} stoichiometric coefficients
 ρ ρ'/ρ_0'

Subscripts

α, i, j, k, l sum, product or matrix indices

o denotes condition at reservoir

e denotes local equilibrium value

∞ denotes infinite-rate equilibrium value

$*$ denotes value at throat, $A = 1$

f denotes value at freezing

I INTRODUCTION

The stagnation enthalpies encountered in the flow of gases through nozzles at low supersonic velocities are usually sufficiently low so that chemical kinetics are unimportant. Such flows may be accurately described by simple equations which consider the participation of only the translational and rotational degrees of freedom of the molecules (constant γ). However, in the high temperature flows occurring in hypersonic nozzles, such simplified considerations are no longer applicable because of the interchange of energy between the internal and translational degrees of freedom and the coupling of the chemistry with the gas dynamics through dissociation. Figure 1 shows that at stagnation conditions pertinent to the present study, a significant portion of the total energy resides in the internal energy modes.

The gas dynamic and chemical behavior of a high temperature gas undergoing expansion in complete equilibrium may be calculated with reasonable precision (Sec. II). Complete chemical equilibrium, however, implying infinite reaction rates, is a condition which may only be approached, to a greater or lesser degree, in the expansion of high temperature real gases. Studies of the effects of chemical nonequilibrium, in particular nozzle flows^{1, 2, 3, 4} involving only a single dissociating molecular species, have shown that the flow properties may depart considerably from their local equilibrium values. The effect of finite chemical reaction rates, as well as nozzle geometry, may result in actual freezing of the gas composition at some point in the nozzle.

The purpose of this report is to present quantitative estimates for the effect of flow freezing on the departure of test section properties from their equilibrium values in the expansion of air through hypersonic wind tunnel nozzles. The analysis has considered stagnation temperatures from 4000°K to 6000°K and stagnation pressures from 100 to 1000 atmospheres, representing a range of stagnation enthalpies of either current or future interest. The expansions are considered for two nozzle configurations; a two-dimensional wedge-type nozzle with a sharp throat and a hyperbolic axisymmetric nozzle

which is conical for large area ratios. The solutions cover a comprehensive range of geometries for both types of nozzle.

The outline of the report is as follows. The equilibrium chemical composition of the gas at the reservoir condition is first computed for all stagnation states by the method outlined in Sec. II. The equilibrium (infinite-rate) expansions are then calculated, the solutions providing both the gas dynamic behavior and gas composition as a function of temperature. Because of their usefulness, the results of the equilibrium calculations are included in this report in tabular and graphical form.

The concept of a local chemical relaxation length⁵ is then introduced (Sec. III) and used to develop an approximate criterion for freezing. This concept was first used to develop a freezing criterion in Ref. 3, for both a pure diatomic gas or diatomic gas plus any diluent. Some air calculations were also performed in Ref. 3. The present kinetic model for air assumes finite reaction rates for oxygen, with nitrogen and nitric oxide assumed to remain in chemical (infinite-rate) equilibrium. A relaxation length is calculated, based upon the equilibrium flow properties, and used to determine the approximate nozzle location at which appreciable freezing has occurred, i.e., to predict, approximately, the final chemical state of the expanding flow for finite reaction rates.

Finally (Sec. IV), calculation of the nozzle expansions are completed with all chemical species fixed at their "freezing" mass fractions. The equilibrium solutions serve as a basis of comparison for the frozen (zero-rate) solutions. Both the equilibrium and frozen expansion processes are isentropic.¹⁴ The comparisons have been referred to as providing quantitative "estimates" since although the calculations of the frozen expansions are in themselves exact, the criterion for the selection of the equilibrium state to serve as input to the frozen calculations is approximate.

II SOLUTION OF THE EQUILIBRIUM FLOW

A. Governing Equations

It is assumed that the gas is a mixture of ideal gases, that the flow is quasi-one-dimensional, and that diffusion, heat conduction and viscous processes are of negligible significance. Steady, adiabatic, critical flow is assumed to exist in the nozzle.

The equations which determine the flow are,

Conservation of Momentum:

$$u' du' + \frac{dp'}{\rho'} = 0 \quad (1)$$

where u' = velocity
 p' = pressure
 ρ' = density

Global Conservation of Energy:

$$\frac{u'^2}{2} + H' = H_0' \quad (2)$$

where H' = mixture enthalpy (cal/gm)

Global Conservation of Mass:

$$m' = \rho' u' A' \quad (3)$$

where m' = mass flow
 A' = cross-sectional area

The state equations are,

Thermodynamic State:

$$p' = \rho' \frac{R_0}{\bar{\mu}} T' \quad (4)$$

where $\bar{\mu}$ = molecular weight of mixture and is given by

$$\bar{\mu} = \frac{1}{\sum_{i=1}^s \gamma_i} \quad (5)$$

where γ_i = mass concentration of species i in moles per unit mass.

Caloric State:

$$H' = \sum_{i=1}^s \gamma_i h_i' \quad (6)$$

where h_i' = molar enthalpy of i th species including thermal and formation contributions. h_i' is only a function of temperature.

In dimensionless form, the equations are written

$$u du + \frac{dp}{\rho} = 0 \quad (7)$$

$$\frac{u^2}{2} + H = H_0 \quad (8)$$

$$m = \rho u A \quad (9)$$

$$p = \rho T \frac{\sum_{i=1}^s \gamma_i}{\sum_{i=1}^s \gamma_{i_0}} \quad (10)$$

$$H = \mu \sum_{i=1}^s \gamma_i h_i \quad (11)$$

where

$$u = u' / \sqrt{\frac{R_o T_o'}{\mu}}$$

$$H = H' / \frac{R_o T_o'}{\mu}$$

$$p = p' / p_o'$$

$$\rho = \rho' / \rho_o'$$

$$T = T' / T_o'$$

$$A = A' / A'_*$$

μ = molecular weight of undissociated (cold) gas

R_o = Universal gas constant

A'_* = throat area

Except for the molecular weight, μ , the reference conditions for the non-dimensional forms are those at the equilibrium reservoir state.

B. Equilibrium Analysis

The methods and notation of Brinkley⁶ were used for the equilibrium analysis wherever applicable. At the end of this section, the Brinkley technique is extended to include the computation of states along an isentropic path.

The chemical formula of the i th species may be expressed in vectorial form as

$$y_i = (\alpha_{i1}, \alpha_{i2}, \dots, \alpha_{ik}, \dots, \alpha_{im}) \quad (i=1, 2, \dots, s) \quad (12)$$

where α_{ik} is the number of atoms of the k th chemical element per molecule of the i th species and m is the number of elements present. If the rank of the matrix of α_{ik} is c , there exist c linearly independent y_i , and $(s-c)$ dependent y_i which are given by linear combinations of the c independent ones.

$$\sum_{j=1}^c \nu_{lj} y_j = y_l \quad (l = c+1, c+2, \dots, s) \quad (13)$$

As expressed by Eq. (13), ν_{lj} are coefficients in the linear dependencies of vectors y_l upon y_j .

In the equilibrium analysis the independent species are designated ($j = 1, 2, \dots, c$) and are called "components." The number of components c usually equals the number of chemical elements present m . Equations (13) correspond to $(s-c)$ chemical reactions postulated to form the dependent species if the formula vectors are replaced with chemical symbols.

It is useful to consider a hypothetical system. This system has the same atomic constitution as the actual system, but is chemically combined such that only components are present. If Q_k is the number of gram-atoms of the k th element present, and q'_j is the number of moles of the j th component contained in the hypothetical system, then

$$\sum_{j=1}^c \alpha_{jk} q'_j = Q_k \quad (k=1, 2, \dots, m) \quad (14)$$

The q'_j are normalized by

$$q_j = \frac{q'_j}{\sum_{j=1}^c q'_j} \quad (15)$$

thereby scaling the total size of the system if q_j are considered to be numbers of moles.

Global mass conservation may be expressed by

$$\sum_{j=1}^c n_j \mu_j + \sum_{l=c+1}^s n_l \mu_l = \sum_{j=1}^c q_j \mu_j \quad (16)$$

where μ_j is the molecular weight and n_j is the number of moles of j th species. Mass is conserved in each formation reaction of Eqs. (13) so that

$$\mu_l = \sum_{j=1}^c \nu_{lj} \mu_j \quad (l = c+1, c+2, \dots, s) \quad (17)$$

Substituting μ_l from Eq. (17) and equating coefficients of μ_j in Eq. (16) gives

$$n_j + \sum_{l=c+1}^s \nu_{lj} n_l = q_j \quad (j = 1, 2, \dots, c) \quad (18)$$

Division of Eq. (18) by the total number of moles n gives

$$X_j + \sum_{l=c+1}^s \nu_{lj} X_l = \frac{q_j}{n} \quad (j = 1, 2, \dots, c) \quad (19)$$

where X are mole fractions. By definition

$$\sum_{j=1}^c X_j + \sum_{l=c+1}^s X_l = 1 \quad (20)$$

Equation (19) is summed over j to give

$$\sum_{j=1}^c X_j + \sum_{l=c+1}^s \nu_l X_l = \frac{1}{n} \quad (21)$$

where

$$\nu_l = \sum_{j=1}^c \nu_{lj}$$

Substituting for X_j from Eq. (20) into Eq. (21) results in

$$1 + \sum_{\ell=c+1}^s (\nu_{\ell} - 1) X_{\ell} = \frac{1}{n} \quad (22)$$

Therefore, Eq. (19) may be written

$$X_j = q_j - \sum_{\ell=c+1}^s [\nu_{\ell j} - q_j (\nu_{\ell} - 1)] X_{\ell} \quad (j = 1, 2, \dots, c) \quad (23)$$

giving c of the s equations necessary for determining the equilibrium composition at a specified temperature and pressure. The remaining equations are

$$X_{\ell} = K_{x\ell} \prod_{j=1}^c X_j^{\nu_{\ell j}} \quad (\ell = c+1, c+2, \dots, s) \quad (24)$$

where $K_{x\ell}$ are equilibrium constants based on mole fractions. These constants are related to $K_{p\ell}$ by

$$K_{x\ell} = K_{p\ell} p^{-(\nu_{\ell} - 1)} \quad (\ell = c+1, c+2, \dots, s) \quad (25)$$

$K_{p\ell}$ are calculated from chemical potentials by

$$K_{p\ell} = \exp \left(- \frac{\Delta F_{\ell}^{\circ}}{R_0 T'} \right) \quad (26)$$

where ΔF_{ℓ}° is the change in free energy at standard pressure for the ℓ th reaction. The ΔF_{ℓ}° were calculated by means of polynomial fits to various tabulated and derived thermodynamic functions provided by R. E. Duff of Los Alamos Scientific Laboratory. Equations (23) and (24) determine the equilibrium composition when temperature and pressure are specified; therefore, they can be employed for the reservoir state calculations.

For computation along an isentropic path, the Brinkley method must be modified. The composition and pressure will be computed at various temperatures for the entropy at the prescribed reservoir state. Since pressure

is an additional unknown quantity, one more equation is required. A statement that entropy is a constant is the desired equation.

$$s_0 = \frac{1}{\bar{\mu}} \sum_{i=1}^s x_i s_i^{\circ} - \sum_{i=1}^s x_i \ln x_i - \ln p' \quad (27)$$

s_0 is the entropy (per unit mass) calculated at the reservoir state, and $\bar{\mu}$ is the mixture molecular weight which is calculated from

$$\bar{\mu} = \sum_{i=1}^s x_i \mu_i$$

s_i° is the molar entropy of the i th species at standard pressure. Simultaneous solution of the nonlinear algebraic equations (23), (24), and (27) gives the composition and pressure at various temperatures along an isentrope characterized by s_0 . The Newton-Raphson method as employed in the solution is outlined in Appendix A.

Additional quantities are computed from the results of the solution. Concentrations in moles per unit mass γ_i are found from

$$\gamma_i = \frac{x_i}{\bar{\mu}} \quad (i = 1, 2, \dots, s) \quad (28)$$

Density is found from Eq. (4), enthalpy from Eq. (6), velocity from Eq. (2), and mass flow per unit area m'/A' from Eq. (3). The state at which mass flow per unit area goes through a maximum defines the conditions at the throat of the equilibrium nozzle. The local to throat area ratios are then found by dividing the maximum m'/A' by the local m'/A' values. A Mach number is calculated at each step from the expression

$$M = u / \sqrt{\left(\frac{p}{\rho}\right)_{\text{isentropic equilibrium}}} \quad (29)$$

The thermodynamic state is independent of the form of $A(x)$ because the satisfaction of equilibrium conditions at any area is independent of the history of the flow.

The equilibrium air expansions were calculated on the CAL IBM-704 computer* for reservoir temperatures of 4000, 5000, 6000, 7000, and 8000°K and reservoir pressures of 100, 300, and 1000 atmospheres. The calculations assumed a 13 chemical specie system for air. The solutions for the gas dynamic properties and gas composition are presented for each equilibrium expansion in Tables 1-16. In addition, the air composition is shown as a function of area ratio for each case in Figs. 2-17.

*The Fortran programming for IBM machine computation was done by D. B. Larson, Computer Applications Branch, Systems Research Department, Cornell Aeronautical Laboratory. The IBM-704 program used in the solution of the equilibrium flow is available at CAL. In the event further equilibrium flow calculations are required, details will be provided upon request.

III APPROXIMATE SOLUTIONS FOR FINITE-RATE AIR EXPANSIONS

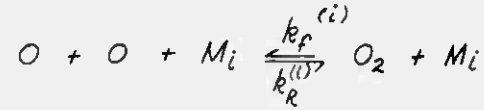
A. Relaxation Length Criterion for Freezing

The solution of nonequilibrium flows, which involve finite reaction rates, is rendered difficult by the need for simultaneous solution of inter-related chemical rate equations and the gas dynamic equations. Also, at the present time, the magnitudes of the required rate constants, and their temperature dependence, are still not known with certainty. It is worthwhile, therefore, to investigate a simple method for the approximate calculation of the final state of a gas undergoing expansion with finite reaction rates.

The present approach is that of Ref. 3 in which specific nonequilibrium airflows in hypersonic nozzles were calculated on the basis of a relaxation length. The results of the previous studies^{2,3} have shown that for flows involving a single relaxing species, the use of a local relaxation length, evaluated for the corresponding equilibrium flow, provides an excellent estimate of the final frozen state of the gas obtained from exact finite-rate solutions. Accordingly, a relaxation length is introduced in the air calculations on the basis of an assumption concerning the relative importance of the various chemical reactions.

The energy associated with the normally inert degrees of freedom for the air species, as a fraction of the total enthalpy, is shown in Fig. 1. It is seen that over the range of reservoir conditions pertinent to the present frozen expansion calculations, i.e., from 4000 to 6000°K, oxygen dissociation is the most important internal mode as it represents the source of greatest energy loss due to freezing. The percentage of the gas enthalpy associated with nitrogen dissociation is small compared with that of oxygen. Furthermore, since the energy associated with the formation of nitric oxide is small and essentially constant over a wide range of temperatures and pressures, the potential energy loss due to freezing of the nitric oxide composition is also quite small. Consequently, a relaxation length is derived assuming that only oxygen dissociation-recombination reactions occur at finite rates.

The reaction may be written



- where
- $M_1 =$ oxygen atom
 - $M_2 =$ oxygen molecule
 - $M_3 =$ nitrogen atom
 - $M_4 =$ nitrogen molecule
 - $M_5 =$ nitric oxide molecule

The equilibrium constant in terms of molar concentrations per unit mass (γ_i) has the assumed form

$$K_e(T') = \frac{k_F^{(i)}}{k_R^{(i)}} = \rho' \frac{\gamma_{Oe}^2}{\gamma_{O_2e}} \quad (30)$$

where $k^{(i)}$ are reaction rate coefficients. The subscript e denotes the local equilibrium value. The rate equation is then

$$\begin{aligned} \frac{d\gamma_0}{dt} = u' \frac{d\gamma_0}{dx'} &= 2\rho' k_F^{(2)} \gamma_{O_2}^2 + 2\rho' k_F^{(1)} \gamma_0 \gamma_{O_2} - 2\rho'^2 k_R^{(2)} \gamma_0^2 \gamma_{O_2} \\ &\quad - 2\rho'^2 k_R^{(1)} \gamma_0^3 + 2\rho' \gamma_{O_2} \sum_{i=3}^5 k_F^{(i)} \gamma_{M_i} - 2\rho'^2 \gamma_0^2 \sum_{i=3}^5 k_R^{(i)} \gamma_{M_i} \end{aligned} \quad (31)$$

On substituting Eq. (30) and rearranging, Eq. (31) becomes

$$u' \frac{d\gamma_0}{dx'} = 2\rho' K_e k_R^{(2)} \gamma_{O_2}^2 \left\{ 1 - \frac{\rho' \gamma_0^2}{K_e \gamma_{O_2}} \right\} \left\{ 1 + \beta_1 \frac{\gamma_0}{\gamma_{O_2}} + \sum_{i=3}^5 \beta_i \frac{\gamma_{M_i}}{\gamma_{O_2}} \right\} \quad (32)$$

where

$$\beta_i = \frac{k_f^{(i)}}{k_f^{(2)}}$$

Now the conservation equation for oxygen atoms is

$$\gamma_o + \gamma_{NO} + 2\gamma_{O_2} = \text{CONST.}$$

therefore $\gamma_{O_2} = B - \frac{\gamma_o}{2}$ where $B = \text{CONST} - \frac{\gamma_{NO}}{2}$

Defining

$$k_R^{(2)} = k_{R_0}^{(2)} T^{-2}$$

$$x = x'/l$$

l = length characterizing nozzle geometry

$$= \frac{L}{\alpha} = \frac{\text{half throat height (cm)}}{\text{tangent of nozzle semi-angle}}$$

$$\psi = \frac{2l s_o'^2}{\sqrt{R_o T_o'}} k_{R_0}^{(2)}$$

and substituting in Eq. (32), noting that K_e (Eq. 30) is defined for equilibrium values of the γ_i , there results

$$\frac{d\gamma_o}{dx} = -\frac{\psi s_o'^2}{\alpha T^2} \left\{ 1 + \beta_1 \frac{\gamma_o}{\gamma_{O_2}} + \sum_{i=3}^5 \beta_i \frac{\gamma_{M_i}}{\gamma_{O_2}} \right\} \left\{ B - \frac{\gamma_o}{2} \right\} \quad (33)$$

$$\left\{ \gamma_o + \frac{B\gamma_{oe}}{B - \frac{\gamma_{oe}}{2}} \right\} \left\{ \gamma_o - \gamma_{oe} \right\}$$

where γ_{oe} = local finite-rate equilibrium value of γ_o , i.e., the equilibrium value of γ_o for the actual temperature and density distribution.

Equation (33) is then of the form introduced by Heims⁵

i. e. ,

$$\frac{d\gamma_0}{dx} = -\frac{\gamma_0 - \gamma_{0e}}{r} \quad (34)$$

where

$$r = \frac{r'}{l} = \frac{u T^2}{\psi_0^2 \left[1 + \beta_1 \frac{\gamma_0}{\gamma_{02}} + \sum_{i=3}^5 \beta_i \frac{\gamma_{Mi}}{\gamma_{02}} \right] \left\{ \beta - \frac{\gamma_0}{2} \right\} \left\{ \gamma_0 + \frac{B \gamma_{0e}}{\beta - \frac{\gamma_{0e}}{2}} \right\}} \quad (35)$$

The rate equation, Eq. (34), which incorporates a local relaxation length r , is used to derive an approximate freezing criterion for the finite-rate flow. The freezing criterion is given in a general form in Ref. 3 and its development is repeated here for completeness.

For flow near equilibrium, $\gamma_0 - \gamma_{0e} \ll \gamma_{0e}$ and it follows from Eq. (34) that $\left| \frac{d\gamma_0}{dx} \right| \ll \frac{\gamma_{0e}}{r}$. For near frozen flow, $\gamma_{0e} \ll \gamma_0$ so that $\left| \frac{d\gamma_0}{dx} \right| \approx \frac{\gamma_0}{r} \gg \frac{\gamma_{0e}}{r}$. Thus an indication of where significant freezing has occurred may be obtained by setting $\left| \frac{d\gamma_0}{dx} \right| = \frac{\gamma_{0e}}{r}$. This equality may be evaluated on the basis of the infinite rate equilibrium flow by using the average values of $\frac{d\gamma_0}{dx}$ and γ_0 through the freezing region. That is

$$\frac{d\gamma_0}{dx} = \frac{1}{2} \left(\frac{d\gamma_0}{dx} \right)_\infty$$

$$\gamma_{0e} = \frac{1}{2} (\gamma_0)_\infty$$

to give

$$\left(\frac{d\gamma_0}{dx} \right)_\infty = \frac{\gamma_{0e}}{r_\infty} \quad \text{or} \quad \left(\frac{d\gamma_0}{dA} \right)_\infty \left(\frac{dA}{dx} \right) = \frac{\gamma_{0e}}{r_\infty} \quad (36)$$

where the subscript ∞ refers to infinite-rate equilibrium values.

Some remarks should be made at this point on the selection of "equilibrium" values. As mentioned earlier in this section, the concept of

a local chemical relaxation length has been found useful for flows in which only a single mode of relaxation is involved, such as the dissociation relaxation of a diatomic gas, with or without inert diluent. For the more complex case of air, the relaxation length criterion has been applied to two simplified kinetic models of air in which the only finite-rate reactions considered are the oxygen dissociation and recombination processes. All species except O and O_2 were assumed to act only as second or third body colliders for the oxygen dissociation-recombination kinetics. The appropriate reaction rate constants were obtained from simple collision theory. Vibrational equilibrium was assumed for all molecular species.

Two basic models were considered in the calculations. In the first, the nitrogen atom and molecule and nitric oxide mass concentrations were frozen at their respective reservoir values during the expansion. In the second, these mass concentrations were taken as those for infinite-rate equilibrium (Sec. II). The flows with oxygen atom-molecule equilibration corresponding to these two models were used in the solution of Eq. (36).

Both models gave values for the frozen degree of oxygen dissociation (α_f) which agreed quite closely up to stagnation temperatures of 6000°K. For example, in a typical hyperbolic nozzle ($L/a = 1.0$) for a stagnation temperature of 5000°K and a stagnation pressure of 100 atm., $\alpha_f = .125$ with N_2 , N , and NO frozen at their reservoir concentrations and $\alpha_f = .149$ with N_2 , N , and NO in infinite-rate equilibrium. Since these are the limiting conditions for the N_2 , N , and NO reactions, this comparison demonstrates that oxygen dissociation-recombination reactions play the major role in air kinetics. The second model has been used in the calculations reported herein, i. e., the equilibrium solutions of Sec. II were used to evaluate relaxation lengths from Eq. (35).

In the above calculations the magnitude of $k_R^{(2)}$ at 3000°K has been taken as $1.16 \times 10^{15} \text{ cm}^6 \text{ mole}^{-2} \text{ sec}^{-1}$, from the results of Byron's⁸ interferometric studies of oxygen dissociation rates. Then since the temperature dependence of the recombination rate coefficient has been assumed as

$$k_R^{(2)} \sim T^{-2} \quad \text{(following Ref. 3)}$$

then

$$k_{R_0}^{(2)} = 1.16 \times 10^{15} \left(\frac{3000}{T_0'} \right)^2 \frac{\text{cm}^6}{\text{mole}^2 \text{sec}}$$

The remaining rate constants for the second or third bodies (β_i) were determined from ordinary collision theory. The form of the rate coefficient is, from collision theory⁹

$$k_f \sim \frac{KD'^2}{\sigma\sqrt{\mu_{ij}}} \left(\frac{\Theta'_{D_i}}{T'} \right)^\eta e^{-\frac{\Theta'_{D_i}}{T'}}$$

where K = steric factor

D' = average diameter of colliding particles

μ_{ij} = reduced mass of colliding particles (i and j)

$$= \frac{\mu_i + \mu_j}{\mu_i \mu_j}$$

η = constant

σ = symmetry number = 1 unlike particles
= 2 like particles

Θ'_{D_i} = characteristic dissociation temperature for species i

For oxygen (from Ref. 8),

$$\frac{k_f^{(1)}}{k_f^{(2)}} = \beta_1 = 35 \frac{T'}{\Theta'_D}$$

For N_2 and NO the steric factors and molecular diameters were assumed the same as for O_2 , whence

$$\frac{k_f^{(i)}}{k_f^{(2)}} = \frac{\sigma_2 \sqrt{\mu_{O_2, O_2}}}{\sigma_i \sqrt{\mu_{i, O_2}}}$$

then for N_2 ,

$$\frac{k_f^{(4)}}{k_f^{(2)}} = \beta_4 = 2.07$$

and NO ,

$$\frac{k_f^{(5)}}{k_f^{(2)}} = \beta_5 = 2.033$$

For N , the steric factor and atomic diameter were assumed to be the same as for O , so

$$\frac{k_f^{(3)}}{k_f^{(1)}} = 1.047$$

whence

$$\frac{k_f^{(3)}}{k_f^{(2)}} = \frac{k_f^{(3)}}{k_f^{(1)}} \frac{k_f^{(1)}}{k_f^{(2)}} = 1.047 \left(35 \frac{T'}{\theta_D'} \right) = 36.6 \frac{T'}{\theta_D'}$$

Relaxation lengths may then be calculated from Eq. (35).

Equation (36) is solved graphically to locate the point of freezing in the nozzle. The slopes $\left(\frac{d\gamma_0}{dA} \right)_\infty$ are obtained graphically from tangents to the curve of oxygen atom mass concentration as a function of area ratio. Calculated values of $(\gamma_0/r)_\infty$ and the value of $\left(\frac{d\gamma_0}{dA} \right)_\infty \left(\frac{dA}{dx} \right)$ are plotted over a range of area ratios. The area ratio at which these two curves cross is the location at which significant freezing has occurred. The frozen value of γ_0 that can be expected for finite-rate flow is given by the value of $\gamma_{0\infty}$ which corresponds to this area ratio. Figure 18 shows the solution of Eq. (36) for the 5000°K, 100 atm. case.

B. Nozzle Geometry Considered

The nozzle geometries considered are given by the general expression $A = 1 + x^n$. These nozzles are symmetric about the throat for even values of the exponent n . In particular, two nozzle geometries have been considered which correspond to values of the exponent equal to 1 and 2. For $n = 1$, the

nozzle is a simple two-dimensional wedge-type nozzle with a sharp throat. The nozzle parameter, $\ell = L/a$, which enters the equation for the area ratio through the relationship $x = \frac{x'}{L/a}$, is given by one-half the throat height in centimeters divided by the tangent of half the total expansion angle. For $n = 2$, the nozzle is an axisymmetric hyperbolic nozzle with a smooth throat and which becomes a conical nozzle for large values of the area ratio, i. e., for nozzle areas not close to the throat. The nozzle geometry parameter is given by the throat radius in centimeters divided by the tangent of the asymptotic half angle.

The nozzle geometry parameter, L/a , represents the rapidity of the nozzle expansion. For a given throat size, small values of L/a correspond to large expansion angles and therefore to rapidly expanding nozzles. On the other hand, large values of the parameter L/a represent small expansion angles and accordingly correspond to gradually expanding nozzles. Many of the nozzles currently used for hypersonic flow research are designed with a value of L/a of about unity. In the present analyses, values of L/a of 0.1, 1, and 10 have been used to bracket the values of current design practice.

C. Results of Approximate Finite-Rate Solutions

The results of the relaxation length criterion calculations for flow in a hyperbolic axisymmetric and wedge-type nozzle are shown in Figs. 19, 20, and 21. The calculations were performed for stagnation temperatures of 4000, 5000, and 6000°K and stagnation pressures from 100 to 1000 atmospheres, for three values of the nozzle geometry parameter L/a (0.1, 1.0, 10).

Figure 19 shows the area ratio for freezing (A_f) plotted against the stagnation pressure for each stagnation temperature. In all cases freezing occurs fairly early in the nozzle ($A_f < 25$). Further, freezing in the nozzle is delayed by an increase in reservoir pressure, an increase in reservoir temperature, and by the use of gradually expanding nozzles (larger L/a).

The frozen degree of oxygen dissociation, α_f (the mass fraction of oxygen atoms to total oxygen) is given by

$$\alpha_f = \frac{\gamma_{O_f}}{\gamma_{O_f} + \gamma_{NO_f} + 2\gamma_{O_2f}}$$

where the subscript f denotes the value at oxygen freezing. The fraction of the stagnation enthalpy represented by frozen chemical energy is given by

$$\frac{H_f}{H_o} = \frac{\mu}{H_o} \left\{ \gamma_{O_f} \frac{\Theta_{DO_2}}{2} + \gamma_{N_f} \frac{\Theta_{DN_2}}{2} + \gamma_{NO_f} \left(\frac{\Theta_{DO_2} + \Theta_{DN_2}}{2} - \Theta_{DNO} \right) \right\}$$

where

$$\Theta_{Di} = \frac{\Theta'_{Di}}{T_o'}$$

The characteristic dissociation temperatures (Θ'_{Di}) assumed for oxygen, nitrogen and nitric oxide are 59,400°K, 113,200°K, and 75,500°K respectively^{7,10}.

The frozen degree of dissociation and H_f/H_o are plotted versus the stagnation pressure for each stagnation temperature in Figs. 20 and 21 respectively. Figure 20 shows that the frozen level of oxygen dissociation is appreciably reduced by an increase in stagnation pressure. This indicates that high stagnation pressures are required in order to reduce the static enthalpy loss through freezing at high levels of dissociation. Figure 21 shows, for example, that at a stagnation temperature of 6000°K and a stagnation pressure of 100 atm., as much as 20% of the total enthalpy may be frozen chemical energy. A wedge nozzle is superior to a hyperbolic nozzle of the same L/a because of a lower frozen degree of dissociation.

IV SOLUTIONS FOR EXPANSION AFTER FREEZING

For the simplified kinetic model of air, the exact finite-rate solution is approximated by assuming equilibrium flow up to the freezing point followed by a chemically-frozen flow downstream. This approximation was introduced by Bray¹ for the case of a pure diatomic gas. The area ratio for freezing as determined by the methods outlined in the last section, represents a unique point in the equilibrium solution. The equilibrium gasdynamic properties and composition at this area ratio are the initial values for the subsequent chemically-frozen expansion.

In the frozen expansion calculations, vibrational equilibrium is assumed with the energy taken as that for a quantized linear oscillator. The total gas enthalpy for translational, rotational and vibrational equilibrium, may then be written as

$$\begin{aligned}
 H = 3T + \mu \left\{ \gamma_{O_2} \left(\frac{T}{2} + \frac{\Theta_{VO_2}}{e^{\Theta_{VO_2}/T} - 1} \right) + \gamma_{N_2} \left(\frac{T}{2} + \frac{\Theta_{VN_2}}{e^{\Theta_{VN_2}/T} - 1} \right) \right. \\
 + \gamma_{NO} \left(\frac{T}{2} + \frac{\Theta_{VNO}}{e^{\Theta_{VNO}/T} - 1} \right) + \gamma_{O} \left(T + \frac{\Theta_{DO_2}}{2} \right) \\
 \left. + \gamma_N \left(T + \frac{\Theta_{DN_2}}{2} \right) + \gamma_{NO} \left(\frac{\Theta_{DO_2} + \Theta_{DN_2}}{2} - \Theta_{DNO} \right) \right\}
 \end{aligned} \tag{37}$$

where μ = molecular weight undissociated gas (28.85)

$$\Theta_{Vi} = \frac{\Theta'_{Vi}}{T_0'}$$

The characteristic vibrational temperatures (Θ'_{Vi}) used for oxygen, nitrogen and nitric oxide are 2300°K, 3390°K and 2740°K, respectively.

The method of solution is as follows. Since the gas composition is now frozen, all γ_i in Eq. (37) are known constants and the gas enthalpy may be simply determined for any specified temperature ratio T. The velocity is then calculated from Eq. (8).

The frozen expansion is isentropic (by virtue of zero reaction rates¹⁴), hence

$$dH - \frac{dp}{\rho} = 0 \quad (38)$$

Then from Eq. (10), in which both $\sum \gamma_{i_0}$ and $\sum \gamma_i$ are now constant, we have

$$\int \frac{dH}{T} - \frac{\sum \gamma}{\sum \gamma_{i_0}} \ln T - \frac{\sum \gamma}{\sum \gamma_{i_0}} \ln \rho = \text{CONST.} \quad (39)$$

where $\sum \gamma = \sum \gamma_i$ at freezing

$$= (\gamma_{O_2} + \gamma_{N_2} + \gamma_{NO} + \gamma_O + \gamma_N)_f$$

Substituting Eq. (37) for H, the left side of Eq. (39) is evaluated to obtain

$$\begin{aligned} & \frac{1}{\sum \gamma} \left(\frac{3}{\mu} + \frac{\sum \gamma_2}{2} + \sum \gamma_1 - \frac{\sum \gamma_i}{\mu \sum \gamma_{i_0}} \right) \ln T \\ & + \frac{\gamma_{O_2}}{\sum \gamma} \left(\frac{1}{T} \frac{\theta_{VO_2}}{e^{\theta_{VO_2}/T-1}} - \ln \frac{e^{\theta_{VO_2}/T-1}}{e^{\theta_{VO_2}/T}} \right) \\ & + \frac{\gamma_{N_2}}{\sum \gamma} \left(\frac{1}{T} \frac{\theta_{VN_2}}{e^{\theta_{VN_2}/T-1}} - \ln \frac{e^{\theta_{VN_2}/T-1}}{e^{\theta_{VN_2}/T}} \right) \\ & + \frac{\gamma_{NO}}{\sum \gamma} \left(\frac{1}{T} \frac{\theta_{VNO}}{e^{\theta_{VNO}/T-1}} - \ln \frac{e^{\theta_{VNO}/T-1}}{e^{\theta_{VNO}/T}} \right) - \frac{1}{\mu \sum \gamma_{i_0}} \ln \rho = \text{CONST.} \end{aligned} \quad (40)$$

where

$$\begin{aligned}\sum \gamma_2 &= (\gamma_{O_2} + \gamma'_{N_2} + \gamma_{NO})_f \\ \sum \gamma_1 &= (\gamma_O + \gamma'_N)_f\end{aligned}$$

Equation (40) relates ρ and τ explicitly for flow with frozen dissociation and equilibrium vibration. The constant is evaluated initially for equilibrium values at the point of freezing. The density is then calculated from Eq. (40) for all subsequent τ . The pressure is next obtained from Eq. (10). Also the area ratio from

$$A = \frac{(\rho u)_*}{\rho_{1L}}$$

and a Mach number is calculated at each step from

$$M = u / \sqrt{\left(\frac{dp}{d\rho}\right)_{\substack{\text{isentropic} \\ \text{frozen}}}}$$

The frozen air expansions were calculated on the CAL Datatron computer* and the results for all initial reservoir states and all nozzle configurations are tabulated in Tables 17 to 26. The parameters in each table commence with their values at freezing, i.e., the equilibrium values at the appropriate A_f . The behavior of the flow temperature, pressure, density, velocity and Mach number during expansion through the hyperbolic-type nozzles from each initial reservoir state is shown in Figs. 22-31. The corresponding equilibrium solutions are included to show the calculated location of freezing in the nozzle and to provide a basis of comparison for the frozen expansions. Only the results for the extreme nozzle shapes ($l = 0.1, 10$) are shown; data for the $l = 1.0$ hyperbolic nozzle flows, as well as for all the wedge-type nozzle flows may be extracted from the tables.

*The programming for Datatron machine computation was done by V.L. Widler, Head, Data Handling Section, Hypersonic Tunnel Department, Cornell Aeronautical Laboratory.

V FURTHER KINETIC CONSIDERATIONS

In the application of a relaxation length freezing criterion for air it has been assumed that the freezing of the oxygen kinetics, taken here as the governing chemical mechanism, implies the simultaneous freezing of all kinetics. Actually this assumption has little significance in the present cases since at the predicted freezing temperatures, little dissociation energy exists in the N and NO, and consequently, only a small amount of enthalpy is involved whether these species are assumed to freeze or not.

However, an analysis similar to that outlined in Sec. III may be performed for a different chemical species. The appropriate equations would all be of the same form as those given previously for oxygen. Now if relaxation length considerations were to indicate freezing of this species at area ratios earlier than those predicted in Sec. III on the basis of oxygen kinetics, the previous assumption of simultaneous freezing of all species would result in a greater loss of static enthalpy because of the freezing of oxygen at higher temperatures. This in turn could result in significant changes in some of the gas dynamic properties calculated in Sec. IV. It was considered expedient, therefore, to indicate the approximate solution to a specific case as dictated by the kinetics of some species other than oxygen.

The 6000°K, 100 atmosphere reservoir case was chosen as it involved the greatest amount of initial oxygen dissociation and is therefore the case most sensitive to earlier oxygen freezing. Furthermore, since the equilibrium solution exhibited a more rapid decrease in \mathcal{X}_N compared to \mathcal{X}_O (Fig. 9), the analysis was based on the nitrogen recombination kinetics. Citing only the results, the application of a relaxation length criterion indicated the freezing of nitrogen approximately at the throat for all nozzle configurations. Then, consistent with the previous assumption, the nitric oxide and oxygen were frozen simultaneously with nitrogen and the resultant frozen expansion is indicated by the dashed profiles in Fig. 29.

It is seen that the calculated frozen expansions determined by the nitrogen kinetics may differ appreciably from those determined by oxygen kinetics. The

difference is mainly dependent on the location of oxygen freezing. However, an argument against the freezing of nitrogen is provided by the nitric oxide "shuffle" reactions. The reactions



provide two fast two-body processes for equilibration of $N - N_2$ and $N - NO$ which have not been considered in the nitrogen three-body processes discussed above.

VI CONCLUSIONS

A method has been described to estimate the effects of finite chemical reaction rates on the one-dimensional expansion of air in hypersonic nozzles. Numerical solutions have been computed for reservoir temperatures from 4000°K to 6000°K and reservoir pressures from 100 to 1000 atmospheres. The calculations have considered a range of wedge and axisymmetric nozzle shapes. The air was assumed to be at rest and in chemical equilibrium at the reservoir state. The flow parameters and gas composition in the infinite-rate equilibrium expansion from each reservoir state were calculated, and a relaxation length criterion, based on the equilibrium solution, was used to indicate the approximate location of freezing for finite-rate airflow in each nozzle configuration. The resultant frozen air expansions have been presented in tabular and graphical form.

The results of the analysis have shown that in all cases, freezing occurred fairly early in the nozzle downstream of the throat, at area ratios less than about 25 (Fig. 19). As a result of such early freezing the frozen degree of dissociation may be quite large (Fig. 20) representing an appreciable loss in the static enthalpy. It is seen, for example (Fig. 21), that in the high temperature, low pressure cases, the unavailable enthalpy owing to freezing may be as much as 19% of the stagnation enthalpy.

The following features are evident in the results. The effect of the static enthalpy loss through freezing is to reduce the pressure, velocity and temperature at a particular nozzle location (area ratio) from the corresponding equilibrium values, and to increase the density and Mach number. While the change in temperature and Mach number may be considerable, the density and velocity are relatively unaffected by freezing.

As expected, the effects of freezing are minimized for larger L/a values, i.e., by the use of gradually expanding nozzles. In practice, however, limitations will be imposed by boundary layer growth in the nozzle and a compromise will be required between maximizing L/a and maintaining a reasonable nozzle size. In this respect the wedge nozzle is superior to the hyperbolic nozzle for

a given L/a by virtue of a lower frozen degree of dissociation of the flow (later freezing). It should be noted that the effect of a change in the nozzle L/a parameter also reflects the effect of a change in the kinetic rates, in particular $k_{R_0}^{(2)}$. Since L/a and the recombination rate constant $k_{R_0}^{(2)}$ occur in the rate equation as a product (in ψ), a change in L/a is comparable to a similar change in $k_{R_0}^{(2)}$, the product remaining the same. This factor permits a simple compensation for discrepancies in existing rate constant data. Also noticeable in the results is the reduction in the frozen degree of dissociation with increase in reservoir pressure. This indicates that high reservoir pressures are required in order to reduce the static enthalpy loss through freezing in the operation of hypersonic wind tunnels at high stagnation temperatures. This requirement is compatible with aerodynamic requirements for testing at very high Mach numbers.

The present nonequilibrium airflow calculations are meant as approximate estimates of the gross features of particular finite-rate nozzle flows. In the interests of simplicity several effects have been omitted from the approximations used, notably the neglect of the nitrogen and nitric oxide reactions at finite rates in the simplified kinetic model of air. However, since the assumption of both zero and infinite rates for reactions involving these species resulted in relatively small changes in the frozen levels of dissociation (Sec. 3.1), the calculated expansions from each reservoir state should represent realistic approximations to actual gas behavior in the nozzle. Ultimate verification must come from comparisons with exact solutions to more complex kinetic models. Such a program is presently underway at CAL.

APPENDIX A
 NEWTON-RAPHSON METHOD^{11,12,13} FOR
 SOLVING THE EQUILIBRIUM PROBLEM

The use of the Newton-Raphson method for the iterative solution of these simultaneous nonlinear algebraic equations was originally suggested by Brinkley⁶ for the determination of equilibrium composition at a given temperature and pressure. Brinkley's method is directly applicable to the computation of the stagnation state; however, certain modifications are introduced for computing composition and pressure at a given entropy for various temperatures along the expansion. Only the modified form is presented here because the essential features of the Brinkley method are contained therein. Equations (23) and (27) are expressed as

$$F_j = 0 \quad (j = 1, 2, \dots, c, c+1) \quad (\text{A-1})$$

where

$$F_j = q_j + \sum_{l=c+1}^s [q_l (\nu_l - 1) - \nu_{lj}] X_l - X_j \quad (\text{A-2})$$

$(j = 1, 2, \dots, c)$

$$F_{c+1} = \sum_{i=1}^s X_i (S_i^\circ - \mu_i s_0 - \ln X_i) - \ln p' \quad (\text{A-3})$$

For given S_0 and T' , values of X_j and p' (the $(c+1)$ st independent variable) must be guessed such that Equations (A-1) are satisfied. X_l are related to X_j by Equation (24).

$$X_l = K_{X_l} \prod_{j=1}^c X_j^{\nu_{lj}} \quad (l = c+1, c+2, \dots, s) \quad \text{Repeat (24)}$$

The Newton-Raphson method provides a means of improving successive guesses by utilizing a Taylor expansion of F_j about X_j and p' to first order terms. This leads to a set of fractional corrections $h_k^{(r)}$ ($k=1, 2, \dots, c, c+1$) applicable to the X_j and p' values obtained at the r th iteration. The improved $(r+1)$ st values of the independent variables are found from

$$X_k^{(r+1)} = X_k^{(r)} (1 + h_k^{(r)}) \quad (k=1, 2, \dots, c) \quad (\text{A-4})$$

and

$$p'^{(r+1)} = p'^{(r)} (1 + h_{c+1}^{(r)}) \quad (\text{A-5})$$

The set of h_k is computed from a set of linear equations expressed in matrix notation by

$$\begin{bmatrix} A_{jk}^{(r)} \end{bmatrix} \begin{bmatrix} h_k^{(r)} \end{bmatrix} = \begin{bmatrix} F_j^{(r)} \end{bmatrix} \quad \begin{matrix} (j=1, 2, \dots, c, c+1) \\ (k=1, 2, \dots, c, c+1) \end{matrix} \quad (\text{A-6})$$

$h_k^{(r)}$ and $F_j^{(r)}$ are column vectors

$$A_{jk} = X_j \delta_{jk} + \sum_{l=c+1}^s \nu_{lk} \left[\nu_{lj} - q_j (\nu_l - 1) \right] X_l \quad (\text{A-7})$$

$$\delta_{jk} = 0 \quad \text{for } j \neq k \quad (j=1, 2, \dots, c)$$

$$\delta_{jk} = 1 \quad \text{for } j = k \quad (k=1, 2, \dots, c)$$

$$A_{j,c+1} = \sum_{l=c+1}^s (\nu_l - 1) \left[\nu_{lj} - q_j (\nu_l - 1) \right] X_l \quad (j=1, 2, \dots, c) \quad (\text{A-8})$$

$$\left. \begin{aligned} A_{c+1,k} &= \left[1 - (S_k^0 - \mu_k s_0 - \ln X_k) \right] X_k + \\ &\quad \sum_{l=c+1}^s \nu_{lk} \left[1 - (S_l^0 - \mu_l s_0 - \ln X_l) \right] X_l \end{aligned} \right\} \quad (k=1, 2, \dots, c) \quad (\text{A-9})$$

$$A_{c+1,c+1} = 1 + \sum_{l=c+1}^s (\nu_l - 1) \left[1 - (S_l^0 - \mu_l s_0 - \ln X_l) \right] X_l \quad (\text{A-10})$$

The $(r+1)$ st iteration is started by calculating $h_k^{(r)}$ from Equation (A-6) using the formulas in Equations (24), (A-2), (A-3), (A-7), (A-8), (A-9), and (A-10). Improved values of λ_j and p' are found from Equations (A-4) and (A-5), and improved values of λ_ℓ are found from Equation (24) using $\lambda_j^{(r+1)}$ and $p'^{(r+1)}$. The cycle begins again with the computation of $[h_k^{(r+1)}]$ from Equation (A-6). When all h_k become equal to or smaller than a prescribed maximum fractional error ϵ_h , the computation is terminated.

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T	P	ρ	ρ̄	M	A	T _{N2}	T _{O2}	T _A	T _N	T _O	T _{N0}	T _{O0}	T _{N0}	T _{O0}	T _N	T _O	T _N	T _O	T _N	T _O	T _N	T _O	T _N	T _O	
1.00	1.00	0.01	1.00	0.00	0.00	0.00	50.15-02	32.19-03	30.07-05	11.30-02	3327-02	1144-13	3115-10	1276-07	5160-10	3609-13	3609-13	3609-13	3609-13	3609-13	3609-13	3609-13	3609-13	3609-13	3609-13
56	574	0.00	1.746	0.00	1.462	0.1	51.30-02	34.19-03	23.75-05	10.37-02	3190-02	7691-14	2150-10	9717-08	1559-16	203-13	203-13	203-13	203-13	203-13	203-13	203-13	203-13	203-13	203-13
56	574	0.00	1.746	0.00	1.462	0.1	51.30-02	34.19-03	23.75-05	10.37-02	3190-02	7691-14	2150-10	9717-08	1559-16	203-13	203-13	203-13	203-13	203-13	203-13	203-13	203-13	203-13	203-13
56	574	0.00	1.746	0.00	1.462	0.1	51.30-02	34.19-03	23.75-05	10.37-02	3190-02	7691-14	2150-10	9717-08	1559-16	203-13	203-13	203-13	203-13	203-13	203-13	203-13	203-13	203-13	203-13

Table 2. EQUILIBRIUM AIRFLOW EXPANSION
 $T_0 = 4000^\circ\text{K}$, $P_0 = 300 \text{ atm}$, $\rho_0 = 2.604 \times 10^{-2} \text{ gm/cm}^3$,
 $H_0 = 4.705$, $(pu)_* = .6551 \text{ at } T = .909$, $\bar{\mu}_0 = 28.50 \text{ gm/mole}$

T	ρ	P	\dot{u} (ft/sec)	M	A	TH_2	TO_2	TA	TN	TO	TNO	TNI	TO_1	TNO'	TN'	TO'	TO''	TC'
1.00	1.00	1.00	0.000	0.00	1.00	0.00	0.00	3219-03	1640-05	6296-03	3391-02	8772-14	2018-10	8092-08	1078-16	1250-13	6257-08	3655-08
1.08	1.00	0.91	0.000	0.00	1.00	0.00	0.00	3219-03	1291-05	5747-03	3250-02	4737-14	1378-10	6105-08	4866-17	6948-14	3101-06	3018-08
1.16	0.92	0.82	0.000	0.00	1.17	0.01	0.00	3219-03	1005-05	4216-03	3150-02	2491-14	9245-11	4350-08	2141-17	3762-14	2222-06	2335-08
1.24	0.94	0.75	0.000	0.00	1.34	0.01	0.00	3219-03	7735-06	2707-03	3050-02	1279-14	8056-11	3346-08	9049-16	1961-14	1571-06	1793-06
1.32	0.96	0.67	0.000	0.00	1.61	0.01	0.00	3219-03	5875-06	2018-03	2857-02	6369-15	5941-11	2429-08	3579-16	1012-14	1090-08	1345-06
1.40	0.98	0.61	0.000	0.00	1.99	0.01	0.00	3219-03	4401-06	1315-03	2657-02	3071-15	2496-11	1736-08	1435-16	5011-15	7421-09	9966-09
1.48	1.00	0.56	0.000	0.00	2.49	0.01	0.00	3219-03	3249-06	6315-03	2508-02	1438-15	1546-11	1222-08	9355-19	2397-15	4953-09	7279-09
1.56	1.02	0.52	0.000	0.00	3.11	0.01	0.00	3219-03	2360-06	2904-03	2358-02	6500-16	9357-12	8452-09	1906-19	1106-15	3236-09	5226-09
1.64	1.04	0.48	0.000	0.00	3.96	0.01	0.00	3219-03	1686-06	2521-03	2208-02	8228-16	5521-12	5743-09	6448-20	6904-16	2065-09	3683-07
1.72	1.06	0.45	0.000	0.00	5.03	0.01	0.00	3219-03	1182-06	2168-03	2061-02	1182-16	3171-12	3827-09	2066-20	4066-16	1286-09	2544-07
1.80	1.08	0.42	0.000	0.00	6.42	0.01	0.00	3219-03	8128-07	1845-03	1911-02	4733-17	1765-12	2496-09	6240-21	6476-17	7797-10	1720-09
1.88	1.10	0.40	0.000	0.00	8.17	0.01	0.00	3219-03	5469-07	1553-03	1771-02	1809-17	9567-13	1594-09	1770-21	3262-17	6592-10	1136-09
1.96	1.12	0.38	0.000	0.00	10.37	0.01	0.00	3219-03	3586-07	1291-03	1629-02	1678-18	5003-13	9927-10	4666-22	1205-17	821-10	7310-15
2.04	1.14	0.36	0.000	0.00	13.76	0.01	0.00	3219-03	2305-07	1059-03	1491-02	2266-18	2523-13	6023-10	1153-22	1160-16	144-10	4979-10
2.12	1.16	0.34	0.000	0.00	18.39	0.01	0.00	3219-03	1438-07	8270-04	1358-02	2224-19	1223-13	3552-10	2816-25	1363-18	7698-11	2784-10
2.20	1.18	0.32	0.000	0.00	24.54	0.01	0.00	3219-03	8710-08	6826-04	1228-02	2243-19	5682-14	2051-10	5443-24	1157-19	1926-11	1636-10
2.28	1.20	0.30	0.000	0.00	33.45	0.01	0.00	3219-03	5107-08	5346-04	1101-02	6378-20	2520-14	1125-10	1050-24	1178-19	1926-11	9368-11
2.36	1.22	0.28	0.000	0.00	45.53	0.01	0.00	3219-03	2890-08	4311-04	9815-03	11680-20	1063-14	5987-11	1757-25	5082-20	5997-12	5089-11
2.44	1.24	0.26	0.000	0.00	61.88	0.01	0.00	3219-03	1574-08	3097-04	8877-03	4077-21	4239-15	3066-11	1757-26	3990-21	3991-12	4667-11
2.52	1.26	0.24	0.000	0.00	83.71	0.01	0.00	3219-03	8210-09	2283-04	7603-03	9028-22	1591-15	1502-11	3597-27	1610-21	1673-12	1355-11
2.60	1.28	0.22	0.000	0.00	112.95	0.01	0.00	3219-03	4688-09	1642-04	6598-03	11609-22	5586-16	7012-12	4415-26	3154-22	8593-13	8594-12
2.68	1.30	0.20	0.000	0.00	152.35	0.01	0.00	3219-03	1933-09	1149-04	5665-03							
2.76	1.32	0.18	0.000	0.00	204.62	0.01	0.00	3219-03	8659-10	7812-05	4807-03							
2.84	1.34	0.16	0.000	0.00	277.26	0.01	0.00	3219-03	3615-10	5136-05	4026-03							
2.92	1.36	0.14	0.000	0.00	377.20	0.01	0.00	3219-03	1410-10	3255-05	3324-03							
3.00	1.38	0.12	0.000	0.00	514.01	0.01	0.00	3219-03	5082-11	1979-05	2700-03							
3.08	1.40	0.10	0.000	0.00	696.61	0.01	0.00	3219-03	1149-05	1149-05	2154-03							
3.16	1.42	0.08	0.000	0.00	946.61	0.01	0.00	3219-03	4982-12	6326-06	1683-03							
3.24	1.44	0.06	0.000	0.00	1288.01	0.01	0.00	3219-03	1321-12	3282-06	1286-03							
3.32	1.46	0.04	0.000	0.00	1752.01	0.01	0.00	3219-03	3071-13	1590-06	8562-04							
3.40	1.48	0.02	0.000	0.00	2378.01	0.01	0.00	3219-03	6133-14	7124-07	6901-04							
3.48	1.50	0.01	0.000	0.00	3249.01	0.01	0.00	3219-03	1028-14	2914-07	4810-04							
3.56	1.52	0.00	0.000	0.00	4370.01	0.01	0.00	3219-03	1402-15	1072-07	3219-04							
3.64	1.54	0.00	0.000	0.00	5853.01	0.01	0.00	3219-03	1503-16	3478-08	2054-04							
3.72	1.56	0.00	0.000	0.00	7918.01	0.01	0.00	3219-03	1209-17	9729-09	1238-04							
3.80	1.58	0.00	0.000	0.00	10710.01	0.01	0.00	3219-03	6893-19	2377-09	6976-05							
3.88	1.60	0.00	0.000	0.00	14360.01	0.01	0.00	3219-03	2288-20	4288-10	5821-05							
3.96	1.62	0.00	0.000	0.00	19370.01	0.01	0.00	3219-03	5793-22	6183-11	1699-05							
4.04	1.64	0.00	0.000	0.00	26180.01	0.01	0.00	3219-03	6812-24	6379-12	7026-06							
4.12	1.66	0.00	0.000	0.00	35490.01	0.01	0.00	3219-03	3524-26	4297-13	2476-06							
4.20	1.68	0.00	0.000	0.00	48200.01	0.01	0.00	3219-03	1661-14	7085-07	7085-07							
4.28	1.70	0.00	0.000	0.00	6480.01	0.01	0.00	3219-03	6268-29	1661-14	7085-07							
4.36	1.72	0.00	0.000	0.00	8800.01	0.01	0.00	3219-03	2681-32	3060-16	1537-07							
4.44	1.74	0.00	0.000	0.00	11840.01	0.01	0.00	3219-03	1615-36	2031-18	2278-08							
4.52	1.76	0.00	0.000	0.00	16000.01	0.01	0.00	3219-03	3322-21	3322-21	1963-09							
4.60	1.78	0.00	0.000	0.00	21400.01	0.01	0.00	3219-03	5922-25	5922-25	7499-11							
4.68	1.80	0.00	0.000	0.00	28800.01	0.01	0.00	3219-03	4268-30	4268-30	7815-13							

Table 3.

EQUILIBRIUM AIRFLOW EXPANSION

$T_0' = 4000^\circ\text{K}$, $\rho_0' = 1000 \text{ atm.}$, $\rho_0' = 8.744 \times 10^{-2} \text{ gm/cm}^3$,
 $H_0 = 4.599$, $(\rho u)^* = .6547$ at $T = .903$, $\bar{\mu}_0 = 28.70 \text{ gm/mole}$

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T	P	ρ	M	A	T _{N₂}	T _{O₂}	T _A	T _N	T _O	T _{N₂}	T _{O₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}	T _{N₂}															
1.00	1.00 01	1.00 01	.0000 00	.0000 00	2.477-01	.2987-02	.3219-03	.5692-04	.4196-02	.9999-11	.1520-08	.2816-08	.2156-12	.4855-12	.6855-12	.8855-12	.1085-12	.1335-12	.1585-12	.1835-12	.2085-12	.2335-12	.2585-12	.2835-12	.3085-12	.3335-12	.3585-12	.3835-12	.4085-12	.4335-12	.4585-12	.4835-12	.5085-12	.5335-12	.5585-12	.5835-12	.6085-12	.6335-12	.6585-12	.6835-12	.7085-12	.7335-12	.7585-12	.7835-12	.8085-12	.8335-12	.8585-12	.8835-12	.9085-12	.9335-12	.9585-12	.9835-12	1.0085-12

Table 6.

EQUILIBRIUM AIRFLOW EXPANSION

$T_0' = 5000^\circ K$, $P_0' = 300 \text{ atm}$., $P_0' = 1.995 \times 10^{-2} \text{ gm/cm}^3$,
 $H_0' = 5.313$, $(\rho u)^* = .6697 \text{ at } T = .913$, $\bar{\mu}_0 = 27.28 \text{ gm/mole}$

T	p	p'	(H/sec.)	M	A	M ₂	T ₀₂	T _A	T _N	T ₀	T _{W0}	T _{N1}	T ₀₂	T _{W0}	T _{N0}	T _{W0}	T ₀	T _{N0}	T ₀	T _{N0}
1.00	100.00	100.01	0.0000	0.0000	0.0000	0.0000	68600-03	3219-03	7444-03	1019-01	2934-02	1793-08	1366-07	2760-05	3105-09	5201-08	3531-06	2428-05		
.98	80.00	86.06	0.2674	0.4450	1.4771	0.1477	7307-03	3219-03	6438-03	1008-01	2939-02	1193-08	1181-07	2373-05	1889-09	3738-06	2973-06	2092-05		
.96	60.00	82.00	0.8200	0.6370	1.1516	0.1156	7880-03	3219-03	5563-03	9984-02	2945-02	7615-08	8411-06	2021-05	1121-09	2644-06	2466-06	1791-05		
.94	40.00	67.00	1.4916	0.7660	1.0461	0.1046	8528-03	3219-03	4756-03	9822-02	2951-02	3015-09	7741-08	1716-05	6497-10	1838-06	2065-06	1322-05		
.92	20.00	61.00	2.3116	0.9210	1.0001	0.1000	9280-03	3219-03	4034-03	9677-02	2956-02	3175-09	8266-08	1446-05	5266-10	1256-08	1697-06	1074-05		
.90	10.00	53.00	3.2054	1.1040	1.0092	0.1009	1009-02	3219-03	3380-03	9508-02	2960-02	1943-09	5051-09	1207-05	4203-10	8415-09	1193-06	6913-06		
.88	5.00	44.00	4.2634	1.3020	1102-02	1102-02	1102-02	3219-03	2830-03	9320-02	2963-02	1173-09	4011-06	9980-06	3203-10	5826-09	1115-06	5732-06		
.86	2.50	35.00	5.5680	1.5150	1206-02	1206-02	1206-02	3219-03	2339-03	9111-02	2962-02	6908-02	3145-08	8179-06	2601-11	5525-09	6666-07	5059-06		
.84	1.25	28.00	7.2420	1.7410	1324-02	1324-02	1324-02	3219-03	1915-03	8888-02	2958-02	3970-10	2433-08	6636-06	2601-11	5525-09	6666-07	5059-06		
.82	0.625	22.00	9.5640	2.0150	1465-02	1465-02	1465-02	3219-03	1581-03	8633-02	2946-02	2221-10	1853-08	5326-06	1360-11	4201-10	5421-07	3826-06		
.80	0.3125	17.00	12.5880	2.3420	1640-02	1640-02	1640-02	3219-03	1244-03	8395-02	2933-02	1211-10	1359-08	4225-06	6375-12	8501-10	5241-07	3011-06		
.78	0.15625	12.00	16.5120	2.6280	1763-02	1763-02	1763-02	3219-03	9888-04	8050-02	2920-02	6409-11	1022-08	3231-06	2677-12	8771-10	5106-07	2338-08		
.76	0.078125	8.00	21.1680	2.8710	1942-02	1942-02	1942-02	3219-03	7719-04	7833-02	2895-02	4281-11	5206-09	1950-06	5178-13	1474-10	1164-07	1791-06		
.74	0.0390625	5.00	27.0000	3.0810	2138-02	2138-02	2138-02	3219-03	5966-04	7373-02	2859-02	1930-11	3508-09	1662-06	2082-13	7751-11	1155-07	1353-06		
.72	0.01953125	3.00	34.5600	3.2540	2383-02	2383-02	2383-02	3219-03	4546-04	6958-02	2788-02	7798-12	3590-09	1462-06	2082-13	7751-11	7935-08	1051-05		
.70	0.009765625	1.80	43.6800	3.3940	2593-02	2593-02	2593-02	3219-03	3412-04	6591-02	2725-02	3588-12	2442-09	1076-06	2082-13	7751-11	7935-08	1051-05		
.68	0.0048828125	1.00	54.7200	3.5020	2832-02	2832-02	2832-02	3219-03	2517-04	6171-02	2651-02	3588-12	1574-09	7792-07	2082-13	7751-11	7935-08	1051-05		
.66	0.00244140625	0.60	68.2800	3.5840	3098-02	3098-02	3098-02	3219-03	1823-04	5723-02	2564-02	3667-13	9960-10	5218-07	2082-13	7751-11	7935-08	1051-05		
.64	0.001220703125	0.40	84.9600	3.6440	3360-02	3360-02	3360-02	3219-03	1294-04	5256-02	2463-02	4270-13	6066-10	3619-07	2082-13	7751-11	7935-08	1051-05		
.62	0.0006103515625	0.25	104.6400	3.6900	3676-02	3676-02	3676-02	3219-03	8973-05	4763-02	2351-02	5011-15	3578-10	2275-07	2082-13	7751-11	7935-08	1051-05		
.60	0.00030517578125	0.15	130.3200	3.7240	4000-02	4000-02	4000-02	3219-03	6063-05	4255-02	2225-02	5801-14	2015-10	1688-07	2082-13	7751-11	7935-08	1051-05		
.58	0.000152587890625	0.09	163.6800	3.7480	4322-02	4322-02	4322-02	3219-03	3979-05	3791-02	2089-02	6685-15	1062-10	1070-07	2082-13	7751-11	7935-08	1051-05		
.56	7.62e-05	0.05	208.3200	3.7640	4622-02	4622-02	4622-02	3219-03	2525-05	3301-02	1942-02	7685-15	501-11	6544-06	1257-15	1021-09	2736-08	1741-06		
.54	4.76e-05	0.03	266.8800	3.7720	4944-02	4944-02	4944-02	3219-03	1542-05	2811-02	1768-02	8840-15	263-11	3636-06	2473-16	1021-09	2736-08	1741-06		
.52	2.98e-05	0.02	340.3200	3.7780	5260-02	5260-02	5260-02	3219-03	9014-06	2339-02	1623-02	1040-15	1176-11	2143-08	2473-16	1021-09	2736-08	1741-06		
.50	1.86e-05	0.01	437.7600	3.7820	5570-02	5570-02	5570-02	3219-03	5005-06	1891-02	1456-02	6090-17	4893-12	1132-06	2473-16	1021-09	2736-08	1741-06		
.48	1.16e-05	0.01	564.9600	3.7840	5861-02	5861-02	5861-02	3219-03	2619-06	1478-02	1287-02	1227-17	1630-10	5611-09	2473-16	1021-09	2736-08	1741-06		
.46	7.26e-06	0.01	726.2400	3.7850	6129-02	6129-02	6129-02	3219-03	1275-06	1111-02	1119-02	1227-17	1630-10	5611-09	2473-16	1021-09	2736-08	1741-06		
.44	4.54e-06	0.01	926.6400	3.7860	6368-02	6368-02	6368-02	3219-03	6762-07	7968-02	9548-03	3146-15	1880-13	1090-09	2473-16	1021-09	2736-08	1741-06		
.42	2.84e-06	0.01	1160.6400	3.7860	6574-02	6574-02	6574-02	3219-03	3266-07	5415-03	7982-03	3146-15	1880-13	1090-09	2473-16	1021-09	2736-08	1741-06		
.40	1.77e-06	0.01	1432.3200	3.7860	6747-02	6747-02	6747-02	3219-03	8777-08	3463-03	6521-03	3176-20	1420-10	6956-14	1844-25	1395-10	1413-10	4230-11		
.38	1.11e-06	0.01	1741.4400	3.7860	6881-02	6881-02	6881-02	3219-03	2644-08	2065-03	5159-03	2779-22	2108-15	445-11	5861-27	1006-20	1467-13	4230-11		
.36	6.94e-07	0.01	2101.4400	3.7860	6986-02	6986-02	6986-02	3219-03	1603-03	1134-03	4011-03	1544-23	3236-16	1091-11	5371-22	2651-14	1088-11	4230-11		
.34	4.34e-07	0.01	2520.3200	3.7860	7065-02	7065-02	7065-02	3219-03	992-09	5722-04	2996-03									
.32	2.71e-07	0.01	2996.6400	3.7860	7123-02	7123-02	7123-02	3219-03	5909-11	4595-04	2132-03									
.30	1.69e-07	0.01	3530.8800	3.7860	7165-02	7165-02	7165-02	3219-03	3784-10	2592-04	1475-03									
.28	1.05e-07	0.01	4115.8400	3.7860	7194-02	7194-02	7194-02	3219-03	2599-11	1041-04	1041-04									
.26	6.56e-08	0.01	4742.3200	3.7860	7214-02	7214-02	7214-02	3219-03	1712-12	3613-05	9561-04									
.24	4.10e-08	0.01	5401.4400	3.7860	7227-02	7227-02	7227-02	3219-03	1044-13	1044-13	5788-04									
.22	2.56e-08	0.01	6080.6400	3.7860	7235-02	7235-02	7235-02	3219-03	6188-14	2437-06	3219-04									
.20	1.60e-08	0.01	6777.7600	3.7860	7240-02	7240-02	7240-02	3219-03	3108-15	4268-07	1607-04									
.18	1.00e-08	0.01	7481.2800	3.7860	7242-02	7242-02	7242-02	3219-03	1567-17	5177-08	6976-05									
.16	6.31e-09	0.01	8180.6400	3.7860	7243-02	7243-02	7243-02	3219-03	894-20	3844-09	2515-05									
.14	4.14e-09	0.01	8874.4000	3.7860	7244-02	7244-02	7244-02	3219-03	564-20	2851-10	7026-06									
.12	2.76e-09	0.01	9561.7600	3.7860	7244-02	7244-02	7244-02	3219-03	3397-26	2080-12	1384-06									
.10	1.81e-09	0.01	10242.3200	3.7860	7244-02	7244-02	7244-02	3219-03	2258-15	1537-07	1384-06									
.08	1.19e-09	0.01	10905.8400	3.7860	7244-02	7244-02	7244-02	3219-03	1524-09	1226-18	1384-06									
.06	7.77e-10	0.01	11550.7200	3.7860	7244-02	7244-02	7244-02	3219-03	1033-32	1833-32	1384-06									
.04	5.11e-10	0.01	12177.2800	3.7860	7244-02	7244-02	7244-02	3219-03	6097-31											
.02	3.34e-10	0.01	12786.2400	3.7860	7244-02	7244-02	7244-02	3219-03												

Table 8. EQUILIBRIUM AIRFLOW EXPANSION
 $T_0' = 6000^{\circ}\text{K}$, $p_0' = 100$ atm., $p_0 = 5.078 \times 10^{-3}$ gm/cm³,
 $H_0 = 6.229$, $(pu)_* = .7035$ at $T = .907$, $\bar{p}_0 = 25.00$ gm/mole

T	ρ	P	\dot{M} (M/sec)	M	A cm ²	T_{N_2}	T_{O_2}	T_A	T_N	T_O	T_{NO}	T_{N_2}	T_{O_2}	T_{NO^*}	T_N	T_O	T_{NO}	T_{NO^*}	T_N	T_O	T_{NO}	T_{NO^*}	
1.00	.100 01	.100 01	.0000 00	.000 00	.000 00	.2435-.01	.2042-.02	.3219-.03	.2239-.03	.5396-.02	.5005-.02	.5126-.09	.4211-.07	.1369-.05	.2759-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.98	.099 00	.099 00	.2157 04	.439 00	.1495 01	.2439-.01	.2138-.02	.3219-.03	.2193-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.96	.098 00	.098 00	.4054 04	.878 00	.3164 01	.2448-.01	.2147-.02	.3219-.03	.2169-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.94	.097 00	.097 00	.6000 04	.1360 00	.5000 01	.2457-.01	.2156-.02	.3219-.03	.2190-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.92	.096 00	.096 00	.8200 04	.2160 00	.7000 01	.2466-.01	.2165-.02	.3219-.03	.2213-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.90	.095 00	.095 00	1.0700 04	.3240 00	1.0000 01	.2475-.01	.2174-.02	.3219-.03	.2230-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.88	.094 00	.094 00	1.3400 04	.4620 00	1.4142 01	.2484-.01	.2183-.02	.3219-.03	.2247-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.86	.093 00	.093 00	1.6300 04	.6360 00	1.9571 01	.2493-.01	.2192-.02	.3219-.03	.2264-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.84	.092 00	.092 00	1.9500 04	.8520 00	2.6628 01	.2502-.01	.2201-.02	.3219-.03	.2281-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.82	.091 00	.091 00	2.3000 04	.1150 00	3.5556 01	.2511-.01	.2210-.02	.3219-.03	.2300-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.80	.090 00	.090 00	2.6800 04	.1660 00	4.6727 01	.2520-.01	.2219-.02	.3219-.03	.2319-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.78	.089 00	.089 00	3.1000 04	.2300 00	6.0916 01	.2529-.01	.2228-.02	.3219-.03	.2338-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.76	.088 00	.088 00	3.5600 04	.3120 00	7.8272 01	.2538-.01	.2237-.02	.3219-.03	.2357-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.74	.087 00	.087 00	4.0700 04	.4160 00	9.9339 01	.2547-.01	.2246-.02	.3219-.03	.2376-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.72	.086 00	.086 00	4.6400 04	.5460 00	12.4406 01	.2556-.01	.2255-.02	.3219-.03	.2395-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.70	.085 00	.085 00	5.2800 04	.7080 00	16.3653 01	.2565-.01	.2264-.02	.3219-.03	.2414-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.68	.084 00	.084 00	6.0000 04	.9000 00	21.5182 01	.2574-.01	.2273-.02	.3219-.03	.2433-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.66	.083 00	.083 00	6.8100 04	.1150 00	28.8801 01	.2583-.01	.2282-.02	.3219-.03	.2452-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.64	.082 00	.082 00	7.7200 04	.1500 00	38.8801 01	.2592-.01	.2291-.02	.3219-.03	.2471-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.62	.081 00	.081 00	8.8500 04	.2000 00	52.3333 01	.2601-.01	.2300-.02	.3219-.03	.2490-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.60	.080 00	.080 00	10.2000 04	.2700 00	71.4286 01	.2610-.01	.2309-.02	.3219-.03	.2509-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.58	.079 00	.079 00	11.7800 04	.3600 00	98.7619 01	.2619-.01	.2318-.02	.3219-.03	.2528-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.56	.078 00	.078 00	13.6100 04	.4700 00	134.8333 01	.2628-.01	.2327-.02	.3219-.03	.2547-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.54	.077 00	.077 00	15.7100 04	.6000 00	181.8182 01	.2637-.01	.2336-.02	.3219-.03	.2566-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.52	.076 00	.076 00	18.0900 04	.7600 00	247.2727 01	.2646-.01	.2345-.02	.3219-.03	.2585-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.50	.075 00	.075 00	20.8700 04	.9600 00	337.7778 01	.2655-.01	.2354-.02	.3219-.03	.2604-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.48	.074 00	.074 00	24.0800 04	.1260 00	463.1579 01	.2664-.01	.2363-.02	.3219-.03	.2623-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.46	.073 00	.073 00	27.7500 04	.1600 00	631.5789 01	.2673-.01	.2372-.02	.3219-.03	.2642-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.44	.072 00	.072 00	31.9200 04	.2000 00	863.1579 01	.2682-.01	.2381-.02	.3219-.03	.2661-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.42	.071 00	.071 00	36.6300 04	.2500 00	1166.6667 01	.2691-.01	.2390-.02	.3219-.03	.2680-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.40	.070 00	.070 00	41.9200 04	.3100 00	1571.4286 01	.2700-.01	.2399-.02	.3219-.03	.2699-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.38	.069 00	.069 00	47.8500 04	.3800 00	2100.0000 01	.2709-.01	.2408-.02	.3219-.03	.2718-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.36	.068 00	.068 00	54.4800 04	.4600 00	2777.7778 01	.2718-.01	.2417-.02	.3219-.03	.2737-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.34	.067 00	.067 00	61.8700 04	.5500 00	3636.3636 01	.2727-.01	.2426-.02	.3219-.03	.2756-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.32	.066 00	.066 00	70.0800 04	.6500 00	4727.2727 01	.2736-.01	.2435-.02	.3219-.03	.2775-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.30	.065 00	.065 00	79.1800 04	.7600 00	6060.6061 01	.2745-.01	.2444-.02	.3219-.03	.2794-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.28	.064 00	.064 00	89.2500 04	.8800 00	7692.3077 01	.2754-.01	.2453-.02	.3219-.03	.2813-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.26	.063 00	.063 00	100.3500 04	.1000 00	9672.7273 01	.2763-.01	.2462-.02	.3219-.03	.2832-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.24	.062 00	.062 00	113.5500 04	.1200 00	12045.4545 01	.2772-.01	.2471-.02	.3219-.03	.2851-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.22	.061 00	.061 00	128.9000 04	.1400 00	14909.0909 01	.2781-.01	.2480-.02	.3219-.03	.2870-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.20	.060 00	.060 00	146.4500 04	.1600 00	18363.6364 01	.2790-.01	.2489-.02	.3219-.03	.2889-.03	.5261-.02	.4949-.02	.5261-.09	.4683-.06	.1377-.05	.2671-.10	.6173-.04	.6337-.06	.7003-.06	.6337-.06	.6173-.04	.6337-.06	.7003-.06	.6337-.06
.18	.059 00	.059 00	166.2500 04	.1800 00	22454.5455 01	.2799-.01																	

T	ρ	P	$\frac{d\rho}{dP}$	M	A	ρ_{H_2}	T_{O_2}	T_A	T_N	T_0	T_{N_2}	T_{O_2}	T_{N_2}	T_{N_2}	T_{O_2}	T_{N_2}	T_{O_2}	T_{N_2}	T_{O_2}	T_{N_2}	T_{O_2}	T_{N_2}	T_{O_2}
1.00	1.00 01	1.00 00	0.000 00	0.00 00	1.500 01	0.2425-01	9907-03	3219-03	9314-03	8058-02	1344-02	5138-07	2104-08	1701-07	1966-05	3601-05							
.99	.910 00	.890 00	-.2376 04	4.36 00	1.169 01	-.2433-01	1039-02	3219-03	8460-03	7968-02	9421-02	4367-07	1386-06	1267-05	1687-05								
.98	.627 00	.590 00	-.3358 04	6.24 00	1.169 01	-.2433-01	1039-02	3219-03	8460-03	7968-02	9421-02	4367-07	1386-06	1267-05	1687-05								
.97	.479 00	.440 00	-.4110 04	7.73 00	1.053 01	-.2444-01	1153-02	3219-03	8577-03	7796-02	8381-02	4563-08	1437-05	1437-05									
.96	.327 00	.290 00	-.4864 04	9.03 00	1.009 01	-.2449-01	1218-02	3219-03	8737-03	7687-02	7359-02	4793-08	1471-05	1471-05									
.95	.175 00	.140 00	-.5628 04	10.00 01	1.000 01	-.2450-01	1291-02	3219-03	8977-03	7566-02	6336-02	5041-06	1522-05	1522-05									
.94	.023 00	.000 00	-.6402 04	11.05 01	1.015 01	-.2459-01	1371-02	3219-03	9279-03	7451-02	5136-02	5312-06	1589-06	1589-06									
.93	.000 00	.000 00	-.7186 04	12.41 01	1.047 01	-.2466-01	1460-02	3219-03	9653-03	7339-02	4285-02	5658-07	1666-06	1666-06									
.92	.000 00	.000 00	-.7990 04	13.96 01	1.096 01	-.2472-01	1558-02	3219-03	10093-03	7233-02	3802-02	6051-08	1756-06	1756-06									
.91	.000 00	.000 00	-.8813 04	15.71 01	1.159 01	-.2477-01	1666-02	3219-03	10635-03	7143-02	3417-02	6484-09	1856-06	1856-06									
.90	.000 00	.000 00	-.9656 04	17.65 01	1.236 01	-.2481-01	1785-02	3219-03	11240-03	7058-02	3129-02	6938-10	1970-06	1970-06									
.89	.000 00	.000 00	-.1051 05	19.77 01	1.330 01	-.2483-01	2058-02	3219-03	11915-03	6980-02	2941-02	7404-11	2099-06	2099-06									
.88	.000 00	.000 00	-.1166 05	22.16 01	1.443 01	-.2485-01	2234-02	3219-03	12663-03	6914-02	2851-02	7937-12	2234-06	2234-06									
.87	.000 00	.000 00	-.1294 05	24.81 01	1.576 01	-.2490-01	2384-02	3219-03	13486-03	6854-02	2851-02	8534-13	2384-06	2384-06									
.86	.000 00	.000 00	-.1436 05	27.84 01	1.766 01	-.2495-01	2569-02	3219-03	14395-03	6800-02	2851-02	9197-14	2569-06	2569-06									
.85	.000 00	.000 00	-.1593 05	31.26 01	1.976 01	-.2500-01	2768-02	3219-03	15392-03	6751-02	2851-02	9924-15	2768-06	2768-06									
.84	.000 00	.000 00	-.1766 05	35.07 01	2.230 01	-.2505-01	2981-02	3219-03	16480-03	6707-02	2851-02	10724-16	2981-06	2981-06									
.83	.000 00	.000 00	-.1956 05	39.28 01	2.541 01	-.2511-01	3210-02	3219-03	17662-03	6668-02	2851-02	11658-17	3170-06	3170-06									
.82	.000 00	.000 00	-.2163 05	43.91 01	2.924 01	-.2518-01	3452-02	3219-03	18942-03	6634-02	2851-02	12744-18	3417-06	3417-06									
.81	.000 00	.000 00	-.2387 05	49.07 01	3.398 01	-.2525-01	3706-02	3219-03	20329-03	6605-02	2851-02	13980-19	3684-06	3684-06									
.80	.000 00	.000 00	-.2638 05	54.87 01	3.974 01	-.2533-01	3976-02	3219-03	21834-03	6580-02	2851-02	15377-20	3981-06	3981-06									
.79	.000 00	.000 00	-.2916 05	61.41 01	4.752 01	-.2541-01	4253-02	3219-03	23468-03	6558-02	2851-02	16934-21	4317-06	4317-06									
.78	.000 00	.000 00	-.3222 05	68.70 01	5.711 01	-.2550-01	4537-02	3219-03	25232-03	6539-02	2851-02	18661-22	4694-06	4694-06									
.77	.000 00	.000 00	-.3557 05	76.85 01	6.939 01	-.2560-01	4826-02	3219-03	27146-03	6524-02	2851-02	20568-23	5117-06	5117-06									
.76	.000 00	.000 00	-.3922 05	85.87 01	8.519 01	-.2570-01	5115-02	3219-03	29209-03	6512-02	2851-02	22664-24	5594-06	5594-06									
.75	.000 00	.000 00	-.4326 05	95.78 01	1.056 02	-.2580-01	5399-02	3219-03	31421-03	6502-02	2851-02	24960-25	6134-06	6134-06									
.74	.000 00	.000 00	-.4769 05	106.60 01	1.321 02	-.2591-01	5673-02	3219-03	33884-03	6494-02	2851-02	27457-26	6740-06	6740-06									
.73	.000 00	.000 00	-.5251 05	118.34 01	1.663 02	-.2603-01	5933-02	3219-03	36506-03	6488-02	2851-02	30154-27	7414-06	7414-06									
.72	.000 00	.000 00	-.5773 05	131.02 01	2.105 02	-.2614-01	6173-02	3219-03	39304-03	6483-02	2851-02	33051-28	8249-06	8249-06									
.71	.000 00	.000 00	-.6345 05	144.65 01	2.672 02	-.2625-01	6389-02	3219-03	42282-03	6480-02	2851-02	36148-29	9249-06	9249-06									
.70	.000 00	.000 00	-.6967 05	159.34 01	3.395 02	-.2636-01	6589-02	3219-03	45457-03	6478-02	2851-02	39545-30	10414-06	10414-06									
.69	.000 00	.000 00	-.7649 05	175.18 01	4.312 02	-.2646-01	6737-02	3219-03	48910-03	6477-02	2851-02	43242-31	11754-06	11754-06									
.68	.000 00	.000 00	-.8391 05	192.28 01	5.470 02	-.2656-01	6866-02	3219-03	52643-03	6476-02	2851-02	47340-32	13294-06	13294-06									
.67	.000 00	.000 00	-.9193 05	210.74 01	6.932 02	-.2666-01	6973-02	3219-03	56688-03	6475-02	2851-02	51847-33	15044-06	15044-06									
.66	.000 00	.000 00	-.1005 06	230.57 01	8.768 02	-.2677-01	7055-02	3219-03	61042-03	6474-02	2851-02	56744-34	17004-06	17004-06									
.65	.000 00	.000 00	-.1081 06	251.88 01	1.117 03	-.2679-01	7117-02	3219-03	65746-03	6473-02	2851-02	61941-35	19154-06	19154-06									
.64	.000 00	.000 00	-.1166 06	274.68 01	1.428 03	-.2684-01	7163-02	3219-03	70800-03	6472-02	2851-02	67940-36	21404-06	21404-06									
.63	.000 00	.000 00	-.1260 06	300.07 01	1.843 03	-.2688-01	7195-02	3219-03	76214-03	6471-02	2851-02	74040-37	23854-06	23854-06									
.62	.000 00	.000 00	-.1373 06	328.16 01	2.407 03	-.2693-01	7217-02	3219-03	81918-03	6470-02	2851-02	80340-38	26454-06	26454-06									
.61	.000 00	.000 00	-.1505 06	359.05 01	3.194 03	-.2695-01	7231-02	3219-03	88022-03	6469-02	2851-02	86840-39	29204-06	29204-06									
.60	.000 00	.000 00	-.1657 06	392.74 01	4.322 03	-.2695-01	7236-02	3219-03	94526-03	6468-02	2851-02	93540-40	32154-06	32154-06									
.59	.000 00	.000 00	-.1830 06	429.33 01	5.994 03	-.2696-01	7242-02	3219-03	101530-03	6467-02	2851-02	100540-41	35204-06	35204-06									
.58	.000 00	.000 00	-.2024 06	469.82 01	8.570 03	-.2696-01	7243-02	3219-03	109074-03	6466-02	2851-02	108640-42	38454-06	38454-06									
.57	.000 00	.000 00	-.2239 06	514.31 01	12.274 04	-.2696-01	7243-02	3219-03	118218-03	6465-02	2851-02	117340-43	41904-06	41904-06									
.56	.000 00	.000 00	-.2475 06	563.80 01	1.950 04	-.2696-01	7243-02	3219-03	129062-03	6464-02	2851-02	126740-44	45654-06	45654-06									
.55	.000 00	.000 00	-.2733 06	618.29 01	2.696 04	-.2696-01	7244-02	3219-03	141606-03	6463-02	2851-02	136940-45	49704-06	49704-06									
.54	.000 00	.000 00	-.3015 06	678.78 01	3.612 04	-.2696-01	7244-02	3219-03	155950-03	6462-02	2851-02	148040-46	54154-06	54154-06									
.53	.000 00	.000 00	-.3329 06	745.27 01	4.807 05	-.2696-01	7244-02	3219-03	172304-03	6461-02	2851-02	160040-47	59004-06	59004-06									
.52	.000 00	.000 00	-.3675 06	818.76 01	6.383 05	-.2696-01	7244-02	3219-03	191758-03	6460-02	2851-02	172940-48	64354-06	64354-06									
.51	.000 00	.000 00	-.4053 06	899.25 01	8.462 05	-.2696-01	7244-02	3219-03	214602-03	6459-02	2851-02	186740-49	70304-06	70304-06									

Table 13. EQUILIBRIUM AIRFLOW EXPANSION

$T_0 = 7000^\circ\text{K}$, $p_0 = 1000 \text{ atm}$, $\rho_0 = 4.460 \times 10^{-2} \text{ gm/cm}^3$,
 $H_0 = 5.949 \text{ (pu)}_*$, $p_0 = .904$, $\bar{\mu}_0 = 25.62 \text{ gm/mole}$

T	ρ	ρ	P	$\frac{u}{(ft/sec)}$	M	A	T_{N_2}	T_{O_2}	T_A	T_N	T_O	T_{NO}	T_{N_2}	T_{O_2}	T_{NO}	T_{N_2}	T_{O_2}	T_{NO}	T_{NO}	T_{NO}	T_{NO}	T_{NO}	
1.00	1.00	1.00	1.00	0.00	0.00	0.00	2271-01	6678-03	2219-03	2219-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
1.10	1.10	1.10	1.10	0.10	0.10	0.10	2280-01	6720-03	2220-03	2220-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
1.20	1.20	1.20	1.20	0.20	0.20	0.20	2290-01	6770-03	2230-03	2230-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
1.30	1.30	1.30	1.30	0.30	0.30	0.30	2300-01	6820-03	2240-03	2240-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
1.40	1.40	1.40	1.40	0.40	0.40	0.40	2310-01	6870-03	2250-03	2250-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
1.50	1.50	1.50	1.50	0.50	0.50	0.50	2320-01	6920-03	2260-03	2260-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
1.60	1.60	1.60	1.60	0.60	0.60	0.60	2330-01	6970-03	2270-03	2270-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
1.70	1.70	1.70	1.70	0.70	0.70	0.70	2340-01	7020-03	2280-03	2280-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
1.80	1.80	1.80	1.80	0.80	0.80	0.80	2350-01	7070-03	2290-03	2290-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
1.90	1.90	1.90	1.90	0.90	0.90	0.90	2360-01	7120-03	2300-03	2300-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
2.00	2.00	2.00	2.00	1.00	1.00	1.00	2370-01	7170-03	2310-03	2310-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
2.10	2.10	2.10	2.10	1.10	1.10	1.10	2380-01	7220-03	2320-03	2320-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
2.20	2.20	2.20	2.20	1.20	1.20	1.20	2390-01	7270-03	2330-03	2330-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
2.30	2.30	2.30	2.30	1.30	1.30	1.30	2400-01	7320-03	2340-03	2340-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
2.40	2.40	2.40	2.40	1.40	1.40	1.40	2410-01	7370-03	2350-03	2350-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
2.50	2.50	2.50	2.50	1.50	1.50	1.50	2420-01	7420-03	2360-03	2360-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
2.60	2.60	2.60	2.60	1.60	1.60	1.60	2430-01	7470-03	2370-03	2370-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
2.70	2.70	2.70	2.70	1.70	1.70	1.70	2440-01	7520-03	2380-03	2380-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
2.80	2.80	2.80	2.80	1.80	1.80	1.80	2450-01	7570-03	2390-03	2390-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
2.90	2.90	2.90	2.90	1.90	1.90	1.90	2460-01	7620-03	2400-03	2400-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
3.00	3.00	3.00	3.00	2.00	2.00	2.00	2470-01	7670-03	2410-03	2410-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
3.10	3.10	3.10	3.10	2.10	2.10	2.10	2480-01	7720-03	2420-03	2420-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
3.20	3.20	3.20	3.20	2.20	2.20	2.20	2490-01	7770-03	2430-03	2430-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
3.30	3.30	3.30	3.30	2.30	2.30	2.30	2500-01	7820-03	2440-03	2440-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
3.40	3.40	3.40	3.40	2.40	2.40	2.40	2510-01	7870-03	2450-03	2450-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
3.50	3.50	3.50	3.50	2.50	2.50	2.50	2520-01	7920-03	2460-03	2460-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
3.60	3.60	3.60	3.60	2.60	2.60	2.60	2530-01	7970-03	2470-03	2470-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
3.70	3.70	3.70	3.70	2.70	2.70	2.70	2540-01	8020-03	2480-03	2480-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
3.80	3.80	3.80	3.80	2.80	2.80	2.80	2550-01	8070-03	2490-03	2490-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
3.90	3.90	3.90	3.90	2.90	2.90	2.90	2560-01	8120-03	2500-03	2500-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02
4.00	4.00	4.00	4.00	3.00	3.00	3.00	2570-01	8170-03	2510-03	2510-03	9910-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02	1622-02

Table 16. EQUILIBRIUM AIRFLOW EXPANSION

$T_0 = 8000^\circ\text{K}$, $P_{O_2} = 1000$ atm., $\rho_{O_2} = 3.722 \times 10^{-2}$ gm/cm 3 ,

$H_{O_2} = 6.289$, $(\rho u)^* = .7105$ at $T = .910$, $\bar{P}_{O_2} = 24.43$ gm/mole

l = 0.1

l = 1.0

l = 10

T	l = 0.1			l = 1.0			l = 10			T	l = 0.1			l = 1.0			l = 10			A	M	u'	P	A
	P	u'	M	A	M	u'	P	A	M		u'	P	A	M	u'	P	A	M	u'					
.844	.400	.333	.510	.1134	.141	.1134	.73	.196	.140	.6560	.1795	.1795	.1795	.626	.985	.601	.7545	.243	.3113	.01	.7545	.243	.3113	.01
.84	.394	.326	.5143	.1143	.141	.1143	.72	.187	.132	.6643	.1858	.1858	.1858	.62	.953	.576	.7587	.244	.3100	.01	.7587	.244	.3100	.01
.82	.392	.293	.5352	.1193	.149	.1193	.70	.170	.116	.6805	.1998	.1998	.1998	.58	.852	.498	.7729	.252	.317	.01	.7729	.252	.317	.01
.81	.393	.263	.5553	.1251	.156	.1251	.68	.154	.102	.6963	.2156	.2156	.2156	.56	.760	.429	.7867	.261	.326	.01	.7867	.261	.326	.01
.79	.396	.235	.5747	.1317	.164	.1317	.66	.139	.898	.7117	.2335	.2335	.2335	.54	.675	.368	.8003	.270	.334	.01	.8003	.270	.334	.01
.76	.280	.210	.5934	.1394	.171	.1394	.64	.125	.784	.7268	.2540	.2540	.2540	.52	.597	.314	.8136	.280	.348	.01	.8136	.280	.348	.01
.74	.285	.185	.6116	.1481	.186	.1481	.62	.113	.682	.7415	.2773	.2773	.2773	.50	.525	.266	.8266	.289	.362	.01	.8266	.289	.362	.01
.72	.293	.165	.6292	.1580	.194	.1580	.60	.101	.591	.7560	.3040	.3040	.3040	.48	.461	.224	.8395	.300	.380	.01	.8395	.300	.380	.01
.70	.292	.146	.6463	.1692	.202	.1692	.58	.898	.503	.7701	.3347	.3347	.3347	.46	.402	.188	.8521	.310	.400	.01	.8521	.310	.400	.01
.68	.292	.129	.6629	.1820	.210	.1820	.56	.797	.437	.7840	.3701	.3701	.3701	.44	.349	.156	.8644	.321	.477	.01	.8644	.321	.477	.01
.66	.293	.113	.6791	.1965	.221	.1965	.54	.706	.373	.7976	.4111	.4111	.4111	.42	.301	.129	.8766	.333	.545	.01	.8766	.333	.545	.01
.64	.293	.098	.6949	.2131	.218	.2131	.52	.622	.316	.8109	.4589	.4589	.4589	.40	.258	.106	.8885	.345	.685	.01	.8885	.345	.685	.01
.62	.294	.085	.7104	.2320	.226	.2320	.50	.545	.267	.8240	.5149	.5149	.5149	.38	.220	.089	.9003	.358	.850	.01	.9003	.358	.850	.01
.60	.294	.074	.7254	.2536	.235	.2536	.48	.476	.223	.8368	.5809	.5809	.5809	.36	.186	.072	.9118	.372	.963	.02	.9118	.372	.963	.02
.58	.294	.064	.7402	.2785	.244	.2785	.46	.413	.186	.8494	.6590	.6590	.6590	.34	.156	.058	.9231	.387	.1003	.02	.9231	.387	.1003	.02
.56	.298	.055	.7546	.3072	.253	.3072	.44	.357	.154	.8618	.7521	.7521	.7521	.32	.107	.043	.9342	.402	.190	.02	.9342	.402	.190	.02
.54	.298	.047	.7687	.3405	.262	.3405	.42	.306	.128	.8740	.8640	.8640	.8640	.30	.087	.032	.9451	.419	.278	.02	.9451	.419	.278	.02
.52	.299	.040	.7826	.3791	.272	.3791	.40	.261	.102	.8859	.9994	.9994	.9994	.28	.079	.024	.9562	.437	.377	.02	.9562	.437	.377	.02
.50	.299	.033	.7962	.4244	.282	.4244	.38	.221	.082	.8976	.1165	.1165	.1165	.26	.066	.019	.9674	.456	.489	.02	.9674	.456	.489	.02
.48	.299	.028	.8095	.4776	.293	.4776	.36	.186	.065	.9091	.1368	.1368	.1368	.24	.052	.014	.9764	.478	.573	.02	.9764	.478	.573	.02
.46	.300	.023	.8225	.5406	.304	.5406	.34	.155	.051	.9204	.1622	.1622	.1622	.22	.044	.010	.9864	.501	.648	.02	.9864	.501	.648	.02
.44	.300	.019	.8353	.6156	.315	.6156	.32	.128	.040	.9314	.1941	.1941	.1941	.20	.034	.007	.9962	.528	.803	.02	.9962	.528	.803	.02
.42	.300	.016	.8478	.7056	.327	.7056	.30	.105	.030	.9422	.2347	.2347	.2347	.18	.026	.006	.1006	.557	.893	.02	.1006	.557	.893	.02
.40	.300	.013	.8601	.8144	.340	.8144	.28	.846	.023	.9529	.2871	.2871	.2871	.16	.019	.004	.1215	.591	.117	.03	.1215	.591	.117	.03
.38	.300	.010	.8722	.9469	.353	.9469	.26	.675	.017	.9632	.3557	.3557	.3557	.14	.014	.003	.1424	.631	.291	.03	.1424	.631	.291	.03
.36	.296	.007	.8840	.1110	.367	.1110	.24	.531	.012	.9734	.4472	.4472	.4472	.12	.010	.002	.1624	.678	.412	.03	.1624	.678	.412	.03
.34	.296	.004	.8957	.1312	.383	.1312	.22	.412	.008	.9833	.5201	.5201	.5201	.10	.007	.001	.1824	.736	.342	.03	.1824	.736	.342	.03
.32	.297	.002	.9070	.1567	.399	.1567	.20	.313	.006	.9930	.6448	.6448	.6448	.08	.005	.000	.2024	.811	.527	.03	.2024	.811	.527	.03
.30	.297	.001	.9182	.1890	.417	.1890	.18	.233	.004	.1002	.9927	.9927	.9927	.06	.003	.000	.2224	.857	.708	.03	.2224	.857	.708	.03
.28	.298	.001	.9291	.2307	.436	.2307	.16	.168	.003	.1012	.1360	.1360	.1360	.04	.002	.000	.2424	.912	.834	.04	.2424	.912	.834	.04
.26	.298	.002	.9397	.2851	.456	.2851	.14	.117	.002	.1021	.1930	.1930	.1930	.02	.001	.000	.2624	.978	.133	.04	.2624	.978	.133	.04
.24	.299	.002	.9502	.3575	.479	.3575	.12	.783	.003	.1029	.2870	.2870	.2870	.006	.000	.000	.2824	.106	.211	.04	.2824	.106	.211	.04
.22	.299	.001	.9603	.4558	.505	.4558	.10	.489	.004	.1038	.4558	.4558	.4558	.005	.000	.000	.3024	.117	.311	.04	.3024	.117	.311	.04
.20	.300	.000	.9702	.5922	.534	.5922	.08	.374	.003	.1042	.845	.845	.845	.004	.000	.000	.3224	.132	.545	.04	.3224	.132	.545	.04
.18	.300	.000	.9799	.7871	.567	.7871	.06	.277	.003	.1046	.900	.900	.900	.003	.000	.000	.3424	.150	.799	.04	.3424	.150	.799	.04
.16	.298	.000	.9893	.1075	.605	.1075	.04	.197	.003	.1050	.965	.965	.965	.002	.000	.000	.3624	.168	.133	.04	.3624	.168	.133	.04
.14	.298	.000	.9993	.1521	.650	.1521	.02	.134	.003	.1054	.1052	.1052	.1052	.002	.000	.000	.3824	.187	.310	.04	.3824	.187	.310	.04
.12	.299	.000	.1007	.2254	.707	.2254	.005	.842	.004	.1059	.129	.129	.129	.001	.000	.000	.4024	.190	.555	.04	.4024	.190	.555	.04
.10	.299	.000	.1016	.3565	.779	.3565	.004	.478	.004	.1067	.150	.150	.150	.000	.000	.000	.4224	.179	.834	.04	.4224	.179	.834	.04
.09	.299	.000	.1020	.4859	.824	.4859	.003	.231	.004	.1071	.184	.184	.184	.000	.000	.000	.4424	.151	.108	.04	.4424	.151	.108	.04
.08	.299	.000	.1025	.6223	.877	.6223	.002	.168	.005	.1075	.210	.210	.210	.000	.000	.000	.4624	.111	.311	.04	.4624	.111	.311	.04
.07	.299	.000	.1029	.7714	.941	.7714	.001	.127	.005	.1080	.250	.250	.250	.000	.000	.000	.4824	.108	.545	.04	.4824	.108	.545	.04
.06	.299	.000	.1033	.1273	.102	.1273	.004	.08	.005	.1085	.286	.286	.286	.000	.000	.000	.5024	.107	.857	.04	.5024	.107	.857	.04
.05	.299	.000	.1037	.2905	.112	.2905	.004	.058	.005	.1090	.320	.320	.320	.000	.000	.000	.5224	.107	.117	.04	.5224	.107	.117	.04
.04	.299	.000	.1042	.4004	.126	.4004	.003	.042	.005	.1095	.358	.358	.358	.000	.000	.000	.5424	.107	.311	.04	.5424	.107	.311	.04
.03	.299	.000	.1046	.5718	.146	.5718	.002	.030	.006	.1100	.400	.400	.400	.000	.000	.000	.5624	.107	.545	.04	.5624	.107	.545	.04
.02	.299	.000	.1050	.1983	.180	.1983	.001	.022	.006	.1105	.442	.442	.442	.000	.000	.000	.5824	.107	.857	.04	.5824	.107	.857	.04
.01	.299	.000	.1054	.3128	.252	.3128	.001	.143	.005	.1107	.487	.487	.487	.000	.000	.000	.6024	.107	.117	.04	.6024	.107	.117	.04

Table 17a. EXPANSION AFTER FREEZING - WEDGE NOZZLE

$T_0' = 4000^\circ\text{K}$, $p_0' = 100$ atm.

$l = 0.1$											
T	P	P	u'	M	A	T	P	P	u'	M	A
$l = 1.0$											
T	P	P	u'	M	A	T	P	P	u'	M	A
$l = 10$											
T	P	P	u'	M	A	T	P	P	u'	M	A
.88	.502	.00	.437	.00	.437	.00	.437	.00	.437	.00	.437
.86	.484	.00	.394	.00	.394	.00	.394	.00	.394	.00	.394
.84	.428	.00	.356	.00	.356	.00	.356	.00	.356	.00	.356
.82	.385	.00	.325	.00	.325	.00	.325	.00	.325	.00	.325
.80	.343	.00	.297	.00	.297	.00	.297	.00	.297	.00	.297
.78	.303	.00	.270	.00	.270	.00	.270	.00	.270	.00	.270
.76	.265	.00	.249	.00	.249	.00	.249	.00	.249	.00	.249
.74	.228	.00	.204	.00	.204	.00	.204	.00	.204	.00	.204
.72	.194	.00	.181	.00	.181	.00	.181	.00	.181	.00	.181
.70	.163	.00	.160	.00	.160	.00	.160	.00	.160	.00	.160
.68	.135	.00	.141	.00	.141	.00	.141	.00	.141	.00	.141
.66	.109	.00	.123	.00	.123	.00	.123	.00	.123	.00	.123
.64	.086	.00	.108	.00	.108	.00	.108	.00	.108	.00	.108
.62	.065	.00	.093	.00	.093	.00	.093	.00	.093	.00	.093
.60	.047	.00	.074	.00	.074	.00	.074	.00	.074	.00	.074
.58	.032	.00	.059	.00	.059	.00	.059	.00	.059	.00	.059
.56	.020	.00	.046	.00	.046	.00	.046	.00	.046	.00	.046
.54	.011	.00	.034	.00	.034	.00	.034	.00	.034	.00	.034
.52	.006	.00	.024	.00	.024	.00	.024	.00	.024	.00	.024
.50	.003	.00	.016	.00	.016	.00	.016	.00	.016	.00	.016
.48	.002	.00	.011	.00	.011	.00	.011	.00	.011	.00	.011
.46	.001	.00	.007	.00	.007	.00	.007	.00	.007	.00	.007
.44	.001	.00	.005	.00	.005	.00	.005	.00	.005	.00	.005
.42	.000	.00	.003	.00	.003	.00	.003	.00	.003	.00	.003
.40	.000	.00	.002	.00	.002	.00	.002	.00	.002	.00	.002
.38	.000	.00	.001	.00	.001	.00	.001	.00	.001	.00	.001
.36	.000	.00	.001	.00	.001	.00	.001	.00	.001	.00	.001
.34	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.32	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.30	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.28	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.26	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.24	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.22	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.20	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.18	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.16	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.14	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.12	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.10	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.09	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.08	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.07	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.06	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.05	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.04	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.03	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.02	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000
.01	.000	.00	.000	.00	.000	.00	.000	.00	.000	.00	.000

Table 17b. EXPANSION AFTER FREEZING - HYPERBOLIC NOZZLE
 $T_0' = 4000^\circ K, P_0' = 100 \text{ atm.}$

$l = 1.0$

$l = 1.0$

$l = 0.1$

T	P	A	M	A	T	P	u'	M	A	T	P	u'	M	A	T	P	u'	M	A																		
							(ft./sec.)					(ft./sec.)					(ft./sec.)																				
77	282	00	214	00	5865	04	170	01	1396	01	.651	137	00	878	01	7067	04	223	01	.2384	01	.558	740	01	406	01	7826	04	265	01	3085	01					
76	270	00	202	00	5958	04	172	01	1437	01	.64	129	00	815	01	7151	04	225	01	2498	01	.54	604	01	353	01	7047	04	277	01	4372	01					
75	246	00	180	00	6138	04	179	01	1529	01	.62	116	00	708	01	7301	04	233	01	2726	01	.52	585	01	299	01	8081	04	282	01	488	01					
74	224	00	159	00	6313	04	187	01	1633	01	.60	104	00	613	01	7448	04	242	01	2989	01	.50	513	01	252	01	8212	04	292	01	5482	01					
73	203	00	141	00	6484	04	195	01	1751	01	.58	924	00	528	01	7591	04	251	01	3290	01	.48	447	01	211	01	8341	04	302	01	6184	01					
72	184	00	124	00	6649	04	203	01	1886	01	.56	824	00	453	01	7732	04	260	01	3638	01	.46	388	01	176	01	8467	04	313	01	7074	01					
71	166	00	108	00	6811	04	211	01	2039	01	.54	725	00	386	01	7869	04	269	01	4042	01	.44	335	01	145	01	8591	04	325	01	8024	01					
70	150	00	946	01	6968	04	219	01	2213	01	.52	659	00	327	01	8004	04	279	01	4513	01	.42	287	01	119	01	8713	04	337	01	8924	01					
69	134	00	823	01	7122	04	227	01	2413	01	.50	569	00	276	01	8137	04	289	01	5064	01	.40	245	01	863	02	8832	04	350	01	9368	01					
68	120	00	712	01	7272	04	236	01	2641	01	.48	489	00	231	01	8267	04	299	01	5713	01	.38	207	01	774	02	8950	04	363	01	1045	01					
67	107	00	614	01	7419	04	244	01	2904	01	.46	424	00	192	01	8394	04	310	01	6483	01	.36	174	01	616	02	9065	04	378	01	1478	01					
66	952	01	526	01	7563	04	254	01	3207	01	.44	366	00	159	01	8519	04	322	01	7401	01	.34	145	01	485	02	9178	04	393	01	1747	01					
65	862	01	449	01	7704	04	263	01	3559	01	.42	318	00	130	01	8662	04	334	01	8505	01	.32	119	01	376	02	9284	04	410	01	2080	01					
64	742	01	381	01	7842	04	273	01	3969	01	.40	268	00	105	01	8763	04	347	01	9842	01	.30	976	02	288	02	9397	04	427	01	2517	01					
63	651	01	321	01	7977	04	283	01	4449	01	.38	227	00	84	02	8881	04	360	01	1147	02	.28	788	02	217	02	9503	04	447	01	3082	01					
62	568	01	269	01	8109	04	293	01	5014	01	.36	190	00	67	02	8997	04	375	01	1349	02	.26	628	02	161	02	9607	04	468	01	3823	01					
61	483	01	224	01	8239	04	304	01	5684	01	.34	158	00	53	02	9111	04	390	01	1599	02	.24	494	02	117	02	9709	04	491	01	4812	01					
60	426	01	185	01	8367	04	316	01	6483	01	.32	131	00	41	02	9222	04	407	01	1915	02	.22	382	02	827	03	9808	04	517	01	6158	01					
59	381	01	151	01	8492	04	328	01	7442	01	.30	107	00	31	02	9332	04	424	01	2317	02	.20	290	02	571	03	9905	04	546	01	8033	01					
58	311	01	123	01	8615	04	340	01	8603	01	.28	862	00	23	02	9439	04	443	01	2836	02	.18	215	02	381	03	9999	04	580	01	1077	01					
57	264	01	990	02	8735	04	354	01	1002	02	.26	688	00	17	02	9544	04	465	01	3516	02	.16	156	02	245	03	1009	05	618	01	1471	01					
56	222	01	788	02	8852	04	368	01	1177	02	.24	541	00	12	02	9666	04	488	01	4424	02	.14	108	02	149	03	1018	05	665	01	2071	01					
55	185	01	620	02	8969	04	383	01	1394	02	.22	418	00	9	02	9763	04	513	01	5660	02	.12	722	03	852	04	1027	05	722	01	3114	01					
54	152	01	482	02	9082	04	400	01	1667	02	.20	318	00	6	02	9843	04	543	01	7380	02	.10	450	03	643	04	1035	05	796	01	4854	01					
53	125	01	369	02	9193	04	417	01	2016	02	.18	239	00	4	02	9938	04	576	01	9946	02	.09	343	03	304	04	1040	05	841	01	6466	01					
52	101	01	278	02	9302	04	436	01	2465	02	.16	170	00	3	02	1003	05	614	01	1350	03	.08	254	03	200	04	1044	05	895	01	8704	01					
51	84	02	206	02	9408	04	457	01	3054	02	.14	119	00	2	02	1012	05	661	01	1919	03	.07	181	03	125	04	1048	05	960	01	1218	01					
50	63	02	150	02	9512	04	480	01	3838	02	.12	792	00	1	02	1021	05	718	01	2856	03	.06	122	03	722	05	1052	05	104	02	1795	01					
49	49	02	106	02	9613	04	506	01	4905	02	.10	494	00	1	02	1029	05	791	01	4542	03	.05	769	04	378	05	1056	05	114	02	2847	01					
48	37	02	735	03	9712	04	534	01	6390	02	.09	377	00	1	02	1034	05	836	01	5927	03	.04	436	04	172	05	1060	05	128	02	4933	01					
47	27	02	491	03	9808	04	567	01	8515	02	.08	279	00	1	02	1038	05	890	01	7976	03	.03	210	04	621	05	1064	05	149	02	1032	01					
46	20	02	316	03	9902	04	606	01	1167	03	.07	199	00	1	02	1042	05	954	01	1116	04	.02	750	05	147	06	1068	05	183	01	2880	01					
45	14	02	193	03	9993	04	651	01	1456	03	.06	134	00	1	02	1046	05	1046	05	1046	05	.01	129	05	115	07	1072	05	268	01	1669	01					
44	93	03	110	03	1008	05	708	01	2462	03	.05	843	00	1	02	1050	05	114	02	2602	04																
43	56	03	573	04	1017	05	780	01	3910	03	.04	479	00	1	02	1054	05	128	02	4566	04																
42	44	03	394	04	1021	05	824	01	5098	03	.03	231	00	1	02	1059	05	148	02	9440	04																
41	32	03	259	04	1026	05	878	01	6854	03	.02	825	00	1	02	1063	05	182	02	2632	05																
40	24	03	162	04	1030	05	941	01	9580	03	.01	142	00	1	02	1067	05	257	02	1324	06																
39	18	03	938	05	1034	05	102	02	1410	04																											
38	9	03	492	05	1038	05	112	02	2229	04																											
37	5	04	224	05	1042	05	126	02	3907	04																											
36	2	04	811	06	1046	05	146	02	8064	04																											
35	0	05	193	06	1051	05	180	02	2243	05																											
34	0	05	172	07	1055	05	253	02	1294	06																											

Table 18a. EXPANSION AFTER FREEZING - WEDGE NOZZLE

$T_0' = 4000^\circ\text{K}$, $P_0' = 300$ atm.

$l = 10$

$l = 1.0$

$l = 0.1$

T	ρ	P	u' (ft/sec.)	M	A	T	P	P	u' (ft/sec.)	M	A	T	P	P	u' (ft/sec.)	M	A	T	P	u' (ft/sec.)	M	A		
.776	.293 00	.225 00	.5790 04	.167 01	.1361 01	.684	.167 0	.113 00	.6766 04	.208 01	.2037 01	.597	.960-01	.504-01	.7523 04	.247 01	.2037 01	.597	.960-01	.504-01	.7523 04	.247 01	.2037 01	
.76	.273 00	.205 00	.5939 04	.171 01	.1425 01	.68	.164 0	.114 00	.6798 04	.207 01	.2069 01	.58	.870-01	.497-01	.7643 04	.252 01	.2069 01	.58	.870-01	.497-01	.7643 04	.252 01	.2069 01	
.74	.249 00	.182 00	.6120 04	.179 01	.1516 01	.66	.183 00	.965-01	.6956 04	.215 01	.2239 01	.56	.773-01	.426-01	.7783 04	.261 01	.2239 01	.56	.773-01	.426-01	.7783 04	.261 01	.2239 01	
.72	.227 00	.161 00	.6296 04	.186 01	.1619 01	.64	.188 00	.841-01	.7110 04	.223 01	.2434 01	.54	.683-01	.363-01	.7920 04	.271 01	.2434 01	.54	.683-01	.363-01	.7920 04	.271 01	.2434 01	
.70	.206 00	.142 00	.6467 04	.194 01	.1736 01	.62	.120 00	.731-01	.7261 04	.232 01	.2656 01	.52	.602-01	.308-01	.8054 04	.281 01	.2656 01	.52	.602-01	.308-01	.8054 04	.281 01	.2656 01	
.68	.186 00	.125 00	.6633 04	.202 01	.1868 01	.60	.107 00	.633-01	.7408 04	.240 01	.2910 01	.50	.527-01	.259-01	.8185 04	.291 01	.2910 01	.50	.527-01	.259-01	.8185 04	.291 01	.2910 01	
.66	.166 00	.105 00	.6794 04	.210 01	.2020 01	.58	.954-01	.545-01	.7552 04	.249 01	.3203 01	.48	.460-01	.217-01	.8315 04	.301 01	.3203 01	.48	.460-01	.217-01	.8315 04	.301 01	.3203 01	
.64	.151 00	.938-01	.6952 04	.218 01	.2192 01	.56	.847-01	.468-01	.7694 04	.258 01	.3541 01	.46	.399-01	.181-01	.8441 04	.312 01	.3541 01	.46	.399-01	.181-01	.8441 04	.312 01	.3541 01	
.62	.136 00	.833-01	.7106 04	.227 01	.2389 01	.54	.749-01	.399-01	.7832 04	.268 01	.3933 01	.44	.344-01	.148-01	.8566 04	.324 01	.3933 01	.44	.344-01	.148-01	.8566 04	.324 01	.3933 01	
.60	.122 00	.721-01	.7257 04	.235 01	.2615 01	.52	.660-01	.338-01	.7968 04	.277 01	.4390 01	.42	.292-01	.120-01	.8668 04	.336 01	.4390 01	.42	.292-01	.120-01	.8668 04	.336 01	.4390 01	
.58	.108 00	.621-01	.7404 04	.244 01	.2875 01	.50	.579-01	.285-01	.8101 04	.287 01	.4925 01	.40	.252-01	.991-02	.8808 04	.349 01	.4925 01	.40	.252-01	.991-02	.8808 04	.349 01	.4925 01	
.56	.963-01	.533-01	.7548 04	.253 01	.3175 01	.48	.505-01	.235-01	.8231 04	.298 01	.5555 01	.38	.213-01	.797-02	.8926 04	.362 01	.5555 01	.38	.213-01	.797-02	.8926 04	.362 01	.5555 01	
.54	.842-01	.455-01	.7689 04	.262 01	.3522 01	.46	.438-01	.199-01	.8359 04	.309 01	.6302 01	.36	.179-01	.634-02	.9041 04	.377 01	.6302 01	.36	.179-01	.634-02	.9041 04	.377 01	.6302 01	
.52	.751-01	.386-01	.7828 04	.272 01	.3927 01	.44	.378-01	.164-01	.8485 04	.320 01	.7193 01	.34	.149-01	.499-02	.9154 04	.392 01	.7193 01	.34	.149-01	.499-02	.9154 04	.392 01	.7193 01	
.50	.659-01	.325-01	.7953 04	.282 01	.4402 01	.42	.325-01	.134-01	.8608 04	.333 01	.8264 01	.32	.123-01	.387-02	.9265 04	.409 01	.8264 01	.32	.123-01	.387-02	.9265 04	.409 01	.8264 01	
.48	.575-01	.273-01	.8096 04	.293 01	.4960 01	.40	.277-01	.109-01	.8729 04	.345 01	.9561 01	.30	.100-01	.296-02	.9374 04	.426 01	.9561 01	.30	.100-01	.296-02	.9374 04	.426 01	.9561 01	
.46	.495-01	.227-01	.8226 04	.304 01	.5622 01	.38	.234-01	.877-02	.8848 04	.359 01	.1114 02	.28	.811-02	.223-02	.9481 04	.446 01	.1114 02	.28	.811-02	.223-02	.9481 04	.446 01	.1114 02	
.44	.431-01	.187-01	.8354 04	.315 01	.6412 01	.36	.197-01	.697-02	.8964 04	.373 01	.1310 02	.26	.647-02	.165-02	.9585 04	.467 01	.1310 02	.26	.647-02	.165-02	.9585 04	.467 01	.1310 02	
.42	.370-01	.153-01	.8479 04	.327 01	.7360 01	.34	.164-01	.549-02	.9079 04	.389 01	.1553 02	.24	.508-02	.120-02	.9787 04	.490 01	.1553 02	.24	.508-02	.120-02	.9787 04	.490 01	.1553 02	
.40	.315-01	.125-01	.8602 04	.340 01	.8507 01	.32	.135-01	.428-02	.9191 04	.405 01	.1858 02	.22	.393-02	.852-03	.9786 04	.516 01	.1858 02	.22	.393-02	.852-03	.9786 04	.516 01	.1858 02	
.38	.267-01	.100-01	.8722 04	.353 01	.9907 01	.30	.110-01	.328-02	.9300 04	.423 01	.2248 02	.20	.299-02	.588-03	.9883 04	.545 01	.2248 02	.20	.299-02	.588-03	.9883 04	.545 01	.2248 02	
.36	.224-01	.798-02	.8841 04	.367 01	.1163 02	.28	.892-02	.248-02	.9408 04	.442 01	.2751 02	.18	.222-02	.393-03	.9978 04	.578 01	.2751 02	.18	.222-02	.393-03	.9978 04	.578 01	.2751 02	
.34	.187-01	.628-02	.8956 04	.383 01	.1378 02	.26	.711-02	.182-02	.9513 04	.463 01	.3411 02	.16	.160-02	.282-03	.1007 05	.617 01	.3411 02	.16	.160-02	.282-03	.1007 05	.617 01	.3411 02	
.32	.154-01	.488-02	.9070 04	.399 01	.1648 02	.24	.560-02	.132-02	.9616 04	.486 01	.4290 02	.14	.112-02	.184-03	.1016 05	.653 01	.4290 02	.14	.112-02	.184-03	.1016 05	.653 01	.4290 02	
.30	.126-01	.374-02	.9181 04	.417 01	.1992 02	.22	.433-02	.933-03	.9716 04	.512 01	.5487 02	.12	.743-03	.878-04	.1025 05	.721 01	.5487 02	.12	.743-03	.878-04	.1025 05	.721 01	.5487 02	
.28	.102-01	.282-02	.9290 04	.436 01	.2435 02	.20	.329-02	.648-03	.9814 04	.541 01	.7154 02	.10	.463-03	.456-04	.1033 05	.794 01	.7154 02	.10	.463-03	.456-04	.1033 05	.794 01	.7154 02	
.26	.814-02	.209-02	.9397 04	.456 01	.3016 02	.18	.244-02	.433-03	.9909 04	.574 01	.9541 02	.09	.354-03	.313-04	.1037 05	.839 01	.9541 02	.09	.354-03	.313-04	.1037 05	.839 01	.9541 02	
.24	.644-02	.152-02	.9501 04	.479 01	.3791 02	.16	.176-02	.278-03	.1000 05	.612 01	.1308 03	.08	.262-03	.206-04	.1042 05	.893 01	.1308 03	.08	.262-03	.206-04	.1042 05	.893 01	.1308 03	
.22	.498-02	.108-02	.9602 04	.505 01	.4844 02	.14	.123-02	.170-03	.1009 05	.659 01	.1858 03	.07	.188-03	.128-04	.1046 05	.958 01	.1858 03	.07	.188-03	.128-04	.1046 05	.958 01	.1858 03	
.20	.377-02	.745-03	.9701 04	.534 01	.6309 02	.12	.820-03	.969-04	.1018 05	.715 01	.2766 03	.06	.126-03	.783-05	.1050 05	.104 02	.2766 03	.06	.126-03	.783-05	.1050 05	.104 02	.2766 03	
.18	.280-02	.498-03	.9797 04	.566 01	.8406 02	.10	.511-03	.504-04	.1027 05	.788 01	.4397 03	.05	.792-04	.390-05	.1054 05	.114 02	.4397 03	.05	.792-04	.390-05	.1054 05	.114 02	.4397 03	
.16	.203-02	.320-03	.9891 04	.605 01	.1152 03	.09	.390-03	.346-04	.1031 05	.833 01	.5736 03	.04	.450-04	.177-05	.1058 05	.128 02	.5736 03	.04	.450-04	.177-05	.1058 05	.128 02	.5736 03	
.14	.142-02	.196-03	.9983 04	.650 01	.1634 03	.08	.289-03	.228-04	.1035 05	.887 01	.7717 03	.03	.217-04	.638-06	.1062 05	.149 02	.7717 03	.03	.217-04	.638-06	.1062 05	.149 02	.7717 03	
.12	.944-03	.112-03	.1007 05	.707 01	.2429 03	.07	.206-03	.142-04	.1039 05	.931 01	.1079 04	.02	.773-05	.152-06	.1066 05	.183 02	.1079 04	.02	.773-05	.152-06	.1066 05	.183 02	.1079 04	
.10	.586-03	.582-04	.1016 05	.779 01	.3856 03	.06	.139-03	.823-05	.1043 05	.103 02	.1590 04	.01	.133-05	.143-07	.1070 05	.253 02	.1590 04	.01	.133-05	.143-07	.1070 05	.253 02	.1590 04	
.09	.450-03	.400-04	.1020 05	.823 01	.5027 03	.05	.876-04	.196-05	.1048 05	.112 02	.2515 04	.01					.2515 04	.01						
.08	.333-03	.264-04	.1024 05	.876 01	.6758 03	.04	.497-04	.108-06	.1052 05	.127 02	.4413 04	.01					.4413 04	.01						
.07	.238-03	.164-04	.1029 05	.940 01	.9444 03	.03	.240-04	.708-06	.1056 05	.168 02	.9120 04	.01					.9120 04	.01						
.06	.161-03	.993-05	.1033 05	.1033 05	.1033 05	.02	.857-05	.170-06	.1060 05	.181 02	.2541 05	.01					.2541 05	.01						
.05	.101-03	.500-05	.1037 05	.112 02	.2197 04	.01																		
.04	.576-04	.228-05	.1041 05	.126 05	.3849 04	.01																		
.03	.278-04	.825-06	.1045 05	.146 02	.7941 04	.01																		
.02	.996-05	.196-06	.1050 05	.180 02	.2208 05	.01																		
.01	.172-05	.172-07	.1054 05	.254 02	.2208 05	.01																		

Table 18b. EXPANSION AFTER FREEZING - HYPERBOLIC NOZZLE

$T_0' = 4000^\circ K$, $P_0' = 300$ atm.

$l = 0.1$											$l = 1.0$											$l = 10$										
T	P	P	P	A	M	A	T	P	P	u'	M	A	T	P	P	u'	M	A	T	P	P	u'	M	A								
										(ft./sec.)						(ft./sec.)						(ft./sec.)										
.668	.188 00	.112 00	.6737 04	.209 01	.2032 01	.57	.895-01	.506-01	.7593 04	.253 01	.3407 01	.495	.533-01	.261-01	.811 0-	.290 01	.534 01	.48	.261-01	.811 0-	.290 01	.534 01	.48									
.66	.182 00	.106 00	.6801 04	.210 01	.2097 01	.56	.843-01	.468-01	.7633 04	.256 01	.3485 01	.48	.481-01	.270-01	.831 0-	.290 01	.542 01	.46	.417-01	.831 0-	.290 01	.542 01	.46									
.64	.146 00	.823-01	.6959 04	.218 01	.2277 01	.54	.743-01	.399-01	.7773 04	.265 01	.3591 01	.46	.360-01	.157-01	.848 0-	.319 01	.563 01	.44	.360-01	.848 0-	.319 01	.563 01	.44									
.62	.131 00	.803-01	.7113 04	.226 01	.2483 01	.52	.650-01	.338-01	.7909 04	.275 01	.3684 01	.42	.309-01	.125-01	.858 0-	.341 01	.580 01	.42	.309-01	.858 0-	.341 01	.580 01	.42									
.60	.117 00	.595-01	.7263 04	.235 01	.2719 01	.50	.575-01	.285-01	.8143 04	.285 01	.3784 01	.40	.263-01	.104-01	.870 0-	.364 01	.600 01	.40	.263-01	.870 0-	.364 01	.600 01	.40									
.58	.104 00	.598-01	.7410 04	.244 01	.2991 01	.48	.502-01	.239-01	.8375 04	.295 01	.3922 01	.38	.223-01	.078-01	.882 0-	.387 01	.627 01	.38	.223-01	.882 0-	.387 01	.627 01	.38									
.56	.924-01	.513-01	.7554 04	.253 01	.3305 01	.46	.433-01	.199-01	.8604 04	.306 01	.4178 01	.36	.187-01	.057-01	.891 0-	.417 01	.654 01	.36	.187-01	.891 0-	.417 01	.654 01	.36									
.54	.817-01	.437-01	.7695 04	.262 01	.3669 01	.44	.376-01	.164-01	.8840 04	.318 01	.4368 01	.34	.156-01	.035-01	.900 0-	.456 01	.682 01	.34	.156-01	.900 0-	.456 01	.682 01	.34									
.52	.719-01	.371-01	.7833 04	.272 01	.4093 01	.42	.322-01	.134-01	.9054 04	.330 01	.4636 01	.32	.128-01	.017-01	.911 0-	.494 01	.710 01	.32	.128-01	.911 0-	.494 01	.710 01	.32									
.50	.631-01	.313-01	.7968 04	.282 01	.4590 01	.40	.275-01	.109-01	.9266 04	.342 01	.4975 01	.30	.105-01	.002-01	.918 0-	.540 01	.756 01	.30	.105-01	.918 0-	.540 01	.756 01	.30									
.48	.550-01	.252-01	.8101 04	.292 01	.5175 01	.38	.233-01	.087-01	.9482 04	.356 01	.5326 01	.28	.084-01	.000-01	.926 0-	.596 01	.804 01	.28	.084-01	.926 0-	.596 01	.804 01	.28									
.46	.477-01	.218-01	.8231 04	.303 01	.5869 01	.36	.195-01	.066-01	.9697 04	.370 01	.5726 01	.26	.067-01	.000-01	.935 0-	.646 01	.856 01	.26	.067-01	.935 0-	.646 01	.856 01	.26									
.44	.412-01	.189-01	.8358 04	.315 01	.6697 01	.34	.163-01	.054-01	.9967 04	.385 01	.6172 01	.24	.051-01	.000-01	.943 0-	.700 01	.906 01	.24	.051-01	.943 0-	.700 01	.906 01	.24									
.42	.353-01	.147-01	.8483 04	.327 01	.7692 01	.32	.134-01	.042-01	.1030 04	.402 01	.6652 01	.22	.041-01	.000-01	.950 0-	.750 01	.956 01	.22	.041-01	.950 0-	.750 01	.956 01	.22									
.40	.301-01	.119-01	.8606 04	.339 01	.8897 01	.30	.110-01	.030-01	.1074 04	.419 01	.7277 01	.20	.032-01	.000-01	.957 0-	.790 01	.1000 01	.20	.032-01	.957 0-	.790 01	.1000 01	.20									
.38	.255-01	.090-01	.8727 04	.353 01	.1037 02	.28	.088-01	.024-01	.1122 04	.438 01	.7977 01	.18	.026-01	.000-01	.964 0-	.810 01	.1050 01	.18	.026-01	.964 0-	.810 01	.1050 01	.18									
.36	.214-01	.074-01	.8845 04	.367 01	.1218 02	.26	.070-01	.020-01	.1171 04	.459 01	.8656 01	.16	.021-01	.000-01	.971 0-	.820 01	.1070 01	.16	.021-01	.971 0-	.820 01	.1070 01	.16									
.34	.178-01	.061-01	.8960 04	.382 01	.1444 02	.24	.054-01	.016-01	.1222 04	.482 01	.9362 01	.14	.017-01	.000-01	.978 0-	.820 01	.1070 01	.14	.017-01	.978 0-	.820 01	.1070 01	.14									
.32	.147-01	.047-01	.9074 04	.399 01	.1728 02	.22	.042-01	.012-01	.1274 04	.508 01	.1000 01	.12	.014-01	.000-01	.985 0-	.810 01	.1030 01	.12	.014-01	.985 0-	.810 01	.1030 01	.12									
.30	.120-01	.037-01	.9185 04	.416 01	.2090 02	.20	.032-01	.009-01	.1326 04	.537 01	.1075 01	.10	.012-01	.000-01	.992 0-	.790 01	.975 01	.10	.012-01	.992 0-	.790 01	.975 01	.10									
.28	.970-02	.269-02	.9294 04	.435 01	.2558 02	.18	.026-01	.008-01	.1379 04	.570 01	.1152 01	.08	.010-01	.000-01	.999 0-	.760 01	.925 01	.08	.010-01	.999 0-	.760 01	.925 01	.08									
.26	.775-02	.192-02	.9400 04	.456 01	.3171 02	.16	.021-01	.007-01	.1431 04	.608 01	.1237 01	.06	.009-01	.000-01	.1000 0-	.720 01	.865 01	.06	.009-01	.1000 0-	.720 01	.865 01	.06									
.24	.639-02	.145-02	.9504 04	.479 01	.3989 02	.14	.017-01	.006-01	.1484 04	.650 01	.1327 01	.04	.008-01	.000-01	.1000 0-	.670 01	.800 01	.04	.008-01	.1000 0-	.670 01	.800 01	.04									
.22	.471-02	.103-02	.9605 04	.504 01	.5102 02	.12	.014-01	.005-01	.1537 04	.706 01	.1431 01	.02	.007-01	.000-01	.1000 0-	.600 01	.725 01	.02	.007-01	.1000 0-	.600 01	.725 01	.02									
.20	.357-02	.708-03	.9704 04	.533 01	.6652 02	.10	.010-01	.004-01	.1590 04	.778 01	.1552 01	.00	.006-01	.000-01	.1000 0-	.530 01	.650 01	.00	.006-01	.1000 0-	.530 01	.650 01	.00									
.18	.265-02	.573-03	.9800 04	.566 01	.8872 02	.09	.008-01	.003-01	.1642 04	.827 01	.1675 01	.00	.005-01	.000-01	.1000 0-	.460 01	.575 01	.00	.005-01	.1000 0-	.460 01	.575 01	.00									
.16	.192-02	.404-03	.9894 04	.604 01	.1217 03	.08	.007-01	.003-01	.1693 04	.885 01	.1800 01	.00	.004-01	.000-01	.1000 0-	.390 01	.500 01	.00	.004-01	.1000 0-	.390 01	.500 01	.00									
.14	.134-02	.285-03	.9985 04	.650 01	.1728 03	.07	.006-01	.002-01	.1744 04	.936 01	.1917 01	.00	.003-01	.000-01	.1000 0-	.320 01	.430 01	.00	.003-01	.1000 0-	.320 01	.430 01	.00									
.12	.890-03	.105-03	.1007 05	.706 01	.2573 03	.06	.005-01	.002-01	.1799 04	.1000 01	.2000 01	.00	.002-01	.000-01	.1000 0-	.250 01	.350 01	.00	.002-01	.1000 0-	.250 01	.350 01	.00									
.10	.553-03	.550-04	.1016 05	.778 01	.4091 03	.05	.004-01	.001-01	.1852 04	.1000 01	.2200 01	.00	.001-01	.000-01	.1000 0-	.180 01	.270 01	.00	.001-01	.1000 0-	.180 01	.270 01	.00									
.08	.423-03	.379-04	.1020 05	.822 01	.5338 03	.04	.003-01	.001-01	.1903 04	.1000 01	.2400 01	.00	.001-01	.000-01	.1000 0-	.140 01	.210 01	.00	.001-01	.1000 0-	.140 01	.210 01	.00									
.06	.313-03	.249-04	.1025 05	.875 01	.7183 03	.03	.002-01	.001-01	.1954 04	.1000 01	.2600 01	.00	.001-01	.000-01	.1000 0-	.100 01	.160 01	.00	.001-01	.1000 0-	.100 01	.160 01	.00									
.07	.223-03	.155-04	.1029 05	.939 01	.1005 04	.02	.001-01	.000-01	.2005 04	.1000 01	.2800 01	.00	.000-01	.000-01	.1000 0-	.070 01	.120 01	.00	.000-01	.1000 0-	.070 01	.120 01	.00									
.06	.151-03	.097-05	.1033 05	.102 02	.1481 04	.01	.000-01	.000-01	.2056 04	.1000 01	.3000 01	.00	.000-01	.000-01	.1000 0-	.040 01	.080 01	.00	.000-01	.1000 0-	.040 01	.080 01	.00									
.05	.949-04	.470-05	.1037 05	.112 02	.2343 04	.00	.000-01	.000-01	.2107 04	.1000 01	.3200 01	.00	.000-01	.000-01	.1000 0-	.030 01	.060 01	.00	.000-01	.1000 0-	.030 01	.060 01	.00									
.04	.539-04	.213-05	.1041 05	.126 02	.4112 04	.00	.000-01	.000-01	.2158 04	.1000 01	.3400 01	.00	.000-01	.000-01	.1000 0-	.020 01	.040 01	.00	.000-01	.1000 0-	.020 01	.040 01	.00									
.03	.259-04	.771-06	.1046 05	.146 02	.8503 04	.00	.000-01	.000-01	.2209 04	.1000 01	.3600 01	.00	.000-01	.000-01	.1000 0-	.010 01	.020 01	.00	.000-01	.1000 0-	.010 01	.020 01	.00									
.02	.927-05	.182-06	.1050 05	.180 02	.1371 05	.00	.000-01	.000-01	.2260 04	.1000 01	.3800 01	.00	.000-01	.000-01	.1000 0-	.000 01	.000 01	.00	.000-01	.1000 0-	.000 01	.000 01	.00									
.01	.159-05	.144-07	.1054 05	.262 02	.1373 06	.00	.000-01	.000-01	.2311 05	.1000 01	.4000 01	.00	.000-01	.000-01	.1000 0-	.000 01	.000 01	.00	.000-01	.1000 0-	.000 01	.000 01	.00									

Table 19a. EXPANSION AFTER FREEZING - WEDGE NOZZLE

 $T_0' = 4000^\circ\text{K}$, $P_0' = 1000$ atm.

l = 10

l = 1.0

l = 0.1

T	P	P	u'	M	A	T	P	P	u'	M	A	T	P	P	u'	M	A	T	P	P	u'	M	A	
.697	.200 00	.138 00	.6463 04	.196 01	.1789 01	.609	.116 00	.700-01	.7251 04	.235 01	.2742 01	.536	.714-01	.379-01	.7819 04	.269 01	.4131 01							
.68	.183 00	.124 00	.6604 04	.201 01	.1905 01	.60	.110 00	.656-01	.7318 04	.237 01	.2858 01	.52	.645-01	.339-01	.7828 04	.275 01	.4513 01							
.66	.165 00	.108 00	.6767 04	.209 01	.2060 01	.58	.983-01	.565-01	.7464 04	.246 01	.3145 01	.50	.565-01	.286-01	.8062 04	.285 01	.5063 01							
.64	.149 00	.945-01	.6925 04	.217 01	.2236 01	.56	.872-01	.484-01	.7606 04	.255 01	.3476 01	.48	.693-01	.234-01	.8193 04	.296 01	.5711 01							
.62	.134 00	.822-01	.7080 04	.225 01	.2438 01	.54	.771-01	.413-01	.7746 04	.264 01	.3860 01	.46	.428-01	.193-01	.8321 04	.307 01	.6480 01							
.60	.120 00	.711-01	.7231 04	.234 01	.2669 01	.52	.679-01	.350-01	.7884 04	.274 01	.4307 01	.44	.369-01	.161-01	.8448 04	.318 01	.7307 01							
.58	.107 00	.613-01	.7378 04	.243 01	.2935 01	.50	.595-01	.295-01	.8018 04	.284 01	.4831 01	.42	.317-01	.131-01	.8671 04	.343 01	.8035 01							
.56	.946-01	.525-01	.7523 04	.252 01	.3242 01	.48	.519-01	.205-01	.8150 04	.294 01	.5449 01	.40	.228-01	.085-02	.8812 04	.356 01	.8835 01							
.54	.836-01	.448-01	.7664 04	.261 01	.3598 01	.46	.451-01	.170-01	.8306 04	.305 01	.6181 01	.38	.192-01	.684-02	.8929 04	.371 01	.9598 02							
.52	.736-01	.380-01	.7803 04	.271 01	.4013 01	.44	.389-01	.139-01	.8506 04	.317 01	.7054 01	.36	.160-01	.538-02	.9044 04	.407 01	.913 02							
.50	.646-01	.320-01	.7939 04	.281 01	.4500 01	.42	.284-01	.113-01	.8652 04	.341 01	.9375 01	.34	.132-01	.417-02	.9266 04	.420 01	.7315 02							
.48	.563-01	.268-01	.8072 04	.292 01	.5073 01	.40	.241-01	.906-02	.8890 04	.355 01	.1093 02	.32	.108-01	.320-02	.9476 04	.439 01	.2834 02							
.46	.489-01	.223-01	.8202 04	.302 01	.5752 01	.38	.202-01	.721-02	.8990 04	.369 01	.1284 02	.30	.868-02	.241-02	.9479 04	.460 01	.3514 02							
.44	.422-01	.184-01	.8330 04	.314 01	.6562 01	.36	.168-01	.567-02	.9005 04	.384 01	.1523 02	.26	.662-02	.178-02	.9479 04	.480 01	.4222 02							
.42	.365-01	.151-01	.8456 04	.326 01	.7536 01	.34	.139-01	.440-02	.9118 04	.401 01	.1623 02	.24	.544-02	.129-02	.9582 04	.493 01	.4422 02							
.40	.308-01	.122-01	.8579 04	.338 01	.8715 01	.32	.113-01	.337-02	.9228 04	.418 01	.2205 02	.22	.421-02	.918-03	.9683 04	.509 01	.5657 02							
.38	.261-01	.984-02	.8700 04	.352 01	.1016 02	.30	.915-02	.254-02	.9336 04	.437 01	.2698 02	.20	.370-02	.633-03	.9781 04	.538 01	.7378 02							
.36	.219-01	.783-02	.8818 04	.366 01	.1414 02	.28	.730-02	.188-02	.9442 04	.456 01	.3346 02	.18	.237-02	.423-03	.9876 04	.570 01	.9843 02							
.34	.183-01	.616-02	.8934 04	.381 01	.1692 02	.26	.574-02	.137-02	.9546 04	.481 01	.4209 02	.16	.171-02	.272-03	.9969 04	.609 01	.1350 03							
.32	.151-01	.478-02	.9048 04	.397 01	.1692 02	.24	.444-02	.968-03	.9647 04	.507 01	.5384 02	.14	.119-02	.166-03	.1066 05	.655 01	.1918 03							
.30	.123-01	.366-02	.9160 04	.415 01	.2046 02	.22	.337-02	.668-03	.9745 04	.535 01	.7021 02	.12	.795-03	.945-04	.1015 05	.711 01	.2858 03							
.28	.994-02	.276-02	.9269 04	.434 01	.2504 02	.20	.250-02	.446-03	.9841 04	.568 01	.9366 02	.10	.496-03	.491-04	.1023 05	.784 01	.4546 03							
.26	.793-02	.204-02	.9375 04	.455 01	.3103 02	.18	.181-02	.287-03	.9934 04	.607 01	.1285 03	.09	.378-03	.337-04	.1028 05	.829 01	.5933 03							
.24	.623-02	.148-02	.9479 04	.478 01	.3903 02	.16	.126-02	.175-03	.1003 05	.652 01	.1825 03	.08	.280-03	.222-04	.1032 05	.882 01	.7085 03							
.22	.482-02	.105-02	.9681 04	.503 01	.4991 02	.14	.839-03	.998-04	.1011 05	.709 01	.2718 03	.07	.199-03	.138-04	.1036 05	.946 01	.117 04							
.20	.366-02	.726-03	.9880 04	.532 01	.6506 02	.12	.523-03	.356-04	.1024 05	.826 01	.5640 03	.05	.847-04	.420-05	.1044 05	.103 02	.1647 04							
.18	.272-02	.485-03	.9777 04	.564 01	.8677 02	.10	.399-03	.234-04	.1029 05	.879 01	.7590 03	.04	.481-04	.190-05	.1049 05	.127 02	.4577 04							
.16	.196-02	.312-03	.9871 04	.602 01	.1190 03	.09	.295-03	.146-04	.1037 05	.943 01	.1062 04	.03	.231-04	.686-06	.1053 05	.147 02	.9468 04							
.14	.137-02	.190-03	.9962 04	.648 01	.1690 03	.08	.210-03	.845-05	.1037 05	.102 02	.1565 04	.02	.826-05	.163-06	.1057 05	.180 02	.2647 05							
.12	.912-03	.109-03	.1005 05	.704 01	.2515 03	.07	.894-04	.443-05	.1041 05	.112 02	.2477 04	.01	.142-05	.144-07	.1061 05	.234 02	.1531 06							
.10	.566-03	.564-04	.1014 05	.776 01	.3998 03	.06	.142-03	.845-05	.1041 05	.112 02	.2477 04	.01	.142-05	.144-07	.1061 05	.234 02	.1531 06							
.09	.434-03	.388-04	.1018 05	.820 01	.5216 03	.05	.508-04	.201-05	.1045 05	.126 02	.4347 04													
.08	.321-03	.255-04	.1022 05	.873 01	.7018 03	.04	.244-04	.727-06	.1049 05	.146 02	.8990 04													
.07	.229-03	.159-04	.1027 05	.937 01	.9816 03	.03	.244-04	.727-06	.1049 05	.146 02	.8990 04													
.06	.155-03	.521-05	.1031 05	.102 02	.1446 04	.02	.180-05	.174-06	.1054 05	.180 02	.2508 05													
.05	.974-04	.483-05	.1035 05	.112 02	.2288 04	.01	.150-05	.144-07	.1058 05	.238 02	.1453 06													
.04	.553-04	.719-05	.1039 05	.125 02	.4015 04																			
.03	.266-04	.294-06	.1043 05	.145 02	.8299 04																			
.02	.952-05	.188-06	.1048 05	.179 02	.2314 05																			
.01	.164-05	.173-07	.1052 05	.250 02	.1339 06																			

Table 19b. EXPANSION AFTER FREEZING - HYPERBOLIC NOZZLE

$T_0' = 4000^\circ\text{K}$, $P_0' = 1000$ atm.

$l = 0.1$ $l = 1.0$ $l = 10$

T	P	M	A	T	P	u'	M	A	T	P	u'	M	A
						(ft./sec.)					(ft./sec.)		
.766	.215 00	.158 00	.7360 04	.190 01	.1690 01	.648	.766 00	.648	.648	.766 00	.904 04	.259 01	.3893 01
.76	.209 00	.152 00	.7416 04	.193 01	.1722 01	.64	.731 01	.64	.64	.656 01	.9098 04	.262 01	.4024 01
.74	.192 00	.136 00	.7600 04	.201 01	.1835 01	.62	.656 01	.62	.62	.588 01	.9247 04	.271 01	.4407 01
.72	.175 00	.121 00	.7779 04	.208 01	.1932 01	.60	.588 01	.60	.60	.524 01	.9393 04	.280 01	.4845 01
.70	.160 00	.107 00	.7954 04	.216 01	.2106 01	.58	.524 01	.58	.58	.466 01	.9537 04	.289 01	.5348 01
.68	.145 00	.945 01	.8125 04	.224 01	.2268 01	.56	.466 01	.56	.56	.413 01	.9679 04	.298 01	.5929 01
.66	.132 00	.831 01	.8293 04	.232 01	.2452 01	.54	.413 01	.54	.54	.368 01	.9819 04	.308 01	.6602 01
.64	.119 00	.729 01	.8457 04	.240 01	.2660 01	.52	.368 01	.52	.52	.319 01	.9956 04	.318 01	.7387 01
.62	.107 00	.638 01	.8617 04	.249 01	.2897 01	.50	.319 01	.50	.50	.279 01	.1009 05	.329 01	.8307 01
.60	.962 01	.553 01	.8775 04	.257 01	.3168 01	.48	.279 01	.48	.48	.242 01	.1022 05	.340 01	.9392 01
.58	.861 01	.478 01	.8930 04	.266 01	.3478 01	.46	.242 01	.46	.46	.209 01	.1036 05	.352 01	.1068 02
.56	.748 01	.412 01	.9081 04	.276 01	.3835 01	.44	.209 01	.44	.44	.179 01	.1049 05	.364 01	.1222 02
.54	.682 01	.353 01	.9231 04	.285 01	.4249 01	.42	.179 01	.42	.42	.153 01	.1061 05	.377 01	.1407 02
.52	.603 01	.300 01	.9377 04	.295 01	.4729 01	.40	.153 01	.40	.40	.129 01	.1074 05	.391 01	.1632 02
.50	.531 01	.254 01	.9521 04	.306 01	.5289 01	.38	.129 01	.38	.38	.108 05	.1086 05	.405 01	.1908 02
.48	.465 01	.214 01	.9663 04	.316 01	.5948 01	.36	.108 05	.36	.36	.08 01	.1098 05	.421 01	.2248 02
.46	.406 01	.179 01	.9802 04	.328 01	.6727 01	.34	.08 01	.34	.34	.07 01	.1110 05	.437 01	.2675 02
.44	.352 01	.148 01	.9939 04	.340 01	.7654 01	.32	.07 01	.32	.32	.06 01	.1122 05	.455 01	.3214 02
.42	.303 01	.122 01	.1007 05	.352 01	.8767 01	.30	.06 01	.30	.30	.05 01	.1134 05	.474 01	.3905 02
.40	.259 01	.993 02	.1021 05	.366 01	.1011 02	.28	.05 01	.28	.28	.04 01	.1145 05	.495 01	.4803 02
.38	.220 01	.801 02	.1034 05	.380 01	.1175 02	.26	.04 01	.26	.26	.03 01	.1156 05	.518 01	.5990 02
.36	.186 01	.640 02	.1046 05	.395 01	.1377 02	.24	.03 01	.24	.24	.02 01	.1167 05	.544 01	.7586 02
.34	.155 01	.505 02	.1059 05	.411 01	.1628 02	.22	.02 01	.22	.22	.01 01	.1178 05	.572 01	.9778 02
.32	.128 01	.384 02	.1071 05	.428 01	.1944 02	.20	.01 01	.20	.20	.01 01	.1188 05	.604 01	.1286 03
.30	.105 01	.302 02	.1084 05	.446 01	.2347 02	.18	.01 01	.18	.18	.01 01	.1199 05	.640 01	.1732 03
.28	.852 02	.228 02	.1096 05	.467 01	.2867 02	.16	.01 01	.16	.16	.01 01	.1209 05	.683 01	.2398 03
.26	.680 02	.169 02	.1107 05	.489 01	.3551 02	.14	.01 01	.14	.14	.01 01	.1218 05	.733 01	.3440 03
.24	.536 02	.123 02	.1119 05	.513 01	.4464 02	.12	.01 01	.12	.12	.01 01	.1228 05	.795 01	.5161 03
.22	.415 02	.873 03	.1130 05	.540 01	.5711 02	.10	.01 01	.10	.10	.01 01	.1237 05	.874 01	.8243 03
.20	.315 02	.603 03	.1141 05	.571 01	.7451 02	.09	.01 01	.09	.09	.01 01	.1246 05	.922 01	.1076 04
.18	.233 02	.402 03	.1152 05	.606 01	.9948 02	.08	.01 01	.08	.08	.01 01	.1255 05	.980 01	.1445 04
.16	.169 02	.259 03	.1162 05	.646 01	.1366 03	.07	.01 01	.07	.07	.01 01	.1264 05	.105 02	.2016 04
.14	.118 02	.158 03	.1172 05	.695 01	.1940 03	.06	.01 01	.06	.06	.01 01	.1273 05	.114 02	.2957 04
.12	.885 03	.902 04	.1182 05	.754 01	.2881 03	.05	.01 01	.05	.05	.01 01	.1281 05	.125 02	.4647 04
.10	.493 03	.472 04	.1192 05	.829 01	.4550 03	.04	.01 01	.04	.04	.01 01	.1289 05	.140 02	.8086 04
.09	.379 03	.326 04	.1196 05	.875 01	.5903 03	.03	.01 01	.03	.03	.01 01	.1298 05	.167 02	.1261 05
.08	.283 03	.217 04	.1201 05	.931 01	.7879 03	.02	.01 01	.02	.02	.01 01	.1307 05	.206 02	.2598 05
.07	.203 03	.156 04	.1206 05	.998 01	.1091 04	.01	.01 01	.01	.01	.01 01	.1316 05	.279 02	.4135 06
.06	.139 03	.800 05	.1210 05	.108 02	.1588 04								
.05	.891 04	.426 05	.1215 05	.119 02	.2472 04								
.04	.516 04	.197 05	.1219 05	.133 02	.4254 04								
.03	.355 04	.732 06	.1224 05	.155 02	.8571 04								
.02	.184 05	.1228 05	.1228 05	.190 02	.2304 05								
.01	.173 05	.160 07	.1233 05	.272 02	.1253 06								

Table 20a. EXPANSION AFTER FREEZING - WEDGE NOZZLE

 $T_0' = 5000^\circ\text{K}$, $P_0' = 100$ atm.

$l = 10$ $l = 1.0$ $l = 0.1$

T	P	P	M	A	T	ρ	u' (ft./sec.)	M	A	T	ρ	P	u' (ft./sec.)	M	A	T	ρ	P	u' (ft./sec.)	M	A
.714	.150 00	.102 00	.216 01	.2223 01	.60	.576-01	.9301 04	.277 01	.4946 01	.513	.270-01	.129-01	.1011 05	.324 01	.2704 01						
.73	.143 05	.938-01	.220 01	.2341 01	.58	.513-01	.9446 04	.286 01	.5467 01	.50	.248-01	.116-01	.1020 05	.333 01	.2167 02						
.68	.127 00	.826-01	.228 01	.2529 01	.56	.455-01	.9589 04	.295 01	.5069 01	.48	.216-01	.959-02	.1033 05	.344 01	.1168 03						
.64	.115 00	.725-01	.236 01	.2743 01	.54	.402-01	.9730 04	.305 01	.6768 01	.46	.187-01	.804-02	.1046 05	.356 01	.1585 04						
.64	.104 00	.634-01	.244 01	.2985 01	.52	.354-01	.9868 04	.315 01	.7584 01	.44	.161-01	.662-02	.1058 05	.368 01	.1565 04						
.62	.932-01	.552-01	.253 01	.3261 01	.50	.310-01	.1000 05	.325 01	.8543 01	.42	.138-01	.540-02	.1071 05	.381 01	.1708 02						
.62	.935-01	.478-01	.261 01	.3577 01	.48	.270-01	.1014 05	.337 01	.9675 01	.40	.117-01	.437-02	.1083 05	.395 01	.2034 03						
.62	.935-01	.412-01	.270 01	.3941 01	.46	.234-01	.1027 05	.348 01	.1102 02	.38	.985-02	.350-02	.1096 05	.410 01	.2486 02						
.62	.935-01	.354-01	.280 01	.4360 01	.44	.202-01	.1040 05	.360 01	.1263 02	.36	.823-02	.277-02	.1108 05	.425 01	.3006 02						
.64	.595-01	.302-01	.289 01	.4846 01	.42	.173-01	.1053 05	.373 01	.1458 02	.34	.682-02	.217-02	.1120 05	.442 01	.3472 02						
.62	.517-01	.257-01	.299 01	.5412 01	.40	.147-01	.1066 05	.387 01	.1694 02	.32	.559-02	.167-02	.1131 05	.460 01	.4146 02						
.62	.366-01	.217-01	.310 01	.6075 01	.38	.124-01	.1078 05	.401 01	.1985 02	.30	.453-02	.127-02	.1143 05	.473 01	.5114 02						
.62	.364-01	.182-01	.321 01	.6857 01	.36	.104-01	.1090 05	.417 01	.2345 02	.28	.363-02	.951-03	.1154 05	.509 01	.6321 02						
.62	.297-01	.125-01	.332 01	.7784 01	.34	.860-02	.1102 05	.433 01	.2796 02	.26	.287-02	.668-03	.1165 05	.523 01	.7923 02						
.62	.217-01	.831-02	.344 01	.8891 01	.32	.706-02	.1114 05	.451 01	.3369 02	.24	.223-02	.501-03	.1176 05	.540 01	.1009 03						
.62	.184-01	.668-02	.357 01	.1022 02	.30	.573-02	.1126 05	.470 01	.4104 02	.22	.171-02	.351-03	.1186 05	.577 01	.1307 03						
.62	.184-01	.531-02	.370 01	.1184 02	.28	.460-02	.1137 05	.491 01	.5063 02	.20	.128-02	.239-03	.1197 05	.610 01	.1730 04						
.62	.154-01	.417-02	.384 01	.1382 02	.26	.384-02	.1148 05	.514 01	.6333 02	.18	.937-03	.158-03	.1207 05	.646 01	.2344 04						
.62	.129-01	.324-02	.399 01	.1627 02	.24	.284-02	.1159 05	.539 01	.8046 02	.16	.666-03	.996-04	.1217 05	.688 01	.3268 04						
.62	.109-01	.247-02	.415 01	.1932 02	.22	.218-02	.1170 05	.567 01	.1041 03	.14	.458-03	.599-04	.1226 05	.740 01	.4771 04						
.62	.863-02	.247-02	.451 01	.2319 02	.20	.163-02	.1181 05	.599 01	.1374 03	.12	.300-03	.337-04	.1236 05	.802 01	.6714 04						
.62	.595-02	.186-02	.472 01	.2814 02	.18	.120-02	.1191 05	.635 01	.1857 03	.10	.185-03	.173-04	.1245 05	.881 01	.1150 04						
.62	.532-02	.137-02	.494 01	.3456 02	.16	.854-03	.1201 05	.677 01	.2583 03	.09	.141-03	.118-04	.1249 05	.930 01	.1508 04						
.62	.432-02	.990-03	.519 01	.5445 02	.14	.588-03	.1211 05	.727 01	.3721 03	.08	.104-03	.776-05	.1253 05	.989 01	.2086 04						
.62	.281-02	.479-03	.546 01	.7009 02	.12	.387-03	.1220 05	.788 01	.5610 03	.07	.738-04	.483-05	.1258 05	.106 02	.2845 04						
.62	.185-02	.317-03	.577 01	.9206 02	.10	.259-03	.1229 05	.867 01	.9007 03	.06	.498-04	.279-05	.1262 05	.115 02	.4714 04						
.62	.132-02	.202-03	.612 01	.1238 03	.08	.182-03	.1234 05	.915 01	.1179 04	.05	.314-04	.147-05	.1266 05	.126 02	.6671 04						
.62	.916-03	.122-03	.701 01	.2453 03	.06	.135-03	.1238 05	.972 01	.1589 04	.04	.178-04	.665-06	.1271 05	.141 02	.1171 05						
.62	.377-03	.695-04	.761 01	.3675 03	.05	.649-04	.1243 05	.104 02	.2224 04	.03	.859-05	.240-06	.1275 05	.164 02	.2414 05						
.62	.288-03	.248-04	.884 01	.7642 03	.04	.113-04	.1256 05	.139 02	.3274 04	.02	.307-05	.572-07	.1279 05	.202 02	.4738 05						
.62	.214-03	.163-04	.939 01	.1026 04	.02	.407-05	.1264 05	.186 02	.5169 04	.01	.530-06	.540-08	.1283 05	.274 02	.4847 05						
.62	.153-03	.102-04	.101 02	.1430 04	.01	.708-06	.1269 05	.301 02	.2950 06												
.62	.104-03	.596-05	.109 02	.2095 04																	
.62	.650-04	.315-05	.120 02	.3289 04																	
.62	.378-04	.144-05	.125 05	.5715 04																	
.62	.318-04	.929-06	.156 02	.1166 05																	
.62	.673-05	.128-06	.192 02	.3192 05																	
.62	.120-05	.108-07	.277 02	.1790 06																	

Table 21a. EXPANSION AFTER FREEZING - WEDGE NOZZLE

T₀' = 5000°K, p₀' = 200 atm.

$l = 10$

$l = 1.0$

$l = 0.1$

T	P	A	M	A	T	ϵ	P	u' (ft/sec.)	M	A	T	P	u' (ft/sec.)	M	A	T	P	u' (ft/sec.)	M	A		
.746	.194	.00	.140	.00	.7495	.04	.198	.01	.1804	.01	.652	.905	.8723	.04	.248	.01	.3356	.01	.447	.01	.624	.01
.74	.191	.00	.136	.00	.7550	.04	.200	.01	.1840	.01	.64	.850	.8817	.04	.253	.01	.3537	.01	.457	.01	.634	.01
.72	.174	.00	.126	.00	.7730	.04	.207	.01	.1970	.01	.62	.763	.8971	.04	.261	.01	.3872	.01	.471	.01	.648	.01
.70	.158	.00	.108	.00	.7906	.04	.215	.01	.2118	.01	.60	.682	.9122	.04	.270	.01	.4256	.01	.485	.01	.663	.01
.65	.144	.00	.937	.01	.8077	.04	.223	.01	.2285	.01	.58	.608	.9270	.04	.279	.01	.4698	.01	.498	.01	.678	.01
.66	.130	.00	.823	.01	.8245	.04	.231	.01	.2474	.01	.56	.540	.9416	.04	.288	.01	.5208	.01	.512	.01	.692	.01
.64	.117	.00	.720	.01	.8410	.04	.239	.01	.2689	.01	.54	.478	.9559	.04	.298	.01	.5799	.01	.525	.01	.707	.01
.62	.105	.00	.627	.01	.8571	.04	.248	.01	.2934	.01	.52	.421	.9700	.04	.308	.01	.6493	.01	.540	.01	.722	.01
.60	.944	.01	.544	.01	.8729	.04	.256	.01	.3214	.01	.50	.369	.9839	.04	.319	.01	.7299	.01	.554	.01	.737	.01
.58	.843	.01	.470	.01	.8885	.04	.265	.01	.3536	.01	.48	.322	.9975	.04	.330	.01	.8254	.01	.568	.01	.752	.01
.56	.750	.01	.404	.01	.9037	.04	.274	.01	.3907	.01	.46	.279	.1011	.05	.341	.01	.9389	.01	.582	.01	.767	.01
.54	.665	.01	.345	.01	.9186	.04	.284	.01	.4337	.01	.44	.241	.1024	.05	.353	.01	1.075	.02	.596	.01	.782	.01
.52	.587	.01	.293	.01	.9333	.04	.294	.01	.4837	.01	.42	.206	.1037	.05	.366	.01	1.238	.02	.610	.01	.797	.01
.50	.515	.01	.247	.01	.9478	.04	.304	.01	.5423	.01	.40	.176	.1050	.05	.380	.01	1.437	.02	.624	.01	.812	.01
.48	.451	.01	.208	.01	.9619	.04	.315	.01	.6114	.01	.38	.148	.1063	.05	.394	.01	1.681	.02	.638	.01	.827	.01
.46	.392	.01	.173	.01	.9759	.04	.327	.01	.6932	.01	.36	.124	.1075	.05	.409	.01	1.982	.02	.652	.01	.842	.01
.44	.339	.01	.143	.01	.9896	.04	.339	.01	.7908	.01	.34	.103	.1087	.05	.426	.01	2.360	.02	.666	.01	.857	.01
.42	.291	.01	.117	.01	1.003	.05	.351	.01	.9081	.01	.32	.849	.1099	.05	.443	.01	2.838	.02	.680	.01	.872	.01
.40	.248	.01	.953	.02	1.016	.05	.364	.01	1.050	.02	.30	.691	.1111	.05	.462	.01	3.452	.02	.694	.01	.887	.01
.38	.210	.01	.767	.02	1.029	.05	.378	.01	1.224	.02	.28	.555	.1123	.05	.482	.01	4.250	.02	.708	.01	.902	.01
.36	.177	.01	.611	.02	1.042	.05	.393	.01	1.439	.02	.26	.440	.1134	.05	.505	.01	5.306	.02	.722	.01	.917	.01
.34	.147	.01	.483	.02	1.055	.05	.409	.01	1.707	.02	.24	.344	.1145	.05	.530	.01	6.729	.02	.736	.01	.932	.01
.32	.121	.01	.373	.02	1.067	.05	.426	.01	2.046	.02	.22	.264	.1156	.05	.558	.01	8.684	.02	.750	.01	.947	.01
.30	.990	.02	.285	.02	1.079	.05	.445	.01	2.478	.02	.20	.199	.1167	.05	.589	.01	11.44	.03	.764	.01	.962	.01
.28	.799	.02	.215	.02	1.091	.05	.465	.01	3.040	.02	.18	.146	.1177	.05	.625	.01	15.43	.03	.778	.01	.977	.01
.26	.635	.02	.159	.02	1.103	.05	.487	.01	3.780	.02	.16	.104	.1187	.05	.667	.01	21.40	.03	.792	.01	.992	.01
.24	.498	.02	.115	.02	1.115	.05	.512	.01	4.773	.02	.14	.720	.1197	.05	.716	.01	30.76	.03	.806	.01	1.007	.01
.22	.384	.02	.810	.03	1.126	.05	.539	.01	6.133	.02	.12	.475	.1207	.05	.777	.01	46.24	.03	.820	.01	1.022	.01
.20	.290	.02	.557	.03	1.137	.05	.569	.01	8.041	.02	.10	.294	.1216	.05	.854	.01	74.02	.03	.834	.01	1.037	.01
.18	.214	.02	.370	.03	1.148	.05	.604	.01	1.079	.03	.08	.224	.1221	.05	.901	.01	96.72	.03	.848	.01	1.052	.01
.16	.154	.02	.236	.03	1.158	.05	.645	.01	1.490	.03	.06	.166	.1225	.05	.958	.01	130.1	.04	.862	.01	1.067	.01
.14	.107	.02	.143	.03	1.168	.05	.693	.01	2.129	.03	.07	.119	.1230	.05	1.032	.02	181.7	.04	.876	.01	1.082	.01
.12	.797	.03	.814	.04	1.178	.05	.742	.01	3.182	.03	.06	.804	.1234	.05	1.112	.02	267.0	.04	.890	.01	1.097	.01
.10	.44	.03	.423	.04	1.188	.05	.827	.01	5.061	.03	.05	.509	.1238	.05	1.222	.02	420.5	.04	.904	.01	1.112	.01
.08	.337	.03	.291	.04	1.197	.05	.873	.01	6.591	.03	.04	.291	.1243	.05	1.372	.02	733.3	.04	.918	.01	1.127	.01
.06	.251	.03	.192	.04	1.197	.05	.928	.01	8.834	.03	.03	.141	.1247	.05	1.592	.02	1503	.05	.932	.01	1.142	.01
.04	.175	.03	.121	.04	1.202	.05	.995	.01	12.29	.04	.02	.111	.1252	.05	1.952	.02	4141	.05	.946	.01	1.157	.01
.02	.122	.03	.764	.05	1.206	.05	1.082	.01	17.97	.04	.01	.804	.1256	.05	2.281	.02	2347	.06	.960	.01	1.172	.01
.00	.777	.04	.373	.05	1.211	.05	1.118	.02	28.16	.04	.00	.294	.1256	.05	2.612	.02	3317	.06	.974	.01	1.187	.01
.04	.447	.04	.172	.05	1.215	.05	1.133	.02	4.881	.04	.00	.224	.1256	.05	2.943	.02	4500	.06	.988	.01	1.202	.01
.03	.219	.04	.629	.06	1.220	.05	1.144	.02	6.926	.04	.00	.166	.1256	.05	3.274	.02	6060	.06	1.002	.01	1.217	.01
.02	.801	.05	.153	.06	1.224	.05	1.190	.02	27.04	.05	.00	.104	.1256	.05	3.605	.02	8200	.06	1.016	.01	1.232	.01
.01	.143	.05	.136	.07	1.229	.05	1.270	.02	1504	.06	.00	.899	.1256	.05	3.936	.02	10900	.06	1.030	.01	1.247	.01

Table 21b. EXPANSION AFTER FREEZING - HYPERBOLIC NOZZLE

$T_0' = 5000^\circ K, p_0' = 200 \text{ atm.}$

$l = 0.1$										$l = 1.0$										$l = 10$									
T	P	P	u'	M	A	T	P	P	u'	M	A	T	P	P	u'	M	A	T	P	P	u'	M	A						
			(ft./sec.)						(ft./sec.)						(ft./sec.)						(ft./sec.)								
.679	.121	.00	.8255	.230	.01	.575	.510	.01	.9380	.284	.01	.5511	.255	.01	.1011	.330	.01	.49	.118	.01	.1011	.330	.01						
.66	.110	.00	.8411	.236	.01	.56	.466	.01	.9488	.291	.01	.5664	.238	.01	.1018	.338	.01	.48	.109	.01	.1018	.338	.01						
.64	.989	.01	.8572	.245	.01	.54	.411	.01	.9630	.301	.01	.6653	.206	.01	.1031	.349	.01	.46	.982	.01	.1031	.349	.01						
.62	.888	.01	.8730	.253	.01	.52	.362	.01	.9769	.311	.01	.7458	.177	.01	.1044	.362	.01	.44	.784	.02	.1044	.362	.01						
.60	.794	.01	.8885	.262	.01	.50	.317	.01	.9907	.322	.01	.8604	.151	.01	.1057	.375	.01	.42	.599	.02	.1057	.375	.01						
.58	.708	.01	.9037	.271	.01	.48	.276	.01	.1004	.333	.01	.9521	.125	.01	.1069	.388	.01	.40	.484	.02	.1069	.388	.01						
.56	.629	.01	.9187	.280	.01	.46	.239	.01	.1018	.344	.01	.1085	.104	.01	.1081	.403	.01	.38	.388	.02	.1081	.403	.01						
.54	.556	.01	.9334	.290	.01	.44	.208	.01	.1031	.356	.01	.1244	.080	.01	.1094	.418	.01	.36	.307	.02	.1094	.418	.01						
.52	.490	.01	.9478	.300	.01	.42	.176	.01	.1044	.369	.01	.1437	.056	.01	.1106	.435	.01	.34	.240	.02	.1106	.435	.01						
.50	.429	.01	.9620	.310	.01	.40	.149	.01	.1056	.383	.01	.1671	.032	.01	.1117	.452	.01	.32	.185	.02	.1117	.452	.01						
.48	.374	.01	.9759	.321	.01	.38	.126	.01	.1069	.397	.01	.1958	.008	.01	.1129	.471	.01	.30	.141	.02	.1129	.471	.01						
.46	.325	.01	.9897	.333	.01	.36	.105	.01	.1081	.412	.01	.2315	.002	.01	.1143	.492	.01	.28	.399	.02	.1143	.492	.01						
.44	.280	.01	.1003	.345	.01	.34	.873	.02	.1093	.429	.01	.2763	.002	.01	.1152	.515	.01	.26	.772	.03	.1152	.515	.01						
.42	.240	.01	.1016	.357	.01	.32	.716	.02	.1105	.446	.01	.3331	.002	.01	.1163	.541	.01	.24	.245	.02	.1163	.541	.01						
.40	.204	.01	.1030	.371	.01	.30	.581	.02	.1117	.465	.01	.4061	.002	.01	.1173	.569	.01	.22	.187	.02	.1173	.569	.01						
.38	.173	.01	.1042	.385	.01	.28	.466	.02	.1128	.486	.01	.5014	.002	.01	.1184	.600	.01	.20	.140	.02	.1184	.600	.01						
.36	.145	.01	.1055	.400	.01	.26	.368	.02	.1140	.509	.01	.6277	.002	.01	.1194	.637	.01	.18	.103	.02	.1194	.637	.01						
.34	.120	.01	.1067	.416	.01	.24	.287	.02	.1151	.534	.01	.7984	.002	.01	.1204	.679	.01	.16	.730	.03	.1204	.679	.01						
.32	.987	.02	.1080	.433	.01	.22	.220	.02	.1162	.562	.01	.1034	.002	.01	.1214	.729	.01	.14	.501	.03	.1214	.729	.01						
.30	.845	.02	.1104	.452	.01	.20	.165	.02	.1172	.593	.01	.1366	.002	.01	.1223	.790	.01	.12	.329	.03	.1223	.790	.01						
.28	.739	.02	.1138	.472	.01	.18	.121	.02	.1183	.629	.01	.1849	.002	.01	.1232	.869	.01	.10	.202	.03	.1232	.869	.01						
.26	.645	.02	.1155	.495	.01	.16	.858	.03	.1193	.671	.01	.2575	.002	.01	.1241	.917	.01	.09	.154	.03	.1241	.917	.01						
.24	.599	.02	.1169	.519	.01	.14	.590	.03	.1202	.720	.01	.3715	.002	.01	.1250	.974	.01	.08	.114	.03	.1250	.974	.01						
.22	.551	.03	.1189	.547	.01	.12	.388	.03	.1212	.781	.01	.5610	.002	.01	.1258	.104	.02	.07	.806	.04	.1258	.104	.02						
.20	.505	.02	.1198	.577	.01	.10	.239	.03	.1221	.859	.01	.9023	.002	.01	.1264	.124	.02	.06	.544	.04	.1264	.124	.02						
.18	.469	.02	.1215	.603	.01	.09	.182	.03	.1226	.906	.01	.1182	.002	.01	.1272	.142	.02	.05	.342	.04	.1272	.142	.02						
.16	.421	.02	.1230	.633	.01	.08	.134	.03	.1235	.964	.01	.1595	.002	.01	.1280	.159	.02	.04	.194	.04	.1280	.159	.02						
.14	.383	.03	.1249	.662	.01	.07	.955	.04	.1245	.103	.02	.2335	.002	.01	.1287	.162	.02	.03	.936	.05	.1287	.162	.02						
.12	.341	.03	.1268	.692	.01	.06	.646	.04	.1259	.112	.02	.3295	.002	.01	.1295	.199	.02	.02	.633	.05	.1295	.199	.02						
.10	.305	.02	.1287	.722	.01	.05	.407	.04	.1273	.123	.02	.5210	.002	.01	.1303	.280	.02	.01	.357	.06	.1303	.280	.02						
.08	.263	.03	.1306	.752	.01	.04	.231	.04	.1288	.138	.02	.9132	.002	.01	.1312	.471	.02	.00	.188	.06	.1312	.471	.02						
.06	.226	.04	.1325	.782	.01	.03	.112	.04	.1305	.156	.02	.1884	.002	.01	.1321	.869	.02	.00	.104	.07	.1321	.869	.02						
.04	.193	.03	.1344	.812	.01	.02	.601	.05	.1323	.176	.02	.2637	.002	.01	.1330	.162	.02	.00	.633	.07	.1330	.162	.02						
.02	.157	.03	.1363	.842	.01	.01	.694	.06	.1346	.196	.02	.3537	.002	.01	.1340	.280	.02	.00	.335	.05	.1340	.280	.02						
.00	.121	.04	.1382	.872	.01	.00	.550	.08	.1366	.226	.02	.5014	.002	.01	.1350	.471	.02	.00	.257	.06	.1350	.471	.02						

Table 22a. EXPANSION AFTER FREEZING - WEDGE NOZZLE

 $T_0' = 5000^\circ K$, $p_0' = 300$ atm.

$I = 10$

$I = 1.0$

$I = 0.1$

T	P	A	M	A	T	P	u'	M	A	T	P	P	u'	M	A	T	P	u'	M	A	T	P	u'	M	A
							(ft/sec.)						(ft/sec.)					(ft/sec.)					(ft/sec.)		
.718	.145 00	.114 00	.7765 04	.210 01	.2058 01	.625	.460-01	.8872 04	.258 01	.3834 01	.602-01	.207-01	.9646 04	.300 01	.6799 01										
.70	.152 00	.122 00	.7918 04	.216 01	.2194 01	.62	.444-01	.8911 04	.259 01	.3924 01	.587-01	.197-01	.9688 04	.303 01	.7030 01										
.68	.138 00	.898-01	.8089 04	.223 01	.2370 01	.60	.384-01	.9063 04	.268 01	.4316 01	.540-01	.167-01	.9827 04	.313 01	.7884 01										
.66	.124 00	.788-01	.8257 04	.231 01	.2569 01	.58	.331-01	.9212 04	.277 01	.4767 01	.508-01	.141-01	.9963 04	.324 01	.8884 01										
.64	.112 00	.689-01	.8421 04	.240 01	.2796 01	.56	.284-01	.9358 04	.286 01	.5288 01	.559-01	.118-01	.1010 05	.335 01	.1007 02										
.62	.101 00	.599-01	.8582 04	.248 01	.3054 01	.54	.242-01	.9502 04	.296 01	.5893 01	.624-01	.875-02	.1023 05	.346 01	.1149 02										
.60	.900-01	.519-01	.8740 04	.257 01	.3350 01	.52	.414-01	.9644 04	.306 01	.6599 01	.693-02	.803-02	.1036 05	.349 01	.1318 02										
.58	.802-01	.448-01	.8895 04	.266 01	.3680 01	.50	.174-01	.9783 04	.317 01	.7429 01	.740-01	.650-02	.1049 05	.371 01	.1527 02										
.56	.714-01	.384-01	.9047 04	.275 01	.4083 01	.48	.126-01	.9921 04	.328 01	.8408 01	.818-01	.424-02	.1062 05	.385 01	.1771 02										
.54	.632-01	.328-01	.9196 04	.285 01	.4539 01	.46	.274-01	.1008 05	.339 01	.9573 01	.988-02	.336-02	.1074 05	.399 01	.2077 02										
.52	.557-01	.278-01	.9342 04	.295 01	.5070 01	.44	.987-02	.1019 05	.351 01	.1097 02	.818-02	.263-02	.1088 05	.415 01	.2456 02										
.50	.488-01	.236-01	.9486 04	.305 01	.5692 01	.42	.202-01	.1032 05	.364 01	.1265 02	.671-02	.203-02	.1110 05	.440 01	.3337 02										
.48	.423-01	.196-01	.9628 04	.316 01	.6426 01	.40	.172-01	.1045 05	.377 01	.1469 02	.545-02	.154-02	.1122 05	.468 01	.4315 02										
.46	.370-01	.163-01	.9767 04	.327 01	.7298 01	.38	.145-01	.1057 05	.392 01	.1721 02	.436-02	.114-02	.1133 05	.489 01	.5330 02										
.44	.319-01	.135-01	.9904 04	.339 01	.8339 01	.36	.121-01	.1070 05	.407 01	.2032 02	.345-02	.847-03	.1145 05	.512 01	.6077 02										
.42	.274-01	.110-01	.1004 05	.352 01	.9592 01	.34	.101-01	.1082 05	.423 01	.2422 02	.289-02	.609-03	.1156 05	.537 01	.8494 02										
.40	.233-01	.896-02	.1017 05	.365 01	.1111 02	.32	.826-02	.1094 05	.441 01	.2917 02	.295-02	.427-03	.1166 05	.565 01	.1101 03										
.38	.197-01	.720-02	.1030 05	.379 01	.1298 02	.30	.671-02	.1106 05	.460 01	.3552 02	.154-02	.291-03	.1177 05	.596 01	.1450 03										
.36	.165-01	.572-02	.1043 05	.394 01	.1517 02	.28	.426-02	.1118 05	.480 01	.4381 02	.113-02	.192-03	.1187 05	.632 01	.1972 03										
.34	.137-01	.449-02	.1056 05	.410 01	.1817 02	.26	.332-02	.1129 05	.503 01	.5478 02	.801-03	.121-03	.1197 05	.674 01	.2744 03										
.32	.113-01	.348-02	.1068 05	.427 01	.2182 02	.24	.255-02	.1140 05	.528 01	.6958 02	.531-03	.728-04	.1207 05	.724 01	.3967 03										
.30	.921-02	.266-02	.1080 05	.446 01	.2649 02	.22	.191-02	.1151 05	.555 01	.8997 02	.295-02	.410-04	.1216 05	.785 01	.5946 03										
.28	.841-02	.199-02	.1092 05	.466 01	.3256 02	.20	.140-02	.1162 05	.586 01	.1187 03	.361-03	.210-04	.1226 05	.863 01	.9654 03										
.26	.688-02	.147-02	.1104 05	.488 01	.4059 02	.18	.999-03	.1172 05	.622 01	.1605 03	.233-03	.145-04	.1230 05	.911 01	.1265 04										
.24	.588-02	.106-02	.1115 05	.512 01	.5138 02	.16	.688-03	.1183 05	.663 01	.2231 03	.189-03	.144-04	.1235 05	.968 01	.1704 04										
.22	.554-02	.747-03	.1126 05	.540 01	.6221 02	.14	.453-03	.1192 05	.713 01	.3214 03	.125-03	.545-05	.1239 05	.104 02	.2395 04										
.20	.465-02	.512-03	.1137 05	.570 01	.8705 02	.12	.280-03	.1202 05	.773 01	.4845 03	.888-04	.587-05	.1243 05	.112 02	.3533 04										
.18	.365-02	.330-03	.1148 05	.605 01	.1172 03	.10	.213-03	.1211 05	.850 01	.7778 03	.600-04	.340-05	.1248 05	.123 02	.5592 04										
.16	.265-02	.216-03	.1158 05	.645 01	.1523 03	.08	.157-03	.1216 05	.897 01	.1018 04	.378-04	.178-05	.1252 05	.139 02	.9810 04										
.14	.195-02	.153-03	.1169 05	.694 01	.2328 03	.06	.112-03	.1220 05	.954 01	.1372 04	.215-04	.12-06	.1256 05	.160 02	.2026 05										
.12	.945-03	.739-04	.1178 05	.752 01	.3493 03	.04	.479-04	.1225 05	.102 02	.1920 04	.104-04	.295-06	.1261 05	.198 02	.5641 05										
.10	.641-03	.392-04	.1188 05	.828 01	.5781 03	.02	.432-05	.1229 05	.111 02	.2827 04	.371-05	.688-07	.1261 05	.290 02	.3257 06										
.08	.364-03	.173-04	.1197 05	.929 01	.9782 03	.04	.377-06	.1234 05	.122 02	.4463 04	.640-06	.550-08	.1265 05	.290 02	.3257 06										
.07	.161-03	.139-04	.1202 05	.996 01	.1365 04	.02	.827-06	.1238 05	.158 02	.1607 05															
.06	.109-03	.649-05	.1206 05	.108 02	.2002 04	.02			.194 02	.4452 05															
.05	.692-04	.232-05	.1211 05	.119 02	.3148 04	.01			.273 02	.2548 06															
.04	.396-04	.152-05	.1215 05	.133 02	.5479 04																				
.03	.193-04	.556-06	.1220 05	.154 02	.1120 05																				
.02	.700-05	.135-06	.1224 05	.190 02	.3076 05																				
.01	.124-05	.110-07	.1229 05	.1276 02	.1733 06																				

Table 22b. EXPANSION AFTER FREEZING - HYPERBOLIC NOZZLE

$T_0 = 5000^\circ K$, $P_0 = 300$ atm.

$l = 0.1$ $l = 1.0$ $l = 10$

T	P	P	u' (ft./sec.)	M	A	T	P	u' (ft./sec.)	M	A	T	P	P	u' (ft./sec.)	M	A	T	P	P	u' (ft./sec.)	M	A		
.59	.747-01	.626-01	.8815 04	.263 01	.3963 01	.499	.368-01	.177-01	.9609 04	.310 01	.7380 01	.429	.205-01	.848-02	.350 01	.7380 01	.429	.205-01	.848-02	.350 01	.7380 01	.429	.205-01	.848-02
.58	.704-01	.595-01	.8892 04	.265 01	.4167 01	.48	.322-01	.149-01	.9742 04	.320 01	.8310 01	.42	.191-01	.773-02	.357 01	.8310 01	.42	.191-01	.773-02	.357 01	.8310 01	.42	.191-01	.773-02
.56	.624-01	.338-01	.9044 04	.275 01	.4621 01	.46	.279-01	.124-01	.9879 04	.331 01	.9470 01	.40	.162-01	.625-02	.371 01	.9470 01	.40	.162-01	.625-02	.371 01	.9470 01	.40	.162-01	.625-02
.54	.551-01	.268-01	.9193 04	.284 01	.5149 01	.44	.240-01	.102-01	.1001 05	.343 01	.1086 02	.38	.136-01	.500-02	.385 01	.1086 02	.38	.136-01	.500-02	.385 01	.1086 02	.38	.136-01	.500-02
.52	.483-01	.244-01	.9339 04	.294 01	.5766 01	.42	.205-01	.831-02	.1015 05	.356 01	.1254 02	.36	.114-01	.396-02	.400 01	.1254 02	.36	.114-01	.396-02	.400 01	.1254 02	.36	.114-01	.396-02
.50	.428-01	.205-01	.9483 04	.305 01	.6490 01	.40	.174-01	.672-02	.1028 05	.369 01	.1459 02	.34	.944-02	.309-02	.416 01	.1459 02	.34	.944-02	.309-02	.416 01	.1459 02	.34	.944-02	.309-02
.48	.369-01	.171-01	.9624 04	.315 01	.7347 01	.38	.147-01	.538-02	.1041 05	.383 01	.1710 02	.32	.773-02	.239-02	.433 01	.1710 02	.32	.773-02	.239-02	.433 01	.1710 02	.32	.773-02	.239-02
.46	.323-01	.142-01	.9763 04	.327 01	.8366 01	.36	.123-01	.425-02	.1053 05	.398 01	.2023 02	.30	.627-02	.181-02	.452 01	.2023 02	.30	.627-02	.181-02	.452 01	.2023 02	.30	.627-02	.181-02
.44	.275-01	.117-01	.9900 04	.339 01	.9587 01	.34	.101-01	.333-02	.1066 05	.414 01	.2414 02	.28	.502-02	.136-02	.472 01	.2414 02	.28	.502-02	.136-02	.472 01	.2414 02	.28	.502-02	.136-02
.42	.235-01	.095-02	1.003 05	.351 01	1.1106 02	.32	.831-02	.257-02	1.078 05	.431 01	.2912 02	.26	.396-02	.994-03	.495 01	.2912 02	.26	.396-02	.994-03	.495 01	.2912 02	.26	.396-02	.994-03
.40	.200-01	.073-02	1.017 05	.364 01	1.286 02	.30	.674-02	.195-02	1.090 05	.450 01	.3553 02	.24	.308-02	.713-03	.519 01	.3553 02	.24	.308-02	.713-03	.519 01	.3553 02	.24	.308-02	.713-03
.38	.168-01	.059-02	1.030 05	.378 01	1.506 02	.28	.540-02	.146-02	1.102 05	.470 01	.4390 02	.22	.236-02	.500-03	.546 01	.4390 02	.22	.236-02	.500-03	.546 01	.4390 02	.22	.236-02	.500-03
.36	.141-01	.040-02	1.042 05	.393 01	1.780 02	.26	.426-02	.107-02	1.113 05	.493 01	.5500 02	.20	.176-02	.340-03	.577 01	.5500 02	.20	.176-02	.340-03	.577 01	.5500 02	.20	.176-02	.340-03
.34	.117-01	.033-02	1.055 05	.409 01	2.123 02	.24	.331-02	.767-03	1.125 05	.517 01	.7001 02	.18	.129-02	.224-03	.612 01	.7001 02	.18	.129-02	.224-03	.612 01	.7001 02	.18	.129-02	.224-03
.32	.095-02	.026-02	1.067 05	.426 01	2.559 02	.22	.253-02	.538-03	1.136 05	.544 01	.9073 02	.16	.916-03	.141-03	.653 01	.9073 02	.16	.916-03	.141-03	.653 01	.9073 02	.16	.916-03	.141-03
.30	.075-02	.025-02	1.079 05	.445 01	3.119 02	.20	.190-02	.366-03	1.146 05	.575 01	1.200 03	.14	.612-03	.085-04	.761 01	1.200 03	.14	.612-03	.085-04	.761 01	1.200 03	.14	.612-03	.085-04
.28	.621-02	.168-02	1.091 05	.465 01	3.851 02	.18	.139-02	.241-03	1.157 05	.610 01	1.627 03	.12	.425-03	.245-04	.837 01	1.627 03	.12	.425-03	.245-04	.837 01	1.627 03	.12	.425-03	.245-04
.26	.491-02	.123-02	1.103 05	.487 01	4.621 02	.16	.086-03	.152-03	1.177 05	.651 01	2.268 03	.09	.193-03	.167-04	.883 01	2.268 03	.09	.193-03	.167-04	.883 01	2.268 03	.09	.193-03	.167-04
.24	.382-02	.087-03	1.114 05	.511 01	6.131 02	.14	.676-03	.913-04	1.187 05	.699 01	4.958 03	.08	.142-03	.110-04	.934 01	4.958 03	.08	.142-03	.110-04	.934 01	4.958 03	.08	.142-03	.110-04
.22	.292-02	.621-03	1.126 05	.539 01	7.938 02	.12	.443-03	.513-04	1.196 05	.758 01	7.990 03	.07	.101-03	.081-05	.101 02	7.990 03	.07	.101-03	.081-05	.101 02	7.990 03	.07	.101-03	.081-05
.20	.219-02	.423-03	1.137 05	.569 01	10.49 03	.10	.273-03	.263-04	1.201 05	.834 01	10.48 04	.06	.681-04	.036-05	.129 02	10.48 04	.06	.681-04	.036-05	.129 02	10.48 04	.06	.681-04	.036-05
.18	.160-02	.279-03	1.147 05	.604 01	14.20 03	.09	.207-03	.180-04	1.201 05	.880 01	14.16 04	.05	.428-04	.206-05	.156 02	14.16 04	.05	.428-04	.206-05	.156 02	14.16 04	.05	.428-04	.206-05
.16	.114-02	.176-03	1.158 05	.644 01	19.79 03	.08	.153-03	.118-04	1.206 05	.936 01	19.86 04	.04	.243-04	.036-06	.184 02	19.86 04	.04	.243-04	.036-06	.184 02	19.86 04	.04	.243-04	.036-06
.14	.078-03	.106-03	1.168 05	.692 01	28.56 03	.07	.109-03	.073-05	1.210 05	1.002 01	28.93 04	.03	.117-04	.038-06	.212 02	28.93 04	.03	.117-04	.038-06	.212 02	28.93 04	.03	.117-04	.038-06
.12	.511-03	.596-04	1.177 05	.751 01	43.14 03	.06	.073-04	.042-05	1.215 05	1.092 01	43.33 04	.02	.041-05	.038-06	.232 02	43.33 04	.02	.041-05	.038-06	.232 02	43.33 04	.02	.041-05	.038-06
.10	.317-03	.306-04	1.187 05	.826 01	65.93 03	.05	.046-04	.022-05	1.219 05	1.192 01	66.46 04	.01	.017-05	.038-06	.256 02	66.46 04	.01	.017-05	.038-06	.256 02	66.46 04	.01	.017-05	.038-06
.09	.241-03	.210-04	1.192 05	.872 01	91.00 03	.04	.026-04	.010-05	1.223 05	1.34 02	91.61 04	.01	.017-05	.038-06	.281 02	91.61 04	.01	.017-05	.038-06	.281 02	91.61 04	.01	.017-05	.038-06
.08	.178-03	.137-04	1.196 05	.927 01	122.8 04	.03	.0126-04	.0364-06	1.228 05	1.55 02	123.05	.01	.017-05	.038-06	.311 02	123.05	.01	.017-05	.038-06	.311 02	123.05	.01	.017-05	.038-06
.07	.128-03	.095-05	1.201 05	.994 01	172.2 04	.02	.0049-05	.0874-07	1.232 05	1.91 02	168.9 05	.01	.017-06	.038-06	.347 02	168.9 05	.01	.017-06	.038-06	.347 02	168.9 05	.01	.017-06	.038-06
.05	.853-04	.495-05	1.205 05	1.08 02	254.0 04	.01	.00772-06	.0840-08	1.237 05	2.62 02	273.4 06	.00	.017-06	.038-06	.384 02	273.4 06	.00	.017-06	.038-06	.384 02	273.4 06	.00	.017-06	.038-06
.04	.305-04	.118-05	1.210 05	1.18 02	401.9 04	.01	.00207-06	.049 04	1.240 05	3.49 04	401.9 04	.00	.017-06	.038-06	.428 02	401.9 04	.00	.017-06	.038-06	.428 02	401.9 04	.00	.017-06	.038-06
.03	.147-04	.026-06	1.219 05	1.54 02	145.6 05	.01	.00126-06	.0126-06	1.241 05	4.65 05	145.6 05	.00	.017-06	.038-06	.476 02	145.6 05	.00	.017-06	.038-06	.476 02	145.6 05	.00	.017-06	.038-06
.02	.528-05	.101-06	1.223 05	1.89 02	405.3 05	.01	.00049-05	.0874-07	1.242 05	6.19 02	405.3 05	.00	.017-06	.038-06	.528 05	405.3 05	.00	.017-06	.038-06	.528 05	405.3 05	.00	.017-06	.038-06
.01	.908-06	.840-08	1.228 05	2.73 02	234.2 06	.01	.000772-06	.0840-08	1.237 05	3.49 04	401.9 04	.00	.017-06	.038-06	.572 02	401.9 04	.00	.017-06	.038-06	.572 02	401.9 04	.00	.017-06	.038-06

Table 23a. EXPANSION AFTER FREEZING - WEDGE NOZZLE
 $T_0' = 5000^\circ K$, $p_0' = 1000$ atm.

$l = 10$

$l = 1.0$

$l = 0.1$

T	P	P	P	A	T	ρ	P	u' (ft./sec.)	M	A	T	ρ	P	u' (ft./sec.)	M	A
.638	.107 00	.666-01	.8335 04	.239 01	.552	.563-01	.300-01	.9164 04	.282 01	.5059 01	.481	.318-01	.148-01	.8750 04	.314 01	.8-17 01
.62	.674-01	.586-01	.8481 04	.245 01	.54	.522-01	.272-01	.9252 04	.286 01	.5402 01	.48	.316-01	.146-01	.8757 04	.320 01	.8-71 01
.60	.870-01	.506-01	.8640 04	.253 01	.52	.459-01	.230-01	.9397 04	.296 01	.6052 01	.46	.273-01	.121-01	.9894 04	.332 01	.865-01
.58	.875-01	.436-01	.8796 04	.262 01	.50	.401-01	.194-01	.9540 04	.307 01	.6615 01	.44	.235-01	.097-03	.1003 05	.344 01	.1107 01
.56	.887-01	.373-01	.8950 04	.271 01	.48	.349-01	.162-01	.9681 04	.317 01	.7718 01	.42	.201-01	.81-02	.1116 05	.356 01	.1270 01
.54	.897-01	.318-01	.9100 04	.281 01	.46	.302-01	.134-01	.9819 04	.329 01	.8792 01	.40	.170-01	.653-02	.1219 05	.364 01	.1487 01
.52	.934-01	.269-01	.9248 04	.291 01	.44	.222-01	.932-02	.1009 05	.341 01	.1008 02	.36	.150-01	.417-02	.1322 05	.384 01	.1744 01
.50	.467-01	.221-01	.9393 04	.301 01	.42	.189-01	.789-02	.1035 05	.367 01	.1163 02	.34	.993-02	.328-02	.1353 05	.398 01	.2052 01
.48	.477-01	.189-01	.9536 04	.312 01	.40	.159-01	.584-02	.1048 05	.381 01	.1353 02	.32	.814-02	.251-02	.1379 05	.415 01	.2467 01
.46	.352-01	.157-01	.9676 04	.323 01	.38	.133-01	.462-02	.1035 05	.386 01	.1586 02	.30	.660-02	.191-02	.1391 05	.431 01	.4624 01
.44	.303-01	.129-01	.9814 04	.335 01	.36	.110-01	.361-02	.1048 05	.412 01	.1874 02	.28	.528-02	.143-02	.1410 05	.471 01	.4477 01
.42	.259-01	.106-01	.9950 04	.348 01	.34	.902-02	.279-02	.1072 05	.429 01	.2237 02	.26	.417-02	.105-02	.1115 05	.493 01	.5610 01
.40	.220-01	.854-02	.1008 05	.361 01	.32	.732-02	.212-02	.1084 05	.447 01	.2689 02	.24	.375-02	.751-03	.1126 05	.518 01	.7147 01
.38	.186-01	.684-02	.1021 05	.375 01	.30	.586-02	.158-02	.1096 05	.468 01	.4562 02	.22	.248-02	.528-03	.1137 05	.545 01	.9256 01
.36	.155-01	.542-02	.1034 05	.390 01	.28	.463-02	.116-02	.1108 05	.490 01	.5088 02	.20	.186-02	.358-03	.1158 05	.611 01	.1225 03
.34	.129-01	.424-02	.1047 05	.406 01	.26	.360-02	.835-03	.1119 05	.514 01	.6473 02	.18	.136-02	.236-03	.1179 05	.700 01	.1634 03
.32	.106-01	.328-02	.1059 05	.423 01	.24	.275-02	.588-03	.1130 05	.541 01	.8386 02	.16	.925-03	.149-03	.1188 05	.789 01	.2314 03
.30	.857-02	.248-02	.1072 05	.441 01	.22	.206-02	.398-03	.1141 05	.572 01	.1109 03	.14	.662-03	.694-04	.1199 05	.904 01	.3344 03
.28	.87-02	.186-02	.1084 05	.461 01	.20	.151-02	.262-03	.1152 05	.607 01	.1502 03	.12	.434-03	.503-04	.1188 05	.959 01	.5059 03
.26	.843-02	.137-02	.1095 05	.483 01	.18	.107-02	.166-03	.1162 05	.647 01	.2094 03	.10	.267-03	.258-04	.1198 05	.835 01	.8153 03
.24	.823-02	.986-03	.1107 05	.507 01	.16	.736-03	.996-04	.1172 05	.696 01	.3023 03	.08	.203-03	.176-04	.1202 05	.881 01	.1069 04
.22	.824-02	.893-03	.1118 05	.534 01	.14	.683-03	.560-04	.1182 05	.755 01	.4571 03	.06	.150-03	.118-04	.1207 05	.947 01	.1445 04
.20	.843-02	.471-03	.1129 05	.565 01	.12	.498-03	.287-04	.1191 05	.830 01	.7361 03	.07	.106-03	.718-05	.1211 05	.109 02	.2027 04
.18	.878-02	.310-03	.1140 05	.599 01	.10	.226-03	.197-04	.1196 05	.876 01	.9652 03	.06	.431-04	.615-05	.1216 05	.190 02	.2993 04
.16	.127-02	.196-03	.1150 05	.639 01	.08	.167-03	.129-04	.1201 05	.931 01	.1303 04	.05	.256-04	.987-06	.1220 05	.120 02	.4742 04
.14	.875-03	.118-03	.1160 05	.687 01	.07	.118-03	.801-05	.1205 05	.998 01	.1828 04	.04	.256-04	.987-06	.1225 05	.134 02	.4930 04
.12	.871-03	.665-04	.1170 05	.745 01	.06	.800-04	.464-05	.1210 05	.108 02	.2698 04	.03	.123-04	.355-06	.1229 05	.155 02	.1724 05
.10	.855-03	.347-04	.1180 05	.820 01	.05	.503-04	.243-05	.1214 05	.119 02	.4272 04	.02	.440-05	.845-07	.1233 05	.191 02	.4811 05
.08	.268-03	.234-04	.1185 05	.866 01	.04	.286-04	.110-05	.1219 05	.155 02	.7499 04	.01	.756-06	.840-08	.1236 05	.260 02	.2760 06
.06	.198-03	.154-04	.1189 05	.920 01	.03	.138-04	.398-06	.1223 05	.190 02	.6322 05						
.04	.951-04	.553-05	.1198 05	.107 02	.02	.492-05	.958-07	.1227 05	.268 02	.2501 06						
.02	.899-04	.291-05	.1203 05	.118 02	.01	.847-06	.840-08	.1232 05								
.00	.341-04	.136-05	.1207 05	.132 02												
.02	.165-04	.479-06	.1212 05	.153 02												
.02	.590-05	.116-06	.1216 05	.187 02												
.01	.102-05	.112-07	.1221 05	.257 02												

Table 23b. EXPANSION AFTER FREEZING - HYPERBOLIC NOZZLE

$T_0 = 5000^\circ K$, $p_0 = 1000$ atm.

$l = 0.1$
 $l = 1.0$
 $l = 10$

T	P	P	M	A	T	P	P	M	A	T	P	P	M	A	T	P	M	A
			(ft/sec.)					(ft/sec.)					(ft/sec.)			(ft/sec.)		
63E	148 00	968-01	9085 04	219 01	2265 01	575	415-01	217-01	1293 05	6691 01	147-01	864-02	300 01	6691 01	495	147-01	864-02	300 01
66	138 00	884-01	9222 04	232 01	2390 01	56	381-01	194-01	1104 05	7220 01	137-01	763-02	314 01	7220 01	48	137-01	763-02	314 01
67	128 00	781-01	9451 04	241 01	2576 01	54	358-01	166-01	1119 05	8222 01	115-01	663-02	324 01	8222 01	46	115-01	663-02	324 01
68	118 00	687-01	9576 04	249 01	2785 01	52	299-01	141-01	1134 05	8954 01	89	595-02	334 01	8954 01	44	89	595-02	334 01
69	108 00	593-01	9749 04	257 01	3023 01	50	263-01	120-01	1148 05	9854 01	72	523-02	345 01	9854 01	42	72	523-02	345 01
70	98 00	526-01	9918 04	266 01	3293 01	48	230-01	101-01	1163 05	1095 02	56	459-02	357 01	1095 02	40	56	459-02	357 01
71	88 00	457-01	1009 05	275 01	3602 01	46	201-01	84-0-02	1177 05	1285 02	38	411-02	369 01	1285 02	38	38	411-02	369 01
72	78 00	396-01	1025 05	284 01	3957 01	44	174-01	69-0-02	1191 05	1456 02	36	381-01	381 01	1456 02	36	36	381-01	381 01
73	68 00	341-01	1041 05	294 01	4365 01	42	150-01	57-0-02	1204 05	1684 02	34	345-02	395 01	1684 02	34	34	345-02	395 01
74	58 00	291-01	1057 05	304 01	4837 01	40	128-01	46-0-02	1218 05	1948 02	32	325-02	409 01	1948 02	32	32	325-02	409 01
75	48 00	246-01	1072 05	315 01	5387 01	38	109-01	37-0-02	1231 05	2271 02	30	285-02	424 01	2271 02	30	30	285-02	424 01
76	38 00	203-01	1087 05	326 01	6030 01	36	914-02	29-0-02	1244 05	2670 02	28	250-02	440 01	2670 02	28	28	250-02	440 01
77	28 00	170-01	1103 05	337 01	6787 01	34	762-02	23-0-02	1257 05	3166 02	26	219-02	457 01	3166 02	26	26	219-02	457 01
78	18 00	147-01	1117 05	349 01	7686 01	32	629-02	18-0-02	1270 05	3798 02	24	190-02	475 01	3798 02	24	24	190-02	475 01
79	8 00	121-01	1132 05	362 01	8759 01	30	514-02	14-0-02	1282 05	4606 02	22	169-02	496 01	4606 02	22	22	169-02	496 01
80	0 00	994-02	1146 05	376 01	1005 02	28	415-02	10-0-02	1295 05	5517 01	20	149-02	517 01	5517 01	20	20	149-02	517 01
81	0 00	507-02	1161 05	390 01	1162 02	26	330-02	7-0-02	1307 05	6541 01	18	128-02	541 01	6541 01	18	18	128-02	541 01
82	0 00	548-02	1175 05	405 01	1355 02	24	258-02	5-0-02	1319 05	7681 01	16	110-02	568 01	7681 01	16	16	110-02	568 01
83	0 00	514-02	1188 05	422 01	1593 02	22	199-02	3-0-02	1331 05	8981 01	14	95-02	598 01	8981 01	14	14	95-02	598 01
84	0 00	503-02	1202 05	439 01	1893 02	20	150-02	2-0-02	1342 05	1038 03	12	81-02	631 01	1038 03	12	12	81-02	631 01
85	0 00	311-02	1215 05	459 01	2273 02	18	110-02	1-0-02	1353 05	1230 03	10	68-02	669 01	1230 03	10	10	68-02	669 01
86	0 00	236-02	1228 05	479 01	2764 02	16	786-03	114-03	1364 05	1430 03	8	54-02	713 01	1430 03	8	8	54-02	713 01
87	0 00	176-02	1241 05	502 01	3406 02	14	582-03	69-0-04	1375 05	1630 03	6	44-02	766 01	1630 03	6	6	44-02	766 01
88	0 00	129-02	1254 05	527 01	4263 02	12	388-03	3-0-04	1385 05	1830 03	4	36-02	820 01	1830 03	4	4	36-02	820 01
89	0 00	915-03	1266 05	555 01	5431 02	10	222-03	2-02-04	1395 05	1978 03	2	30-04	892 01	1978 03	2	2	30-04	892 01
90	0 00	535-03	1279 05	587 01	7061 02	8	170-03	139-04	1405 05	962 01	0	25-04	962 01	962 01	0	0	25-04	962 01
91	0 00	425-03	1290 05	623 01	9399 02	6	126-03	92-0-05	1405 05	102 02	0	21-05	102 02	102 02	0	0	21-05	102 02
92	0 00	275-03	1302 05	665 01	1287 03	4	908-04	578-05	1410 05	118 02	0	17-05	118 02	118 02	0	0	17-05	118 02
93	0 00	167-03	1313 05	714 01	1824 03	2	622-04	339-05	1415 05	146 02	0	13-05	146 02	146 02	0	0	13-05	146 02
94	0 00	962-04	1324 05	775 01	2700 03	0	388-04	181-05	1419 05	130 02	0	10-05	130 02	130 02	0	0	10-05	130 02
95	0 00	506-04	1335 05	852 01	4239 03	0	231-04	839-06	1424 05	146 02	0	8-05	146 02	146 02	0	0	8-05	146 02
96	0 00	351-04	1340 05	899 01	5473 03	0	115-04	313-06	1429 05	169 02	0	7-05	169 02	169 02	0	0	7-05	169 02
97	0 00	235-04	1345 05	955 01	7259 03	0	428-05	781-07	1433 05	207 02	0	6-05	207 02	207 02	0	0	6-05	207 02
98	0 00	149-04	1350 05	102 02	9966 03	0	790-06	750-08	1438 05	291 02	0	5-05	291 02	291 02	0	0	5-05	291 02
99	0 00	685-05	1355 05	111 02	1434 04	0			1443 05		0				0			
100	0 00	475-05	1360 05	122 02	2201 04	0			1448 05		0				0			
101	0 00	236-05	1365 05	137 02	3718 04	0			1453 05		0				0			
102	0 00	657-05	1370 05	158 02	5315 04	0			1458 05		0				0			
103	0 00	457-05	1375 05	170 02	7191 05	0			1463 05		0				0			
104	0 00	219-05	1380 05	195 02	1901 05	0			1468 05		0				0			
105	0 00	201-07	1380 05	281 02	9753 05	0			1473 05		0				0			

Table 24a. EXPANSION AFTER FREEZING - WEDGE NOZZLE
 $T_0' = 6000^\circ\text{K}$, $P_0' = 100 \text{ atm}$.

$l = 0.1$												$l = 1.0$												$l = 10$											
T	P	P	M	A	T	o	P	u'	M	A	T	P	u'	M	A	T	P	u'	M	A	T	P	u'	M	A										
			(ft./sec.)					(ft./sec.)					(ft./sec.)					(ft./sec.)					(ft./sec.)												
.73	.198 00	.138 00	.8502 04	.1803 01	.63	.780 00	.455-01	.1010 05	.261 01	.3851 01	.55	.300-01	.1130 05	.319 01	.8957 01																				
.74	.190 00	.130 00	.8600 04	.1861 01	.62	.741-01	.471-01	.1019 05	.272 01	.4021 01	.54	.282-01	.1137 05	.331 01	.9455 01																				
.75	.174 00	.116 00	.8702 04	.1987 01	.60	.687-01	.471-01	.1035 05	.281 01	.4398 01	.52	.249-01	.1151 05	.341 01	.1087 02																				
.76	.159 00	.103 00	.8800 04	.2129 01	.58	.598-01	.471-01	.1051 05	.290 01	.4828 01	.50	.219-01	.1165 05	.352 01	.1188 02																				
.77	.145 00	.910-01	.9164 04	.2290 01	.56	.535-01	.471-01	.1066 05	.300 01	.5322 01	.48	.192-01	.1179 05	.364 01	.1342 02																				
.78	.131 00	.802-01	.9344 04	.241 01	.54	.476-01	.471-01	.1082 05	.309 01	.5893 01	.46	.167-01	.1193 05	.376 01	.1525 02																				
.79	.119 00	.704-01	.9521 04	.250 01	.52	.422-01	.471-01	.1112 05	.320 01	.6525 01	.44	.144-01	.1207 05	.389 01	.1743 02																				
.80	.108 00	.615-01	.9695 04	.258 01	.50	.373-01	.471-01	.1127 05	.330 01	.7328 01	.42	.124-01	.1220 05	.402 01	.2004 02																				
.81	.969-01	.535-01	.9865 04	.267 01	.48	.327-01	.471-01	.1141 05	.342 01	.8234 01	.40	.896-02	.1234 05	.416 01	.2334 02																				
.82	.869-01	.464-01	.1020 05	.277 01	.44	.280-01	.471-01	.1156 05	.356 01	.1058 02	.36	.753-02	.1247 05	.432 01	.2716 02																				
.83	.776-01	.400-01	.1036 05	.286 01	.42	.234-01	.471-01	.1170 05	.373 01	.1210 02	.34	.627-02	.1260 05	.448 01	.3234 02																				
.84	.691-01	.343-01	.1052 05	.296 01	.40	.184-01	.471-01	.1184 05	.393 01	.1395 02	.32	.517-02	.1272 05	.465 01	.3806 02																				
.85	.612-01	.292-01	.1067 05	.307 01	.48	.137-01	.471-01	.1211 05	.423 01	.1619 02	.30	.421-02	.1297 05	.504 01	.4472 02																				
.86	.540-01	.247-01	.1083 05	.318 01	.46	.88-01	.471-01	.1224 05	.440 01	.1896 02	.28	.339-02	.1310 05	.526 01	.5240 02																				
.87	.474-01	.208-01	.1098 05	.329 01	.44	.111-01	.471-01	.1237 05	.458 01	.2240 02	.26	.269-02	.1322 05	.551 01	.6084 03																				
.88	.414-01	.173-01	.1098 05	.341 01	.42	.818-02	.471-01	.1250 05	.477 01	.2673 02	.24	.210-02	.1333 05	.578 01	.7084 03																				
.89	.359-01	.144-01	.1113 05	.354 01	.40	.760-02	.471-01	.1263 05	.499 01	.3226 02	.22	.161-02	.1345 05	.608 01	.8306 03																				
.90	.309-01	.118-01	.1127 05	.367 01	.38	.713-02	.471-01	.1275 05	.522 01	.3942 02	.20	.121-02	.1356 05	.641 01	.9813 03																				
.91	.265-01	.959-02	.1142 05	.381 01	.36	.610-02	.471-01	.1288 05	.548 01	.4884 02	.18	.887-03	.1368 05	.680 01	.1169 04																				
.92	.225-01	.771-02	.1156 05	.397 01	.34	.487-02	.471-01	.1300 05	.577 01	.6148 02	.16	.632-03	.1378 05	.725 01	.1344 04																				
.93	.189-01	.613-02	.1170 05	.413 01	.32	.383-02	.471-01	.1312 05	.609 01	.7837 02	.14	.434-03	.1389 05	.778 01	.1580 04																				
.94	.158-01	.481-02	.1184 05	.430 01	.30	.295-02	.471-01	.1323 05	.647 01	.1030 03	.12	.286-03	.1399 05	.844 01	.1884 04																				
.95	.130-01	.372-02	.1197 05	.449 01	.28	.225-02	.471-01	.1334 05	.690 01	.1381 03	.10	.177-03	.1409 05	.926 01	.2219 04																				
.96	.106-01	.284-02	.1211 05	.470 01	.26	.166-02	.471-01	.1345 05	.741 01	.1904 03	.09	.135-03	.1414 05	.977 01	.2636 04																				
.97	.845-02	.212-02	.1224 05	.492 01	.24	.119-02	.471-01	.1356 05	.799 01	.2718 03	.08	.100-03	.1419 05	.104 07	.3139 04																				
.98	.678-02	.155-02	.1237 05	.517 01	.22	.830-03	.471-01	.1366 05	.803 01	.4056 03	.07	.716-04	.1424 05	.111 07	.3707 04																				
.99	.528-02	.111-02	.1249 05	.544 01	.20	.552-03	.471-01	.1376 05	.853 01	.6056 03	.06	.489-04	.1428 05	.120 02	.4384 04																				
.00	.404-02	.770-03	.1262 05	.576 01	.18	.446-03	.471-01	.1386 05	.893 01	.8336 03	.05	.312-04	.1433 05	.132 02	.5246 04																				
.01	.301-02	.334-03	.1274 05	.611 01	.16	.296-03	.471-01	.1396 05	.931 01	.1111 04	.04	.180-04	.1437 05	.148 07	.6396 04																				
.02	.219-02	.205-03	.1286 05	.652 01	.14	.198-03	.471-01	.1406 05	.989 01	.1111 04	.03	.891-05	.1442 05	.171 05	.8171 05																				
.03	.154-02	.148-03	.1297 05	.701 01	.12	.143-03	.471-01	.1415 05	.115 02	.2220 04	.02	.605-07	.1447 05	.210 02	.1063 05																				
.04	.103-02	.118-03	.1308 05	.761 01	.10	.886-04	.471-01	.1424 05	.126 02	.3431 04	.01	.400-08	.1451 05	.305 02	.1451 05																				
.05	.650-03	.625-04	.1319 05	.837 01	.08	.636-04	.471-01	.1433 05	.141 02	.5843 04																									
.06	.507-03	.435-04	.1324 05	.883 01	.06	.472-04	.471-01	.1441 05	.164 02	.1161 05																									
.07	.382-03	.291-04	.1330 05	.938 01	.04	.372-04	.471-01	.1449 05	.201 02	.3062 05																									
.08	.278-03	.185-04	.1335 05	.101 02	.03	.287-04	.471-01	.1457 05	.242 02	.1610 06																									
.09	.193-03	.110-04	.1342 05	.129 02	.02	.205-05	.471-01	.1465 05	.284 02																										
.10	.126-03	.599-05	.1345 05	.109 02	.01	.134-05	.471-01	.1473 05																											
.11	.745-04	.108-05	.1350 05	.134 02	.00			.1481 05																											
.12	.679-04	.108-05	.1355 05	.156 02	.00			.1489 05																											
.13	.612-04	.280-06	.1360 05	.191 02	.00			.1497 05																											
.14	.548-05	.277-07	.1365 05	.271 02	.00			.1505 05																											

Table 24b. EXPANSION AFTER FREEZING - HYPERBOLIC NOZZLE

$T_0 = 6000^\circ\text{K}$, $P_0 = 100$ atm.

$l = 0.1$													$l = 1.0$													$l = 10$												
T	P	P	u'	M	A	T	P	P	u'	M	A	T	P	P	u'	M	A	T	P	P	u'	M	A															
			(ft./sec.)						(ft./sec.)						(ft./sec.)						(ft./sec.)																	
.50	.650-01	.367-01	.1020 05	.273 01	.4501 01	.514	.230-01	.107-01	.1141 05	.336 01	.1138 02	.44	.950-02	.390-02	.1217 05	.386 01	.1138 02	.44	.950-02	.390-02	.1217 05	.386 01	.1138 02															
.51	.219-01	.245-01	.1027 05	.280 01	.4694 01	.50	.209-01	.950-02	.1151 05	.348 01	.1238 02	.42	.845-02	.318-02	.1230 05	.408 01	.1238 02	.42	.845-02	.318-02	.1230 05	.408 01	.1238 02															
.52	.353-01	.297-01	.1043 05	.289 01	.5176 01	.48	.182-01	.784-02	.1155 05	.360 01	.1494 02	.40	.716-02	.257-02	.1243 05	.423 01	.1494 02	.40	.716-02	.257-02	.1243 05	.423 01	.1494 02															
.53	.492-01	.255-01	.1059 05	.299 01	.5729 01	.46	.158-01	.659-02	.1179 05	.372 01	.1602 02	.38	.602-02	.205-02	.1256 05	.438 01	.1602 02	.38	.602-02	.205-02	.1256 05	.438 01	.1602 02															
.54	.365-01	.218-01	.1075 05	.309 01	.6373 01	.44	.136-01	.543-02	.1193 05	.384 01	.1839 02	.36	.502-02	.162-02	.1269 05	.454 01	.1839 02	.36	.502-02	.162-02	.1269 05	.454 01	.1839 02															
.55	.385-01	.186-01	.1090 05	.319 01	.7117 01	.42	.116-01	.443-02	.1206 05	.398 01	.2126 02	.34	.415-02	.128-02	.1281 05	.472 01	.2126 02	.34	.415-02	.128-02	.1281 05	.472 01	.2126 02															
.56	.398-01	.159-01	.1105 05	.330 01	.7992 01	.40	.989-02	.359-02	.1220 05	.412 01	.2475 02	.32	.339-02	.972-03	.1294 05	.441 01	.2475 02	.32	.339-02	.972-03	.1294 05	.441 01	.2475 02															
.57	.296-01	.132-01	.1120 05	.341 01	.9022 01	.38	.833-02	.287-02	.1233 05	.427 01	.2906 02	.30	.274-02	.736-03	.1306 05	.511 01	.2906 02	.30	.274-02	.736-03	.1306 05	.511 01	.2906 02															
.58	.422-01	.908-02	.1148 05	.355 01	.1171 02	.34	.696-02	.227-02	.1246 05	.443 01	.3441 02	.28	.218-02	.546-03	.1318 05	.534 01	.3441 02	.28	.218-02	.546-03	.1318 05	.534 01	.3441 02															
.59	.222-01	.742-02	.1163 05	.378 01	.1347 02	.32	.577-02	.178-02	.1259 05	.460 01	.4114 02	.26	.172-02	.285-03	.1342 05	.586 01	.4114 02	.26	.172-02	.285-03	.1342 05	.586 01	.4114 02															
.60	.191-01	.603-02	.1177 05	.392 01	.1540 02	.30	.472-02	.137-02	.1271 05	.479 01	.4971 02	.24	.151-02	.400-03	.1430 05	.658 01	.479 01	.24	.151-02	.400-03	.1430 05	.658 01	.479 01															
.61	.163-01	.483-02	.1190 05	.406 01	.1822 02	.28	.383-02	.104-02	.1284 05	.499 01	.6077 02	.22	.101-02	.198-03	.1533 05	.816 01	.6077 02	.22	.101-02	.198-03	.1533 05	.816 01	.6077 02															
.62	.342-01	.485-02	.1190 05	.406 01	.1822 02	.28	.306-02	.777-03	.1286 05	.521 01	.7528 02	.20	.746-03	.134-03	.1544 05	.850 01	.7528 02	.20	.746-03	.134-03	.1544 05	.850 01	.7528 02															
.63	.16-01	.386-02	.1204 05	.422 01	.2147 02	.26	.241-02	.568-03	.1308 05	.545 01	.9463 02	.18	.540-03	.872-04	.1575 05	.989 01	.9463 02	.18	.540-03	.872-04	.1575 05	.989 01	.9463 02															
.64	.961-02	.303-02	.1217 05	.439 01	.2593 02	.24	.187-02	.407-03	.1320 05	.572 01	.1209 03	.16	.379-03	.544-04	.1596 05	.105 02	.1209 03	.16	.379-03	.544-04	.1596 05	.105 02	.1209 03															
.65	.791-02	.235-02	.1230 05	.457 01	.3088 02	.22	.142-02	.284-03	.1332 05	.602 01	.1575 03	.14	.257-03	.322-04	.1606 05	.888 01	.1575 03	.14	.257-03	.322-04	.1606 05	.888 01	.1575 03															
.66	.644-02	.179-02	.1243 05	.477 01	.3729 02	.20	.106-02	.192-03	.1344 05	.635 01	.2096 03	.12	.166-03	.179-04	.1626 05	.1278 04	.2096 03	.12	.166-03	.179-04	.1626 05	.1278 04	.2096 03															
.67	.518-02	.134-02	.1256 05	.498 01	.4591 02	.18	.770-03	.126-03	.1354 05	.674 01	.2862 03	.10	.101-03	.905-05	.1646 05	.1288 04	.2862 03	.10	.101-03	.905-05	.1646 05	.1288 04	.2862 03															
.68	.18-02	.989-03	.1268 05	.521 01	.5754 02	.16	.543-03	.788-04	.1366 05	.718 01	.4025 03	.09	.763-04	.402-05	.1626 05	.105 02	.4025 03	.09	.763-04	.402-05	.1626 05	.105 02	.4025 03															
.69	.320-02	.713-03	.1281 05	.547 01	.7279 02	.14	.370-03	.469-04	.1376 05	.771 01	.5870 03	.08	.560-04	.249-05	.1630 05	.112 02	.5870 03	.08	.560-04	.249-05	.1630 05	.112 02	.5870 03															
.70	.245-02	.590-03	.1293 05	.576 01	.9413 02	.12	.240-03	.261-04	.1386 05	.836 01	.8936 03	.07	.397-04	.249-05	.1630 05	.112 02	.8936 03	.07	.397-04	.249-05	.1630 05	.112 02	.8936 03															
.71	.184-02	.341-03	.1305 05	.609 01	.1243 03	.10	.147-03	.133-04	.1396 05	.918 01	.1457 04	.06	.267-04	.144-05	.1630 05	.112 02	.1457 04	.06	.267-04	.144-05	.1630 05	.112 02	.1457 04															
.72	.135-02	.225-03	.1316 05	.646 01	.1684 03	.09	.111-03	.908-05	.1401 05	.968 01	.1916 04	.05	.168-04	.753-06	.1639 05	.133 02	.1916 04	.05	.168-04	.753-06	.1639 05	.133 02	.1916 04															
.73	.956-03	.142-03	.1327 05	.689 01	.2348 03	.08	.819-04	.594-05	.1406 05	.103 02	.2592 04	.04	.956-05	.344-06	.1644 05	.150 02	.2592 04	.04	.956-05	.344-06	.1644 05	.150 02	.2592 04															
.74	.557-03	.653-04	.1338 05	.740 01	.3393 03	.07	.582-04	.370-05	.1410 05	.110 02	.3635 04	.03	.462-05	.125-06	.1649 05	.173 02	.3635 04	.03	.462-05	.125-06	.1649 05	.173 02	.3635 04															
.75	.21-03	.485-04	.1349 05	.802 01	.5132 03	.06	.394-04	.214-05	.1415 05	.119 02	.5354 04	.02	.166-05	.286-07	.1653 05	.214 02	.5354 04	.02	.166-05	.286-07	.1653 05	.214 02	.5354 04															
.76	.266-03	.247-04	.1359 05	.881 01	.8249 03	.05	.249-04	.113-05	.1420 05	.131 02	.8445 04	.01	.287-06	.260-08	.1457 05	.303 02	.8445 04	.01	.287-06	.260-08	.1457 05	.303 02	.8445 04															
.77	.203-03	.165-04	.1364 05	.929 01	.1079 04	.04	.142-04	.516-06	.1424 05	.147 02	.1473 05						.1473 05																					
.78	.150-03	.114-04	.1369 05	.987 01	.1450 04	.03	.692-05	.188-06	.1429 05	.170 02	.3020 05						.3020 05																					
.79	.106-03	.669-05	.1374 05	.106 02	.2020 04	.02	.251-05	.442-07	.1434 05	.210 02	.8314 05						.8314 05																					
.80	.733-04	.409-05	.1379 05	.114 02	.2953 04	.01	.441-06	.520-08	.1438 05	.277 02	.4710 06						.4710 06																					
.81	.467-04	.217-05	.1384 05	.126 02	.4618 04																																	
.82	.270-04	.100-05	.1389 05	.141 02	.7974 04																																	
.83	.133-04	.376-06	.1393 05	.163 02	.1613 05																																	
.84	.490-05	.912-07	.1398 05	.200 02	.4342 05																																	
.85	.888-06	.786-08	.1403 05	.289 02	.2396 06																																	

Table 25a. EXPANSION AFTER FREEZING - WEDGE NOZZLE

 $T_0' = 6000^\circ\text{K}$, $P_0' = 300 \text{ atm}$.

$l = 0.1$

$l = 1.0$

$l = 10$

T	$l = 0.1$					$l = 1.0$					$l = 10$				
	T	P	u' (ft./sec.)	M	A	T	P	u' (ft./sec.)	M	A	T	P	u' (ft./sec.)	M	A
.663	.110 00	.684-01	.9440 04	.239 01	.2875 01	.575	.450-00	.1066 05	.295 01	.6221 01	.552	.200-01	.908-02	.1154 05	.1293 02
.664	.109 00	.675-01	.9462 04	.244 01	.2904 01	.556	.412-04	.1078 05	.306 01	.6724 01	.530	.197-01	.892-02	.1156 05	.1300 02
.665	.108 00	.666-01	.9484 04	.249 01	.2933 01	.541	.365-01	.1093 05	.316 01	.7490 01	.468	.172-01	.746-02	.1170 05	.1485 02
.666	.107 00	.657-01	.9506 04	.254 01	.3155 01	.526	.365-01	.1093 05	.316 01	.7490 01	.466	.149-01	.618-02	.1184 05	.1695 02
.667	.106 00	.648-01	.9528 04	.259 01	.3377 01	.511	.321-01	.1108 05	.326 01	.8382 01	.444	.128-01	.510-02	.1197 05	.1947 02
.668	.105 00	.639-01	.9550 04	.264 01	.3600 01	.496	.286-01	.1123 05	.337 01	.9429 01	.422	.109-01	.418-02	.1211 05	.2252 02
.669	.104 00	.630-01	.9572 04	.269 01	.3822 01	.481	.246-01	.1137 05	.348 01	.1066 02	.400	.929-02	.336-02	.1224 05	.2623 02
.670	.103 00	.621-01	.9594 04	.274 01	.4044 01	.466	.214-01	.1152 05	.360 01	.1213 02	.388	.785-02	.269-02	.1238 05	.3091 02
.671	.102 00	.612-01	.9616 04	.279 01	.4266 01	.451	.184-01	.1166 05	.372 01	.1389 02	.366	.654-02	.213-02	.1250 05	.3690 02
.672	.101 00	.603-01	.9638 04	.284 01	.4488 01	.436	.158-01	.1180 05	.386 01	.1671 02	.344	.561-02	.166-02	.1263 05	.4367 02
.673	.100 00	.594-01	.9660 04	.289 01	.4710 01	.421	.135-01	.1193 05	.400 01	.1859 02	.322	.443-02	.128-02	.1276 05	.5290 02
.674	.099 00	.585-01	.9682 04	.294 01	.4932 01	.406	.114-01	.1207 05	.414 01	.2175 02	.300	.359-02	.973-03	.1288 05	.6450 02
.675	.098 00	.576-01	.9704 04	.299 01	.5154 01	.391	.953-02	.1220 05	.430 01	.2567 02	.288	.287-02	.728-03	.1301 05	.8004 02
.676	.097 00	.567-01	.9726 04	.304 01	.5376 01	.376	.791-02	.1233 05	.447 01	.3060 02	.266	.226-02	.531-03	.1313 05	.1007 03
.677	.096 00	.558-01	.9748 04	.309 01	.5598 01	.361	.650-02	.1246 05	.466 01	.3585 02	.244	.175-02	.380-03	.1324 05	.1288 03
.678	.095 00	.549-01	.9770 04	.314 01	.5820 01	.346	.528-02	.1259 05	.485 01	.4489 02	.222	.133-02	.268-03	.1336 05	.1679 03
.679	.094 00	.540-01	.9792 04	.319 01	.6042 01	.331	.424-02	.1272 05	.507 01	.5541 02	.200	.990-03	.179-03	.1347 05	.2237 03
.680	.093 00	.531-01	.9814 04	.324 01	.6264 01	.316	.335-02	.1284 05	.531 01	.6938 02	.188	.719-03	.117-03	.1359 05	.3056 03
.681	.092 00	.522-01	.9836 04	.329 01	.6486 01	.301	.261-02	.1298 05	.557 01	.8532 02	.166	.507-03	.733-04	.1369 05	.4303 03
.682	.091 00	.513-01	.9858 04	.334 01	.6708 01	.286	.199-02	.1308 05	.586 01	.1145 03	.144	.344-03	.436-04	.1380 05	.6273 04
.683	.090 00	.504-01	.9880 04	.339 01	.6930 01	.271	.149-02	.1320 05	.619 01	.1518 03	.122	.223-03	.243-04	.1390 05	.8697 04
.684	.089 00	.495-01	.9902 04	.344 01	.7152 01	.256	.109-02	.1331 05	.657 01	.2061 03	.100	.136-03	.123-04	.1400 05	.1563 04
.685	.088 00	.486-01	.9924 04	.349 01	.7374 01	.241	.771-03	.1342 05	.700 01	.2985 03	.088	.103-03	.841-05	.1405 05	.2657 04
.686	.087 00	.477-01	.9946 04	.354 01	.7596 01	.226	.527-03	.1353 05	.752 01	.4385 03	.088	.760-04	.550-05	.1410 05	.4784 04
.687	.086 00	.468-01	.9968 04	.359 01	.7818 01	.211	.345-03	.1363 05	.815 01	.6354 03	.077	.540-04	.342-05	.1414 05	.7908 04
.688	.085 00	.459-01	.9990 04	.364 01	.8040 01	.196	.212-03	.1374 05	.896 01	.926 04	.066	.365-04	.198-05	.1419 05	.1210 05
.689	.084 00	.450-01	.1000 04	.369 01	.8262 01	.181	.161-03	.1384 05	.944 01	.1344 04	.055	.230-04	.104-05	.1424 05	.2097 04
.690	.083 00	.441-01	.1000 04	.374 01	.8484 01	.166	.119-03	.1393 05	.100 02	.1812 04	.044	.132-04	.677-06	.1428 05	.3848 05
.691	.082 00	.432-01	.1000 04	.379 01	.8706 01	.151	.850-04	.1398 05	.107 02	.2331 04	.033	.639-05	.175-06	.1433 05	.6261 05
.692	.081 00	.423-01	.1000 04	.384 01	.8928 01	.136	.577-04	.1388 05	.116 02	.3711 04	.022	.221-05	.416-07	.1437 05	.1092 05
.693	.080 00	.414-01	.1000 04	.389 01	.9150 01	.121	.367-04	.1398 05	.128 02	.5825 04	.011	.405-06	.260-08	.1442 05	.3330 02
.694	.079 00	.405-01	.1000 04	.394 01	.9372 01	.106	.211-04	.1402 05	.143 02	.1010 05					
.695	.078 00	.396-01	.1000 04	.399 01	.9594 01	.091	.103-04	.1406 05	.166 02	.2054 05					
.696	.077 00	.387-01	.1000 04	.404 01	.9816 01	.076	.103-04	.1410 05	.204 02	.5597 05					
.697	.076 00	.378-01	.1000 04	.409 01	.1000 04	.061	.677-06	.1414 05	.304 02	.3114 06					
.698	.075 00	.369-01	.1000 04	.414 01	.1000 04										
.699	.074 00	.360-01	.1000 04	.419 01	.1000 04										
.700	.073 00	.351-01	.1000 04	.424 01	.1000 04										
.701	.072 00	.342-01	.1000 04	.429 01	.1000 04										
.702	.071 00	.333-01	.1000 04	.434 01	.1000 04										
.703	.070 00	.324-01	.1000 04	.439 01	.1000 04										
.704	.069 00	.315-01	.1000 04	.444 01	.1000 04										
.705	.068 00	.306-01	.1000 04	.449 01	.1000 04										
.706	.067 00	.297-01	.1000 04	.454 01	.1000 04										
.707	.066 00	.288-01	.1000 04	.459 01	.1000 04										
.708	.065 00	.279-01	.1000 04	.464 01	.1000 04										
.709	.064 00	.270-01	.1000 04	.469 01	.1000 04										
.710	.063 00	.261-01	.1000 04	.474 01	.1000 04										
.711	.062 00	.252-01	.1000 04	.479 01	.1000 04										
.712	.061 00	.243-01	.1000 04	.484 01	.1000 04										
.713	.060 00	.234-01	.1000 04	.489 01	.1000 04										
.714	.059 00	.225-01	.1000 04	.494 01	.1000 04										
.715	.058 00	.216-01	.1000 04	.499 01	.1000 04										
.716	.057 00	.207-01	.1000 04	.504 01	.1000 04										
.717	.056 00	.198-01	.1000 04	.509 01	.1000 04										
.718	.055 00	.189-01	.1000 04	.514 01	.1000 04										
.719	.054 00	.180-01	.1000 04	.519 01	.1000 04										
.720	.053 00	.171-01	.1000 04	.524 01	.1000 04										
.721	.052 00	.162-01	.1000 04	.529 01	.1000 04										
.722	.051 00	.153-01	.1000 04	.534 01	.1000 04										
.723	.050 00	.144-01	.1000 04	.539 01	.1000 04										
.724	.049 00	.135-01	.1000 04	.544 01	.1000 04										
.725	.048 00	.126-01	.1000 04	.549 01	.1000 04										
.726	.047 00	.117-01	.1000 04	.554 01	.1000 04										
.727	.046 00	.108-01	.1000 04	.559 01	.1000 04										
.728	.045 00	.099-01	.1000 04	.564 01	.1000 04										
.729	.044 00	.090-01	.1000 04	.569 01	.1000 04										
.730	.043 00	.081-01	.1000 04	.574 01	.1000 04										
.731	.042 00	.072-01	.1000 04	.579 01	.1000 04										
.732	.041 00	.063-01	.1000 04	.584 01	.1000 04										
.733	.040 00	.054-01	.1000 04	.589 01	.1000 04										
.734	.039 00	.045-01	.1000 04	.594 01	.1000 04										
.735	.038 00	.036-01	.1000 04	.599 01	.1000 04										
.736	.037 00	.027-01	.1000 04	.604 01	.1000 04										
.737	.036 00	.018-01	.1000 04	.609 01	.1000 04										
.738	.035 00	.009-01	.1000 04	.614 01	.1000 04										
.739	.034 00	.000-01	.1000 04	.619 01	.1000 04										
.740	.033 00	.000-01	.1000 04	.624 01	.1000 04										
.741	.032 00	.000-01	.1000 04	.629 01	.1000 04										
.742	.031 00	.000-01	.1000 04	.634 01	.1000 04										
.743	.030 00	.000-01	.1000 04	.639 01	.1000 04										
.744	.029 00	.000-01	.1000 04	.644 01	.1000 04										
.745	.028 00	.000-01	.1000 04	.649 01	.1000 04										
.746	.027 00	.000-01	.1000 04	.654 01	.1000 04										
.747	.026 00	.000-01	.1000 04	.659 01	.1000 04										
.748	.025 00	.000-01	.1000 04	.664 01	.1000 04										
.749	.024 00	.000-01	.1000 04	.669 01	.1000 04										
.750	.023 00	.000-01	.1000 04	.674 01	.1000 04										
.751	.022 00	.000-01	.1000 04	.679 01	.1000 04										

$l = 0.1$														$l = 1.0$														$l = 10$													
T	P	P	u'	M	A	T	p	P	u'	M	A	T	p	P	u'	M	A	T	p	P	u'	M	A																		
			(ft/sec.)						(ft/sec.)						(ft/sec.)						(ft/sec.)																				
.523	.375-01	.184-01	.1073	.309	.7388	.451	.165-01	.690-02	.1152	.359	.1542	.394	.920-02	.335-02	.1190	.480	.1542	.394	.920-02	.335-02	.1190	.480	.1542	.394																	
.52	.348-01	.185-01	.1082	.317	.7066	.444	.152-01	.618-02	.1160	.370	.1667	.38	.814-02	.286-02	.1208	.495	.1667	.38	.814-02	.286-02	.1208	.495	.1667	.38																	
.51	.297-01	.139-01	.1037	.328	.8983	.42	.129-01	.504-02	.1174	.383	.1930	.36	.678-02	.226-02	.1222	.510	.1930	.36	.678-02	.226-02	.1222	.510	.1930	.36																	
.48	.250-01	.116-01	.1112	.339	.1019	.40	.110-01	.406-02	.1188	.397	.2252	.34	.559-02	.176-02	.1235	.525	.2252	.34	.559-02	.176-02	.1235	.525	.2252	.34																	
.46	.224-01	.961-02	.1127	.350	.1162	.38	.921-02	.325-02	.1201	.412	.2649	.32	.456-02	.135-02	.1248	.540	.2649	.32	.456-02	.135-02	.1248	.540	.2649	.32																	
.44	.194-01	.791-02	.1141	.363	.1334	.36	.768-02	.256-02	.1214	.428	.3144	.30	.366-02	.107-02	.1260	.558	.3144	.30	.366-02	.107-02	.1260	.558	.3144	.30																	
.42	.164-01	.645-02	.1155	.376	.1543	.32	.634-02	.200-02	.1228	.445	.3769	.28	.293-02	.759-03	.1273	.580	.3769	.28	.293-02	.759-03	.1273	.580	.3769	.28																	
.40	.144-01	.521-02	.1169	.390	.1797	.28	.518-02	.154-02	.1241	.463	.4566	.26	.230-02	.553-03	.1285	.602	.4566	.26	.230-02	.553-03	.1285	.602	.4566	.26																	
.38	.127-01	.416-02	.1183	.404	.2110	.22	.418-02	.116-02	.1253	.483	.5598	.22	.178-02	.394-03	.1297	.630	.5598	.22	.178-02	.394-03	.1297	.630	.5598	.22																	
.36	.980-02	.329-02	.1197	.420	.2501	.22	.333-02	.864-03	.1266	.504	.6957	.20	.135-02	.274-03	.1300	.660	.6957	.20	.135-02	.274-03	.1300	.660	.6957	.20																	
.34	.810-02	.257-02	.1210	.437	.2992	.22	.261-02	.630-03	.1278	.528	.8774	.18	.105-02	.184-03	.1321	.688	.8774	.18	.105-02	.184-03	.1321	.688	.8774	.18																	
.32	.662-02	.198-02	.1223	.455	.3618	.24	.202-02	.449-03	.1290	.554	.1125	.18	.720-03	.120-03	.1332	.710	.1125	.18	.720-03	.120-03	.1332	.710	.1125	.18																	
.30	.536-02	.150-02	.1236	.474	.4428	.22	.153-02	.312-03	.1302	.583	.1471	.16	.505-03	.747-04	.1343	.750	.1471	.16	.505-03	.747-04	.1343	.750	.1471	.16																	
.28	.428-02	.112-02	.1249	.496	.5491	.20	.113-02	.210-03	.1314	.616	.1966	.14	.341-03	.442-04	.1354	.780	.1966	.14	.341-03	.442-04	.1354	.780	.1966	.14																	
.26	.334-02	.816-03	.1261	.519	.6911	.18	.820-03	.137-03	.1325	.653	.2856	.12	.220-03	.244-04	.1364	.810	.2856	.12	.220-03	.244-04	.1364	.810	.2856	.12																	
.24	.260-02	.593-03	.1274	.545	.8945	.16	.576-03	.854-04	.1336	.697	.3811	.10	.159-03	.123-04	.1374	.840	.3811	.10	.159-03	.123-04	.1374	.840	.3811	.10																	
.22	.195-02	.406-03	.1286	.573	.1154	.14	.389-03	.505-04	.1347	.748	.5568	.08	.101-03	.838-05	.1384	.880	.5568	.08	.101-03	.838-05	.1384	.880	.5568	.08																	
.20	.147-02	.274-03	.1298	.606	.1538	.12	.252-03	.280-04	.1358	.811	.8585	.06	.735-04	.546-05	.1430	.920	.8585	.06	.735-04	.546-05	.1430	.920	.8585	.06																	
.18	.105-02	.179-03	.1309	.643	.2104	.10	.153-03	.142-04	.1368	.891	.1404	.04	.522-04	.338-05	.1483	.960	.1404	.04	.522-04	.338-05	.1483	.960	.1404	.04																	
.16	.749-03	.112-03	.1320	.686	.2965	.08	.115-03	.961-05	.1373	.939	.1853	.02	.351-04	.195-05	.1533	.100	.1853	.02	.351-04	.195-05	.1533	.100	.1853	.02																	
.14	.503-03	.664-04	.1331	.735	.4336	.08	.846-04	.627-05	.1378	.998	.2516	.04	.221-04	.102-05	.1583	.108	.2516	.04	.221-04	.102-05	.1583	.108	.2516	.04																	
.12	.329-03	.268-04	.1342	.798	.6640	.07	.599-04	.386-05	.1382	.107	.3543	.04	.153-04	.462-06	.1603	.120	.3543	.04	.153-04	.462-06	.1603	.120	.3543	.04																	
.10	.200-03	.167-04	.1352	.877	.1082	.06	.403-04	.224-05	.1387	.116	.5243	.04	.603-05	.167-06	.1607	.130	.5243	.04	.603-05	.167-06	.1607	.130	.5243	.04																	
.08	.152-03	.127-04	.1357	.925	.1426	.04	.253-04	.116-05	.1392	.127	.8313	.04	.215-05	.405-07	.1612	.140	.8313	.04	.215-05	.405-07	.1612	.140	.8313	.04																	
.06	.111-03	.923-05	.1362	.983	.1932	.04	.164-04	.532-06	.1397	.142	.1459	.05	.370-06	.270-08	.1617	.150	.1459	.05	.370-06	.270-08	.1617	.150	.1459	.05																	
.04	.750-04	.515-05	.1367	.105	.2715	.04	.094-05	.192-06	.1401	.165	.3015	.05					.3015	.05																							
.02	.533-04	.299-05	.1372	.114	.4008	.04	.246-05	.459-07	.1406	.203	.8397	.05					.8397	.05																							
.00	.191-04	.713-06	.1381	.125	.6339	.04	.001	.429-06	.1410	.224	.4847	.06					.4847	.06																							
.00	.927-05	.259-06	.1386	.163	.2283	.05																																			
.00	.323-05	.621-07	.1391	.200	.5324	.05																																			
.00	.581-05	.540-08	.1395	.284	.3616	.06																																			

Table 26a. EXPANSION AFTER FREEZING - WEDGE NOZZLE

$T_0' = 6000^\circ K, P_0' = 1000 \text{ atm.}$

$l = 0.1$													$l = 1.0$													$l = 10$												
T	P	M	A	T	P	M	A	T	P	M	A	T	P	M	A	T	P	M	A	T	P	M	A															
		u'				u'				u'				u'				u'				u'																
		(ft./sec.)				(ft./sec.)				(ft./sec.)				(ft./sec.)				(ft./sec.)				(ft./sec.)																
.591	.643-01	.1006 05	.274 01	.532 01	.302-01	.148-01	.8874 01	.441	.149-01	.320 01	.8874 01	.441	.149-01	.320 01	.8874 01	.441	.609-02	.1161 05	.366 01	.609-02	.1161 05	.366 01	.609-02	.1161 05	.366 01													
.58	.603-01	.1015 05	.280 01	.4789 01	.278-01	.129-01	.9576 01	.44	.148-01	.330 01	.9576 01	.44	.148-01	.330 01	.9576 01	.44	.603-02	.1162 05	.371 01	.603-02	.1162 05	.371 01	.603-02	.1162 05	.371 01													
.56	.573-01	.1031 05	.289 01	.5312 01	.241-01	.108-01	.1086 02	.42	.126-01	.341 01	.1086 02	.42	.126-01	.341 01	.1086 02	.42	.591-02	.1175 05	.384 01	.591-02	.1175 05	.384 01	.591-02	.1175 05	.384 01													
.54	.473-01	.1047 05	.299 01	.5920 01	.209-01	.894-02	.1240 02	.40	.107-01	.353 01	.1240 02	.40	.107-01	.353 01	.1240 02	.40	.596-02	.1186 05	.398 01	.596-02	.1186 05	.398 01	.596-02	.1186 05	.398 01													
.52	.416-01	.1062 05	.309 01	.6629 01	.179-01	.735-02	.1648 02	.38	.898-02	.365 01	.1648 02	.38	.898-02	.365 01	.1648 02	.38	.249-02	.1202 05	.413 01	.249-02	.1202 05	.413 01	.249-02	.1202 05	.413 01													
.51	.365-01	.1078 05	.320 01	.7463 01	.153-01	.595-02	.1781 02	.42	.179-01	.378 01	.1781 02	.42	.179-01	.378 01	.1781 02	.42	.194-02	.1216 05	.429 01	.194-02	.1216 05	.429 01	.194-02	.1216 05	.429 01													
.48	.318-01	.1093 05	.331 01	.8448 01	.130-01	.484-02	.1920 02	.34	.130-01	.392 01	.1920 02	.34	.130-01	.392 01	.1920 02	.34	.169-02	.1222 05	.446 01	.169-02	.1222 05	.446 01	.169-02	.1222 05	.446 01													
.46	.275-01	.1108 05	.343 01	.9621 01	.109-01	.387-02	.2256 02	.32	.109-01	.407 01	.2256 02	.32	.109-01	.407 01	.2256 02	.32	.407-02	.1225 05	.484 01	.407-02	.1225 05	.484 01	.407-02	.1225 05	.484 01													
.44	.237-01	.1122 05	.355 01	.1103 02	.912-02	.308-02	.3202 02	.28	.912-02	.422 01	.3202 02	.28	.912-02	.422 01	.3202 02	.28	.324-02	.1267 05	.505 01	.324-02	.1267 05	.505 01	.324-02	.1267 05	.505 01													
.42	.203-01	.1137 05	.368 01	.1273 02	.753-02	.239-02	.3875 02	.26	.753-02	.439 01	.3875 02	.26	.753-02	.439 01	.3875 02	.26	.254-02	.1280 05	.529 01	.254-02	.1280 05	.529 01	.254-02	.1280 05	.529 01													
.41	.172-01	.1151 05	.382 01	.1480 02	.616-02	.184-02	.4745 02	.24	.616-02	.457 01	.4745 02	.24	.616-02	.457 01	.4745 02	.24	.197-02	.1292 05	.555 01	.197-02	.1292 05	.555 01	.197-02	.1292 05	.555 01													
.38	.143-01	.1165 05	.396 01	.1734 02	.498-02	.139-02	.5888 02	.22	.498-02	.480 01	.5888 02	.22	.498-02	.480 01	.5888 02	.22	.149-02	.1304 05	.584 01	.149-02	.1304 05	.584 01	.149-02	.1304 05	.584 01													
.36	.121-01	.1179 05	.412 01	.2051 02	.397-02	.104-02	.7415 02	.20	.397-02	.522 01	.7415 02	.20	.397-02	.522 01	.7415 02	.20	.110-02	.1316 05	.617 01	.110-02	.1316 05	.617 01	.110-02	.1316 05	.617 01													
.34	.100-01	.1192 05	.428 01	.2449 02	.312-02	.756-03	.9497 02	.18	.312-02	.547 01	.9497 02	.18	.312-02	.547 01	.9497 02	.18	.798-03	.1327 05	.654 01	.798-03	.1327 05	.654 01	.798-03	.1327 05	.654 01													
.32	.823-02	.1206 05	.446 01	.2955 02	.241-02	.540-03	.1240 03	.16	.241-02	.576 01	.1240 03	.16	.241-02	.576 01	.1240 03	.16	.560-03	.1338 05	.694 01	.560-03	.1338 05	.694 01	.560-03	.1338 05	.694 01													
.31	.663-02	.1219 05	.465 01	.3608 02	.183-02	.375-03	.1654 03	.14	.183-02	.609 01	.1654 03	.14	.183-02	.609 01	.1654 03	.14	.379-03	.1349 05	.743 01	.379-03	.1349 05	.743 01	.379-03	.1349 05	.743 01													
.28	.533-02	.1232 05	.486 01	.4465 02	.136-02	.253-03	.2264 03	.12	.136-02	.646 01	.2264 03	.12	.136-02	.646 01	.2264 03	.12	.244-03	.1359 05	.812 01	.244-03	.1359 05	.812 01	.244-03	.1359 05	.812 01													
.26	.423-02	.1245 05	.509 01	.5606 02	.986-03	.165-03	.3194 05	.10	.986-03	.689 01	.3194 05	.10	.986-03	.689 01	.3194 05	.10	.148-03	.1369 05	.892 01	.148-03	.1369 05	.892 01	.148-03	.1369 05	.892 01													
.24	.326-02	.1257 05	.535 01	.7157 02	.693-03	.103-03	.4674 03	.09	.693-03	.740 01	.4674 03	.09	.693-03	.740 01	.4674 03	.09	.112-03	.1374 05	.941 01	.112-03	.1374 05	.941 01	.112-03	.1374 05	.941 01													
.22	.245-02	.1269 05	.563 01	.9311 02	.469-03	.614-04	.6716 03	.08	.469-03	.802 01	.6716 03	.08	.469-03	.802 01	.6716 03	.08	.821-04	.1379 05	.999 01	.821-04	.1379 05	.999 01	.821-04	.1379 05	.999 01													
.20	.185-02	.1281 05	.595 01	.1238 03	.304-03	.346-04	.1169 04	.07	.304-03	.882 01	.1169 04	.07	.304-03	.882 01	.1169 04	.07	.581-04	.1384 05	.1107 02	.581-04	.1384 05	.1107 02	.581-04	.1384 05	.1107 02													
.18	.134-02	.1293 05	.631 01	.1688 03	.185-03	.177-04	.1541 04	.06	.185-03	.939 01	.1541 04	.06	.185-03	.939 01	.1541 04	.06	.391-04	.1388 05	.127 02	.391-04	.1388 05	.127 02	.391-04	.1388 05	.127 02													
.16	.948-03	.1304 05	.674 01	.2372 03	.166-03	.117-04	.2089 04	.05	.166-03	.987 01	.2089 04	.05	.166-03	.987 01	.2089 04	.05	.246-04	.1393 05	.143 02	.246-04	.1393 05	.143 02	.246-04	.1393 05	.143 02													
.14	.643-03	.1315 05	.724 01	.3457 03	.103-03	.765-05	.2689 05	.04	.103-03	.106 02	.2689 05	.04	.103-03	.106 02	.2689 05	.04	.140-04	.1398 05	.165 02	.140-04	.1398 05	.165 02	.140-04	.1398 05	.165 02													
.12	.419-03	.1326 05	.785 01	.5275 03	.727-04	.474-05	.4341 04	.03	.727-04	.114 02	.4341 04	.03	.727-04	.114 02	.4341 04	.03	.673-05	.1402 05	.204 02	.673-05	.1402 05	.204 02	.673-05	.1402 05	.204 02													
.11	.256-03	.1337 05	.863 01	.8563 03	.491-04	.274-05	.6870 04	.02	.491-04	.126 02	.6870 04	.02	.491-04	.126 02	.6870 04	.02	.241-05	.1407 05	.324 02	.241-05	.1407 05	.324 02	.241-05	.1407 05	.324 02													
.09	.164-03	.1342 05	.910 01	.1126 04	.309-04	.144-05	.1386 05	.01	.309-04	.141 02	.1386 05	.01	.309-04	.141 02	.1386 05	.01	.413-06	.1412 05	.508 02	.413-06	.1412 05	.508 02	.413-06	.1412 05	.508 02													
.08	.143-03	.1347 05	.967 01	.1522 04	.176-04	.164-06	.2480 05	.01	.176-04	.163 02	.2480 05	.01	.176-04	.163 02	.2480 05	.01	.270-08	.1412 05	.508 02	.270-08	.1412 05	.508 02	.270-08	.1412 05	.508 02													
.07	.102-03	.1352 05	.104 02	.2134 04	.850-05	.238-06	.3391 05	.01	.850-05	.201 02	.3391 05	.01	.850-05	.201 02	.3391 05	.01																						
.06	.668-04	.1356 05	.112 02	.4452 04	.306-05	.567-07	.4900 05	.01	.306-05	.277 02	.4900 05	.01	.306-05	.277 02	.4900 05	.01																						
.05	.435-04	.1361 05	.123 02	.6752 04	.205-05				.205-05																													
.04	.246-04	.1366 05	.138 02	.8634 04	.176-04				.176-04																													
.03	.121-04	.1371 05	.160 02	.1769 05	.340-06				.340-06																													
.02	.438-05	.1376 05	.197 02	.4867 05	.810-07				.810-07																													
.01	.771-06	.1380 05	.271 02	.2756 06	.810-08				.810-08																													

Table 26b. EXPANSION AFTER FREEZING - HYPERBOLIC NOZZLE

$T_0' = 6000^\circ K$, $p_0' = 1000$ atm.

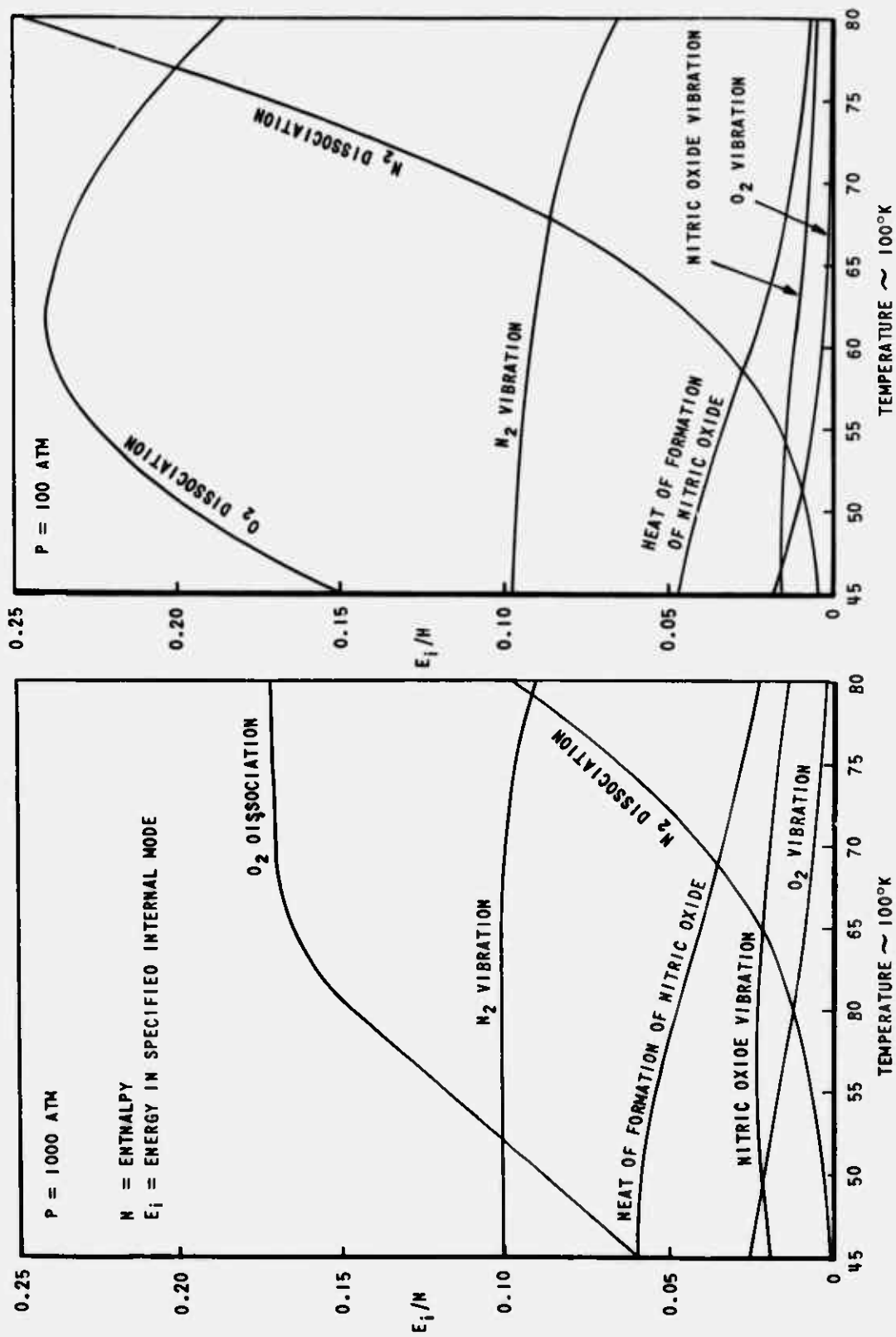
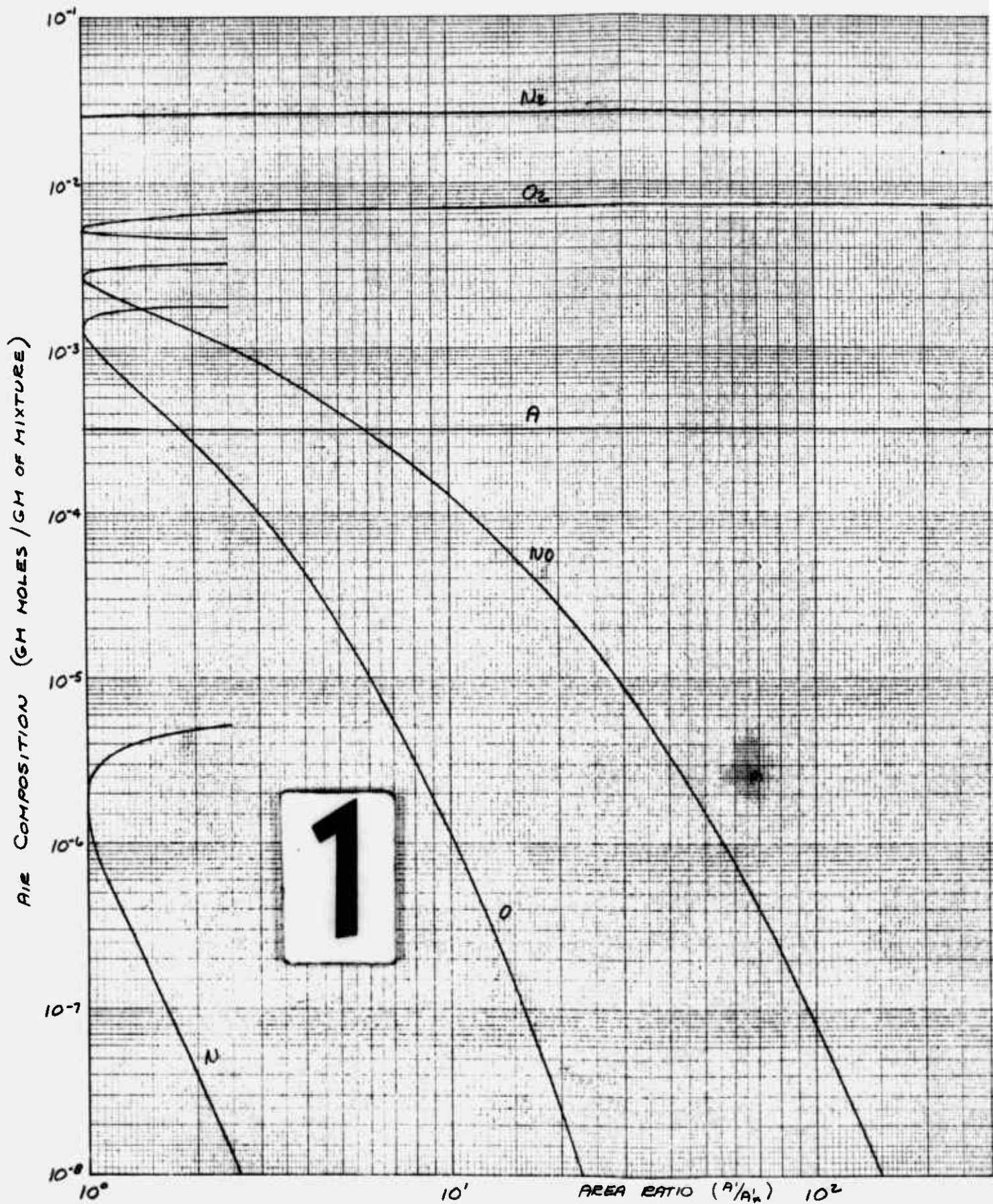
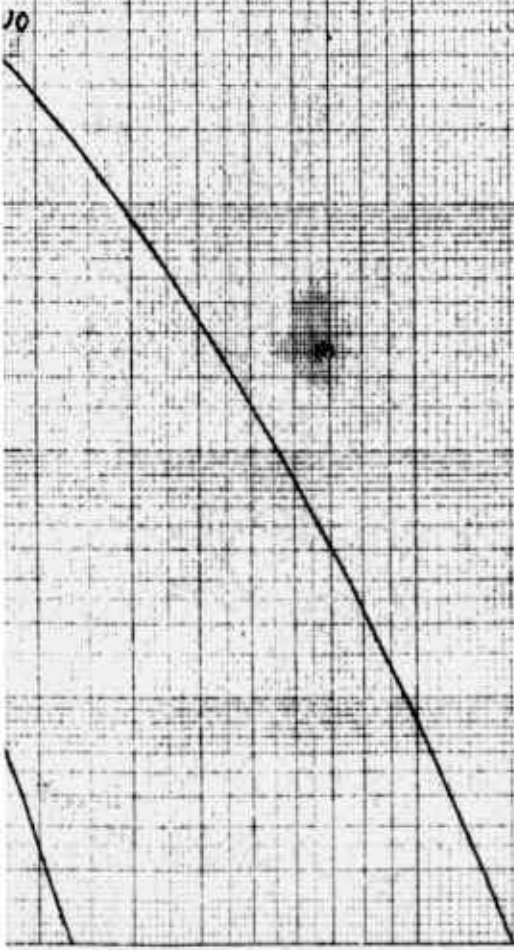


Figure 1 FRACTION OF THE ENTHALPY OF EQUILIBRIUM AIR WHICH IS IN THE SPECIFIED ENERGY MODE
 (REFERENCE: CAL REPORT NO. BE-1007-A-3)



AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC

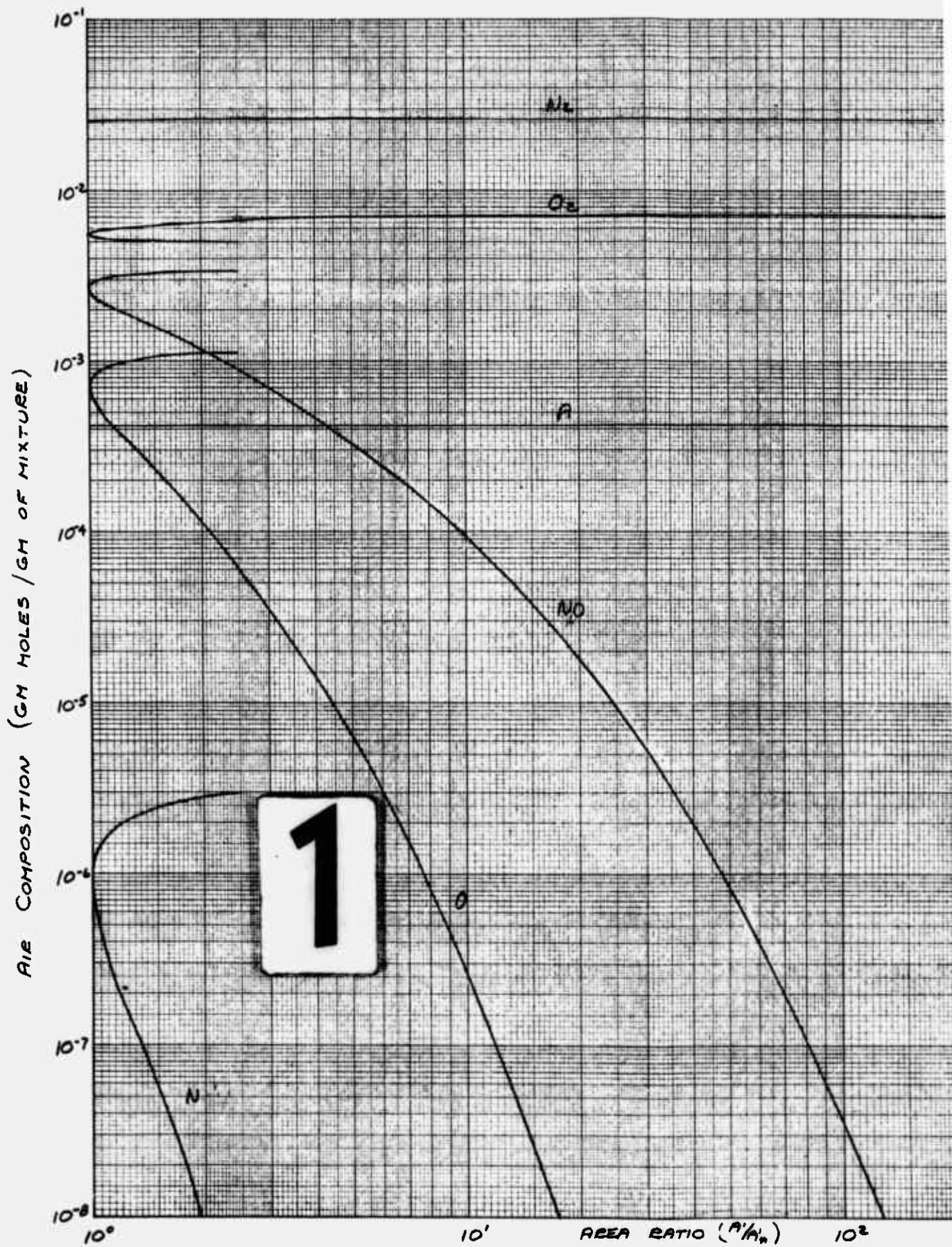
FIGURE NO. 2
 $T_0 = 4000^\circ K$
 $P_0 = 100 \text{ ATM}$



2

AREA RATIO (A/A^*) 10^2 10^3 10^4

VS AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION



AIR COMPOSITION VS AREA RATIO IN AN

FIGURE NO. 3
 $T_0 = 4000^\circ\text{K}$
 $P_0 = 300\text{ ATM}$

2

u_c

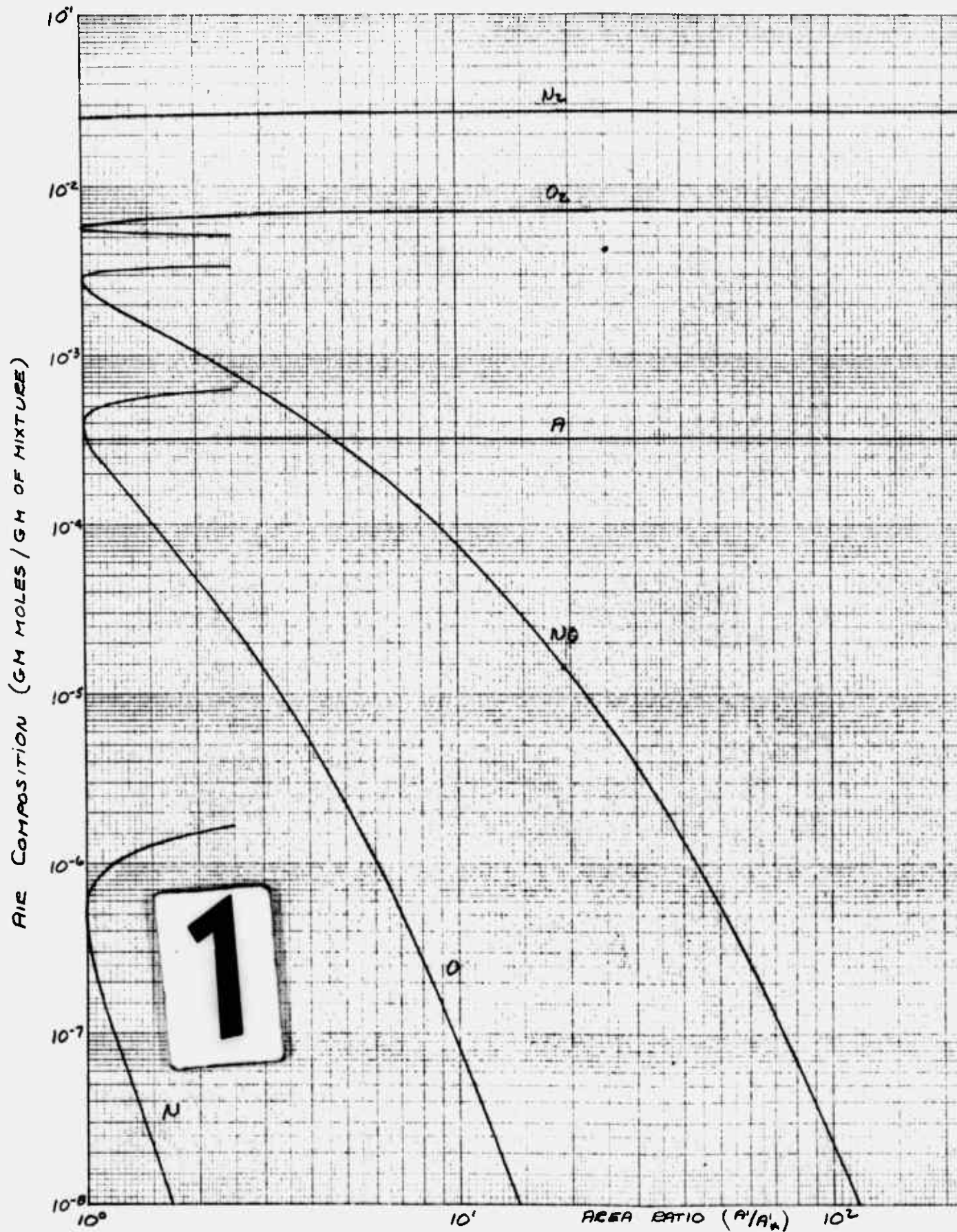
Q_c

A

NO

AREA RATIO (A/A_0) 10^2 10^3 10^4

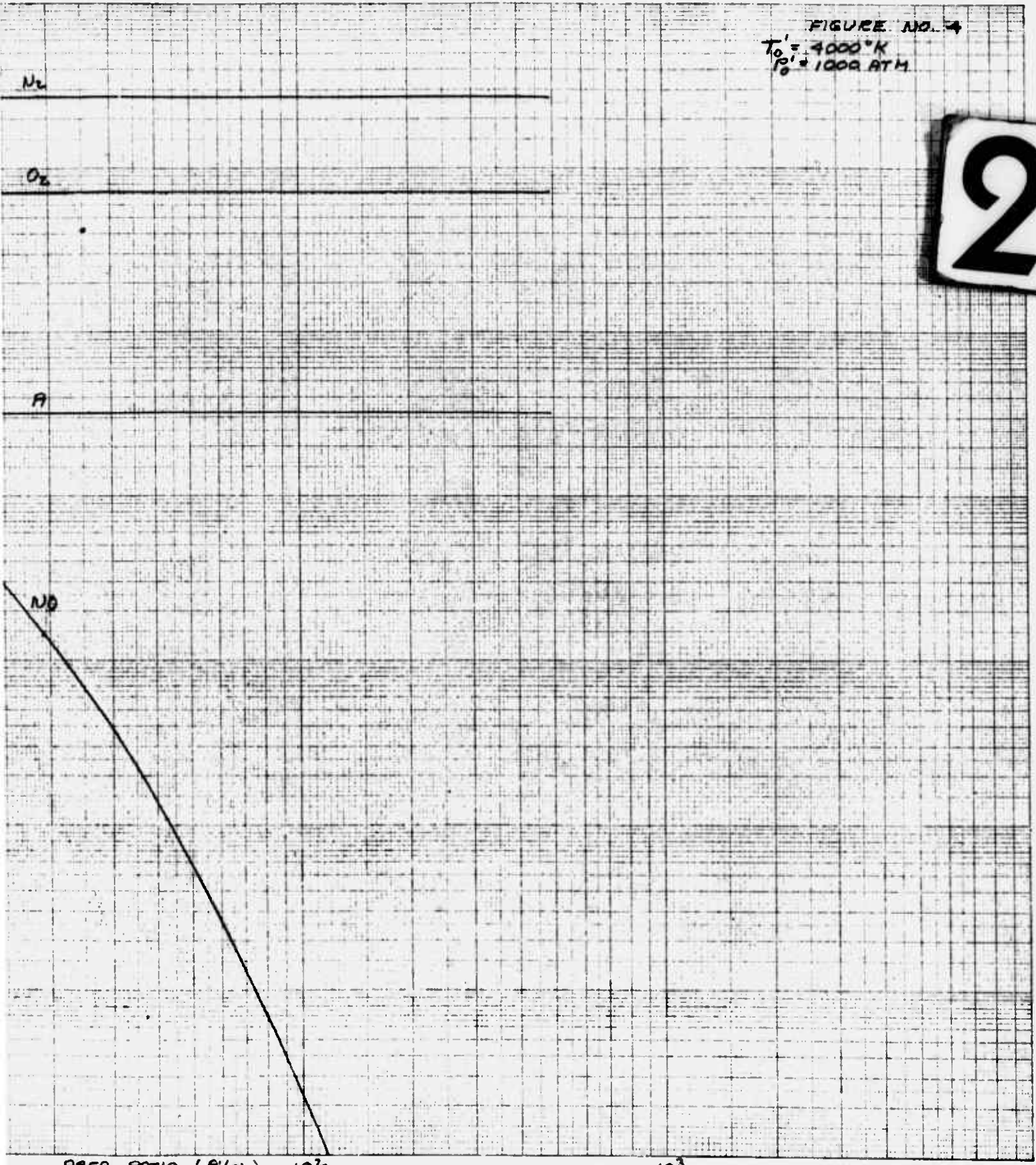
ION VS AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION



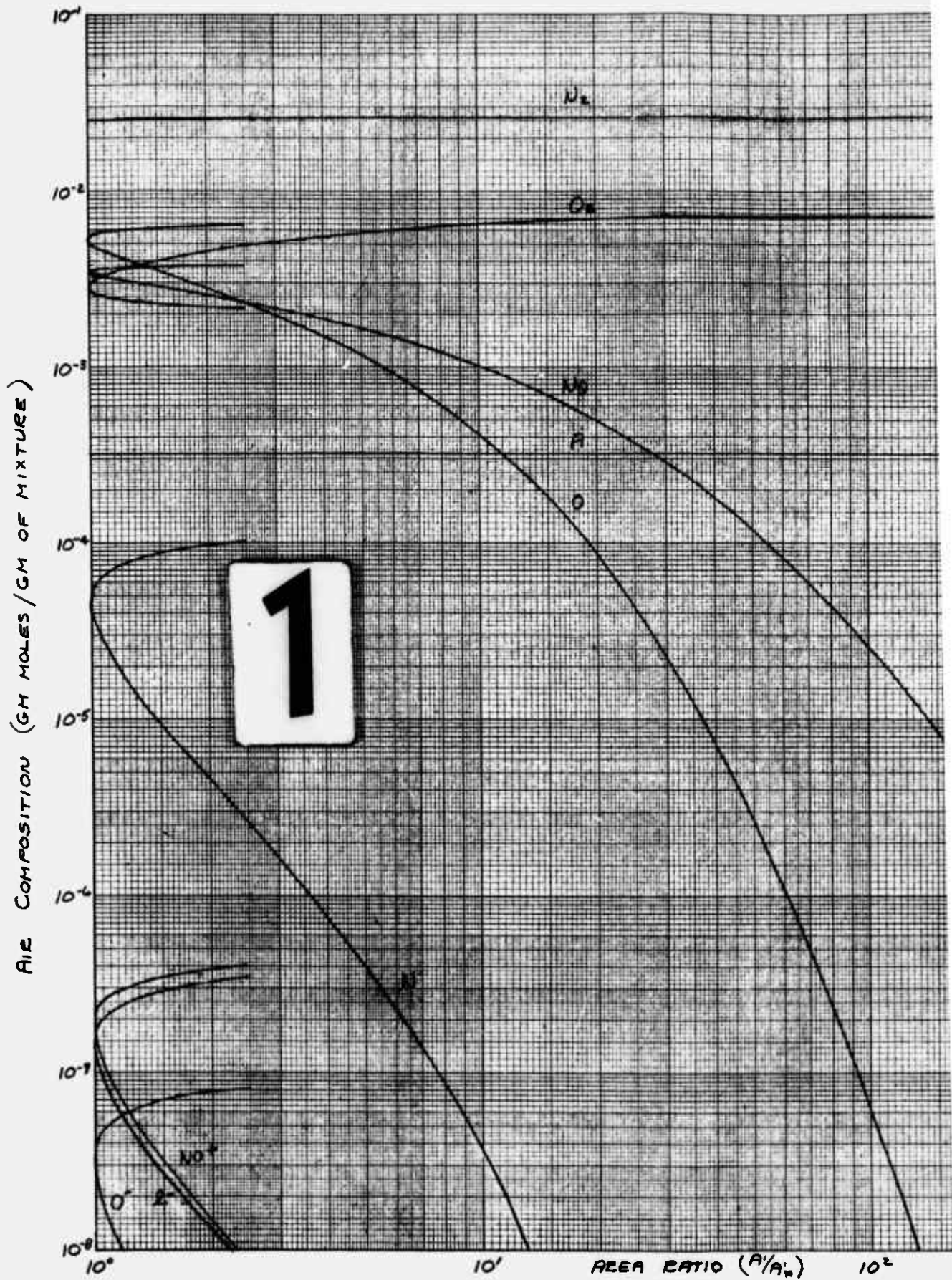
AIR COMPOSITION VS AREA RATIO IN AN J.S

FIGURE NO. 4
 $T_0 = 4000^\circ K$
 $P_0 = 1000 \text{ ATM}$

2

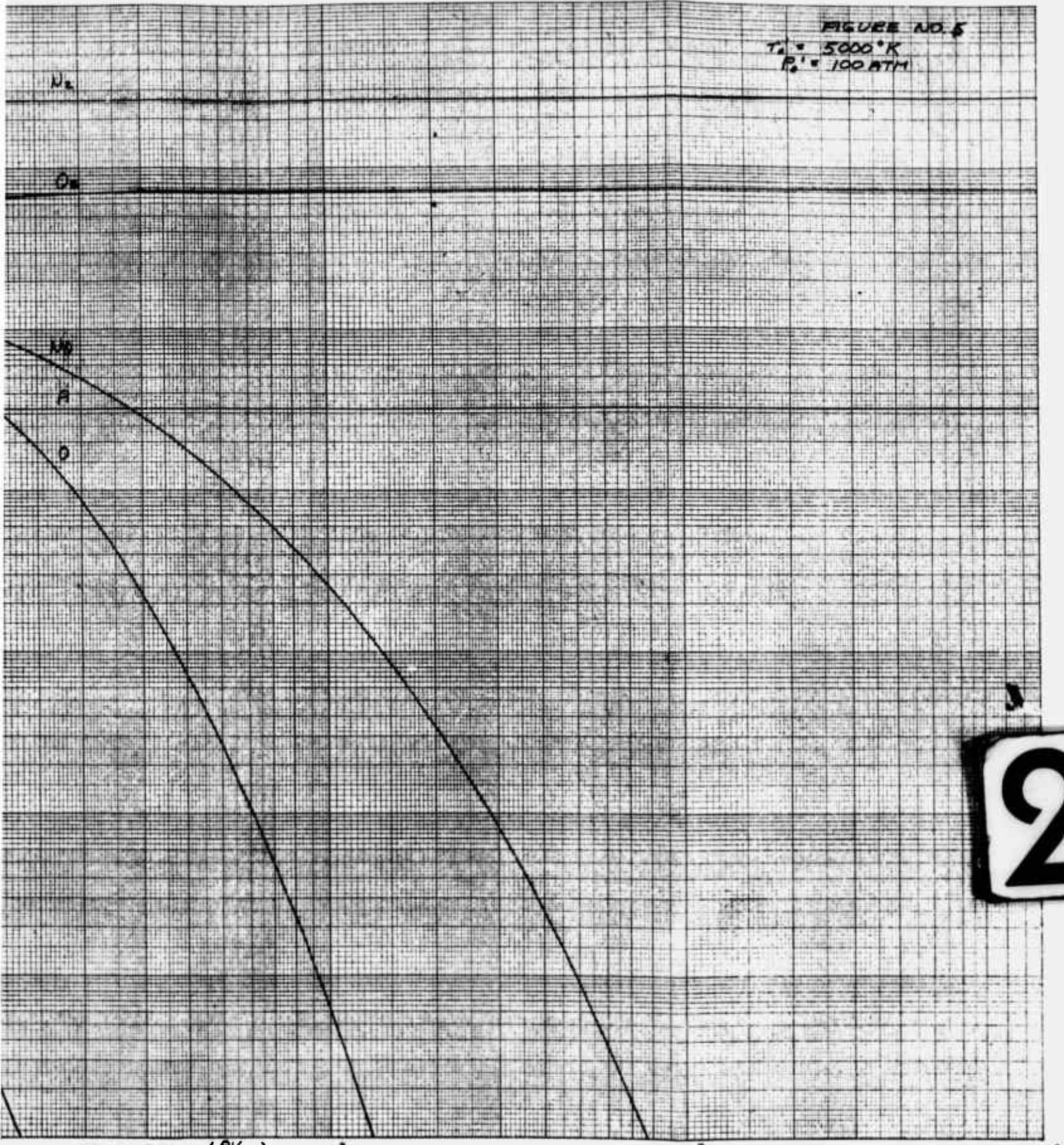


ON VS AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION



AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC FLOW

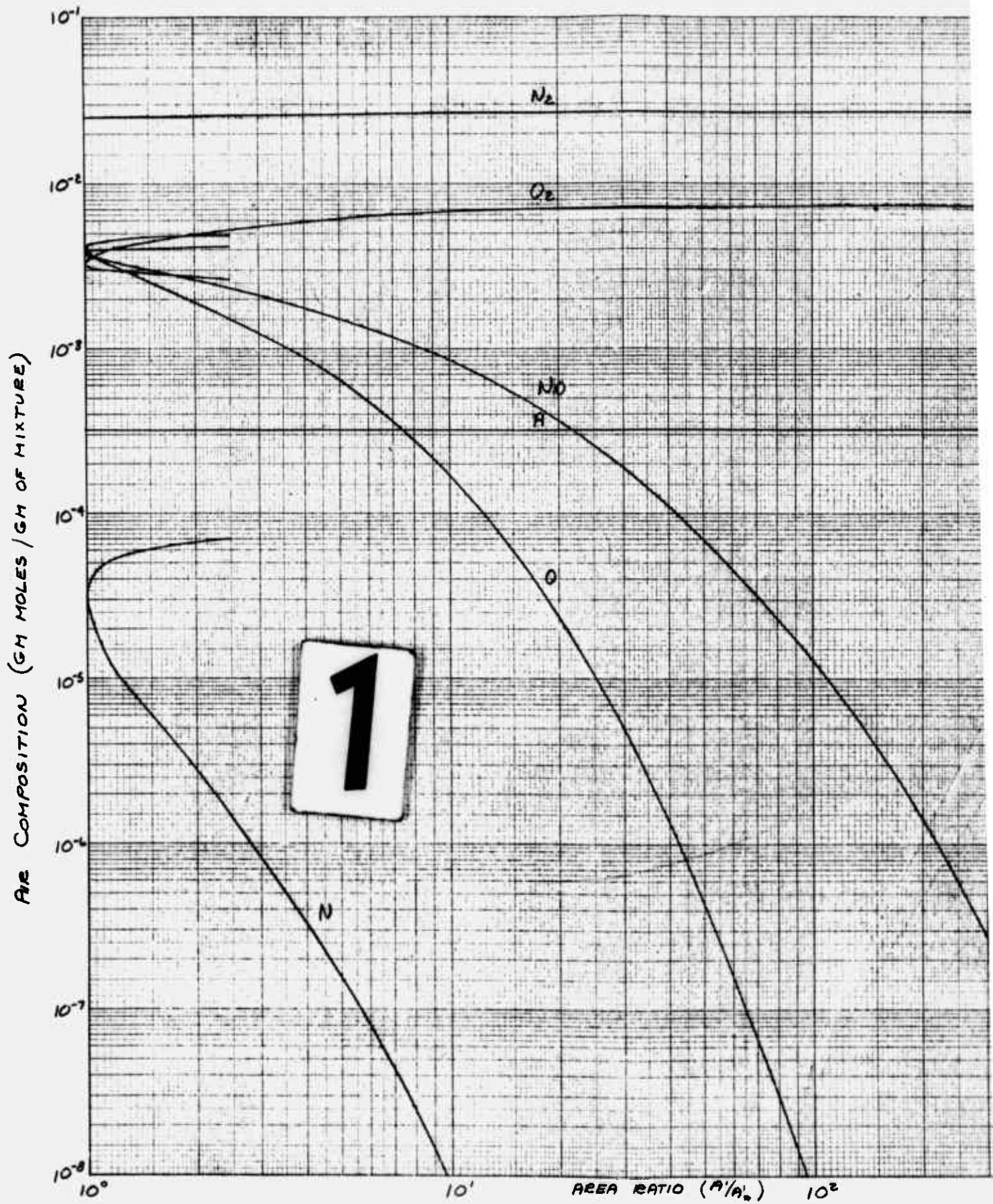
FIGURE NO. 5
 $T_0 = 5000^\circ\text{K}$
 $P_0 = 100\text{ ATM}$



2

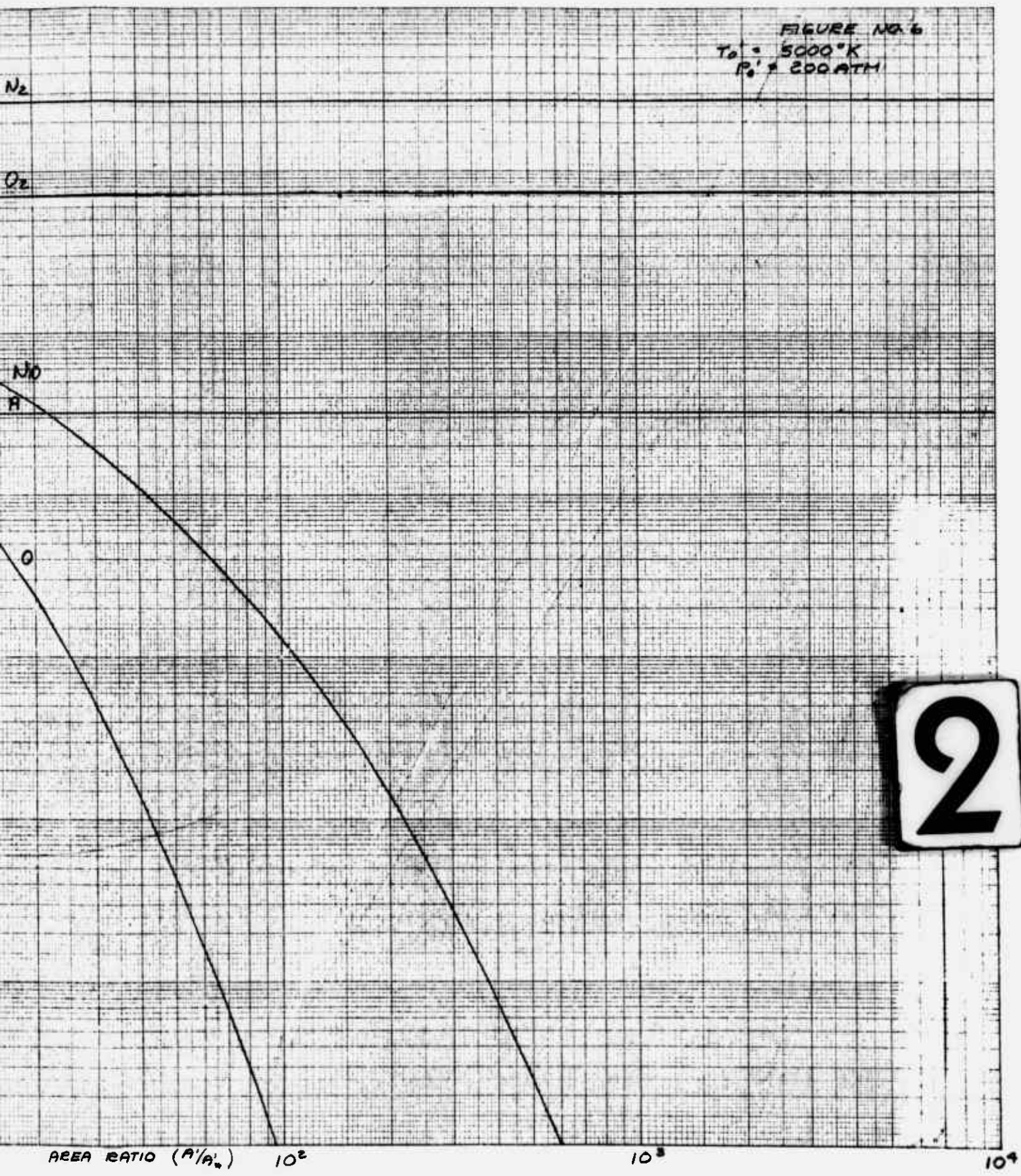
AREA RATIO (A/A_0) 10^2 10^3 10^4

VS AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION



AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC FLOW

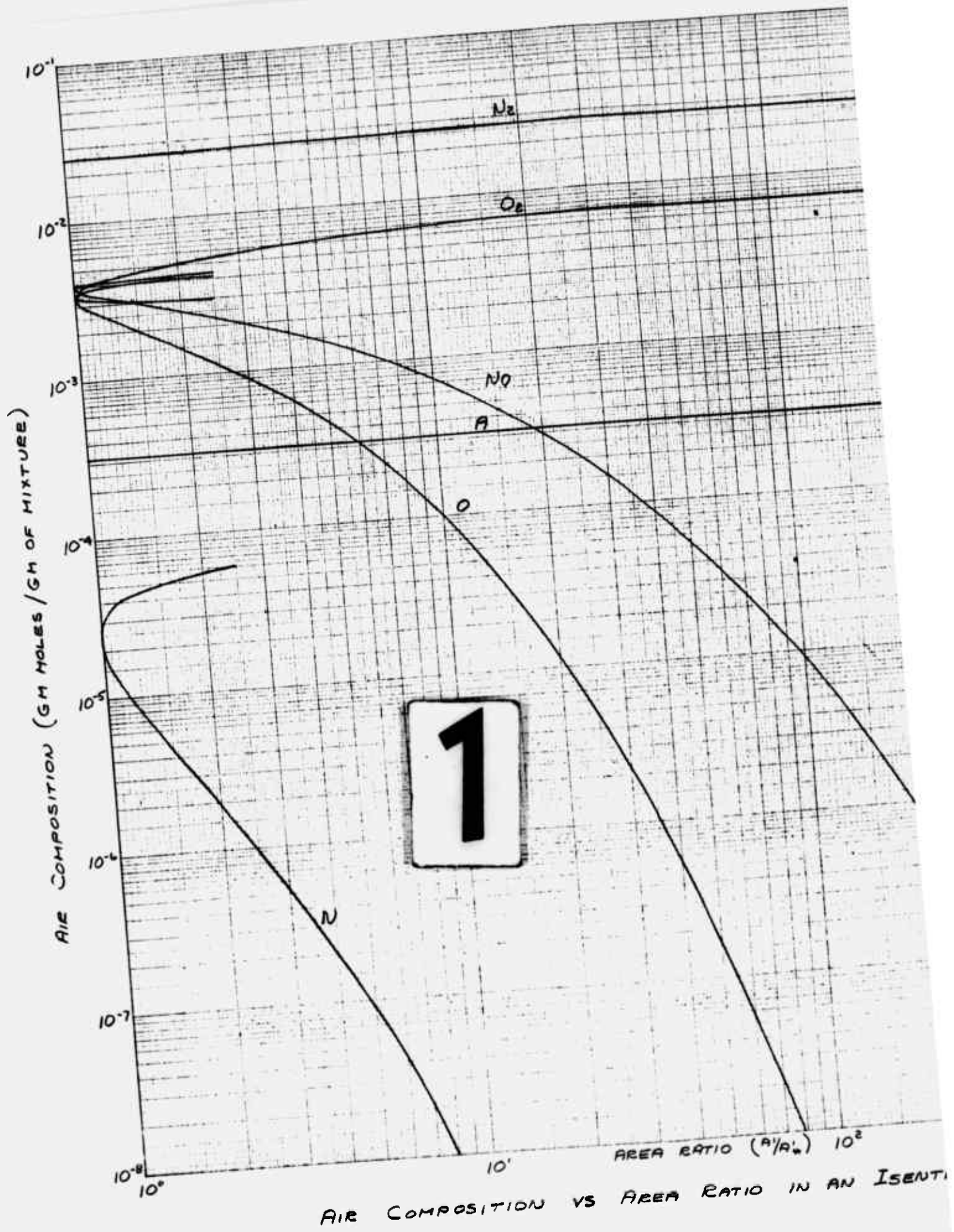
FIGURE NO. 6
 $T_0 = 5000^\circ\text{K}$
 $P_0 = 200\text{ ATM}$



2

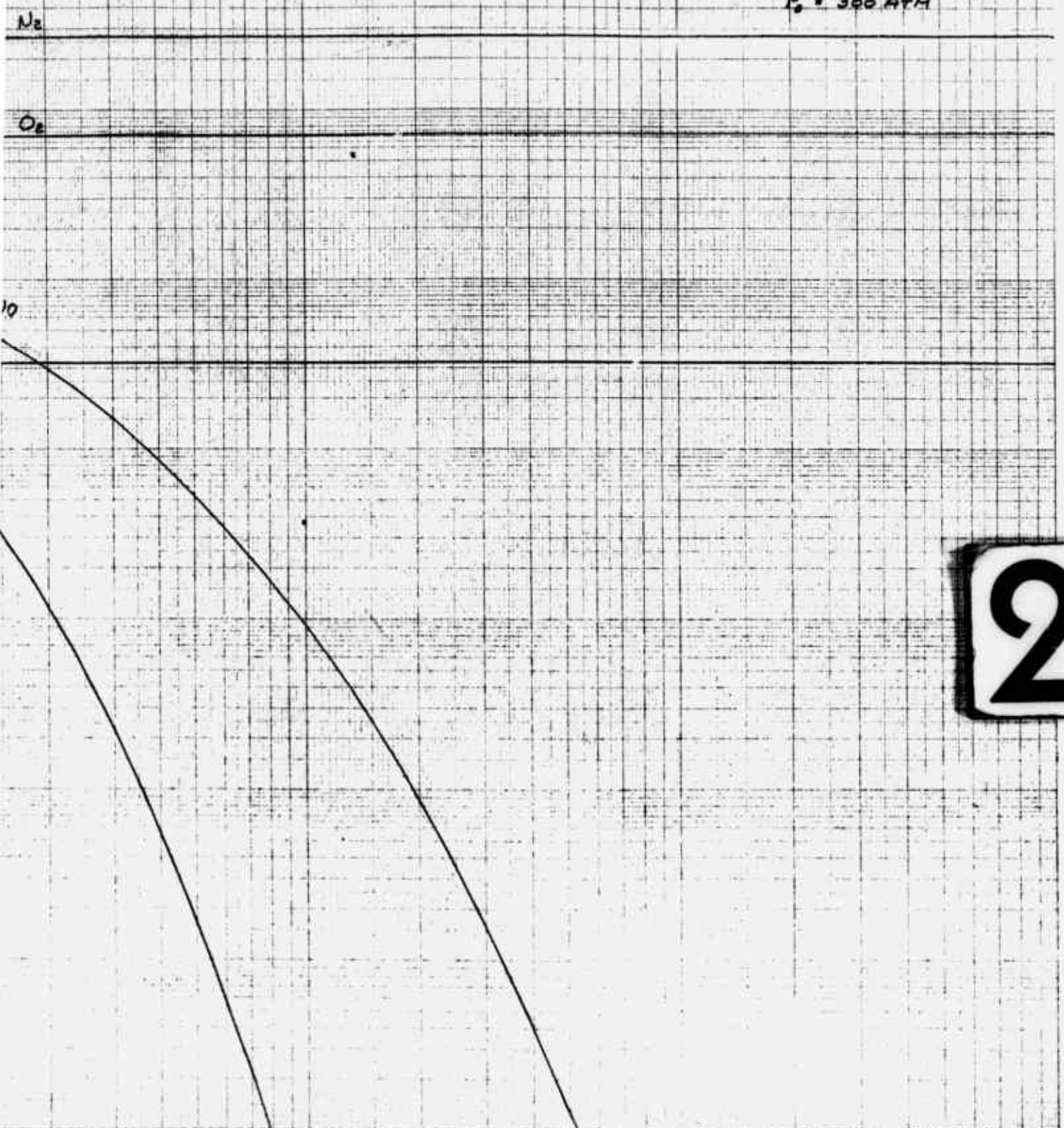
AREA RATIO (A/A^*) 10^1 10^2 10^3 10^4

VS AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION



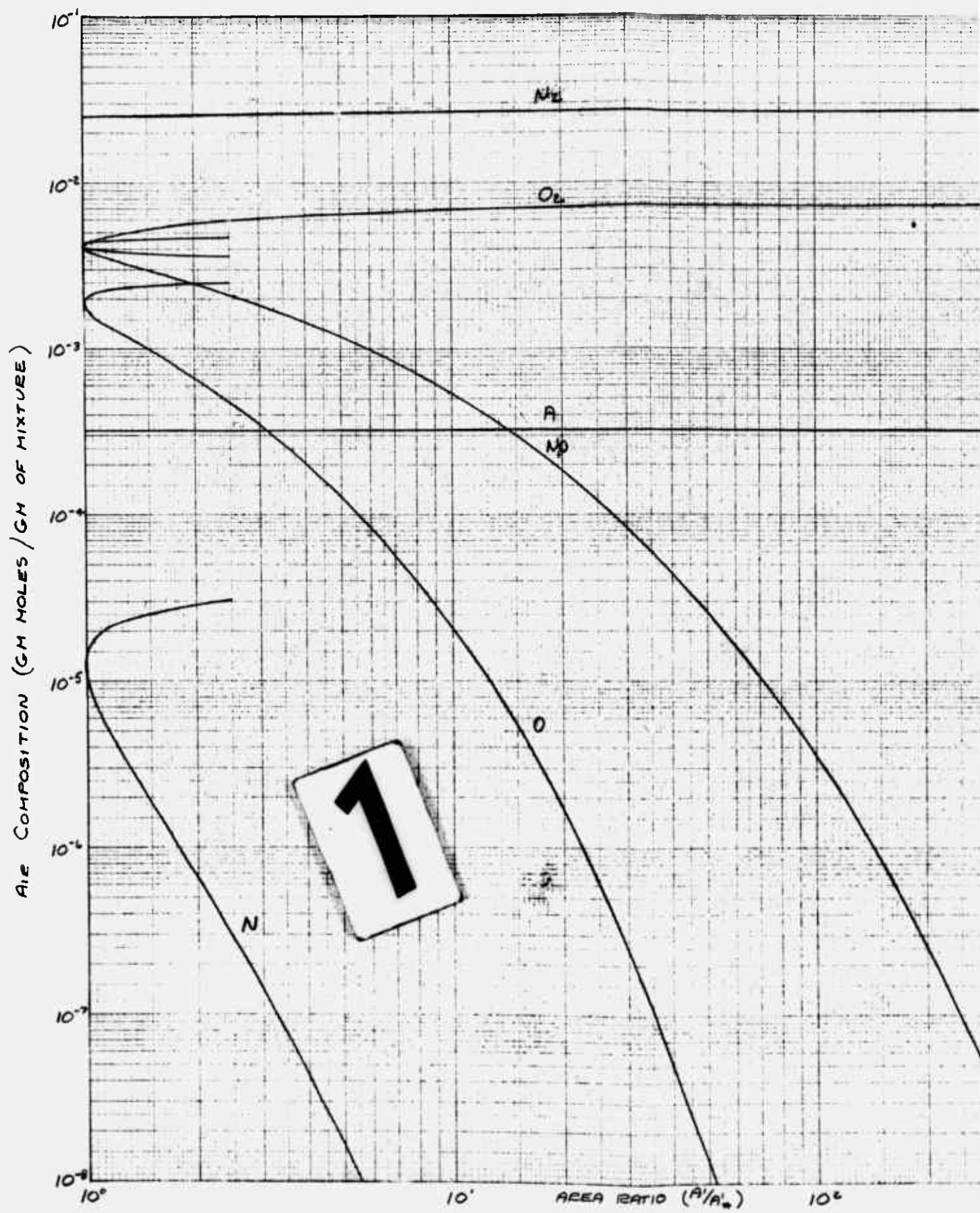
AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC FLOW

FIGURE NO. 7
 $T_0^* = 5000^\circ K$
 $P_0^* = 300 \text{ ATM}$



2

VS AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION



AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC

FIGURE NO. 8

$T_0 = 5000^\circ\text{K}$
 $P_0 = 1000\text{ ATM}$

2

N_2

O_2

P

30

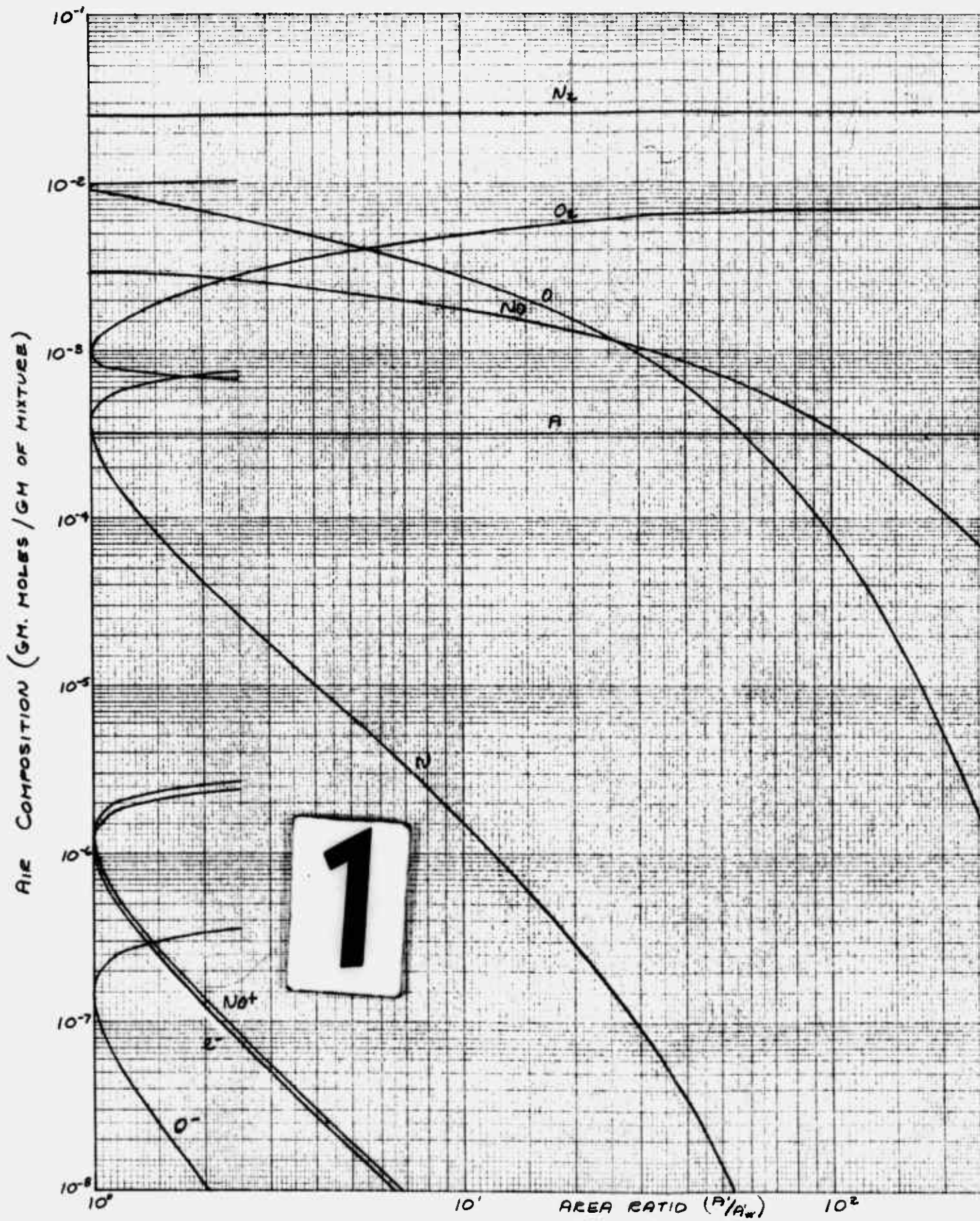
AREA RATIO (A/A_*)

10^2

10^3

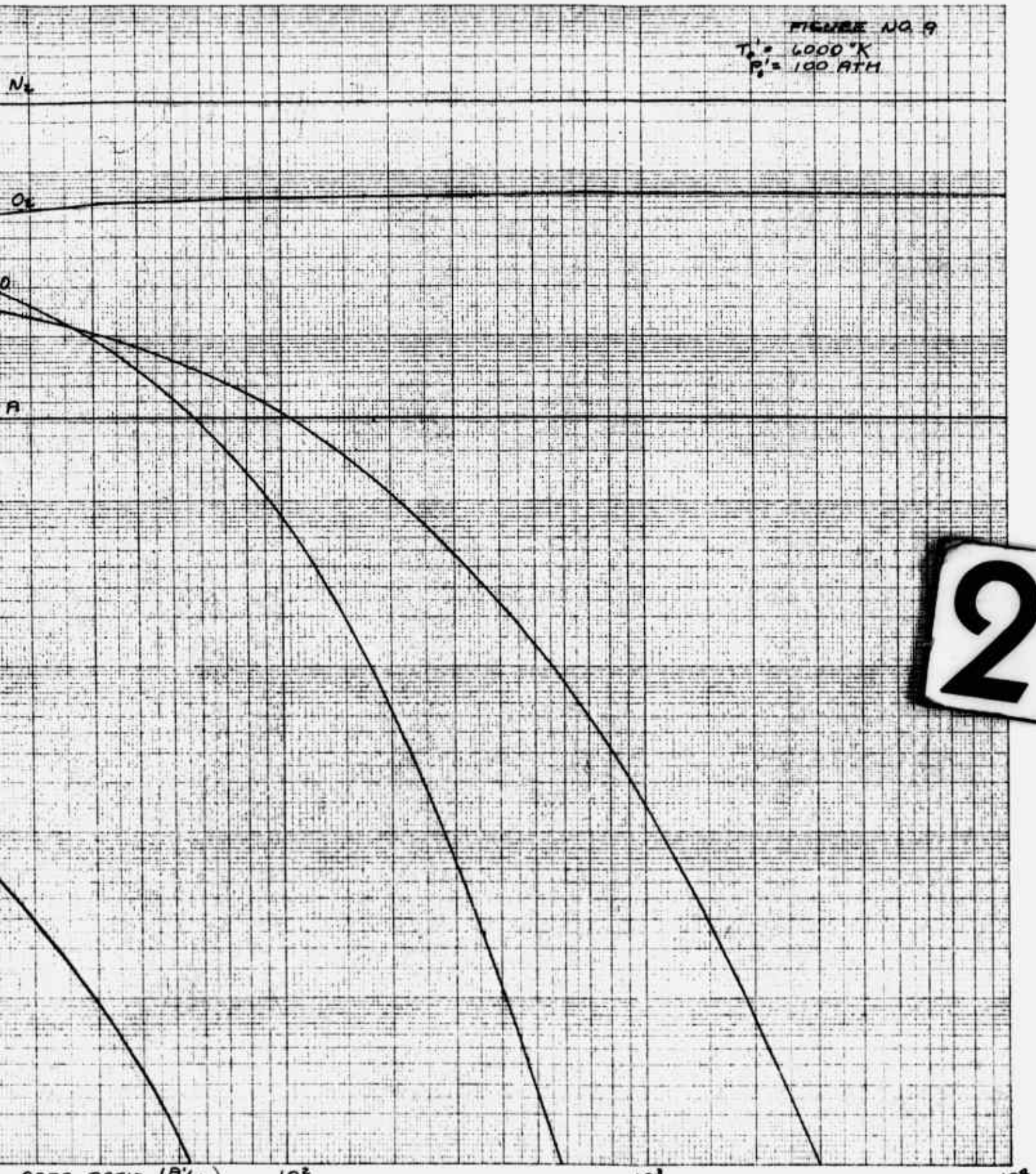
10^4

AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION



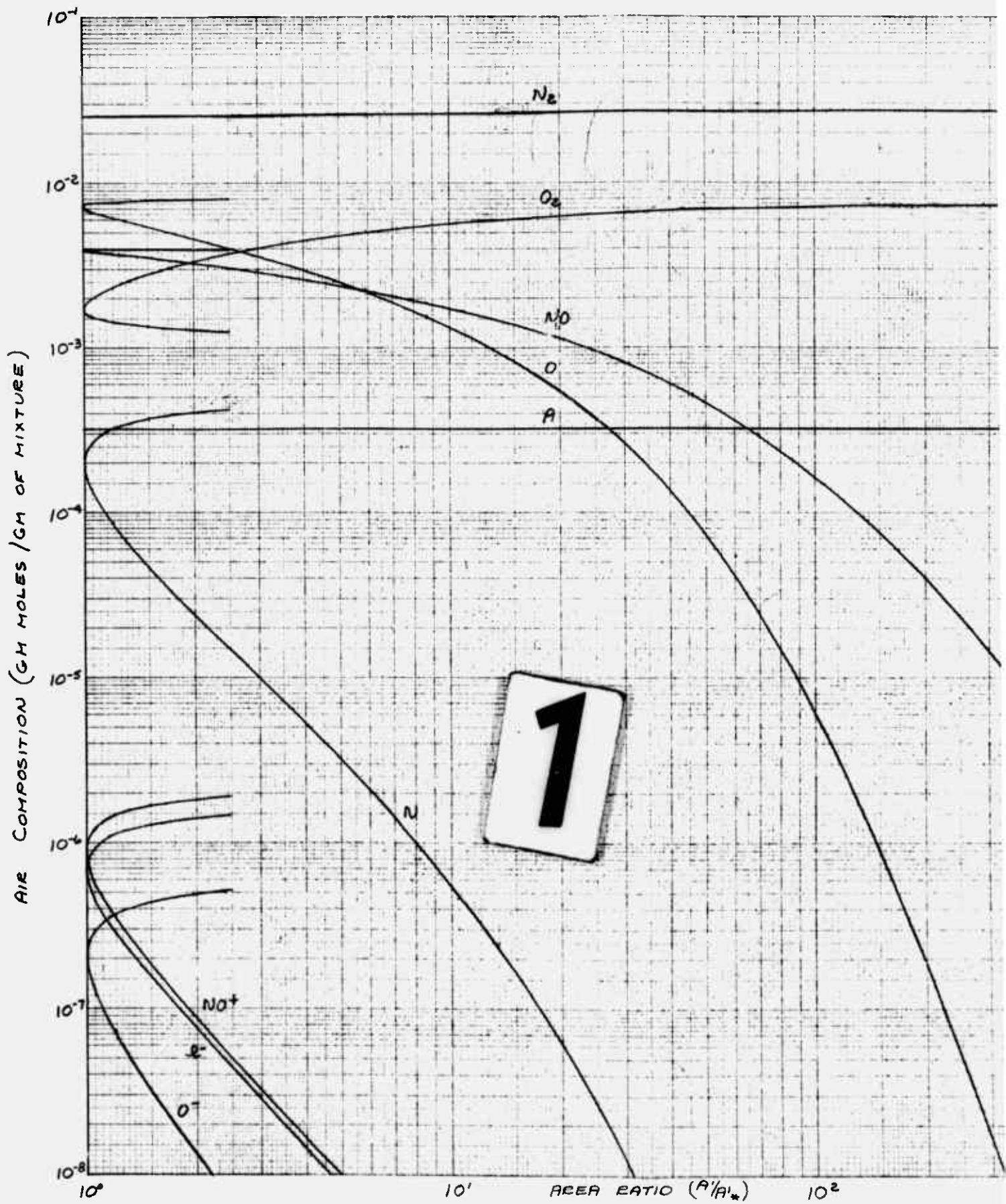
AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC

FIGURE NO. 9
 $T_0 = 6000^\circ K$
 $P_0 = 100 \text{ ATM}$



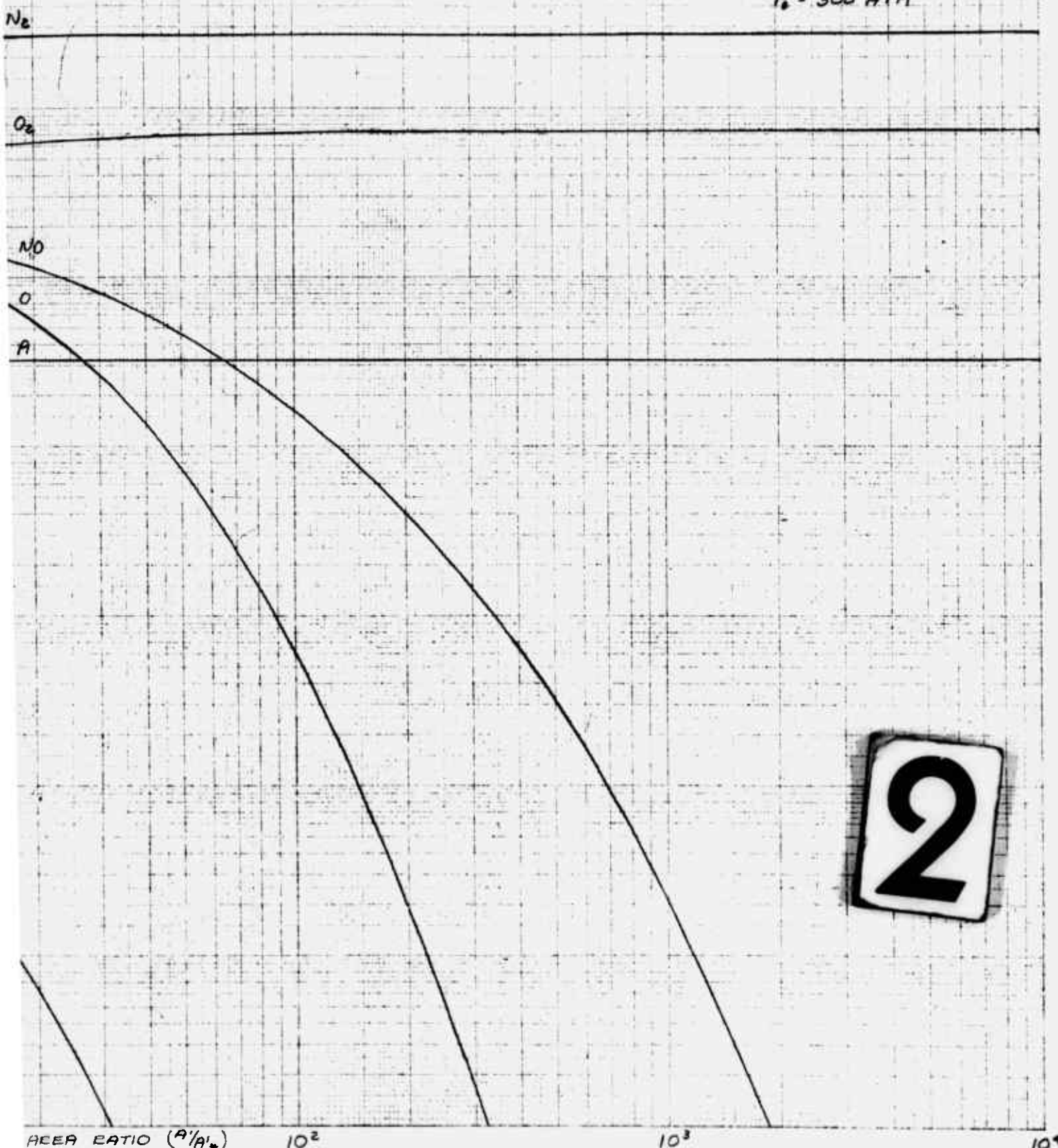
2

AREA RATIO (A/A^*) 10^2 10^3 10^4
AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION



AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC FLOW

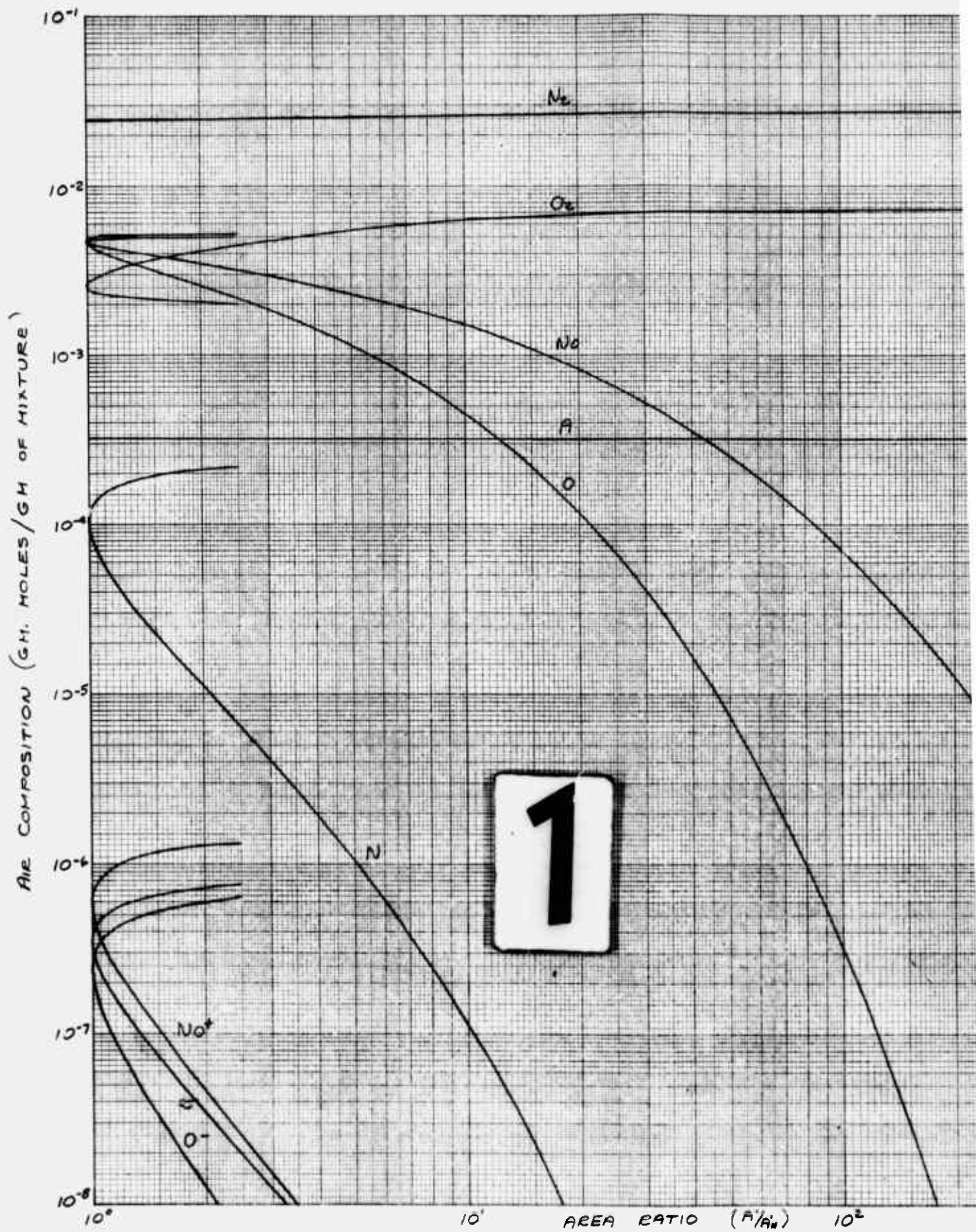
FIGURE NO. 10
 $T_0 = 6000^\circ\text{K}$
 $P_0 = 300\text{ ATM}$



2

AREA RATIO (A/A^*) 10^2 10^3 10^4

AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION



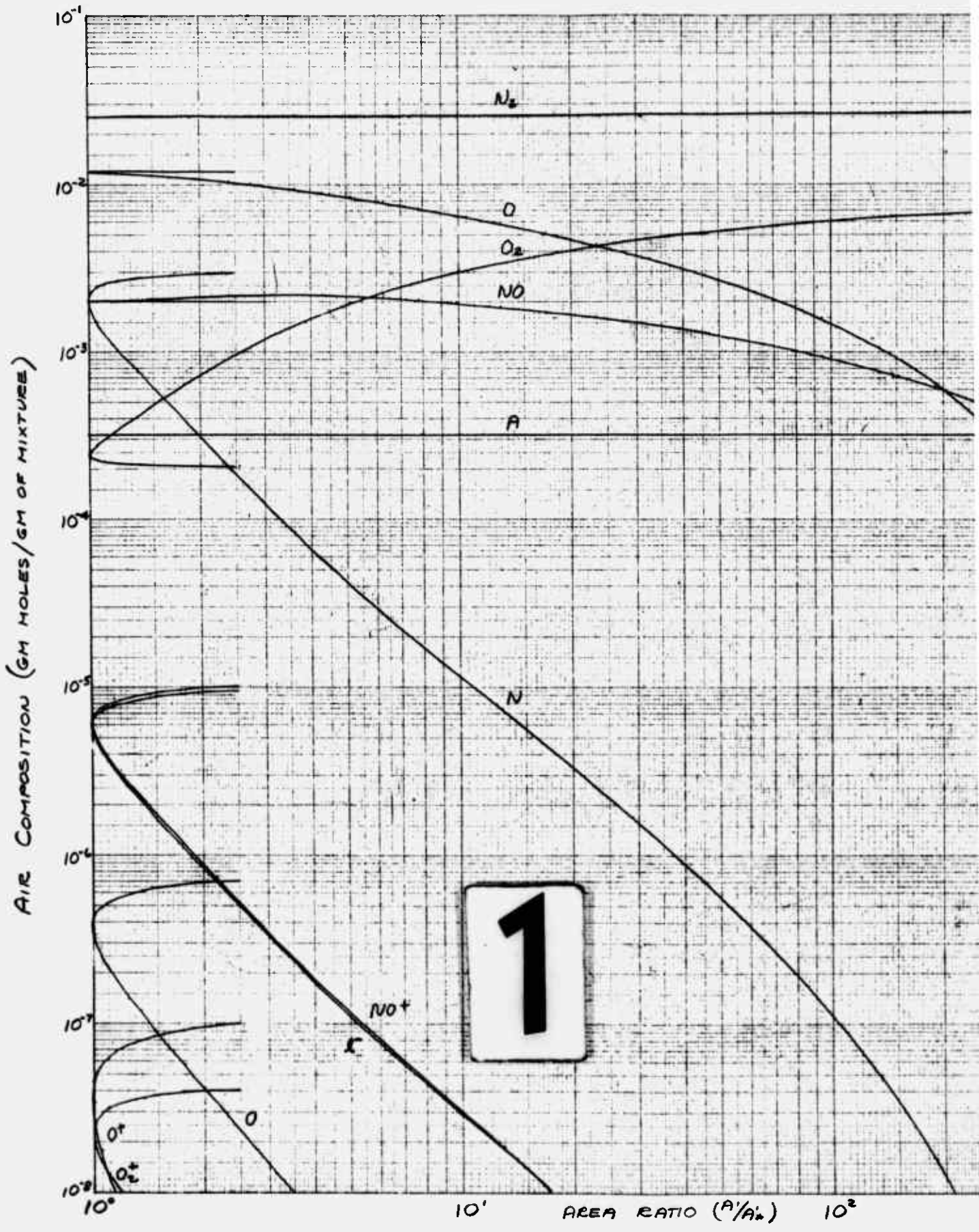
AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC EQUIL

FIGURE NO. 11
6000°K
1000ATM

2

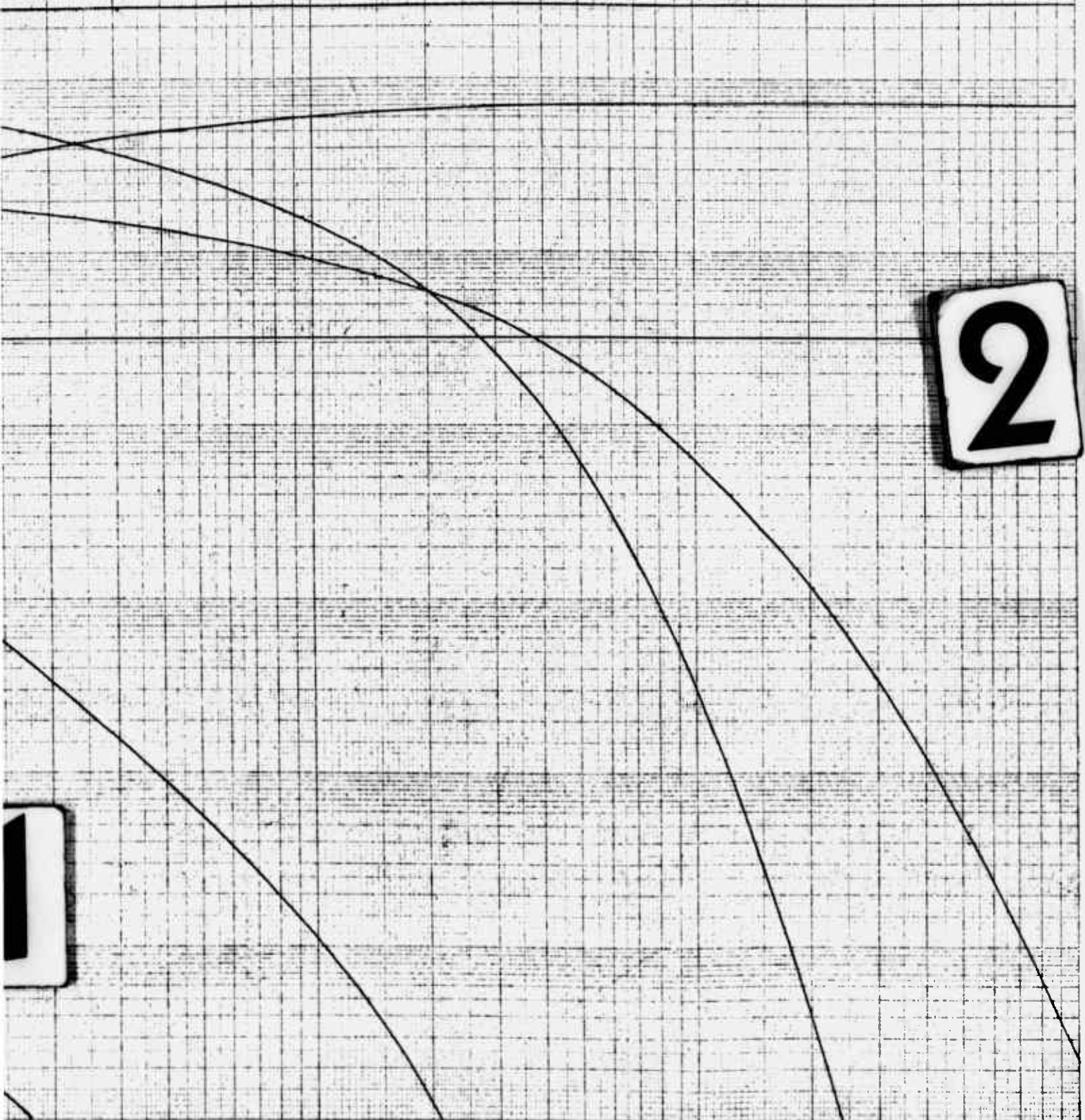
AREA RATIO (A/A_0) 10^2 10^3 10^4

RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION

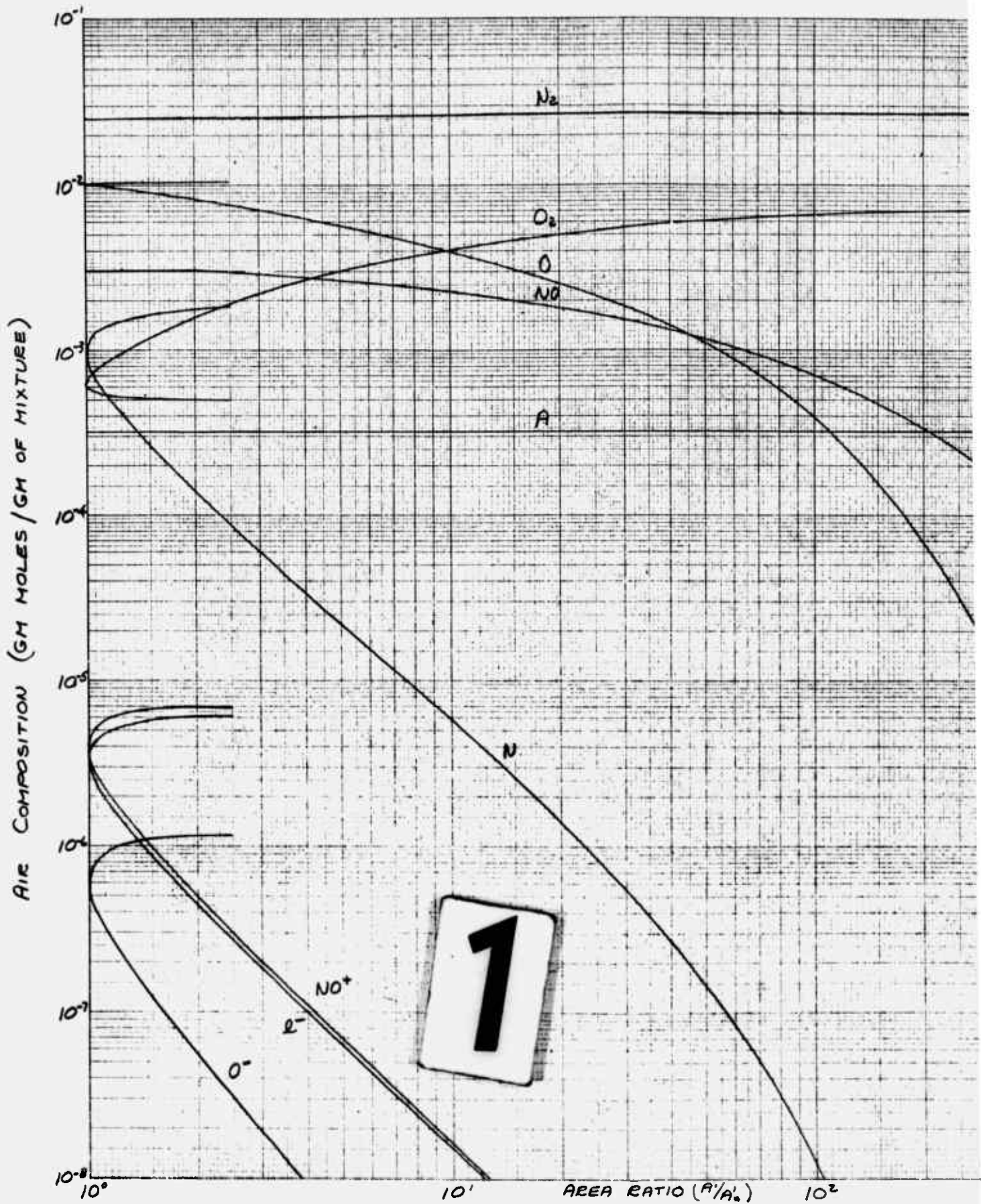


AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC

FIGURE NO. 12
 $T_0 = 7000^\circ\text{K}$
 $P_0 = 100\text{ ATM}$

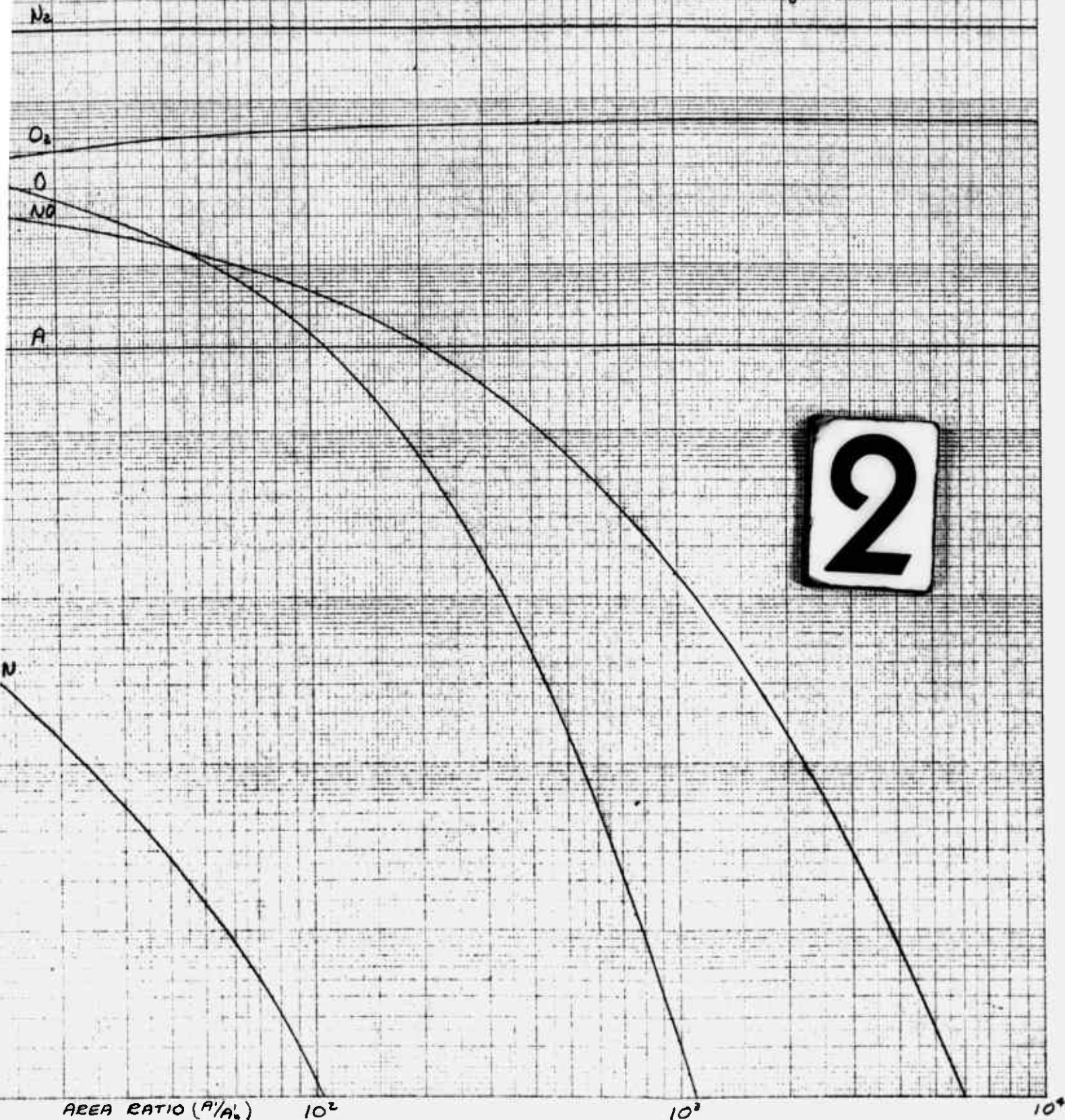


AREA RATIO (A/A₀) 10² 10³ 10⁴
VS AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION

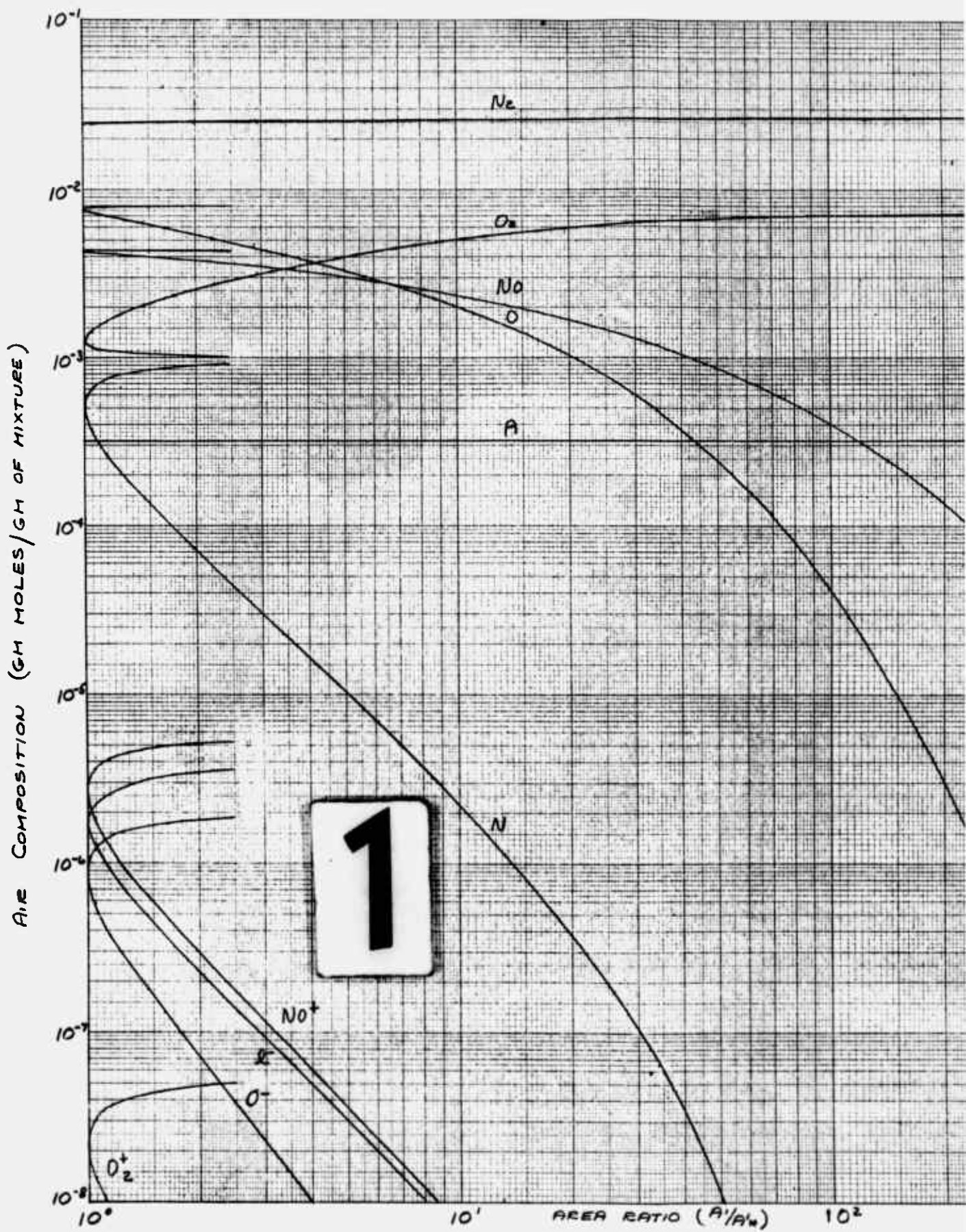


AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC FLOW

FIGURE NO. 13
 $T_0 = 7000 \text{ K}$
 $P_0 = 300 \text{ ATM}$

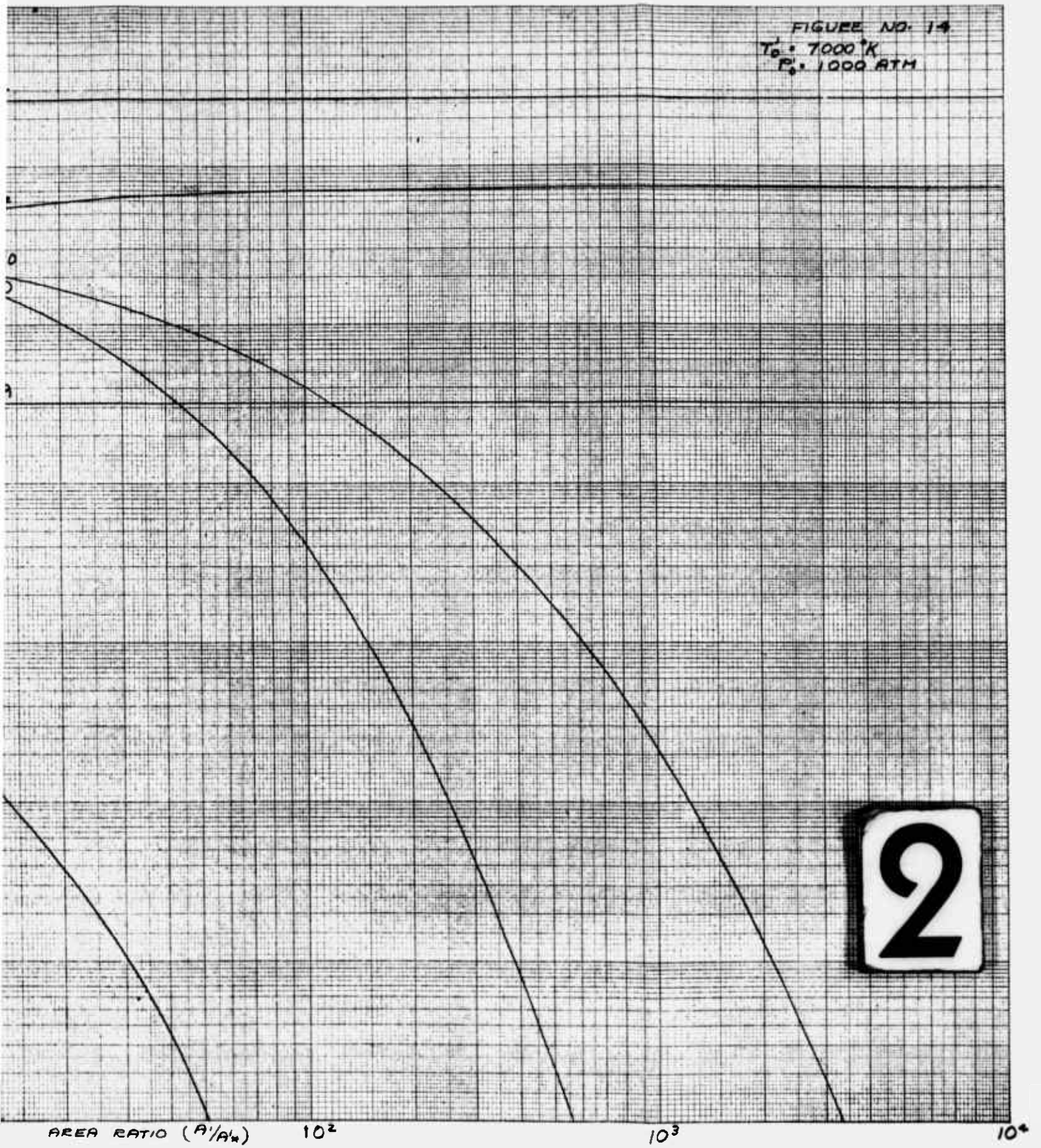


ON VS AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION

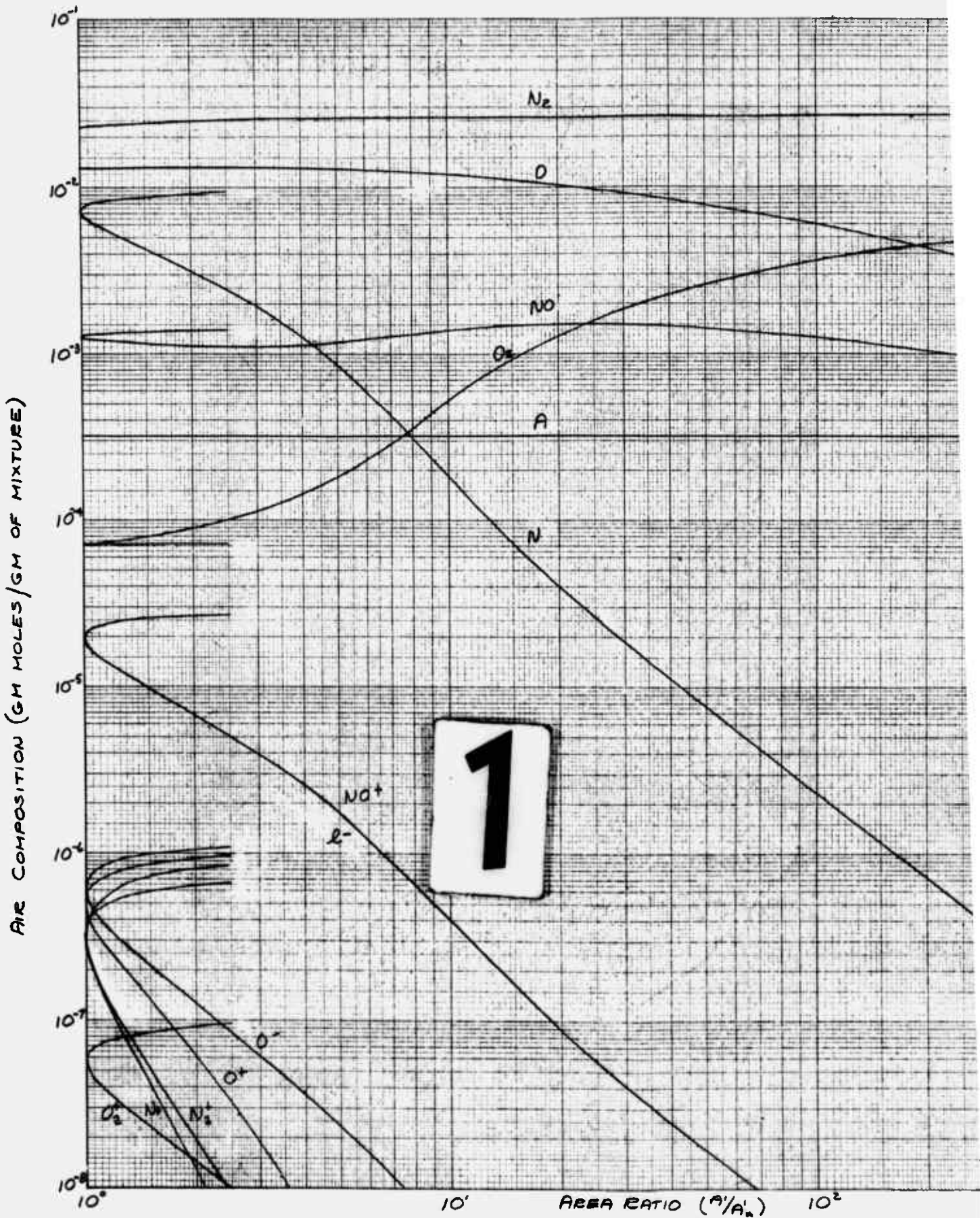


AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC

FIGURE NO. 14
 $T_0 = 7000^\circ\text{K}$
 $P_0 = 1000\text{ ATM}$

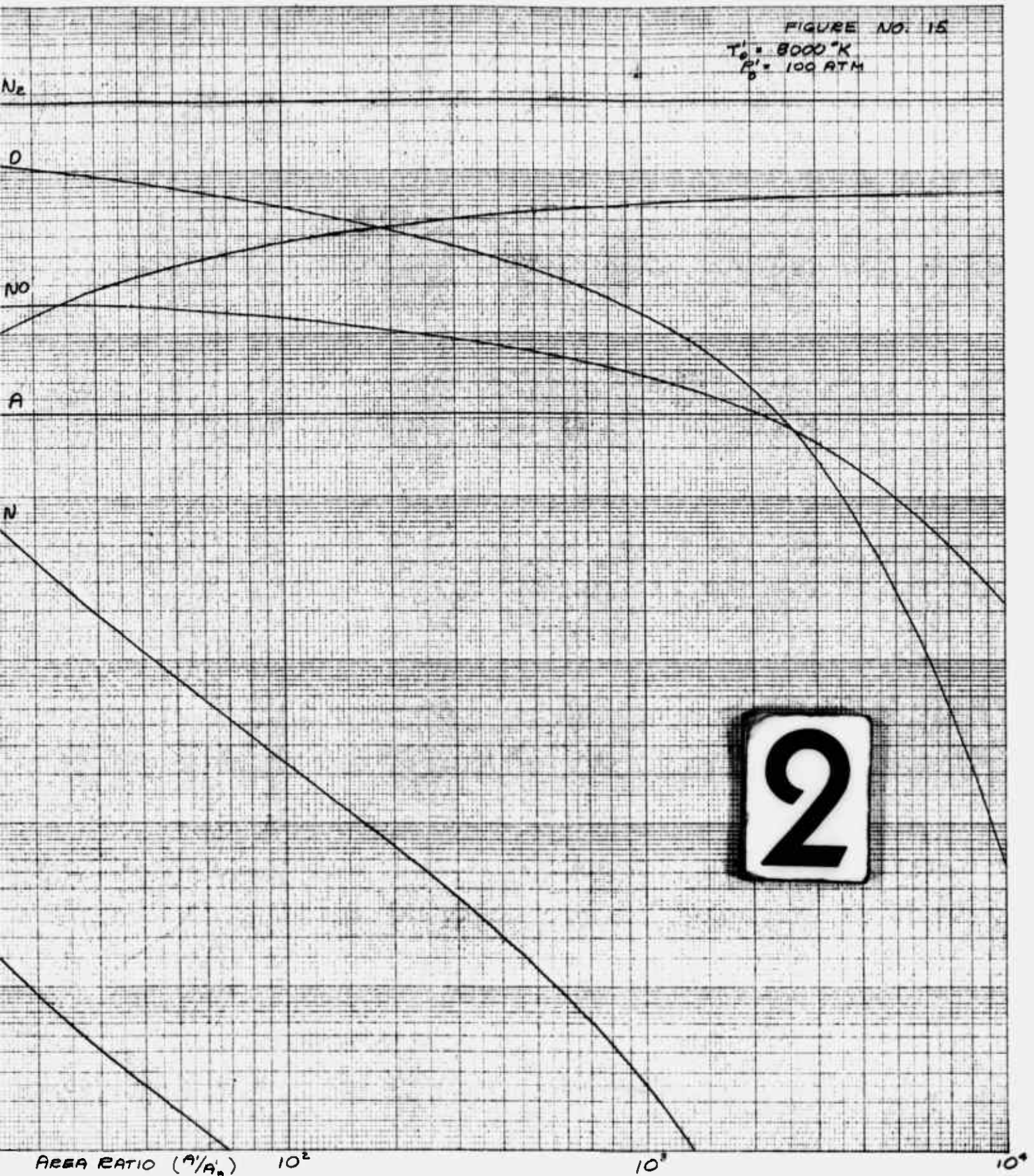


VS AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION

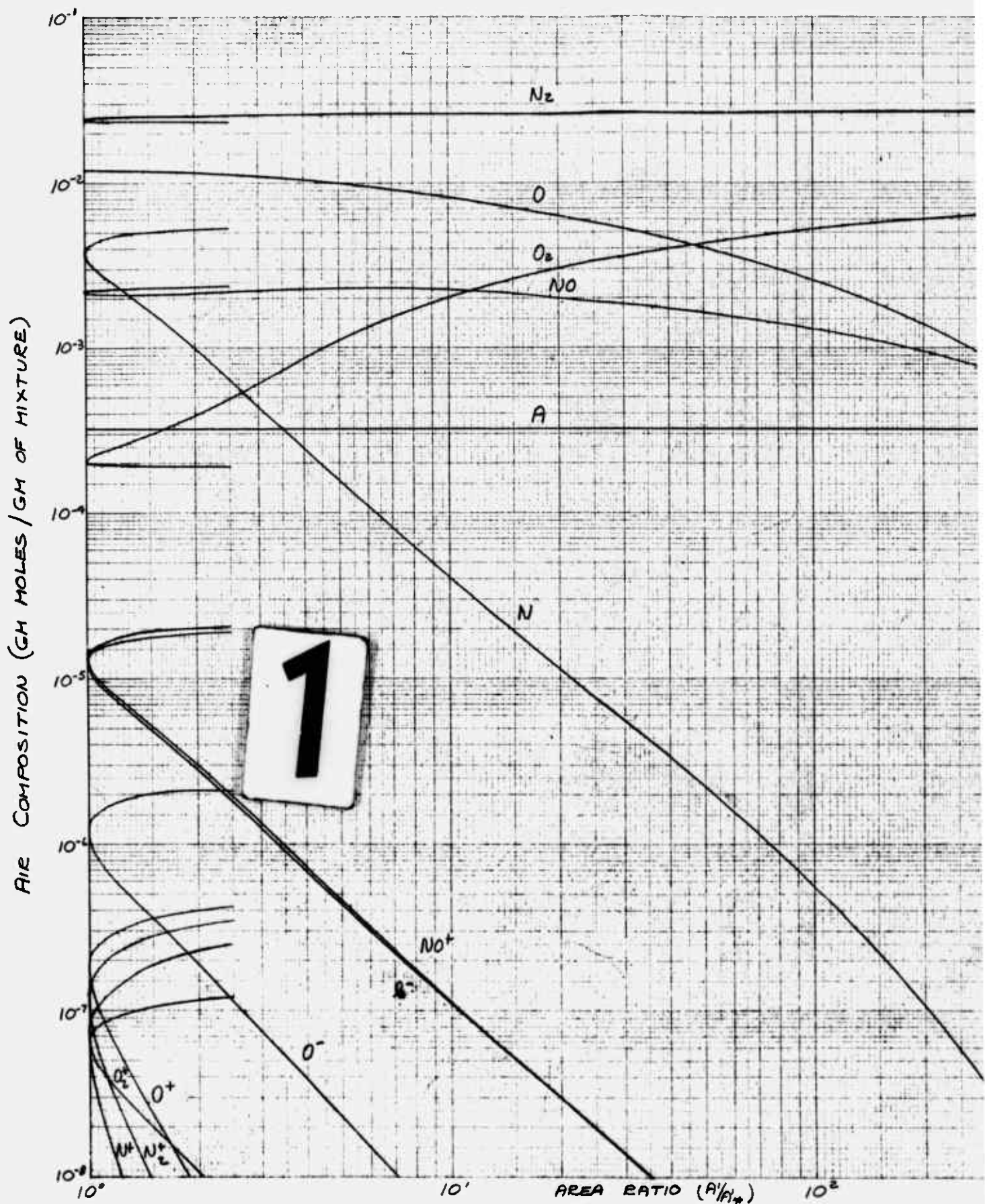


AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC FLOW

FIGURE NO. 15
 $T_0' = 8000^\circ\text{K}$
 $P_0' = 100\text{ ATM}$



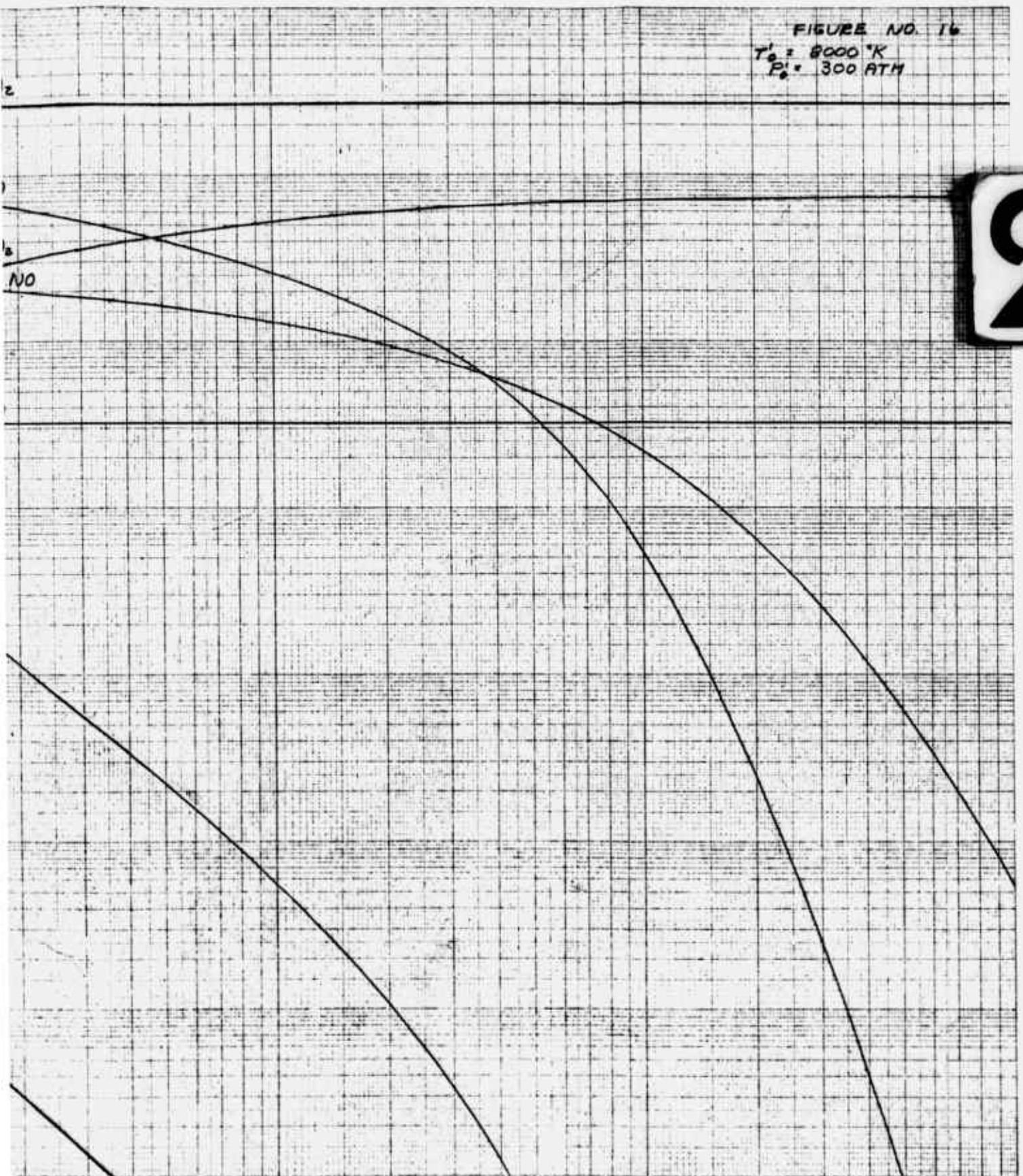
AREA RATIO (A/A_0) 10^2 10^3 10^4
VS AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION



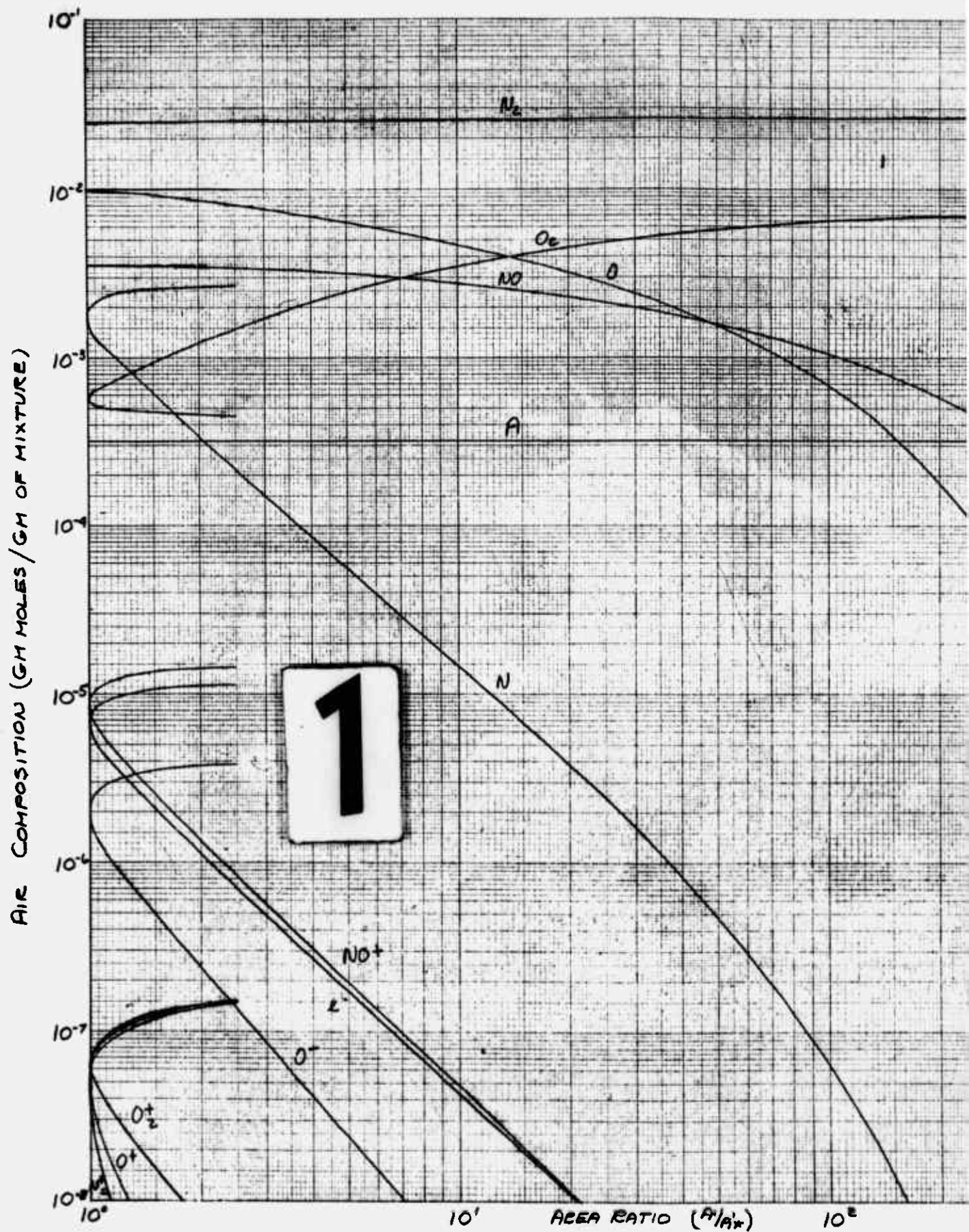
AIR COMPOSITION VS AREA RATIO IN AN ISENTROP

FIGURE NO. 16
 $T_0 = 8000^\circ K$
 $P_0 = 300 \text{ ATM}$

2

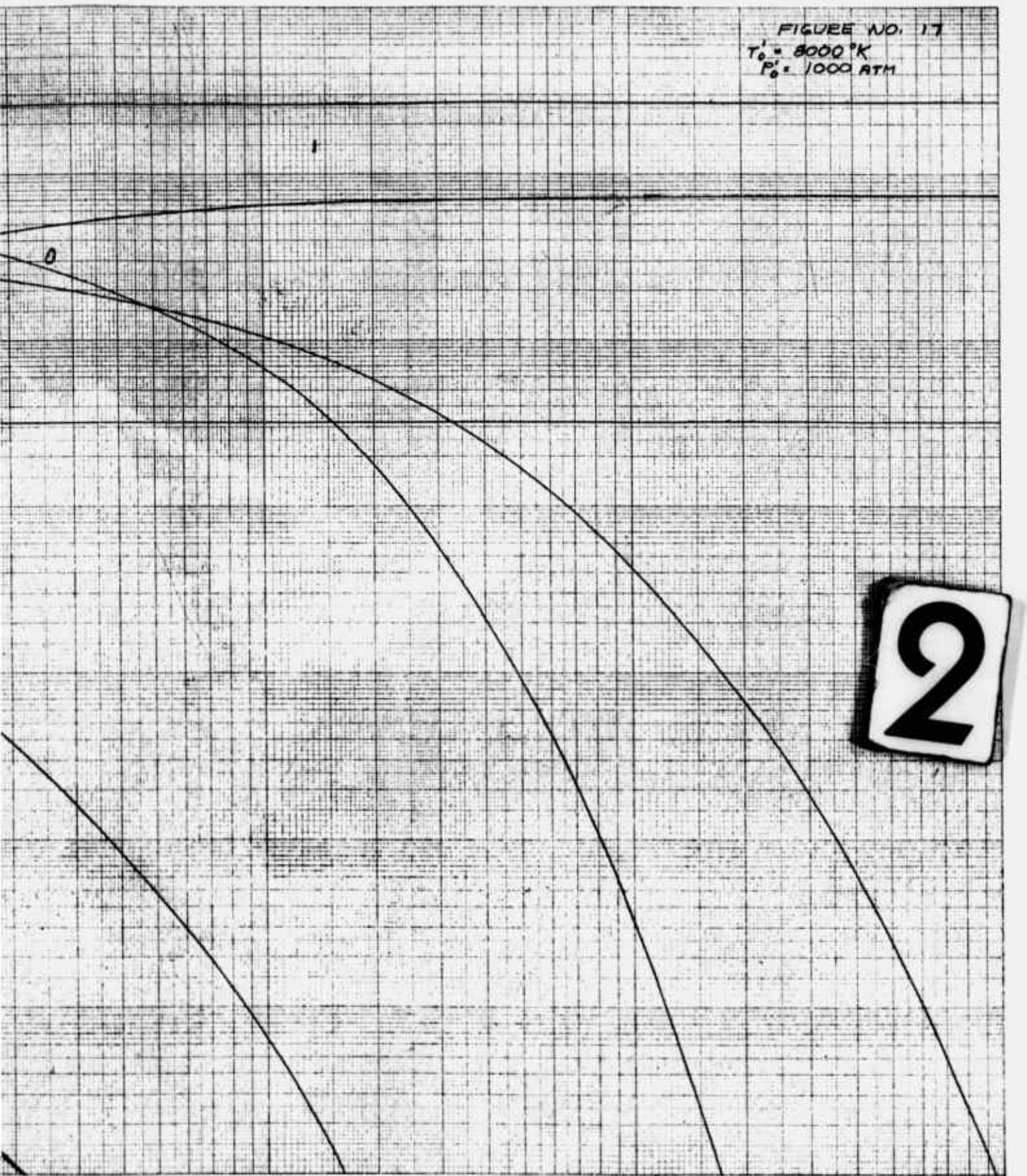


AREA RATIO (A/A^*) 10^2 10^3 10^4
VS AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION



AIR COMPOSITION VS AREA RATIO IN AN ISENTROPIC

FIGURE NO. 17
 $T_0 = 8000^\circ\text{K}$
 $P_0 = 1000\text{ ATM}$



AREA RATIO (A/A^*) 10^2 10^3 10^4
AREA RATIO IN AN ISENTROPIC EQUILIBRIUM EXPANSION

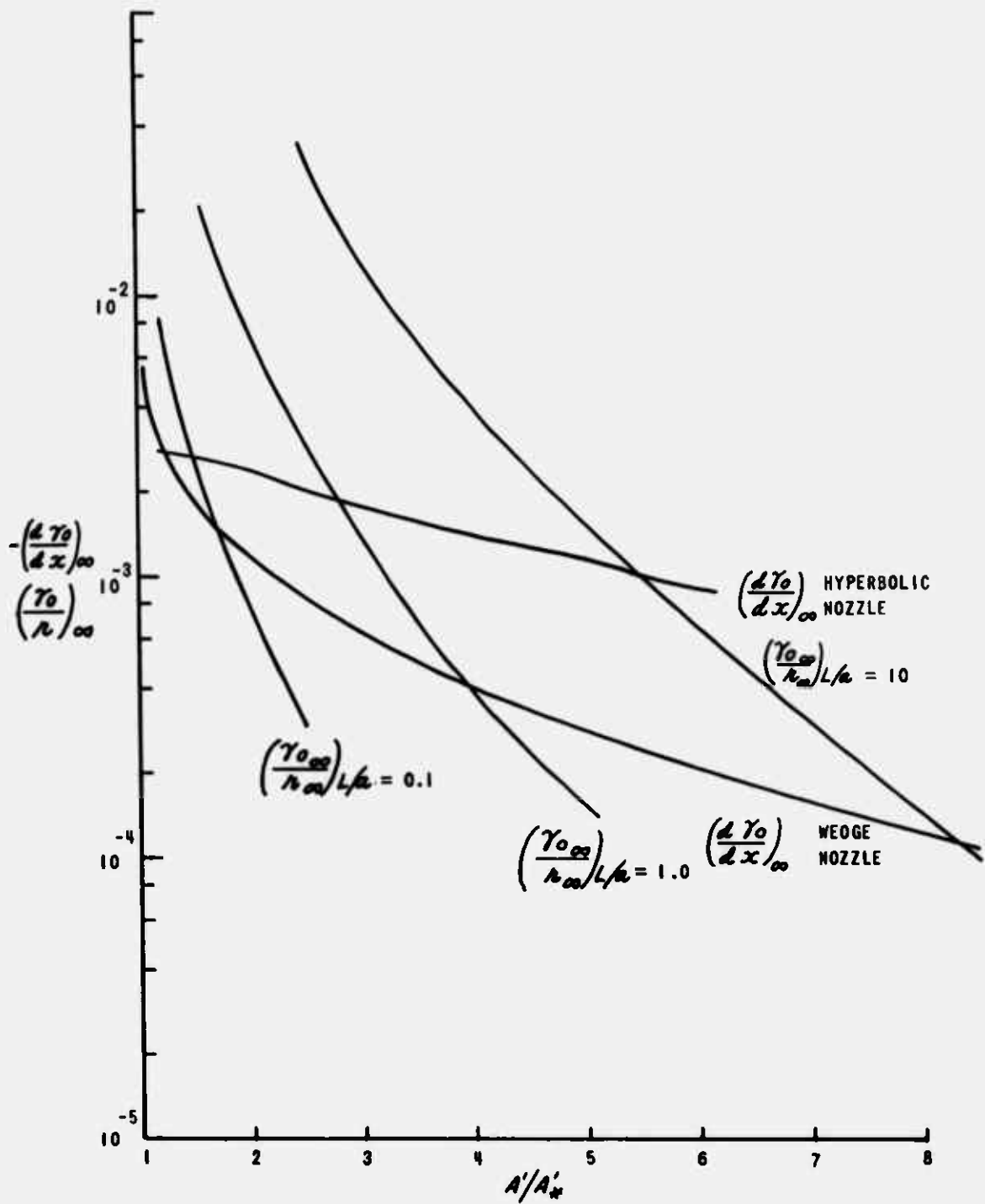


Figure 18 SAMPLE SOLUTION OF EQUATION (36) $T_0' = 5000^\circ \text{ K}$, $P_0' = 100 \text{ ATM}$.

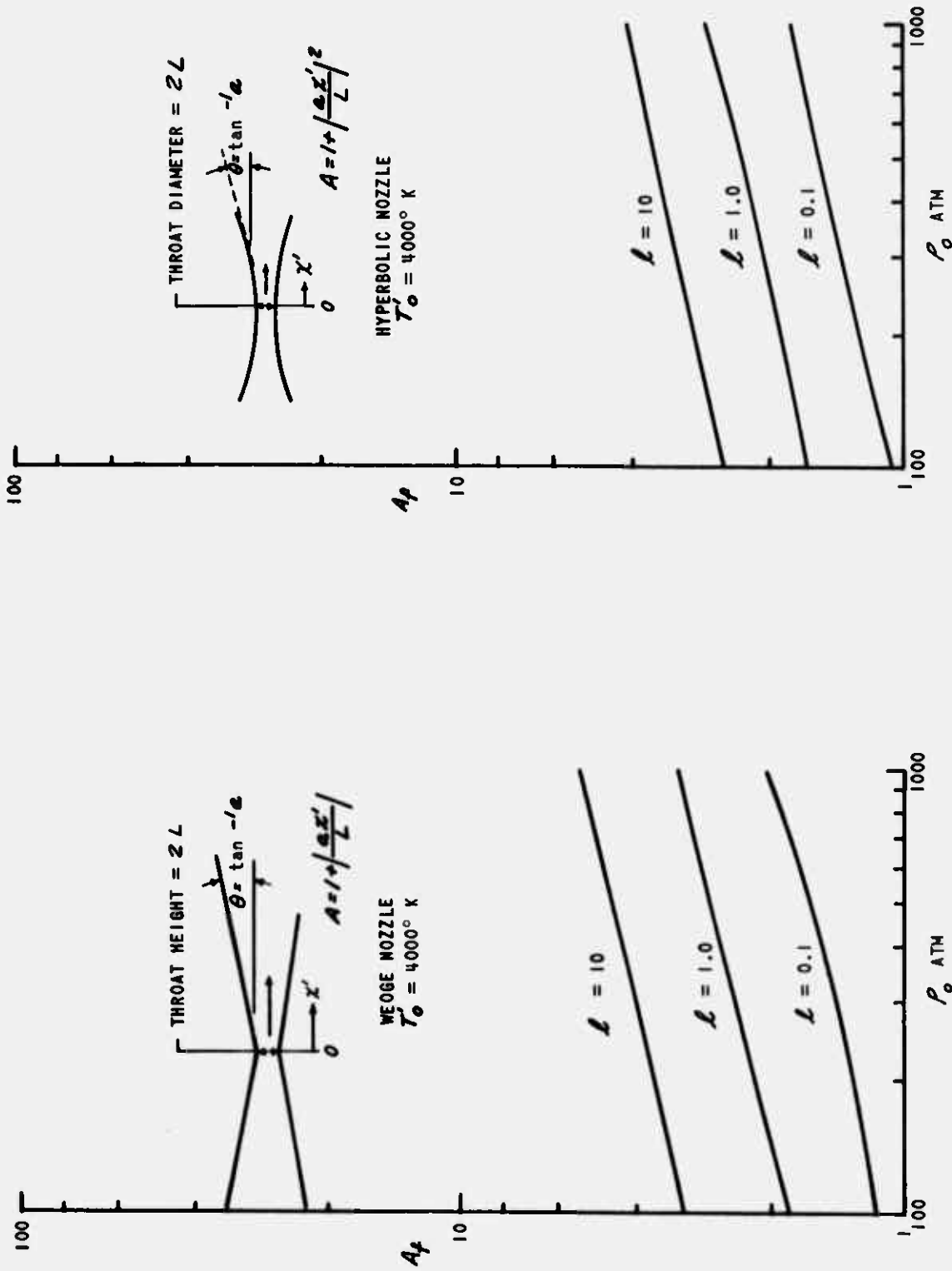


Figure 19 (a) EFFECT OF STAGNATION PRESSURE AND NOZZLE GEOMETRY ON THE AREA RATIO FOR FREEZING FOR A SIMPLIFIED AIR MODEL.

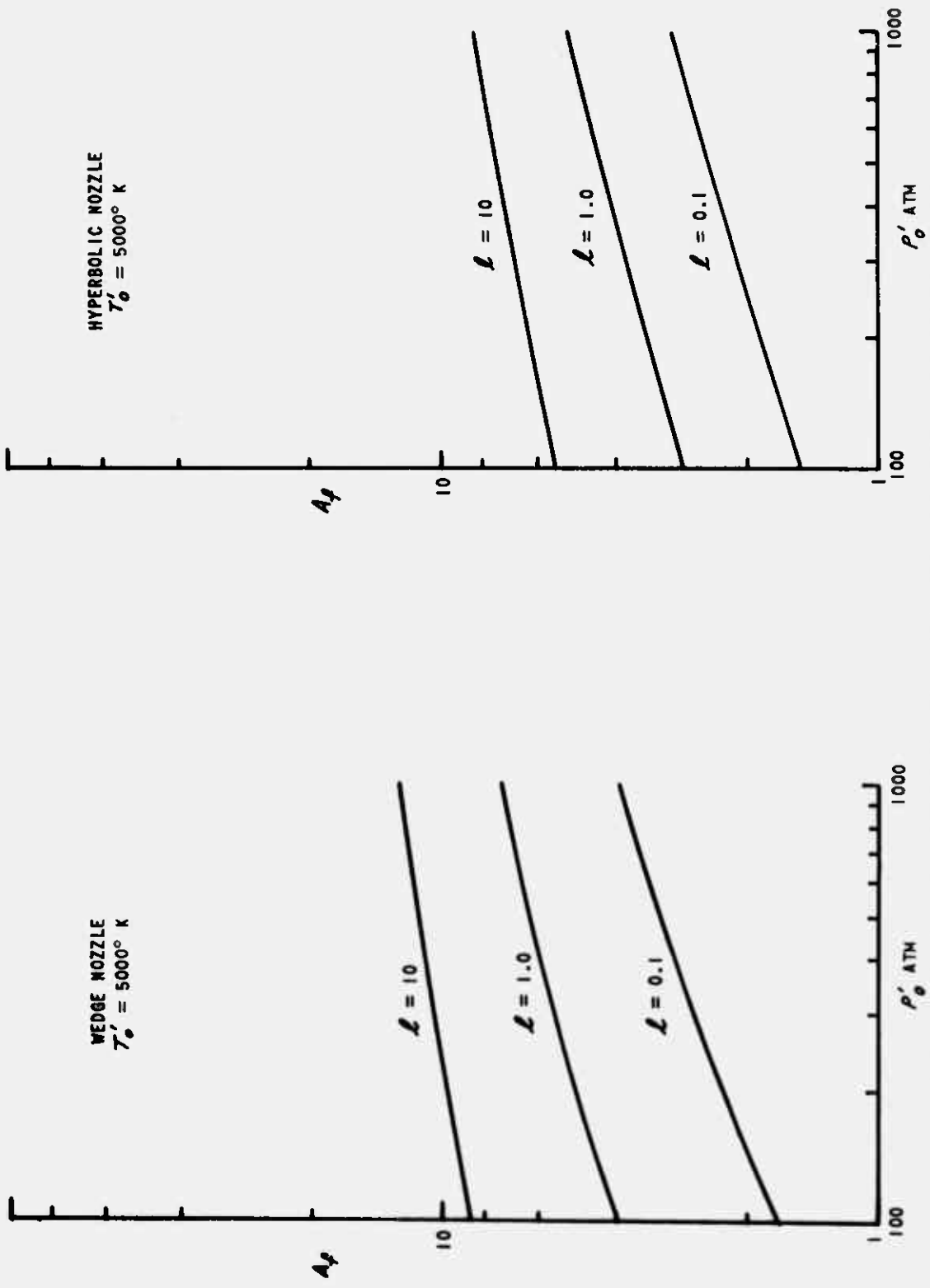


Figure 19 (b) EFFECT OF STAGNATION PRESSURE AND NOZZLE GEOMETRY ON THE AREA RATIO FOR FREEZING FOR A SIMPLIFIED AIR MODEL.

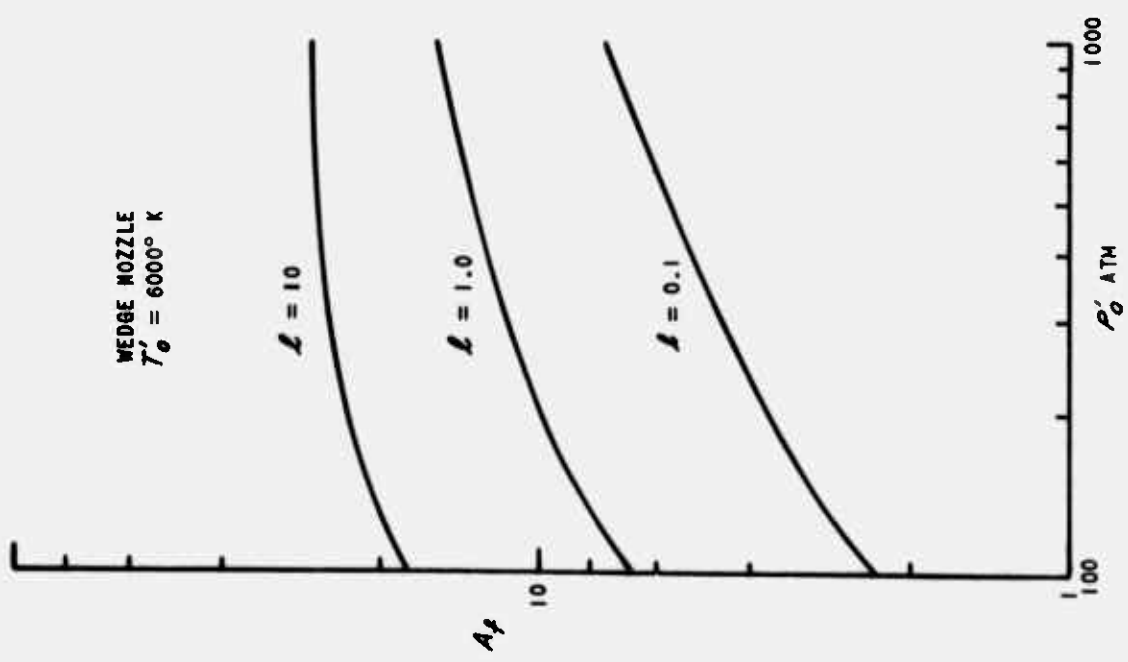
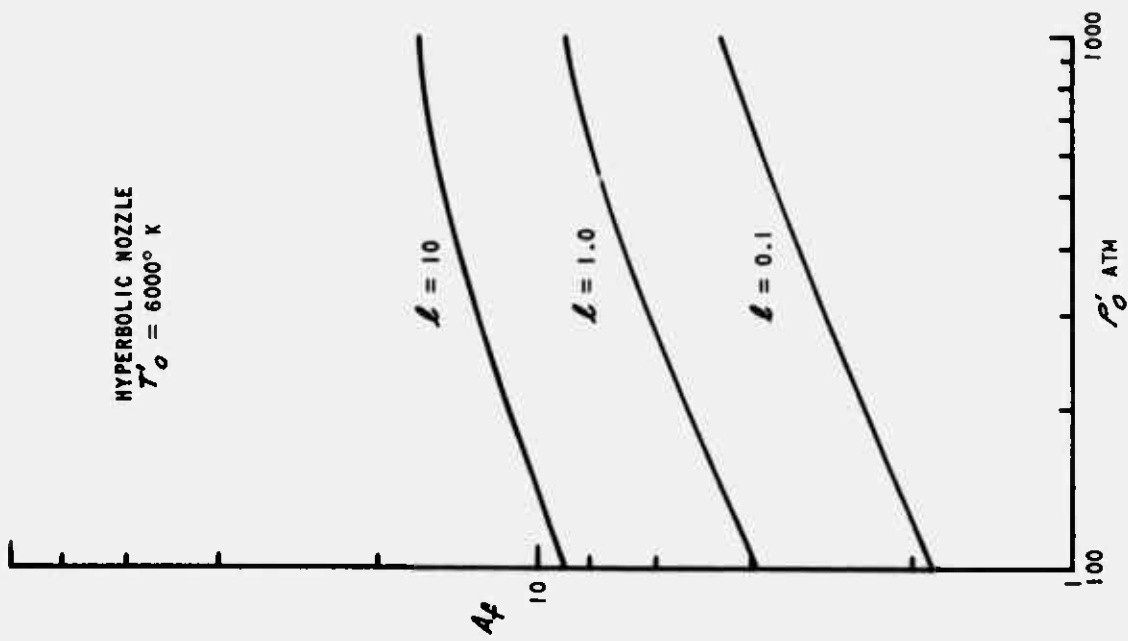


Figure 19 (c) EFFECT OF STAGNATION PRESSURE AND NOZZLE GEOMETRY ON THE AREA RATIO FOR FREEZING FOR A SIMPLIFIED AIR MODEL.

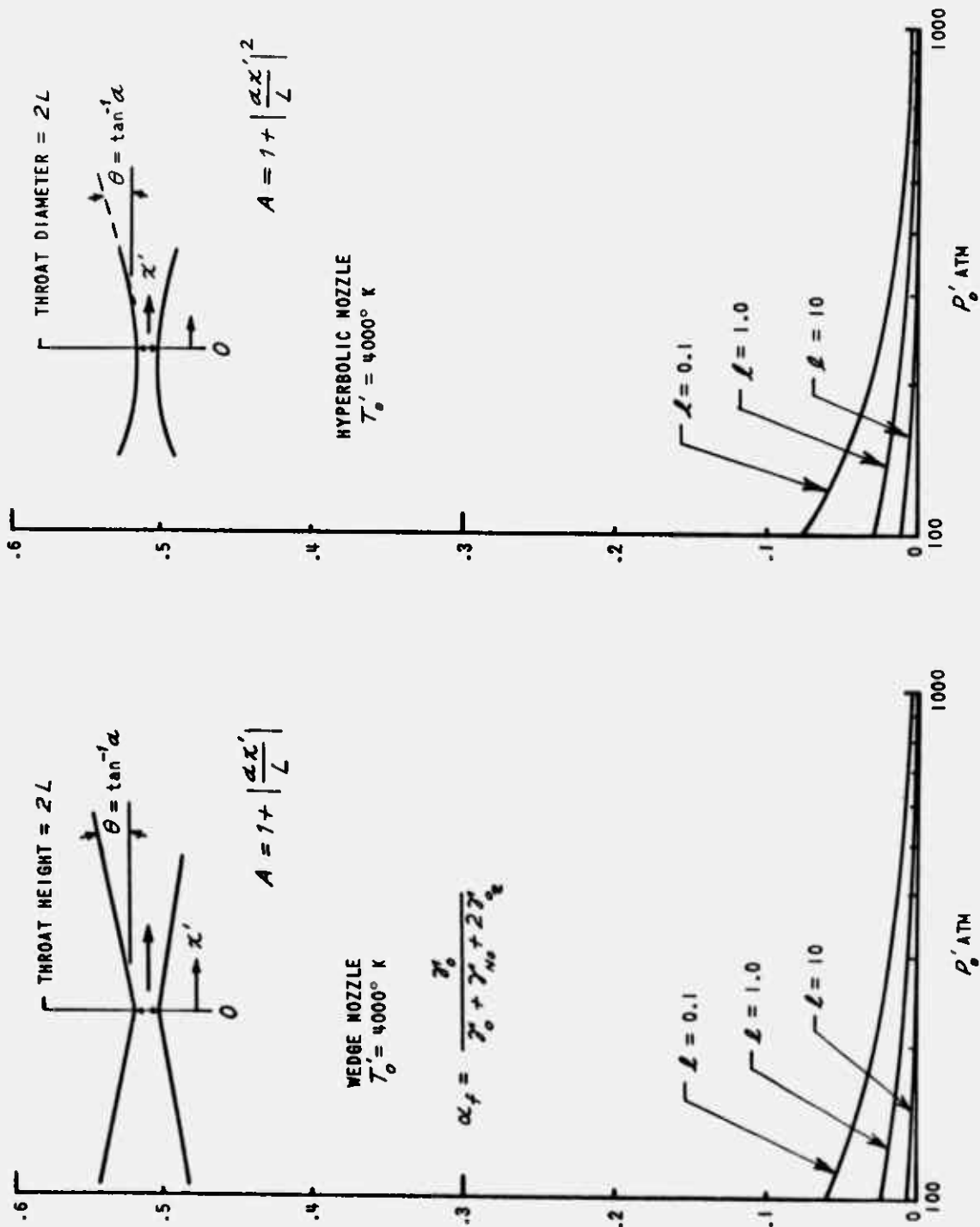


Figure 20 (a) EFFECT OF STAGNATION PRESSURE AND NOZZLE GEOMETRY ON THE FROZEN DEGREE OF OXYGEN DISSOCIATION FOR A SIMPLIFIED AIR MODEL.

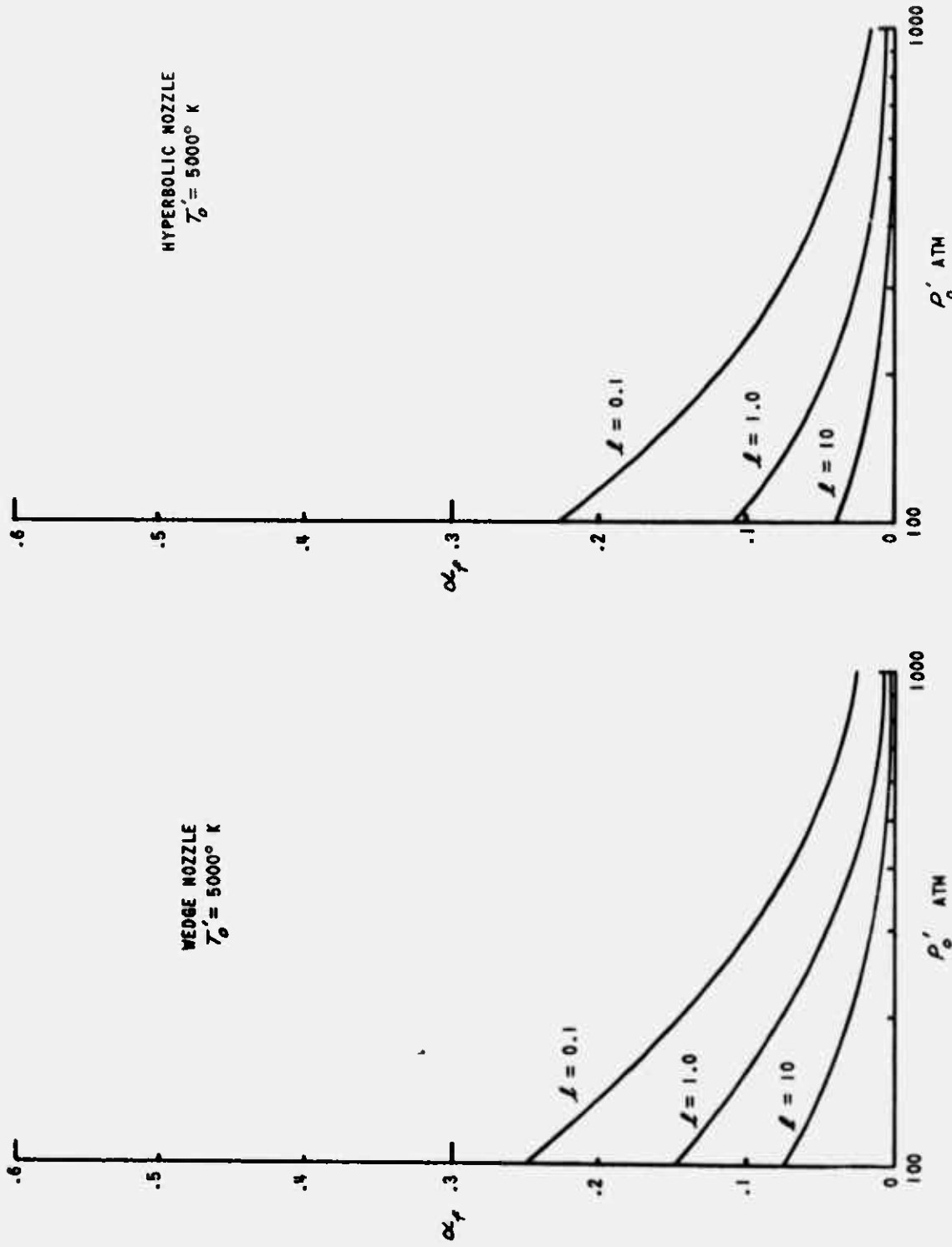


Figure 20 (b) EFFECT OF STAGNATION PRESSURE AND NOZZLE GEOMETRY ON THE FROZEN DEGREE OF OXYGEN DISSOCIATION FOR A SIMPLIFIED AIR MODEL.

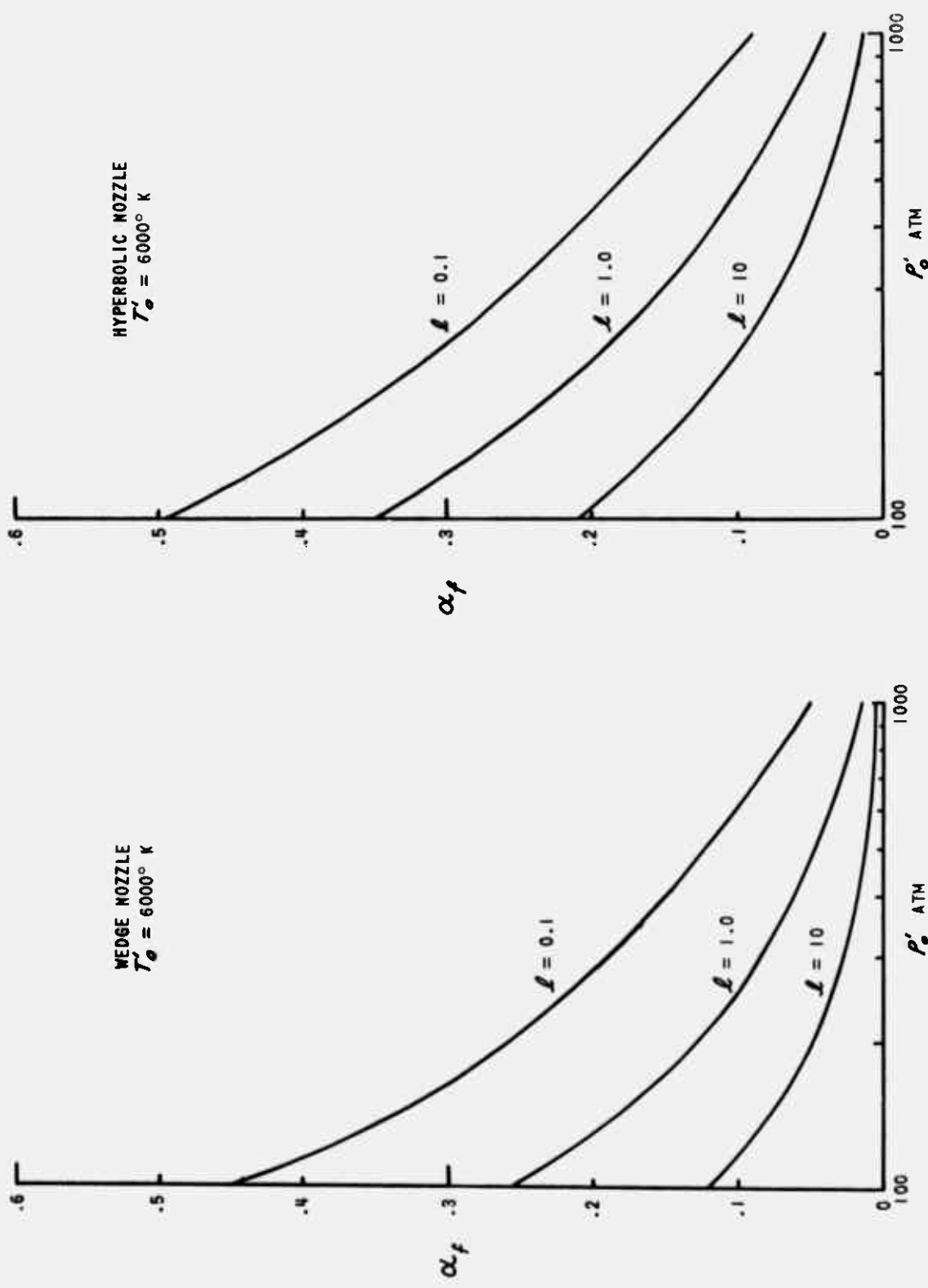


Figure 20 (c) EFFECT OF STAGNATION PRESSURE AND NOZZLE GEOMETRY ON THE FROZEN DEGREE OF OXYGEN DISSOCIATION FOR A SIMPLIFIED AIR MODEL.

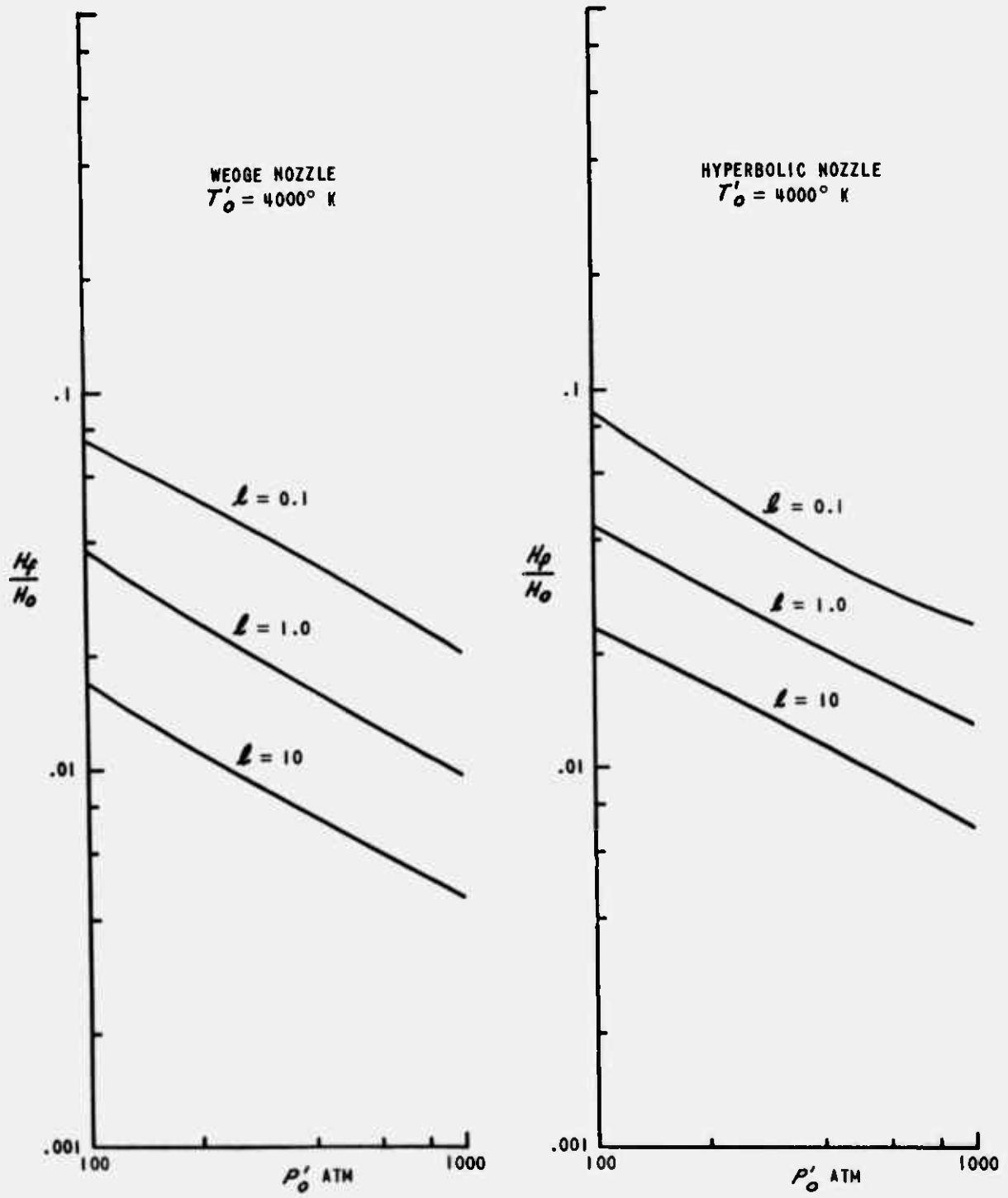


Figure 21 (a) EFFECT OF STAGNATION PRESSURE AND NOZZLE GEOMETRY ON THE FROZEN CHEMICAL ENERGY FOR A SIMPLIFIED AIR MODEL

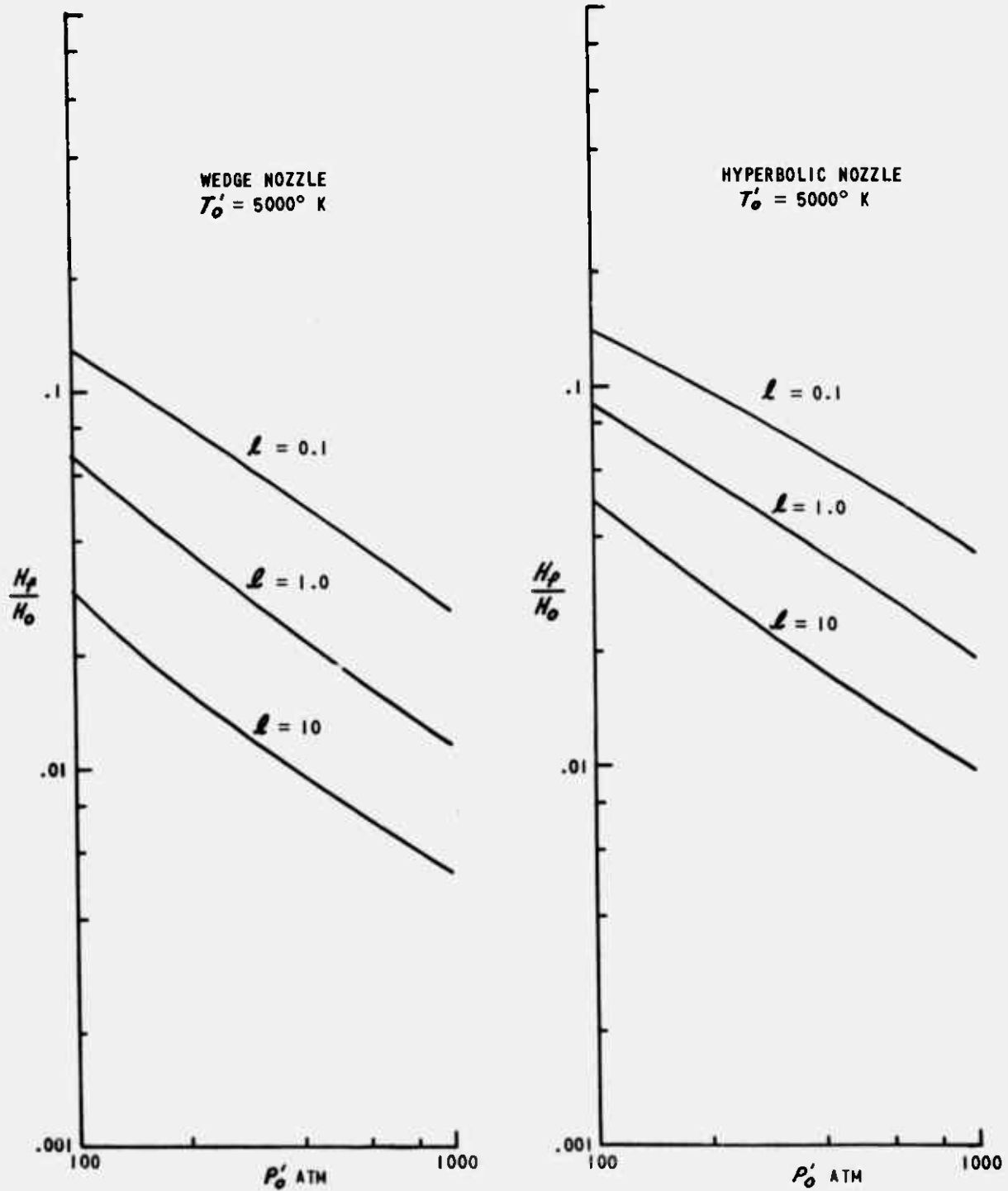


Figure 21 (b) EFFECT OF STAGNATION PRESSURE AND NOZZLE GEOMETRY ON THE FROZEN CHEMICAL ENERGY FOR A SIMPLIFIED AIR MODEL

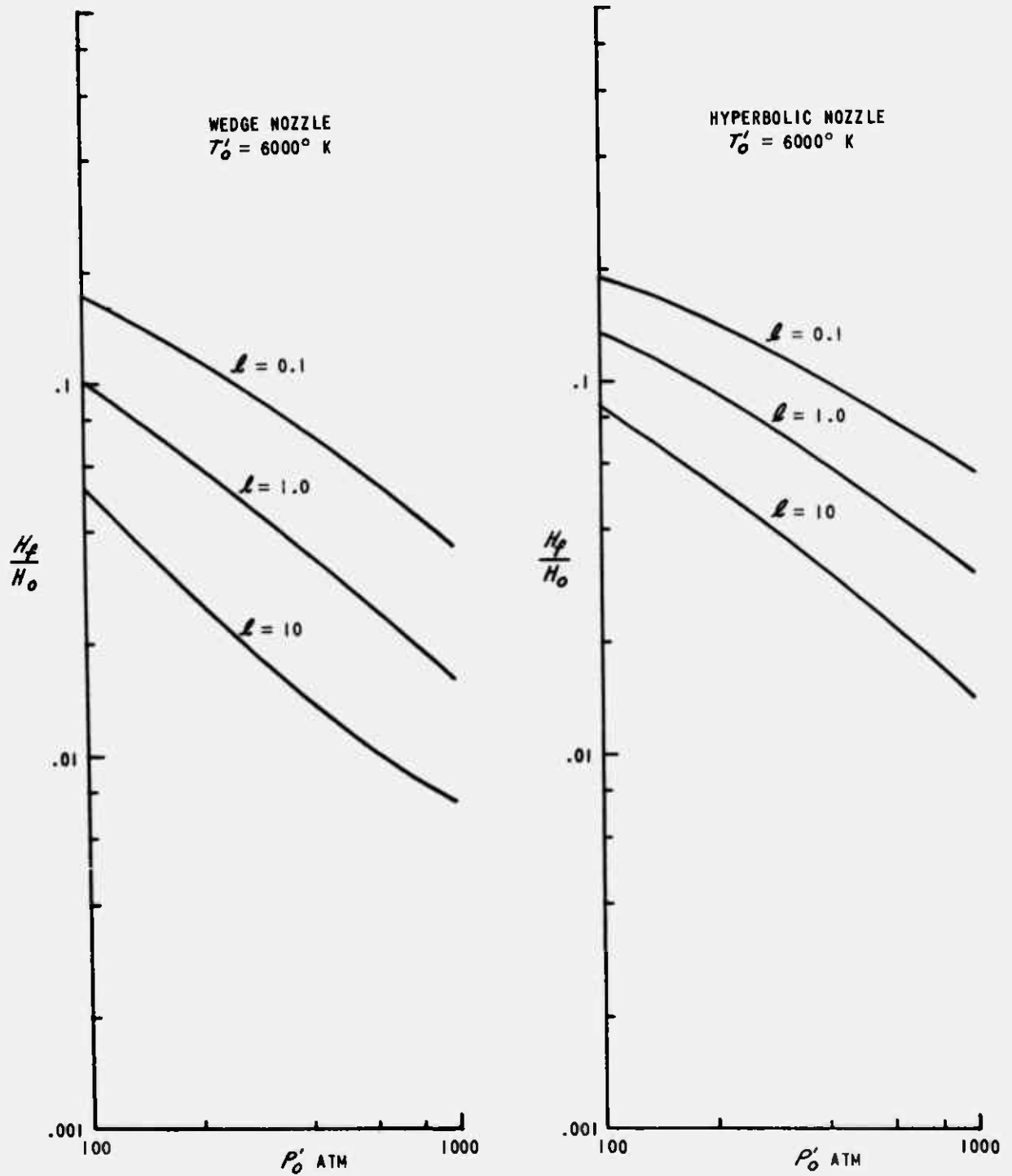


Figure 21 (c) EFFECT OF STAGNATION PRESSURE AND NOZZLE GEOMETRY ON THE FROZEN CHEMICAL ENERGY FOR A SIMPLIFIED AIR MODEL

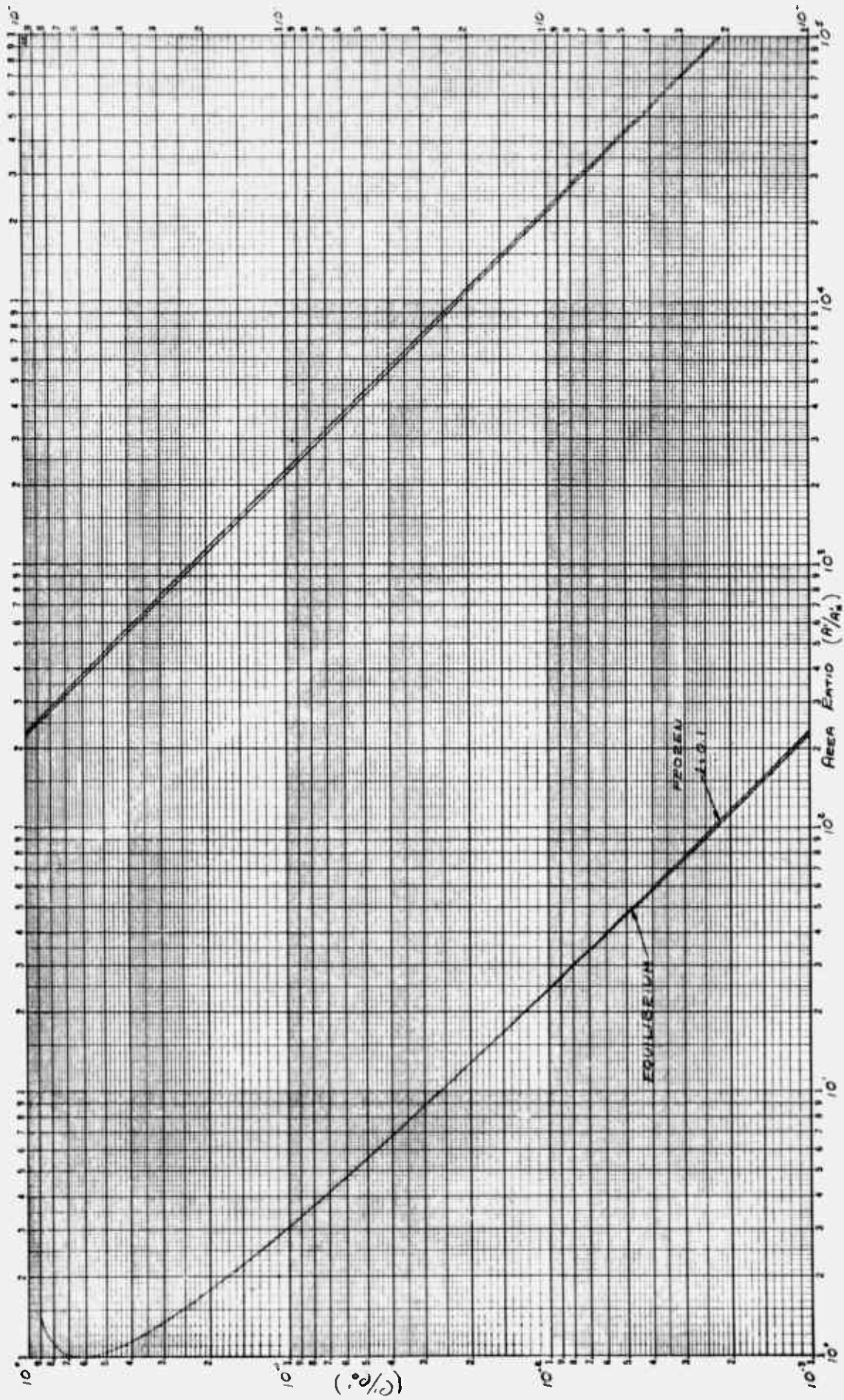


FIGURE NO 33.2 HYPERBOLIC NOZZLE $T_0 = 4000^\circ K$ $P_0 = 100 \text{ ATM}$

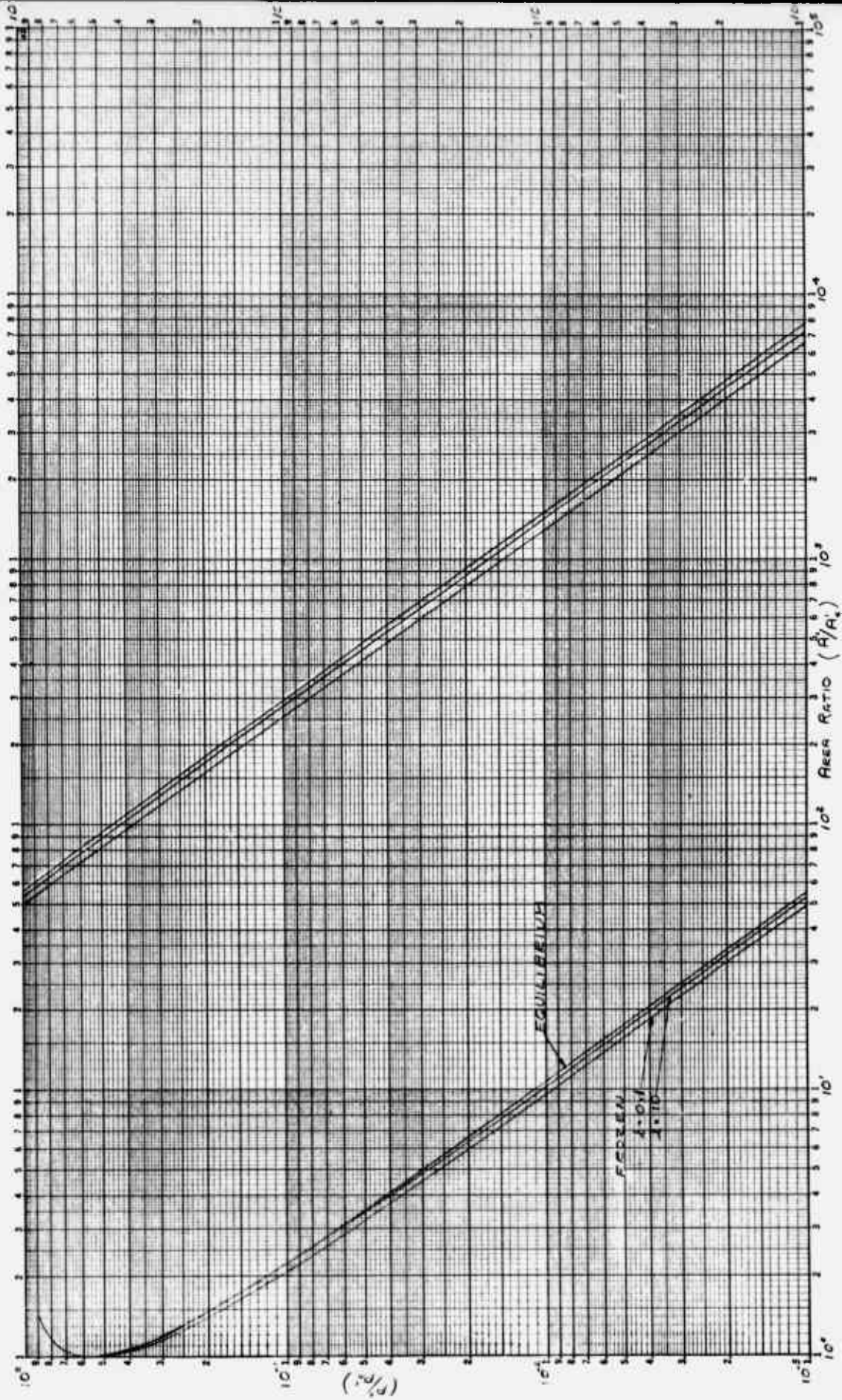


FIGURE NO. 22.6 HYPERBOLIC NOZZLE $T_0' = 4000^\circ K$ $P_0' = 100 \text{ A-M}$

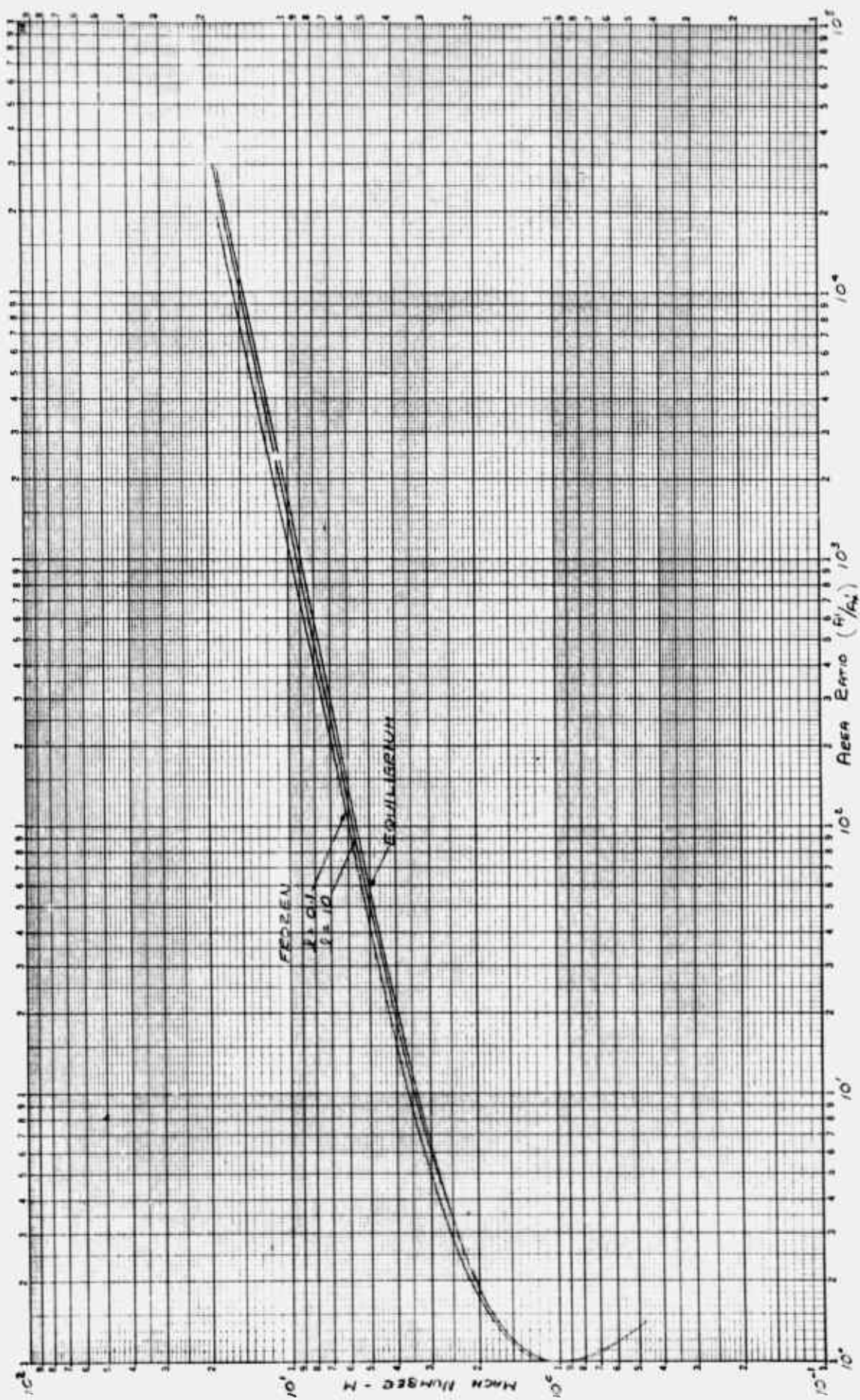


FIGURE 100 IS: HYPERBOLIC NOZZLE $T_0 = 4000^\circ K$ $P_0 = 100 \text{ ATM}$

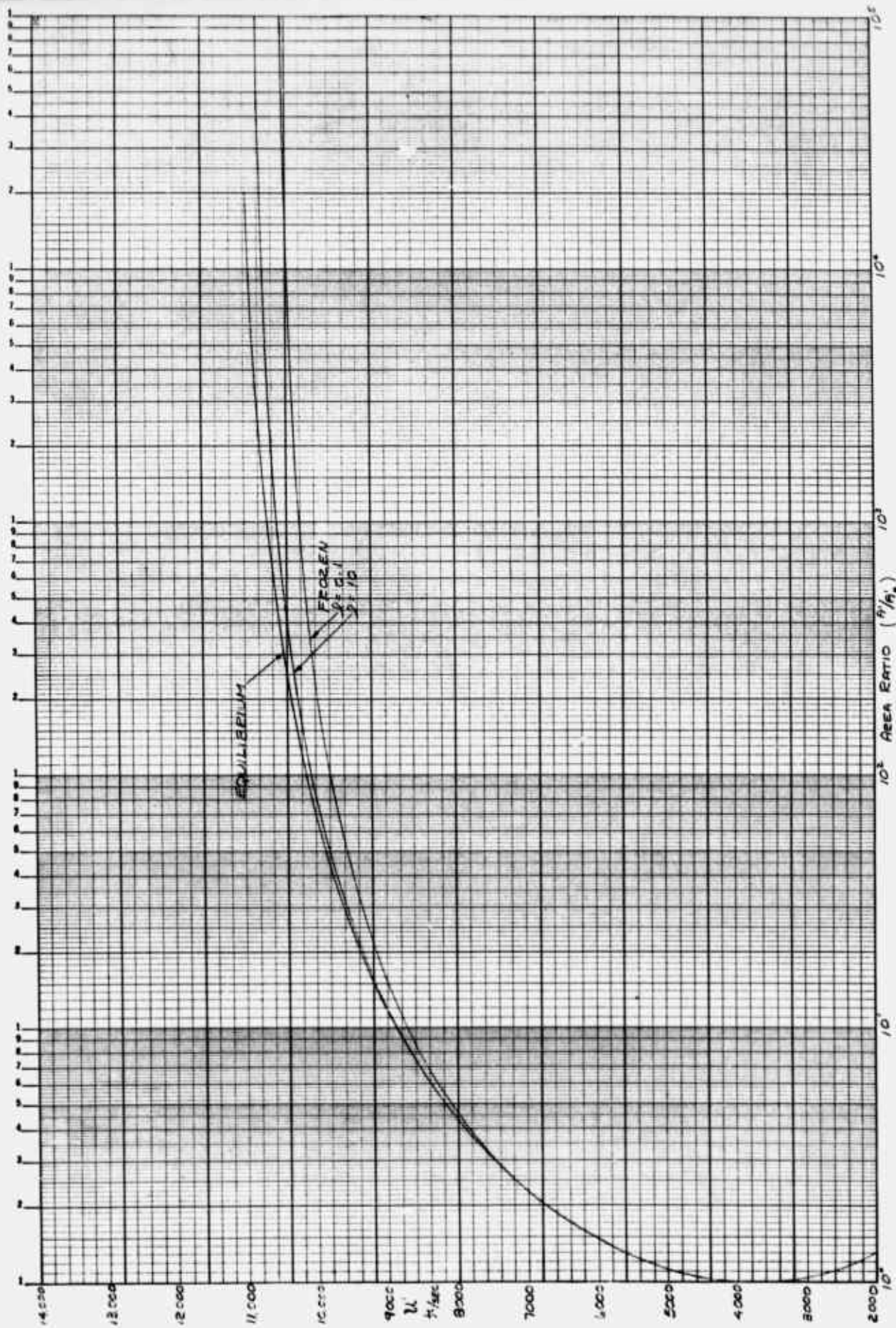


FIGURE NO. 22.3 HYPERSOLIC NOZZLE $T_0 = 4000^\circ K$ $\gamma_0 = 1.0017 M$

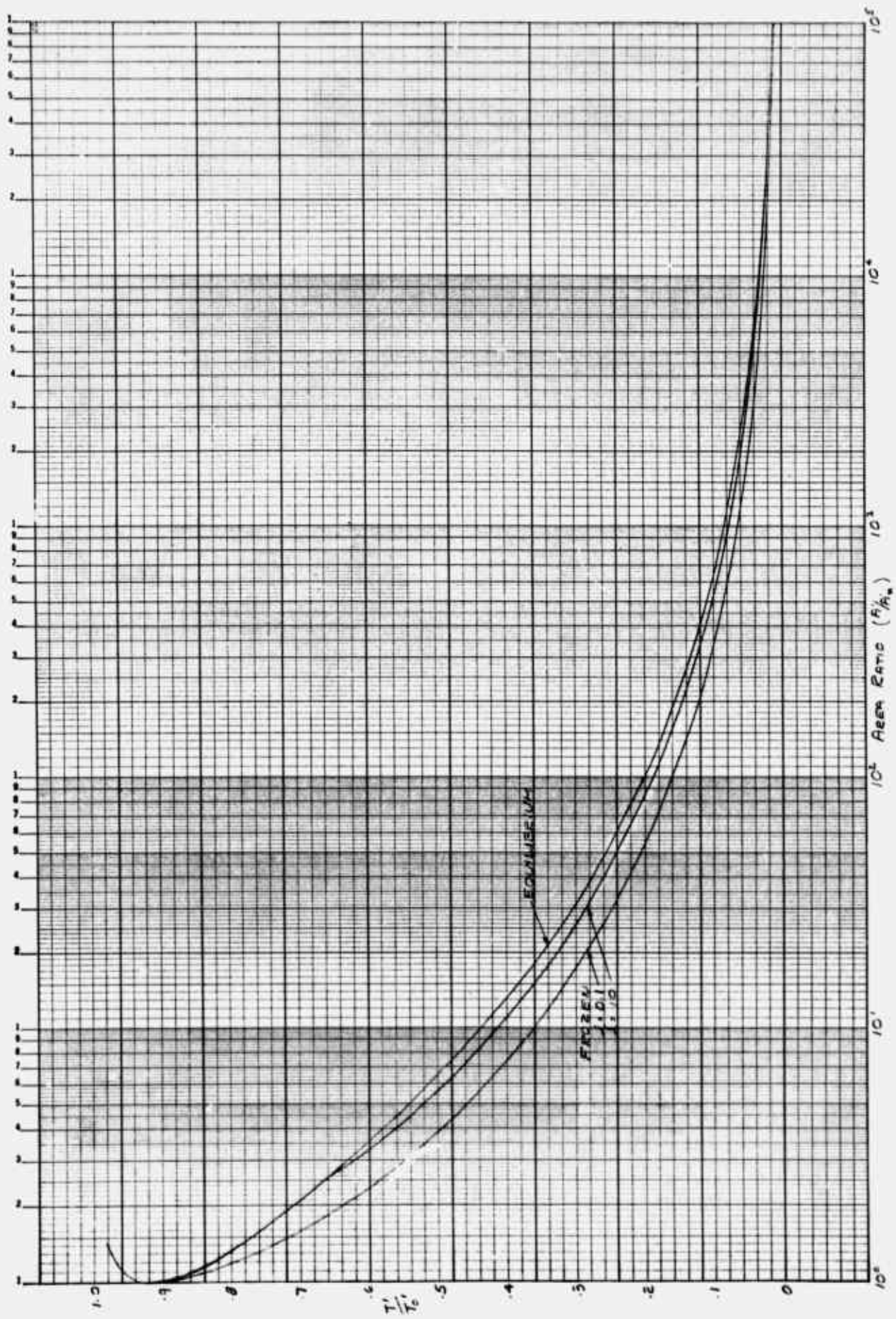


FIGURE NO. 22c HYPERBOLIC NOZZLE $T_0 = 4000^\circ K$ $P_0 = 100$ ATM

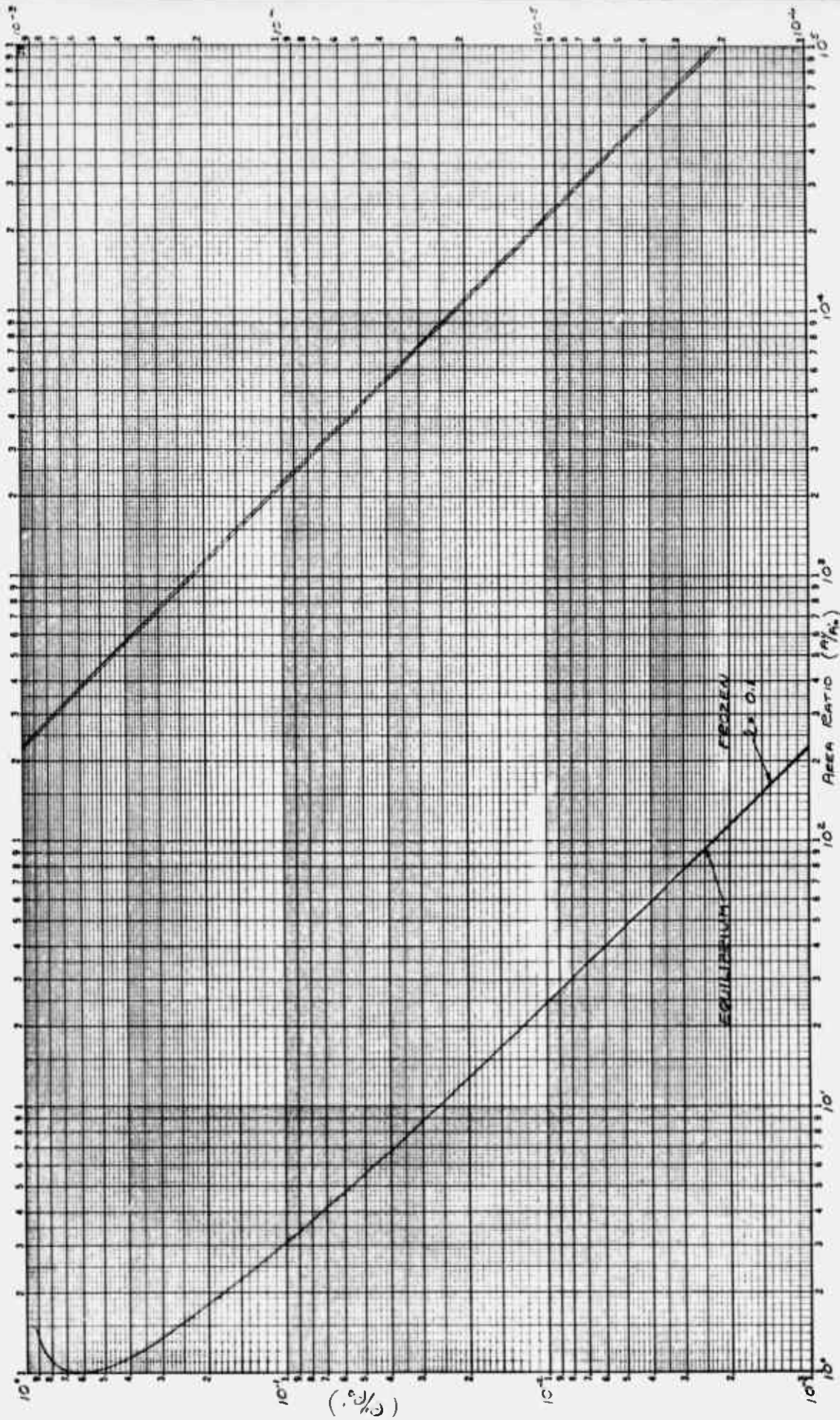


FIGURE NO 29a HYPERBOLIC NOZZLE $T_0 = 4000^\circ K$ $P_0 = 300 \text{ ATM}$

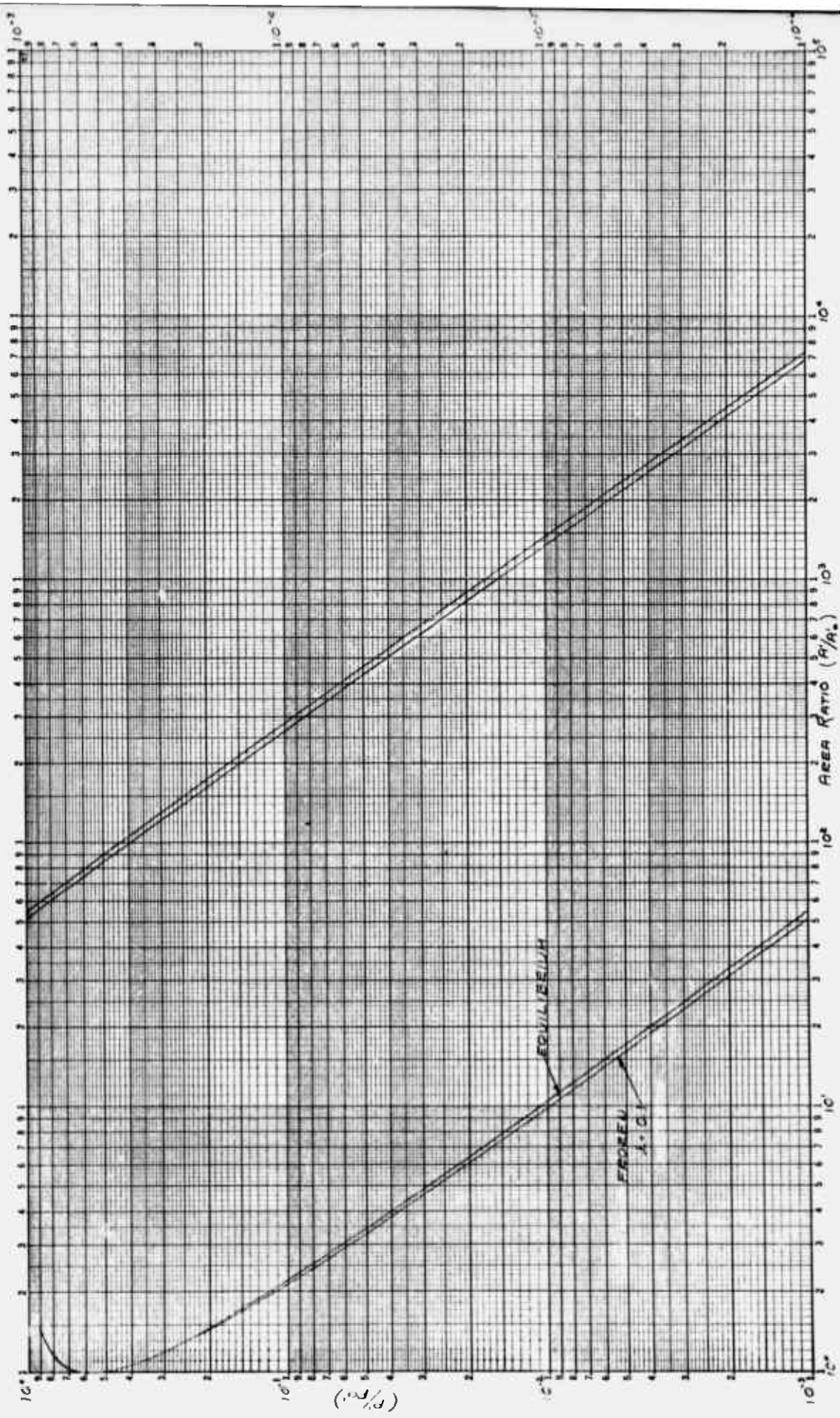


FIGURE NO. 23b HYPERBOLIC NOZZLE $T_0 = 4000^\circ K$ $P_0 = 300$ ATM

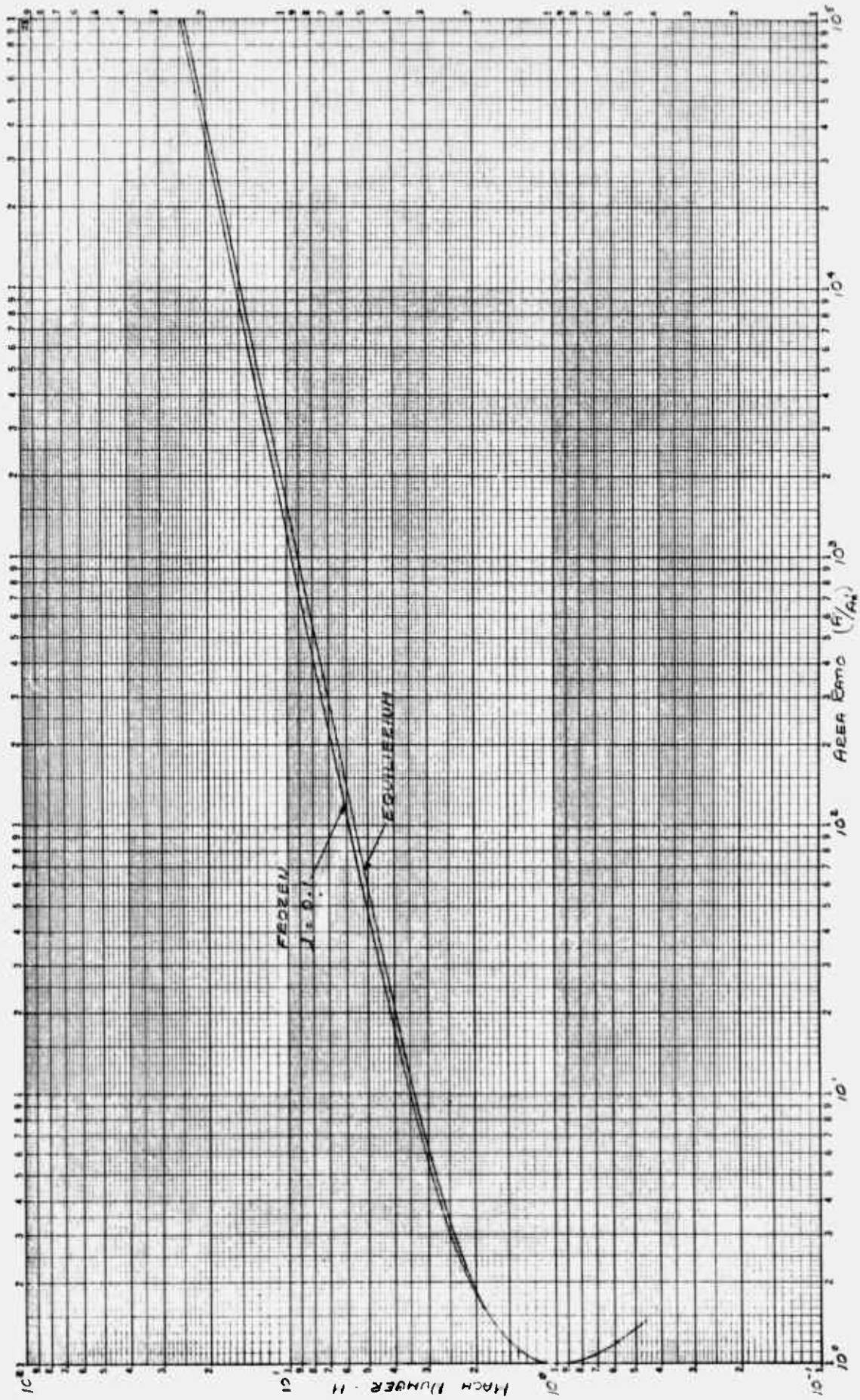


FIGURE 10. 250 HYPERBOLIC NOZZLE T₀ = 4000°K P₀' = 300 ATM

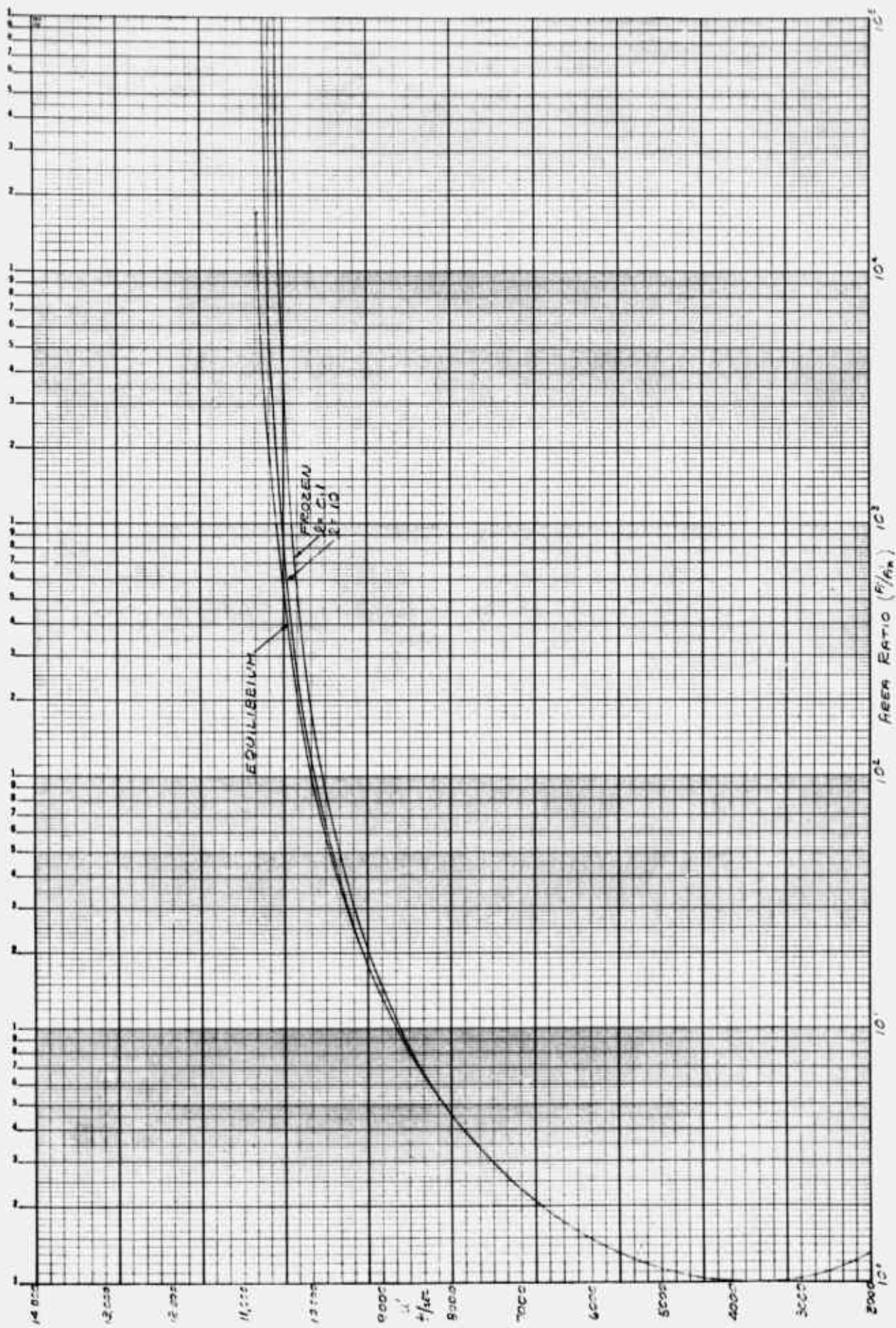


FIGURE NO. 23J COMPRESSION NOZZLE $T_0 = 4000^\circ\text{K}$ $P_0 = 300 \text{ ATM}$

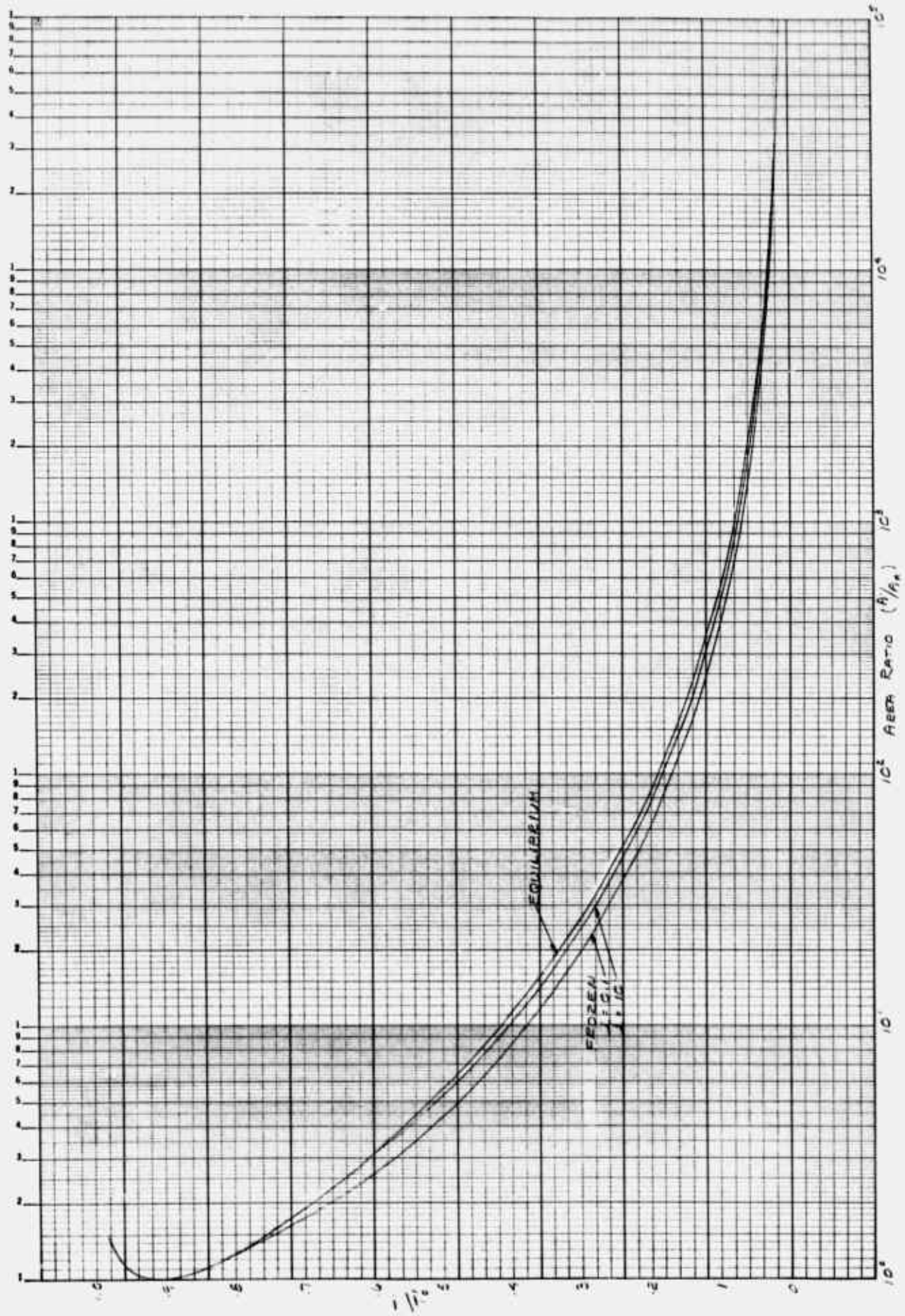


FIGURE NO. 23e HYPERBOLIC NOZZLE $T_0 = 4000^\circ K$ $P_0 = 300$ ATM

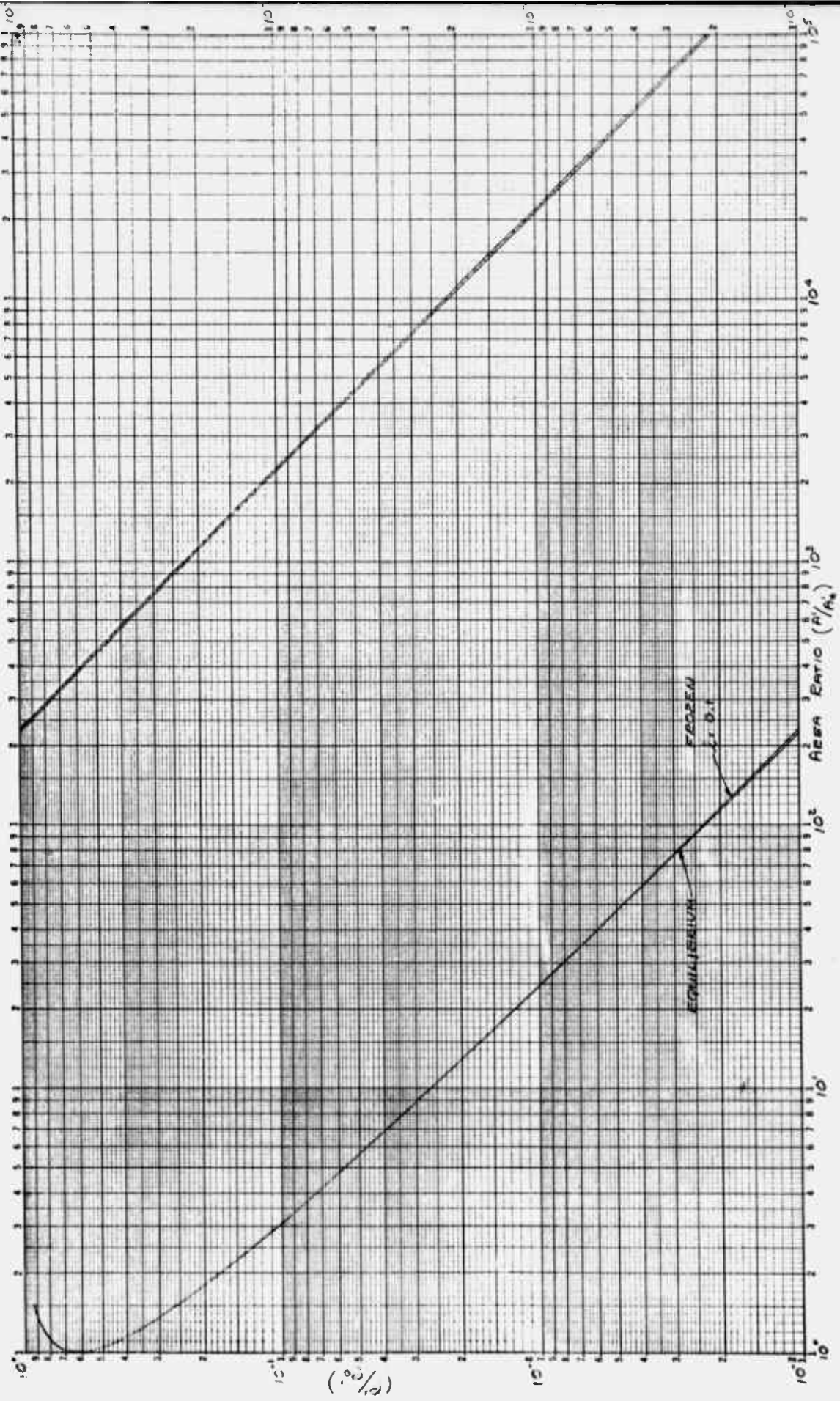


FIGURE NO. 24.2. HYPERBOLIC NOZZLE $T_0' = 4000^\circ K$ $P_0' = 1000$ ATM

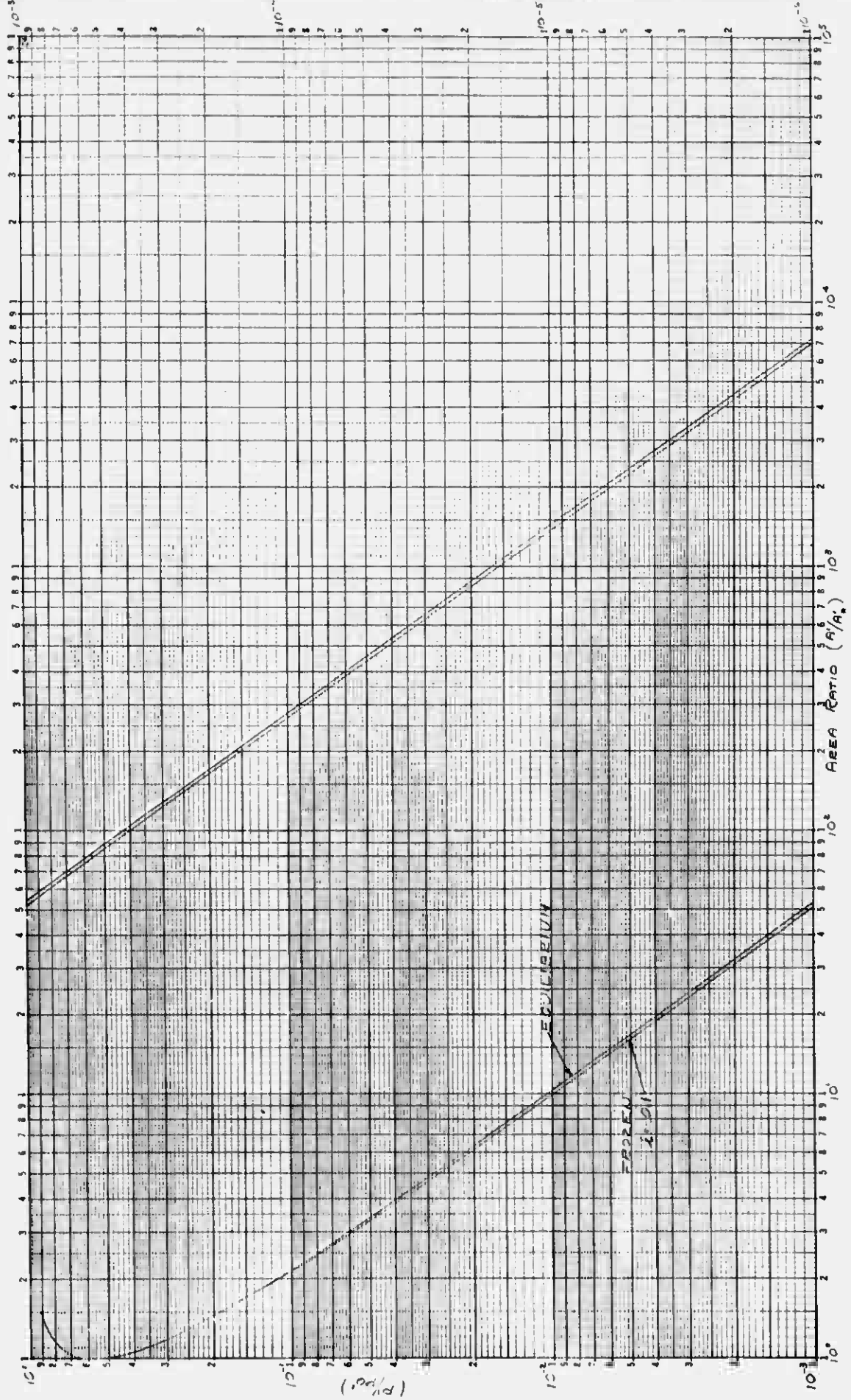


FIGURE NO. 246 HYPERBOLIC NOZZLE $T_0 = 4000^\circ K$ $P_0 = 1000$ ATM

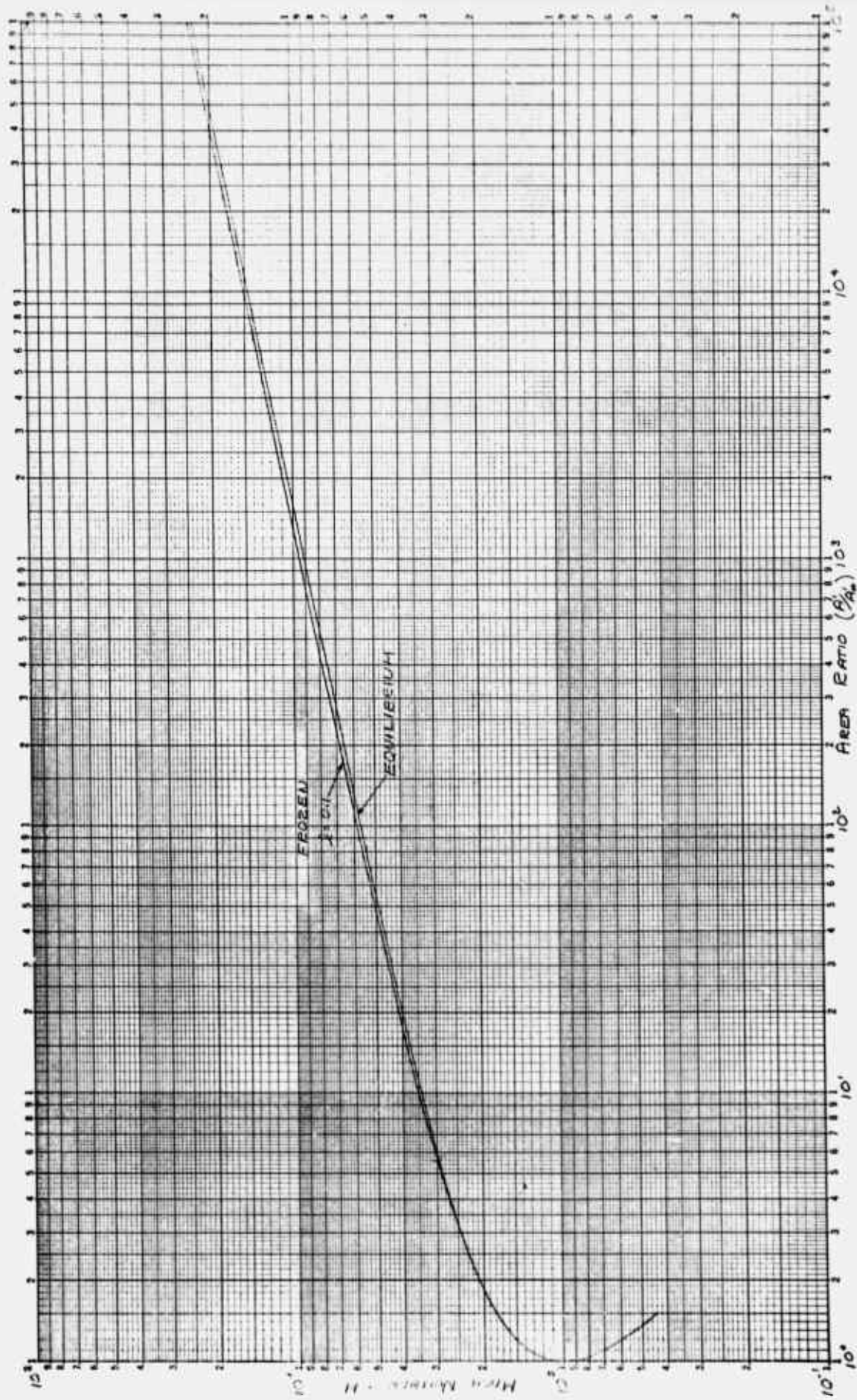


FIGURE NO 24c HYPERBOLIC NOZZLE $T_0 = 4000^\circ\text{K}$ $P_0 = 1000 \text{ ATM}$

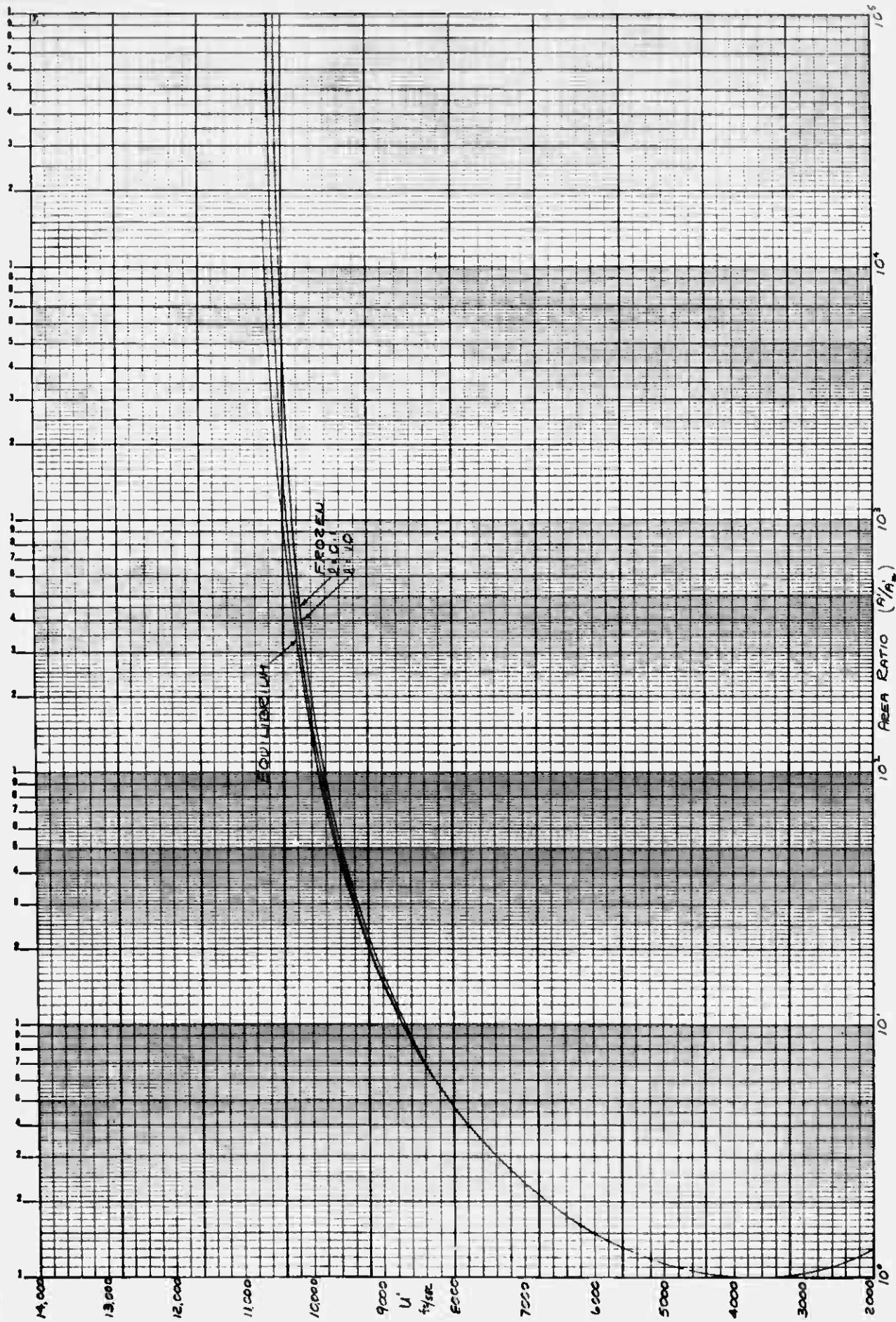


FIGURE NO. 24d HYPERBOLIC NOZZLE $T_0' = 4000^\circ K$ $P_0' = 1000 \text{ ATM}$

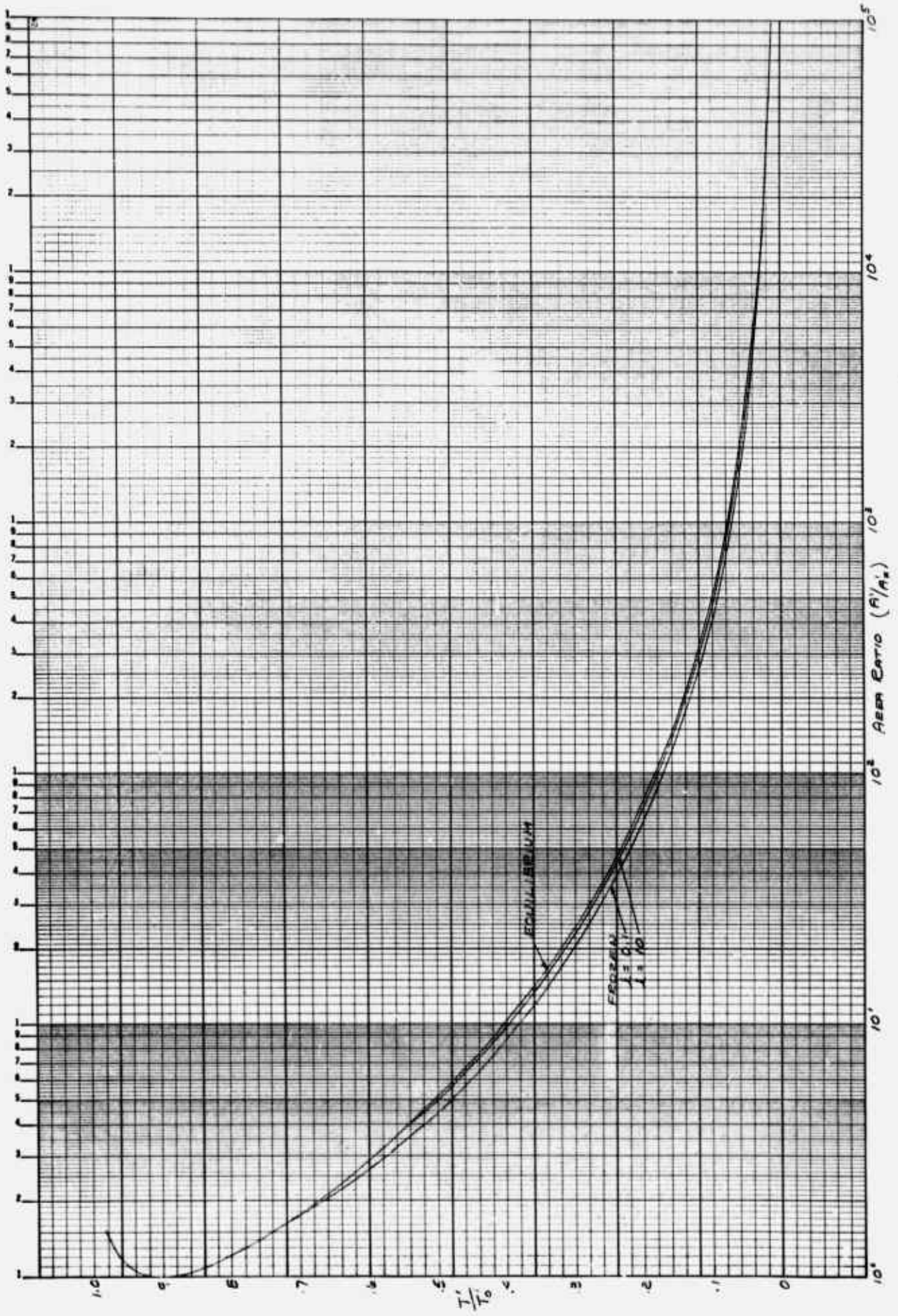


FIGURE NO. 24c HYPERSONIC NOZZLE $T_0' = 4000^\circ\text{K}$ $P_0' = 1000 \text{ ATM}$

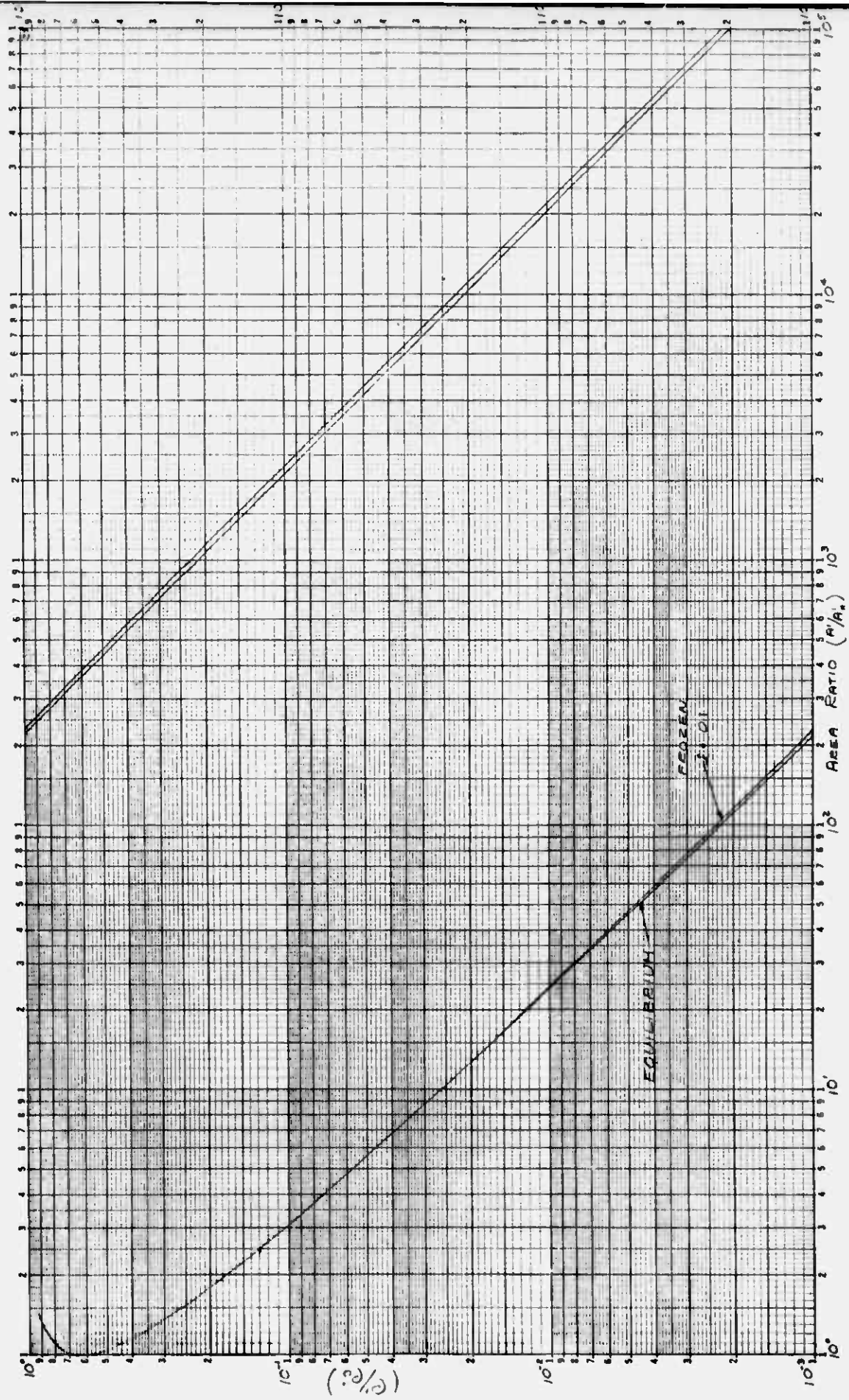


FIGURE NO. 25. HYPERBOLIC NOZZLE $T_0 = 5000^\circ K$ $P_0 = 100 \text{ ATM}$

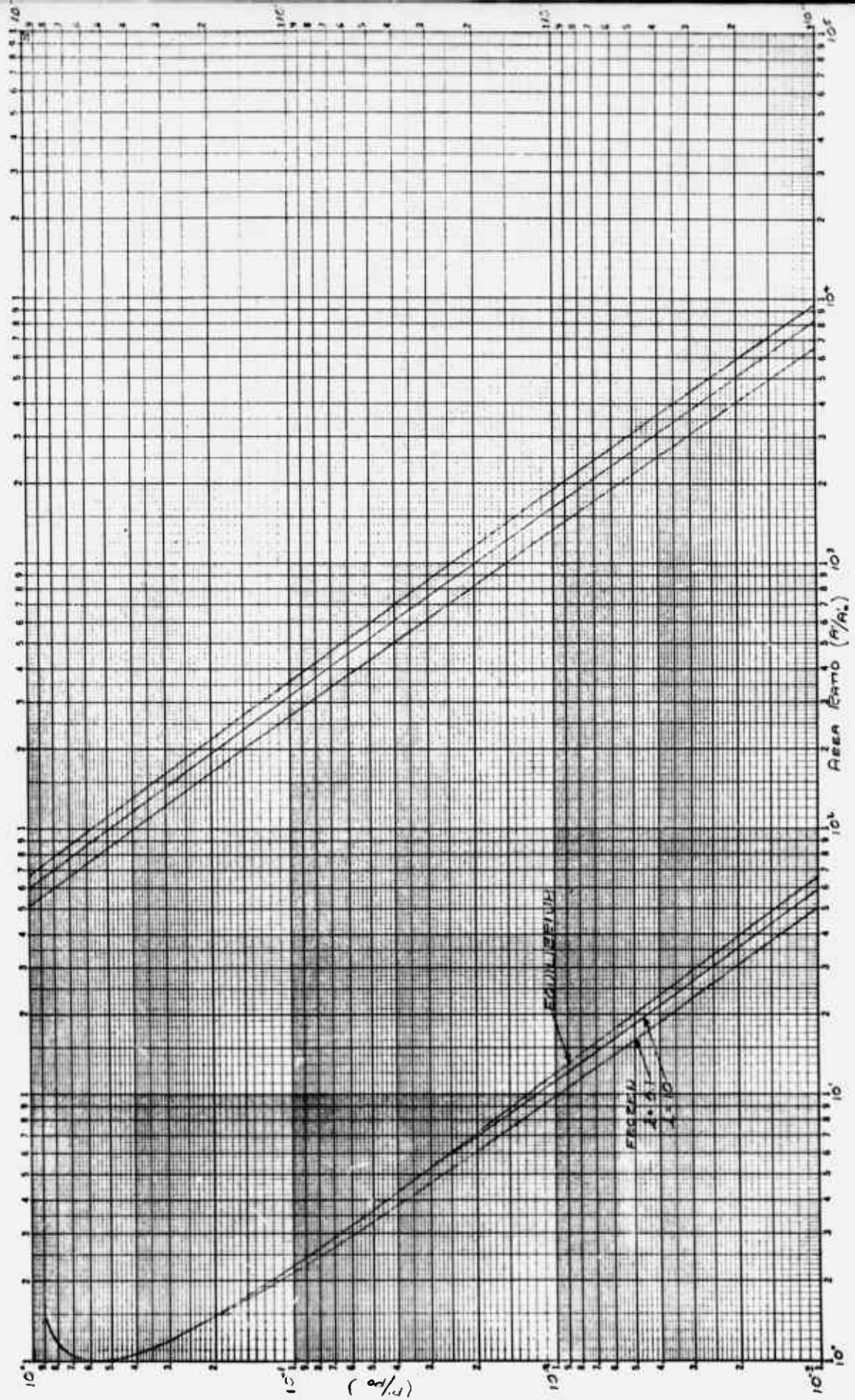


FIGURE NO. 25b HYPERBOLIC NOZZLE $T_0 = 5000^\circ\text{K}$ $P_0 = 100 \text{ ATM}$

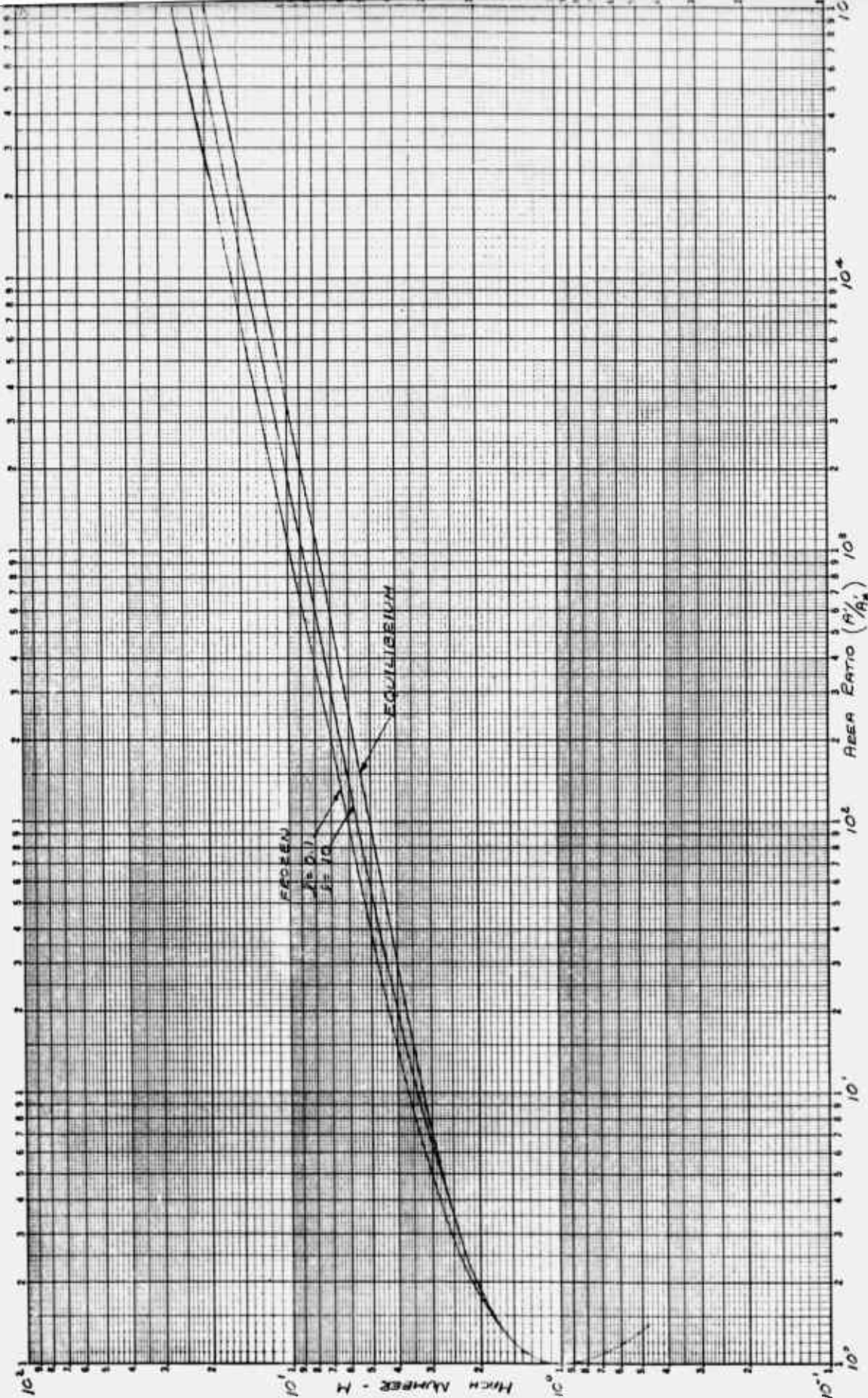


FIGURE NO. 25c HYPERBOLIC NOZZLE T₀' = 5000°K P₀' = 100 ATM

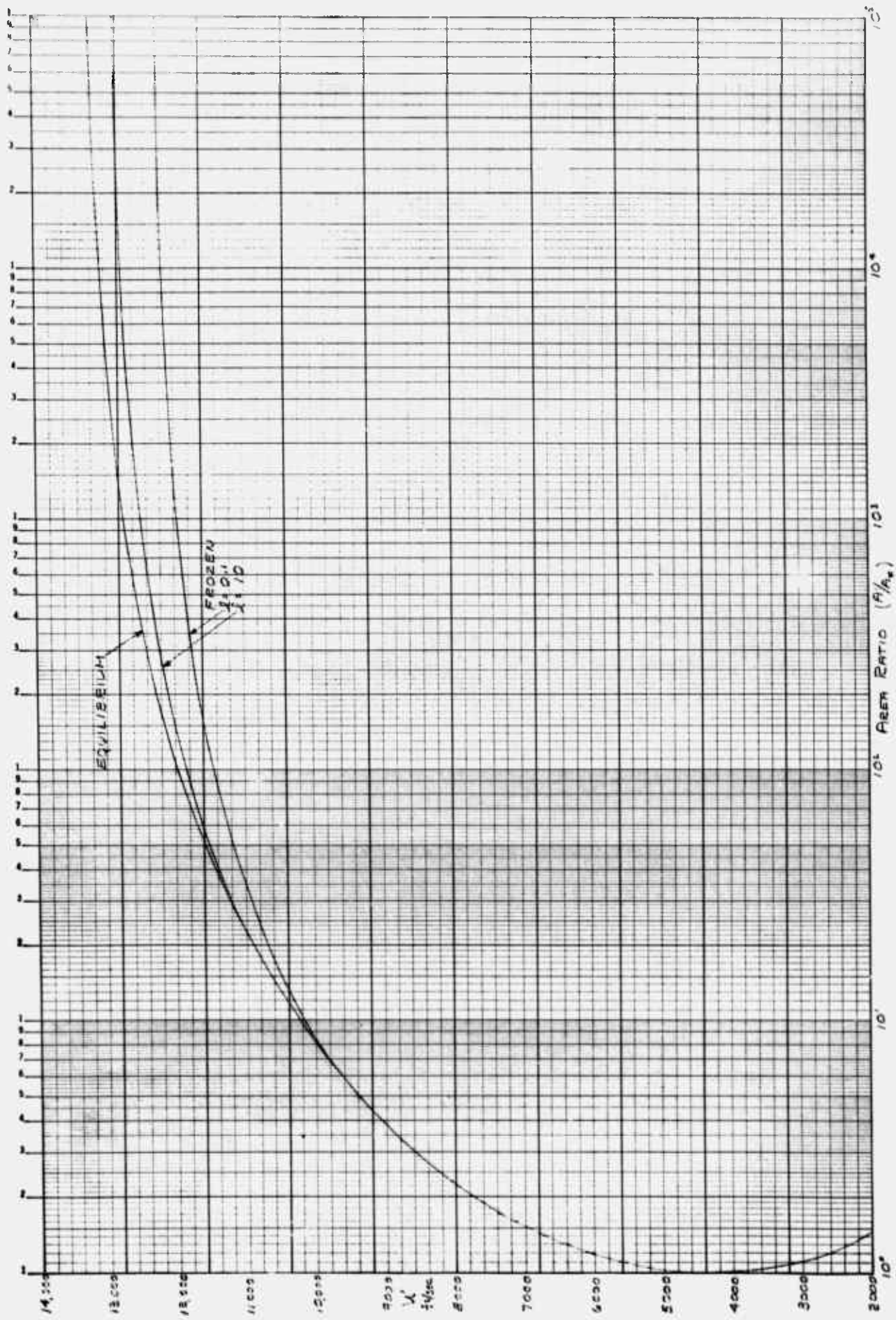


FIGURE NO. 25d HYPERBOLIC LOSS $T_0 = 5000 K$

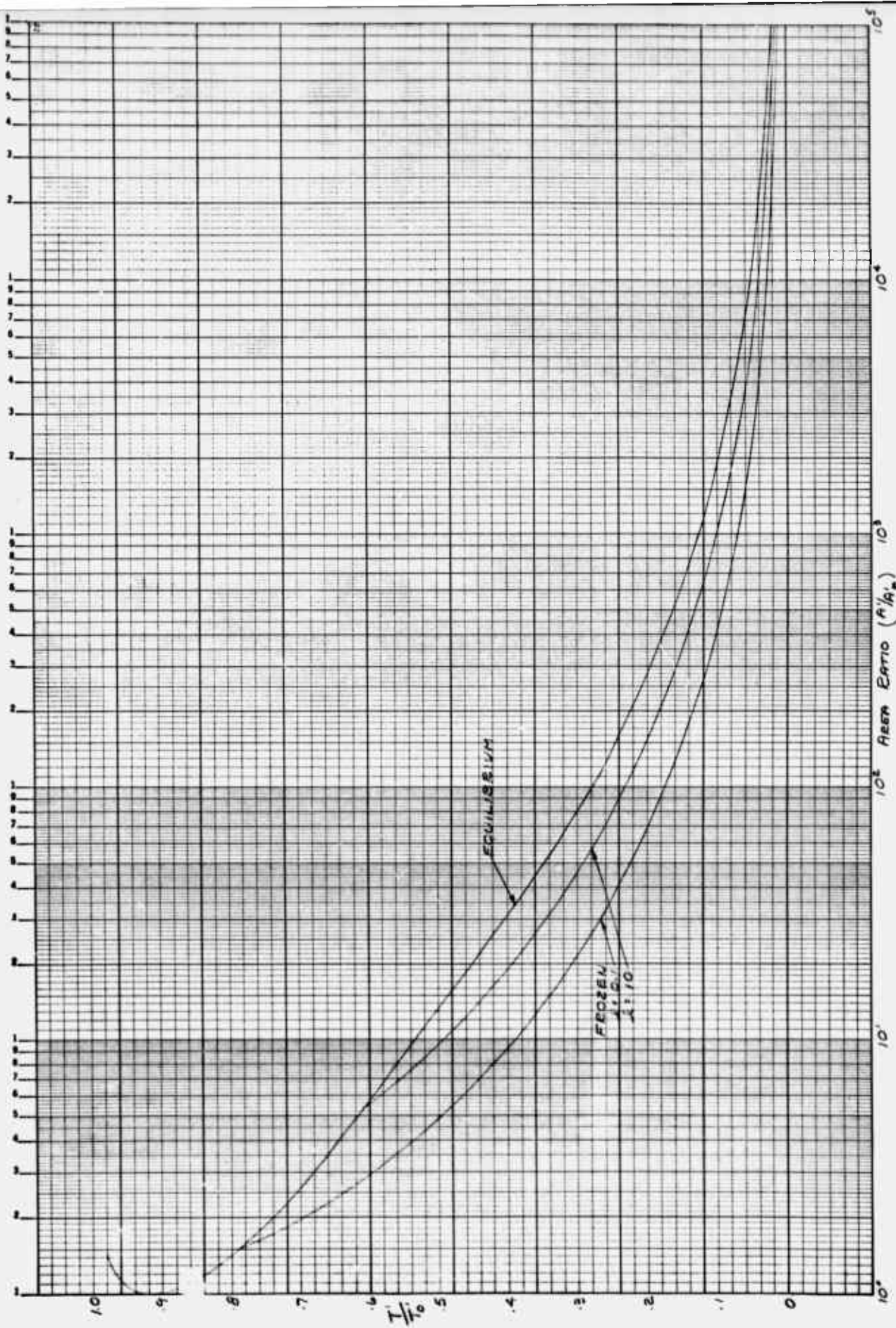


FIGURE NO. 25e HYPERBOLIC NOZZLE $T_0 = 5000^\circ K$ $P_0 = 100 \text{ ATM}$

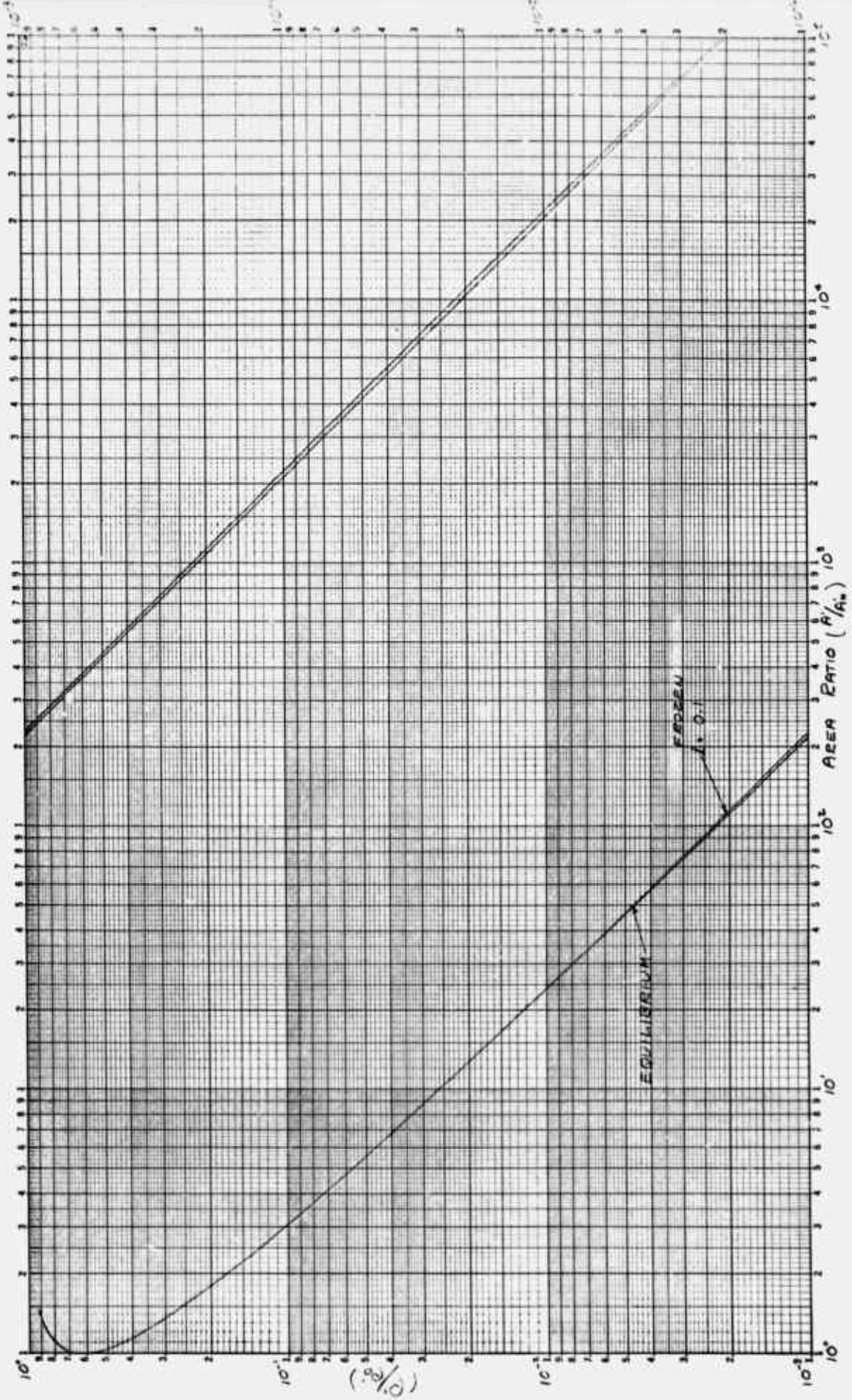


FIGURE NO. 26a HYPERSONIC NOZZLE $T_1 = 5000^\circ K$ $P_1 = 200 \text{ ATM}$

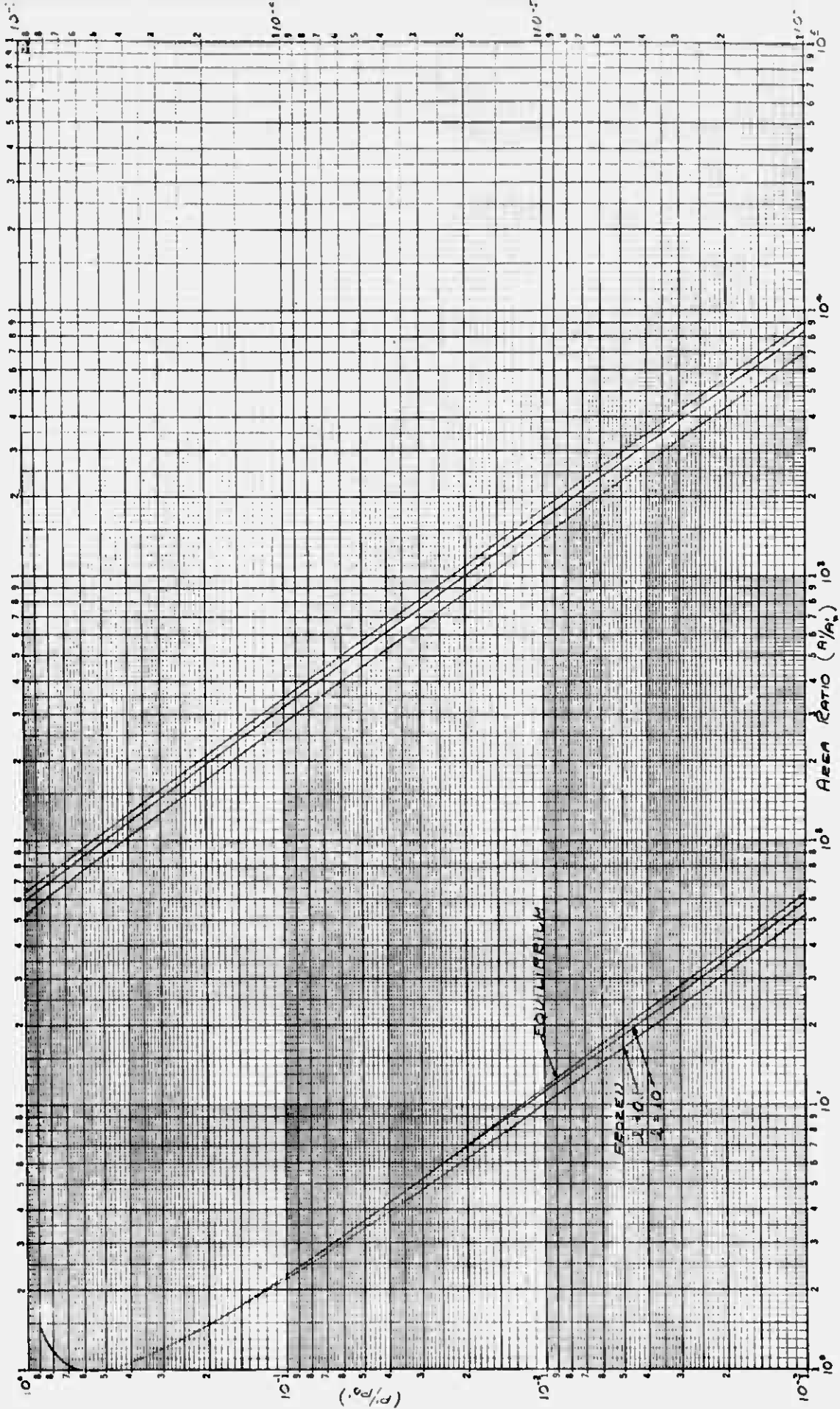


FIGURE NO. 266 HYPERBOLIC NOZZLE $T'_0 = 5000^\circ K$ $P'_0 = 200 \text{ ATM}$

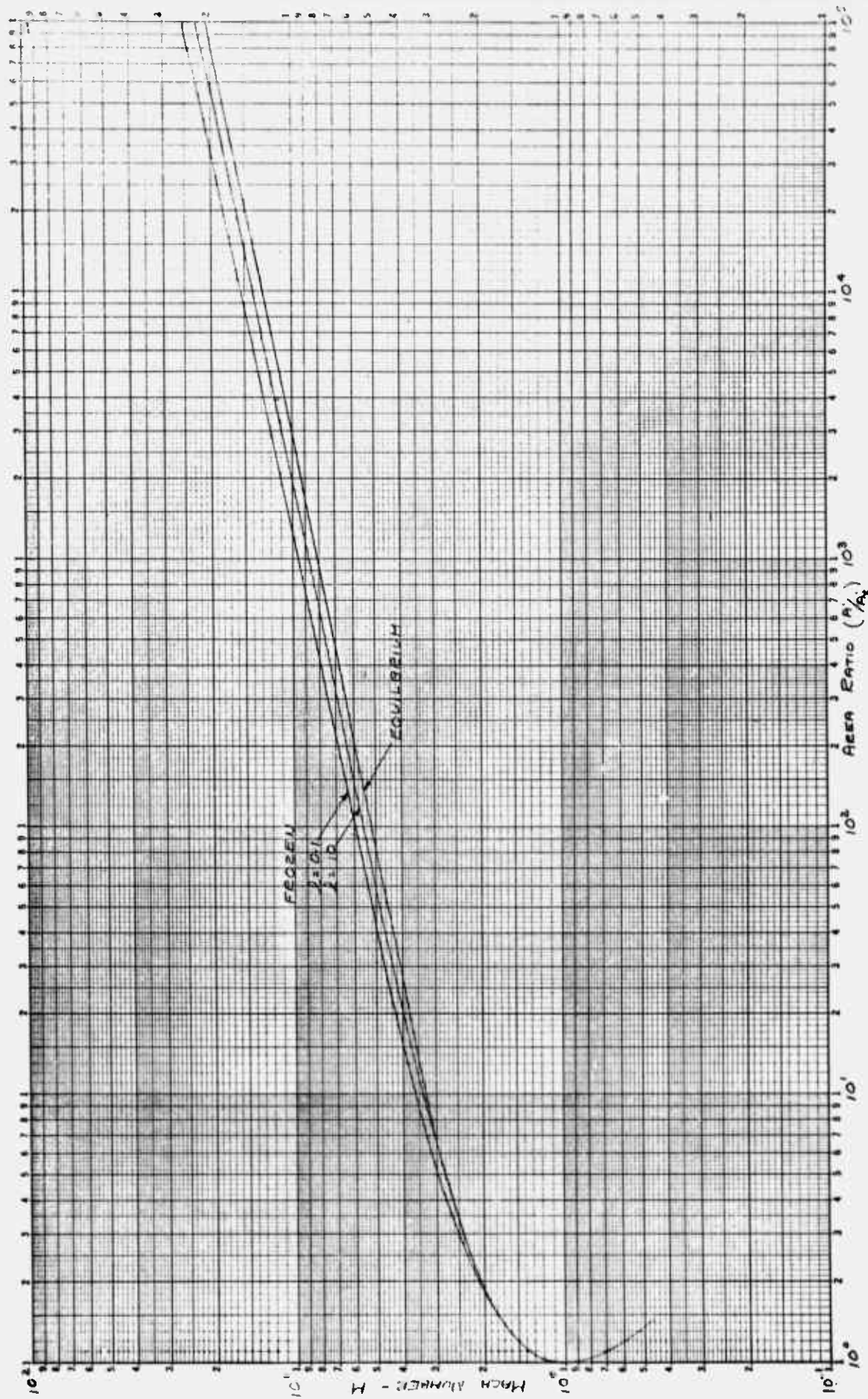


FIGURE NO. 266 AIR FLOW IN A CONVERGENT-DIVERGENT NOZZLE $T_0 = 5000^\circ R$ $P_0 = 200 \text{ ATM}$

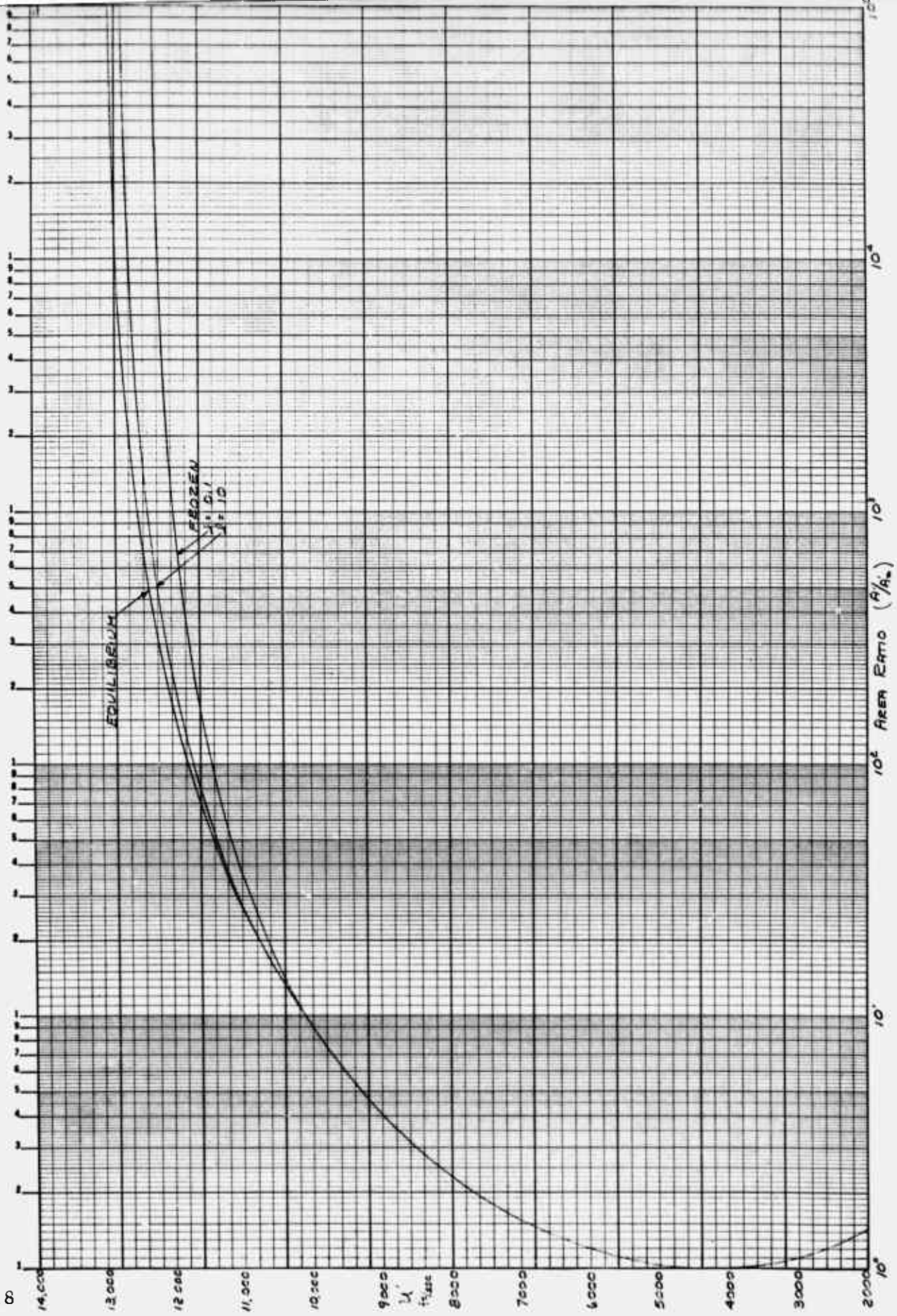


FIGURE NO. 263 HYPHENONIC NOZZLE $T_0 = 5000^\circ K$ $P_0 = 200 ATM$

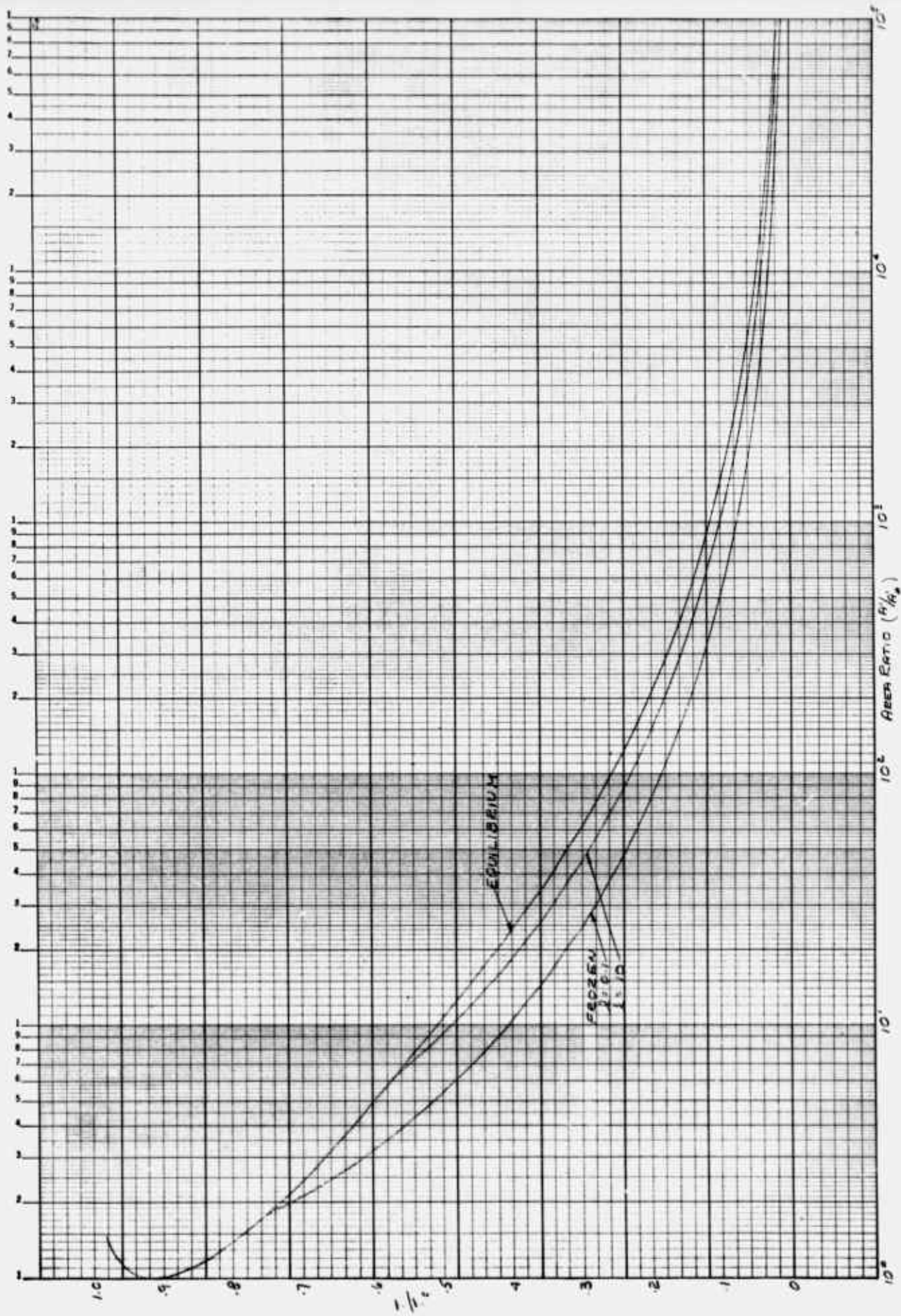


FIGURE NO 26c HYPERBOLIC NOZZLE $T_1 = 5000^\circ K$ $P_1 = 200 \text{ ATM}$

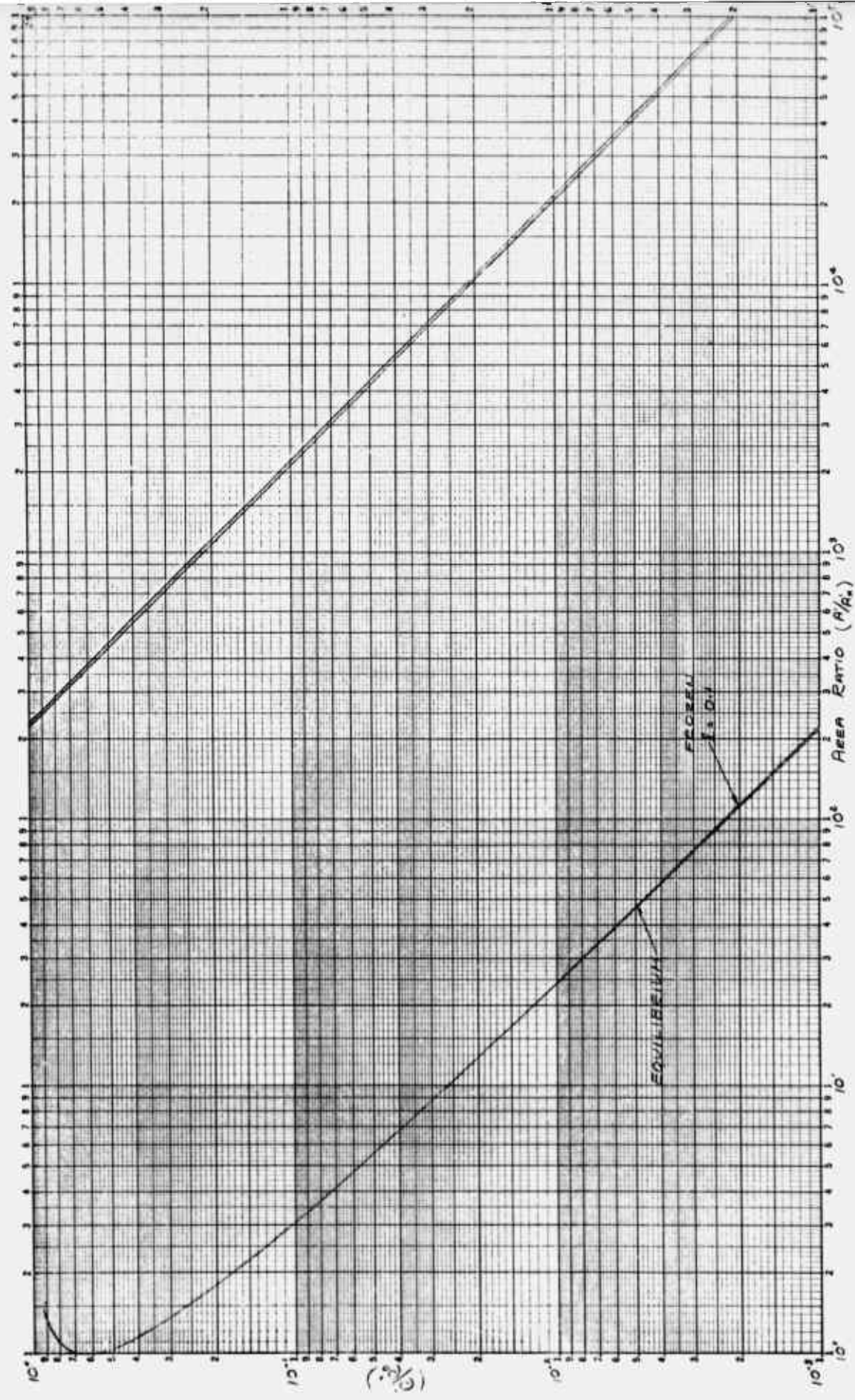


FIGURE NO. 27a NOZZLE $T_0 = 5000^\circ K$ $P_0 = 300 \text{ ATM}$

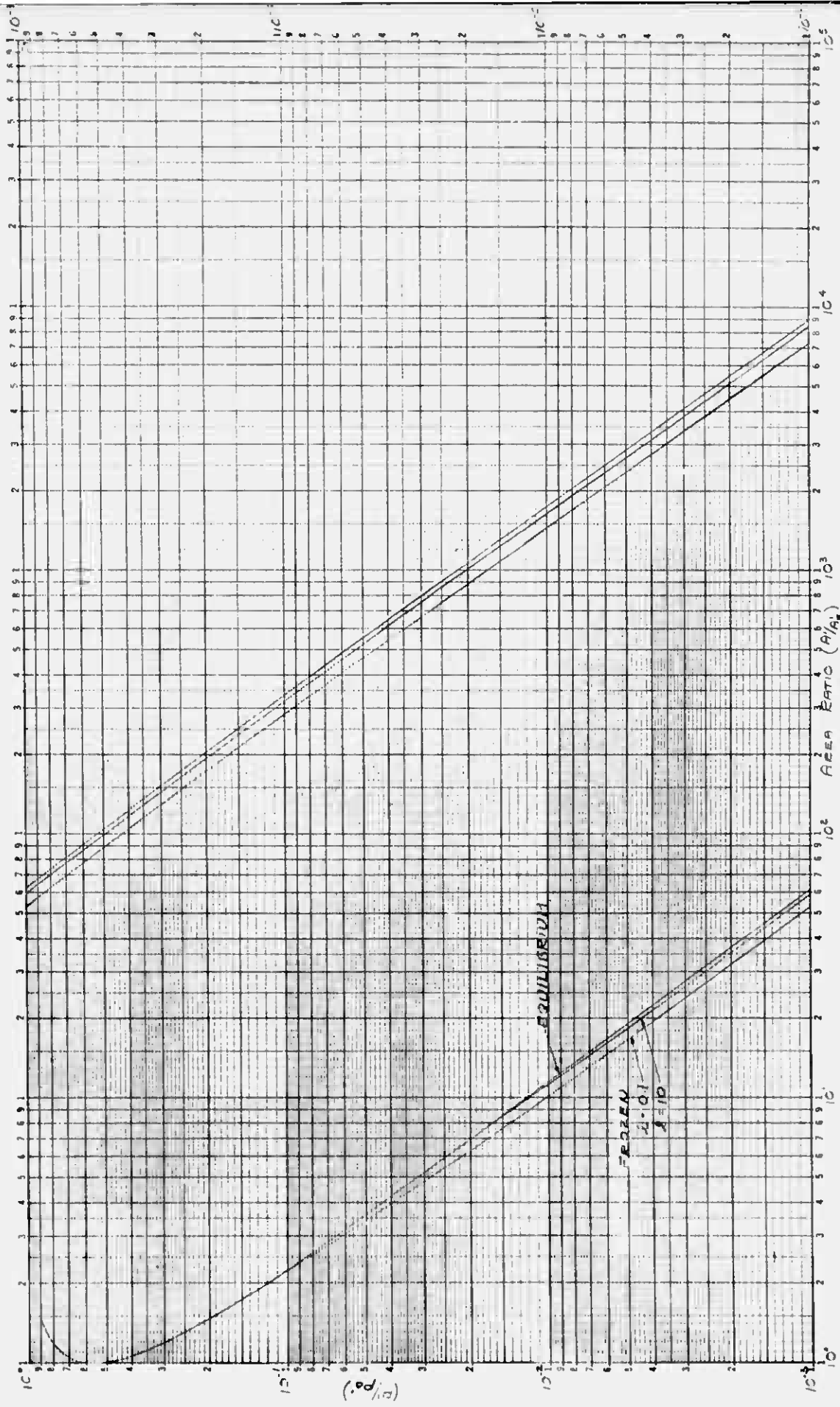


FIGURE NO. 276 HYPERBOLIC NOZZLE $T_0 = 5000^\circ K$ $P_0 = 300 \text{ ATM}$

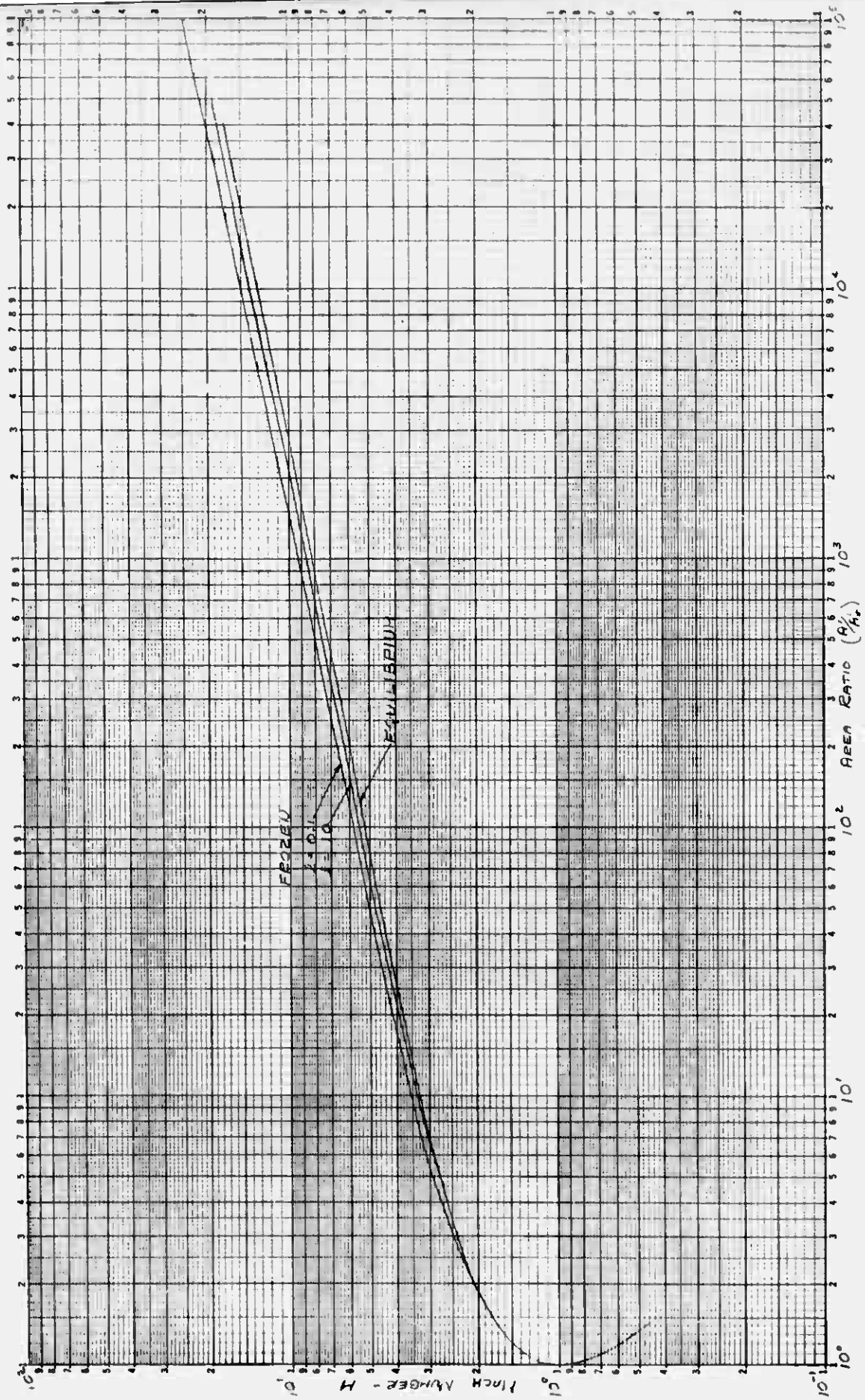


FIGURE NO. 27c HYPERBOLIC NOZZLE T₀ = 5000°K T₁ = 300 ATM

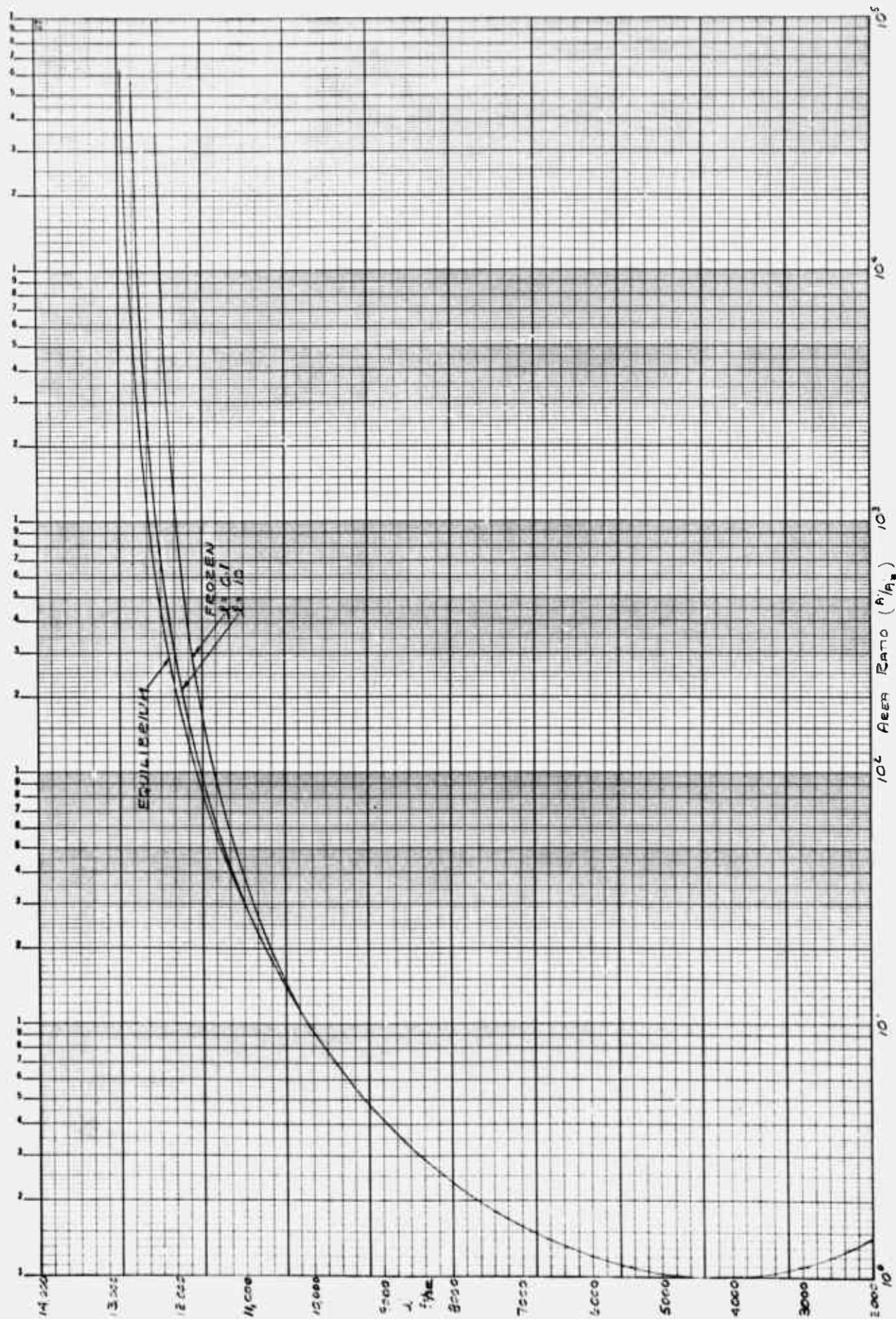


FIGURE NO. 27d HYPERBOLIC NOZZLE $T_0 = 5000^\circ K$ $P_0 = 300 \text{ ATM}$

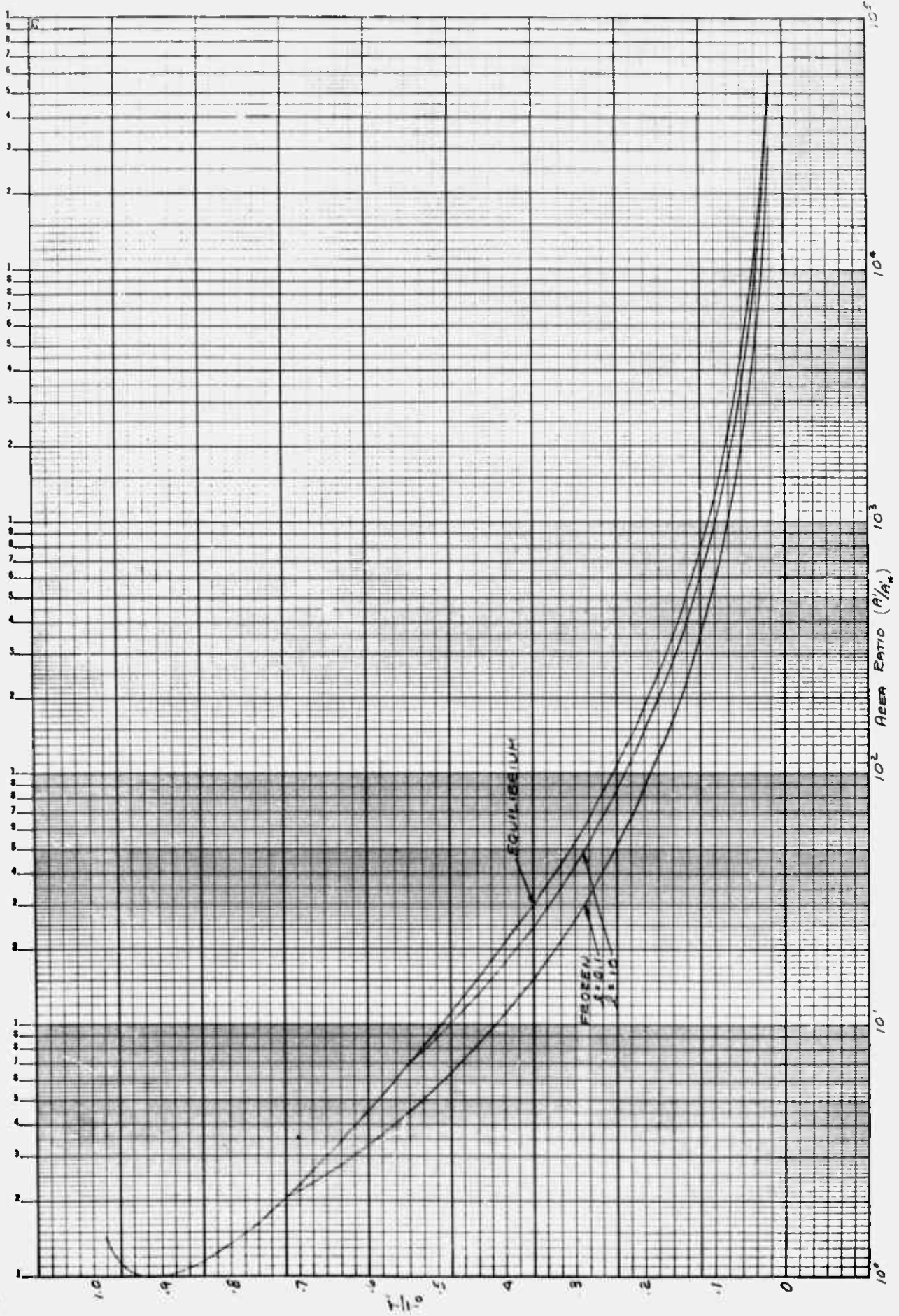


FIGURE NO. 27e HYPERBOLIC NOZZLE $T_c = 5000^\circ K$ $P_c = 300 \text{ ATM}$

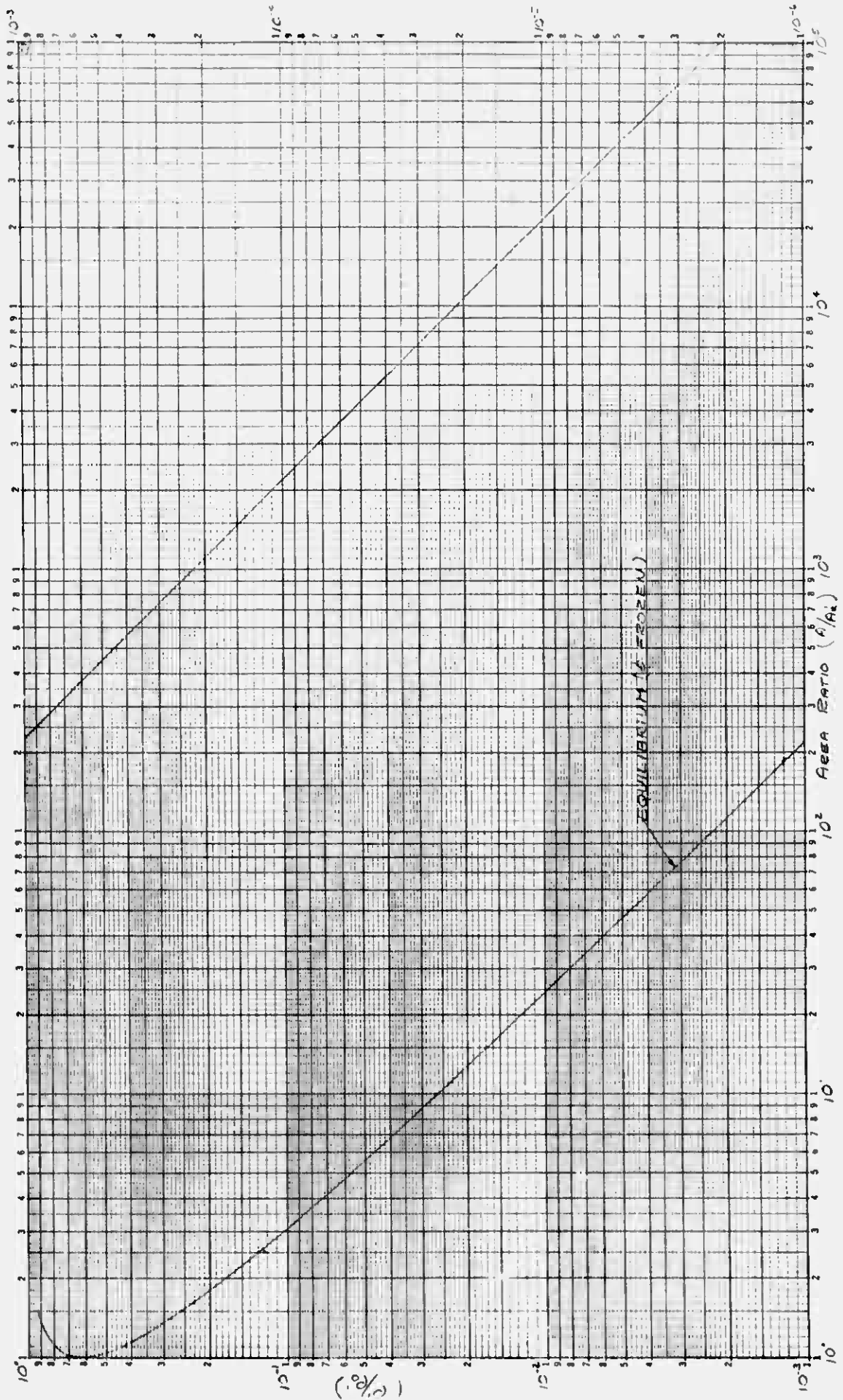


FIGURE NO. 28a HYPERBOLIC NOZZLE $T_0 = 5000^{\circ}K$ $P_0 = 1000 ATM$

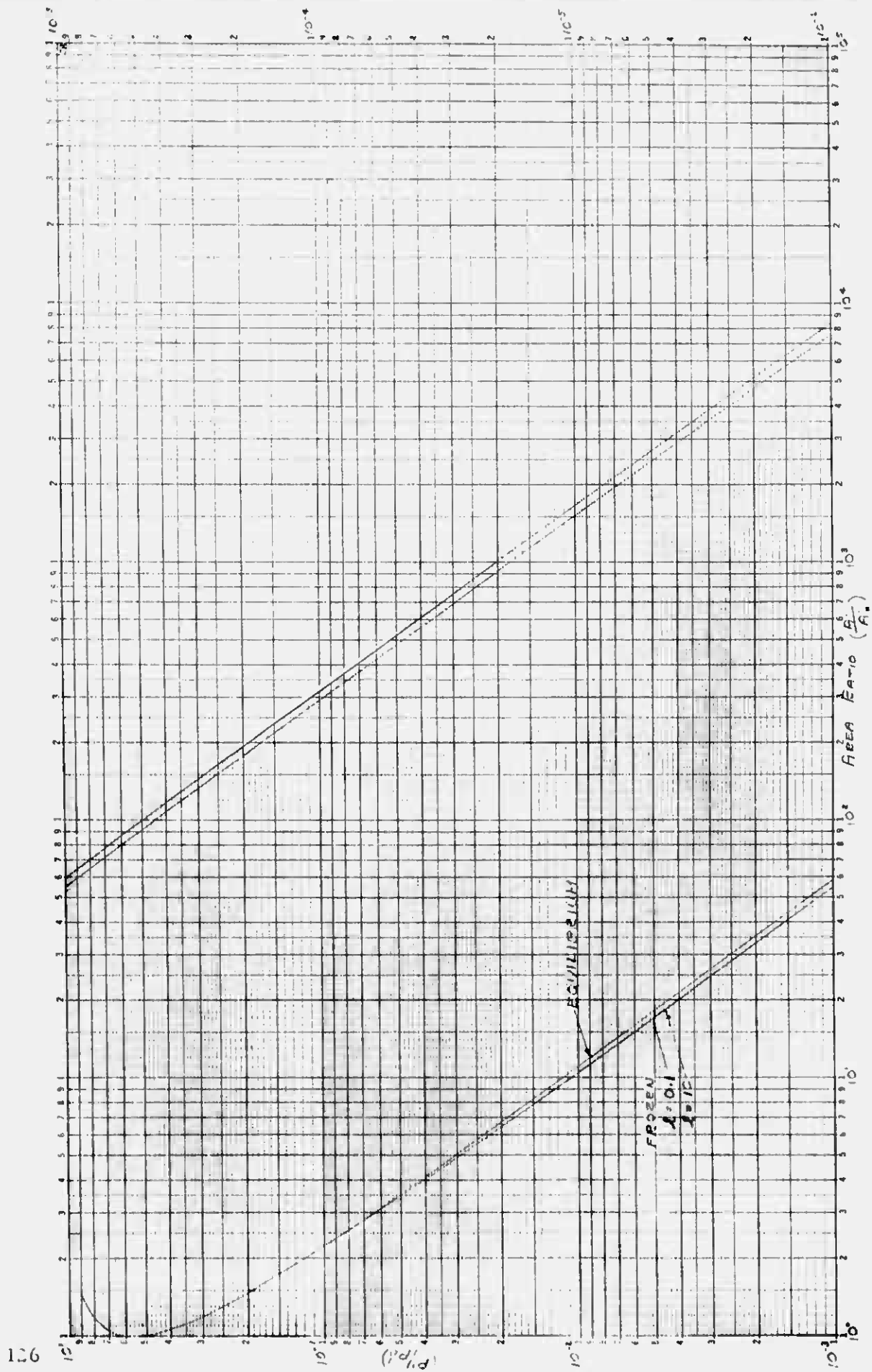


FIGURE NO. 28b HYPERBOLIC NOZZLE $T'_0 = 5000^\circ K$ $P'_0 = 1000 \text{ N/CM}^2$

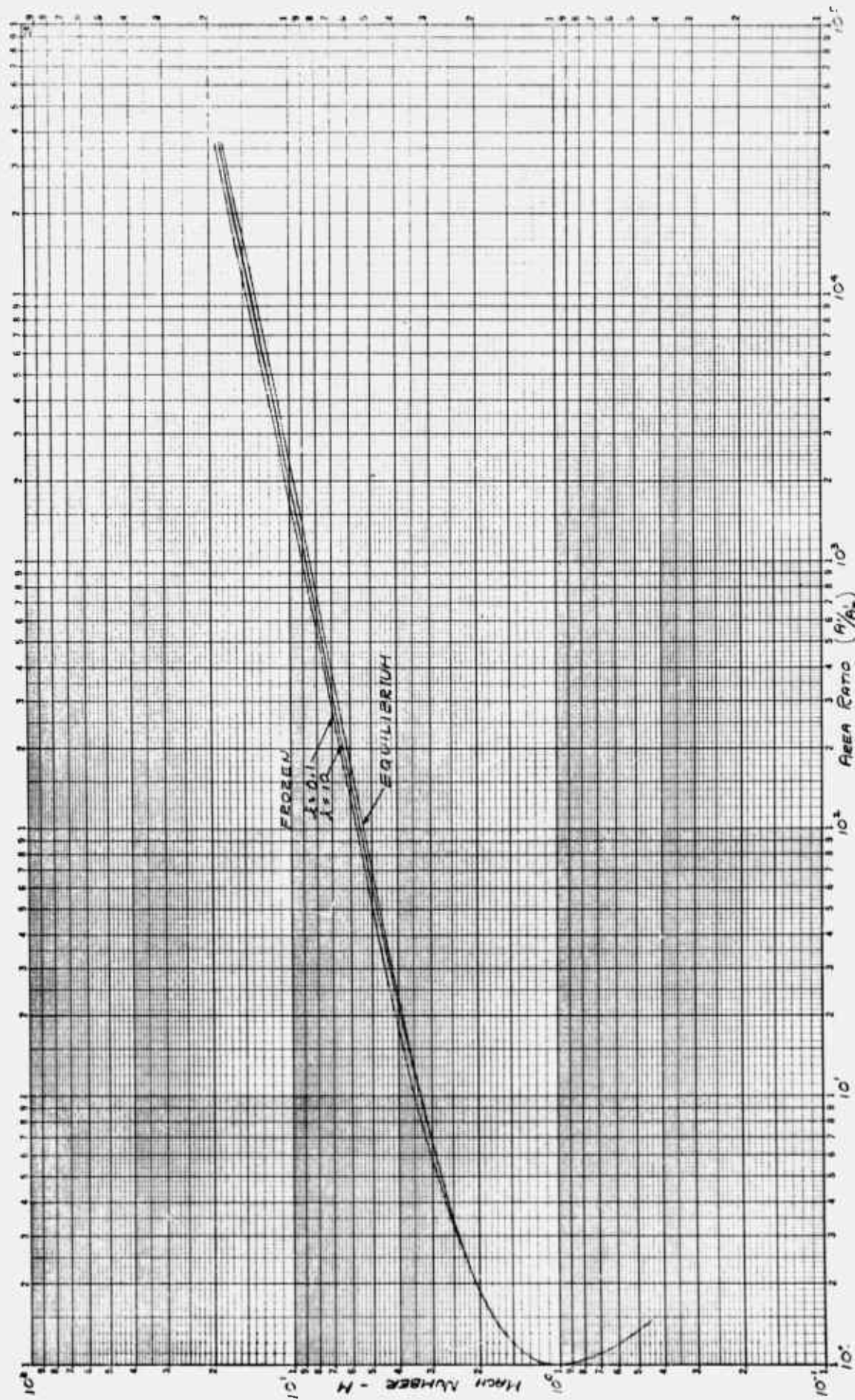


FIGURE NO. 28c HYPERBOLIC NOZZLE $T_0 = 5000^\circ K$ $P_0 = 1000 \text{ ATM}$

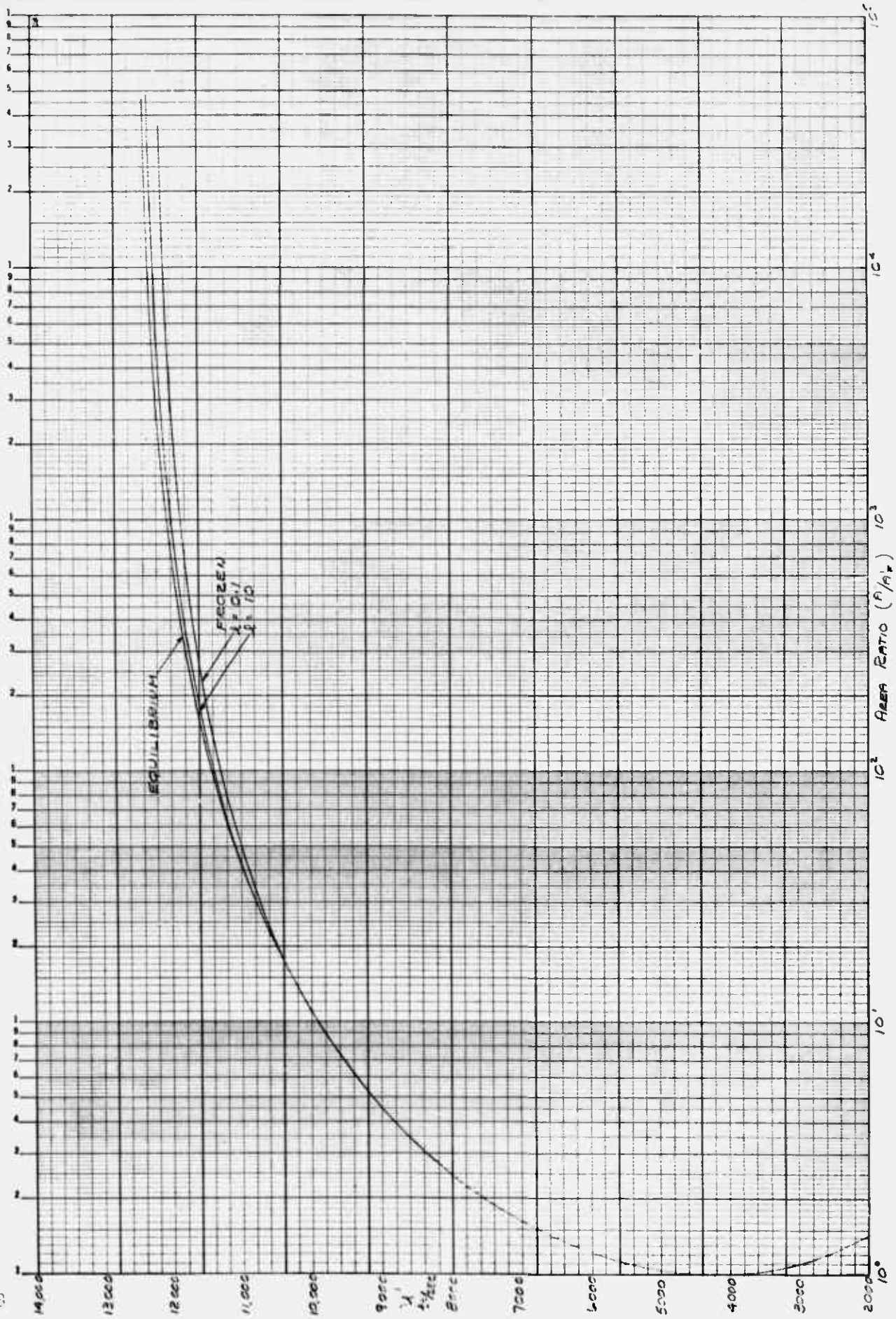


FIGURE NO. 28d HYPERBOLIC NOZZLE T₀ = 5000°K P_i = 1000 ATM

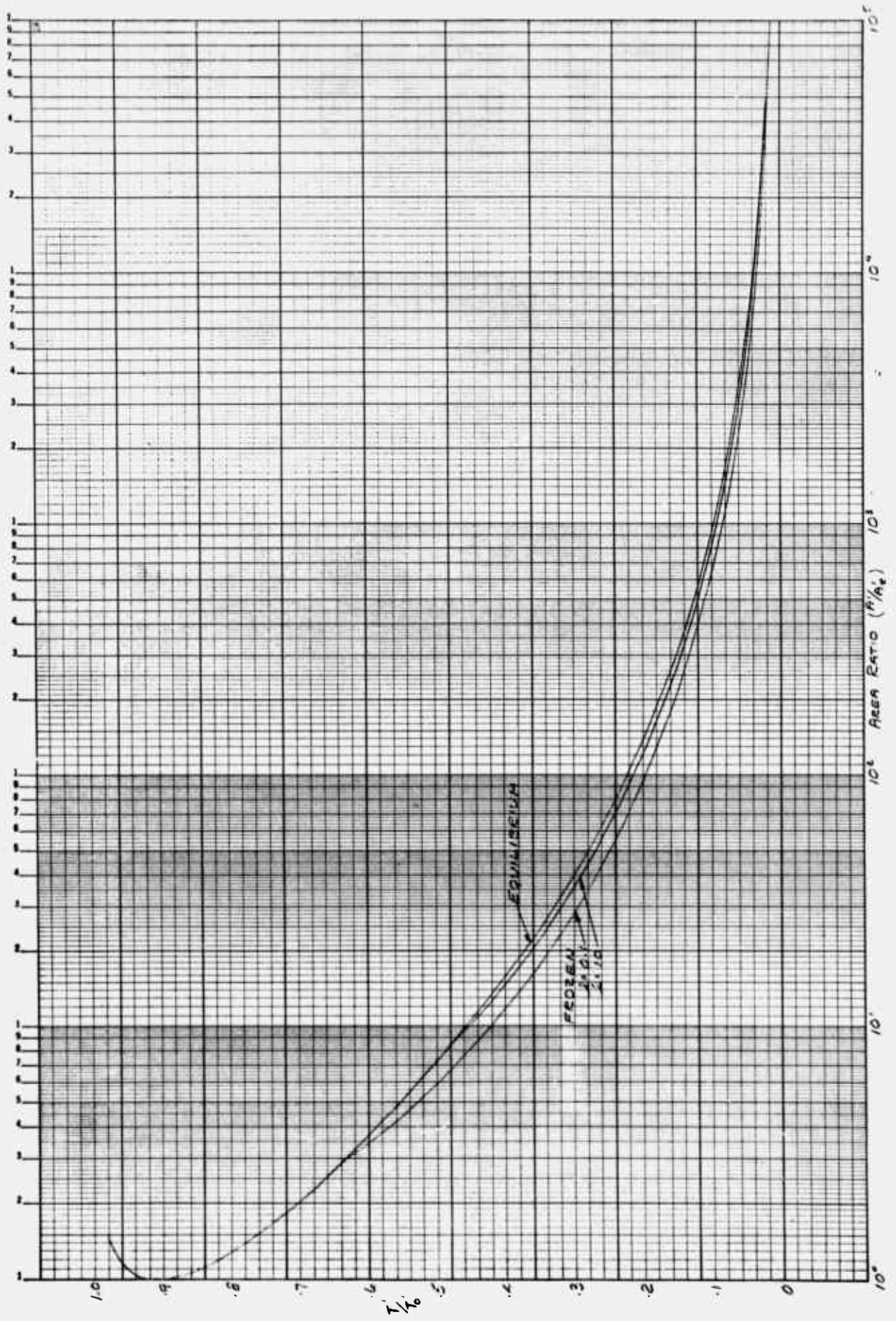


FIGURE NO. 28c HYPERBOLIC NOZZLE $T_1 = 5000^\circ\text{K}$ $P_1 = 1000\text{ ATM}$

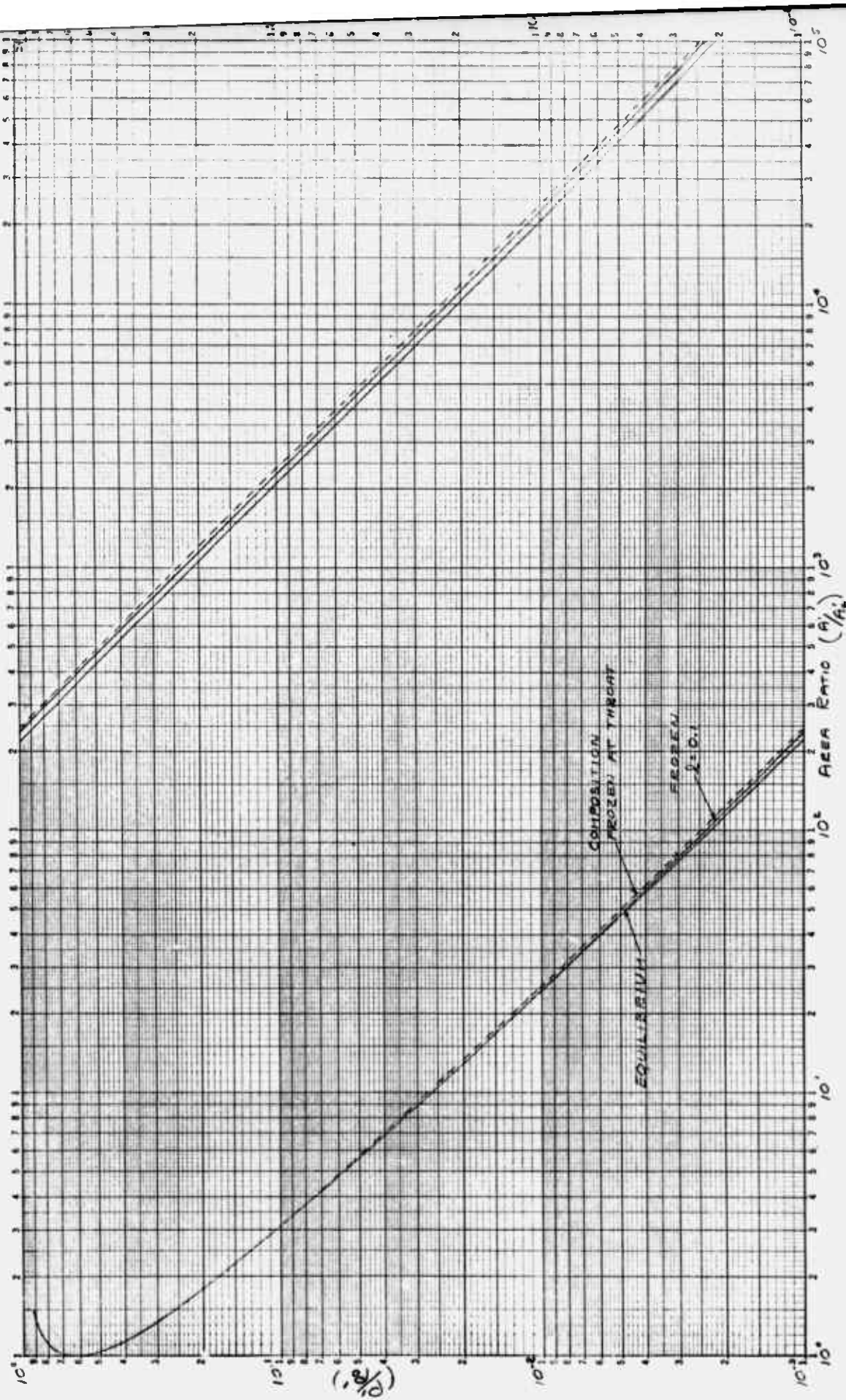


FIGURE NO. 29a HYPERBOLIC NOZZLE $T_0' = 6000^\circ K$ $P_0' = 100 \text{ ATM}$

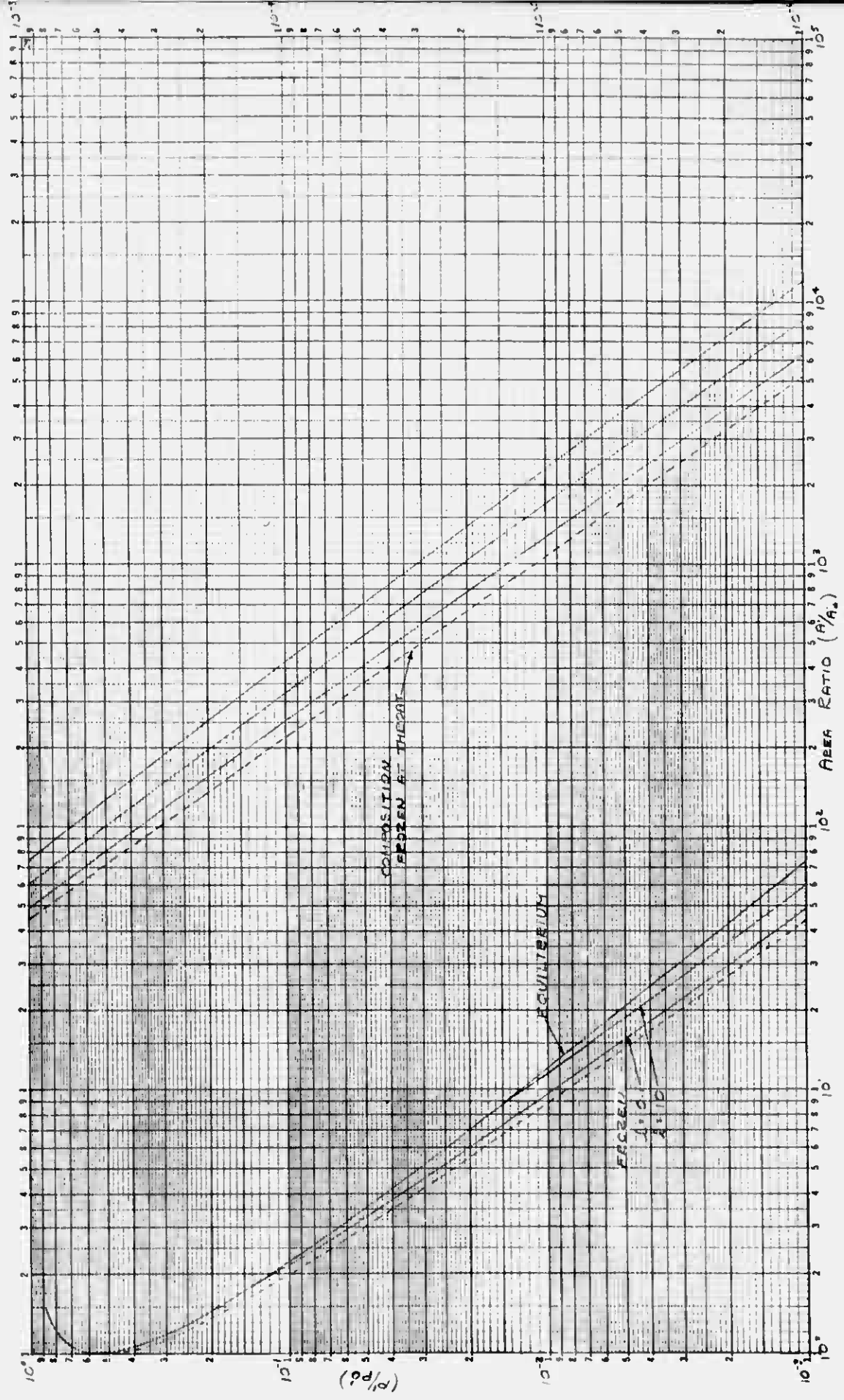


FIGURE NO. 296 HYPERBOLIC NOZZLE $T_c' = 6000^{\circ}K$ $P_c' = 100 \text{ ATM}$

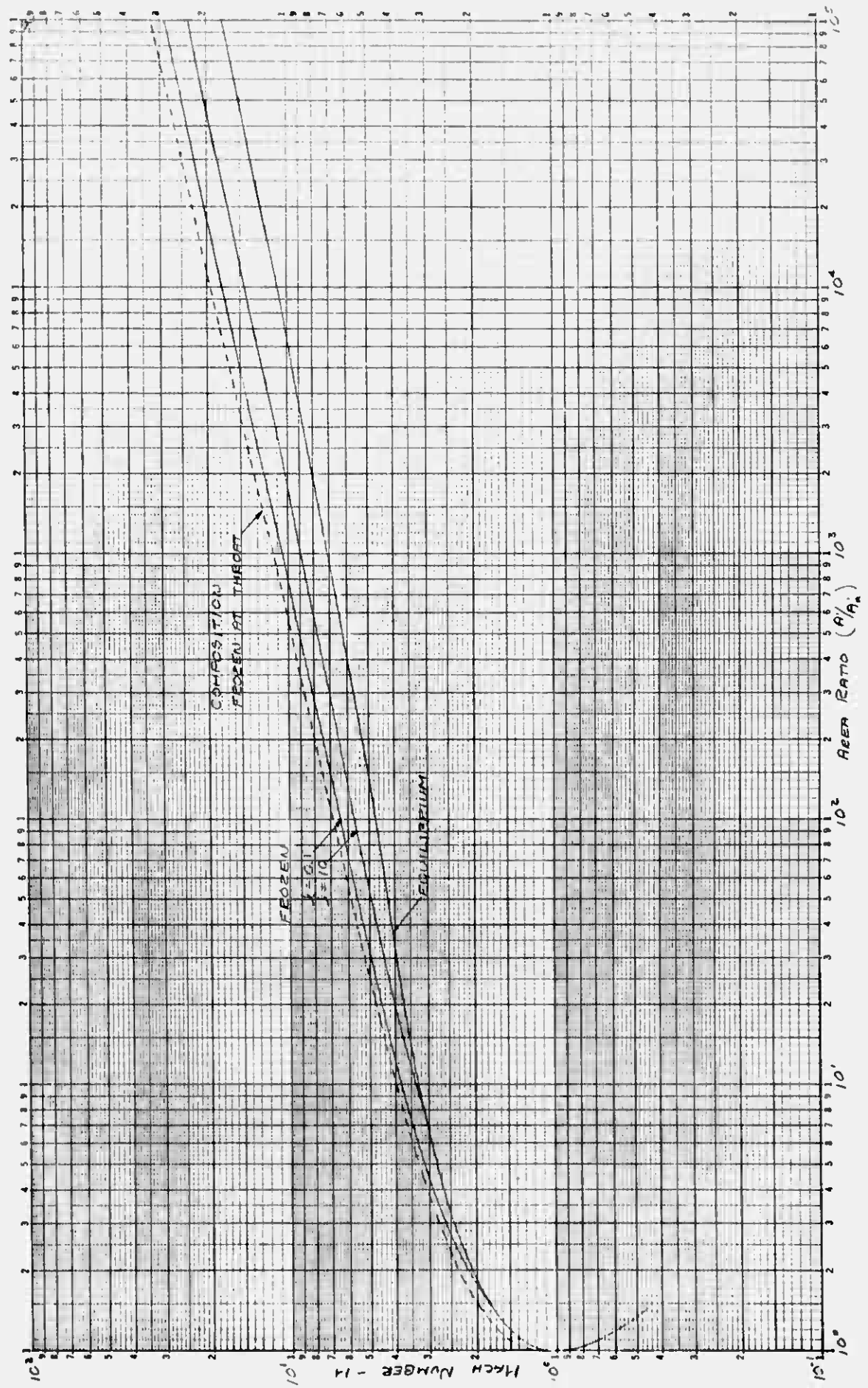


FIGURE NO. 29c HYPERBOLIC NOZZLE $T_0 = 6000^\circ K$ $P_0 = 100$ ATM

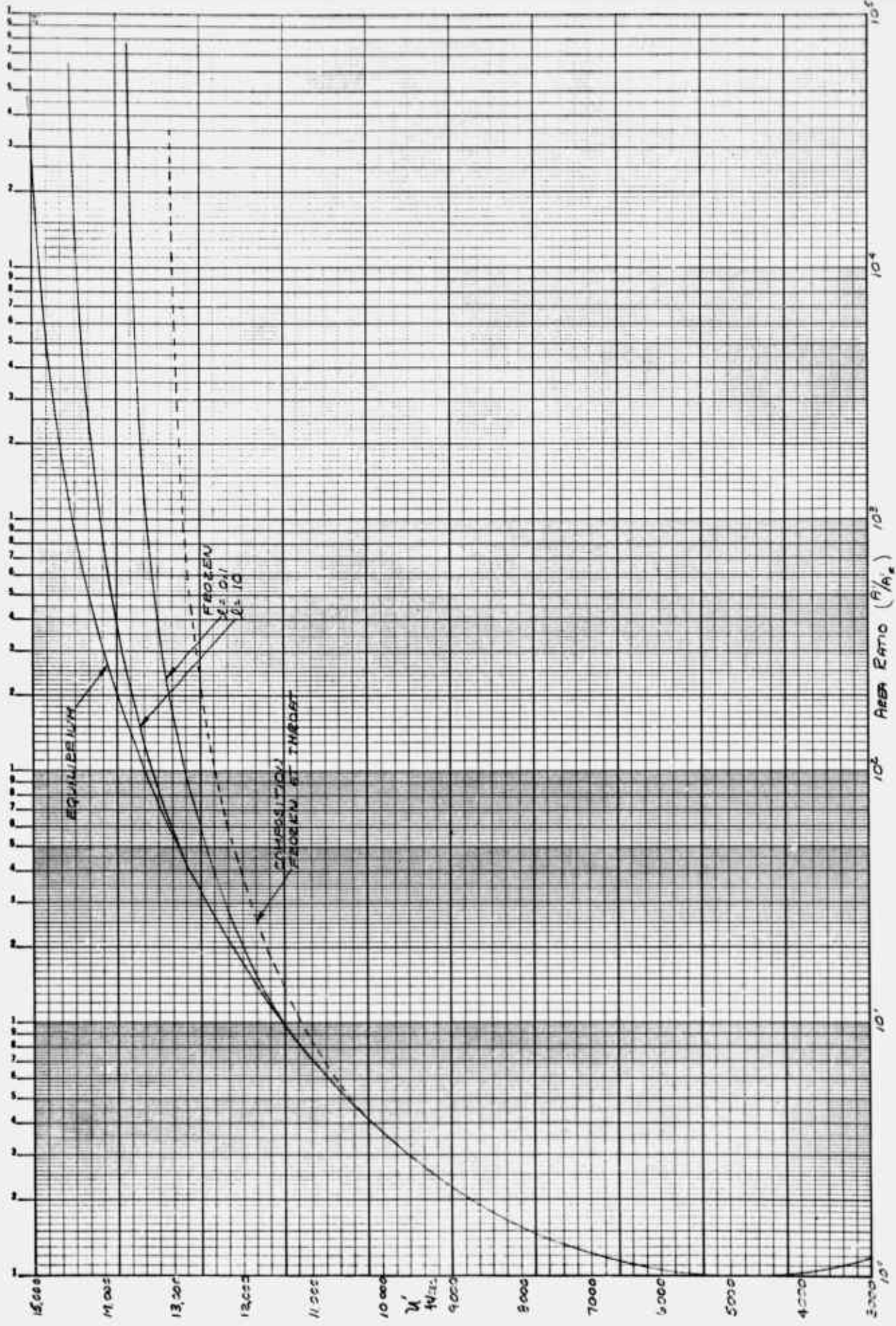


FIGURE NO 294 HYPERBOLIC NOZZLE $T_0 = 6000^\circ K$ $P_0 = 100 \text{ ATM}$

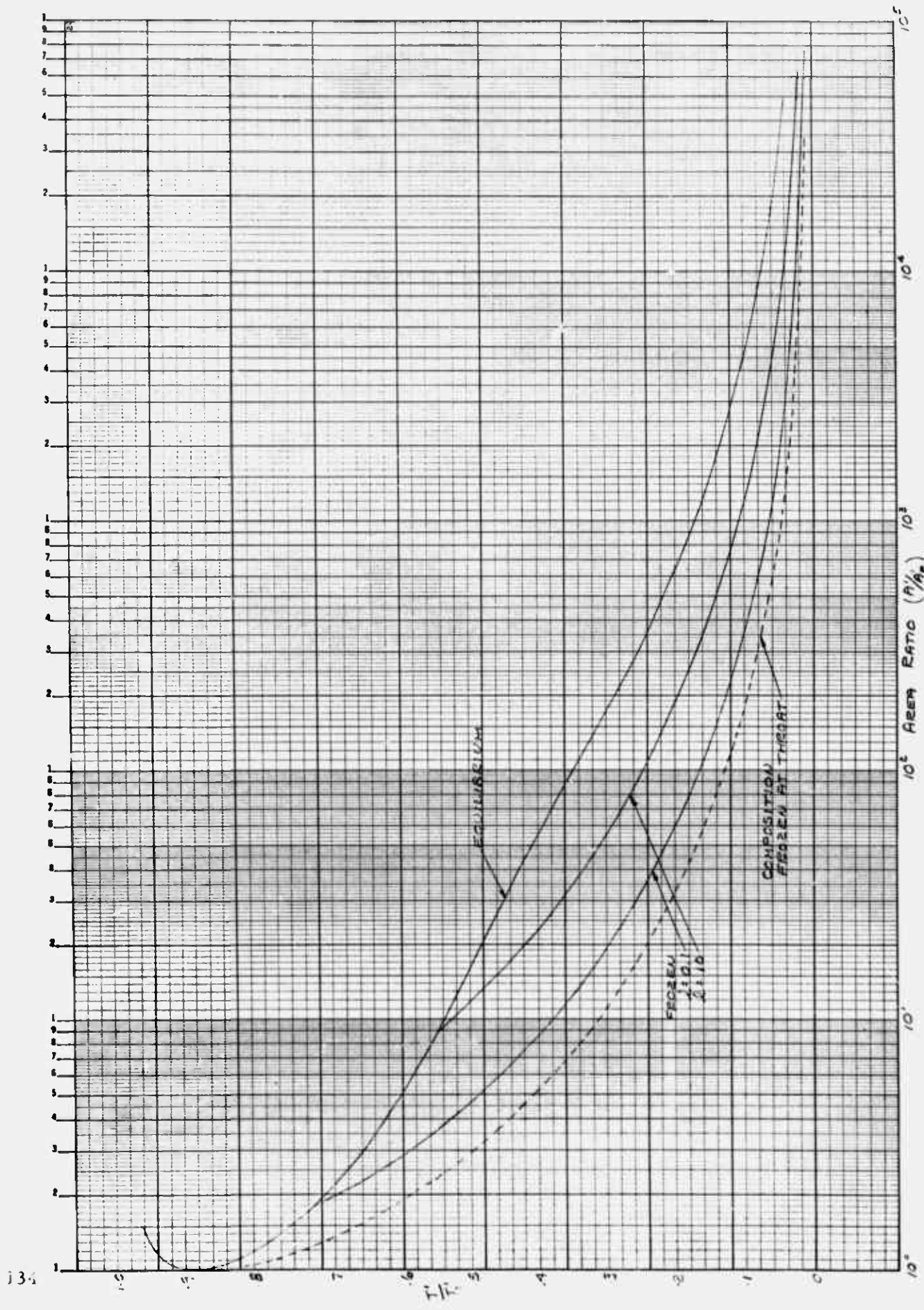


FIGURE NO 29E HYPHEN-SONIC NOZZLE $T_0 = 6000^\circ K$ $P_0 = 100 \text{ ATM}$

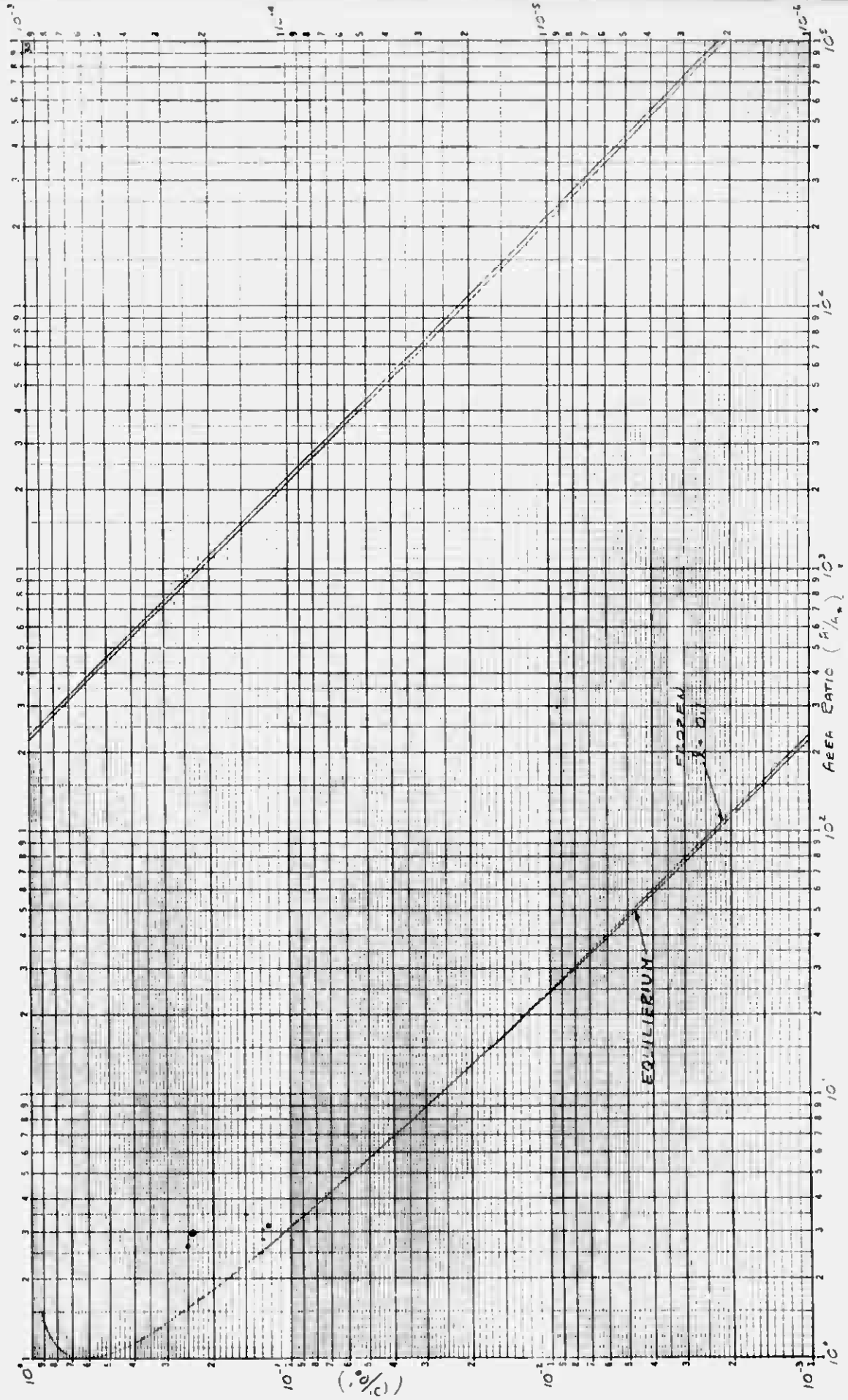


FIGURE NO. 30a HYPERBOLIC NOZZLE $T_0 = 600^\circ R$ $P_0 = 30$ P.S.I.A.

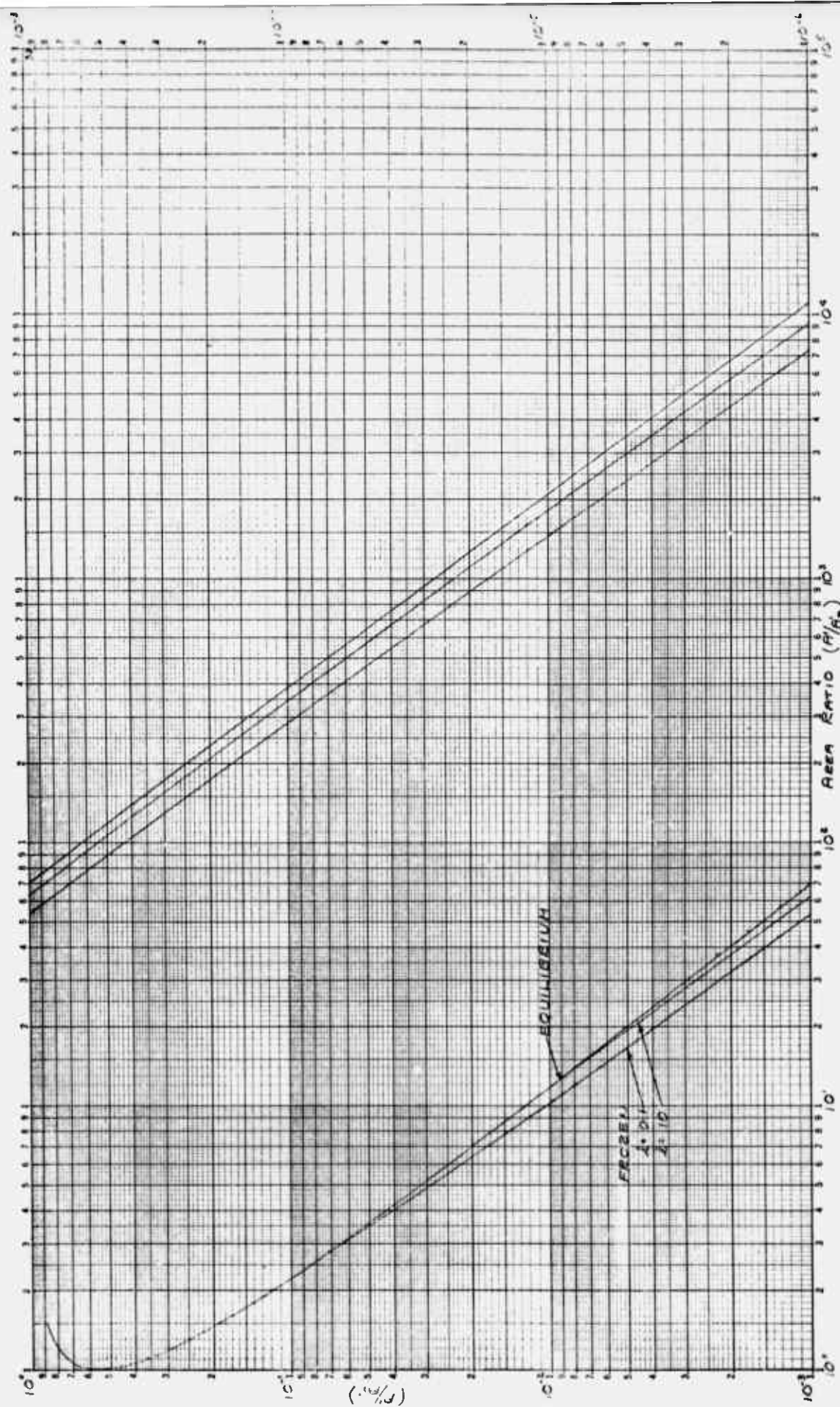


FIGURE NO. 30% HYPERBOLIC NOZZLE $T_0 = 6000^\circ K$ $P_0 = 300 \text{ ATM}$

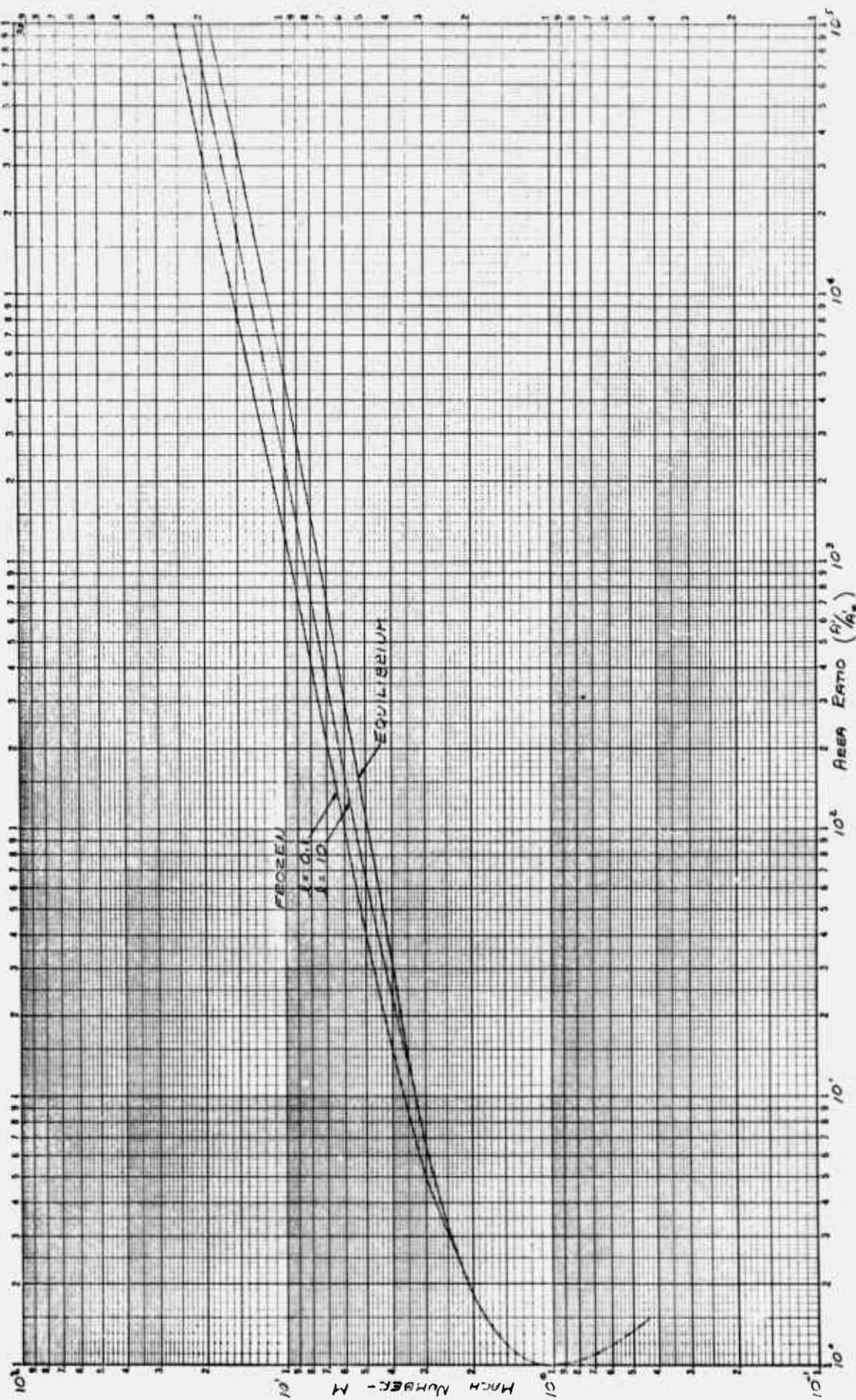


FIGURE NO. 30c HYPERBOLIC NOZZLE $T_i = 6000^\circ K$ $P_0 = 300 \text{ ATM}$

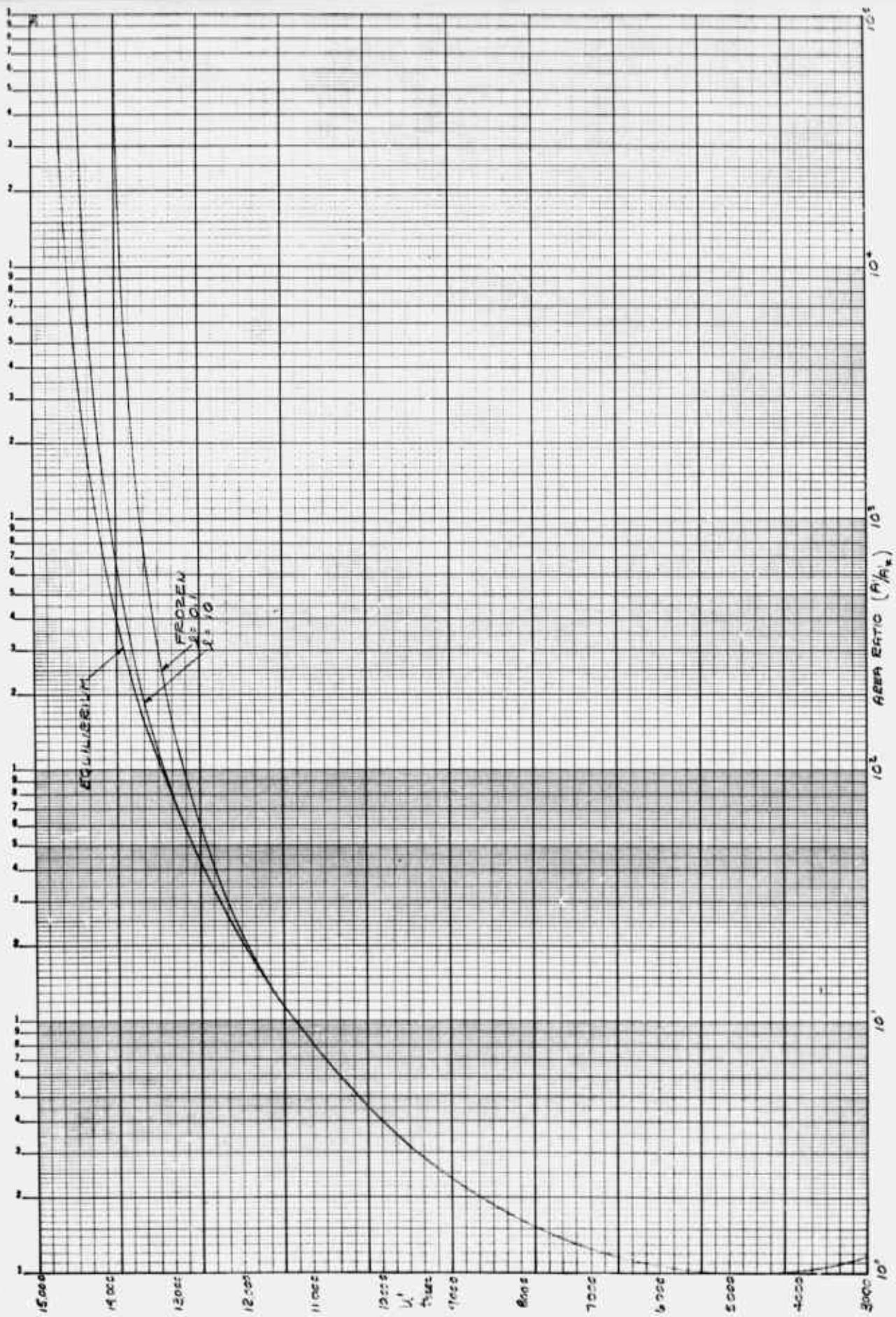


FIGURE NO. 30d HYPERSONIC NOZZLE $T_0 = 6000^\circ K$ $P_0 = 300 \text{ ATM}$

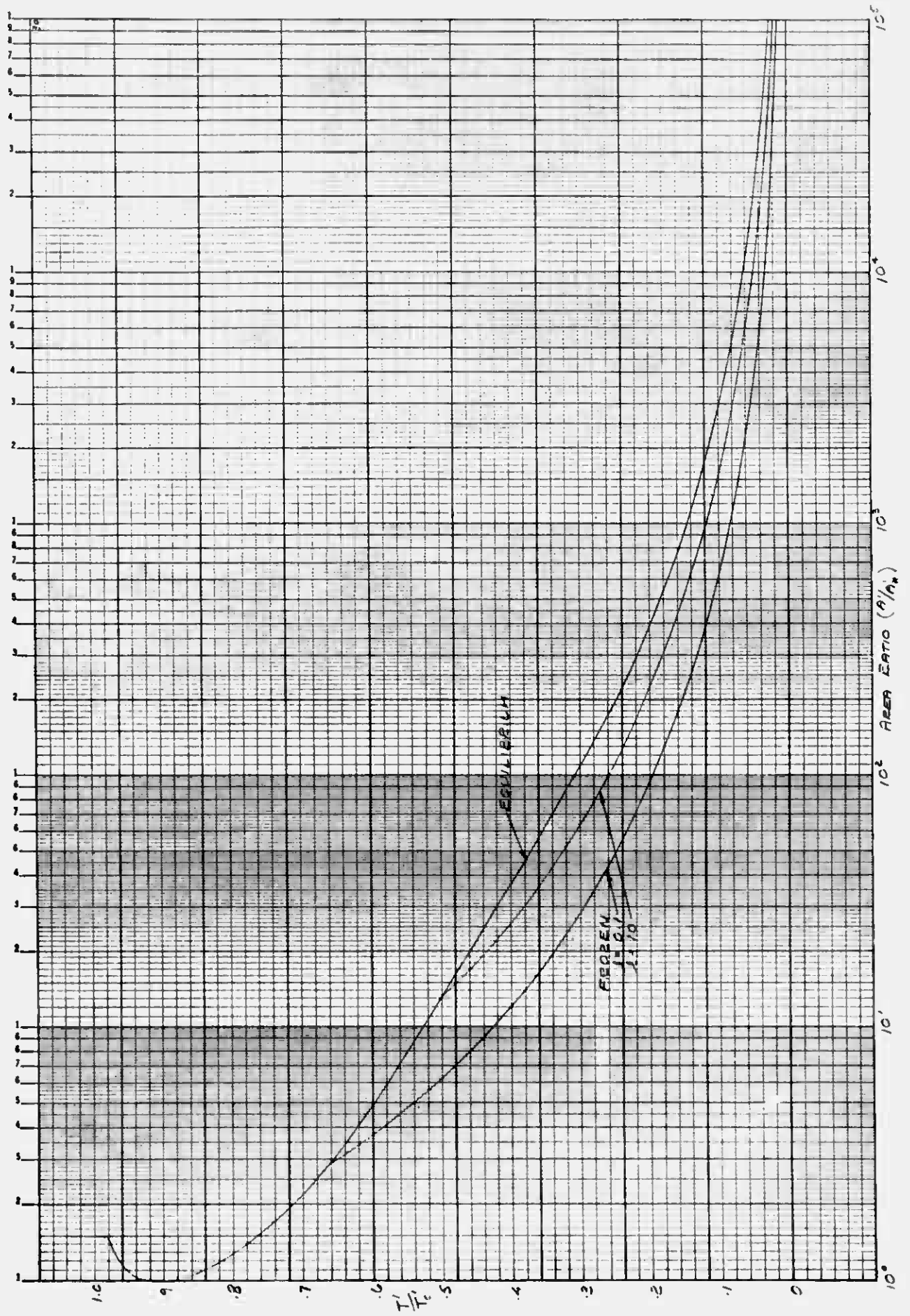


FIGURE NO 30e. HYPERBOLIC NOZZLE $T_0 = 6000^\circ K$ $P_0 = 300 \text{ ATM}$

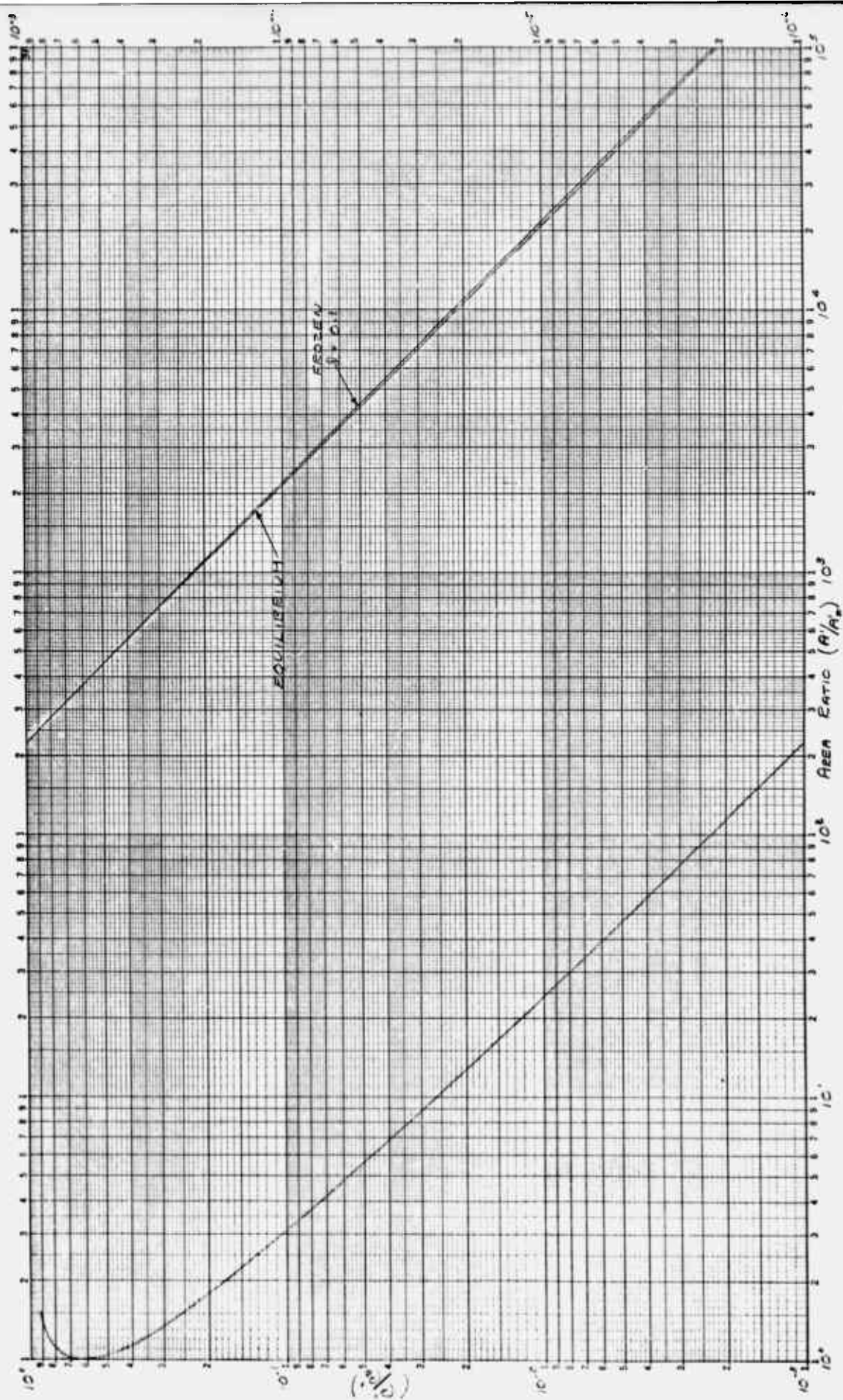


FIGURE NO. 31a HYPERBOLIC NOZZLE $T_0 = 6000\text{ K}$ $P_0 = 1000\text{ ATM}$

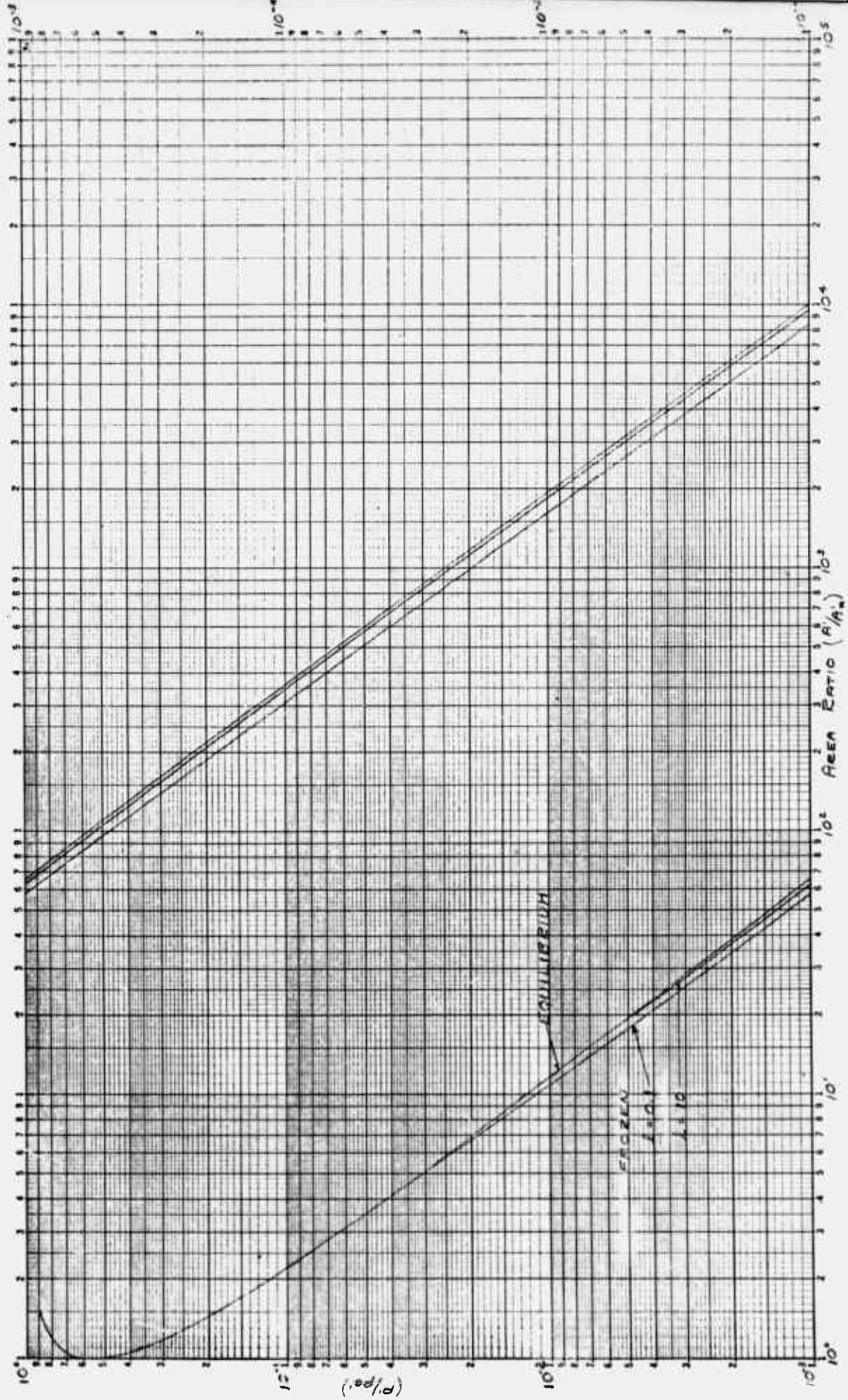


FIGURE NO. 316 HYPERBOLIC NOZZLE $T_0 = 6000^\circ K$ $P_0 = 1000 \text{ ATM}$

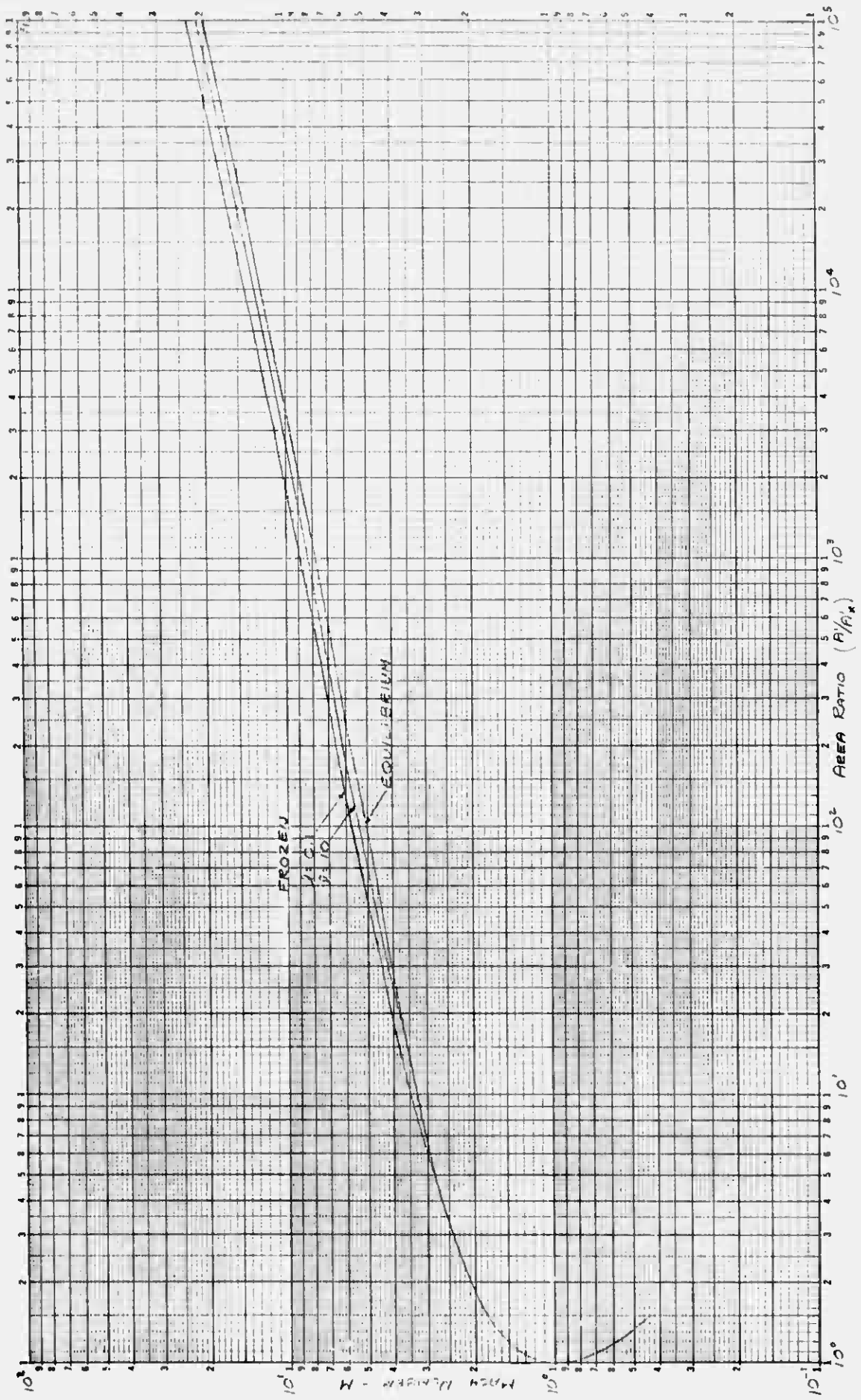


FIGURE NO. 31C HYPERBOLIC NOZZLE T₀ = 6000°K P₀ = 1000 ATM



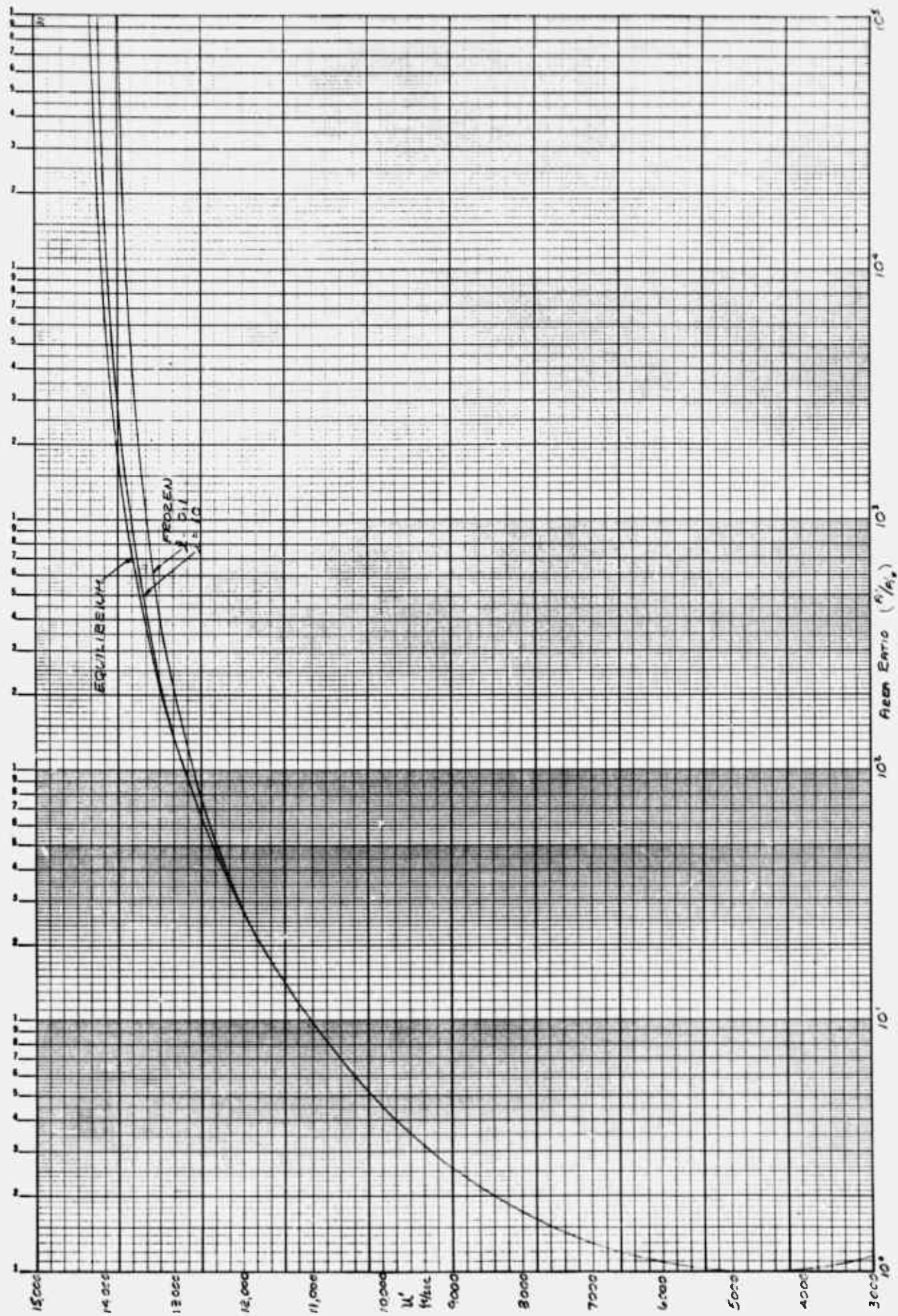


FIGURE NO. 31d HYPERSONIC NOZZLE $T_0 = 6000^\circ K$ $P_0 = 1000$ ATM

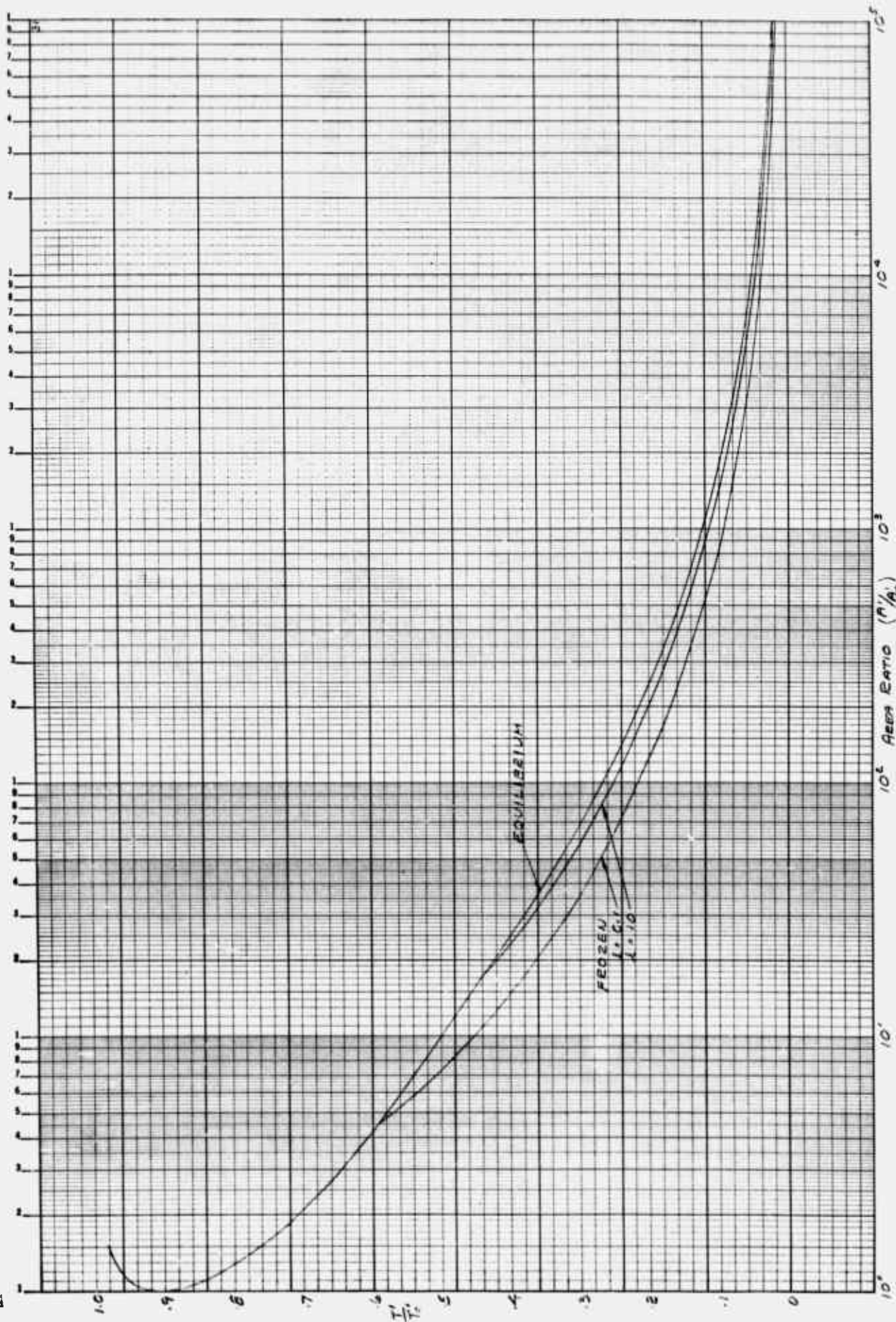


FIGURE NO. 31c HYPERBOLIC NOZZLE $T_0 = 6000^\circ K$ $P_0 = 1000 \text{ ATM}$