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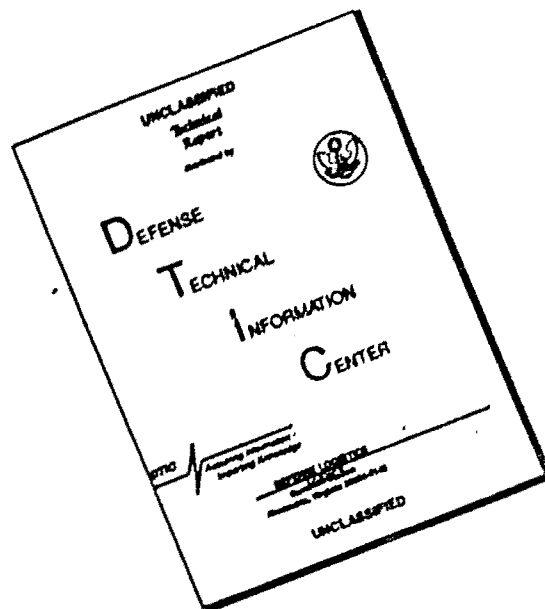
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ANTENNA LABORATORY

Technical Report No. 60

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BACKWARD-WAVE RADIATION FROM PERIODIC
STRUCTURES AND APPLICATION TO THE DESIGN
OF FREQUENCY-INDEPENDENT ANTENNAS

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by

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Contract AF33(657)-8460

Hitch Element Nr. 62405454

760D — Project 4028, Task 402824

Aeronautical Systems Division

Project Engineer E. Turner, ASRNCF-1

DECEMBER 1962

Sponsored by:

AERONAUTICAL SYSTEMS DIVISION

WRIGHT-PATTERSON AIR FORCE BASE, OHIO



ELECTRICAL ENGINEERING RESEARCH LABORATORY
ENGINEERING EXPERIMENT STATION
UNIVERSITY OF ILLINOIS
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Several members of the Antenna Laboratory staff have contributed to the measurements reported herein. The helix-fed monopole experiments and tests of the log-periodic bent zigzag were done by John W. Greiser. Model construction and testing of the zigzag, helix, and dipole array antennas was done by Bradley Martin, Ron Grant, and Eddie Young.

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1. INTRODUCTION

One characteristic common to a large number of unidirectional frequency-independent log-periodic and log-spiral antennas is that radiation is directed toward the apex or feed point of the structure^{1,2,3}. This property is essential to the frequency-independent behavior of the finite antenna since it makes less important the end effect due to truncation on the side of the large elements of the structure. That this is so can be seen from the requirement that the total current on the structure must decay with distance from the feed point to avoid a large reflection from the large-end truncation. This in turn requires that the fields along the antenna structure decay more rapidly than inversely with distance. This last condition is met only when the far field pattern vanishes in the direction of the antenna structure.

In attempting to explain this property and more generally to understand the operation of log-periodic antennas it is found useful to think of the antenna as a locally periodic structure whose period varies slowly, increasing linearly with distance from the apex. This report will develop the idea by describing the results obtained experimentally with a number of uniformly periodic antennas. A more rigorous and detailed examination of several of the structures will be contained in subsequent reports.

2 PERIODIC STRUCTURES

Consider first the somewhat idealized problem of the diffraction of a plane wave by an infinite, periodic grating. Let the z-axis lie in the plane of the grating, perpendicular to the lines of the grating as shown in Figure 1. It is well known that a number of diffracted waves are produced. If the incident wave has a propagation vector \vec{k} with a projection β_0 on the z-axis, the diffracted wave of order n will have a propagation vector \vec{k}_n with a projection

$$\beta_n = \beta_0 - np \quad n\text{-integer} \quad (1)$$

on the z-axis. In this formula $p = \frac{2\pi}{a}$ where a is the period of the grating.

The wave characterized by β_0 is the fundamental wave; those described by β_n ($n \neq 0$) are the space harmonics. Only a finite number of the vectors \vec{k}_n are real, those for which

$$|\beta_n| < k = \omega\sqrt{\mu\epsilon} \quad (2)$$

Equation (2) defines the "visible range" of the space spectrum which represents waves propagating obliquely with respect to the grating axis. The length of the propagation vector \vec{k}_n for these oblique waves is equal to the intrinsic phase constant of the medium, k , as shown in Figure 1. For all waves outside the visible range the components of the propagation vectors normal to the surface are imaginary and the waves are evanescent waves traveling along the plane of the grating. For a finite grating the beams produced by the oblique waves are not infinitely sharp. The width of beams nearly broadside to the grating is approximately the inverse of the length of the grating measured in wavelengths. The relative amplitudes of the various beams depend on the detailed form of the lines of the grating.

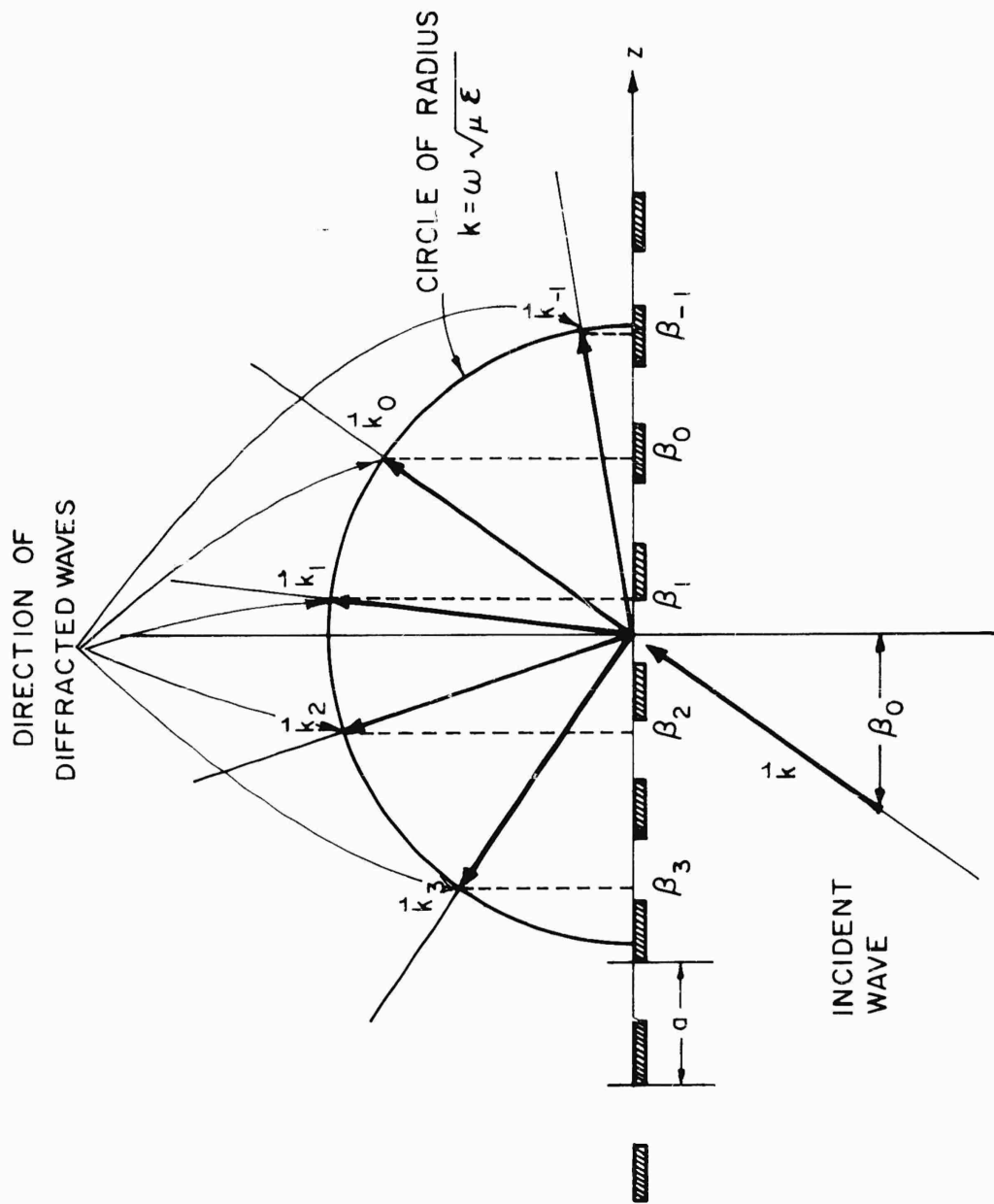


Figure 1. Diffracted waves produced by a periodic grating

The same description applies to the diffraction of an incident wave having a complex propagation vector or to any wave guided along an infinite grating and having a phase constant β_0 in that direction. For example, Figure 2 shows a dielectric slab bounded on one side by a conductor and on the other side by a grating. If this supports a slow fundamental wave ($\beta_0 > k$) and if the period a is small, p will be large and all the $\beta_n = \beta_0 - np$ (for n positive or negative integer) will be larger than k . None of the diffracted waves has a real direction of propagation which means that no oblique wave occurs. If now the spacing is increased, p will become smaller and all the points β_n will move toward β_0 . The space harmonic phase constant β_1 which is nearest the visible range will eventually obtain a magnitude less than k . When $\beta_1 = -k$ the diffraction occurs in the negative direction (backward wave). If the spacing is further increased the points β_2 , then β_3 , and so on will enter the circle of radius k , and several oblique waves can result, propagating at angles from the z -direction which may be obtained from the construction shown in Figure 2.

$$\cos \theta_n = \frac{\beta_n}{k} \quad (3)$$

Since the oblique waves carry power away from the grating, the fields near the grating will decrease as a function of distance along the structure. Thus the propagation constants of the fundamental and all of the space harmonics will be complex whenever any of the space harmonics correspond to an oblique wave.

A compact representation of the frequency dependence of the propagation constant is afforded by a plot of frequency versus phase constant. These plots are sometimes called $\omega - \beta$ or $k - \beta$ diagrams or Brillouin diagrams. In this report the ordinate will be the period measured in free-space wavelengths, and the abscissa will be the period measured in wavelengths along the structure.

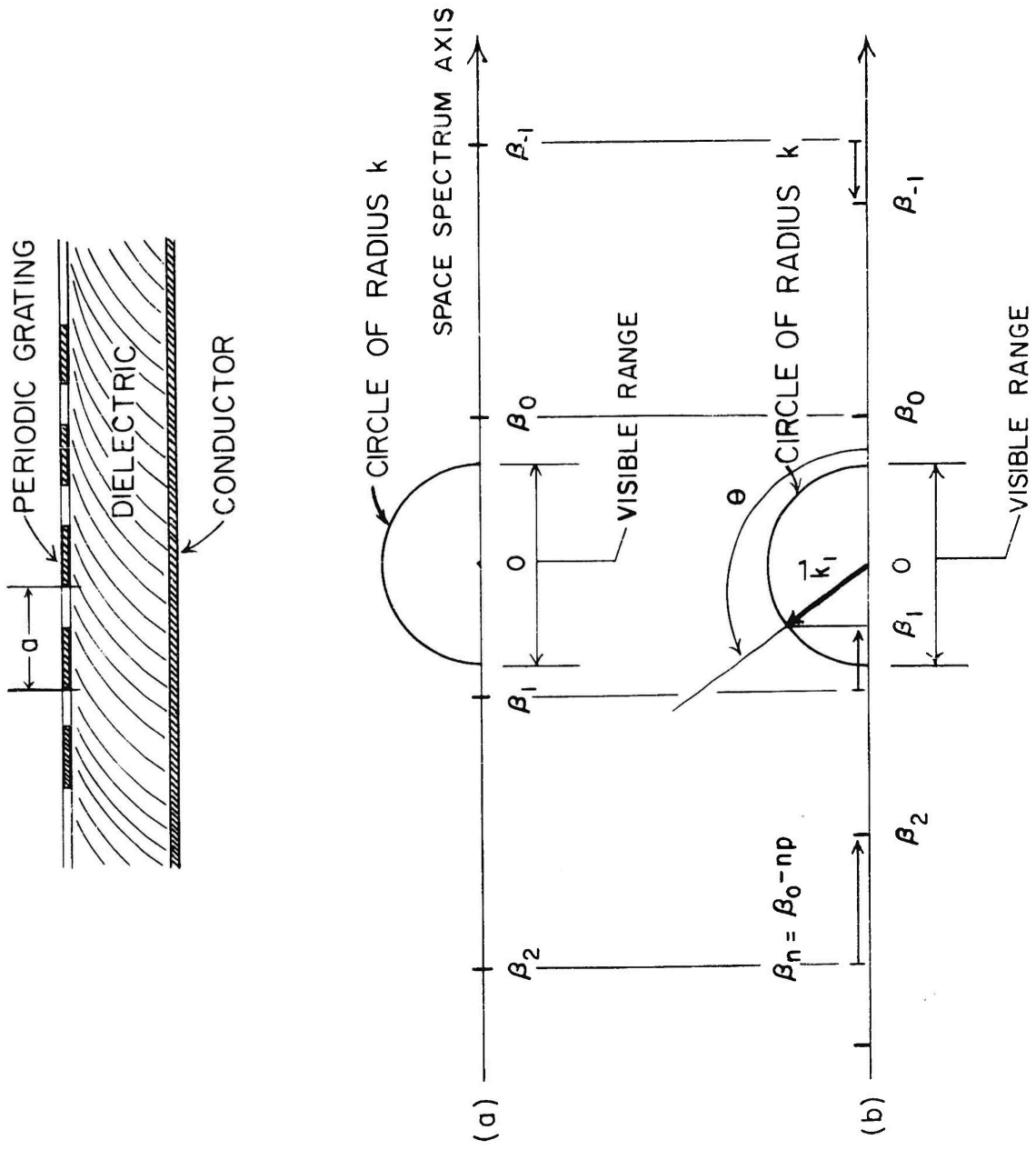


Figure 2. A periodic grating imposed on a slow wave transmission system

If division by p is performed, Equation (1) becomes

$$\frac{a}{\lambda_n} = \frac{a}{\lambda_0} - \lambda_n - \text{wavelength of } n\text{th wave} \quad (4)$$

so that the representation of each space harmonic is displaced one unit from that of the fundamental. The condition that all space harmonics be outside the visible range is expressed by

$$\left| \frac{a}{\lambda_n} \right| = \left| \frac{a}{\lambda_0} - n \right| > \frac{a}{\lambda} \quad \text{for all } n$$

and in particular

$$\frac{a}{\lambda} < \frac{a}{\lambda_0} < 1 - \frac{a}{\lambda} \quad (5)$$

This condition is satisfied by all points inside the triangle on the Brillouin diagram shown in Figure 3. A fundamental slow wave is represented by a line whose slope is less than one. For small values of a/λ , all space harmonics are far from the visible range, but, as points on the slow wave line approach the right-hand edge of the triangle, the first space harmonic approaches the visible range, and conditions for backward wave radiation are established. The shape of the fundamental phase curve will be modified in the vicinity of the edge of the triangle by coupling between the first space harmonic and a free space wave directed along the structure toward the feed point. Coupling between evanescent space harmonics may also occur within the triangle, distorting the straight line plot shown in Figure 3. The nature of the phase curve in the Brillouin diagram must, of course, be determined for each structure.

Since the propagation constants become complex when a space harmonic enters the visible range, the currents are attenuated. It is therefore possible to build a periodic structure long enough so that the currents are negligible

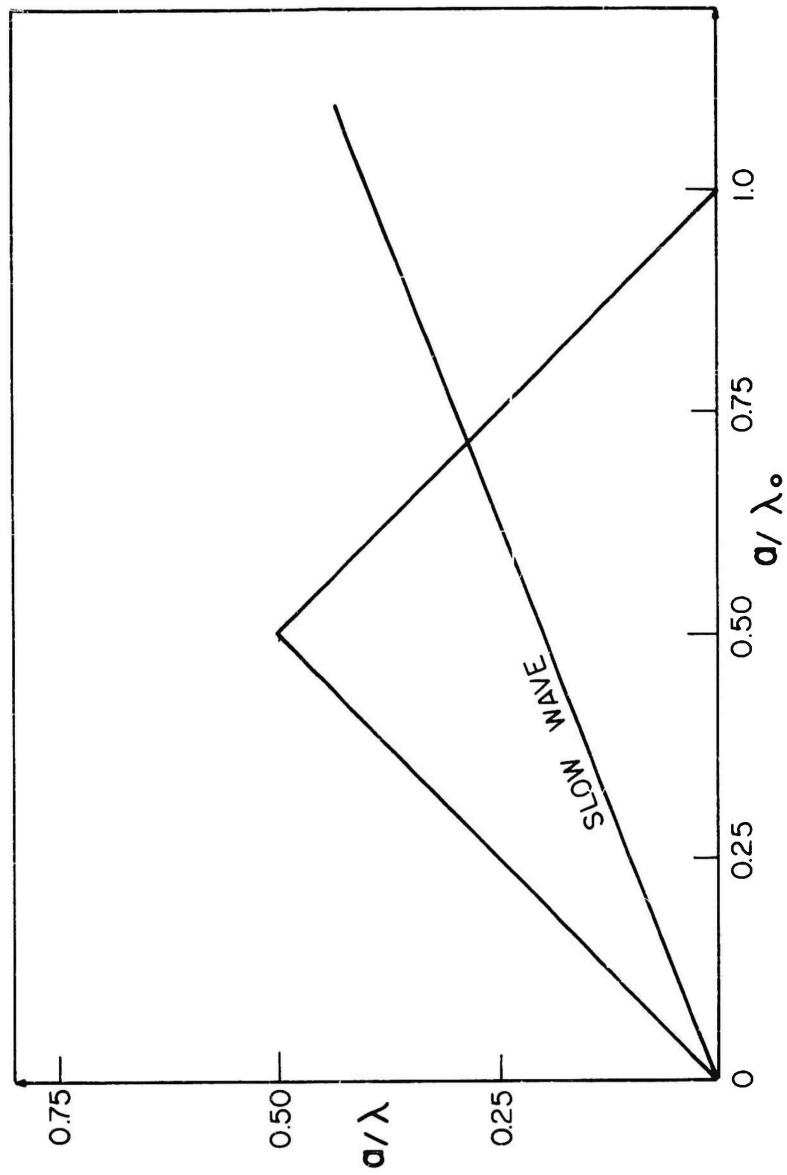


Figure 3. A Brillouin diagram showing a slow wave phase constant

at the end. This type of current distribution is very useful for antennas. Again assuming a single fundamental wave the amplitude will be of the form $e^{-\alpha z}$ which gives rise to a radiation pattern given by

$$P(\theta) = \frac{1}{1 - jx} \quad (6)$$

where

$$x = \frac{k}{a} \left(\frac{\beta}{k} - \cos \theta \right)$$

Unlike the pattern of a uniform amplitude distribution of length L given by

$$P(\theta) = \frac{\sin \psi}{\psi}$$

where

$$\psi = kL \left(\frac{\beta}{k} - \cos \theta \right)$$

the pattern of Equation (6) has no side lobes. When forward waves are used to produce the radiation field all of the antenna elements are excited by the radiation field. The antenna current distribution in that case experiences a sharp discontinuity at the point where the antenna conductors terminate, as well as at the feed point. When the radiation is due to a backward wave, however, the currents decay with distance from the feed-point and the discontinuity at the opposite end of the antenna will be negligible if the antenna is of sufficient length.

If the antenna is considered as an array of discrete sources instead of the continuous aperture treated above, the pattern is given by

$$P(\theta) = \frac{1}{1 - z} \quad (7)$$

where

$$z = e^{-\alpha a - jka \left(\frac{\beta}{k} - \cos \theta \right)}$$

The magnitude of Equation (7) is presented in Figure 4 where the exponent is given by

$$-A + j\varphi = -\alpha a + jka\left(\frac{\beta}{k} - \cos \theta\right) \quad (8)$$

The curves of Figure 4 represent universal array factors for arrays having exponentially tapered excitation. The polar plots of radiation patterns for arrays of isotropic sources with this excitation can be obtained from these curves by applying the transformation between z and θ given in Equation (7). Several patterns deduced from Equation (7) for $\beta/k = 4$ with $A = 0.3$ and $A = 0.6$ are presented in Figure 5. The first pattern ($\frac{a}{\lambda} = 0.187$) is in the excess phase shift range of the Brillouin diagram, i.e., a/λ_0 is inside the triangle. At $\frac{a}{\lambda} = 0.2$ the first space harmonic is at the boundary of the visible range. The following patterns depict the frequency scanning that would be expected if the slowness factor, β/k and the attenuation factor α both remain constant with frequency

In a log-periodic grating the period increases progressively with distance along the structure. As a wave propagates along the grating it will successively reach points where the various conditions outlined above will occur. If the rate of increase of the period is slow, each small section of the structure will produce about the same complex of diffracted waves as if it were uniformly periodic with the average period of the log-periodic section. For the small periods near one end of the log-periodic grating all space harmonics propagate along the structure. Some distance away, however, the period is correct for a backward wave to enter the visible range. For a slightly larger period this harmonic produces an oblique wave. In this region of the structure the near field will be attenuated as all the space harmonic propagation constants become

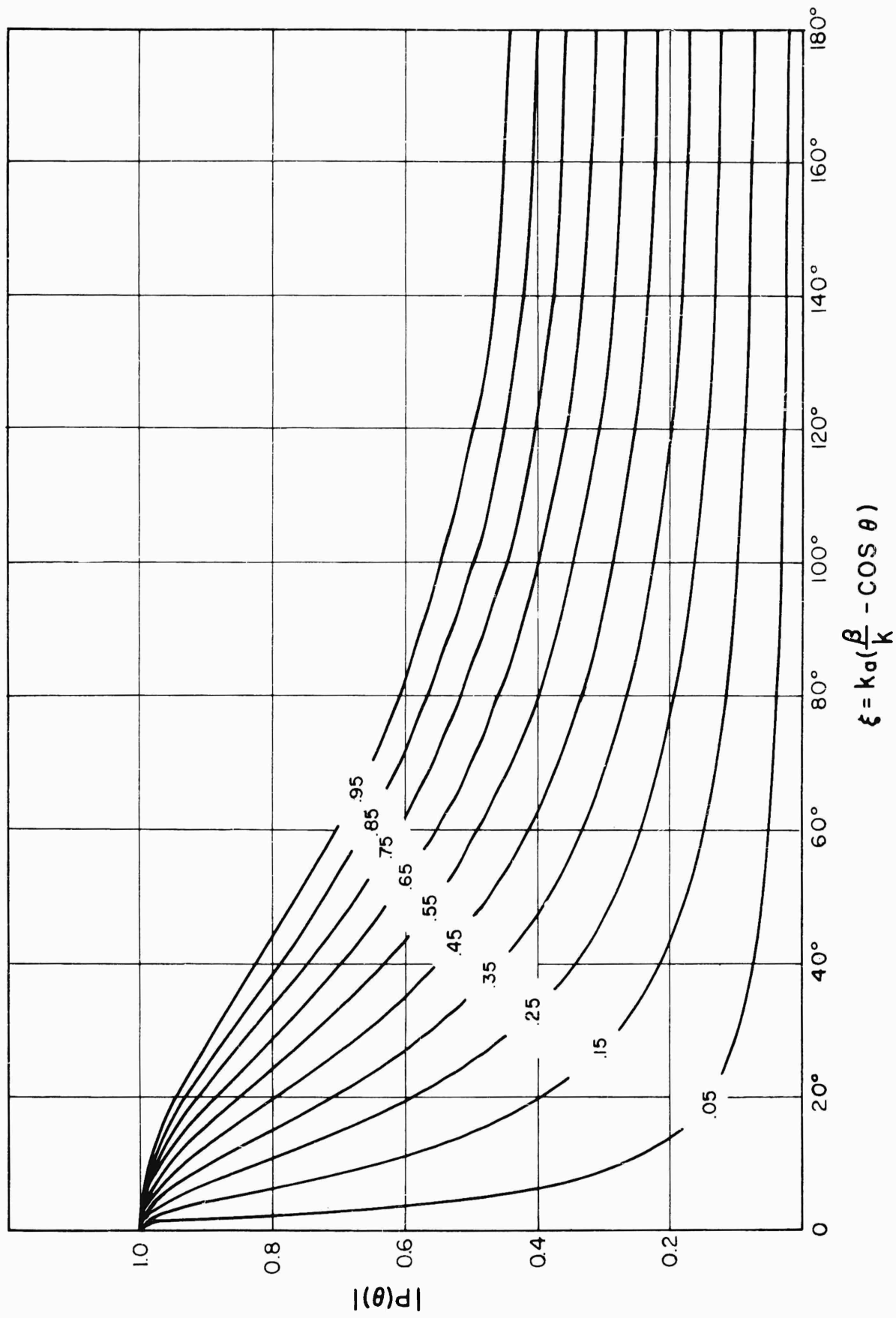


Figure 4. Universal pattern chart for exponential current distributions on discrete arrays 16

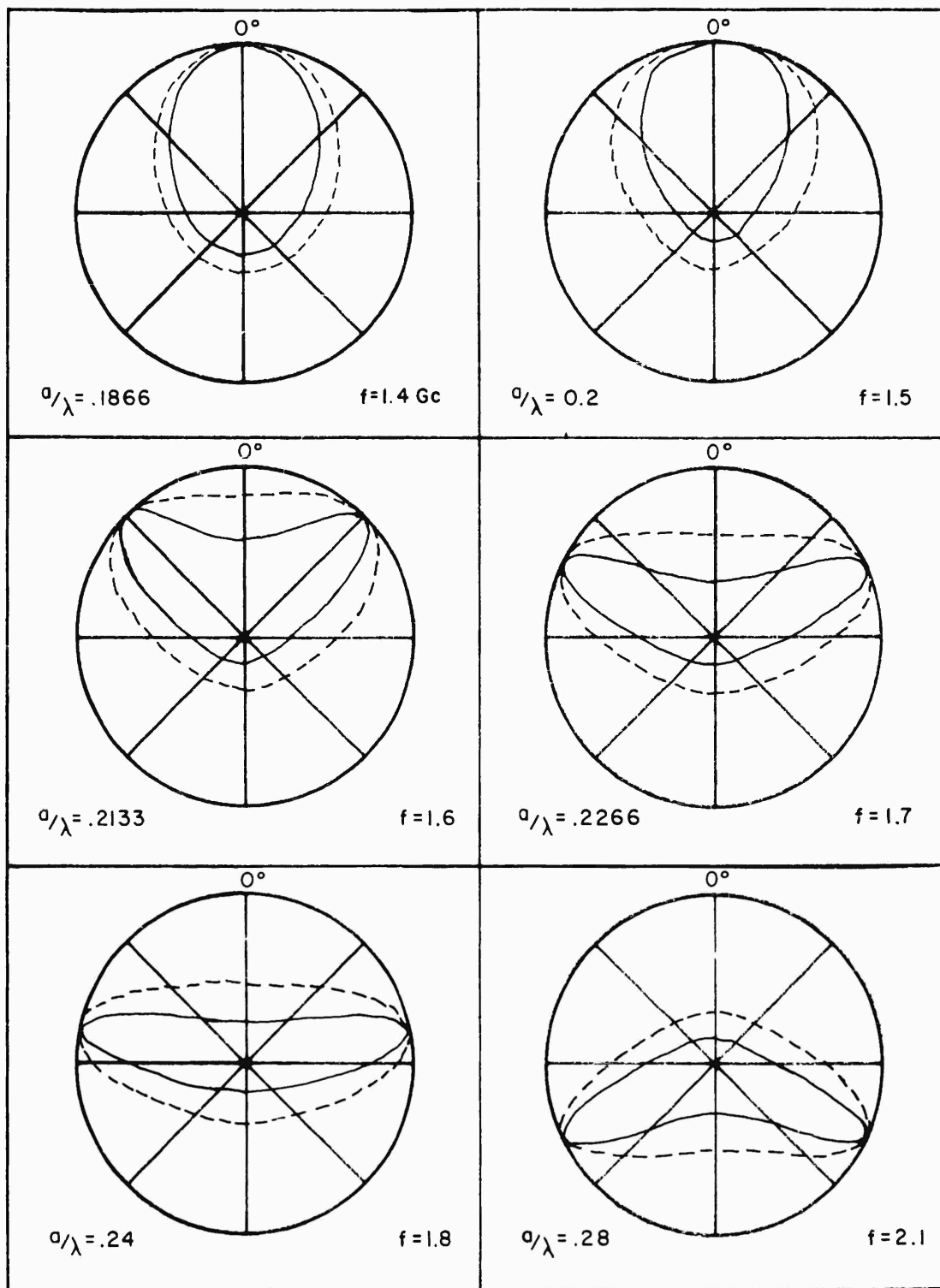


Figure 5. Radiation patterns typical of exponential taper slow wave current distributions $\Lambda = 0.3$ ——— $\Lambda = 0.6$ - - - -

complex numbers. If the coupling is strong enough, the attenuation of the near fields will be almost complete before the periodicity (which results in a backward wave) changes. If the coupling is too weak, the currents will penetrate this region and will produce endfire radiation making it impossible to truncate the structure satisfactorily. When the frequency is increased the region where the backward wave is produced (which has been called the active region) will move in the direction of decreasing period. When several cells of the periodic structure are included in the active region, the variations with frequency may be quite small, while too large coupling may allow considerable variation within a log-period.

3. HELIX-FED MONOPOLE ARRAY

An array of identical elements (not necessarily the lines of grating) placed periodically along a transmission line and coupled to it will also produce a radiation pattern which can be analyzed as a sum of waves having the $e^{-j\beta_n z}$ dependence on the z coordinate. This may be deduced from Floquet's theorem. While in general several values of β_0 , and a sum of the corresponding fields would be required to describe the situation completely, in many practical cases one of these values will correspond to a dominant field and the others can be neglected.

As an example consider the array of monopole antennas connected to a helical delay line as shown in Figure 6. The fundamental wave phase constant can be approximated by considering the current to propagate along the helical wire with free-space velocity. This yields

$$\beta_0 = k \csc \psi \quad (9)$$

where ψ is the pitch angle of the helix. Since $\csc \psi > 1$ the fundamental wave is slow.

If the influence of the monopoles on the fundamental wave phase constant is neglected, the element phasing of the array may be approximately determined by periodically sampling the phase of the slow fundamental wave. The sampling rate determines what higher order waves (space harmonics) may be associated with the structure, some of which might be in the visible range. Several waves that agree in phase with a particular sampling of the slow fundamental wave are shown in Figure 7. Because of the multiple-valued nature of phase, the possible values of phase for the fundamental wave are represented by a

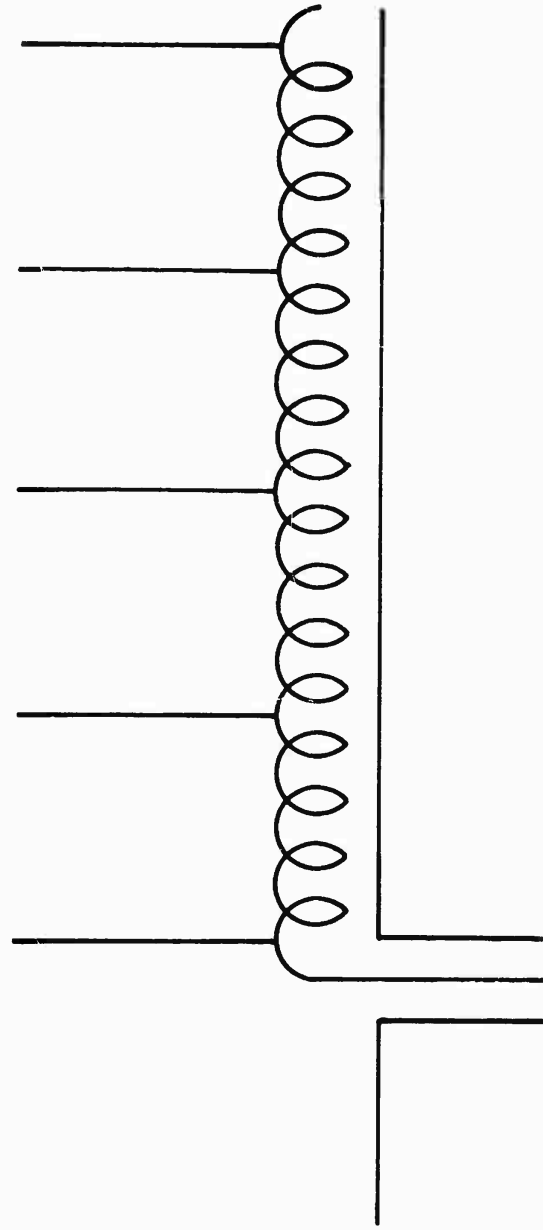


Figure 6. A periodic monopole array with a helical delay line feed

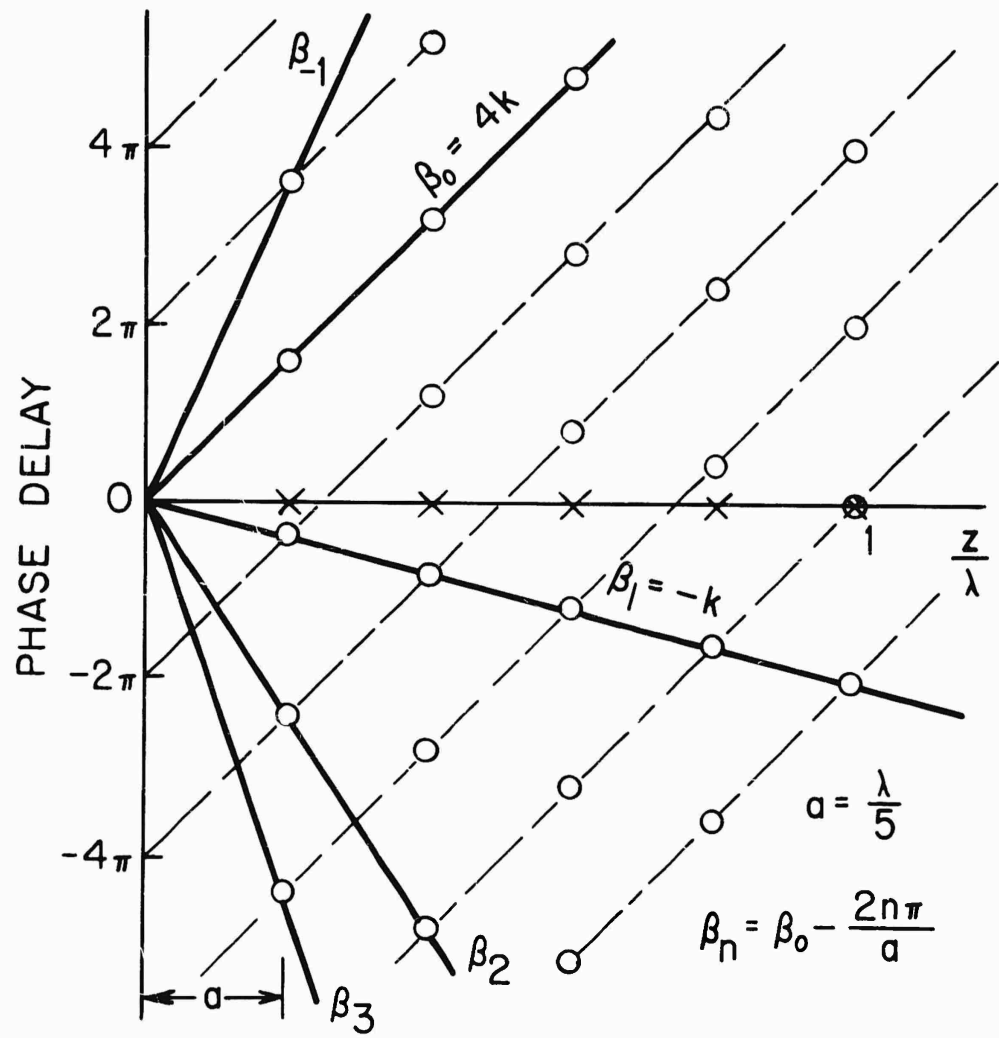


Figure 7. Space harmonics for sampling a slow wave at a specific rate

family of parallel lines displaced by $2n\pi$ radians along the phase axis. Such a family of lines with slope $\beta_0 = 4k$ is shown in Figure 7. We could characterize this fundamental wave by the relative slowness factor, $\beta_0/k = 4$. The phases obtained by sampling with a period $a = \lambda/5$ are indicated by small circles on the phase lines for the fundamental wave. Joining the first column of these points to the origin yields the phase lines of the space harmonics. It is noted that the first space harmonic ($n = 1$) in Figure 7 is a backward wave. All other space harmonics are removed from the visible range. The condition illustrated in Figure 7 is necessary for backfire radiation $\beta_1 = -k$. Other conditions are readily discernable. For broadside, $\beta_1 = 0$ and for endfire, $\beta_1 = k$.

To check the validity of the foregoing simple theory, helix-fed monopole arrays such as that shown in Figure 8 were constructed and tested. The pitch angle of the helix was 18.4 degrees so that the fundamental wave phase constant ignoring the loading effect of the monopoles would be approximately $3.2k$. The helix was wound with number 18 wire on a 9.16-inch diameter fiber tube. On UPM-2 (Uniform Periodic Monopole model 2) 5.7-cm elements were placed every three turns of the helix so that the period of the radiating structure was 4.5 cm. Typical measured azimuthal radiation patterns are shown in Figure 9. Below 1100 Mc the patterns were poorly formed in contrast to the nicely-shaped beams obtained when the backward wave appears. Backward wave radiation is predominant from 1100 to 1500 Mc where the scanning of the beam begins to be discernable. At 1600 Mc two maxima occur at angles with respect to the antenna axis. From the directions of these maxima (52 degrees off axis) the fundamental wave phase constant can be computed as $3.55k$. Evidently then the additional slowing of the fundamental wave is due to the monopoles. The radiation patterns at higher frequencies yield further values of the wavelength of the fundamental wave as given in Table I.

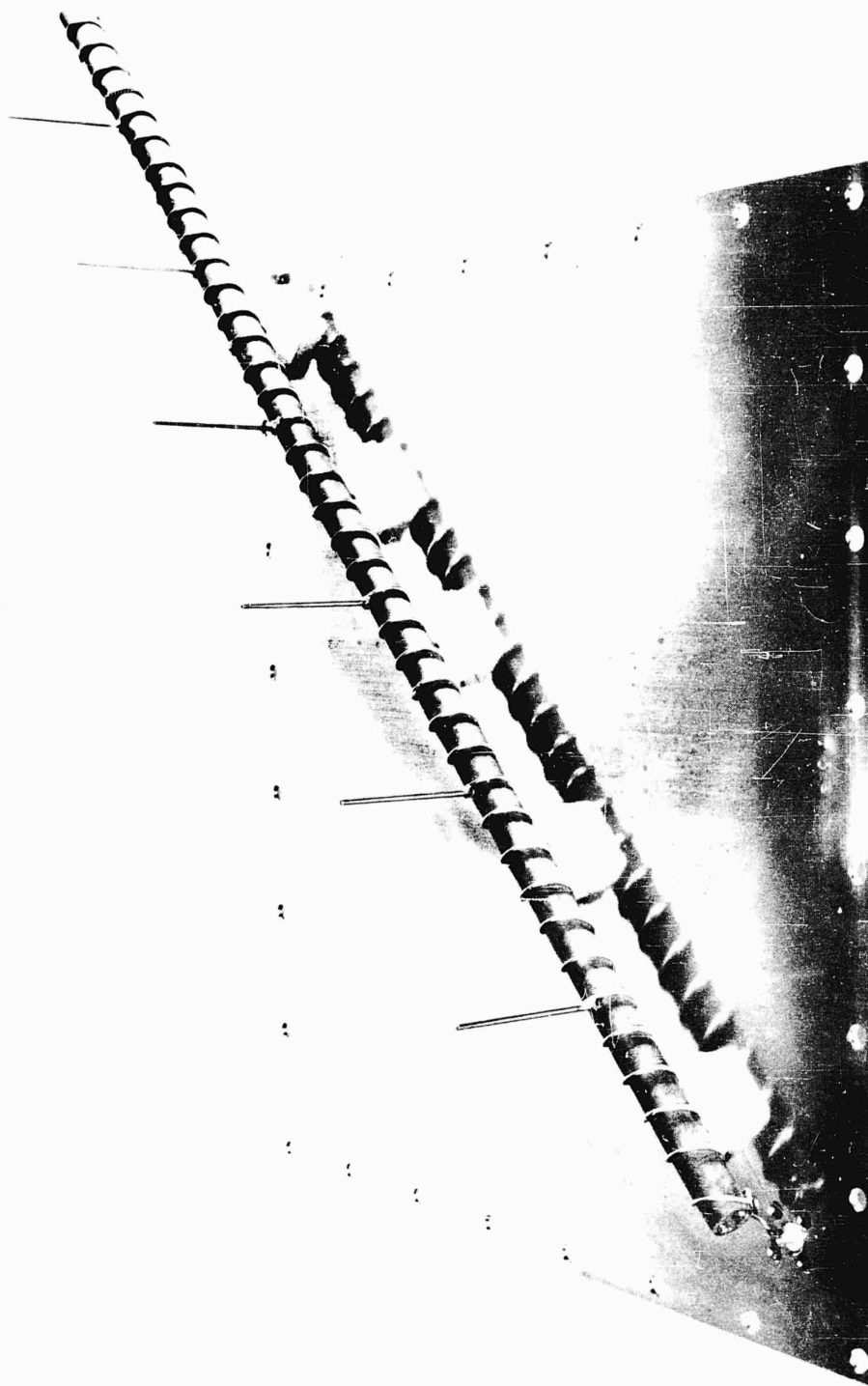


Figure 8. Experimental model of a helix-fed monopole array

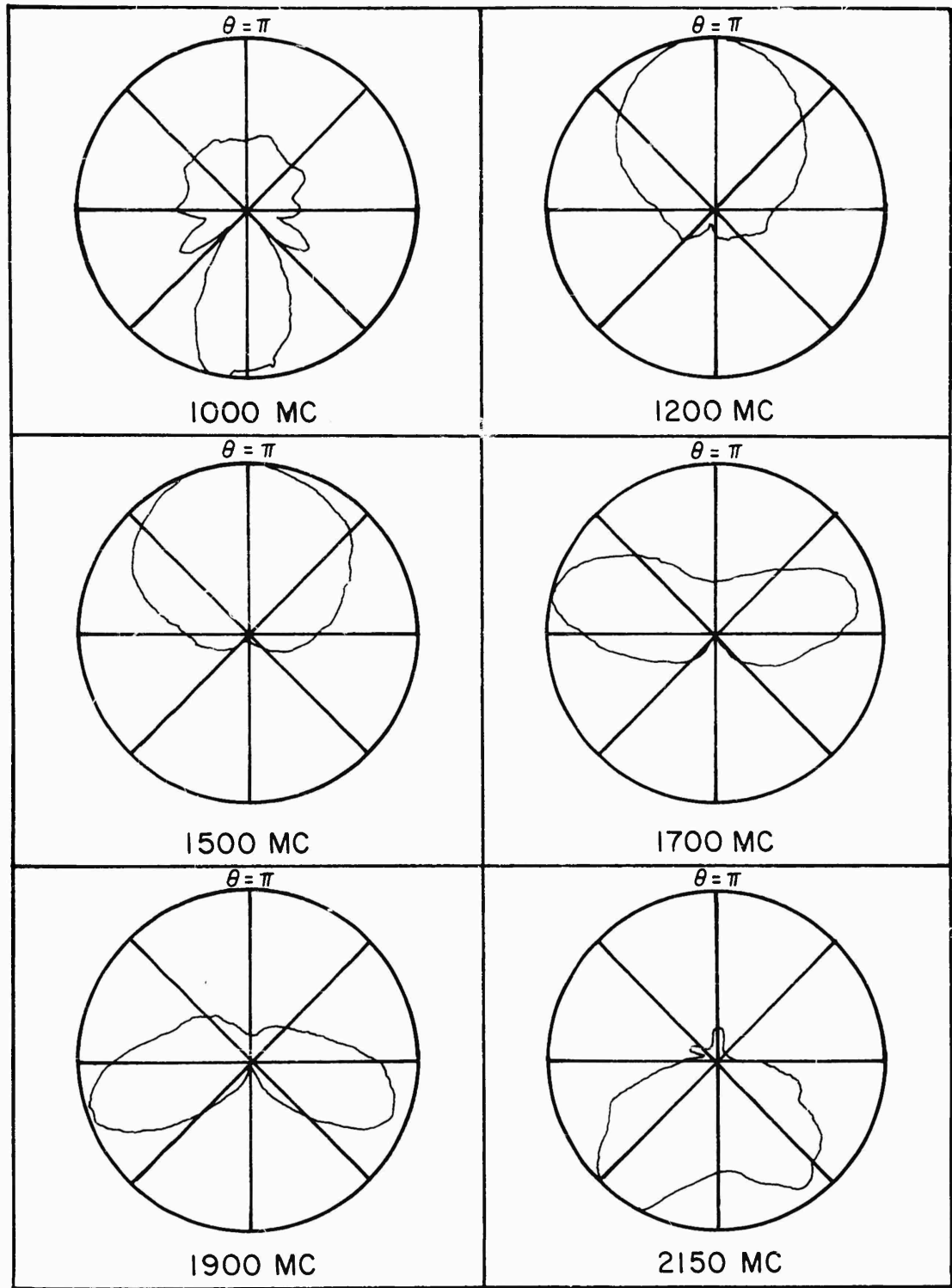


Figure 9. H-plane radiation pattern of a helix-fed periodic monopole array

TABLE I

Beam scanning angle antenna model UPM-2, $a = 4.5$ cm

<u>Frequency Mc</u>	a/λ	<u>Angle Max.</u>	a/λ_0
1600	0.240	128	0.851
1650	0.247	114	0.900
1700	0.254	105	0.932
1750	0.262	96	0.971
1800	0.270	86	1.02
1850	0.278	80	1.05
1900	0.285	72	1.09
1950	0.292	63	1.13
2000	0.300	55	1.17
2050	0.308	51	1.19
2150	0.322	35	1.26
2700	0.405	152	1.64
2900	0.435	121	1.78

The results listed in Table 2 are for Antenna UPM-2-1/2 which is the model that resulted when alternate elements were removed from UPM-2. All of its parameters are the same as the previous antenna except that the spacing between elements has been doubled.

The above results for the helix fed monopoles lead to the Brillouin diagram of Figure 10. Note that the same ordinate for both antennas occurs at a frequency for UPM-2-1/2 that is half that for UPM-2. This is a direct consequence of doubling the spacing of the monopoles. The broken line on the diagram represents the assumption that the phase velocity measured along a turn of the feed helix is that of free-space; i.e., $\beta_0 = k \csc \psi$. The effect of monopole loading on the propagation constant is shown by the departure of a phase curve from this line. As expected this effect is greater for UPM-2 than for the model with only half as many elements.

It should be noted that between 2150 and 2700 Mc in the case of UPM-2 and between 1200 and 1600 Mc in the case of UPM-2-1/2 there is another frequency band in which no space harmonic is in the visible region. The first space harmonic has scanned from backfire to endfire and departed from the visible region. However, at 2700 Mc (for UPM-2) and 1600 Mc (for UPM-2-1/2) the second space harmonic has entered the visible region. If the fundamental wave velocity is slow enough, the second space harmonic will also scan from backfire to endfire. The presence of the second region devoid of oblique waves is indicated in Figure 10 by the second triangle bounded by the lines

$$\frac{a}{\lambda_0} = 1 + \frac{a}{\lambda}$$

and

$$\frac{a}{\lambda_0} = 2 - \frac{a}{\lambda}$$

TABLE II

Beam scanning angle antenna model UPM-2-1/2, $a = 9$ cm

<u>Frequency Mc</u>	<u>a/λ</u>	<u>Angle Max.</u>	<u>a/λ_0</u>
800	0.240	128	0.850
850	0.255	107	0.926
900	0.270	100	0.952
950	0.285	100	0.953
1000	0.300	92	0.993
1050	0.315	73	1.10
1100	0.330	61	1.16
1150	0.345	53	1.21
1200	0.360	44	1.26
1600	0.478	132	1.68
1700	0.508	110	1.78
1800	0.538	87	2.03
1900	0.568	70	2.19
2000	0.600	53	2.36

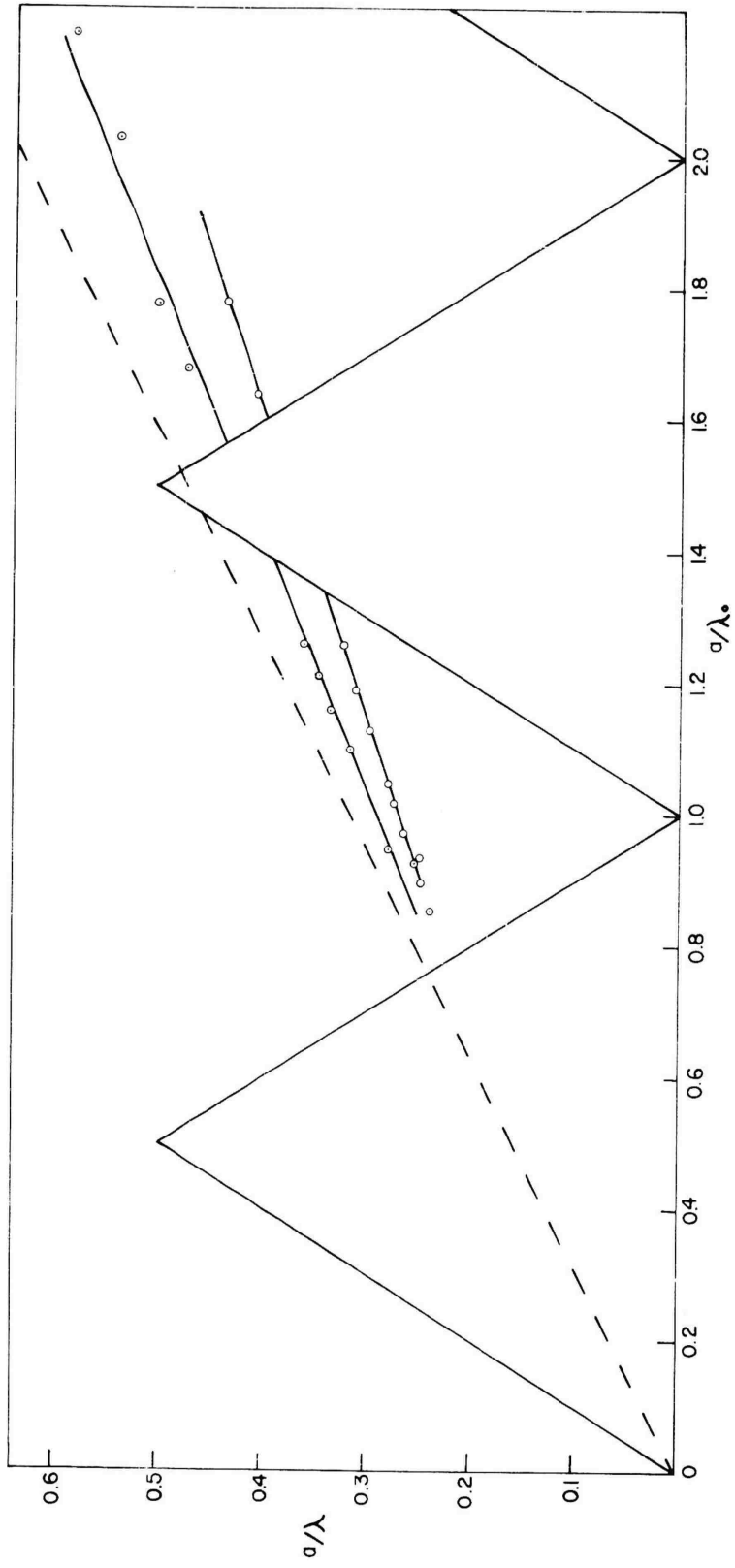


Figure 10. Brillouin diagram for helix-fed monopole arrays

Several tapered or log-periodic models of the helix-fed monopole array were tested with tapers defined by the taper angle α_t in the range from 20 degrees to 6 degrees. The angle α_t is the angle between the axis or center line of the structure and a co-planar line through the outer extremities of the structure as shown in Figure 11. These structures did not show frequency-independent properties in the range of tapers tested. The performance of models with the smaller tapers, however, was more nearly constant with frequency than that of models with larger taper.

As was indicated in the preceding section, the poor performance of the truncated tapered model for all but the smallest tapers is an indication of weak coupling between the feed wave and the radiated waves. Such loose coupling allows an overly large active region to form. When elements associated with a space harmonic inside the visible region carry appreciable current, energy will be radiated in directions other than backfire. In the case of tight coupling the attenuation constant becomes sizable even inside the triangle of Figure 3, and the elements with appreciable current are all associated with a backward space harmonic. This condition of loose coupling in the case of the uniform periodic structure is indicated by the formation of distinct beams as the frequency is scanned since a large active region is required to form these relatively narrow beams. Where coupling is stronger, the active region on the uniform periodic structure is much smaller giving very broad beams which tend to coalesce into a single beam which widens as frequency is increased. This characteristic is well illustrated by the antennas of the following section.

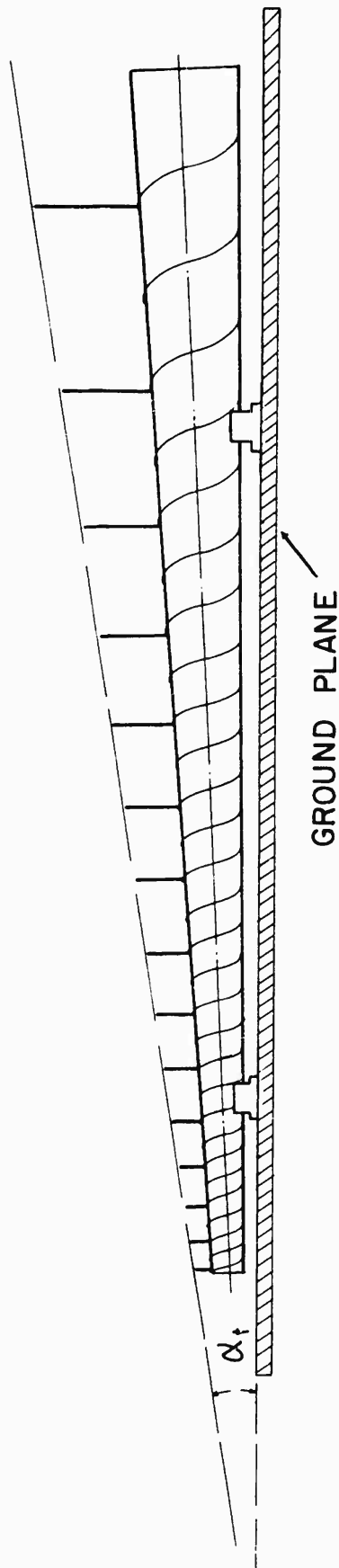


Figure 11. A log-periodic helix-fed monopole array

4 THE ZIG ZAG AND HELIX ANTENNAS

The zig zag and the helical wires shown in Figure 12 are uniformly periodic versions of antennas which have previously been well studied in the log-periodic version. The bifilar helix corresponds to the conical log-spiral antenna³. The log-periodic zig zag^{4,5,6} has been operated as a bifilar antenna in free space and as a horizontally polarized antenna over a conducting ground screen. The bent log-periodic zig zag⁷ has been shown to be a useful vertically polarized antenna over a conducting ground screen. These antennas are constructed of conducting wire following a zig zag or helical path of pitch angle ψ and period a as indicated in Figure 12.

For the purpose of computing the radiation field produced by oscillating currents in these wires, these periodic structures can be considered to be linear arrays where each cell of the structure is an element of the array. Computation of the array factor depends upon the phasing between cells. Once again the assumption of a traveling wave of current on the zig zag or helix proves accurate enough to be useful. If we assume a current wave

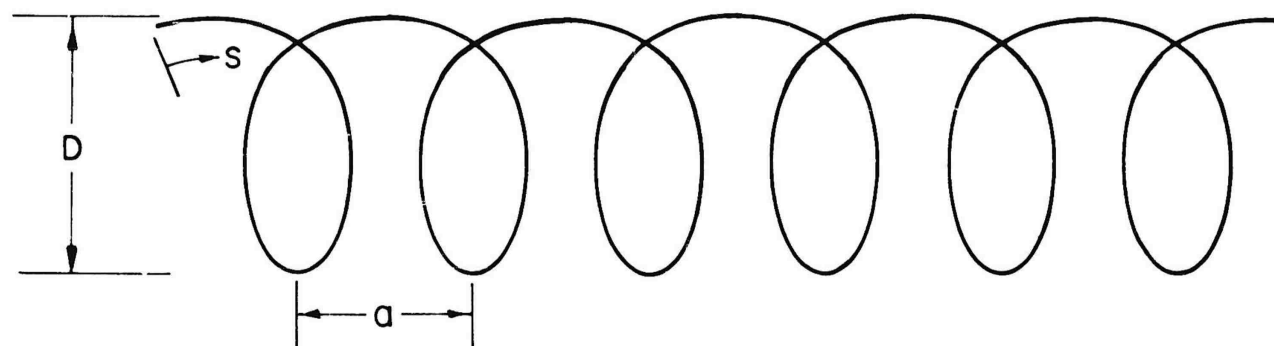
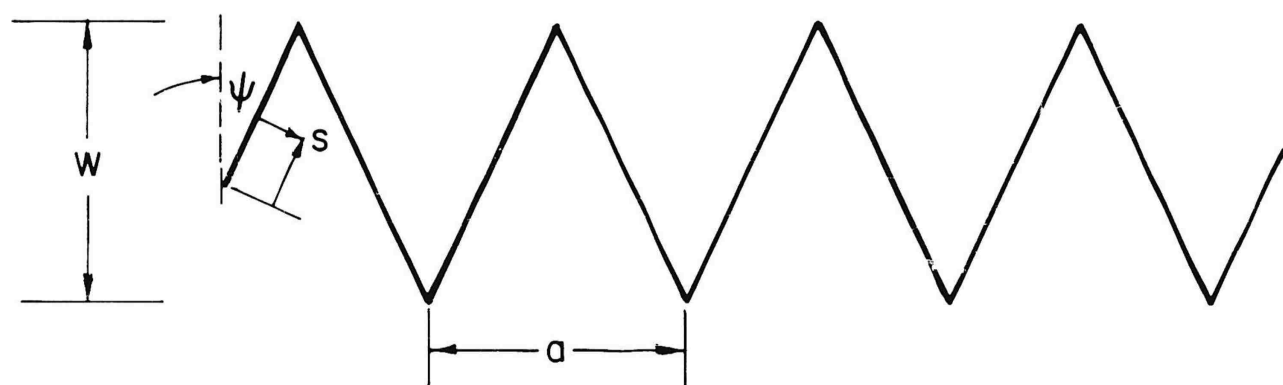
$$I(s) = e^{-jks} \quad (10)$$

where k is the free-space phase constant and s is the distance measured along the wire, then the phasing between cells depends upon the length of wire contained in each cell. The phase delay can be characterized by the phase constant

$$\beta_0 = k \csc \psi$$

for the fundamental wave on these structures as was obtained in the preceding section. Division by p yields

$$a/\lambda_0 = \frac{a}{\lambda} \csc \psi \quad (11)$$



$$\tan \psi = \frac{a}{\pi D}$$

Figure 12. Periodic zig zag and helical wire structures

and by substituting Equation (11) in Equation (5) the condition for backward wave radiation predicted by this approximate theory is seen to be

$$\frac{a}{\lambda} = \frac{1}{1 + \csc \psi} \quad (12)$$

The validity of the foregoing theory, and in particular, the assumption concerning the phase constant of the fundamental wave has been tested by making measurements on monofilar and bifilar zig zag and helical antennas. The monofilar zig zag was fed against a short vertical wire as shown in Figure 13. A Microdot cable was used for the zig zag so that the energy is brought to the feed-point inside the antenna itself. For sufficiently high attenuation of currents along the zig zag, the currents on the outside of the feed cable will become negligible at a short distance from the feedpoint. By measuring the electric vector in the principal E-plane of the antenna, only the field due to the currents on the zig zag will be observed. The results of these measurements are shown in Figure 14. From the parameters of the zig zag

$$w = 7.76 \text{ cm}$$

$$a = 4 \text{ cm}$$

$$\psi = 14.5^\circ$$

the preceding theory would predict a backward space harmonic entering the visible range at frequency of 1.5 Gc. Backward wave radiation would be expected at frequencies somewhat below 1.5 Gc. since the antenna is finite. Strong coupling would also cause the onset of the backward wave at a lower frequency than predicted above. The highest gain should occur at these lower frequencies because of the excess phase shift and also because the small attenuation of current at these frequencies allows a deeper penetration of currents into the structure.

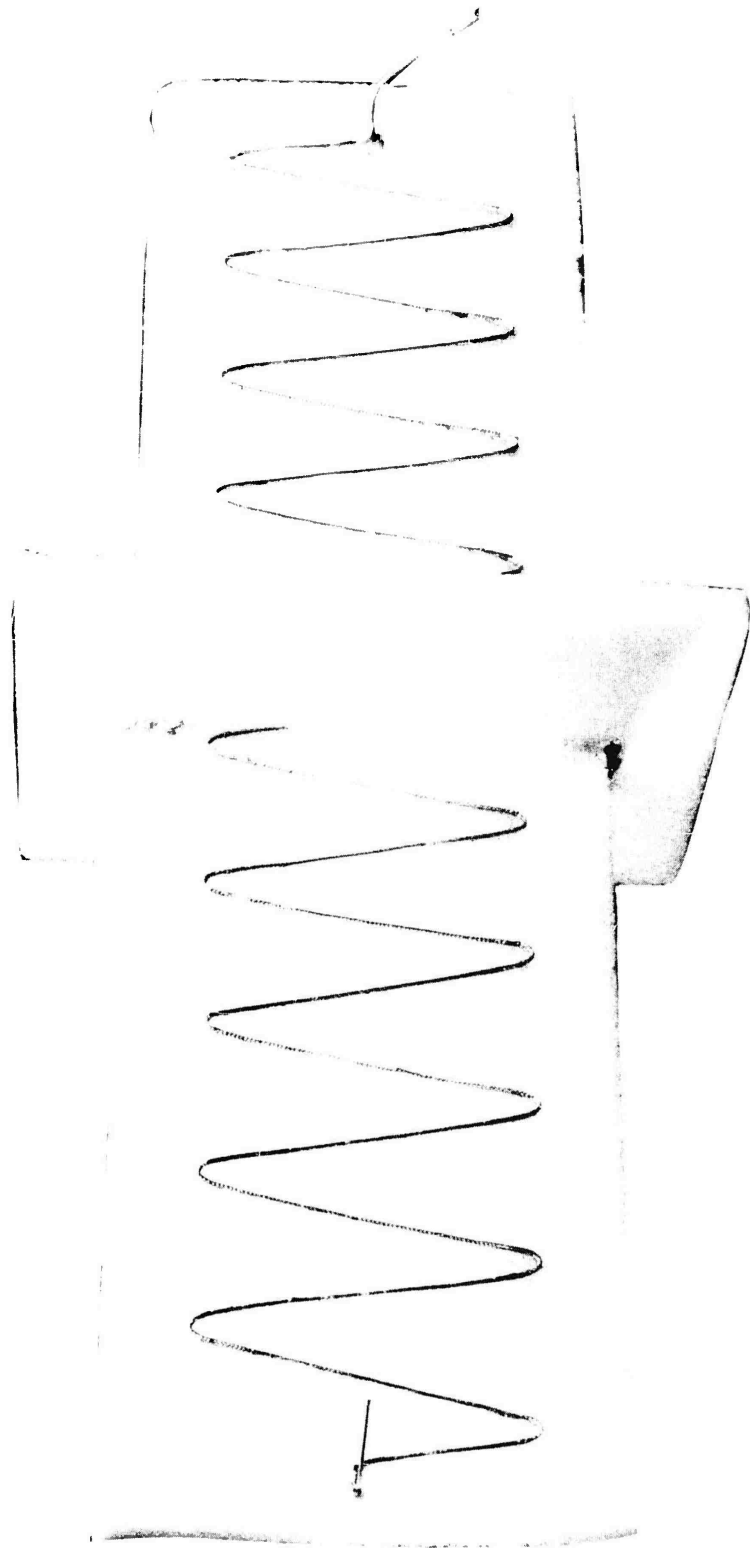


Figure 13. A monofilar zig zag wire antenna

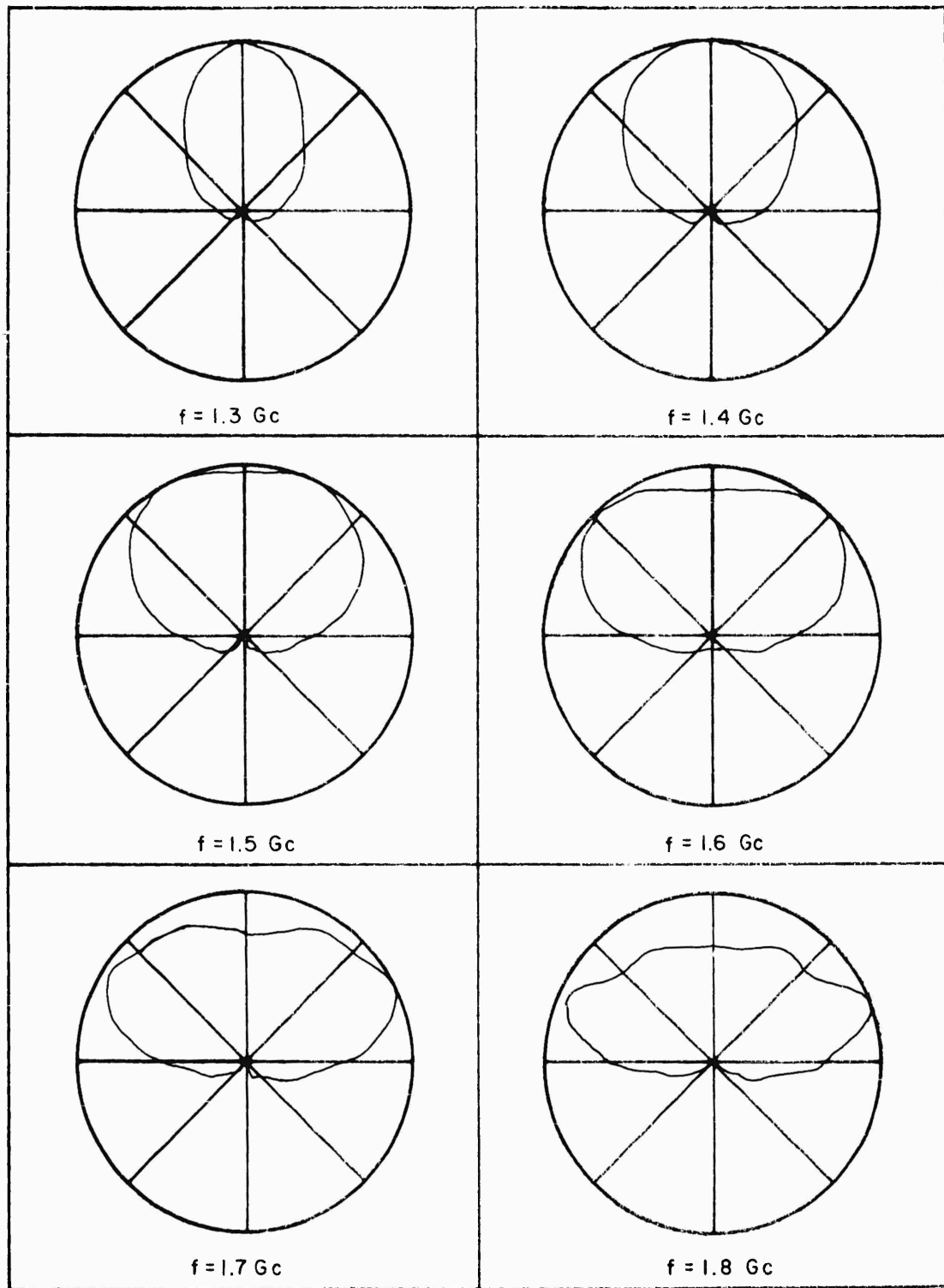


Figure 14. H-plane radiation patterns of a monofilar zig zag antenna

A number of bifilar zig zag antennas have also been tested. In this case the detector (bolometer or crystal) was mounted directly at the feedpoint of the antenna, and the antenna conductors were used to conduct the audio signal (1000 cycle square wave modulation) to the recorder. With this method of feed it was a simple matter to truncate the antenna at a number of successively decreasing lengths and obtain an estimate of the depth of penetration of currents on the antenna. The results of this series of measurements are shown in Figure 15. It is readily observed that the current is practically negligible beyond the fourth cell since the pattern obtained with 3 or more cells remains unchanged.

According to the approximate theory a bifilar zig zag antenna with the same parameters as given above would also have a backward space harmonic at 1500 Gc as before. Below this frequency the pattern should be highly directive, and above this frequency the maximum of the beam should scan away from backfire, through broadside, to endfire. The actual performance of this antenna is shown in Figure 16.

Several factors which are quantitatively unknown at present may serve to explain deviations from the simple theory. At the lowest frequency there is a small lobe in the endfire direction. This is probably evidence of end effect on the antenna. If the current wave on the structure is not sufficiently attenuated, it will be reflected from the open end of the structure. This reflected current wave will produce backward wave radiation, but in the endfire direction. The length necessary to avoid this end effect at any given frequency is dependent upon the attenuation of the currents. The dependence of the attenuation upon the parameters of several different structures is a subject of continuing investigation at our laboratory. This attenuation also governs the shape of the patterns at the higher frequencies.

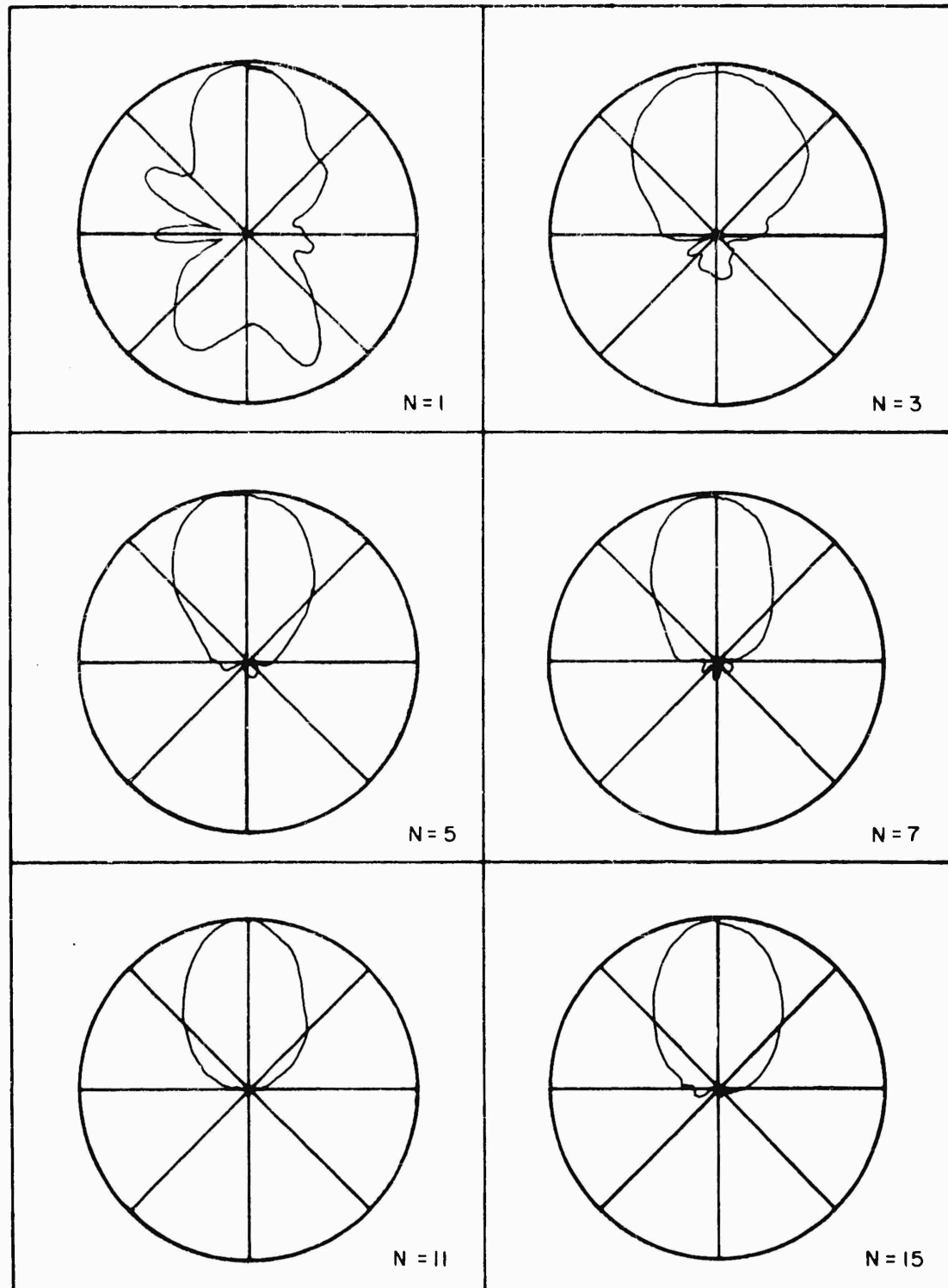


Figure 15. H-plane radiation patterns of a bifilar zig zag antenna as a function of number of cells

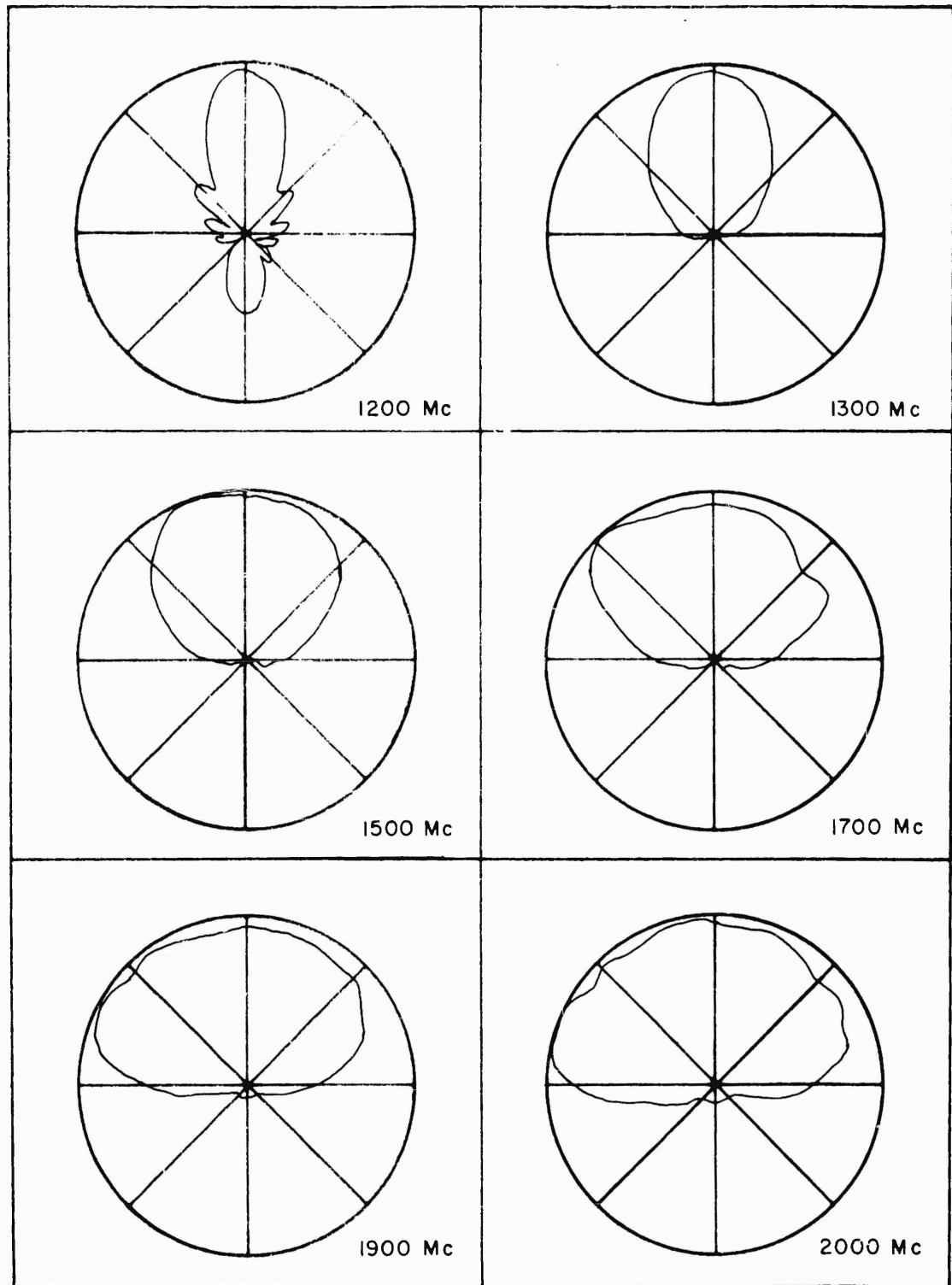


Figure 16a. H-plane radiation patterns of a bifilar zig zag antenna as a function of frequency
Pitch = 4 cm, Pitch width = 7.76 cm, Pitch angle = 15°

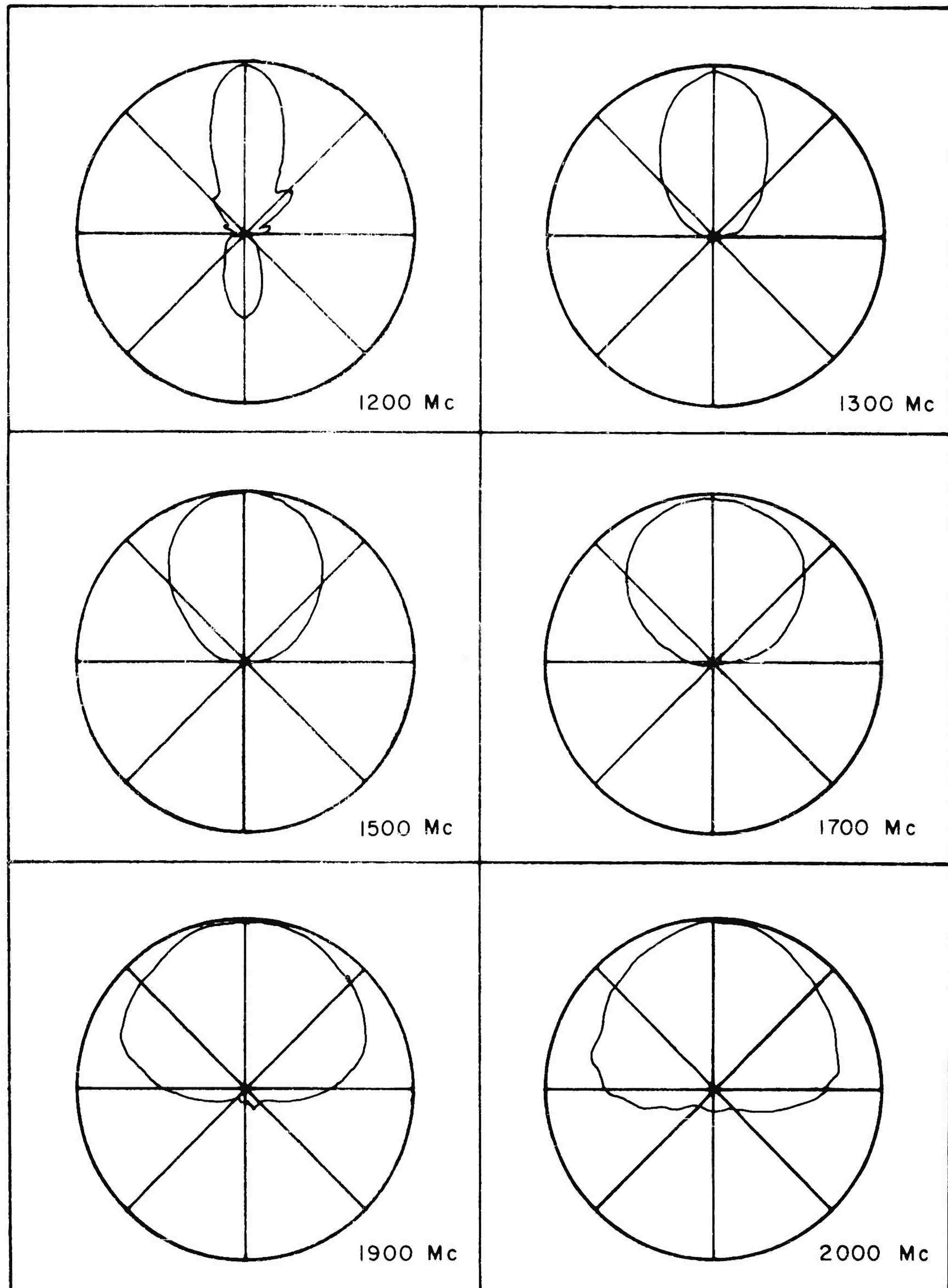


Figure 16b. E-plane radiation patterns of a bifilar zig zag antenna as a function of frequency
 Pitch = 4 cm, Pitch width = 7.76 cm, Pitch angle = 15°

As mentioned before the approach of space harmonics near to the visible range will modify the fundamental wave phase constant. This modification will involve a variation in the phase constant previous estimated by Equation (9) as well as the appearance of an attenuation constant. Furthermore, there may be other fundamental wave constants for the zig zag wire in addition to the one given by Equation (9) which we have assumed here to be predominant.

The measurements described above have also been made on monofilar and bifilar helix antennas and similar results have been obtained. The zig zag and helical antennas operating in the backfire condition have a smaller cross section in terms of the wavelength than the conventional endfire zig zag and helical antennas.

A Brillouin diagram for the bifilar zig zag is shown in Figure 17. The broken line results from the assumption of propagation at free-space velocity along the wire. This curve is given by

$$\frac{a}{\lambda_0} = \frac{a}{\lambda} \csc \psi$$

The measured points on Figure 17 were determined by establishing a standing wave on the zig zag and measuring the distance along the axis between nulls. The standing waves were produced by a short circuiting plate 60 inches square at the end of a zig zag with 15 cells. At $\frac{a}{\lambda} = 0.2$ the current distribution begins a transition from a standing wave to a rapidly decaying wave. Some typical records of the near field measurements are shown in Figure 18. A value of $\frac{a}{\lambda} = 0.2$ corresponds to the frequency at which backfire radiation patterns are observed from this zig zag antenna.

The Brillouin diagram in Figure 17 is different from others appearing in this report in that the phase curve does not start at the origin of the diagram.

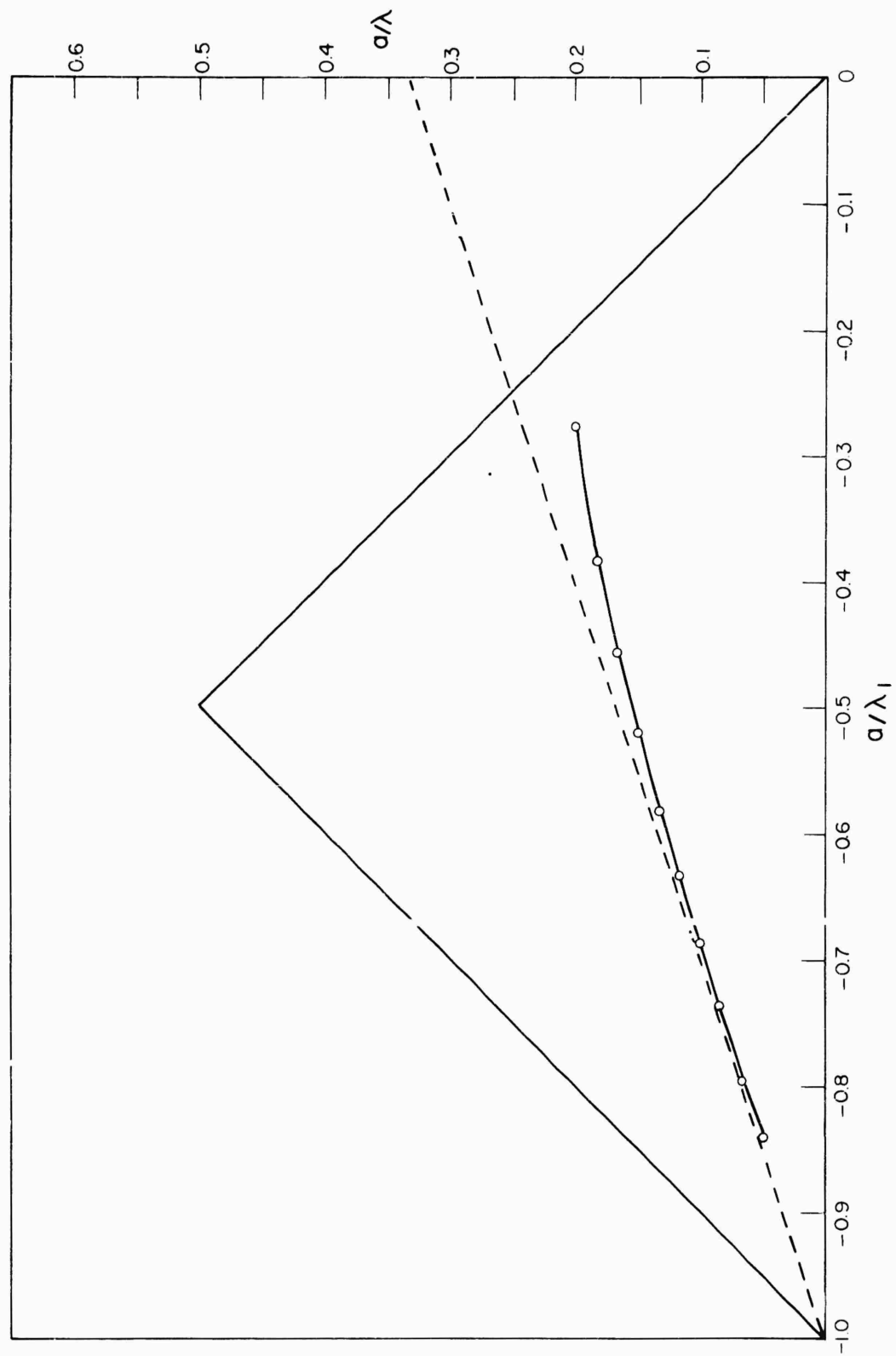
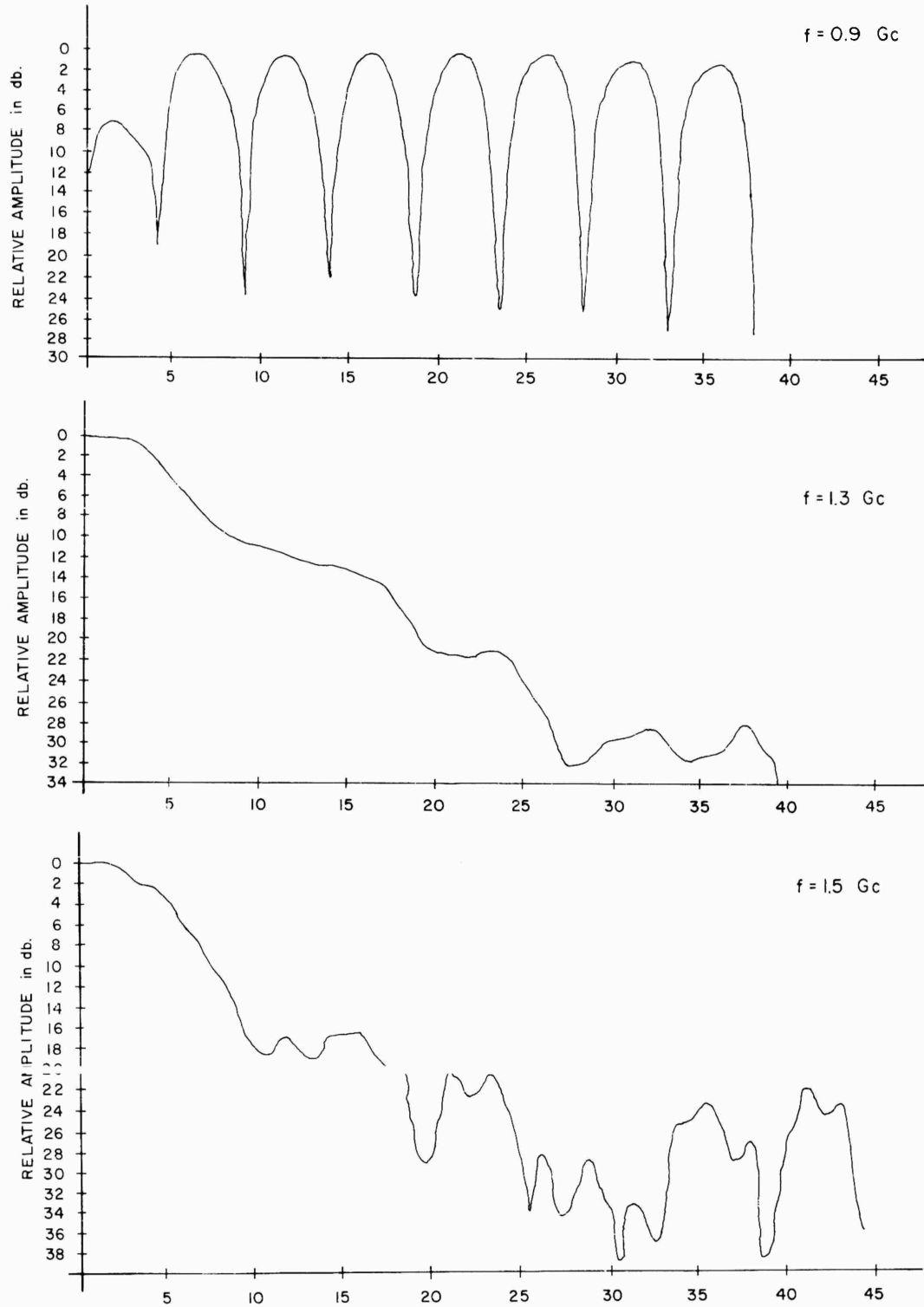


Figure 17. Brillouin diagram for a bifilar zig zag



PROBE POSITION in cm. CURRENT AMPLITUDE DISTRIBUTION BIFILAR ZIG-ZAG ANTENNA.
PITCH=5 cm., PITCH WIDTH = 7.07cm., PITCH ANGLE = 19.5 DEGREES.

Figure 18. Current amplitude distribution for a bifilar zig zag antenna
Pitch = 5 cm, Pitch width = 7.07 cm, Pitch angle = 19.5°

This is a characteristic of the backward wave. The Brillouin diagram represents one cell of a periodic figure; each cell is called a Brillouin zone. It has been the practice here to use that zone which most nearly corresponds to the measured results. In the case of Figure 17 the curve is plotted in the $n = -1$ zone to indicate the observed phase progression toward the feed point. This curve also indicates that the wave length along the structure increases with frequency from a minimum at zero frequency given by the period of the structure. This corresponds to the plus minus polarity change along the structure that would be observed if the structure were excited by direct current.

Several log-periodic versions of the zig zag antenna have been studied⁴. The bifilar log-periodic zig zag antenna is shown in Figure 19. Figure 20 is a typical radiation pattern of this antenna. The monofilar horizontally-polarized zig zag antenna is shown in Figure 21 with typical patterns in Figure 22. Several models of the vertically-polarized bent zig zag⁴ are shown in Figure 23. The evidence of Figure 15 shows that the currents on a zig zag wire are highly attenuated when the coupling between the backward space harmonic and the free space wave occurs. Hence, it is to be expected that it should be possible to convert this periodic structure into a frequency independent antenna by applying a taper. Furthermore, the angle of taper need not be kept very small in order that the log-periodic variations in performance be smoothed out.

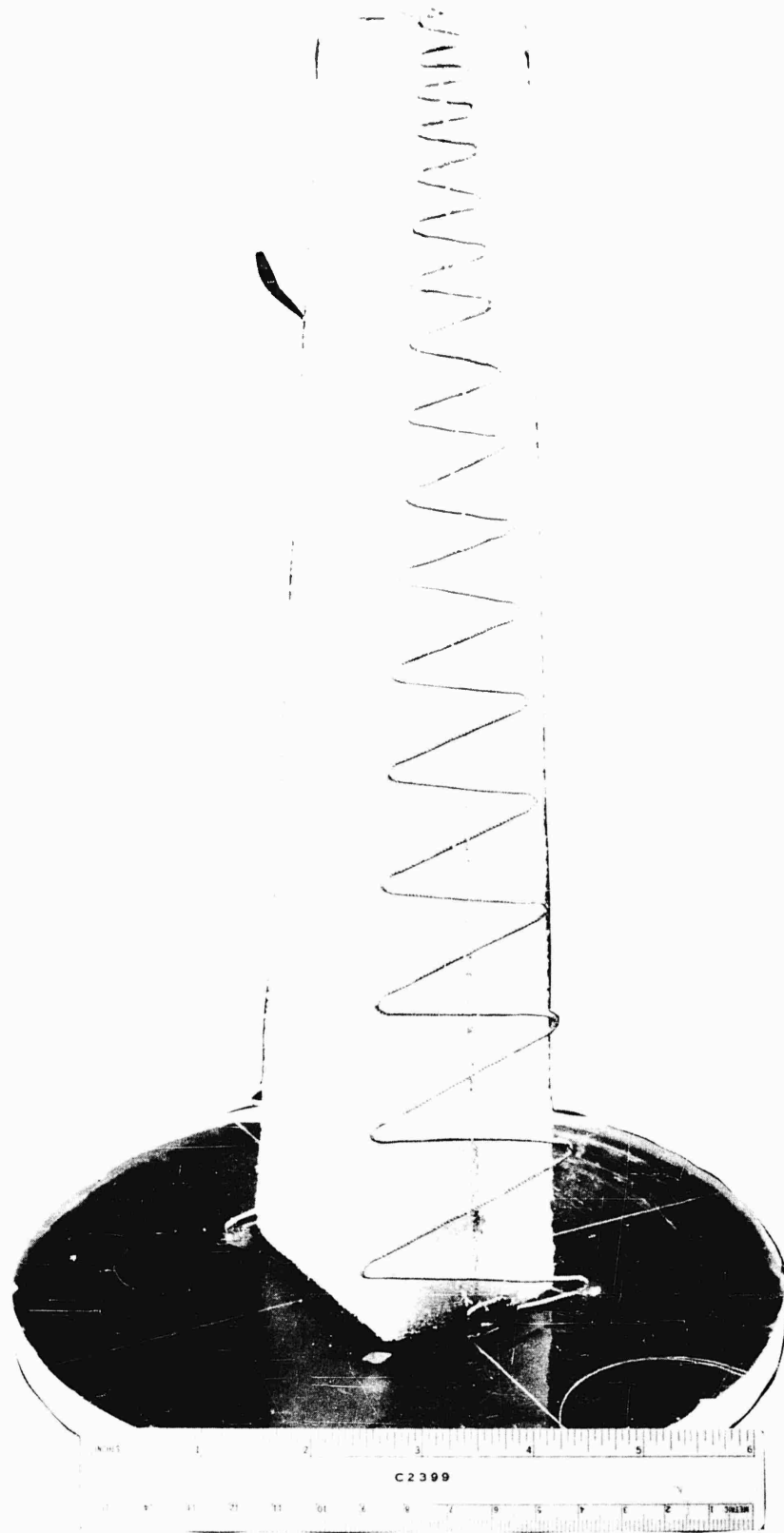


Figure 19. A log-periodic bifilar zig zag antenna

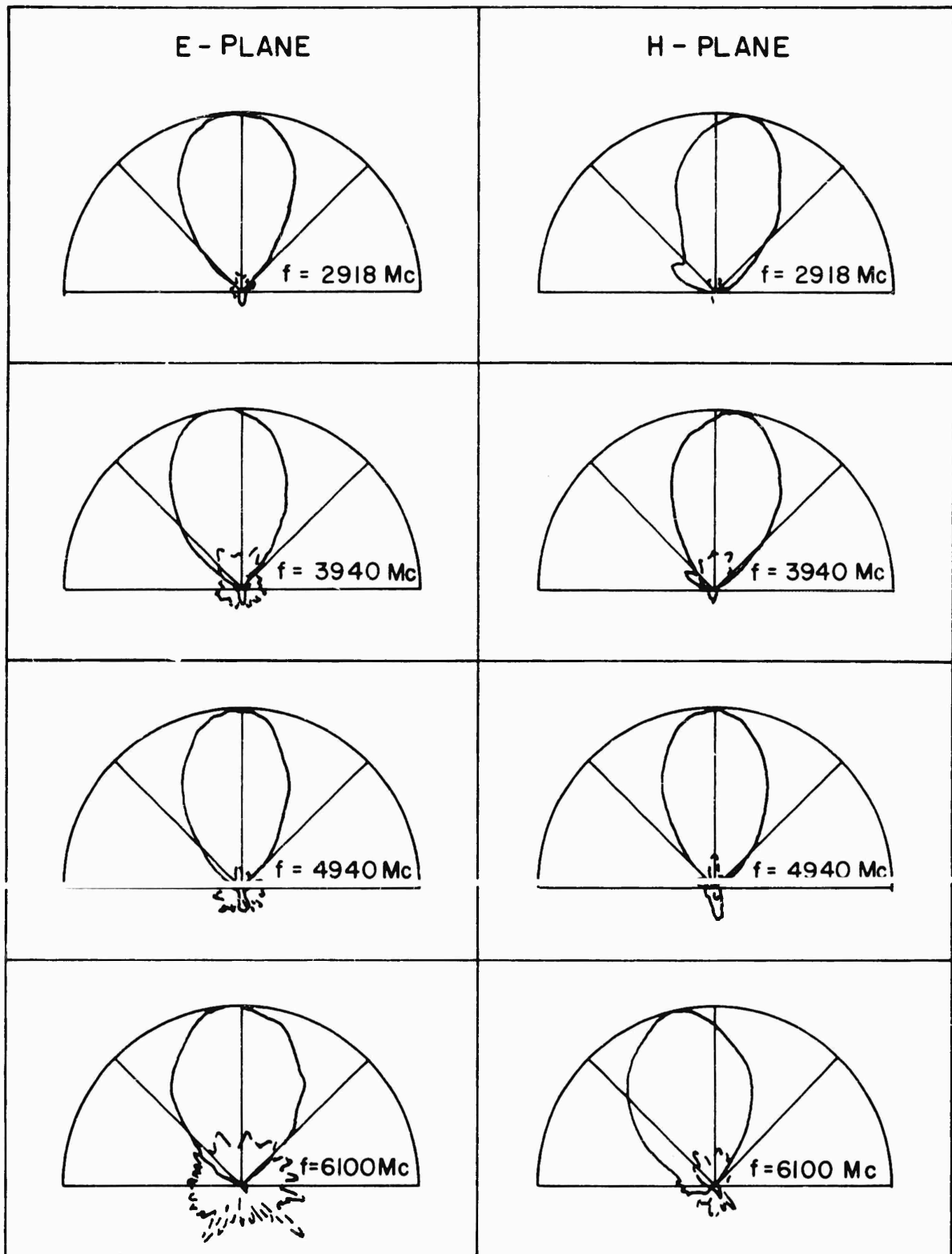


Figure 20. Radiation patterns of a log-periodic bifilar zig zag antenna



Figure 2 . A log-periodic monofilar zig zag over ground

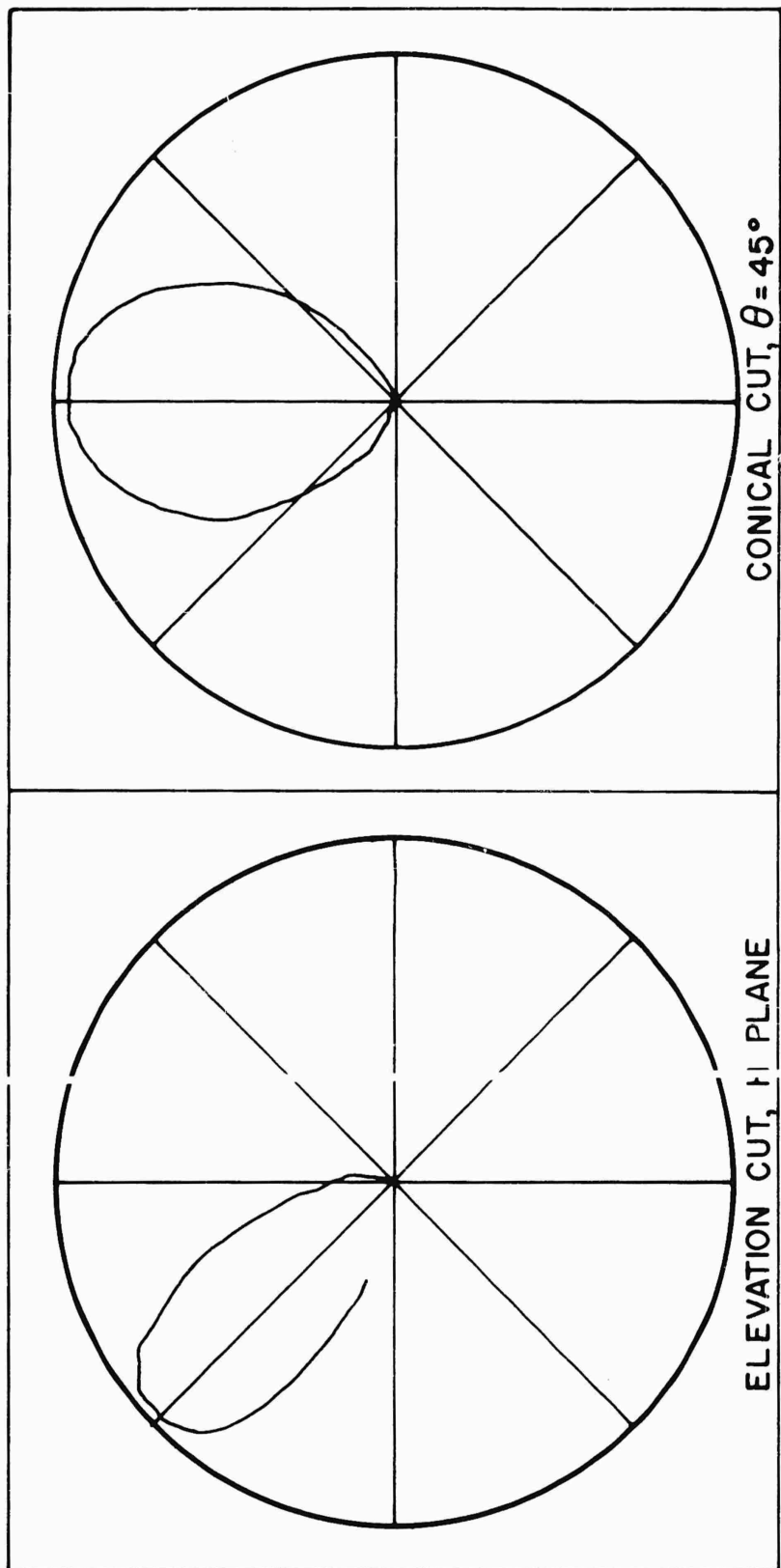


Figure 22. Radiation patterns of a log-periodic monofilar zig zag over ground

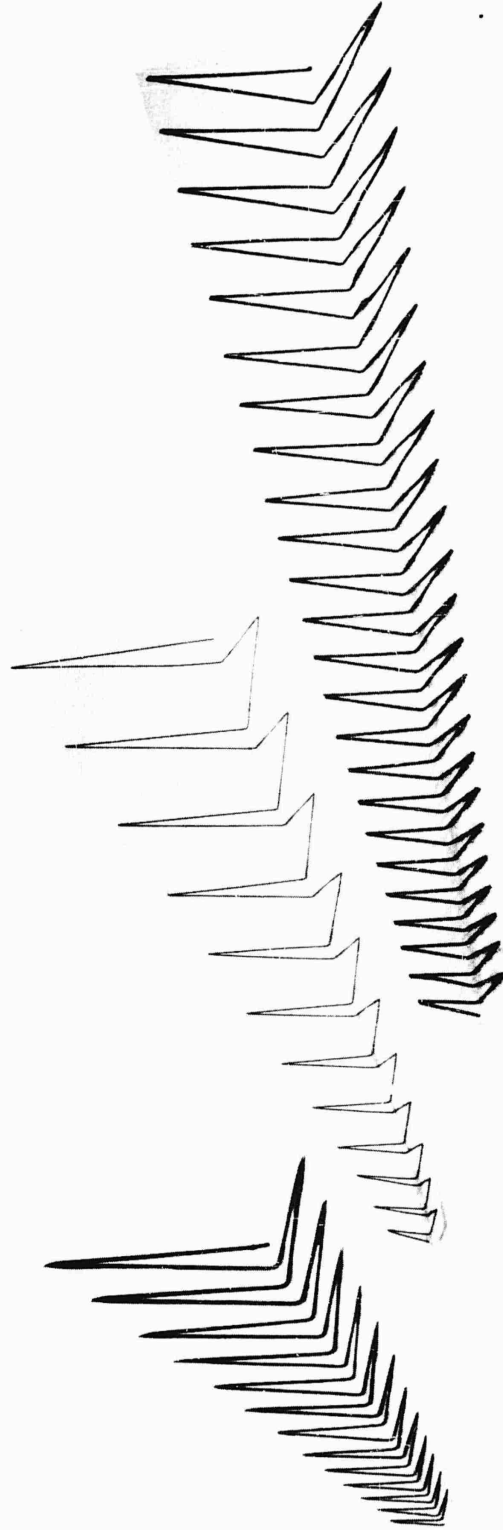


Figure 23. Vertically-polarized log-periodic zig zag over ground

5. PERIODIC STRUCTURES WITH RESONANT ELEMENTS

The periodic zig zag and helix antennas have similar Brillouin diagrams. They are both characterized by a perturbation of the slow wave line shown in Figure 3. The perturbation occurs at the boundary of the triangle where the first backward space harmonic crosses into the visible region. It is interesting to note that one structure serves dual functions as transmission line and radiating elements in both the zig zag and the helix. There are other periodic structures which make excellent frequency independent antennas in the tapered (log-periodic) version and yet which have a different type of Brillouin diagram. The periodic dipole array shown schematically in Figure 24 is the foremost example of this type⁷. In this case the functions of transmission line and radiating element are performed by distinct, although interacting, elements.

The Brillouin diagram of the periodic dipole array is characterized by certain frequency bands where waves can propagate along the structure with essentially undiminished amplitude. In other bands rapid attenuation of the feeder current occurs even though the phase constant of the currents along the feeder corresponds to a point in the interior of the triangle, far removed from the boundary. The periodic loading of the transmission line in this case evidently produces an effect analogous to periodic loading in a waveguide. In the latter case passbands and stopbands alternate in the frequency spectrum. In the stopbands the propagation constants of all the space harmonics are complex and energy does not penetrate a large distance into the structure.

Typical feeder voltage plots obtained on a uniform periodic dipole, using the short-circuit termination as previously described, are shown in Figure 25.

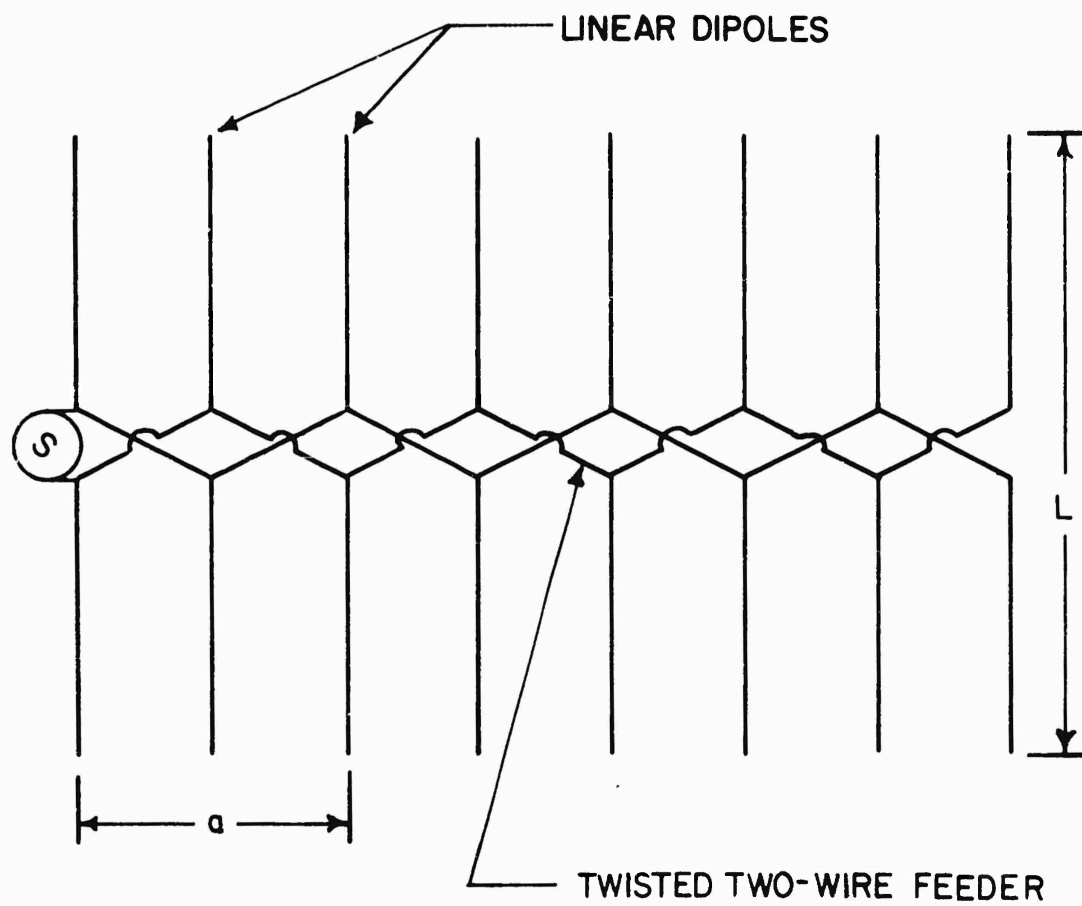


Figure 24. A periodic array of dipoles

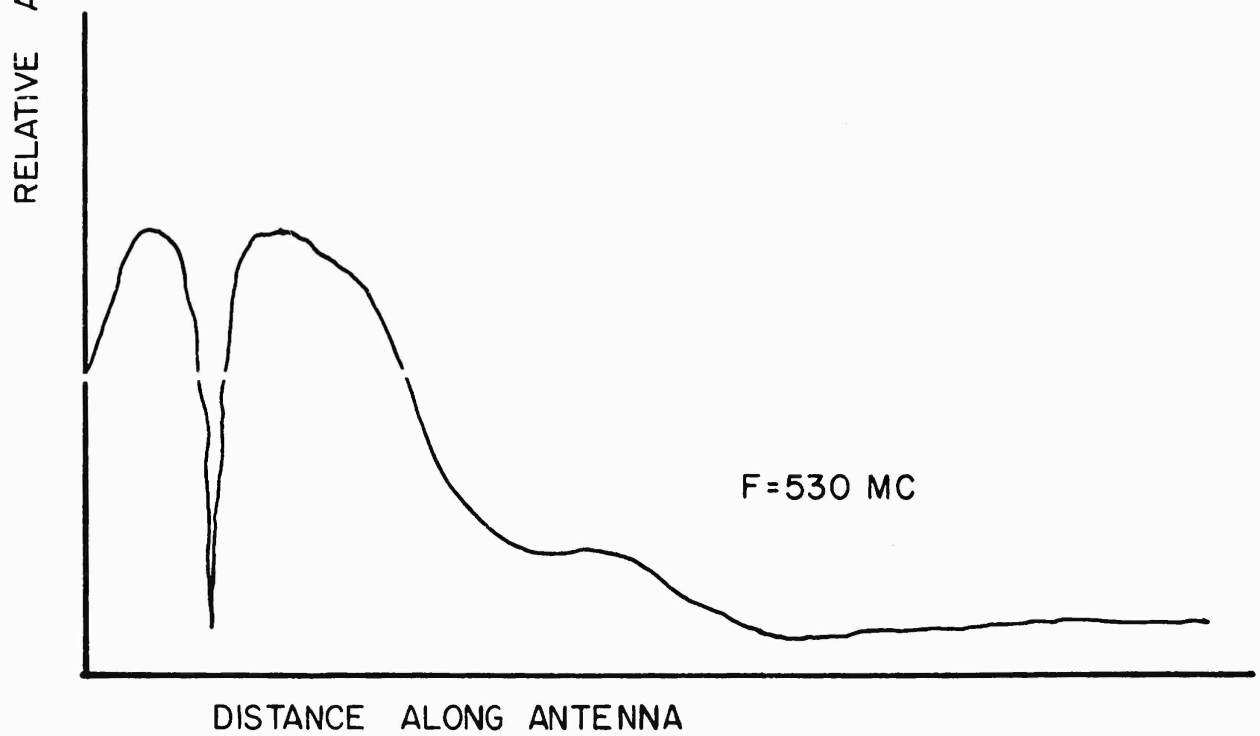
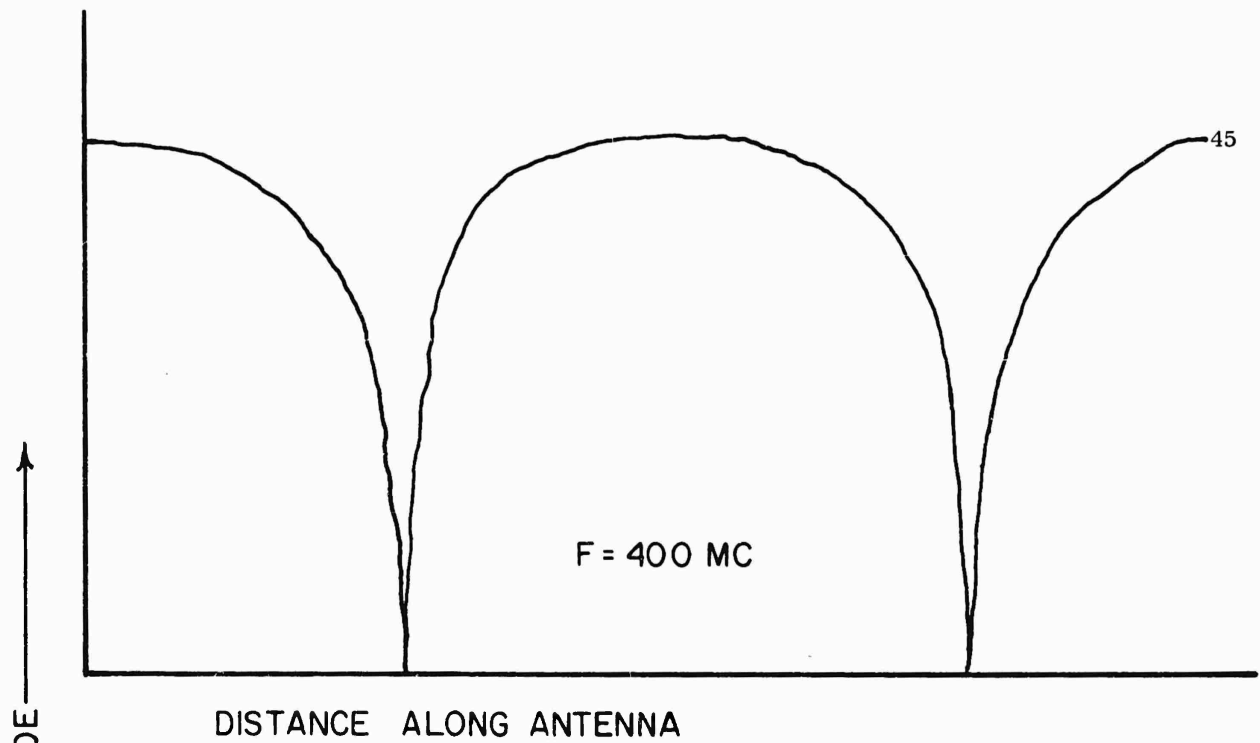


Figure 25. Feeder voltage versus distance on a periodic dipole array

From the standing wave characterized by the deep nulls at 400 Mc it is apparent that this frequency is in the passband of the structure. At 530 Mc, however, the field decays so rapidly that the short-circuit no longer influences the near-field distribution. This indicates that 530 Mc is in the stopband. The Brillouin diagram constructed from a series of such plots is shown in Figure 26. The slant line in Figure 26 represents a wave with free-space velocity. At low frequencies a slow wave propagates along the dipole array. As we approach the half-wave resonant frequency, however, the slowness increases quite rapidly with increasing frequency so that the group velocity $\frac{d\omega}{d\beta}$ is very small. In infinite closed periodic structures the phase constant curve continues to the center of the triangle ($a/\lambda_0 = 0.5$) at which point the group velocity is zero (point A in Figure 26). The propagation constant for all space harmonics becomes complex at this point and the phase constant remains fixed while the attenuation constant varies with frequency inside the stopband. The phase shift per cell of each space harmonic inside the stopband is some multiple of π radians. The stopband is produced by coupling between forward and backward waves on the structure rather than by coupling to a free-space wave. In the dipole array this coupling is predominant near the resonant frequencies of the elements. The Brillouin diagram for the finite length dipole array can be expected to be perturbed somewhat from the idealized case of the infinite, lossless periodic structure.

Above the first stopband is another passband similar to the one at lower frequencies except that the wave on the line is fast over a portion of the band. Even though the phase velocity along the line is fast, there is little radiation in this band because of the twisted feeder shown in Figure 24. The phase velocity corresponding to the dipole excitation remains slow. At the frequency

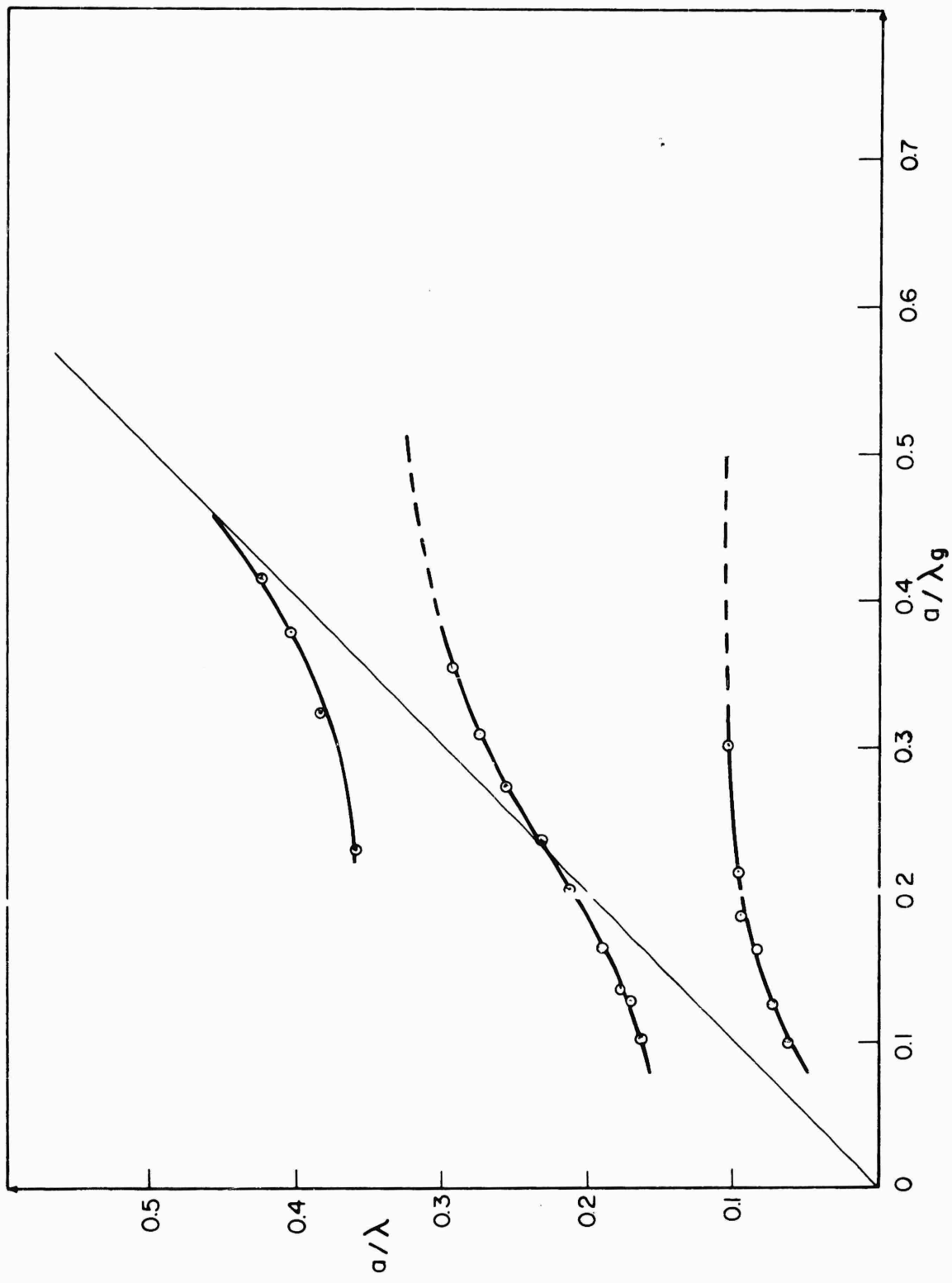


Figure 26. Brillouin diagram for feeder voltage on a periodic dipole array

where the dipoles again possess resistive input impedance (near one wavelength) the velocity along the line reduces to the free-space value. Above this frequency the feeder wave is again slow; the velocity diminishing rapidly as the edge of another stopband is approached. The properties of the second stopband are similar to the first except for being located near the frequency where the elements are three half wavelengths long. The number of stopbands displayed by a particular dipole array depends upon the density of dipoles. Increasing the number of dipoles increases the capacitive loading per unit length at the lower frequencies and thereby influences the phase velocity. This in turn makes it possible for several resonances of the dipoles to occur within the frequency span limited by $0 < \frac{a}{\lambda} < 0.5$. Applications of this phenomenon have been made to multi-band antennas¹⁰.

The radiation patterns of the uniform dipole array are essentially the same as those obtained from other periodic structures having exponential current distributions. In passbands the pattern is multi-lobed as expected from a standing wave excitation of the dipoles. In the stopbands, however, a well-formed unidirectional beam is obtained. Patterns of the uniform dipole array which are typical of the passband and stopband are shown in Figure 27.

The essential role of the twisted feeder in producing the backfire radiation pattern is illustrated by means of the series of Brillouin diagrams described below. Consider first the idealized diagram shown in Figure 28a. Let us suppose that this gives the phase constant of the feeder current, $\beta_0 = \frac{2\pi}{\lambda_0}$. Even though these results were measured for the feeder voltage rather than current, the phase progression of both on an infinite structure should agree. The phase shift from cell to cell would be $\beta_0 a$. The phase shift in the current from one dipole to the next would be half this value. However, at each dipole

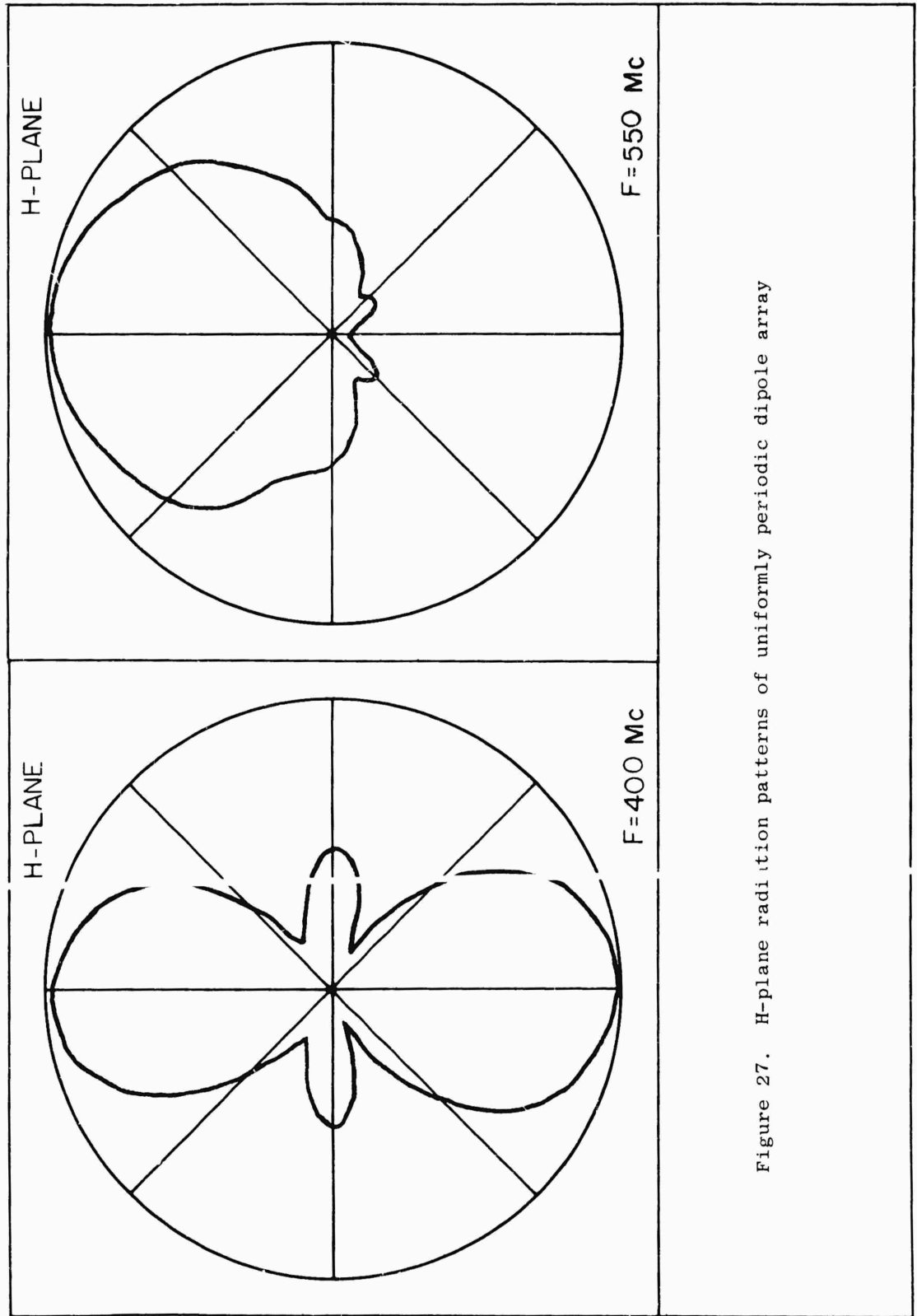


Figure 27. H-plane radiation patterns of uniformly periodic dipole array

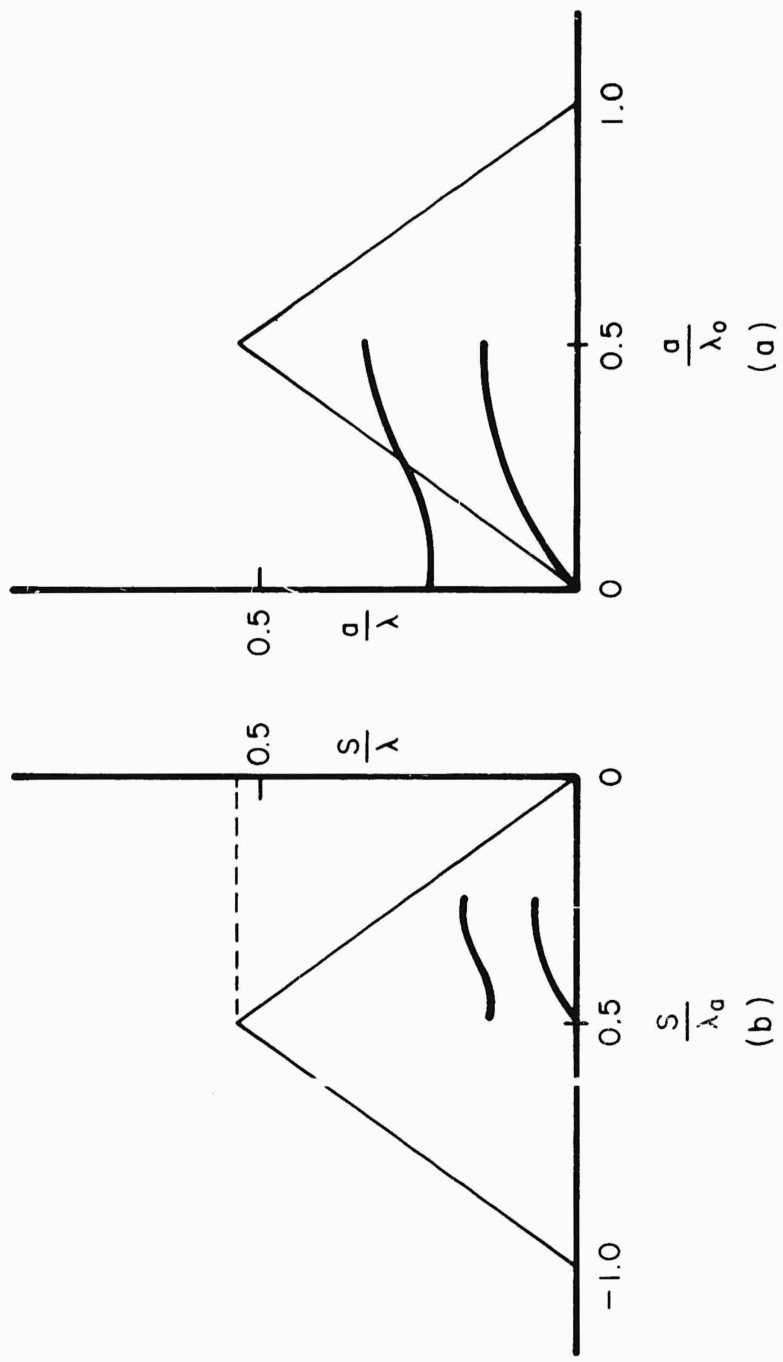


Figure 28. Transformation of measured Brillouin diagram of feeder voltage along periodic dipole array to diagram showing phasing of dipoles

the twist in the feeder adds an addition π radians. To calculate the phase shift between dipoles spaced by $s = a/2$ we can compute a phase constant for the antennas

$$\beta_a s = \frac{\beta_o a}{2} - \pi \quad (13)$$

or, in terms of wavelength λ_a of the wave progressing from dipole to dipole

$$\frac{s}{\lambda_a} = \frac{s}{\lambda_o} - 1/2 \quad (14)$$

Hence the Brillouin diagram for the dipole currents which corresponds to Figure 28a for the feeder currents would appear as shown in Figure 28b. Using the actual data measured on the uniform dipole array from Figure 26 leads to the diagram for the dipole current shown in Figure 29. Note that the phase progression in the dipole currents is opposite to that of the feeder currents. Note also that all points are well within the triangle, removed from the visible range. The radiation is therefore produced by a slow backward wave along the dipoles.

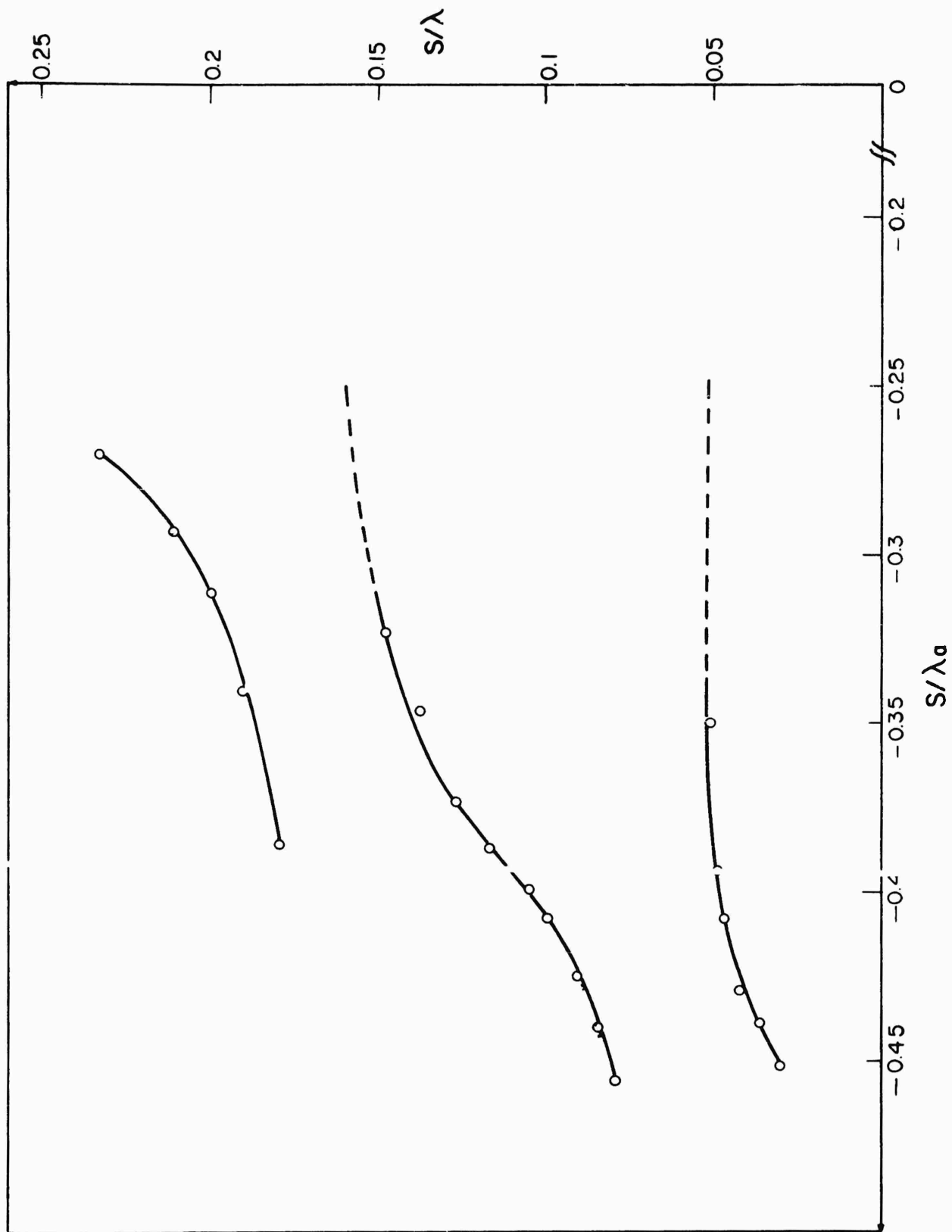


Figure 29. Brillouin diagram for dipole currents

6. CONCLUSIONS

The treatment of the various periodic structures described in this report has been made suggestive and descriptive to illustrate the underlying principle. Detailed studies of most of the structures described here will be the subject of technical reports to follow. Although the relation between periodic structures and log-periodic structures has been emphasized here, the usefulness of the periodic antenna itself should not be overlooked. The periodic antenna has useful properties not shared with log-periodic antennas. Among the notable properties of periodic antennas are the frequency-scanning capability of some of these structures and the absence of sidelobes in the backfire mode. The Brillouin diagram has long been used as a tool in studying and explaining the performance of the closed periodic structures. Here an extension is made to open structures and an interpretation of the diagram for antennas is given. The backfire property is required of the periodic structure to allow tapering to a successful log-periodic antenna.

As our knowledge of these antennas increases it should be possible to satisfy most antenna specifications as to polarization, gain and bandwidth. For example, a gain equivalent to the gain of a linear array of dipoles with Hansen-Woodyard excess phase shift has been obtained with a backfire bifilar helical antenna with a pitch angle of 45 degrees. Needless to say, this antenna has a very narrow bandwidth for this gain. However, gains of this order should be obtainable with the log-periodic version of this antenna if an extremely slow rate of taper were used. In this way, high gain and large bandwidth antennas could be built, but at the expense of very large structures. Where the gain requirements are more moderate a given bandwidth can be achieved with much smaller structures such as the log-spiral of more conventional dimensions³.

There are many advantages to the viewpoint of periodic structures in antenna design, particularly when the number of elements is large. Treating each element separately in such a case becomes vastly complicated because of the large number of mutual impedances needed to describe the system adequately. From the point of view of periodic structures, the coupling between elements is incorporated in the theory of the infinite structure. This allows the designer to reckon by the forest instead of by the tree.

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Air Force Systems Command
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