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AFF.PL-TR-66-30

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**INTERIM REPORT, ADVANCED
AERODYNAMIC SPIKE CONFIGURATIONS**

Rocketdyne Advanced Projects, Large Engines

**Rocketdyne
A Division of North American Aviation, Inc.,
6633 Canoga Avenue, Canoga Park, California**

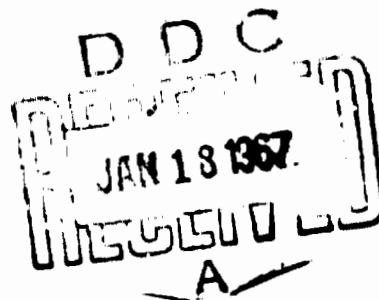
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**Air Force Rocket Propulsion Laboratory
Research and Technology Division
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Air Force Systems Command
United States Air Force**



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FORWORD

This report was prepared in compliance with Contract AFO4(611)-9948 and Line Item 4 of DD1423 covering the period 1 July 1964 through 15 December 1965. This study was conducted for the Air Force Rocket Propulsion Laboratory, Edwards, California. The program structure number is 750G and the project number is 3058. The Rocketdyne internal report number is R6769.

This technical report has been reviewed and is approved.

Roy Silver
Project Engineer
Air Force Rocket Propulsion
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ABSTRACT

Investigations of the aerodynamic spike nozzle concept are discussed in this report. These investigations include experimental cold-flow testing of high-area ratio aerospikes and aerospike nozzles with various combustor configurations and parametric analytical application studies for the nozzle concept.

One cold-flow test series investigated the performance of very high area ratio ($\epsilon = 150$) short length aerospikes using helium as the test fluid. A ten percent length contoured nozzle and a six percent length conical nozzle were tested. Theoretical and experimental performance results are presented.

The second cold-flow test series determined the performance of a series of aerospikes having various combustor configurations. The effect of nozzle base bleed and intermodule bleed on performance was investigated. Combustor configurations consisted of shrouded and unshrouded continuous annular (toroidal) combustors and multichamber configurations with eight and sixteen discrete conventional combustors clustered around a common spike. Spacing between chambers, spike length, and engine shrouding were varied for the multichamber configurations. All nozzles had a area ratio of 50. Theoretical and experimental performance results are presented.

Analytical and design studies were made to determine effective methods of utilizing toroidal and multichamber constructions for aerodynamic spike configurations over a wide range of thrust level, chamber pressure, and nozzle area ratio. Design layouts at several thrust levels of interest are presented. Heat transfer studies establishing cooling feasibility and parametric weight studies are described. Combustor effects on nozzle performance are discussed.

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INTRODUCTION AND SUMMARY

During recent years, various new thrust chamber configurations have been introduced. The ultimate objective of these advanced concepts has been to provide efficient nozzle performance with short, light-weight structures. One promising approach to this goal is referred to as the aerodynamic spike nozzle concept. Figure 1 shows a model of an aerodynamic spike nozzle with an advanced (toroidal) combustion chamber along with a similar thrust conventional engine. In this configuration, the nozzle, as we know it today, is virtually eliminated.

The aerodynamic spike was readily envisioned as a method of shortening the spike (plug) contour. High pressure gases are exhausted from an annular-type combustion chamber with low-pressure gases coming out of the central portion. By this action an interface, similar to a nozzle, is formed between the flows. The thrust contribution normally attributed to a nozzle is obtained by the pressure of the secondary gases acting over the base region. Outwardly, this configuration looks much like a short length plug. However, the introduction of secondary gases produces flow fields (Fig. 2) and performance comparable with much longer plug nozzle types. This secondary flow has proven to be of benefit to nozzle performance.

Performance of the aerodynamic spike nozzle is a function of various nozzle geometric parameters, of the amount of secondary flow, of the manner in which this secondary flow is introduced and of the relative energy between the primary and secondary streams. Investigation of these parameters was initiated under North American Aviation independent research studies in 1959. Since that time, the aerodynamic spike nozzle has been evaluated both experimentally and theoretically. Study

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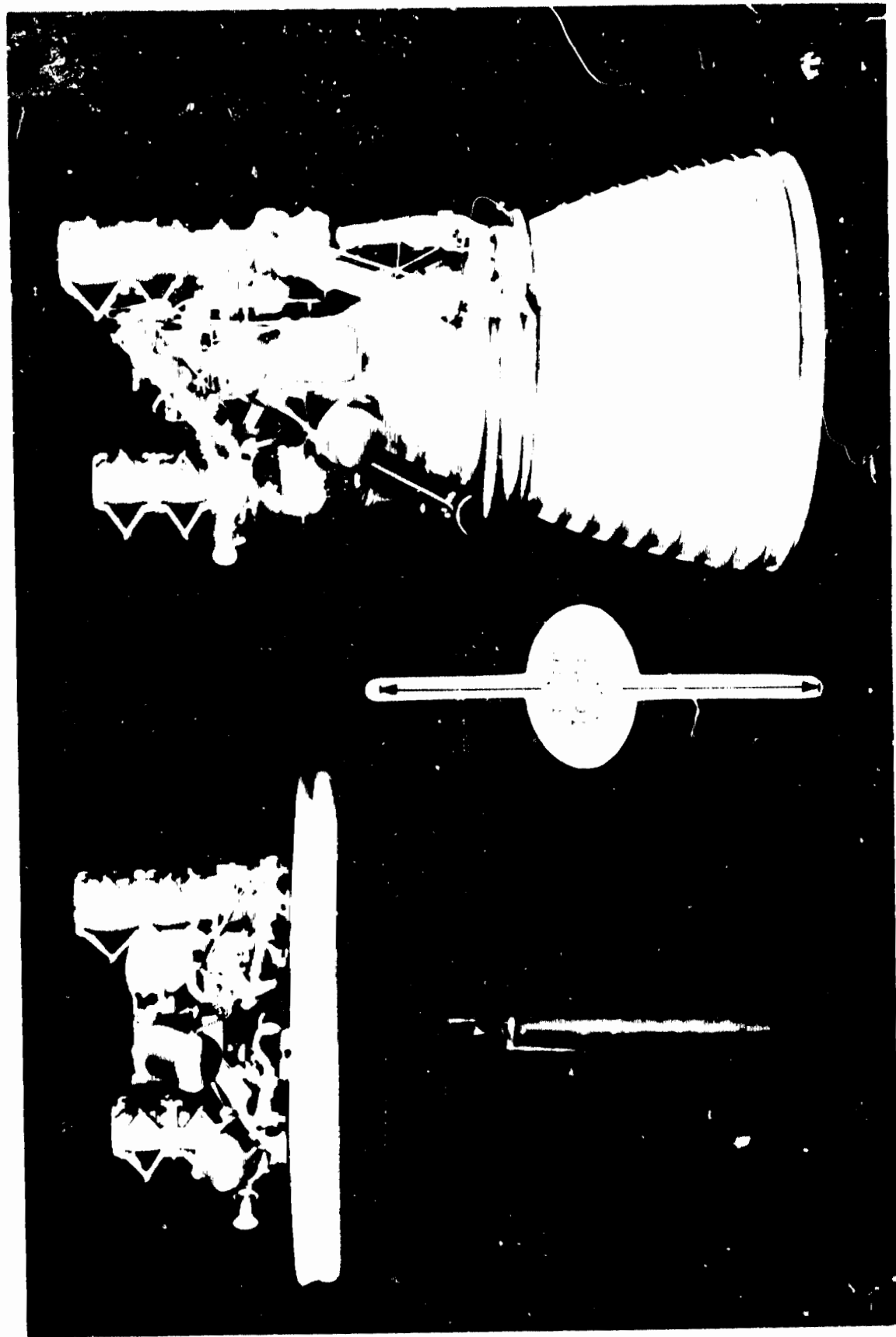


Fig. 1 Aerodynamic Spike Engine With Conventional Engine of Similar Thrust

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Fig.2 Spike Nozzle Concepts

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programs have systematically investigated the various performance parameters and evaluated their influence on nozzle efficiency. The result of this continuous effort is a comprehensive knowledge and understanding of the aerodynamic spike concept.

Investigations have shown that the use of the aerodynamic spike configuration reduces engine length, weight, and cooling surfaces exposed to primary combustion products. These short nozzles exhibited very high nozzle efficiencies, equal to and in most cases superior to the performance of the conventional 80 percent length optimally contoured bell nozzle. In addition to the high nozzle efficiency at design pressure ratios, the aerodynamic spike nozzle provides an extremely high degree of altitude compensation. The requirement for low pressure secondary flows also provides a convenient high performance method of utilizing turbine exhaust gases.

Although verification of these potential gains had been achieved, several aspects of the aerodynamic spike nozzle concept had not been explored. In order to further the development of this concept, the Advanced Aerodynamic Spike Configurations Study was initiated in July 1964 under contract AF04(611)-9948. It was the goal of this study to: (1) evaluate its performance characteristics at high area ratios, (2) compare methods of applying the concept to advanced vehicle configurations, and (3) demonstrate nozzle performance capabilities in a comprehensive hot-firing test series.

All areas of investigation have been completed except for the hot-firing task. Effort in this area has been broadened to include investigation of liquid injection thrust vector control and slipstream effects. This effort will continue through February 1967. This report summarizes the work completed through December 15, 1965, in all areas except the hot-firing task.

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A cold-flow test program was conducted under this contract in two tasks. The goal of the first task was to evaluate aerodynamic spike nozzle performance at high area ratio. A 10-percent-length nozzle contoured for maximum primary thrust and with a 150 area ratio and a 45 degree conical nozzle 5 percent in length with an area ratio of 130 were tested using helium as the primary and secondary fluid. A nozzle efficiency of 98.6 percent was achieved with secondary flow with the 10-percent length, contoured nozzle. The effect of the quantity and method of introduction of secondary flow was investigated. Measurements were made of the pressure distribution in the wake of the nozzles. Good agreement was obtained between theoretical performance predictions and experimental data and the wake measurements verified the analytical flow models used. This program has been completed and the results are presented in this report.

A second cold-flow test series investigated the effect of combustor configuration on aerodynamic spike nozzle performance. The specific goal was to couple closely the effects of nozzle contour, combustor shape and the use of secondary gas. To accomplish this, a group of multichamber and annular aerodynamic spike nozzles were tested. These particular cold-flow data combined with available data for various toroidal configurations may be utilized to evaluate the potential performance of combustor and nozzle designs. An additional cold-flow model which was tested, was a scaled version of a 10,000-pound thrust hot-firing thrust chamber. A direct comparison of cold-flow and hot-firing performance will be made with these geometrically similar nozzles. This cold-flow test series has been completed and the results are presented in this report.

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Analytical and design studies were made to determine effective methods of utilizing toroidal and multichamber constructions for aerodynamic spike configurations. Design layouts were completed at thrust levels of 40,000 pounds, 350,000 pounds, 658,000 pounds, and 2,000,000 pounds. Heat transfer studies establishing cooling feasibility and parametric weight studies were conducted. The results are presented in this report.

A hot-firing aerodynamic spike nozzle using NTO/UDMH- N_2H_4 (50-50) propellants is being tested under this program. The thrust chamber will generate 10,000-pounds sea level thrust at 500 psia chamber pressure, an area ratio of 25 and using a nozzle length which is only 12 percent of an equivalent 15 degree conical nozzle. A series of tests at both sea level (at Rocketdyne's Research Facility) and altitude (at the Air Force Facility, Arnold Engineering Development Center, AEDC) is planned for this thrust chamber. Test hardware includes both uncooled and water cooled thrust chambers, and checkout testing has been initiated to demonstrate hardware integrity. In December, 1965, the hot-firing phase of the program was broadened to include investigations of liquid injection thrust vector control, nozzle base configurations and slipstream performance. The hot-firing effort will be reported at the conclusion of the program.

The first section of this report contains a qualitative description of the principles of operation and the flow regimes for the aerodynamic spike nozzle concept. This should serve to quickly familiarize the reader with the concept and more readily grasp the detailed results presented in the following sections.

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THE AERODYNAMIC SPIKE NOZZLE CONCEPT

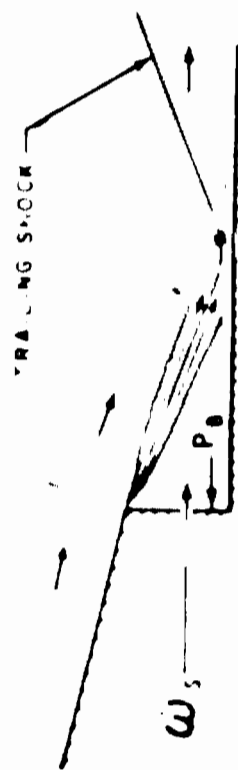
The aerodynamic spike nozzle concept is based upon the fact that, by suitable design, an ideal, maximum-efficiency spike nozzle can be truncated to a small fraction of its initial length with only a small loss in efficiency. As the spike contour length decreases, the nozzle base area increases and the pressure acting on the base pressure area provides a performance contribution compensating, in part, for the diminishing performance of the primary (isotropic) flow field. In addition, the proper use of secondary mass bleed into the base region of a truncated spike nozzle increases the base pressure contribution, compared to a zero-bleed system, and results in a relatively short nozzle with the high overall performance.

FLOW FIELD BEHAVIOR

An understanding of the primary flow field behavior and the base pressure phenomenon is essential to the formulation of an analytical model of the aerodynamic spike nozzle. The phenomenon is depicted in Fig. 3 for a highly simplified model of uniform flow over a backward-facing step. Reattachment and simultaneous change of direction of the potential flow field produces a recirculating flow in the base which is instrumental in establishing the base pressure. The recirculating fluid consists of low-energy, boundary-layer flow, which is turned back by the increasing pressure gradient in the region of reattachment. This process is viscous in nature.

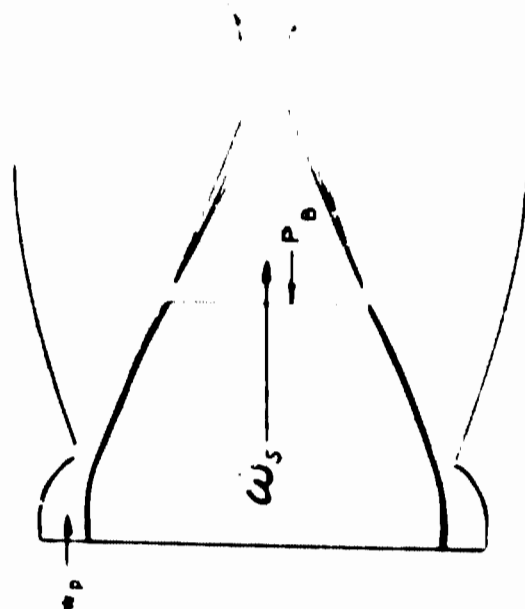
During operation at high pressure ratios (chamber pressure-to-ambient pressure), the characteristics of the primary flow field upstream of the base, shown as Region 1 in Fig. 4, are determined only by the

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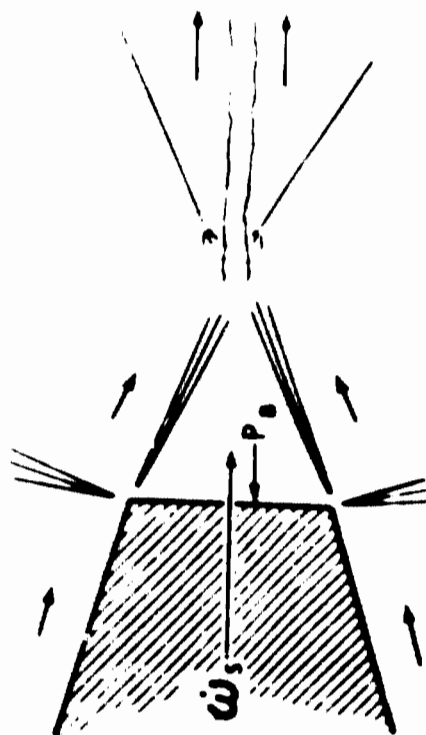


RESTRICTED WAKE NO BLEED
(a)

RESTRICTED WAKE WITH BLEED
(b)



AEROSPIKE
(d)



FREE WAKE WITH BLEED
(c)

Figure 3 . Aerospike Nozzle Principle of operation

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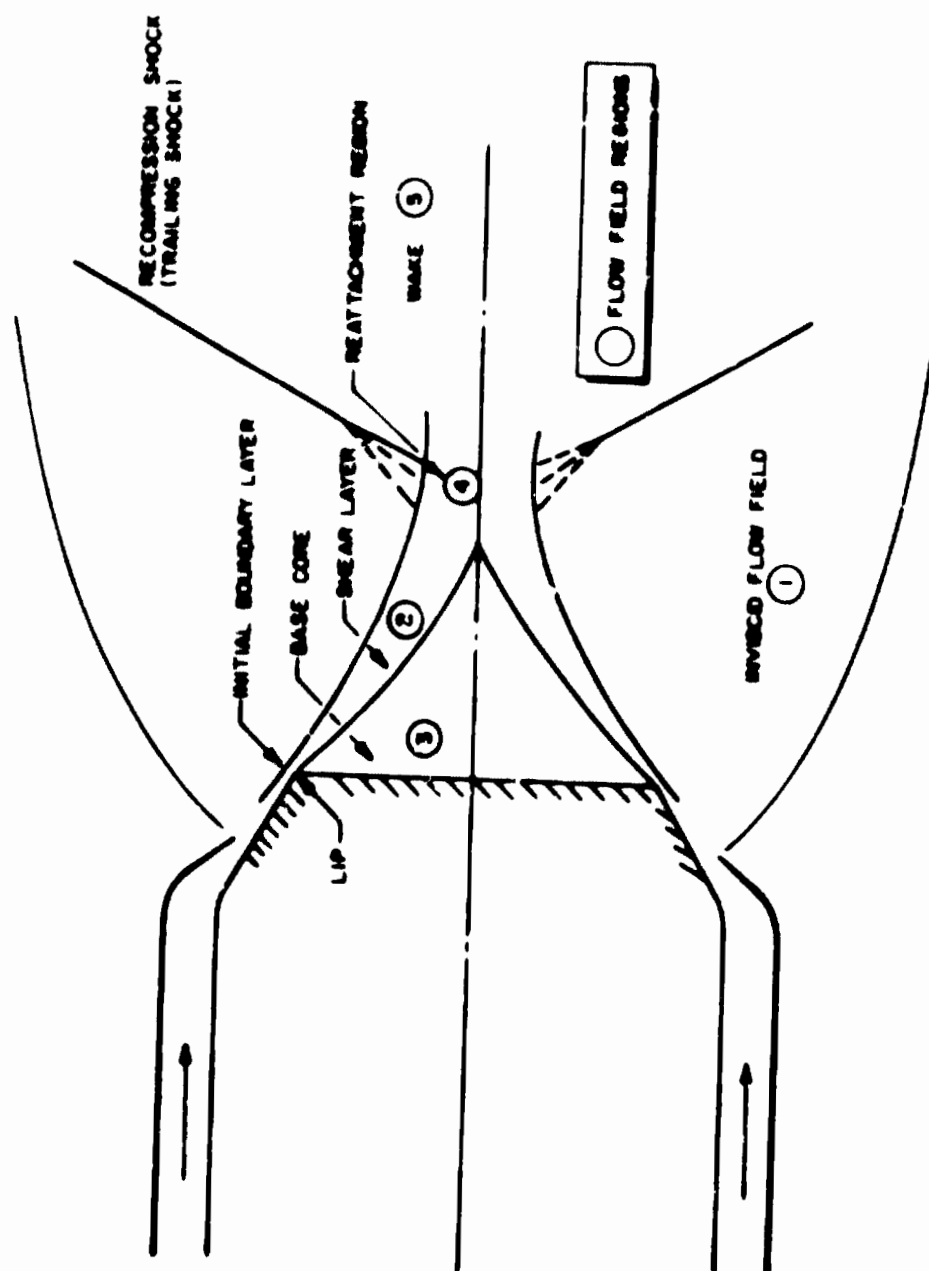


Figure 4 . Aerospike Flow Field Model

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throat and contour geometry. In Region 2, the flow expands around the lower lip of the model and detaches, forming a free shear layer which separates the external flow from a region of subsonic recirculating gases in the base. The inner free-jet boundary is not affected by ambient pressure waves from the outer-jet boundary, and thus is independent of pressure ratio. The flow along the inner-jet boundary and its adjacent shear layer impinges on the centerline where it reattaches and recompresses through a trailing shock. This condition is referred to as closed-wake flow, and the base pressure is constant and higher than ambient so that a positive thrust acting on the base is developed. Ambient pressure effects are not felt on the nozzle contour or base. The basic mechanism governing the base pressure in this regime is flow reattachment.

When a small amount of secondary flow is introduced into the base (at a constant ambient pressure) and the base pressure increases, the inner free-jet boundary of the primary stream still impinges on the centerline; however, the angle of impingement becomes shallower as the base pressure increases (Fig. 5). Schlieren photographs of a typical configuration are shown in Fig. 6, for increasing secondary flowrates at the design pressure ratio. Higher base pressures result because the secondary flow modifies the shear layer characteristics, i.e., increases the viscous entrainment region between the primary and secondary flow regions. The modification of the shear layer is accompanied by a change in the flow in the reattachment region (Region 4) resulting in increased base pressure.

As the amount of secondary bleed increases, the base pressure also increases until a condition is reached where the inner boundary of the primary flow no longer impinges on the axis. Some of the base bleed

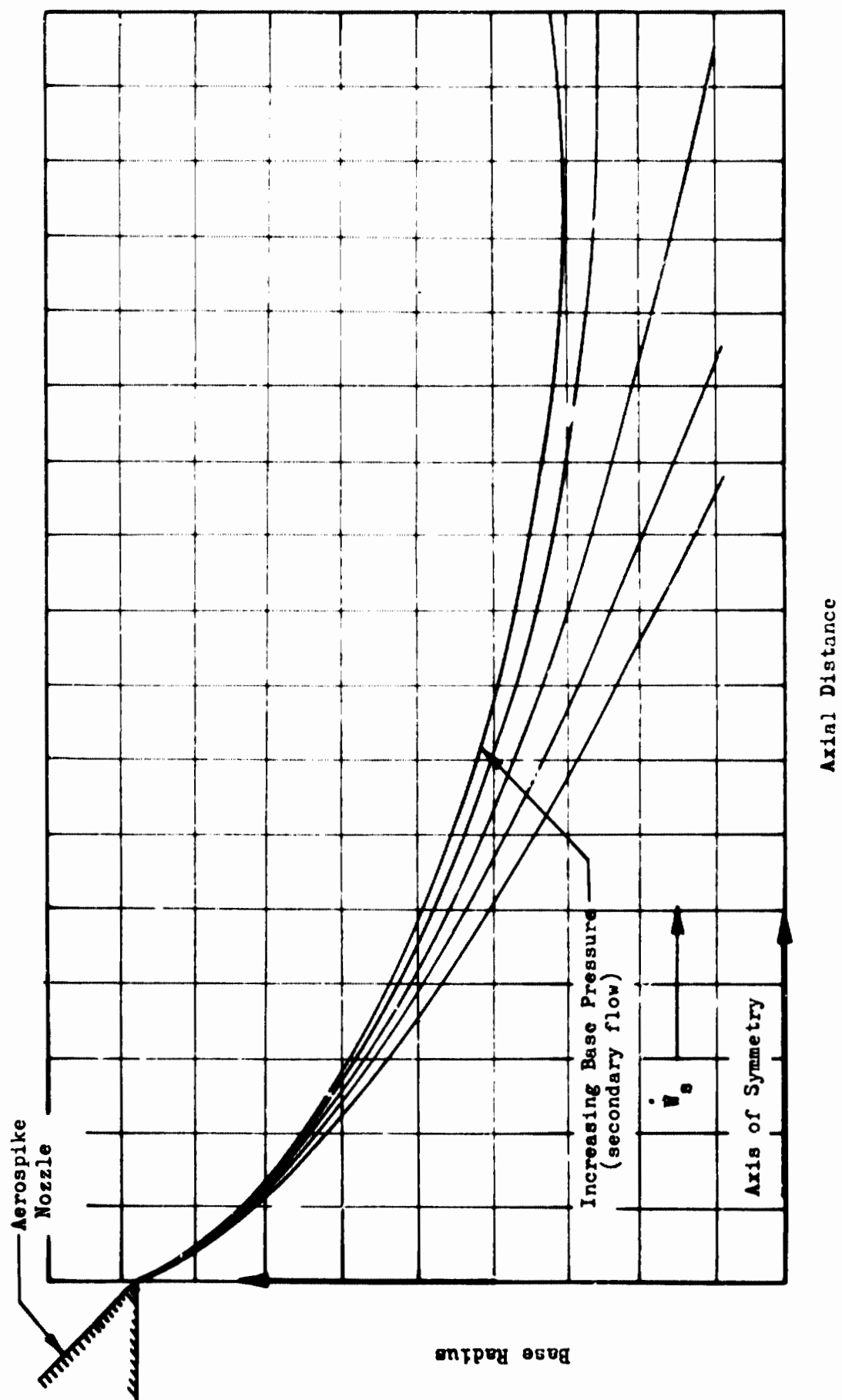


Fig. 5. Typical Solution of Aerodynamic Spike Free Jet Boundary with Various Secondary Flows

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(a) $\dot{W}_s/\dot{W}_p = 0$ percent
PR = 1162



(b) $\dot{W}_s/\dot{W}_p = 0.48$ percent
PR = 1176



(c) $\dot{W}_s/\dot{W}_p = 1.02$ percent
PR = 1164



(d) $\dot{W}_s/\dot{W}_p = 1.56$ percent
PR = 1176

Figure 6. Optimum Nozzle (12-Percent Length) With Increasing Secondary Flowrate, Schlieren Photographs

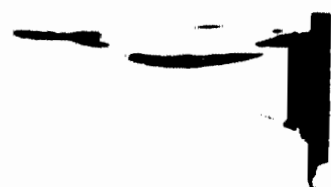
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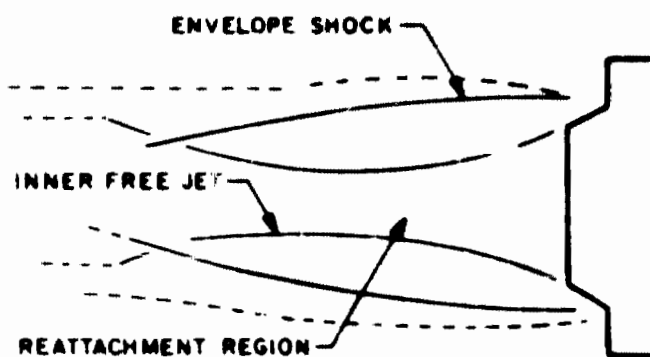
then is transmitted into the wake region through a central core; this core grows as the secondary bleed rate continues to increase. A decreasing pressure gradient then exists in the base region, and the secondary flow is accelerated by pressure as well as viscous forces.

As the pressure ratio decreases, the nature of the flow field changes considerably. The intersection of the envelope shock and the inner free-jet boundary moves upstream toward the reattachment point as the pressure ratio decreases. This can be observed in the series of Schlieren photographs in Fig. 7. When the reattachment point (Fig. 7b and 7c) is reached, the wake starts to open. The base region then begins to feel the influence of the higher ambient pressure. When the wake opens, the base pressure no longer remains constant (at a constant secondary flowrate), but increases with increasing ambient pressure (decreasing pressure ratios). This open-wake base pressure is, in many cases, greater than ambient pressure. Further decreases in pressure ratio will cause the envelope shock to impinge finally on the nozzle contour (Fig. 7f), causing recompression of the primary flow. The recompression phenomenon yields increased wall pressures at high ambient pressures, eliminating overexpansion losses common to conventional high-area-ratio nozzles operating at low altitudes. Thus, base pressure and nozzle recompression compensate for the ambient condition, and are responsible for the altitude compensating feature of the aerospike nozzle. The wall pressures due to recompression can be considerably higher than ambient or base pressures. Conventional bell nozzles cannot experience recompression nor adjusting nozzle exit pressure (comparable to aerospike base pressure) since the primary flow field is internal to the nozzle hardware. The aerospike nozzle, therefore, exhibits a performance advantage over a conventional nozzle since the recompression and base pressure phenomena result in good low-altitude performance for a high-area-ratio nozzle without compromising design point performance.

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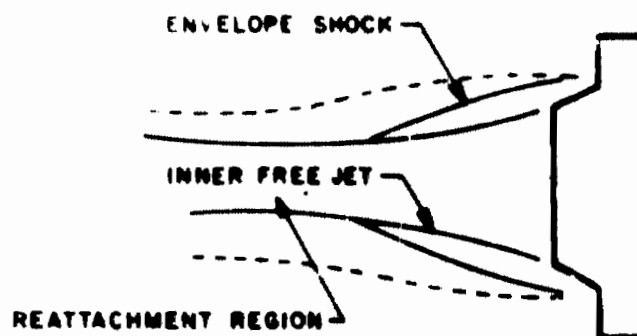
(a) $PR = 899$



CLOSE WAKE ($P_0 = \text{CONST.}$)



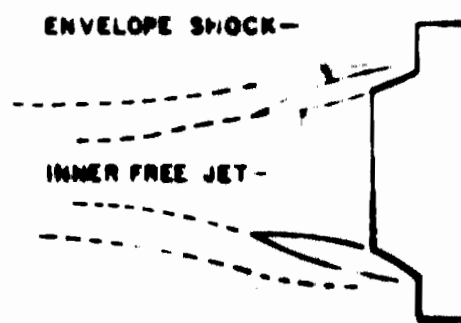
(b) $PR = 397$



OPENING WAKE (TRANSITION)



(c) $PR = 279$



OPEN WAKE

Figure 7. Flow Field Behavior With Pressure Ratio, Schlieren
Photographs, Shrouded Ideal Contour ($\epsilon = 45$,
 $L = 15$ Percent, $\gamma = 1.4$, $\dot{w}_s = 1$ Percent)

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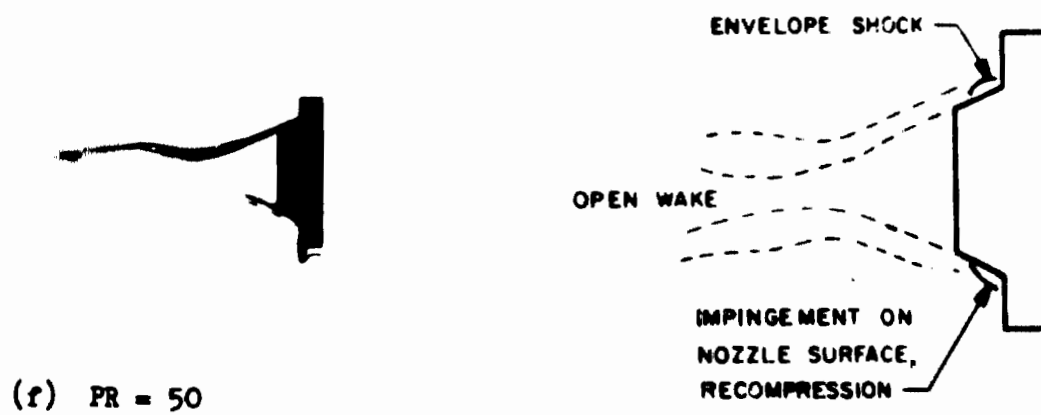
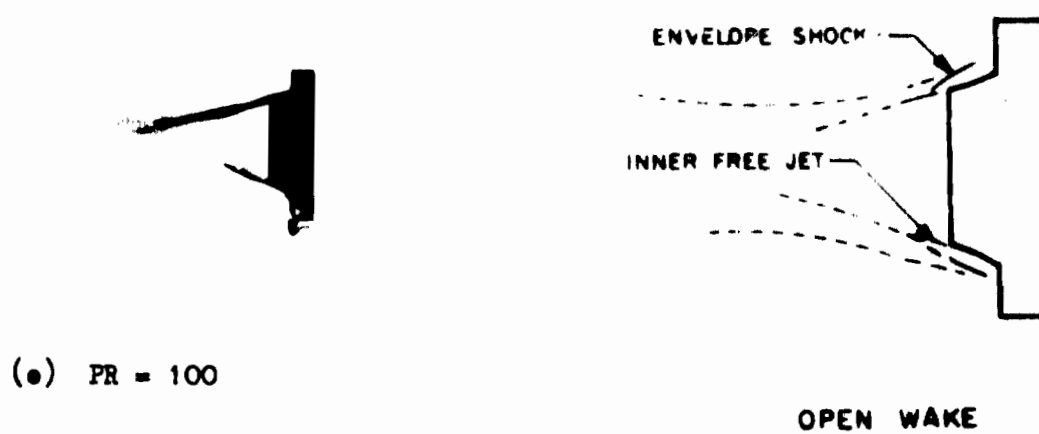
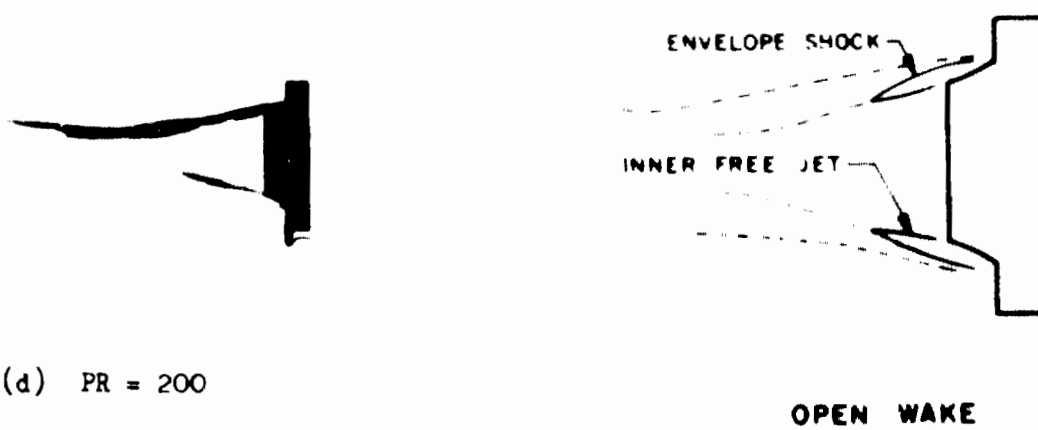


Fig. 7. Concluded

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SECONDARY FLOW EFFECTS

Introduction of a secondary flow into the base region improves the base pressures developed as shown in Fig. 8 . As the secondary flow increases from the no base bleed case, the nozzle efficiency will increase due to the increase in base pressure although the total flowrate increases. There is a limit to the gain in efficiency and an optimum flowrate exists for each configuration. This can be determined by observing the design efficiency with increasing secondary flowrate, Fig. 9 . Normally, efficiency improvements over the no secondary flow case are achieved with secondary flows which are a small percentage of the primary flow. Secondary flows also eliminate rapid decrease in efficiency with pressure ratio (Fig. 10) and improve altitude compensation.

Nozzle length and secondary flowrate are interrelated in that the performance gain with secondary flow and the optimum secondary flowrate are increased for shorter centerbody lengths (Fig. 11). Each aerospoke configuration can be designed such that the secondary flow and length requirements are balanced to produce a configuration with an optimum efficiency versus altitude curve.

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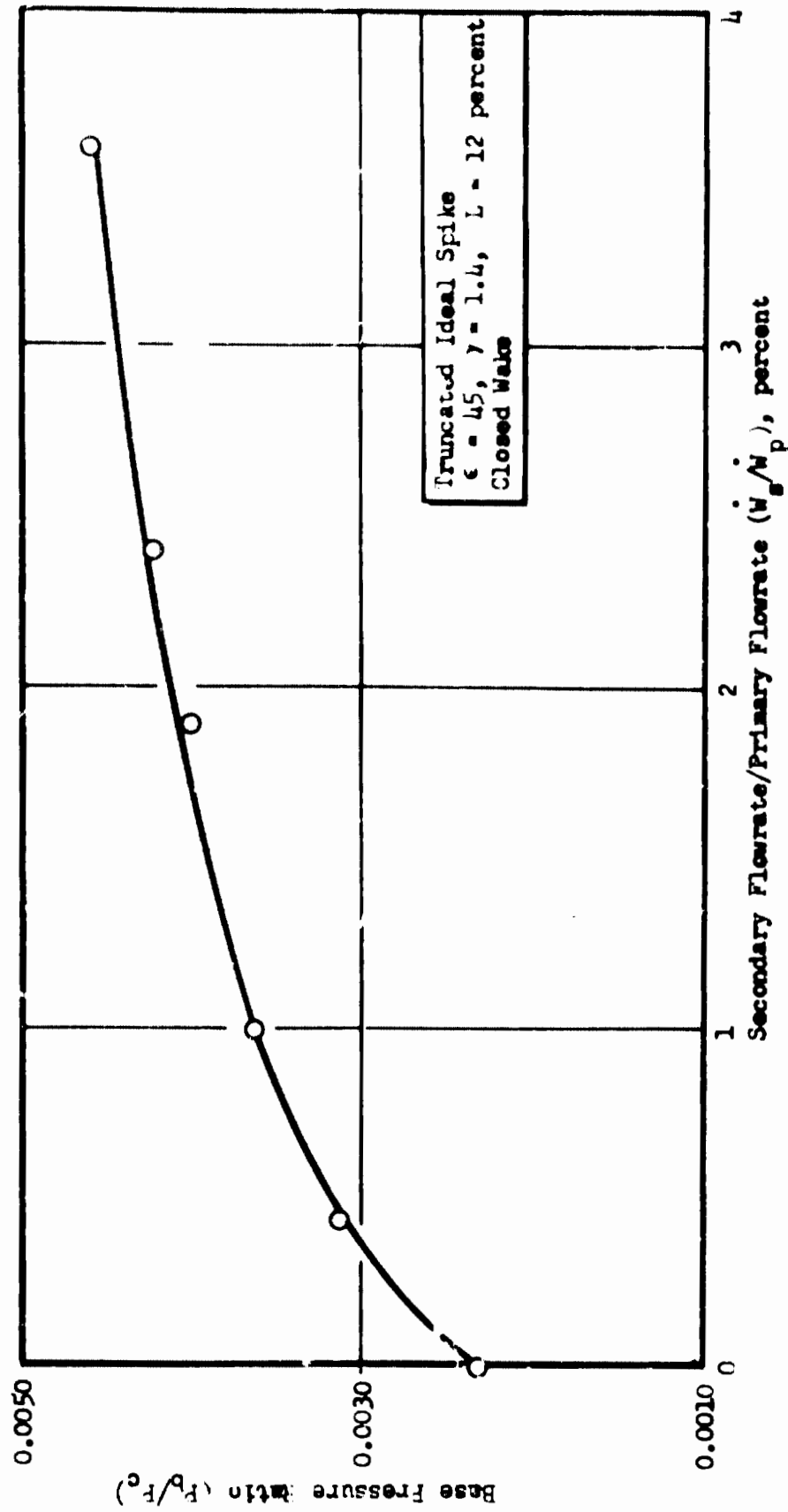


Figure 8 . Base Pressure vs Secondary Flowrate

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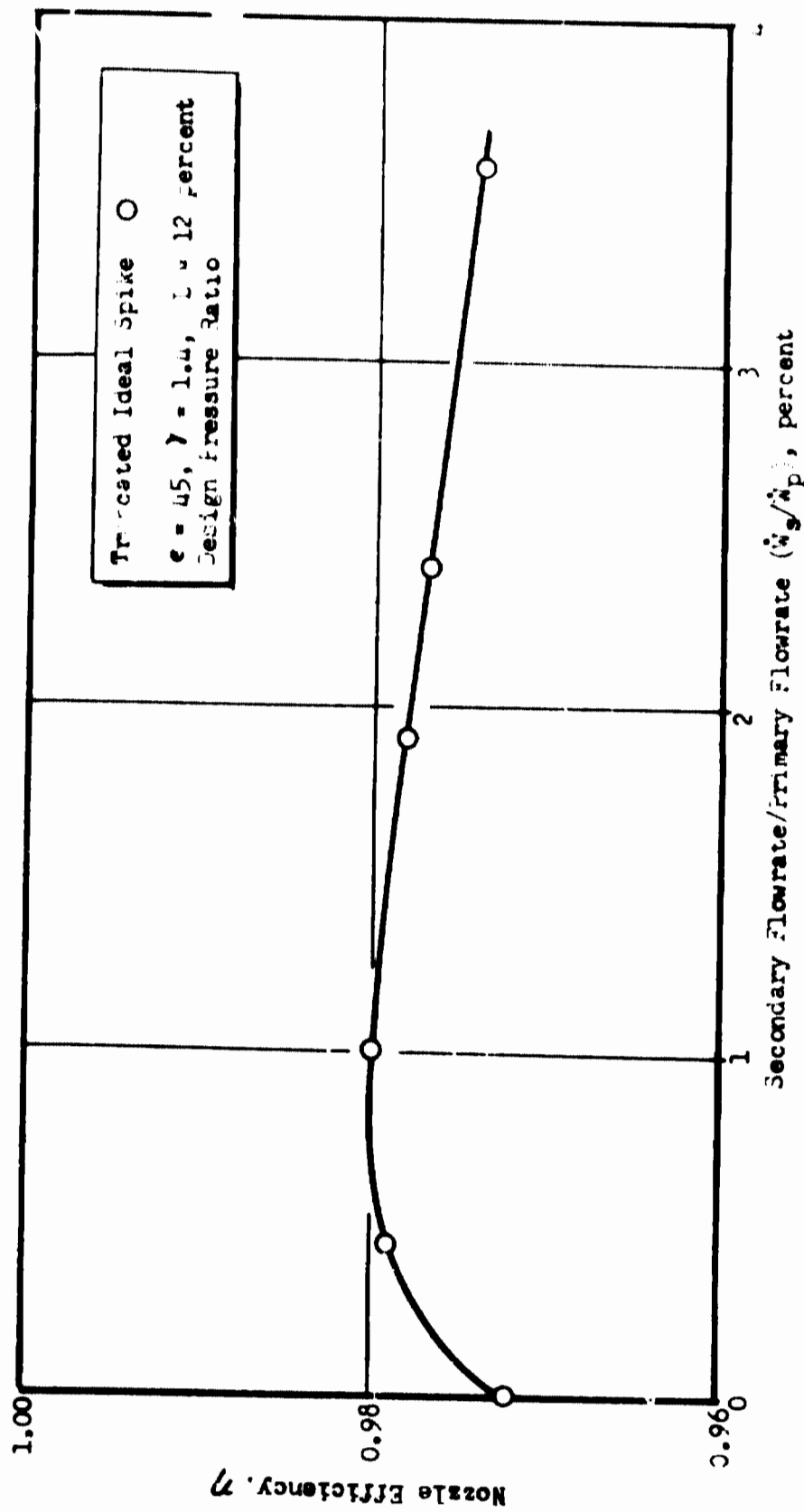


Figure 9 . Nozzle efficiency vs Secondary Flowrate, 12-percent length.

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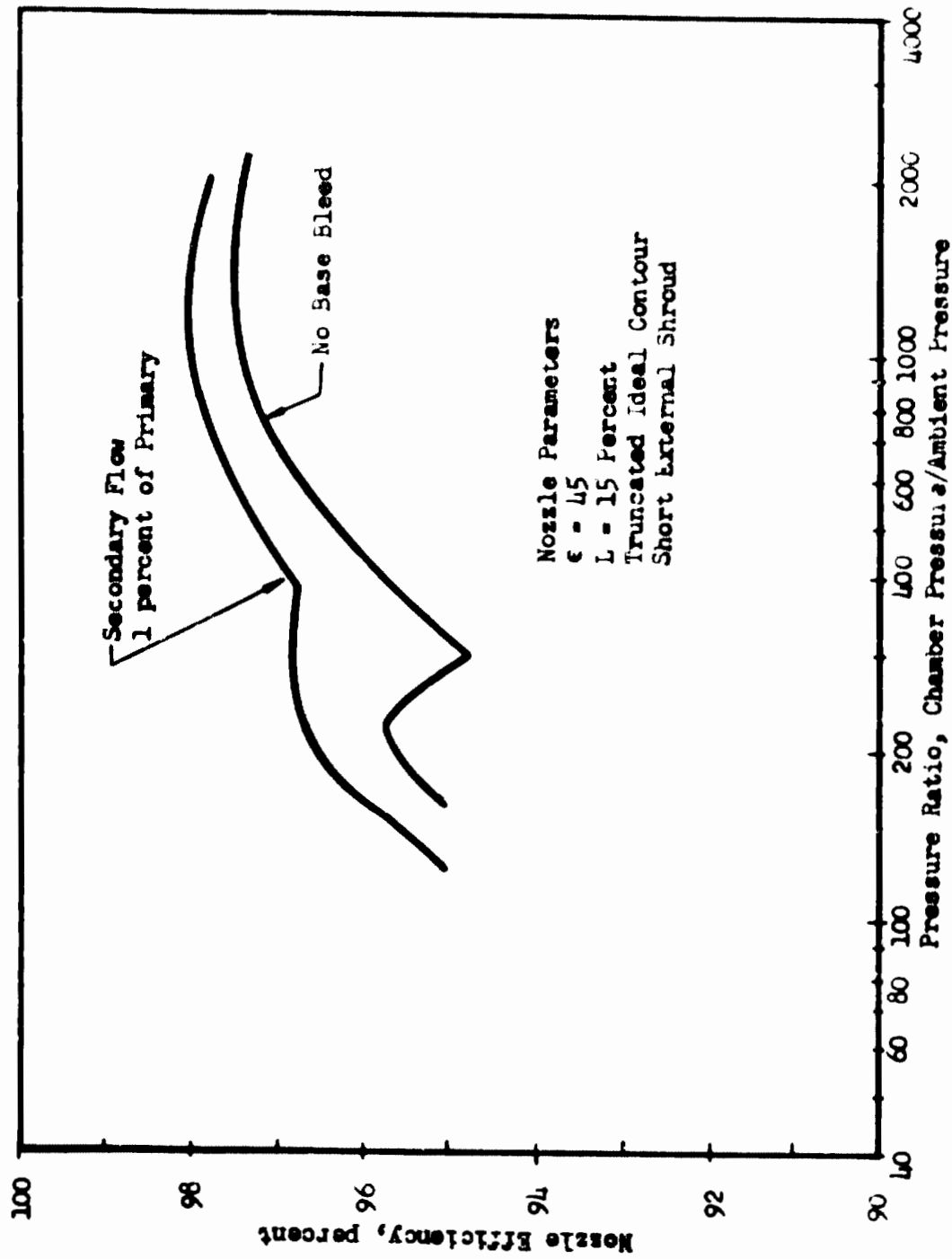


Figure 10. Nozzle Efficiency vs Pressure Ratio with Secondary Flow

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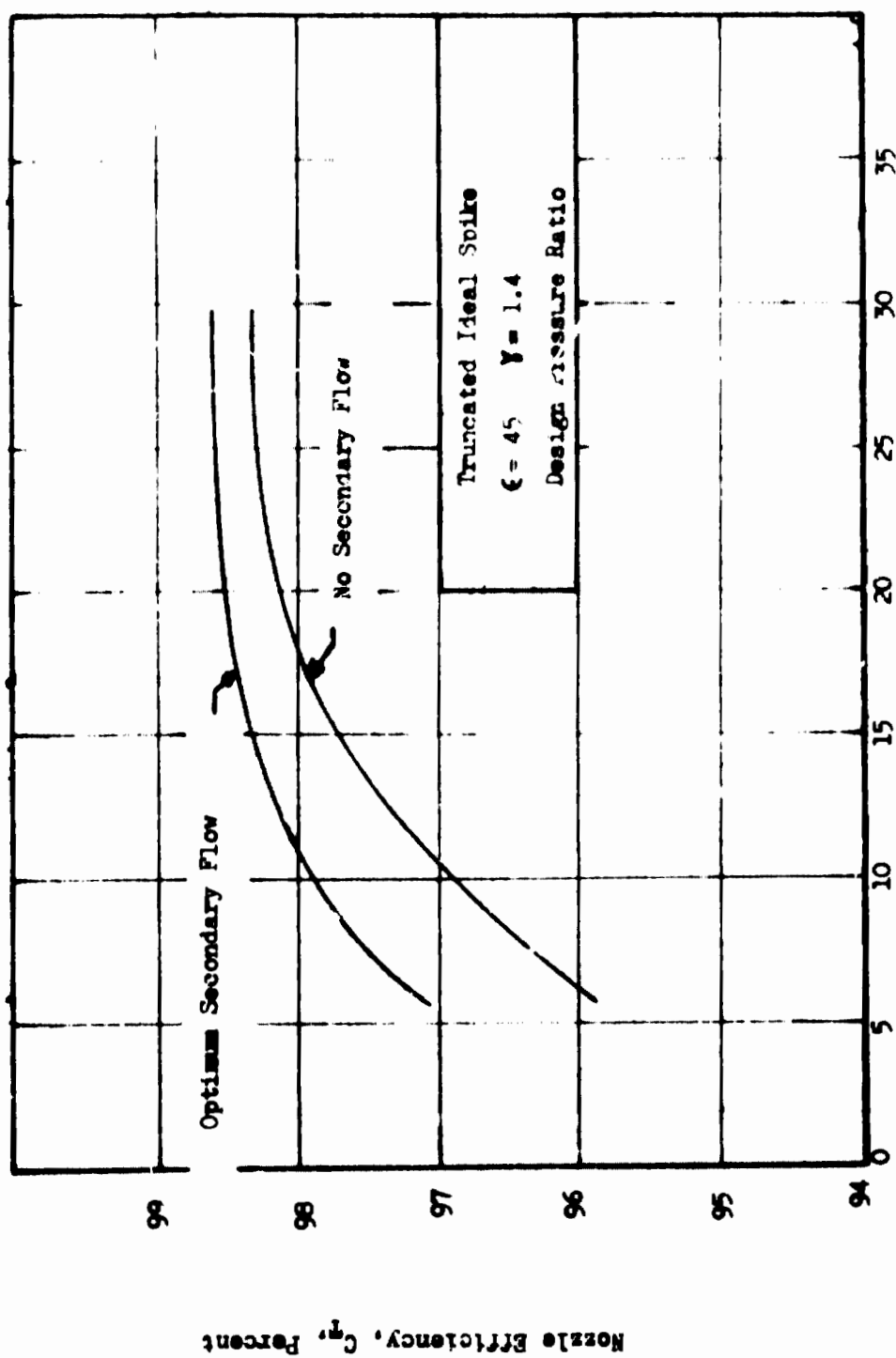


Fig. 11. Variation of Nozzle Efficiency with Length

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HIGH-AREA-RATIO NOZZLE STUDY

Analytical and experimental studies of the aerodynamic spike nozzle with expansion area ratios as high as 53 have shown this concept to be capable of achieving high performance efficiency over a wide range of pressure ratios with a short nozzle length. In this program, a test series was designed to investigate aerodynamic spike nozzle performance at much higher area ratios ($\epsilon = 150$). The major objectives of this cold flow program were:

1. To determine potential aerodynamic spike performance at high area ratios ($\epsilon = 150$).
2. To evaluate theoretical methods of analyzing high-area-ratio aerodynamic spike nozzles.

The models selected for testing were a contoured nozzle with 10 percent (of a 15 degree conical nozzle) axial length and a 45 degree conical nozzle with 6 percent axial length (Fig. 12). Both models were tested with various secondary flows to augment performance. Helium was used for both the primary and the secondary flows.

The test program concentrated on the evaluation of the high performing contoured model for pressure ratios from 160 to 79,000 and secondary flowrates from 0 to 5 percent of the primary flowrate. Several base injection configurations were tested. A total of 45 data points were obtained with the contoured model. Testing of the 45 degree conical model was conducted in the high pressure ratio regime to evaluate theoretical methods of analyzing aerodynamic spike nozzles with high exit flow angles. A total of 15 data points were obtained with the conical model.

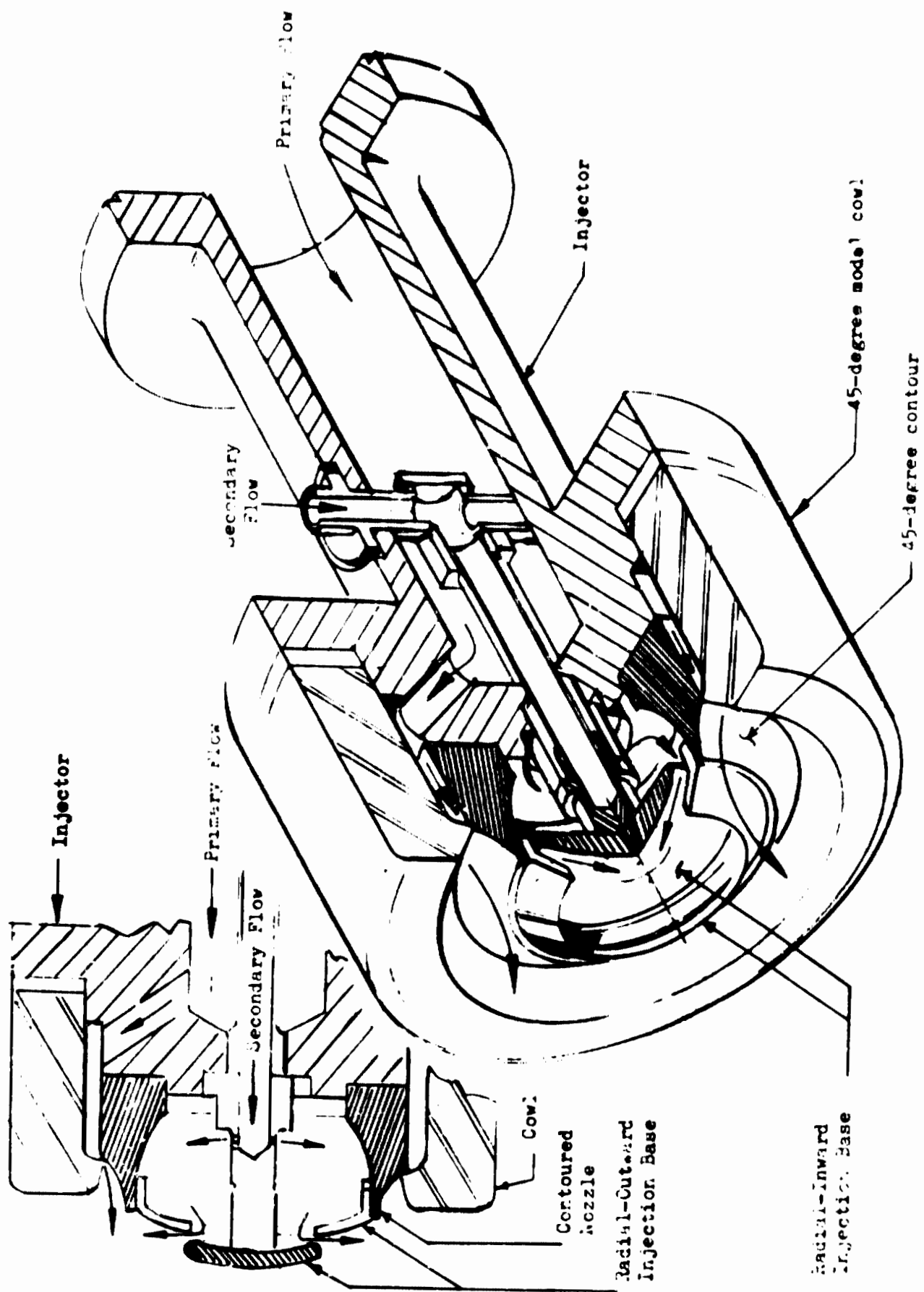


Fig. 12 High-Angle Injection Models

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A detailed discussion of the models, instrumentation, test method, and test facility was presented in Ref. 1.

PERFORMANCE DEFINITION

In the following sections the performance of the models has been evaluated in terms of nozzle efficiency, C_T (see Appendix 1). The efficiency, C_T , is equal to

$$C_T = C_F / C_{F_{opt}} (1 + \dot{W}_s / \dot{W}_p)$$

C_F can be broken down as follows:

$$C_F = C_{F_{int}} - C_{F_{drag}} + \frac{P_{cowl}}{P_c} \epsilon_{cowl} + \frac{P_b}{P_c} \epsilon_b - \frac{P_a}{P_c} \epsilon_{tot} \quad (1)$$

The areas of the nozzle upon which the forces represented by these terms act are indicated in the sketch of the aerodynamic spike nozzle control surface in Fig. 13.

The intrinsic thrust coefficient $C_{F_{int}}$ is defined as the sum of the momentum and the pressure forces acting on the primary nozzle throat and the nozzle contour, divided by the term $P_c A^*_t$. The $C_{F_{drag}}$ term is the thrust coefficient loss caused by boundary layer drag in the primary nozzle. The primary thrust coefficient ($C_{F_{int}} - C_{F_{drag}}$) acts on the annular area between points 2 (the outer expansion point) and 3 of Fig. 13. The term $(P_{cowl}/P_c) \epsilon_{cowl}$ is the thrust coefficient increment caused by the pressure on the outer contour of the primary nozzle; and it acts on the annular region between points 1 and 2. The term $(P_b/P_c) \epsilon_b$ is the thrust coefficient increment caused by base pressure, which acts on the area between points 3 and 4. The $(P_a/P_c) \epsilon_{tot}$ term represents the loss in thrust coefficient caused by ambient pressure acting on the nozzle over the area between points 1 and 6.

Definitions

$$\begin{aligned} A^*_t &= \text{Aerodynamic Throat Area} \\ \epsilon_{tot} &= A_{tot}/A^*_t \\ \epsilon_e &= A_e/A^*_t \\ \epsilon_b &= A_b/A^*_t \\ \epsilon_p &= (A_e - A_b)/A^*_t \\ \epsilon_{cowl} &= (A_{tot} - A_e)/A^*_t \end{aligned}$$

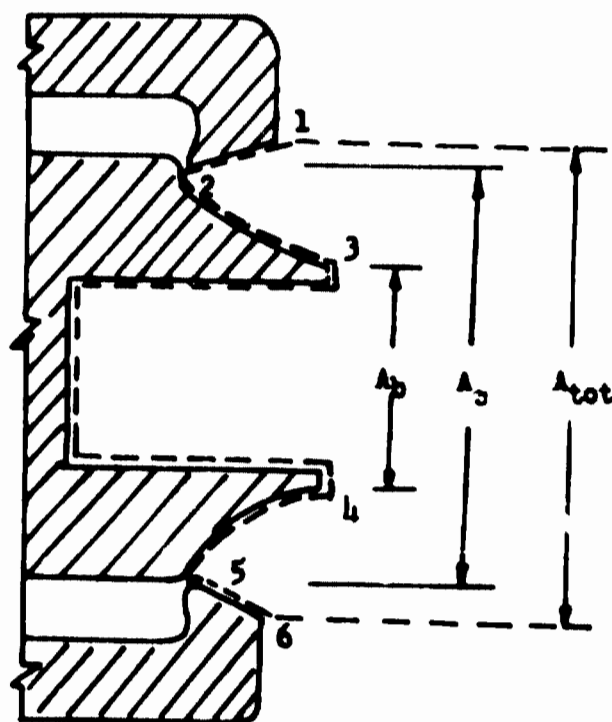


Fig. 13. Aerodynamic Spike Nozzle Control Surface

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The test data used in the following discussions of the test results are given in Appendix 2. Note that the efficiencies, C_T , are presented with and without the thrust contribution of the outer cowl. The primary flow was attached to the outer cowl surface and produced a small thrust contribution $\left[(P_{\text{cowl}} - P_a) / P_c \right] \epsilon_{\text{cowl}}$ at high pressure ratios; and the flow separated from the surface and produced a small drag at low pressure ratios. It was considered best to discuss the data neglecting the cowl contribution to simplify the comparison between the experimental data and the predicted performance. Therefore, the results presented in the following discussions do not include the $\left[(P_{\text{cowl}} - P_a) / P_c \right] \epsilon_{\text{cowl}}$ term; and the effective exit area of the nozzle becomes A_e . Then the breakdown of nozzle thrust coefficient is

$$C_F = C_{F_{\text{int}}} - C_{F_{\text{drag}}} + \frac{P_b}{P_c} \epsilon_b - \frac{P_a}{P_c} \epsilon_e \quad (2)$$

THE CONTOURED AERODYNAMIC SPIKE MODEL

A contoured aerodynamic spike with an axial length 10-percent that of an equivalent 15 degree cone and an expansion area ratio of 150:1 was designed to determine potential performance at high area ratios. A summary of the 45 data points obtained with this model is given in Table 1. The model was tested with an open base cavity with secondary flow introduced through an orifice recessed in the cavity. Flow emerges radially through eight holes in the orifice. Base configurations which injected secondary flow radially inward and outward at the base exit plane were also tested to determine the effect of these methods of secondary flow injection on performance.

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TABLE 1
HIGH-AREA-RATIO TEST PROGRAM SUMMARY, CONTOURED MODEL

Base Geometry	Secondary Flow, percent $\dot{w}_p$	P_c/P_a	Area Ratio A_o/A^*_t	Percent Length	Number of Tests
Open Cavity	0	160-69,000	147.5	9.89	19
	0	66,000	156.8	9.87	1
	1-5.1	73,000	147.5	9.89	5
	1.1-4.75	1124-9935	147.5	9.89	8
Radial-Inward (Large Gap)	0, 1.5	60,000	147.5	9.89	2
	1.39, 1.72, 2.73	60,000	156.8	9.87	3
Radial-Inward (Small Gap)	2.04	55,000	156.8	9.87	1
Radial-Outward	0-2.05	50,000	156.8	9.87	3
Instrumented Sting (1/4 inch diameter)	0, 4.79, 4.83	60,000	156.8	9.87	3
					—
					45

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During testing of the contoured model the model was disassembled once. Reassembly of the model resulted in an approximately 0.0006 inch change in the model aerodynamic throat gap which changed the model area ratio from 147.5 to 156.8. The change in area ratio is indicated in the table summarizing the tests with this model. However, it causes a difference of only 0.04 percent in the thrust coefficient. In view of this small difference it is reasonable to neglect the change in area ratios in the analysis of the model.

Experimental Performance

The contoured model was tested with an open base cavity and with no secondary flow over a pressure ratio range of 160 to 70,000. It was also tested with secondary flow at a high pressure ratio of approximately 73,000 and at several intermediate pressure ratios from 1100 to 10,000. A photograph of this model is shown in Fig. 14. In these tests the secondary flow was introduced into the base cavity using the radial-outward injection orifice which can be seen in the photograph.

The efficiencies from the tests without secondary flow over the pressure ratio range from 160 to 70,000 are presented in Fig. 15. The curve through these points indicates peaks in efficiency at pressure ratios of approximately 1600 and 25,000 (design pressure ratio). For comparison, a fully-expanded, fixed-flow nozzle is also shown on the figure. The base pressures corresponding to these tests are plotted versus pressure ratio in Fig. 16.

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Fig. 14. Contoured Aerodynamic Film Turbine, 1000 RPM, 1000 HP

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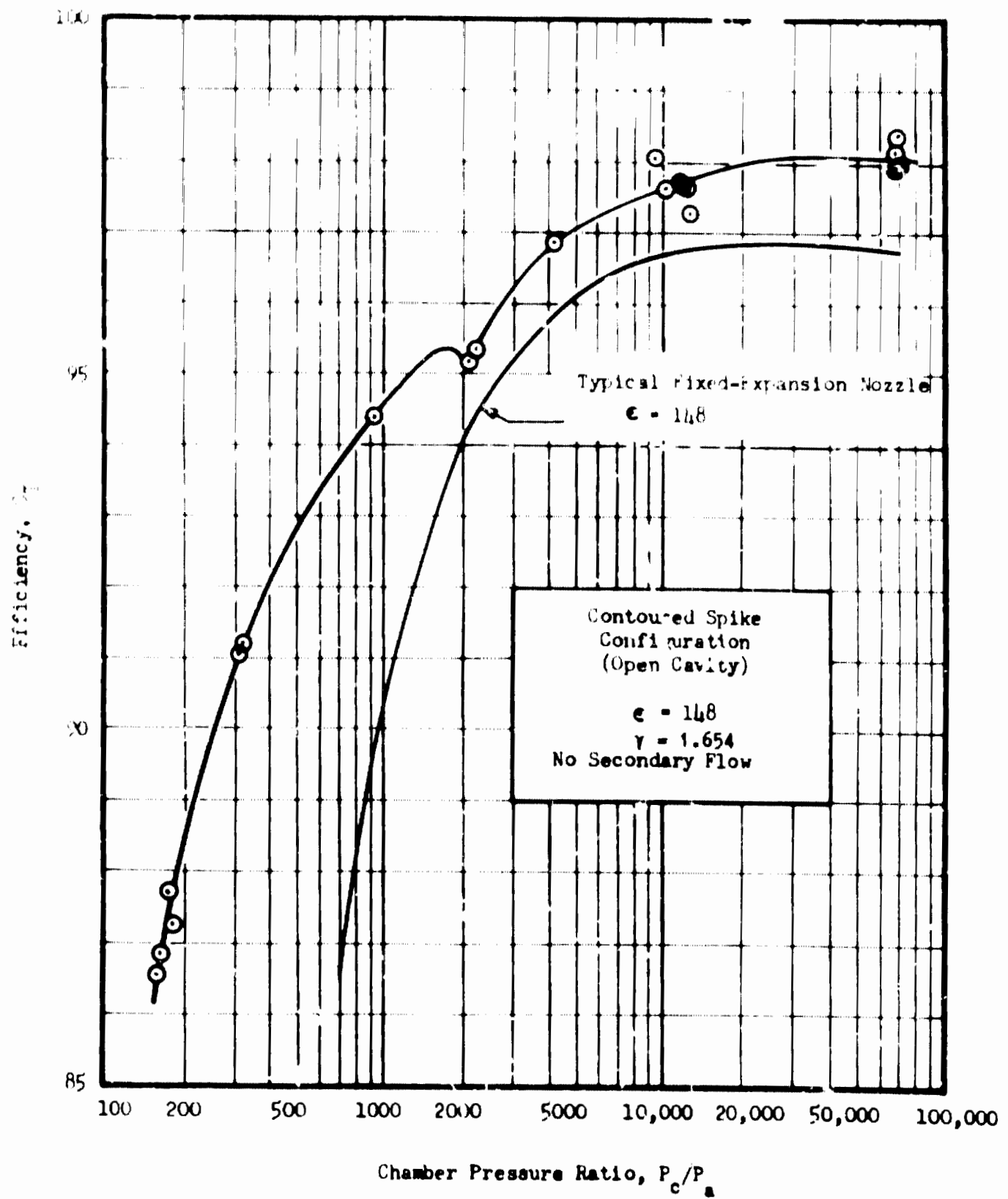


Fig. 15. Efficiency vs Chamber Pressure Ratio, Contoured Aerodynamic Spike Nozzle

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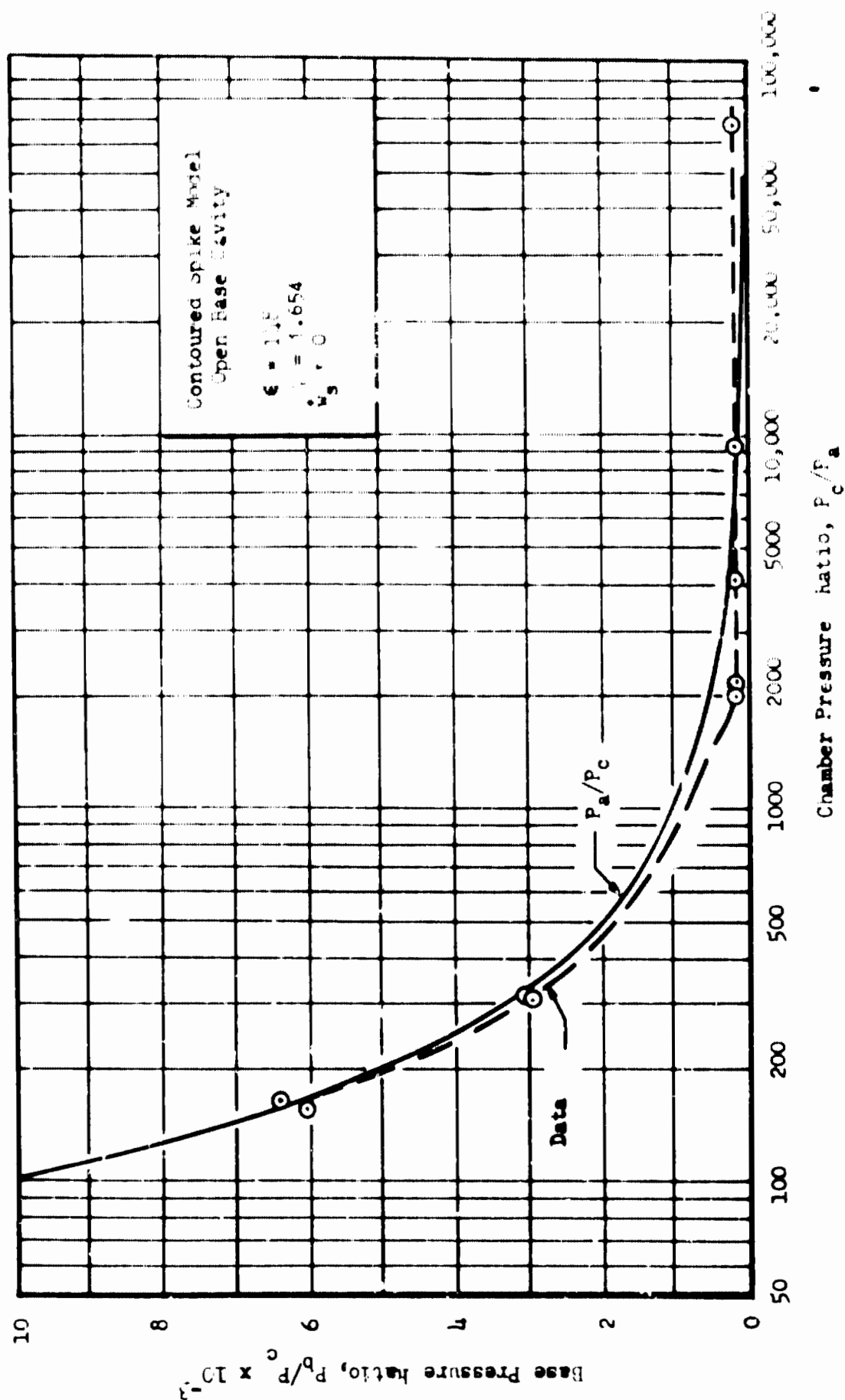


Fig. 16. Base Pressure Ratio vs Chamber Pressure Ratio. Contoured Aerodynamic Spike Nozzle Configuration

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In the low pressure ratio range from 150 to 1800, the wake of the contoured spike nozzle was open and the base pressure was slightly less than ambient pressure. In this region, C_m rises to over 95 percent and is much greater than that which would be expected from a 148:1 area ratio, fixed-expansion nozzle. The efficiency is comparable to that of a nozzle of lower area ratio. This can also be deduced from an inspection of the components of aerodynamic spike performance. If Eq 2 is further broken down by separating the $(P_a/P_c) \epsilon_s$ term into its components $(P_a/P_c) \epsilon_b$ and $(P_a/P_c) \epsilon_p$, where ϵ_p or $(\epsilon_s - \epsilon_b)$ is the area ratio of the primary nozzle expansion surface, the factors contributing to performance are:

$$C_F = C_{F_{int}} - C_{F_{drag}} + \frac{P_b - P_a}{P_c} \epsilon_b - \frac{P_a}{P_c} \epsilon_p$$

When the base pressure of the spike nozzle is equal to ambient pressure the term $[(P_b - P_a)/P_c] \epsilon_b$ is equal to zero (shown in Fig. 16); the remaining equation is equivalent to that of fixed-expansion nozzle

$$C_F = C_{F_{int}} - C_{F_{drag}} - \frac{P_a}{P_c} \epsilon_p$$

Thus, if the aerodynamic spike nozzle is compared to a fixed expansion nozzle of the same area ratio as the primary nozzle of the spike, the performance of the two nozzles can differ only by the differences in their intrinsic performance and the drag losses of their primary flow fields. In the case of the 148:1 spike the primary nozzle area ratio is 42:1; therefore, since the base pressure is almost equal to ambient pressure at low pressure ratios, the efficiency of the spike nozzle is

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very closely related to that of a 42:1 area ratio, fixed-expansion nozzle in this regime. However, at low pressure ratios, the occurrence of recompression in the primary nozzle of aerodynamic spike nozzles can result in further increases in performance.

In the high pressure ratio region from a pressure ratio of 2100 to 70,000 the contoured nozzle efficiency with no secondary flow increases from 95.2 percent to 98.1 percent. In this region, the wake is closed; and the base pressure does not change with pressure ratio. The difference between ambient and base pressure becomes less as pressure ratio increases until the two are equal at a pressure ratio of approximately 8000. Then, as pressure ratio is increased further, the base pressure is increasingly greater than ambient pressure and produces a positive thrust. The nozzle efficiency in this region is higher than that of the fixed-expansion nozzle with an area ratio of 148. At design pressure ratio (25,000), the efficiency peaks at approximately 98.13 percent.

The difference between the closed wake and open wake cone can be visualized by an inspection of Schlieren photographs of the contoured nozzle being tested in the low and high pressure ratio regions. Two such photographs are presented in Fig. 17. In Fig. 17a the photograph shows the nozzle wake at a pressure ratio of 56. At this pressure ratio the wake is open and the base pressure is approximately equal to ambient pressure. In Fig. 17b, the photograph shows the nozzle wake at a pressure ratio of 69,000 which is well above the pressure ratio at which the wake closes. At this pressure ratio the flow is fully expanded; the base pressure is greater than ambient pressure and does not change with pressure ratio.

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a. Open wake, Pressure Ratio = 52,000



b. Closed wake, Pressure Ratio = 52,000

Fig. 17 Contoured Nozzle Flow Fields

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Secondary flow was injected into the base region with the recessed orifice to augment performance. Several secondary flowrates were tested at high pressure ratios to determine the maximum efficiency that could be obtained. The pressure ratio varied from 66,800 to 79,100 during these tests. An average value, 73,000, is referred to when the efficiencies are compared. Since the difference in pressure ratio could theoretically make only a 0.02 percent difference in the performance, the data was not normalized to one pressure ratio. The efficiencies for these tests are presented versus secondary flowrate in Fig. 18. A maximum efficiency of 98.6 percent was obtained with a secondary flowrate of 1.4 percent of the primary flow, an increase of 0.5 percent over the case with no secondary flow. Performance equal to or in excess of the zero secondary flow case is achieved with secondary flows up to four percent of the primary; and performance was higher than that of a comparable area ratio bell nozzle for all secondary flowrates tested.

The base pressures for the tests are plotted versus secondary flow in Fig. 19. Base pressure increases with the addition of secondary flow. A change in the rate of increase occurs at a secondary flow of 1.4 percent. This change in slope occurs at the same secondary flowrate for which maximum efficiency was obtained.

The efficiencies resulting from the addition of secondary flow in the intermediate pressure ratio range are plotted versus pressure ratio in Fig. 20. The addition of secondary flow allows a high efficiency to be maintained throughout the tested pressure ratio range. A C_T greater than 96.5 percent is achieved at all pressure ratios greater than 8 percent of design pressure ratio. The gains in efficiency achieved with secondary flow at various pressure ratios are compiled

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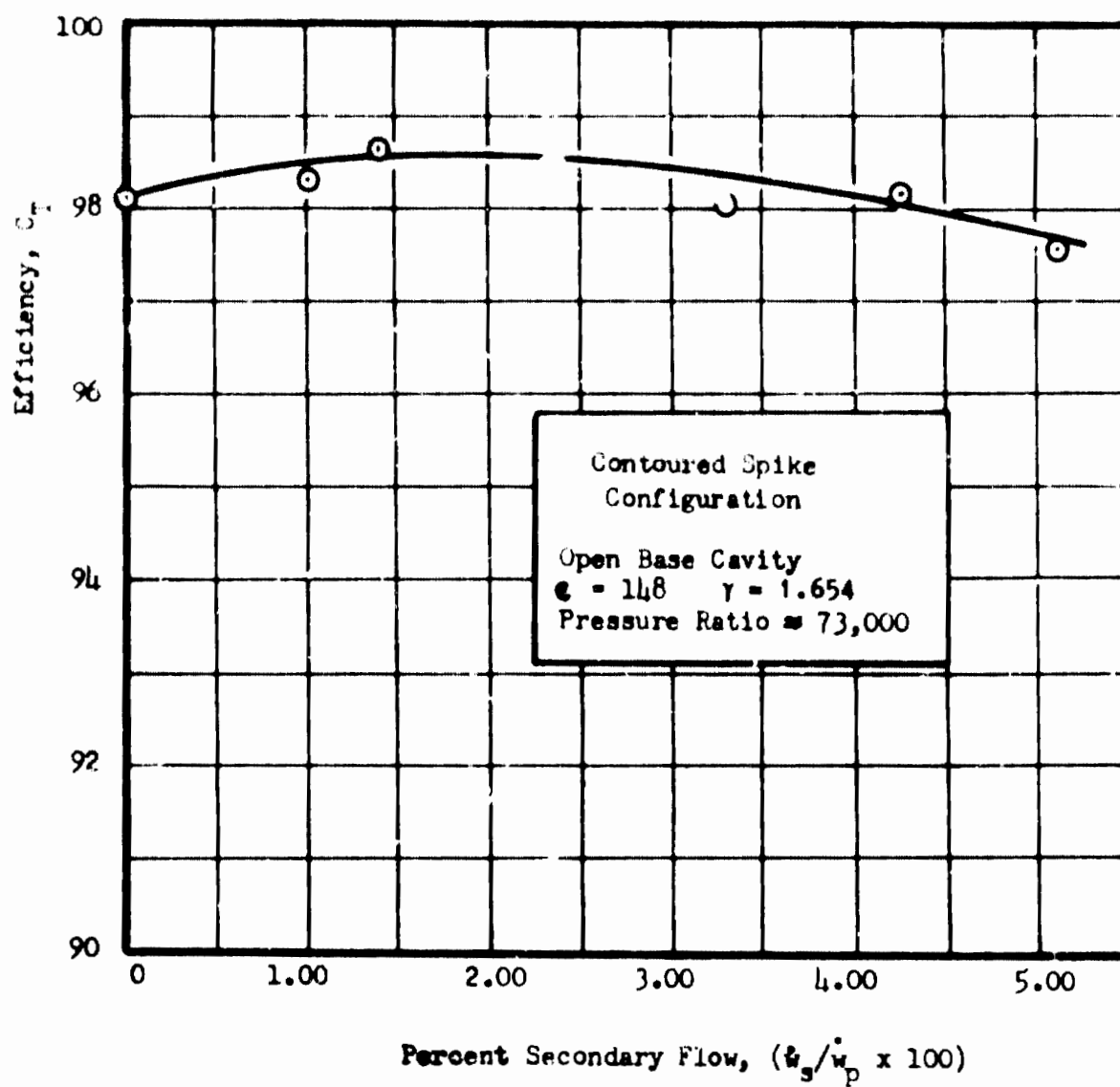


Fig. 18 Efficiency vs Secondary Flow
Contoured Aerodynamic Spike Configuration

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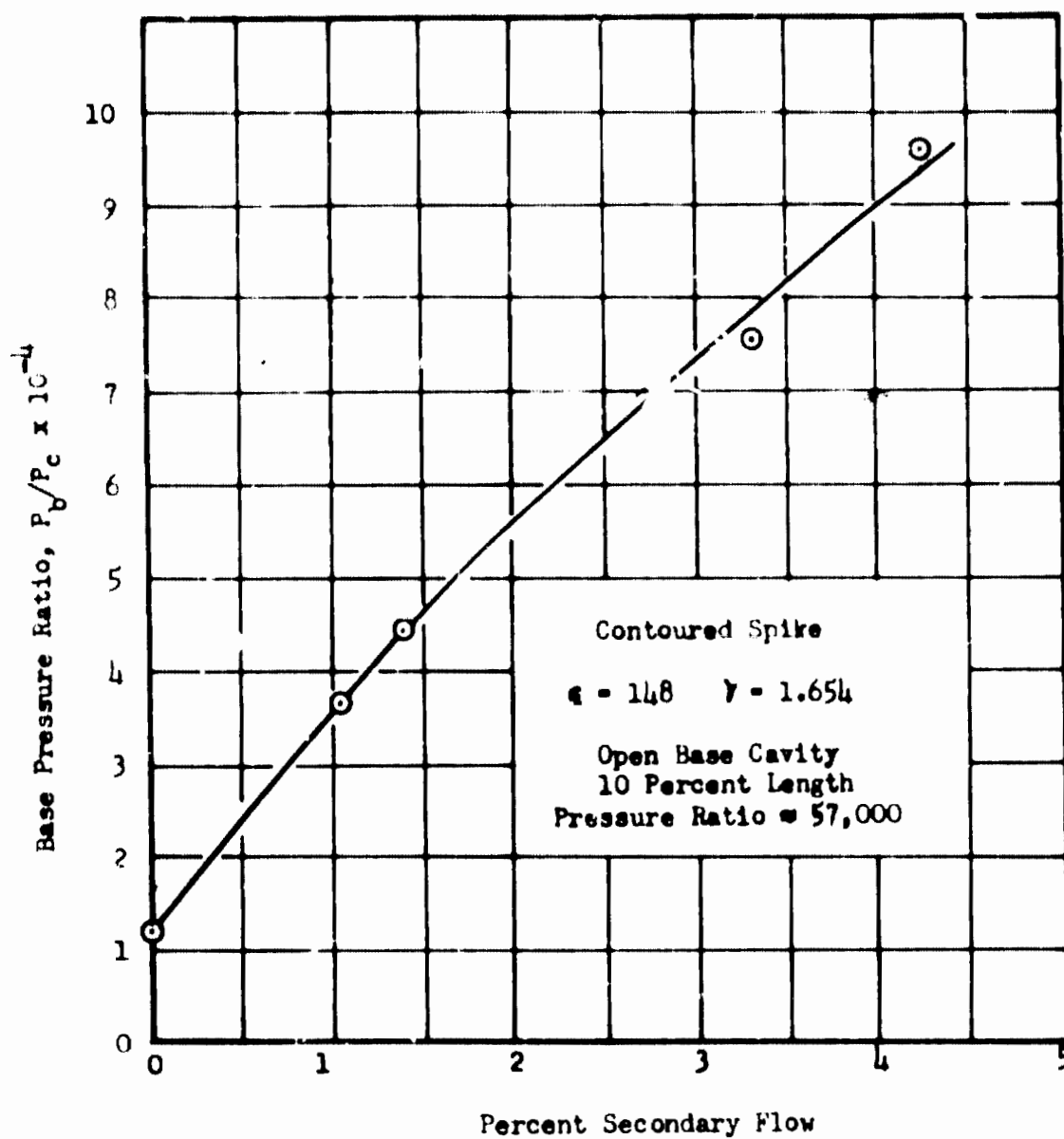


Fig. 19. Base Pressure Ratio versus Secondary Flow, Contoured Spike Model

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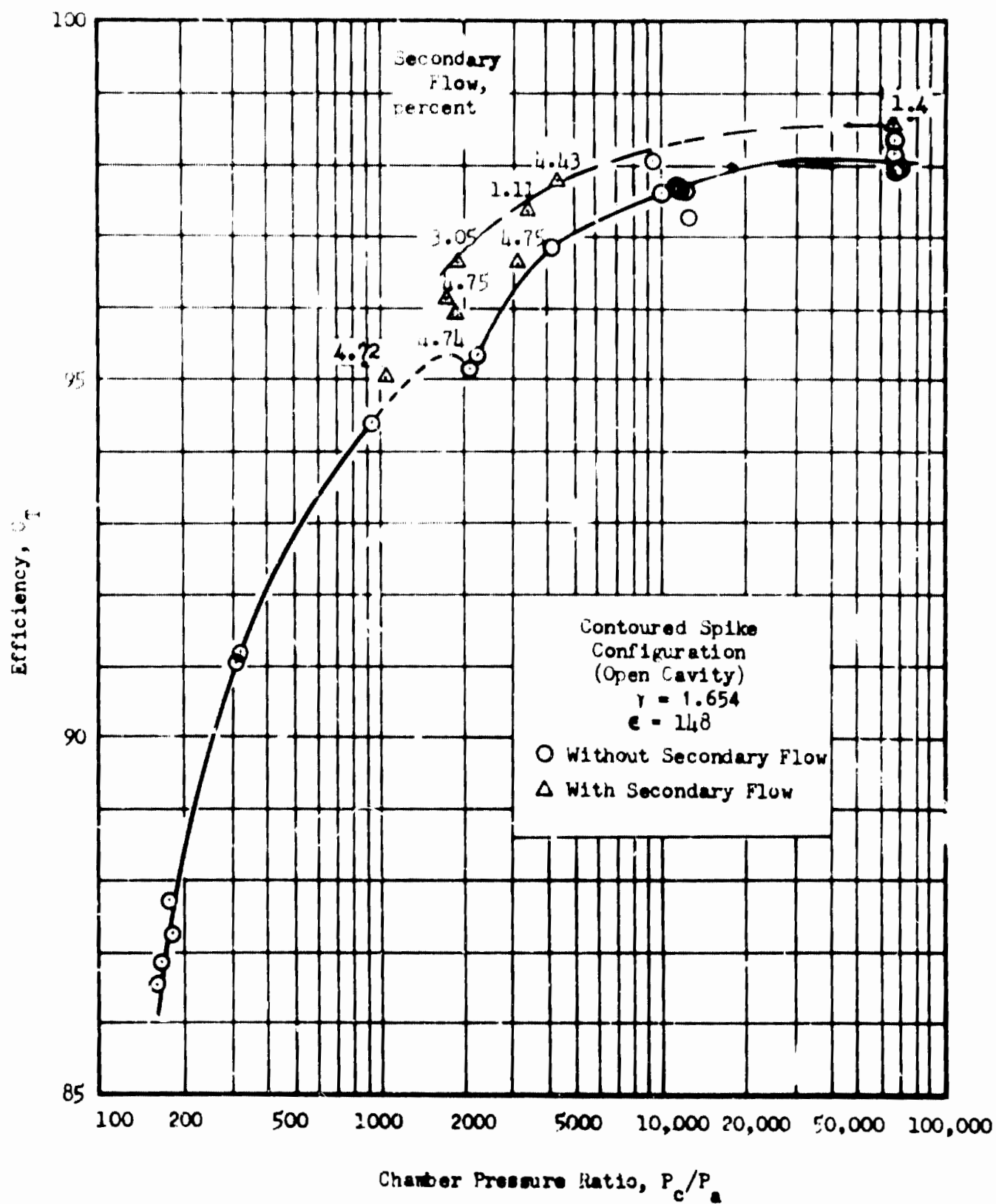


Fig. 20. Efficiency vs Chamber Pressure Ratio
 Contoured Aerodynamic Spike Nozzle

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in Table 2. Note that these secondary flowrates do not necessarily represent those with which maximum efficiency would be attained; they do indicate the performance potential with secondary flow in the tested pressure ratio range.

TABLE 2

Efficiency Increases Achieved from Secondary Flow

P_c/P_a	$\dot{w}_s/\dot{w}_p$, percent	ΔC_T , percent
1850	3.05	+1.3
3300	1.11	+1.1
4200	4.43	+1.1
73,000	1.40	+0.5

The base pressures are plotted for several pressure ratios with secondary flowrates of 1.0 and 4.75 percent of primary flow in Fig. 21. It can be seen that secondary flow increases the base pressure at all pressure ratios tested. Also, in the intermediate pressure ratio region around 4000 a secondary flow of 4.75 percent will increase base pressure above ambient pressure.

Comparison with Theoretical Predictions, Closed-Wake Regime

The theoretical efficiency of the contoured model was predicted prior to testing and presented in Ref. 1. The closed-wake performance predicted for the zero-secondary-flow case is compared with the experimental data in Fig. 22. The predicted efficiency at design pressure ratio was 98.2 percent; the experimental value was 98.1 percent.

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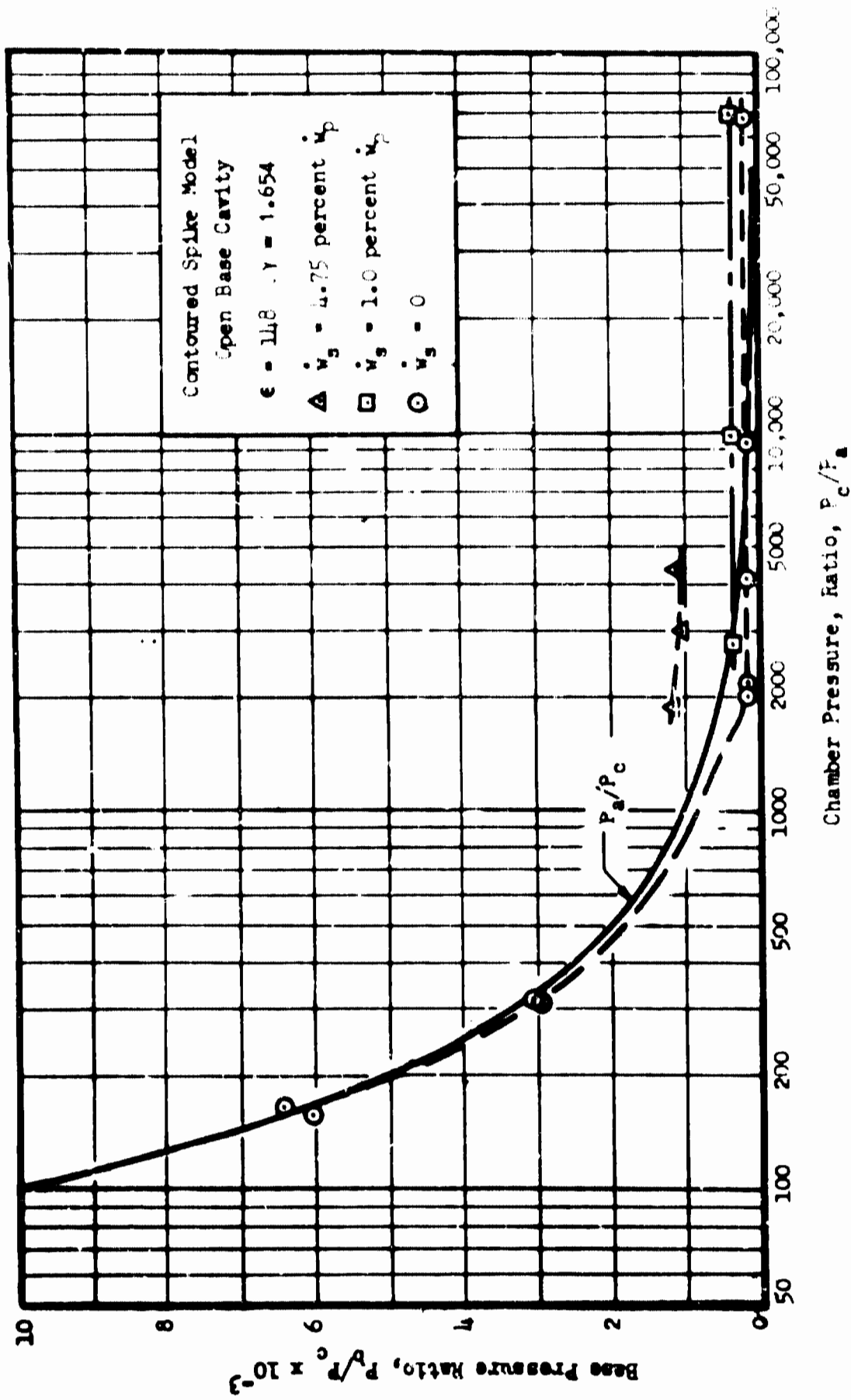


Fig. 21. Base Pressure Ratio vs Chamber Pressure Ratio. Contoured Aerodynamic Spike Nozzle Configuration

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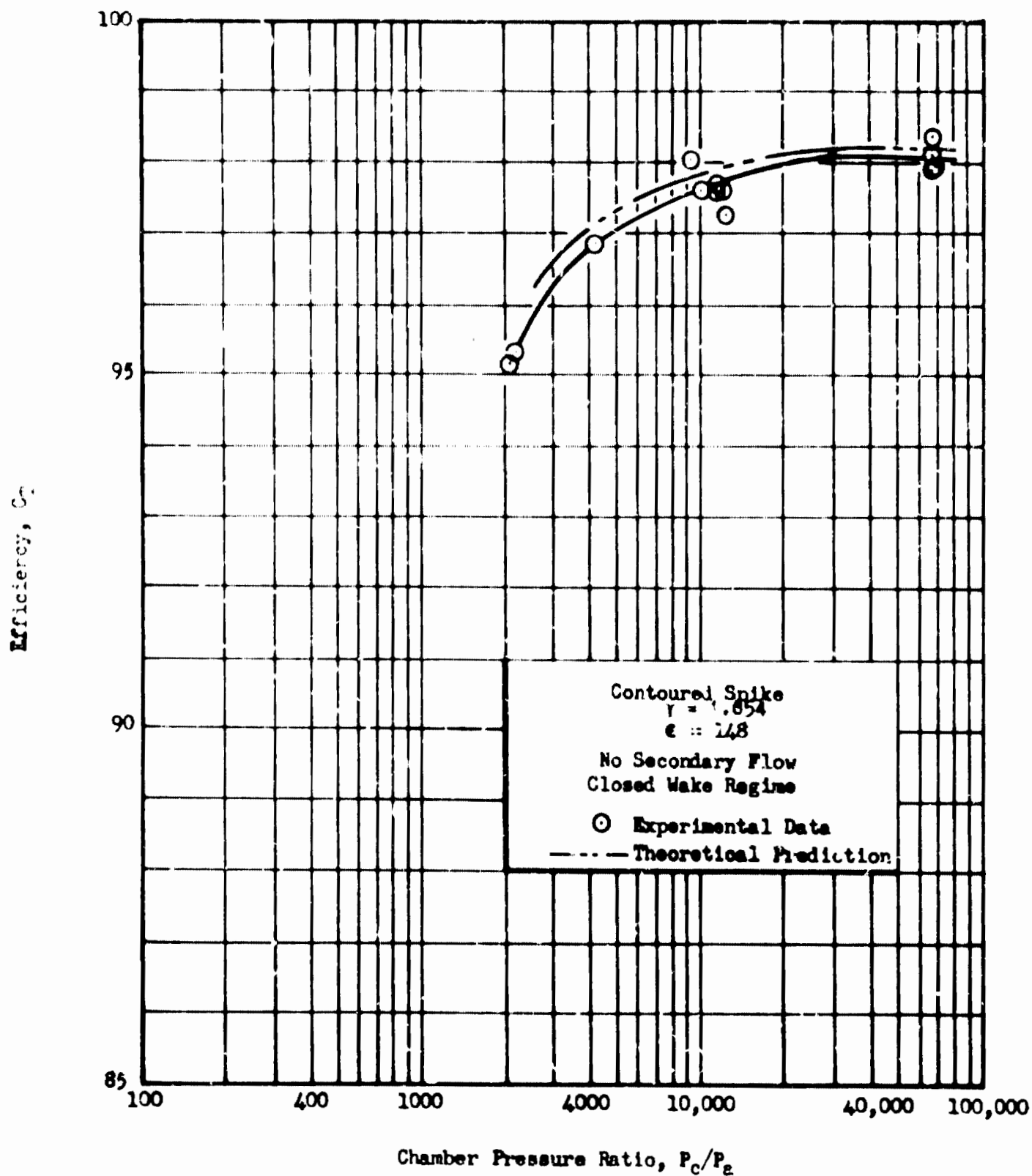


Fig. 22a Experimental and Theoretical Efficiencies of Contoured Model versus Pressure Ratio, Closed Wake Regime

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The experimental wall pressures were measured and are compared with the theoretical values in Fig. 23. The experimental values are lower than the predicted values near the model throat and higher along the rest of the nozzle wall.

In theoretically predicting the base pressure of the models, many of the ideas advanced by Korst and Nash were adopted for use, the most important aspect being the fact that the wake recompression phenomena controls the base pressure. The theoretically predicted base pressures for zero secondary flow are compared with the average measured base pressures in the closed-wake regime in Fig. 24. The theoretically predicted base pressure with no secondary flow was $P_b/P_c = 0.000158$; the average measured value was $P_b/P_c = 0.00012$.

The base pressure of the contoured model was predicted for bleed rates up to $\dot{w}_s/\dot{w}_p = 1.16$ percent. Furthermore, it was predicted that the small bleed regime would end at this point. The theoretical base pressures are plotted with the experimental results in Fig. 25. It can be seen that the theoretically predicted end of the small bleed regime occurs near the change in slope in the experimental curve. It is approximately at this change in slope where the maximum efficiency is achieved from the addition of secondary flow. The theoretically predicted efficiency with 1.16 percent secondary flow was 98.7 percent at the design pressure ratio as compared to the measured value of 98.6 percent.

Comparison with Theoretical Predictions, Open-Wake Regime

The nozzle efficiency predicted in Ref 1 for the open-wake regime is compared with the experimental data in Fig. 26, along with the closed-wake regime results. In this regime the difference between theory and

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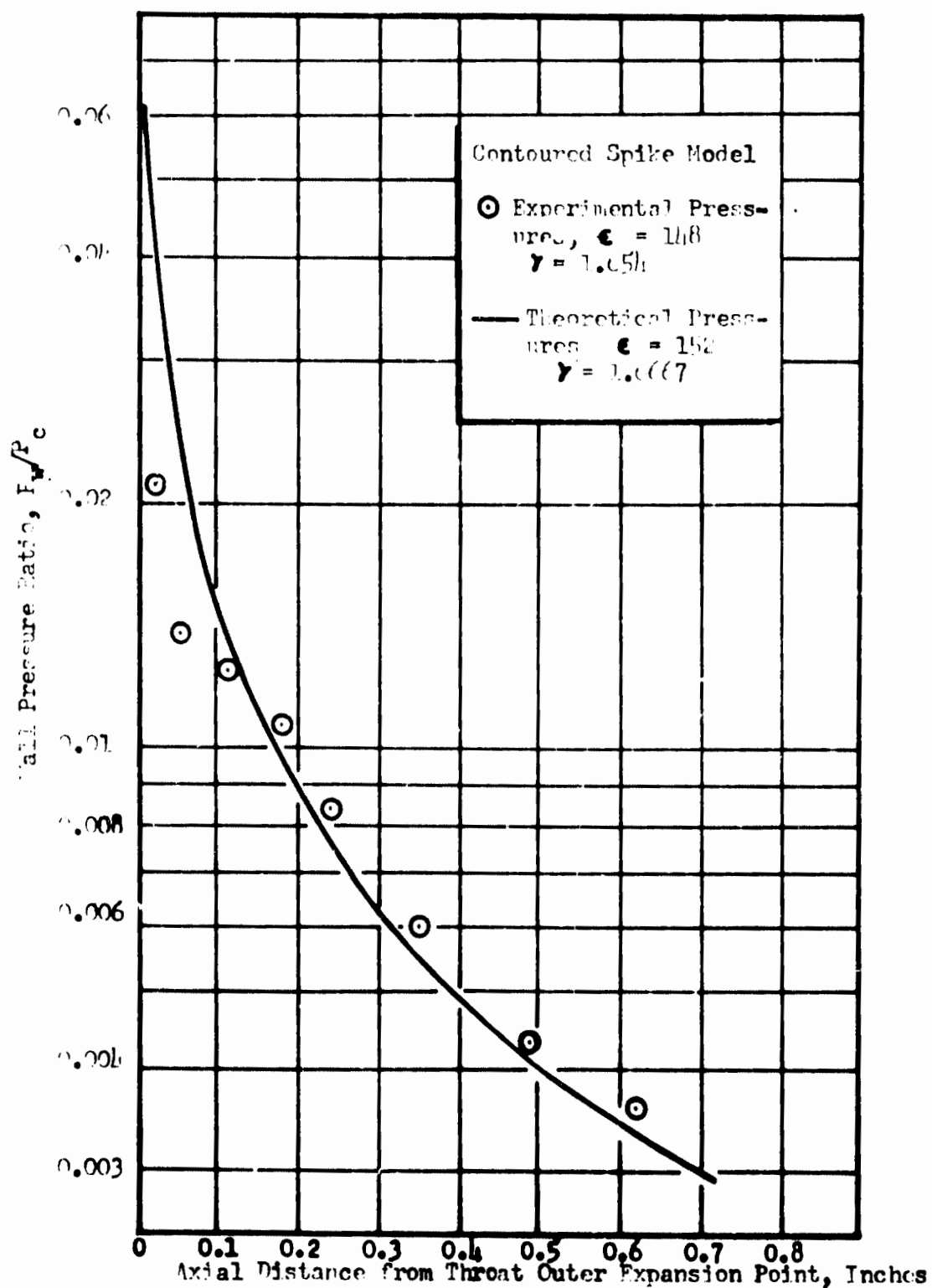


Fig.23. Theoretical and Experimental Wall Pressure Profiles, Contoured Spike Model

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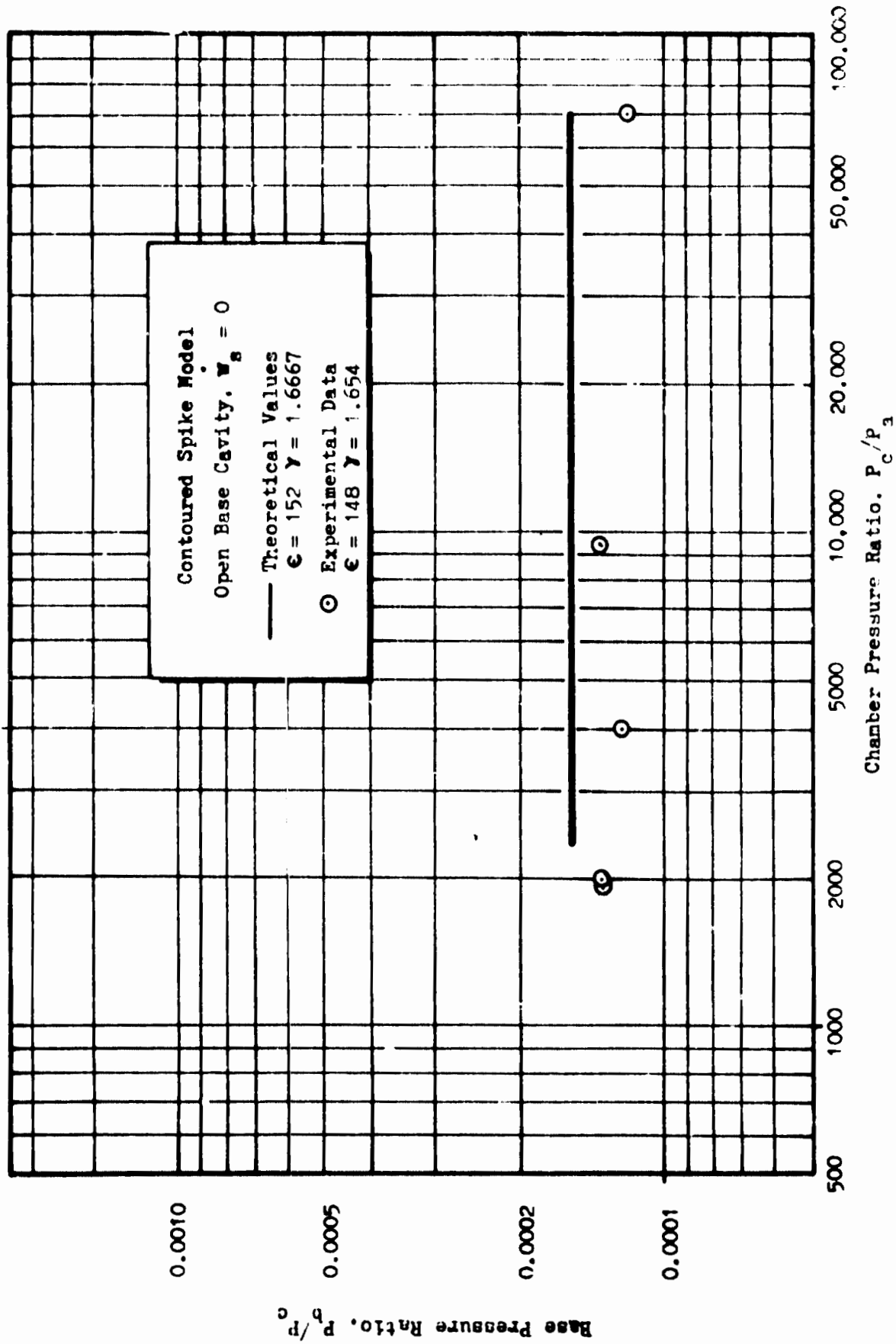


Fig. 24. Comparison of Theoretical and Experimental Base Pressure.
Closed Wake Regime

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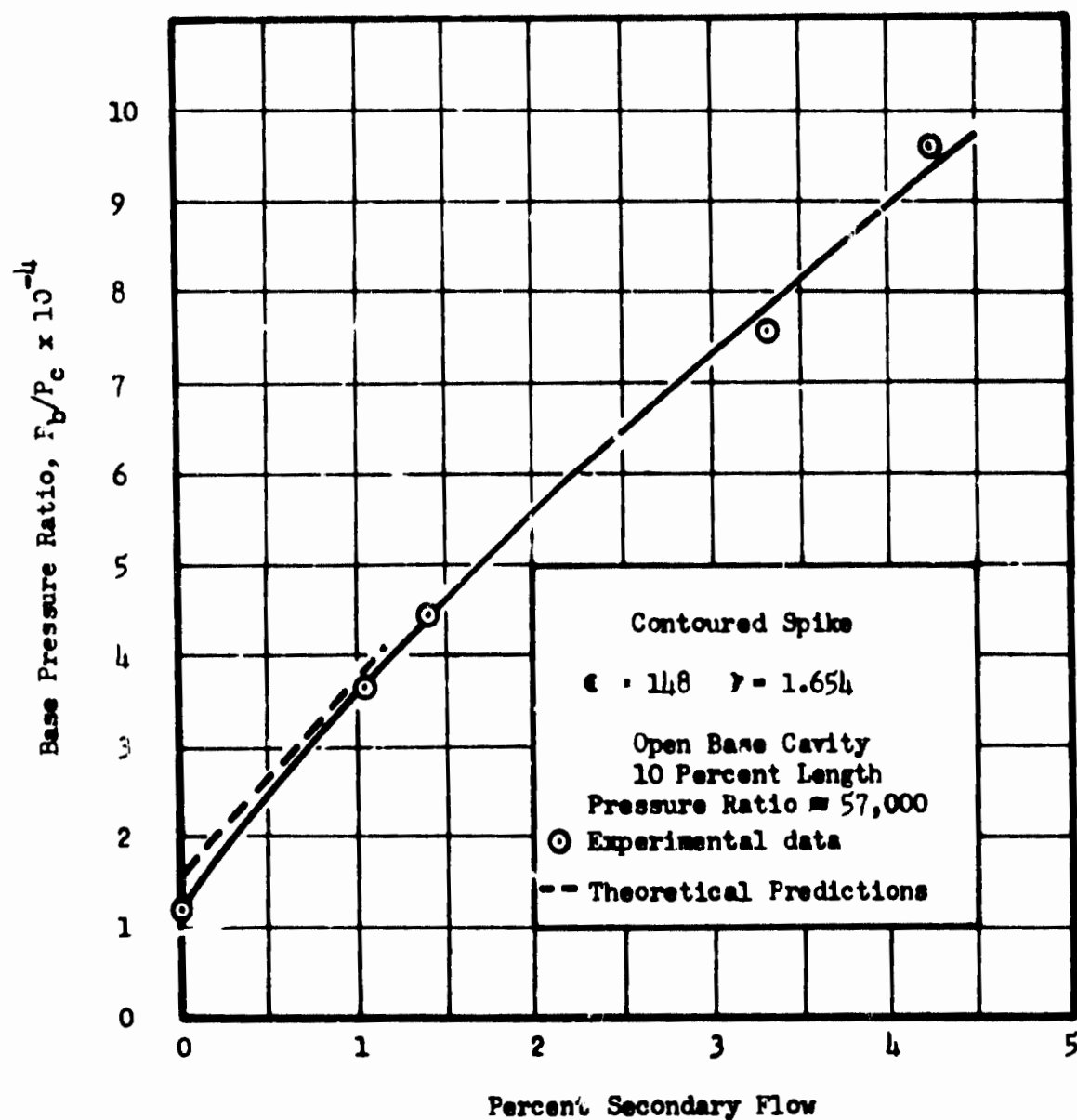


Fig. 25. Comparison of Theoretical with Experimental Base Pressures, Small Secondary Flows

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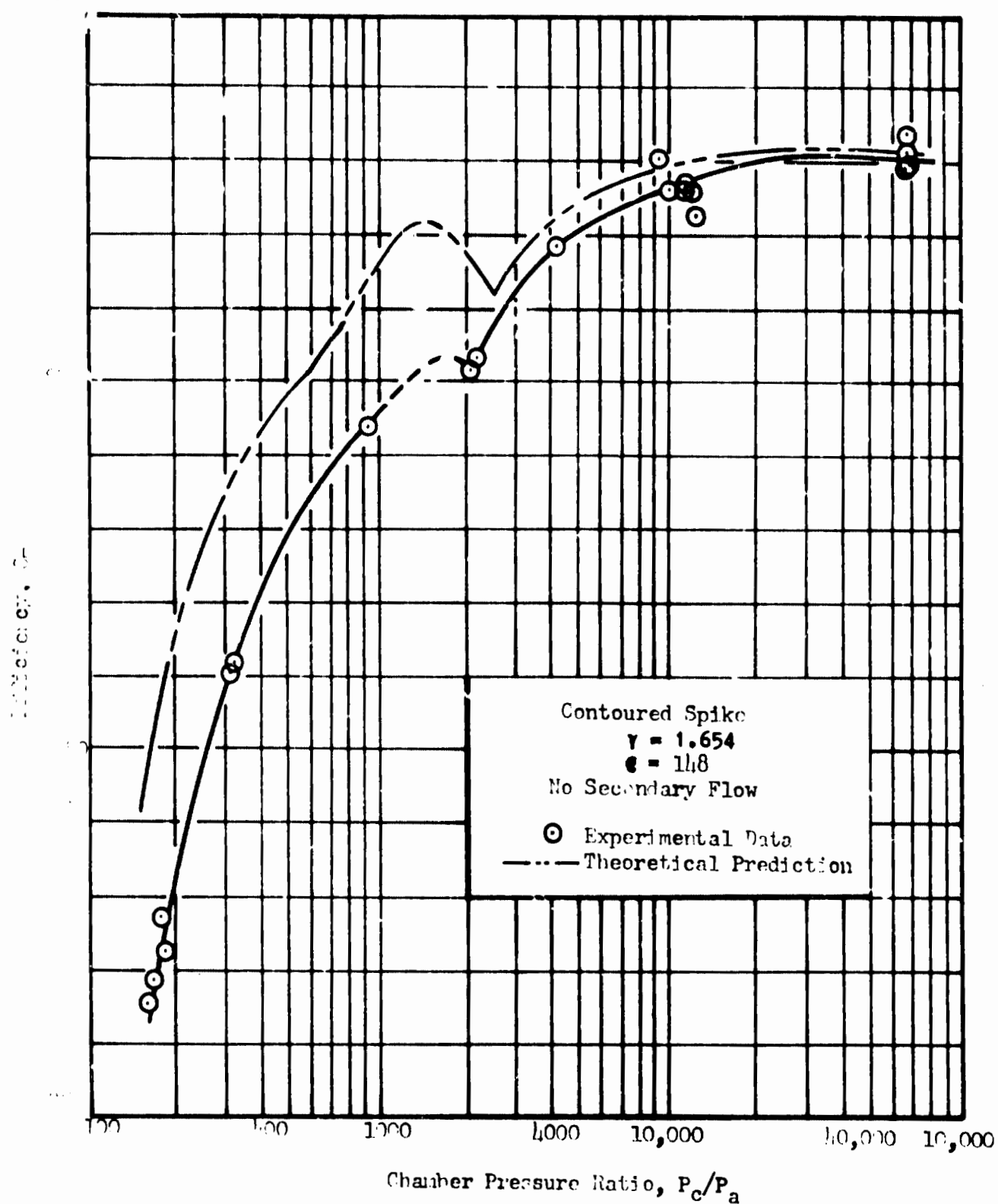


Fig. 26. Experimental and Theoretical Efficiencies of Contoured Model Versus Pressure Ratio

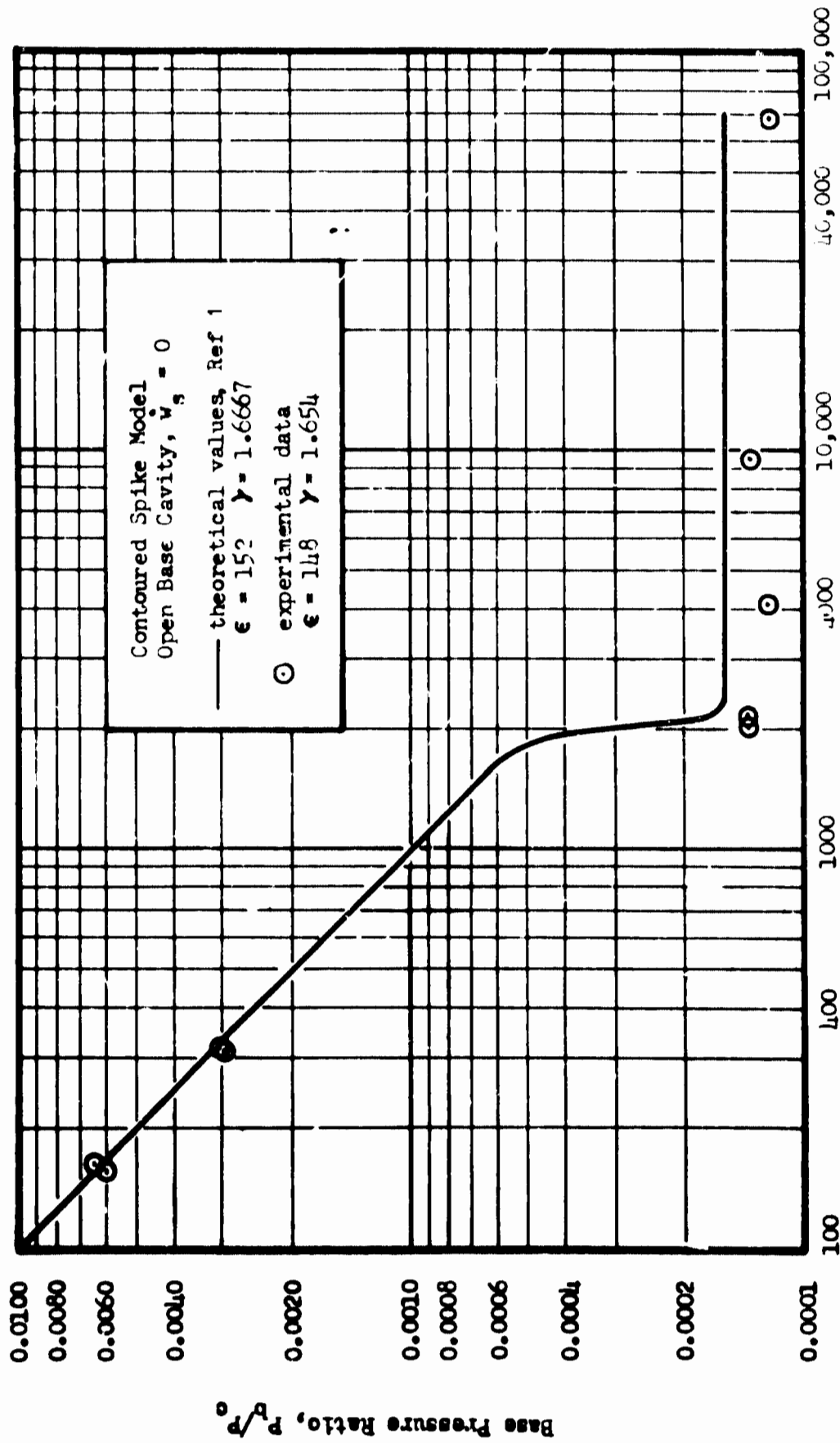
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experiment varies from 1.5 to 3 percent. The experimental base pressures are plotted with the predicted values in Fig. 27. The difference between experiment and prediction in the open wake region are small. Therefore, the difference between the theoretical and actual performance was attributed almost entirely to the analysis of the primary performance.

The theoretical primary nozzle pressure profiles were predicted for the open-wake regime in Ref 1. The methods used in the analysis had previously produced satisfactory results for cold-flow ($\gamma = 1.40$) and hot-firing ($\gamma = 1.23$) models. Recompression which occurred at a pressure ratio of 160 is indicated by the experimental wall pressures which are plotted in Fig. 28. These data are compared with the predicted recompression for a pressure ratio of 150. The difference between the actual and predicted recompression is partially caused by the variance between the actual primary nozzle geometry and the geometric assumptions used in the theoretical flow-field analysis. The theoretical calculation assumes a Prandtl-Meyer point expansion at the outer cowl lip (also the throat location) to find the position of the free jet boundary; whereas the actual expansion point has a finite radius and the expansion is influenced by the cowl pressure (slightly lower than ambient). Further, if a choked flow condition occurs before the assumed throat location, overexpansion would occur before the cowl exit point is reached. All of these factors tend to delay and reduce recompression. Further investigations of the analytical solution for the primary flow field is also warranted. To obtain high computational accuracy at this area ratio it becomes increasingly important to maintain an extremely fine flow net.

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Chamber Pressure Ratio, P_c/P_a

Fig. 27. Comparison of Theoretical and Experimental Base Pressures

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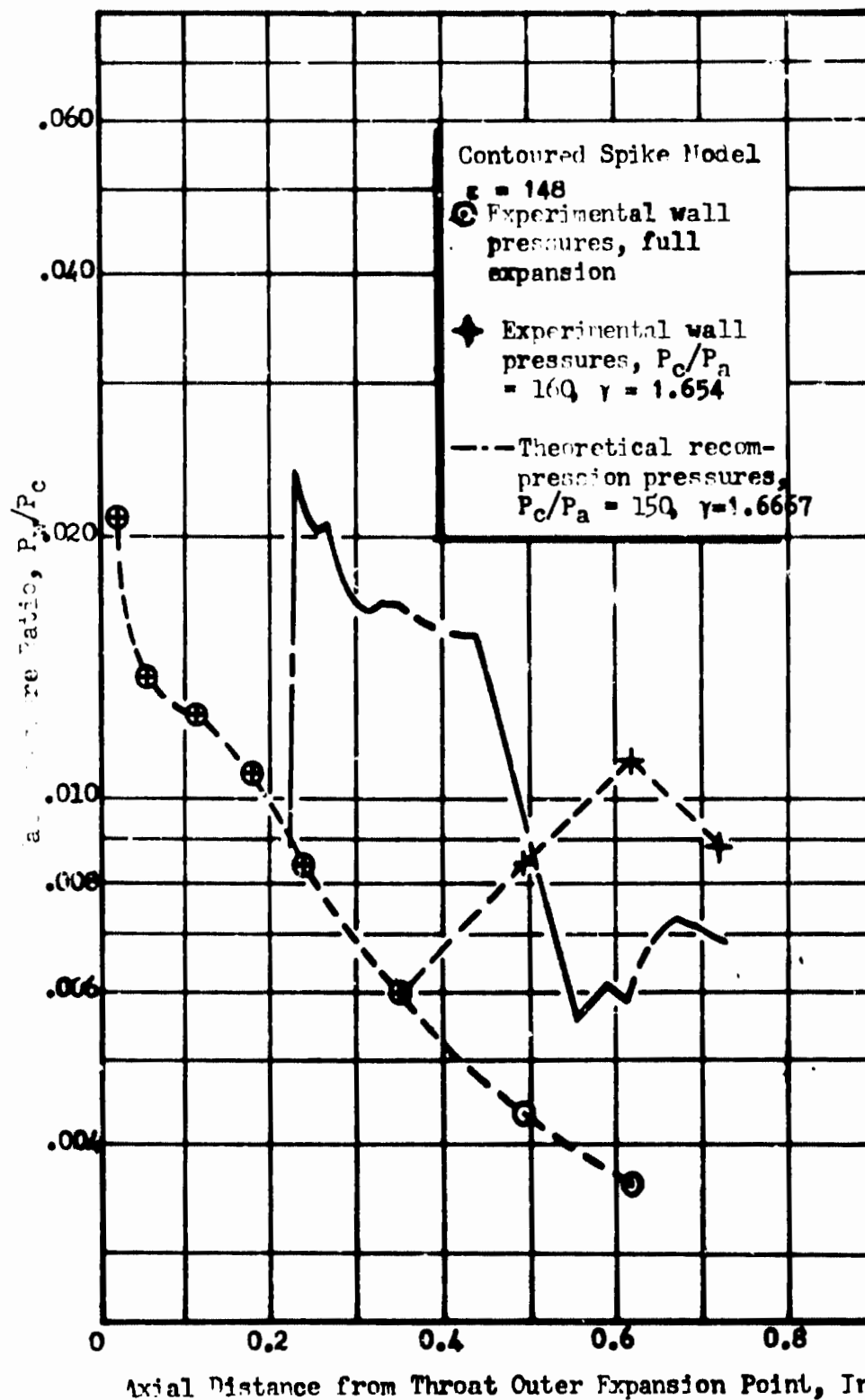


Fig. 28. Theoretical and Experimental Wall Pressures with Recompression, Contoured Spike Model

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Base Geometry Study

It was postulated from base-pressure theory that methods of secondary flow injection that introduce the secondary flow with no axial momentum and at a low Mach number would result in the most efficient use of secondary flow to increase base pressures. A radial-inward and a radial-outward secondary flow injector (Fig. 29 and 30 , respectively) were designed and fabricated to evaluate this postulate. The radial-inward fixture was designed to allow two annular gap spacings so that the Mach number at which a secondary flow was introduced could be changed.

The base pressures with these secondary flow injection methods in a pressure ratio range of 44,000-69,800 are plotted versus secondary flowrate in Fig. 31 . The base pressures with the recessed orifice are also plotted for comparison. Because the base pressures are a small part of the total thrust for this configuration, a large change in base pressure produces only a small change in efficiency. Also, the base pressures are not a complete indication of the effect of secondary flow on thrust with these methods of injection. The geometrical limitations of the base area did not allow designs of the base plates which would result in pure radial-inward and pure radial-outward secondary flow injection; there was some axial momentum to the secondary flow in the base exit plane in both cases. This axial momentum contributes to the thrust and the nozzle efficiency.

The model performance with the tested methods of secondary flow injection is shown on Fig. 32 . The results indicate that the large-gap radial-inward injection method was not as efficient as the recessed orifice method; however, the large-gap was slightly better than the small-gap,

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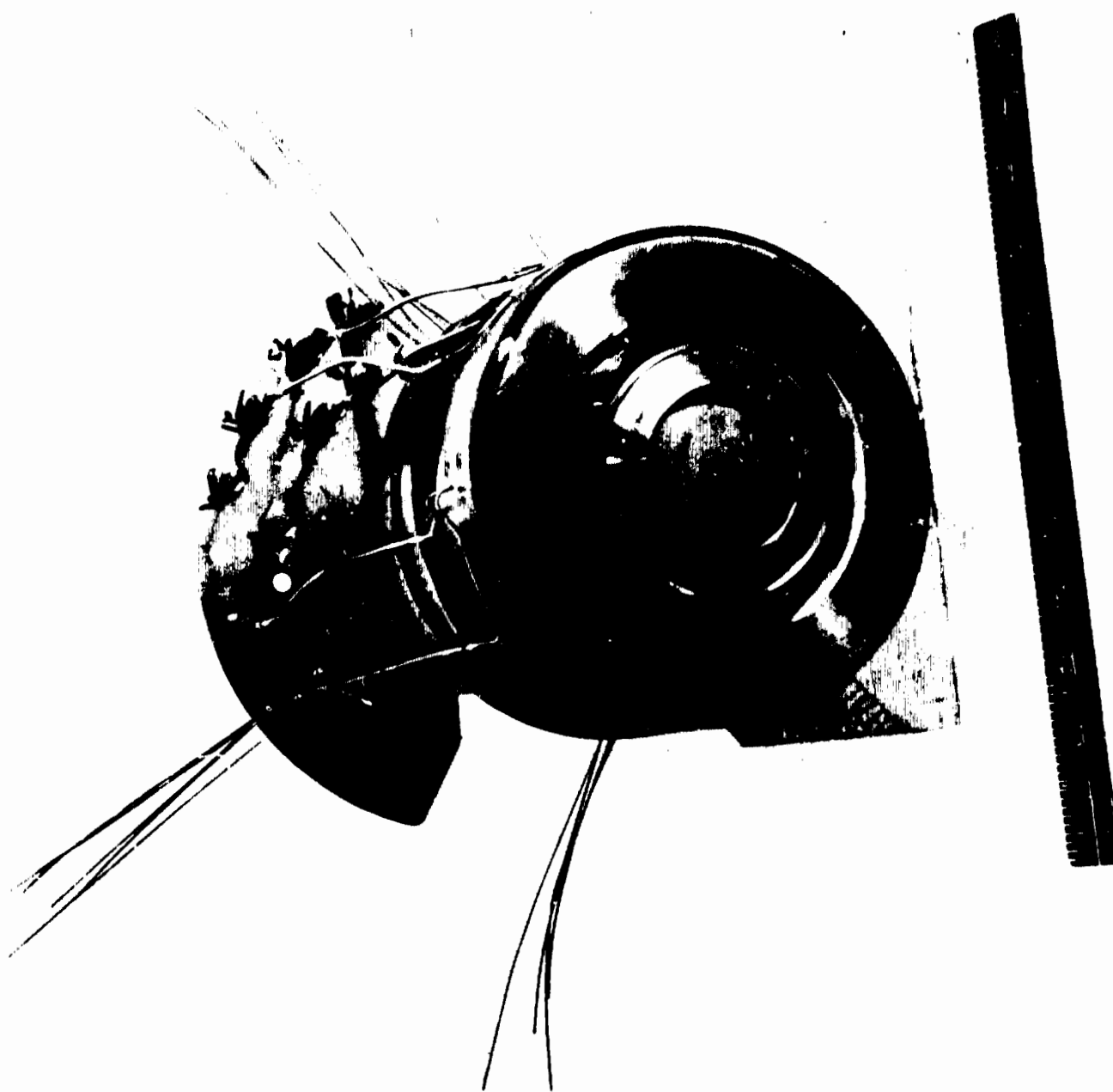


Fig. 29. Radial-Inward Secondary Injection Configuration Mounted on the Contoured Nozzle

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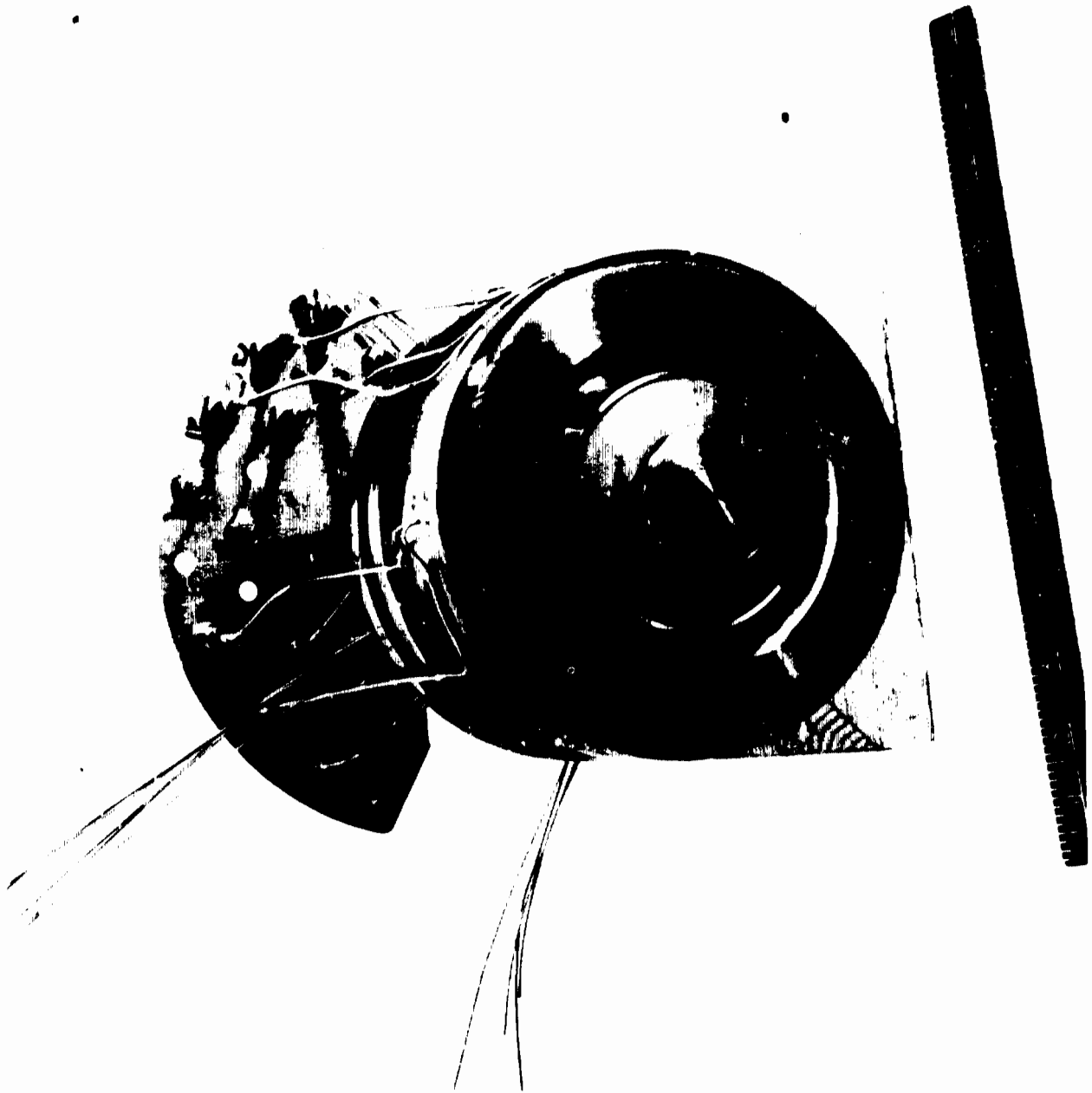


Fig. 30. Radial-Outward Injection Configuration Mounted on the Contoured Nozzle

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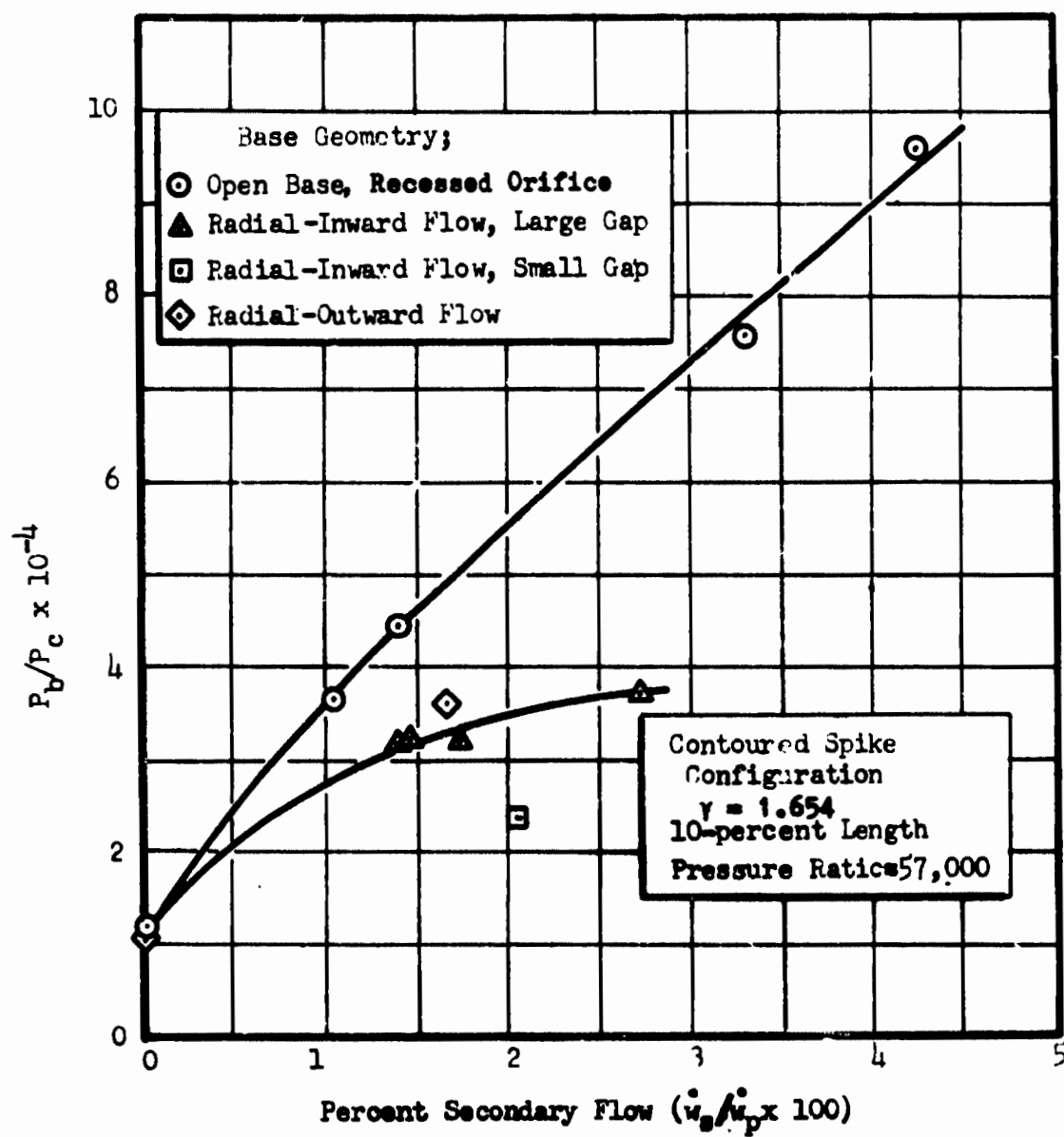


Fig. 31. Base Pressure Ratio vs Secondary Flowrate
Contoured Aerodynamic Spike

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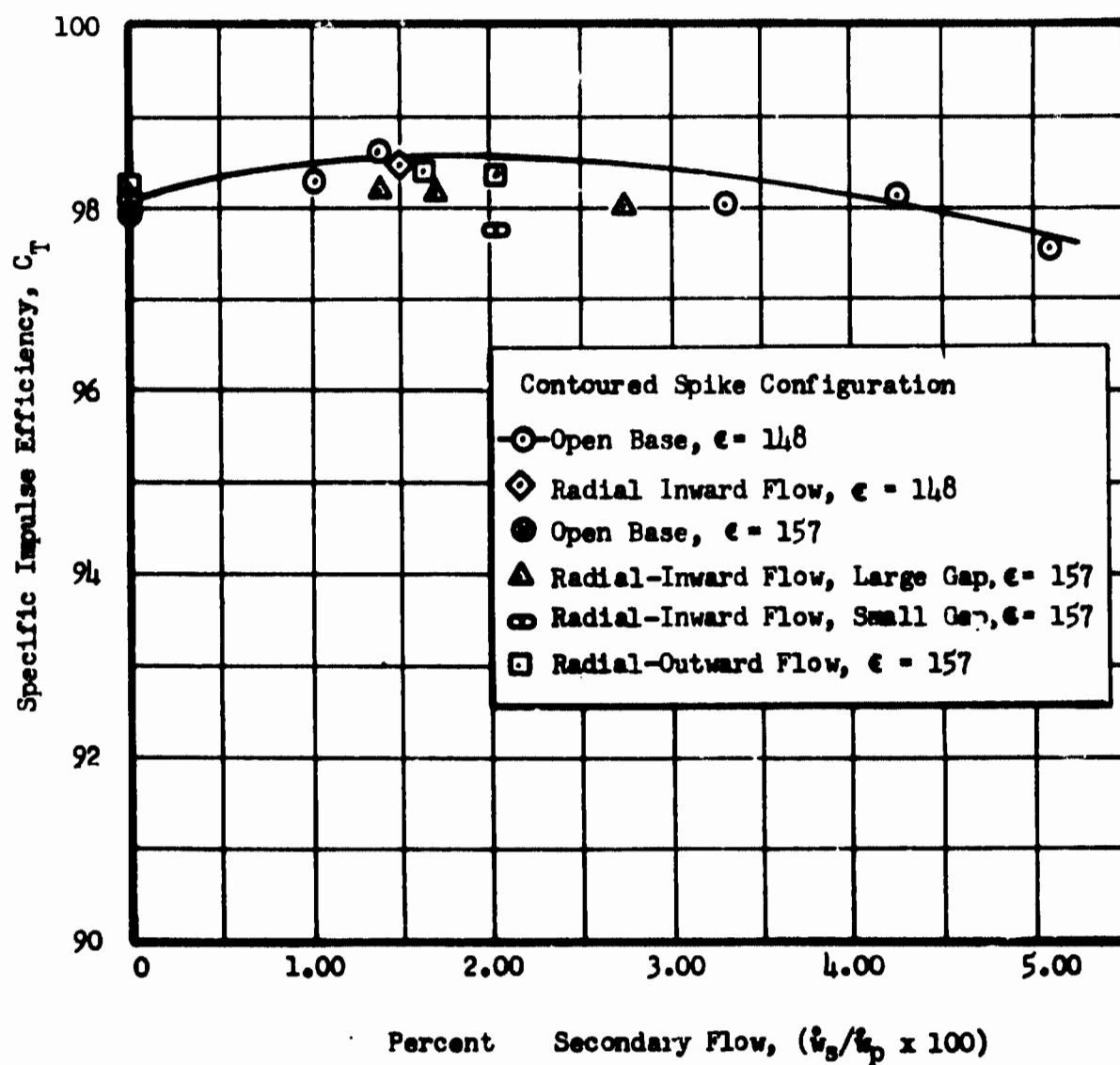


Fig. 32. Specific Impulse Efficiency vs Secondary Flow, Contoured Aerodynamic Spike Configuration, Pressure Ratio $\approx 57,000$.

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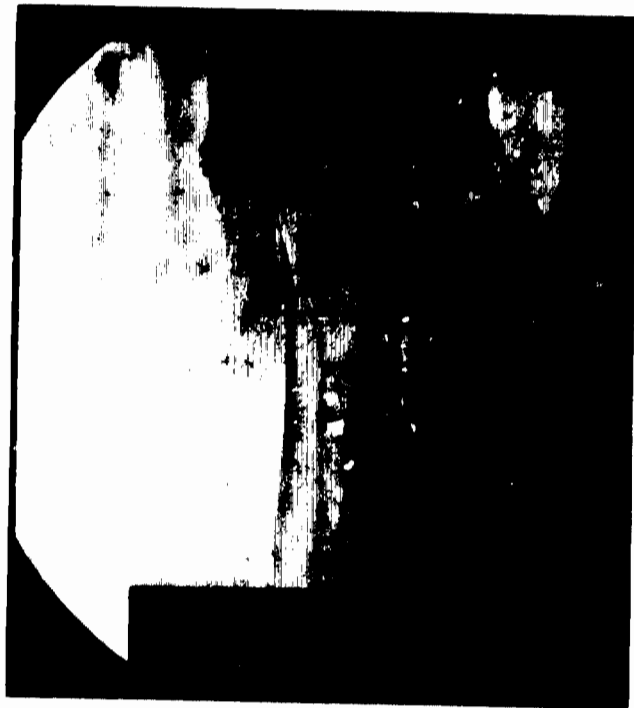
radial-inward injection method. The secondary flow was injected subsonically for the recessed orifice and the large-gap radial-inward methods; however, it was injected supersonically in the small-gap radial-inward method. This indicates that the secondary flow should be introduced into the base region at a low velocity when it is introduced radially inward. The base pressures also indicate that the radial-out injection method is slightly better than the large-gap radial-inward method. The maximum efficiency for the large-gap radial-inward injection method occurred at a secondary flowrate of 1.4 percent. A change in the slope of the base pressure versus secondary flow curve also occurs at this point.

The efficiency and base pressure of the radial-outward injection method are slightly higher than that of large-gap radial-inward method. This is contrary to what would be expected from the fact that the secondary flow of the radial-outward method is supersonic and that of the radial-inward method, subsonic. The higher base pressure appears to be the result of the different secondary flow-primary stream interaction. The Schlieren photographs of the wakes indicate that the radially-outward method affects the wake differently than the two other methods. The Schlierens for these methods of injection with approximately 1.5 percent secondary flow and at a closed-wake pressure ratio are shown in Fig. 33. In contrast to the wakes of the recessed orifice and the radial-inward methods of injection (Fig. 33a and 33b), a distinct disturbance of the primary flow field caused by secondary flow is seen near the outlet of the radial-outward configuration.

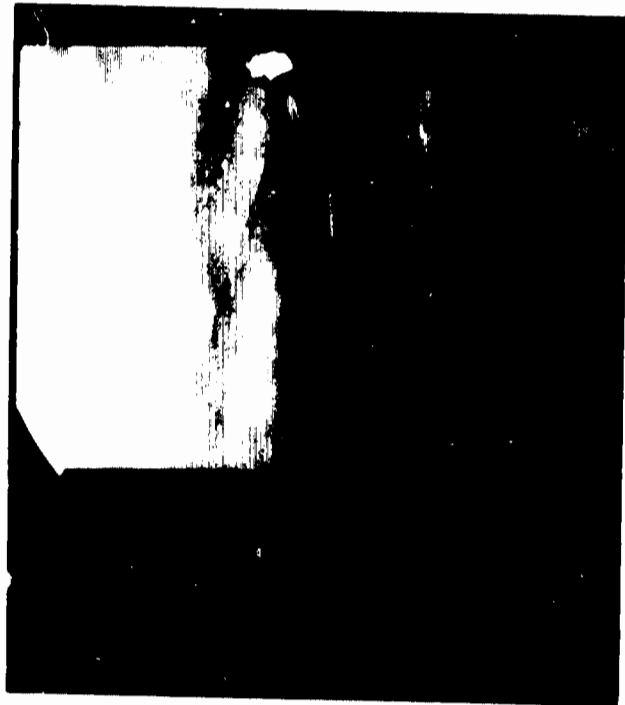
THE CONICAL AERODYNAMIC SPIKE MODEL

A 45 degree, conical aerodynamic spike with an axial length 6 percent of an equivalent 15 degree cone and an expansion area ratio of 150:1 was tested.

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a. Recessed Orifice Injection,
P.R. = 68,700 $\dot{w}_s/\dot{w}_p = 1.4 \%$



b. Radial-Inward Injection, P.R. = 58,300
 $\dot{w}_s/\dot{w}_p = 1.5 \%$



c. Radial-Outward Injection, P.R. = 44,000
 $\dot{w}_s/\dot{w}_p = 1.66 \%$

Fig. 33 , Flow Fields with Recessed Orifice Radial-Inward, and Radial-Outward Injection Configurations

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A summary of the 15 tests completed with this model is given in Table 3. The model was tested with an open base cavity and the recessed orifice method of secondary flow injection. A photograph of this model is presented in Fig. 34 .

Experimental Performance

The conical model was tested over a pressure ratio range of 48,000 to 61,000 with secondary flows from 0 to 3.1 percent of the primary flow. The difference in pressure ratios results in a maximum theoretical difference of only 0.04 percent in C_T , so it was considered reasonable to neglect this difference in comparing the efficiencies. The efficiencies of these tests are presented versus secondary flow in Fig. 35 . A maximum efficiency of 96.2 percent was realized with a secondary flowrate of 2.03 percent; an increase of 1.2 percent in efficiency over the no secondary flow case. The base pressures for these tests (Fig. 36) indicated a change in slope when $\dot{w}_s/\dot{w}_p = 1.6$ percent.

Comparison with Theoretical Predictions

The efficiency was not predicted for the conical model in Ref 1 ; however, base pressure and primary flow field analyses were subsequently completed.

The base pressure was predicted using the same recompression criteria that were applied to the contoured model. The base pressure resulting from this nozzle wake analysis was $P_b/P_c = 0.00071$ and the experimental base pressure was $P_b/P_c = 0.00066$. The difference between the predicted and the experimental base pressures is equivalent to a difference of 0.25 percent in the overall efficiency.

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TABLE 3
HIGH-AREA-RATIO TEST PROGRAM SUMMARY, CONICAL MODEL

Base Geometry	Secondary Flow, Percent w_p	P_c/P_a	Area Ratio	Percent Length	Number of Tests
Open Cavity	0-3.08	60,000	129.9	5.9	2 (dynamic tests)
	0	2600-9400			2 (dynamic tests)
	0-5	60,000			4
Instrumented Sting (1/4 inch diameter)	0	50,000	129.9		1
	3.9	47,664			1
Uninstrumented Sting (0.049 inch diameter)	0	50,000	129.9		1
					15

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Fig. 34 Recessed Orifice Injection Configuration, Critical Nozzle

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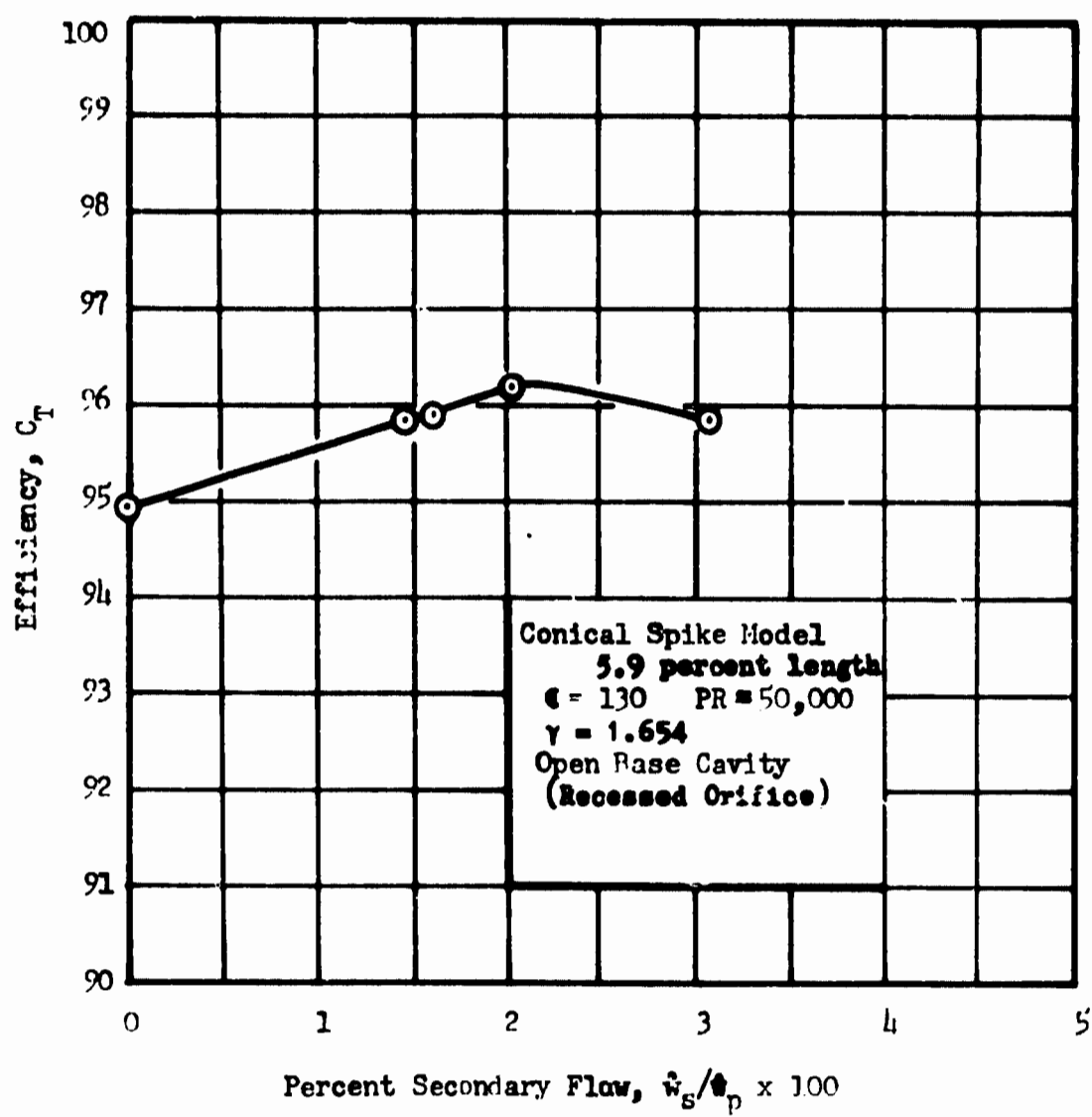


Fig. 35. Efficiency Versus Secondary Flowrate, Conical Aerodynamic Spike

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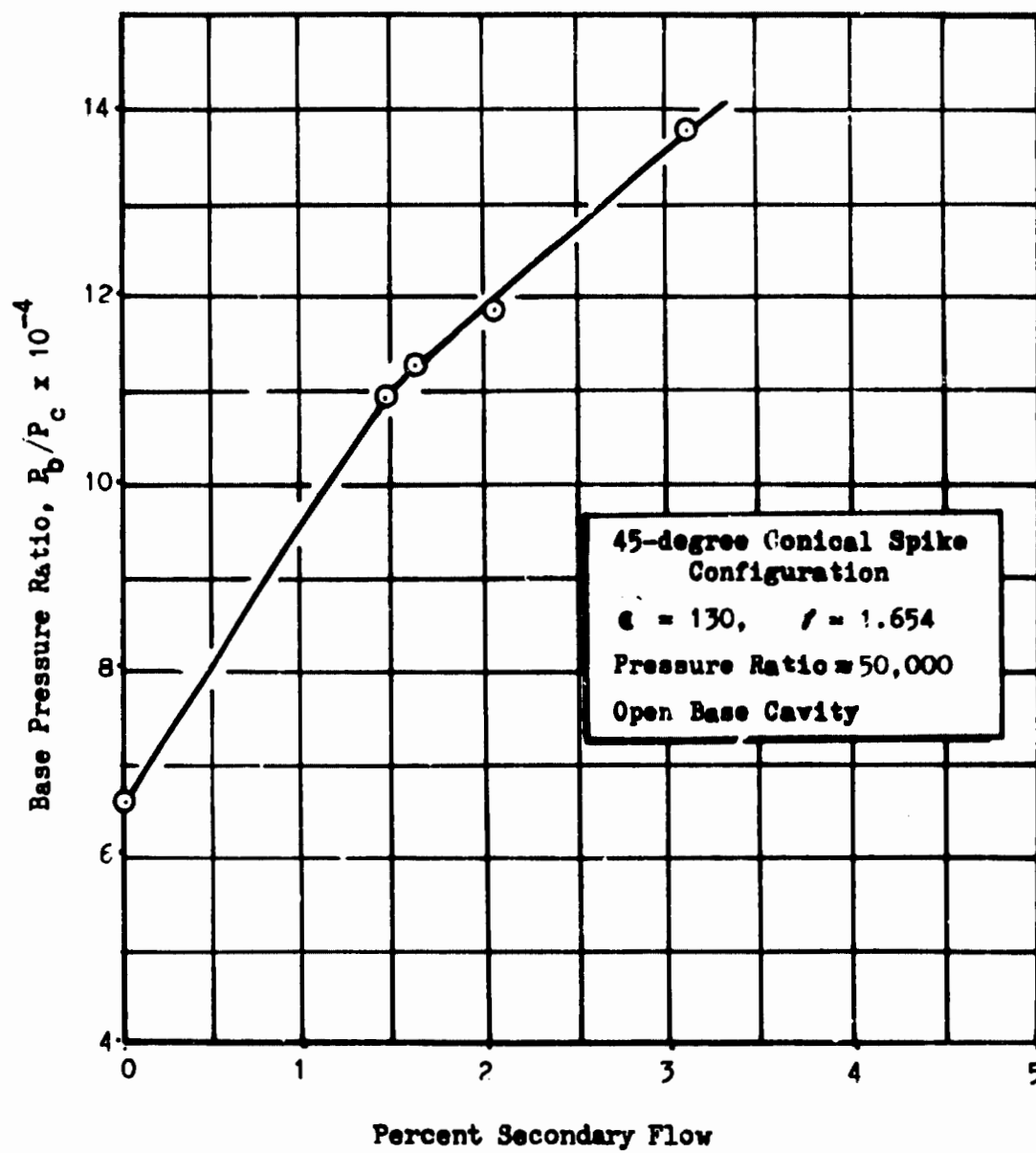


Fig. 36. Base Pressure Ratio vs Secondary Flowrate,
45-degree Aerodynamic Spike

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To satisfy the recompression criteria it was necessary for the flow to separate from the primary nozzle wall before it reached the end of the nozzle. The base pressure analysis thus led to the prediction that the primary flow should separate from the nozzle wall at a point about 0.17 inch from the throat outer expansion point. The primary nozzle experimental wall pressures plotted in Fig. 37 indicate that the primary flow did in fact separate from the nozzle wall at approximately the predicted point. The fact that the separation point was determined by the base pressure solution shows that separations are influenced by the wake recompression phenomena. This makes the base pressure theory a very powerful tool in uncovering unusual flow situations of this sort.

Further confirmation of the interrelation of base pressure and flow separation was gained by comparing the nozzle pressure profiles for various amounts of secondary flow (varying base pressure). These data are indicated in Fig. 38. The variance in the separation point and the influence of base pressure on the nozzle wall pressures in the separated region is evident.

CONCLUSIONS

1. The high performance ($C_T = 98.6$ percent) of a contoured, high area ratio aerodynamic spike model with secondary flow has been demonstrated.
2. The theoretical prediction of nozzle performance in the closed wake regime agreed within 0.1 percent of the experimental data.
3. Additional analytical and experimental effort is required to obtain a better understanding of high area ratio nozzle recompression phenomenon.

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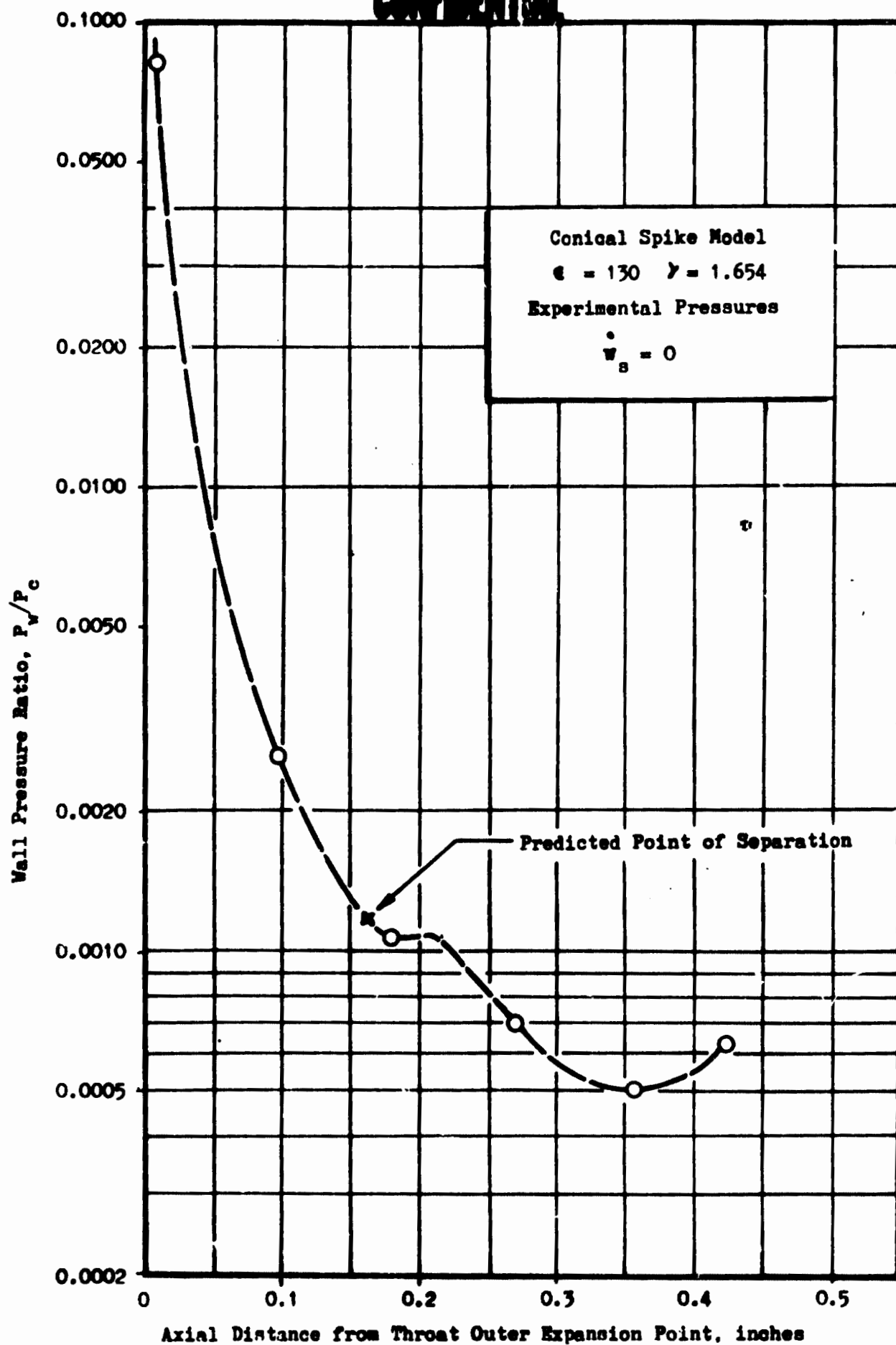


Fig. 37. Experimental Wall Pressure Profile Without Secondary Flow.
Conical Spike Model

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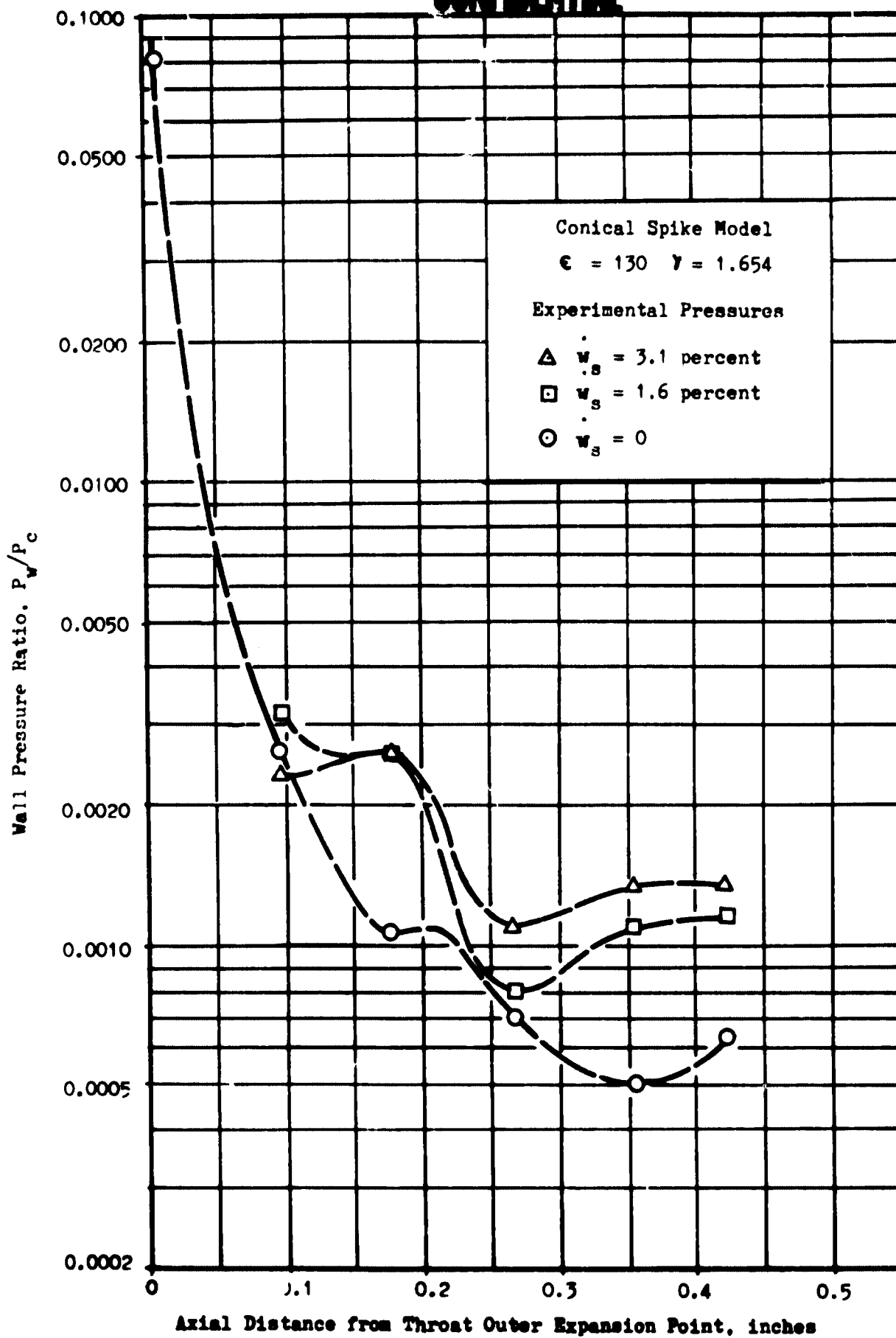


Fig. X Experimental Wall Pressure Profile with and without Secondary Flow, Conical Spike Model

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4. The most efficient method of injecting secondary flow that was tested is the recessed orifice method. However, low Mach number radial-in and radial-out injection methods, also provide effective means of injecting secondary flow.
5. Primary flow separation effects were theoretically determined for the 45 degree conical aerodynamic spike nozzle. The method used should be of value for analysis of other aerospike contours.

EXPERIMENTAL INVESTIGATION OF THE WAKE

A number of experimental tests were devoted to surveying the aerodynamic spike wake. An instrumented wake probe or "sting" was mounted in the center of the model's base along the centerline of the aerospike wake flow field. The contoured model, fitted with the wake probe, is shown in Fig. 39. The sting was equipped with six small static pressure taps along the surface of the probe. These taps enabled the reading of wake centerline pressures during any given run.

As noted in the first quarterly progress report (Ref. 1), there are three basic secondary flow regimes of interest in the closed-wake aerospike base pressure problem, (1) the no bleed regime, (2) the small bleed regime, and (3) the large bleed regime. The wakes of these three regimes were investigated for the conical and contoured spike models.

The first regime investigated was the no bleed regime at high pressure ratios. In Ref. 1, it was stated, (referring to Fig. 40) upstream of the base (Region 1) the flow is determined by the body shape and aerospike throat, and details can be obtained from a characteristic solution. In Region 2, the flow expands around the lower lip of the model and separates forming a free shear layer with constant pressure mixing (subregion b) which separates the external flow (subregion c)

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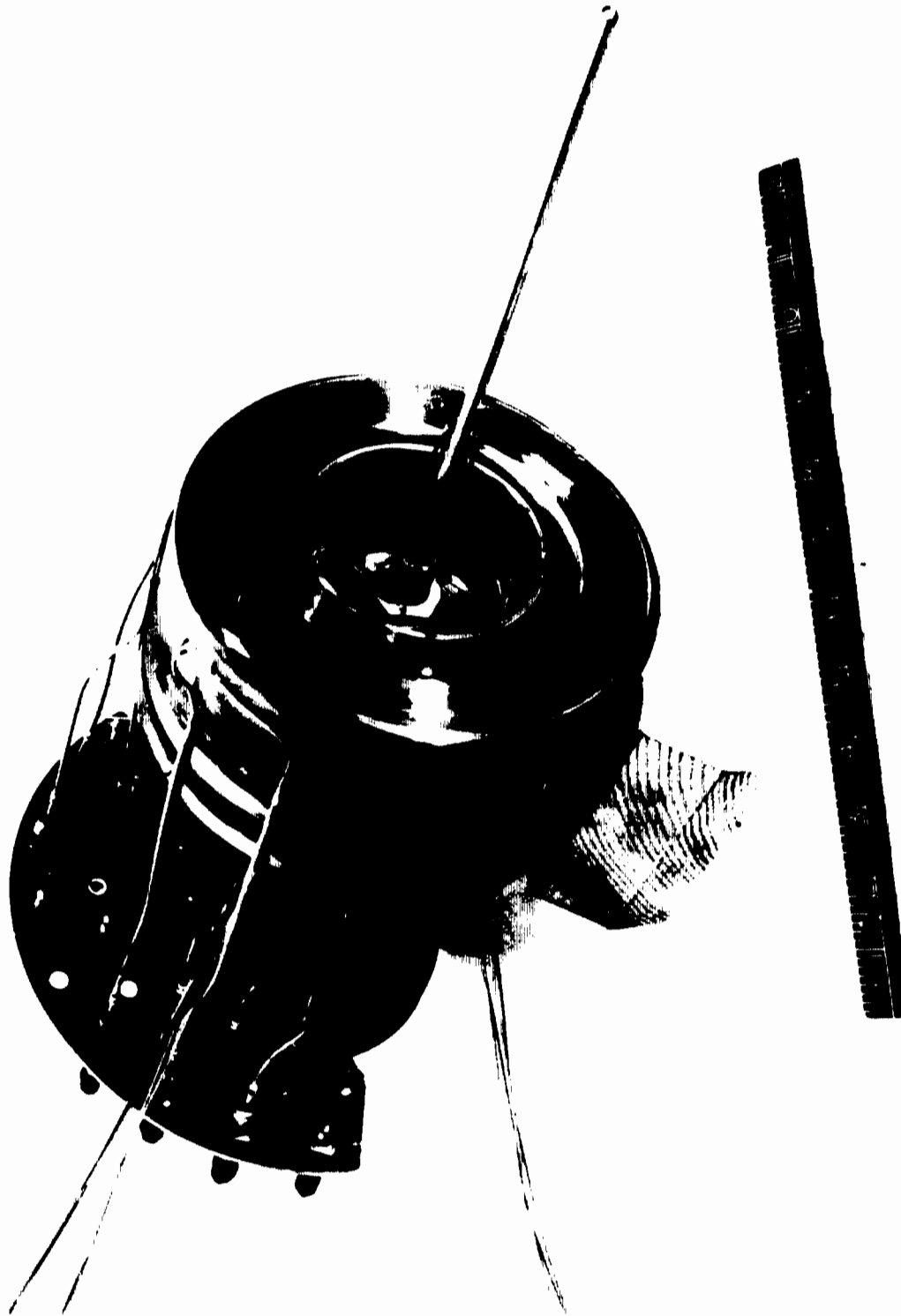


Fig. 39. Instrumented Wake Probe Mounted on the Contoured High-Area-Ratio Aerodynamic Spike Nozzle

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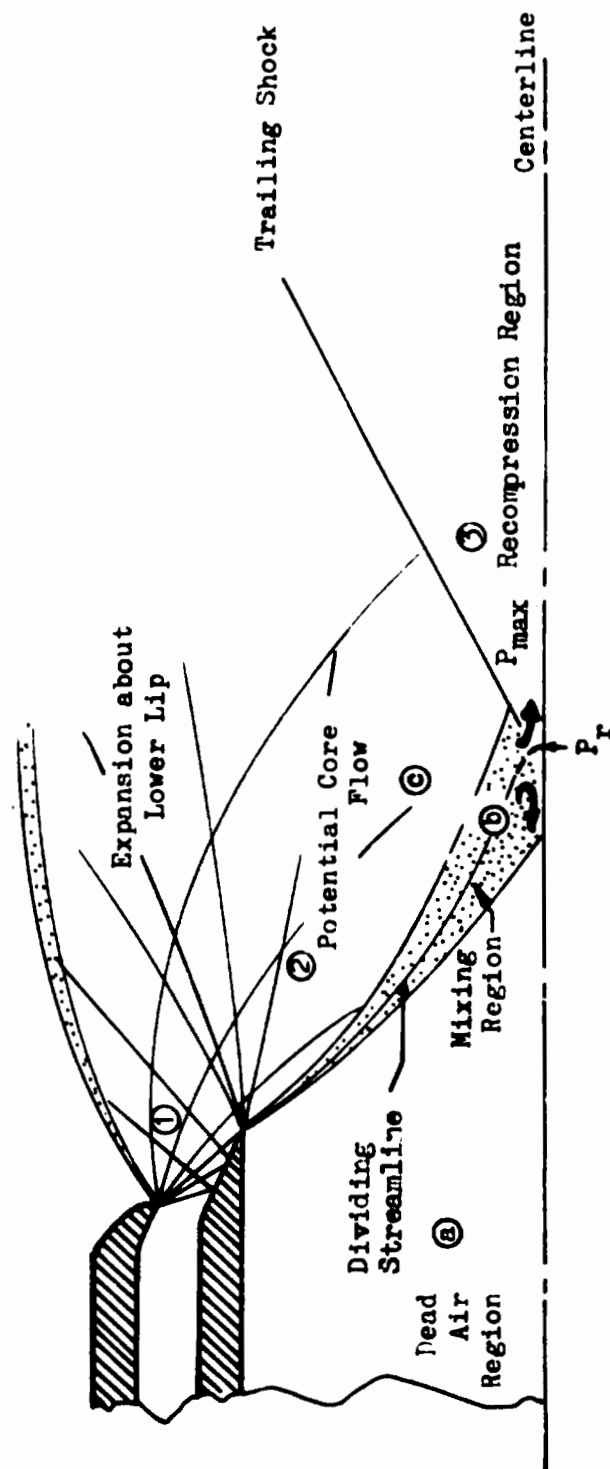


Fig. 40. Aerospike Flow Field Model, No-Bleed Regime, Closed-Wake

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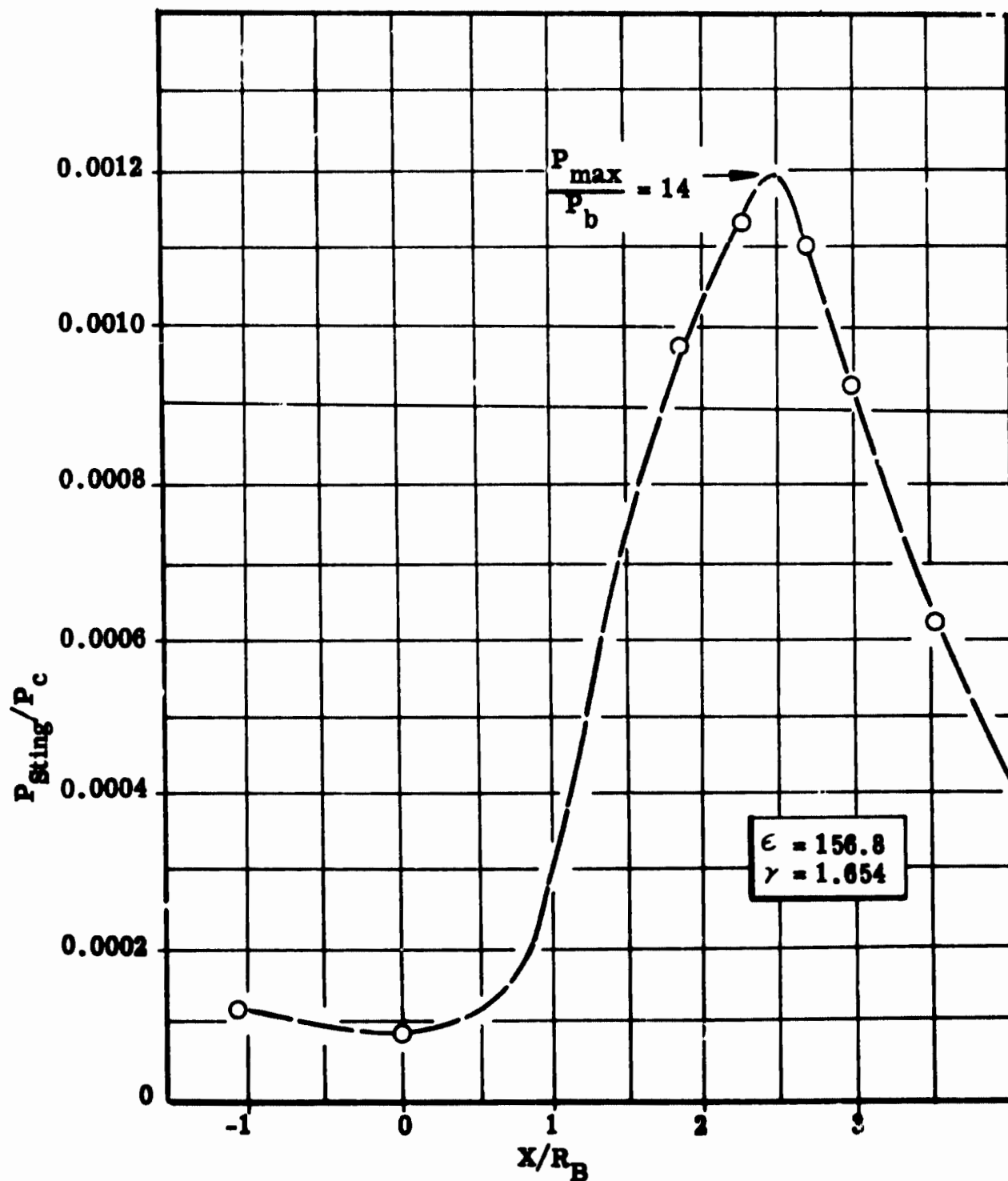
from a "dead air region" of recirculating flow (subregion a). The free jet boundary and its adjacent shear layer then impinges on the centerline core where the flow reattaches and recompresses through a trailing shock separating regions 2 and 3 .

The first objective of the wake probe experiments on the aerodynamic spike was to define the centerline wake pressure profile for the no bleed case and determine $P_{\max}/P_b$. The results of the sting pressure measurements for the contoured and conical models is shown in Fig. 41 and 42 . Within the base cavity the centerline pressure is equal to the base pressure. Near the point on the axis where the shear layer of the free jet begins to impinge (see Fig. 40), the pressure rises rapidly to a maximum. This occurs at the point where the inviscid jet boundary as calculated from the characteristics program, impinges on the axis. The maximum pressure corresponds to the pressure immediately following the trailing shock. This shock is produced by the turning of the incident flow field back to a direction parallel to the centerline of the model. The pressure drops rapidly after $P_{\max}$ due to the diminishing strength of the trailing shock caused by the primary expansion waves.

When a small amount of bleed (4.5 percent) was added to the base of the conical spike, the base pressure increased and the centerline maximum pressure, as seen in Fig. 42, decreased from a value of $P_{\max}/P_c = 0.012$ to a value of $P_{\max}/P_c = 0.0020$.

This decrease in $P_{\max}$ is due to the fact that the angle of impingement of the free jet boundary has decreased because of the higher base pressure. A lower turning angle for the primary stream means a smaller pressure rise through the trailing shock. Since $P_{\max}$, in this

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Distance Along Sting/Base Radius (From Nozzle Exit Plane)

Figure 41. Centerline Wake Pressure Profile Contoured Spike Configuration, No Bleed

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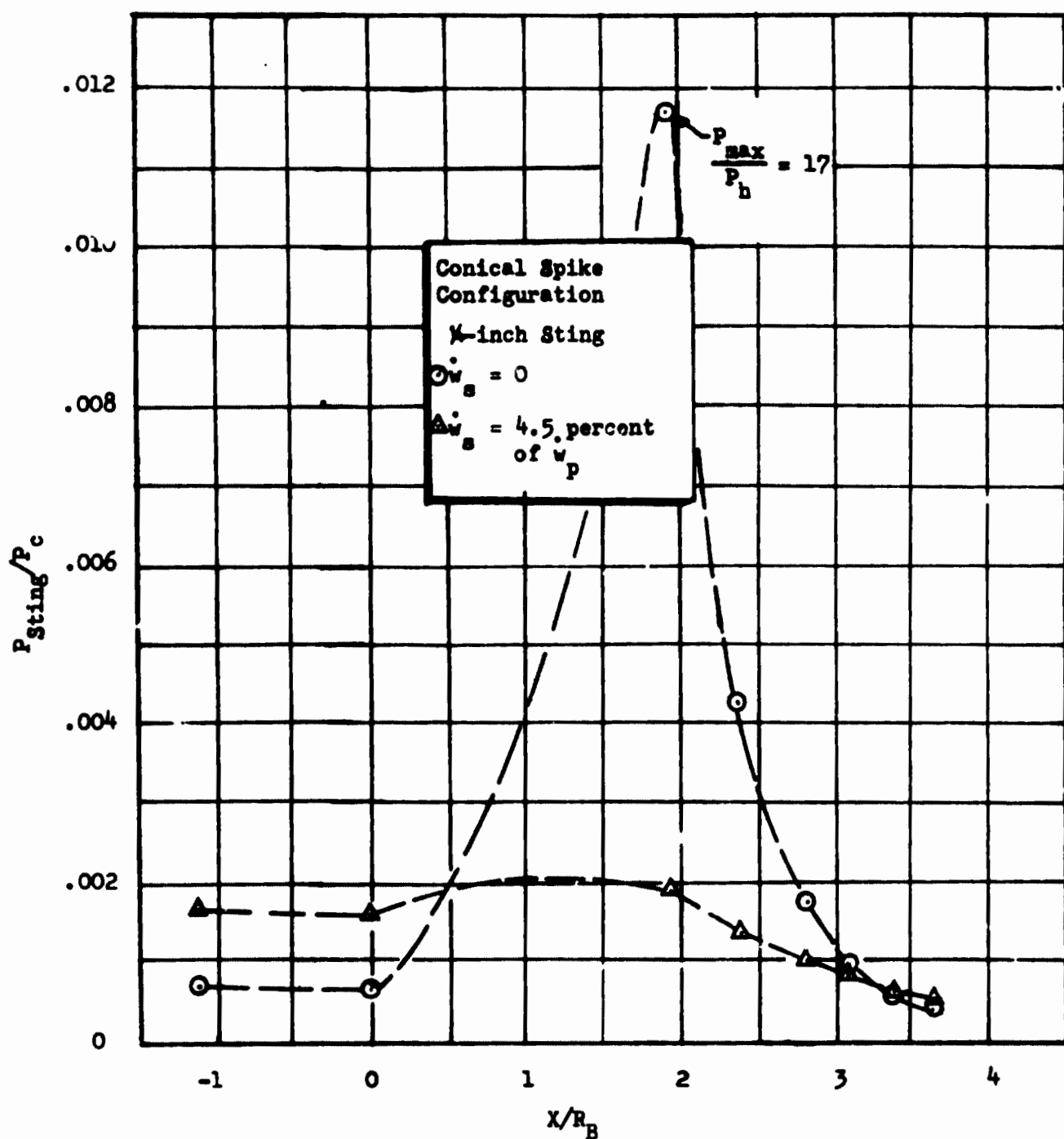


Fig. 42 Centerline Wake Pressure Profile, Conical Spike

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case, is still higher than P_b , this indicates that the wake is still in the small bleed regime, where some recompression still occurs. It should be noted that while 4.5 percent can be considered a "small bleed" rate for the conical model, it definitely is not "small" for the contoured model. This flowrate pushes the contoured model base pressure into the high bleed regime, i.e., where no recompression pressure rise above P_b is noted.

A picture of the contoured model with sting, operating in the high bleed regime is shown in the Schlieren photograph of the model operating at a pressure ratio of 58,000, (see Fig. 43). The inner primary jet boundary first dips down, then up, forming a continuous boundary between primary and secondary. In Addy's thesis on ejectors (Ref 2), he hypothesizes that a stable solution for the base pressure in this regime is guaranteed by the criteria of choking of the secondary stream at its minimum area. Thus, the object of testing the aerospike with large bleed was to determine if Addy's criteria is valid. If so, it then would be useful in obtaining a large bleed base pressure theory.

The wake survey of the large bleed flow field for the contoured model is shown in Fig. 44 . A monotonically decreasing centerline pressure is noted outward along the sting axis. This profile is indicative of flow in a choked nozzle. The choked pressure ratio corresponding to a secondary throat is found for helium to have a value $P/P_b = 0.49$. From the sting pressure measurements, the choked pressure ratio occurs at a distance, measured from the end of the model, of $X/R_b = 1.6$. From the Schlieren of Fig. 43 , the minimum area occurs approximately at the same distance. Thus, it may be concluded that Addy's hypothesis is valid in the large bleed regime, i.e., choking of the secondary does occur at the minimum wake area and may be used as a necessary condition for a stable base pressure solution.

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Fig. 43. Wake-Flow Study for Contoured
Nozzle, High Bleed Rate
P. R. = 58,000

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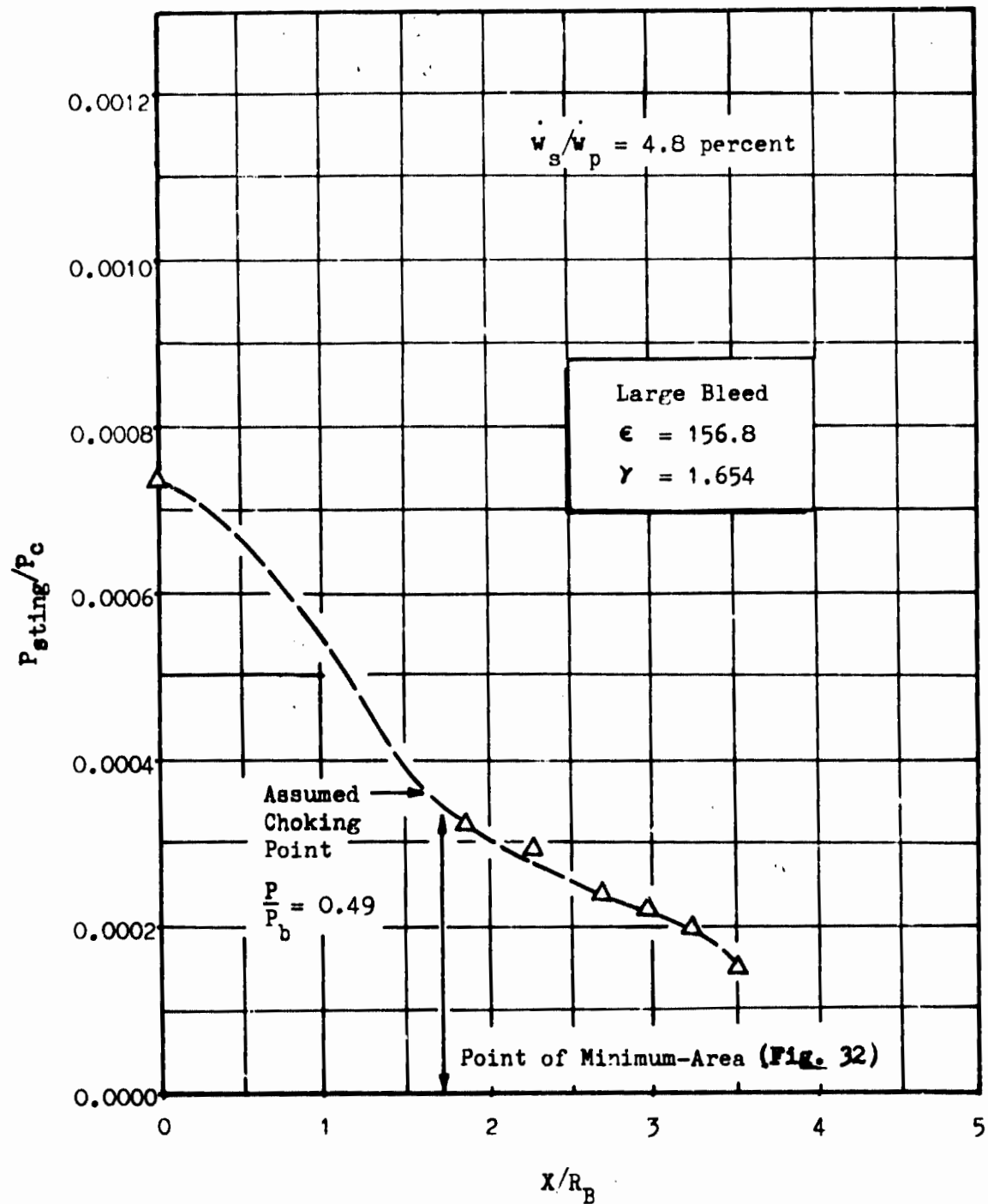


Fig.44. Centerline Wake Pressure Profile Contoured Spike Configuration . Large Bleed

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In summary, several significant conclusions can be drawn from this wake study.

1. The wake survey with the 1/4" sting in the no bleed regime demonstrated the sharp pressure rise at reattachment which wake theoretical models qualitatively predict.
2. The centerline pressure profile in the small bleed regime for the conical nozzle was found to diminish considerably in magnitude from the no bleed case but a small pressure rise was still noticeable, justifying the present analytical methods and flow model for this distinct regime.
3. Choking of the secondary flow was shown to occur in the large bleed regime. Use of this evidence has been made in constructing a base pressure solution for the large bleed regime.

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COLD-FLOW TESTING OF COMBUSTOR CONFIGURATIONS

The main purpose of this cold-flow test program is to obtain experimental data for aerodynamic spike nozzles having various combustor configurations. The specific goal is to couple closely the effects of nozzle contour, combustor shape, and the use of secondary gas. To accomplish this, a group of multichamber and annular aerodynamic spike nozzles was tested. The models were designed to achieve maximum performance representative of the combustor configuration so that a comparison of relative performance could be made. In addition, a cold-flow model scaled from the hot-firing model was tested to obtain a direct comparison between hot-flow and cold-flow data for geometrically similar models. A total of 256 tests were achieved. A description of the models tested and of the test results is presented herein.

MODEL SELECTION

The models tested in this program are listed in Table 4. A cold-flow nozzle geometrically scaled from 10,000 pound thrust hot-firing aerospike nozzle was evaluated using various methods of introducing secondary flow into the nozzle base region. These models are designated as Group I, Nos. 1 through 5.

The models in Groups II and III were all of the same area ratio (50) and, except for model 9, of the same total length. These models were used to investigate the effect of combustor configuration on aerospike nozzle performance. The Group II models have continuous annular throats whereas the Group III models are aerospike nozzles with clustered conventional bell chambers forming the combustion chamber and initial expansion surface.

Table 5 gives a length comparison for all of the models referenced to both percent length of a 15 degree half angle conical nozzle and an ideal spike nozzle. Module area ratios are given for comparison to overall cluster area ratio of the multichambers. The models are discussed in the following pages.

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TABLE 4
COLD-FLOW MODEL DESCRIPTION

Group	Number	Description
I	-	Scaled duplicate of the hot-firing model, $\epsilon_o = 25$
	1	Radial-inward secondary flow
	2	Recessed radial-outward secondary flow
	3	Open base
	4	Supersonic axial secondary flow
	5	Porous plate
II	-	Annular reference models (continuous throats, $\epsilon_o = 50$)
	6	Point expansion nozzle
	7	Shrouded nozzle
III	-	Multichamber models, $\epsilon_{CL} = 50$, circular exit chambers
	8	Eight touching chambers, $\epsilon_M = 30.2$, no shroud, no centerbody
	9	Eight touching chambers, $\epsilon_M = 30.2$, no nozzle extension
	10	Eight touching chambers, $\epsilon_M = 30.2$
	11	Eight chambers with spacing between chambers of $1/3$ the exit diameter, $\epsilon_M = 20.7$
	12	Sixteen touching chambers, $\epsilon_M = 20.7$

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TABLE 5
AEROSPIKE NOZZLE LENGTH COMPARISON

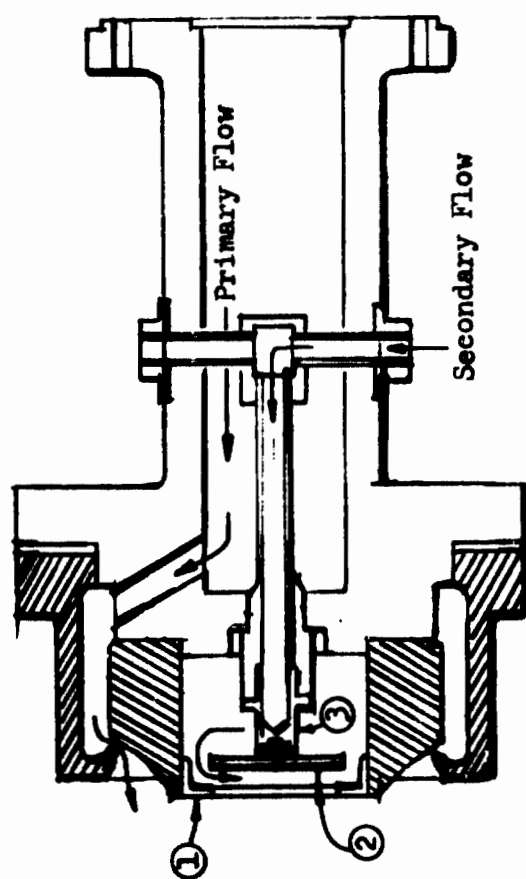
Model Number	N	ϵ_N	δ/D_0	θ_T	Relative Nozzle Lengths		
					Measured From Throat, L_N		Measured From Module Exit, L_p
					Percent of 15 deg. cone	Percent of Ideal Nozzle	
1-5	-	-	-	-	12	9	-
6	-	-	-	-	30	16	-
7	-	-	-	-	30	16	-
8, 9	3	30.2	0.01	5.4	22	12	0.0
10	8	30.2	0.01	5.4	30	16	4.0
11	8	20.7	0.31	9.5	30	16	6.5
12	16	20.7	0.02	9.5	30	16	10

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Scaled Hot-Firing Model

A geometrically scaled version of the 10,000-pound thrust hot-firing model evaluated in this program was designed and tested. This model was selected to provide a direct comparison of data between geometrically similar hot-firing and cold-flow models and to provide additional design information with regard to efficient methods of introducing secondary flow into the base region. The nozzle is an ideal (isentropic) contour ($\gamma = 1.25$) truncated to a length which is 12 percent of a 15-degree conical nozzle with an ϵ_0 of 25. The model is shown schematically in Fig. 45 with the radial-inward base configuration mounted. Other base injection methods tested include: a recessed radial-outward injection configuration which is obtained by placing the circular plate (2) flush with the nozzle exit and recessing plate (1) within the cavity; open base injection with the base plates removed; and two conical nozzles replacing the injection orifice (3) which inject secondary flow supersonically into the base region. The assembled model is shown in Fig. 46 with the various secondary gas injection devices displayed to the right of the model. The two components at the top are the supersonic nozzles. Below these nozzles are two 8-hole orifices for controlling the secondary flow for all configurations other than the supersonic nozzles. The second row from the bottom contains the two components required for either the radial-inward or radial-outward configuration. The spacer required for the radial outward configuration is at the bottom right of the photo. A flat porous plate (rigimesh) mounted flush with the nozzle exit was also used. This plate is at the bottom left of the group.



Conical Nozzle $\epsilon = 15$



Conical Nozzle $\epsilon = 3.5$

Fig. 45 Cold-Flow Model. Scaled Version of 10,000 Pound Thrust Hot-Firing Chamber

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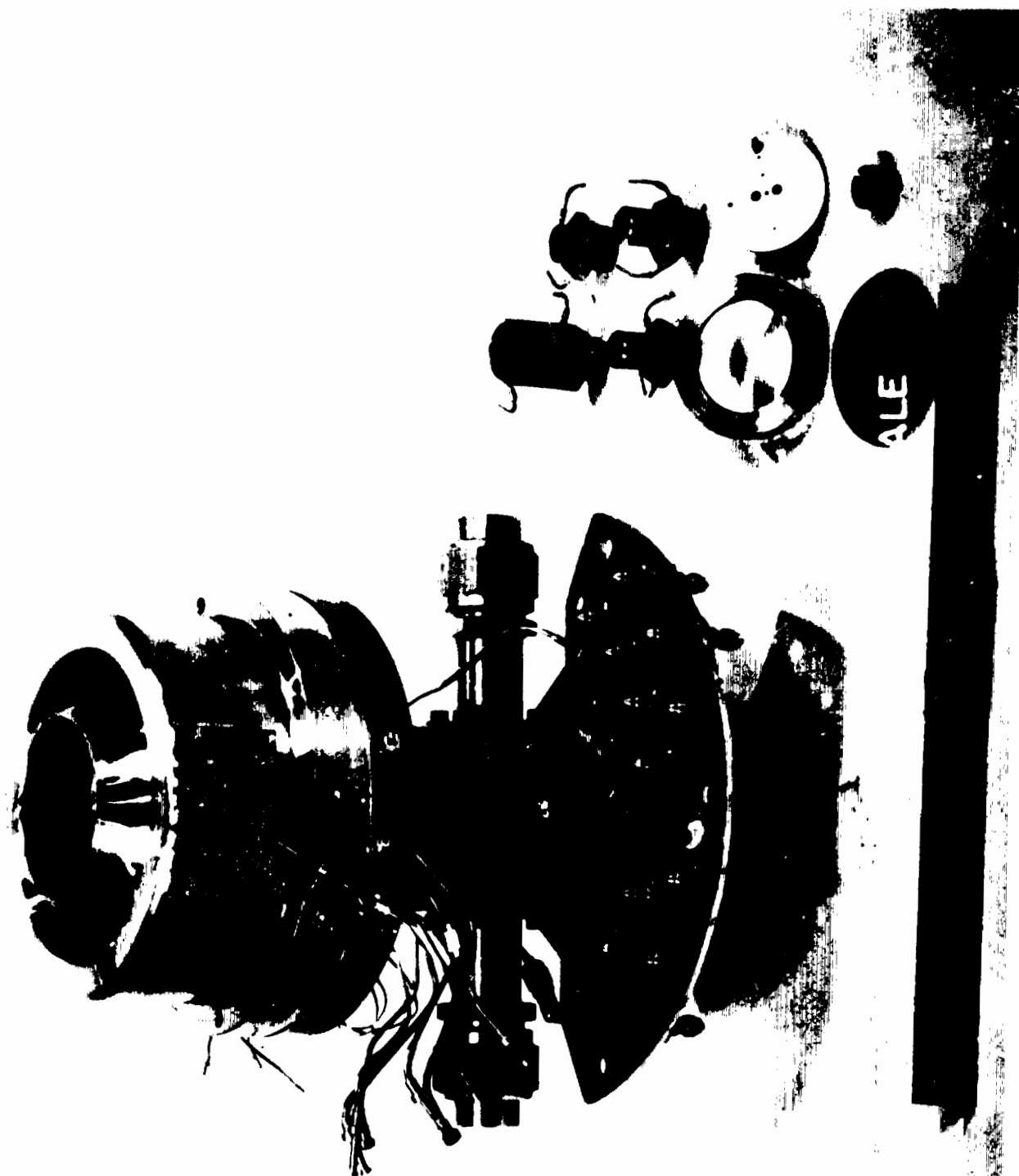


Fig. 46 Scaled Hot-Firing Model

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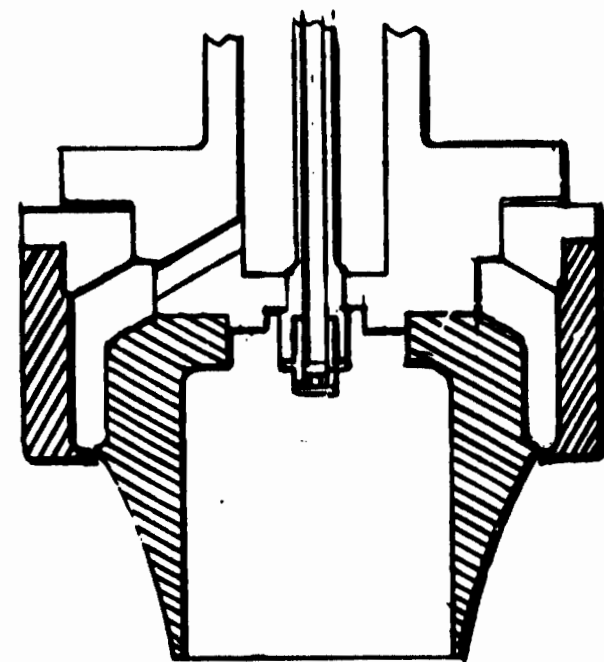
Annular Reference Models

Two continuous-throat annular reference models were tested; one is a "point expansion" design and the other is "shrouded". They are illustrated in Fig. 47. The assembled point expansion nozzle is shown in Fig. 48 and the shrouded nozzle assembly is shown in Fig. 49. Each of these models was designed for an area ratio of 50 and an axial length from the outer-throat expansion point equal to 30 percent of a 15-degree conical nozzle of the same area ratio. The contour for the point-expansion nozzle was developed by generating an ideal spike contour with an area ratio of 50 and a γ of 1.4 and subsequently truncating it to 30 percent length.

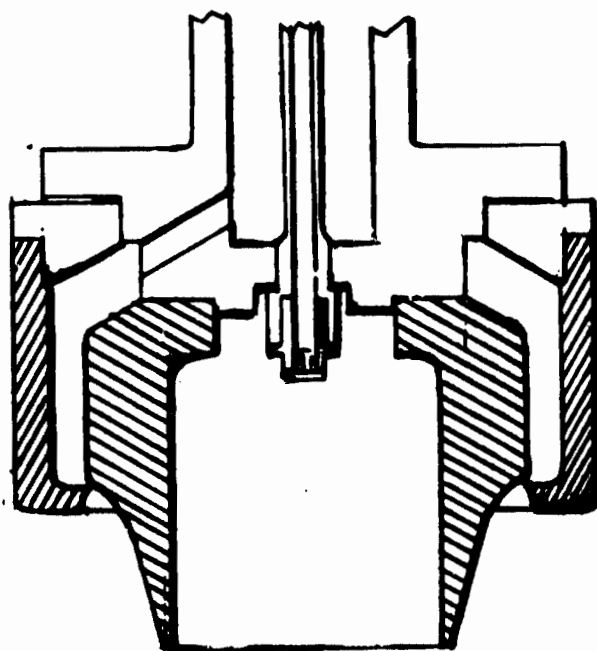
The shrouded annular nozzle was designed to approximate the type of shroud for a typical hot-firing nozzle using storable propellants. Proper shrouding of annular nozzles will provide expansion conditions which are favorable for maintaining chemical equilibrium (shifting equilibrium). The selected shroud was an annular cone shape with a 10 degree divergence half angle. The nozzle was shrouded to an area ratio of 3 and the centerbody was designed to give good primary flow field and base pressure characteristics.

The design of shrouded spike contours is different from the point expansion spike nozzle. For the point expansion nozzle the outer flow perimeter freely expands at the throat to ambient conditions. For the shrouded nozzle the expansion of the outer flow perimeter is contained from the throat by a physical surface of short axial length. The shrouded spike design procedure generates spike contours based on a selected shroud inclination angle and shroud configuration. The steps followed to design the shrouded nozzle were (refer to Fig. 50):

- a) A shroud inclination angle β for the 10 degree half angle cone shroud was selected based on previous work (Fig. 50a).



a. Shrouded Nozzle



b. Point Expansion Nozzle

Fig.47. Annular Reference Models

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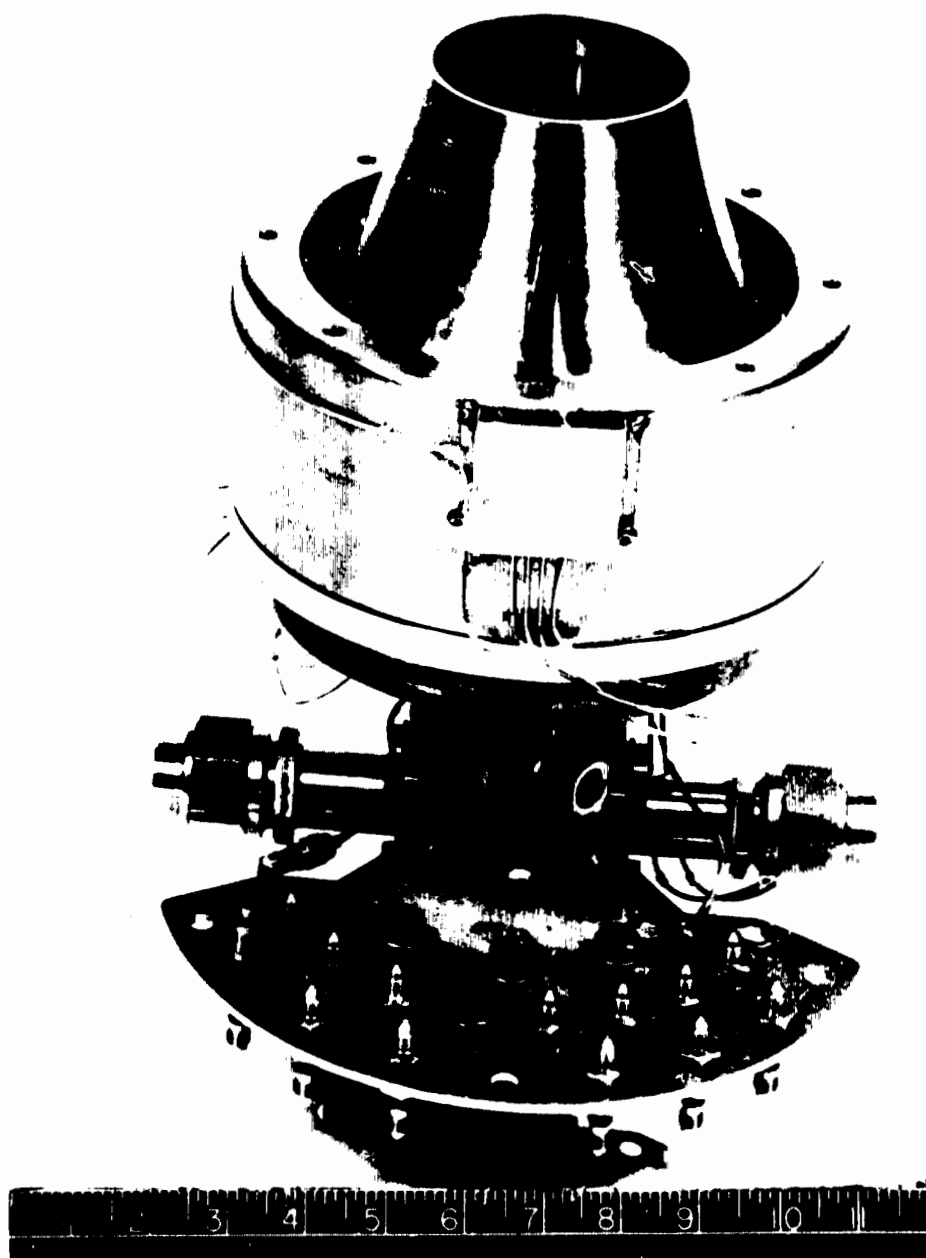


Fig. 48. Point Expansion Annular Reference Model, $\epsilon_0 = 50$

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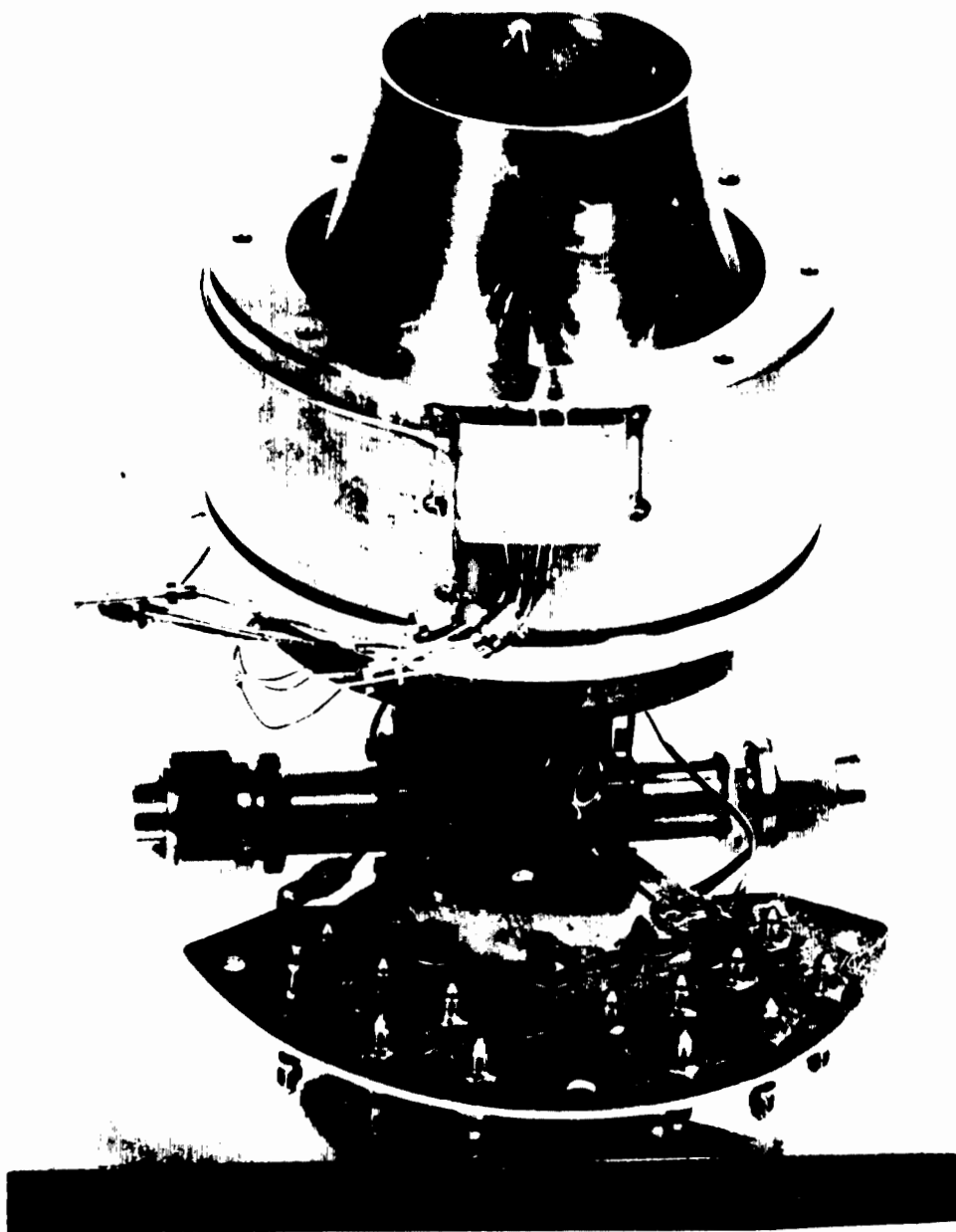
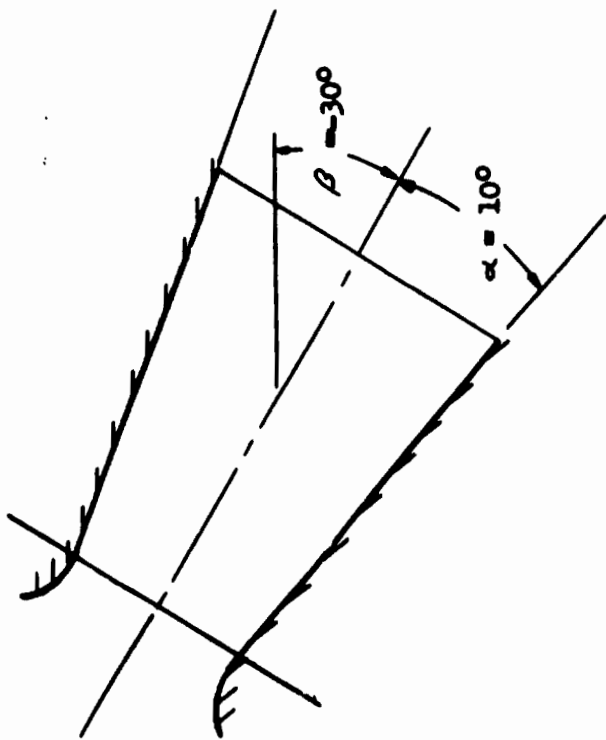
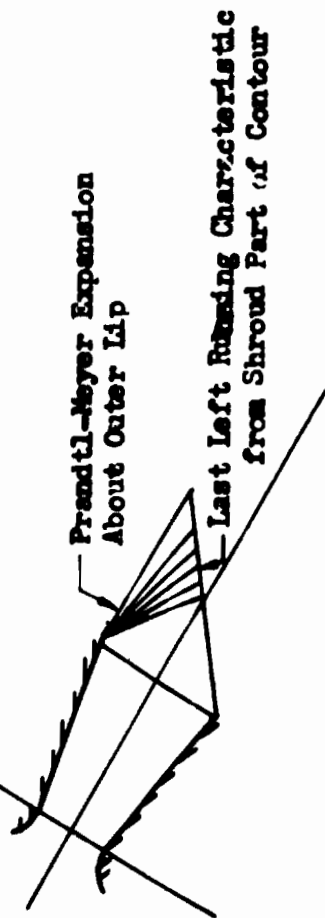


Fig. 49 Shrouded Annular Nozzle, $\epsilon = 50$

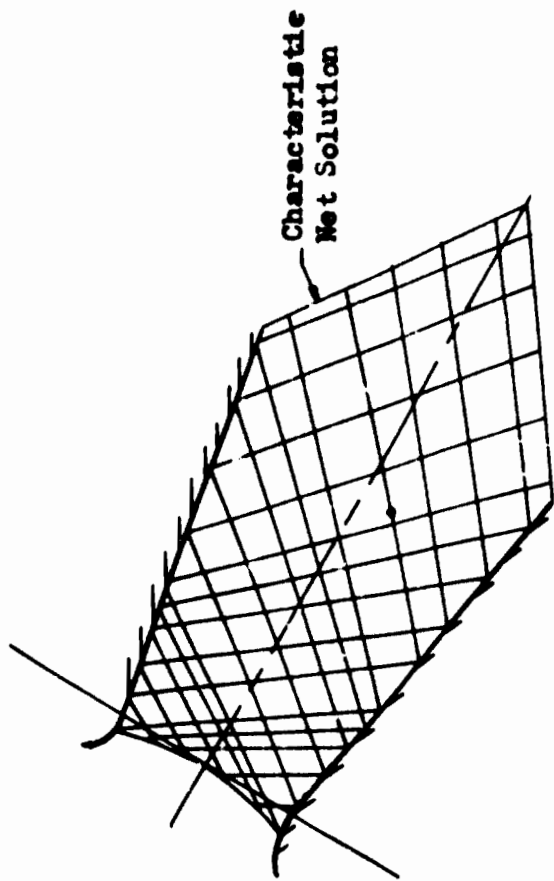
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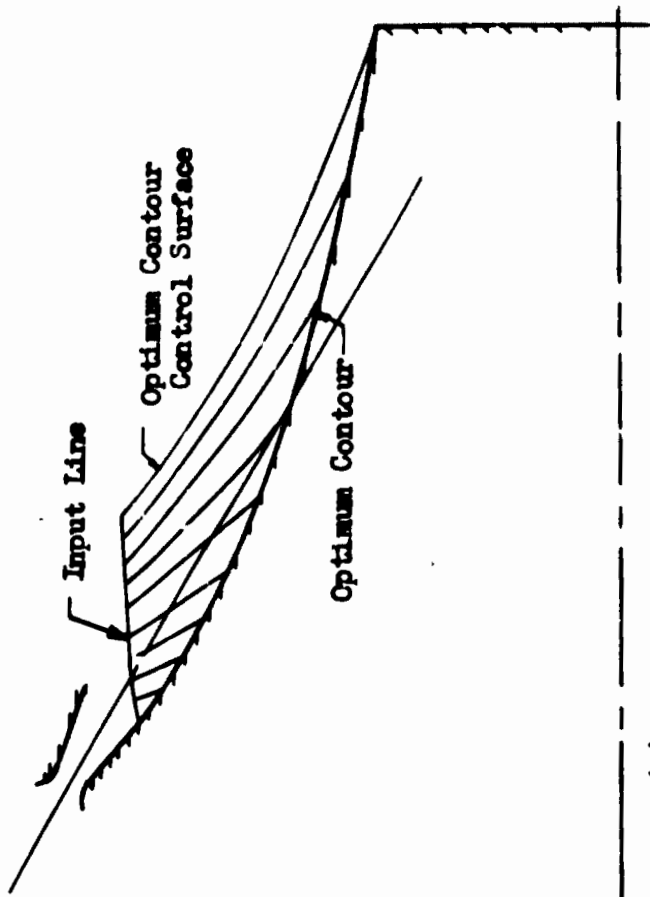
(a) Shroud Parameters



(c) Point Expansion at Outer Lip



(b) Shroud Flow Field



(d) Contour Design

Fig. 50 Design of Shrouded Annular Nose

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- b) The flow net (Fig. 50b) was computed to the end of the shroud using the method of characteristics for axisymmetric flow.
- c) The left characteristic line (input line) from the point on the contour corresponding to the end of the shrouded portion of the contour was extended by turning the flow about the end of the shroud in an expansion fan (Fig. 50c).
- d) The extended left characteristic line was used to generate a series of optimum (maximum thrust) control surfaces, each surface defining a nozzle of different length. By computing the characteristic net between the control surface and the input line, the nozzle contour was developed.

The above design procedure can produce a set of contours (various lengths) for a selected shroud inclination angle. The inclination angle may be varied arbitrarily within certain limits, with a different set of contours resulting for each β angle selected. The best inclination angle is determined by designing contours for several inclination angles and selecting the angle that gives highest performance. In this case the results of a previous study indicated that a good β angle for these conditions was -30 degrees.

A different nozzle length results for each different point on the input line selected to generate a design. The shrouded annular nozzle contour selected consisted of an 80 percent length optimum nozzle truncated to 30 percent length. This nozzle was selected from a series of contours of various lengths as the contour yielding the best combination of primary performance and base pressure.

Multichamber Models

Three basic multichamber models were tested, the 8 touching, 8 spaced and 16 touching models (listed in Table 4). The 8 touching models had two basic configurations, i.e., zero centerbody length and a spike centerbody extended to 30 percent length. Two configurations were tested for the 16 touching model; one with open spaces between the modules and one with a filler plate between modules.

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The typical model assembly is illustrated in Fig. 51. Each model has an overall cluster area ratio of 50 (determined by D_{CL} in Fig. 52), and utilizes 80 percent length individual bell chambers in its respective cluster. A cylindrical shroud tangent to the individual chamber exits encloses to multichambers. Each bell was designed for maximum thrust with air. Assemblies of the 8 chambers touching, 8 chambers spaced and 16 chambers touching multichamber models are shown in Figs. 53, 54, and 55.

All of the configurations except models Number III-8 and III-9 have spike centerbodies of sufficient length to provide an overall length, L_M , equal to 30 percent of a 15-degree conical nozzle. Figure 53 shows model III-10 with the 30 percent spike installed and the model III-9 centerbody (no spike extension) in the lower right hand corner of the photo. Model III-8 is a stripped down version of model III-9 and is shown installed in the RNTF in Fig. 56. The procedure used to design the multichamber models will be discussed below.

The following equation (derived in Ref. 3) which describes the inter-relationship of the clustering geometric variables was used to design the multichamber models.

$$\frac{C_{CL}}{C_M} = \frac{1}{N} \left[\frac{(1 + \delta/D_s) \cos \theta_T}{\sin (\arctan \cos \theta_T \tan \frac{180}{N})} + \cos \theta_T \right]^2$$

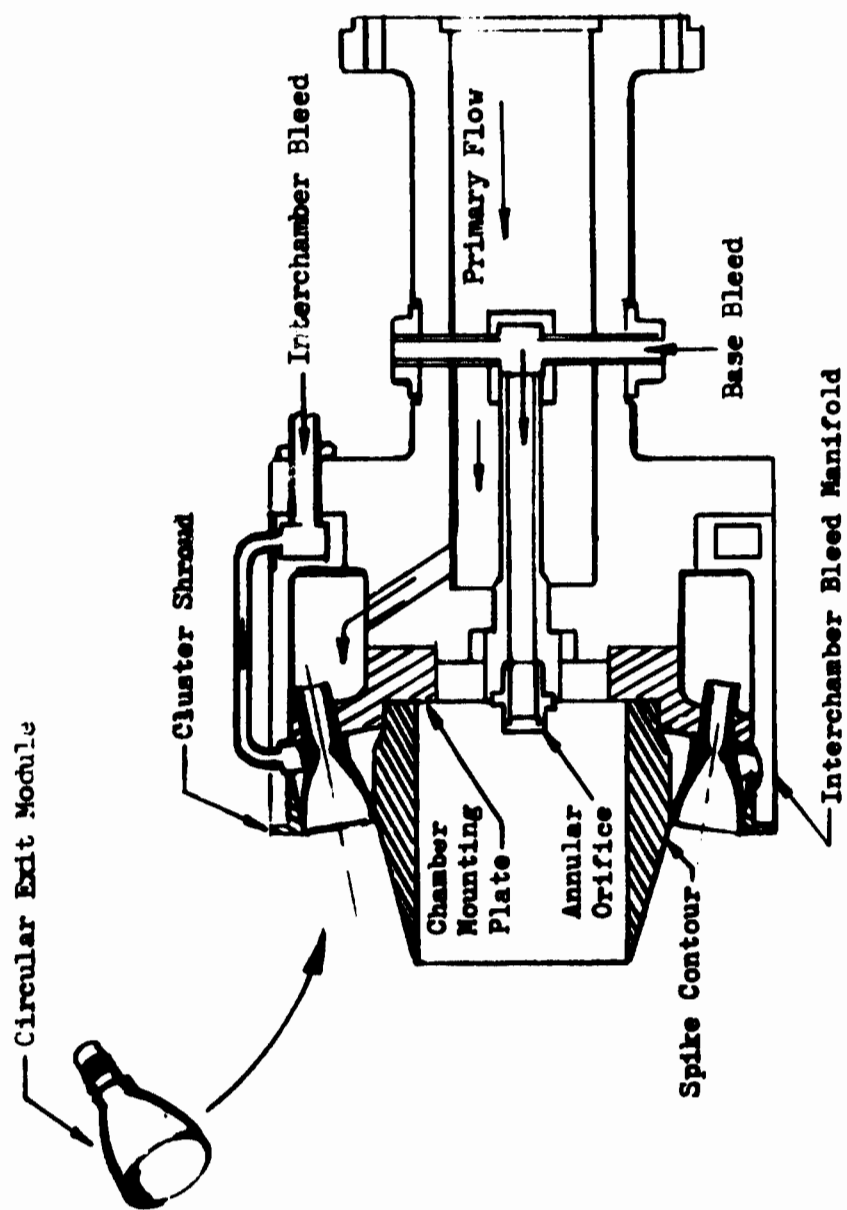


Fig 51 Multichamber Model Configuration

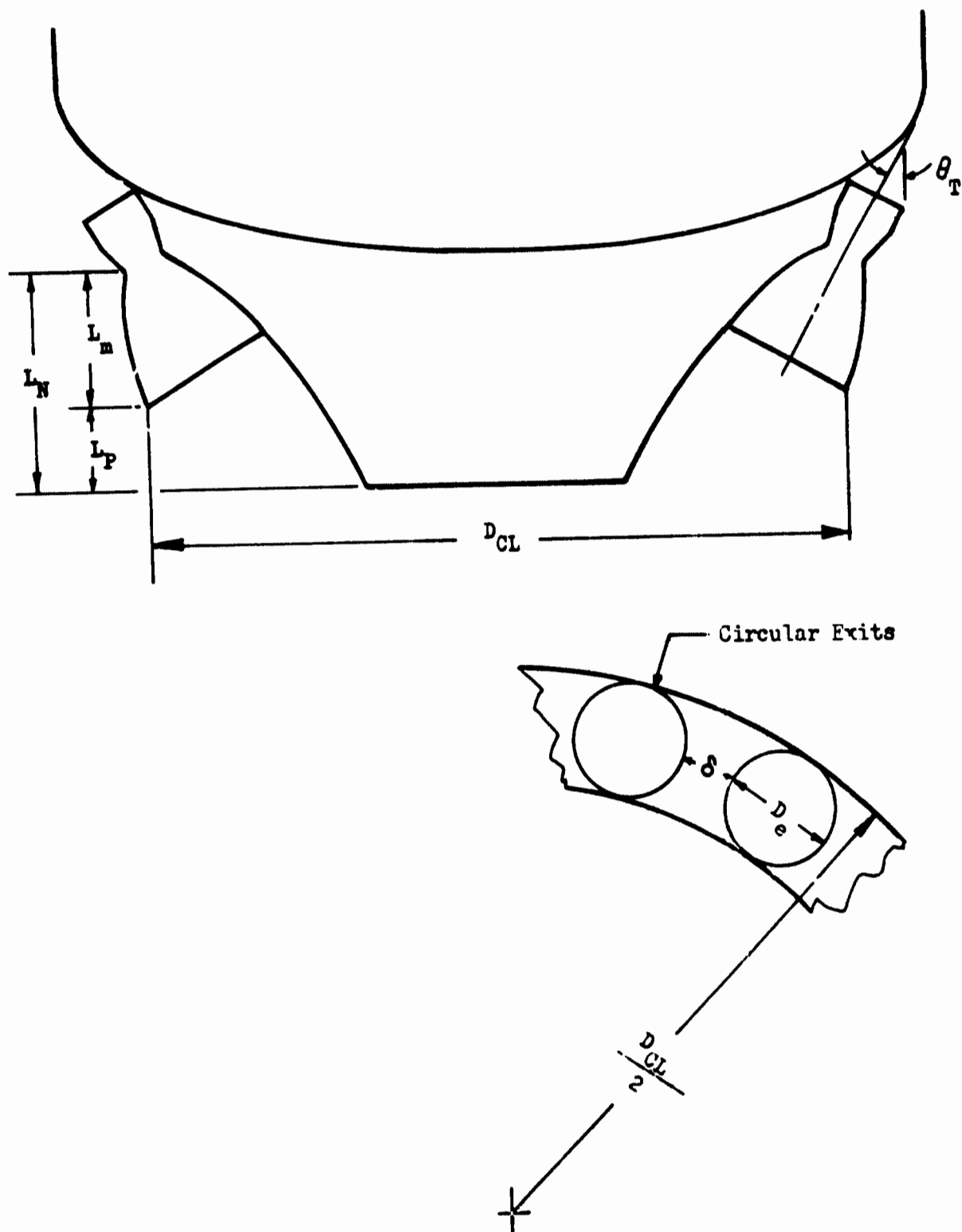


Fig. 52 Multichamber Nomenclature

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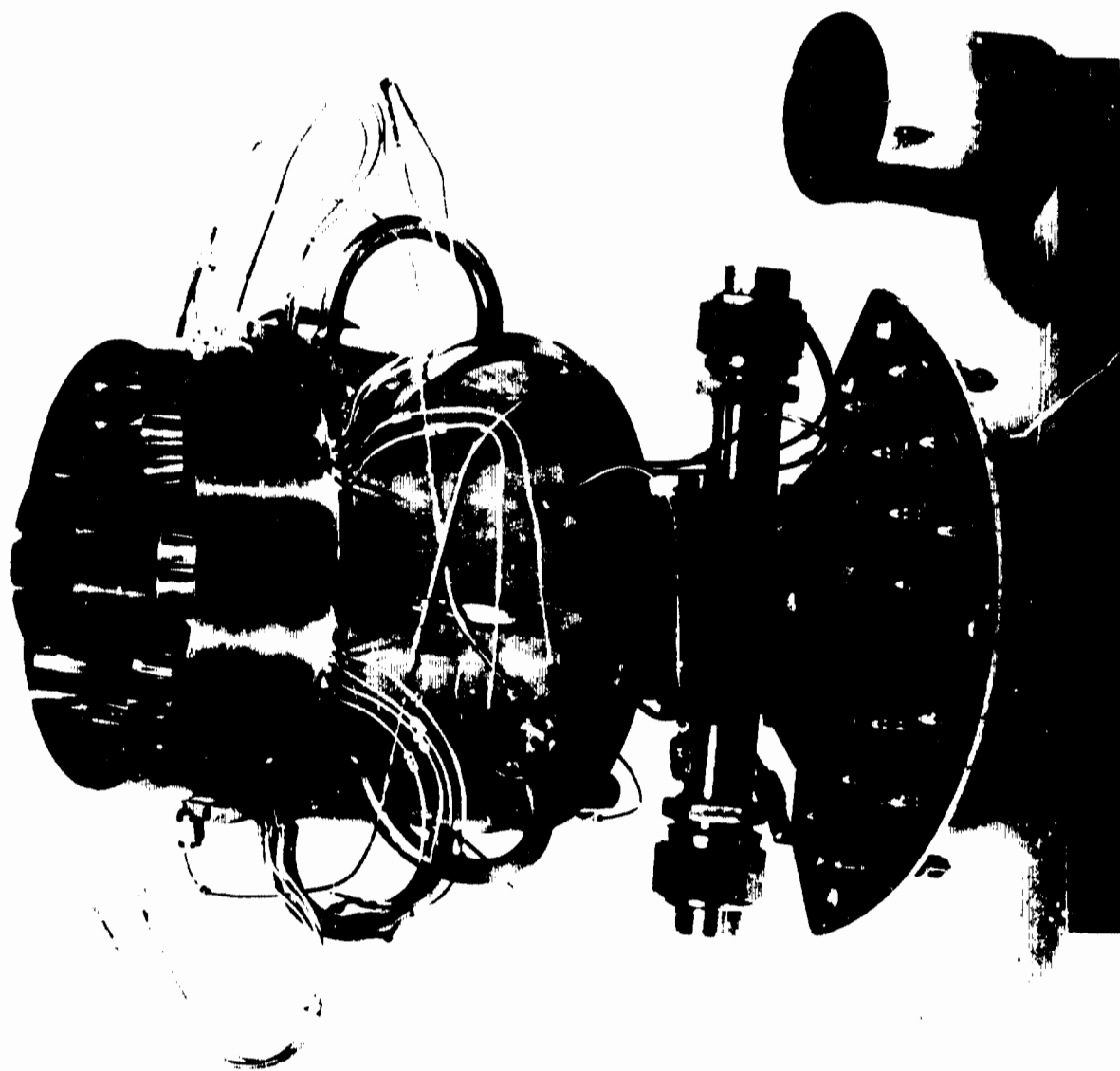


Fig. 53 Eight Chambers Touching Multi chamber, $\epsilon_{CL} = 50$

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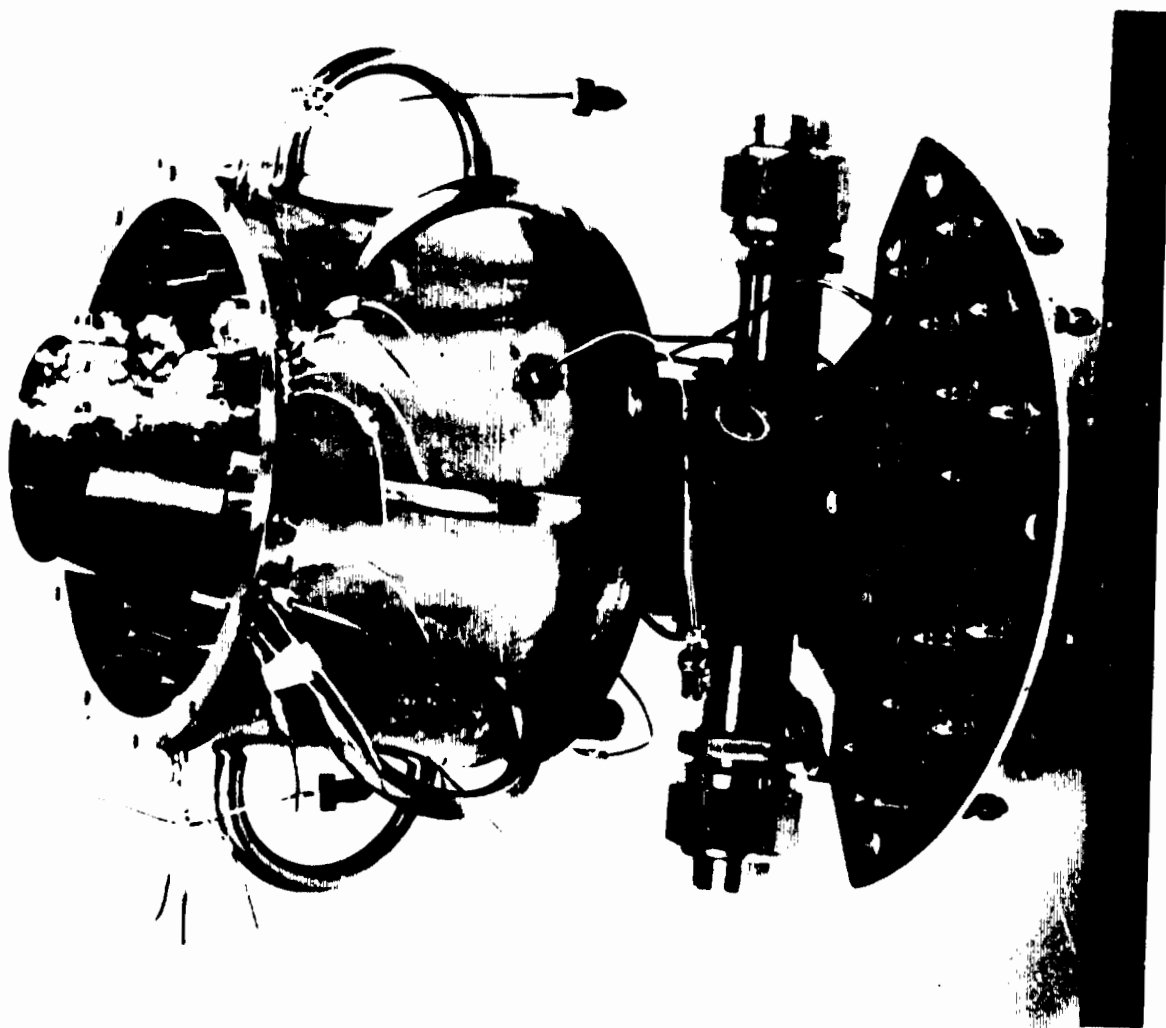


Fig. 54 Eight Chambers Spaced Multichamber, $\epsilon_{CL} = 50$

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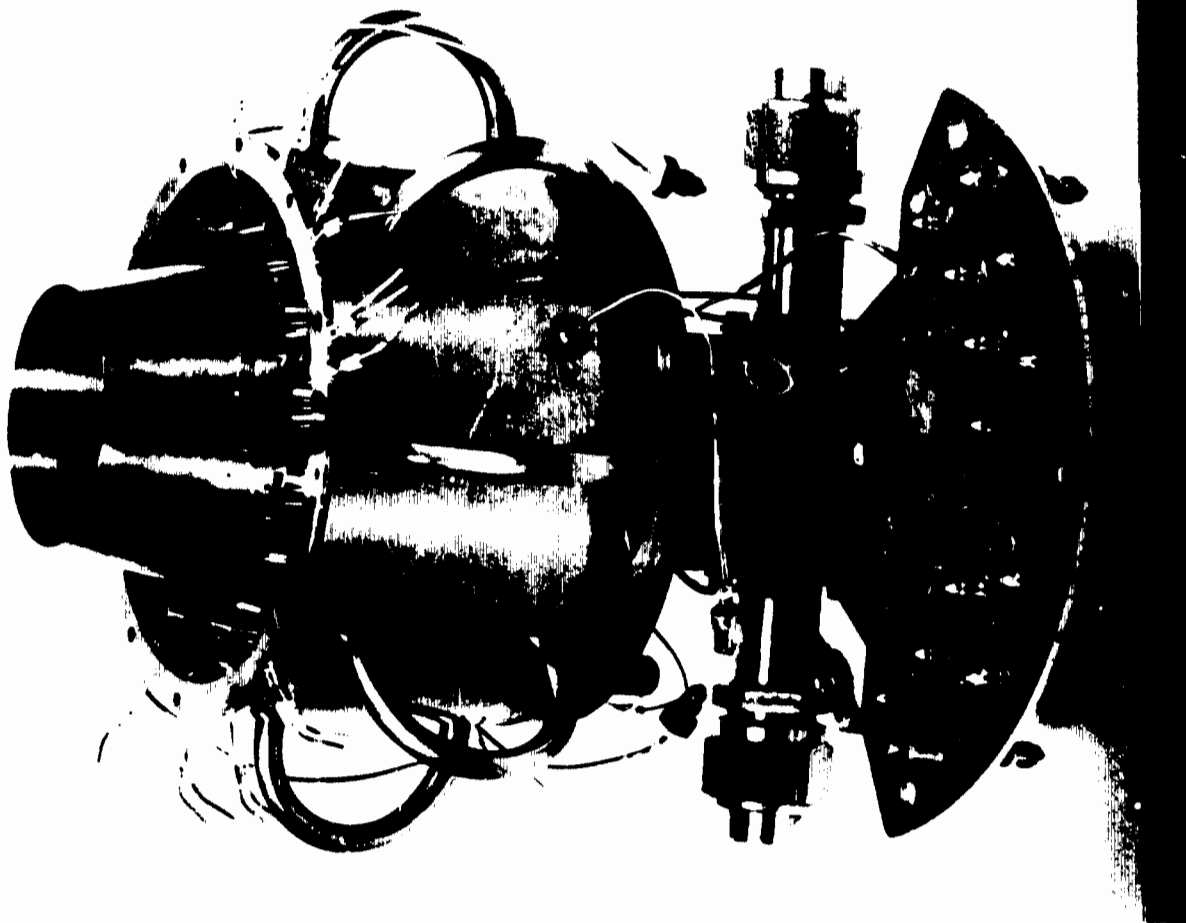


Fig. 55 Sixteen Chambers Touching Multichamber, $\in_{CL} = 50$

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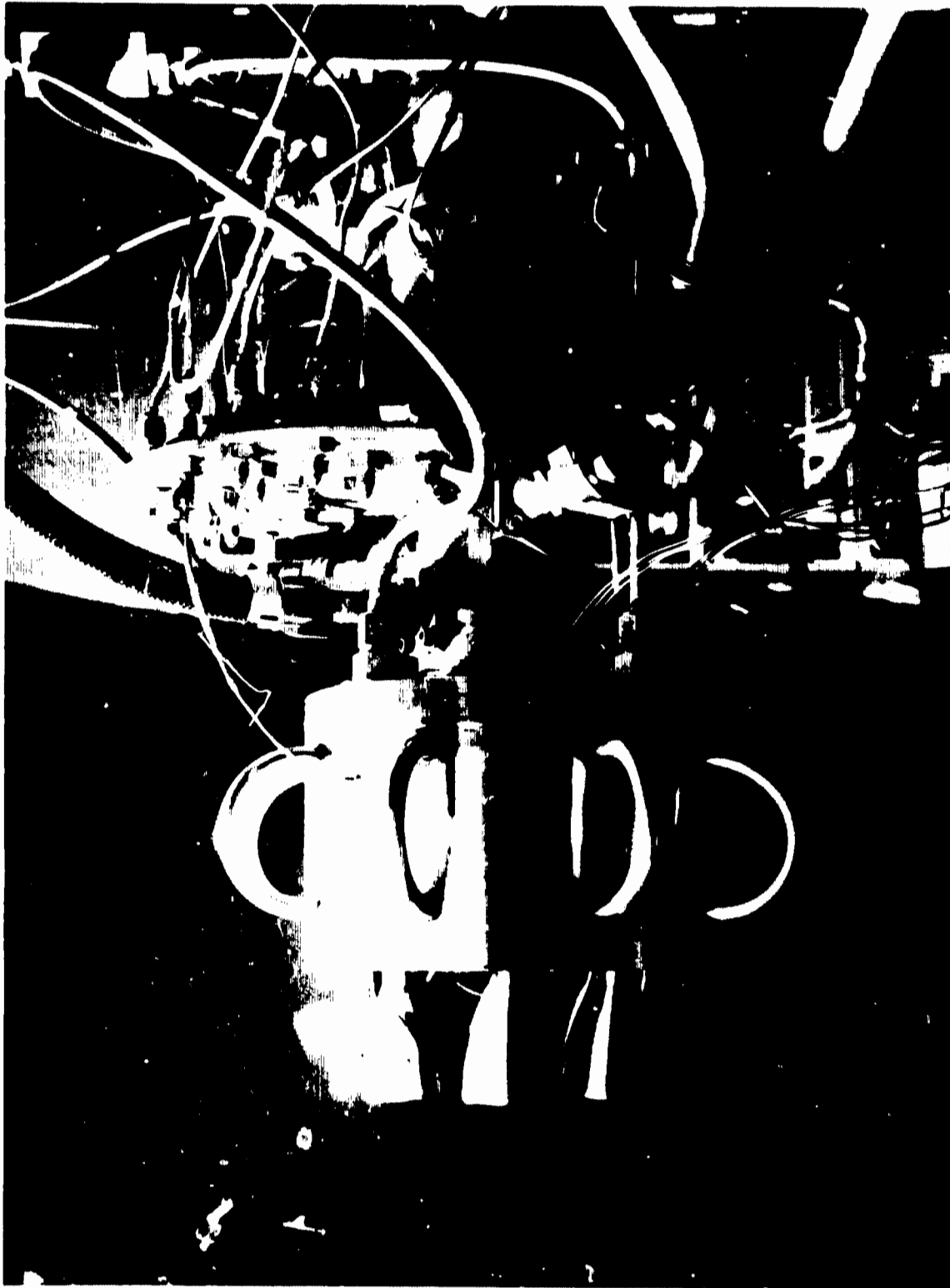


Fig. 56 RMF Installation of Stripped Down Version of Eight Chamber Touching Multichamber.

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Referring to Fig. 52, the first step in designing a multichamber model is to select independently the number of chambers N , the gap spacing δ , and the overall area ratio ϵ_{CL} . Two quantities must then be determined simultaneously, the modular exit area ratio ϵ_M and the tilt angle θ_T . To do this, a module exit area ratio is first assumed. The tilt angle is then determined from the difference between Prandtl-Meyer angles corresponding to the cluster or overall area ratio ($\epsilon_{CL} = 50$ in this case) and the module area ratio. Now that the tilt angle is known a new module exit area ratio can be calculated from the above equation. The process is repeated until sufficient accuracy is obtained.

The tilt angle and module area ratio have now been fixed and the radial dimension of point a (Fig. 57) is determined. An ideal spike is designed for the same area ratio as the overall or cluster area ratio of the multichamber as if it had a point expansion about point c. Point b is then selected at the same radial distance as point a and the ideal contour is translated axially so that point a and b coincide. The ideal contour is then truncated at the desired length. This gives a relatively good match in angle between the module and the spike at point a.

This process was carried out for all of the multichamber nozzles with spike extensions. For the two models with 8 chambers the theoretical contours were approximated by conical spikes, the difference in performance being only 0.01 percent.

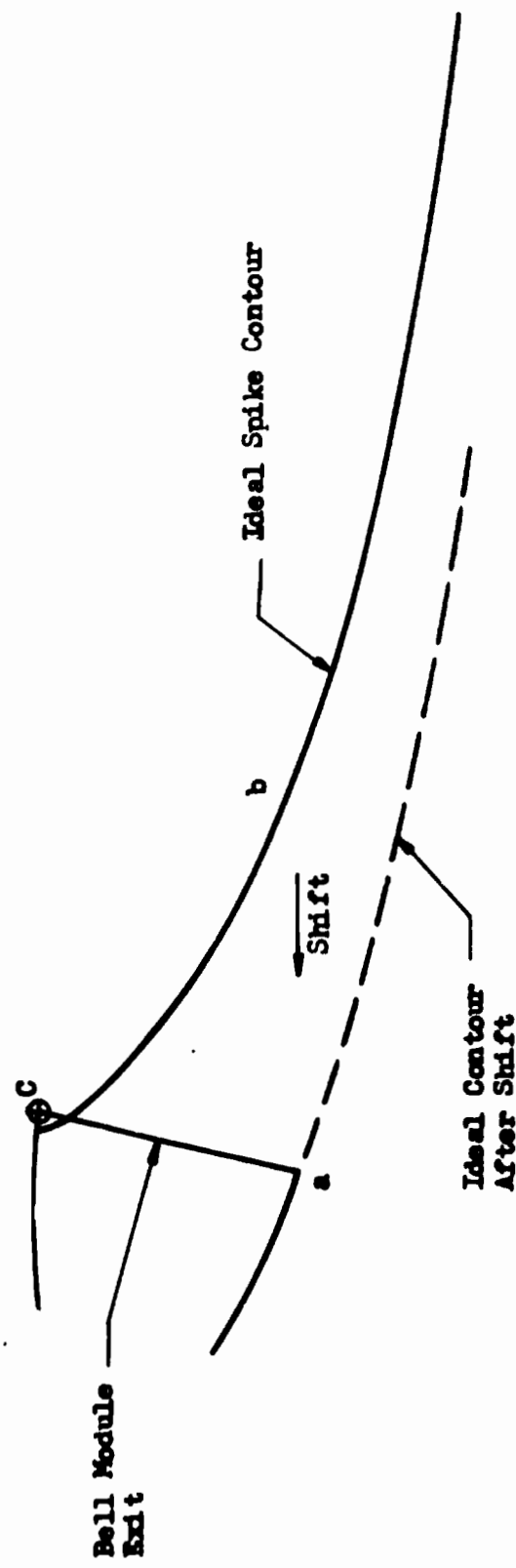


Fig. 57 Design of Spike Contour for Multichamber Models

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TEST PROGRAM

A total of 256 tests were conducted during a 6-week period. All of the configurations were tested over a pressure ratio range approximating sea level to design pressure ratios. The effect of secondary flow was investigated for all configurations over the entire pressure ratio range. Intersegmental (i.s.) bleed was used for the multichamber configurations in addition to secondary flow.

Model I-3, the scaled hot-firing model, was tested using both air and CP_4 gas. Several secondary-flow injection methods were investigated for the scaled hot-firing model.

Performance Calculations

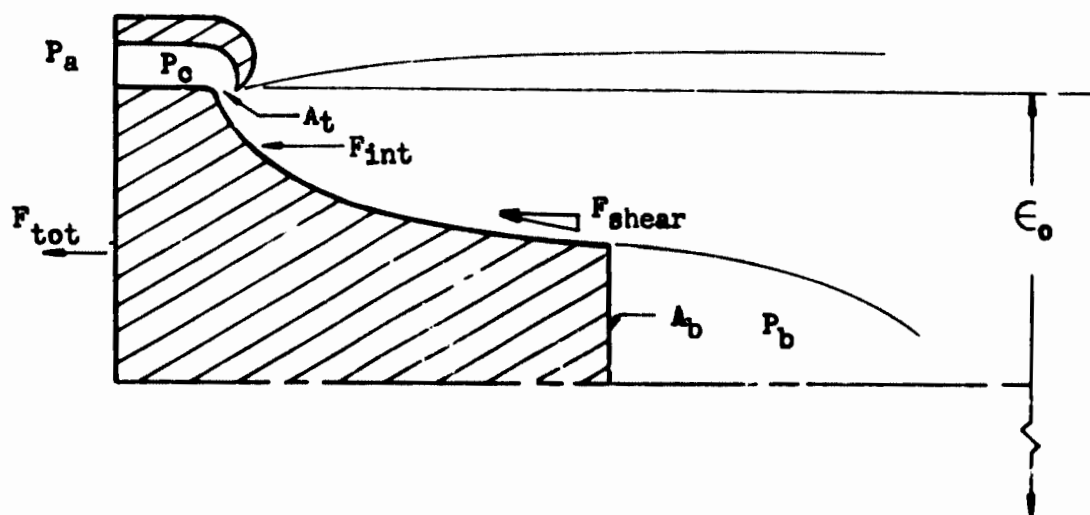
Primary flow field theoretical performance was calculated for the annular models using the method of characteristics (Ref 4 and 5) for the potential flow and the integral momentum equation for the drag losses (Ref 6 through 9). Solutions for both the potential flow field and drag loss have been developed on electronic computer programs used at Rocketdyne. Overall performance was then predicted by adding the contributions from experimental base pressure and ambient drag loss. Total nozzle performance is obtained by a summation of all contributing factors which are listed as follows:

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1. Potential flow (intrinsic nozzle performance)
2. Boundary layer drag loss
3. Base pressure contribution
4. Ambient drag

$$C_{F_{tot}} = C_{F_{int}} - C_{F_{drag}} + C_{F_b} - C_{F_{Amb.}}$$

With the aid of the figure below, these terms are defined as follows:



$$C_{F_{tot}} = \text{overall nozzle performance, } \frac{F_{tot}}{P_c A_t}$$

$$C_{F_{int}} = \text{potential flow field performance, } \frac{F_{int}}{P_c A_t}$$

$$C_{F_{drag}} = \text{boundary layer drag, } \frac{F_{shear}}{A_t P_c}$$

$$C_{F_b} = \text{base pressure contribution, } \frac{P_b}{P_c} \frac{A_b}{A_t} = \frac{P_b}{P_c} E_b$$

$$C_{F_{Amb.}} = \text{ambient drag, } \frac{P_a}{P_c} E_0$$

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Nozzle efficiency, C_T , is then calculated by comparing $C_{F_{tot}}$ to the ideal $C_{F_{opt}}$ at a given pressure ratio, P_a/P_c .

$$C_T = \frac{C_{F_{tot}}}{C_{F_{opt}}}$$

where

$$C_{F_{opt}} = \sqrt{\frac{2\gamma^2}{\gamma-1} \left(\frac{2}{\gamma+1}\right)^{\frac{\gamma+1}{\gamma-1}} \left[1 - \left(\frac{P_a}{P_c}\right)^{\frac{\gamma-1}{\gamma}}\right]}$$

$C_{F_{tot}}$ is obtained in a slightly different manner for the experimental data.

$$C_{F_{tot}} = \frac{F_{tot}}{P_{c_{Mod}} A_{Mod}^*}$$

$$A_{Mod}^* = \sqrt{\frac{T_{c_{Mod}}}{T_{c_v}}} \frac{P_{c_v}}{P_{c_{Mod}}} \frac{f_v}{f_{Mod}} A_{t_v} C_{D_v}$$

$$C_{F_{tot}} = \frac{F_{tot}}{P_{c_v} A_{t_v} C_{D_v} f_v} \sqrt{\frac{T_{c_v}}{T_{c_{Mod}}}}$$

in which

- F_{tot} = total measured force
- P_{c_v} = flowmeter chamber pressure
- A_{t_v} = flowmeter throat area

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C_{Dv}	=	flowmeter throat discharge coefficient
T_{cv}	=	flowmeter chamber temperature
T_{cMod}	=	model chamber temperature
f_v	=	flowmeter weight flow coefficient
f_{Mod}	=	model weight flow coefficient

Since $A_{Mod}^* = C_{Dv} A_t$, all experimental performances are presented with respect to A_{Mod}^* , the aerodynamic throat area, rather than A_t , the geometrical throat area. A_{Mod}^* was also used in calculating theoretical performance in order to be consistent.

Critical data for all of the models is tabulated in Appendix 3.

Scaled Hot-Firing Model - Air Tests

The principal objectives of the tests with this model were:

1. Determine the overall nozzle performance, with and without secondary flow over an altitude range from sea level to design altitude.
2. Test several base configurations and evaluate secondary-flow injection methods.
3. Determine nozzle performance and base pressures using a gas, CF_4 , having a ratio of specific heats which approximates that of hot-firing gases. Compare these CF_4 data with the air data and the data to be obtained in the hot-firing program.

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The open-base model was first tested with air over a pressure ratio range from 20 to 600 (design pressure ratio is approximately 5:5) without secondary flow. A reference performance with secondary flow was then obtained with the same model by varying the secondary flow rate at pressure ratios of 35, 170, and 540. The secondary flow giving maximum efficiency at each pressure ratio was determined. Secondary flow was introduced using an 8-hole orifice recessed within the open base (Component 3 in Fig. 45, p.79). This configuration (Model I-3, Table 4, p.76) is used as a reference for comparison with the other base configurations and injection methods.

Tests were then performed with air using the other base injection methods. These were the radially-in, radially-out, porous plate and supersonic nozzle configurations (see Table 4, p.76). The supersonic nozzle configuration consisted of secondary flow being injected through each of two conical nozzles of area ratio 3.5 and 15 respectively. Each configuration was tested at pressure ratios of 35, 170, and 540 using the optimum secondary flow rate determined from the open-base configuration tests.

The results of the RNTF (Rocket Nozzle Test Facility) tests are shown in Fig. 58 and are tabulated in Appendix 3. Near design pressure ratio ($P_c/P_a = 540$) the thrust efficiency was 96.5 percent with the open base configuration and no secondary flow. For the open base configuration secondary flow (air) was varied from 0 to 3 percent of primary flow with a resulting nozzle efficiency peak of 97.6 percent (see Fig. 59) occurring at 2 percent secondary flow. These efficiencies with air are lower than usually expected because the contour is designed for $\gamma = 1.25$.

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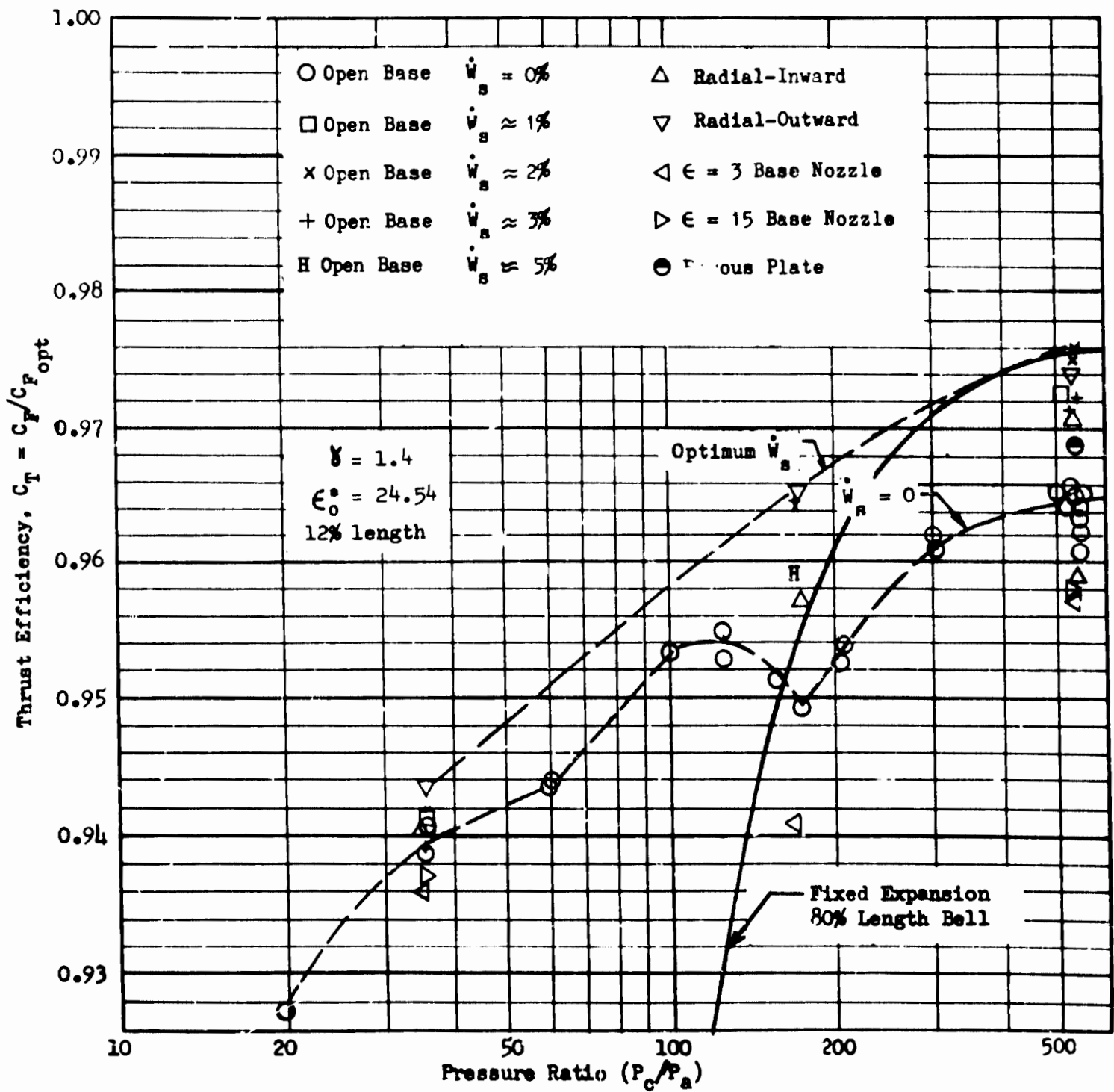


Fig. 58 Performance vs Pressure Ratio, Scaled Hot-Firing Model

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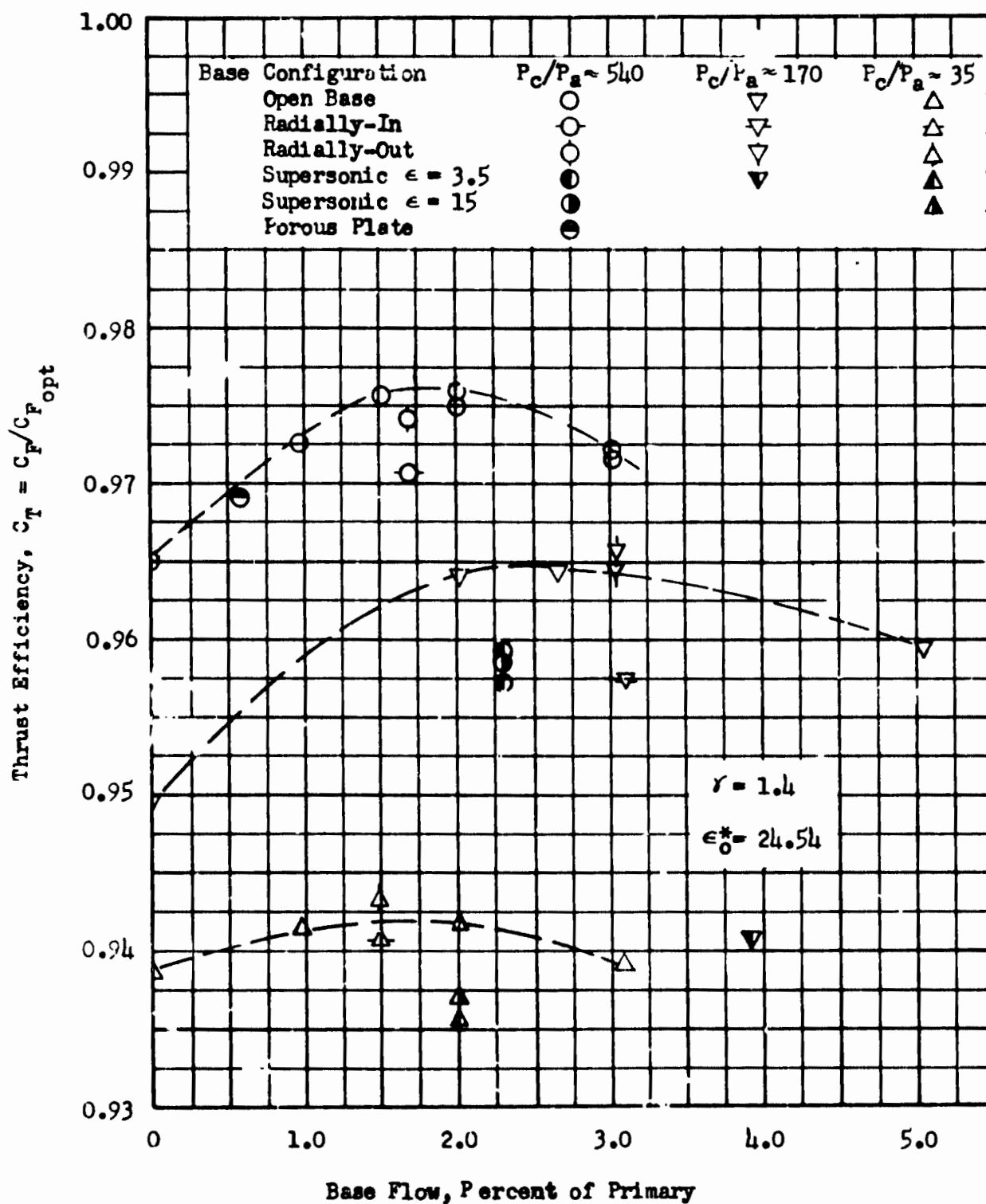


Fig. 59 Performance vs Base Flow Rate, Scaled Hot-Firing Model

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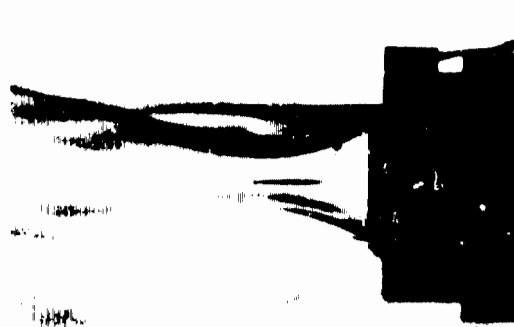
Figure 59 shows that the porous plate base gives essentially the same performance as the open cavity. The radially-out base gives very nearly the same performance as the open cavity showing slightly lower performance at design pressure ratio but slightly higher performance at the lower pressure ratios. A significant drop in performance is exhibited by the radially-in base at design pressure ratio and the wake closing point (pressure ratio 170). Both base supersonic nozzles exhibit low performances throughout the operating range.

Figure 60 presents Schlieren photographs of tests with the various base configurations at approximately the same secondary flow. The only configuration exhibiting a perceptibly different base flow field was the supersonic injection model where the supersonic secondary flow field shocks are readily seen.

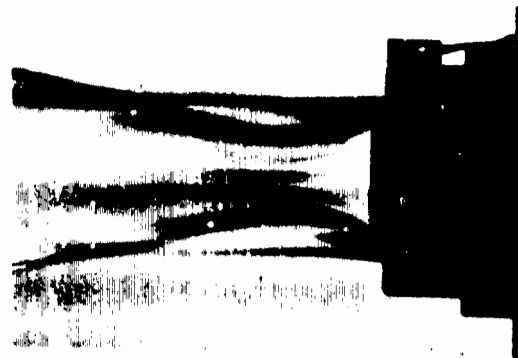
Referring to the efficiency curve, Fig. 58, it can be observed that a performance dip occurs at a pressure ratio of approximately 170, the point at which the base flow changes from the closed to the open-wake regime. This point is further verified by observing the base pressure vs pressure ratio plot, Fig. 61, where the base pressure remains steady above a pressure ratio of 170. Introduction of secondary flow at this pressure ratio gives substantial performance increases for the open, radially-out and radially-in base configurations. Both the open base and the radially-out base give a performance increase of about 1.5 percent.

At a pressure ratio of about 35, small gains in efficiency were noted with addition of base bleed with all base configurations except the supersonic injection. For all pressure ratios the optimum secondary flow appears to be between 1.5 and 2.5 percent of primary flow.

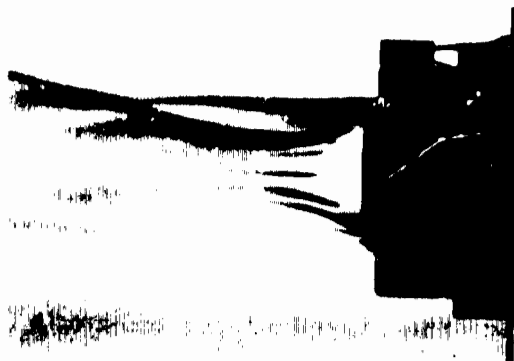
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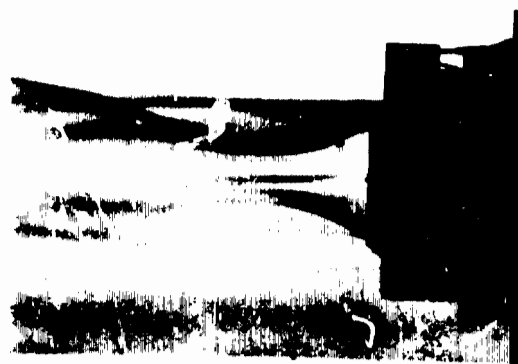
a) Open Base
 $P_c/P_a = 540, \dot{W}_s = 1.5\%$



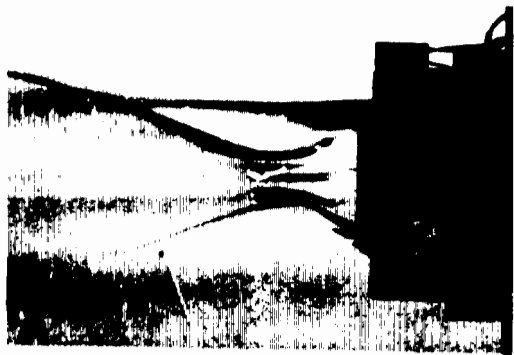
b) Open Base
 $P_c/P_a = 539, \dot{W}_s = 3.0\%$



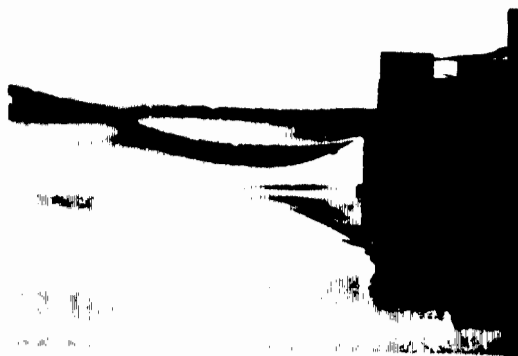
c) Radially-Inward Base
 $P_c/P_a = 536, \dot{W}_s = 1.7\%$



d) Radially-Outward Base
 $P_c/P_a = 540, \dot{W}_s = 1.7\%$



e) Supersonic Base, $\epsilon = 3.5$
 $P_c/P_a = 536, \dot{W}_s = 2.1\%$



f) Porous Plate Base
 $P_c/P_a = 525, \dot{W}_s = 2.2\%$

Fig. 60 Schlieren Photographs of Various Base Configurations,
 $\epsilon_0 \approx 25$, Scaled Hot-Firing Model

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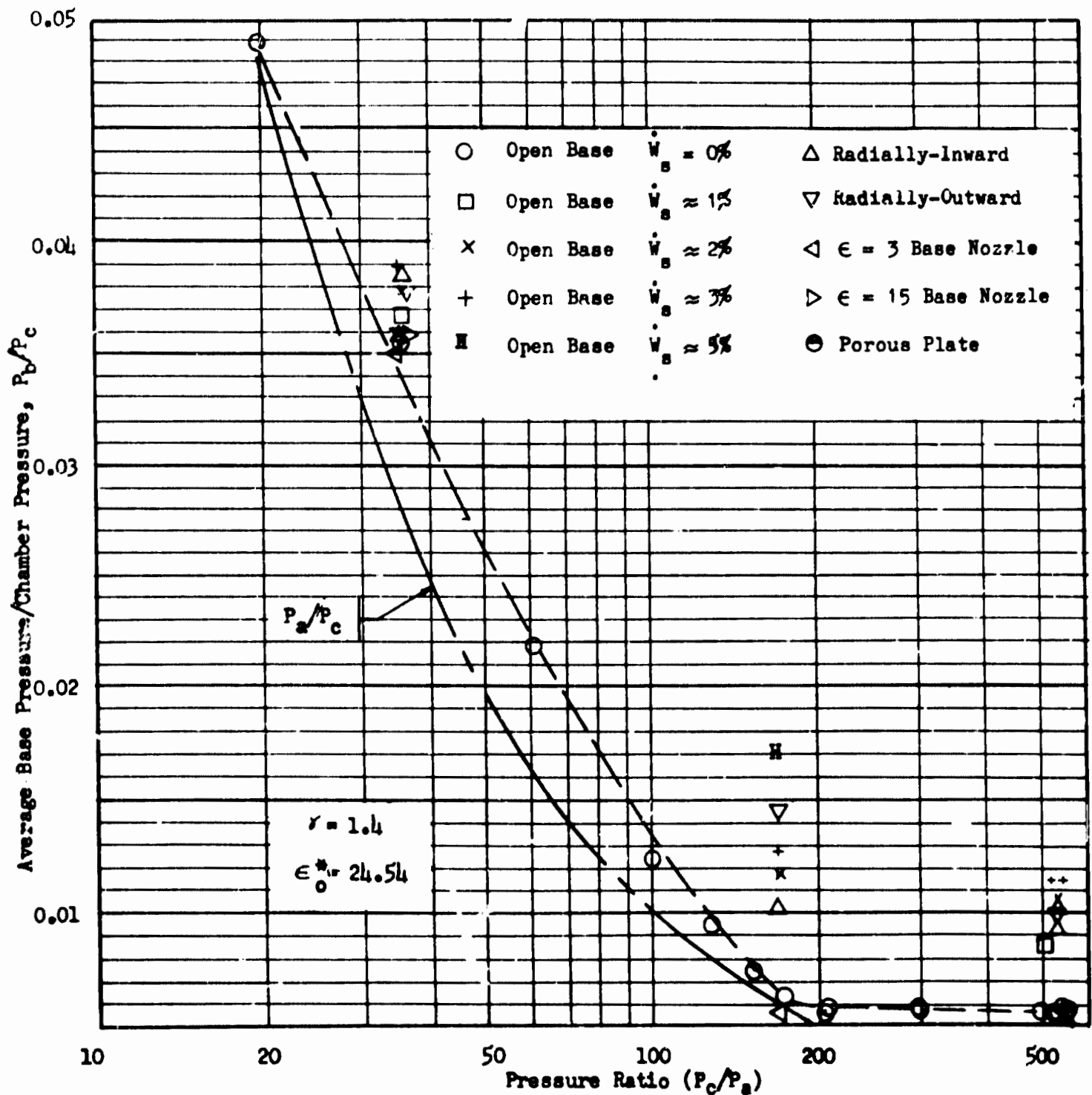


Fig. 61. Base Pressure Curves for Scaled Hot-Firing Model

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The performance of a fixed expansion, 80 percent length bell of 24.54 area ratio is shown for comparison in Fig. 58. The bell performance was computed using a nozzle vacuum efficiency of 98.56 percent and a constant drag loss equal to 0.9 percent of the theoretical vacuum thrust coefficient. These values were determined from bell nozzle theoretical efficiency curves and theoretical drag computations for a 27.5 area ratio J-2 cold flow model of the same size and operating at the same chamber pressure.

The efficiencies of the bell and the aerospike are the same at design pressure ratio even though the bell nozzle length is 6.6 times greater than the aerospike. At a pressure ratio of 100 (~ 20 percent of design) the fixed expansion bell has an efficiency of 91.3 percent compared to 95.8 percent for the altitude compensating aerospike. At a pressure ratio of 50 (10 percent of design pressure ratio) the fixed expansion bell efficiency has dropped to 78.7 percent compared to 94.8 percent for the aerospike. It should be noted that advanced booster engines initially operate at 10 to 15 percent of design pressure ratio. A 16 percent length aerospike designed for air was tested with air under NASA contract (Ref. 11) and yielded design efficiencies of 98.4 percent with secondary flow and 97.2 percent without secondary flow demonstrating design efficiencies substantially higher than a comparable 80 percent length bell. This comparison clearly demonstrates that a short aerodynamic spike nozzle is at least comparable in performance to an 80 percent length bell at design pressure ratio and has considerably higher performance than the bell at lower than design pressure ratio.

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The open base, radially-in, radially-out and the porous plate base plates all showed relatively good base pressure increases with introduction of secondary flow (see Fig. 61). This resulted in net increases in efficiencies. However, the supersonic base injection showed very little or no increase in base pressure in most cases. Thus, when the performance was charged with the additional mass flow for the base, a performance loss resulted.

Theoretical and experimental wall pressures for this nozzle are presented in Fig. 62. Near the throat ($X/R^* \approx 0$) agreement between data and theory is not as good as further down the nozzle contour. This occurs because the pressure gradient near the throat is steep and even small diameter pressure taps cover a significant portion of the actual pressure range.

The pressure profile down to a pressure ratio of 61 was constant. Below 61 a pressure rise was noted along the contour due to nozzle recompression. Since at low pressure ratios these pressures did not change with secondary flowrate, it can be concluded that the flow did not separate from the contour. This is also evidenced by observing the Schlieren photographs (Fig. 63).

Scaled Hot-Firing Model - CF_4 Tests

Ten tests were conducted using CF_4 gas as the test fluid. All tests were performed with the open base configuration. In addition to achieving high performance, this configuration allows a more reliable determination of average base pressure. The base pressure is relatively uniform across the face of the cavity and a good average base pressure is easily obtained.

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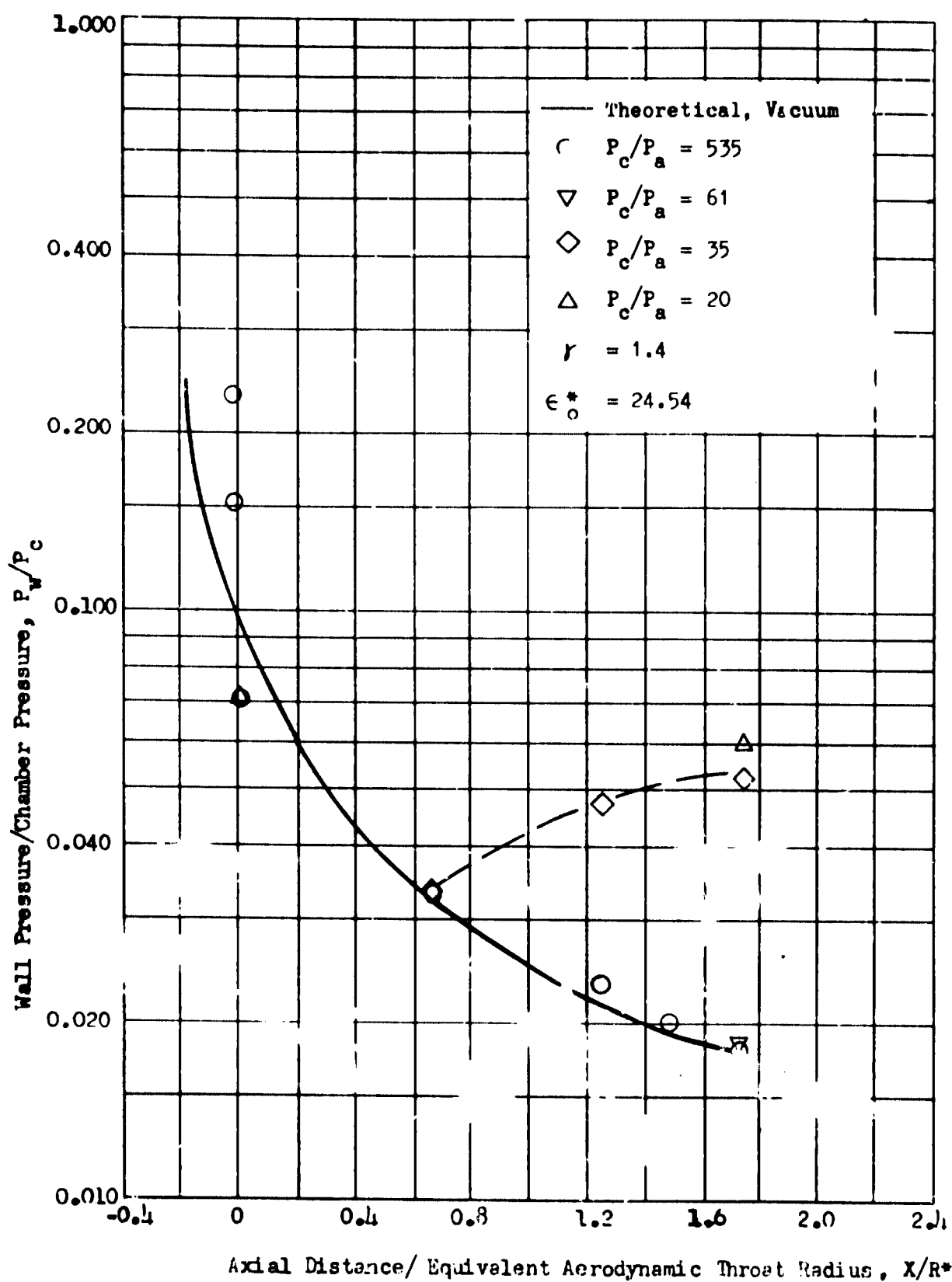


Fig. 62. Wall Pressure Profile for Scaled Hot-Firing Model. $\dot{w}_s = 0$

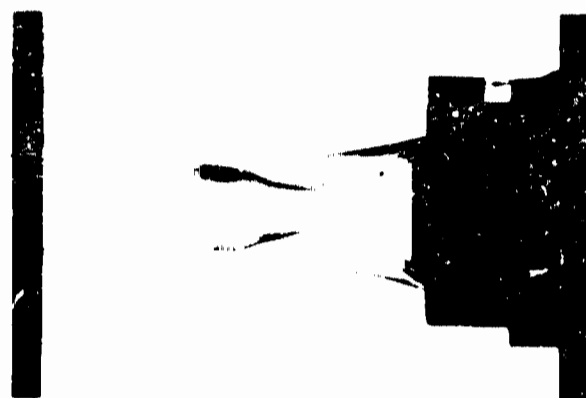
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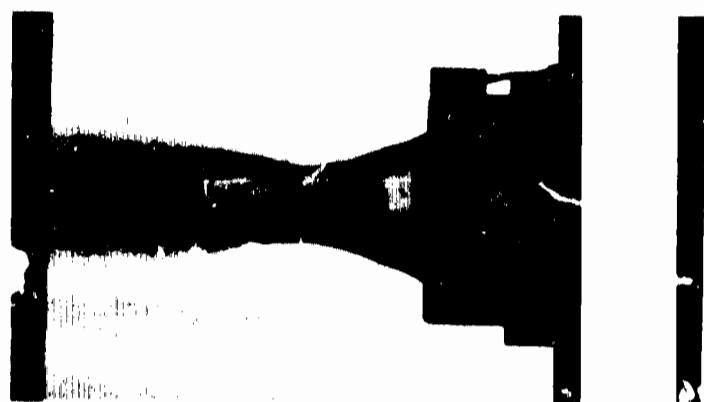
(a) $P_c/P_a = 524$

$\dot{W}_B = 0\%$



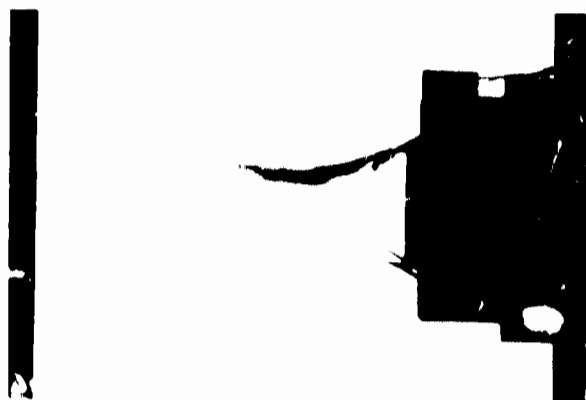
(b) $P_c/P_a = 173$

$\dot{W}_S = 0\%$



(c) $P_c/P_a = 36$

$\dot{W}_B = 0\%$



(d) $P_c/P_a = 35$

$\dot{W}_S = 2\%$

Fig. 63. Schlieren Photographs on Scaled Hot-Firing Spike Nozzle, $\gamma = 1.4$, Open Base

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In the initial phase of the CF_4 testing, it was necessary to determine if, and under what conditions, condensation of CF_4 would occur in the flow field. This was found necessary since examination of a pressure-enthalpy diagram (see Fig. 6b) for CF_4 indicated that in the expansion process, the pressure and temperature could fall inside the saturation region. For example, starting at a chamber pressure of 150 psia at a temperature of 70 deg F and isentropically expanding over the design pressure ratio of 253, the process end point (the dashed line in Fig. 6b) falls just inside the saturation region. Since condensation could affect the base pressure values, initial tests at chamber pressures of 50, 100, and 150 psia were conducted to determine the operating conditions required to avoid condensation. An ultraviolet light was projected across the flow field to detect droplet formation. Polaroid photographs were taken and visual observations were made for each test.

At a chamber pressure of 150 psia, condensation was observed to occur about two-thirds of an exit diameter downstream of the exit of the nozzle (foggy region to the left of the nozzle in Fig. 6b). When the chamber pressure was reduced to approximately 100 psia (a more favorable expansion as shown on the pressure-enthalpy diagram) no condensation was observed. All further CF_4 testing was performed at or below a chamber pressure of 100 psia. The values of P_b/P_c were 0.0066, 0.0066 and 0.0067 for P_c values of 50, 100 and 150 respectively. Thus it appeared that condensation had negligible effect on base pressure. In all, eight tests were performed with no secondary flow over a pressure ratio range of 35 to 290 and two tests were performed with secondary flow near design pressure ratio. Data for these tests is tabulated in Appendix 3 and summarized in Figs. 65 and 66.

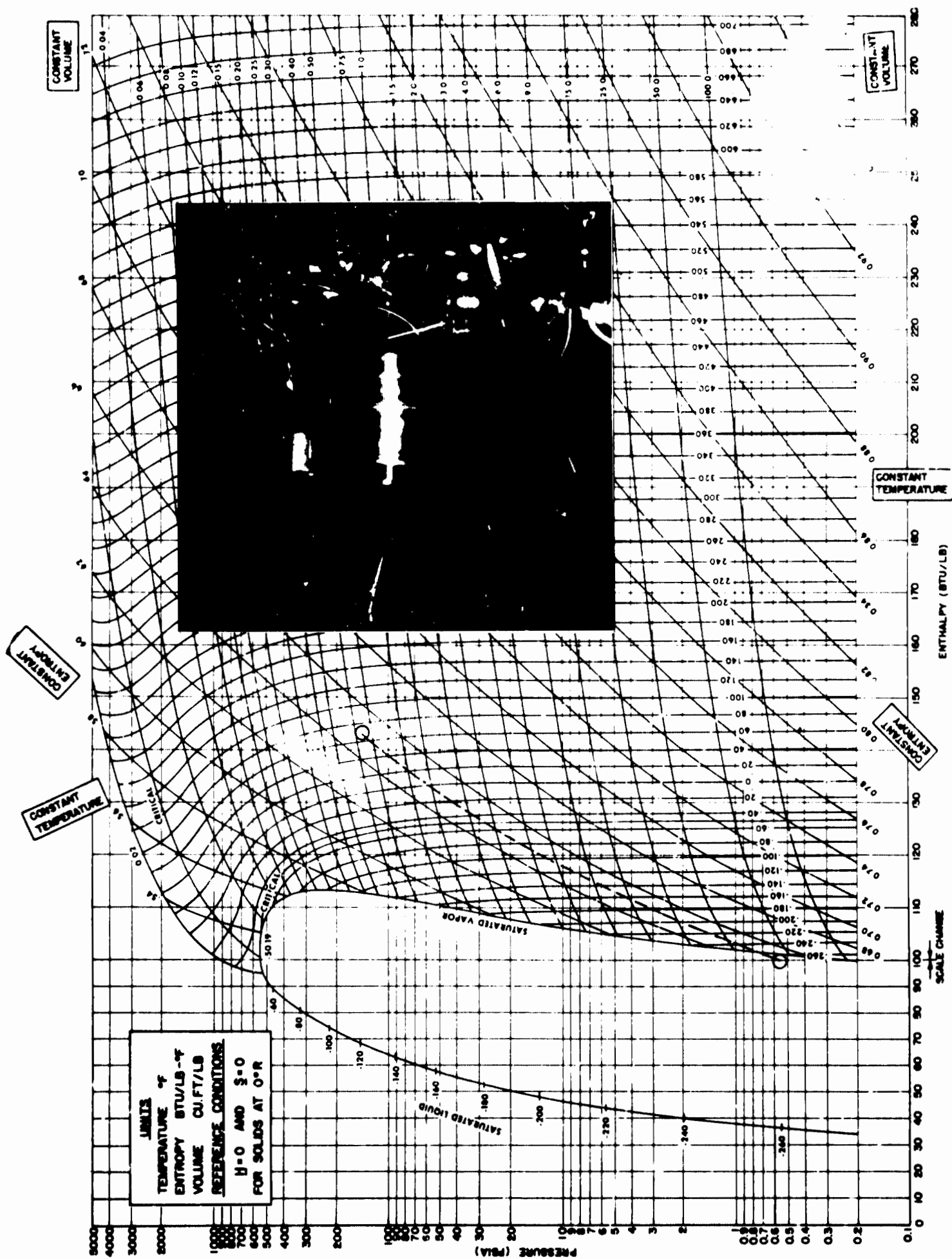


Figure 61 Pressure-Enthalpy Diagram For Carbon Tetrafluoride (CF₄)

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Figure 65 shows the performance of the $\epsilon_o^* = 24.26$ nozzle using CF_4 . Maximum performance attained at design pressure ratio (253) was 95.6 percent. This was increased to 96.8 percent by addition of 1.7 percent CF_4 base bleed. Examination of the base pressure curve, Fig. 66, shows the value of P_b/P_c to remain at 0.0067 down to a pressure ratio of approximately 120. At this point the base pressure starts to rise because the wake opens.

One of the principle reasons for testing with CF_4 was to have a cold-flow gas with a γ similar to that of the hot-firing model. Upon examining several gases CF_4 appeared to be the most reasonable gas to use. It had the necessary low γ and could be expanded to a low enough pressure without changing state. The equivalent γ for the hot-firing model is 1.25. At the time of selection of CF_4 , available information indicated that the γ of this gas would be close to 1.25. Since this is a relatively new gas available on a commercial basis, relatively little physical data was available until some time after the model was tested. The data shows that γ has a very wide variation from the chamber condition to the ambient condition. For example at $P_c = 100$ psia and $T_c = 530$ degrees Rankine, $\gamma = 1.18$. Expanding to $P_a = 0.2$ psia isentropically results in a $\gamma = 1.30$. This makes it quite difficult to arrive at an equivalent constant γ to use in an analysis involving the assumption of a perfect gas.

A parallel effort was simultaneously conducted at Rocketdyne evaluating the properties of CF_4 gas. In this effort it was found that it would be necessary to arrive at an ideal thrust coefficient (C_{Fopt}) for a given expansion process by considering the actual enthalpy change of the gas rather than calculating the ideal thrust coefficient from the

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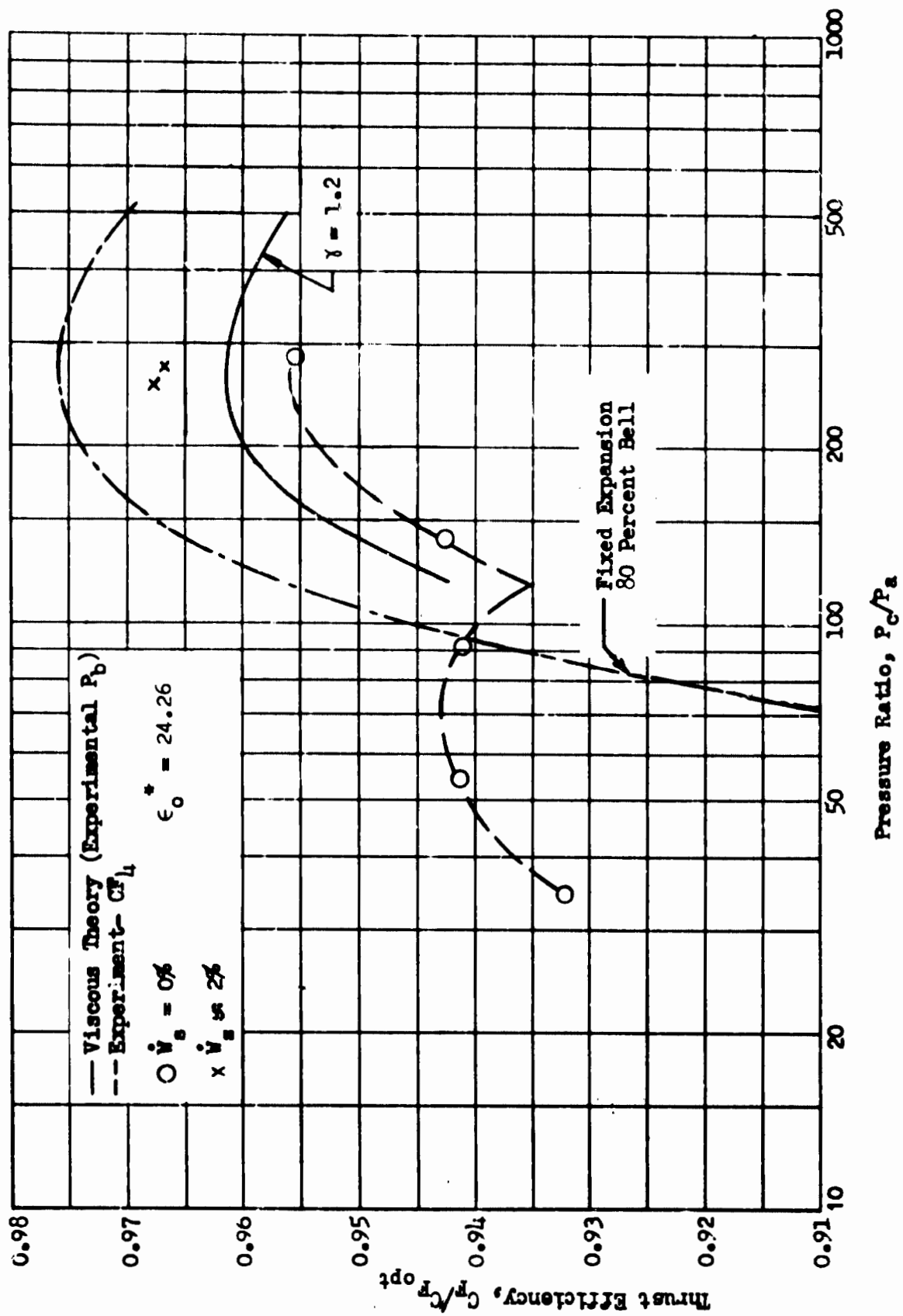


Fig. 65 Performance vs Pressure Ratio, Scaled Hot-Firing Model, CF_{L1} Tests

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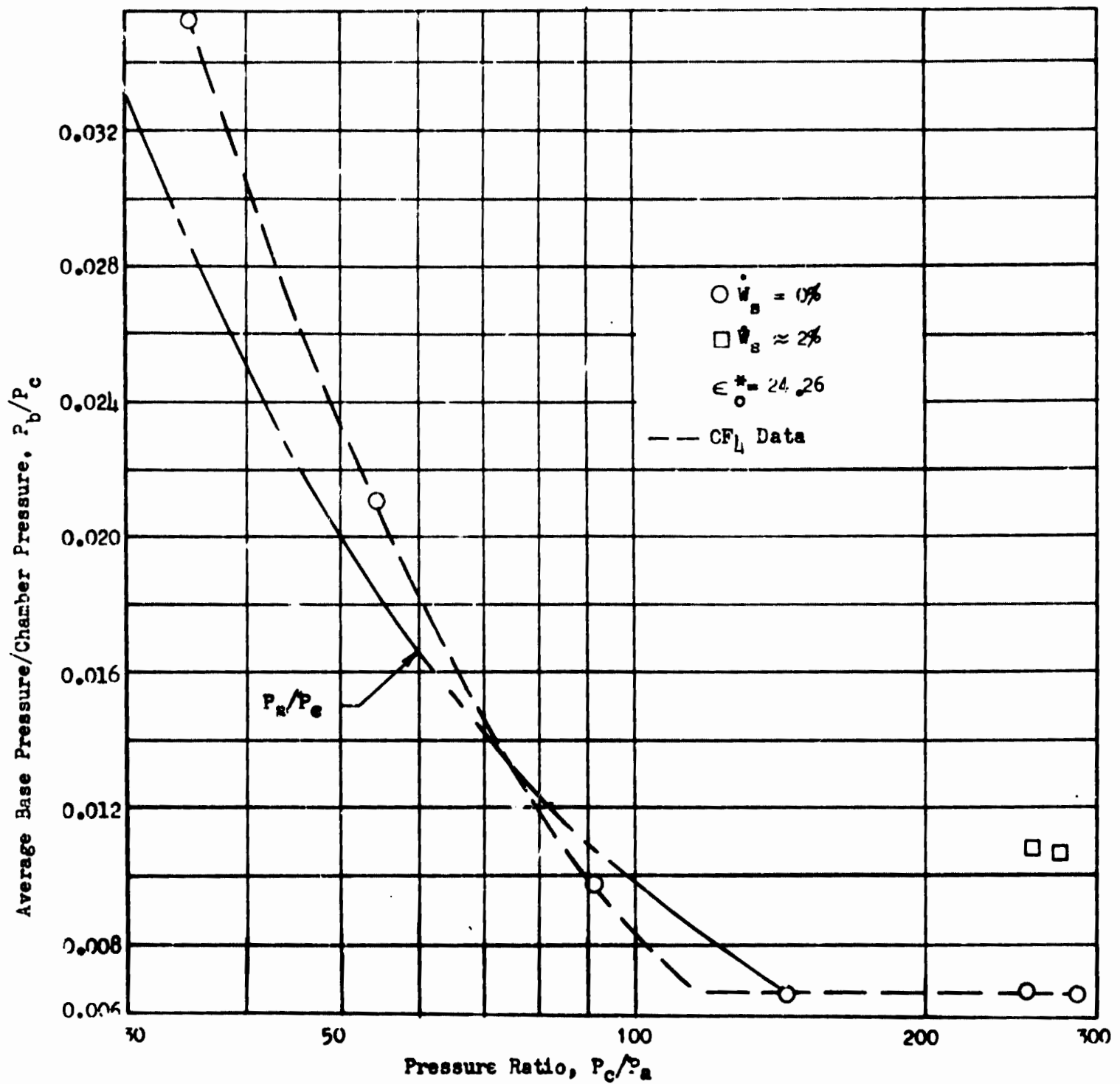


Fig. 66. Base Pressure vs Pressure Ratio, cooled Hot-Firing Model, CF_4 Tests

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usual one-dimensional ideal gas equations assuming a constant γ and pressure ratio. The method arrived at is summarized in Appendix 4. Using the real gas properties a C_{Fopt} is arrived at for a particular set of conditions ($P_c, T_c, P_a, \Delta S = 0$) and is used in calculating nozzle efficiency.

$$C_T = \frac{C_{F \text{ experimental}}}{C_{F \text{ opt}} \left| \begin{array}{l} \text{real} \\ \text{gas} \end{array} \right.}$$

These are the experimental values shown in Fig. 65. In this figure is also shown the theoretical performance curve (using experimental base pressures) for the $\epsilon_0^* = 24.26$ nozzle. The analysis for $\gamma = 1.2$ fell above the experimental curve. The amount of deviation is approximately 0.6 percent. This deviation could be caused by the accuracy limitations of the CF_4 properties. Reference 10 indicates that accuracy is limited by the equation of state used.

A representative value of γ for the operating range over which the nozzle was tested was found to lie somewhere between 1.20 and 1.21 (from the CF_4 properties). The representative γ is calculated from the real gas C_{Fopt} from

$$C_{Fopt} = \sqrt{\left[\left(\frac{2}{\gamma-1} \right) \left(\frac{2}{\gamma+1} \right)^{\frac{\gamma+1}{\gamma-1}} \right] \left[1 - \left(\frac{P_a}{P_c} \right)^{\frac{\gamma-1}{\gamma}} \right]}$$

The real gas C_{Fopt} and the pressure ratio are substituted in the above equation and the equation is solved for γ . This value of γ is called the process γ .

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The performance of a fixed expansion, 80 percent length bell of 24.26 area ratio is shown for comparison in Fig. 65. The bell performance was computed using a nozzle vacuum efficiency of 98.56 percent and a constant drag loss equal to 0.8 percent of the theoretical vacuum thrust coefficient. These values were determined from bell nozzle theoretical efficiency curves and theoretical drag computations for a similar cold flow bell nozzle.

The efficiency of the 80 percent length bell nozzle at design pressure ratio is 97.6 percent compared to 96.8 percent measured for the 12 percent length aerospike. The 0.8 percent lower performance for the aerospike tends to indicate that for lower γ gases somewhat longer aerospike lengths are required to achieve efficiencies equal to a bell at design pressure ratio. However, the theoretically predicted C_T (using measured base pressures) for the aerospike is also 0.6 percent higher than the measured values. Usually this type of theoretical prediction agrees with experimental data within 0.25 percent. If the theoretical values are more nearly correct the aerospike with secondary flow is only 0.2 percent lower performing at design pressure ratio than the bell. Theoretical analysis of this aerospike nozzle indicates that a gain of approximately 1.1 percent in efficiency at design pressure ratio would be achieved by increasing the aerospike length from 12 percent to 25 percent (both 12 percent and 25 percent lengths will be tested in the hot-firing phase of this program). This would result in design efficiencies between 97.9 and 98.5 depending on whether the gain is added to the experimental or to the theoretical aerospike performance curve.

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At a design pressure ratio of 100 (40 percent of design pressure ratio) the bell performance is approximately 0.5 percent higher than the experimental aerospike performance without secondary flow. Based on the similar effect of secondary flow on performance for this model with air and CF_4 it is expected that CF_4 secondary flow would increase performance between 1.0 to 1.5 percent at a pressure ratio of 100 bringing the experimental aerospike performance from 0.5 to 1.0 percent above the bell. The previous comments about the uncertainty of the experimental performance and the performance effects of a longer nozzle length also apply at this pressure ratio and would further increase the performance advantage over the bell to approximately 2.0 to 2.5 percent.

At a pressure ratio of 50 (20 percent of design pressure ratio) the fixed expansion bell performance is 84.4 percent compared to 94.1 percent for the experimental aerospike without secondary flow.

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Base Pressure Calculations

Theoretical and empirical methods of determining base pressures have been developed (Ref 11) and are in use at Rocketdyne. The theoretical methods are sub-grouped into three separate flow regimes; (1) small bleed, closed-wake, (2) large bleed, choked flow through the wake recompression zone, and (3) open-wake, low pressure ratio. Regimes (1) and (2) are at high nozzle operating pressure ratios, preventing ambient pressure from communicating with the base. Regime (3) is at low pressure ratios, giving a large base flow core which is not choked.

The essential difference between the small bleed and large bleed theories is in the recompression mechanism where the wake coalesces. For small bleed there is a recirculation of the base flow from the recompression zone back into the base flow region. As the bleed rate increases the amount of recirculation is reduced until no recirculation occurs but outflow from the base region through the recompression zone is the prevailing mode. The exact transition point is not easily determined but corresponds roughly to the maximum performance point in a performance vs base bleed curve (See Fig. 59).

Data of the hot-firing model for the open cavity base has been re-plotted in Fig. 67 , 68 and 69 along with the theoretical predictions of base pressure for this nozzle. For the air tests, the transition from small to large bleed is shown to occur at $\dot{W}_s/\dot{W}_p = 1.55$ percent. This compares to a maximum efficiency point on Fig. 59 of $\dot{W}_s/\dot{W}_p = 2.0$. The same theory applied to the CF_4 gas tests is shown in Fig. 68. Agreement in both cases is good.

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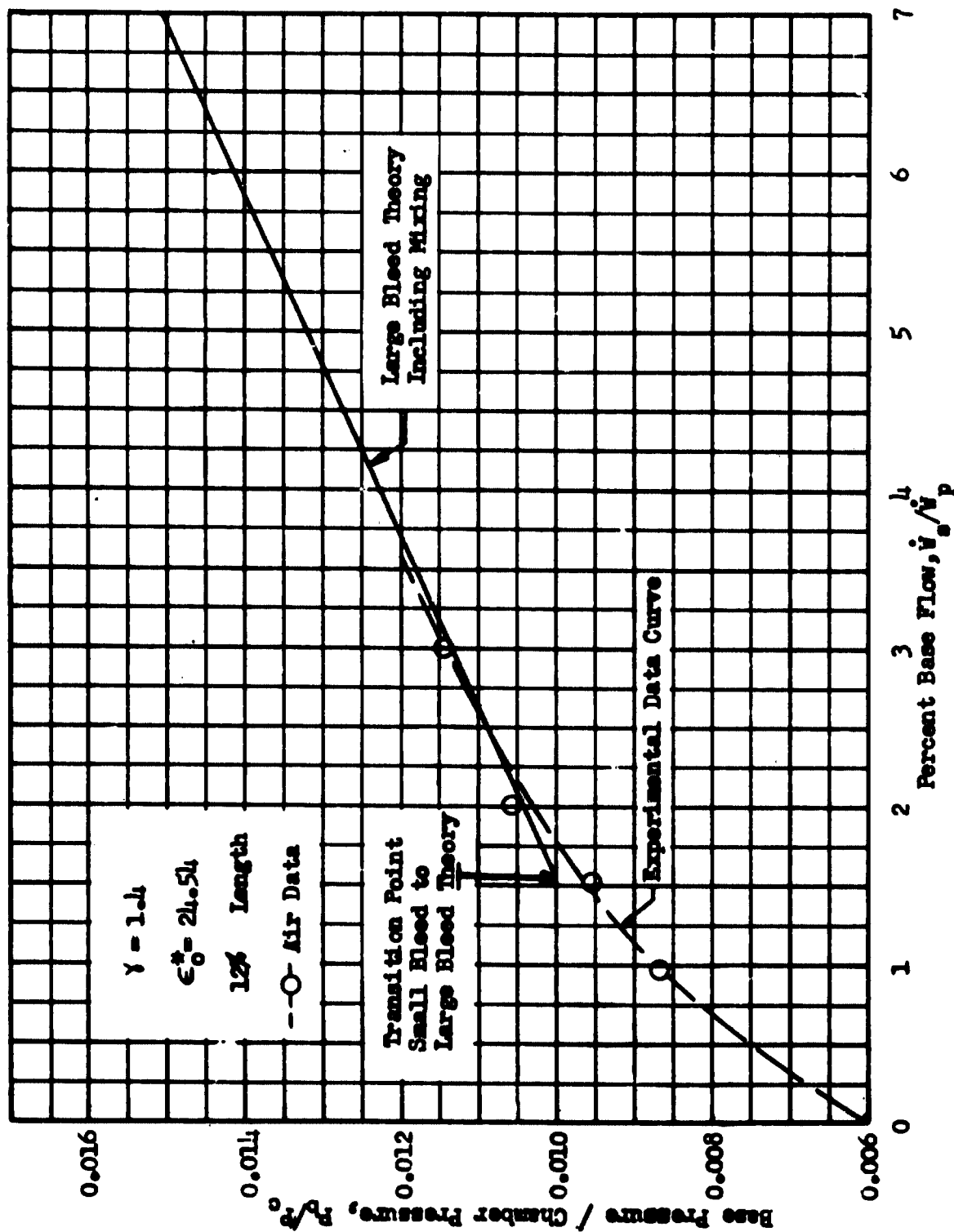


Fig. 67 Base Pressure vs Percent Base Bleed for Closed-Wake Flow, Scaled Hot-Firing Model, Air.

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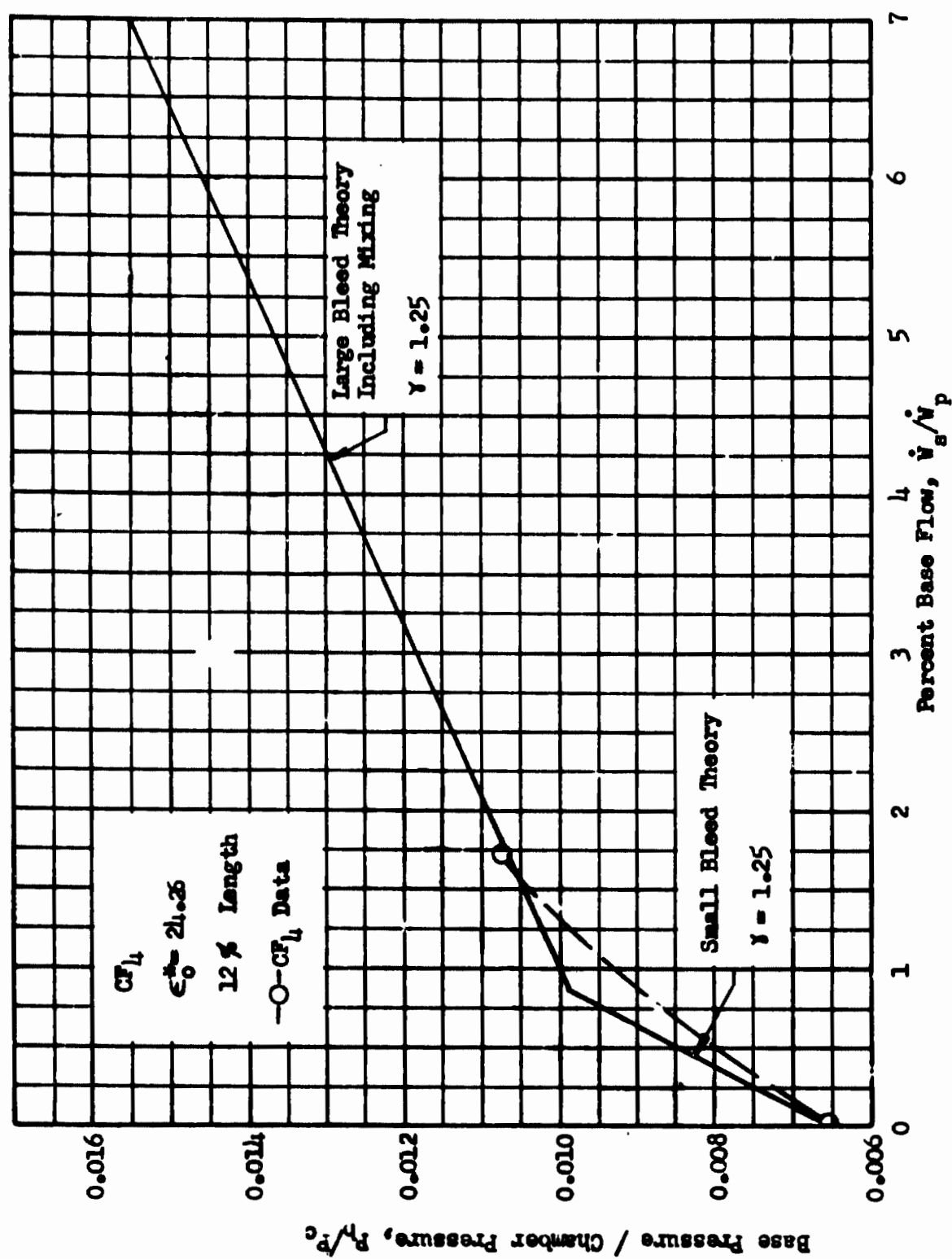


Fig. 68 Base Pressure vs Percent Base Bleed for Closed-Wake Flow, Scaled Hot-Firing Model, CF_{14} Tests

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The open-wake theory was applied to the same nozzle at a pressure ratio of $P_o/P_a = 61$. In this case the theory predicted pressures slightly higher than the data (Fig. 69).

Annular Reference Models

The principal objectives of testing the continuous-throat annular reference models ($\epsilon_o = 50$) were:

1. Determine performance for both shrouded and unshrouded continuous-throat aerodynamic spike nozzles over a wide pressure ratio range with and without secondary flow for comparison with the multichamber performance.
2. Record base pressures for comparison with multichamber base pressure values.
3. Determine the ambient pressure compensating characteristics of these nozzles.

These models were tested (with air) over a pressure ratio range from 100 to 1500 and a secondary flow (air) range from 0 to 3 percent of primary flow. Secondary flow was introduced from an annular orifice recessed within the centerbody. An open-cavity base configuration was used throughout the tests. Fifty-six tests were accomplished with these models.

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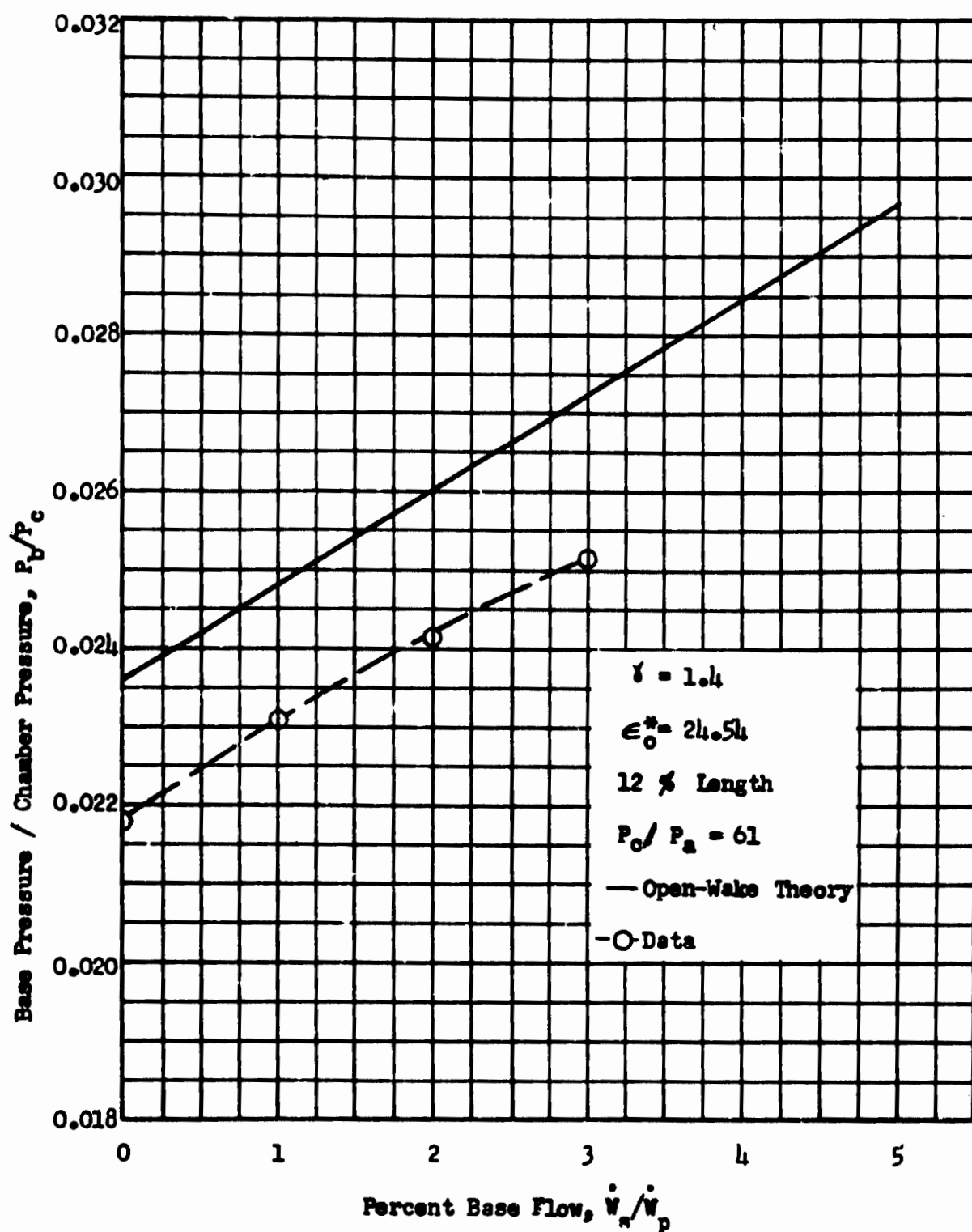


Fig. 69 Base Pressure vs Percent Base Bleed for Open-Wake Flow, Scaled Hot-Firing Model

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Point Expansion Model

Performance results of cold-flow testing of the point expansion model (model II-6, Table 3), are shown in Fig. 70 and in Appendix 3. Experimentally, the nozzle efficiency reached a value of 98.6 percent at a pressure ratio of 1375 and no secondary flow.

The performance at design pressure ratio (1375) peaked at 98.8 with the addition of 0.9 percent secondary flow (See Fig. 71). Efficiency gains were small since the nozzle (30 percent length) already has a high efficiency without secondary flow, leaving little margin for improvement. However, when secondary flow is available this configuration still provides a high performance means of utilizing it.

The performance curve at a pressure ratio of 490, becomes discontinuous, corresponding to the transition from closed to open base wake flow (See also Fig. 72 showing the transition in base pressure at a pressure ratio of 490). Adding secondary flow to the base at this point increased the nozzle efficiency from 97.3 with no secondary flow to 97.8 with 1.0 percent secondary flow (See Fig. 71). As normally occurs at the transition point, an appreciable increase in performance can be realized with the proper addition of secondary flow.

Secondary flow was added to the base at a pressure ratio of 150. Figure 71 shows that substantial efficiency gains were obtained raising the zero secondary flow efficiency from 94.8 to 96.0 percent at the optimum secondary flowrate of 1.8 percent.

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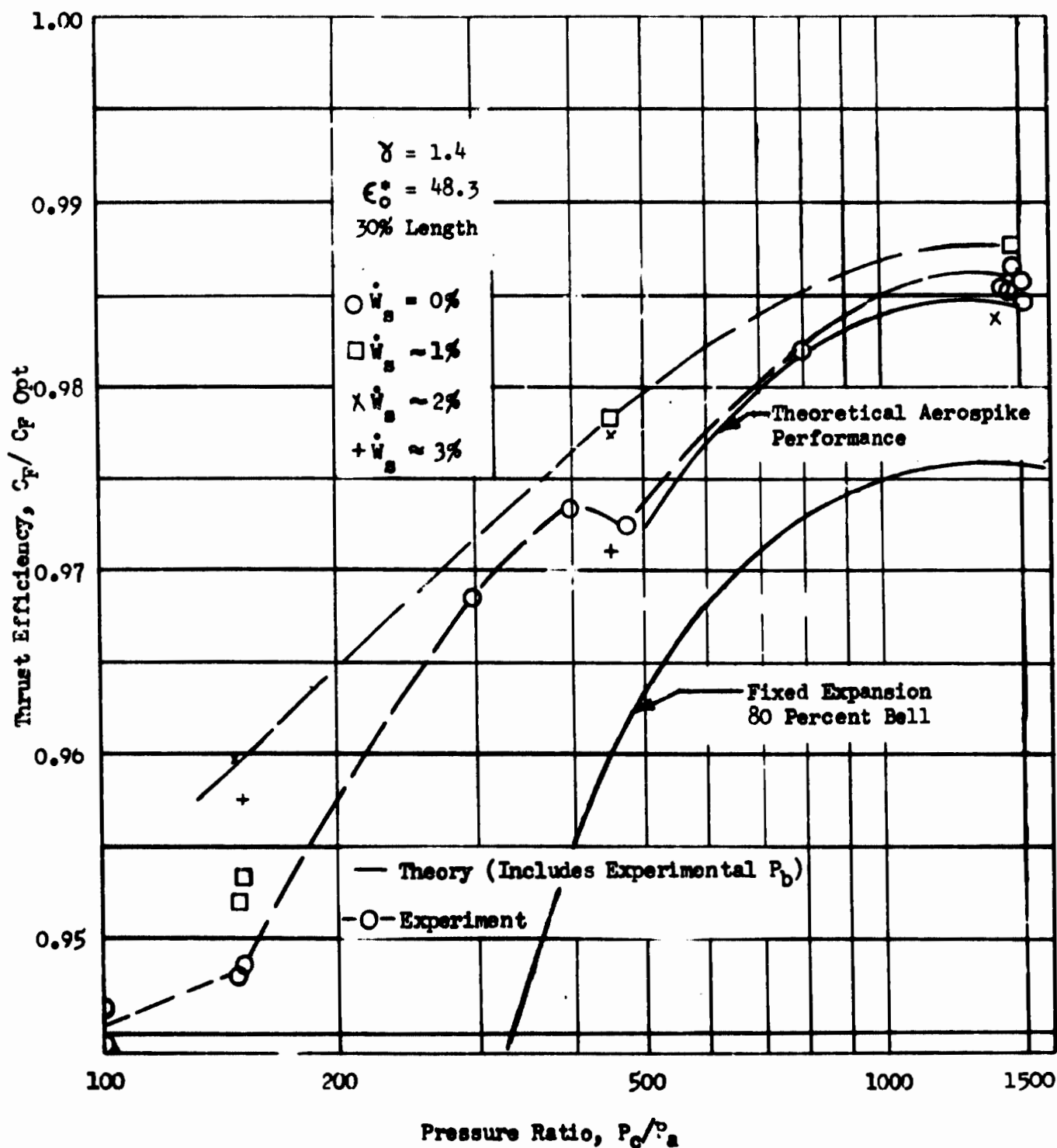


Fig. 70 Thrust Efficiency vs Pressure Ratio, Point Expansion Spike Nozzle

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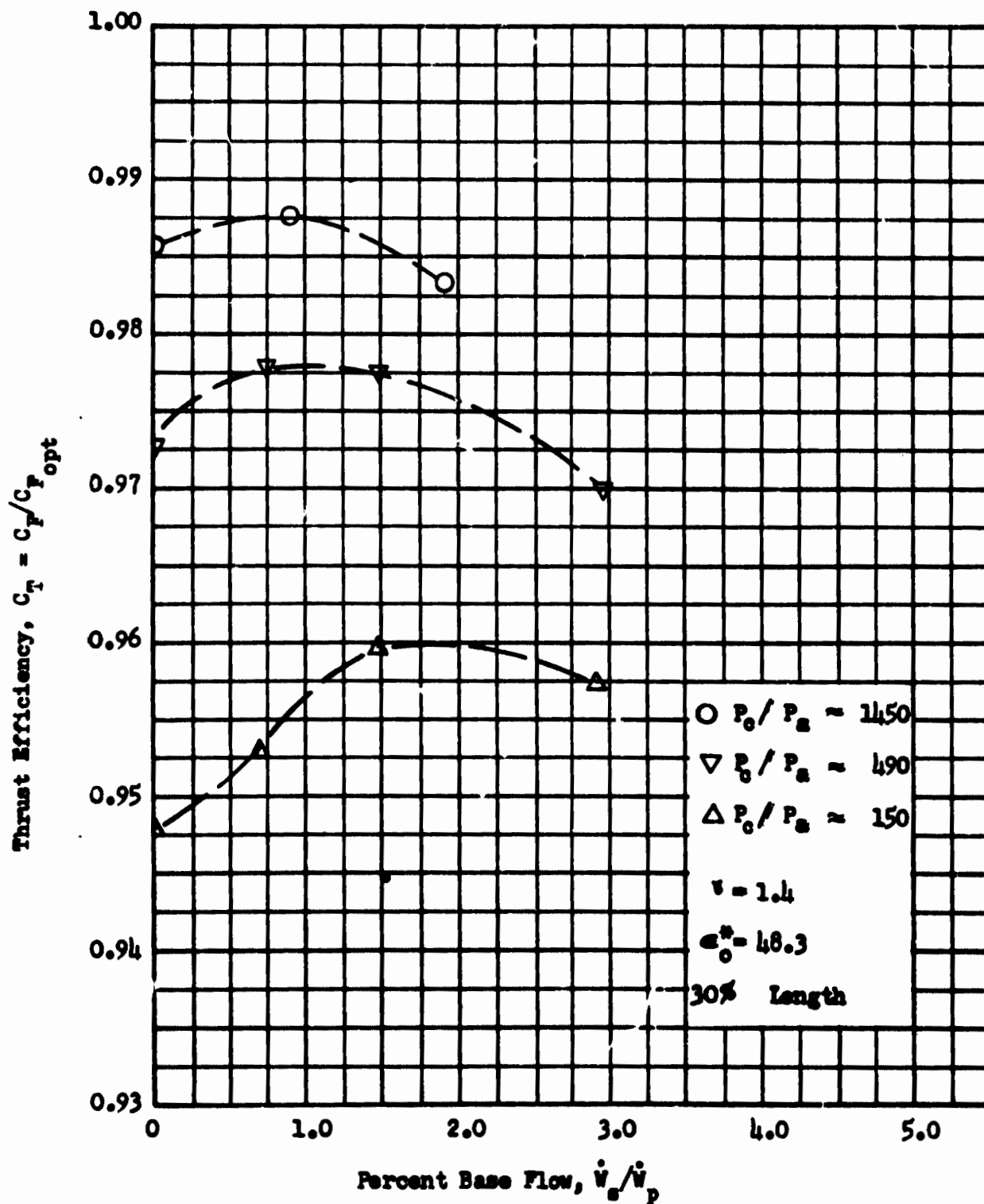


Fig. 71 Thrust Efficiency vs Percent Base Flow, Point Expansion Spike Nozzle

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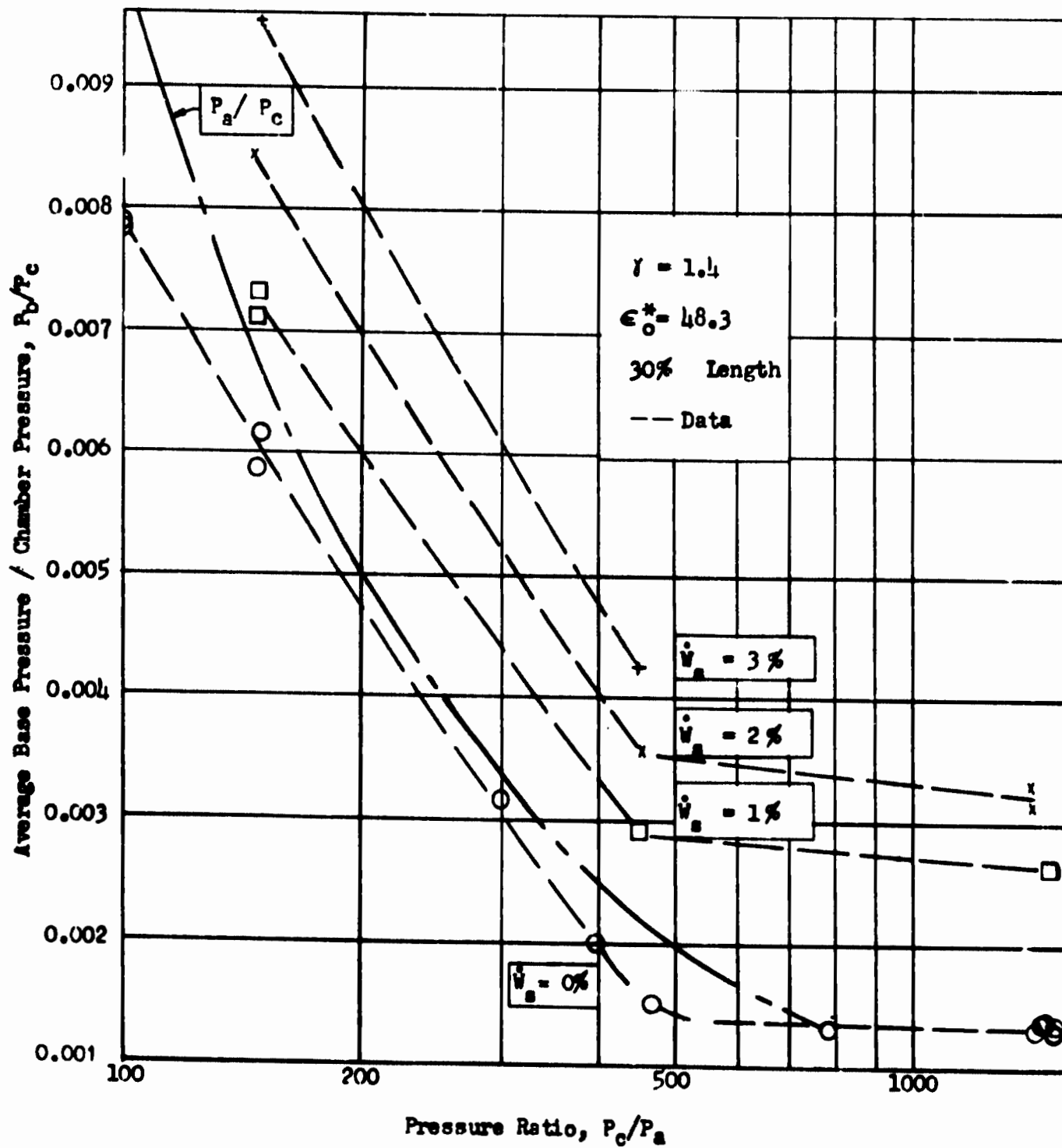


Fig. 72 Base Pressure vs Pressure Ratio for Point Expansion Spike Nozzle

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The performance of a fixed expansion, 80 percent length bell of 48.3 area ratio is shown for comparison in Fig. 70. The bell performance was computed using a nozzle vacuum efficiency of 98.65 percent and a constant drag loss equal to 1.0 percent of the theoretical vacuum thrust coefficient. These values were determined from bell nozzle theoretical efficiency curves and theoretical drag computations for a similar cold flow bell nozzle.

The efficiency of the 80 percent length bell nozzle is 97.6 percent at design pressure ratio compared to 98.8 percent for the 30 percent length aerospike. At a pressure ratio of 500 (36 percent of design pressure ratio) the bell nozzle efficiency is 96.3 percent compared to 98.0 percent for the aerospike. At a pressure ratio of 150 (11 percent of design pressure ratio) the fixed expansion bell efficiency is 86.4 percent compared to 96.0 percent for the aerospike.

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Using the method of characteristics for axially symmetric flow, the point expansion nozzle was analysed for primary flow field performance. The experimental base pressure performance contribution was then added to the inviscid performance. Shear stress and friction drag were calculated and the drag loss was subtracted from the inviscid theory. This resulted in the viscous theory curve shown in Fig. 70 which agrees very well with experimental results.

Experimental and theoretical contour pressure profiles are shown in Fig. 73 . Again, agreement is very good between theory and experiment. Recompression is shown to occur below a pressure ratio of 300.

Schlieren photographs for tests at both high and low pressure ratios with and without secondary flow are shown in Fig. 74 .

Shrouded Annular Model

Design expansion area ratio for the shrouded annular spike model was the same as the point expansion spike. As built and flow checked, the area ratio, ϵ_0^* , was 48.6. Efficiency for this model was, in general, 0.5 percent lower than for the point expansion model, although, since this model was designed, techniques of designing shrouded nozzles have improved and experience shows that it is possible to achieve shrouded nozzle performance comparable with point expansion nozzles.

At peak performance (Fig. 75) for no secondary flow the shrouded nozzle efficiency was 98.0 percent. Essentially no efficiency increase was noted (Fig. 76) with the addition of secondary flow at design pressure ratio.

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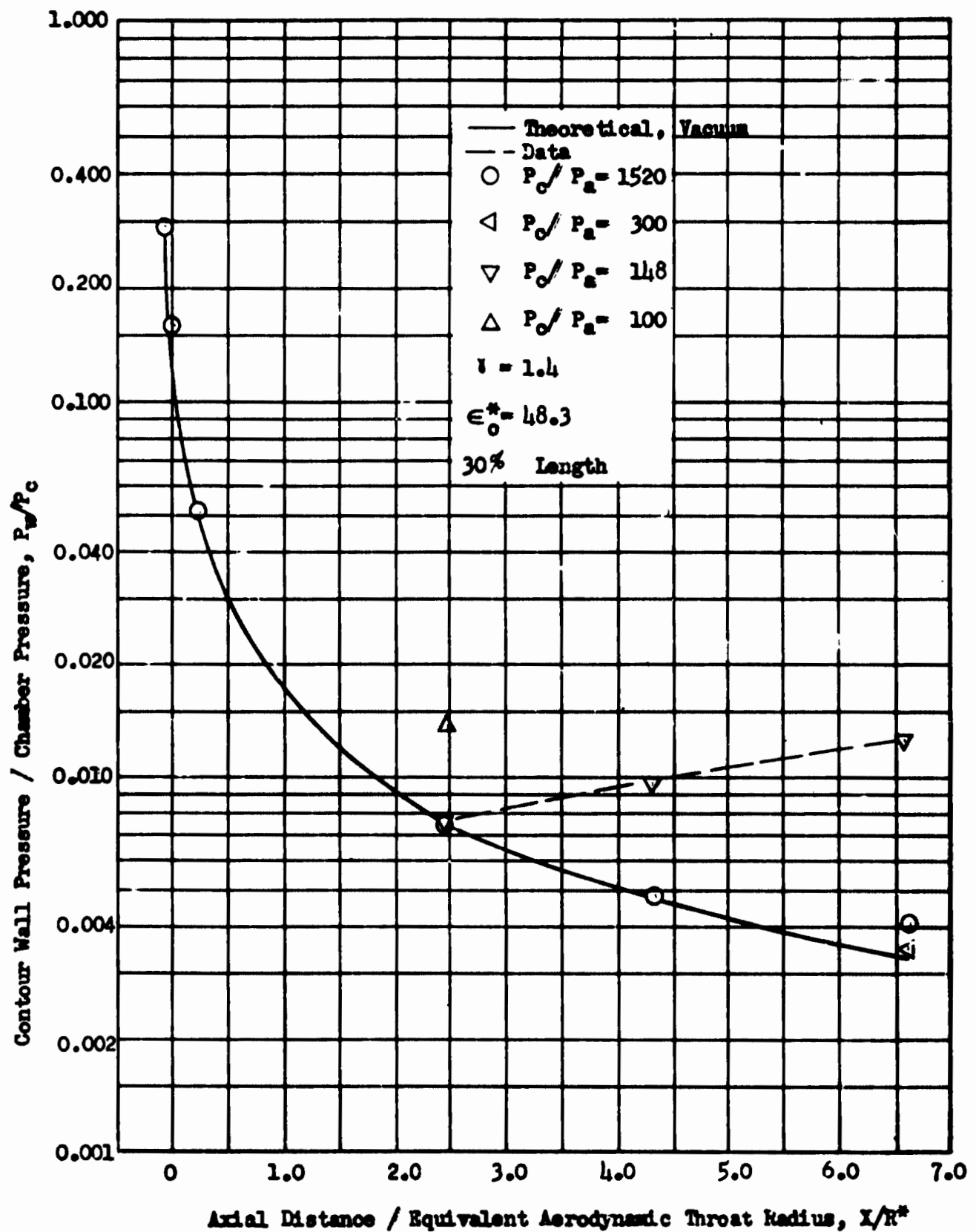
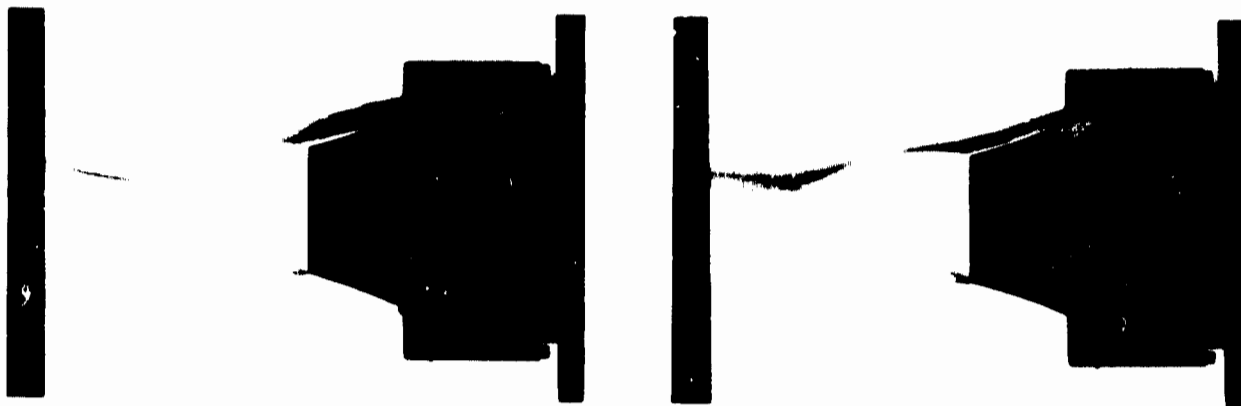


Fig. 73 Contour Pressure Profile, Point Expansion Spike Nozzle

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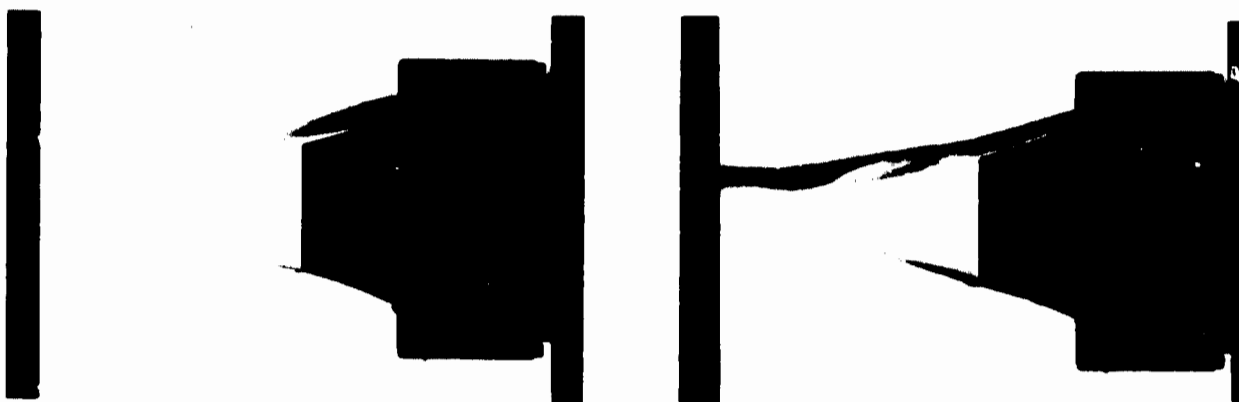


(a) $P_c/P_a = 1467$

$\dot{W}_s = 0\%$

(b) $P_c/P_a = 151$

$\dot{W}_s = 0\%$



(c) $P_c/P_a = 1412$

$\dot{W}_s = 2\%$

(d) $P_c/P_a = 147$

$\dot{W}_s = 2\%$

Fig. 74 Schlieren Photographs of Point
Expansion Model Spike Nozzle

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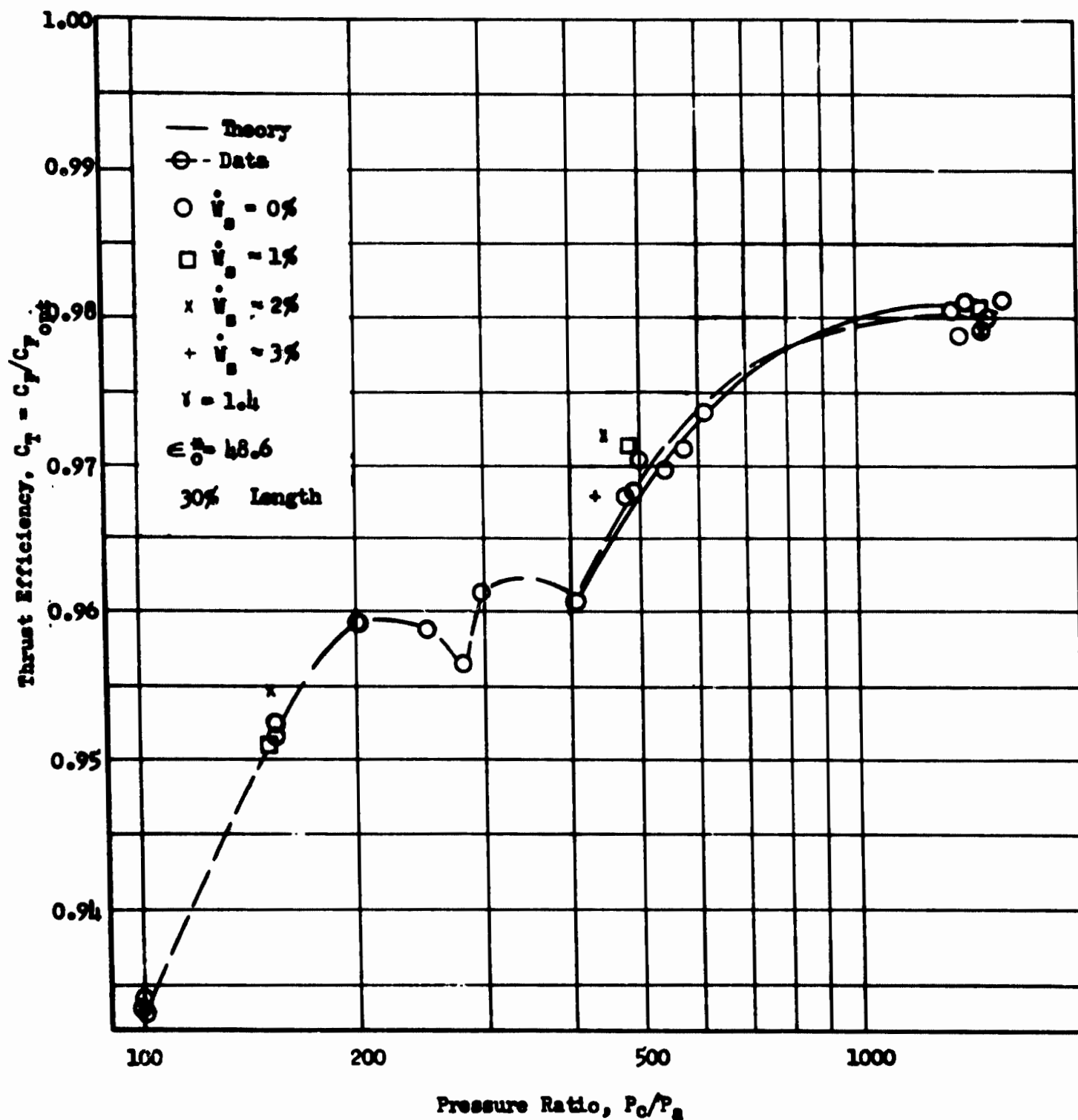


Fig. 75 Thrust Efficiency vs Pressure Ratio, Shrouded Spike Nozzle

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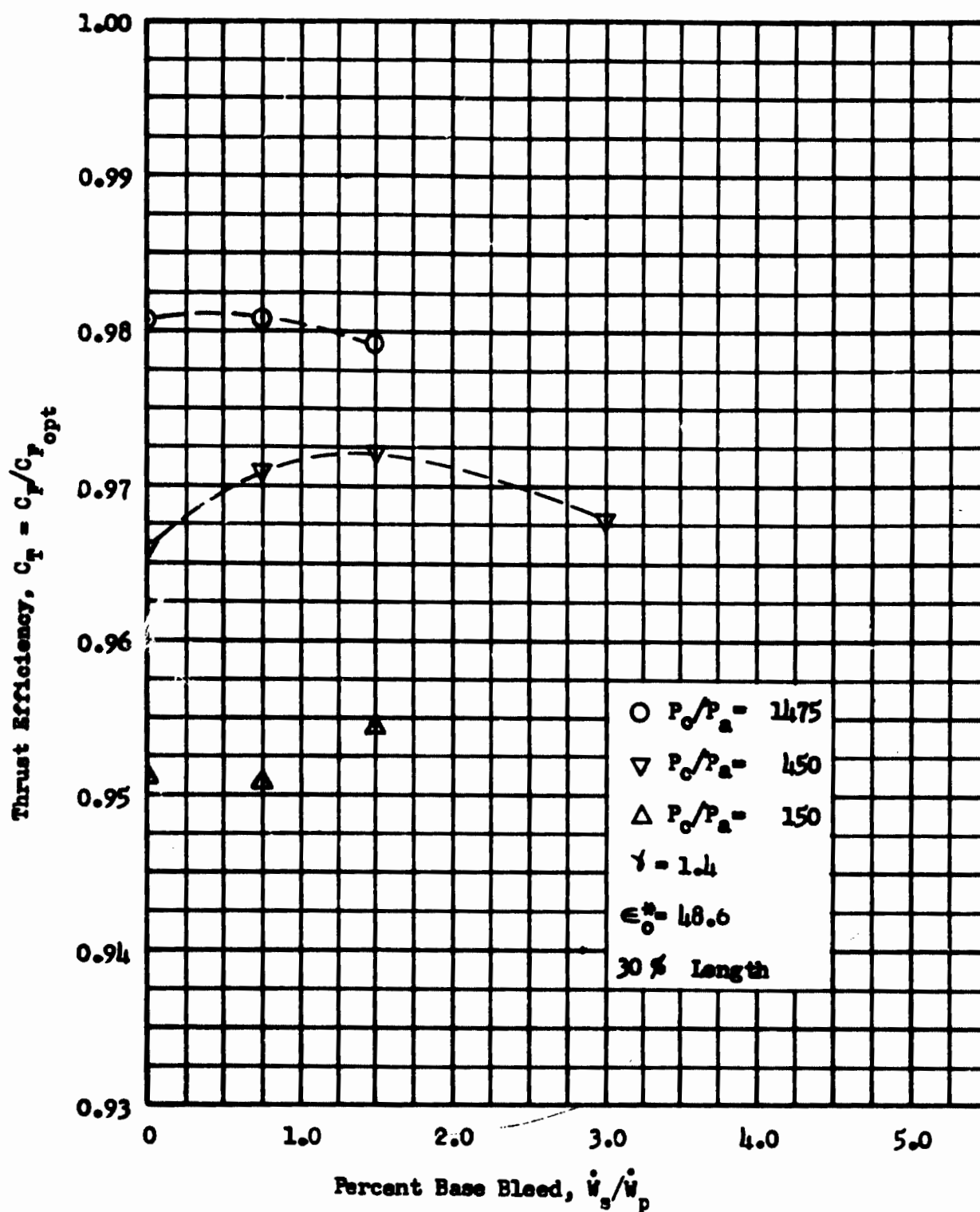


Fig. 76 Thrust Efficiency vs Percent Base Bleed, Shrouded Spike Nozzle

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Two dips in the performance curve can be observed; one at a pressure ratio of 400 and the second at a pressure ratio of approximately 290. The base pressure curve (Fig. 77) shows that the transition from closed to open wake occurred at a pressure ratio of 400. No unusual base pressure trends can be noted at a pressure ratio of 290. Therefore, this second dip must be caused by some other condition. At a pressure ratio of 290 the contour pressure profile (Fig. 78) is the same as for high pressure ratios. Shroud pressures (not shown) are also the same as for high pressure ratios. When the pressure ratio is reduced to 200 wall pressures at the end of the contour increase (Fig. 78) indicating either nozzle recompression or separation from the contour. In the characteristic solution to the primary flow field this pressure ratio (290) corresponds approximately to the pressure along the last characteristic line from the end of the shroud to the end of the contour. This suggests that below a pressure ratio of 290 recompression waves between the shroud and inner contour are causing an increase in contour pressure (down to a pressure ratio of 200) which is not completely offset by the increase in ambient pressure force in the opposite direction. Examination of the Schlieren photographs, Fig. 79 shows that the flow does not appear to be separating from the contour and compression waves are impinging on the contour at pressure ratios around 250.

Secondary base bleed was added near a pressure ratio of 400 (Fig. 76). At a pressure ratio of 450 performance increased from 96.6 percent at zero bleed to 97.2 percent at 1.5 percent bleed. At the low pressure ratio end ($P_o/P_a = 150$) of the performance curve, efficiency was increased from 95.1 percent to 95.5 percent with 1.5 percent bleed.

Theoretical performance (including drag losses) and wall pressure (vacuum) profiles agree very well with the data for this nozzle (Fig. 75 and 78).

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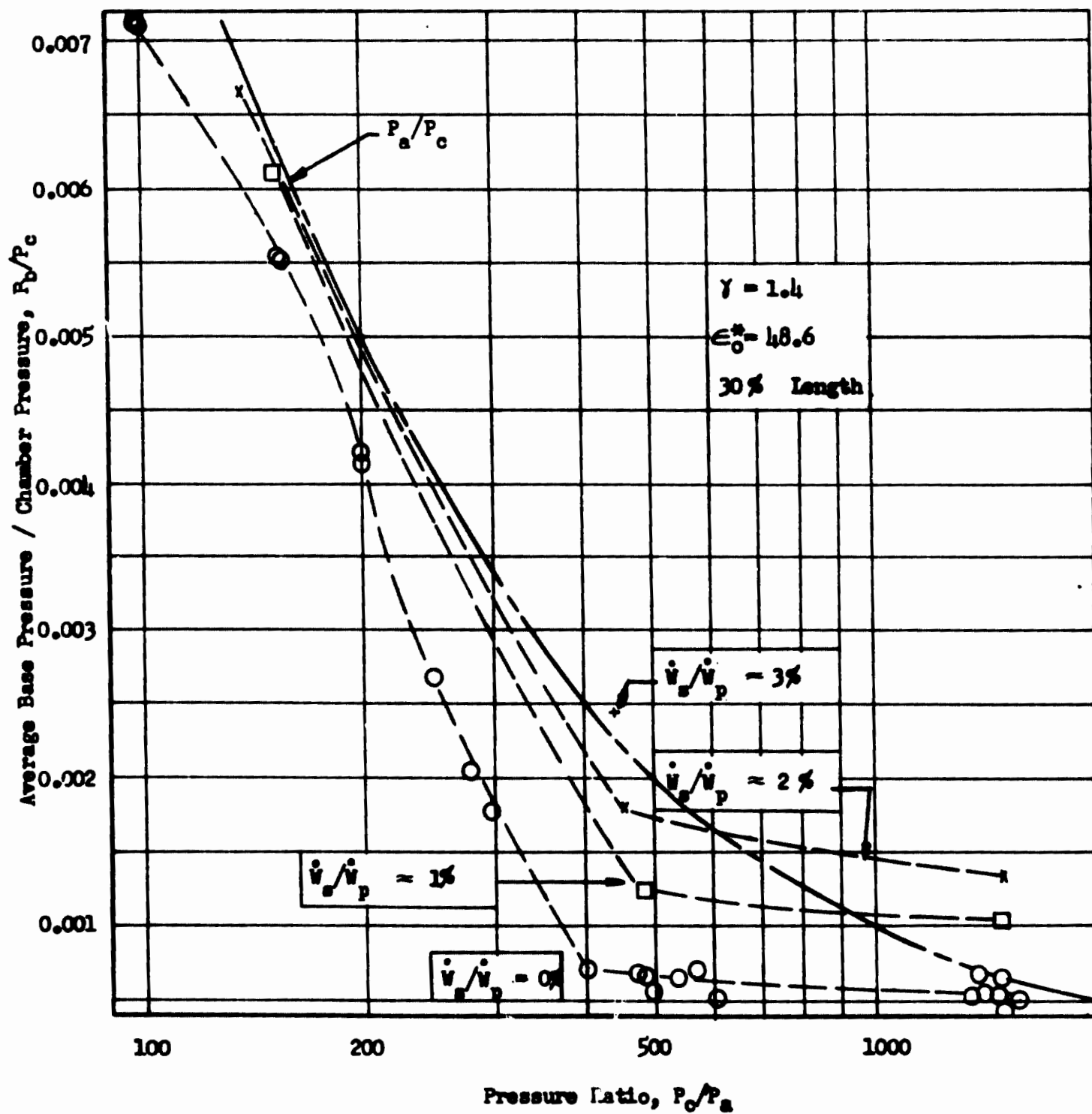


Fig. 77 Base Pressure vs Pressure Ratio for Shrouded Spike Nozzle

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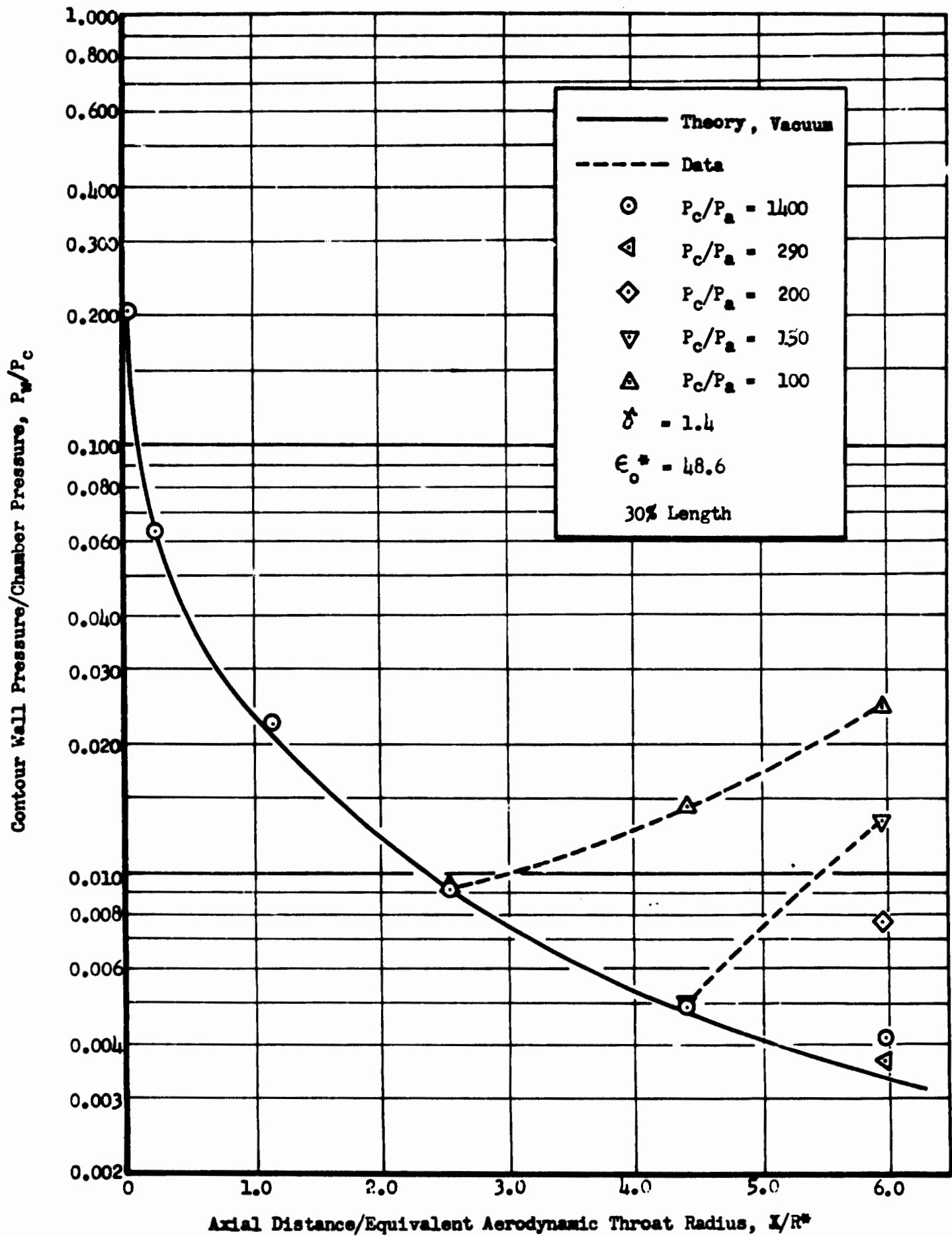
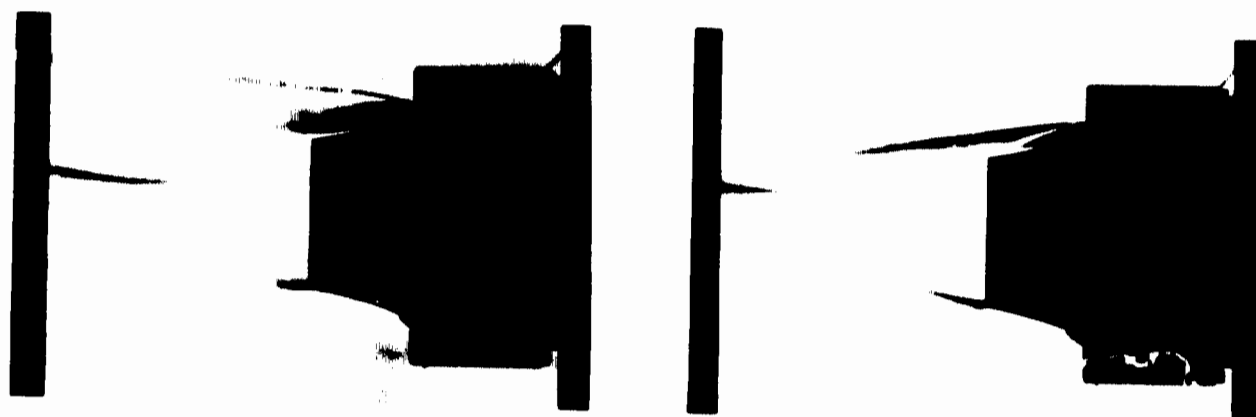


Fig. 78 Contour Pressure Profile, Shrouded Spike Nozzle.

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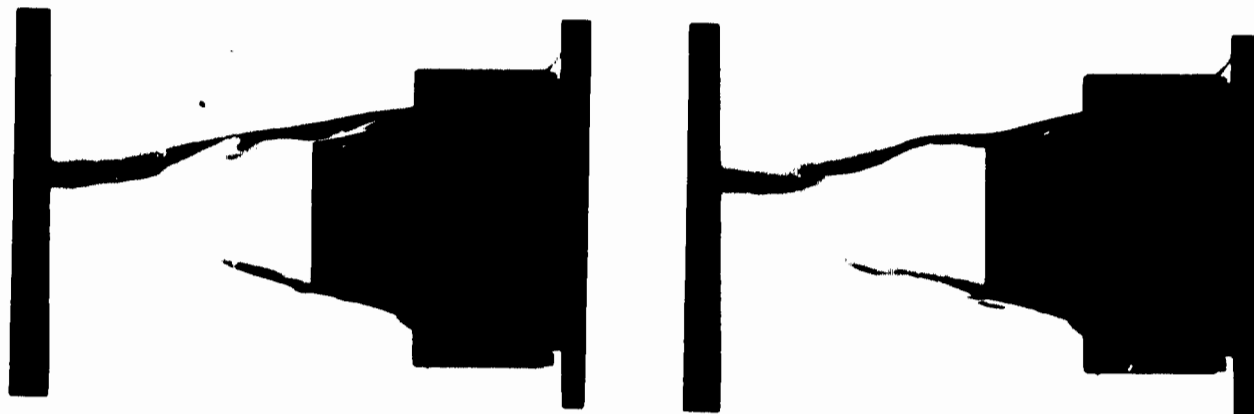


(a) $P_c/P_a = 1525$

$\dot{W}_s = 0\%$

(b) $P_c/P_a = 248$

$\dot{W}_s = 0\%$



(c) $P_c/P_a = 155$

$\dot{W}_s = 0\%$

(d) $P_c/P_a = 101$

$\dot{W}_s = 0\%$

Fig. 79 Schlieren Photographs of Shrouded Annular Spike Nozzle

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Multichamber Models

Although the performance of multichamber spike nozzles has previously been investigated in considerable detail, data are lacking for the effects of secondary gas flow on performance for this combustor nozzle configuration. The purpose of this test series was to obtain performance data for multichamber spikes with secondary flow. Secondary flow was introduced into both the centerbody region ($\dot{W}_g$) and the region between the individual chambers ($\dot{W}_{i.s.}$) in an effort to obtain maximum overall performance. The principal test objectives are as follows:

1. Determine the maximum performance achievable through the use of secondary flow with the multichamber configurations and compare the data with the data from the reference models.
2. Determine whether secondary flow alters the relative effects on performance of the multichamber variables such as nozzle length, spacing, primary chamber area ratio and number of chambers.
3. Record and evaluate intersegmental and centerbody base pressures with and without interchamber and base bleed.
4. Determine the effect of interchamber bleed on the nozzle pressure profiles along the primary chamber centerline and between chambers.
5. Perform tests with one nozzle of the cluster plugged to simulate engine-out performance.

A total of 141 tests were accomplished with the multichamber configurations. The eight touching chamber models (Models III-9 and III-10) were tested over a pressure ratio range of from 100 to 1500 (design pressure ratio for $\epsilon_{CL} = 50$) with intersegmental and base bleed rates

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from 0 to 3 percent of the primary flowrate. Engine-out tests were performed by plugging one of the nozzles of Model III-9. Several tests were performed on a stripped down version (Model III-8). The cluster outer shroud and the spike contour (see Fig.56 p.93) were removed to obtain this configuration which simulated engines extending considerably beyond a vehicle external fairing and tank bottom.

Model III-11 (Fig.54 p.91) consists of eight individual 80-percent length bell nozzles with an area ratio of 20.7. The lower individual nozzle area ratio (compared to $\epsilon_M = 30.2$ for Models III-9 and III-10) for this eight chamber configuration results in a spacing between the module exits. The distance between module exits (δ) is 0.31 times the module exit diameter D_e . This model was tested over the same range of pressure ratios, intermodule and centerbody bleed flowrates that were used with the eight touching chamber configurations. However, testing with intersegmental bleed was limited to design pressure ratio.

Model III-12 consists of 16 touching chambers of ϵ_M equal to 20.7 placed around a central spike, giving an overall 30 percent length nozzle with a cluster area ratio of 50. This model is shown installed in the Rocket Nozzle Test Facility in Fig. 80. Tests were conducted with this model over a pressure ratio range from 100 to 1800 with intersegmental and centerbody bleed rates to 3 percent of primary flow.

To see if an improvement in performance with intersegmental bleed could be obtained, the intersegmental area in the region between the tangent points of the touching chambers and the outer shroud was blocked off using the scalloped plate shown in Fig.81. The scalloped plate served to isolate the interchamber region from ambient conditions. Tests were

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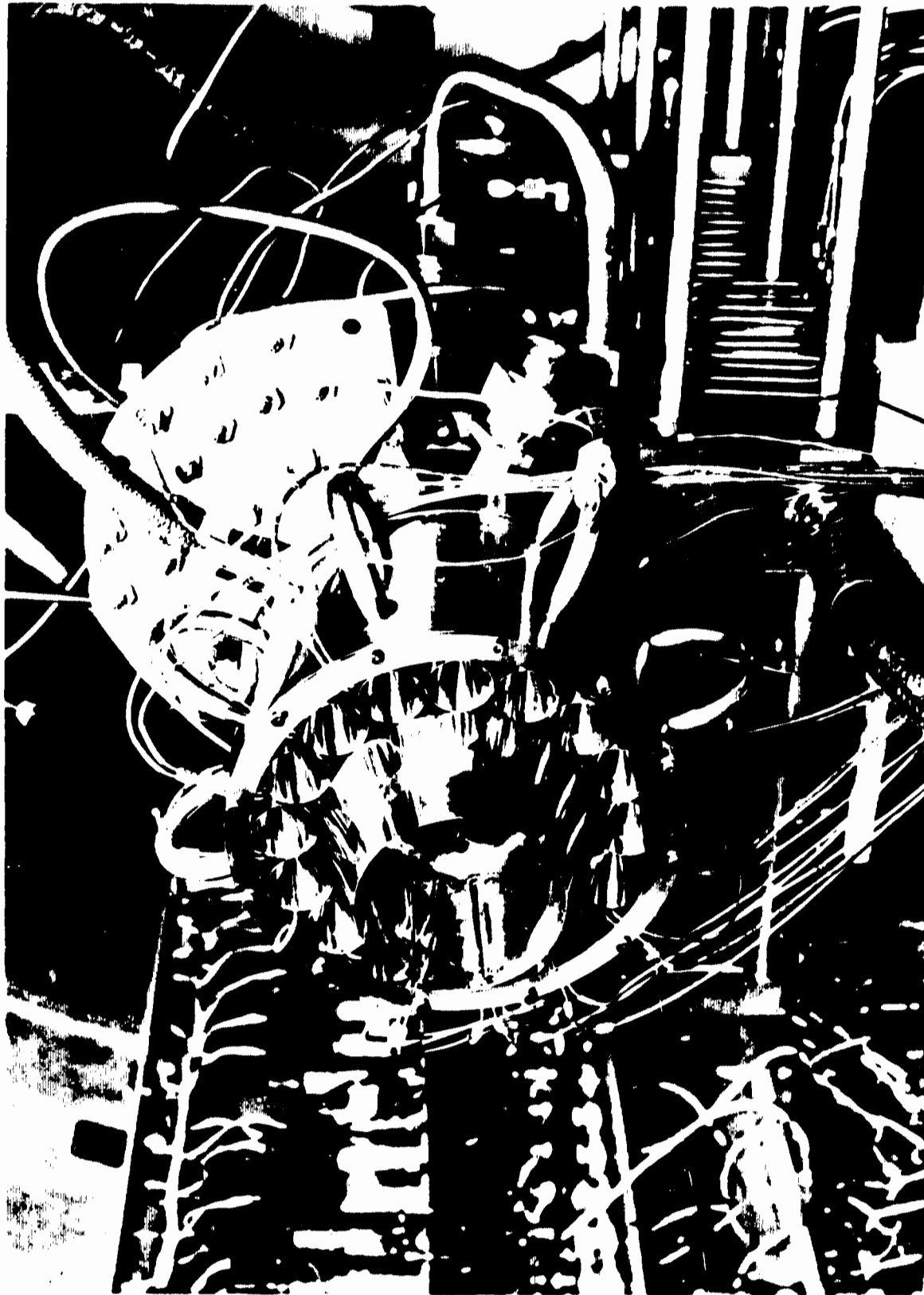


Fig.80 Sixteen Module Multichamber Installation in Rocket Nozzle Test Facility, $C_{QL} = 50$

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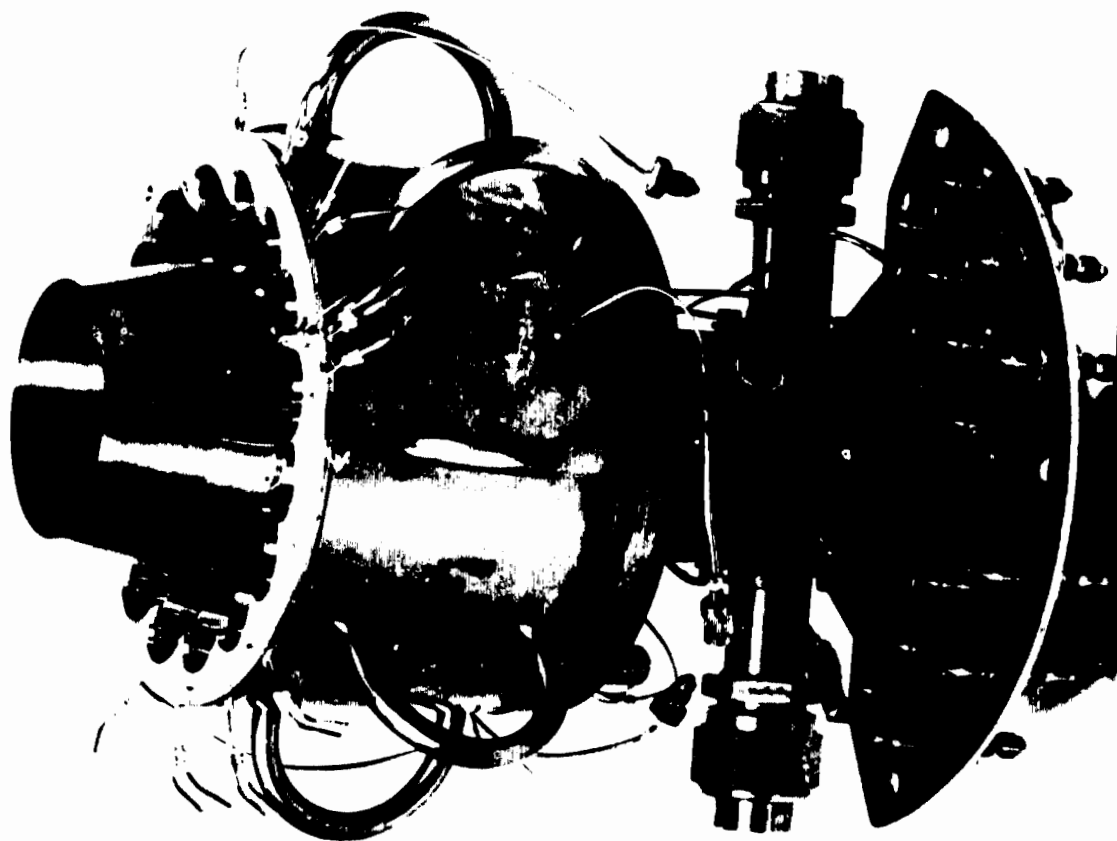


Fig. 81 Sixteen Chamber Assembly with Interchamber Scallop

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conducted with this scalloped 16-chamber configuration over a pressure ratio range from 150 to 1400 with interchamber and centerbody bleed rates to 4 percent of primary flow.

8 Touching Chambers - No Spike

The first of the multichambers tested was model III-9, 8 touching chambers with no spike. Figure 82 shows the experimental performance for this model. Peak performance was 96.7 percent at a pressure ratio of 1400 although the performance curve is relatively flat from pressure ratios of 600 to 1400. Base bleed was introduced into the base region via a radial-bleed orifice deep in the base cavity (see Fig. 51). Bleed rates were varied from 0 to 1.5 percent of primary flow rate. As shown in Fig. 83 no improvement in performance was obtained with base bleed at the high pressure ratio.

A performance curve dip occurs at a pressure ratio of 280 which is also the corresponding break in the base pressure curve (Fig. 84), indicating the wake closing point in the base region. Performance with no secondary bleed at this pressure ratio was 94.2 percent. Figure 83 shows a performance increase to 94.8 with 0.7 percent secondary bleed.

A sharp point of inflection in the base pressure curve for zero base bleed is observed at a pressure ratio of 240. A similar point of inflection is noted in the pressure curve for tap 3 (Fig. 85) at a pressure ratio of 240. This tap is located on the cylindrical centerbody which forms the inner envelope of the modules and is midway between the exits of adjacent modules. Thus it records the pressure which is acting on the jets of adjacent nozzles.

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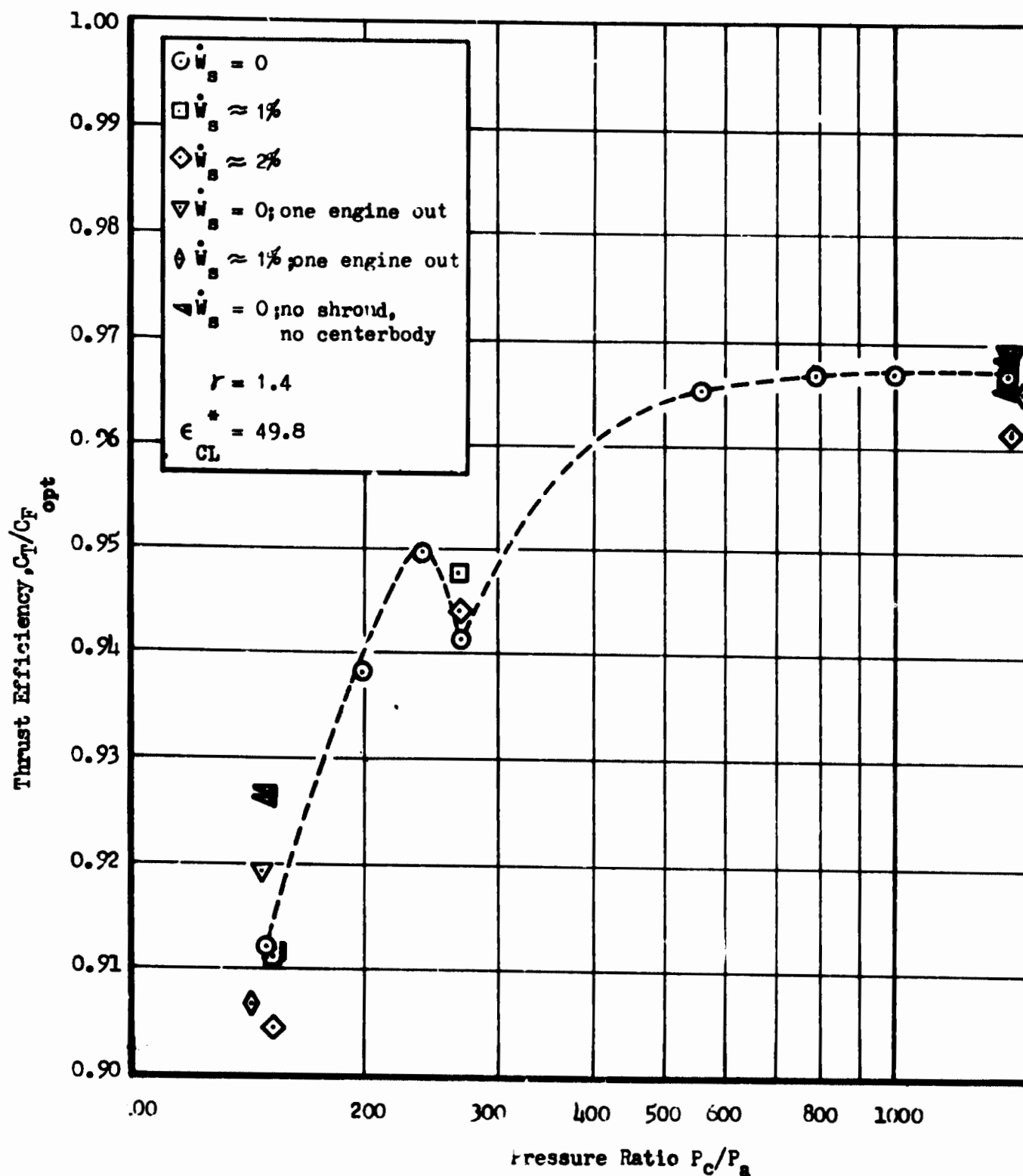


Fig. 82 Thrust Efficiency vs Pressure Ratio, 6 Module Touching Multichamber, No Spike

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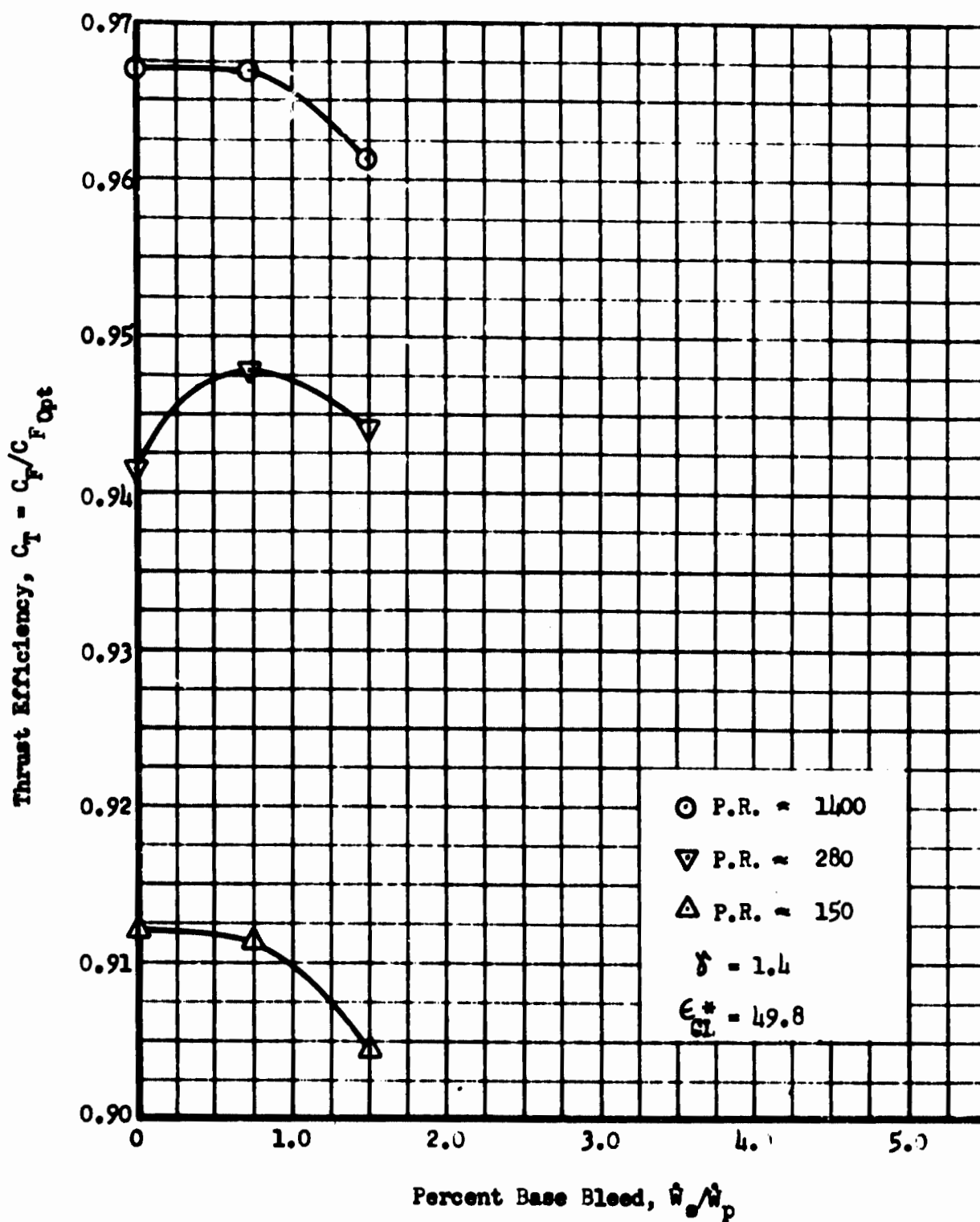


Fig. 83 Thrust Efficiency vs Percent Base Bleed, 8 Module Touching Multichamber, No Spike

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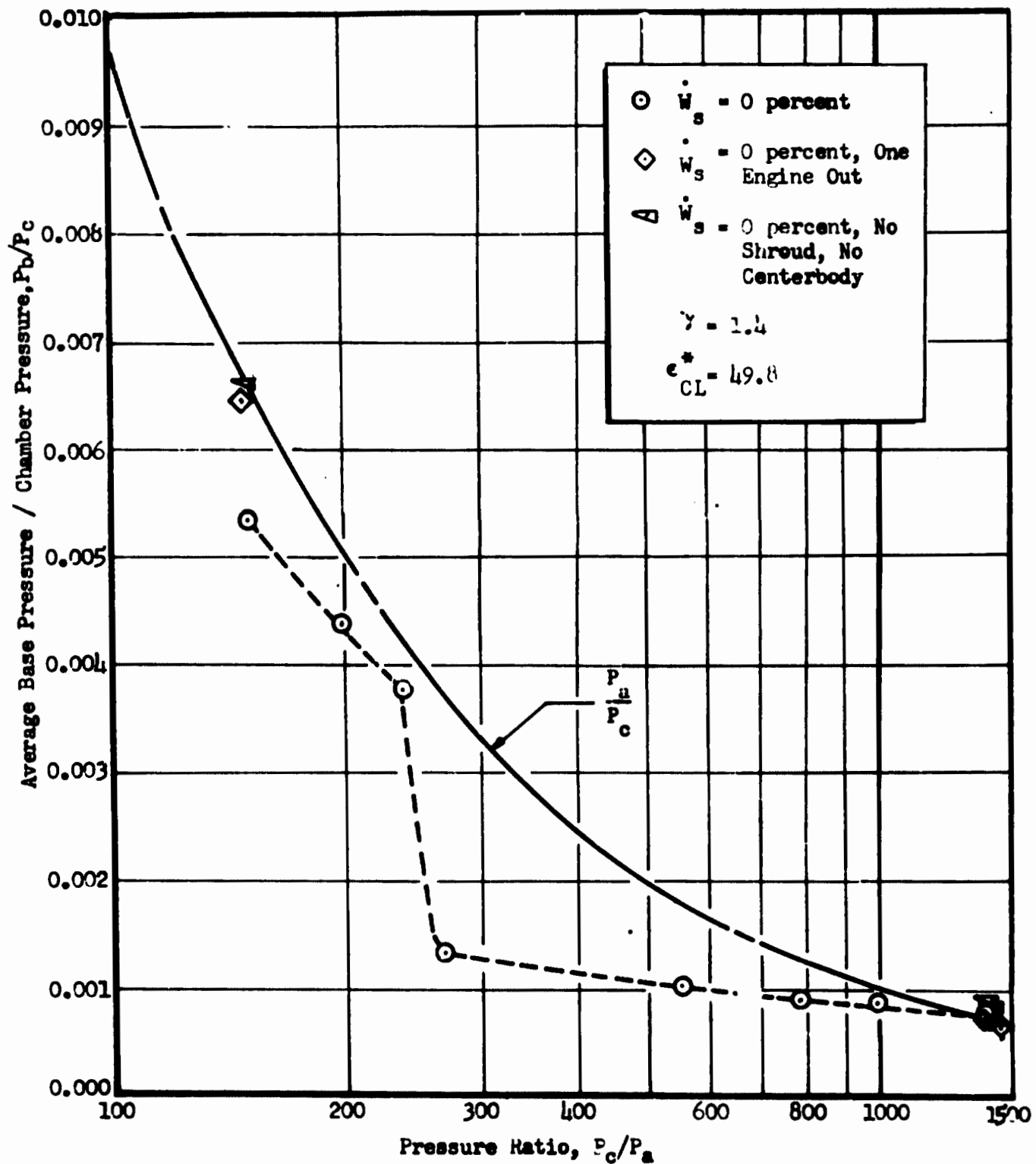


Figure 84 . Base Pressure vs Pressure Ratio, 8 Module Touching Multichamber, No Spike

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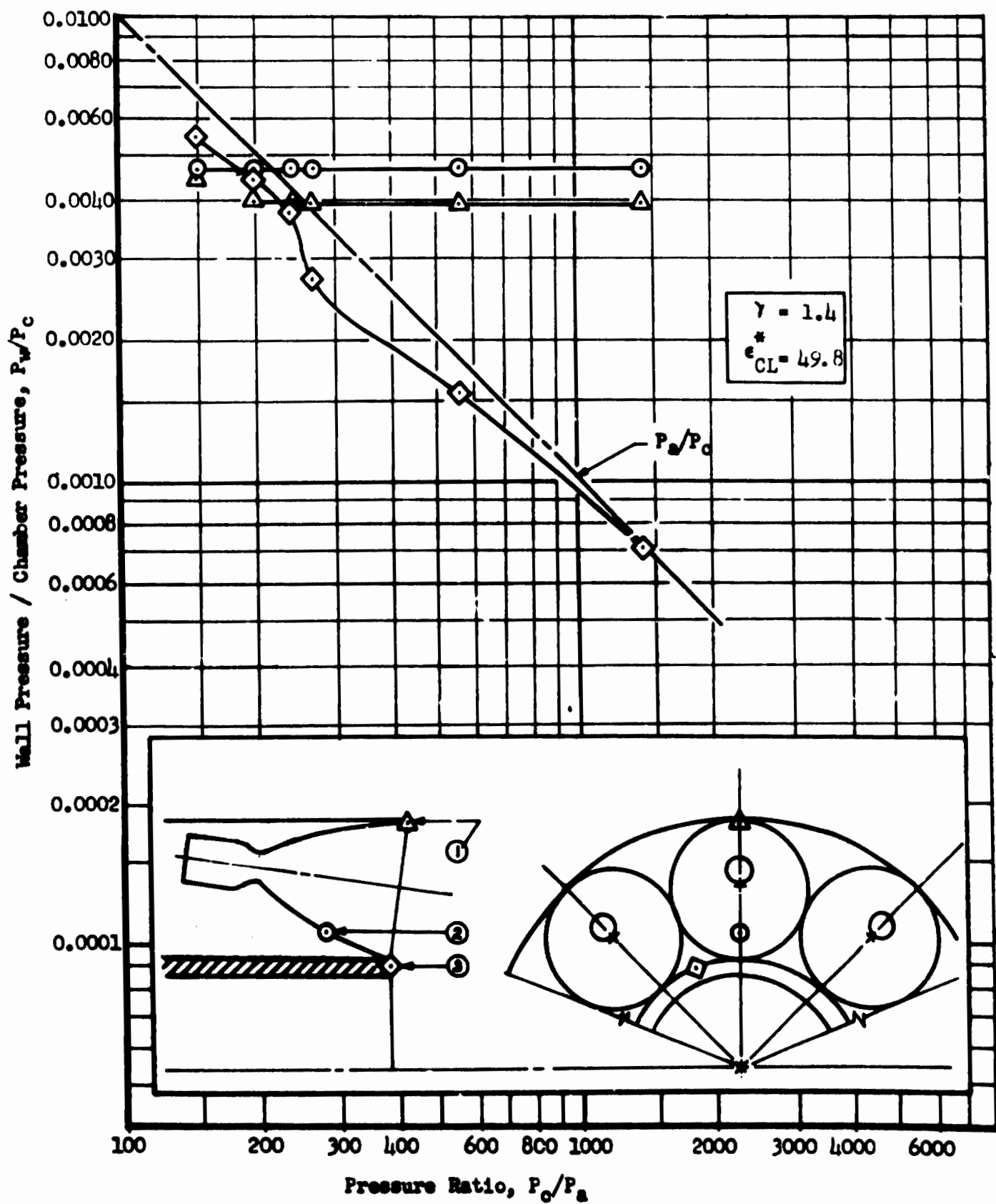


Figure 85 . Wall Pressure vs Pressure Ratio, 8 Module Touching Multichamber No Spike

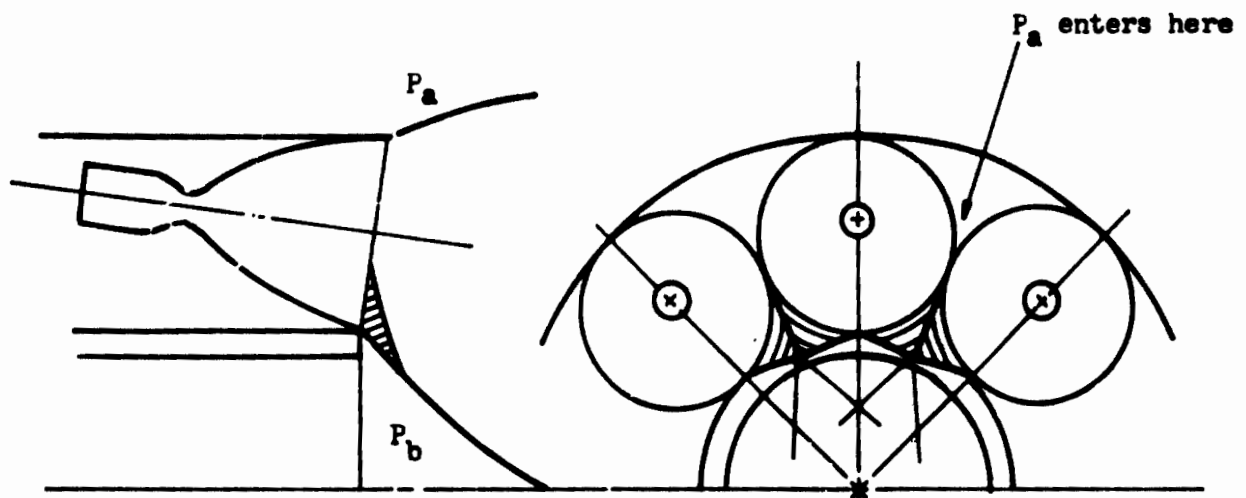
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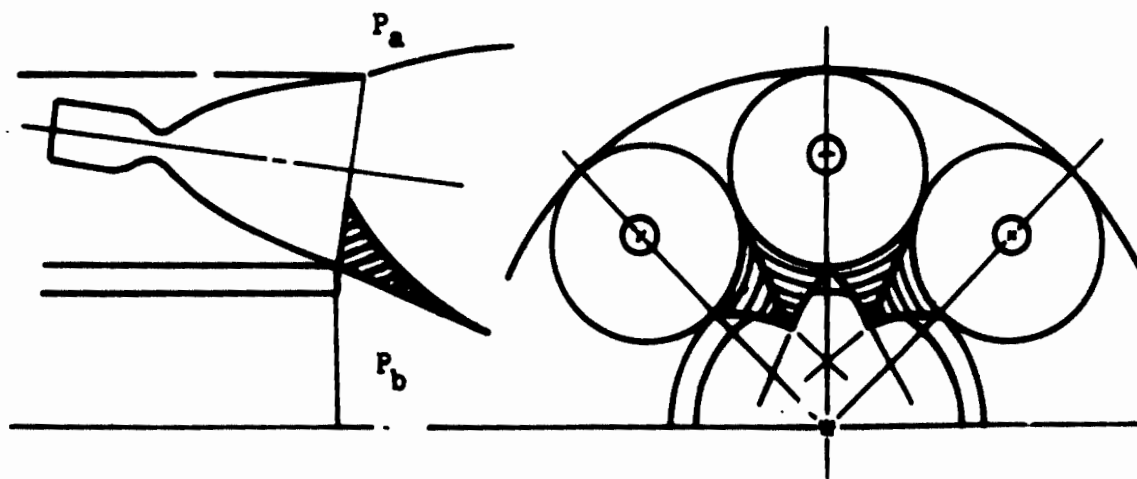
Noting the trends in base pressure and pressure at tap 3, the following postulation is made to explain the base pressure trends of Fig. 84 for the zero base flow case. When the nozzle is operating at a high pressure ratio (above 300) the module jets will impinge on each other and coalesce into a common (but complex) flow field. This impingement pattern terminates close to the module exits exposing a small flow area for ambient air to enter the base region from between the modules (see Fig. 86a). At a pressure ratio of 1400, $P_a = P_b$ (see Fig. 84) and no net flow occurs into the base. As P_c/P_a is decreased, P_a rises more rapidly than P_b and flow into the base region results. When P_c/P_a reaches 500, $P_b/P_a \approx 0.5$ and flow into the base should be choked.

Further increases in P_a can not be communicated to P_b , however flow into the base will increase in proportion to P_a . Somewhere between a pressure ratio of 280 and 240 the increase in base bleed from the ambient causes the wake to open resulting in a steep rise in P_b because; 1) open wake flow allows better communication of ambient pressure to the base and 2) the module wakes coalesce much further downstream, as shown in Fig. 86 b and allow a larger area for ambient flow to bleed into the base region. The pressure ratio P_b/P_a is now much greater than 0.5 and choking of the flow into the base does not occur. This allows P_b to closely follow P_a (see Fig. 84 for $P_c/P_a < 240$).

At a pressure ratio of 150 the performance with no secondary flow was 91.2 percent and showed no increase with the addition of secondary flow (see Fig. 83). The pressure profile curve of Fig. 85 shows a rising pressure near the module exit, indicating flow separation from the module.



a) Module Jets Coalescing at High Pressure Ratio



b) Module Jets Coalescing at Intermediate Pressure Ratio

Fig. 86 Module Jet Structure, 8 Modules
Touching Multichamber, No Spike

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In the closed wake regime the base pressure is not as constant as in the nozzles with spike extensions. This is most likely due to the fact that the base region is never completely isolated from the ambient in this nozzle. Ambient pressure is felt from the region behind the modules through the intermodule wakes where the base can be communicated to the ambient.

Base bleed had very little beneficial effect on this model. Essentially no increase in performance was noted at design pressure ratio or at low pressure ratios for any bleed rates. Small gains were noted at the curve dip point.

Engine-Out Tests

Flow through one chamber of Model III-9 was stopped by inserting a plug in the throat of the chamber. Surprisingly no decrement in performance was noted over the symmetrically flowing case with or without secondary flow (see Fig. 82). In fact at a pressure ratio of 150 a small increase (approximately 0.8 percent) in performance was noted for the no bleed case. Again, this is likely due to the fact that with one engine off, ambient was allowed to communicate more readily with the base. This is verified by the base pressure curve, Fig. 84 , which shows an increase in base pressure for the engine out, compared to the symmetrically flowing case, especially at low pressure ratios. At a pressure ratio of 1400, performance and base pressure were approximately the same with one engine out as with no engines out.

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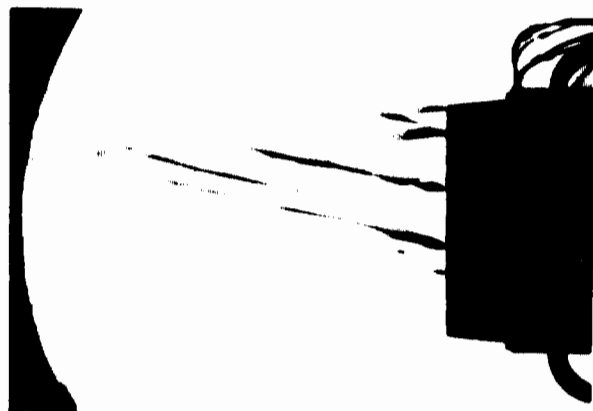
Stripped Model

A version of Model III-9 was tested with no centerbody duct or outer cluster shroud (see Fig. 86). This was called Model III-8.

Essentially this was simply an open cluster of 8 engines. Referring to Fig. 82 , performance at high pressure ratios was slightly lowered but at low pressure ratio, performance was increased about 1.0 percent due to higher overall base and intermodule pressures at zero secondary flow (see Fig. 84).

Schlieren photographs of Models III-8 and III-9 are shown in Fig. 87 .

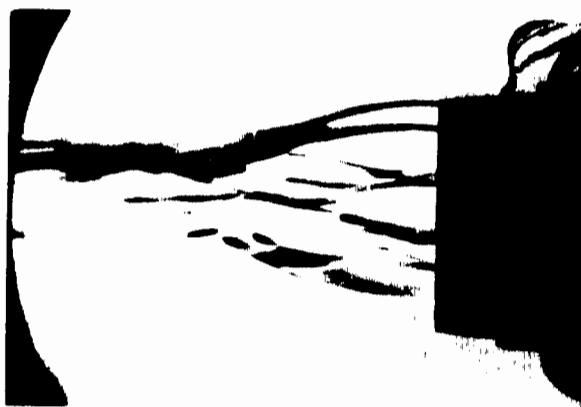
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(a) Model III-9

$$P_c/P_a = 1467$$

$$\dot{W}_s = 0\%$$



(b) Model III-9

$$P_c/P_a = 249$$

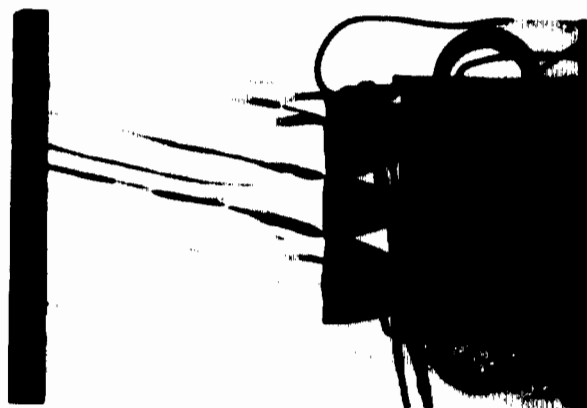
$$\dot{W}_s = 0\%$$



(c) Model III-9

$$P_c/P_a = 150$$

$$\dot{W}_s = 0\%$$



(d) Model III-8

$$P_c/P_a = 1387$$

$$\dot{W}_s = 0\%$$

Fig. 87 Schlieren Photographs for 8 Module
Touching Multichamber, No Spike

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8 Modules Touching With Spike Centerbody

Model III-10, Fig. 53, has 8 modules touching with a spike centerbody extending the nozzle length, L_N , to 30 percent of a 15 degree cone of $\epsilon = 50$. The nominal cluster area ratio is 50 and the model is essentially model III-9 with the spike replacing the short cylindrical centerbody.

This model has provisions for bleeding flow into the spaces between the modules (intersegmental bleed, $\dot{W}_{i.s.}$) in addition to base bleed, $\dot{W}_g$. With the combination of intersegmental bleed and base bleed at various bleed rates, a variety of possible combinations of $\dot{W}_{i.s.}$ and $\dot{W}_g$ could be used. However, a systematic approach to the testing can reduce the number of tests required to obtain significant data. The approach used was to first optimize the intersegmental bleed at zero base bleed and then, using the optimum $\dot{W}_{i.s.}$ optimize the base bleed. As it turned out the best nozzle performance was obtained with $\dot{W}_{i.s.} = 0$. An explanation will be given for this result later in this section.

Referring to Fig. 88 and the data in Appendix 3, the performance of this nozzle is shown for a pressure ratio range from 150 to 8000. At zero intersegmental and base bleed rates the performance reached a maximum value of 97.1 percent at a pressure ratio of 1450. Referring to Fig. 89 it can be seen that the addition of either intersegmental or base bleed did not increase performance at high pressure ratios. Examination of the base pressure curve, Fig. 90, shows that intersegmental bleed does not improve the base pressures at high pressure ratios. While introduction of intersegmental bleed increased the intersegmental pressure (see data in Appendix 3), the resulting increase in thrust for the additional mass flow was low, causing a drop in overall efficiency.

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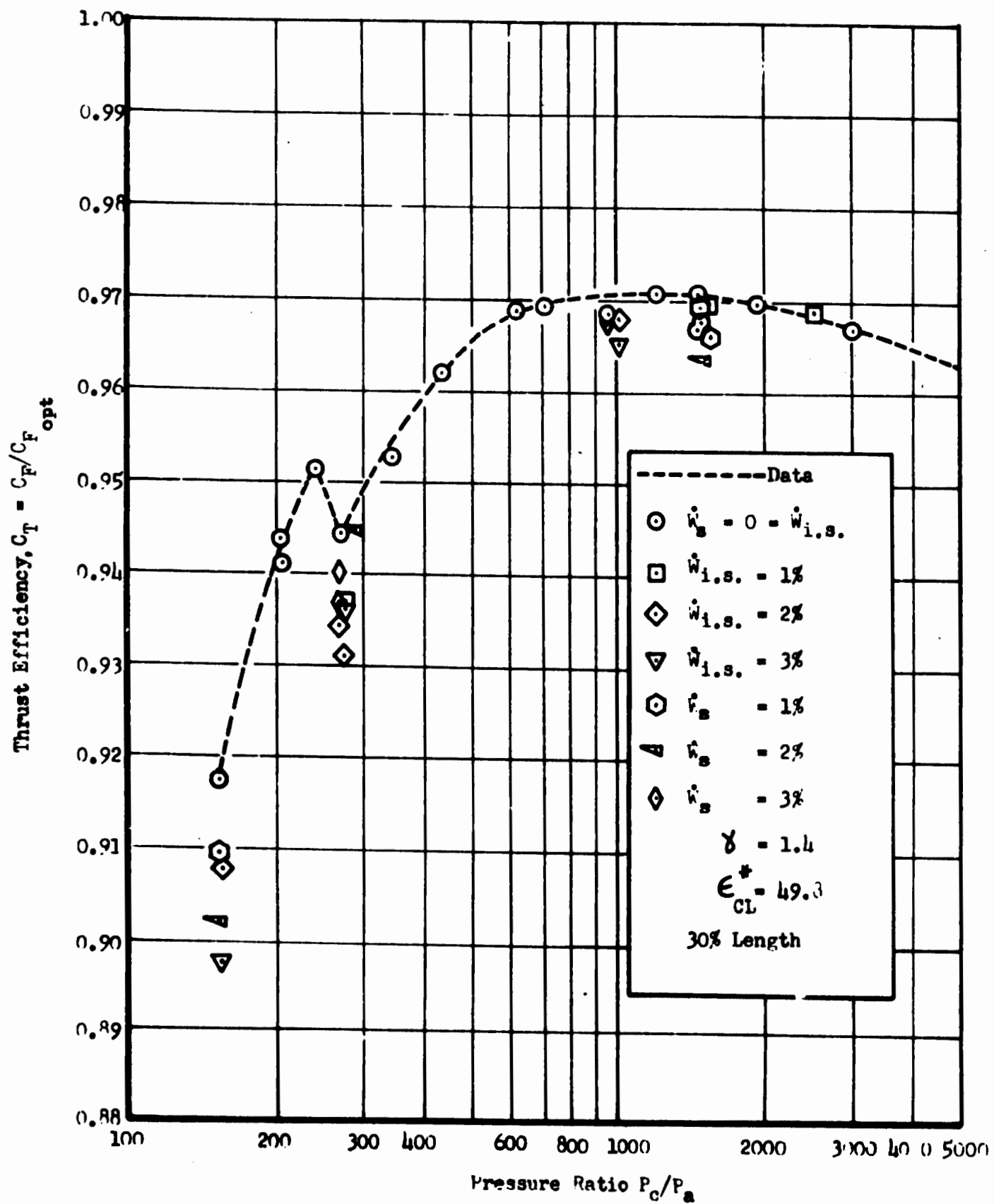


Fig. 88 Thrust Efficiency vs Pressure Ratio, 8 Modules Touching Multichamber, 30 Percent Length

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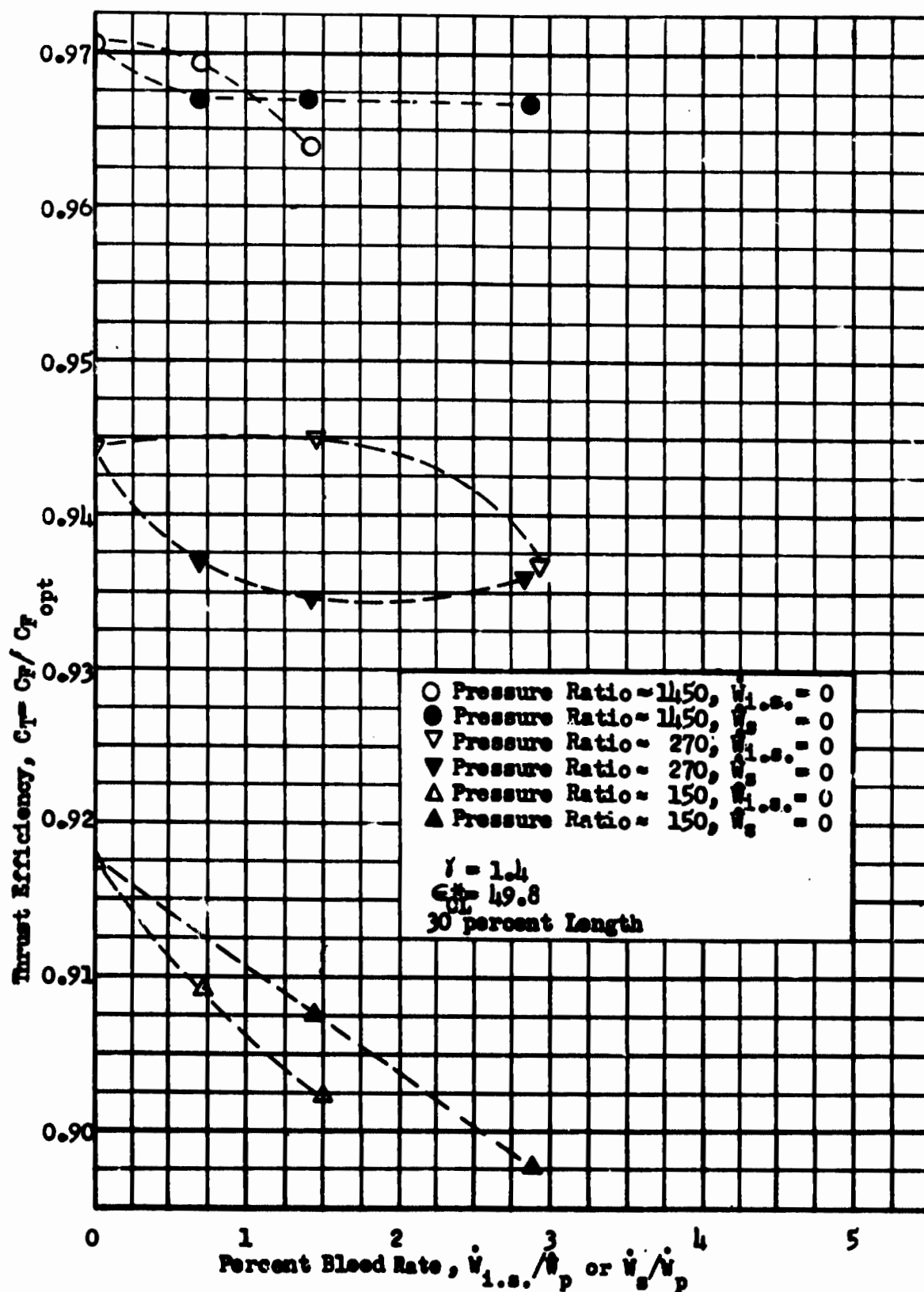


Fig. 89 Thrust Efficiency vs Bleed Rate, 8 Module Touching Multichamber, 30 percent Length

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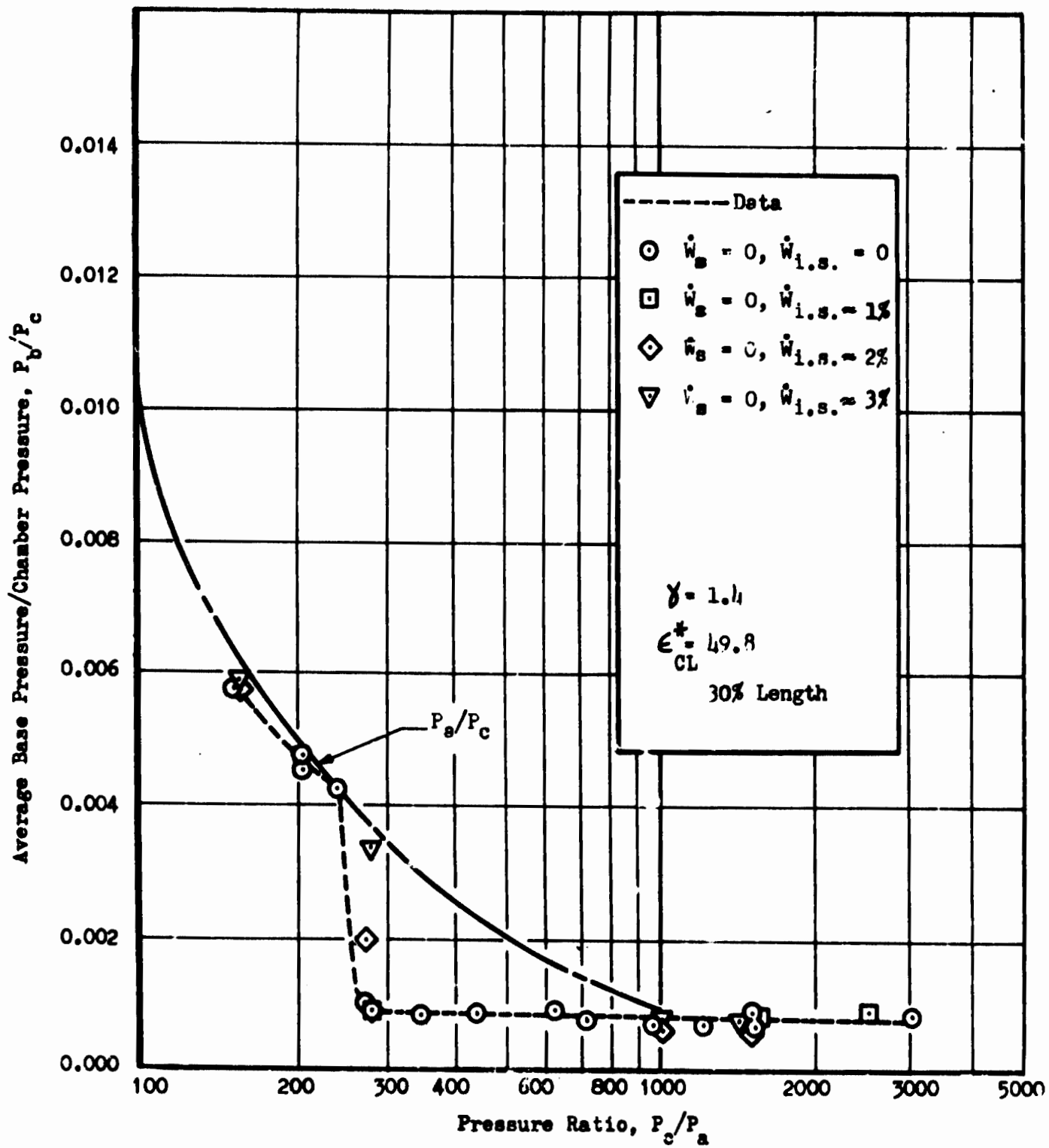


Figure 90 Base Pressure vs Pressure Ratio, 8 Modules Touching Multichamber, 30 Percent Length

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Bleed addition apparently causes the following phenomenon to occur: Referring to the efficiency vs base bleed curve (Fig. 71) for the point expansion annular nozzle, it is worth noting that for small bleed rates, base pressures and nozzle efficiencies increase. However, for larger bleed rates the efficiencies decrease. These are known as the small bleed and large bleed regimes of the base flow. It is also known that mass bleed can be replaced by an equivalent boundary layer or momentum thickness in the approach section. Two reasons can be given for the formation of a large momentum thickness in the multi-chamber nozzle. First, a series of shocks are caused by the coalescing of the primary flow fields from the modules. The action of these shocks intercepting the contour may well cause a thickening of the boundary layer and an increase in the momentum thickness along the contour. Second, bleed from the spaces between the modules can easily be entrained in the boundary layer along the contour, whether or not intermodule bleed is introduced. This is because of the large openings to the ambient behind and above the module. Both conditions may cause a considerable increase in the equivalent momentum thickness, along the contour and thus at the end of the centerbody, over the annular nozzle case.

Referring to the plot of Fig. 91, two curves are shown for performance vs bleed rate. The performance curve for the annular nozzle shows the normal increase in performance for small base bleed rates and decrease for large bleed rates. The multichamber curve shows the same trend but a lower efficiency due to primary flow field shock losses. Both curves of Fig. 91 assume the same momentum thickness at the end of the contour. If it now can be assumed that the mass bleed between the modules causes an increase in entrained air in the boundary layer along

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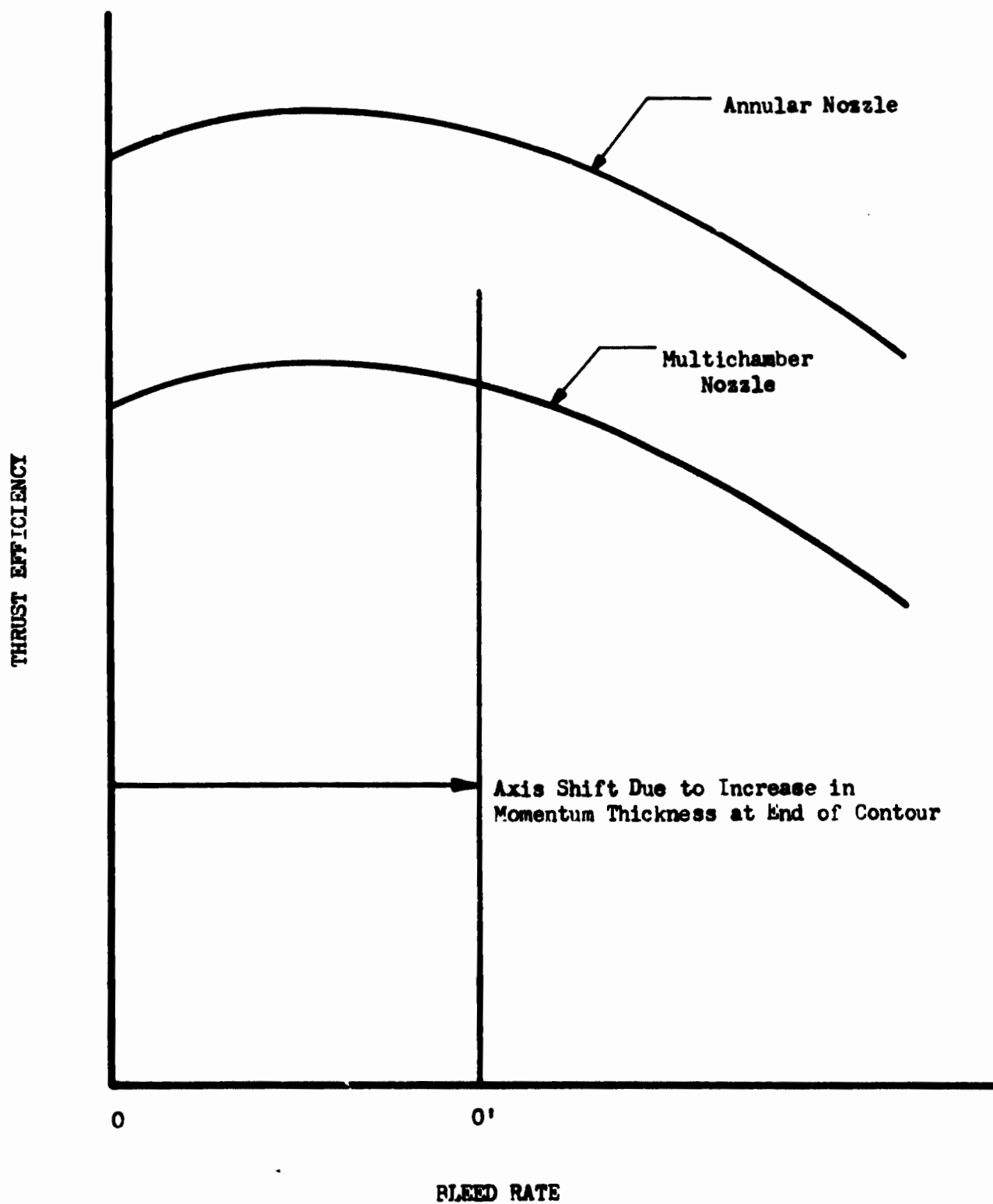


Fig. 91 Thrust Efficiency vs Bleed Rate
for Annular and Multichamber Nozzle

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the contour, an increase in momentum thickness occurs for the multi-chamber nozzle. This increase in momentum thickness for the multi-chamber can now be equated to some positive base bleed rate and one can obtain the efficiency vs actual bleed rate curve for the multi-chamber by shifting the zero bleed axis from 0 to 0'. Now note that the zero bleed point is past the optimum bleed point for the case of little or no momentum thickness. Thus, no amount of either intersegmental or base bleed can increase the performance of this hypothetical nozzle. This curve is qualitatively similar to the experimental data shown in Fig. 89.

The transition point from closed to open-wake base flow for this nozzle occurs at a pressure ratio of 270, as shown in Fig. 88 and 90. Again, no performance improvements are obtained by either intersegmental or base bleed.

Base pressure rises sharply at the transition pressure ratio (270) and then increases at a reduced rate below a pressure ratio of 240. Note that this condition is very similar to the base pressure curve of Fig. 84 (p.144) for model III-9. This characteristic base pressure trend for model III-10 shown in Fig. 90 is similar to that of model III-9. The same explanation for this phenomenon that was given for model III-9 applies. Choking of flow into the base may be occurring in the region between pressure ratios of 240 and 500. Evidence for this is the lower than critical pressure ratio between P_b and P_a . At the lowest pressure ratio at which the nozzle was tested, $P_c/P_a = 150$, the same phenomenon is observed in performance, i.e., at zero intersegmental and base flow the efficiency was 91.7 percent and as either intersegmental or base bleed was increased, performance decreased.

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Figures 92 , 93 , 94 , and 95 show the pressure profiles for this nozzle. Figures 92 and 93 show the wall pressure profiles for various wall taps versus nozzle pressure ratio. In Fig. 92 the pressure taps are in line with the centerline of the module with two taps located in the module and three taps on the contour. The trends are as anticipated with pressures decreasing with increasing pressure ratios on the taps further on down the contour. In Fig. 93 the taps are located between the modules. The tap near the exit plane of the modules follows the ambient pressure while the last two taps follow ambient only to pressure ratios of 300 to 400. Beyond this point the pressures on the contour rise indicating that the wake between the nozzles is moving back towards the throat. The pressure rise is due to shock interaction. Figures 94 and 95 show the same data but plotted in a different manner. The pressures along the module centerline continually decrease at high pressure ratios; however, the pressure profile curves move up with decreasing pressure ratio indicating that recompression may be occurring on the contour as P_a increases. On the other hand the pressure profiles between the modules show adverse pressure gradients to the nozzle exit because of a complex flow field along this plane.

Eight Modules Spaced

The final 8-module configuration tested, Model III-11, was the model with spacing between the modules and an overall length of 30 percent. This model has the lowest performance of all models tested. Peak performance (shown in Fig. 96) of 96.2 percent occurred at a pressure ratio of 950. This pressure ratio is optimum for a one-dimensional ideal area ratio of 37.4. Since the efficiency maximizes at this point, 950 is considered the design pressure ratio for this nozzle. The addition of base bleed at this pressure ratio caused the overall nozzle performance to decrease (Fig. 97).

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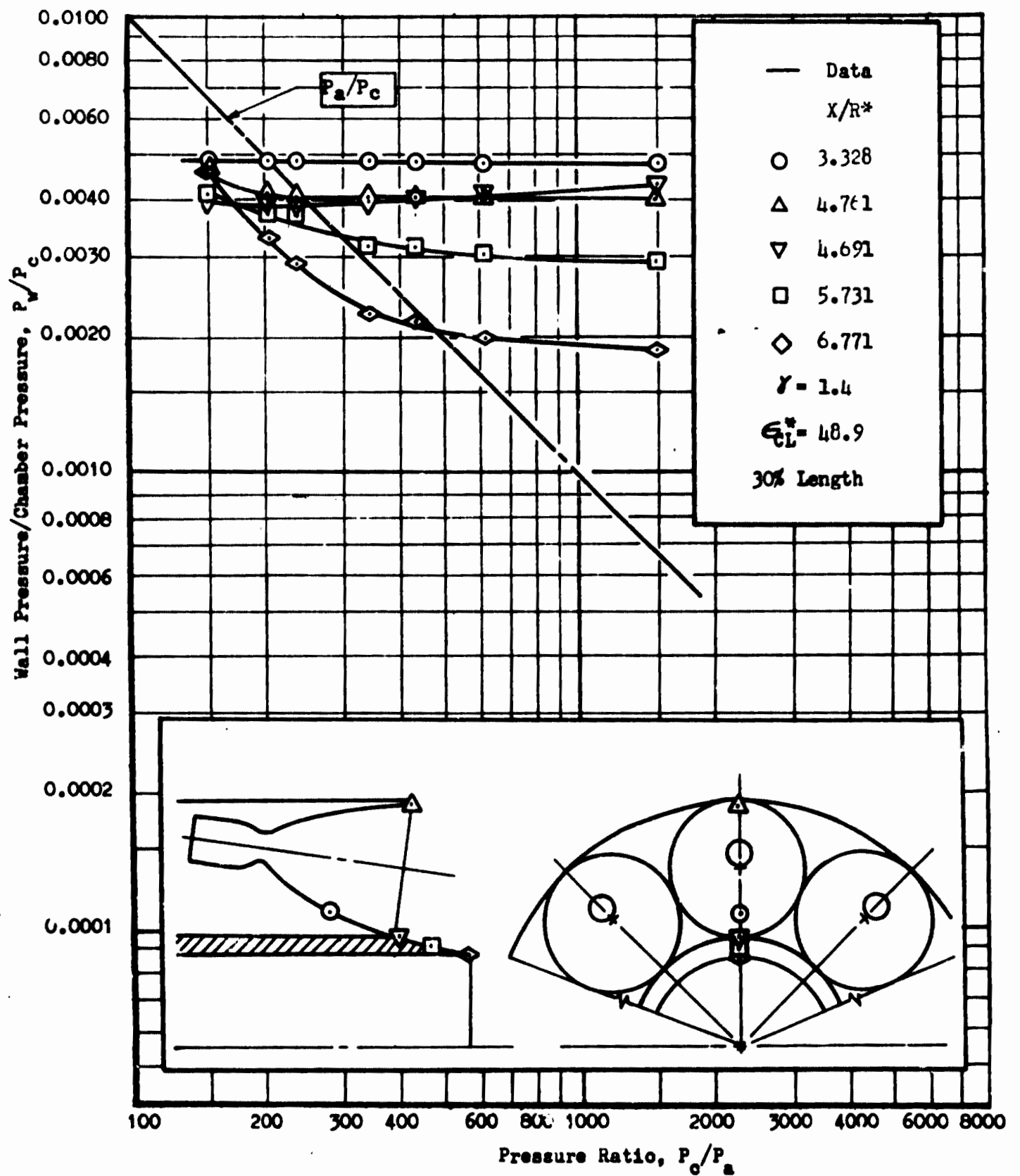


Fig. 92 Module Centerline Wall Pressure vs Pressure Ratio, 8 Modules Touching Multichamber, 30 Percent Length

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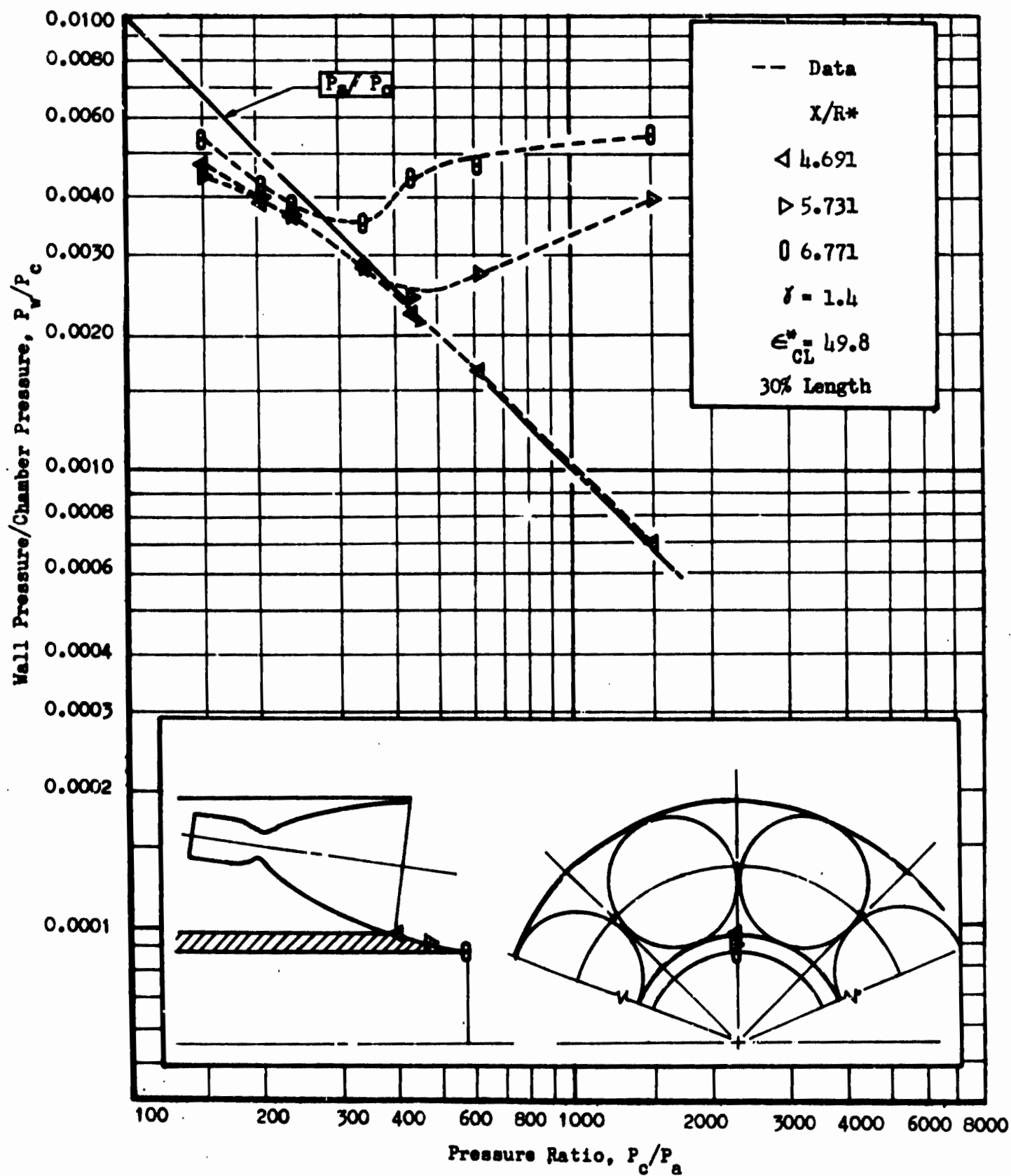


Fig. 93 Wall Pressure Between Modules vs Pressure Ratio,
8 Modules, Touching Multichamber, 30 Percent Length

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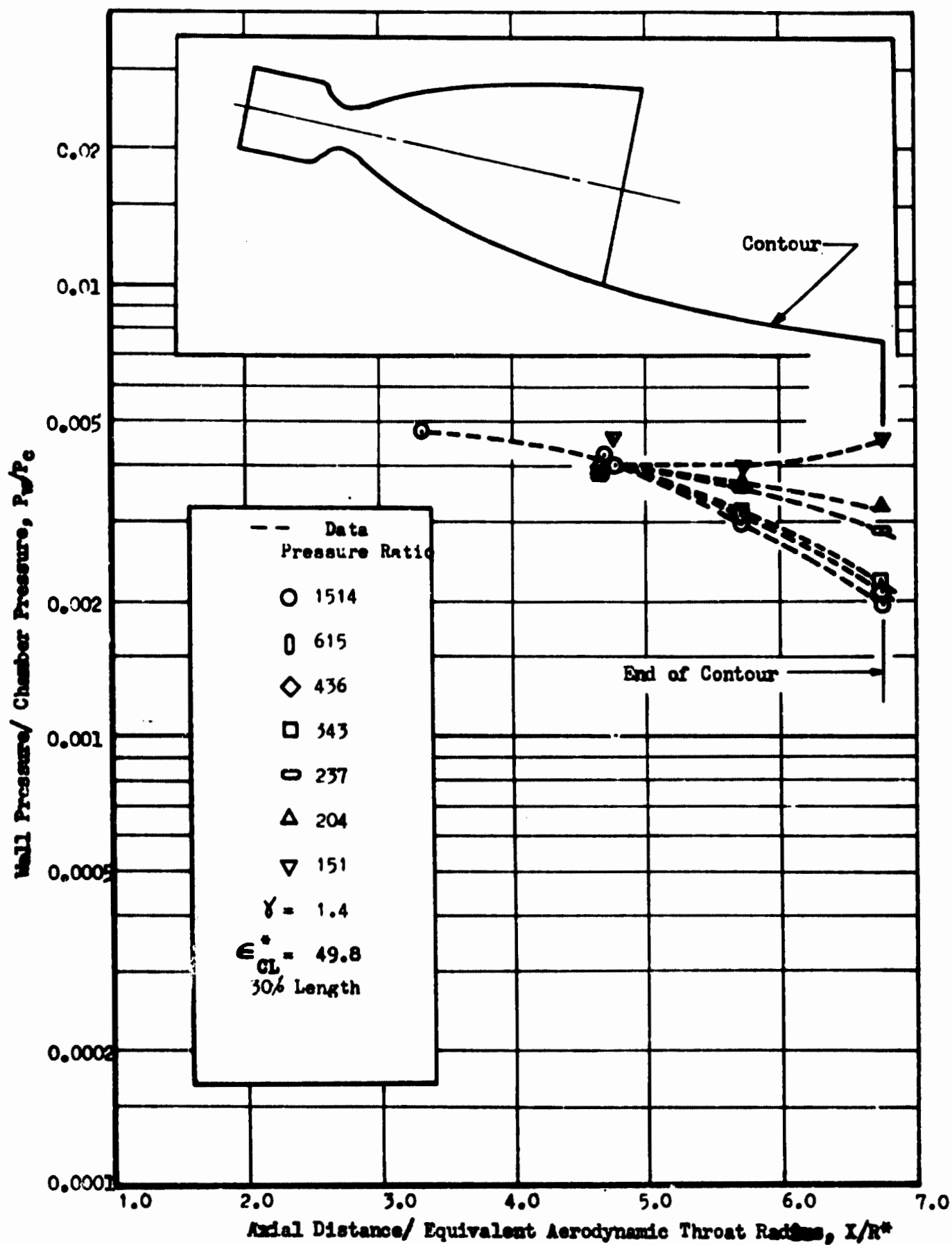


Fig. 94 Module Centerline Wall Pressures vs Axial Length, 6 Module Touching Multichamber, 50 Percent Length

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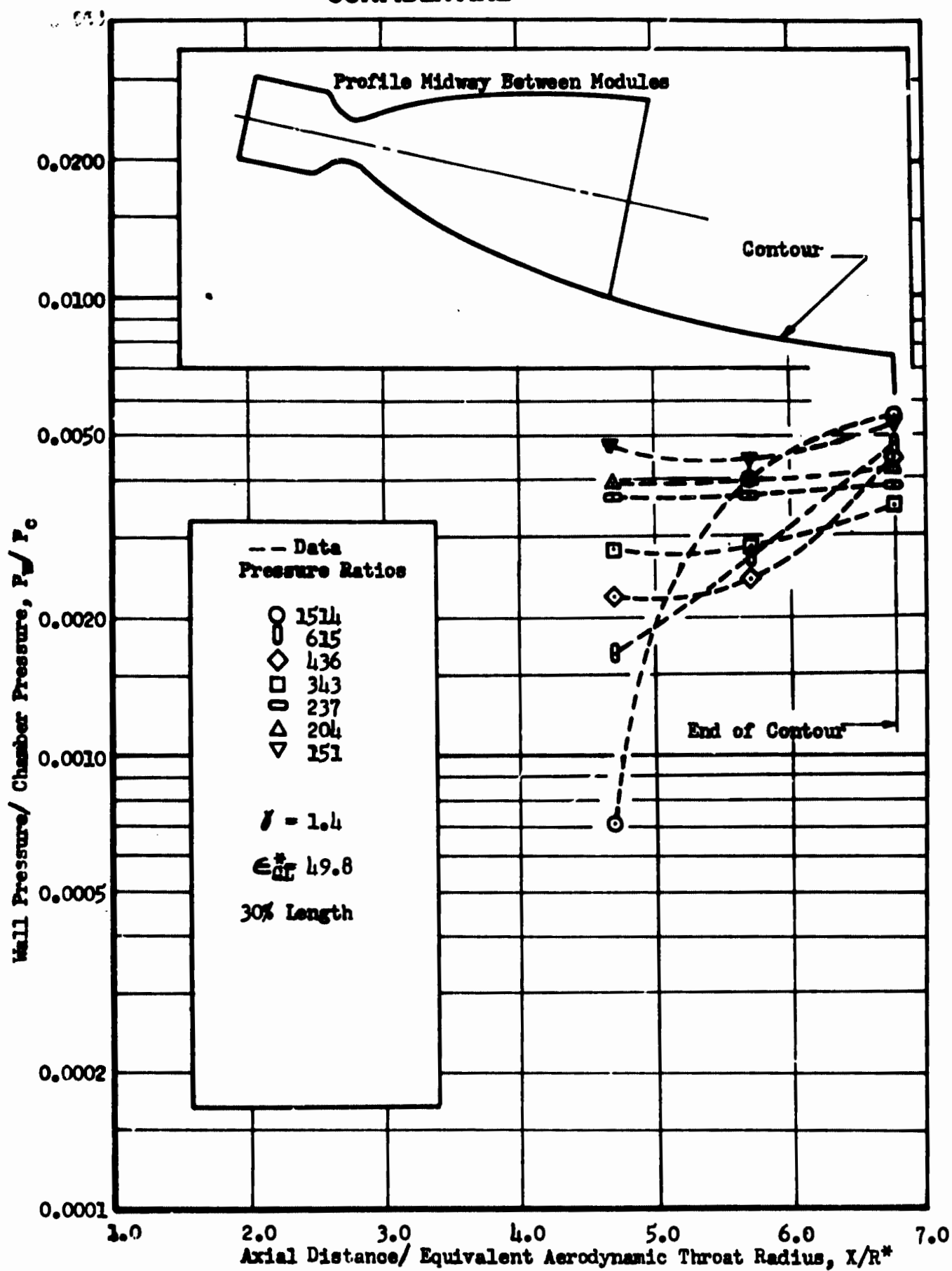


Fig. 9b Wall Pressure Between Modules vs Axial Length,
8 Modules Touching Multichamber, 30 Percent Length

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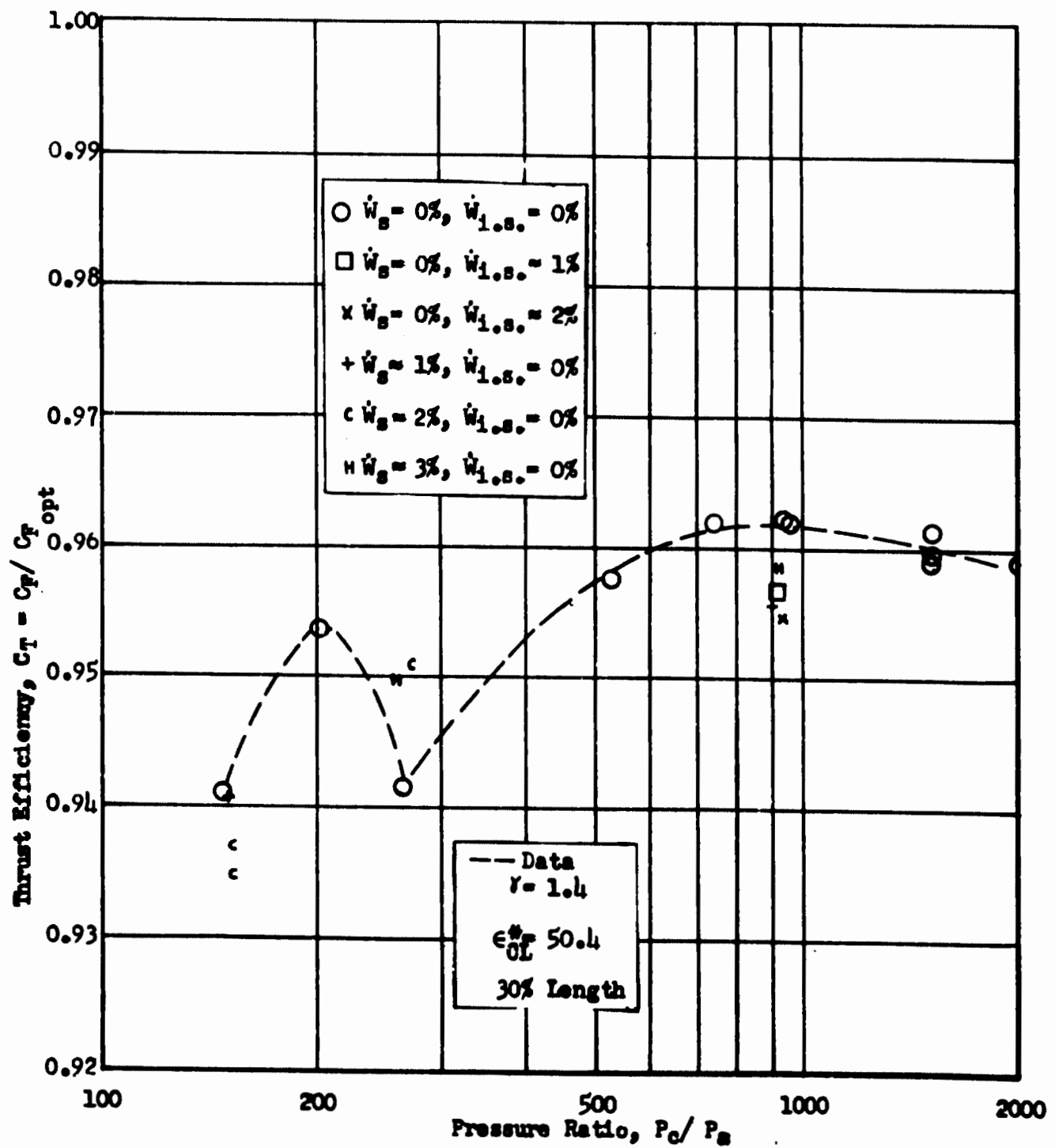


Fig. 96 Thrust Efficiency vs Pressure Ratio, 8 Modules Spaced Multichamber, 30 percent Length

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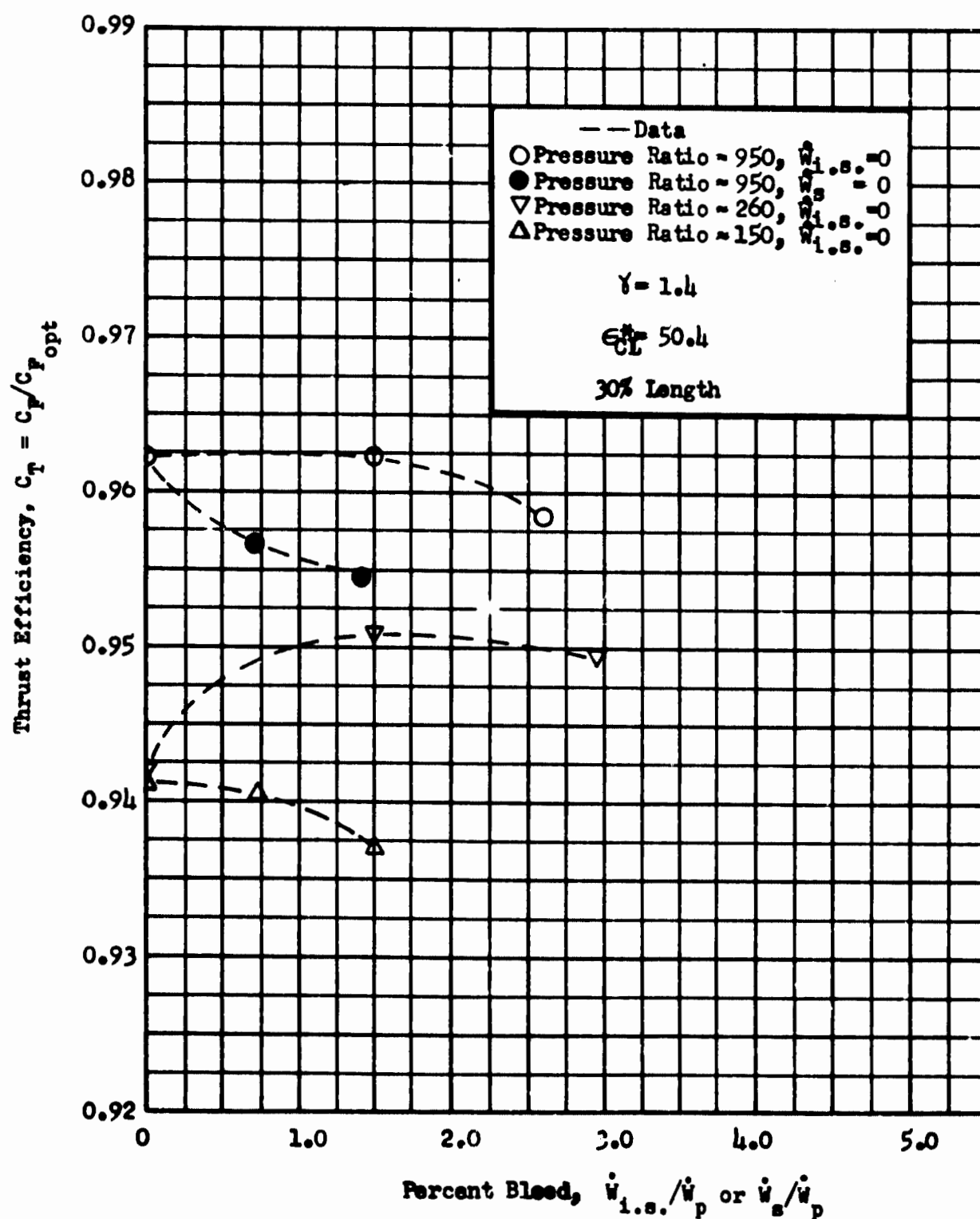


Fig. 97 Thrust Efficiency vs Percent Bleed, 8 Module Spaced Multichamber, 30 percent Length

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The transition from closed to open-wake flow occurred at a pressure ratio of 270 (Fig. 98). Addition of base bleed at this pressure ratio increased performance from 94.2 to 95.1 percent at an optimum bleed rate of 1.5 percent. This increase in performance was apparently caused by an increase in wall contour pressures. At zero base bleed the wall pressure, P_w/P_c , at the end of the contour was 0.00196 and increased to 0.00327 for 1.5 percent base bleed. This bleed appears to be causing separation from the contour, resulting in an efficiency increase. In contrast, introduction of base bleed into Model III-10, 8 touching multichamber, did not cause an increase in contour pressure and thus efficiency did not increase.

A sharp increase in performance occurs at a pressure ratio of 200, due to a rapid rise in base pressure from the closed wake condition. Performance then falls off as pressure ratio is decreased beyond this point.

The lowest pressure ratio at which tests were conducted on this nozzle was 150. Addition of base bleed caused a loss in performance.

Use of intersegmental bleed caused a loss in performance at design pressure ratio. The explanation for this loss is similar to that given for the previous multichamber models. The base pressure curve, Fig. 98 , also shows the same trend as the previous model. In addition, this curve verifies the transition point to be near a pressure ratio of 270.

The module and plug wall pressure profiles of Fig. 99 , 100, 101 and 102 show the same trend as for model III-10.

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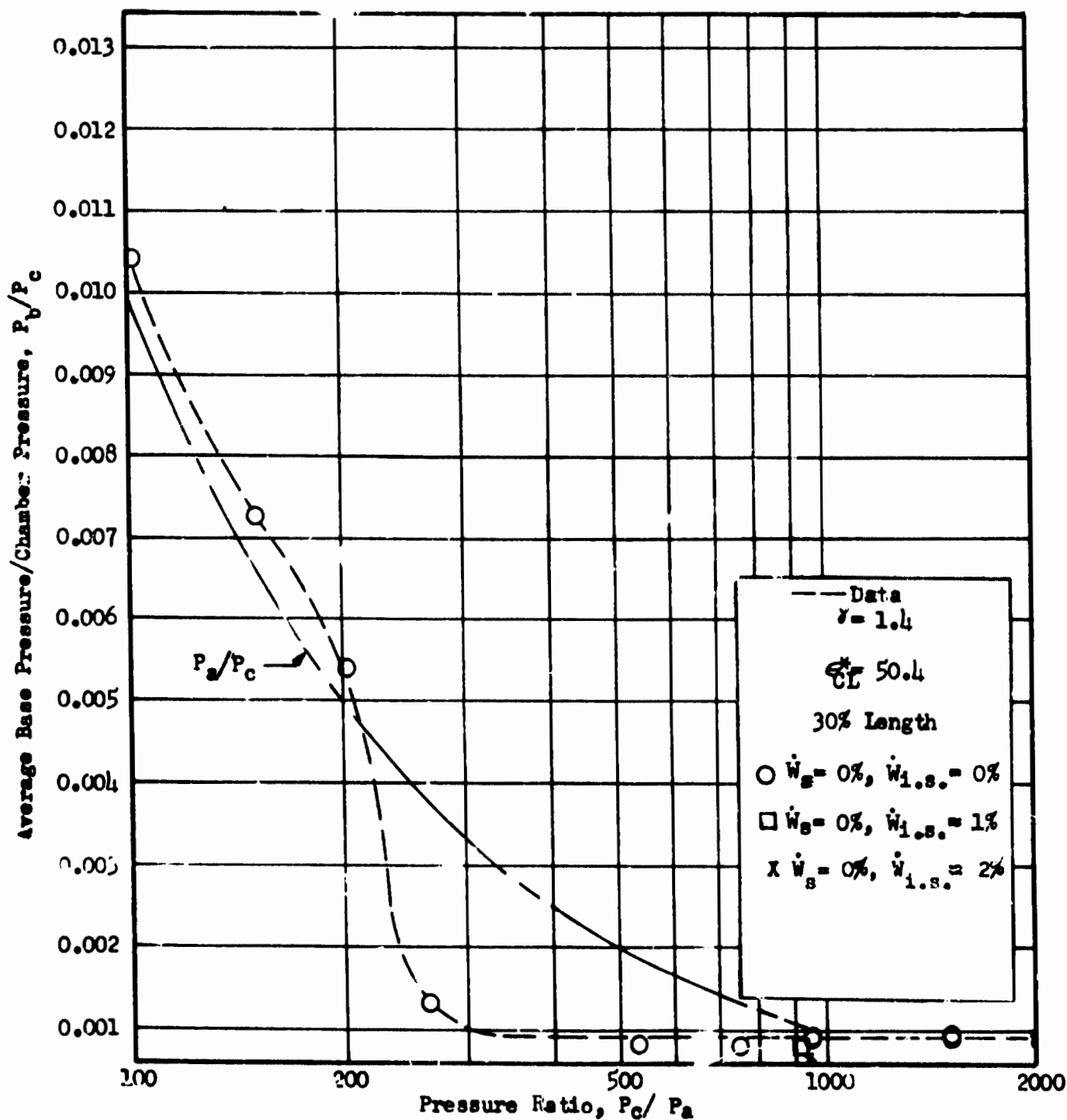


Fig. 98 Base Pressure vs Pressure Ratio, 8 Module Spaced Multichamber, 30 percent Length

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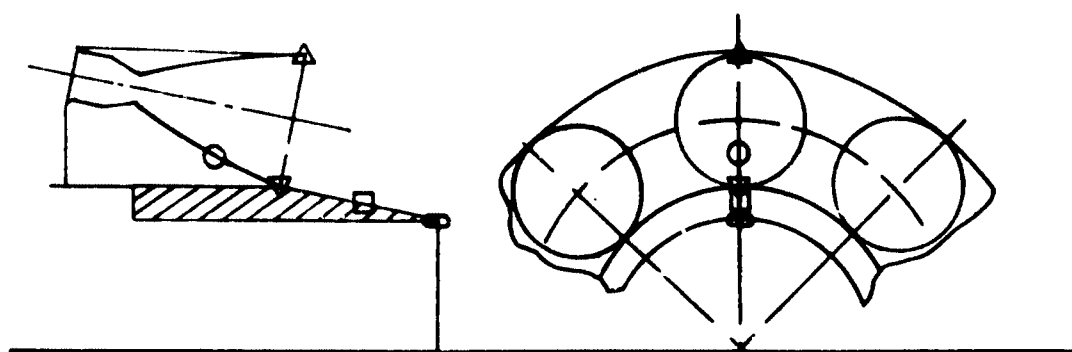
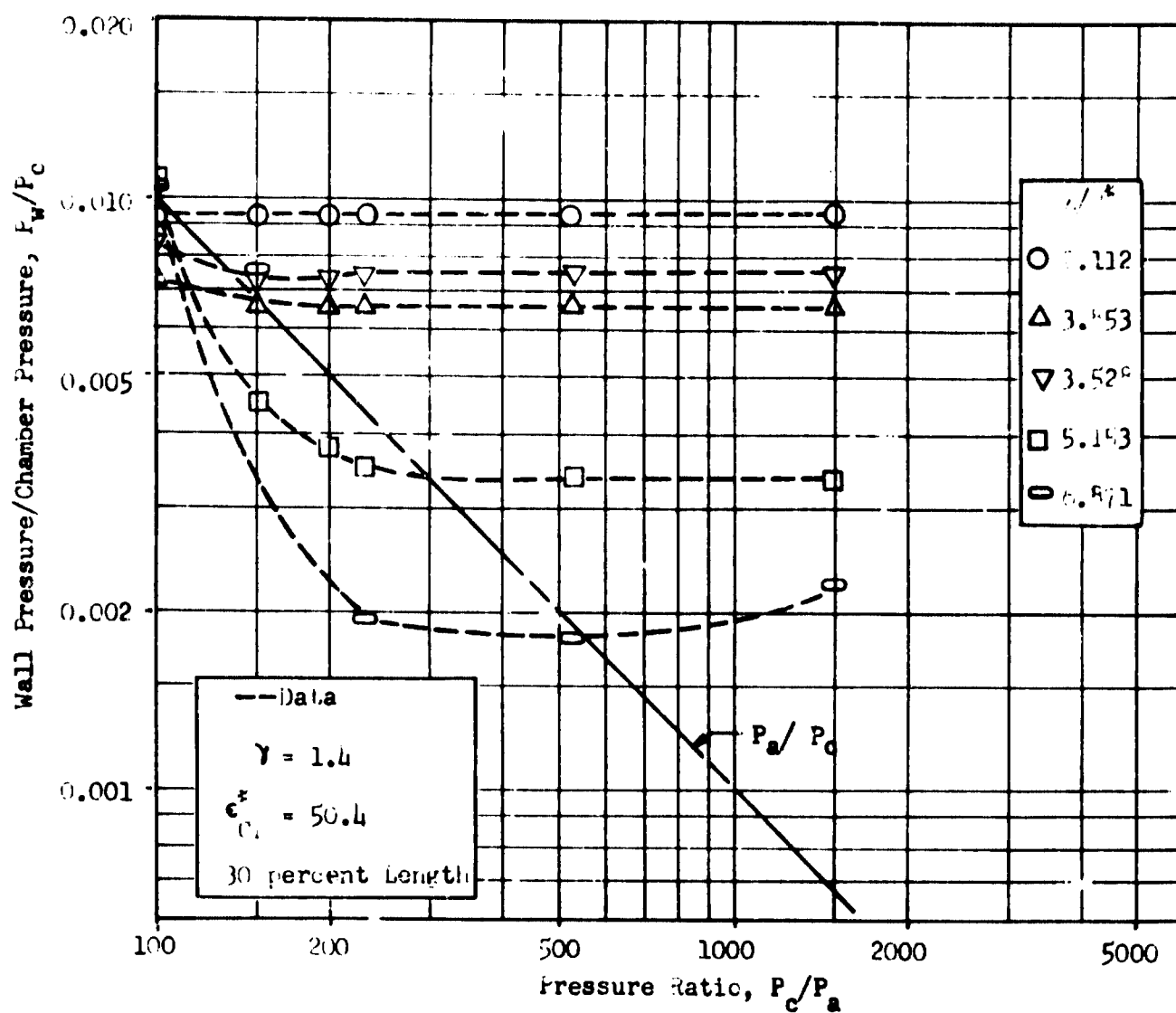


Figure 99. Module Centerline Wall Pressure vs Pressure Ratio, 8 Module Spaced Multichamber, 30-percent Length

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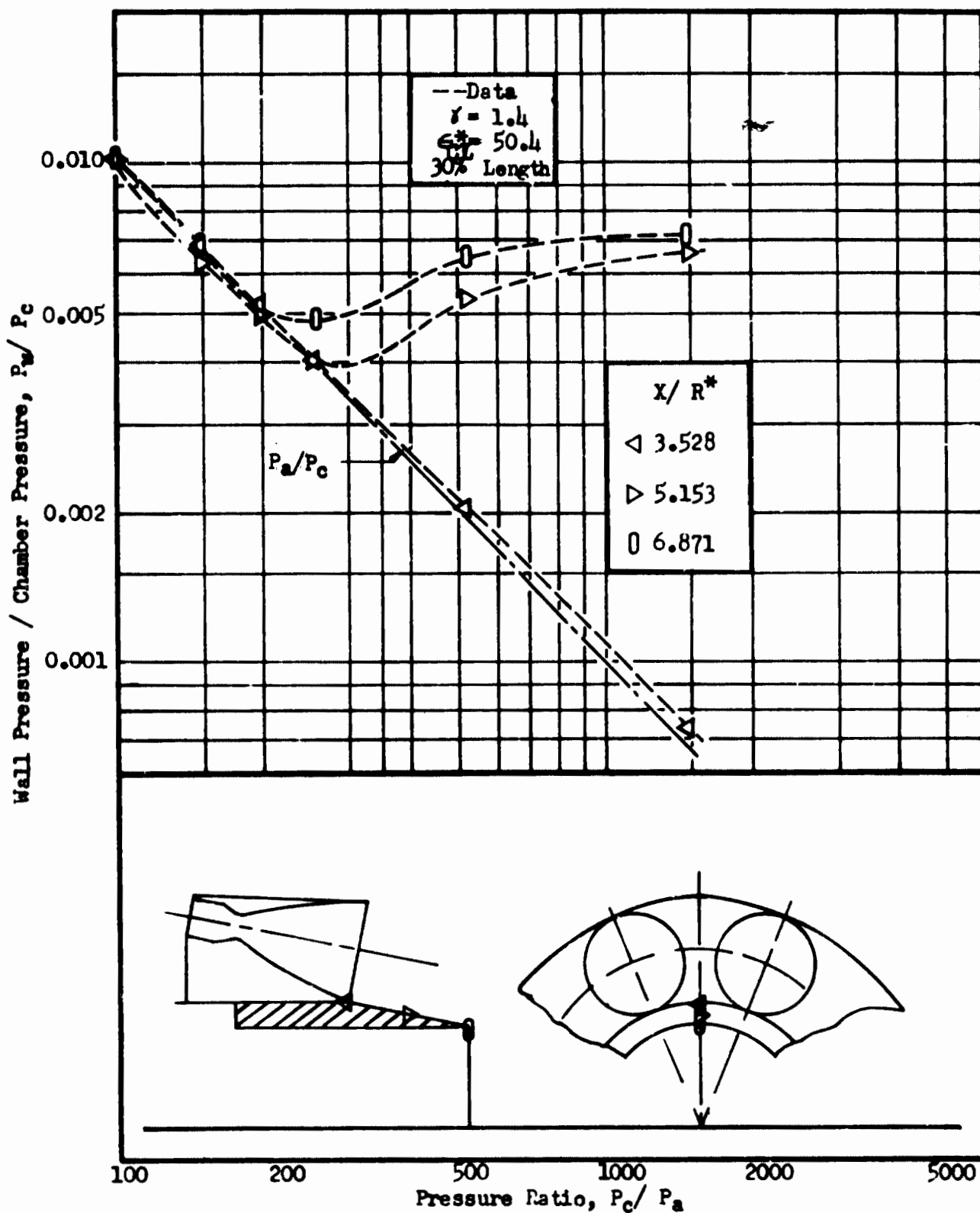


Fig.100 Wall Pressure Between Modules vs Pressure Ratio, 8 Modules Spaced Multichamber, 30 Percent Length

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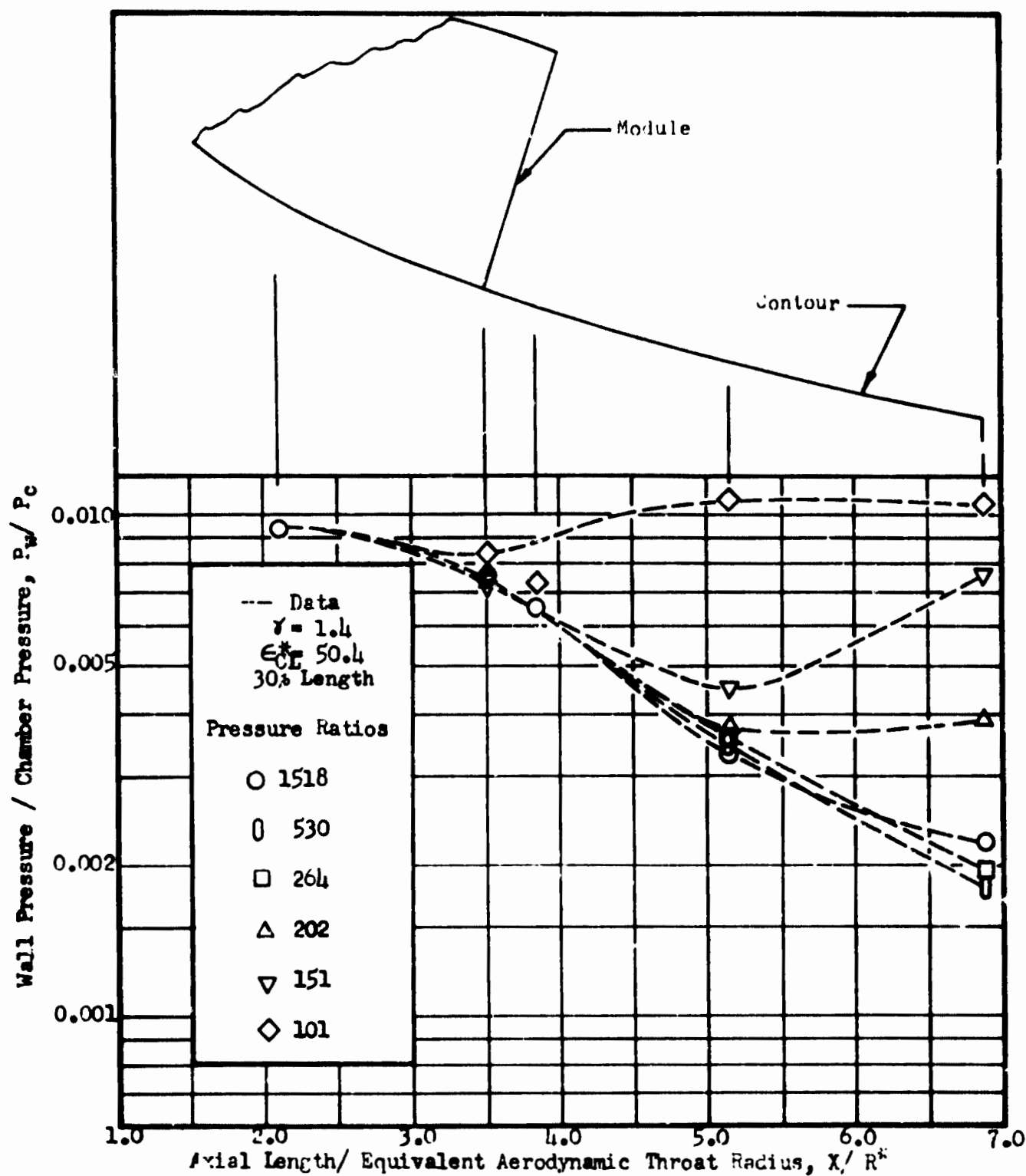


Fig.101 Module Centerline Wall Pressure vs Axial Distance, 8 Modules Spaced Multichamber, 30 percent Length

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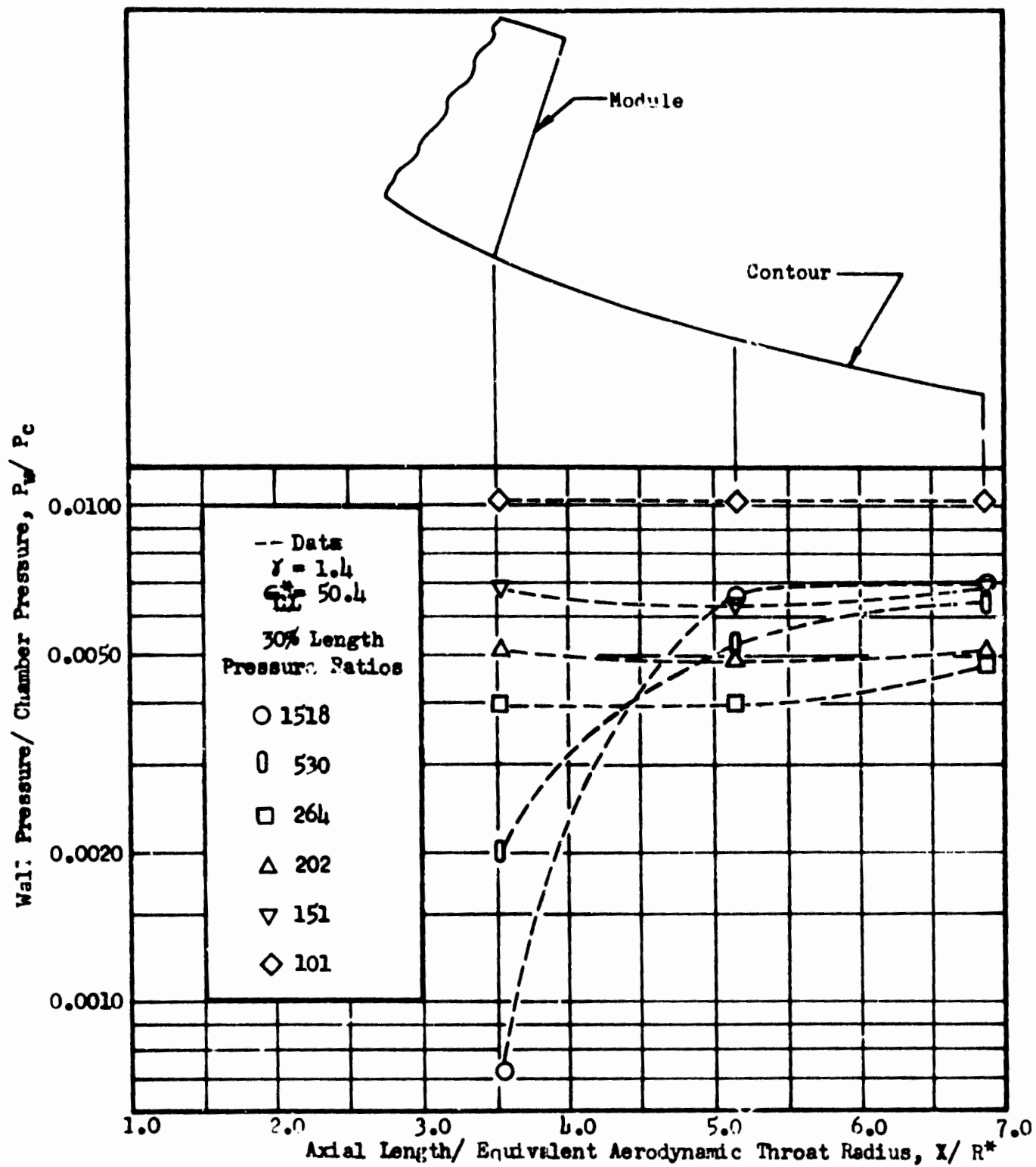


Fig. 102 Wall Pressure Profile Between Modules vs Axial Distance, 8 Module Spaced Multichamber, 30 Percent Length

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Sixteen Module Multichamber

The final multichamber model tested was model III-12, the 16 touching modules with the centerbody spike extension. Performance for this model is shown in Fig. 103. The highest performance attained with no base or intermodule bleed (See Fig. 103) was 96.7 percent at a pressure ratio of 1200. The base flow transition point from closed to open-wake occurred at a pressure ratio of 370, (See also base pressure curve Fig. 104).

As shown by Fig. 103 and 105, no performance gains were noted with any of the intermodule bleed rates used.

At design pressure ratio (1200) and the transition point, performance increases were obtained at 0.7 percent base bleed. Due to the fact that this model was designed with 16 modules, the primary flow more closely approximates an annular nozzle, the shocks are weaker and the spaces between the modules are smaller. All these factors tend to reduce the momentum thickness and therefore the bleed performance curves, Fig. 105, more closely approximate the annular nozzle case.

The pressure profile curves, Fig. 106, 107, 108 and 109 are similar to those for the 8 module chambers.

In an attempt to improve the intersegmental pressures a filler plate was placed in the exit plane of the modules to help keep up the intersegmental pressures (Fig. 81). The performance results of this are shown in Fig. 110. At the high pressure ratio end, $P_o/P_a = 1300$, the performance with no intersegmental bleed was 96.6 percent as opposed to 96.7 percent for the no filler plate model. Since this is within the accuracy of the data scatter, essentially no performance

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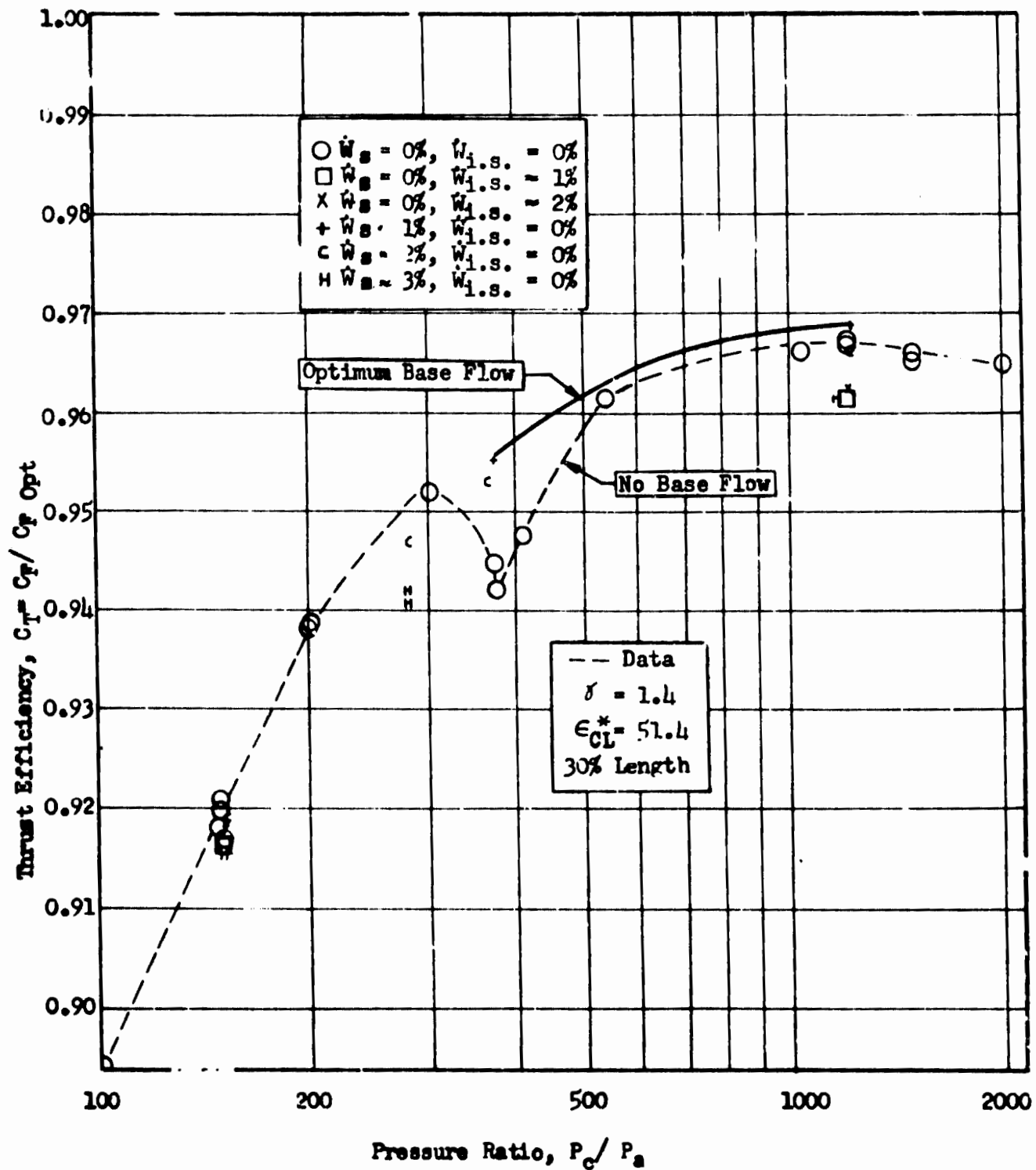


Fig. 103 Thrust Efficiency vs Pressure Ratio,
16 Module Multichamber, 30 percent Length

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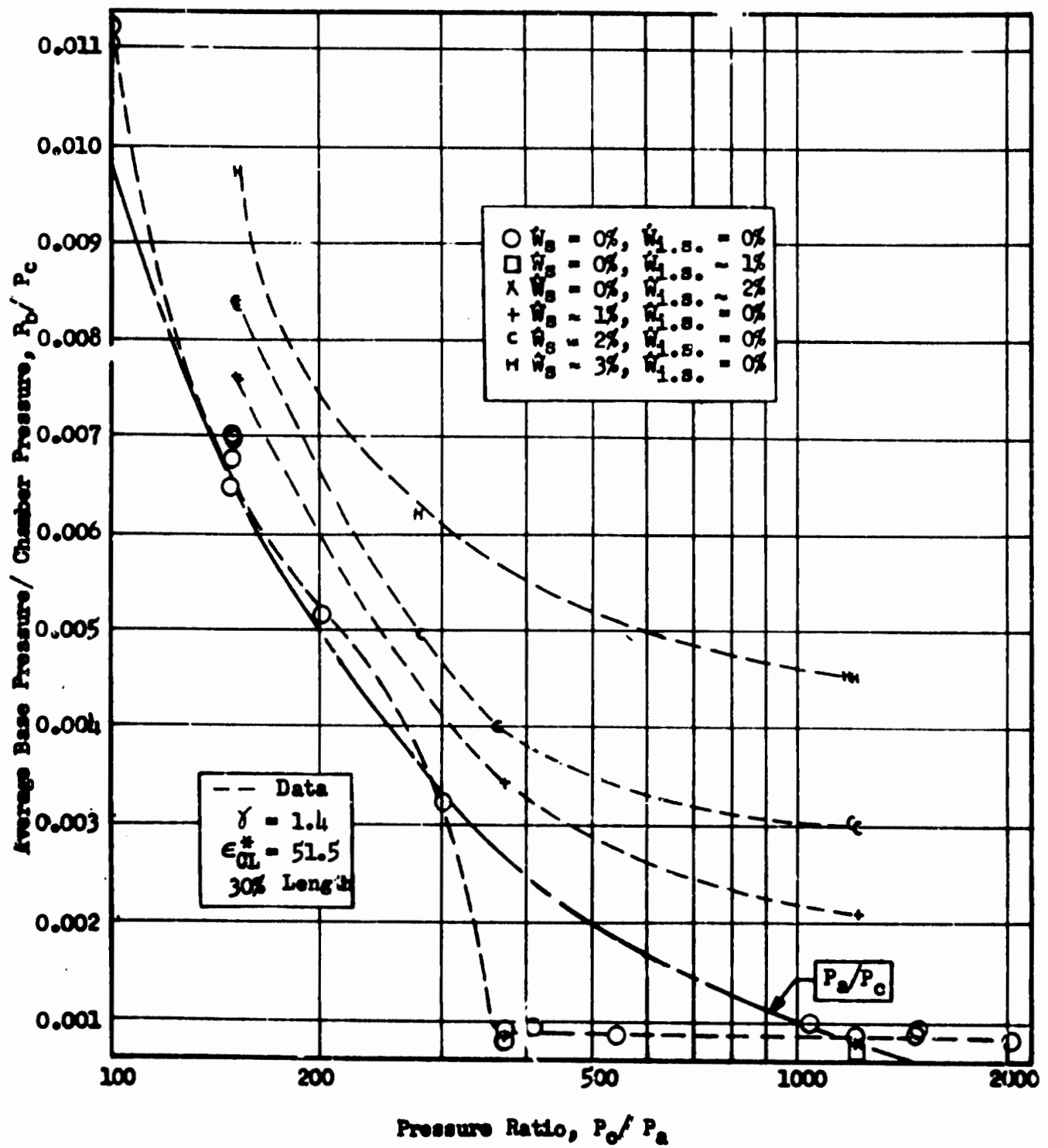


Fig.104 Base Pressure vs Pressure Ratio,
16 Module Multichamber, 30 percent Length

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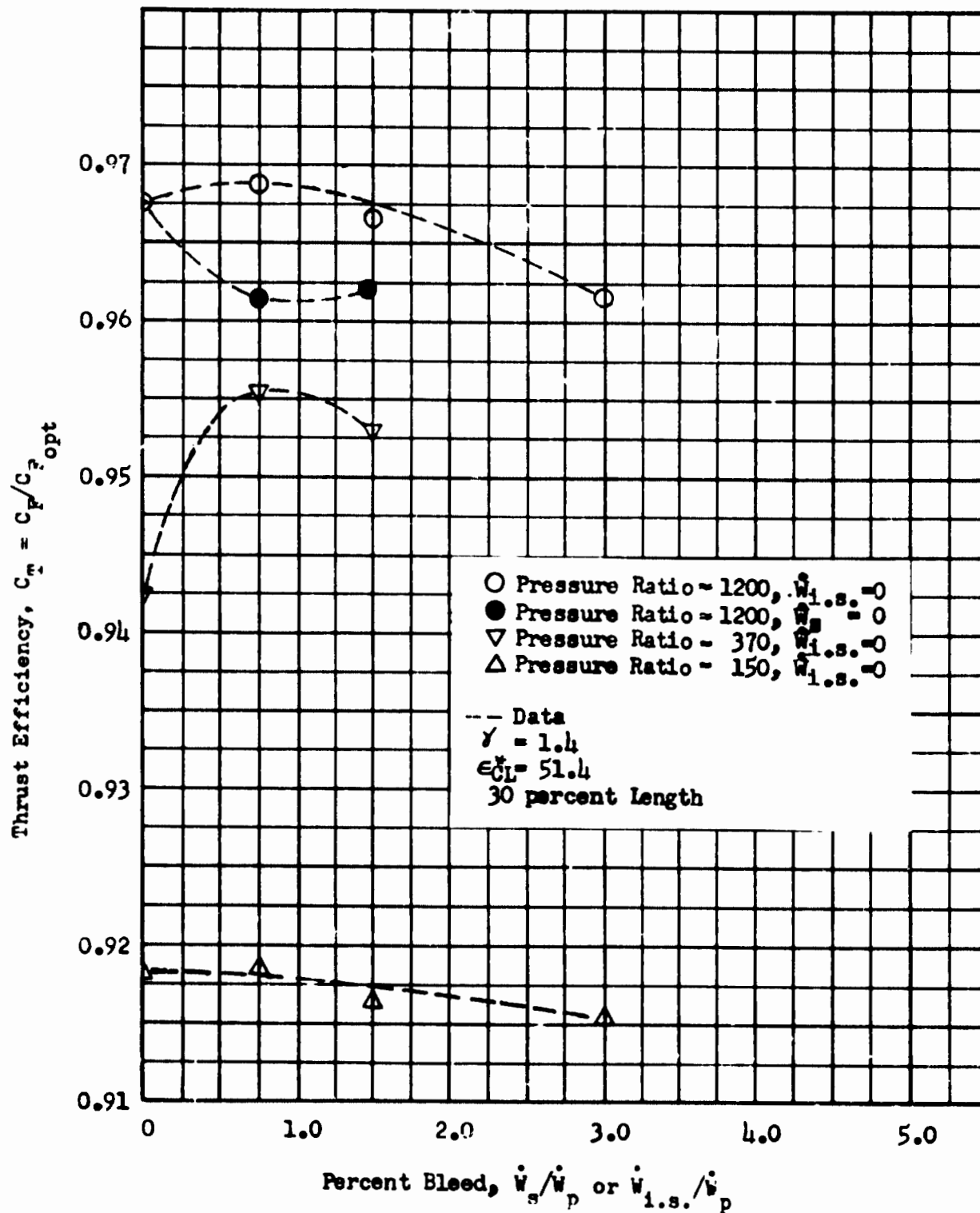


Fig. 105 Thrust Efficiency vs Percent Bleed,
16 Module Multichamber, 30 percent Length

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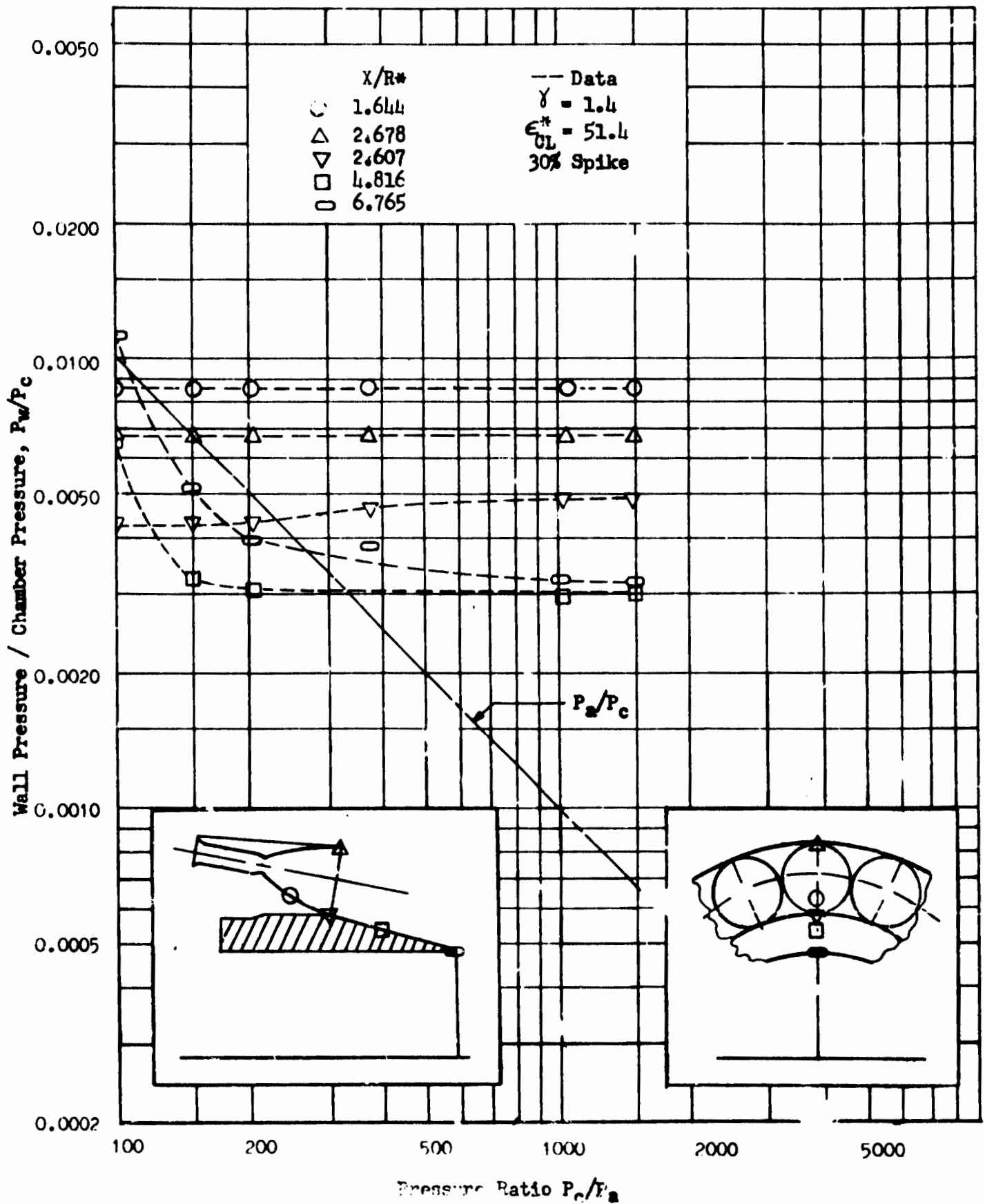


Fig. 106 Module Centerline Wall Pressure vs Pressure Ratio, 16 Module Multichamber 30 percent Length

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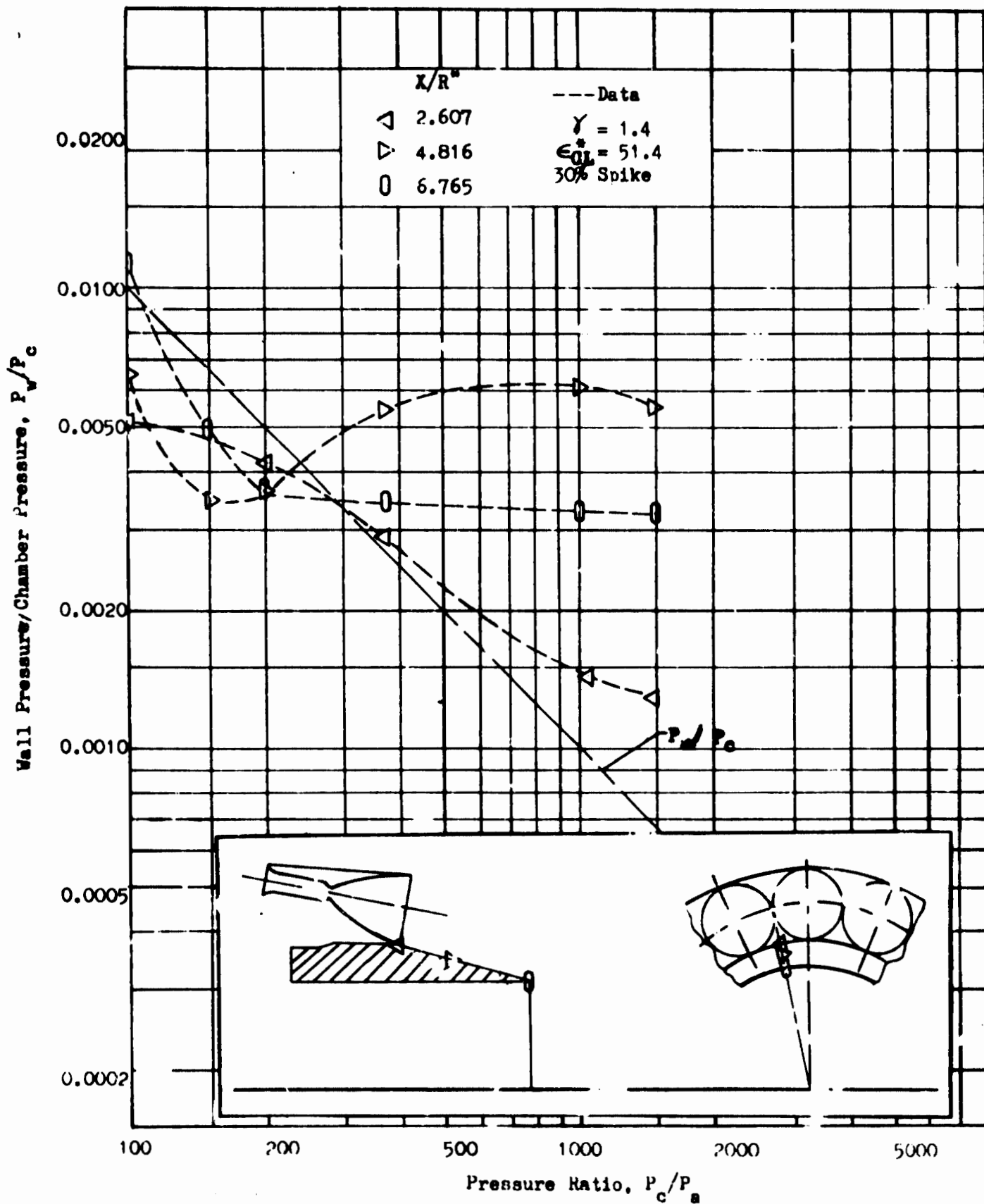


Fig. 107 Wall Pressure Between Modules vs Pressure Ratio, 16 Module Multichamber, 30 Percent Length

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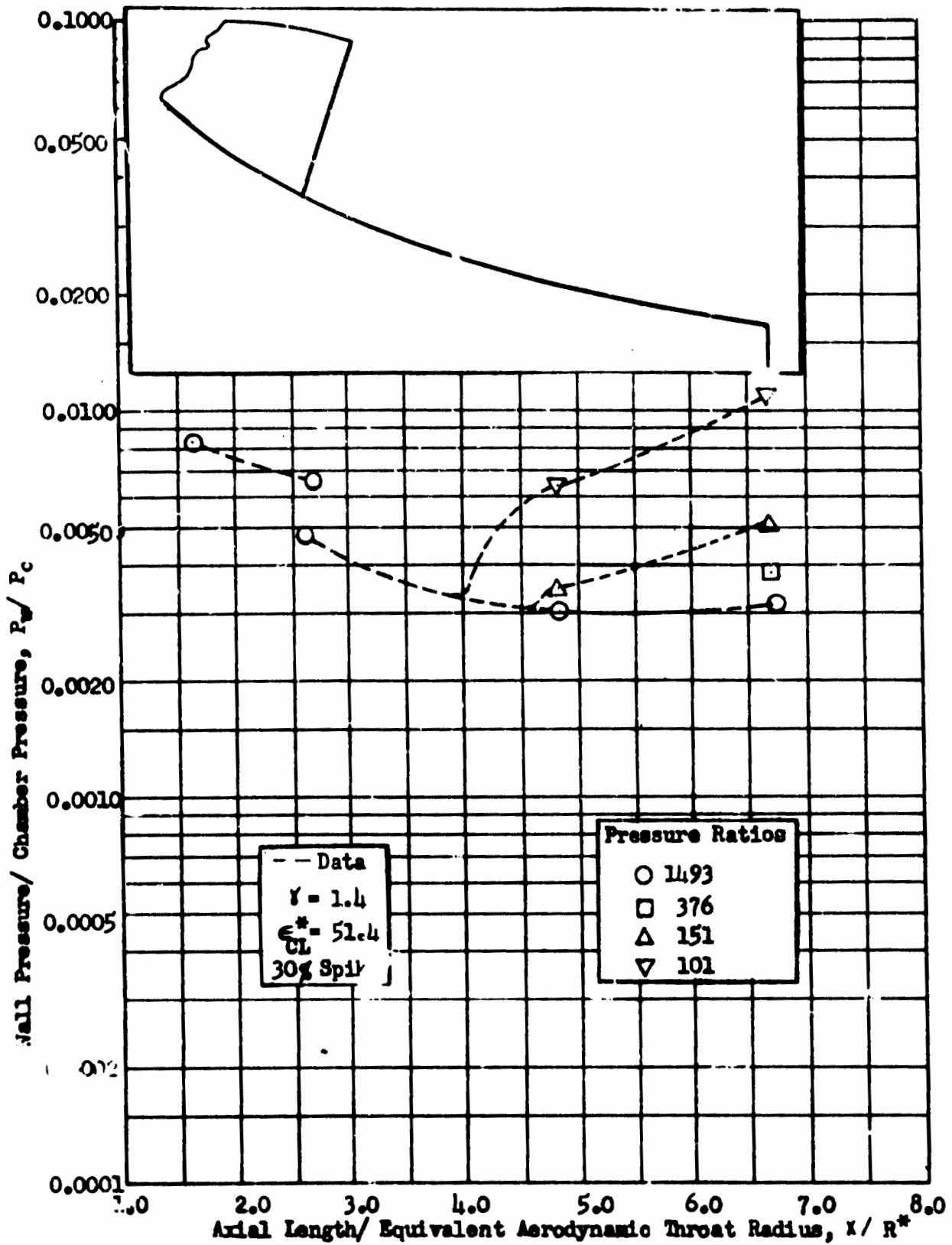


Fig. 108 Module Centerline Wall Pressure vs Axial Length, 16 Module Multichamber, 30 percent Length

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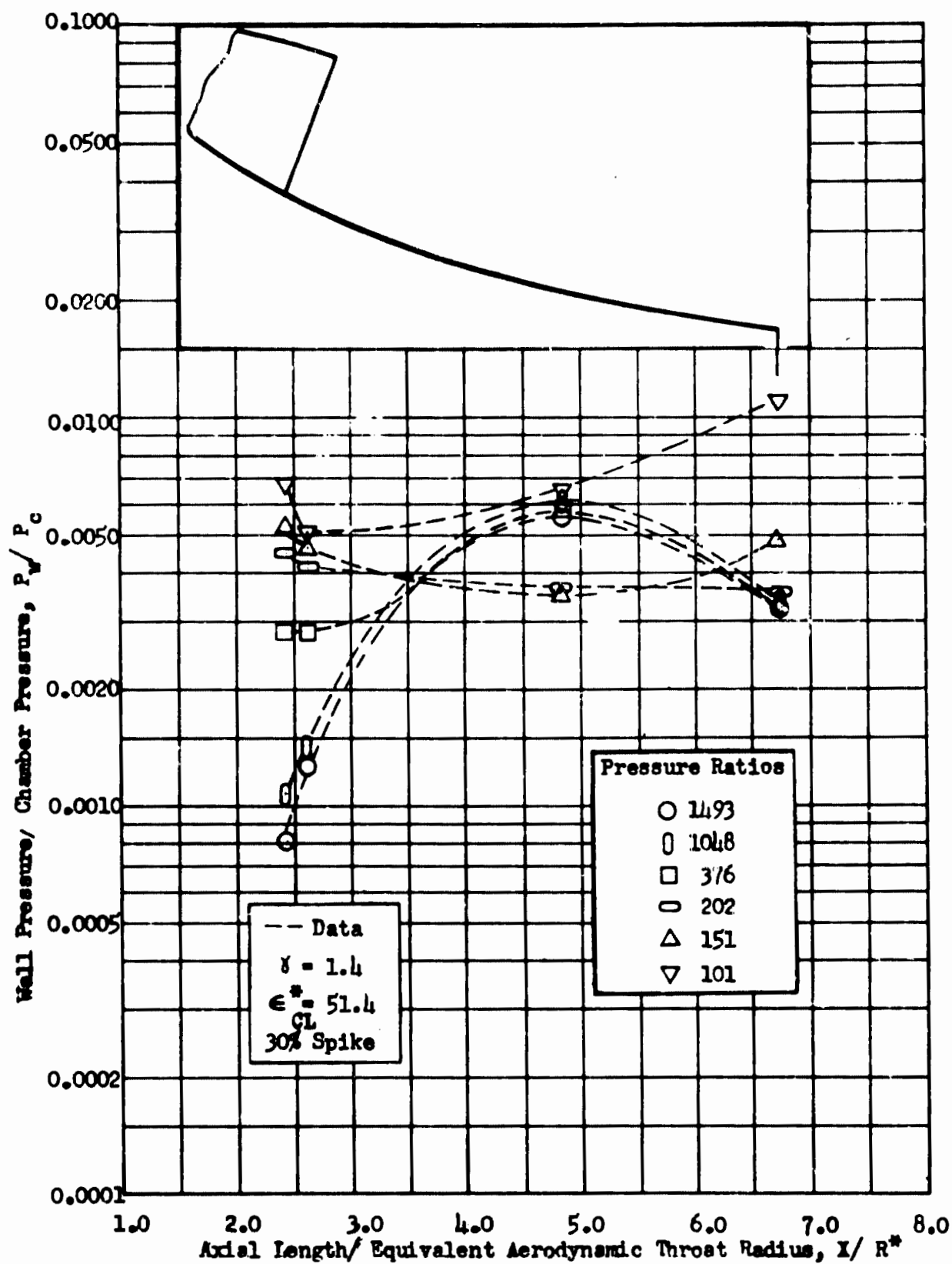


Fig. 109 Wall Pressure Between Modules vs Axial Length, 16 Module Multichamber, 30 Percent Length

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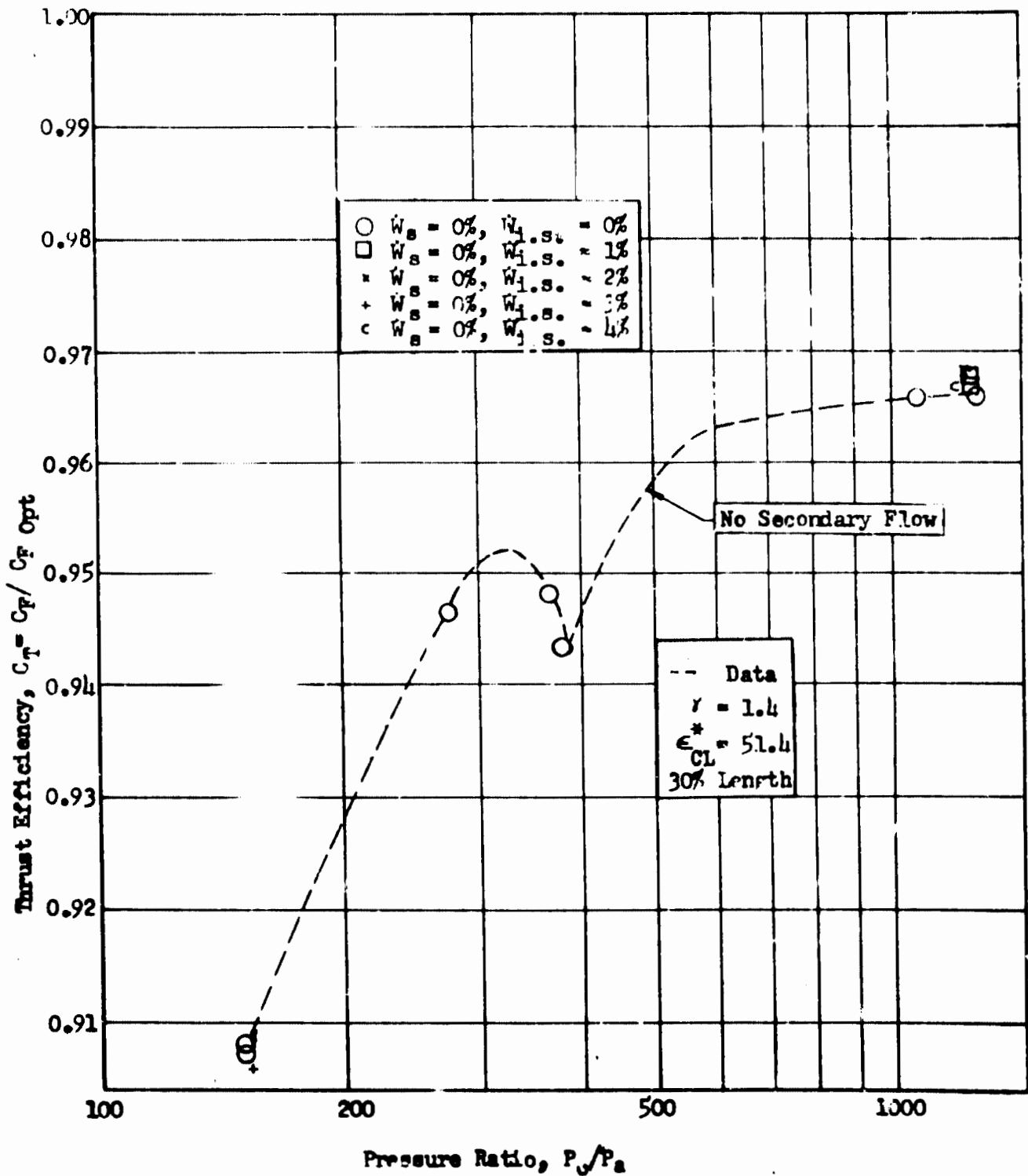


Fig. 110 Thrust Efficiency vs Pressure Ratio, 16 Module Multichamber with Intersegmental Filler Plate

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change resulted by addition of the filler plate. One factor here was that there was no actual seal between the filler plate and the modules and ambient could still bleed into the spaces behind the modules. Performance improved about 0.2 percent with the introduction of 1-2 percent intersegmental bleed, as compared to a decrease of approximately 0.5 percent for the same model without the filler plates. Use of intersegmental bleed at a pressure ratio of 150 resulted in a slight decrease in performance. The combined use of intersegmental and base bleed resulted in approximately 0.5 percent decrease in efficiency at both low (150) and high (250) pressure ratios. Base pressures for this model are shown in Fig. 111. While intersegmental bleed at high pressure ratio had no effect on centerbody base pressure for the model without the filler plate (Fig. 104), it significantly increased base pressure for the model with the filler plate. The performance curve dip point occurs at about the same place in both configurations but at low pressure ratios (150) there is a loss in efficiency of over 1 percent for the nozzle with the filler plate. The reason is that flow behind the modules is restricted resulting in lower intersegmental pressures.

DISCUSSION OF RESULTS

$\epsilon = 25$ Models

The test results show the following characteristics for this nozzle:

1. Good performance can be attained with this nozzle over a pressure ratio range from sea level to design altitude with the proper base bleed and base configuration.

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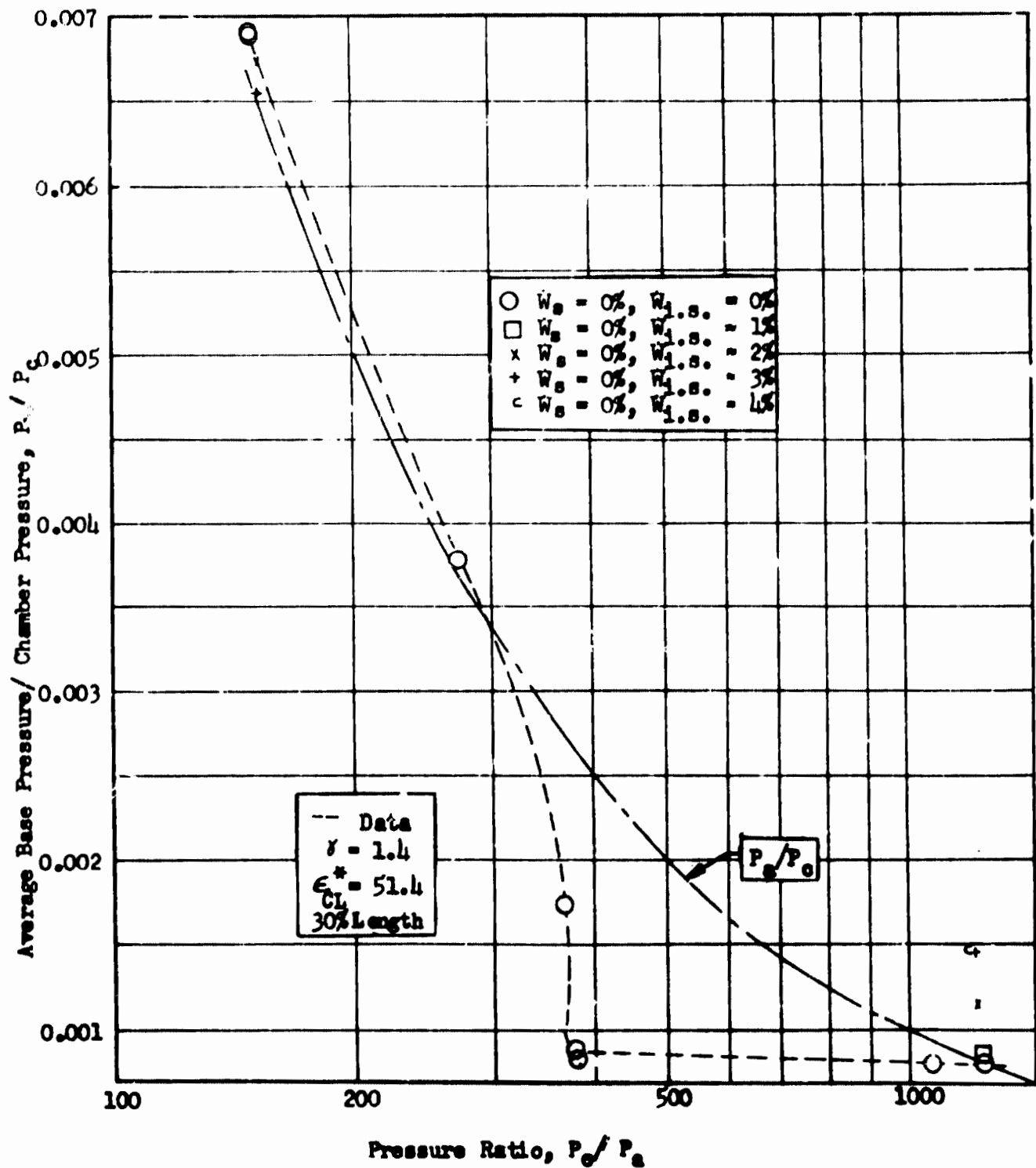


Fig. 111 Base Pressure vs Pressure Ratio, 16 Module Multichamber with Intersegmental Filler Plate

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2. The best performing base configurations were the open cavity, the radially-outward base, and the porous-plate base.
3. Supersonic injection into the base causes a loss in performance.
4. Optimum secondary flowrate is between 2 and 2.5 percent of primary flow over the test range for this nozzle.
5. Theoretical computations of the effect of secondary flow on base pressure agreed well with the data.
6. Base pressures were higher for CF_4 than for air. Based on these results, hot firing base pressure predictions for zero secondary flow would be higher than the air. Correlation of the data with hot-firing data will be conducted later in the program.

A summary of the performance for the $\epsilon_0 = 25$ nozzle is given in Table 6. The performance is based on values achieved at design pressure ratio with zero and the optimum value of secondary flow. Secondary flow for the porous plate was limited to 0.6 percent due to flow restrictions in the plate and pressure restrictions in the base cavity.

$\epsilon = 50$ Annular Models

The $\epsilon = 50$ group of models was tested primarily for the purpose of evaluating different combustor configurations. For the purpose of comparison a point expansion truncated ideal spike was tested as the reference for all of the $\epsilon = 50$ models. Figure 112 shows the performance of this nozzle to be the highest of all models tested at all

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TABLE 6
SUMMARY PERFORMANCE OF $\epsilon_o = 25$ NOZZLE

Nozzle	¹ Pressure Ratio P_c/F_a	² Base Flow Percent $\dot{W}_s/\dot{W}_p$	Performance C_F measured / C_F opt	Base Pressure P_b/P_c
$\epsilon_o = 25$, Air Open Base	540 540	0 2.0	96.5 97.6	.0060 .0105
$\epsilon_o = 25$, Air Radially-Out Base	540	1.7	97.4	.0010
$\epsilon_o = 25$, Air Radially-In Base	540	1.7	97.1	.0093
$\epsilon_o = 25$, Air $\epsilon_o = 3.5$ Base Nozzle	540	2.3	95.9	.0053
$\epsilon_o = 25$, Air $\epsilon_o = 15$ Base Nozzle	540	2.3	95.9	.0050
$\epsilon_o = 25$, Air Porous Plate Base	540	0.6	96.9	-
$\epsilon_o = 25$, CF ₄ Open Base	290 280	0 1.7	95.6 96.8	.0067 .0108

1. Design pressure ratio
2. Approximately optimum base bleed for all configurations except the porous plate

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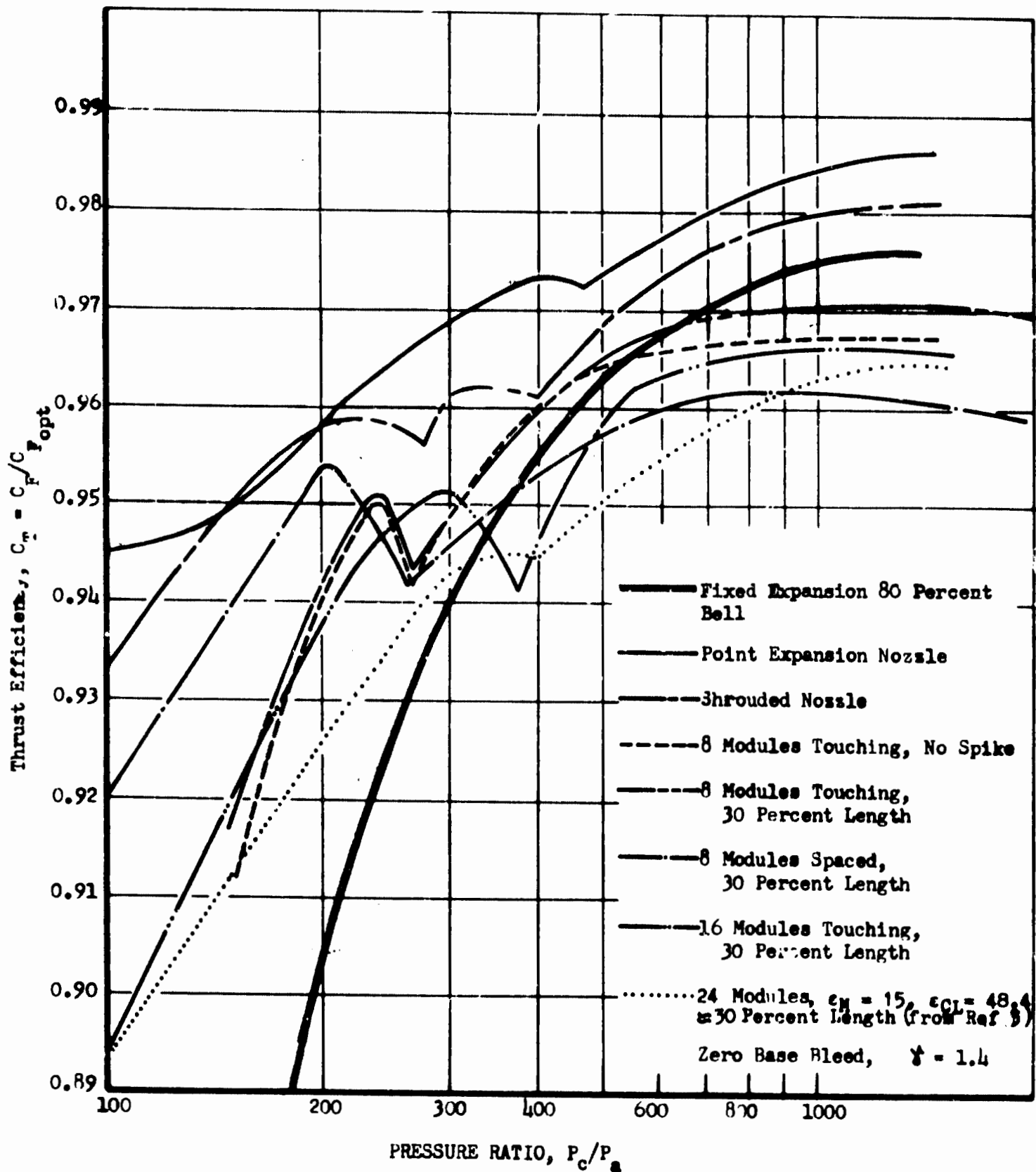


Figure 112 Comparison of Experimental Performance of $\epsilon_{CL} = 50$
Annular and Multichamber Nozzles

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pressure ratios. This is the usual case when testing with a non-reacting gas since chemical kinetics are not involved and ideal potential flow is the sole contribution to primary performance. However, when hot reacting gases are considered as the propellant, the chemical kinetics of the gases play a significant role in primary performance. As previously explained the shrouded spike nozzle was tested as a representative design for a hot gas nozzle. The air tests do not reveal any chemical kinetic performance benefits but only the difference in non-reacting gas performance between the nozzles. Figure 112 shows that for the particular shroud design selected the potential performance loss was approximately 0.5 percent from the reference model over the major portion of the operating range. Since the shrouded nozzle was designed, more recent experience and technology has shown that improved shrouded nozzle designs are possible. In most cases it is theoretically possible to reduce the shrouded nozzle potential flow loss to a very small value.

Table 7 is a summary of performance and base pressure values for these nozzles. Referring to Table 7 and Fig 112 the following observations can be made concerning these two nozzles:

1. Performance is high for both nozzles with the point expansion nozzle having slightly over 0.5 percent greater performance throughout the pressure ratio range of 300 to 1500.
2. At very low pressure ratios the shrouded nozzle shows better altitude compensating characteristics and has performance equal to the point expansion model.

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TABLE 7
SUMMARY PERFORMANCE OF $\epsilon = 50$ NOZZLES

Nozzle	¹ Pressure Ratio P_c/P_a	² Base Flow Percent $\dot{W}_s/\dot{W}_p$	Performance C_p measured C_p opt	Base Pressure P_b/P_c
$\epsilon_0 = 50$ point expansion	1450	0	98.6	0.0014
	1450	0.9	98.8	0.0026
$\epsilon_0 = 50$ shrouded	1475	0	98.0	0.0006
	1475	0.7	98.1	0.0011
$\epsilon_{CL} = 50$ 8 modules touching no centerbody extension	1400	0	96.7	0.0008
	1400	0.7	96.7	—
$\epsilon_{CL} = 50$ 8 modules touching spike centerbody	1400	0	97.1	0.0008
	1400	0.7	96.9	—
$\epsilon_{CL} = 50$ 8 modules spaced spike centerbody	950	0	96.2	0.0009
	950	1.5	96.2	—
$\epsilon_{CL} = 50$ 16 modules touching spike centerbody	1200	0	96.7	0.0009
	1200	0.7	96.9	0.0021
$\epsilon_{CL} = 50$ 16 modules touching with filler plate spike centerbody	1300	0	96.6	0.0006
	1300	2.0 ($\dot{W}_{1s}/\dot{W}_p$)	96.8	0.0013

1. Pressure ratio at which maximum efficiency occurs

2. Approximate optimum $\dot{W}_s$ ($\dot{W}_{1s} = 0$) or $\dot{W}_{1s}$ ($\dot{W}_s = 0$)

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3. Secondary flow improves performance by only a small amount for both nozzles. This is primarily because nozzle performance without secondary flow is already high.
4. From design pressure ratio down to the open wake transition point, the point expansion nozzle has about twice the base pressure as the shrouded nozzle (See Fig. 72 and 77). However, below the transition point the base pressure of the shrouded nozzle rises more rapidly than the base pressure of the point expansion nozzle. This accounts for the improved altitude compensating characteristics of the shrouded nozzle. Nevertheless, even though the compensation is better the shrouded nozzle only matches but never exceeds the performance of the point expansion model.
5. If chemical kinetics are considered and it can be shown that the shrouded nozzle has a higher I_{sp} (close to full shifting) performance for hot gases, then the shrouded nozzle could give the higher overall performance at all pressure ratios. The amount of chemical equilibrium achieved during expansion depends chiefly upon the propellants, mixture ratio, chamber pressure, thrust level, and shroud design.

6-50 Multichamber Models

Three basic multichamber models were tested, the 8 touching, 8 spaced and 16 touching models (listed in Table 7). The 8 touching model had two basic configurations, i.e., zero centerbody length and a spike

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centerbody extended to 30 percent length. Two configurations were tested for the 16 touching model; one with open spaces between the modules and one with a filler plate between modules.

Of all the multichamber models, the 8 touching model had the highest performance in zero and extended centerbody lengths. Figure 112 shows that addition of the centerbody improved the performance of this model about 0.4 percent over the range of operation. Referring to the discussion of the test results on these two nozzles, the following comments can be made:

1. Performance for this model was in general 1-2 percent below that of the reference model (point expansion).
2. Addition of either base bleed or intersegmental bleed did not in general increase the performance of either configuration of this model.
3. No performance degradation was noted for one engine out at either design pressure ratio or at very low pressure ratios. This result is applicable to this configuration only. Other test results (Ref 3) indicate performance losses are obtained with engine out configurations.

When the module area ratio of the 8 module multichamber was reduced to 20.7, spaces resulted between the nozzles. A comparison of the performance of the 8 spaced multichamber unit to the other models tested is made in Fig. 112. At high pressure ratios the performance of the 8 spaced model is lower than the other models. This can be attributed to: (1) a basically low module area ratio, and (2) shock losses in the primary flow field because of the spacing.

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At low pressure ratios the performance for this nozzle is higher than any of the other multichambers. The spacing is beneficial at pressure ratios below 240. Inspection of Appendix 3 shows that the intersegmental pressures are higher for the 8 spaced models than they are for the 8 touching model at low pressure ratios. This configuration had the lowest effective area ratio of the models tested. Peak efficiency occurred at a pressure ratio of 950 compared to 1200 to 1400 for the other models. When it is further noted that the basic module area ratio is low (thus module design pressure ratio is low) it is easy to see why this model has good performance at low pressure ratios.

Figure 112 shows that the model with the 16 touching modules had a slightly lower performance level than the 8 chamber model. The wake closure point occurred at a somewhat higher pressure ratio and low pressure ratio compensation was about as good as the 8 modules touching models. Although increasing the number of modules is usually associated with increasing the performance, this was not so for the given ground rules for these multichambers. The ground rules were: (1) the cluster area ratio shall remain constant, and (2) for a given number of modules the modules shall touch. With these restrictions the module area ratio is fixed. Thus, the module area ratio for the 8 chamber touching model was 30.2 and for the 16 chamber was 20.7. This means that the basic primary flow field performance for the modules was greater for the 8 module unit than for the 16 module. Although the shock and intermodule pressure losses are less for the 16 module model this did not make up for the basically greater performance of the higher area ratio 8 module touching units. This infers that there is an optimum number of modules which will maximize the module performance-shock-intermodule pressure trade-off. An additional factor which may have

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influenced the relative performance of these models is the spacing ratio, δ/D_0 . The value of δ/D_0 was 0.020 for the 16 chamber model compared to 0.012 for the 8 chamber model. This would tend to cause relatively higher transition losses for the 16 chamber model. However, data from Ref 12 indicates that this difference in δ/D_0 should result in less than 0.1 percent difference in efficiency between the models.

For comparison purposes a multichamber spike nozzle tested and reported in Ref 3 was included in Fig. 112. This model consisted of 24 touching modules of area ratio 15 spaced around a spike centerbody. The cluster area ratio, ϵ_{CL} , was 48.4 and the overall length was approximately 30 percent of a 15 degree conical nozzle of the same area ratio. This model corresponds closely to the 16 chamber configuration tested in this program. Data from this reference appears to agree well with the 16 chamber data, particularly with respect to efficiencies ($\dot{W}_g = C$) at design pressure ratio, the transition pressure ratio and low pressure ratio. The wake transition point pressure ratio is approximately 400 for the 24 chamber model compared to 370 for the 16 chamber model which is consistent with the general trend toward higher transition point pressure ratios as the continuous throat configuration is approached.

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ANALYTICAL AND DESIGN STUDIES OF AEROSPIKE COMBUSTORS

Analytical design studies were performed to investigate various engine/vehicle configurations incorporating the aerodynamic spike nozzle. Combustor concepts that were considered included several types of toroidal combustors and cylindrical combustors (multichambers) with discrete circular throats and various shaped expansion sections. Associated with the integration of the various combustor concepts into vehicle systems, consideration was given to envelope requirements, nozzle cooling, nozzle performance, engine weight, upper and lower stage, plumbing, turbomachinery, controls, and methods of thrust vector control. The range of engine parameters considered were

Chamber pressures from 300 to 3000 psia

Thrusts from 20,000 to 2,000,000 pounds

Expansion area ratios up to 150

N_2O_4 /UDMH- N_2H_4 (50-50) Propellants

SUMMARY

Ideally the objective of these studies was to determine which type of combustor could be utilized most effectively with an aerodynamic spike nozzle at a particular operating point in the parameter range of interest. The normal criteria for selection of a particular combustor would include detailed consideration of engine performance, engine weight, nozzle cooling, turbomachinery, design complexity, fabrication technique and cost, development time and costs, engine reliability and overall cost effectiveness. The scope of this study was such that only a few of the aforementioned items could be treated in any detail. Therefore only a limited number of general conclusions were obtained in this study.

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Specific items which were treated in this work included the following. Investigations were made to establish the geometric effects of various multichamber exit shapes and to determine the relative envelopes of engine and vehicle configurations. A summary of toroidal combustor and multichamber effects on nozzle performance is presented. Also included is a brief description of multichamber and toroidal aerospike performance programs which were developed partially utilizing data generated in this program. A parametric weight comparison was made of single bell, multichamber and toroidal chamber aerospike engines of 2,000,00 pounds thrust over a wide range of chamber pressure and area ratio.

The two most heavily emphasized studies were in the areas of nozzle heat transfer and system design. Detailed heat transfer studies were made to establish limits of regenerative cooling feasibility for multichamber and toroidal chamber aerospikes utilizing N_2O_4 /UDMH- N_2H_4 (50-50) propellants. The studies were conducted over a wide range of chamber pressure, area ratio, and thrust level. Design layouts were made for typical single bell, multichamber, and toroidal aerospike engines at four specific thrust levels of interest. The features of the configurations are described along with advantages, disadvantages, and potential problem areas.

A summary of major conclusions covering the analysis and design section is presented at the end of this section.

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COMBUSTOR DESCRIPTION

Two basic types of combustor seem suitable for use with the aerodynamic spike nozzle. These are the toroidal combustor and the multichamber combustor. There are many variations of each of these basic concepts and each has its own advantage and disadvantages. The geometric relationships for throat area, area ratio, etc. are also unique for each concept. This section presents an introduction to these combustor concepts and their geometric characteristics.

Toroidal Combustor Configuration

The chief feature of the toroidal combustion chamber is that it provides a continuous or near continuous annular throat which is the most desirable type to achieve maximum performance from the annular aerodynamic spike nozzle. Disturbances to the sonic and supersonic flow caused by structural members in the flow field or discrete combustors result in nozzle performance losses.

Three variations of the toroidal combustor concept are shown in Fig. 113. The sonic tube combustor is the simplest type in that the combustor is formed and self-supported by rows of individual, formed tubes which may be regeneratively cooled or film cooled. The throat is formed by swaging the tubes. The cooling circuit is simple and a minimum of external structural support is used. The chief disadvantages of this configuration are high heat flux is encountered at the throat, high stresses must be sustained by the tubing, and flow disturbances result from expansion around the throat structure. These flow disturbances can be minimized by using aerodynamic shaped tube trailing edges.

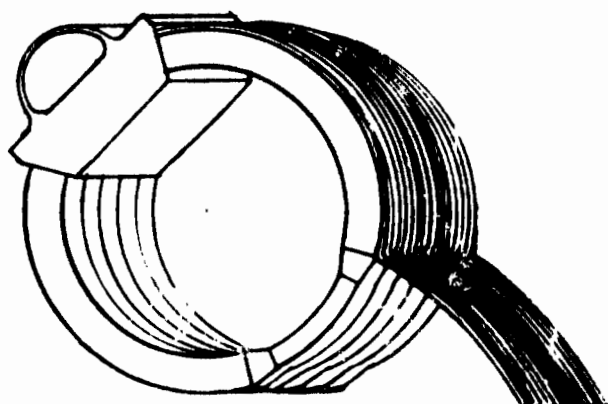
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The subsonic tube configuration alleviates all the problems of the sonic tube. An efficient structural member is placed in the subsonic region of the combustor where disturbances to the flow are negligible, and where the peak heat load is less than at the continuous annular throat. The disadvantages of this concept are increased weight and complexity of the structure and cooling system.

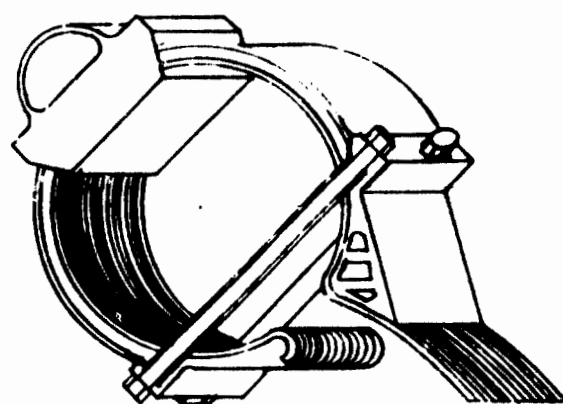
The full baffle annular combustion chamber is the highest performing configuration and the peak heat flux is minimum. A continuous annular throat is formed with rows of thin walled tubing. Structural support is provided by cooled baffles and a variety of external structure types. This chamber type is the heaviest of the three but it is relatively simple in construction concepts.

Many variations of these basic designs have been considered and are continually being improved upon at Rocketdyne. It should be noted that the complete annular engine may be formed by a number of independent straight or curved combustor segments or as a continuous single circular unit. The building block engine concept has many advantages which become more important as the total engine size increases.

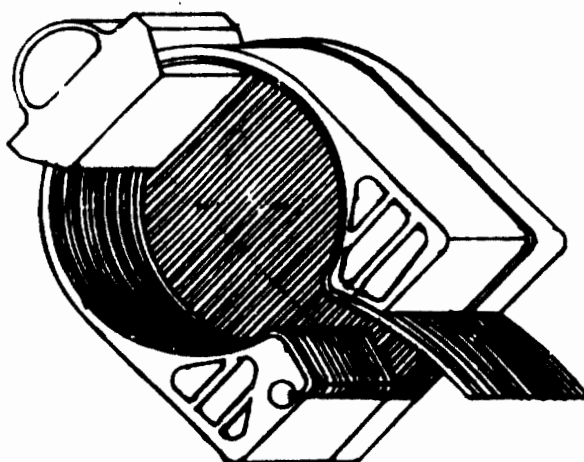
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SONIC TUBE



SUBSONIC TUBE



FULL BAFFLE ANNULAR

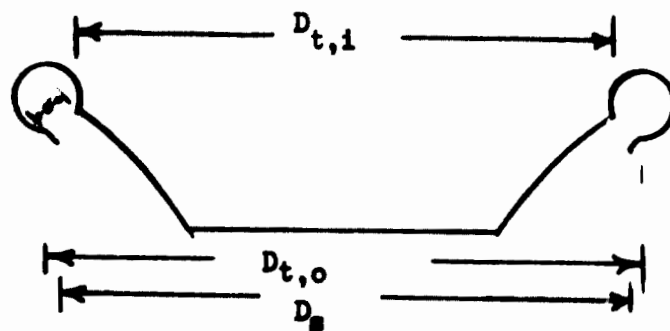
Fig.113. Toroidal Combustor Configurations

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Toroidal Combustor Geometry

The toroidal aerospike engine is geometrically unique from the multi-chamber configuration or the conventional engine in that the nozzle area ratio is determined by the throat geometry. This can be seen by the equations below which are applicable to a circular continuous annular throat. The symbols are illustrated in the sketch below.



Shrouded Aerospike Geometry

$$A_t = \pi \delta (D_{t1} + D_{to})/2 \rightarrow \pi \delta D_{to}/2$$

$$A_o = \pi D_o^2/4 \rightarrow \pi D_{to}^2/4$$

$$\epsilon = A_o/A_t \rightarrow D_{to}/2\delta$$

At a given thrust level and chamber pressure (A_t) the area ratio and throat gap are determined by the throat (engine) diameter. More exact relationships for various toroidal configurations (e.g. sonic tube throats and straight chamber segments) may be found in Ref. 17 .

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Multichamber Configurations

There are probably as many variations of the multichamber concept as there are of the toroidal concept. The basic theme of this configuration is to utilize existing engine technology in the construction of an advanced annular engine. This concept consists of conventional combustion chambers clustered around a central aerospike nozzle as shown in Fig. 114 .

This configuration provides some of the altitude compensating characteristics of aerospike nozzles while allowing a conventional approach to the design of those components of the engine which produce a major portion of the total thrust. The principal disadvantage to this concept is that performance is considerably below that which can be achieved with a continuous annular throat. To achieve the desired high performance annular flow configuration, the nozzle portion of the conventional chamber may be modified in various degrees as shown in Fig. 115 . As the nozzle exits approach the annular shape, the nozzles approach a two-dimensional configuration. The advantages of the flat exit modules are that flow impingement losses are minimized and that (this will be discussed in the next section) a high engine area ratio can be achieved with a low module area ratio. This allows the flow to be exposed to ambient pressure sooner and hence a higher degree of altitude compensation capability is achieved. The major disadvantages of the two-dimensional module are (1) long length is required to achieve a high theoretical thrust efficiency, (2) frictional losses are increased by the large module surface area, (3) performance losses are caused by rotational flow in the module, and (4) structural requirements are severe.

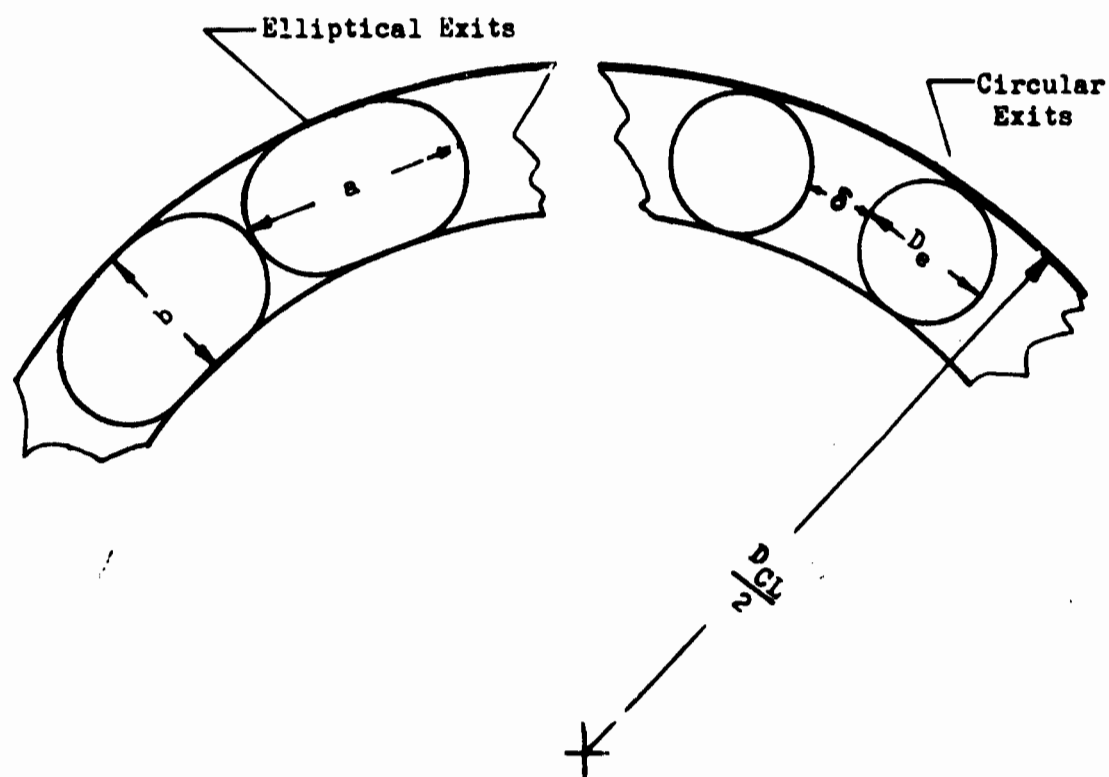
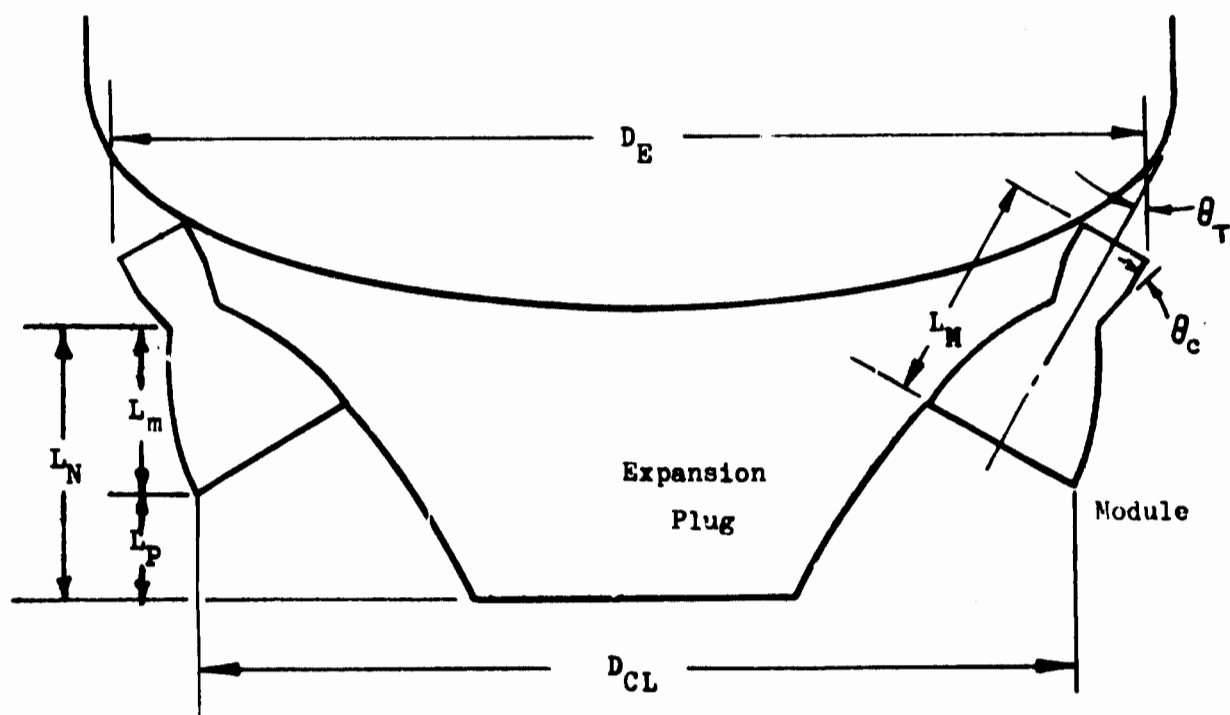
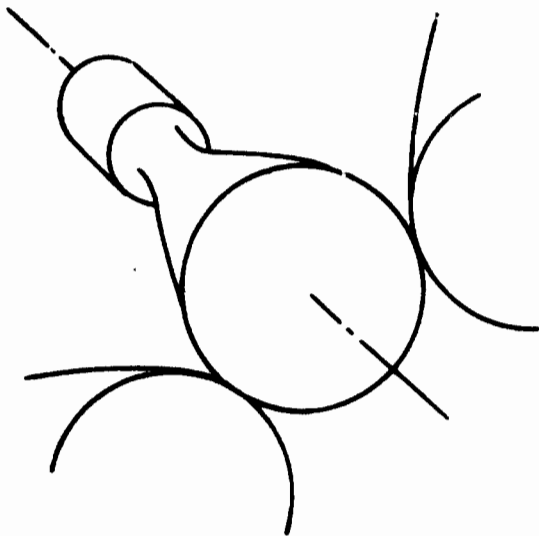
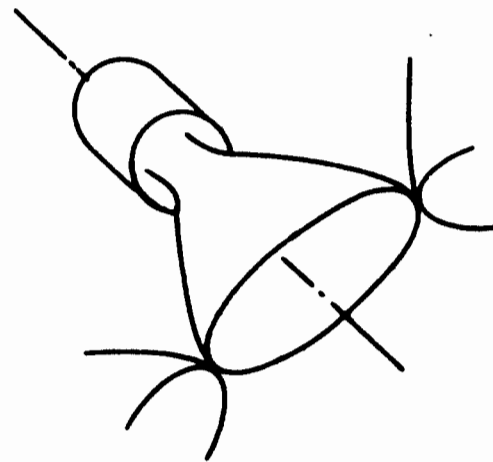


Fig. 114 Multichamber Nomenclature

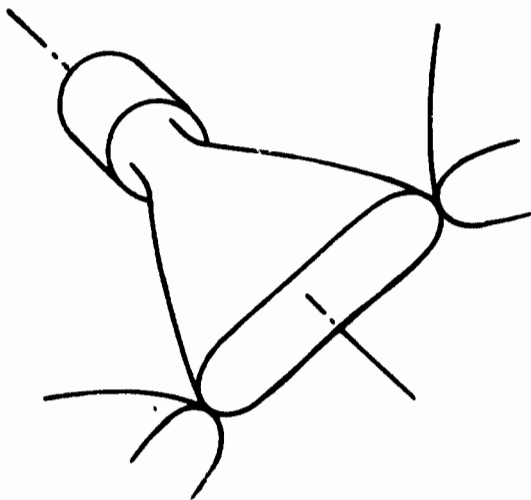
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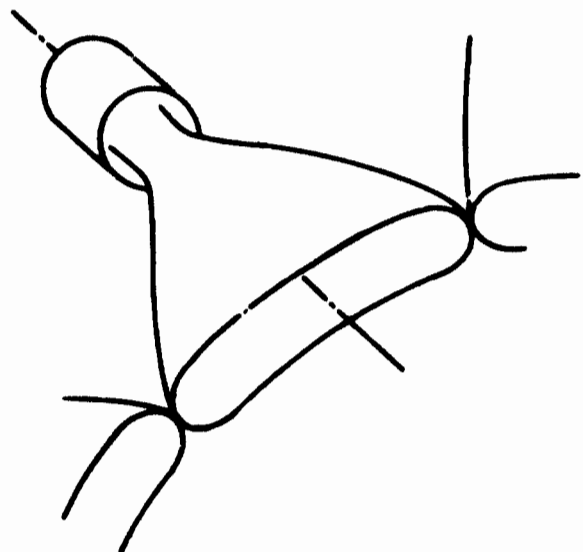
Circular Exits



Conventional Elliptical Exits



Straight Elliptical Exits



Curved Elliptical Exits

Figure 115 Advanced Modular Exit Shapes

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Multichamber Combustor Geometry

The principal characteristics of multichamber systems are the number of modules, the module expansion area ratio, and the system geometric area ratio, the latter being equal to the circular area enclosing the module exit (i.e., $\pi D_{CL}^2/4$ in Fig. 114) divided by the total throat area. These parameters are, in turn, governed by the shape of the module exits, the spacing between modules, and the inclination or "tilt" angle of the individual modules.

The relationship between the modules and the overall system is generally expressed in terms of an "amplification factor," representing the ratio of the system area ratio to the module area ratio. For circular module exits, this factor is

$$\frac{\epsilon_{CL}}{\epsilon_M} = \frac{1}{N} \left[\frac{(1 + \delta/D_o) \cos \theta_T}{\sin \left[\arctan (\cos \theta_T \tan \frac{180}{N}) \right]} + \cos \theta_T \right]^2$$

Where N = number of modules
 ϵ_{CL} = system geometric area ratio
 ϵ_M = module area ratio
 δ, θ_T are as indicated in Fig.

The variation of amplification factor with gap spacing and numbers of modules for circular exit modules with $\theta_T = 20$ and 10 degrees is shown in Figs. 116 and 117. Tilt angle has only a small effect on amplification factor; these data are therefore representative over the general range of interest, from approximately 5 to 30 degrees. The curves illustrate

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Tilt Angle = 20 degrees

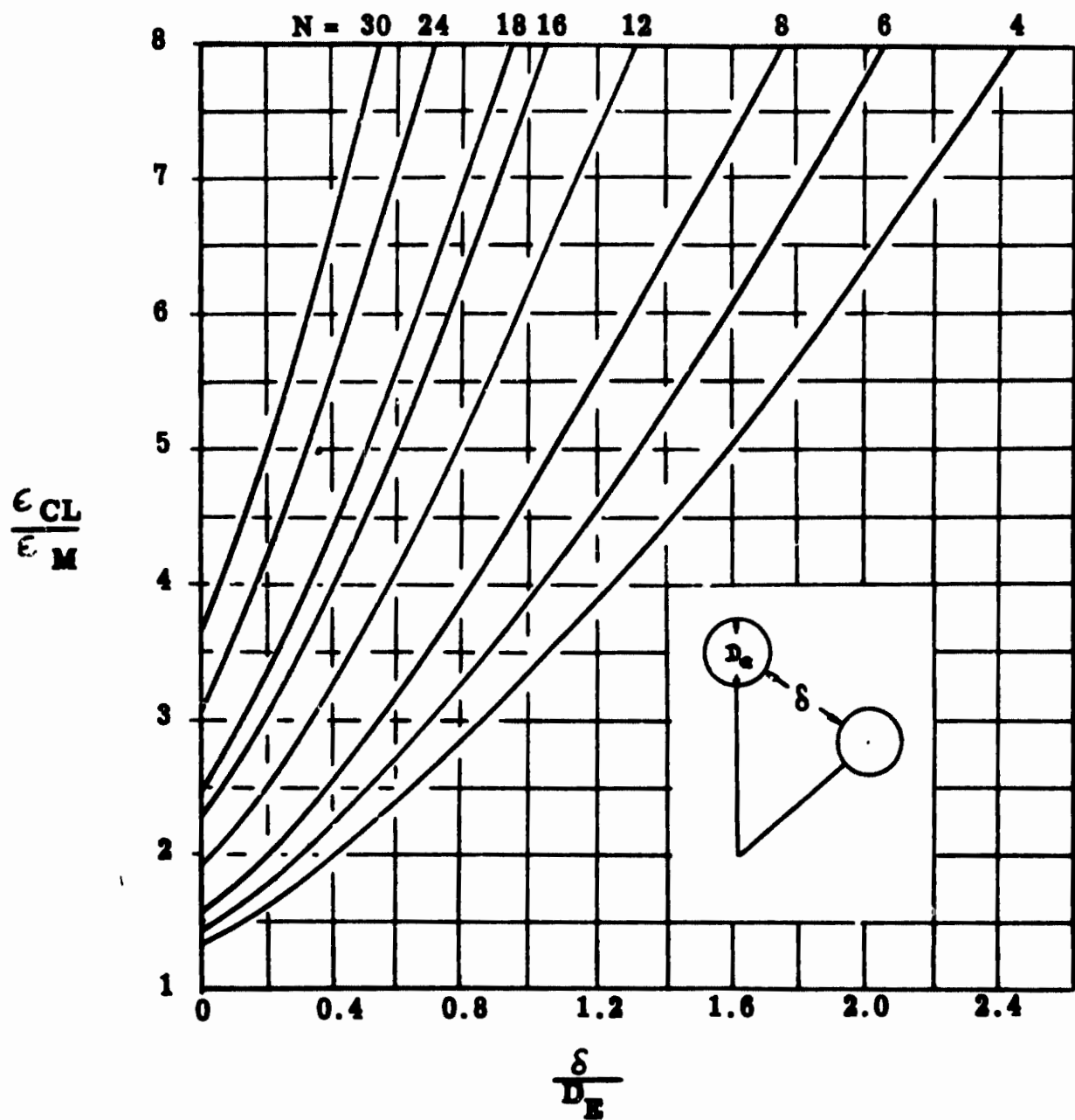
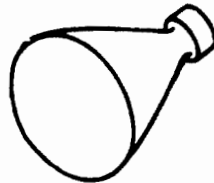


Figure 116. Geometric Amplification Factor as a Function of Circular Gap Spacing Ratio and Number of Modules

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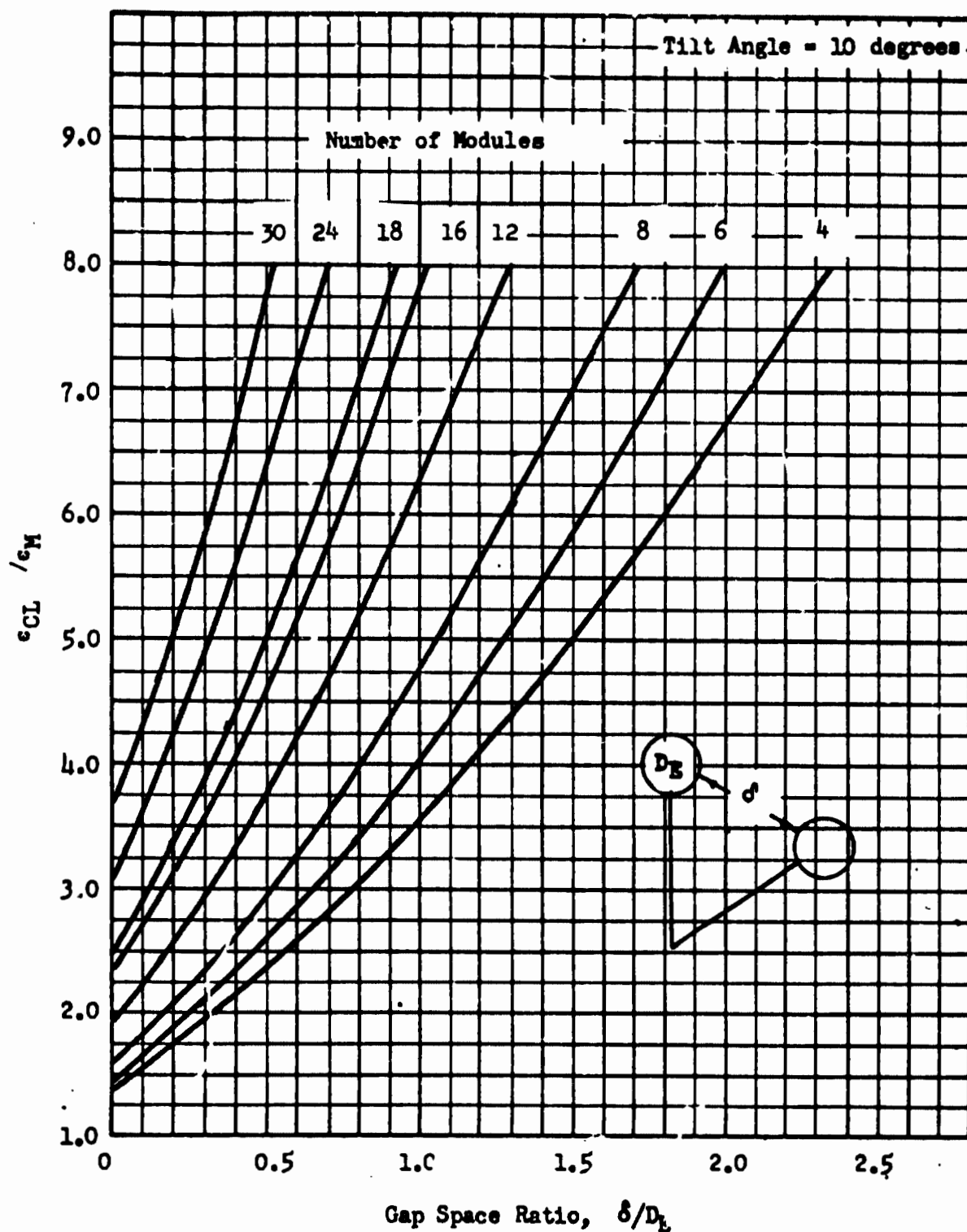


Figure 117. Geometric Amplification Factor as a Function of Circular Gap Spacing Ratio and Number of Modules

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that high amplification factors may be achieved by either increasing the number of chambers or increasing the spacing between chamber exits.

Amplification factors for the non-circular exit shapes shown in Fig. 115 are presented in Fig. 118 as a function of the slenderness ratio, a/b , and number of modules. The governing equations for these systems are shown below.

Conventional Elliptical Exit Shape

$$\frac{\epsilon_{CL}}{\epsilon_H} = \frac{1}{N} \left[\sqrt{\frac{a}{b}} \cot \frac{180}{N} + \sqrt{\frac{b}{a}} \cos \theta_T \right]^2$$

Straight Elliptical Exit Shape

$$\frac{\epsilon_{CL}}{\epsilon_H} = \tan \frac{180}{N} \left[\frac{a/b}{\tan \frac{180}{N}} + \cos \theta_T \right]^2 / 4(a/b - 1) + \pi$$

Curved Elliptical Exit Shape

$$\frac{\epsilon_{CL}}{\epsilon_H} = \frac{\frac{1}{\pi} \left(\frac{a}{b}\right)^2 N^2 + 2 \frac{a}{b} N \cos \theta_T + \cos^2 \theta_T}{\pi N \left[1 + \frac{4}{\pi} \left(\frac{a}{b} - 1\right) \right]}$$

It is important to note that although amplification factors for the non-circular systems are higher than for corresponding circular-exit configurations, system studies such as Ref. 12 have indicated that the disadvantages cited previously tend to offset the potential benefits of non-circular systems.

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Tilt Angle = 20 degrees Modules Touching

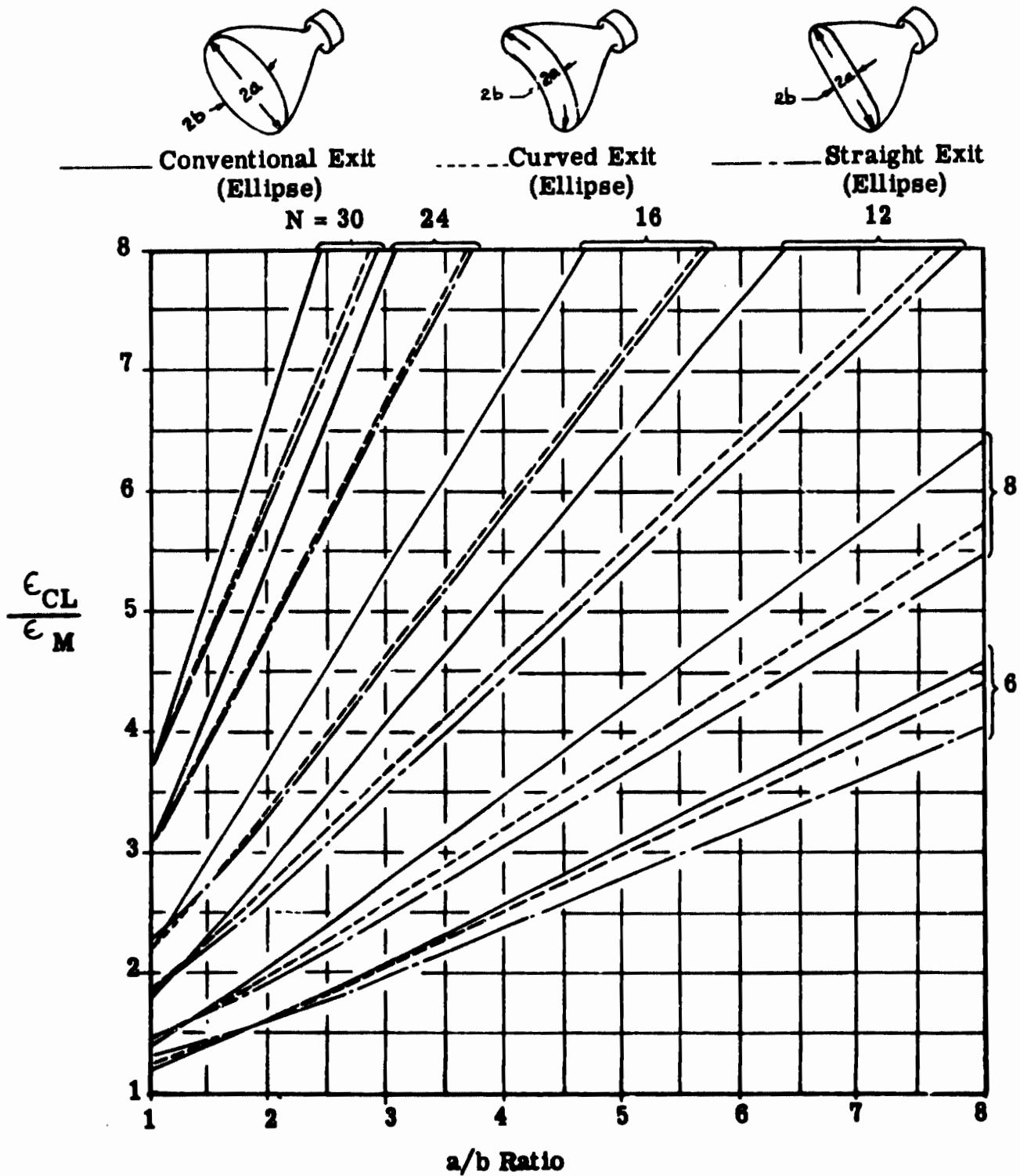


Figure 118 Amplification Factor as a Function of Ellipse Ratio and Number of Modules

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ENGINE AND VEHICLE ENVELOPE REQUIREMENTS

The range of chamber pressure (500 psia to 3000 psia), thrust level (20K to 2000K), and area ratio (to 150) investigated in this study encompasses a wide range of engine and vehicle diameters. Therefore some approximate dimensional studies were made to gain some initial insight into the relative engine and vehicle sizes being considered and the effect of chamber pressure, area ratio, and thrust level on relative engine and vehicle envelope.

Figure 119 shows the relative engine and combustor dimensions to scale for a group of toroidal engines of 150 area ratio over the thrust range from 20,000 to 2,000,000 pounds. The same relative dimensions are approximately applicable to multichamber configurations. The combustion chamber diameters are sized to be a minimum of six inches and/or provide a chamber characteristic length greater than 30 inches. It can be seen that at low thrust levels, high chamber pressures and high area ratios, the combustor dimensions become a significant fraction of the engine diameter.

The diameters of a number of existing vehicles and preliminary design vehicles utilizing $\text{H}_2\text{O}_4/\text{UDMH-H}_2\text{H}_4$ (50-50) propellants were correlated with thrust as shown in Fig. 120. The straight lines represent a variation of vehicle diameter with the cube root of engine thrust which is an approximate relation in frequent use. These correlation lines were superimposed on plots of toroidal engine diameter vs. chamber pressure shown in Fig. 121, 122, and 123. These curves are also roughly applicable to multichamber engines. The data indicates that for the range of area ratios, chamber pressures, and thrust levels considered it is unlikely that a vehicle envelope will seriously restrict the selection of optimum engine operating pressure and area ratio. A comparison of the trends of vehicle and engine diameter with thrust level does indicate that the selection of area ratio and chamber pressure tends to become more restricted as thrust level increases.

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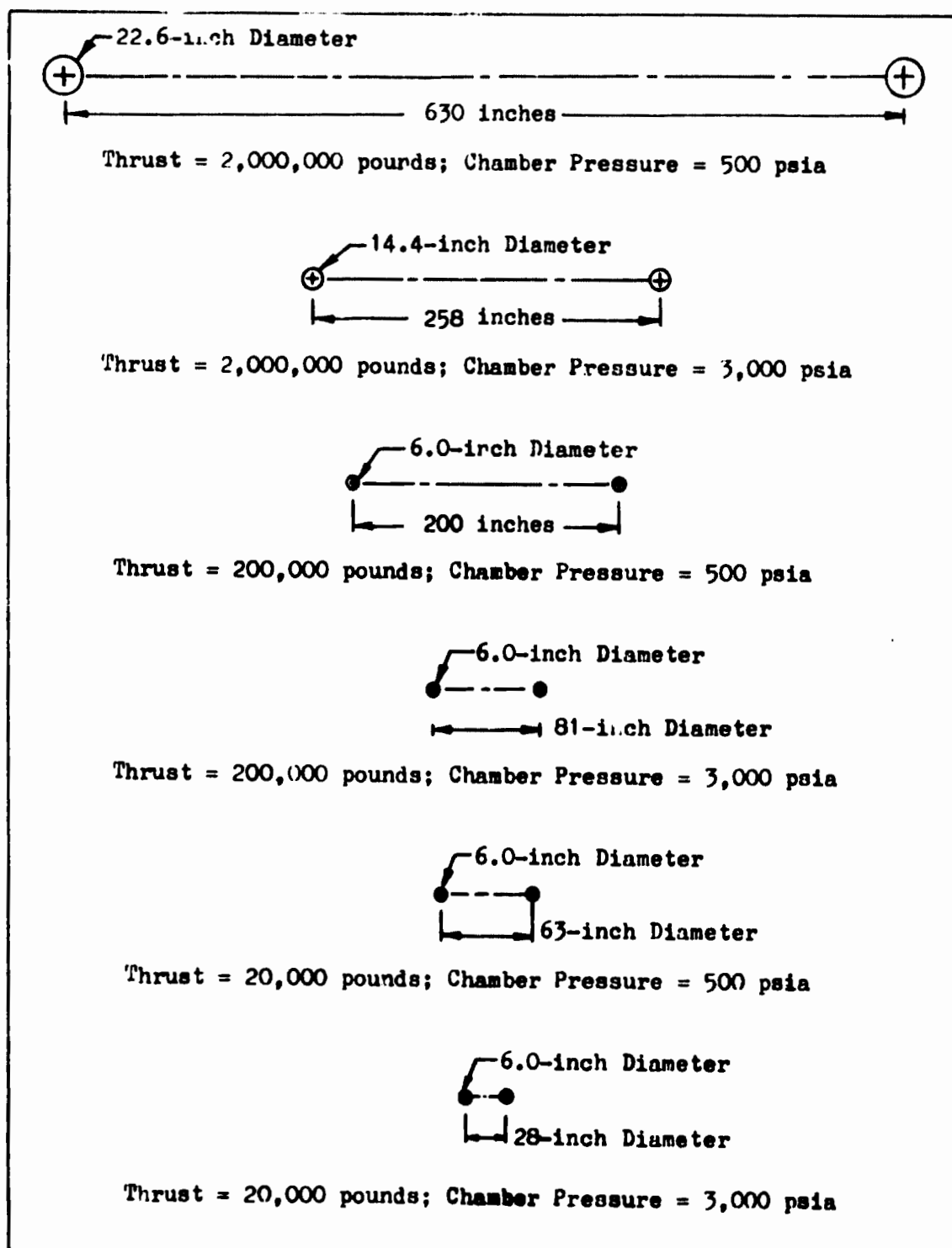


Fig. 119 Limit Combustor Dimensions, $\epsilon = 150$

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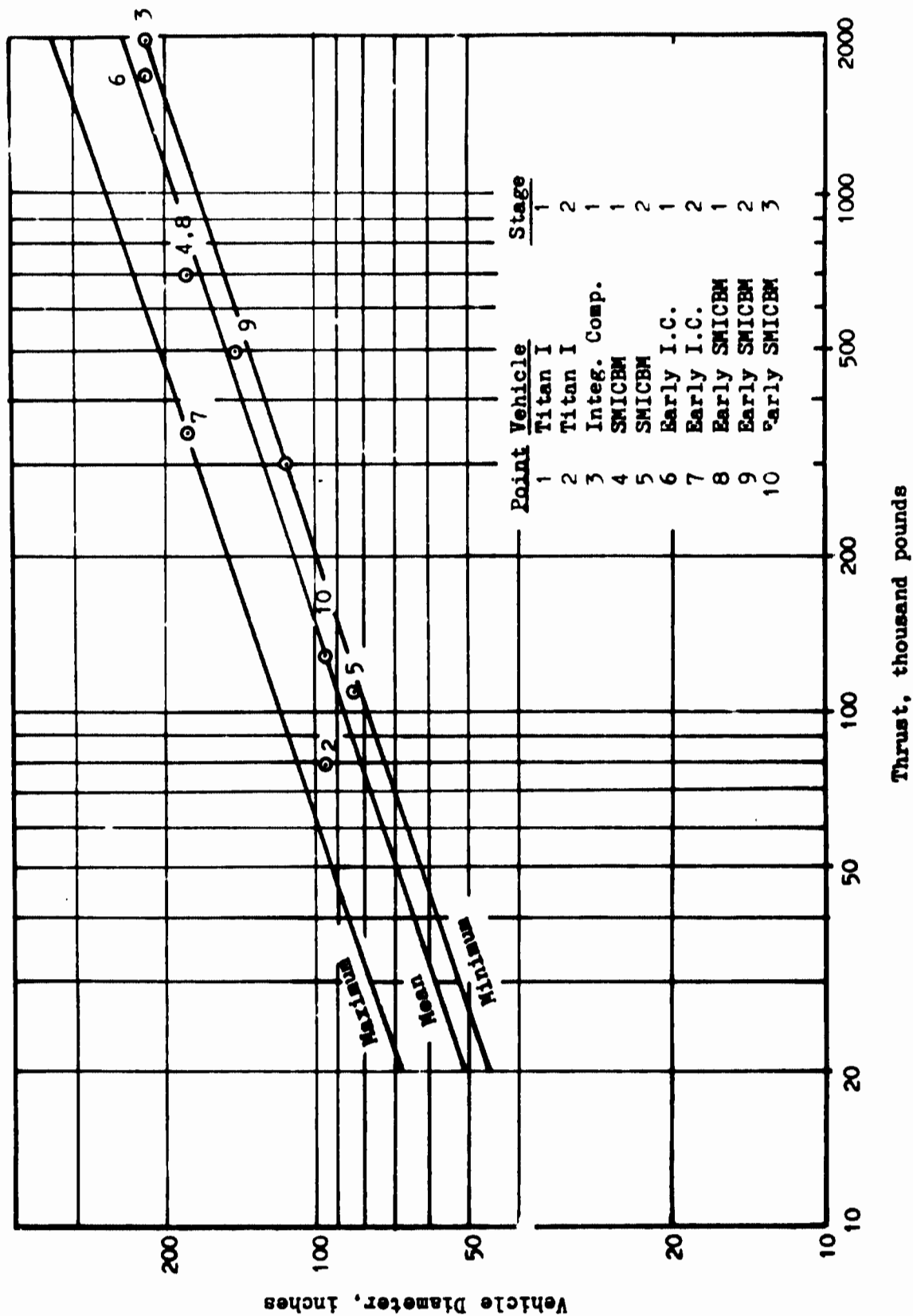


Fig. 120 Vehicle Diameter Correlation with Stage Thrust

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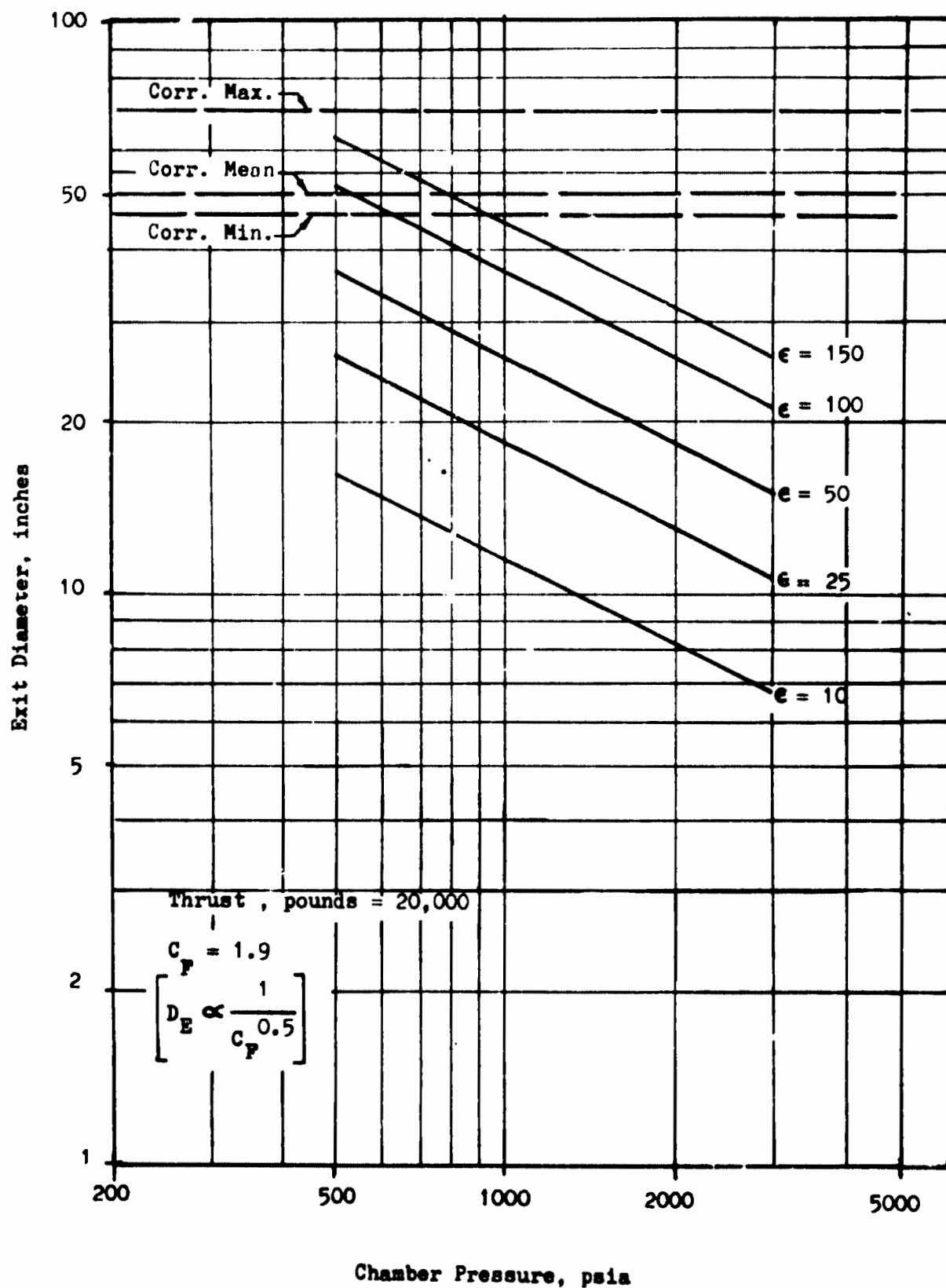


Fig.121 Toroidal Engine Envelope($F = 20,000$ pounds)

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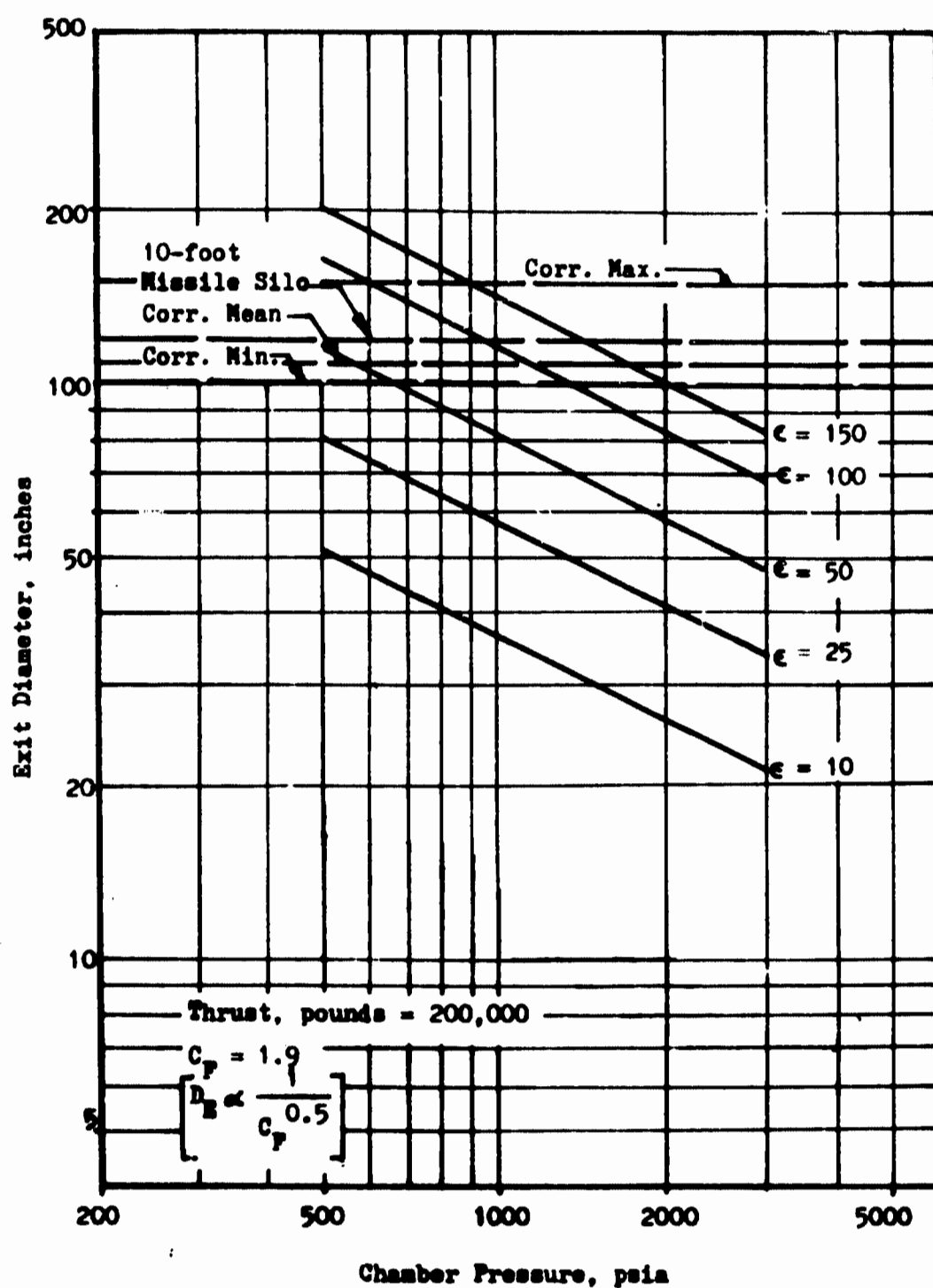


Fig. 22. Toroidal Engine Envelope ($F = 200,000$ pounds)

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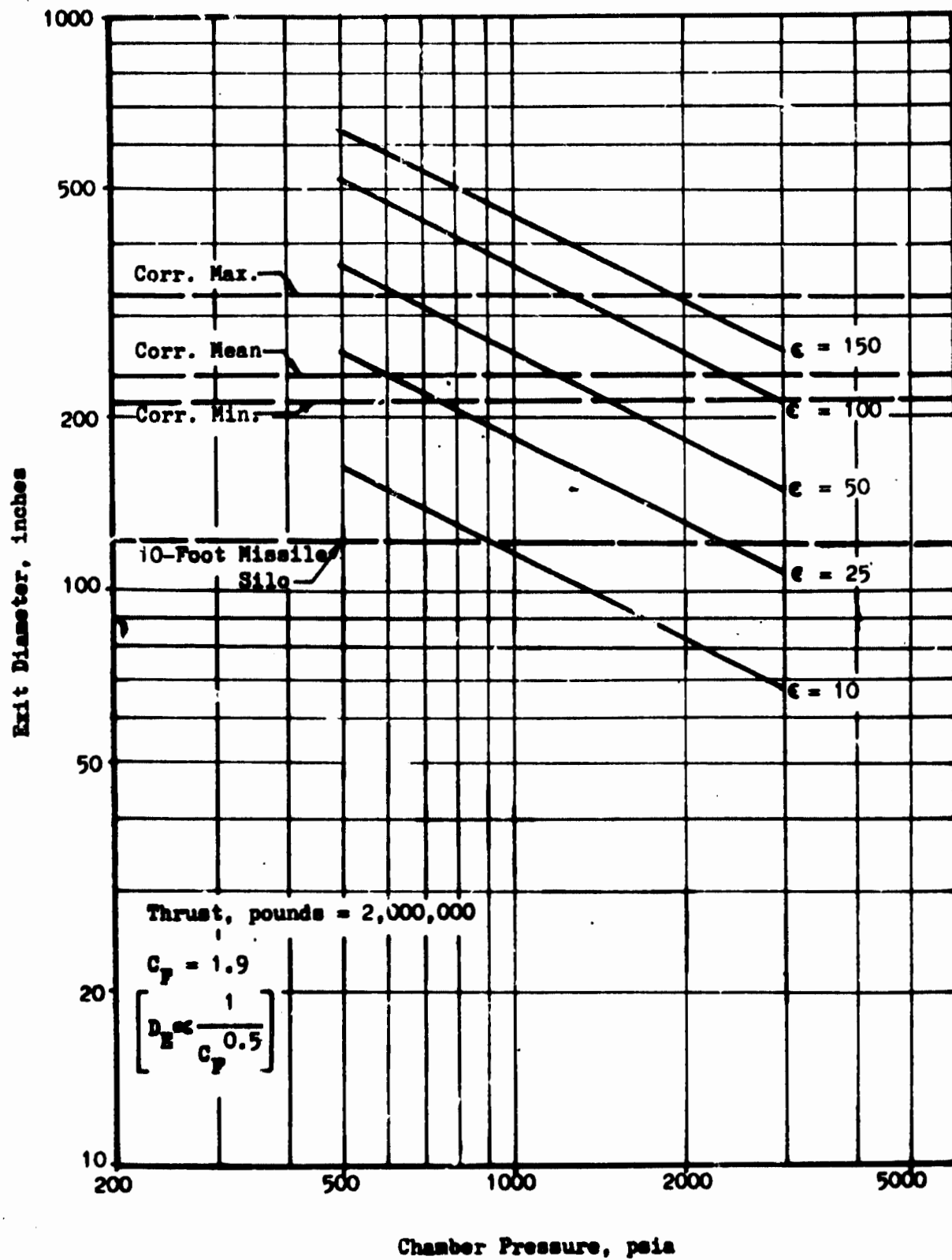


Fig 123 Toroidal Engine Envelope ($F = 2,000,000$ pounds)

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PERFORMANCE

In this section the effects of geometrical nozzle and combustor parameters on advanced aerodynamic spike configurations are discussed. The discussion is limited to the partial effect of each of these parameters as has been established from empirical and analytical studies conducted under this and other contracts. The interrelationship of these parameters and their optimization through system or mission studies was outside the scope of this study. A review of current performance analysis techniques is also presented.

Combustor Geometry Effects

The combustor geometry affects the combustion and gas expansion performance of the thrust chamber. The combustion efficiency (η_{C_e}) is chiefly a function of the injector design and is affected by the combustion geometry to a lesser degree. In the present discussion it is assumed that the main effect of combustion geometry is upon expansion efficiency, η_{C_F} (or C_T) and that the combustor concepts considered, toroidal and multichamber, have been designed (or developed) to attain equal combustion efficiencies.

Toroidal Configurations. Four configurations of the toroidal combustion chamber concept as shown in Fig. 113 have been examined in detail; the sonic tube, the subsonic tube, the full baffle annular, and the sunular. In all of the first three configurations structural members (inserts) are allowed to extend across the combustion chamber introducing disturbances in the flow of the gases. Proper shaping of the insert surface is possible in all cases to minimize the disturbance introduced.

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For the case of the annular toroidal configuration the expansion efficiency losses are only those caused by friction drag on the nozzle wall and by streamline divergence losses at the nozzle exit plane, as there is no disturbance of the potential flowfield in the combustion chamber.

The circular-type subsonic tube toroidal configuration disturbs the potential flowfield, but because this disturbance occurs in the subsonic regime of the flow, and because the spacing between tubes is larger (than for sonic tubes) the losses sustained by this configuration are of relatively small magnitude. Five tenths of one percent decrease in C_T was experienced in testing of a 240 subsonic tube unit of tube spacing-to-tube diameter ratio (s/d) of approximately one. These losses are caused by friction and pressure drag developed on the tube surface, and by disturbance of the throat flow (sonic line) which affects the pressure on the nozzle wall and the base pressure. Larger spacings (s/d) lead to reduction of all four forms of performance degradation. Proper contouring of downstream tube surfaces, as will be shown for the case of the sonic tube, lead to further reduction of performance losses.

The higher expansion performance losses are experienced by the circular-type sonic tube toroidal configuration. The disturbance in the flow for this configuration takes the form of increased boundary layer surface area, separation of the flow behind the tubes, shocks, and disturbance of the sonic line. Theoretical work on this configuration has shown that increasing the tube spacing leads to reduction of expansion performance losses, and that for any tube spacing the performance losses can be reduced to tenths of one percent through incorporation of ideally contoured trailing edges in the space immediately behind the tubes.

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These trailing surfaces prevent flow separation with associated shock disturbances, reducing thusly the pressure drop, and the shock stagnation pressure losses. Though surface area is increased, the reduction in pressure drag and stagnation pressure losses offset noticeably the increase in friction drag.

The lower losses in performance of sonic tube configurations are obtained through the incorporation of a full length ideally contoured trailing edge. Heat transfer and fabrication considerations, however, dictate the allowable length for the trailing edge. The ideally contoured baffle length can be truncated in a manner depicted in Fig. 125, without sacrificing excessively in performance. This latter point is illustrated in Fig. 126, a graph of nozzle expansion efficiency η_{c_p} as a function of nozzle area ratio for the ideally contoured trailing surface, at various degrees of truncation. Even for the most severe degree of truncation considered, h/D_t of 0.103, the performance loss is not higher than 0.35 percent for a tube spacing ϕ/d_t of one, and gas specific heat ratios of 1.15 to 1.25. The loss indicated is the sum of divergence and pressure drag losses incurred in the combustion chamber through deformation of the inviscid flow field. This net loss is a function of the tube and throat geometry and constitutes a fixed loss in thrust coefficient which is not recoverable in the supersonic portion of the nozzle, but is rather dissipated in the shock and viscous flow structure downstream of the tubes. As the value of this loss is fixed, an increase in overall expansion area ratio makes it a diminishing fraction of the overall thrust coefficient.

Friction drag losses for the toroidal combustion chamber using tapered sonic tubes have been shown to be nearly equal to losses in the annular toroidal combustion chamber. This may be arrived at from the following observations: drag upstream of the geometric throat (subsonic flow

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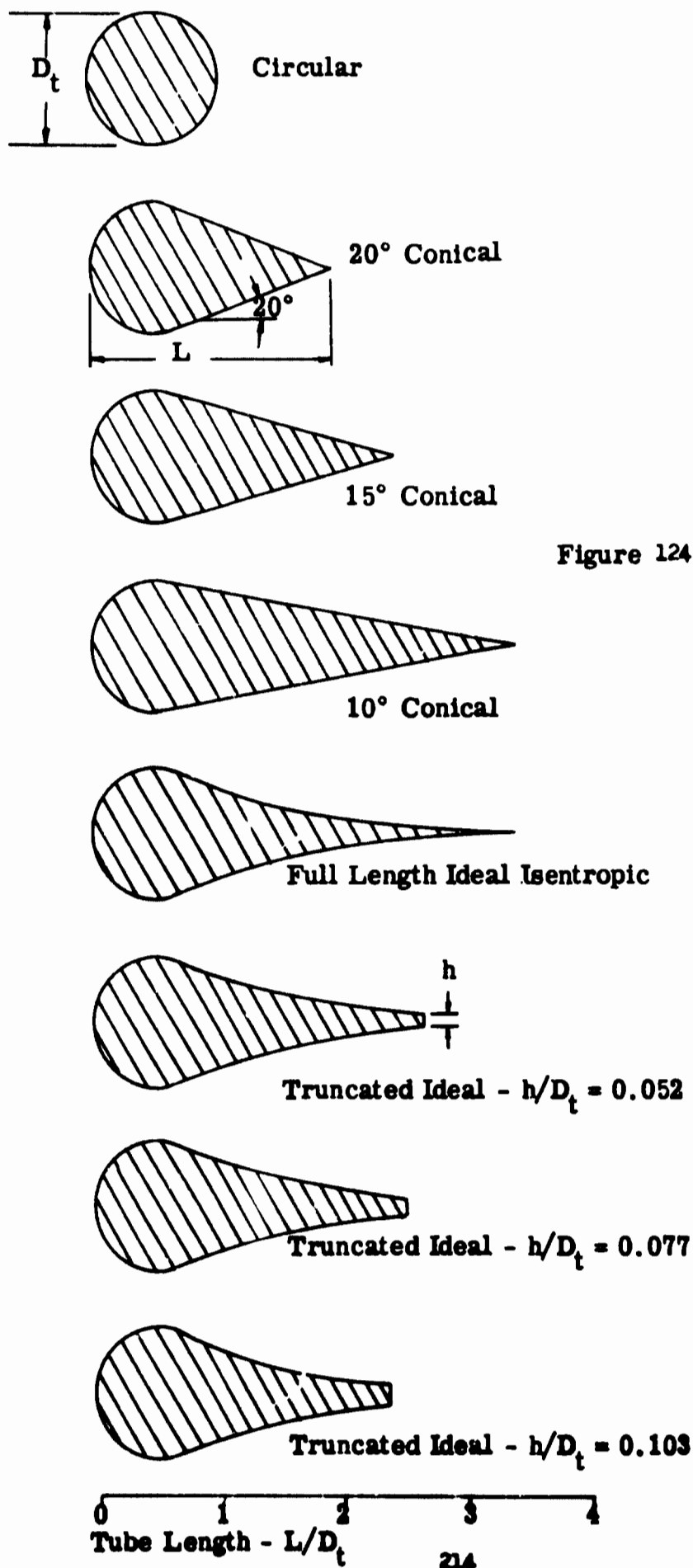


Figure 124. Toroidal Throat Tube Contour Shapes

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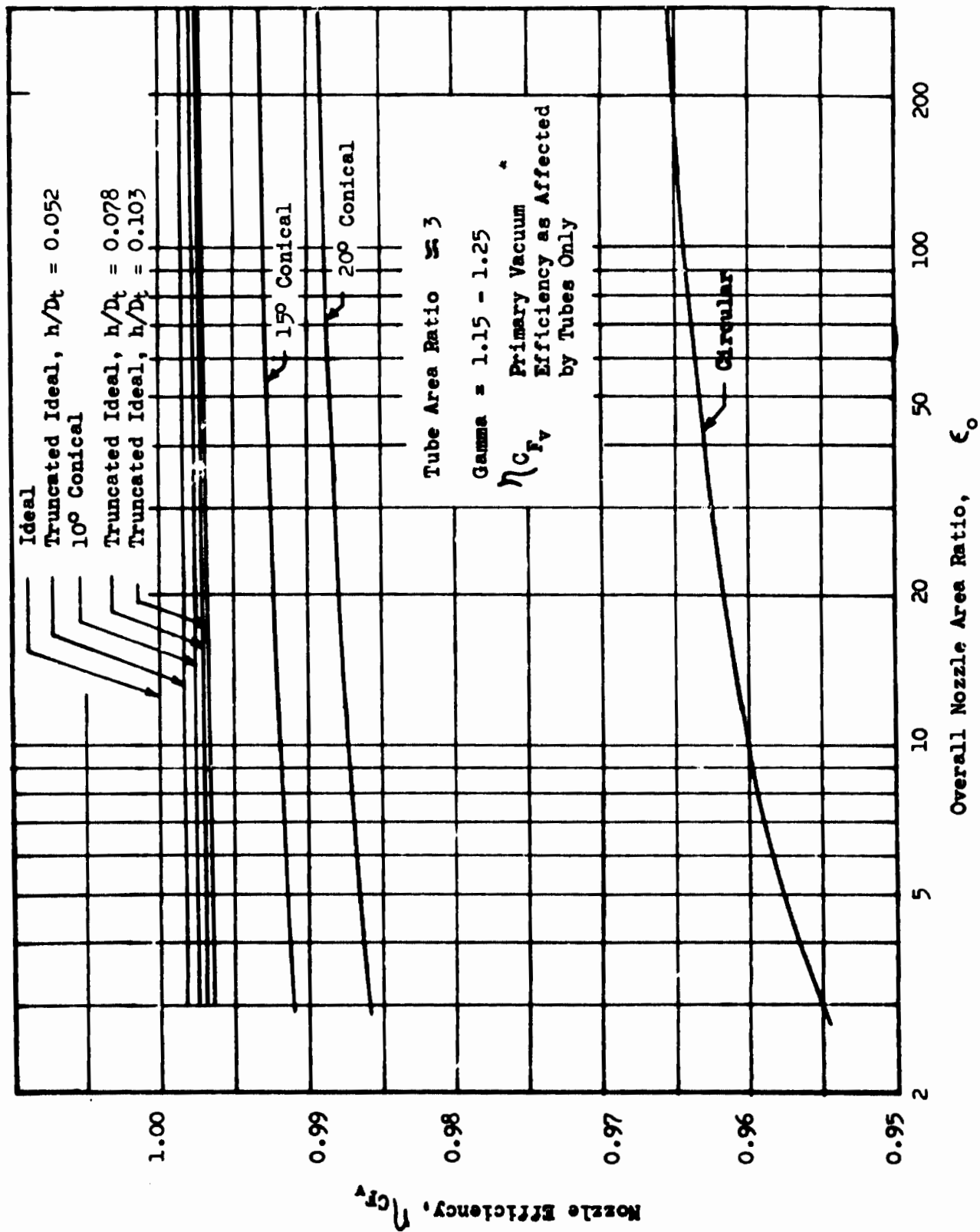


Fig. 125. Effect of Sonic Throat Tube Shapes on Vacuum Efficiency

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region) of either configuration is negligible, tapered sonic tubes present a large wetted surface area (drag is directly related to surface area) but allow a significant reduction in nozzle axial length when expanding to equal flow conditions. The result is that drag losses for equivalent annular and tapered sonic tube toroidal configurations are essentially equal. Typical values calculated for LOX-H₂ annular and sonic tube toroidal systems with overall expansion area ratio of 6 are shown in the table below.

TABLE 8

Comparison of Toroidal Chamber Drag Losses

	Annular	Tube - 15° Conical Trailing Surface
Tube Area Ratio (ϵ_t)	0	2.96
Overall Area Ratio (ϵ_o)	6.00	6.00
Ideal Thrust Coefficient (C_F)	1.6811	1.6811
Contour Drag Loss (ΔC_{F_D})	.0170	.0064 (from $\epsilon =$ 2.96 to 6.00)
Tube Drag Loss (ΔC_{F_D})	0	.0113
Total Friction Drag (% Ideal C_F)	1.01	1.05

From the above discussion it follows that the differences in performance indicated in Fig.125 between the ideal and the various toroidal tube configurations also represent the differences between toroidal-tube and full annular toroidal combustion chambers including drag losses.

For comparison the losses to be expected for a circular type sonic tube and for tubes having conical trailing edges have also been included in Fig.125. Even a 20 degree conical trailing edge achieves a significant gain in performance over the circular sonic type (on the order of 2.5 percent).

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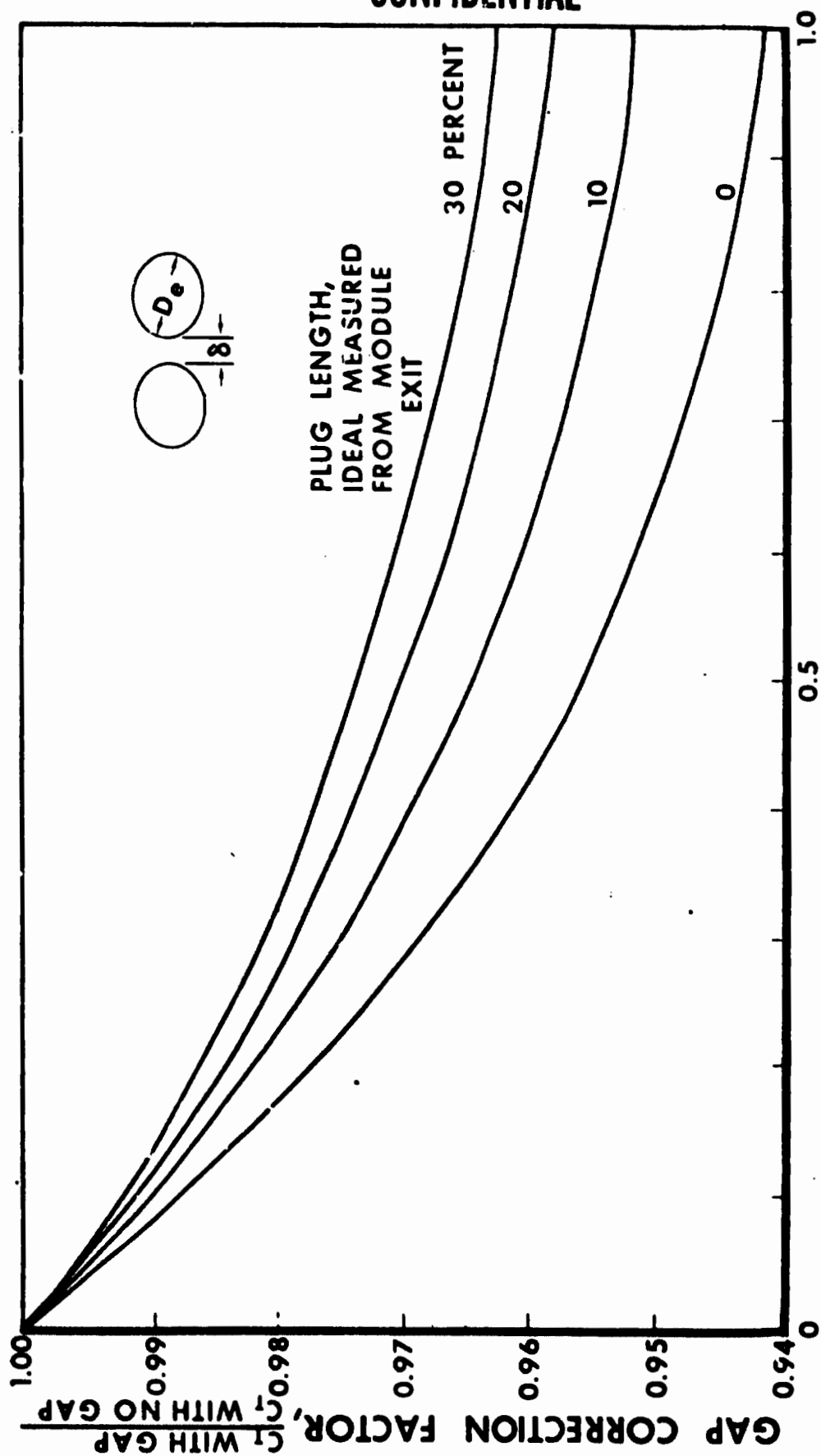
For equal combustion chamber conditions and equal insert cross-sectional area the performance loss due to pressure drag per structural member is of the same magnitude for both the untapered sonic tube (circular) and the baffled annular combustor configurations. Because of increased surface the friction drag is higher for the baffled annular configuration. The number of required baffles are however fewer than the sonic tubes or even the subsonic tubes, therefore making this configuration the less subject to expansion performance degradation. A 48-baffle unit tested in cold flow conditions with a baffle-to-baffle width ratio δ/w of 100:1 indicated performance losses of approximately 3 tenths of one percent. Calculated losses for this configuration were 0.23 percent.

Multichamber Systems

Module spacing and exit shape are the principal combustor variables affecting system performance. Experimental data defining the influence of these parameters are limited, however, estimates of the gap correction factor can be determined on the basis of cold-flow results from this program and from data presented in Ref. 3. The data shown in Fig. 126 indicate that substantial losses can be incurred in systems having sizable gaps between module exits, particularly in systems having short plug lengths. The reduction of these losses in longer systems indicates that some degree of recovery occurs.

Performance data for non-circular exit systems indicate no advantage relative to circular-exit configurations (Ref. 12). These data, however, were obtained for modules having circular-throat modules. Probable causes of this low performance are increased friction drag on the relatively large module surface area and rotational flow in the module induced by the transition from a circular throat to a nearly two-dimensional nozzle.

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GAP SPACING, δ/D_e

Figure 126. Effect of Module Spacing on Propulsion System Performance

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Nozzle Length

As is the case with bell and conical nozzles, increasing the length of toroidal aerospike configurations increases the nozzle (potential) performance, increases the drag losses, and increases the overall thrust chamber weight. Of course the rate at which all these quantities increase with length differs with the nozzle type. The nozzle length required for a certain application is obtained from mission-optimization studies. This section discusses the effect of nozzle length on expansion performance (C_p) without regard to mission or payload.

Toroidal Configurations. The basic toroidal configuration is the annular. It has been established through cold flow testing that the truncated ideal isentropic spike contour used in conjunction with the annular toroidal configuration is the highest overall performing of the contour types. Optimum contours (contours designed for maximum primary thrust in a given nozzle length) yield higher primary performance, but their lower base pressures make this configuration perform lower than the truncated ideal isentropic spike contour. Longer lengths would be required of optimum contours to achieve total performance equal to the truncated ideal spike.

To achieve full ideal expansion an isentropic spike nozzle must have a full length. This maximum length, expressed in terms of a 15 degree cone, increases with an increase in expansion area ratio, and with an increase in specific heat ratio. The same can be said of the truncated ideal spike nozzle contour. To achieve a given nozzle efficiency, longer truncated ideal spike contours are required as expansion area ratio increases, and as specific heat ratio increases. For given expansion area ratio and specific heat ratio increasing the nozzle length increases nozzle efficiency (C_p) continuously even when adding

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the optimum amount of secondary flow in the base of the aerospike. There is a length, however, beyond which the performance increases are not significant. This can be seen from Fig. 127 a plot of nozzle efficiency with secondary flow versus nozzle length for an expansion area ratio of 45 and a specific heat ratio of 1.4. Beyond a nozzle length of 30 percent (in terms of a 15 degree cone) the performance gains caused by increasing length are extremely small. As length increases the gains from secondary flow diminish as can be seen by comparing the "no secondary" and "with secondary" performance efficiency curves in Fig. 127. The secondary flow required for optimum performance is also reduced as the gains diminish. At a different area ratio and gamma (with different propellants) the length required for the above trends to repeat is however different.

Multichamber Systems. The aerodynamic performance of multichamber systems increases with increasing length in a manner similar to that noted in annular combustor systems. However, it is important to recognize that the length of a multichamber system is comprised of module length and a plug nozzle length; the plug nozzle length by itself is not an adequate indicator of system aerodynamic efficiency.

The cold-flow data generated in this program and the data presented in Ref. 12 were compiled to ascertain the relationship between design point aerodynamic efficiency, $C_{T_{des}}$ and plug length and number of modules. The resulting correlation is shown in Fig. 128. A locus of points representing any total system length could be superimposed on the data in Fig. 128; as shown by the typical example on Fig. 128, the result is a nearly constant C_T , with a gradual decay indicated as number of modules increases. It is evident that for plug lengths beyond approximately 15 percent (based on the length of an ideal spike), further increases in performance are small and number of modules has little effect on efficiency.

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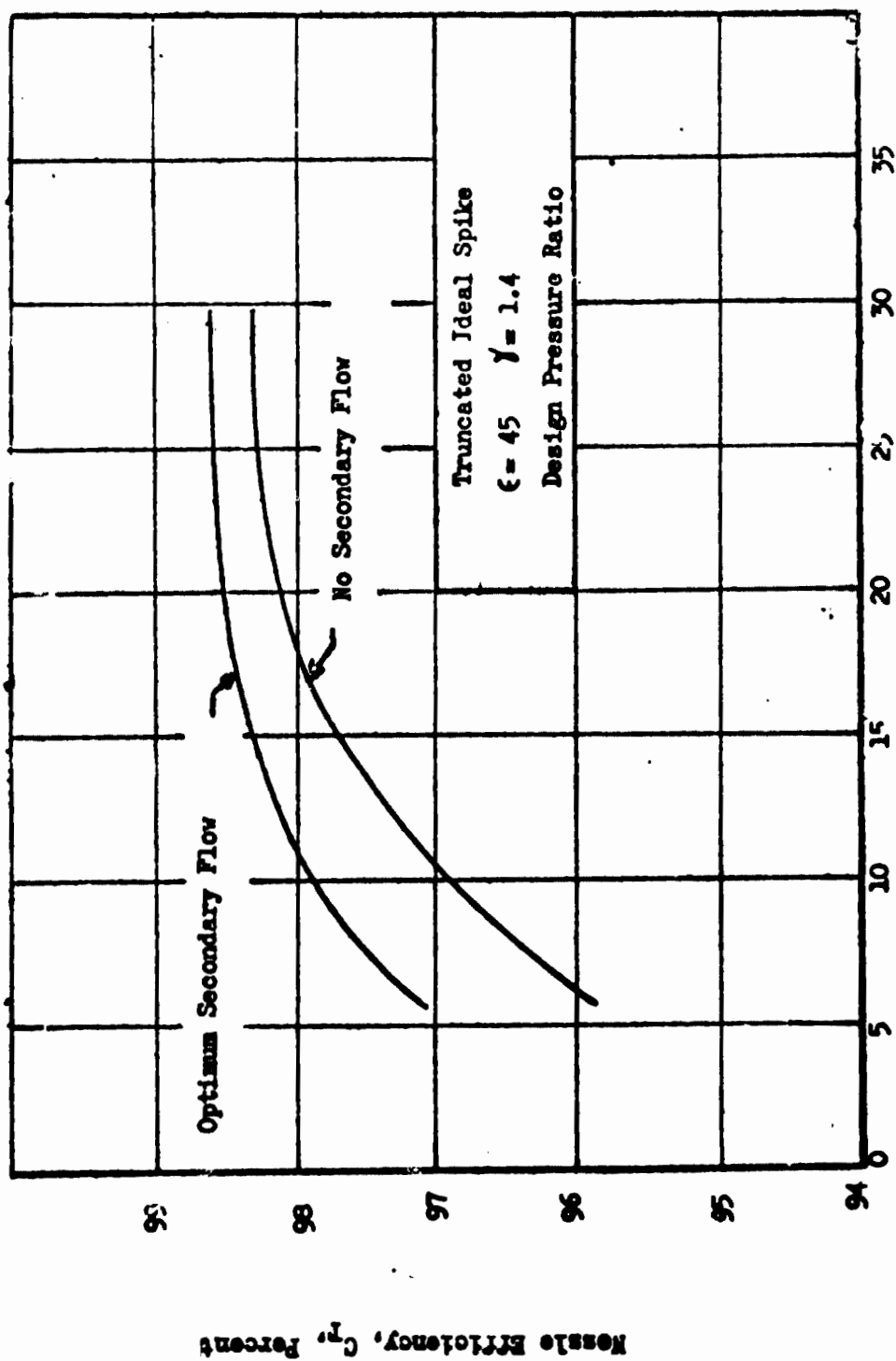


Fig. 127 Variation of Nozzle Efficiency with Length

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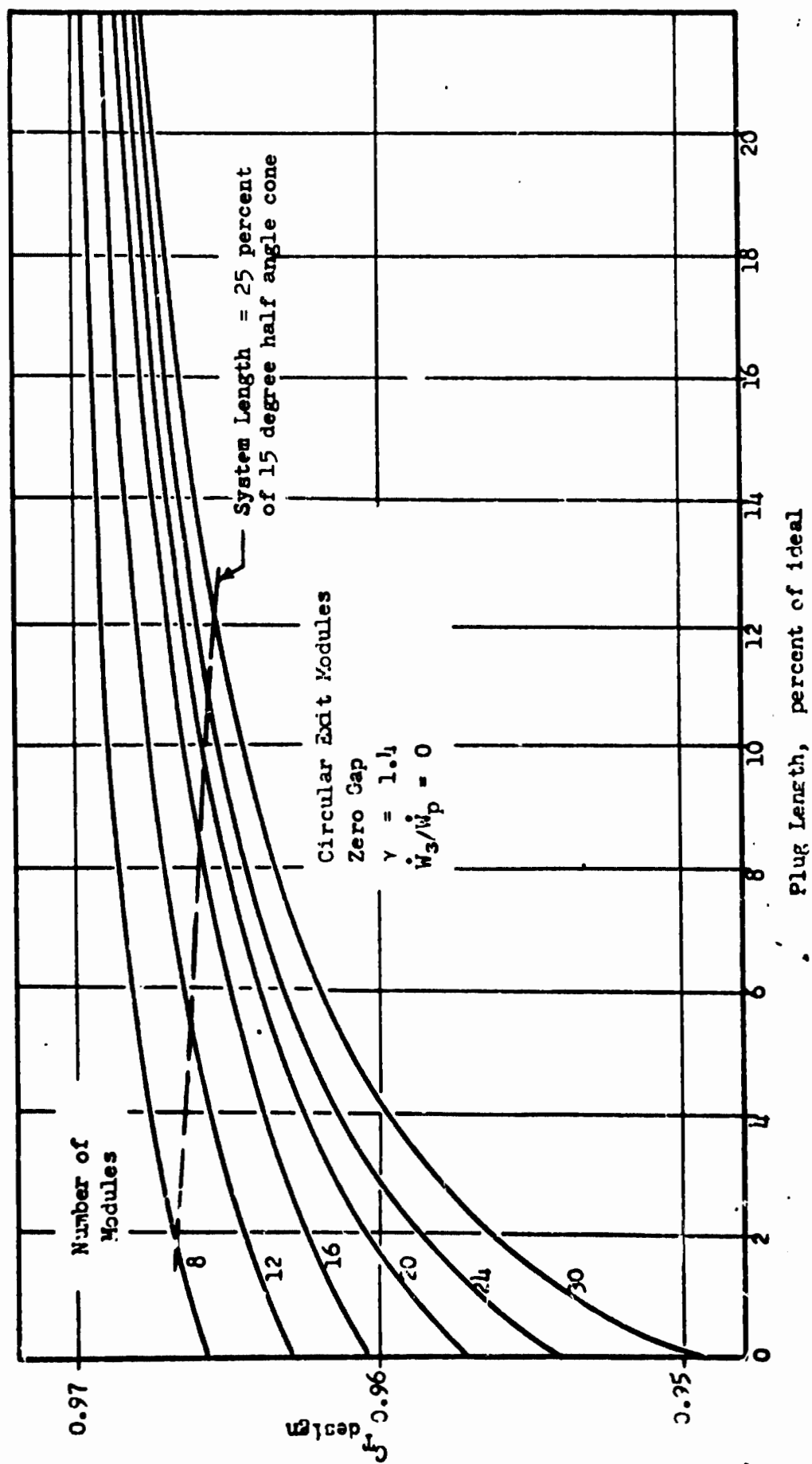


Figure 12a Effect of Plug Length and Number of Modules on Thrust Efficiency

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Performance Analysis Techniques

The performance analysis technique as developed at Rocketdyne for use with aerodynamic spike configurations is a collection of theoretical procedures and refined empirical equations which take into account inviscid primary performance, viscous primary losses, kinetic losses, base pressure without secondary flow, the effect of secondary flow and secondary flow properties on base pressure, and the effect of varying ambient pressure. Computer programs exist for the complete performance analysis of the toroidal and multichamber configurations. The main features of these programs and the techniques employed are reviewed briefly in the following subsections. For a complete discussion on these programs Ref. 18 and 19 are available.

Toroidal Configurations. The computer program for the annular toroidal aerospike configurations is capable of designing an ideal spike configuration for a given thrust or a given throat area utilizing any of the following three propellants; LOX-H₂, NTO-50-50, and LOX-RP; at the major mixture ratios of interest. The nozzle design is then subjected to a method of characteristics analysis which yields divergence losses for the primary flow at any operating pressure ratio, and a boundary layer analysis which yields friction drag losses. From built-in tables, kinetic losses are evaluated; and from empirical equations the base pressures are calculated. These separate contributions are then combined with the ambient pressure drag to obtain overall nozzle output in the form of thrust, nozzle thrust coefficient, and/or nozzle efficiency in vacuum. The basic equations used are:

$$(1) F = P_c A_t \left[C_{F_{i,v}} - \Delta C_{F_{div.}} - \Delta C_{F_{drag}} - \Delta C_{F_{kin.}} \right] + P_b A_b - P_a A_e$$

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$$(2) \dot{W}_T = \frac{P_{c_p} A_{t_p} g}{C_p} + \frac{P_{c_s} A_{t_s} g}{C_s}$$

$$(3) C_F = \frac{F}{P_{c_p} A_t [1 + \dot{W}_s / \dot{W}_p]}$$

Calculated values from use of these three equations can then be utilized to derive nozzle efficiency C_T or specific impulse efficiency η_{I_s} values for any pressure ratio, given a value of the combustion efficiency η_{C*} , and a suitable reference for thrust coefficient and specific impulse, i.e., $C_{F_{opt}}$ and $I_{s_{opt}}$. A flow diagram for the program is shown in Fig. 129. In the regime of pressure ratios where the ambient pressures influence the base pressure (open wake) the latter are not calculated in the program. Equations are given in Ref. 19 which will allow the calculation of the base pressure in the open-wake through use of any of two empirical techniques. Ref. 19 also gives a detailed description of theoretical and empirical equations used in the design and analysis of the toroidal aerospike overall performance, as well as a description of program operational procedures.

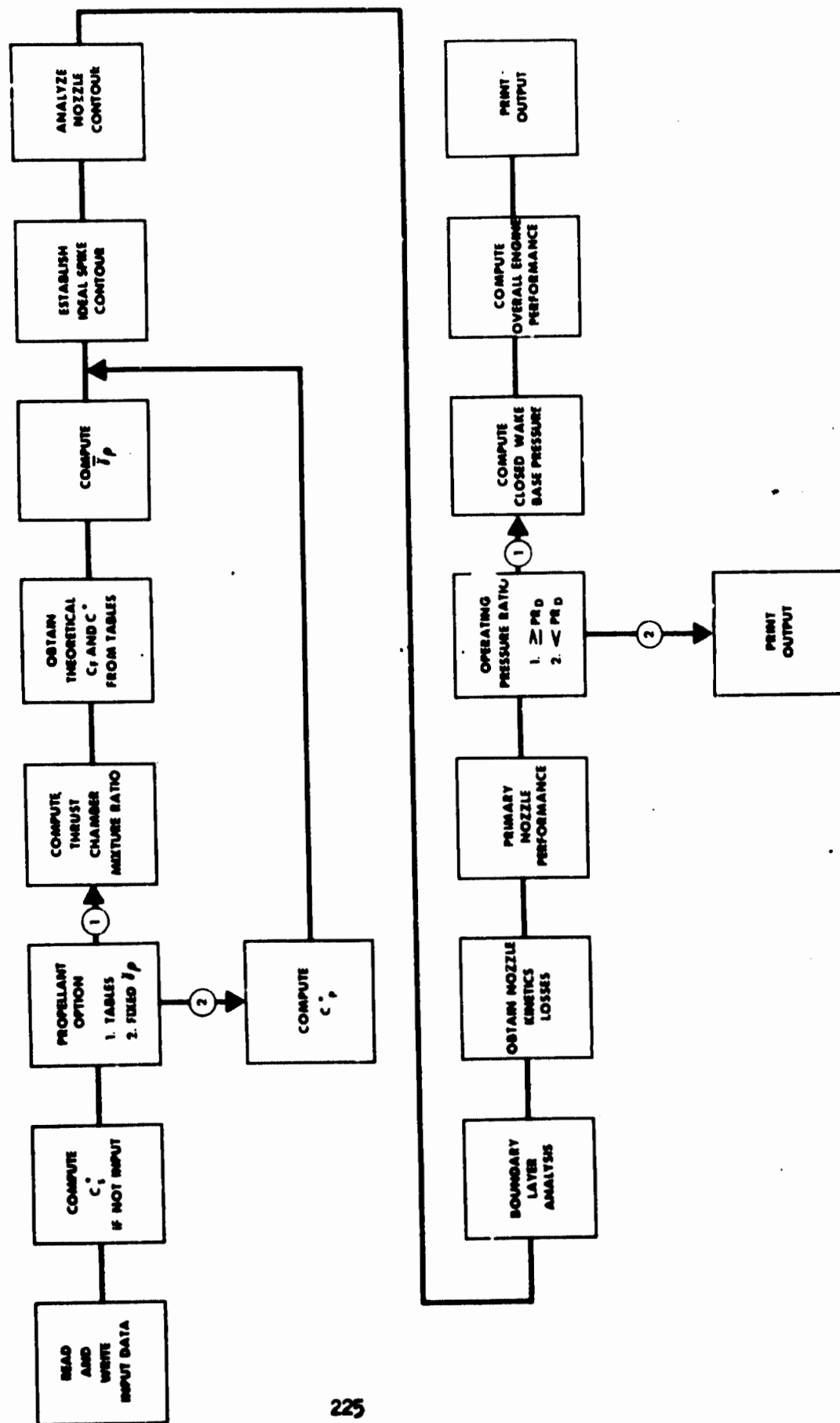
Losses caused by introduction of structural members across the flow are not calculated in the program but can be included into equation (1) through the use of information in Fig. 125, and the equation:

$$C_{F_{pins}} = (1 - \eta_p) C_{F_{i,v}}$$

where η_p is obtained from Fig. 125.

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Fig. 129 Flow Diagram, Aerodynamic Spike Engine Design Program



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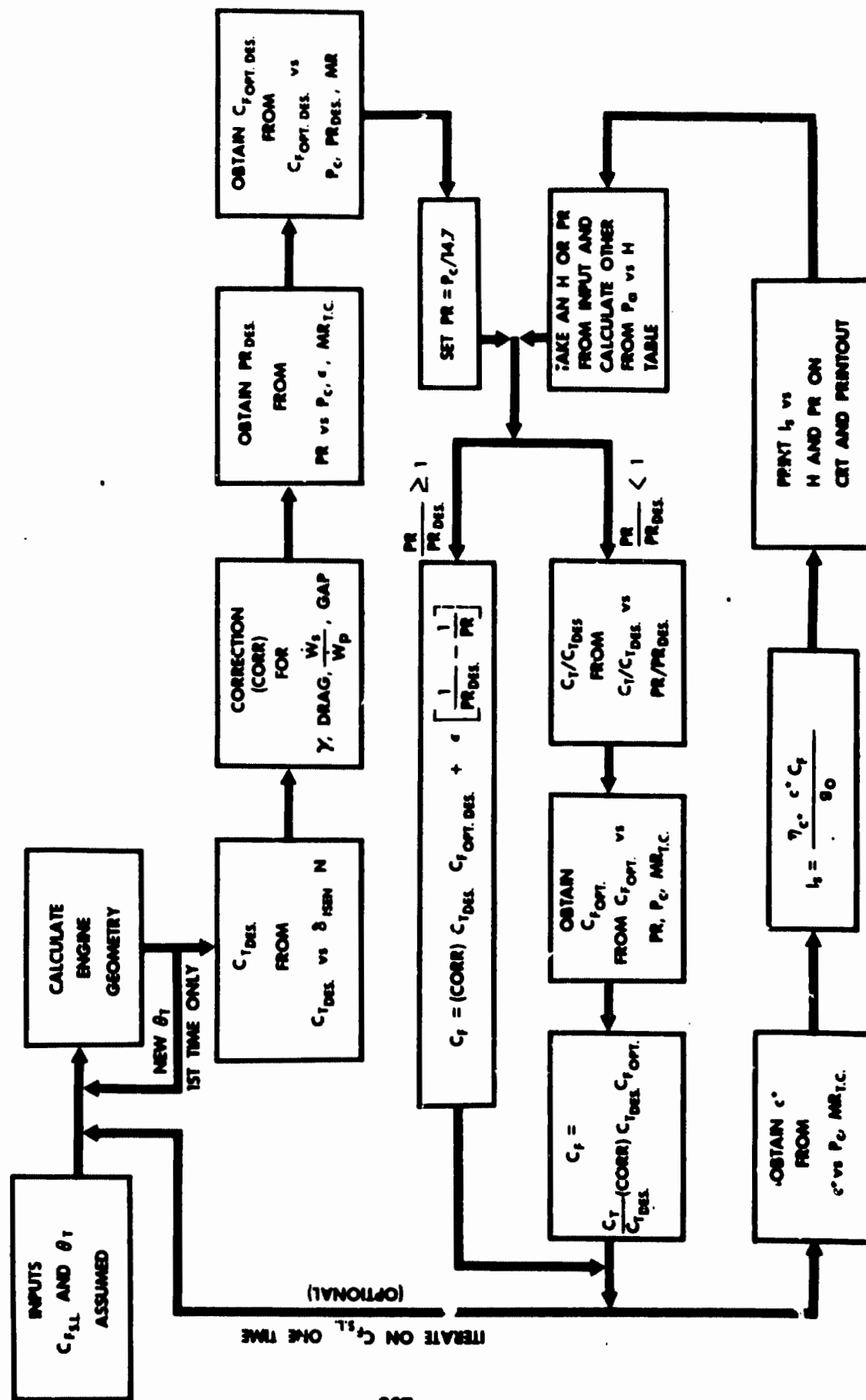
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Multichamber Configurations. Computer programs developed under NAS8-20237 (Multichamber, Plug Nozzle Systems Analysis) are currently used at Rocketdyne for estimation of multichamber propulsion system performance. The procedure is based on a combination of empirical correlations such as those shown in Figs. 126 and 127 to establish the uncorrected design point efficiency and the effect of module spacing, semiempirical procedures for prediction of the base contribution and for translation of cold-flow data to hot-firing performance, and theoretical methods for prediction of drag and performance variation with altitude in the closed-wake regime. In addition to computing performance, the programs perform the geometric design of any desired system on the basis of thrust, diameter, chamber pressure, length, mixture ratio, and number of modules.

A comprehensive description of the performance analysis method outlined in Fig. 130 is presented in Ref. 18. The method in Fig. 130 incorporates a normalized C_T curve, i.e., the $C_T/C_{T_{\text{design}}}$ vs PR/PR_{des} curve, shown in Fig. 131 to compute the variation of C_T with pressure ratios or altitudes below the design point. The use of a generalized altitude-compensation curve represents a critical assumption in the overall performance evaluation procedure. Application of a curve of this type on a "universal" basis to all combinations of module and system expansion area ratio and to any gas specific heat ratio presumes that sufficient substantiating data are available to warrant its use. Actually, the experimental data in this area are somewhat limited, but many examples, such as the data shown in Fig. 132 demonstrate that a universal altitude-compensation curve may in fact be a reasonable assumption. However, additional experimental data are required to verify the validity of this technique, particularly for area ratios in excess of 50:1 and for gamma values other than 1.4

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Fig. 130 . Flow Diagram for Multichamber System Performance Program



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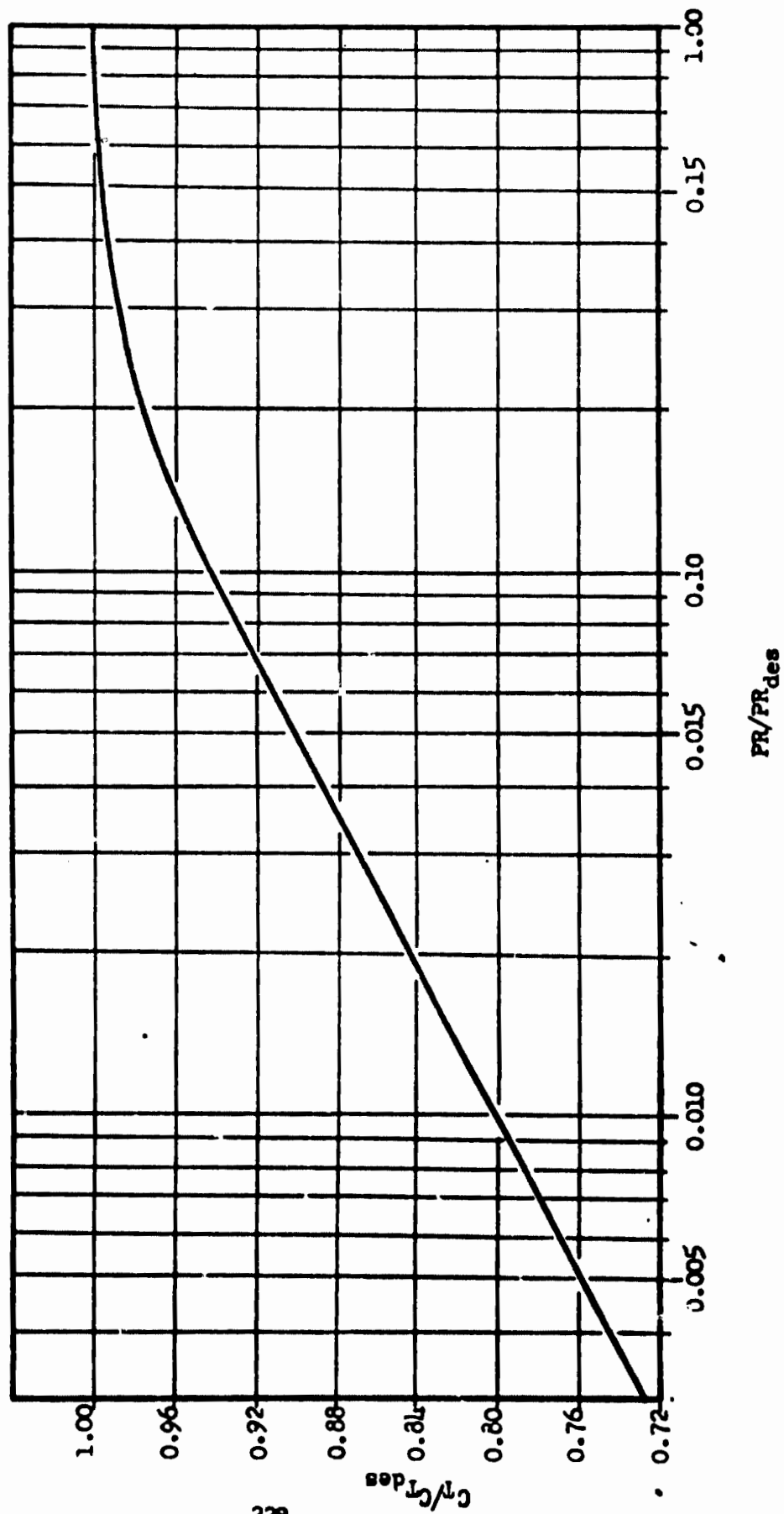


Figure 131. Altitude Compensation Curve

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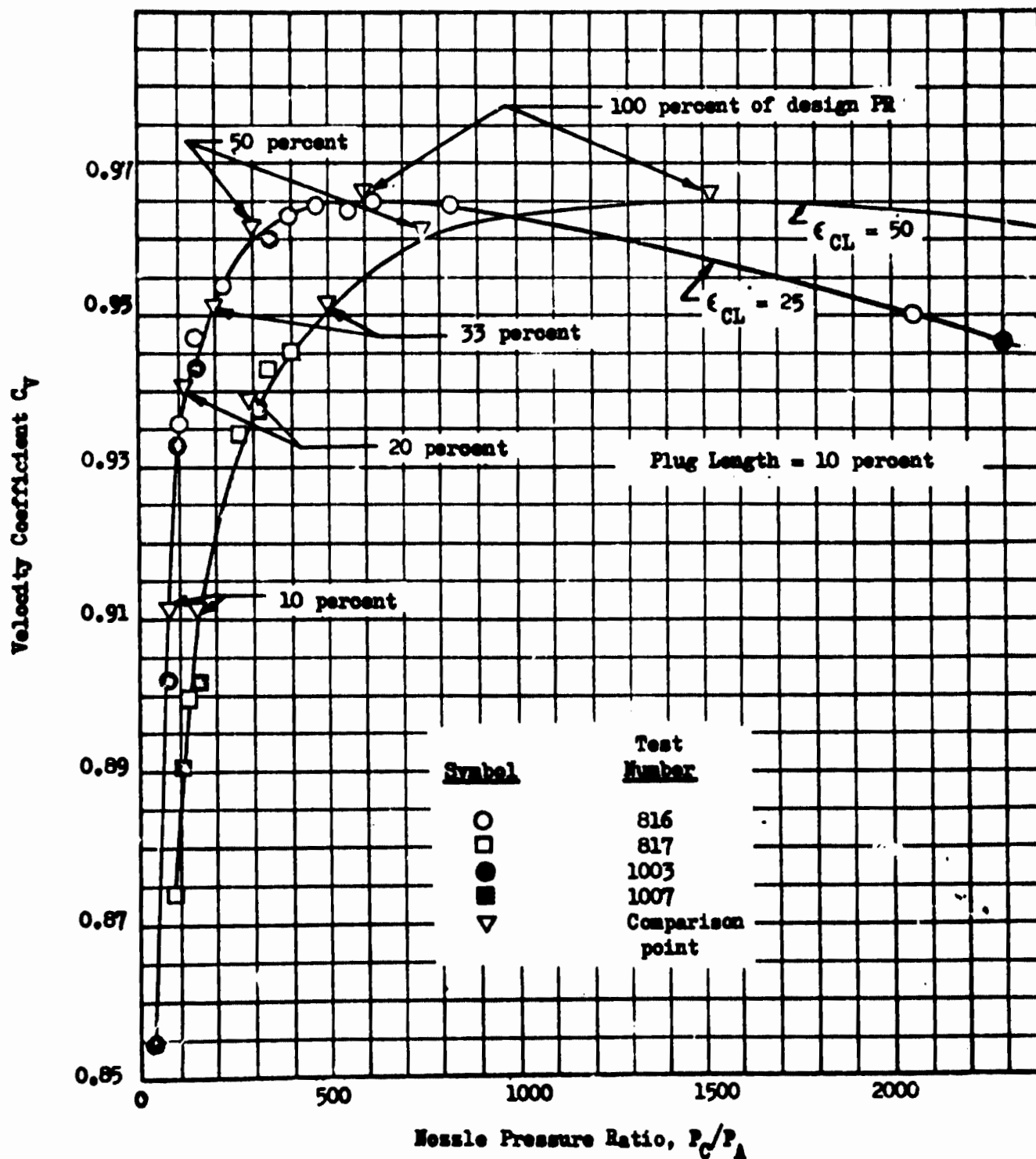
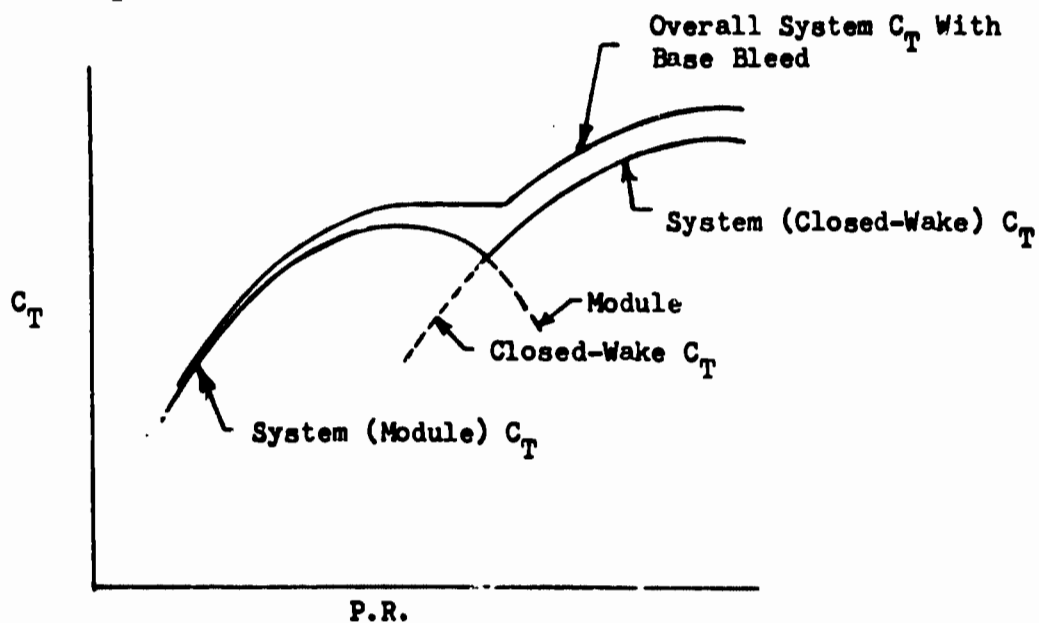


Figure 132. Effects of Cluster and Modular Area Ratio on Design Performance

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An alternative, more flexible approach currently in use avoids the simplified universal C_T technique. This method is based on a "tilted module" analysis for pressure ratios below the module design pressure ratio and a method equivalent to the annular, closed-wake analysis for higher pressure ratios. The module analysis includes a theoretical separation criterion which permits the analysis to proceed accurately regardless of the degree of overexpansion. An empirical approach is used in the transition region between the two methods, with the performance trend dictated by the presence or absence of base bleed. With no base bleed, the module performance continues to prevail beyond the module design pressure ratio, resulting in a "trough" in the delivered C_T curve (see sketch). Since the general tendency indicated by cold-flow data is for base bleed to eliminate this trough, a simplified approach was employed, in which the presence of any quantity of base bleed is assumed to cause the C_T curve to be horizontal between the module design pressure ratio and the intersection with the system closed-wake C_T curve.



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An important aspect of performance computation became apparent from data generated during the experimental multichamber investigation conducted in this program. From data showing the variation of C_T vs pressure ratio, it was evident that effective expansion area ratio (i.e., design pressure ratio) could be predicted more accurately based on a "scaloped" exit area rather than on the area of the circle enclosing the module exits. As shown in Fig. 133 this factor is significant in systems having relatively few modules. Scaloped area ratio is therefore utilized as the basis for computing system design pressure ratio in the computer program.

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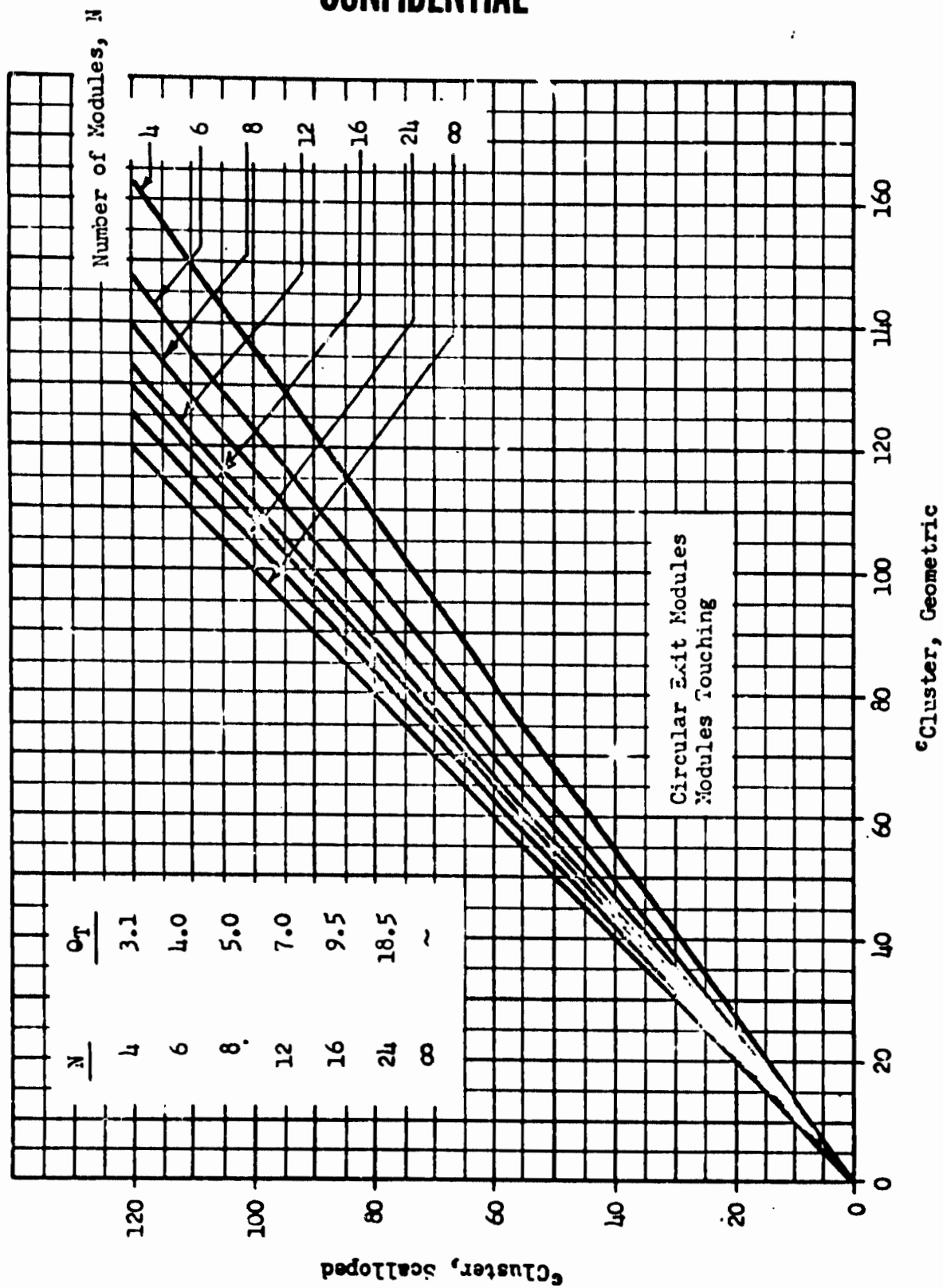


Figure 133. Scalloped and Geometrical Cluster Expansion Area Ratio Exchange Curves

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ENGINE WEIGHT COMPARISON

A parametric study was made to compare the weight of toroidal and multichamber aerospike engines and conventional single bell engines utilizing N_2O_4 /UDMH- N_2H_4 (50-50) propellants. The engines were compared at a thrust level of 2,000,000 pounds over a range of chamber pressures from 1000 psia to 3000 psia and a range of area ratios from 20 to 150. The method of analysis and results are presented in the following paragraphs.

Method of Analysis

Engine weights were computed for multichamber and toroidal aerospike engines and conventional single bell engines. The characteristics of the engines evaluated and the range of parameters investigated are listed in Table 9 .

The study was conducted at a fixed sea level thrust of 2,000,000 pounds. The aerospike engines all had a total length from the throat to the nozzle exit plane equal to 20 percent of a 15 degree conical nozzle. The single bell engines were 80 percent in length. Area ratios from 20 to 150 were investigated for the aerospike engines and from 20 to 100 for the bell engines. Chamber pressures from 1000 psia to 3000 psia were investigated for the aerospike engines and from 1000 psia to 2000 psia for the bell engines.

Three variations of the multichamber configuration were investigated, an eight module configuration with eight sets of individual fuel and oxidizer turbopumps, a sixteen module configuration with sixteen turbopump sets $M_{T/P}$, and a sixteen module configuration with eight turbopump sets. The eight module configurations are approximately 20 percent in length to the exit of the modules and therefore require no spike nozzle extension.

Toroidal aerospike weights were computed using an existing computer program developed for annular nozzle weight analysis. Multichamber weights were

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TABLE 9
CHARACTERISTICS OF ENGINE SYSTEMS
P = 2,000,000 Pounds; $N_2O_4/UDME-N_2H_4$ (50-50)

Configuration	Number of Turbopump Sets	Missile Length (percent 15 degree cone)	P ₂ Range (psia)	ε Range
8 Module Multichamber	8	20 (no spike)	1000-3000	20-150
16 Module Multichamber	16	20 (8.6 to 10.6 percent spike)	1000-3000	20-150
	8	20 (8.6 to 10.6 percent spike)	1000-3000	20-150
Toroidal	8	20	1000-3000	20-150
Single Bell	1	80	1000-2000	20-150

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computed using both an existing bell engine weight computer program and the annular nozzle weight program. Weight relationships for structure supporting the multichamber modules and the multichamber spike were based upon weight analyses of structural drawings of H-1 cluster configurations and large (18 to 30 million pounds thrust) multichamber LO_2/LH_2 aerospike engines (Ref. 18).

The engines were all assumed to obtain their turbine drive fluid by tapping off main combustion chamber gases. All engines were assumed to be regeneratively cooled (with N_2H_4 -UDMH below $P_c = 1500$ and with N_2O_4 at chamber pressure of 1500 psia and above). The results of parametric heat transfer studies were used to determine tube pressure drop and consequent pump discharge pressure requirements.

Results

Engine weights for the various configurations are shown v. area ratio in Figs 134 through 137. Several trends can be seen from these data. Engine weight increases very rapidly with increasing area ratio, the rate of increase decreases with increasing chamber pressure. The single bell engine system increases in weight more rapidly than the other configurations, however, it is lighter than the sixteen chamber configurations up to area ratios between 60 and 100. The single bell engine is approximately equal in weight to the eight module configuration and the toroidal aerospike at low area ratio but rapidly becomes considerably heavier than the aerospikes as area ratio increases.

The sixteen module configurations are consistently heavier than the eight module configuration because of the weight of the spike nozzle extension. The use of fewer turbopumps in the sixteen module configuration results in consistently lower engine weights.

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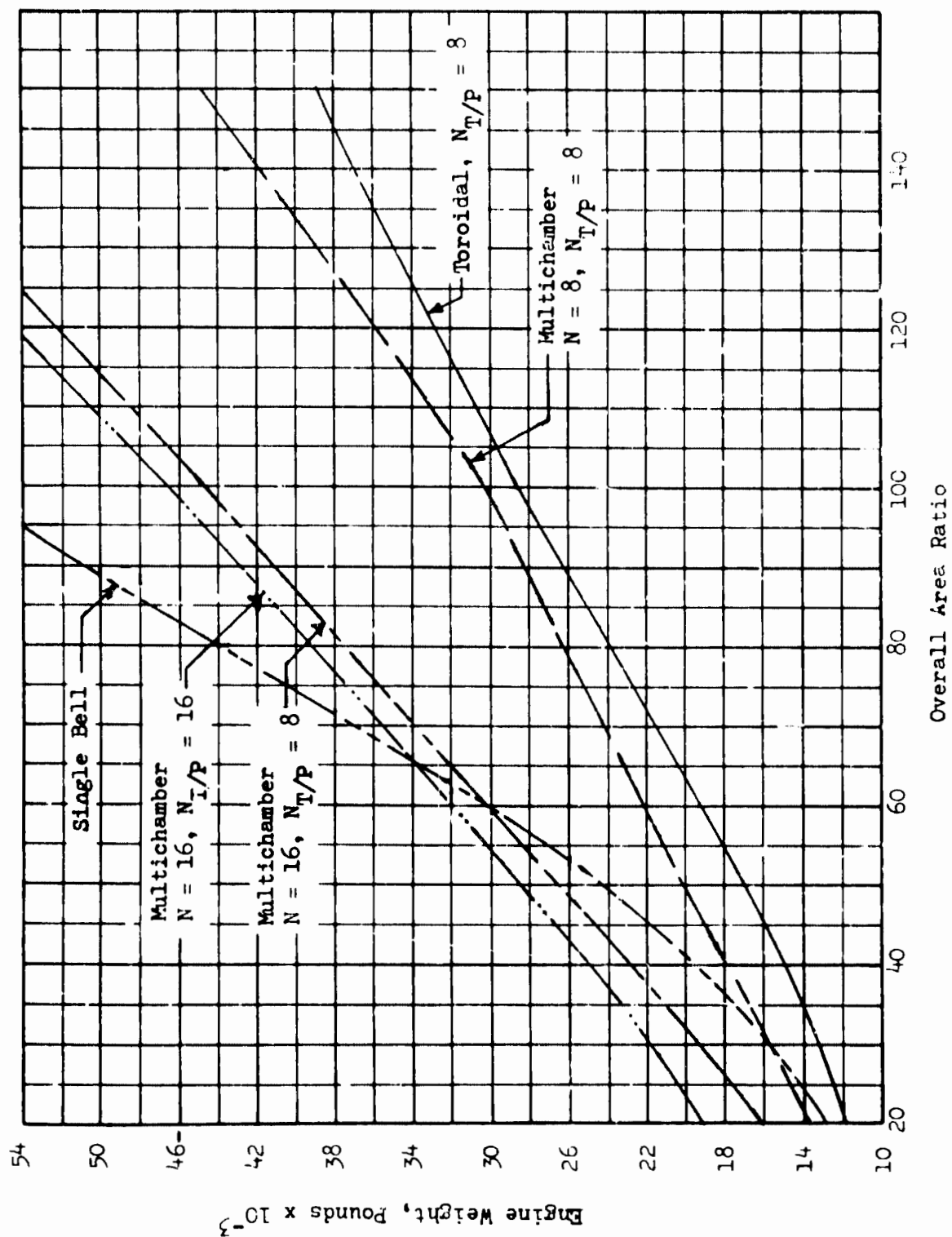


Fig. 134. Engine Weight vs Area Ratio - $F = 2,000,000; P_c = 1000 \text{ psi}$

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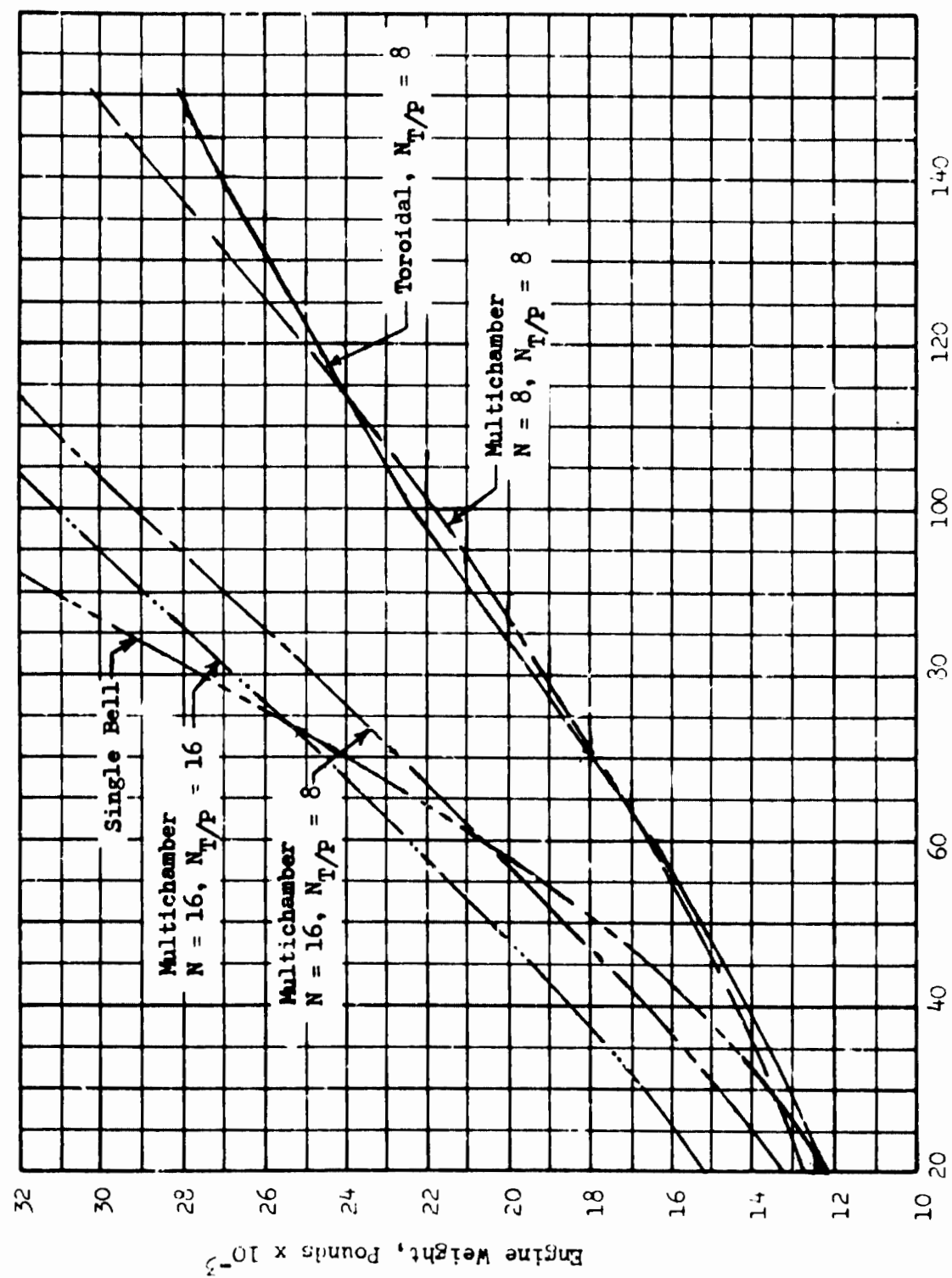


Fig. J35 Engine Weight vs. Area Ratio - $F = 2,000,000$ Pounds; $P_c = 1500$ psia

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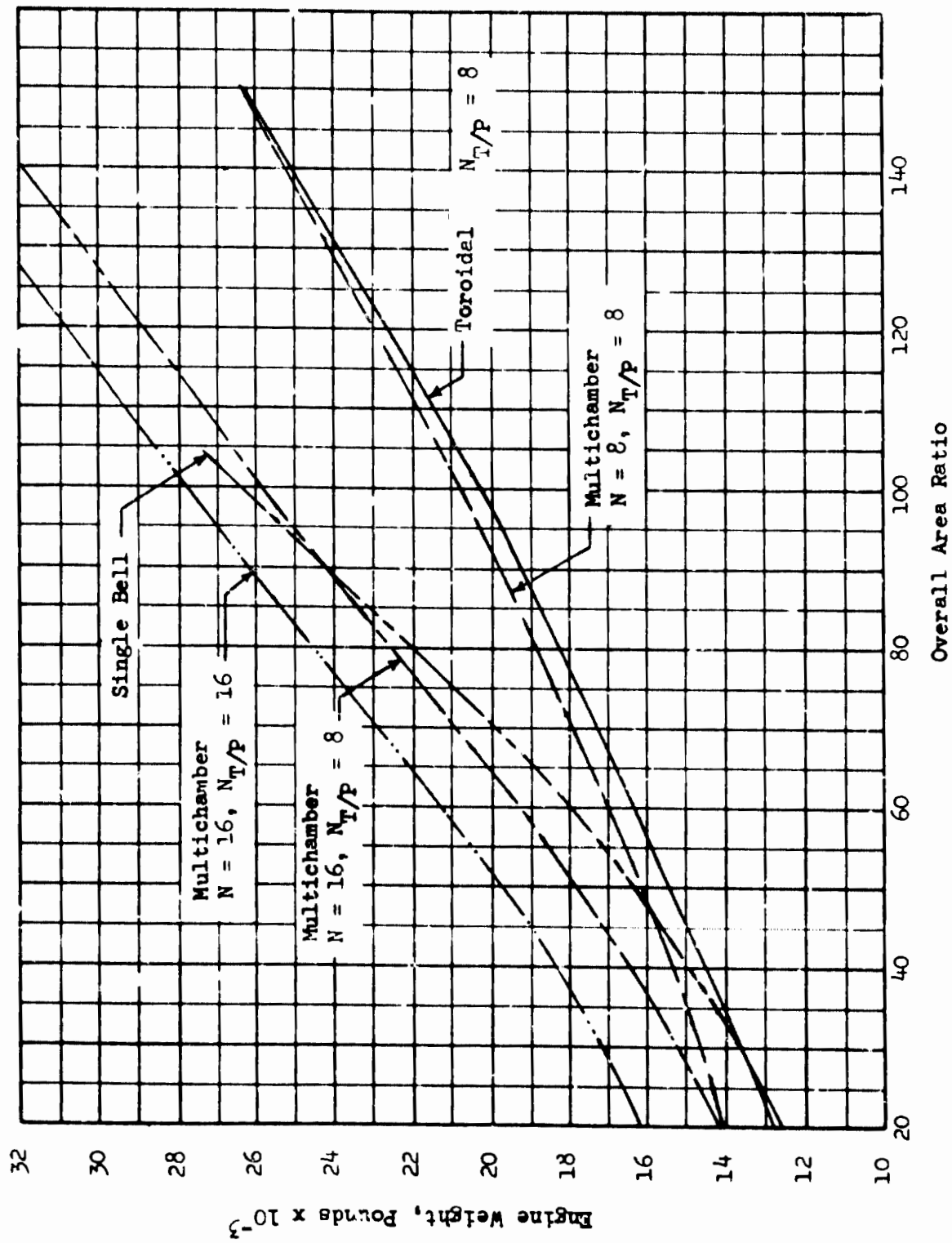


Fig. 136. Engine Weight vs Area Ratio - $F = 2,000,000$ Pounds;
 $P_c = 2000$ psia

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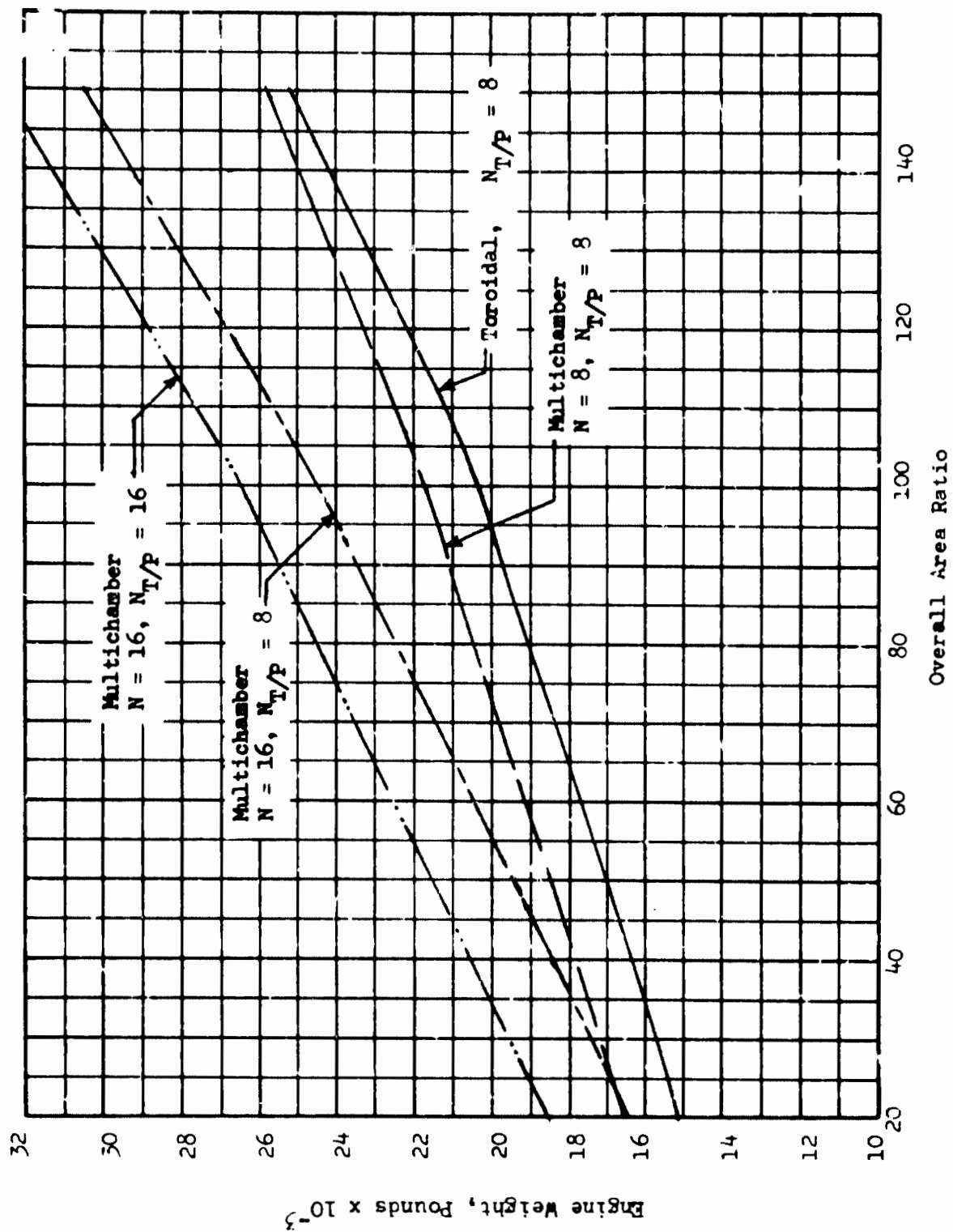


Fig. 137 Engine Weight vs Area Ratio - $F = 2,000,000$ Pounds; $P_c = 3000$ psia

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The eight module multichamber configuration is generally slightly heavier than the toroidal configuration although in certain areas the weights of these two configurations are approximately the same.

The same data is replotted vs chamber pressure in Fig. 138 and 139 for constant area ratios of 20, 50, 100, and 150. The following weight trends can be observed from this type of plot. The engine weights all tend to reach a minimum value with chamber pressure. The chamber pressure at which a minimum weight is achieved increases with increasing area ratio. The single bell engine weights are much more sensitive to chamber pressure than the other configurations at high area ratios and they also achieve a minimum weight at higher chamber pressures than the other configurations. The toroidal configuration weight appears to be the least sensitive to variations in chamber pressure.

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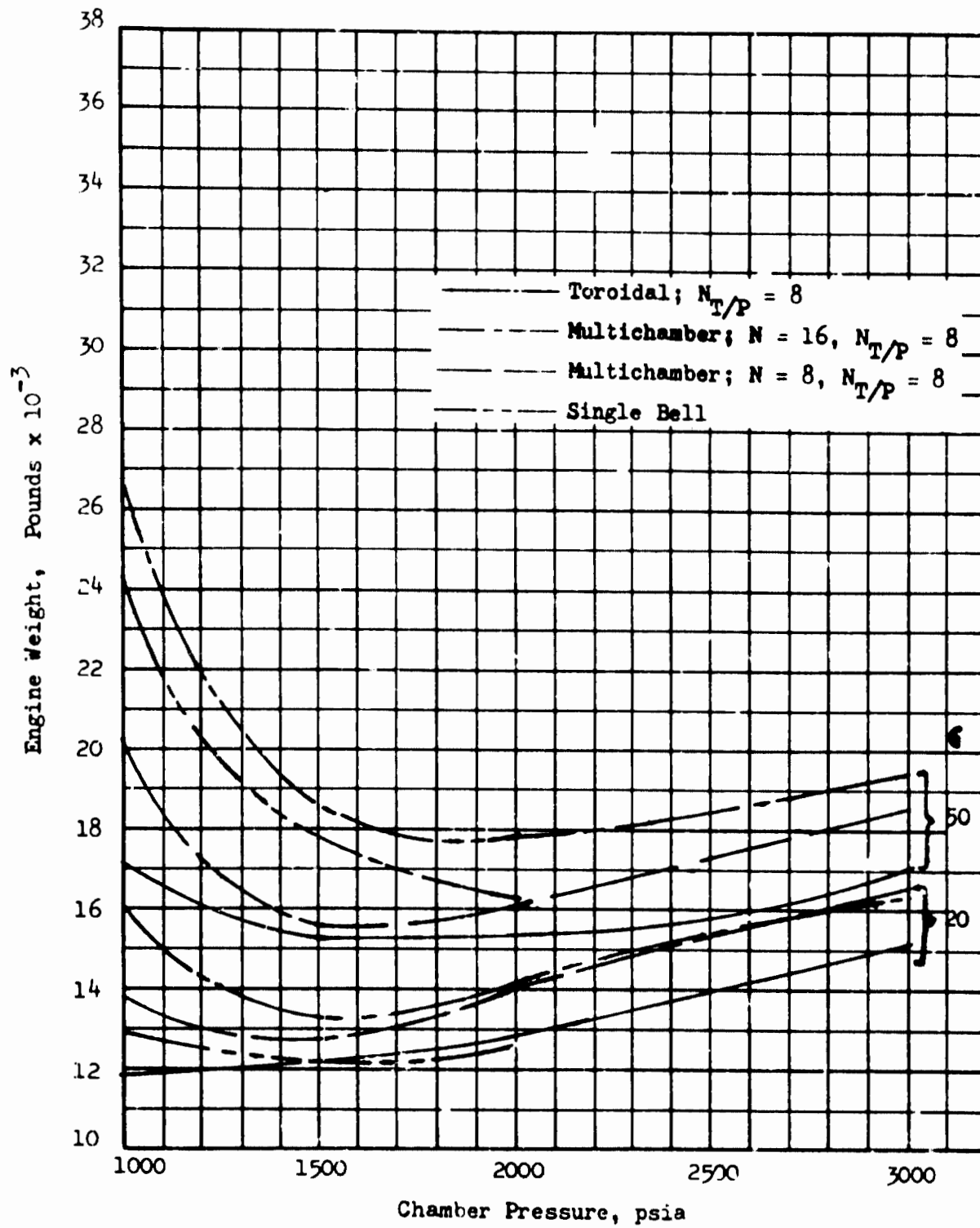


Fig. 138. Engine Weight vs Chamber Pressure - $\epsilon = 20$ and 50

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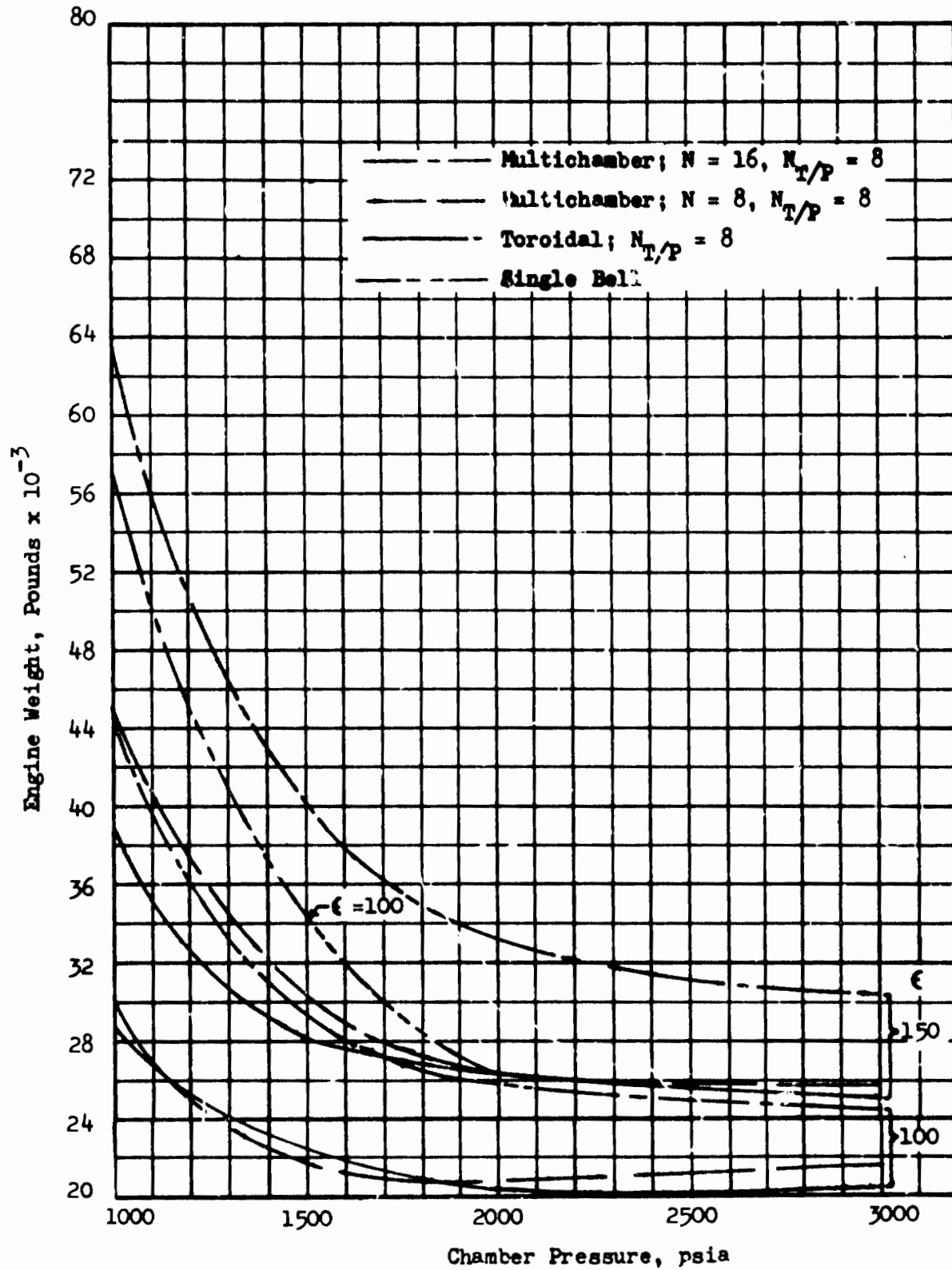


Fig. 139. Engine Weight vs Chamber Pressure - $\epsilon = 100$ and 150

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HEAT TRANSFER STUDIES

A primary consideration in the selection of a suitable combustor configuration for aerodynamic spike nozzles is regenerative cooling feasibility. Therefore, heat transfer studies were conducted to determine regenerative cooling limits (chamber pressure, area ratio, and thrust) for aerodynamic spike nozzles with toroidal combustion chambers and with clustered conventional chambers.

The engines studied utilize the storable propellants N_2O_4 and N_2H_4 -UDMH (50-50). Both propellants were considered for the coolant. The range of thrust investigated varied from 3000 pounds to 300,000 pounds for conventional single chambers and from 10,000 pounds to 2,000,000 pounds for toroidal aerospike. Other parameters which were investigated included area ratios to 150 and chamber pressures from 300 to 3000 psia.

Practical regenerative cooling limits were established by performing a numerical integration of pressure drop and bulk temperature rise along the coolant flowpath for numerous cases sufficient to cover the desired engine parameter range.

The results are summarized in curves showing the variation in coolant pressure drop requirements with chamber pressure, thrust level, coolant, and (for toroidal combustors) area ratio for aerospike engines using conventional chambers and toroidal combustors.

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Relative Cooling Capabilities of the Propellants

Before the coolant pressure drop requirements for thrust chambers utilizing N_2O_4 and N_2H_4 -UDMH (50-50) are discussed, it is helpful to analyze the cooling capabilities of the two possible coolants to better understand their characteristics under specific conditions. Therefore, a discussion of the merits of both candidate coolants is presented.

The regenerative cooling capabilities of both candidate coolants depend greatly upon the coolant pressure. Below the critical pressure of N_2O_4 (approximately 1500 psia) UDMH- N_2H_4 is the superior coolant. Above its critical pressure, N_2O_4 is the better coolant. This is primarily because the heat transfer coefficient is increased (approximately doubled) by the endothermic dissociation of N_2O_4 to NO_2 at the coolant tube wall (Ref. 13).

The cooling capabilities of both candidate coolants at subcritical pressures are compared in Fig. 140. Under these pressures, the coolant wall temperature must be kept approximately equal to the saturation temperature of the coolant. If the wall temperature is above the saturation temperature, bulk boiling occurs. This will cause tube burnout.

The wall temperatures shown in Fig. 141 for N_2O_4 are the corresponding saturation temperatures for vapor pressures of 500 psia ($T_{wc} = 660$ deg. R) and 1500 psia ($T_{wc} = 760$ deg. R). The wall temperatures shown for

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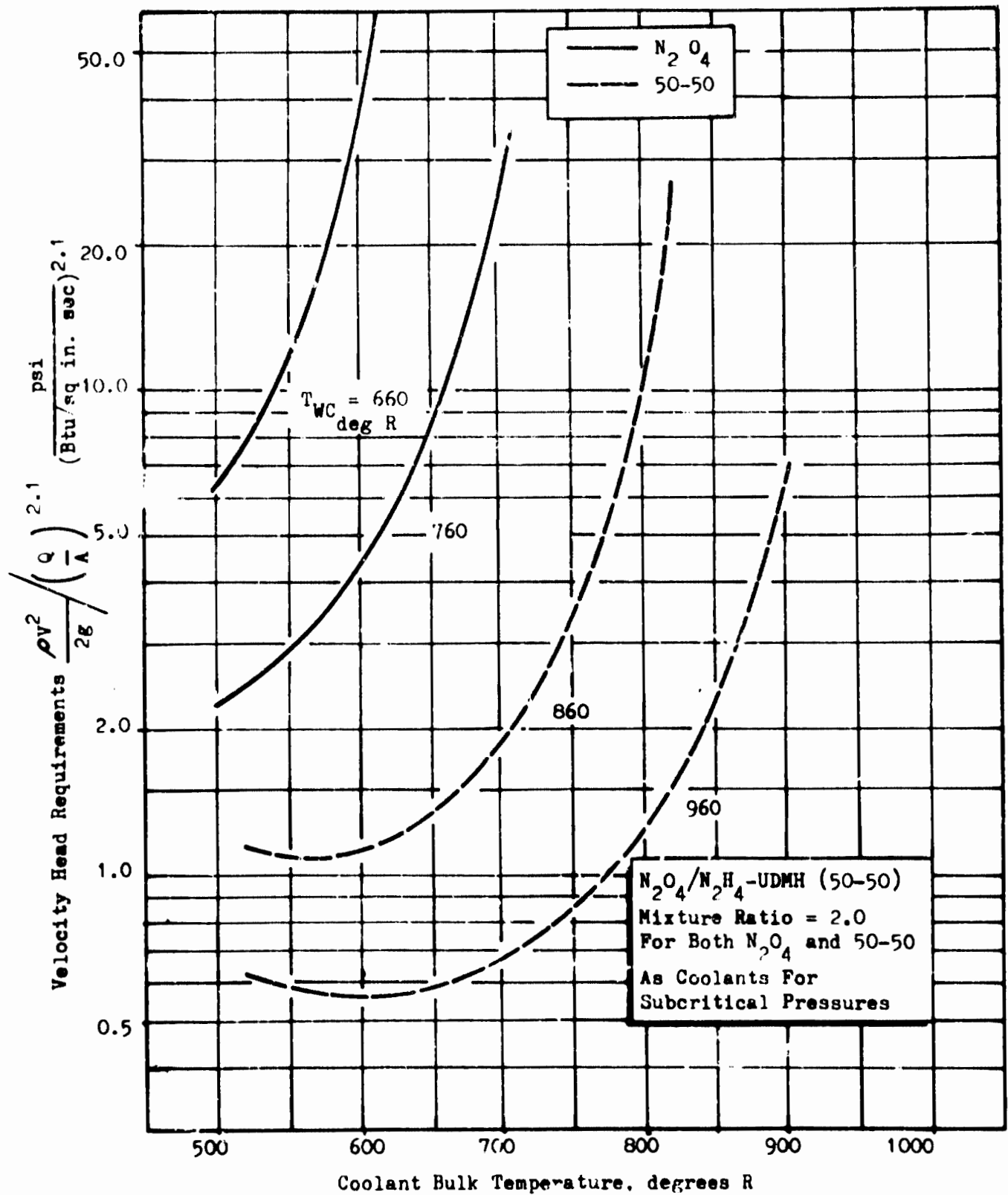


Fig. 140 Coolant Velocity Head Requirements vs Coolant Bulk and Wall Temperature

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N_2H_4 -UDMH (50-50) are the saturation temperature for a vapor pressure of 500 psia ($T_{wc} = 860$ deg. R) and an experimentally determined upper allowable temperature of 500 deg. F. Above this wall temperature exothermic decomposition of the fuel can occur as reported in Ref. 14. At a vapor pressure of 1500 psia the saturation temperature of 50-50 fuel is above the 500 deg. F wall temperature limit.

A small increase in N_2O_4 bulk temperature sharply increases the coolant velocity head (and pressure drop) requirement. The required velocity head increases by a factor of four when the bulk temperature increases from 500 deg. R to 650 deg. R for a coolant wall temperature of 760 deg. R. For the same vapor pressure of 500 psia and the same bulk temperature of 600 deg. R, the velocity head requirement of N_2O_4 coolant is 30 times as large as the requirement for 50-50 fuel. These results clearly indicate the superior cooling capability of 50-50 fuel at subcritical pressures.

The velocity head requirements for both coolants at supercritical pressures are shown in Fig. 141. The coolant side wall temperatures of 960 deg. R for 50-50 fuel and 1060 deg. R for N_2O_4 are the maximum allowable. A 600 deg. F wall temperature limit appears necessary with N_2O_4 coolant to prevent oxidation of the tube wall. For a coolant bulk temperature range from 500 deg. R to 750 deg. R, the velocity head requirement of 50-50 fuel is approximately six times as large as the requirement for N_2O_4 . Thus N_2O_4 is the superior coolant at supercritical pressures.

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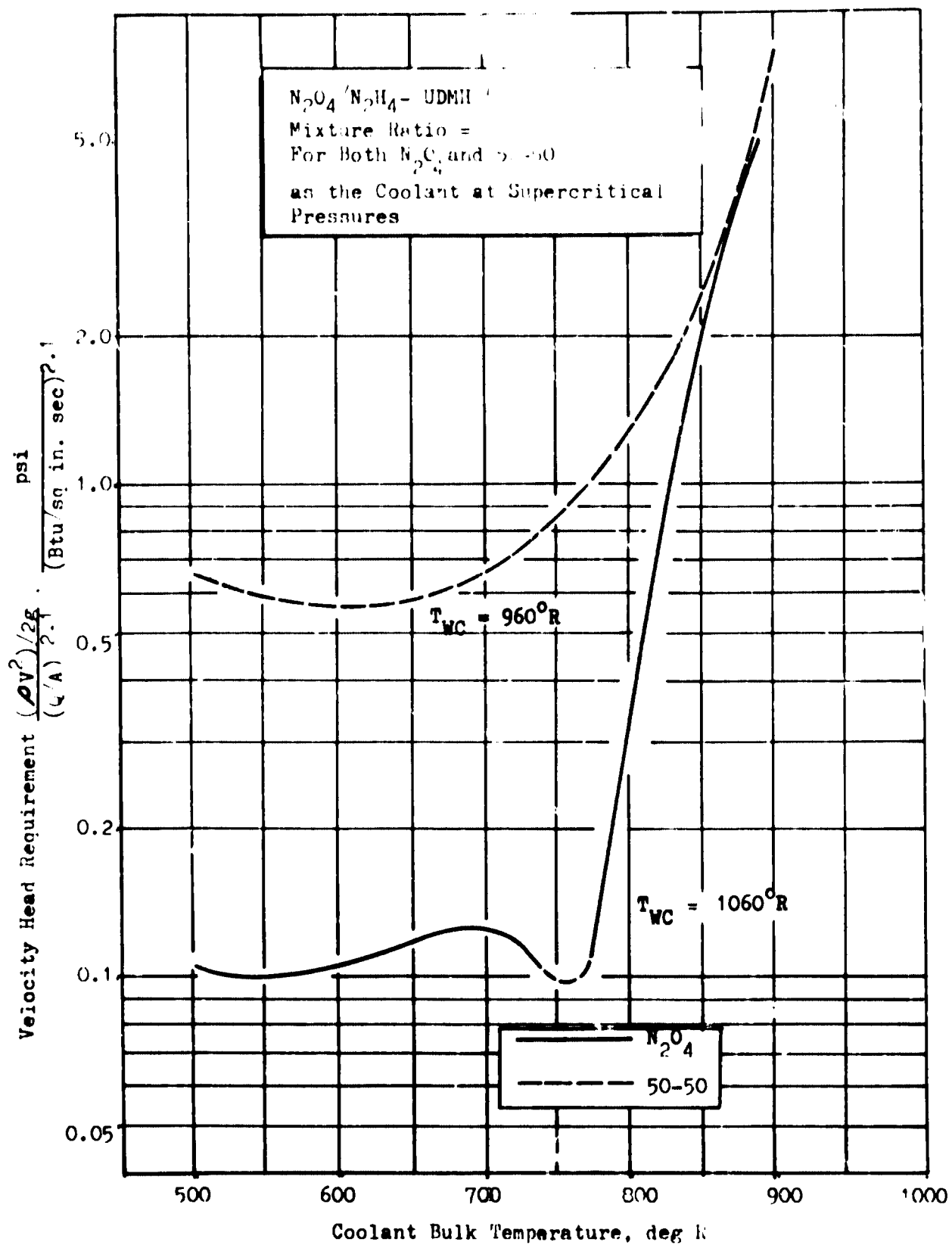


Fig. 141 Coolant Velocity Head Requirements vs Coolant Bulk Temperature and Wall Temperature

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Regenerative Cooling Limits for Conventional Combustors

To investigate the regenerative cooling limits for multichamber aerospike with a total thrust range from 20,000 pounds to 2,000,000 pounds it is necessary to determine the limits for multichamber modules of much lower thrust level. This is because conventional chambers clustered in groups of 8 or more comprise a typical multichamber aerospike configuration. As will be shown these modules become increasingly difficult to cool regeneratively as the module thrust level decreases. In this study module thrusts from 3,000 pounds to 300,000 pounds were analyzed to cover the total multichamber engine thrust range of interest.

The criterion used to judge regenerative cooling feasibility is the coolant pressure drop. This is the most practical criterion. However, it is the most difficult to obtain. Each case requires numerical integration along the coolant flow path using a digital computer program. In this analysis of conventional chambers N_2H_4 -UDMH (50-50) was used as the coolant at chamber pressures below 1500 psia and N_2O_4 was used at chamber pressures above 1500 psia. The resultant parametric pressure drop curves and the method of analysis are discussed in the following paragraphs.

Method of Analysis. For the analysis of conventional thrust chambers cooled with UDMH- N_2H_4 (50-50) the specific cases analyzed on the IBM computer were thrusts of 10,000 pounds, 60,000 pounds, and 300,000 pounds and chamber pressures of 50 psia, 150 psia, 600 psia, and 1200 psia. The nozzles were assumed to have an area ratio of 100 but were regeneratively

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cooled to area ratios of 3, 3, 30 and 30, respectively, at each of the above chamber pressures. The specific cases analyzed are listed in Table 10 .

For the analysis of conventional chambers with N_2O_4 cooling, the operating ranges were chamber pressure from 1500 psia to 3000 psia and engine thrust levels from 3,000 pounds to 300,000 pounds. The nozzles were assumed to be entirely regeneratively cooled with an area ratio of 100. The specific cases analyzed are tabulated in Table 11 .

The thrust chamber utilizes N_2O_4 / UDMH- N_2H_4 (50-50) propellants at a mixture ratio of 2.0. Frozen equilibrium C^* performance (100 percent of theoretical) and a nozzle thrust coefficient of 1.8 were assumed. A single downpass coolant circuit was used to obtain the lowest coolant pressure drop conditions.

The local heat flux Q/A which must be dissipated through the chamber wall is given by

$$Q/A = h_g (T_{AW} - T_{WG})$$

The gas side film coefficient h_g was determined by the simplified Bartz equation

$$h_g = \frac{0.026}{d_H^{0.2}} G^{0.8} \frac{C_p^{0.2}}{N_{Pr}^{0.6}} \sigma$$

where
$$\sigma = \left[\frac{1}{2} \left[\frac{T_{WG}}{T_{AW}} \right] \left[1 + \frac{\gamma-1}{2} M^2 \right] + \frac{1}{2} \right]^{-0.68} \left[1 + \frac{\gamma-1}{2} M^2 \right]^{-0.12}$$

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TABLE 10.
SUMMARY OF REGENERATIVE COOLING OF BELL CHAMBERS WITH UDMH-N₂H₄ (50-50)

Thrust 1000 pounds	Chamber Pressure, psia	Contraction Ratio	Regeneratively Cooled Area Ratio	Number of Tubes	Maximum Coolant Velocity (ft/sec)	Number of Tube Splices	T _{WC} Maximum deg. F	Pressure Drop Chamber Pressure
10	600	3.0	30	400	275	2	500	4.40
	50	2.0	3	1200	86	0	295	0.50
60	1200	2.0	40	350	387	1	500	2.40
	600	2.0	30	400	189	1	500	1.05
	150	2.0	8	750	90	1	340	0.31
	50	2.0	3	1100	40	0	295	0.02
300	1200	2.0	30	400	294	1	500	1.01
	600	2.0	30	450	152	1	500	0.51
	150	2.0	8	1000	74	0	340	0.15
	50	2.0	3	1200	33	0	295	0.01

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TABLE 11
SUMMARY OF REGENERATIVE COOLING OF BELL CHAMBERS WITH N_2O_4 AT SUPERCRITICAL PRESSURE

Thrust, 1000 pounds	Chamber Pressure, P_c psia	Contraction Ratio, ϵ_c	Combustor Length, inches	Number of Tubes	$(Q/A)_{max}$ $\frac{Btu}{in^2 sec}$	Maximum Coolant Velocity (ft/sec)	Coolant Tube Pressure Drop ΔP (psi)	Bulk Temp- erature Rise ΔT (deg F)
3	1500	9	6.1	150	35.6	640	2267	328
10	1600	6	8.5	140	33.8	260	469	281
	1750	6	8.4	200	36.6	700	3142	285
50	1900	4	12.1	150	34.0	240	305	234
	2050	4	12.0	200	36.4	460	841	240
	2100	4	12.0	210	37.2	640	1478	248
	2150	4	11.9	250	38.0	970	3958	265
300	2300	3	16.6	200	34.0	210	662	192
	2500	3	16.4	250	36.6	380	1535	195
	2600	3	16.4	280	38.0	600	2940	199

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and is, simply stated, a function of the properties of the combustion products and the local mass velocity. The adiabatic wall temperature T_{AW} is relatively invariant throughout the nozzle and is nearly equal to the combustion temperature. It is relatively insensitive to all chamber operating conditions except mixture ratio. The gas side wall temperature T_{WG} is a variable dependent upon the maximum operating temperature which a selected tube wall material can sustain while maintaining a satisfactory strength. For this analysis inconel X and 347 stainless steel were used for chambers cooled with fuel and oxidizer, respectively. The maximum useful wall temperature T_{WG} used for these materials was 1600 deg F.

Typical peak heat fluxes encountered at the throat of conventional chambers and continuous annular throat toroidal combustors are shown in Fig. 142. These curves were computed assuming a T_{WG} equal to 1600 deg F and using the equations above for h_g and Q/A . When considering a conventional chamber δ_T is the throat radius, while δ_T is the throat gap for a continuous annular throat toroidal combustor. δ_T may be computed from

$$\delta_{T_{Bell}} = \sqrt{\frac{A_T}{\pi}}$$

$$\delta_{T_{annular}} = \sqrt{\frac{A_T}{4\pi\epsilon}}$$

Most practical applications are within the range of δ_T shown.

For steady state heat conduction the heat flux conducted through the tube wall satisfies the relationship

$$Q/A = \frac{k}{X} (T_{WG} - T_{WC})$$

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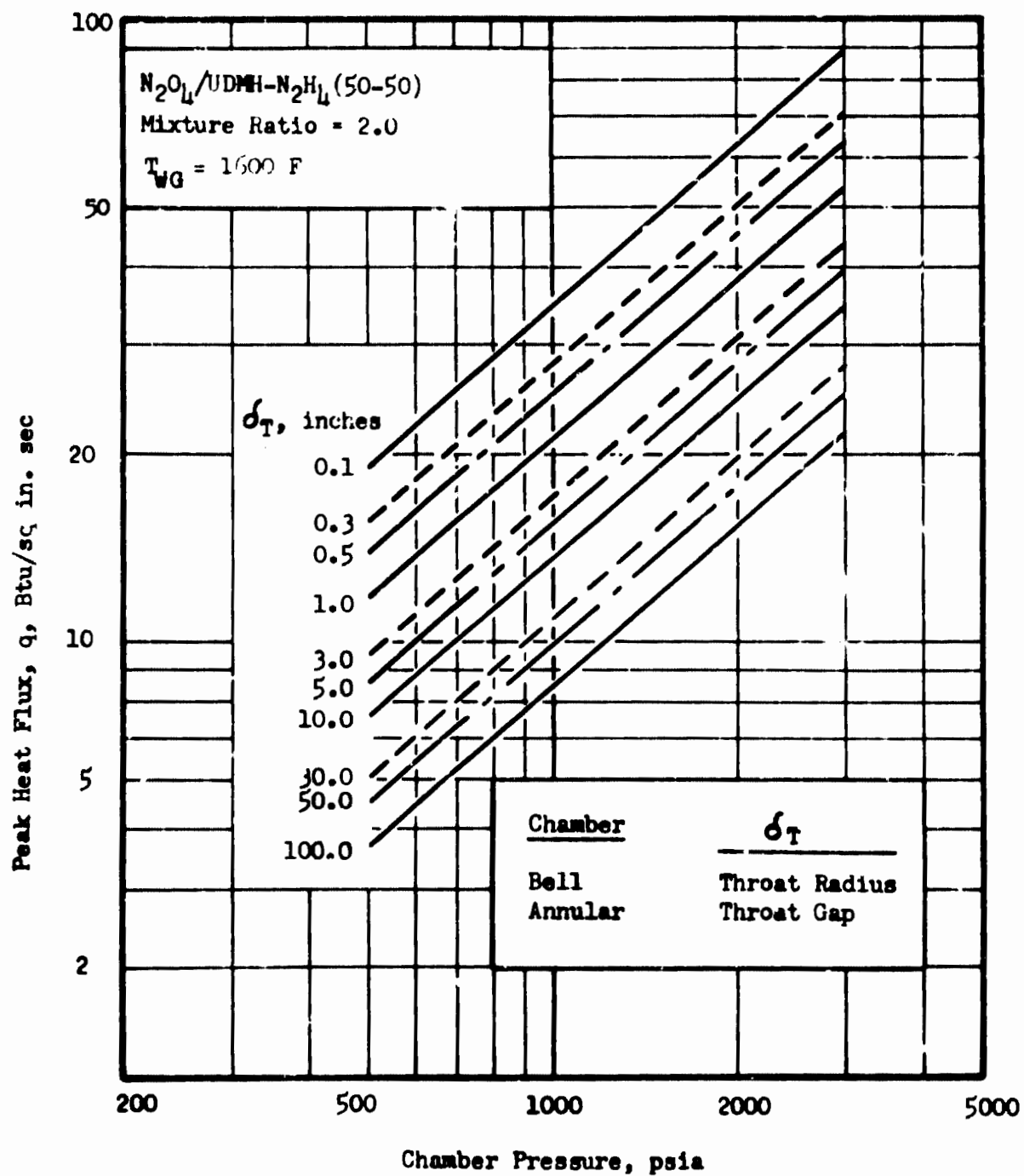


Fig. 142 Peak Heat Fluxes for Bell Nozzles and Continuous Annular Throat Toroidal Combustor

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where k and X are the material thermal conductivity and wall thickness, respectively, and T_{WC} is the coolant side wall temperature. For this analysis a wall thickness (inconel X) of .01 inch and a maximum coolant side wall temperature of 500 deg. F were assumed with fuel coolant. For chambers cooled with N_2O_4 a wall thickness (347 stainless steel) of 0.01 inch and a maximum coolant side wall temperature of 600 deg. F was used.

Figure 143 shows the maximum heat flux that can be passed through a tube wall. By imposing the maximum possible temperature differential across a given material, the maximum possible heat flux is determined as a function of wall thickness. The results are shown for three selected materials; 347 stainless steel, inconel X, and a molybdenum alloy TZM. Stainless steel and inconel X are materials with a maximum useful temperature of approximately 1600 deg. F. The working temperature of TZM was also assumed to be 1600 deg. F for comparative purposes although its maximum allowable temperature is approximately 2500 deg. F. From the graph the merits of a refractory material can be easily realized.

For a practical tube wall thickness of 0.01 inch, the maximum heat flux which can be passed through a 347 stainless steel tube wall is 41 Btu/sq. in. sec. For 0.012 inch inconel X tubing a peak heat flux of 41 Btu/sq. in. sec. can be passed through the wall. In certain applications where tubing strength is a factor, inconel X is preferable to 347 stainless steel because its strength is much greater.

The local heat flux is absorbed entirely by the coolant according to the following expression which must be satisfied simultaneously with the previous two steady state expressions

$$Q/A = h_c (T_{WC} - T_{BC})$$

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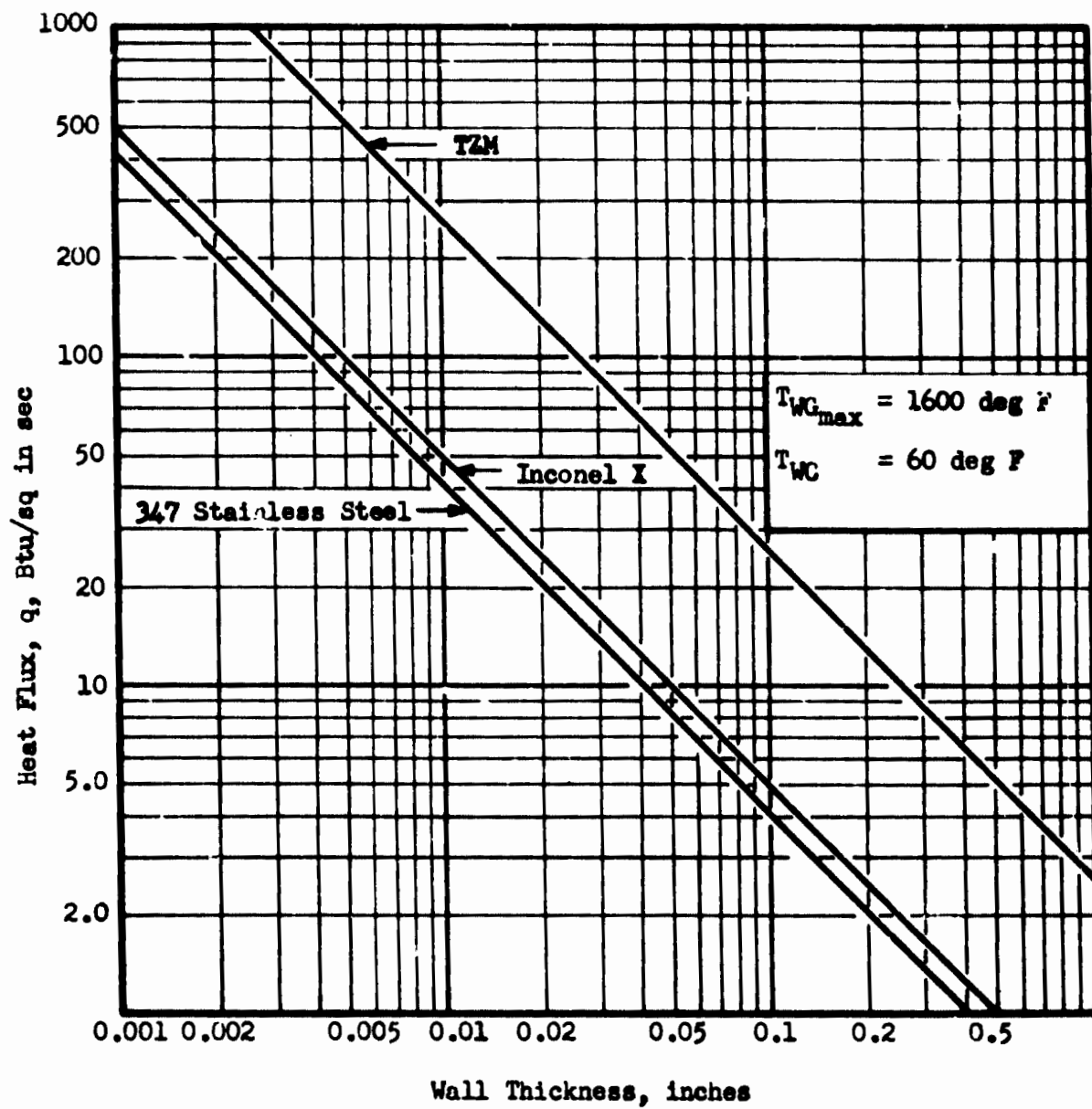


Fig.143. Heat Conduction Limits of Various Materials

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where T_{BC} is the coolant bulk temperature and the coolant side film coefficient h_c is computed from an empirical correlation of experimental data developed at Rocketdyne.

$$N_{Nu} = \frac{h_c D}{k} = 0.005 Re^{0.95} Pr^{0.4} \phi$$

The enhancement factor ϕ is used for N_2O_4 cooling at supercritical pressure to account for the large increase in its cooling capacity caused by the endothermic dissociation of N_2O_4 to NO_2 at the tube wall.

The relationships described above are programmed for machine computation. The three equations describing the heat flux are solved simultaneously at numerous stations along the thrust chamber using imposed restrictions such as maximum T_{WC} , tube thickness, maximum T_{WC} , etc. Coolant bulk temperature rise, velocity and pressure drop are computed at the same stations and, where applicable, numerically integrated. The cooling feasibility curves discussed in the following paragraphs were generated using this computer program.

Results. The coolant jacket pressure drop with N_2O_4 coolant at supercritical pressures is shown as a function of chamber pressure in Fig. 144. The sharp inflection of the curves clearly defines the maximum feasible operating chamber pressure within a narrow band for a given thrust level. The smallest engine which was regeneratively cooled was approximately 3000 pounds thrust with a maximum chamber pressure limit of 1500 psia. For the maximum thrust level considered of 300,000 pounds, the limiting chamber pressure was approximately 2650 psia. For the intermediate thrust levels of 10,000 pounds and 50,000 pounds, the limiting chamber pressures were approximately 1750 psia and 2150 psia respectively.

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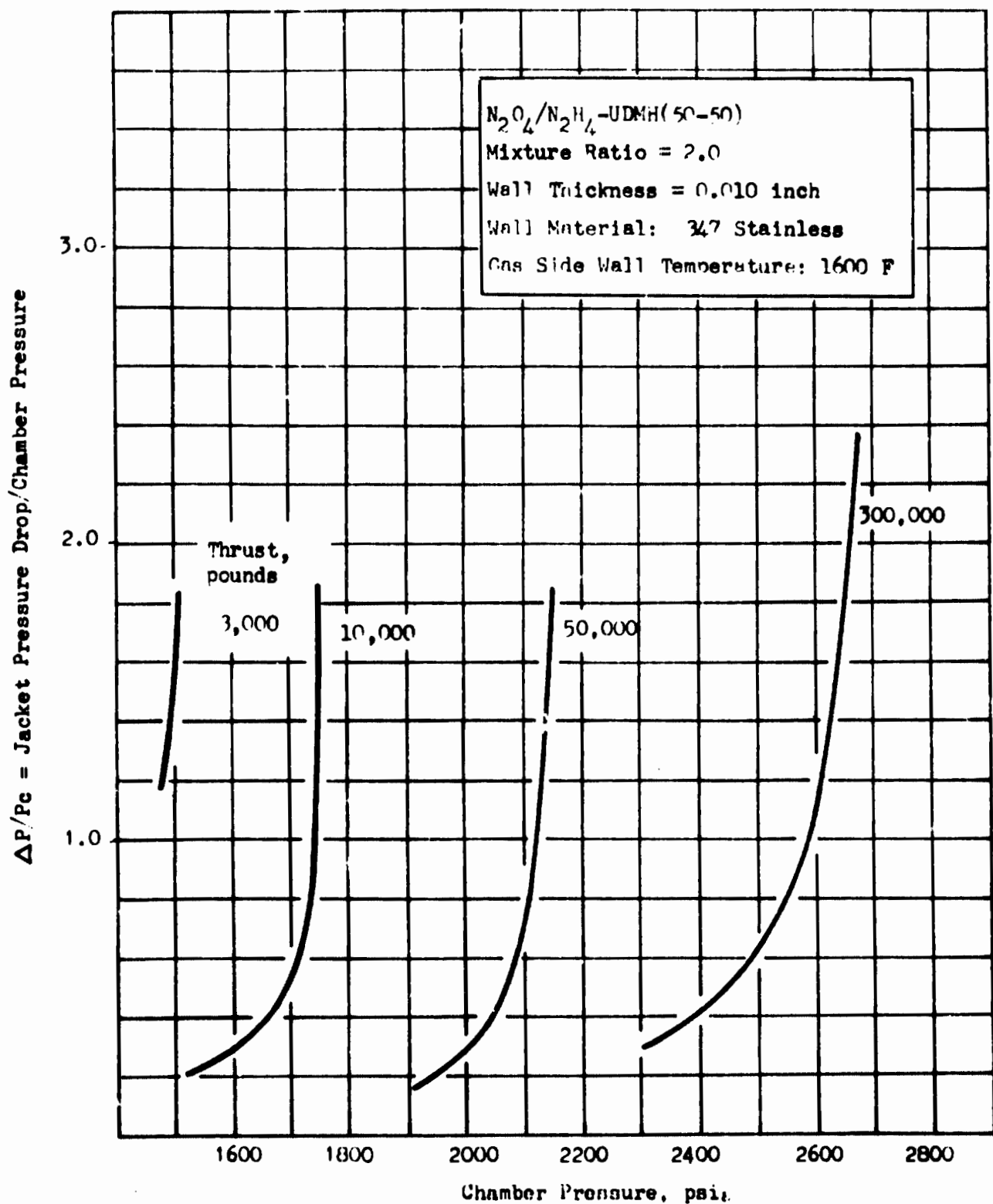


Fig.144. Tube Bundle Pressure Drop vs Chamber Pressure
for Bell Thrust Chamber Using N_2O_4 Coolant

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The data is replotted in Fig. 145 showing the limiting chamber pressure vs thrust level with ratio of tube pressure drop to chamber pressure as a parameter. Since a very small gain in the maximum operating chamber pressure limit (100 psi to 200 psi) is experienced by increasing the $\Delta P/P_c$ from 0.4 to 1.8 it is more likely that the lower limit curve would be used in an actual engine application.

For use in a multichamber aerodynamic spike nozzle application over a thrust range from 20,000 to 2,000,000 pounds a cluster of 8 chambers would have individual thrusts of from 2500 to 250,000 pounds. The curves indicate that regenerative cooling with N_2O_4 above its critical pressure is feasible for conventional thrust chambers in this thrust range. Extrapolation of the $\Delta P/P_c = 0.4$ curve to 2500 pounds thrust shows a maximum chamber pressure of approximately 1350 psia. The same curve indicates a maximum chamber pressure of approximately 2375 psia for a 250,000 pound thrust engine. A cluster of 16 engines with a total thrust of 2,000,000 pounds and an individual engine thrust of 125,000 pounds has a maximum chamber pressure limit of approximately 2200 psia. Thus for the same total thrust level the use of a larger number of clustered engines will reduce the maximum engine operating pressure a significant amount.

The coolant pressure drop with UDMH- N_2H_4 (50-50) coolant is shown as a function of chamber pressure in Fig. 146. It can be seen that the pressure drop requirements increase gradually over a wide range of chamber pressure making it rather difficult to select a distinct maximum operating chamber pressure. If an arbitrary $\Delta P/P_c$ limit of 2.0 (which is far in excess of the normal design value) is assumed then maximum chamber pressure for thrusts of 10,000 pounds, 60,000 pounds and 300,000 pounds are 250 psia, 1200 psia, and 2000 psia, respectively.

The data are replotted in terms of maximum chamber pressure as a function of thrust level in Fig. 147. Using the $\Delta P/P_c = 2.0$ curve for a module thrust of 2500 pounds an eight-module, fuel cooled, multichamber configuration

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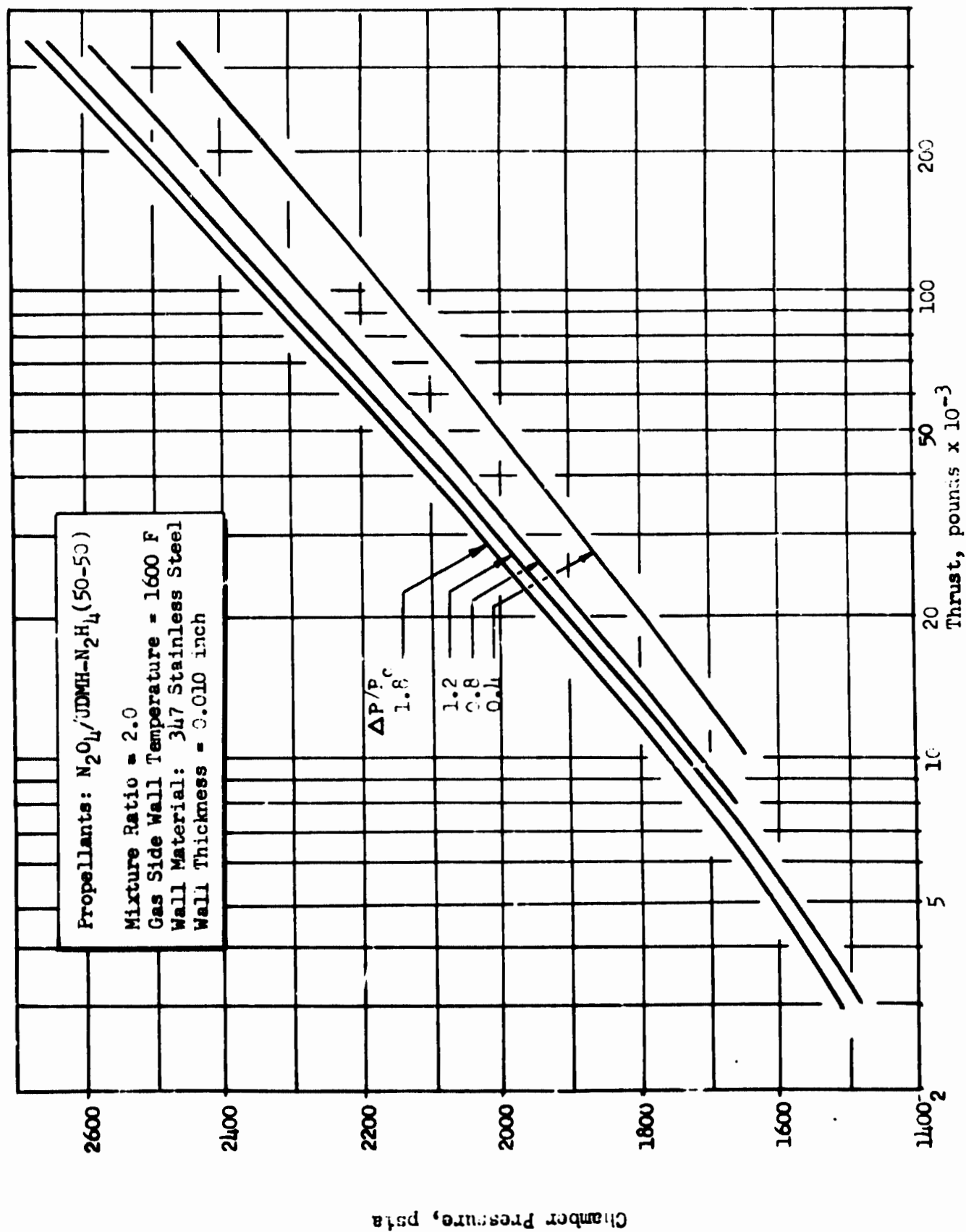


Figure 145. Regenerative Cooling Limits for Bell Thrust Chambers, Using N_2O Coolant

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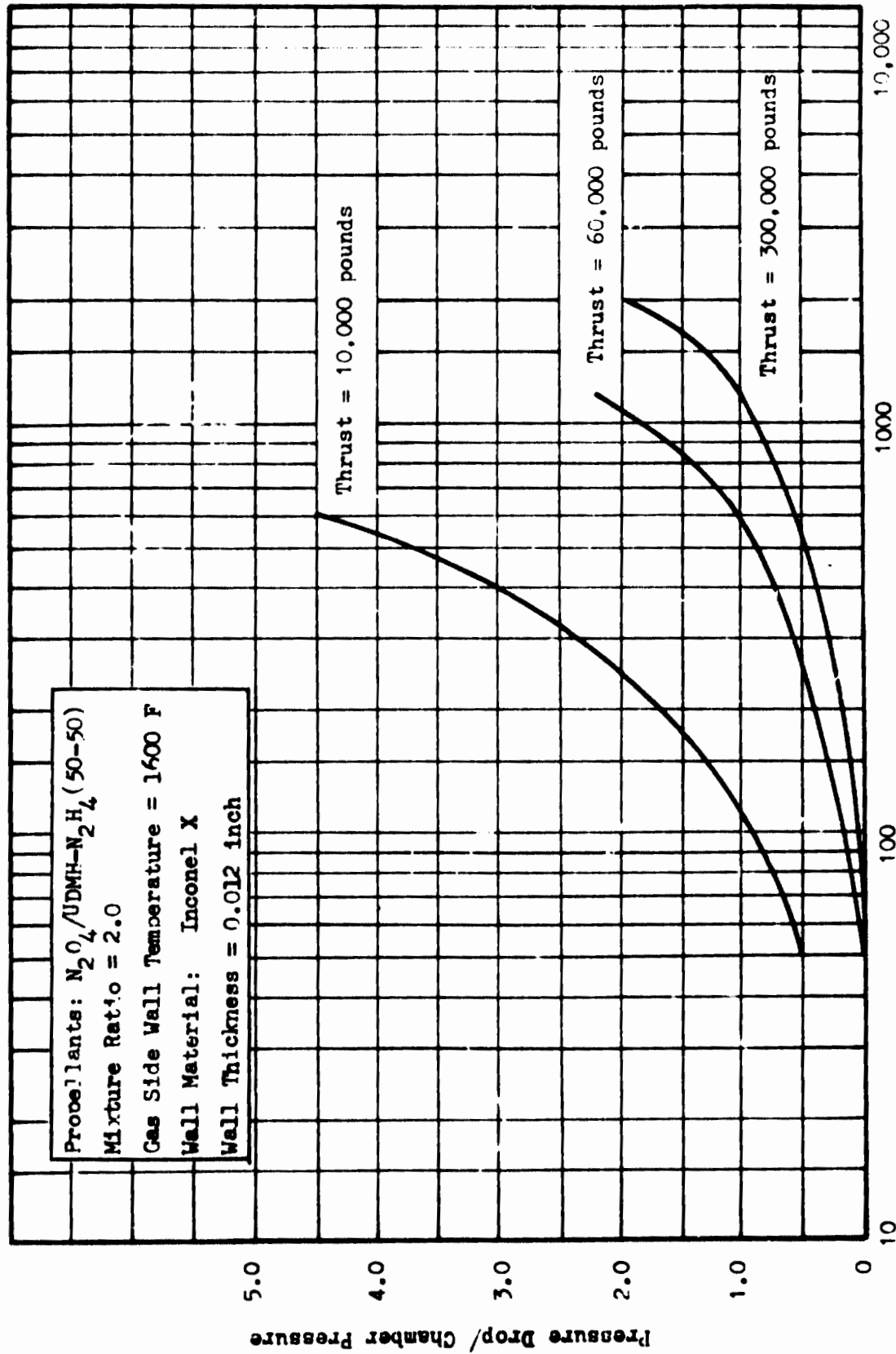


Fig.146. Pressure Drop/Chamber Pressure vs Chamber Pressure for Bell Thrust Chambers Using $UDMH-N_2H_4$ (50-50) as Coolant

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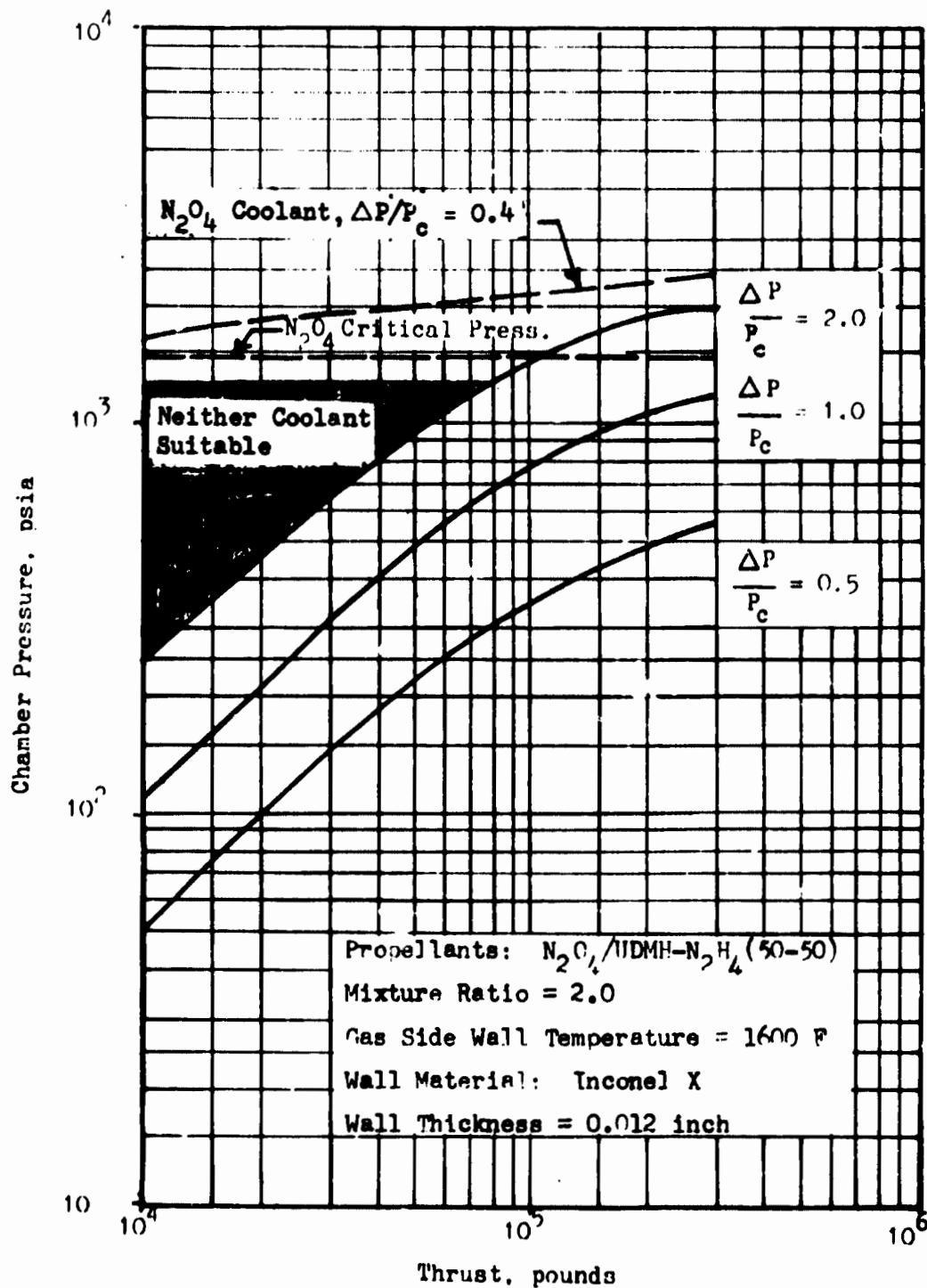


Fig. 147 Regenerative Cooling Feasibility Limits for Bell Thrust Chambers Using UDMH - N_2H_4 (50-50) as Coolant

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would have a maximum chamber pressure of approximately 70 psia. With N_2O_4 coolant at supercritical pressure this same module size could operate at 1350 psia with a $\Delta P/P_c = 0.4$. At this thrust level there is therefore a large range of chamber pressure (approximately 70 to 1250 psia) over which neither coolant is satisfactory. This occurs because cooling with N_2O_4 at subcritical pressure results in tube pressure drops higher than with fuel coolant and cooling with supercritical N_2O_4 requires that the coolant exit the tubes at approximately 1500 psia, regardless of the chamber pressure. Since a nominal injector pressure drop is 10 to 20 percent of the chamber pressure, the excess of the tube exit pressure over the required injector inlet pressure is wasted. From Fig. 147 it appears that this awkward region (between $P_c = 1250$ psia and the $\Delta P/P_c = 2$ curve) where neither coolant is entirely satisfactory at intermediate chamber pressures extends to a module thrust level of approximately 80,000 pounds or an eight-module multichamber thrust level of 640,000 pounds. The range of undesirable chamber pressures decreases, however, as the thrust level increases.

The maximum chamber pressure with fuel cooling for an eight-module multichamber configuration of 2,000,000 pounds thrust is approximately 2,000 psia ($\Delta P/P_c = 2.0$ curve) compared to approximately 2400 psia for chambers cooled with N_2O_4 .

Regenerative Cooling Limits for Toroidal Combustors

Maximum chamber pressure limits with full regenerative cooling were determined for aerodynamic spike thrust chambers using a toroidal type chamber construction. Machine computation of pressure drops and bulk temperature rise were conducted assuming a continuous annular throat configuration. The results also represent upper limits for other types of toroidal chamber construction such as the subsonic tube and the sonic tube shown in Fig. 113

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The chambers were analyzed using UDMH- N_2H_4 (50-50) coolant and N_2O_4 coolant at both subcritical and supercritical pressure. The results are presented in parametric curves of maximum chamber pressure as a function of the ratio of engine thrust to engine diameter and of area ratio.

Method of Analysis. The method of analysis for toroidal chambers is similar to that described for the conventional chambers with one major difference. A boundary layer approach (Ref. 15 and 16) was employed to calculate the gas side convective coefficients of the annular nozzles.

The conventional tube material selected for the study was 347 stainless steel with a tube thickness of 0.010 inch. The material was assumed to have a maximum allowable temperature of 1600 deg. F. The hoop radius of the combustion chamber was three inches with the engine having an ϵ equal to 100 and a 20-percent length nozzle. For the overall area ratio, a thrust coefficient of 1.8 was assumed.

At the subcritical pressures, the coolant-side wall temperature was assumed equal to the saturation temperature. This saturation temperature is determined by the allowable coolant vapor pressure. The coolant vapor pressure must be less than the coolant static pressure to prevent a bulk boiling condition. At the critical pressure, the coolant-side wall temperature was taken as 500 deg. F for 50-50 fuel. Above this temperature, the capability of 50-50 fuel was found to be limited because of tube failure apparently caused by rapid thermal decomposition at the wall. With N_2O_4 as the coolant, the limiting wall temperature was 600 deg. F. Above this wall temperature, oxidation occurs which limits the cooling design. As the chamber pressure is increased from the critical pressures for either coolant, the coolant wall temperature is forced down because of the limitation placed on the gas side wall temperature. When the coolant wall temperature is decreased, the weight flow requirement per tube increases. In

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order to meet the weight flow requirement per tube, multiple-pass cooling circuits were necessary. The number of passes varied for the different operating conditions that were analyzed.

A multipass configuration is illustrated in Fig. 148 . The coolant flow circuit begins at the injector, proceeds to the nozzle skirt exit, and continues back through another set of tubes to the injector. This constitutes a 2-pass cooling circuit. For other cooling circuits, the pattern will be similar but with more passes.

A similar-type cooling circuit was assumed for the shroud part of the toroidal thrust chamber. The total coolant flowrate was split, half of it cooling the nozzle part of the thrust chamber and the other half cooling the shroud part. It was assumed that the pressure drop and temperature rise were the same in either section.

The pressure drop evaluation was conducted for continuous annular throat toroidal thrust chambers only. Similar computations to include configurations such as the segmented annular throat toroidal chamber, the subsonic toroidal chamber, and the sonic toroidal chamber were not done. However, the limits established by the present study are also applicable as upper limits for the other toroidal combustors. Each of the previously mentioned design configurations have more surface area which must be cooled than its counterpart continuous-throat annular chamber. Thus it would be expected that the former designs will require higher pressure drops and bulk temperature rises.

The study was conducted for engines with a combustor hoop radius of three times an area ratio of 100. But the results are applicable to other hoop dimensions and area ratios. The total heat input in the combustor varies slightly with combustor hoop radius. Thus, the pressure drop is approximately

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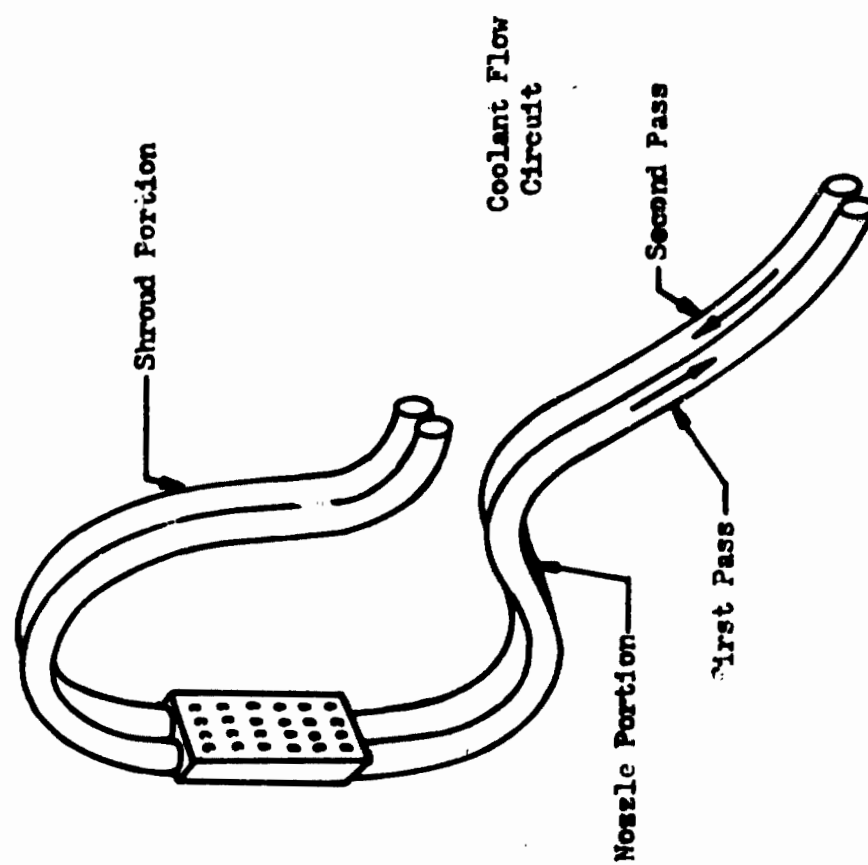


Fig. 148 Toroidal Combustor

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the same. For the annular engine the heating conditions at a given chamber pressure normalize as a function of engine thrust to annular throat diameter F/D . From the simplified relationships below for a continuous throat toroidal aerospike it can be seen that specifying the thrust and throat diameter determines the throat gap and area ratio at a given chamber pressure.

$$F = P_c A_t C_F = P_c C_F \pi d_T D$$

$$\epsilon = A_c/A_t = D/4 d_T$$

$$F/D = P_c C_F \pi D/4 \epsilon$$

Results. Pressure drop and gas side wall temperature limit curves for UDMH- N_2H_4 (50-50) and N_2O_4 as coolants are shown in Figs. 149 and 150. The values are plotted as a function of chamber pressure and the ratio of thrust to engine diameter. The region to the left of the lines of constant T_{WC} is unfeasible since the lines represent a condition where T_{WB} equals T_{WC} . The limit lines of constant T_{WC} also represent a condition where the coolant bulk temperature equals the coolant side wall which in turn assumes an infinite coolant velocity and pressure drop. The limit lines based upon constant values of $\Delta P/P_c$ are more realistic since they show the practical limitations of coolant pressure drop based upon detailed analysis of the engine coolant circuit.

It can be seen that the $\Delta P/P_c$ limit curves correspond closely to the T_{WC} and T_{WB} limit curves for N_2O_4 cooling at supercritical pressures but are considerably below the T_{WC} and T_{WB} limit curves for cooling with fuel and N_2O_4 at subcritical pressure. This is because the velocity head requirement for N_2O_4 above its critical pressure is almost constant for a considerable range of bulk temperature values (Fig. 141) whereas it is not for fuel and N_2O_4 at subcritical pressures (Fig. 140).

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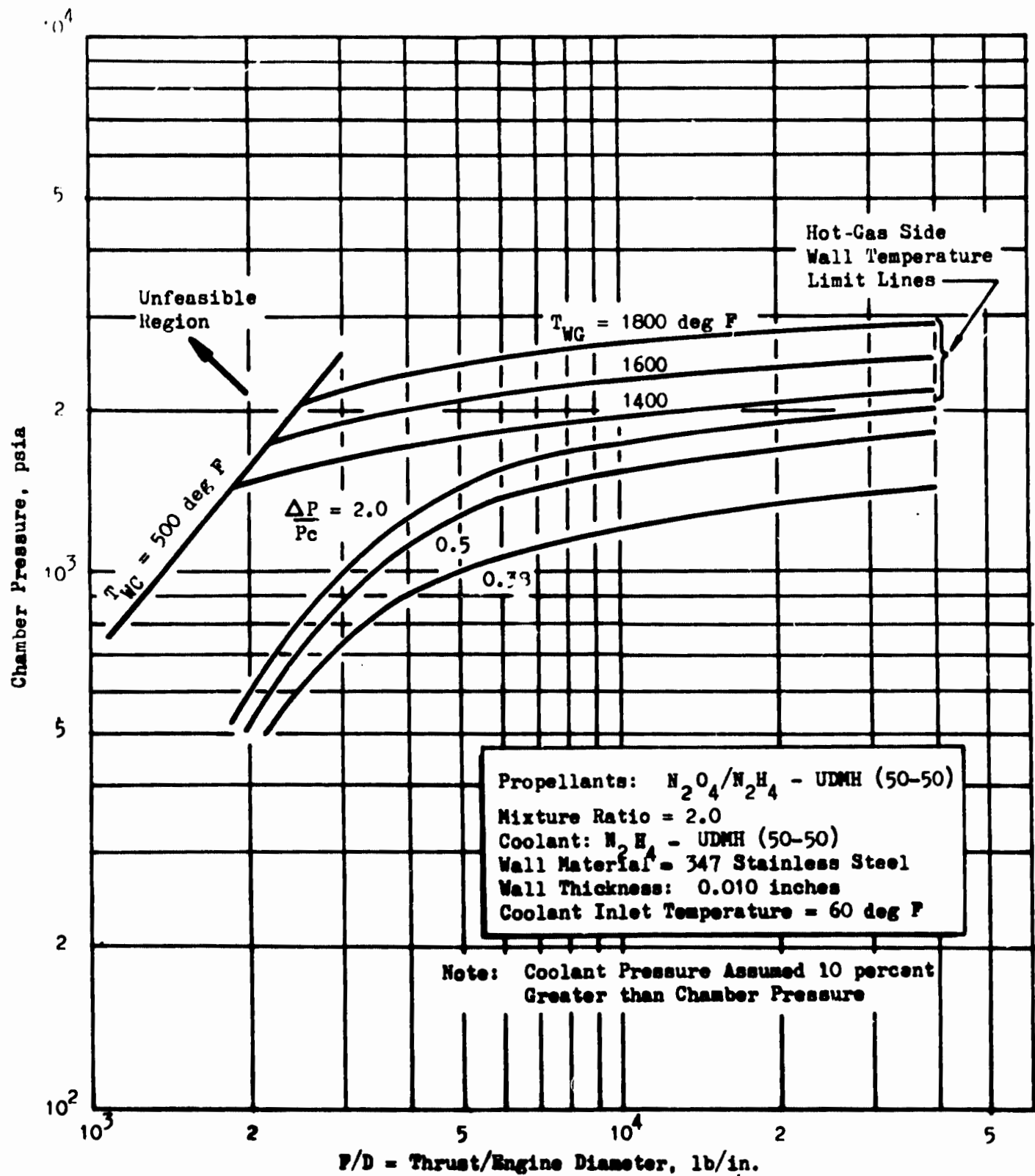


Fig.149 Cooling Feasibility Limits and Pressure Drops for Continuous Annular Throat Toroidal Combustors Using N_2H_4 -UDMH as Coolant

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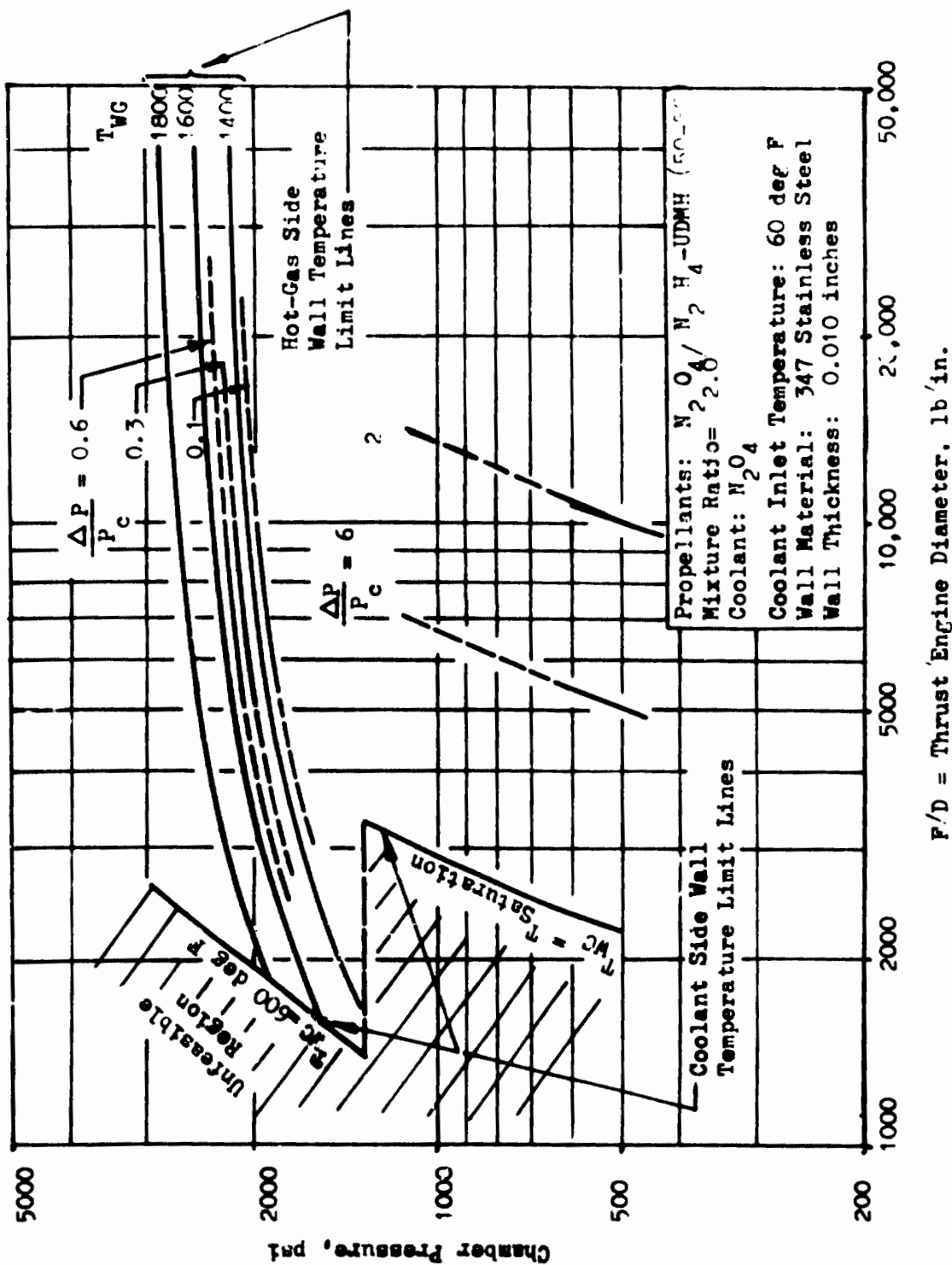


Fig. 150 Cooling Feasibility Limits and Pressure Drops for Continuous Annular Throat Toroidal Combustors Using N_2O_4 as Coolant

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The pressure drop limit curves are replotted in more recognizable terms in Figs. 151 and 152. Figures 151 and 152 show the maximum area ratio as a function of chamber pressure for thrust levels from 10,000 pounds to 2,000,000 pounds. The limit curves for fuel coolant are based upon a $\Delta P/P_c$ value of 2.0. The limit curves for N_2O_4 coolant at subcritical and supercritical pressures are based upon constant $\Delta P/P_c$ values of 2.0 and 0.6 respectively. It should be noted that the bell chamber limit curves were essentially independent of area ratio while the limiting chamber pressure for annular nozzles is a strong function of area ratio.

For both fuel and oxidizer coolant the curves in Figs. 151 and 152 show similar trends. As the thrust level decreases the range of area ratios and chamber pressures which can be regeneratively cooled decreases. For an engine thrust level of 20,000 pounds and intermediate chamber pressures of 300 to approximately 1250 psia, cooling with N_2O_4 below its critical pressure is not feasible while fuel coolant is feasible only to area ratios of approximately 5. However extrapolation and interpolation of the limit curves for supercritical N_2O_4 to 1250 psia chamber pressure and 20,000 pounds thrust indicates that an area ratio of approximately 30 may be regeneratively cooled. This is similar to the situation encountered for conventional chambers of low thrust level.

For the upper thrust level of interest, 2,000,000 pounds, the chamber pressure limit for a nominal area ratio of 40 is approximately 1800 psia with fuel coolant and approximately 2275 for N_2O_4 coolant. These values are comparable with the eight-module 2,000,000 pound thrust multichamber limits of 2000 psia and 2400 psia for fuel and oxidizer coolants, respectively.

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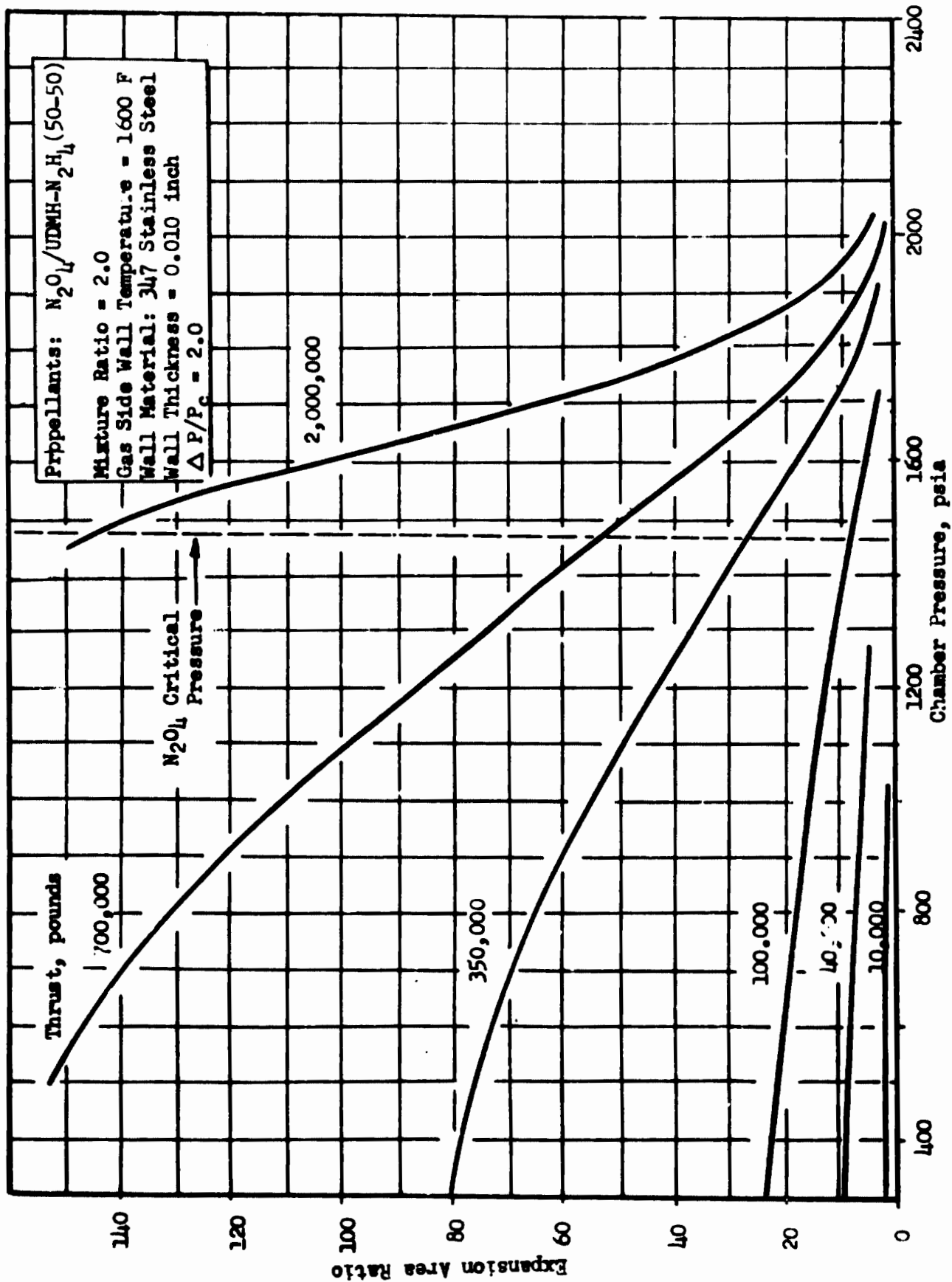


Figure.151 Regenerative Cooling Limits for Continuous Throat Toroidal Combustors Using UDMH- N_2H_4 (50-50) as Coolant

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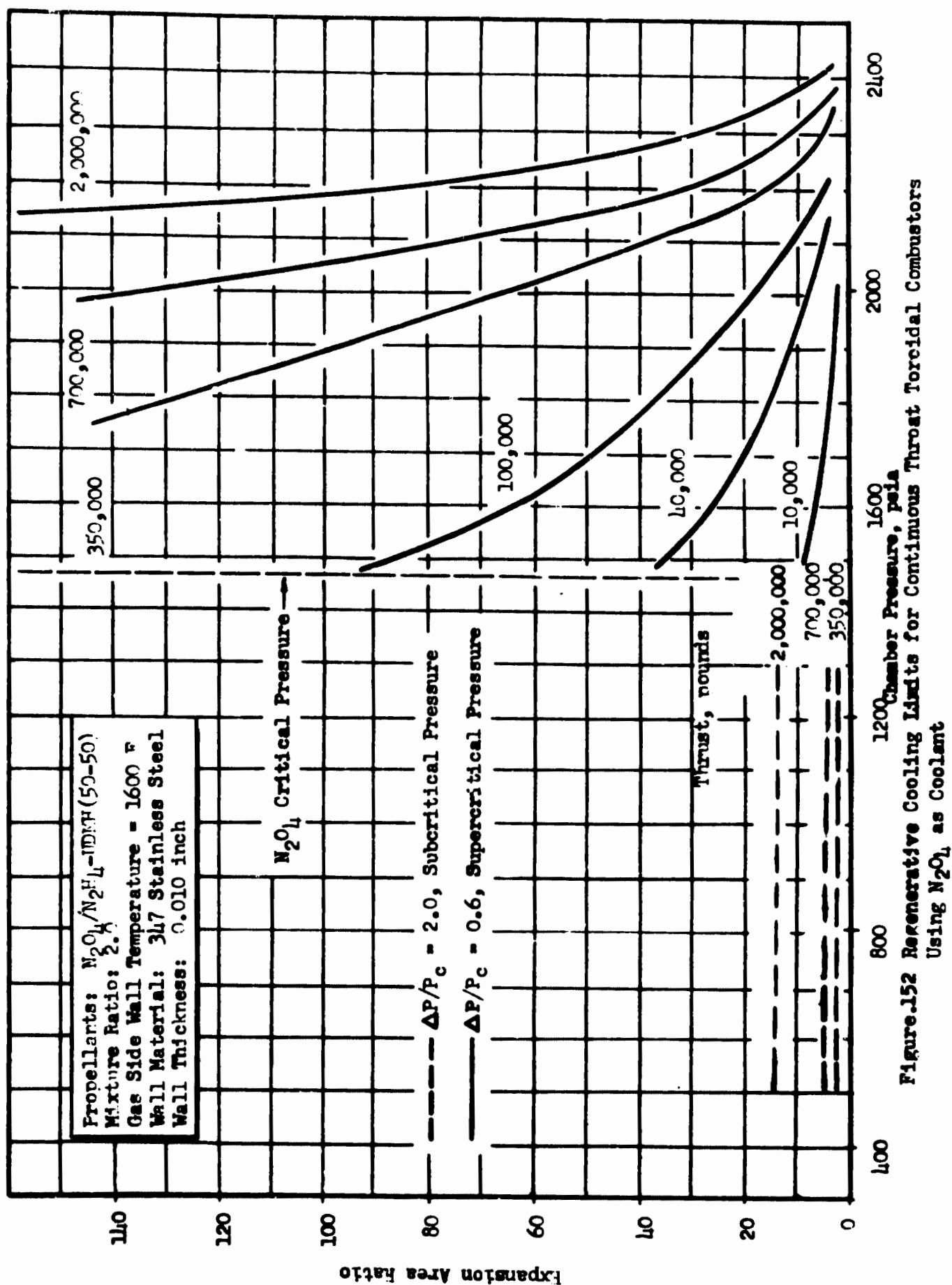


Figure.152 Regenerative Cooling Limits for Continuous Throat Toroidal Combustors Using N_2O_4 as Coolant

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Alternate Design Techniques

The effort in this study concentrated on establishing regenerative cooling limits for aerospike combustors using conventional materials. It should be noted however that the region of applicability of these combustor concepts can be extended by alternate design techniques. Thus, marginal designs shown in the figures can be cooled with judicious changes from the set conditions specified in the study. In the subsequent discussion, the above desirable changes will be discussed in conjunction with the aerospike design.

Increase Coolant Wall Temperature. Near the throat region at high chamber pressures, the coolant-side wall temperatures were lower than the maximum allowable value. This was because of the limitation placed on the gas-side wall temperature. Thus by selecting a material which can withstand a higher gas-side wall temperature, an increase in the coolant side wall temperature can be realized.

From the heat conduction equation

$$Q/A = \frac{k}{X} (T_{WC} - T_{WC})$$

increase in the conductivity of a selected material will also be beneficial. This will reduce the temperature gradient through the coolant tube walls.

Another property of a selected material is the yield strength. With a higher strength material, the minimum tube thickness can be decreased. This in turn will increase the coolant wall temperature. Thus it would be desirable to select a material which has a higher gas-side maximum allowable wall temperature, higher thermal conductivity, and higher yield strength. Refractory metals will fit the three categories.

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Curvature Effects at the Throat Region. The major problem in cooling the aerospoke design is the high heat flux located at the throat region. In order to cool this portion of the nozzle, a high coolant mass velocity is necessary. Consequently a high jacket pressure loss is induced (See Fig. 153). One means of decreasing the pressure drop is to utilize the enhancement of the coolant associated with particular tube curvatures. Rocketdyne has investigated curvature effects. An example of the results can be seen in Fig. 154 . A definite increase in cooling capability is realized when the coolant undergoes a rapid turning. A considerable amount of theoretical and experimental effort is still necessary to correlate influencing items such as the effect of the ratio of tube diameter to radius of curvature and bulk Reynolds number.

Mass Transfer Cooling. Augmenting the fully regenerative design with mass transfer cooling methods will reduce the heat input to the coolant. Consequently, a lower pressure drop can be realized.

Possible methods are transpiration cooling, film cooling, and ablation cooling. Transpiration cooling involves the introduction through a porous wall. Film cooling is realized by introducing a film of coolant onto the gas-side region through discrete slots or openings. The limiting case of film cooling is transpiration cooling. Ablation cooling is accomplished by utilizing a wall material that will melt, sublime, or decompose when introduced to the hot gas stream. These methods are similar in that the coolant material absorbs heat from the main stream gas and is then injected back into the main stream. Thus the overall heat flux which enters the coolant jacket is reduced. In some cases, this reduction can be considerable. It is quite feasible that ablation cooling may be applicable as a single means of cooling.

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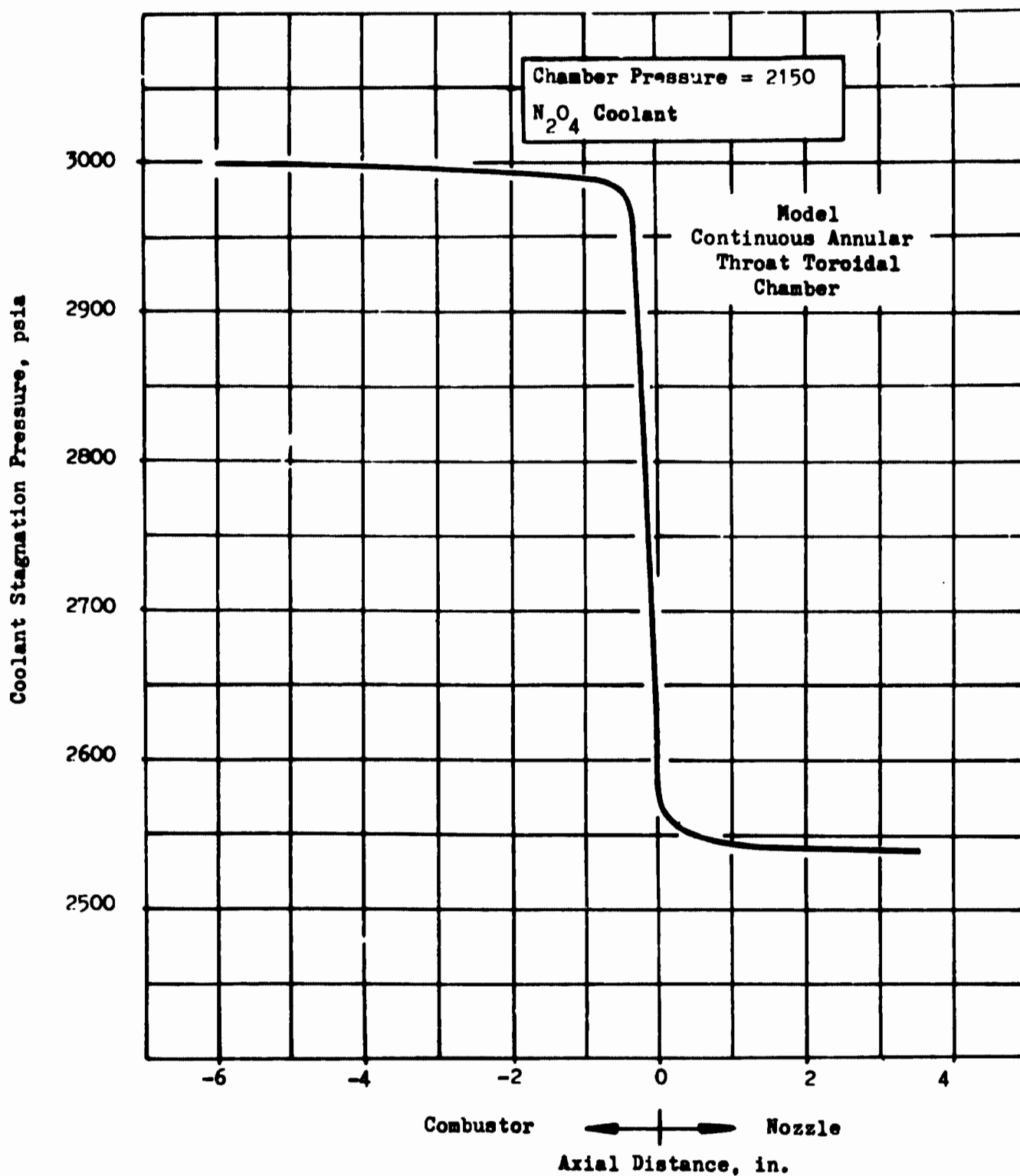


Fig.153. Typical Stagnation Pressure of Coolant vs. Axial Length

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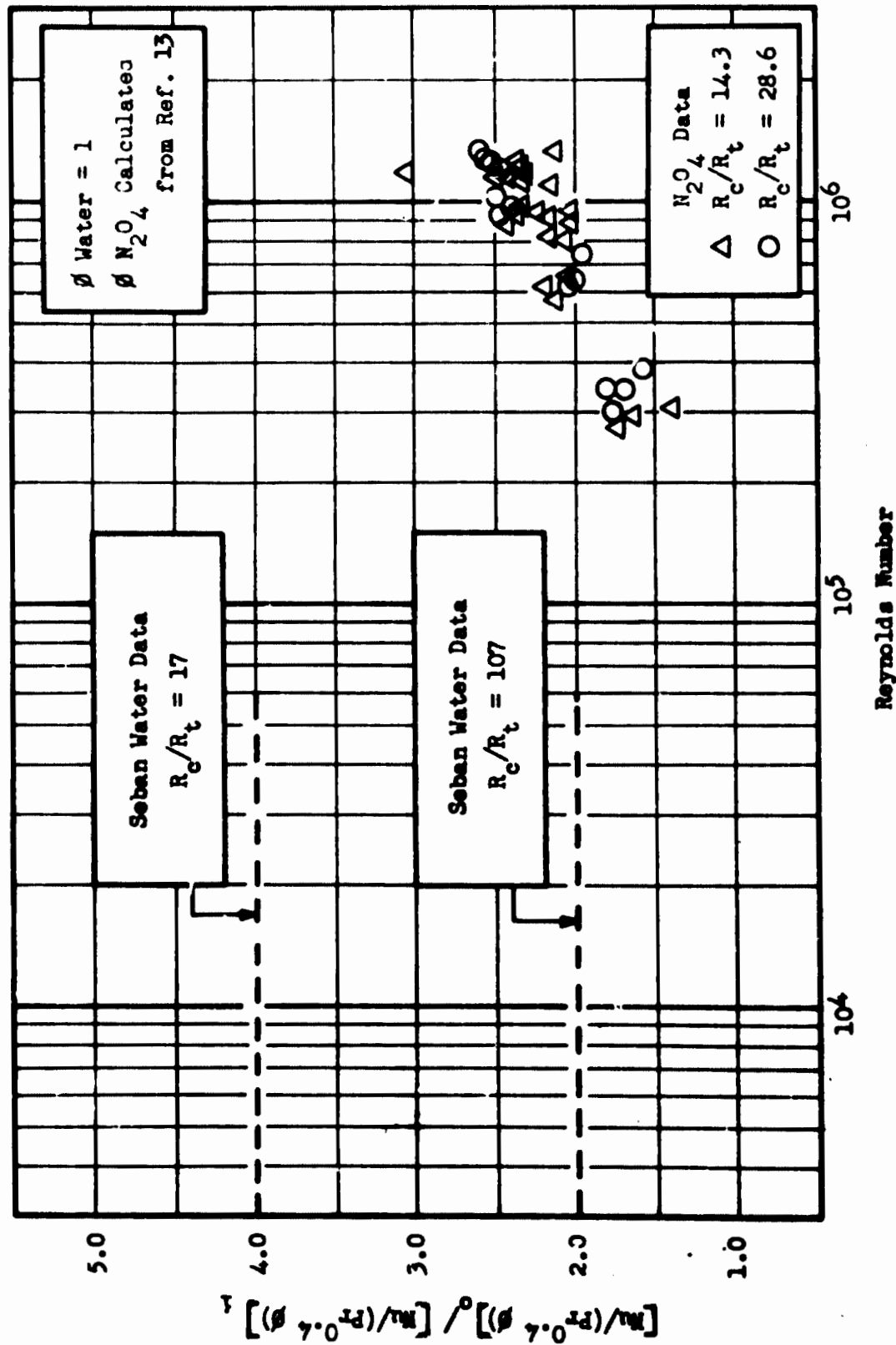


FIG. 154 . CONCAVE TO CONVEX SURFACE HEAT TRANSFER RATIO FOR CURVED TUBE EXPERIMENTS, CORRECTED FOR DISSOCIATION INFLUENCES

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Conclusions

Significant conclusions resulting from this study are the following:

1. Regenerative cooling of both multichamber and toroidal chamber aerospike becomes increasingly difficult as engine thrust level is decreased. At the 20,000 pound thrust level regenerative cooling of either multichamber or toroidal chamber aerospike appears possible only with N_2O_4 coolant at supercritical pressures. An alternate design approach such as an ablative chamber may be desirable for low thrust moderate chamber pressure applications.
2. For the upper thrust level range of interest, 2,000,000 pounds, the maximum chamber pressures for regenerative cooling attainable with a toroidal aerospike are approximately 200 psi lower than with an eight-module multichamber and are approximately the same as with a sixteen-module aerospike.
3. Regenerative cooling limits for the multichamber engines are relatively insensitive to either the module area ratio or the cluster area ratio. The chamber pressure limits for an annular throat configuration are a strong inverse function of area ratio.
4. N_2O_4 above its critical pressure is a better coolant than UDMH- N_2H_4 (50-50). Below the critical pressure of N_2O_4 the superiority of the coolants is reversed.
5. The range of feasibility of both combustor concepts may be extended from that indicated here by using alternate design techniques such as refractory tubing or coatings and partial or full mass transfer cooling.

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DESIGN STUDIES

The objective of this portion of the program was to determine effective methods of utilizing toroidal and multichamber constructions for aerodynamic spike configurations. Combustors considered included several toroidal types and clustered conventional chambers with both circular and noncircular exits. The studies covered a range consistent with Air Force propulsion requirements. These requirements include thrusts from 20,000 pounds to 2,000,000 pounds, chamber pressures from 300 psia to 3000 psia, and expansion area ratio of 150.

Employing design guidelines presented in the analysis section of this report, layouts of representative systems which use multichamber or toroidal aerodynamic spike nozzles were made together with corresponding conventional single bell engine systems. The design points selected for each system are shown in Table 12. These points cover the parameter range of interest and were selected to take advantage of previous design investigations at the same operating conditions.

TABLE 12

POINT DESIGN PARAMETERS

Thrust (1000 pounds)	Chamber Pressure (psia)	Area Ratio
40	500	100
350	2000	150
658	300	10
2000	2000	50

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The purpose of these layouts was to gain insight into the structural and operational aspects of systems employing the toroidal and multichamber combustor concepts and to appraise the systems size and complexity relative to the more conventional bell engine system. In Table 13 the major characteristics of the systems investigated at each of the four selected design points are presented. When designing the engine systems, different multichamber configurations (round and splayed exits, Fig. 155) and different toroidal combustor configurations (subsonic tube and baffled annular, Fig. 113) were selected. The purpose of this was to become familiar with the structural and functional aspects of the different combustors. The choice of combustor at a given design point was arbitrary. The aerodynamic spike nozzle lengths shown were also selected arbitrarily and do not represent the results of a performance optimization. The paragraphs that follow describe the design features of each of the selected systems; advantages, disadvantages, and potential problem areas are exposed in the process.

Point Designs - 40,000-Pound Thrust Level

Layouts of typical 40,000-pound thrust multichamber and toroidal chamber aerodynamic spike engines together with a conventional bell thrust chamber are shown in Figs. 156 , 157 , and 158 . The overall expansion area ratio of each engine is 100 and the chamber pressure is 500 psia.

The multichamber configuration consists of a cluster of 12 conventional regeneratively cooled chambers with tangent chamber exits. With tangent circular exits, the ratio of the overall area ratio ϵ_{CL} to the module

TABLE 13. DESIGN STUDY SUMMARY

Missile Type	Combustor Type	Type Cooling	Propellant Feed (Power Source)	Secondary Gas Source	Thrust (1000 lbs)	Chamber Pressure (psia)	Type TVC	Area Ratio	Missile Length from Throat (% cone)
Aerospike	12-Circular Exit Multichamber	Regenerative	Pump Fed (Chamber Tapoff)	Turbine Exhaust	40	500	Gimbal	100	14.0
Aerospike	Subsonic Tube	Regenerative	Pump Fed (Chamber Tapoff)	Turbine Exhaust	40	500	Gimbal	100	29.3
Bell	Cylindrical	Regenerative	Pump Fed (Chamber Tapoff)	---	40	500	Gimbal	100	80.0
Aerospike	8-Splayed Exit Multichamber	Regenerative	Pump Fed (Chamber Tapoff)	Turbine Exhaust	350	2000	Liquid Injection	150	18.9
Aerospike	Baffled Annular	Regenerative	Pump Fed (Chamber Tapoff)	Turbine Exhaust	350	2000	Liquid Injection	150	33.8
Bell	Cylindrical	Regenerative	Pump Fed (Chamber Tapoff)	---	350	2000	---	150	80.0
Aerospike	12-Circular Exit Multichamber	Ablative	Pressure Fed	Chamber Tapoff	658	300	---	11.5	17.3
Aerospike	Baffled Annular	Ablative	Pressure Fed	Chamber Tapoff	658	300	---	8.2	27.8
Bell	Cylindrical	Ablative	Pressure Fed	---	658	300	---	8	80.0
Aerospike	8-Circular Exit Multichamber	Regenerative	Pump Fed (Chamber Tapoff)	Turbine Exhaust	2000	2000	Liquid Injection	60	17.9
Aerospike	Baffled Annular	Regenerative	Pump Fed (Chamber Tapoff)	Turbine Exhaust	2000	2000	Liquid Injection	55	31.6
Bell	Cylindrical	Regenerative	Pump Fed (Chamber Tapoff)	---	2000	2000	---	35	80.0

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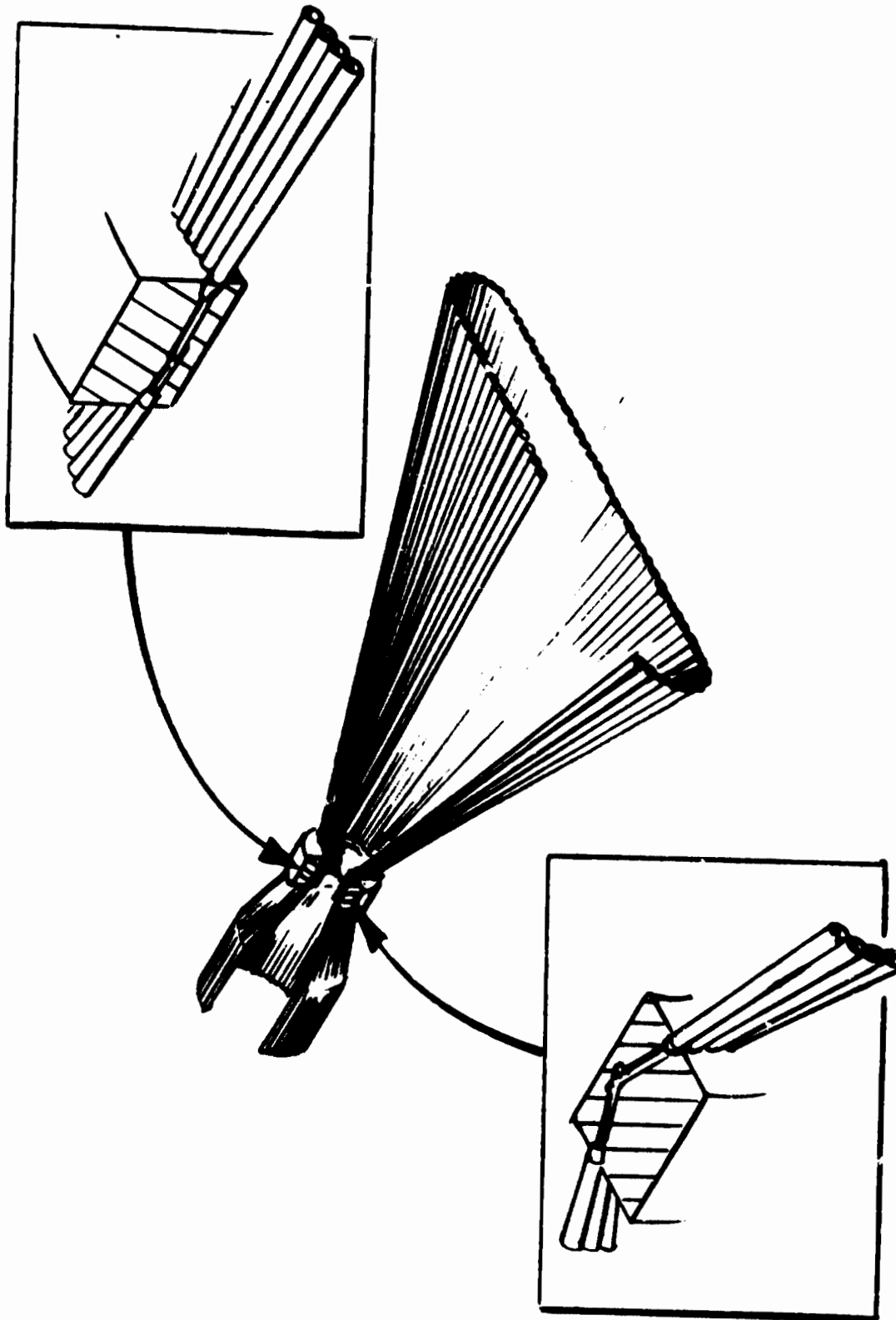
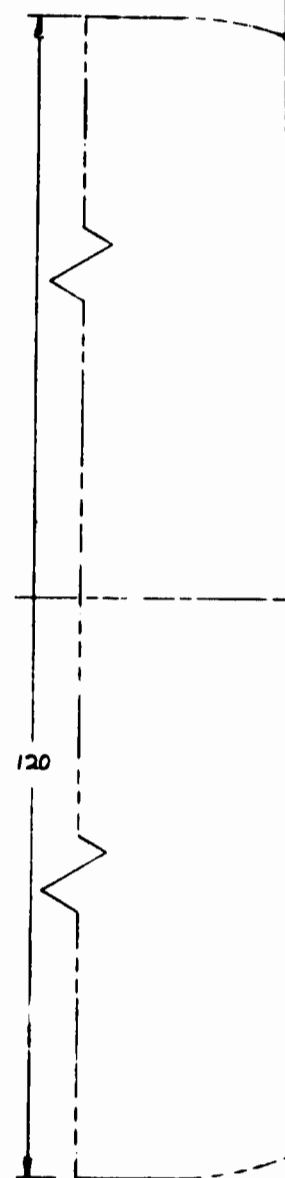
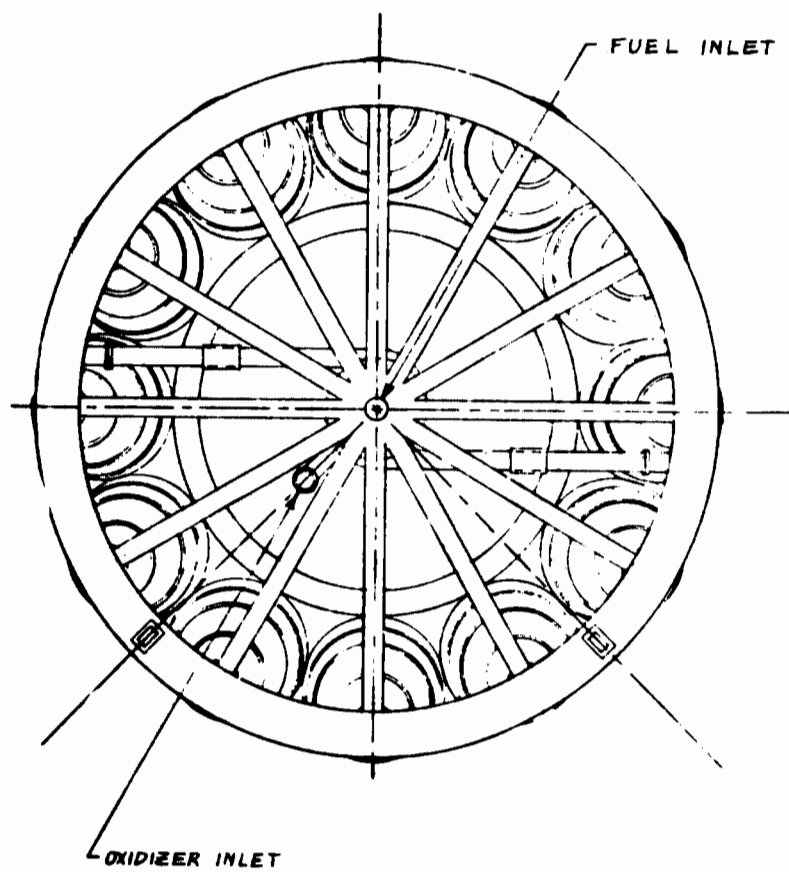
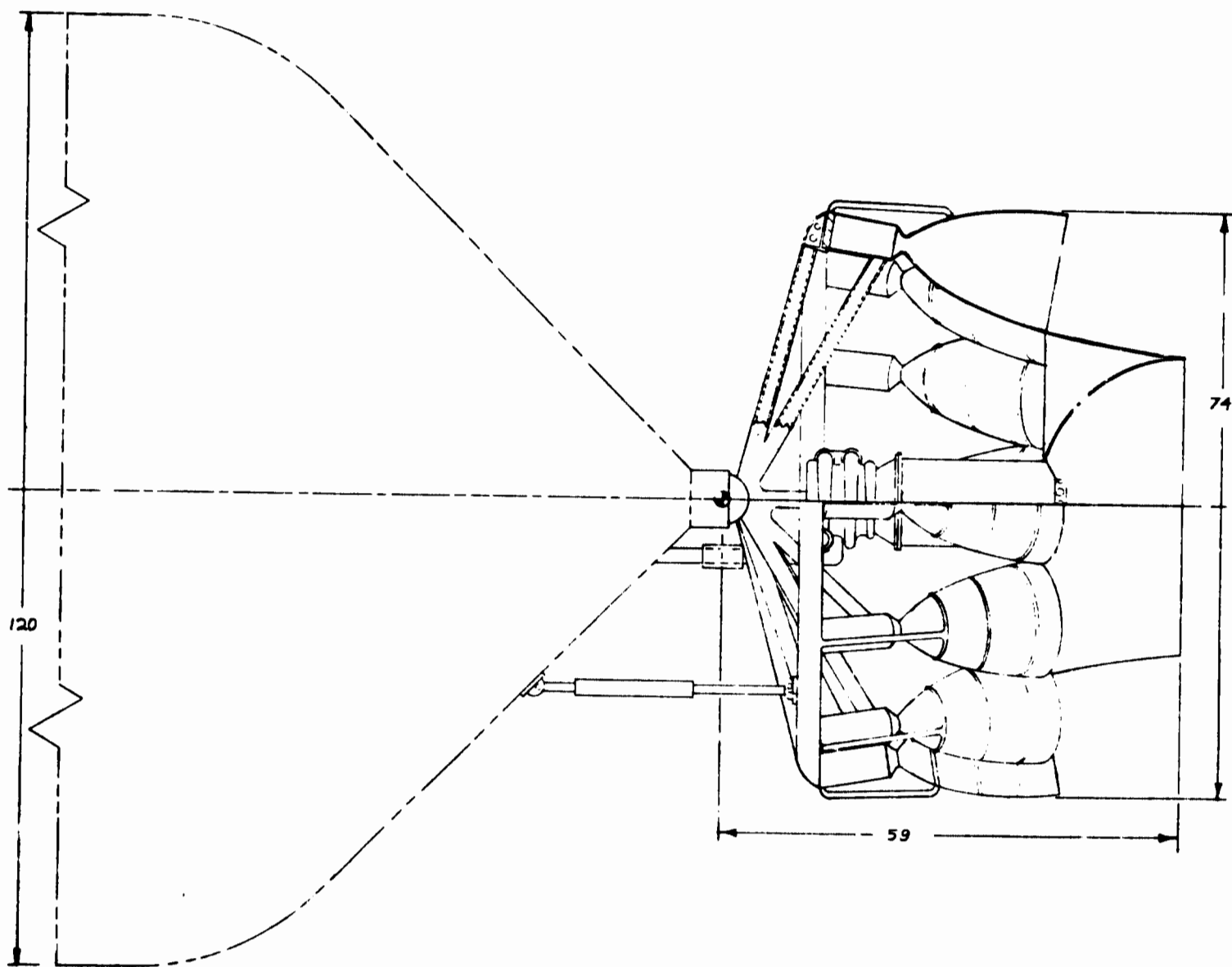


Fig.155. Splayed Exit Multichamber

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MAJOR SYSTEM PARAMETERS

$F = 40,000 \text{ LB}_f \text{ (VACUUM)}$

$P_c = 500 \text{ PSIA (NOZZLE STAGNATION)}$

$\epsilon = 100$

$\epsilon_M = 51.8$

PROPELLANTS • NTO/50-50

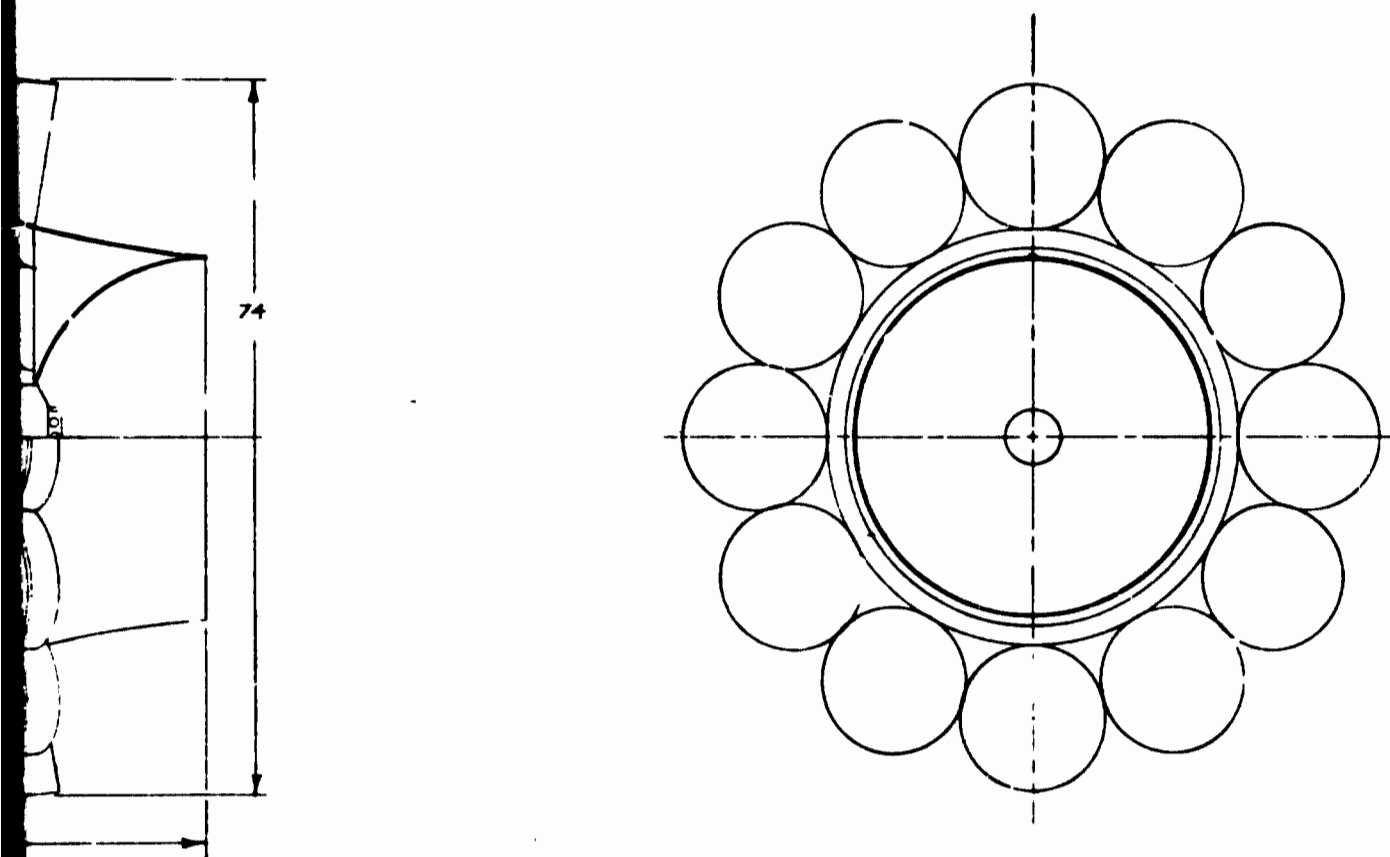
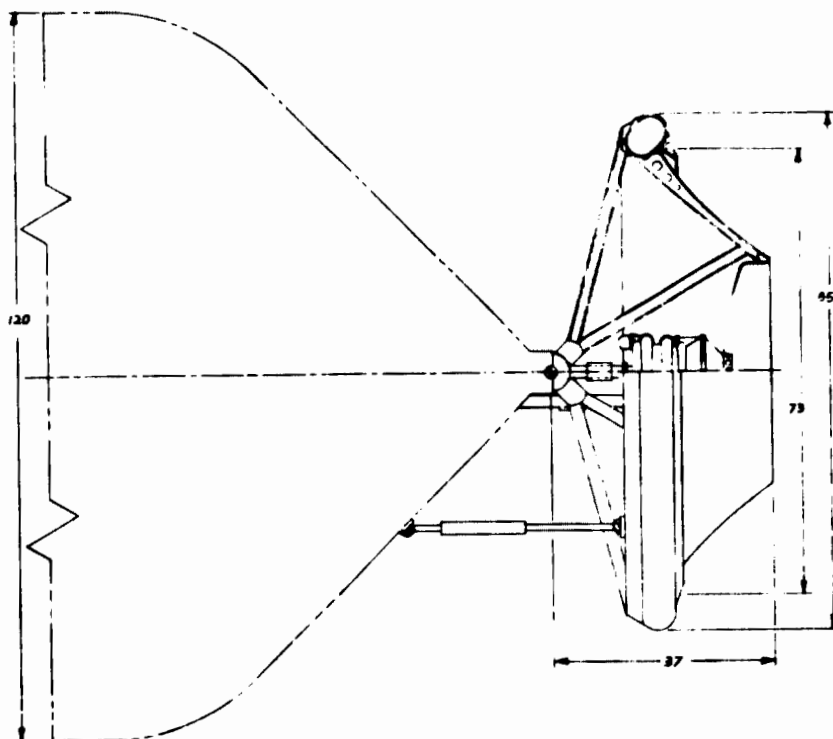
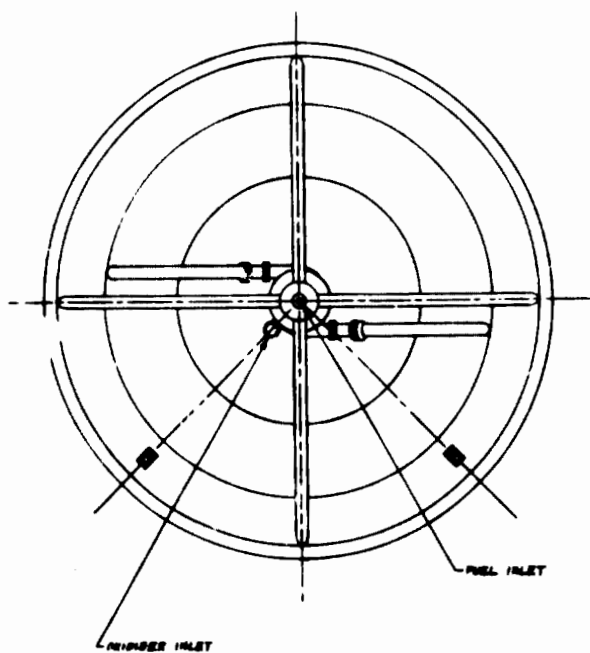
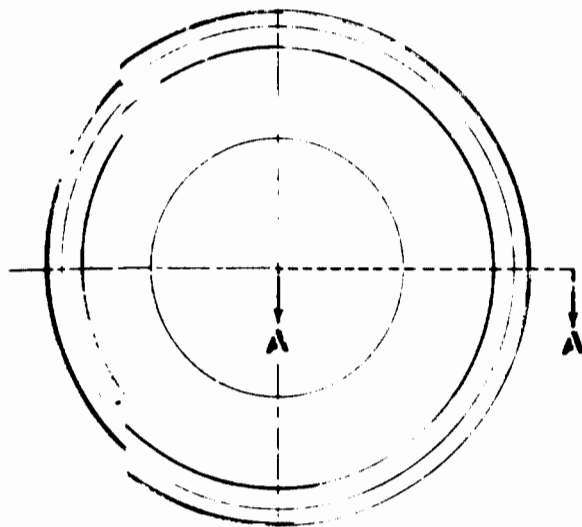
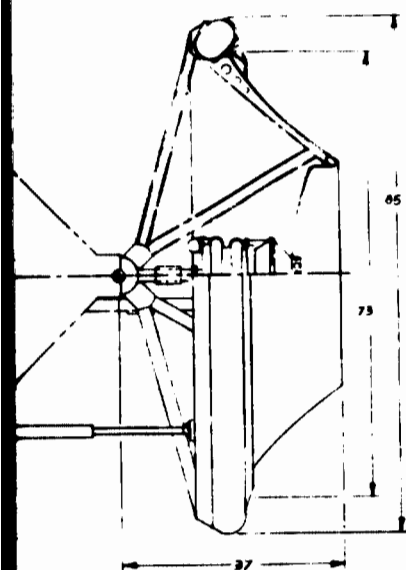


Fig.156. Aerospike Engine System,
Multichamber, Low Thrust,
and Low Chamber Pressure

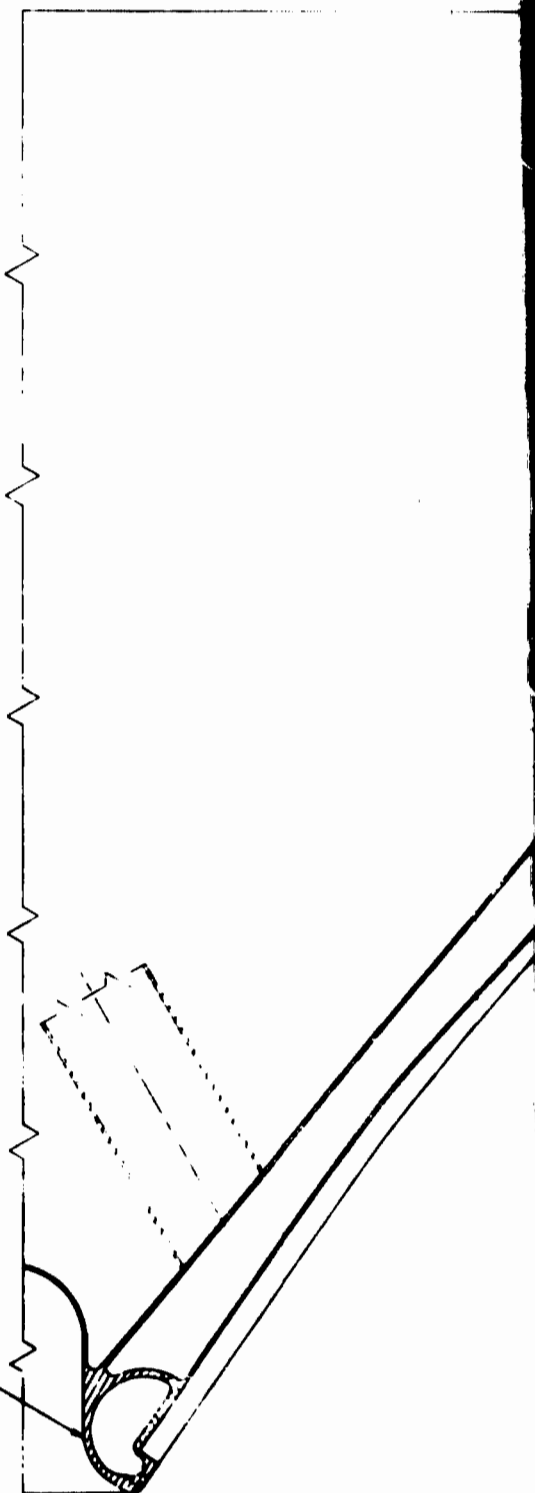


MAJOR SYSTEM PARAMETERS

F = 40,000 LBS (MAXIMUM)
B = 500 PSIA (DESIGN STRESS)
S = 100
PROPELLANTS = HTD/50-50



BRIDGE FEED MANIFOLD



NOSE SYSTEM PARAMETERS

= 40,000 LB. (MAXIMUM)
 = 500 PSIA (NOZZLE STIMULATION)
 = 100
 PROPELLANTS = NT0/50-50

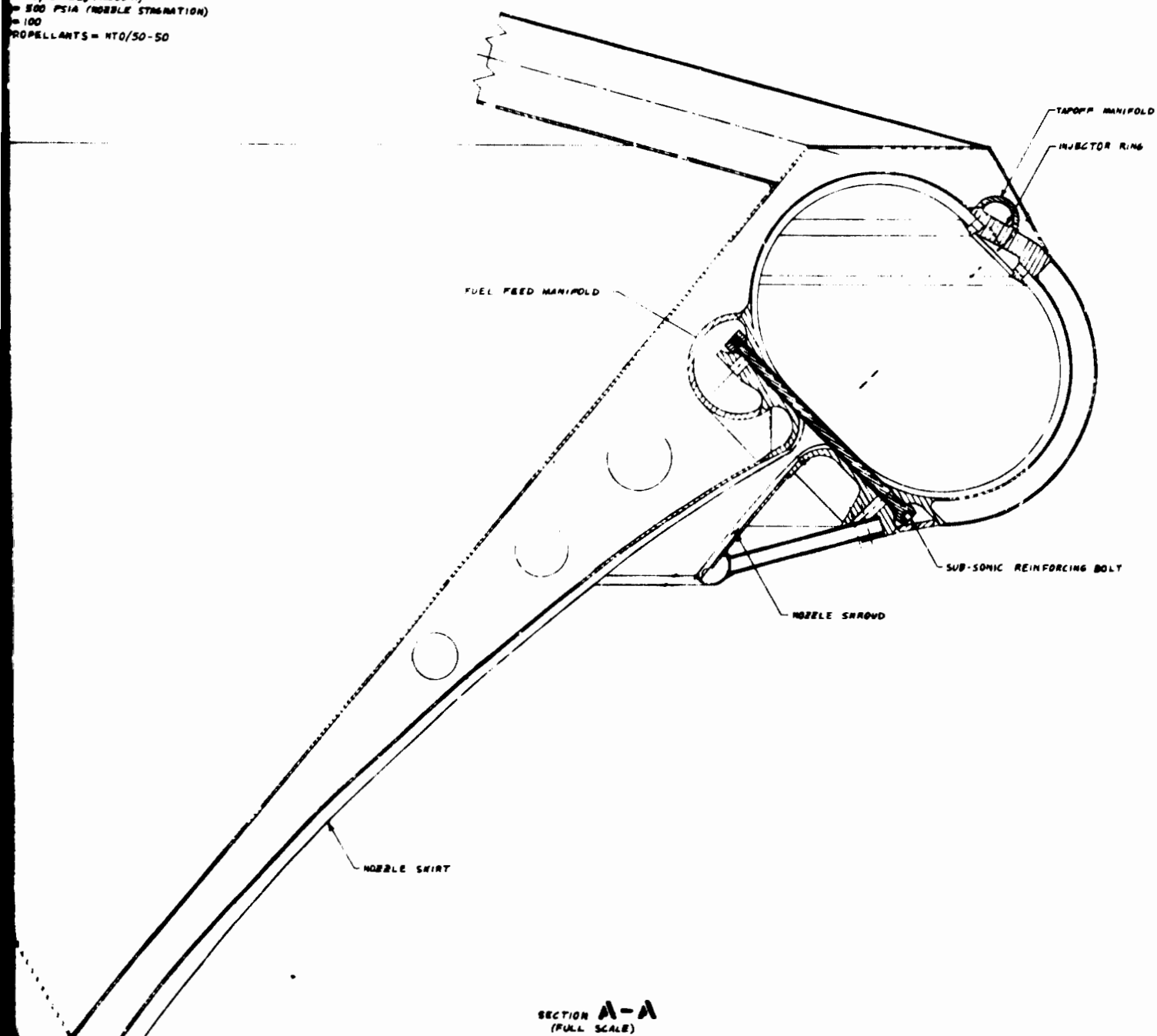
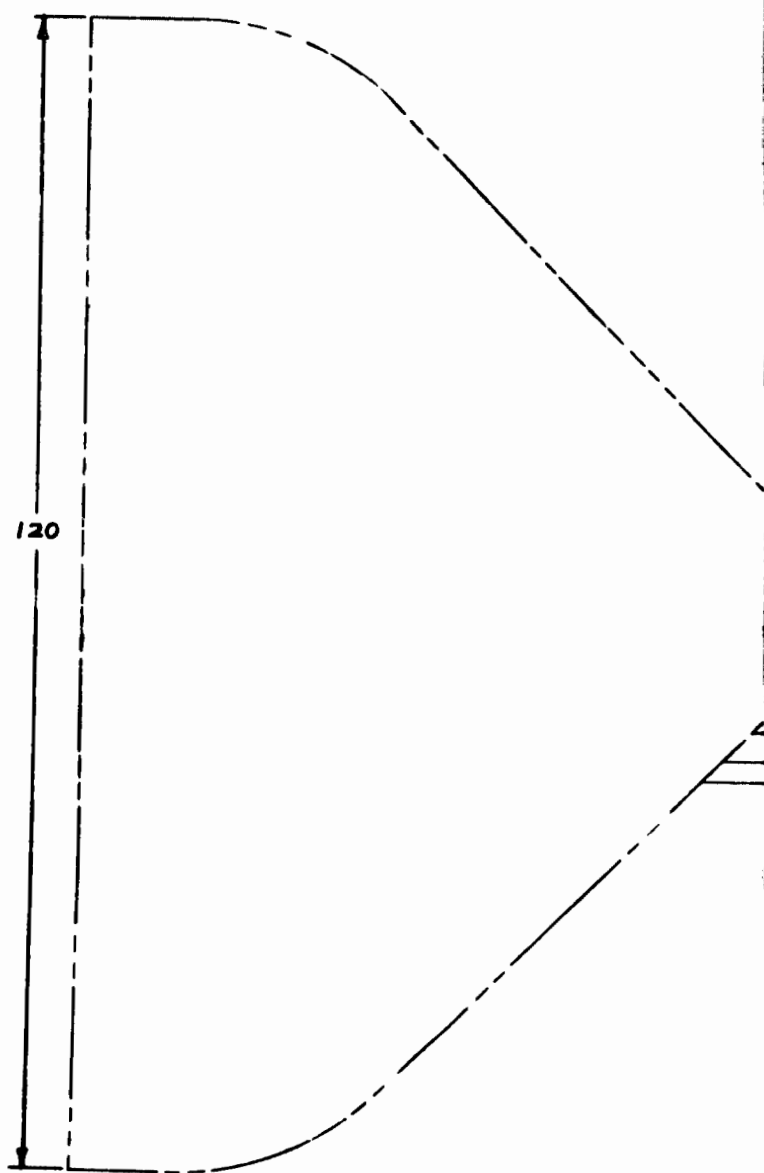
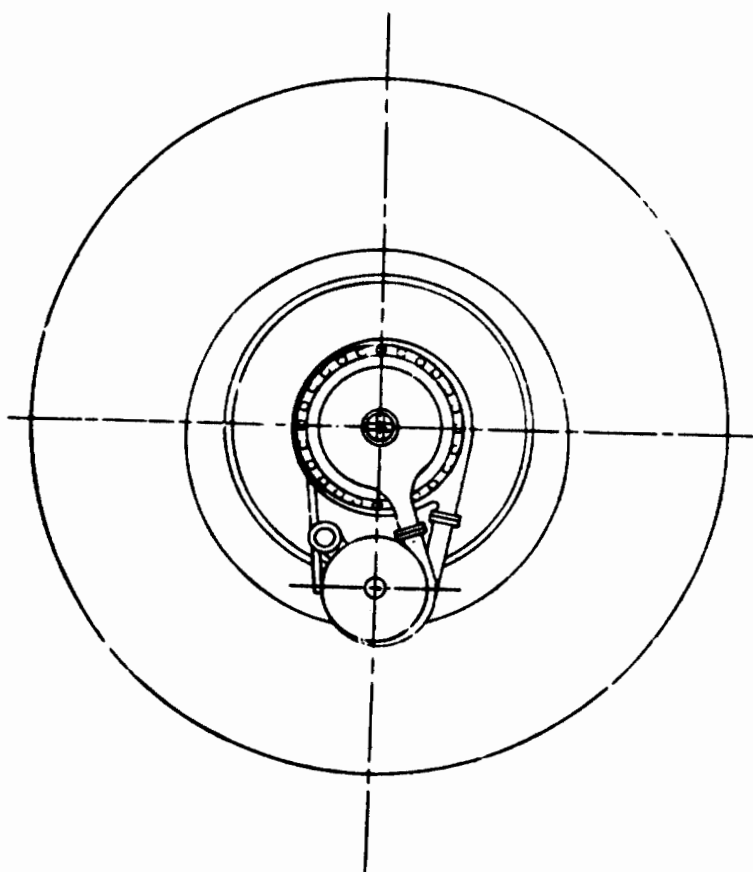
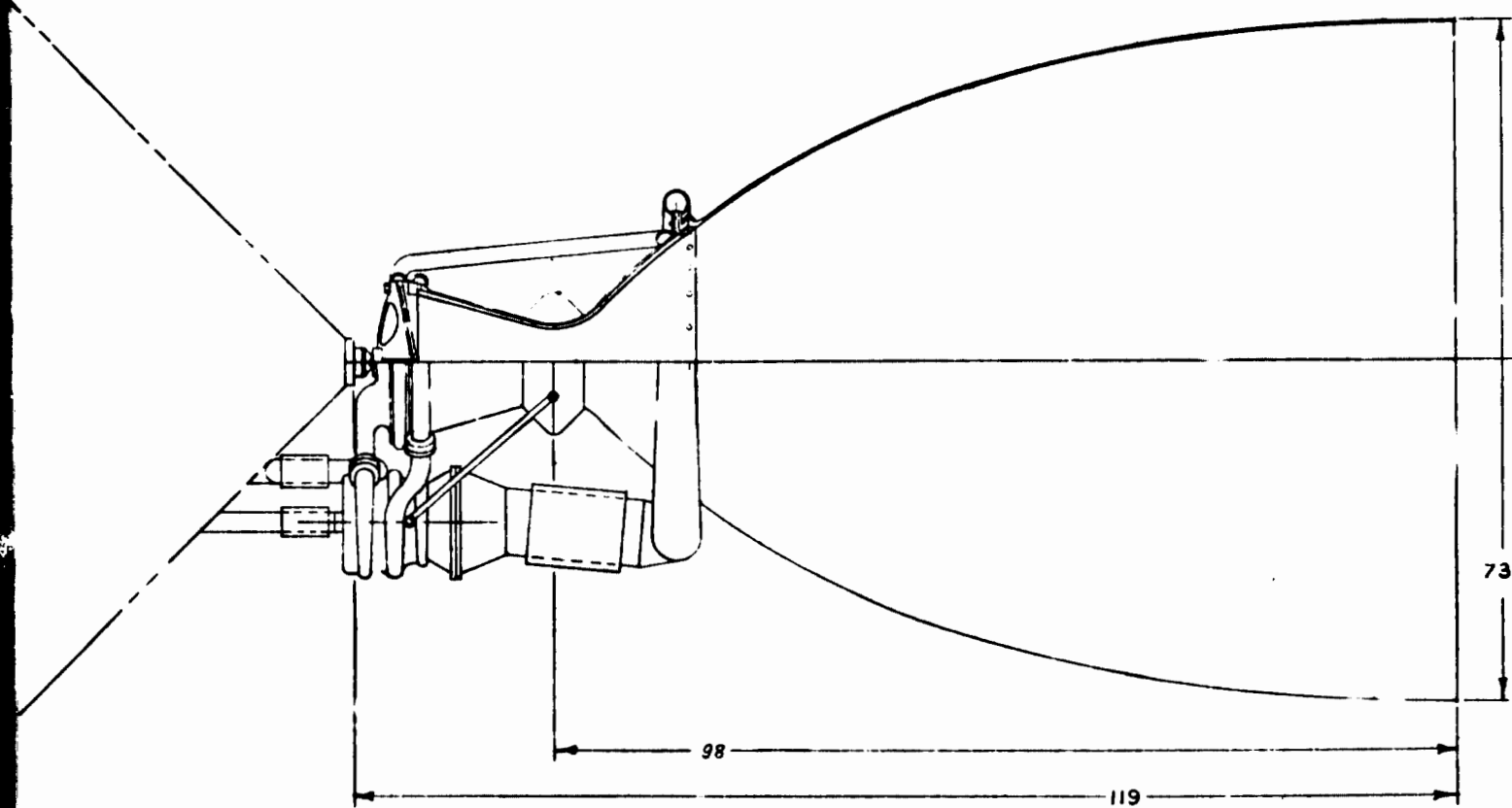


Fig. 157. Aerospike Engine System,
 Toroidal, Low Thrust,
 Low Chamber Pressure





2.

MAJOR SYSTEM PARAMETERS

$F = 40,000 \text{ LB}_f$ (VACUUM)

$P_c = 500 \text{ PSIA}$ (NOZZLE STAGNATION)

$\epsilon = 100$

PROPELLANTS = NTO/50-50

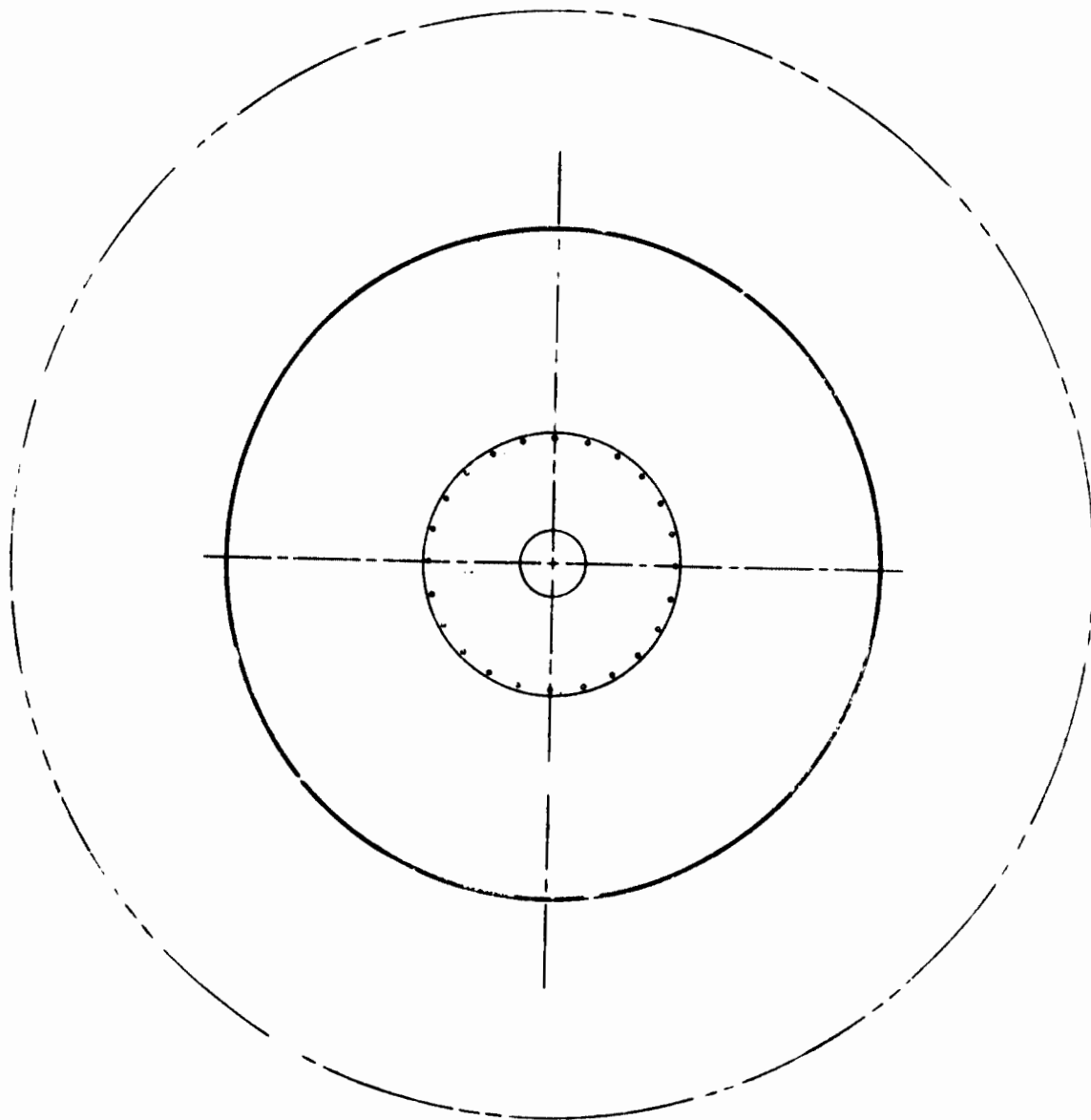


Fig. 158. Conventional Bell Engine System,
Low Thrust, Low Chamber Pressure

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area ratio C_M is essentially (with a weak dependence on module tilt angle, Ref. 3) a function only of the number of clustered chambers. The selection of 12 modules with circular touching exits fixes C_M at 51.8. The overall nozzle length L_N from the module throat to the plug exit (see Fig. 114) is 29.3 percent of an equivalent 15 degree conical nozzle. The length to the multichamber exits is 16.8 percent.

A simple point gimbal and conventional hydraulic actuator are employed. The oxidizer inlet duct passes through the center of the gimbal joint. Tubular columns transmit thrust loads to the gimbal block from a structural ring into which the module injector blocks are mounted. The ring also contains the tangential propellant distribution manifolds. Propellants are fed to the modules from a single shaft, back-to-back turbopump. Propellants are routed directly to the tangential distribution manifold. Turbine exhaust provides secondary flow for the plenum chamber type centerbody.

The engine was designed with a single downpass coolant through the modules to a module area ratio of 15. An ablative nozzle extension is used from this point to the module exit. The spike portion of the nozzle is fabricated of radiation cooled material.

The toroidal combustor configuration shown is regeneratively cooled and is supported in the chamber region by regeneratively cooled support tubes passing through the chamber walls. The nozzle length from the throat to the exit is 14 percent of an equivalent 15 degree conical nozzle.

System aspects of the toroidal design are essentially similar to those of the multichamber design. The same gimbal and central turbopump arrangement is used. Thrust mounts should be somewhat simpler and lighter as a uniform circumferential thrust force is applied as opposed to twelve discrete loads.

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The combustion chamber was sized to a minimum combustion length of six inches from injector face to throat. This produces a chamber characteristic length ($L^* = 186$ inches) greatly in excess of that used in conventional combustors ($L^* = 30$ to 50 inches). Recent experimental data using F_2/H_2 indicates the high combustion efficiencies can be achieved in toroidal combustors with diameters of only 3 inches. Therefore, it is likely that small diameter combustors could be used at this thrust level. The oval combustor contour is used to minimize induced bending moments on the support pins.

Oxidizer enters at the nozzle exit and cools the nozzle and inboard chamber section. Fuel is used to cool the support pin and outboard chamber region. Turbine drive gas is obtained by tapping into the primary combustion chamber through the injector face. Turbine exhaust gases are directed radially outward into the base region.

A conventional single bell engine system is shown for comparison in Fig. 158. The envelope length for the bell chamber is significantly longer than for the aerodynamic spike configurations. The axial length from the outer throat point to the nozzle exit (expressed as percent of a 15 degree cone) is 14 percent, 29.3 percent and 80 percent for the toroidal, multichamber and bell configurations, respectively. The percent axial length to the exit of the multichamber module is 16.8 percent. This factor is of significance because this length can be reduced only by decreasing the module area ratio. Module area ratio can be reduced by increasing the number of modules while maintaining a touching exit condition or by introducing gaps between chamber exits. Increasing the number of chambers increases system complexity and makes cooling more difficult whereas the introduction of gaps between chambers has been shown (Ref. 3) to lower performance.

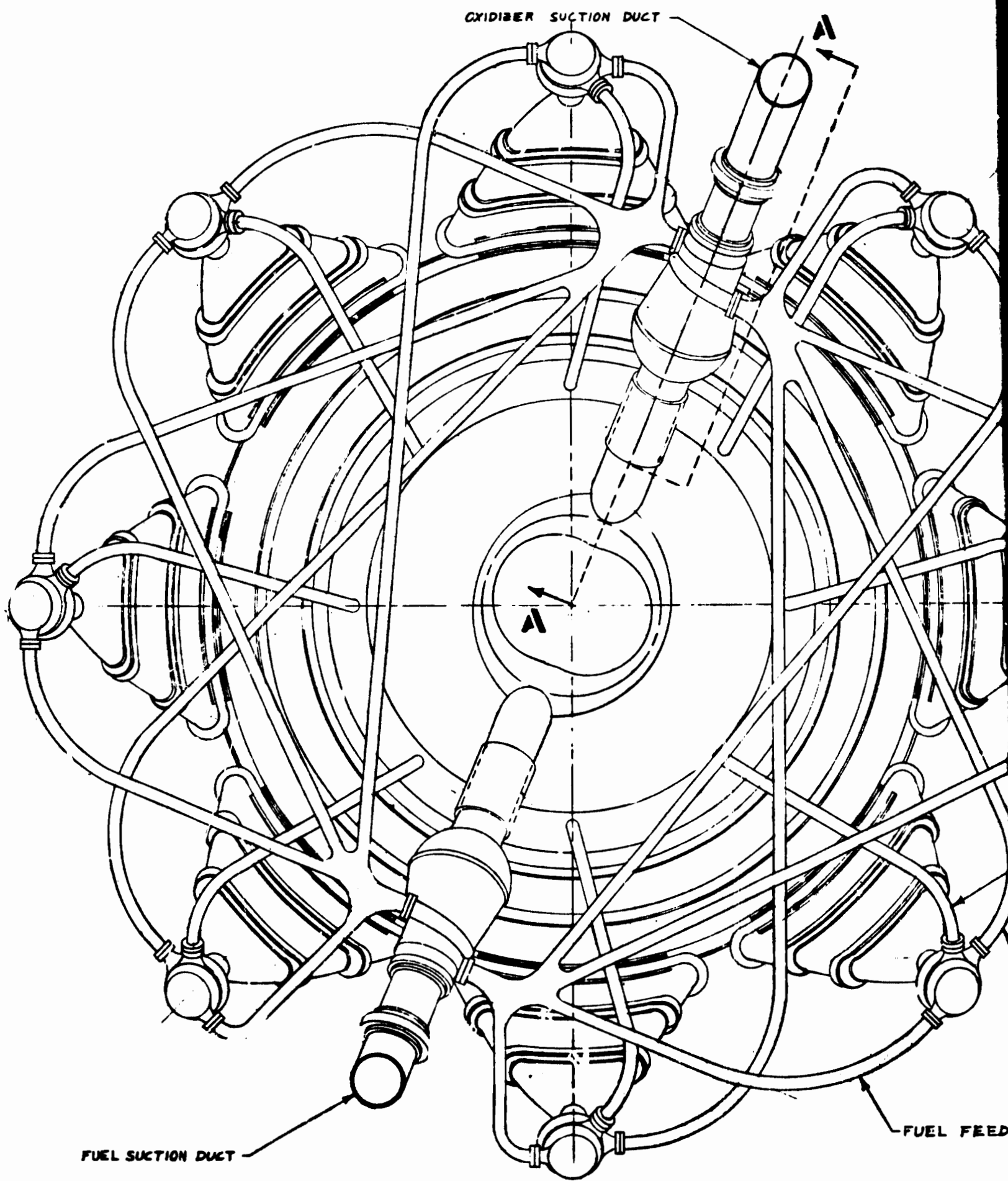
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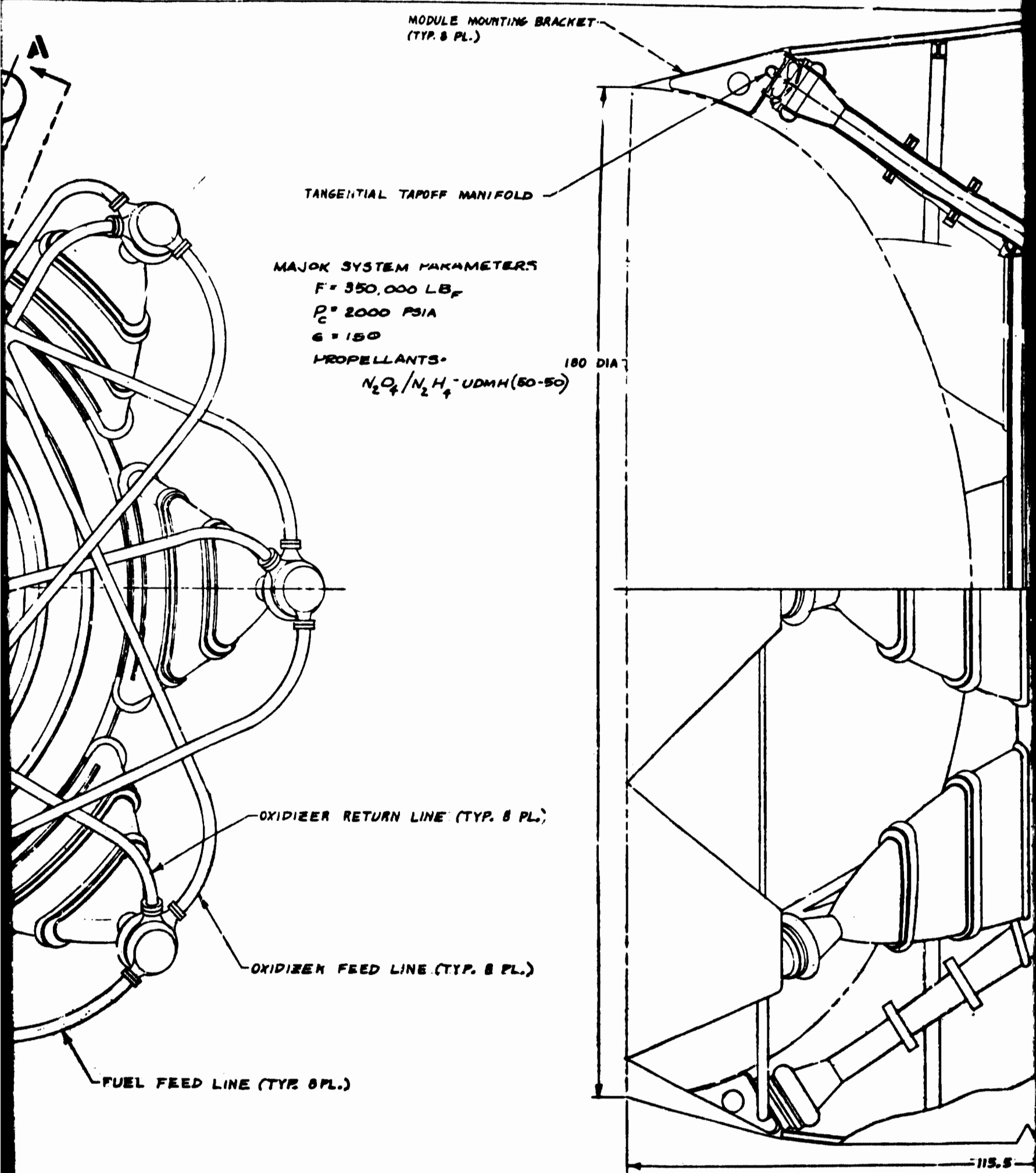
Point Designs - 350,000-pound Thrust Level

On Figures 159 through Figs 163 are shown layouts of multichamber and toroidal chamber aerodynamic spike engines and a single bell chamber engine. These engines produce approximately 350,000 pounds thrust at a chamber pressure of 2000 psia and an area ratio of 150.

350K Multichamber Aerospike. The splayed exit multichamber was investigated at this thrust level. The primary purpose of elongating the exit is to achieve an axisymmetric annular flow field at the module exit plane. The elongated exits also allow low module area ratio to be achieved with a small number of clustered chambers. The engine has eight regeneratively cooled chambers with each chamber exit extending over a 38 degree arc. The module area ratio is 13.8. The reduction in area ratio compared to circular exit clusters is easily seen by comparing this configuration to the 40,000-pound thrust design which has twelve chambers with a module area ratio of 51.8 and a cluster area of 100.

Module length is 57.8 percent of a 15 degree cone whose circular exit area encloses the 38 degree arc subtended by the splayed chamber and 210 percent of a 15 degree cone of 13.8 area ratio. Analytical studies of splayed module performance indicate that even though the module exit area can be reduced with splayed exits, for maximum module thrust the module nozzle length should be a high percentage (70 to 80) of the length of a 15 degree conical nozzle having an exit diameter equal to the exit span of the module. This can be shown from a vacuum performance analysis of a two-dimensional module. Figure 164 shows the maximum vacuum performance of two-dimensional nozzles of various lengths with a square throat of unit dimensions and constant exit dimensions of 7.3 and unity. This module design corresponds to an eight touching module multichamber configuration with a cluster area ratio of 50.





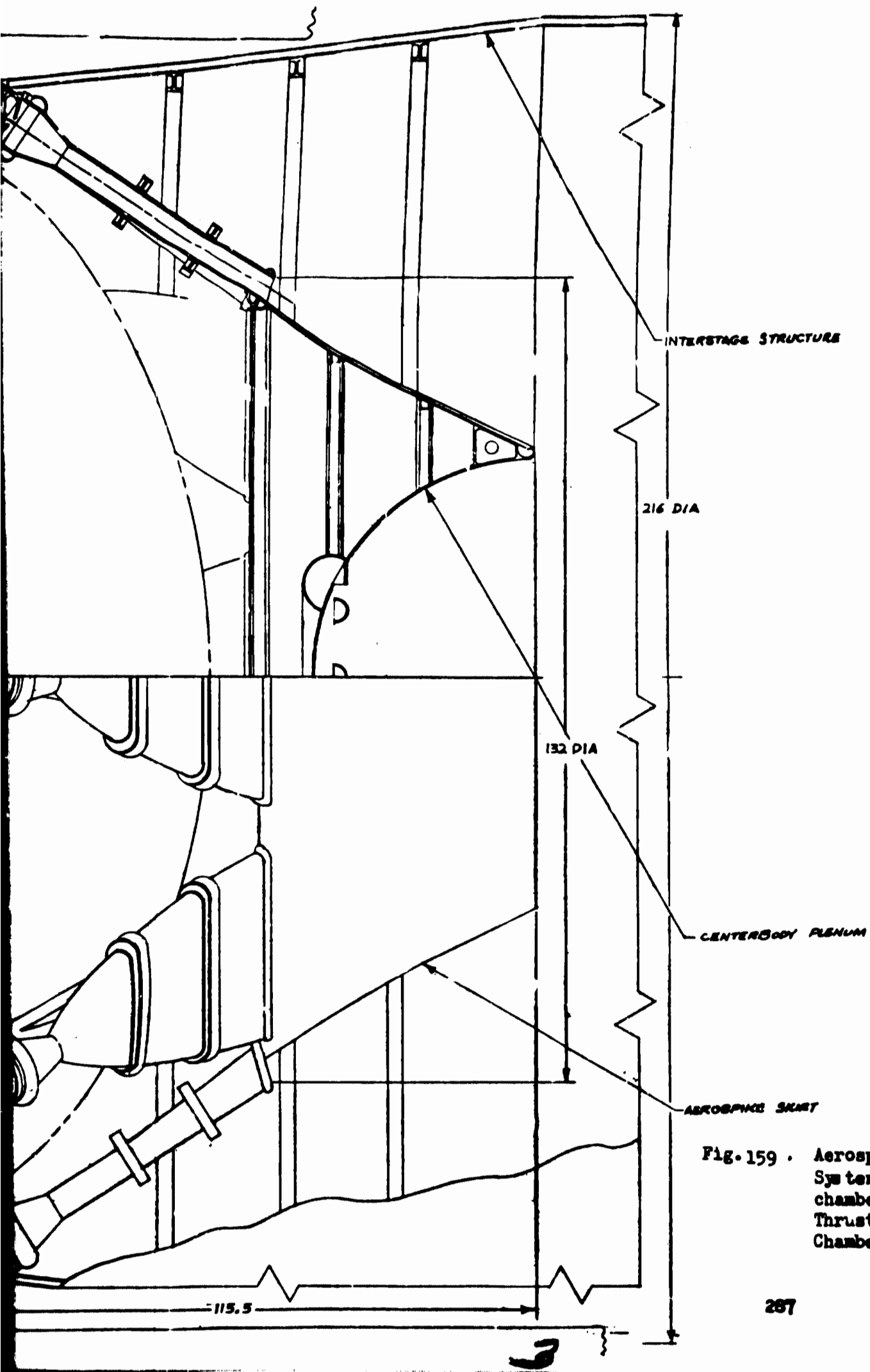
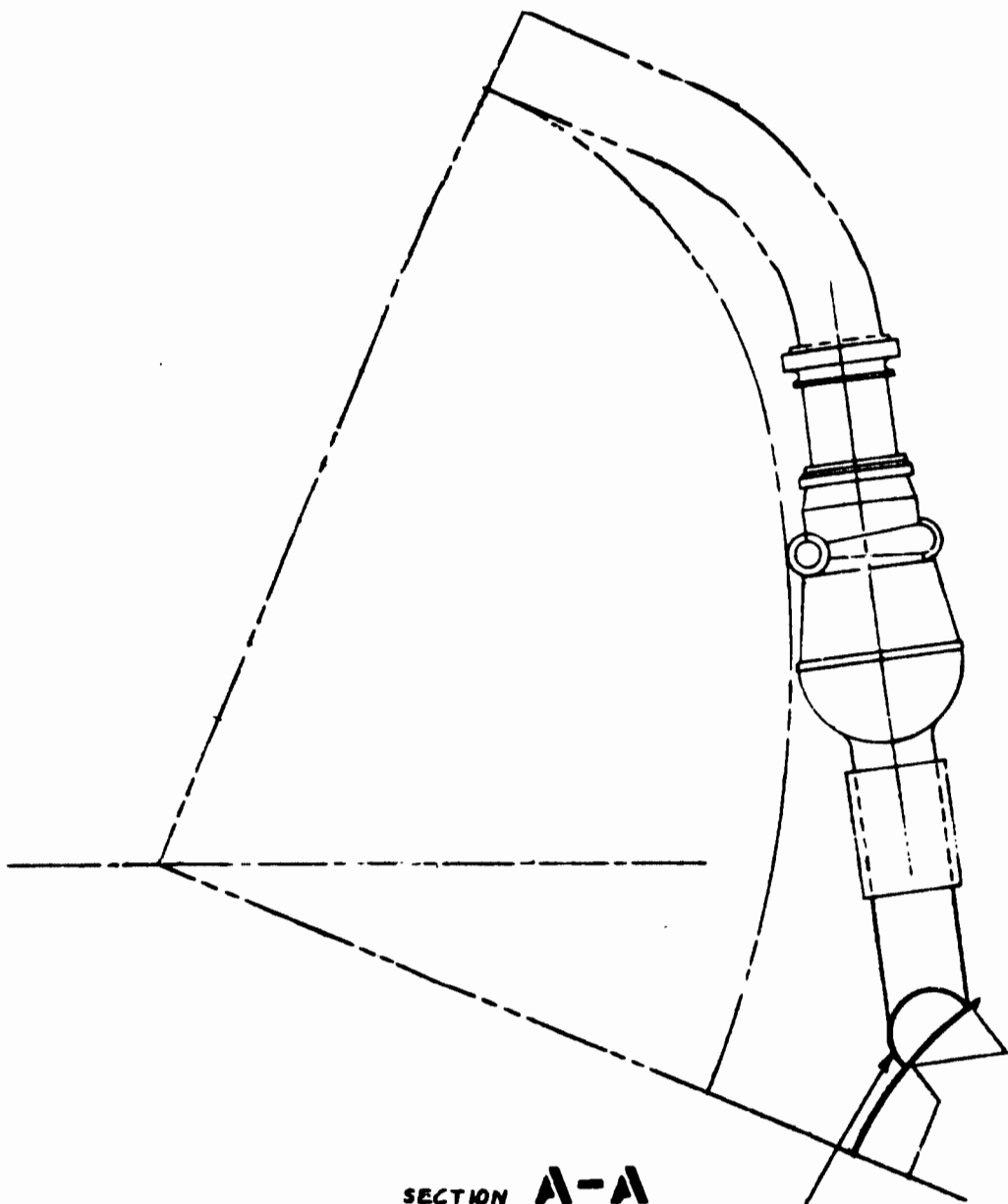


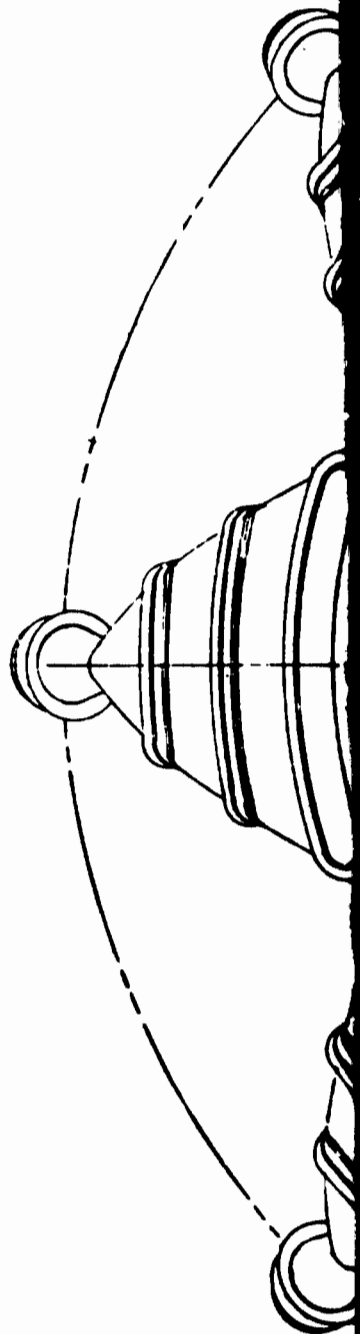
Fig. 159 . Aerospike Engine System, Multi-chamber, Medium Thrust, High Chamber Pressure

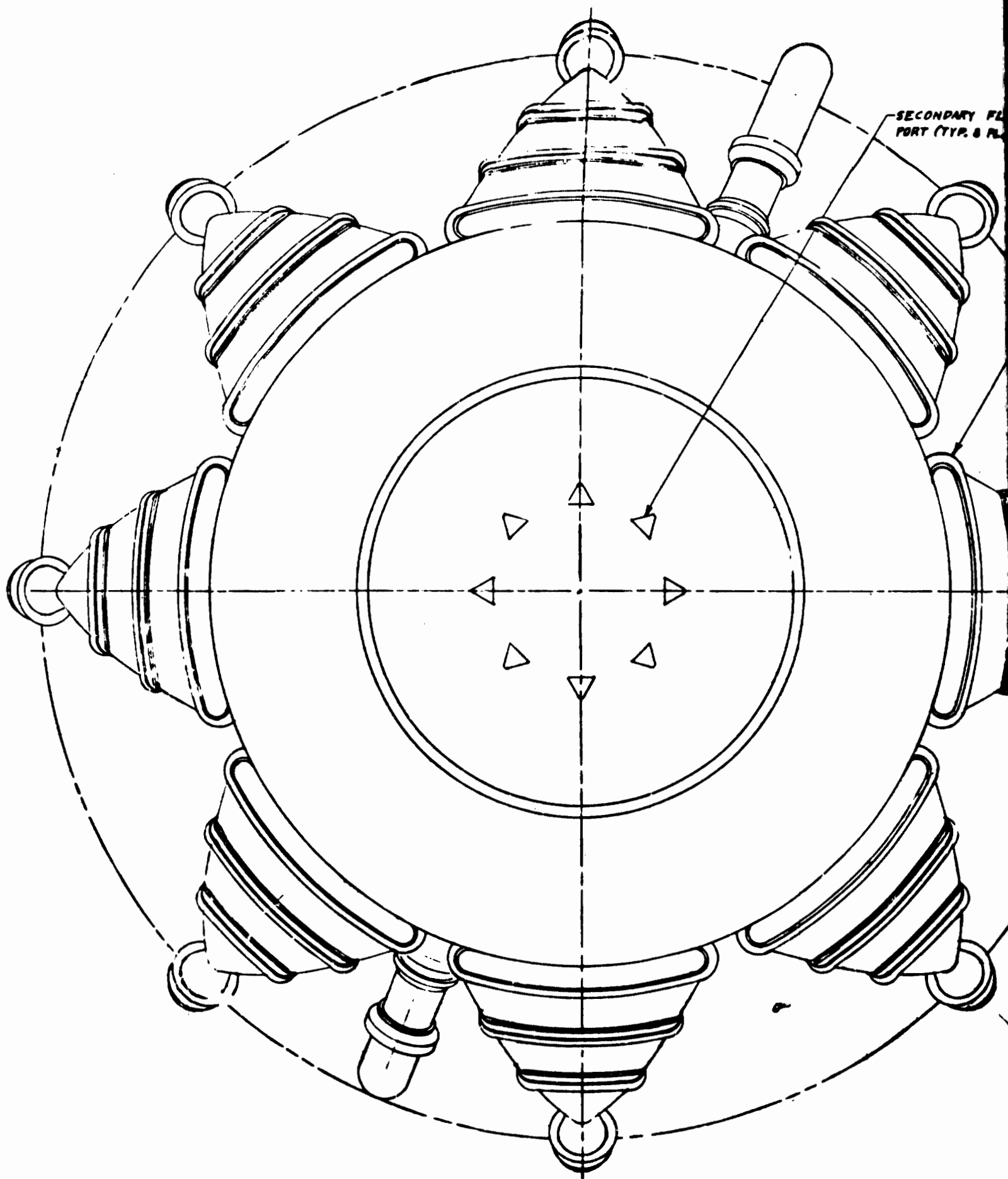


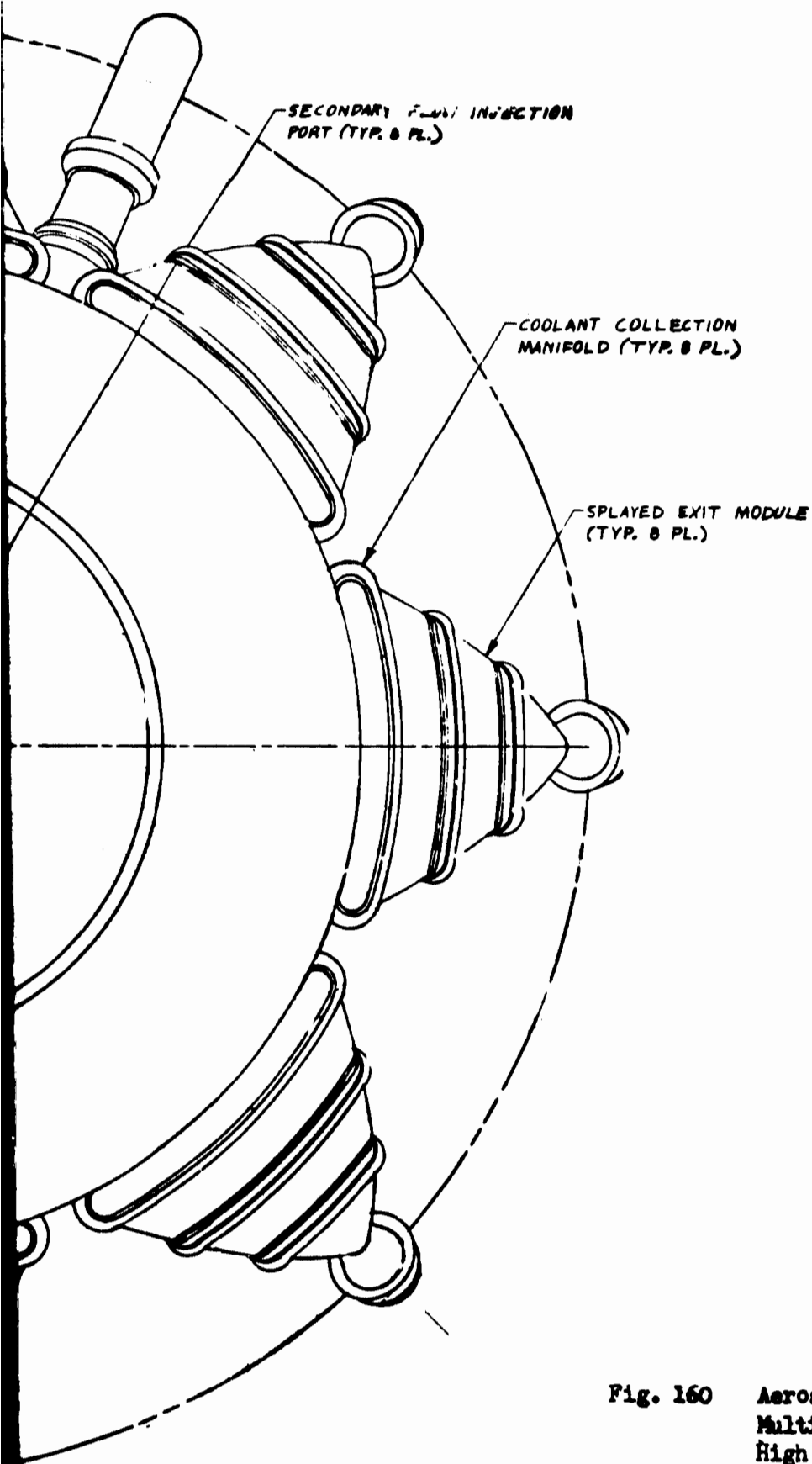
SECTION A-A

SECONDARY FLOW DISTRIBUTION
MANIFOLD

NOTE: PLUMBING OMITTED
FROM SIDE AND BOTTOM
VIEWS FOR CLARITY







MAJOR SYSTEM PARAMETERS

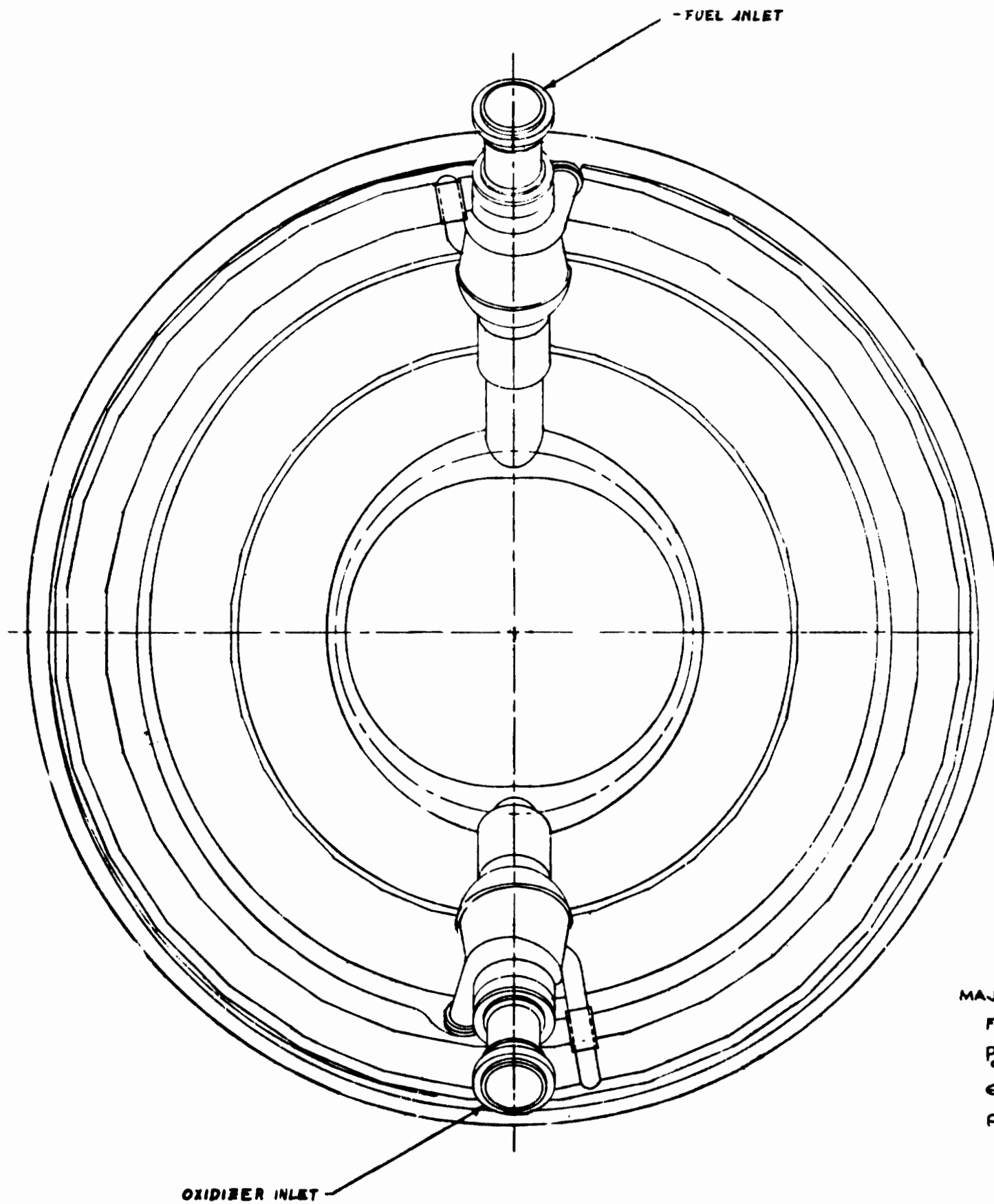
$F = 350,000 \text{ LB}_f$

$P_c = 2000 \text{ PSIA}$

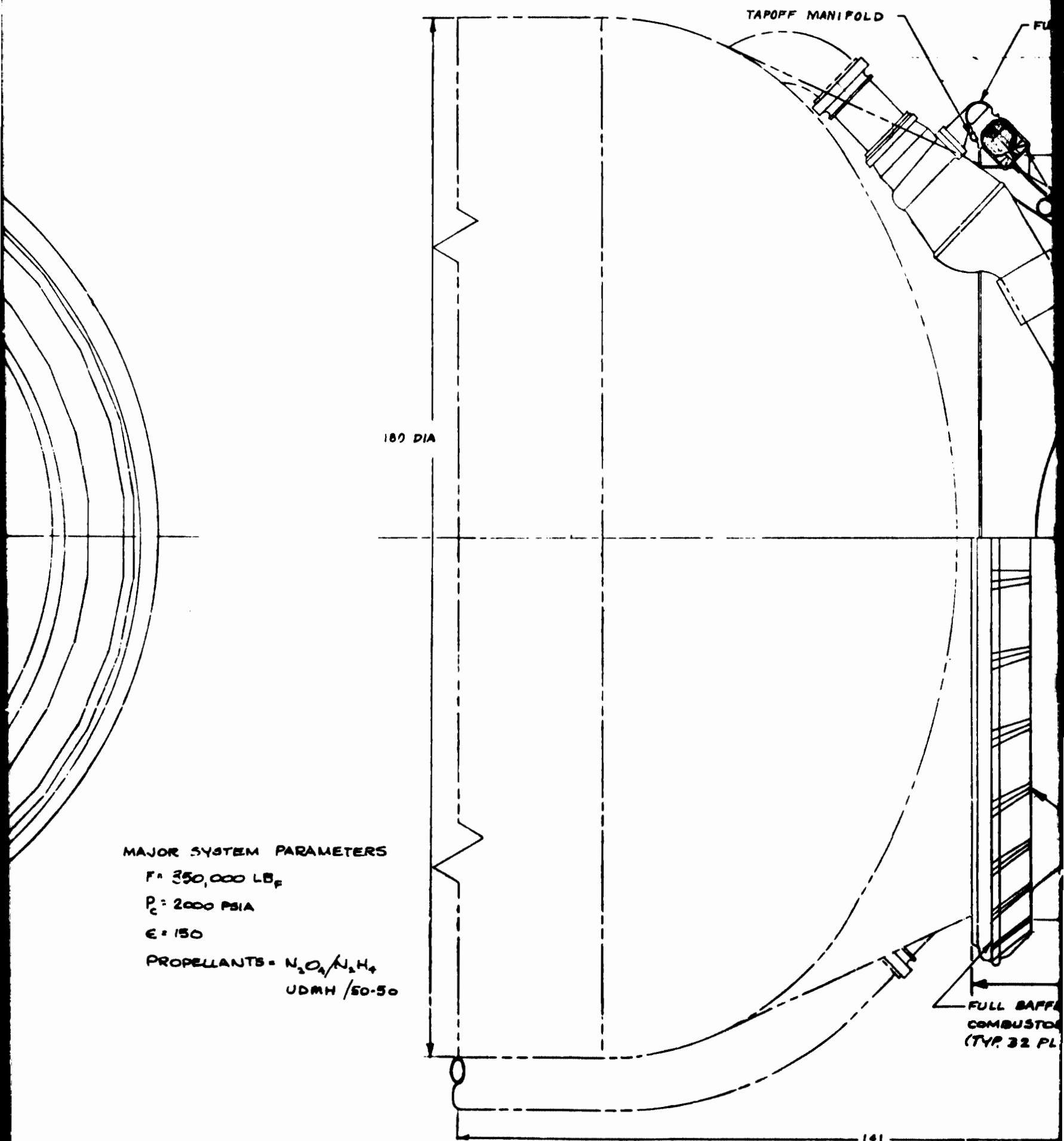
$\theta = 150$

PROPELLANTS = $\text{N}_2\text{O}_4/\text{N}_2\text{H}_4\text{-UDMH (50-50)}$

Fig. 160 Aerospike Engine System,
Multichamber, Medium Thrust,
High Chamber Pressure



MAJOR S
F = 350
P_c = 200
E = 150
PROPE



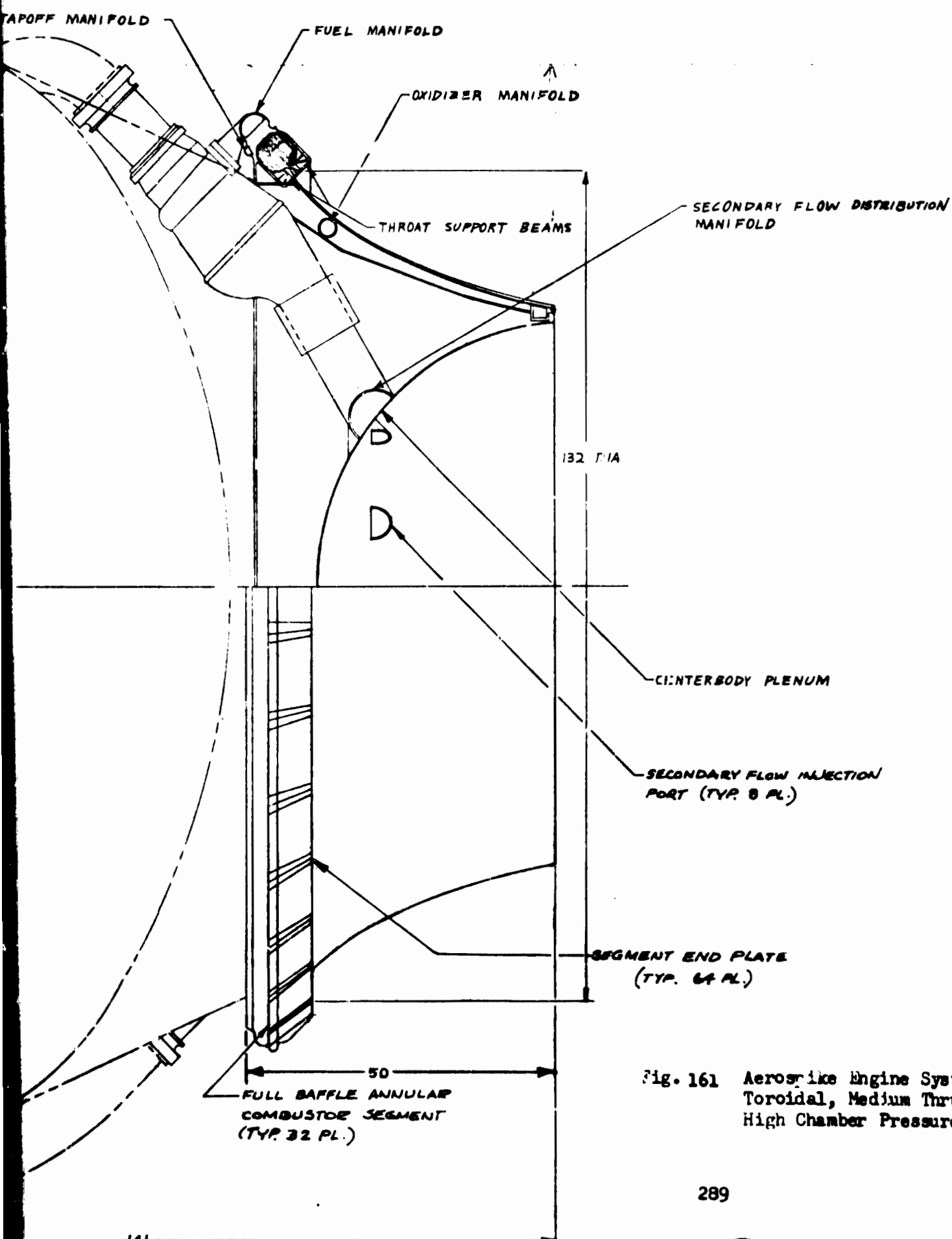
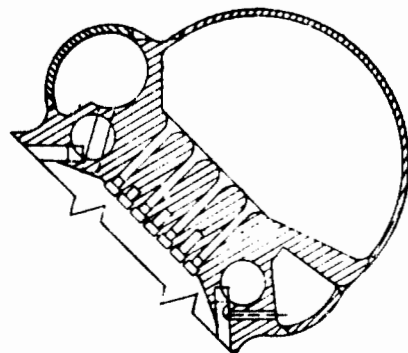
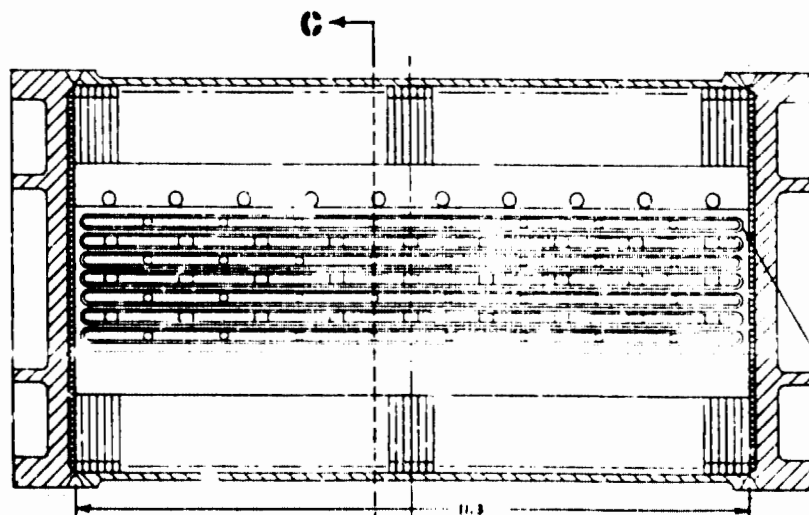


Fig. 161 Aerospike Engine System, Toroidal, Medium Thrust, High Chamber Pressure

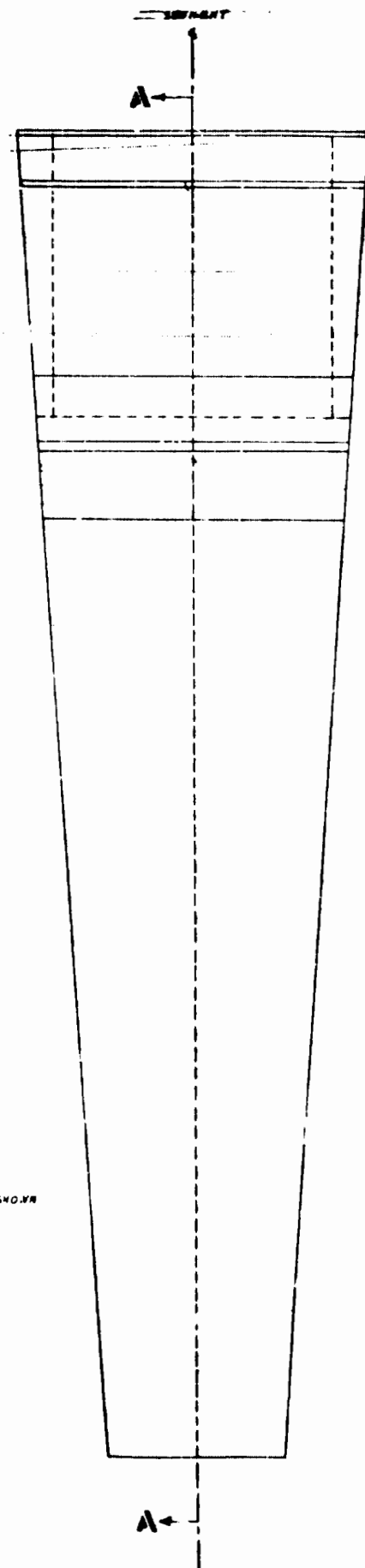


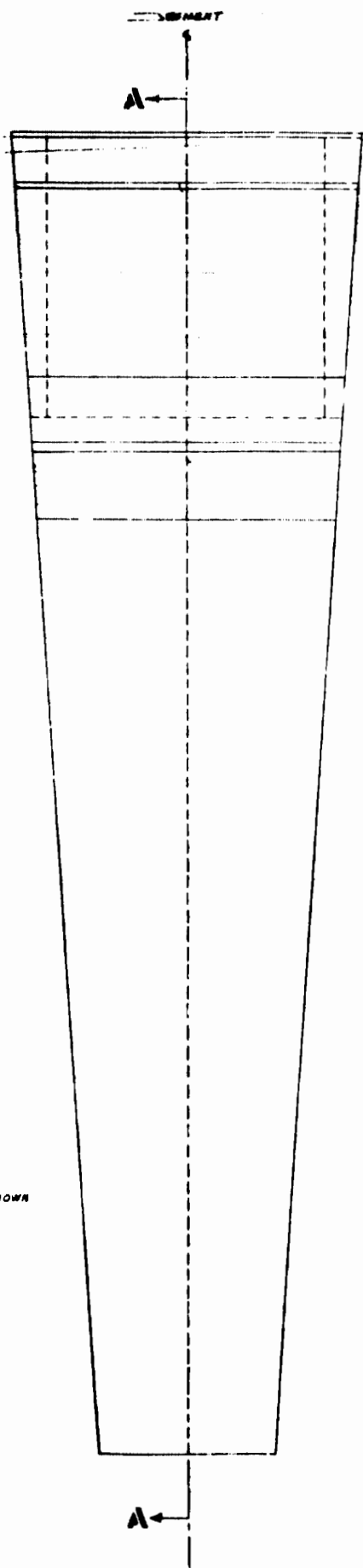
SECTION C-C
(FULL SCALE)



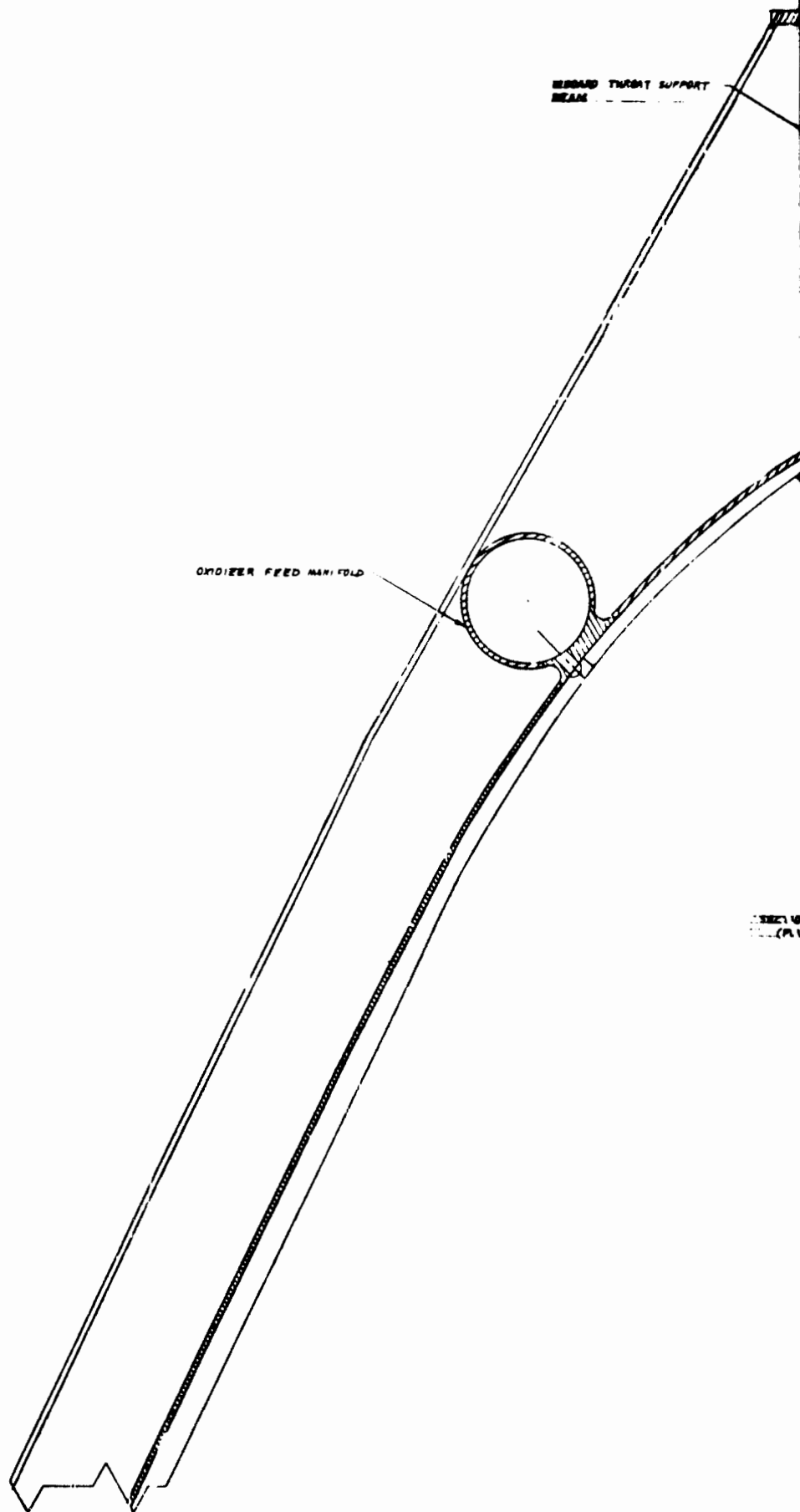
SECTION B-B
(FULL SCALE)

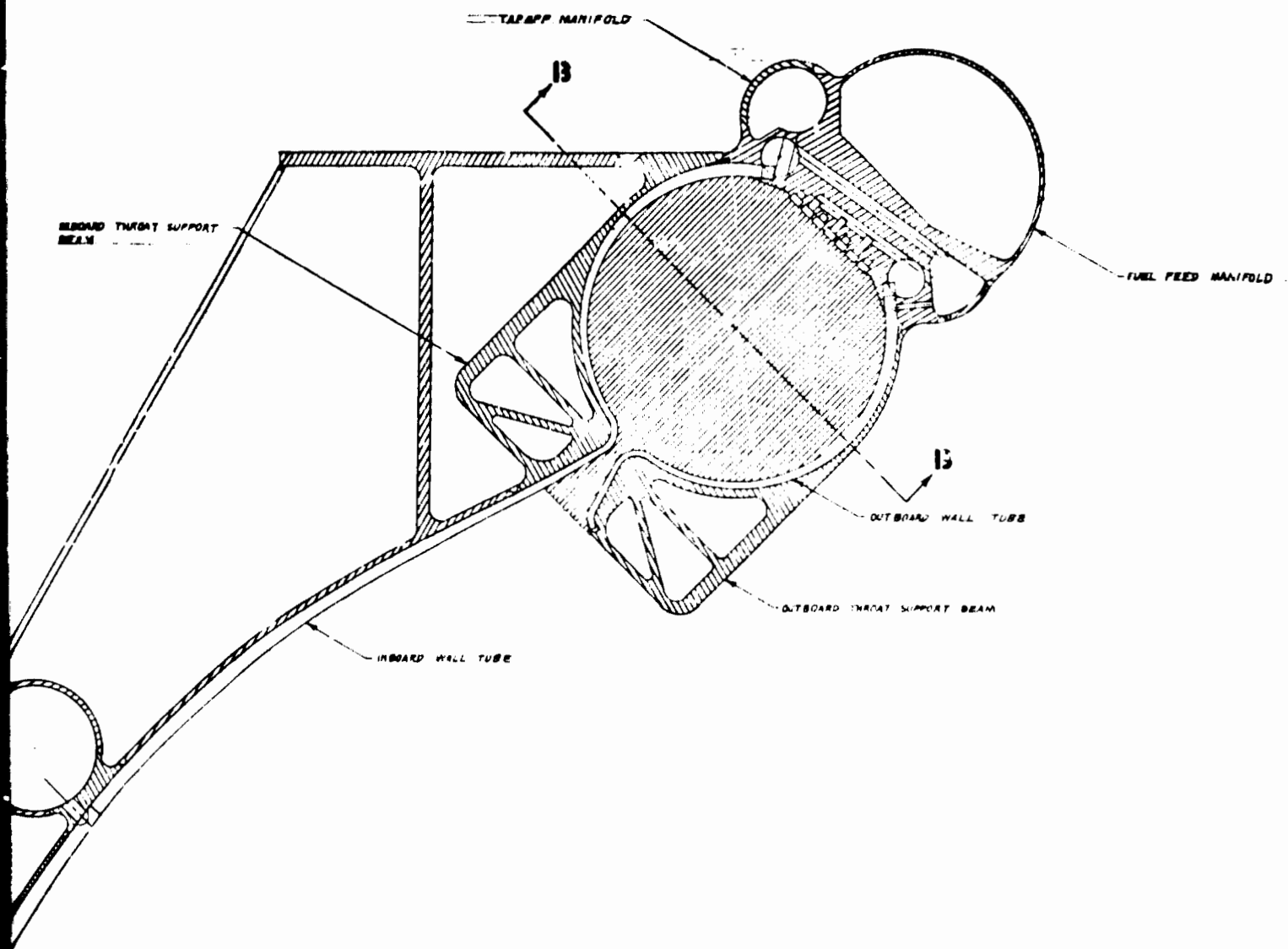
INJECTOR STRIPS NOT SHOWN





INJECTOR STRIPS NOT SHOWN





SECTION A-A
(FULL SCALE)

Fig. 162 Aerospike Combustor Segment,
Toroidal, Medium Thrust,
High Chamber Pressure.

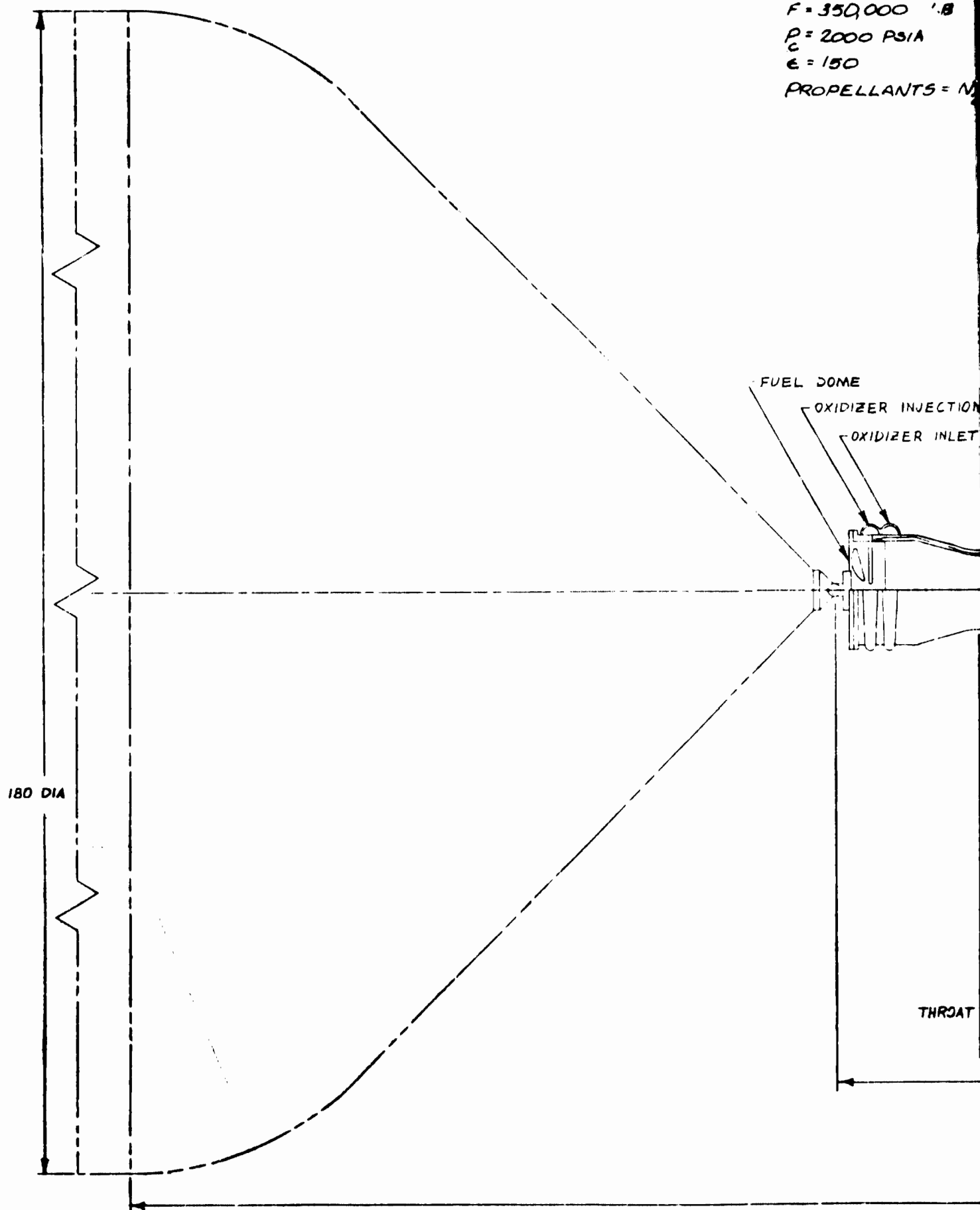
MAJOR SYSTEM PAR

$F = 350,000 \text{ LB}$

$P_c = 2000 \text{ PSIA}$

$\epsilon = 150$

PROPELLANTS = N



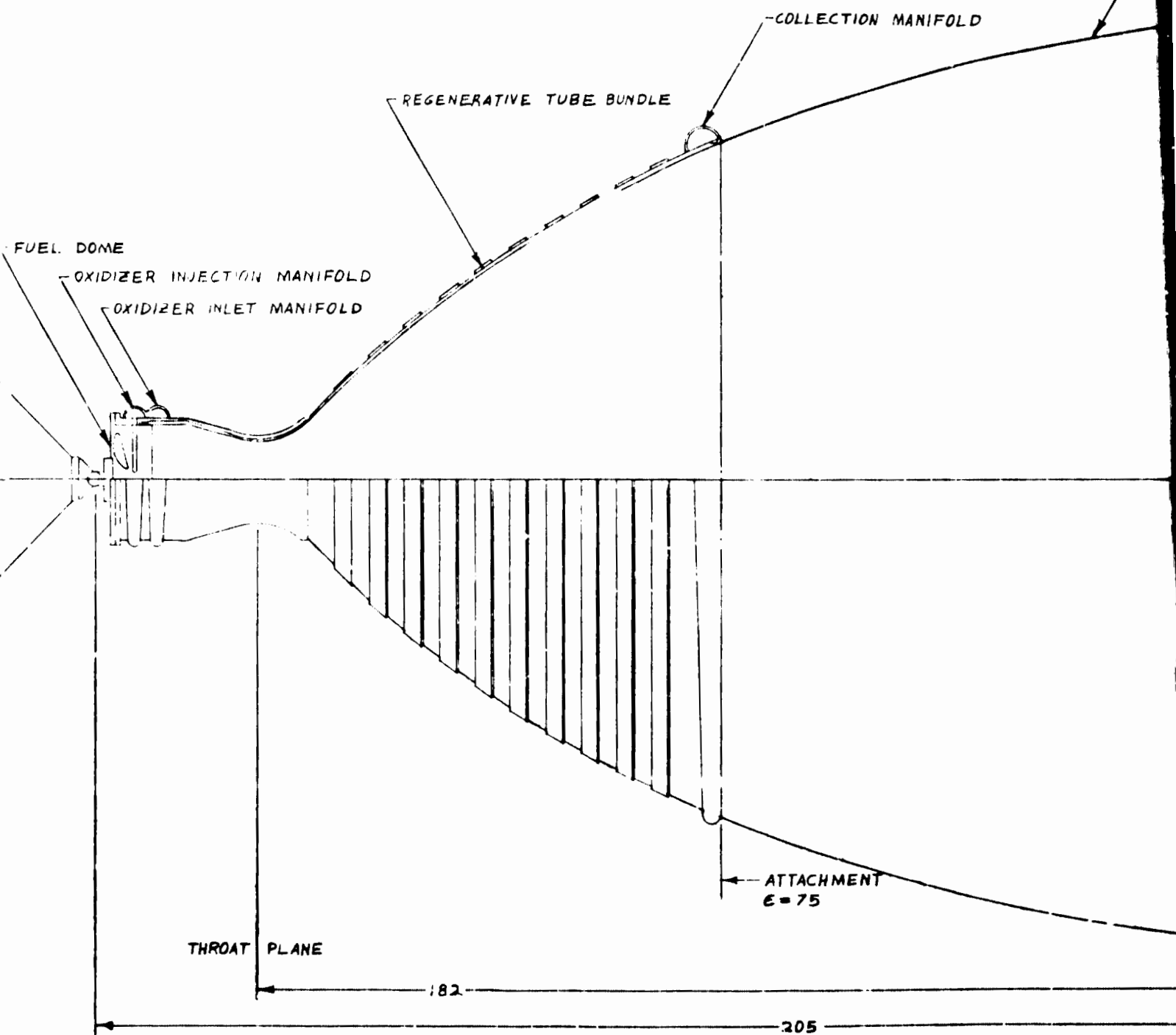
MAJOR SYSTEM PARAMETERS

$F = 350,000 \text{ LB}$

$P_c = 2000 \text{ PSIA}$

$\epsilon = 150$

PROPELLANTS = N_2O_4 / N_2H_4 - UDMH (50-50)



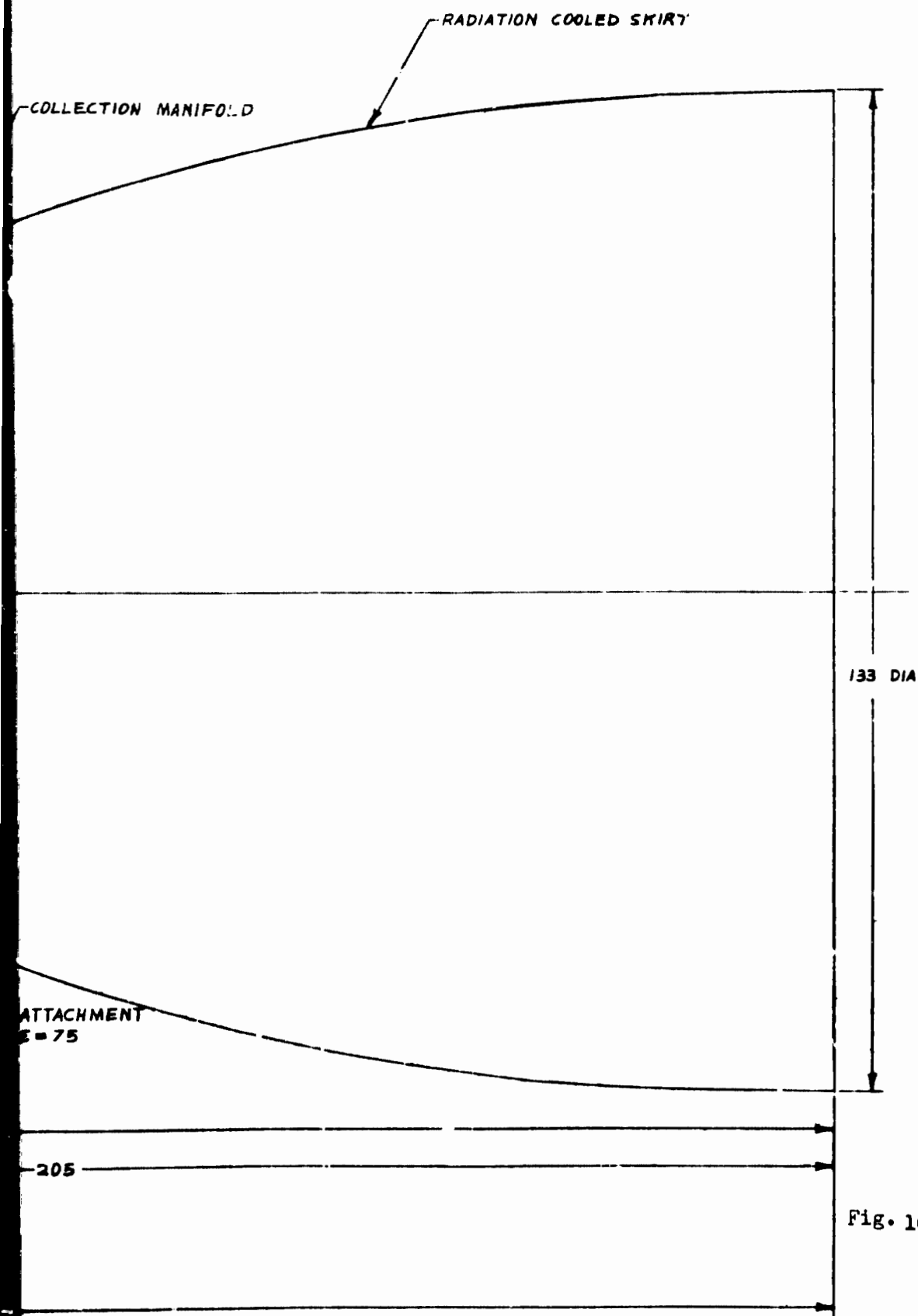


Fig. 163 Conventional Thrust Chamber, Bell, Medium Thrust, High Chamber Pressure

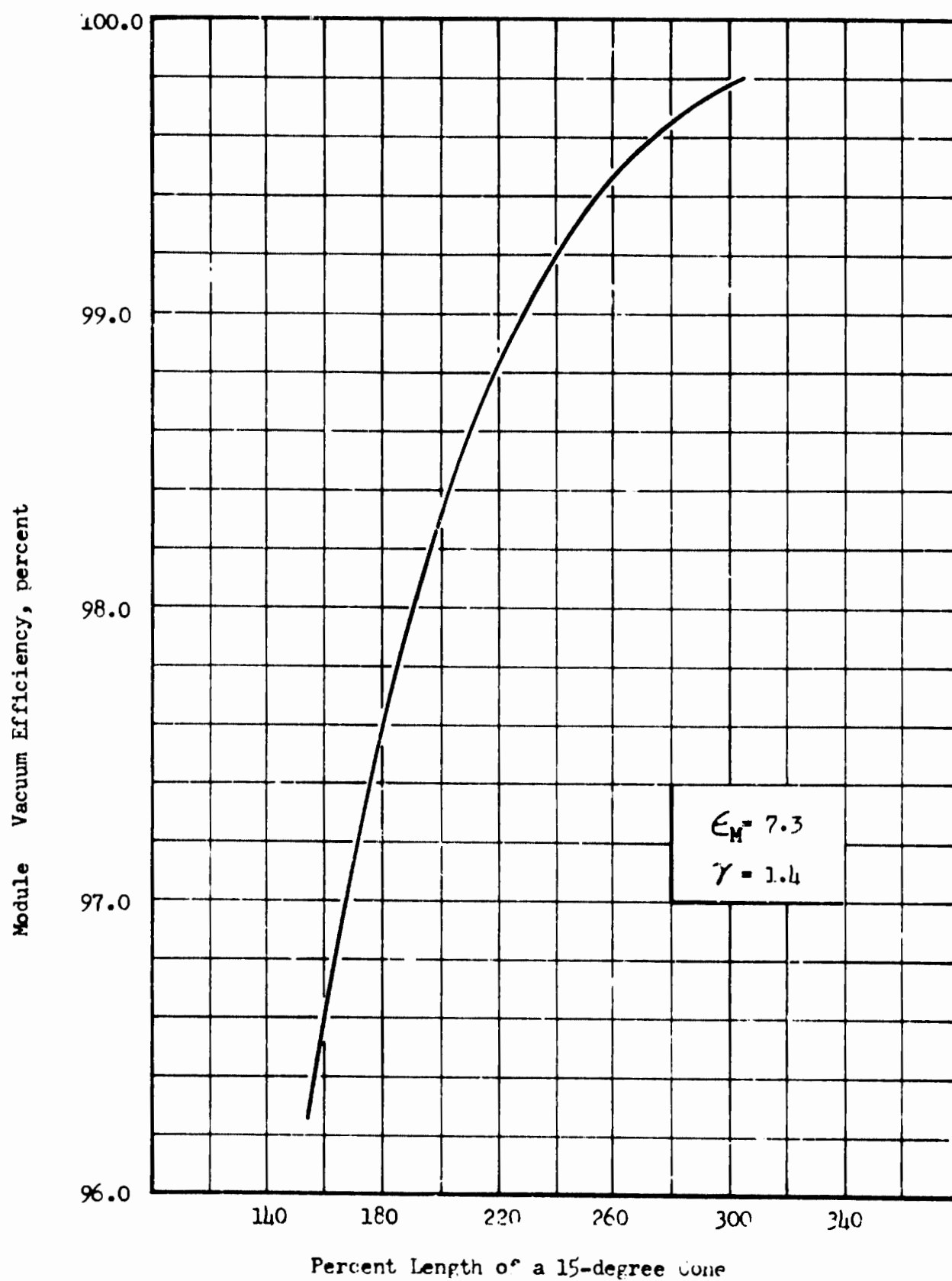


Fig. 164 Maximum Performance vs Percent Length for a Two-Dimensional Nozzle

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A set of two turbopumps, one fuel and one oxidizer, feed propellants through individual lines to each thrust chamber. It can be seen that the use of a pair of pumps (mounted off the engine centerline) with eight chambers requires eight different high pressure ducts for each pump. The shorter ducts would require orificing to match propellant distribution between the ducts.

Simpler options that could be employed if interchangeability constraints are neglected include one set of pumps for every module or feeding each two modules from a pump placed between them. Provision of one pump set per module (single or dual shaft) would facilitate pump fed development testing on a module level and allow direct operation with 2, 4, or 6 modules out. Feeding each two modules from a single shaft, back-to-back pump placed between them would allow operation with 4 modules out in the event of pump failure. Feeding each two adjacent modules from alternate fuel and oxidizer pumps placed between them would not allow module out operation in the event of pump failure.

Feeding all chambers from a central single shaft turbopump would require placing the ambient temperature portion of the machine inside the fuel tank, or dimpling the tank bottom to accommodate it. If these options are unacceptable, a decrease in centerbody plenum depth or an increase in interstage structure length and weight would be necessary.

A major disadvantage of the splayed nozzle multichamber combustor compared to a similar circular exit combustor lies in the difficulty of fabricating regenerative tube bundles in the splayed shape. It is

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expected that the fabrication of ablative or radiation cooled nozzles in this shape would present no problems as serious as those anticipated in a regenerative bundle. If the splayed bundle exit is curved around a radius as in the drawing, at most only pairs of tubes in any assembly would be interchangeable, and in some cases even these pairs would be right and left hand versions of the same contour, requiring a different forming die for each tube in the bundle. If the exit is made straight, so that the cluster exit is polygonal, at most groups of four tubes per bundle could be interchangeable.

An alternate nozzle fabrication method was reviewed which offered promise of forming the splayed nozzle shape by an assembly of straight tapered tubes identical in cross-sectional contour but cut off at varying lengths at the module exit. Figure 155 illustrates the method.

Instead of forming the convergent-divergent contour of the chamber from continuous tubes which become non-interchangeable aft of the module throat, the axisymmetric combustion chamber is first formed of one shape of identical tubes which are brazed into holes in a transition ring at the module throat. These holes lead immediately into nozzle tubes that are brazed into the other end of the short ring. The nozzle tubes in the plane of nozzle divergence enter the ring at the angle of divergence. Tubes in the non-divergent nozzle plane enter the ring parallel to the nozzle axis. Intermediate tubes enter at intermediate angles. Thus, the bending of tubes to various angles is replaced by the drilling of holes at varying angles. Film cooling of the transition ring may be necessary.

Modules are cooled with N_2O_4 in a single downpass flow pattern in order to minimize coolant bulk temperature at the chamber throat. From the collection manifold, coolant must flow aft to cool the aerospike skirt.

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Several alternative flow transition methods exist. From the standpoint of structural strength and leak tight coolant sealing a promising procedure would be to make the inside module nozzle tubes and the skirt tubes immediately aft of them as one continuous tube (which might include one or more brazed tube splices). Coolant flow from the outside module tubes could be either manifolded and ducted back to the module injector or flow between modules as shown and enter the inner continuous tubes through slots cut in the sides not exposed to hot gas. This option has the disadvantage that coolant velocity and pressure drop in the skirt must be increased to offset the lowered N_2O_4 flowrate. If the exterior chamber tube flow is utilized for skirt cooling, extra skirt tubes must be included to fill the gap aft of where it passes between chambers. A disadvantage of either sort of continuous module-skirt tube construction was the aspect of including modules and skirt in one brazed assembly. Apart from severe tolerance requirements, a replacement of a defective module would be difficult. A construction method permitting module substitution on a "plug in" basis is preferable. The module-skirt transition configuration shown in Fig 159 employs a segment transition manifold to permit removal of the module from a bolted flange on the skirt.

Exhaust pressure inside the splayed module nozzles exerts forces tending to distort the contour into an axisymmetric, circular exit bell contour. Nozzle banding or other external structure must be fastened around the brazed tube bundle to resist these loads. A detailed weight comparison between a circular exit module and a comparable module with a 2:1 elliptical exit shape was made in Ref. 18. Even with this relatively moderate ellipse ratio the elliptical exit shaped nozzle was heavier than the circular exit nozzle by a factor of two. This relative weight ratio becomes greater as the nozzle approaches a two-dimensional shape.

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Chamber thrust loads are transmitted into the vehicle shell through brackets which diffuse the point loads into a continuous line load. The chamber injectors are bolted directly to these brackets. Tapoff gases tapped from a port on the axis of each injector pass through a sleeve and into a tangential collection manifold threading through small cut-outs in the bracket webs. Turbopump mounts are fastened to two adjacent thrust brackets. Turbine exhaust gas is manifolded and distributed through eight ports in the centerbody plenum.

350K Toroidal Aerospike. A full combustion zone baffle combustor was chosen to represent the toroidal family of combustion at this design parameter level. A layout of the engine is shown in Fig. 161 .

In the full baffle annular toroidal chamber, a rectangular throat slot releases primary gas from a cylindrical combustion volume. Chamber pressure is contained in a structural box formed by an injector bar opposite the throat slot, two chamber half shells, an end plate across each end of the cylinder, and two beams, inboard and outboard of the throat slot which stretch between end plates. The chamber half shells are exposed to the usual hoop and axial tension stresses present in a pressurized cylinder, while bending moments incurred in slitting the cylinder down one side are absorbed in the throat support beams.

The engine pictured is composed of 32 such segments, arranged in a 32 sided polygon. Selection of segment number (N) was constrained primarily by weight tradeoff which determined an optimum end plate separation to be 11.3 inches. With the selection of an end plate separation, and a value of area ratio, the number of segments in the engine was limited to a small range of integers dependent on end plate thickness.

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An aerospike skirt length of 19% the length of a 15° half angle cone to an area ratio of 150 is shown in the engine layout. An outboard shroud to an area ratio of 3.5 was used. A hemispheric plenum center-body was used, with a toroidal manifold to tangentially distribute turbine exhaust from the torbopump outlets.

The combustor segment injector (Fig. 162) provides the following flow scheme; single up pass inboard wall tube, injector face tapoff, and double pass outboard wall tubes. Tapoff gas is tapped from the chamber at the side of the face near the outside fuel injector strip. An insulated sleeve ducts the gas through the end cap feed passage and into the tapoff manifold. Fuel is fed from a manifold on the back of the block through down holes directly into milled grooves in the injector face. The grooves feed face strips which inject the fluid in the selected pattern. Oxidizer is introduced from a tapered toroidal manifold located near the top of the skirt. The coolant is double passed downwards to cool the lower skirt and then flows upwards to the combustion chamber in a single pass. The single pass wall tubes start flattened at the feed manifold, become circular in cross section at the throat, and return to an oval cross section toward the injector to reduce coolant velocity. The wall tube bundle is brazed into a continuous groove in the injector block. The N_2O_4 flows into a deeper groove with holes drilled in the groove bed. These holes cross to a deep drilled hole traversing the injector block lengthwise. The coolant flow splits into two parts, one flowing along the deep drilled hole to cool the end plates, the other passing through cross holes to a third welded manifold which feeds the downpass tubes of the outboard wall bundle. The up pass tubes of this bundle feed a second deep drilled hole containing the return flow from the end plates. Small cross holes then feed oxidizer to the injection strip grooves.

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The engine was assumed fixed, with thrust vector control provided by side liquid injection of N_2O_4 .

Comparison to 350K Bell Engine. The overall engine length of the 80% bell engine shown in Fig. 163 is 205 inches. On this same basis of length from the exit plane to the forwardmost point on the engine, the multichamber and toroidal engines are 45% and 40% respectively of the bell chamber length. The overall diameters of these engines were 147 percent and 125 percent the diameter of the conventional engine.

A comparison on the basis of physical overall length has questionable validity at this design point, as the degree of engine/vehicle integration varies among the designs. If a comparison is made on the basis of length attributable to the engine over and above that of its associated tank bottom (45 degree cone for bell engine, 0.7 ellipse for aerospikes), the multichamber and toroidal engine lengths are both 26% of the bell length. The provision of a conical tank bottom for the bell engine would further increase the length and weight of interstage structure in this upper stage application.

Medium Thrust Low Chamber Pressure Engine Design

Multichamber, toroidal aerodynamic spike engines and a single bell engine which are suitable as the propulsion system for a medium thrust low chamber pressure application are presented in Figs. 165 through 169. The engines generate 658,000 pounds of thrust at a chamber pressure of 300 psia. Propellants are supplied to the thrust chambers by tank pressure. Area ratio was limited by the 17 foot tank diameter

13

OXIDIZER DOME
FUEL
INJECTION
MANIFOLD

AERODYNAMIC
BOAT TAIL
SHROUD

ABLATIVE
COOLED
MODULE
(12 REQ'D)

TAPOFF (SECONDARY FLOW)
DUCT (12 REQ'D)

113

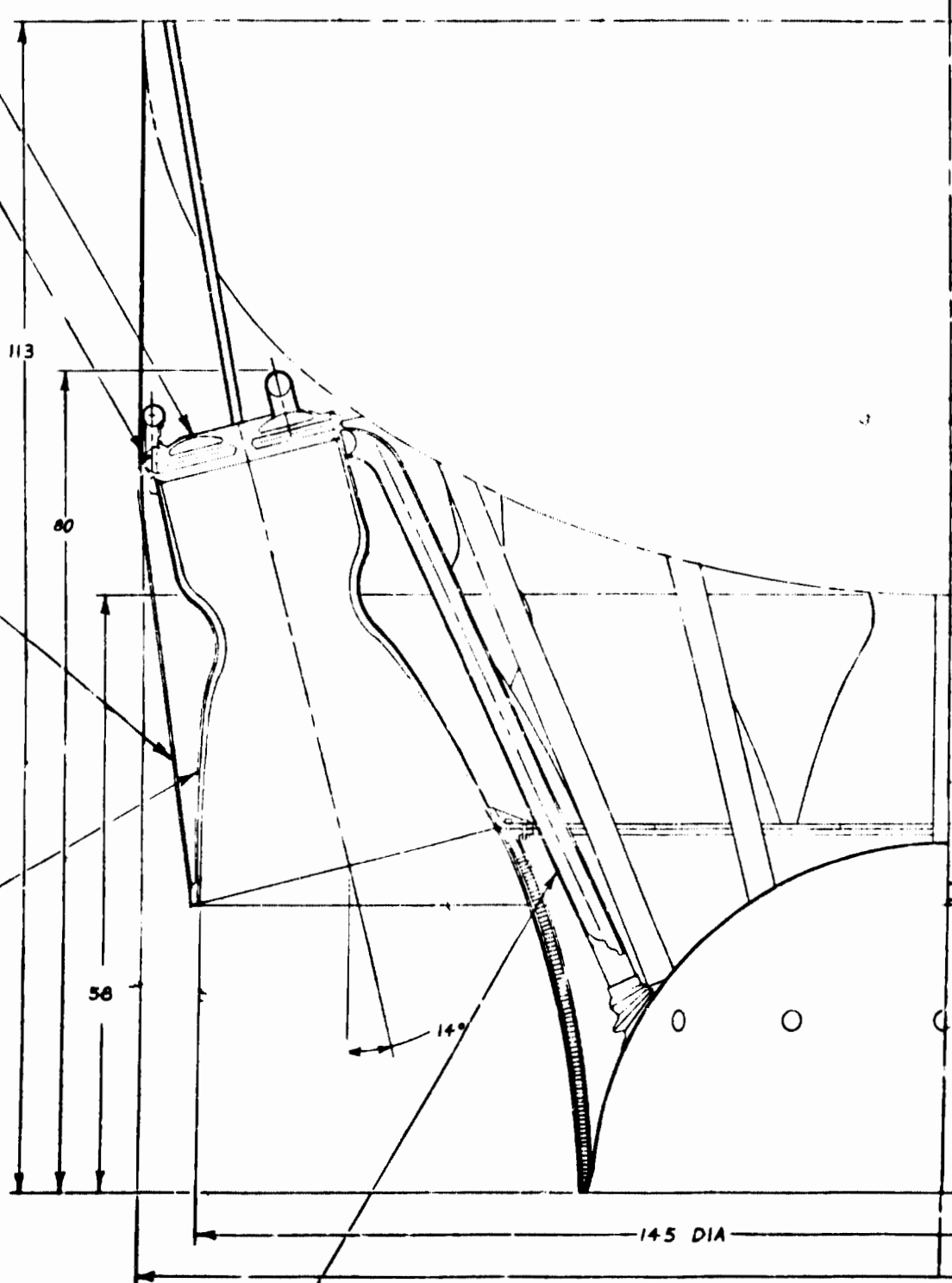
80

58

14°

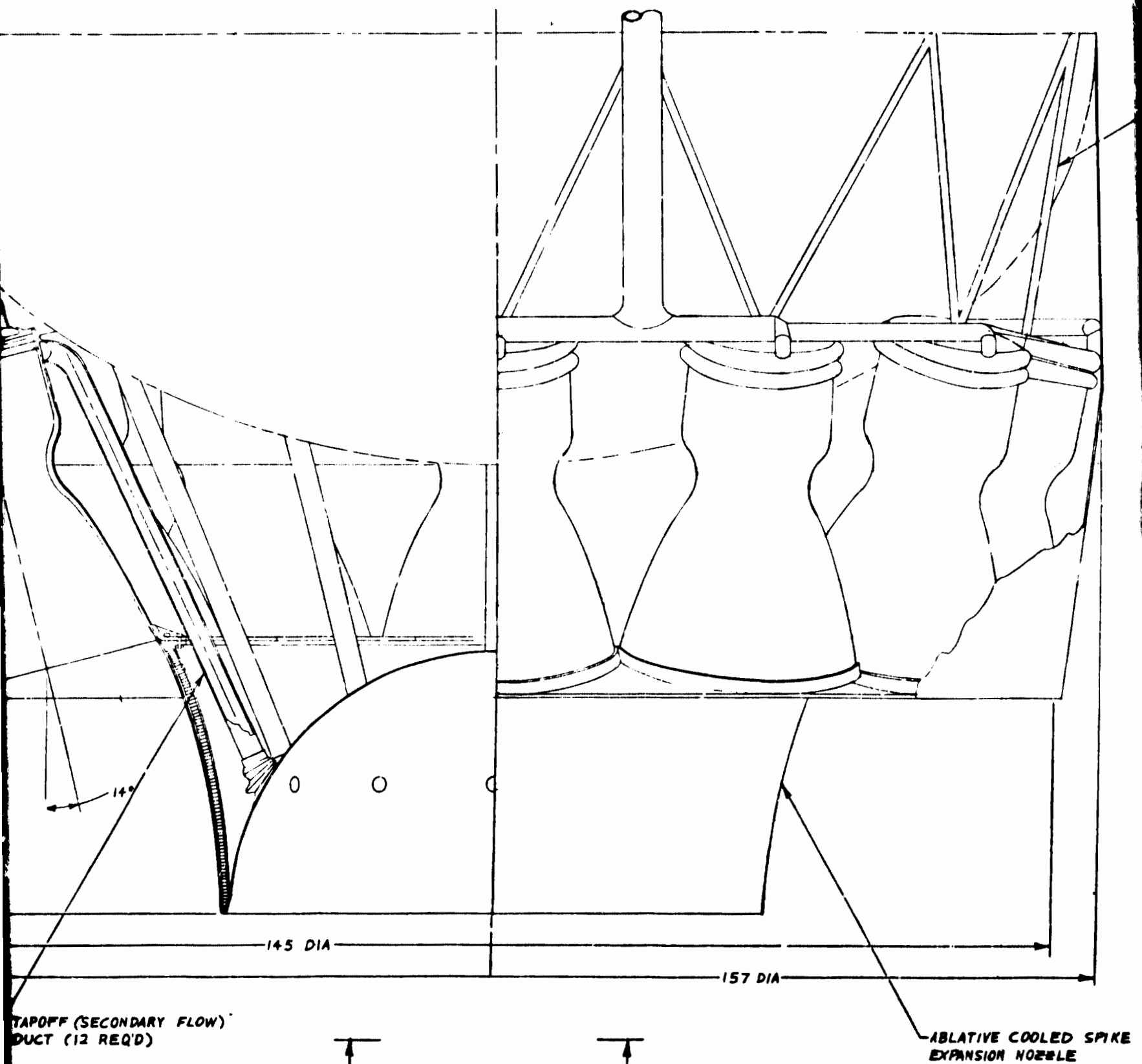
145 DIA

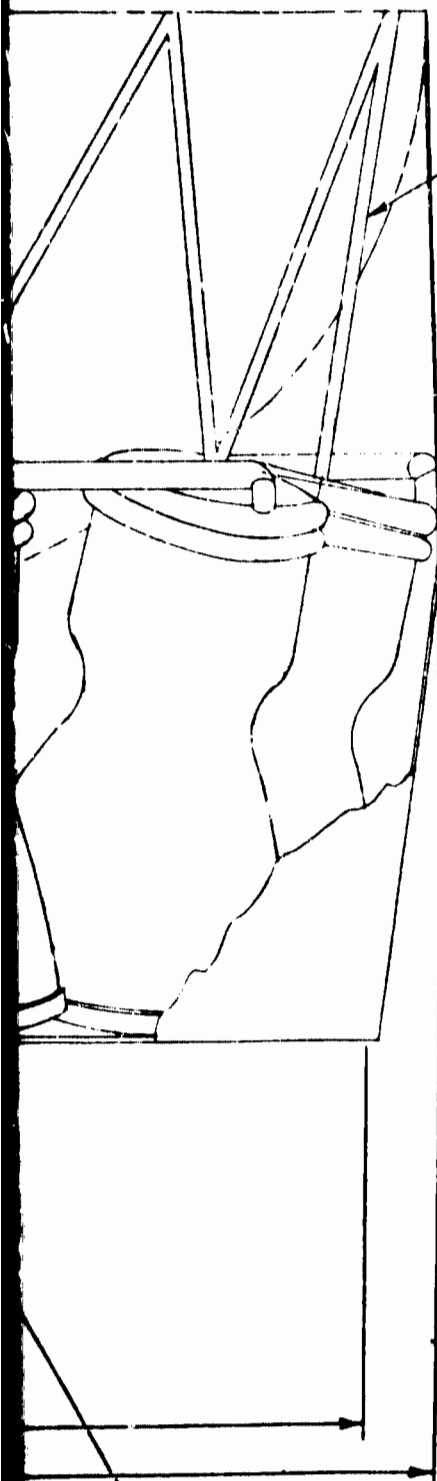
A



13

13





TUBULAR THRUST STRUT
(24 REQ'D)

MAJOR SYSTEM PARAMETERS

$F = 657,780 \text{ LB}_F$ (SEA LEVEL)

$P = 300 \text{ PSIA}$ (NOZZLE STAGNATION)

$\epsilon_n = 11.5$

$\epsilon_m = 5.41$

$N = 12$ BELL CHAMBERS

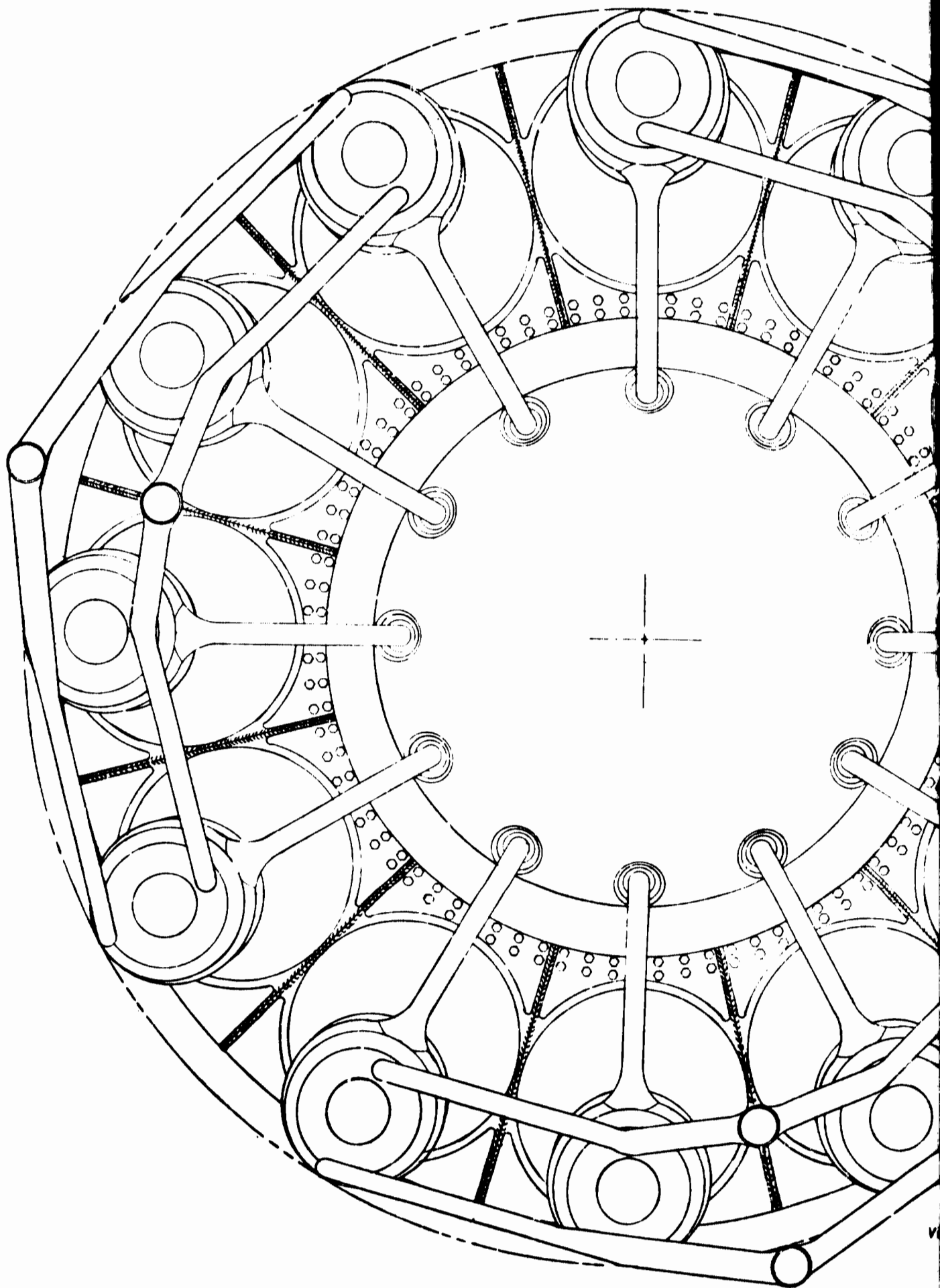
PROPELLANTS = $\text{N}_2\text{O}_4 / \text{N}_2\text{H}_4$ - UDMH (50-50)

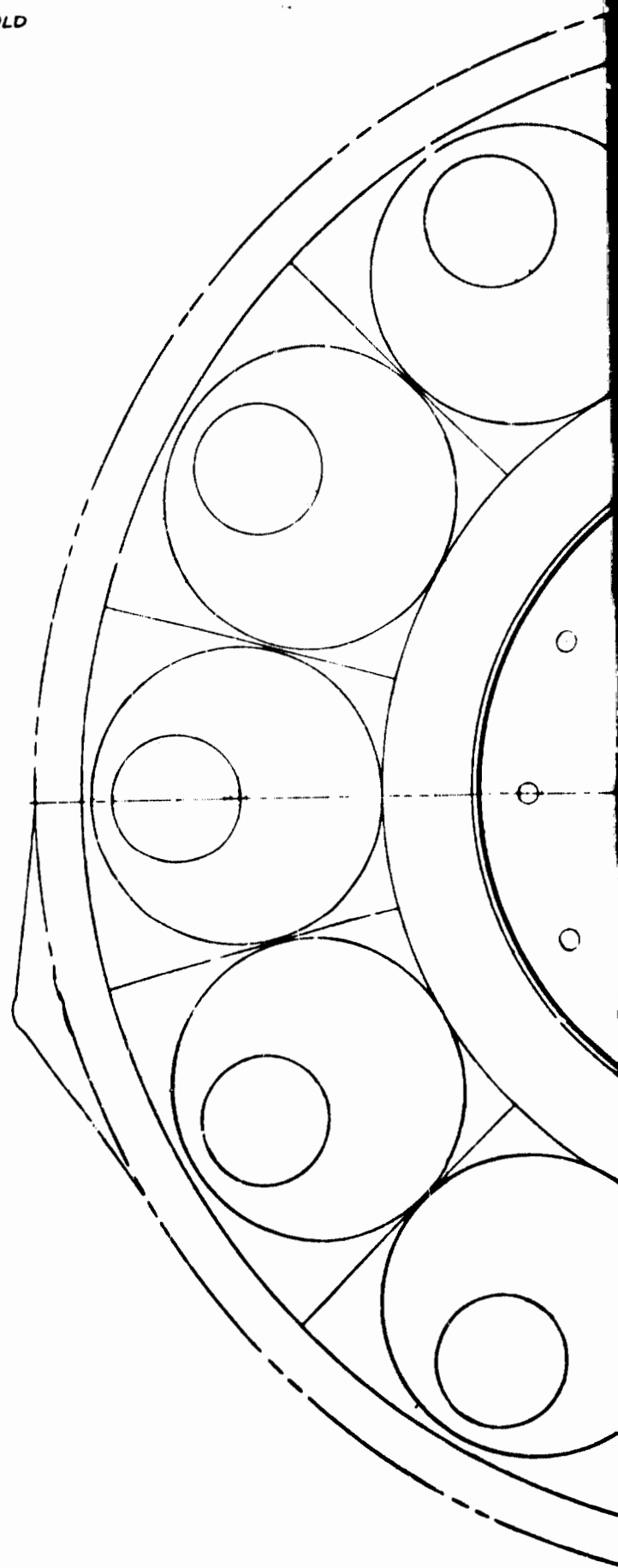
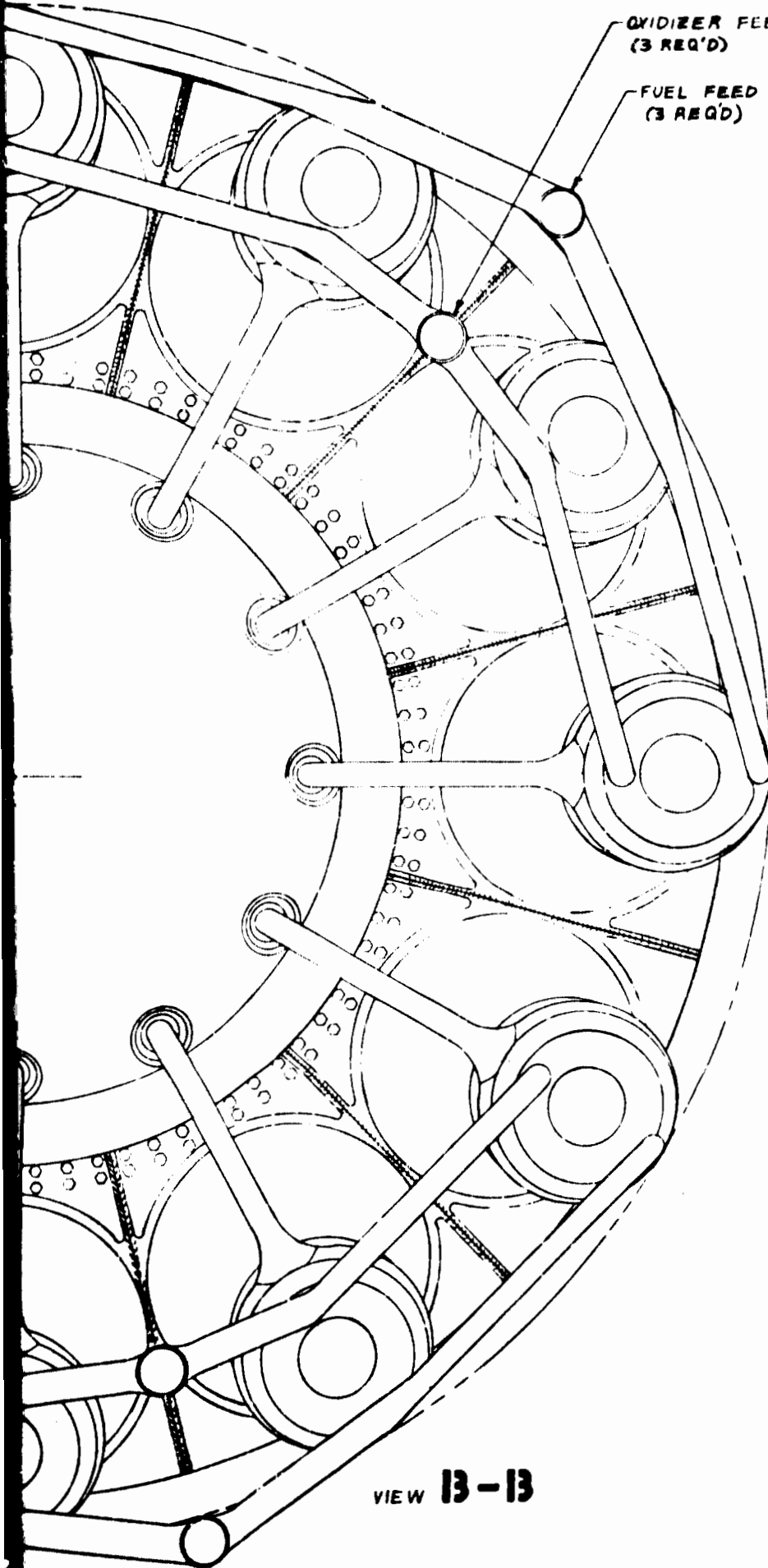
NOTE: The area ratio described by the scalloped perimeter of the module exits is 10.0

ABLATIVE COOLED SPIKE
EXPANSION NOZZLE

Fig. 165

Multichamber Aerodynamic Spike
Engine System. Medium Thrust,
Low Chamber Pressure.





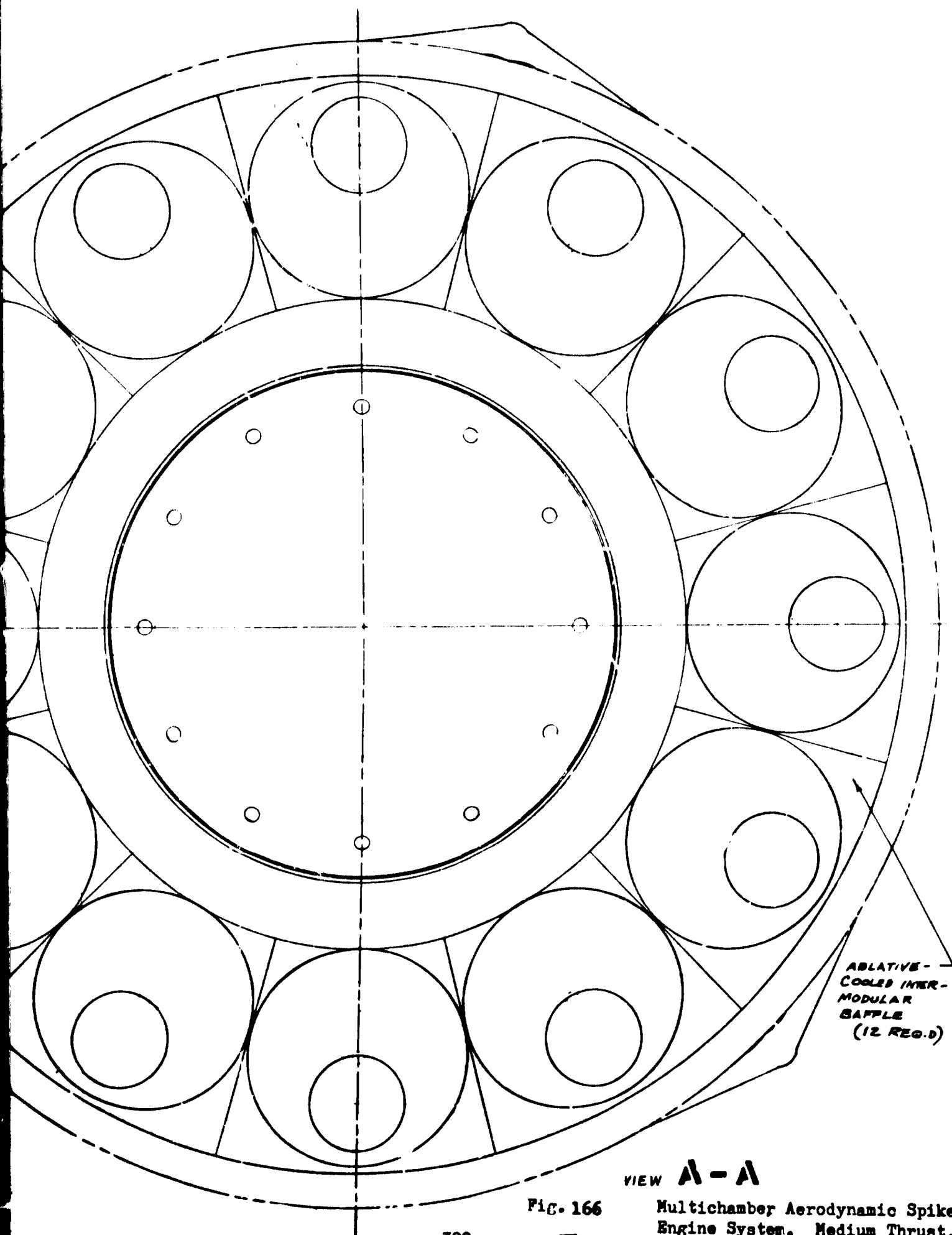
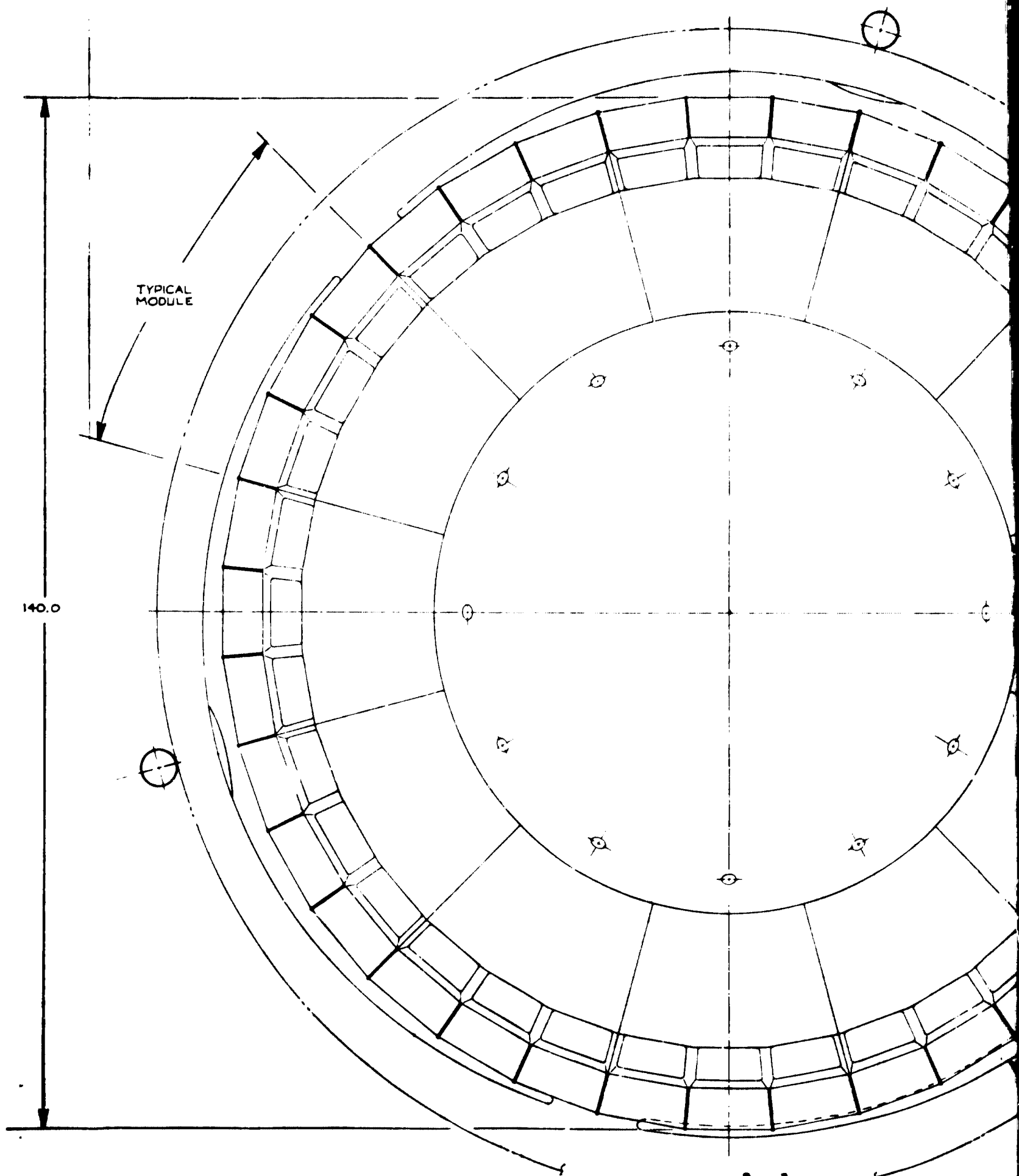


Fig. 166

3

VIEW A - A

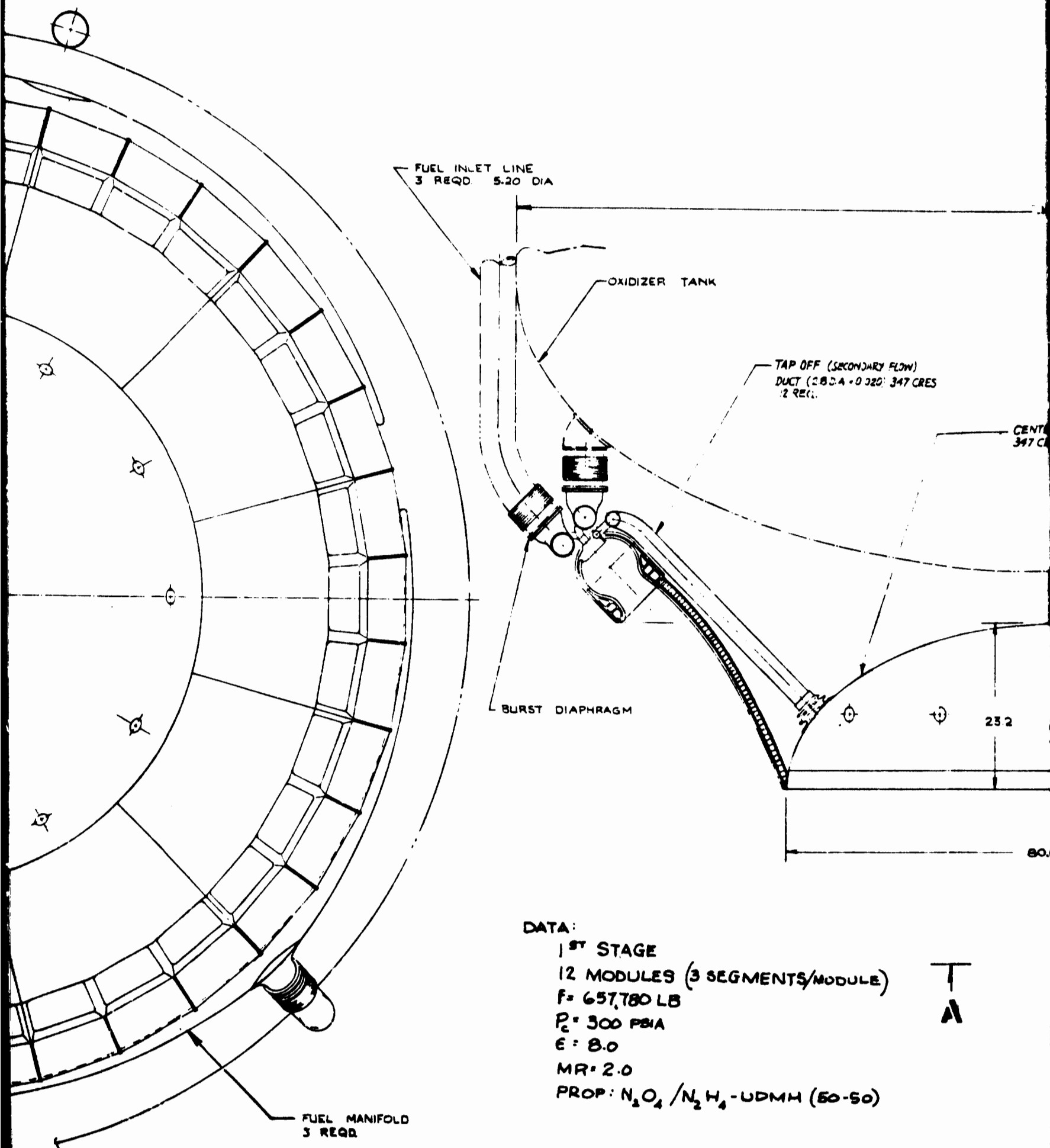
Multichamber Aerodynamic Spike
Engine System, Medium Thrust,
Low Chamber Pressure.

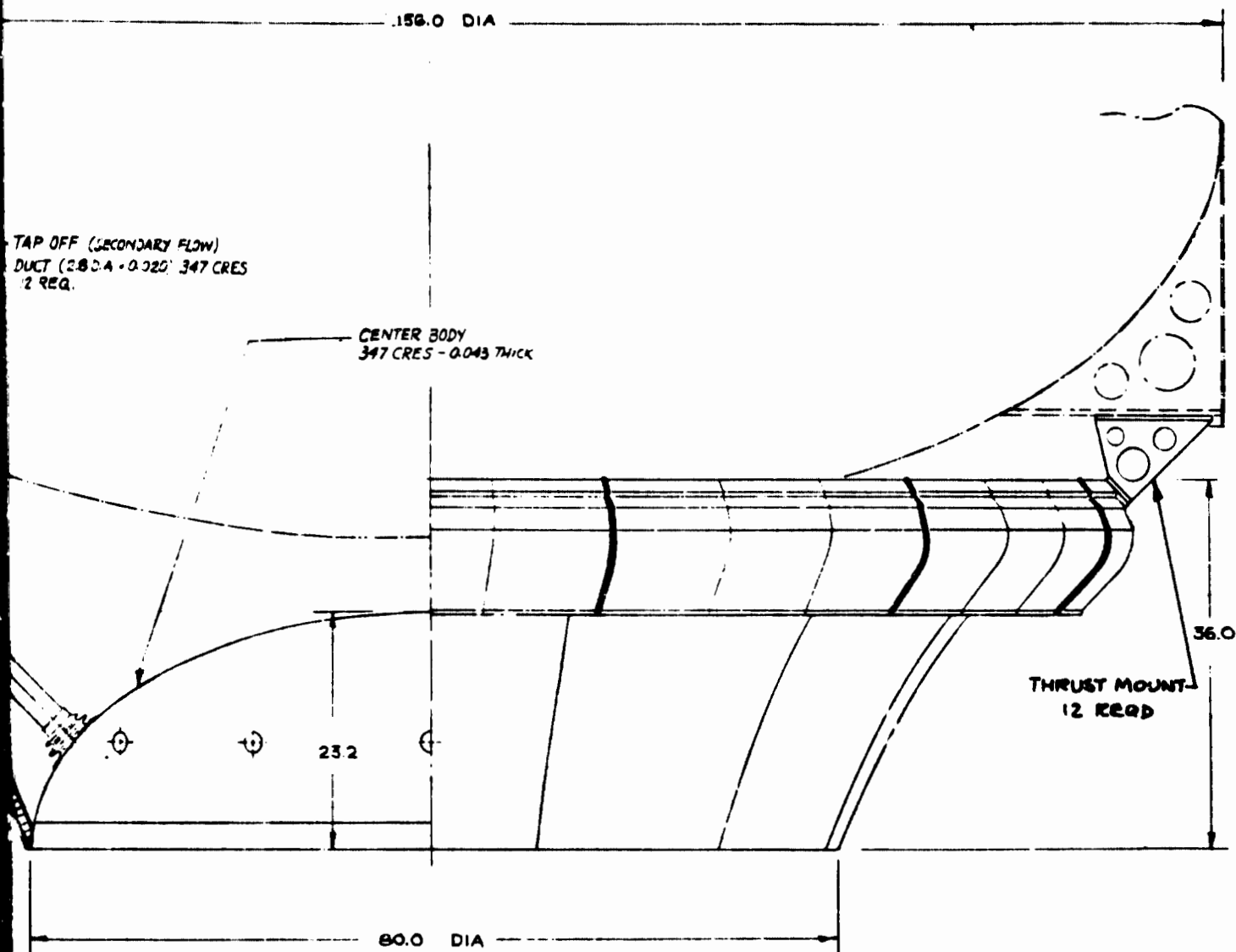


TYPICAL
MODULE

140.0

VIEW A-A





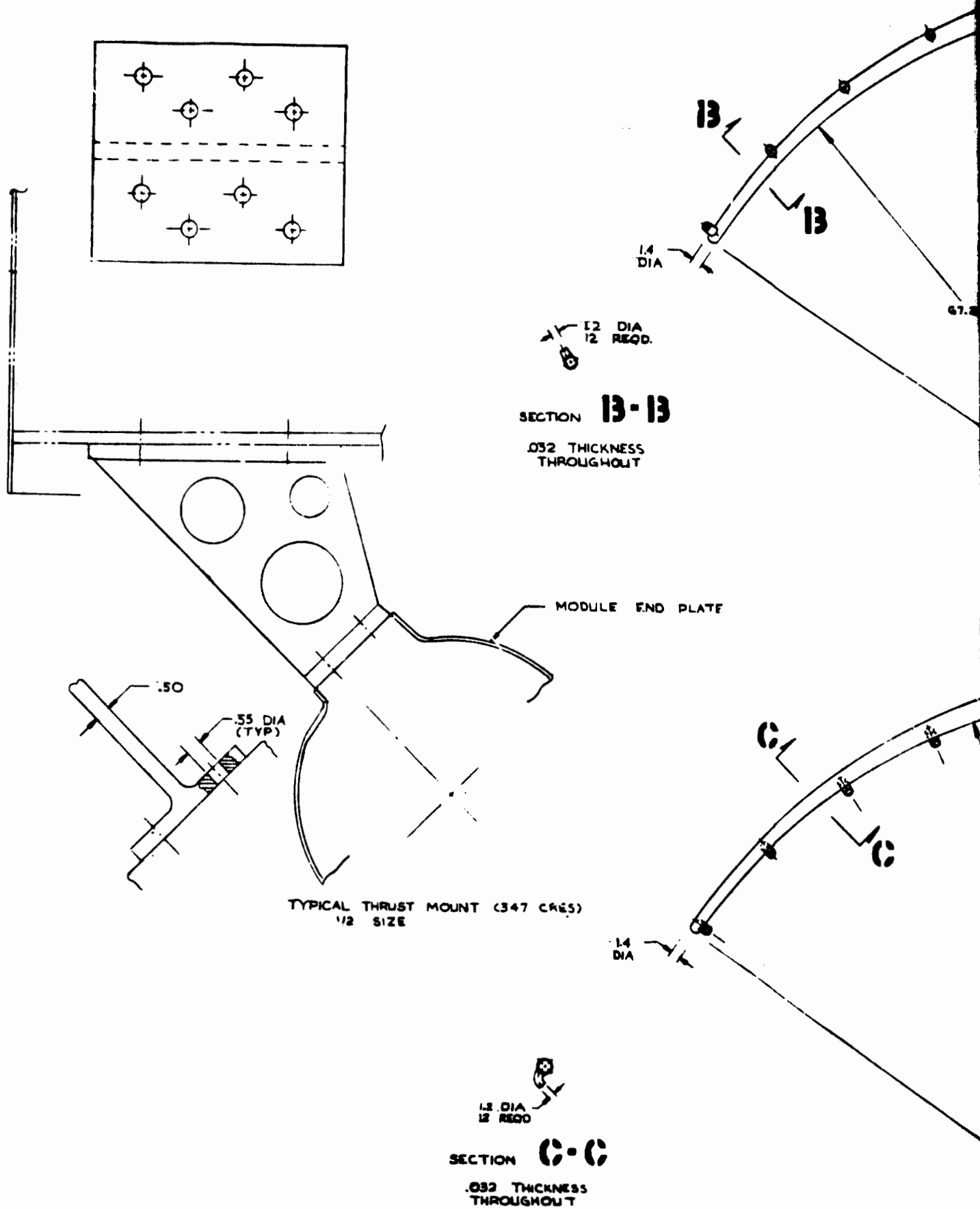
NTS/MODULE)



Fig. 167

Toroidal Aerodynamic Spike Engine.
Medium Thrust. Low Chamber Pressure.

MM (50-50)



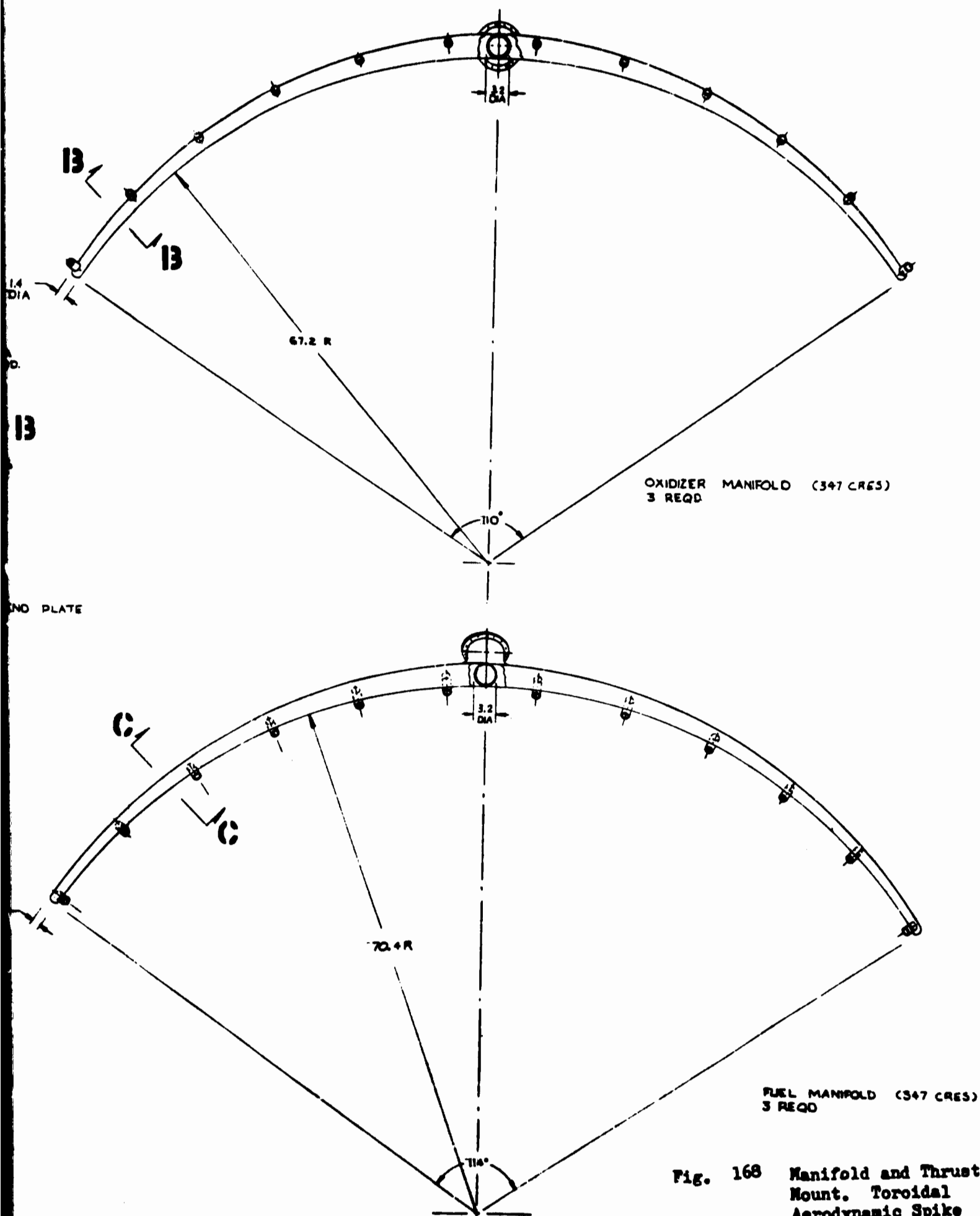
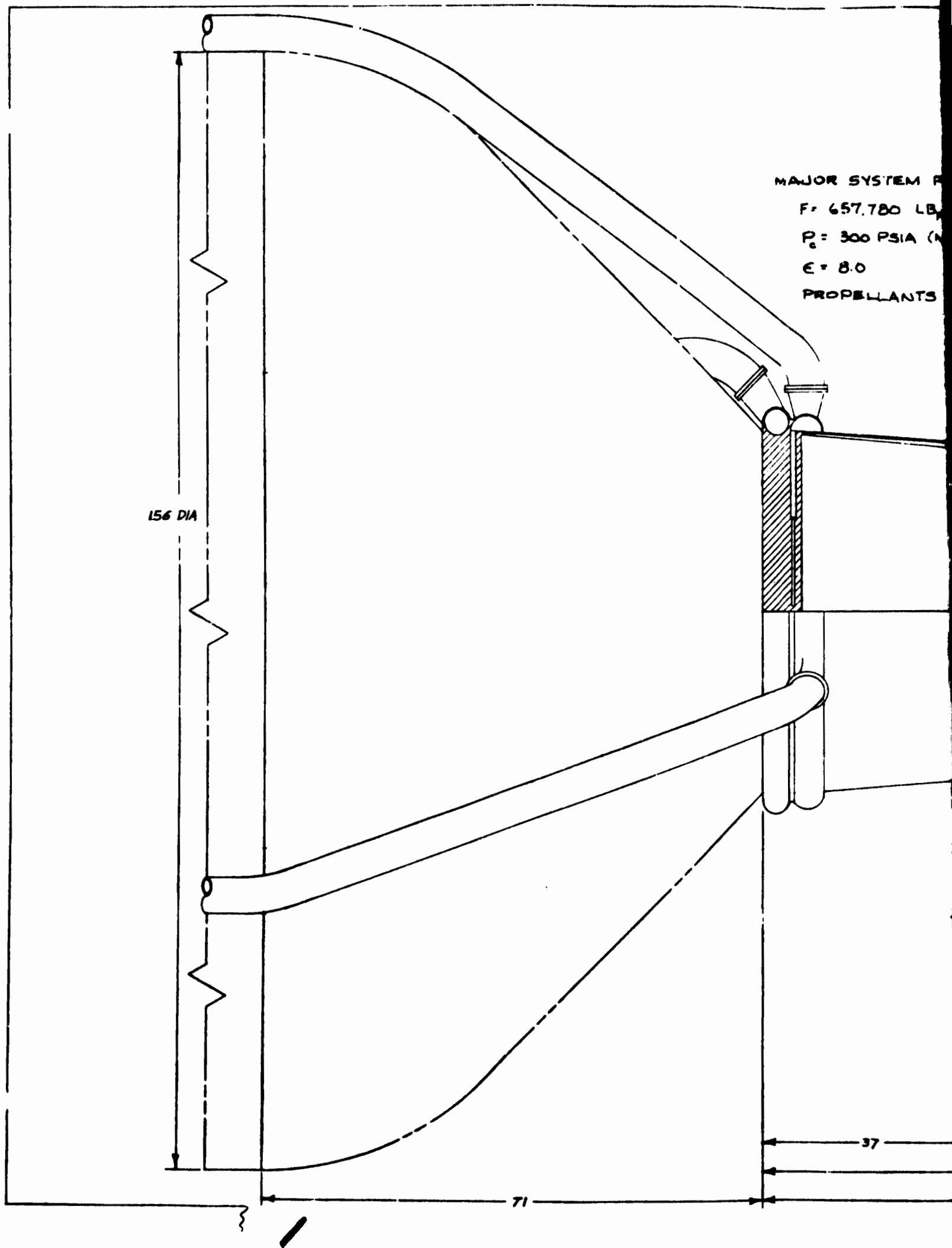


Fig. 168 Manifold and Thrust Mount. Toroidal Aerodynamic Spike Engine.



MAJOR SYSTEM PARAMETERS

$F = 657,780 \text{ LB}_f$ (SEA LEVEL)

$P_0 = 300 \text{ PSIA}$ (NOZZLE STAGNATION)

$\epsilon = 8.0$

PROPELLANTS = $\text{N}_2\text{O}_4 / \text{N}_2\text{H}_4$ - UDMH (50-50)

JET SEPARATION LIMITED ENVELOPE ($\epsilon = 8.0$)

BOATTAIL LINE

THROAT PLANE

37

120

157

205

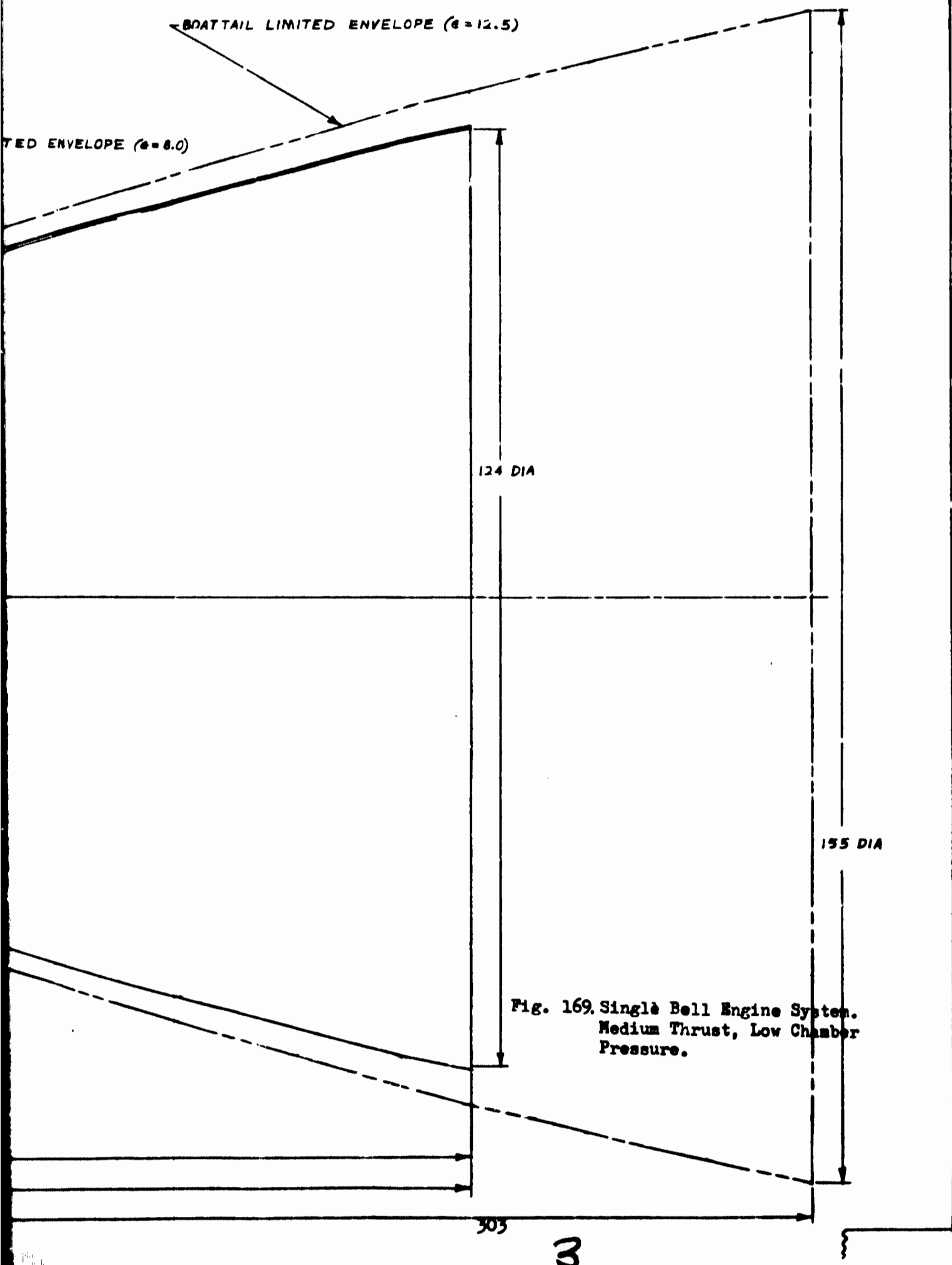


Fig. 169. Single Bell Engine System.
Medium Thrust, Low Chamber
Pressure.

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(fixed by a maximum overland transportation envelope) for the toroidal and multichamber engines and by nozzle separation for the single bell engine system. Table 14 summarizes the envelopes found for these booster configurations.

The annular toroidal combustor is divided into thirty-six (36) segments by full combustion zone baffles. Each group of three segment is plumbed in common to form twelve (12) modules. The modules are fed in groups of four from three fuel and three oxidizer ducts, each fitted with burst diaphragms. Engine start is initiated by pressurizing the propellant tanks. Cutoff is accomplished by propellant depletion. These sequences are also practical for the analogous multichamber configuration. The multichamber design (Fig. 165) employs twelve chambers, each bell module being analogous to a three segment module of the toroidal configuration. The bell modules extend to an area ratio of 5.4 which brings the exits nearly tangent. A small exit separation is necessary to accommodate the structural rings and ablative liners.

Although regenerative cooling of a sonic tube toroidal combustor is feasible for these engine parameters, ablative cooling was employed in the present study since regenerative pressure drop is reflected directly as a tank weight increase in pressure fed stages.

Both multichamber and toroidal combustors are cooled by the ablation of a phenolic refracil liner which is bonded to the structural shells with a high temperature adhesive. An ablative liner thickness of 0.63 inch would be required at the throat of either combustor for cooling over the 91 second burning duration. Char erosion of the throat dimension may be held to 6 - 8 percent of ablative thickness by in-

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Table 14 Engine Envelop Summary

Thrust Pounds	Engine Type	Nozzle Length, From Throat, L_N		Engine length, From Turbopump Inlets		Engine Length, From Elliptic Tank Bottom		Engine Diameter inches
		inches	Percent of 15 degree cone	inches	Percent of 15 degree cone	inches	Percent of 15 degree cone	
658,000	Toroidal	26.5	17.7	41.5	26.4	30.5	17.7	156.0
658,000	Multichamber	54.3	36.2	80.0	51.0	58.0	33.7	156.0
658,000	Single Bell	120.0	80.0	157.0	100.0	172.0*	100.0	124.0
2,000,000	Toroidal	62.6	19.0	98.5	45.0	68.2	26.2	216.0
2,000,000	Multichamber	104.0	30.0	144.5	66.0	100.0	38.5	216.0
2,000,000	Single Bell	202.0	80.0	218.5	100.0	260.0*	100.0	164.0

*This gives an indication of the relative comparison of total vehicle length affected by the engine configuration. The conical tank bottom normally used with the single bell engine requires a longer tank structure. The value shown is measured from the actual bell exit to a fictitious elliptic tank bottom which contains the same quantity of propellant as the conical tank bottom.

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jecting approximately 2 percent of fuel film coolant along the chamber walls, based on LEM engine tests. A 8 percent surface regression corresponds to throat area increases of 2 percent, 1.5 percent, and 0.5 percent for the annular toroidal, multichamber, and single bell combustors respectively.

Multichamber combustors should show char and erosion depths slightly less than those experienced in annular combustors under similar surface conditions, since the heat streamlines diverge radially, i.e., the cross sectional perimeter exposed to hot gas is less than the perimeter being charred. This effect is small at the 658K design point, the diminution in heat flux at the char layer amounting to 5 percent when half charred and 9 percent at full char. At lower module thrusts and longer burning times, this effect would become more important.

Thrust load transmission in the toroidal design is accomplished by supporting the centerbody and skirt loads by a honeycomb sandwich shell backing the ablative coolant layer. This shell is welded to the inboard throat support beams of the toroidal segments. Engine thrust is transmitted to the vehicle through twelve thrust mounts welded to the segment end caps bounding each module. The load path in the multichamber configuration is somewhat more complex, as it was assumed here that some weight could be saved by utilizing the outer structural shells of the bell modules as members to transmit expansion nozzle and centerbody components to the module thrust structure. These shells could be built up of welded sections and ablative liners bonded and cured in place. A reinforcement ring was placed around the module exits to distribute the nozzle line load and bending moment into the twelve members. The rings also provide a convenient place to weld

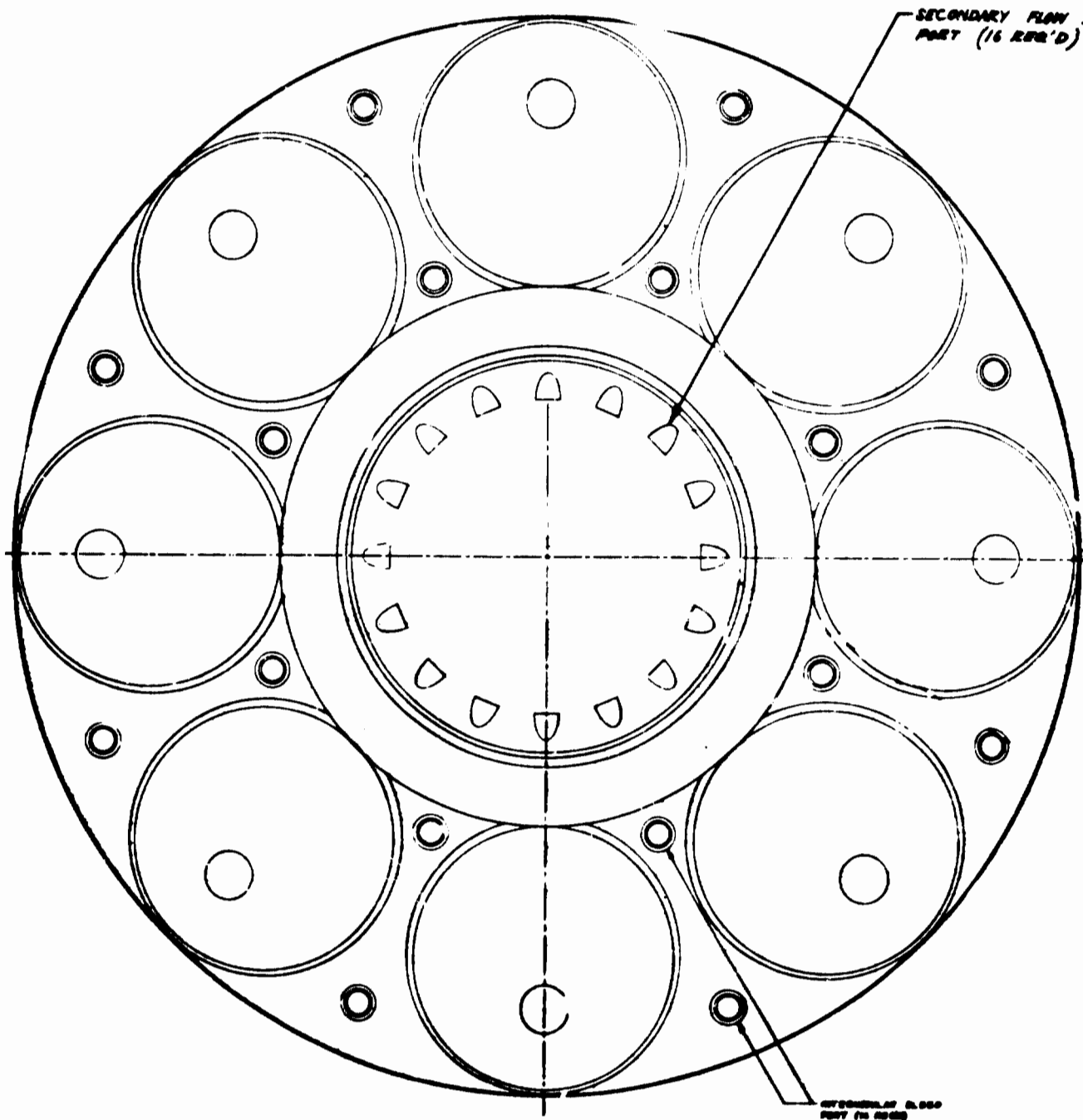
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ablative cooled baffle plates which seal the boattail from recirculating gas. A bolted connection is shown at the interface of the spike nozzle and the bell modules. The ablative liners of each module and the spike are case and cured as independent units.

The thrust structure shown in Fig. 165 is composed of twenty-four (24) tubular thrust struts arranged in a lattice. The struts are 17-7PH steel as is the propellant tankage. Welding of 24 such struts into place would be considerably cheaper than the construction of a semi-monocoque or sandwich shell over the same span. A monocoque shell of thickness constrained by compressive yield stress (0.016 inch) was found to be unstable in the local buckling mode. Local reinforcement around the strut attachment points will be necessary to diffuse the loads into the membrane. The placement of anti-slosh and anti-vortex baffles on the tank interior would be coordinated with these attach points to minimize the weight of such reinforcement.

High Thrust, High Chamber Pressure Engine Design

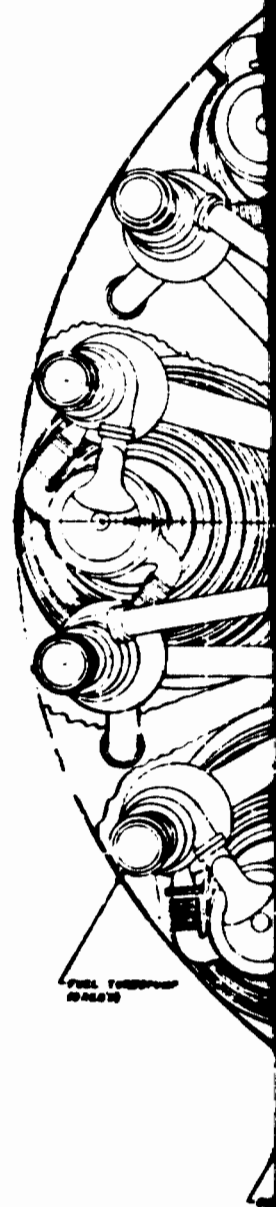
The last design point evaluated was for an engine system which operates at high (2000 psia) chamber pressure and delivers 2,000,000 pounds of thrust at sea level. Typical multichamber and toroidal aerodynamic spike engines and a single bell chamber engine which meet these requirements are shown in Figs. 170, 171, and 172. These engines are regeneratively cooled with N_2O_4 at supercritical pressure. Parallel turbines driven by primary combustor tapoff gases are used. Both engines contain eight modules, each fed by its own separate oxidizer and fuel turbopump. The area ratios of the annular engines were limited by an 18 foot vehicle diameter. Jet separation at sea level



SECONDARY FLOW IN SECTION
PART (16 REV'D)

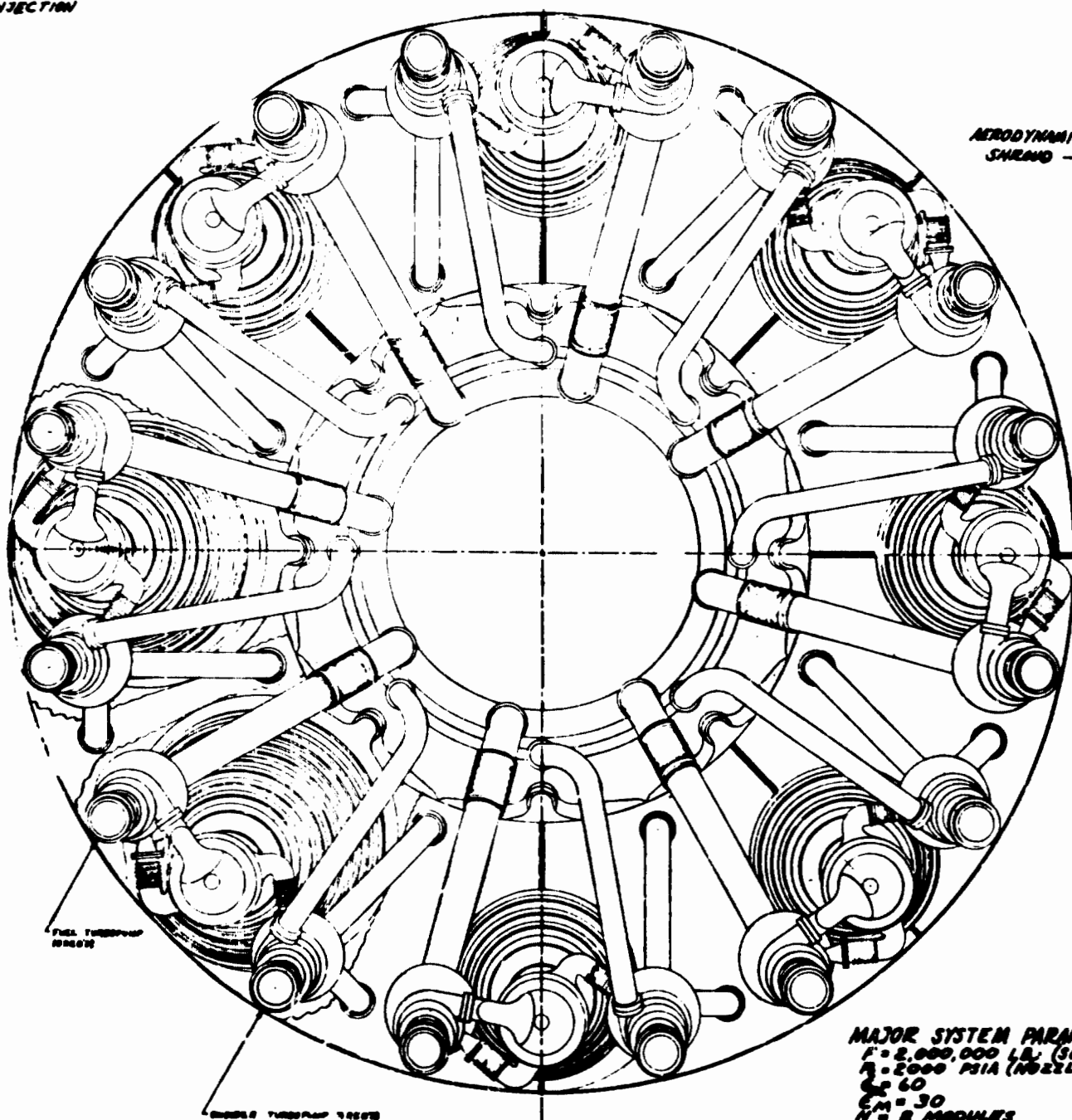
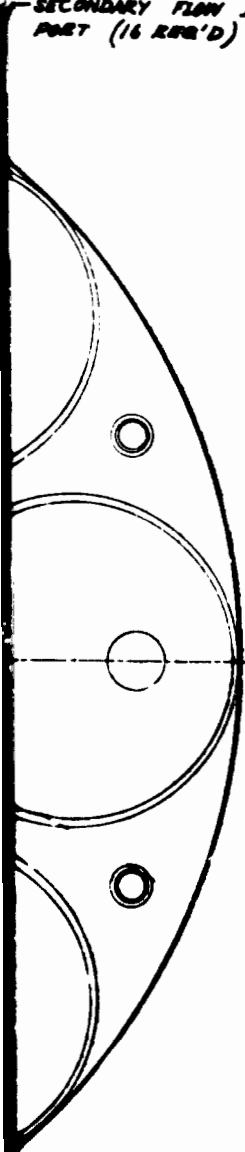
SECTIONAL VIEW
PART (16 REV'D)

SECTION B-B



1

SECONDARY FLOW INJECTION
PORT (16 RPP'D)



AERODYNAMIC DYNAMIC
SHEAR

NOZZLE FUEL INLET

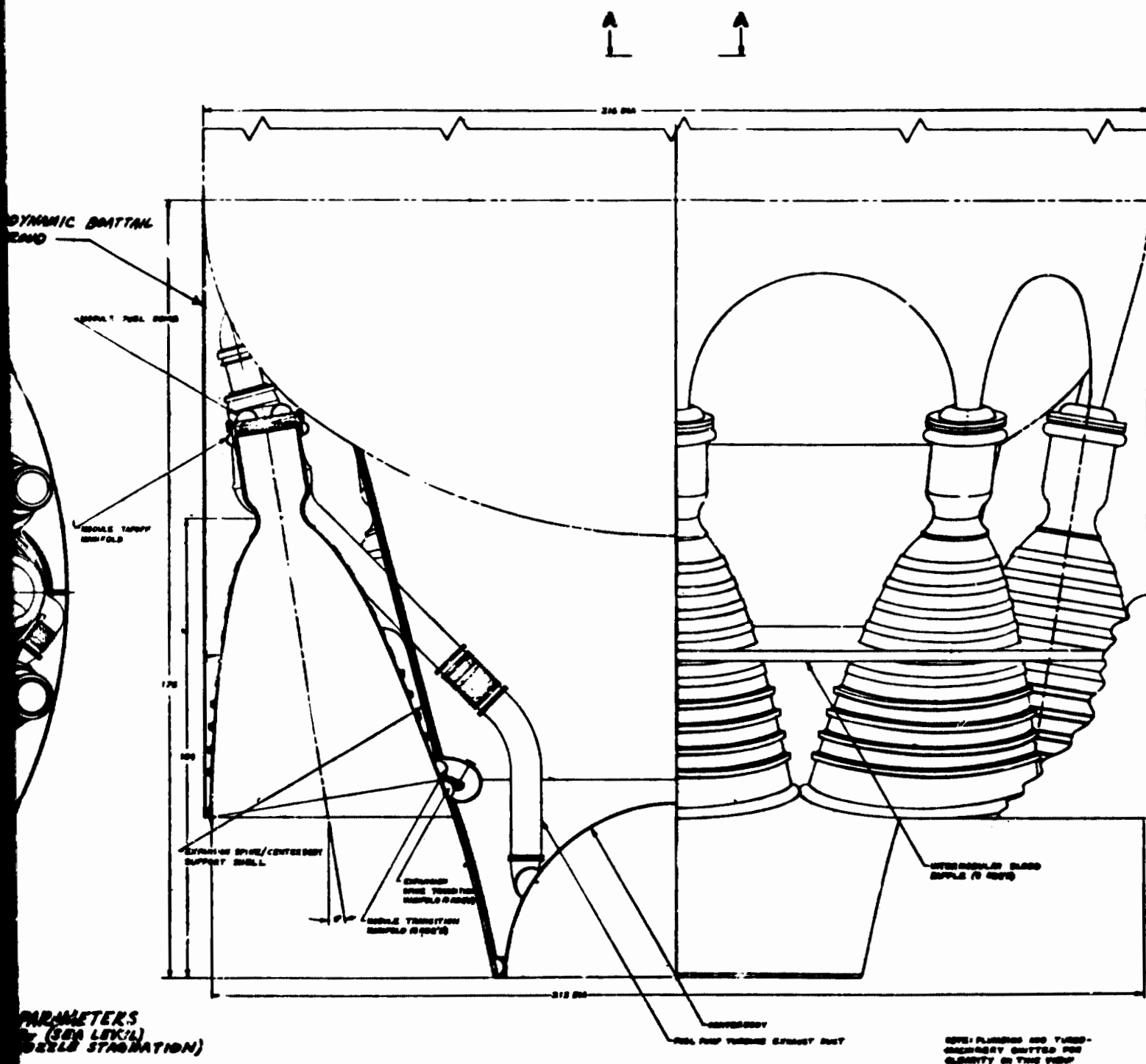
NOZZLE TAPOFF
ORIFICE

FUEL TAPOFF
ORIFICE

NOZZLE TAPOFF ORIFICE

MAJOR SYSTEM PARAMETERS
 $F = 2,000,000$ LBS (SEA LEVEL)
 $P = 2000$ PSIA (NOZZLE STAGNATION)
 $\gamma = 1.2$
 $M = 30$
 $N = 8$ MODULES
 PROPELLANTS = N_2O_4/N_2H_4 - UDMH (S)

NOTE: The area ratio defined
by the scalloped perimeter of
the module exits is 50.7.

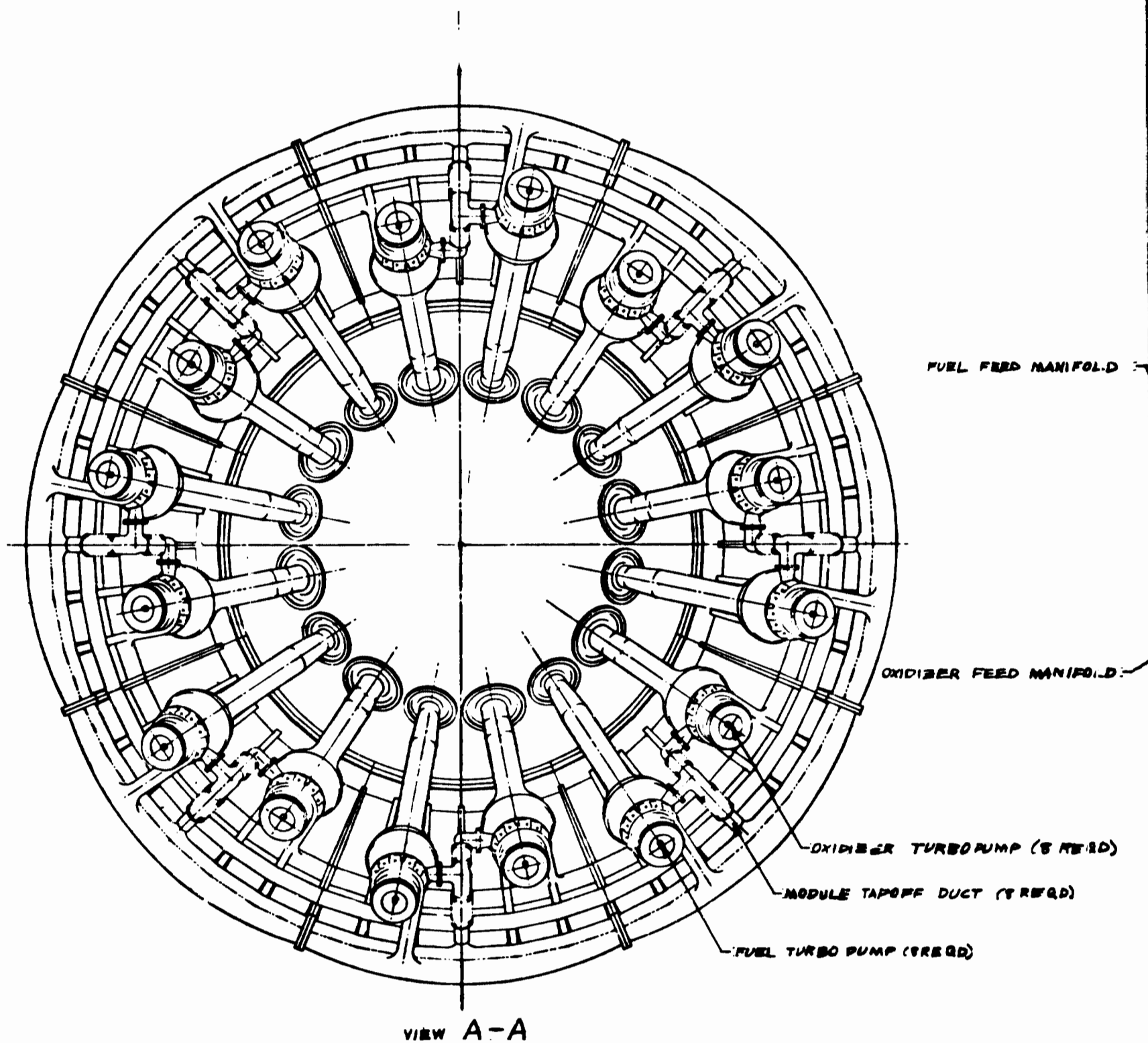


PARAMETERS
(SEE LEX/1)
(SEE STAGNATION)

$\frac{1}{2} \rho_0 / \frac{1}{2} \rho_0 - UDMH (50-50)$

A ratio defined
by the perimeter of
the spike is 50.7.

Fig. 170 Multichamber Aerodynamic
Spike Engine System High
Thrust, High Chamber
Pressure.



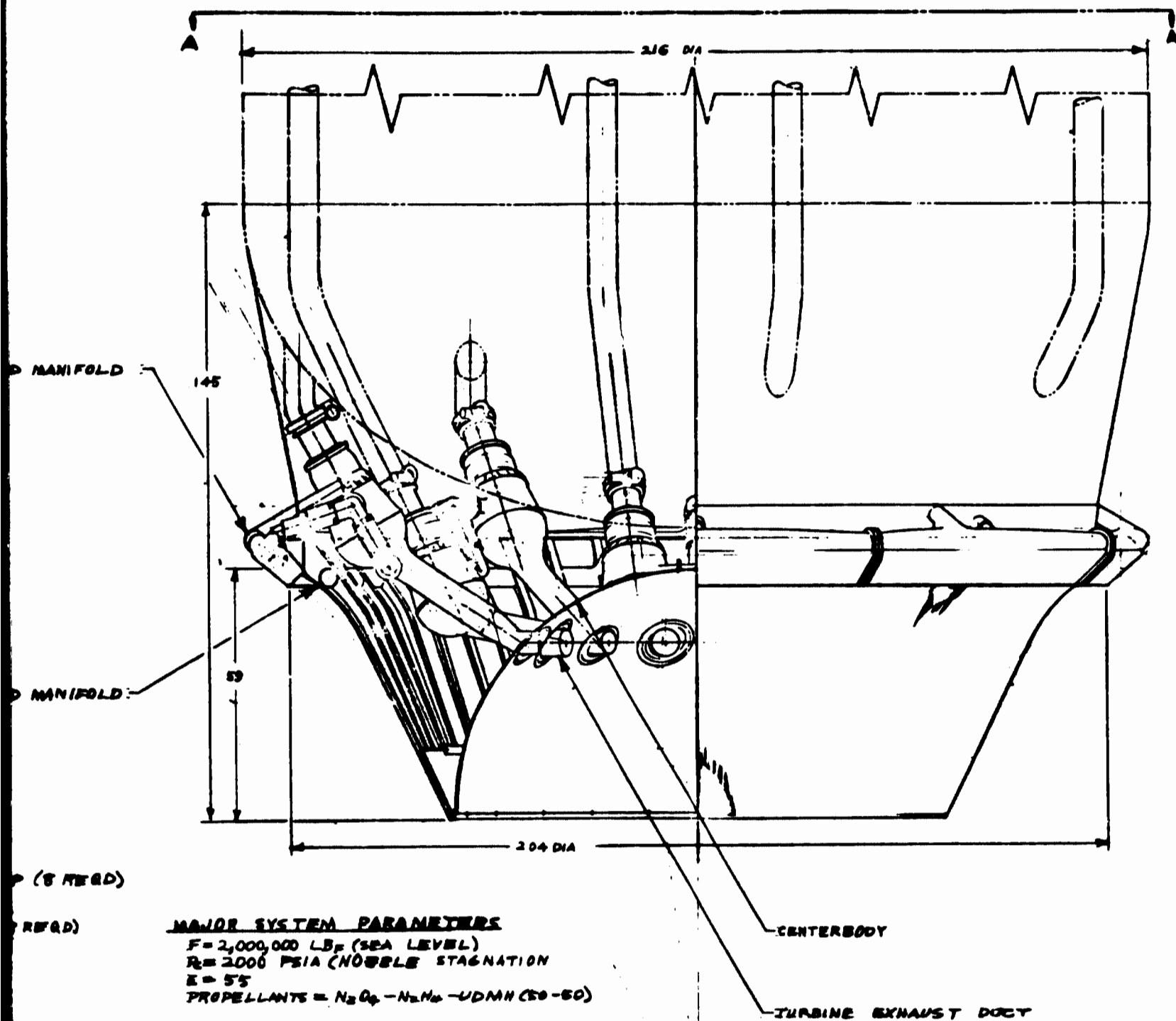
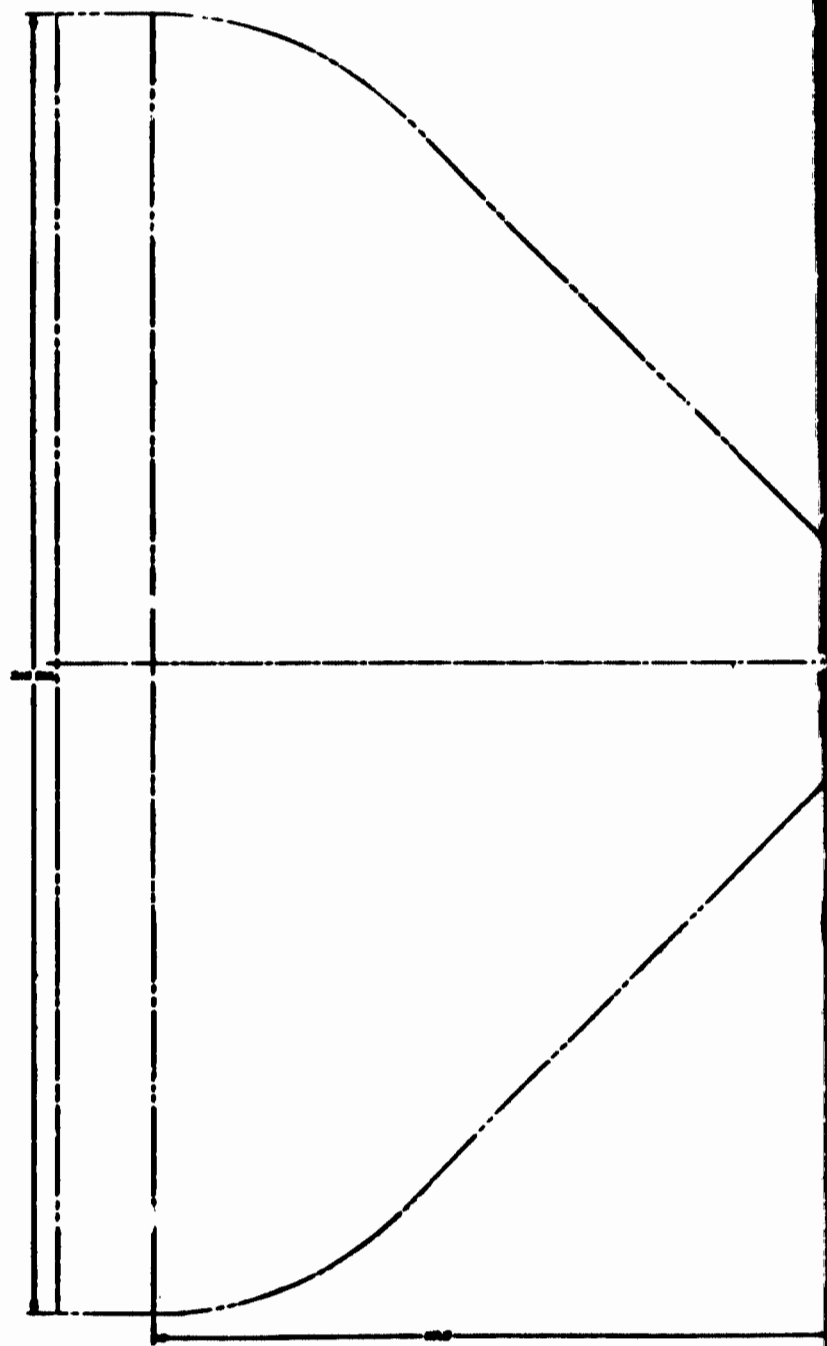
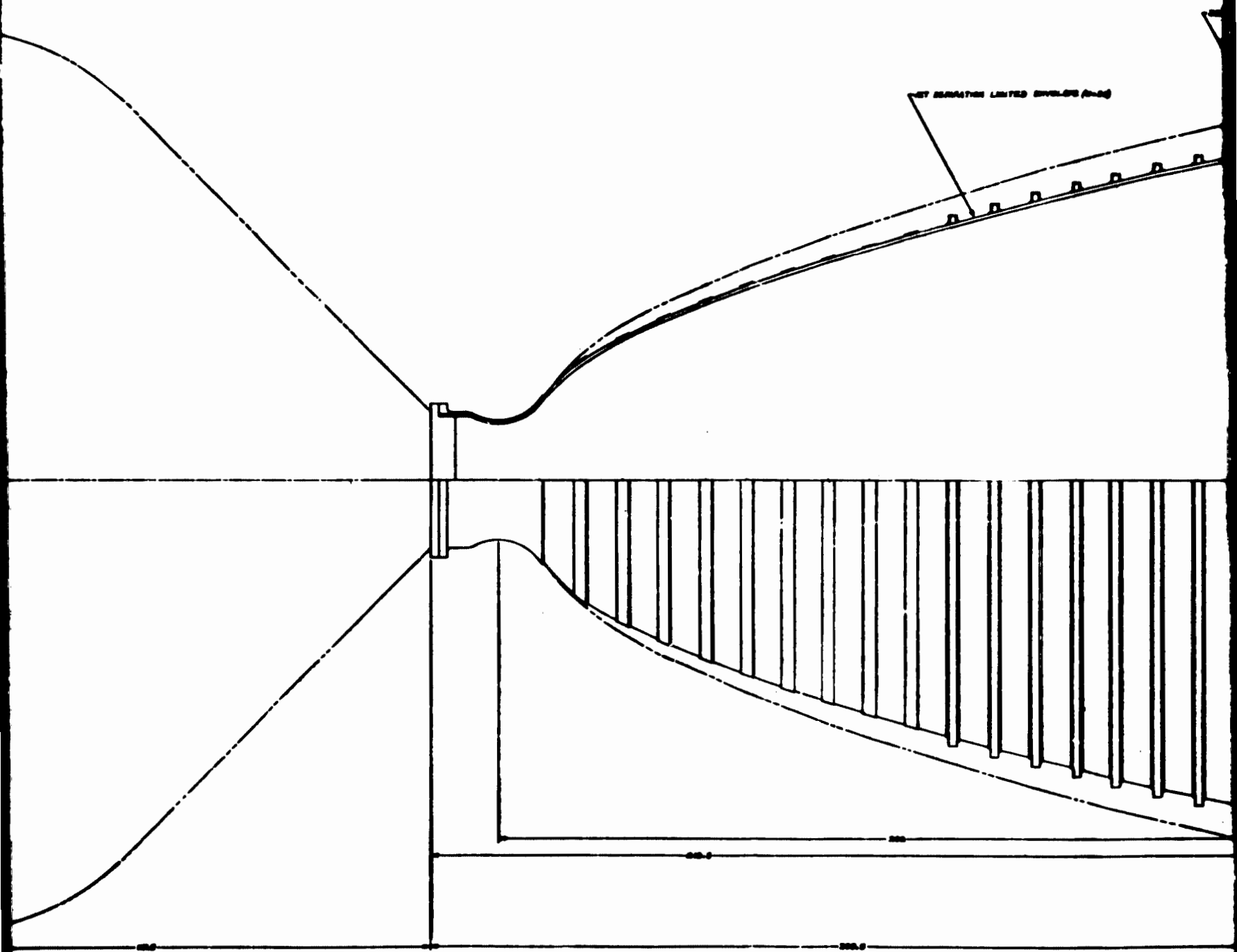
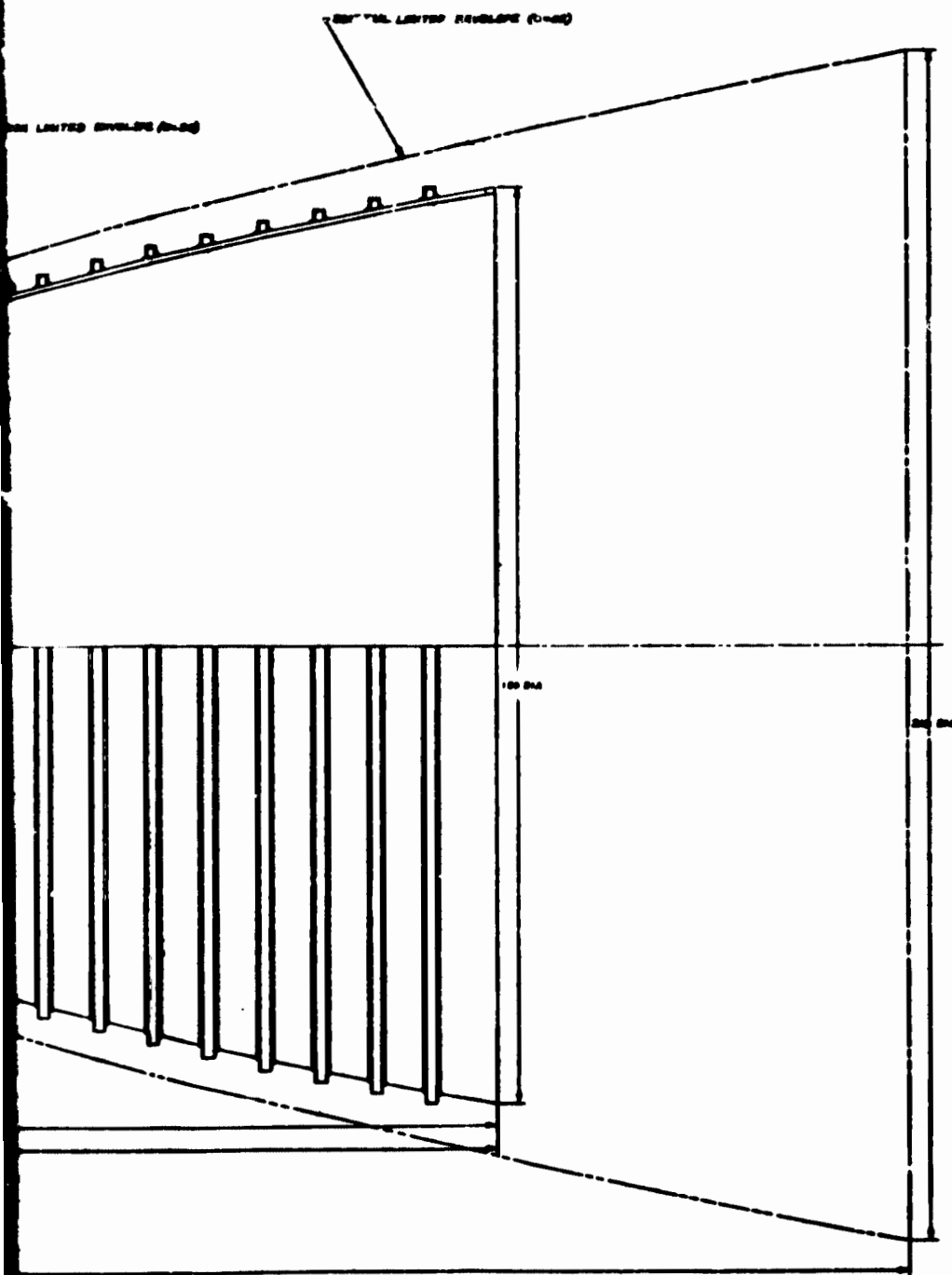


Fig. 171 Toroidal Aerodynamic Spike Engine System. High Thrust, High Chamber Pressure.



1.





NOZZLE SYSTEM PARAMETERS
 $P = 3,000,000$ LB. / SQ. IN. (SEA LEVEL)
 $Q = 2000$ PSIA (NOZZLE STAGNATION)
 $Q = 0.00$
 PROPELLANTS = H_2, O_2 - (SEA LEVEL)

Fig.172 Single Bell Engine.
 High Thrust High
 Chamber Pressure.

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constrained the area ratio of the bell thrust chamber to a much lower value of 35. Dimensions for these engine systems are given in Table 14. Multichamber module area ratio was set at 30 to provide nearly tangent exits without sea level separation of the bell modules. The toroidal combustor is shrouded to an area ratio of 3.5 to maintain chemical reaction equilibrium during the initial part of the expansion process. An aerospike nozzle length of 19 percent of a 15 degree half angle cone of equivalent area ratio was selected for the toroidal combustor. An equal percent length multichamber combustor would have had no common spike, as all of this length would be taken by the bell modules. A 30 percent length configuration with a common spike was assumed for layout purposes, as this value corresponded to that of the cold-flow model tested.

Several turbopump mounting positions were considered for the toroidal configuration. The radial inclined position was selected since it (1) had short propellant discharge ducts which were closely coupled to the combustor and supported the turbopumps, (2) packaged within the dimensional confines of a module, (3) made provision for a parallel turbine tapoff system, and (4) minimized the length of hot gas ducting. Mounting the pumps outboard of the toroidal combustor required very long turbine discharge ducting to feed secondary flow to the aerospike centerbody. A common axis turbopump with back-to-back turbines could be packaged within a module if mounted "horizontally" (axis oriented in the circumferential direction perpendicular to the vehicle centerline), but this produced poor exit conditions for the turbine exhaust gases and required elbows ahead of the pump inlets (increased NPSH requirements). This configuration required as much separation between the top of the toroidal combustor polygon and the tank bottom as the radial inclined position and so offered no engine length saving.

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Turbopump mounting in the 2000K multichamber aerospike design resolved to a choice between placing the machinery with axes nearly parallel to the vehicle centerline and with discharges opposite the bell module injectors or opposite the module/common expansion spike transition. The former option was chosen as it permits placing the turbomachinery nearer the module thrust structure, at points where the bell modules are comparatively rigid, and where the lengths of oxidizer inlet, fuel discharge, and oxidizer and fuel turbine tapoff lines are minimized. As turbopumps are placed between, rather than inboard of the bell modules, maintenance access to them may be gained after engine/vehicle mating through doors in the non-loadbearing outer shroud. Mounting the oxidizer turbine between chambers also places its discharge in a favorable position for the introduction of intermodular bleed gas, as shown in Fig. 170. This mounting does have the disadvantage of long oxidizer coolant feed ducts.

Coolant transfer between multichamber modules and the expansion nozzle tube bundle was accomplished by placing eight collection manifolds around the expansion nozzle and ducting the flow to eight distribution manifolds around the module exits. The bolted flanges shown could be welded if disassembly for maintenance is not necessary.

Theoretical minimum pressure drop is achieved in regenerative multichamber combustors along a single downpass flow path. This flow path is inconvenient from a systems standpoint as it requires an extra duct to return the coolant to the module injectors.

At high chamber pressures where combustion chamber dimensions are relatively small and at high thrusts where relatively large manifold areas are required for constant manifold velocity, another effect is

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observed. Figures 173 and 174 are sketches of a multichamber module injector sized to the flow requirements of the 2000K design point. It can be seen that the injector used with the single downpass cooling path requires four tangential distribution manifolds whose space requirements become awkward for the manifold velocities assumed. In contrast, an up pass injector requires two less welded manifolds and allows the use of a thinner injector block. Additional injector block thickness is required in the downpass injector as space for the tapoff manifold. In this configuration, both tapoff ports and coolant tube feed holes must be located near the injector face. In the up pass injector, the tapoff manifold may be located aft of the injector face plane, since the coolant feed manifold does not interfere with it.

An alternate mounting for the oxidizer pump opposite the module/spike transition was also considered for this application. A pass-and-one-half flow circuit was visualized in which oxidizer would flow first aft and then forward to cool the spike nozzle then transfer to the bell chamber in a single up pass. The position of the pump discharge opposite the flow transition was found to offer no significant advantage over the configuration shown in Fig. 170. A double pass spike, although containing 30 percent fewer tubes, requires two manifolds at its forward end, one for distribution and one for collection, in addition to a turning manifold at its aft end and the distribution manifold around the bell module exit. This amounts to an extra manifold over the single up pass configuration pictured. In the analogous pass-and-one-half inboard wall toroidal configuration of Fig. 171, this extra manifold is obviated by a direct two-for-one tube splice, which is geometrically inconvenient in a multichamber combustor.

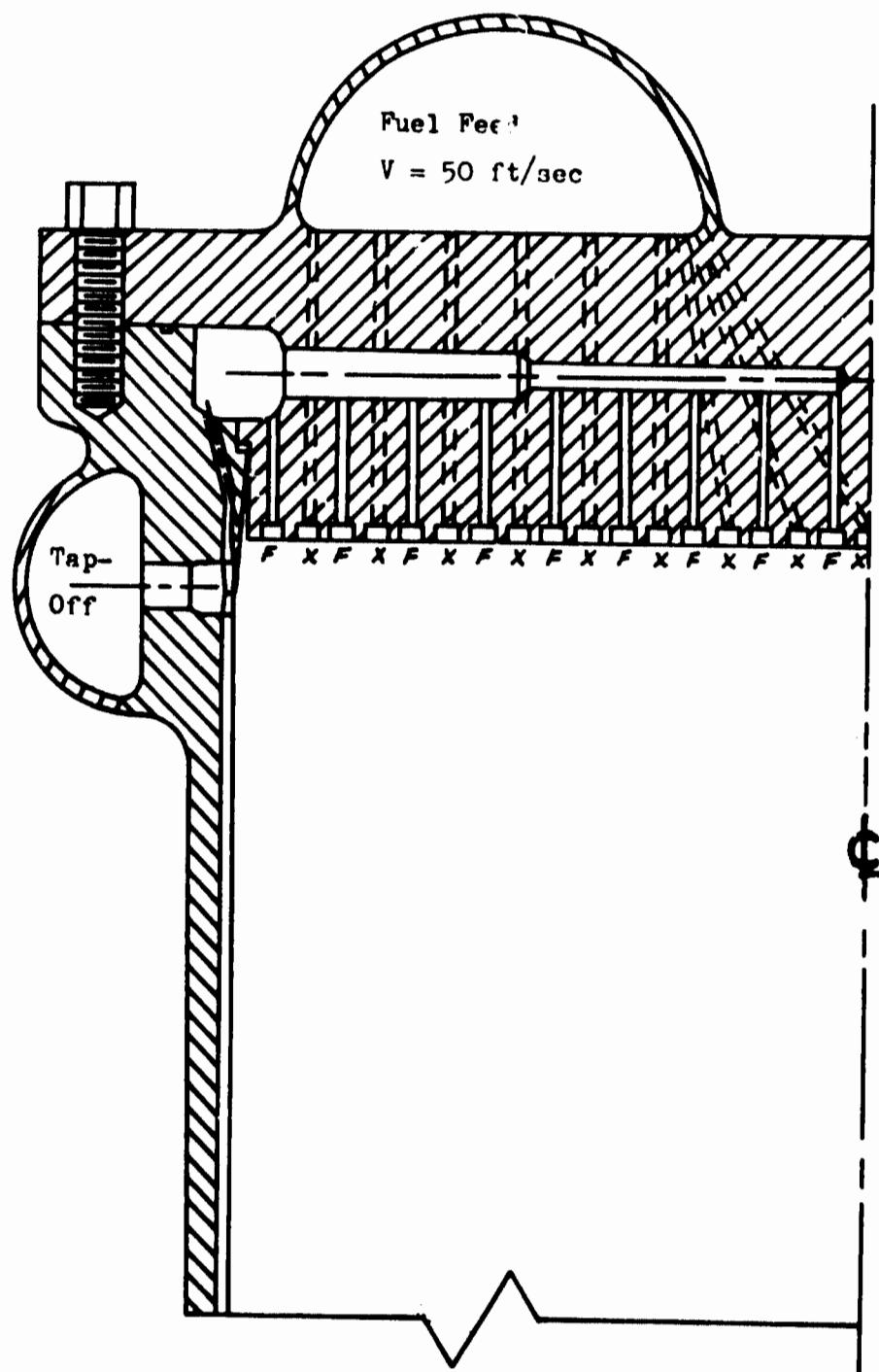


Fig. 173. Up Pass Flow Path Injector

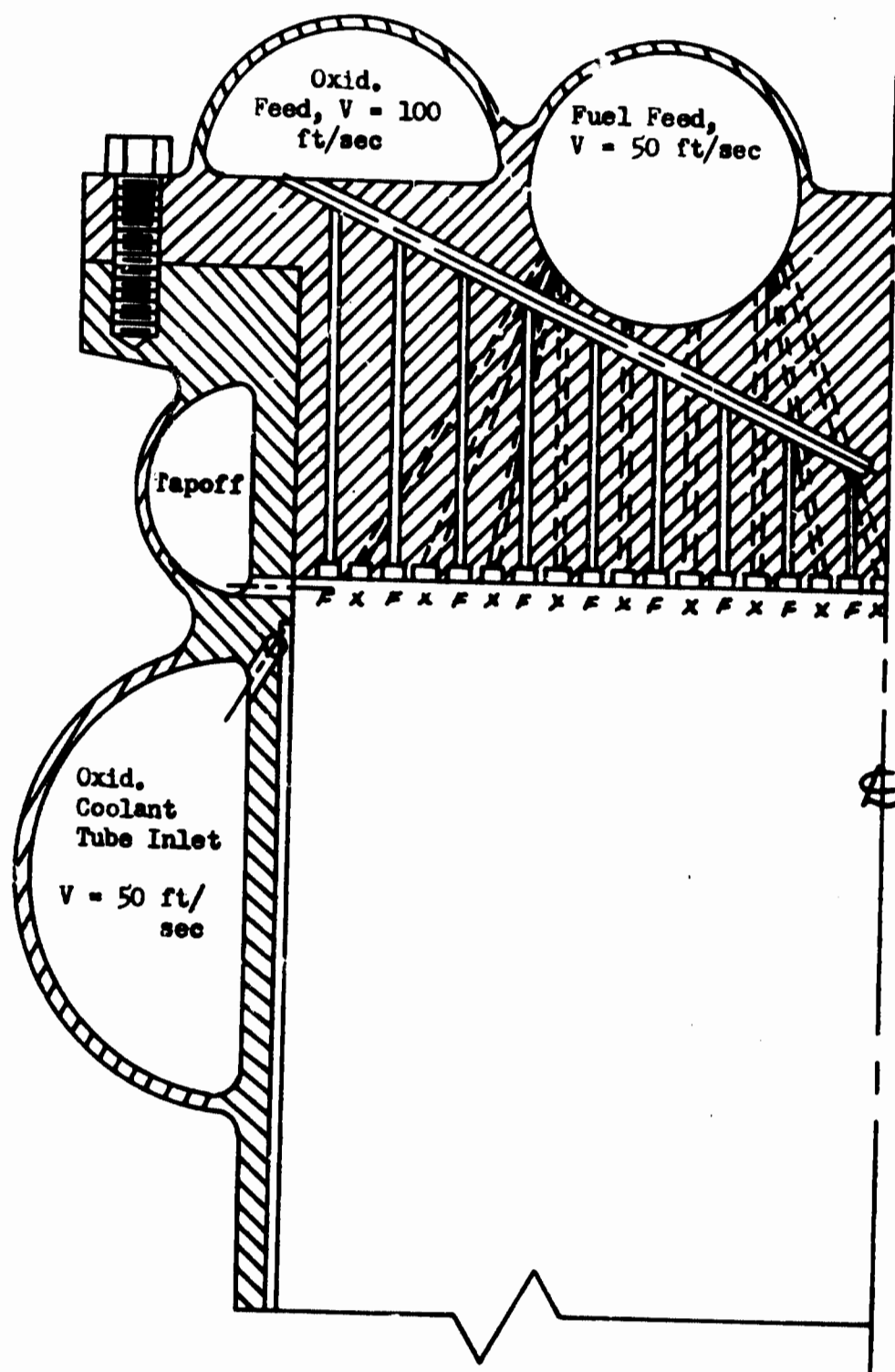
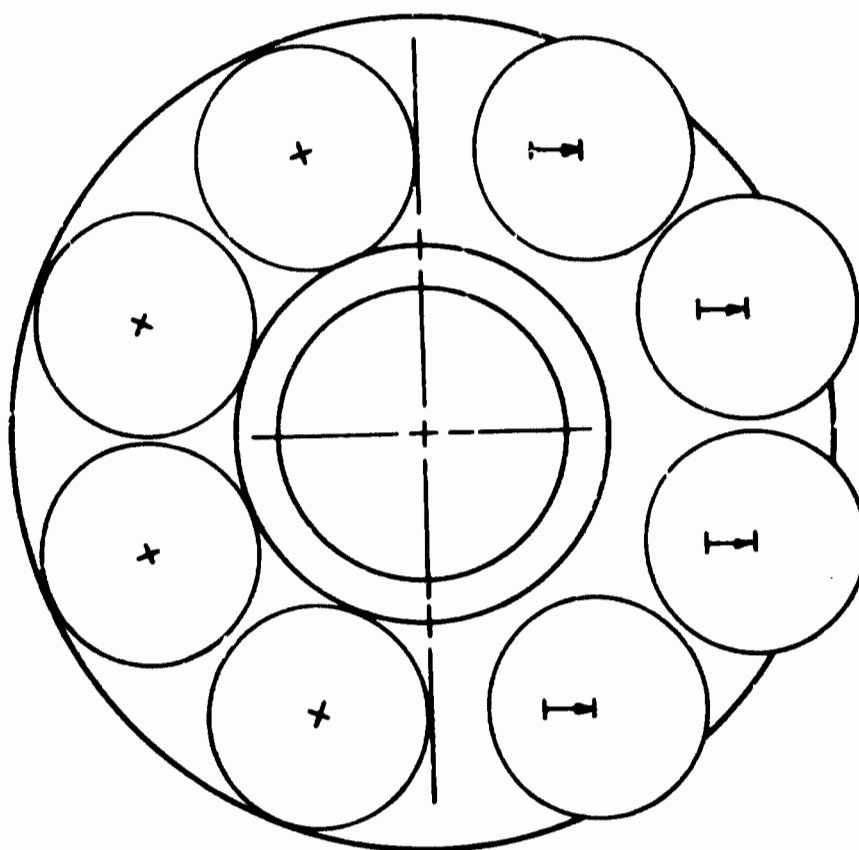


Fig. 174 Single Down Pass Flow Path Injector

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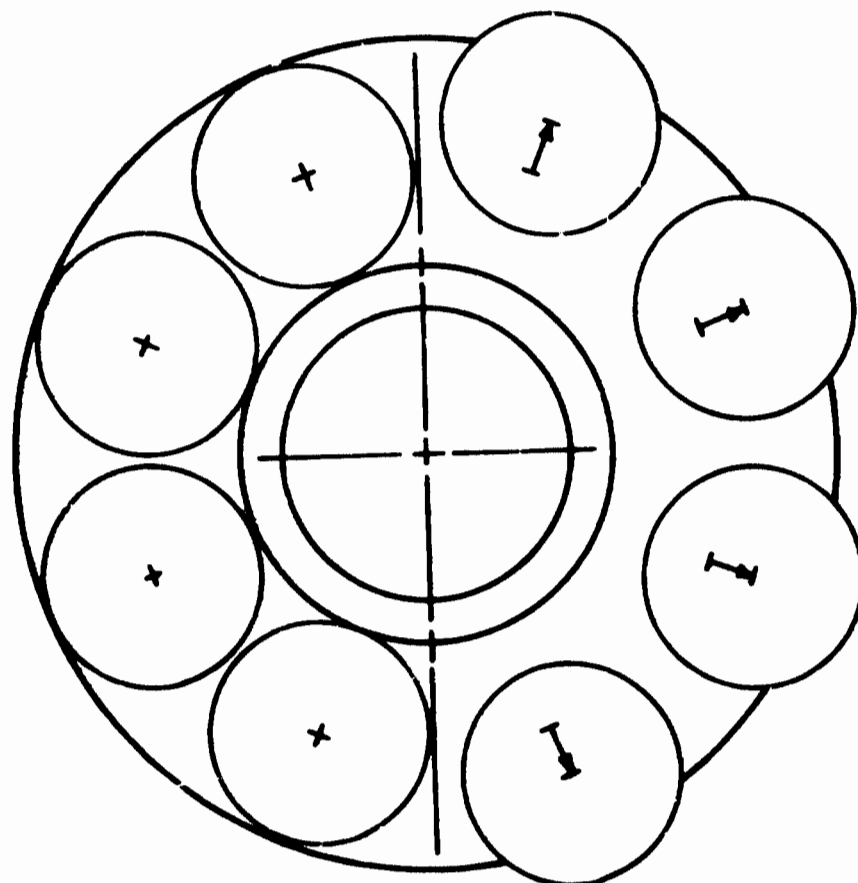
Thrust vector control requirements are satisfied by side injection of liquid N_2O_4 in the 2000K systems shown. Mechanical gimbaling by conventional and cam ring gimbals was considered for the toroidal configuration. A high weight was computed for a conventional point gimbal at this large diameter. The cam ring gimbal was found to be somewhat lighter, but required two 2870 horsepower gas turbines (comparable to the output of an extra turbopump) to actuate the rings tangentially. Combustor and spike nozzle segment rotation requires hot gas seals and propellant transfer bellows. It was concluded that mechanical TVC methods were competitive if a 6 degree displacement were used over a large fraction of the burning time, but if the time averaged requirement was closer to 1-1½ degrees, as was expected, side fluid injection would be more feasible.

The hinging or gimbaling of modules was also investigated in connection with the 2000K multichamber configuration, but side liquid injection was selected for the engine layout. Major areas where gimbaling of multichamber bell chambers differs from gimbaling of bell clusters include increased complexity of intermodular bleed baffling and the module/common expansion spike coolant transition. In the fixed module configuration, intermodular bleed gas (if required) can be contained between a common outboard shroud, the spike/centerbody thrust structure, forward baffles around each chamber fitting with omega joints to accept the oxidizer turbine exhaust ducts, and the outside of the chamber nozzles, as shown. If these chambers were made movable, the outboard shroud must be segmented, and the gas ducts must either be placed asymmetrically or gas must be ducted from both turbopumps. If four chambers were hinged radially (Fig. 175a) to produce a side force equivalent to a 6-degree gimbal of the entire engine, each



(b) MANEUVER:
Yaw About Vertical
Axis By Module Gimballing
(2 Plane) $\Delta\theta = 15$ Degrees
For 6 Degrees Equivalent
Gimbal

Roll Mode
Possible



(a) MANEUVER:
Yaw About Vertical
Axis By Module
Hinging (1 Plane)
 $\Delta\theta = 20$ Degrees For
6 Degrees Equivalent
Gimbal

No Roll Mode
Possible

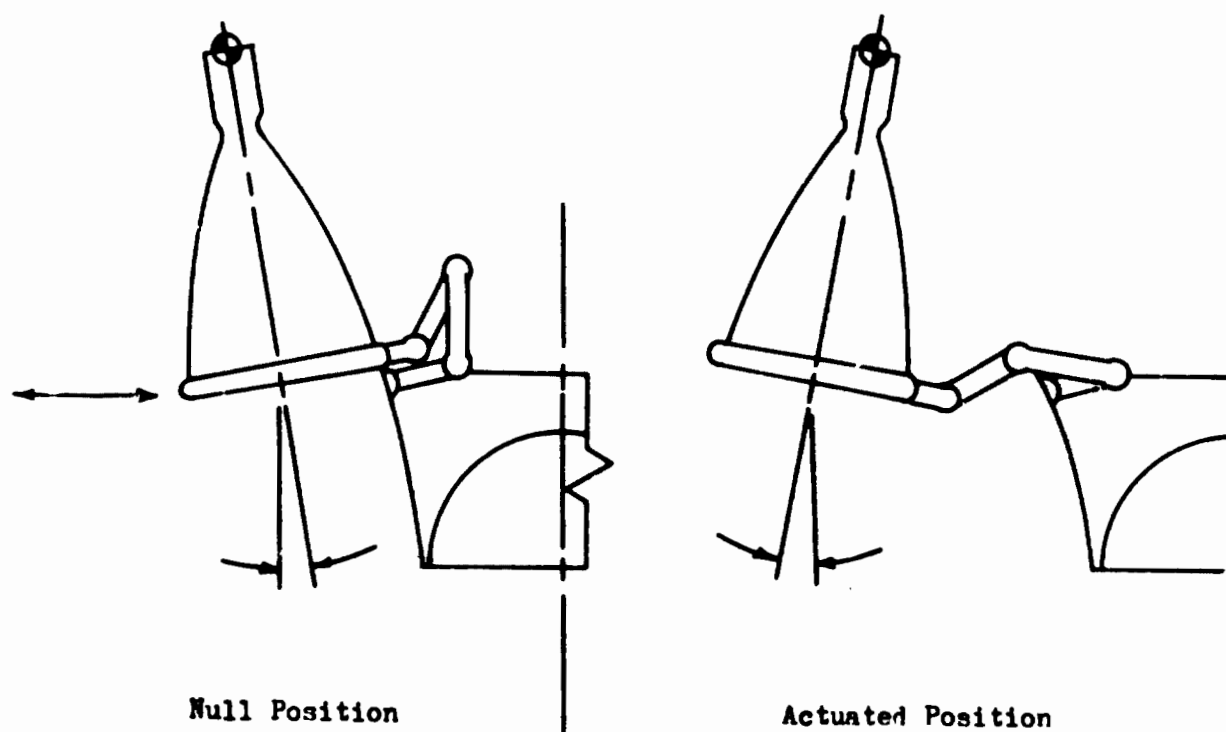
Fig. 175 Multichamber Thrust Vector Control By Module Displacement

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chamber would have to be rotated outward from its nominal position of $\beta = +9$ degrees to $\beta = -11$ degrees, a total travel of 20 degrees. This rotation corresponds to a linear translation of 32 inches at the module exit plane. If four chambers were gimbaled in the direction of desired boattail motion (Fig. 175b) to produce an equivalent 6 degree gimbal side force, each chamber would have to be rotated 15 degrees from the $\beta = +9$ degree position. This corresponds to a translation of 26 inches at the module exit plane. The ducting used to transfer coolant across the moduled spike transition must absorb these translations. Bellows with the necessary elastic deflection would be very long. Another device for this span would be an arrangement of three swivel joints (Fig. 176). It would also be possible to employ ablative cooling on the common spike in multichamber combustors with gimbaled modules.

The transmission of thrust components from the 2000K multichamber expansion spike and centerbody was accomplished through a honeycomb shell independent of the module thrust mounts. This shell also serves to exclude intermodular bleed gas from the engine compartment. The shell accepts the line load from the forward end of the spike transition manifold and transmits it to the tank bottom. Here it is assumed that baffling inside the tank transmits the load into the cylindrical vehicle shell. Moment resisting brackets, diffuse the distinct module thrust loads into the same vehicle shell.

(a) Swivel Jointed Coolant Transfer Line Adapted to Module Hinging



(b) Swivel Jointed Coolant Transfer Line Adapted To Module Gimballing

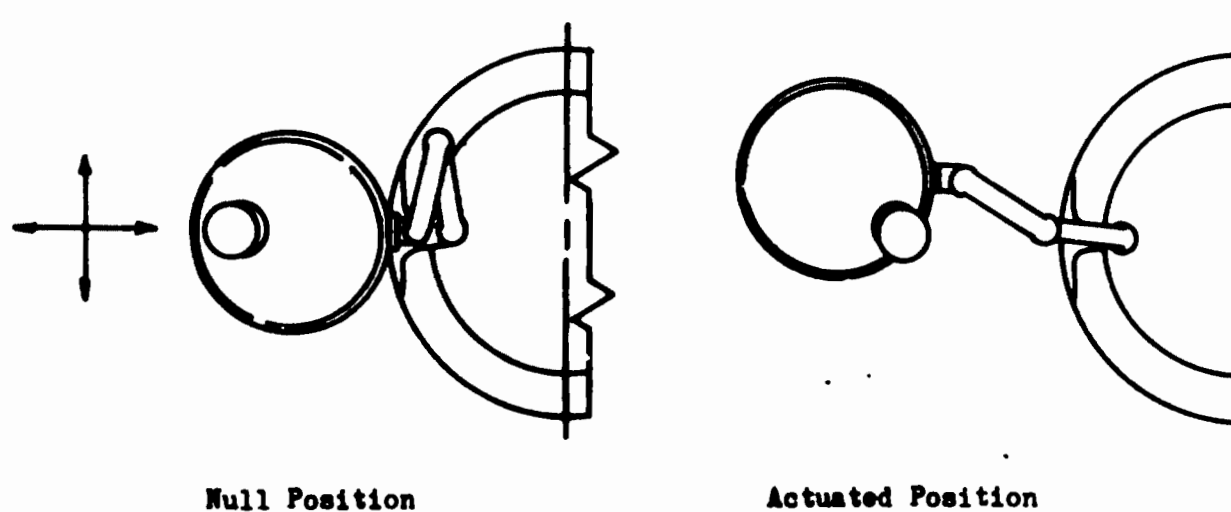


Fig. 176 Module/Spike Coolant Transfer For Multichamber Engine Mechanical Thrust Vector Control Systems

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CONCLUSIONS

The following major conclusions resulting from this study are summarized below. They are listed under headings of performance, weight, heat transfer, design, and general conclusions.

Performance

- (1) The performance of the continuous annular throat aerospike nozzle is at least comparable to and in many instances better than the 80 percent length bell nozzle at design pressure ratio. Aerospike performance is significantly better than the bell at low pressure ratios.
- (2) Performance of the continuous annular throat aerospike is approximately 1.5 percent greater than the best multichamber configuration at all pressure ratios.
- (3) Nozzle shrouds, sonic pins in the throat, and chamber baffles in toroidal chambers can be designed to influence nozzle efficiency by less than 1/2 percent.
- (4) No performance advantage can be gained by using a large number of multichamber modules. Eight touching chambers will perform as well as any larger number.
- (5) Tests with elongated module exit shapes showed no performance advantage over circular exit modules.
- (6) Intermodule bleed may provide a promising method of disposing of turbine exhaust gases provided the region between chambers is isolated from ambient pressure.

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Weight

- (1) The toroidal aerospike configuration was generally lighter in weight than the lightest multichamber configuration and the single bell engine at the 2,000,000 pound thrust level and over a wide range of chamber pressure and area ratio.
- (2) The eight touching multichamber configuration was considerably lighter than a sixteen module configuration at the 2,000,000 pound thrust level.
- (3) Elongated module exit chambers will be several times heavier than circular exit configurations, the difference in weight becoming greater as the exit shape a/b ratio increases.

Heat Transfer

- (1) Regenerative cooling of multichamber configurations becomes more difficult as the number of modules increases. The selection of number of modules for a given application could well be influenced by coolant pressure drop requirements.
- (2) Regenerative cooling requirements for continuous throat toroidal configurations are approximately the same as for a sixteen module multichamber configuration.
- (3) The use of N_2O_4 as a coolant at supercritical pressure may well be preferable to using UDMH- N_2H_4 (50-50) even when chamber pressure is considerably below the critical pressure of N_2O_4 .

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Design

- (1) From the standpoint of design complexity, the multichamber combustor appears to require more complex thrust structure than the toroidal configurations.
- (2) Use of tangential tapered manifolds in plumbing together multichamber modules, as opposed to point-to-point plumbing, results in a much cleaner design.
- (3) Splayed exit multichamber configurations are difficult to fabricate. The long length and high tilt angle associated with this combustor results in a considerably larger engine envelope compared to other aerospike configurations.
- (4) Considerations of development cost savings through sub-scale testing (segmentation) are not as stringent at thrusts near 40K as at higher thrust levels. Testing would probably proceed from heat transfer and injector evaluation with truncated multichamber modules or toroidal test segments directly to full thrust chamber testing under simulated altitude conditions.

At higher thrust levels, the development cost savings obtainable from sub-scale testing become increasingly significant. Unless multichamber engines of very great N are considered (pressure drop and simplicity goals point to N as low as performance will permit) toroidal combustors can always be segmented to lower test thrust levels than multichambers.

- (5) Static and dynamic envelope lengths for single bell engines are significantly greater than those for either toroidal or multichamber aerospikes. Differentiation between overall lengths of

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toroidal and multichamber aerospike engines requires knowledge of module number of the latter and optimum expansion nozzle lengths of each.

- (6) The continuous nature of the toroidal combustion chamber spike nozzle surface eliminates a class of design problems associated with the discontinuity of multichamber combustors at the module/spike nozzle interface. Regenerative coolant transmission across this interface in the nominal circular exit module-common axisymmetric spike configuration requires a collection manifold around each module exit, a transfer duct, and a distribution manifold around the spike.

General

Based on the combination of factors considered the following conclusions are made.

- (1) The toroidal aerospike configuration is superior to the multichamber configuration for an annular aerodynamic spike nozzle based on performance, weight, cooling considerations, and design considerations. A multichamber configuration would perhaps be preferable if an engine system were needed which could utilize existing hardware.
- (2) Consideration of performance, weight, cooling capability, and design complexity leads to the conclusion that multichamber configurations should be of conventional circular touching exit design. An eight module configuration is superior to configurations with a greater number of modules in all criteria considered in this study. A good criteria for selecting the number of modules for a booster engine is to use the fewest number (down to eight) which will provide near touching circular exits and a non-separated module flow.

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NOMENCLATURE

a	Speed of sound
A	Area
a^*	Speed of sound at $M = 1$
A^*	Aerodynamic throat area
A_b	Aerospike base area
A_e	Nozzle exit area
A_t	Primary throat area
a_t	Module throat area
C^*	Characteristic velocity
C_D	Nozzle discharge coefficient
C_F	Thrust coefficient of performance, $F/P_c A_t$
C_{Fb}	Base thrust coefficient
C_{Fdrag}	Thrust coefficient loss from drag
C_{Fint}	Primary nozzle thrust coefficient
C_{Fopt}	Maximum C_F referenced to pressure ratio
C_{Fp}	Primary nozzle thrust coefficient
C_{Fpi}	Ideal thrust coefficient based on primary fluid properties
C_p	Heat capacity at constant pressure
C_T	Nozzle Efficiency
d	Toroidal tube diameter in the throat region
D	Toroidal tube diameter in the chamber region
D_{CL}	Multichamber envelope diameter
D_e	Module exit diameter
f	Weight flow function, $\dot{W} \sqrt{T_o} / P_o A_t$
F	Thrust
F_b	Thrust contribution from aerospike base

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F_{int}, F_p	Primary nozzle thrust
F_{opt}, F_{pi}	Ideal thrust based on primary fluid properties and pressure ratio
g_c	Dimensional constant, $32.174 \text{ ft-lb}_m/\text{lb}_f\text{-sec}^2$
G	Mass velocity
g	32.2 ft/sec^2
H, h	Enthalpy
h_c	Coolant-side film heat transfer coefficient
h_g	Gas-side film heat transfer coefficient
I_s	Specific impulse
I_{spi}	Ideal specific impulse based on primary fluid properties and pressure ratio
J	Conversion factor, $778.26 \text{ ft-lb}_f/\text{Btu}$
K	1000 pounds thrust
K_1	Empirical base pressure factor
k	Thermal conductivity
L^*	Characteristic length
L_m	Projected axial length from module throat to module exit
L_N	Total nozzle axial length from throat
L_p	Length of multichamber plug from module exit to plug exit
$\dot{m}$	Mass flow
M	Mach number
M_{es}	Mach number of secondary fluid at base exit plane
N	Number of modules per cluster
P	Pressure
P_a	Ambient pressure
P_b	Base pressure
P_c	Primary chamber pressure

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P_{cowl}	Average pressure acting on nozzle cowl
P_{max}	Maximum pressure in recompression region
P_r	Pressure at the flow reattachment point
P_w	Primary nozzle wall pressure
P.R.	Pressure ratio, P_c/P_a
$q, Q/A$	Heat flux
$\bar{R}$	Universal gas constant
R^*	Equivalent aerodynamic throat radius, $\sqrt{A^*/\pi}$
R_B	Base radius at nozzle exit
R_c	Toroidal combustion chamber radius
R_t	Equivalent geometrical throat radius, $\sqrt{A_t/\pi}$
S	Entropy
s	Length
T	Temperature
T^*	Temperature at $M = 1$
T_{AW}	Adiabatic wall temperature
T_B	Coolant bulk temperature
T_{WC}	Coolant-side wall temperature
T_{WG}	Gas-side wall temperature
T_p	Primary gas total temperature
T_x	Reference temperature
T_∞	Free stream temperature
V, v	Velocity
V_∞	Free stream velocity
$\dot{w}_p$	Primary fluid flowrate
$\dot{w}_s$	Secondary fluid flowrate
X	Axial distance along sting from nozzle exit plane
x	Wall thickness

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GREEK SYMBOLS

α	Shroud half angle measured from shroud tilt angle β
β	Shroud tilt angle
γ	Ratio of specific heats
δ	Gap between modules or toroidal tubes
ϵ ϵ ϵ	Nozzle area ratio
ϵ_b	Base area ratio
ϵ_c	Module contraction ratio
ϵ_{CL}	Multichamber geometric area ratio
ϵ_{CL}^*	Multichamber geometric area ratio referenced to A^*
ϵ_{cowl}	Cowl area ratio
ϵ_M	Module area ratio
ϵ^*	Nozzle area ratio referenced to A^*
ϵ_{total}	Nozzle area ratio including cowl and base areas
θ_c	Module contraction half angle
θ_T	Module tilt angle
μ	Viscosity
μ_∞	Free stream viscosity
ρ	Density
ρ_∞	Free stream density
ρ^*	Density at $M = 1$
ϕ	Heat transfer enhancement factor from curvature effects
Φ	Heat transfer enhancement factor from chemical dissociation

SUBSCRIPTS

a	Ambient conditions
b	Base

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c	Chamber conditions
e	Exit conditions
i.s.	Intersegmental (between modules)
M	Individual module
Mod	Model
o	Stagnation conditions
p	Primary flow
s	Secondary flow
v	Venturi flowmeter
w	Wall
∞	Free stream conditions

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APPENDIX 1

METHOD OF ANALYSIS OF HIGH-AREA-RATIO COLD-FLOW DATA

C_T was defined in the first quarterly progress report as follows:

$$C_T = \frac{I_s}{I_{spi}} = \frac{F_p + F_b}{(1 + \frac{\dot{w}_s}{\dot{w}_p}) F_{pi}}$$

where I_s = the actual specific impulse
 F_b = the base thrust, $\int P_b dA_b$
 F_p = the net primary thrust
 I_{spi} = ideal specific impulse based on primary fluid properties
 F_{pi} = ideal thrust for $\dot{w}_p$ weight flowrate and properties

Substituting the relationships $F_m = F_p + F_b$ and $C_{Fopt} = \frac{F_{pi}}{P_c A_t^*}$,

where F_m = total measured net thrust
 A_t^* = primary aerodynamic throat area

and rearranging terms results in

$$C_T = \frac{F_m}{(1 + \frac{\dot{w}_s}{\dot{w}_p}) C_{Fopt} P_c A_t^*}$$

A flow function (f_p) was calculated using one dimensional, isentropic, compressible flow theory for critical flow (Ref 6). This function,

$$f_p = \frac{\dot{w}_p \sqrt{T_p}}{P_c A_t^*}, \text{ includes real gas effects for the gas at the nozzle}$$

throat. Thus:

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$$C_T = \frac{F_m}{(1 + \frac{\dot{w}_s}{\dot{w}_n}) C_{F_{opt}} \frac{\dot{w}_p \sqrt{T_p}}{f_p}} = \frac{F_m f_F}{C_{F_{opt}} \dot{w}_T \sqrt{T_p}}$$

The factors F_m and T_p were measured directly; the factors f_p , $\dot{w}_T$ and $C_{F_{opt}}$ are obtained using measured data and gas properties.

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APPENDIX 2

HIGH-AREA-RATIO TEST DATA

Test Number	Chamber Pressure, psia	F _{tot.l.} , pounds	F _{covl.} , pounds	P _{base} , psia	v _p , lb/sec	v _s v _p , percent	P _c /P _a	C _T total	C _T without covl
Contoured Model, Open Base $\epsilon = 147.5$									
5	932.7	140.5	0.25	0.114	0.8418		10327	97.81	97.64
7	936.4	141.1	0.28	0.112	0.8430		12687	97.86	97.67
8	922.2	138.4	0.28	0.100	0.8359		12799	97.46	97.26
9	924.0	138.9	0.27	0.096	0.8281		11737	97.93	97.74
10	928.8	140.0	0.38	0.091	0.8275		69173	96.26	97.99
12	932.7	141.9	0.38	0.114	0.8373		68634	98.67	98.41
13	918.0	139.5	0.38	0.108	0.8208		66217	98.46	98.19
14	930.5	144.5	0.38	0.412	0.8364	1.40	68747	98.88	98.62
15	932.0	144.0	0.38	0.340	0.8381	1.03	71782	98.56	98.30
16	926.2	148.3	0.38	No Data	0.8348	5.10	66805	97.98	97.55
17	928.2	146.4	0.38	0.700	0.8361	3.30	79125	98.29	98.03
18	928.8	147.8	0.38	0.888	0.8406	4.25	72575	98.41	98.16
21	919.6	123.9	-0.15	2.786	0.8273		317	91.08	91.19
22	937.0	126.1	-0.15	2.749	0.8430		312	90.95	91.06
23	930.7	117.2	-0.17	5.559	0.8401		157	86.45	86.58
25	906.9	114.6	-0.17	5.817	0.8224		164	86.76	86.89
27	917.0	138.4	0.24	0.124	0.8297		9552	98.24	96.07
29	920.6	130.6	-0.08	No Data	0.8312		936	94.34	94.40
30	920.3	132.8	-0.12	0.126	0.8311		2024	95.08	95.17
31	920.8	136.2	0.11	0.112	0.8313		4142	96.91	96.83
32	921.3	133.3	0	0.128	0.8325		2169	95.35	95.35
33	936.1	140.8	0.07	0.358	0.8394	1.1:	3316	97.37	97.33
34	937.8	142.1	-0.02	0.415	0.8435	3.05	1837	56.65	96.66
35	934.9	146.2	0.11	0.855	0.8401	4.43	4213	97.88	97.81

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APPENDIX 2 (CONT.)

Test Number	Chamber Pressure, psia	F total, pounds	F cowl, pounds	P base, psia	W p lb/sec	W s p, percent	P c / P a	C T total	C T without cowl
36	944.2	141.9	0.11	1.095	0.8475	4.72	1124	95.11	95.03
37	940.1	144.0	-0.17	0.918	0.8556	4.75	1733	96.06	96.17
38	933.1	143.7	0.06	0.973	0.8395	4.75	3036	96.69	96.65
39	932.4	141.9	-0.03	1.059	0.8411	4.74	1816	95.91	95.93
40	930.4	142.1	0.25	0.319	0.8322	1.06	9935	99.00	98.83
41	926.0	117.0	-0.24	No Data	0.8344	0	178	87.10	87.28
42	922.1	117.5	-0.24	No Data	0.8363	0	177	87.60	87.78
44	749.7	111.4	0.28	0.065	0.6671	0	12,432	97.93	97.68
Contoured Model, Radial-Inward Secondary Flow Injection (Large Gap), $\epsilon = 147.5$									
45	929.7	141.2	0.38	0.106	0.8363	0	69,836	98.42	98.16
46	939.8	145.2	0.38	0.298	0.8455	1.50	58,315	98.75	98.49
Contoured Model, Radial-Inward Secondary Flow Injection (Large Gap), $\epsilon = 156.8$									
47	943.0	135.6	0.38	No Data	0.8036	0	58,000	98.24	97.96
48	956.0	137.8	0.38	No Data	0.8132	0	58,000	98.61	98.34
51	906.4	131.6	0.38	0.281	0.7634	1.72	52,798	98.46	98.18
52	920.1	133.4	0.38	0.276	0.7745	1.39	58,103	98.48	98.20
53	916.5	134.5	0.38	0.339	0.7725	2.73	49,143	98.29	98.02
Contoured Model, Radial-Inward Secondary Flow Injection (Small Gap), $\epsilon = 156.8$									
54	912.0	132.8	0.38	0.211	0.7710	2.04	55,141	98.05	97.77

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APPENDIX 2 (CONT.)

Test Number	P _c psia	F _{total} , pounds	F _{cowl} , pounds	P _{base} , psia	$\dot{w}_p$ lb/sec	$\dot{w}_s/\dot{w}_p$, percent	P _c /P _a	C _T total	C _T without cowl
Contoured Model, Open Base Cavity, $\epsilon = 156.8$									
55	911.25	130.3	0.38	0.077	0.7650	0.0	66,400	98.24	97.95
Contoured Model, 1/4 inch Instrumented Sting in Wake, $\epsilon = 156.8$									
56	911.68	130.3	0.38	0.079	0.7660	0.0	52,873	98.23	97.94
58	920.41	137.5	0.38	0.905	0.7762	4.79	61,938	97.95	97.68
59	913.52	136.7	0.38	0.753	0.7698	4.83	60,077	98.27	98.00
Contoured Model, Radial Outward Secondary Flow Injection, $\epsilon = 156.8$									
60	908.22	133.4	0.38	No Data	0.7695	2.05	53,634	98.64	98.36
61	911.87	130.7	0.38	0.097	0.7681	0.0	56,141	98.55	98.26
62	912.99	133.7	0.37	0.324	0.7719	1.66	44,031	98.66	98.39
Conical Model, Open Base Cavity, $\epsilon = 129.9$									
65	898.74	157.9	0.15	0.589	0.9557	0.0	52,769	95.09	95.00
66	890.69	161.6	No Data	1.066	0.9495	2.03	48,273	96.18	95.88
67	Dynamic Test								
68	Dynamic Test								
69	885.34	164.3	0.42	1.216	0.9505	3.08	60,857	96.05	95.80
70	886.28	162.0	0.41	0.992	0.9513	1.61	52,037	96.14	95.90
71	893.83	162.7	0.40	0.975	0.9606	1.46	52,480	95.91	95.67

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APPENDIX 2 (CONT.)

Test Number	P _C psia	F _{total} , pounds	F _{cowl} , pounds	P _{base} , psia	$\dot{w}_p$ lb/sec	$\dot{w}_s/\dot{w}_p$ percent	P _C /P _a	C _T total	C _T without cowl
Conical Model, 1/4 inch Instrumented Sting, $\epsilon = 129.9$									
73	897.72	157.7	0.13	0.636	0.9591	0	55,137	94.95	94.87
74	897.93	157.9	0.14	0.635	0.9616	0	51,773	95.03	94.95
75	891.66	156.8	0.14	0.631	0.9528	0	50,384	95.15	95.06
76	894.19	157.3	0.09	0.640	0.9533	0	52,632	95.29	95.23
77	894.14	166.5	0.51	1.460	0.9569	4.47	47,664	96.45	96.16
Conical Model, 0.049 Inch Plain Sting, $\epsilon = 129.9$									
78	887.67	156.4	0.06	0.607	0.9507	0	50,158	95.31	95.27
Conical Model, Open Base Cavity, $\epsilon = 129.9$									
79	Dynamic Test								
80	Dynamic Test								

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APPENDIX 3 COLD-FLOW TEST DATA

Test Number	Chamber Pressure psia	P _{total} pounds	P _{base} psia	P _{1.s.} psia	$\dot{V}_P$ lb/sec	$\dot{V}_0/\dot{V}_P$ percent	$\dot{V}_{1.s.}/\dot{V}_P$ percent	P/P _a	C _T total
Model I-3, Scaled Hot Firing Model, $\epsilon_0^* = 24.54$, Air, Open Base									
22	150.2	144.7	0.885	-	2.102	0	-	527.0	0.9663
23	150.5	145.0	0.887	-	2.105	0	-	537.5	0.9653
24	150.5	145.1	0.889	-	2.104	0	-	524.1	0.9653
25	151.2	136.1	-	-	2.118	0	-	126.0	0.9532
26	150.6	136.0	1.440	-	2.115	0	-	126.1	0.9550
27	150.5	136.9	1.128	-	2.116	0	-	153.9	0.9516
29	150.2	138.1	0.892	-	2.111	0	-	201.6	0.9523
30	149.8	144.2	0.884	-	2.094	0	-	531.2	0.9655
31	149.5	140.8	0.885	-	2.102	0	-	300.3	0.9605
32	150.6	145.3	0.894	-	2.114	0	-	551.6	0.9650
34	150.8	134.1	1.860	-	2.147	0	-	100.6	0.9536
39	150.6	145.0	0.892	-	2.142	0	-	530.9	0.9600
40	150.6	145.2	0.902	-	2.142	0	-	545.7	0.9623
44	150.9	138.0	0.973	-	2.200	0	-	173.0	0.9494
45	150.8	129.3	3.283	-	2.222	0	-	60.4	0.9438
46	151.4	130.2	3.302	-	2.194	0	-	60.8	0.9442
47	151.3	124.8	5.382	-	2.217	0	-	35.5	0.9409
52	149.9	123.6	5.334	-	2.195	0	-	35.2	0.9388
53	150.4	115.9	7.361	-	2.194	0	-	19.8	0.9272
54	150.7	145.4	0.909	-	2.172	0	-	540.9	0.9634

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	P _{total} pounds	P _{base} psia	P _{i.s.} psia	$\dot{W}_P$ lb/sec	$\dot{W}_g/\dot{W}_P$ percent	$\dot{W}_{i.s.}/\dot{W}_P$ percent	P/P _c ₂	C _T total
Model I-3, Scaled Hot Firing Model, $\epsilon_o^* = 24.54$, Air, Open Base									
22	100.5	95.0	0.601	-	1.412	0	-	298.8	0.9621
24	100.4	92.8	0.600	-	1.413	0	-	206.8	0.9541
25	50.2	48.3	0.287	-	0.702	0	-	497.0	0.9654
55	150.0	148.2	1.314	-	2.193	0.983	-	509.1	0.9725
63	149.7	124.8	5.515	-	2.145	0.976	-	35.2	0.9414
67	150.4	149.1	1.438	-	2.161	1.512	-	539.8	0.9760
59	151.0	150.3	1.552	-	2.123	2.013	-	535.1	0.9750
60	151.0	143.1	1.778	-	2.140	2.010	-	170.9	0.9642
64	148.8	125.2	5.626	-	2.142	2.027	-	35.2	0.9418
66	150.4	149.8	1.590	-	2.159	2.009	-	537.0	0.9760
56	150.8	151.1	1.724	-	2.192	3.013	-	539.1	0.9723
57	150.0	151.3	1.724	-	2.200	3.022	-	523.2	0.9714
61	151.2	143.9	1.917	-	2.136	2.648	-	169.1	0.9645
65	148.0	125.8	5.749	-	2.141	3.072	-	35.0	0.9390
62	151.2	146.3	2.621	-	2.128	5.021	-	166.8	0.9593

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	P _{total} pounds	P _{base} psia	P _{i.s.} psia	$\dot{W}_p$ lb/sec	$\dot{W}_b/\dot{W}_p$ percent	$\dot{W}_{i.s.}/\dot{W}_p$ percent	P/P _a	C _T total
Model I-1, Scaled Hot Firing Model, $\epsilon_o^* = 24.54$, Air, Radial-Inward Base									
71	150.7	149.1	1.395	-	2.165	1.701	-	535.7	0.9708
72	150.4	142.9	1.545	-	2.177	3.098	-	168.9	0.9575
73	150.4	142.9	1.480	-	2.189	3.098	-	168.7	0.9574
74	150.8	126.2	5.873	-	2.180	1.511	-	35.5	0.9408
75	150.7	126.5	5.369	-	2.184	1.507	-	35.4	0.9414
Model I-2, Scaled Hot Firing Model, $\epsilon_o^* = 24.54$, Air, Radial-Outward Base									
76	150.7	126.6	5.392	-	2.169	1.511	-	35.2	0.9435
77	150.6	126.5	5.684	-	2.179	1.511	-	35.2	0.9474
78	151.0	144.4	2.181	-	2.193	3.050	-	170.6	0.9644
79	150.7	144.3	2.171	-	2.186	3.059	-	169.4	0.9656
80	150.9	149.8	1.519	-	2.193	1.728	-	539.9	0.9741

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	F _{total} pounds	P _{base} psia	P _{i.s.} psia	$\dot{W}_p$ lb/sec	$\dot{W}_s/\dot{W}_p$ percent	$\dot{W}_{i.s.}/\dot{W}_p$ percent	P/P _a	C _T total
Model I-4, Scaled Hot Firing Model, $\epsilon_o^* = 24.54$, Air, Supersonic Base, $\epsilon = 3.5$									
83	150.2	147.7	0.809	-	2.125	2.296	-	535.5	0.9589
84	151.0	148.2	0.813	-	2.128	2.254	-	527.4	0.9574
85	151.2	142.2	0.848	-	2.131	3.893	-	172.6	0.9407
86	150.6	126.4	5.342	-	2.140	2.015	-	35.5	0.9341
Model I-4, Scaled Hot Firing Model, $\epsilon_o^* = 24.54$, Air, Supersonic Base, $\epsilon = 15$									
87	150.2	126.2	5.410	-	2.132	2.024	-	35.3	0.9371
88	150.3	117.7	0.804	-	2.129	2.283	-	510.2	0.9580
Model I-5, Scaled Hot Firing Model, $\epsilon_o^* = 24.54$, Air, Porous Plate Base									
104	150.2	146.6	-	-	2.167	0.604	-	525.2	0.9687

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	P _{total} pounds	P _{base} psia	P _{i.s.} psia	$\dot{W}_F$ lb/sec	$\dot{W}_S/\dot{W}_P$ percent	$\dot{W}_{i.s.}/\dot{W}_P$ percent	P _c /P _a	C _m total
Model I-3, Scaled Hot Firing Model, $\epsilon_o^* = 24.26$, CP ₄ , Open Base									
42	150.0	150.9	1.002	-	3.721	0	-	255.4	condensation*
96	49.1	47.5	0.323	-	1.136	0	-	144.4	0.9464
98	99.4	101.1	0.654	-	2.365	0	-	287.2	0.9555
99	99.4	92.5	0.967	-	2.362	0	-	91.5	0.9412
100	99.2	88.9	2.091	-	2.342	0	-	54.3	0.9414
101	99.2	84.4	3.495	-	2.346	0	-	35.0	0.9319
102	49.9	51.9	0.535	-	1.163	1.733	-	275.4	0.9665
103	49.8	51.8	0.539	-	1.159	1.739	-	258.9	0.9676

*Because of the effects of two-phase flow, C_p was not calculated for test 42. P_b/P_c is 0.0067, 0.0066 and 0.0066 for tests 42, 96 and 98 respectively, indicating little or no effect on performance due to P_c or condensation.

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	P _{total} pounds	P _{base} psia	P _{i.s.} psia	$\dot{W}_p$ lb/sec	$\dot{W}_g/\dot{W}_p$ percent	$\dot{W}_{i.s.}/\dot{W}_p$ percent	P/P _c a	C ₀ total
Model II-6, Point Expansion, $\epsilon_0^* = 48.30$, Air, Ope Base									
106	150.4	154.3	0.204	-	2.203	0	-	1525.2	0.9848
107	151.2	154.5	0.199	-	2.197	0	-	1520.7	0.9859
108	149.4	151.8	0.210	-	2.204	0	-	1475.6	0.9867
110	150.8	154.0	0.203	-	2.182	0	-	1436.0	0.9855
111	149.5	152.3	0.209	-	2.200	0	-	1461.4	0.9853
112	148.5	143.4	0.471	-	2.152	0	-	298.4	0.9686
113	149.4	15.9	0.1	-	2.177	0	-	307.2	0.9736
115	150.2	147.6	0.232	-	2.192	0	-	472.1	0.9727
116	150.5	151.2	0.207	-	2.184	0	-	707.2	0.9820
117	150.4	135.0	1.177	-	2.200	0	-	100.4	0.9163
118	151.0	135.3	1.191	-	2.184	0	-	100.7	0.9111
119	151.4	138.9	0.234	-	2.159	0	-	100.5	0.9186
120	149.8	137.4	0.881	-	2.163	0	-	117.0	0.9180

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	P _{total} pounds	P _{base} psia	P _{fil.} psia	$\dot{W}_p$ lb/sec	$\frac{\dot{W}_p}{\dot{W}_p}$ percent	$\frac{\dot{W}_{fil.}}{\dot{W}_p}$ percent	P/p _o ps	C_m total
Model II-6, Point Expansion, $\epsilon_o^* = 48.30$, Air, Case Base									
121	150.0	139.2	1.102	-	2.156	0.697	-	149.2	0.9533
122	149.8	139.0	1.066	-	2.154	0.705	-	148.0	0.9510
123	149.2	138.5	1.064	-	2.150	0.710	-	147.8	0.9513
129	150.6	149.4	0.441	-	2.175	0.735	-	452.6	0.9783
132	151.4	157.1	0.401	-	2.188	0.952	-	1481.0	0.9977
125	148.4	139.4	1.253	-	2.137	1.490	-	146.8	0.9597
128	150.2	149.9	0.534	-	2.164	1.471	-	453.2	0.9775
133	148.6	154.8	0.464	-	2.147	1.927	-	1410.3	0.9839
134	150.7	156.9	0.499	-	2.183	1.902	-	1403.3	0.9838
126	151.5	144.5	1.443	-	2.184	2.914	-	150.1	0.9575
127	148.6	150.5	0.630	-	2.154	2.956	-	452.5	0.9744

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	P _{total} pounds	P _{base} psia	P _{i.s.} psia	$\dot{W}_p$ lb/sec	$\dot{W}_g/\dot{W}_p$ percent	$\dot{W}_{i.s.}/\dot{W}_p$ percent	P/P _c	C _T tqtal
Model III-7, Shrouded Nozzle, $\epsilon_o^* = 48.64$, Air, Open Base									
136	151.6	144.2	0.098	-	2.064	0	-	1491.1	0.9793
137	148.6	141.0	0.100	-	2.037	0	-	1381.9	0.9789
138	150.2	138.5	0.102	-	2.068	0	-	571.9	0.9712
140	149.4	123.8	1.065	-	2.039	0	-	99.5	0.9333
141	149.8	124.0	1.064	-	2.032	0	-	100.4	0.9330
142	149.5	123.8	1.068	-	2.028	0	-	99.1	0.9339
143	150.8	130.2	0.833	-	2.023	0	-	154.9	0.9515
144	150.6	130.2	0.835	-	2.031	0	-	153.6	0.9525
145	149.2	131.2	0.617	-	2.015	0	-	200.6	0.9593
146	149.4	131.4	0.630	-	2.013	0	-	199.1	0.9592
147	149.2	133.4	0.266	-	2.003	0	-	297.6	0.9613
148	148.8	131.9	0.398	-	2.004	0	-	248.2	0.9589
149	149.8	135.2	0.107	-	2.018	0	-	403.2	0.9608
150	149.9	138.0	0.100	-	2.027	0	-	538.9	0.9698
151	151.7	138.8	0.100	-	2.053	0	-	486.4	0.9684

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	P _{total} pounds	P _{inlet} psia	P _{is-c} psia	$\dot{W}_p$ lb/sec	$\dot{W}_g/\dot{W}_p$ percent	$\dot{W}_i/\dot{W}_p$ percent	P/p c/s	C _T total
Model III-7, Shrouded Nozzle, $\epsilon_c^* = 48.64$, Air, Open Base									
152	151.0	138.8	0.106	-	2.053	0	-	470.3	0.9600
153	151.2	134.2	0.309	-	2.051	0	-	278.2	0.9565
155	80.5	76.4	0.043	-	1.078	0	-	1355.0	0.9526
158	73.2	69.5	0.041	-	0.971	0	-	1114.6	0.9810
160	102.2	97.2	0.044	-	1.353	0	-	1510.0	0.9801
176	100.7	92.2	0.058	-	1.345	0	-	495.1	0.9704
173	100.9	95.9	0.054	-	1.354	0	-	1177.5	0.9793
174	102	97.7	0.052	-	1.369	0	-	1581.7	0.9813
175	100.8	93.2	0.053	-	1.318	0	-	607.0	0.9738
161	101.8	97.4	0.107	-	1.350	0.747	-	1173.9	0.9807
153	101.8	94.0	0.127	-	1.365	0.712	-	476.7	0.9713
168	100.6	87.5	0.14	-	1.355	0.752	-	150.8	0.9511
162	101.6	88.0	0.138	-	1.356	1.491	-	1493.5	0.9702
164	101.6	92.4	0.192	-	1.366	1.402	-	1117.1	0.9720
167	101.3	88.3	0.672	-	1.356	1.400	-	151.0	0.9546
156	100.6	91.2	0.207	-	1.353	3.007	-	1130.1	0.9579

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	F _{total} pounds	P _{base} psia	P _{i.s.} psia	$\dot{W}_p$ lb/sec	$\dot{W}_b/\dot{W}_p$ percent	$\dot{W}_{i.s.}/\dot{W}_p$ percent	P _c /P _a	ζ_T total
Model III-9, Eight Chamber Touching Multichamber, $\zeta_{CL}^* = 49.8$, No Extension									
239	100.2	96.7	0.080	0.072	1.384	0	0	1401.4	0.9684
231	99.8	84.8	0.532	0.604	1.389	0	0	148.40	0.9122
232	99.5	88.0	0.433	0.336	1.375	0	0	197.85	0.9385
233	99.8	90.0	0.378	0.397	1.384	0	0	237.51	0.9497
234	100.0	89.6	0.135	0.326	1.380	0	0	266.03	0.9416
235	100.0	94.1	0.105	0.168	1.381	0	0	554.02	0.9656
236	100.1	95.5	0.088	0.122	1.375	0	0	785.71	0.9671
237	100.3	96.1	0.036	0.101	1.381	0	0	994.05	0.9672
238	100.2	96.6	0.076	0.072	1.383	0	0	1408.29	0.9670
240	100.3	97.4	-	0.078	1.387	0.738	0	1402.80	0.9669
243	100.4	91.4	-	-	1.390	0.732	0	267.02	0.9478
245	100.8	85.9	-	0.587	1.394	0.764	0	153.03	0.9114
246	100.4	85.7	-	0.586	1.393	0.764	0	152.38	0.9111

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	P _{total} pounds	P _{stage} psia	P _{inlet} psia	Q _p lb/sec	W _s /W _p percent	W _{i.s.} /W _p percent	P/P _c	C _m total
Model III-9, Eight Chambers Touching Multichamber, $\epsilon_{CL}^* = 49.8$, No Extension									
241	100.5	98.0	-	0.087	1.395	1.494	0	1412.49	0.9611
242	100.4	91.7	-	0.356	1.391	1.500	0	267.82	0.9441
247	100.5	86.0	-	0.593	1.404	1.504	0	153.01	0.9045
Model III-9, Eight Chambers Touching Multichamber, $\epsilon_{CL}^* = 49.8$, No Extension, Engine Out									
257	98.3	82.4	0.073	0.067	1.190	0	0	1412.13	0.9690
258	98.1	82.3	0.066	0.066	1.177	0	0	1451.18	0.9601
263	98.3	73.1	0.632	0.640	1.108	0	0	147.96	0.9195
260	98.1	82.7	-	0.069	1.187	0.589	0	1466.59	0.9655
261	98.2	72.4	-	0.667	1.191	0.588	0	143.17	0.9067
Model III-8, Eight Chambers Touching Multichamber, $\epsilon_{CL}^* = 49.8$, No Center-body, No Shroud									
253	99.9	95.3	0.078	0.076	1.385	0	0	1411.81	0.9657
254	100.1	95.5	0.090	0.073	1.384	0	0	1407.48	0.9697
255	99.9	86.2	0.659	-	1.393	0	0	151.99	0.9068
256	100.0	86.1	0.661	0.658	1.395	0	0	151.65	0.9061

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	P _{total} pounds	P _{base} psia	P _{i.s.} psia	i _p lb/sec	i _g /i _p percent	i _g /i _p percent	P _o /P _a	C _m total
Model III-10, Eight Chambers Touching Multichamber C _{LI} = 49.8, 30° Length									
'80	100.1	97.0	-	-	1.402	0	0	1036.17	0.0629
'82	100.0	97.7	0.091	0.066	1.379	0	0	1500.15	0.0700
'83	100.4	97.0	0.072	0.059	1.367	0	0	1514.10	0.0698
'84	100.4	95.2	0.082	0.147	1.375	0	0	703.00	0.0695
'85	100.4	93.5	0.091	0.216	1.389	0	0	135.76	0.0610
'86	100.3	91.7	0.087	0.283	1.373	0	0	313.00	0.0529
'87	100.4	96.3	0.073	0.105	1.374	0	0	959.93	0.0686
'88	100.4	96.6	0.076	0.082	1.370	0	0	1008.62	0.0707
'89	99.8	94.3	0.096	0.165	1.364	0	0	614.01	0.0687
'90	99.5	88.3	0.472	0.472	1.383	0	0	203.12	0.0437
'91	99.7	88.3	0.453	0.453	1.385	0	0	203.75	0.0410
'92	99.9	85.1	0.575	0.574	1.388	0	0	150.88	0.0474

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	F _{total} pounds	P _{base} psia	P _{i.s.} psi	$\dot{W}_p$ lb/sec	$\dot{W}_g/\dot{W}_p$ percent	$\dot{W}_i/\dot{W}_p$ percent	P/P ₀	C _T total
Model III-10, Eight Chambers Touching Multichamber $\epsilon_{CL}^* = 49.8$, 30' Length									
193	100.0	89.8	0.102	0.349	1.404	0	0	268.60	0.9414
194	100.0	90.1	0.428	0.405	1.399	0	0	277.08	0.9514
221	101.2	97.6	-	0.067	1.378	0	0	1491.31	0.9675
196	100.9	99.0	0.005	0.031	1.402	0	0	7944.88	0.9585
197	101.0	98.4	0.090	0.040	1.403	0	0	3014.03	0.9660
205	100.9	97.6	-	0.070	1.396	0	0	1469.56	0.9707
198	101.2	98.5	0.094	0.067	1.403	0	0.259	2521.18	0.9688
199	101.2	98.6	0.087	0.189	1.407	0	1.133	1550.48	0.9608
206	101.2	98.2	-	0.139	1.409	0	0.707	1473.93	0.9503
211	100.2	90.1	0.093	0.348	1.399	0	0.712	273.70	0.9368

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	P _{base} psia	P _{i.s.} psia	$\dot{W}_P$ lb/sec	$\dot{W}_S/\dot{W}_P$ percent	$\dot{W}_{i.s.}/\dot{W}_P$ percent	P _c /P _a	C _T total
Model III-10, Eight Chambers Touching Multichamber $\epsilon_{CL}^* = 49.8$, 30% Length								
207	101.3	0.062	0.223	1.411	0	1.398	1498.30	0.9670
210	100.2	0.067	0.226	1.397	0	1.437	1007.14	0.9680
212	100.4	0.198	0.376	1.417	0	1.424	265.12	0.9345
213	100.2	0.093	0.361	1.406	0	1.435	273.40	0.9310
216	100.3	0.580	0.580	1.412	0	1.432	153.55	0.9077
208	101.6	0.085	0.365	1.414	0	2.877	1442.77	0.9667
209	100.0	0.084	0.362	1.395	0	2.906	1015.85	0.9651
214	100.4	0.337	0.415	1.410	0	2.866	273.79	0.9362
215	100.3	0.590	0.594	1.411	0	2.873	154.09	0.8976
218	100.8	-	0.680	1.390	0.729	0	1485.41	0.9694
219	101.2	-	0.663	1.383	0.725	0	1522.72	0.9664
223	100.8	-	0.358	1.377	0.728	0	1516.70	0.9045

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	P _{base} psia	P _{i.s.} psia	$\dot{V}_P$ lb/sec	$\dot{W}_g/\dot{W}_f$ percent	$\dot{W}_{i.s.}/\dot{W}_P$ percent	P/P _a	C _T total
Model III-10, Eight Chambers Touching Multichamber $\xi_{CL}^* = 49.8$, 30% Length								
226	99.8	-	0.574	1.392	0.732	0	150.24	0.9092
220	101.5	-	0.071	1.391	1.415	0	1503.48	0.2637
222	101.2	-	0.355	1.389	1.450	0	283.39	0.9450
227	101.0	-	0.581	1.398	1.492	0	151.56	0.9021
224	100.4	-	-	1.374	2.959	0	266.60	0.9368
225	99.8	-	0.358	1.384	2.982	0	265.09	0.9405

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	F _{total} pounds	P _{base} psia	P _{i.s.} psia	$\dot{W}_p$ lb/sec	$\dot{W}_g/\dot{W}_p$ percent	$\dot{W}_{i.s.}/\dot{W}_p$ percent	P _c /P _a	C _T total
Model III-11, Eight Chambers Spaced Multichamber, $\epsilon_{CL}^* = 50.4, 30\%$ Length									
266	100.6	83.79	1.046	0.977	1.376	0	0	101.24	0.9200
267	100.8	87.58	0.732	0.644	1.372	0	0	150.85	0.9411
268	100.6	89.53	0.543	0.492	1.375	0	0	202.04	0.9536
269	100.4	89.26	0.133	0.374	1.377	0	0	263.63	0.9416
270	100.6	94.17	0.085	0.136	1.377	0	0	748.62	0.9621
271	100.5	94.93	0.094	0.106	1.379	0	0	958.70	0.9621
272	100.7	95.79	0.096	0.067	1.384	0	0	1514.74	0.9591
273	101.0	95.83	0.100	0.067	1.386	0	0	1519.25	0.9597
274	100.9	95.89	0.098	0.068	1.390	0	0	1517.75	0.9614
275	101.0	96.27	0.097	0.030	1.394	0	0	2022.02	0.9591
276	101.0	93.20	0.087	0.191	1.404	0	0	530.35	0.9576
277	101.2	95.31	0.085	0.150	1.405	0	0.713	916.17	0.9567
278	101.2	95.84	0.072	0.180	1.402	0	1.424	938.95	0.9546
287	100.8	88.11	-	0.654	1.393	0.737	0	152.12	0.9406
280	101.2	96.67	-	0.107	1.402	1.506	0	940.17	0.9623
283	101.2	92.02	-	0.369	1.417	1.490	0	271.05	0.9510
285	101.0	88.59	-	-	1.387	1.511	0	153.33	0.9348
286	101.0	88.50	-	0.654	1.381	1.521	0	152.69	0.9370
281	101.2	97.29	-	0.108	1.402	2.627	0	919.16	0.9586
282	101.1	93.02	-	0.370	1.416	2.929	0	257.23	0.9497

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	F total pounds	P base psia	P i.s. psia	$\dot{W}_p$ lb/sec	$\dot{W}_g/\dot{W}_p$ percent	$\dot{W}_{i.s.}/\dot{W}_p$ percent	P/P _a	C _T total
Model III-12, Sixteen Chamber Touching Multichamber, $\zeta_{CL}^* = 51.4$, 30% Length									
292	101.4	80.10	1.116	0.739	1.353	0	0	101.99	0.8944
293	101.2	79.91	1.133	0.783	1.350	0	0	101.02	0.8944
294	101.1	83.63	0.709	0.560	1.350	0	0	150.83	0.9200
295	101.1	83.73	0.707	0.559	1.352	0	0	150.95	0.9210
296	101.1	86.43	0.522	0.443	1.352	0	0	202.49	0.9589
297	101.0	86.34	0.521	0.431	1.353	0	0	201.86	0.9384
299	101.1	89.42	0.095	-	1.357	0	0	410.66	0.9479
300	101.0	88.94	0.325	0.329	1.355	0	0	302.35	0.9522
301	100.8	88.76	0.089	0.261	1.342	0	0	375.91	0.9423
302	101.0	93.60	0.101	0.100	1.347	0	0	1047.83	0.9664
303	101.0	94.29	0.094	0.072	1.346	0	0	1492.98	0.9655
304	100.9	94.25	0.088	0.073	1.345	0	0	1483.82	0.9661
305	100.9	94.64	0.083	0.060	1.344	0	0	2013.17	0.9650
352	149.5	135.40	0.132	0.269	2.023	0	0	545.46	0.9617
353	149.5	131.49	0.118	0.393	2.021	0	0	372.21	0.9449
354	149.5	138.94	0.130	0.128	2.020	0	0	1220.11	0.9672
355	149.5	123.31	0.968	0.848	2.020	0	0	149.82	0.9180
356	149.8	123.35	1.016	0.894	2.020	0	0	150.38	0.9180
306	101.2	94.35	0.069	0.231	1.352	0	0.751	1218.25	0.9615
308	101.2	95.08	0.081	0.360	1.464	0	1.464	1218.25	0.9623

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	F _{total} pounds	P _{base} psia	P _{i.s.} psia	$\dot{W}_p$ lb/sec	$\dot{W}_g/\dot{W}_p$ percent	$\dot{W}_{i.s.}/\dot{W}_p$ percent	P _c /P _a	C _T total
Model III-12, Sixteen Chamber Touching Multichamber, $\epsilon_{CL}^* = 51.4, 30\%$ Length									
313	101.3	95.03	0.213	0.088	1.368	0.753	0	1229.82	0.9688
320	101.5	84.60	0.771	0.557	1.371	0.735	0	153.55	0.9183
321	101.5	84.60	0.776	0.553	1.367	0.734	0	152.74	0.9184
347	101.6	91.07	0.348	0.281	1.371	0.760	0	372.12	0.9555
309	101.3	95.56	0.309	0.095	1.363	1.531	0	1209.26	0.9669
310	101.3	95.59	0.303	0.089	1.364	1.534	0	1229.82	0.9666
314	101.4	89.87	0.502	0.347	1.369	1.509	0	279.57	0.9472
319	101.5	85.21	0.850	0.556	1.372	1.512	0	153.26	0.9190
322	101.6	85.10	0.855	0.677	1.376	1.524	0	152.62	0.9166
348	101.5	91.47	0.406	0.269	1.363	1.531	0	365.03	0.9531
311	101.3	96.37	0.462	-	1.368	3.041	0	1174.90	0.9614
312	101.3	96.56	0.458	0.089	1.366	3.040	0	1209.26	0.9617
315	101.4	90.61	0.630	-	1.369	3.022	0	278.02	0.9407
316	101.5	90.80	0.629	0.345	1.374	3.021	0	278.03	0.9421
317	101.5	86.23	0.987	0.596	1.369	3.020	0	153.34	0.9159
318	101.5	86.23	0.987	0.554	1.371	3.023	0	153.34	0.9165

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APPENDIX 3 COLD-FLOW TEST DATA (Cont.)

Test Number	Chamber Pressure psia	P _{total} pounds	P _{base} psia	P _{i.s.} psia	$\dot{W}_p$ lb/sec	$\dot{W}_s/\dot{W}_p$ percent	$\dot{W}_{i.s.}/\dot{W}_p$ percent	P/P _c	C _T total
Model III-12, Sixteen Chambers Touching Multichamber With Filler Plate, $\epsilon_{CL}^* = 51.4, 30\%$ Length									
324	101.1	82.6	0.699	0.278	1.343	0	0	150.33	0.9081
325	101.1	82.6	0.697	0.275	1.343	0	0	150.23	0.9072
326	101.1	88.3	0.381	0.202	1.341	0	0	274.40	0.9465
327	101.1	89.4	0.177	0.181	1.345	0	0	367.25	0.9483
328	101.2	93.8	0.082	0.159	1.345	0	0	1077.40	0.9659
329	101.1	94.1	0.080	0.162	1.342	0	0	1269.78	0.9661
337	101.5	89.1	0.085	0.184	1.364	0	0	380.31	0.9436
338	101.6	89.2	0.091	0.185	1.367	0	0	377.32	0.9475
330	101.1	95.0	0.086	-	1.345	0	0.762	1253.10	0.9567
331	101.2	95.0	0.087	0.419	1.346	0	0.760	1245.69	0.9679
334	101.4	95.8	0.116	0.596	1.353	0	1.547	1230.13	0.9680
339	101.5	84.2	0.684	0.612	1.378	0	1.450	153.16	0.9087
335	101.5	97.2	0.148	0.950	1.360	0	2.988	1226.14	0.9679
340	101.6	85.2	0.666	0.942	1.376	0	2.948	153.29	0.9060
336	101.5	97.9	0.150	1.127	1.364	0	3.999	1205.75	0.9608
341	101.6	84.7	0.763	0.615	1.379	0.754	1.444	153.42	0.9018
344	101.6	97.8	0.242	0.855	1.378	0.746	2.656	1222.18	0.9629
345	101.6	97.8	0.231	0.853	1.379	0.748	2.643	1334.73	0.9602
342	101.6	85.3	0.839	0.610	1.380	1.545	1.442	152.99	0.9012
343	101.6	98.2	0.311	0.853	1.377	1.547	2.647	1222.18	0.9603

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APPENDIX 4

WEIGHT FLOW AND WEIGHT FLOW DEPENDENT PARAMETER CALCULATIONS FOR
TETRAFLUOROMETHANE (CF_4)

At Rocketdyne's Rocket Nozzle Test Facility (RNTF) metering the mass-flow of the test fluids is accomplished through the use of critical flow nozzles (Sonic Venturi Meters).

For a perfect gas the equation of continuity, the perfect gas equation and the isentropic relations to go from the reservoir stagnation conditions to the throat leads to the following equation

$$\dot{W} = f \frac{A^* P_0}{\sqrt{T_0}} \quad (1)$$

where

$$f = \sqrt{\frac{\gamma}{R} \left(\frac{2}{\gamma+1} \right)^{\frac{\gamma+1}{\gamma-1}}}$$

When the geometrical throat area is used Eq. 1 should be multiplied by a discharge coefficient (C_w) to account for viscous effects and distortions in the sonic velocity profile.

The term f is called the critical flow constant and historically has been referred to as Fliegner's constant. The above relationship is however based on the assumption that the gas has a specific heat ratio (γ) that is independent of pressure and temperature and a compressibility factor of unity. For most gases at high pressures and/or low temperatures significant errors in mass flow calculations are introduced

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if the above relations are used. For example at the operating temperatures and pressure employed at RNTF with air as a test fluid errors on the order of 1 percent could be introduced into the mass flow calculations if the ideal ratio of specific heats ($\gamma = 1.40$) was employed.

To circumvent this problem critical flow functions that take into account such "real-gas" effects as compressibility and specific heat variations with temperature and pressure are employed.

The method employed to obtain the pressure-temperature dependent critical flow function is based on a procedure where the throat static state is assumed and the upstream stagnation state at the same entropy, but at an enthalpy that is increased by the enthalpy change needed to accelerate the gas to the speed of sound, is determined. Use of this method requires either tabulated values of entropy, enthalpy, specific volume or density and sonic velocity as a function of temperature and pressure or an equation of state which will give suitable first and second derivatives.

The detailed procedure involves the following steps

1. For a given stagnation temperature (T_0) and pressure (P_0) estimate the throat static pressure (P^*) and temperature (T^*) having an entropy (S_0) the same as that at the stagnation conditions.
2. Determine the local sonic velocity for the throat static conditions and solve for the enthalpy, required to obtain the sonic velocity using the following equation

$$\Delta h = a^{*2}/2gJ \quad (2)$$

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3. Determine the stagnation enthalpy (h_o) required to obtain the sonic velocity.

$$h_o = h^* + \Delta h \quad (3)$$

4. For the given stagnation entropy (S_o) and calculated enthalpy (h_o) determine the corresponding stagnation pressure (P_o') and temperature (T_o'). If P_o' and T_o' are not equal to the initial specified P_o and T_o step 1 through 4 is repeated until agreement is obtained.
5. The pressure-temperature dependent critical flow function for a specific gas is then calculated using the following equation

$$f(T_o, P_o) = \frac{\dot{W} \sqrt{T_o}}{P_o A^*} = \frac{C^* a^* \sqrt{T_o}}{P_o} \quad (4)$$

The gas properties of air required for the above calculations can be obtained from Ref. 20. However as the pressure and temperature dependent critical flow function is available in various published papers (Ref. 21 and 22) additional calculation was not required.

For Tetrafluoromethane the Martin-Hou equation of state (Ref. 23) was used to obtain the pressure-temperature volume relationship. Tabulated values of entropy and enthalpy were obtained from Ref. 24. The ratio of the specific heats was calculated in the manner outlined in Ref. 10 and the sonic velocity calculations are described in Ref. 25.

To obtain the one dimensional ideal thrust coefficient the following fundamental thrust equation is used

$$F = \dot{m} V_o + (P_o - P_a) A_o \quad (5)$$

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For optimum conditions ($P_e = P_a$) the above equation reduces to

$$F_{opt} = \dot{m} V_e \quad (6)$$

Dividing through by $P_o A^*$ the relationship for the one dimensional ideal optimum thrust coefficient is

$$C_{Fopt} = \frac{F_{opt}}{P_o A^*} = \frac{\dot{m} V_e}{P_o A^*}$$

which reduces to

$$C_{Fopt} = \frac{\rho^* a^* V_e}{P_o} = \frac{f(T_o, P_o) V_e}{\sqrt{T_o}} \quad (7)$$

If the pressure-temperature dependent critical flow function is available the one dimensional optimum thrust coefficient can be readily obtained by calculation of the exit velocity obtained for an isentropic expansion of the flow from reservoir stagnation (P_o) to ambient pressure (P_e) as given by the following equation

$$V_e = \sqrt{2g_c J (h(T_o, P_o) - h(P_e, S_o))}$$

A series of these calculations have indicated that for the operating temperatures and pressures employed at the RNTF a representative ratio of specific heats can be employed to obtain an optimum C_F . For Air the representative γ is 1.4 and for CF_4 the representative γ is 1.2.

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13. ABSTRACT		
Investigations of the aerodynamic spike nozzle concept are discussed in this report. Cold-flow test programs to evaluate high area ratio aerodynamic spike nozzles and combustor configurations for aerodynamic spike nozzles were completed. A description of the models tested and the test results are presented. Analytical and design studies of the aerodynamic spike nozzle concept were conducted and the results are presented.		

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14 KEY WORDS	LINK A		LINK B		LINK C	
	ROLE	WT	ROLE	WT	ROLE	WT
1. Aerodynamic nozzles 2. Multichamber nozzles 3. Effect of Secondary flow 4. Base configuration effects 5. Cold-flow testing 6. Nozzle performance 7. Nozzle base pressure 8. Engine designs 9. Nozzle heat transfer 10. Nozzle weight						

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