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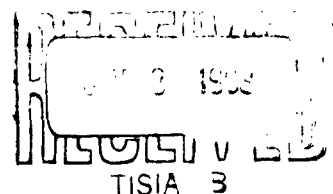
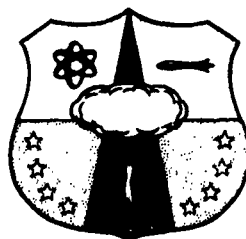
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ANALYSIS OF ARGUS BOMB DEBRIS

Mathematical Model

TECHNICAL DOCUMENTARY REPORT NUMBER AFSWC-TDR-62-127, Vol II

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**Research Directorate
AIR FORCE SPECIAL WEAPONS CENTER
Air Force Systems Command
Kirtland Air Force Base
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FOREWORD

This is the final report of the work by Lockheed Missiles & Space Company performed under Air Force Contract AF 29(601)-4419 with the Air Force Special Weapons Center, 1 June 1961 — 21 December 1962. It is presented in two volumes: AFSWC TDR-62-127, Vol I, Behavior of the Debris and Related Phenomena, classified Secret-Restricted Data; and AFSWC TDR-62-127, Vol II, Mathematical Model, unclassified.

The Report is identified for Lockheed purposes as LMSC-B007043, Code No. 2-96-62-1.

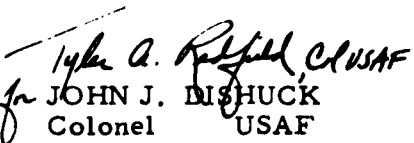
ABSTRACT

This volume contains a detailed description of the analytical methods used in constructing the Monte Carlo model and code. The various mechanisms contributing to the energy losses of heavy particles moving through the atmosphere are reviewed, and it is concluded that for the cases of interest here only the elastic collisions need to be taken into account. An outline is given of a statistical treatment of inelastic collisions together with a derivation of the corresponding probability distribution. The probability distribution for the beta decays of fission particles is also derived, and lastly, the logical construction of the code for the calculation of a history of a given particle is described in detail.

PUBLICATION REVIEW

This report has been reviewed and is approved.


DONALD I. PRICKETT
Colonel USAF
Director, Research Directorate


for JOHN J. DISHUCK
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DCS/Plans & Operations

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INTRODUCTION

This report is a continuation of a study carried out by the Theoretical Physics Group at Lockheed on the motion of the bomb debris. This volume describes the mathematical background of the Monte Carlo code used in this study and the code itself.

We would like to acknowledge the contributions of A. J. Cook to the formulation and execution of the Monte Carlo calculations.

SUMMARY

In any Monte Carlo model it is advantageous to limit the number of microscopic processes which have to be treated statistically. In the model of behavior of fission particles in the atmosphere, the most important processes are perhaps the collision of these particles with the atmospheric atoms. This is the subject of Section 1, *Energy Loss of Fission Particles Released at High Altitudes*, where the contributions of the elastic and inelastic collision to the slowing down of a heavy particle are briefly examined. It is found that approximate calculations of such contributions are valid for velocities up to about 5×10^7 cm/sec, and that, for the same velocities, a good first approximation consists of neglecting the energy losses due to inelastic collision.

With this assumption, it is possible to integrate out the contributions of the elastic collisions, and only the inelastic collisions have to be treated statistically. The appropriate probability distribution is derived in Section 2, *Inelastic Collisions of Fission Particles in the Atmosphere*. This distribution depends only on the cross section for the collision and the initial altitude, and is strongly determined by the analytical assumption made on the behavior of the density with altitude. The different forms of the distribution in various atmospheres are briefly examined. The choice of the final form is governed by simplicity of formulation and the necessity for rapidly developing a working code.

In Section 3, *Beta Decay of Fission Fragments*, a probability distribution for the beta decay of a typical fission particle is derived. The assumption is made that the activity of a collection of fission particles is adequately given by the Way-Wigner law, and a prescription for obtaining a good approximation to this law is given.

In Section 4 , IBM 7090 Code for the Monte Carlo Model, the detailed steps in the calculation of a history of a fragment are described. It must be pointed out that all the steps shown and the associated numerical procedures were chosen primarily to develop in a reasonable time a rapid code. Thus, a prescription for decay times differing slightly from that of Section 3, was adopted. Section 4 also contains an outline of the logical flow of the code. Section 5 contains a listing of the current code together with the output of a sample run.

Section 1

ENERGY LOSS OF FISSION PARTICLES RELEASED AT HIGH ALTITUDES

In this section the different mechanisms contributing to the stopping power of the atmosphere on neutral and ionized fission particles are reviewed. The slowing down of a fission particle is due to its elastic and inelastic collisions with the ambient atoms, and of the latter collisions we consider those giving rise to ionization, electron capture, and electron loss.

For particle velocities below about 5×10^7 cm/sec elastic collisions dominate, the energy loss being governed by the transport cross section through the law

$$\frac{dv}{dt} = - \frac{n(s)}{2} \sigma_{tr} v^2 \quad (1.1)$$

where $n(s)$ is the number density of the ambient medium. The evaluation of σ_{tr} depends essentially on the interaction potential between the colliding systems. For heavy atoms, the potential can be calculated to an accuracy of 10 percent on the basis of the statistical model for the electrons (Ref. 1). Thus,

$$U(r) = \frac{Z_1 Z_2 e^2}{r} \chi(\psi r/a) \quad (1.2)$$

where $\chi(x)$ is the screening function in the Thomas-Fermi potential, Z_1 and Z_2 are the atomic numbers of the interacting atoms, r is the internuclear distance,

$$a = \left(9\pi^2/128 \right)^{1/3} \hbar^2/me^2 = 4.7 \times 10^{-9} \text{ cm} \quad (1.3)$$

and

$$\psi = \left(Z_1^{1/2} + Z_2^{1/2} \right)^{2/3} \quad (1.3)'$$

Using the interaction potential (1.2), Firsov (Ref. 2) obtains an expression for σ_{tr} which he approximates by

$$\sigma_{tr} = 2\pi e^4 M_1 M_2 \left(Z_1 Z_2 / E_{cm} (M_1 + M_2) \right)^2 \ln \left(1 + \frac{0.7 E_{cm}}{30.5 Z_1 Z_2 \psi} \right) \quad (1.4)$$

where E_{cm} is the energy in ev in the center of mass system:

$$E_{cm} = \mu E / M_1$$

$$\mu = M_1 M_2 / (M_1 + M_2)$$

The resultant stopping power* is

$$W_E = 1.3 \times 10^{-13} \frac{Z_1^2 Z_2^2}{M_2 E / M_1} \ln \left(1 + \frac{0.23 \mu E}{M_1 Z_1 Z_2 \psi} \right) \text{ cm}^2 \text{ ev} \quad (1.5)$$

To obtain the energy loss due to excitation and ionization, Firsov (Ref. 3) assumes that there is a friction-like force between the orbital electrons of the two atoms while they are passing each other. The resultant conversion of the kinetic energy of relative motion into excitation energy, is due to the transfer of momentum by electrons

*Stopping power is the average energy loss per incident particle per centimeter path in a gas of unit number density.

from one particle to the other in the region where the electronic shells overlap. The energy lost to electron excitation or ionization at a given impact parameter R_0 (cm) and velocity V (cm/sec) is

$$\epsilon = \frac{(Z_1 + Z_2)^{5/3} \times 4.3 \times 10^{-8} v}{\left[1 + 3.1(Z_1 + Z_2)^{1/3} 10^7 R_0\right]^5} \quad (1.6)$$

Integrating over all impact parameters to obtain the total stopping power gives

$$W_E = 2\pi \int_0^\infty \epsilon R_0 dR_0 = 0.234 \times 10^{-22} (Z_1 + Z_2) v \text{ cm}^2 \text{ ev} \quad (1.7)$$

The ionization cross section at a velocity v is given by

$$\sigma = \sigma_0 \left[(v/v_0)^{1/5} - 1 \right]^2 \quad (1.8)$$

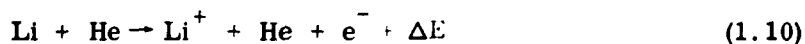
with

$$\left. \begin{aligned} \sigma_0 &= \frac{32.7}{(Z_1 + Z_2)^{2/3}} 10^{-16} \text{ cm}^2 \\ \text{and} \\ v_0 &= \frac{23.3 E_i}{(Z_1 + Z_2)^{5/3}} 10^6 \text{ cm/sec} \end{aligned} \right\} \quad (1.9)$$

E_1 in (ev) being the first ionization potential of the gas atom. The variation of σ with velocity was computed from Eq. (1.8) for $Z_1 = 45$ $Z_2 = 7$:

v (cm/sec)	σ (cm ² $\times 10^{16}$)
3×10^6	0.499
5×10^6	0.897
8×10^6	1.421
1×10^7	1.732
3×10^7	4.064
5×10^7	5.748

A comparison of the predictions of Eq. (1.8) with experiment has been carried out by Fedorenko (Ref. 4). The velocity range of the colliding ions varied from 7×10^6 to 9×10^7 cm/sec, and in this region there is agreement between theory and experiment to within a factor of 2. Equation (1.8) is even useful for the lighter atoms, where one finds it to agree to within a factor of 3. A comparison of the theory with the experimental data of Ref. 5 for electron loss cross sections for lithium in helium:



is made below

v (cm/sec)	σ (cm ² $\times 10^{-16}$) (Firsov)	σ (cm ² $\times 10^{-16}$) (expt)
4×10^7	1.45	0.6
6×10^7	2.52	1.0
8×10^7	3.54	1.3

A comparison of the stopping powers due to elastic collisions with those due to ionizing collisions may be made with the help of Eqs. (1.5) and (1.7). As a typical example,

consider a fission ion of atomic mass 100 and atomic number 45. The stopping powers are:

v (cm/sec)	W_E (cm ² ev) (elastic)	W_E (cm ² ev) (inelastic)
4×10^7	1.655×10^{-13}	4.69×10^{-14}
1×10^7	1.79×10^{-13}	1.17×10^{-14}

The stopping power due to inelastic scattering falls off rapidly with decreasing energy, being 30 percent of that due to elastic scattering at a velocity of 4×10^7 cm/sec, and only 7 percent at a velocity of 1×10^7 cm/sec.

The stopping power due to electron capture (charge transfer) is more difficult to estimate. For lack of sufficient theoretical or experimental data, it is necessary to rely on empirical rules. From an examination of available experimental data on charge transfer reactions, Hasted (Ref. 6) has observed that the maximum charge-transfer cross section occurs at a velocity v_m of the incident particle given by

$$\frac{a \Delta E}{v_m h} \approx 1 \quad (1.11)$$

where ΔE is the energy defect measured in electron volts and "a" has the dimension of length. Hasted claims the best fit is given by $a = 8 \text{ \AA}$.

If we express ΔE in ev ,

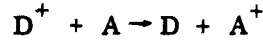
$$v_m = 1.9 \times 10^7 \Delta E \text{ cm/sec} \quad (1.12)$$

For velocities in the adiabatic region, the charge transfer cross section varies according to

$$\sigma = c \exp(-k a \Delta E/v) \quad (1.13)$$

where c and k are constants for any particular reaction. There is, of course, no rigorous theoretical basis for Eq. (1.13). For velocities, greater than that for which $\sigma_{\max}$ occurs, σ falls off with increasing energy as some inverse power of v .

For a typical reaction



the energy difference will be of the order of 7 ev, so that the velocity at which $\sigma_{\max}$ occurs is approximately 1.3×10^8 cm/sec. It would thus appear that $\sigma_{\max}$ is reached for velocities well outside the range of velocities with which we are concerned.

The stopping power due to capture is

$$\sum_n E_n \sigma_{c,n} + \frac{mE}{M_1} \sum_n \sigma_{c,n}$$

For a velocity of 4×10^7 cm/sec, $E = 83.6$ kev

and

$$\frac{mE}{M_1} = 0.455 \text{ ev}$$

The value of $\sigma_{\max}$ will be of order of 10^{-16} cm² and, at a velocity of 4×10^7 cm/sec, σ should be much less than $\sigma_{\max}$ according to Eq. (1.13). Nevertheless, to obtain a gross overestimate of the effect of charge exchange on the energy loss, let us assume that at $v = 4 \times 10^7$ cm/sec, σ is 10^{-15} cm². Assuming E_n to be approximately 10 ev, we find the stopping power due to charge transfer must be less than 1×10^{-14} cm² ev, which is less than that due to inelastic scattering. Thus, energy losses due to charge transfer can be neglected.

Neglecting the energy losses due to inelastic collisions altogether, we expand the logarithm in Eq. (1.4) to obtain

$$\sigma_{tr} \sim \frac{a^2}{x^2} \frac{1}{E} \quad \text{i.e.,} \quad \sigma_{tr} \sim 1/v^2 \quad (1.14)$$

From Eqs. (1.1) and (1.14)

$$\frac{dv}{dt} = -K N \quad (1.15)$$

where K is a function of A and Z , and N is the number density of the atmosphere. Because K is a slowly varying function of its arguments, the error involved in working with $K = 1.8 \times 10^{-3}$ (the value for a typical fragment of $A = 100$ and $Z = 45$) will not be great.

For a particle moving along a straight line path making an angle θ with the vertical



$$dz = ds \cos \theta \quad (1.16)$$

Introducing the density of the atmosphere $\rho(z)$ and

$$N = \frac{A' \rho(z)}{M} \quad (1.17)$$

where A' is Avogadro's number and M the mean molecular weight of the atmospheric atoms, we can write Eq. (1.15)

$$\frac{dv}{dt} = - \frac{K A'}{M \cos \theta} \rho(z)$$

which can be integrated to give

$$v^2 = v_o^2 - \frac{2K A'}{M \cos \theta} \int_{z_o}^z \rho(z) dz \quad (1.19)$$

The precise form of the stopping law used depends upon the assumptions made concerning $\rho(z)$ in evaluating Eq. (1.19). The simplest, and the one adopted here is that the hydrostatic condition

$$dp = -g \rho(z) dz \quad (1.20)$$

is satisfied. Then, if we neglect the variation of g with altitude, Eq. (1.19) gives

$$v^2 = v_o^2 + \frac{2K A'}{M g \cos \theta} (p(z) - p(z_o)) \quad (1.21)$$

Section 2

INELASTIC COLLISIONS OF FISSION PARTICLES IN THE ATMOSPHERE

2.1 THE CHARGE STATE OF A BEAM OF PARTICLES

According to the results of the preceding section, the electron capture and loss cross sections do not contribute to the energy losses of particles moving through the atmosphere at velocities equal to or less than about 5×10^7 cm/sec. Nonetheless, these cross sections can be of importance in determining the overall charge state of a collection of particles.

Let n_i and n denote the equilibrium number densities of the debris ions and atoms, respectively. Neglecting the formation of more highly ionized states and negative ions of the debris we have in equilibrium

$$n_i \sigma_c = n \sigma_\ell \quad (2.1)$$

where σ_c and σ_ℓ are the capture and loss cross sections. The charged fraction of the beam is

$$f(i) = \frac{n_i}{n + n_i} = \frac{1}{1 + \sigma_c/\sigma_\ell} \quad (2.2)$$

For a typical electron loss reaction



we can use Eq. (1.8) with E_i of the order of 7 ev. The capture cross section can be estimated with the help of Hasted's (Ref. 7) empirical relation analogous to Eq. (1.13)

$$\sigma_c = c \exp \left\{ - a \Delta E / 4 h \nu \right\} \quad (2.3)$$

Taking $a\Delta E/4h \approx 3.3 \times 10^7$ for a typical charge transfer reaction



we have the following

$V \text{ (cm/sec)}$	$\sigma_L (\text{cm}^2 \times 10^{-16})$	$\sigma_C (\text{cm}^2 \times 10^{-16})$
4×10^7	7.64	.44
1×10^7	2.96	.037

We see that σ_C falls relatively more rapidly with energy than does σ_L , and over the range of velocities of interest $\sigma_L > \sigma_C$. Hence, from Eq. (2.2), the fraction of the beam which remains charged is greater than 1/2. There is some experimental confirmation of this result (Ref. 8).

2.2 RANDOM INELASTIC COLLISIONS

In addition to making rough estimates like Eq. (2.2) possible, the inelastic cross sections determine the probability for a particle to undergo a charge-changing collision. To determine the probability distribution for such a collision, we consider a neutral particle moving through a medium of density N along a path s making an angle θ with the vertical. Let σ be the cross-section for ionization of the particle.

The change in the number n of neutral particles along a segment of path ds is given by the well-known attenuation law

$$dn = -n\sigma N ds \quad (2.4)$$

and, using Eqs. (1.16) and (1.17), this can be written

$$\frac{dn}{n} = - \frac{B}{\cos \theta} \rho(z) dz \quad (2.5)$$

with

$$B = \frac{\sigma A'}{M} \quad (2.6)$$

Integrating Eq. (2.5) from an arbitrary initial altitude z_0 to an arbitrary final altitude z , we have

$$n/n_0 = \exp \left\{ - \frac{B}{\cos \theta} P(z, z_0) \right\} \quad (2.7)$$

where

$$P(z, z_0) = \int_{z_0}^z \rho(z) dz \quad (2.8)$$

Because $\cos \theta$ and $P(z, z_0)$ have the same sign and are negative for particles moving downward, n/n_0 is always a decreasing exponential. Observe that the integral Eq. (2.8) also occurs in the stopping law, Eq. (1.19).

Let n_c be the number of particles colliding with the ambient atoms in the interval (z_0, z) . The fraction

$$\frac{n_c}{n_0} = 1 - \frac{n}{n_0} \quad (2.9)$$

is the probability for a particle to have an ionizing collision before reaching the altitude z . Differentiating

$$\frac{n_c}{n_0} = 1 - \exp \left\{ - \frac{B}{\cos \theta} P(z, z_0) \right\} \quad (2.10)$$

gives the spatial rate of collision

$$\frac{dn_c}{n_0} = \frac{B}{\cos \theta} \exp \left\{ - \frac{B}{\cos \theta} P(z, z_0) \right\} \rho(z) dz \quad (2.11)$$

The density $\rho(z)$ is defined in $0 < z < \infty$. If the integrated density diverges, that is if

$$P(\infty, z_0) = \int_{z_0}^{\infty} \rho(z) dz = +\infty \quad (2.12)$$

then Eq. (2.11) is a normalized probability density for collisions and Eq. (2.10) is the corresponding probability distribution. If the integrated density $P(\infty, z_0)$ is finite, the fraction of particles escaping to infinity without undergoing an ionizing collision is finite:

$$\frac{n_{\infty}}{n_0} = \exp \left\{ -\frac{B}{\cos \theta} P(\infty, z_0) \right\} \quad (2.13)$$

the fraction colliding in the atmosphere is $1 - n_{\infty}/n_0$; and hence, the probability distribution for collisions in the open interval $z_0 < z < \infty$ is

$$\frac{1 - n_0}{1 - n_{\infty}/n_0} \quad (2.14)$$

The standard Monte Carlo procedure is to choose a random number R from the uniform distribution on $(0, 1)$ and to solve the equation

$$R = \frac{1 - n/n_0}{1 - n_{\infty}/n_0} \quad (2.15)$$

for the altitude z at which a collision occurs. A collection of altitudes so determined has a distribution approximating Eq. (2.14). Calculating z directly from Eq. (2.15) can lead to complicated and slow computations because we have to solve the equation

$$\int_{z_0}^z \rho(z) dz = \frac{-\cos \theta}{B} \ln \left[1 - R \left(1 - \exp \left\{ -\frac{B}{\cos \theta} \int_{z_0}^{\infty} \rho(z) dz \right\} \right) \right] \quad (2.16)$$

for z .

Alternatively, we can interpret Eq. (2.10) as a normalized distribution on the closed interval $z_0 \leq z \leq +\infty$ with a jump discontinuity at the point $z = +\infty$. The probability associated with $z = +\infty$ is n_∞/n_0 . With the discontinuous distribution, the procedure for determining z is to solve

$$R = 1 - n/n_0 \quad (2.17)$$

for z if

$$R < 1 - n_\infty/n_0 \quad (2.18)$$

holds and to set $z = +\infty$ if Eq. (2.18) fails. Because R and $1 - R$ are simultaneously uniformly distributed on $(0, 1)$, we solve, in practice,

$$P(z, z_0) = - \frac{\cos \theta}{B} \ln R \quad (2.19)$$

for z if

$$R > n_\infty/n_0 \quad (2.20)$$

and set $z = \infty$ if Eq. (2.20) fails.

For a finite atmosphere, one in which $\rho(z)$ is defined for $0 \leq z \leq H$, we use the same procedure, with the fraction n_H/n_0 replacing the fraction n_∞/n_0 . In practice, we solve Eq. (2.19) for z and say that the particle has reached H without suffering a collision if $z > H$.

2.3 COLLISIONS IN VARIOUS ATMOSPHERES

The explicit calculation of the collision altitude is uniquely determined by the assumption made on the behavior of $\rho(z)$ with z and the resultant evaluation of Eq. (2.8).

2.3.1 Tabulated Atmosphere

Suppose $\rho(z)$ is known as a table of values of ρ vs. z in an interval $0 < c < z < H$. By a suitable interpolation rule we can determine $\rho(z_0)$ for any z_0 in the interval. We can also construct values of $P(c, z)$ and $P(H, z)$, and by interpolation, those of $P(c, z_0)$ and $P(H, z_0)$. Then the probability of escaping over the upper boundary H without a collision between the starting point z_0 and H , is

$$n_H/n_0 = \exp \left\{ - \frac{B}{\cos \theta} P(H, z_0) \right\} \quad (2.21)$$

and the probability distribution for collisions in the interval (H, z_0) is

$$\frac{1 - n/n_0}{1 - n_H/n_0} \quad (2.22)$$

with n/n_0 given by Eq. (2.7). Equating (2.22) to a random number R and solving for z , yields a collision point distributed according to Eq. (2.14), i.e.,

$$\int_{z_0}^z \rho(z) dz = - \frac{\cos \theta}{B} \ln \left[1 - R(1 - n_H/n_0) \right] \quad (2.23)$$

Interpolation among the tabulated values of the integrated density gives z .

2.3.2 Constant Atmosphere

Let $\rho(z) = \rho$ a constant in the interval $0 < c < z < H$. In this case

$$P(z, z_0) = \rho(z - z_0) \quad (2.24)$$

and the probability of escaping over the upper boundary is

$$n_H/n_0 = \exp \left\{ - \frac{B}{\cos \theta} \rho(H - z_0) \right\} \quad (2.25)$$

Because the integrated density diverges at infinity, we can replace a finite atmosphere with constant density by an infinite atmosphere with the same constant density. In such an atmosphere, the probability distribution for collisions is simply

$$1 - n/n_0 \quad (2.26)$$

Choosing a random number R and solving for z , we get

$$z = z_0 + \frac{\cos \theta}{\rho B} \ln R \quad (2.27)$$

If this value of z fails to satisfy

$$c < z < H$$

it is rejected as a possible collision point. Note that the probability of rejecting such a z is

$$\int_H^\infty \frac{B}{\cos \theta} \exp \left\{ - \frac{B\rho}{\cos \theta} (z - z_0) \right\} \rho dz = \exp \left\{ - \frac{B\rho}{\cos \theta} (H - z_0) \right\} \quad (2.28)$$

which is precisely the probability of escape over the upper boundary H .

2.3.3 Linear Atmosphere

Suppose the density decreases linearly according to

$$\rho(z) = b - az, \quad a > 0 \quad (2.29)$$

in $0 < c < z < H$. Because $\rho(z) \geq 0$, we have

$$b/a > H \quad (2.30)$$

The integrated density is

$$P(z, z_0) = (z - z_0) \left[b - \frac{a}{2} (z + z_0) \right] \quad (2.31)$$

a quadratic polynomial with zeros at z_0 and

$$z = \frac{2b}{a} - z_0 \quad (2.32)$$

The fact that $z_0 < H$, and Eq. (2.30) imply

$$\frac{2b}{a} - z_0 > H \quad (2.33)$$

Hence, the second zero occurs above H . The collision point is determined in the usual manner.

2.3.4 Exponentially Decreasing Atmosphere

Suppose the density is given by

$$\rho(z) = a \exp \{ - b(z - c) \} \quad (2.34)$$

with $a, b > 0$ in $0 < c < z < H$. The integrated density becomes

$$P(z, z_0) = \frac{a}{b} \left[\exp \{ - b(z_0 - c) \} - \exp \{ - b(z - c) \} \right] = q(z_0) - q(z) \quad (2.35)$$

with

$$q(z) = \frac{a}{b} \exp \{ - b(z - c) \}$$

The probability of escape over the upper boundary H is now

$$n_H/n_0 = \exp \left\{ - \frac{B}{\cos \theta} \left[q(z_0) - q(H) \right] \right\} \quad (2.36)$$

and solving the equation

$$R = \frac{1 - n/n_o}{1 - n_H/n_o}$$

for z gives

$$z = c - \frac{1}{b} \ln \left[\frac{b}{a} (q(z_o) - P) \right] \quad (2.37)$$

where

$$P = - \frac{\cos \theta}{B} \ln \left[1 - R(1 - n_H/n_o) \right]$$

2.3.5 Hydrostatic Atmosphere

The previous assumptions concerning $\rho(z)$ are either manifestly unsuitable or lead to computations which are too slow for Monte Carlo calculations. The hydrostatic relation, Eq. (1.20)

$$dp(z) = - g \rho(z) dz$$

where $p(z)$ is the pressure at altitude z and g is the acceleration due to gravity can be integrated to give

$$P(z, z_o) = \frac{p_o - p}{g} \quad (2.38)$$

where g is assumed constant over the altitudes of interest. The fraction surviving Eq. (2.7) becomes

$$n/n_o = \exp \left\{ - \frac{B}{\cos \theta} \frac{p_o - p}{g} \right\} \quad (2.39)$$

Using the alternative procedure, Eqs. (2.19) and (2.20), and solving for the collision pressure rather than the collision altitude gives

$$p = p_o + g \frac{\cos \theta}{B} \ln R \quad (2.40)$$

as a provisional value of p to be accepted only if

$$p > p_H \quad (2.41)$$

Interpolation in the table of p vs z (Section 5) determines the collision altitude. The altitudes so determined have

$$\frac{1 - n/n_o}{1 - n_H/n_o} \quad (2.42)$$

as a normalized probability distribution.

The assumptions usually made in integrating the hydrostatic relation are (i)

$$\rho(z) = \frac{M}{kT} p(z) \quad (2.43)$$

where k is Boltzmann's constant, M the molecular weight, and T the temperature; (ii) the variation of g , M , and T can be neglected. In the presence of these assumptions, we easily find that

$$\rho(z) = \rho(z_o) \exp \left\{ - \frac{Mg}{kT} (z - z_o) \right\} \quad (2.44)$$

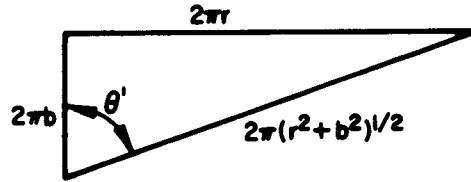
an exponentially decreasing atmosphere, [cf Eq. (2.34)].

2.4 COLLISIONS ALONG A SPIRAL PATH

Let the z' axis of a new rectangular coordinate system have a polar angle θ_0 with respect to the z axis. Suppose a particle travels along a spiral path, say the helix

$$\begin{aligned}x' &= r \cos u \\y' &= r \sin u \\z' &= bu\end{aligned}\tag{2.45}$$

where r is the radius of gyration and $2\pi b$ is the distance the particle advances along the z' axis in one revolution. If we unroll the path for a single revolution, we get the following sketch



Here θ' is the pitch angle of the spiral. We see that the parameter u is connected with the arc length s by the relation

$$u = s / (r^2 + b^2)^{1/2}\tag{2.46}$$

and that

$$\cos \theta' = b / (r^2 + b^2)^{1/2}\tag{2.47}$$

holds. Thus, we have

$$z' = bs / (r^2 + b^2)^{1/2} = s \cos \theta'\tag{2.48}$$

or

$$dz' = \cos \theta' ds\tag{2.49}$$

Moreover, because the polar angle of the z' axis is θ_0 we have, with respect to the z axis,

$$dz = \cos \theta_0 dz' \quad (2.50)$$

Combining Eqs. (2.49) and (2.50) gives

$$dz = \cos \theta_0 \cos \theta' ds \quad (2.51)$$

Comparing Eq. (2.51) with Eq. (1.16) shows that the analogue for Eq. (2.5) in the case of a spiral path is

$$\frac{dn}{n} = - \frac{B}{\cos \theta_0 \cos \theta'} \rho(z) dz \quad (2.52)$$

Thus, we may simply replace $\cos \theta$ by the product

$$\cos \theta_0 \cos \theta' \quad (2.53)$$

in the formulas for straight line paths to obtain the formulas appropriate for spiral paths.

We also make the same replacement when applying Eq. (1.21) to describe the slowing down along a spiral path.

Section 3

BETA DECAY OF FISSION FRAGMENTS

A correct statistical treatment of beta decay would require a knowledge of all decay chains and the lifetimes and branching ratios of all the elements in these chains. Because such detailed data are not known experimentally, we are forced to make model assumptions. In this we are guided by a few well-established experimental facts about beta decay. According to Way and Wigner (Ref. 9) the combined beta activity of all fission products and succeeding generations stays roughly constant for 1 sec and then drops as $t^{-1.2}$. The length of the decay chains varies, but on the average about three betas are emitted per fission product. We define the beta activity $A(t)$ to be the average number of betas per fission product per unit time so that

$$\int_0^{\infty} A(t) dt = 3 \quad (3.1)$$

With this normalization, the Way-Wigner law takes the form

$$A(t) = \begin{cases} \frac{1}{2}, & t \leq 1 \text{ sec} \\ \frac{1}{2} t^{-1.2}, & t > 1 \text{ sec} \end{cases} \quad (3.2)$$

In our model we assume that all fission products produce exactly three electrons. For the Monte Carlo method, we need probability distributions for each of the three decays.

Let us introduce the fractions of fission products n_0 , n_1 , n_2 , and n_3 , which are present after 0, 1, 2, and 3 decays have taken place. At $t = 0$, no decays have occurred, so that the initial conditions are

$$n_0 = 1 \text{ and } n_1 = n_2 = n_3 = 0 \quad (3.3)$$

Let us introduce three positive functions, $f_1(t)$, $f_2(t)$, and $f_3(t)$, describing the rate of production of betas by first, second, and third decays. The fractions n_i obey differential equations of the form

$$\frac{dn_0}{dt} = -f_1(t)n_0$$

$$\frac{dn_1}{dt} = f_1(t)n_0 - f_2(t)n_1 \quad (3.4)$$

$$\frac{dn_2}{dt} = f_2(t)n_1 - f_3(t)n_2$$

and the normalization condition for all times

$$n_3 = 1 - n_0 - n_1 - n_2 \quad (3.5)$$

Because there are not enough experimental data to determine the three rate functions, we can make the assumption that they have a common value, say $f(t)$.

Let us introduce the scaled time

$$s = \int_0^t f(u)du \quad (3.6)$$

The system [Eq. (3.4)] simplifies to

$$\left. \begin{aligned} \frac{dn_0}{ds} &= -n_0 \\ \frac{dn_1}{ds} &= n_0 - n_1 \\ \frac{dn_2}{ds} &= n_1 - n_2 \end{aligned} \right\} \quad (3.7)$$

which has the solution

$$\left. \begin{aligned} n_0 &= e^{-s} \\ n_1 &= s e^{-s} \\ n_2 &= \frac{s^2}{2} e^{-s} \end{aligned} \right\} \quad (3.8)$$

satisfying the initial conditions required by Eq. (3.3).

We note that

$$\int_0^{\infty} n_i(s) ds = 1, \quad i = 0, 1, 2, \quad (3.9)$$

holds for each of Eqs. (3.8). In terms of the scaled time s , the analogue of the rate function f is unity. Consequently, we can identify n_i , $i = 0, 1, 2$ as the probability density of the $(i + 1)$ st decay time in scaled time. The corresponding densities in real time are

$$f(t)n_i \int_0^t f(u) du, \quad i = 0, 1, 2 \quad (3.10)$$

Because first, second, and third decays for an individual particle occur sequentially, we need a procedure for choosing three random variables t_1 , t_2 , and t_3 satisfying

$$0 < t_1 < t_2 < t_3 \quad (3.11)$$

such that t_i is a sample from the distribution of i^{th} decay times Eq. 3.10. Our strategy is to make use of the one-one, monotone, and continuous relation between s and t , Eq. (3.6), to solve the analogous problem in scaled time, and then to transform the random variable s_i into random variables t_i .

If u_i , $i = 1, 2, 3$, are independent random variables each with e^{-u} as probability density, then the random variable $s_2 = u_1 + u_2$ has $n_1(s) = se^{-s}$ as probability density, and the random variable $s_3 = u_1 + u_2 + u_3 = s_2 + u_3$ has $n_2(s) = (s^2/2)e^{-s}$ as probability density. Consequently, we solve the problem in scaled time by choosing three random numbers, R_i , $i = 1, 2, 3$, from the uniform distribution on $(0, 1)$, by setting $u_i = -\ln R_i$, and by taking

$$s_1 = u_1 = -\ln R_1$$

$$s_2 = u_1 + u_2 = s_1 - \ln R_2 \quad (3.12)$$

$$\text{and} \quad s_3 = u_1 + u_2 + u_3 = s_2 - \ln R_3$$

Requiring the total activity resulting from all three generations to reproduce the Way-Wigner law yields

$$A(t) = f(t) \left[n_0 + n_1 + n_2 \right] = \frac{ds}{dt} \left[1 + s + \frac{s^2}{2} \right] e^{-s} \quad (3.13)$$

Integrating Eq. (3.13) with respect to t gives

$$\int_0^t A(t) dt = \int_0^s \left[1 + s + \frac{s^2}{2} \right] e^{-s} ds \quad (3.14)$$

Under the hypothesis that the Way-Wigner law holds, the relation Eq. (3.14) between s and t is equivalent to Eq. (3.6) but does not involve a knowledge of $f(t)$. Carrying out the integrations in Eq. (3.14) and solving for t gives

$$t = \begin{cases} 2s & 0 \leq s \leq 1/2 \\ \left[\frac{5}{6 - 2s} \right]^5, & 1/2 < s \end{cases} \quad (3.15)$$

with

$$s = 3 - \left[3 + 2s + \frac{s^2}{2} \right] e^{-s}$$

Combining Eqs. (3.12) and (3.15) gives decay times t_i , $i = 1, 2, 3$, satisfying (3.11),

The uniform rate function $f(t)$ is nearly constant for $0 \leq t \leq 1$ and decreases for $t > 1$. In fact, manipulating Eq. (3.14) yields

$$f(t) = \begin{cases} \frac{1}{2} + \left[\frac{e^s - \left(1 + s + \frac{s^2}{2} \right)}{2 + 2s + s^2} \right], & t \leq 1 \text{ sec}, \\ \left[1 + \frac{4 + 2s}{2 + 2s + s^2} \right] \frac{1}{5t}, & t > 1 \text{ sec} \end{cases} \quad (3.16)$$

with the value of s for which $t = 1$ being approximately 0.51.

A simpler, alternative way to obtain three decay times for a particle is to choose three samples, t , from the distribution with the Way-Wigner law as probability density, to order the samples so that Eq. (3.11) holds, and then to declare the resulting t_i to be the i^{th} decay time. This procedure amounts to having different rate functions in the differential [Eq. (3.4)].

Interpreted as a probability density, the Way-Wigner law takes the form

$$w(t) = \begin{cases} 1/6 & , t \leq 1 \text{ sec} \\ t^{-1.2}/6 & , t > 1 \text{ sec} \end{cases} \quad (3.17)$$

and the corresponding probability distribution is

$$W(t) = \begin{cases} t/6 & , t \leq 1 \text{ sec} \\ 1 - 5t^{-0.2}/6 & , t > 1 \text{ sec} \end{cases} \quad (3.18)$$

To obtain a sample from this distribution, we choose a random number, R , from the uniform distribution on $(0, 1)$ and set

$$t = W^{-1}(R) \quad (3.19)$$

Because $R = W(t)$ is a monotone, increasing, and continuous function, ordering the three random numbers, R , to satisfy

$$0 < R_1 < R_2 < R_3 \quad (3.20)$$

is equivalent to ordering the three corresponding samples, t , to satisfy Eq. (3.11). The probability densities for the minimum, middle, and maximum of three independent random numbers are

$$\begin{aligned} p_1(R) &= 3(1 - R)^2 \\ p_2(R) &= 6R(1 - R) \\ p_3(R) &= 3R^2 \end{aligned} \quad (3.21)$$

We regard $R = W(t)$ as a mapping from real time, t , to another scale time, R . In the alternative procedure, the $p_i(R)$, $i = 1, 2, 3$, are the densities of i^{th} decays in scale time, R . The corresponding rates at which the fractions n_0 , n_1 , and n_2 decrease are

$$\begin{aligned}\frac{dn_0}{dR} &= -p_1(R) \\ \frac{dn_1}{dR} &= p_1(R) - p_2(R) \\ \frac{dn_2}{dR} &= p_2(R) - p_3(R)\end{aligned}\tag{3.22}$$

Integrating Eq. (3.22) with the initial conditions (3.3) gives

$$\begin{aligned}n_0 &= (1 - R)^3 \\ n_1 &= 3R(1 - R)^2 \\ n_2 &= 3R^2(1 - R)\end{aligned}\tag{3.23}$$

By introducing three different rate functions

$$\begin{aligned}g_1(R) &= \frac{3}{1 - R} \\ g_2(R) &= \frac{2}{1 - R} \\ g_3(R) &= \frac{1}{1 - R}\end{aligned}\tag{3.24}$$

we can rewrite Eq. (3. 22) as

$$\begin{aligned}\frac{dn_0}{dR} &= -g_1(R) n_0 \\ \frac{dn_1}{dR} &= g_1(R) n_0 - g_2(R) n_1 \\ \frac{dn_2}{dR} &= g_2(R) n_1 - g_3(R) n_2\end{aligned}\tag{3. 25}$$

which is an analog of the system [Eq. (3. 7)] in the first model.

By using Eq. (3. 19) to transform Eq. (3. 25) from scale time, R , to real time, t , we get a system of differential equations of the form Eq. (3. 4) in which the rate functions are

$$\begin{aligned}f_1(t) &= \frac{3}{6-t} \\ f_2(t) &= \frac{2}{6-t} \\ f_3(t) &= \frac{1}{6-t}\end{aligned}\tag{3. 26}$$

for $0 \leq t \leq 1$ and

$$\begin{aligned}f_1(t) &= 3/5t \\ f_2(t) &= 2/5t \\ f_3(t) &= 1/5t\end{aligned}\tag{3. 27}$$

for $t > 1$. These rate functions increase for $0 \leq t \leq 1$ and decrease as $1/t$ for $t > 1$.

We adopt the procedure of Eqs. (3.18, 19, and 20) as the model for beta decays primarily because it leads to simpler computations. Moreover, the rate of successive decays decreases. For a typical fission fragment this behavior of decay rates seems intuitively plausible because of the excess of the neutron-to-proton ratio of the particle, which gives rise to its instability, decreases with successive decays.

The graphs of injection density in Ref. 10 are based upon still another prescription for the decay times. In those computations we used the relation

$$t = \left[\frac{5 \exp s}{6 + 4s + s^2} \right]^5 + \left(\frac{5}{6} \right) \left[\frac{s}{0.4 + 10s^3} - \frac{s}{1 + 10s^2} \right] \quad (3.28)$$

with

$$s = s_i = - \ln R_i, \quad i = 1, 2, 3 \quad (3.29)$$

to compute the decay times. Ordering the random numbers R_i , chosen from the uniform distribution on $(0, 1)$, to satisfy

$$0 < R_3 < R_2 < R_1 < 1 \quad (3.30)$$

insures that the t_i increase with i . Equation (3.28) is an analytic approximation for the two relations in Eq. (3.15).

For a triple of random numbers ordered as in Eq. (3.30), $s_3 = - \ln R_3$ is the largest value produced by Eq. (3.29); for the same triple, $s_3 = - (\ln R_1 + \ln R_2 + \ln R_3)$ is the largest value produced by Eq. (3.12). Thus it is clear that the third decay times produced by the prescription of Eqs. (3.28), (3.29), and (3.30) must be smaller than those produced by the prescription of Eqs. (3.12) and (3.15).

What is true for third decays holds in general: the total distribution of decay times, without regard for decay number, produced by the present prescription has many more early times and for fewer late times than do the distributions produced by the two previous prescriptions, which approximate the Way-Wigner law.

Figures 1 and 2 show, for two sets of parameters, the variation of injection density with distance for the three prescriptions for the decay times; Figures 3 and 4 show the variation of injection density with altitude for the same data. With 2.5×10^4 histories, the results obtained from Eqs. (3.12) and (3.15) are almost identical with those obtained from Eqs. (3.18), (3.19), and (3.20). The effect of the preponderance of early decay times in the third prescription, Eqs. (3.28), (3.29), and (3.30), is to suppress the tails and to accentuate the central peak in the distributions of injection density.

We observe that the parameter change (increasing the velocity) broadens the central peak for all prescriptions and that the broadening is greatest for the third prescription.

The discussion of the relative influence of the various parameters in Section 3 of Ref. 10 is based upon the comparative shapes of the injection density curves and is facilitated by using the third prescription to magnify these effects. On the other hand effects which occur at late times are minimized by the third prescription. Our computations suggest that the assumption of a uniform decay rate, the first prescription, also tends to obscure effects occurring at late times. Consequently, for statistics concerning effects at late times, we recommend the second prescription for decay times, Eqs. (3.18), (3.19), and (3.20). This second prescription is in the current version of the code.

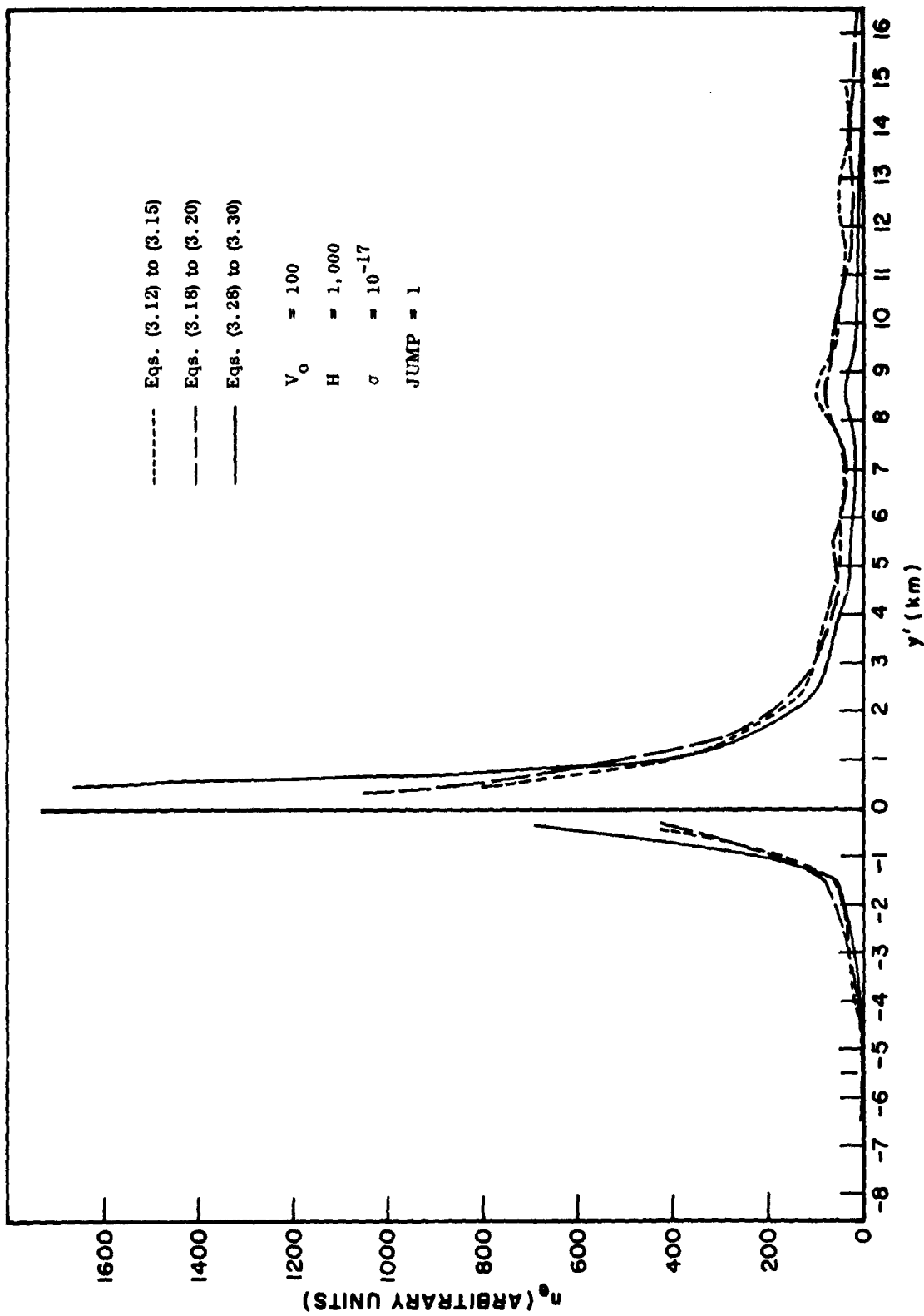


Fig. 1 Variation of Injection Density With Distance for Different Prescriptions of Decay Times

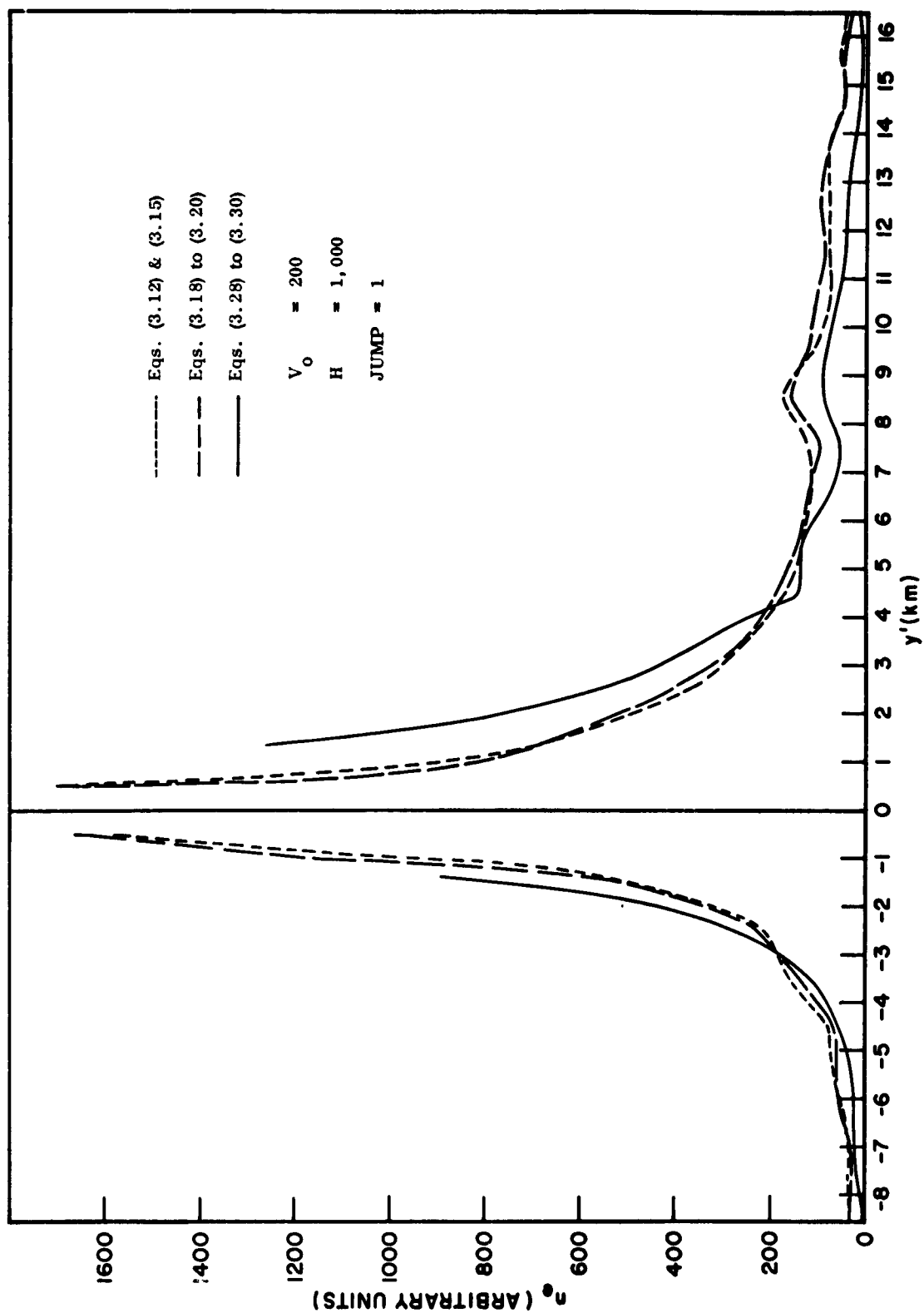


Fig. 2 Variation of Injection Density With Distance for Different Prescriptions of Decay Times

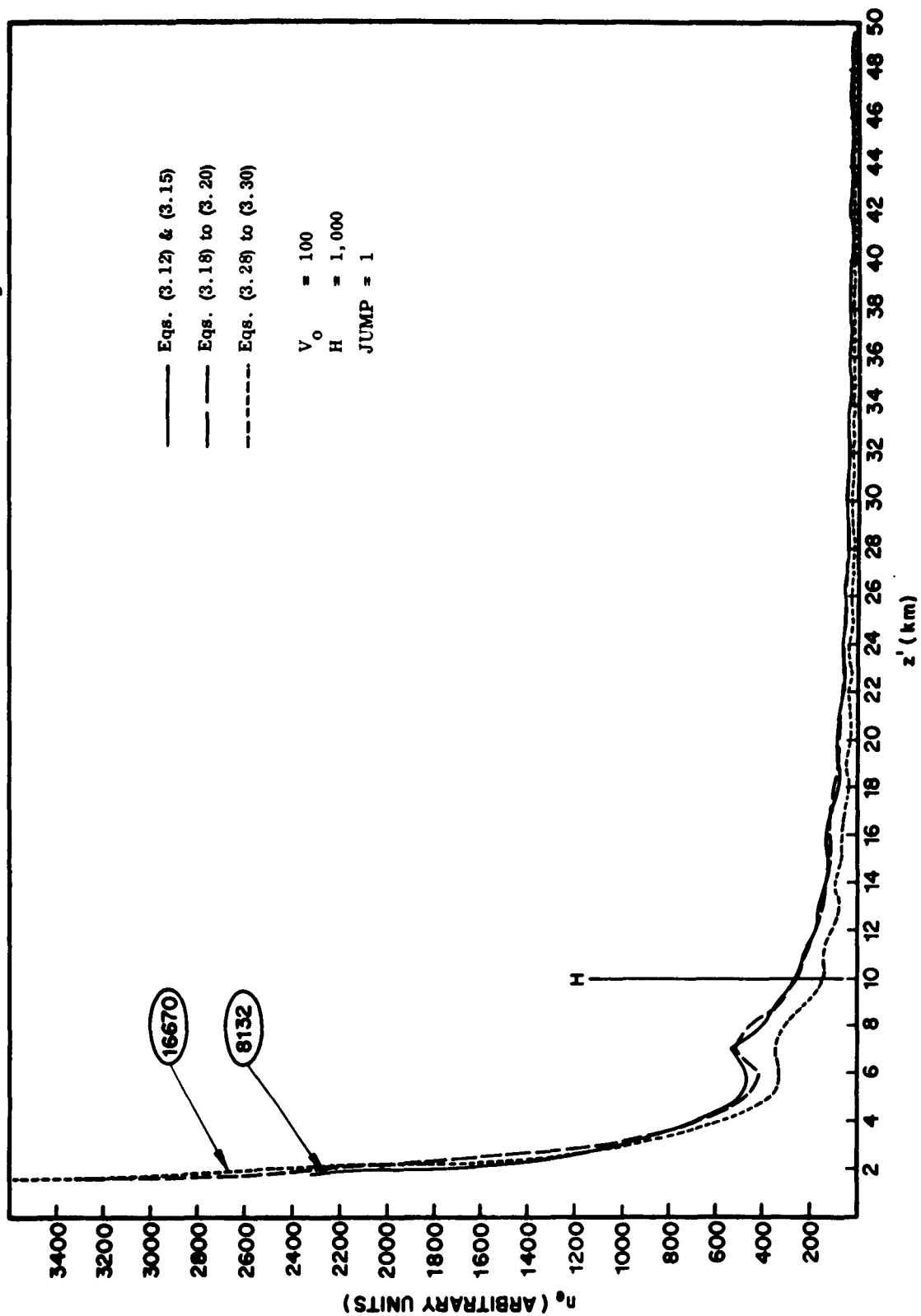


Fig. 3 Variation of Injection Density With Altitude for Different Prescriptions of Decay Times

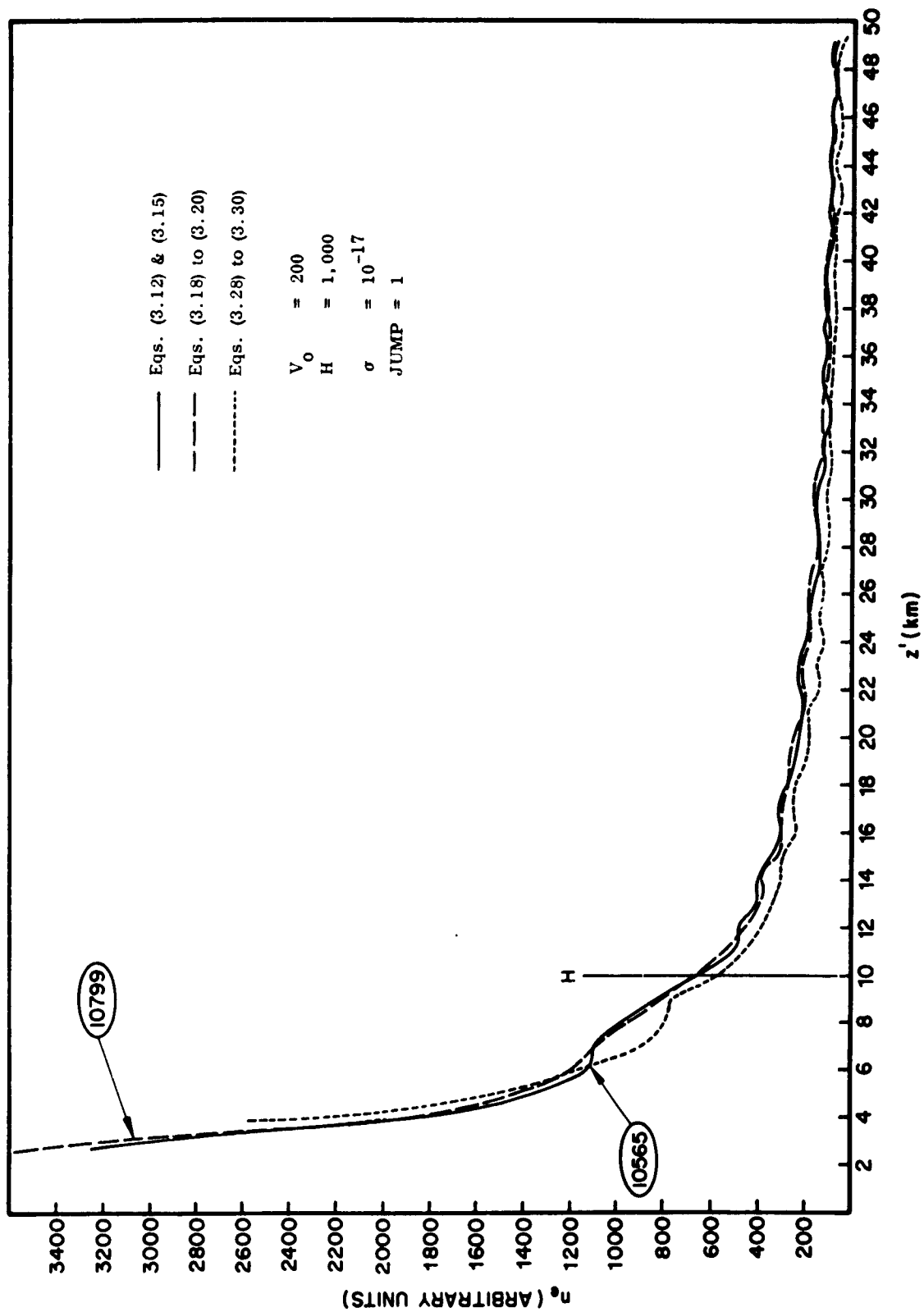


Fig. 4 Variation of Injection Density With Altitude for Different Prescriptions of Decay Times

Section 4
IBM 7090 CODE FOR THE MONTE CARLO MODEL

The fraction of the beam which is ionized is a free parameter and constitutes one of the input constants of the problem. A random number chosen between 0 and 1, compared with this fraction, decides whether the particle considered is neutral or ionized. From then on, a special counter (I) keeps track of the charge on the particle.

The three decay times are computed from three random numbers chosen independently from a uniform distribution on (0, 1) and then ordered to satisfy

$$0 < R_1 < R_2 < R_3 < 1 \quad (4.1)$$

The decay times are obtained by the prescription, derived from Eqs. (3.18) and (3.17),

$$t_i = \begin{cases} 6R_i & , \text{ if } R_i \leq 1/6 \\ \left[\frac{5}{6(1-R_i)} \right]^5 & , \text{ if } R_i > 1/6 \end{cases} \quad (4.2)$$

A particle initially neutral is taken as traveling in a straight line in a direction chosen from a uniform distribution on a hemisphere. Figure 1 shows the coordinates of the particle with θ and φ taken as uniformly distributed between 0 and π ; and 0 and 2π , respectively. On ionization by collision or beta decay, the particle is constrained to spiral about the magnetic field line passing through the point at which ionization occurs, thus neglecting the lateral displacement equal to the radius of gyration. Because the latter is an order of magnitude lower than the mean free path, the resultant error in the coordinates of the fragment will, on the average, be negligible. To follow the motion of the ionized particles, we go to a coordinate system in which the z' -axis is parallel to the magnetic field through the origin. In this (magnetic coordinate) system, the polar angle of the particle position θ' is also its pitch angle.* For the geometry of Fig. 5 we get

$$\cos \theta' = \cos \theta \cos \theta_0 - \sin \theta \sin \theta_0 \sin \varphi \quad (4.3)$$

$$\cos \varphi' = (\sin \theta / \sin \theta') \cos \varphi \quad (4.4)$$

Also, from the figure, we see that if the particle moves a distance ds along the spiral it will rise through a verticle distance given by

$$dz = ds \cos \theta' \cos \theta_0 \quad (4.5)$$

This equation, which is the same as Eq. (2.51), is used to obtain the effective path length, because, in spiralling, the ionized particle has a greater probability of collision than a neutral particle moving through the same verticle distance. The ionized particle remains on the spiral until it is slowed down to rest, neutralized by collision, or ceases to be of interest because it has decayed three times. If it remains on the spiral, it is followed to the conjugate point. The coordinates of every decay point are noted, but the motion of the ionized particle remains unaffected.

*For initially ionized particles, θ' is chosen from a uniform distribution on a hemisphere with the polar axis parallel to the magnetic field, and the calculation proceeds as above.

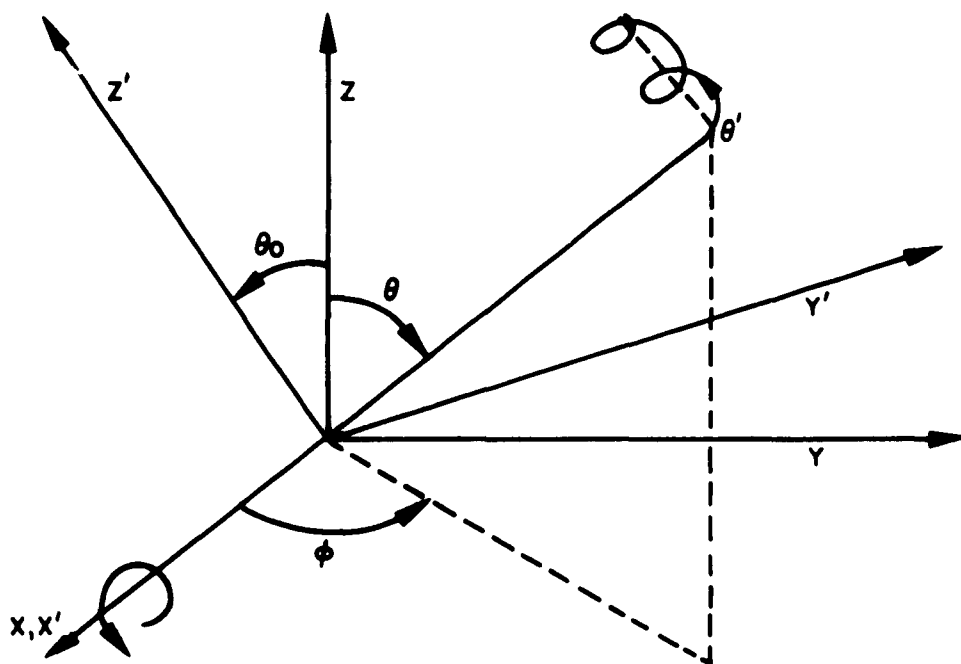


Fig. 5 Coordinate Systems Used

Throughout its passage through the atmosphere the particle's velocity is reduced according to Eq. (1.21) until it escapes with the velocity it has at the altitude H . Let v_{n-1} , v_n and p_{n-1} , p_n be the values of the velocity and pressure at any two consecutive points z_{n-1} , z_n along the path. Generalizing Eq. (1.21), we have

$$v_n^2 = v_{n-1}^2 + \frac{2kA'}{Mg \cos \theta} (p_{n-1} - p_n) \quad (4.5)$$

Similarly, generalizing Eq. (2.40) yields

$$p_n = p_{n-1} + \frac{Mg \cos \theta}{\sigma_i A'} \ln R \quad (4.6)$$

where use has been made of Eq. (2.6). Combining Eqs. (4.5) and (4.6) gives the alternative form for the slowing down law:

$$v_n^2 = v_{n-1}^2 + \frac{2k}{\sigma_i} \ln R \quad (4.7)$$

In the code we use the notation,

$$\frac{Mg \cos \theta}{A' \sigma_i} = A_i, \quad \frac{2kA'}{Mg \cos \theta} = B, \quad \text{and} \quad \frac{2k}{\sigma_i} = C_i \quad (4.8)$$

We note the appearance of the inelastic collision cross section σ_i in Eq. (4.7), although the corresponding collisions are ignored as sources of energy loss. The explanation is immediate if we remember that the slowing down of a particle must be proportional to its path length. The effect of different types of inelastic collision cross sections can be studied by varying the constants A_i and C_i . The effect of various elastic collision cross sections could be investigated by varying k in the constants B and C_i .

A collision with an atmospheric atom reduces the charge on the particle by unity, the probability for electron capture being definitely greater than that for loss because of

the relatively high values of the ionization potentials beyond the first. The motion of the neutralized particle is followed by reverting to the unprimed coordinate system by means of the transformation inverse to Eqs. (4.3) and (4.4), viz.,

$$\cos \theta = \cos \theta' \cos \theta_0 + \sin \theta' \sin \theta_0 \sin \theta', \quad (4.9)$$

$$\cos \theta = (\sin \theta' / \sin \theta) \cos \theta' \quad (4.10)$$

where θ' is the azimuthal angle in the magnetic coordinate system and is chosen from a uniform distribution between 0 and π .

Decays and inelastic collisions are independent, and therefore the time intervals to decays and collisions are used to determine which event occurs first. By means of a random number, the pressure at the point of collision is determined; the pressure is a known function of the altitude which can be determined from the tables reproduced for convenience, in Section 6. Hence, the distance travelled and the time to cover this distance are found, and this time is compared with the time to first decay. If the time to decay is shorter, the time to collision is reduced by this amount and the residue compared with the time to second decay. If the time to collision is shorter, the time to first decay is reduced, and a new collision time is calculated and compared with it.

The need for two slowing down equations arises as follows. Consider a neutral particle at a starting point z_{n-1} and suppose it is to undergo an ionizing collision at a point z_n . We determine p_n and hence v_n by either Eq. (4.5) or Eq. (4.7). Suppose, however, we find that a decay will occur enroute to z_n , at z'_n . There is no direct method of determining this point and so we proceed in the following way: we calculate the average velocity from z_{n-1} to z_n and, with the time to decay, find the path length to z_n and hence z'_n and p'_n . To proceed with the history we require v'_n . It would clearly be very inaccurate to use v_n or the above average because the point z'_n can be far below z_n and very close to z_{n-1} . Equation (4.7) is now useless and we have to use Eq. (4.5).

At each calculation of the collision time, the new pressure is compared with that at the altitude H to determine whether the particle escapes from the atmosphere. Neutral particles which would escape are checked for possible decays before they could do so, because in case of decay, their path in the atmosphere is lengthened, they are slowed down more, and might even be stopped. Neutral particles which do escape are checked for decays up to the altitude of 20,000 km above which they are considered to be lost.

The calculation thus proceeds step by step until the history of a particle is terminated by one of the following:

- three decays
- loss at the conjugate point
- loss in atmosphere by slowing down to rest
- loss in atmosphere by scattering in the backward direction
($\cos \theta$ or $\cos \theta'$ negative in Eq. (4.4) or (4.9))
- loss by escaping from the atmosphere and traveling out of region of interest (neutral or neutralized particles only)

The code is set out in eight blocks of instructions, each designed to cover a particular aspect of a particle's history according to the following scheme:

<u>Instruction Set No.</u>	<u>Function</u>
100	Initialization
200	Collision Routine for Neutral Particles (CN)
300	Collision Routine for Ionized Particles (CI)
400	Decay Routine for Neutral Particles (DN)
500	Decay Routine for Ionized Particles (DI)
600	Escape Routine for Neutral Particles (EN)
800	Escape Routine for Ionized Particles (EI)
6600	Escape Routine for Neutral Particles with zero ionization cross section (EN [*])

The details of all the steps involved are shown in the flow charts of Figs. 6 through 16.

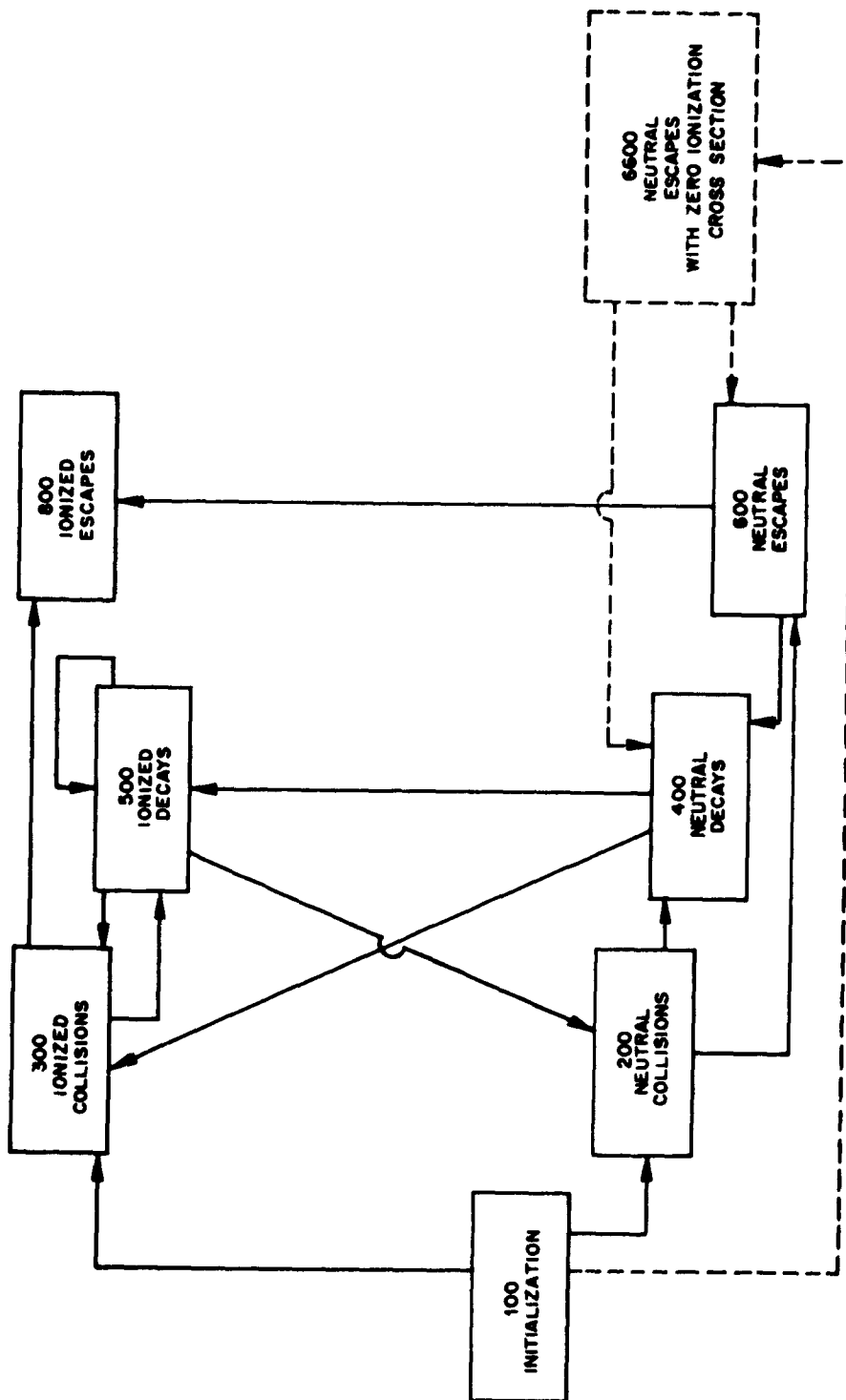


Fig. 6 Some Possible History Paths in Terms of the Coding Blocks. (Dashed lines refer to initial stages of calculations with zero ionization cross sections. Subroutines, exits, and history terminations not shown for clarity.)

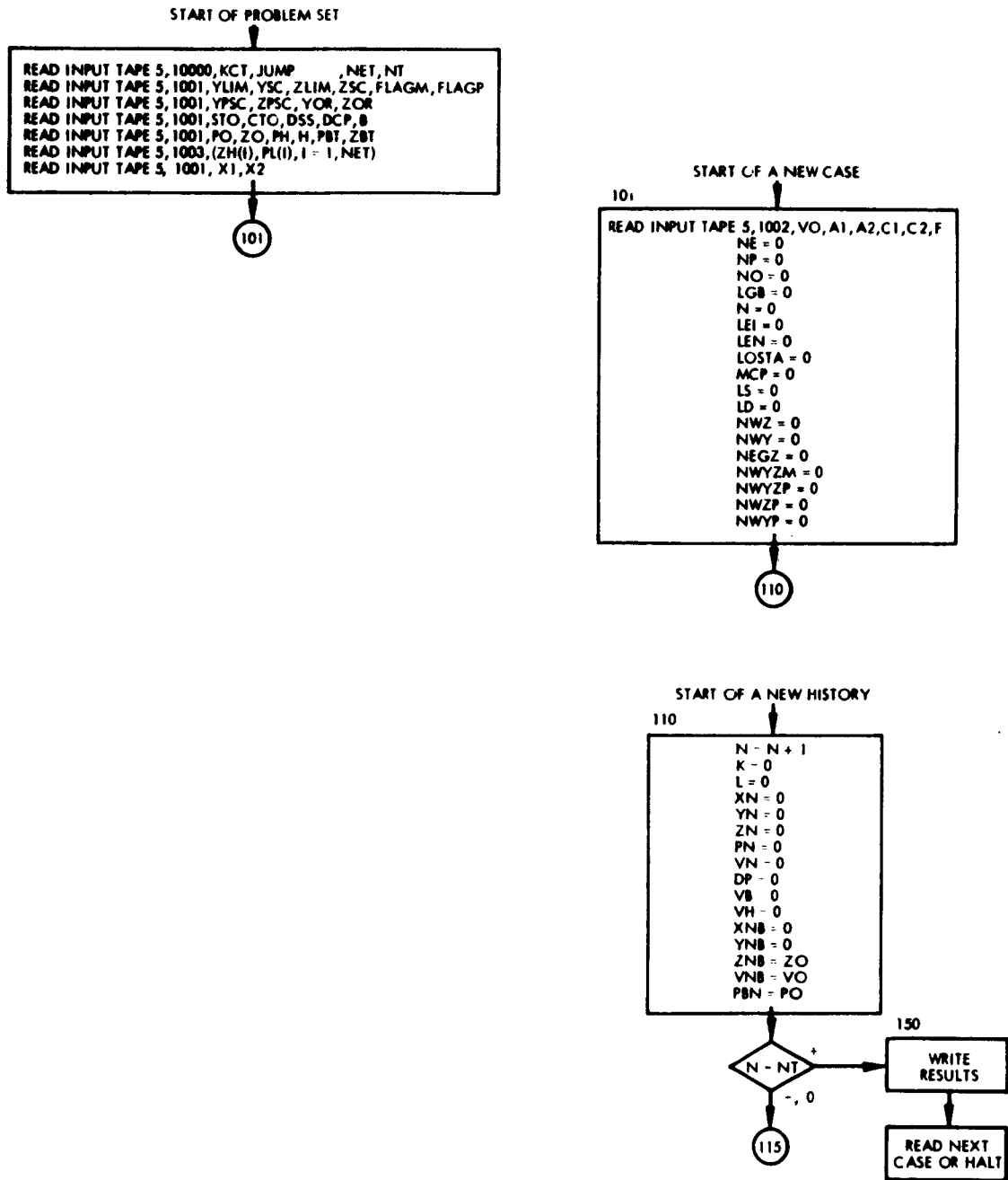


Fig. 8 Initialization Flow Chart

CALCULATION OF DECAY TIMES

Eqs. (3.28, 29, and 30)

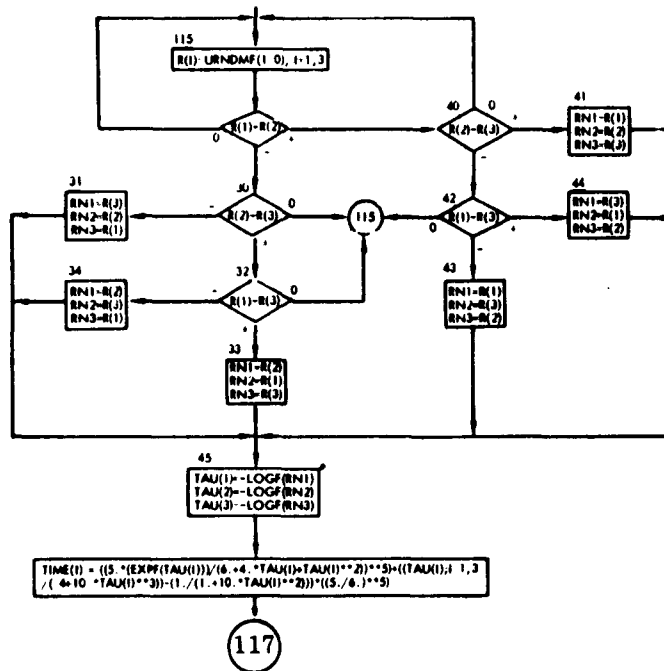


Fig. 9a Decay Times Flow Chart (used in production runs for Ref. 10)

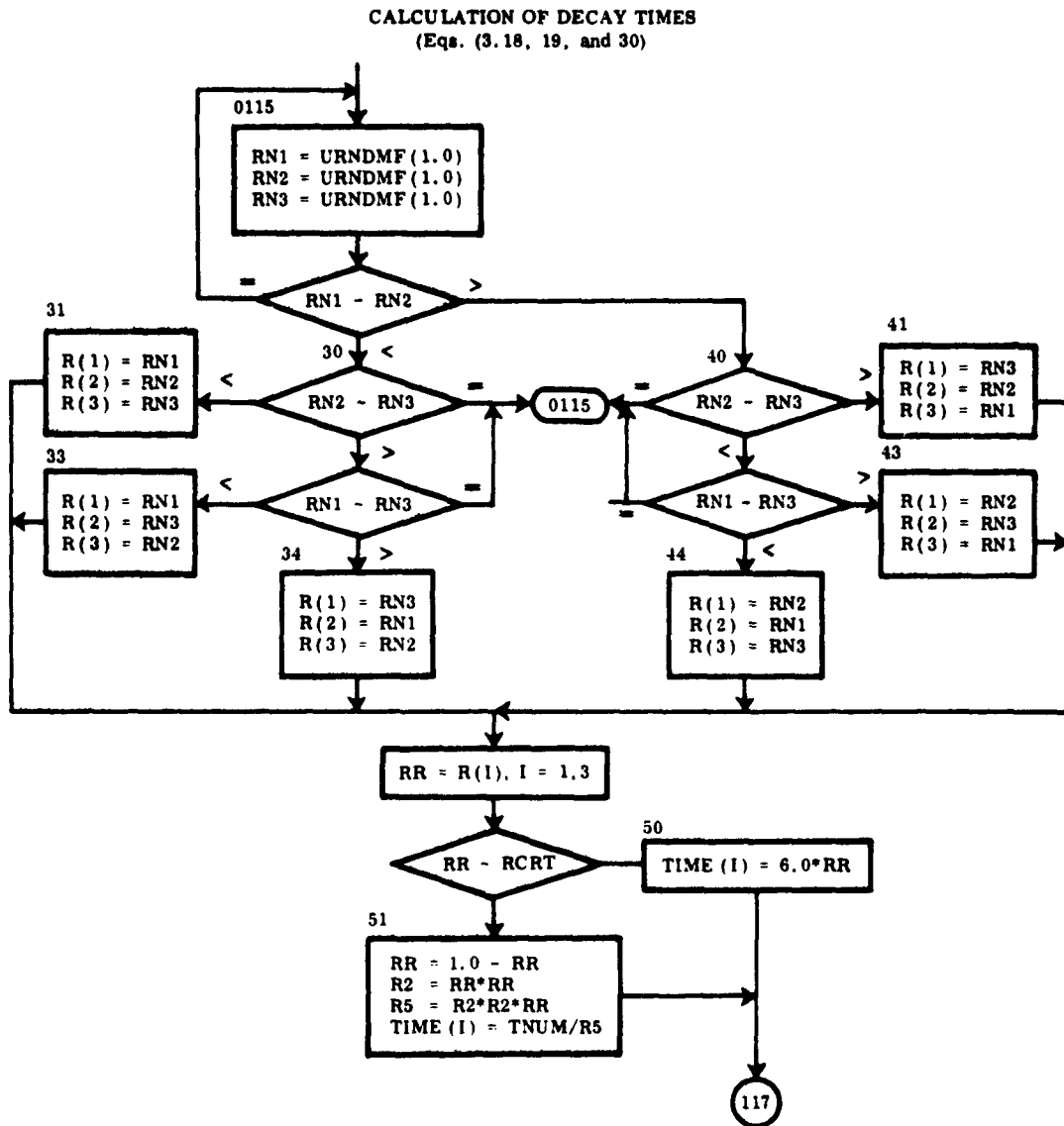


Fig. 9b Decay Times Flow Chart Yielding Correct Late Time Effects

CALCULATION OF REDUCED TIMES AND INITIAL CONDITIONS

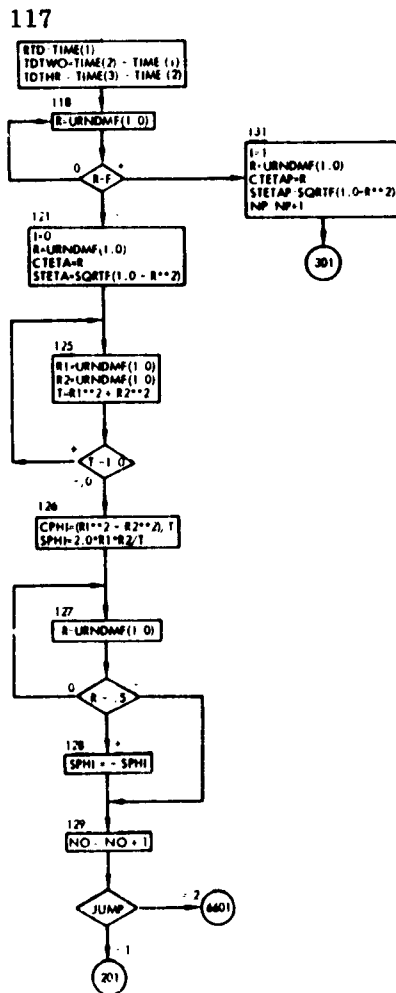


Fig. 9c Decay Times Flow Chart (completion)

CALCULATION OF TIMES TO COLLISION OF NEUTRAL PARTICLES

201

$RN = \text{URNDMF}(1.0)$
 $PN = PNB + A1 * CTETA * \text{LOGF}(RN)$

PN - PH
 0, -
 +

601

INTERPOLATE FOR ALTITUDE
 IN PRESSURE TABLE (5600)

203

$DZO = ZN - ZNB$
 $DSO = DZO / CTETA$
 $DXO = DSO * STETA * CPHI$
 $DYO = DSO * STETA * SPHI$
 $YN = YNB + DYO$
 $XN = XNB + DXO$
 $T = VNB^2 + C1 * \text{LOGF}(RN)$

T
 -1.0
 +

214

$NE = NE + 3 - L$
 $LOSTA = LOSTA + 1$

110

220

$VN = \text{SQRTF}(T)$
 $VB = 0.5 * (VN + VNB)$
 $RTC = DSO / VB$

401

GENERAL ERROR EXIT

250

WRITE DIAGNOSTIC
 OUTPUT

HALT

Fig. 10 Neutral Collision Flow Chart

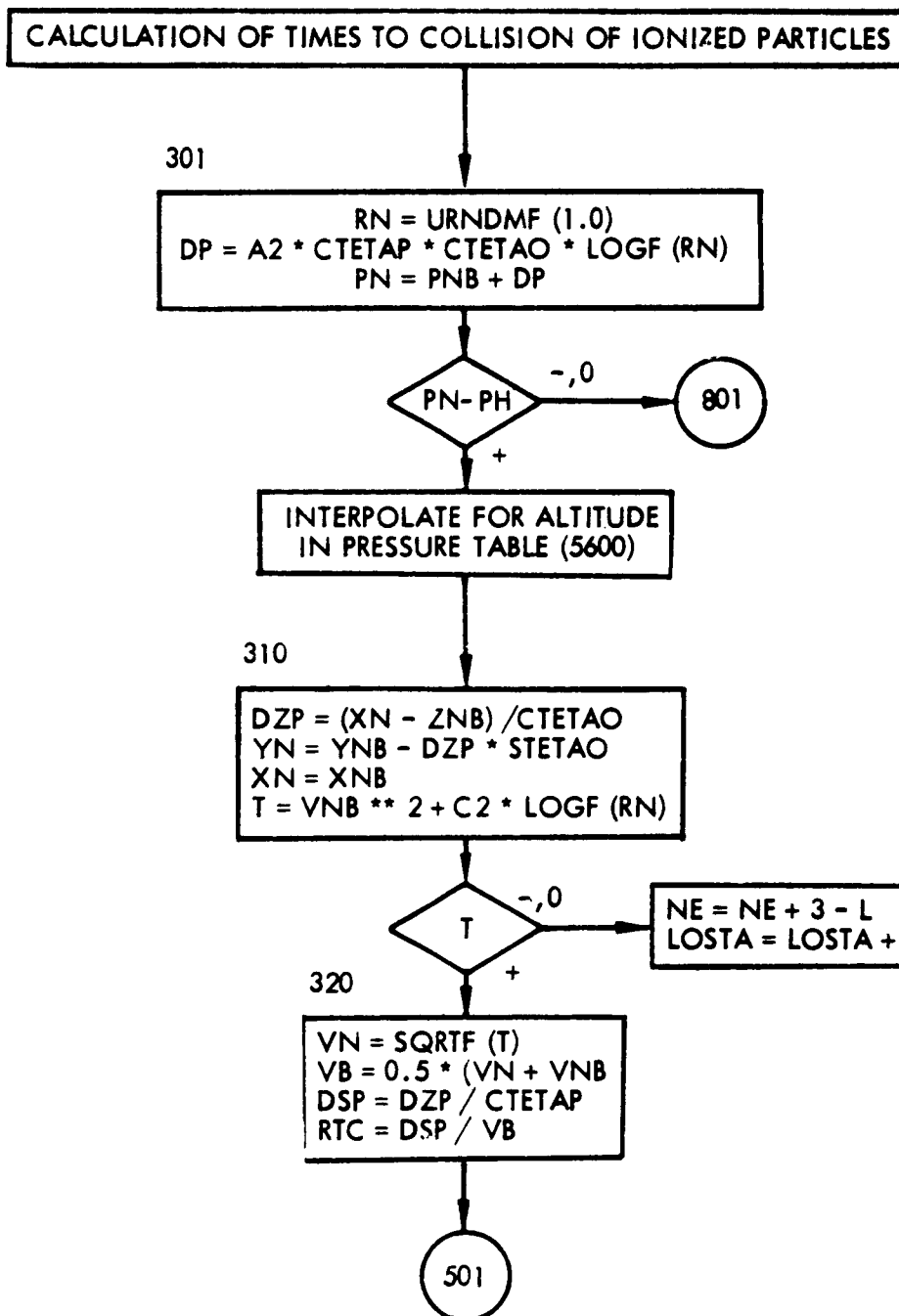


Fig. 11 Ionized Collision Flow Chart

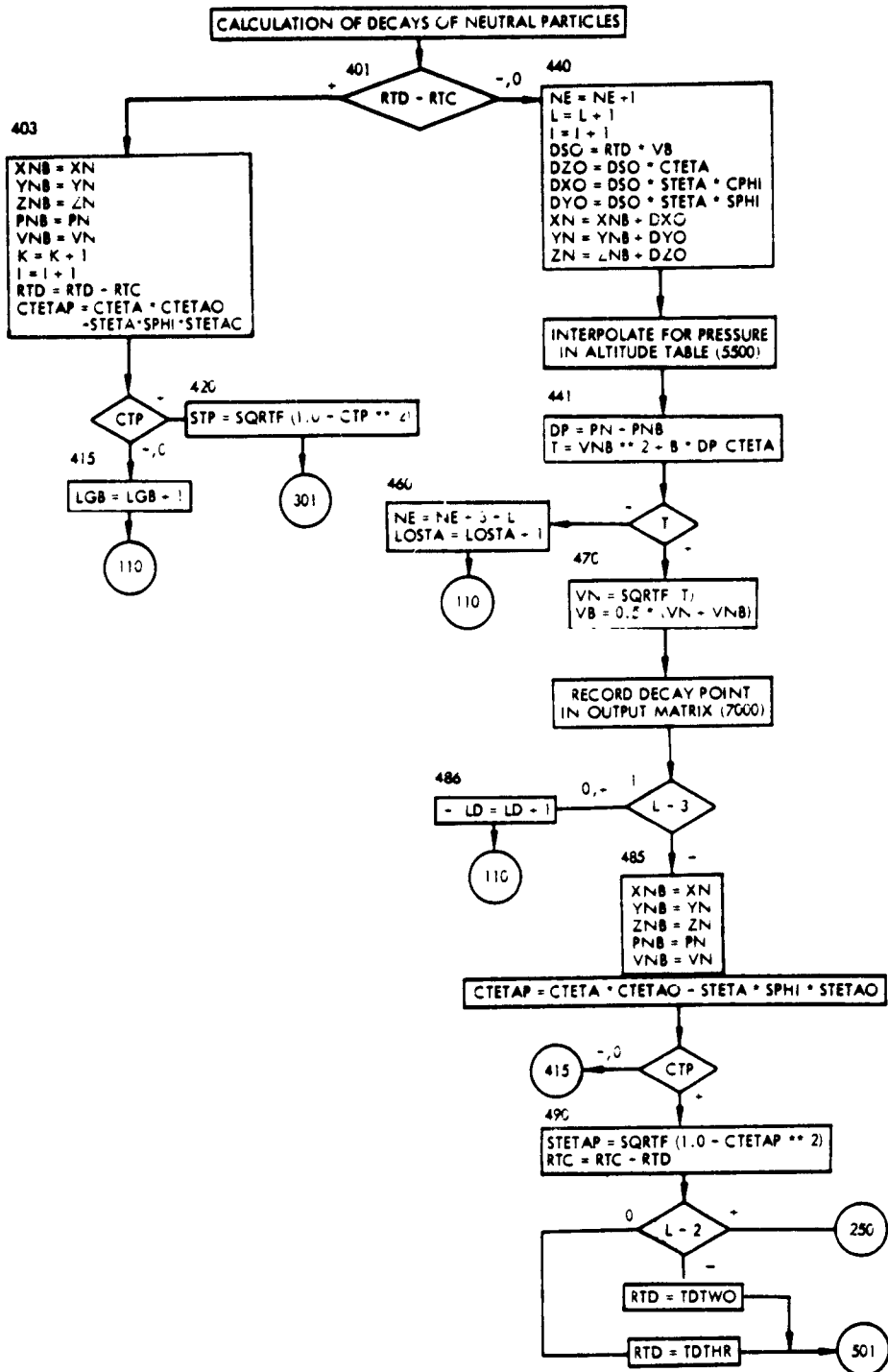


Fig. 12 Neutral Decay Flow Chart

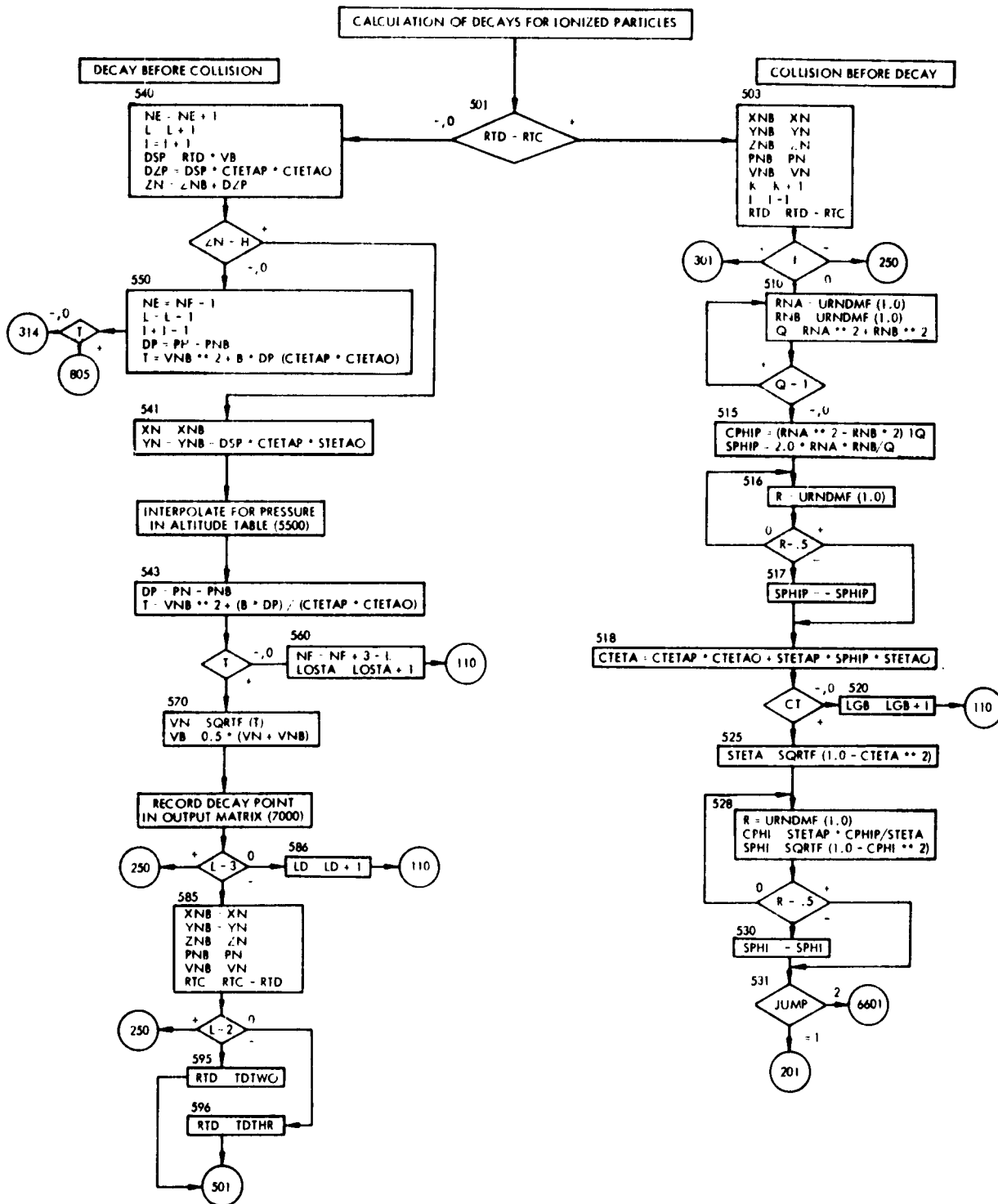


Fig. 13 Ionized Decay Flow Chart

ESCAPE ROUTINE FOR NEUTRALS WITH ZERO IONIZATION CROSS-SECTION

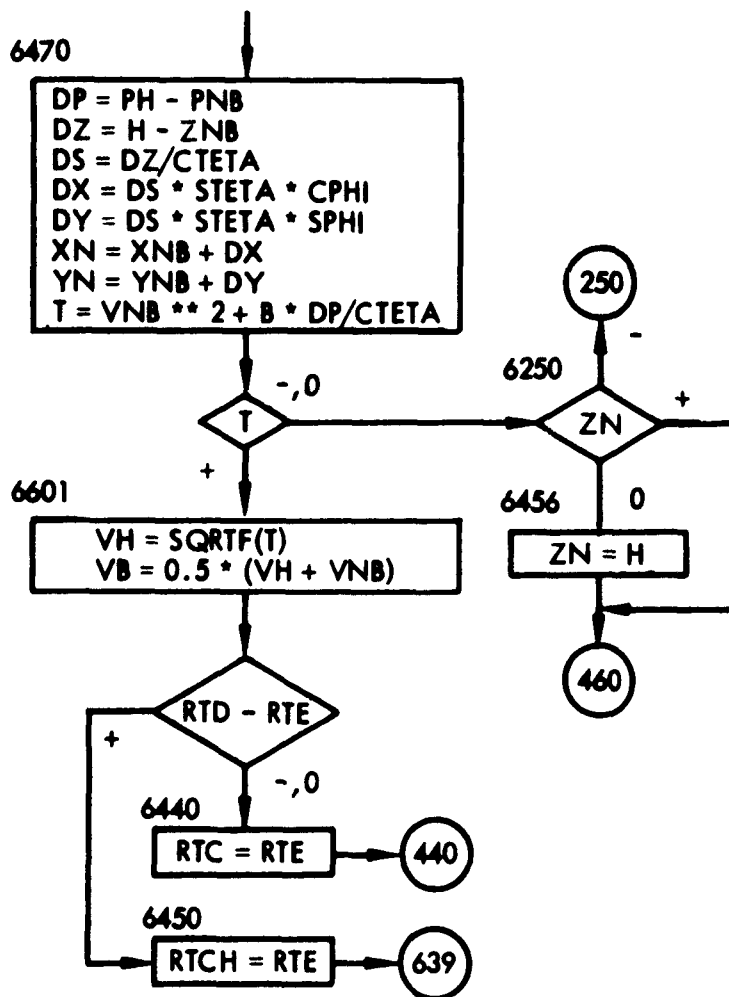


Fig. 16 Neutral Escape ($\sigma_i = 0$) Flow Chart

Section 5

FORTRAN LISTING AND SAMPLE PROBLEM

This is the final version of the code using Eqs. (3.18), (3.19), and (3.20) for the decay times. This version gives correct late time effects.

```

*      FORTRAN                                00002
C      207-85  ORMONDE  X45343  DEMO FINAL VERSION
C      CHANGED PROGRAM TO USE TWO SIGMAS FOR EACH CASE W/COLUMN ONE OF NEGA-
C      TIVE MATRIX NONE ZERO  AUGUST 14, 1962
C      DEMO WITH BOTH PLOT AND MATRIX 5-31-62  BACKWARD TEST IS IN 00003
C      MONTE CARLO FOR DEMO  MAIN PROGRAM ORMONDE 52-10 X45219 00004
C      NEW NAME OLD NAME  DESCRIPTION 00005
C      KCT KOUNTY TOTAL CARD COUNT 00006
C      JUMP INDICATOR-CROSS-SECTION 00007
C      NO NUMBER OF NEUTRAL PARTICLES (N ZERO) 00008
C      NP NUMBER OF IONIZED PARTICLES (N+) 00009
C      FRI F FRACTION NEUTRAL 00010
C      NET N6 NUMBER OF ENTRIES IN TABLE 00011
C      NTP NT TOTAL NUMBER OF PARTICLES 00012
C      KCS KOUNT CARD COUNT FLAG 00013
C      CTO CTETAO COSINE THETA ZERO 00014
C      STO STETAO SIN THETA ZERO 00015
C      CTP CTETAP COSINE THETA PRIME 00016
C      STP STETAP SIN THETA PRIME 00017
C      CT CTETA COSINE THETA 00018
C      ST STETA SIN THETA 00019
C      CP CPHI COSIN PHI 00020
C      SP SPHI SIN PHI 00021
C      CPP CPHIP COSINE PHI PRIME 00022
C      SPP SPHIP SIN PHI PRIME 00023
C      00024
C      00025
C      00026
C      00027
C      00028
C      DIMENSION T(3)
C      DIMENSION R(3),TAU(3),TIME(3),ZH(50),PL(50),S(3)
C      DIMENSION MP(19,50),MN(19,50)
C      DIMENSION ISUMMP(19),ISUMMN(19),IROW(50)
C      EQUIVALENCE (KCT,KOUNTY),(FRI,F), (KCS,KOUNT),(CTETAO,CTO) 00031
C      1,(STETAO,STO),(CTETAP,CTP),(STETAP,STP),(CTETA,CT),(STETA,ST),(SPH 00032
C      2,SP),(CPHI,CP),(CPHIP,CPP),(SPHIP,SPP) 00033
1000  FORMAT (12I6) 00034
1001  FORMAT (6F12,0) 00035
1002  FORMAT (6E12,8) 00036
1003  FORMAT (2E12,8) 00037
1007  FORMAT(11H ,8I8)
1008  FORMAT(11H 4X,3HLGB5X,3HLEN5X,3HLE15X,3HMCP6X,2HLS5X,2HLD6X,5HLOST)
1010  1) 00040
1010  FORMAT (6H1 NO=16,5H NP=16,6H NWY=16,6H NWZ=16,7H NWYP=16, 00041
1010  17H NWZP=16,8H NWYZM=16,8H NWYZP=16,7H NEGZ=16) 00042
1011  FORMAT(11H 7X,2HVO14X,2HPP15X,1HML15X,2HA115X,2HA215X,2HC115X,2HC2) 00044
1012  FORMAT (6E16,8,I5)
1013  FORMAT(11H 7X,2HZO14X,4HYLIM11X,3HYSC12X,4HZLIM11X,3HZSC15X,1HBI0X,
1013  14HJUMP)
1014  FORMAT(5E17,8) 00046
1015  FORMAT(7E16,8)
1016  FORMAT(1HC)
1021  FORMAT (40H0 HISTOGRAM FOR POSITIVE VALUES OF Y ) 00047

```

```

1022 FORMAT(1H ,1916)
1023 FORMAT (40H1 HISTOGRAM FOR NEGATIVE VALUES OF Y )
      READ INPUT TAPE 5,1000,KCT,JUMP,NET,NT
      READ INPUT TAPE 5,1001,YLIM,YSC,ZLIM,ZSC,FLAGM,FLAGP
      READ INPUT TAPE 5,1001,YPSC,ZPSC,YOR,ZOR
      READ INPUT TAPE 5,1001,STO,CTO,DSS,DCP,B
      READ INPUT TAPE 5,1001,PO,ZO,PH,H,PBT,ZBT
      READ INPUT TAPE 5,1003,(ZH(I),PL(I),I=1,NET)
      READ INPUT TAPE 5, 1001, X1,X2
      DUMMY=INTRMF(X1,X2)
      KOUNT=0
      REWIND 27
      RYPSC=1.0/YPSC
      RZPSC=1.0/ZPSC
      TNUM=(5./6.)**5
      RCRT=1./6.
C
C
C
C
C
C
C
C
C
C*****00062
C*****00063
C*****00064
C*****00065
C*****00066
C*****00067
C*****00068
C*****00069
C*****00070
C*****00071
C*****00072
C*****00073

```

```

C*****START OF A NEW CASE*****00074
C*****00075
101 READ INPUT TAPE 5,1002,VO,A1,A2,C1,C2,F
      NE=0
      NP=0
      NO=0
      LGB=0
      N=0
      LEI=0
      LEN=0
      LOSTA=0
      MCP=0
      LS=0
      LD = 0
      NWZ=0
      NWY=0
      NFGZ=0
      NWYZM=0
      NWYZP=0
      NWZP=0
      NWYP=0
C*****00077
C*****00078
C*****00079
C*****00080
C*****00081
C*****00082
C*****00083
C*****00084
C*****00085
C*****00086
C*****00087
C*****00088
C*****00089
C*****00090
C*****00091
C*****00092
C*****00093
C*****START OF A NEW HISTORY*****00094
C*****00095
C*****00096
110      N=N+1
      K=0
      L=0
      XN=0
C*****00097
C*****00098
C*****00099
C*****00100

```

	YN=0	00101
	ZN=0	00102
	PN=0	00103
	VN=0	00104
	DP=0	00105
	VB=0	00106
	VH=0	00107
	XNB=0	00108
	YNB=0	00109
	ZNB=Z0	00110
	VNB=V0	00111
	PNB=PN	00112
		00113
C	*****HAVE NT PARTICLES BEEN PROCESSED*****	00114
C		00115
	IF(N-NT)0115,0115,0150	00116
C	*****	00117
C	*****END OF CASE*****	00118
C	*****	00119
150	CONTINUE	00120
	DO 152 IY=1,19	
	ISUMMP(IY)=0	
	ISUMMN(IY)=0	
	DO 152 IZ=5,40	
	ISUMMP(IY)=MP(IY,IZ)+ISUMMP(IY)	
	ISUMMN(IY)=MN(IY,IZ)+ISUMMN(IY)	
152	CONTINUE	
	DO 155 IZ=1,50	
	IROW(IZ)=0	
	DO 155 IY=1,19	
	IROW(IZ)=IROW(IZ)+MP(IY,IZ)+MN(IY,IZ)	
155	CONTINUE	
	WRITE OUTPUT TAPE 6,1010,NC,NP,NWY,Nv7,NWYP,NWZP,NwYZM,NxYZP,NEGZ	00121
	WRITE OUTPUT TAPE 6,1008	00122
	WRITE OUTPUT TAPE 6,1007,LGB,LEN,LEI,MCP,LS,LD,LOSTA	00123
	WRITE OUTPUT TAPE 6,1015,V0,PH,H,A1,A2,C1,C2	00124
	WRITE OUTPUT TAPE 6,1012,Z0,YLIM,YSC,ZLIM,ZSC,B,JUMP	00126
	WRITE OUTPUT TAPE 6,1021	00128
	WRITE OUTPUT TAPE 6,1022,MP	00129
	WRITE OUTPUT TAPE 6,1023	00130
	WRITE OUTPUT TAPE 6,1022,MN	00131
	WRITE OUTPUT TAPE 6, 1016	
	WRITE OUTPUT TAPE 6, 1022, ISUMMP	
	WRITE OUTPUT TAPE 6, 1022, ISUMMN	
	WRITE OUTPUT TAPE 6, 1022, IROW	
	DO 8000 I=1,19	
	DO 8000 J=1,50	
	MN(I,J)=0	00133
	MP(I,J)=0	00134
8000	CONTINUE	00135
	END FILE 27	00136

```

                                YN=0                                00101
                                ZN=0                                00102
                                PN=0                                00103
                                VN=0                                00104
                                DP=0                                00105
                                VD=0                                00106
                                VH=0                                00107
                                XNB=0                               00108
                                YNB=0                               00109
                                ZNB=Z0                             00110
                                VNR=V0                             00111
                                PNB=P0                             00112
C *****HAVE NT PARTICLES BEEN PROCESSED***** 00113
C                                00114
                                IF(N-NT)0115,0115,0150          00115
C *****END OF CASE***** 00116
C ***** 00117
C ***** 00118
C ***** 00119
150 CONTINUE 00120
    DO 152 IY=1,19
      ISUMMP(IY)=0
      ISUMMN(IY)=0
      DO 152 IZ=5,40
        ISUMMP(IY)=MP(IY,IZ)+ISUMMP(IY)
        ISUMMN(IY)=MN(IY,IZ)+ISUMMN(IY)
152 CONTINUE
    DO 155 IZ=1,50
      IROW(IZ)=0
      DO 155 IY=1,19
        IROW(IZ)=IROW(IZ)+MP(IY,IZ)+MN(IY,IZ)
155 CONTINUE
      WRITE OUTPUT TAPE 6,1010,NC,NP,NWY,NvZ,NxYP,NWZP,NwYZM,NxYZP,NEGZ 00121
      WRITE OUTPUT TAPE 6,1008 00122
      WRITE OUTPUT TAPE 6,1007,LGB,LEN,LEI,MCP,LS,LD,LOSTA 00123
      WRITE OUTPUT TAPE 6,1015,VO,PH,H,A1,A2,C1,C2 00124
      WRITE OUTPUT TAPE 6,1012,ZO,YLIM,YSC,ZLIM,ZSC,B,JUMP 00126
      WRITE OUTPUT TAPE 6,1021 00128
      WRITE OUTPUT TAPE 6,1022,MP 00129
      WRITE OUTPUT TAPE 6,1023 00130
      WRITE OUTPUT TAPE 6,1022,MN 00131
      WRITE OUTPUT TAPE 6, 1016
      WRITE OUTPUT TAPE 6, 1022, ISUMMP
      WRITE OUTPUT TAPE 6, 1022, ISUMMN
      WRITE OUTPUT TAPE 6, 1022, IROW
      DO 8000 I=1,19
      DO 8000 J=1,50
        MN(I,J)=0 00133
        MP(I,J)=0 00134
      CONTINUE 00135
8000 00136
      END FILE 27

```

	KOUNT=KOUNT+1	00138
0151	IF (KOUNT-KOUNTY)101,151,151	00139
	JUMP=2	00140
	GO TO 0101	00141
C		00142
C		00143
C		00144
C		00145
C		00146
C		00147
C		00148
C		00149
C		00150
C		00151
C		00152
C	*****	00153
C	*****CALCULATION OF DECAY TIMES*****	00154
C	*****	00155
0115	RN1=URNDMF(1.0)	00158
	RN2=URNDMF(1.0)	00159
	RN3=URNDMF(1.0)	00160
30	IF(RN1-RN2)30,0115,40	00161
31	IF(RN2-RN3)31,0115,32	00162
	R(1)=RN1	00163
	R(2)=RN2	
	R(3)=RN3	00165
	GO TO 45	00166
32	IF(RN1-RN3)33,0115,34	00167
33	R(1)=RN1	00168
	R(2)=RN3	00169
	R(3)=RN2	00170
	GO TO 45	00171
34	R(1)=RN3	00172
	R(2)=RN1	00173
	R(3)=RN2	00174
	GO TO 45	00175
40	IF(RN2-RN3)42,0115,41	00176
41	R(1)=RN3	00177
	R(2)=RN2	00178
	R(3)=RN1	00179
	GO TO 45	00180
42	IF(RN1-RN3)44,0115,43	00181
43	R(1)=RN2	00182
	R(2)=RN3	00183
	R(3)=RN1	00184
	GO TO 45	00185
44	R(1)=RN2	00186
	R(2)=RN1	00187
	R(3)=RN3	00188
45	DO 0117 I=1,3	00189
	RR=R(I)	
	IF(RR-RCRT) 50,50,51	
50	TIME(I)=6.*RR	
	GO TO 0117	00193
51	RR=1.-RR	
	R2=RR*RR	
	R5=R2*R2*RR	
	TIME(I)=TNUM/R5	
0117	CONTINUE	00196

	RTD=TIME(1)	00197
	TD TWO=TIME(2)-TIME(1)	00198
	TDTHR=TIME(3)-TIME(2)	00199
0120	CONTINUE	00200
C*****CHOOSE INITIAL DIRECTION OF MOTION AND TYPE OF PARTICLE*****		00201
0118	R=URNDMF(1.0)	00202
	IF(R-F)0121,0118,0131	00203
0121	I=0	00204
0122	R=URNDMF(1.0)	00205
	CTETA=R	00206
	STETA=SQRTF(1.0-R**2)	00207
0125	R1=URNDMF(1.0)	00208
	R2=URNDMF(1.0)	00209
	T=R1**2+R2**2	00210
	IF(T-1.0)0126,0126,0125	00211
0126	CPHI=(R1**2-R2**2)/T	00212
	SPHI=2.0*R1*R2/T	00213
0127	R=URNDMF(1.0)	00214
	IF(R-0.5)0129,0127,0128	00215
0128	SPHI=-SPHI	00216
0129	NO=NO+1	00217
	GO TO (0201,6601),JUMP	00218
0131	I=1	00219
0132	R=URNDMF(1.0)	00220
	CTETAP=R	00221
	STETAP=SQRTF(1.0-R**2)	00222
	NP=NP+1	00223
	GO TO 0301	00224
		00225
		00226
		00227
		00228
		00229
		00230
		00231
		00232
		00233
C*****		00234
C*****CALCULATION OF TIMES TO COLLISION OF NEUTRAL PARTICLES*****		00235
C*****		00236
0201	RN=URNDMF(1.0)	00237
	PN=PNB+A1*CTETA*LOGF(RN)	
C*****DOES PARTICLE ESCAPE WITHOUT COLLISION*****		00239
	IF(PN-PH)0601,0501,204	00240
204	IF(PN-PBT)202,110,110	00241
202	ASSIGN 203 TO IH	00242
	GO TO 5600	00243
203	DZO=ZN-ZNB	00244
	DSO=DZO/CTETA	00245
0208	DXO=DSO*STETA*CPHI	00246

	DYO=DSO*STETA*SPHI	00247
	YN=YNB+DYO	00248
	XN=XNB+DXO	00249
	T=VNB**2+C1*LOGF(RN)	
	IF (T)0214,0214,0220	00251
0214	NE=NE+3-L	00252
	LOSTA=LOSTA+1	00253
C*****	PARTICLE SLOWED DOWN TO REST.END HISTORY.SIMILARLY AT OTHER POINTS**	00254
	GO TO 0110	00255
0220	VN=SQRTF(T)	00256
	VB=0.5*(VN+VNB)	00257
	RTC=DSO/VB	00258
	GO TO 0401	00259
0250	WRITE OUTPUT TAPE 6,0251,K,L,I	00260
0251	FORMAT(3110)	00261
	CALL DUMP	00262
C*****	CALCULATION OF DECAYS OF NEUTRAL PARTICLES*****	00263
C*****	C*****	00264
C*****	C*****	00265
0401	CONTINUE	00266
	IF (RTD-RTC)0440,0440,0403	00267
C*****	C*****COLLISION BEFORE DECAY*****	00268
0403	XNB=XN	00269
	YNB=YN	00270
	ZNB=ZN	00271
	PNB=PN	00272
	VNB=VN	00273
	K=K+1	00274
	J=J+1	00275
	RTD=RTD-RTC	00276
	CTETAP=CTETA*CTETA0-STETA*SPHI*STETA0	00277
	IF(CTP)0415,0415,0420	00278
0415	LGB=LGB+1	00279
	GO TO 0110	00280
C*****	END HISTORY. SIMILARLY AT ALL OTHER PCINTS OF PROGRAM*****	00281
0420	STETAP=SQRTF(1.0-CTETAP**2)	00282
	GO TO 0301	00283
C*****	C*****DECAY BEFORE COLLISION*****	00284
0440	NE=NE+1	00285
	L=L+1	00286
	J=J+1	00287
	DSO=RTD*VB	00288
	DZO=DSO*CTETA	00289
	DXO=DSO*STETA*CPHI	00290
	DYO=DSO*STETA*SPHI	00291
	XN=XNB+DXO	00292
	YN=YNB+DYO	00293
	ZN=ZNB+DZO	00294
	IF(ZN-ZBT) 110,110,439	00295
439	ASSIGN 441 TO IP	00296
	GO TO 5500	00297
441	DP=PN-PNB	00298
	T=VNB**2+B*DP/CTETA	00299

0460	IF (T)0460,0460,0470	00300
	NE=NE+3-L	00301
	LOSTA=LOSTA+1	00302
	GO TO 0110	00303
0470	VN=SQRTF(T)	00304
	VB=0.5*(VN+VNB)	00305
	ASSIGN 1 TO MCALL	00306
	GO TO 7000	00307
1	CONTINUE	00308
	IF (L-3)0485,0486,0250	00309
0486	LO=LO+1	00310
	GO TO 0110	00311
0495	XNR=XN	00312
	YNB=YN	00313
	ZNB=ZN	00314
	PNB=PN	00315
	VNB=VN	00316
	CTETAP=CTETA*CTETAO-STETA*SPHI*STETAO	00317
0490	IF (CTP)0415,0415,0490	00318
	STETAP=SQRTF(1.0-CTETAP**2)	00319
0491	RTC=RTC-RTD	00320
	IF (L-2)0495,0496,0250	00321
0495	RTD=TDTHR	00322
	GO TO 0501	00323
0496	RTD=TDTHR	00324
	GO TO 0501	00325
C	*****CALCULATION OF TIMES TO COLLISION OF IONISED PARTICLES*****	00326
C	*****	00327
C	*****	00328
0301	RN=URNDMF(1.0)	00329
	DP=A2*CTETAP*CTETAO*LOGF(RN)	
	PN=PNB+DP	00331
C	***** DOES PARTICLE ESCAPE WITHOUT COLLISION*****	00332
	IF (PN-PH)0801,0801,0307	00333
0307	IF (PN-PBT)308,110,110	00334
308	ASSIGN 310 TO IH	00335
	GO TO 5600	00336
310	DZP=(ZN-ZNB)/CTETAO	00337
	YN=YNB-DZP*STETAO	00338
	XN=XNB	00339
	T=VNB**2+C2*LOGF(RN)	
	IF (T)0314,0314,0320	00341
0314	NE=NE+3-L	00342
	LOSTA=LOSTA+1	00343
	GO TO 0110	00344
0320	VN=SQRTF(T)	00345
	VR=0.5*(VN+VNR)	00346
	DSP=DZP/CTETAP	00347
	RTC=DSP/VB	00348
	GO TO 0501	00349
C		00350
C		00351
C		00352
C		00353
C		00354

64

	NE=NE-1	00409
	L=L-1	00410
	I=I-1	00411
	DP=PH-PNB	00412
	T=VNB**2+B*DP/(CTETAP*CTETA0)	00413
0541	IF (T) 0314, 0314, 0805	00414
	XN=XNB	00415
542	ASSIGN 543 TO IP	00416
	GO TO 5500	00417
543	DP=PN-PNB	00418
	T=VNB**2+(B*DP)/(CTETAP*CTETA0)	00419
	IF (T) 0560, 0560, 0570	00420
0560	NE=NE+3-L	00421
	LOSTA=LOSTA+1	00422
	GO TO 0110	00423
0570	VN=SQRT(T)	00424
	VR=0.5*(VN+VNB)	00425
	ASSIGN 2 TO MCALL	00426
	GO TO 7000	00427
2	CONTINUE	00428
	IF (L-3) 0585, 0586, 0250	00429
0586	LD=LD+1	00430
	GO TO 0110	00431
0585	XNB=XN	00432
	YNB=YN	00433
	ZNB=ZN	00434
	PNB=PN	00435
	VNB=VN	00436
	RTC=RTC-RTD	00437
	IF (L-2) 0595, 0596, 0250	00438
0595	RTD=TDTHR	00439
	GO TO 0501	00440
0596	RTD=TDTHR	00441
	GO TO 0501	00442
		00443
		00444
		00445
		00446
		00447
		00448
		00449
		00450
		00451
	*****	00452
	*****ESCAPE ROUTINE FOR NEUTRALS WITH ZERO IONISATION CROSS-SECTION*****	00453
	*****	00454
		00455
6601	CONTINUE	00456
	DP=PH-PNB	00457
	DZ=H-ZNB	00458
	DS=DZ/CTETA	00459
	DX=DS*STETA*CPhi	00460
		00461

	DY=DS*STETA*SPHI	00462
	XN=XNB+DX	00463
	YN=YNB+DY	00464
	T=VNB**2+B*DP/CTETA	00465
6250	IF (T) 6250,6250,6470	00466
6456	IF (ZN) 0250,6456,0460	00467
	ZN=H	00468
6470	GO TO 0460	00469
	VH=SQRTF(T)	00470
	VB=0.5*(VH+VNB)	00471
	RTE=DS/VB	00472
6327	IF (RTD-RTE) 6440,6440,6450	00473
6440	RTC=RTE	00474
6450	GO TO 0440	00475
	RTCH=RTF	00476
	GO TO 0639	00477
C	*****	00478
C	***** ESCAPE ROUTINE FOR NEUTRALS *****	00479
C	*****	00480
0601	CONTINUE	00481
	DP=PH-PNB	00482
	DZ=H-ZNB	00483
	DS=DZ/CTETA	00484
	DX=DS*STETA*CPHI	00485
	DY=DS*STETA*SPHI	00486
	XN=XNB+DX	00487
	YN=YNB+DY	00488
	T=VNB**2+B*DP/CTETA	00489
	IF (T) 0615,0615,0620	00490
0615	IF (ZN) 0250,0616,0214	00491
0616	ZN=H	00492
0620	GO TO 0214	00493
	VH=SQRTF(T)	00494
	VB=0.5*(VH+VNB)	00495
	RTCH=DS/VB	00496
	GO TO 0630	00497
0630	IF (RTD-RTCH) 0635,0635,0639	00498
0635	RTC=RTCH+9000.0/(CTETA*VH)	00499
	GO TO 0440	00500
639	LEN=LEN+1	00501
0640	RTS=DSS/(CTETA*VH)	00502
	RTD=RTD-RTCH	00503
	IF (RTD-RTS) 0650,0650,0680	00504
0650	NE=NE+1	00505
	L=L+1	00506
	ZNB=H	00507
	DS=RTD*VH	00508
	DZ=DS*CTETA	00509
	DX=DS*STETA*CPHI	00510
	DY=DS*STETA*SPHI	00511
	ZN=ZNB+DZ	00512
	XN=XNB+DX	00513
	YN=YNB+DY	00514
	ASSIGN 3 TO MCALL	00515
	GO TO 7000	00516

	VB=0.5*(VN+VNB)	00571
	ASSIGN 4 TO MCALL	00572
	GO TO 7000	00573
4	CONTINUE	00574
	IF (L-3) 0850, 0851, 0250	00575
0851	LD=LD+1	00576
	GO TO 0110	00577
0850	XNB=XN	00578
	YNB=YN	00579
	ZNB=ZN	00580
	PNB=PN	00581
	VNB=VN	00582
	RTH=RTH-RTD	00583
0860	IF (L-2) 0860, 0862, 0250	00584
	RTD=TD TWO	00585
0862	GO TO 0820	00586
	RTD=TD THR	00587
0870	GO TO 0820	00588
	RTD=RTD-RTH	00589
	RTCP=DCP/(CTETAP*VH)	00590
	ZNB=H	00591
	DSP=RTH*VB	00592
	YNB=YNB-DSP*CTETAP*STETAO	00593
	GO TO 0900	00594
0900	IF (RTD-RTCP) 0905, 0905, 0950	00595
0905	NE=NE+1	00596
	L=L+1	00597
	DSP=RTD*VH	00598
	DZP=DSP*CTETAP*CTETAO	00599
	XN=XNB	00600
	YN=YNB-DSP*CTETAP*STETAO	00601
	ZN=ZNB+DZP	00602
	ASSIGN 5 TO MCALL	00603
	GO TO 7000	00604
5	CONTINUE	00605
	IF (L-3) 0920, 0919, 0250	00606
0919	LD=LD+1	00607
	GO TO 0110	00608
0920	RTCP=RTCP-RTD	00609
	XNB=XN	00610
	YNB=YN	00611
	ZNB=ZN	00612
0925	IF (L-2) 0925, 0926, 0250	00613
	RTD=TD TWO	00614
0926	GO TO 0900	00615
	RTD=TD THR	00616
950	GO TO 0900	00617
	CONTINUE	00618
4900	MCP=MCP+1	00619
	CONTINUE	00620
	GO TO 0110	00621
C		00622
C	*****	00624

```

C ***** INTERPPOLATION SUBROUTINE FOR PRESSURE***** 00625
C ***** 00626
5500 IF (ZN-ZH(1)) 5520,5510,5501 00627
5501 IF (ZN-ZH(NET)) 5502,5515,5525 00628
5502 DO 5504 I=1,NET 00629
      IF (ZN-ZH(I)) 5503,5504,5504 00630
5503 PN=((ZN-ZH(I-1))*PL(I)-(ZN-ZH(I))*PL(I-1))/(ZH(I)-ZH(I-1)) 00631
      PN=10.**PN 00632
      GO TO 5599 00633
5504 CONTINUE 00634
      GO TO 5599 00635
5510 PN=PL(I) 00636
      PN=10.**PN 00637
      GO TO 5599 00638
5515 PN=PL(NET) 00639
      PN=10.**PN 00640
      GO TO 5599 00641
5520 WRITE OUTPUT TAPE 6,5521,ZN 00642
5521 FORMAT(1H 3X,9HALTITUDE=E16.8,21H BELOW RANGE OF TABLE) 00643
      GO TO 5510 00644
5525 WRITE OUTPUT TAPE 6,5526,ZN 00645
5526 FORMAT(1H 3X,9HALTITUDE=E16.8,21H ABOVE RANGE OF TABLE) 00646
      GO TO 5515 00647
5599 GO TO IP,(441,543,827) 00648
C ***** INTERPPOLATION SUBROUTINE FOR ALTITUDES***** 00649
C ***** 00650
5600 X=LOGF(PN)*.43429448 00651
      IF (X-PL(1)) 5602,5610,5620 00652
5601 IF (X-PL(NET)) 5625,5615,5603 00653
5602 IF (X-PL(1)) 5605,5605,5604 00654
5603 DO 5605 I=1,NET 00655
      IF (X-PL(I)) 5605,5605,5604 00656
5604 ZN=((X-PL(I-1))*ZH(I)-(X-PL(I))*ZH(I-1))/(PL(I)-PL(I-1)) 00657
      GO TO 5699 00658
5605 CONTINUE 00659
      GO TO 5699 00660
5610 ZN=ZH(1) 00661
      GO TO 5699 00662
5615 ZN=ZH(NET) 00663
      GO TO 5699 00664
5620 WRITE OUTPUT TAPE 6,5621,X 00665
5621 FORMAT(1H 3X,6HLOG P=E16.8,21H ABOVE RANGE OF TABLE) 00666
      GO TO 5610 00667
5625 WRITE OUTPUT TAPE 6,5626,X 00668
5626 FORMAT(1H 3X,6HLOG P=E16.8,21H BELOW RANGE OF TABLE) 00669
      GO TO 5615 00670
5699 GO TO IH,(203,310) 00671
C 00672
C 00673
C 00674
C 00675
C 00676
C 00677
C *****PREPARATION OF OUTPUT MATRIX***** 00678
C ***** 00679
C ***** 00680

```

7000	CONTINUE	00681
	IF (FLAGP) 7009,7020,7010	00682
7009	YP=(YN*CTO)+((ZN-ZO)*STO)	00683
	ZP=((ZN-ZO)*CTO)-(YN*STO)	00684
	GO TO 7008	00685
7010	YP=YN	00686
	ZP=ZN	00687
7008	IF(RYPSC-ABSF(YP)) 7050,7050,7011	00688
7011	IF(RZPSC-ABSF(ZP)) 7060,7060,7012	00689
7012	CONTINUE	
7020	IF(FLAGM) 7019,7999,7027	00691
7019	YP=YN	00692
	ZP=ZN	00693
	GO TO 7021	00694
7027	CONTINUE	00695
	ZP=((ZN-ZO)*(CTO)-(YN*STO)	00696
	YP=(YN*CTO)+((ZN-ZO)*STO)	00697
	IF(ZP) 7026,7026,7021	00698
7026	NEGZ=NEGZ+1	00699
	GO TO 7999	00700
7021	IZ=(ZP/ZSC)+1.0	
	IF(49-IZ) 7030,7022,7022	
7022	IF(YP) 7120,7130,7130	
7120	IY=-YP/YSC+1.0	
	IF(18-XABSF(IY)) 7035,7125,7125	
7125	MN(IY,IZ)=MN(IY,IZ)+1	
	GO TO 7999	
7130	IY=YP/YSC+1.0	
	IF(18-XABSF(IY)) 7035,7132,7132	
7132	MP(IY,IZ)=MP(IY,IZ)+1	
	GO TO 7999	
7030	NWZ=NWZ+1	00712
	IF(19-XABSF(IY)) 7031,7999,7999	
7031	NWYZM=NWYZM+1	00714
	GO TO 7999	00715
7035	NWY=NWY+1	00716
	IF(50-IZ) 7036,7999,7999	00717
7036	NWYZM=NWYZM+1	00718
	GO TO 7999	00719
7050	NWYP=NWYP+1	00720
	IF(RZPSC-ABSF(ZP)) 7051,7999,7999	00721
7051	NWYZP=NWYZP+1	00722
	GO TO 7999	00723
7060	NWZP=NWZP+1	00724
	GO TO 7999	00725
7999	CONTINUE	
	GO TO MCALL,(1,2,3,4,5)	00727
	END	00728
*	DATA	

List of Symbols

KCT	Total card count
JUMP	Indicator cross section
NET	Number of entries in table of atmosphere
Nf	Total number of particles to be processed
Y LIM	Highest value of Y' in output matrix
YSC	Size of grid on Y' in output matrix
Z LIM	Highest value of Z' in output matrix
ZSC	Size of grid on Z' in output matrix
FLAGM	Indicator for matrix
FLAGP	Indicator for plot routine
YPSC	Y scale factor for plot routine
ZPSC	Z scale factor for plot routine
YOR	Y position of origin on plot
ZOR	Z position of origin on plot
STO	$\sin \theta_0$
CTO	$\cos \theta_0$
DSS	Distance beyond which particle is ignored
DCP	Distance to conjugate point
B	See Eq. (4.8)
P_0	Pressure at starting point
Z_0	Starting altitude
PH	Pressure at cut-off altitude
H	Cut-off altitude
PBT	Pressure at lower cut-off altitude
ZBT	Lower cut-off altitude
$X_1 X_2$	Initialization values for the random number generator (IBM only)

STORAGE LOCATIONS FOR VARIABLES APPEARING IN DIMENSION AND EQUIVALENCE STATEMENTS

	DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT	
CPHIP	4439	10526	CPHI	4439	10527	CPP	4438	10526	CP	4439	10527
CTETAP	4444	10534	CTETA	4442	10532	CTC	4446	10536	CTP	4446	10534
FRI	4448	10540	F	4448	10540	INOM	4483	10273	ISUMPP	4402	10316
KCS	4447	10537	KCT	4449	10541	KCUNT	4447	10537	KCUNT	4449	10541
PL	4232	10211	PL	4374	10426	R	4433	10521	SPHIP	4437	10525
SPP	4437	10525	SP	4440	10530	S	4424	10344	STETAP	4445	10535
STETA	4441	10531	STO	4445	10535	STP	4443	10533	STETAP	4445	10535
TIVE	4427	10513	T	4436	10524	ZH	4424	10510	TAU	4441	10531

STORAGE LOCATIONS FOR VARIABLES NOT APPEARING IN CPPCN, DIMENSION, OR EQUIVALENCE STATEMENT

	LEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT
AI	2333	04435	A2	2332	04434	R	2331	04433	C1	2330	04432	C2
DCP	2328	04430	DP	2327	04427	DSC	2326	04426	DSP	2325	04425	DS
DSS	2323	04423	DUMMY	2322	04422	DXC	2321	04421	CK	2320	04420	DYO
CV	2319	04416	DZO	2317	04415	DZP	2316	04414	CZ	2315	04413	FLAG
FLAGP	2313	04411	H	2312	04410	IM	2311	04407	IP	2310	04406	I
IV	2308	04404	I2	2307	04403	JUPP	2306	04402	K	2305	04401	LD
LFI	2302	04377	LEN	2302	04376	LGB	2301	04375	LCSTA	2300	04374	LE
LS	2298	04372	MCALL	2297	04371	MCP	2296	04370	NEG2	2295	04367	N
NET	2293	04365	NO	2292	04364	NP	2291	04363	N	2290	04362	NT
NYVP	2288	04350	NY	2287	04357	NYZP	2286	04356	NYZP	2285	04355	NWZP
NW2	2283	04353	PBT	2282	04352	PH	2281	04351	PNB	2280	04350	PN
PO	2276	04346	Q	2277	04345	PI	2276	04344	R2	2275	04343	R5
RCRT	2273	04341	RNI	2272	04340	RA2	2271	04337	RN3	2270	04336	RNA
RNB	2268	04334	RN	2267	04333	RA	2266	04332	RICH	2265	04331	RTCP
RTC	2263	04327	RTD	2262	04326	RTE	2261	04325	ATH	2260	04324	ATS
RYVSC	2258	04322	RZPSC	2257	04321	OTDTHR	2256	04320	TCTWO	2255	04317	INLM
VR	2253	04315	VH	2252	04314	VNR	2251	04313	VN	2250	04312	VO
XI	2248	04310	X2	2247	04307	XAR	2246	04306	XN	2245	04305	X
YLIM	2243	04303	YNA	2242	04302	YN	2241	04301	YOR	2240	04300	YP
YPSC	2238	04276	YSL	2237	04275	ZBT	2236	04274	ZLM	2235	04273	ZNB
ZN	2233	04271	ZOR	2232	04270	ZC	2231	04267	ZP	2230	04266	ZPSC
ZSC	2228	04264										

NO-	25000	NP-	0	MPV-	816	MMZ-	3805	NNVP-	0	MMZP-	0	NNVZM-	166	NNVZP-	0	NECZ-	5441
LGB	LER	LEI	MCP	LS	LO	LOZIA	682	A1	A2	C1	C2						
VC	1717	13019	5322	101	14366												
YC	0.48999999E-06	0.9000000E-03	0.23300000E-02	0.23300000E-02	0.23300000E-02	0.23300000E-02	0.23300000E-02	0.23300000E-02	0.23300000E-02	0.23300000E-02	0.23300000E-02	0.23300000E-02	0.23300000E-02	0.23300000E-02	0.23300000E-02	0.23300000E-02	0.23300000E-02
ZC	0.12500000E-04	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02	0.5000000E-02
HISTOGRAM FOR POSITIVE VALUES OF Y																	
5212	1840	1000	848	319	352	259	192	103	78	57	35	28	19	10	15	0	0
1697	998	735	513	420	300	205	153	64	75	47	33	33	20	22	9	4	0
1203	654	489	372	288	210	162	101	79	63	37	25	20	19	8	5	4	2
859	421	325	242	167	152	117	67	57	34	25	13	5	7	4	1	2	3
404	313	190	151	115	74	63	37	23	23	9	7	6	3	4	1	0	0
403	180	158	89	74	57	49	219	95	48	31	18	22	6	8	4	0	0
221	121	57	49	38	35	27	70	52	23	22	15	19	11	3	4	0	0
113	72	44	32	31	37	45	50	28	26	16	22	15	7	12	8	3	1
102	49	38	29	35	34	27	46	29	22	14	10	14	6	12	5	1	0
92	51	39	25	22	24	24	33	22	16	11	7	13	4	5	3	4	0
98	51	42	22	22	12	18	27	21	17	9	10	7	4	10	4	1	0
80	43	30	26	17	16	17	19	23	15	3	3	0	1	4	3	2	2
69	27	29	32	16	26	17	20	13	8	13	3	2	3	4	2	1	1
59	36	18	25	16	15	11	11	12	11	4	4	3	0	4	2	1	0
52	29	16	20	9	11	12	11	6	8	2	6	0	2	4	1	4	3
53	33	21	19	16	12	12	17	12	3	7	6	0	2	4	1	3	1
58	32	23	15	15	11	5	9	10	7	3	1	2	1	2	1	1	0
52	18	16	17	7	10	7	12	8	4	6	4	4	4	2	0	1	1
51	13	16	8	11	3	13	5	10	11	8	4	2	2	1	2	0	0
46	21	17	10	17	10	11	9	8	2	4	1	4	4	1	2	1	0
39	18	16															

Section 6
ATMOSPHERIC PARAMETERS AS A FUNCTION OF ALTITUDE
NEAR SUNSPOT MAXIMUM

altitude (km)	pressure (dyne/cm ²)
100	1.74×10^{-1}
120	3.4×10^{-2}
140	1.04×10^{-2}
160	5.1×10^{-3}
180	3.1×10^{-3}
200	1.95×10^{-3}
220	1.20×10^{-3}
240	8.5×10^{-4}
260	6.4×10^{-4}
280	4.7×10^{-4}
300	3.6×10^{-4}
320	2.7×10^{-4}
340	2.04×10^{-4}
360	1.54×10^{-4}
380	1.23×10^{-4}
400	9.8×10^{-5}
450	5.2×10^{-5}
500	2.9×10^{-5}
600	1.00×10^{-5}
700	3.5×10^{-6}
800	1.32×10^{-6}
900	4.9×10^{-7}
1000	1.90×10^{-7}
1200	3.2×10^{-8}
1400	6.7×10^{-9}
1600	2.1×10^{-9}
1800	1.14×10^{-9}
2000	9.5×10^{-10}
2500	7.2×10^{-10}

**ATMOSPHERIC PARAMETERS AS A FUNCTION OF ALTITUDE
NEAR SUNSPOT MINIMUM**

altitude (km)	pressure (dyne/cm ²)	
100	1.74	10 ⁻¹
120	2.1	10 ⁻²
140	4.6	10 ⁻³
160	1.86	10 ⁻³
180	9.1	10 ⁻⁴
200	5.0	10 ⁻⁴
220	2.8	10 ⁻⁴
240	1.77	10 ⁻⁴
260	1.14	10 ⁻⁴
280	7.6	10 ⁻⁵
300	5.1	10 ⁻⁵
320	3.5	10 ⁻⁵
340	2.34	10 ⁻⁵
360	1.66	10 ⁻⁵
380	1.14	10 ⁻⁵
400	8.3	10 ⁻⁶
450	3.6	10 ⁻⁶
500	1.66	10 ⁻⁶
600	3.4	10 ⁻⁷
700	7.9	10 ⁻⁸
800	2.4	10 ⁻⁸
900	1.26	10 ⁻⁸
1000	9.8	10 ⁻⁹
1200	7.2	10 ⁻⁹
1400	6.2	10 ⁻⁹
1600	5.1	10 ⁻⁹
1800	4.3	10 ⁻⁹
2000	3.8	10 ⁻⁹
2500	2.8	10 ⁻⁹

Section 7
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