

AEDC-TR-65-125

**ARCHIVE COPY
DO NOT LOAN**

cy1



LIGHT ENERGY REACHING THE GRATING OF A SPECTROMETER

This document has been approved for public release
its distribution is unlimited.

*per AEDC-TR-75/5
AD A01110P
Dtd July 1975*

W. E. Bair

ARO, Inc.

July 1965

Property of AEDC
F40600-74-C-0001

**VON KÁRMÁN GAS DYNAMICS FACILITY
ARNOLD ENGINEERING DEVELOPMENT CENTER
AIR FORCE SYSTEMS COMMAND
ARNOLD AIR FORCE STATION, TENNESSEE**

AEDC TECHNICAL LIBRARY



5 0720 00031 0807

NOTICES

When U. S. Government drawings, specifications, or other data are used for any purpose other than a definitely related Government procurement operation, the Government thereby incurs no responsibility nor any obligation whatsoever, and the fact that the Government may have formulated, furnished, or in any way supplied the said drawings, specifications, or other data, is not to be regarded by implication or otherwise, or in any manner licensing the holder or any other person or corporation, or conveying any rights or permission to manufacture, use, or sell any patented invention that may in any way be related thereto.

Qualified users may obtain copies of this report from the Defense Documentation Center.

LIGHT ENERGY REACHING THE
GRATING OF A SPECTROMETER

W. E. Bair*

ARO, Inc.

This document has been approved for public release
its distribution is unlimited. *Pw DDC HTR-15/5*
AD A011 700
Dtd July 198

*Consultant, ARO, Inc., and Professor, University of Illinois

FOREWORD

The work reported herein was sponsored by Arnold Engineering Development Center (AEDC), Air Force Systems Command (AFSC), Arnold Air Force Station, Tennessee under Program Element 62405334, Project 8952.

The results of research presented were obtained by ARO, Inc. (a subsidiary of Sverdrup and Parcel, Inc.), contract operator of the AEDC under Contract AF 40(600)-1000. The research was conducted under ARO Project Numbers VL3310 and VW2236, and the report was submitted by the author on May 26, 1965.

The author wishes to thank Dr. Ray Hefferlin for his encouragement that this report be published and J. O. Hornkohl for assistance in this work and in preparing this report for publication.

This technical report has been reviewed and is approved.

Terry L. Hershey
Captain, USAF
Aerospace Sciences Division
DCS/Research

Donald R. Eastman, Jr.
DCS/Research

ABSTRACT

The effective field of view of a spectrometer, when used with an external collecting lens, is shown to be defined by the width and height of the image of the slit. The energy, E_λ , of wavelength λ , which reaches the grating of the spectrometer, is very closely approximated as

$$E_\lambda = \frac{wh}{\pi} \left[\sin^{-1} \left(\frac{d^2}{4\bar{z}^2 + d^2} \right) \right] I_\lambda dz$$

where

w = width of slit image

h = height of slit image

d = width of lens stop

$\bar{z}$ = distance from slit image to lens

I_λ = intensity of light emitted

z = coordinate distance from slit image
toward lens

CONTENTS

	<u>Page</u>
ABSTRACT.	iii
NOMENCLATURE.	v
I. PRIMARY CONSIDERATIONS	1
II. DEVELOPMENT	1
III. DISCUSSION	4

ILLUSTRATIONS

Figures

1.	Optical Diagram Showing Limiting Planes for the Determination of the Effective Stops	7
2.	Optical Projection of the Effective Solid Angle for a Point	8
3.	Typical Layout of Apparatus	9

TABLES

I.	Limiting Planes.	11
II.	Limiting Angles.	12
III.	Limits of Integration and z Functions	13
IV.	Modified z Functions and Limits of Integration	14

NOMENCLATURE

d	Width of lens stop
d_c	Width of collimator image
d'_c	Width of collimator
dv	Element of volume
E_λ	Energy of wavelength λ reaching grating, per unit time

f	Focal length of lens
h	Height of slit image
h'	Height of slit
I_λ	Intensity of light emitted, w/cm^3
w	Width of slit image
w'	Width of slit
x	Horizontal distance from optical axis
y	Vertical distance from optical axis
z	Distance from slit image toward lens
$\bar{z}$	Distance from slit image to lens
z'	Distance from slit to lens
z_c	Distance from slit image to collimator image
z'_c	Distance from slit to collimator
α	Transformed horizontal variable
β	Transformed vertical variable
γ	Angle from line parallel to axis to right stop
δ	Angle from line parallel to axis to left stop
λ	Wavelength of light observed
ϕ	Angle from line parallel to axis to upper stop
ψ	Angle from line parallel to axis to lower stop
Ω	Solid angle

SECTION I PRIMARY CONSIDERATIONS

In order to utilize the maximum resolution capability of a grating spectrometer, it is necessary to illuminate the entire ruled area of the grating. The collimating mirrors of a well-designed spectrometer are sized to fully illuminate the grating. To prevent stray light in the spectrometer from causing false indications, it is desirable to select a lens stop and slit-to-lens distance which will cause full illumination of the collimator without overillumination. When this is accomplished, the solid angle of the lens stop will be the same as the solid angle of the collimator when both are viewed from the slit. The solid angle of the lens stop will then be the same as the solid angle of the collimator image when viewed from the slit image. This is the condition chosen for the development which follows.

SECTION II DEVELOPMENT

The energy which reaches the grating of the spectrometer is determined by integrating, over the field of emission, the intensity of the emitted radiation which reaches the grating.

$$E_{\lambda} = \int \frac{1}{4\pi} I_{\lambda} \Omega \, dv \quad (1)$$

The effective solid angle through which the radiation will reach the grating is limited by (1) the slit image, (2) the collimator image, or (3) the collecting lens stop. In the following analysis, the collecting lens stop and the collimator image are both assumed to be square with widths d and d_c , respectively. For this case the effective solid angle will be that subtended by a rectangle.

As shown in Fig. 1, the field of emission is divided by planes into regions for which various combinations control the solid angle. Point A, for example, is controlled on its upper angle, ϕ , by the lens and on its lower angle, ψ , by the collimator image, whereas the horizontal angles, γ and δ , are controlled by the slit image on the right and the lens on the left.

The effective rectangle for point A is shown projected on the slit image, collimator image, and lens planes in Fig. 2. In terms of the

limiting angles ϕ , ψ , γ , and δ , the solid angle subtended by the rectangle is

$$\Omega = \sin^{-1}(\sin \phi \sin \gamma) + \sin^{-1}(\sin \phi \sin \delta) + \sin^{-1}(\sin \psi \sin \gamma) + \sin^{-1}(\sin \psi \sin \delta) \quad (2)$$

In general, it is sufficiently accurate to assume that

$$\partial^2 I_\lambda / \partial x^2 = 0 \quad \text{and} \quad \partial^2 I_\lambda / \partial y^2 = 0 \quad (3)$$

By assuming that the second derivatives are zero and that variations in I_λ transverse to the optical axis are linear in x and y , each element of volume ($dx \, dy \, dz$) off of the axis may be summed with the other three elements whose x and y coordinates have the same magnitudes. The total contribution of these four elements, which by the symmetry of position each emits to the grating through the same solid angle, will be the same as though each possessed an intensity equal to the mean intensity for the z -plane in which they reside. This results in the symmetry which permits treatment of I_λ as a function of z alone and also permits the evaluation of the total solid angle as

$$\Omega = 4 \sin^{-1}(\sin \gamma \sin \phi) \quad (4)$$

Substituting

$$\sin \gamma = \tan \gamma / \sqrt{1 + \tan^2 \gamma} \quad \text{and} \quad \sin \phi = \tan \phi / \sqrt{1 + \tan^2 \phi}$$

the integral becomes

$$E_\lambda = \int \frac{I_\lambda}{\pi} \iint \sin^{-1} \frac{\tan \gamma \tan \phi}{\sqrt{(1 + \tan^2 \gamma)(1 + \tan^2 \phi)}} \, dy \, dx \, dz \quad (5)$$

Table I shows the equations of the limiting planes, x_1 , x_2 , ..., and Table II shows the values of γ and ϕ for each range of z and x or y as appropriate. The values for $z > z_c$ are not included since this is assumed to be out of the field of emission, as shown in Fig. 3. (In order to experimentally apply the derived result of this report, the location of the collimator image should be determined.)

Upon substitution of the appropriate values of $\tan \gamma$ and $\tan \phi$, along with the accompanying limits, Eq. (4) expands to nine double integrals for each range of z . The first of these double integrals, for $z < 0$, is

$$\int_{x_4}^{x_3} \int_{y_4}^{y_3} \sin^{-1} \frac{\tan \gamma_{43} \tan \phi_{43}}{\sqrt{(1 + \tan^2 \gamma_{43})(1 + \tan^2 \phi_{43})}} \, dy \, dx$$

This and the other integrals can be simplified by substituting $\alpha = \tan \gamma$ and $\beta = \tan \phi$. The first integral then becomes

$$(\bar{z} - z)^2 \int_{\frac{w+d}{2\bar{z}}}^{\frac{d}{2\bar{z}}} \int_{\frac{h+d}{2\bar{z}}}^{\frac{d}{2\bar{z}}} \sin^{-1} \frac{\alpha \beta}{\sqrt{(1+\alpha^2)(1+\beta^2)}} d\beta d\alpha \quad (6)$$

Similar substitution in the other integrals will result in generation of various functions of z for the various limits. The integrands will be identical. Table III lists these functions and the corresponding limits.

Since the arcsin is an "odd" function, integration from

$$-\frac{d+w}{2\bar{z}} \text{ to } \frac{d+w}{2\bar{z}} \text{ or from } -\frac{d_c+w}{2z_c} \text{ to } \frac{d_c+w}{2z_c}$$

will yield zero. After eliminating these zero terms, the functions of z become constants as shown in Table IV. Inasmuch as the constants are identical for both ranges of z , the complete integral can be written as

$$E_\lambda = \int \frac{I_\lambda}{\pi} \left[z_c^2 \int_{\frac{d_c-w}{2z_c}}^{\frac{d}{2\bar{z}}} \int_{\frac{d_c-h}{2z_c}}^{\frac{d}{2\bar{z}}} \sin^{-1} \frac{\alpha \beta}{\sqrt{(1+\alpha^2)(1+\beta^2)}} d\beta d\alpha + z_c \bar{z} \int_{\frac{d_c-w}{2z_c}}^{\frac{d}{2\bar{z}}} \int_{\frac{d}{2\bar{z}}}^{\frac{d+h}{2\bar{z}}} \sin^{-1} \dots d\beta d\alpha + z_c \bar{z} + \int_{\frac{d}{2\bar{z}}}^{\frac{d+w}{2\bar{z}}} \int_{\frac{d_c-h}{2z_c}}^{\frac{d}{2\bar{z}}} \sin^{-1} \dots d\beta d\alpha + \bar{z}^2 \int_{\frac{d}{2\bar{z}}}^{\frac{d+w}{2\bar{z}}} \int_{\frac{d}{2\bar{z}}}^{\frac{d+h}{2\bar{z}}} \sin^{-1} \dots d\beta d\alpha \right] dz \quad (7)$$

These four remaining integrals can be evaluated by integration by parts setting

$$u = \sin^{-1} \frac{\alpha \beta}{\sqrt{(1+\alpha^2)(1+\beta^2)}} \quad \text{and} \quad dv = d\beta$$

in the first integration and similarly in the second. It is of interest to note, however, that the range of integration in each integral is small and that a close approximation can be obtained by fixing the integrand at the value corresponding to the center of the overall range, $\alpha = \beta = \frac{d}{2\bar{z}}$. Upon evaluation in this manner, Eq. (1) finally becomes

$$E_\lambda = \frac{wh}{\pi} \left[\sin^{-1} \left(\frac{d^2}{4\bar{z}^2 + d^2} \right) \right] \int_{-\bar{z}}^{\bar{z}} I_\lambda dz \quad (8)$$

Equation (8) may be expressed in terms of the actual slit dimensions, w' and h' , the distance from the slit to the lens, z' , and the focal length of the lens, f . In these terms, it becomes

$$E_{\lambda} = \frac{w' h'}{\pi} \left(\frac{f}{z' - f} \right)^2 \left[\sin^{-1} \left(\frac{(z' - f)^2 d^2}{4 f^2 z'^2 + (z' - f)^2 d^2} \right) \right] \int I_{\lambda} dz \quad (9)$$

Equations (8) and (9) may both be further simplified by noting that $d \ll \bar{z}$ or $d \ll z'$ and that, for small values of the argument, the arcsin is approximately equal to the argument. With these substitutions, Eqs. (8) and (9) become

$$E_{\lambda} = \frac{w h d^2}{4 \pi \bar{z}^2} \int I_{\lambda} dz = \frac{w' h' d^2}{4 \pi z'^2} \int I_{\lambda} dz \quad (10)$$

This equation can be stated in either of two ways. First, the light energy reaching the grating of a spectrometer is proportional to the area of the slit image, the solid angle of the lens, or collimator image when viewed from the slit image, and the integral of the variation of the intensity of the emitted light along the axis of the spectrometer; second, the light energy which reaches the grating of the spectrometer is proportional to the area of the slit, the solid angle of the lens or collimator when viewed from the slit, and the integral of the variation of the intensity of the emitted light along the axis of the spectrometer.

SECTION III DISCUSSION

Because the integrand of the final integral to be evaluated is only the intensity function, the axial variations in emitted intensity cannot be detected by an axial shift of the optical system. For a circularly symmetrical emitting field, an Abel inversion technique¹ can be used. For non-circular fields, a similar technique in which sets of observations are made with the optical axis aligned in two perpendicular directions will permit analysis. The accuracy of this analysis will be somewhat less than that of the Abel inversion but can be improved to a satisfactory level by an increase in the number of observations.

Equation (10) shows that, while the field of view of a spectrometer has the width and height of the slit image at the slit image and increases

¹Griem, Hans R. Plasma Spectroscopy. New York, McGraw-Hill, 1964, p. 176.

in area in both directions along the z axis approximately as the square of the distance from the slit image, the fraction of the emitted energy reaching the grating is inversely proportional to the square of the distance, and the resultant energy reaching the grating is therefore independent of the distance.

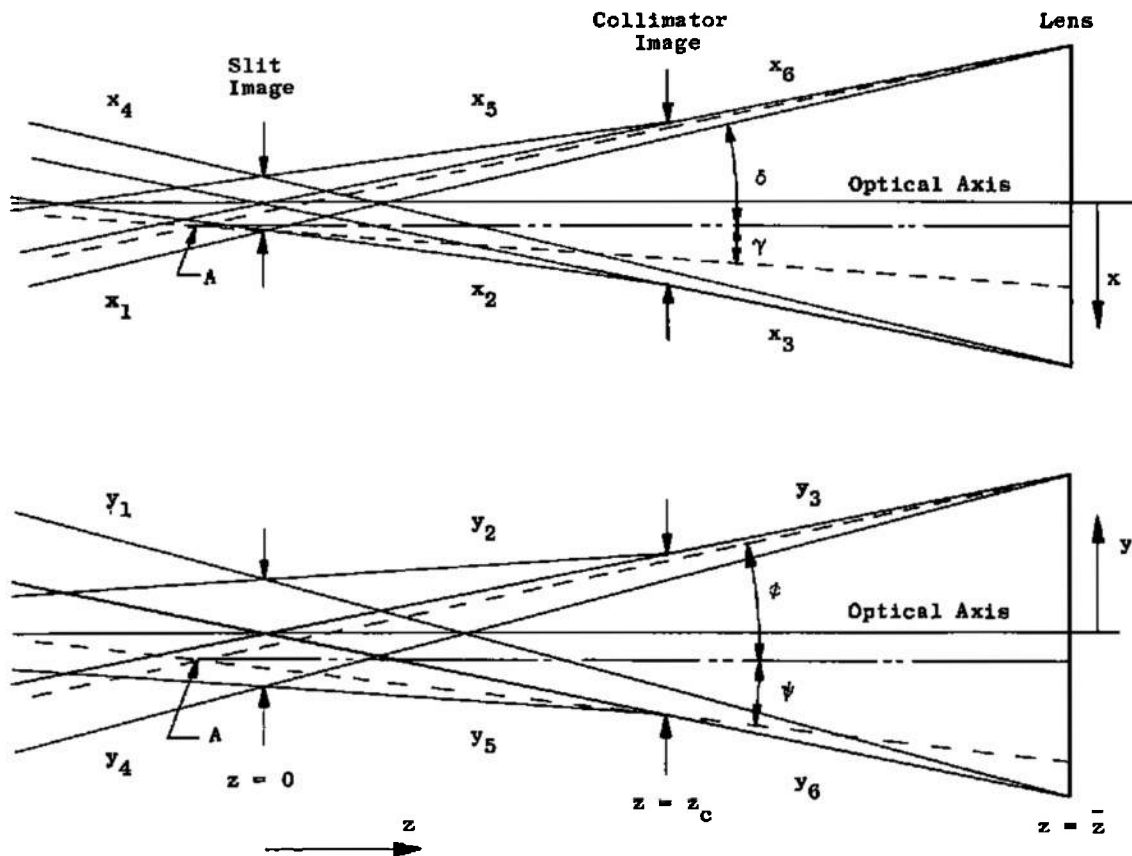


Fig. 1 Optical Diagram Showing Limiting Planes for the Determination of the Effective Stops

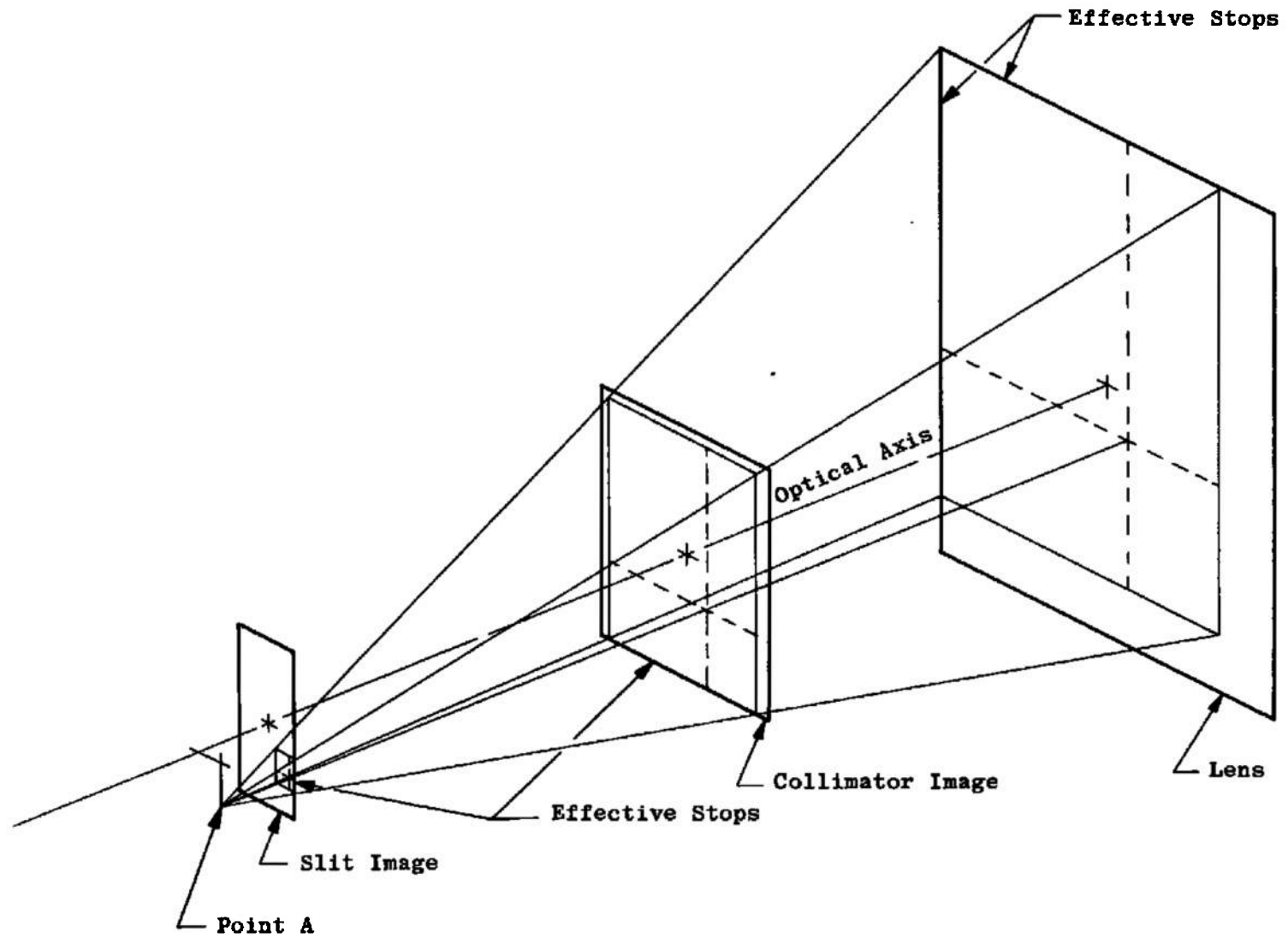


Fig. 2 Optical Projection of the Effective Solid Angle for a Point

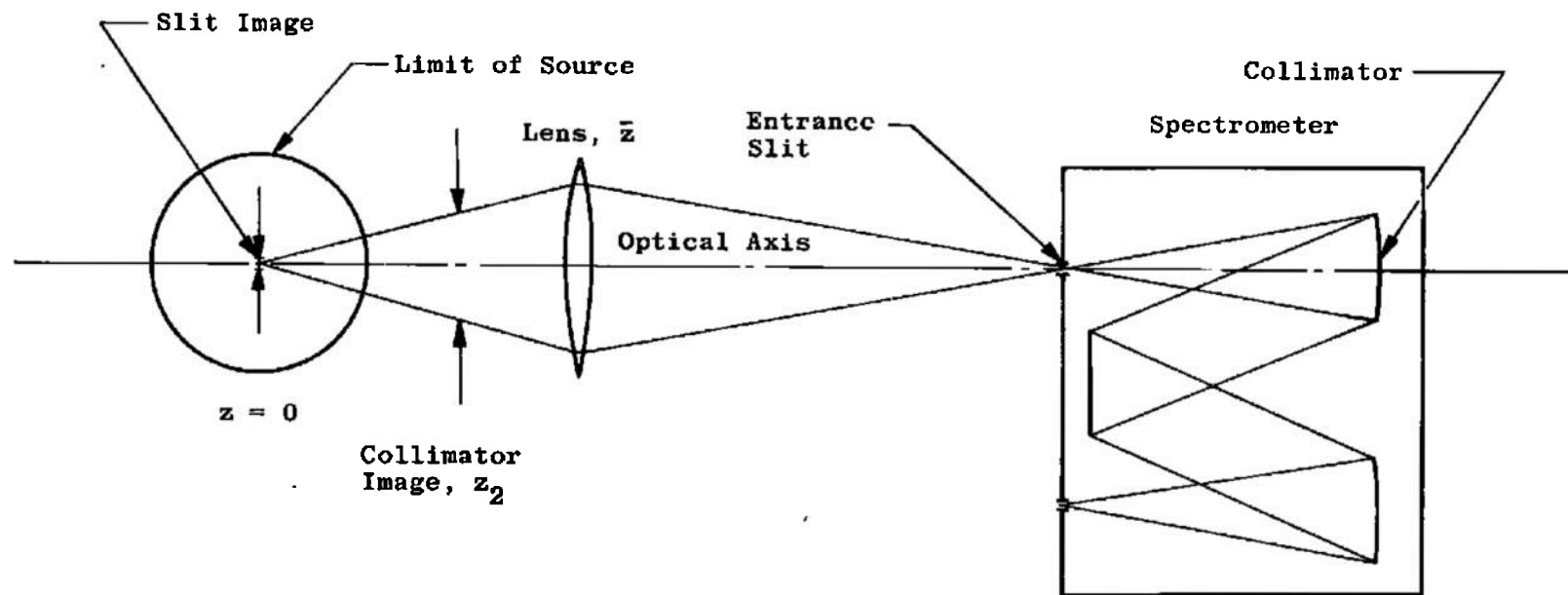


Fig. 3 Typical Layout of Apparatus

TABLE I
LIMITING PLANES

Horizontal Limits

$$x_1 = \frac{w}{2} - \frac{w+d}{2} \cdot \frac{z}{z_c}$$

$$x_2 = \frac{w}{2} + \frac{d_c-w}{2} \cdot \frac{z}{z_c}$$

$$x_3 = \frac{d_c}{2} \cdot \frac{z}{z_c}$$

$$x_4 = -\frac{w}{2} + \frac{w+d}{2} \cdot \frac{z}{z_c}$$

$$x_5 = -\frac{w}{2} - \frac{d_c-w}{2} \cdot \frac{z}{z_c}$$

$$x_6 = -\frac{d_c}{2} \cdot \frac{z}{z_c}$$

Vertical Limits

$$y_1 = \frac{h}{2} - \frac{h+d}{2} \cdot \frac{z}{z_c}$$

$$y_2 = \frac{h}{2} + \frac{d_c-h}{2} \cdot \frac{z}{z_c}$$

$$y_3 = \frac{d_c}{2} \cdot \frac{z}{z_c}$$

$$y_4 = -\frac{h}{2} + \frac{h+d}{2} \cdot \frac{z}{z_c}$$

$$y_5 = -\frac{h}{2} - \frac{d_c-h}{2} \cdot \frac{z}{z_c}$$

$$y_6 = -\frac{d_c}{2} \cdot \frac{z}{z_c}$$

$$\frac{d_c}{z_c} = \frac{d}{z}$$

TABLE II
LIMITING ANGLES

z Range	x Range	Horizontal Angle
$-\infty < z < 0$	$x_2 < x < x_1$	$\gamma_{21} = \tan^{-1} \left(x - \frac{w}{2} \right) / z$
$-\infty < z < z_c$	$x_3 < x < x_2$	$\gamma_{32} = \tan^{-1} \left(\frac{d_c}{2} - x \right) / (z_c - z)$
$-\infty < z < z_c$	$x_4 < x < x_3$	$\gamma_{43} = \tan^{-1} \left(\frac{d}{2} - x \right) / (\bar{z} - z)$
$0 < z < z_c$	$x_5 < x < x_4$	$\gamma_{54} = \tan^{-1} \left(\frac{w}{2} + x \right) / z$
z Range	y Range	Vertical Angle
$-\infty < z < 0$	$y_2 < y < x_1$	$\phi_{21} = \tan^{-1} \left(y - \frac{h}{2} \right) / z$
$-\infty < z < z_c$	$y_3 < y < x_2$	$\phi_{32} = \tan^{-1} \left(\frac{d_c}{2} - y \right) / (z_c - z)$
$-\infty < z < z_c$	$y_4 < y < x_3$	$\phi_{43} = \tan^{-1} \left(\frac{d}{2} - y \right) / (\bar{z} - z)$
$0 < z < z_c$	$y_5 < y < x_4$	$\phi_{54} = \tan^{-1} \left(\frac{h}{2} + y \right) / z$

TABLE III
LIMITS OF INTEGRATION AND z FUNCTIONS

a. $z < 0$

β - Limits	$-\frac{d+h}{2\bar{z}}$	$\frac{d_c-h}{2z_c}$	$\frac{d}{2\bar{z}}$	$\frac{d+h}{2\bar{z}}$
α - Limits				
$-(d+w)/2z$	$(-z)(-z)$	$(z_c-z)(-z)$	$(\bar{z}-z)(-z)$	
$(d_c-w)/2z_c$	$(-z)(z_c-z)$	$(z_c-z)(z_c-z)$	$(\bar{z}-z)(z_c-z)$	
$d/2\bar{z}$	$(-z)(\bar{z}-z)$	$(z_c-z)(\bar{z}-z)$	$(\bar{z}-z)(\bar{z}-z)$	
$(d+w)/2\bar{z}$				

b. $0 < z < z_c$

β - Limits	$\frac{d_c-h}{2z_c}$	$\frac{d_c-h}{2z_c}$	$\frac{d}{2\bar{z}}$	$\frac{d+h}{2\bar{z}}$
α - Limits				
$-(d_c-w)/2z_c$	$z \cdot z$	$z_c \cdot z$	$\bar{z} \cdot z$	
$(d_c-w)/2z_c$	$z \cdot z_c$	$z_c \cdot z_c$	$\bar{z} \cdot z_c$	
$d/2\bar{z}$	$z \cdot \bar{z}$	$z_c \cdot \bar{z}$	$\bar{z} \cdot \bar{z}$	
$(d+w)/2\bar{z}$				

TABLE IV
MODIFIED z FUNCTIONS AND LIMITS OF INTEGRATION

a. $z < 0$

β - Limits

	$\frac{d_c - h}{2 z_c}$	$\frac{d}{2 \bar{z}}$	$\frac{d + h}{2 \bar{z}}$
<u>α - Limits</u>			
$(d + w)/2 \bar{z}$	$z_c \cdot \bar{z}$		$z \cdot \bar{z}$
$d/2 \bar{z}$	$z_c \cdot z_c$		$\bar{z} \cdot z_c$
$(d_c - w)/2 z_c$			

b. $0 < z < z_c$

β - Limits

	$\frac{d_c - h}{2 z_c}$	$\frac{d}{2 \bar{z}}$	$\frac{d + h}{2 \bar{z}}$
<u>α - Limits</u>			
$(d + w)/2 \bar{z}$	$z_c \cdot \bar{z}$		$\bar{z} \cdot \bar{z}$
$d/2 \bar{z}$	$z_c \cdot z_c$		$\bar{z} \cdot z_c$
$(d_c - w)/2 z_c$			

DOCUMENT CONTROL DATA - R&D

(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)

1. ORIGINATING ACTIVITY (Corporate author) Arnold Engineering Development Center ARO, Inc. Operating Contractor Arnold Air Force Station, Tennessee		2a. REPORT SECURITY CLASSIFICATION UNCLASSIFIED	
		2b. GROUP N/A	
3. REPORT TITLE LIGHT ENERGY REACHING THE GRATING OF A SPECTROMETER			
4. DESCRIPTIVE NOTES (Type of report and inclusive dates) N/A			
5. AUTHOR(S) (Last name, first name, initial) Bair, W. E. ARO, Inc.		This document has been approved for public release its distribution is unlimited. <i>Rev DDC 1772-1515 AP 49/16 100/1975 Date July 1975</i>	
6. REPORT DATE July 1965	7a. TOTAL NO. OF PAGES 20	7b. NO. OF REFS 1	
8a. CONTRACT OR GRANT NO. AF 40(600)-1000	9a. ORIGINATOR'S REPORT NUMBER(S) AEDC-TR-65-125		
b. PROJECT NO. 8952			
c. Program Element 62405334	9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report) N/A		
d.			
10. AVAILABILITY/LIMITATION NOTICES Qualified requesters may obtain copies of this report from DDC.			
11. SUPPLEMENTARY NOTES N/A		12. SPONSORING MILITARY ACTIVITY Arnold Engineering Development Center, Air Force Systems Command, Arnold Air Force Station, Tennessee	
13. ABSTRACT The effective field of view of a spectrometer, when used with an external collecting lens, is shown to be defined by the width and height of the image of the slit. The energy, E_λ , of wavelength λ , which reaches the grating of the spectrometer, is very closely approximated as $E_\lambda = \frac{wh}{\pi} \left[\sin^{-1} \left(\frac{d^2}{4z^2 + d^2} \right) \right] \int I_\lambda dz$ where w = width of slit image h = height of slit image d = width of lens stop z = distance from slit image to lens I_λ = intensity of light emitted z = coordinate distance from slit image toward lens			

14. KEY WORDS	LINK A		LINK B		LINK C	
	ROLE	WT	ROLE	WT	ROLE	WT
spectrometers						
lens						
wavelength						
light energy						

INSTRUCTIONS

1. **ORIGINATING ACTIVITY:** Enter the name and address of the contractor, subcontractor, grantee, Department of Defense activity or other organization (*corporate author*) issuing the report.

2a. **REPORT SECURITY CLASSIFICATION:** Enter the overall security classification of the report. Indicate whether "Restricted Data" is included. Marking is to be in accordance with appropriate security regulations.

2b. **GROUP:** Automatic downgrading is specified in DoD Directive 5200.10 and Armed Forces Industrial Manual. Enter the group number. Also, when applicable, show that optional markings have been used for Group 3 and Group 4 as authorized.

3. **REPORT TITLE:** Enter the complete report title in all capital letters. Titles in all cases should be unclassified. If a meaningful title cannot be selected without classification, show title classification in all capitals in parenthesis immediately following the title.

4. **DESCRIPTIVE NOTES:** If appropriate, enter the type of report, e.g., interim, progress, summary, annual, or final. Give the inclusive dates when a specific reporting period is covered.

5. **AUTHOR(S):** Enter the name(s) of author(s) as shown on or in the report. Enter last name, first name, middle initial. If military, show rank and branch of service. The name of the principal author is an absolute minimum requirement.

6. **REPORT DATE:** Enter the date of the report as day, month, year; or month, year. If more than one date appears on the report, use date of publication.

7a. **TOTAL NUMBER OF PAGES:** The total page count should follow normal pagination procedures, i.e., enter the number of pages containing information.

7b. **NUMBER OF REFERENCES:** Enter the total number of references cited in the report.

8a. **CONTRACT OR GRANT NUMBER:** If appropriate, enter the applicable number of the contract or grant under which the report was written.

8b, 8c, & 8d. **PROJECT NUMBER:** Enter the appropriate military department identification, such as project number, subproject number, system numbers, task number, etc.

9a. **ORIGINATOR'S REPORT NUMBER(S):** Enter the official report number by which the document will be identified and controlled by the originating activity. This number must be unique to this report.

9b. **OTHER REPORT NUMBER(S):** If the report has been assigned any other report numbers (*either by the originator or by the sponsor*), also enter this number(s).

10. **AVAILABILITY/LIMITATION NOTICES:** Enter any limitations on further dissemination of the report, other than those

imposed by security classification, using standard statements such as:

- (1) "Qualified requesters may obtain copies of this report from DDC."
- (2) "Foreign announcement and dissemination of this report by DDC is not authorized."
- (3) "U. S. Government agencies may obtain copies of this report directly from DDC. Other qualified DDC users shall request through _____."
- (4) "U. S. military agencies may obtain copies of this report directly from DDC. Other qualified users shall request through _____."
- (5) "All distribution of this report is controlled. Qualified DDC users shall request through _____."

If the report has been furnished to the Office of Technical Services, Department of Commerce, for sale to the public, indicate this fact and enter the price, if known.

11. **SUPPLEMENTARY NOTES:** Use for additional explanatory notes.

12. **SPONSORING MILITARY ACTIVITY:** Enter the name of the departmental project office or laboratory sponsoring (*paying for*) the research and development. Include address.

13. **ABSTRACT:** Enter an abstract giving a brief and factual summary of the document indicative of the report, even though it may also appear elsewhere in the body of the technical report. If additional space is required, a continuation sheet shall be attached.

It is highly desirable that the abstract of classified reports be unclassified. Each paragraph of the abstract shall end with an indication of the military security classification of the information in the paragraph, represented as (TS), (S), (C), or (U).

There is no limitation on the length of the abstract. However, the suggested length is from 150 to 225 words.

14. **KEY WORDS:** Key words are technically meaningful terms or short phrases that characterize a report and may be used as index entries for cataloging the report. Key words must be selected so that no security classification is required. Identifiers, such as equipment model designation, trade name, military project code name, geographic location, may be used as key words but will be followed by an indication of technical context. The assignment of links, rules, and weights is optional.