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REPORT NO. RS-TR-65-3

THEORETICAL EFFECTS OF REENTRY AERODYNAMIC HEATING
ON THE EXTERNAL SKIN STRUCTURE OF AMRAD
EXPERIMENT NUMBER ONE

by

W. G. Burleson and R. A. Reynolds

April 1965

Sponsored by
Advanced Research Projects Agency
Project DEFENDER
ARPA Order 198



U S ARMY MISSILE COMMAND
REDSTONE ARSENAL, ALABAMA

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AMC Management Structure Code No. 5900.21.16229

**Stress and Thermodynamics Analysis Branch
Structures and Mechanics Laboratory
Directorate of Research and Development
U. S. Army Missile Command
Redstone Arsenal, Alabama**

ABSTRACT

Calculated reentry aerodynamic heating effects on the external skin of an ICBM reentry test vehicle having a relatively low weight-to-drag ratio are presented in this report. The vehicle is a blunt cone with the aft portion designed to fail just after maximum heating and the forward portion designed to survive to impact.

The tape-wound, reinforced plastic heat shield is subjected to maximum reentry heating rates between 125×10^4 and 650×10^4 kcal/m²hr. Resulting external and internal surface temperature histories are given. Effects of extreme trajectory, vehicle characteristics, and atmosphere variations on the aluminum substructure temperature histories are discussed.

ACKNOWLEDGMENT

Grateful acknowledgment is made to Mr. R. Eppes and Mr. M. W. Goodwin, for their contributions of Appendixes B, C, and D.

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INTRODUCTION

As a part of the ARPA experimental reentry radar discrimination program, the U.S. Army Missile Command (USAMICOM) has been engaged in the design and fabrication of several typical, lightweight ICBM reentry vehicles having various ballistic factors. Vehicle No. 1, which is discussed in this report, is a blunt cone, ablative skin vehicle designed to survive intact to an altitude of 30.48 kilometers. At this altitude the forward portion of the vehicle separates from the destructible aft frustum. The forward portion of the vehicle is designed to survive to impact so that recorded data can be obtained.

The purposes of this report are:

To show the type of reentry environment to which the vehicle is exposed.

To show the calculated ablative heat shield requirements.

To predict external surface temperatures along the external surface of the blunt cone vehicle.

To assist in determining the criteria for initiating separation of the recovery capsule.

VEHICLE DESCRIPTION AND ENVIRONMENT

The vehicle is a blunt cone having a nose radius of 0.15875 meter (6.25 inches) and a cone half angle of 14 degrees (Figure 1). The initial ballistic coefficient, $W/C_D A$, is approximately 537 kg/m² (110 lb/ft²). The forward portion of the vehicle, termed the recovery tip in Figure 1, contains a tape recorder and associated recovery gear and is designed to survive reentry to impact. The aft portion of the vehicle, the destructible frustum, is designed to fail at a reentry altitude just below 30.48 kilometers (100,000 feet). This type vehicle skin design is advantageous due to the critical weight limitations and other vital criteria specified in the vehicle experiment requirements.

Shielding of the reentry vehicle during ascent by use of a shroud is considered necessary to prevent heat from soaking through the heat shield to vital components before the reentry phase begins. Nominal reentry conditions are 6,096 m/sec (20,000 ft/sec) at an angle of 23 degrees below the local horizon. Shown in Figure 2 are the calculated velocity and altitude histories. These trajectory parameters were calculated by the Advanced Systems Laboratory, USAMICOM.

The vehicle spins about its centerline axis, and the initial angle-of-attack is less than 5 degrees.

THEORETICAL PROCEDURES AND BASIC ASSUMPTIONS

Aerodynamic heating to the vehicle was calculated by real gas procedures based on the widely accepted methods of Fay and Riddell, and of Rose, Probst, and Adams. Aerodynamic heating, ablation, conduction, pressure distribution, and weight calculation procedures used by Stress and Thermodynamics Analysis Branch are described briefly in Appendixes A, B, and C. To obtain a simple internal configuration on a hemisphere when the external radius and required thicknesses versus angular station are known, a method was developed whereby the weight is kept to a minimum while the specified thicknesses are met or slightly exceeded at all spherical stations. This procedure, as explained in Appendix D, is for an internal surface described by a spherical sector with the radius originating on the vehicle centerline.

Temperature limits were set on the aluminum substructure, as determined by the sensitivity of internal components and the mechanical properties of aluminum alloys versus temperature. For the recovery tip the design temperature is approximately 378° K, and for the destructible frustum a design temperature of 478° K was selected. Based on these substructure limits, parameter studies were made for each vehicle station to determine the thickness of ablation material required to limit the aluminum to the specified temperature limits.

Ablation calculations are based on the assumption that the fabricated material is of a quality at least equal to that of the "lap-wound" glass-phenolic produced by Westinghouse Electric Corporation and tested in ABMA aerodynamic heating simulation facilities in 1959 and 1960.^{1, 2}

The initial skin temperature, at the beginning of reentry, was estimated to be 355° K to account for heat radiated in from the shroud during ascent.

The net effects of a small angle-of-attack (5 degrees or less) on the heating to a spinning vehicle are assumed to be negligible so that zero angle-of-attack procedures can be used. Some investigators³ state that this approach is conservative.

HEAT SHIELD MATERIALS

The reinforced plastic heat shield selected for Vehicle No. 1 is "lap-wound" glass-phenolic. This material was selected because of its low cost, availability, suitability to tape winding, and adequacy as a heat shield in a relatively mild heating environment.

The lap-winding technique is extremely flexible⁴ since the laminations are parallel to the vehicle centerline and a flat tape is used.² The orientation of the tape in relation to the gas flow, though questionable at the beginning in 1958, proved to be of no importance when tested in the severe environment of rocket motor exhaust jets.^{1, 2} The ablation results for lap-wound materials were quite comparable with those of tape-wrapped materials having laminations making a 20-degree angle with the cone surface (each lamination sloping away from the centerline toward the rear of the vehicle).

Glass-phenolic, asbestos-phenolic, and Thermolag T-230⁵ were considered for protection of the recovery tip bullhead from base aerodynamic heating. Of these materials the Thermolag T-230, a subliming compound, appears to be the most practical, weightwise. The base region is subjected to low heating rates for a short period of time after separation near 30.48 kilometers. Since the shear and heating are low in the base region, a reinforced plastic is considered unnecessary to prevent pitting and gouging.

RESULTS AND DISCUSSION

1. Aerodynamic Heating

Calculated real gas convective heating rates to a hot wall are presented in Figure 3 for the recovery tip and in Figure 4 for the destructible frustum. Maximum reentry aerodynamic heating occurs near an altitude of 38 kilometers (125,000 feet). The peak heating rates are between 125×10^4 kcal/m²hr on the aft destructible frustum and 650×10^4 kcal/m²hr at the 30-degree station on the hemisphere. The period of significant reentry heating above an altitude of 30.48 kilometers is about 20 seconds. Figure 3 shows that no significant aerodynamic heating occurs after 45 seconds, corresponding to an altitude of approximately 24 kilometers. The calculated heat fluxes on the recovery tip drop quite rapidly after 38 seconds, due to the sharp decrease in velocity resulting from a significant change in ballistic coefficient when the recovery tip separates from the aft frustum.

2. Skin Temperature Histories

Calculated external surface and internal substructure temperatures are shown in Figures 5 through 14 for several vehicle stations. For the recovery tip (Figures 5 through 10) the substructure temperatures peak at or near impact. The calculated bulkhead temperatures are shown in Figure 11 for Thermolag T-230, a subliming material on the outside of aluminum.

In Figures 12 through 14 are calculated external and internal surface temperature histories for three stations on the aft destructible frustum. The aluminum substructure temperature rises rapidly near 40 seconds, due to the recession of the ablation front toward the substructure.

Surface temperature distributions at several altitudes are presented in Figure 15. Below an altitude of 40.9 kilometers (134,000 feet) the entire vehicle surface has reached the ablation temperature.

3. Ablation

Ablation-depth histories calculated at selected stations along the vehicle are shown in Figure 16. As expected, the forward stations begin ablating at altitudes above 200,000 feet and the aft stations begin ablating at altitudes of approximately 150,000 feet. The ablation depths at three altitudes are plotted versus body station in Figure 17. From these ablation depths the weight of ablation material removed versus time or altitude was determined by procedures outlined in Appendixes B and C. Figure 18 shows the calculated ablation weight-loss versus flight time. At 100,000 feet the total weight of material lost is almost 25 pounds or 15.6 percent of the initial vehicle weight. Approximately 5 pounds have been removed from the recovery tip and 20 pounds from the destructible frustum at 100,000 feet. For a constant C_{DA} this weight loss results in the reduction of the ballistic coefficient from 110 lb/ft² to approximately 93 lb/ft².

4. Heat Shield Requirements

The total heat shield requirements necessary to limit the internal substructure to 378° K (220° F) on the recovery tip and 478° K (400° F) at 100,000 feet on the aft destructible frustum are shown in Figure 19. The calculated glass-phenolic thicknesses are between 14 and 24 millimeters (0.55 and 0.94 inch) on the recovery tip. Thicknesses vary from 3 millimeters (0.118 inch) at the aft end to 4 millimeters (0.153 inch) at the fore end of the destructible frustum.

Calculated total heat shield and aluminum substructure weights are tabulated in Table I. The total skin weight required is approximately 65 pounds, of which almost 45 pounds are on the destructible frustum. Seventy percent of the total skin weight is attributed to the glass-phenolic heat shield.

5. Initiation of Separation of Recovery Tip

In determining a criterion for initiation of separation, several devices such as timers, temperature sensors, and deceleration switches were considered. The deceleration or "g" switch was selected as being the most practical. As a result of the variation of "g" levels, aerodynamic loading, and subsequent effects of aerodynamic heating on the substructure due to variations in trajectories and vehicle parameters, additional reentry analyses of the destructible frustum became necessary. In addition to the nominal trajectory, minimum and maximum deceleration flights were analyzed. The primary differences in the trajectory parameters were determined by the Advanced Systems Laboratory, USAMICOM, and are shown in Table II.

Calculated aluminum substructure temperatures versus altitude for the destructible frustum are shown in Figures 20, 21, and 22. As anticipated, these data show the substructure temperature at 30.48 kilometers to be highest for the vehicle flying the minimum "g" trajectory. The substructure temperature is lowest at any given altitude for the maximum "g" trajectory. This trend is reasonable due to the large variation in flight time from 100 kilometers to 30.48 kilometers and the time dependence of heat flow through an ablation material having a low thermal diffusivity. The flight time from 100 kilometers to 30.48 kilometers is approximately 34.5 and 25.5 seconds, respectively, for the minimum and maximum "g" trajectories.

Immediately below an altitude of 30.48 kilometers the substructure temperatures rise sharply. This is primarily due to the proximity of the receding ablation front to the aluminum substructure.

CONCLUSIONS

AMRAD Vehicle No. 1 is exposed to a relatively mild reentry environment. The major portion of the vehicle is exposed to maximum aerodynamic heating rates of 300×10^4 kcal/m²hr or slightly less.

The calculated glass-phenolic heat shield required for Vehicle No. 1 weighs about 46 pounds with 62 percent of this located on the destructible frustum. The aluminum substructure weighs approximately 19 pounds with 87.5 percent of this located on the destructible frustum.

At any given altitude above 30 kilometers, the calculated substructure temperature for the aft destructible frustum increases as the vehicle trajectory goes from the maximum, to nominal, to minimum deceleration cases. The increase in flight time to a given altitude is the major factor in this trend.

Table I. Skin Weights

Vehicle section	Aluminum thickness (in.)	Aluminum weight (lb)	Heat shield weight (lb)	Total skin weight (lb)
Recovery tip	0.054	2.485	17.423	*19.908
Destructible frustum	0.054	16.62	28.28	44.90

*Includes insulation and substructure on recovery tip bulkhead.

Table II. Relationships Between Maximum and Minimum Deceleration Trajectories Compared With the Nominal

Parameter	Maximum "g"	Minimum "g"
$W/C_D A$	90% nominal	110% nominal
Reentry velocity	104% nominal	95% nominal
Reentry angle	26 degrees	20 degrees
Wind	Headwind	Tailwind

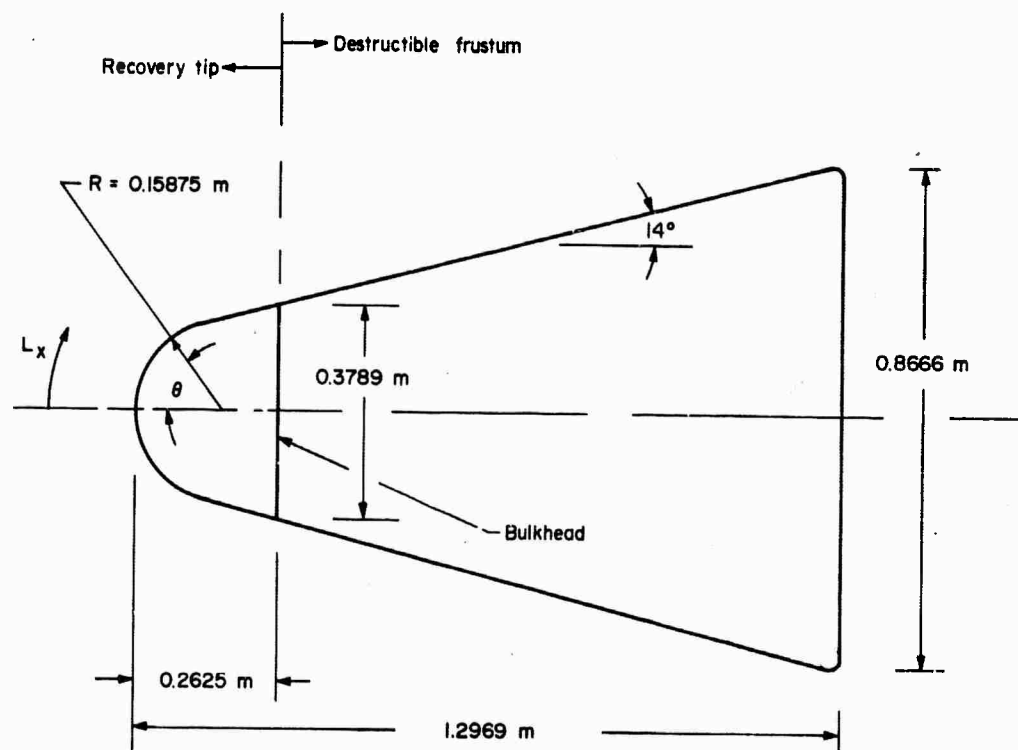


Figure 1. Sketch of AMRAD Vehicle, Number One

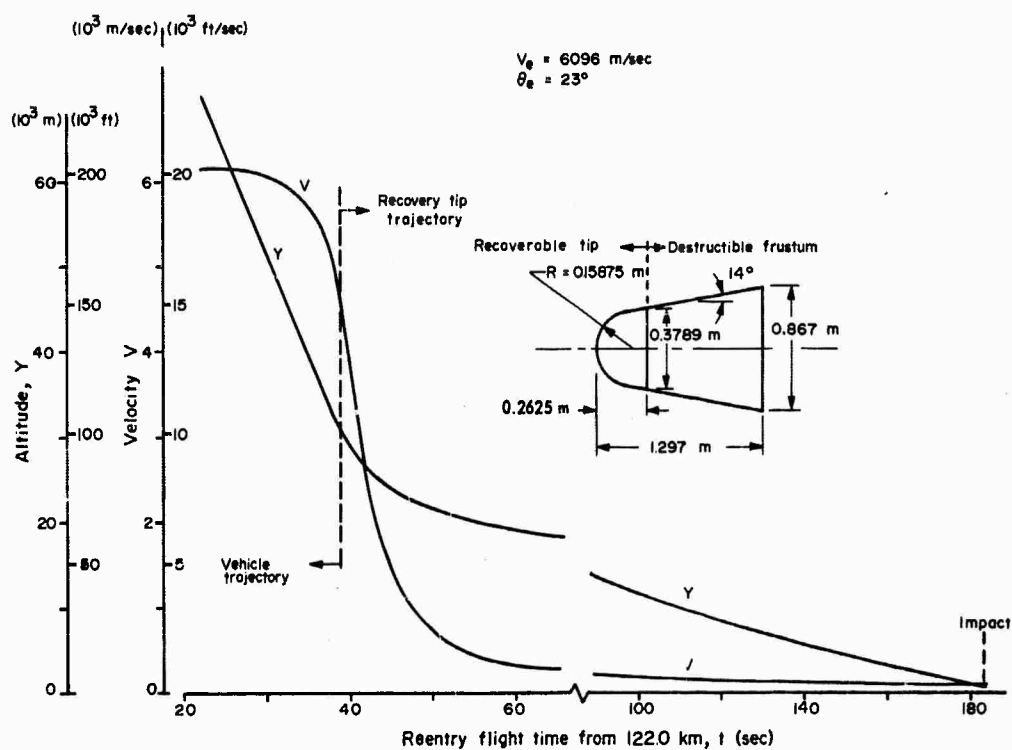


Figure 2. Reentry Trajectory for Vehicle to 30.48 Kilometers and for Recovery Tip to Impact

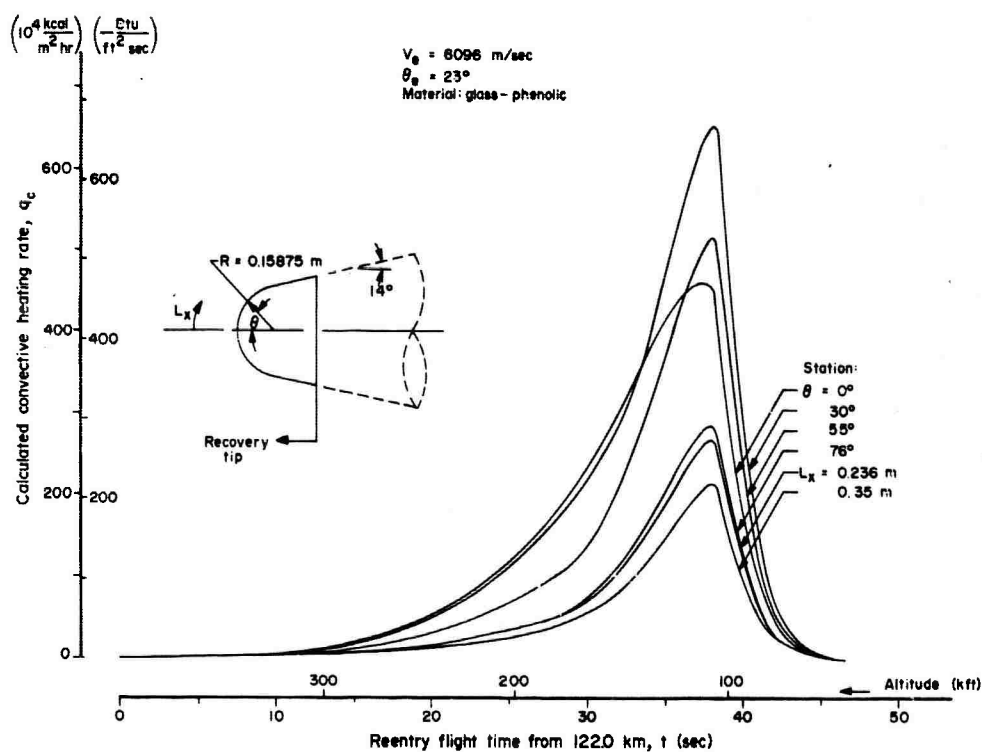


Figure 3. Calculated Convective Heating Rates for Recovery Tip

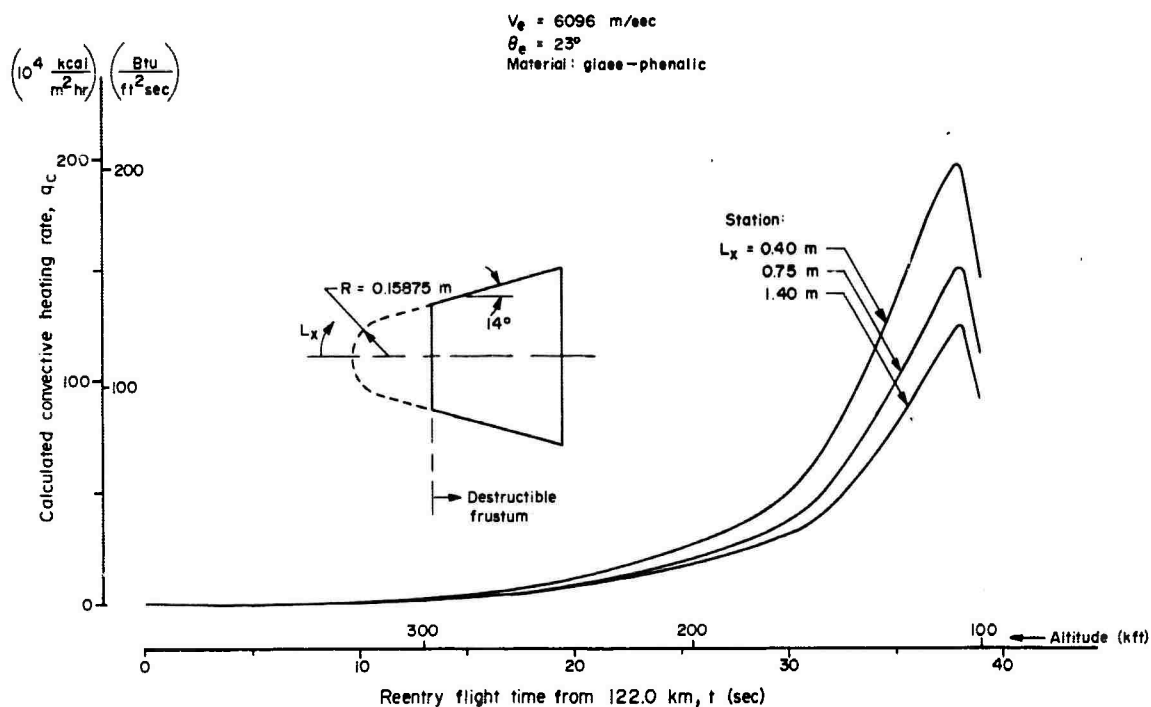


Figure 4. Calculated Convective Heating Rates for Destructible Frustum

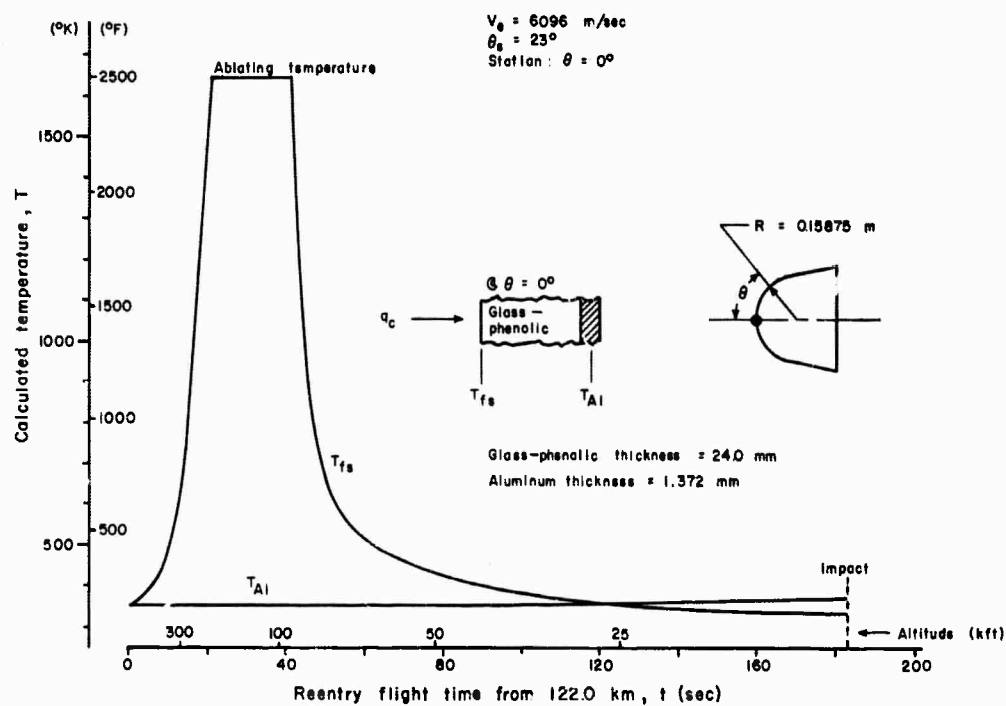


Figure 5. Calculated Exposed and Unexposed Surface Temperature Histories at the Stagnation Point of the Recovery Tip

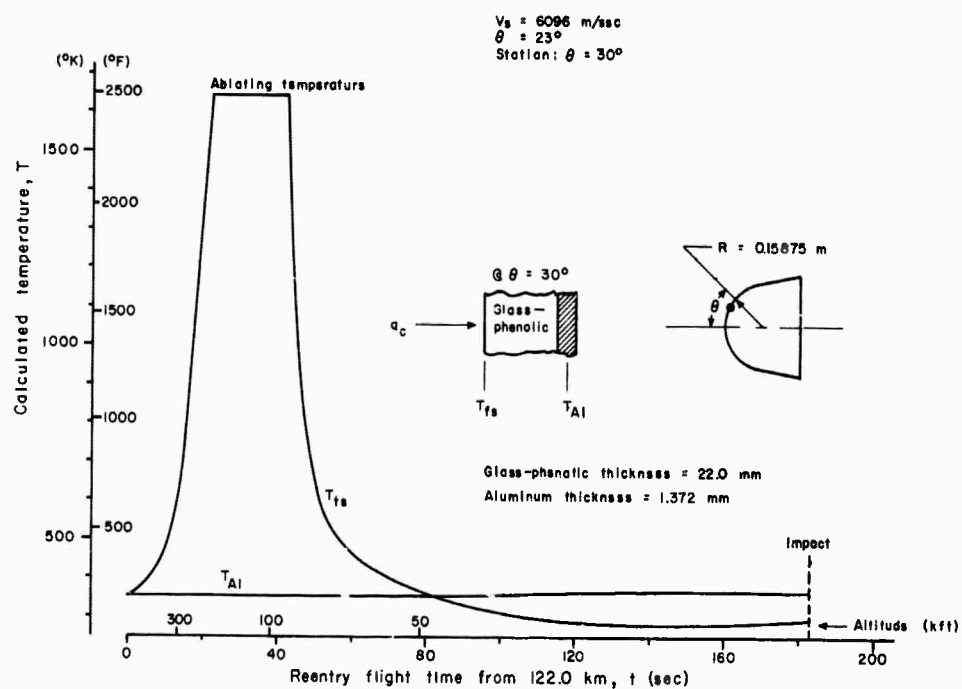


Figure 6. Calculated Exposed and Unexposed Surface Temperature Histories at the 30-Degree Station of the Recovery Tip

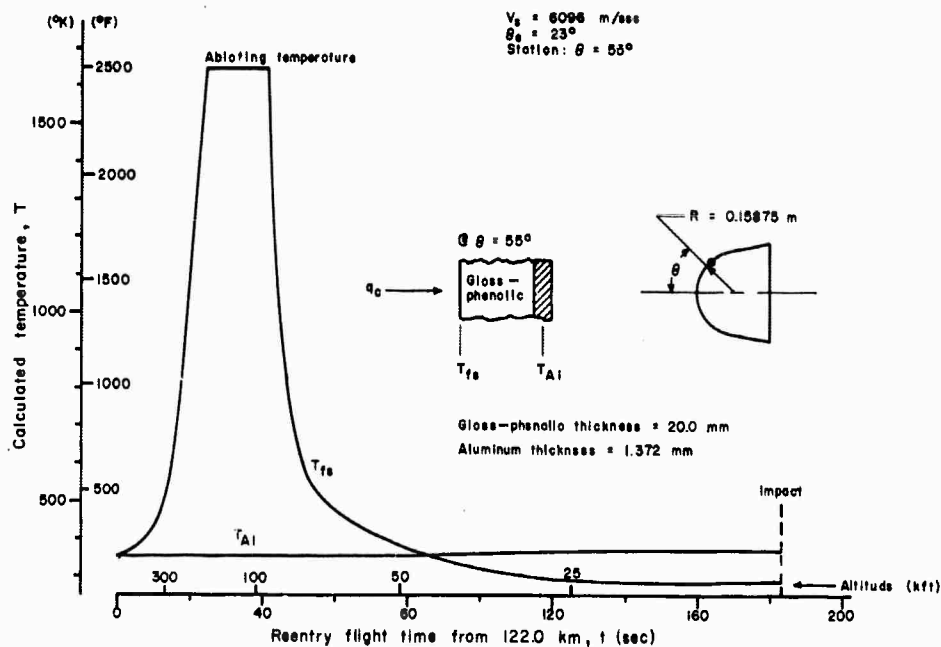


Figure 7. Calculated Exposed and Unexposed Surface Temperature Histories at the 55-Degree Station of the Recovery Tip

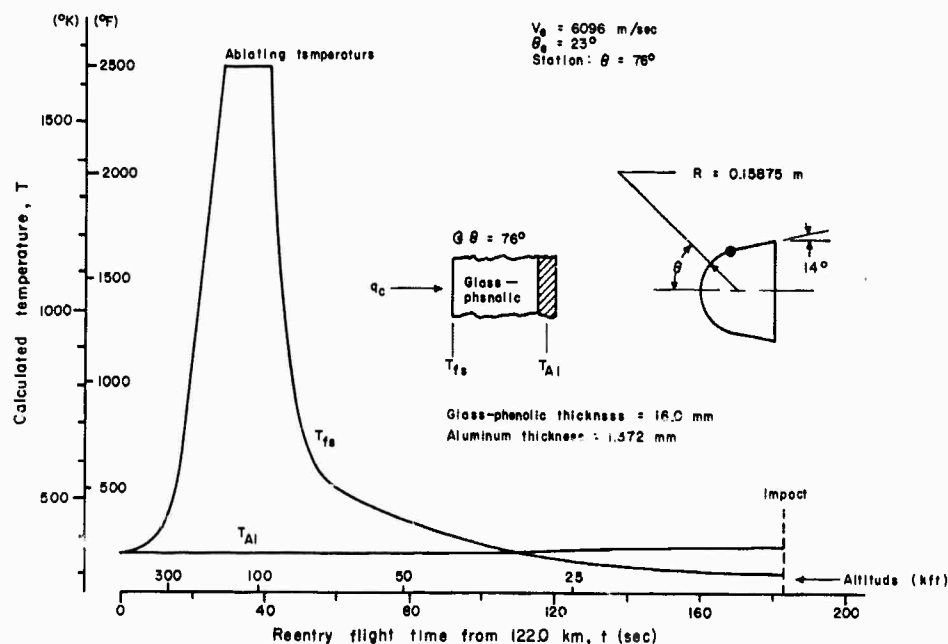


Figure 8. Calculated Exposed and Unexposed Surface Temperature Histories at the 76-Degree Station of the Recovery Tip

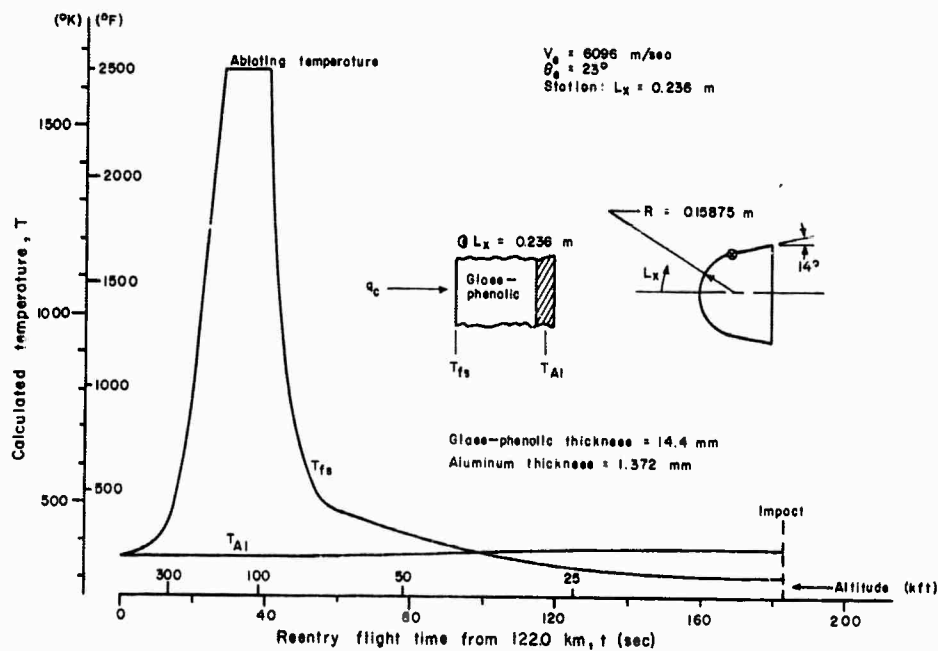


Figure 9. Calculated Exposed and Unexposed Surface Temperature Histories at the $L_x = 0.236$ -M Station of the Recovery Tip

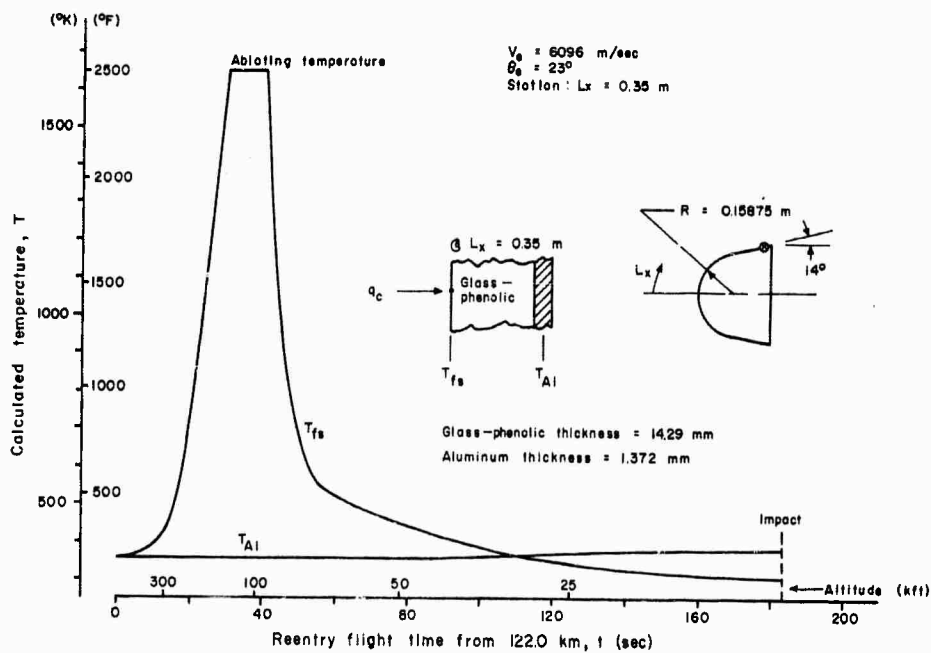


Figure 10. Calculated Exposed and Unexposed Surface Temperature Histories at the $L_x = 0.35$ -M Station of the Recovery Tip

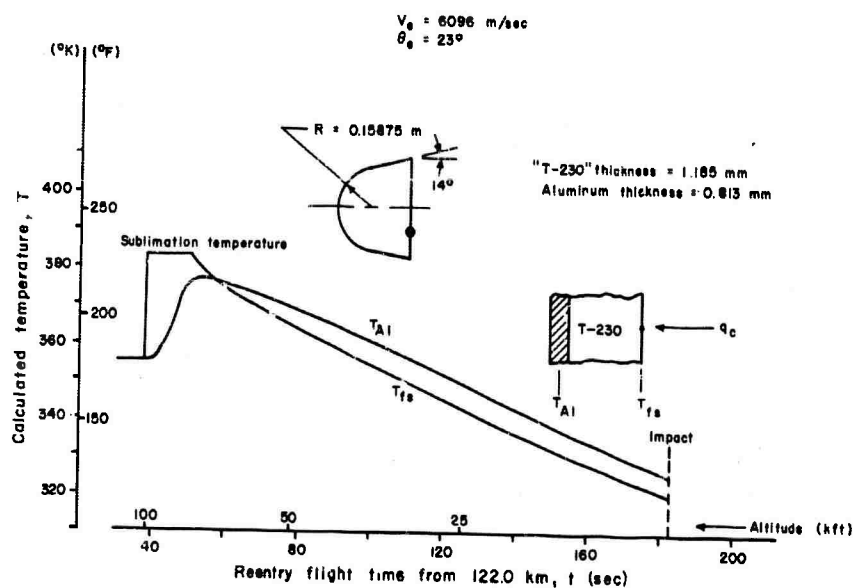


Figure 11. Calculated Exposed and Unexposed Surface Temperature Histories on the Bulkhead of the Recovery Tip

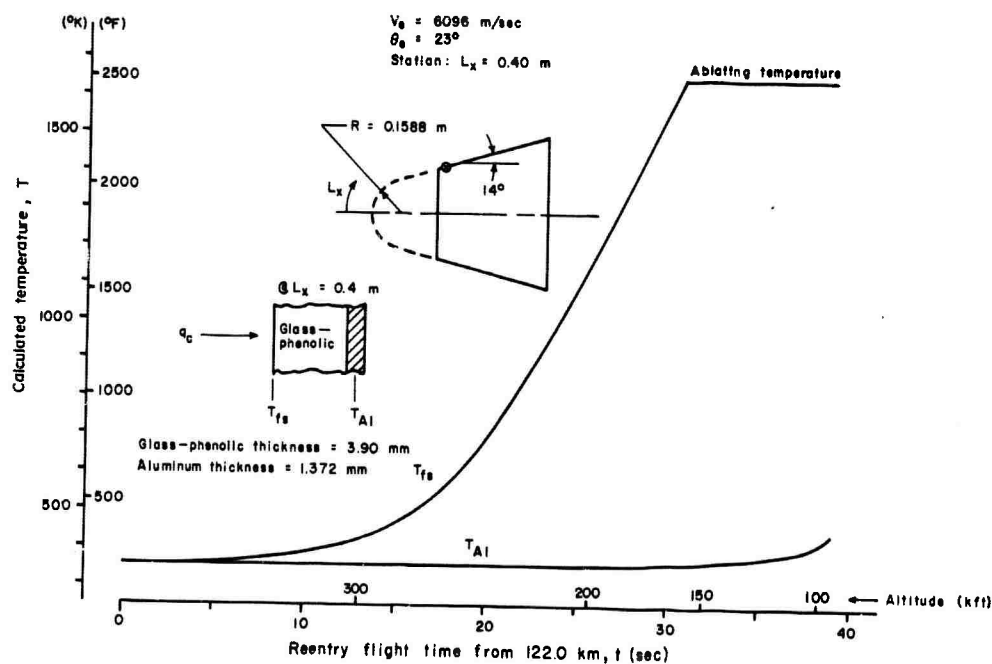


Figure 12. Calculated Exposed and Unexposed Surface Temperature Histories at the $L_x = 0.4$ -M Station of the Destructible Frustum

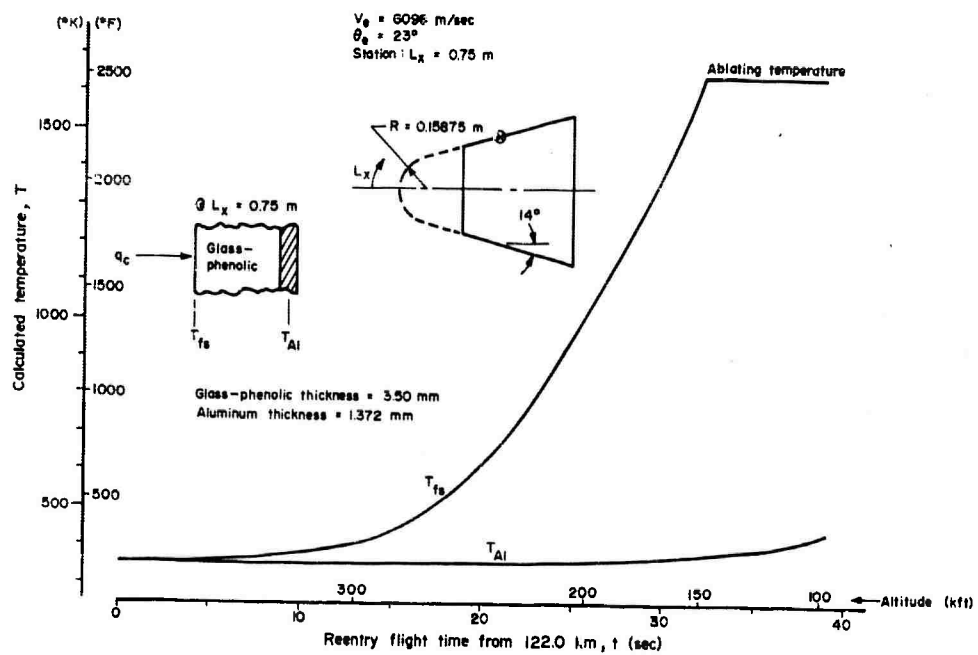


Figure 13. Calculated Exposed and Unexposed Surface Temperature Histories at the $L_x = 0.75$ -M Station of the Destructible Frustum

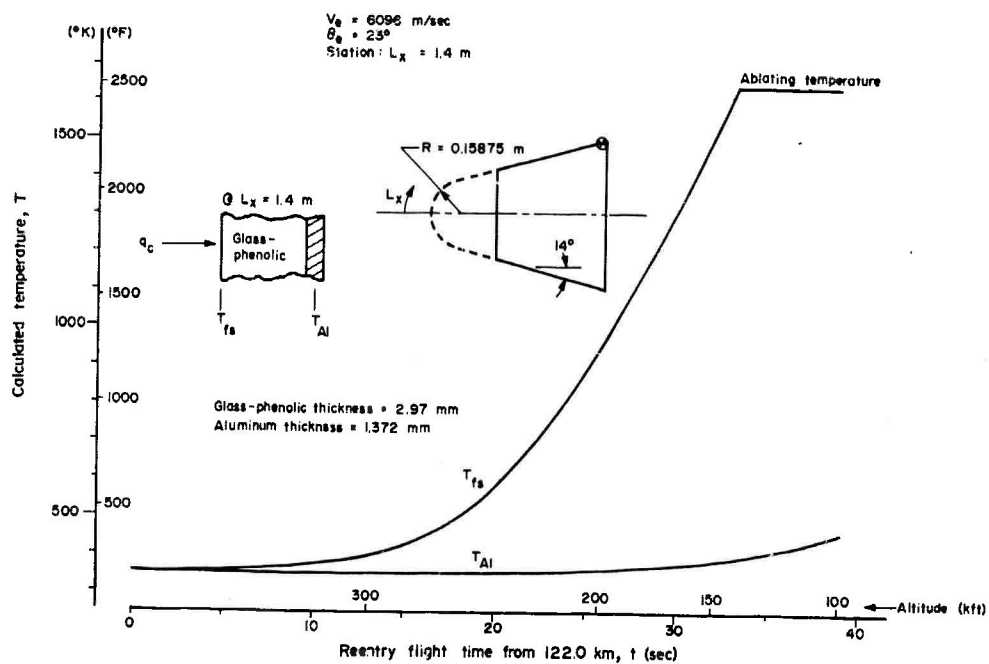


Figure 14. Calculated Exposed and Unexposed Surface Temperature Histories at the $L_x = 1.4$ -M Station of the Destructible Frustum

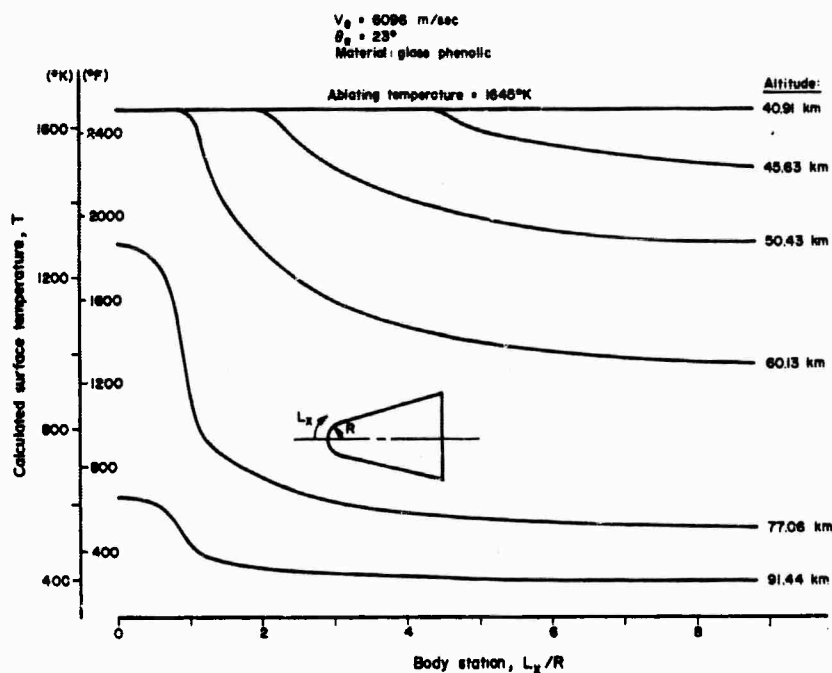


Figure 15. Calculated Exposed Surface Temperature Distributions

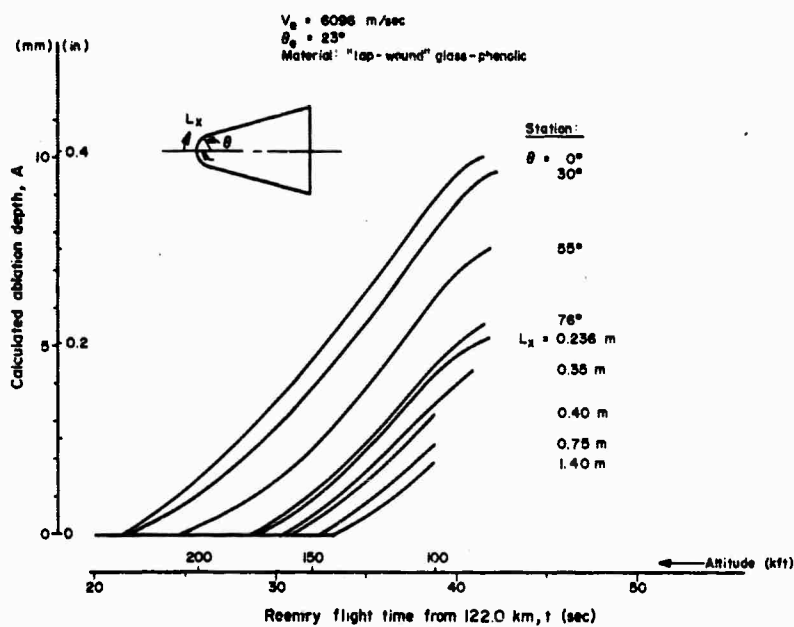


Figure 16. Calculated Histories of Ablation Depths for Stations

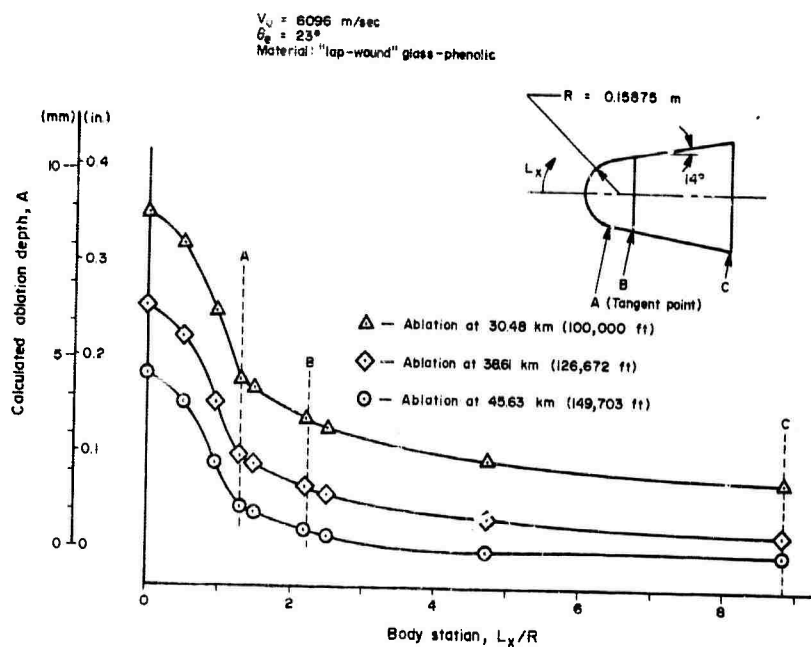


Figure 17. Calculated Ablation Depths at Three Altitudes Versus Body Station

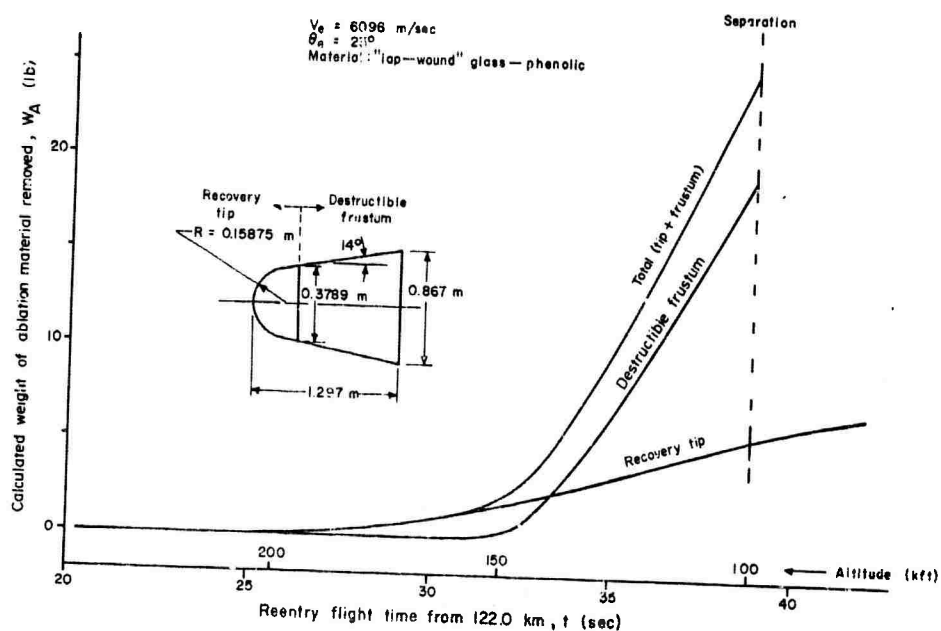


Figure 18. Calculated History of Weight Removed by Ablation

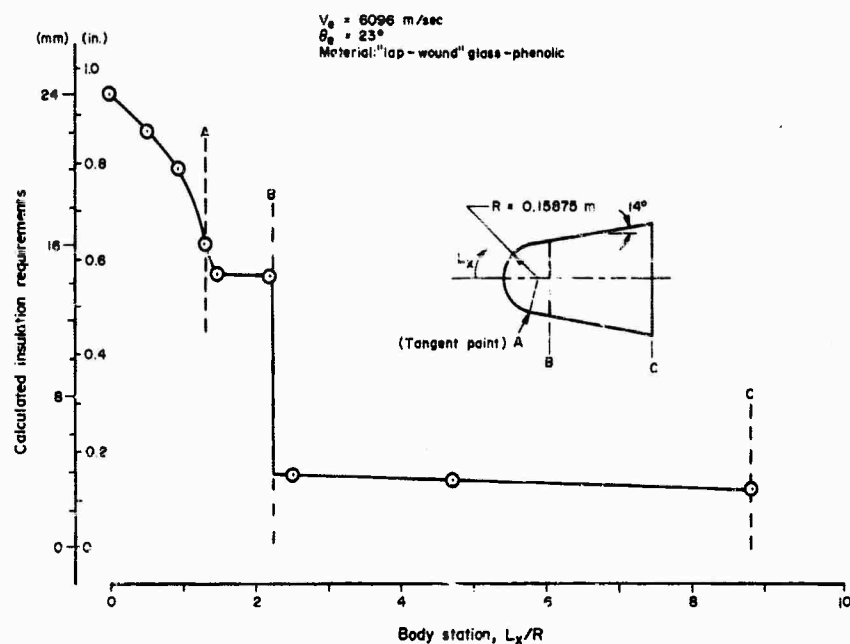


Figure 19. Calculated Total Insulation Thickness Requirements

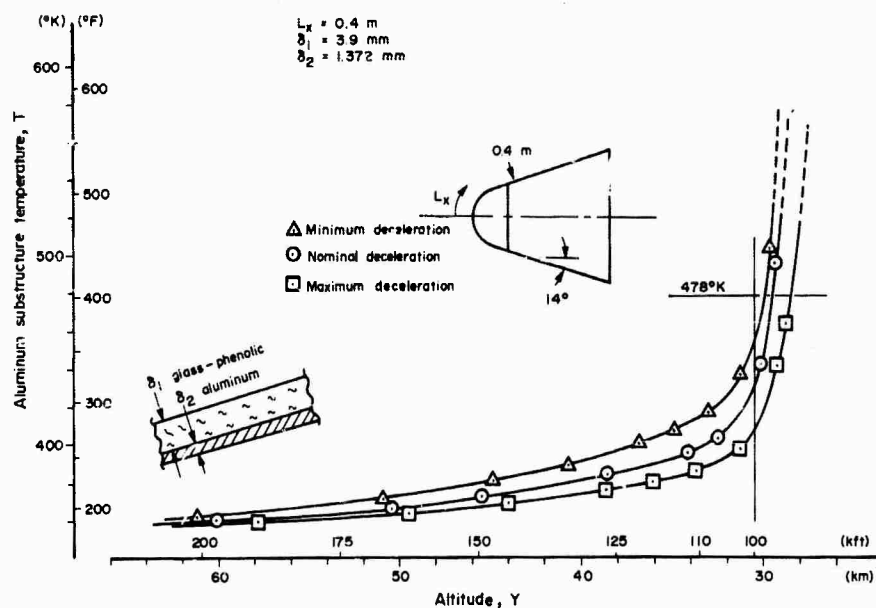


Figure 20. Calculated Substructure Temperature Histories for Forward Station of Aft Frustum

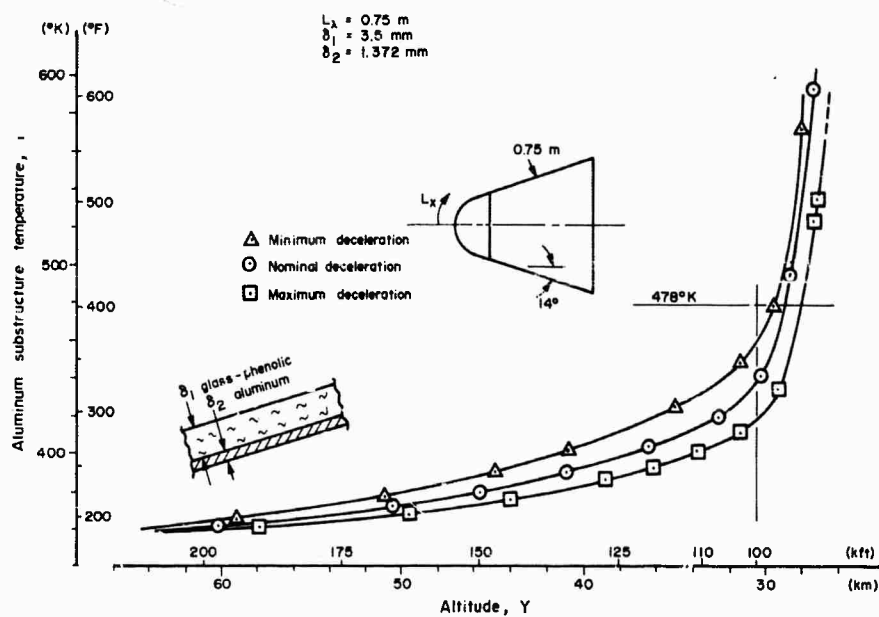


Figure 21. Calculated Substructure Temperature Histories for Intermediate Station of Aft Frustum

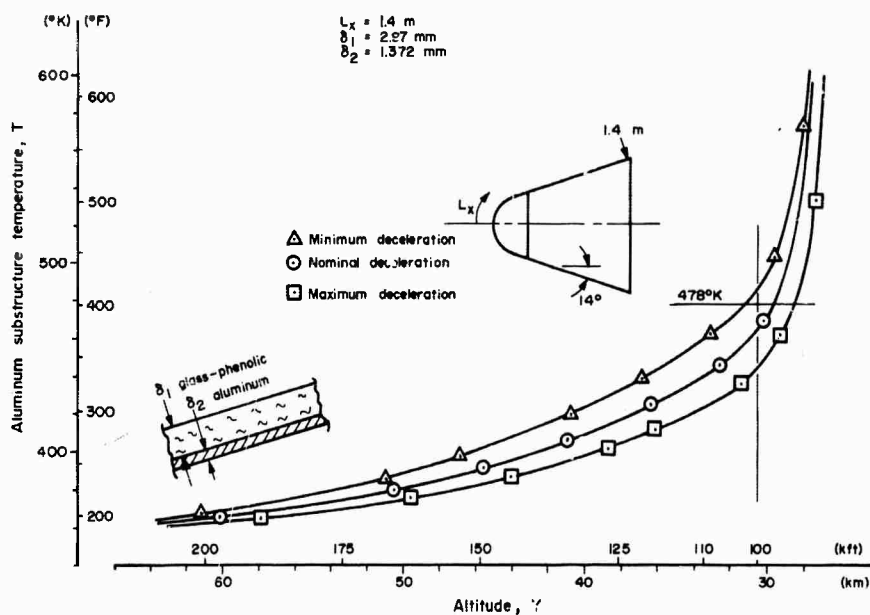


Figure 22. Calculated Substructure Temperature Histories for Aft Station of Frustum

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Appendix A

USAMICOM AERODYNAMIC HEATING METHODS

Widely accepted real gas methods are employed in the USAMICOM theoretical heating analyses. At the stagnation point the Fay and Riddell method with a modified Lewis number (L) contribution⁶ is used. The equation for q_c at $\theta = 0^\circ$ is

$$q_c = C_1 D_n^{-1/2} (\rho_w \mu_w)^{0.1} (\rho_\delta \mu_\delta)^{0.4} \left(\frac{P_\delta}{\rho_\delta} \right)^{0.25} \left[1 + (L - 1) \left(\frac{h_{D_\delta} - h_{D_w}}{h_\delta - h_w} \right) \right]^{0.48} (h_s - h_w)$$

where C_1 is a constant.

At body stations other than the stagnation point, the laminar heating rate is found by modifying the stagnation point rate according to the pressure distribution.

For turbulent flow the theoretical heating rates are based on methods developed by AVCO⁷ with the modified L contribution inserted.

$$q_c = C_2 S^{-1} P_r^{-2/3} \mu_\delta Re_\delta^{0.8} \left[1.037 [G(X)] \right]^{0.2} \left[1 + (L - 1) \left(\frac{h_{D_\delta} - h_{D_w}}{h_\delta - h_w} \right) \right]^{0.48} (h_r - h_w)$$

To be conservative in the design of hardware, both laminar and turbulent heating rates are calculated at any given station except the stagnation point. The higher heating rate is then selected for use in determining the structure response. In this manner, transition is effected and no other margins of safety are incorporated.

Ideal gas procedures based on methods of Sibulkin, Eckert, and Van Driest have also been used extensively in the past. By proper modifications the reference temperature ideal gas procedure gives heating rates comparable to the real gas procedure.⁸

The pressure distribution on a hemisphere is determined from the modified Newtonian impact theory matched with a Prandtl-Meyer expansion to the tangent point. For the frustum, a blast wave method is used to find the pressure decay between the tangent point and the sharp cone value. These procedures are slightly conservative

compared to the GASL 3-D method of characteristics.⁹ Results from the blunt cone pressure routines used herein have been favorably compared with experimental pressure data.⁹

The viscosity, compressibility factor, specific heat ratios, local enthalpy, local temperature, local speed of sound, and local density are taken from data published by C. G. Hansen¹⁰ and J. Hilsenrath.¹¹

On the hemisphere a modified Newtonian flow theory is used to determine the velocity gradient.

Before and after ablation, a forward finite difference heat conduction procedure is used. During ablation a special conduction procedure applicable to conduction in a material having a receding surface is utilized. Both of these procedures compare well with exact solutions.

Ablation of material in flight is based on experimental results of material performance tests in liquid propellant rocket motors. The average effective heat of ablation, H_A , versus heating rates (Figure 23) is determined by use of ablation depth measurements and metallic calorimeters.

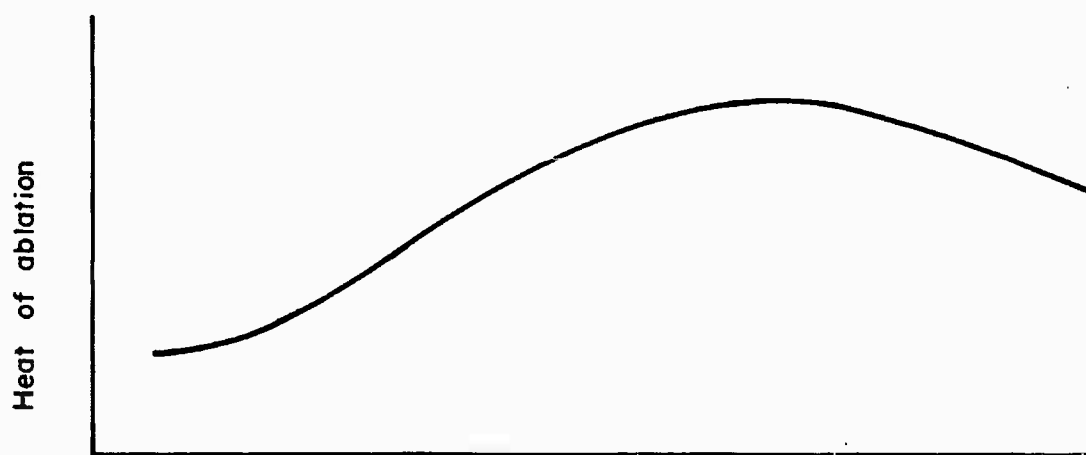


Figure 23. Experimental Thermal Performance of a Reinforced Plastic

Ablation and calibration models used in the tests had tip diameters from 19.05 to 635 millimeters. The stagnation temperatures were from 1920° to 4700° K and the pressures were between 70,000 and 105,000 kg/m². Hot wall heat fluxes ranged between 50×10^4 and 2000×10^4 kcal/m²hr.

Even though the rocket motor exhaust gas composition differs considerably from air, excellent flight and theoretical ablation correlations have been obtained using this semiempirical method. One subscale and three full-scale IRBM vehicles flying near Mach 15 were recovered after flight and measured for material removal during the JUPITER research and development program.^{12, 13, 14} These ablation depth correlations were for glass-melamine, glass-phenolic, refrasil-phenolic, and asbestos-phenolic materials. The flight ablation depths of all four materials agreed very closely with the predicted values, especially on the hemispherical portion of the blunt cones.

Good comparisons have also been obtained between theoretical and flight data for the heat shield on a BIG JOE capsule reentering the earth's atmosphere approximately 6,096 m/sec.^{14, 15}

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Appendix B

VOLUME OF HEMISPHERICAL SECTION

Often in heat transfer work and in the design of blunt vehicles, it is necessary to calculate the weight of material removed by ablation or to determine the entire skin weight of hemispherical tips. To obtain the weight it is required that the volume be known.

The volume of the spherical section shown in Figure 24 is readily computed with the following equation:

$$V_t = 2\pi\Delta\theta \sum_{n=1}^{n=\phi/\Delta\theta} [R_o^2\delta_n - R_o\delta_n^2 + \delta_n^3/3] \sin \theta_n \quad (1)$$

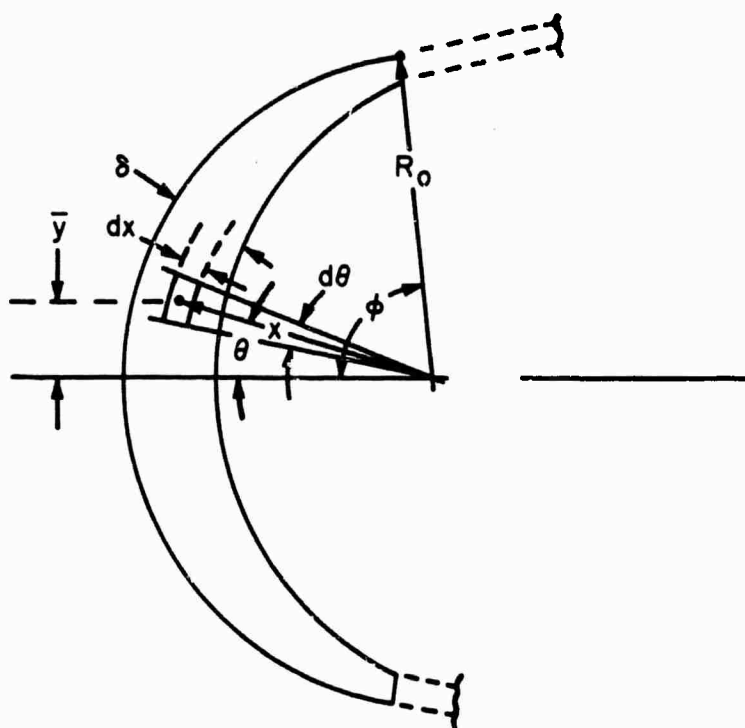


Figure 24. Volume of a Spherical Section

This equation is derived as follows:

x is the radius vector to the center of gravity of the incremental area

12

$\bar{y} = x \sin \theta$ is the moment arm

$dA = x d\theta dx$ is the incremental area

$$dV = 2\pi \bar{y} dA = 2\pi x^2 \sin \theta d\theta dx$$

$$\begin{aligned} \therefore V_t &= 2\pi \int_{\theta=0^\circ}^{\theta=\phi} \int_{R_o-\delta}^{R_o} x^2 \sin \theta d\theta dx \\ &= \frac{2\pi}{3} \int_{\theta=0^\circ}^{\theta=\phi} \left[R_o^3 - (R_o - \delta)^3 \right] \sin \theta d\theta \end{aligned} \quad (2)$$

$$V_t = 2\pi \Delta\theta \sum_{n=1}^{n=\phi/\Delta\theta} \left[R_o^2 \delta_n - R_o \delta_n^2 + \delta_n^3/3 \right] \sin \theta_n \quad (3)$$

By proper selection of the incremental angle, $\Delta\theta$, commensurate with the particular variation of wall thickness, accurate volumes on a spherical tip can be obtained by use of Equation (3). The thickness δ_n , measured normal to the external surface, is the average thickness over the $\Delta\theta$ at increment n .

Appendix C

VOLUME CALCULATION FOR FRUSTUMS OF RIGHT CIRCULAR CONES

Equations determining the volume for frustums of right circular cones were derived using Pappus' second proposition:

"If a figure of area A revolves about an axis in its plane but not cutting it, then for a complete revolution, the volume of the solid generated is:

$$V = 2\pi\bar{y}A \quad (4)$$

where $\bar{y}$ is the distance from the axis to the center of gravity of A. "

The frustum volume equations were deduced for a linear and a nonlinear variation of skin thickness, δ , with length, L_x .

1. Linear Variation of Thickness With Length

The volume of the frustum of a right circular cone having a linear variation of thickness with length, L_x , may be calculated by adding the volume of the solid generated by the rectangular area "A" (Figure 25) to the volume of the solid generated by the triangular area "B" in the following manner:

For area "A" the volume is

$$V_A = 2\pi\delta_2 L_x \left[R \sin \theta + \frac{L_x}{2} \cos \theta - \frac{\delta_2}{2} \sin \theta \right] \quad (5)$$

and for area "B" the volume is

$$V_B = 2\pi L_x \left(\frac{\delta_1 + \delta_2}{2} \right) \left[R \sin \theta + \frac{L_x}{3} \cos \theta - \left(\delta_1 + \frac{\delta_1 - \delta_2}{3} \right) \sin \theta \right] \quad (6)$$

Combining Equations (5) and (6) gives the total volume, V_t

$$V_t = 2\pi L_x \left(\frac{\delta_1 + \delta_2}{2} \right) \left[R \sin \theta + \left(\frac{\delta_1 + 2\delta_2}{\delta_1 + \delta_2} \right) \left(\frac{L_x}{3} \right) \cos \theta - \left(\frac{\delta_1^2 + \delta_1\delta_2 + \delta_2^2}{\delta_1 + \delta_2} \right) \frac{\sin \theta}{3} \right] \quad (7)$$

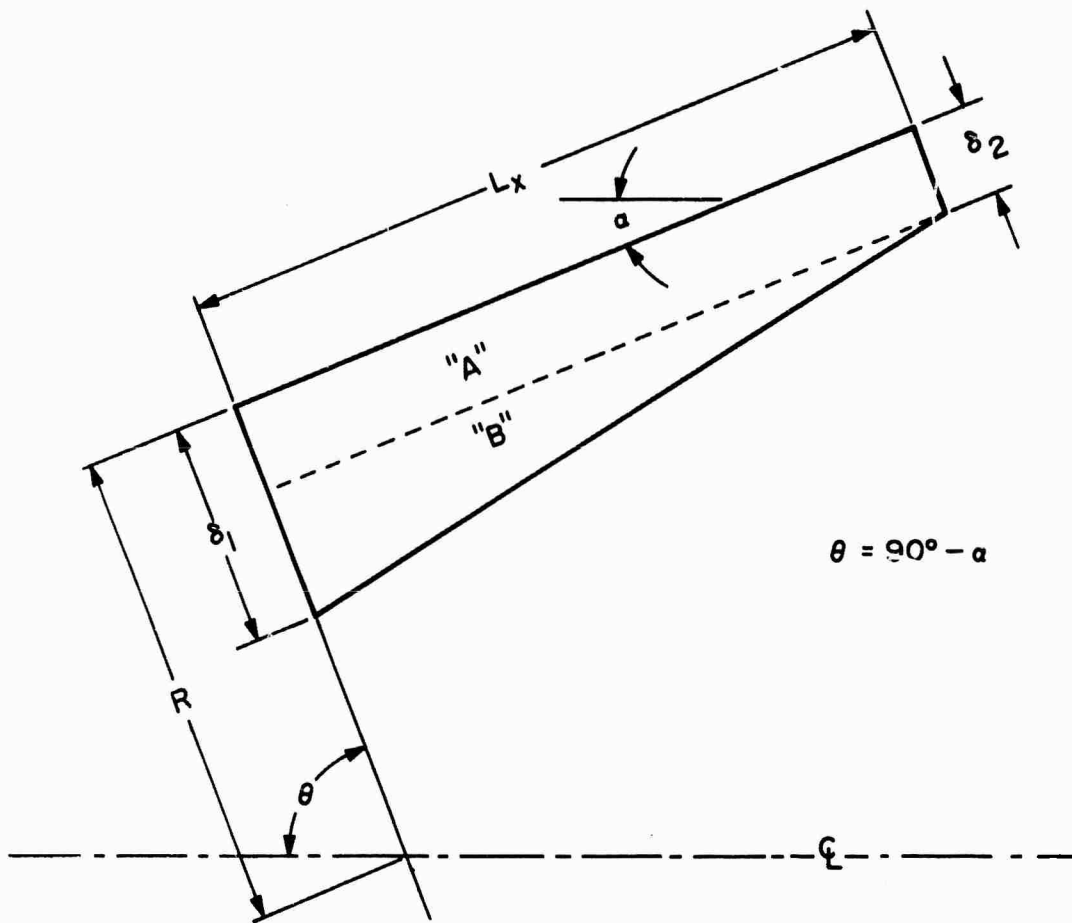


Figure 25. Linear Variation of Thickness With Length (L)

2. Nonlinear Variation of Thickness With Length

The volume of the frustum of a right circular cone having a nonlinear variation of thickness with length can be calculated from the following equation where n is the increment being considered in the x direction:

$$V_t = 2\pi\Delta x \sum_{n=1}^{n = x_b/\Delta x} \left[R\delta_n + \frac{\cos \theta x_n \delta_n}{\sin^2 \theta} - \frac{\delta_n^2}{2} \right] \quad (8)$$

In deriving Equation (8) (Figure 26):

The incremental area is $dA = \delta dL$

The moment arm is y_c

The incremental volume is $dV = 2\pi y_c \delta dL$

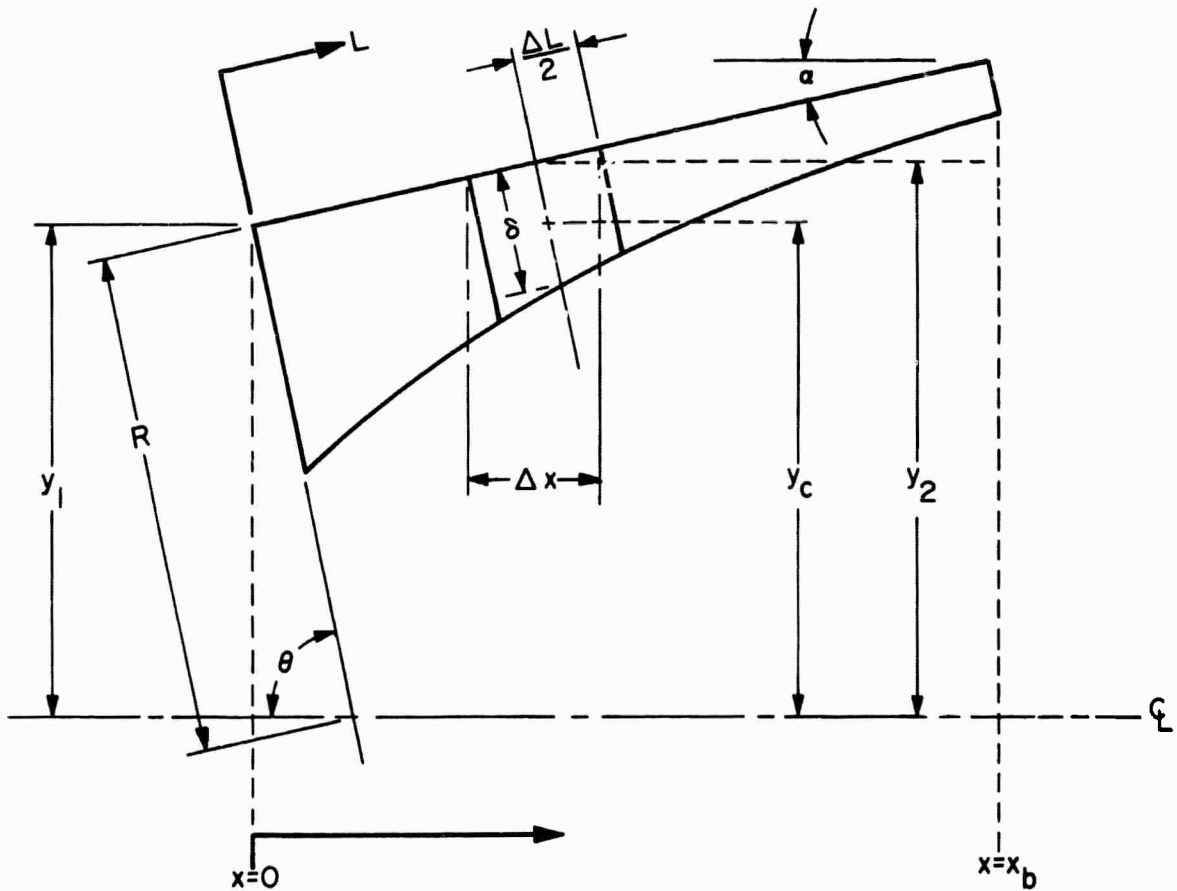


Figure 26. Nonlinear Variation of Thickness With Length (L)

Other pertinent equations are:

$$dL = \frac{dx}{\sin \theta}$$

$$Y_1 = R \sin \theta$$

$$Y_2 = Y_1 + x \cot \theta$$

$$Y_c = Y_2 - \frac{\delta}{2} \sin \theta$$

$$\therefore Y_c = R \sin \theta + x \cot \theta - \frac{\delta}{2} \sin \theta$$

Equation (8) can be used to accurately determine the volume of ablation material removed due to hypersonic flight in the atmosphere and the volume of an entire frustum of nonlinear thickness with length.

Appendix D

SIMPLE INTERNAL SURFACE DESCRIPTION FOR A HEMISPHERICAL TIP HAVING A SKIN THICKNESS VARYING WITH ANGULAR STATION

In the design of reentry vehicles, it is frequently desirable or necessary to deviate slightly from optimum ablation material or heat-sink thickness requirements on a hemispherical tip to simplify the internal surface configuration. A simple internal configuration is advantageous due to reduced costs of fabrication, especially for vehicles that are to be produced only in limited numbers.

For a given external spherical configuration and for known skin thickness requirements varying with angular stations (Figure 27), a procedure has been derived for determining an internal surface configuration described by a spherical sector with the radius originating on the vehicle centerline.

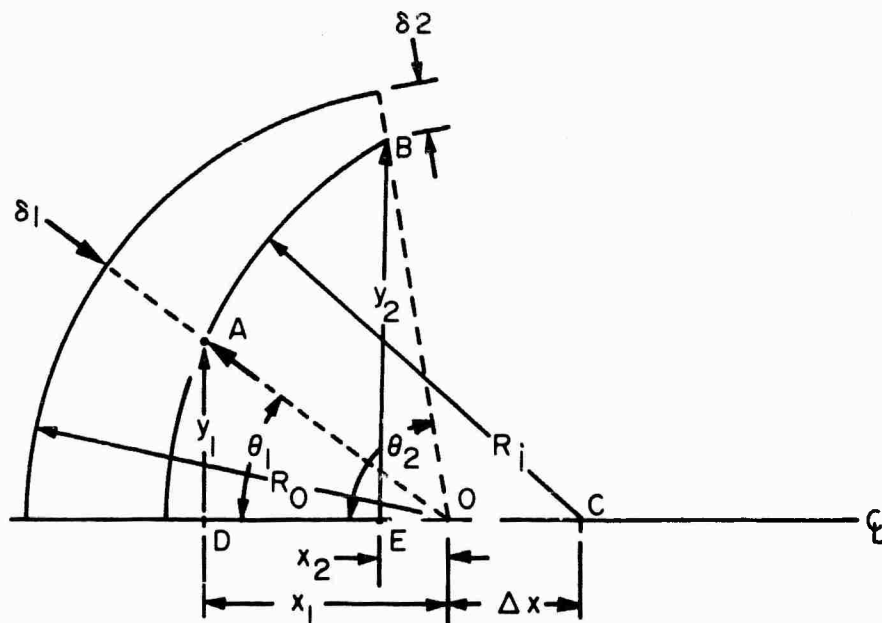


Figure 27. Procedure for Describing a Simple Internal Surface Configuration

Known parameters required for solution of the internal configuration are (Figure 27):

R_o - External radius

δ_1 - Skin thickness measured normal to the external surface
at any known θ_1

δ_2 - Skin thickness measured normal to the external surface
at any known θ_2

It is required to find:

Center location, C, on the centerline for the internal surface

Internal surface radius, R_i

Calculated skin thicknesses at any desired angular station

With the known parameters listed in Figure 27 let

$$x_1 = (R_o - \delta_1) \cos \theta_1$$

$$x_2 = (R_o - \delta_2) \cos \theta_2$$

$$y_1 = (R_o - \delta_1) \sin \theta_1$$

$$y_2 = (R_o - \delta_2) \sin \theta_2$$

Then from triangle ACD

$$y_1^2 + (x_1 + \Delta x)^2 = R_i^2 \quad (9)$$

and from triangle BCE

$$y_2^2 + (x_2 + \Delta x)^2 = R_i^2 \quad (10)$$

Solving Equations (9) and (10) simultaneously results in

$$y_1^2 - y_2^2 + (x_1 + \Delta x)^2 - (x_2 + \Delta x)^2 = 0$$

or

$$(x_1^2 + y_1^2) - (x_2^2 + y_2^2) + 2\Delta x(x_1 - x_2) = 0 \quad (11)$$

and

$$\Delta x = \frac{(x_2^2 + y_2^2) - (x_1^2 + y_1^2)}{2(x_1 - x_2)} \quad (12)$$

Equation (12) defines the location of the internal surface center lying on the vehicle centerline.

Substituting the Δx from Equation (12) into Equation (9) yields the solution for the internal radius

$$R_i = \sqrt{y_i^2 + (x_i + \Delta x)^2} \quad (13)$$

To find the skin thickness at any spherical station, θ , let

$$x = (R_o - \delta_\theta) \cos \theta$$

and

$$y = (R_o - \delta_\theta) \sin \theta$$

then from right triangle relations

$$y^2 + (x + \Delta x)^2 = R_i^2 \quad (14)$$

where Δx is length found from solution of Equation (12). Substituting x and y into Equation (14) gives

$$(R_o - \delta_\theta)^2 \sin^2 \theta + [(R_o - \delta_\theta) \cos \theta + \Delta x]^2 = R_i^2$$

which expands to

$$(R_o - \delta_\theta)^2 + 2\Delta x(R_o - \delta_\theta) \cos \theta + (\Delta x^2 - R_i^2) = 0 \quad (15)$$

Solving for $R_o - \delta_\theta$ in Equation (15) yields

$$R_o - \delta_\theta = \frac{-2\Delta x \cos \theta \pm \sqrt{4\Delta x^2 \cos^2 \theta - 4(\Delta x^2 - R_i^2)}}{2} \quad (16)$$

Since $R_o - \delta_\theta$ must be positive for the hemispheres considered, the radical in Equation (16) must be positive; thus solving for δ_θ , the skin thickness, at any angular station, θ , gives

$$\delta_\theta = R_o + \Delta x \cos \theta - \sqrt{R_i^2 - \Delta x^2 \sin^2 \theta} \quad (17)$$

To quickly obtain the best solution of an internal hemispherical configuration with the center on the vehicle centerline, several pairs of required skin thicknesses (determined by stress and thermodynamic

analyses) at known angular stations are investigated by use of a high-speed digital computer. The calculated skin thickness obtained from the computer program for each internal surface configuration (one configuration for each pair of skin thicknesses input to the program) is compared with known skin thickness requirements previously determined from stress and thermodynamic analyses.

Selection of the best internal surface configuration is then made from the skin thickness comparisons by considering primarily the effects of skin thickness deviations on accomplishment of the mission and the effects of skin thickness deviations on the total weight of the hemispherical section.

With the skin thickness incorporated as an output to the configuration procedure, the weight of the material on a hemisphere is readily obtained by use of the volume equations presented in Appendix B.

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Security Classification

DOCUMENT CONTROL DATA - R&D

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1. ORIGINATING ACTIVITY (Corporate author) Structures and Mechanics Laboratory Directorate of Research and Development U. S. Army Missile Command <u>Redstone Arsenal, Alabama</u>		2a. REPORT SECURITY CLASSIFICATION Unclassified	
		2b. GROUP	
3. REPORT TITLE THEORETICAL EFFECTS OF REENTRY AERODYNAMIC HEATING ON THE EXTERNAL SKIN STRUCTURE OF AMRAD EXPERIMENT NUMBER ONE			
4. DESCRIPTIVE NOTES (Type of report and inclusive dates)			
5. AUTHOR(S) (Last name, first name, initial) Burleson, W. G. and Reynolds, R. A.			
6. REPORT DATE 30 April 1965		7a. TOTAL NO. OF PAGES 38	7b. NO. OF REFS 15
8a. CONTRACT OR GRANT NO.		9a. ORIGINATOR'S REPORT NUMBER(S) RS-TR-65-3	
b. PROJECT NO.			
c. AMC Management Structure Code No. 5900.21.16229		9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report) AD _____	
d.			
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13. ABSTRACT Calculated reentry aerodynamic heating effects on the external skin of an ICBM reentry test vehicle having a relatively low weight-to-drag ratio are presented in this report. The vehicle is a blunt cone with the aft portion designed to fail just after maximum heating and the forward portion designed to survive to impact. The tape-wound, reinforced plastic heat shield is subjected to maximum reentry heating rates between 125×10^4 and 650×10^4 kcal/m ² hr. Resulting external and internal surface temperature histories are given. Effects of extreme trajectory, vehicle characteristics, and atmosphere variations on the aluminum substructure temperature histories are discussed.			

DD FORM 1 JAN 64 1473

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