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Probability of Detecting Ships With an OTH Radar System

[Unclassified Title]

JON DAVID WILSON

*Radar Analysis Staff
Radar Division*

July 10, 1974

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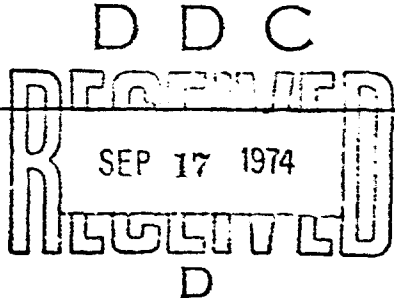
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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) (U) An over-the-horizon (OTH) radar uses ionospheric reflection of high-frequency radio waves to propagate to areas far beyond the normal radar horizon. Two principle probabilities are associated with an OTH radar: the probability of successfully propagating to a given region via the ionosphere and the probability of detecting a target in sea clutter, given that propagation occurred. A particular radar system was examined and tables of probabilities were generated for various ionospheric and target parameters. An example illustrates the method of combining these probabilities to obtain a composite probability of (Continued)		

20. Abstract (Continued)

detection. The probability of propagating was calculated by a computer program that used radar parameters, the ionospheric parameters, the geographical location, and the time of day and year as inputs. The probability of detection involved a computer implementation of the radar range equation.

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PROBABILITY OF DETECTING SHIPS WITH AN OTH RADAR SYSTEM [Unclassified Title]

INTRODUCTION

(U) This report is based on one phase of a study being conducted at the Naval Research Laboratory (NRL) [1-6] to compare the cost and effectiveness of three different radar systems used for ocean surveillance. The three candidate systems are an airborne radar, a satellite-borne radar, and a ground-based over-the-horizon (OTH) radar. For this report, the probability of detection of one particular OTH system has been calculated. The methods used, however, can be applied to any OTH system.

PROBABILITY OF PROPAGATION

(S) The ability of a radar system to propagate to a given range at a given time of the year was found by using RADARC, which is a computer program written by the Institute of Telecommunication Sciences to meet OTH radar analysis requirements as specified by NRL [7]. This program calculates the median clutter-to-noise ratio (C/N) for an OTH radar. The size of the backscatter area is calculated from virtual height ionograms using geometrical optics techniques. The noise considered includes atmospheric, galactic, and man-made sources. Atmospheric and ionospheric losses are included and the C/N is calculated from the radar range equation. This calculation was performed for sporadic E , E , F_1 , and F_2 layer propagation modes. If the clutter return and signal return are assumed to be affected by the ionosphere in a similar manner, propagation is defined by requiring the signal return from 1000-m² target to be large enough against noise to yield a probability of detection P_D equal to 0.9 and a probability of false alarm P_{fa} equal to 10^{-6} for a Type 1 OTH FM-CW radar system [6]. This system has the following parameters:

- 100-kw average power
- 0.1-s frequency sweep (prf = 10 per second)
- 20- μ s compressed pulse length
- 2.5-km horizontal aperture, receive ($\approx 0.25^\circ - 1^\circ$), transmit ($\approx 6^\circ - 10^\circ$).

We now calculate the C/N required for propagation.

(S) First, in order to obtain a $P_{fa} = 10^{-6}$ and a $P_D = 0.9$, the integrated signal-to-noise ratio (S/N) should be 13 dB. The FM-CW radar system is assumed to have 10 frequency sweeps per second, a coherent integration time of 25 s, and a total integration time of 250 s. From Rubin and DiFranco [8], the noncoherent integration gain for 10 noncoherent pulses is found to be 7 dB. With coherent integration, the noise spectrum extends from -5 to +5 Hz and is separated into 250 doppler bins of width 0.04 Hz. Thus,

Note: Manuscript submitted May 14, 1974.

the required S/N per doppler bin is 6 dB, (13 dB - 7 dB), and the S/N in a cycle bandwidth is -8 dB, or [6 dB + 10 log (0.04)]. Since the signal and clutter are assumed to propagate in a similar manner, the signal-to-clutter ratio (S/C) is given by

$$\frac{S}{C} = \frac{\sigma_T}{\frac{\sigma_0 \theta_B R c \tau}{2}} = -33 \text{ dB} \quad (1)$$

where

- σ_T = target cross section (30 dBsm),
- σ_0 = relative sea clutter cross section (-17 dB)
- θ_B = antenna beamwidth (1°)
- R = radar range, 1000 n.mi.
- c = speed of light
- τ = effective pulse width, 20 μ s.

Now, the required C/N for propagation is calculated from

$$\frac{C}{N} = \frac{\frac{S}{N}}{\frac{S}{C}} = 25 \text{ dB.}^* \quad (2)$$

Even though the main antenna pattern is wired into RADARC, the received clutter and noise powers are independent of the receive antenna beamwidth,† and consequently, RADARC can be used to calculate propagation for the FM-CW radar system. The only alterations made to the program were to eliminate printed output and to add the punched output used in calculating the propagation statistics.

(S) The ability to propagate was found for four months, (January, April, July, or October), two times (day or night), and three sunspot numbers (20, 45, or 75, which are the 25th, 50th, and 75th percentiles). The radar is situated in Maine (latitude 45° N, longitude 67° W). For each of the 24 conditions, the radar model RADARC was used to calculate the C/N every 2 hr for three azimuth angles (14° , 59° , and 104°), spanning a 90° sector. For each set of parameters, one-bounce propagation via four layers (sporadic E, E, F_1 , F_2) was considered and the maximum C/N chosen. The number of occasions out of 18 (6 times, 2 hr apart, and 3 azimuths) that the C/N exceeded 25 dB is given in Tables 1-24. We can interpret these numbers divided by 18 as a probability of propagation. If

*Specifically, a C/N of 25 dB is equivalent to our defined propagation at 1000 n.mi. for a 30-dB target and the particular frequency that yields a 1° beamwidth. For other ranges, targets, and frequencies, 25 dB was still used since C/N varies rapidly with range and hence a change in the threshold (25 dB) would have little effect on the region of propagation.

†When the transmit beamwidth is larger than the receive beamwidth, the receive array is sampling an extended source. When the beamwidth narrows, the clutter (or atmospheric noise) patch narrows, but the gain of the array increases.

(U) Table 1
 Number of successful propagations out of 18 possible opportunities, in January, in nighttime with SNS=20 as a function of range and frequency

RANGE (NM)	MONTH = JAN		NIGHT			SUN SPOT = 20			
	FREQUENCY (MHZ)								
	6	9	12	15	18	21	24	27	
500	16	13	9	0	0	0	0	0	
1000	18	16	13	10	7	3	0	0	
1500	17	2	0	0	0	0	0	0	
2000	15	5	0	0	0	0	0	0	

(U) Table 2
 Number of successful propagations out of 18 possible opportunities, in January, in daytime with SSN=20 as a function of range and frequency

RANGE (NM)	MONTH = JAN		DAY			SUN SPOT = 20			
	FREQUENCY (MHZ)								
	6	9	12	15	18	21	24	27	
500	18	18	9	0	0	0	0	0	
1000	16	18	18	14	4	0	0	0	
1500	3	9	13	12	8	3	0	0	
2000	2	4	4	5	5	5	0	0	

(U) Table 3
 Number of successful propagations out of 18 possible opportunities, in April, in nighttime with SSN=20 as a function of range and frequency

RANGE (NM)	MONTH = APR NIGHT SUN SPOT = 20							
	FREQUENCY (MHZ)							
	6	9	12	15	18	21	24	27
500	18	12	6	0	0	0	0	0
1000	18	16	12	8	3	0	0	0
1500	15	8	4	0	0	0	0	0
2000	12	10	5	1	0	0	0	0

(U) Table 4
 Number of successful propagations out of 18 possible opportunities, in April, in daytime with SSN=20 as a function of range and frequency

RANGE (NM)	MONTH = APR DAY SUN SPOT = 20							
	FREQUENCY (MHZ)							
	6	9	12	15	18	21	24	27
500	18	18	4	0	0	0	0	0
1000	8	16	15	11	2	0	0	0
1500	0	4	9	10	1	0	0	0
2000	0	2	5	7	5	0	0	0

(U) Table 5
 Number of successful propagations out of 18 possible opportunities, in July, in nighttime with SSN=20 as a function of range and frequency

RANGE (NM)	MONTH ■ JUL	NIGHT			SUN SPOT ■ 20			
	FREQUENCY (MHZ)							
	6	9	12	15	18	21	24	27
500	18	18	15	4	3	0	0	0
1000	18	18	18	17	15	8	5	2
1500	13	11	6	1	0	0	0	0
2000	7	11	6	3	0	0	0	0

(U) Table 6
 Number of successful propagations out of 18 possible opportunities, in July, in daytime with SSN=20 as a function of range and frequency

RANGE (NM)	MONTH ■ JUL	DAY			SUN SPOT ■ 20			
	FREQUENCY (MHZ)							
	6	9	12	15	18	21	24	27
500	17	16	16	2	1	0	0	0
1000	5	13	17	10	13	13	6	1
1500	0	3	9	8	0	0	0	0
2000	0	1	2	3	3	0	0	0

(U) Table 7
 Number of successful propagations out of 18 possible opportunities, in October, in nighttime with SSN=20 as a function of range and frequency

RANGE (NM)	MONTH = OCT		NIGHT		SUN SPOT = 20			
	FREQUENCY (MHZ)							
	6	9	12	15	18	21	24	27
500	18	15	9	2	0	0	0	0
1000	18	18	15	12	8	4	2	0
1500	16	7	1	0	0	0	0	0
2000	14	10	1	0	0	0	0	0

(U) Table 8
 Number of successful propagations out of 18 possible opportunities, in October, in daytime with SSN=20 as a function of range and frequency

RANGE (NM)	MONTH = OCT		DAY		SUN SPOT = 20			
	FREQUENCY (MHZ)							
	6	9	12	15	18	21	24	27
500	18	18	9	0	0	0	0	0
1000	11	18	18	17	6	2	0	0
1500	3	7	14	15	8	2	0	0
2000	0	4	6	9	13	7	0	0

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(U) Table 9
Number of successful propagations out of 18 possible opportunities, in January, in nighttime with SSN=45 as a function of range and frequency

RANGE (NM)	MONTH = JAN		NIGHT			SUN SPOT = 45		
	FREQUENCY (MHZ)							
	6	9	12	15	18	21	24	27
500	16	13	8	0	0	0	0	0
1000	18	16	13	9	5	3	0	0
1500	17	5	0	0	0	0	0	0
2000	15	11	0	0	0	0	0	0

(U) Table 10
Number of successful propagations out of 18 possible opportunities, in January, in daytime with SSN=45 as a function of range and frequency

RANGE (NM)	MONTH = JAN		DAY			SUN SPOT = 45		
	FREQUENCY (MHZ)							
	6	9	12	15	18	21	24	27
500	18	18	13	0	0	0	0	0
1000	15	18	18	16	7	0	0	0
1500	3	8	15	14	11	7	2	0
2000	1	6	9	5	8	7	5	0

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(U) Table 11
 Number of successful propagations out of 18 possible opportunities, in April, in nighttime with SSN=45 as a function of range and frequency

RANGE (NM)	MONTH = APR		NIGHT		SUN SPOT = 45		FREQUENCY (MHZ)		
	6	9	12	15	18	21	24	27	
	500	18	13	5	6	0	0	0	0
1000	18	17	14	8	3	0	0	0	
1500	14	14	5	2	0	0	0	0	
2000	12	13	8	4	0	0	0	0	

(U) Table 12
 Number of successful propagations out of 18 possible opportunities, in April, in daytime with SSN=45 as a function of range and frequency

RANGE (NM)	MONTH = APR		DAY		SUN SPOT = 45		FREQUENCY (MHZ)		
	6	9	12	15	18	21	24	27	
	500	17	18	3	0	0	0	0	0
1000	5	13	18	9	2	0	0	0	
1500	0	3	8	12	7	0	0	0	
2000	0	2	5	6	8	4	0	0	

(U) Table 13
 Number of successful propagations out of 18 possible
 opportunities, in July, in nighttime with SSN=45
 as a function of range and frequency

RANGE (NM)	MONTH = JUL		NIGHT		SUN SPOT = 45		FREQUENCY (MHZ)		
	6	9	12	15	18	21	24	27	
	500	18	18	15	3	2	0	0	0
1000	18	18	18	16	14	8	5	2	
1500	12	15	7	3	0	0	0	0	
2000	6	14	6	6	1	0	0	0	

(U) Table 14
 Number of successful propagations out of 18 possible
 opportunities, in July, in daytime with SSN=45
 as a function of range and frequency

RANGE (NM)	MONTH = JUL		DAY		SUN SPOT = 45		FREQUENCY (MHZ)		
	6	9	12	15	18	21	24	27	
	500	16	18	15	2	1	0	0	0
1000	5	11	17	8	13	13	6	1	
1500	0	2	6	13	1	0	0	0	
2000	0	0	2	2	8	0	0	0	

(U) Table 15
 Number of successful propagations out of 18 possible opportunities, in October, in nighttime with SSN=45 as a function of range and frequency

RANGE (NM)	MONTH = OCT		NIGHT		SUN SPOT = 45			
	FREQUENCY (MHZ)							
	6	9	12	15	18	21	24	27
500	18	15	9	0	0	0	0	0
1000	18	18	15	12	8	4	1	0
1500	15	12	3	0	0	0	0	0
2000	14	14	5	1	0	0	0	0

(U) Table 16
 Number of successful propagations out of 18 possible opportunities, in October, in daytime with SSN=45 as a function of range and frequency

RANGE (NM)	MONTH = OCT		DAY		SUN SPOT = 45			
	FREQUENCY (MHZ)							
	6	9	12	15	18	21	24	27
500	18	18	16	0	0	0	0	0
1000	10	18	18	17	13	1	0	0
1500	3	6	12	18	14	8	2	0
2000	0	2	5	9	13	13	8	1

(U) Table 17
 Number of successful propagations out of 18 possible opportunities, in January, in nighttime with SSN=75 as a function of range and frequency

RANGE (NM)	MONTH = JAN		NIGHT		SUN SPOT = 75		FREQUENCY (MHZ)		
	6	9	12	15	18	21	24	27	
	500	16	13	8	0	0	0	0	0
1000	10	15	13	9	4	1	0	0	
1500	10	10	1	0	0	0	0	0	
2000	15	14	2	0	0	0	0	0	

(U) Table 18
 Number of successful propagations out of 18 possible opportunities, in January, in daytime with SSN=75 as a function of range and frequency

RANGE (NM)	MONTH = JAN		DAY		SUN SPOT = 75		FREQUENCY (MHZ)		
	6	9	12	15	18	21	24	27	
	500	10	10	12	2	0	0	0	0
1000	2	10	10	16	9	4	0	0	
1500	3	7	13	16	13	10	5	2	
2000	2	4	7	12	10	10	7	5	

(U) Table 19
 Number of successful propagations out of 18 possible opportunities, in April, in nighttime with SSN=75 as a function of range and frequency

RANGE (NM)	MONTH = APR		NIGHT		SUN SPOY = 75		FREQUENCY (MHZ)	
	6	9	12	15	18	21	24	27
500	18	14	5	0	0	0	0	0
1000	18	18	14	8	3	0	0	0
1500	15	18	11	4	0	0	0	0
2000	11	15	14	6	2	0	0	0

(U) Table 20
 Number of successful propagations out of 18 possible opportunities, in April, in daytime with SSN=75 as a function of range and frequency

RANGE (NM)	MONTH = APR		DAY		SUN SPOY = 75		FREQUENCY (MHZ)	
	6	9	12	15	18	21	24	27
500	16	18	7	0	0	0	0	0
1000	5	14	18	14	4	0	0	0
1500	0	3	7	12	11	5	0	0
2000	0	2	4	7	11	10	3	0

(U) Table 21
 Number of successful propagations out of 18 possible opportunities, in July, in nighttime with SSN=75 as a function of range and frequency

RANGE (NM)	MONTH = JUL		NIGHT	SUN SPOT = 75				
	6	9		FREQUENCY (MHZ)				
	6	9	12	15	18	21	24	27
500	18	18	14	3	1	0	0	0
1000	18	18	18	15	14	7	5	1
1500	12	15	10	6	1	0	0	0
2000	6	14	13	7	4	0	0	0

(U) Table 22
 Number of successful propagations out of 18 possible opportunities, in July, in daytime with SSN=75 as a function of range and frequency

RANGE (NM)	MONTH = JUL		DAY	SUN SPOT = 75				
	6	9		FREQUENCY (MHZ)				
	6	9	12	15	18	21	24	27
500	14	18	17	1	1	0	0	0
1000	2	10	18	9	17	16	5	1
1500	0	2	5	13	4	0	0	0
2000	0	0	2	3	7	1	0	0

(U) Table 23
 Number of successful propagations out of 18 possible opportunities, in October, in nighttime with SSN=75 as a function of range and frequency

RANGE (NM)	MONTH ■ OCT		NIGHT		SUN SPOT ■		75	
	FREQUENCY (MHZ)							
	6	9	12	15	18	21	24	27
500	18	15	9	0	0	0	0	0
1000	18	18	15	12	7	3	0	0
1500	15	15	7	1	0	0	0	0
2000	13	17	12	3	0	0	0	0

(U) Table 24
 Number of successful propagations out of 18 possible opportunities, in October, in daytime with SSN=75 as a function of range and frequency

RANGE (NM)	MONTH ■ OCT		DAY		SUN SPOT ■		75	
	FREQUENCY (MHZ)							
	6	9	12	15	18	21	24	27
500	18	18	17	4	0	0	0	0
1000	9	18	18	18	16	7	0	0
1500	2	5	11	18	15	14	8	3
2000	0	3	6	9	16	13	13	8

the tables are compared, the following general conclusions can be reached about propagation when using the optimal frequency for a given range:

- Better at night than during the day
- Better in winter than in summer
- For the sunspot numbers considered, better for the higher sunspot numbers
- Propagation is very close to 100% for the shorter ranges.

The following conclusions can be reached about frequency preferences:

- Higher frequencies during daytime
- Higher frequencies during summertime
- Higher frequencies for higher sunspot numbers
- Higher frequencies for longer ranges.

PROBABILITY OF DETECTION

(U) In the previous section successful propagation was defined in terms of detection of targets against noise. Consequently, in this section we will consider only the detection of targets in sea clutter.

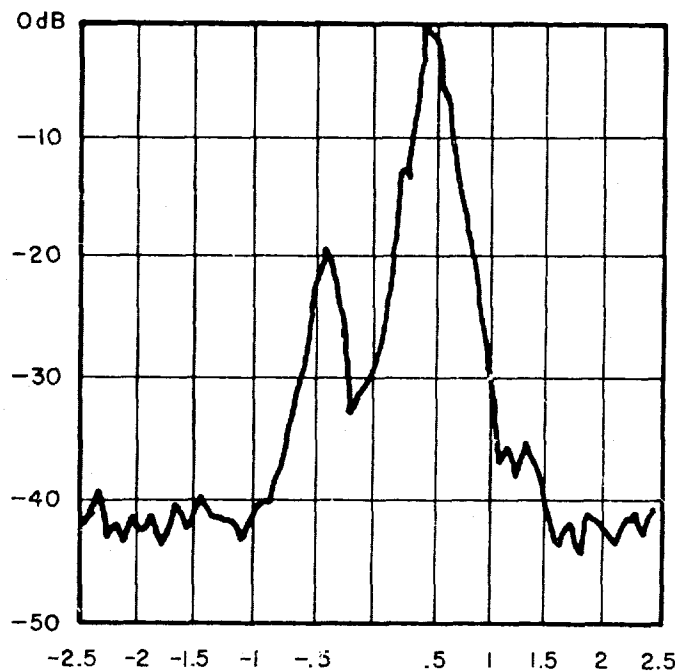
(C) The basic assumption is that the target return (small region) and the clutter return (extended region) will be affected in the same way by passage through the ionosphere. This allows us to calculate the S/C at the input to the processor from the target and clutter radar cross sections. The principal signal enhancement is from doppler processing with an additional noncoherent integration of the doppler cells.

(S) The S/C was calculated from Eq. (1) with three different target cross sections, 1000-m² and 3000-m² destroyers and a 50,000-m² aircraft carrier; and four ranges, 500, 1000, 1500, and 2000 n.mi, for each target type. The doppler processing gain was calculated for a set of radial velocities from -30 to +30 knots and a range of operating frequencies from 5 to 30 MHz. We assumed the target to be in one doppler cell and a 2-dB loss for processing and target doppler spread. The clutter level in a given doppler cell was obtained by normalizing a sample clutter spectrum. Two sample clutter spectra were derived from a working paper by Dr. James R. Barnum of Stanford Research Institute [9]. One asymmetrical spectrum represents the type of clutter spectrum observed with approaching (or receding) winds. The other spectrum is symmetric and is typical of the spectra observed in crosswind conditions.

(U) One observed clutter spectrum was used to generate both spectra. This particular spectrum was chosen on the basis of its clean appearance, but all of the candidate spectra from Ref. 9 have certain features in common, such as the Bragg scatter peaks, the lowered level of clutter between these peaks, and the even lower level of clutter in the doppler cells outside of the peak. The symmetrical (crosswind) clutter spectrum was obtained by averaging the clutter cells symmetrically placed about the carrier frequency. This process yielded a spectrum that appears to be a valid approximation to observed

crosswind spectra. This approximation was used because there was always at least a small asymmetry in the levels of the approaching and receding Bragg scattering lines of the observed spectra (an asymmetry would favor either the approaching or receding targets).

(U) The asymmetrical clutter spectrum is shown in Fig. 1. This spectrum was extended to ± 5 Hz at a -42 dB level. The sea clutter, of course, does not have a plateau at some particular level below the Bragg line peak but has been measured on the Madre radar (with a 70-dB dynamic range) to drop off to at least 65 to 70 dB below the peak at ± 5 Hz. The -42 dB plateau seems to be a feature of the radar on which the spectrum was measured. This would make little difference in our results: If the target is not in a Bragg line peak, it is detected. The two large spikes correspond to the Bragg scatter of ocean waves. The relative amplitude of the two spikes is a function of the angle of the ocean wavefront to the radar wavefront and hence depends on local wind direction [10]. The doppler offset of these spikes from the carrier frequency depends on the carrier frequency. The particular spectrum shown as measured at 20 MHz. At other radar frequencies, the spectral line spacing expands and contracts with the square root of the carrier frequency [11].



(U) Fig. 1—Typical clutter doppler spectrum

(S) The doppler cell in which the target appears is calculated from the radial speed V_r and operating wavelength λ by

$$\text{Doppler cell} = \frac{2V_r}{\lambda(0.04)} \quad (3)$$

(S) The clutter energy in that cell is calculated from the normalized clutter spectrum (shifted by the operating frequency). The S/C obtained for this radial speed and operating frequency combination is interpolated into a table of values, giving the P_d for 10 pulses [8]. For purposes of display, an array of symbols indicating the probability level for each combination of speed and frequency is printed. The P_d results for the approaching wind clutter spectrum are given in Figs. 2-13 and the crosswind results are given in Figs. 14-25. In the figures, an integer N indicates that P_d is between $0.1(N)$ and $0.1(N + 1)$ and a blank indicates that P_d is less than 0.1. The following observations can be made.

- Smaller targets can be detected only at the higher radial velocities, whereas the largest target can be detected in all doppler cells except those occupied by the Bragg scatter lines.
- Better detection performance is observed in the nonsymmetrical spectrum. This can be attributed (a) to the concentration of clutter energy in the larger Bragg scatter peak where detection is impossible in any case, and (b) to the consequent reduction of clutter energy in the remaining doppler cells.
- Targets can be detected in more of the doppler cells at higher frequencies. This is because the target doppler is proportional to frequency, whereas the clutter spectrum expands as the square root of the frequency. Thus, as the frequency is raised targets obscured by the clutter peak move into doppler cells of lower clutter.

(U) This last point may be the result of using one clutter spectrum taken at one carrier frequency and expanded and contracted for other frequencies. The clutter spectrum is affected by both sea state and frequency, but we did not have available sufficient data to make quantitative adjustment to the assumed spectrum. The doppler level in the cells away from the Bragg lines increases with the carrier frequency, and our sample spectrum was measured at a relatively high frequency. This means that at low frequencies the clutter levels used in our calculation are too high, but again, it would not affect our results; if a target is not in a Bragg line peak, it is detected.

(U) The preceding detection curves (Figs. 2-25) were based on the assumption that $\sigma_0 = -17$ dB. However, since there is some controversy over the value of σ_0 (Barnum has data that indicate $\sigma_0 = -23$ dB [12]), additional detection curves are generated for $\sigma_0 = -23$ dB. These curves are displayed in Figs. 26-49. Obviously the only difference between the results and the previous results is an improvement of 6 dB.

RESULTS

(S) To obtain a composite P_d , we multiply the probability of propagation (from Tables 1-24) by the probability of detection given that propagation is successful (Figs. 2-49). Two examples, one for $\sigma_0 = -17$ dB the other for $\sigma_0 = -23$ dB, are shown in Figs. 50 and 51, respectively. The composite P_d for each of four ranges is plotted vs radial speed. The target has a 3000-m^2 radar cross section in April, in daytime under crosswind conditions, with a sunspot number of 45. The operating frequency for each range is the frequency that yields the best composite P_d over the largest speed range. Only closing speeds are shown because of the symmetrical clutter spectrum. From these curves it appears that it is very difficult to detect a 3000-m^2 target at radial speeds below 15 knots if $\sigma_0 = -17$ dB and

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5													
6													
7													
8													
9													
10													
11													
12													
13													
14													
15													
16													
17													
18													
19													
20													
21													
22													
23													
24													
25													
26													
27													
28													
29													
30													

(S) Fig. 2— P_d of 1000-m² target at 500-n.mi. range in approaching sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5													
6													
7													
8													
9													
10													
11													
12													
13													
14													
15													
16													
17													
18													
19													
20													
21													
22													
23													
24													
25													
26													
27													
28													
29													
30													

(S) Fig. 3 — P_d of 1000-m² target at 1000-n.mi. range in approaching sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	9999999751												
6	9999999972												3
7	99999999983												1567
8	999999999995												168998
9	9999999999961												7999999
10	9999999999972												489999999
11	99999999999983						1						599999999
12	99999999999994						1						699999999
13	99999999999995						2						299999999
14	999999999999951						2						279999999
15	999999999999991						131						899999999
16	999999999999997						42						499999999
17	999999999999972						531						199999999
18	999999999999992						541						599999999
19	999999999999998						641						199999999
20	999999999999999						652						699999999
21	9999999999999994						1452						279999999
22	9999999999999995						1463						399999999
23	9999999999999999						563						899999999
24	99999999999999991						574						899999999
25	99999999999999991						574						499999999
26	99999999999999996						674						499999999
27	99999999999999997						685						999999999
28	99999999999999997						785						199999999
29	99999999999999998						796						699999999
30	99999999999999992						1796						699999999

(S) Fig. 4 - P_d of 1000-m² target at 1500-n.mi. range in approaching sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	999986642												
6	99999999663												1
7	999999999751												234
8	999999999992												35675
9	9999999999993												4678867
10	99999999999994												157897689
11	999999999999951												2689987999
12	999999999999991												279999999
13	999999999999972												899999999
14	999999999999992						1						149999999
15	999999999999998						1						599999999
16	9999999999999994						1						199999999
17	9999999999999994						21						699999999
18	99999999999999991						21						299999999
19	99999999999999996						31						799999999
20	99999999999999996						32						389999999
21	99999999999999991						12						499999999
22	99999999999999992						131						199999999
23	99999999999999998						231						599999999
24	99999999999999998						241						599999999
25	99999999999999998						241						199999999
26	99999999999999999						352						299999999
27	99999999999999994						352						699999999
28	99999999999999994						452						799999999
29	99999999999999998						462						299999999
30	99999999999999998						463						399999999

(S) Fig. 5 - P_d of 1000-m² target at 2000-n.mi. range in approaching sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5													599
6													1179999
7													38999999
8													499999999
9													1599999999
10													17999999999
11													279999999999
12													8999999999999
13													49999999999999
14													599999999999999
15													1599999999999999
16													1999999999999999
17													2799999999999999
18													2999999999999999
19													8999999999999999
20													4899999999999999
21													4999999999999999
22													19999999999999999
23													19999999999999999
24													69999999999999999
25													69999999999999999
26													29999999999999999
27													29999999999999999
28													29999999999999999
29													89999999999999999
30													89999999999999999

(S) Fig. 6-- P_d of 3000-m² target at 500-n.mi. range in approaching sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5													37
6													5999
7													1699999
8													28999999
9													499999999
10													5999999999
11													169999999999
12													1799999999999
13													7999999999999
14													38999999999999
15													99999999999999
16													499999999999999
17													999999999999999
18													599999999999999
19													1699999999999999
20													1999999999999999
21													7999999999999999
22													28999999999999999
23													29999999999999999
24													89999999999999999
25													99999999999999999
26													49999999999999999
27													49999999999999999
28													59999999999999999
29													19999999999999999
30													19999999999999999

(S) Fig. 7-- P_d of 3000-m² target at 1000-n.mi. range in approaching sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	99999999961					13321							3
6	99999999982					25421						1599	
7	999999999994					147542						279999	
8	9999999999981					158754						4899999	
9	99999999999971					29865						59999999	
10	999999999999982					1379761						1899999999	
11	999999999999993					1489871						2799999999	
12	999999999999994					599982						2899999999	
13	999999999999995					299992						3999999999	
14	9999999999999901					399993						4999999999	
15	9999999999999994					499994						5999999999	
16	9999999999999971					58999						1999999999	
17	9999999999999992					59999						6999999999	
18	9999999999999998					199991						1799999999	
19	9999999999999999					199991						2999999999	
20	9999999999999994					299991						8999999999	
21	9999999999999994					299991						3999999999	
22	9999999999999998					399992						3999999999	
23	9999999999999999					389992						9999999999	
24	99999999999999901					99993						4999999999	
25	99999999999999901					99993						5999999999	
26	99999999999999907					99994						1599999999	
27	99999999999999907					199994						1999999999	
28	99999999999999907					199994						1999999999	
29	99999999999999908					199995						6999999999	
30	99999999999999902					199995						7999999999	

(S) Fig. 8-- P_d of 3000-m² target at 1500-n.mi range in approaching sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	9999999983					11							1
6	99999999951					21							279
7	999999999971					1421							48999
8	9999999999983					25421							1599999
9	99999999999994					6532							26999999
10	999999999999995					14653							399999999
11	999999999999991					25854							4999999999
12	9999999999999971					26965							5999999999
13	9999999999999992					7976							1699999999
14	9999999999999998					189861							1999999999
15	9999999999999994					199971							2799999999
16	9999999999999994					25998							8999999999
17	9999999999999999					26998							3899999999
18	9999999999999995					7999							4999999999
19	9999999999999996					7999							9999999999
20	99999999999999971					8999							5999999999
21	9999999999999991					8999							1999999999
22	9999999999999992					19999							1999999999
23	9999999999999998					15999							6999999999
24	9999999999999998					69991							1799999999
25	9999999999999999					69991							2999999999
26	99999999999999983					79991							2499999999
27	99999999999999994					79991							2999999999
28	99999999999999904					79991							8999999999
29	99999999999999905					89992							3999999999
30	99999999999999909					89992							4999999999

(S) Fig. 9-- P_d of 3000-m² target at 2000-n.mi. range in approaching sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5		951											159
6		99972					1						27999
7		999983					2						389999
8		99999951					131						159999999
9		999999961					252						169999999
10		999999972					363						279999999
11		999999983					474						389999999
12		999999994					585						499999999
13		999999999					686						999999999
14		99999999951					696						159999999
15		99999999991					797						199999999
16		99999999997					393						799999999
17		999999999992					494						299999999
18		999999999998					15951						899999999
19		9999999999993					15951						999999999
20		9999999999998					14961						499999999
21		99999999999991					696						199999999
22		99999999999995					797						599999999
23		99999999999995					797						599999999
24		999999999999991					898						199999999
25		999999999999992					898						299999999
26		999999999999997					898						799999999
27		999999999999997					999						799999999
28		999999999999997					999						799999999
29		9999999999999993					999						399999999
30		9999999999999993					999						399999999

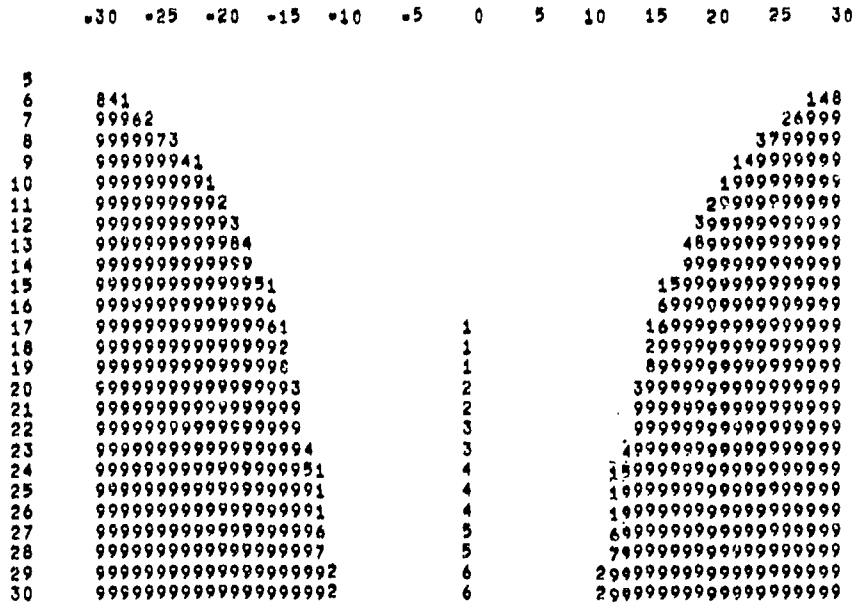
(S) Fig. 14— P_d of a 1000-m² target at 500-n.mi. range in crosswind sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5		2											2
6		9841											1489
7		999961											16999
8		9999973											379999
9		9999984											4899999
10		99999951											159999999
11		999999961					1						169999999
12		999999972					1						279999999
13		999999983					1						389999999
14		999999993					2						399999999
15		9999999994					131						499999999
16		99999999991					3						199999999
17		99999999995					4						599999999
18		999999999961					5						169999999
19		999999999992					5						299999999
20		999999999997					6						799999999
21		9999999999992					6						799999999
22		99999999999993					171						799999999
23		99999999999999					171						999999999
24		999999999999994					181						499999999
25		999999999999994					181						499999999
26		999999999999995					191						599999999
27		9999999999999991					292						199999999
28		9999999999999991					292						199999999
29		9999999999999996					292						699999999
30		9999999999999996					393						699999999

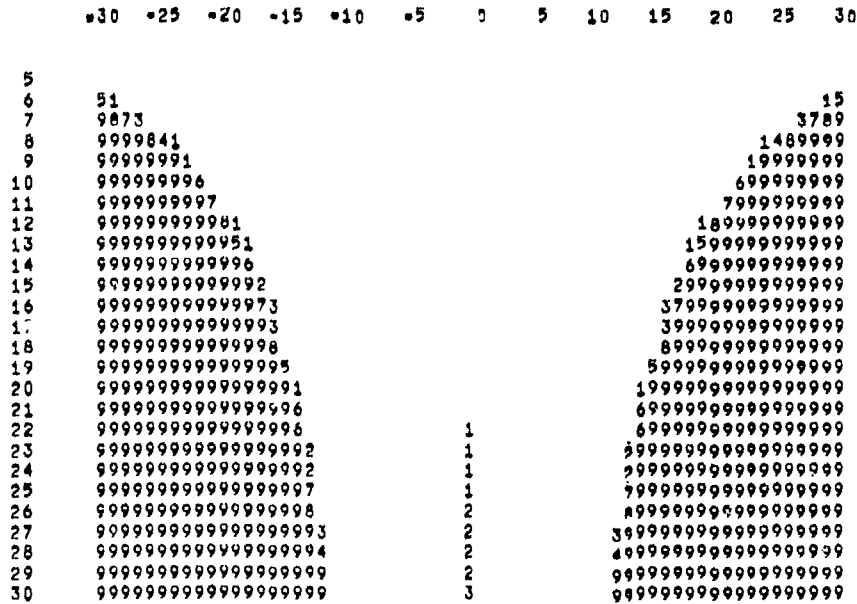
(S) Fig. 15— P_d of a 1000-m² target at 1000-n.mi. range in crosswind sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)



(S) Fig. 16 - P_d of a 1000-m² target at 1500-n.mi. range in crosswind sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)



(S) Fig. 17 - P_d of a 1000-m² target at 2000-n.mi. range in crosswind sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5			99961				37973						16999
6			9999883				159951						3889999
7			999999951				169961						159999999
8			99999999961				389983						16999999999
9			99999999972				499994						27999999999
10			99999999984				99999						48999999999
11			999999999991				169961						1999999999999
12			9999999999961				179971						1699999999999
13			9999999999996				189981						6999999999999
14			99999999999992				299992						2999999999999
15			99999999999998				399993						8999999999999
16			999999999999984				99999						489999999999999
17			9999999999999991				99999						199999999999999
18			9999999999999995				99999						599999999999999
19			9999999999999996				99999						699999999999999
20			9999999999999992				99999						299999999999999
21			9999999999999992				169961						299999999999999
22			9999999999999997				179971						799999999999999
23			9999999999999998				79997						899999999999999
24			9999999999999994				89998						499999999999999
25			9999999999999994				89998						499999999999999
26			9999999999999999				99999						999999999999999
27			9999999999999999				99999						999999999999999
28			9999999999999999				99999						999999999999999
29			9999999999999996				99999						699999999999999
30			9999999999999996				99999						699999999999999

(S) Fig. 18— P_d of a 3000-m² target at 500-n.mi. range in crosswind sea clutter, $\sigma_0 = -17$ dB

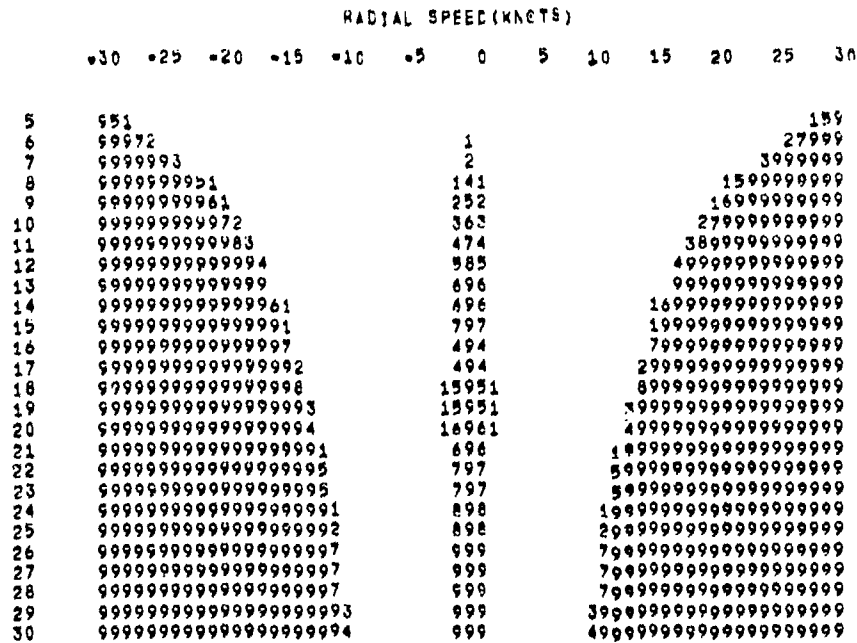
RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5			994				131						499
6			9999611				252						1169999
7			9999982				363						2899999
8			999999994				15851						499999999
9			99999999951				26962						15999999999
10			999999999961				37973						16999999999
11			999999999972				898						27999999999
12			999999999998				19991						89999999999
13			9999999999994				19991						4999999999999
14			99999999999994				19951						4999999999999
15			999999999999951				29952						159999999999999
16			999999999999991				38983						199999999999999
17			9999999999999962				38983						269999999999999
18			9999999999999992				49994						999999999999999
19			9999999999999998				49994						999999999999999
20			99999999999999983				59995						389999999999999
21			9999999999999994				999						499999999999999
22			9999999999999991				999						199999999999999
23			9999999999999991				19991						199999999999999
24			9999999999999995				19951						599999999999999
25			9999999999999996				19991						699999999999999
26			9999999999999992				19991						299999999999999
27			9999999999999992				29992						299999999999999
28			9999999999999992				29992						299999999999999
29			9999999999999997				29992						799999999999999
30			9999999999999998				39993						899999999999999

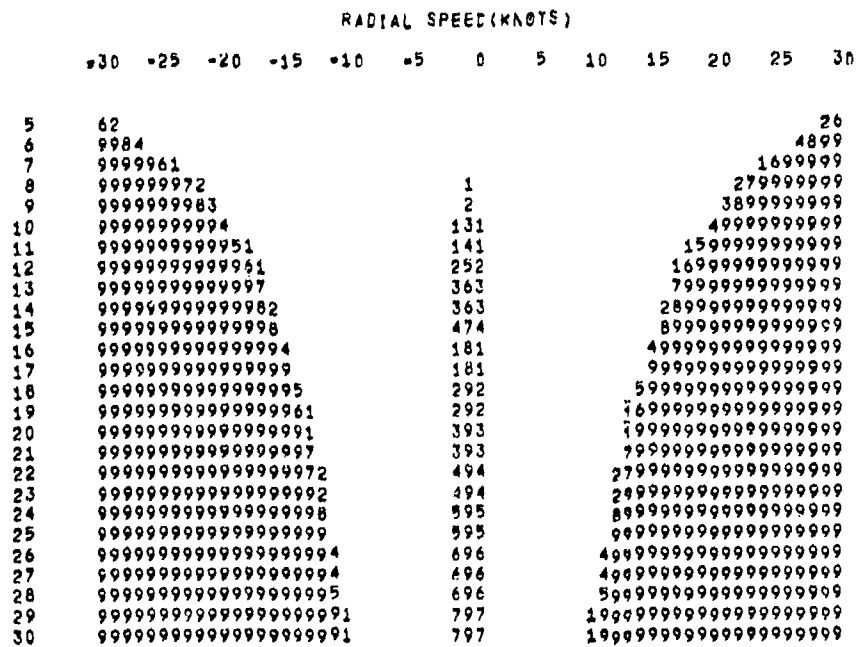
(S) Fig. 19— P_d of a 3000-m² target at 1000-n.mi. range in crosswind sea clutter, $\sigma_0 = -17$ dB

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(S) Fig. 20 -- P_d of a 3000-m² target at 1500-n.mi. range in crosswind sea clutter, $\sigma_0 = -17$ dB



(S) Fig. 21 -- P_d of a 3000-m² target at 2000-n.mi. range in crosswind sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	9999999993					1799999999971						3999999999	
6	9999999995					3999999999993						5999999999	
7	99999999971					5999999999995						1799999999999	
8	999999999981					1699999999961						1899999999999	
9	999999999992					2799999999972						2999999999999	
10	9999999999993					3999999999993						3999999999999	
11	9999999999999					4999999999994						9999999999999	
12	99999999999995					15999999999951						5999999999999	
13	999999999999991					6999999999996						1999999999999	
14	999999999999997					1999999999997						7999999999999	
15	9999999999999982					29999999999982						2899999999999	
16	9999999999999992					38999999999983						2999999999999	
17	9999999999999999					3999999999999						9999999999999	
18	99999999999999994					19999999999991						4999999999999	
19	99999999999999994					19999999999991						4999999999999	
20	99999999999999995					159999999999951						5999999999999	
21	999999999999999951					6999999999996						1999999999999	
22	999999999999999951					6999999999996						1999999999999	
23	999999999999999956					7999999999997						6999999999999	
24	999999999999999957					7999999999997						7999999999999	
25	999999999999999957					3999999999993						7999999999999	
26	999999999999999992					3999999999993						7999999999999	
27	999999999999999992					4999999999994						2999999999999	
28	999999999999999993					4999999999994						3999999999999	
29	999999999999999993					5999999999995						3999999999999	
30	999999999999999995					1999999999991						6999999999999	

(S) Fig. 22— P_d of a 50,000-m² target at 500-n.mi. range in crosswind sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	9999999993					1799999999971						3999999999	
6	9999999995					2899999999982						5999999999	
7	99999999996					3999999999993						6999999999	
8	9999999999981					99999999999						1899999999999	
9	9999999999992					1699999999961						2999999999999	
10	99999999999993					1799999999971						3999999999999	
11	999999999999994					899999999998						4999999999999	
12	999999999999995					3999999999993						9999999999999	
13	999999999999996					4999999999994						6999999999999	
14	9999999999999971					5999999999995						1799999999999	
15	9999999999999991					6999999999996						1999999999999	
16	9999999999999998					1999999999991						8999999999999	
17	99999999999999992					2999999999992						2999999999999	
18	99999999999999992					2799999999972						2999999999999	
19	99999999999999999					3899999999983						9999999999999	
20	999999999999999999					99999999999						9999999999999	
21	999999999999999994					99999999999						4999999999999	
22	999999999999999995					99999999999						5999999999999	
23	999999999999999995					99999999999						9999999999999	
24	999999999999999995					1599999999951						9999999999999	
25	9999999999999999951					6999999999996						1999999999999	
26	999999999999999996					6999999999996						6999999999999	
27	999999999999999997					6999999999996						7999999999999	
28	999999999999999997					7999999999997						7999999999999	
29	999999999999999999					7999999999997						9999999999999	
30	9999999999999999992					7999999999997						2999999999999	

(S) Fig. 23— P_d of a 50,000-m² target at 1000-n.mi. range in crosswind sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	.30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	999999995						29999999992						599999999
6	99999999971						49999999994						17999999999
7	999999999982						69999999996						28999999999
8	999999999994						79999999997						49999999999
9	999999999995						29999999992						59999999999
10	999999999996						39999999993						69999999999
11	9999999999971						49999999994						79999999999
12	9999999999991						999999999						79999999999
13	9999999999992						16999999961						29999999999
14	9999999999992						16999999961						29999999999
15	9999999999999						17999999971						99999999999
16	99999999999994						899999998						49999999999
17	99999999999995						899999998						59999999999
18	99999999999999						399999993						99999999999
19	99999999999999						499999994						69999999999
20	999999999999996						499999994						69999999999
21	999999999999991						599999995						19999999999
22	999999999999991						599999995						19999999999
23	999999999999992						699999996						89999999999
24	999999999999992						199999991						89999999999
25	999999999999999						199999991						99999999999
26	9999999999999952						299999992						29999999999
27	999999999999992						299999992						29999999999
28	999999999999993						299999992						39999999999
29	999999999999999						399999993						99999999999
30	999999999999999						399999993						99999999999

(S) Fig. 24— P_d of a 50,000-m² target at 1500-n.mi. range in crosswind sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

	.30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	999999972						4999999996						279999999
6	9999999994						28999999982						49999999999
7	99999999996						39999999993						69999999999
8	999999999991						49999999994						19999999999
9	9999999999992						699999996						29999999999
10	9999999999993						17999999971						39999999999
11	9999999999994						18999999981						49999999999
12	9999999999999						999999999						99999999999
13	99999999999996						399999993						49999999999
14	999999999999991						399999993						19999999999
15	999999999999997						499999994						79999999999
16	999999999999981						599999995						18999999999
17	999999999999992						699999996						29999999999
18	999999999999999						199999991						99999999999
19	999999999999993						199999991						39999999999
20	999999999999993						299999992						39999999999
21	999999999999999						299999992						99999999999
22	999999999999999						299999992						99999999999
23	999999999999995						399999993						59999999999
24	999999999999995						9999999						59999999999
25	999999999999996						9999999						69999999999
26	999999999999999						9999999						99999999999
27	999999999999999						9999999						99999999999
28	9999999999999991						199999991						19999999999
29	9999999999999997						199999991						79999999999
30	9999999999999998						199999991						89999999999

(S) Fig. 25— P_d of a 50,000-m² target at 2000-n.mi. range in crosswind sea clutter, $\sigma_0 = -17$ dB

RADIAL SPEED (KNOTS)

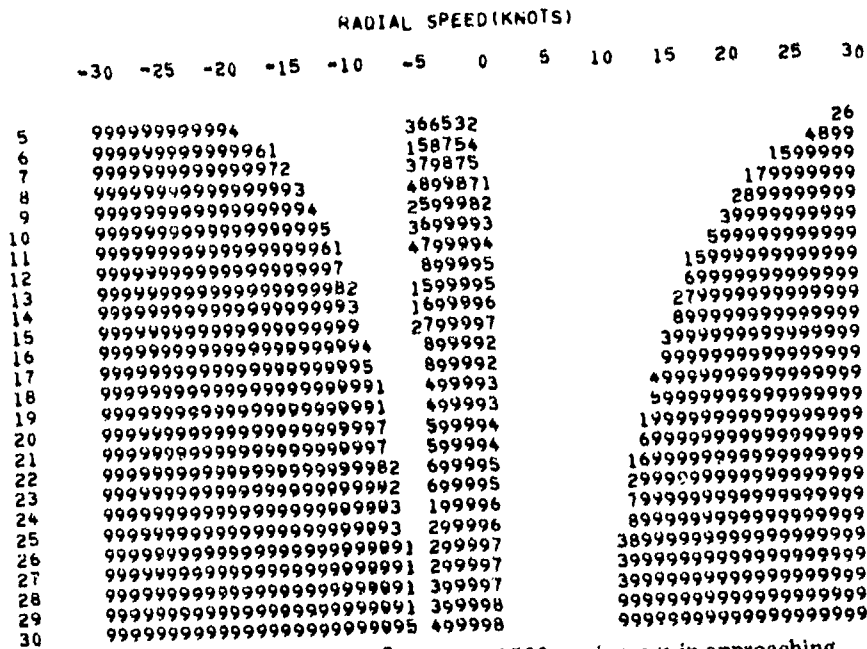
	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5													
6													
7													
8													
9													
10													
11													
12													
13													
14													
15													
16													
17													
18													
19													
20													
21													
22													
23													
24													
25													
26													
27													
28													
29													
30													

(S) Fig. 26— P_d of a 1000-m² target at 500-n.mi. range in approaching sea clutter, $\sigma_0 = -23$ dB

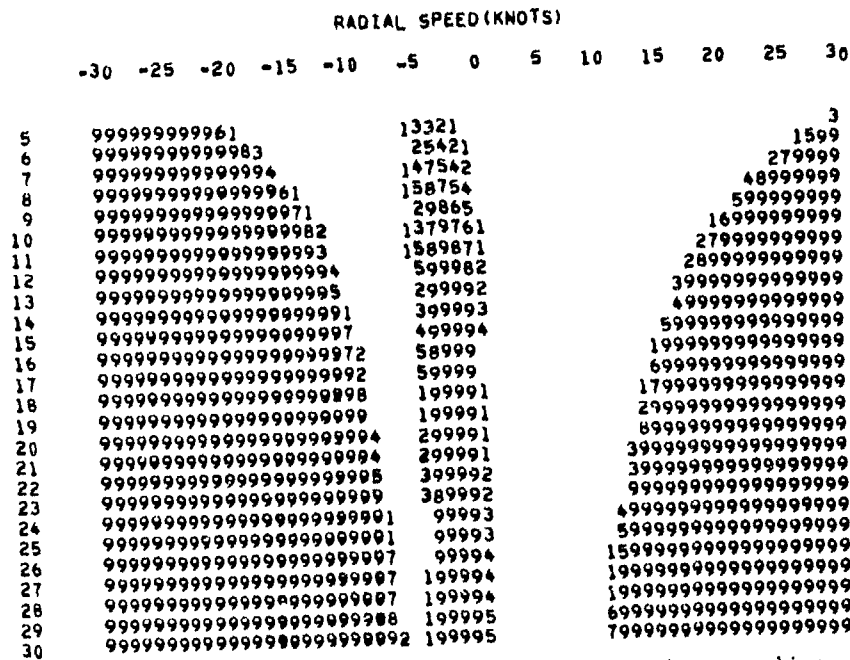
RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5													
6													
7													
8													
9													
10													
11													
12													
13													
14													
15													
16													
17													
18													
19													
20													
21													
22													
23													
24													
25													
26													
27													
28													
29													
30													

(S) Fig. 27— P_d of a 1000-m² target at 1000-n.mi. range in approaching sea clutter, $\sigma_0 = -23$ dB



(S) Fig. 28-- P_d of a 1000-m² target at 1500-n.mi. range in approaching sea clutter, $\sigma_0 = -23$ dB



(S) Fig. 29-- P_d of a 1000-m² target at 2000-n.mi. range in approaching sea clutter, $\sigma_0 = -23$ dB

RADIAL SPEED(KNOTS)

-30 -25 -20 -15 -10 -5 0 5 10 15 20 25 30

5	99999999999994	27999999971	2899
6	999999999999961	4999999993	4499999
7	999999999999972	1599999994	169999999
8	999999999999993	1799999996	27999999999
9	9999999999999941	28999999971	38999999999
10	9999999999999951	4899999998	4999999999999
11	9999999999999961	5999999993	599999999999999
12	99999999999999731169999994		199999999999999
13	99999999999999842169999995		279999999999999
14	99999999999999931299999995		899999999999999
15	9999999999999999062299999996		489999999999999
16	9999999999999999964399999997		149999999999999
17	99999999999999999905499999997		599999999999999
18	999999999999999999906499999998		169999999999999
19	9999999999999999999908499999999		299999999999999
20	99999999999999999999909569999999		799999999999999
21	9999999999999999999999097699999993		799999999999999
22	9999999999999999999999909799999993		399999999999999
23	999999999999999999999999098799999994		499999999999999
24	999999999999999999999999909799999994		999999999999999
25	99999999999999999999999999909799999995		199999999999999
26	999999999999999999999999999909799999995		599999999999999
27	9999999999999999999999999999909799999995		599999999999999
28	99999999999999999999999999999909799999996		699999999999999
29	999999999999999999999999999999909799999996		199999999999999
30	9999999999999999999999999999999909799999997		299999999999999

(S) Fig. 32— P_d of a 3000-m² target at 1500-n.mi. range in approaching sea clutter, $\sigma_0 = -23$ dB

RADIAL SPEED(KNOTS)

-30 -25 -20 -15 -10 -5 0 5 10 15 20 25 30

5	999999999999771	489999994	599
6	999999999999983	1699999961	1179999
7	999999999999994	2799999981	389999999
8	9999999999999961	499999993	499999999
9	9999999999999971	1599999994	16999999999
10	9999999999999982	1699999995	1799999999999
11	9999999999999993	299999991	2899999999999
12	99999999999999941	389999991	8999999999999
13	9999999999999999091	399999992	4999999999999
14	9999999999999999961	999999992	599999999999999
15	99999999999999999973	199999993	169999999999999
16	999999999999999999931169999994		299999999999999
17	99999999999999999999821699999995		279999999999999
18	999999999999999999999831799999995		399999999999999
19	9999999999999999999999051799999996		899999999999999
20	9999999999999999999999962399999996		489999999999999
21	9999999999999999999999964399999991		499999999999999
22	9999999999999999999999999499999991		199999999999999
23	9999999999999999999999999949999991		199999999999999
24	99999999999999999999999999659999991		699999999999999
25	99999999999999999999999999849999992		699999999999999
26	99999999999999999999999999859999992		299999999999999
27	99999999999999999999999999859999992		299999999999999
28	99999999999999999999999999859999993		399999999999999
29	99999999999999999999999999859999993		899999999999999
30	99999999999999999999999999859999994		899999999999999

(S) Fig. 33— P_d of a 3000-m² target at 2000-n.mi. range in approaching sea clutter, $\sigma_0 = -23$ dB

RADIAL SPEED(KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	99994						116999611						49999
6	999999961						3899983						167999999
7	9999999973						4999994						379999999
8	99999999994						6999996						49999999999
9	9999999999951						7999997						1599999999999
10	9999999999997						2999992						7999999999999
11	99999999999993						2999992						3999999999999
12	99999999999984						3999993						4899999999999
13	999999999999991						4999994						1999999999999
14	9999999999999951						5999995						1599999999999
15	9999999999999992						6999996						2999999999999
16	9999999999999997						1999991						7999999999999
17	99999999999999993						1999991						3999999999999
18	99999999999999998						1999991						8999999999999
19	99999999999999999						2999992						9999999999999
20	99999999999999995						2999992						5999999999999
21	99999999999999995						2999992						5999999999999
22	99999999999999999						3999993						9999999999999
23	999999999999999991						99999						1999999999999
24	999999999999999996						99999						6999999999999
25	999999999999999997						99999						7999999999999
26	9999999999999999991						99999						1999999999999
27	9999999999999999991						99999						1999999999999
28	9999999999999999992						99999						2999999999999
29	9999999999999999998						99999						8999999999999
30	9999999999999999999						99999						9999999999999

(S) Fig. 38— P_d of a 1000-m² target at 500-n.mi. range in crosswind sea clutter, $\sigma_0 = -23$ dB

RADIAL SPEED(KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	9972						363						2799
6	9999944						15851						4499999
7	999999951						26962						159999999
8	9999999972						38983						279999999
9	99999999983						1599951						38999999999
10	999999999994						69996						49999999999
11	9999999999995						29992						59999999999
12	99999999999991						39993						1999999999999
13	999999999999972						39993						2799999999999
14	999999999999997						49994						7999999999999
15	9999999999999983						59995						3899999999999
16	99999999999999941						69996						1499999999999
17	99999999999999995						69996						5999999999999
18	999999999999999951						79997						1599999999999
19	999999999999999991						79997						1999999999999
20	999999999999999997						89998						7999999999999
21	999999999999999997						29992						7999999999999
22	9999999999999999993						29992						3999999999999
23	99999999999999999943						39993						3999999999999
24	9999999999999999998						39993						8999999999999
25	99999999999999999991						49994						1999999999999
26	99999999999999999995						49994						5999999999999
27	99999999999999999995						59995						5999999999999
28	99999999999999999995						59995						5999999999999
29	999999999999999999991						59995						1999999999999
30	999999999999999999992						69996						2999999999999

(S) Fig. 39— P_d of a 1000-m² target at 1000-n.mi. range in crosswind sea clutter, $\sigma_0 = -23$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5							2						389
6							141						1159999
7							252						1799999
8							474						384999999
9							15851						499999999
10							26962						15999999999
11							797						16999999999
12							898						79999999999
13							999						29999999999
14							19991						38999999999
15							19991						49999999999
16							27972						19999999999
17							27972						15999999999
18							38983						19999999999
19							38983						69999999999
20							49994						27999999999
21							999						39999999999
22							999						89999999999
23							999						89999999999
24							999						49999999999
25							19991						59999999999
26							19991						19999999999
27							19991						19999999999
28							19991						19999999999
29							19991						69999999999
30							29992						79999999999

(S) Fig. 40— P_d of a 1000-m² target at 1500-n.mi. range in crosswind sea clutter, $\sigma_0 = -23$ dB

RADIAL SPEED (KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5							1						159
6							1						27999
7							2						4999999
8							141						159999999
9							252						169999999
10							363						279999999
11							474						389999999
12							585						499999999
13							696						999999999
14							696						169999999
15							797						199999999
16							494						799999999
17							494						299999999
18							15951						899999999
19							15951						399999999
20							16961						499999999
21							696						199999999
22							797						599999999
23							797						699999999
24							898						199999999
25							898						299999999
26							999						799999999
27							999						799999999
28							999						899999999
29							999						399999999
30							999						499999999

(S) Fig. 41— P_d of a 1000-m² target at 2000-n.mi. range in crosswind sea clutter, $\sigma_0 = -23$ dB

RADIAL SPEED(KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	99999962					699999996						269999999	
6	999999983					1899999981						38999999999	
7	9999999995					2999999992						59999999999	
8	999999999991					4999999994						1999999999999	
9	9999999999991					599999995						199999999999999	
10	9999999999992					699999996						299999999999999	
11	9999999999993					1799999971						399999999999999	
12	999999999999999					899999998						999999999999999	
13	999999999999995					299999992						599999999999999	
14	999999999999999					399999993						999999999999999	
15	999999999999997					499999994						799999999999999	
16	9999999999999971					499999994						179999999999999	
17	9999999999999991					599999995						199999999999999	
18	9999999999999999					199999991						999999999999999	
19	9999999999999992					199999991						299999999999999	
20	9999999999999993					199999991						399999999999999	
21	9999999999999999					299999992						999999999999999	
22	9999999999999999					299999992						999999999999999	
23	9999999999999994					289999982						499999999999999	
24	9999999999999995					9999999						599999999999999	
25	9999999999999995					9999999						599999999999999	
26	9999999999999999					9999999						999999999999999	
27	9999999999999999					9999999						999999999999999	
28	9999999999999999					9999999						999999999999999	
29	9999999999999997					9999999						799999999999999	
30	9999999999999997					19999991						799999999999999	

(S) Fig. 42-- P_d of a 3000-m² target at 500-n.mi. range in crosswind sea clutter, $\sigma_0 = -23$ dB

RADIAL SPEED(KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	9999833					559999955						3389999	
6	999999951					179999971						159999999	
7	999999972					289999982						27999999999	
8	99999999984					399999993						4899999999999	
9	999999999995					9999999						5999999999999	
10	9999999999992					6999996						2999999999999	
11	99999999999972					179999971						2799999999999	
12	99999999999983					189999981						3899999999999	
13	99999999999994					8999998						4999999999999	
14	999999999999995					9999999						5999999999999	
15	999999999999996					9999999						6999999999999	
16	9999999999999991					4999994						1999999999999	
17	9999999999999997					5999995						7999999999999	
18	9999999999999991					5999995						1999999999999	
19	9999999999999992					6999996						2999999999999	
20	9999999999999999					6999996						9999999999999	
21	9999999999999993					7999997						3999999999999	
22	9999999999999999					7999997						3999999999999	
23	9999999999999994					1999991						4999999999999	
24	9999999999999999					1999991						9999999999999	
25	9999999999999999					2999992						9999999999999	
26	9999999999999995					2999992						5999999999999	
27	9999999999999996					2999992						6999999999999	
28	9999999999999996					3999993						6999999999999	
29	9999999999999999					3999993						9999999999999	
30	9999999999999991					4999994						1999999999999	

(S) Fig. 43-- P_d of a 3000-m² target at 1000-n.mi. range in crosswind sea clutter, $\sigma_0 = -23$ dB

RADIAL SPEED(KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	99994						116999611					49999	
6	999999961						3899983					169999999	
7	9999999973						4999994					379999999	
8	99999999941						6999996					14999999999	
9	999999999951						7999997					1599999999999	
10	999999999997						2499992					7999999999999	
11	9999999999993						2999992					3999999999999	
12	99999999999984						3999993					489999999999999	
13	999999999999991						4999994					199999999999999	
14	9999999999999951						5999995					15999999999999999	
15	9999999999999992						6999996					29999999999999999	
16	9999999999999997						1999991					79999999999999999	
17	99999999999999993						1999991					34999999999999999	
18	99999999999999998						1999991					89999999999999999	
19	99999999999999999						2999992					99999999999999999	
20	999999999999999995						2999992					59999999999999999	
21	999999999999999995						2999992					59999999999999999	
22	999999999999999999						3999993					99999999999999999	
23	9999999999999999991						99999					19999999999999999	
24	9999999999999999997						99999					79999999999999999	
25	9999999999999999997						99999					79999999999999999	
26	9999999999999999991						99999					19999999999999999	
27	9999999999999999992						99999					29999999999999999	
28	9999999999999999992						99999					29999999999999999	
29	9999999999999999998						99999					89999999999999999	
30	9999999999999999999						99999					99999999999999999	

(S) Fig. 44-- P_d of a 3000-m² target at 1500-n.mi. range in crosswind sea clutter, $\sigma_0 = -23$ dB

RADIAL SPEED(KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	99961						37973					16999	
6	99999883						1599951					3889999	
7	9999999941						1699961					149999999	
8	99999999961						3899983					16999999999	
9	999999999972						4999994					27999999999	
10	9999999999983						99999					3899999999999	
11	99999999999991						69996					1999999999999	
12	999999999999951						1799971					159999999999999	
13	999999999999996						1899981					699999999999999	
14	9999999999999992						2899982					299999999999999	
15	9999999999999998						3999993					899999999999999	
16	99999999999999984						99999					489999999999999	
17	99999999999999991						99999					199999999999999	
18	99999999999999995						99999					599999999999999	
19	99999999999999996						99999					699999999999999	
20	99999999999999992						99999					299999999999999	
21	99999999999999992						69996					299999999999999	
22	99999999999999997						1799971					799999999999999	
23	99999999999999998						79997					899999999999999	
24	99999999999999993						89998					399999999999999	
25	99999999999999994						89998					499999999999999	
26	99999999999999999						89998					999999999999999	
27	99999999999999999						99999					999999999999999	
28	99999999999999999						99999					999999999999999	
29	999999999999999995						99999					599999999999999	
30	999999999999999996						99999					699999999999999	

(S) Fig. 45-- P_d of a 3000-m² target at 2000-n.mi. range in crosswind sea clutter, $\sigma_0 = -23$ dB

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RADIAL SPEED(KNOTS)

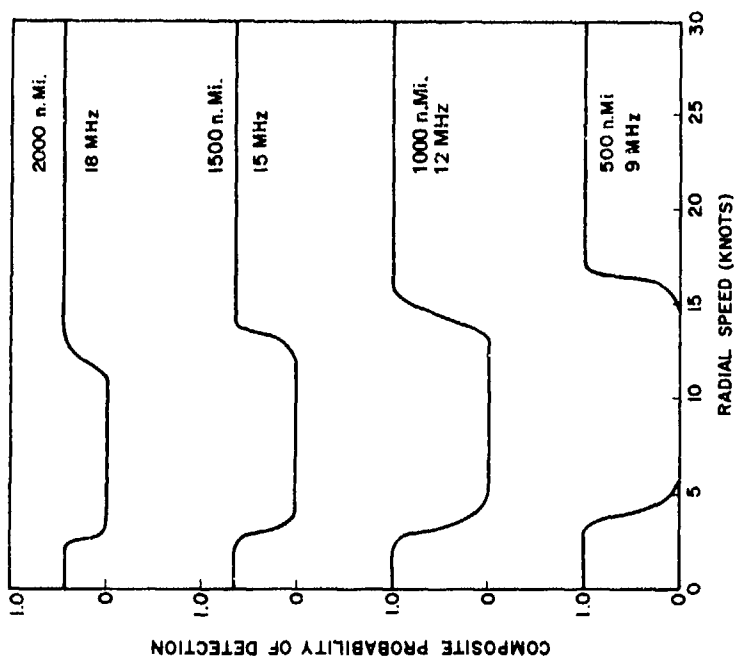
	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	9999999996												6999999999
6	999999999981												189999999999
7	999999999993												399999999999
8	9999999999994												49999999999999
9	99999999999996												69999999999999
10	999999999999971												1799999999999999
11	999999999999992												2799999999999999
12	9999999999999982												3899999999999999
13	9999999999999993												9999999999999999
14	9999999999999999												1499999999999999
15	99999999999999995												1599999999999999
16	999999999999999961												1699999999999999
17	999999999999999991												1999999999999999
18	999999999999999997												3999999999999999
19	9999999999999999977												3999999999999999
20	9999999999999999982												4899999999999999
21	9999999999999999993												1999999999999999
22	99999999999999999993												1999999999999999
23	99999999999999999999												2999999999999999
24	99999999999999999999												2999999999999999
25	99999999999999999999												6999999999999999
26	9999999999999999999985												7999999999999999
27	9999999999999999999996												7999999999999999
28	99999999999999999999961												7999999999999999
29	999999999999999999999618												1699999999999999
30	999999999999999999999614												1999999999999999

(S) Fig. 48— P_d of a 50,000-m² target at 1500-n.mi. range in crosswind sea clutter, $\sigma_0 = -23$ dB

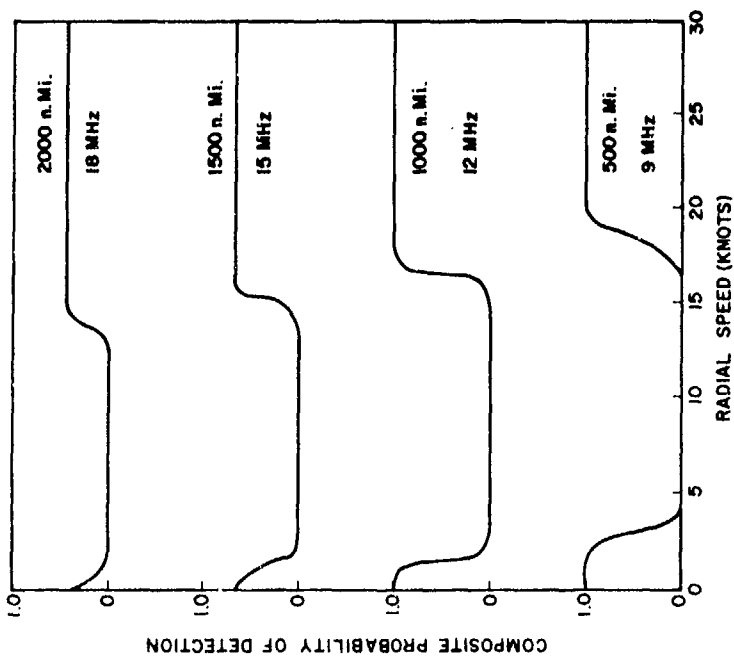
RADIAL SPEED(KNOTS)

	-30	-25	-20	-15	-10	-5	0	5	10	15	20	25	30
5	9999999993												3999999999
6	999999999995												599999999999
7	99999999999971												17999999999999
8	99999999999981												18999999999999
9	99999999999992												29999999999999
10	999999999999994												49999999999999
11	9999999999999999												99999999999999
12	99999999999999961												1599999999999999
13	99999999999999991												6999999999999999
14	99999999999999997												2999999999999999
15	999999999999999982												2999999999999999
16	999999999999999992												3899999999999999
17	999999999999999999												3999999999999999
18	9999999999999999994												1999999999999999
19	99999999999999999994												1999999999999999
20	99999999999999999995												1599999999999999
21	999999999999999999991												6999999999999999
22	9999999999999999999991												6999999999999999
23	999999999999999999996												7999999999999999
24	999999999999999999997												7999999999999999
25	999999999999999999997												3999999999999999
26	999999999999999999992												4999999999999999
27	9999999999999999999993												4999999999999999
28	9999999999999999999993												4999999999999999
29	9999999999999999999993												5999999999999999
30	9999999999999999999999												1999999999999999

(S) Fig. 49— P_d of a 50,000-m² target at 2000-n.mi. range in crosswind sea clutter, $\sigma_0 = -23$ dB



(S) Fig. 51—Composite P_d of a 3000-m^2 target in crosswind sea clutter, $\sigma_0 = -23$ dB



(S) Fig. 50—Composite P_d of a 3000-m^2 target in crosswind sea clutter, $\sigma_0 = -17$ dB

below 13 knots if $\sigma_0 = -23$ dB. The composite P_d 's are limited at long ranges by the probability of propagation. Thus, the composite P_d would be raised by any feature which improves propagation, such as allowing multiple-bounce propagation or increasing power.

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- 1 OF 1
- 1 - AD NUMBER: 531281
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