

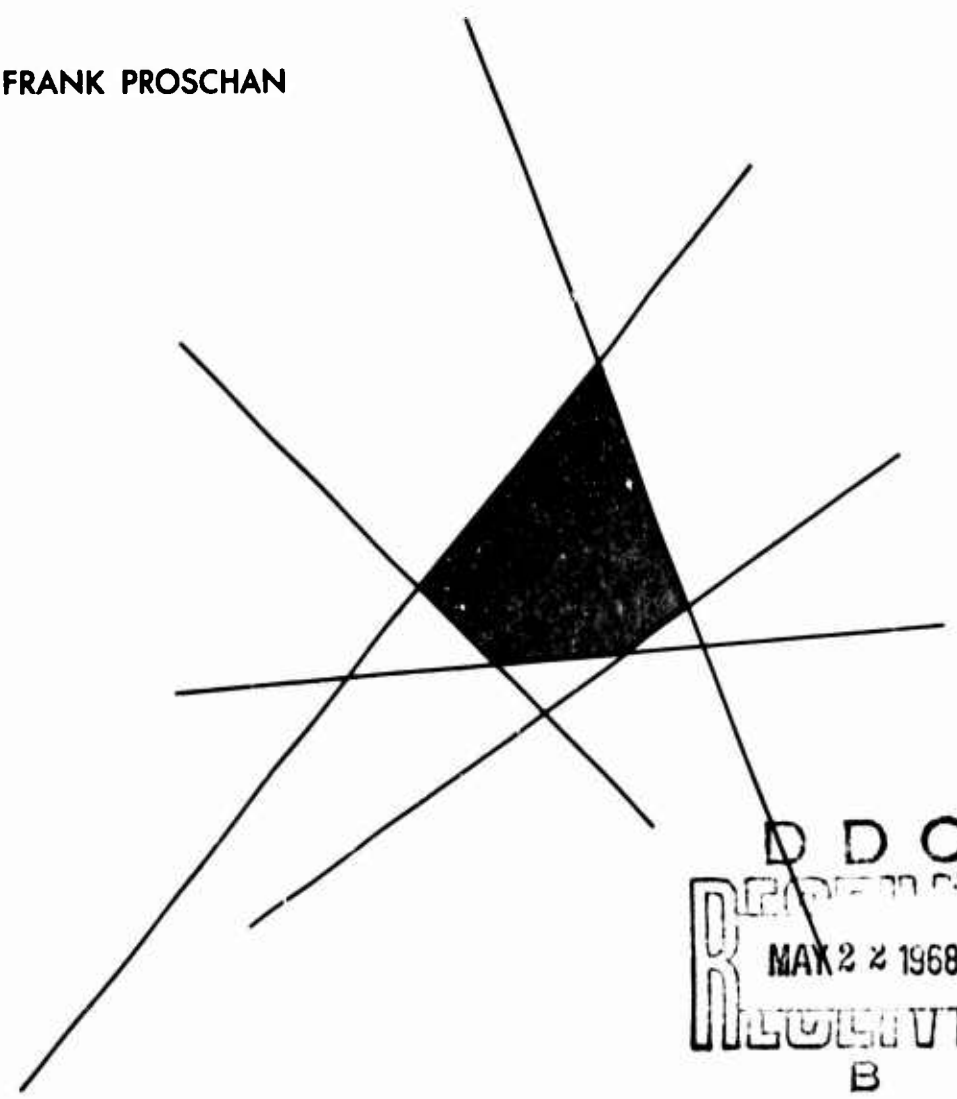
53012-32-107
ORC 68-7
APRIL 1968

A NOTE ON TESTS FOR MONOTONE FAILURE RATE BASED ON INCOMPLETE DATA

by

RICHARD E. BARLOW and FRANK PROSCHAN

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Berkeley, California

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[†] This research has been partially supported by the Office of Naval Research under Contract Nonr-3656(18), the National Science Foundation under Grant GK-1684, the National Science Foundation under Grant GP-7417, and the U.S. Army Research Office-Durham, Contract DA-31-124-ARO-D-331 with the University of California. Reproduction in whole or in part is permitted for any purpose of the United States Government.

ACKNOWLEDGEMENTS

We would like to acknowledge the help of T. A. Bray,
R. Pyke, and R. Wolff.

ABSTRACT

Tests for exponential versus IFRA distributions based on incomplete data are defined and shown to be unbiased. The tests are motivated by a class of tests considered in detail by Bickel and Doksum. Tests for exponential versus IFR distributions based on the ranks of total time on test statistics are also considered.

A NOTE ON TESTS FOR MONOTONE
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Richard E. Barlow[†] and Frank Proschan

1. INTRODUCTION AND SUMMARY

Let $0 \equiv X_{(0)} \leq X_{(1)} \leq X_{(2)} \leq \dots \leq X_{(n)}$ be the order statistics of a (complete) random sample from a population with distribution F and density f such that $F(0) = 0$. Bickel and Doksum (1968) consider the problem of testing

$$H_0 : F(t) = 1 - e^{-\lambda t} \quad t \geq 0, \lambda > 0$$

versus

$$H_1 : F \text{ IFR}$$

(i.e., $-\log[1 - F(t)]$ convex on $[0, \infty)$).

Let $D_i = (n-i+1)(X_{(i)} - X_{(i-1)})$, $i = 1, 2, \dots, n$. They consider tests based on statistics of the form

$$\frac{\sum_{i=1}^n a_i D_i}{\sum_{i=1}^n D_i}$$

where $a_1 \geq a_2 \geq \dots \geq a_n$. The test, ϕ_a , rejects H_0 when

$$\frac{\sum_{i=1}^n a_i D_i}{\sum_{i=1}^n D_i} \geq c_{a,a,n}. \quad \text{They compute the asymptotic relative efficiency of}$$

[†]Research partially supported by the Office of Naval Research, Contract Nonr-3656(18) with the University of California, and the Boeing Scientific Research Laboratories. This report is also appearing as a Boeing Scientific Research Laboratories Document.

various such tests relative to selected parametric alternatives. Such tests were shown to be unbiased against IFRA (for increasing failure rate average) alternatives by Barlow and Proschan (1966) and hence a fortiori for IFR alternatives. [See also Birnbaum, Esary and Marshall (1965) for justification of the IFRA assumption.]

The purpose of this note is to show that analogous tests designed to treat incomplete samples of failure data are also unbiased against IFRA alternatives. Let X_i be the time to failure of the i^{th} item in a sample of size n . Let L_i be a given truncation time for the i^{th} item and let

$$Z_i = \min(X_i, L_i) \quad i = 1, 2, \dots, n.$$

Let $0 \equiv Z_{(0)} \leq Z_{(1)} \leq \dots \leq Z_{(k)}$ be the first k observed failure times. Note that "withdrawals" may occur between $Z_{(i)}$ and $Z_{(i+1)}$ and that k is, in general, a random variable. Let $n(u)$ be the (random) number of items on test at time u .

We define a test, ϕ_a^* , (a modification of ϕ_a) which rejects H_0 in favor of

$$H_1' : F \text{ IFRA}$$

(i.e., $-\{\log[1 - F(t)]\}/t$ nondecreasing on $[0, \infty)$) when

$$W_a = \frac{\sum_{i=1}^k a_i \int_{Z_{(i-1)}}^{Z_{(i)}} n(u) du}{\int_0^{Z_{(k)}} n(u) du} \geq c_{\alpha, a, k}^*.$$

Note that $\int_{Z_{(i-1)}}^{Z_{(i)}} n(u) du$ represents the total time on test between the $(i-1)^{\text{st}}$ and

i^{th} observed failures. The distribution of W_a can be computed under H_0 using

the fact that $Y_i = \int_{Z_{(i-1)}}^{(Z_{(i)})} n(u)du$ ($i = 1, 2, \dots, k$) are distributed as

independent exponential random variables under H_0 conditioned on the value of k .

We show that ϕ_a^* is an unbiased test for IFRA alternatives for weights

$a = (a_1, a_2, \dots, a_n)$ for which $a_1 \geq a_2 \geq \dots \geq a_n$.

2. DISTRIBUTION OF W_a UNDER H_0

Let $r(t) = f(t)/[1 - F(t)]$ be the failure rate function for F . We will need the following lemma, stated without proof in Bray, Crawford, and Proschan (1967).

Lemma 1.

For any distribution F ($F(0) = 0$) with failure rate $r(t)$,

$$Y_i = \int_{Z_{(i-1)}}^{Z_{(i)}} r(u)n(u)du, \quad i = 1, 2, \dots, k \text{ are independently distributed with}$$

density e^{-y} .

Proof:

$$\text{Let } Y_1 = \int_0^{Z_{(1)}} r(u)n(u)du \text{ and } S_0(t) = \int_0^t r(u)n(u)du. \text{ Note that } S_0(t)$$

is well defined up to the time of the first observed failure since $n(u)$ depends only on the specified truncation times L_i ($i = 1, 2, \dots, n$) up until $Z_{(1)}$.

Then

$$\begin{aligned} P[Y_1 > y_1] &= P[S_0(Z_{(1)}) > y_1] = P[Z_{(1)} > S_0^{-1}(y_1)] = \\ &= \exp[-S_0(S_0^{-1}(y_1))] = e^{-y_1}. \end{aligned}$$

Thus Y_1 has density e^{-y_1} .

$$\text{Now let } Y_2 = \int_{Z_{(1)}}^{Z_{(2)}} r(u)n(u)du \text{ and } S_{x_1}(t) = \int_{x_1}^t r(u)n(u)du. \text{ Note that}$$

conditionally on $Z_{(1)} = x_1$, S_{x_1} is well defined for $x_1 \leq t < Z_{(2)}$. Hence

$$\begin{aligned}
 P[Y_2 > y_2 \mid Z_{(1)} = x_1] &= P[S_{x_1}(Z_{(2)}) > y_2 \mid Z_{(1)} = x_1] = \\
 &= P[Z_{(2)} > S_{x_1}^{-1}(y_2) \mid Z_{(1)} = x_1] = \exp\left[-S_{x_1}\left(S_{x_1}^{-1}(y_2)\right)\right] = e^{-y_2}.
 \end{aligned}$$

Thus Y_2 is independent of Y_1 and also exponentially distributed with mean 1. If we continue in this manner, conditioning on previous events, we establish the lemma. ||

Under H_0 , $r(t) \equiv \lambda$ and we see from the lemma that, given k observed failures,

$$W_a \stackrel{\text{st}}{=} \frac{\sum_{i=1}^k a_i Y_i}{\sum_{j=1}^k Y_j},$$

where $\stackrel{\text{st}}{=}$ denotes stochastic equality and $Y_1, Y_2, \dots, Y_k$ are independent, exponentially distributed random variables with unit mean.

3. UNBIASEDNESS UNDER IFRA ALTERNATIVES

We need the following lemma to establish unbiasedness. Define

$$R(t) = \int_0^t r(u)du \quad \text{and} \quad T(t) = \int_0^t n(u)du .$$

Lemma 2.

If $\frac{R(t)}{t}$ is nondecreasing in $t \geq 0$, $n(t) \geq 0$, and $\frac{T(t)}{t}$ is nonincreasing in $t \geq 0$, then

$$(i) \quad r(t) \geq \frac{\int_0^t r(u)du}{t} \geq \frac{\int_0^t r(u)dT(u)}{T(t)}$$

$$(ii) \quad \frac{\int_0^t r(u)dT(u)}{T(t)} \quad \text{is nondecreasing in } t \geq 0 ,$$

when the indicated integrals exist.

Proof:

To show (i). The first inequality follows from differentiating $\frac{R(t)}{t}$. Since $\frac{R(t)}{t} \geq 0$ is nondecreasing in $t \geq 0$, we can approximate $R(t)$ arbitrarily closely from below by a positive linear combination of functions of the form

$$R(t) = \begin{cases} 0 & 0 \leq t < x \\ t & t \geq x \end{cases}$$

[cf. Barlow, Marshall, and Proschan (1967)]. By the Lebesgue monotone convergence theorem, we need only establish the second inequality in (ii) for functions $R(t)$ of this type. Hence for $t \geq x$,

$$\frac{\int_0^t n(u) dR(u)}{T(t)} = \frac{n(x)x + \int_x^t n(u) du}{T(t)} = 1 + \frac{xn(x) - T(x)}{T(t)}.$$

This is nondecreasing in $t \geq x$ since (a) $T(t)$ is nondecreasing in $t \geq 0$, and (b) $xn(x) - T(x) \leq 0$ since $\frac{T(x)}{x}$ is nonincreasing in $x \geq 0$.

To show (ii). Clearly

$$\frac{d}{dt} \left[\frac{\int_0^t r(u)n(u) du}{\int_0^t n(u) du} \right] \geq 0$$

if and only if

$$r(t)n(t) \int_0^t n(u) du \geq n(t) \int_0^t r(u)n(u) du$$

which follows from (i). ||

Note that if $r(t)$ is nondecreasing in $t \geq 0$, then (ii) follows for all $n(t) \geq 0$.

Lemma 2 may be used in testing for IFRA in models other than the one described in the introduction; see for example the model of Bray, Crawford, and Proschan (1967).

Theorem 1.

If F is IFRA with failure rate $r(t)$ and $Z_{(1)} \leq Z_{(2)} \leq \dots \leq Z_{(k)}$ are the observed failure times, $n(t) \geq 0$ for $t \geq 0$, and $\frac{T(t)}{t} \geq 0$ is nonincreasing in $t \geq 0$, then (conditional on k),

$$W_a = \frac{\sum_{i=1}^k a_i \int_{Z_{(i-1)}}^{Z_{(i)}} n(u) du}{\int_0^{Z_{(k)}} n(u) du} \geq \frac{\sum_{i=1}^k a_i Y_i}{\sum_{i=1}^k Y_i}$$

where $a_1 \geq a_2 \geq \dots \geq a_n$ and $Y_1, Y_2, \dots, Y_k$ are independently distributed as exponential random variables with unit mean.

Proof:

Since $n(u) \geq 0$ and $T(t)/t$ is nonincreasing, Lemma 2 applies, yielding

$$\frac{\beta_i}{\alpha_i} = \frac{\int_0^{Z_{(i)}} r(u)n(u) du}{\int_0^{Z_{(i)}} n(u) du}$$

nondecreasing in $i = 1, 2, \dots, k$. By Lemma 1 we need only show that

$$(1) \quad \frac{\sum_{i=1}^k a_i \int_{Z_{(i-1)}}^{Z_{(i)}} n(u) du}{\int_0^{Z_{(k)}} n(u) du} \geq \frac{\sum_{i=1}^k a_i \int_{Z_{(i-1)}}^{Z_{(i)}} r(u)n(u) du}{\int_0^{Z_{(k)}} r(u)n(u) du}$$

i.e.,

$$\frac{\sum_{i=1}^k a_i (\alpha_i - \alpha_{i-1})}{\alpha_k} = \frac{\sum_{i=1}^k a_i (\beta_i - \beta_{i-1})}{\beta_k}$$

where $\alpha_0 = \beta_0 \equiv 0$. Note that

$$\sum_{i=1}^k a_i (\alpha_i - \alpha_{i-1}) = (a_1 - a_2)\alpha_1 + (a_2 - a_3)\alpha_2 + \dots + a_k \alpha_k = \sum_{i=1}^k \Delta_i \alpha_i$$

where $\Delta_i = a_i - a_{i+1} \geq 0$ for $i = 1, 2, \dots, k-1$ and $\Delta_k = a_k$. Hence

$$\frac{\beta_i}{\alpha_i} \leq \frac{\beta_k}{\alpha_k} \quad \text{implies} \quad \sum_{i=1}^k \frac{\Delta_i \alpha_i}{\alpha_k} \geq \sum_{i=1}^k \frac{\Delta_i \beta_i}{\beta_k}, \text{ which proves (1). } ||$$

4. APPLICATION OF TOTAL TIME ON TEST

Assuming an exponential distribution, the results of Bickel and Doksum (1968) may be used to establish the asymptotic normality of W_a in the incomplete data case for selected vectors $a = (a_1, \dots, a_k)$. Perhaps, the most useful test is the total time on test statistic. In the case of a complete sample of size n , this is S_1^* in the Bickel-Doksum paper, obtained by choosing $a_1 = -1/(n+1)$, after algebraic manipulation. In the case of incomplete data as described in the introduction, with k failures observed; the total time on test statistic is

$$W_{a^\circ} = \frac{\sum_{i=1}^{k-1} (k-i) \int_{Z_{(i-1)}}^{Z_{(i)}} n(u) du}{\int_0^{Z_{(k)}} n(u) du},$$

obtained by choosing $a^\circ = (k-1, k-2, \dots, 1, 0)$.

The exact distribution conditioned on the number of observed failures $k \geq 2$ is easily computed in this case. Table 1 is a short table of percentage points. Note that, under H_0

$$W_{a^\circ} \stackrel{\text{st}}{=} U_1 + U_2 + \dots + U_{k-1}$$

when U_i ($i = 1, 2, \dots, k-1$) are independent uniform random variables on $[0, 1]$. Since the distribution of W_{a° is symmetric about $\frac{k-1}{2}$, we tabulate upper percentiles only.

TABLE 1: PERCENTILES χ_α OF TOTAL TIME ON TEST STATISTIC, W_{a°

$k-1 \backslash \alpha$	.900	.950	.975	.990	.995
2	1.553	1.684	1.776	1.859	1.900
3	2.157	2.331	2.469	2.609	2.689
4	2.753	2.953	3.120	3.300	3.411
5	3.339	3.565	3.754	3.963	4.097
6	3.917	4.166	4.376	4.610	4.762
7	4.489	4.759	4.988	5.244	5.413
8	5.056	5.346	5.592	5.869	6.053
9	5.619	5.927	6.189	6.487	6.683
10	6.178	6.504	6.781	7.097	7.307
11	6.735	7.077	7.369	7.702	7.924
12	7.289	7.647	7.953	8.302	8.535

k = number of failures observed in incomplete sample

$$P[W_{a^\circ} \leq \chi_\alpha] = \alpha$$

5. MONOTONE TESTS UNDER IFR ALTERNATIVES

Bickel and Doksum (1968) define a test ϕ to be monotone in the normalized spacings $D_1, \dots, D_n$ if $\phi(D'_1, \dots, D'_n) \leq \phi(D_1, \dots, D_n)$ for all $(D_1, \dots, D_n)$ and $(D'_1, \dots, D'_n)$ such that for $i < j$, $D'_i \geq D'_j$ implies $D_i \geq D_j$. We show

that if D_i is replaced by $\int_{Z_{(i-1)}}^{Z_{(i)}} n(u) du$ in the incomplete data case, then a

monotone test is unbiased for testing H_0 versus H_1 when $n(u) \geq 0$ for $u \geq 0$. The test rejects H_0 for large values of ϕ .

We need

Lemma 3.

Let $r(u) \uparrow$ and $n(u) \geq 0$ for $u \geq 0$. Then for $0 \leq a < b \leq c < d$,

$$\frac{\int_a^b n(u)r(u)du}{\int_a^b n(u)du} \leq \frac{\int_c^d n(u)r(u)du}{\int_c^d n(u)du}.$$

Proof:

$$\frac{\int_a^b n(u)r(u)du}{\int_a^b n(u)du} \leq \frac{r(b) \int_a^b n(u)du}{\int_a^b n(u)du} \leq \frac{r(c) \int_c^d n(u)du}{\int_c^d n(u)du} \leq \frac{\int_c^d n(u)r(u)du}{\int_c^d n(u)du}. \quad ||$$

From Lemma 3, we immediately obtain

Theorem 2.

Let ϕ be a monotone test of H_0 versus H_1 based on a sample of incomplete data as described in the introduction. Then

$$E \left[\phi \left(\int_0^{Z^{(1)}} n(u) du, \dots, \int_{Z^{(k-1)}}^{Z^{(k)}} n(u) du \right) \mid F \text{ IFR} \right] \geq \\ \geq E[\phi(Y_1, \dots, Y_k) \mid F \text{ exponential}],$$

where $Y_1, \dots, Y_k$ independent exponentially distributed random variables.

Proof:

For $i < j$,

$$\frac{\int_{Z^{(i-1)}}^{Z^{(j)}} n(u) du}{\int_{Z^{(i-1)}}^{Z^{(i)}} n(u) du} \leq \frac{\int_{Z^{(i-1)}}^{Z^{(j)}} r(u) n(u) du}{\int_{Z^{(i-1)}}^{Z^{(i)}} r(u) n(u) du} \stackrel{\text{st}}{=} \frac{Y_j}{Y_i}.$$

The inequality follows from Lemma 3; the stochastic equality follows from Lemma 1.

$$\text{Thus } \phi(Y_1, \dots, Y_k) \stackrel{\text{st}}{\leq} \phi \left(\int_0^{Z^{(1)}} n(u) du, \dots, \int_{Z^{(k-1)}}^{Z^{(k)}} n(u) du \right). \text{ The}$$

conclusion follows by taking expectations. ||

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DOCUMENT CONTROL DATA - R&D		
(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)		
1 ORIGINATING ACTIVITY (Corporate author) University of California, Berkeley		2a REPORT SECURITY CLASSIFICATION Unclassified
		2b GROUP
3 REPORT TITLE A NOTE ON TESTS FOR MONOTONE FAILURE RATE BASED ON INCOMPLETE DATA		
4 DESCRIPTIVE NOTES (Type of report and inclusive dates) Research Report		
5 AUTHOR(S) (Last name, first name, initial) BARLOW, Richard E. PROSCHAN, Frank		
6 REPORT DATE April 1968	7a TOTAL NO OF PAGES 14	7b NO OF REFS 5
8a CONTRACT OR GRANT NO. Nonr-3656(18)	9a ORIGINATOR'S REPORT NUMBER(S) ORC 68-7	
b. PROJECT NO NR 042 238		
c Research Project No.: WW 041	9b OTHER REPORT NO(S) (Any other numbers that may be assigned this report)	
d		
10 AVAILABILITY/LIMITATION NOTICES Distribution of this document is unlimited.		
11 SUPPLEMENTARY NOTES SEE TITLE PAGE	12 SPONSORING MILITARY ACTIVITY Mathematical Science Division	
13 ABSTRACT Tests for exponential versus IFRA distributions based on incomplete data are defined and shown to be unbiased. The tests are motivated by a class of tests considered in detail by Bickel and Doksum. Tests for exponential versus IFR distributions based on the ranks of total time on test statistics are also considered.		

DD FORM 1473
1 JAN 64

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14 KEY WORDS	LINK A		LINK B		LINK C	
	ROLE	WT	ROLE	WT	ROLE	WT
Monotone Failure Rate IFRA Distributions Exponential Total Time on Test Unbiased Tests						

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