

ASD-TR-68-19

AD 675643

# COMPUTER PROGRAM FOR REDUCING STATIC PROPELLER TEST DATA

*GERALD T. CAFARELLI*

*MATTHEW H. CHOPIN*

TECHNICAL REPORT ASD-TR-68-19

JUNE 1968

OCT 4 1968

This document has been approved for public  
release and sale; its distribution is unlimited.

DEPUTY FOR ENGINEERING  
AERONAUTICAL SYSTEMS DIVISION  
AIR FORCE SYSTEMS COMMAND  
WRIGHT-PATTERSON AIR FORCE BASE, OHIO

Reproduced by the  
CLEARINGHOUSE  
for Federal Scientific & Technical  
Information Springfield Va. 22151

## NOTICE

When Government drawings, specifications, or other data are used for any purpose other than in connection with a definitely related Government procurement operation, the United States Government thereby incurs no responsibility nor any obligation whatsoever; and the fact that the Government may have formulated, furnished, or in any way supplied the said drawings, specifications, or other data, is not to be regarded by implication or otherwise as in any manner licensing the holder or any other person or corporation, or conveying any rights or permission to manufacture, use, or sell any patented invention that may in any way be related thereto.

This document has been approved for public release and sale; its distribution is unlimited.

Copies of this report should not be returned unless return is required by security considerations, contractual obligations, or notice on a specific document.

ASD-TR-68-19

**COMPUTER PROGRAM FOR REDUCING  
STATIC PROPELLER TEST DATA**

*GERALD T. CAFARELLI*

*MATTHEW H. CHOPIN*

**This document has been approved for public  
release and sale; its distribution is unlimited.**

**FOREWORD**

This report was prepared by the V/STOL Propulsion Branch, Directorate of Propulsion and Power Subsystems Engineering, Deputy for Engineering, Aeronautical Systems Division, under System 478A. Work was accomplished from July 1966 to November 1967. The authors served as project engineers.

This report was released by the authors in April 1968.

The authors wish to express their appreciation to Major Allan Gay, Directorate of Computation Services, Deputy for Engineering, for developing the computer program and applying the curve-fit technique to the data reduction as described in this report.

This technical report has been reviewed and is approved.



**JAMES G. BARRETT**  
Technical Director  
Directorate of Propulsion and  
Power Subsystems Engineering

ABSTRACT

A computer program using a curve-fit technique was developed to reduce performance data obtained from static tests of aircraft propellers. The entire program is written in Fortran IV language for use on the IBM 7094 computer located at Wright-Patterson AFB, Ohio.

The program accepts static whirl rig test data (ie, raw RPM, horsepower, and thrust data) obtained at a fixed blade angle and reduces it into pertinent propeller relationships. The program first reduces the test data into various coefficients and computes the propeller tip Mach number. A curve fit technique then fits running curves through the test thrust and horsepower data points at the test tip Mach numbers. Intermediate horsepower and thrust values are determined from the fitted curves at selected Mach number increments, and all coefficients are recomputed. This results in a presentation of the reduced data in two forms, coefficients computed from the actual test data and coefficients obtained at specific constant Mach number increments from the fitted curves. The data is presented in tabular printout form. This is a general program and is written so that the order of the curve fit, the Mach number increment, the number of test data points and the Mach number range can be varied.

The entire program deck and all nonstandard subroutines are included. Detail instructions are provided which should allow the program to be used by technicians or students who are familiar with Fortran IV language.

CONTENTS

SECTION		PAGE
I	INTRODUCTION	1
II	COMPUTER PROGRAM	2
	1. Program Operation	2
	2. Subroutine XIPLSQ	2
	3. Data Input	7
III	PROGRAM PARAMETERS	8
	1. Namelists	8
	2. Equations	9
	3. Other Program Variables	9
IV	COMPARISON OF CURVES	12
APPENDIX	COMPUTER PROGRAM	15

ILLUSTRATIONS

FIGURE		PAGE
1.	Sample Input Data	3
2.	Typical Rig Data Sheet	4
3.	Sample Coding Form	5
4.	Typical Computer Printout	6
5.	Comparison of Thrust Curve-Fit Data to Raw Data	13
6.	Comparison of Horsepower Curve-Fit Data to Raw Data	14

## SECTION I

### INTRODUCTION

This program was developed to reduce data accumulated during an extensive series of static tests of propellers for the XC-142A V/STOL aircraft conducted at Wright-Patterson Air Force Base, Ohio. These tests are described in detail in a report being prepared entitled "Propeller Static Performance Tests for V/STOL Aircraft." The program is complete in that it contains all non-standard subroutines.

The program reduces RPM and corrected horsepower and thrust data at any given blade angle and computes Power Coefficient ( $C_p$ ), Thrust Coefficient ( $C_t$ ),  $C_t/C_p$ , Figure of Merit (F.M.) and thrust/horsepower (TH/HP). Propeller tip Mach number is calculated using propeller diameter, RPM and ambient temperature. A curve fit technique is then employed to fit a running selected degree polynomial using least squares to NPHP (horsepower) or NPTH (thrust) consecutive test data points (see NAMELIST) at the test tip Mach numbers. In this case, a 2nd degree polynomial was fit to 6 consecutive data points. Intermediate horsepower and thrust values are determined from the fitted curves at the selected Mach number increments. The routine proceeds until smoothed curves for horsepower (HPI) and thrust (THI), and derived coefficient values plus corresponding RPM and tip speed (TIPS), have been computed at all of the selected increments of Mach number. The procedure is essentially one of creating equal tabular entries through a smoothing technique rather than through an interpolative procedure.

The Namelist variables establish the boundaries of the program, such as the Mach number increments and range, number of data points fitted by the polynomial, and the degree of the polynomial. All variables can be changed to adapt the program to other uses.

## SECTION II

### COMPUTER PROGRAM

#### 1. PROGRAM OPERATION

The computer program is designed to provide parameters for aircraft propellers at specified tip Mach number increments by fitting curves to data for horsepower and thrust versus Mach number at a set blade angle and re-computing values for the parameters at the predetermined Mach number increments. A flow chart showing the order of the program and the data input is given in Figure 1. Data is obtained from a test rig data sheet, such as is shown in Figure 2, and coded for the computer as shown in Figure 3.

For a given blade angle, the data must be presented to the computer at increasing values of RPM. After receiving the data input, the computer calculates the various parameters from the test data, including Mach number,  $C_t$ ,  $C_p$ ,  $C_t/C_p$ , F.M., and TH/HP, according to the appropriate equations (given in the list of program variables). Values are printed out on the output sheet, Figure 4, as Raw Data Points.

Subroutine XIPLSQ is then called to fit a 6-point, 2nd order, least squares curve through the data points for HP and TH at test tip Mach numbers. Then the computer determines values for HP and TH from the fitted curves that correspond to the selected Mach numbers, and uses these values to recompute values for all parameters at the selected Mach numbers. These values are then printed out on the output sheet as shown on Figure 4 under Fitted Curve Data for Constant Mach Number Increments.

The computer then reads in the data for a new blade angle (2nd Beta, 3rd Beta, etc.) and repeats the computations.

#### 2. SUBROUTINE XIPLSQ

The least squares curve is fitted by means of Subroutine XIPLSQ. HPI and THI values are computed as functions of the independent variable BMACH by

ORDER OF INPUT SEQUENCE

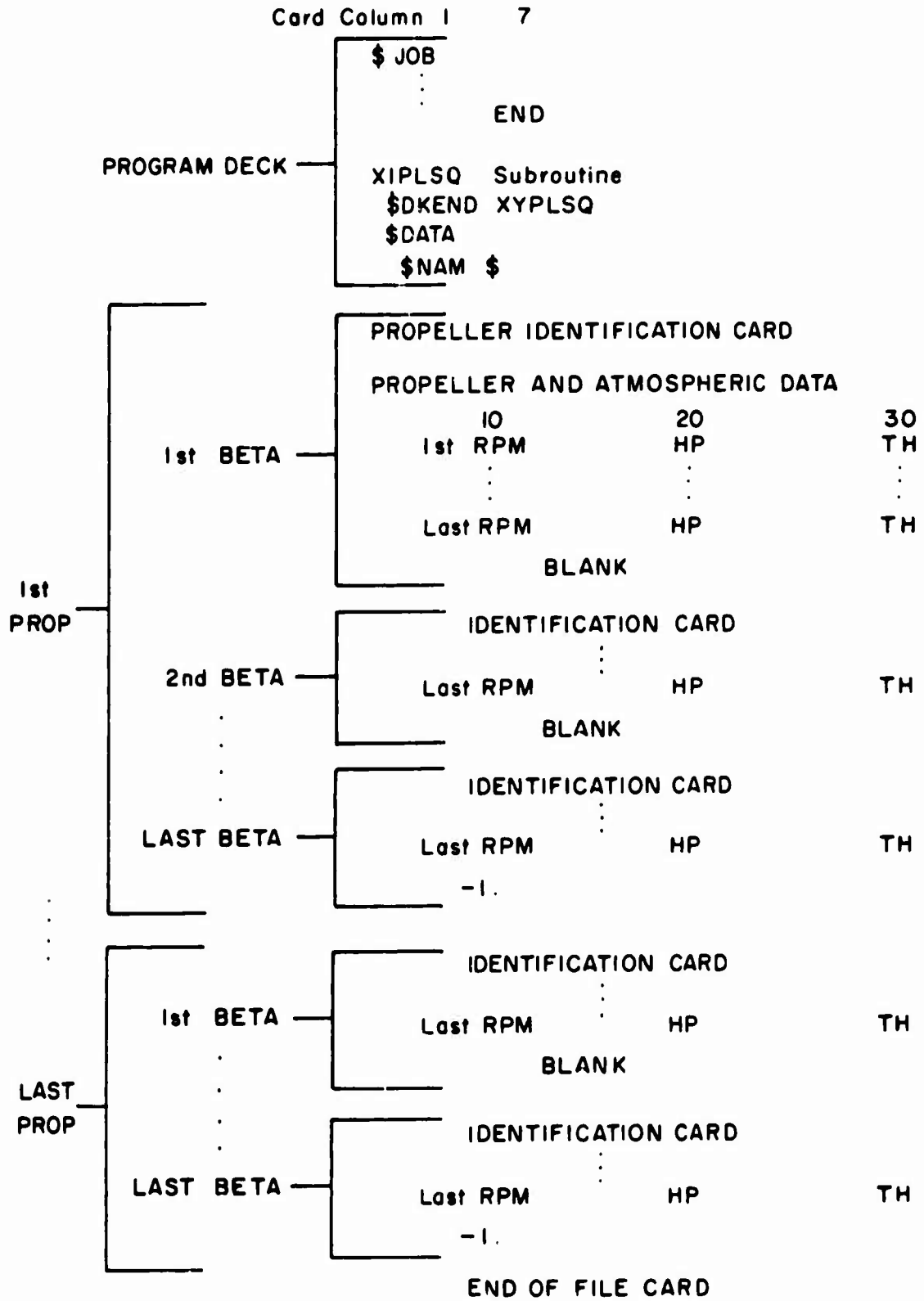


Figure 1. Sample Input Data





STATIC PROP PERFORMANCE

2FF13A1-4A 7JAN66 RUN #0 230 WALLS DOWN 15000 FT-LR

BETA=12.1 AF= -0. DIA=15.625 NBL=4 TEMPC= -4.0 TEMPR= 486.49 SIGMA=1.0500

\*\*\*\*\* RAW DATA POINTS \*\*\*\*\*

RPM	HP	TH	TMACH	RCT	RCP	RCT/CP	RFM	RTH/HP
652.	372.	2762.	0.494	0.1655	0.0721	2.2964	0.7454	7.4247
702.	475.	3237.	0.552	0.1683	0.0739	2.2786	0.7450	6.3424
749.	530.	3714.	0.568	0.1685	0.0741	2.2752	0.7455	6.4034
797.	723.	4354.	0.604	0.1730	0.0767	2.2559	0.7497	5.9658
848.	853.	4790.	0.643	0.1696	0.0751	2.2589	0.7425	5.6155
895.	1049.	5952.	0.661	0.1753	0.0775	2.2611	0.7555	5.3078
955.	1283.	6382.	0.724	0.1774	0.0794	2.2342	0.7509	4.9317
1003.	1517.	7103.	0.760	0.1799	0.0808	2.2255	0.7532	4.6774
1052.	1784.	7876.	0.797	0.1812	0.0823	2.2032	0.7485	4.4148
1096.	2060.	8695.	0.831	0.1843	0.0840	2.1945	0.7519	4.2209
1142.	2435.	9833.	0.870	0.1901	0.0882	2.1551	0.7499	3.9574
1194.	2884.	10837.	0.905	0.1940	0.0910	2.1323	0.7494	3.7646
1239.	3224.	11619.	0.932	0.1956	0.0930	2.1028	0.7421	3.6039

\*\*\*\*\* FITTED CURVE DATA FOR CONSTANT MACH NUMBER INCREMENTS \*\*\*\*\* (HP, 6 POINT 2ND ORDER, TH, 6 POINT 2ND ORDER)

MACH	HP	TH	TIPS	RPM	CT	CP	CT/CP	FY	TH/HP
0.725	1293.	6379.	743.	957.	0.1775	0.0793	2.239	0.753	4.934
0.770	1453.	6392.	810.	990.	0.1793	0.0805	2.227	0.753	4.745
0.775	1615.	7329.	837.	1023.	0.1800	0.0811	2.219	0.751	4.576
0.800	1804.	7956.	864.	1059.	0.1819	0.0823	2.209	0.752	4.411
0.825	2022.	8574.	891.	1088.	0.1843	0.0842	2.190	0.750	4.241
0.850	2262.	9243.	918.	1121.	0.1872	0.0861	2.174	0.750	4.086
0.875	2529.	9934.	944.	1154.	0.1898	0.0882	2.152	0.748	3.930
0.900	2819.	10663.	971.	1187.	0.1926	0.0904	2.131	0.746	3.784
0.925	3134.	11430.	998.	1220.	0.1954	0.0926	2.111	0.745	3.647

Figure 4. Typical Computer Printout

means of a polynomial smoothing process; this process resembles nonlinear interpolation in that it considers several points of the HP and TH versus AMACH tabular data function on either side of the desired BMACH value in determining a least squares polynomial, and this polynomial is then used to determine the smoothed HPI and THI values.

Smoothing in the vicinity of the ends of the test data array will not produce as satisfactory results as in the center because there are not sufficient data points available on both sides of the desired BMACH argument. The polynomial is always fit to the predetermined number of test data points, however, so additional data points from the other side are used to augment the least squares input data. If the desired BMACH value is out of range of the test data, however, extrapolative smoothing would be required, which would give results of even less reliability.

Note that if the fitted polynomial is of the Nth degree,  $N + 1$  data points are required to develop the smoothing polynomial.

### 3. DATA INPUT

The first data input card (propeller identification card) shows which propeller data is being computed. The second card gives the basic propeller data and atmospheric conditions at the time that the test was run, including the number of blades, propeller diameter, activity factor, blade angle setting, temperature ( $^{\circ}\text{C}$ ), and density ratio (air factor). The first RPM value with its corresponding HP and TH values is punched on the third card, and values for increasing RPMs are punched on succeeding cards. A blank card is placed after the last RPM-HP-TH card if another blade angle run is to be computed for that propeller; if no more blade angle runs are to be made, a "-1." card (with -1. punched within the first 10 spaces) follows.

SECTION III  
PROGRAM PARAMETERS

1. NAMELIST

The variables in the Namelist control various aspects of the program. They are set at specified values by the DATA statement near the beginning of the program deck.

There is one Namelist, NAM, for this program, consisting of the following variables:

- VL = VL + VS, - minimum selected Mach number for curve-fitted data (VL set at 0.500)
- VH - maximum selected Mach number for curve fitted data (VH set at 1.000)
- VS - increment increase in selected Mach numbers (VS set at 0.025)
- NPTH - maximum number of raw thrust points considered at one time for a curve fit (NPHP set at 6)
- NPHP - maximum number of raw horsepower points considered at one time for a curve fit (NPHP set at 6)
- NDTH - order of the polynomial used for fitting the thrust curve. (NDTH is set at 2; that is, a running polynomial of the form  $C_0 + C_1 x + C_2 x^2$  is used in smoothing the thrust data unless modified by parameter control.)
- NDHP - see information for NDTH, above (set at 2).

Namelist values can be modified by the simple procedure of replacing one card. For example, if the value for VH (maximum Mach number) is to be changed from 1.000 to 0.900, the following card would be removed

Card Column 2

\$ NAM \$ (the first card after the \$ DATA control card)

and the following card inserted:

Card Column 2

\$ NAM VH = .9\$

2. EQUATIONS

The following equations are used in computing the parameters.

$$TR = 1.8(TC + 273.16)$$

$$AMACH = \left(\frac{\pi}{60}\right) \frac{(RPM) (DIA)}{(49.04) \sqrt{TR}}$$

$$CT = CT(TH) = 0.1518 \times 10^7 \frac{TH}{(RPM)^2 (DIA)^4}$$

$$CTI = CT(THI) \quad (\text{see THI})$$

$$CP = CP(HP) = 0.5 \times 10^{11} \frac{HP}{(RPM)^3 (DIA)^5}$$

$$CPI = CP(HPI) \quad (\text{see HPI})$$

$$FM = FM(CT, CP) = 0.798 \frac{|CT|^{1.5}}{CP} ; \quad \text{if } CT < 0, \text{ FM is set at minus value.}$$

$$FMI = FM(CTI, CPI)$$

3. OTHER PROGRAM VARIABLES

a. Nonsubscripted Variables

NBL - number of blades per propeller (reference data)

AF - activity factor (reference data)

DIA - diameter of propeller, feet

RPM - propeller speed (revolutions per minute)

CT - coefficient of thrust

CP - coefficient of power

FM - Figure of Merit

TIPS - actual tip speed, ft/sec

b. Subscripted Variables

HEAD - propeller identification

B - BETA, blade angle, degrees (reference data)

TC - TEMPC, ambient temperature (°C)

S - "sigma" = (air factor) density ratio ( $\sigma$ )

TR - TEMPR, ambient temperature (°R)

HP - corrected horsepower; (Corrected HP =  $\frac{\text{Test HP}}{\sigma}$ )

TH - corrected thrust, pounds (Corrected TH =  $\frac{\text{Test TH}}{\sigma}$ )

AMACH - actual tip Mach number

BMACH - selected Mach number for curve fit

THI - thrust values determined from the smoothed thrust curve.

HPI - horsepower values determined from the smoothed horsepower curve.

FMI - interpolated figure of merit

CTI - interpolated coefficient of thrust

CPI - interpolated coefficient of power

c. Counters

NP - number of propellers

NB - number of blade angles

N - number of cards per blade angle run

NV-J-1 - number of selected Mach numbers per run

d. Miscellaneous Parameters

$$AF - \text{activity factor} = \frac{100,000}{16} \int_{0.2}^{1.0} \frac{b}{DIA} \left(\frac{r}{R}\right)^3 d\left(\frac{r}{R}\right)$$

ASD-TR-68-19

b - blade width, feet

R - total blade radius, feet

r - radius along blade, feet

$\sigma$  - density ratio;  $\sigma = \frac{\rho}{\rho_0}$  (reference data)

$\rho$  - local density, lb sec<sup>2</sup>/ft<sup>4</sup>

$\rho_0$  - sea level standard density, lb sec<sup>2</sup>/ft<sup>4</sup>

## SECTION IV

### COMPARISON OF CURVES

A comparison of the computer curve-fit data with hand-faired data for thrust and horsepower is shown in Figures 5 and 6. These figures show that the test data and the computer curve-fit provide very good agreement. The curve-fit results in a substantial smoothing of the data.

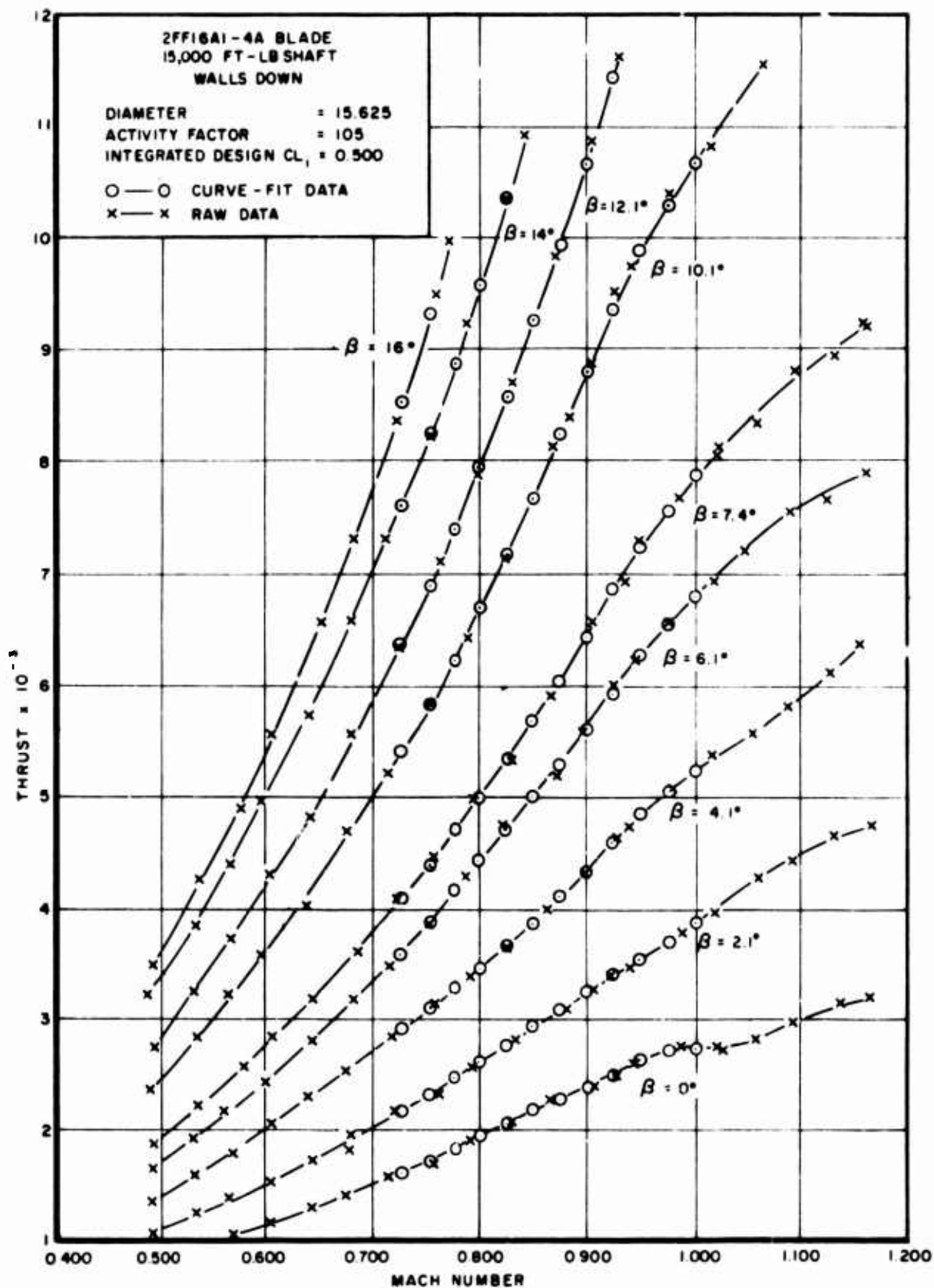


Figure 5. Comparison of Thrust Curve-Fit Data to Raw Data

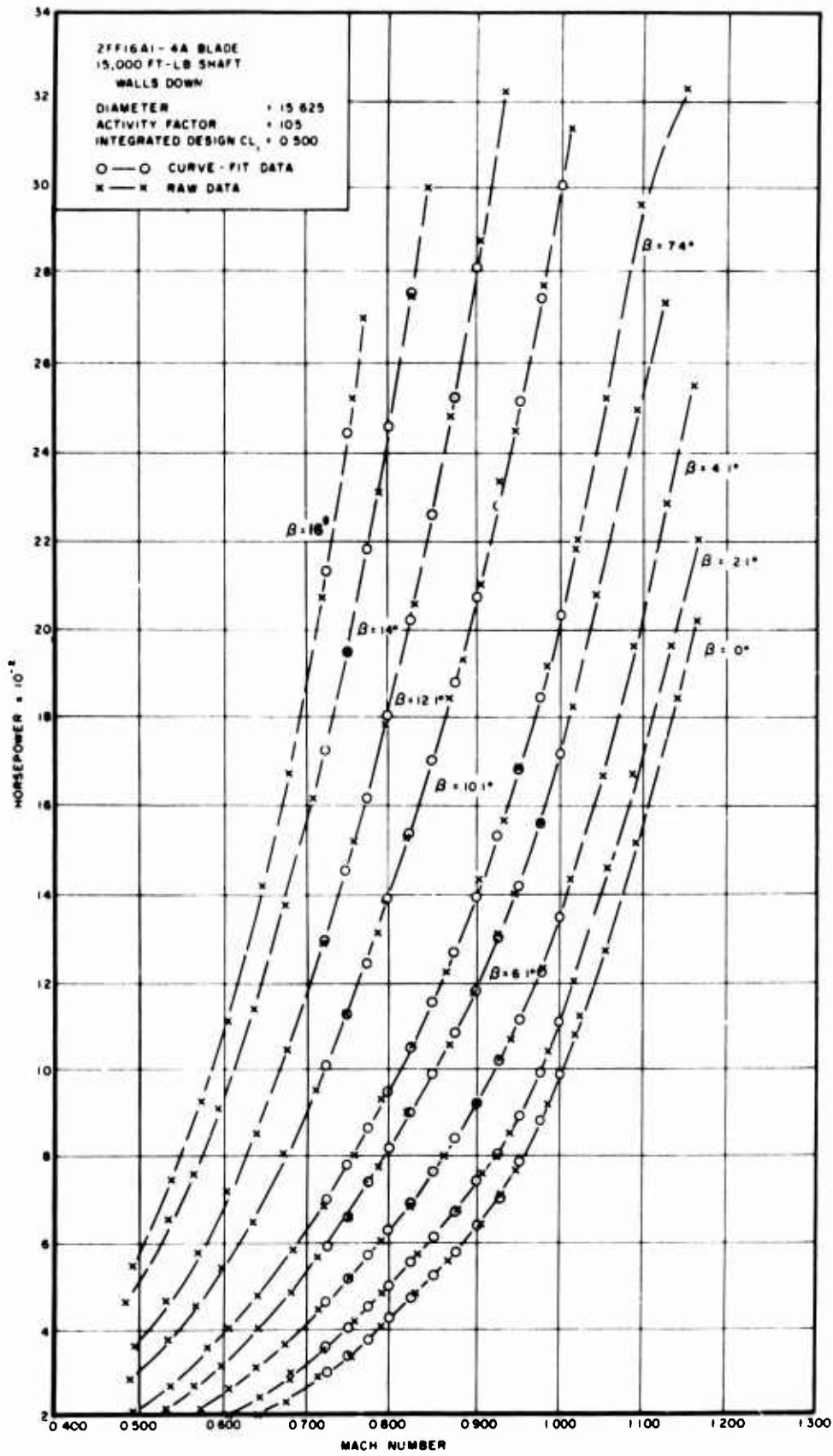


Figure 6. Comparison of Horsepower Curve-Fit Data to Raw Data

APPENDIX  
COMPUTER PROGRAM

This appendix presents the basic computer program and the necessary subroutines, followed by an explanation of the subroutines.

```

$IRJOB PROP MAP
$IBFTC CHOPN DECK
  DIMENSION HEAD(13),B(30),TC(30),S(30),TR(30),HPI(30),TH(30),
  1 AMACH(30),EMACH(60,60),THI(60),HPI(60),FMI(60),FMI(60,60),
  2 CTI(60,60),CPI(60,60)
  DATA ZC/273.16/,COFT/49.04/,COFCT/.1518E7/,COFCP/.5E11/,
  1 COFFMA,798/VL/.5/,VH/1./,VS/.025/,NPTH/6/,NPHP/6/,
  2 NDTH/2/,NDHP/2/,LIST/0/
  NAMELIST/NAM/VL,VH,VS,NPTH,NPHP,NDTH,NDHP,LIST
C NAMELIST NAM PARAMETERS,
C VL(VS)VH = LOW, STEP, HIGH, MACH NUMBER TABULAR INTERVAL (SMOOTHED).
C NPTH, NPHP = NUMBER OF POINTS USED IN SMOOTHING THRUST, HORSEPOWER.
C NDTH, NDHP = DEGREE OF POLYNOMIAL USED IN SMOOTHING TH AND HP.
C LIST = 0,1 LEAST SQUARES ANALYSIS NOT USED (0), USED (1).
  PIO60=4.*DATAN(1.00)/60.
  10 READ(5,NAM)
  NP=0
  15 NP=NP+1
  DO 20 K=1,30
  DO 20 L=1,30
  CTI(K,L)=0.
  20 CPI(K,L)=0.
  NR=0
  25 NB=NB+1
  READ(5,30)(HEAD(J),J=1,13)
  30 FORMAT(13A6)
  READ(5,35)NBL,AF,DIA,B(NB),TC(NB),S(NB)
  35 FORMAT(1I0,5F10.5)
  TR(NB)=1.8*(TC(NB)+ZC)
  WRITE(6,40)(HEAD(J),J=1,13),B(NB),AF,DIA,NBL,TC(NB),TR(NB),S(NB)
  40 FORMAT(24H1STATIC PROP PERFORMANCE/////1H0,13A6/7H0 BETA=F4.1,
  14H AF=,
  2 F5.1,5H DIA=F6.3,5H NBL=,11,7H TEMPC=F5.1,7H TEMPR=F7.2,
  3 7H SIGMA=F6.4)
  WRITE(6,45)
  FORMAT(28H0***** RAW DATA POINTS *****/
  45 1 1H0,7X,3HRPM,4X,2HHP,4X,2HTH,1X,5HTMACH,7X,3HRCT,7X,3HRCP,4X,
  2 6HRCT/CP,7X,3HRFM,4X,6HRTTH/HP)
  N=0
  50 N=N+1
  READ(5,55)RPM,HP(N),TH(N)
  55 FORMAT(3F10.1)
  TEST=RPM
  IF(TEST.LE.0.) GO TO 75
  AMACH(N)=(PIO60*RPM*DIA)/(COFT*SQRT(TR(NB)))
  CT=COFCT*TH(N)/(RPM**2*DIA**4)

```

```

CP=COFCP*HP(N)/(RPM**3*DIA**5)
CTOCP=CT/CP
FM=COFFM*SIGN(ABS(CT)**1.5,CT)/CP
THOHP=TH(N)/HP(N)
WRITE(6,70)RPM,HP(N),TH(N),AMACH(N),CT,CP,CTOCP,FM,THOHP
FORMAT(5X,3F6.0,F6.3,5F10.4)
GO TO 50
70
75 N=N-1
WRITE(6,80)NPH,NDHP,NPTH,NDTH
FORMAT(66H0**** FTTED CURVE DATA FOR CONSTANT MACH NUMBER
1 INCREMENTS *****5H (HP,12.6H PCINT,12,14HND ORDER. TH,12,
2 6H POINT,12,9HND ORDER)/
3 1H0,6X,4HMACH,5X,2HHP,5X,2HTH,3X,4HTIPS,4X,
4 3HRPM,6X,2HCT,5X,2HCP,2X,5HCT/CP,5X,2HFM,2X,5HTH/HP)
J=0
STEP=0.
82 J=J+1
83 STEP=STEP+1.
BMACH(J,NB)=VL+STEP*VS
IF(BMACH(J,NB).LT.AMACH(1)) GO TO 83
IF(BMACH(J,NB).GT.AMACH(N).OR.BMACH(J,NB).GT.VH) GO TO 90
CALL XIPLSQ(AMACH,HP,BMACH(J,NB),HPI(J),
1 N,MINO(N,NPH),NDHP,LIST,LE)
CALL XIPLSQ(AMACH,TH,BVACH(J,NB),THI(J),
1 N,MINO(N,NPTH),NDTH,LIST,LE2)
TIP=BMACH(J,NB)*COFT*SORT(TR(NB))
RPM=TIP/(PI060*DIA)
CTI(J,NB)=COFCT*THI(J)/(RPM**2*DIA**4)
CPI(J,NB)=COFCP*HPI(J)/(RPM**3*DIA**5)
CTOCP=CTI(J,NB)/CPI(J,NB)
FMI(NB,J)=COFFM*SIGN(ABS(CTI(J,NB)**1.5,CTI(J,NB))/CPI(J,NB)
THOHP=THI(J)/HPI(J)
WRITE(6,85)BMACH(J,NB),HPI(J),THI(J),TIP,RPM,CTI(J,NB),
1 CPI(J,NB),CTOCP,FMI(NB,J),THOHP
85 FORMAT(5X,F6.3,4F7.0,F8.4,F7.4,3F7.3)
GO TO 82
90 NV=J-1
95 IF(TEST.EQ.0.) GO TO 25
110 IF(TEST.EQ.-1.) GO TO 15
GO TO 10
END

```

```

*TRFCT XYP LSG DECK
SUBROUTINE XIPLSQ (X,Y,XI,YI,N,NP,LD,LIST,LE)
DIMENSION X(1),Y(1),C(11)
LE=0
LD1=LD+1
IF (N) 1,1,2
1  LE=1
   RETURN
2  IF (NP) 3,3,4
3  LF=2
   RETURN
4  IF (N-NP) 5,6,6
5  LF=3
   RETURN
6  IF (X(1)-X(N)) 7,7,8
7  DO 11 I=1,N
   K1=I
   IF (X(I)-XI) 11,12,10
11 CONTINUE
   GO TO 14
8  DO 13 I=1,N
   K1=N
   IF (X(I)-XI) 10,12,13
13 CONTINUE
14 K1=N+1-NP
   GO TO 17
10 K1=K1-1
12 K1=K1-(NP-1)/2
   IF (K1) 9,9,15
   K1=1
   GO TO 17
15 IF (K1-NP-1-N) 17,17,16
16 K1=N+1-NP
17 CALL PLSQ (X(K1),Y(K1),NP,LD,C,LIST,EMAX,ERM,S,EMEQ),
   YI=C(1)
   DO 18 I=2,LD1
18 YI=YI*XI+C(I)
   RETURN
END

```



```

20 DO 20 I=1,NP
C(I,NPJ)=B(I,J)
C
C SET TO PERFORM N ELIMINATION SWEEPS (I=1,N)
C
NP1=NP+1
NPK=NP+KP
DO 120 I=1,NP
IPI=I+1
C SEARCH FOR NEXT PIVOT ROW (I-TH PIVOT IS IN COL. I)
C
ATPE=0.
DO 40 J=I,NP
IF (ABS(C(J,I))-ATPE) 40,30,30
30 ATPE=ABS(C(J,I))
IPIV=J
40 CONTINUE
C OPERATE ON THE PIVOT ROW
C
IF (ATPE) 210,210,50
50 DO 60 J=IPI,NPK
60 PIV(J)=C(IPIV,J)/C(IPIV,I)
C PERFORM ELIMINATIONS BELOW THE DIAGONAL (COL. I)
C
IFROM=NP
ITO=NP
70 IF (IFROM-IPIV) 80,100,80
80 RM=-C(IFROM,I)
DO 90 J=IPI,NPK
90 C(ITO,J)=C(IFROM,J)+RM*PIV(J)
ITO=ITO-1
100 IFROM=IFROM-1
IF (IFROM-I) 110,70,70
C PUT THE I-TH PIVOT ROW IN THE VACATED ROW I
C
110 DO 120 J=IPI,NPK
120 C(I,J)=PIV(J)
C NOW DO THE BACK SOLUTION
C
I=NP
130 IPI=I

```

```

MTXEQ046
MTXEQ047
MTXEQ048
MTXEQ049
MTXEQ050
MTXEQ051
MTXEQ052
MTXEQ053
MTXEQ054
MTXEQ055
MTXEQ056
MTXEQ057
MTXEQ058
MTXEQ059
MTXEQ060
MTXEQ061
MTXEQ062
MTXEQ063
MTXEQ064
MTXEQ065
MTXEQ066
MTXEQ067
MTXEQ068
MTXEQ069
MTXEQ070
MTXEQ071
MTXEQ072
MTXEQ073
MTXEQ074
MTXEQ075
MTXEQ076
MTXEQ077
MTXEQ078
MTXEQ079
MTXEQ080
MTXEQ081
MTXEQ082
MTXEQ083
MTXEQ084
MTXEQ085
MTXEQ086
MTXEQ087
MTXEQ088
MTXEQ089
MTXEQ090
MTXEQ091

```

```

I=I-1
IF (I) 160,160,140
DO 150 J=NP1,NPK
DO 150 L=IP1,NP
C(I,J)=C(I,J)-C(I,L)*C(L,J)
GO TO 130
C
C MOVE THE SOLUTION TO ARRAY X(I,J)
C
C 160 DO 170 J=1,KP
NPJ=NP+J
DO 170 I=1,NP
170 X(I,J)=C(I,NPJ)
180 RETURN
C
190 WRITE (6,1000) NP,KP
RETURN
210 WRITE (6,1001)
RETURN
1000 FORMAT(3HON=112,5H K=112,35H ARE INCORRE T FOR SUBROUTINE MTXEQ)
1001 FORMAT (37HODET(A)=0 IN CALL TO SUBROUTINE MTXEQ)
END
MTXEQ092
MTXEQ093
MTXEQ094
MTXEQ095
MTXEQ096
MTXEQ097
MTXEQ098
MTXEQ099
MTXEQ100
MTXEQ101
MTXEQ102
MTXEQ103
MTXEQ104
MTXEQ105
MTXEQ106
MTXEQ107
MTXEQ109
MTXEQ111
MTXEQ112
MTXEQ113
MTXEQ114

```

```

$IBFTC PLSQ. DECK
SUBROUTINE PLSQ(X,Y,N,K,C,LIST,EMAX,ERMS,EMEQ)
C
C PLSQ POLYNOMIAL LEAST SQUARE CURVE FIT
C
C PLSQ WILL FIT A GIVEN SET OF DATA TO A
C POLYNOMIAL OF DEGREE K OF THE FORM...
C  $Y=C(K+1)+C(K)*X+C(K-1)*X**2+...+C(2)*X**(K-1)+C(1)*X**K$ 
C
C PLSQ THEN COMPUTES THE MAXIMUM ERROR AND ROOT
C MEAN SQUARE ERROR OBTAINED BY USING THE C
C COEFFICIENTS TO RE-COMPUTE Y FROM X
C
C USAGE...
C
C DIMENSION X(N), Y(N), C(L)
C WHERE L IS K+1
C CALL PLSQ(X,Y,N,K,C,LIST,EMAX,ERMS,EMEQ)
C
C WHERE,
C X IS THE ARRAY OF N INDEPENDENT VARIABLES
C Y IS THE ARRAY OF N DEPENDENT VARIABLES
C N IS THE NUMBER OF INDEPENDENT(DEPENDENT)
C VARIABLES
C K IS THE DEGREE OF THE LEAST SQUARES POLYNOMIAL
C C IS THE ARRAY OF THE COEFFICIENTS,HIGH ORDER
C TO LOW ORDER, OF THE LEAST SQUARES POLYNOMIAL
C LIST =0 SUPPRESSES THE ERROR ANALYSIS OUTPUT
C =1 GIVES THE ERROR ANALYSIS OUTPUT
C
C EMAX IS THE MAXIMUM ABSOLUTE ERROR OBTAINED
C BY USING THE COMPUTED C COEFFICIENTS TO
C APPROXIMATE THE DEPENDENT VARIABLE
C
C ERMS IS THE ROOT MEAN SQUARE ERROR OBTAINED
C BY USING THE COMPUTED C COEFFICIENTS TO
C APPROXIMATE THE DEPENDENT VARIABLE
C
C
C

```

PLSQ0001  
 PLSQ0002  
 PLSQ0003  
 PLSQ0004  
 PLSQ0005  
 PLSQ0006  
 PLSQ0007  
 PLSQ0008  
 PLSQ0009  
 PLSQ0010  
 PLSQ0011  
 PLSQ0012  
 PLSQ0013  
 PLSQ0014  
 PLSQ0015  
 PLSQ0016  
 PLSQ0017  
 PLSQ0018  
 PLSQ0019  
 PLSQ0020  
 PLSQ0021  
 PLSQ0022  
 PLSQ0023  
 PLSQ0024  
 PLSQ0025  
 PLSQ0026  
 PLSQ0027  
 PLSQ0028  
 PLSQ0029  
 PLSQ0030  
 PLSQ0031  
 PLSQ0032  
 PLSQ0033  
 PLSQ0034  
 PLSQ0035  
 PLSQ0036  
 PLSQ0037  
 PLSQ0038  
 PLSQ0039  
 PLSQ0040  
 PLSQ0041  
 PLSQ0042  
 PLSQ0043  
 PLSQ0044  
 PLSQ0045

```

C      EMEQ IS THE MAXIMUM DEVIATION FROM UNITY
C      IN THE LINEAR SYSTEM CHECK SOLUTION
C
C      PLSO CALLS SUBROUTINE MTXEQ
C
C      PLSO USES 1309 CELLS OF BLANK COMMON
C
C      COMMON   MTXEQT(664), CF, DIF, I, J, JC, JK,
C      *        L, LL, LU, M, SUM, XI, XM(576),
C      *        XMAX, XMIN, XP, YC, YM(48)
C      DIMENSION X(N), Y(N), C(24),
C      *        XDP(48), XYDP(24)
C      EQUIVALENCE (MTXEQT(1),XDP(1)), (MTXEQT(97),XYDP(1))
C      LOGICAL LIST
C      DOUBLE PRECISION CF, XDP, XI, XMAX, XMIN, XP, XYDP
C      DATA KMAX/ 23/..
C
C      CHECK K AND N FOR PROPER RANGE
C
C      IF (K .GT. KMAX .OR. N .LE. K .OR. K .LE. 0) GO TO 200
C      L=K+1
C
C      FIND MINIMUM AND MAXIMUM VALUES FOR X
C
C      XMIN=X(1)
C      XMAX=X(1)
C      DO 10 I=2,N
C      XMIN=AMIN(XMIN,X(I))
C      XMAX=AMAX(XMAX,X(I))
C
C      ZERO DOUBLE PRECISION ARRAYS FOR SUMMING
C
C      M=2*K+1
C      DO 20 I=1,M
C      XDP(I)=0.0D+00
C      DO 25 I=1,L
C      XYDP(I)=0.0D+00
C
C      TRANSFORM RANGE OF X TO (-1,+1) AND
C      COMPUTE SUMS OF POWERS OF X AND SUMS
C      OF Y TIMES POWERS OF X
C
C      LL=K+2
C      LU=2*K+1

```

PLSQ0046  
 PLSQ0047  
 PLSQ0048  
 PLSQ0049

PLSQ0051  
 PLSQ0052  
 PLSQ0053  
 PLSQ0054  
 PLSQ0055  
 PLSQ0056  
 PLSQ0057  
 PLSQ0058  
 PLSQ0059

PLSQ0060  
 PLSQ0061  
 PLSQ0062  
 PLSQ0063  
 PLSQ0064  
 PLSQ0065

PLSQ0066  
 PLSQ0067  
 PLSQ0068  
 PLSQ0069  
 PLSQ0070  
 PLSQ0071

PLSQ0072  
 PLSQ0073  
 PLSQ0074  
 PLSQ0075  
 PLSQ0076  
 PLSQ0077

PLSQ0078  
 PLSQ0079  
 PLSQ0080  
 PLSQ0081  
 PLSQ0082  
 PLSQ0083

PLSQ0084  
 PLSQ0085  
 PLSQ0086  
 PLSQ0087  
 PLSQ0088  
 PLSQ0089

PLSQ0090  
 PLSQ0091

```

DO 40 I=1,N
XP=1.0D+00
XI=2.0D+00*(X(I)-XMIN)/(XMAX-XMIN)-1.0D+00
DO 30 J=1,L
XDP(J)=XDP(J)+XP
XYDP(J)=XYDP(J)+XP*Y(I)
XP=XP*XI
30 DO 40 J=LL,LU
XDP(J)=XDP(J)+XP
XP=XP*XI
40
C
C STORE ABOVE COMPUTED SUMS IN ARRAY XM
C AND COMPUTE ROW SUMS FOR CHECK SOLUTION
C
DO 50 I=1,L
LL=I+L
YM(LL)=0.0
LU=(I-1)*L
JK=I-1
DO 50 J=1,L
JK=JK+1
JC=LU+J
XM(JC)=XDP(JK)
YM(LL)=YM(LL)+XM(JC)
50 DO 60 I=1,L
YM(I)=XYDP(I)
60
C
C SOLVE THE SYSTEM XM*C=YM
C
C CALL MTXEQ(XM,YM,LM,2)
C
C REORDER AND MOVE SOLUTION TO C AND FIND
C MAXIMUM ERROR IN CHECK SOLUTION
C
EMEQ=0.0
DO 70 I=1,L
JK=K-I+2
C(JK)=YM(I)
JC=I+L
70 EMEQ=AMAX1(EMEQ,ABS(YM(JC)-1.0))
C
C ADJUST COEFFICIENTS FOR ORIGINAL RANGE
C OF X
C
CF=(XMAX-XMIN)/2.0D+00
DO 80 I=1,K

```

```

PLSQ0072
PLSQ0093
PLSQ0094
PLSQ0095
PLSQ0096
PLSQ0097
PLSQ0098
PLSQ0099
PLSQ0100
PLSQ0101
PLSQ0102
PLSQ0103
PLSQ0104
PLSQ0105
PLSQ0106
PLSQ0107
PLSQ0108
PLSQ0109
PLSQ0110
PLSQ0111
PLSQ0112
PLSQ0113
PLSQ0114
PLSQ0115
PLSQ0116
PLSQ0117
PLSQ0118
PLSQ0119
PLSQ0120
PLSQ0121
PLSQ0122
PLSQ0123
PLSQ0124
PLSQ0125
PLSQ0126
PLSQ0127
PLSQ0128
PLSQ0129
PLSQ0130
PLSQ0131
PLSQ0132
PLSQ0133
PLSQ0134
PLSQ0135
PLSQ0136
PLSQ0137

```

```

80      DO 80 J=1,I
        C(J)=C(J)/CF
        CF=(XMAX+XMIN)/2.0D+00
        DO 90 I=1,K
            M=L-I+1
            DO 90 J=2,M
                C(J)=-CF*C(J-1)+C(J)
        C
        C      INITIATE PRINT OF ERROR ANALYSIS IF LIST .NE. 0
        C      IF (LIST) WRITE (6,1001)
        C
        C      COMPUTE MAXIMUM AND ROOT MEAN SQUARE ERRORS
        C      AND OUTPUT ERROR ANALYSIS IF LIST .NE. 0
        C
        C      EMAX=0.0
        C      SUM=0.0
        DO 130 I=1,N
            YC=C(I)
            DO 100 J=1,K
                YC=YC*X(I)+C(J+1)
            DIF=YC-Y(I)
            IF (.NOT. LIST) GO TO 120
            IF (I .GT. L) GO TO 110
            WRITE (6,1002) I, X(I), Y(I), YC, DIF, C(I)
            GO TO 120
        110 WRITE (6,1002) I, X(I), Y(I), YC, DIF
        120 EMAX=AMAX1(EMAX,ABS(DIF))
        130 SUM=SUM+DIF**2
        ERMS=SQRT(SUM/FLOAT(N))
        IF (LIST) WRITE (6,1003) FMAX, ERMS, EMEG
        RETURN
        C
        C      GIVE ERROR MESSAGE AND RETURNS
        C
        200 WRITE (6,1000) N,K
        RETURN
        1000 FORMAT (3HON=,I12,3H K=,I12,29HINCORRECT FOR SUBROUTINE PLSQ)
        1001 FORMAT (1H1,20X,32HPL50 POLYNOMIAL LEAST SQUARE
            *24HCURVE FIT ERROR ANALYSIS//
            *6H0 I,11X,9HX - GIVEN,11X,9HY - GIVEN,11X,
            *10HY - FITTED,12X,5HEMFO,16X,4HR(I)//)
        1002 FORMAT (1X,15,FX,5(1PF)4.6,6X))
        1003 FORMAT (1H0,9X,5HEMAX=,1PF15.6,9X,5HERMS=,F15.6,
            *OX,5HEMFO=,F15.6)
        END
        C
        C      $DATA
        C      $NAM $
        C      $EOF
    
```

PLSQ0138  
 PLSQ0139  
 PLSQ0140  
 PLSQ0141  
 PLSQ0142  
 PLSQ0143  
 PLSQ0144  
 PLSQ0145  
 PLSQ0146  
 PLSQ0147  
 PLSQ0148  
 PLSQ0149  
 PLSQ0150  
 PLSQ0151  
 PLSQ0152  
 PLSQ0153  
 PLSQ0154  
 PLSQ0155  
 PLSQ0156  
 PLSQ0157  
 PLSQ0158  
 PLSQ0159  
 PLSQ0160  
 PLSQ0161  
 PLSQ0162  
 PLSQ0163  
 PLSQ0164  
 PLSQ0165  
 PLSQ0166  
 PLSQ0167  
 PLSQ0168  
 PLSQ0169  
 PLSQ0170  
 PLSQ0173  
 PLSQ0174  
 PLSQ0176  
 PLSQ0177  
 PLSQ0178  
 PLSQ0179  
 PLSQ0180  
 PLSQ0181  
 PLSQ0182  
 PLSQ0183  
 PLSQ0184  
 PLSQ0185

EXPLANATION OF  
SUBROUTINE MTXEQ

MTXEQ, Matrix Equation Solver, solves the system of linear equations expressed by the matrix equation  $AX = B$ , using single precision floating arithmetic.

Control:

To solve the matrix equation,

$$AX = B$$

the following calling sequence is used:

```
DIMENSION A(N,N), X(N,K), B(N,K)
CALL MTXEQ(A,X,B,N,K)
```

where

- A - is the N by N coefficient matrix. The A matrix is not destroyed.
- X - will be the N by K solution matrix.
- B - is the N by K right-hand-side matrix. The B matrix is not destroyed.
- N - is the number of equations, i.e., rows in A, X and B.  
( $1 \leq N \leq 24$ )
- K - is the number of solution, i.e., columns in X and B.  
( $K > 0$  and  $(N+K) \leq 26$ )

Other Programming Information:

1. Other subprograms used - None.

2. Error conditions -

- a. The following ranges of N and K are allowed:

$$(1 \leq N \leq 24)$$

$$K > 0 \text{ and } (N+K) \leq 26$$

When violations of the above ranges are detected by MTXEQ, a message is written and FXEM is called. The upper limits on N and (N+K) may be altered by changing a DIMENSION and a DATA statement.

- b. If the A matrix has  $\text{DET}(A) = 0$ , a message is written and FXEM is called.

- c. Common usage -

MTXEQ uses 664 cells of blank common.

Method:

The matrix  $C = [A, B]$  is formed in blank common. Subsequent operations are performed on the C matrix, thus preserving the A and B matrices. Elementary row operations are performed to eliminate elements below the main diagonal of the augmented matrix C. To reduce the propagation of round-off error, the i-th pivot element is chosen to be an element having maximum magnitude in the i-th sub-column. Finally, a back solution gives the desired matrix, X. The number of floating point arithmetic operations required using this method is of the order of  $2/3 (N^3 + 3KN^2)$ .

EXPLANATION OF  
SUBROUTINE PLSQ

PLSQ, Polynomial Least Square Curve Fit, will fit a given set of data to a polynomial of degree K of the form:

$$Y = C_1 X^k + C_2 X^{k-1} + \dots + C_k X + C_{k+1}$$

An error analysis of the fit is optionally given.

Control:

DIMENSION X(N), Y(N), C(L)

where L is K+1

CALL PLSQ(X,Y,N,K,C,LIST,EMAX,ERMS,EMEQ)

where

X is the array of N independent variables.

Y is the array of dependent variables.

N is the number of independent (dependent) variables.

K is the degree of the least squares polynomial.

C is the array of the coefficients, high order to low order, of the least squares polynomial.

LIST = 0 suppresses the error analysis output.

= 1 gives the error analysis output.

EMAX is the maximum absolute error obtained by using the computed C coefficients to approximate the dependent variable.

ERMS is the root mean square error obtained by using the computed C coefficients to approximate the dependent variable.

EMEQ is the maximum deviation from unity in the linear system check solution.

Other Programming Information:

1. Other subroutines used:

PLSQ calls MTXEQ to solve the normal equations and FXEM for return to the system on error conditions.

2. Error conditions:

PLSQ checks for the following errors:

- a.  $K > 23$
- b.  $N \leq K$
- c.  $K \leq 0$

Upon detecting an error a pertinent message is given and FXEM is called for error tracing and return to the system.

3. Common usage:

PLSQ uses 1309 cells of blank common.

Method:

PLSQ fits a set of observed data,  $[x_i, y_i]$ , with a polynomial of the form:

$$Y = C_1 X^k + C_2 X^{k-1} + \dots + C_k X + C_{k+1}$$

by solving the normal equations for the  $C_i$ 's. A transformation of the range of X to (-1,1) gives a partial decoupling of the normal equations which improves the accuracy of the solution. Double precision arithmetic is performed at critical points in the computation.

UNCLASSIFIED

Security Classification

DOCUMENT CONTROL DATA - R & D

(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)

1. ORIGINATING ACTIVITY (Corporate author) Deputy for Engineering Aeronautical Systems Division Wright-Patterson Air Force Base, Ohio	2a. REPORT SECURITY CLASSIFICATION UNCLASSIFIED
	2b. GROUP

3. REPORT TITLE  
COMPUTER PROGRAM FOR REDUCING STATIC PROPELLER TEST DATA

4. DESCRIPTIVE NOTES (Type of report and inclusive dates)

5. AUTHOR(S) (First name, middle initial, last name)  
Cafarelli, Gerald T.  
Chopin, Matthew H.

6. REPORT DATE June 1968	7a. TOTAL NO. OF PAGES 41	7b. NO. OF REFS 0
-----------------------------	------------------------------	----------------------

8a. CONTRACT OR GRANT NO.  b. PROJECT NO. 478A  c.  d.	9a. ORIGINATOR'S REPORT NUMBER(S) ASD-TR-68-19
	9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report)

10. DISTRIBUTION STATEMENT  
This document has been approved for public release and sale; its distribution is unlimited.

11. SUPPLEMENTARY NOTES	12. SPONSORING MILITARY ACTIVITY Deputy for Engineering Wright-Patterson Air Force Base, Ohio 45433
-------------------------	--

13. ABSTRACT

A computer program using a curve-fit technique was developed to reduce performance data obtained from static tests of aircraft propellers. The entire program is written in Fortran IV language for use on the IBM 7094 computer, located at Wright-Patterson AFB, Ohio.

The program accepts static whirl rig test data (ie, raw RPM, horsepower, and thrust data) obtained at a fixed blade angle and reduces it into pertinent propeller relationships. The program first reduces the test data into various coefficients and computes the propeller tip Mach number. A curve fit technique then fits running curves through the test thrust and horsepower data points at the test tip Mach numbers. Intermediate horsepower and thrust values are determined from the fitted curves at selected Mach number increments, and all coefficients are recomputed. This results in a presentation of the reduced data in two forms, coefficients computed from the actual test data and coefficients obtained at specific constant Mach number increments from the fitted curves. The data is presented in tabular printout form. This is a general program and is written so that the order of the curve fit, the Mach number increment, the number of test data points and the Mach number range can be varied.

The entire program deck and all nonstandard subroutines are included. Detail instructions are provided which should allow the program to be used by technicians or students who are familiar with Fortran IV language.

UNCLASSIFIED

Security Classification

14	KEY WORDS	LINK A		LINK B		LINK C	
		ROLE	WT	ROLE	WT	ROLE	WT
	Computer Program Aircraft Propeller Static Tests Data Reduction						

UNCLASSIFIED

Security Classification