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SURFACE SCATTER STUDY

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The University of Arizona
Tucson, Arizona 85721

February 1974

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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) The angular spectrum of plane waves approach to scalar diffraction theory has been extended to include scattering. An instrument was designed and constructed to measure scattered light distributions from aluminized glass surfaces. Diffuse reflectance measurements were made on samples having varying degrees of surface finish. Results of these measurements as a function of angle of incidence and wavelength are reported.		

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FOREWORD

This is the final report for the surface scatter study program undertaken by the Optical Sciences Center, University of Arizona, Tucson, Arizona. The work was performed under Air Force Contract F04701-72-C-0181. The program was carried out under the auspices of the Air Force Space and Missile Systems Organization.

The principal investigator for the Optical Sciences Center was Roland V. Shack. The project engineer and co-investigator was Michael A. DeBell.

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SUMMARY

Scattering theory is developed as an extension of the angular spectrum of plane waves approach to diffraction. Expressions useful in the evaluation of scatter are obtained through the introduction of random perturbations in the pupil function. When the surface statistics are known the expected value of the transfer function can be found. The particular case of a surface with Gaussian statistics is then treated and expressions are derived that predict the scattered flux distribution for a surface with such statistics.

Apparatus is described that is capable of measuring the scattered flux distribution in the range of two to ninety degrees from the specular direction. Using this apparatus the distribution of light scattered by a variety of plane mirror surfaces as a function of roughness, angle of incidence, and wavelength is measured experimentally.

The intensity of the scattered light is shown to vary with the inverse square of the wavelength when the total scattered flux is small compared to the specularly reflected flux. This theory is consistent with the data.

A numerical integration of the scattered light distribution yields the total scattered flux. A relationship between the total scattered flux and the surface roughness is derived. The theoretical results and the estimated roughness were found to be of the same order of magnitude.

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INTRODUCTION

When light is incident upon a surface the reflected flux can be described by considering two components, the specular component and the diffuse component. The specular component is reflected in the plane of incidence at an angle equal to the angle of incidence and is coherent with the incident beam. Light scattered away from the specular direction is said to be diffusely reflected. Diffusely reflected light is a diffraction phenomena and its distribution is attributable to the surface properties of the reflector. Properties that can be used to characterize such surfaces are roughness, autocorrelation length, and the statistical distributions of these two parameters.

Two special cases are of interest: the perfect reflector and the perfectly diffuse, or Lambertian, reflector. A perfect reflector alters the direction and not the distribution of the incident light. A plane surface that is perfectly diffuse obeys Lambert's cosine law, $I(\theta) = I_0 \cos \theta$, where $I(\theta)$ is the radiant intensity at an angle θ to the surface and I_0 is the radiant intensity measured normal to the surface. Theories put forth should reduce to these special cases in the limit and it is in this regard that we mention them.

Previous Theoretical Work

Scattering from surfaces is a diffraction phenomena and as such has been treated as a boundary value problem where Maxwell's equations are applied. Two categories exist in this general body of theory: that in which scattering is treated for a specific model of the surface and that in which the surface is statistically described by a distribution of heights and slopes about a mean surface.

Examples of theoretical approaches, for a specific surface model, have been proposed by Beckman and Spizzichino (1963), Berreman (1967), Hunderi and Beaglehole (1970), and Twersky (1957). Twersky and Berreman have considered surface models for which it is possible to obtain exact solutions for the electromagnetic field. In these cases the Kirchhoff approximations are applied to the boundary conditions in order to evaluate the Helmholtz integral. Their models consist of randomly distributed hemispherical irregularities on an otherwise smooth surface. Twersky arrived at complete solutions by considering only perfect conductors while Berreman made first-order calculations applicable to surfaces of any conductivity. Hunderi and Beaglehole adopted an approach that yields the reflectance of a surface model consisting of spheres located just above a smooth metal surface. Although this model of a scattering surface is not as realistic as that of Berreman, it can be solved exactly for a metal with any conductivity.

Theory relating to periodically rough surfaces is discussed by Beckmann and Spizzichino. They use the Kirchhoff method of approximating the boundary conditions on a perfectly conducting periodic surface and then find the

corresponding field by using the Helmholtz integral. Making additional approximations they deal with the surfaces that are not perfect conductors.

Perhaps the best known theory dealing with statistical scatter from surfaces having roughness distributions is that of Davies (1954). His theory considers only the phase modulation of the incident light by the height variations along the surface. The specular and scattered light are found by summing the radiation from Huygens wavelets at the surface. The height variation is then assumed to be normally distributed about its mean with an rms deviation of σ . The scattering theory then predicts that the ratio of the specular reflectivity of a rough surface to that of a smooth surface varies as

$$R/R_o = e^{-(4\pi\sigma/\lambda)^2}$$

and makes similar predictions about the angular distribution of scattered light. The approximations made in this development limit the theory so that it is valid only if the typical distance separating surface structures is on the order of a wavelength or larger. This theory of Davies was extended by Bennett and Porteus (1961) and by Porteus (1963). Work by Beckmann and Spizzichino (1963) also extended the statistical approach of Davies.

Previous Experimental Investigations

Lord Rayleigh (1901) was one of the earliest investigators of scattered light. He noted the effect of poorly polished surfaces on optical performance. His work examined the effects caused by surface roughness, wavelength, and angle of incidence on the reflected beam. The variation in brightness with angle of observation for various surfaces was studied by Jones (1922). He used what he termed a "goniophotometer"; a device having means of directing a collimated beam on a sample surface and a photometer arm arranged to measure the brightness of the surface. The angle of illumination could be varied and the angle of viewing held constant or vice versa. Slater (1935) improved on this goniophotometer and was able to provide quantitized measurements in either transmission or reflection.

Photometric measurements by Hunter (1940) employed a barrier layer photocell to measure the diffuse reflectance of a broad range of samples. His work included a detailed report on sources of error. Hunter used aluminized "perfect mirrors" as reference standards. Some of the first work where scattering itself was a primary concern was reported by Aughey and Baum (1954). The scattering profiles they measured led them to direct conclusions about the physical properties of the scatterer.

The scattering theory of Davies (1954) was expanded and experimentally investigated by Bennett and Porteus (1961). From this work and work that followed shortly thereafter (Bennett, 1963 and Porteus, 1963) the reflectance properties of samples with a measured surface roughness were directly compared to theory. In their work Bennett and Porteus reported good agreement between the measurements on their samples and the theory they had

developed. The thrust of these measurements led to investigations at the Optical Sciences Center by D. McKenney, L. Mott, G. Orme and M. DeBell.

Semplak (1965) and Blazey (1967) along with others (see annotated bibliography) used lasers as a light source for their scattering measurements. Blazey, using a goniometric scanning device reported results in good agreement with the Beckmann theory. His measurements were made on multi-layer dielectric coatings typical of those used in the laser industry.

Orme (1972), using a clever diffraction technique, was able to explore the zeros of a single slit diffraction pattern and evaluate scatter to within one-third of a degree of the specular beam. Orme made wide angle measurements using a goniometric device. Using this technique he was able to explore all but the limited region of, 1.5° to 5° , from the specular direction, in the plane of incidence. His work, as had the work of Aughey and Baum, pointed to the possibility that scatter was caused by two different mechanisms. The inability of Orme to make measurements in the 1.5° to 5° range and the questions raised concerning multiple scattering phenomena have provided the stimulation to undertake the work reported here.

II

THEORY

The Angular Spectrum of Plane Waves Approach to Diffraction Theory

The aim of this section is to cast diffraction theory in a format that will make it useful in examining the effects of scattering. We will distinguish scatter from diffraction by defining scatter as "diffraction from a surface or medium whose properties are statistical in nature." Our approach will be to consider a disturbance in an initial plane, P_1 , and to derive the necessary theory that will allow us to predict the field in a subsequent plane, P_2 .

Let the complex amplitude distribution at the plane P_1 be $U(x,y,0)$ and consider the geometry shown in Fig. 1 below. The scalar disturbance on P_1

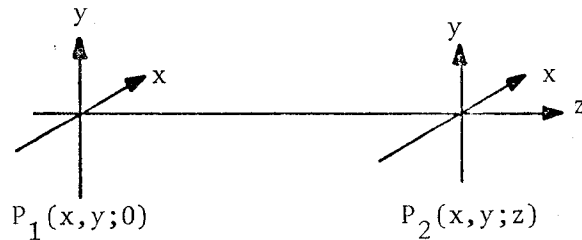


Fig. 1. Geometry of planes P_1 and P_2 .

will be considered the only radiation contributing to the field at P_2 . It will be assumed that the light propagating from P_1 to P_2 obeys the Helmholtz equation. Further we will assume that the Fourier transform of the scalar field $U(x,y,0)$ exists. (We can make this assumption since as Goodman points out, "physical possibility is a valid and sufficient condition for the existence of a transform.")

We can now define the Fourier transform relationships that exist for planes P_1 and P_2 .

$$A_o(\xi, \eta; 0)^{\dagger} = \iint_{-\infty}^{\infty} U_o(x, y; 0) e^{-i2\pi(x\xi + y\eta)} dx dy \quad (1)$$

$$A(\xi, \eta; z) = \iint_{-\infty}^{\infty} U(x, y; z) e^{-i2\pi(x\xi + y\eta)} dx dy \quad (2)$$

$$U_o(x, y; 0) = \iint_{-\infty}^{\infty} A_o(\xi, \eta; 0) e^{i2\pi(\xi x + \eta y)} d\xi d\eta \quad (3)$$

$$U(x, y; z) = \iint_{-\infty}^{\infty} A(\xi, \eta; z) e^{i2\pi(\xi x + \eta y)} d\xi d\eta. \quad (4)$$

(+z has a parametric relationship since it is a function of the observation plane.)

Notice that the integrand in Eqs. (3) and (4) has a form similar to that of a plane wave. The equation for a unit amplitude plane wave is

$$e^{i\vec{k} \cdot \vec{r}}.$$

Here $\vec{k}$ is the propagation vector and $\vec{r}$ is the position vector (see Fig. 2).

$$\vec{k} = \frac{2\pi}{\lambda} (\alpha \bar{x} + \beta \bar{y} + \gamma \bar{z}) \quad (5)$$

$$\vec{r} = x\bar{x} + y\bar{y} + z\bar{z} \quad (6)$$

where

$\bar{x}$, $\bar{y}$ and $\bar{z}$ are unit vectors, and,

α , β and γ are direction cosines

$$\alpha^2 + \beta^2 + \gamma^2 = 1.$$

The unit amplitude plane wave can then be rewritten as:

$$e^{i\vec{k} \cdot \vec{r}} = e^{i(\alpha x + \beta y + \gamma z)2\pi/\lambda}. \quad (7)$$

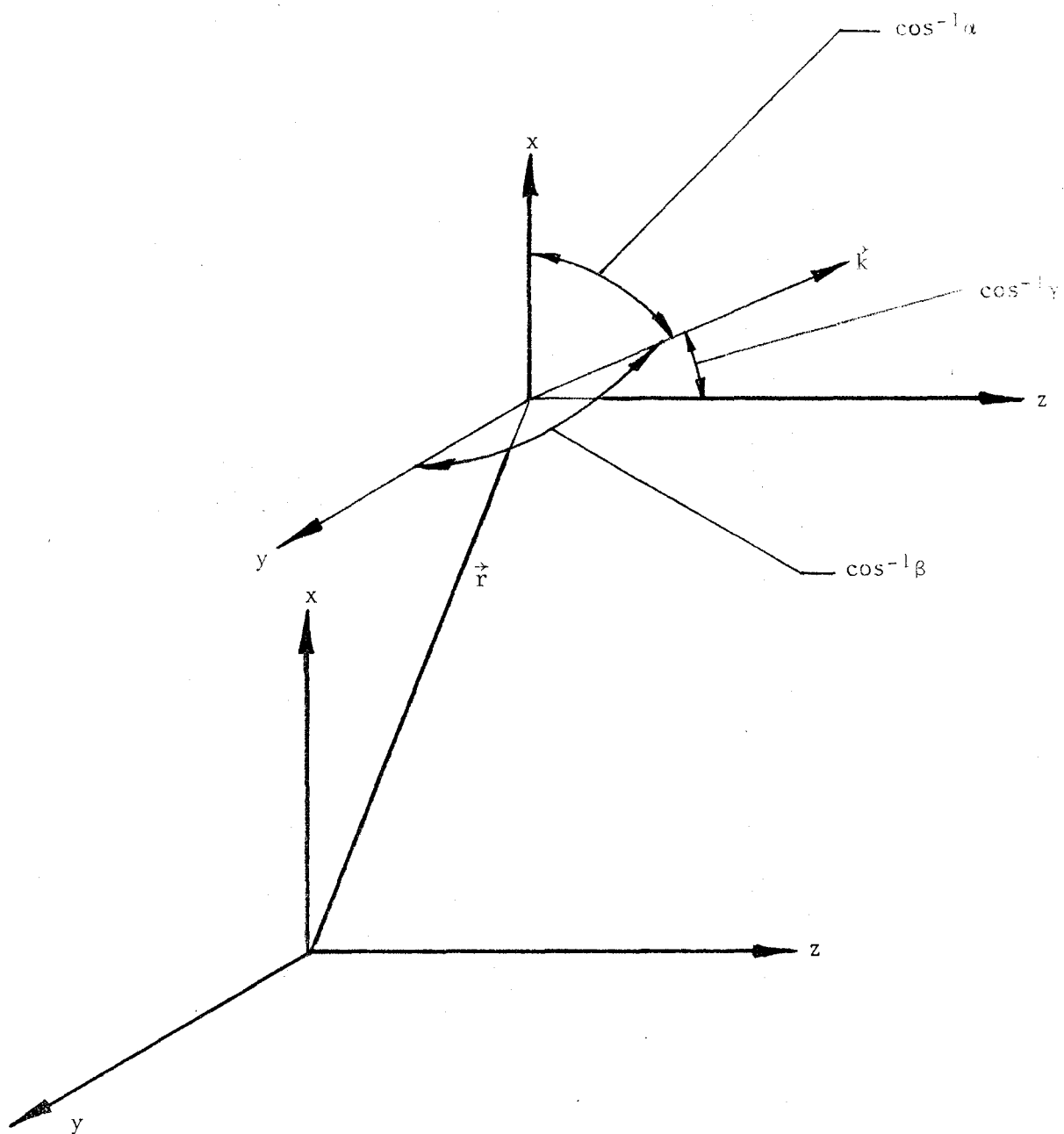


Fig. 2. Relationship of the propagation vector to its direction cosines.

Across the plane $z = 0$, the integrand of Eq. (3) can be thought of as the intersection of that plane with a plane wave traveling with direction cosines:

$$\alpha = \lambda \xi, \quad \beta = \lambda \eta \quad \text{and} \quad \gamma = \sqrt{1 - (\lambda \xi)^2 - (\lambda \eta)^2}. \quad (8)$$

It now becomes convenient to scale the variables x , y , and z to the wavelength, λ . These new variables are denoted $\hat{x}$, $\hat{y}$, and $\hat{z}$;

$$\hat{x} = \frac{x}{\lambda}; \quad \hat{y} = \frac{y}{\lambda}; \quad \hat{z} = \frac{z}{\lambda}. \quad (9)$$

With this notation, Eqs. (1) - (4) can be rewritten as:

$$A_0(\alpha, \beta; 0) = \iint_{-\infty}^{\infty} U_0(\hat{x}, \hat{y}; 0) e^{-i2\pi(\alpha\hat{x} + \beta\hat{y})} d\hat{x}d\hat{y} \quad (10)$$

$$A(\alpha, \beta; \hat{z}) = \iint_{-\infty}^{\infty} U(\hat{x}, \hat{y}; \hat{z}) e^{-i2\pi(\alpha\hat{x} + \beta\hat{y})} d\hat{x}d\hat{y} \quad (11)$$

$$U_0(\hat{x}, \hat{y}; 0) = \iint_{-\infty}^{\infty} A_0(\alpha, \beta; 0) e^{i2\pi(\alpha\hat{x} + \beta\hat{y})} d\alpha d\beta \quad (12)$$

$$U(\hat{x}, \hat{y}; \hat{z}) = \iint_{-\infty}^{\infty} A(\alpha, \beta; \hat{z}) e^{i2\pi(\alpha\hat{x} + \beta\hat{y})} d\alpha d\beta. \quad (13)$$

Here we have cast the integrand into the form of plane waves modified by Fourier coefficients.

The disturbances in planes P_1 and P_2 must also satisfy the Helmholtz equation:

$$(\nabla^2 + k^2)U = 0. \quad (14)$$

Here,

$$k = 2\pi/\lambda$$

$$\nabla^2 = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}.$$

In the scaled coordinate system, $\hat{\nabla}^2 = \lambda^2 \nabla^2$, and $\hat{k}^2 = \lambda^2 k^2 = (2\pi)^2$. With these substitutions, Eq. (14) becomes:

$$(\hat{\nabla}^2 + (2\pi)^2)U = 0. \quad (15)$$

If we apply Eq. (15) to Eq. (13) we get:

$$\iint_{-\infty}^{\infty} (\hat{\nabla}^2 + (2\pi)^2) A(\alpha, \beta; \hat{z}) e^{i2\pi(\alpha\hat{x} + \beta\hat{y})} d\alpha d\beta = 0 \quad (16)$$

or

$$\begin{aligned} \iint_{-\infty}^{\infty} & \left[\frac{\partial^2}{\partial \hat{z}^2} A(\alpha, \beta; \hat{z}) e^{i2\pi(\alpha\hat{x} + \beta\hat{y})} + A(\alpha, \beta; \hat{z}) (i2\pi\alpha)^2 e^{i2\pi(\alpha\hat{x} + \beta\hat{y})} \right. \\ & + A(\alpha, \beta; \hat{z}) (i2\pi\beta)^2 e^{i2\pi(\alpha\hat{x} + \beta\hat{y})} \\ & \left. + 2\pi^2 A(\alpha, \beta; \hat{z}) e^{i2\pi(\alpha\hat{x} + \beta\hat{y})} \right] d\alpha d\beta = 0 \end{aligned} \quad (17)$$

hence,

$$\iint_{-\infty}^{\infty} \left[\frac{\partial^2}{\partial \hat{z}^2} A(\alpha, \beta; \hat{z}) + 4\pi^2 A(\alpha, \beta; \hat{z}) (1 - \alpha^2 - \beta^2) \right] e^{i2\pi(\alpha\hat{x} + \beta\hat{y})} d\alpha d\beta = 0. \quad (18)$$

The Fourier transform of the function in brackets is zero so the function itself must be identically zero. Thus we can write:

$$\frac{\partial^2}{\partial \hat{z}} A(\alpha, \beta; \hat{z}) + 4\pi^2 \gamma^2 A(\alpha, \beta; \hat{z}) = 0, \quad (19)$$

since $\gamma^2 = (1 - \alpha^2 - \beta^2)$. This equation has a solution of the form:

$$A(\alpha, \beta; \hat{z}) = A_0(\alpha, \beta; 0) e^{i2\pi\gamma\hat{z}}. \quad (20)$$

Equation (2) then relates the Fourier transforms of the scalar fields in planes P_1 and P_2 . Indeed Eq. (20) can be rewritten in terms of a transfer function for free space, H ;

$$A(\alpha, \beta; \hat{z}) = A_0(\alpha, \beta; 0) H(\alpha, \beta; \hat{z}). \quad H(\alpha, \beta; \hat{z}) = e^{i2\pi\gamma\hat{z}} \quad (21)$$

We have thus far applied no restrictions on γ and two regions of interest are apparent; that for real values of γ and that for imaginary values.

$$\begin{aligned} \gamma &= [1 - (\alpha^2 + \beta^2)]^{\frac{1}{2}} \quad \text{for } (\alpha^2 + \beta^2) \leq 1 \quad \gamma \text{ is } \underline{\text{real}} \\ &\quad \text{for } (\alpha^2 + \beta^2) > 1 \quad \gamma \text{ is } \underline{\text{imaginary}} \end{aligned} \quad (22)$$

Where γ is real the various plane wave components of the angular spectrum propagate in different directions and thus reach the "observation point" in plane P_2 with an associated phase factor

$$e^{i2\pi\gamma\hat{z}}.$$

When γ is imaginary the exponential

$$e^{i2\pi\gamma\hat{z}}$$

becomes a damping function of the form $e^{-K\hat{z}}$ where $K = 2\pi\sqrt{(\alpha^2 + \beta^2) - 1}$. Waves characterized by these values of γ are rapidly attenuated in the $\hat{z}$ direction.

The spread function associated with our transfer function is its Fourier transform.

$$F\{e^{i2\pi\gamma\hat{z}}\} = \left(i - \frac{1}{2\pi\hat{r}}\right) \left(\frac{e^{i2\pi\hat{r}}}{\hat{r}}\right) \left(\frac{\hat{z}}{\hat{r}}\right). \quad (23)$$

This spread function can be cast into the form:

$$a(\hat{r})e^{i\phi(\hat{r})} \quad \text{where} \quad \hat{r}^2 = \hat{x}^2 + \hat{y}^2 + \hat{z}^2. \quad (24)$$

The righthand side of Eq. (23) is straightforwardly separated into its real and imaginary components, $a + ib$;

$$-\underbrace{\left(\frac{\hat{z}}{\hat{r}}\right) \left(\frac{\sin 2\pi\hat{r}}{\hat{r}} + \frac{\cos 2\pi\hat{r}}{2\pi\hat{r}^2}\right)}_a + i \left[\underbrace{\left(\frac{\hat{z}}{\hat{r}}\right) \left(\frac{\cos 2\pi\hat{r}}{\hat{r}} - \frac{\sin 2\pi\hat{r}}{2\pi\hat{r}^2}\right)}_b \right]. \quad (25)$$

To represent this in phasor form we first recall the graphical representation shown in Fig. 3.

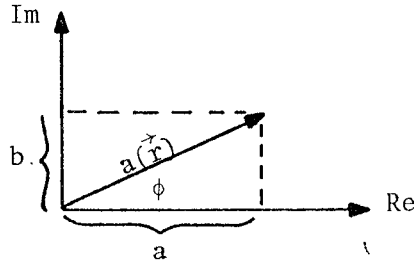


Fig. 3. Phasor representation.

$$a(\hat{r}) = \sqrt{a^2 + b^2} = \frac{\hat{z}}{2\pi\hat{r}^3} [1 + (2\pi\hat{r})^2]^{1/2} \quad (26)$$

The phase can be expressed as:

$$\phi = \arctan\left(\frac{b}{a}\right) = 2\pi\hat{r} - \arctan(2\pi\hat{r}). \quad (27)$$

Hence our spread function can be written as:

$$a(\hat{r})e^{i\phi(\hat{r})} = \frac{\hat{z}}{2\pi\hat{r}^3} (1 + (2\pi\hat{r})^2)^{1/2} e^{i(2\pi\hat{r} - \tan 2\pi\hat{r})}. \quad (28)$$

The measurements we wish to make have two characteristics that should be considered: measurements are made on a spherical surface and they are made at a distance from the aperture plane that is large compared to the size of the "initial disturbance" and the wavelength of the light that is propagating. Figure 4 shows the geometry that we wish to consider.

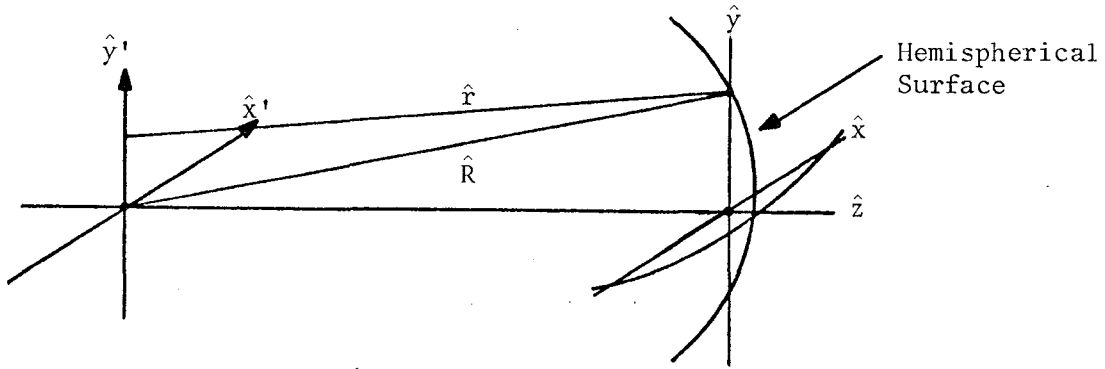


Fig. 4. Relationship of diffraction plane to observation surface.

The primed (') plane is the pupil plane and the spherical surface of radius $\hat{R}$ is where we wish to measure the resultant disturbance. In terms of what has been previously discussed we can write:

$$A(\alpha, \beta; \hat{z}) = A_0(\alpha, \beta; 0) e^{i2\pi\gamma\hat{z}}$$

$$U(\hat{x}, \hat{y}; \hat{z}) = F\{A(\alpha, \beta; \hat{z})\}$$

and can then conclude,

$$U(\hat{x}, \hat{y}; \hat{z}) = F\{A_0(\alpha, \beta; 0) e^{i2\pi\gamma\hat{z}}\}. \quad (29)$$

Now by the convolution theorem we have:

$$\begin{aligned}
 U(\hat{x}, \hat{y}; \hat{z}) &= F\{A_0(\alpha, \beta; 0)\} * F\{e^{i2\pi\gamma\hat{z}}\} \\
 &= U(\hat{x}', \hat{y}'; 0) * \left(i - \frac{1}{2\pi\hat{R}}\right) \frac{\hat{z}}{\hat{R}} \frac{e^{i2\pi\hat{R}}}{\hat{R}}.
 \end{aligned} \tag{30}$$

The convolution integral can then be taken "over" the pupil plane:

$$U(\hat{x}, \hat{y}; \hat{z}) = \iint_{-\infty}^{\infty} U(\hat{x}', \hat{y}'; 0) \left(i - \frac{1}{2\pi\hat{r}}\right) \left(\frac{\hat{z}}{\hat{r}}\right) \left(\frac{e^{i2\pi\hat{r}}}{\hat{r}}\right) d\hat{x}' d\hat{y}' \tag{31}$$

where

$$\hat{r} = \sqrt{(\hat{x} - \hat{x}')^2 + (\hat{y} - \hat{y}')^2 + \hat{z}^2}.$$

Now assume that we are many wavelengths away from the pupil plane. The term $1/2\pi\hat{r}$ then becomes insignificant in the integral compared to the other term. Equation 31 can then be approximated by:

$$U(\hat{x}, \hat{y}; \hat{z}) = i \iint_{-\infty}^{\infty} U(\hat{x}', \hat{y}'; 0) \left(\frac{\hat{z}}{\hat{r}}\right) \left(\frac{\hat{R}}{\hat{r}}\right)^2 \left(\frac{e^{i2\pi\hat{r}}}{\hat{R}}\right) d\hat{x}' d\hat{y}'. \tag{32}$$

Substituting $\hat{R} + (\hat{r} - \hat{R}) = \hat{r}$, Eq. (36) is rewritten as

$$U(\hat{x}, \hat{y}; \hat{z}) = i \iint_{-\infty}^{\infty} U(\hat{x}', \hat{y}'; 0) \left(\frac{\hat{z}}{\hat{R}}\right) \left(\frac{\hat{R}}{\hat{r}}\right)^2 \left(\frac{e^{i2\pi\hat{R}}}{\hat{R}}\right) e^{i2\pi(\hat{r} - \hat{R})} d\hat{x}' d\hat{y}'. \tag{33}$$

But

$$\hat{r} - \hat{R} = \frac{\hat{x}'^2 + \hat{y}'^2}{\hat{r} + \hat{R}} - \frac{2\hat{R}}{\hat{r} + \hat{R}} (\alpha_0 \hat{x}' + \beta_0 \hat{y}'),$$

where

$$\alpha_o = \frac{\hat{x}}{\hat{R}}; \quad \beta_o = \frac{\hat{y}}{\hat{R}}; \quad \gamma_o = \frac{\hat{z}}{\hat{R}}.$$

Equation (33) can now be expressed in terms of the direction cosines and the radius $\hat{R}$.

$$U(\alpha_o, \beta_o; \hat{R}) = \frac{i\gamma_o e^{i2\pi\hat{R}}}{\hat{R}} \iint_{-\infty}^{\infty} U(\hat{x}', \hat{y}'; 0) \left(\frac{\hat{R}}{\hat{r}}\right)^2 e^{i2\pi\left(\frac{\hat{x}'^2 + \hat{y}'^2}{\hat{r} + \hat{R}}\right)} \\ \times e^{-i2\pi \frac{2\hat{R}}{\hat{r} + \hat{R}} (\alpha_o \hat{x}' + \beta_o \hat{y}')} dx' dy'. \quad (35)$$

We now make two approximations:

$$(a) \quad \hat{R} + \hat{r} = 2\hat{R} \left(1 + \frac{\hat{r} - \hat{R}}{2\hat{R}}\right) \approx 2\hat{R}, \text{ since } \frac{\hat{r} - \hat{R}}{\hat{R}} \ll 1 \text{ and}$$

$$(b) \quad \frac{\hat{R}}{\hat{r}} = \frac{\hat{r} + \hat{R} - \hat{r}}{\hat{r}} = 1 + \frac{\hat{R} - \hat{r}}{\hat{r}}$$

$$\therefore \left(\frac{\hat{R}}{\hat{r}}\right)^2 = 1 + \frac{2(\hat{R} - \hat{r})}{\hat{r}} + \left(\frac{\hat{R} - \hat{r}}{\hat{r}}\right)^2 \approx 1,$$

$$\text{since } \frac{\hat{R} - \hat{r}}{\hat{r}} \ll 1. \quad (36)$$

When the approximations expressed in Eqs. (36) are substituted into Eq. (35) we have:

$$U(\alpha_o, \beta_o; \hat{R}) \approx \frac{i\gamma_o e^{i2\pi\hat{R}}}{\hat{R}} \iint_{-\infty}^{\infty} U(\hat{x}', \hat{y}'; 0) e^{i2\pi\left(\frac{\hat{x}'^2 + \hat{y}'^2}{2\hat{R}}\right)} \\ \times e^{-i2\pi(\alpha_o \hat{x}' + \beta_o \hat{y}')} d\hat{x}' d\hat{y}'. \quad (37)$$

Equation (37) is the classical Fresnel diffraction expression modified by a spherical wave. The further approximation that

$$e^{i2\pi \left(\frac{\hat{x}'^2 + \hat{y}'^2}{2R} \right)}$$

is equal to 1 leads to the result:

$$U(\alpha_o, \beta_o; \hat{R}) \approx \frac{i\gamma_o e^{i2\pi\hat{R}}}{\hat{R}} \iint_{-\infty}^{\infty} U(\hat{x}', \hat{y}'; 0) e^{-i2\pi(\alpha_o \hat{x}' + \beta_o \hat{y}')} d\hat{x}' d\hat{y}'. \quad (38)$$

This is the Fraunhofer pattern as modified by a spherical wave. From Eq. (11) we know that Eq. (38) can be rewritten as:

$$U_o(\alpha_o, \beta_o; \hat{R}) \approx \frac{i\gamma_o e^{i2\pi\hat{R}}}{\hat{R}} A_o(\alpha_o, \beta_o; 0). \quad (39)$$

We have a spherical wave modulated by the Fourier transform of the disturbance in the initial plane. Now let

$$U(\hat{x}', \hat{y}') = a_o \tau(\hat{x}', \hat{y}'). \quad (40)$$

From Eqs. (39) and (40) we can write

$$\begin{aligned} \frac{\hat{R}}{i\gamma_o} e^{-i2\pi\hat{R}} U(\alpha_o, \beta_o, \hat{R}) &= A(\alpha_o, \beta_o) \\ &= a_o \iint_{-\infty}^{\infty} \tau(\hat{x}', \hat{y}') e^{-i2\pi(\alpha_o \hat{x}' + \beta_o \hat{y}')} d\hat{x}' d\hat{y}'. \end{aligned} \quad (41)$$

The power theorem will give us the total flux, Φ , viz.,

$$\iint_{-\infty}^{\infty} \frac{\hat{R}^2}{\gamma_o^2} |U(\alpha_o, \beta_o, \hat{R})|^2 d\alpha_o d\beta_o = a_o^2 \iint_{-\infty}^{\infty} |\tau(\hat{x}', \hat{y}')|^2 d\hat{x}' d\hat{y}' = \Phi. \quad (42)$$

Noting that $d\omega = d\alpha_0 d\beta_0 / \gamma_0$, Eq. (42) can be rewritten as:

$$\iint_{\Omega} \frac{\hat{R}^2}{\gamma_0} |U(\alpha_0, \beta_0, \hat{R})|^2 d\omega = \frac{a_0^2 a}{\lambda^2} = \Phi = \text{total power.} \quad (43)$$

The radiant intensity, $I(\text{w/sr})$, is then

$$I(\alpha_0, \beta_0) = \frac{d\Phi}{d\omega} = \frac{\hat{R}^2}{\gamma_0} |U(\alpha_0, \beta_0, \hat{R})|^2 = \gamma_0 |A(\alpha_0, \beta_0)|^2. \quad (44)$$

We note that the radiant intensity is directly proportional to γ and thus we have a cosine dependence.

Scattering Theory

In general the pupil function will include random perturbations that will lead to scatter. In order to treat these perturbations we consider the transfer function V , which is the Fourier transform of the spread function, i.e., $|A|^2 \leftrightarrow V$. The autocorrelation theorem allows us to write the transfer function as in Eq. (45) below.

$$\begin{aligned} V(\hat{\xi}', \hat{\eta}') &= \iint_{-\infty}^{\infty} U(\hat{x}' + \frac{\hat{\xi}'}{z}, \hat{y}' + \frac{\hat{\eta}'}{z}) \\ &\quad \times U^*(\hat{x}' - \frac{\hat{\xi}'}{z}, \hat{y}' - \frac{\hat{\eta}'}{z}) d\hat{x}' d\hat{y}' \end{aligned} \quad (45)$$

$$\begin{aligned} &= a_0^2 \iint_{-\infty}^{\infty} \tau(\hat{x}' + \frac{\hat{\xi}'}{z}, \hat{y}' + \frac{\hat{\eta}'}{z}) \\ &\quad \times \tau^*(\hat{x}' - \frac{\hat{\xi}'}{z}, \hat{y}' - \frac{\hat{\eta}'}{z}) d\hat{x}' d\hat{y}'. \end{aligned} \quad (46)$$

If we assume that the pupil function has random phase variations and no amplitude variations (such as a mirror in the pupil would introduce) we can write τ as:

$$\tau = |\tau| e^{i2\pi(\hat{W}_O + \hat{W}_R)}, \quad (47)$$

where $\hat{W}_R$ indicates the random component. Further, if we introduce the notation:

$$W(+) = W(x + \frac{\hat{\xi}'}{z}, y + \frac{\hat{\eta}'}{z})$$

and

$$W(-) = W(x - \frac{\hat{\xi}'}{z}, y - \frac{\hat{\eta}'}{z}), \quad (48)$$

and take the average, we obtain

$$\begin{aligned} \langle V(\hat{\xi}', \hat{\eta}') \rangle &= a_0^2 \iint_{-\infty}^{\infty} |\tau(+)| |\tau(-)| e^{i2\pi(\hat{W}_0(+) - \hat{W}_0(-))} \\ &\quad \times \langle e^{i2\pi(\hat{W}_R(+) - \hat{W}_R(-))} \rangle d\hat{x}' d\hat{y}'. \end{aligned} \quad (49)$$

The term,

$$\langle e^{i2\pi(\hat{W}_R(+) - \hat{W}_R(-))} \rangle$$

in Eq. (49) is the only term of the equation that is random. For stationary processes, such as those which describe mirror surfaces, this term is not a function of x' or y' and may thus be taken outside of the integral.

$$\begin{aligned} \langle V(\hat{\xi}', \hat{\eta}') \rangle &= e^{i2\pi(\hat{W}_R(+) - \hat{W}_R(-))} a_0^2 \iint_{-\infty}^{\infty} |\tau(+)| |\tau(-)| \\ &\quad \times e^{i2\pi(\hat{W}_0(+) - \hat{W}_0(-))} d\hat{x}' d\hat{y}' \end{aligned} \quad (50)$$

The expected value of the transfer function may be written as:

$$\langle V(\hat{\xi}', \hat{\eta}') \rangle = \langle e^{i2\pi(\hat{W}_R(+) - \hat{W}_R(-))} \rangle V_0. \quad (51)$$

Here V_0 can be thought of as a transfer function for a surface without irregularities and the expected value of the term containing the random components as a transfer function for the irregularities. It remains to

determine the form of this expected value. Let us assume a normal distribution for $W_R(+)$ - $W_R(-)$. From random variable theory we find that the expected value for two, real valued, stationary, jointly normal, random processes $X(+)$ and $Y(+)$ is given by:

$$\langle e^{X(+)} + e^{iY(+)} \rangle = e^{[\eta_x + i\eta_y + \frac{1}{2}(\mu_{20} + i2\mu_{11} - \mu_{02})]}, \quad (52)$$

where

$$\eta_x = \langle X(+) \rangle$$

$$\eta_y = \langle Y(+) \rangle \quad \text{and}$$

$$\mu_{jk} = \langle (X - \eta_x)^j (Y - \eta_y)^k \rangle.$$

In our case, $X = 0$ and $H(+) = 2\pi(\hat{W}(+) - \hat{W}(-))$ and:

$$\eta_x = \langle X(+) \rangle = 0$$

$$\mu_{20} = 0$$

$$\mu_{11} = 0.$$

$$\langle e^{iY(+)} \rangle = \langle e^{i2\pi(\hat{W}_R(+)) - \hat{W}_R(-)} \rangle = e^{i\eta_y - \frac{1}{2}\mu_{02}}. \quad (53)$$

For our problem,

$$\eta_y = \langle 2\pi(\hat{W}(+) - \hat{W}(-)) \rangle = \langle 2\pi\hat{W}(+) \rangle - \langle 2\pi\hat{W}(-) \rangle = 0, \quad (54)$$

since in a stationary process the expected value of $W(+)$ and $W(-)$ are identical. We also find:

$$\begin{aligned} \mu_{02} &= \langle [2\pi(W_R(+)) - W_R(-)] - 2\pi\hat{W}_R(+)) - 2\pi\hat{W}_R(-)]^2 \rangle \\ &= 2\pi^2 [\underbrace{\langle \hat{W}_R^2(+) \rangle}_{\sigma_W^2} - \underbrace{\langle 2\hat{W}_R(+)\hat{W}_R(-) \rangle}_{2R(\hat{\xi}', \hat{\eta}')} + \underbrace{\langle \hat{W}_R^2(-) \rangle}_{\sigma_W^2}] \end{aligned}$$

$$= 2\pi^2 [2(\hat{\sigma}_W^2 + R(\hat{\xi}', \hat{\eta}'))] \quad (55)$$

$$= 2(2\pi)^2 \hat{\sigma}_W^2 [1 - C(\hat{\xi}', \hat{\eta}')], \quad (56)$$

where

$$C(\hat{\xi}', \hat{\eta}') = \frac{R(\hat{\xi}', \hat{\eta}')}{\hat{\sigma}_W^2}.$$

Here $C(\hat{\xi}', \hat{\eta}')$ is the normalized autocorrelation function. Equation (52) can then be written:

$$\left\langle e^{i2\pi(\hat{W}_R(+)-\hat{W}_R(-))} \right\rangle = e^{-(2\pi)^2 \hat{\sigma}_W^2 [1 - C(\hat{\xi}', \hat{\eta}')] } \quad (57)$$

$$= e^{-(2\pi)^2 \hat{\sigma}_W^2} + \left(1 - e^{-(2\pi)^2 \hat{\sigma}_W^2}\right) C', \quad (58)$$

where

$$C' = \frac{e^{(2\pi)^2 \hat{\sigma}_W^2} C}{e^{(2\pi)^2 \hat{\sigma}_W^2} - 1}. \quad (59)$$

When the irregularities have a Gaussian distribution as we have assumed, we can then say several things with respect to Eq. (58).

- (a) We have placed no restrictions (yet) on the magnitude of $\hat{\sigma}_W$.
- (b) The effective transfer function can be thought of in two parts; a scattered part with an arbitrary autocorrelation function C' , and a constant specular component. These components are illustrated in Fig. 5a.
- (c) The associated spread function is a delta function with an associated scattering function. The Fourier transform of C' is shown in Fig. 5b.

From Eq. (58) we see that the total flux in the spread function distribution can be divided into two parts, that is,

$$\Phi = \Phi_C + \Phi_H. \quad (60)$$

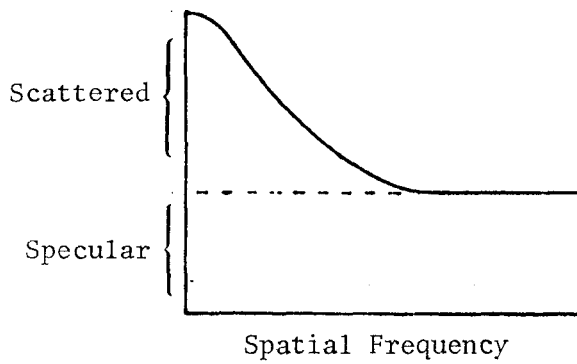


Fig. 5a. Transfer function.

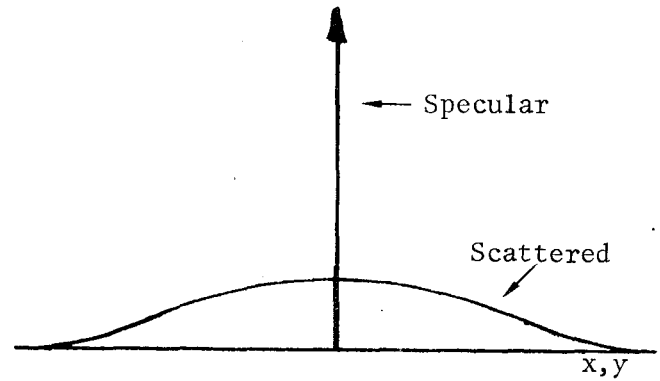


Fig. 5b. Spread function.

The fraction of the light in the specular part is given by

$$\Phi_C/\Phi = e^{-(2\pi)^2 \hat{\sigma}_W^2}, \quad (61)$$

and the scattered fraction by

$$\Phi_H/\Phi = 1 - e^{-(2\pi)^2 \hat{\sigma}_W^2}. \quad (62)$$

The fractions Φ_H and Φ_C can be determined radiometrically, and the magnitude of the irregularities can be inferred by the consequent relation

$$\hat{\sigma}_W^2 = \frac{1}{(2\pi)^2} \ln(1 + \Phi_H/\Phi_C), \quad (63)$$

which, as Φ_H/Φ_C becomes small, approaches

$$\hat{\sigma}_W^2 \approx \frac{1}{(2\pi)^2} (\Phi_H/\Phi_C). \quad (64)$$

The shape of the autocorrelation function of the irregularities can be inferred from the measurable scattering function. The function C' in Eq. (59) and the scattering function are a Fourier transform pair, and the desired autocorrelation function C can be obtained from C' by

$$C = \frac{\ln(1 + (\phi_H/\phi_C)C')}{\ln(1 + (\phi_H/\phi_C))}, \quad (65)$$

which, for small ϕ_H/ϕ_C , becomes simply

$$C \approx C'. \quad (66)$$

This development has shown that it is possible to obtain the statistical properties of mirror surface irregularities by radiometric measurement of the light scattered by the mirror.

III

EXPERIMENTAL APPARATUS AND TECHNIQUE

Apparatus

A schematic diagram of the apparatus used is shown in Fig. 6. To minimize the effects of dust and dirt the equipment was set up in a closed-off area of the Optical Testing Laboratory. The sample and the associated detector optics were further isolated by means of a black velvet tent hung from the ceiling and enclosing the immediate area.

The light source employed was a Spectra-Physics Model 165 Argon Ion Laser. The laser was used in its single-mode configuration with the power adjusted to 20 mw. Two modes of regulation are available in this laser; current regulation and light regulation. In all instances the light regulation mode was used. This mode varies the current supplied by the power supply to assure intensity regulation to within one percent. A further feature of this particular laser is an aperture within the cavity which permits adjustment of the beam diameter. This aperture was set near its maximum opening, 300 μ m, to minimize the effects of diffraction.

Light leaving the laser was directed toward the sample by employing two front-surfaced mirrors. The beam then passed through a chopper which modulated the beam at 666 Hz. The chopped light then passed through a single blackened aperture before striking the sample surface. Stray light associated with the laser and light scattered by the beam-directing mirrors and chopper is restricted by this aperture. The sample area is defined by the black velvet tent.

The specular component of the radiation reflected by the sample passes back through the tent. In the case of "normal" incidence the specular beam returned through the aperture by which it entered. The beam in such instances is not precisely normal to the sample surface since it would then effectively become part of the laser cavity and alter the characteristics of the incident beam. Instead the specular and reflected beam are separated by 10 minutes of arc. In the case of non-normal incidence the specular beam passes through a well-defined aperture in the tent and is subsequently directed into a Rayleigh's horn light trap.

The detector in all instances was a Phillip's one-inch end on photomultiplier having an S-20 photocathode. Light reaches the photomultiplier by way of a rigid fiber-optic probe. Such a probe offers several distinct advantages in light sampling. First, substantially the entire cross-section of the fiber bundle is a collector. In addition, the field of view can be restricted to several degrees owing to the propagation properties of fiber bundles, (see Appendix A), and lastly the diameter of the bundle was small compared to that of the photomultiplier allowing both increased angular resolution throughout the scattered field and the ability to probe within half a degree of the incident or specular beams.

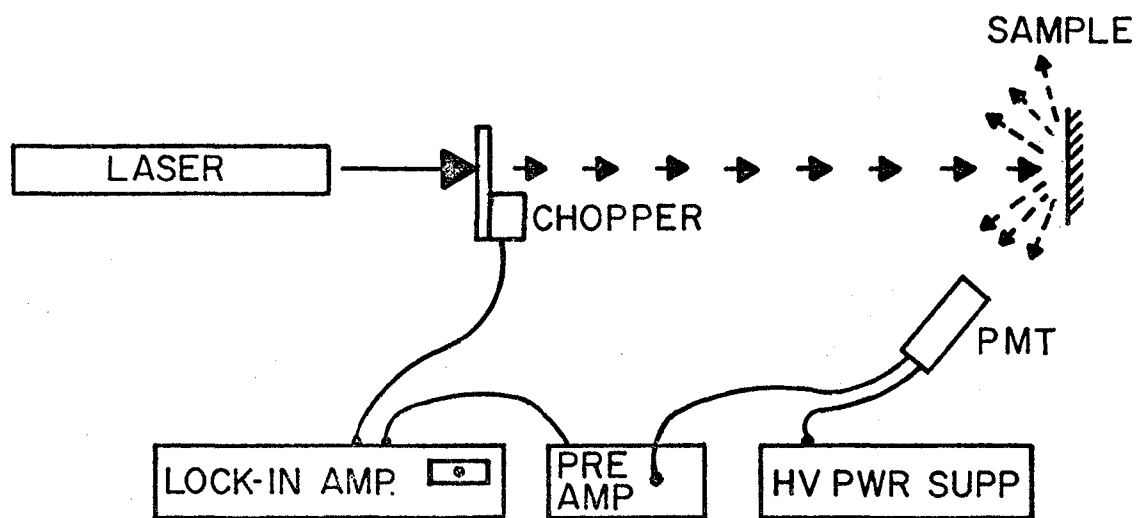


Fig. 6. Schematic diagram of scatter measurement apparatus.

The detector probe unit was mounted on a rigid arm that could be rotated in either of two orthogonal directions. Rotation about a vertical axis was accomplished by means of a massive precision rotary table. In turn the rigid arm was attached to the rotary table by means of a worm gear arrangement which allowed rotation about the horizontal axis. The intersection of these two axes defined the sample location. Figure 7 illustrates this configuration in detail.

The sample holder also had two degrees of rotation; one about the vertical axis and a second about the horizontal axis. The horizontal axis always was in the plane of the sample and the vertical axis always intersected the center of the sample. Alignment of all four axes involved in sample and detector orientation was conducted prior to each experimental run.

Experimental Procedures

The geometry of the measurements is illustrated in Fig. 8. The distance from the sample to the fiber-optic probe is 25 cm. The probe is .3 cm in diameter giving it an angular subtense of .25 degrees.

In order to facilitate a straightforward data reduction routine, only the rotary table was moved during any data run.

The measurement procedure is then as follows: the laser beam is accurately adjusted to strike the center portion of the sample under test by moving the two small mirrors previously mentioned. Subsequently the fiber-optics probe, sample, and rotary table are properly aligned and adjusted with respect to the incident beam. A freshly coated magnesium oxide (MgO) reference sample known to have a diffuse reflectance in excess of ninety-eight percent across the visible spectrum was placed in the sample holder. Scattering measurements from the MgO sample were integrated to calculate the incident intensity of the incoming radiation.

The sample to be measured is then placed in the holder and the scatter field is measured by moving the fiber probe from a position near the specular beam toward the plane of the sample. This motion is accomplished by moving the rotary table in steps toward increasingly larger angles. Typically the scatter was measured at thirty different angles during a given run. At each angle a voltage measurement proportional to the intensity level of the scattered field was recorded. These measurements were then recorded as the ratio of scattered light to reflected light vs. angle from the specular beam. This comprises the raw data.

To compensate for unwanted stray light the sample was entirely removed from its holder and the beam was allowed to exit through the black velvet tent. In this sense the sample can be thought of as perfectly reflecting and any resulting measurements of scattered radiation can then be attributed to background. A background measurement was taken in conjunction with each run. These readings were subtracted from the raw data.

Another source of unwanted light was due to the divergence and finite extent of the laser beam itself.

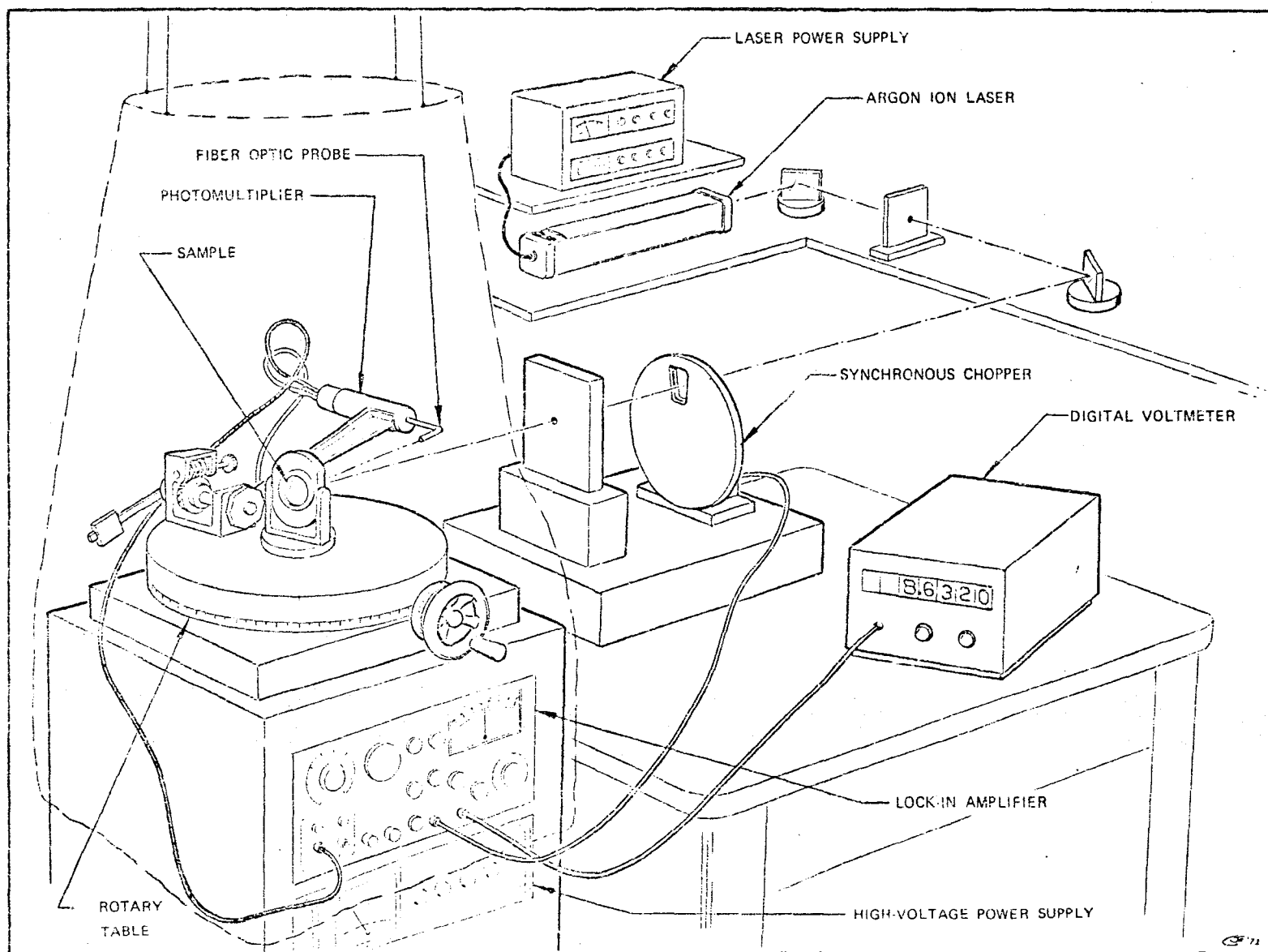


Fig. 7. Drawing of the scatter measurement apparatus.

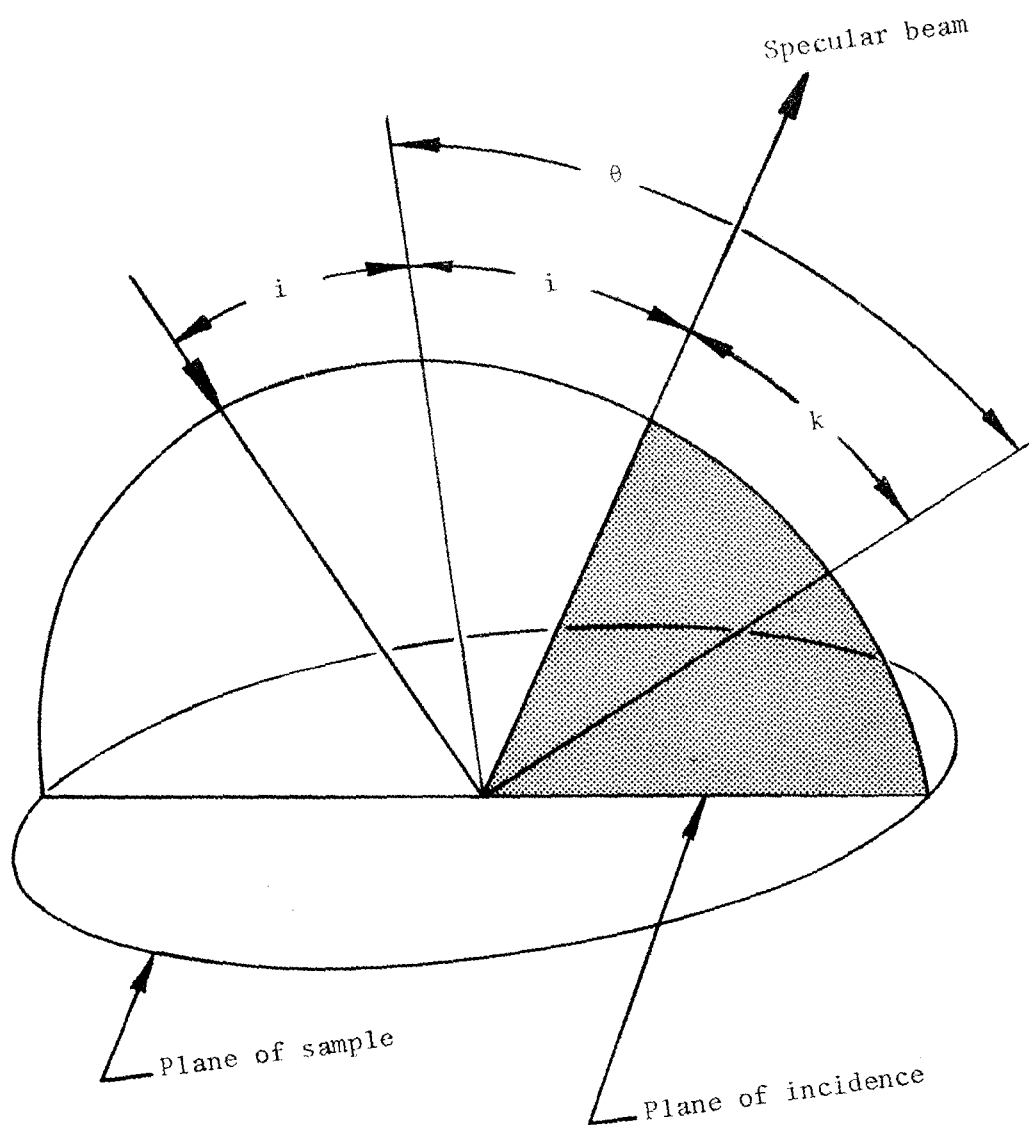


Fig. 8. Geometry of the measurements.

Compensation for the error introduced by beam spread was made in a similar fashion to that used for the background measurements. Again the sample was removed from the sample holder and "no sample" was considered to be the perfect reflector. In this instance, however, the probe was moved to the position of its virtual image as seen when looking into the actual sample. This geometry is shown in Fig. 9. The probe is then moved away from the transmitted beam and measurements are taken at angles corresponding to those taken when the actual sample was in place. These measurements are also subtracted from the initial raw data. They were recorded as "beam-spread" measurements. These measurements became noise limited when the probe was 6 degrees from the incident beam.

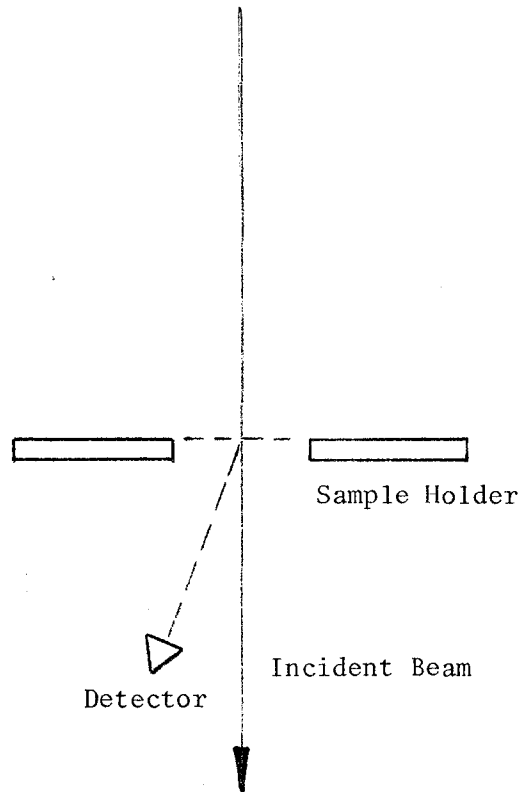


Fig. 9. Geometry of the beam spread measurements.

IV

DATA AND RESULTS

The distribution of light scattered by a plane mirror as a function of surface roughness, angle of incidence, and wavelength are reported in this section. General results are compared with the theory.

Background Data

As noted in the section on Experimental Procedure, the background measurements were due to spread of the laser beam. As these measurements were all taken through the sample holder with no sample in place, it was expected that all measurements would be the same. Figures 10 and 11 show, however, that the values of the background varied considerably. The cause for these background differences is not clear, but several things should be pointed out with respect to them. First, the angular extent of the background is confined to within eight degrees of the specular beam, with most detail of any note being within six degrees of the specular beam. In some cases the small angle data has a shape very similar to that of a particular background measurement, and in others there is no strong correlation. The net result is that these background measurements, which should all be identical, reduce our confidence in the small angle data (that data between 1.5° and 6°). Data taken outside this range appears to be reliable.

Because of discrepancies in the background measurements we have presented much of the data in a dual format. In the first format we subtracted the background that was taken in conjunction with the particular set of measurements. The second format presents the data with the "best-fit" background subtracted.

Presentation of the Data

A measure of the total flux, Φ , incident on the samples was obtained by performing a numerical integration of the scattered light distribution from the magnesium oxide reference sample. These integrations were made in conjunction with each set of measurements.

Background data describing the flux distribution of the incident beam is then subtracted from measurements of the intensity of the scattered field. These data are represented by η' . The corrected data is then normalized by dividing by Φ and the data from each run can now be plotted to yield the scattered light distribution of the sample.

These distributions are plotted as modified log-log plots with the ordinate being $\log \eta / \cos \theta$ (where $\eta = \eta' / \Phi$ is the scatter coefficient); where θ is the angular position of the measurement with respect to the normal to the sample. The abscissa in these plots is $\log (\sin \theta - \sin i)$; where i is the angle of incidence (see Fig. 8). We now have $\theta = k+i$, k being the angle

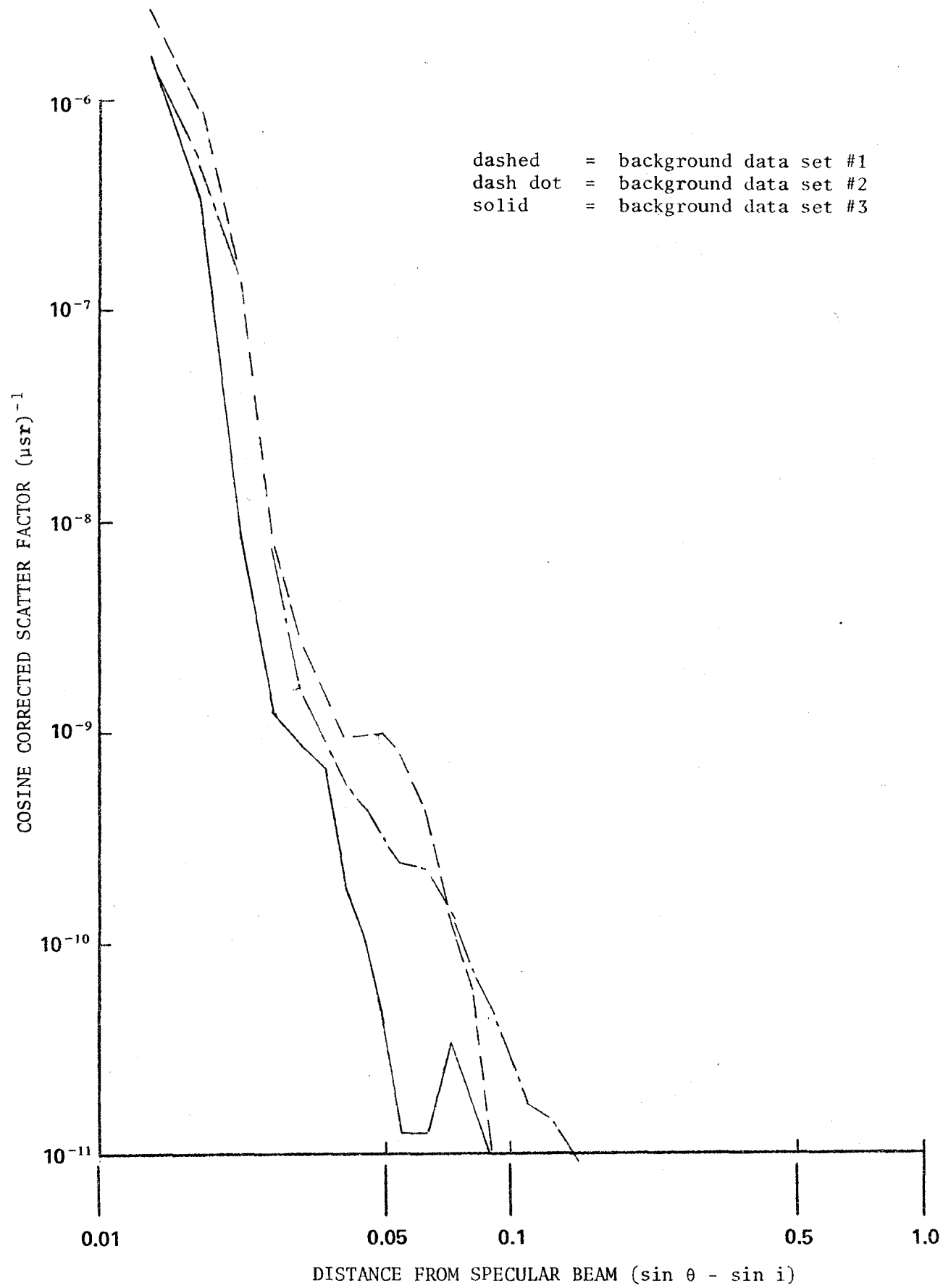


Fig. 10. Measurements of the background due to beam spread.

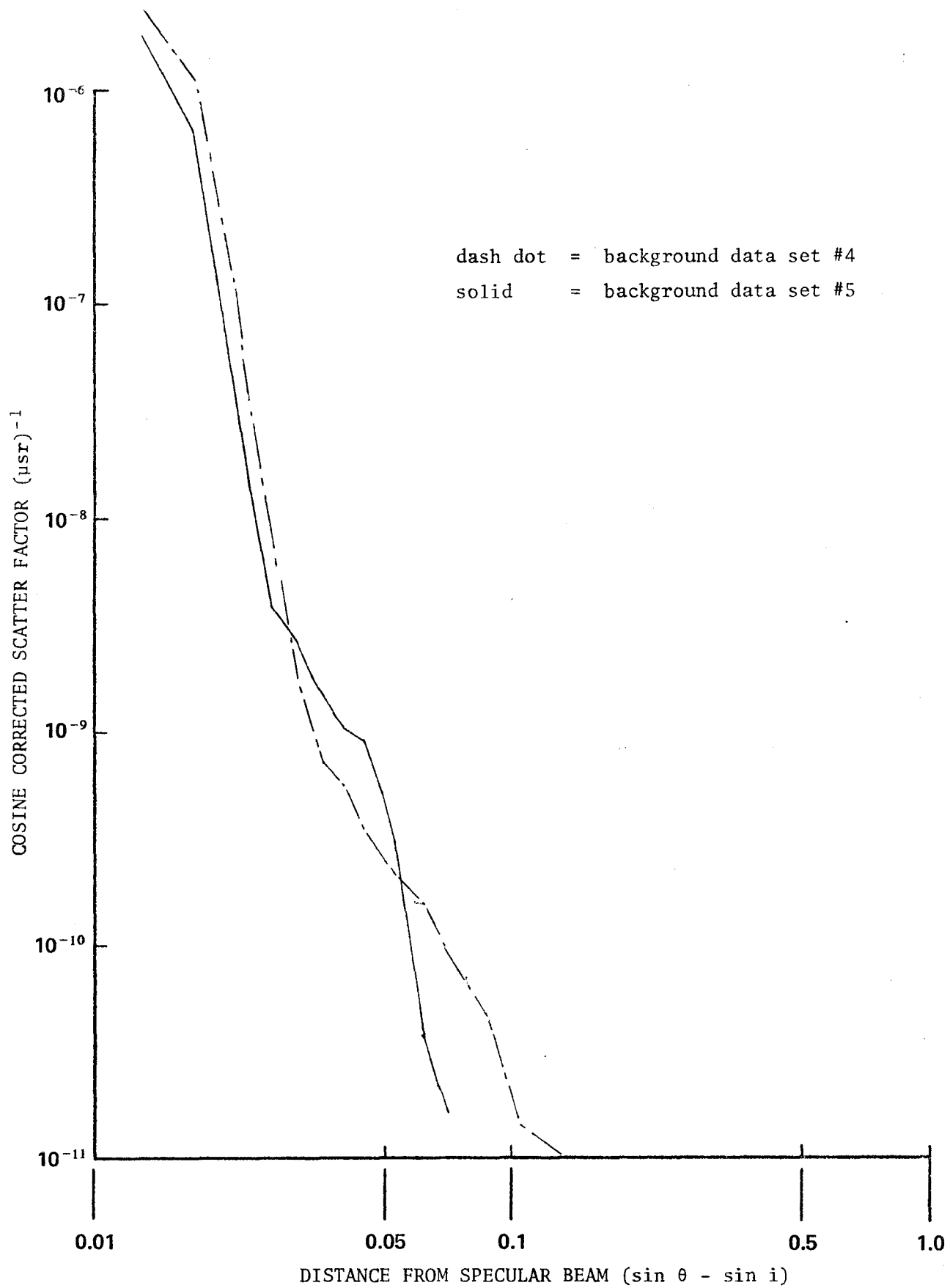


Fig. 11. Measurements of the background due to beam spread.

from the specular beam to the measurement. To illustrate the effect that these plotting coordinates exercise on the data, intermediate steps are illustrated in Figs. 12, 13, and 14 for samples 247 and MgO.

Figure 12 is a log-log plot of η vs. the angle k from the specular beam. In Fig. 13 we have plotted the same information, however, we have now divided the scattered flux by $\cos\theta$. The effects of this division are seen easily at the larger angles where $\cos\theta$ is small and the plotted values are noticeably higher. The result of this division is of particular note in the case of the MgO sample where the curve has become almost flat. (A flat plot would indicate a perfect Lambertian surface.)

Figure 14 illustrates the change of scale in the abscissa when we shift from $\log(k)$ to $\log(\sin\theta - \sin i)$. In this case we have used data for $i = 0^\circ$ and $i = 45^\circ$ from sample 247. The change in scale for normal incidence measurements can be noted for both MgO and sample 247.

The data, at least in the large-angle region where it is well-behaved, appears to follow an inverse power law, and must eventually level off to a finite maximum value for very small angles, although this leveling does not show in the data. A function that may be used to represent this behavior is

$$I = I_0 [1 + (\rho/\rho_0)^2]^{-(s/2)}, \quad (67)$$

where I_0 is the central maximum radiant intensity, $\rho = \sqrt{\alpha^2 + \beta^2}$ is the direction cosine of the scattering angle (assuming the scattering function is a figure of revolution), ρ_0 is a scale factor measuring the width of the scattering function, and s is the rate at which the function decreases for large angles. For small angles where $\rho/\rho_0 \ll 1$,

$$I \approx I_0 [1 - \frac{s}{2} (\rho/\rho_0)^2], \quad (68)$$

and for large angles where $\rho/\rho_0 \gg 1$,

$$I \approx (I_0 \rho_0^s) \rho^{-s}. \quad (69)$$

The total flux scattered out to a radius ρ^* is given by

$$\Phi_s(\rho^*) = 2\pi \int_0^{\rho^*} I \rho d\rho = \frac{2\pi I_0 \rho_0^2}{2-s} \left\{ [1 + (\rho^*/\rho_0)^2]^{\frac{1}{2}(-s)} - 1 \right\}, \quad s < 2, \quad (70)$$

and the total flux scattered, $\Phi_s(1) = \Phi_H$, is obtained by setting $\rho^* = 1$.

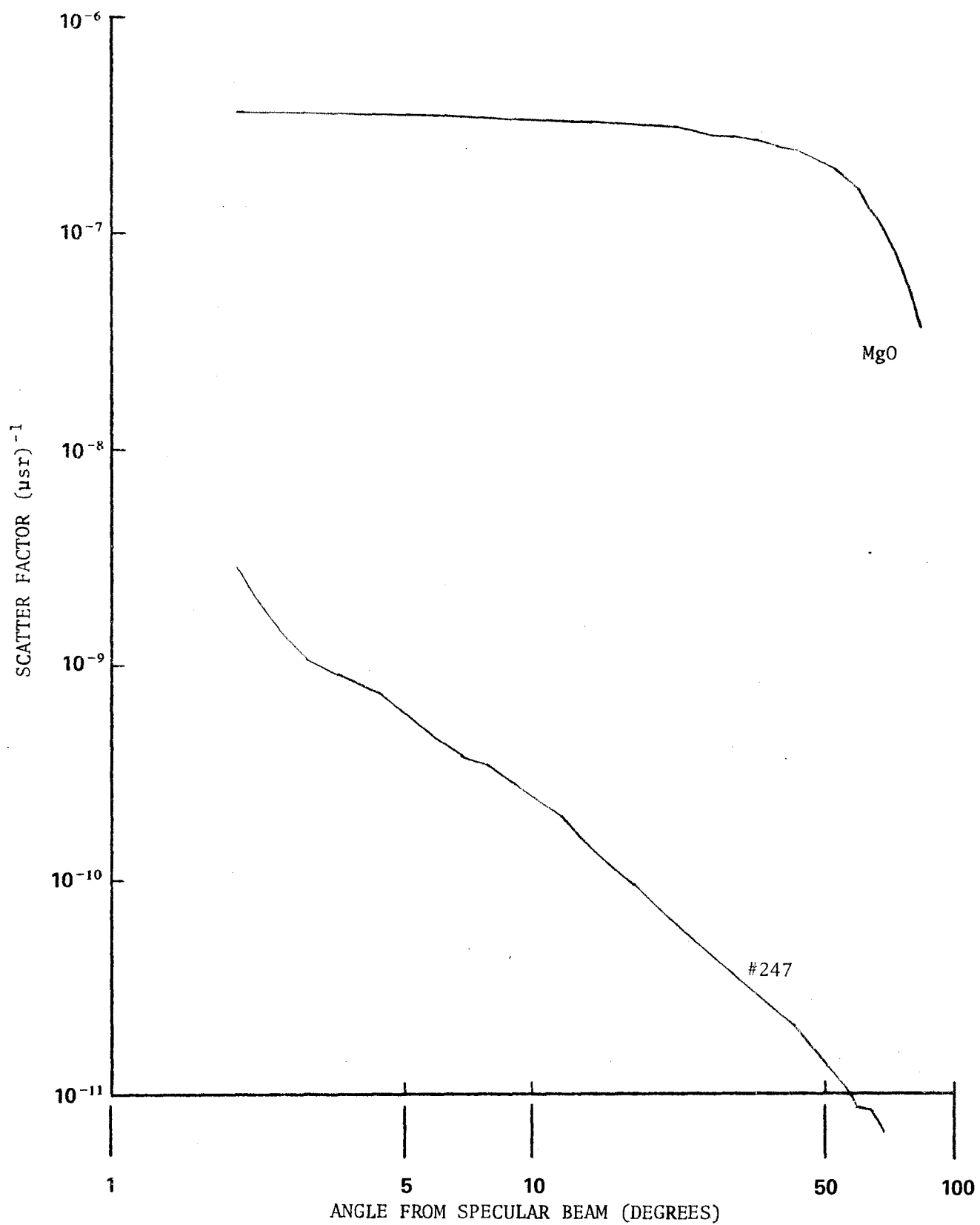


Fig. 12. Scatter vs. angle from specular beam; normal incidence.

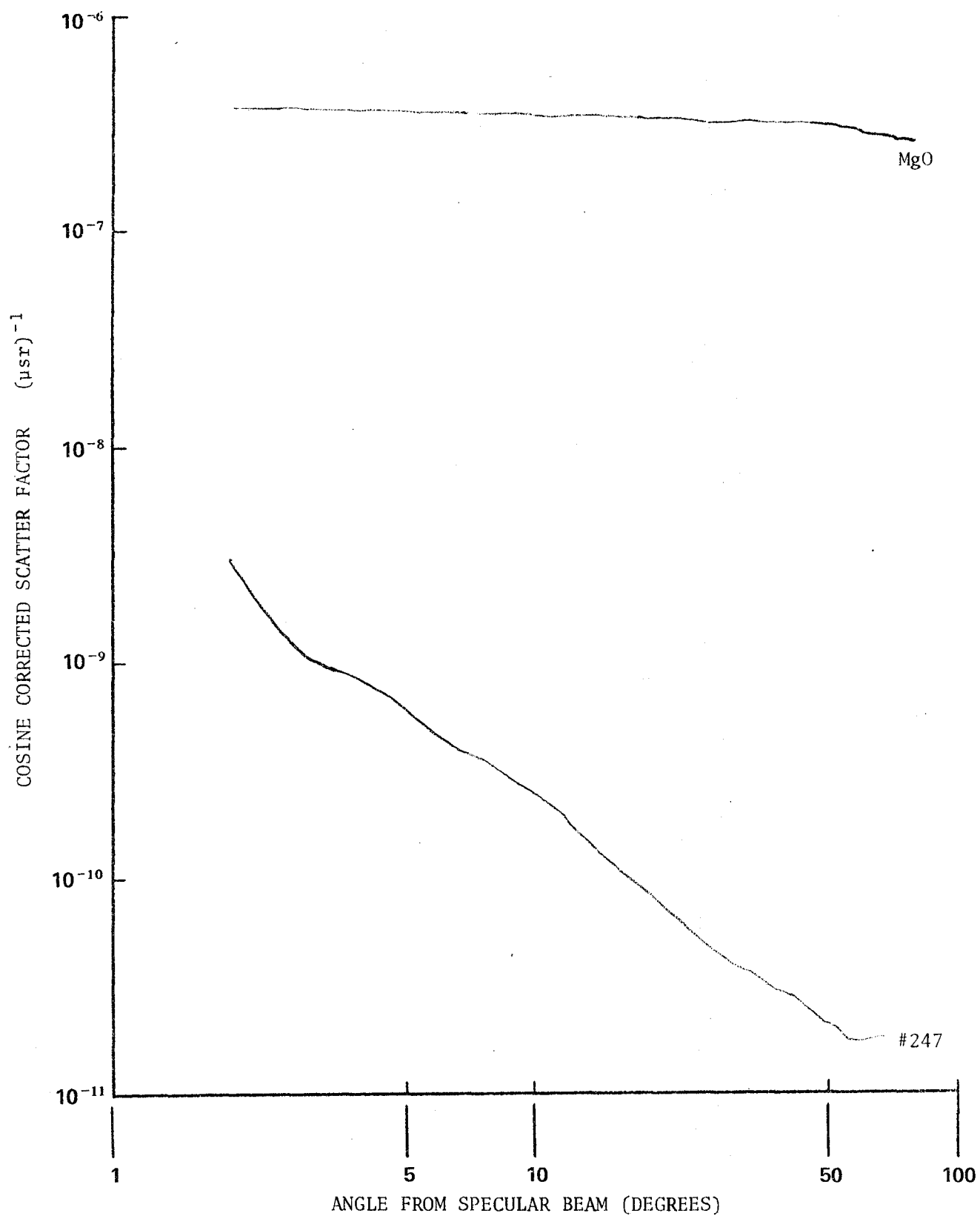


Fig. 13. Scatter vs. angle from specular beam; normal incidence.

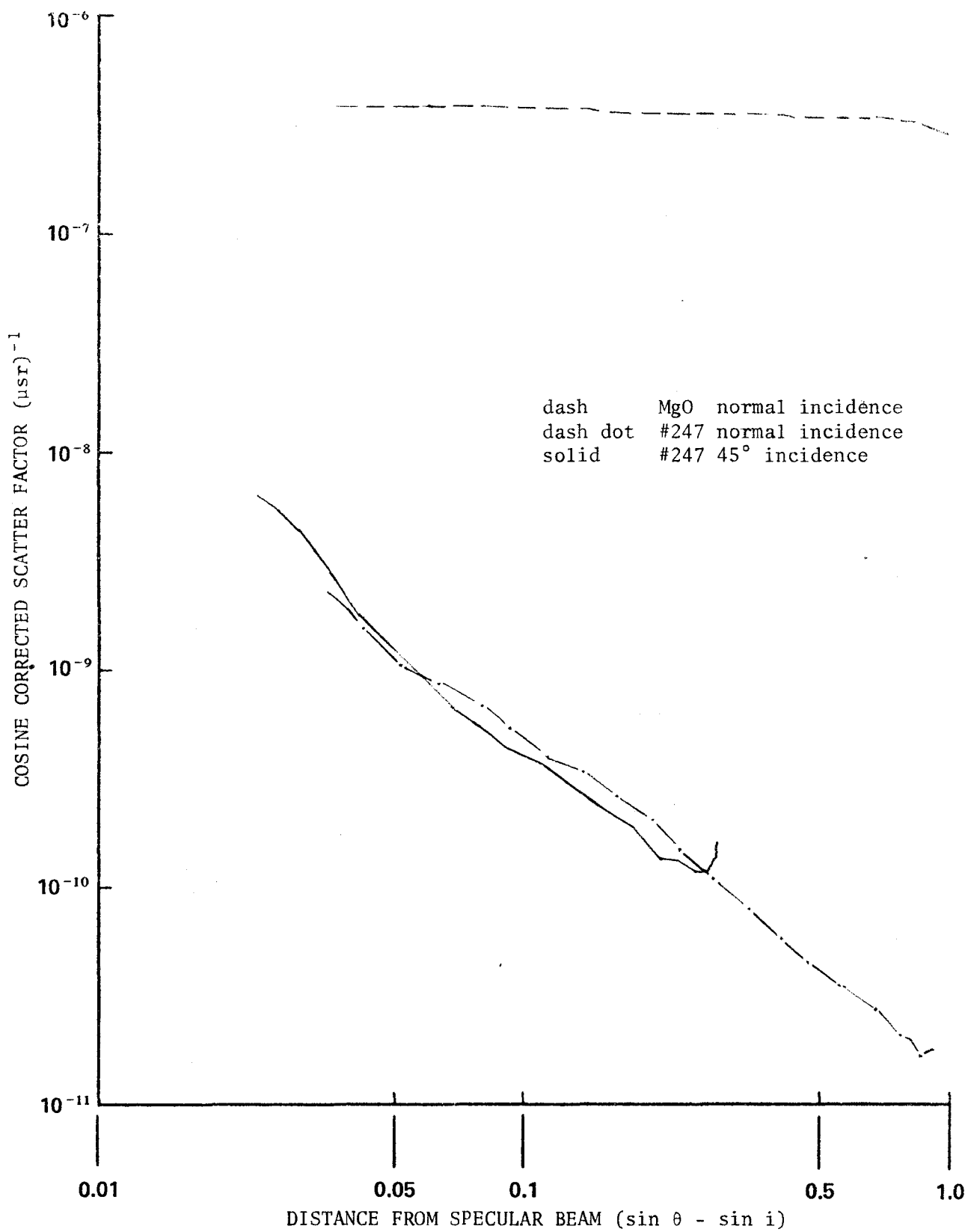


Fig. 14. An example of scatter data plotted vs. the distance from the specular beam.

In the limit for $\rho_o \ll 1$, we obtain

$$\Phi_H \approx \frac{2\pi I_o \rho_o^s}{2-s}. \quad (71)$$

If we compare this with Eq. (69), we see that we can obtain an approximate value for the total scattered flux by the relation

$$\Phi_H \approx \frac{2\pi}{2-s} I(1), \quad (72)$$

without knowing the values of I_o and ρ_o .

Scatter as a Function of Surface Roughness

Variations in surface roughness were obtained by employing a variety of grinding polishing techniques as outlined in Appendix A. The scattered light distributions of all samples listed in Table 3, Appendix A, were measured at normal incidence. The results of these measurements are shown in Figs. 15 and 16.

It should be noted that the slope of the wide angle portion of the polished samples is close to being flat for the angles beyond six degrees. The slopes vary from about 1.25 to 2.0. Also of significance is the change of shape brought about by subtracting the appropriate background. Selection of this background appears to have substantially removed the anomaly in the plots of samples 236, 222, 247, and EDF 3-4.

Samples 221 and 229 are ground samples and exhibit a behavior close to that of MgO. No specular beam was detectable when these samples were illuminated at normal incidence.

Separate scattering phenomena may account for the kink in the plots of polished samples at approximately six degrees. However, uncertainty of the background data necessitates further research to determine if this is true.

Scatter as a Function of Angle of Incidence

In the general case, light is not normally incident upon an optical surface. The behavior of scattered radiation when light is incident upon a sample at angles between 0° and 60° was investigated. In all cases the measurements were made in the plane of incidence and only include measurements in the shaded portion of Fig. 8. (A modification to the existing apparatus is suggested, [see "Suggestions for Future Research"] that will allow measurement throughout the plane of incidence and planes orthogonal to the plane of incidence.)

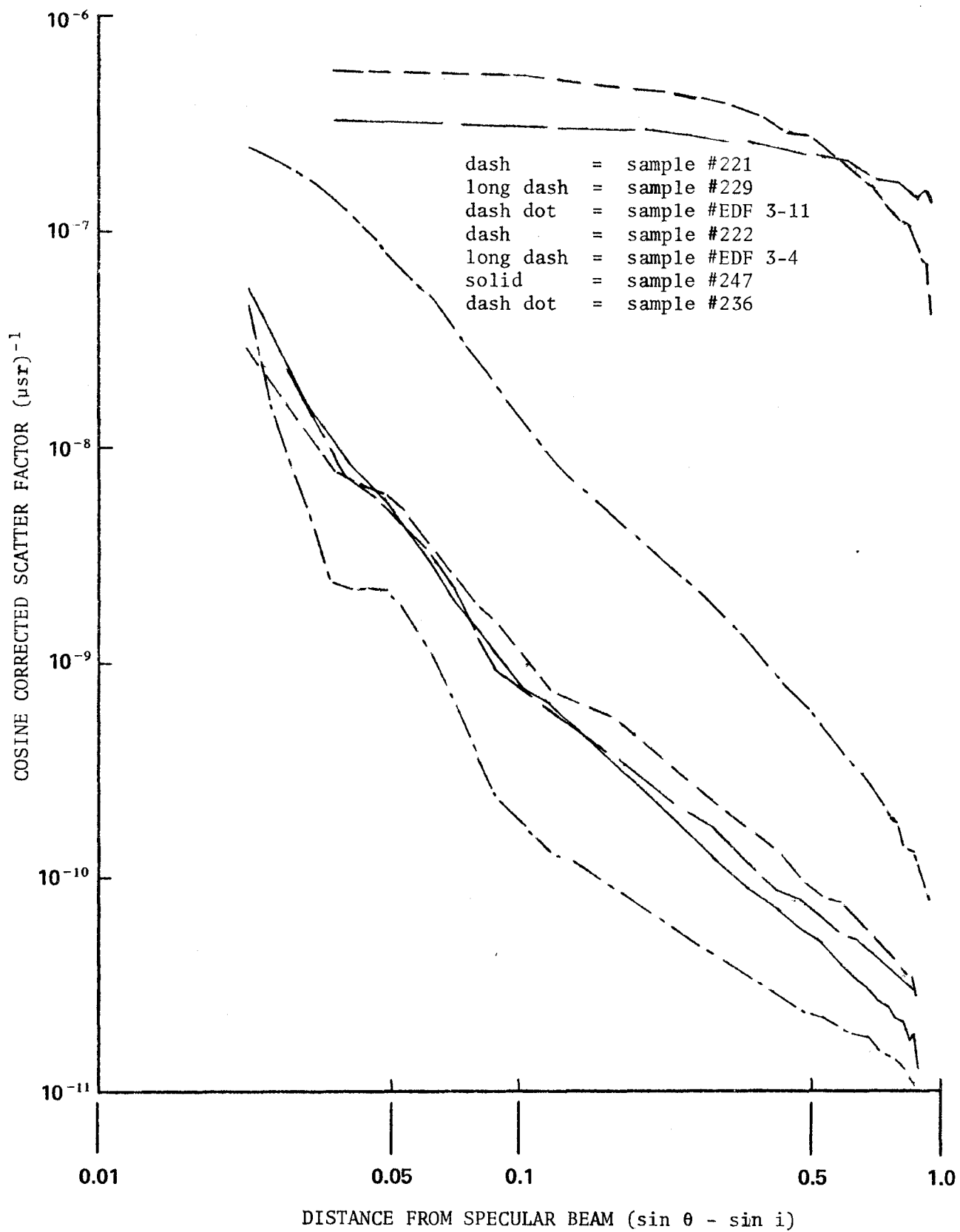


Fig. 15. Scatter as a function of surface roughness, normal incidence; corrected for background measured in conjunction with this data.

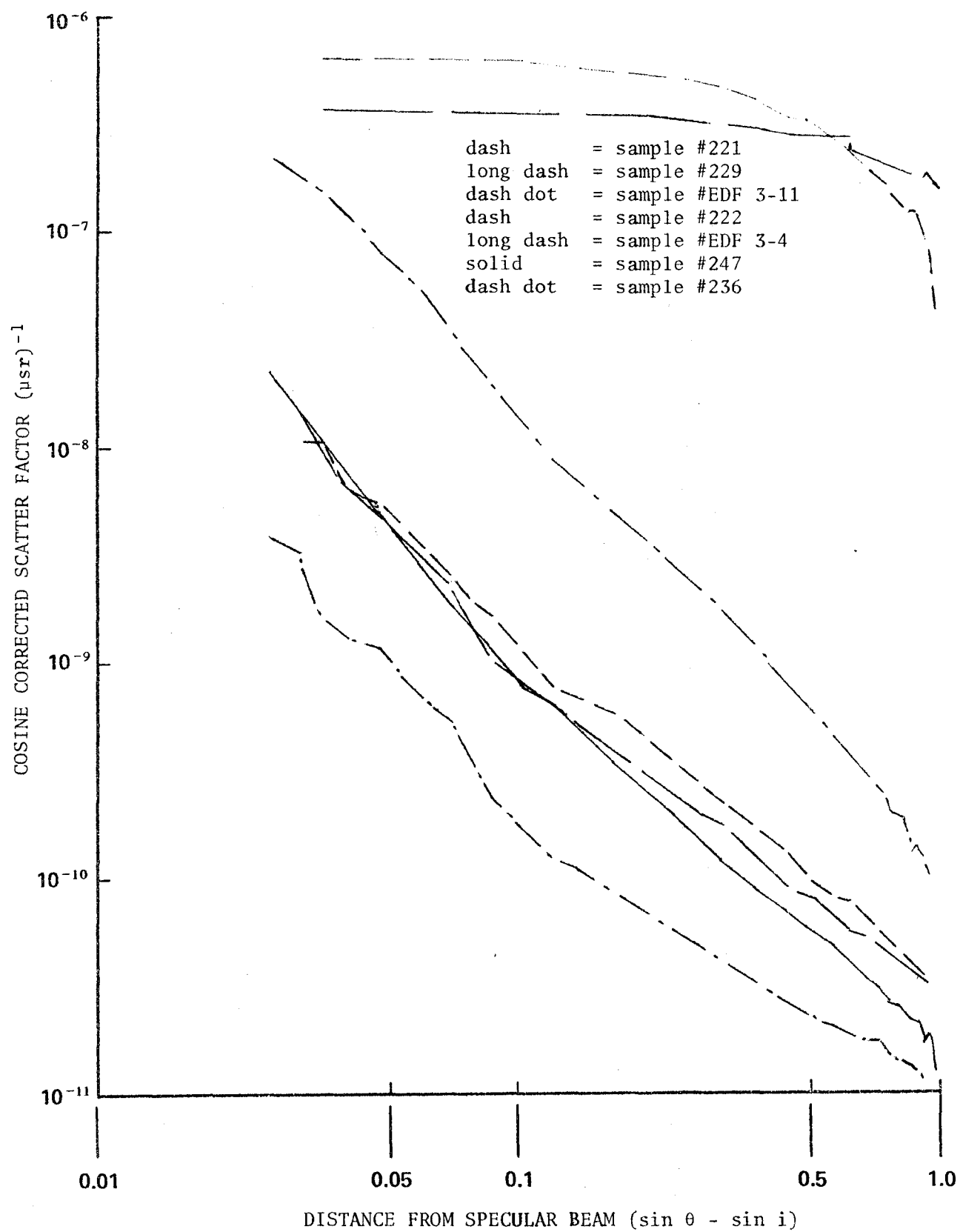


Fig. 16. Scatter as a function of surface roughness, normal incidence; corrected for best fit background (see discussion).

The results of a series of measurements, with the beam incident at various angles, is shown in Figs. 17 and 18. In Fig. 17 a strong anomaly is present, which is substantially removed when a more judicious background is selected as shown in Fig. 18.

The slopes of these curves is close to 1.5. In Fig. 18 the individual curves exhibit close agreement with each other. More extensive research should be pursued to substantiate this type of agreement.

Scatter as a Function of Wavelength

An original intent of the research reported here was to measure the scattered light distribution of samples at two different wavelengths: one in the visible portion of the spectrum and a second in the mid-infrared. As research progressed, it became evident that satisfactory results could not be obtained if the original wavelength regions were retained. A decision was made to use two wavelengths in the visible portion of the spectrum for the following reasons:

- (1) Two measurements in such widely separated regions of the spectrum would require that the separate laser sources be used. It is unlikely that these sources could be aligned to illuminate identical portions of the sample under test.
- (2) In order to measure the light levels associated with wide angle scatter, two separate detectors are necessary. It is difficult to insure that the absolute energy and the collection area of each detector be well known.
- (3) A reference sample that would be useful in both the infrared and visible was unknown.

In contrast, the availability of an argon-ion laser simplified the associated problems of measurement immediately. A prism internal to the cavity of the laser permits selection of several laser lines without the alteration of beam direction. The lines used were 514.5 nm (green) and 459.0 nm (blue). A photomultiplier exhibits good response at each of the available lines allowing a single detector configuration to be used for both wavelengths. Furthermore, the diffuse reflectance of MgO exceeds .98 throughout the spectral region of the laser. This allowed an MgO sample to be used as a reference. Detector response, laser power output, reflectance of intermediary mirrors, and transmittance of the fiber-optic probe could all be reduced to a single proportionality factor. This factor is obtained by taking the ratio of the integrated diffuse reflectance of the MgO reference at the two wavelengths of concern.

To measure relative scatter as a function of wavelength, an MgO reference sample is placed in the sample holder. Its diffuse reflectance is measured at the first of the two wavelengths. The reference is removed from the sample holder and replaced with the sample under study. The diffuse reflectance of the sample is then measured at the first wavelength. The laser is then tuned to the second of the chosen wavelengths, and the diffuse

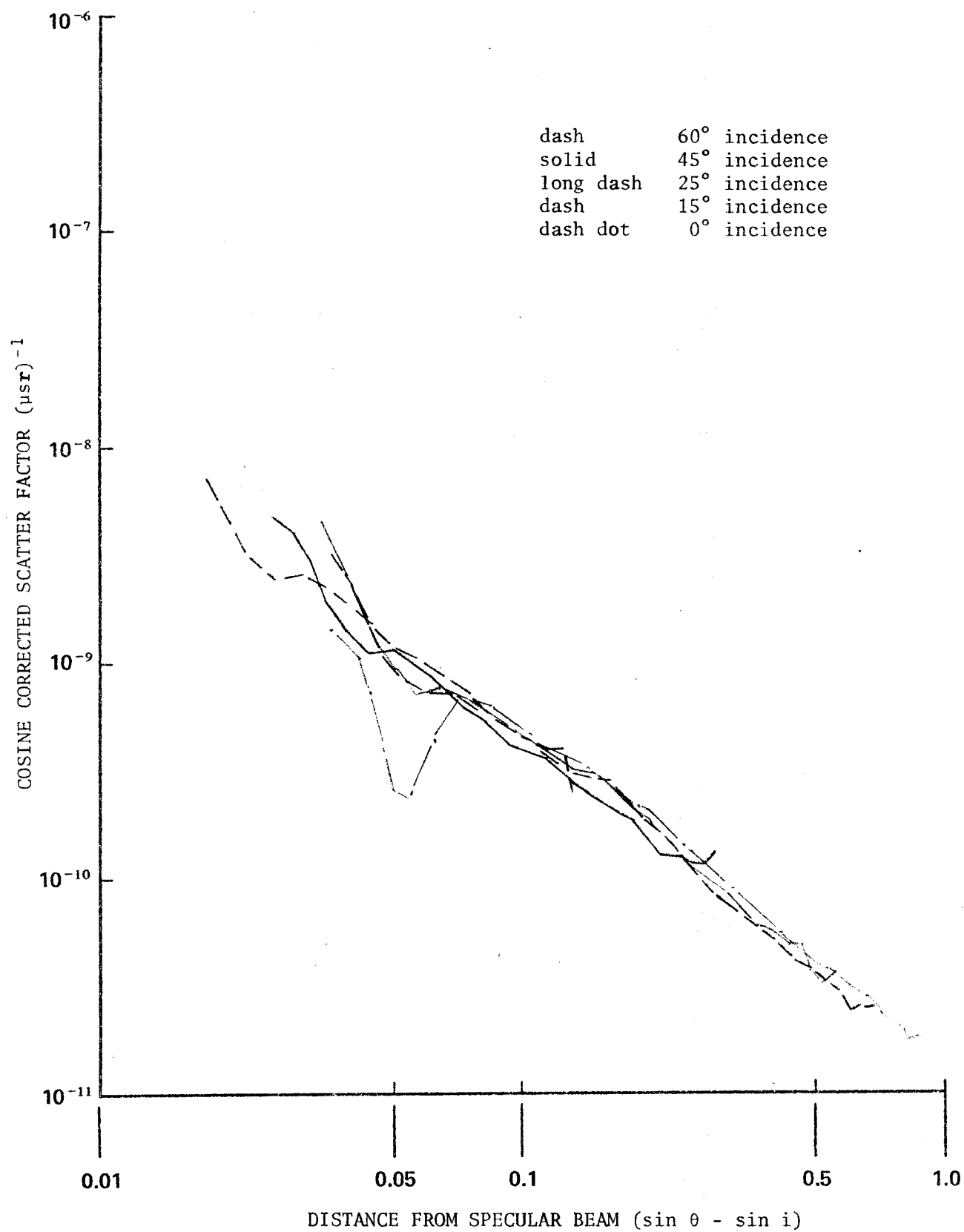


Fig. 17. Scatter from sample #247 as a function of angle of incidence corrected for background measured in conjunction with this data.

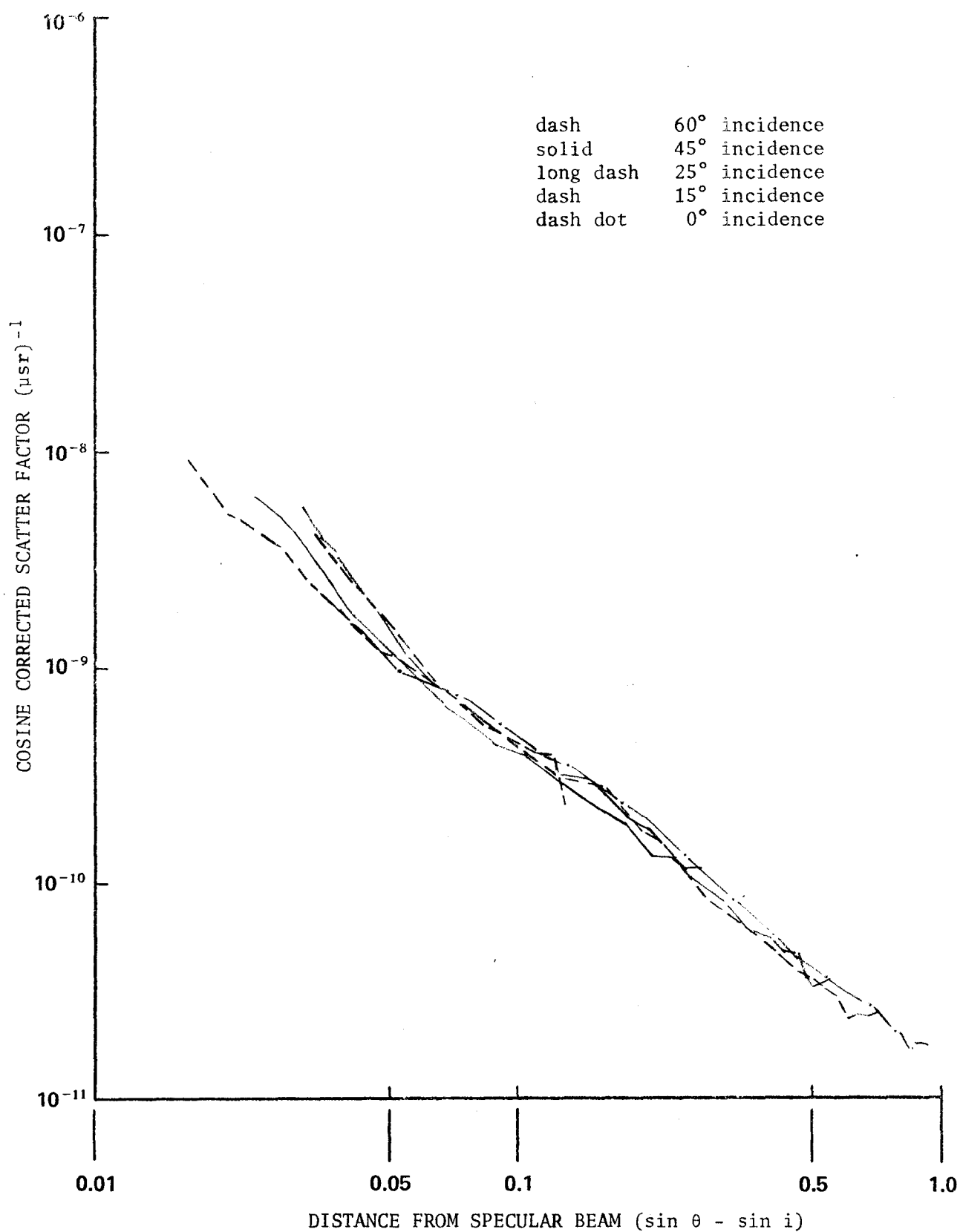


Fig. 18. Scatter from sample #247 as a function of angle of incidence corrected for best fit background (see discussion).

reflectance is measured at this wavelength. (It should be noted that the change of wavelength does not alter the position of any optics outside the laser cavity, and that the laser beam in both cases strikes the same portion of the sample.) The test sample is now replaced by the reference sample in the sample holder, and the diffuse reflectance of the reference at the second wavelength is measured.

A numerical integration performed on the data taken from the reference measurements yields the relative intensity of the incident radiation with the thru-put of the entire system (reflectance, transmission, photocathode response and electronics) taken into account. The ratio of the resultant integrations is a scale factor that is then used to "correct" the measurements from the test sample for all effects except for wavelength. The result of these measurements is shown in Figs. 19, 20, & 21. All measurements were made at normal incidence.

In order to predict the wavelength dependence of the scattering function for large angles, we first combine Eqs. (69) and (71), obtaining

$$I = \frac{2-s}{2\pi} \phi_s(1) \rho^{-s}. \quad (73)$$

The form of the scattering function should not vary with wavelength, so the slope s should not be dependent on wavelength. Furthermore, if the scattered fraction of the flux is small, the total scattered flux is given by

$$\phi_H = 1 - e^{-(2\pi)^2 \hat{\sigma}_w^2} \approx (2\pi)^2 (\sigma_w/\lambda)^2, \quad (74)$$

so that ϕ_H , and therefore I , should vary inversely as the square of the wavelength. This is consistent with the data.

Numerical Integration of the Scattered Light Distributions

A numerical integration of the scattered light distribution yields ϕ_H , the net scattered flux if we can assume the distribution is rotationally symmetric, and that the contribution due to the fraction of light not included in the integral is small. These assumptions appear reasonable as we have no evidence to the contrary. The results of these integrations are listed in Table 1.

Further, from the theory we know that the rms surface roughness, $\hat{\sigma}_w$, is given by

$$\hat{\sigma}_w^2 = \frac{1}{(2\pi)^2} \ln \left(1 + \frac{\phi_H}{\phi_C} \right). \quad (75)$$

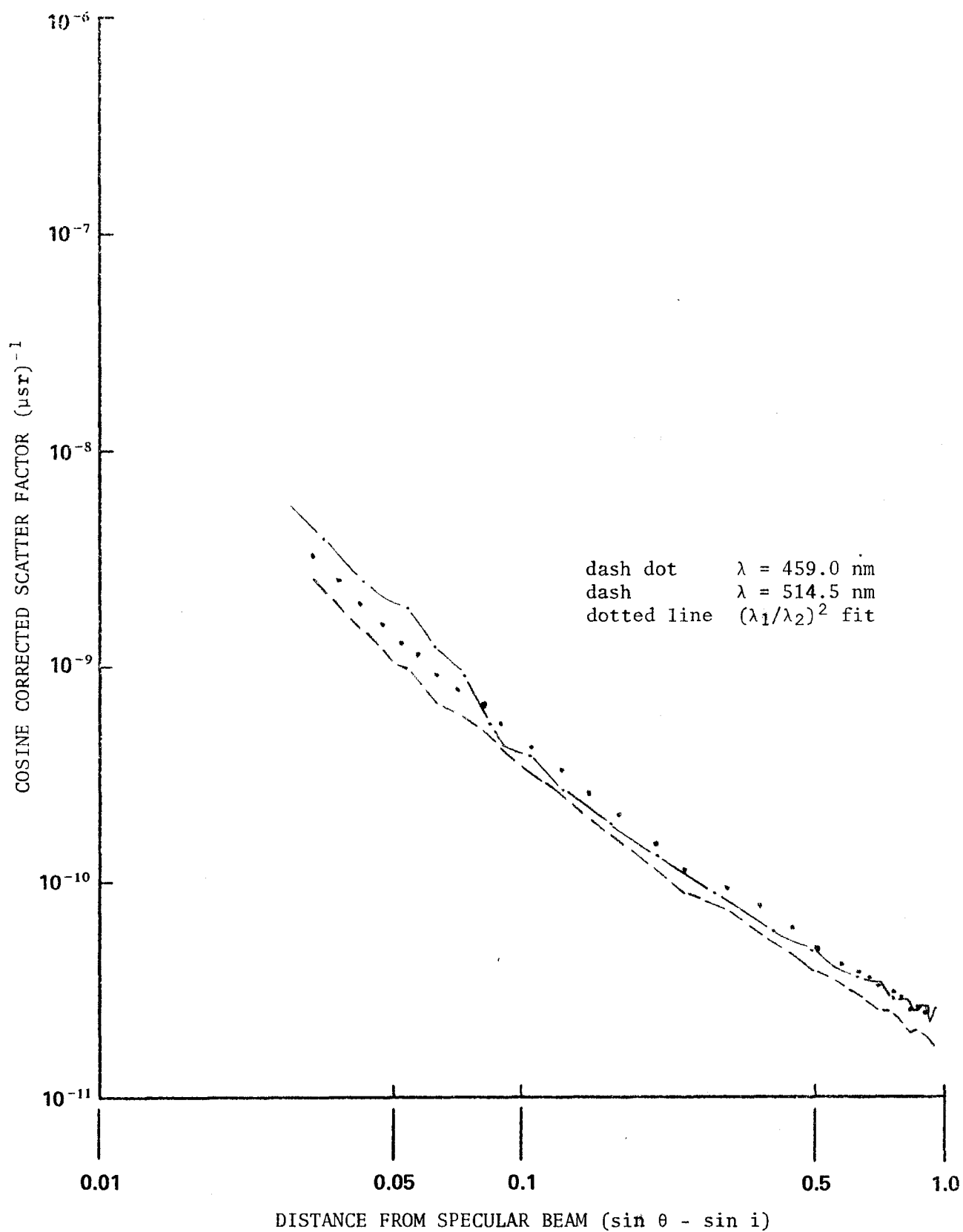


Fig. 19. Scatter as a function of wavelength, sample #236.

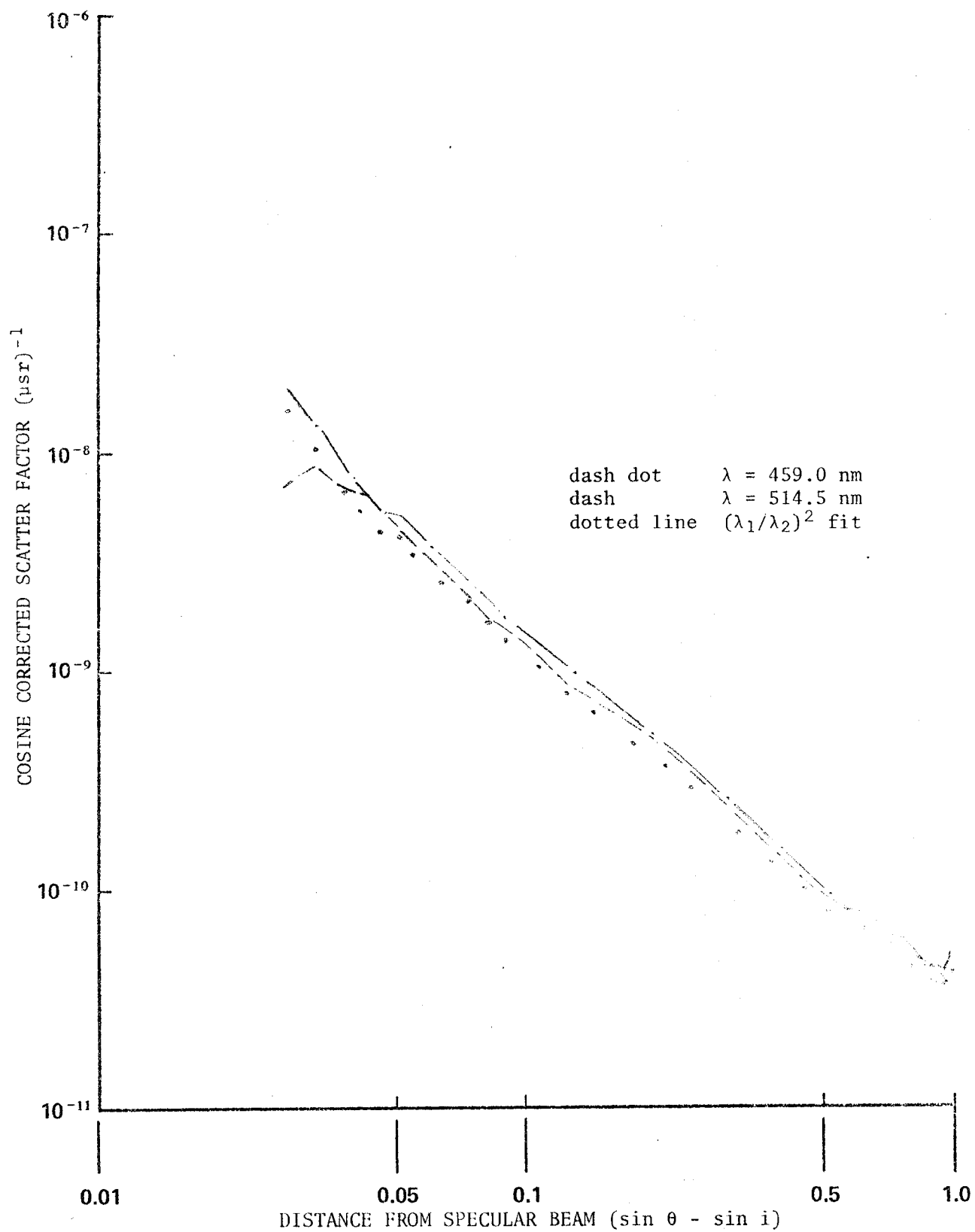


Fig. 20. Scatter as a function of wavelength, sample #247.

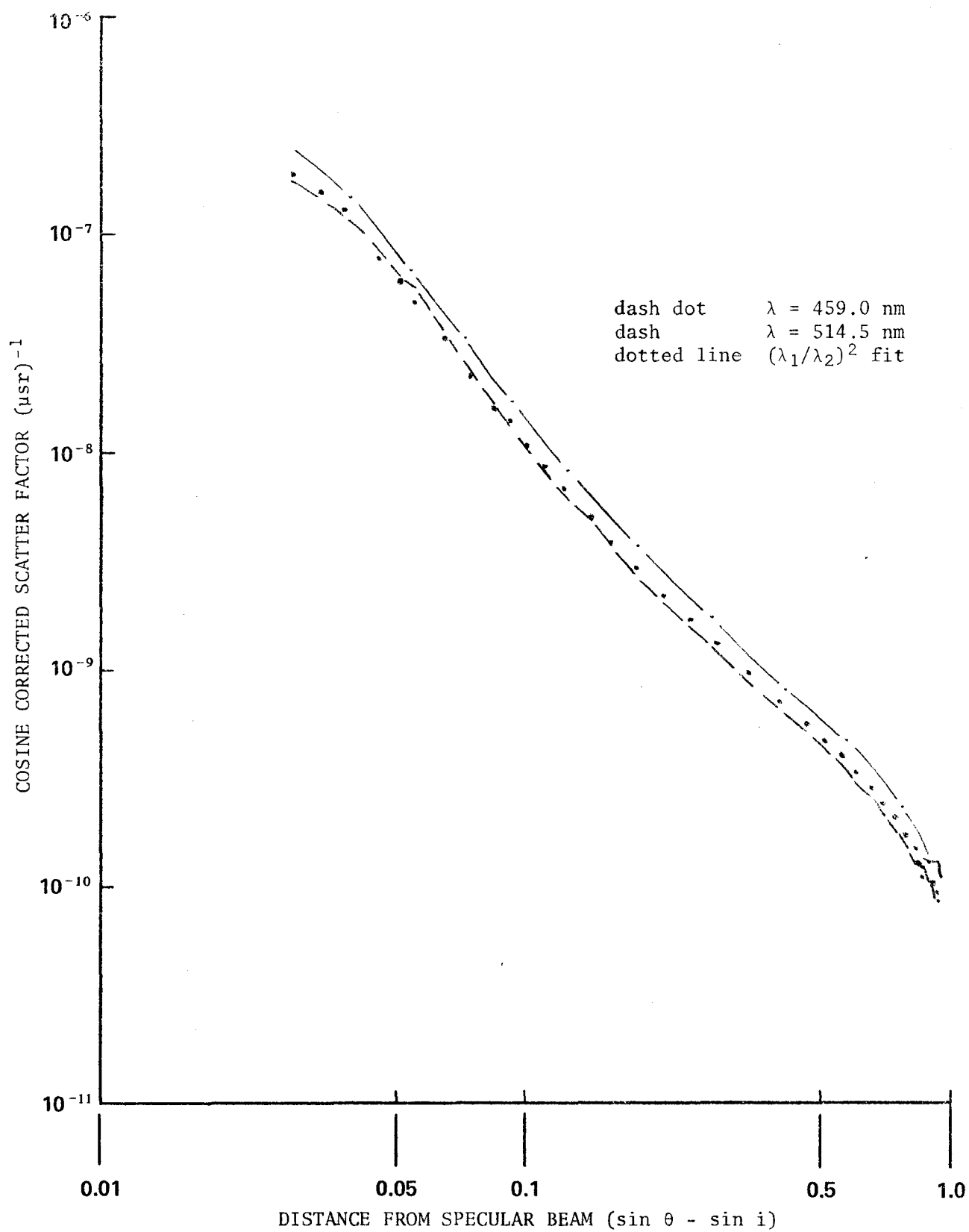


Fig. 21. Scatter as a function of wavelength, sample #EDF 3-11.

Since $\Phi = \Phi_H + \Phi_C$, we can make the assumption that $\Phi_C = \Phi$ when Φ_H is very small. This is the case for all but the two ground surfaces, samples 221 and 229. The rms roughness is then given by

$$\sigma_w^2 \cong \frac{1}{(2\pi)^2} \ln \left(1 + \frac{\Phi_H}{\Phi} \right) \lambda^2. \quad (76)$$

Calculations of σ_w are given in Table 2. These results exhibit an order of magnitude agreement with the estimated roughness values.

TABLE 1
RESULTS OF THE NUMERICAL INTEGRATION
OF THE SCATTERED LIGHT DISTRIBUTIONS

<u>Sample No.</u>	<u>Integrated Scatter (%)</u>
236	0.014
247	0.033
EDF 3-4	0.038
222	0.046
EDF 3-11	0.38
229	69.5*
221	71.1*

*In the case of the ground samples, no specular beam was apparent and these figures represent the total diffuse reflectance.

TABLE 2
CALCULATED RMS SURFACE ROUGHNESS, σ_w

<u>Sample No.</u>	<u>Φ_H/Φ</u>	<u>σ_w (nm)</u>
236	0.00014	0.95
247	0.00033	1.5
EDF 3-4	0.00038	1.6
222	0.00046	1.8
EDF 3-4	0.0038	5.1

SUGGESTIONS FOR FUTURE RESEARCH

In conducting the research presented in this report several ideas for improving the measurements and our understanding of surface scattering have been kindled. These ideas are summarized below.

- (1) A redesign of the existing apparatus is possible that will allow one to scan through the specular beam and thus make measurements over the entire plane of incidence. This can be accomplished by introducing an offset into the fiber-optic probe.
- (2) Through the use of a lens to focus the incident laser beam onto the hemisphere an exact Fourier transform can be formed. Approximations involving the quadratic phase factor can then be eliminated.
- (3) An investigation of surface profiles using the techniques of stereo-electron microscopy could yield more accurate measurement of auto-correlation function and the surface height distribution.
- (4) Surfaces that are partially polished, and surfaces that are polished and then partially ground as well as materials other than glass should be investigated.

APPENDIX A

SAMPLE PREPARATION

This section deals with sample selection, polishing, cleaning and coating. An original goal of the research reported here was to choose samples that bracketed the types of surfaces typically produced in optical component manufacture. Coatings for these surfaces we produced were carefully controlled and in all cases we believe had less effect on overall scatter than did the condition of the substrates. All surface roughnesses are reported as a combination of coating plus substrate roughness.

Substrate Materials and Preparations

Samples used in these experiments were of two different types of glass. The hardness range of conventional optical glass was well bracketed by the choice of substrates. The large majority of the substrates were made of fused silica of the Homosil trademark. These substrates were of exceptional quality and essentially free from bubbles and sleeks. All substrates were 3.17 cm in diameter and 0.63-cm thick. Fused silica is one of the hardest of the conventional optical substrates. The remaining substrates were made of optical quality extra dense flint glass. The particular category in this case is known as EDF3. EDF3 is one of the softest optical glasses and it was chosen as a substrate for this particular reason.

Surface preparation of the different samples is outlined in Table 3. All samples were finished to be closely flat. Grinding and polishing procedures are more closely described by Mott (1971) and Orme (1972). Surface roughness in the samples varied from 1.0 nm to 3,000 nm. The EDF3 samples were much more prone to small scratches as might be expected. In all, thirty-two samples were prepared and of these, eight were selected for investigation.

Cleaning

The prepared samples were cleaned prior to coating with aluminum. Cleaning consisted of careful washing with Liquinox, a mild detergent, under very warm, filtered tap water. Such soaping was repeated three times for each individual sample. Samples were then mounted in a sample holder while held in distilled water. Once in a holder, samples were moved to an ultrasonic cleaner filled with distilled water for rinsing. Purity of the distilled water in the ultrasonic cleaner was monitored through resistance measurements. The water was changed several times, until it was substantially as pure as it was before the samples were added. Once rinsed the samples were set to dry in a dust-free atmosphere. Dry samples were removed from the sample holders and placed in individual boxes being supported by the edge of their backside. Mott (1971) used a similar cleaning technique, which he describes more completely.

Coating

Cleaned dry samples were then placed in a high vacuum chamber and coated to opacity with pure aluminum. Coating technique varied from the standard only in that excessive care was taken to allow the chamber to reach a pressure below 2×10^{-6} torr prior to coating. Opacity was monitored by watching the extinction of the tungsten evaporating filament through the substrates. The samples were allowed to cool to room temperature prior to removal from the chamber. Each coating run contained ten different samples. Once coated, samples were returned to their individual storage boxes. After all samples were coated, the best samples of each type were selected for measurement. This selection was made on the basis of individual inspection of each sample while held under a microscope illuminator in an otherwise dark room. Samples that had coating nonuniformities, streaks or pinholes were rejected as were those with waterspots, large scratches or otherwise questionable appearance. Prior to each scatter measurement run, samples were again individually inspected for flaws. Dust was removed using a commercially available pressurized air can. After each sample was measured for scatter, it was returned to its individual box.

TABLE 3

SURFACING PROCEDURES AND ROUGHNESSES

<u>Sample Number</u>	<u>Substrate Material</u>	<u>Lap Material</u>	<u>Polishing Medium</u>	<u>Polishing Time</u>	<u>Force Applied kg/cm²</u>	<u>Approximate Surface (nm) Roughness</u>
236	Quartz	Optical Quality Pitch	CeO*(milled 2000 hr)	8 hr	.2	1.0
			Distilled H ₂ O* w/same lap	8 hr	.2	
247	Quartz	Wood (end cut fir)	CeO (unmilled)	4 hr	.3	4.0
222	Quartz	Plate Glass	Al ₂ O ₃ (1μm diam)	1 hr	.12	12
221	Quartz	Cast Iron	Al ₂ O ₃ (2μm diam)	20 min	.15	100
229	Quartz	Cast Iron	Al ₂ O ₃ (30μm diam)	20 min	.15	1500
EDF3-4	EDF-3	Optical Quality Pitch	CeO(milled 2000 hr)	8 hr	.12	2.5**
			H ₂ O*(distilled w/same lap)	8 hr	.12	
EDF3-11	EDF-3	Optical Quality Pitch	CeO (milled 500 hr)	4 hr	.12	15**

*Closed circulation system.

**Soft glasses exhibit a strong tendency to scratch and sleek.

APPENDIX B

PROPERTIES OF THE FIBER-OPTIC PROBE

The fiber-optic bundle offers several unique advantages in the collection of the scattered radiation. Being rigid, it is self-supporting and, in effect, transfers the detector to the end of the fiber bundle. Furthermore, being small in cross-section, one is allowed to probe the space near the specular direction without the detector scattering light back towards the sample. Finally, fiber-optic bundles have the property that off-axis light leaves the bundle both attenuated and distributed away from the normal direction. Figures 22 and 23 illustrate this. Correct baffling between the end of the fiber-optic bundle and the detector can then eliminate much of the stray and background radiation.

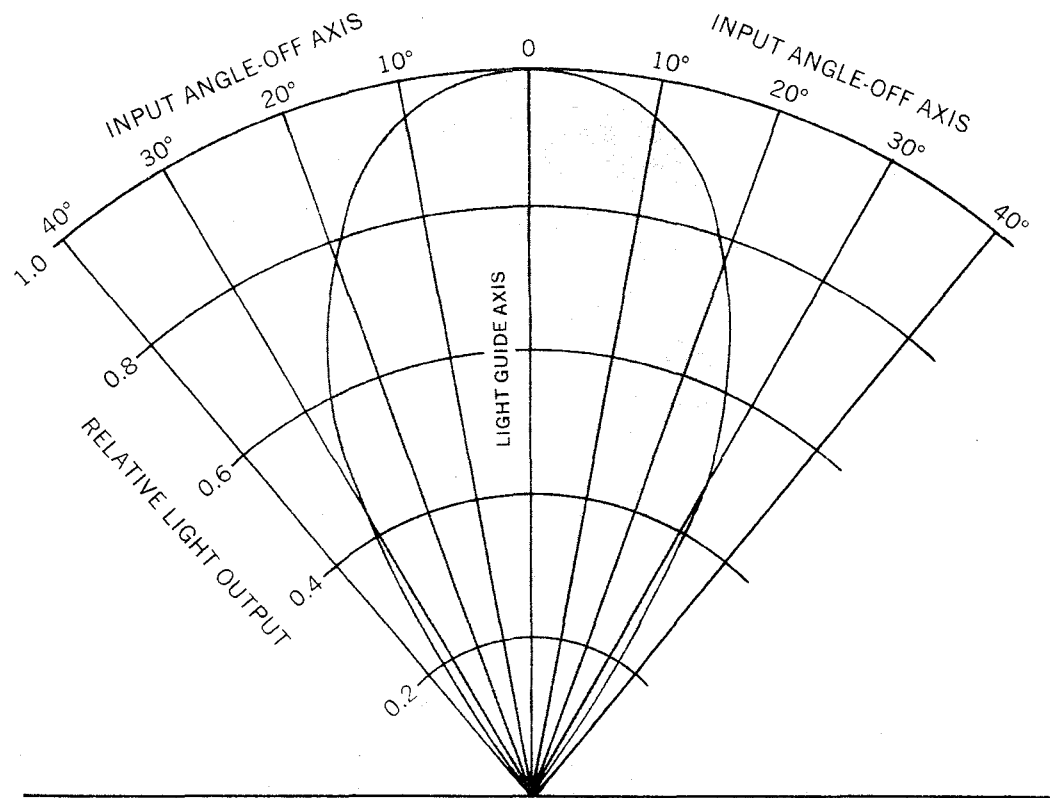


Fig. 22. Relative light output vs. input direction of collimated light for a fiber-optic probe.

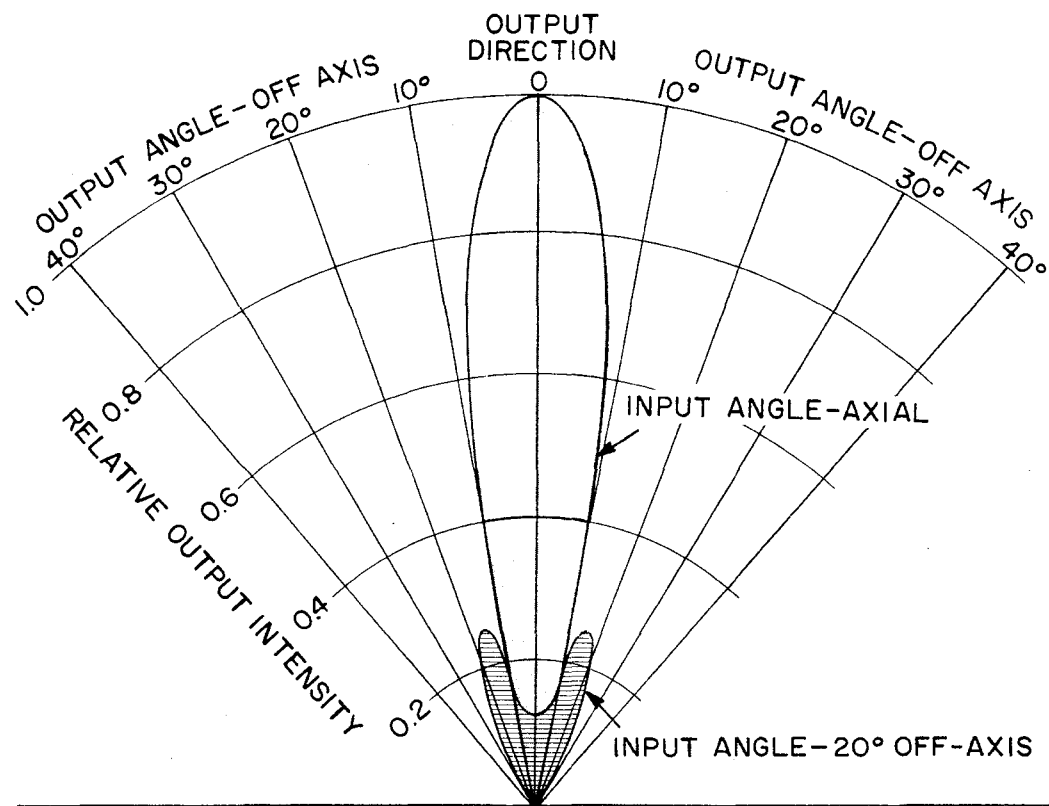


Fig. 23. Relative output intensity vs. output direction for a fiber-optic probe.

APPENDIX C

LITERATURE LISTING

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Forward scatter measurements are made on particles in solution. Measurements are all made in the plane of the incident and transmitted light. Single wavelength measurements at mercury green were made over a dynamic range of 10^6 .

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Beaglehole, D. and Hunderi, O., "Study of the Interaction of Light with Rough Metal Surfaces," *Phys. Rev. B*, 2:309-29, July, 1970.

This paper described experimental results in the measurement of the reflectivity and scattering of microscopically rough surfaces. Measurements made confirm the good fit to the authors' theory. The theory is based on a random distribution of spheres on a surface. Plasmon effects as well as the additional fields from induced currents are discussed. Comparison is made to the results predicted by scalar theory. Measurements fall in the wide angle category.

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Height Distribution of Surface Irregularities," *J. Opt. Soc. Am.*,
53:1389-94, Dec., 1963.

*Early theory of specular reflectance as developed
by Porteus and Bennett is applied to ground glass
surfaces. It is shown that the height distribu-
tion of a surface may be found by taking the in-
verse Fourier transform of the square root of the
coherent reflectance function. Wavelength vs.
surface grind are plotted.*

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faces," *J. Opt. Soc. Am.*, 60:1577, Nov., 1970.

*The scalar theory as developed by Davies and
Bennett and Porteus is reviewed. Instrumentation
is described which measures light scattered be-
tween 1.5 and 20 degrees from the specular direc-
tion. Measurements are made with the light at
normal incidence to the sample. Experimental
technique is described in detail.*

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(Abstract follows on next page.)

The roughness of a plane surface is related to its specular reflectance. Scalar theory is used and an expression for reflectance dependent upon the rms height of surface irregularities and the autocovariance length is derived following the work of Davies.

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Technique for producing and preparing extremely smooth optical surfaces is discussed. Ellipsometric methods are employed to measure surface films on samples that are highly polished.

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Describes a detailed experimental study to explore the influence of surface roughness conditions on the reflection characteristics of metal surfaces for nonthermal radiation. The test surfaces were prepared by standard optical grinding techniques using a range of grit sizes. Biangular, specular, and hemispherical-angular reflectance measurements are discussed in terms of the optical rms surface roughness, the wavelength of the reflected radiation, and the surface material. The results are compared with available predictions from theoretical analysis.

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Beckmann theory of scattering is applied to the particular case of dielectric laser mirrors. Wavelength dependent expressions are derived and qualitative experimental results are presented. The case of non-normal incidence is considered and measurements were made in this mode.

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Dalmas, J., "Diffusion de la Lumière par une Demi-Sphère, Posée sur une Surface Plane, D'un Matériau de Même Nature," *Nouv. Rev. d'Optique Appliquée*, 1:167-70, Jan., 1970.

(Abstract follows on next page.)

Scattered light from a hemisphere on a plane surface of the same material is considered. One solution is arrived at by integrating the Helmholtz equation using a separation of variable technique. Employing the method of Twersky a good approximation to metallic surfaces can be made by assuming perfect conduction.

Dave, J. V. and Gazdag, J., "A Modified Fourier Transform Method for Multiple Scattering Calculations in a Plane Parallel Mie Atmosphere," *Appl. Opt.*, 9:1457, June, 1970.

Davies, H., "The Reflection of Electromagnetic Waves from a Rough Surface," *Proc. IEEE*, 101:209-14, July, 1954.

A "scalar scattering" theory is presented which considers just the phase modulation of the incident and outgoing light by the height variations along the surface. The resultant radiation distribution thus depends upon the phase of the wavelets, the phase of the incident field when it reaches a point on the surface. If the height variation is assumed gaussian with an rms deviation σ , this theory predicts the ratio of the specular reflectance of a smooth surface to vary as

$$\frac{R_{\sigma}}{R_0} \propto e^{-(4\pi\sigma/\lambda)^2}.$$

Similarly, predictions about the angular distribution of the scattered light are also made.

Depew, C. A. and Weir, R. D., "Surface Roughness Determination by the Measurement of Reflectance," *Appl. Opt.*, 10:969-70, April, 1970.

Experimental work done to determine the surface roughness of metals using reflectance measurements, and the Bennett and Porteus theory. Comparison with mechanical measurements is made. The results are said to substantiate the results of Bennett and Porteus.

Dietz, R. W. and Bennett, J. M., "Bond Tested Techniques for Producing Supersmooth Optical Surfaces," AD-644 340, Feb., 1966.

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A method for producing very smooth surfaces on optical materials such as fused quartz or glass is described. The material being polished is kept immersed in a slurry of polishing compound and the final polishing is done with water containing no abrasive. Surfaces as smooth as 3A rms have been produced by this method.

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Elson, J. M. and Ritchie, R. H., "Photon Interactions at a Rough Metal Surface," *Phys. Rev. B*, 4:4129, Dec., 1971.

The process of diffuse scattering and surface-plasmon creation by photons at a rough metal surface is discussed. A theoretical analysis employing quantum perturbation theory is used to calculate this scatter assuming a free electron model. Results that consider polarization are obtained and compared to those of Davies. The authors argue that their approach is better than that of Davies and that in fact his approach fails in the limit.

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Experiments are described that measure both plasmon-induced scattering and roughness-induced light scattering in aluminum films. In particular, the more recent theory of Elson and Ritchie is compared to results predicted by the scalar theory. Particular attention is paid to near UV wavelengths.

Estes, L. E., Narducci, L. M. and Tuft, R. A., "The Scattering of Light from a Rotating Ground Glass," Elec. Eng. Dept., Worcester Polytechnic Institute, 1971.

The statistics of a coherent light beam scattered by a rotating ground are investigated. The scattered light amplitude is confirmed to be a stochastic Gaussian variable. The scattered light power spectrum is shown to be a Gaussian function of the frequency. The experimental results agree very closely with theoretical predictions.

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The work of C. T. Tai is applied to electromagnetic scattering in radially inhomogeneous spheres. In particular equations are derived for computer use. The study applies to antenna theory.

Germogenova, O. A. and Siegel, A., "Intensity Fluctuations in Forward Scattering and Temporal Coherence," *Appl. Opt.*, 8:1849, Sept., 1969.

Forward scattering by a nonergodic system of identical particles is considered. The relation between the temporal correlation function of the scattered radiation and its second order

intensity moments is established. Estimates of this effect using infrared laser beam propagating through fog give results comparable to those of Tatarskii.

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