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Report No. MSD-P69-144

Contract No. 00019-68-C-02 **47**

AD 859286

COLLOCATION FLUTTER ANALYSIS STUDY

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VOLUME II.

FLUENC - COMPUTER PROGRAM TO CALCULATE
STRUCTURAL INFLUENCE COEFFICIENTS

APRIL 1969



MISSILE SYSTEMS DIVISION

HUGHES

HUGHES AIRCRAFT COMPANY

SEP 25 1969

C O F A
C O L L O C A T I O N F L U T T E R A N A L Y S I S
S T U D Y

VOLUME II

FLUENC - Computer Program to Calculate
Structural Influence Coefficients

Prepared by the Dynamics and Environment
Section Personnel, Hughes Aircraft Company
Under Contract No. 0019-68-C-0247

April 1969

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ABSTRACT

A displacement solution for the calculation of structural influence coefficients (SIC's) is presented. The formulation utilizes the lumped parameter approach that is consistent with collocation flutter solutions. The structure is synthesized as concentrated mass elements connected by massless elastic plates and/or beams. There are two methods of generating the mass matrix; they are: 1) lumped concentrated mass points, 2) consistent mass matrices. Along with the calculation of the SIC's, the natural vibration modes and frequencies are calculated. There are two options for punching out the flexibility matrix for use in subsequent COFA computer programs. Option 1, punches out the full flexibility matrix; Option 2, punches out the reduced flexibility matrix eliminating the rows and columns pertaining to structural attach points.

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1.0 INTRODUCTION

In order to determine the aeroelastic behavior of a wing or control surface, it is necessary to know the aerodynamics, elastic properties and mass distributions of the structure. The overall aeroelastic analysis is usually divided into four separate parts as shown in Figure 1.

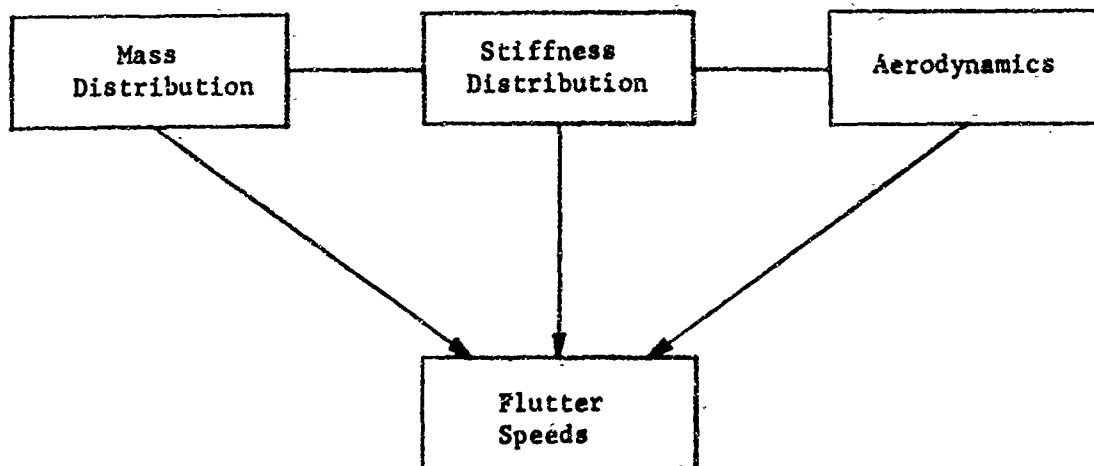


Figure 1. Analysis Procedure

This portion of the report describes the computation of the mass and stiffness distribution. The geometry of a wing or tail surface is too complex for the successful use of closed form analytical techniques. Therefore, a numerical type of analysis must be used. The end product of this analysis is the generation of overall influence coefficient and mass matrices referred to a set of node points arbitrarily picked on the surface of the structure. The finite element method (see Refs. 2 and 3) was used to form the required matrices for a planar structure. This technique is especially suited to solve complex structures and as used in the analysis is general enough to handle the following:

1. Combinations of beam and plate elements
2. Arbitrary boundary conditions
3. Lumped or distributed stiffnesses and masses

A discussion of the theory and computer program which calculates the influence coefficient and the mass matrix as well as the structural modes and frequencies is given in the following sections.

2.0 NOMENCLATURE

C	=	Unknown Boundary Constants
D	=	Plate Rigidity Constant
E	=	Modulus of Elasticity
F	=	Force
K	=	Stiffness Coefficients
M	=	Bending/Torsional Moment
p	=	Pressure
T	=	Coordinate Transformation
t	=	Thickness
w	=	Linear Displacement in z direction
x, y, z	=	Coordinate Axes
s	=	Linear Displacement
$\frac{d^2}{dx^2}$	=	Curvature
ρ	=	Density
σ	=	Stress
ν	=	Poisson's Ratio
$\frac{\partial}{\partial x}$	=	Partial Derivative
[]	=	Square Matrix
{ }	=	Column Matrix
[]	=	Row Matrix

3.0 TECHNICAL DISCUSSION

3.1 Influence Coefficients

The stiffness method approach is first used to obtain an overall stiffness matrix of the structure. This matrix is reduced by partitioning and then inverted to obtain the influence coefficients at any desired set of control points. The number of control points are denoted by N . At each node, three degrees of freedom are specified: two rotations and the normal displacement. Therefore, a stiffness matrix of approximately $3N$ degrees of freedom is first formed by superimposing individual plate and plane grid beam element global coordinate matrices. The matrix will be somewhat smaller than $3N$ degrees of freedom since boundary restraint conditions will reduce the size of the matrix. To illustrate the matrix condensation method used in the computer program, we will assume that we have N control point normal displacements and M displacements which must be eliminated. The overall stiffness matrix is given as

$$[K] = \begin{bmatrix} K_{NN} & K_{NM} \\ K_{MN} & K_{MM} \end{bmatrix} \quad (1)$$

The structural equilibrium matrix equation can be written as

$$\begin{bmatrix} K_{NN} & K_{NM} \\ K_{MN} & K_{MM} \end{bmatrix} \begin{Bmatrix} \delta_N \\ \delta_M \end{Bmatrix} = \begin{Bmatrix} F_N \\ F_M \end{Bmatrix} \quad (2)$$

We now assume that forces at the points to be eliminated are small and can be neglected. Therefore,

$$\begin{bmatrix} K_{NN} & K_{NM} \\ K_{MN} & K_{MM} \end{bmatrix} \begin{Bmatrix} \delta_N \\ \delta_M \end{Bmatrix} = \begin{Bmatrix} F_N \\ 0 \end{Bmatrix} \quad (3)$$

or

$$[K_{NN}]\{\delta_N\} + [K_{NM}]\{\delta_M\} = \{F_N\}$$

and

$$[K_{MN}]\{\delta_N\} + [K_{MM}]\{\delta_M\} = \{0\}$$

Therefore

$$\{\delta_M\} = -[K_{MM}]^{-1} [K_{MN}]\{\delta_N\} \quad (3a)$$

and

$$\left([K_{NN}] - [K_{NM}][K_{MM}]^{-1}[K_{MN}] \right) \{\delta_N\} = \{F_N\}$$

and since

$$[K_{MN}]^T = [K_{NM}]$$

we have

$$\{\delta_N\} = \left([K_{NN}] - [K_{MN}]^T [K_{MM}]^{-1} [K_{MN}] \right)^{-1} \{F_N\} \quad (4)$$

If we now let

$$[f_{NN}] = \left([K_{NN}] - [K_{MN}]^T [K_{MM}]^{-1} [K_{MN}] \right)^{-1}$$

then Equation (4) can be written as

$$\{\delta_N\} = [f_{NN}] \{F_N\} \quad (5)$$

The matrix $[f_{NN}]$ is called the structural influence coefficient matrix. The application of loads at the control points yield displacements at the control points by carrying out the matrix multiplication indicated in Equation (5).

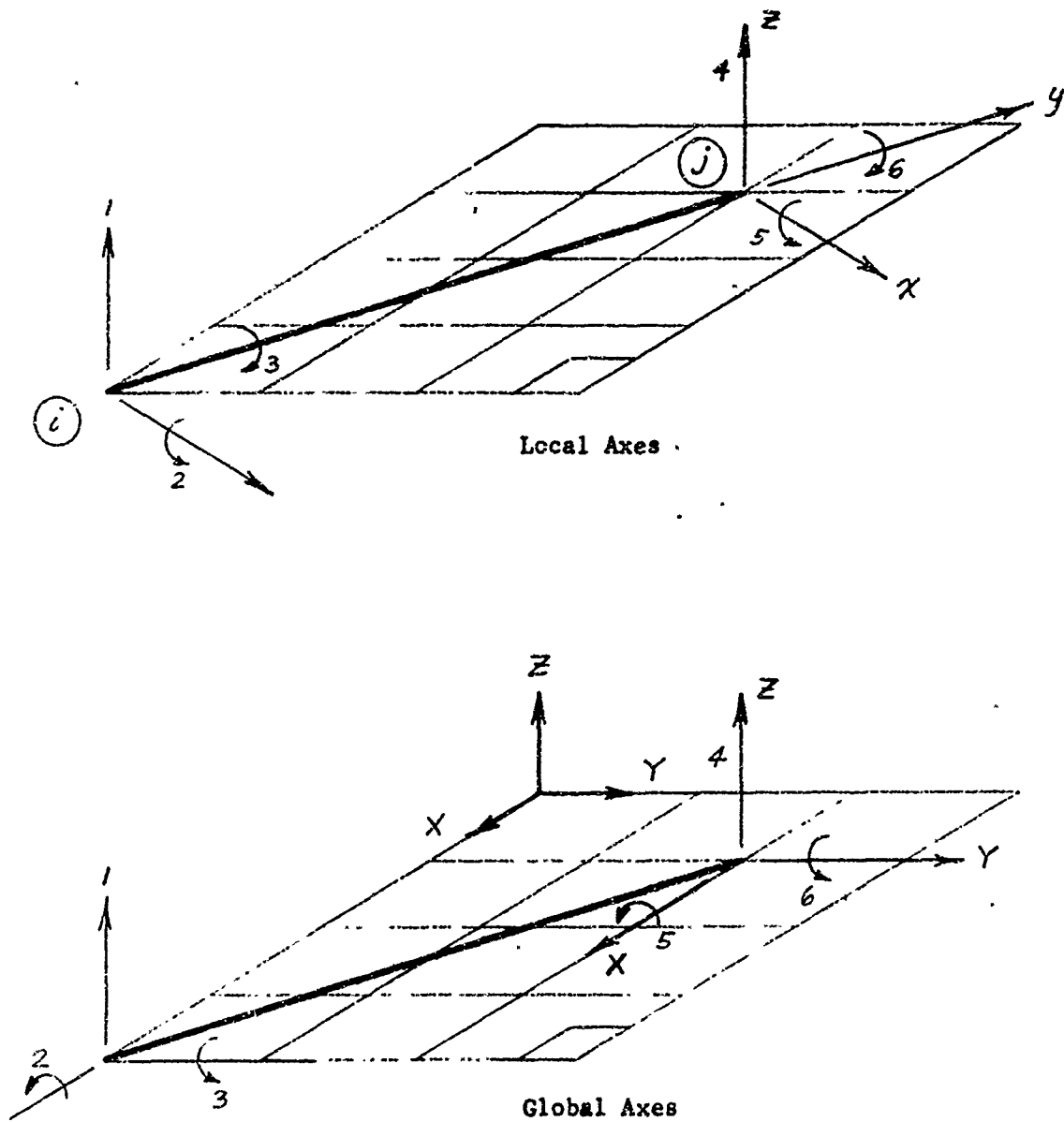


Figure 2. Plane Grid Beam Local and Global Coordinate System

The computer program FLUENC carries out the required operations to obtain the influence coefficient matrix $[f_{NN}]$. A detailed description of the program can be found in Section 4.0. The program is written to form a 50 x 50 influence coefficient matrix. The influence coefficient matrix is punched out on cards in a format compatible with the Collocation Flutter Program.

The plane grid beam global coordinate stiffness matrix used in the program was obtained from Reference 1 and is given in Table 1. The local and global coordinate systems are shown in Figure 2. The figure also contains the sign convention for the six degrees of freedom for each element.

The triangular plate stiffness matrix given in Reference 2 was used in the computer program. The plate element can be materially or geometrically orthotropic as treated in Reference 3. Stiffened plates can be considered to be geometrically orthotropic. The sign convention and nodal degrees of freedom are shown in Figure 3.

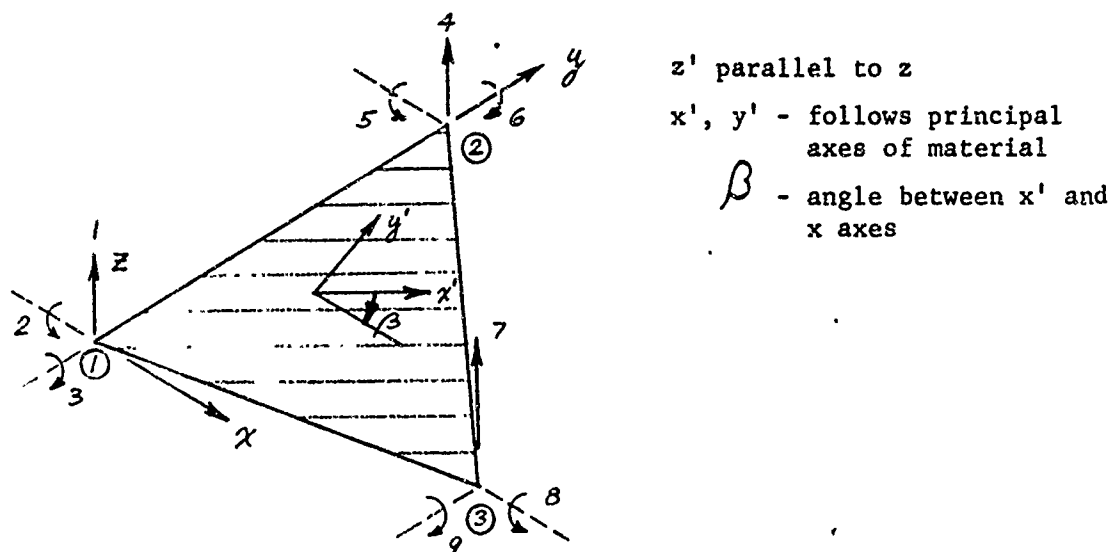


Figure 3. Orthotropic Triangular Element

Following the analysis given in Reference 2, the deflection shape of the plate element is assumed to be of the form

$$w = C_1 + C_2 x + C_3 y + C_4 x^2 + C_5 xy + C_6 y^2 + C_7 x^3 + C_8 (xy^2 + x^2y) + C_9 y^3$$

or

$$w = [N] \{C\} \quad (6)$$

The unknown constants $C_1, C_2, \dots, C_9$ can be written in terms of the nodal displacements $\delta_1, \delta_2, \dots, \delta_9$ by using the boundary conditions

$$\begin{aligned} \text{at } x=0, y=0 & \quad \begin{cases} w = \delta_1 \\ \partial w / \partial y = \delta_2 \\ \partial w / \partial x = -\delta_3 \end{cases} \\ \text{at } x=0, y=y_2 & \quad \begin{cases} w = \delta_4 \\ \partial w / \partial y = \delta_5 \\ \partial w / \partial x = -\delta_6 \end{cases} \\ \text{at } x=x_3, y=y_3 & \quad \begin{cases} w = \delta_7 \\ \partial w / \partial y = \delta_8 \\ \partial w / \partial x = -\delta_9 \end{cases} \end{aligned} \quad (7)$$

Using Equation (6) in conjunction with the boundary conditions given by Equation (7) yields

$$\begin{Bmatrix} \delta_1 \\ \delta_2 \\ \delta_3 \\ \delta_4 \\ \delta_5 \\ \delta_6 \\ \delta_7 \\ \delta_8 \\ \delta_9 \end{Bmatrix} = [N] \begin{Bmatrix} C_1 \\ C_2 \\ C_3 \\ C_4 \\ C_5 \\ C_6 \\ C_7 \\ C_8 \\ C_9 \end{Bmatrix} \quad (8)$$

where $C =$

$$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & y_2 & 0 & 0 & y_2^2 & 0 & 0 & y_2^3 \\ 0 & 0 & 1 & 0 & 0 & 2y_2 & 0 & 0 & 3y_2^2 \\ 0 & -1 & 0 & 0 & -y_2 & 0 & 0 & -y_2^2 & 0 \\ 1 & x_3 & y_3 & x_3^2 & x_3 y_3 & y_3^2 & x_3^3 & x_3 y_3^2 + x_3^2 y_3 & y_3^3 \\ 0 & 0 & 1 & 0 & x_3 & 2y_3 & 0 & 2x_3 y_3 + x_3^2 & 3y_3^2 \\ 0 & -1 & 0 & -2x_3 & -y_3 & 0 & -3x_3^2 & -(y_3^2 + 2x_3 y_3) & 0 \end{bmatrix}$$

The constant vector $\{c\}$ can be obtained in terms of the nodal displacements by inverting the matrix $[C]$. Therefore,

$$\{c\} = [C]^{-1} \{\delta\} \quad (9)$$

The curvatures for a flat plate element are given by

$$\{\epsilon\} = \begin{Bmatrix} \epsilon_x \\ \epsilon_y \\ \epsilon_{xy} \end{Bmatrix} = - \begin{Bmatrix} \partial^2 w / \partial x^2 \\ \partial^2 w / \partial y^2 \\ 2 \partial^2 w / \partial x \partial y \end{Bmatrix} \quad (10)$$

Substituting Equation (6) into Equation (10) yields

$$\{\epsilon\} = [Q] \{c\} \quad (11)$$

where

$$[Q] = \begin{bmatrix} 0 & 0 & 0 & -2 & 0 & 0 & -4x & -2y & 0 \\ 0 & 0 & 0 & 0 & 0 & -2 & 0 & -2x & -6y \\ 0 & 0 & 0 & 0 & -2 & 0 & 0 & -(4x+4y) & 0 \end{bmatrix}$$

Substituting Equation (9) into Equation (11) yields

$$\{\epsilon\} = [Q] [C]^{-1} \{\delta\} = [B] \{\delta\} \quad (12)$$

If initial strains are neglected then the moment-curvature relationships can be written in the form

$$\{\sigma\} = \begin{Bmatrix} M_x \\ M_y \\ M_{xy} \end{Bmatrix} = [D] \{\epsilon\} \quad (13)$$

where

$$[D] = \begin{bmatrix} D_x & D_1 & 0 \\ D_1 & D_y & 0 \\ 0 & 0 & D_{xy} \end{bmatrix} \quad (14)$$

for a materially or geometrically orthotropic plate. For an isotropic plate Equation (14) reduces to

$$[D] = \frac{E t^3}{12(1-\nu^2)} \begin{bmatrix} 1 & \nu & 0 \\ \nu & 1 & 0 \\ 0 & 0 & \frac{1-\nu}{2} \end{bmatrix} \quad (15)$$

The $[D]$ matrix must undergo a transformation if the principal axes of the material do not coincide with the local coordinate axes. The components of strain in one coordinate axes system are related to the components of strain in another coordinate axes system by the matrix equation

$$\{\epsilon'\} = [T]^T \{\epsilon\} \quad (16)$$

(The prime refers to the components of strain referred to the $x'-y'$ axes in Figure 3)

where

$$[T]^T = \begin{bmatrix} \cos^2 \beta & \sin^2 \beta & -2 \sin \beta \cos \beta \\ \sin^2 \beta & \cos^2 \beta & 2 \sin \beta \cos \beta \\ \sin \beta \cos \beta & \sin \beta \cos \beta & \cos^2 \beta - \sin^2 \beta \end{bmatrix} \quad (17)$$

Since the internal work is constant no matter which coordinate system is used

$$\{\sigma'\}^T \{\epsilon'\} = \{\sigma\}^T \{\epsilon\} \quad (18)$$

or by Equation (13)

$$\{\epsilon'\}^T [D'] \{\epsilon'\} = \{\epsilon\}^T [D] \{\epsilon\}$$

and by using Equation (16)

$$\{\epsilon\}^T [T] [D'] [T]^T \{\epsilon\} = \{\epsilon\}^T [D] \{\epsilon\}$$

Therefore

$$[D] = [T] [D'] [T]^T \quad (19)$$

The stiffness matrix for a typical element ① ② ③ is given by

$$[K] = \iint_A [B]^T [D] [B] dx dy \quad (20)$$

or by Equations (12) and (19)

$$[K] = [C^{-1}]^T \left(\iint_A [Q]^T [T] [D'] [T]^T [Q] dx dy \right) [C]^{-1} \quad (21)$$

Now let

$$[\bar{D}] = \iint_A [Q]^T [T] [D'] [T]^T [Q] dx dy$$

and carrying out the indicated matrix multiplications yields

$$[\bar{D}] = \iint_A (\text{see Table 1}) dx dy \quad (22)$$

In order to simplify the integration required for evaluating the matrix in Equation (22), it is suggested in Reference 2 that the independent variables be changed as shown in Figure 4.

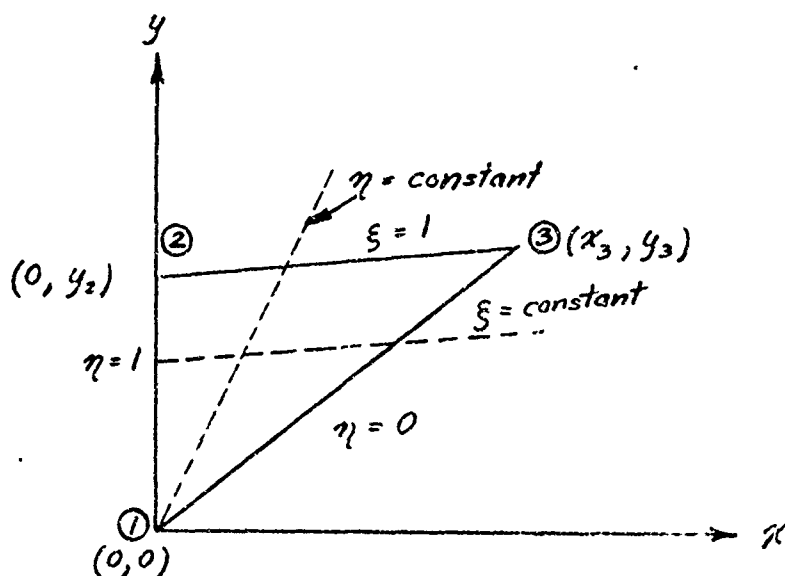


Figure 4
Coordinate Transformation

The relationships

$$\begin{aligned} x &= \xi (1 - \eta) x_3 \\ y &= \xi [(1 - \eta) y_3 + \eta y_2] \end{aligned} \quad (23)$$

are used for the change of variables. The terms in Equation (22) can now be evaluated by using the relationship

$$I(x^m, y^n) = \iint x^m y^n dx dy$$

or

$$I(x^m, y^n) = \iint x^m y^n |J(x, y)| d\xi d\eta \quad (24)$$

where

$$J(x, y) = \begin{vmatrix} \frac{\partial x}{\partial \xi} & \frac{\partial x}{\partial \eta} \\ \frac{\partial y}{\partial \xi} & \frac{\partial y}{\partial \eta} \end{vmatrix} \quad (25)$$

Substituting Equation (23) into Equation (25) yields

$$J(x, y) = \xi x_3 y_2 \quad (26)$$

Substituting Equations (23) and (26) into Equation (24) yields

$$I(x^m, y^n) = \int_0^1 \int_0^1 \xi^{m+n+1} (1-\eta)^m [(1-\eta)y_3 + \eta y_2]^n x_3^{m+1} y_2 d\xi d\eta \quad (27)$$

which can easily be evaluated for any m and n.

3.2 Mass Matrix

D'Alembert's principle can be used for the formulation of the mass matrix. If masses are attached to the nodes of the structure, then the nodal dynamic forces are

$$\{P\} = -[M] \frac{d^2\{\delta\}}{dt^2} \quad (28)$$

where

$$[M] = \begin{bmatrix} M_1 & & 0 \\ & M_2 & \\ 0 & & \ddots \\ & & & M_n \end{bmatrix} \quad (29)$$

is a diagonal matrix. The mass of beam and plate elements are usually distributed throughout the structure. Therefore, the distributed pressure loading can be written in the form

$$p = -\rho \frac{d^2 w}{dt^2} \quad (30)$$

Substituting Equations (6) and (9) into Equation (30) yields

$$p = -\rho [N][C]^{-1} \{\ddot{\delta}\}$$

or

$$p = -\rho [R] \{\ddot{\delta}\} \quad (31)$$

where

$$[R] = [N][C]^{-1}$$

Since the equivalent element nodal forces can be computed from the equation

$$\{P\}^e = - \int_V [R]^T p dV \quad (32)$$

then

$$\{P\}^e = \left\{ \int_V [R]^T [R] \rho dV \right\} \{\ddot{\delta}\} \quad (33)$$

Therefore the elemental consistent mass matrix is given by

$$[m]^e = \int [R]^T [R] \rho dV \quad (34)$$

The consistent mass matrices given in Reference 2 (see Tables 3 and 4) are used in the computer program.

Once the elemental consistent mass and/or lumped mass matrices are computed, then the overall matrix is obtained by following the same technique as used in assembling the overall stiffness matrix.

The overall mass matrix is reduced by using Equation (3a). We again assume that we have N control point normal displacements and M displacements which must be eliminated. The overall mass matrix can be written in the form

$$[M] = \begin{bmatrix} M_{NN} & M_{NM} \\ M_{MN} & M_{MM} \end{bmatrix} \quad (35)$$

and the displacements

$$\{\delta\} = \begin{Bmatrix} \delta_N \\ \delta_M \end{Bmatrix} \quad (36)$$

From Equation (3a) we have

$$\{\delta_M\} = -[K_{MM}]^{-1}[K_{MN}]\{\delta_N\} \quad (3a)$$

Since the virtual work of the reduced mass system must equal the virtual work of the true mass system

$$-\{\Delta\delta_N\}^T[M_r]\{\ddot{\delta}_N\} = -\{\Delta\delta\}^T[M]\{\ddot{\delta}\} \quad (37)$$

where

$\{\Delta\delta_N\}$ = virtual displacements of control points

$\{\Delta\delta\}$ = virtual displacements of complete system

$[M_r]$ = overall reduced mass matrix

Equation (37) can be rewritten in the form

$$\{\Delta\delta_N\}^T[M_r]\{\ddot{\delta}_N\} = [\Delta\delta_N^T \quad \Delta\delta_M^T][M]\begin{Bmatrix} \delta_N \\ \delta_M \end{Bmatrix} \quad (38)$$

Substituting Equation (3a) into Equation (38) yields

$$\{\Delta\delta_N\}^T[M_r]\{\ddot{\delta}_N\} = \{\Delta\delta_N\}^T \left[I \quad -[K_{NM}][K_{MM}]^{-1} \right] [M] \begin{bmatrix} I \\ -[K_{MM}]^{-1}[K_{MN}] \end{bmatrix} \{\ddot{\delta}_N\}$$

which yields the result

$$[M_r] = \left[I \quad -[K_{NM}][K_{MM}]^{-1} \right] [M] \begin{bmatrix} I \\ [K_{MM}]^{-1}[K_{MN}] \end{bmatrix} \quad (39)$$

The reduced mass matrix given by Equation (39) is calculated in the computer program.

3.3 Modes and Frequencies

Since the design engineer may find it useful to know the mode shapes and natural frequencies of the structure, this information can be obtained by using the NMØDE option in the computer program. If no external forces are present then the reduced mass and influence coefficient matrices are related to one another by the relationship

$$[f_{NN}]^{-1} \{ \delta_N \} = - [M_r] \{ \ddot{\delta}_N \} \quad (40)$$

For determining natural frequencies, the deflections $\{ \delta_N \}$ can be written as

$$\{ \delta_N \} = \{ \delta_o \} \sin \omega t \quad (41)$$

Substituting Equation (41) into Equation (40) yields

$$[f_{NN}]^{-1} \{ \delta_o \} = \omega^2 [M_r] \{ \delta_o \} \quad (42)$$

The solution of Equation (42) yields the natural frequencies, ω , and the mode shapes $\{ \delta_o \}$. Since $[f_{NN}]^{-1}$ and $[M_r]$ are both symmetrical matrices, the mass matrix $[M_r]$ can be triangularized

$$[M_r] = [L] [L]^T \quad (43)$$

where

$$[L] = \begin{bmatrix} l_{11} & 0 & 0 & \dots & 0 \\ l_{21} & l_{22} & 0 & \dots & 0 \\ \vdots & \vdots & l_{33} & \dots & \vdots \\ l_{n1} & \dots & \dots & \dots & l_{nn} \end{bmatrix}$$

Substituting Equation (43) into Equation (42) yields

$$[f_{NN}]^{-1} \{ \delta_o \} = \omega^2 [L] [L]^T \{ \delta_o \}$$

$$[L]^{-1} [f_{NN}]^{-1} \{\delta_o\} = \omega^2 [L]^T \{\delta_o\} \quad (44)$$

Since

$$[L^T]^{-1} [L^T] = [I]$$

Equation (44) may be written

$$[L]^{-1} [f_{NN}]^{-1} [L^T]^{-1} [L]^T \{\delta_o\} = \omega^2 [L]^T \{\delta_o\} \quad (44a)$$

or

$$[A] \{\bar{\delta}_o\} = \omega^2 \{\delta_o\} \quad (45)$$

where

$$[A] = [L]^{-1} [f_{NN}]^{-1} [L^T]^{-1}$$

$$\{\bar{\delta}_o\} = [L]^T \{\delta_o\}$$

An eigenvalue subroutine using the Givens method was used in the computer program package to solve Equation (45). The Givens method is fully described in Reference 4.

Note that the dynamical matrix $[A]$ in the form described above is real and symmetric which is required by the Givens method. Conveniently, $[L]$ and $[L^T]$ are in triangular form which is used in the computer program package to save core storage space.

4.0 PROGRAM DESCRIPTION

Computer program FLUENC written in FORTRAN IV carries out the operations set forth in Section 3.0 for generating the structural influence coefficients and mass matrices required by the Collocation Flutter Program. Briefly, the structure is assumed to be representable by a planar network of beams and triangular plate elements connected at discrete joints. At each joint, if there are no restraints, the program assumes three degrees of freedom; that is, one displacement normal to the plane of the structure and two rotations. The program first synthesizes the stiffness and mass matrices for the entire structure including all degrees of freedom from the data input for the beam and triangular plate elements and from the restraint information input for the joints. It then reduces the stiffness and mass matrices by eliminating all the rotational degrees of freedom and leaving only the normal displacements. As a final step, the program inverts the reduced stiffness matrix to obtain the influence coefficients.

Other features of the program include the option to compute lumped masses or to compute the consistent mass matrices for the beam and triangular plate elements or both. Also, the triangular plate elements may have either isotropic or orthotropic properties. There is an additional option to expand the reduced frequency matrix to include the degrees of freedom representing the restraint joint (one joint on a movable surface; two joints on a fixed component). This is accomplished by adding one or two zero rows and columns to the reduced flexibility matrix corresponding to the mass numbers of the attach points involved.

In the sections that follow detailed instructions are given for the preparation of input data and a description is given of the output illustrated with several sample problems. Also included are listings and flow charts of the program and a discussion of the processing requirements.

4.1 Description of Program Input

The following instructions describe the input data, their physical units, and the FORTRAN format they must be punched with. The input quantities' names, all in capitals, are their FORTRAN names and, for reference, their equivalent names in Section 3.0 are listed in Appendix D.

4.1.1 Title Card, format (12A6)

Two cards; any alphanumeric statement in columns 1 to 72.

4.1.2 Problem Size and Control Information, format (7I5)

Column	1 - 5	6 - 10	11 - 15	16 - 20	21 - 25	26 - 30	31 -
Name	NJTS	NR	NBE	NPE	NMØDE	MKEY	NLUMP

NJTS = number of joints in structure (50 maximum)
 NR = number of joints with one or more restraints
 NBE = number of beam elements in structure
 NPE = number of triangular plate elements in structure
 NMØDE = number of eigenvalues and eigenvectors desired (9 maximum)
 MKEY = 1. do not compute consistent mass terms for beam and/or triangular plate elements
 = 2. compute consistent mass terms for beam and/or triangular plate elements
 NLUMP = number of lumped masses input. Only lumped masses corresponding to the normal displacement at each joint may be input.

4.1.3 Material Properties

(a) Number of Materials, format (I5)

Column	1 - 5
Name	NMAT

NMAT = number of materials for which properties are input (10 max.)

(b) Properties, format (4E10.3)

Input NMAT number of cards, one for each material.

Column	1 - 10	11 - 20	21 - 30	31 - 40
Name	YM(1)	PR(1)	GE(1)	DENS(1)

YM(i) = Young's modulus of elasticity divided by 10^6 ; psi
 PR(i) = Poisson's ratio
 GE(i) = modulus of rigidity; psi. If input as 0, it will be computed from the following formula:

$$GE(i) = \frac{YM(i)}{2 [1 + PR(i)]}$$

DENS(i) = material density; lb/in³. Not required if MKEY = 1

4.1.4 Joint Coordinate Cards, format (10X, 2E10.3)

Input NJTS number of cards, one for each joint. Also, the structure is assumed to lie in the x-y plane.

Column	1 - 10	11 - 20	21 - 30
Name	m	X(m)	Y(m)

m = joint number (must be input consecutively starting with 1).
May be placed anywhere between columns 1 and 10

X(m) = x coordinate of joint m; inches

Y(m) = y coordinate of joint m; inches

4.1.5 Joint Restraint Information, format (4I5)

Input NR number of cards, one for each joint with one or more restraints.

Column	1 - 5	6 - 10	11 - 15	16 - 20
Name	JT	M1	M2	M3

JT = number of joint having one or more restraints

M1 = 0 free in the z direction

= 1 fixed in the z direction

M2 = 0 free to rotate about the x axis

= 1 fixed about the x axis

M3 = 0 free to rotate about the y axis

= 1 fixed about the y axis

4.1.6 Lumped Masses, format (I5, 5X, E10.3)

Input NLUMP number of cards, one for each lumped mass.

Column	1 - 5	6 - 10	11 - 20
Name	JMASS	blank	RSMASS

JMASS = number of joint for which lumped mass is input

RSMASS = lumped mass, lb.

If more than one lumped mass is input for a particular joint, the program will sum the masses.

4.1.7 Beam Element Properties, format (3E10.3, 3I5)

Input NBE number of cards, one for each beam element.

Column	1 - 10	11 - 20	21 - 30	31 - 45	36 - 40	41 - 45
Name	AR	XI	YJ	MAT	JTNR	JTFR

AR = area of beam cross section, in²

XI = moment of inertia of area, in⁴

YJ = effective torsional moment of inertia, in⁴

MAT = material code corresponding to one of the materials input under paragraph 4.1.3.

JTNR, JTFR = joint numbers at the ends of the beam element

4.1.8 Triangular Plate Element Properties, format (E10.3, 5I5)

Input NPE number of cards, one for each triangular plate element.

Column	1 - 10	11 - 15	16 - 20	21 - 25	26 - 30	31 - 35
Name	PTH	MAT	JT1	JT2	JT3	NDX

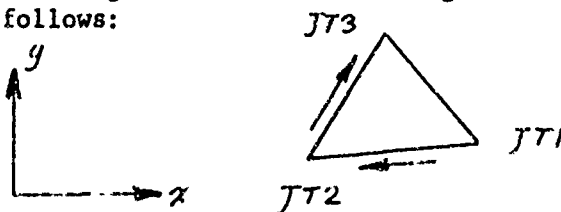
PTH = plate thickness, in.

MAT = material code corresponding to one of the materials input under paragraph 4.1.3

JT1, JT2, JT3 = joint numbers at the three corners of the triangular plate

Restrictions:

- a) The order of the joint numbers must be given in a clockwise manner as follows:



- b) The angle formed by the edges of the triangular plate at JT1 must not be 90°.

NDX = 0 the plate has isotropic properties and the flexural rigidity terms are computed from

$$DX = DY = \frac{YM(MAT) \times PTH^3}{12 \{ 1 - [PR(MAT)]^2 \}}$$

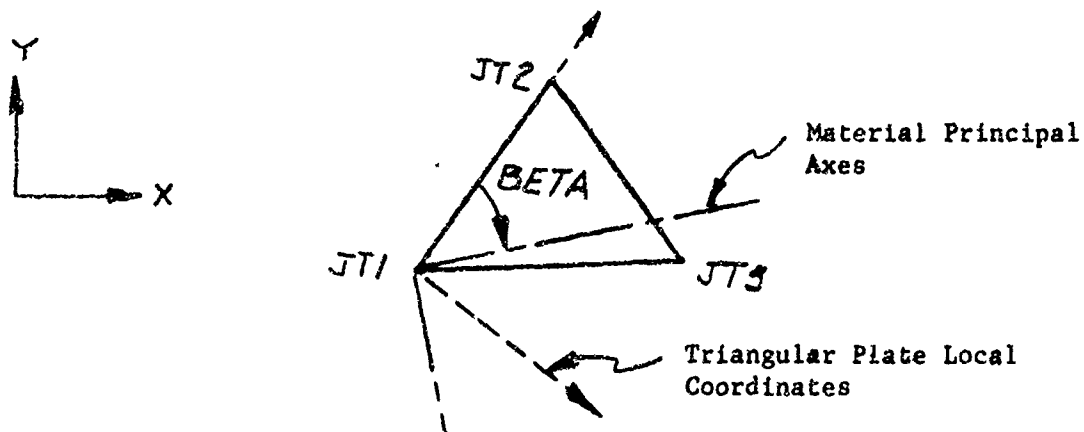
$$D1 = [PR(MAT)] \times DX$$

- = 1 the plate has orthotropic properties and the flexural rigidity terms are input by the next card [format (4E10.3)]

Column	1 - 10	11 - 20	21 - 30	31 - 40	41 - 50
Name	DX	DY	D1	DKY	BETA

DX, DY, D1, DKY = flexural rigidity terms, in.lb.

BETA = angle between material principal axes and the triangular plate local coordinates as shown below



4.1.9 Option to Expand Reduced Flexibility Matrix

Note: The following card (NCOD) is always required at the end of all input data for any one particular case, whether or NOT the option is to be executed.

FORMAT (1I6)		
Column	1-6	
Name	NCOD	
Item	(1)	

NCOD = 0 Option not executed

= 1 Option executed

If NCOD = 1, the following card is required

FORMAT (3I8)			
Column	1-8	9-16	17-24
Name	NR	NNE	NWO
Item	(1)	(2)	(3)

NR = Number of boundary points used (1 or 2)

NNE = Mass number of first attach point

NWO = Mass number of second attach point, if NR = 2

NWO = 0 or left blank if NR = 1

To input more than one problem, the user need only repeat the cards in paragraph 4.1.1 through 4.1.8 for each additional problem.

4.2 Description of Program Output

The program prints out all the input data for every problem followed by the solution consisting of the reduced upper right triangular stiffness (lb/in), flexibility (in/lb) and weight (lb) matrices as well as the modes and frequencies when these are requested on the card in paragraph 4.1.2. The stiffness, flexibility, and mass matrices that are printed/punched out only contain terms that are associated with the normal displacement "z". This is done so that when the flexibility matrix is used in subsequent collocation flutter analyses only the essential degrees of freedom are included in the flutter analyses. Also, the matrices are reduced to eliminate control points associated with fixed points (boundaries). If it is desirable to include the boundary points, it is only necessary to intersperse rows and columns of zero's at the proper place in the matrices. Immediately following the joint restraint information in the output, the program prints out the coordinate numbers assigned by the program to the normal displacements at each unrestrained joint. The elements in all the reduced output matrices are ordered according to these coordinate numbers.

In addition, the program punches out the entire flexibility and weight matrices row by row with the format (1P6E12.5) which is compatible with the input requirements of the Collocation Flutter Program. Each punched matrix is identified by a little card as the first card.

4.3 Sample Problems

To illustrate the use of program FLUENCE, three sample problems are included in Appendix A. Each sample problem starts with a problem statement and is followed by a listing of the input data and the output of the program. The first sample problem is a simply supported uniform beam composed of five beam segments. The second is a uniform cantilever plate divided into 72 triangular plate elements, and the third is a lumped mass and beam network simulating a missile control surface.

4.4 Processing Requirements

Program FLUENCE has been run on the GE-635 computer and it required about 31,000 cells of core storage. It is expected that the program storage requirement will be about the same on other digital computers. In addition to using the input and output files, 05 and 06, which are standard for the GE-635 computer, the program requires six other peripheral files, five of which are designated in the program by the numeric codes 07, 08, 19, 10 and 11, and the sixth is the card punch file.

There is no general formula for determining the run time required for a problem, but if a GE-635 computer is used, an estimate may be made from the times required for the three sample problems in Appendix A, which are as follows:

Sample Problem No.	No. of Joints	No. of Beam Elements	No. of Plate Elements	Consistent Masses Computed	Lumped Masses Input	No. of Modes & Freqs Computed	Run Time Hr.
1	6	5	0	Yes	No	4	0.0015
2	50	0	72	Yes	No	9	0.0691
3	29	45	0	No	Yes	9	0.0161

4.5 Program Listing and Flow Chart

In the event future changes are needed in the program, a listing of the program is included in Appendix B. The program consists of a MAIN deck, 24 subroutines and one function subprogram. MAIN has the function of reading in data, numbering the coordinates (subroutine C00RDN), generating the codes for assembling the stiffness and weight matrices and calling the subroutines which develop the stiffness and mass terms for the beam and triangular plate elements. When the entire stiffness and weight matrices have been established for the whole structure, the MAIN program calls a subroutine which reduces these matrices as discussed before and determines the modes and frequencies as well.

The 24 subroutines and one function subprogram can be divided conveniently into five groups according to their function. The first group consists of those routines that develop the beam stiffness terms; these are TRANS and BEAMK. The second group consists of the routines which determine the beam mass terms; these are TRANS and BEAMM. The third group develops the triangular plate stiffness terms and these are PLATEK, CMAT, MINV, DINMAT, MATMPY, DMAT, DBLINT and PLYMP. The fourth group determines the triangular plate mass terms and these consist of PLATEM, CMAT, MINV, DINMTM, MATMPY, DBLINT and PLYMP. The fifth group of subroutines reduces the stiffness and

and mass matrices, finds the eigenvalues and eigenvectors and outputs the solution. This group is comprised of EIGEN, VIVID, ZRØMAK, ZRØMAM, SYMINV, EIGMAT, BIGMAT, LØØP1, LØØP2, LØØP3 and LØØP4.

Since the program listing is annotated extensively with comment statements, no further explanatory remarks are given here for the program. However, to facilitate the understanding of the interrelationships among the many subroutines, a flow chart of the entire FLUENC program is included in Appendix C.

$\frac{12EI}{L^3}$					
$\frac{6EI}{L^2} m$	$\frac{4EI}{L} m^2 + \frac{GJ}{L} l^2$				
$-\frac{6EI}{L^2} l$	$-\frac{4EI}{L} lm + \frac{GJ}{L} lm$	$\frac{4EI}{L} l^2 + \frac{GJ}{L} m^2$			
$-\frac{12EI}{L^3}$	$-\frac{6EI}{L^2} m$	$\frac{6EI}{L^2} l$			
$\frac{6EI}{L^2} m$	$\frac{2EI}{L} m^2 - \frac{GJ}{L} l^2$	$-\frac{2EI}{L} lm - \frac{GJ}{L} lm$	$-\frac{6EI}{L^2} m$	$\frac{4EI}{L} m^2 + \frac{GJ}{L} l^2$	
$-\frac{6EI}{L^2} l$	$-\frac{2EI}{L} lm - \frac{GJ}{L} lm$	$\frac{2EI}{L} l^2 - \frac{GJ}{L} m^2$	$\frac{6EI}{L^2} l$	$-\frac{4EI}{L} lm + \frac{GJ}{L} lm$	$\frac{4EI}{L} l^2 + \frac{GJ}{L} m^2$

Symmetric

$$l = \frac{X_j - X_i}{L}$$

$$m = \frac{Y_j - Y_i}{L}$$

X_i, Y_i, X_j, Y_j are the global end coordinates of the beam in Figure 2

Table 1. Plane Grid Beam Stiffness Matrix in Global Coordinates

$$[m] = \rho AL$$

27

$\frac{13}{35} + \frac{6I}{5AL^2}$					
$\frac{11L}{210} + \frac{I}{10AL}$	$\frac{L^2}{105} + \frac{2I}{15A}$		Symmetric		
0	0	$\frac{J}{3A}$			
$\frac{9}{70} - \frac{6I}{5AL^2}$	$\frac{13L}{420} - \frac{I}{10AL}$	0	$\frac{13}{35} + \frac{6I}{5AL^2}$		
$-\frac{13L}{420} + \frac{I}{10AL}$	$-\frac{L^2}{140} - \frac{I}{30A}$	0	$-\frac{11L}{210} - \frac{I}{10AL}$	$\frac{L^2}{105} + \frac{2I}{15A}$	
0	0	$\frac{J}{6A}$	0	0	$\frac{J}{3A}$

Table 3. Consistent Mass Matrix for Beam in Local Coordinates

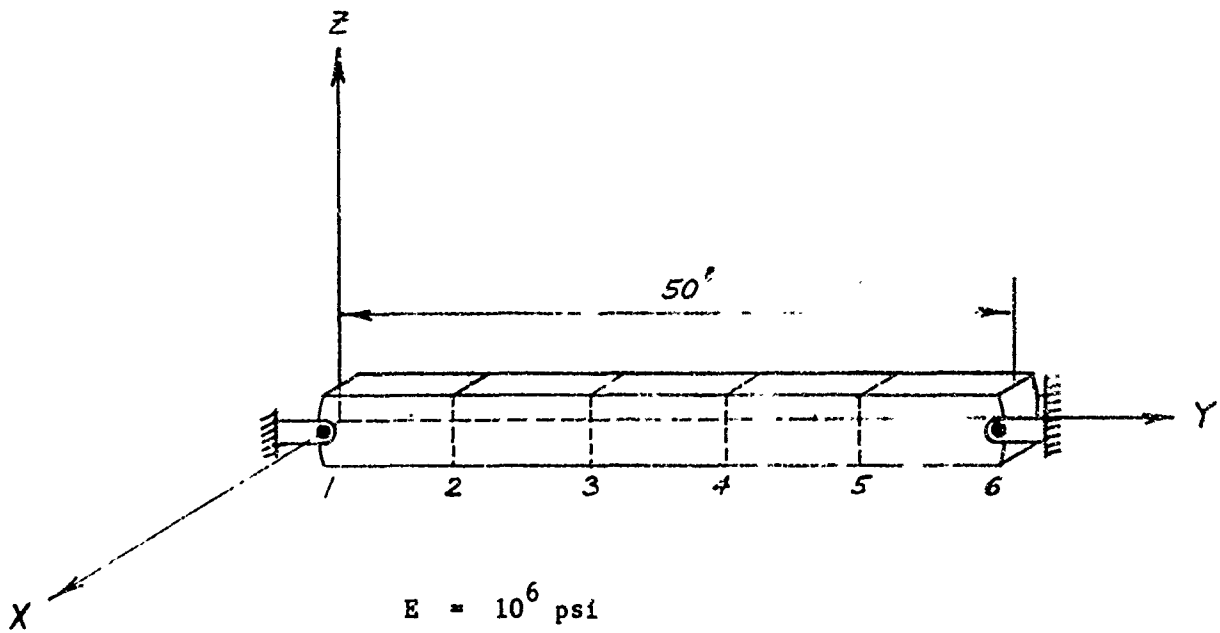
References

1. Tezcan, S. S., "Computer Analysis of Plane and Space Structures", Journal of the Structural Division, ASCE, April 1966
2. Przemieniecki, J. S., "Theory of Matrix Structural Analysis", McGraw-Hill Book Co., New York, 1968
3. Zienkiewicz, O. C., "The Finite Element Method in Structural and Continuum Mechanics", McGraw-Hill Publishing Company Limited, London, 1967
4. Bishop, R. E.D, Gladwell, G. M. L., and Michaelson, S., "The Matrix Analysis of Vibration", Cambridge University Press, London, 1965

APPENDIX A

Three Sample Problems - Input and Output

Sample Problem No. 1
Simply Supported Beam



$$E = 10^6 \text{ psi}$$

$$\nu = 0.33$$

$$\rho = 0.012 \text{ lb/in}^3$$

$$A = 100 \text{ in}^2$$

$$I = 2 \text{ in}^4$$

$$J = 4 \text{ in}^4$$

Calculate first five vibration modes and frequencies using the consistent mass matrix option.

Listing of Input Data Cards

SIMPLY SUPPORTED BEAM WITH 4 JOINTS
AUGUST 1968

	6	7	8	9	4	2
1.	1					
	1	0.11		0.		0.010
	1	0.		0.		
	2	0.		10.		
	3	0.		20.		
	4	0.		30.		
	5	0.		40.		
	6	0.		50.		
	1	1	0	1		
	2	1	0	1		
100.	2.			4.	1	2
100.	2.			4.	1	3
100.	2.			4.	1	4
100.	2.			4.	1	5
100.	2.			4.	1	6

NOT REPRODUCIBLE

Program Output

SIMPLY-SUPPORTED BEAM WITH 6 JOINTS
AUGUST 1968

NJTS = 6 NR = 2 NBE = 5 NPE = 0 NMODE = 4 NKEY = 2 NLUMP = 0

MATERIAL PROPERTIES
NO. YOUNG'S MODULUS POISSON RATIO MODULUS OF RIGIDITY DENSITY
1 0.10000E 07 0.3300 0.37594E 06 0.12000E-01

JOINT COORDINATES
JOINT NO. X COORD. Y COORD.
1 0. 0.
2 0. 10.00000
3 0. 20.00000
4 0. 30.00000
5 0. 40.00000
6 0. 50.00000

JOINT RESTRAINT CORE
JOINT NO. Z DISPLACEMENT ROTATION ABOUT X ROTATION ABOUT Y
1 1 0 1
6 1 0 1

COORDINATE NUMBERS FOR EACH Z DISPLACEMENT AT EACH UNRESTRAINED JOINT
JOINT NO. COORD. NO.
2 1
3 2
4 3
5 4

BEAM ELEMENT PROPERTIES
ELEMENT NO. A I J MAT JOINT 1 JOINT 2
1 100.0000 2.0000 4.0000 1 1 2
2 100.0000 2.0000 4.0000 1 2 3
3 100.0000 2.0000 4.0000 1 3 4
4 100.0000 2.0000 4.0000 1 4 5
5 100.0000 2.0000 4.0000 1 5 6

REDUCED UPPER TRIANGULAR STIFFNESS MATRIX

ROW 1 0.19751E 05 -0.19005E 05 0.92679E 04 -0.20670E 04

ROW 2 0.28019E 05 -0.21072E 05 0.62679E 04

ROW 3 0.26019E 05 -0.19005E 05
ROW 4 0.19751E 05

REDUCED UPPER TRIANGULAR FLEXIBILITY MATRIX

ROW 1 0.53333E-03 0.75000E-03 0.66667E-03 8.38333E-03
ROW 2 0.12000E-02 0.11333E-02 0.66667E-03
ROW 3 0.12000E-02 0.75000E-03
ROW 4 0.53333E-03

REDUCED UPPER TRIANGULAR WEIGHT MATRIX

ROW 1 0.11172E 02 0.93900E 00 -0.56295E 00 0.21468E 00
ROW 2 0.10609E 02 0.11537E 01 -0.56295E 00
ROW 3 0.10609E 02 0.93900E 00
ROW 4 0.11172E 02

HERE ARE THE EIGENVALUES AND EIGENVECTORS

EIGENVECTOR NUMBER 1
 CORRESPONDING TO 1.0030593E 04
 6.1803364E-01 9.9999962E-01 1.0000000E 00 6.1803418E-01

EIGENVECTOR NUMBER 2
 CORRESPONDING TO 1.6120593E 05
 1.0000000E 00 6.1803418E-01 -6.1803363E-01 -9.9999968E-01

EIGENVECTOR NUMBER 3
 CORRESPONDING TO 8.4178930E 05
 1.0000000E 00 -6.1803399E-01 -6.1803401E-01 1.0000000E 00

EIGENVECTOR NUMBER 4
 CORRESPONDING TO 2.9858634E 06
 -6.1803397E-01 1.0000000E 00 -9.9999993E-01 6.1803399E-01

HERE ARE THE NATURAL FREQUENCIES

THE NATURAL FREQUENCY NUMBER	1	2	3	4	CPS
THE NATURAL FREQUENCY NUMBER	1	2	3	4	19,948
THE NATURAL FREQUENCY NUMBER	2	3	4	1	63,981
THE NATURAL FREQUENCY NUMBER	3	4	1	2	144,023
THE NATURAL FREQUENCY NUMBER	4	1	2	3	275,824

SAMPLE PROBLEM NO. 1a

Simply Supported Beam

Identical to Sample Problem 1 with the addition of lumped mass input at joint 3 and 4.

Program Output

1
SIMPLY SUPPORTED BEAM WITH 6 JOINTS - USING BOTH CONSISTENT MASS MATRIX
OPTION AND LUMPED MASS INPUT AT JOINTS 3 AND 4.
)

JOINTS = 6 NR = 2 NRE = 5 NPE = 0 NMODE = 4 MKEY = 2 NLUMP = 2
)

1
MATERIAL PROPERTIES
NO. YOUNG'S MODULUS POISSON RATIO MODULUS OF RIGIDITY DENSITY
1 0.1000E 07 0.3300 0.3759E 06 0.1200E-01
)

JOINT COORDINATES
JOINT NO. X COORD. Y COORD.
1 0. 0.
2 0. 10.0000
3 0. 20.0000
4 0. 30.0000
5 0. 40.0000
6 0. 50.0000
)

JOINT RESTRAINT CODE
JOINT NO. Z DISPLACEMENT ROTATION ABOUT X ROTATION ABOUT Y
1 1 0 1
6 1 0 1
38
)

COORDINATE NUMBERS FOR EACH Z DISPLACEMENT AT EACH UNRESTRAINED JOINT
JOINT NO. COORD. NO.
1 1
2 2
3 3
4 4
5 4
)

LUMPED WEIGHTS
JOINT NO. WEIGHT
3 20.0000
4 30.0000
)

BEAM ELEMENT PROPERTIES
ELEMENT NO. A I J HAI JOINT 1 JOINT 2
1 100.0000 2.0000 4.0000 1 2
2 100.0000 2.0000 4.0000 1 3
3 10.0000 2.0000 4.0000 1 4
4 100.0000 2.0000 4.0000 1 5
5 100.0000 2.0000 4.0000 1 6
)

REDUCED UNIFORM TRIANGULAR STIFFNESS MATRIX
)

ROW 1 0.19751E 05 -0.19005E 05 0.62679E 04 -0.20670E 04

ROW 2 0.28019E 05 -0.21072E 05 0.82679E 04

ROW 3 0.28019E 05 -0.19005E 05

ROW 4 0.19751E 05

REDUCED UPPER TRIANGULAR FLEXIBILITY MATRIX

ROW 1 0.53333E-03 0.75000E-03 0.66667E-03 0.38333E-03

ROW 2 0.12000E-02 0.11333E-02 0.66667E-03

ROW 3 0.12000E-02 0.75000E-03

ROW 4 0.53333E-03

REDUCED UPPER TRIANGULAR DEFLECTION MATRIX

ROW 1 0.11172E 02 0.93900E 00 -0.56295E 00 0.21468E 00

ROW 2 0.30609E 02 0.11537E 01 -0.56295E 00

ROW 3 0.40609E 02 0.93900E 00

ROW 4 0.11172E 02

HERE ARE THE EIGENVALUES AND EIGENVECTORS

EIGENVECTOR NUMBER 1
 CORRESPONDING TO 0.0004330E 03
 6.0476160E-01 9.9286114E-01 1.0000000E 00 6.1375684E-01

EIGENVECTOR NUMBER 2
 CORRESPONDING TO 1.0007120E 05
 1.0000000E 00 7.2539523E-01 -5.6665802E-01 -8.8326765E-01

EIGENVECTOR NUMBER 3
 CORRESPONDING TO 6.7652134E 05
 8.9313311E-01 -1.9308592E-01 -1.8372997E-01 1.0000000E 00

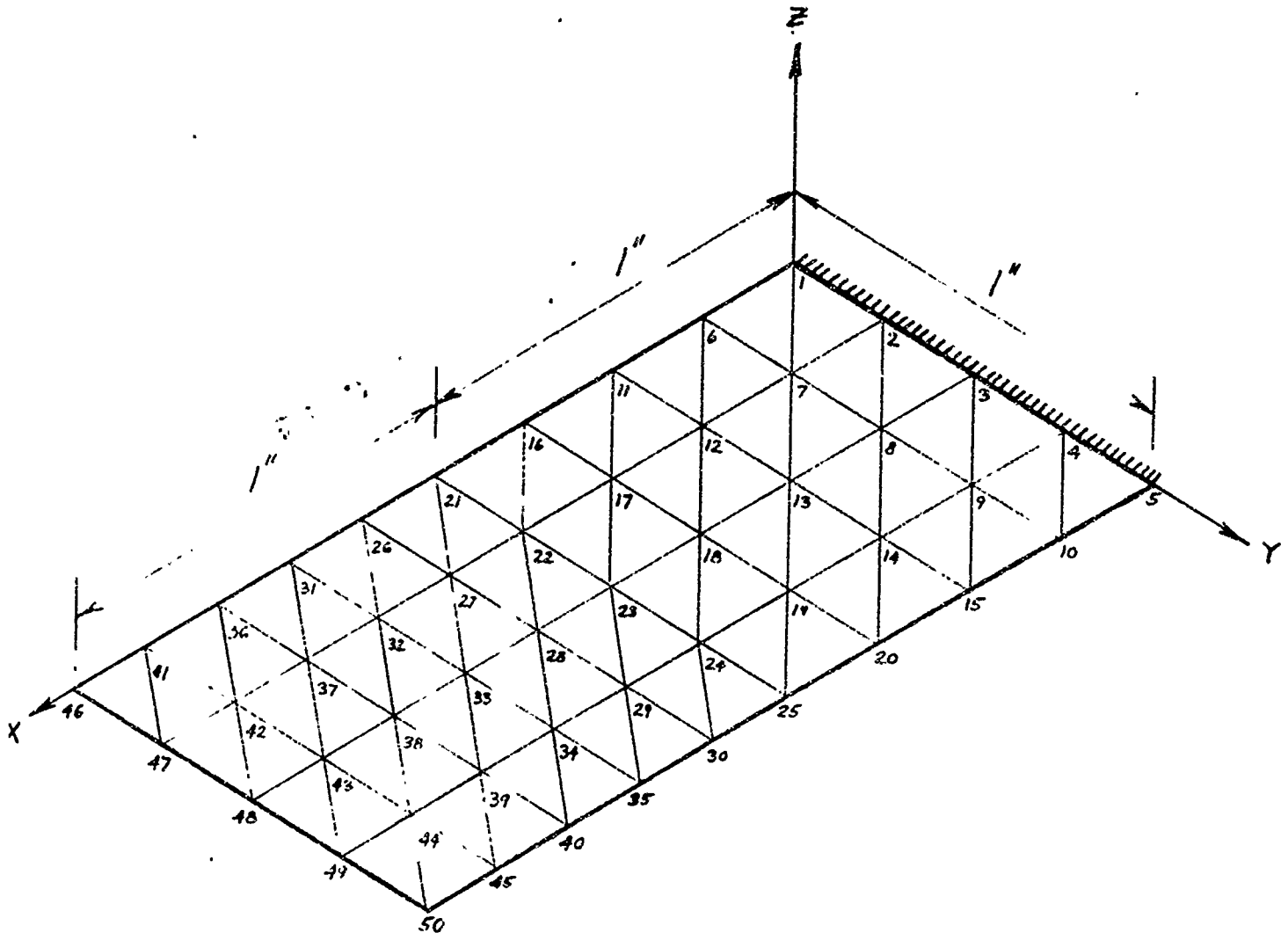
EIGENVECTOR NUMBER 4
 CORRESPONDING TO 1.3253830E 06
 1.0000000E 00 -5.389472E-01 3.9625669E-01 -9.1981947E-01

HERE ARE THE NATURAL FREQUENCIES

THE NATURAL FREQUENCY NUMBER 1 IS 10.054 CPS
 THE NATURAL FREQUENCY NUMBER 2 IS 50.347 CPS
 THE NATURAL FREQUENCY NUMBER 3 IS 130.906 CPS
 THE NATURAL FREQUENCY NUMBER 4 IS 183.228 CPS

Sample Problem No. 2

Cantilever Plate



$$E = 3 \times 10^7 \text{ psi}$$

$$\nu = 0.3$$

$$\rho = 0.283 \text{ lb/in}^3$$

$$t = 0.1 \text{ in.}$$

Listing of Input Data Cards

CANTILEVER PLATE WITH 50 JOINTS
AUGUST 1968

50	2	0	72	9	2	0
1						
30.	0.3		0.			0.285
1	0.		0.			
2	0.		.25			
3	0.		.5			
4	0.		.75			
5	0.		1.			
6	.25		0.			
7	.25		.25			
8	.25		.5			
9	.25		.75			
10	.25		1.			
11	.5		0.			
12	.5		.25			
13	.5		.5			
14	.5		.75			
15	.5		1.			
16	.75		0.			
17	.75		.25			
18	.75		.5			
19	.75		.75			
20	.75		1.			
21	1.		0.			
22	1.		.25			
23	1.		.5			
24	1.		.75			
25	1.		1.			
26	1.2		0.			
27	1.2		.25			
28	1.2		.5			
29	1.2		.75			
30	1.2		1.			
31	1.4		0.			
32	1.4		.25			
33	1.4		.5			
34	1.4		.75			
35	1.4		1.			
36	1.6		0.			
37	1.6		.25			
38	1.6		.5			
39	1.6		.75			
40	1.6		1.			
41	1.8		0.			
42	1.8		.25			
43	1.8		.5			
44	1.8		.75			
45	1.8		1.			
46	2.0		0.			
47	2.0		.25			
48	2.0		.5			

NOT REPRODUCIBLE

NOT REPRODUCIBLE

49	2.0	.75		
50	2.0	1.		
1	1	1	1	
2	1	1	1	
3	1	1	1	
4	1	1	1	
5	1	1	1	
0.1	1	1	7	6
0.1	1	1	2	7
0.1	1	2	8	7
0.1	1	2	3	8
0.1	1	3	9	8
0.1	1	3	4	9
0.1	1	4	10	9
0.1	1	4	5	10
0.1	1	6	12	11
0.1	1	6	7	12
0.1	1	7	13	12
0.1	1	7	8	13
0.1	1	8	14	13
0.1	1	8	9	14
0.1	1	9	15	14
0.1	1	9	10	15
0.1	1	11	17	16
0.1	1	11	12	17
0.1	1	12	18	17
0.1	1	12	13	18
0.1	1	13	19	18
0.1	1	13	14	19
0.1	1	14	20	19
0.1	1	14	15	20
0.1	1	16	22	21
0.1	1	16	17	22
0.1	1	17	23	22
0.1	1	17	18	23
0.1	1	18	24	23
0.1	1	18	19	24
0.1	1	19	25	24
0.1	1	19	20	25
0.1	1	21	27	26
0.1	1	21	22	27
0.1	1	22	28	27
0.1	1	22	23	28
0.1	1	23	29	28
0.1	1	23	24	29
0.1	1	24	30	29
0.1	1	24	25	30
0.1	1	26	32	31
0.1	1	26	27	32
0.1	1	27	33	32
0.1	1	27	28	33
0.1	1	28	34	33

0.1	1	28	29	34
0.1	1	29	35	34
0.1	1	29	30	35
0.1	1	31	37	36
0.1	1	31	32	7
0.1	1	32	38	37
0.1	1	32	33	38
0.1	1	33	39	38
0.1	1	33	34	39
0.1	1	34	40	39
0.1	1	34	35	40
0.1	1	36	42	41
0.1	1	36	37	42
0.1	1	37	43	42
0.1	1	37	38	43
0.1	1	38	44	43
0.1	1	38	39	44
0.1	1	39	45	44
0.1	1	39	40	45
0.1	1	41	47	46
0.1	1	41	42	47
0.1	1	42	48	47
0.1	1	42	43	48
0.1	1	43	49	48
0.1	1	43	44	49
0.1	1	44	50	49
0.1	1	44	45	50

EXTRACTED FROM

Program Output

CANTILEVER PLATE WITH 50 JOINTS
AUGUST 1968

NJTS = 50 MN = 5 MRE = 0 NPL = 12 MNUF = 9 MKEY = 2 MLUMP = 0

MATERIAL PROPERTIES
NO. YOUNG'S MODULUS POISSON RATIO MODULUS OF RIGIDITY DENSITY
1 0.10000E+08 0.30000 0.11510E+08 0.20300E+00

JOINT COORDINATES
JOINT NO. X COORD. Y COORD.

1	0.	0.
2	0.25000	0.
3	0.	0.50000
4	0.	0.75000
5	0.	1.00000
6	0.25000	0.
7	0.25000	0.25000
8	0.25000	0.50000
9	0.25000	0.75000
10	0.25000	1.00000
11	0.50000	0.
12	0.50000	0.25000
13	0.50000	0.50000
14	0.50000	0.75000
15	0.50000	1.00000
16	0.75000	0.
17	0.75000	0.25000
18	0.75000	0.50000
19	0.75000	0.75000
20	0.75000	1.00000
21	1.00000	0.
22	1.00000	0.25000
23	1.00000	0.50000
24	1.00000	0.75000
25	1.00000	1.00000
26	1.25000	0.
27	1.25000	0.25000
28	1.25000	0.50000
29	1.25000	0.75000
30	1.25000	1.00000
31	1.50000	0.
32	1.50000	0.25000
33	1.50000	0.50000
34	1.50000	0.75000
35	1.50000	1.00000
36	1.75000	0.
37	1.75000	0.25000
38	1.75000	0.50000
39	1.75000	0.75000
40	1.75000	1.00000
41	2.00000	0.
42	2.00000	0.25000
43	2.00000	0.50000
44	2.00000	0.75000
45	2.00000	1.00000

NOT REPRODUCIBLE

46	2.00000	0.20000
47	2.00000	0.50000
48	2.00000	0.70000
49	2.00000	1.00000
50	2.00000	1.00000

JOINT NO.	RESTRAINT	CODE	ROTATION ABOUT X	ROTATION ABOUT Y
1	1	1	1	1
2	1	1	1	1
3	1	1	1	1
4	1	1	1	1
5	1	1	1	1

COORDINATE NUMBERS FOR EACH Z DISPLACEMENT AT EACH UNRESTRAINED JOINT

JOINT NO.	COORD. NO.
6	1
7	2
8	3
9	4
10	5
11	6
12	7
13	8
14	9
15	10
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REDUCED UPPER TRIANGULAR STIFFNESS MATRIX

ROW	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																			
0.38184E	06	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	0.44329E	02	0.18083E	02	0.85105E	03	0.24876E	03	0.56185E	02	0.24970E	04	0.3134E	04	0.5134E	04	0.22117E	04	0.95578E	04	0.48208E	04	0.33144E	03	0.37753E	01	0.24479E	02	-	0.13544E	03	0.95810E	02	-	0.26885E	02	-	0.23826E	03	-	0.56024E	05	-	0.6024E	05	-	0.56024E	05	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	0.44329E	02	0.18083E	02	0.85105E	03	0.24876E	03	0.56185E	02	0.24970E	04	0.3134E	04	0.5134E	04	0.22117E	04	0.95578E	04	0.48208E	04	0.33144E	03	0.37753E	01	0.24479E	02	-	0.13544E	03	0.95810E	02	-	0.26885E	02	-	0.23826E	03	-	0.56024E	05	-	0.6024E	05	-	0.56024E	05	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	0.44329E	02	0.18083E	02	0.85105E	03	0.24876E	03	0.56185E	02	0.24970E	04	0.3134E	04	0.5134E	04	0.22117E	04	0.95578E	04	0.48208E	04	0.33144E	03	0.37753E	01	0.24479E	02	-	0.13544E	03	0.95810E	02	-	0.26885E	02	-	0.23826E	03	-	0.56024E	05	-	0.6024E	05	-	0.56024E	05	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	0.44329E	02	0.18083E	02	0.85105E	03	0.24876E	03	0.56185E	02	0.24970E	04	0.3134E	04	0.5134E	04	0.22117E	04	0.95578E	04	0.48208E	04	0.33144E	03	0.37753E	01	0.24479E	02	-	0.13544E	03	0.95810E	02	-	0.26885E	02	-	0.23826E	03	-	0.56024E	05	-	0.6024E	05	-	0.56024E	05	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	0.44329E	02	0.18083E	02	0.85105E	03	0.24876E	03	0.56185E	02	0.24970E	04	0.3134E	04	0.5134E	04	0.22117E	04	0.95578E	04	0.48208E	04	0.33144E	03	0.37753E	01	0.24479E	02	-	0.13544E	03	0.95810E	02	-	0.26885E	02	-	0.23826E	03	-	0.56024E	05	-	0.6024E	05	-	0.56024E	05	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	0.44329E	02	0.18083E	02	0.85105E	03	0.24876E	03	0.56185E	02	0.24970E	04	0.3134E	04	0.5134E	04	0.22117E	04	0.95578E	04	0.48208E	04	0.33144E	03	0.37753E	01	0.24479E	02	-	0.13544E	03	0.95810E	02	-	0.26885E	02	-	0.23826E	03	-	0.56024E	05	-	0.6024E	05	-	0.56024E	05	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	0.44329E	02	0.18083E	02	0.85105E	03	0.24876E	03	0.56185E	02	0.24970E	04	0.3134E	04	0.5134E	04	0.22117E	04	0.95578E	04	0.48208E	04	0.33144E	03	0.37753E	01	0.24479E	02	-	0.13544E	03	0.95810E	02	-	0.26885E	02	-	0.23826E	03	-	0.56024E	05	-	0.6024E	05	-	0.56024E	05	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	0.44329E	02	0.18083E	02	0.85105E	03	0.24876E	03	0.56185E	02	0.24970E	04	0.3134E	04	0.5134E	04	0.22117E	04	0.95578E	04	0.48208E	04	0.33144E	03	0.37753E	01	0.24479E	02	-	0.13544E	03	0.95810E	02	-	0.26885E	02	-	0.23826E	03	-	0.56024E	05	-	0.6024E	05	-	0.56024E	05	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	0.44329E	02	0.18083E	02	0.85105E	03	0.24876E	03	0.56185E	02	0.24970E	04	0.3134E	04	0.5134E	04	0.22117E	04	0.95578E	04	0.48208E	04	0.33144E	03	0.37753E	01	0.24479E	02	-	0.13544E	03	0.95810E	02	-	0.26885E	02	-	0.23826E	03	-	0.56024E	05	-	0.6024E	05	-	0.56024E	05	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	0.44329E	02	0.18083E	02	0.85105E	03	0.24876E	03	0.56185E	02	0.24970E	04	0.3134E	04	0.5134E	04	0.22117E	04	0.95578E	04	0.48208E	04	0.33144E	03	0.37753E	01	0.24479E	02	-	0.13544E	03	0.95810E	02	-	0.26885E	02	-	0.23826E	03	-	0.56024E	05	-	0.6024E	05	-	0.56024E	05	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	0.44329E	02	0.18083E	02	0.85105E	03	0.24876E	03	0.56185E	02	0.24970E	04	0.3134E	04	0.5134E	04	0.22117E	04	0.95578E	04	0.48208E	04	0.33144E	03	0.37753E	01	0.24479E	02	-	0.13544E	03	0.95810E	02	-	0.26885E	02	-	0.23826E	03	-	0.56024E	05	-	0.6024E	05	-	0.56024E	05	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	0.44329E	02	0.18083E	02	0.85105E	03	0.24876E	03	0.56185E	02	0.24970E	04	0.3134E	04	0.5134E	04	0.22117E	04	0.95578E	04	0.48208E	04	0.33144E	03	0.37753E	01	0.24479E	02	-	0.13544E	03	0.95810E	02	-	0.26885E	02	-	0.23826E	03	-	0.56024E	05	-	0.6024E	05	-	0.56024E	05	-	0.1882E	06	-	0.95888E	05	-	0.34859E	05	0.58053E	04	-	0.18982E	06	-	0.62329E	05	0.58326E	05	-	0.87619E	05	-	0.47619E	05	-	0.40357E	04	-	0.24939E	05	-	0.15114E	05	0.61324E	02	-	0.14326E	04	-	0.28584E	04	-	0.94039E	01	-	0.11348E	03	-	0.12755E	03	-	0.55807E	01	-	0.26342E	02	

[illegible][illegible][illegible][illegible][illegible][illegible][illegible]

0.13069F 05	0.13380F 06	0.51585E 05	0.91479E 04	0.62446E 03	-0.38538E 05	-0.24677E 05	-0.43732E 04
-0.23088E 03	0.10935F 04	0.08527E 04	0.01091F 04	0.19621E 04	0.52598E 02	-0.27012E 03	-0.24016E 04
-0.080307F 03	-0.15751F 02	0.61999E 02	0.50149E 03	0.63386E 03	0.31198E 03	0.25867E 01	-0.88471E 02
-0.10324E 03	-0.67642E 02						
ROW 9							
0.11651F 07	0.19591F 06	-0.62174E 04	0.28216E 05	0.45631E 04	-0.44531E 06	-0.36827E 05	0.95424E 03
0.13192E 05	0.14546E 06	0.51782E 05	-0.12568E 03	0.11858E 04	-0.32188E 04	-0.41348E 05	-0.25752E 05
-0.38870F 03	0.12032F 04	0.95147E 04	0.04171E 04	-0.12512E 02	0.74619E 02	-0.34250E 03	-0.22324E 04
0.45844E 01	-0.21563F 02	0.96548E 02	0.47033E 03	0.73569E 03	-0.89119E 08	0.48561E 01	-0.17623E 02
-0.13869F 03							
ROW 10							
0.36886E 06	0.18220E 04	-0.89781E 04	0.22910E 05	0.18003E 05	-0.19105E 06	-0.38717E 03	0.20156E 04
0.73738E 04	0.58920E 05	-0.69881E 02	0.26285E 03	-0.17723E 03	0.93778E 03	-0.17984E 05	0.11649E 01
0.10528E 03	-0.23368E 03	0.45183E 04	-0.33534E 03	0.18885E 02	-0.52562E 02	-0.19777E 03	-0.11564E 04
-0.69746E 01	0.28589E 02	-0.68175E 02	0.28089E 03	-0.27491E 08	0.18305E 01	-0.53933E 01	0.16976E 02
ROW 11							
0.35288E 06	0.18835E 06	0.18849E 06	-0.55925E 05	0.71471E 04	-0.28277E 06	-0.71813E 05	0.36801E 05
0.37913E 04	0.77836E 05	0.88813E 05	-0.51393E 04	0.44591E 04	-0.52396E 03	-0.23873E 05	-0.47407E 04
0.37492E 03	-0.26596E 03	0.69735E 04	0.94662E 04	0.27286E 04	-0.17648E 03	5.46339E 02	-0.18418E 04
-0.18530E 04	-0.89578E 01	0.53530E 01	0.29566E 03	0.56742E 03	0.22286E 03	0.98868E 01	0.54648E 08
ROW 12							
0.11533E 07	0.58680F 06	0.19565E 06	-0.36627E 05	0.25794E 05	-0.47324E 06	-0.77388E 05	0.43939E 05
0.25477E 04	0.57780E 05	0.66350E 05	-0.35886E 04	0.18327E 04	-0.35323E 03	-0.45737E 05	-0.21782E 05
0.32838E 03	0.52112E 03	0.18583E 05	0.888438E 04	0.16522E 04	0.17855E 03	-0.12866E 03	-0.24583E 04
-0.66012E 03	-0.18442E 03	0.14685E 02	0.30107E 03	0.41716E 03	0.13917E 03	0.29530E 02	
ROW 13							
0.13688E 07	0.58988E 06	0.18113E 06	0.15953E 05	-0.47495E 03	-0.44383E 06	-0.74388E 05	0.28896E 05
0.16471E 05	0.16888E 06	0.65948E 05	0.65676E 03	0.91180E 03	-0.14518E 04	-0.44383E 05	-0.22416E 05
-0.43282E 03	0.96850E 03	0.98912E 04	0.80463E 04	0.17288E 04	0.98581E 02	-0.16725E 03	-0.22836E 04
-0.74648E 03	-0.16894E 02	0.93629E 01	0.36483E 03	0.38469E 03	0.17895E 03		-0.22642E 04
ROW 14							
0.11623E 07	0.19689F 06	-0.65144E 04	0.29482E 05	-0.63282E 03	-0.48882E 06	-0.48891E 05	0.17445E 04
0.16953E 05	0.18102E 06	0.63876E 05	-0.21955E 03	0.79989E 03	-0.18751E 04	-0.45739E 05	-0.25238E 05
-0.44788E 03	0.11844F 04	0.18583E 05	0.88173E 04	-0.23892E 02	0.73612E 02	-0.27899E 03	-0.22799E 04
0.57087E 01	-0.14869E 02	0.48800E 02	0.31016E 03	0.49844E 03			
ROW 15							
0.36446E 06	0.18134E 14	-0.87278E 04	0.22488E 05	0.20080F 05	-0.28934E 06	-0.39149E 03	0.21659E 04
0.57594E 04	0.76567F 05	-0.26862E 02	0.33247E 03	-0.25252E 03	0.16419E 04	-0.19220E 05	-0.28826E 02
-0.85285E 01	-0.88557E 03	0.48738E 04	-0.24177E 08	0.27442E 02	-0.55573E 02	0.25152E 03	-0.11998E 04
-0.77578E 01	0.18294E 02	-0.67515E 02	0.28535E 03				
ROW 16							
0.44138E 06	-0.17758E 06	0.98868E 05	-0.33875E 05	0.07856E 04	-0.38504E 06	-0.75217E 05	0.36482E 02
0.38886E 04	0.18736F 06	0.99306E 05	-0.18739E 05	0.68247E 04	-0.88783E 03	-0.32572E 05	-0.35578E 05
0.45542E 03	-0.35745E 03	0.84581E 04	0.11531E 04	0.27472E 04	-0.27255E 03	0.77618E 02	-0.13681E 04
-0.65077E 03	0.14396F 02	-0.3886E 01					-0.23577E 04
ROW 17							
0.13178E 07	-0.47859E 06	0.17585E 06	-0.32448E 05	0.45997E 05	-0.69852E 06	-0.61988E 05	0.34231E 05
-0.35387E 04	0.22734E 06	0.63832E 05	-0.92299E 04	0.24819E 04	0.16215E 04	-0.57787E 05	-0.2372E 05
0.75374E 03	-0.78641E 02	0.12381E 05	0.94540E 04	0.15463E 04	0.36639E 02	0.78415E 02	-0.19819E 04
-0.36104F 03	-0.88857E 02						-0.17693E 04
ROW 18							
0.15178E 07	-0.47894E 06	0.91262E 05	0.17844E 05	0.97879E 04	-0.66886E 06	-0.59298E 05	0.24575E 05
0.17379E 05	0.71683E 06	0.82553E 05	0.42250E 03	0.49399E 03	-0.12517E 04	-0.56935E 05	-0.28268E 05
-0.36818E 03	0.18110E 04	0.11957E 05	0.94316E 04	0.19613E 04	0.35537E 02	-0.66616E 02	-0.19422E 04
-0.55416E 03							-0.16555E 04

0.13445E 07	-0.19765E 06	-0.45270E 04	0.40296E 02	0.74303E 04	-0.70580E 06	-0.38395E 05	0.21825E 03	-0.92294E 04
0.16066E 05	-0.23205E 06	0.71001E 05	0.58048E 02	0.48071E 03	-0.14596E 04	-0.58341E 05	-0.29550E 02	0.11454E 03
-0.51798E 03	0.11030E 04	0.12514E 05	0.90099E 04	-0.63015E 01	0.63037E 02	-0.12485E 03	-0.14084E 04	-0.19615E 04
ROW 20								
0.46118E 06	0.25798E 04	-0.12779E 05	0.20383E 05	0.31808E 05	-0.31273E 06	-0.15648E 03	0.15244E 04	-0.78883E 04
0.63435E 04	0.10286E 06	-0.25765E 02	0.43659E 03	-0.49370E 03	0.28080E 04	-0.25835E 05	-0.19989E 02	-0.28931E 02
0.96359E 02	-0.89167E 03	0.62808E 04	-0.41070E 01	0.33644E 02	-0.81453E 02	0.29577E 03	-0.10961E 04	
ROW 21								
0.55052E 06	-0.18136E 06	0.87610E 05	-0.63348E 05	0.67948E 04	-0.63140E 06	-0.10124E 06	0.46486E 05	-0.19069E 05
0.37236E 04	0.11561E 06	0.10786E 06	-0.10324E 05	0.67201E 04	-0.66918E 03	-0.31325E 05	-0.36102E 05	-0.44189E 04
0.49174E 03	-0.41527E 03	0.49700E 04	0.75563E 04	0.11695E 04	-0.13827E 03	0.78427E 02		
ROW 22								
0.15456E 07	-0.46403E 06	0.16862E 06	-0.31335E 05	0.53124E 05	-0.75364E 06	-0.98647E 05	0.44776E 05	-0.11892E 05
-0.74344E 04	0.24235E 06	1.68704E 05	-0.82298E 04	0.14320E 04	0.29514E 04	-0.57779E 05	-0.27238E 05	-0.37416E 04
0.95383E 03	-0.46776E 03	0.66379E 04	0.608370E 04	0.62064E 03	0.14584E 02			
ROW 23								
0.17318E 07	-0.46621E 06	0.83757E 05	0.14752E 05	0.17646E 04	-0.71703E 06	-0.87107E 05	0.26743E 05	-0.18331E 04
0.14903E 05	0.23413E 06	0.87962E 05	0.30311E 04	0.13806E 03	-0.59745E 03	-0.57525E 05	-0.27673E 05	-0.54928E 04
-0.13429E 03	0.21974E 03	0.05905E 04	0.56967E 04	0.11831E 04				
ROW 24								
0.15599E 07	-0.19213E 06	0.82638E 04	0.44777E 05	0.38968E 03	-0.76147E 06	-0.49934E 05	-0.18237E 03	-0.74577E 04
0.13802E 05	0.24722E 06	0.75124E 05	0.66871E 02	0.53729E 03	-0.55328E 03	-0.58132E 05	-0.29281E 05	0.36518E 02
-0.32809E 03	0.32699E 03	0.04278E 04	0.05151E 04					
ROW 25								
0.56681E 06	0.26711E 04	-0.14294E 05	0.31548E 05	0.26674E 05	-0.34249E 06	0.86702E 02	0.18129E 04	-0.80798E 04
0.58565E 04	0.11854E 06	-0.59953E 02	0.50601E 03	-0.74769E 03	0.26897E 04	-0.26529E 05	0.14421E 01	-0.59528E 02
0.16884E 03	-0.05214E 03	0.45461E 04						
ROW 26								
0.55249E 06	-0.18096E 06	0.88540E 05	-0.34144E 05	0.68787E 04	-0.33861E 06	-0.18887E 06	0.47192E 05	-0.19441E 05
0.38185E 04	0.18204E 06	0.18188E 06	-0.13835E 05	0.73288E 04	-0.85158E 03	-0.17217E 05	-0.22175E 05	-0.60528E 03
-0.28782E 03	-0.23886E 03							
ROW 27								
0.15767E 07	-0.47698E 06	0.12578E 06	-0.32482E 05	0.53475E 05	-0.75733E 06	-0.88415E 05	0.44361E 05	-0.12287E 05
-0.94317E 04	0.23124E 06	0.80378E 05	-0.47039E 04	0.17330E 04	0.38955E 04	-0.38571E 05	-0.14517E 05	-0.17374E 04
0.68992E 03								
ROW 28								
0.17711E 07	-0.48881E 06	0.05057E 05						

0.17585F 07	-0.48128E 06	0.65008E 05	0.15448E 05	0.21303E 05	-0.67639E 06	-0.54348E 05	0.31258E 05	-0.84090E 03
0.61312E 03	0.15221E 06	0.33543E 05	-0.13831E 04					
ROW 34								
0.15746E 07	-0.19745E 06	-0.81659E 04	0.43493E 05	0.19506E 05	-0.71017E 06	-0.28926E 05	-0.14952E 03	-0.59496E 04
0.17563E 04	0.15235E 06	0.34188E 05						
ROW 35								
0.56827E 06	0.24849E 04	-0.13506E 05	0.29938E 05	0.38170E 05	-0.32243E 06	0.52442E 02	0.14828E 04	-0.54193E 04
0.13498E 03	0.21844E 05							
ROW 36								
0.39709E 06	-0.21258E 04	0.77381E 05	-0.29837E 05	0.59883E 04	-0.12768E 06	0.44879E 04	0.48167E 05	-0.23387E 05
0.59849E 04								
ROW 37								
0.13551E 07	-0.54129E 06	0.17814E 06	-0.33274E 05	0.65615E 05	-0.59277E 06	0.38498E 05	0.38182E 05	-0.11616E 05
ROW 38								
0.15786E 07	-0.25175E 06	0.98535E 05	0.54714E 04	0.92647E 05	-0.40788E 06	0.55173E 05	0.16593E 05	
ROW 39								
0.13663E 07	-0.24518E 06	-0.33837E 04	0.57444E 04	0.95985E 05	-0.40488E 06	0.44781E 05		
ROW 40								
0.48428E 06	0.94742E 03	-0.38154E 04	0.28926E 04	0.83852E 05	-0.18737E 06			
ROW 41								
0.18859E 06	-0.11884E 06	0.58978E 05	-0.21853E 05	0.49778E 04				
ROW 42								
0.48597E 06	-0.14789E 06	0.14888E 06	-0.32388E 05					
ROW 43								
0.68876E 06	-0.38735E 06	0.85332E 05						
ROW 44								
0.55299E 06	-0.17597E 06							
ROW 45								
0.17383E 06								

REDUCED UPPER TRIANGULAR FLEXIBILITY MATRIX

ROW 1								
0.92988E-05	0.37856E-05	0.16145E-05	0.73691E-06	0.55368E-07	0.15767E-04	0.18815E-04	0.58149E-05	0.32322E-05
0.12937E-05	0.28012E-04	0.14958E-04	0.18435E-04	0.68436E-05	0.38731E-05	0.23889E-04	0.19381E-04	0.14844E-04
0.19837E-04	0.72375E-05	0.27163E-04	0.22633E-04	0.18238E-04	0.14103E-04	0.18283E-04	0.38352E-04	0.25917E-04
0.21547E-04	0.73747E-04	0.33514E-04	0.33514E-04	0.29181E-04	0.24868E-04	0.28637E-04	0.16493E-04	0.36788E-04
0.32438E-04	0.28138E-04	0.23892E-04	0.19786E-04	0.40824E-04	0.35886E-04	0.31885E-04	0.27140E-04	0.22937E-04
ROW 2								
0.33772E-05	0.28889E-05	1.13218E-05	0.51092E-06	0.85699E-05	0.74597E-05	0.58253E-05	0.41237E-05	0.27659E-05
0.12884E-04	0.11264E-04	0.95479E-05	0.77473E-05	0.68538E-05	0.16738E-04	0.15845E-04	0.13298E-04	0.11489E-04
0.97848E-05	0.19888E-04	0.18878E-04	0.16381E-04	0.14586E-04	0.12708E-04	0.22859E-04	0.21899E-04	0.19323E-04
0.17537E-04	0.15735E-04	0.25882E-04	0.24132E-04	0.22353E-04	0.28564E-04	0.18769E-04	0.28941E-04	0.27167E-04
0.25388E-04	0.21588E-04	0.21886E-04	0.31879E-04	0.38283E-04	0.28421E-04	0.26634E-04	0.24843E-04	
ROW 3								
0.27446E-05	0.19422E-05	0.18671E-05	0.49852E-05	0.54866E-05	0.58463E-05	0.53889E-05	0.43832E-05	0.85783E-05
0.88978E-05	0.89978E-05	0.87131E-05	0.81117E-05	0.12222E-04	0.12328E-04	0.12324E-04	0.12125E-04	0.11768E-04
0.15888E-04	0.15184E-04	0.15853E-04	0.14887E-04	0.14627E-04	0.17931E-04	0.17895E-04	0.17817E-04	0.17670E-04
0.17468E-04	0.29759E-04	0.28684E-04	0.28684E-04	0.20465E-04	0.28295E-04	0.23577E-04	0.21488E-04	0.23188E-04
0.21588E-04	0.23158E-04	0.26388E-04	0.26388E-04	0.20173E-04	0.28295E-04	0.23577E-04	0.21488E-04	0.23188E-04

ROW 5	0.29675E-05	0.23205E-05	0.27156E-05	0.36817E-05	0.49978E-05	0.62435E-05	0.67818E-05	0.53947E-05	0.66346E-05
	0.79819E-05	0.92600E-05	0.10319E-04	0.81391E-05	0.96487E-05	0.10977E-04	0.12276E-04	0.13501E-04	0.18755E-04
	0.12072E-04	0.13392E-04	0.14605E-04	0.15967E-04	0.13185E-04	0.14501E-04	0.15817E-04	0.17121E-04	0.18412E-04
	0.15620E-04	0.16934E-04	0.18246E-04	0.19552E-04	0.20895E-04	0.18055E-04	0.19367E-04	0.20678E-04	0.21984E-04
	0.23286E-04	0.20400E-04	0.21401E-04	0.23111E-04	0.24418E-04	0.25721E-04			
ROW 6	0.54226E-05	0.78158E-06	0.19845E-05	0.34579E-05	0.58049E-05	0.95107E-05	0.21902E-05	0.39879E-05	0.60055E-05
	0.67833E-05	0.11949E-04	0.40239E-05	0.62108E-05	0.85082E-05	0.11269E-04	0.14176E-04	0.16731E-04	0.20282E-05
	0.10504E-04	0.13156E-04	0.15938E-04	0.17403E-05	0.98497E-05	0.12373E-04	0.15003E-04	0.17188E-04	0.9123E-05
	0.11669E-04	0.14216E-04	0.16831E-04	0.19495E-04	0.18963E-04	0.13405E-04	0.16043E-04	0.18658E-04	0.21291E-04
	0.12764E-04	0.15297E-04	0.17860E-04	0.20463E-04	0.23094E-04				
ROW 7	0.42373E-04	0.27834E-04	0.18181E-04	0.11628E-04	0.62007E-05	0.61896E-04	0.47387E-04	0.34873E-04	0.24968E-04
	0.16592E-04	0.78254E-04	0.64644E-04	0.51754E-04	0.40255E-04	0.29884E-04	0.77765E-04	0.64961E-04	
	0.52952E-04	0.41667E-04	0.18363E-03	0.90677E-04	0.71979E-04	0.65753E-04	0.53946E-04	0.11631E-03	0.10351E-03
	0.90885E-04	0.70556E-04	0.66474E-04	0.12902E-03	0.11631E-03	0.10372E-03	0.91344E-04	0.79120E-04	0.14177E-03
	0.12909E-03	0.11652E-03	0.10411E-03						
ROW 8	0.23370E-04	0.18824E-04	0.14888E-04	0.10110E-04	0.45279E-04	0.40850E-04	0.34182E-04	0.28073E-04	0.22618E-04
	0.61456E-04	0.55497E-04	0.49398E-04	0.43130E-04	0.37059E-04	0.31986E-04	0.67879E-04	0.61765E-04	0.55366E-04
	0.49139E-04	0.80199E-04	0.68199E-04	0.73945E-04	0.67650E-04	0.61381E-04	0.98754E-04	0.92823E-04	0.86260E-04
	0.79974E-04	0.73684E-04	0.11110E-03	0.10485E-03	0.98585E-04	0.92380E-04	0.86989E-04	0.12344E-03	0.11178E-03
	0.11092E-03	0.10463E-03	0.96349E-04						
ROW 9	0.19296E-04	0.17280E-04	0.14689E-04	0.12811E-04	0.11622E-04	0.10399E-04	0.31465E-04	0.29890E-04	0.47758E-04
	0.47540E-04	0.46963E-04	0.45744E-04	0.44810E-04	0.59618E-04	0.59184E-04	0.58368E-04	0.57258E-04	0.55844E-04
	0.71401E-04	0.70716E-04	0.69891E-04	0.68839E-04	0.67612E-04	0.83130E-04	0.82356E-04	0.81482E-04	0.80464E-04
	0.70348E-04	0.94808E-04	0.94811E-04	0.93313E-04	0.92114E-04	0.91842E-04	0.10653E-03	0.19568E-03	0.10477E-03
	0.10378E-03	0.10273E-03							
ROW 10	0.20480E-04	0.21898E-04	0.23807E-04	0.26421E-04	0.30306E-04	0.34124E-04	0.38833E-04	0.43665E-04	0.49239E-04
	0.43526E-04	0.47402E-04	0.50937E-04	0.46146E-04	0.50893E-04	0.54079E-04	0.57996E-04	0.61765E-04	0.56733E-04
	0.60625E-04	0.64667E-04	0.68598E-04	0.72463E-04	0.67352E-04	0.71314E-04	0.75276E-04	0.79213E-04	0.83118E-04
	0.77979E-04	0.81940E-04	0.85955E-04	0.89835E-04	0.93758E-04	0.88686E-04	0.92567E-04	0.96528E-04	0.10046E-03
	0.10439E-03								
ROW 11	0.30394E-04	0.14267E-04	0.20879E-04	0.26712E-04	0.35122E-04	0.45119E-04	0.24867E-04	0.31196E-04	0.38935E-04
	0.47685E-04	0.57126E-04	0.32653E-04	0.48375E-04	0.48516E-04	0.57245E-04	0.66373E-04	0.41574E-04	0.49627E-04
	0.57949E-04	0.66638E-04	0.75558E-04	0.50588E-04	0.50891E-04	0.67299E-04	0.75938E-04	0.84732E-04	0.59626E-04
	0.68149E-04	0.36297E-04	0.85211E-04	0.93936E-04	0.69033E-04	0.77396E-04	0.82863E-04	0.94469E-04	0.10316E-03
ROW 12	0.10247E-03	0.85748E-04	0.66234E-04	0.50365E-04	0.36480E-04	0.15018E-03	0.12556E-03	0.10295E-03	0.83195E-04
	0.65326E-04	0.17933E-03	0.15543E-03	0.13245E-03	0.11128E-03	0.91382E-04	0.28797E-03	0.18455E-03	0.16164E-03
	0.13974E-03	0.11875E-03	0.23853E-03	0.21339E-03	0.19059E-03	0.16841E-03	0.14676E-03	0.26511E-03	0.24212E-03
	0.21918E-03	0.10788E-03	0.17514E-03	0.29373E-03	0.27880E-03	0.24809E-03	0.22573E-03	0.20365E-03	
ROW 13	0.76472E-04	0.65702E-04	0.55311E-04	0.45877E-04	0.12298E-03	0.11201E-03	0.10024E-03	0.88365E-04	0.77126E-04
	0.15155E-03	0.13991E-03	0.12798E-03	0.11579E-03	0.10394E-03	0.17963E-03	0.16772E-03	0.15562E-03	0.14345E-03
	0.13136E-03	0.20754E-03	0.19558E-03	0.18337E-03	0.17119E-03	0.15935E-03	0.23538E-03	0.22329E-03	0.21115E-03
	0.10896E-03	0.18677E-03	0.26328E-03	0.25189E-03	0.23893E-03	0.22675E-03	0.21455E-03		
ROW 14	0.68769E-04	0.60996E-04	0.56369E-04	0.50734E-04	0.98653E-04	0.96953E-04	0.93712E-04	0.89532E-04	0.12671E-03
	0.12540E-03	0.12290E-03	0.12081E-03	0.11641E-03	0.15357E-03	0.15156E-03	0.14925E-03	0.14642E-03	0.14322E-03
	0.10833E-03	0.17011E-03	0.17568E-03	0.17293E-03	0.16955E-03	0.16701E-03	0.20469E-03	0.20226E-03	0.19950E-03
	0.19468E-03	0.23306E-03	0.23129E-03	0.22687E-03	0.22689E-03	0.22689E-03	0.22689E-03		

ROW 14

0.06442E-04	0.69219E-04	0.79372E-04	0.85356E-04	0.91858E-04	0.98079E-04	0.10310E-03	0.10362E-03	0.11402E-03
0.11680E-03	0.12299E-03	0.12809E-03	0.13034E-03	0.13484E-03	0.14141E-03	0.14788E-03	0.15495E-03	0.16319E-03
0.15972E-03	0.16626E-03	0.17274E-03	0.17912E-03	0.18588E-03	0.19302E-03	0.19911E-03	0.19765E-03	0.20487E-03
0.20208E-03	0.20952E-03	0.21685E-03	0.22254E-03	0.22908E-03	0.23644E-03	0.24378E-03	0.25117E-03	0.25867E-03

ROW 15

0.04899E-04	0.68478E-04	0.72585E-04	0.85555E-04	0.10055E-03	0.11714E-03	0.01567E-04	0.94047E-04	0.10096E-03
0.12315E-03	0.14022E-03	0.14352E-03	0.14154E-03	0.13215E-03	0.12754E-03	0.16342E-03	0.12588E-03	0.16434E-03
0.15518E-03	0.17052E-03	0.18618E-03	0.14858E-03	0.16315E-03	0.17899E-03	0.19339E-03	0.20099E-03	0.17128E-03
0.18525E-03	0.20894E-03	0.21622E-03	0.23178E-03	0.24378E-03	0.25867E-03	0.27507E-03	0.28449E-03	0.29370E-03

ROW 16

0.22717E-03	0.19158E-03	0.16802E-03	0.13386E-03	0.10009E-03	0.20194E-03	0.24597E-03	0.21237E-03	0.10197E-03
0.15378E-03	0.33354E-03	0.29831E-03	0.26413E-03	0.23198E-03	0.20141E-03	0.38449E-03	0.33970E-03	0.33254E-03
0.24859E-03	0.25072E-03	0.43531E-03	0.40875E-03	0.38645E-03	0.33338E-03	0.38883E-03	0.40615E-03	0.45168E-03
0.41759E-03	0.38416E-03	0.35131E-03	0.35131E-03	0.35131E-03	0.35131E-03	0.35131E-03	0.35131E-03	0.35131E-03

ROW 17

0.17565E-03	0.15613E-03	0.14801E-03	0.12468E-03	0.24378E-03	0.22585E-03	0.20730E-03	0.18979E-03	0.17096E-03
0.20369E-03	0.27544E-03	0.25666E-03	0.24174E-03	0.21913E-03	0.34351E-03	0.32489E-03	0.35688E-03	0.28699E-03
0.26808E-03	0.39309E-03	0.37431E-03	0.35537E-03	0.33644E-03	0.31733E-03	0.44258E-03	0.42374E-03	0.40477E-03
0.38272E-03	0.36667E-03	0.36667E-03	0.36667E-03	0.36667E-03	0.36667E-03	0.36667E-03	0.36667E-03	0.36667E-03

ROW 18

0.15487E-03	0.14863E-03	0.14147E-03	0.20875E-03	0.20555E-03	0.20161E-03	0.19388E-03	0.18897E-03	0.25888E-03
0.25382E-03	0.24059E-03	0.24312E-03	0.23698E-03	0.38272E-03	0.38272E-03	0.29289E-03	0.29857E-03	0.28472E-03
0.35260E-03	0.34814E-03	0.34336E-03	0.33613E-03	0.33256E-03	0.40833E-03	0.39577E-03	0.39094E-03	0.38574E-03
0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03

ROW 19

0.15680E-03	0.16062E-03	0.17728E-03	0.18522E-03	0.19371E-03	0.20188E-03	0.20845E-03	0.22198E-03	0.23024E-03
0.23183E-03	0.24713E-03	0.25482E-03	0.26697E-03	0.27546E-03	0.28492E-03	0.29242E-03	0.30024E-03	0.31221E-03
0.37874E-03	0.32928E-03	0.33772E-03	0.34682E-03	0.35749E-03	0.36883E-03	0.37457E-03	0.38384E-03	0.39148E-03
0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03

ROW 20

0.18248E-03	0.14764E-03	0.16246E-03	0.18449E-03	0.20567E-03	0.22862E-03	0.18817E-03	0.28738E-03	0.22462E-03
0.24935E-03	0.27280E-03	0.27968E-03	0.24973E-03	0.27054E-03	0.29236E-03	0.31478E-03	0.27171E-03	0.29228E-03
0.31327E-03	0.33587E-03	0.35132E-03	0.31327E-03	0.33467E-03	0.35587E-03	0.37767E-03	0.39983E-03	0.39983E-03
0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03

ROW 21

0.36582E-03	0.32895E-03	0.28054E-03	0.24394E-03	0.28962E-03	0.44312E-03	0.39769E-03	0.35451E-03	0.31456E-03
0.27679E-03	0.51726E-03	0.47241E-03	0.42863E-03	0.38695E-03	0.34096E-03	0.59878E-03	0.54621E-03	0.58237E-03
0.45092E-03	0.41873E-03	0.66417E-03	0.61971E-03	0.57508E-03	0.53299E-03	0.49122E-03	0.45122E-03	0.45122E-03
0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03

ROW 22

0.29899E-03	0.27541E-03	0.25289E-03	0.22976E-03	0.39455E-03	0.37113E-03	0.34669E-03	0.32192E-03	0.29796E-03
0.46698E-03	0.44264E-03	0.41781E-03	0.39278E-03	0.36803E-03	0.33803E-03	0.31401E-03	0.48985E-03	0.46392E-03
0.43887E-03	0.61815E-03	0.58537E-03	0.56833E-03	0.53512E-03	0.50986E-03	0.50986E-03	0.50986E-03	0.50986E-03
0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03

ROW 23

0.26968E-03	0.26891E-03	0.25116E-03	0.34993E-03	0.34429E-03	0.33786E-03	0.32958E-03	0.32086E-03	0.41942E-03
0.41328E-03	0.48629E-03	0.38237E-03	0.38237E-03	0.40873E-03	0.48215E-03	0.47583E-03	0.46710E-03	0.45861E-03
0.55791E-03	0.55115E-03	0.54304E-03	0.53607E-03	0.52775E-03	0.52775E-03	0.52775E-03	0.52775E-03	0.52775E-03
0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03

ROW 24

0.26928E-03	0.27489E-03	0.30819E-03	0.31734E-03	0.32686E-03	0.33595E-03	0.34361E-03	0.37391E-03	0.38327E-03
0.39288E-03	0.40219E-03	0.41887E-03	0.41887E-03	0.44538E-03	0.45088E-03	0.46848E-03	0.47749E-03	0.50593E-03
0.51551E-03	0.52513E-03	0.53461E-03	0.53461E-03	0.53461E-03	0.53461E-03	0.53461E-03	0.53461E-03	0.53461E-03
0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03

ROW 25

0.38118E-03	0.28891E-03	0.20188E-03	0.11453E-03	0.34827E-03	0.36783E-03	0.32979E-03	0.35332E-03	0.37888E-03
0.40438E-03	0.43171E-03	0.39174E-03	0.41681E-03	0.44126E-03	0.46772E-03	0.49491E-03	0.45412E-03	0.47677E-03
0.59433E-03	0.53884E-03	0.55791E-03	0.55791E-03	0.55791E-03	0.55791E-03	0.55791E-03	0.55791E-03	0.55791E-03
0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03	0.38827E-03

ROW 26	0.55423E-03	0.49007E-03	0.44053E-03	0.40187E-03	0.35755E-03	0.65858E-03	0.68270E-03	0.54922E-03	0.49020E-03
0.45151E-03	0.75982E-03	0.70428E-03	0.65002E-03	0.59822E-03	0.54848E-03	0.86858E-03	0.89563E-03	0.83563E-03	0.75842E-03
0.69771E-03	0.64698E-03								
ROW 27	0.47059E-03	0.44043E-03	0.41047E-03	0.38147E-03	0.35002E-03	0.56983E-03	0.53786E-03	0.50649E-03	0.47503E-03
0.69763E-03	0.66683E-03	0.63530E-03	0.60351E-03	0.57204E-03	0.54048E-03	0.79570E-03	0.76453E-03	0.73277E-03	0.70075E-03
0.66405E-03									
ROW 28	0.43166E-03	0.41047E-03	0.38147E-03	0.35002E-03	0.31857E-03	0.52558E-03	0.49411E-03	0.46264E-03	0.43117E-03
0.62066E-03	0.61975E-03	0.60848E-03	0.59674E-03	0.58406E-03	0.57138E-03	0.72430E-03	0.71162E-03	0.69894E-03	0.68626E-03
0.65205E-03	0.64055E-03	0.62905E-03	0.61755E-03	0.60605E-03	0.59455E-03	0.74382E-03	0.73232E-03	0.72082E-03	0.70932E-03
0.62020E-03	0.60870E-03	0.59720E-03	0.58570E-03	0.57420E-03	0.56270E-03	0.71374E-03	0.70224E-03	0.69074E-03	0.67924E-03
0.61188E-03	0.60038E-03	0.58888E-03	0.57738E-03	0.56588E-03	0.55438E-03	0.70374E-03	0.69224E-03	0.68074E-03	0.66924E-03
0.60348E-03	0.59198E-03	0.58048E-03	0.56898E-03	0.55748E-03	0.54598E-03	0.69374E-03	0.68224E-03	0.67074E-03	0.65924E-03
0.59508E-03	0.58358E-03	0.57208E-03	0.56058E-03	0.54908E-03	0.53758E-03	0.68374E-03	0.67224E-03	0.66074E-03	0.64924E-03
0.58668E-03	0.57518E-03	0.56368E-03	0.55218E-03	0.54068E-03	0.52918E-03	0.67374E-03	0.66224E-03	0.65074E-03	0.63924E-03
0.57828E-03	0.56678E-03	0.55528E-03	0.54378E-03	0.53228E-03	0.52078E-03	0.66374E-03	0.65224E-03	0.64074E-03	0.62924E-03
0.56988E-03	0.55838E-03	0.54688E-03	0.53538E-03	0.52388E-03	0.51238E-03	0.65374E-03	0.64224E-03	0.63074E-03	0.61924E-03
0.56148E-03	0.54998E-03	0.53848E-03	0.52698E-03	0.51548E-03	0.50398E-03	0.64374E-03	0.63224E-03	0.62074E-03	0.60924E-03
0.55308E-03	0.54158E-03	0.53008E-03	0.51858E-03	0.50708E-03	0.49558E-03	0.63374E-03	0.62224E-03	0.61074E-03	0.59924E-03
0.54468E-03	0.53318E-03	0.52168E-03	0.51018E-03	0.49868E-03	0.48718E-03	0.62374E-03	0.61224E-03	0.60074E-03	0.58924E-03
0.53628E-03	0.52478E-03	0.51328E-03	0.50178E-03	0.49028E-03	0.47878E-03	0.61374E-03	0.60224E-03	0.59074E-03	0.57924E-03
0.52788E-03	0.51638E-03	0.50488E-03	0.49338E-03	0.48188E-03	0.47038E-03	0.60374E-03	0.59224E-03	0.58074E-03	0.56924E-03
0.51948E-03	0.50798E-03	0.49648E-03	0.48498E-03	0.47348E-03	0.46198E-03	0.59374E-03	0.58224E-03	0.57074E-03	0.55924E-03
0.51108E-03	0.49958E-03	0.48808E-03	0.47658E-03	0.46508E-03	0.45358E-03	0.58374E-03	0.57224E-03	0.56074E-03	0.54924E-03
0.50268E-03	0.49118E-03	0.47968E-03	0.46818E-03	0.45668E-03	0.44518E-03	0.57374E-03	0.56224E-03	0.55074E-03	0.53924E-03
0.49428E-03	0.48278E-03	0.47128E-03	0.45978E-03	0.44828E-03	0.43678E-03	0.56374E-03	0.55224E-03	0.54074E-03	0.52924E-03
0.48588E-03	0.47438E-03	0.46288E-03	0.45138E-03	0.43988E-03	0.42838E-03	0.55374E-03	0.54224E-03	0.53074E-03	0.51924E-03
0.47748E-03	0.46598E-03	0.45448E-03	0.44298E-03	0.43148E-03	0.41998E-03	0.54374E-03	0.53224E-03	0.52074E-03	0.50924E-03
0.46908E-03	0.45758E-03	0.44608E-03	0.43458E-03	0.42308E-03	0.41158E-03	0.53374E-03	0.52224E-03	0.51074E-03	0.49924E-03
0.46068E-03	0.44918E-03	0.43768E-03	0.42618E-03	0.41468E-03	0.40318E-03	0.52374E-03	0.51224E-03	0.50074E-03	0.48924E-03
0.45228E-03	0.44078E-03	0.42928E-03	0.41778E-03	0.40628E-03	0.39478E-03	0.51374E-03	0.50224E-03	0.49074E-03	0.47924E-03
0.44388E-03	0.43238E-03	0.42088E-03	0.40938E-03	0.39788E-03	0.38638E-03	0.50374E-03	0.49224E-03	0.48074E-03	0.46924E-03
0.43548E-03	0.42398E-03	0.41248E-03	0.40098E-03	0.38948E-03	0.37798E-03	0.49374E-03	0.48224E-03	0.47074E-03	0.45924E-03
0.42708E-03	0.41558E-03	0.40408E-03	0.39258E-03	0.38108E-03	0.36958E-03	0.48374E-03	0.47224E-03	0.46074E-03	0.44924E-03
0.41868E-03	0.40718E-03	0.39568E-03	0.38418E-03	0.37268E-03	0.36118E-03	0.47374E-03	0.46224E-03	0.45074E-03	0.43924E-03
0.41028E-03	0.39878E-03	0.38728E-03	0.37578E-03	0.36428E-03	0.35278E-03	0.46374E-03	0.45224E-03	0.44074E-03	0.42924E-03
0.40188E-03	0.39038E-03	0.37888E-03	0.36738E-03	0.35588E-03	0.34438E-03	0.45374E-03	0.44224E-03	0.43074E-03	0.41924E-03
0.39348E-03	0.38198E-03	0.37048E-03	0.35898E-03	0.34748E-03	0.33598E-03	0.44374E-03	0.43224E-03	0.42074E-03	0.40924E-03
0.38508E-03	0.37358E-03	0.36208E-03	0.35058E-03	0.33908E-03	0.32758E-03	0.43374E-03	0.42224E-03	0.41074E-03	0.39924E-03
0.37668E-03	0.36518E-03	0.35368E-03	0.34218E-03	0.33068E-03	0.31918E-03	0.42374E-03	0.41224E-03	0.40074E-03	0.38924E-03
0.36828E-03	0.35678E-03	0.34528E-03	0.33378E-03	0.32228E-03	0.31078E-03	0.41374E-03	0.40224E-03	0.39074E-03	0.37924E-03
0.35988E-03	0.34838E-03	0.33688E-03	0.32538E-03	0.31388E-03	0.30238E-03	0.40374E-03	0.39224E-03	0.38074E-03	0.36924E-03
0.35148E-03	0.33998E-03	0.32848E-03	0.31698E-03	0.30548E-03	0.29398E-03	0.39374E-03	0.38224E-03	0.37074E-03	0.35924E-03
0.34308E-03	0.33158E-03	0.32008E-03	0.30858E-03	0.29708E-03	0.28558E-03	0.38374E-03	0.37224E-03	0.36074E-03	0.34924E-03
0.33468E-03	0.32318E-03	0.31168E-03	0.30018E-03	0.28868E-03	0.27718E-03	0.37374E-03	0.36224E-03	0.35074E-03	0.33924E-03
0.32628E-03	0.31478E-03	0.30328E-03	0.29178E-03	0.28028E-03	0.26878E-03	0.36374E-03	0.35224E-03	0.34074E-03	0.32924E-03
0.31788E-03	0.30638E-03	0.29488E-03	0.28338E-03	0.27188E-03	0.26038E-03	0.35374E-03	0.34224E-03	0.33074E-03	0.31924E-03
0.30948E-03	0.29798E-03	0.28648E-03	0.27498E-03	0.26348E-03	0.25198E-03	0.34374E-03	0.33224E-03	0.32074E-03	0.30924E-03
0.30108E-03	0.28958E-03	0.27808E-03	0.26658E-03	0.25508E-03	0.24358E-03	0.33374E-03	0.32224E-03	0.31074E-03	0.29924E-03
0.29268E-03	0.28118E-03	0.26968E-03	0.25818E-03	0.24668E-03	0.23518E-03	0.32374E-03	0.31224E-03	0.30074E-03	0.28924E-03
0.28428E-03	0.27278E-03	0.26128E-03	0.24978E-03	0.23828E-03	0.22678E-03	0.31374E-03	0.30224E-03	0.29074E-03	0.27924E-03
0.27588E-03	0.26438E-03	0.25288E-03	0.24138E-03	0.22988E-03	0.21838E-03	0.30374E-03	0.29224E-03	0.28074E-03	0.26924E-03
0.26748E-03	0.25598E-03	0.24448E-03	0.23298E-03	0.22148E-03	0.20998E-03	0.29374E-03	0.28224E-03	0.27074E-03	0.25924E-03
0.25908E-03	0.24758E-03	0.23608E-03	0.22458E-03	0.21308E-03	0.20158E-03	0.28374E-03	0.27224E-03	0.26074E-03	0.24924E-03
0.25068E-03	0.23918E-03	0.22768E-03	0.21618E-03	0.20468E-03	0.19318E-03	0.27374E-03	0.26224E-03	0.25074E-03	0.23924E-03
0.24228E-03	0.23078E-03	0.21928E-03	0.20778E-03	0.19628E-03	0.18478E-03	0.26374E-03	0.25224E-03	0.24074E-03	0.22924E-03
0.23388E-03	0.22238E-03	0.21088E-03	0.19938E-03	0.18788E-03	0.17638E-03	0.25374E-03	0.24224E-03	0.23074E-03	0.21924E-03
0.22548E-03	0.21398E-03	0.20248E-03	0.19098E-03	0.17948E-03	0.16798E-03	0.24374E-03	0.23224E-03	0.22074E-03	0.20924E-03
0.21708E-03	0.20558E-03	0.19408E-03	0.18258E-03	0.17108E-03	0.15958E-03	0.23374E-03	0.22224E-03	0.21074E-03	0.19924E-03
0.20868E-03	0.19718E-03	0.18568E-03	0.17418E-03	0.16268E-03	0.15118E-03	0.22374E-03	0.21224E-03	0.20074E-03	0.18924E-03
0.20028E-03	0.18878E-03	0.17728E-03	0.16578E-03	0.15428E-03	0.14278E-03	0.21374E-03	0.20224E-03	0.19074E-03	0.17924E-03
0.19188E-03	0.18038E-03	0.16888E-03	0.15738E-03	0.14588E-03	0.13438E-03	0.20374E-03	0.19224E-03	0.18074E-03	0.16924E-03
0.18348E-03	0.17198E-03	0.16048E-03	0.14898E-03	0.13748E-03	0.12598E-03	0.19374E-03	0.18224E-03	0.17074E-03	0.15924E-03
0.17508E-03	0.16358E-03	0.15208E-03	0.14058E-03	0.12908E-03	0.11758E-03	0.18374E-03	0.17224E-03	0.16074E-03	0.14924E-03
0.16668E-03	0.15518E-03	0.14368E-03	0.13218E-03	0.12068E-03	0.10918E-03	0.17374E-03	0.16224E-03	0.15074E-03	0.13924E-03
0.15828E-03	0.14678E-03	0.13528E-03	0.12378E-03	0.11228E-03	0.10078E-03	0.16374E-03	0.15224E-03	0.14074E-03	0.12924E-03
0.14988E-03	0.13838E-03	0.12688E-03	0.11538E-03	0.10388E-03	0.09238E-03	0.15374E-03	0.14224E-03	0.13074E-03	0.11924E-03
0.14148E-03	0.12998E-03	0.11848E-03	0.10698E-03	0.09548E-03	0.08398E-03	0.14374E-03	0.13224E-03	0.12074E-03	0.10924E-03
0.13308E-03	0.12158E-03	0.11008E-03	0.09858E-03	0.08708E-03	0.07558E-03	0.13374E-03	0.12224E-03	0.11074E-03	0.09924E-03
0.12468E-03	0.11318E-03	0.10168E-03	0.09018E-03	0.07868E-03	0.06718E-03	0.12374E-03	0.11224E-03	0.10074E-03	0.08924E-03
0.11628E-03	0.10478E-03	0.09328E-03	0.08178E-03	0.07028E-03	0.05878E-03	0.11374E-03	0.10224E-03	0.09074E-03	0.07924E-03
0.10788E-03	0.09638E-03	0.08488E-03	0.07338E-03	0.06188E-03	0.05038E-03	0.10374E-03	0.09224E-03	0.08074E-03	0.06924E-03
0.09948E-03	0.08798E-03	0.07648E-03	0.06498E-03	0.05348E-03	0.04198E-03	0.09374E-03	0.08224E-03	0.07074E-03	0.05924E-03
0.09108E-03	0.07958E-03	0.06808E-03	0.05658E-03	0.04508E-03	0.03358E-03	0.08374E-03	0.07224E-03	0.06074E-03	0.04924E-03
0.08268E-03	0.07118E-03	0.05968E-03	0.04818E-03	0.03668E-03	0.02518E-03	0.07374E-03	0.06224E-03	0.05074E-03	0.03924E-03
0.07428E-03	0.06278E-03	0.05128E-03	0.03978E-03	0.02828E-03	0.01678E-03	0.06374E-03	0.05224E-03	0.04074E-03	0.02924E-03
0.06588E-03	0.05438E-03	0.04288E-03	0.03138E-03	0.01988E-03	0.00838E-03	0.05374E-03	0.04224E-03		

NOT REPRODUCIBLE

ROW 44 0-12707E-02 0-12741E-02

ROW 45 0-13282E-02

REDUCED UPPER TRIANGULAR WEIGHT MATRIX

ROW 1
0-42674E-03 0-22531E-04 -0-08832E-04 0-11392E-04 0-32178E-04 0-18499E-03 -0-42997E-04 0-21805E-04
-0-88666E-05 -0-19222E-04 0-23520E-05 -0-25422E-05 -0-53180E-07 0-83799E-05 0-25211E-04 0-43490E-05
0-57877E-07 0-45331E-06 -0-25548E-05 -0-39842E-05 -0-13930E-06 -0-13665E-06 0-95964E-06 0-28349E-05
0-15941E-05 0-21784E-06 0-38647E-07 0-38872E-06 -0-88872E-06 -0-59512E-06 0-12799E-06 -0-30764E-07 0-90121E-07
0-26547E-06 0-18943E-06 0-54211E-07 0-95300E-06 -0-21171E-07 -0-65204E-07 -0-42977E-07 -0-15310E-07 -0-33498E-08

ROW 2
0-13172E-02 0-58823E-04 -0-59192E-05 0-31915E-04 0-86641E-05 0-24982E-05 0-33351E-04 -0-14617E-04 0-18260E-04
-0-84894E-08 -0-62897E-04 -0-51190E-04 -0-16094E-05 -0-74788E-05 0-15830E-05 0-24568E-04 0-22673E-04 0-59080E-05
-0-48477E-06 -0-64451E-06 -0-75489E-05 -0-85717E-05 -0-38230E-06 0-25818E-06 0-21324E-05 0-26926E-05
0-13432E-05 0-25823E-06 -0-85836E-07 0-68235E-06 -0-81224E-06 -0-49493E-06 -0-14881E-06 0-24359E-07 0-15941E-06
0-22882E-06 0-15631E-06 0-52544E-07 -0-53583E-08 -0-34919E-07 -0-48189E-07 -0-35639E-07 -0-16113E-07 0-15941E-06

ROW 3
0-13895E-02 0-52486E-04 -0-78875E-04 -0-16741E-04 -0-44856E-04 0-24359E-05 0-32835E-04 -0-42743E-04 0-90728E-06
-0-57516E-05 -0-52274E-04 -0-69822E-04 -0-48788E-05 -0-47779E-06 0-20489E-05 0-21181E-04 0-22971E-04 0-59188E-05
0-13895E-06 -0-89597E-04 -0-63272E-05 -0-63408E-05 -0-33816E-05 -0-34089E-07 0-24032E-06 0-17367E-05 0-26422E-05
0-14188E-05 0-18298E-07 -0-71950E-07 -0-47893E-06 -0-77281E-06 -0-54330E-06 -0-38232E-08 0-14279E-07 0-12231E-06
0-28250E-06 0-17865E-06 0-56859E-09 -0-34371E-08 -0-24781E-07 -0-41914E-07 -0-42411E-07

ROW 4
0-13359E-02 0-21947E-03 0-66937E-05 0-98966E-05 -0-42888E-04 0-24238E-03 0-95317E-04 0-15786E-06 0-15822E-05
-0-33898E-05 -0-68475E-04 -0-51862E-04 -0-67878E-07 0-21838E-06 0-21583E-05 0-24832E-04 0-25834E-04 -0-41563E-07
0-13724E-06 -0-14281E-05 -0-88186E-05 -0-18534E-04 0-19655E-07 -0-27495E-07 0-48229E-06 0-17188E-05 0-3224E-05
-0-66283E-08 0-54168E-08 -0-14572E-06 -0-14173E-06 -0-19184E-05 -0-22451E-08 -0-34342E-08 0-43758E-07 0-89321E-07
0-28884E-04 -0-41344E-09 0-27777E-09 -0-86644E-08 -0-12622E-07 -0-61235E-07

ROW 5
0-35848E-03 -0-42519E-05 0-18113E-04 -0-26434E-04 0-31474E-04 0-54589E-04 0-19268E-06 -0-11689E-05 0-48880E-05
-0-81151E-05 -0-27452E-04 -0-21594E-07 0-29244E-08 -0-28473E-06 -0-13458E-05 0-28441E-07 0-11344E-06
-0-22655E-06 0-75144E-07 0-34111E-05 0-61861E-09 -0-29699E-07 0-74182E-07 -0-76113E-07 0-93444E-06 -0-15846E-08
0-73243E-08 -0-27457E-07 0-38972E-07 -0-25688E-06 -0-38229E-09 -0-26224E-08 0-73580E-08 -0-12829E-07 0-65798E-07
-0-18435E-09 0-34557E-09 -0-12833E-08 0-26389E-08 -0-13492E-07

ROW 6
0-43484E-03 0-23688E-03 -0-87688E-04 0-35859E-04 -0-14436E-04 0-31334E-04 0-98229E-04 -0-48568E-04 0-23161E-04
-0-23446E-04 -0-67156E-04 0-68489E-06 -0-22638E-05 -0-26375E-06 0-26375E-06 0-02874E-05 0-21397E-04 0-63031E-05
-0-58184E-06 0-51257E-06 -0-26978E-05 -0-76272E-05 -0-33288E-05 -0-32824E-07 -0-87718E-07 0-86923E-08 0-24556E-05
0-18878E-06 0-14887E-06 0-22891E-07 -0-26889E-06 -0-76787E-06 -0-47248E-06 -0-87734E-07 -0-82854E-08 0-69157E-07
0-28414E-06 0-11371E-06 0-31246E-07 0-38323E-08

ROW 7
0-14142E-02 0-52578E-04 -0-38556E-05 0-36259E-04 0-78885E-05 0-22896E-03 0-22331E-04 -0-13991E-04 0-16879E-04
-0-39925E-06 -0-59846E-04 -0-51512E-04 -0-23289E-05 -0-19672E-06 0-69746E-06 0-28545E-04 0-19684E-04 0-39192E-05
-0-82898E-07 0-43761E-06 -0-57383E-05 -0-64889E-05 -0-24641E-05 -0-28162E-06 0-14111E-06 0-16485E-05 0-21182E-05
0-48470E-05 0-18288E-06 -0-18288E-06 -0-43874E-07 -0-43874E-06 -0-68329E-06 -0-35968E-06 -0-93873E-07 0-11124E-07 0-97987E-07
0-13677E-06 0-89835E-07 0-38715E-07

ROW 8
0-13941E-02 0-53510E-04 -0-88038E-04 -0-16888E-04 -0-44564E-04 0-22125E-03 0-22246E-04 -0-29582E-04 0-73869E-06
-0-55835E-04 -0-58817E-04 -0-58817E-04 -0-45888E-05 -0-35888E-06 0-14888E-05 0-18488E-04 0-24888E-04 0-46888E-05
0-14110E-06 -0-65857E-06 -0-58827E-05 -0-68888E-05 -0-25254E-05 -0-25254E-05 0-18412E-06 0-14288E-05 0-23110E-05
0-13378E-05 0-12888E-07 -0-44878E-07 -0-36888E-06 -0-58888E-06 -0-48888E-06 -0-19118E-08 0-11432E-07 0-78111E-07
0-11432E-07

NOT REPRODUCIBLE

ROW 20	0.41879E-03	-0.5591E-05	0.13278E-04	-0.30279E-04	0.23728E-04	-0.83747E-05	0.37029E-06	0.13225E-05	-0.14206E-07
	-0.2133E-05	-0.18952E-04	-0.18134E-06	0.67192E-07	-0.56812E-06	0.34340E-06	0.34980E-06	0.51925E-08	-0.14206E-07
	0.72809E-07	0.17139E-06	-0.13440E-05	-0.11071E-08	0.27410E-08	-0.27840E-07	0.31590E-07	0.44339E-06	
ROW 21	0.37530E-03	0.19010E-03	-0.67950E-04	0.28454E-04	-0.11042E-04	0.30221E-02	-0.37631E-04	0.12298E-04	
	-0.67741E-05	-0.18206E-04	-0.51176E-04	0.41977E-05	-0.27896E-05	0.20594E-06	0.41680E-05	0.15075E-04	0.32031E-05
	-0.7110E-06	0.41200E-06	-0.25848E-05	-0.67167E-05	-0.15224E-05	-0.13950E-04	0.22041E-07		
ROW 22	0.1134E-02	0.54017E-04	-0.12827E-05	0.27278E-04	0.75739E-05	0.17401E-03	0.14007E-04	-0.13113E-04	0.11239E-04
	0.67283E-05	-0.26101E-04	-0.32887E-04	0.12841E-06	0.38604E-06	-0.76254E-04	0.13635E-04	0.13294E-04	0.23563E-05
	-0.55175E-06	0.76490E-07	-0.37280E-05	-0.41970E-05	-0.13148E-05	-0.93010E-07			
ROW 23	0.11323E-02	0.47261E-04	-0.63576E-04	-0.14439E-04	-0.26480E-04	0.18422E-03	0.12889E-04	-0.21744E-04	-0.28940E-05
	-0.89830E-05	-0.26825E-04	-0.37400E-04	-0.31010E-05	-0.54734E-06	-0.15999E-05	0.13250E-04	0.12235E-04	0.31292E-05
	-0.28990E-07	-0.72746E-06	-0.36430E-05	-0.44774E-05	-0.13050E-05				
ROW 24	0.11490E-02	0.19446E-03	0.82519E-05	0.16860E-04	-0.58619E-04	0.17982E-03	0.55405E-04	0.28624E-05	0.57830E-05
	-0.53232E-05	-0.46734E-04	-0.55689E-04	0.29432E-06	0.62982E-06	-0.23427E-04	0.12640E-04	0.15262E-04	0.4497E-07
	0.14692E-06	-0.30149E-06	-0.44014E-05	-0.49493E-05					
ROW 25	0.35309E-03	-0.57900E-05	0.1281E-04	-0.28303E-04	0.26254E-04	0.21033E-04	-0.11045E-05	-0.32130E-06	-0.19054E-07
	-0.15778E-05	-0.10330E-04	-0.15610E-06	-0.71521E-07	-0.16982E-06	-0.24412E-06	0.55405E-05	-0.40310E-06	-0.10141E-06
	0.21531E-04	-0.28829E-06	-0.18531E-05						
ROW 26	0.37105E-03	0.18806E-03	-0.68270E-04	0.28760E-04	-0.11625E-04	0.25966E-05	0.83989E-04	-0.37550E-04	0.16950E-04
	-0.63150E-05	-0.79201E-05	-0.40333E-04	0.42642E-05	-0.23739E-05	0.32184E-06	0.70149E-05	0.18223E-04	0.38792E-06
	0.65266E-06	0.94997E-07							
ROW 27	0.11284E-02	0.48811E-04	-0.28812E-06	0.27173E-04	0.85822E-05	0.17842E-04	0.14619E-04	-0.12989E-04	0.11364E-04
	0.76980E-05	-0.22764E-04	-0.36804E-04	0.14311E-05	0.24058E-06	-0.10773E-06	0.15126E-04	0.11262E-04	0.17280E-05
	-0.31879E-06								
ROW 28	0.11230E-02	0.41429E-04	-0.63339E-04	-0.17862E-04	-0.59030E-04	0.10712E-05	0.11920E-04	-0.22233E-04	-0.26500E-05
	-0.77655E-05	-0.23575E-04	-0.33399E-04	-0.16556E-05	-0.13336E-06	-0.46688E-07	0.14762E-04	0.12022E-04	0.25240E-05
ROW 29	0.11377E-02	0.18932E-03	0.89315E-05	0.15659E-04	-0.58254E-04	0.18150E-03	0.58366E-04	0.19400E-05	0.02805E-05
	-0.43230E-05	-0.31800E-04	-0.31847E-04	0.41590E-07	0.10056E-05	-0.56742E-06	0.16558E-04	0.12866E-04	
ROW 30	0.33313E-03	-0.59170E-05	0.11080E-04	-0.28627E-04	0.26656E-04	0.24387E-04	-0.12457E-05	0.10733E-05	-0.43534E-06
	0.12783E-06	-0.17226E-04	-0.14651E-06	0.85431E-07	-0.57764E-06	0.13276E-05	0.59915E-05		
ROW 31	0.37543E-03	0.19092E-03	-0.66600E-04	0.28220E-04	-0.11014E-04	-0.37849E-05	0.76134E-04	-0.42023E-04	0.17886E-04
	-0.65537E-05	-0.19658E-04	-0.56517E-04	0.11374E-04	-0.52279E-05	0.11880E-05			
ROW 32	0.11233E-02	0.51889E-04	0.38663E-06	0.27840E-04	0.33918E-05	0.16633E-03	0.59456E-05	-0.15268E-04	0.12262E-04
	0.33828E-05	-0.35531E-04	-0.39090E-04	0.33380E-05	-0.66187E-07				
ROW 33	0.11262E-02	0.44070E-04	-0.62720E-04	-0.19075E-04	-0.62884E-04	0.17534E-03	0.59915E-06	-0.25804E-04	-0.19756E-05
	-0.23272E-04	-0.33670E-04	-0.37262E-04	-0.23582E-05					

9.17796E-02	0.14177E-03	0.95535E-05	0.14485E-04	-0.63487E-04	0.16349E-03	2.46444E-04	0.12450E-03	8.46478E-02
0.80667E-05	-0.48066E-04	-0.27071E-04						

[illegible]

ROW	35								
0.34431E-03	-0.5752E-05	0.12055E-04	-0.26919E-04	0.19448E-04	0.10243E-04	-0.58716E-06	-0.9801E-06	0.35050E-05	
0.02404E-05	-0.28118E-06								

-0.02106E-05 -0.20318E-04

80W 36
 0.3779E-03 0.28266E-03 -0.6359E-04 0.26162E-04 -0.12011E-04 0.50121E-04 0.12036E-03 -0.60325E-04 0.32645E-04
 -0.11799E-04

6.117085-04

ROW 37
 0.116987-N2 0.63533E-N4 11.42868E-N5 8.2686NE-N4 0.12725E-N5 0.29524E-N4 -0.1342E-N4 0.12585E-N4

ROW	JN	ROW	JN
0.11611E+02	0.50000E+04	-0.06278E+04	-0.20401E+05
			-0.28176E+04
			0.22072E+03
			0.23342E+04
			-0.16692E+04

ROW 39

8.11975E+02	8.21002E+03	0.13571E+05	0.17752E+04	-0.35053E+04	0.23341E+03	8.43800E+04
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ROW	ID	DATE	TIME	STATUS
00	0-36888E-01	-0.16202E+05	9.1111E-04	0.5414E-04
01	0-36888E-01	-0.16202E+05	9.1111E-04	0.42861E-04

PAM 41
 P-86339E-N4 H-59140E-N4 -W-34040E-04 P-14584E-N4 -P-66648E-05

row	42	9.49425E-03	-1.82155E-04	1.26418E-04	0.11511E-04
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00W 43
0.53042E-03 -0.77820E-04 -0.24295E-04

FORM 44
8-47322E-03 0-71210E-04

45
 45
 0-12485E-03

NOT REPRODUCIBLE

HERE ARE THE EIGENVALUES AND EIGENVECTORS

EIGENVECTOR NUMBER	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150	151	152	153	154	155	156	157	158	159	160	161	162	163	164	165	166	167	168	169	170	171	172	173	174	175	176	177	178	179	180	181	182	183	184	185	186	187	188	189	190	191	192	193	194	195	196	197	198	199	200	201	202	203	204	205	206	207	208	209	210	211	212	213	214	215	216	217	218	219	220	221	222	223	224	225	226	227	228	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379	380	381	382	383	384	385	386	387	388	389	390	391	392	393	394	395	396	397	398	399	400	401	402	403	404	405	406	407	408	409	410	411	412	413	414	415	416	417	418	419	420	421	422	423	424	425	426	427	428	429	430	431	432	433	434	435	436	437	438	439	440	441	442	443	444	445	446	447	448	449	450	451	452	453	454	455	456	457	458	459	460	461	462	463	464	465	466	467	468	469	470	471	472	473	474	475	476	477	478	479	480	481	482	483	484	485	486	487	488	489	490	491	492	493	494	495	496	497	498	499	500	501	502	503	504	505	506	507	508	509	510	511	512	513	514	515	516	517	518	519	520	521	522	523	524	525	526	527	528	529	530	531	532	533	534	535	536	537	538	539	540	541	542	543	544	545	546	547	548	549	550	551	552	553	554	555	556	557	558	559	560	561	562	563	564	565	566	567	568	569	570	571	572	573	574	575	576	577	578	579	580	581	582	583	584	585	586	587	588	589	590	591	592	593	594	595	596	597	598	599	600	601	602	603	604	605	606	607	608	609	610	611	612	613	614	615	616	617	618	619	620	621	622	623	624	625	626	627	628	629	630	631	632	633	634	635	636	637	638	639	640	641	642	643	644	645	646	647	648	649	650	651	652	653	654	655	656	657	658	659	660	661	662	663	664	665	666	667	668	669	670	671	672	673	674	675	676	677	678	679	680	681	682	683	684	685	686	687	688	689	690	691	692	693	694	695	696	697	698	699	700	701	702	703	704	705	706	707	708	709	710	711	712	713	714	715	716	717	718	719	720	721	722	723	724	725	726	727	728	729	730	731	732	733	734	735	736	737	738	739	740	741	742	743	744	745	746	747	748	749	750	751	752	753	754	755	756	757	758	759	760	761	762	763	764	765	766	767	768	769	770	771	772	773	774	775	776	777	778	779	780	781	782	783	784	785	786	787	788	789	790	791	792	793	794	795	796	797	798	799	800	801	802	803	804	805	806	807	808	809	810	811	812	813	814	815	816	817	818	819	820	821	822	823	824	825	826	827	828	829	830	831	832	833	834	835	836	837	838	839	840	841	842	843	844	845	846	847	848	849	850	851	852	853	854	855	856	857	858	859	860	861	862	863	864	865	866	867	868	869	870	871	872	873	874	875	876	877	878	879	880	881	882	883	884	885	886	887	888	889	890	891	892	893	894	895	896	897	898	899	900	901	902	903	904	905	906	907	908	909	910	911	912	913	914	915	916	917	918	919	920	921	922	923	924	925	926	927	928	929	930	931	932	933	934	935	936	937	938	939	940	941	942	943	944	945	946	947	948	949	950	951	952	953	954	955	956	957	958	959	960	961	962	963	964	965	966	967	968	969	970	971	972	973	974	975	976	977	978	979	980	981	982	983	984	985	986	987	988	989	990	991	992	993	994	995	996	997	998	999	1000	1001	1002	1003	1004	1005	1006	1007	1008	1009	1010	1011	1012	1013	1014	1015	1016	1017	1018	1019	1020	1021	1022	1023	1024	1025	1026	1027	1028	1029	1030	1031	1032	1033	1034	1035	1036	1037	1038	1039	1040	1041	1042	1043	1044	1045	1046	1047	1048	1049	1050	1051	1052	1053	1054	1055	1056	1057	1058	1059	1060	1061	1062	1063	1064	1065	1066	1067	1068	1069	1070	1071	1072	1073	1074	1075	1076	1077	1078	1079	1080	1081	1082	1083	1084	1085	1086	1087	1088	1089	1090	1091	1092	1093	1094	1095	1096	1097	1098	1099	1100	1101	1102	1103	1104	1105	1106	1107	1108	1109	1110	1111	1112	1113	1114	1115	1116	1117	1118	1119	1120	1121	1122	1123	1124	1125	1126	1127	1128	1129	1130	1131	1132	1133	1134	1135	1136	1137	1138	1139	1140	1141	1142	1143	1144	1145	1146	1147	1148	1149	1150	1151	1152	1153	1154	1155	1156	1157	1158	1159	1160	1161	1162	1163	1164	1165	1166	1167	1168	1169	1170	1171	1172	1173	1174	1175	1176	1177	1178	1179	1180	1181	1182	1183	1184	1185	1186	1187	1188	1189	1190	1191	1192	1193	1194	1195	1196	1197	1198	1199	1200	1201	1202	1203	1204	1205	1206	1207	1208	1209	1210	1211	1212	1213	1214	1215	1216	1217	1218	1219	1220	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NOT REPRODUCIBLE

EIGENVECTOR NUMBER 7
CORRESPONDING TO 1.7501530E 10
-1.0600879E-01 -4.2296745E-02 -1.1112333E-01 9.4331717E-02 2.0041379E-01 6.4204345E-02
-1.0361408E-01 -7.0220013E-02 1.7056659E-01 5.1084369E-01 2.7178799E-01 -1.1319053E-01
-2.1433201E-01 7.4702497E-02 5.5755368E-01 5.7348539E-01 -4.7469770E-02 -3.4759420E-01
-1.3400930E-01 3.0450106E-01 7.7272730E-01 2.5504050E-02 -3.9060222E-01 -2.3070004E-01
-7.9537000E-01 8.559599E-01 5.7730060E-02 -3.7740155E-01 -1.9577907E-01 3.7627295E-01
-1.2055652E-01 -1.5326722E-01 -1.9555979E-01 5.0702436E-02 4.4003194E-01 5.0369403E-01
-0.6926320E-02 -2.1190833E-01 -1.7798899E-01 9.1759127E-02 1.0000000E 00 3.4910105E-01
-1.0607690E-01 -3.7443474E-01 -2.4227099E-01

EIGENVECTOR NUMBER 8
CORRESPONDING TO 2.6717637E 10
-6.6422000E-01 -5.1034002E-01 -4.2460090E-01 -3.0272240E-01 -1.4560013E-01 -7.1545954E-01
-1.7609942E-01 -6.7001331E-01 -4.6143620E-01 -2.1063632E-01 3.4936472E-01 3.0027935E-03
-4.1520101E-02 5.3331205E-02 2.6193635E-01 1.0000000E 00 0.9322210E-01 4.0331724E-01
-4.9664120E-01 6.4001503E-01 5.7419531E-01 4.2422572E-01 2.6299009E-01 7.3829619E-01
-3.3011120E-01 -3.7424004E-01 -2.9433837E-01 -3.2613491E-01 -3.4251430E-01 -3.0312624E-01
-7.0632005E-01 -6.1112500E-01 -5.4779473E-01 -5.5021771E-01 -5.0105000E-01 -1.4360307E-01
-1.0061044E-01 -2.5006722E-02 -1.9773070E-02 -0.9958304E-02 0.5450917E-01 0.7190740E-01
-9.3906379E-01 9.5329414E-01 0.0056630E-01

EIGENVECTOR NUMBER 9
CORRESPONDING TO 4.1560024E 10
-4.3037630E-01 -6.6936680E-03 1.0041001E-01 2.2613313E-02 -2.4785900E-01 -0.3947799E-01
-6.0040405E-03 3.9005055E-01 0.7623704E-02 -6.1076903E-01 -0.2626345E-01 0.0230925E-02
-5.3105007E-01 1.0051402E-01 -7.0004956E-01 -5.0073042E-01 1.4670007E-01 4.0050010E-01
-7.2201010E-02 -0.0021923E-01 -1.9712706E-02 1.0004444E-01 2.3616310E-01 7.0070392E-03
-4.3976157E-01 9.0779975E-02 -1.0025669E-02 -5.9391035E-02 -5.0400103E-02 -0.7915545E-02
-4.0030569E-01 -1.1002594E-01 -3.1425066E-01 -6.7074904E-02 3.7100735E-01 7.0050100E-01
-1.1926194E-01 -4.5043051E-01 -2.7503707E-02 7.6240514E-01 9.1303102E-01 -7.7500135E-02
-5.0794306E-01 1.6225750E-02 1.0000000E 00

HERE ARE THE NATURAL FREQUENCIES

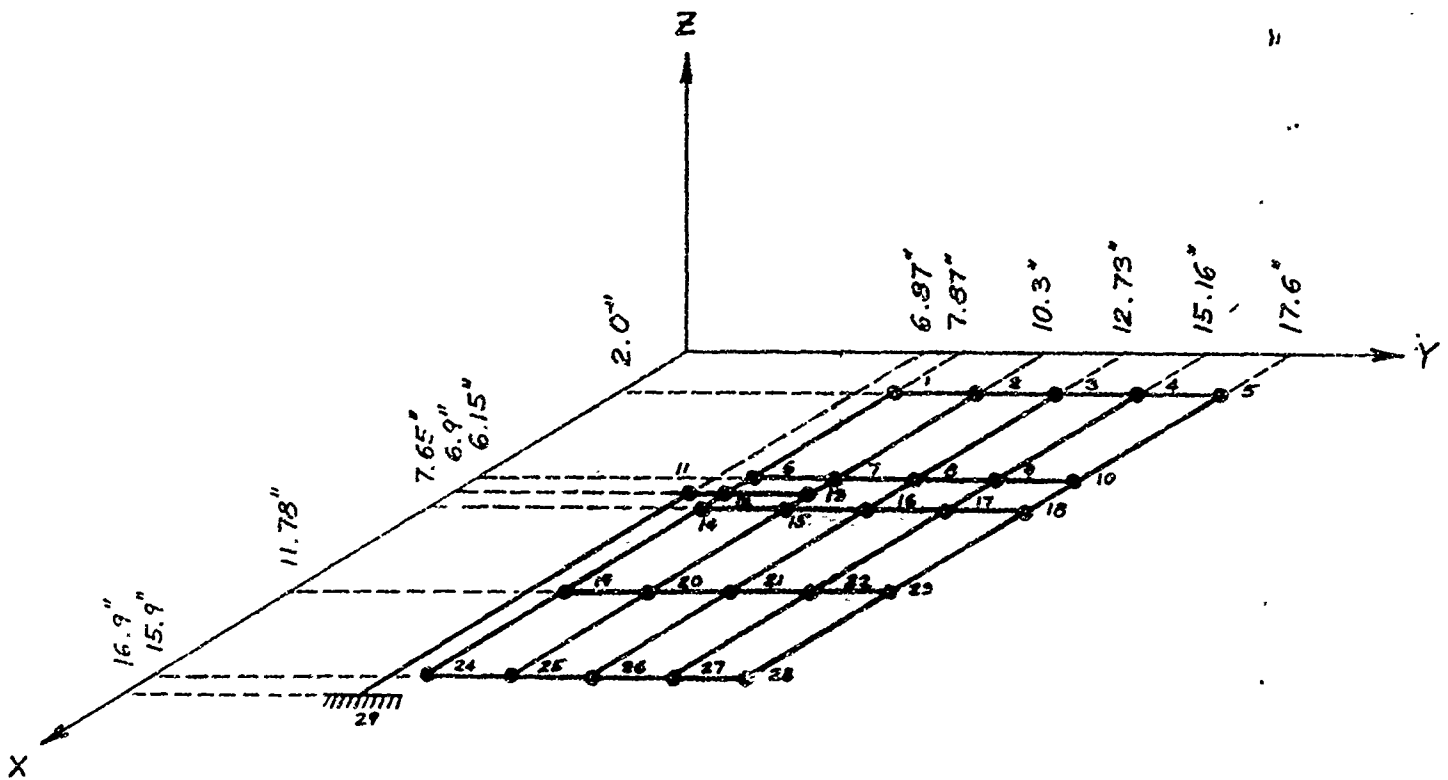
THE NATURAL FREQUENCY NUMBER	1	IS	764.610	CPS
THE NATURAL FREQUENCY NUMBER	2	IS	3438.107	CPS
THE NATURAL FREQUENCY NUMBER	3	IS	4058.889	CPS
THE NATURAL FREQUENCY NUMBER	4	IS	11001.007	CPS
THE NATURAL FREQUENCY NUMBER	5	IS	13177.622	CPS
THE NATURAL FREQUENCY NUMBER	6	IS	20579.985	CPS
THE NATURAL FREQUENCY NUMBER	7	IS	21103.287	CPS
THE NATURAL FREQUENCY NUMBER	8	IS	20814.720	CPS
THE NATURAL FREQUENCY NUMBER	9	IS	20274.123	CPS

EXTRACTED FROM

Sample Problem No. 3

Missile Control Surface Model
(Modeled with beam elements and lumped weights)

Find first five natural modes and frequencies.



Note: Joint 11 is restrained from rotating about y

Lumped Masses

Joint No.	Mass lb.
1	0.050
2	0.110
3	0.115
4	0.125
5	0.196
6	0.155
7	0.305
8	0.305
9	0.305
10	0.165
11	0.060
12	0.165
13	0.005
14	0.183
15	0.325
16	0.310
17	0.280
18	0.140
19	0.062
20	0.078
21	0.078
22	0.078
23	0.080
24	0.033
25	0.051
26	0.051
27	0.051
28	0.042
29	0.050

Beam Element Properties

Member i - j	Moment-of-Inertia Area	Torsional Constant
	inch ⁴	
1-2	0.0009	0.0055
2-3	0.0009	0.0055
3-4	0.0009	0.0055
4-5	0.0018	0.0055
6-7	0.0164	0.0300
7-8	0.0164	0.0300
8-9	0.0164	0.0300
9-12	0.0164	0.0300
12-13	0.0160	0.0300
14-15	0.0147	0.0280
15-16	0.0147	0.0280
16-17	0.0147	0.0280
17-18	0.0147	0.0280
19-20	0.0053	0.0010
20-21	0.0053	0.0010
21-22	0.0053	0.0010
22-23	0.0053	0.0010
24-25	0.0031	0.0006
25-26	0.0031	0.0006
26-27	0.0031	0.0006
27-28	0.0031	0.0006
1-6	0.0013	0.0026
2-7	0.0027	0.0054
3-8	0.0027	0.0054
4-9	0.0027	0.0054
5-10	0.0026	0.0029
6-12	0.0503	0.1000
12-14	0.0503	0.1000
7-13	0.0255	0.0510
13-15	0.0255	0.0510
8-16	0.0380	0.0750
9-17	0.0380	0.0750
10-18	0.0377	0.0750
14-19	0.0017	0.0034
15-20	0.0035	0.0070
16-21	0.0035	0.0070
17-22	0.0035	0.0070
18-23	0.0017	0.0029
11-12	100.0000	0.0100
11-29	0.3200	0.0790
19-24	0.0017	0.0030
20-25	0.0017	0.0030
21-26	0.0035	0.0070
22-27	0.0035	0.0070
23-28	0.0017	0.0029

$$E = 3 \times 10^7 \text{ psi}$$

$$\nu = 0.3$$

Listing of Input Data Cards

MISSILE CONTROL SURFACE MODEL WITH 29 JOINTS
AUGUST 1968

29	2	45	0	9	1	29
1						
30.	0.5		0.		0.	
1	2.0		7.87			
2	2.0		10.5			
3	2.0		12.73			
4	2.0		15.16			
5	2.0		17.6			
6	6.15		7.87			
7	6.15		10.5			
8	6.15		12.73			
9	6.15		15.16			
10	6.15		17.6			
11	6.9		6.87			
12	6.9		7.87			
13	6.9		10.5			
14	7.65		7.87			
15	7.65		10.5			
16	7.65		12.73			
17	7.65		15.16			
18	7.65		17.6			
19	11.78		7.87			
20	11.78		10.5			
21	11.78		12.73			
22	11.78		15.16			
23	11.78		17.6			
24	15.9		7.87			
25	15.9		10.5			
26	15.9		12.73			
27	15.9		15.16			
28	15.9		17.6			
29	16.9		6.87			
11	0	0	1			
20	1	1	1			
1	0.05					
2	0.11					
3	0.115					
4	0.125					
5	0.196					
6	0.155					
7	0.305					
8	0.305					
9	0.305					
10	0.165					
11	0.06					
12	0.165					
13	0.005					
14	0.183					
15	0.325					
16	0.31					
17	0.28					

18	0.14				
19	0.062				
20	0.078				
21	0.078				
22	0.078				
23	0.08				
24	0.033				
25	0.051				
26	0.051				
27	0.051				
28	0.042				
29	0.050				
0.	0.0009	0.0055	1	1	2
0.	0.0009	0.0055	1	2	3
0.	0.0009	0.0055	1	3	4
0.	0.0018	0.0055	1	4	5
0.	0.0164	0.03	1	5	7
0.	0.0164	0.13	1	7	8
0.	0.0164	0.13	1	8	9
0.	0.0164	0.03	1	9	10
0.	0.016	0.03	1	12	13
0.	0.0147	0.028	1	14	15
0.	0.0147	0.028	1	15	16
0.	0.0147	0.028	1	16	17
0.	0.0147	0.028	1	17	18
0.	0.0053	0.001	1	19	20
0.	0.0053	0.001	1	20	21
0.	0.0053	0.001	1	21	22
0.	0.0053	0.001	1	22	23
0.	0.0031	0.006	1	24	25
0.	0.0031	0.006	1	25	26
0.	0.0031	0.006	1	26	27
0.	0.0031	0.006	1	27	28
0.	0.0013	0.0026	1	1	6
0.	0.0027	0.0054	1	2	7
0.	0.0027	0.0054	1	3	8
0.	0.0027	0.0054	1	4	9
0.	0.0026	0.0029	1	5	10
0.	0.0503	0.1	1	6	12
0.	0.0503	0.1	1	12	14
0.	0.0255	0.051	1	7	13
0.	0.0255	0.051	1	13	15
0.	0.038	0.075	1	8	16
0.	0.038	0.075	1	9	17
0.	0.0377	0.075	1	10	18
0.	0.0017	0.0034	1	14	19
0.	0.0035	0.007	1	15	20
0.	0.0035	0.007	1	16	21
0.	0.0035	0.007	1	17	22
0.	0.0017	0.0029	1	18	23
0.	100.	0.01	1	11	12
0.	0.32	0.079	1	11	29

0.	0.0017	0.003	1	19	24
0.	0.0017	0.003	1	20	25
0.	0.0035	0.007	1	21	26
0.	0.0035	0.007	1	22	27
0.	0.0017	0.0029	1	23	28

Program Output

END OF PROGRAM

MISSILE CONTROL SURFACE MODEL WITH 29 JOINTS

AUGUST 1968

UNIT = 20 MR = 2 MRL = 45 MPE = 0 MPODE = 9 MKEY = 1 MUMP = 29

MATERIAL PROPERTIES
 NO. YOUNG'S MODULUS POISSON RATIO MODULUS OF RIGIDITY DENSITY
 1 9.3000E 08 0.30000 0.11530E 08 8.

JOINT COORDINATES

JOINT NO.	X COORD.	Y COORD.
1	2.00000	1.00000
2	2.00000	10.30000
3	2.00000	12.70000
4	2.00000	14.10000
5	2.00000	17.60000
6	6.15000	7.00000
7	6.15000	10.30000
8	6.15000	17.70000
9	6.15000	15.10000
10	6.15000	17.60000
11	6.90000	6.00000
12	6.90000	7.00000
13	6.90000	10.30000
14	7.65000	7.00000
15	7.65000	10.30000
16	7.65000	12.70000
17	7.65000	15.10000
18	7.65000	17.60000
19	11.70000	7.00000
20	11.70000	10.30000
21	11.70000	12.70000
22	11.70000	15.10000
23	11.70000	17.60000
24	15.90000	7.00000
25	15.90000	10.30000
26	15.90000	12.70000
27	15.90000	15.10000
28	15.90000	17.60000
29	16.90000	6.00000

JOINT RESTRAINT CODE

JOINT NO.	Z DISPLACEMENT	ROTATION ABOUT X	ROTATION ABOUT Y
1	1	1	1
2	1	1	1
3	1	1	1
4	1	1	1
5	1	1	1
6	1	1	1
7	1	1	1
8	1	1	1
9	1	1	1
10	1	1	1
11	1	1	1
12	1	1	1
13	1	1	1
14	1	1	1
15	1	1	1
16	1	1	1
17	1	1	1
18	1	1	1
19	1	1	1
20	1	1	1
21	1	1	1
22	1	1	1
23	1	1	1
24	1	1	1
25	1	1	1
26	1	1	1
27	1	1	1
28	1	1	1
29	1	1	1

COORDINATE NUMBERS FOR EACH Z DISPLACEMENT AT EACH UNRESTRAINED JOINT

JOINT NO.	COORD. NO.
1	1
2	2
3	3
4	4
5	5
6	6
7	7
8	8
9	9
10	10
11	11
12	12
13	13
14	14
15	15
16	16
17	17
18	18
19	19
20	20
21	21
22	22
23	23
24	24
25	25
26	26
27	27
28	28
29	29

NOT REPRODUCIBLE

NOT REPRODUCIBLE

LUMPFED WEIGHTS

JOINT NO. WEIGHT

1 0.0500

2 0.1100

3 0.1150

4 0.1250

5 0.1900

6 0.1550

7 0.3050

8 0.3050

9 0.1650

10 0.1650

11 0.1650

12 0.1650

13 0.1850

14 0.1850

15 0.3750

16 0.3100

17 0.2000

18 0.1400

19 0.0620

20 0.0700

21 0.0700

22 0.0700

23 0.0700

24 0.4350

25 0.0510

26 0.0510

27 0.0510

28 0.0420

29 0.0500

BEAR ELEMENT PROPERTIES

ELEMENT NO.

1 0.0000

2 0.0000

3 0.0000

J

0.0055

0.0055

0.0055

MAY

1

1

1

JOINT 1

1

2

3

JOINT 2

1

2

3

NOT REPRODUCIBLE

NOT REPRODUCIBLE

REDUCED UPPER TRIANGULAR STIFFNESS MATRIX

ROW 1		0.06370E 04	-0.10372E 05	0.43303E 04	-0.11434E 04	0.18516E 03	-0.19469E 05	0.49571E 04	0.10394E 04	-0.10302E 03
		0.74071E 02	-0.16368E 04	0.19325E 05	-0.30610E 04	-0.30340E 04	0.60852E 03	-0.25693E 03	-0.12255E 03	-0.21745E 01
		0.20821E 01	-0.01275E 00	0.30503E 01	-0.24938E 00	0.37647E 00	-0.53375E 00	0.31600E 00	-0.47100E 00	-0.13917E 00
		0.13291E-01								
ROW 2		0.20272E 05	-0.21023E 05	0.60005E 04	-0.14128E 04	0.41947E 04	-0.36024E 05	0.28599E 04	0.13471E 04	-0.29345E 02
		0.27036E 04	-0.53409E 04	0.34012E 05	-0.42998E 03	-0.60817E 04	-0.62565E 03	-0.15365E 03	-0.11234E 03	0.32691E 00
		0.13398E 02	0.10761E 02	0.43540E 01	-0.16751E 00	0.20311E 00	-0.27459E 01	-0.11971E 01	-0.30642E 00	-0.50225E-01
ROW 3		0.30019E 05	-0.23913E 05	0.50000E 04	0.17271E 04	0.31501E 04	-0.20526E 05	0.30601E 04	0.07509E 03	-0.16150E 04
		0.12202E 04	-0.15187E 04	0.23309E 03	-0.20905E 03	0.11340E 05	-0.49307E 03	-0.39950E 03	0.13107E 01	0.41306E 00
		-0.11200E 03	0.04309E 01	0.11333E 01	-0.54035E 00	-0.30371E 00	0.19166E 02	-0.10747E 01	-0.00094E 00	
ROW 4		0.35030E 05	-0.13590E 05	-0.15172E 03	0.20009E 04	0.26002E 04	-0.21412E 05	0.40015E 04	0.64310E 03	-0.10490E 04
		-0.1111E 0	0.0111E 0	0.0111E 0	0.0111E 0	0.0111E 0	0.0111E 0	0.0111E 0	0.0111E 0	0.0111E 0

RECEIVED

72:

1 NOV 1964

2 NOV 68

NO 1

40

[illegible]

ROW 5	0.12121E 05	0.14984E 03	0.44181E 02	0.12191E 04	0.44253E 04	0.17727E 03	0.15410E 03	0.15688E 03	0.32540E 03
	0.36594E 02	0.47458E 02	0.27465E 03	0.40055E 03	0.98047E 04	0.46764E 03	0.12745E 03	0.38319E 01	0.11910E 02
	0.56238E 02	0.31910E 02	0.51089E 03	0.95181E 03	0.13530E 01	0.93892E 01			
ROW 6	0.62807E 02	0.74782E 06	0.94104E 05	0.21837E 05	0.29938E 04	0.23869E 06	0.11222E 08	0.56881E 06	0.54317E 07
	0.78634E 05	0.15897E 05	0.66798E 04	0.14826E 04	0.53089E 04	0.25777E 01	0.17654E 03	0.11861E 03	0.38269E 02
	0.97516E 03	0.56051E 02	0.41797E 02	0.17177E 02	0.73897E 08				
ROW 7	0.43331E 07	0.50141E 06	0.31141E 06	0.18158E 05	0.51545E 06	0.28952E 06	0.67228E 07	0.70567E 05	0.29776E 07
	0.12239E 06	0.51069E 05	0.50182E 04	0.50182E 03	0.50182E 03	0.13744E 04	0.25888E 03	0.10385E 03	0.06910E 02
	0.13109E 04	0.23713E 03	0.19014E 02	0.19014E 02					
ROW 8	0.87938E 06	0.47870E 04	0.76228E 05	0.18785E 06	0.15349E 06	0.29888E 05	0.14110E 05	0.18888E 06	0.36673E 30
	0.13488E 06	0.11986E 05	0.18048E 03	0.51089E 03	0.19943E 05	0.40331E 03	0.72374E 02	0.10344E 03	0.12888E 03
	0.30835E 04	0.17787E 03	0.75148E 02						
ROW 9	0.78198E 06	0.31887E 04	0.26485E 05	0.37328E 05	0.15956E 05	0.70105E 04	0.29979E 05	0.13489E 06	0.43694E 06
	0.18446E 06	0.17818E 03	0.18388E 03	0.68875E 03	0.19243E 05	0.56628E 03	0.25777E 02	0.4382E 02	0.18679E 03
	0.38888E 04	0.19762E 03							
ROW 10	0.32158E 06	0.44139E 04	0.63475E 04	0.12238E 04	0.14177E 04	0.64281E 04	0.12678E 05	0.18821E 06	0.25710E 06
	0.15172E 02	0.01726E 02	0.19164E 03	0.90481E 03	0.98549E 04	0.53888E 01	0.14148E 02	0.69718E 02	0.15674E 03
	0.20820E 04								
ROW 11	0.17888E 07	0.19994E 07	0.32981E 06	0.21365E 06	0.29282E 06	0.98888E 05	0.24283E 05	0.39738E 04	0.23969E 04
	0.41588E 04	0.24663E 04	0.88465E 03	0.17838E 03	0.99710E 02	0.13978E 03	0.77438E 02	0.50434E 02	0.13183E 02
ROW 12	0.25195E 08	0.16063E 07	0.11253E 08	0.20228E 06	0.13921E 06	0.34675E 05	0.56888E 04	0.33892E 05	0.40568E 04
	0.27639E 04	0.12568E 04	0.21810E 03	0.57925E 04	0.21637E 03	0.36544E 03	0.11893E 02	0.32188E 02	
ROW 13	0.13641E 08	0.52055E 06	0.67305E 07	0.58988E 05	0.81838E 04	0.28828E 04	0.63838E 03	0.53419E 05	0.24247E 04
	0.18841E 03	0.13694E 03	0.58209E 03	0.78512E 04	0.22189E 03	0.22977E 03	0.57862E 02		
ROW 14	0.62167E 07	0.68926E 06	0.84837E 05	0.17532E 05	0.25987E 04	0.35568E 05	0.13163E 04	0.15888E 04	0.34254E 03
	0.12187E 03	0.78824E 04	0.49888E 03	0.37836E 03	0.10781E 03	0.11752E 02			
ROW 15	0.43185E 07	0.44449E 06	0.98821E 05	0.14948E 05	0.25488E 04	0.58738E 05	0.36121E 03	0.14351E 04	0.23727E 03
	0.59889E 03	0.95839E 04	0.21205E 03	0.24131E 03	0.88296E 02				
ROW 16	0.04315E 06	0.43355E 06	0.67245E 05	0.91798E 03	0.14139E 04	0.59128E 05	0.18181E 04	0.69393E 03	0.23474E 03
	0.28677E 03	0.91971E 04	0.58817E 03	0.14834E 03					
ROW 17	0.76125E 06	0.38137E 06	0.24407E 03	0.17832E 04	0.17458E 04	0.39328E 05	0.25519E 04	0.55816E 02	0.11882E 03
	0.39111E 03	0.81188E 04	0.37639E 03						
ROW 18	0.31213E 06	0.88647E 02	0.27658E 03	0.78250E 03	0.22157E 04	0.28817E 05	0.79818E 01	0.43558E 02	0.14365E 03
	0.33854E 03	0.41343E 04							
ROW 19	0.85668E 05	0.47934E 05	0.27688E 05	0.67282E 04	0.18186E 04	0.72441E 04	0.39688E 04	0.25735E 03	0.87764E 02

0.74730E 02

ROW 20 0.13911E 06 -0.11803E 06 0.48182E 05 -0.64630E 04 0.39580E 04 -0.12142E 05 -0.28724E 04 0.13792E 04 -0.28031E 03

ROW 21 0.18527E 06 -0.11801E 06 0.26942E 05 0.26947E 03 0.28675E 04 -0.13399E 05 0.31878E 04 0.00975E 03

ROW 22 0.14375E 06 -0.47169E 05 -0.95025E 02 0.13010E 04 0.31995E 04 -0.14789E 05 0.39842E 04

ROW 23 0.35523E 05 0.78831E 02 -0.20181E 03 0.88768E 03 0.39857E 04 -0.76779E 04

ROW 24 0.15548E 05 -0.27452E 05 0.16544E 05 -0.48397E 04 0.61450E 03

ROW 25 0.73158E 05 -0.63827E 05 0.23654E 05 -0.38210E 04

ROW 26 0.97933E 05 -0.63957E 05 0.15830E 05

ROW 27 0.74114E 05 -0.27225E 05

ROW 28 0.15845E 05

REFLECTOR UPPER TRIANGULAR FLEXIBILITY MATRIX

ROW 1 0.46916E-03 0.38422E-03 0.35257E-03 0.36603E-03 0.51584E-04 0.79629E-04 0.10505E-03 0.12039E-03
0.15181E-03 0.87414E-03 0.19157E-04 0.44482E-04 -0.12834E-04 0.96582E-05 0.32235E-04 0.54675E-04 0.72882E-04
-0.28877E-03 -0.18272E-03 -0.16479E-03 -0.14581E-03 -0.12589E-03 -0.37738E-03 -0.35554E-03 -0.30152E-03
-0.32311E-03

ROW 2 0.49723E-03 0.55666E-03 0.02817E-03 0.69754E-03 0.76772E-04 0.17215E-03 0.26864E-03 0.36271E-03 0.45575E-03
0.88844E-03 0.44482E-04 0.33517E-03 0.12415E-04 0.98810E-04 0.18953E-03 0.28169E-03 0.37412E-03 -0.18282E-03
-0.18376E-03 -0.28785E-04 0.64638E-04 0.15182E-03 -0.39384E-03 -0.31146E-03 -0.22954E-03 -0.14684E-03 -0.63813E-04

ROW 3 0.76888E-03 0.92198E-03 0.18782E-02 0.18282E-03 0.26489E-03 0.43803E-03 0.61332E-03 0.78656E-03 0.89273E-03
0.68888E-04 0.27715E-03 0.37889E-04 0.18888E-03 0.35367E-03 0.52361E-03 0.69536E-03 -0.16977E-03 -0.21599E-04
0.33833E-03 0.28742E-03 0.48821E-03 -0.39228E-03 -0.24259E-03 -0.92822E-04 0.68194E-04 0.21458E-03

ROW 4 0.12342E-02 0.14961E-02 0.12738E-03 0.35738E-03 0.61186E-03 0.87835E-03 0.11439E-02 0.98285E-02 0.95134E-04
0.31941E-03 0.62882E-04 0.28185E-03 0.42882E-03 0.77932E-03 0.18425E-02 -0.15379E-03 0.65915E-04 0.29248E-03
0.52825E-03 0.73869E-03 -0.38821E-03 -0.16456E-03 0.68825E-04 0.28915E-03 0.52897E-03

ROW 5 0.19592E-02 0.15278E-03 0.44992E-03 0.78556E-03 0.11438E-02 0.15147E-02 0.91140E-05 0.12057E-03 0.41284E-03
0.88889E-04 0.37445E-03 0.69459E-03 0.18418E-02 0.14841E-02 -0.13718E-03 0.15715E-03 0.46217E-03 0.78150E-03
0.11111E-02 -0.38887E-03 -0.78847E-04 0.22577E-03 0.53499E-03 0.84932E-03

ROW 6 0.24126E-04 0.49431E-04 0.74743E-04 0.18885E-03 0.12546E-03 0.87419E-05 0.19162E-04 0.44586E-04 0.14287E-04
0.39581E-04 0.64881E-04 0.98285E-04 0.11562E-03 -0.12788E-04 0.12557E-04 0.37834E-04 0.63122E-04 0.80519E-04
-0.38688E-04 -0.14428E-04 0.18844E-04 0.36128E-04 0.51584E-04

ROW 7 0.1E-02 0.2E-02 1.32E-03 -0.3E-03 0.417E-03 0.834E-03 0.887E-03 0.17E-03 0.4E-03 0.1E-03

	0.2710E-03	0.3130E-03	0.4063E-03	0.2426E-03	0.475E-03	0.11048E-03	0.20000E-03	0.3100E-03	0.2200E-03
	0.60734E-04	0.15960E-03	0.25069E-03	0.34232E-03					
ROW 8									
	0.40335E-03	0.57455E-03	0.74614E-03	0.89279E-03	0.69813E-04	0.22741E-03	0.64906E-04	0.22170E-03	0.30981E-03
	0.56080E-03	0.23233E-03	0.29710E-04	0.19133E-03	0.35080E-03	0.52345E-03	0.69264E-03	0.64460E-05	0.15/68E-03
	0.39229E-03	0.40791E-03	0.65495E-03						
ROW 9									
	0.83727E-03	0.11019E-02	0.90211E-05	0.95140E-03	0.31961E-03	0.90216E-04	0.31408E-03	0.56110E-03	0.82169E-03
	0.10000E-02	0.00296E-04	0.20544E-03	0.52955E-03	0.70104E-03	0.10371E-02	0.71037E-05	0.25070E-03	0.47594E-03
	0.74349E-03	0.90306E-03							
ROW 10									
	0.14727E-02	0.91147E-03	0.12047E-03	0.41217E-03	0.11564E-03	0.40668E-03	0.73304E-03	0.10064E-02	0.14540E-02
	0.65752E-04	0.30020E-03	0.70040E-03	0.10464E-02	0.13954E-02	0.10297E-04	0.34577E-03	0.67529E-03	0.10000E-02
	0.13473E-02								
ROW 11									
	0.87000E-03	0.07420E-03	0.00149E-05	0.07421E-03	0.88350E-05	0.89201E-05	0.90214E-03	0.91130E-05	0.07420E-05
	0.00359E-05	0.00290E-05	0.00222E-05	0.01150E-05	0.07406E-05	0.00370E-05	0.00302E-05	0.00233E-05	0.01169E-05
ROW 12									
	0.10163E-04	0.44400E-04	0.19164E-04	0.44409E-04	0.09013E-04	0.90143E-04	0.12027E-03	0.10170E-04	0.44409E-04
	0.60000E-04	0.95151E-04	0.12000E-03	0.10179E-04	0.44500E-04	0.09013E-04	0.95100E-04	0.12039E-03	
ROW 13									
	0.13523E-03	0.44512E-04	0.13521E-03	0.27740E-03	0.31964E-03	0.43220E-04	0.44221E-04	0.13564E-03	0.22750E-03
	0.31957E-03	0.41200E-03	0.44073E-04	0.13570E-03	0.27754E-03	0.31951E-03	0.41100E-03		
ROW 14									
	0.24129E-04	0.49438E-04	0.74754E-04	0.10000E-03	0.12500E-03	0.51439E-04	0.76609E-04	0.10192E-03	0.12720E-03
	0.15259E-03	0.70564E-04	0.10301E-03	0.12905E-03	0.15431E-03	0.17967E-03			
ROW 15									
	0.14100E-03	0.23339E-03	0.32567E-03	0.41034E-03	0.79746E-04	0.17235E-03	0.26902E-03	0.39755E-03	0.49040E-03
	0.11110E-03	0.20377E-03	0.29642E-03	0.30908E-03	0.40209E-03				
ROW 16									
	0.40373E-03	0.57506E-03	0.74092E-03	0.10336E-03	0.27050E-03	0.44025E-03	0.61139E-03	0.70334E-03	0.13662E-03
	0.30616E-03	0.47615E-03	0.64674E-03	0.81037E-03					
ROW 17									
	0.03770E-03	0.11024E-02	0.17210E-03	0.36676E-03	0.61041E-03	0.67679E-03	0.11306E-02	0.15324E-03	0.40542E-03
	0.65920E-03	0.91490E-03	0.11734E-02						
ROW 18									
	0.14120E-02	0.13944E-03	0.46107E-03	0.70662E-03	0.11453E-02	0.15024E-02	0.10300E-03	0.50229E-03	0.10235E-03
	0.11061E-02	0.15346E-02							
ROW 19									
	0.37317E-03	0.36295E-03	0.34020E-03	0.34451E-03	0.44408E-03	0.72276E-03	0.67183E-03	0.62916E-03	0.59054E-03
	0.57020E-03								
ROW 20									
	0.45027E-03	0.54107E-03	0.62710E-03	0.70539E-03	0.80340E-03	0.74122E-03	0.83475E-03	0.90660E-03	0.97993E-03
ROW 21									
	0.73315E-03	0.91040E-03	0.10400E-02	0.65399E-03	0.04936E-03	0.10401E-02	0.12223E-02	0.14000E-02	
ROW 22									
	0.12044E-02	0.14007E-02	0.62035E-03	0.93093E-03	0.12361E-02	0.15402E-02	0.10414E-02		
ROW 23									
	0.10176E-02	0.60300E-03	0.10005E-02	0.14240E-02	0.10549E-02	0.22972E-02			

ROW 24	0.16762E-02	0.14871E-02	0.13328E-02	0.12236E-02	0.11308E-02
ROW 25	0.15410E-02	0.15670E-02	0.15941E-02	0.16311E-02	
ROW 26	0.17884E-02	0.19734E-02	0.21474E-02		
ROW 27	0.23496E-02	0.27002E-02			
ROW 28	0.32988E-02				

REDUCED UPPER TRIANGULAR WEIGHT MATRIX

ROW 1	0.50000E-01	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
ROW 2	0.11000E 00	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
ROW 3	0.11582E 00	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
ROW 4	0.12580E 00	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
ROW 5	0.18680E 00	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
ROW 6	0.15500E 00	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
ROW 7	0.30500E 00	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
ROW 8	0.30500E 00	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
ROW 9	0.30500E 00	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.
	0.	0.	0.	0.	0.	0.	0.	0.	0.

[illegible]

HERE ARE THE EIGENVALUES AND EIGENVECTORS

EIGENVECTOR NUMBER 1

CORRESPONDING TO 1.0001270E 05

7.567196E-02 2.736202E-01 4.056802E-01 7.116900E-01 9.443354E-01 8.091636E-02
 2.712741E-01 4.025450E-01 7.850290E-01 9.340480E-01 8.282018E-01 8.172252E-02
 2.731350E-01 8.295070E-02 2.747537E-01 4.050843E-01 7.087406E-01 9.360060E-01
 9.197926E-02 2.991745E-01 5.115418E-01 7.345741E-01 9.299281E-01 1.165092E-01
 3.341726E-01 5.536607E-01 7.755131E-01 1.000000E 00

EIGENVECTOR NUMBER 2

CORRESPONDING TO 4.6656182E 05

-3.074070E-01 -4.760260E-01 -4.092040E-01 -5.107503E-01 -5.465090E-01 -5.159633E-02
 -6.739273E-02 -8.511254E-02 -1.418392E-01 -1.171047E-01 7.928541E-04 -2.170194E-03
 -1.020153E-02 4.744119E-02 4.722479E-02 4.471306E-02 3.747701E-02 2.685693E-02
 4.204392E-01 4.425511E-01 4.626226E-01 4.767681E-01 4.002161E-01 9.129032E-01
 9.335401E-01 9.540349E-01 9.771205E-01 1.000000E 00

EIGENVECTOR NUMBER 3

CORRESPONDING TO 6.5344921E 06

2.146230E-01 2.309371E-01 2.476323E-01 2.591607E-01 2.630717E-01 2.050056E-02
 1.124916E-02 -1.401324E-02 -5.049010E-02 -1.141137E-01 1.000000E-02 1.291442E-02
 1.704045E-03 1.238600E-02 -5.787737E-03 -4.942160E-02 -1.126402E-01 -1.017566E-01
 3.629885E-01 2.080953E-01 4.173977E-02 -1.390864E-01 -3.292207E-01 1.000000E 00
 6.040576E-01 3.592976E-01 4.158011E-02 -2.675010E-01

EIGENVECTOR NUMBER 4

CORRESPONDING TO 8.0003014E 06

3.039769E-01 2.396016E-01 2.091650E-01 1.770175E-01 2.005694E-01 -2.316207E-02
 -7.724971E-02 -1.150248E-01 -1.244100E-01 -1.129740E-01 -2.620105E-02 -4.997575E-02
 -1.043791E-01 -7.701524E-02 -1.305493E-01 -1.504013E-01 -1.569900E-01 -1.411520E-01
 -3.506702E-01 -2.292544E-01 -8.530620E-02 0.091304E-02 2.625990E-01 -4.064891E-01
 -1.322251E-01 2.400270E-01 6.196743E-01 1.000000E 00

EIGENVECTOR NUMBER 5

CORRESPONDING TO 1.063140E 07

1.000000E 00 0.094497E-01 5.401720E-01 -6.271140E-02 -7.742793E-01 1.607876E-01
 2.452103E-01 2.102061E-01 4.746392E-02 -1.022122E-01 0.710327E-02 1.293590E-01
 2.006700E-01 9.370546E-02 1.751053E-01 1.700071E-01 5.193000E-02 -1.391650E-01
 -4.044000E-02 3.133247E-02 7.150250E-02 6.306566E-02 2.000500E-02 -1.546406E-01
 -6.405211E-02 1.550640E-02 7.674061E-02 1.210197E-01

EIGENVECTOR NUMBER 6

CORRESPONDING TO 2.0904734E 07

1.000000E 00 4.005475E-01 -1.000000E-01 -2.906376E-01 -1.000937E-01 -1.754407E-01
 -2.044100E-01 -2.109280E-01 0.469350E-02 5.132007E-01 -1.472700E-01 -2.006714E-01
 -3.130515E-01 -2.410130E-01 -3.378451E-01 -7.303748E-01 1.067306E-01 5.502270E-01
 -7.720451E-02 -1.725412E-01 -1.541236E-01 -5.912036E-03 2.232600E-01 6.077103E-01
 3.259014E-01 -3.053977E-03 -2.432791E-01 -4.100700E-01

EIGENVECTOR NUMBER 7

CORRESPONDING TO 4.010730E 07

1.000000E 00 9.005355E-02 -5.067357E-01 -4.307009E-01 3.095538E-01 1.215220E-01
 0.261014E-02 4.010730E-03 -6.709247E-02 -9.337552E-02 1.100374E-01 1.196949E-01
 1.042004E-01 1.201204E-01 1.169501E-01 6.066293E-02 -1.000000E-02 -7.092406E-02
 1.263077E-01 1.201204E-01 1.044005E-01 6.364270E-02 1.173267E-02 -1.010007E-01
 -1.230157E-01 -5.417200E-02 -1.970024E-02 -5.210110E-03

EIGENVECTOR NUMBER 8

CORRESPONDING TO 8.591000E 07

-3.143002F-02 1.749340E-01 3.070406E-01 2.372204E-01 5.367450E-02 -1.089170E-01
-1.052694E-01 -2.424075E-01 -2.499517E-01 -2.107620E-01 1.920226E-02 -8.693394E-03
-8.206203E-02 0.431237E-02 2.544566E-02 -7.546933E-02 -1.065463E-02 3.348329E-02
1.800000E-00 6.277108E-01 4.540980E-01 5.769463E-01 9.998031E-01 -4.604210E-02
-5.465751E-01 -7.750676E-01 -5.072669E-01 -1.070619E-01

EIGENVECTOR NUMBER 9

CORRESPONDING TO 7.410150E 07

-4.6607439F-02 -5.0956407E-02 -5.007490E-02 -4.559305E-02 -1.419997E-02 9.0869517E-02
9.0839625E-02 6.2602114E-02 4.276700E-02 4.072011E-02 7.775700E-02 7.6825145E-02
5.9377179F-02 5.534615E-02 2.531306E-02 -7.340677E-02 -3.691906E-02 -1.233920E-02
3.197650E-01 -2.642002E-01 -5.334036E-01 -1.260344E-01 2.215110E-01 1.000000E 00
-1.333313E-01 -6.975071E-01 -2.102470E-01 9.007520E-01

HERE ARE THE NATURAL FREQUENCIES

THE NATURAL FREQUENCY NUMBER	1	IS	69.845	CPS
THE NATURAL FREQUENCY NUMBER	2	IS	129.890	CPS
THE NATURAL FREQUENCY NUMBER	3	IS	486.842	CPS
THE NATURAL FREQUENCY NUMBER	4	IS	474.760	CPS
THE NATURAL FREQUENCY NUMBER	5	IS	518.938	CPS
THE NATURAL FREQUENCY NUMBER	6	IS	896.850	CPS
THE NATURAL FREQUENCY NUMBER	7	IS	1807.934	CPS
THE NATURAL FREQUENCY NUMBER	8	IS	1238.934	CPS
THE NATURAL FREQUENCY NUMBER	9	IS	1370.042	CPS

APPENDIX B

Program FLUENC Listing

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S      FORTRAN DECK
CHAIN  PROGRAM FLUENC-FOR GENERATING STIFFNESS,FLEXIBILITY AND MASS
C      MATRICES FROM PLANE GRID BEAM AND TRIANG. PLATE ELEMENTS
      DIMENSION TITLE(20),YH(10),PR(10),GE(10),DENS(10),X(50),Y(50),
1 NR1(50),NR2(50),NR3(50),N1(50),N2(50),N3(50),NOSC(9),DCS(2),
1 STM(6,6),SHM(5,6),PLTK(9,9),PLTM(9,9),SSTF(11325),SM(11325),
1 RSMASS(150),A(11325),VALU(9),TEMP(50),B(150),C(100),DUM3(150),
1 F(150,3),IDUM4(50),JMASS(50)
      INTEGER OUT
      EQUIVALENCE(SSTF(1),SM(1),A(1)),(STM(1,1),SHM(1,1),PLTK(1,1),
1 PLTM(1,1))
5001 FORMAT(12A6)
5002 FORMAT(16I5)
5003 FORMAT(8E10,3)
5004 FORMAT(10X,2E10,3)
5005 FORMAT(3E10,3,3I5)
5006 FORMAT(E10,3,3I5)
5007 FORMAT(15,5X,E10,3)
5008 FORMAT(1H1,12A6/1X,12A6)
5009 FORMAT(///6HNJTS =1,5X,6H NR =13,5X,6H NRE =13,5X,6H NPE =13,5X,
1 7HNMODE =13,5X,6H HKEY =13,5X,6H NLUMP =13,5X,6H)
5010 FORMAT(///75H MATERIAL PROPERTIES *****
1 *****//3HNO. YOUNG'S MODULUS POISSON RATIO
1 MODULUS OF RIGIDITY DENSITY,10(/12,6X,E12,5,9X,17,5,10X,E12,6,
1 16X,E12,5))
5011 FORMAT(///34HJOINT COORDINATES/35HJOINT NO. X
1 COORD. Y COORD.)
5012 FORMAT(15,7X,E10,5,5X,E10,5)
5013 FORMAT(///64HJOINT RESTRAINT CODE *****
1 *****//67HJOINT NO. Z DISPLACEMENT ROTATION ABOUT X
1 ROTATION ABOUT Y)
5014 FORMAT(15,11X,119,120)
5015 FORMAT(///75HELEMENT PROPERTIES *****
1 *****//75HELEMENT NO. A I
1 J MAT JOINT 1 JOINT 2)
5016 FORMAT(16,8X,F0,4,4X,F0,4,4X,F0,4,2X,12,6X,12,9X,12)
5017 FORMAT(///122HTRIANGULAR PLATE ELEMENT
1 PROPERTIES *****
1 *****//122HELEMENT NO. T MAT JOINT 1 JOINT 2 JOINT
1 3 DX DY D1 DXY DETA)
5018 FORMAT(16,8,FR,4,3X,12,6X,12,9X,12,8X,12,6X,E11,5,3X,E11,5,3X,
1 E11,5,3X,E11,5,3X,E6,2)
5019 FORMAT(///60HCOORDINATE NUMBERS FOR EACH Z DISPLACEMENT AT EACH UN
1 RESTRAINED JOINT//5HJOINT NO. COORD. NO.)
5020 FORMAT(15,11X)
5021 FORMAT(///24HUNWEIGHTS/25HJOINT NO. WGT
1 HT)
5022 FORMAT(15,6,FR,10,4)
5023 FORMAT(15,6,FR,10,4)
C      DISC ASSIGNMENTS
      IN=6
      CALL FLGEOF(IN,IV)
      OUT=6

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MDISC=7
NDISC=8
IDISC=9
JDISC=10
KDISC=11
C   BEGIN INPUT OF DATA
100 READ(IN,1000) (TITLE(I),I=1,24)
    IF(IV.NE.0) CALL EXIT
    REWIND MDISC
    REWIND NDISC
    REWIND IDISC
    REWIND JDISC
    REWIND KDISC
    WRITE(OUT,0000) (TITLE(I),I=1,24)
    READ(IN,1001) NJTS,NR,NBE,NPE,NMODE,MKEY,NLUMP
C   NJTS=NO. OF JOINTS, NR=NO. OF JOINTS WITH RESTRAINTS
C   NBE=NO. OF BEAM ELEMENTS, NPE=NO. OF TRIANGULAR PLATE ELEMENTS
C   NMODE=NO. OF EIGENVALUES AND EIGENVECTORS DESIRED
C   MKEY = 1 DO NOT COMPUTE ELEMENTAL CONSISTENT MASS TERMS
C   MKEY = 2 COMPUTE ELEMENTAL CONSISTENT MASS TERMS
C   NLUMP = NO. OF LUMPED MASSES INPUT
    WRITE(OUT,0001) NJTS,NR,NBE,NPE,NMODE,MKEY,NLUMP
C   INPUT MATERIAL PROPERTIES
    READ(IN,1001) NMAT
    DO 10 I=1,NMAT
        READ(IN,1002) YM(I),PR(I),GE(I),DENS(I)
C   YM=YOUNG'S MOD./10**6, PR=POISSON RATIO, GE=MOD. OF RIGIDITY
C   DENS=DENSITY
        IF(GE(I).EQ.0.) GE(I)=YM(I)/(2.*(1.+PR(I)))
        YM(I)=YM(I)*1.E6
    10 GE(I)=GE(I)*1.E6
    WRITE(OUT,0002) (I,YM(I),PR(I),GE(I),DENS(I),I=1,NMAT)
    DO 200 I=1,NMAT
200 DENS(I)=DENS(I)/(32.174*12.)
C   INPUT JOINT COORDINATES
    READ(IN,1003) (X(M),Y(M),M=1,NJTS)
    WRITE(OUT,0003)
    WRITE(OUT,0004) (M,X(M),Y(M),M=1,NJTS)
C   INPUT JOINT RESTRAINT CODE
C   0=FREE
C   1=CLAMPED
    DO 12 I=1,NJTS
        NR1(I)=0
        NR2(I)=0
        NR3(I)=0
        N1(I)=0
        N2(I)=0
    12 N3(I)=0
        IF(NR.EQ.0) GO TO 80
        WRITE(OUT,0006)
        DO 11 I=1,NR
            READ(IN,1001) JT,M1,M2,M3

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      NR1(JT)=M1
      NR2(JT)=M2
      NR3(JT)=M3
      WRITE(OUT,1007) JT,M1,M2,M3
11  CONTINUE
80  CONTINUE
C   GENERATE COORDINATE NUMBERS FOR EACH DEGREE OF FREEDOM, " IF
C   CLAMPED, NORMAL DISPLACEMENTS ARE NUMBERED FIRST
C   N1, N2, N3 CONTAIN COORD. NUMBERS FOR EACH JOINT
C   NREDU = NO. OF NORMAL DISPLACEMENTS
C   NDF = NO. OF DEGREES OF FREEDOM INCLUDING ROTATIONS
      CALL COORDN(NR1,NR2,NR3,N1,N2,N3,NJIS,NREDU,NDF)
      WRITE(OUT,1020)
      DO 50 I=1,NJTS
      IF(NR1(I).EQ.1) GO TO 50
      WRITE(OUT,1021) I,N1(I)
50  CONTINUE
C   INPUT LUMPED MASSES
      IF(NLUMP.EQ.0) GO TO 250
      READ(IN,1006) ((JMASS(I),RSMASS(I)),I=1,NLUMP)
      WRITE(OUT,1022)
      DO 251 I=1,NLUMP
      WRITE(OUT,1023) JMASS(I),RSMASS(I)
      RSMASS(I)=RSMASS(I)/(32.174*12.)
251  CONTINUE
250  CONTINUE
      NSSIF=NDF*(NDF+1)/2
      DO 13 I=1,NSSIF
13  SSTF(I)=0.
      IF(NBE.EQ.1) GO TO 200
C   BEGIN TO GENERATE BEAM STIFFNESS TERMS
      WRITE(OUT,1008)
      DO 14 NM=1,NBE
C   INPUT BEAM ELEMENT PROPERTIES
      READ(IN,1004) AR,XI,YJ,MAT,JTNR,JTFR
C   AR=AREA OF BEAM CROSS SECTION, XI=AREA MOMENT OF INERTIA,
C   YJ=EFFECTIVE TORSIONAL MOMENT OF INERTIA, MAT=MATERIAL CODE
C   JTNR,JTFR=JOINT NUMBERS AT ENDS
      WRITE(OUT,1009) NM,AR,XI,YJ,MAT,JTNR,JTFR
C   SET UP CODE NUMBERS
      NOSC(1)=N1(JTNR)
      NOSC(2)=N2(JTNR)
      NOSC(3)=N3(JTNR)
      NOSC(4)=N1(JTFR)
      NOSC(5)=N2(JTFR)
      NOSC(6)=N3(JTFR)
      IF(MKEY.EQ.1) GO TO 253
C   STORE INFO. FOR LATER USE
      WRITE(IDISC) AR,XI,YJ,MAT,JTNR,JTFR,(NOSC(I),I=1,6)
253  CONTINUE
      X1=X(JTNR)
      X2=X(JTFR)
      Y1=Y(JTNR)

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Y2=Y(JTFR)
FLNTH=SQRT((X2-X1)**2+(Y2-Y1)**2)
CALL TRANS(X1,X2,Y1,Y2,FLNTH,DCS)
E=YH(MAT)
G=GE(MAT)
CALL HFAMK(FLNTH,E,G,X1,YJ,STM,DCS)
DO 15 K=1,N
IF(NOSC(K).EQ.0) GO TO 15
I=NOSC(K)
DO 16 N=1,N
IF(NOSC(N).EQ.0) GO TO 16
J=NOSC(N)
IF(J.LT.I) GO TO 16
MM=(2*I+(J-1)*(2*NDF-1))/2
SSTF(MM)=SSTF(MM)+STM(K,N)
16 CONTINUE
15 CONTINUE
14 CONTINUE
200 CONTINUE
IF(NRE.EQ.1) GO TO 300
C BEGIN TO GENERATE TRIANGULAR PLATE STIFFNESS TERMS
WRITE(OUT,1010)
DO 17 NM=1,NPE
C INPUT TRIANGULAR PLATE ELEMENT PROPERTIES
READ(IN,1005) PTH,MAT,JT1,JT2,JT3,NDX
C PTH=PLATE THICKNESS, MAT=MATERIAL CODE,
C JT1,JT2,JT3=JOINT NUMBERS AT CORNERS, ANGLE AT JT1 MUST NOT BE
C 90 DEGREES
C DX,DY,DI,DXY,BETA - FLEXURAL RIGIDITY TERMS AND ANGLE OF MATERIAL
C PRINCIPAL AXES W/ TRIANGLE LOCAL AXES
IF(NDX.EQ.1) READ(IN,1002) DX,DY,DI,DXY,BETA
IF(NDX.EQ.1) GO TO 18
BETA=0.
DX=(YH(MAT)*PTH**3)/(12.*(1.-PR(MAT)**2))
DY=DX
DI=PR(MAT)*DX
DXY=((1.-PR(MAT))/2.)*DX
18 BETA=BETA/17.2258
WRITE(OUT,1011) NM,PTH,MAT,JT1,JT2,JT3,DX,DY,DI,DXY,BETA
C SET UP CODE NUMBERS
NOSC(1)=N1(JT1)
NOSC(2)=N2(JT1)
NOSC(3)=N3(JT1)
NOSC(4)=N1(JT2)
NOSC(5)=N2(JT2)
NOSC(6)=N3(JT2)
NOSC(7)=N1(JT3)
NOSC(8)=N2(JT3)
NOSC(9)=N3(JT3)
IF(MKEY.EQ.1) GO TO 200
C STORE INFO. FOR LATER USE
WRITE(IDISC) PTH,MAT,JT1,JT2,JT3,(NOSC(I),I=1,9)

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```

224 CONTINUE
  RX1=X(JT1)
  RX2=X(JT2)
  RY1=Y(JT1)
  RY2=Y(JT2)
  Y2=SQRT((BX2-RX1)**2+(BY2-RY1)**2)
  CALL TRANS(RX1,RX2,BY1,BY2,Y2,DCS)
  X3=DCS(2)*(X(JT3)-RX1)-DCS(1)*(Y(JT3)-RY1)
  Y3=DCS(1)*(X(JT3)-RX1)+DCS(2)*(Y(JT3)-RY1)
  CALL PLATEK(Y2,X3,Y3,DX,DY,DI,DXY,HETA,DCS,PLTK)
  DO 19 K=1,1
  IF(NOSC(K).EQ.0) GO TO 19
  I=NOSC(K)
  DO 20 N=1,4
  IF(NOSC(N).EQ.0) GO TO 20
  J=NOSC(N)
  IF(J.LT.1) GO TO 20
  MM=(2*J+(1-1)*(2*NDF-1))/2
  SSTF(MM)=SSTF(MM)+PLTK(K,N)
20 CONTINUE
19 CONTINUE
17 CONTINUE
310 CONTINUE
C   STORE FOR REDUCTION
  DO 21 I=1,NDF
  NS=(2*I+(1-1)*(2*NDF-1))/2
  NE=(2*NDF+(1-1)*(2*NDF-1))/2
  21 WRITE(IDISC) (SSTF(J),J=NS,NE)
  REWIND IDISC
  DO 22 I=1,NSSTF
  22 SM(I)=0.
  IF(MKEY.EQ.1) GO TO 25F
  IF(NBE.EQ.0) GO TO 201
C   GENERATE BEAM MASS MATRICES
  DO 23 NM=1,NBE
  READ(IDISC) AR,X1,YJ,MAT,JTNR,JTFR,(NOSC(I),I=1,6)
  X1=X(JTNR)
  X2=X(JTFR)
  Y1=Y(JTNR)
  Y2=Y(JTFR)
  FLNTH=SQRT((X2-X1)**2+(Y2-Y1)**2)
  CALL TRANS(X1,X2,Y1,Y2,FLNTH,DCS)
  RHO=DENS(MAT)
  CALL BEAMH(FLNTH,RHO,AR,X1,YJ,SMM,DCS)
  DO 24 K=1,1
  IF(NOSC(K).EQ.0) GO TO 24
  I=NOSC(K)
  DO 25 N=1,4
  IF(NOSC(N).EQ.0) GO TO 25
  J=NOSC(N)
  IF(J.LT.1) GO TO 25
  MM=(2*J+(1-1)*(2*NDF-1))/2
  SM(MM)=SM(MM)+SMM(K,N)

```

```

25 CONTINUE
24 CONTINUE
23 CONTINUE
201 CONTINUE
    IF(NPE.EQ.1) GO TO 301
C   GENERATE TRIANGULAR PLATE MASS MATRICES
    DO 26 NM=1,NPE
        READ(IDISC) PTH,MAT,JT1,JT2,JT3,(NOSC(I),I=1,9)
        RX1=X(JT1)
        RX2=X(JT2)
        RY1=Y(JT1)
        RY2=Y(JT2)
        Y2=SQRT((BX2-BX1)**2+(RY2-RY1)**2)
        CALL TRANS(BX1,BX2,RY1,RY2,Y2,DCS)
        X3=DCS(2)*(X(JT3)-BX1)-DCS(1)*(Y(JT3)-RY1)
        Y3=DCS(1)*(X(JT3)-BX1)+DCS(2)*(Y(JT3)-RY1)
        PRHO=DENS(MAT)
        CALL PLATEM(Y2,X3,Y3,PRHO,PTH,DCS,PLTH)
        DO 27 K=1,9
            IF(NOSC(K).EQ.0) GO TO 27
            I=NOSC(K)
            DO 28 N=1,9
                IF(NOSC(N).EQ.0) GO TO 28
                J=NOSC(N)
                IF(J.LT.I) GO TO 28
                NM=(2*J+(I-1)*(2*NDF-1))/2
                SM(NM)=SM(NM)+PLTH(K,N)
28          CONTINUE
27          CONTINUE
26          CONTINUE
301 CONTINUE
C   STORE FOR REDUCTION
225 CONTINUE
    DO 250 I=1,NLUMP
        NN=JMASS(I)
        IF(N1(NN).EQ.0) GO TO 258
        NNN=N1(NN)
        NS=(2*NNN+(NNN-1)*(2*NDF-1))/2
        SM(NS)=SM(NS)+RMASS(NNN)
258 CONTINUE
    DO 29 I=1,NDF
        NS=(2*I+(I-1)*(2*NDF-1))/2
        NF=(2*NDF+(I-1)*(2*NDF-1))/2
29 WRITE(NDISC) (SM(J),J=NS,NF)
    NOMASS=NDF-NREDU
    CALL FIGEN(A,VALU,TEMP,R,C,DUM,F,1DUM4,1DISC,JDISC,KDISC,NDISC,
    1MDISC,NDF,NMODF,NMODE,NREDU,NOMASS)
    GO TO 100
END

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*      FORTRAN DECK
CCOORDN      ASSIGNS A COORD. NO. TO EACH DEGREE OF FREEDOM AT EACH JOINT
C      NR1,NR2,NR3 = ARRAYS CONTAINING RESTRAINT INFO. FOR EACH DEGREE
C      OF FREEDOM AT EACH JOINT (FREE=0, CLAMPED=1)
C      N1,N2,N3 = COORD. NO. FOR EACH DEGREE OF FREEDOM (NORMAL
C      DISPLACEMENTS ARE NUMBERED FIRST)
C      NJTS = NO. OF JOINTS
C      NREDOU = NO. OF NORMAL DISPLACEMENTS
C      NDF = TOTAL NO. OF DEGREES OF FREEDOM (INCLUDING ROTATIONS)
SUBROUTINE COORDN(NR1,NR2,NR3,N1,N2,N3,NJTS,NREDOU,NDF)
DIMENSION NR1(50),NR2(50),NR3(50),N1(50),N2(50),N3(50)
NO=1
DO 10 I=1,NJTS
  IF(NR1(I).EQ.1) GO TO 10
  N1(I)=NO
  NO=NO+1
10 CONTINUE
  NREDOU=NREDOU+1
  DO 20 I=1,NJTS
    IF(NR2(I).EQ.1) GO TO 21
    N2(I)=NO
    NO=NO+1
  21 IF(NR3(I).EQ.1) GO TO 20
    N3(I)=NO
    NO=NO+1
  20 CONTINUE
  NDF=NDF+1
  RETURN
END

```

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1      FORTRAN DECK
CTRANS      TRANSFORMATION DIRECTION COSINES
C      X1,Y1 = COORDS. OF POINT 1
C      X2,Y2 = COORDS. OF POINT 2
C      FL = DISTANCE BETWEEN POINTS 1 AND 2
C      DCS = DIRECTION COSINES OF VECTOR FROM POINT 1 TO POINT 2
      SUBROUTINE TRANS(X1,X2,Y1,Y2,FL,DCS)
      DIMENSION DCS(2)
      DCS(1)=(X2-X1)/FL
      DCS(2)=(Y2-Y1)/FL
      RETURN
      END

```

```

S      FORTRAN DECK
CHEAMK      PLANE GRID BEAM ELEMENT STIFFNESS MATRIX IN SYSTEM COORDS.
C      FL = BEAM LENGTH
C      E = YOUNG'S MODULUS
C      G = MODULUS OF RIGIDITY
C      XI = AREA MOMENT OF INERTIA
C      YJ = EFFECTIVE TORSIONAL MOMENT OF INERTIA
C      STM = STIFFNESS MATRIX
C      DCS = DIRECTION COSINES
C      SUBROUTINE BEAMK(FL,E,G,XI,YJ,STM,DCS)
C      DIMENSION STM(6,6),DCS(2)
C      Z1=E*XI/FL
C      Z2=G*YJ/FL
C      STM(1,1)=12.*Z1/(FL*FL)
C      STM(2,1)=6.*Z1*DCS(2)/FL
C      STM(2,2)=4.*Z1*DCS(2)*DCS(2)+Z2*DCS(1)*DCS(1)
C      STM(3,1)=-6.*Z1*DCS(1)/FL
C      STM(3,2)=(-4.*Z1+Z2)*DCS(1)*DCS(2)
C      STM(3,3)=4.*Z1*DCS(1)*DCS(1)+Z2*DCS(2)*DCS(2)
C      STM(4,1)=-STM(1,1)
C      STM(4,2)=-STM(2,1)
C      STM(4,3)=-STM(3,1)
C      STM(4,4)=STM(1,1)
C      STM(5,1)=STM(2,1)
C      STM(5,2)=2.*Z1*DCS(2)*DCS(2)-Z2*DCS(1)*DCS(1)
C      STM(5,3)=-Z2*Z1+Z2)*DCS(1)*DCS(2)
C      STM(5,4)=-STM(2,1)
C      STM(5,5)=STM(2,2)
C      STM(6,1)=STM(3,1)
C      STM(6,2)=STM(3,3)
C      STM(6,3)=2.*Z1*DCS(1)*DCS(1)-Z2*DCS(2)*DCS(2)
C      STM(6,4)=-STM(3,1)
C      STM(6,5)=STM(3,2)
C      STM(6,6)=STM(3,3)
C      DO 10 I=2,6
C      N=I-1
C      DO 10 J=1,N
C      STM(J,I)=STM(I,J)
C      RETURN
C      END

```

```

S      FORTRAN DECK
CBEFAMH      PLANE GRID BEAM ELEMENT MASS MATRIX IN SYSTEM COORDS.
C      FL = BEAM LENGTH
C      RHO = DENSITY
C      A = CROSS SECTIONAL AREA
C      XI = AREA MOMENT OF INERTIA
C      XJ = EFFECTIVE TORSIONAL MOMENT OF INERTIA
C      SMM = MASS MATRIX
C      DCS = DIRECTION COSINES
SUBROUTINE BEFAMH(FL,RHO,A,XI,YJ,SMM,DCS)
DIMENSION SMM(6,6),DCS(2)
Z1=RHO*A*FL
Z2=FL**2
Z3=XI/A
DD=Z1*(13./30.+(6.*Z3)/(5.*Z2))
CC=Z1*(11.*FL/10.+Z3/(10.*FL))
AA=Z1*(Z2/30.+2.*Z3/15.)
T1=Z1*YJ/(5.*A)
RR=Z1*(9./10.-(6.*Z3)/(5.*Z2))
QQ=Z1*(13.*FL/120.-Z3/(10.*FL))
SS=-Z1*(Z2/120.+Z3/30.)
PP=Z1*YJ/(5.*A)
SMM(1,1)=DD
SMM(2,1)=CC*DCS(2)
SMM(2,2)=AA*DCS(2)*DCS(2)+T1*DCS(1)*DCS(1)
SMM(3,1)=-CC*DCS(1)
SMM(3,2)=(-AA+T1)*DCS(1)*DCS(2)
SMM(3,3)=AA*DCS(1)*DCS(1)+T1*DCS(2)*DCS(2)
SMM(4,1)=RR
SMM(4,2)=QQ*DCS(2)
SMM(4,3)=-QQ*DCS(1)
SMM(4,4)=SMM(1,1)
SMM(5,1)=-SMM(4,2)
SMM(5,2)=SS*DCS(2)*DCS(2)+PP*DCS(1)*DCS(1)
SMM(5,3)=(-SS+PP)*DCS(1)*DCS(2)
SMM(5,4)=-SMM(2,1)
SMM(5,5)=SMM(2,2)
SMM(6,1)=-SMM(4,3)
SMM(6,2)=SMM(5,3)
SMM(6,3)=SS*DCS(1)*DCS(1)+PP*DCS(2)*DCS(2)
SMM(6,4)=-SMM(5,1)
SMM(6,5)=SMM(3,2)
SMM(6,6)=SMM(3,3)
DO 10 I=2,6
N=I-1
DO 10 J=1,N
10 SMM(J,I)=SMM(I,J)
RETURN
END

```

* FORTRAN DECK

CPLATEK

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C     THIS SUBROUTINE DETERMINES THE STIFFNESS MATRIX OF A
C     TRIANGLE PLATE ELEMENT IN SYSTEM COORDS.
C     Y2,X3,Y3 = COORDS. OF PLATE CORNERS IN LOCAL COORDINATES
C     DX,DY,D1,DOXY,RETA = FLEXURAL RIGIDITY TERMS AND ANGLE OF MATERIAL
C     PRINCIPAL AXES W/O TRIANGLE LOCAL AXES
C     DCS = DIRECTION COSINES
C     PLTK = STIFFNESS MATRIX
C     SUBROUTINE PLATEK(Y2,X3,Y3,DX,DY,D1,DOXY,RETA,DCS,PLTK)
C     DIMENSION PLTK(9,9),C(9,9),CINV(9,9),P(9,9),R(9,9)
C     DIMENSION T(9,9),STIFF(9,9),DCS(2)
C     EQUIVALENCE(P(1,1),STIFF(1,1)),                     (R(1,1),T(1,1))
C     CALL CHAT(Y2,X3,Y3,C)
C     CALL MINV(C,CINV,9)
C     CALL DINMAT(Y2,X3,Y3,DX,DY,D1,DOXY,RETA,P)
C     CALL MATMPY(P,CINV,R,9)
C     DO 10 I=2,9
C     N=I-1
C     DO 10 J=1,N
C     ZZ1=CINV(1,J)
C     ZZ2=CINV(J,1)
C     CINV(1,J)=ZZ2
C     CINV(J,1)=ZZ1
C 10   CONTINUE
C     CALL MATMPY(CINV,R,STIFF,9)
C     DO 400 I=1,9
C     DO 400 J=1,9
C 400   T(I,J)=0.
C     T(1,1)=1.
C     T(4,4)=1.
C     T(7,7)=1.
C     T(2,2)=DCS(2)
C     T(3,3)=DCS(2)
C     T(5,5)=DCS(2)
C     T(6,6)=DCS(2)
C     T(8,8)=DCS(2)
C     T(9,9)=DCS(2)
C     T(2,3)=-DCS(1)
C     T(5,6)=-DCS(1)
C     T(8,9)=-DCS(1)
C     T(3,2)=DCS(1)
C     T(6,5)=DCS(1)
C     T(9,8)=DCS(1)
C     CALL MATMPY(STIFF,T,C,9)
C     T(2,3)=DCS(1)
C     T(5,6)=DCS(1)
C     T(8,9)=DCS(1)
C     T(3,2)=-DCS(1)
C     T(6,5)=-DCS(1)
C     T(9,8)=-DCS(1)
C     CALL MATMPY(T,C,PLTK,9)
C     RETURN

```

```

1      FORTRAN DECK
CCHAT
C      THIS SUBROUTINE FORMS THE C MATRIX RELATING THE CORNER
C      DISPLACEMENTS TO THE POLYNOMIAL DEFLECTION COEFFICIENTS
C      FOR THE TRIANGULAR PLATE ELEMENT
C      Y2,X3,Y3 = COORDS. OF PLATE CORNERS IN LOCAL COORDINATES
C      C = C MATRIX
C      SUBROUTINE CMAT(Y2,X3,Y3,C)
C      DIMENSION C(9,9)
C      DO 10 I=1,9
C      DO 10 J=1,9
10    C(I,J)=0.
C      C(1,1)=1.
C      C(2,3)=1.
C      C(3,2)=-1.
C      C(4,1)=1.
C      C(4,3)=Y2
C      C(4,6)=Y2**2
C      C(4,9)=Y2**3
C      C(5,3)=1.
C      C(5,6)=2.*Y2
C      C(5,9)=3.*Y2**2
C      C(6,2)=-1.
C      C(6,5)=-Y2
C      C(6,8)=-Y2**2
C      C(7,1)=1.
C      C(7,2)=X3
C      C(7,3)=Y3
C      C(7,4)=X3**2
C      C(7,5)=X3*Y3
C      C(7,6)=Y3**2
C      C(7,7)=X3**3
C      C(7,8)=X3*Y3**2+Y3*X3**2
C      C(7,9)=Y3**3
C      C(8,3)=1.
C      C(8,5)=X3
C      C(8,6)=2.*Y3
C      C(8,8)=2.*X3*Y3+X3**2
C      C(8,9)=3.*Y3**2
C      C(9,2)=-1.
C      C(9,4)=-2.*X3
C      C(9,5)=-Y3
C      C(9,7)=-3.*X3**2
C      C(9,8)=-(Y3**2+2.*X3*Y3)
C      RETURN
C      END

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$      FORTRAN DECK
CMINV      MATRIX INVERSION SUBROUTINE
C      A = MATRIX TO BE INVERTED
C      U = INVERTED MATRIX
C      NM = ORDER OF MATRIX (.LE.9)
C      SUBROUTINE MINV(A,U,NM)
C      DIMENSION A(9,9),U(9,9)
C      DO 9001 I=1,NM
C      DO 9001 J=1,NM
C      U(I,J)=0.0
C      IF (I.EQ.J) U(I,J)=1.0
9001 CONTINUE
C      EPS=0.00000001
C      DO 9015 I=1,NM
C      K=1
C      IF (I-NM) 9021,9007,9021
9021 IF (A(I,I)-EPS) 9005,9006,9007
9005 IF (-A(I,I)-EPS) 9006,9006,9007
9006 K=K+1
C      DO 9023 J=1,NM
C      U(I,J)=U(I,J)+U(K,J)
9023 A(I,J)=A(I,J)+A(K,J)
C      GO TO 9021
9007 DIV=A(I,I)
C      DO 9009 J=1,NM
C      U(I,J)=U(I,J)/DIV
9009 A(I,J)=A(I,J)/DIV
C      DO 9015 MM=1,NM
C      DELT=A(MM,I)
C      IF (ABS(DELT)-EPS) 9015,9015,9016
9016 IF (MM-I) 9010,9015,9010
9010 DO 9011 J=1,NM
C      U(MM,J)=U(MM,J)-U(I,J)*DELT
9011 A(MM,J)=A(MM,J)-A(I,J)*DELT
9015 CONTINUE
C      DO 9033 I=1,NM
C      DO 9033 J=1,NM
9033 A(I,J)=U(I,J)
C      RETURN
C      END

```

```

*      FORTRAN DECK
CDINMAT
C      THIS SUBROUTINE DETERMINES THE DOUBLE INTEGRAL MATRIX FOR
C      THE K EQUATION FOR THE TRIANGULAR PLATE ELEMENT
C      Y2,X3,Y3 = COORDS. OF PLATE CORNERS IN LOCAL COORDINATES
C      DX,DY,D1,DXY,BETA = FLEXURAL RIGIDITY TERMS AND ANGLE OF MATERIAL
C      PRINCIPAL AXES W/O TRIANGLE LOCAL AXES
C      P = DOUBLE INTEGRAL MATRIX
C      SUBROUTINE DINMAT(Y2,X3,Y3,DX,DY,D1,DXY,BETA,P)
C      DIMENSION P(9,9),D(3,3)
C      DO 10 I=1,9
C      DO 10 J=1,9
10  P(I,J)=0.
C      CALL DMAT(DX,DY,D1,DXY,BETA,D)
C      A1=DBLINT(Y2,X3,Y3,0,0)
C      A2=DBLINT(Y2,X3,Y3,1,0)
C      A3=DBLINT(Y2,X3,Y3,2,0)
C      A4=DBLINT(Y2,X3,Y3,0,1)
C      A5=DBLINT(Y2,X3,Y3,0,2)
C      A6=DBLINT(Y2,X3,Y3,1,1)
C      P(4,4)=4.*D(1,1)*A1
C      P(4,5)= 4.*D(1,3)*A1
C      P(4,6)=4.*D(1,2)*A1
C      P(4,7)=12.*D(1,1)*A2
C      P(4,8)=4.*(D(1,1)*A4+D(1,2)*A2+2.*D(1,3)*(A2+A4))
C      P(4,9)=12.*D(1,2)*A4
C      P(5,5)=4.*D(3,3)*A1
C      P(5,6)= 4.*D(3,2)*A1
C      P(5,7)= 12.*D(3,1)*A2
C      P(5,8)= 4.*(D(3,1)*A4+D(3,2)*A2+2.*D(3,3)*(A2+A4))
C      P(5,9)= 12.*D(3,2)*A4
C      P(6,6)=4.*D(2,2)*A1
C      P(6,7)=12.*D(2,1)*A2
C      P(6,8)=4.*(D(2,1)*A4+D(2,2)*A2+2.*D(2,3)*(A2+A4))
C      P(6,9)=12.*D(2,2)*A4
C      P(7,7)=36.*D(1,1)*A3
C      P(7,8)=12.*(D(1,1)*A6+D(1,2)*A3+2.*D(1,3)*(A3+A6))
C      P(7,9)=36.*D(1,2)*A6
C      P(8,8)=4.*(D(1,1)*A5+D(1,2)*A6+2.*D(1,3)*(A6+A5))
1      +4.*(D(2,1)*A6+D(2,2)*A3+2.*D(2,3)*(A3+A6))
1      +8.*(D(3,1)*A6+D(3,2)*A3+2.*D(3,3)*(A3+A6))
1      +8.*(D(3,1)*A5+D(3,2)*A6+2.*D(3,3)*(A6+A5))
C      P(8,9)=12.*(D(1,2)*A5+D(2,2)*A6+2.*D(3,2)*(A6+A5))
C      P(9,9)=36.*D(2,2)*A5
C      DO 20 I=1,9
C      N=I+1
C      DO 20 J=N,9
20  P(J,I)=P(I,J)
C      RETURN
C      END

```

1 FORTRAN DECK

CHAI MPY

C MULTIPLIES MATRICES A AND B TO GET C, ALL OF ORDER N*N

 SUBROUTINE MATMPY(A,B,C,N)

 DIMENSION A(9,9),B(9,9),C(9,9)

 DO 10 I=1,N

 DO 10 J=1,N

 C(I,J)=0.

 DO 10 K=1,N

10 C(I,J)=C(I,J)+A(I,K)*B(K,J)

 RETURN

 END

* FORTRAN DECK

CDRLINT

```

C        THIS SUBROUTINE EVALUATES THE DOUBLE INTEGRALS APPEARING IN THE
C        EQUATIONS FOR K AND M FOR THE TRIANGULAR PLATE ELEMENT
C        Y2,X3,Y3 = COORDS. OF PLATE CORNERS IN LOCAL COORDINATES
C        M,N = POWER OF X AND Y RESPECTIVELY, PRZEMIENIECKI, PAGE 305
C        FUNCTION DRLINT(Y2,X3,Y3,M,N)
C        DIMENSION A1(2),B1(2),P1(2),P2(2),P3(2)
C        EQUIVALENCE(R1(1),P3(1))
C        IF(M-1) 40,41,42
40       P1(1)=1.0
C        N1=0
C        GO TO 43
41       P1(1)=-1.0
C        P1(2)=1.0
C        N1=1
C        GO TO 43
42       CONTINUE
C        A1(1)=-1.0
C        A1(2)=1.0
C        B1(1)=-1.0
C        B1(2)=1.0
C        M1=1
C        MM=M-1
C        DO 10 J=1,MM
C        CALL PLYMP(A1,1,B1,M1,P1,N1)
C        NN1=N1+1
C        DO 10 I=1,NN1
C        R1(I)=P1(I)
C        M1=N1
10       CONTINUE
43       CONTINUE
C        IF(N-1) 50,51,52
50       P2(1)=1.0
C        N2=0
C        GO TO 53
51       P2(1)=-Y3+Y2
C        P2(2)=Y3
C        N2=1
C        GO TO 53
52       CONTINUE
C        A1(1)=-Y3+Y2
C        A1(2)=Y3
C        B1(1)=-Y3+Y2
C        B1(2)=Y3
C        M1=1
C        NN=N-1
C        DO 20 J=1,NN
C        CALL PLYMP(A1,1,B1,M1,P2,N2)
C        NN2=N2+1
C        DO 20 I=1,NN2
C        R1(I)=P2(I)

```

```

      M1=N2
20  CONTINUE
23  CONTINUE
      CALL PLYMP(P1,N1,P2,N2,P3,N3)
      NN3=N3+1
      SOL=0.
      DO 30 I=1,NN3
      SOL=SOL+(X1***(M+1))*Y2*(1./FLOAT(M+N+2))* P3(I)*(1./FLOAT(N3+2-1))
30  CONTINUE
      INT=SOL
      RETURN
      END

```

```

1      FORTRAN DECK
CPLYMP      1775
C      POLYNOMIAL MULTIPLY
SUBROUTINE PLYMP(A,L,B,M,C,N)
C      C1-430L      9-1-64
      DIMENSION A(1),B(1),C(1)
      N = L + M
      L1 = N + 1
      DO 1 I = 1,L1
1      C(I) = 0
      L2 = L + 1
      M2 = M + 1
      DO 1 I = 1,L2
      DO 1 J = 1,M2
      K = I+J
1      C(K-1) = C(K-1) + A(I)*B(J)
      DO 2 K = 1,L1
      I1 = K
2      IF(C(K)) 3,2,3
3      CONTINUE
4      IF(I1 - 1) 5,5,6
6      N = L1 - I1
      M2 = N + 1
      DO 7 J = 1,M2
      N1 = J + I1 - 1
7      C(J) = C(N1)
5      RETURN
      END

```

```

      FORTRAN DICK
CPLATEM
C      THIS SUBROUTINE DETERMINES THE MASS MATRIX OF A
C      TRIANGLE PLATE ELEMENT IN SYSTEM COORDS.
C      Y2,X3,Y3 = COORDS. OF PLATE CORNERS IN LOCAL COORDINATES
C      PRHO = DENSITY
C      PTH = PLATE THICKNESS
C      DCS = DIRECTION COSINES
C      PLTH = MASS MATRIX
      SUBROUTINE PLATEM(Y2,X3,Y3,PRHO,PTH,DCS,PLTH)
      DIMENSION PLTH(9,9),C(9,9),CINV(9,9),P(9,9),R(9,9)
      DIMENSION T(9,9),FMASS(9,9),DCS(2)
      EQUIVALENCE(P(1,1),FMASS(1,1)), (R(1,1),T(1,1))
      CALL CMAT(Y2,X3,Y3,C)
      CALL MINV(C,CINV,9)
      CALL DINMTH(Y2,X3,Y3,PRHO,PTH,P)
      CALL MATMPY(P,CINV,R,9)
      DO 10 I=2,9
      N=I-1
      DO 10 J=1,N
      Z1=CINV(1,J)
      Z2=CINV(J,1)
      CINV(1,J)=Z2
      CINV(J,1)=Z1
10  CONTINUE
      CALL MATMPY(CINV,R,FMASS,9)
      DO 400 I=1,9
      DO 400 J=1,9
400  T(I,J)=0.
      T(1,1)=1.
      T(4,4)=1.
      T(7,7)=1.
      T(2,2)=DCS(2)
      T(3,3)=DCS(2)
      T(5,5)=DCS(2)
      T(6,6)=DCS(2)
      T(8,8)=DCS(2)
      T(9,9)=DCS(2)
      T(2,3)=-DCS(1)
      T(5,6)=-DCS(1)
      T(8,9)=-DCS(1)
      T(3,2)=DCS(1)
      T(6,5)=DCS(1)
      T(9,8)=DCS(1)
      CALL MATMPY(FMASS,T,C,9)
      T(2,3)=DCS(1)
      T(5,6)=DCS(1)
      T(8,9)=DCS(1)
      T(3,2)=-DCS(1)
      T(6,5)=-DCS(1)
      T(9,8)=-DCS(1)
      CALL MATMPY(T,C,PLTH,9)
      RETURN
      END

```

```

$      FORTRAN DECK
CDINMTM
C      THIS SUBROUTINE DETERMINES THE DOUBLE INTEGRAL MATRIX FOR
C      THE TRIANGULAR PLATE M MATRIX - PRZEMIENIECKI, PAGE 304
C      Y2,X3,Y3 = COORDS. OF PLATE CORNERS IN LOCAL COORDINATES
C      PRHO = DENSITY
C      PTH = PLATE THICKNESS
C      P = DOUBLE INTEGRAL MATRIX
C      SUBROUTINE DINMTM(Y2,X3,Y3,PRHO,PTH,P)
      DIMENSION P(9,9)
      P(1,1)=DBLINT(Y2,X3,Y3,0,0)
      P(2,1)=DBLINT(Y2,X3,Y3,1,0)
      P(2,2)=DBLINT(Y2,X3,Y3,2,0)
      P(3,1)=DBLINT(Y2,X3,Y3,0,1)
      P(3,2)=DBLINT(Y2,X3,Y3,1,1)
      P(3,3)=DBLINT(Y2,X3,Y3,0,2)
      P(4,1)=P(2,2)
      P(4,2)=DBLINT(Y2,X3,Y3,3,0)
      P(4,3)=DBLINT(Y2,X3,Y3,2,1)
      P(4,4)=DBLINT(Y2,X3,Y3,4,0)
      P(5,1)=P(3,2)
      P(5,2)=P(4,3)
      P(5,3)=DBLINT(Y2,X3,Y3,1,2)
      P(5,4)=DBLINT(Y2,X3,Y3,3,1)
      P(5,5)=DBLINT(Y2,X3,Y3,2,2)
      P(6,1)=P(3,3)
      P(6,2)=P(5,3)
      P(6,3)=DBLINT(Y2,X3,Y3,0,3)
      P(6,4)=P(5,4)
      P(6,5)=DBLINT(Y2,X3,Y3,1,3)
      P(6,6)=DBLINT(Y2,X3,Y3,0,4)
      P(7,1)=P(4,2)
      P(7,2)=P(4,4)
      P(7,3)=P(5,4)
      P(7,4)=DBLINT(Y2,X3,Y3,5,0)
      P(7,5)=DBLINT(Y2,X3,Y3,4,1)
      P(7,6)=DBLINT(Y2,X3,Y3,3,2)
      P(7,7)=DBLINT(Y2,X3,Y3,6,0)
      P(8,1)=P(5,3)+P(4,3)
      P(8,2)=P(6,4)+P(5,4)
      P(8,3)=P(6,5)+P(5,5)
      P(8,4)=P(7,6)+P(7,5)
      P(8,5)=DBLINT(Y2,X3,Y3,2,3)+P(7,6)
      P(8,6)=DBLINT(Y2,X3,Y3,1,4)+DBLINT(Y2,X3,Y3,2,3)
      P(8,7)=DBLINT(Y2,X3,Y3,4,2)+DBLINT(Y2,X3,Y3,3,3)
      P(8,8)=DBLINT(Y2,X3,Y3,2,4)+DBLINT(Y2,X3,Y3,4,2)
      P(9,1)=P(6,3)
      P(9,2)=P(6,5)
      P(9,3)=P(6,6)
      P(9,4)=DBLINT(Y2,X3,Y3,2,3)
      P(9,5)=DBLINT(Y2,X3,Y3,1,4)

```

```

P(0,6)=DBLINT(Y2,X3,Y3,0,2)
P(0,7)=DBLINT(Y2,X3,Y3,3,3)
P(0,8)=DBLINT(Y2,X3,Y3,1,5)+DBLINT(Y2,X3,Y3,2,4)
P(0,9)=DBLINT(Y2,X3,Y3,0,6)
DO 10 I=1,9
DO 10 J=1,1
10 P(I,J)=P(I,J)+PRHO*PTH
DO 20 I=2,9
N=I-1
DO 20 J=1,N
P(J,I)=P(I,J)
20 CONTINUE
RETURN
END

```

```

S      FORTRAN DECK
CEIGEN  REDUCES STIFFNESS MATRIX AND INVERTS IT, REDUCES MASS MATRIX
C      DETERMINES EIGENVALUES AND EIGENVECTORS
C      THE ARGUMENTS ARE=
C      A - VECTOR OF LENGTH NRDF*(NRDF+1)/2
C      VALU - VECTOR OF LENGTH NEIG
C      TEMP,B,C,DUM3, - VECTORS OF LENGTH NRDF OR NMASS (SMALLER)
C      E - MATRIX OF DIMENSION (NRDF,3)
C      IDUM4 - VECTOR OF LENGTH NRDF OR NMASS (SMALLER)
C      ITAPE,JTAPE, NTAPE, MTAPE, - THESE ARE VARIOUS TAPES
C      NRDF - NUMBER OF DEGREES OF FREEDOM OF THE SYSTEM
C      NEIG - NUMBER OF EIGENVALUES DESIRED
C      NVEC - NUMBER OF EIGENVECTORS DESIRED
C      NMASS=NO. OF NORMAL DISPLACEMENTS
C      NOMASS=NO. OF ROTATIONAL DEGREES OF FREEDOM
C      STIFF IS ON MTAPE IN COMPACT FORM
C      MASS IS ON NTAPE IN COMPACT FORM
SUBROUTINE EIGEN(A,VALU,TEMP,B,C,DUM3,E,IDUM4,ITAPE,JTAPE,KTAPF,
1NTAPE,MTAPE,NRDF,NEIG,NVEC,NMASS,NOMASS)
  DIMENSION DUM3(NRDF),IDUM4(1),A(1),VALU(1),B(1),C(1),E(NRDF,3),
1TEMP(1)
  DIMENSION ILOW(50),IHIGH(50)
  INTEGER OUT
  DATA Q1/6HFLEXIB/,Q2/6HILITY /,Q3/6HMATRIX/
  DATA Q4/6HWEIGHT/,Q5/6H MATRI/,Q6/6HX /
  DO 56 I=1,NMASS
    ILOW(I)=1
56  IHIGH(I)=NMASS
    OUT=6
    REWIND MTAPE
    REWIND NTAPE
    NTEMP=NMASS
    CALL DIVID(NMASS,NOMASS,MTAPE,JTAPE,ITAPE,A,B)
    CALL ZROMAK(A,B,C,DUM3,NMASS,NOMASS,ITAPE,JTAPE,MTAPE,KTAPF)
    CALL DIVID(NMASS,NOMASS,MTAPE,JTAPE,ITAPE,A,B)
    CALL ZROMAK(A,B,C,DUM3,NMASS,NOMASS,ITAPE,JTAPE,NTAPE,KTAPF)
345  CONTINUE
    REWIND MTAPE
    REWIND NTAPE
    NREDU=NMASS
    NRMX=NREDU*(NREDU+1)/2
    READ(MTAPE) (A(I),I=1,NRMX)
    WRITE(OUT,5500)
5500  FORMAT(//85HREDUCED UPPER TRIANGULAR
1STIFFNESS MATRIX)
    DO 5501 I=1,NREDU
      NS=(2*I+(1-1)*(2*NREDU-1))/2
      NE=(2*NREDU+(1-1)*(2*NREDU-1))/2
      WRITE(OUT,5502) I,(A(J),J=NS,NE)
5502  FORMAT(/3HROW,14,8(/9E14.5))
5501  CONTINUE
      CALL SYMINV(A,NREDU)
      WRITE(OUT,5503)
5503  FORMAT(//89HREDUCED UPPER TRIANGULAR
1FLEXIBILITY MATRIX)
      PUNCH 5602, ((ILOW(K),IHIGH(K)),K=1,NREDU)
5602  FORMAT (18I4)
      DO 5504 I=1,NREDU
        NS=(2*I+(1-1)*(2*NREDU-1))/2
        NE=(2*NREDU+(1-1)*(2*NREDU-1))/2
5504  WRITE(OUT,5502) I,(A(J),J=NS,NE)

```

```

PUNCH 6011, 01,02,03
6011 FORMAT(3A6)
DO 5507 I=1,NREDU
  II=I-1
  IF(II.EQ.0) GO TO 5508
  DO 5509 J=1,II
    NU=(2*I+(J-1)*(2*I-J))/2+(J-1)*(NREDU-I)
5509 R(J)=A(NU)
5508 CONTINUE
  NS=(2*I+(I-1)*(2*NREDU-I))/2
  NE=(2*NREDU+(I-1)*(2*NREDU-I))/2
  J=I
  DO 5510 JJ=NS,NE
    R(J)=A(JJ)
5510 J=J+1
  PUNCH 6010,(R(J),J=1,NREDU)
6010 FORMAT(1P6E12.5)
5507 CONTINUE
C   OPTION TO EXPAND REDUCED FLEXIBILITY MATRIX TO FULL MATRIX BY
C   INSERTING 1 OR 2 ZERO ROWS AND COLUMNS REPRESENTING ATTACH POINTS.
C   CODE , NCOD = 1  OPTION EXECUTED , NCOD = 0  OPTION NOT EXECUTED
  READ(5,560) NCOD
  560 FORMAT (I6)
  IF(NCOD) 580,580,570
  570 CALL FULFL (A,NREDU)
  580 READ(NTAPE) (A(I),I=1,NRMX)
  DO 6012 I=1,NRMX
6012 A(I)=A(I)*32.174*12.
  WRITE(OUT,5505)
5505 FORMAT(///79H R E D U C E D   U P P E R   T R I A N G U L A R
1 H F I G H T   M A T R I X)
  DO 5506 I=1,NREDU
    NS=(2*I+(I-1)*(2*NREDU-I))/2
    NE=(2*NREDU+(I-1)*(2*NREDU-I))/2
5506 WRITE(OUT,5502) I,(A(J),J=NS,NE)
  PUNCH 6011, 04,05,06
  DO 5511 I=1,NREDU
    II=I
    IF(II.EQ.0) GO TO 5512
    DO 5513 J=1,II
      NU=(2*I+(J-1)*(2*I-J))/2+(J-1)*(NREDU-I)
5513 R(J)=A(NU)
5512 CONTINUE
    NS=(2*I+(I-1)*(2*NREDU-I))/2
    NE=(2*NREDU+(I-1)*(2*NREDU-I))/2
    J=I
    DO 5514 JJ=NS,NE
      R(J)=A(JJ)
5514 J=J+1
    PUNCH 6010,(R(J),J=1,NREDU)
5511 CONTINUE
  IF(NEIG.EQ.0) RETURN
  NMAX=NTMP*(NTMP+1)/2
  30 CONTINUE
C   READ IN THE MASS MATRIX
  REWIND NTAPE
  READ(NTAPE) (A(I),I=1,NRMX)
  REWIND NTAPE
  355 CONTINUE
  CALL EIGMAT(NTMP,A,VALU,TEMP,R,C,DUM3,E,(DUM4,NTAPE,NTAPE,JTAPE,
1ITAPE,NEIG,NVEC)

```

```

100 CONTINUE
DO 60 I=1,NEIG
DUM3(I)=SORT(VALU(I))/6.2831853
60 CONTINUE
WRITE(OUT,9009)
: WRITE(OUT,9005) (I,DUM3(I),I=1,NEIG)
9009 FORMAT(1H1,43X.33WHERE ARE THE NATURAL FREQUENCIES ///)
9005 FORMAT(35X,29HTHE NATURAL FREQUENCY NUMBER 13,2X,2HIS 12.3,2X,
13HCPS)
9008 FORMAT(1H1,38X.43WHERE ARE THE EIGENVALUES AND EIGENVECTORS ///)
RETURN
END

```

S FORTRAN DECK
 CFULFL EXPANDS REDUCED FLEXIBILITY MATRIX BY INSERTING 1 OR 2 ZERO
 C ROWS AND COLUMNS REPRESENTING ATTACH POINTS.
 C THE ARGUMENTS ARE
 C B(I) = REDUCED FLEXIBILITY MATRIX IN COMPACT FORM
 C NXC = ORDER OF REDUCED FLEX. MATRIX
 C INPUT DATA REQUIRED
 C NR = NO. OF ATTACH POINTS (1 OR 2)
 C NNE,NWO = MASS NUMBERS OF ATTACH POINTS 1 AND 2 RESP.

SURROUTINE FULFL(R,NXC)
 DIMENSION B(1),D(1275),C(50)
 DATA /07/6HEXPAND/,08/6HED FLE/,09/6HXIBILI/,010/6HTY MAT/,011/6HRI
 1X /
 READ(5,1)NR,NNE,NWO
 1 FORMAT (9I8)
 MS=NXC+NR
 MMS=MS*(MS+1)/2
 DO 50 I=1,MMS
 50 D(I)=0.0
 JJJ=0
 KK=0
 JJ=0
 DO 100 J=1,MS
 IF(J.EQ.NNE.OR.J.EQ.NWO)GO TO 99
 I=JJ+1
 JJ=I+NXC-J+JJJ
 KKK=J-1
 DO 98 JK=I,JJ
 KKK=KKK+1
 KK=KK+1
 IF(KKK.EQ.NNE.OR.KKK.EQ.NWO)GO TO 96
 GO TO 97
 96 KK=KK+1
 97 D(KK)=B(JK)
 98 CONTINUE
 GO TO 100
 99 KK=KK+MS-J+1
 JJJ=JJJ+1
 100 CONTINUE
 WRITE(6,2)
 2 FORMAT(//86HUPPER TRIANGLE-EXPANDED FL
 1 EXIBILITY MATRIX)
 DO 10 I=1,MS
 NS=(2*I+(I-1)*(2*MS-I))/2
 NE=(2*MS+(I-1)*(2*MS-I))/2
 WRITE(6,3)I,(D(J),J=NS,NE)
 3 FORMAT(/3HROW,14/(9F14.5))
 10 CONTINUE
 PUNCH 4,07,08,09,010,011
 4 FORMAT(5A6)
 DO 20 I=1,MS
 II=I-1
 IF(II.EQ.0) GO TO 18
 DO 19 J=1,II
 NU=(2*I+(J-1)*(2*I-J))/2+(J-1)*(MS-I)
 19 C(J)=D(NU)
 18 CONTINUE
 NS=(2*I+(I-1)*(2*MS-I))/2
 NE=(2*MS+(I-1)*(2*MS-I))/2
 J=I

```
DO 16 JJ=NS,NE  
C(J)=D(JJ)  
16 J=J+1  
PUNCH 5,(C(J),J=1,MS)  
5 FORMAT(1P6E12.5)  
20 CONTINUE  
RETURN  
END
```

266
27
275
280
27
200
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300

```

9      FORTRAN DECK
CDIVID
C      N=NO. OF NORMAL DISPLACEMENTS
C      M=NO. OF ROTATIONAL D.O.F.
C      NTPE-CONTAINS STIFFNESS (OR MASS) MATRIX
C      MTPE-K12 (M12) STORED
C      ITPE-K13 (M13) STORED
C      A- DUMMY STORAGE VECTOR, LARGER OF (N*(N+1)/2 OR M*(M+1)/2)
SUBROUTINE DIVID (N,M,NTPE,MTPE,ITPE,A,B)
  DIMENSION A(1),B(1)
  REWIND ITPE
  REWIND NTPE
  REWIND MTPE
  NMAX=N*(N+1)/2
  MMAX=M*(M+1)/2
  NM=N+M
  ICNT=0
  DO 10 I=1,N
    II=NM-I+1
    READ(NTPE) (R(J),J=1,II)
    ID=II-M
    DO 20 J=1,ID
      ICNT=ICNT+1
      A(ICNT)=B(J)
      ID1=ID+1
      JCNT=0
      DO 30 J=ID1,II
        JCNT=JCNT+1
      R(JCNT)=B(J)
      WRITE(MTPE) (R(J),J=1,M)
10    CONTINUE
      WRITE(ITPE) (A(J),J=1,NMAX)
      REWIND MTPE
      REWIND ITPE
      ID=0
      ICNT=0
      DO 50 I=1,M
        II=M-ICNT
        READ(NTPE) (R(J),J=1,II)
        ICNT=ICNT+1
        DO 60 J=1,II
          ID=ID+1
60      A(ID)=R(J)
50    CONTINUE
      RETURN
  END

```

```

$      FORTRAN DECK
CZROMAK
C      D IS A DUMMY VECTOR WITH STORAGE N OR M (LARGER)
C      A IS A DUMMY VECTOR WITH STORAGE  $N*(N+1)/2$  OR  $M*(M+1)/2$  (LARGER)
C      R IS A DUMMY VECTOR WITH STORAGE N OR M (LARGER)
C      C IS A DUMMY VECTOR WITH STORAGE N OR M (LARGER)
C      N=NO. OF NORMAL DISPLACEMENTS
C      M=NO. OF ROTATIONAL D.O.F.
C      N1PE CONTAINS K1 MATRIX
C      M1PE CONTAINS K12 MATRIX
C      I1PE SCRATCH TAPE
C      K1PE STORES  $K12*K2*(-1)$ 
C      A INITIALLY CONTAINS  $K2^2$  INVERSE
C*** REDUCED STIFFNESS MATRIX IS STORED ON I1PE
SUBROUTINE ZROMAK(A,B,C,D,N,M,N1PE,M1PE,I1PE,K1PE)
  DIMENSION A(1),B(1),C(1),D(1)
  DOUBLE PRECISION SUM,DP1,DP2
  CALL SYMINV(A,M)
  REWIND M1PE
  REWIND I1PE
  REWIND N1PE
  REWIND K1PE
  NMAX=N*(N+1)/2
  MMAX=M*(M+1)/2
  DO 10 KK=1,N
    READ(M1PE) (R(1),I=1,M)
    ICNT=0
    DO 1000 IK=1,M
      JJ=IK
      JK=IK
      DO 20 J=JJ,M
        ICNT=ICNT+1
20      C(J)=A(ICNT)
        IJ=JJ-1
        JA=M
        ID=IK
        DO 30 J=1,JJ
          IF (JJ.EQ.0) GO TO 30
          C(J)=A(ID)
          JA=JA-1
          ID=ID+JA
30      CONTINUE
        SUM=0.000
        DO 40 J=1,M
          DP1=B(J)
          DP2=C(J)
          SUM=SUM+DP1*DP2
40      R(JK)=SUM
1000 CONTINUE
        WRITE (I1PE) (D(J),J=1,M)
        WRITE (K1PE) (D(J),J=1,M)
10      CONTINUE
        REWIND I1PE

```

```

REWIND MTPE
REWIND NTPE
REWIND KTPE
READ (NTPE) (A(J),J=1,NMAX)
ICNT=0
DO 60 KK=1,N
  READ (ITPE) (D(J),J=1,M)
  KI=KK
  DO 70 KJ=1,N
    READ(MTPE)(C(J),J=1,M)
    KP=KJ
    IF(KP.LT.KI) GO TO 70
    SUM=0.000
    DO 80 KR=1,M
      DP1=D(KR)
      DP2=C(KR)
80    SUM=SUM +DP1*DP2
    ICNT=ICNT+
    SM=SUM
    A(ICNT)=A(ICNT)-SM
70  CONTINUE
  REWIND MTPE
60  CONTINUE
  REWIND NTPE
  REWIND MTPE
  REWIND ITPE
  WRITE(ITPE) (A(I),I=1,NMAX)
  REWIND ITPE
  RETURN
END

```

```

$      FORTRAN DECK
CZROMAM
C      N=NO. OF NORMAL DISPLACEMENTS
C      M=NO. OF ROTATIONAL D.O.F.
C      NTPF CONTAINS M11 MATRIX
C      MTPF CONTAINS M12 MATRIX
C      ITPE SCRATCH TAPE
C      KTFE CONTAINS K12*K22**(-1)
C***  REDUCED MASS MATRIX IS STORED ON ITPE
      SUBROUTINE ZROMAM(A,B,C,D,N,M,NTPF,MTPF,ITPE,KTFE)
      DIMENSION A(1),B(1),C(1),D(1)
      DOUBLE PRECISION SUM1,SUM2,DP1,DP2,DP3
      NMAX=N*(N+1)/2
      REWIND MTPF
      REWIND ITPE
      REWIND NTPF
      REWIND KTFE
      NMAX=N*(N+1)/2
      DO 10 KK=1,N
      READ(KTFE) (R(I),I=1,M)
      ICNT=0
      DO 1000 IK=1,M
      JJ=IK
      JK=IK
      DO 20 J=JJ,M
      ICNT=ICNT+1
20  C(J)=A(ICNT)
      JJ=JJ-1
      JA=M
      ID=IK
      DO 30 J=1,JJ
      IF(JJ.EQ.0) GO TO 30
      C(J)=A(ID)
      JA=JA-1
      ID=ID+JA
30  CONTINUE
      SUM1=1.D0
      DO 50 J=1,M
      DP1=B(J)
      DP2=C(J)
50  SUM1=SUM1+DP1*DP2
      D(JK)=SUM1
1000 CONTINUE
      WRITE(ITPE) (D(J),J=1,M)
10  CONTINUE
      REWIND ITPE
      REWIND MTPF
      REWIND NTPF
      REWIND KTFE
      READ(NTPF) (A(J),J=1,NMAX)
      DO 60 KK=1,N
      READ(MTPF) (R(J),J=1,M)

```

```

      READ(ITPE) (O(J),J=1,N)
      DO 70 KJ=1,N
      READ(KTPE) (C(J),J=1,N)
      SUM1=0.00
      SUM2=0.00
      DO 80 KR=1,M
      DP1=B(KR)
      DP2=D(KR)
      DP3=C(KR)
      SUM1=SUM1+DP1*DP3
      SUM2=SUM2+DP2*DP3
      SM1=SUM1
      SM2=SUM2
      IF (KJ.GE.KK) MM=(2*KJ+(KK-1)*(2*NMASS-KK))/2
      IF (KJ.GE.KK) A(MM)=A(MM)-SM1+SM2
      IF (KJ.LE.KK) MM=(2*KK+(KJ-1)*(2*NMASS-KJ))/2
      IF (KJ.LE.KK) A(MM)=A(MM)-SM1
70  CONTINUE
      REWIND KTPE
80  CONTINUE
      REWIND NTP-
      REWIND MTP-
      REWIND ITPE
      REWIND KTPE
      WRITE(ITPE) (A(I),I=1,NMAX)
      REWIND ITPE-
      RETURN
      END

```

```

C      FORTRAN DECK
CSYMINV
C      A IS THE UPPER TRIANGLE OF THE SYMMETRIC MATRIX TO BE INVERTED.
C      ELEMENTS ARE STORED ROWWISE.
C      N = ORDER OF MATRIX
C      PROGRAM INVERTS IN PLACE.
      SUBROUTINE SYMINV(A,N)
      DIMENSION A(1)
      NMAX=N*(N+1)/2
      A(1)=SQRT(A(1))
      DO 100 IJ=N,N
100  A(IJ)=A(IJ)/A(1)
      A(1)=1.0/A(1)
      IM1=1
      IJ=N
      DO 1000 I=1,N
      II=IJ+1
      IJ=II
      DO 200 J=I,N
      JMI=J-I
      LI=I
      LJ=J
      DO 120 L=1,IM1
      A(IJ)=A(IJ)-A(LI)*A(LJ)
      LI=LI+N-L
120  LJ=LJ+JMI
200  IJ=IJ+1
      A(II)=SQRT(A(II))
      JI=I
      JJ=J
      DO 300 J=1,IM1
      A(JI)=A(JJ)*A(JI)
      IF(J-IM1)300,420,420
300  JP1=J+1
      JL=JJ
      LI=JI
      DO 400 L=JP1,IM1
      JL=JL+1
      LI=LI+N-L+1
400  A(JI)=A(JI)+A(JL)*A(LI)
420  A(JI)=-A(JI)/A(II)
      JI=JI+N-J
      JJ=JJ+N-J+1
      IF(I-N)600,900,900
600  IP1=I+1
      IJ=II
      DO 700 J=IP1,N
      IJ=IJ+1
700  A(IJ)=A(IJ)/A(II)
900  A(II)=1.0/A(II)
1000 IM1=1
      II=1

```

```

DO 1000 I=1,N
JJ=11
IJ=11
DO 1400 J=1,N
A(IJ)=A(IJ)*A(JJ)
JP1=J+1
IF (JP1-N) 1100,1100,1400
1100 IL=JJ
JL=JJ
DO 1200 L=JP1,N
IL=IL+1
JL=JL+1
1200 A(IJ)=A(IJ)+A(IL)*A(JL)
JJ=JL+1
1400 IJ=IJ+1
2000 II=IJ
RETURN
END

```

.....

```

9      FORTRAN DECK
CEIGMAT
C      THIS SUBROUTINE FINDS THE EIGENVALUES AND EIGENVECTORS FOR
C      SYMMETRIC MASS AND STIFFNESS MATRICES.
C      THE ARGUMENTS ARE--
C      N- ORDER OF MATRICES.
C      A- DUMMY VECTOR WITH DIMENSION IN MAIN PROGRAM OF  $N*(N+1)/2$ 
C      VALU- STORAGE FOR EIGENVALUES. MUST BE DIMENSIONED IN THE MAIN
C            PROGRAM AS A VECTOR OF LENGTH NEIG.
C      TEMP,B,C,D,- DUMMY VECTORS WITH DIMENSION OF N IN MAIN PROGRAM.
C      F- DUMMY ARRAY WITH DIMENSIONS OF (N,3) IN MAIN PROGRAM.
C      IDUM- DUMMY INTEGER VECTOR WITH DIMENSION OF N IN MAIN PROGRAM.
C      MTAPE- TAPE WHERE STIFFNESS MATRIX IS STORED IN COMPACT FORM.
C      NTAPE- TAPE WHERE MASS MATRIX IS STORED IN COMPACT FORM.
C      JTAPE,ITAPE- SCRATCH TAPES.
C      NEIG- NUMBER OF EIGENVALUES DESIRED.
C      NVEC- NUMBER OF EIGENVECTORS DESIRED. MUST BE EQUAL TO OR LESS
C            THAN NEIG.
C      THE MASS AND STIFFNESS MATRICES ARE STORED IN COMPACT FORM AS
C      VECTORS. ONLY THE UPPER TRIANGLE OF THESE MATRICES(BY ROWS) IS
C      STORED.
C      SUBROUTINE EIGMAT(N,A,VALU,TEMP,B,C,D,F,IDUM,MTAPE,NTAPE,JTAPE,
C      ITAPE,NEIG,NVEC)
C      DIMENSION A(1),TEMP(1),VALU(1),B(1),C(1),D(1),F(N,3),IDUM(1)
C      DOUBLE PRECISION SUM,SUM1
C      INTEGER OUT
C      OUT=6
C      REWIND ITAPE
C      REWIND JTAPE
C      REWIND NTAPE
C      REWIND MTAPE
C      M=?*N
C      NMAX=N*(N+1)/2
C* * * * *
C      STEP 1
C      READ IN M BY ROWS IN COMPACTED FORM
C      REPLACE M BY (1)TRANPOSE, WHERE M=L*(L)TRANPOSE
C      CALCULATE FIRST ROW
C      READ (NTAPE) (A(I),I=L,NMAX)
C      REWIND NTAPE
C      6 CONTINUE
C      A(1)=SORT(A(1))
C      DO 10 I=2,N
C      10 A(I)=A(I)/A(1)
C      CALCULATE ALL THE OTHER ROWS
C      IND=N
C      DO 10 I=2,N
C      IND=IND+1
C      SUM=0.00
C      KI=1-1
C      DO 50 JJ=L,KI
C      MJ=(M-JJ)*(JJ-1)/2+I

```

```

200 SUM=SUM+A(MJ)*A(MJ)
   A(IND)=DSQRT(A(IND)-SUM)
   IF(IND.EQ.NMAX) GO TO 100
   SUM1=A(IND)
   K1=1+1
   DO 99 J=K1.N
     IND=IND+1
     SUM=0.00
     I1=1-1
     DO 60 JJ=1.I1
       K=(M-JJ)*(JJ-1)/2
       KI=K+1
       KJ=K+J
60    SUM=SUM+A(KI)*A(KJ)
     A(IND)=(A(IND)-SUM)/SUM1
99    CONTINUE
100   CONTINUE
101   CONTINUE
C     CHECK FOR SINGULAR MASS MATRIX
      DO 102 I=1.N
        KI=(M-I)*(I-1)/2+1
        IF(A(KI).EQ.0.) GO TO 1090
102   CONTINUE
C     THIS COMPLETES STEP 1
C * * * * *
C     STEP 2
C     WRITE (L)TRANSPOSE ON TAPE BY COLUMNS
C     PUT (L)TRANSPOSE INTO TEMPORARY STORAGE (TEMP--A VECTOR)
C     AND THEN WRITE TEMP ON TAPE
      KTAPF=NTAPF
310   IND=0
      DO 340 J=L.N
        DO 330 I=1.J
          IND=IND+1
          M11=(M-I)*(I-1)/2+J
          TEMP(IND)=A(M11)
330   CONTINUE
      WRITE(KTAPF) (TEMP(JJ),JJ=1,IND)
      IND=0
340   CONTINUE
C     THIS COMPLETES STEP 2
C * * * * *
C     STEP 3
C     ((L)TRANSPOSE) INVERSE REPLACES (L)TRANSPOSE IN CORE
C     REPLACEMENT IS DONE BY LAST COLUMN FIRST--WORKING UP THE COLUMN
      DO 410 I=1.N
        IND=(I*(M+1-1))/2-N
410   A(IND)=1./A(IND)
      DO 499 J=2.N
        IJ=(N+2)-J
        DO 490 I=2.IJ
          IND=(N+J+1-1)*(IJ-1)/2
          SUM=0.00

```

```

      KI=JJ-1+2
      DO 450 K=K1,JJ
      IDK=IND+K
      MK=(M-K)*(K-1)/2+JJ
450  SUM=SUM+A(IDK)*A(MK)
      IND=IND+JJ
      IDI=IND-I+1
460  A(IND)=-SUM+A(IDI)
499  CONTINUE
C    END OF STEP 3
C* * * * *
C    STEP 4
C    U=((L)TRANPOSE)INVERSE
C    WRITE U ON TAPE BY ROWS
C    WRITE(JTAPE) (A(I),I=L,NMAX)
C    FINISHED WITH STEP 4
C* * * * *
C    STEP 5
C    WRITE U ON TAPE BY COLUMNS STARTING WITH THE LAST COLUMN FIRST
C    PUT U (LAST COLUMN FIRST) INTO TEMP AND THEN WRITE ON TAPE
      IND=0
      DO 550 K=L,N
      J=N-K+1
      DO 560 I=1,J
      IND=IND+1
      M12=(M-I)*(I-1)/2+J
      TEMP(IND)=A(M12)
560  CONTINUE
      WRITE(JTAPE) (TEMP(JJ),JJ=L,IND)
      IND=0
575  CONTINUE
C    END OF STEP 5
C* * * * *
C    STEP 6
C    FORM KU
C    READ K INTO CORF
C    READ U INTO CORF A COLUMN AT A TIME IN REVERSE ORDER
C    REPLACE K BY KU COLUMN BY COLUMN STARTING WITH THE LAST COLUMN
C    AND WORKING UP THE COLUMN
      READ(JTAPE) (A(I),I=1,NMAX)
      REWIND JTAPE
      DO 690 JJ=L,N
      J=N+1-JJ
      READ(JTAPE) (TEMP(I),I=L,J)
      DO 690 II=1,J
      I=J+1-II
      SUM=0.D0
      DO 650 K=1,I
      MK1=(M-K)*(K-1)/2+J
650  SUM=SUM+A(MK1)*TEMP(K)
      IND=(M-I)*(I-1)/2+J
      IF(I.EQ.J) GO TO 680

```

```

      KI=(M-I)*(I-1)/2
      I=I+1
      DO 660 K=I,J
      KIK=K1+K
660  SUM=SUM+A(KIK)*TEMP(K)
680  CONTINUE
      A(IND)=SUM
690  CONTINUE
C    END OF STEP 6
C * * * * *
C    STEP 7
C    FORM((L)INVERSE)*KU
C    KU IS IN CORE
C    READ IN L COLUMN BY COLUMN AND CALCULATE ((L)INVERSE)*KU
C    ROW BY ROW
C    CALCULATE THE FIRST ROW
      REWIND NTAPE
      READ(NTAPE) TEMP(1)
      DO 710 I=1,N
710  A(I)=A(I)/TEMP(1)
C    NOW CALCULATE THE REST OF THE ROWS
      IND=N
      DO 799 I=2,N
      READ (NTAPE) (TEMP(JJ),JJ=1,I)
      DO 799 J=1,N
      IND=IND+1
      JJ=I-1
      SUM=0.D0
      DO 750 K=1,JJ
      MK2=(M-K)*(K-1)/2+J
750  SUM=SUM+TEMP(K)*A(MK2)
799  A(IND)=(A(IND)-SUM)/TEMP(I)
C    STEP 7 IS COMPLETE
C * * * * *
C    STEP 8
C    DETERMINE EIGENVALUES AND EIGENVECTORS OF THE NEW MATRIX
C    CHANGE THE SIGN OF A IN ORDER TO OBTAIN THE SMALLEST
C    EIGENVALUE FIRST
      DO 800 I=1,NMAX
800  A(I)=-A(I)
      CALL HIGHMAT(A,VALU,TEMP,8,C,D,E,IDUM,N,NEIG,NVEC,MTAPE)
C    CHANGE VALU BACK
      DO 850 I=1,NF16
850  VALU(I)=-VALU(I)
C    STEP 8 IS COMPLETE
C * * * * *
C    STEP 9
C    CHANGE EIGENVECTORS BACK
C    READ U INTO CORE BY ROWS
C    READ UNCHANGED EIGENVECTORS INTO CORE ONE AT A TIME
C    CHANGE AND PRINT EIGENVECTORS
      IF(NVEC.EQ.0) GO TO 2000
      WRITE(OUT,1001)

```

```

      REWIND ITAPE
      READ(ITAPE) (A(I), I=1, NMAX)
      REWIND HTAPE
      DO 909 JJ=1, NVFC
      READ(HTAPE) (TEMP(I), I=1, N)
      IND=0
      DO 910 I=1, N
      SUM=0.00
      DO 909 J=1, N
      IND=IND+1
909  SUM=SUM+A(IND)*TEMP(J)
910  TEMP(I)=SUM
C     NORMALIZE THE EIGENVECTOR
      SUM=TEMP(I)
      DO 939 II=1, N
      IF(ABS(SUM)-ABS(TEMP(II))) 938, 939, 939
938  SUM=TEMP(II)
939  CONTINUE
      IF(SUM) 940, 947, 940
940  CONTINUE
      DO 941 II=1, N
      TEMP(II)=TEMP(II)/SUM
941  CONTINUE
947  CONTINUE
999  WRITE(OUT, 4000) JJ, VALU(JJ), (TEMP(I), I=1, N)
C     STEP 9 IS COMPLETE
C * * * * *
      GO TO 2000
4000  FORMAT (1H*, 19H EIGENVECTOR NUMBER 15/12X, 17H CORRESPONDING TO
11PE15.7/(1H 1P6E15.7))
4001  FORMAT(1H1.58X, 43HHERE ARE THE EIGENVALUES AND EIGENVECTORS ///)
4002  FORMAT(1H1.58X, 27HTHE MASS MATRIX IS SINGULAR ///)
1090  WRITE(OUT, 1000)
2000  RETURN
      END

```

9 FORTRAN DECK

CHIGNAT

C PROG.AUTHORS M.ELSON AND R.E.FUNDERLIC.CENTRAL DATA PROCESSING,4,1.0⁶ b

 SURROUTINE HIGNAT(A,VALU,VALL,UPPERD,DIAG,V,T,INTER,NN,NEIG,NVFL,

 MTAPE)

 DIMENSION A(1),VALU(1),VALL(1),UPPERD(1),DIAG(1),V(1),T(NN,3),

 INTER(1)

 REWIND MTAPE

 NZ=0

 N=NN

 IF(N.LE.2)GO TO 49

 NP1=N+1

 NM1=N-1

 NM2=N-2

 NI2P1=N*2+1

 IX=L

 DO 10 I=1,NM2

 SIGMA2=0.

 IP1=I+1

 DO 5 J=IP1,N

 IJ=IX+J

1 SIGMA2=SIGMA2+A(IJ)**2

 SIGMA=SQRT(SIGMA2)

 II=IX+I

 DIAG(1)=A(II)

 IIP1=IX+I+1

 UPPERD(1)=-SIGN(SIGMA,A(IIP1))

 T(1,2)=SIGMA

 IF(ABS(SIGMA).GT.ABS(A(IIP1)))GO TO 2

 UPPERD(1)=A(IIP1)

 A(IIP1)=0.

 GO TO 10

2 A(IIP1)=SQRT(1.+ABS(A(IIP1))/SIGMA)

 SQTGAM=-SIGN(SIGMA*A(IIP1),UPPERD(1))

 IP2=I+2

 DO 5 J=IP2,N

 IJ=IX+J

3 A(IJ)=A(IJ)/SQTGAM

 JK1=I*(2*N-I-1)/2

 JX=JK1

 IIX=JK1

 DO 5 J=IP1,N

 VALL(J)=0.

 JK=JK1+J

 DO 4 K=IP1,J

 IK=IX+K

 VALL(J)=VALL(J)+A(JK)*A(IK)

4 JK=JK+N-K

 IF(J.EQ.N)GO TO 6

 CALL LOUPL(J+2,NP1,VALL(J),A(JX),A(IIX))

5 JX=JX+N-J

6 DELGAM=0.

 DO 7 J=IP1,N

```

      IJ=IX+J
7  DELGAM=DELGAM+A(IJ)*VALL(J)
   DGO2=.5*DELGAM
   DO 6 J=IP1,N
      IJ=IX+J
8  T(I,J)=VALL(J)-DGO2*A(IJ)
   DO 4 II=IP1,N
      III=IX+II
   CALL LOOP2(A(III),A(IX),T(NZ,1),T(II,1),A(III)-I(1,NP1))
   IX=III+N-1
10  IX=IX+N-1
   M=N*(N+1)/2
   UPPERD(NM1)=A(M-1)
   T(NM1,2)=UPPERD(NM1)**2
   DIAG(NM1)=A(M-2)
   DIAG(N)=A(M)
   ENORM=AMAX1(ABS(DIAG)+ABS(UPPERD),ABS(DIAG(N))+ABS(UPPERD(NM1)))
   DO 11 I=2,NM1
      ENRTHP=ABS(DIAG(I))+ABS(UPPERD(I))+ABS(UPPERD(I-1))
11  IF(ENRTHP.GT.ENORM)ENORM=ENRTHP
   DO 12 I=1,NEIG
      VALU(I)=ENORM
12  VALL(I)=-ENORM
   DO 14 I=1,NEIG
13  ROOT=.5*(VALU(I)+VALL(I))
      IF(ROOT.EQ.VALL(I).OR.ROOT.EQ.VALU(I))GO TO 14
      NAGREE=0
      PM2=0.
      PM1=1.
      DO 21 J=1,N
         IF(PM2.NE.0.)GO TO 15
14  PM1=SIGN(1.,PM1)
         GO TO 17
15  IF(PM1.NE.0.)GO TO 17
16  P=-SIGN(1.,PM2)
         PM2=0.
         IF(T(J-1,2)) 18,14,18
17  P=DIAG(J)-ROOT-T(J-1,2)*PM2/PM1
         PM2=1.
18  IF(P)21,19,20
19  PM2=PM1
         IF(PM2)21,20,20
20  NAGREE=NAGREE+1
21  PM1=P
      DO 23 J=1,NEIG
         IF(J.LE.NAGREE)GO TO 22
         IF(VALU(J).LE.ROOT)GO TO 13
         VALU(J)=ROOT
         GO TO 23
22  VALL(J)=ROOT
23  CONTINUE
      GO TO 13

```

```

24 CONTINUE
   IF (NVEC.EQ.0) GO TO 49
   EPSLON=ENORM*1.E-4
   COMPL1=COMPL(1)
   DO 48 J=1,NVEC
   DO 25 J=1,N
      V(J)=1.
      T(J,2)=DIAG(J)-VALU(1)
      IF (J.EQ.N) GO TO 24
      T(J,3)=UPPFRD(J)
25  T(J+1,1)=UPPFRD(J)
26  T(N,3)=0.
      DO 29 J=1,N
      IF (ABS(T(J,2)).LT.1.E-17) T(J,2)=EPSLON
      T(J,1)=T(J,2)
      T(J,2)=T(J,3)
      T(J,3)=0.
      IF (J.EQ.N) GO TO 30
      INTER(J)=0
      JP1=J+1
      IF (ABS(T(JP1,1)).LE.ABS(T(J,1))) GO TO 28
      INTER(J)=1
      DO 27 K=J,1
      TEMP=T(J,K)
      T(J,K)=T(JP1,K)
27  T(JP1,K)=TEMP
28  TMULTP=T(JP1,1)/T(J,1)
      VALL(J)=OR(INTER(J),AND(TMULTP,COMPL1))
      T(JP1,2)=T(JP1,2)-TMULTP*T(J,2)
29  T(JP1,3)=T(JP1,3)-TMULTP*T(J,3)
30  ITER=1
31  DO 32 J=1,N
      L=N+1-J
32  V(1)=(V(L)-T(L,2)*V(L+1)-T(L,3)*V(L+2))/T(L,1)
      VNORM=0.
      DO 33 L=1,N
33  VNORM=VNORM+V(L)**2
      VNORM=SQRT(VNORM)
      DO 34 J=1,N
34  V(J)=V(J)/VNORM
      IF (ITER.EQ.2) GO TO 36
      ITER=2
      DO 35 L=2,N
      LM1=L-1
      TRY=VALL(LM1)
      IF (AND(TRY,1).EQ.0) GO TO 35
      VTEMP=V(LM1)
      V(LM1)=V(L)
      V(L)=VTEMP
35  V(L)=V(L)-VALL(LM1)*V(LM1)
      GO TO 31
36  IF (VNORM.EQ.0.) V(1)=1.
      IIX=(N*N-N-6)/2

```

```

DO 57 KK=1,NM2
IIP1=N-KK
UTV=0.
CALL LOOP3(UTV,A(IIX),V(NZ),IIP1+1,NP1)
CALL LOOP4(A(IIX),V(NZ),NP1,IIP1+1,UTV)
57 IIX=IIX+IIP1-N-2
WRITE(NTAPE) (V(ICH),ICH=1,N)
48 CONTINUE
59 RETURN
END

```

1 FORTRAN DECK

CLOOP1

```
SUBROUTINE LOOP1(JP2,NP1,SGAMPJ,AJX,AIX)
  DIMENSION AJX(1), AIX(1)
  DO 1 L=JP2,NP1
1  SGAMPJ=SGAMPJ+AJX(L)*AIX(L)
  RETURN
END
```

H
B
H
H
H

2 FORTRAN DECK

CLOOP2

```
SUBROUTINE LOOP2(AIIX,AIX,S,SI,AIII,IP1,NP1)
  DIMENSION AIIX(1),AIX(1),S(1)
  DO 2 JJ=IP1,NP1
2  AIIX(JJ)=AIIX(JJ)-AIII*S(JJ)-SI*AIX(JJ)
  RETURN
END
```

H
B
H
H
H

3 FORTRAN DECK

CLOOP3

```
SUBROUTINE LOOP3(UTV,AIIX,V,IIP2,NP1)
  DIMENSION AIIX(1), V(1)
  DO 3 J=IIP2,NP1
3  UIV=UTV+AIIX(J)*V(J)
  RETURN
END
```

B
B
H
H
H

4 FORTRAN DECK

CLOOP4

```
SUBROUTINE LOOP4(AIIX,V,NP1,IIP2,UTV)
  DIMENSION AIIX(1),V(1)
  DO 4 K=IIP2,NP1
4  V(K)=V(K)-AIIX(K)*UTV
  RETURN
END
```

B
B
H
H
H

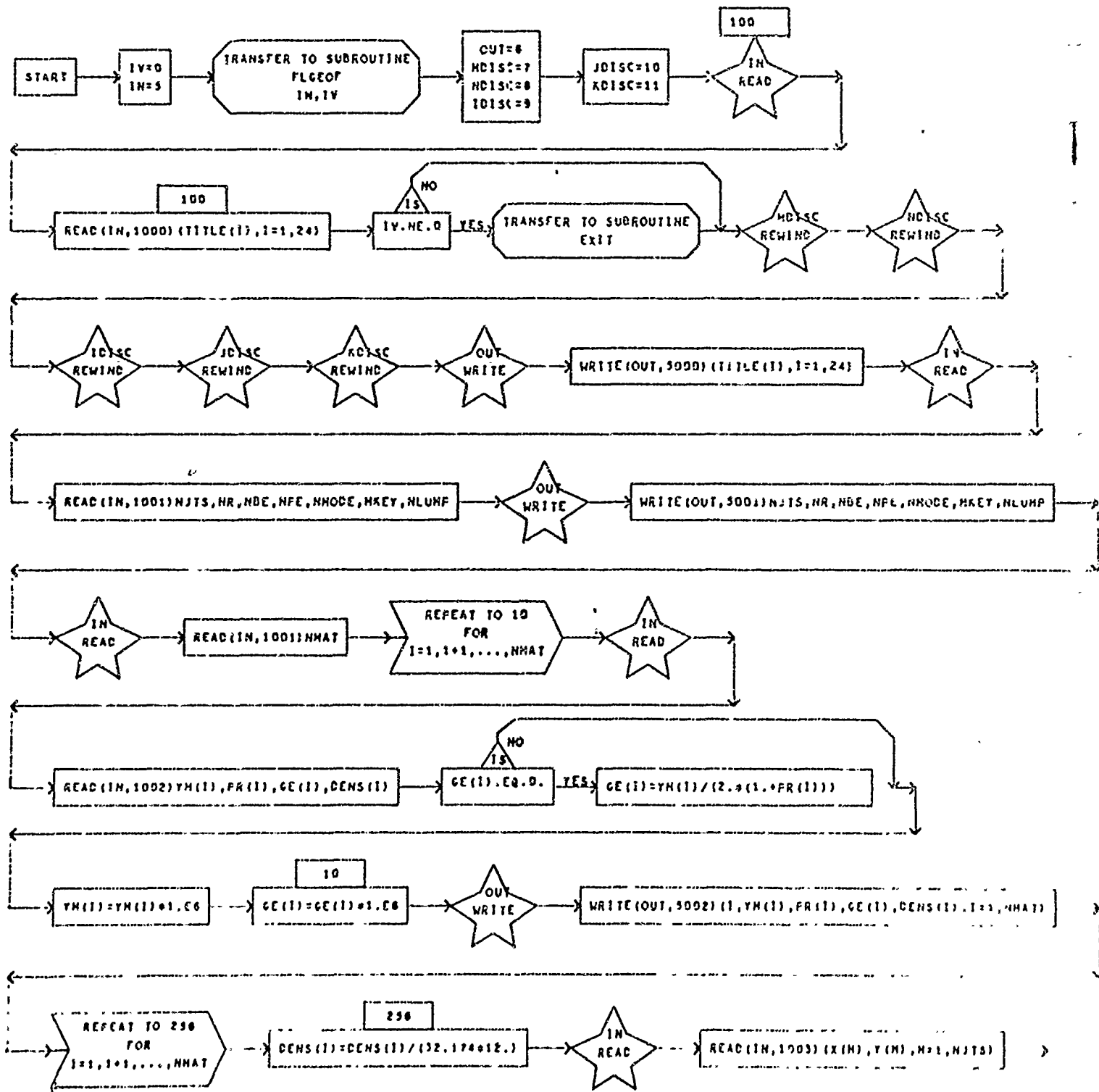
APPENDIX C

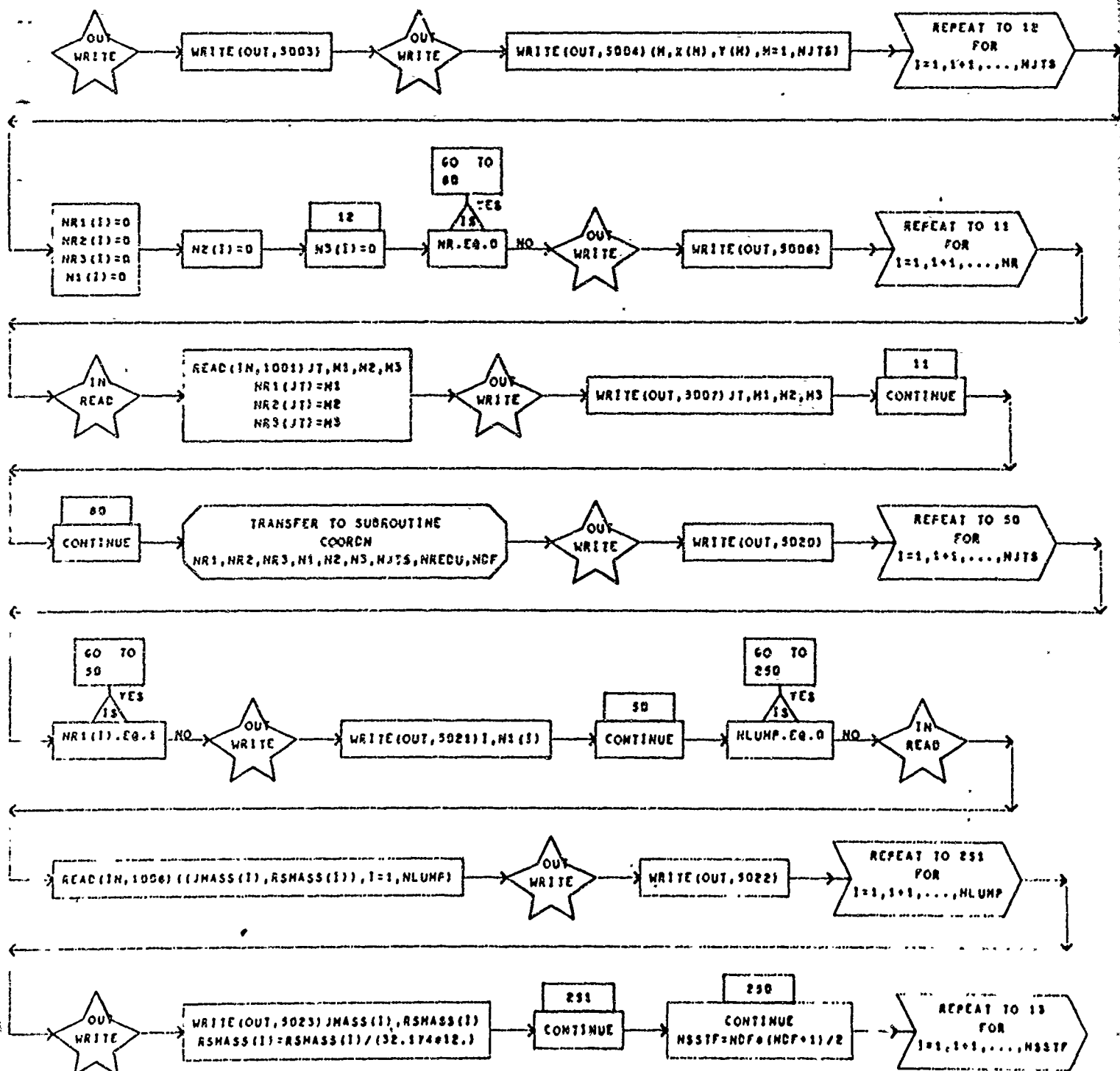
Program FLUENC FLOW CHART

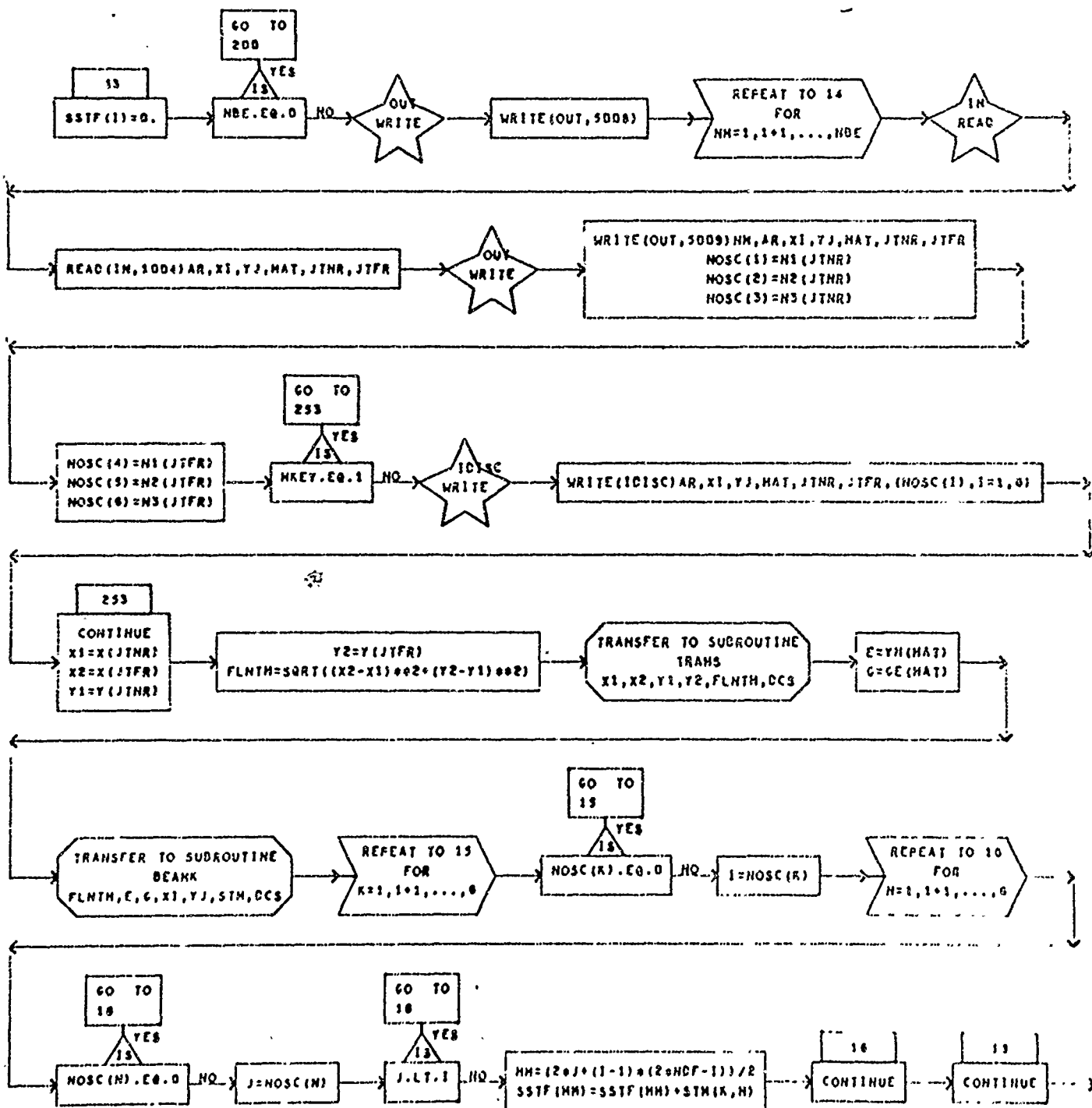
MAIN PROGRAM FLUENC-FOR GENERATING STIFFNESS,FLEXIBILITY AND MASS
MATRICES FROM PLANE GRID BEAM AND TRIANG. PLATE ELEMENTS

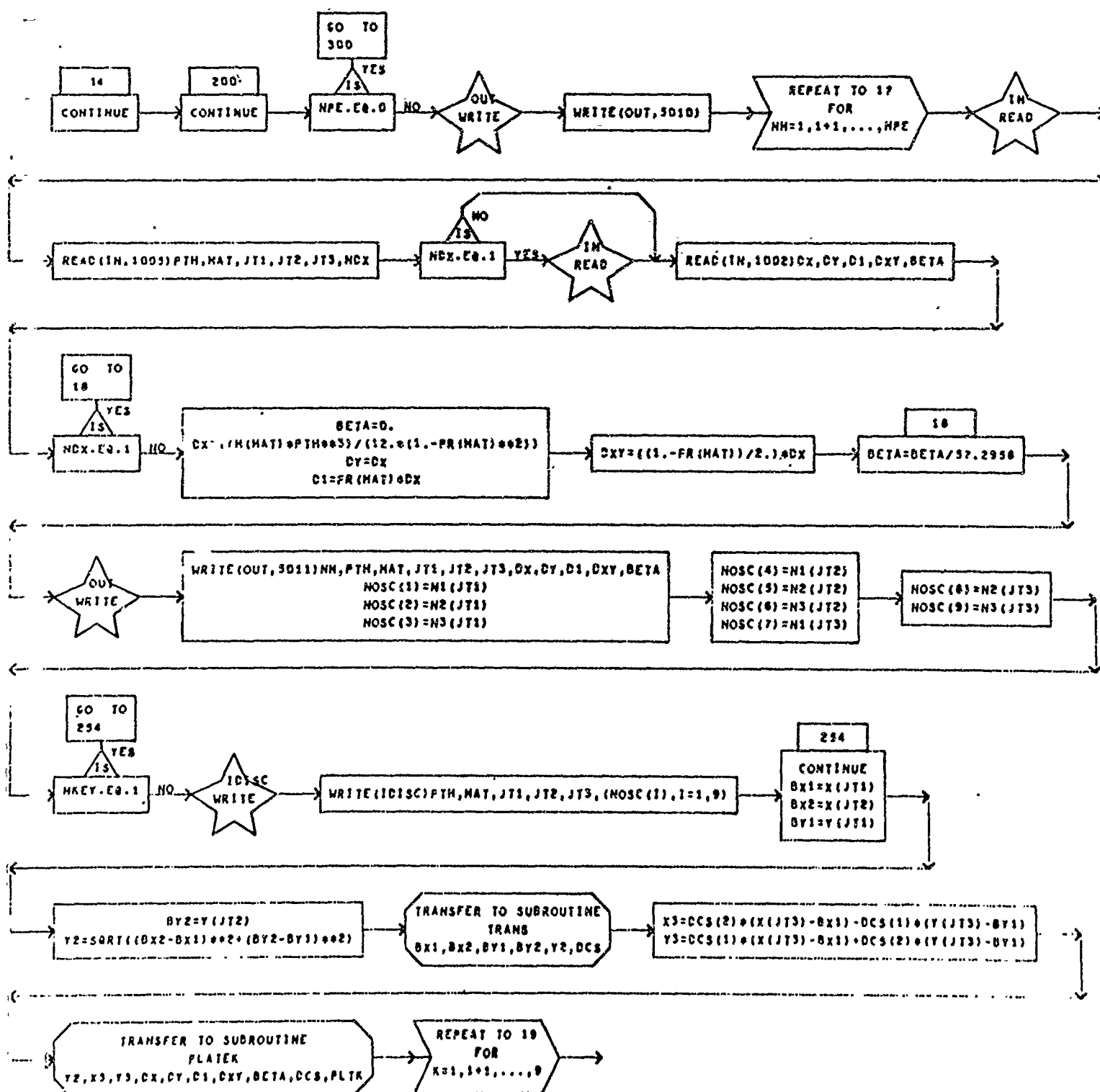
D I M E N S I O N E D V A R I A B L E S

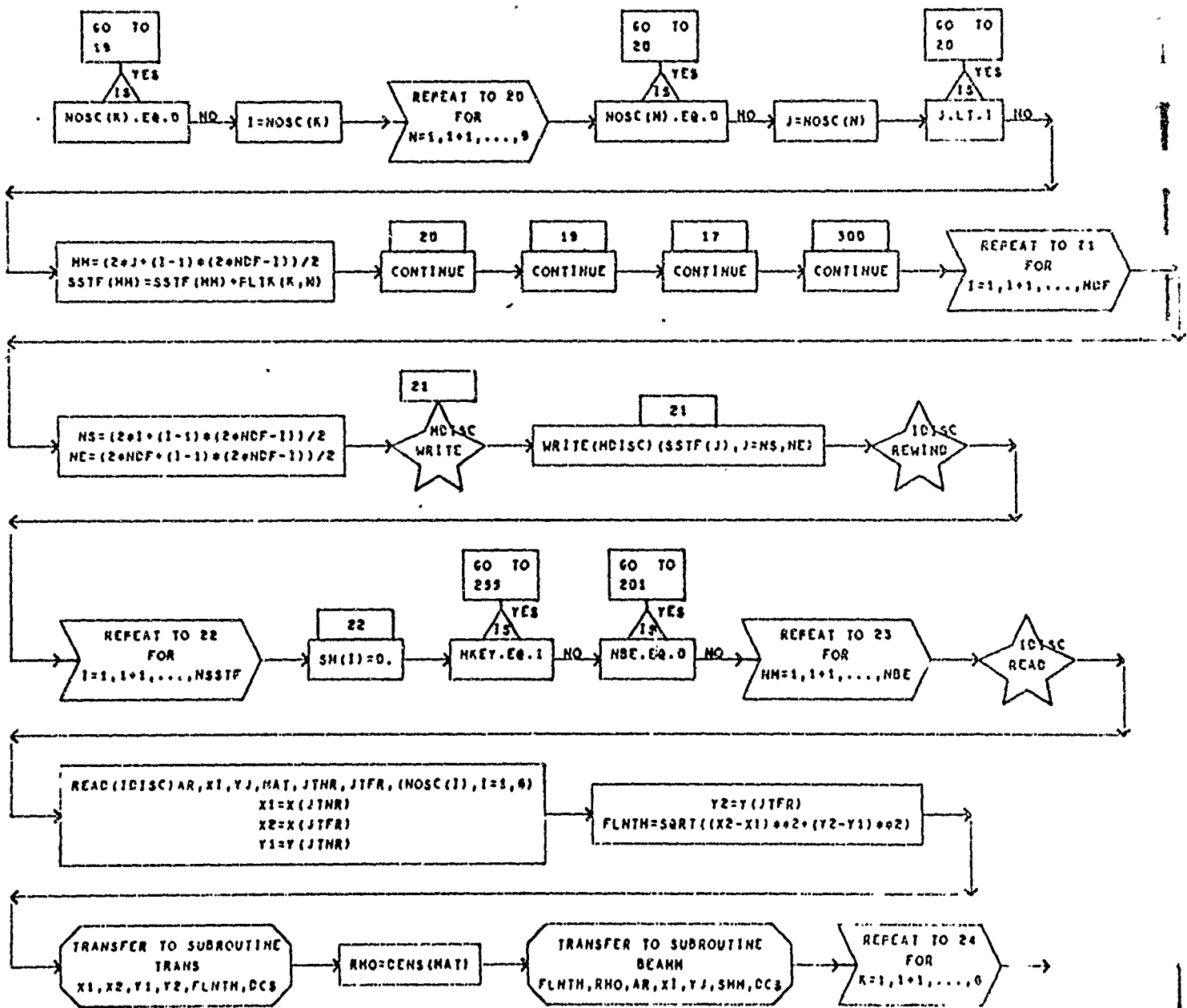
SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
TITLE	24	YM	10	PR	10	GE	10	DENS	10
X	50	T	50	NR1	50	NR2	50	NR3	50
M1	50	NR	50	N3	50	NOBC	9	CCS	2
STM	6,6	SMH	6,6	PLTK	9,9	PLYH	9,9	ESTF	11325
SH	11325	RSHASS	50,A(1	25),VA	LU(9	TEMP	50	B	150
C	100	CUM3	150	F	150,3	ICUM4	50	JMASS	50

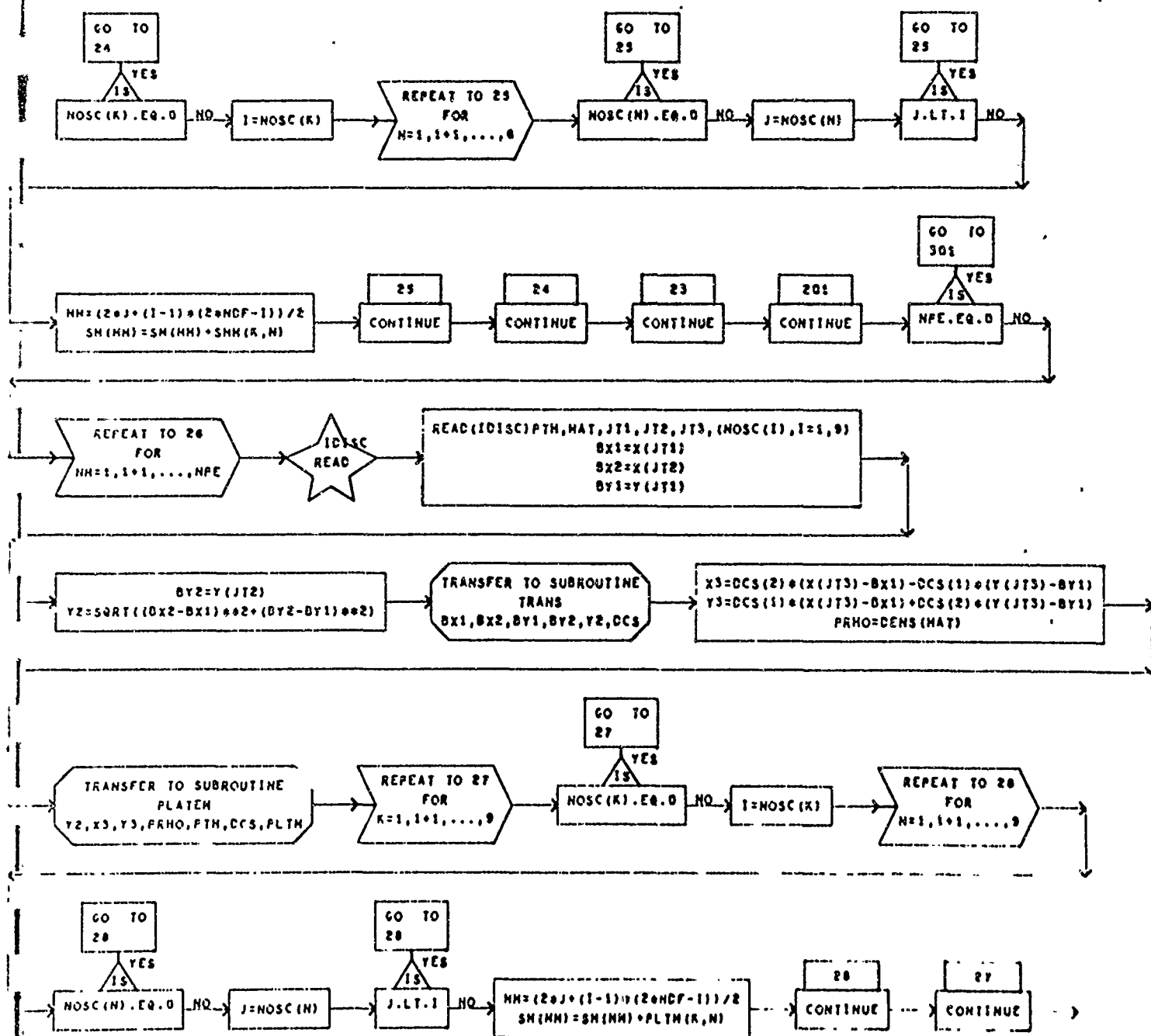






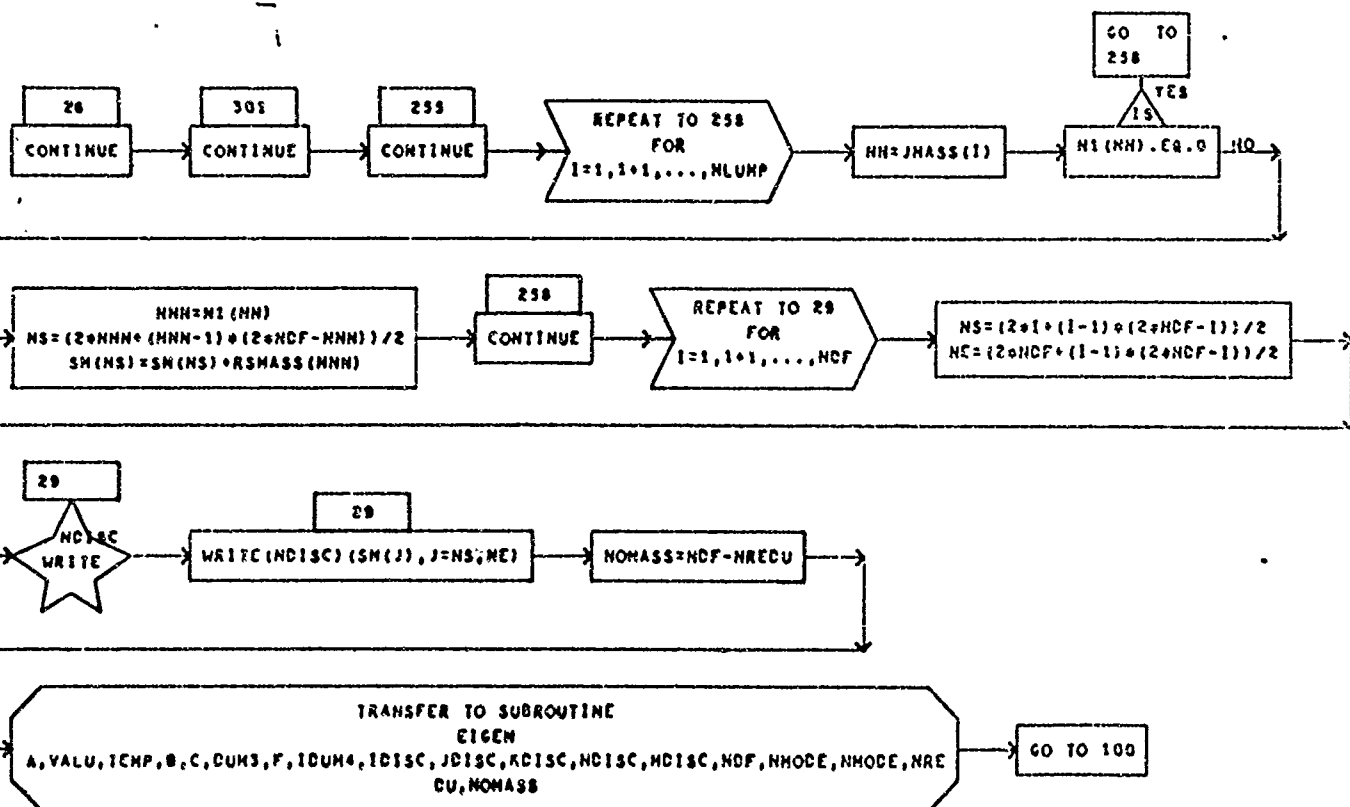






MAIN PROGRAM

PAGE



BEAMK PLANE GRID BEAM ELEMENT STIFFNESS MATI X IN SYSTEM COORDS.

FL = BEAM LENGTH

E = YOUNG'S MODULUS

G = MODULUS OF RIGIDITY

XI = AREA MOMENT OF INERTIA

YJ = EFFECTIVE TORSIONAL MOMENT OF INERTIA

STM = STIFFNESS MATRIX

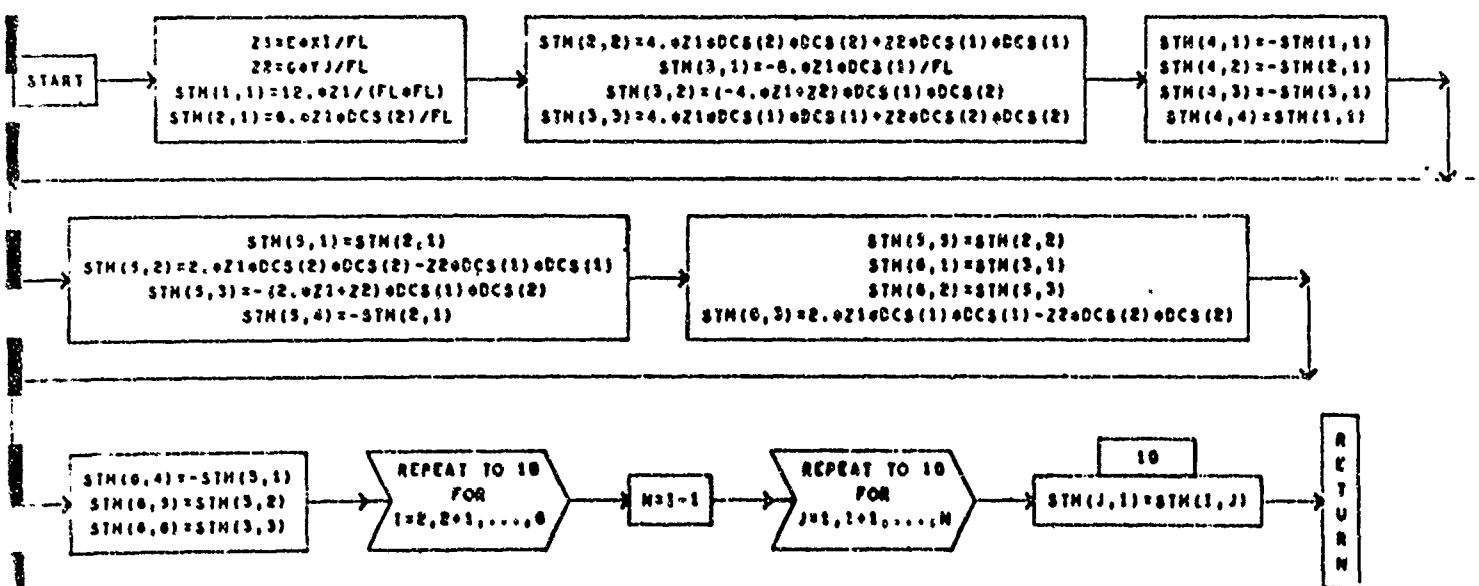
DCS = DIRECTION COSINES

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
STM	6, 6	DCS	2						

SUBROUTINE BEAMK (FL, E, G, XI, YJ, STM, DCS)

PAGE 1



CIMNTH

THIS SUBROUTINE DETERMINES THE DOUBLE INTEGRAL MATRIX FOR
THE TRIANGULAR PLATE M MATRIX - FRZEMIENTECKI, PAGE 304

Y2,X3,Y3 = COORDS. OF PLATE CORNERS IN LOCAL COORDINATES

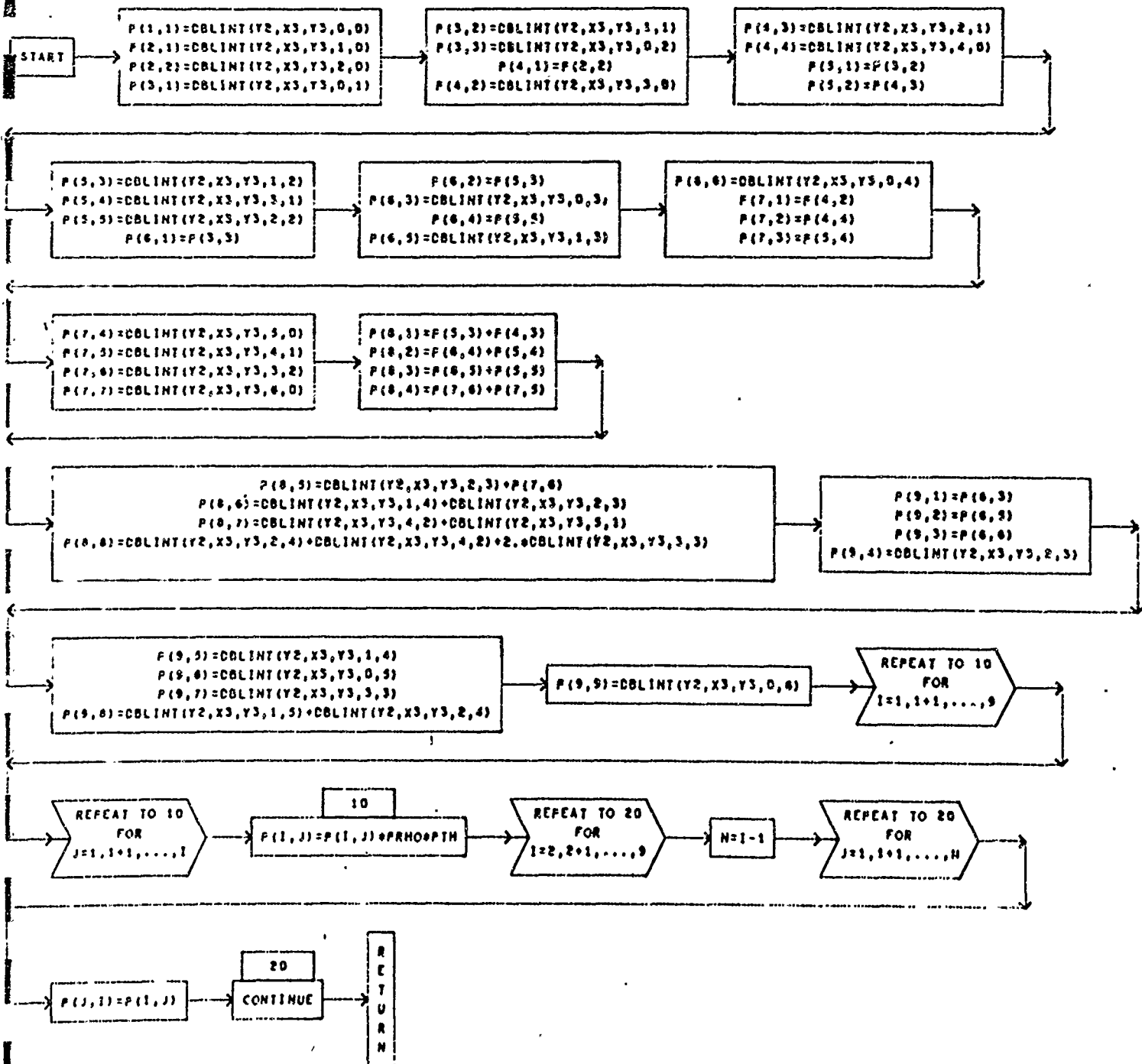
PRHO = DENSITY

PTH = PLATE THICKNESS

P = DOUBLE INTEGRAL MATRIX

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGE
P	9,9								



MINV MATRIX INVERSION SUBROUTINE

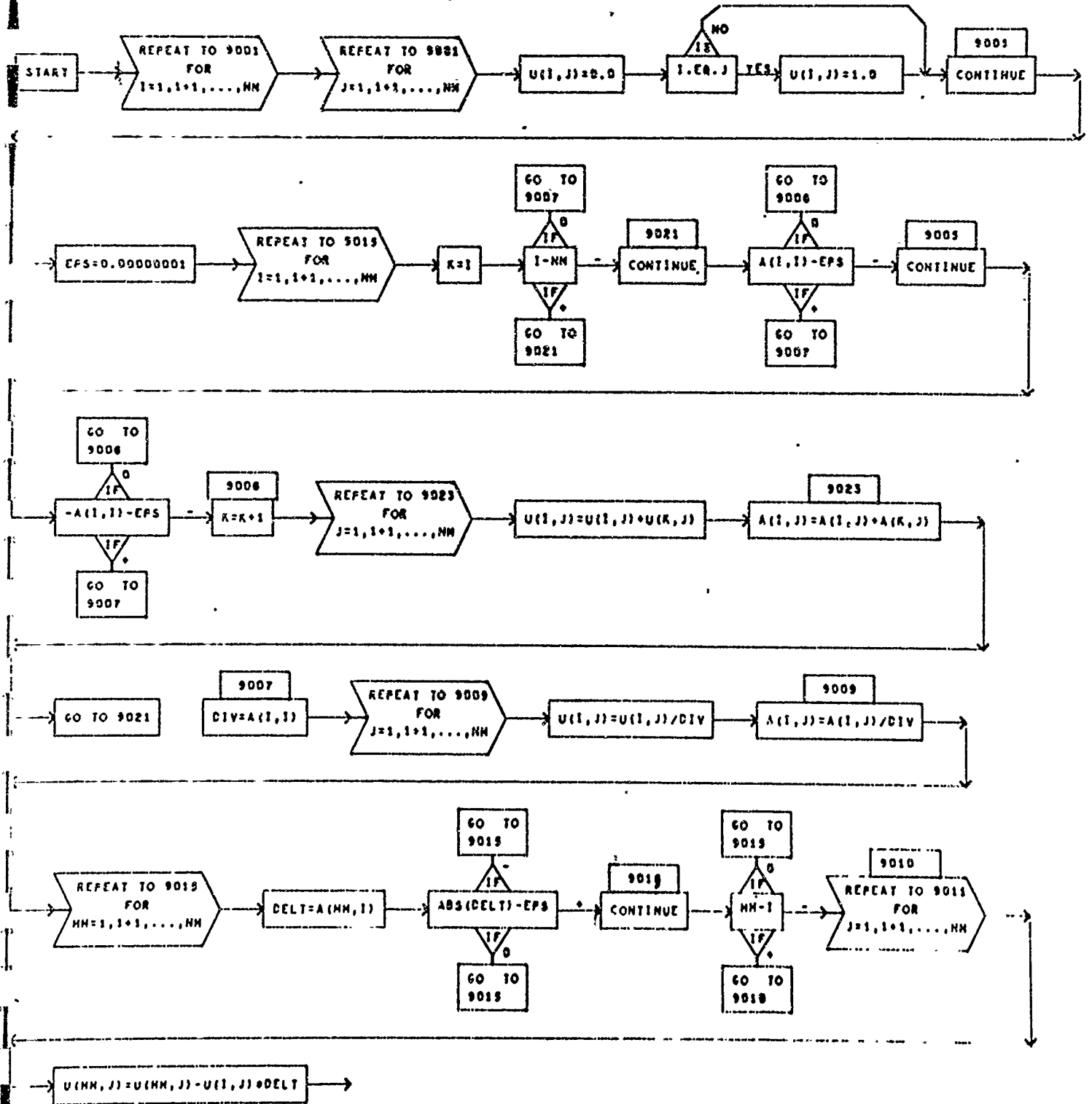
A = MATRIX TO BE INVERTED

U = INVERTED MATRIX

NN = ORDER OF MATRIX (I.E. 9)

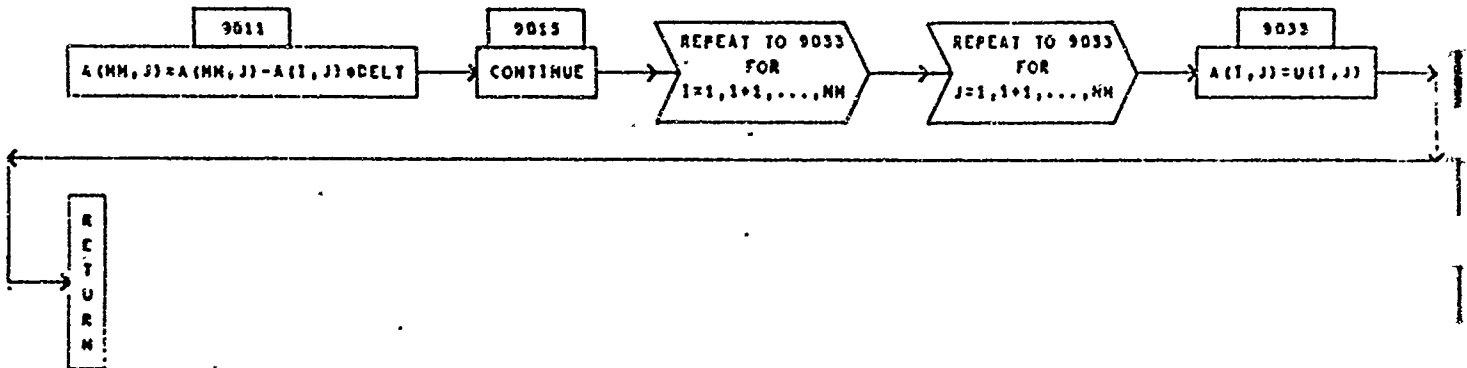
D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
A	9,9	U	9,9						



SUBROUTINE MINV(A,U,NM)

PAGE



EIGEN REDUCES STIFFNESS MATRIX AND INVERTS IT, REDUCES MASS MATRIX
 DETERMINES EIGENVALUES AND EIGENVECTORS

THE ARGUMENTS ARE:

A - VECTOR OF LENGTH $NRDF \cdot (NRDF + 1) / 2$

VALU - VECTOR OF LENGTH NEIG

TEMP, B, C, DUNS, - VECTORS OF LENGTH NRDF OR NMASS (WHATEVER)

E - MATRIX OF DIMENSION (NRDF, 3)

IDUM4 - VECTOR OF LENGTH NRDF OR NMASS (WHATEVER)

ITAPE, JTAPE, HTAPE, MTAPE, - THESE ARE VARIOUS TAPES

NRDF - NUMBER OF DEGREES OF FREEDOM OF THE SYSTEM

NEIG - NUMBER OF EIGENVALUES DESIRED

NVEC - NUMBER OF EIGENVECTORS DESIRED

NMASS=NO. OF NORMAL DISPLACEMENTS

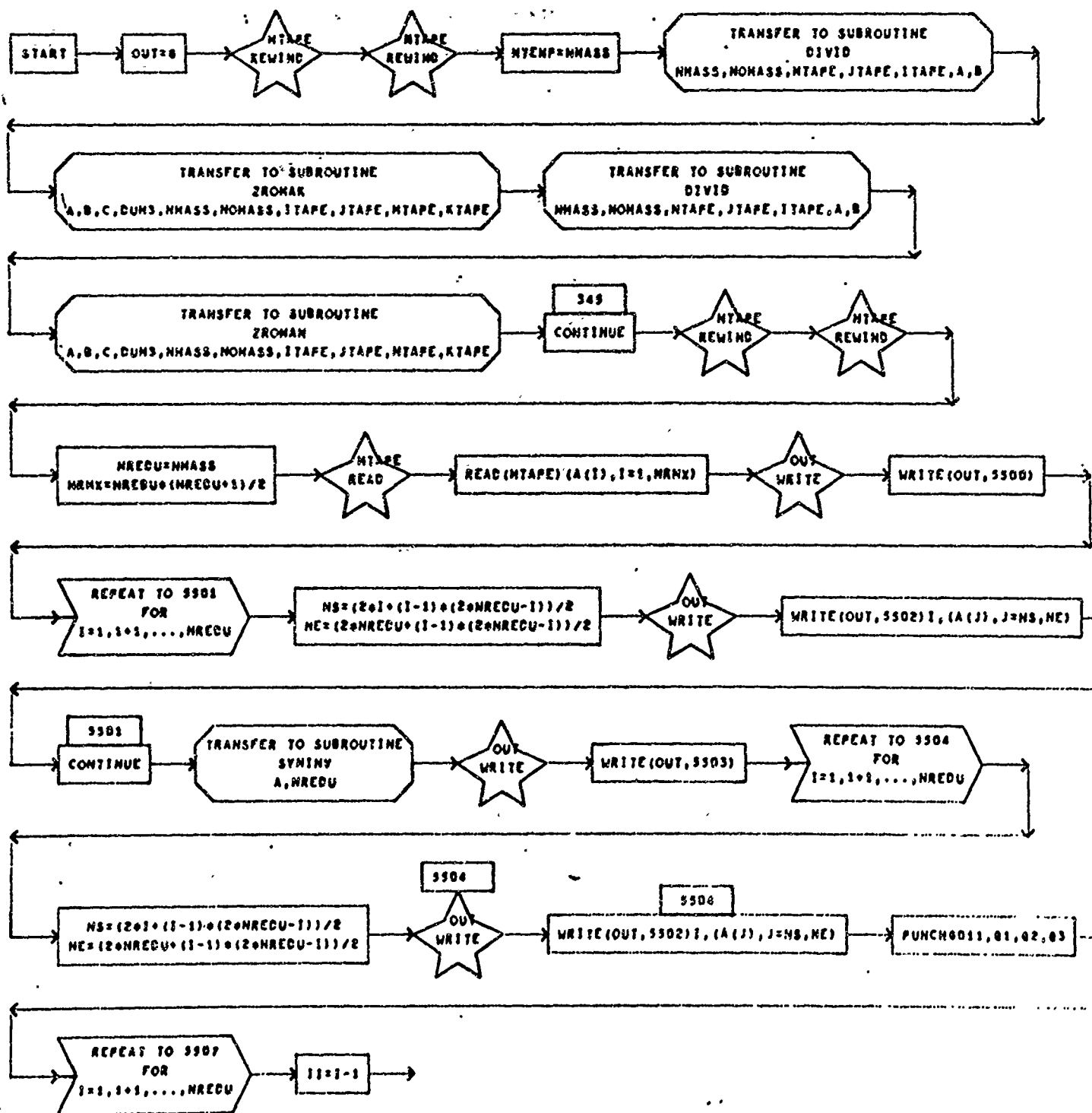
NOHASS=NO. OF ROTATIONAL DEGREES OF FREEDOM

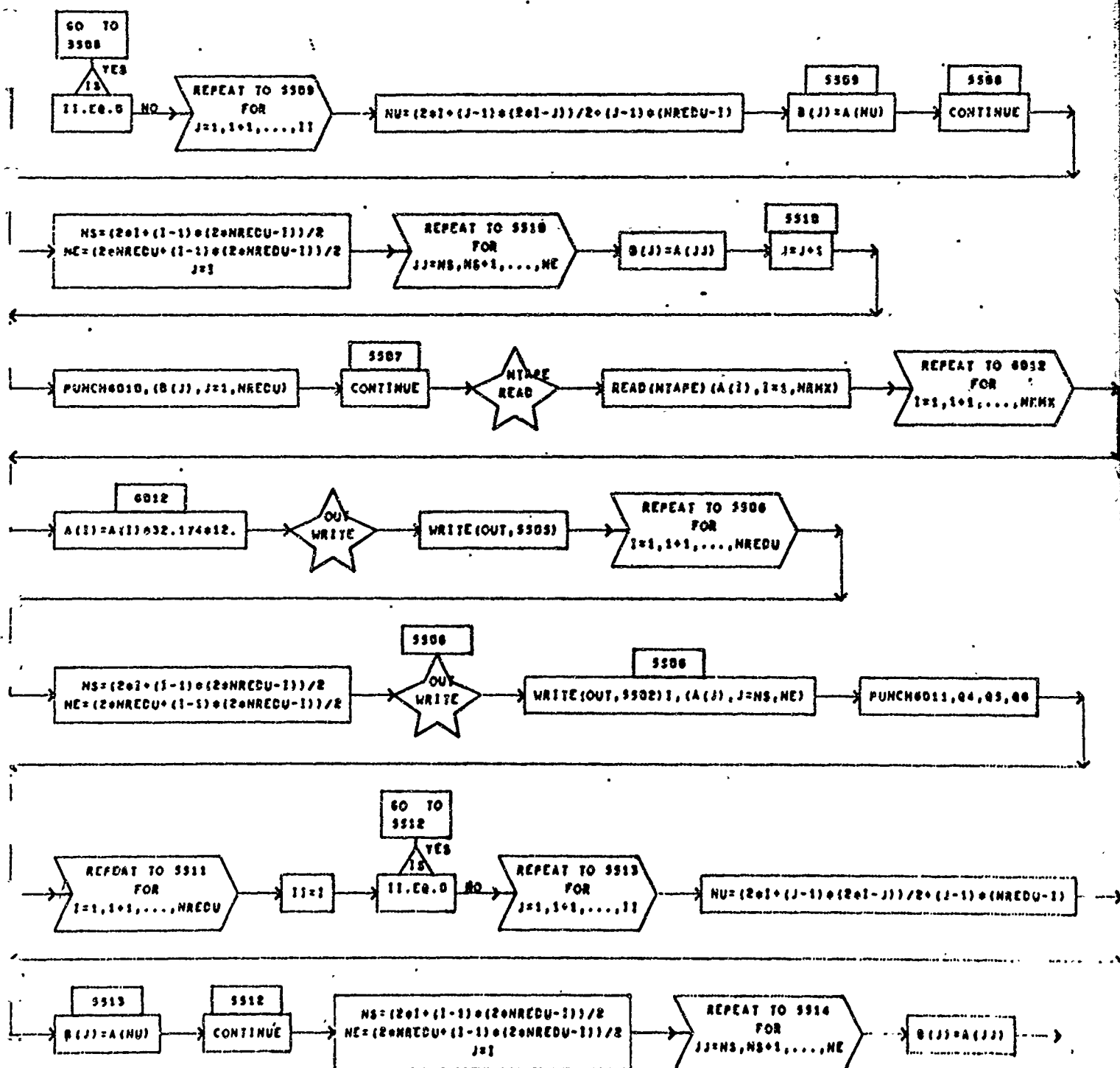
STIFF IS ON HTAPE IN COMPACT FORM

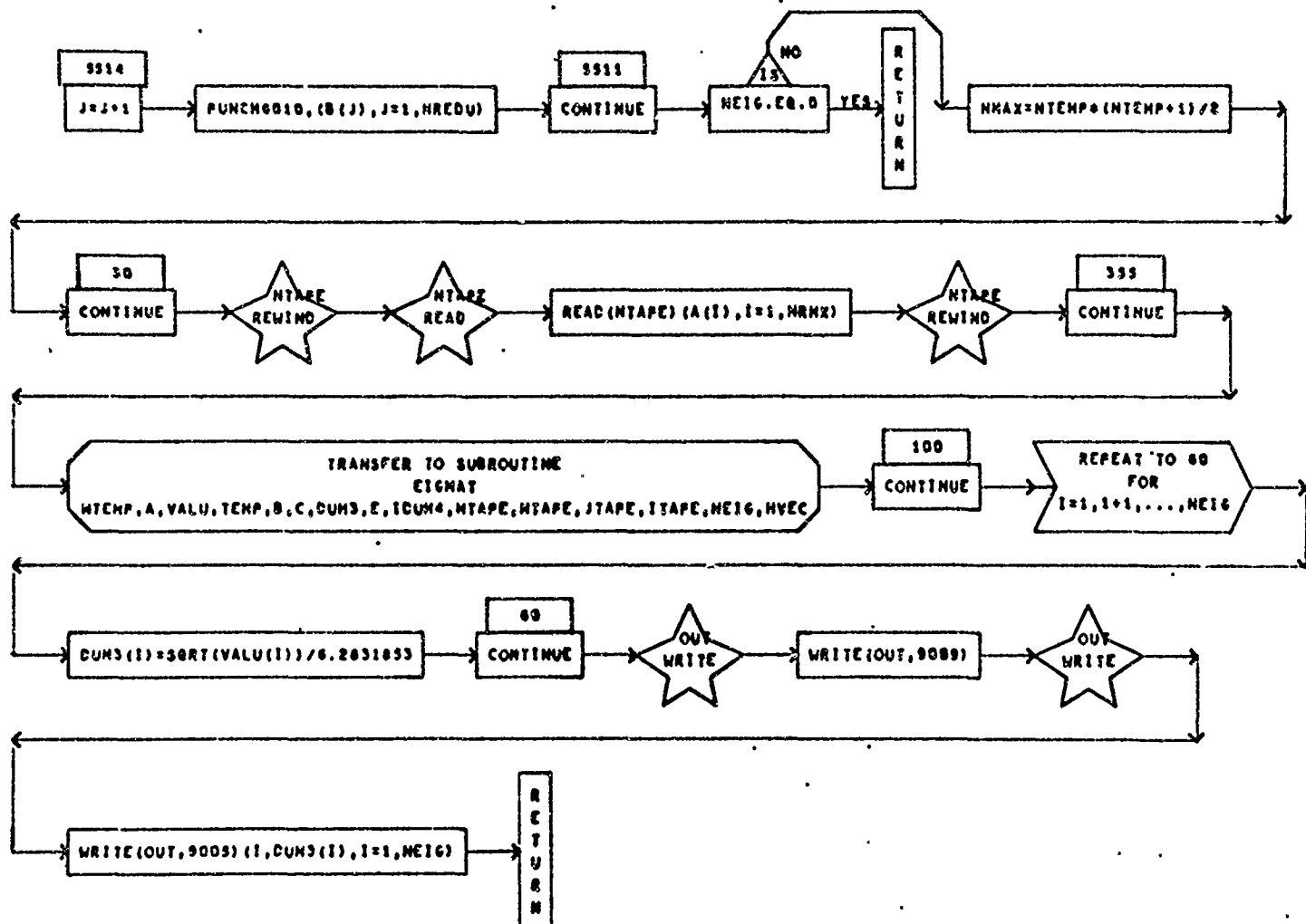
MASS IS ON MTAPE IN COMPACT FORM

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
DUNS	NRDF	IDUM4	1	A	1	VALU	1	B	1
C	1	E	NRDF, 3	TEMP	1				







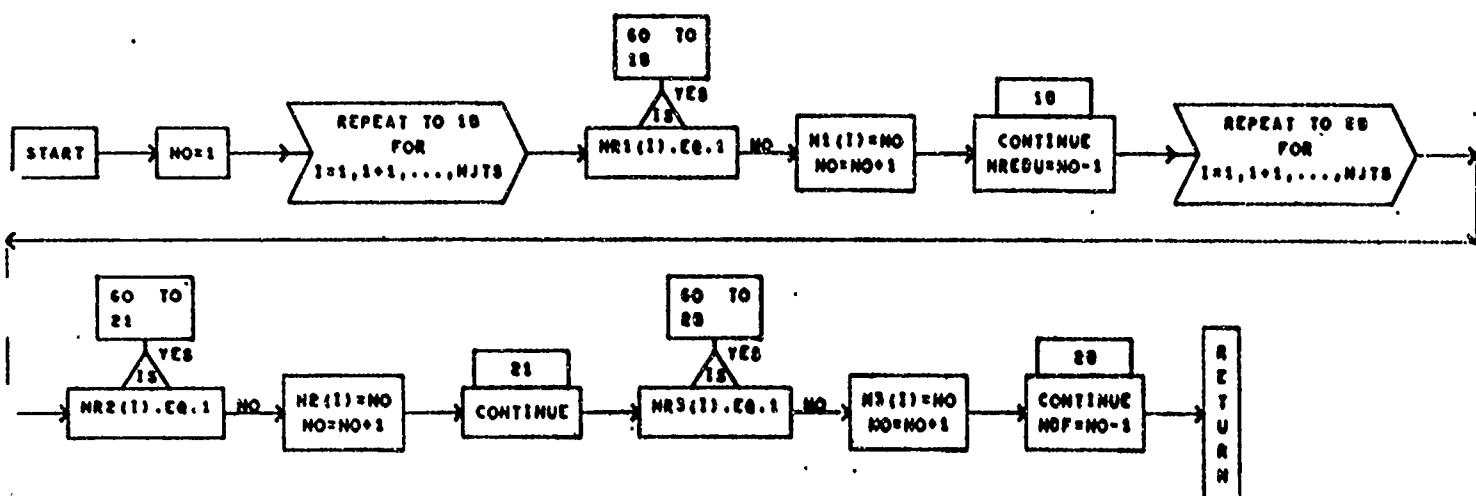
COORDM ASSIGNS A COORD. NO. TO EACH DEGREE OF FREEDOM AT EACH JOINT
 NR1,NR2,NR3 = ARRAYS CONTAINING RESTRAINT INFO. FOR EACH DEGREE
 OF FREEDOM AT EACH JOINT (FREE=0, CLAMPED=1)
 N1,N2,N3 = COORD. NO. FOR EACH DEGREE OF FREEDOM (NORMAL
 DISPLACEMENTS ARE NUMBERED FIRST)
 NJTS = NO. OF JOINTS
 NREBU = NO. OF NORMAL DISPLACEMENTS
 NDF = TOTAL NO. OF DEGREES OF FREEDOM (INCLUDING ROTATIONS)

S I M U L A T I O N S V A R I A B L E S

SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE
NR1	SB	NR2	SB	NR3	SB	N1	SB	N2	SB
N3	SB								

SUBROUTINE COORDM(NR1,NR2,NR3,N1,N2,N3,NJTS,NREBU,NDF)

PAGE 1



06LINE

THIS SUBROUTINE EVALUATES THE DOUBLE INTEGRALS APPEARING IN THE
 EQUATIONS FOR κ AND μ FOR THE TRIANGULAR PLATE ELEMENT
 $x_2, x_3, x_4 =$ COORDS. OF PLATE CORNERS IN LOCAL COORDINATES
 $\mu, \mu =$ POWER OF x AND y RESPECTIVELY, PRZENIENIECKI, PAGE 383

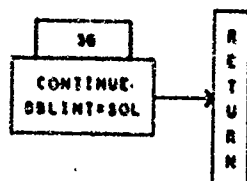
DIMENSIONED VARIABLES

SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE
A1	2	B1	7	P1	7	P2	7	P3	7



FUNCTION DBLINT(Y2,X3,V3,N,N)

PAGE 2



DMAT

THIS SUBROUTINE DETERMINES THE FLEXURAL RIGIDITY MATRIX IN
TRIANGLE LOCAL COORDINATES

DX,DY,D1,DXV,BETA = FLEXURAL RIGIDITY TERMS AND ANGLE OF MATERIAL
PRINCIPAL AXES W/O TRIANGLE LOCAL AXES

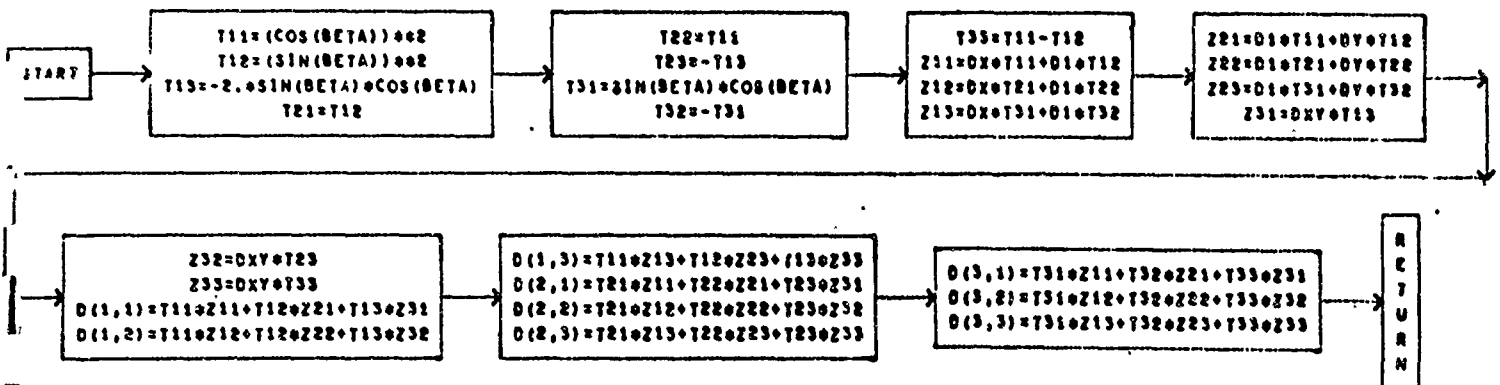
D = FLEXURAL RIGIDITY MATRIX IN TRIANGLE LOCAL COORDS.

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
D	3,3								

SUBROUTINE DMAT(DX,DY,D1,DXV,BETA,D)

PAGE 1



TRANS TRANSFORMATION DIRECTION COSINES

$X1, Y1$ = COORDS. OF POINT 1

$X2, Y2$ = COORDS. OF POINT 2

FL = DISTANCE BETWEEN POINTS 1 AND 2

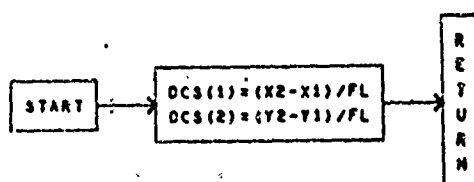
DCS = DIRECTION COSINES OF VECTOR FROM POINT 1 TO POINT 2

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
DCS	2								

SUBROUTINE TRANS(X1,X2,Y1,Y2,FL,DCS)

PAGE 1



DIMMAT

THIS SUBROUTINE DETERMINES THE DOUBLE INTEGRAL MATRIX FOR

THE K EQUATION FOR THE TRIANGULAR PLATE ELEMENT

Y2,X3,Y3 = COORDS. OF PLATE CORNERS IN LOCAL COORDINATES

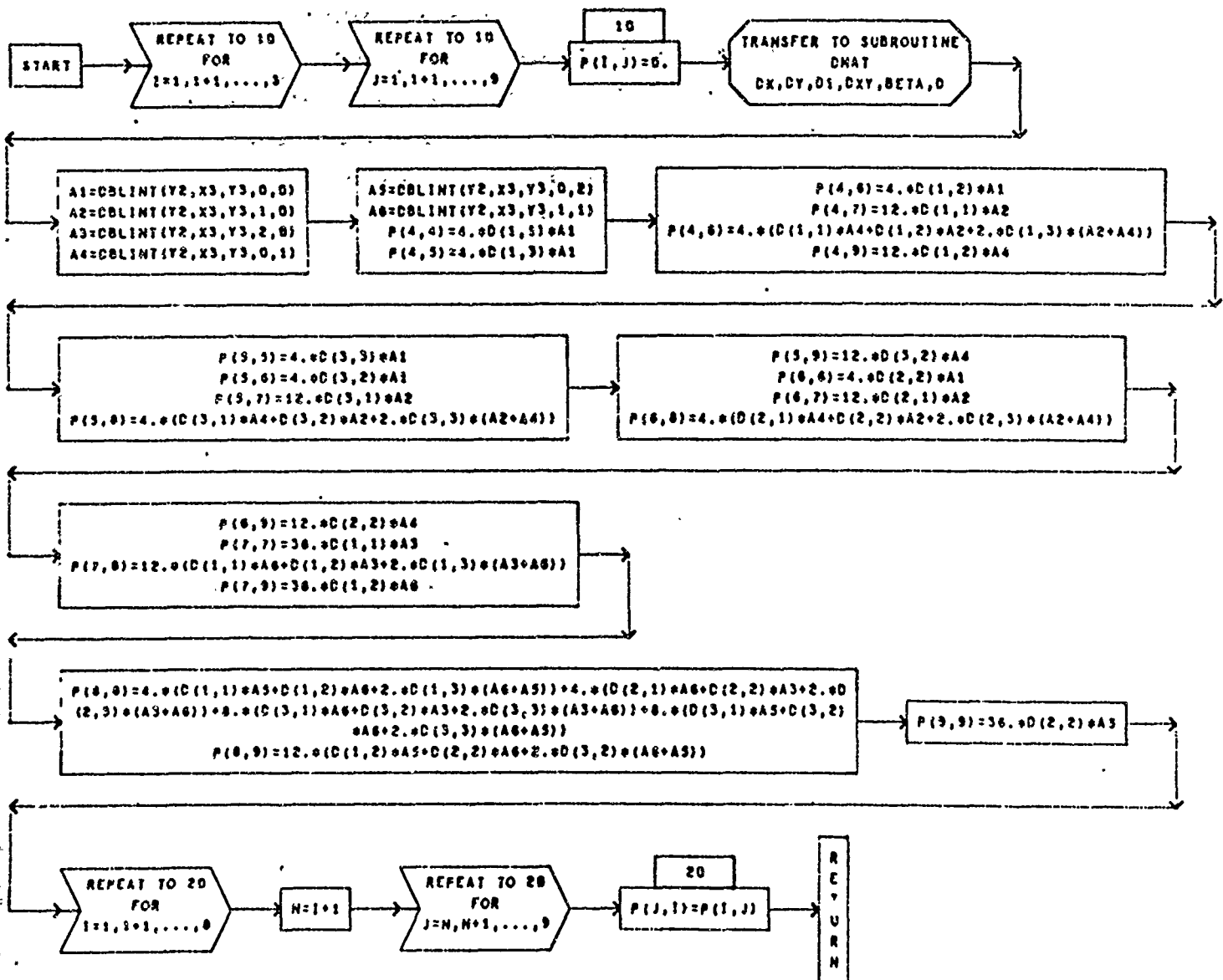
DX,DY,D1,DXY,BETA = FLEXURAL RIGIDITY TERMS AND ANGLE OF MATERIAL

PRINCIPAL AXES W/O TRIANGLE LOCAL AXES

P = DOUBLE INTEGRAL MATRIX

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
P	9,9	D	3,3						



CHAT

THIS SUBROUTINE FORMS THE C MATRIX RELATING THE CORNER
DISPLACEMENTS TO THE POLYNOMIAL DEFLECTION COEFFICIENTS
FOR THE TRIANGULAR PLATE ELEMENT

X2,X3,Y3 = COORDS. OF PLATE CORNERS IN LOCAL COORDINATES

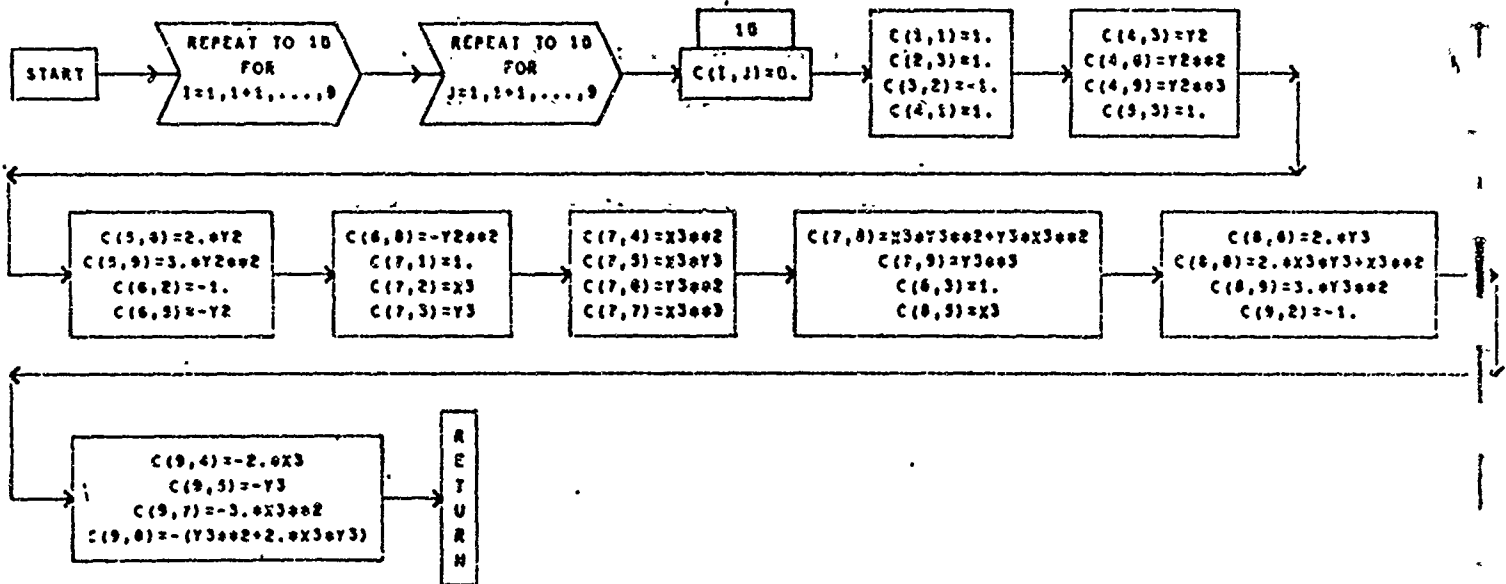
C = C MATRIX

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
C	9,9								

SUBROUTINE CMAT(Y2,X3,Y3,C)

PAGE 1



PLATE

THIS SUBROUTINE DETERMINES THE STIFFNESS MATRIX OF A
TRIANGLE PLATE ELEMENT IN SYSTEM COORDS.

X2,X3,Y3 = COORDS. OF PLATE CORNERS IN LOCAL COORDINATES

DX,DY,DS,CXY,BETA = FLEXURAL RIGIDITY TERMS AND ANGLE OF MATERIAL

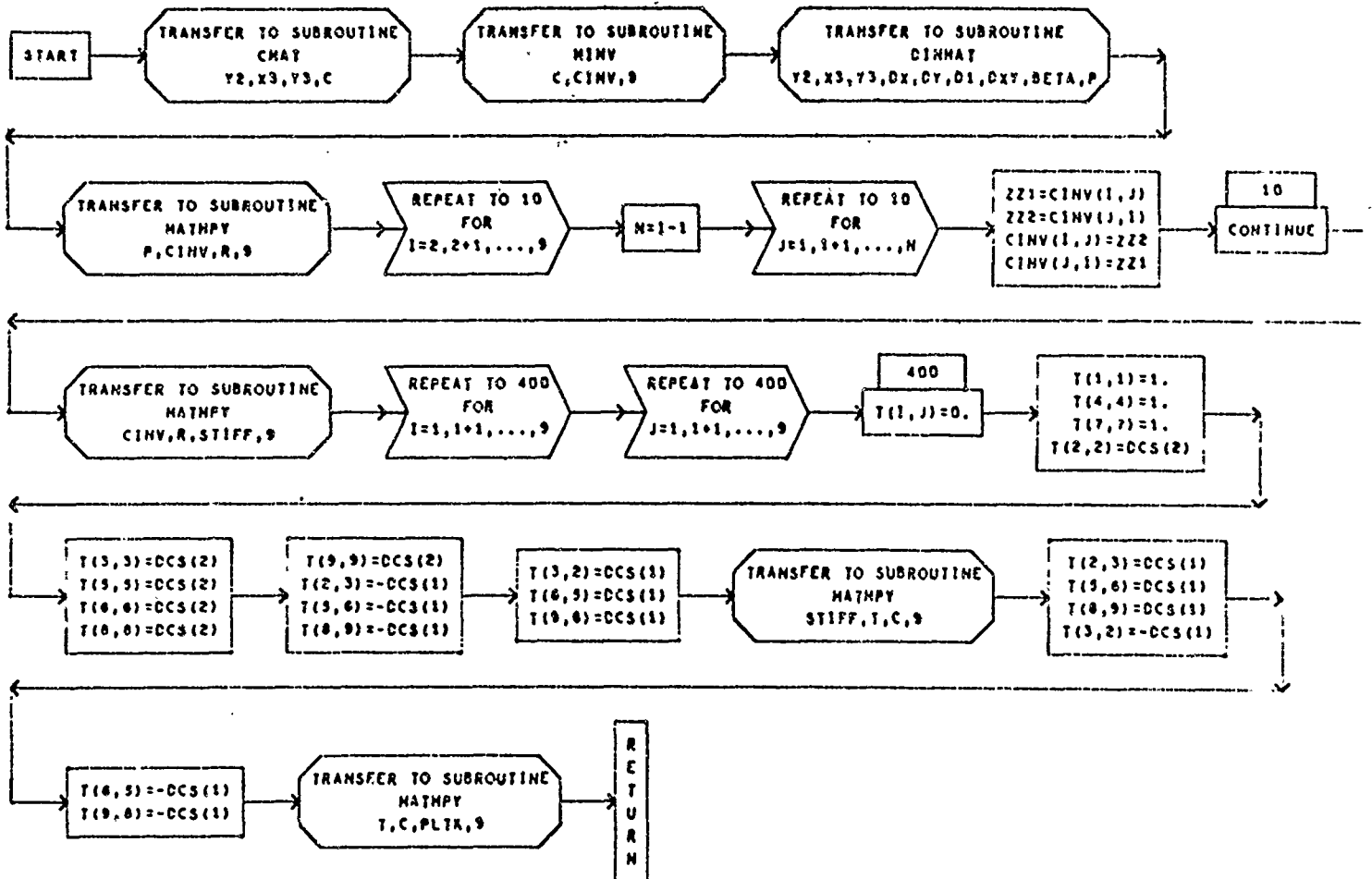
PRINCIPAL AXES W/O TRIANGLE LOCAL AXES

DCS = DIRECTION COSINES

PLTK = STIFFNESS MATRIX

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
PLTK	9,9	C	9,9	CINV	9,9	P	9,9	R	9,9
T	9,9	STIFF	9,9	DCS	2				



PLATEM

THIS SUBROUTINE DETERMINES THE MASS MATRIX OF A
TRIANGLE PLATE ELEMENT IN SYSTEM COORDS.

Y2,X3,Y3 = COORDS. OF PLATE CORNERS IN LOCAL COORDINATES

PRHO = DENSITY

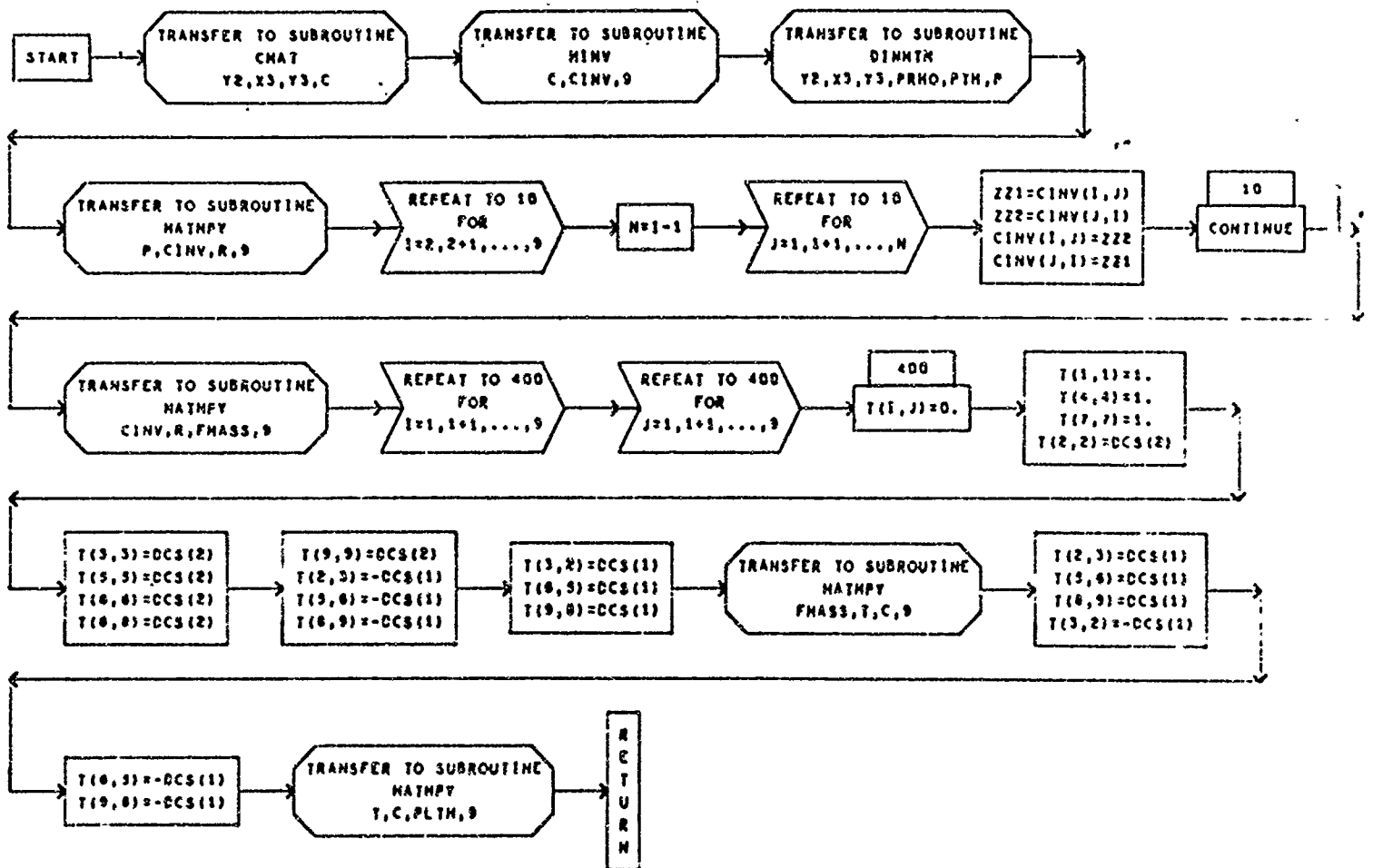
PTH = PLATE THICKNESS

DCS = DIRECTION COSINES

PLTH = MASS MATRIX

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
PLTH	9,9	C	9,9	CINV	9,9	P	9,9	R	9,9
T	9,9	FMASS	9,9	DCS	2				



BEAM PLANE GRID BEAM ELEMENT MASS MATRIX IN SYSTEM COORDS.

FL = BEAM LENGTH

RHO = DENSITY

A = CROSS SECTIONAL AREA

XI = AREA MOMENT OF INERTIA

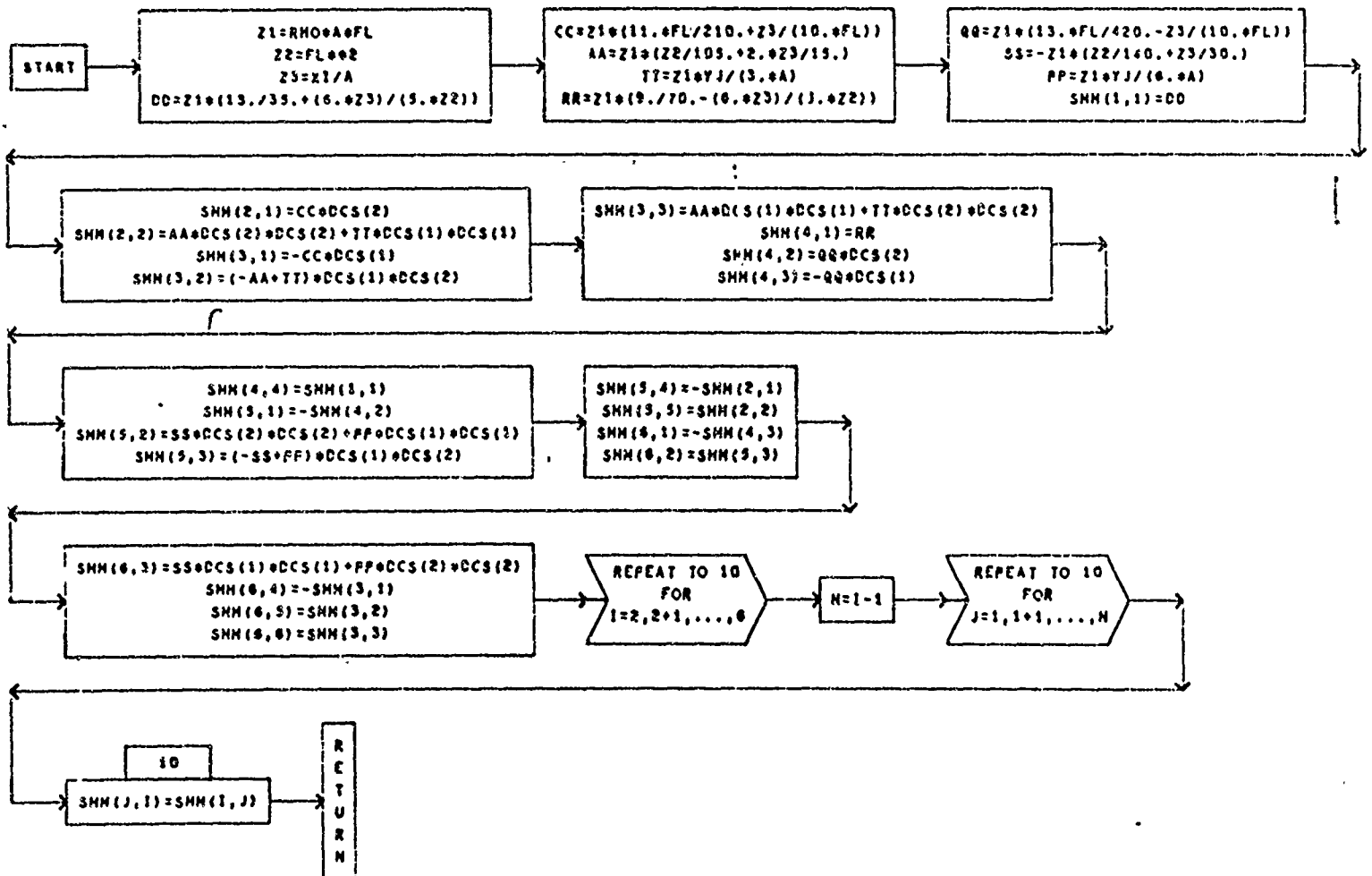
XJ = EFFECTIVE TORSIONAL MOMENT OF INERTIA

SMM = MASS MATRIX

DCS = DIRECTION COSINES

D I M E N S I O N S V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
SMM	9,6	DCS	2						



DIVIS

N=NO. OF NORMAL DISPLACEMENTS

M=NO. OF ROTATIONAL D.O.F.

HTPE-CONTAINS STIFFNESS (OR MASS) MATRIX

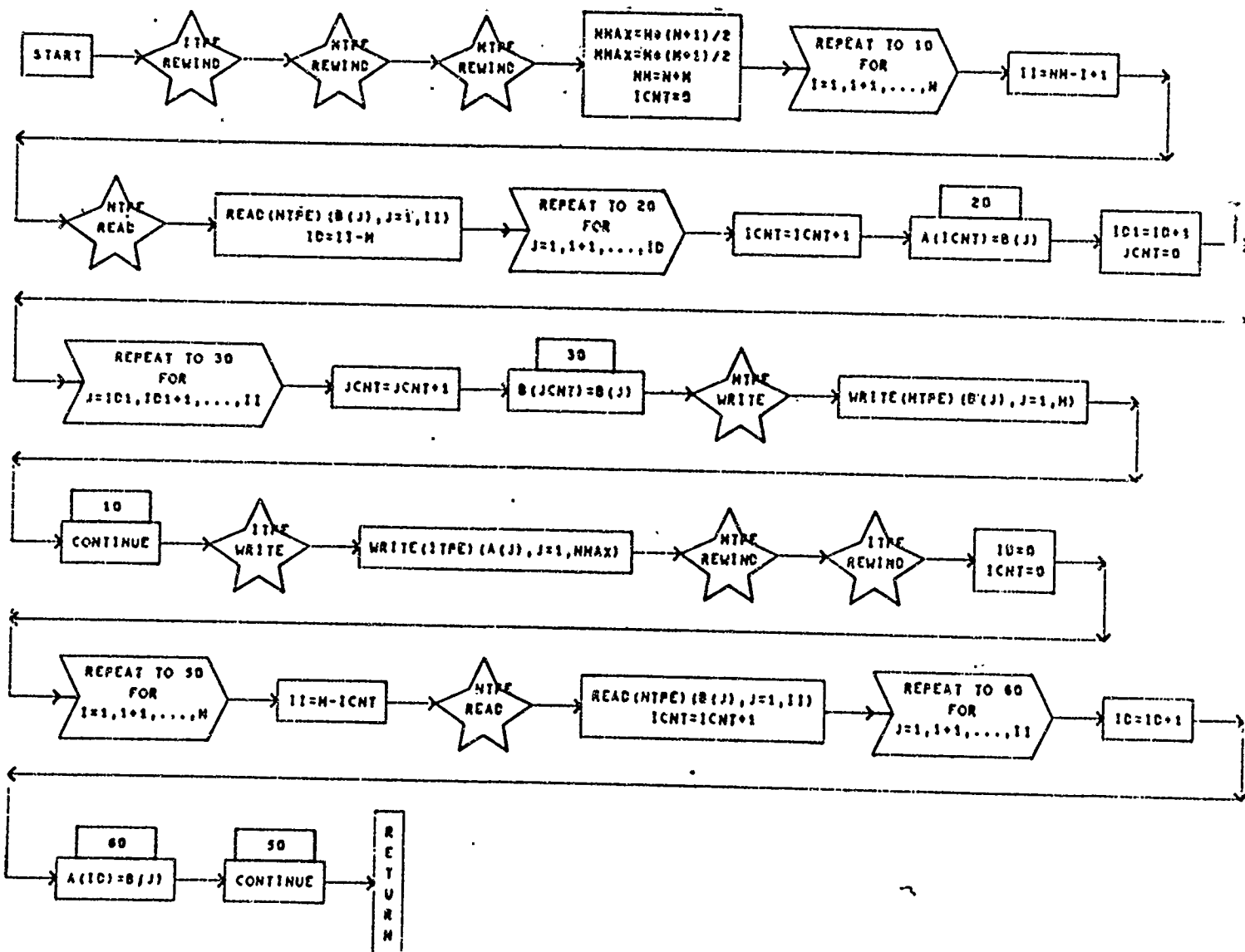
HTPE-K12 (M12) STORED

ITPE-K11 (M11) STORED

A- DUMMY STORAGE VECTOR, LARGER OF $M(M+1)/2$ OR $N(N+1)/2$

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
A	1	B	1						



ZROMAK

B IS A DUMMY VECTOR WITH STORAGE N OR N (LARGER)

A IS A DUMMY VECTOR WITH STORAGE $N(N+1)/2$ OR $N(N+1)/2$ (LARGER)

B IS A DUMMY VECTOR WITH STORAGE N OR N (LARGER)

C IS A DUMMY VECTOR WITH STORAGE N OR N (LARGER)

N=NO. OF NORMAL DISPLACEMENTS

M=NO. OF ROTATIONAL D.O.F.

N1PE CONTAINS K11 MATRIX

N1PE CONTAINS K12 MATRIX

11PE SCRATCH TAPE

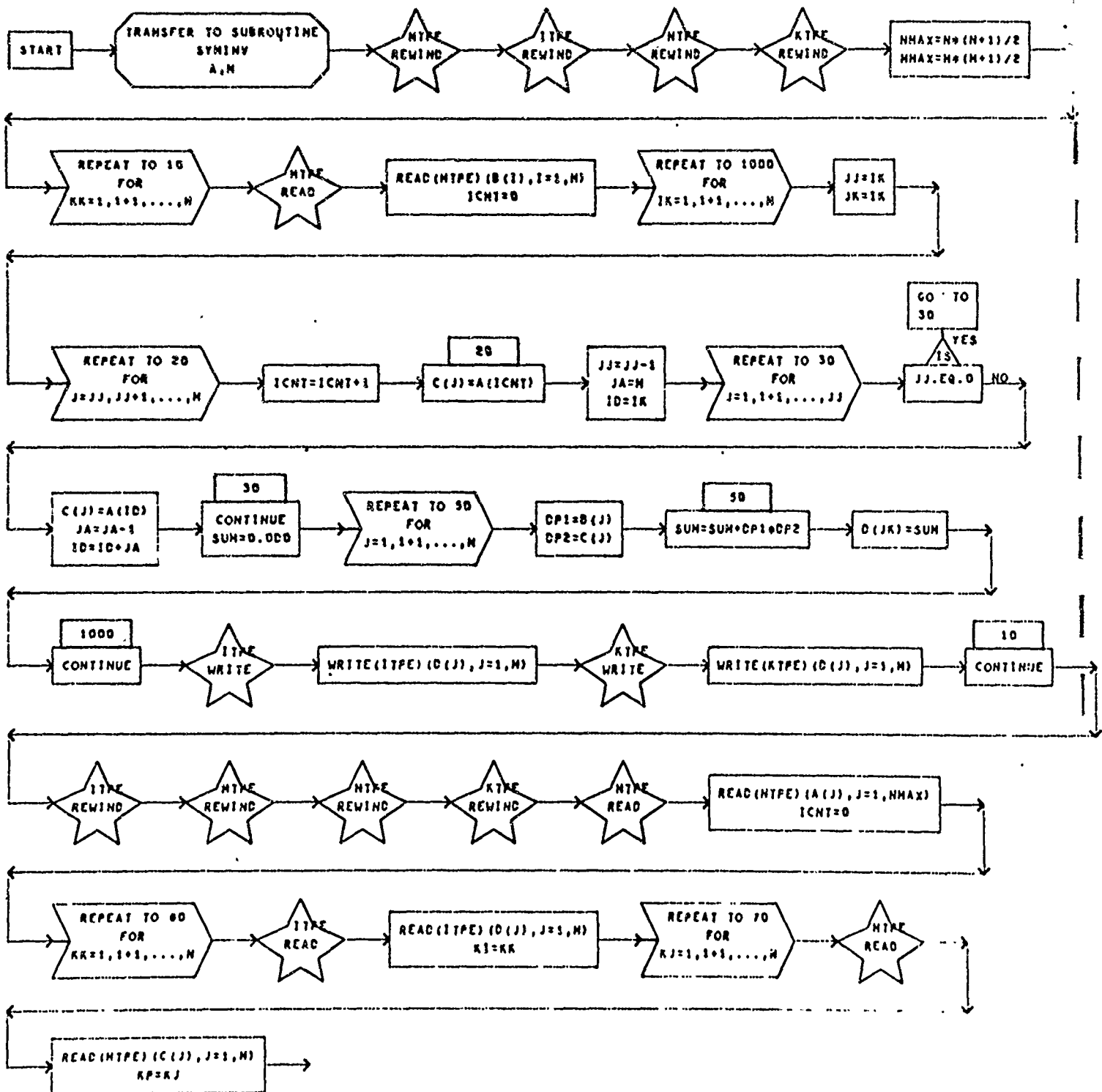
K1PE STORES K12+K22+(-1)

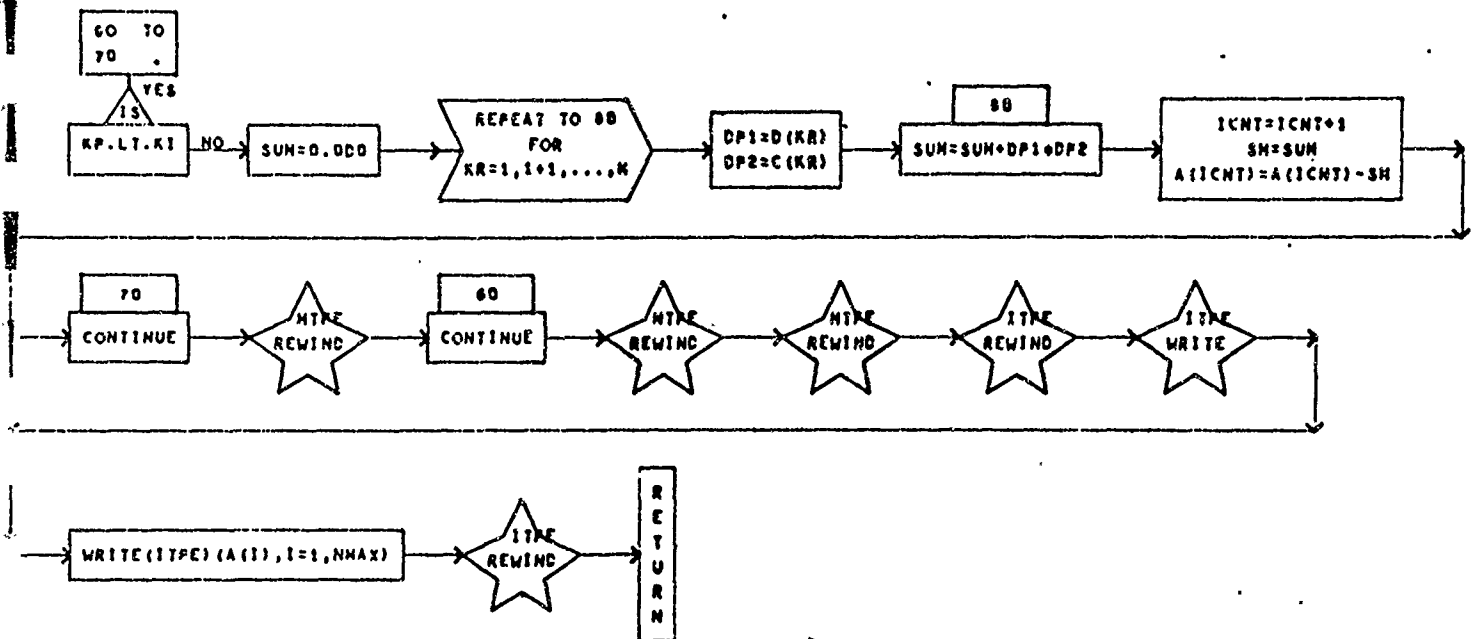
A INITIALLY CONTAINS K22 INVERSE

*** REDUCED STIFFNESS MATRIX IS STORED ON 11PE

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
A	1	B	1	C	1	D	1		





ZROMAN

N=NO. OF NORMAL DISPLACEMENTS

M=NO. OF ROTATIONAL D.O.F.

HTPE CONTAINS H11 MATRIX

HTPE CONTAINS H12 MATRIX

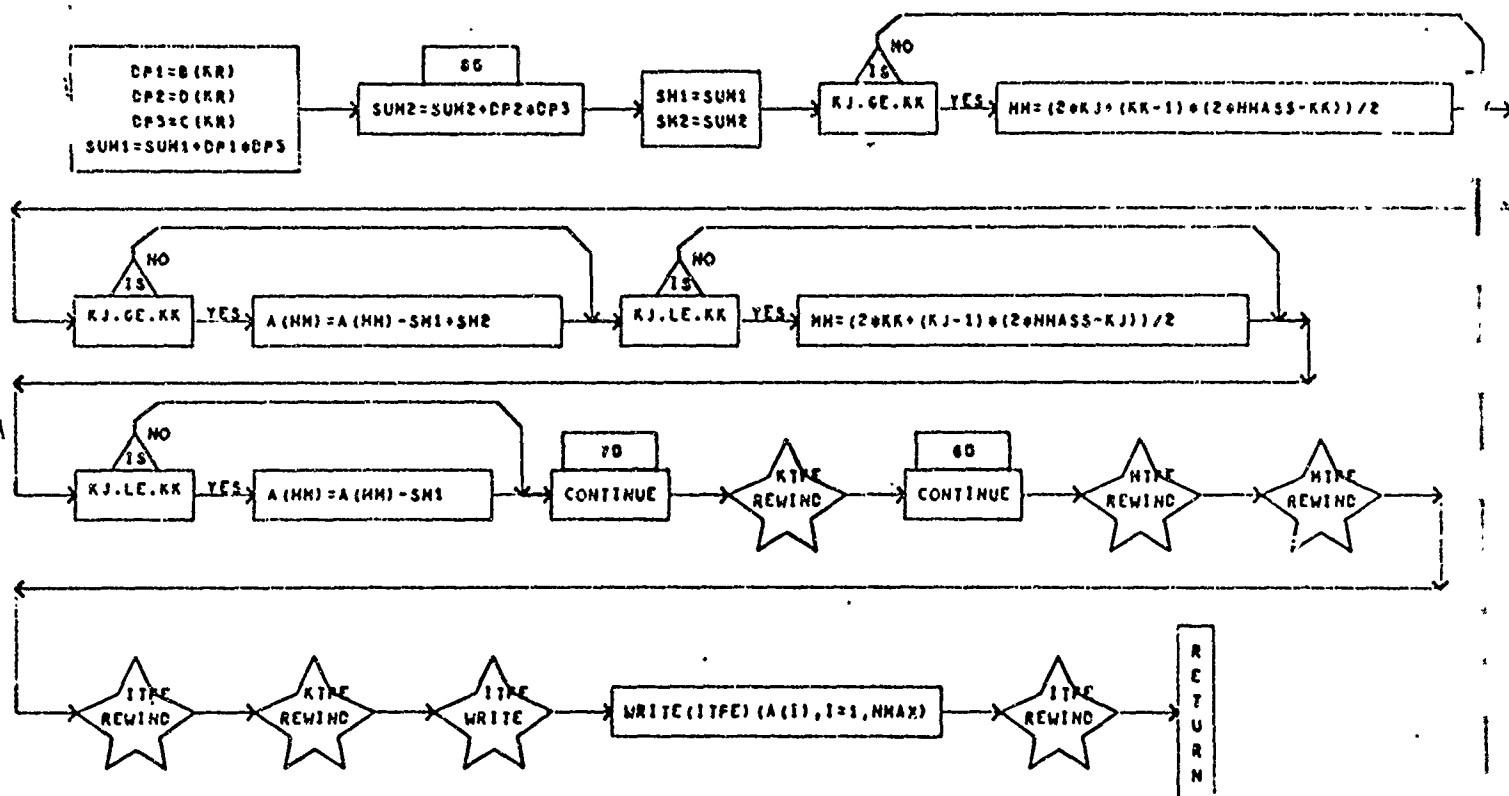
ITPE SCRATCH TAPE

K1PE CONTAINS K12+K22+(-1)

*** REDUCED MASS MATRIX IS STORED ON ITPE

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
A	1	B	1	C	1	D	1		



MAINPY

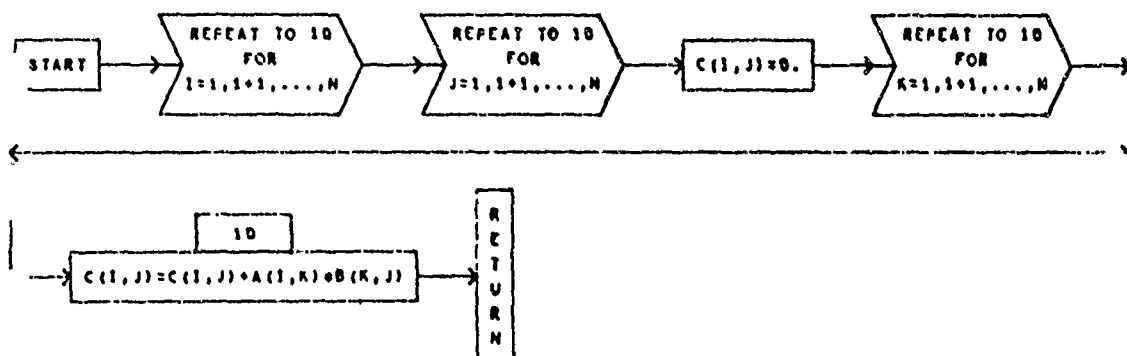
MULTIPLIES MATRICES A AND B TO GET C, ALL OF ORDER N*N

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
A	9,9	B	9,9	C	9,9				

SUBROUTINE MATMPY (A,B,C,N)

PAGE 1.



LOOP1

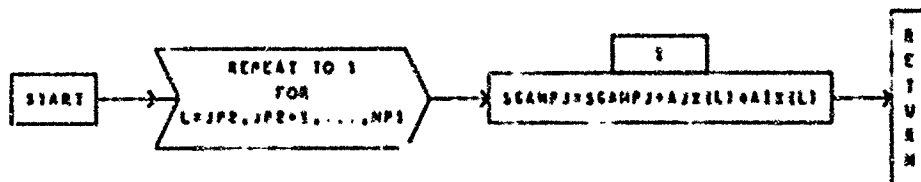
5
1

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE
AIX	1	AIX	1						

SUBROUTINE LOOP1(JPR,NPI,SCAMPJ,AIX,AIX)

PAGE 1



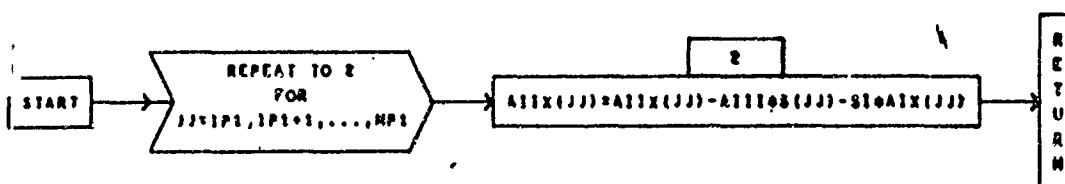
LOOP2

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE
A11X	1	A1X	1	S	1				

SUBROUTINE LOOP2(A11X,A1X,S,S1,A11I,IP1,NP1)

PAGE 1



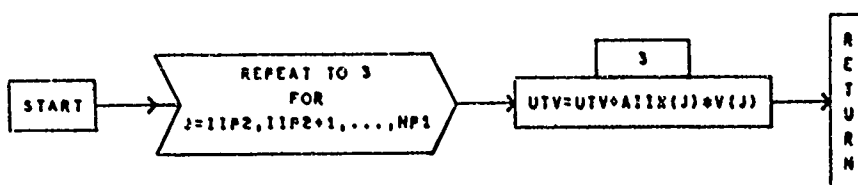
LOOP3

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
AIIX	1	V	1						

SUBROUTINE LOOP3(UTV,AIIX,V,IIP2,NP1)

PAGE 1



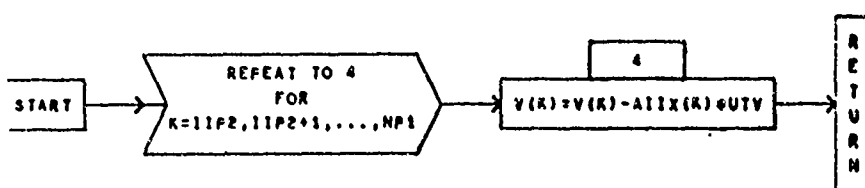
LOOP4

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE	SYMBOL	STORAGE
AIX	1	V	1						

SUBROUTINE LOOP4(AIX,V,NP1,IIP2,UTV)

PAGE 1

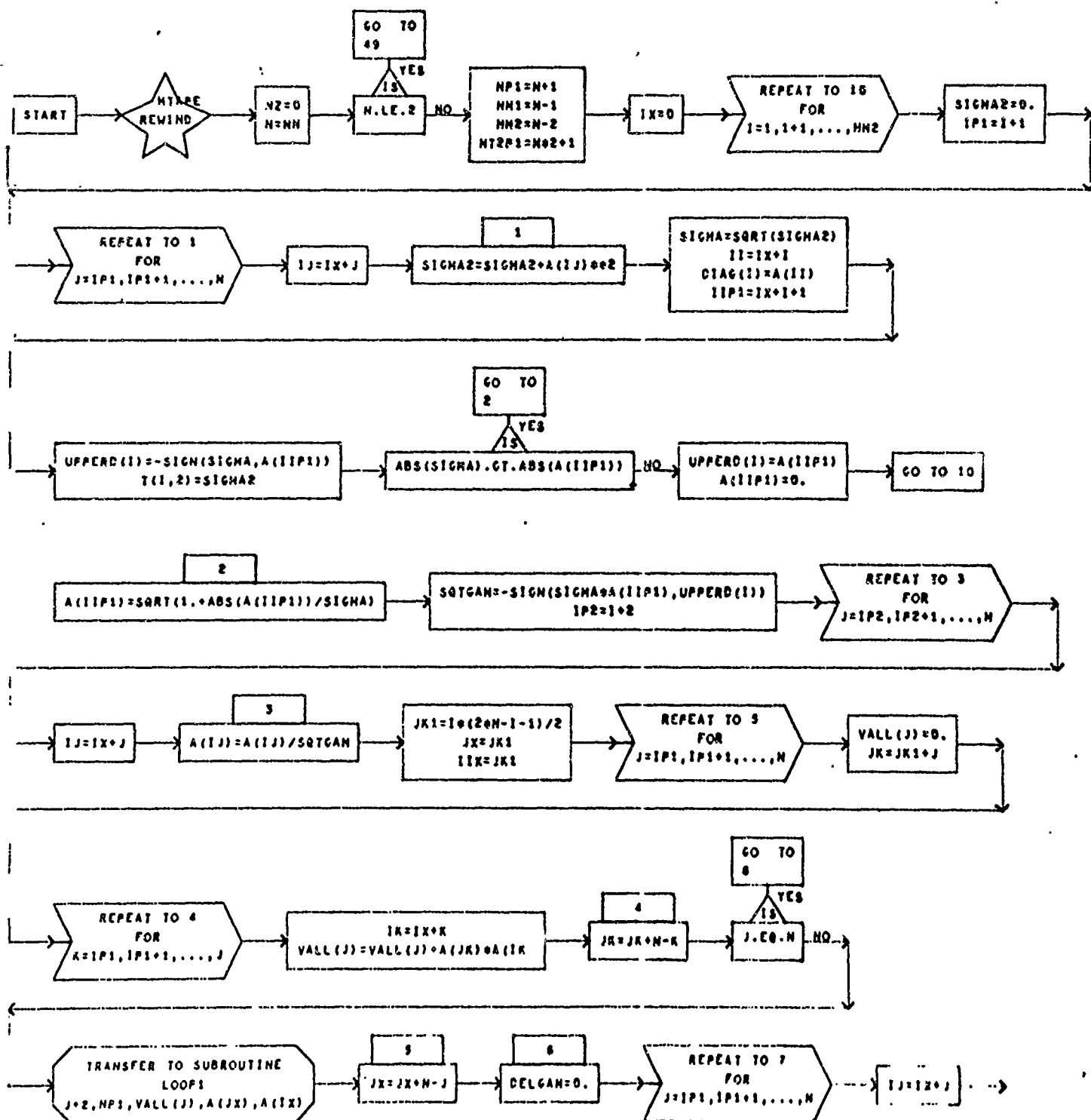


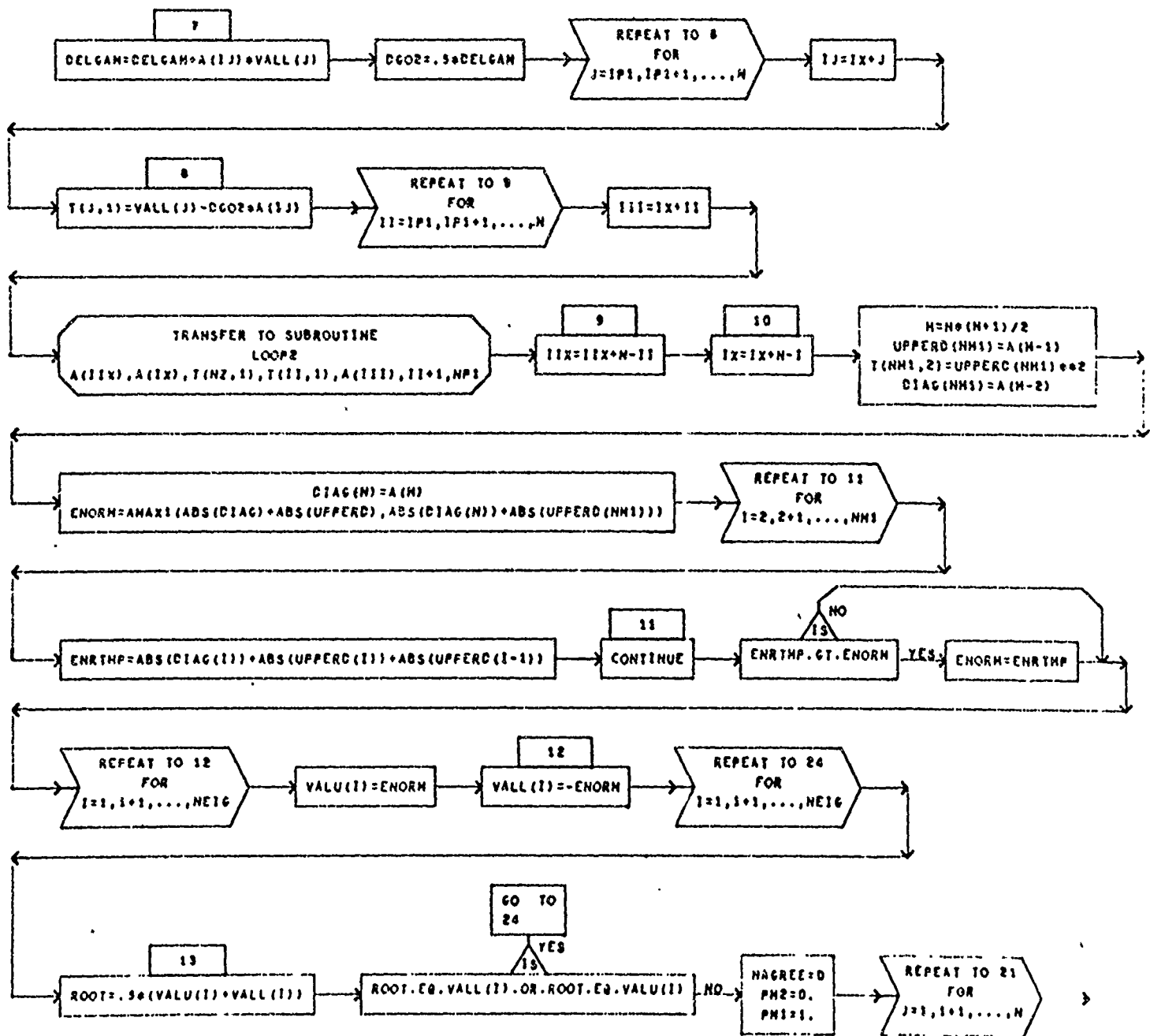
~BIGHAT

PROG. AUTHORS M. ELSON AND R. E. FUNDERLIC, CENTRAL DATA PROCESSING, 4, 1, 68

D I M E N S I O N E D V A R I A B L E S

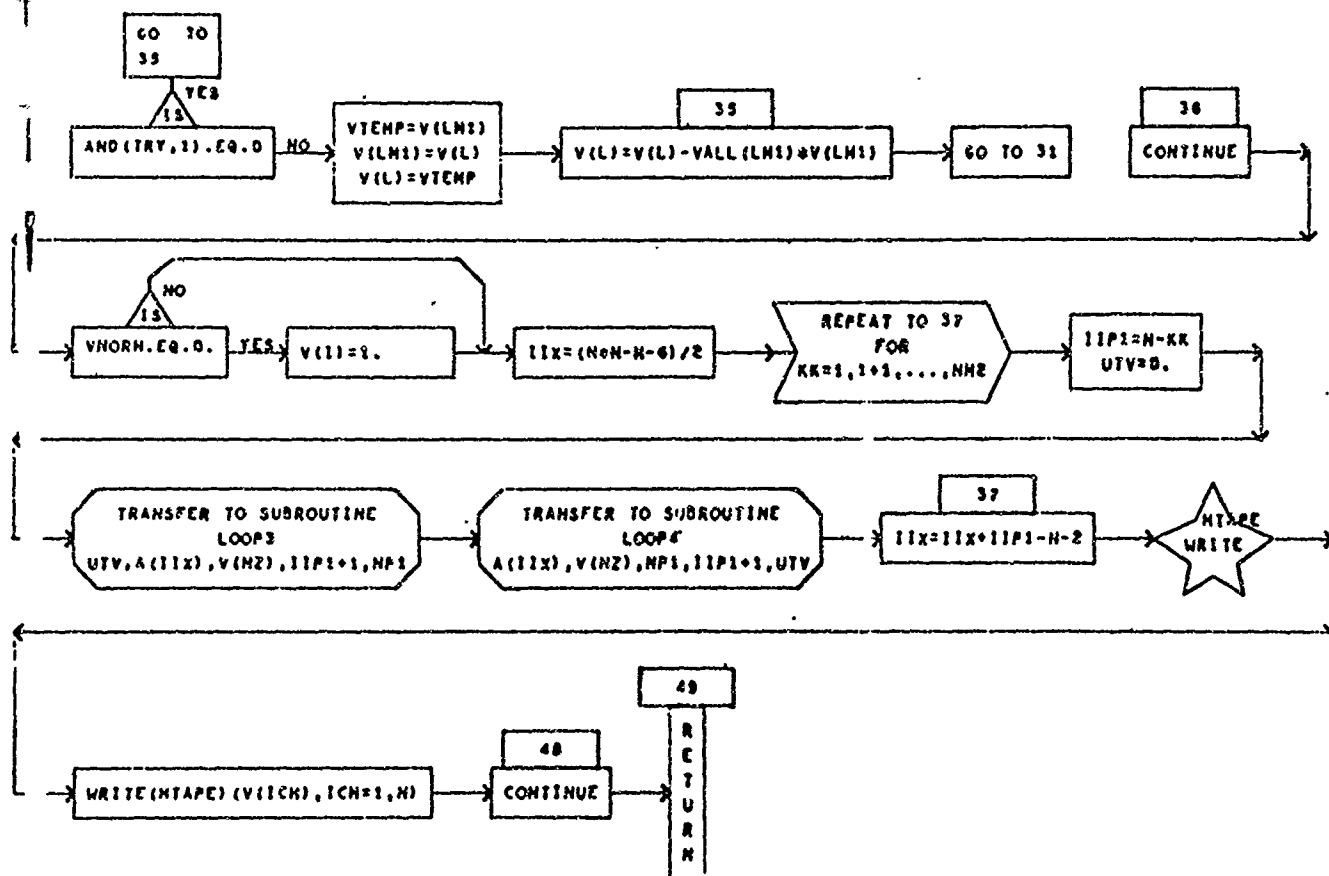
SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
A	1	VALU	1	VALL	1	UPPERD	1	DIAG	1
V	1	T	NN,3	INTER	1				











SYMINV

A IS THE UPPER TRIANGLE OF THE SYMMETRIC MATRIX TO BE INVERTED.

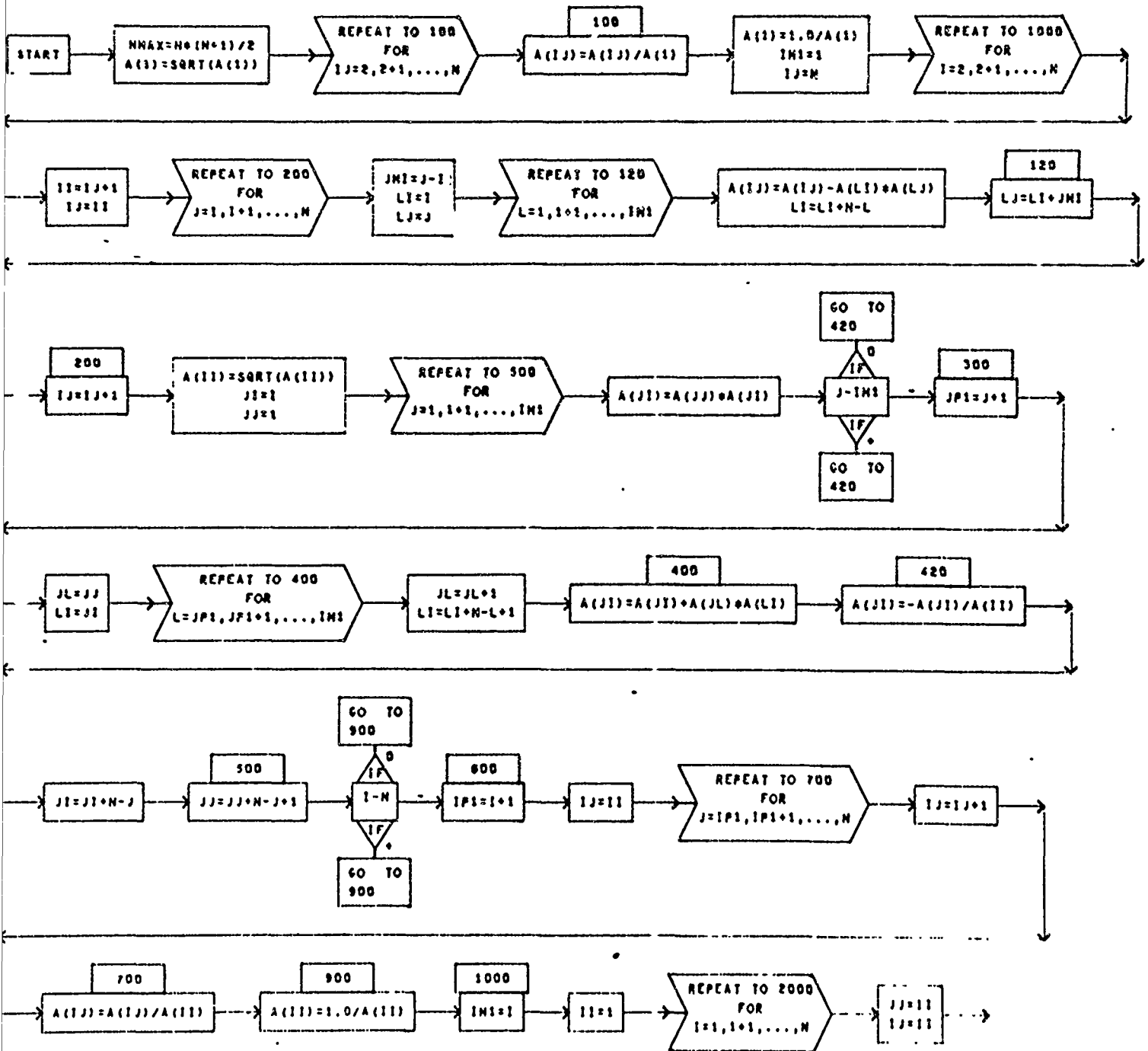
ELEMENTS ARE STORED ROWWISE.

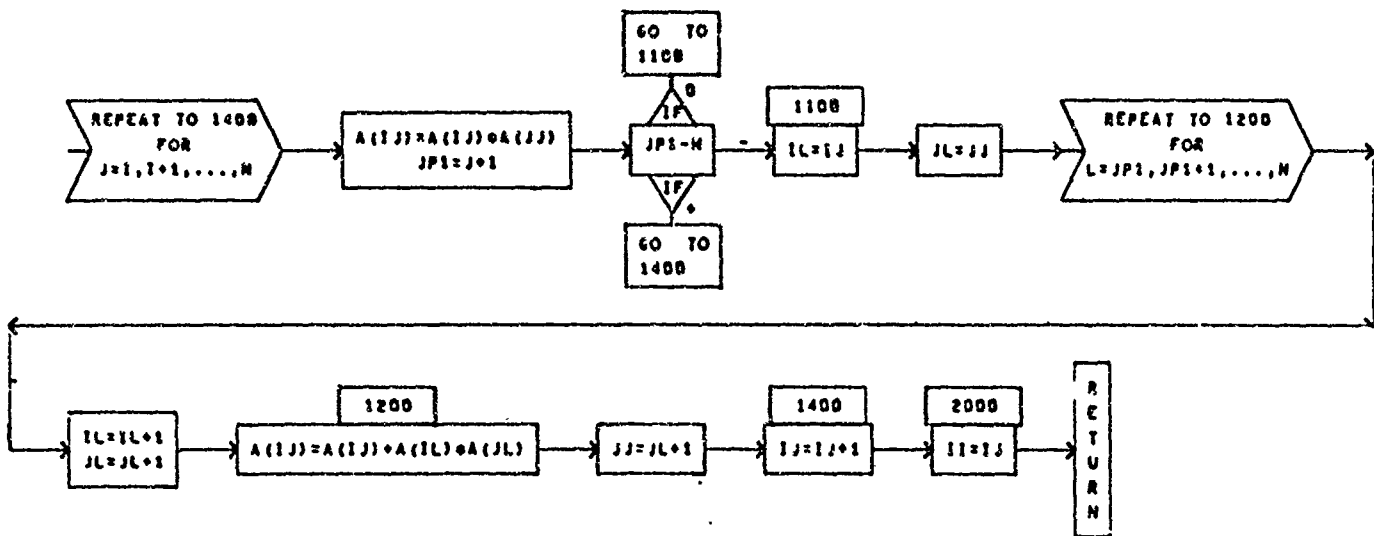
M = ORDER OF MATRIX

PROGRAM INVERTS IN PLACE.

D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
A	1								





EIGMAT

THIS SUBROUTINE FINDS THE EIGENVALUES AND EIGENVECTORS FOR
SYMMETRIC MASS AND STIFFNESS MATRICES.

THE ARGUMENTS ARE--

N- ORDER OF MATRICES.

A- DUMMY VECTOR WITH DIMENSION IN MAIN PROGRAM OF $N*(N+1)/2$

VALU- STORAGE FOR EIGENVALUES MUST BE DIMENSIONED IN THE MAIN
PROGRAM AS A VECTOR OF LENGTH NEIG.

TEMP,B,C,D,- DUMMY VECTORS WITH DIMENSION OF N IN MAIN PROGRAM.

E- DUMMY ARRAY WITH DIMENSIONS OF (N,3) IN MAIN PROGRAM.

IDUM- DUMMY INTEGER VECTOR WITH DIMENSION OF N IN MAIN PROGRAM.

MTAPE- TAPE WHERE STIFFNESS MATRIX IS STORED IN COMPACT FORM.

MAAPE- TAPE WHERE MASS MATRIX IS STORED IN COMPACT FORM.

ITAPE,ITAPE- SCRATCH TAPES.

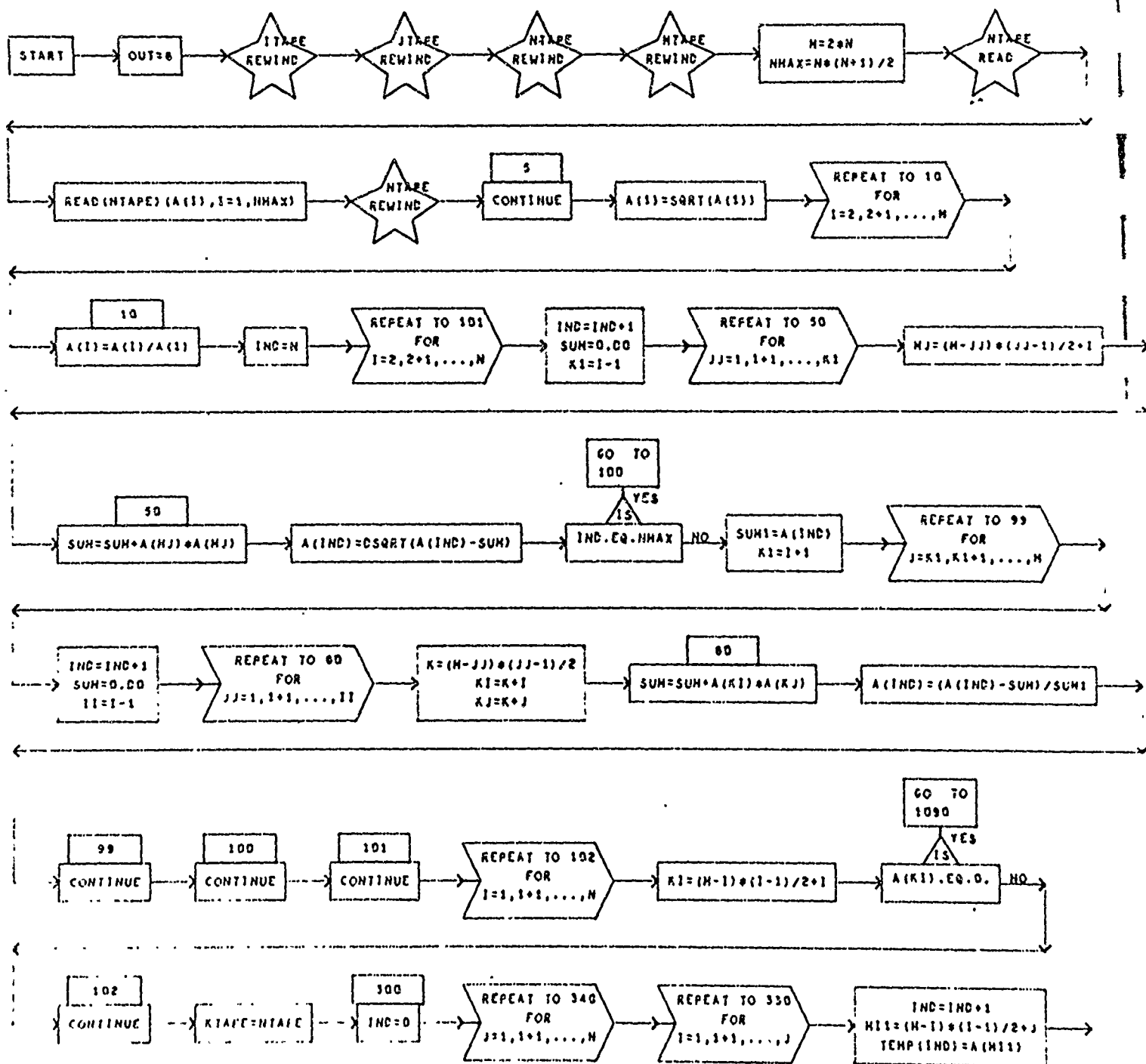
NEIG- NUMBER OF EIGENVALUES DESIRED.

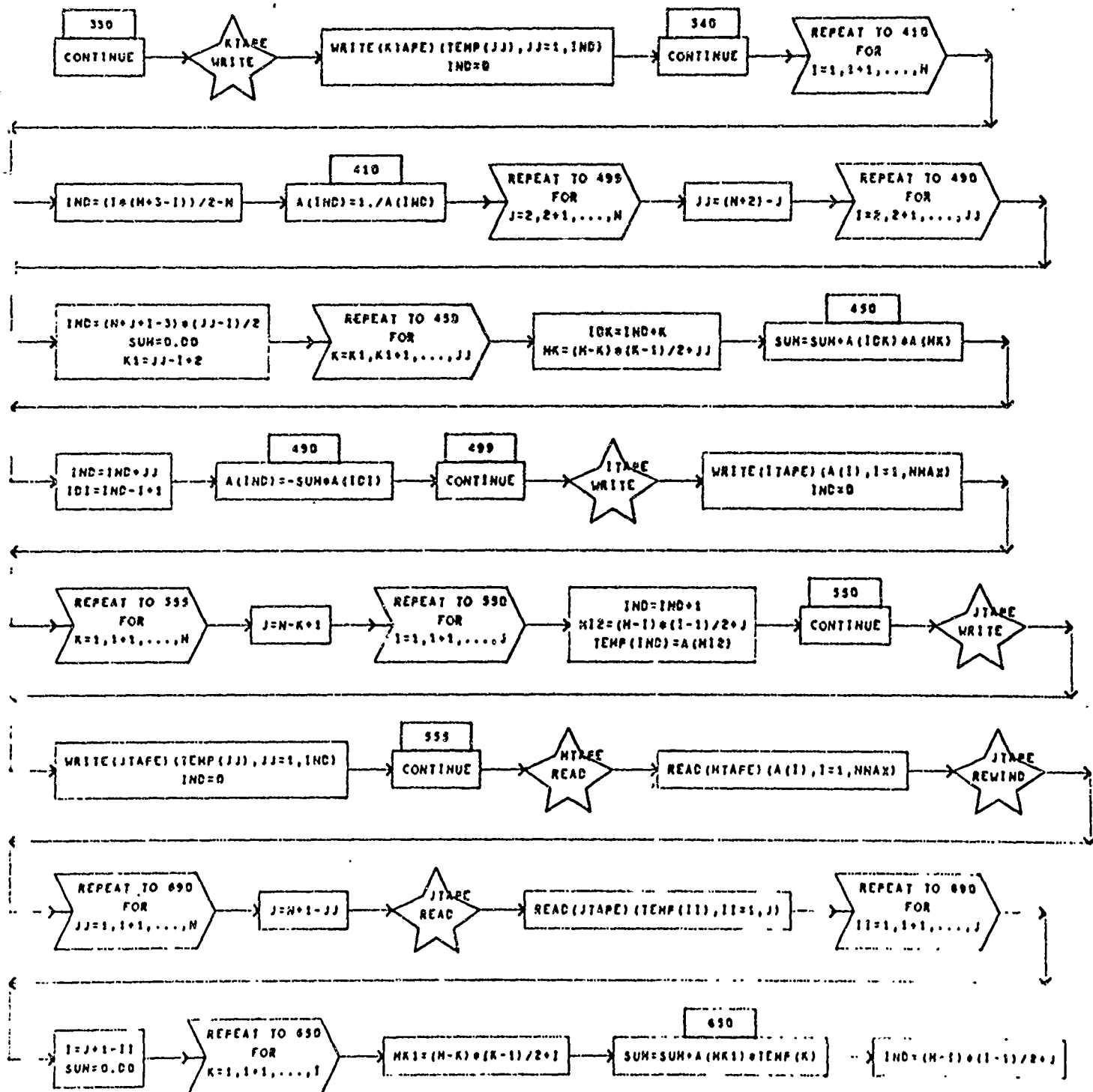
NVEC- NUMBER OF EIGENVECTORS DESIRED. MUST BE EQUAL TO OR LESS
THAN NEIG.

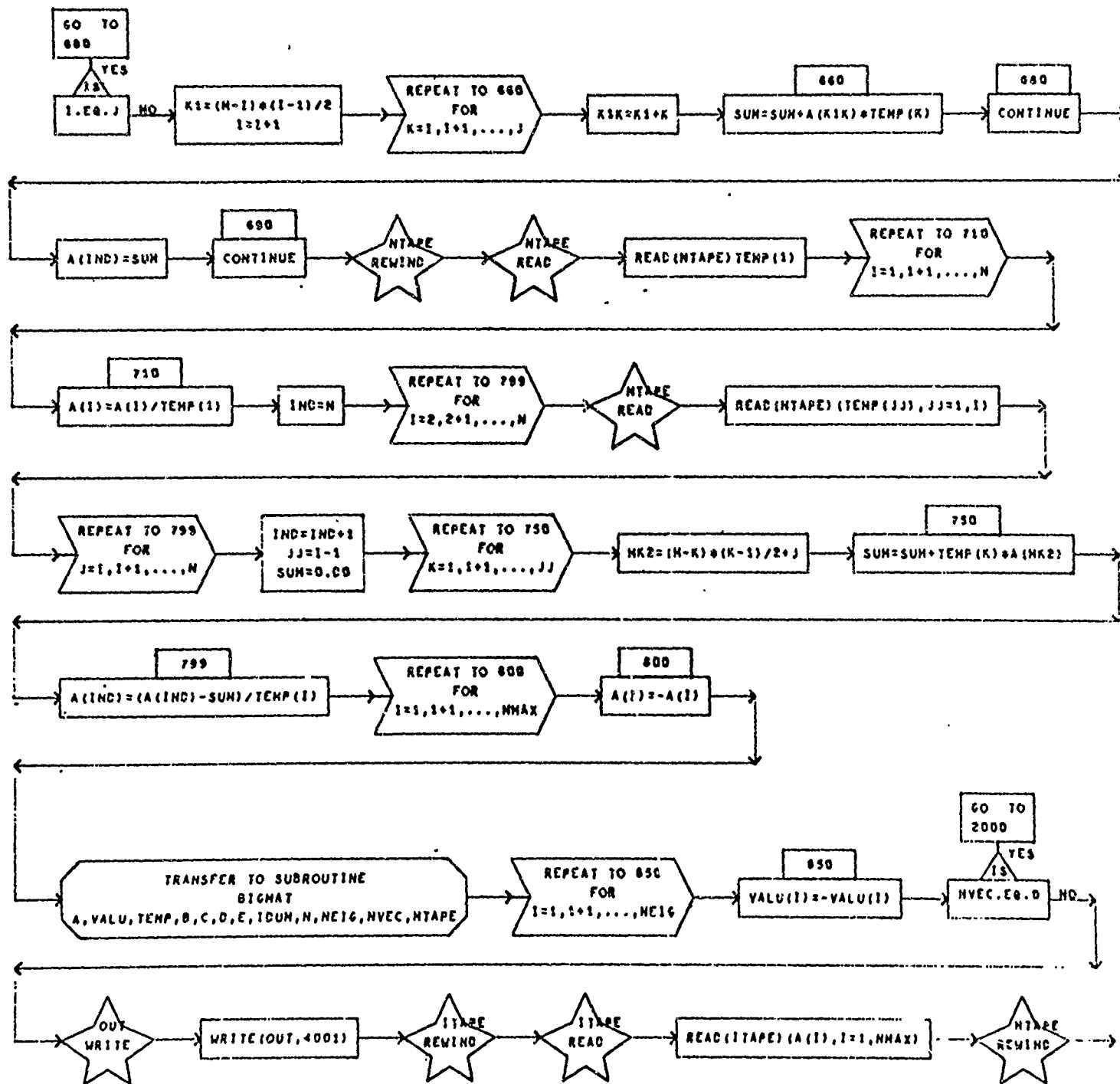
THE MASS AND STIFFNESS MATRICES ARE STORED IN COMPACT FORM AS
VECTORS. ONLY THE UPPER TRIANGLE OF THESE MATRICES(BY ROWS) IS
STORED.

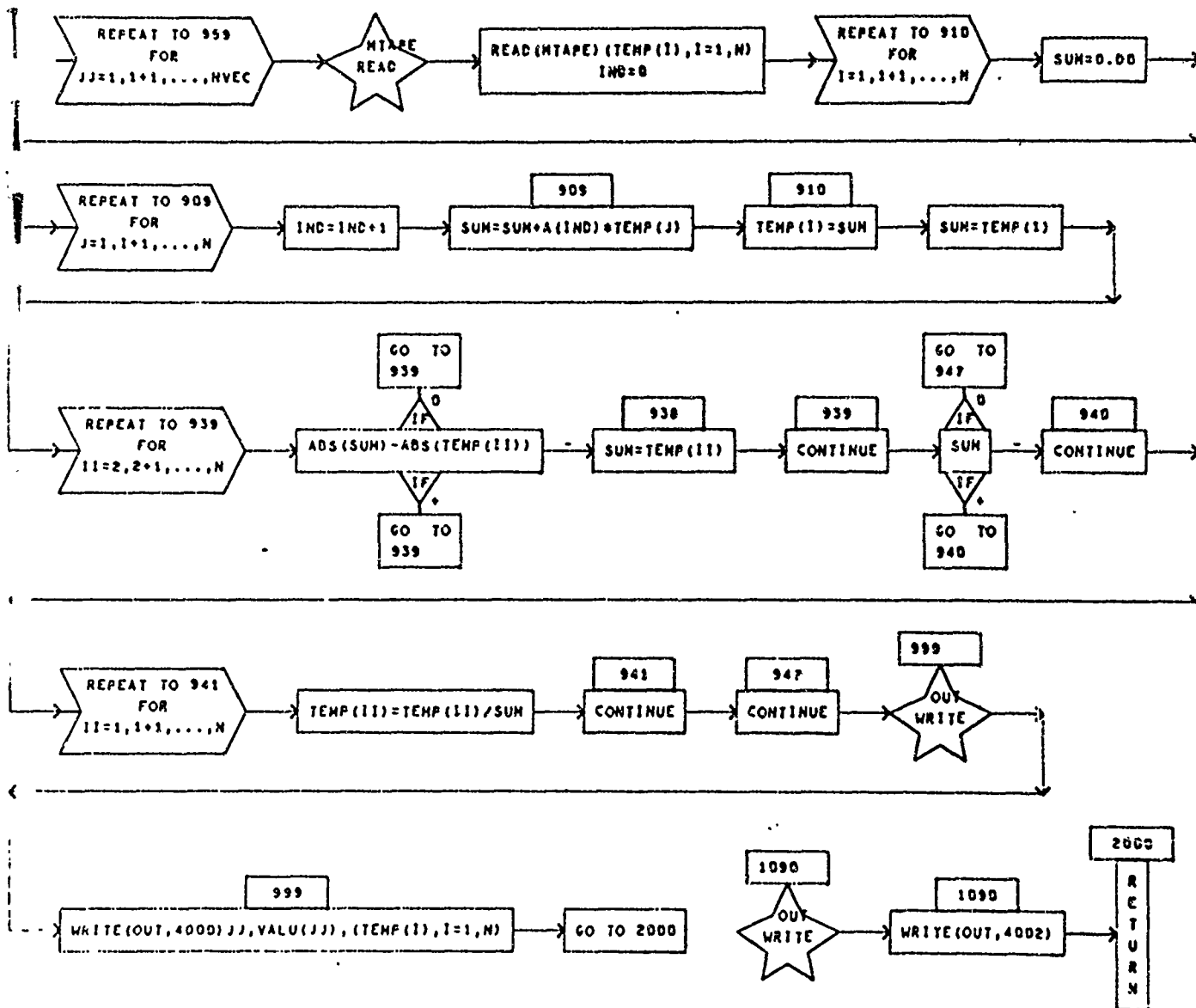
D I M E N S I O N E D V A R I A B L E S

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
A	1	TEMP	1	VALU	1	B	1	C	1
D	1	E	N,3	IDUM	1				









PLYMP

12/68

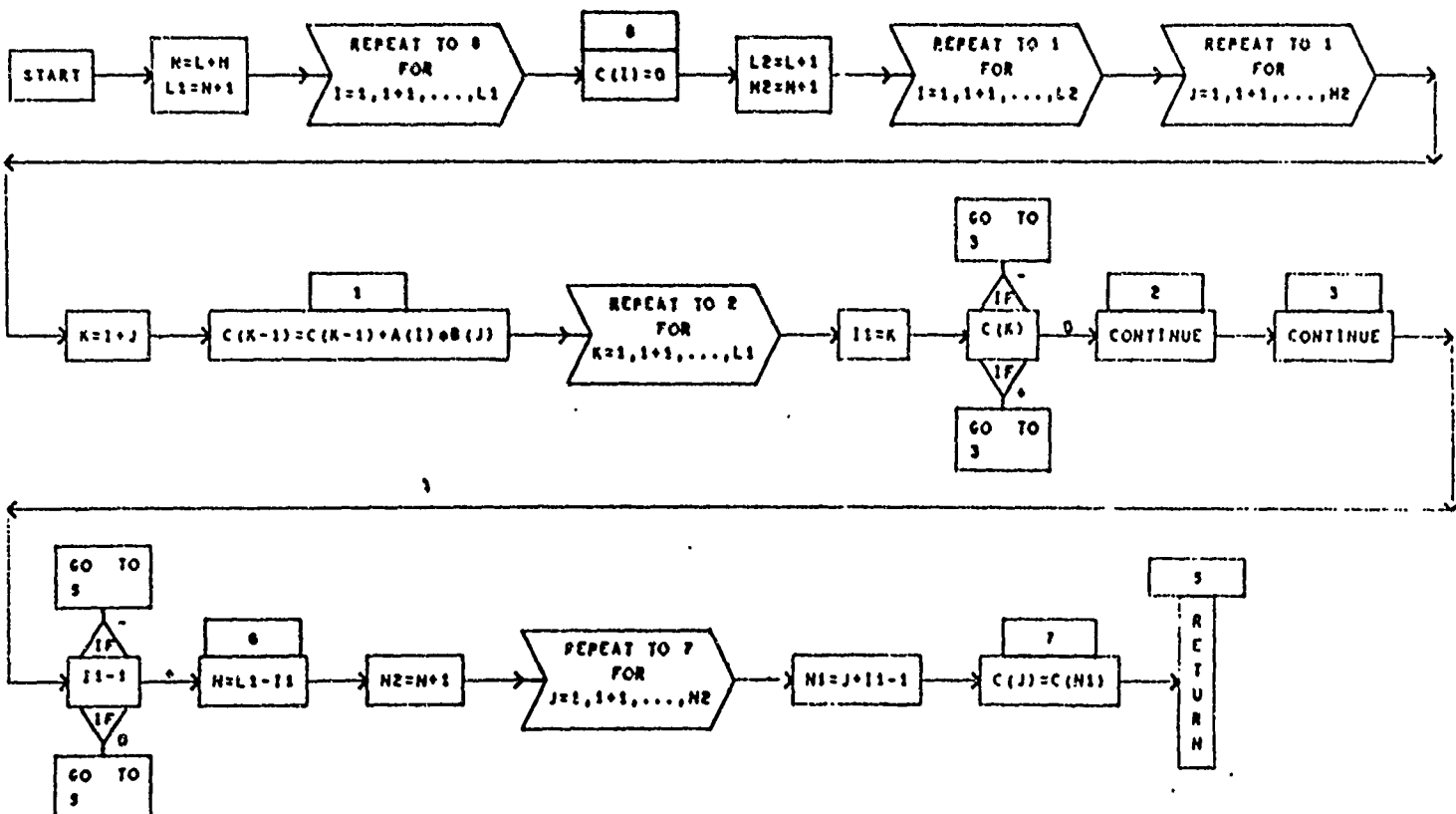
POLYNOMIAL MULTIPLY

DIMENSIONED VARIABLES

SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES	SYMBOL	STORAGES
A	1	B	1	C	1				

SUBROUTINE PLYMP(A,L,B,M,C,N)

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APPENDIX D

Symbol List

Symbol List

Listed below by their FORTRAN names are some of the input quantities to the program and their equivalent names in Section 3.0.

<u>Input Quantity</u>	<u>Symbol in Section 3.0</u>
YM	E
PR	ν
GE	G
DENS	ρ
X	X
Y	Y
RSMAS	M_i
AR	A
XI	I
YJ	J
PTH	t
DX	D_x
DY	D_y
D1	D_1
DXY	D_{xy}
BETA	β

UNCLASSIFIED

Security Classification

DOCUMENT CONTROL DATA - R & D

(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)

1. ORIGINATING ACTIVITY (Corporate author) HUGHES AIRCRAFT COMPANY, MISSILE SYSTEMS DIVISION FALLBROOK AND ROSCOE BLVDS. CANOGA PARK, CALIFORNIA 91304		2a. REPORT SECURITY CLASSIFICATION UNCLASSIFIED
3. REPORT TITLE COLLOCATION FLUTTER ANALYSIS STUDY		2b. GROUP
4. DESCRIPTIVE NOTES (Type of report and inclusive dates) FINAL REPORT (MARCH 1968 THROUGH MARCH 1969)		
5. AUTHOR(S) (First name, middle initial, last name) DYNAMICS AND ENVIRONMENT SECTION, DONALD R. ULBRICH		
6. REPORT DATE APRIL 4, 1969	7a. TOTAL NO. OF PAGES	7b. NO. OF REFS
8a. CONTRACT OR GRANT NO. N00019-68-C-0247	9a. ORIGINATOR'S REPORT NUMBER(S)	
b. PROJECT NO.	9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report)	
c.		
d.		
10. DISTRIBUTION STATEMENT IN ADDITION TO SECURITY REQUIREMENTS WHICH APPLY TO THIS DOCUMENT AND MUST BE OBSERVED BY EACH TRANSMITTAL OF THIS DOCUMENT BY THE AGENCIES OF THE U.S. GOVERNMENT, THIS DOCUMENT MUST HAVE PRIOR APPROVAL OF THE COMMANDER, NSC		
11. SUPPLEMENTARY NOTES	12. SPONSORING MILITARY ACTIVITY NAVAL AIR SYSTEMS COMMANDS DEPARTMENT OF THE NAVY WASHINGTON, D.C.	

13. ABSTRACT

THIS STUDY COVERS THE DEVELOPMENT OF A SET OF COMPUTER PROGRAM TO PERFORM FLUTTER ANALYSIS BY THE COLLOCATION METHOD. WHILE THIS METHOD HAS BEEN KNOWN FOR SOME TIME, ONLY RECENTLY HAVE ADVANCES IN COMPUTER TECHNOLOGY MADE THE METHOD TECHNICALLY AND FINANCIALLY FEASIBLE. THE INGREDIENTS OF A COLLOCATION FLUTTER ANALYSIS ARE 1) A FLEXIBILITY MATRIX, 2) AERODYNAMIC INFLUENCE COEFFICIENT MATRIX, AND 3) AN EIGENVALUE SOLUTION. THIS STUDY IS PRESENTED IN FOUR VOLUMES. VOLUME I CONTAINS A GENERAL PROGRAM DISCUSSION. VOLUME II CONTAINS THE PROGRAM FLUENC WHICH CALCULATES THE FLEXIBILITY MATRIX. VOLUME III CONTAINS A SET OF THREE PROGRAMS TO CALCULATE AERODYNAMIC INFLUENCE COEFFICIENTS FOR SUBSONIC, TRANSONIC, AND SUPERSONIC FLIGHT REGIMES. VOLUME IV CONTAINS THE PROGRAM COMA WHICH SETS UP AND SOLVES THE FLUTTER EIGENVALUE MATRIX.

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