

The public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington VA, 22202-4302. Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to any penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number.  
PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ADDRESS.

1. REPORT DATE (DD-MM-YYYY) 20-08-2018	2. REPORT TYPE Final Report	3. DATES COVERED (From - To) 1-Sep-2014 - 31-May-2018
---	--------------------------------	--

4. TITLE AND SUBTITLE Final Report: Emergent Non-Equilibrium Phenomena in Driven Correlated Materials With Strong Spin-Orbit Coupling	5a. CONTRACT NUMBER W911NF-14-1-0579
	5b. GRANT NUMBER
	5c. PROGRAM ELEMENT NUMBER 611102

6. AUTHORS	5d. PROJECT NUMBER
	5e. TASK NUMBER
	5f. WORK UNIT NUMBER

7. PERFORMING ORGANIZATION NAMES AND ADDRESSES University of Texas at Austin 101 East 27th Street Suite 5.300 Austin, TX 78712 -1532	8. PERFORMING ORGANIZATION REPORT NUMBER
--	--

9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS (ES) U.S. Army Research Office P.O. Box 12211 Research Triangle Park, NC 27709-2211	10. SPONSOR/MONITOR'S ACRONYM(S) ARO
	11. SPONSOR/MONITOR'S REPORT NUMBER(S) 65846-PH.25

12. DISTRIBUTION AVAILABILITY STATEMENT Approved for public release; distribution is unlimited.
--

13. SUPPLEMENTARY NOTES The views, opinions and/or findings contained in this report are those of the author(s) and should not be construed as an official Department of the Army position, policy or decision, unless so designated by other documentation.
---

14. ABSTRACT
--------------

15. SUBJECT TERMS
-------------------

16. SECURITY CLASSIFICATION OF:	17. LIMITATION OF ABSTRACT	15. NUMBER OF PAGES	19a. NAME OF RESPONSIBLE PERSON Gregory Fiete
a. REPORT UU	b. ABSTRACT UU	c. THIS PAGE UU	19b. TELEPHONE NUMBER 512-232-8084

# RPPR Final Report

## as of 14-May-2019

Agency Code:

Proposal Number: 65846PH

**Agreement Number: W911NF-14-1-0579**

### INVESTIGATOR(S):

**Name:** PhD Gregory Fiete  
**Email:** fiete@physics.utexas.edu  
**Phone Number:** 5122328084  
**Principal:** Y

Organization: **University of Texas at Austin**

Address: 101 East 27th Street, Austin, TX 787121532

Country: USA

DUNS Number: 170230239

EIN: 746000203

**Report Date:** 31-Aug-2018

Date Received: 20-Aug-2018

**Final Report** for Period Beginning 01-Sep-2014 and Ending 31-May-2018

**Title:** Emergent Non-Equilibrium Phenomena in Driven Correlated Materials With Strong Spin-Orbit Coupling

**Begin Performance Period:** 01-Sep-2014

**End Performance Period:** 31-May-2018

**Report Term:** 0-Other

Submitted By: PhD Gregory Fiete

Email: fiete@physics.utexas.edu

Phone: (512) 232-8084

**Distribution Statement:** 1-Approved for public release; distribution is unlimited.

**STEM Degrees:** 3

**STEM Participants:** 4

**Major Goals:** The major goal of this project was to theoretically investigate out-of-equilibrium quantum many particle systems that have strong spin-orbit coupling. Particular emphasis was placed on systems with strong correlations. These investigations were carried out with the ultimate aim of finding out-of-equilibrium regimes with interesting properties that might be exploited in applications for the ARO, and DoD more generally. Important progress was made in this direction.

Two examples of out-of-equilibrium regimes with interesting properties are Floquet (periodically driven) systems and pre-thermalized states following a quench to a new Hamiltonian. Both regimes are inherently non-equilibrium and have properties that are quasi-steady state. In a Floquet system, the time averaged (over one period) properties are independent of time, and in the pre-thermalized state there is a time-window of weak time dependence before the system begins to converge more rapidly to a thermal (equilibrium) state. In addition to these two scenarios, we also investigated a quench to a Floquet state: A system initially in equilibrium is suddenly subjected to a periodic drive. This third scenario is a combination of the first two. It turns out (theoretically) that one can obtain an approximate \*time-independent\* Hamiltonian that describes the dynamics for short-to-intermediate times after the quench to the periodic drive. This observation opens new possibilities for "Hamiltonian engineering" in solid-state systems, and may allow new physical regimes to be opened, possibly in "conventional materials" that are well-known and used in existing applications. To this end, we developed a "flow equation approach" based on renormalization group ideas to obtain such a time-independent effective Hamiltonian.

**Accomplishments:** Over the course of this project, the PI and his group have been involved with projects in several different areas under the umbrella of non-equilibrium phenomena: (1) Thermoelectric transport in double Weyl semimetals, (2) Disorder effects in correlated topological insulators, (3) Multi-band Floquet systems with quadratic band touching points and flat bands in two dimensions, (3) Topological magnon bands and unconventional superconductivity in pyrochlore iridates, (4) Thermal conductivity of local moment models with strong spin-orbit coupling, (5) Time-dependent dynamical mean-field theory (DMFT) studies of Hubbard models subjected to time-periodic Hamiltonians and (6) The development of a "flow equation approach" to determining the effective time-independent Hamiltonian of a time-periodic system.

The results from topics (1)-(4) were covered in detail in previous reports, so I will focus here on the main results from (5) and (6).

(5) In our time-dependent DMFT studies of Hubbard models we focused on the so-called "mass imbalanced Hubbard model". In this model the hopping (kinetic energy) for spin up and spin down electrons is different. This

## RPPR Final Report as of 14-May-2019

behavior is realized in effective models of ferromagnets, and other itinerant magnetic systems, for example. We investigated the behavior of the on-site double occupancy as a function of time and the spin-resolved single electron occupation distribution as a function of time, including the quasi-particle jump. We considered quenches on both the Hubbard interaction and the hopping parameters.

For the mass imbalanced model with a quench on the interactions, we found that when the Coulomb interaction is increased under equilibrium conditions, the quasiparticle weights for spin-up and spin-down (the mass imbalance) electrons approach zero simultaneously, indicating the absence of a spin-selective Mott transition. By contrast, our out-of-equilibrium study of the mass-imbalanced Hubbard model suggests that there exists the spin-selective dynamical phase transition (one spin orientation undergoes a fast thermalization at its critical Coulomb interaction strength while the other spin orientation shows prethermalization behavior). The spin-selective dynamical phase transition is characterized by the relaxation behavior of the spin-resolved kinetic energy and the spin-resolved momentum-dependent occupation. To connect with possible experiments, we calculate the spin-resolved two-time optical conductivity, which confirms the spin-selective thermalization plateau. We find that the critical Coulomb interaction of each spin orientation for the spin-selective thermalization grows as the mass imbalance decreases.

In a separate project, we used nonequilibrium dynamical mean-field theory with iterative perturbation theory as an impurity solver to study the recovery of SU(2) symmetry in real time following a hopping integral parameter quench from a mass-imbalanced to a mass-balanced single-band Hubbard model at half filling. A dynamical order parameter  $\gamma(t)$  was defined to characterize the evolution of the system towards SU(2) symmetry. By comparing the momentum-dependent occupation from an equilibrium calculation [with the SU(2) symmetric Hamiltonian after the quench at an effective temperature] with the data from our nonequilibrium calculation, we concluded that the SU(2) symmetry recovered state is a thermalized state. Further evidence from the evolution of the density of states supports this conclusion. We found the order parameter in the weak Coulomb interaction regime undergoes an approximate exponential decay. We numerically investigated the interplay of the relevant parameters (initial temperature, Coulomb interaction strength, initial mass-imbalance ratio) and their combined effect on the thermalization behavior. Finally, we studied evolution of the order parameter as the hopping parameter was changed with either a linear ramp or a pulse. Our results can be useful in strategies to engineer the relaxation behavior of interacting quantum many-particle systems.

In a closely related project to the time-dependent DMFT studies of Hubbard models, we turned our attention to the atomic limit of the on-site part of a multi-orbital Hubbard model. Using exact diagonalization, we studied the spin-orbit coupling and interaction-induced mixing between  $t_{2g}$  and  $e_g$  d-orbital states in a cubic crystalline environment, as commonly occurs in transition metal oxides. We made a direct comparison with the widely used  $t_{2g}$ -only or  $e_g$ -only models, depending on electronic filling. We considered all electron fillings of the d shell and computed the total magnetic moment, the spin, the occupancy of each orbital, and the effective spin-orbit coupling strength (renormalized through interaction effects) in terms of the bare interaction parameters, spin-orbit coupling, and crystal-field splitting, focusing on the parameter ranges relevant to 4d and 5d transition metal oxides. In various limits, we provided perturbative results consistent with our numerical calculations. We found that the  $t_{2g}$ - $e_g$  mixing can be large, with up to 20% occupation of orbitals that are nominally "empty," which has experimental implications for the interpretation of the branching ratio in experiments, and can impact the effective local moment Hamiltonian used to study magnetic phases and magnetic excitations in transition metal oxides. Our results can aid the theoretical interpretation of experiments on these materials, which often fall in a regime of intermediate coupling with respect to electron-electron interactions.

(6) In our work on the development of effective time-independent Hamiltonians, we were guided by the high-frequency Floquet expansions which give an effective time-independent Hamiltonian valid in a restricted part of parameter space. To address this limitation, we developed a theoretical method to generate a highly accurate time-independent Hamiltonian governing the finite-time behavior of a time-periodic system. The method exploits infinitesimal unitary transformation steps, from which renormalization group-like flow equations are derived to produce the effective Hamiltonian. Our tractable method has a range of validity reaching into frequency regimes that are usually inaccessible via high frequency  $\omega$  expansions in the parameter  $h/\omega$ , where  $h$  is the upper limit for the strength of local interactions. We demonstrated our approach on both interacting and non-interacting many-body Hamiltonians where it offers an improvement over the more well-known Magnus expansion and other high frequency expansions. For the interacting models, we compared our approximate results to those found via exact diagonalization. While the approximation generally performs better globally than other high frequency approximations, the improvement is especially pronounced in the regime of lower frequencies and strong external driving. This regime is of special interest because of its proximity to the resonant regime where the effect of a periodic drive is the most dramatic. Our results open a new route towards identifying novel non-equilibrium regimes

## RPPR Final Report as of 14-May-2019

and behaviors in driven quantum many-particle systems.

(3) A few other recent projects were focused on on two-dimensional Floquet systems, one in the presence of disorder, and another in the presence of an external magnetic field. These studies helped expand our knowledge of the phenomenology of non-interacting, periodically driven systems. In the disorder project, we found that disorder can induce transitions from topologically non-trivial states to trivial states or vice versa, both examples of Floquet topological Anderson transitions. As a result of the movement of the minimal gap point through the Brillouin zone as a function of laser parameters, the nature of the topological phases and transitions is laser-parameter dependent. In the Floquet Hofstadter butterfly problem, we studied the effect of the laser on the Chern number

**Training Opportunities:** Two PhD students and one postdoc have been supported on this award in the final reporting period. They have all attended the APS March meeting and given talks, and they have all presented their research at informal seminars in our department. The PI encourages group members to work together, so there have been opportunities for these researchers to guide the progress of younger group members. In addition, group members are encouraged to discuss the results of their research with visitors to our department so that they become familiar explaining their work 1-on-1 to an experienced scientist.

The PI meets regularly 1-on-1 with all group members, and discusses various career opportunities possible with a PhD in theoretical physics. One student has chosen a future career in large scale data analysis. These efforts will help contribute to the overall strength of the US-based technically trained workforce.

**Results Dissemination:** The following papers have been completed (and copies sent to the ARO program manager of this award) in the final reporting period:

L. Du, Q. Chen, A. D. Barr, A. R. Barr, and G. A. Fiete, "Floquet Hofstadter Butterfly on the Kagome and Triangular Lattices", arXiv:1808.02057 (Submitted to PRB)

M. Vogl, P. Laurell, A. D. Barr, and G. A. Fiete, "A flow equation approach to periodically driven quantum systems", arXiv:1808.01697 (Submitted to PRX)

H. Nam, C. Zhang, W. Lee, S. Zhu, H.-J. Gao, Q. Niu, G. A. Fiete, and C.-K. Shih, "Behavior of superconductivity in a Pb/Ag heterostructure with nearly perfect interfacial transparency", (Submitted to PRL).

L. Du, P. Schnase, A. D. Barr, A. R. Barr, and G. A. Fiete, "Floquet topological transitions in extended Kane-Mele models with disorder", Phys. Rev. B **{bf 98}**, 054203 (2018).

P. Laurell and G. A. Fiete, "Magnon thermal Hall effect in kagome antiferromagnets with Dzyaloshinskii-Moriya interactions", arXiv:1804.09783 (Submitted to PRB)

L. Du and G. A. Fiete, "Dynamical recovery of SU(2) symmetry in the mass-quenched Hubbard model", Phys. Rev. B **{bf 97}**, 08512 (2018).

G. L. Stamokostas and G. A. Fiete, "Mixing of  $t_{2g}$ - $e_g$  orbitals in 4d and 5d transition metal oxides", Phys. Rev. B **{bf 97}**, 085150 (2018).

Q. Chen, L. Du, and G. A. Fiete, "Floquet band structure of a semi-Dirac system", Phys. Rev. B **{bf 97}**, 035422 (2018).

L. Du, L. Huang, and G. A. Fiete, "Orbital-selective thermalization plateau in the mass imbalanced Hubbard model", Phys. Rev. B **{bf 96}**, 165151 (2017).

The works have been discussed and are being discussed in seminars and conference attended by the PI and his group members.

## RPPR Final Report as of 14-May-2019

**Honors and Awards:** The PI was awarded a Simons Fellowship from the Simons Foundation. The Fellowship allows the extension of a 6-month sabbatical to a full year. The PI is taking the Fellowship at MIT.

The PI was also elected a Fellow of the American Physical Society (APS) and promoted to Full Professor during this grant period.

### Protocol Activity Status:

**Technology Transfer:** Nothing to Report

### PARTICIPANTS:

**Participant Type:** PD/PI

**Participant:** Gregory A Fiete

**Person Months Worked:** 2.00

**Funding Support:**

Project Contribution:

International Collaboration:

International Travel:

National Academy Member: N

Other Collaborators:

**Participant Type:** Postdoctoral (scholar, fellow or other postdoctoral position)

**Participant:** Liang Du

**Person Months Worked:** 3.00

**Funding Support:**

Project Contribution:

International Collaboration:

International Travel:

National Academy Member: N

Other Collaborators:

**Participant Type:** Graduate Student (research assistant)

**Participant:** Qi Chen

**Person Months Worked:** 6.00

**Funding Support:**

Project Contribution:

International Collaboration:

International Travel:

National Academy Member: N

Other Collaborators:

**Participant Type:** Graduate Student (research assistant)

**Participant:** Georgios Stamokostas

**Person Months Worked:** 6.00

**Funding Support:**

Project Contribution:

International Collaboration:

International Travel:

National Academy Member: N

Other Collaborators:

**Participant Type:** Undergraduate Student

**Participant:** Aaron Barr

**Person Months Worked:** 2.00

**Funding Support:**

Project Contribution:

International Collaboration:

International Travel:

National Academy Member: N



# RPPR Final Report

## as of 14-May-2019

**Publication Type:** Journal Article      Peer Reviewed: Y      **Publication Status:** 1-Published

**Journal:** Physical Review B

Publication Identifier Type: DOI

Publication Identifier: 10.1103/PhysRevB.97.085150

Volume: 97

Issue: 8

First Page #: 085150

Date Submitted: 8/20/18 12:00AM

Date Published: 2/26/18 5:00AM

Publication Location:

**Article Title:** Mixing of eg and t<sub>2g</sub> orbitals

**Authors:** Georgios L. Stamokostas, Gregory A. Fiete

**Keywords:** Hubbard model, multi-orbitals, spin-orbit coupling

**Abstract:** Using exact diagonalization, we study the spin-orbit coupling and interaction-induced mixing between t<sub>2g</sub> and e<sub>g</sub>-orbital states in a cubic crystalline environment, as commonly occurs in transition metal oxides. We make a direct comparison with the widely used t<sub>2g</sub>-only or e<sub>g</sub>-only models, depending on electronic filling. We consider all electron fillings of the d shell and compute the total magnetic moment, the spin, the occupancy of each orbital, and the effective spin-orbit coupling strength (renormalized through interaction effects) in terms of the bare interaction parameters, spin-orbit coupling, and crystal-field splitting, focusing on the parameter ranges relevant to 4d and 5d transition metal oxides. In various limits, we provide perturbative results consistent with our numerical calculations. We find that the t<sub>2g</sub>?e<sub>g</sub> mixing can be large, with up to 20% occupation of orbitals that are nominally "empty," which has experimental implications for the interpretation of the branching ratio

**Distribution Statement:** 1-Approved for public release; distribution is unlimited.

Acknowledged Federal Support: Y

**Publication Type:** Journal Article      Peer Reviewed: Y      **Publication Status:** 1-Published

**Journal:** Physical Review B

Publication Identifier Type: DOI

Publication Identifier: 10.1103/PhysRevB.97.085152

Volume: 97

Issue: 8

First Page #: 085152

Date Submitted: 8/20/18 12:00AM

Date Published: 2/27/18 5:00AM

Publication Location:

**Article Title:** Dynamical recovery of SU(2) symmetry in the mass-quenched Hubbard model

**Authors:** Liang Du, Gregory A. Fiete

**Keywords:** Dynamical lattice models, Hubbard Models, phase transition

**Abstract:** We use nonequilibrium dynamical mean-field theory with iterative perturbation theory as an impurity solver to study the recovery of SU(2) symmetry in real time following a hopping integral parameter quench from a mass-imbalanced to a mass-balanced single-band Hubbard model at half filling. A dynamical order parameter  $\rho(t)$  is defined to characterize the evolution of the system towards SU(2) symmetry. By comparing the momentum-dependent occupation from an equilibrium calculation [with the SU(2) symmetric Hamiltonian after the quench at an effective temperature] with the data from our nonequilibrium calculation, we conclude that the SU(2) symmetry recovered state is a thermalized state. Further evidence from the evolution of the density of states supports this conclusion. We find the order parameter in the weak Coulomb interaction regime undergoes an approximate exponential decay. We numerically investigate the interplay of the relevant parameters (initial temperature, Coulomb interaction

**Distribution Statement:** 1-Approved for public release; distribution is unlimited.

Acknowledged Federal Support: Y



# RPPR Final Report

## as of 14-May-2019

**Publication Type:** Journal Article      Peer Reviewed: Y      **Publication Status:** 4-Under Review  
**Journal:** arXiv (Submitted to Physical Review X)  
Publication Identifier Type: Other      Publication Identifier: arXiv:1808.01697  
Volume:      Issue:      First Page #:  
Date Submitted: 8/20/18 12:00AM      Date Published:  
Publication Location:

**Article Title:** A flow equation approach to periodically driven quantum systems

**Authors:** Michael Vogl, Pontus Laurell, Aaron D. Barr, Gregory A. Fiete

**Keywords:** Floquet, Effective Hamiltonian

**Abstract:** We present a theoretical method to generate a highly accurate  $\hbar$ -time-independent Hamiltonian governing the finite-time behavior of a time-periodic system. The method exploits infinitesimal unitary transformation steps, from which renormalization group-like flow equations are derived to produce the effective Hamiltonian. Our tractable method has a range of validity reaching into frequency regimes that are usually inaccessible via high frequency  $\hbar$  expansions in the parameter  $\hbar/\omega$ , where  $\hbar$  is the upper limit for the strength of local interactions. We demonstrate our approach on both interacting and non-interacting many-body Hamiltonians where it offers an improvement over the more well-known Magnus expansion and other high frequency expansions. For the interacting models, we compare our approximate results to those found via exact diagonalization. While the approximation generally performs better globally than other high frequency approximations, the improvement is especially pronounced.

**Distribution Statement:** 1-Approved for public release; distribution is unlimited.

Acknowledged Federal Support: Y

**Publication Type:** Journal Article      Peer Reviewed: Y      **Publication Status:** 4-Under Review  
**Journal:** arxiv (Submitted to Physical Review B)  
Publication Identifier Type: Other      Publication Identifier: arXiv:1808.02057  
Volume:      Issue:      First Page #:  
Date Submitted: 8/20/18 12:00AM      Date Published:  
Publication Location:

**Article Title:** Floquet Hofstadter Butterfly on the Kagome and Triangular Lattices

**Authors:** Liang Du, Qi Chen, Aaron D. Barr, Ariel R. Barr, Gregory A. Fiete

**Keywords:** Floquet, Hofstadter Butterfly, topological

**Abstract:** In this work we use Floquet theory to theoretically study the influence of monochromatic circularly and linearly polarized light on the Hofstadter butterfly---induced by a uniform perpendicular magnetic field---for both the kagome and triangular lattices. In the absence of the laser light, the butterfly has fractal structure with inversion symmetry about magnetic flux  $\phi=1/4$ , and reflection symmetry about  $\phi=1/2$ . As the system is exposed to an external laser, we find circularly polarized light deforms the butterfly by breaking the mirror symmetry at flux  $\phi=1/2$ . By contrast, linearly polarized light deforms the original butterfly while preserving the mirror symmetry at flux  $\phi=1/2$ . We find the inversion symmetry is always preserved for both linear and circular polarized light. For linearly polarized light, the Hofstadter butterfly depends on the polarization direction. Further, we study the effect of the laser on the Chern number of lowest band in the off-resonance regime (laser frequency

**Distribution Statement:** 1-Approved for public release; distribution is unlimited.

Acknowledged Federal Support: Y

**RPPR Final Report**  
as of 14-May-2019

**Publication Type:** Journal Article

Peer Reviewed: Y

**Publication Status:** 4-Under Review

**Journal:** Submitted to PRL

Publication Identifier Type:

Publication Identifier:

Volume: Issue:

First Page #:

Date Submitted: 8/20/18 12:00AM

Date Published:

Publication Location:

**Article Title:** Behavior of superconductivity in a Pb/Ag heterostructure with nearly perfect transparency

**Authors:** Hyoungdo Nam, Chendong Zhang, Woojoo Lee, Siyuan Zhu, Hong-Jun Gao, Qian Niu, Gregory A. Fiete

**Keywords:** Superconductivity, proximity effect, heterostructure

**Abstract:** The superconducting proximity effect, a long-standing topic of great importance in condensed matter physics, has attracted new interest in the context of topological superconductivity and the associated non-Abelian excitations potentially useful in topological quantum computing. A crucial but unresolved issue is which interfacial and material details determine the efficiency of the proximity effect. In this work, we study an epitaxially grown superconductor (SC)/normal metal (NM) heterostructure (Pb/Ag) and show that the electronic transparency is nearly perfect across the interface. We find a spatially constant superconducting gap determined by local tunneling spectroscopy and magneto response measurements, despite the highly mismatched Fermi surfaces between individual Pb and Ag epitaxial layers, and the large differences in the lattice constants and electronic density of states. The uniform superconducting gap is in contrast to the spatially varying pair potential with a discontinuity

**Distribution Statement:** 1-Approved for public release; distribution is unlimited.

Acknowledged Federal Support: Y

Nothing to report in the uploaded pdf (see accomplishments).