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# Optical Spectroscopy of Low-Phonon, Holmium-Doped Barium Fluoride ( $\text{BaF}_2$ ) Single Crystals

by Ei Ei Brown, Zackery Fleischman, Jason McKay, and  
Mark Dubinskii

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# Optical Spectroscopy of Low-Phonon, Holmium-Doped Barium Fluoride (BaF<sub>2</sub>) Single Crystals

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<b>14. ABSTRACT</b> The development of new solid-state laser materials for mid-IR laser sources continues to be of significant interest for potential applications in remote sensing of biochemical agents, medicine, and IR spectroscopy. Fluorescent materials based on holmium (Ho <sup>3+</sup> )-doped crystals and glasses with narrow phonon spectra cover a wide wavelength range between approximately 1–4 μm. In this work, spectroscopic characterization of the IR emission properties of trivalent Ho <sup>3+</sup> -doped barium fluoride (BaF <sub>2</sub> ) was explored. BaF <sub>2</sub> is particularly attractive due to its low maximum phonon energy of approximately 330 cm <sup>-1</sup> , which leads to low nonradiative decay rates and efficient IR fluorescence. The studied Ho <sup>3+</sup> -doped BaF <sub>2</sub> material was grown by the Bridgman technique. Using approximately 890-nm excitation, IR emissions centered at approximately 2.0, 2.85, and 3.90 μm were observed from Ho <sup>3+</sup> :BaF <sub>2</sub> corresponding to the 5I7→5I8, 5I6→5I7, and 5I5→5I6 transitions of Ho <sup>3+</sup> ions. Spectroscopic results and data modeling including Judd–Ofelt analysis, transitions cross sections, and fluorescence dynamics are discussed.					
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## 1. Introduction

The mid-IR region has recently been a focus area for solid-state laser development because of its uniquely high 3- to 5- $\mu\text{m}$  transmittance through air, as shown in Fig. 1.<sup>1-6</sup> The region overlaps with the energies of the vibrational modes of molecules, and has a variety of applications for environmental monitoring and chemical detection, as well as potential applications in remote sensing of biochemical agents, medicine, and IR spectroscopy. Some applications for mid-IR lasers include free-space communication and remote sensing of trace gases and vapors for pollution detection, as well as blood and breath analysis.

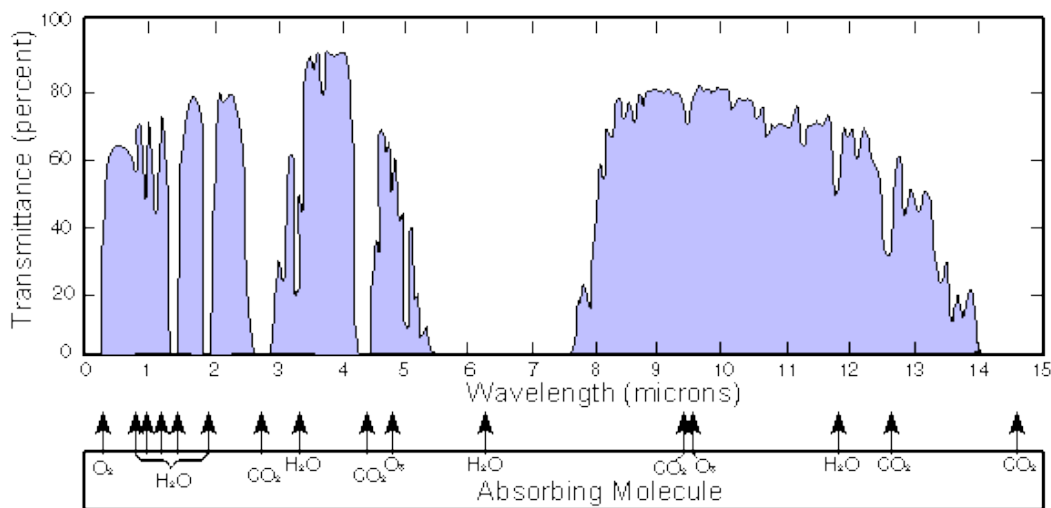


Fig. 1 Transmittance of the atmosphere

The development of rare-earth (RE)-doped host materials with low maximum phonon energies has attracted a great deal of interest for applications in solid-state lasers.<sup>1-7</sup> This is due to the reduced multiphonon relaxation rates that such host materials provide, which lead to higher laser emission efficiencies. Fluorites (calcium fluoride [CaF<sub>2</sub>], strontium fluoride [SrF<sub>2</sub>], and barium fluoride [BaF<sub>2</sub>]) are laser hosts of interest due to their low phonon energies, high thermal conductivities, and compatibility with RE dopants.<sup>8-12</sup> The trivalent RE holmium (Ho<sup>3+</sup>) ion is a favorable optically active center for applications in solid-state gain media. Laser oscillation and mid-IR emission properties from Ho<sup>3+</sup>-doped crystals have been observed in the mid-IR wavelength region at approximately 3.9  $\mu\text{m}$  due to the transition between the <sup>5</sup>I<sub>5</sub> and <sup>5</sup>I<sub>6</sub> state of Ho<sup>3+</sup> ions.<sup>1,13,14</sup> More recently, the enhancement of 3.9- $\mu\text{m}$  emission from Ho<sup>3+</sup> through thulium (Tm<sup>3+</sup>) sensitization has been reported in BaF<sub>2</sub> via approximately 800-nm excitation.<sup>12</sup>

In this work, we present results of spectroscopic investigations of mid-IR (3–5  $\mu\text{m}$ ) emission properties of  $\text{Ho}^{3+}:\text{BaF}_2$  crystals. The Judd–Ofelt (J-O) theory was applied to estimate the radiative rates, radiative lifetimes, and branching ratios for the main IR transitions. The emission cross sections were determined for the several emission bands of interest for IR laser applications.

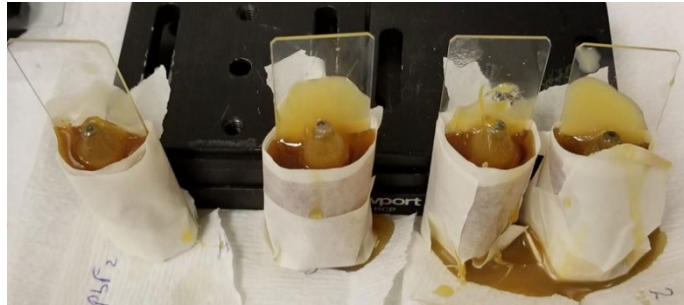
## 2. Experimental Details

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### 2.1 Material Processing and Physical Properties

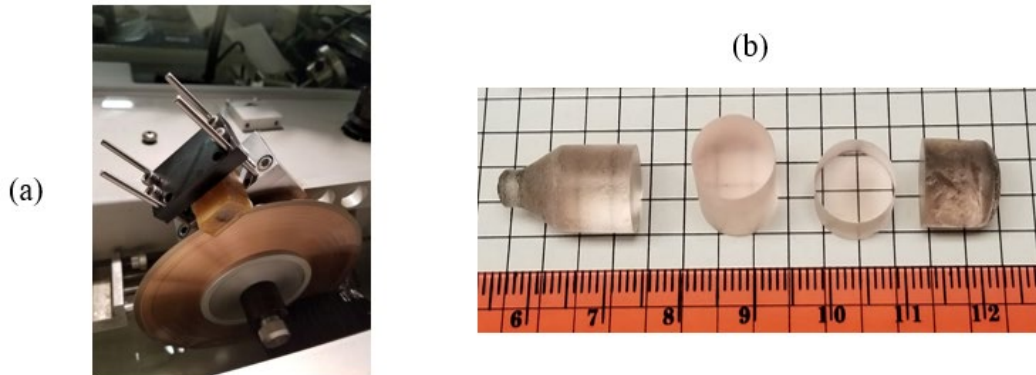
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The studied  $\text{Ho}^{3+}$ -doped  $\text{BaF}_2$  crystals were 5-cm-long cylindrical boules that were grown by the Bridgman technique. There were various  $\text{Ho}^{3+}$  concentrations in the  $\text{BaF}_2$  samples, which were approximately 5.6 mm thick and 1 cm in diameter. Waxing and cutting of the investigated samples was performed prior to spectroscopic measurements. To cut the samples, mounting wax was melted on a glass slide and the boule was placed on the wax before it hardened. After the boule was firmly set on the glass slide, a cup of wax was melted to pour into a housing created by wrapping masking tape around the glass slide. The masking tape left approximately 1 cm of space around the boule, as illustrated in Fig. 2. Once the wax hardened, the tape was removed and, in an attempt to make the wax into a rectangular figure, the wax was melted on a hot plate on all sides until a rectangle was created.



**Fig. 2**  $\text{Ho}^{3+}:\text{BaF}_2$  boules cooling in the wax casing for processing

Then, the sample was cut by a diamond saw (Fig. 3a) at a slow rate to ensure that the boule would not break or crack. After this process, the cut sample was polished by hand on silicon carbide polishing discs starting with 30- $\mu\text{m}$  grit and working down to eventually using a 1- $\mu\text{m}$ -grit disc. This ensures that the sample is fully transparent on the surface and there are no rough spots that could cause undesired scattering. Figure 3b shows the image of  $\text{Ho}^{3+}:\text{BaF}_2$  crystals that were cut and polished.



**Fig. 3** a) Diamond saw cutting through the sample and b)  $\text{Ho}^{3+}:\text{BaF}_2$  samples cut and polished

$\text{BaF}_2$  has a cubic crystal structure with a space group symmetry of  $\text{Fm}\bar{3}\text{m}$ . The unit cell parameter is  $a = 0.62 \text{ nm}$  and the number of molecules per unit cell is  $Z = 4$ .<sup>11,12</sup>  $\text{BaF}_2$  has the density of  $4.89 \text{ g/cm}^3$ . It can be assumed that RE ions are incorporated into the divalent  $\text{Ba}^{2+}$  lattice sites, which require a charge compensation mechanism. It was reported that, for RE doped into fluorites,<sup>11,12,15</sup> the charge is compensated for by an interstitial fluorine ion at the nearest neighbor position of  $\text{C}_{3v}$  symmetry. Some of the physical properties of  $\text{BaF}_2$  crystal are listed in Table 1.<sup>11,12</sup>

**Table 1** Physical characteristics of  $\text{BaF}_2$  crystal

Properties	$\text{BaF}_2$
Transparency	0.2–14 $\mu\text{m}$
Refractive index	1.475
Thermal conductivity	$6 \text{ Wm}^{-1}\text{K}^{-1}$
Thermal expansion coefficient	$18.1 \cdot 10^{-6}/\text{K}$
Maximum phonon energy	$\sim 330 \text{ cm}^{-1}$

## 2.2 Spectroscopic Measurements

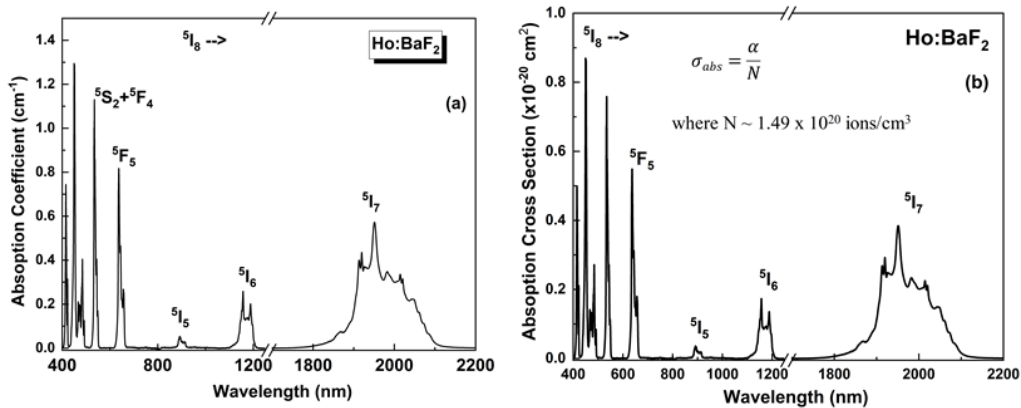
Room-temperature absorption spectra were recorded using a Cary 6000i UV-visible (Vis)-near IR spectrophotometer and a Nicolet 6700 Fourier transform IR spectrometer. All mid-IR fluorescence spectra were excited by a continuous-wave Spectra-Physics Tsunami titanium (Ti):sapphire laser (800–905 nm). Either a Horiba Fluorolog-3 system with an iHR-320 monochromator ( $\lambda_{\text{blaze}}$ : 2  $\mu\text{m}$ , 300 grooves/mm) or a Princeton Instruments Acton SpectraPro 0.15-m monochromator ( $\lambda_{\text{blaze}}$ : 4  $\mu\text{m}$ , 150 grooves/mm) was used to collect the mid-IR emissions. The emission signal was recorded by an Infrared Associates liquid-nitrogen-cooled indium antimonide detector in conjunction with a Stanford Research Systems SR830 dual-phase lock-in amplifier. Fluorescence decay

measurements were carried out using the output of a pulsed (10-ns pulses, 10 Hz) neodymium (Nd): yttrium aluminum garnet (YAG) pumped optical parametric oscillator (OPO) system. The decay signal was recorded with a homemade LabVIEW program using National Instruments data acquisition system. For temperature-dependent emission studies down to 77 K, the sample was mounted on the cold finger of a two-stage, closed-cycle helium refrigerator.

### 3. Results and Discussion

#### 3.1 Absorption Spectra and Judd–Ofelt Analysis

The room-temperature absorption spectrum of  $\text{Ho}^{3+}:\text{BaF}_2$  in the 400- to 2200-nm region is shown in Fig. 4a. The absorption cross section was calculated using a  $\text{Ho}^{3+}$  concentration of approximately  $1.49 \times 10^{20} \text{ cm}^{-3}$  for the  $\text{Ho}^{3+}:\text{BaF}_2$  crystal, as measured by Galbraith Laboratory, Inc., using inductively coupled plasma optical emission spectroscopy (ICP-OES) (Fig. 4b). The characteristic absorption bands of  $\text{Ho}^{3+}$  ions were centered at approximately 1970, 1167, 899, 643, 538, 485, 470, 450, and 416 nm. The average absorption wavelengths were determined using the relation  $\langle \lambda \rangle = \int \lambda \alpha(\lambda) d\lambda / \int \alpha(\lambda) d\lambda$ , where  $\alpha(\lambda)$  is the absorption coefficient as a function of wavelength.



**Fig. 4** a) Room-temperature absorption spectra of  $\text{Ho}^{3+}:\text{BaF}_2$  in the 400- to 2200-nm spectral region. Intra-4f absorption bands from the  $^5\text{I}_8$  ground state to higher excited states of  $\text{Ho}^{3+}$  are indicated. b) Absorption cross-section spectra of a  $\text{Ho}^{3+}:\text{BaF}_2$  crystal.

The J-O theory allows the calculation of RE transition strengths and radiative rates of the levels from measured absorption spectra.<sup>16,17</sup> Nine absorption bands lying between 415 and 1970 nm were selected for evaluation of the three  $\Omega_i$  parameters, known as the J-O intensity parameters. The intensities of the transitions can be distinguished by their line strength,  $S$ , for of each  $SLJ$  state. The experimentally

determined electric dipole transitions can be related to the integrated absorption coefficient by the following expression:

$$S_{meas}^{ed}(J \rightarrow J') = \frac{3hc(2J+1)}{8\pi^3 e^2 N_{RE} \lambda} \frac{9n}{(n^2+2)^2} \int \alpha(\lambda) d\lambda, \quad (1)$$

where  $J$  and  $J'$  are the total angular momentum of the initial and final states, respectively;  $h$  is Planck's constant;  $c$  is the speed of light;  $e$  is the electron charge;  $n$  is refractive index;  $N_{RE}$  is the concentration of  $\text{Ho}^{3+}$  ions in the crystal;  $\lambda$  is the mean wavelength of the absorption band; and  $\int \alpha(\lambda) d\lambda$  is the integrated absorption coefficient.

The J-O intensity parameters  $\Omega_t$  ( $t = 2, 4, 6$ ) can be obtained by a least-squares fitting of the measured line strength to the calculated line strength of the corresponding transitions between  $J$  and  $J'$  manifolds in the following equations:

$$S_{calc}^{ed}(J \rightarrow J') = \sum_{t=2,4,6} \Omega_t \left\langle \left\| (S, L)J \left\| U^{(t)} \right\| (S', L')J' \right\rangle \right|^2, \quad (2)$$

$$S_{calc}^{md}(J \rightarrow J') = \left( \frac{\hbar}{2mc} \right)^2 \left\langle \left\| 4f^n[S, L]J \left\| L + 2S \right\| 4f^n[S', L']J' \right\rangle \right|^2 \quad (3)$$

where  $\left\langle \left\| U^{(t)} \right\| \right\rangle$  are the doubly reduced matrix elements of the unit tensor.

The average transition wavelengths, integrated absorption coefficients, and experimental and calculated line strengths for  $\text{Ho}^{3+}:\text{BaF}_2$  are presented in Table 2. The resulting values for the J-O parameters are  $\Omega_2 = 0.293 \times 10^{-20} \text{ cm}^2$ ,  $\Omega_4 = 1.763 \times 10^{-20} \text{ cm}^2$ , and  $\Omega_6 = 1.47 \times 10^{-20} \text{ cm}^2$ . The obtained J-O intensity parameters are within the range of values reported for other  $\text{Ho}^{3+}$ -doped fluoride materials (Table 3).<sup>18-21</sup> The root-mean-square (rms) deviation between measured and calculated electric dipole line strengths was determined using the following expression:

$$rms = \sqrt{\sum_{i=1}^N \frac{(S_{meas}^{ed} - S_{calc}^{ed})^2}{N-3}}, \quad (4)$$

where  $N$  is the number of absorption bands taken into account. The rms error was calculated to be approximately  $0.19 \times 10^{-20} \text{ cm}^2$ , which is comparable to other rms values reported for  $\text{Ho}^{3+}$ -doped crystals.<sup>18-21</sup>

**Table 2** Integrated absorption coefficients, measured, and calculated line strengths of  $\text{Ho}^{3+}:\text{BaF}_2$

Transitions	Average wavelength	Transitions	Average wavelength	Transitions
$^5\text{I}_7$	1969.86	60.55	2.7	2.48
$^5\text{I}_6$	1167	9.467	0.737	1.087
$^5\text{I}_5$	898.78	1.245	0.126	0.154
$^5\text{F}_5$	642.86	11.318	1.599	1.59
$^5\text{F}_4+^5\text{S}_2$	537.63	10.345	1.748	1.798
$^5\text{F}_3$	484.65	2.786	0.522	0.508
$^3\text{K}_8$	470.22	2.239	0.433	0.297
$^5\text{F}_1+^5\text{G}_6$	449.86	10.57	2.135	2.138
$^5\text{G}_5$	416.56	4.47	0.976	0.779

**Table 3** J-O intensity parameters for  $\text{Ho}^{3+}$ -doped fluoride crystals

Host	$\Omega_2$ ( $10^{-20} \text{ cm}^2$ )	$\Omega_4$ ( $10^{-20} \text{ cm}^2$ )	$\Omega_6$ ( $10^{-20} \text{ cm}^2$ )	$\delta$ ( $10^{-20} \text{ cm}^2$ )	Reference no.
Ho:BaF <sub>2</sub>	0.298	1.784	1.491	0.19	<b>This study</b>
Ho:CaF <sub>2</sub>	0.018	0.57	0.587	...	18
Ho:LaF <sub>3</sub>	1.03	0.98	0.31	...	19
Ho:YLiF <sub>4</sub>	0.96	2.05	1.43	0.18	20
Ho:LuLiF <sub>4</sub>	1.238	2.214	2.111	0.108	21
Ho:GdLiF <sub>4</sub>	1.289	2.309	2.211	0.117	21

Note: La = lanthanum, Y = yttrium, Lu = lutetium, Gd = gadolinium.

Using the obtained emission line strengths, the radiative transition probabilities  $A$  ( $J \rightarrow J'$ ) can be determined by the following equations:

$$A(J \rightarrow J') = \frac{64\pi^4 e^2}{3h(2J+1)} \left[ \frac{n(n^2+2)^2}{9\lambda^3} S_{calc}^{ed}(J \rightarrow J') + n^3 S_{calc}^{md}(J \rightarrow J') \right], \quad (5)$$

$$A_t(J) = \sum_{J'} A(J \rightarrow J') \quad (6)$$

where  $A_t(J)$  is the total transition rate for a given J-manifold.

The radiative lifetime,  $\tau_{rad}$ , is related to the radiative decay rate through

$$\tau_{rad} = \frac{1}{A_t(J)}. \quad (7)$$

Accordingly, the branching ratio,  $\beta$ , for the transition from an emitting level to a lower level is given by

$$\beta(J') = \frac{A(J \rightarrow J')}{A_r(J)}. \quad (8)$$

The radiative transition rates, branching ratios, and radiative and measured lifetimes are presented in Table 4. The emission cross sections were calculated using Füchtbauer–Ladenburg (F-L) equation<sup>22</sup>:

$$\sigma_{emiss}(\lambda) = \frac{\beta \lambda^5 I(\lambda)}{8\pi n^2 c \tau_{rad} \int \lambda I(\lambda) d\lambda} \quad (9)$$

where  $\beta$  and  $\tau_{rad}$  are the branching ratio and radiative lifetime, respectively.  $I(\lambda)$  is the emission intensity at wavelength  $\lambda$  and  $n$  is the refractive index of the host ( $n = 1.47$ ).

**Table 4** Calculated radiative transition probabilities ( $A_{ij}$ ), branching ratios ( $\beta_{ij}$ ), radiative ( $\tau_{meas}$ ), and measured ( $\tau_{meas}$ ) lifetimes of  $\text{Ho}^{3+}:\text{BaF}_2$

Transitions	(nm)	$A_{ij}$ ( $\text{s}^{-1}$ )	$\beta_{ij}$	$\tau_{rad}$ (ms)	$\tau_{meas}$ (ms)
${}^5\text{I}_7 \rightarrow {}^5\text{I}_8$	2010	48.06	1	20.8	17.0
${}^5\text{I}_6 \rightarrow {}^5\text{I}_7$	2850	11.17	0.098	...	...
${}^5\text{I}_6 \rightarrow {}^5\text{I}_8$	1190	103.4	0.902	8.73	6.8
${}^5\text{I}_5 \rightarrow {}^5\text{I}_6$	3900	3.69	0.037	...	...
${}^5\text{I}_5 \rightarrow {}^5\text{I}_7$	1650	56.81	0.571	...	...
${}^5\text{I}_5 \rightarrow {}^5\text{I}_8$	910	38.93	0.392	10.05	0.026

## 3.2 Infrared Emission Studies

### 3.2.1 2 $\mu\text{m}$ Emission

The  $\text{Ho}^{3+}:\text{BaF}_2$  crystal exhibited broad emission band centered at approximately 2  $\mu\text{m}$  ( ${}^5\text{I}_7 \rightarrow {}^5\text{I}_8$ ) with a bandwidth of approximately 0.14  $\mu\text{m}$  at full width at half maximum (Fig. 5). Following optical pumping at 0.89  $\mu\text{m}$ , the room-temperature emission decay transient was nearly exponential with a lifetime value of approximately 17 ms. Using the J-O analysis, the radiative lifetime of the  ${}^5\text{I}_7$  level was calculated to be approximately 20.8 ms, which is in good agreement with the calculated radiative lifetime (19.94 ms) obtained by Einstein's relationship,<sup>23</sup>

$$\tau_{calc} = \frac{\lambda^2}{8\pi c n^2} \left[ \frac{g_1}{g_2} \int \sigma_{abs} d\bar{\nu} \right]^{-1} \quad (10)$$

where  $\sigma_{\text{abs}}$  is the absorption cross section (Fig. 5),  $\lambda$  is the average absorption wavelengths,  $c$  is the speed of light,  $n$  is the index of refraction, and  $g_1$  and  $g_2$  are the ground and excited state degeneracies, respectively.

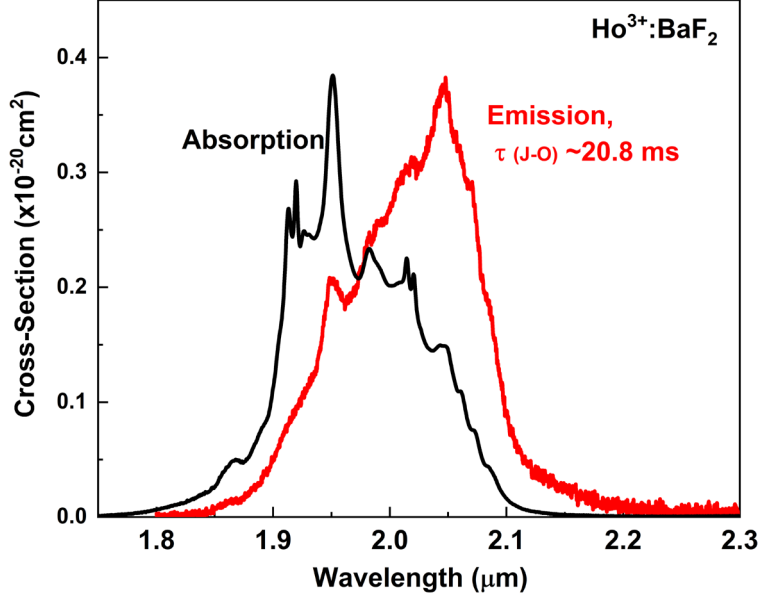


Fig. 5 Absorption and emission cross-section spectra of  ${}^5\text{I}_7 \rightarrow {}^5\text{I}_8$  transition for  $\text{Ho}^{3+}:\text{BaF}_2$

The small difference in the experimental (measured) lifetime and calculated radiative lifetime of the  ${}^5\text{I}_7$  could be due to radiation trapping in the investigated  $\text{Ho}^{3+}:\text{BaF}_2$  sample. Using the available spectroscopic data and radiative lifetime derived from a J-O analysis, the emission cross section of the  ${}^5\text{I}_7 \rightarrow {}^5\text{I}_8$  emission transition was calculated for  $\text{Ho}^{3+}:\text{BaF}_2$  using the F-L method (Eq. 9).<sup>22</sup> The peak emission cross section was determined to be approximately  $0.38 \times 10^{-20} \text{ cm}^2$ , which is slightly smaller than  $\text{Ho}^{3+}:\text{YLiF}_4$  ( $\text{Ho}^{3+}:\text{YLF}$ )<sup>24</sup> and  $\text{Ho}^{3+}:\text{BaY}_2\text{F}_8$  ( $\text{Ho}^{3+}:\text{BYF}$ )<sup>1</sup> (Table 5); however, it was comparable to the reported value of approximately  $0.39 \times 10^{-20} \text{ cm}^2$  for  $\text{Ho}^{3+}:\text{LaF}_3$ .<sup>19</sup> Due to the quasi three-level nature of a potential approximately 2- $\mu\text{m}$  laser based on the  ${}^5\text{I}_7 \rightarrow {}^5\text{I}_8$   $\text{Ho}^{3+}$  transition, a net gain cross section  $g(\lambda)$  can be calculated considering possible ground-state absorption losses at the laser wavelength<sup>25</sup>:

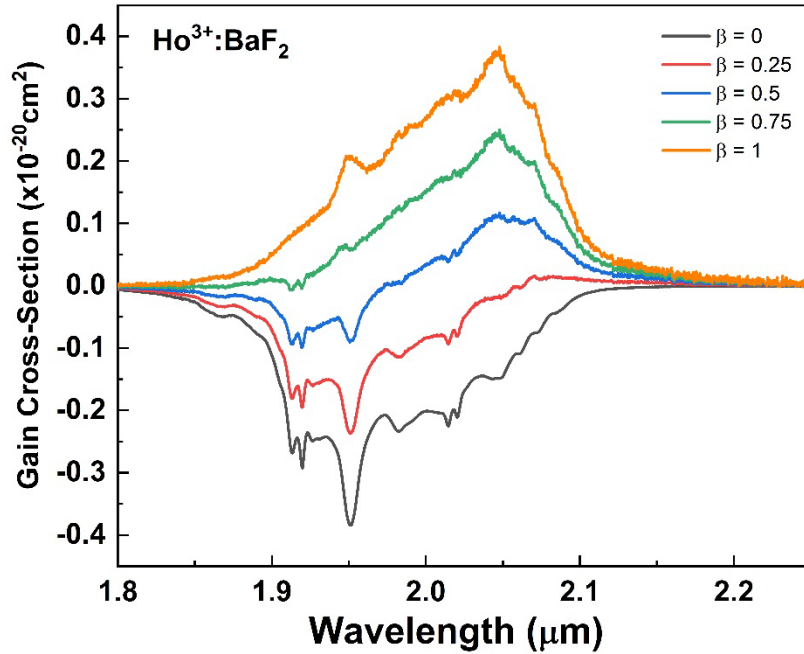
$$g(\lambda) = \beta\sigma_{\text{emis}}(\lambda) - (1 - \beta)\sigma_{\text{abs}}(\lambda) \quad (11)$$

where  $\beta = N_{\text{exc}}/N_{\text{tot}}$  is the ratio of the number of excited  $\text{Ho}^{3+}$  ions relative to the total  $\text{Ho}^{3+}$  ion population, and  $\sigma_{\text{emis}}$  and  $\sigma_{\text{abs}}$  are the emission and absorption cross sections, respectively. The obtained gain cross-section spectra for  $\beta = 0, 0.25, 0.5, 0.75,$  and  $1$  are illustrated in Fig. 6. It can be noticed that nearly 25% population inversion is needed for  $\text{Ho}^{3+}:\text{BaF}_2$  to achieve a positive gain at the longer wavelengths above 2.06  $\mu\text{m}$ .

**Table 5** Comparison of  $\text{Ho}^{3+}:\text{BaF}_2$  and other  $\text{Ho}^{3+}$ -doped fluorides for emission cross sections, and radiative and measured lifetimes

Crystal	$\lambda_{\text{em}} (\mu\text{m})$	$\sigma_{\text{em}} (\lambda)$ ( $10^{-20} \text{ cm}^2$ )	$\tau_{\text{rad}}$ (ms)	$\tau_{\text{meas}}$ (ms)	$\sigma \cdot \tau$ ( $10^{-20} \text{ cm}^2 \cdot \text{ms}$ )
$\text{Ho}:\text{BaF}_2$	2.04	0.38	20.8	16.7	...
$\text{Ho}:\text{YLF}$ (Walsh et al. <sup>24</sup> )	2.06	0.75	13.9	14.0	...
$\text{Ho}:\text{BYF}$ (Eichhorn <sup>1</sup> )	2.06	1.18	...	17.9	...
$\text{Ho}:\text{LaF}_3$ (Hong et al. <sup>19</sup> )	1.93	0.39	25.16	25.81	...
$\text{Ho}:\text{BaF}_2$	2.84	0.57	8.73	6.8	$\sim 3.9$
$\text{Ho}:\text{BYF}$ (Eichhorn <sup>1</sup> )	2.85	0.28	...	5.45	$\sim 1.5$
$\text{Ho}:\text{LaF}_3$ (Hong et al. <sup>19</sup> )	2.85	0.63	18.99	10.37	$\sim 6.5$
$\text{Ho}:\text{BaF}_2$	3.89	0.76	10.05	0.028	$\sim 0.02$
$\text{Ho}:\text{BYF}$ (Eichhorn <sup>1</sup> )	3.89	$\sim 1.5$	...	0.052	$\sim 0.08$

Note: YLF = yttrium lithium fluoride, BYF = barium yttrium fluoride,  $\text{LaF}_3$  = lanthanum trifluoride



**Fig. 6** Gain cross-section spectra of the 2- $\mu\text{m}$  transition in  $\text{Ho}^{3+}:\text{BaF}_2$  for different population inversion ratios ( $\beta = 0, 0.25, 0.5, 0.75,$  and  $1$ )

### 3.2.2 2.8- and 3.9- $\mu\text{m}$ Emissions

Figure 7 shows the room-temperature mid-IR emission spectra of the  $\text{Ho}^{3+}:\text{BaF}_2$  crystal upon excitation at  $0.89 \mu\text{m}$  using a Ti:sapphire laser. The spectra exhibited two emission bands centered at approximately  $2.85$  and  $3.9 \mu\text{m}$ , which are attributed to the  $\text{Ho}^{3+} {}^5\text{I}_6 \rightarrow {}^5\text{I}_7$  and  ${}^5\text{I}_5 \rightarrow {}^5\text{I}_6$ , respectively. A schematic diagram of the relevant lower  $\text{Ho}^{3+}$  levels indicating the excited transition and observed emission lines is shown in Fig. 7. The emission spectra were calibrated for the

experimental setup. It could be seen that both the approximately 2.85- and 3.9- $\mu\text{m}$  emission bands were relatively broad ranging from 2.75 to 3.05  $\mu\text{m}$  and 3.8 to 4.0  $\mu\text{m}$ , respectively.

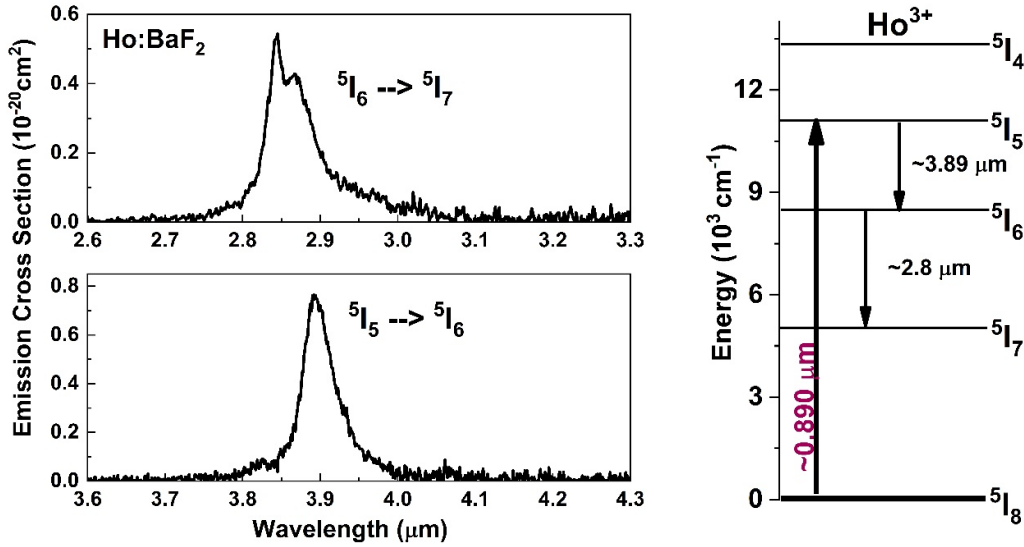
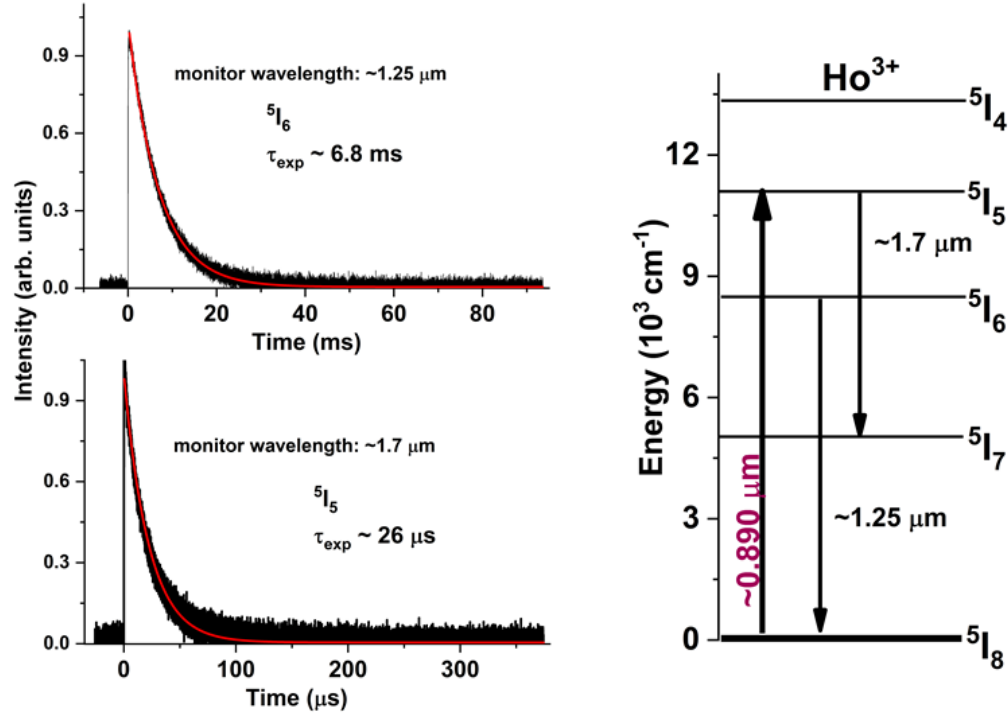


Fig. 7 Emission cross-section spectra of  ${}^5I_6 \rightarrow {}^5I_7$  and  ${}^5I_5 \rightarrow {}^5I_6$  transitions for the  $\text{Ho}^{3+}:\text{BaF}_2$  crystal. The partial energy-level diagram of  $\text{Ho}^{3+}$  indicating the excitation level and the corresponding emission transitions is also shown on the right.

The decay transients of the  ${}^5I_5$  and  ${}^5I_6$  level were determined by using 891-nm excitation of pulsed Nd:YAG-pumped OPO system and can be seen in Fig. 8. The lifetime of the  ${}^5I_6$  level was determined to be approximately 6.8 ms, which agrees reasonably well with the radiative lifetime of 8.73 ms determined by J-O analysis (see Table 4). The emission lifetime of the  ${}^5I_5$  energy level exhibited a significantly shorter lifetime of approximately 26  $\mu\text{s}$ . The observed  ${}^5I_5$  level lifetime was similar to the reported value of 17.5  $\mu\text{s}$  for 1%  $\text{Ho}^{3+}:\text{BaF}_2$  and 28  $\mu\text{s}$  for low concentration 0.35%  $\text{Ho}^{3+}:\text{BaF}_2$ .<sup>12</sup> J-O analysis yielded a radiative lifetime of 10.05 ms for the  ${}^5I_5$  state, which suggests a quantum efficiency of less than 1% at room temperature. Such a low efficiency could be attributed to nonradiative decay processes such as multiphonon relaxations, energy transfer between RE ions, or energy transfer to other impurities in the crystal. The temperature dependence of the  ${}^5I_5$  level decay time measurements are in progress in order to determine the multiphonon relaxation rate, which could be the most likely process for the reduced radiative emission efficiency. The shorter lifetime of the  ${}^5I_5$  energy level makes it difficult for population inversion to occur unless high amounts of energy are pumped into the crystal or a higher  $\text{Ho}^{3+}$  concentration is achieved to increase absorption at the pump wavelength. However, pulsed laser operation at 3.9  $\mu\text{m}$  has been demonstrated with  $\text{Ho}^{3+}:\text{BaY}_2\text{F}_8$ , which has a maximum phonon energy less than 500  $\text{cm}^{-1}$ .<sup>13</sup>



**Fig. 8** Decay transients of  $\text{Ho}^{3+}:\text{BaF}_2$  monitored at approximately  $1.7 \mu\text{m}$  ( ${}^5\text{I}_5 \rightarrow {}^5\text{I}_7$ ) and  $1.25 \mu\text{m}$  ( ${}^5\text{I}_6 \rightarrow {}^5\text{I}_8$ ) for room temperature. The partial energy-level diagram of  $\text{Ho}^{3+}$  indicating the pump level and the measured emission transitions is also depicted on the right.

The mid-IR emission cross-section spectra for  $\text{Ho}^{3+}:\text{BaF}_2$  is expressed in Fig. 7 and the peak emission cross sections at  $2.84$  and  $3.9 \mu\text{m}$  were determined to be  $0.57 \times 10^{-20}$  and  $0.76 \times 10^{-20} \text{ cm}^2$ , respectively. The sigma-tau ( $\sigma\text{-}\tau$ ) product is an important parameter to characterize laser materials since its value is inversely proportional to the laser threshold under continuous wave excitation.<sup>26</sup> The resulting  $\sigma\text{-}\tau$  product for  $2.8\text{-}$  and  $3.9\text{-}\mu\text{m}$  transition were calculated to be approximately  $3.9 \times 10^{-20}$  and  $0.02 \times 10^{-20} \text{ cm}^2\cdot\text{ms}$ , respectively. These emission cross sections and  $\sigma\text{-}\tau$  product are comparable to other Holmium doped fluorides, as shown in Table 5.

The  $\text{Ho}^{3+}$ -doped BYF crystal shown in the table has demonstrated pulsed laser operation at  $3.9 \mu\text{m}$ <sup>13</sup> using high  $\text{Ho}^{3+}$  concentration (30%  $\text{Ho}^{3+}:\text{BYF}$ ). Comparing the samples, it could be possible to use a sample of  $\text{Ho}^{3+}:\text{BaF}_2$  as a possible lasing material especially because the sample studied in this experiment was merely 3%  $\text{Ho}^{3+}$ .

The  $3.9\text{-}\mu\text{m}$  emission arising from the  ${}^5\text{I}_5$  to  ${}^5\text{I}_6$   $\text{Ho}^{3+}$  transition is a potential four-level laser system. As mentioned earlier, the most important requirement for laser emission is population inversion, which can only be maintained for a possible  $3.9\text{-}\mu\text{m}$  laser if the  ${}^5\text{I}_5$  level has a longer lifetime than the  ${}^5\text{I}_6$  level. Figure 8 proved

that is not the case, since the  $^5I_6$  level has a lifetime of 6.8 ms. This makes the continued population inversion rather difficult, as it results in bottlenecks or self-termination. This problem might be overcome through co-doping with a proper sensitizer ion (e.g.,  $Nd^{3+}$ ), which could provide an efficient excitation passage using its 808-nm absorption band. A schematic diagram of energy levels for  $Ho^{3+}$  and  $Nd^{3+}$  indicating the energy transfer process is illustrated in Fig. 9.<sup>27</sup> Overall, the observed spectroscopic parameters for  $Ho^{3+}:BaF_2$  suggested that it could be a possible lasing candidate for mid-IR laser applications.

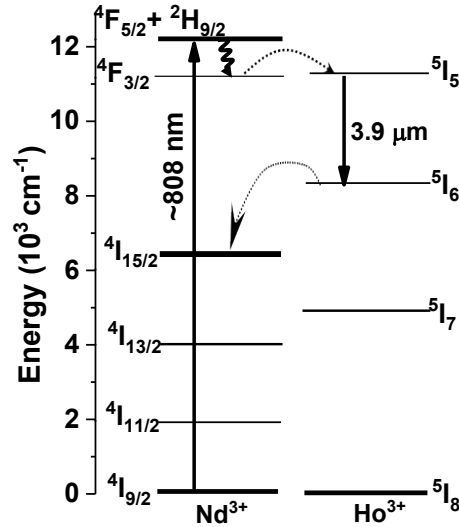


Fig. 9 A schematic diagram of energy levels for  $Ho^{3+}$  and  $Nd^{3+}$  indicating the energy transfer process

#### 4. Conclusions

Preliminary results of the material preparation and IR spectroscopic properties of  $Ho^{3+}$ -doped  $BaF_2$  crystals, grown by the Bridgman technique, were presented. The absorption spectrum of  $Ho^{3+}:BaF_2$  displayed the characteristic  $Ho^{3+}$  transitions in the visible and IR spectral region. The J-O theory was applied and the J-O intensity parameters, radiative probabilities, branching ratios as well as radiative lifetimes were determined. Optical pumping into the  $^5I_8 \rightarrow ^5I_5$  absorption band at approximately 800 nm resulted in the observation of several mid-IR  $Ho^{3+}$  fluorescence bands, which corresponds to the  $^5I_7 \rightarrow ^5I_8$  ( $\sim 2 \mu m$ ),  $^5I_6 \rightarrow ^5I_7$  ( $\sim 2.8 \mu m$ ), and  $^5I_5 \rightarrow ^5I_6$  ( $\sim 3.89 \mu m$ ) transitions. The room-temperature fluorescence lifetimes of the first three excited states of  $Ho^{3+}:BaF_2$  were determined to be approximately 17 ms ( $^5I_7$ ), 6.8 ms ( $^5I_6$ ), and 0.026 ms ( $^5I_5$ ).

Using the J-O modeling and F-L method, the IR peak emission cross sections of approximately 2, 2.8, and 3.9  $\mu m$  were determined to be  $0.38 \times 10^{-20}$ ,

$0.57 \times 10^{-20}$ , and  $0.76 \times 10^{-20} \text{ cm}^2$ , respectively. The comparison of the absorption and emission cross sections for the  ${}^5\text{I}_7 \rightarrow {}^5\text{I}_8$  transition indicates the possibility for a broadly tunable laser covering a region from approximately 2.0  $\mu\text{m}$  to approximately 2.2  $\mu\text{m}$ . The 2- $\mu\text{m}$  gain cross-section spectra revealed that nearly 25% population inversion is required for  $\text{Ho}^{3+}:\text{BaF}_2$  to achieve a positive gain at the long wavelength region between approximately 2.06 and 2.1  $\mu\text{m}$ .

The emission cross section and long lifetime of 2.8  $\mu\text{m}$  give  $\text{Ho}^{3+}:\text{BaF}_2$  a large  $\sigma\text{-}\tau$  product ( $\sim 3.9 \times 10^{-20} \text{ cm}^2\cdot\text{ms}$ ), which is almost three times higher than the values reported for the known laser material  $\text{Ho}^{3+}:\text{BYF}$  crystal.<sup>1</sup> The obtained spectroscopic parameters for 2.8- $\mu\text{m}$  emission compare favorably with other  $\text{Ho}^{3+}$ -doped fluorides, which underlines the potential of this material for 3- $\mu\text{m}$  laser applications.

The 3.9- $\mu\text{m}$  emission ( ${}^5\text{I}_5 \rightarrow {}^5\text{I}_6$  transition) revealed a reasonably high emission cross section; however, with a short lifetime of approximately 0.026 ms. The longer lifetime of the lower excited state  ${}^5\text{I}_6$ , restricts the capability to effectively invert the population, therefore limiting the mode of operation of a potential  $\text{Ho}^{3+}:\text{BaF}_2$  laser. It is found that the near-IR absorption at approximately 0.89  $\mu\text{m}$  is extremely weak in this crystal with an absorption cross section of approximately  $0.036 \times 10^{-20} \text{ cm}^2$ . These issues might be overcome through co-doping with a suitable sensitizer ion, for instance,  $\text{Nd}^{3+}$  or  $\text{Tm}^{3+}$  ions, which could provide an effective excitation channel using their approximately 800-nm absorption bands as well as efficient depopulation of the  ${}^5\text{I}_6$  level for possible population inversion.<sup>12,27</sup>

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## List of Symbols, Abbreviations, and Acronyms

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Ba	barium
BaF <sub>2</sub>	barium fluoride
BYF	barium yttrium fluoride
CaF <sub>2</sub>	calcium fluoride
F	fluorine
Gd	gadolinium
Ho	holmium
ICP-OES	inductively coupled plasma optical emission spectroscopy
InSb	indium antimonide
IR	infrared
J-O	Judd–Ofelt
La	lanthanum
LaF <sub>3</sub>	lanthanum trifluoride
Lu	lutetium
Nd	neodymium
NIR	near IR
OPO	optical parametric oscillator
RE	rare earth
SrF <sub>2</sub>	strontium fluoride
Ti	titanium
Tm	thulium
UV	ultraviolet
Vis	visible
Y	yttrium
YAG	yttrium aluminum garnet
YLF	yttrium lithium fluoride

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