



OPTIMIZING DESIGN PARAMETERS FOR  
ACTIVE FLOW CONTROL  
BOUNDARY-LAYER FENCE  
PERFORMANCE ENHANCEMENT  
ON A DELTA WING

THESIS

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AFIT-ENY-MS-21-M-322

DEPARTMENT OF THE AIR FORCE  
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Presented to the Faculty  
Department of Aeronautical and Astronautical Engineering  
Graduate School of Engineering and Management  
Air Force Institute of Technology  
Air University  
Air Education and Training Command  
in Partial Fulfillment of the Requirements for the  
Degree of Master of Science in Aeronautical Engineering

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March 2021

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## Abstract

Utilizing computational fluid dynamic (CFD) simulations, the presented study is able to further the investigation of replicating and improving upon the performance of a NACA 0012 cropped half-span delta-wing at high angles-of-attack with an active flow control fluidic fence via wall-normal, steady blowing from an optimized single chord-wise slot located at  $z/b = 70\%$ . The data is generated using CREATE-AV Kestrel v10.1rc5 CFD software on the Department of Defense High Performance Computing systems. The flight regime is held constant at a Mach number of 0.18 and a Reynolds number ( $Re$ ) of  $5.0 \times 10^5$ , based on the root chord. Computational solutions are successfully compared to previously obtained experimental wind tunnel results of three configurations; baseline, passive boundary-layer fence (BLF) and AFC slot of a single momentum coefficients ( $C_\mu = 0.49\%$ ), to validate the CFD model prior to slot optimization. Optimization parameters include five reduced slot widths, five slot velocities and eight slot length. Performance parameters compared for validation and optimization are coefficients of lift, drag and pitching moment at angles-of-attack ranging from  $0^\circ$  to  $30^\circ$ . Surface flow visualization was produced via Tecplot 360 to evaluate unique AFC flow characteristics. AFC slot optimization successfully produce an overall dimension reduction and reduction in momentum input of  $33\%$  when compared to the experimental result's highest  $C_\mu = 12\%$ . With these reductions, the optimal AFC slot configuration yielded a  $C_{Lmax,\%Gain} = 41\%$  at  $\alpha = 22^\circ$  compared to the baseline configuration. The optimal AFC slot configuration indicate no destabilizing pitching moment present. Visualization of the compared results show that the AFC slot allow for delay in vortex breakdown for some configurations which provide improved vortex generating lift across the wing surface at increasing angles-of-attack.

*Dedicated to my devoted wife. I give you all love and thankfulness. Without your continual, never-ending love and support, I would never have been able to accomplish my life goals and aspirations nor be the person I am today.*

## Acknowledgements

First and foremost, I have to praise God for giving me health, mental fortitude and physical abilities that have propelled me to this moment in life.

To my children, thank you for being the driving force for me to be the best example that I can be for you. Through my accomplishments, I hope you grow to see that with hard work and dedication you can achieve whatever you set your mind to.

To my parents and grandparents, thank you for instilling in me a love for God and family, and an incredible work ethic. I love you.

To my family, thank you for the complete understanding and never ending support given from afar. I cannot express my love for you enough.

To LtCol Michael Walker, Maj Shawn Naigle, AFIT faculty, staff and peers, thank you for sharing your knowledge and providing support throughout this work.

To all those outside of AFIT who provided top notch support, thank you. To name a few: Capt Matthew Clarey (AFRL/XP), Mr. Charles Lynch (CREATE-AV Kestrel) and a huge thanks to Dr. Brent Rankin (AFRL/RQTC), without your generosity, this task would have never been accomplish.

Finally, to Capt Luke Steinberg, thank you for the friendship that we have built and for the daily lunch sessions. Fishing will be lonely!

Nathan L. Tedder

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## List of Abbreviations, Acronyms and Symbols

|                  |                                      |
|------------------|--------------------------------------|
| $A$              | wing axial force (Fy)                |
| $AR$             | aspect ratio                         |
| $A_{slot}$       | slot area                            |
| $BR$             | blowing ratio                        |
| $C_D$            | coefficient of drag                  |
| $C_L$            | coefficient of lift                  |
| $C_M$            | pitching moment coefficient          |
| $C_p$            | compressible pressure distribution   |
| $C_{Lmax}$       | maximum coefficient of lift          |
| $C_\mu$          | momentum coefficient                 |
| $C_{p,0}$        | incompressible pressure distribution |
| $D$              | drag                                 |
| $L$              | lift                                 |
| $MAC$            | mean aerodynamic chord               |
| $N$              | wing normal force (Fx)               |
| $PM$             | wing pitching moment (Mz)            |
| $Re$             | Reynolds number                      |
| $S$              | wing planform area                   |
| $V_\infty$       | freestream velocity                  |
| $\alpha$         | angle-of-attack                      |
| $\bar{c}$        | wing mean chord                      |
| $\beta$          | Prandtl-Glauert Factor               |
| $\dot{V}$        | volumetric flow rate                 |
| $\dot{m}_{slot}$ | slot mass flow rate                  |

|                  |                                                                                      |
|------------------|--------------------------------------------------------------------------------------|
| $\rho_\infty$    | freestream density                                                                   |
| $b$              | wing half-span                                                                       |
| $c$              | speed of sound                                                                       |
| $c_{root}$       | wing root chord                                                                      |
| $c_{tip}$        | wingtip chord                                                                        |
| $y^+$            | initial cell wall spacing                                                            |
| <b>2D</b>        | two-dimensional                                                                      |
| <b>3D</b>        | three-dimensional                                                                    |
| <b>AD</b>        | Advective Damping                                                                    |
| <b>AFC</b>       | active flow control                                                                  |
| <b>AMR</b>       | adaptive mesh refinement                                                             |
| <b>BC</b>        | boundary conditions                                                                  |
| <b>BLF</b>       | boundary-layer fence                                                                 |
| <b>CAD</b>       | computer-aided design                                                                |
| <b>CFD</b>       | computational fluid dynamics                                                         |
| <b>CREATE-AV</b> | Computational Research Engineering Acquisition Tools and Environments – Air Vehicles |
| <b>DDES</b>      | Delayed-Detached Eddy Simulation                                                     |
| <b>DoD</b>       | Department of Defense                                                                |
| <b>ERDC</b>      | Engineering Research and Development Center                                          |
| <b>EX</b>        | slot extent (length)                                                                 |
| <b>FCV</b>       | finite control volume                                                                |
| <b>GPGPU</b>     | general-purpose graphic processing unit                                              |
| <b>GPU</b>       | graphic processing unit                                                              |
| <b>HPC</b>       | high performance computing                                                           |
| <b>IDDES</b>     | Improved Delayed-Detached Eddy Simulation                                            |

|               |                                                          |
|---------------|----------------------------------------------------------|
| <b>LES</b>    | large eddy simulation                                    |
| <b>LEV</b>    | leading-edge vortex                                      |
| <b>M</b>      | Mach                                                     |
| <b>MLA</b>    | Machine Learning Accelerator                             |
| <b>N-S</b>    | Navier-Stokes                                            |
| <b>NACA</b>   | National Advisory Committee for Aeronautics              |
| <b>PFLOPS</b> | peta ( $10^{15}$ ) floating points operations per second |
| <b>PIV</b>    | particle image velocimetry                               |
| <b>RANS</b>   | Reynolds Averaged Navier-Stokes                          |
| <b>RC</b>     | rotation correction                                      |
| <b>RCS</b>    | radar cross sections                                     |
| <b>S-A</b>    | Spalart-Allmaras                                         |
| <b>std</b>    | standard deviation                                       |
| <b>SW</b>     | slot width                                               |
| <b>TS</b>     | Time Step                                                |
| <b>UG</b>     | User's Guide                                             |

OPTIMIZING DESIGN PARAMETERS FOR ACTIVE FLOW CONTROL  
BOUNDARY-LAYER FENCE PERFORMANCE ENHANCEMENT  
ON A DELTA WING

## I. Introduction

### 1.1 Background and Motivation

When considering the lifting body geometry of a majority of modern fighter, low observable aircraft and blended wing body concepts, research on improved delta-wing aircraft performance characteristics is of significant interest. Particularly, addressing high angle-of-attack flow separation which leads to wing stall and/or reduced aerodynamic performance envelopes. A variety of flow control strategies have been devised in an attempt to postpone stall, improve lift performance and reduce undesirable moment characteristics.

Expanding in delta-wing performance envelopes without the use of geometric modifications that protrude into the airflow (avoiding creating increased radar cross sections (RCS) and drag) would be optimal. Initially, passive flow control methods such as winglets, boundary-layer trips and wing fences [1] were found to be effective at delaying flow separation within certain conditions and provide insight into swept wing stall reduction. Development of active flow control (AFC) strategies, such as fluidic oscillators [2], pulsed jets [3] and fluidic fences [4] provide similar performance enhancements with the ability to activate as needed while avoiding the undesired effects that geometry modifications create. However, additional energy expenditures are necessary for AFC operation, meaning the benefit must outweigh the cost.

Future development of modern aircraft tends to avoid performance enhancement solutions that would detract from stealth capabilities, specifically increased RCS, or contribute to unnecessary drag, especially above sonic speeds. Fortunately, the use of AFC techniques to replicate performance enhancements of passive flow control methods satisfy the requirements of future modern aircraft and provides a solution for flow separation leading to wing stall and undesirable moment characteristics. With the potential for an overall increase in performance at extreme flight envelopes, this development expands the trade space for future delta-wing configuration development.

## **1.2 Problem Statement**

The focus of the presented study is to further the investigation of replication and enhancement of a National Advisory Committee for Aeronautics (NACA) 0012 cropped delta-wing performance at high angles-of-attack using an active flow control wall-normal, steady blowing, fluidic fence from a single slot. Through the use of computational fluid dynamics (CFD) tools, fluidic performance solutions will be compared and validated against previously obtained experimental wind tunnel results. Furthermore, the study seeks to optimize the AFC slot configuration by maximizing AFC performance gains while minimizing required energy input.

## **1.3 Methodology**

Gathering data regarding the effects of high angle-of-attack ( $\alpha$ ) on any operational air asset in real-world scenarios is a challenging process. Testing within an airframe's stall region at low speeds can also prove to be potentially dangerous. However, CFD allows for these high-risk scenarios to be modeled and investigated without the risk and cost associated with experimental testing.

The CFD simulations used in this study were solved with the Computational

Research Engineering Acquisition Tools and Environments – Air Vehicles (CREATE-AV) software Kestrel v10.4rc5 and computed on the U.S. Army Engineering Research and Development Center (ERDC) high performance computing (HPC) systems. This software is widely used by the Department of Defense (DoD) aerospace community to generate data for various fixed wing aircraft scenarios. The wide range of uses and recommendations provide heightened level of confidence in the accuracy of results and robustness of the solver [5, 6]. The software also allows for the use of adaptive mesh refinement (AMR) which allows Kestrel to refine and coarsen the computational grid as necessary for more accurate distribution of computational resources as prescribed by the user.

Three configurations, based upon previous studies, will be modeled and compared to wind-tunnel performance results under similar conditions to determine CFD model accuracy. These configurations will all be based on a NACA 0012 cropped delta-wing with performance results attained from Demoret et al. for a baseline control, passive boundary-layer fence and an AFC fluidic fence. Furthermore, the AFC fluidic fence slot will be optimized under those same flow conditions. Performance characteristics will be quantified as changes in global forces and moments (specifically lift, drag and pitch). A more detailed discussion of the methodology can be found in Chapter III.

## **1.4 Assumptions and Limitations**

This investigation focuses on the ability of an AFC fluidic fence to improve performance of a delta wing. Limited AFC research has been accomplished with respect to swept wings and delta wings. Thus, the focus of the investigation centers around proof of concept and negates application and operational recommendation of the technology implementation.

The original experiment involved an internal chamber being filled from an external

pressurized air source and did not examine the feasibility of including a fluidic fence into a standard wing structure nor the air source within an operational aircraft (bleed air from the engine, ect.). Additionally, the study does not include details regarding how a fluidic fence would integrate into the stability and control system of the aircraft.

This investigation looks to utilize Demoret et al.'s delta-wing experimental results. For this reason, the same configuration was modeled with a relatively thick airfoil that may not directly be applicable to fourth- and fifth-generation delta-wing fighter aircraft. Additionally, the dimensions of the model and free-stream velocity corresponded to a Reynolds number of  $5.0 \times 10^5$ , while an fourth- and fifth-generation high-speed flight envelopes reach Reynolds numbers on the order of  $10^8$ .

## II. Literature Review

### 2.1 Wing Theory

#### 2.1.1 Straight Wing

While considering a symmetric airfoil configured as a straight wing at low speed, lift is generated as angle-of-attack increases due to a pressure differential between the low-pressure upper and high-pressure lower surfaces. The majority of lift is generated over the upper first third of the airfoil section, traveling from leading to trailing edge, with the development of a low pressure region known as a suction peak [7]. The suction peak generally aligns with the angle of the leading-edge sweep as seen in Figure 1. For straight wings, airflow typically travels parallel to the chord or perpendicular to the leading edge due to no leading-edge sweep [8]. The flow for a high aspect ratio straight wing, flow can be considered quasi two-dimensional (2D), where separation and at some point stall generally begins near the trailing edge and propagates toward the leading edge in a uniform manner relative to spanwise location [9].

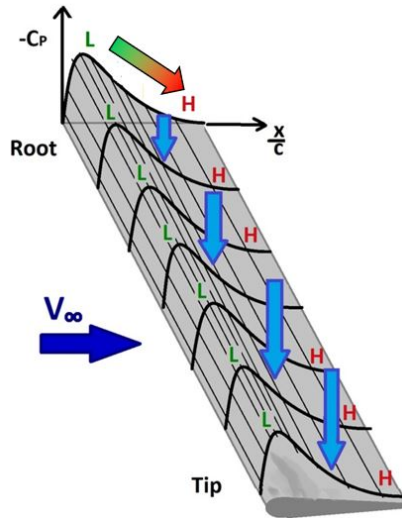


Figure 1. Suction Peak Example [9]

### 2.1.2 Swept Wing

Likewise, a symmetric airfoil configuration as a swept wing at low speed compares to the straight wing with suction peaks aligning with the leading-edge sweep. However, the outboard neighboring suction peak, moving from root chord to tip, is offset aft. The low-pressure suction peak now aligns with an inboard high-pressure region which develops an outboard, spanwise flow that increases in momentum as the flow moves toward the wing tip and trailing edge. Just as swept-wing theory suggested, streamwise velocity components can now be divided into components normal and parallel to the leading edge[10]. Generally, at increased angles-of-attack, the spanwise component of the flow increases while lift generated by the wing is decreased [11]. Ultimately, a non-uniform separation and wing stall generates, beginning at the wingtip and propagates inboard 3-dimensionally, due to the introduction of the crossflow component. Furthermore, as angle-of-attack increases and separation and stall propagation develop, a non-uniform lift distribution occurs along the wing creating a complex pitching moment. The introduction of an abrupt loss of lift at the wing tip can cause a shift in the aerodynamic center, which if considerable, can cause substantial instability of the wing.

### 2.1.3 Delta Wing

Further development of the swept rectangular wing brought about the delta wing; a triangular planform area swept wing with a large root chord. Similar to swept rectangular wings, separation and stall propagation occurs at the wingtip and propagates inboard beginning at the trailing edge, creeping toward the leading edge [9]. However, highly-swept delta wings ( $\Lambda > 45^\circ$ ), at increasing angles-of-attack, develop a leading-edge vortex (LEV) [12]. The steep sweep of the delta-wing allows high-pressure air to rotate around the leading edge and interact with the adjacent suction peak which

creates a high-energy vortical motion of the air along the upper surface of the wing seen in Figure 2. Overall lift is increased as a result of vortex lift generation, seen in Figure 3. The result is a nonlinear lift curve, which is a result of a reduced upper surface pressure aft of the leading edge due to the vortex's low static pressure [13].

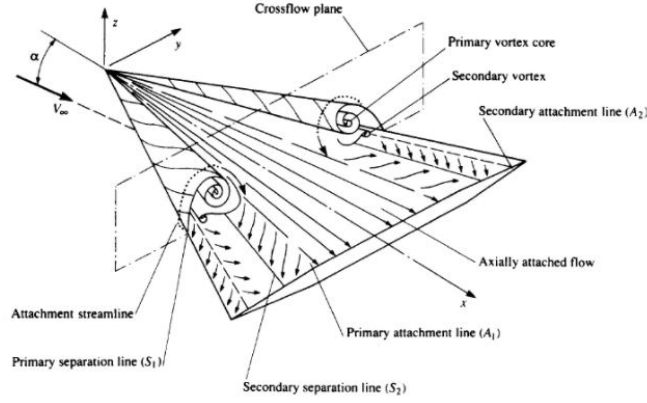


Figure 2. Subsonic Delta-Wing Flow Field [14]

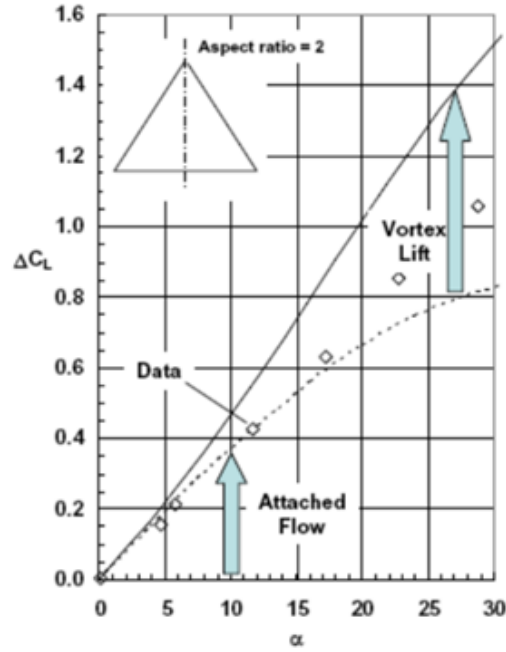


Figure 3. Blunt Delta-Wing Lift-Curve Characteristics ( $AR = 2$ ) [12]

Vortex flow solution and propagation, along with lift dependence, has been demon-

strated to be a function of both  $\alpha$  and  $\Lambda$  as depicted in Figure 4 [14, 15]. This relationship and prediction shows that the vortex flow features can be tracked and accurately related to prior results. Additionally, it can be used for computational model validation through visualization of the vortex core and comparison to these expected results. As delta-wing angle-of-attack increases, LEVs lose momentum,

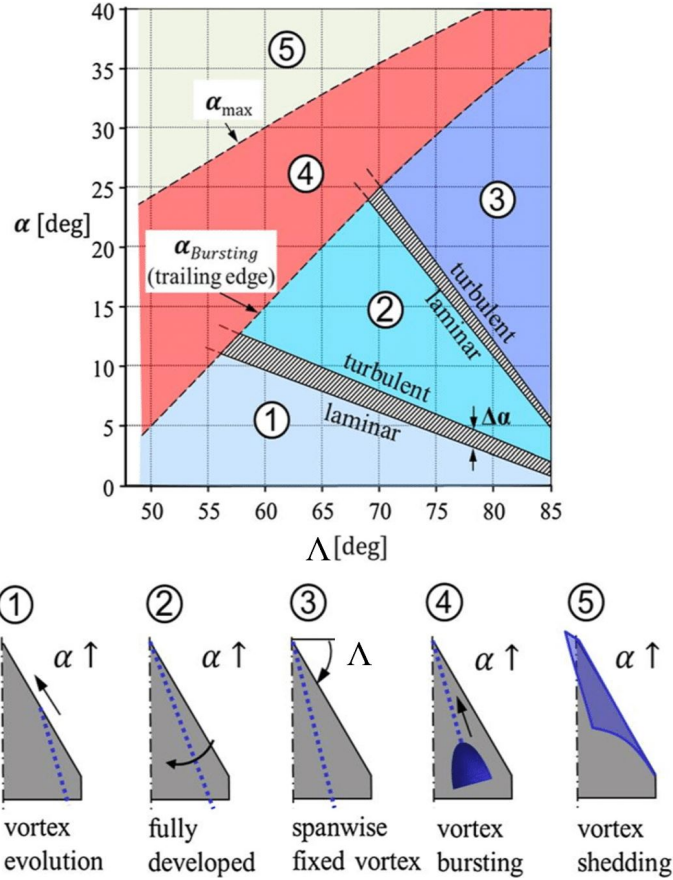


**Figure 4. Delta-Wing Vortex Stages: Wing Sweep ( $\Lambda$ ) vs Angle-of-Attack ( $\alpha$ ) [14]**

separate from the surface and break down. The performance gains are lost resulting in overall loss of lift and unsteady spanwise flow developing across the wing surface, as described previously during swept-wing separation and stall propagation. Spanwise flow moving across a vortex was theorized to reduce vortex core energy leading to the breakdown of the LEV and successive stall of the delta wing [16]. During stall of a delta wing, the aerodynamic center of the wing is shifted forward, similar to a straight

wing. However, delta-wing configurations center of gravity generally lay further aft on the body due to the increased mass associated with the triangular geometry. With this sudden forward shift of the aerodynamic center due to stall, the wing becomes statically unstable as seen in Figure 5. This condition produces destabilizing control characteristic resulting in a drastic pitch up motion at an already high angle-of-attack, unlike straight-wing and most swept-wing configurations which experiencing a pitch down characteristic during stall. This condition occurring at low altitude and at low velocities has resulted in unrecoverable, catastrophic events. For this reason, delta-wing configurations avoid low-speed, high angle-of-attack conditions and have detracted from delta-wing use in large body aircraft.

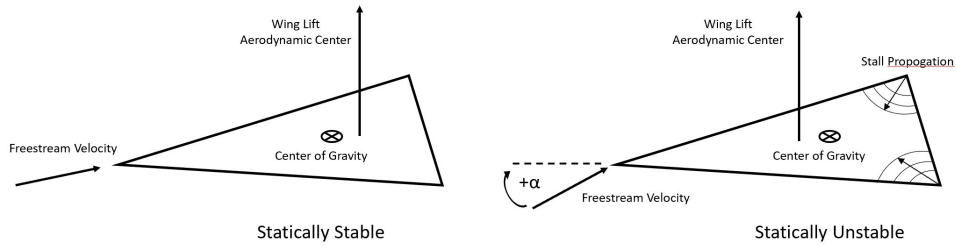


**Figure 5. Delta-Wing Static Stability**

Many modern platforms, the F-22, F-35 and the J-20 fifth-generation fighter aircraft, use cropped delta-wings with forward-swept trailing edges with sweep angles between  $34^\circ$  and  $47^\circ$  [17]. Therefore, the present study chose a moderate  $45^\circ$  sweep delta wing to mimic current modern airframes. Unlike high-swept delta wings, which produce higher energy LEV, the  $45^\circ$  sweep delta wing is anticipated to produce lower energy LEV with performance results comparable to prior swept-wing studies.

## 2.2 Flow Control

The practice of manipulating airflow over an aerodynamic body in an attempt to positively impact designated performance characteristics is generally characterized as aerodynamic flow control. This control can be implemented either passively, with geometric modifications to the wing, or actively with fluidic actuators that add momentum, generally quantified as a nondimensional momentum coefficient ( $C_\mu$ ), or energy to the flow through entrainment.

### 2.2.1 Passive Flow Control

Aerodynamic improvement by means of passive, or physical mechanisms, was the initial solution to halt or redirect crossflow over a swept-wing geometry. The passive boundary-layer fence (BLF), a flat plate fixed vertically to the upper surface of the wing, attempts to allow areas of the wing outboard of the fence to regain streamwise flow, thus creating lift and preventing stall as illustrated in Figure 6. The passive BLF was initially used in 1938 by Wolfgang Liebe and has been utilized for many years on various US and foreign military aircraft: the Convair F-102 Delta Dagger, the Mikoyan-Gurevich MiG-15, the Mikoyan-Gurevich MiG-17, the Sukhoi Su-17 and the Russian OKB-1 150 bomber [18]. Through experimental research and real-world application, certain passive BLF characteristics have proven to be more productive than others. Attributes documented (negative and positive) include effects related to height of the boundary-layer fence relative to the actual boundary-layer thickness and increased performance relative to chordwise fence placement. Furthermore, optimal spanwise location for a single wing fence was found to be between  $z/b = 0.5$  and  $0.8$  with multiple BLFs out-performing single fences configurations [19, 1, 20, 18].

Salmi's study of a NACA 63<sub>1</sub>-A012 swept wing ( $AR = 8$ ,  $\lambda = 0.45$ ,  $\Lambda = 45^\circ$ ,  $2b = 29$  in) in a 19 ft wind tunnel at a Reynolds number of  $6.0 \times 10^6$  detail the benefits



**Figure 6. Mig-15 Passive Boundary-Layer Fences [21]**

of passive BLFs related to stall propagation [1]. Salmi's baseline wing and passive BLF configurations, shown in Figure 7, at an  $\alpha = 26^\circ$  and  $29^\circ$  respectively depict stall by hash marks and location of the passive fence (highlighted in blue). Analysis of the wing surface reveal the effects of the passive system which allowed continued lift generation outboard of the fence versus the baseline being stalled. Salmi further indicated the most effective passive BLF location, with restrictions, to be between  $z/b = 0.50$  and  $0.80$  [1].

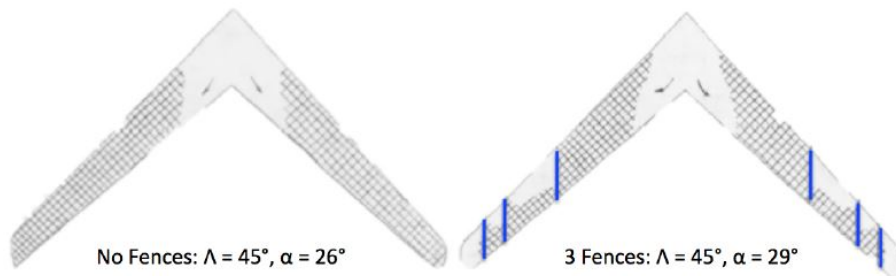


**Figure 7. Swept-Wing Passive Flow Control Stall Propagation [1]**

Pratt and Shields published a 1952 NACA study considered assorted passive flow control devices on a  $45^\circ$  swept wing, seen in Figure 8. Analysis of fence location and BLF configurations of length and height revealed varying performance gains dependent on configuration. Performance gains varied from the baseline configuration

with a 5.9% increase in  $C_{Lmax}$  at a location of  $z/b = 0.575$  with a partial fence that does not wrap around the leading edge and has moderate height, to a 28.7% increase in  $C_{Lmax}$  at a location of  $z/b = 0.575$  with a moderate height, leading edge wrapped BLF. These passive flow control methods producing greater performance gains when the fence continues around the leading edge to the bottom surface of the wing. Furthermore, increased gains were also determined to increase as the fence spanned the entire streamwise length of the upper surface [20].

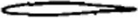
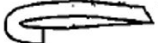
| Fence Location<br>$z/b$                                                                  | Configuration                                                                       | $C_{Lmax}$ | $\alpha C_{Lmax}$ |
|------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|------------|-------------------|
|                                                                                          |    | 1.01       | 21.0              |
|  .575  |  | 1.07       | 25.0              |
|  .575 |  | 1.10       | 27.0              |
|  .575 |  | 1.30       | 27.0              |
|  .575 |  | 1.13       | 27.0              |
|  .80  |  | 1.05       | 27.0              |

Figure 8. Low-Speed Flow Control Characteristics on a  $45^\circ$  Sweptback Wing (AR = 8) [20]

Demoret et al.'s study of the passive BLF on a cropped NACA 0012 delta-wing with the fence located at a spanwise position of  $0.7 z/b$  and beginning at  $0.25 x/c$  on the high-pressure surface which then wrapped the leading edge to extend the entire streamwise length of the low-pressure surface. This configuration resulted in an 8.7% increase in  $C_{Lmax}$  as compared to the baseline wing, pictured in Figure 9. Also, no destabilizing pitching moment characteristics was produced and no significant change in stall angle-of-attack was reported [22].

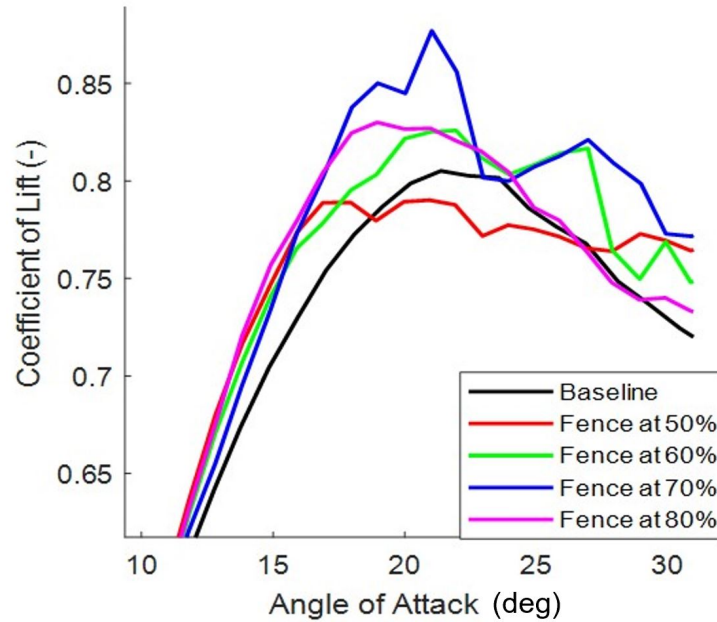


**Figure 9. Demoret NACA 0012 Cropped Delta-Wing Passive Boundary-Layer Fence  $C_L$  Results [22]**

Physical fences, in most cases, are not retractable and are a permanent fixture through all phases of flight. This is a particular issue for many aircraft during cruise when drag penalties due to physical outcroppings diminish flight efficiency. Furthermore, with the requirement for a minimized RCS signature requirement on military low observable aircraft, passive fences are not considered viable solutions for wing performance increase.

### 2.2.2 Active Flow Control

With the application of current knowledge related to swept-wing fluid interaction and passive flow control methods, application of active flow control (AFC) to swept wing geometries was believed as the next step in swept-wing performance improvement. The majority of AFC research centers around straight-wing planforms with recent studies involving swept-wing geometries. Tewes, Greenblatt, Walker and Demoret all document significant performance enhancement with various AFC methods when applied to swept wings, specifically at increased angles-of-attack [11, 23, 9, 22].

Various oscillatory flow research was conducted by both Seifert, in 2008 and Tewes, in 2014. Both studies investigated both straight- and swept-wing interactions with similar conclusions being formulated. Seifert inferred that oscillatory blowing was able to delay stall on a swept wing more effectively than steady blowing and the location of the momentum injection was significant to reduction of the separation bubble [24, 25, 26]. Tewes utilized fluidic oscillators (Figure 10) at a location of  $x/c = 70\%$  on the trailing edge of a NACA 0012 flapped wing. Tewes reported the actuators behaved similar to fluidic fences by reducing the spanwise flow through partial or full flow re-orientation. Furthermore, he suggested momentum added to the flow by the actuators behave similar to vortex generators that bring about counter rotating streamwise vorticity that energizes the boundary-layer and thus allowing flow to remain attached and producing lift [11].

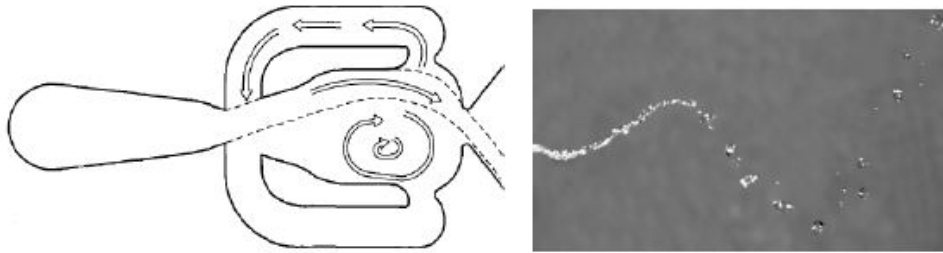


Figure 10. Fluidic Oscillator Function [11]

Additionally, Greenblatt et al.'s study demonstrated the effectiveness of AFC in 3D flows. Specifically the study focused on low aspect ratio ( $AR$ ) swept wings blowing slot application producing parallel flow relative to the leading edge, illustrated in Figure 11, for separation control within the post-stall flight domain. The product of the research revealed an increase in  $C_{Lmax}$  and continued lift being generated after stall. Furthermore, the study deducted that the slot re-energized the leading-edge vortex which contributed to the performance gains mentioned [23].

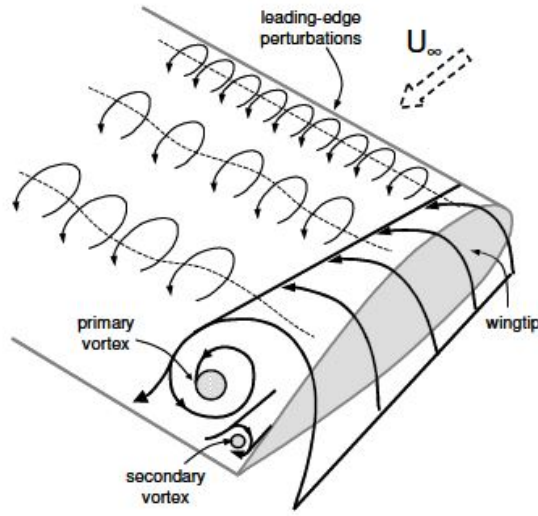


**Figure 11. 2D Leading-Edge Perturbation Separation Control [23]**

The most applicable research related to the current investigation was documented by Walker et al., in 2018 and Demoret et al., in 2020. Walker et al. applied a wall-normal constant blowing velocity AFC slot configuration to a NACA 64<sub>3</sub>-618 baseline swept wing ( $\Lambda = 30^\circ$ ,  $\lambda = 4.3$ ) at  $Re = 1.0 \times 10^5$ . The AFC slot configurations, pictured in Figure 12, was a direct replacement for a passive BLF located at  $0.7 z/b$  runs streamwise from  $0.25 x/c_{eff}$  on the high pressure side of the wing to  $0.75 x/c_{eff}$  on the low pressure side at a width of 0.4 mm. Shown in Figure 13, the study revealed a 12.8% gain in  $\Delta C_{Lmax}$  for the AFC slot at an isentropic blowing ratio ( $BR$ ) of 4 ( $C_\mu = 11.08\%$ ), shown in Equation 1, versus 14.3% gain for the passive fence that

spanned to an additional  $0.25 x/c_{eff}$  along the low pressure side of the wing [9].

$$BR = \frac{U_{slot,avg}}{U_{edge}} \quad (1)$$

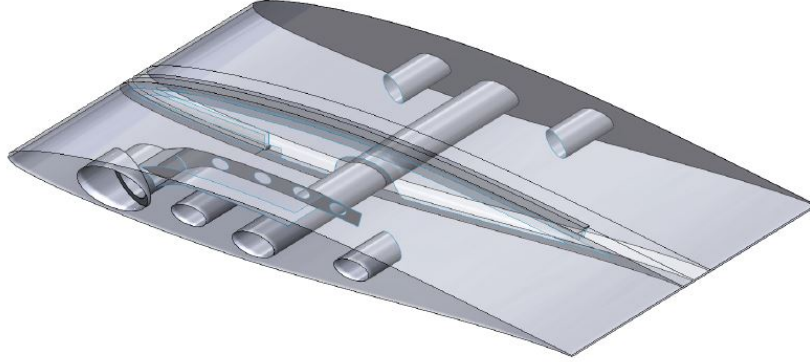


Figure 12. Walker NACA 64<sub>3</sub>-618 30° Swept-Wing AFC Slot Geometry [4]

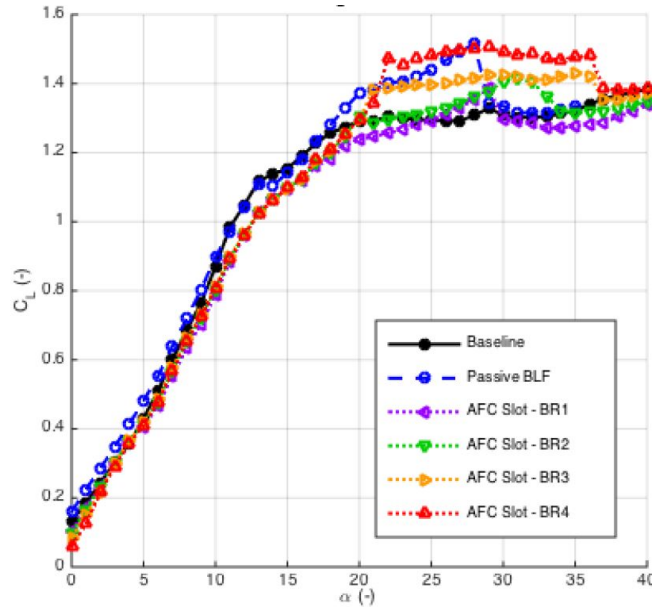


Figure 13. Walker NACA 64<sub>3</sub>-618 30° Swept-Wing  $C_L$  at  $Re = 1.0 \times 10^5$ : Baseline, Passive BLF and AFC Slot [4]

However, the most visible improvement Walker discovered was the disparity in  $C_M$  at high angles of attack, presented in Figure 14. The baseline configuration experiences an increase in  $C_M$  starting at 14° angle-of-attack which indicates the onset of

stall and a steep, but more gradual, pitch up motion. The BLF configuration successfully delayed the onset of stall an additional  $14^\circ$ , to  $28^\circ$  angle-of-attack. However, the BLF  $C_M$  drastically increased, indicating a sudden pitch up condition, when the wing approached stall and was therefore identified as a destabilizing control characteristic [9]. The active flow control method successfully delayed the onset of the negative destabilizing control characteristic another  $7^\circ$ , to  $35^\circ$  angle-of-attack. Although the destabilizing condition existed with the AFC slot, reduction of the magnitude and delay of the onset was successfully achieved [9]. This finding seemingly opened the trade space for slotted wall-normal AFC configuration application to wing geometries that experiences more drastic destabilizing control characteristics, the delta-wing.

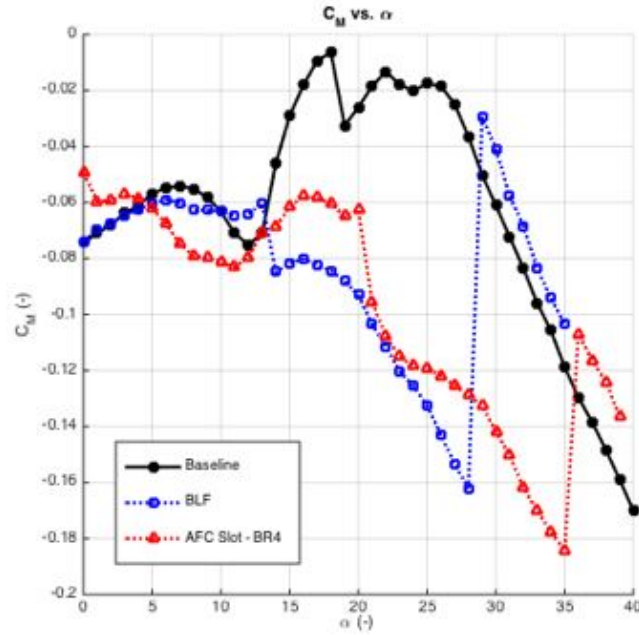


**Figure 14. Walker NACA 64<sub>3</sub>-618 30° Swept Wing  $C_M$  at  $Re = 1.0 \times 10^5$ : Baseline, Passive BLF and AFC Slot [4]**

Walker's stereo-PIV data, illustrated in Figure 15, revealed the creation of two counter rotating vortices, a wingtip vortex and a tip vortex generated by the BLF and AFC slot. Both vortices provide additional momentum by redirecting the flow back down into the boundary-layer, resulting in the increased lift and delay in stall

[9].

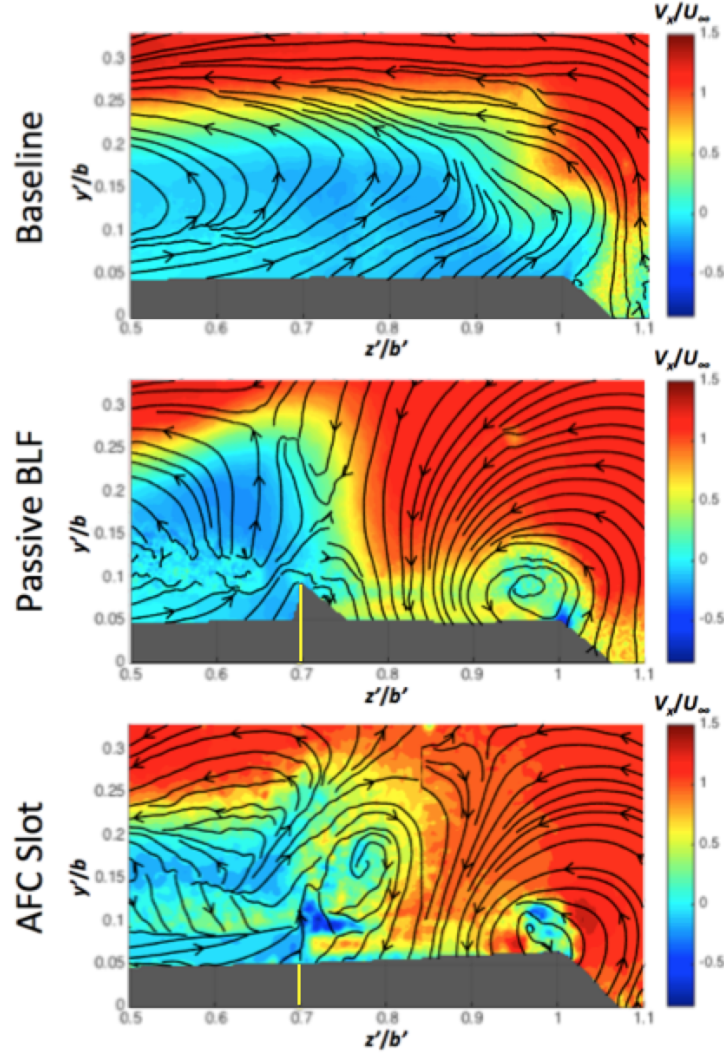


**Figure 15.** Walker 3D Flow-field comparison of Baseline, Passive BLF and AFC Slot ( $BR = 4$ ) in the  $y'$ - $z'$  Plane at  $x'/c = 0.8$  ( $\alpha = 25^\circ$ ); Plot of  $V_x/U_\infty$  with Streamlines of  $V_y/U_\infty$  and  $V_z/U_\infty$  [9]

A continuation of Walker et al. findings were applied to a cropped NACA 0012 delta-wing ( $c_{root} = 14\text{in}$ ,  $c_{tip} = 2.8\text{in}$ ,  $\Lambda = 45^\circ$ ,  $2b = 23.5\text{in}$ ) at  $\text{Re} = 5.0 \times 10^5$  by Demoret. The study attempted to replicate performance improvements of a passive BLF utilizing a wall-normal AFC slot. The constant velocity AFC slot configuration, pictured in Figure 16, was a direct replacement for the passive BLF located at  $0.7 z/b$  which extended chordwise from  $0.25 x/c_{eff}$  on the high pressure side of the wing to

$0.75 x/c_{eff}$  on the low pressure side with a width of 1 mm. However, the passive BLF configuration extended an additional  $0.25 x/c_{eff}$  on the low pressure side of the wing from  $0.75 x/c_{eff}$  to the trailing edge. A gain in  $C_{Lmax} = 60.3\%$  was produced with the AFC slot operating at  $C_{\mu} = 12.22\%$ . These results far exceeded the passive fence configuration, annotated in Figure 17 and delayed the onset of stall an additional  $7^{\circ}$  [22].

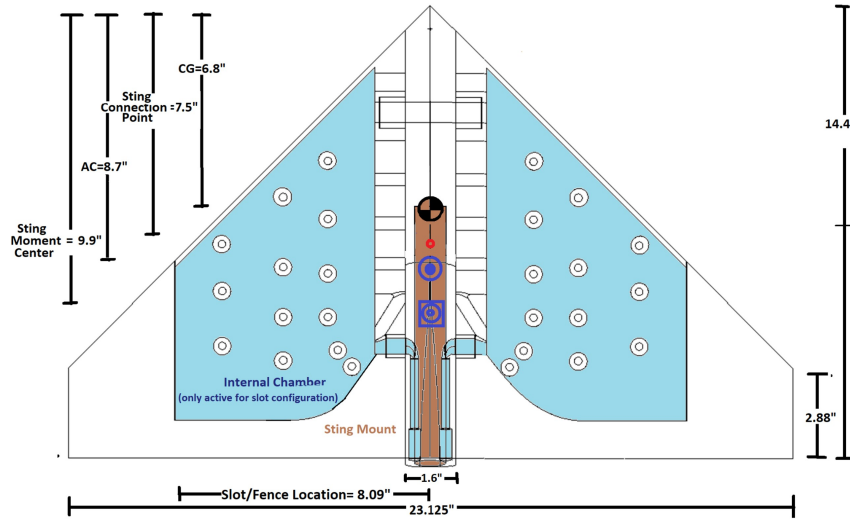


**Figure 16. Demoret NACA 0012 Cropped Delta-Wing AFC Slot Configuration [22]**

Similarly to Walker et.al. findings, the baseline and passive BLF of Demoret et.al. revealed less drastic destabilizing moment characteristics, illustrated in Figure 18. However, the AFC slot configurations showed no destabilizing pitching moment present over the entirety of the angle-of-attack sweep [22].

Demoret et.al. florescent tuft surface flow visualization at both  $25^{\circ}$  (Figure 19) and  $33^{\circ}$  (Figure 20) angle-of-attack demonstrate significant areas of streamwise flow being maintained for the AFC slot, indicating attached flow providing lift, versus the BLF showing spanwise flow, indicating stall. These results support  $C_L$  data provided in Figure 17 above. Demoret noted the increased streamwise flow captured outboard of the AFC slot, demonstrating the ability of to halt spanwise flow comparatively to

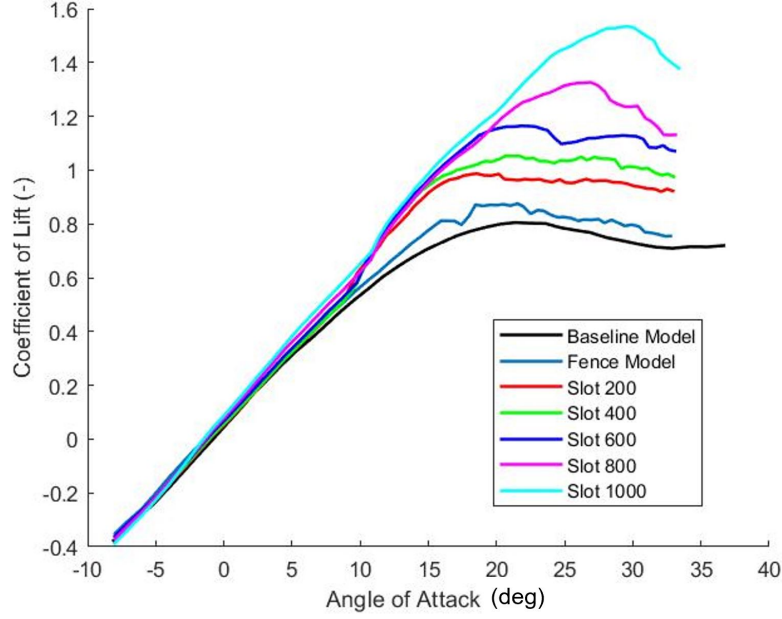


Figure 17. Demoret NACA 0012 Cropped Delta-Wing  $C_L$  at  $Re = 5.0 \times 10^5$ : Baseline, Passive BLF and AFC Slot [22]

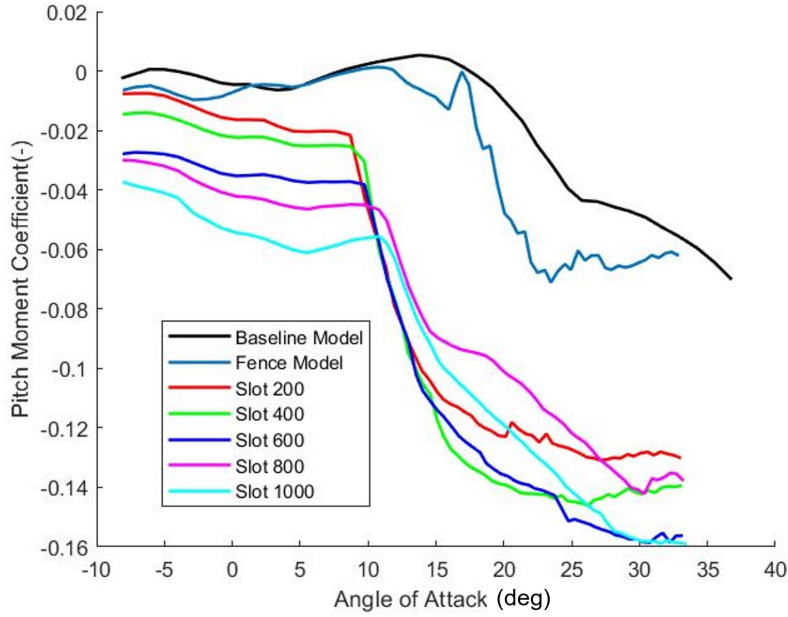


Figure 18. Demoret NACA 0012 Cropped Delta-Wing  $C_M$  at  $Re = 5.0 \times 10^5$ : Baseline, Passive BLF and AFC Slot [22]

the BLF, while also noting the similar streamwise flow inboard of the slot where the BLF model produces spanwise flow characteristics [22]. The area inboard of the

slot appears to be the source of the improved performance characteristics due to the momentum injection interaction, due to the steady blowing slot, with the naturally occurring vortex formed from swept-wing geometries. Additional investigation was recommended to confirm the flow interaction and its contribution to the performance gains.

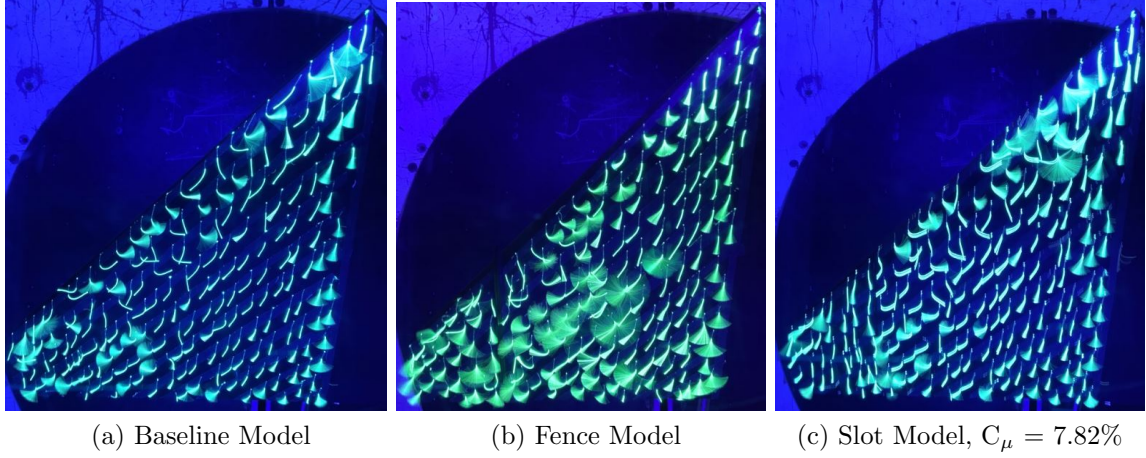


**Figure 19. Demoret NACA 0012 Cropped Delta-Wing Fluorescent-Tuft Visualization,  $\alpha = 25^\circ$  [22]**

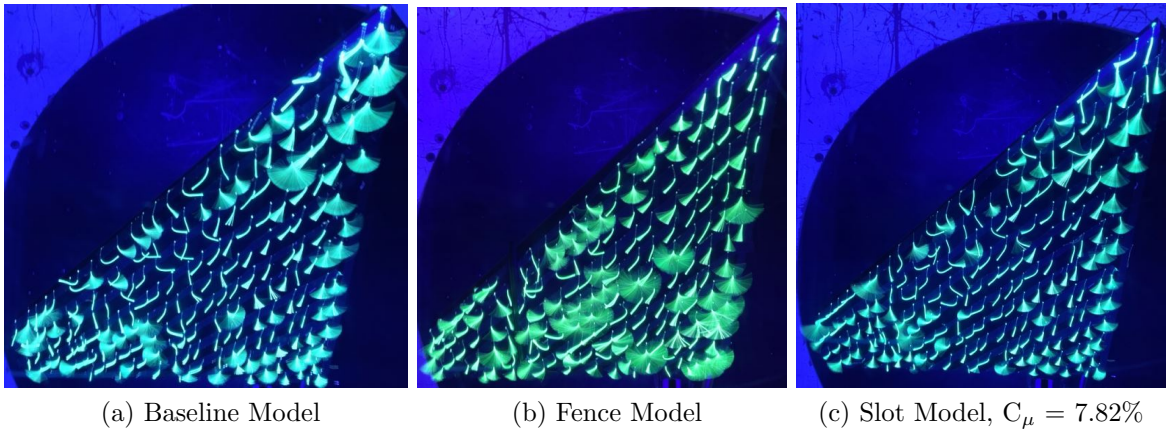


**Figure 20. Demoret NACA 0012 Cropped Delta-Wing Fluorescent-Tuft Visualization,  $\alpha = 33^\circ$  [22]**

As a means of validating Demoret's baseline configuration experimental data, direct comparison of Marzanek et al. presented water tunnel stereo-PIV research,

which utilized a NACA 0012 non-cropped delta-wing with  $\Lambda = 45^\circ$  at  $Re = 3.0 \times 10^5$ , revealed similar results [27]. Overlay of  $C_L$  and  $C_D$  versus  $\alpha$  data, Figures 21 and 22 respectively, affirm Demoret's data by following similar baseline wing trends and producing a baseline wing stall angle-of-attack identical to Marzanek.

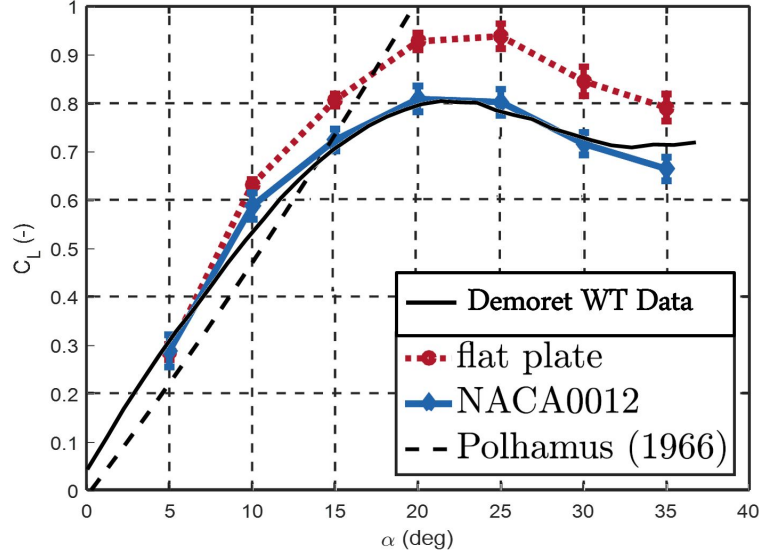


Figure 21.  $C_L$  vs.  $\alpha$  NACA 0012 Delta-Wing: Demoret (Cropped,  $Re = 5.0 \times 10^5$ ) Marzanek (Non-cropped,  $Re = 3.0 \times 10^5$ ) [27]

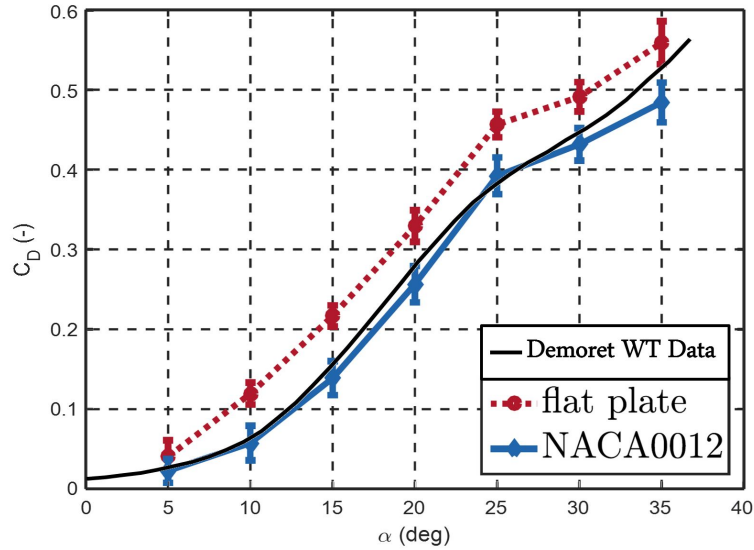


Figure 22.  $C_D$  vs.  $\alpha$  NACA 0012 Delta-Wing: Demoret (Cropped,  $Re = 5.0 \times 10^5$ ) Marzanek (Non-cropped,  $Re = 3.0 \times 10^5$ ) [27]

Considering Walker et al. and Demoret et al. gains associated with the AFC slot, it was understood that physical, full scale production of a volumetric flow capable of reaching  $C_\mu$  values listed were would be difficult. However, overall gains in wing performance was captured at lower scale momentum coefficients that continued to outperform the passive system improvement. The next phase in the evolution of the wall-normal AFC technique would be to optimize the slot relative to full-scaled geometry and attempt to minimize momentum injection while being able to produce similar performance gains demonstrated in the reviewed research.

### 2.2.3 Viscous Effects

Active flow control relies heavily on viscous fluid interactions through fluid entrainment. This is accomplished by energizing the flow with an injection of momentum into the naturally occurring swept wing separation-induced vortex [28]. Vortex theory reveals that viscous losses attribute to vortex breakdown resulting in the eventual loss of swept wing performance at high angles-of-attack [28]. AFC performance gains over that of the passive systems can be attributed to the viscous flow interaction of the vortex and AFC mechanism, specifically at high angles-of-attack. Solfelt and Williams show through computational results that boundary-layer fence performance enhancement success was attributed to vortex generation [29, 30]. These vortices are shown as having the strongest vortical motion when performance benefit are at their peak. Likewise, Walker and Demoret AFC studies revealed a direct relationship between an increase in viscous flow interaction through momentum input within the flow over a wing and an increase in overall wing performance, far exceeding that of passive systems [4, 22].

## 2.3 Computational Fluid Dynamic Theory

The primary purpose of CFD modeling is to provide insight into the flow features around a body. CFD models continually become more robust and closer resemblance of experimental values as computational capabilities advance. Furthermore, with these advances, it allows increasingly more complex flows to be investigated at a comparatively lower cost than experimental tests.

### 2.3.1 Governing Equations

The Navier-Stokes (N-S) equations are the governing equations upon which CFD simulations function. These equations provide the foundation for fluid conservation of mass, momentum and energy. Solving these equations in a closed form has yet to be accomplished without assumptions being applied about the nature of the turbulent fluid flow and its boundary conditions (BC). However, the equations can be solved numerically and iteratively to obtain values of the flow properties.

Within a CFD solution, convergence is achieved when either designated flow feature property values do not change outside of a set tolerance or, in the case of unsteady flow, the average flow feature property values do not change outside of a set tolerance.

For calculation simplification, the fluid flow is treated as a finite control volume (FCV) with application of the N-S equations [31]. The specifications of the computational grid or mesh establish the size of each FCV. Creating small volumes allow for the use of mass, momentum and energy conservation laws which states what mass, momentum and energy leaves one control volume is equal to the mass, momentum and energy entering the adjacent control volume. As these control volumes become smaller, both the accuracy of the results and the computational requirements needed to solve the model increase. Adaptive mesh refinement (AMR) was developed to contest with this ever-increasing requirement cycle.

### **2.3.2 Adaptive Mesh Refinement**

To ensure accurate flow solutions are being produced, computational fluid dynamic simulations require important flow features to be properly resolved and captured. While modeling supersonic flow, shock generation and development is crucial to produce an accurate flow solution, as are laminar and turbulent flow boundaries and vortex shedding to subsonic flow solutions. To sufficiently capture these flow features, the mesh or grid must be precisely aligned with the flow feature and be fine enough to resolve the conservation laws as stated previously. The manual generation of a mesh that perfectly aligns with the different variety of flow features can be tedious and time consuming as each flow feature location must be estimated or calculated, computationally tested, observed and refined manually as needed. However, the application of AMR refines this process and allows the CFD solver to determine where the mesh requires coarsening or refinement based upon flow property gradients to properly balance the accuracy of results and the computational requirements needed to achieve a solution [32]. Figure 23 illustrates the basic concept of AMR where cells are coarsened, or large, in the flow field far away from the body of interest and systematically refined as cells approach the body surface or fluid flow features.

### **2.3.3 Turbulence Models**

CFD is extraordinarily complex due to the subsequent chaotic nature of fluid flow patterns, or turbulence. The application of AMR aids in solving for turbulent flow regions which exhibit highly unsteady flow features, but greatly increases computational requirements due to solving more complex governing equations. Various models have been proposed to manage the bulk properties of the unpredictability of turbulent flow in the utilization of Reynolds Averaged Navier-Stokes (RANS) equations [31]. Users are limited to two RANS models while utilizing Kestrel: Spalart-Allmaras

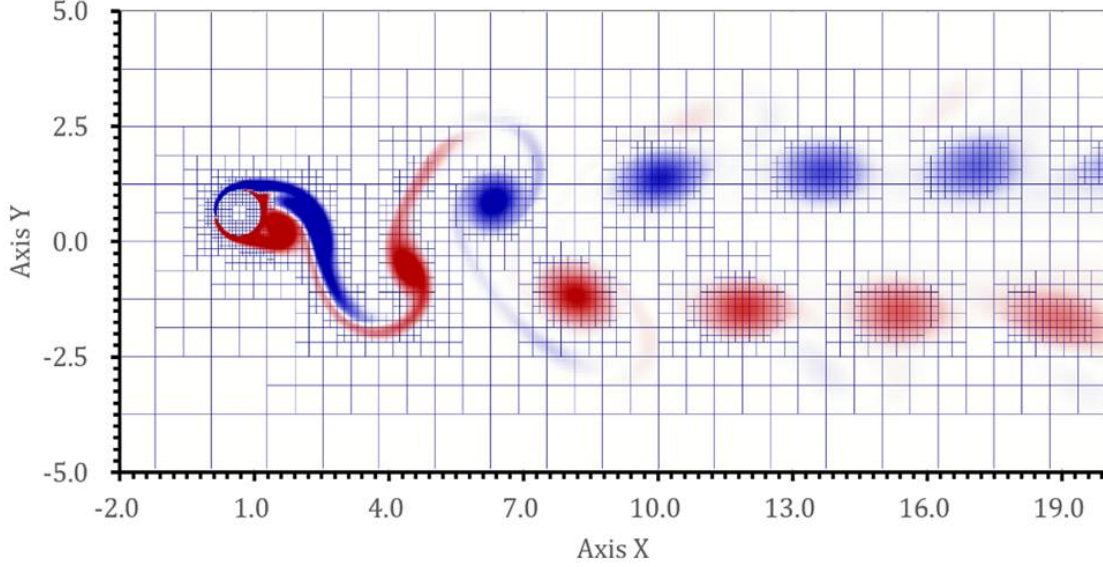


**Figure 23. Active Mesh Refinement (AMR) Cell Density Example [33]**

(S-A) and Menter. According to the Kestrel User's Guide (UG), S-A methods are more appropriate for external flow while Menter is better suited for internal flows [34]. As the S-A one-equation turbulence model was chosen for the presented study, Equation 2 represents the complete S-A turbulence model in dimensional, differential form. Table 1 lists the closure coefficients that were calibrated from empirical data in the literature [35]. In the S-A equation,  $\nu$  is kinematic viscosity,  $\tilde{\nu}$  is a parameter related to kinematic eddy viscosity and  $u$  is velocity. On the right hand side of the equation, the first term corresponds to the production of  $\tilde{\nu}$ , the second term corresponds to the destruction of  $\tilde{\nu}$  and the last term corresponds to the diffusion of  $\nu$  [35]. To fully compute Equation 2, the intermediate functions for  $f_{v1}$ ,  $f_{v2}$ ,  $f_{v3}$ ,  $S$ ,  $f_w$ ,  $g$  and  $r$  are provided in Equations 3 - 10, respectively [35]. In these equations,  $\kappa$  is the turbulence kinetic energy,  $d$  is the distance to the nearest wall,  $S$  is the magnitude of the vorticity and  $\sigma$  is the turbulent Prandtl number.

$$\frac{\partial \tilde{\nu}}{\partial t} + u_j \frac{\partial \tilde{\nu}}{\partial x_j} = c_{b1} \tilde{S} \tilde{\nu} - c_{w1} f_w \left( \frac{\tilde{\nu}}{d} \right)^2 + \frac{1}{\sigma} \left[ \frac{\partial}{\partial x_j} \left( (\tilde{\nu} + \nu) \frac{\partial \tilde{\nu}}{\partial x_j} \right) + c_{b2} \left( \frac{\partial \tilde{\nu}}{\partial x_i} \right) \right] \quad (2)$$

| Variable | Value  |
|----------|--------|
| $c_{b1}$ | 0.1355 |
| $c_{b2}$ | 0.622  |
| $\sigma$ | 0.6667 |
| $\kappa$ | 0.41   |
| $c_{w1}$ | 3.239  |
| $c_{w2}$ | 0.3    |
| $c_{w3}$ | 2      |
| $c_1$    | 7.1    |
| $c_2$    | 5      |

**Table 1. Spalart-Allmaras Closure Constants [35]**

$$\chi = \frac{\tilde{\nu}}{d} \quad (3)$$

$$f_{v1} = \frac{\chi^3}{\chi^3 + c_{v1}^3} \quad (4)$$

$$f_{v2} = \frac{1}{(1 + \chi/c_{v2}^3)} \quad (5)$$

$$f_{v3} = \frac{(1 + \chi f_{v1})(1 + f_{v2})}{\max(\chi, 0.001)} \quad (6)$$

$$\tilde{S} = f_{v3} S + \left( \frac{\tilde{\nu}}{\kappa^2 d^2} \right) f_{v2} \quad (7)$$

$$f_w = g \left[ \frac{1 + c_{w3}^6}{g^6 + c_{w3}^6} \right]^{1/6} \quad (8)$$

$$g = r + c_{w2} (r^6 - r) \quad (9)$$

$$r = \frac{\tilde{\nu}}{\tilde{S}\kappa^2 d^2} \quad (10)$$

The RANS equations introduce Reynolds stress to the N-S equations. Reynolds stress associates with the unsteadiness of the flow but allow for the separation of the fluid velocity and the turbulent fluctuations [31]. RANS methods are typically used for resolving near wall turbulent flow regions near a body and tend to produce inaccurate results where larger eddies form and flow is separated [31]. To solve this issue, large eddy simulation (LES) is utilized to sufficiently capture the large eddies in the separated flow. The combination of RANS and LES gave way to the creation of the Delayed-Detached Eddy Simulation (DDES) and further the Improved Delayed-Detached Eddy Simulation (IDDES) within Kestrel. IDDES resolves the issues related with using both LES and RANS in the boundary-layer by reducing or eliminating the mismatch in values between the two simulations by utilizing a switching function to alternate between RANS and LES based upon grid characteristics and a wall-length scale [36].

Spalart provides a guide to proper gridding practices when using these turbulence models as well as RANS, LES and IDDES methods [37]. For the purposes of the presented study, the S-A turbulence model with IDDES was chosen due to the primary flow being external, vortices being formed from increasing AoA and from the AFC slot jet and large eddies occurring in the separated regions at high AoA. All of which will be simultaneously resolved. For some aerodynamic applications, the S-A model produces similar results to other models but typically reaches solutions faster and thus increases computational efficiency [31].

### 2.3.4 Initial Cell Wall Distance

To accurately model the boundary-layer of a flow, the near wall cells in a mesh or grid must be properly sized to resolve the boundary-layer flow when utilizing turbulence models. This sizing comes in the form of the non-dimensional distance normal to the wall,  $y^+$  [31]. The equation for this term is presented in Equation 11, where  $y$  represents the dimensional distance normal to the wall,  $\tau_w$  is the wall shear stress,  $\rho$  is density of the fluid and  $\nu$  is the kinematic viscosity of the fluid. Spalart recommends a  $y^+$  value of less than 1 being necessary to properly resolve the boundary-layer flow when using the S-A one-equation turbulence model [37]. The settings and values used to establish an appropriate mesh size for this study are discussed in more detail in Chapter III.

$$y^+ = \frac{y \sqrt{\frac{\tau_w}{\rho}}}{\nu} \quad (11)$$

## 2.4 Compressibility Correction

With the onset of increasing flow velocities, compressibility factors must be addressed when computing flow solutions. With a large majority of original NACA data existing within the incompressible realm, simple compressibility corrections were developed to allow this data to be applied up to high velocity compressible flow scenarios, with maximum Mach comparisons around  $M = 0.7$  [38]. The Prandtl-Glauert compressibility correction is the simplest and easiest correction applied to very low speed cases, such as this study. This method is based upon the linearized perturbation velocity potential equation shown in Equation 12 where perturbation velocity potential is given by  $\hat{\phi}$  in the  $x$  and  $y$  direction [38]. Prandtl-Glauert assumes the airfoil is thin and that  $\alpha$  is small as to simplify Equation 12 to the approximation shown in Equation 13, named the Prandtl-Glauert factor ( $\beta$ ) [38].

$$(1 - M_\infty^2) \frac{\partial \hat{\phi}}{\partial x^2} + \frac{\partial \hat{\phi}}{\partial y^2} = 0 \quad (12)$$

$$\beta \equiv \sqrt{1 - M_\infty^2} \quad (13)$$

Application of the Prandtl-Glauert factor to compressible and incompressible pressure distribution through the form of pressure coefficients, the Prandtl-Glauert rule was developed. Given in Equation 14, the rule states if the incompressible pressure distribution ( $C_{p,0}$ ) over an airfoil is known, then the compressible pressure distribution ( $C_p$ ) can be calculated over the same airfoil [38].

$$C_p = \frac{C_{p,0}}{\sqrt{1 - M_\infty^2}} \quad (14)$$

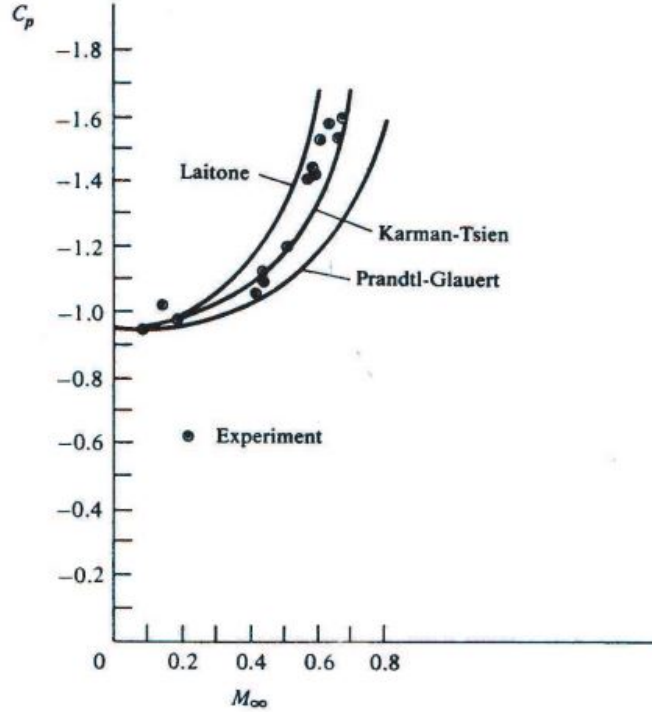


Figure 24. Compressibility Correction Comparison [38]

Due to the limited application and proven errors associated with the Prandtl-Glauert rule at high angle-of-attack and high mach numbers, improvements to the compressibility correction were made. Popular formulas developed include the Karman-Tsien rule and the Laitone rule which account for the shortcomings of the Prandtl-Glauert rule [38]. Comparison of the rules versus experimental results are shown in Figure 24 and indicate the Prandtl-Glauert rule under-predicts results at high mach numbers. However, the solutions converge to similar results at very low Mach numbers making the Prandtl-Glauert rule an appropriate compressibility correction approximation for this study.

### III. Methodology

Computational fluid dynamics simulations require thoughtful application of settings when applied to mesh generation and solver operation to produce accurate and plausible flow solutions. A clear understanding of the operational flow regime, including compressibility and turbulence effects, and flow structure prediction, by anticipating fluid flow physics developed from the wing geometry interaction, was necessary when constructing CFD simulations. Settings used were developed based upon trial and error, solution comparison to physical results for model validation and focused recommendations refined by software manufactures and professionals utilizing the solver to create accurate predictions of similar cases.

#### 3.1 Wind Tunnel Model Characteristics

Utilizing the NACA 0012 airfoil coordinates found in NACA Technical Note 3361 and measurements obtained from Demoret’s study, listed in Table 2, the delta-wing 3D digital geometry was created with SolidWorks v2019 solid modeling computer-aided design (CAD) software[22, 39].

| Wing Geometry                |                        | Free-stream Settings                 |                              |
|------------------------------|------------------------|--------------------------------------|------------------------------|
| Root Chord ( $c_{root}$ )    | 14 in                  | Reynolds Number (Re)                 | 500,000                      |
| Tip Chord ( $c_{tip}$ )      | 2.88 in                | Temperature (T)                      | 300K                         |
| Wing Sweep ( $\Lambda$ )     | 45°                    | Pressure (P)                         | 28.95 in Hg                  |
| Wing Half-Span (b)           | 11.5625 in             | Free-stream Flow Mach ( $M_\infty$ ) | 0.059 ( $V_\infty = 45mph$ ) |
| Angle-of-Attack ( $\alpha$ ) | 0°to30°                |                                      |                              |
| Planform Area (S)            | 195.16 in <sup>2</sup> |                                      |                              |
| Mean Aerodynamic Chord (MAC) | 9.66 in                |                                      |                              |
| Aerodynamic Center (AC)      | 8.7 in                 |                                      |                              |
| Center of Gravity (CG)       | 6.8 in                 |                                      |                              |

| Passive BLF Geometry            |                                 | AFC Slot Geometry    |                                |
|---------------------------------|---------------------------------|----------------------|--------------------------------|
| Location (z/b) *                | 70% (8.225 in from $c_{root}$ ) | Extent               | See Figure 25 (b)              |
| Airfoil Thickness @ 70% z/b (t) | 0.74 in                         | Thickness            | 0.037 in                       |
| Height (0.6t)                   | 0.444 in                        | Air Flow Velocity    | See Table 6                    |
| BLF Thickness                   | 0.037 in                        | Volumetric Flow Rate | 200, 400, 600, 800, 1,000 SLPM |
| Extent/Height                   | See Figure 25 (a)               |                      |                                |

\* Spanwise Location (z)

**Table 2. Demoret et al.’s Wind Tunnel Delta-Wing Geometry/Flow Settings**

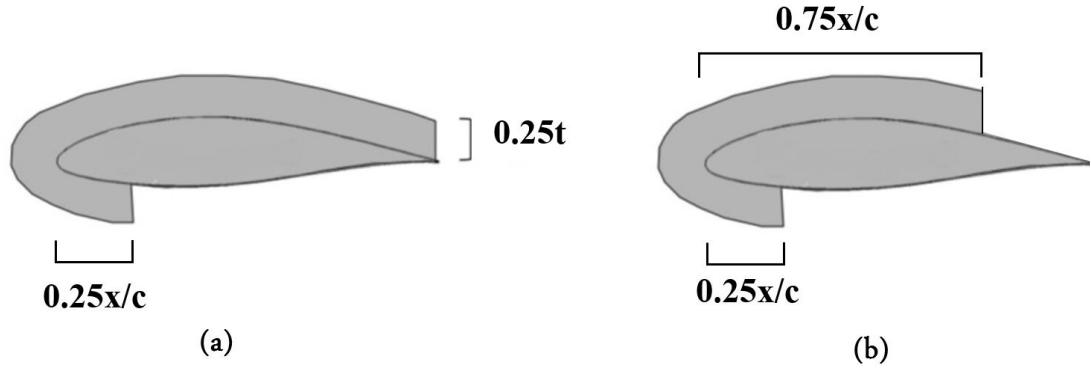


**Figure 25. CFD Model Passive BLF (a) and AFC Slot (b) Configurations [22]**

Production of three models, Figures 26, 27 and 28, represent the CAD geometries used throughout the study. Each model was developed utilizing the dimensions listed in Table 2 above.

### 3.2 Mesh Generation

Mesh generation began with the import of the developed CAD file geometry coordinate database, file type .IGS, into Pointwise v19.1 CFD mesh generation software [40]. Specific settings related to overall mesh generation are listed in Table 3. These

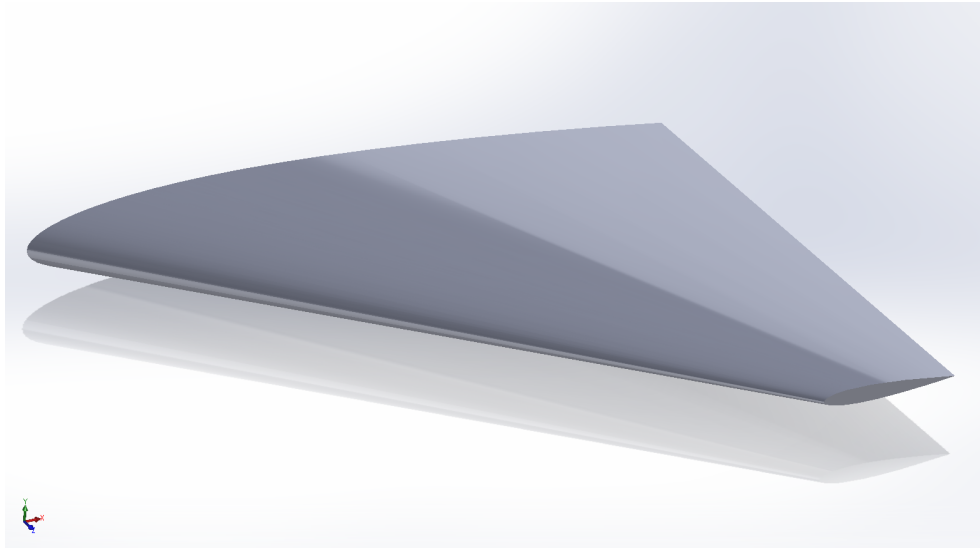


**Figure 26. Baseline Cropped Delta-Wing Configuration**

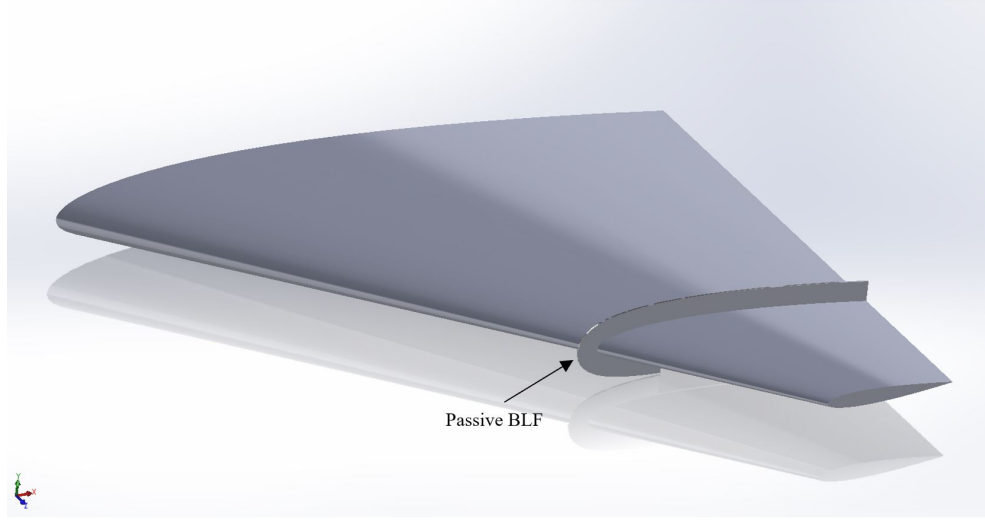


**Figure 27. Passive Boundary-Layer Fence (BLF) Cropped Delta-Wing Configuration**

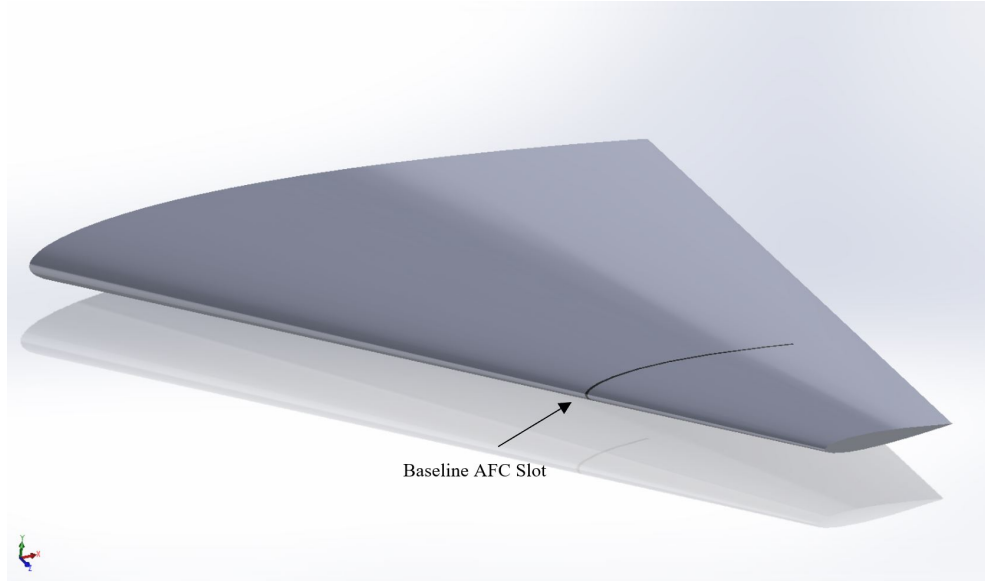


**Figure 28. Active Flow Control (AFC) Cropped Delta-Wing Configuration**

setting produced an initial cell spacing ( $y^+ < 1$ ), as required for the solver to accurately develop near wall fluid interaction while utilizing the Spalart-Allmaras one-equation turbulence model [34]. The 3D anisotropic tetrahedral extrusion (T-Rex) tool was used to generate cells that accurately capture near wall fluid flow development in the boundary-layer [40]. Cell growth rate was recommended at 1.15 to accurately resolve boundary-layer physics [34]. Furthermore, utilizing a maximum

included angle less than  $170^\circ$  assisted in production of an aspect ratio of less than 40 to minimize cell skewness, a mesh characteristic shown at values greater than 40 to produce non-physical flow resulting in reduced solution accuracy [41].

Appropriate boundary conditions were applied to support Demoret et al. wind tunnel flow conditions as detailed in Figure 29. A half-delta wing was modeled as a method to reduce computational expenditure. However, a symmetry plain was utilized to account for the delta wing's omitted geometry and its inclusion of fluid interaction while compiling the simulation solution. Additionally, an outline of the critical flow region was created on the symmetry plain to extend the concentration of cells into the volume above the surface of the wing, depicted in Figure 30. This strategy was implemented to capture predicted flow features, outlined in Section 2.1.3, inherent of the swept delta wing at high angles-of-attack.

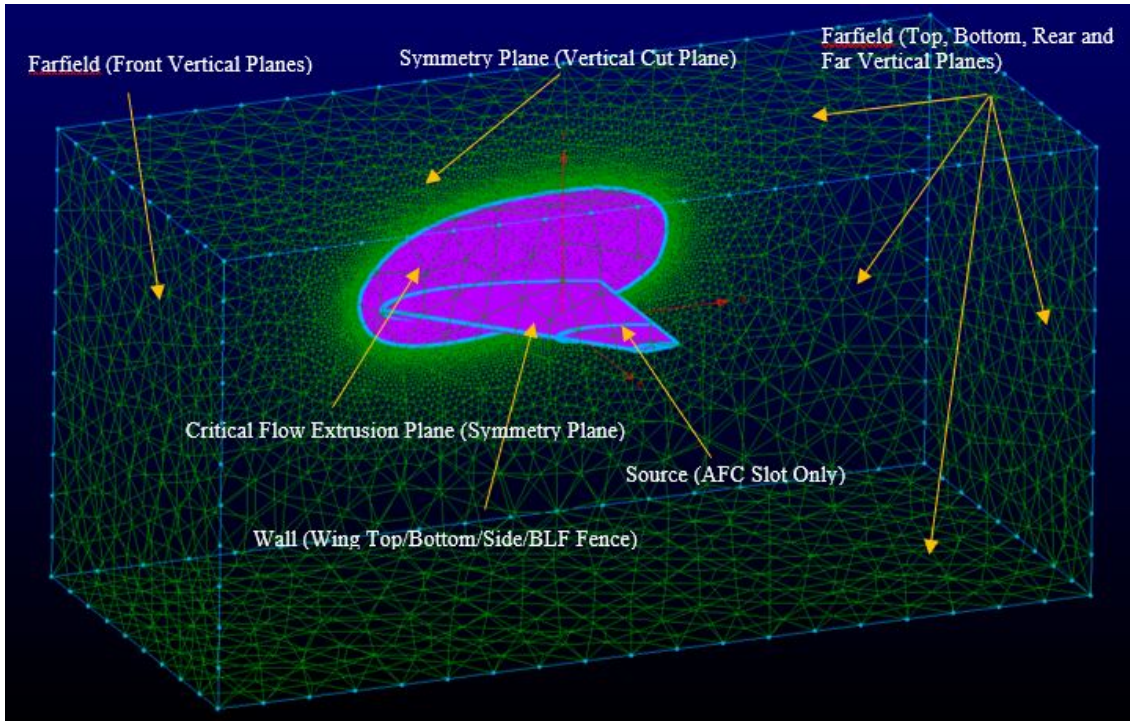


**Figure 29. General Pointwise Mesh Generation, Boundary Conditions and Critical Flow Region**

| General Settings      |                                                                                                         |                                                                   |
|-----------------------|---------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------|
| CAE:                  | Solver                                                                                                  | Kestrel                                                           |
|                       | Dimension                                                                                               | 3D                                                                |
|                       | Boundary Conditions                                                                                     | Symmetry                                                          |
|                       |                                                                                                         | Far-field                                                         |
|                       |                                                                                                         | No Slip Wall                                                      |
|                       | Interface Plane (Source)                                                                                |                                                                   |
| Connectors            |                                                                                                         |                                                                   |
| Nodes                 | ~80 per unit measure                                                                                    |                                                                   |
| Spacing Constraints   | 0.001 (Tip Chord Curvature Regions)                                                                     |                                                                   |
|                       | 0.003-0.004 (Passive BLF and AFC Slot Curvature/BC Interaction Regions)                                 |                                                                   |
|                       | 0.005 (Root Chord Curvature Regions)                                                                    |                                                                   |
| Domain Settings       |                                                                                                         |                                                                   |
| Attributes:           | Mesh Generation                                                                                         | Unstructured                                                      |
|                       | Algorithm                                                                                               | Delauney                                                          |
|                       | Geometry                                                                                                | Triangles                                                         |
|                       | Surface Shape                                                                                           | Database, Closest Point                                           |
|                       | Cells Max Angle                                                                                         | 160                                                               |
| TREX (Symmetry Plane) | Boundary Decay                                                                                          | 0.99 (Wing Surface, Flow Field Concentration<br>0.96 (Far-field)) |
|                       | Max Layers                                                                                              | 20                                                                |
|                       | Full Layers                                                                                             | 0                                                                 |
|                       | Growth Rate                                                                                             | 1.15                                                              |
|                       | Geometry                                                                                                | Triangles and Quads                                               |
|                       | Boundary Conditions                                                                                     | Type Match - Symetry Plane<br>Type Wall - Wing Edge (s = 0.001)   |
|                       | Note: Refine each surface until all cell geometries are fully resolved (i.e. cell count did not change) |                                                                   |
| Block                 |                                                                                                         |                                                                   |
| Attributes            | Boundary Decay                                                                                          | 0.96                                                              |
|                       | Max Edge Growth Rate                                                                                    | 1.8                                                               |
|                       | Aspect Ratio                                                                                            | 0.6                                                               |
| TREX                  | Max Layers                                                                                              | 20                                                                |
|                       | Full Layers                                                                                             | 0                                                                 |
|                       | Growth Rate                                                                                             | 1.15                                                              |
|                       | Isotropic Seed Layers                                                                                   | 2                                                                 |
|                       | Collision Buffer                                                                                        | 2                                                                 |
|                       | Aniso-Iso Blend                                                                                         | 0.6                                                               |
|                       | Skew Criteria Max Angle                                                                                 | 162.5                                                             |
|                       | Boundary Conditions                                                                                     | Type Match - Symetry Plane                                        |
|                       |                                                                                                         | Type Wall - Wing and AFC Slot Surfaces (s = 0.001)                |

Table 3. Pointwise Mesh Generation General Settings

### 3.3 Simulation Setup

#### 3.3.1 Free-stream Flow Correction

Reference conditions were chosen based upon the scaled geometry and Demoret et al. wind tunnel experimental conditions. However, initial simulation results of the baseline configuration failed to capture accurate flow solutions at high angles-of-

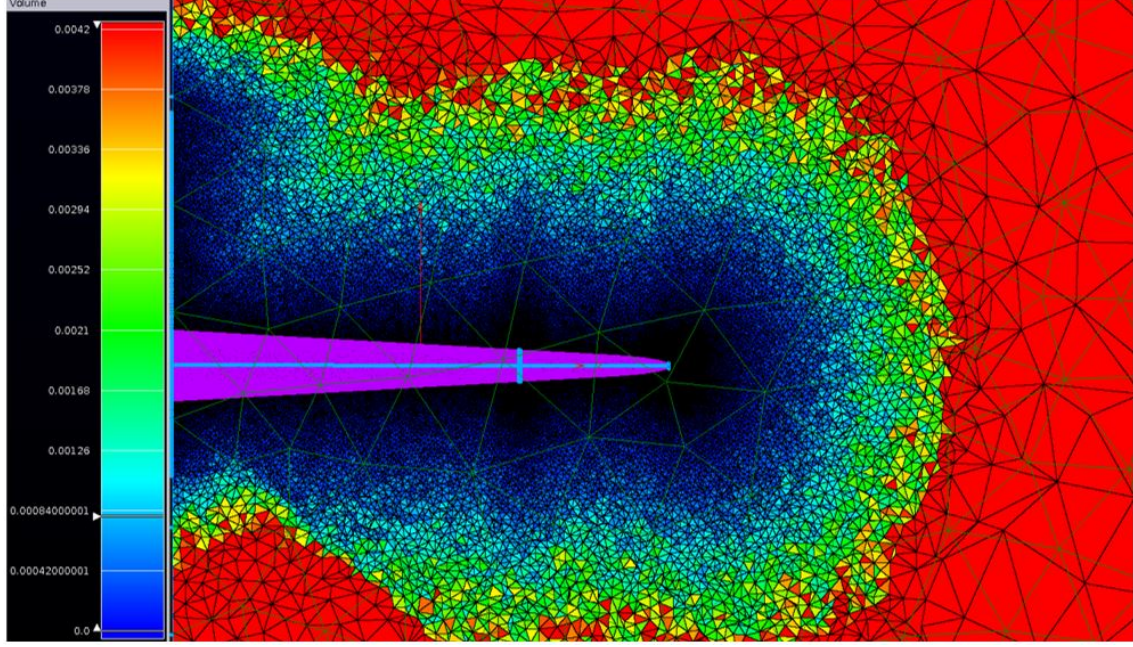


Figure 30. AFC Mesh Critical Flow Region Slice at 11.2 in  $x/c_{root}$  ( $\text{in}^3$ )

attack ( $\alpha > 20^\circ$ ) while utilizing the relatively low experimental free-stream velocity (45 mph at Mach 0.059). Flow visualization indicated no flow separation and raw data revealed a linear progression of  $C_L$ , with no indication of wing stall. Demoret et al. experimental results indicated wing stall and flow separation at an approximate  $\alpha \approx 21^\circ$ . Increase of the iteration quantity and free-stream velocity was recommended for the CFD solver to generate a computational flow solution that accurately captured the simulation flow physics. Detailed in Section 2.4 and computed in Table 4, the Prandtl-Glauert transformation through the Prandtl-Glauert factor ( $\beta$ ) indicated that a change in free-stream Mach number can be accounted for and was found to be within approximately 1.5%. The free-stream Mach number of the flow was therefore increased to 0.18 while maintaining the experimental Reynolds number ( $Re = 5.0 \times 10^5$ ) with the CFD simulation and experimental results continuing to remain comparable. Reynolds number was computed with Equation 15 utilizing the

free-stream velocity ( $U_\infty$ ), wing root chord ( $c_{root}$ ) and kinematic viscosity ( $\nu$ ).

$$Re = \frac{U_\infty c_{root}}{\nu} \quad (15)$$

| Free-stream Mach | $\beta$ | % Change |
|------------------|---------|----------|
| 0.059            | 0.9983  | 1.483    |
| 0.18             | 0.9837  |          |

**Table 4. Prandtl-Glauert Factor Computation**

### 3.3.2 Flow Solver Settings

For the three individual model validation studies and AFC slot optimization study, Table 5 detailed CREATE-AV Kestrel general solver settings pertinent to all cases. Kestrel User Guide recommended the Spalart-Allmaras turbulence model to be used in external flow scenarios involving aircraft structures [34]. Rotation correction (RC) was implemented for enhanced modeling of vortical flows which are prominent flow structures inherent of swept delta-wings, detailed in Section 2.1.3, and expected with implementation of AFC slot steady blowing [34]. Additionally, with the expectation of unsteady, separated flow at high angles of attack, improved delayed-detached eddy simulation (IDDES) was implemented and was cited to improve the solution accuracy for such cases [34]. IDDES was selected to implement hybrid RANS-LES model that behaves as wall-modeled large eddy simulation (LES) when there turbulent inflow exists and a traditional delayed-detached eddy simulation (DDES) model when it does not [34]. Utilizing global time stepping, ranging from 1 (steady, incompressible flow) to 10 (transient, unsteady, incompressible flow), a moderate sub-iteration count of 5 was used to capture the unsteady (time-accurate), compressible flow physics more accurately [34]. The turbulent length scale was chosen relative to the airfoil thickness at the mean aerodynamic chord ( $MAC$ ) [41]. Due to the CAD model and

mesh being generated in units of inches, Kestrel units also followed the imported settings. With that, Kestrel utilizes an uncommon standard unit of mass, the snail, which equates to 1 snail for every 12 slugs. Units of force continue to be in units of pound-force ( $snail * in/s^2$ ). Additionally, the AFC slot "source" boundary condition, further detailed in Section 3.4, utilized a constant slot velocity, static pressure and static temperature. With these constant inputs set, the mass flow input was allowed to "float" and computed by the Kestrel software as necessary.

### 3.3.3 Cartesian Off-Body Settings

To capture flow interaction located in the far-field region of the computational volume, a structured Cartesian of-body mesh was generated, shown in Figure 31. Within Kestrel, SAMAir, a fifth-order, finite-volume solver, was used to generate a controlled far-field region of cells and their volumes with an overlaid grid of refining cells. This dual structured mesh system provided active mesh refinement (AMR), discussed in Section 2.3, and was set to execute after completion of 250 iterations and every 250 iterations thereafter within the far-field region. The focus of AMR, within the Cartesian mesh, was to recognize high gradient flow regions for refinement and coarsens elsewhere, when necessary. Additionally, an overset mesh was used to translate the near-body mesh interactions to and from the far-field. SAMAir coarsens cells by a factor of 4 outward from the near-body mesh to the Cartesian domain extents, excluding the strong gradients regions that require refinement. Furthermore, the Cartesian mesh was solved separately from the near-body mesh as to increase Kestrel's efficiency through reduced far-field cell density and parallel computation [34].

SAMAir inputs included extent bounds of the far-field region and refinement area around the near-body mesh. Based upon the free-stream flow conditions being com-

| Simulation Control                                                                     |                                                                                                                                                                                                                                                                                                                                                                                          |                        |                    |
|----------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------|--------------------|
| Units                                                                                  | ISS (inches, snails, seconds) <i>Note1</i>                                                                                                                                                                                                                                                                                                                                               |                        |                    |
| Startup Iterations                                                                     | 0                                                                                                                                                                                                                                                                                                                                                                                        |                        |                    |
| Scale                                                                                  | 1                                                                                                                                                                                                                                                                                                                                                                                        |                        |                    |
| Global CFD Solver Parameters                                                           |                                                                                                                                                                                                                                                                                                                                                                                          |                        |                    |
| Equation Set                                                                           | Turbulent Navier-Stokes                                                                                                                                                                                                                                                                                                                                                                  |                        |                    |
| Compressible                                                                           | Yes                                                                                                                                                                                                                                                                                                                                                                                      |                        |                    |
| RANS Model                                                                             | Spalart-Allmaras,Vorticity Based                                                                                                                                                                                                                                                                                                                                                         |                        |                    |
| RC                                                                                     | Yes                                                                                                                                                                                                                                                                                                                                                                                      | Transition Solver      | None               |
| IDDES                                                                                  | Yes                                                                                                                                                                                                                                                                                                                                                                                      | QRC                    | No                 |
| CFD Actions                                                                            |                                                                                                                                                                                                                                                                                                                                                                                          |                        |                    |
| Iterations                                                                             | 3500                                                                                                                                                                                                                                                                                                                                                                                     | Time Step <i>Note3</i> | 5*10 <sup>-5</sup> |
| Advective Damping Start                                                                | 0.5                                                                                                                                                                                                                                                                                                                                                                                      | Sub-Iterations         | 5                  |
| Advective Temporal Damping <i>Note3</i>                                                | 0.01                                                                                                                                                                                                                                                                                                                                                                                     | Damping Ramp Fraction  | 0.0                |
| Spatial Accuracy Ramp Fraction                                                         | 0.0                                                                                                                                                                                                                                                                                                                                                                                      |                        |                    |
| Details                                                                                | Time-Accurate Time Solution, Second-Order Spatial and Temporal Accuracy, Newton Nonlinear Convergence Solution Strategy                                                                                                                                                                                                                                                                  |                        |                    |
| KCFD Actions                                                                           |                                                                                                                                                                                                                                                                                                                                                                                          |                        |                    |
| Enable Wall Function                                                                   | Yes                                                                                                                                                                                                                                                                                                                                                                                      | Theta                  | 1.0°               |
| Max Solution Average                                                                   | 300                                                                                                                                                                                                                                                                                                                                                                                      | Relaxation             | 0.9                |
| Fixed Sweeps                                                                           | No                                                                                                                                                                                                                                                                                                                                                                                       | Max Sweeps             | 32                 |
| Sweeps Convergence Criteria                                                            | 1.0*10 <sup>-6</sup>                                                                                                                                                                                                                                                                                                                                                                     | Min Sweeps             | 15                 |
| Details                                                                                | HLLE++ Inviscid Flux, LDD+ Viscous Flux, Weighted Gradient Type, Standard Viscous Flux Jacobian Scheme                                                                                                                                                                                                                                                                                   |                        |                    |
| Free-stream Conditions                                                                 |                                                                                                                                                                                                                                                                                                                                                                                          |                        |                    |
| Known Conditions                                                                       | P-Re-Mach                                                                                                                                                                                                                                                                                                                                                                                | Reynolds Length        | 14 (root chord)    |
| Mach                                                                                   | 0.18                                                                                                                                                                                                                                                                                                                                                                                     | Turbulent Intensity    | -1.0 <i>Note2</i>  |
| Static Pressure                                                                        | 14.2415 psi                                                                                                                                                                                                                                                                                                                                                                              | Beta                   | 0 °                |
| Re                                                                                     | 500000                                                                                                                                                                                                                                                                                                                                                                                   | Temp Increment         | 0.0                |
| α                                                                                      | 0, 10, 14, 16, 18, 20, 22, 24, 26, 28, 30 (deg)                                                                                                                                                                                                                                                                                                                                          |                        |                    |
| Details                                                                                | Native Perfect Gas (Air), Standard Atmosphere Model                                                                                                                                                                                                                                                                                                                                      |                        |                    |
| Boundary Conditions                                                                    |                                                                                                                                                                                                                                                                                                                                                                                          |                        |                    |
| No Slip Wall (Wing Surface)                                                            | Adiabatic<br>Force Account: True<br>Force Account Absolute: True                                                                                                                                                                                                                                                                                                                         |                        |                    |
| Symmetry                                                                               | Force Account: False<br>Patch Force Account Absolute: True                                                                                                                                                                                                                                                                                                                               |                        |                    |
| Far-field                                                                              | Force Account: True<br>Patch Force Account Absolute: True<br>Method: Reimann Invariant<br>Include Momentum Loads: No                                                                                                                                                                                                                                                                     |                        |                    |
| Source:<br>(AFC Slot Only)                                                             | Force Account: True<br>Patch Force Account Absolute: True<br>Method: Constant Total Properties (Specify Static Properties)<br>Include Momentum Loads: Add<br>Reference Frame: Body<br>Turbulence: -1.0, -1.0 <i>Note2</i><br>Mach: Table 6<br>Static Pressure: 15 psi <i>Note4</i><br>Static Temperature: 1255.43 R <i>Note5</i><br>Mass Flow: -1.0 <i>Note2</i><br>Swirl: 0.0, 0.0, 0.0 |                        |                    |
| Mesh Definition                                                                        |                                                                                                                                                                                                                                                                                                                                                                                          |                        |                    |
| Mesh Output Ref Length                                                                 | 1.0 1.0 1.0 (in)                                                                                                                                                                                                                                                                                                                                                                         |                        |                    |
| Mesh Output Ref Point                                                                  | 9.66, 0.0, 0.0 (in)                                                                                                                                                                                                                                                                                                                                                                      |                        |                    |
| Mesh Output Reference Area                                                             | 97.58 in <sup>2</sup>                                                                                                                                                                                                                                                                                                                                                                    |                        |                    |
| Note 1: 1 snail = 12 slugs                                                             |                                                                                                                                                                                                                                                                                                                                                                                          |                        |                    |
| Note 2: Float value                                                                    |                                                                                                                                                                                                                                                                                                                                                                                          |                        |                    |
| Note 3: Required time step study to validate                                           |                                                                                                                                                                                                                                                                                                                                                                                          |                        |                    |
| Note 4: Increased to prevent reverse flow, based upon max surface pressure CFD results |                                                                                                                                                                                                                                                                                                                                                                                          |                        |                    |
| Note 5: Based upon M 0.18, Re = 5 * 10 <sup>5</sup> reference conditions               |                                                                                                                                                                                                                                                                                                                                                                                          |                        |                    |

**Table 5. Kestrel Model Validation and AFC Slot Optimization General Settings**

pressible and subsonic, that the far-field bounds were set at 20 chords aft and 10 chords in all other directions, excluding the symmetry plane, to capture low-speed fluid interaction appropriately, seen in Figure 31 [31]. Additionally, the near-body mesh, seen in Figure 29, was trimmed to accommodate the overset mesh required for SAMAir application, depicted in Figure 32. Using the Kestrel Mesh Manipulation

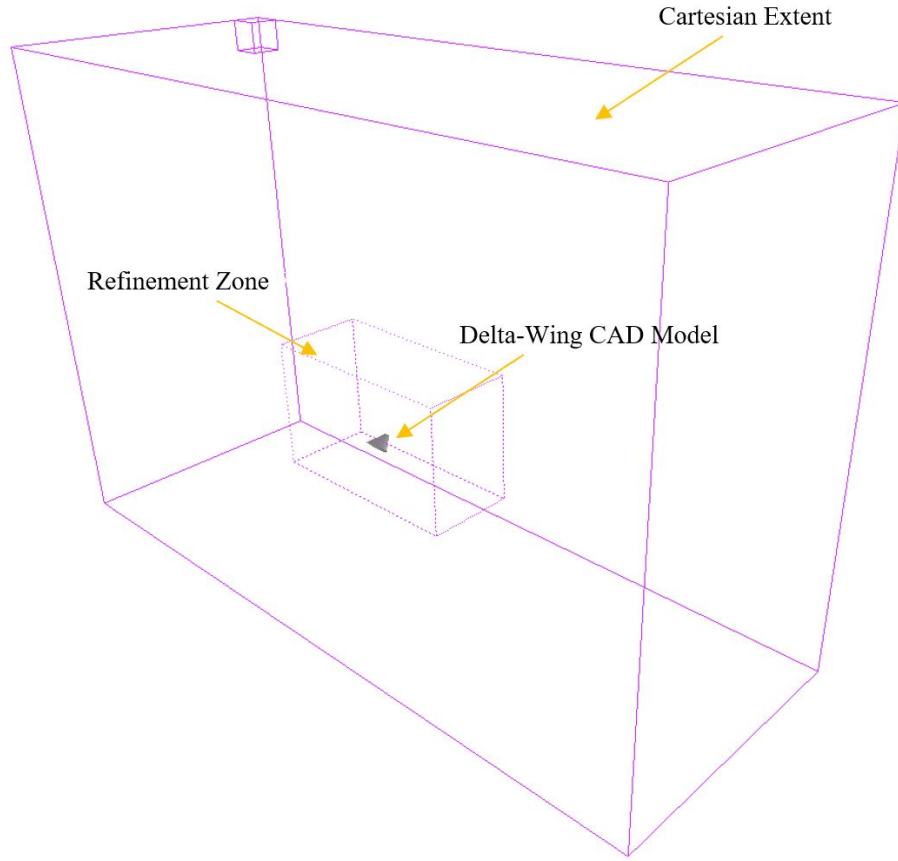


**Figure 31. SAMAir Refinement Zone and Cartesian Extents**

tool, each mesh was trimmed to within 9 inches from the surface of the wing, outside of the critical flow region designated previously. This allowed for the primary, finely resolved mesh to capture all boundary-layer flow interactions and develop near-body flow structures prior to translating those values to the overset mesh for far-field interaction.

### 3.4 Performance Parameters

Using simulation output force files, time averaged global forces and moment measurements in the body fixed reference frame, detailed in Figure 33, were averaged over the final 1000 iterations for each case after sufficient convergence had been ob-

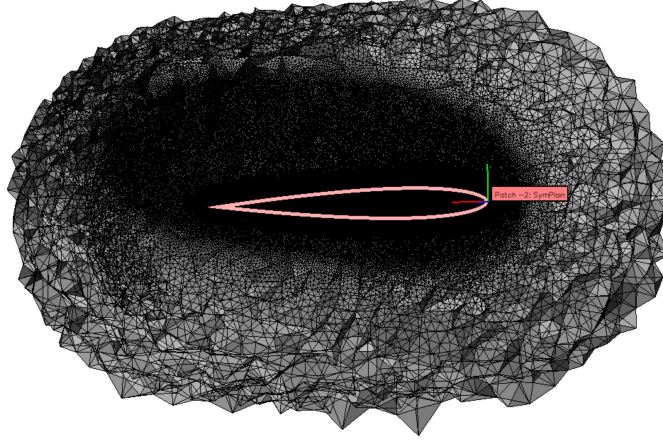


**Figure 32. Near-Body Mesh Trimmed for SAMAir Refinement Zone**

tained. This data was used to generate lift ( $L$ ), drag ( $D$ ) and pitch moment ( $PM$ ), presented in the form of non-dimensional coefficients of lift ( $C_L$ ), drag ( $C_D$ ) and moment ( $C_M$ ), with respect to angle-of-attack ( $\alpha$ ), outlined in Equations 18 - 22. These coefficients will be used to determine the performance of each wing configuration. Variables within these equations are defined as density ( $\rho$ ), free-stream velocity ( $V_\infty$ ), the planform area of the wing ( $S$  given in Equation 16), the mean chord of the wing ( $\bar{c}$ ), wing half-span ( $b$ ), wing root chord ( $c_{root}$ ), wingtip chord ( $c_{tip}$ ) and the x-location of the axis about which the pitching moment was calculated ( $x_{cm}$ ). Below are the equations for lift and drag as a function of normal force ( $N$ ) and axial force ( $A$ ) with the axis transformed to x-back, y-up and z-left [34].

$$S = \frac{b(c_{root} - c_{tip})}{2} + (c_{tip}b) \quad (16)$$

$$D = N \sin(\alpha) - A \cos(\alpha) \quad (17)$$

$$L = N \cos(\alpha) - A \sin(\alpha) \quad (18)$$

$$PM = M_z - [L \cos(\alpha) - D \sin(\alpha)] x_{cm} \quad (19)$$

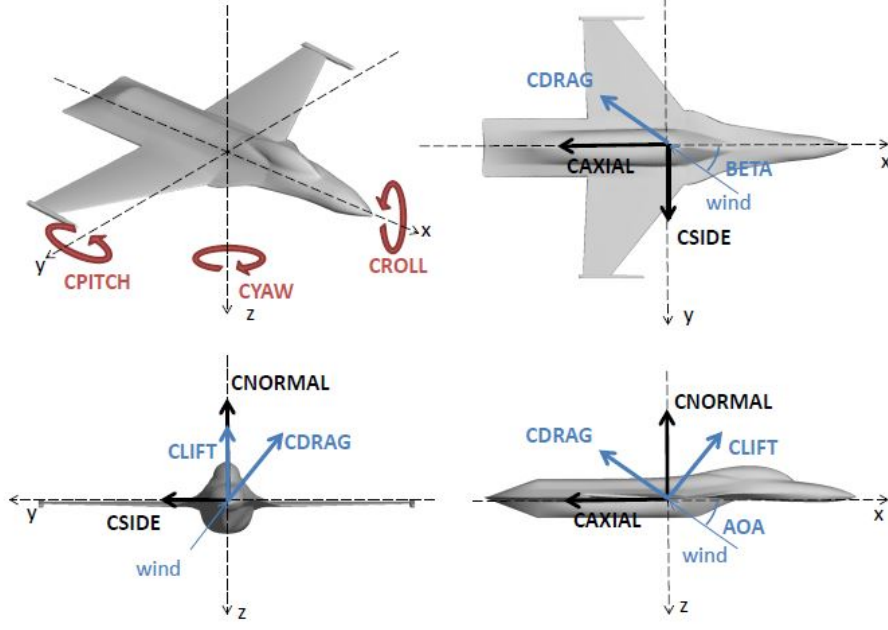


Figure 33. Components of Aerodynamic Force [34]

$$C_D = \frac{D}{\frac{1}{2} \rho V_\infty^2 S} \quad (20)$$

$$C_L = \frac{L}{\frac{1}{2} \rho V_\infty^2 S} \quad (21)$$

$$C_M = \frac{PM}{\frac{1}{2} \rho V_\infty^2 S \bar{c}} \quad (22)$$

The momentum coefficient ( $C_\mu$ ), used to quantify the momentum energy being added to the system, was calculated with the incorporated variables slot area ( $A_{slot}$ ), mass flow rate ( $\dot{m}_{slot}$ ), wing planform area ( $S$ ), volumetric flow rate through the slot ( $\dot{V}$ ), free-stream velocity ( $V_\infty$ ) and the assumption of incompressible flow ( $\rho_\infty = \rho_{slot}$ ). Initial wind tunnel  $C_\mu$  values were calculated at Mach 0.059 and listed in Table 6 along with estimated baseline slot velocities with respect to Demoret et al. measured volumetric flow rates.

$$C_\mu = \frac{\dot{m}_{slot} V_{slot}}{\frac{1}{2} \rho_\infty V_\infty^2 S} * 100 \quad (23)$$

where

$$\dot{m}_{slot} = A_{slot} \rho_{slot} V_{slot} \quad (24)$$

and

$$V_{slot} = \dot{V}/A_{slot} \quad (25)$$

Combining Equations 23 - 25 into a more robust equation yields:

$$C_\mu = 2 \frac{A_{slot}}{S} \frac{\rho_{slot}}{\rho_\infty} \frac{(\dot{V}_{slot}/A_{slot})^2}{V_\infty^2} * 100 \quad (26)$$

Kestrel “source” AFC slot boundary condition settings for constant velocity were input as a Mach number ( $M$ ). With the increase in free-stream Mach number to 0.18 while maintaining an experimental  $Re$  and static pressure, wind tunnel AFC slot volumetric flow parameters required conversion to a scaled slot flow Mach number with respect to updated free-stream conditions. Utilizing the Equation 23 and experimental wind tunnel  $C_\mu$  values, Table 6 detailed wind tunnel slot settings and applicable converted settings for simulation utilization, with applicable designators for each Mach configuration. Additionally, while maintaining the previously identified experimental constants, Kestrel was able to “float,” or adjust, free-stream density, temperature and viscosity as necessary. As a result, free-stream density and viscosity reduced while temperature increased which also allowed Kestrel to produce an increased free-stream speed of sound ( $c$ ) of 20,841.6 in/s. This value was utilized in the production of Mach numbers computed using Equation 27 and listed in Table 6.

$$M_{slot} = \frac{V_{slot}}{c} \quad (27)$$

Comparison of gains or reduction in performance parameters versus momentum quantities, via  $C_\mu$ , were attained utilizing Equation 28 and plotted to that perfor-

|                         | Mach 0.059  |                   |            | Mach 0.18         |            |            |
|-------------------------|-------------|-------------------|------------|-------------------|------------|------------|
| $\dot{V}_{slot}$ (SLPM) | $C_\mu$ (%) | $V_{slot}$ (in/s) | $M_{slot}$ | $V_{slot}$ (in/s) | $M_{slot}$ | Designator |
| 200                     | 0.49        | 777.52            | 0.0574     | 3,643.67          | 0.1748     | M1         |
| 400                     | 1.95        | 1,551.06          | 0.1145     | 7,268.72          | 0.3488     | M2         |
| 600                     | 4.4         | 2,329.90          | 0.1720     | 10,918.61         | 0.5239     | M3         |
| 800                     | 7.82        | 3,106.10          | 0.2293     | 14,556.07         | 0.6984     | M4         |
| 1,000                   | 12.22       | 3,882.82          | 0.2867     | 18,196.02         | 0.8731     | M5         |

**Table 6. AFC Slot (Source) Boundary Condition Conversion**

mance parameter's percent gain or reduction. Variable  $A_{initial}$  and  $B_{final}$  are arbitrary values and were implemented based upon the performance parameter being analyzed. The comparison plots were used for visual aids during analysis of the AFC slot to select the most suitable configuration based upon optimal performance.

$$\%_{gain} = \frac{B_{final} - A_{initial}}{A_{initial}} \quad (28)$$

### 3.5 Convergence Criteria

Confirming computational simulation convergence varied with software application. The Kestrel UG outlined it's specific criteria used for convergence. Output parameters located within the tracking file required plotting for visual inspection of steady-state values occurring. Which specific values that reflected convergence was dependent on the simulation being performed. Initial inspection across all variables within the tracking file was required to identify those parameters exhibiting large, non-uniform oscillations or non-constant values. Furthermore, the number of variable sweeps was to be checked to confirm that parameter was not fixed it's maximum value of 32. If so, the final value was not likely to be accurate. Thus, time-resolution settings were to be adjusted in accordance with the Kestrel UG. Finally, the error and warning logs were also to be checked for complications the simulation experienced throughout the simulation execution. Also, if warnings existed, the solution produced

may not be accurate and solutions to those warnings were to be addressed [34].

## 3.6 Testing Procedure

### 3.6.1 Initial Testing

#### 3.6.1.1 Time-Resolution Study

Recommended by the Kestrel UG to reduce error in key performance indicators and improve convergence, a time-resolution study was performed. Listed in Table 7, solver time-resolution settings analyzed included variations in time step and temporal damping, designated as runs 1 thru 4. While using higher order solvers, increased time to solution was longer for a given step size but production of temporal error was reduced [34]. Furthermore, with the prediction of highly separated, unsteady flow at high angles-of-attack, time step and temporal damping were reduced to allow the solver to fully resolve flow features. The Kestrel UG provided rough orders of magnitude of  $1.0 \times 10^{-3}$  to  $1.0 \times 10^{-4}$  seconds for initial sizing of the time step and 0.1 to 0.01 for temporal damping [34]. The time-resolution study was conducted at a relatively high angle of attach,  $22^\circ$ , utilizing the baseline configuration, so convergence criteria could be attained during production of flow separation and unsteadiness. Normal and axial forces along with the pitching moment, outlined in Section 3.4 for each run were compared for convergence criteria, detailed in Section 3.5, and production of steady state values.

| Run | Time Step          | Adv Temp Damp |
|-----|--------------------|---------------|
| 1   | $5 \times 10^{-5}$ | 0.01          |
| 2   | $2 \times 10^{-5}$ | 0.1           |
| 3   | $5 \times 10^{-5}$ | 0.1           |
| 4   | $5 \times 10^{-4}$ | 0.01          |

**Table 7. Time Step Study Parameters**

### 3.6.1.2 Mesh Refinement

To validate the mesh’s computational application while also reducing computational expense, or computational time, while also achieving a sufficiently converged solution, a grid independence study was performed. For each physical geometry, a total of three independent meshes; coarse, medium and fine, were generated at approximately  $\pm 20\%$  of the medium mesh cell count, detailed in Table 8. Each mesh was required to meet the minimum requirements previously discussed in Section 2.3 for turbulent flow criteria and a  $y^+ < 1$  for near wall boundary-layer interaction. Furthermore, performance measures, outlined in Section 3.4, specifically normal (Fx) forces, axial (Fy) forces and the moment about the z-axis (Mz), were compared within individual groupings of wing geometries at each mesh size to determine mesh convergence, outlined in Section 3.5, and minimal computational utilization to meet that criteria. Due to the study concentrating on improvement of delta-wing performance at high angles-of-attack, at or beyond stall conditions, an angle-of-attack ( $\alpha$ ) of  $22^\circ$  was chosen for the mesh refinement study so convergence criteria could be attained during production of flow separation and unsteadiness. Those results were indicators of the mesh to be utilized for the remainder of the study for each given geometry.

| Configuration | Coarse Mesh |        | Medium Mesh |        | Fine Mesh  |        |
|---------------|-------------|--------|-------------|--------|------------|--------|
|               | Cell Count  | $y^+$  | Cell Count  | $y^+$  | Cell Count | $y^+$  |
| Baseline Wing | 26,592,298  | 0.9432 | 31,181,731  | 0.9386 | 39,353,985 | 0.8624 |
| Passive BLF   | 36,274,945  | 0.9109 | 42,726,349  | 0.9015 | 54,686,837 | 0.9016 |
| AFC Slot      | 28,815,082  | 0.9192 | 31,562,845  | 0.8996 | 48,909,625 | 0.9223 |

Table 8. Grid Independence Cell Count and Initial Cell Spacing ( $y^+$ )

### 3.6.1.3 CFD Model Validation

Computational model performance affirmation with respect to physical data and theory allow confidence in results produced. Furthermore, that confidence allows the

models to be used outside of the comparison to further research and test limits in ways that previously may not have been capable. In this study, all three CFD model configurations were validated through comparison with previously obtained wind tunnel results prior to proceeding with AFC slot optimization. For the experimental baseline and passive BLF model validations, the configurations were replicated utilizing CAD geometries, with mesh generation and Kestrels settings outlined in Sections 3.2 and 3.3 respectively. Furthermore, these configurations were compared to theoretical and experimental results to validate vortical flow features formation within the flow field, via vortex leading edge location and angular propagation based upon  $\alpha$ . The AFC slot validation focused on a single volumetric flow rate chosen from Demoret’s investigation, 200 SLPM or  $C_\mu=0.49\%$ , to produce comparison data. For all geometries, the flow performance measurements compared included coefficient listed in Section 3.4 and were evaluated for convergence as described in Section 3.5. All three configurations were simulated at  $\alpha$ ’s of  $0^\circ$ ,  $10^\circ$  and  $14^\circ$  to  $30^\circ$  in  $2^\circ$  increments. Qualitatively, each performance measure plot was expected to follow trends with respect to Demoret et al. wind tunnel data and quantitatively expected be within 5% of those experimental values. This margin of error incorporates Demoret et al.’s calculated experimental accuracy and uncertainty calculation of approximately  $\pm 2.5\%$  with an additional error margin of  $\pm 2.5\%$  for compressibility correction and general configuration variations [22].

### 3.6.2 Primary Testing

Energy expenditure within an aircraft requires that the benefits of that expenditure outweigh the penalty imposed on the system. Optimization of the AFC slot configuration was necessary to ascertain if performance gains witnessed in the preceding wind tunnel experiment can potentially be replicated through reduction of

momentum energy input by means of geometry and slot flow rate reconfiguration.

### 3.6.2.1 AFC Slot Width Optimization

Comparison of the primary slot width characteristics from wind tunnel model to a scaled model potentially 17 to 20 times the model’s size revealed the original slot width was not suitable for real-world application. Thus, a focus on slot geometry, specifically reduced slot widths (SW), would potentially capture the more realistic, real-world scaled slot geometry while also analyzing the reduced momentum injection effects on the system. This was also a means of optimizing energy input into the system. Utilizing Demoret et al.’s wind tunnel experimental method with the five scaled slot Mach numbers, listed in Table 6, along with the five varying slot width geometries, listed in Table 9, the AFC slot performance of the 25 individual configurations was evaluated through comparison of performance coefficients described in Section 3.4. Furthermore, convergence criteria was also enforced as outlined in Section 3.5. Due to the large quantity and computational expense required to produce detailed, CFD simulation, full angle-of-attack performance parameter curves of 25 configurations, a single angle-of-attack was chosen to represent the configuration’s performance based upon Demoret et al. wind tunnel experimental results, illustrated in Figure 17, which also coincide with validated CFD model results. An angle-of-attack of  $24^\circ$  was chosen as the focus for this analysis due to existing beyond the baseline model stall ( $\alpha = 22^\circ$ ), an  $\alpha$  which all other configurations showed improvement and prior to AFC slot low  $C_\mu$  models experienced the onset of stall. This angle-of-attack also produces sufficient variation between AFC slot  $C_\mu$  modifications as to differentiate between configurations with improved performance. Percentage gains in performance coefficients, specifically coefficient of lift ( $C_L$ ), with respect to momentum coefficient ( $C_\mu$ ), listed in Table 6 and Table 10, will be used to determine the optimal slot width

configuration.

| Designator     | $L_{slot}$ (in) | $W_{slot}$ (in) | $A_{slot}$ (in <sup>2</sup> ) |
|----------------|-----------------|-----------------|-------------------------------|
| SW1 (Original) | 6.85            | 0.037           | 0.25345                       |
| SW2 (80% SW1)  |                 | 0.0296          | 0.20276                       |
| SW3 (60% SW1)  |                 | 0.0222          | 0.15207                       |
| SW4 (40% SW1)  |                 | 0.0148          | 0.10138                       |
| SW5 (20% SW1)  |                 | 0.0074          | 0.05069                       |

**Table 9. Slot Width Geometry Characteristics**

| SW2 | $C(\mu)$ % | SW3 | $C(\mu)$ % | SW4 | $C(\mu)$ % | SW5 | $C(\mu)$ % |
|-----|------------|-----|------------|-----|------------|-----|------------|
| M1  | 0.392      | M1  | 0.294      | M1  | 0.196      | M1  | 0.098      |
| M2  | 1.56       | M2  | 1.17       | M2  | 0.78       | M2  | 0.39       |
| M3  | 3.52       | M3  | 2.64       | M3  | 1.76       | M3  | 0.88       |
| M4  | 6.256      | M4  | 4.692      | M4  | 3.128      | M4  | 1.564      |
| M5  | 9.776      | M5  | 7.332      | M5  | 4.888      | M5  | 2.444      |

**Table 10.  $C_\mu$  as a Function of Slot Width (SW) and Mach (M)**

### 3.6.2.2 AFC Slot Length Optimization

Using the analyzed optimal slot width performance results outlined in Section 3.6.2.1, continued optimization of the AFC slot configuration focused on variation in slot length, or extent (EX), with specific dimensions listed in Table 11 and detailed in Figure 25. Utilizing the optimal slot width configuration and slot velocity, Table 11 was updated to reflect coefficients of momentum ( $C_\mu$ ) obtained from each extent configuration using Equation 26, detailed in Section 3.4. Each configuration was simulated at a single angle-of-attack,  $24^\circ$  for purposes described in Section 3.6.2.1 and was evaluated for convergence as detailed in Section 3.5. Analysis was performed in accordance with Section 3.4 with the generation of performance parameters  $C_L$ ,  $C_D$  and  $C_M$  along with performance gain comparisons versus  $C_\mu$  to determine the optimal configuration.

| Designator                                                                                                                             | Surface Measurement (x/c) |
|----------------------------------------------------------------------------------------------------------------------------------------|---------------------------|
| EX1                                                                                                                                    | -0.25 to 0.75             |
| EX2                                                                                                                                    | -0.25 to 1.0              |
| EX3                                                                                                                                    | -0.25 to 0.5              |
| EX4                                                                                                                                    | 0 to 0.75                 |
| EX5                                                                                                                                    | 0 to 0.5                  |
| EX6                                                                                                                                    | 0 to 0.25                 |
| EX7                                                                                                                                    | 0 to 1.0                  |
| EX8                                                                                                                                    | 0.25 to 1.0               |
| Note:<br>- Zero indicates the leading edge<br>- Negative values follow the bottom surface<br>- Positive values follows the top surface |                           |

**Table 11. Extent Configuration Dimensions**

### 3.6.3 Flow Visualization

Using Tecplot 360 visualization software, the CFD generated flow fields of the baseline, passive BLF, best performing AFC slot wind tunnel configurations and optimized AFC slot configuration were generated in 2D and 3D imagery to compared critical flow feature variations that reveal performance enhancement interactions. Flow field variables to be visualized included surface pressure contours, y-z plane pressure distributions, surface particle streamtraces, velocity magnitude vector fields and velocity magnitude iso-surfaces.

## 3.7 Data Processing

The full MATLAB code for processing the Kestrel output files collected for each run can be found in Appendix A thru I. The general process for producing comparative data visualizations is outlined as follows:

1. Import the *force.dat* files for sweep of angles-of-attack being analyzed
2. Input final iteration count to average data collection over

3. Calculate lift, drag and pitching moment based upon imported body axis reference frame data
4. Calculate coefficients of lift, drag and pitching moment
5. Using an iterative approach, adjust measured distance between mean aerodynamic chord and aerodynamic center ( $x_{cm}$ ) for determination of pitching moment coefficient
6. Plot data
7. Determine optimized configuration solution based upon criteria outlined in Section 3.4 and parameter being analyzed
8. Determine extent  $C_\mu$  based on chosen optimized slot width and Mach configuration
9. Implement processes 1-7 for slot extent optimization
10. Plot and compare performance parameters outlined in Section 3.4 against baseline, passive BLF, wind tunnel AFC Slot results and CFD optimal solution to determine overall performance gains and total energy conserved.
11. Analyze flow field using visualizations as outlined in Section 3.6.3.

### 3.8 Computational Resources

To produce computational results within a suitable and timely manner, it was necessary to use the HPC system described in Chapter 1. Within the HPC network, all simulations conducted were performed on the Onyx system. This system consists of 4,810 standard compute nodes, 4 large-memory compute nodes, 32 GPU compute nodes, 32 Knights Landing (Phi) compute nodes and 64 Machine Learning Accelerator

(MLA) multi-GPGPU nodes (a total of 4,942 compute nodes or 217,128 compute cores) rated at 6.06 peak PFLOPS [42]. Each simulation utilized 44 computational cores per node while varying the number of cores used based upon iterations, mesh size and system availability. For this study, approximately 165 nodes for 1.2 wall-clock hours were utilized to compute 3,500 iterations. An estimate of 87 independent jobs were simulated resulting in approximately 760,000 HPC computational hours used.

## IV. Results and Analysis

### 4.1 Initial Testing

#### 4.1.1 Time-Resolution Analysis

Using the baseline NACA 0012 cropped delta-wing configuration at an angle-of-attack of  $22^\circ$  and configured as outlined in Section 3.6.1.1 and detailed in Table 7, normal and axial forces along with the pitching moment for each run were compared for convergence criteria and production of steady state values as defined in Section 3.5. Summarized parametric analysis of the performance parameters are listed in Table 12 and plotted results are listed in Appendix A. No errors or warnings were indicated in the output log files and variable sweeps were at the minimal value of 15 at the end of each run.

| Run Number                                                                                                        | 1<br>(TS = $5 \times 10^{-5}$<br>AD = 0.01) | 2<br>(TS = $2 \times 10^{-5}$<br>AD = 0.1) | 3<br>(TS = $5 \times 10^{-5}$<br>AD = 0.1) | 4<br>(TS = $5 \times 10^{-4}$<br>AD = 0.01) |
|-------------------------------------------------------------------------------------------------------------------|---------------------------------------------|--------------------------------------------|--------------------------------------------|---------------------------------------------|
| <b>Fx</b> (lb <sub>f</sub> )                                                                                      | 1.267                                       | 1.178                                      | 0.8662                                     | 1.548                                       |
| <b>Fx<sub>std</sub></b> (lb <sub>f</sub> )                                                                        | 0.1099                                      | 0.2641                                     | 0.3183                                     | 0.1332                                      |
| <b>Fy</b> (lb <sub>f</sub> )                                                                                      | 27.84                                       | 30.22                                      | 29.02                                      | 29.73                                       |
| <b>Fy<sub>std</sub></b> (lb <sub>f</sub> )                                                                        | 0.4978                                      | 1.131                                      | 0.9926                                     | 1.146                                       |
| <b>Mz</b> (lb <sub>f</sub> -in)                                                                                   | 39.89                                       | 41.02                                      | 39.34                                      | 42.26                                       |
| <b>Mz<sub>std</sub></b> (lb <sub>f</sub> -in)                                                                     | 1.506                                       | 2.008                                      | 3.254                                      | 1.847                                       |
| <b>Time to Conv (Iter)</b>                                                                                        | 1500                                        | No Convergence                             | No Convergence                             | 1500                                        |
| Note: All values averaged over 1,000 iterations, time step (TS), advective damping (AD), standard deviation (std) |                                             |                                            |                                            |                                             |

**Table 12. CFD Time-Resolution Parametric Analysis: Baseline Model ( $\alpha = 22^\circ$ )**

Qualitatively, steady state values for the three performance parameters had begun to converge for Runs 1 and 4 at approximately 1,500 iterations. Analysis of the steady-state axial (Fx) and moment (Mz) values for Runs 2 and 3 indicated no minimum convergence criteria being met for these settings as the plots continued to have a positive trend upon conclusion of the simulation. Thus, Runs 2 and 3 were eliminated as potential setting parameters. Further comparison of Runs 1 and 4 reveal a reduced

standard deviation (std) and amplitude across the the final 1,000 iterations being average for Run 1, giving a more consistent solution satisfying convergence criteria. For this reason, Run 1 parameters ( $TS = 5 \times 10^{-5}s$  and  $AD = 0.01$ ) will be utilized for the remainder of the study for all simulation configurations.

#### 4.1.2 Mesh Refinement Analysis

Using the NACA 0012 cropped delta-wing baseline, passive BLF and AFC slot  $C_\mu = 0.49\%$  CFD models at an angle-of-attack of  $22^\circ$  and configured as outlined in Section 3.6.1.2 and detailed in Table 8, normal and axial forces along with the pitching moment for each configuration were averaged over 1,000 iterations and analyzed for convergence criteria and steady state values as defined in Section 3.5. Summarized parametric analysis of the performance parameters were listed in Table 13 and plotted results listed were presented in Appendix B. No errors or warnings were indicated in the output log files and variable sweeps were at the minimal value of 15 at the end of each configuration's solution. Flow solution unsteadiness between adjacent values was anticipated due to the mesh study being conducted for each configuration at an angle-of-attack beyond stall conditions. Thus steady state was determined to be minimal oscillation about an average value over 1,000 iterations yielding a small standard deviation (std).

Comparison of the coarse ( $26 \times 10^6$ ), medium ( $31 \times 10^6$ ) and fine ( $39 \times 10^6$ ) mesh cell counts of the baseline CFD configuration produced convergence at approximately 1,500 iterations, for the fine mesh, with small oscillations across all three performance parameters annotated in Table 13. Visual analysis of the moment data about the z-axis for the coarse and medium cell counts, illustrated in Appendix B Figure 67, revealed the solution had not achieved steady state within the 1,000 iterations being averaged due to high amplitude deviations being present in the solution. Re-

|                                                                                                                | CFD Baseline<br>( $\alpha = 22^\circ$ ) |                    |                    | CFD Passive BLF<br>( $\alpha = 22^\circ$ ) |                    |                    | CFD AFC Slot<br>( $C_\mu=0.49\%$ , $\alpha = 22^\circ$ ) |                    |                    |
|----------------------------------------------------------------------------------------------------------------|-----------------------------------------|--------------------|--------------------|--------------------------------------------|--------------------|--------------------|----------------------------------------------------------|--------------------|--------------------|
| Mesh Cell Count                                                                                                | 26 x10 <sup>6</sup>                     | 31x10 <sup>6</sup> | 39x10 <sup>6</sup> | 36x10 <sup>6</sup>                         | 43x10 <sup>6</sup> | 54x10 <sup>6</sup> | 28x10 <sup>6</sup>                                       | 31x10 <sup>6</sup> | 39x10 <sup>6</sup> |
| <b>Fx (lb<sub>f</sub>)</b>                                                                                     | 0.5241                                  | 0.9225             | 1.267              | 0.9672                                     | 0.6087             | 0.3914             | 1.298                                                    | 0.9168             | 1.718              |
| <b>Fx<sub>std</sub> (lb<sub>f</sub>)</b>                                                                       | 0.2609                                  | 0.1499             | 0.1099             | 0.2266                                     | 0.2316             | 0.1551             | 0.1428                                                   | 0.1041             | 0.1168             |
|                                                                                                                |                                         |                    |                    |                                            |                    |                    |                                                          |                    |                    |
| <b>Fy (lb<sub>f</sub>)</b>                                                                                     | 26.28                                   | 27.57              | 27.84              | 28.09                                      | 26.71              | 25.91              | 29.25                                                    | 27.67              | 30.52              |
| <b>Fy<sub>std</sub> (lb<sub>f</sub>)</b>                                                                       | 1.137                                   | 0.9448             | 0.4978             | 1.266                                      | 1.493              | 1.136              | 1.024                                                    | 0.4689             | 0.3545             |
|                                                                                                                |                                         |                    |                    |                                            |                    |                    |                                                          |                    |                    |
| <b>Mz (lb<sub>f</sub>-in)</b>                                                                                  | 36.07                                   | 38.97              | 39.89              | 9.226                                      | 7.612              | 6.873              | 23.12                                                    | 19.21              | 24.33              |
| <b>Mz<sub>std</sub> (lb<sub>f</sub>-in)</b>                                                                    | 4.147                                   | 2.345              | 1.506              | 3.891                                      | 3.393              | 2.614              | 0.6118                                                   | 0.8849             | 0.5491             |
|                                                                                                                |                                         |                    |                    |                                            |                    |                    |                                                          |                    |                    |
| <b>Time to Conv (iter)</b>                                                                                     | NA                                      | NA                 | 1500               | NA                                         | NA                 | 2500               | NA                                                       | NA                 | 2200               |
| Note: All values averaged over 1,000 iterations, TS = $5 \times 10^{-5}$ , AD = 0.01, standard deviation (std) |                                         |                    |                    |                                            |                    |                    |                                                          |                    |                    |

**Table 13. CFD Mesh Refinement Parametric Comparison: Baseline, Passive BLF and AFC Slot Models ( $\alpha = 22^\circ$ )**

sults concluded that the fine mesh achieved the designated convergence criteria and prompted the fine baseline mesh to be utilized in the baseline CFD model validation study.

Comparison of the coarse (36x10<sup>6</sup>), medium (43x10<sup>6</sup>) and fine (54x10<sup>6</sup>) mesh cell counts of the passive BLF CFD configuration produced convergence at approximately 2,500 iterations, for the fine mesh, and small oscillations across all three performance parameters annotated in Table 13. Visual analysis of the axial force data for the coarse and medium cell counts, illustrated in Appendix B Figure 68, revealed the solution had not achieved steady state within the 1,000 iterations being averaged due to high amplitude deviations being present in the solution. Results concluded that the fine mesh achieved the designated convergence criteria and prompted the fine BLF mesh to be utilization in the passive BLF CFD model validation study.

Comparison of the coarse (28x10<sup>6</sup>), medium (31x10<sup>6</sup>) and fine (49x10<sup>6</sup>) mesh cell count of the AFC slot  $C_\mu = 0.49\%$  CFD configuration produced convergence at approximately 2,500 iterations, for the fine mesh, and small oscillations across all three performance parameters annotated in Table 13. Analysis of the axial forces data and momentum data about the z-axis for the coarse and medium cell counts, illustrated in Appendix B Figures 71, 73 respectively, revealed that the solutions

had not achieved steady state within the 1,000 iterations being averaged due to high amplitude deviations being present in the solution. Results concluded that the fine mesh achieves the designated convergence criteria and prompted the fine AFC slot mesh to be utilized the AFC slot,  $C_\mu = 0.49\%$ , CFD model validation study.

#### 4.1.3 CFD Model Validation Analysis

The computational model validation of the NACA 0012 cropped delta-wing baseline, passive BLF and AFC slot  $C_\mu = 0.49\%$  CFD configurations were compared to Demoret et al. wind tunnel experimental data and utilized time-resolution results, listed in Section 4.1.1, and mesh refinement results, listed in Section 4.1.2. Performance parameters, outlined in Section 3.4, were summarized in Table 14 for each of the three CFD model configurations. Each performance, parameter at its given configuration, was averaged over 1,000 iterations and met convergence criteria as outlined in Section 3.5.

|                                                                       |                   | Baseline | BLF    | AFC Slot<br>( $C_\mu=0.49\%$ ) |
|-----------------------------------------------------------------------|-------------------|----------|--------|--------------------------------|
| CFD Max % Deviation<br>From Wind Tunnel (%)                           | $C_D$             | 2.6      | 3.7    | 4.8                            |
|                                                                       | $C_L$             | 3.9      | 7.3    | 4.9                            |
|                                                                       | $C_M$             | 9.8      | 35.9   | 45.7                           |
|                                                                       |                   |          |        |                                |
| $C_{Lmax}$ (-)                                                        | Wind Tunnel Model | 0.8051   | 0.873  | 0.8886                         |
|                                                                       | CFD Model         | 0.8077   | 0.8226 | 0.8773                         |
|                                                                       |                   |          |        |                                |
| Distance from Aero Center (in)<br>(All Wind Tunnel Models = 1.189 in) |                   | 1.32     | 0.99   | 1.28                           |

**Table 14. CFD Validation Parametric Comparison versus Wind Tunnel Data: Baseline, Passive BLF and AFC Slot Models**

#### 4.1.3.1 Baseline CFD Model Validation Analysis

Analysis of the baseline CFD configuration with respect to Demoret et al. wind tunnel experimental data reveal a maximum deviation in coefficient of drag ( $C_D$ ) and lift ( $C_L$ ) performance measures, listed in Table 14, to within 5%, as anticipated. Furthermore,  $C_D$  and  $C_L$  performance curves trended as expected with minimal variation throughout the angle-of-attack sweep, shown in Figures 34 and 35 respectively. Coefficient of momentum ( $C_M$ ) experienced a maximum deviation of more than the anticipated 5% at  $\alpha = 10^\circ$ , shown in Figure 36. However, the following moment solution values trend as expected with the experimental data.

Further validation of the baseline configuration with respect to flow physics generation included visual analysis of vortex core development and location at varying angles-of-attack. Previous studies, discussed in Section 2.1.3 and Figure 4, indicated a shift in the vortex spanwise location, relative to the leading edge, and change in

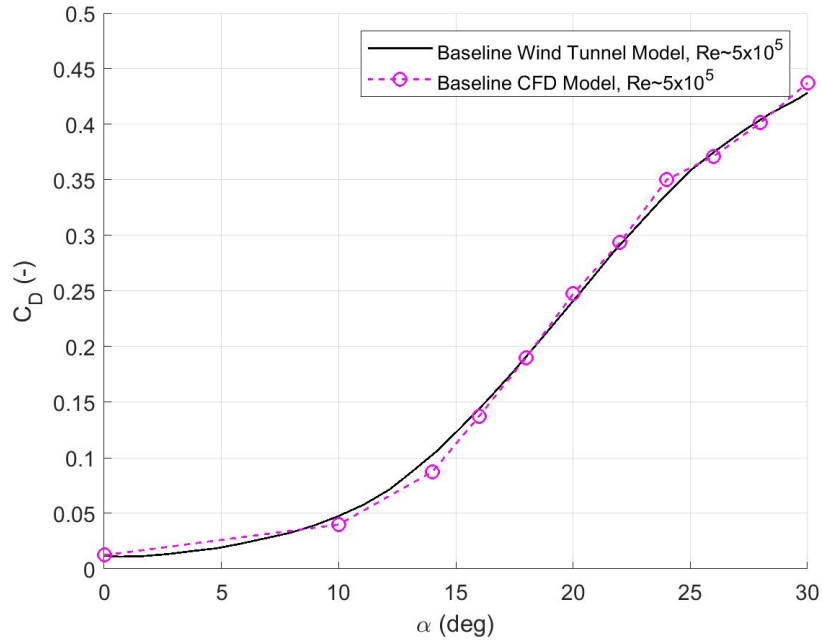


**Figure 34.** NACA 0012 Cropped Delta-Wing Baseline Coefficient of Drag ( $C_D$ ) CFD Model and Wind Tunnel Comparison,  $\alpha = 0^\circ$  to  $30^\circ$ ,  $Re = 5 \times 10^5$

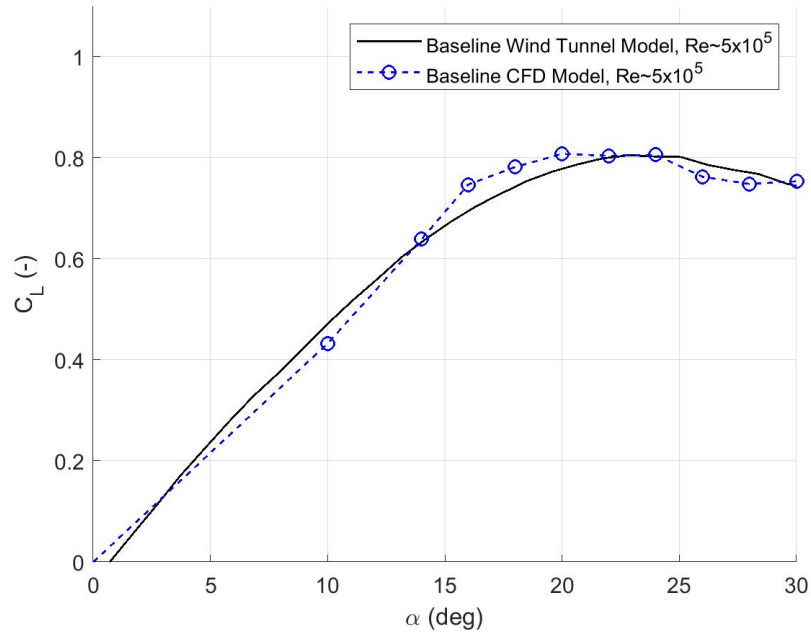


**Figure 35.** NACA 0012 Cropped Delta-Wing Baseline Coefficient of Lift ( $C_L$ ) CFD Model and Wind Tunnel Comparison,  $\alpha = 0^\circ$  to  $30^\circ$ ,  $Re = 5 \times 10^5$

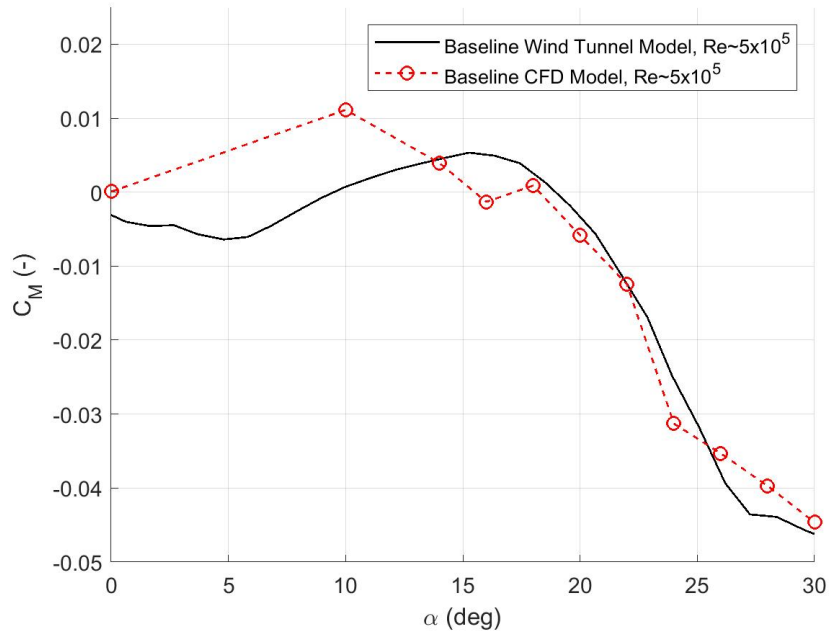


**Figure 36.** NACA 0012 Cropped Delta-Wing Baseline Pitching Moment Coefficient ( $C_M$ ) CFD Model and Wind Tunnel Comparison,  $\alpha = 0^\circ$  to  $30^\circ$ ,  $Re = 5 \times 10^5$

vortex sweep angle, based upon  $\alpha$ , should occur. Baseline CFD model primary vortex core visualizations were produced at  $\alpha = 18^\circ$  and  $24^\circ$ , shown in Figure 37, and confirm variations consistent with literature with a shift in the vortex core, both in sweep and spanwise location. Sweep variation was measured with  $\alpha = 18^\circ$  having a  $63^\circ$  sweep and  $\alpha = 24^\circ$  having a  $74^\circ$  sweep, increasing with angle-of-attack. Furthermore, the spanwise location of the vortex interaction on the leading edge moved inboard as angle-of-attack increased from  $\alpha = 18^\circ$  at 3.8in and  $\alpha = 24^\circ$  at 1in from the root chord ( $c_{root}$ ). Taking all three performance parameters trends, equivalent performance solutions and flow physics into consideration, the baseline CFD model was confirmed to be accurate and valid for the purposes of this study.

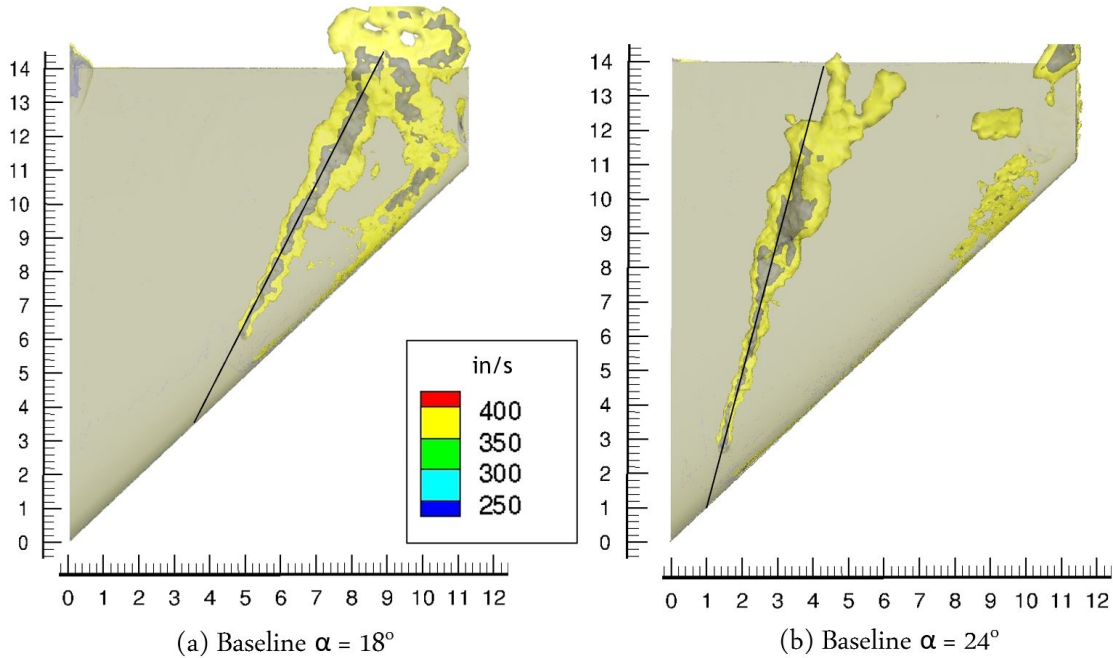


**Figure 37. NACA 0012 Cropped Delta-Wing Baseline CFD Model Vortex Core Comparison,  $\alpha = 18^\circ$  and  $24^\circ$ ,  $Re = 5 \times 10^5$ , Iso-Surface Velocity Magnitude**

#### 4.1.3.2 Passive BLF CFD Model Validation Analysis

Analysis of the passive BLF CFD configuration with respect to Demoret et al. wind tunnel experimental data reveal a maximum deviation in coefficient of drag ( $C_D$ )

performance measures, listed in Table 14, to within 5%, as anticipated. Furthermore, the  $C_D$  performance curve trend as expected with minimal variation throughout the angle-of-attack sweep, shown in Figures 38. Coefficients of lift ( $C_L$ ) and momentum ( $C_M$ ) experienced a maximum deviation of more than the anticipated 5%, shown in Figures 35 and 36 respectively. The lift coefficient curve, Figures 35, trended with the experimental data until stall propagation and varied with a constant negative offset of approximately 7.3% from  $\alpha = 20^\circ$  to  $30^\circ$ . There was no immediate explanation presented as to the source of the displacement. Further investigation was required to resolve the issue. Due to the passive BLF configuration not being the focus of the primary optimization study and  $C_L$  data trends being comparable with experimental trends, produced  $C_L$  CFD results were accepted. The pitching moment coefficient curve, Figure 36, showed maximum variation in the region of a dramatic decrease in moment, from  $\alpha = 20^\circ$  to  $22^\circ$ . However, all other  $C_M$  data followed experimental trends and was within the data constraints.

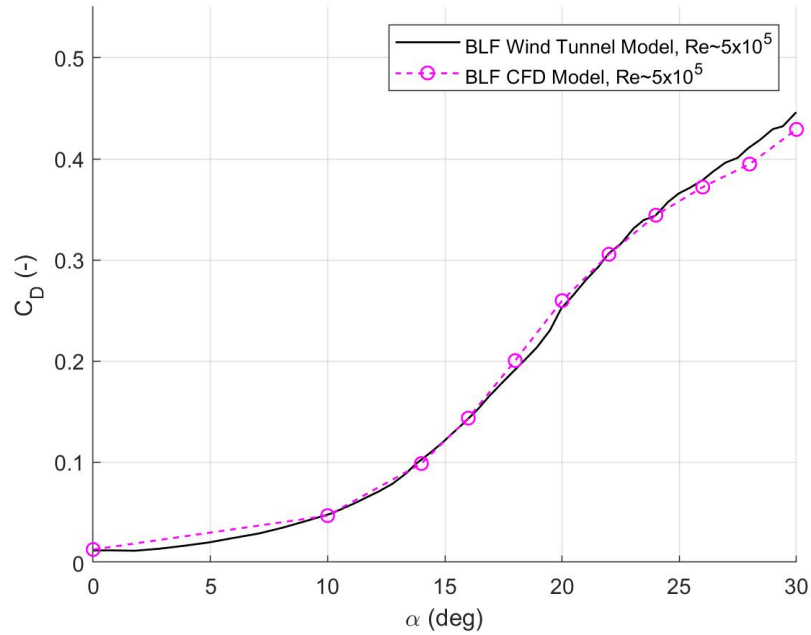


**Figure 38. NACA 0012 Cropped Delta-Wing Passive BLF Coefficient of Drag ( $C_D$ ) CFD Model and Wind Tunnel Comparison,  $\alpha = 0^\circ$  to  $30^\circ$ ,  $Re = 5 \times 10^5$**

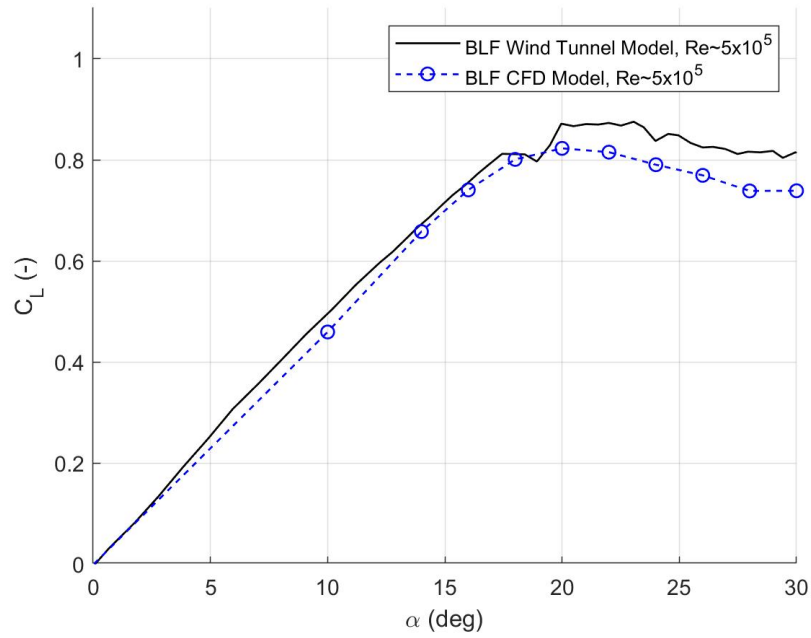


Figure 39. NACA 0012 Cropped Delta-Wing Passive BLF Coefficient of Lift ( $C_L$ ) CFD Model and Wind Tunnel Comparison,  $\alpha = 0^\circ$  to  $30^\circ$ ,  $Re = 5 \times 10^5$

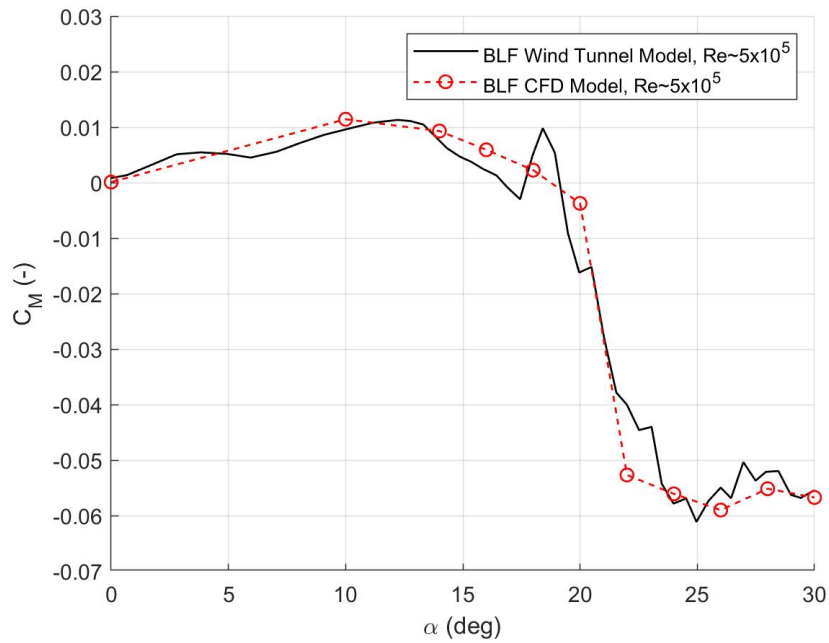


Figure 40. NACA 0012 Cropped Delta-Wing Passive BLF Pitching Moment Coefficient ( $C_M$ ) CFD Model and Wind Tunnel Comparison,  $\alpha = 0^\circ$  to  $30^\circ$ ,  $Re = 5 \times 10^5$

Further validation of the passive BLF configuration flow physics included analysis of the primary vortex core development and location at varying angles-of-attack. Analogous to the baseline CFD model, a shift in the vortex spanwise location, relative to the leading edge, and change in sweep angle based upon angle-of-attack was indicated. Passive BLF CFD model primary vortex core visualizations were produced at  $\alpha = 18^\circ$  and  $24^\circ$ , Figure 41, and confirmed variations consistent with literature with a shift in the vortex core, both in sweep and spanwise location. Sweep variation was measured with  $\alpha = 18^\circ$  having a  $70^\circ$  sweep and  $\alpha = 24^\circ$  having a  $77^\circ$  sweep, increasing with angle-of-attack. Furthermore, the spanwise location of the vortex interaction on the leading edge moved inboard as angle-of-attack increased from  $\alpha = 18^\circ$  at 2.8 in and  $\alpha = 24^\circ$  at 0.8 in from the root chord ( $c_{root}$ ). Taking all three performance parameters trends, equivalent performance solutions and flow physics into consideration, the passive BLF CFD model was confirmed to be accurate and valid for the purposes of this study.

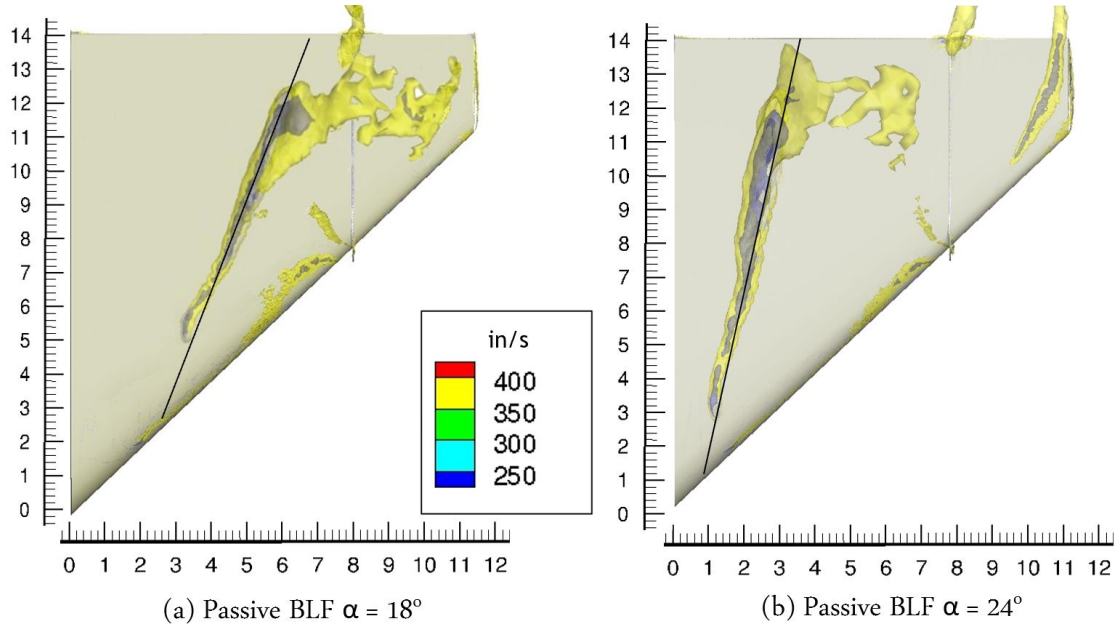


**Figure 41. NACA 0012 Cropped Delta-Wing Passive BLF CFD Model Vortex Core Comparison,  $\alpha = 18^\circ$  and  $24^\circ$ ,  $Re = 5 \times 10^5$ , Iso-Surface Velocity Magnitude**

#### 4.1.3.3 AFC Slot CFD Model Validation Analysis

Analysis of the AFC Slot  $C_\mu = 0.49\%$  CFD configuration with respect to Demoret et al. wind tunnel experimental data reveal a maximum deviation in coefficient of drag ( $C_D$ ) and lift ( $C_L$ ) performance measures, listed in Table 14, being within 5% anticipated. Furthermore, the  $C_D$  and  $C_L$  CFD values trended as expected with minimal variation throughout the angle-of-attack sweep, shown in Figures 42 and 43 respectively, with maximum deviations occurring beyond indicated stall angle-of-attack. Coefficient of momentum experienced a maximum deviation of more than the anticipated 5% at  $\alpha = 24^\circ$ , shown in Figure 44. However, all other solution values with corresponding angles-of-attack trend as expected with the experimental data indicating this solution as a possible outlier.

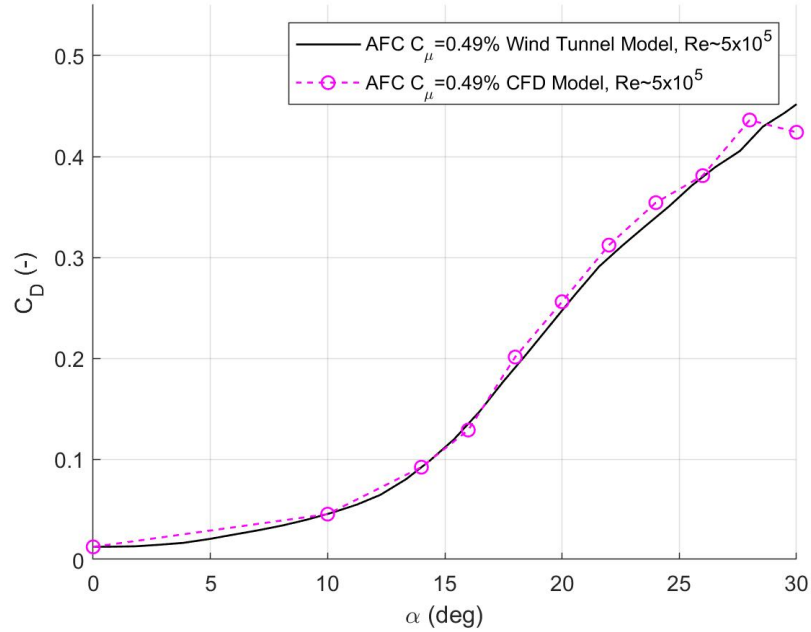


**Figure 42.** NACA 0012 Cropped Delta-Wing AFC Slot Coefficient of Drag ( $C_D$ ) CFD Model and Wind Tunnel Comparison,  $\alpha = 0^\circ$  to  $30^\circ$ ,  $Re = 5 \times 10^5$ ,  $C_\mu = 0.49\%$

Further validation of the AFC Slot  $C_\mu = 0.49\%$  configuration flow physics included analysis of the primary vortex core development and location at varying angles-of-

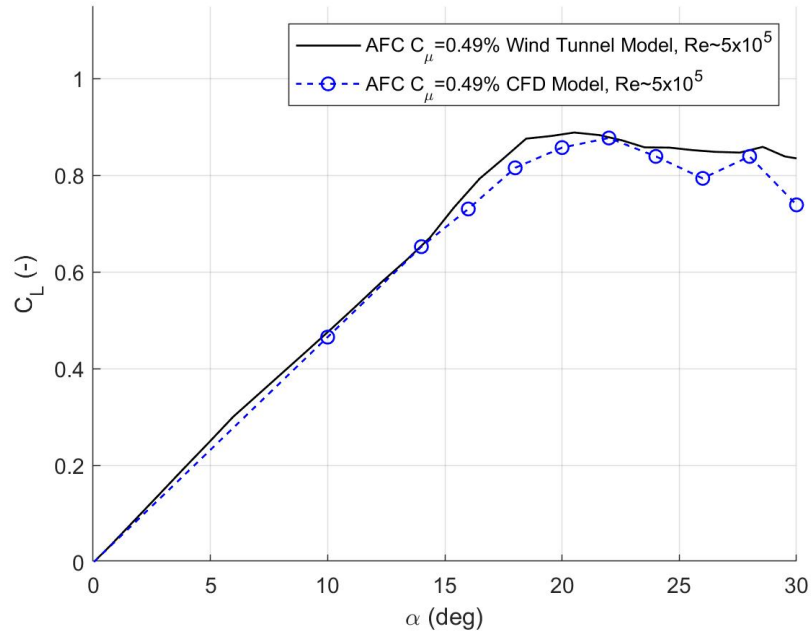


Figure 43. NACA 0012 Cropped Delta-Wing AFC Slot Coefficient of Lift ( $C_L$ ) CFD Model and Wind Tunnel Comparison,  $\alpha = 0^\circ$  to  $30^\circ$ ,  $Re = 5 \times 10^5$ ,  $C_\mu = 0.49\%$

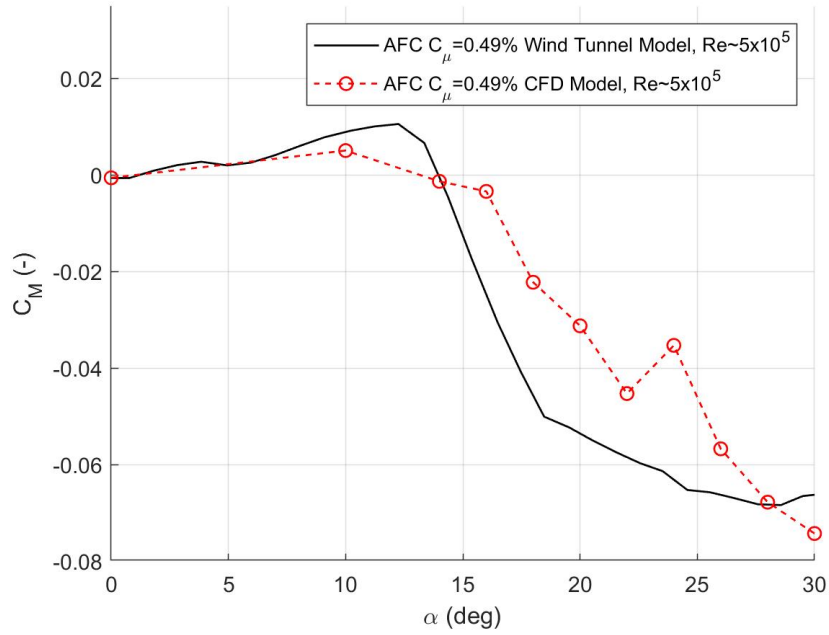


Figure 44. NACA 0012 Cropped Delta-Wing AFC Slot Pitching Moment Coefficient ( $C_M$ ) CFD Model and Wind Tunnel Comparison,  $\alpha = 0^\circ$  to  $30^\circ$ ,  $Re = 5 \times 10^5$ ,  $C_\mu = 0.49\%$

attack. Analogous to the baseline and passive BLF CFD models, a shift in the vortex spanwise location, relative to the leading edge, and change in sweep angle based upon angle-of-attack was indicated. Passive AFC slot model primary vortex core visualizations were produced at  $\alpha = 18^\circ$  and  $24^\circ$ , Figure 45, and confirm variations consistent with literature with a shift in the vortex core, both in sweep and spanwise location. Sweep variation was measured with  $\alpha = 18^\circ$  having a  $65^\circ$  sweep and  $\alpha = 24^\circ$  having a  $74^\circ$  sweep, increasing with angle-of-attack. Furthermore, the spanwise location of the vortex interaction on the leading edge moved inboard as angle-of-attack increased from  $\alpha = 18^\circ$  at 2.6 in and  $\alpha = 24^\circ$  at 0.8 in from the root chord ( $c_{root}$ ). Taking all three performance parameters trends, equivalent performance solutions and flow physics into consideration, the AFC Slot  $C_\mu = 0.49\%$ , CFD model was confirmed to be accurate and valid for the purposes of this study.

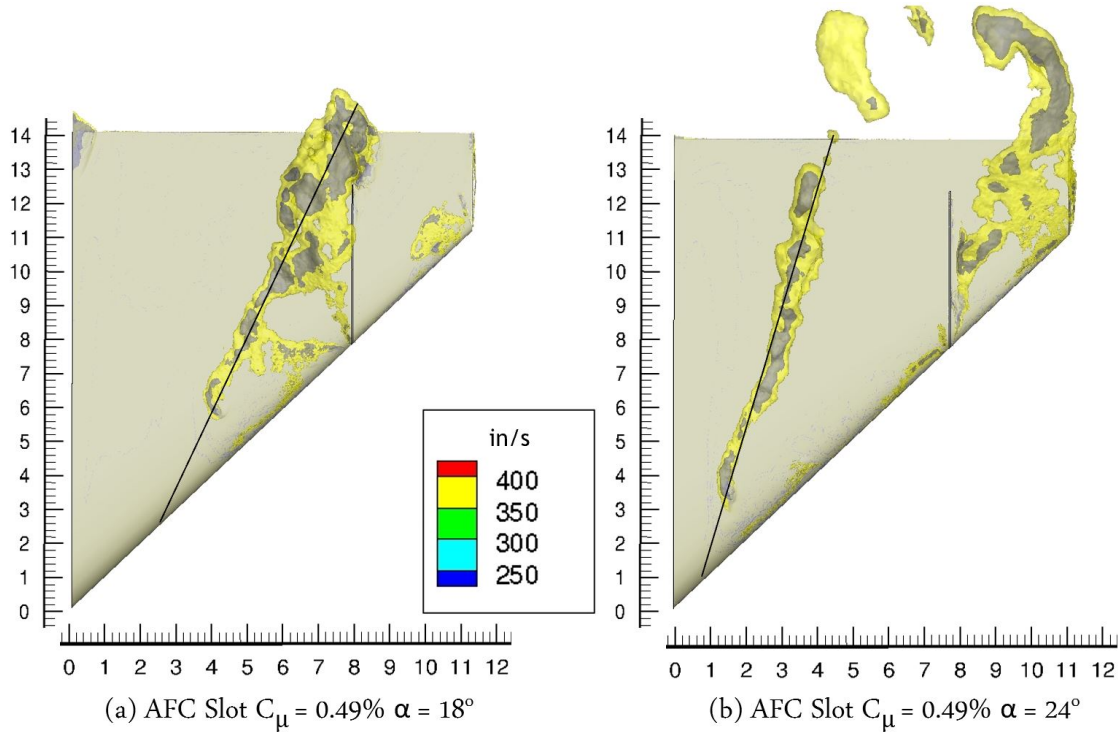


**Figure 45. NACA 0012 Cropped Delta-Wing AFC Slot,  $C_\mu = 0.49\%$ , CFD Model Vortex Core Comparison,  $\alpha = 18^\circ$  and  $24^\circ$ ,  $Re = 5 \times 10^5$ , Iso-Surface Velocity Magnitude**

## 4.2 Primary Testing Results

### 4.2.1 AFC Slot Width Optimization Results

The active flow control (AFC) slot width optimization study utilized the five scaled slot Mach numbers (M1-M5) listed in Table 6, which related slot velocity and ultimately mass flow, along with the five varying slot width (SW1-SW5) geometries, listed in Table 9. The 25 individual AFC slot performance configurations were simulated and performance coefficients described in Section 3.4 were produced for comparison and listed in Table 15. Coefficient of lift ( $C_L$ ) indicated the highest performance gain overall, based upon Demoret et al. experimental results, thus  $C_L$  was focused on as a suitable initial comparative performance measure. All data was gathered at  $\alpha = 24^\circ$  for each configuration as outlined in Section 3.6.2.1.

Calculation of the coefficient of lift percent gains ( $C_{L,\%Gain}$ ) versus baseline CFD coefficient of lift ( $C_{Lmax,Baseline} = 0.8021$ ) indicated the highest performing configurations with respect to increased lift. Comparison of these results revealed the highest lift performance configurations for each slot width (SW) was composed of the highest slot velocity (M5), or Mach, within that grouping. This indicates that the performance of the slot was directly related to momentum introduced to the system ( $C_\mu$ ). This deduction was a parallel assessment to Demoret et al. wind tunnel experimental results. However, with regards to energy reduction, in the form of  $C_{L,\%Gain}$  per  $C_\mu$ , the smallest slot velocity (M1) produced the most efficient use of the momentum added to the system with the least amount of overall gain in lift.

Of the highest lift performance configurations, four solutions produced significant gains which indicated potential candidates for selection as the optimized configuration. Arrangements included two experimental configurations (SW1 at M5 and SW1 at M4), which slot width reduction was deemed necessary for real-world use and removed them from contention, and the highest performing configurations from SW2

|                                                                                            | Designator  | $C_{L,\alpha=24^\circ}$ | $\Delta C_{L,Baseline}$ | $C_{L,\%Gain}$ vs. $C_{Lmax,CFDBaseline}$ | $C_\mu$ (%) | $C_{L,\%Gain} / C_\mu$ |
|--------------------------------------------------------------------------------------------|-------------|-------------------------|-------------------------|-------------------------------------------|-------------|------------------------|
| Wind Tunnel                                                                                | Baseline    | 0.8021                  | 0.0000                  | 0.00                                      | 0           | NA                     |
|                                                                                            | Passive BLF | 0.8505                  | 0.0484                  | 6.03                                      | 0           | NA                     |
|                                                                                            | SW1M1       | 0.8508                  | 0.0487                  | 6.07                                      | 0.49        | 12.39                  |
|                                                                                            | SW1M2       | 0.8861                  | 0.0840                  | 10.47                                     | 1.95        | 5.37                   |
|                                                                                            | SW1M3       | 0.9891                  | 0.1870                  | 23.32                                     | 4.4         | 5.30                   |
|                                                                                            | SW1M4       | 1.1013                  | 0.2992                  | 37.31                                     | 7.82        | 4.77                   |
|                                                                                            | SW1M5       | 1.1484                  | 0.3463                  | 43.17                                     | 12.22       | 3.53                   |
| CFD                                                                                        | SW1M1       | 0.8608                  | 0.0587                  | 7.32                                      | 0.49        | 14.94                  |
|                                                                                            | SW1M2       | 0.9165                  | 0.1144                  | 14.27                                     | 1.95        | 7.32                   |
|                                                                                            | SW1M3       | 0.8694                  | 0.0673                  | 8.39                                      | 4.4         | 1.91                   |
|                                                                                            | SW1M4       | 1.0366                  | 0.2345                  | 29.23                                     | 7.82        | 3.74                   |
|                                                                                            | SW1M5       | 1.0891                  | 0.2870                  | 35.78                                     | 12.22       | 2.93                   |
|                                                                                            | SW2M1       | 0.8887                  | 0.0866                  | 10.80                                     | 0.392       | 27.56                  |
|                                                                                            | SW2M2       | 0.8408                  | 0.0387                  | 4.82                                      | 1.56        | 3.09                   |
|                                                                                            | SW2M3       | 0.9017                  | 0.0996                  | 12.42                                     | 3.52        | 3.53                   |
|                                                                                            | SW2M4       | 0.9645                  | 0.1624                  | 20.24                                     | 6.256       | 3.24                   |
|                                                                                            | SW2M5       | 1.0391                  | 0.2370                  | 29.55                                     | 9.776       | 3.02                   |
|                                                                                            | SW3M1       | 0.9245                  | 0.1224                  | 15.26                                     | 0.294       | 51.91                  |
|                                                                                            | SW3M2       | 0.9211                  | 0.1190                  | 14.83                                     | 1.17        | 12.68                  |
|                                                                                            | SW3M3       | 0.9020                  | 0.0999                  | 12.46                                     | 2.64        | 4.72                   |
|                                                                                            | SW3M4       | 0.9434                  | 0.1413                  | 17.62                                     | 4.692       | 3.75                   |
|                                                                                            | SW3M5       | 0.9984                  | 0.1963                  | 24.48                                     | 7.332       | 3.34                   |
|                                                                                            | SW4M1       | 0.8682                  | 0.0661                  | 8.24                                      | 0.196       | 42.06                  |
|                                                                                            | SW4M2       | 0.8998                  | 0.0977                  | 12.18                                     | 0.78        | 15.61                  |
|                                                                                            | SW4M3       | 0.9147                  | 0.1126                  | 14.04                                     | 1.76        | 7.98                   |
|                                                                                            | SW4M4       | 0.9241                  | 0.1220                  | 15.21                                     | 3.128       | 4.86                   |
|                                                                                            | SW4M5       | 0.8754                  | 0.0733                  | 9.14                                      | 4.888       | 1.87                   |
|                                                                                            | SW5M1       | 0.8615                  | 0.0594                  | 7.41                                      | 0.098       | 75.59                  |
|                                                                                            | SW5M2       | 0.8637                  | 0.0616                  | 7.69                                      | 0.39        | 19.71                  |
|                                                                                            | SW5M3       | 0.9236                  | 0.1215                  | 15.14                                     | 0.88        | 17.21                  |
|                                                                                            | SW5M4       | 0.8928                  | 0.0907                  | 11.30                                     | 1.564       | 7.23                   |
|                                                                                            | SW5M5       | 0.8948                  | 0.0927                  | 11.56                                     | 2.444       | 4.73                   |
| Note:<br>- All Measurements at $\alpha = 24^\circ$ ,<br>- CFD Baseline $C_{Lmax} = 0.8021$ |             |                         |                         |                                           |             |                        |

**Table 15. NACA 0012 Cropped Delta-Wing AFC Slot Width CFD Optimization Data Comparison,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$**

(80% of SW1) and SW3 (60% of SW1) utilizing the highest Mach setting, M5. Comparison of the latter configurations revealed a variation in  $C_L$  of approximately 4%, in favor of SW2 at M5, with a significant variation in  $C_\mu$  of approximately 33%, favoring SW3 at M5. Furthermore, visualization of the data,  $C_{L,\%Gain}$  versus  $C_\mu$  in Figure 46, reveal the overall performance of SW3 as producing lift performance gains with a consistent reduction in output momentum, specifically at low  $C_\mu$  values. For the above-mentioned attributes of the SW3 (0.0222 in) at M5 (Mach = 0.8731) and momentum conservation outweighing the minimal variation in lift gain from SW2 at M5, the afore mentioned configuration was chosen as the optimal selection for use in

the continued AFC slot optimization study.

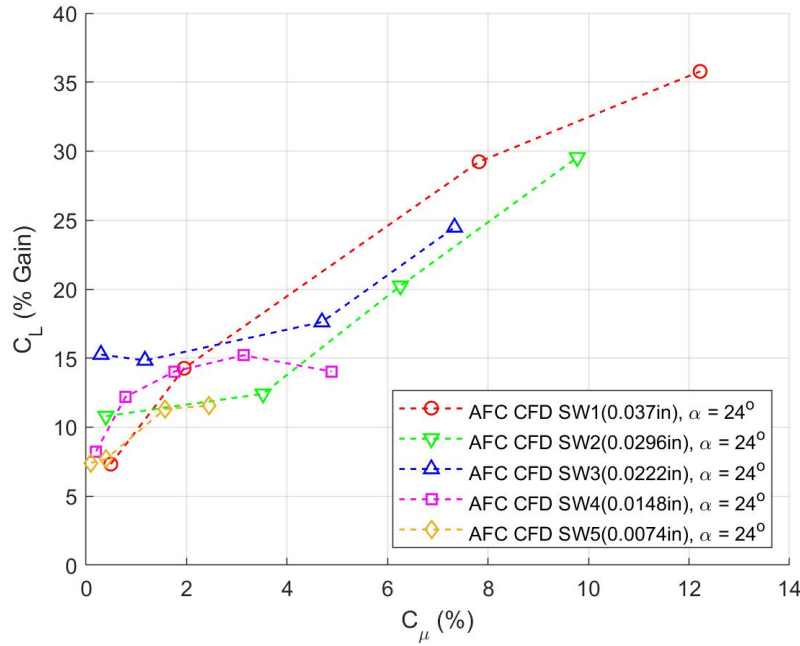


**Figure 46. NACA 0012 Cropped Delta-Wing AFC Slot Width Optimization: Coefficient of Lift Percent Gain ( $C_{L, \%Gain}$ ) vs. Coefficient of Momentum ( $C_{\mu}$ ) Comparison,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$**

#### 4.2.2 AFC Slot Length Optimization Results

The active flow control (AFC) slot length, or extent, optimization study utilized the eight configurations (EX1 thru EX8) outlined in Table 11 along with slot width optimized results described in Section 4.2.1. Updated configuration parameters were computed utilizing the optimized slot width and Mach (SW3 = 0.0222 in at  $M_5 = 0.8731$ ) and listed in Table 16 along with AFC slot performance coefficients, described in Section 3.4. Coefficient of lift ( $C_L$ ) captured the highest performance gain overall, as stated in Section 4.2.1, thus  $C_L$  was focused on as a suitable initial comparative performance measure. All data was gathered at  $\alpha = 24^\circ$  for each configuration as outlined in Section 3.6.2.2.

Similar to the slot width optimization, calculation of the coefficient of lift percent

gains ( $C_{L,\%Gain}$ ) versus baseline CFD coefficient of lift ( $C_{Lmax,Baseline} = 0.8021$ ) indicated the highest performing configurations with respect to increased lift. Comparison of the results annotated in Table 16 revealed the highest lift performance configurations for each slot extent (EX) integrated the largest slot areas in the simulation, in turn relating increased momentum with performance gains. However, configurations incorporating the lower surface of the AFC slot (-0.25 to 0  $x/c$ ) had reduced performance output, with increased  $C_\mu$ , compared to the configuration with equal upper surface AFC slot length, with reduced  $C_\mu$ .

| Designator                                                                                                                                                                                                                     | Surface Measurement<br>(x/c) | Area (in <sup>2</sup> ),<br>Constant SW3 | $C_{L,\alpha=24^\circ}$ | $\Delta C_{L,Baseline}$ | $C_{L,\%Gain}$ vs.<br>$C_{Lmax,CFDBaseline}$ | $C_\mu$ (%) | $C_{L,\%Gain} / C_\mu$ |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------|------------------------------------------|-------------------------|-------------------------|----------------------------------------------|-------------|------------------------|
| EX1                                                                                                                                                                                                                            | -0.25 to 0.75                | 0.1521                                   | 0.9984                  | 0.1963                  | 24.47                                        | 7.332       | 3.34                   |
| EX2                                                                                                                                                                                                                            | -0.25 to 1.0                 | 0.1901                                   | 1.0701                  | 0.268                   | 33.41                                        | 9.165       | 3.65                   |
| EX3                                                                                                                                                                                                                            | -0.25 to 0.5                 | 0.1141                                   | 0.9398                  | 0.1377                  | 17.17                                        | 5.499       | 3.12                   |
| EX4                                                                                                                                                                                                                            | 0 to 0.75                    | 0.1141                                   | 0.9992                  | 0.1971                  | 24.57                                        | 5.499       | 4.47                   |
| EX5                                                                                                                                                                                                                            | 0 to 0.5                     | 0.0760                                   | 0.9558                  | 0.1537                  | 19.16                                        | 3.666       | 5.23                   |
| EX6                                                                                                                                                                                                                            | 0 to 0.25                    | 0.0380                                   | 0.9065                  | 0.1044                  | 13.02                                        | 1.833       | 7.10                   |
| EX7                                                                                                                                                                                                                            | 0 to 1.0                     | 0.1521                                   | 1.1089                  | 0.3068                  | 38.25                                        | 7.332       | 5.22                   |
| EX8                                                                                                                                                                                                                            | 0.25 to 1.0                  | 0.1141                                   | 1.0399                  | 0.2378                  | 29.65                                        | 5.499       | 5.39                   |
| Note:<br>- All measurements simulated at $\alpha = 24^\circ$<br>- CFD Baseline $C_L = 0.8021$<br>- Zero indicates the leading edge<br>- Negative values follow the bottom surface<br>- Positive values follows the top surface |                              |                                          |                         |                         |                                              |             |                        |

**Table 16. NACA 0012 Cropped Delta-Wing, with Optimized Slot Width (SW3 = 0.0222 in), Slot Extent CFD Optimization Data Comparison,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$**

Results from Table 16 were plotted in Figure 47 and likewise detail the increased performance with removal of the lower portion of the AFC slot (-0.25 to 0  $x/c$ ). Furthermore, analysis of similar slot areas, specifically, EX3, EX4 and EX8, experiences a continuous increase in  $C_L$  performance gains as initial slot interaction moved away from the leading edge toward the trailing edge. This indicated that the AFC slot gains were dependent on where the slot interacted chordwise with the flow. Interactions further aft on the wing surface produced higher performance gains compared with interactions near the leading edge. With these reductions in scale and energy injection, the AFC slot was optimized. Additionally, unlike the passive BLF which wraps around the leading edge, the AFC slot hindered performance gains when the

slot momentum interacts with the lower surface of the wing. Section 4.3 detailed the flow field interactions.

Considering the highest coefficient of lift percent gains ( $C_{L,\%Gain}$ ) with substantial  $C_{L,\%Gain}/C_\mu$  output, EX7 produced a 38.25% gain, an increase of 13.77% from the slot width analysis, without an increase in momentum. Thus, the optimal configuration with respect to slot width and extent optimization consisted of the configuration designators SW3 (0.0222 in) with EX7 (0 to 1.0  $x/c$ ) at M5 (Mach = 0.8731). The final computational comparison utilized this configuration for optimized performance parameter generation.

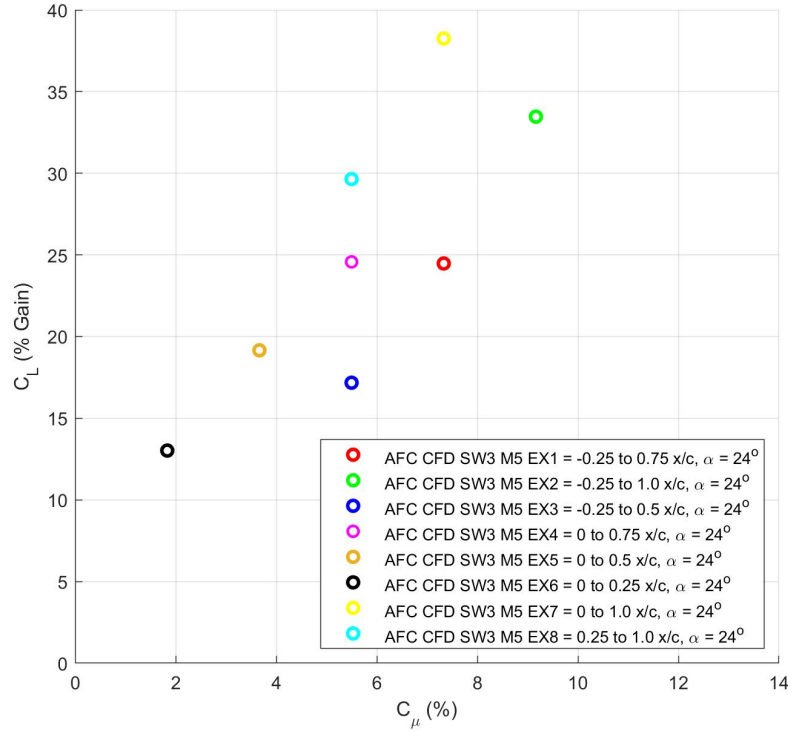


**Figure 47. NACA 0012 Cropped Delta-Wing AFC Slot Length (Extent) Comparison: Coefficient of Lift Percent Gain ( $C_{L,\%Gain}$ ) vs. Coefficient of Momentum ( $C_\mu$ ),  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ , Slot Width (SW3) = 0.0222 in, Mach (M5) = 0.8731**

### 4.3 Flow Visualization

The CFD generated flow fields of the baseline, passive BLF, best performing AFC slot wind tunnel configuration and optimized AFC slot configuration were compared to assess the critical flow features participating in the flow control performance enhancements. These visualizations provide insight into the mechanisms which aided previously reported configurations to outperform applied flow control methods.

Qualitative analysis of the surface pressure contour plots of the upper and lower surfaces of the NACA 0012 cropped delta-wing, Figures 48 and 49 respectively, reveal low and high pressure interactions with the various flow control configurations. Comparison of the upper surface pressure contour reveal large low pressure regions inboard of the AFC slot configurations, (c and d of Figure 48 with slot indicated by the arrow). These low-pressure regions produce suction on the surface which can be attributed to the significant increase in lift performance when compared to the baseline (a) and passive BLF (b with fence location indicated by the arrow). Compared to the passive BLF (b), the AFC slot configurations produce more low-pressure outboard of the slot. Comparison of the slot configurations (c and d) reveal the optimized solution (d) with the longer slot extent produced a larger surface area of low-pressure outboard of the slot. However, the increased momentum of the original wind tunnel model (c) generated a larger area of low-pressure inboard of the AFC slot. Analysis of the AFC slot configuration upper surfaces do not clearly indicate how the optimized AFC slot configuration outperformed the wind tunnel configuration at  $\alpha = 24^\circ$  due to both surface pressure contours being similar in average pressure over the upper surface and not indicating any large disparities.

Analysis of the lower surfaces pressure contours, Figure 49, immediately revealed the distinction among the flow control models. The wind tunnel AFC slot configuration (c) wrapped around the leading edge of the wing, similar to the passive BLF (b),

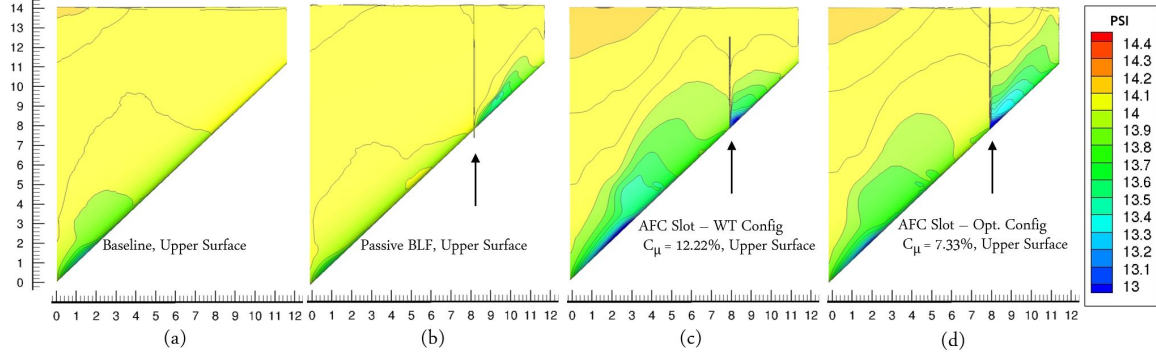


**Figure 48. NACA 0012 Cropped Delta-Wing Upper Surface Pressure (PSI) Contour Plot,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ : (a) Baseline Configuration, (b) Passive BLF Configuration, (c) AFC Slot Wind Tunnel (WT) Configuration,  $C_\mu = 12.22\%$ , (d) AFC Slot Optimized Configuration,  $C_\mu = 7.33\%$**

and injected airflow on the lower surface of the wing. This airflow injection disrupted the high-pressure region necessary to produce lift. The optimized slot configuration (d) does not disrupt the high-pressure region, thus allowing this configuration to outperform the wind tunnel model with increased lift generation.

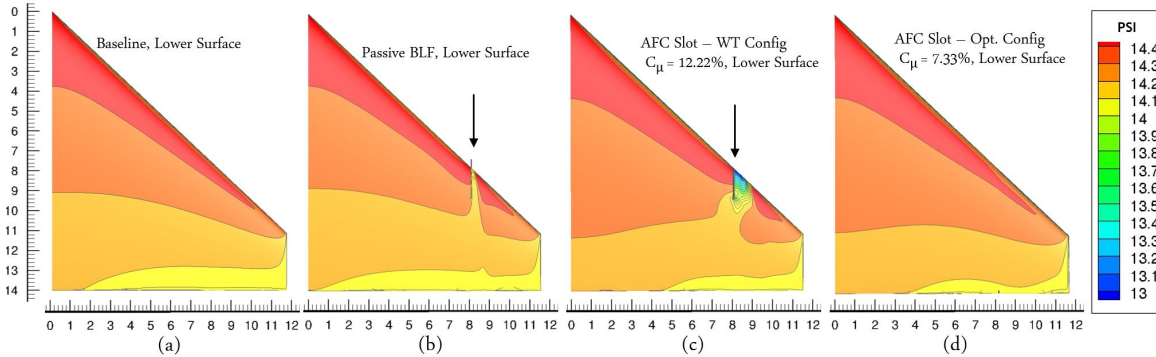


**Figure 49. NACA 0012 Cropped Delta-Wing Lower Surface Pressure (PSI) Contour Plot,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ : (a) Baseline Configuration, (b) Passive BLF Configuration, (c) AFC Slot Wind Tunnel (WT) Configuration,  $C_\mu = 12.22\%$ , (d) AFC Slot Optimized Configuration,  $C_\mu = 7.33\%$**

Extension of the surface contour into slices within the y-z plane provided an additional dimension of the pressure profile above and below the wing's surface. Slices taken at 60% and 80% chord, shown in Figure 50, revealed the large lower pressure regions created above the surface by the AFC slot configurations in columns (c) and (d). At the 80% chord location, the low-pressure region extends further inboard for

the optimized solution compared to the wind tunnel configuration as well as extending outboard of the AFC slot, marked with an arrow. Furthermore, the previously identified wind tunnel AFC slot interference along the lower high-pressure region was plainly identified at the 80% chord slice. The raised circular shape of the low pressure regions across all configurations indicate the presence of the vortex core, identified through delta-wing research and visualized in Section 4.1.3 while validating the CFD models.

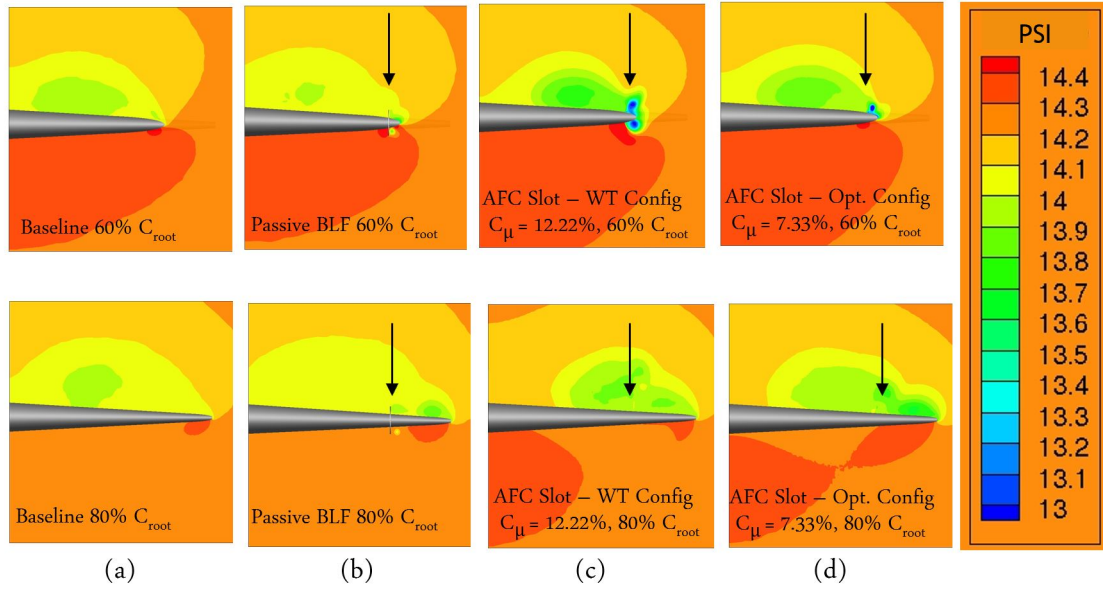


**Figure 50. NACA 0012 Cropped Delta-Wing Y-Z Plane Pressure (PSI) Slice, 60% and 80% Chord,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ : (a) Baseline Configuration, (b) Passive BLF Configuration, (c) AFC Slot Wind Tunnel (WT) Configuration,  $C_\mu = 12.22\%$ , (d) AFC Slot Optimized Configuration,  $C_\mu = 7.33\%$**

Visualization of surface particle streamtraces provided insight into surface flow interaction related to stall propagation. Delta wing theory, detailed in Section 2.1.3, described stall propagation emanating from the wingtip trailing edge and spreading inboard and toward the leading edge. Furthermore, spanwise flow also indicated regions of stall, thus the implementation of the passive BLF to halt spanwise flow and permit streamwise flow to resume outboard of the fence. Figure 51 provided insight into the particle interactions with the flow control mechanisms on the upper

surface of the wing. The baseline configuration (a) was well beyond its stall limits at  $\alpha = 24^\circ$  and clearly show spanwise flow across the majority of the upper surface. The passive BLF (b), with the physical fence marked with an arrow, indicated spanwise flow disruption inboard of the fence and streamwise flow resuming outboard of the fence to the wingtip. The wind tunnel AFC model (c), with the slot marked with an arrow, revealed the flow continuing its streamwise propagation aft of the slot due to the upper surface slot extent of 0 to  $0.75 x/c$  and not continuing to the trailing edge of the wing. Thus, streamwise flow only reoccurred directly outboard of the AFC slot but resumed a spanwise flow direction upon interaction with the unimpeded flow aft of the slot. The optimized AFC slot (d), with the slot indicated by an arrow, continues to the trailing edge and impeded all spanwise flow, similar to the passive BLF. This physical interaction further explained the substantial decrease in surface pressure outboard of the slot, visualized in Figure 48 for the optimized configuration (d).

Continued analysis of lower surface particle streamtraces, illustrated in Figure 52, indicated flow disruption produced by the wind tunnel AFC slot configuration (c). This flow disruption was analogous to the pressure disruption visualized in the

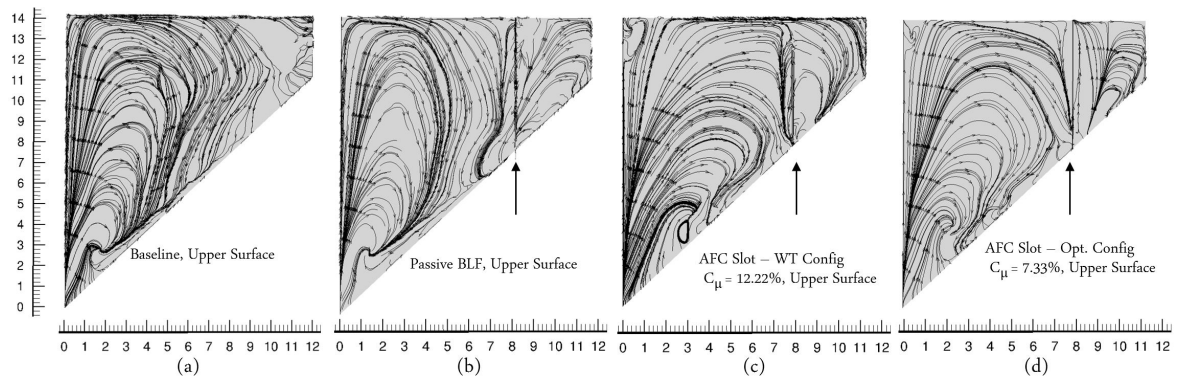


**Figure 51. NACA 0012 Cropped Delta-Wing Upper Surface Particle Streamtrace,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ : (a) Baseline Configuration, (b) Passive BLF Configuration, (c) AFC Slot Wind Tunnel (WT) Configuration,  $C_\mu = 12.22\%$ , (d) AFC Slot Optimized Configuration,  $C_\mu = 7.33\%$**

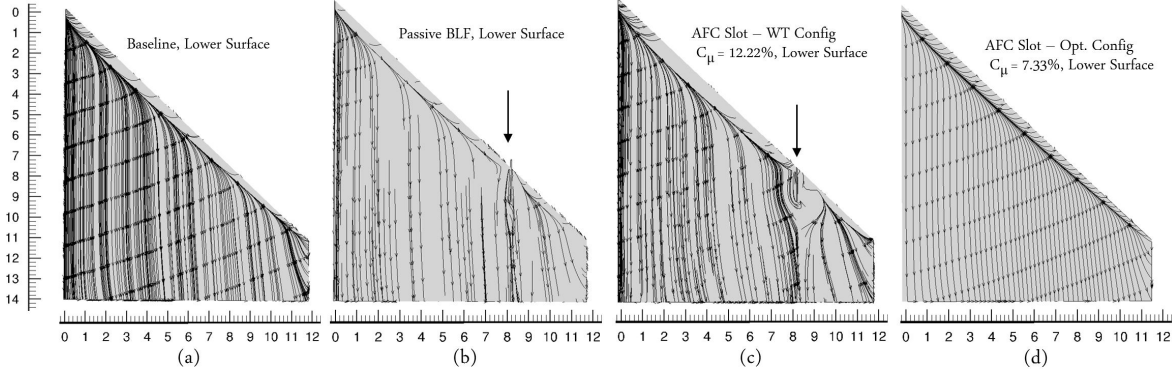


**Figure 52. NACA 0012 Cropped Delta-Wing Lower Surface Particle Streamtrace,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ : (a) Baseline Configuration, (b) Passive BLF Configuration, (c) AFC Slot Wind Tunnel (WT) Configuration,  $C_\mu = 12.22\%$ , (d) AFC Slot Optimized Configuration,  $C_\mu = 7.33\%$**

lower surface pressure contour plot for this configuration, Figure 49(c), affirming the reduced performance being a result of this interaction.

Creation of vector field slices along the y-z plane allowed visualization of the flow field direction while also viewing the magnitude of the flow field velocity. At 40% chord, the vector field provided initial visualization of the primary, leading edge vortex formation along the upper surface of the wing, shown in Figure 53. Specifically, the dark blue coloration indicated a well-developed vortex core propagating inboard toward the root chord ( $c_{root}$ ), shown in the baseline (a) and passive BLF (b) configurations. The AFC slot configurations, wind tunnel (c) and optimized (d), illustrate higher velocity flow above the vortex core, attributed to the AFC slot airflow injection, seemingly driving the core consistently towards the leading edge for both AFC slot configurations.

At 60% chord, the vector field interacted with the flow control devices indicated by arrows in Figure 54. For the baseline (a) and passive BLF (b) configurations, the low velocity primary leading edge vortex core continued within close proximity to the  $c_{root}$  while the primary leading edge vortex core for the AFC slot configurations continued along a path relative to the leading-edge sweep, indicating entrainment of

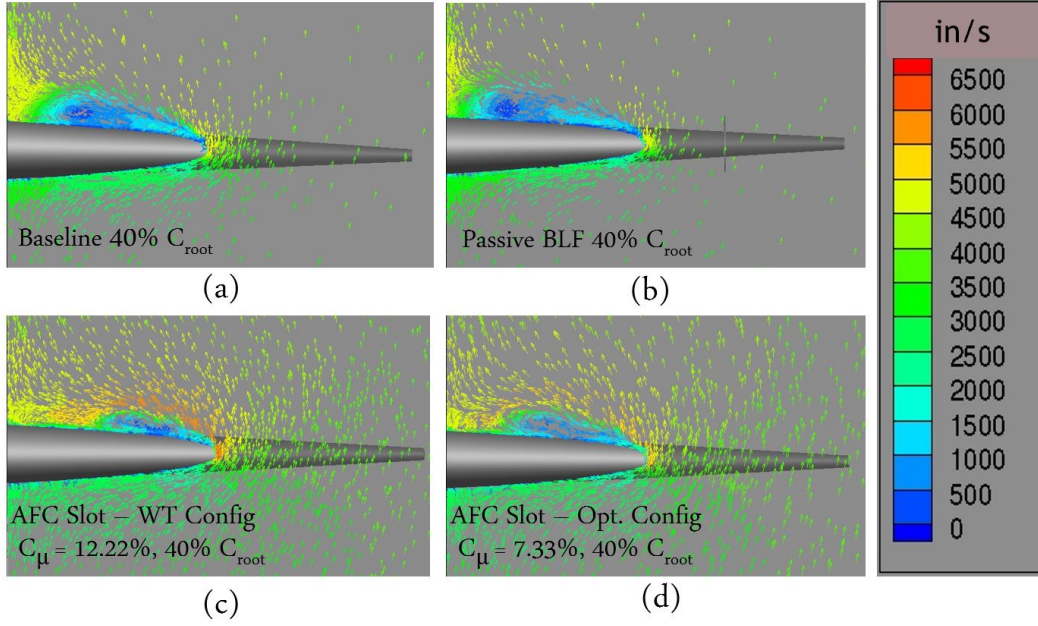


**Figure 53. NACA 0012 Cropped Delta-Wing Y-Z Plane Vector Slice Colored by Velocity Magnitude (in/s) 40% Chord,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ : (a) Baseline Configuration, (b) Passive BLF Configuration, (c) AFC Slot Wind Tunnel (WT) Configuration,  $C_\mu = 12.22\%$ , (d) AFC Slot Optimized Configuration,  $C_\mu = 7.33\%$**

the primary leading edge vortex with the AFC slot airflow.

At 80% chord, the vector field interacted with the flow control devices indicated by arrows in Figure 55. For the baseline (a) and passive BLF (b) configurations, the low velocity primary leading edge vortex core continues near the  $c_{root}$  and visualization of the wing tip vortex comes into view. The passive BLF configuration was seen to have additional flow interaction outboard of the passive fence similar to the interactions illustrated with the wind tunnel (c) and optimized (d) AFC slot configurations. The vortex cores for the AFC slot configurations remained inboard of the slot with a large spiraling vortex remaining over the majority of the wing's upper surface, a further indication of the primary lifting vortex entrainment with the AFC slot airflow. Furthermore, the wingtip vortex of both AFC slot models showed interaction with the slot airflow in a counter rotating manner.

At 100% chord, the vector field interacted with the flow control devices indicated

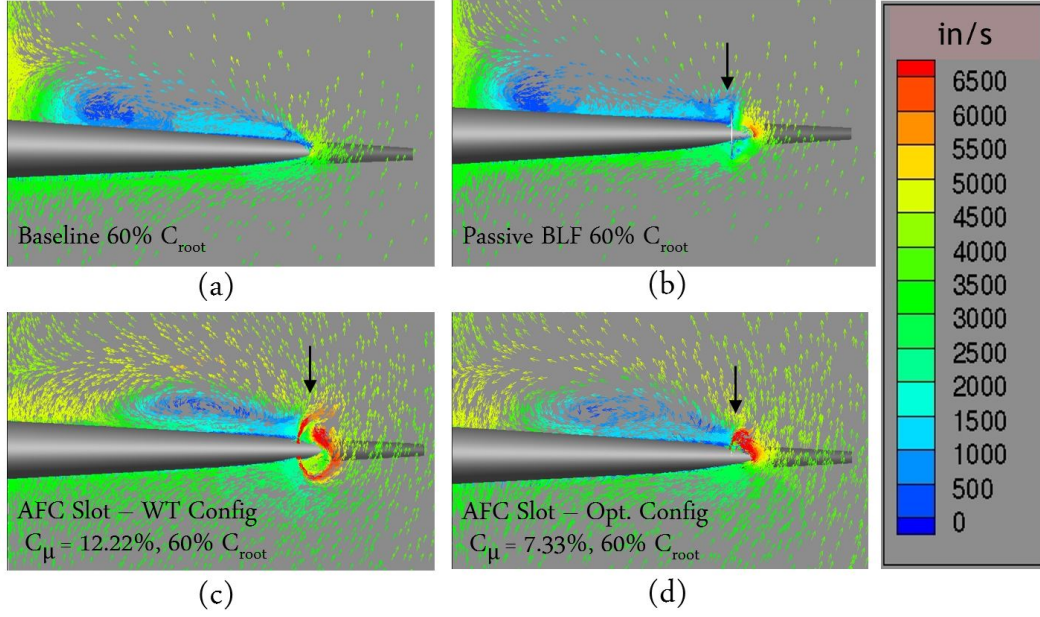


Figure 54. NACA 0012 Cropped Delta-Wing Y-Z Plane Vector Slice Colored by Velocity Magnitude (in/s) 60% Chord,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ : (a) Baseline Configuration, (b) Passive BLF Configuration, (c) AFC Slot Wind Tunnel (WT) Configuration,  $C_\mu = 12.22\%$ , (d) AFC Slot Optimized Configuration,  $C_\mu = 7.33\%$

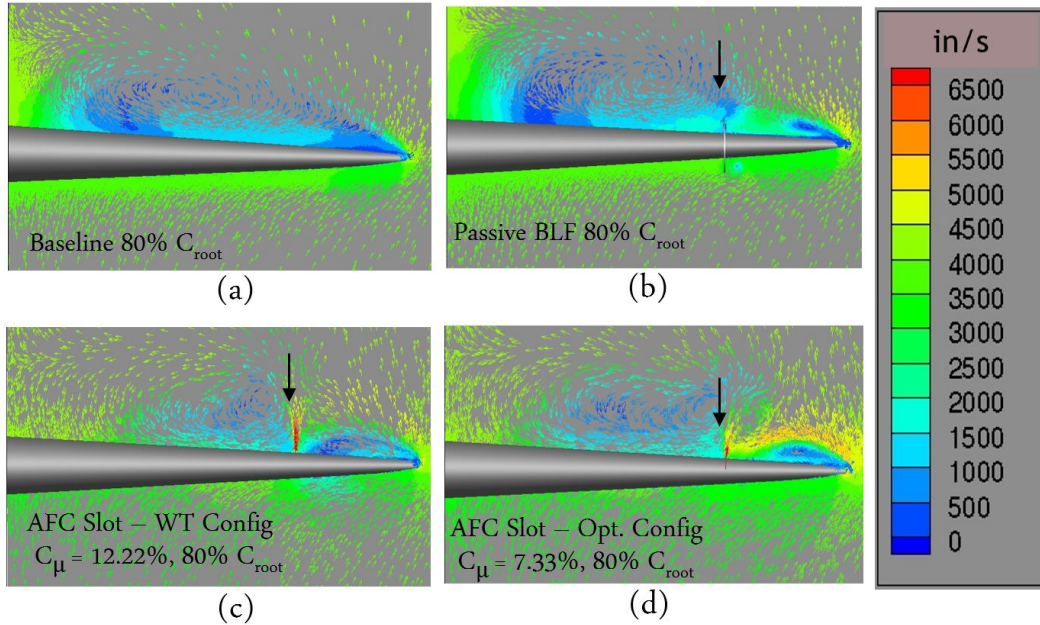


Figure 55. NACA 0012 Cropped Delta-Wing Y-Z Plane Vector Slice Colored by Velocity Magnitude (in/s) 80% Chord,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ : (a) Baseline Configuration, (b) Passive BLF Configuration, (c) AFC Slot Wind Tunnel (WT) Configuration,  $C_\mu = 12.22\%$ , (d) AFC Slot Optimized Configuration,  $C_\mu = 7.33\%$

by arrows in Figure 56. For the baseline (a) and passive BLF (b) configurations, the low velocity vortex core lifted from the surface of the wing, no longer producing vortex lift. However, the BLF wingtip vortex showed to be intact with strong vector rotation energizing the boundary-layer. The wind tunnel AFC slot configuration (c) primary vortex has also lifted from the surface of the wing. Likewise, the wingtip vortex lifted from the surface indicating no additional performance gains were provided from the flow structure. However, the optimized AFC slot configuration (d) primary vortex continued to show low speed vector rotation near the slot and surface of the wing due to the slot extending to the trailing edge. Continued interaction with the wing tip vortex and AFC slot energized the flow outboard of the flow control mechanism. This allowed for the vortex to stay intact and providing vortex lift between the slot and wingtip. The simultaneous interactions of halting the spanwise flow while also injecting momentum into the primary, leading edge vortex and wingtip vortex are attributes of maximum slot extension to the trailing edge. This analysis coincides with previous visualization analysis of pressure distributions and confirms the vortex-slot viscous entrainment interaction being the primary source of lift performance gains.

Utilizing the quantitative velocity magnitude values of the vortex cores illustrated from the y-z plane slices, 3D iso-surfaces of the vortex cores were generated and shown in Figure 57. All configurations were compared at  $\alpha = 24^\circ$ . For both the baseline and passive BLF configurations, as determined through analysis of the y-z plane slices, the primary, leading edge vortex extended within close proximity with the root chord ( $c_{root}$ ) at a steep sweep angle of approximately  $75^\circ$  for the baseline and to  $77^\circ$  for the passive BLF. Furthermore, the leading edge vortex began formation within 1in from the nose of the wing. Vortex interaction with the AFC slot flow entrained the primary vortex of both configurations (c and d) to gravitate toward the source of the injected airflow, reducing the sweep angle of the vortex to  $62^\circ$  for the wind tunnel AFC slot

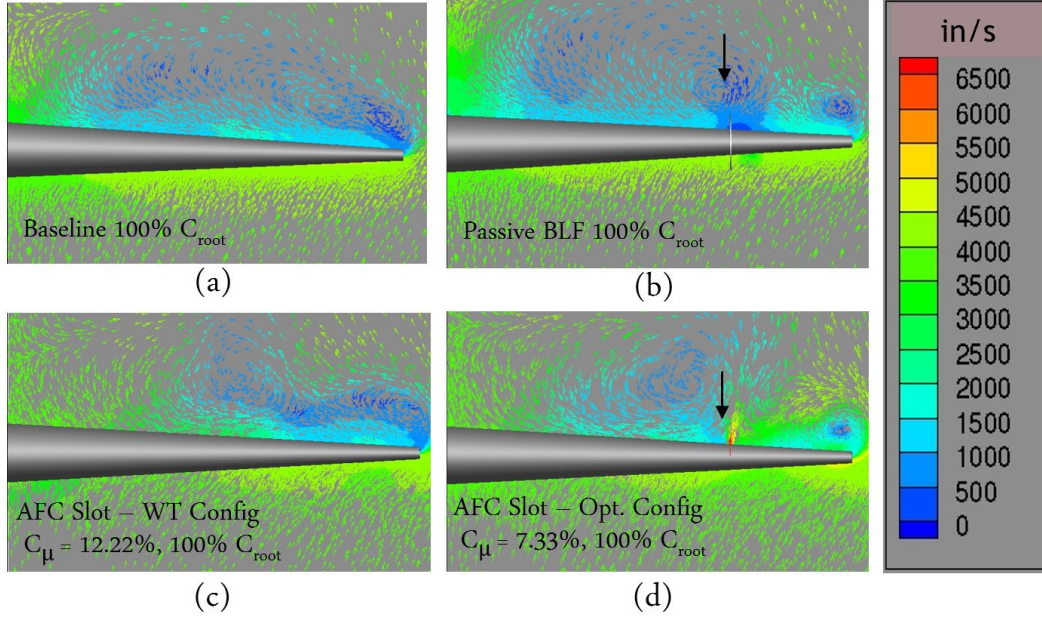


**Figure 56. NACA 0012 Cropped Delta-Wing Y-Z Plane Vector Slice Colored by Velocity Magnitude (in/s) 100% Chord,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ : (a) Baseline Configuration, (b) Passive BLF Configuration, (c) AFC Slot Wind Tunnel (WT) Configuration,  $C_\mu = 12.22\%$ , 100%  $C_{root}$ , (d) AFC Slot Optimized Configuration,  $C_\mu = 7.33\%$**

configuration and  $70^\circ$  for the optimized AFC slot model. Analysis of the wingtip vortex core indicated the vortex propagated to a position over the wing for all flow control methods and remained intact, while the baseline configuration had separated and broken down. Although the wing tip vortex was present over the wing for the passive BLF, both AFC slot models clearly illustrate the wingtip vortex interacting with the AFC slot injected flow and entrained the vortex to the slot leading edge. This visualization further supports the deduction that the primary, leading edge and wingtip vortices interaction with the AFC slot momentum injection being the primary source of lift performance gains. Furthermore, extension of the slot to the trailing edge allowed the wingtip vortex to be undisturbed and showed a well-defined core structure unlike the AFC slot  $0.75 x/c$  upper slot extent of the best performing wind tunnel configuration.

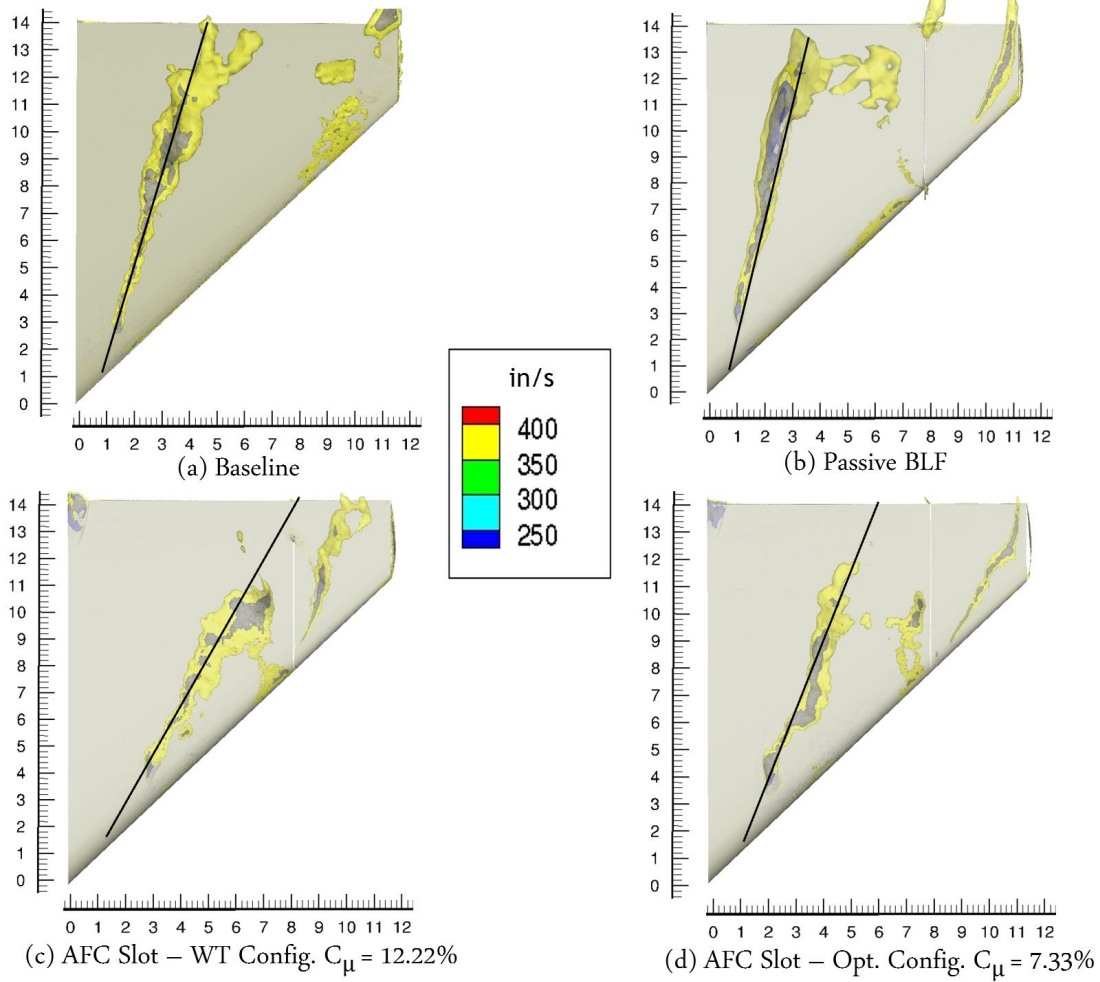


**Figure 57.** NACA 0012 Cropped Delta-Wing Upper Iso-Surface of Low-Velocity Magnitude (in/s) Vortex Cores,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ : (a) Baseline Configuration, (b) Passive BLF Configuration, (c) AFC Slot Wind Tunnel (WT) Configuration,  $C_\mu = 12.22\%$ , (d) AFC Slot Optimized Configuration,  $C_\mu = 7.33\%$

#### 4.4 Final Comparison

Utilizing the optimized AFC slot parameters from Sections 4.2.1 and 4.2.2, performance parameters listed in Section 3.4 over a angle-of-attack sweep of  $0^\circ$  to  $32^\circ$  with a  $Re = 5 \times 10^5$  were produced and compared to wind tunnel experimental configurations. Comparison results were compiled in Table 17 for the wind tunnel baseline model, passive BLF model, AFC slot highest performing configuration ( $C_\mu = 12.22\%$ ) and similar producing  $C_\mu$  model in comparison to the optimized CFD configuration.

The wind tunnel AFC slot  $C_\mu = 12.22\%$  was reported by Demoret et al. with a maximum  $C_{Lmax,\%Gain} = 61.05\%$ . However, with these extraordinary gains produced, the slot dimensions and momentum injected into the system was unrealistic. Reduction and overall optimization of the AFC slot was required. Concluding the optimization study, overall dimensions of the AFC slot were reduced, the slot width by 33.3% and the overall area by 33.3%. According to the coefficient of momentum equation from Section 3.4, momentum reduction scales linearly with area, thus the momentum input was also reduced by 33.3% compared to the wind tunnel's highest input  $C_\mu = 12.22\%$ . With these reductions in scale and energy injection, the optimized AFC slot for the NACA 0012 cropped delta-wing produced a  $C_{Lmax,\%Gain} = 41.09\%$  at  $\alpha = 22^\circ$ ,  $6^\circ$  earlier than the max performing wind tunnel configuration.

| Configuration |                                        | $C_{Lmax}$ | $\alpha_{C_{Lmax}}$<br>(deg) | $C_{L,\%Gain}$ vs.<br>$C_{Lmax,CFDBaseline}$ | $C_\mu$<br>(%) | $C_{Lmax,\%Gain} / C_\mu$ | Slot Mach | Slot Width<br>(in) | Slot Extent<br>(x/c) | Area<br>(in <sup>2</sup> ) |
|---------------|----------------------------------------|------------|------------------------------|----------------------------------------------|----------------|---------------------------|-----------|--------------------|----------------------|----------------------------|
| Wind Tunnel   | Baseline                               | 0.8021     | 22                           | 0                                            | NA             | NA                        | NA        | NA                 | NA                   | NA                         |
|               | Passive BLF                            | 0.8753     | 22                           | 9.13                                         | NA             | NA                        | NA        | NA                 | NA                   | NA                         |
|               | AFC Slot,<br>Max Performance           | 1.2918     | 28                           | 61.05                                        | 12.22          | 5.00                      | 0.8731    | 0.037              | -0.25 - 0.75         | 0.2535                     |
|               | AFC Slot,<br>Comparable<br>Performance | 1.1246     | 26                           | 40.21                                        | 7.82           | 5.14                      | 0.6984    | 0.037              | -0.25 - 0.75         | 0.2535                     |
| CFD           | Optimal AFC Slot                       | 1.1317     | 22                           | 41.09                                        | 7.33           | 5.61                      | 0.8731    | 0.0222             | 0 to 1.0             | 0.1521                     |

**Table 17. NACA 0012 Cropped Delta-Wing Final Optimization Configuration Vs. Demoret et al. Wind Tunnel Results,  $Re = 5 \times 10^5$**

Lift configuration comparisons, via the coefficient of lift ( $C_L$ ), were plotted in Figure 59. The optimized solution produced increased lift at lower angles-of-attack but does not delay stall of the wing in comparison to AFC slot wind tunnel models. The optimized solution improved upon the lift curve slope which can be attributed to energizing the primary, leading edge vortex, through direct air flow injection, and wingtip vortex, through the production of a counter rotating vortex, via the AFC slot which increased the vortex lift being produced, outlined in Section 4.3.

Drag configuration comparisons, via the coefficient of drag ( $C_D$ ), were plotted versus angle-of-attack ( $\alpha$ ) in Figure 59. The plot showed the optimized configuration CFD model trending along the experimental results and producing reduced drag at

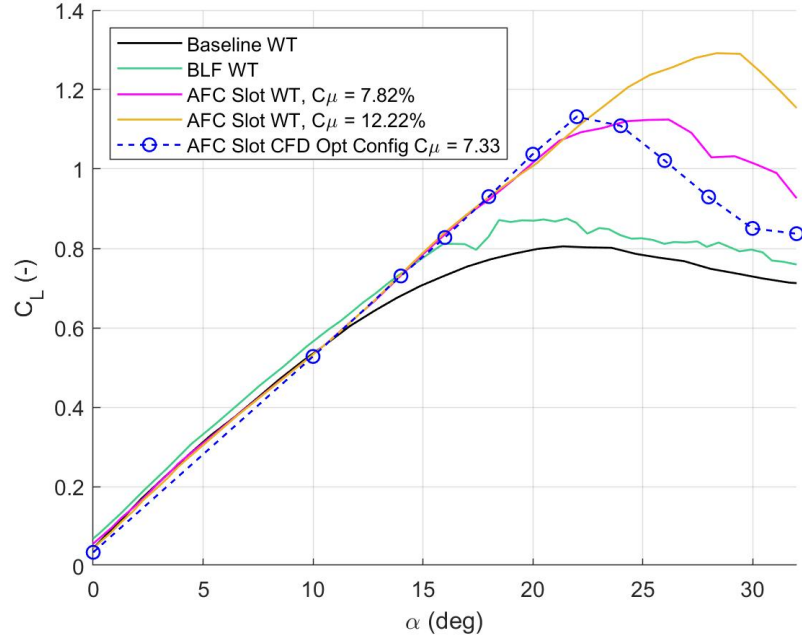


**Figure 58.**  $C_L$  vs  $\alpha$  for NACA 0012 Cropped Delta-Wing Configurations,  $\alpha = 0^\circ$  to  $32^\circ$ ,  $Re = 5 \times 10^5$

increasing angles-of-attack similar to experimental data. Comparison of drag with respect to lift ( $C_L$  vs  $C_D$ ), also known as the drag polar, showed a more useful representation of the configuration's drag characteristics, given in Figure 60. Also trending with experimental data, the optimized AFC slot does achieve its peak lift with a significantly reduced coefficient of drag, unlike the comparable  $C_\mu = 7.82\%$  wind tunnel configuration which almost doubles the drag to achieve the same  $C_{Lmax}$ . However, from Figure 58, the comparable  $C_\mu = 7.82\%$  wind tunnel configuration achieves its  $C_{Lmax}$  an additional  $4^\circ$  after the optimized solution, thus the increased drag associated with achieving the comparable  $C_\mu = 7.82\%$  wind tunnel model's  $C_{Lmax}$  was the result of the increase angle-of-attack.

Pitching moment configuration comparisons, via the moment coefficient ( $C_M$ ), were plotted versus angle-of-attack ( $\alpha$ ) in Figure 61. The plot showed the optimized configuration CFD model trending along the experimental results. For the duration

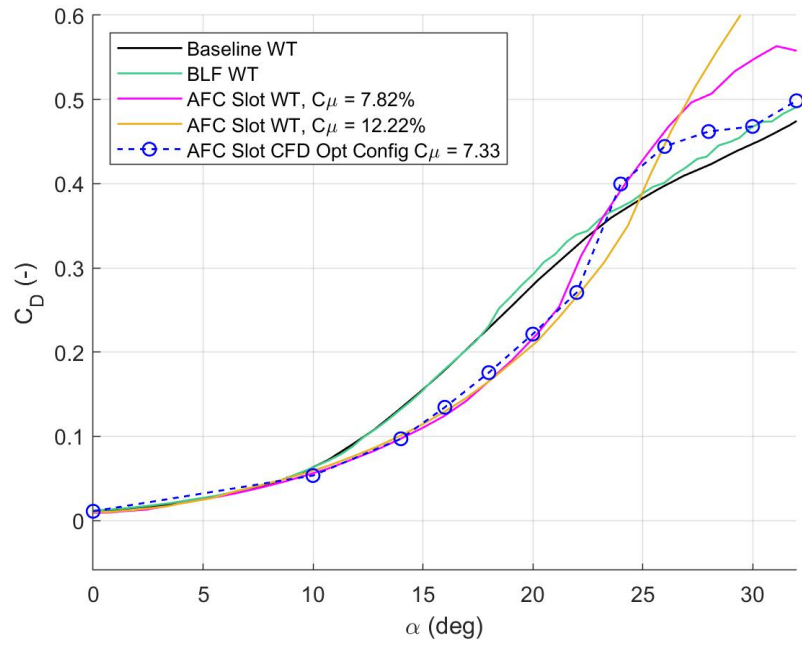


Figure 59.  $C_D$  vs.  $\alpha$  for NACA 0012 Cropped Delta-Wing Configurations,  $\alpha = 0^\circ$  to  $32^\circ$ ,  $Re = 5 \times 10^5$

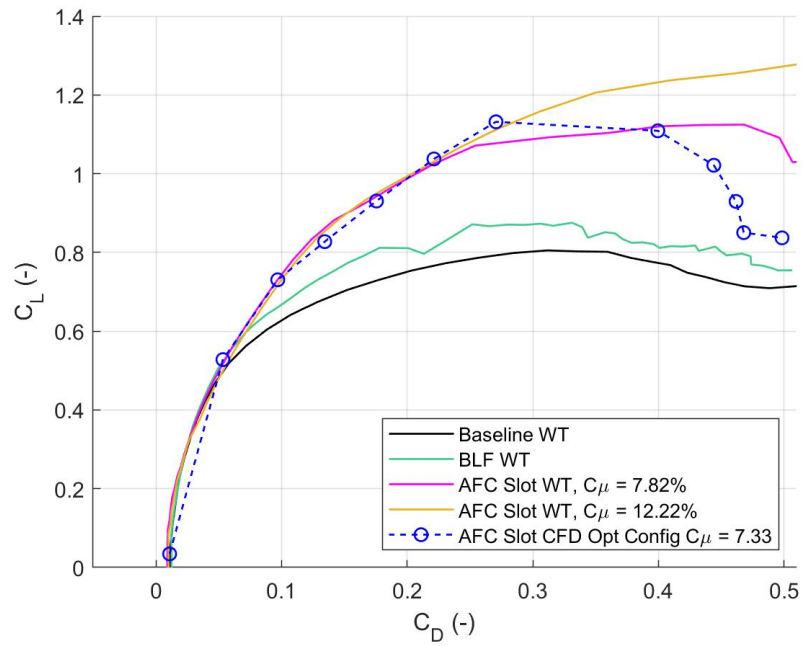


Figure 60.  $C_L$  vs.  $C_D$  (Drag Polar) for NACA 0012 Cropped Delta-Wing Configurations,  $\alpha = 0^\circ$  to  $32^\circ$ ,  $Re = 5 \times 10^5$

of the  $\alpha$  sweep, the optimized AFC slot produced a continuous negative pitching moment. Furthermore, as indicated by the passive BLF data, a destabilizing pitching moment existed within a delta-wing configuration. However, the optimized AFC slot configuration indicated no destabilizing pitching moment being present, coinciding with the wind tunnel AFC slot models.

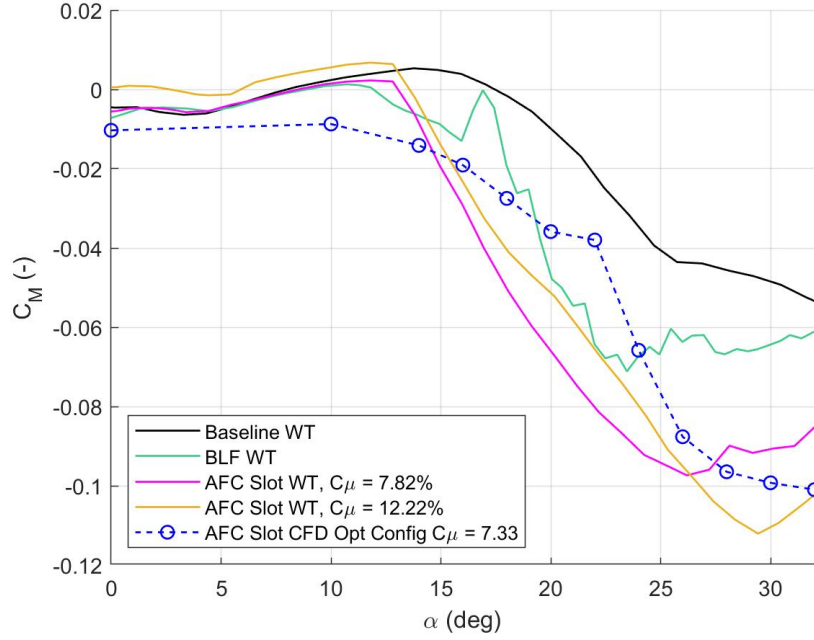


**Figure 61.**  $C_M$  vs.  $\alpha$  for NACA 0012 Cropped Delta-Wing Configurations,  $\alpha = 0^\circ$  to  $32^\circ$ ,  $Re = 5 \times 10^5$

## V. Conclusion

### 5.1 Final Conclusion

Utilizing computational fluid dynamic (CFD) simulations, the presented study was able to further the investigation of replicating and improving upon the performance of a NACA 0012 cropped delta-wing ( $C_{root} = 14$  in,  $C_{tip} = 2.8$  in,  $\lambda = 45^\circ$ ,  $b = 11.5625$  in) at high angles-of-attack with an active flow control (AFC) fluidic fence via wall-normal, steady blowing from an optimized single, chordwise slot located at  $z/b = 70\%$ , matching that of Demoret's preceding study configuration parameters. The data was generated using CREATE-AV Kestrel v10.1rc5 CFD software on the Department of Defense (DoD) High Performance Computing (HPC) systems. The flight regime was held constant at a Mach numbers of 0.18 and a Reynolds number of  $5.0 \times 10^5$ , based on the root chord of 14 in. Computational fluidic performance solutions were successfully compared to previously obtained wind tunnel experimental results of three configurations, baseline, boundary-layer fence and AFC slot of a single momentum coefficients ( $C_\mu = 0.49\%$ ), to validate the CFD model prior to slot optimization. Performance parameters compared were coefficients of lift ( $C_L$ ), drag ( $C_D$ ) and pitching moment ( $C_M$ ) at angles-of-attack ( $\alpha$ ) ranging from  $0^\circ$  to  $30^\circ$ . Optimization parameters included five reduced slot widths, five slot velocities converted to Mach number for use in Kestrel and eight slot length (or extent) configurations. Reduced slot widths were generated in increments of 20% from the original experimental configured slot width. Slot Mach numbers were developed from experimental coefficients of momentum ( $C_\mu = 0.49\%$ ,  $1.95\%$ ,  $4.4\%$ ,  $7.82\%$  and  $12.22\%$ ) at given volumetric flow rates (200, 400, 600, 800 and 1,000 SLPM). Slot extents varied in length beginning at  $0.25 x/c$  on the lower surface of the wing and continuing around the leading edge to the trailing edge along the upper surface. Performance parameters

used to validate the CFD model, obtained from computationally generated forces and moments, was also used during optimization to capture, compare and assess overall performance gains which also determined the optimal slot parameter configuration. Furthermore, surface flow visualization was assessed with Tecplot 360 in an effort to reveal the unique AFC flow interaction with momentum injecting vortices.

Table 18 shows a summary of the optimization parameters and significant comparative results from experimental results for the present study. Computational results produced accurate comparisons to experimental results, where performance parameter trends and developed fluid structures were analogous with delta-wing characteristics. The optimization produced an overall dimension reduction of the AFC slot, with the slot width reduced by 40%, which likewise reduced the overall area by 40%. With the reduction in area, the momentum input was also decreased by 40% compared to the wind tunnel's highest input  $C_\mu = 12.22\%$ . Removal of the lower  $0.25 x/c$  significantly improved performance due to a negative impact upon the high-pressure region of the lower wing surface. Continuation of the slot on the low-pressure surface from  $0.75 x/c$  to the trailing edge provided an additional performance gain by impeding spanwise flow that translates to stall propagation, injecting added momentum over the lifting surface of the wing and continuing flow interaction with the leading-edge and wingtip vortices. Slot extent analysis indicated that the AFC slot gains were dependent on where the slot interacted chordwise with the flow. Interactions further aft on the wing surface produced higher performance gains compared with interactions near the leading edge. These gain improvements were attributed to the simultaneous interactions of halting the spanwise flow while also injecting momentum into the primary, leading edge vortex and wingtip vortex. With these reductions in scale and energy injection, the optimized AFC slot for the NACA 0012 cropped delta-wing produced a  $C_{Lmax, \%Gain} = 41.09\%$  at an  $\alpha = 22^\circ$ ,  $6^\circ$  earlier than the max performing wind

tunnel configuration. Additionally, the optimized AFC slot configuration indicated no destabilizing pitching moment being present, coinciding with experimental wind tunnel results.

| Optimized AFC Slot Parameters                   |          |
|-------------------------------------------------|----------|
| Slot Width (in)                                 | 0.0222   |
| Slot Extent (x/c)                               | 0 to 1.0 |
| Mach                                            | 0.873    |
| Spanwise Location (z/b)                         | 0.7      |
| Slot Area (in <sup>2</sup> )                    | 0.152    |
| $C_\mu$ (%)                                     | 7.33     |
| $C_{Lmax}$                                      | 1.13     |
| $\alpha_{C_{Lmax}}$                             | 22       |
| $C_{L,\%Gain}$ vs. $C_{Lmax,CFDBaseline}$       | 41.09    |
| $C_{L,\%Gain} / C_\mu$                          | 5.61     |
|                                                 |          |
| Wind Tunnel AFC Slot Max Performance Comparison |          |
| Momentum Reduction (%)                          | -40.10   |
| $\Delta C_L$                                    | 0.1601   |
| $C_{L,\%Reduction}$ vs. $C_{Lmax,WTMax}$        | -12.39   |
| $\Delta \alpha_{C_{Lmax}}$ (deg)                | 7        |

**Table 18. NACA 0012 Cropped Delta-Wing Optimization Parameter Summary,  $Re = 5 \times 10^5$**

Visualizations supported the deduction that the primary and wingtip vortices interaction with the AFC slot momentum injection being the primary source of lift performance enhancement. The optimized solution was seen to improve upon total lift which can be attributed to energizing the primary vortex through direct air flow injection and entrainment, and wingtip vortex through the production of a counter rotating vortex, via the AFC slot, increasing the production of vortex lift. The extension of the AFC slot to the trailing edge provided continuous interaction with the primary and wing tip vortices by energizing the flow structures both inboard and outboard of the active flow mechanism. Furthermore, extension of the slot permitted the wingtip vortex to be undisturbed, halting the spanwise flow, allowing the structure to hold a well-defined core across the wing surface. This allowed for the vortices

to stay intact and provided vortex lift across the wing surface at increasing angle-of-attack. Visualization analysis of pressure distributions confirms the vortex-slot viscous entrainment interaction supporting the conclusion of this interaction being the primary source of lift performance gains.

## 5.2 Future Work

The scope of the current research was the product of previous studies and their results and lessons learned. Reflection of the results produced from the parameters studied revealed additional optimization or reconfiguration of the AFC slot on the NACA 0012 cropped delta-wing was necessary to further reduce momentum, to more realistic thresholds, and improve upon the vortex-slot interaction. Additional areas of interest to be researched include, but are not limited to, a focused investigation on active flow mechanisms physical interaction, including solid slots, sectioned slots, jets, their combination, and steady or pulsed blowing, with a swept wing leading edge vortex, and optimization of the slots spanwise location and sweep angle due to the leading-edge vortex physical characteristics dependence on wing geometry and angle-of-attack. Further investigation also includes effects of multiple spanwise AFC slots on swept wing performance, with the AFC slots capable of being activated and deactivate depending on the leading-edge vortex location during an angle-of-attack sweep, and examination of performance and entrainment effects when applying supersonic slot velocities.

Scheduled continuation of flow control research includes determination of effect of optimal placement of passive vortex generators on a T-38, and flight test of vortex generator configuration with comparison to experimental data, and characterization of wake roll-up utilizing a NACA 0012. Additionally, AFC specific research includes as study of orifice (jet/small slot) geometry, orientation, and location to instigate

lift vortex formation at low angles-of-attack through small perturbation vorticity generation and leading-edge flow separation to enhance lift at low angles-of-attack.

## Appendix A. Time-Resolution Plots

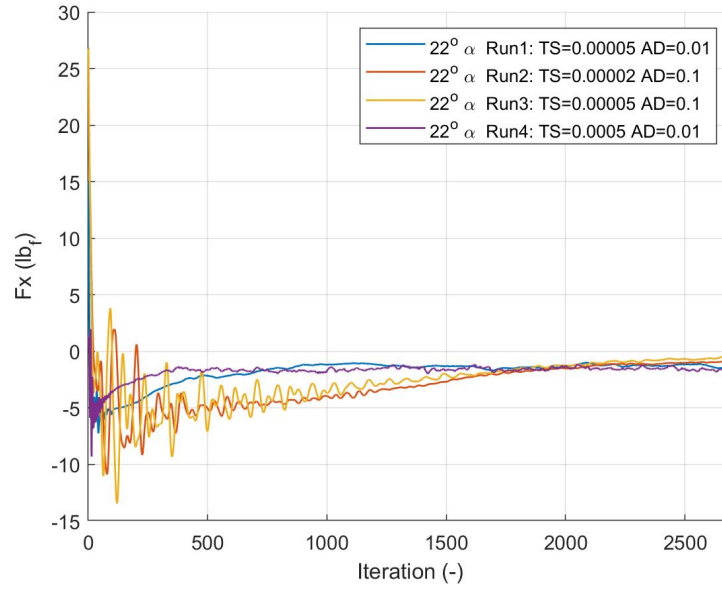


Figure 62. NACA 0012 Cropped Delta-Wing Baseline CFD Model Axial Force ( $F_x$ ) Time Resolution Results,  $\alpha = 22^\circ$ ,  $Re = 5 \times 10^5$ , Time Step (TS) and Advective Damping (AD)

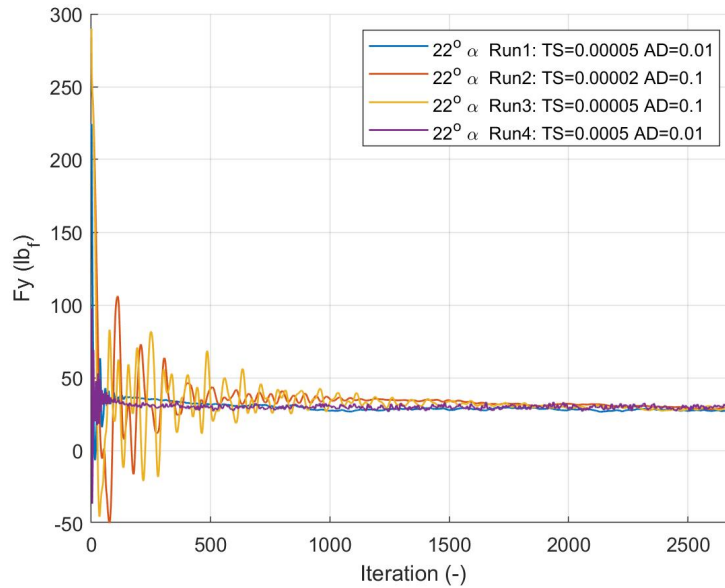


Figure 63. NACA 0012 Cropped Delta-Wing Baseline CFD Model Normal Force ( $F_y$ ) Time Resolution Results,  $\alpha = 22^\circ$ ,  $Re = 5 \times 10^5$ , Time Step (TS) and Advective Damping (AD)

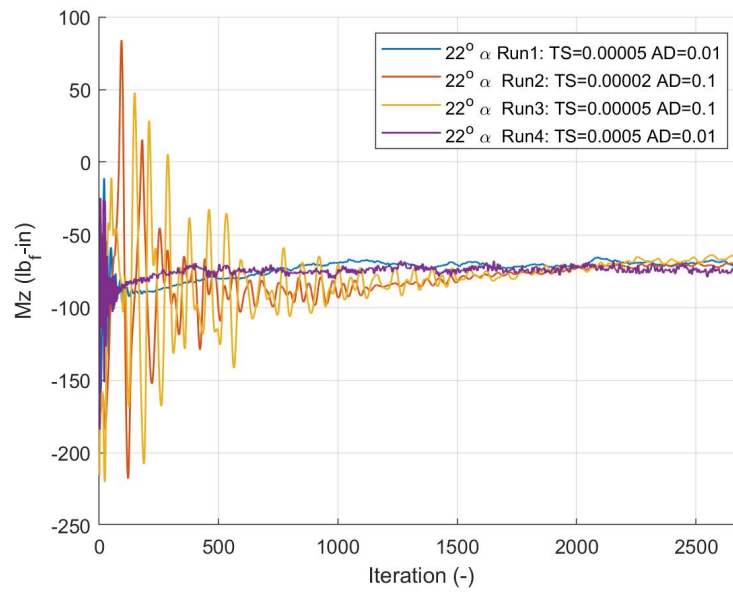


**Figure 64. NACA 0012 Cropped Delta-Wing Baseline CFD Model Moment About Z-Axis (Mz) Time Resolution Results,  $\alpha = 22^\circ$ ,  $Re = 5 \times 10^5$ , Time Step (TS) and Advective Damping (AD)**

## Appendix B. Mesh Refinement Plots

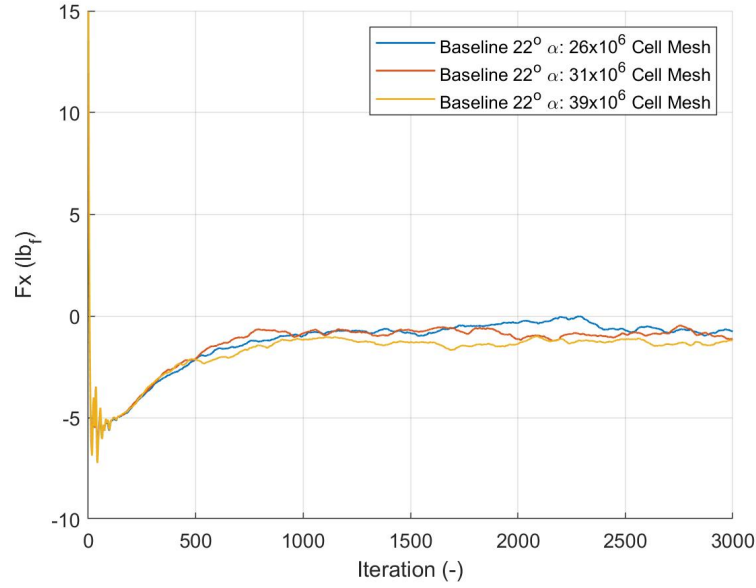


Figure 65. NACA 0012 Cropped Delta-Wing Baseline Axial Force ( $F_x$ ) Per Iteration CFD Mesh Study Results,  $\alpha = 22^\circ$ ,  $\text{Re} = 5 \times 10^5$

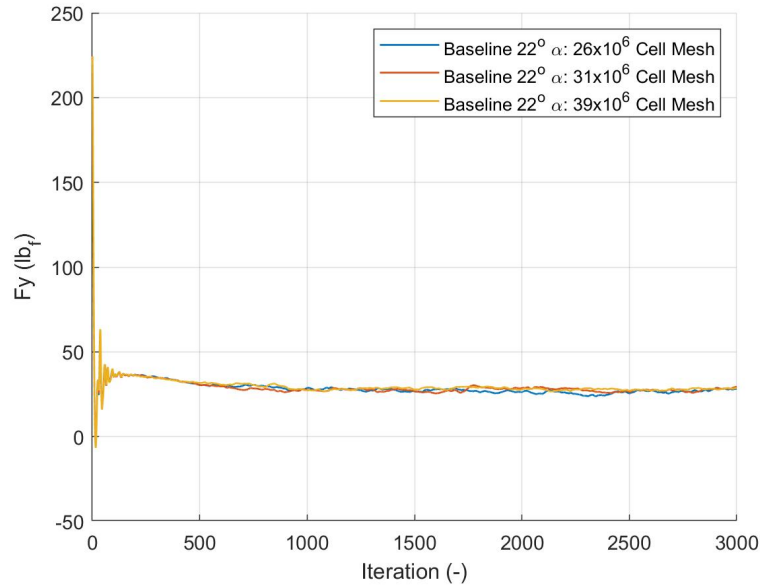


Figure 66. NACA 0012 Cropped Delta-Wing Baseline Normal Force ( $F_y$ ) Per Iteration CFD Mesh Study Results,  $\alpha = 22^\circ$ ,  $\text{Re} = 5 \times 10^5$

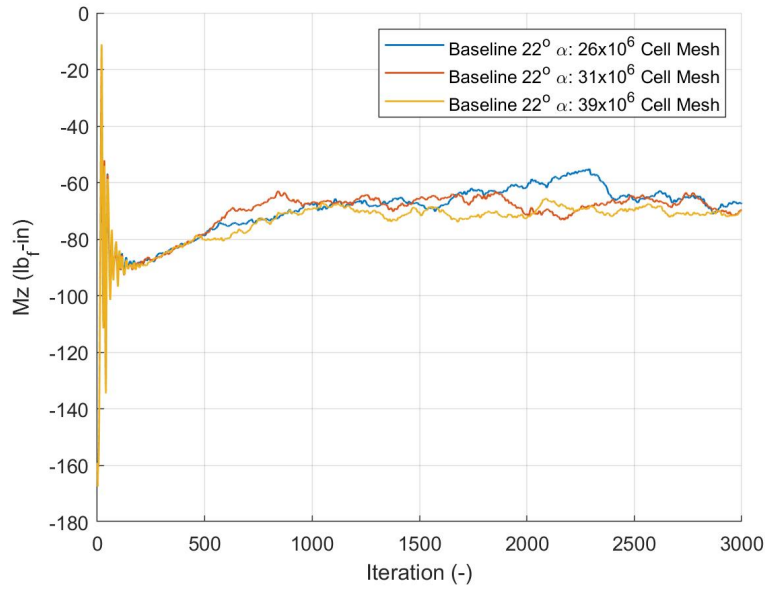


Figure 67. NACA 0012 Cropped Delta-Wing Baseline Moment About Z-Axis ( $M_z$ ) Per Iteration CFD Mesh Study Results,  $\alpha = 22^\circ$ ,  $\text{Re} = 5 \times 10^5$

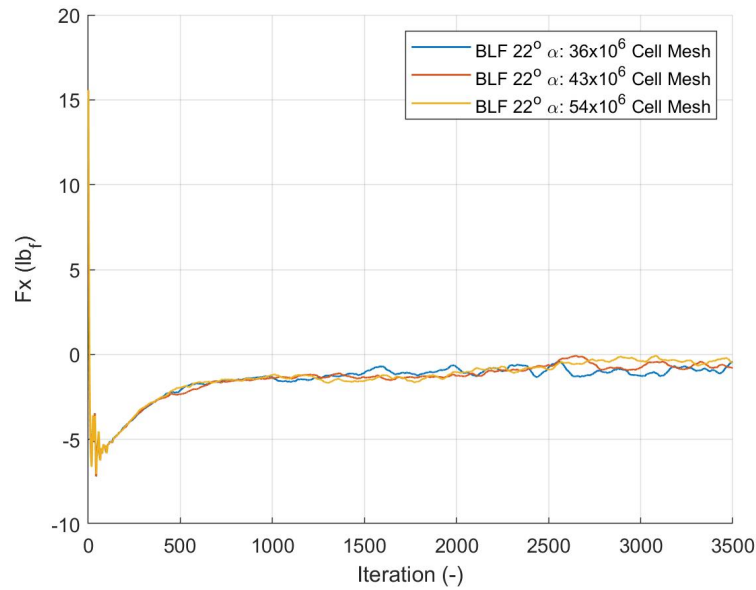


Figure 68. NACA 0012 Cropped Delta-Wing Passive BLF Axial Force ( $F_x$ ) Per Iteration CFD Mesh Study Results,  $\alpha = 22^\circ$ ,  $\text{Re} = 5 \times 10^5$

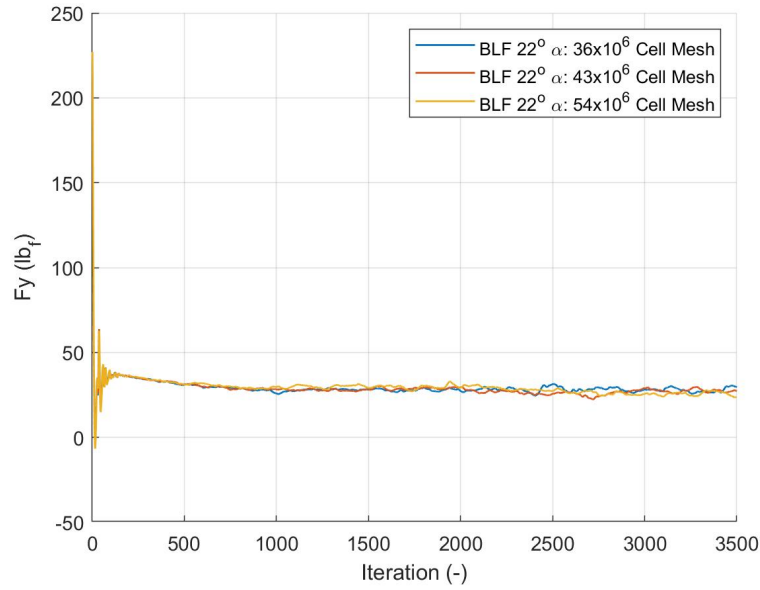


Figure 69. NACA 0012 Cropped Delta-Wing Passive BLF Normal Force ( $F_y$ ) Per Iteration CFD Mesh Study Results,  $\alpha = 22^\circ$ ,  $\text{Re} = 5 \times 10^5$

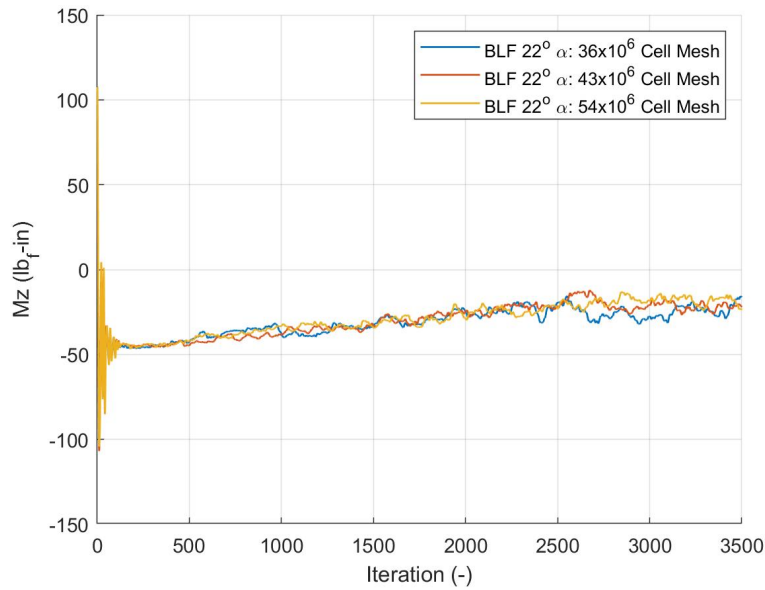


Figure 70. NACA 0012 Cropped Delta-Wing Passive BLF Moment About Z-Axis ( $M_z$ ) Per Iteration CFD Mesh Study Results,  $\alpha = 22^\circ$ ,  $\text{Re} = 5 \times 10^5$

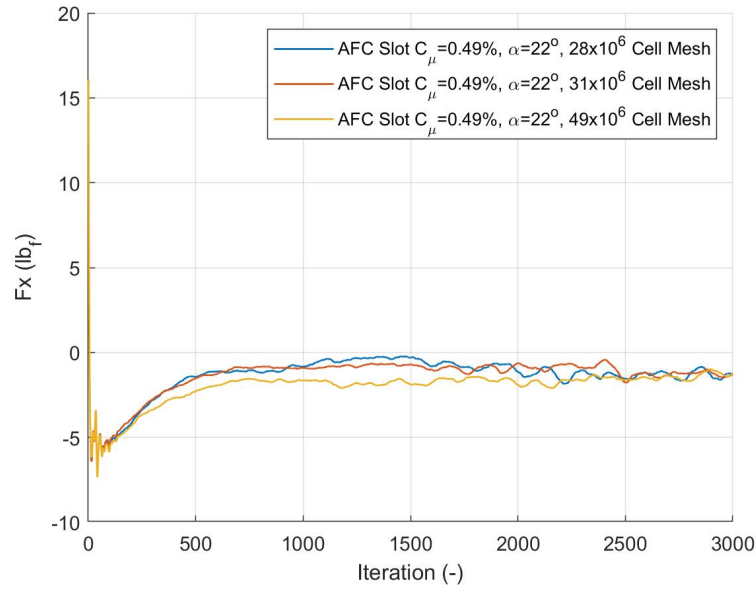


Figure 71. NACA 0012 Cropped Delta-Wing AFC Slot Axial Force ( $F_x$ ) Per Iteration CFD Mesh Study Results,  $\alpha = 22^\circ$ ,  $\text{Re} = 5 \times 10^5$ ,  $C_\mu = 0.49\%$

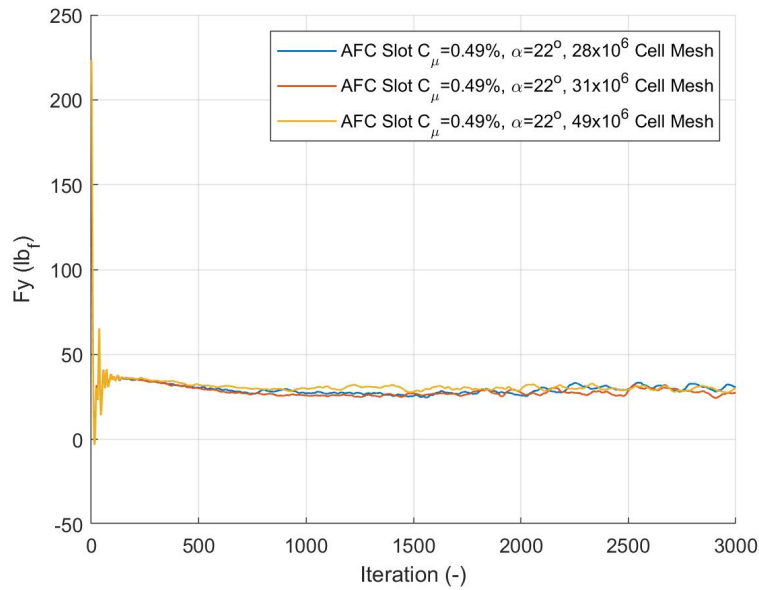


Figure 72. NACA 0012 Cropped Delta-Wing AFC Slot Normal Force ( $F_y$ ) Per Iteration CFD Mesh Study Results,  $\alpha = 22^\circ$ ,  $\text{Re} = 5 \times 10^5$ ,  $C_\mu = 0.49\%$

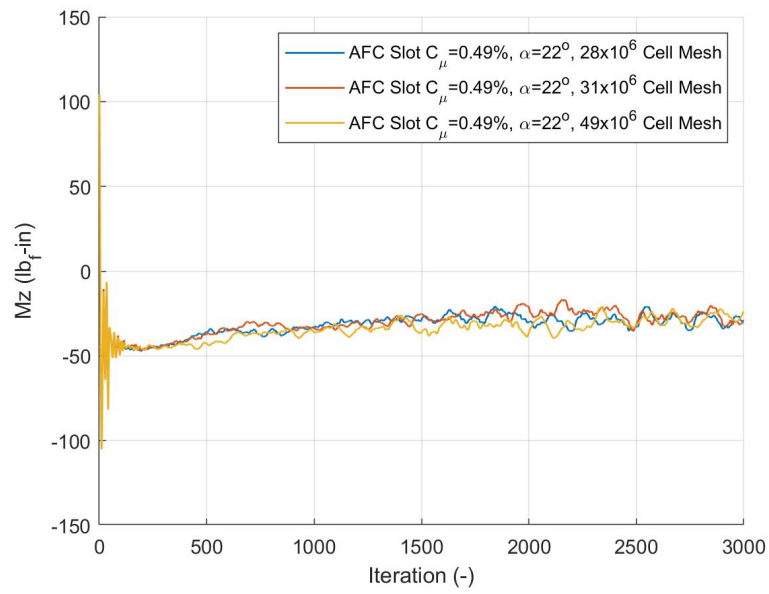


**Figure 73. NACA 0012 Cropped Delta-Wing AFC Slot Moment About Z-Axis ( $M_z$ ) Per Iteration CFD Mesh Study Results,  $\alpha = 22^\circ$ ,  $\text{Re} = 5 \times 10^5$ ,  $C_\mu = 0.49\%$**

## Appendix C. Flow Visualization Compilation

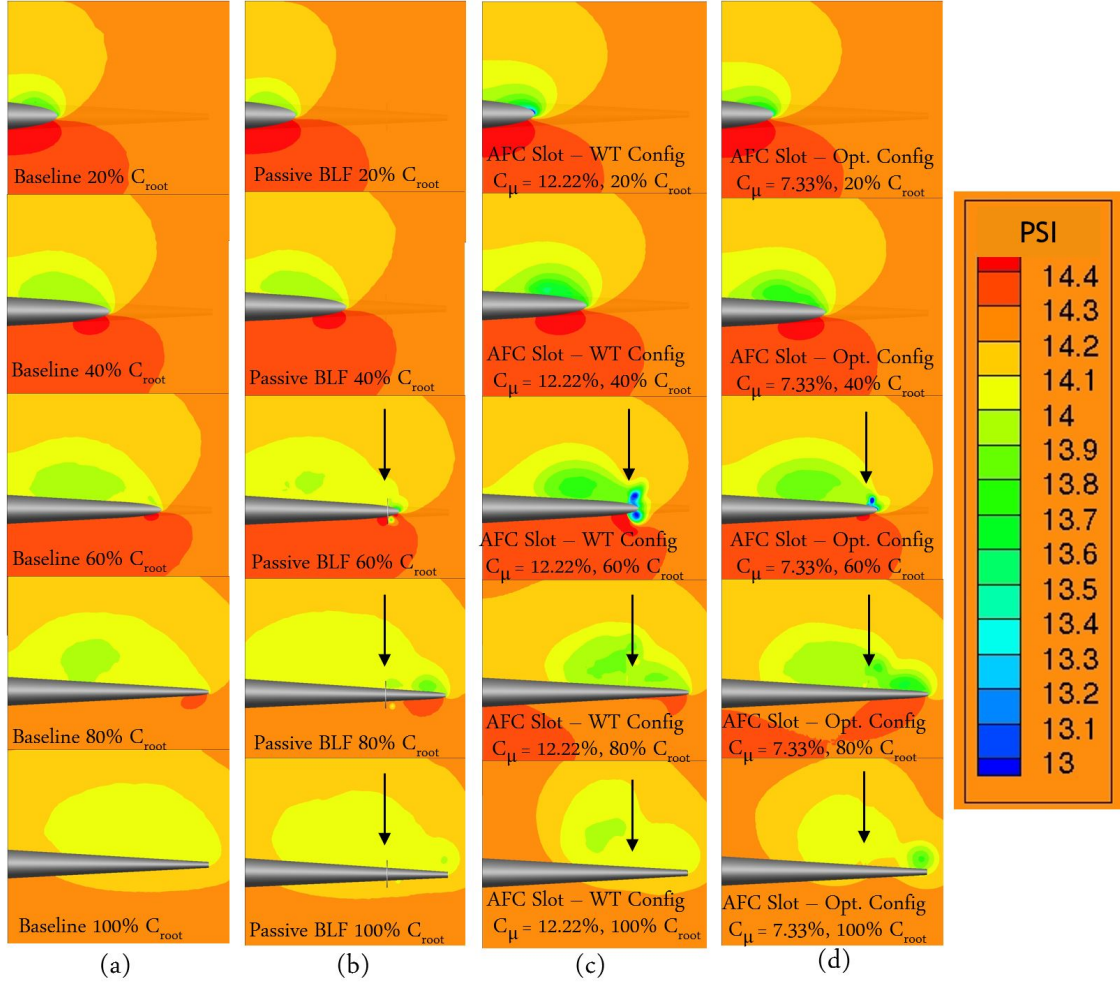


**Figure 74.** NACA 0012 Cropped Delta-Wing Y-Z Plane Pressure (PSI) Slice Contour Plot,  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ : (a) Baseline Configuration, (b) Passive BLF Configuration, (c) AFC Slot Wind Tunnel (WT) Configuration,  $C_{\mu} = 12.22\%$ , (d) AFC Slot Optimized Configuration,  $C_{\mu} = 7.33\%$

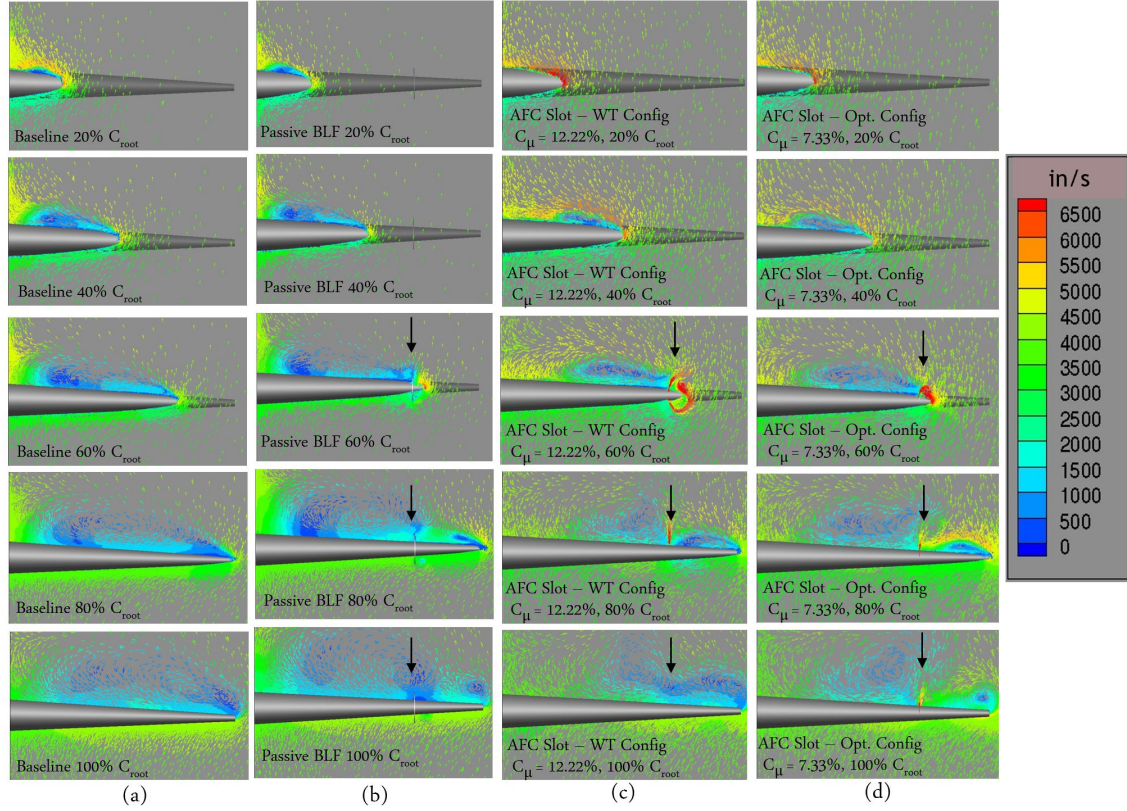


Figure 75. NACA 0012 Cropped Delta-Wing Y-Z Plane Vector Slice Colored by Velocity Magnitude (in/s),  $\alpha = 24^\circ$ ,  $Re = 5 \times 10^5$ : (a) Baseline Configuration, (b) Passive BLF Configuration, (c) AFC Slot Wind Tunnel (WT) Configuration,  $C_\mu = 12.22\%$ , (d) AFC Slot Optimized Configuration,  $C_\mu = 7.33\%$

## Appendix D. MATLAB Script: Baseline Comparison

```
1 %% Basic Configuration Data Comparison
2 clear all; close all; clc; format compact; format short;
3 %% Basic COnfiguration Wind Tunnel Data (1.5 degree correction
   applied to all comparison cases)
4 Alpha_Baseline2=1.5+...
5 [-8.17894442052277;-7.16850773849801;-6.15464379090849;...
6 -5.04877209800816;-4.02932120636633;-3.00640352702020;...
7 -1.98382443346184;-0.870213403716582;0.153319187693818;...
8 1.17508365277160;2.19900159794485;3.30928370940170;...
9 4.32751503348324;5.34186930698045;6.44211101586254;...
10 7.45523765217682;8.46819102061274;9.56920569459411;...
11 10.6678210098701;11.6756459136262;12.7671846976348;...
12 13.7663130389622;14.8512817871214;15.9311893169993;...
13 17.0110707277628;18.0844673115262;19.1538944819053;...
14 20.2221014158863;21.3721215112022;22.4257937648188;...
15 23.5698166553147;24.6991922407033;25.7472428560031;...
16 26.8830239002552;28.0967117595190;29.2310840568254;...
17 30.4510280084815;31.6729762552610;32.9017417048610;...
18 34.2275325071614;35.4596797612262;36.7847709966838];...
19 CD_Base2=...
20 [0.0326396226315288;0.0273554591561591;0.02320762912...
21 52264;0.0184655617641355;0.0156734227994947;0.013931...
22 8232188933;0.0127460003513771;0.0110429698239139;0.0...
23 115328779992575;0.0132684007837646;0.01594624739861...
24 14;0.0186260816468254;0.0227511043823911;0.027425377...
25 8944443;0.0325465190807324;0.0391042044857320;0.0473...
26 291339011119;0.0578153893612589;0.0714274594986400;0...
27 .0882968225391222;0.107396801468250;0.12837527862316...
28 1;0.152008514898266;0.177050724527485;0.203713593209...
29 787;0.230608840670329;0.257527050009981;0.2850390953...
30 55441;0.311662701851170;0.335885212499362;0.35962757...
31 0078000;0.378102215918811;0.393975988177553;0.4094634...
32 43267234;0.422979456980625;0.438129375146260;0.452553...
33 360061481;0.469150907399056;0.488570671603892;0.51410...
34 4483039872;0.536274210618872;0.565069415967284];
35 CL_Base2=...
36 [-0.380686716946657,-0.335679522978898,-0.28809803698...
37 6591,-0.235205472140068,-0.180638051940071,-0.1234544...
38 23606297,-0.0655693172981972,-0.00446862170388157,0.0...
39 533671656873325,0.110388299123664,0.169693355141534,...
40 0.227263490287654,0.279476897333351,0.32863898256204...
41 2,0.375560539057904,0.422360052709387,0.4700363760260...
42 67,0.517777718341523,0.561913793013043,0.604151005786...
43 968,0.641842476206843,0.673795777863523,0.70451924645...
44 7192,0.729874924214394,0.754142327869694,0.7725926727...
45 70825,0.786833165496932,0.798718935717348,0.805103685...
46 529550,0.802634940849533,0.801598645011175,0.78608838...
47 7524569,0.776596912840933,0.767880111293073,0.7484587...
48 51498765,0.737187298271561,0.724400980387816,0.713740...
49 363550526,0.709249314247855,0.715390882106700,0.71448...
50 6482896382,0.719886109135885]';
51 CM_Base2=...
52 [-0.00241933648422381;-0.000994749356042714;0.00052513...
53 8889181397;0.000531995120895268;-0.000127610521605613;...
54 -0.00112181497128817;-0.00238738588975404;-0.004014823...
```

```

55 77348298;-0.00458591893002119;-0.00447507033838957;-0.0...
56 0570421624022764;-0.00639759228464273;-0.006060593543...
57 11681;-0.00452373994614179;-0.00254238263866779;-0.000...
58 802608455539601;0.000686585846786974;0.0019224715481...
59 3012;0.00305034068341110;0.00384085470805589;0.0046514...
60 9185638424;0.00533251814807207;0.00492217834961218;0.0...
61 0390892393185356;0.00131507381415635;-0.0018753227054...
62 2222;-0.00563731602852632;-0.0109907490359497;-0.016914...
63 9235037892;-0.0248236615415000;-0.0317363120696212;-0.0...
64 393746528162185;-0.0435606742506112;-0.043896906122957...
65 7;-0.0457089065451211;-0.0471099572765705;-0.04925656335...
66 62850;-0.0525805261396649;-0.0556579516727002;-0.0595181...
67 996791140;-0.0641550435894548;-0.0701361258272115];
68
69
70 %% Import Kestrel Data
71 [AoA_0] = importdata('0AoA_forces.dat',' ',23);
72 [AoA_10] = importdata('10AoA_forces.dat',' ',23);
73 [AoA_14] = importdata('14AoA_forces.dat',' ',23);
74 [AoA_16] = importdata('16AoA_forces.dat',' ',23);
75 [AoA_18] = importdata('18AoA_forces.dat',' ',23);
76 [AoA_20] = importdata('20AoA_forces.dat',' ',23);
77 [AoA_22] = importdata('22AoA_39Mil_TS-0.00005_AD-0.01_forces.
    dat',' ',23); % Run1: TS=0.00005_AD=0.01
78 [AoA_24] = importdata('24AoA_forces.dat',' ',23);
79 [AoA_26] = importdata('26AoA_forces.dat',' ',23);
80 [AoA_28] = importdata('28AoA_forces.dat',' ',23);
81 [AoA_30] = importdata('30AoA_forces.dat',' ',23);
82
83 [AoA_22_26Mil] = importdata('22AoA_26Mil_forces.dat',' ',23);
84 [AoA_22_31Mil] = importdata('22AoA_31Mil_forces.dat',' ',23);
85 [AoA_22_Run2] = importdata('22AoA_TS-0.00002_AD-0.1_forces.dat
    ',' ',23); % Run2: TS=0.00002_AD=0.1
86 [AoA_22_Run3] = importdata('22AoA_TS-0.00005_AD-0.1_forces.dat
    ',' ',23); % Run3: TS=0.00005_AD=0.1
87 [AoA_22_Run4] = importdata('22AoA_TS-0.0005_AD-0.01_forces.dat
    ',' ',23); % Run4: TS=0.0005_AD=0.01
88
89 %% Axial Forces
90 Iter = 1000; %Number of iterations to average over
91
92 fx_0AoA = mean(AoA_0.data(([length(AoA_0.data)-Iter:end]),3));
93 fx_10AoA = mean(AoA_10.data(([length(AoA_10.data)-Iter:end])
    ,3));
94 fx_14AoA = mean(AoA_14.data(([length(AoA_14.data)-Iter:end])
    ,3));
95 fx_16AoA = mean(AoA_16.data(([length(AoA_16.data)-Iter:end])
    ,3));
96 fx_18AoA = mean(AoA_18.data(([length(AoA_18.data)-Iter:end])
    ,3));
97 fx_20AoA = mean(AoA_20.data(([length(AoA_20.data)-Iter:end])
    ,3));
98 fx_22AoA = mean(AoA_22.data(([length(AoA_22.data)-Iter:end])
    ,3));
99 fx_24AoA = mean(AoA_24.data(([length(AoA_24.data)-Iter:end])
    ,3));
100 fx_26AoA = mean(AoA_26.data(([length(AoA_26.data)-Iter:end])
    ,3));

```

```

101 fx_28AoA = mean(AoA_28.data((length(AoA_28.data)-Iter:end),3));
102 fx_30AoA = mean(AoA_30.data((length(AoA_30.data)-Iter:end),3));
103
104 fx_22AoA_26Mil = mean(AoA_22_26Mil.data((length(AoA_22_26Mil.data)-Iter:end),3));
105 fx_22AoA_31Mil = mean(AoA_22_31Mil.data((length(AoA_22_31Mil.data)-Iter:end),3));
106
107 fx_22AoA_Run2 = mean(AoA_22_Run2.data((length(AoA_22_Run2.data)-Iter:end),3));
108 fx_22AoA_Run3 = mean(AoA_22_Run3.data((length(AoA_22_Run3.data)-Iter:end),3));
109 fx_22AoA_Run4 = mean(AoA_22_Run4.data((length(AoA_22_Run4.data)-Iter:end),3));
110
111 %% Vertical Forces
112 fy_0AoA = mean(AoA_0.data((length(AoA_0.data)-Iter:end),4));
113 fy_10AoA = mean(AoA_10.data((length(AoA_10.data)-Iter:end),4));
114 fy_14AoA = mean(AoA_14.data((length(AoA_14.data)-Iter:end),4));
115 fy_16AoA = mean(AoA_16.data((length(AoA_16.data)-Iter:end),4));
116 fy_18AoA = mean(AoA_18.data((length(AoA_18.data)-Iter:end),4));
117 fy_20AoA = mean(AoA_20.data((length(AoA_20.data)-Iter:end),4));
118 fy_22AoA = mean(AoA_22.data((length(AoA_22.data)-Iter:end),4));
119 fy_24AoA = mean(AoA_24.data((length(AoA_24.data)-Iter:end),4));
120 fy_26AoA = mean(AoA_26.data((length(AoA_26.data)-Iter:end),4));
121 fy_28AoA = mean(AoA_28.data((length(AoA_28.data)-Iter:end),4));
122 fy_30AoA = mean(AoA_30.data((length(AoA_30.data)-Iter:end),4));
123
124 fy_22AoA_26Mil = mean(AoA_22_26Mil.data((length(AoA_22_26Mil.data)-Iter:end),4));
125 fy_22AoA_31Mil = mean(AoA_22_31Mil.data((length(AoA_22_31Mil.data)-Iter:end),4));
126
127 fy_22AoA_Run2 = mean(AoA_22_Run2.data((length(AoA_22_Run2.data)-Iter:end),4));
128 fy_22AoA_Run3 = mean(AoA_22_Run3.data((length(AoA_22_Run3.data)-Iter:end),4));
129 fy_22AoA_Run4 = mean(AoA_22_Run4.data((length(AoA_22_Run4.data)-Iter:end),4));
130
131 %% Moment about the z-axis
132 L = -1.75; % Correction for incorrect location of Moment
           Reference point in CFD Settings
133 Mz_0 = mean(AoA_0.data((length(AoA_0.data)-Iter:end),8))/L;
134 Mz_10 = mean(AoA_10.data((length(AoA_10.data)-Iter:end),8))/L;

```

```

135 Mz_14 = mean(AoA_14.data((([length(AoA_14.data)-Iter:end])),8))/
      L;
136 Mz_16 = mean(AoA_16.data((([length(AoA_16.data)-Iter:end])),8))/
      L;
137 Mz_18 = mean(AoA_18.data((([length(AoA_18.data)-Iter:end])),8))/
      L;
138 Mz_20 = mean(AoA_20.data((([length(AoA_20.data)-Iter:end])),8))/
      L;
139 Mz_22 = mean(AoA_22.data((([length(AoA_22.data)-Iter:end])),8))/
      L;
140 Mz_24 = mean(AoA_24.data((([length(AoA_24.data)-Iter:end])),8))/
      L;
141 Mz_26 = mean(AoA_26.data((([length(AoA_26.data)-Iter:end])),8))/
      L;
142 Mz_28 = mean(AoA_28.data((([length(AoA_28.data)-Iter:end])),8))/
      L;
143 Mz_30 = mean(AoA_30.data((([length(AoA_30.data)-Iter:end])),8))/
      L;
144
145 Mz_22AoA_26Mil = mean(AoA_22_26Mil.data((([length(AoA_22_26Mil.
      data)-Iter:end])),8))/L;
146 Mz_22AoA_31Mil = mean(AoA_22_31Mil.data((([length(AoA_22_31Mil.
      data)-Iter:end])),8))/L;
147
148 Mz_22AoA_Run2 = mean(AoA_22_Run2.data((([length(AoA_22_Run2.
      data)-Iter:end])),8))/L;
149 Mz_22AoA_Run3 = mean(AoA_22_Run3.data((([length(AoA_22_Run3.
      data)-Iter:end])),8))/L;
150 Mz_22AoA_Run4 = mean(AoA_22_Run4.data((([length(AoA_22_Run4.
      data)-Iter:end])),8))/L;
151
152 %% Lift
153 AoA = [0 10 14 16 18 20 22 24 26 28 30];
154 L_0 = fy_0AoA*cosd(AoA(:,1))+fx_0AoA*sind(AoA(:,1));
155 L_10 = fy_10AoA*cosd(AoA(:,2))+fx_10AoA*sind(AoA(:,2));
156 L_14 = fy_14AoA*cosd(AoA(:,3))+fx_14AoA*sind(AoA(:,3));
157 L_16 = fy_16AoA*cosd(AoA(:,4))+fx_16AoA*sind(AoA(:,4));
158 L_18 = fy_18AoA*cosd(AoA(:,5))+fx_18AoA*sind(AoA(:,5));
159 L_20 = fy_20AoA*cosd(AoA(:,6))+fx_20AoA*sind(AoA(:,6));
160 L_22 = fy_22AoA*cosd(AoA(:,7))+fx_22AoA*sind(AoA(:,7));
161 L_24 = fy_24AoA*cosd(AoA(:,8))+fx_24AoA*sind(AoA(:,8));
162 L_26 = fy_26AoA*cosd(AoA(:,9))+fx_26AoA*sind(AoA(:,9));
163 L_28 = fy_28AoA*cosd(AoA(:,10))+fx_28AoA*sind(AoA(:,10));
164 L_30 = fy_30AoA*cosd(AoA(:,11))+fx_30AoA*sind(AoA(:,11));
165
166 %% Drag
167
168 D_0 = fx_0AoA*cosd(AoA(:,1))+fy_0AoA*sind(AoA(:,1));
169 D_10 = fx_10AoA*cosd(AoA(:,2))+fy_10AoA*sind(AoA(:,2));
170 D_14 = fx_14AoA*cosd(AoA(:,3))+fy_14AoA*sind(AoA(:,3));
171 D_16 = fx_16AoA*cosd(AoA(:,4))+fy_16AoA*sind(AoA(:,4));
172 D_18 = fx_18AoA*cosd(AoA(:,5))+fy_18AoA*sind(AoA(:,5));
173 D_20 = fx_20AoA*cosd(AoA(:,6))+fy_20AoA*sind(AoA(:,6));
174 D_22 = fx_22AoA*cosd(AoA(:,7))+fy_22AoA*sind(AoA(:,7));
175 D_24 = fx_24AoA*cosd(AoA(:,8))+fy_24AoA*sind(AoA(:,8));
176 D_26 = fx_26AoA*cosd(AoA(:,9))+fy_26AoA*sind(AoA(:,9));
177 D_28 = fx_28AoA*cosd(AoA(:,10))+fy_28AoA*sind(AoA(:,10));
178 D_30 = fx_30AoA*cosd(AoA(:,11))+fy_30AoA*sind(AoA(:,11));

```

```

179
180 %% Pitching Moment
181 x_cm = 1.62; % in - Estimated distance from Aero Center
182 MomRef_L = 1;% in - NA
183
184 PM_0 = (Mz_0/MomRef_L)-(L_0*cosd(0)*x_cm)+(D_0*-sind(0)*x_cm)
185 ;
186 PM_10 = (Mz_10/MomRef_L)-(L_10*cosd(10)*x_cm)+(D_10*-sind(10)*
187 x_cm);
188 PM_14 = (Mz_14/MomRef_L)-(L_14*cosd(14)*x_cm)+(D_14*-sind(14)*
189 x_cm);
190 PM_16 = (Mz_16/MomRef_L)-(L_16*cosd(16)*x_cm)+(D_16*-sind(16)*
191 x_cm);
192 PM_18 = (Mz_18/MomRef_L)-(L_18*cosd(18)*x_cm)+(D_18*-sind(18)*
193 x_cm);
194 PM_20 = (Mz_20/MomRef_L)-(L_20*cosd(20)*x_cm)+(D_20*-sind(20)*
195 x_cm);
196 PM_22 = (Mz_22/MomRef_L)-(L_22*cosd(22)*x_cm)+(D_22*-sind(22)*
197 x_cm);
198 PM_24 = (Mz_24/MomRef_L)-(L_24*cosd(24)*x_cm)+(D_24*-sind(24)*
199 x_cm);
200 PM_26 = (Mz_26/MomRef_L)-(L_26*cosd(26)*x_cm)+(D_26*-sind(26)*
201 x_cm);
202 PM_28 = (Mz_28/MomRef_L)-(L_28*cosd(28)*x_cm)+(D_28*-sind(28)*
203 x_cm);
204 PM_30 = (Mz_30/MomRef_L)-(L_30*cosd(30)*x_cm)+(D_30*-sind(30)*
205 x_cm);
206
207 %% Coeffiecient of Lift
208 CL_0 =(L_0*2)/(0.67764*0.0009518*((3751.5/12)^2));
209 CL_10 =(L_10*2)/(0.67764*0.0009518*((3751.5/12)^2));
210 CL_14 =(L_14*2)/(0.67764*0.0009518*((3751.5/12)^2));
211 CL_16 =(L_16*2)/(0.67764*0.0009518*((3751.5/12)^2));
212 CL_18 =(L_18*2)/(0.67764*0.0009518*((3751.5/12)^2));
213 CL_20 =(L_20*2)/(0.67764*0.0009518*((3751.5/12)^2));
214 CL_22 =(L_22*2)/(0.67764*0.0009518*((3751.5/12)^2));
215 CL_24 =(L_24*2)/(0.67764*0.0009518*((3751.5/12)^2));
216 CL_26 =(L_26*2)/(0.67764*0.0009518*((3751.5/12)^2));
217 CL_28 =(L_28*2)/(0.67764*0.0009518*((3751.5/12)^2));
218 CL_30 =(L_30*2)/(0.67764*0.0009518*((3751.5/12)^2));
219
220 CLlist = [CL_0 CL_10 CL_14 CL_16 CL_18 CL_20 CL_22 CL_24 CL_26
221 CL_28 CL_30];
222
223 %% Coeffiecient of Drag
224 CD_0 =(D_0*2)/(0.67764*0.0009518*((3751.5/12)^2));
225 CD_10 =(D_10*2)/(0.67764*0.0009518*((3751.5/12)^2));
226 CD_14 =(D_14*2)/(0.67764*0.0009518*((3751.5/12)^2));
227 CD_16 =(D_16*2)/(0.67764*0.0009518*((3751.5/12)^2));
228 CD_18 =(D_18*2)/(0.67764*0.0009518*((3751.5/12)^2));
229 CD_20 =(D_20*2)/(0.67764*0.0009518*((3751.5/12)^2));
230 CD_22 =(D_22*2)/(0.67764*0.0009518*((3751.5/12)^2));
231 CD_24 =(D_24*2)/(0.67764*0.0009518*((3751.5/12)^2));
232 CD_26 =(D_26*2)/(0.67764*0.0009518*((3751.5/12)^2));
233 CD_28 =(D_28*2)/(0.67764*0.0009518*((3751.5/12)^2));
234 CD_30 =(D_30*2)/(0.67764*0.0009518*((3751.5/12)^2));
235
236 CDlist = [CD_0 CD_10 CD_14 CD_16 CD_18 CD_20 CD_22 CD_24 CD_26

```

```

225         CD_28 CD_30];
226 %% Moment Coeffiecient
227 c_bar = 9.66; % in - Mean Aerodynamic Chord for CFD Model
228 CM_0 =(PM_0*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
229 CM_10 =(PM_10*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
230 CM_14 =(PM_14*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
231 CM_16 =(PM_16*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
232 CM_18 =(PM_18*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
233 CM_20 =(PM_20*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
234 CM_22 =(PM_22*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
235 CM_24 =(PM_24*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
236 CM_26 =(PM_26*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
237 CM_28 =(PM_28*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
238 CM_30 =(PM_30*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
239
240 CMlist = [CM_0 CM_10 CM_14 CM_16 CM_18 CM_20 CM_22 CM_24 CM_26
            CM_28 CM_30];
241
242 %% Plot for Baseline Comparison
243 % figure(1)
244 % hold on
245 % plot(Alpha_Baseline2,CD_Base2, 'k', 'LineWidth',0.9)
246 % plot(AoA,CDlist,'m--o', 'LineWidth',0.9)
247 % grid on
248 % xlabel('\alpha (deg)')
249 % ylabel('C_D (-)')
250 % xlim([0 30])
251 % ylim([0 0.5])
252 % %title('Coefficient of Drag at RE~5e^5')
253 % legend('Baseline Wind Tunnel Model, Re~5x10^5','Baseline CFD
            Model, Re~5x10^5','Location','northeast')
254 % hold off
255
256 % figure(2)
257 % hold on
258 % plot(Alpha_Baseline2,CL_Base2, 'k', 'LineWidth',0.9)
259 % plot(AoA,CLlist,'b--o', 'LineWidth',0.9)
260 % grid on
261 % xlabel('\alpha (deg)')
262 % ylabel('C_L (-)')
263 % xlim([0 30])
264 % ylim([0 1.1])
265 % %title('Coefficient of Drag at RE~5e^5')
266 % legend('Baseline Wind Tunnel Model, Re~5x10^5','Baseline CFD
            Model, Re~5x10^5','Location','northeast')
267 % hold off
268 %
269 % figure(3)
270 % hold on
271 % plot(Alpha_Baseline2,CM_Base2, 'k', 'LineWidth',0.9)
272 % plot(AoA,CMlist,'r--o', 'LineWidth',0.9)
273 % grid on
274 % xlabel('\alpha (deg)')
275 % ylabel('C_M (-)')
276 % xlim([0 30])
277 % ylim([-0.05 0.025])
278 % %title('Pitch Moment Coefficient at RE~5e^5')

```

```

279 % legend('Baseline Wind Tunnel Model, Re~5x10^5','Baseline CFD
      Model, Re~5x10^5','Location','northeast')
280 % hold off
281
282 %% Grid Study Plots
283
284 figure (4) % Iterations vs fx
285 hold on
286 plot (AoA_22_26Mil.data(:,1),AoA_22_26Mil.data(:,3), '
      LineWidth',.9)
287 plot (AoA_22_31Mil.data(:,1),AoA_22_31Mil.data(:,3), '
      LineWidth',.9)
288 plot (AoA_22.data(:,1),AoA_22.data(:,3), 'LineWidth',.9)
289 grid on
290 legend('Baseline 22^o \alpha: 26x10^6 Cell Mesh','Baseline 22^
      o \alpha: 31x10^6 Cell Mesh','Baseline 22^o \alpha: 39x10^6
      Cell Mesh')
291 xlabel('Iteration (-)')
292 ylabel('Fx (lb_f)')
293 hold off
294
295 % figure (5) % Iterations vs fy
296 % hold on
297 % plot (AoA_22_26Mil.data(:,1),AoA_22_26Mil.data(:,4), '
      LineWidth',.9)
298 % plot (AoA_22_31Mil.data(:,1),AoA_22_31Mil.data(:,4), '
      LineWidth',.9)
299 % plot (AoA_22.data(:,1),AoA_22.data(:,4), 'LineWidth',.9)
300 % grid on
301 % legend('Baseline 22^o \alpha: 26x10^6 Cell Mesh','Baseline
      22^o \alpha: 31x10^6 Cell Mesh','Baseline 22^o \alpha: 39
      x10^6 Cell Mesh')
302 % xlabel('Iteration (-)')
303 % ylabel('Fy (lb_f)')
304 % hold off
305 %
306 % figure (7) % Iterations vs Mz
307 % hold on
308 % plot (AoA_22_26Mil.data(:,1),AoA_22_26Mil.data(:,8), '
      LineWidth',.9)
309 % plot (AoA_22_31Mil.data(:,1),AoA_22_31Mil.data(:,8), '
      LineWidth',.9)
310 % plot (AoA_22.data(:,1),AoA_22.data(:,8), 'LineWidth',.9)
311 % grid on
312 % legend('Baseline 22^o \alpha: 26x10^6 Cell Mesh','Baseline
      22^o \alpha: 31x10^6 Cell Mesh','Baseline 22^o \alpha: 39
      x10^6 Cell Mesh')
313 % xlabel('Iteration (-)')
314 % ylabel('Mz (lb_f-in)')
315 % hold off
316
317 %% Settings Plots
318 % figure (8) % Iterations vs fx, TS = Time Step, AD = Temporal
      Advective Damping
319 % hold on
320 % plot (AoA_22.data(:,1),AoA_22.data(:,3), 'LineWidth',.9)
321 % plot (AoA_22_Run2.data(:,1),AoA_22_Run2.data(:,3), 'LineWidth
      ',.9)

```

```

322 % plot (AoA_22_Run3.data(:,1),AoA_22_Run3.data(:,3),'LineWidth
    ',.9)
323 % plot (AoA_22_Run4.data(:,1),AoA_22_Run4.data(:,3),'LineWidth
    ',.9)
324 % xlim([0 2700])
325 % grid on
326 % legend('22^o \alpha Run1: TS=0.00005 AD=0.01','22^o \alpha
    Run2: TS=0.00002 AD=0.1','22^o \alpha Run3: TS=0.00005 AD
    =0.1','22^o \alpha Run4: TS=0.0005 AD=0.01')
327 % xlabel('Iteration (-)')
328 % ylabel('Fx (lb_f)')
329 % hold off
330 %
331 % figure (9) % Iterations vs fy
332 % hold on
333 % plot (AoA_22.data(:,1),AoA_22.data(:,4),'LineWidth',.9)
334 % plot (AoA_22_Run2.data(:,1),AoA_22_Run2.data(:,4),'LineWidth
    ',.9)
335 % plot (AoA_22_Run3.data(:,1),AoA_22_Run3.data(:,4),'LineWidth
    ',.9)
336 % plot (AoA_22_Run4.data(:,1),AoA_22_Run4.data(:,4),'LineWidth
    ',.9)
337 % xlim([0 2700])
338 % grid on
339 % legend('22^o \alpha Run1: TS=0.00005 AD=0.01','22^o \alpha
    Run2: TS=0.00002 AD=0.1','22^o \alpha Run3: TS=0.00005 AD
    =0.1','22^o \alpha Run4: TS=0.0005 AD=0.01')
340 % xlabel('Iteration (-)')
341 % ylabel('Fy (lb_f)')
342 % hold off
343 %
344 % figure (10) % Iterations vs Mz
345 % hold on
346 % plot (AoA_22.data(:,1),AoA_22.data(:,8),'LineWidth',.9)
347 % plot (AoA_22_Run2.data(:,1),AoA_22_Run2.data(:,8),'LineWidth
    ',.9)
348 % plot (AoA_22_Run3.data(:,1),AoA_22_Run3.data(:,8),'LineWidth
    ',.9)
349 % plot (AoA_22_Run4.data(:,1),AoA_22_Run4.data(:,8),'LineWidth
    ',.9)
350 % xlim([0 2700])
351 % grid on
352 % legend('22^o \alpha Run1: TS=0.00005 AD=0.01','22^o \alpha
    Run2: TS=0.00002 AD=0.1','22^o \alpha Run3: TS=0.00005 AD
    =0.1','22^o \alpha Run4: TS=0.0005 AD=0.01')
353 % xlabel('Iteration (-)')
354 % ylabel('Mz (lb_f-in)')
355 % hold off

```

## Appendix E. MATLAB Script: Passive BLF Comparison

```
1 %% Passive BLF Configuration Data Comparison
2 clear all; close all; clc; format compact; format short;
3 %% Passive BLF Wind Tunnel Data (1.5 degree correction applied
  to all comparison cases)
4 Alpha_BLF_1=1.5+...
5 [-8.06594564259070;-7.14241231732519;-6.03905594741620;...
6 -5.01406378048430;-3.98721923601549;-2.87195351727540;...
7 -1.85058803650554;-0.831110322743736;0.275151806711067;...
8 1.29346471552093;2.31597900276951;3.42813304789199;...
9 4.45108375100950;5.55684707512697;6.57167414343638;...
10 7.58705903612775;8.69009006482263;9.70504580065541;...
11 10.7161174843277;11.2642436005670;11.8166774071110;...
12 12.2766843085277;12.8266085308312;13.3790159996166;...
13 13.8375751427264;14.3856475805125;14.9354617926899;...
14 15.3929723623862;15.9414105042531;16.4688861494385;...
15 16.9094889255359;17.4240418013865;17.9837233404080;...
16 18.4646453036484;18.9881016785306;19.5209239626320;...
17 20.0480920643511;20.4921008071506;21.0161537952655;...
18 21.5513155912465;21.9819661259102;22.4844514540255;...
19 23.0266031504895;23.4649469590941;23.9788010755111;...
20 24.4993216153161;24.9404098936923;25.4654301290090;...
21 25.9851110721517;26.4294113964856;26.9572368515206;...
22 27.4879036272060;27.9159749086103;28.4552397489093;...
23 28.9719941570135;29.4032901602970;29.9353877441201;...
24 30.4579590792370;30.8794429116547;31.4044874140582;...
25 31.9278672633083;32.3622515736385;32.8915967016012];
26 CD_BLF_1=...
27 [0.0331859562592513;0.0285589439023825;0.0225065331772370;...
28 0.0189468223940387;0.0158403087605802;0.0131311169034887;...
29 0.0122527914619488;0.0124686038531358;0.0121007596222725;...
30 0.01399411574444537;0.0168024120917713;0.0202655564151916;...
31 0.0245968486909978;0.0291105237603469;0.0348275369759939;...
32 0.0415565640185381;0.0491966039352059;0.0596374268695133;...
33 0.0712235463740903;0.0783859677428014;0.0880240892437888;...
34 0.0983355252004903;0.108101954523449;0.118749897647422;...
35 0.128576970063239;0.140223144052195;0.152845063683076;...
36 0.165098099722719;0.178263738604623;0.190669762413875;...
37 0.200917116172463;0.213283639422009;0.230302422336980;...
38 0.251856410673102;0.265348318598858;0.280169649171469;...
39 0.293079995746426;0.306468524342820;0.316087744265308;...
40 0.331153701240424;0.339352993468659;0.343805149187245;...
41 0.357367274638073;0.365487071651346;0.371746744842184;...
42 0.378965080879246;0.387348160309275;0.396148794017582;...
43 0.400919634435716;0.410355844881111;0.418992542285874;...
44 0.429377784632715;0.432161428908286;0.445358004857721;...
45 0.449511061662298;0.454432235165533;0.466615637205070;...
46 0.473488130419345;0.473825618553497;0.483262801297828;...
47 0.490134615871489;0.495193519187196;0.506592291154017];
48 CL_BLF_1=...
49 [-0.354173691100548,-0.309063999932849,-0.259899691306692,...
50 -0.201576490582196,-0.140228135605584,-0.0784330946201286,...
51 -0.0228956859968763,0.0306396081385506,0.0818251136500848,...
52 0.134125047245865,0.190880848861979,0.249375733204867,...
53 0.306594385654906,0.357250871754507,0.405853817460111,...
54 0.455048376575644,0.503867637134175,0.552607044125295,...
```

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55 0.596166557862589,0.617511770875898,0.642365030513726,...
56 0.663583807519691,0.685775470178208,0.710600796703577,...
57 0.730284120516020,0.750511830740319,0.773647392520254,...
58 0.791158054932682,0.811773620986288,0.811217504491707,...
59 0.810796219594365,0.796534564440700,0.829074572567749,...
60 0.871414723998235,0.866595878432624,0.870649689280734,...
61 0.869767400527153,0.872958391535774,0.867711724905650,...
62 0.875307331477488,0.864330969244883,0.837270800264997,...
63 0.851219132828200,0.848402048276708,0.833399307819857,...
64 0.824406222320952,0.825560420849990,0.821339590367901,...
65 0.811456051420846,0.816016858774003,0.814771168240697,...
66 0.817599478203143,0.803887629919240,0.814774241132624,...
67 0.802847471376179,0.792555675655018,0.796901461921134,...
68 0.790083394307436,0.769385076296350,0.766250555705866,...
69 0.760289976252899,0.754334128100513,0.754700161457019]';
70 CM_BLF_1=...
71 [-0.00645565729432271;-0.00543366737074639;-0.00497230375830425;...
72 -0.00626840903527524;-0.00812639164827980;-0.00967798053293440;...
73 -0.00945309222782101;-0.00865038220961338;-0.00670502210461011;...
74 -0.00488751112138329;-0.00454480696604581;-0.00481732423437155;...
75 -0.00548800757156123;-0.00442664971617944;-0.00282825806744191;...
76 -0.00138620542503159;-0.000204421890390911;...
77 0.000817753587349030;0.00130240859034837;0.00109615288671430;
78 0.000464851194557061;-0.00149193626706634;-0.00380972808029311;...
79 -0.00533306500332433;-0.00620595983241655;-0.00759321564382312;...
80 -0.00870105692850148;-0.0108249745414312;-0.0129892457825265;...
81 -0.00516853422314401;-0.000189350755310846;-0.00462159855872107;...
82 -0.0191437591914945;-0.0261932152732147;-0.0251904959472022;...
83 -0.0378876638882588;-0.0478485428343769;-0.0499899927653833;...
84 -0.0545965073248441;-0.0540169594750646;-0.0642403701311685;...
85 -0.0678397210048976;-0.0669126861227226;-0.0711347448349583;...
86 -0.0673556117123620;-0.0649522888342130;-0.0668780318358190;...
87 -0.0603695865129550;-0.0637109281367164;-0.0621148519578112;...
88 -0.0619758111857658;-0.0662567712765227;-0.0668173655521368;...
89 -0.0655033106457927;-0.0660623006320958;-0.0655506777401585;...
90 -0.0645042350127906;-0.0634239194747829;-0.0619745103601840;...
91 -0.0628071667857057;-0.0612590184216668;-0.0608586271989955;...
92 -0.0620809601781004]+0.01;
93

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94
95 %% Import Kestrel Data
96 [AoA_0] = importdata('0AoA_forces.dat',' ',23);
97 [AoA_10] = importdata('10AoA_forces.dat',' ',23);
98 [AoA_14] = importdata('14AoA_forces.dat',' ',23);
99 [AoA_16] = importdata('16AoA_forces.dat',' ',23);
100 [AoA_18] = importdata('18AoA_forces.dat',' ',23);
101 [AoA_20] = importdata('20AoA_forces.dat',' ',23);
102 [AoA_22] = importdata('22AoA_36Mil_forces.dat',' ',23);
103 [AoA_24] = importdata('24AoA_forces.dat',' ',23);
104 [AoA_26] = importdata('26AoA_forces.dat',' ',23);
105 [AoA_28] = importdata('28AoA_forces.dat',' ',23);
106 [AoA_30] = importdata('30AoA_forces.dat',' ',23);
107
108 [AoA_22_36Mil] = importdata('22AoA_36Mil_forces.dat',' ',23);
109 [AoA_22_43Mil] = importdata('22AoA_43Mil_forces.dat',' ',23);
110 [AoA_22_54Mil] = importdata('22AoA_54Mil_forces.dat',' ',23);
111
112 %% Axial Forces
113 Iter = 1000; %Number of iterations to average overe
114
115 fx_0AoA = mean(AoA_0.data(([length(AoA_0.data)-Iter:end]),3));
116 fx_10AoA = mean(AoA_10.data(([length(AoA_10.data)-Iter:end])
    ,3));
117 fx_14AoA = mean(AoA_14.data(([length(AoA_14.data)-Iter:end])
    ,3));
118 fx_16AoA = mean(AoA_16.data(([length(AoA_16.data)-Iter:end])
    ,3));
119 fx_18AoA = mean(AoA_18.data(([length(AoA_18.data)-Iter:end])
    ,3));
120 fx_20AoA = mean(AoA_20.data(([length(AoA_20.data)-Iter:end])
    ,3));
121 fx_22AoA = mean(AoA_22.data(([length(AoA_22.data)-Iter:end])
    ,3));
122 fx_24AoA = mean(AoA_24.data(([length(AoA_24.data)-Iter:end])
    ,3));
123 fx_26AoA = mean(AoA_26.data(([length(AoA_26.data)-Iter:end])
    ,3));
124 fx_28AoA = mean(AoA_28.data(([length(AoA_28.data)-Iter:end])
    ,3));
125 fx_30AoA = mean(AoA_30.data(([length(AoA_30.data)-Iter:end])
    ,3));
126
127 fx_22AoA_36Mil = mean(AoA_22_36Mil.data(([length(AoA_22_36Mil.
    data)-Iter:end]),3));
128 fx_22AoA_43Mil = mean(AoA_22_43Mil.data(([length(AoA_22_43Mil.
    data)-Iter:end]),3));
129 fx_22AoA_54Mil = mean(AoA_22_54Mil.data(([length(AoA_22_54Mil.
    data)-Iter:end]),3));
130 %% Vertical Forces
131 fy_0AoA = mean(AoA_0.data(([length(AoA_0.data)-Iter:end]),4));
132 fy_10AoA = mean(AoA_10.data(([length(AoA_10.data)-Iter:end])
    ,4));
133 fy_14AoA = mean(AoA_14.data(([length(AoA_14.data)-Iter:end])
    ,4));
134 fy_16AoA = mean(AoA_16.data(([length(AoA_16.data)-Iter:end])
    ,4));
135 fy_18AoA = mean(AoA_18.data(([length(AoA_18.data)-Iter:end])

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    ,4));
136 fy_20AoA = mean(AoA_20.data((length(AoA_20.data)-Iter:end)
    ,4));
137 fy_22AoA = mean(AoA_22.data((length(AoA_22.data)-Iter:end)
    ,4));
138 fy_24AoA = mean(AoA_24.data((length(AoA_24.data)-Iter:end)
    ,4));
139 fy_26AoA = mean(AoA_26.data((length(AoA_26.data)-Iter:end)
    ,4));
140 fy_28AoA = mean(AoA_28.data((length(AoA_28.data)-Iter:end)
    ,4));
141 fy_30AoA = mean(AoA_30.data((length(AoA_30.data)-Iter:end)
    ,4));
142
143 fy_22AoA_36Mil = mean(AoA_22_36Mil.data((length(AoA_22_36Mil.
    data)-Iter:end)),4));
144 fy_22AoA_43Mil = mean(AoA_22_43Mil.data((length(AoA_22_43Mil.
    data)-Iter:end)),4));
145 fy_22AoA_54Mil = mean(AoA_22_54Mil.data((length(AoA_22_54Mil.
    data)-Iter:end)),4));
146 %% Moment about the z-axis
147 L = -2.7; % Correction for incorrect location of Moment
    Reference point in CFD Settings
148 Mz_0 = mean(AoA_0.data((length(AoA_0.data)-Iter:end)),8))/L;
149 Mz_10 = mean(AoA_10.data((length(AoA_10.data)-Iter:end)),8))/
    L;
150 Mz_14 = mean(AoA_14.data((length(AoA_14.data)-Iter:end)),8))/
    L;
151 Mz_16 = mean(AoA_16.data((length(AoA_16.data)-Iter:end)),8))/
    L;
152 Mz_18 = mean(AoA_18.data((length(AoA_18.data)-Iter:end)),8))/
    L;
153 Mz_20 = mean(AoA_20.data((length(AoA_20.data)-Iter:end)),8))/
    L;
154 Mz_22 = mean(AoA_22.data((length(AoA_22.data)-Iter:end)),8))/
    L;
155 Mz_24 = mean(AoA_24.data((length(AoA_24.data)-Iter:end)),8))/
    L;
156 Mz_26 = mean(AoA_26.data((length(AoA_26.data)-Iter:end)),8))/
    L;
157 Mz_28 = mean(AoA_30.data((length(AoA_30.data)-Iter:end)),8))/
    L;
158 Mz_30 = mean(AoA_30.data((length(AoA_30.data)-Iter:end)),8))/
    L;
159
160 Mz_22AoA_36Mil = mean(AoA_22_36Mil.data((length(AoA_22_36Mil.
    data)-Iter:end)),8))/L;
161 Mz_22AoA_43Mil = mean(AoA_22_43Mil.data((length(AoA_22_43Mil.
    data)-Iter:end)),8))/L;
162 Mz_22AoA_54Mil = mean(AoA_22_54Mil.data((length(AoA_22_54Mil.
    data)-Iter:end)),8))/L;
163
164 %% Lift
165 AoA = [0 10 14 16 18 20 22 24 26 28 30];
166
167 L_0 = fy_0AoA*cosd(AoA(:,1))+fx_0AoA*sind(AoA(:,1));
168 L_10 = fy_10AoA*cosd(AoA(:,2))+fx_10AoA*sind(AoA(:,2));
169 L_14 = fy_14AoA*cosd(AoA(:,3))+fx_14AoA*sind(AoA(:,3));

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170 L_16 = fy_16AoA*cosd(AoA(:,4))+fx_16AoA*sind(AoA(:,4));
171 L_18 = fy_18AoA*cosd(AoA(:,5))+fx_18AoA*sind(AoA(:,5));
172 L_20 = fy_20AoA*cosd(AoA(:,6))+fx_20AoA*sind(AoA(:,6));
173 L_22 = fy_22AoA*cosd(AoA(:,7))+fx_22AoA*sind(AoA(:,7));
174 L_24 = fy_24AoA*cosd(AoA(:,8))+fx_24AoA*sind(AoA(:,8));
175 L_26 = fy_26AoA*cosd(AoA(:,9))+fx_26AoA*sind(AoA(:,9));
176 L_28 = fy_28AoA*cosd(AoA(:,10))+fx_28AoA*sind(AoA(:,10));
177 L_30 = fy_30AoA*cosd(AoA(:,11))+fx_30AoA*sind(AoA(:,11));
178
179 %% Drag
180
181 D_0 = fx_0AoA*cosd(AoA(:,1))+fy_0AoA*sind(AoA(:,1));
182 D_10 = fx_10AoA*cosd(AoA(:,2))+fy_10AoA*sind(AoA(:,2));
183 D_14 = fx_14AoA*cosd(AoA(:,3))+fy_14AoA*sind(AoA(:,3));
184 D_16 = fx_16AoA*cosd(AoA(:,4))+fy_16AoA*sind(AoA(:,4));
185 D_18 = fx_18AoA*cosd(AoA(:,5))+fy_18AoA*sind(AoA(:,5));
186 D_20 = fx_20AoA*cosd(AoA(:,6))+fy_20AoA*sind(AoA(:,6));
187 D_22 = fx_22AoA*cosd(AoA(:,7))+fy_22AoA*sind(AoA(:,7));
188 D_24 = fx_24AoA*cosd(AoA(:,8))+fy_24AoA*sind(AoA(:,8));
189 D_26 = fx_26AoA*cosd(AoA(:,9))+fy_26AoA*sind(AoA(:,9));
190 D_28 = fx_28AoA*cosd(AoA(:,10))+fy_28AoA*sind(AoA(:,10));
191 D_30 = fx_30AoA*cosd(AoA(:,11))+fy_30AoA*sind(AoA(:,11));
192
193 %% Pitching Moment
194 x_cm = 0.9; % in - Estimated distance from Aero Center
195 MomRef_L = 1;% in - NA
196
197 PM_0 = (Mz_0/MomRef_L)-(L_0*cosd(0)*x_cm)+(D_0*-sind(0)*x_cm)
198 ;
199 PM_10 = (Mz_10/MomRef_L)-(L_10*cosd(10)*x_cm)+(D_10*-sind(10)*
200 x_cm);
201 PM_14 = (Mz_14/MomRef_L)-(L_14*cosd(14)*x_cm)+(D_14*-sind(14)*
202 x_cm);
203 PM_16 = (Mz_16/MomRef_L)-(L_16*cosd(16)*x_cm)+(D_16*-sind(16)*
204 x_cm);
205 PM_18 = (Mz_18/MomRef_L)-(L_18*cosd(18)*x_cm)+(D_18*-sind(18)*
206 x_cm);
207 PM_20 = (Mz_20/MomRef_L)-(L_20*cosd(20)*x_cm)+(D_20*-sind(20)*
208 x_cm);
209 PM_22 = (Mz_22/MomRef_L)-(L_22*cosd(22)*x_cm)+(D_22*-sind(22)*
210 x_cm);
211 PM_24 = (Mz_24/MomRef_L)-(L_24*cosd(24)*x_cm)+(D_24*-sind(24)*
212 x_cm);
213 PM_26 = (Mz_26/MomRef_L)-(L_26*cosd(26)*x_cm)+(D_26*-sind(26)*
214 x_cm);
215 PM_28 = (Mz_28/MomRef_L)-(L_28*cosd(28)*x_cm)+(D_28*-sind(28)*
216 x_cm);
217 PM_30 = (Mz_30/MomRef_L)-(L_30*cosd(30)*x_cm)+(D_30*-sind(30)*
218 x_cm);
219
220 %% Coeffiecient of Lift
221 CL_0 =(L_0*2)/(0.67764*0.0009518*((3751.5/12)^2));
222 CL_10 =(L_10*2)/(0.67764*0.0009518*((3751.5/12)^2));
223 CL_14 =(L_14*2)/(0.67764*0.0009518*((3751.5/12)^2));
224 CL_16 =(L_16*2)/(0.67764*0.0009518*((3751.5/12)^2));
225 CL_18 =(L_18*2)/(0.67764*0.0009518*((3751.5/12)^2));
226 CL_20 =(L_20*2)/(0.67764*0.0009518*((3751.5/12)^2));
227 CL_22 =(L_22*2)/(0.67764*0.0009518*((3751.5/12)^2));

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```

217 CL_24 =(L_24*2)/(0.67764*0.0009518*((3751.5/12)^2));
218 CL_26 =(L_26*2)/(0.67764*0.0009518*((3751.5/12)^2));
219 CL_28 =(L_28*2)/(0.67764*0.0009518*((3751.5/12)^2));
220 CL_30 =(L_30*2)/(0.67764*0.0009518*((3751.5/12)^2));
221
222 CLlist = [CL_0 CL_10 CL_14 CL_16 CL_18 CL_20 CL_22 CL_24 CL_26
            CL_28 CL_30];
223
224 %% Coeffiecient of Drag
225 CD_0 =(D_0*2)/(0.67764*0.0009518*((3751.5/12)^2));
226 CD_10 =(D_10*2)/(0.67764*0.0009518*((3751.5/12)^2));
227 CD_14 =(D_14*2)/(0.67764*0.0009518*((3751.5/12)^2));
228 CD_16 =(D_16*2)/(0.67764*0.0009518*((3751.5/12)^2));
229 CD_18 =(D_18*2)/(0.67764*0.0009518*((3751.5/12)^2));
230 CD_20 =(D_20*2)/(0.67764*0.0009518*((3751.5/12)^2));
231 CD_22 =(D_22*2)/(0.67764*0.0009518*((3751.5/12)^2));
232 CD_24 =(D_24*2)/(0.67764*0.0009518*((3751.5/12)^2));
233 CD_26 =(D_26*2)/(0.67764*0.0009518*((3751.5/12)^2));
234 CD_28 =(D_28*2)/(0.67764*0.0009518*((3751.5/12)^2));
235 CD_30 =(D_30*2)/(0.67764*0.0009518*((3751.5/12)^2));
236
237 CDlist = [CD_0 CD_10 CD_14 CD_16 CD_18 CD_20 CD_22 CD_24 CD_26
            CD_28 CD_30];
238
239 %% Moment Coeffiecient
240 c_bar = 9.66;
241 CM_0 =(PM_0*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
242 CM_10 =(PM_10*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
243 CM_14 =(PM_14*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
244 CM_16 =(PM_16*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
245 CM_18 =(PM_18*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
246 CM_20 =(PM_20*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
247 CM_22 =(PM_22*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
248 CM_24 =(PM_24*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
249 CM_26 =(PM_26*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
250 CM_28 =(PM_28*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
251 CM_30 =(PM_30*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
252
253 CMlist = [CM_0 CM_10 CM_14 CM_16 CM_18 CM_20 CM_22 CM_24 CM_26
            CM_28 CM_30];
254
255 %% Plot
256 % figure(1)
257 % hold on
258 % plot(Alpha_BLF_1,CD_BLF_1, 'k', 'LineWidth',0.9)
259 % plot(AoA,CDlist,'m--o', 'LineWidth',0.9)
260 % grid on
261 % xlabel('\alpha (deg)')
262 % ylabel('C_D (-)')
263 % xlim([0 30])
264 % ylim([0 0.55])
265 % %title('Coefficient of Drag at Re~5e^5')
266 % legend('BLF Wind Tunnel Model, Re~5x10^5','BLF CFD Model, Re
~5x10^5','Location','northeast')
267 % hold off
268
269 % figure(2)
270 % hold on

```

```

271 % plot(Alpha_BLF_1,CL_BLF_1, 'k', 'LineWidth',0.9)
272 % plot(AoA,CLlist,'b--o', 'LineWidth',0.9)
273 % grid on
274 % xlabel('\alpha (deg)')
275 % ylabel('C_L (-)')
276 % xlim([0 30])
277 % ylim([0 1.1])
278 % %title('Coefficient of Drag at Re~5e^5')
279 % legend('BLF Wind Tunnel Model, Re~5x10^5','BLF CFD Model, Re
~5x10^5','Location','northeast')
280 % hold off
281 %
282 figure(3)
283 hold on
284 plot(Alpha_BLF_1,CM_BLF_1, 'k', 'LineWidth',0.9)
285 plot(AoA,CMList,'r--o', 'LineWidth',0.9)
286 grid on
287 xlabel('\alpha (deg)')
288 ylabel('C_M (-)')
289 xlim([0 30])
290 ylim([-0.07 0.03])
291 %title('Coefficient of Drag at Re~5e^5')
292 legend('BLF Wind Tunnel Model, Re~5x10^5','BLF CFD Model, Re~5
x10^5','Location','northeast')
293 hold off
294
295 %% Grid Study Plots
296
297 % figure (4) % Iterations vs fx
298 % hold on
299 % plot (AoA_22_36Mil.data(:,1),AoA_22_36Mil.data(:,3), '
LineWidth',.9)
300 % plot (AoA_22_43Mil.data(:,1),AoA_22_43Mil.data(:,3), '
LineWidth',.9)
301 % plot (AoA_22_54Mil.data(:,1),AoA_22_54Mil.data(:,3), '
LineWidth',.9)
302 % grid on
303 % legend('BLF 22^o \alpha: 36x10^6 Cell Mesh','BLF 22^o \alpha
: 43x10^6 Cell Mesh','BLF 22^o \alpha: 54x10^6 Cell Mesh')
304 % xlabel('Iteration (-)')
305 % ylabel('Fx (lb_f)')
306 % xlim([0 3500])
307 % hold off
308 %
309 % figure (5) % Iterations vs fy
310 % hold on
311 % plot (AoA_22_36Mil.data(:,1),AoA_22_36Mil.data(:,4), '
LineWidth',.9)
312 % plot (AoA_22_43Mil.data(:,1),AoA_22_43Mil.data(:,4), '
LineWidth',.9)
313 % plot (AoA_22_54Mil.data(:,1),AoA_22_54Mil.data(:,4), '
LineWidth',.9)
314 % grid on
315 % legend('BLF 22^o \alpha: 36x10^6 Cell Mesh','BLF 22^o \alpha
: 43x10^6 Cell Mesh','BLF 22^o \alpha: 54x10^6 Cell Mesh')
316 % xlabel('Iteration (-)')
317 % ylabel('Fy (lb_f)')
318 % xlim([0 3500])

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```

319 % hold off
320 %
321 % figure (7) % Iterations vs Mz
322 % hold on
323 % plot (AoA_22_36Mil.data(:,1),AoA_22_36Mil.data(:,8), '
    LineWidth',.9)
324 % plot (AoA_22_43Mil.data(:,1),AoA_22_43Mil.data(:,8), '
    LineWidth',.9)
325 % plot (AoA_22_54Mil.data(:,1),AoA_22_54Mil.data(:,8), '
    LineWidth',.9)
326 % grid on
327 % legend('BLF 22^o \alpha: 36x10^6 Cell Mesh','BLF 22^o \alpha
    : 43x10^6 Cell Mesh','BLF 22^o \alpha: 54x10^6 Cell Mesh')
328 % xlabel('Iteration (-)')
329 % ylabel('Mz (lb_f-in)')
330 % xlim([0 3500])
331 % hold off
332 %

```

## Appendix F. MATLAB Script: AFC Slot Comparison

```
1 %% AFC Windtunnel Configuration at Slot 200 SLPM Equivalent
   Mach Comparison
2 clear all; close all; clc; format compact; format short;
3 %% AFC 200 SLPM Wind Tunnel Data (Used Data Corrected for Slot
   Forces)
4 % (1.5 degree correction applied to all comparison cases)
5 %Corrected - Includes Slot Forces (Used because slot force
   accounting was
6 % not used on CFD Model
7 Alpha_Slot_200=1.5+...
8 [-7.325360000000000;-7.12619691322077;-6.01826819591974;...
9 -4.99732769885743;-3.97582237402429;-2.86342706392424;...
10 -1.84094117227809;-0.728418723321121;0.294384067844568;...
11 1.31593289300810;2.33851440655027;3.45016976776966;...
12 4.47206617206829;5.49070656871355;6.59454368653200;...
13 7.61119362226182;8.71646655625306;9.73406169439868;...
14 10.7501841133734;11.8546234227027;12.8685771271328;...
15 13.8843050386178;14.9877156184099;15.9766275933576;...
16 16.9667764697981;18.0387374621311;19.0188898729756;...
17 20.0827728221427;21.0581188095630;22.0214926072595;...
18 23.0756100723189;24.0351895977165;25.0254177062543;...
19 26.0886845757370;27.0624075174387;28.0010985196644;...
20 29.0358902266110;30.0067726241810;30.9823507347488;...
21 32.0290971475978;32.9765237666068];
22 CD_Slot_200=...
23 [0.0320851692367218;0.0273815158308049;0.022028068283...
24 1334;0.0189948756536030;0.0167746691423112;0.01383175...
25 73836602;0.0130883781625435;0.0132404288164375;0.01360...
26 89776067175;0.0151711588370946;0.0170179100405769;0.02...
27 08589907757831;0.0251307316165439;0.0292991820534647;...
28 0.0343779160466618;0.0399904833734356;0.04714885833623...
29 37;0.0548359613605498;0.0646154741009459;0.080281580552...
30 7789;0.0987049411330914;0.119516801309473;0.147431051406...
31 686;0.176492397770010;0.203682297126652;0.2342171005386...
32 91;0.262088029070669;0.291016585238808;0.3114467560713...
33 94;0.330436992680708;0.350846091507866;0.3712437809582...
34 23;0.389332297209873;0.405519824046928;0.4295591767327...
35 85;0.443403369553939;0.460859536482907;0.4769916770151...
36 77;0.488632311142265;0.510383332757284;0.521800095686450];
37 CL_Slot_200=...
38 [-0.335479659988982;-0.289723542352643;-0.2383758075032...
39 50;-0.185735224621090;-0.131647542404540;-0.07400863802...
40 58560;-0.0179183018172943;0.0357991832424506;0.0877594...
41 908739248;0.139620538444450;0.192033665532018;0.247965...
42 668019429;0.300433823974841;0.344503558646343;0.392427...
43 083770628;0.436480378822970;0.485037273214251;0.530485...
44 368755756;0.576947549000008;0.624408759142942;0.671359...
45 983759139;0.733289050863228;0.793372641556728;0.833976...
46 884518732;0.875995042630878;0.881499492606525;0.888641...
47 572961824;0.883404282806119;0.872417014112908;0.857981...
48 275529303;0.857459131143811;0.852351843832441;0.848668...
49 821163629;0.847173246376986;0.858961211546805;0.839120...
50 243942654;0.830986259074614;0.828885307451839;0.800747...
51 889683352;0.814787518311700;0.795533401163343];
52 CM_Slot_200=...
```

```

53 [-0.00889959111869580;-0.00778045651020314;-0.007310345...
54 19728563;-0.00768453754214641;-0.00878640412371663;-0.0...
55 101995079971602;-0.0106242428121077;-0.010620921998711...
56 2;-0.00912260756273299;-0.00794144387024076;-0.00724631...
57 706996894;-0.00799818316211891;-0.00742068458948495;-0....
58 00588142736053394;-0.00387951969514295;-0.002152077560...
59 13230;-0.000813989534200628;7.53100690620058e
    -05;0.000576047750594334;-0.00334800935435651;-0.0145503...
60 535703555;-0.0274290694087500;-0.0405778396192745;-0.05...
61 08147274565507;-0.0600713073812277;-0.0623202507925946...
62 ;-0.0649580225354113;-0.0675484100666562;-0.06971550741...
63 67166;-0.0713675481322402;-0.0752711253271166;-0.075739...
64 2784226241;-0.0768935292888157;-0.0782355024377671;-0.0...
65 783986741164982;-0.0765276274596814;-0.075983837650995...
66 9;-0.0754625886066138;-0.0737799892519261;-0.0730929027...
67 786348;-0.0745404094970535]+0.01;
68
69 % Uncorrected Data
70 % Alpha_Slot_200_UN=1.5+...
71 [-8.13930569650318;-7.12694507515062;-6.02140811853273;...
72 -5.00170105594408;-3.98198111516462;-2.87036265170578;...
73 -1.84851324989122;-0.829147376904798;0.278405572171361;...
74 0.830926257583539;1.29568572893127;1.84718260035369;...
75 2.40197787987524;2.86990616314340;3.42386719604621;...
76 3.89045100146877;4.44232258507587;5.45367108933443;...
77 6.55597231268537;7.56639951144478;8.66928705589410;...
78 9.68113243597496;10.6947912580051;11.7961467191067;...
79 12.8093111578703;13.8364110334608;14.9500955001699;...
80 15.9579723471582;16.9664225058238;18.0282886988279;...
81 19.0036122250817;20.0556137860657;21.0148460077832;...
82 21.9702533986755;22.9384955211547;23.9902030711724;...
83 24.9551128961650;25.9233516796538;26.9910982455396;...
84 27.9409309963523;28.9897676706375;29.9562597573613;...
85 30.8989470972295;31.9683622607734;32.9188182156738];...
86 % CD_Slot_200_UN=...
87 [0.0249842840892673;0.0195604134915005;0.0143834216638...
88 751;0.0108549143990608;0.00816881835012328;0.004879311...
89 46539239;0.00395781966804512;0.00365483992792561;0.004...
90 28241322482735;0.00474407790921938;0.0057582558648709...
91 8;0.00645273970293498;0.00751031094048318;0.0094122348...
92 9896528;0.0110575635340329;0.0132817317745282;0.015133...
93 5148856012;0.0188803112856184;0.0240003722774144;0.029...
94 4918706354342;0.0366716976789302;0.0443669347927839;0...
95 0532532582951283;0.0695916787031502;0.088008587337434...
96 5;0.108464773625040;0.136824436503663;0.16582820991150...
97 7;0.192436036579450;0.223461254556216;0.25112573246278...
98 7;0.280867767929434;0.301227165976154;0.32037888054629...
99 5;0.341135419249444;0.360932278333196;0.37833276340675...
100 3;0.395976505144352;0.419017614622716;0.43261089695018...
101 3;0.450796231404737;0.466349160853958;0.47795232912708...
102 8;0.500123088459546;0.510802744409361];
103 % CL_Slot_200_UN
    =[-0.338646961351646,-0.292659862392328,-0.2411828826456...
104 14,-0.188464920242479,-0.134672726701926,-0.07674586574...
105 51916,-0.0206952235870607,0.0327214552553833,0.0852759...
106 690471117,0.111281942933680,0.136480593829496,0.161400...
107 738366892,0.188758512195716,0.217317919068340,0.244851...
108 486437686,0.271984976572820,0.297302530690163,0.341155...

```

```

109 632833166,0.389200881638037,0.433137445034258,0.481804...
110 530093597,0.527245178134752,0.573548540644765,0.620590...
111 739659397,0.667430345563330,0.729049497802401,0.789167...
112 505771261,0.829338662373363,0.871178430668242,0.876339...
113 382985236,0.883045943420430,0.877744734569981,0.866324...
114 720972384,0.851908768417901,0.851104984074884,0.845491...
115 955167970,0.841154026490747,0.839286128027530,0.850683...
116 644332506,0.830355379707657,0.821697577864173,0.819037...
117 753064181,0.790070686515306,0.803237872240048,0.783570...
118 560967676]';
119 % CM_Slot_200_UN=...
120 [-0.00834979338577161;-0.00715681206848110;-0.0065466537...
121 4145752;-0.00688203234423188;-0.00779458060051240;-0.009...
122 27762017151896;-0.00966528705279758;-0.0095679478086160...
123 9;-0.00825205444560790;-0.00753024158239537;-0.006931591...
124 21437764;-0.00624167419865799;-0.00627780524635620;-0.00...
125 677685305657774;-0.00714047929698264;-0.00719647138574...
126 427;-0.00666526788181024;-0.00520675806074079;-0.0033756...
127 8081036960;-0.00182896399677014;-0.000752203860571932;...
128 -8.69837691748233e
      -05;0.000220931046794505;-0.00394263893098121;-0.01545796...

129 10548854;-0.0286247777470567;-0.0421161886578441;-0.0526...
130 581066968622;-0.0622903713117134;-0.0649164366029284;-0....
131 0679676602655533;-0.0710301613427541;-0.073605044751386...
132 5;-0.0757827756531143;-0.0801753059813129;-0.08113066871...
133 99231;-0.0827144357251951;-0.0846946079541785;-0.0854294...
134 231628424;-0.0841215861740769;-0.0841665989358836;-0.084...
135 2169756662313;-0.0831993253281970;-0.0831674320221782;...
136 -0.0852008474669002];
137
138
139 %% Import Kestrel Data
140 [AoA_0] = importdata('0AoA_forces.dat',' ',23);
141 [AoA_10] = importdata('10AoA_forces.dat',' ',23);
142 [AoA_14] = importdata('14AoA_forces.dat',' ',23);
143 [AoA_16] = importdata('16AoA_forces.dat',' ',23);
144 [AoA_18] = importdata('18AoA_forces.dat',' ',23);
145 [AoA_20] = importdata('20AoA_forces.dat',' ',23);
146 [AoA_22] = importdata('22AoA_49Mil_forces.dat',' ',23);
147 [AoA_24] = importdata('24AoA_forces.dat',' ',23);
148 [AoA_26] = importdata('26AoA_forces.dat',' ',23);
149 [AoA_28] = importdata('28AoA_forces.dat',' ',23);
150 [AoA_30] = importdata('30AoA_forces.dat',' ',23);
151
152 [AoA_22_28Mil] = importdata('22AoA_28Mil_forces.dat',' ',23);
153 [AoA_22_31Mil] = importdata('22AoA_31Mil_forces.dat',' ',23);
154
155 %% Axial Forces
156 Iter = 1000; %Number of iterations to average over
157
158 fx_0AoA = mean(AoA_0.data((([length(AoA_0.data)-Iter:end])),33))
      ;
159 fx_10AoA = mean(AoA_10.data((([length(AoA_10.data)-Iter:end])
      ,33)));
160 fx_14AoA = mean(AoA_14.data((([length(AoA_14.data)-Iter:end])
      ,33)));
161 fx_16AoA = mean(AoA_16.data((([length(AoA_16.data)-Iter:end])

```

```

    ,33));
162 fx_18AoA = mean(AoA_18.data((length(AoA_18.data)-Iter:end)
    ,33));
163 fx_20AoA = mean(AoA_20.data((length(AoA_20.data)-Iter:end)
    ,33));
164 fx_22AoA = mean(AoA_22.data((length(AoA_22.data)-Iter:end)
    ,33));
165 fx_24AoA = mean(AoA_24.data((length(AoA_24.data)-Iter:end)
    ,33));
166 fx_26AoA = mean(AoA_26.data((length(AoA_26.data)-Iter:end)
    ,33));
167 fx_28AoA = mean(AoA_28.data((length(AoA_28.data)-Iter:end)
    ,33));
168 fx_30AoA = mean(AoA_30.data((length(AoA_30.data)-Iter:end)
    ,33));
169
170 fx_22AoA_28Mil = mean(AoA_22_28Mil.data((length(AoA_22_28Mil.
    data)-Iter:end)),33));
171 fx_22AoA_31Mil = mean(AoA_22_31Mil.data((length(AoA_22_31Mil.
    data)-Iter:end)),33));
172
173 %% Vertical Forces
174 fy_0AoA = mean(AoA_0.data((length(AoA_0.data)-Iter:end)),34))
    ;
175 fy_10AoA = mean(AoA_10.data((length(AoA_10.data)-Iter:end)
    ,34));
176 fy_14AoA = mean(AoA_14.data((length(AoA_14.data)-Iter:end)
    ,34));
177 fy_16AoA = mean(AoA_16.data((length(AoA_16.data)-Iter:end)
    ,34));
178 fy_18AoA = mean(AoA_18.data((length(AoA_18.data)-Iter:end)
    ,34));
179 fy_20AoA = mean(AoA_20.data((length(AoA_20.data)-Iter:end)
    ,34));
180 fy_22AoA = mean(AoA_22.data((length(AoA_22.data)-Iter:end)
    ,34));
181 fy_24AoA = mean(AoA_24.data((length(AoA_24.data)-Iter:end)
    ,34));
182 fy_26AoA = mean(AoA_26.data((length(AoA_26.data)-Iter:end)
    ,34));
183 fy_28AoA = mean(AoA_28.data((length(AoA_28.data)-Iter:end)
    ,34));
184 fy_30AoA = mean(AoA_30.data((length(AoA_30.data)-Iter:end)
    ,34));
185
186 fy_22AoA_28Mil = mean(AoA_22_28Mil.data((length(AoA_22_28Mil.
    data)-Iter:end)),34));
187 fy_22AoA_31Mil = mean(AoA_22_31Mil.data((length(AoA_22_31Mil.
    data)-Iter:end)),34));
188
189 %% Moment about the z-axis
190 L = -1.28; % Correction for incorrect location of Moment
    Reference point in CFD Settings
191 Mz_0 = mean(AoA_0.data((length(AoA_0.data)-Iter:end)),38))/L;
192 Mz_10 = mean(AoA_10.data((length(AoA_10.data)-Iter:end)),38)
    /L;
193 Mz_14 = mean(AoA_14.data((length(AoA_14.data)-Iter:end)),38)
    /L;

```

```

194 Mz_16 = mean(AoA_16.data((([length(AoA_16.data)-Iter:end])),38))
      /L;
195 Mz_18 = mean(AoA_18.data((([length(AoA_18.data)-Iter:end])),38))
      /L;
196 Mz_20 = mean(AoA_20.data((([length(AoA_20.data)-Iter:end])),38))
      /L;
197 Mz_22 = mean(AoA_22.data((([length(AoA_22.data)-Iter:end])),38))
      /L;
198 Mz_24 = mean(AoA_24.data((([length(AoA_24.data)-Iter:end])),38))
      /L;
199 Mz_26 = mean(AoA_26.data((([length(AoA_26.data)-Iter:end])),38))
      /L;
200 Mz_28 = mean(AoA_28.data((([length(AoA_28.data)-Iter:end])),38))
      /L;
201 Mz_30 = mean(AoA_30.data((([length(AoA_30.data)-Iter:end])),38))
      /L;
202
203 Mz_22AoA_28Mil = mean(AoA_22_28Mil.data((([length(AoA_22_28Mil.
      data)-Iter:end])),38))/L;
204 Mz_22AoA_31Mil = mean(AoA_22_31Mil.data((([length(AoA_22_31Mil.
      data)-Iter:end])),38))/L;
205
206 %% Lift
207 AoA = [0 10 14 16 18 20 22 24 26 28 30];
208
209 L_0 = fy_0AoA*cosd(AoA(:,1))+fx_0AoA*sind(AoA(:,1));
210 L_10 = fy_10AoA*cosd(AoA(:,2))+fx_10AoA*sind(AoA(:,2));
211 L_14 = fy_14AoA*cosd(AoA(:,3))+fx_14AoA*sind(AoA(:,3));
212 L_16 = fy_16AoA*cosd(AoA(:,4))+fx_16AoA*sind(AoA(:,4));
213 L_18 = fy_18AoA*cosd(AoA(:,5))+fx_18AoA*sind(AoA(:,5));
214 L_20 = fy_20AoA*cosd(AoA(:,6))+fx_20AoA*sind(AoA(:,6));
215 L_22 = fy_22AoA*cosd(AoA(:,7))+fx_22AoA*sind(AoA(:,7));
216 L_24 = fy_24AoA*cosd(AoA(:,8))+fx_24AoA*sind(AoA(:,8));
217 L_26 = fy_26AoA*cosd(AoA(:,9))+fx_26AoA*sind(AoA(:,9));
218 L_28 = fy_28AoA*cosd(AoA(:,10))+fx_28AoA*sind(AoA(:,10));
219 L_30 = fy_30AoA*cosd(AoA(:,11))+fx_30AoA*sind(AoA(:,11));
220
221 %% Drag
222
223 D_0 = fx_0AoA*cosd(AoA(:,1))+fy_0AoA*sind(AoA(:,1));
224 D_10 = fx_10AoA*cosd(AoA(:,2))+fy_10AoA*sind(AoA(:,2));
225 D_14 = fx_14AoA*cosd(AoA(:,3))+fy_14AoA*sind(AoA(:,3));
226 D_16 = fx_16AoA*cosd(AoA(:,4))+fy_16AoA*sind(AoA(:,4));
227 D_18 = fx_18AoA*cosd(AoA(:,5))+fy_18AoA*sind(AoA(:,5));
228 D_20 = fx_20AoA*cosd(AoA(:,6))+fy_20AoA*sind(AoA(:,6));
229 D_22 = fx_22AoA*cosd(AoA(:,7))+fy_22AoA*sind(AoA(:,7));
230 D_24 = fx_24AoA*cosd(AoA(:,8))+fy_24AoA*sind(AoA(:,8));
231 D_26 = fx_26AoA*cosd(AoA(:,9))+fy_26AoA*sind(AoA(:,9));
232 D_28 = fx_28AoA*cosd(AoA(:,10))+fy_28AoA*sind(AoA(:,10));
233 D_30 = fx_30AoA*cosd(AoA(:,11))+fy_30AoA*sind(AoA(:,11));
234
235 %% Pitching Moment
236 x_cm = 1.3; % in - Estimated distance from Aero Center
237 MomRef_L = 1; % in - NA
238
239 PM_0 = (Mz_0/MomRef_L)-(L_0*cosd(0)*x_cm)+(D_0*-sind(0)*x_cm)
      ;
240 PM_10 = (Mz_10/MomRef_L)-(L_10*cosd(10)*x_cm)+(D_10*-sind(10)*

```

```

    x_cm);
241 PM_14 = (Mz_14/MomRef_L)-(L_14*cosd(14)*x_cm)+(D_14*-sind(14)*
    x_cm);
242 PM_16 = (Mz_16/MomRef_L)-(L_16*cosd(16)*x_cm)+(D_16*-sind(16)*
    x_cm);
243 PM_18 = (Mz_18/MomRef_L)-(L_18*cosd(18)*x_cm)+(D_18*-sind(18)*
    x_cm);
244 PM_20 = (Mz_20/MomRef_L)-(L_20*cosd(20)*x_cm)+(D_20*-sind(20)*
    x_cm);
245 PM_22 = (Mz_22/MomRef_L)-(L_22*cosd(22)*x_cm)+(D_22*-sind(22)*
    x_cm);
246 PM_24 = (Mz_24/MomRef_L)-(L_24*cosd(24)*x_cm)+(D_24*-sind(24)*
    x_cm);
247 PM_26 = (Mz_26/MomRef_L)-(L_26*cosd(26)*x_cm)+(D_26*-sind(26)*
    x_cm);
248 PM_28 = (Mz_28/MomRef_L)-(L_28*cosd(28)*x_cm)+(D_28*-sind(28)*
    x_cm);
249 PM_30 = (Mz_30/MomRef_L)-(L_30*cosd(30)*x_cm)+(D_30*-sind(30)*
    x_cm);
250
251 %% Coeffiecient of Lift
252 CL_0 =(L_0*2)/(0.67764*0.0009518*((3751.5/12)^2));
253 CL_10 =(L_10*2)/(0.67764*0.0009518*((3751.5/12)^2));
254 CL_14 =(L_14*2)/(0.67764*0.0009518*((3751.5/12)^2));
255 CL_16 =(L_16*2)/(0.67764*0.0009518*((3751.5/12)^2));
256 CL_18 =(L_18*2)/(0.67764*0.0009518*((3751.5/12)^2));
257 CL_20 =(L_20*2)/(0.67764*0.0009518*((3751.5/12)^2));
258 CL_22 =(L_22*2)/(0.67764*0.0009518*((3751.5/12)^2));
259 CL_24 =(L_24*2)/(0.67764*0.0009518*((3751.5/12)^2));
260 CL_26 =(L_26*2)/(0.67764*0.0009518*((3751.5/12)^2));
261 CL_28 =(L_28*2)/(0.67764*0.0009518*((3751.5/12)^2));
262 CL_30 =(L_30*2)/(0.67764*0.0009518*((3751.5/12)^2));
263
264 CLlist = [CL_0 CL_10 CL_14 CL_16 CL_18 CL_20 CL_22 CL_24 CL_26
    CL_28 CL_30];
265
266 %% Coeffiecient of Drag
267 CD_0 =(D_0*2)/(0.67764*0.0009518*((3751.5/12)^2));
268 CD_10 =(D_10*2)/(0.67764*0.0009518*((3751.5/12)^2));
269 CD_14 =(D_14*2)/(0.67764*0.0009518*((3751.5/12)^2));
270 CD_16 =(D_16*2)/(0.67764*0.0009518*((3751.5/12)^2));
271 CD_18 =(D_18*2)/(0.67764*0.0009518*((3751.5/12)^2));
272 CD_20 =(D_20*2)/(0.67764*0.0009518*((3751.5/12)^2));
273 CD_22 =(D_22*2)/(0.67764*0.0009518*((3751.5/12)^2));
274 CD_24 =(D_24*2)/(0.67764*0.0009518*((3751.5/12)^2));
275 CD_26 =(D_26*2)/(0.67764*0.0009518*((3751.5/12)^2));
276 CD_28 =(D_28*2)/(0.67764*0.0009518*((3751.5/12)^2));
277 CD_30 =(D_30*2)/(0.67764*0.0009518*((3751.5/12)^2));
278
279 CDlist = [CD_0 CD_10 CD_14 CD_16 CD_18 CD_20 CD_22 CD_24 CD_26
    CD_28 CD_30];
280
281 %% Moment Coeffiecient
282 c_bar = 9.66;
283 CM_0 =(PM_0*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
284 CM_10 =(PM_10*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
285 CM_14 =(PM_14*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
286 CM_16 =(PM_16*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);

```

```

287 CM_18 =(PM_18*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
288 CM_20 =(PM_20*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
289 CM_22 =(PM_22*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
290 CM_24 =(PM_24*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
291 CM_26 =(PM_26*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
292 CM_28 =(PM_28*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
293 CM_30 =(PM_30*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
294
295 CMlist = [CM_0 CM_10 CM_14 CM_16 CM_18 CM_20 CM_22 CM_24 CM_26
            CM_28 CM_30];
296
297
298 %% Plot
299 % figure(1)
300 % hold on
301 % plot(Alpha_Slot_200,CD_Slot_200, 'k', 'LineWidth',0.9)
302 % %plot(Alpha_Slot_200_UN,CD_Slot_200_UN, 'g', 'LineWidth
    ',0.9)
303 % plot(AoA,CDlist,'m--o', 'LineWidth',0.9)
304 % grid on
305 % xlabel('\alpha (deg)')
306 % ylabel('C_D (-)')
307 % xlim([0 30])
308 % ylim([0 0.55])
309 % legend('AFC C_{\mu}=0.49% Wind Tunnel Model, Re~5x10^5','AFC
    C_{\mu}=0.49% CFD Model, Re~5x10^5','Location','northeast
    ')
310 % hold off
311
312 % figure(2)
313 % hold on
314 % plot(Alpha_Slot_200,CL_Slot_200, 'k', 'LineWidth',0.9)
315 % %plot(Alpha_Slot_200_UN,CL_Slot_200_UN, 'g', 'LineWidth
    ',0.9)
316 % plot(AoA,CLlist,'b--o', 'LineWidth',0.9)
317 % grid on
318 % xlabel('\alpha (deg)')
319 % ylabel('C_L (-)')
320 % xlim([0 30])
321 % ylim([0 1.15])
322 % legend('AFC C_{\mu}=0.49% Wind Tunnel Model, Re~5x10^5','AFC
    C_{\mu}=0.49% CFD Model, Re~5x10^5','Location','northeast
    ')
323 % hold off
324 %
325 % figure(3)
326 % hold on
327 % plot(Alpha_Slot_200,CM_Slot_200, 'k', 'LineWidth',0.9)
328 % %plot(Alpha_Slot_200_UN,CM_Slot_200_UN, 'g', 'LineWidth
    ',0.9)
329 % plot(AoA,CMlist,'r--o', 'LineWidth',0.9)
330 % grid on
331 % xlabel('\alpha (deg)')
332 % ylabel('C_M (-)')
333 % xlim([0 30])
334 % ylim([-0.08 0.035])
335 % legend('AFC C_{\mu}=0.49% Wind Tunnel Model, Re~5x10^5','AFC
    C_{\mu}=0.49% CFD Model, Re~5x10^5','Location','northeast

```

```

    ')
336 % hold off
337
338 %% Grid Study Plots
339
340 % figure (4) % Iterations vs fx
341 % hold on
342 % plot (AoA_22_28Mil.data(:,1),AoA_22_28Mil.data(:,3), '
    LineWidth',.9)
343 % plot (AoA_22_31Mil.data(:,1),AoA_22_31Mil.data(:,3), '
    LineWidth',.9)
344 % plot (AoA_22.data(:,1),AoA_22.data(:,3), 'LineWidth',.9)
345 % grid on
346 % legend('AFC Slot C_{\mu}=0.49%, \alpha=22^o, 28x10^6 Cell
    Mesh','AFC Slot C_{\mu}=0.49%, \alpha=22^o, 31x10^6 Cell
    Mesh','AFC Slot C_{\mu}=0.49%, \alpha=22^o, 49x10^6 Cell
    Mesh')
347 % xlabel('Iteration (-)')
348 % ylabel('Fx (lb_f)')
349 % xlim([0 3000])
350 % hold off
351 %
352 % figure (5) % Iterations vs fy
353 % hold on
354 % plot (AoA_22_28Mil.data(:,1),AoA_22_28Mil.data(:,4), '
    LineWidth',.9)
355 % plot (AoA_22_31Mil.data(:,1),AoA_22_31Mil.data(:,4), '
    LineWidth',.9)
356 % plot (AoA_22.data(:,1),AoA_22.data(:,4), 'LineWidth',.9)
357 % grid on
358 % legend('AFC Slot C_{\mu}=0.49%, \alpha=22^o, 28x10^6 Cell
    Mesh','AFC Slot C_{\mu}=0.49%, \alpha=22^o, 31x10^6 Cell
    Mesh','AFC Slot C_{\mu}=0.49%, \alpha=22^o, 49x10^6 Cell
    Mesh')
359 % xlabel('Iteration (-)')
360 % ylabel('Fy (lb_f)')
361 % xlim([0 3000])
362 % hold off
363 %
364 figure (7) % Iterations vs Mz
365 hold on
366 plot (AoA_22_28Mil.data(:,1),AoA_22_28Mil.data(:,8), '
    LineWidth',.9)
367 plot (AoA_22_31Mil.data(:,1),AoA_22_31Mil.data(:,8), '
    LineWidth',.9)
368 plot (AoA_22.data(:,1),AoA_22.data(:,8), 'LineWidth',.9)
369 grid on
370 legend('AFC Slot C_{\mu}=0.49%, \alpha=22^o, 28x10^6 Cell Mesh
    ','AFC Slot C_{\mu}=0.49%, \alpha=22^o, 31x10^6 Cell Mesh',
    'AFC Slot C_{\mu}=0.49%, \alpha=22^o, 49x10^6 Cell Mesh')
371 xlabel('Iteration (-)')
372 ylabel('Mz (lb_f-in)')
373 xlim([0 3000])
374 hold off

```

## Appendix G. MATLAB Script: AFC Slot Width Optimization

```

1 %% AFC Slot Width Optimization
2 %clear all; close all; clc; format compact; format short;
3 %% Baseline, Passive BLF and AFC Slot, Freestream M = 0.059,
   SW1, M1-M5 Wind Tunnel Uncorrected Data
4 alpha = 1;
5 Alpha_Baseline2=alpha+...
6 [-8.17894442052277;-7.16850773849801;-6.15464379090849;...
7 -5.04877209800816;-4.02932120636633;-3.00640352702020;...
8 -1.98382443346184;-0.870213403716582;0.153319187693818;...
9 1.17508365277160;2.19900159794485;3.30928370940170;...
10 4.32751503348324;5.34186930698045;6.44211101586254;...
11 7.45523765217682;8.46819102061274;9.56920569459411;...
12 10.6678210098701;11.6756459136262;12.7671846976348;...
13 13.7663130389622;14.8512817871214;15.9311893169993;...
14 17.0110707277628;18.0844673115262;19.1538944819053;...
15 20.2221014158863;21.3721215112022;22.4257937648188;...
16 23.5698166553147;24.6991922407033;25.7472428560031;...
17 26.8830239002552;28.0967117595190;29.2310840568254;...
18 30.4510280084815;31.6729762552610;32.9017417048610;...
19 34.2275325071614;35.4596797612262;36.7847709966838];...
20 CD_Base2=...
21 [0.0326396226315288;0.0273554591561591;0.02320762912...
22 52264;0.0184655617641355;0.0156734227994947;0.013931...
23 8232188933;0.0127460003513771;0.0110429698239139;0.0...
24 115328779992575;0.0132684007837646;0.01594624739861...
25 14;0.0186260816468254;0.0227511043823911;0.027425377...
26 8944443;0.0325465190807324;0.0391042044857320;0.0473...
27 291339011119;0.0578153893612589;0.0714274594986400;0...
28 .0882968225391222;0.107396801468250;0.12837527862316...
29 1;0.152008514898266;0.177050724527485;0.203713593209...
30 787;0.230608840670329;0.257527050009981;0.2850390953...
31 55441;0.311662701851170;0.335885212499362;0.35962757...
32 0078000;0.378102215918811;0.393975988177553;0.4094634...
33 43267234;0.422979456980625;0.438129375146260;0.452553...
34 360061481;0.469150907399056;0.488570671603892;0.51410...
35 4483039872;0.536274210618872;0.565069415967284];
36 CL_Base2=...
37 [-0.380686716946657,-0.335679522978898,-0.28809803698...
38 6591,-0.235205472140068,-0.180638051940071,-0.1234544...
39 23606297,-0.0655693172981972,-0.00446862170388157,0.0...
40 533671656873325,0.110388299123664,0.169693355141534,...
41 0.227263490287654,0.279476897333351,0.32863898256204...
42 2,0.375560539057904,0.422360052709387,0.4700363760260...
43 67,0.517777718341523,0.561913793013043,0.604151005786...
44 968,0.641842476206843,0.673795777863523,0.70451924645...
45 7192,0.729874924214394,0.754142327869694,0.7725926727...
46 70825,0.786833165496932,0.798718935717348,0.805103685...
47 529550,0.802634940849533,0.801598645011175,0.78608838...
48 7524569,0.776596912840933,0.767880111293073,0.7484587...
49 51498765,0.737187298271561,0.724400980387816,0.713740...
50 363550526,0.709249314247855,0.715390882106700,0.71448...
51 6482896382,0.719886109135885]';
52 CM_Base2=...
53 [-0.00241933648422381;-0.000994749356042714;0.00052513...
```

```

54 8889181397;0.000531995120895268;-0.000127610521605613;...
55 -0.00112181497128817;-0.00238738588975404;-0.004014823...
56 77348298;-0.00458591893002119;-0.00447507033838957;-0.0...
57 0570421624022764;-0.00639759228464273;-0.006060593543...
58 11681;-0.00452373994614179;-0.00254238263866779;-0.000...
59 802608455539601;0.000686585846786974;0.0019224715481...
60 3012;0.00305034068341110;0.00384085470805589;0.0046514...
61 9185638424;0.00533251814807207;0.00492217834961218;0.0...
62 0390892393185356;0.00131507381415635;-0.0018753227054...
63 2222;-0.00563731602852632;-0.0109907490359497;-0.016914...
64 9235037892;-0.0248236615415000;-0.0317363120696212;-0.0...
65 393746528162185;-0.0435606742506112;-0.043896906122957...
66 7;-0.0457089065451211;-0.0471099572765705;-0.04925656335...
67 62850;-0.0525805261396649;-0.0556579516727002;-0.0595181...
68 996791140;-0.0641550435894548;-0.0701361258272115];
69
70
71 Alpha_BLF_1=alpha+...
72 [-8.06594564259070;-7.14241231732519;-6.03905594741620;...
73 -5.01406378048430;-3.98721923601549;-2.87195351727540;...
74 -1.85058803650554;-0.831110322743736;0.275151806711067;...
75 1.29346471552093;2.31597900276951;3.42813304789199;...
76 4.45108375100950;5.55684707512697;6.57167414343638;...
77 7.58705903612775;8.69009006482263;9.70504580065541;...
78 10.7161174843277;11.2642436005670;11.8166774071110;...
79 12.2766843085277;12.8266085308312;13.3790159996166;...
80 13.8375751427264;14.3856475805125;14.9354617926899;...
81 15.3929723623862;15.9414105042531;16.4688861494385;...
82 16.9094889255359;17.4240418013865;17.9837233404080;...
83 18.4646453036484;18.9881016785306;19.5209239626320;...
84 20.0480920643511;20.4921008071506;21.0161537952655;...
85 21.5513155912465;21.9819661259102;22.4844514540255;...
86 23.0266031504895;23.4649469590941;23.9788010755111;...
87 24.4993216153161;24.9404098936923;25.4654301290090;...
88 25.9851110721517;26.4294113964856;26.9572368515206;...
89 27.4879036272060;27.9159749086103;28.4552397489093;...
90 28.9719941570135;29.4032901602970;29.9353877441201;...
91 30.4579590792370;30.8794429116547;31.4044874140582;...
92 31.9278672633083;32.3622515736385;32.8915967016012];
93 CD_BLF_1=...
94 [0.0331859562592513;0.0285589439023825;0.0225065331772370;...
95 0.0189468223940387;0.0158403087605802;0.0131311169034887;...
96 0.0122527914619488;0.0124686038531358;0.0121007596222725;...
97 0.01399411574444537;0.0168024120917713;0.0202655564151916;...
98 0.0245968486909978;0.0291105237603469;0.0348275369759939;...
99 0.0415565640185381;0.0491966039352059;0.0596374268695133;...
100 0.0712235463740903;0.0783859677428014;0.0880240892437888;...
101 0.0983355252004903;0.108101954523449;0.118749897647422;...
102 0.128576970063239;0.140223144052195;0.152845063683076;...
103 0.165098099722719;0.178263738604623;0.190669762413875;...
104 0.200917116172463;0.213283639422009;0.230302422336980;...
105 0.251856410673102;0.265348318598858;0.280169649171469;...
106 0.293079995746426;0.306468524342820;0.316087744265308;...
107 0.331153701240424;0.339352993468659;0.343805149187245;...
108 0.357367274638073;0.365487071651346;0.371746744842184;...
109 0.378965080879246;0.387348160309275;0.396148794017582;...
110 0.400919634435716;0.410355844881111;0.418992542285874;...
111 0.429377784632715;0.432161428908286;0.445358004857721;...

```

```

112 0.449511061662298;0.454432235165533;0.466615637205070;...
113 0.473488130419345;0.473825618553497;0.483262801297828;...
114 0.490134615871489;0.495193519187196;0.506592291154017];
115 CL_BLF_1=...
116 [-0.354173691100548,-0.309063999932849,-0.259899691306692,...
117 -0.201576490582196,-0.140228135605584,-0.0784330946201286,...
118 -0.0228956859968763,0.0306396081385506,0.0818251136500848,...
119 0.134125047245865,0.190880848861979,0.249375733204867,...
120 0.306594385654906,0.357250871754507,0.405853817460111,...
121 0.455048376575644,0.503867637134175,0.552607044125295,...
122 0.596166557862589,0.617511770875898,0.642365030513726,...
123 0.663583807519691,0.685775470178208,0.710600796703577,...
124 0.730284120516020,0.750511830740319,0.773647392520254,...
125 0.791158054932682,0.811773620986288,0.811217504491707,...
126 0.810796219594365,0.796534564440700,0.829074572567749,...
127 0.871414723998235,0.866595878432624,0.870649689280734,...
128 0.869767400527153,0.872958391535774,0.867711724905650,...
129 0.875307331477488,0.864330969244883,0.837270800264997,...
130 0.851219132828200,0.848402048276708,0.833399307819857,...
131 0.824406222320952,0.825560420849990,0.821339590367901,...
132 0.811456051420846,0.816016858774003,0.814771168240697,...
133 0.817599478203143,0.803887629919240,0.814774241132624,...
134 0.802847471376179,0.792555675655018,0.796901461921134,...
135 0.790083394307436,0.769385076296350,0.766250555705866,...
136 0.760289976252899,0.754334128100513,0.754700161457019]';
137 CM_BLF_1=...
138 [-0.00645565729432271;-0.00543366737074639;-0.00497230375830425;...
139 -0.00626840903527524;-0.00812639164827980;-0.00967798053293440;...
140 -0.00945309222782101;-0.00865038220961338;-0.00670502210461011;...
141 -0.00488751112138329;-0.00454480696604581;-0.00481732423437155;...
142 -0.00548800757156123;-0.00442664971617944;-0.00282825806744191;...
143 -0.00138620542503159;-0.000204421890390911;...
144 0.000817753587349030;0.00130240859034837;0.00109615288671430;
145 0.000464851194557061;-0.00149193626706634;-0.00380972808029311;...
146 -0.00533306500332433;-0.00620595983241655;-0.00759321564382312;...
147 -0.00870105692850148;-0.0108249745414312;-0.0129892457825265;...
148 -0.00516853422314401;-0.000189350755310846;-0.00462159855872107;...
149 -0.0191437591914945;-0.0261932152732147;-0.0251904959472022;...
150 -0.0378876638882588;-0.0478485428343769;-0.0499899927653833;...
151 -0.0545965073248441;-0.0540169594750646;-0.0642403701311685;...
152 -0.0678397210048976;-0.0669126861227226;-0.0711347448349583;...
153 -0.0673556117123620;-0.0649522888342130;-0.0668780318358190;...
154 -0.0603695865129550;-0.0637109281367164;-0.0621148519578112;...

```

```

155 -0.0619758111857658;-0.0662567712765227;-0.0668173655521368;...
156 -0.0655033106457927;-0.0660623006320958;-0.0655506777401585;...
157 -0.0645042350127906;-0.0634239194747829;-0.0619745103601840;...
158 -0.0628071667857057;-0.0612590184216668;-0.0608586271989955;...
159 -0.0620809601781004]+0.01;
160
161 Alpha_Slot_200_JD=alpha+...
162 [-8.13930569650318;-7.12694507515062;-6.02140811853273;...
163 -5.00170105594408;-3.98198111516462;-2.87036265170578;...
164 -1.84851324989122;-0.829147376904798;0.278405572171361;...
165 0.830926257583539;1.29568572893127;1.84718260035369;...
166 2.40197787987524;2.86990616314340;3.42386719604621;...
167 3.89045100146877;4.44232258507587;5.45367108933443;...
168 6.55597231268537;7.56639951144478;8.66928705589410;...
169 9.68113243597496;10.6947912580051;11.7961467191067;...
170 12.8093111578703;13.8364110334608;14.9500955001699;...
171 15.9579723471582;16.9664225058238;18.0282886988279;...
172 19.0036122250817;20.0556137860657;21.0148460077832;...
173 21.9702533986755;22.9384955211547;23.9902030711724;...
174 24.9551128961650;25.9233516796538;26.9910982455396;...
175 27.9409309963523;28.9897676706375;29.9562597573613;...
176 30.8989470972295;31.9683622607734;32.9188182156738];...
177 CD_Slot_200_JD=...
178 [0.0249842840892673;0.0195604134915005;0.0143834216638...
179 751;0.0108549143990608;0.00816881835012328;0.004879311...
180 46539239;0.00395781966804512;0.00365483992792561;0.004...
181 28241322482735;0.00474407790921938;0.0057582558648709...
182 8;0.00645273970293498;0.00751031094048318;0.0094122348...
183 9896528;0.0110575635340329;0.0132817317745282;0.015133...
184 5148856012;0.0188803112856184;0.0240003722774144;0.029...
185 4918706354342;0.0366716976789302;0.0443669347927839;0...
186 0532532582951283;0.0695916787031502;0.088008587337434...
187 5;0.108464773625040;0.136824436503663;0.16582820991150...
188 7;0.192436036579450;0.223461254556216;0.25112573246278...
189 7;0.280867767929434;0.301227165976154;0.32037888054629...
190 5;0.341135419249444;0.360932278333196;0.37833276340675...
191 3;0.395976505144352;0.419017614622716;0.43261089695018...
192 3;0.450796231404737;0.466349160853958;0.47795232912708...
193 8;0.500123088459546;0.510802744409361];
194 CL_Slot_200_JD=...
195 [-0.338646961351646,-0.292659862392328,-0.2411828826456...
196 14,-0.188464920242479,-0.134672726701926,-0.07674586574...
197 51916,-0.0206952235870607,0.0327214552553833,0.0852759...
198 690471117,0.111281942933680,0.136480593829496,0.161400...
199 738366892,0.188758512195716,0.217317919068340,0.244851...
200 486437686,0.271984976572820,0.297302530690163,0.341155...
201 632833166,0.389200881638037,0.433137445034258,0.481804...
202 530093597,0.527245178134752,0.573548540644765,0.620590...
203 739659397,0.667430345563330,0.729049497802401,0.789167...
204 505771261,0.829338662373363,0.871178430668242,0.876339...
205 382985236,0.883045943420430,0.877744734569981,0.866324...
206 720972384,0.851908768417901,0.851104984074884,0.845491...
207 955167970,0.841154026490747,0.839286128027530,0.850683...
208 644332506,0.830355379707657,0.821697577864173,0.819037...

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209 753064181,0.790070686515306,0.803237872240048,0.783570...
210 560967676]';
211 CM_Slot_200_JD=...
212 [-0.00834979338577161;-0.00715681206848110;-0.0065466537...
213 4145752;-0.00688203234423188;-0.00779458060051240;-0.009...
214 27762017151896;-0.00966528705279758;-0.0095679478086160...
215 9;-0.00825205444560790;-0.00753024158239537;-0.006931591...
216 21437764;-0.00624167419865799;-0.00627780524635620;-0.00...
217 677685305657774;-0.00714047929698264;-0.00719647138574...
218 427;-0.00666526788181024;-0.00520675806074079;-0.0033756...
219 8081036960;-0.00182896399677014;-0.000752203860571932;...
220 -8.69837691748233e
    -05;0.000220931046794505;-0.00394263893098121;-0.01545796...

221 10548854;-0.0286247777470567;-0.0421161886578441;-0.0526...
222 581066968622;-0.0622903713117134;-0.0649164366029284;-0...
223 0679676602655533;-0.0710301613427541;-0.073605044751386...
224 5;-0.0757827756531143;-0.0801753059813129;-0.08113066871...
225 99231;-0.0827144357251951;-0.0846946079541785;-0.0854294...
226 231628424;-0.0841215861740769;-0.0841665989358836;-0.084...
227 2169756662313;-0.0831993253281970;-0.0831674320221782;...
228 -0.0852008474669002];
229
230 Alpha_Slot_400_JD=alpha+...
231 [-8.14107995734776;-7.12810380397329;-6.02294002587198;...
232 -5.00100829505852;-3.98065584668460;-2.87139441735438;...
233 -1.84952770602303;-0.829170803599483;0.280451313638561;...
234 0.832112928356729;1.29695570220239;1.84800350937919;...
235 2.40181187810453;2.86816341968855;3.42161042868440;...
236 3.88872287648642;4.43966731528486;5.45162906889796;...
237 6.55437032751475;7.56363601108004;8.66657245565575;...
238 9.67845705484742;10.6909516992006;11.7958743891732;...
239 12.8114141249747;13.8346778549107;14.9378776008161;...
240 15.9387749238412;16.9346122624383;18.0179820522858;...
241 18.9964023200859;20.0620812411592;21.0303959822269;...
242 22.0041179249296;22.9715615402812;24.0260517121405;...
243 24.9988278640787;25.9736340670725;27.0422333311487;...
244 27.9946973069450;29.0418733935211;29.9959334967865;...
245 30.9671914337833;32.0001766548288;32.9663708286242];...
246 CD_Slot_400_JD=...
247 [0.00569768908582134;0.000653616631782971;-0.0040173...
248 3492747906;-0.00742990193772587;-0.0102174497790087;...
249 -0.0133023270693763;-0.0142207914583933;-0.014594291...
250 7647373;-0.0142093229799219;-0.0138959193545874;-0.01...
251 26582858300000;-0.0117907234379582;-0.01058897412493...
252 04;-0.00846719539239434;-0.00710909653460416;-0.00465...
253 318894119242;-0.00296639088322539;0.001052522621462...
254 43;0.00651350808441484;0.0117933998076995;0.01891820...
255 08004069;0.0261482628131217;0.0342962335695831;0.043...
256 8656700474776;0.0552077756509481;0.0693740477420460;...
257 0.105172507392724;0.139528921009682;0.1679357319248...
258 90;0.199834155989705;0.226344669145139;0.25453057310...
259 9369;0.277085828367057;0.300568277707328;0.322077310...
260 429307;0.346829752414292;0.367124558895408;0.3862760...
261 86830406;0.412179568299533;0.427395948086337;0.44643...
262 3916573160;0.462425886927703;0.482117157303679;0.493...
263 772336860829;0.513431234800692];
264 CL_Slot_400_JD=...

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265 [-0.340528694281068,-0.293888778754073,-0.242807582020...
266 513,-0.187730196836646,-0.133267182896577,-0.077840128...
267 4080720,-0.0217711282459079,0.0326966095383901,0.08744...
268 56269616597,0.112540493770281,0.137827493036031,0.162...
269 271372214259,0.188582455220084,0.215469612627635,0.242...
270 458020182855,0.270152174087562,0.294486423567305,0.338...
271 989921342888,0.387501859615882,0.430206551500381,0.478...
272 925498707463,0.524407741473837,0.569476408715038,0.620...
273 301913918239,0.669660695436623,0.727211335640237,0.776...
274 209533096261,0.808978395884902,0.837441349306045,0.865...
275 408433204394,0.875399313732268,0.884603942028837,0.882...
276 816602113635,0.887824566473365,0.886173907128255,0.883...
277 512051474941,0.887516935802066,0.892614264341189,0.904...
278 916129219707,0.887378470447064,0.876959494318545,0.861...
279 114645048685,0.862448778909116,0.836979355690106,0.834...
280 003572518458]';
281 CM_Slot_400_JD=...
282 [-0.00959850700301111;-0.00874982906994464;-0.007907456...
283 16336122;-0.00881500204053227;-0.00980820493121330;-0.0...
284 110651682189337;-0.0113239431035566;-0.011840219262665...
285 1;-0.0108308275197412;-0.0103000706859604;-0.0095246466...
286 1322938;-0.00857190190790365;-0.00834770619569028;-0.00...
287 849964062857796;-0.00863106772547918;-0.00879291315863...
288 069;-0.00837630719200007;-0.00694002271937745;-0.005296...
289 62406811701;-0.00331477093293976;-0.00212958191237636;...
290 -0.00145238375830875;-0.000726417246053755;-0.00025042...
291 8208528577;-0.00158101230521345;-0.0119384093858803;-0...
292 .0278569646668860;-0.0391783362526073;-0.0469237967756...
293 573;-0.0566692689865733;-0.0616690489485235;-0.06525804...
294 91857559;-0.0682765276124359;-0.0731923881907869;-0.075...
295 6053897214873;-0.0829084605615219;-0.0854438243424612;...
296 -0.0882944149254450;-0.0890506385715564;-0.08978128770...
297 85074;-0.0915346082694105;-0.0921384186320555;-0.092891...
298 1886500812;-0.0935403064400923;-0.0928891979397311];...
299
300 Alpha_Slot_600_JD=alpha+...
301 [-8.15250305008806;-7.13851290714992;-6.03051364430308;...
302 -5.01117589838906;-3.99037918445528;-2.87932753037828;...
303 -1.85626236599775;-0.834814878555532;0.274142141001341;...
304 0.826066351573143;1.29116820600337;1.84275410005435;...
305 2.39770025991947;2.86382014537051;3.41749994600344;...
306 3.88381537566056;4.43571125667504;5.44782988317605;...
307 6.55176145418855;7.56357115087161;8.66644528646187;...
308 9.67834967266616;10.6916630962418;11.7982876029726;...
309 12.8131855970119;13.8340664829350;14.9467350593083;...
310 15.9674637590202;16.9845101257540;18.0875632637920;...
311 19.0966204643189;20.1633774635334;21.1396071845055;...
312 22.1110566367845;23.0677525891127;24.1201163602511;...
313 25.0488677017462;25.9941081509589;27.0518668176482;...
314 28.0270018230895;29.0770736345079;30.0501514516892;...
315 31.0001085712215;32.0467826847915;33.0096335195687];...
316 CD_Slot_600_JD=...
317 [-0.0130658913688246;-0.0180842416071628;-0.022456305...
318 0802255;-0.0257976158492426;-0.0287702976700154;-0.03...
319 20076226532163;-0.0324107936394564;-0.03261643771122...
320 30;-0.0319837811121743;-0.0315085156292136;-0.0299661...
321 090276477;-0.0291775542254593;-0.0280246271852704;-0...
322 0256038813179883;-0.0238580183687156;-0.021228450678...

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323 7270; -0.0191196323640248; -0.0149694630879372; -0.009078...
324 06619669437; -0.00304101045471653; 0.00383001613165229...
325 ; 0.0113398715173390; 0.0197058169479430; 0.030249908478...
326 1012; 0.0403212498678895; 0.0524337189708148; 0.06698199...
327 27082439; 0.0825577218736728; 0.103000268644405; 0.13377...
328 6722358127; 0.185679142766743; 0.238490168158967; 0.2693...
329 60459893327; 0.299375454581163; 0.324196829528256; 0.351...
330 115142779436; 0.367985743075838; 0.376515906340747; 0.39...
331 9577001851152; 0.422730003720431; 0.444102434599543; 0.4...
332 65101086216071; 0.483472381511884; 0.501379222405195; ...
333 0.518553198817997];
334 CL_Slot_600_JD=...
335 [-0.352643716618924, -0.304928391262603, -0.250839956313...
336 286, -0.198513681158485, -0.143579491215208, -0.086253772...
337 9155831, -0.0289137259544743, 0.0267106567212663, 0.08075...
338 42895829787, 0.106127658431716, 0.131689431538560, 0.156...
339 703991061284, 0.184221784490254, 0.210863253686253, 0.23...
340 8098553737877, 0.264947411815210, 0.290290735103814, 0.3...
341 34960608009534, 0.384734959325207, 0.430137762522489, 0...
342 478790626509576, 0.524293854844864, 0.570230897122041, 0...
343 .622861303021514, 0.671539470632569, 0.726562931104796, 0...
344 .785603513336904, 0.839404996363596, 0.890361669785317, 0...
345 .939204378913497, 0.981687959342012, 0.992035968075043, 0...
346 .998643041172583, 1.00124086382455, 0.988191524579992, 0...
347 983274465995295, 0.940587830428161, 0.914328522403276, 0...
348 915133143717022, 0.921639764091660, 0.914291915191565, 0...
349 918616737493617, 0.897359802082030, 0.886408446997923, 0...
350 879886809143175]';
351 CM_Slot_600_JD=...
352 [-0.00723738933360987; -0.00620776301636090; -0.00619294...
353 458505423; -0.00651444951696916; -0.00743876910006222; -0...
354 .00861584790279979; -0.00966118845439566; -0.0105746532...
355 004899; -0.00980569395259948; -0.00916198942512294; -0.00...
356 848389612122977; -0.00782406485606092; -0.0076584206531...
357 9508; -0.00782905371730899; -0.00814129622862258; -0.0082...
358 4703629731736; -0.00807708135388103; -0.006707450540029...
359 11; -0.00524683155342631; -0.00386734839632959; -0.002368...
360 46368680112; -0.00158201749017828; -0.00111774076086887...
361 ; -0.000634937187145405; -0.00138717124650150; -0.0105812...
362 981760175; -0.0222199752206172; -0.0342678895374102; -0.0...
363 456083761608960; -0.0577344485022751; -0.06970409688556...
364 46; -0.0754547156471550; -0.0791776508059520; -0.08150487...
365 85559114; -0.0829557505717916; -0.0847154169596503; -0.08...
366 23035973940487; -0.0858402438505193; -0.084752948869612...
367 3; -0.0857334788596333; -0.0837092498012970; -0.085689331...
368 5450340; -0.0917963917474111; -0.0940930991685665; -0.097...
369 4335038708480];
370
371 Alpha_Slot_800_JD=alpha+...
372 [-8.16532994130786; -7.15071579092200; -6.04244860884083; ...
373 -5.02099510922208; -4.00074350475546; -2.89013300970893; ...
374 -1.86673672339860; -0.845557601359153; 0.262744376454180; ...
375 0.815668234712962; 1.28098830005780; 1.83392968241970; ...
376 2.38963009158842; 2.85600354947695; 3.41124262157922; ...
377 3.87728372488066; 4.42928798070192; 5.44207749788951; ...
378 6.54701850023257; 7.55851760590759; 8.66181167361823; ...
379 9.67231113504006; 10.6858135558792; 11.7945702669411; ...
380 12.8095448979892; 13.8303756931133; 14.9434105377481; ...

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381 15.9616233762802;16.9770125159476;18.0751112575024;...
382 19.0870816918115;20.1944651800602;21.2080328942639;...
383 22.1973387095223;23.1762140686440;24.2493579805815;...
384 25.2214289083073;26.1923382924692;27.2178579547376;...
385 28.1285669372076;29.1882477121527;30.1384264568971;...
386 31.0873604704253;32.0796152955456;33.0318609966642];...
387 CD_Slot_800_JD=...
388 [-0.00681050693390072;-0.0126543294087441;-0.0182495...
389 693770797;-0.0214166231427484;-0.0251674028323114;-0...
390 .0284813491243448;-0.0295284521703782;-0.0300352983...
391 439126;-0.0297999387101721;-0.0295720385414848;-0.02...
392 82132488021699;-0.0273310852132612;-0.026210383664...
393 1072;-0.0240278454672732;-0.0220435932508557;-0.0190...
394 684670650371;-0.0168993698727356;-0.01216566243845...
395 81;-0.00643704479454368;-0.000469991253904901;0.0068...
396 1634235048144;0.0143941708545328;0.022555795883598...
397 0;0.0335793770283875;0.0439463538650867;0.0560009143...
398 510980;0.0702808537518199;0.0848501778814416;0.10300...
399 2466782877;0.128061227791715;0.152144243602451;0.182...
400 336909797974;0.215148357201335;0.275067267157616;0.3...
401 20558261523750;0.362479685381631;0.396531037918776;...
402 0.429234176477427;0.457465813635064;0.4677768042418...
403 04;0.494369876697358;0.510196123102673;0.52428205263...
404 3874;0.518416110561748;0.533085621458722];
405 CL_Slot_800_JD=...
406 [-0.366247569549657,-0.317870438818895,-0.2634978559...
407 96289,-0.208927669846718,-0.154571608219602,-0.09771...
408 37712223667,-0.0400225453233562,0.0153172162849387,...
409 0.0686661296398034,0.0950996977124353,0.1208928993...
410 96894,0.147345053057996,0.175662782841257,0.2025731...
411 84086938,0.231462205167657,0.258020120152550,0.2834...
412 78382821840,0.328859784193542,0.379704711000120,0.4...
413 24778109798272,0.473876342402648,0.517889545618680...
414 ,0.564027033267523,0.618918797249851,0.667678243993...
415 874,0.722648579523156,0.782077615939359,0.833210844...
416 835199,0.882409908178346,0.925998118771882,0.971571...
417 395935769,1.02500675704765,1.07121349306802,1.09274...
418 928998711,1.10322282802753,1.12034462316562,1.12360...
419 156582039,1.12456603399776,1.09117884162421,1.02935...
420 696942839,1.03220012662585,1.01223881378076,0.98989...
421 6799890378,0.921229823462180,0.903460668486540]';
422 CM_Slot_800_JD=...
423 [-0.00271428206765456;-0.00189706750827400;-0.001585...
424 10093408801;-0.00257006623435670;-0.003639827594117...
425 15;-0.00377285117644621;-0.00528002084311486;-0.0060...
426 4783914821188;-0.00542639016919631;-0.0048547859236...
427 7664;-0.00467522918668672;-0.00464200994639661;-0.00...
428 484881943788308;-0.00517612644732052;-0.00576129489...
429 607823;-0.00558567933442236;-0.00544667475420462;-0...
430 00388856835124193;-0.00257735756993069;-0.001209129...
431 76751777;0.000188843218942158;0.00126966991609235;0...
432 .00194730019213918;0.00226867902786383;0.0020075243...
433 3835763;-0.00655633847238418;-0.0191938207372223;-0.0...
434 288876484116350;-0.0402225780133489;-0.0509736602055...
435 526;-0.0593875338193712;-0.0673592849128238;-0.074871...
436 3020188131;-0.0814793195538752;-0.0864569567583774;-0...
437 .0922018627535162;-0.0947708467128809;-0.09736442547...
438 76938;-0.0959300891773638;-0.0898902740886361;-0.0917...

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439 042960490281;-0.0905853919434668;-0.089976876926054...
440 0;-0.0848269056017114;-0.0859492228960141];
441
442 Alpha_Slot_1000_JD=alpha+...
443 [-8.19296176515518;-7.17933574587292;-6.07141593961330;...
444 -5.05068766637736;-4.01478390175705;-2.90376884270189;...
445 -1.88070289398938;-0.858610138673839;0.251892829170128;...
446 0.805045079373169;1.27096880298182;1.82550033419823;...
447 2.29328670403366;2.84752853218911;3.40257829519855;...
448 3.86968238230243;4.42287620882581;5.43862308343971;...
449 6.54573182715474;7.55713986284914;8.66098722550410;...
450 9.67236449623901;10.6852903591628;11.7936837267243;...
451 12.8112788281600;13.8329825727792;14.9471087553110;1...
452 5.9664578225023;16.9791398538928;18.0817616704432;...
453 19.0886948118036;20.1847033352771;21.2029090750168;...
454 22.2183661266420;23.2279674798223;24.3299915044846;...
455 25.3283955867359;26.3157875287581;27.3957186622302;...
456 28.3760532549829;29.4314555943111;30.3576518649962;...
457 31.2810950601421;32.2836331725416;33.2135410784349];
458 CD_Slot_1000_JD=...
459 [-0.0193797893655357;-0.0259114877416335;-0.03258667...
460 37823424;-0.0372877316448054;-0.0409895595179842;-0.0...
461 451211540031038;-0.0465323825799716;-0.046985848615...
462 9102;-0.0470235007266426;-0.0471019968699758;-0.04558...
463 46122476344;-0.0447892744155420;-0.0432186377043500;...
464 -0.0416831615990399;-0.0400375162366334;-0.037384285...
465 6392081;-0.0350786936687696;-0.0303777956122959;-0.02...
466 17416728583107;-0.0157560312384841;-0.00811648099009...
467 559;-0.000582397437687672;0.00780414749527014;0.0186...
468 951181907445;0.0294869235072628;0.0417640755961384;...
469 0.0566192455906378;0.0718139381421382;0.08864026042...
470 94024;0.109696609944029;0.131368096438492;0.15524846...
471 0024663;0.184343329546123;0.215847194077492;0.248784...
472 760521435;0.293162365698196;0.352499161384842;0.4063...
473 87379826736;0.458282454622353;0.500207681789809;0.54...
474 2355888075449;0.570273045623037;0.586548858269573;...
475 0.595084080898688;0.601632791661711];
476 CL_Slot_1000_JD=...
477 [-0.395553132478767,-0.348223986795931,-0.29421982134...
478 7971,-0.240418790630072,-0.169462472469212,-0.1121755...
479 65857211,-0.0548346870548746,0.00147404922605309,0.05...
480 71572729111181,0.0838330672852779,0.110266492551626,...
481 0.138405114959061,0.166814012293967,0.19358481061487...
482 2,0.222273055606256,0.249958342381286,0.2766782314731...
483 33,0.325196125920342,0.378340100431535,0.423316912878...
484 281,0.473001955093872,0.517946139059006,0.56347214502...
485 0504,0.617978556741035,0.669517203304557,0.7254133653...
486 91840,0.785999845181785,0.838338127376218,0.884666105...
487 104343,0.933051366361309,0.973282227247636,1.01465360...
488 923606,1.06577930934517,1.11505039826875,1.1581110922...
489 4280,1.20586235163683,1.23704752376115,1.255492945757...
490 42,1.27981308396896,1.29183424562026,1.29013981004425...
491 1.24474333567583,1.19536645118314,1.13760565033506,1.0...
492 9614563559966]';
493 CM_Slot_1000_JD=...
494 [0.00507017714348937;0.00614418826676139;0.006842971...
495 85030537;0.00699513112022954;0.00437741572681731;0.0...
496 0282945856269266;0.00113340818135327;0.000333189608...

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497 933874;0.000586231571137447;0.000924799225952278;0.0...
498 00824185731205280;0.000767407000762050;0.0003493200...
499 57341334;-0.000162324801487116;-0.00074296932765326...
500 5;-0.00125212658580521;-0.00147376228469160;-0.001264...
501 98499510802;0.00179972763032268;0.00314076315957652...
502 ;0.00435342405830659;0.00526227344420236;0.006221210...
503 03062758;0.00675959969365219;0.00639421820758831;-0....
504 00220469951161398;-0.0136034339227159;-0.0230183035...
505 253696;-0.0325897625335028;-0.0410750732024380;-0.046...
506 7011262564439;-0.0522773449139122;-0.05960919917759...
507 88;-0.0671714951745267;-0.0740194214401699;-0.0823273...
508 039146220;-0.0909191500060944;-0.0970089485628756;...
509 -0.103913781913880;-0.108509186502984;-0.11207993050...
510 2852;-0.109408392847778;-0.105477991507032;-0.101058...
511 260651483;-0.0975542197429547];
512
513 %% Import Kestrel Data
514
515 [SW1_M1] = importdata('SW1/OptimizationData/M1_Run1_forces.dat
516 ',',',',23);
517 [SW1_M2] = importdata('SW1/OptimizationData/M2_forces.dat',', '
518 ',23);
519 [SW1_M3] = importdata('SW1/OptimizationData/M3_forces.dat',', '
520 ',23);
521 [SW1_M4] = importdata('SW1/OptimizationData/M4_forces.dat',', '
522 ',23);
523 [SW1_M5] = importdata('SW1/OptimizationData/M5_forces.dat',', '
524 ',23);
525
526 [SW2_M1] = importdata('SW2/OptimizationData/M1_forces.dat',', '
527 ',23);
528 [SW2_M2] = importdata('SW2/OptimizationData/M2_forces.dat',', '
529 ',23);
530 [SW2_M3] = importdata('SW2/OptimizationData/M3_forces.dat',', '
531 ',23);
532 [SW2_M4] = importdata('SW2/OptimizationData/M4_forces.dat',', '
533 ',23);
534 [SW2_M5] = importdata('SW2/OptimizationData/M5_forces.dat',', '
535 ',23);
536
537 [SW3_M1] = importdata('SW3/OptimizationData/M1_forces.dat',', '
538 ',23);
539 [SW3_M2] = importdata('SW3/OptimizationData/M2_forces.dat',', '
540 ',23);
541 [SW3_M3] = importdata('SW3/OptimizationData/M3_forces.dat',', '
542 ',23);
543 [SW3_M4] = importdata('SW3/OptimizationData/M4_forces.dat',', '
544 ',23);
545 [SW3_M5] = importdata('SW3/OptimizationData/M5_forces.dat',', '
546 ',23);
547
548 [SW4_M1] = importdata('SW4/OptimizationData/M1_forces.dat',', '
549 ',23);
550 [SW4_M2] = importdata('SW4/OptimizationData/M2_forces.dat',', '
551 ',23);
552 [SW4_M3] = importdata('SW4/OptimizationData/M3_forces.dat',', '
553 ',23);
554 [SW4_M4] = importdata('SW4/OptimizationData/M4_forces.dat',', '
555 ',23);
556

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```

    ,23);
537 [SW4_M5] = importdata('SW4/OptimizationData/M5_forces.dat',' ',
    ,23);
538
539 [SW5_M1] = importdata('SW5/OptimizationData/M1_forces.dat',' ',
    ,23);
540 [SW5_M2] = importdata('SW5/OptimizationData/M2_forces.dat',' ',
    ,23);
541 [SW5_M3] = importdata('SW5/OptimizationData/M3_forces.dat',' ',
    ,23);
542 [SW5_M4] = importdata('SW5/OptimizationData/M4_forces.dat',' ',
    ,23);
543 [SW5_M5] = importdata('SW5/OptimizationData/M5_forces.dat',' ',
    ,23);
544
545 SW_M = {SW1_M1, SW1_M2, SW1_M3, SW1_M4, SW1_M5, SW2_M1, SW2_M2,
    SW2_M3, SW2_M4, SW2_M5, SW3_M1, SW3_M2, SW3_M3, SW3_M4,
    SW3_M5, SW4_M1, SW4_M2, SW4_M3, SW4_M4, SW4_M5, SW5_M1,
    SW5_M2, SW5_M3, SW5_M4, SW5_M5};
546
547 %% Axial Forces
548 Iter = 1000; %Number of iterations to average over
549 k = 0;
550 for i = 1:length(SW_M)
551     I = SW_M{i};
552     k=k+1;
553     fx_I = mean(I.data((([length(I.data)-Iter:end]),33))); %
        Time Avg at 33
554     fx(:,k) = fx_I;
555 end
556 fx_3_check = mean(SW1_M3.data((([length(SW1_M3.data)-Iter:end]),
    ,33)));
557
558 %% Vertical Forces
559 k = 0;
560 for j = 1:length(SW_M)
561     J = SW_M{j};
562     k=k+1;
563     fy_J = mean(J.data((([length(J.data)-Iter:end]),34))); %
        Time Avg at 34
564     fy(:,k) = fy_J;
565 end
566 fy_3_Check = mean(SW1_M3.data((([length(SW1_M3.data)-Iter:end]),
    ,34)));
567
568 %% Moment about the z-axis
569 x_cor = -1.28; % Correction for incorrect location of Moment
    Reference point in CFD Settings
570 k = 0;
571 for e = 1:length(SW_M)
572     E = SW_M{e};
573     k=k+1;
574     Mz_E = mean(E.data((([length(E.data)-Iter:end]),38)))/x_cor;
        % Time Avg at 38
575     Mz(:,k) = Mz_E;
576 end
577 Mz_3_Check = mean(SW1_M3.data((([length(SW1_M3.data)-Iter:end]
    ),38)))/x_cor;

```

```

578
579 %% Lift
580 AoA = 24;
581 k = 0;
582 for p = 1:length(SW_M)
583     FX_L = fx(p);
584     FY_L = fy(p);
585     k=k+1;
586     L_P = FY_L*cosd(AoA)-FX_L*sind(AoA);
587     L(:,k) = L_P;
588 end
589 L_3_Check = fy(:,3)*cosd(AoA)+fx(:,3)*sind(AoA);
590
591 %% Drag
592 k = 0;
593 for q = 1:length(SW_M)
594     FX_D = fx(q);
595     FY_D = fy(q);
596     k=k+1;
597     D_P = FX_D*cosd(AoA)+FY_D*sind(AoA);
598     D(:,k) = D_P;
599 end
600 D_3_Check = fx(:,3)*cosd(AoA)+fy(:,3)*sind(AoA);
601
602 %% Pitching Moment
603 x_cm = 1.3; % in - Estimated distance from Aero Center
604 MomRef_L = 1; % in - NA
605 % PM_0 = (Mz_0/MomRef_L)-(L_0*cosd(0)*x_cm)+(D_0*-sind(0)*
        x_cm);
606 k = 0;
607 for z = 1:length(SW_M)
608     L_PM = L(z);
609     D_PM = D(z);
610     Mz_PM = Mz(z);
611     k=k+1;
612     PM_Z = (Mz_PM/MomRef_L)-(L_PM*cosd(AoA)*x_cm)+(D_PM*-sind(
        AoA)*x_cm);
613     PM(:,k) = PM_Z;
614 end
615 PM_3_Check = (Mz(:,3)/MomRef_L)-(L(:,3)*cosd(AoA)*x_cm)+(D
        (:,3)*-sind(AoA)*x_cm);
616
617 %% Coeffiecient of Lift
618 k = 0;
619 for v = 1:length(SW_M)
620     L_CL = L(v);
621     k=k+1;
622     CL_V = (L_CL*2)/(0.67764*0.0009518*((3751.5/12)^2));
623     CL(:,k) = CL_V;
624 end
625 CL_3_Check = (L(:,3)*2)/(0.67764*0.0009518*((3751.5/12)^2));
626
627 %% Coeffiecient of Drag
628 % CD_0 =(D_0*2)/(0.67764*0.0009518*((3751.5/12)^2));
629 k = 0;
630 for w = 1:length(SW_M)
631     D_CD = D(w);
632     k=k+1;

```

```

633     CD_W = (D_CD*2)/(0.67764*0.0009518*((3751.5/12)^2));
634     CD(:,k) = CD_W;
635 end
636 CD_3_Check = (D(:,3)*2)/(0.67764*0.0009518*((3751.5/12)^2));
637
638 %% Moment Coeffiecient
639 c_bar = 9.66;
640 % CM_0 =(PM_0*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
641 k = 0;
642 for x = 1:length(SW_M)
643     PM_CM = PM(x);
644     k=k+1;
645     CM_X = (PM_CM*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar)
646     CM(:,k) = CM_X;
647 end
648 CM_3_Check =(PM(:,3)*2)/(0.67764*0.0009518*((3751.5/12)^2)*
    c_bar);
649
650 %% Momentum Cefficient (C_mu) and Blowing Ratio (BR)
    Calcualtion
651 V_inf = 3751.5; % in/s
652 C_mu = [0.49, 1.95, 4.4, 7.82, 12.22, 0.392, 1.56, 3.52,
    6.256, 9.776, 0.294, 1.17, 2.64, 4.692, 7.332, 0.196, 0.78,
    1.76, 3.128, 4.888, 0.098, 0.39, 0.88, 1.564, 2.444];
653 V_slot = [3643.67, 7268.72, 10918.61, 14556.07, 18196.02];
654
655 BR = V_slot/V_inf;
656
657 %% Percent Gain/Reduction CL/CD/CM
658 CL_Base_24AoA = 0.8021; % <--CFD, WT =0.8021
659 CD_Base_24AoA = 0.3503; % <--CFD, WT =0.3478
660 CM_Base_24AoA = -0.03129; % <--CFD, WT =-0.028291
661
662 CL_BLF_24AoA = 0.8505; %WT
663 CD_BLF_24AoA = 0.3567; %WT
664 CM_BLF_24AoA = -0.06696; %WT
665
666 CL_AFC_WT = [0.8508, 0.8861, 0.98912, 1.10134, 1.14839,]; % 24
    AoA Wind tunnel values in order of Cmu (M1, M2, M3, M4, M5)
667 CD_AFC_WT = [0.3423, 0.32275, 0.32244, 0.31237, 0.24135,]; %
    24AoA Wind tunnel values in order of Cmu (M1, M2, M3, M4,
    M5)
668 CM_AFC_WT = [-0.08023, -0.0758, -0.08285, -0.08556,
    -0.07247,]; % 24AoA Wind tunnel values in order of Cmu (M1,
    M2, M3, M4, M5)
669
670 CL_Combine = [CL, CL_Base_24AoA, CL_BLF_24AoA, CL_AFC_WT];
671 CD_Combine = [CD, CD_Base_24AoA, CD_BLF_24AoA, CD_AFC_WT];
672 CM_Combine = [CM, CM_Base_24AoA, CM_BLF_24AoA, CM_AFC_WT];
673
674 CL_PerGain = 100*((CL_Combine-CL_Base_24AoA)/abs(CL_Base_24AoA
    ));
675
676 CD_PerRed = 100*((CD_Combine-CD_Base_24AoA)/abs(CD_Base_24AoA)
    );
677
678 CM_PerRed = 100*((CM_Combine-CM_Base_24AoA)/abs(CM_Base_24AoA)

```

```

    );
679
680 %% CD, CL, CM vs Alpha Plots
681 % figure()
682 % hold on
683 % plot(Alpha_Baseline2,CD_Base2, 'k--*', 'LineWidth',0.9)
684 % plot(Alpha_BLF_1,CD_BLF_1,'--p','Color', [0.25 0.80 0.54],
    'LineWidth',0.9)
685 % plot(Alpha_Slot_200_JD,CD_Slot_200_JD, 'r--v', 'LineWidth
    ',0.9)
686 % plot(Alpha_Slot_400_JD,CD_Slot_400_JD, 'g--^', 'LineWidth
    ',0.9)
687 % plot(Alpha_Slot_600_JD,CD_Slot_600_JD, 'b-->', 'LineWidth
    ',0.9)
688 % plot(Alpha_Slot_800_JD,CD_Slot_800_JD, 'm--<', 'LineWidth
    ',0.9)
689 % plot(Alpha_Slot_1000_JD,CD_Slot_1000_JD, '--s', 'LineWidth
    ',0.9)
690 % plot(AoA,CD(:,1),'ro',AoA,CD(:,2),'go',AoA,CD(:,3),'bo',AoA,
    CD(:,4),'mo',AoA,CD(:,5),'o','LineWidth',0.9)
691 % grid on
692 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
    assigned is Orange (M5)
693 % xlim([23 25])
694 % xlabel('\alpha (deg)')
695 % ylabel('Uncorrected C_D (-)')
696 % hold off
697 % %title('Coefficient of Drag at 45 mph')
698 % legend('Baseline Model','BLF Model','Slot Model, C\mu
    =0.49%', 'Slot Model, C\mu=1.95%', 'Slot Model, C\mu=4.40%',
    'Slot Model, C\mu=7.82%', 'Slot Model, C\mu=12.22%', 'SW1 M1
    ', 'SW1 M2', 'SW1 M3', 'SW1 M4', 'SW1 M5', 'Location', 'best')
699 % %legend('Windtunnel Basic Model','Fence Model','Slot Model,
    600 SLPM%')
700 % %legend('Windtunnel Basic Model','CFD Basic Model','Location
    ', 'best')
701 %
702 % figure()
703 % hold on
704 % plot(Alpha_Baseline2,CL_Base2, 'k--*', 'LineWidth',0.9)
705 % plot(Alpha_BLF_1,CL_BLF_1,'--p','Color', [0.25 0.80 0.54],
    'LineWidth',0.9)
706 % plot(Alpha_Slot_200_JD,CL_Slot_200_JD, 'r--v', 'LineWidth
    ',0.9)
707 % plot(Alpha_Slot_400_JD,CL_Slot_400_JD, 'g--^', 'LineWidth
    ',0.9)
708 % plot(Alpha_Slot_600_JD,CL_Slot_600_JD, 'b-->', 'LineWidth
    ',0.9)
709 % plot(Alpha_Slot_800_JD,CL_Slot_800_JD, 'm--<', 'LineWidth
    ',0.9)
710 % plot(Alpha_Slot_1000_JD,CL_Slot_1000_JD, '--s','LineWidth
    ',0.9)
711 % plot(AoA,CL(:,1),'ro',AoA,CL(:,2),'go',AoA,CL(:,3),'bo',AoA,
    CL(:,4),'mo',AoA,CL(:,5),'o','LineWidth',0.9)
712 % grid on
713 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
    assigned is Orange (M5)
714 % xlim([23 25])

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```

715 % xlabel('\alpha (deg)')
716 % ylabel('Uncorrected C_L (-)')
717 % hold off
718 % legend('Baseline Model','Fence Model','Slot Model, C\mu
      =0.49%', 'Slot Model, C\mu=1.95%', 'Slot Model, C\mu=4.40%',
      'Slot Model, C\mu=7.82%', 'Slot Model, C\mu=12.22%', 'SW1 M1
      ', 'SW1 M2', 'SW1 M3', 'SW1 M4', 'SW1 M5', 'Location', 'best')
719 % %title('Coefficient of Lift at 45 mph')
720 % %legend('Windtunnel Basic Model','CFD Basic Model','Location
      ', 'best')
721 %
722 % figure()
723 % hold on
724 % plot(Alpha_Baseline2,CM_Base2, 'k--*', 'LineWidth',0.9)
725 % plot(Alpha_BLF_1,CM_BLF_1,'--p','Color',[0.25 0.80 0.54], '
      LineWidth',0.9)
726 % plot(Alpha_Slot_200_JD,CM_Slot_200_JD, 'r--v', 'LineWidth
      ',0.9)
727 % plot(Alpha_Slot_400_JD,CM_Slot_400_JD, 'g--^', 'LineWidth
      ',0.9)
728 % plot(Alpha_Slot_600_JD,CM_Slot_600_JD, 'b-->', 'LineWidth
      ',0.9)
729 % plot(Alpha_Slot_800_JD,CM_Slot_800_JD, 'm--<', 'LineWidth
      ',0.9)
730 % plot(Alpha_Slot_1000_JD,CM_Slot_1000_JD, '--s', 'LineWidth
      ',0.9)
731 % plot(AoA,CM(:,1),'ro',AoA,CM(:,2),'go',AoA,CM(:,3),'bo',AoA,
      CM(:,4),'mo',AoA,CM(:,5),'o','LineWidth',0.9)
732 % grid on
733 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
      assigned is Orange (M5)
734 % xlim([23 25])
735 % xlabel('\alpha (deg)')
736 % ylabel('Uncorrected C_M (-)')
737 % hold off
738 % legend('Baseline Model','Fence Model','Slot Model, C\mu
      =0.49%', 'Slot Model, C\mu=1.95%', 'Slot Model, C\mu=4.40%',
      'Slot Model, C\mu=7.82%', 'Slot Model, C\mu=12.22%', 'SW1 M1
      ', 'SW1 M2', 'SW1 M3', 'SW1 M4', 'SW1 M5', 'Location', 'best')
739 % %title('Pitch Moment Coefficient at 45 mph')
740 % %The coefficient curves are superimposed, providng evidence
      that the data is good
741
742 %% Same Plots as above w/different markers
743 % figure()
744 % hold on
745 % plot(Alpha_Baseline2,CD_Base2, 'k:.', 'LineWidth',1.5)
746 % plot(Alpha_BLF_1,CD_BLF_1,':.','Color',[0.25 0.80 0.54], '
      LineWidth',1.5)
747 % plot(Alpha_Slot_200_JD,CD_Slot_200_JD, 'r:.', 'LineWidth
      ',1.5)
748 % plot(Alpha_Slot_400_JD,CD_Slot_400_JD, 'g:.', 'LineWidth
      ',1.5)
749 % plot(Alpha_Slot_600_JD,CD_Slot_600_JD, 'b:.', 'LineWidth
      ',1.5)
750 % plot(Alpha_Slot_800_JD,CD_Slot_800_JD, 'm:.', 'LineWidth
      ',1.5)
751 % plot(Alpha_Slot_1000_JD,CD_Slot_1000_JD, ':.','LineWidth

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    ',1.5)
752 % plot(AoA,CD(:,1),'ro',AoA,CD(:,2),'go',AoA,CD(:,3),'bo',AoA,
    CD(:,4),'mo',AoA,CD(:,5),'o','LineWidth',1.1)
753 % grid on
754 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
    assigned is Orange (M5)
755 % xlim([23 26.5])
756 % ylim([0.23 0.39])
757 % xlabel('\alpha (deg)')
758 % ylabel('C_D (-)')
759 % hold off
760 % %title('Coefficient of Drag at 45 mph')
761 % legend('Baseline WT','BLF WT','AFC WT, C\mu=0.49%', 'AFC WT,
    C\mu=1.95%', 'AFC WT, C\mu=4.40%', 'AFC WT, C\mu=7.82%', 'AFC
    WT, C\mu=12.22%', 'AFC CFD, C\mu=0.49%', 'AFC CFD, C\mu
    =1.95%', 'AFC CFD, C\mu=4.40%', 'AFC CFD, C\mu=7.82%', 'AFC
    CFD, C\mu=12.22%', 'Location','east')
762 % %legend('Windtunnel Basic Model','Fence Model','Slot Model,
    600 SLPM%')
763 % %legend('Windtunnel Basic Model','CFD Basic Model','Location
    ','best')
764 %
765 % figure()
766 % hold on
767 % plot(Alpha_Baseline2,CL_Base2, 'k:.', 'LineWidth',1.5)
768 % plot(Alpha_BLF_1,CL_BLF_1,':.','Color', [0.25 0.80 0.54], '
    LineWidth',1.5)
769 % plot(Alpha_Slot_200_JD,CL_Slot_200_JD, 'r:.', 'LineWidth
    ',1.5)
770 % plot(Alpha_Slot_400_JD,CL_Slot_400_JD, 'g:.', 'LineWidth
    ',1.5)
771 % plot(Alpha_Slot_600_JD,CL_Slot_600_JD, 'b:.', 'LineWidth
    ',1.5)
772 % plot(Alpha_Slot_800_JD,CL_Slot_800_JD, 'm:.', 'LineWidth
    ',1.5)
773 % plot(Alpha_Slot_1000_JD,CL_Slot_1000_JD, ':.','LineWidth
    ',1.5)
774 % plot(AoA,CL(:,1),'ro',AoA,CL(:,2),'go',AoA,CL(:,3),'bo',AoA,
    CL(:,4),'mo',AoA,CL(:,5),'o','LineWidth',1.1)
775 % grid on
776 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
    assigned is Orange (M5)
777 % xlim([23 26.5])
778 % xlabel('\alpha (deg)')
779 % ylabel('C_L (-)')
780 % hold off
781 % legend('Baseline WT','BLF WT','AFC WT, C\mu=0.49%', 'AFC WT,
    C\mu=1.95%', 'AFC WT, C\mu=4.40%', 'AFC WT, C\mu=7.82%', 'AFC
    WT, C\mu=12.22%', 'AFC CFD, C\mu=0.49%', 'AFC CFD, C\mu
    =1.95%', 'AFC CFD, C\mu=4.40%', 'AFC CFD, C\mu=7.82%', 'AFC
    CFD, C\mu=12.22%', 'Location','east')
782 % %title('Coefficient of Lift at 45 mph')
783 % %legend('Windtunnel Basic Model','CFD Basic Model','Location
    ','best')
784 %
785 % figure()
786 % hold on
787 % plot(Alpha_Baseline2,CM_Base2, 'k:.', 'LineWidth',1.5)

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788 % plot(Alpha_BLF_1,CM_BLF_1,':','Color',[0.25 0.80 0.54], '
      LineWidth',1.5)
789 % plot(Alpha_Slot_200_JD,CM_Slot_200_JD, 'r:', 'LineWidth
      ',1.5)
790 % plot(Alpha_Slot_400_JD,CM_Slot_400_JD, 'g:', 'LineWidth
      ',1.5)
791 % plot(Alpha_Slot_600_JD,CM_Slot_600_JD, 'b:', 'LineWidth
      ',1.5)
792 % plot(Alpha_Slot_800_JD,CM_Slot_800_JD, 'm:', 'LineWidth
      ',1.5)
793 % plot(Alpha_Slot_1000_JD,CM_Slot_1000_JD,':','LineWidth
      ',1.5)
794 % plot(AoA,CM(:,1),'ro',AoA,CM(:,2),'go',AoA,CM(:,3),'bo',AoA,
      CM(:,4),'mo',AoA,CM(:,5),'o','LineWidth',1.1)
795 % grid on
796 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
      assigned is Orange (M5)
797 % xlim([23 26.5])
798 % xlabel('\alpha (deg)')
799 % ylabel('C_M (-)')
800 % hold off
801 % legend('Baseline WT','BLF WT','AFC WT, C\mu=0.49%', 'AFC WT,
      C\mu=1.95%', 'AFC WT, C\mu=4.40%', 'AFC WT, C\mu=7.82%', 'AFC
      WT, C\mu=12.22%', 'AFC CFD, C\mu=0.49%', 'AFC CFD, C\mu
      =1.95%', 'AFC CFD, C\mu=4.40%', 'AFC CFD, C\mu=7.82%', 'AFC
      CFD, C\mu=12.22%', 'Location','east')
802 % %title('Pitch Moment Coefficient at 45 mph')
803 % %The coefficient curves are superimposed, providng evidence
      that the data is good
804
805 %% Slot Comparison All CL,CD,CM
806 % figure ()
807 % hold on
808 % yline(CL_Base_24AoA, '--k')
809 % plot(AoA,CL(:,1),'ro',AoA,CL(:,2),'go',AoA,CL(:,3),'bo',AoA,
      CL(:,4),'mo',AoA,CL(:,5),'o','LineWidth',0.9) % SW1 - M1,M2
      ,M3,M4,M5
810 % plot(AoA,CL(:,6),'rv',AoA,CL(:,7),'gv',AoA,CL(:,8),'bv',AoA,
      CL(:,9),'mv',AoA,CL(:,10),'v','LineWidth',0.9) % SW2 - M1,
      M2,M3,M4,M5
811 % plot(AoA,CL(:,11),'r^',AoA,CL(:,12),'g^',AoA,CL(:,13),'b^',
      AoA,CL(:,14),'m^',AoA,CL(:,15),'^','LineWidth',0.9) % SW3 -
      M1,M2,M3,M4,M5
812 % plot(AoA,CL(:,16),'rs',AoA,CL(:,17),'gs',AoA,CL(:,18),'bs',
      AoA,CL(:,19),'ms',AoA,CL(:,20),'s','LineWidth',0.9) % SW4 -
      M1,M2,M3,M4,M5
813 % plot(AoA,CL(:,21),'rd',AoA,CL(:,22),'gd',AoA,CL(:,23),'bd',
      AoA,CL(:,24),'md',AoA,CL(:,25),'d','LineWidth',0.9) % SW5 -
      M1,M2,M3,M4,M5
814 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
      assigned is Orange (M5)
815 % grid on
816 % legend('Baseline','SW1 M1','SW1 M2','SW1 M3','SW1 M4','SW1
      M5','SW2 M1','SW2 M2','SW2 M3','SW2 M4','SW2 M5','SW3 M1',
      'SW3 M2','SW3 M3','SW3 M4','SW3 M5','SW4 M1','SW4 M2','SW4
      M3','SW4 M4','SW4 M5','SW5 M1','SW5 M2','SW5 M3','SW5 M4',
      'SW5 M5','Location','best')
817 % xlabel('\alpha (deg)')

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818 % ylabel('C_{L Uncorrected} (-)')
819 % hold off
820 %
821 % figure ()
822 % hold on
823 % yline(CD_Base_24AoA, '--k')
824 % plot(AoA,CD(:,1),'ro',AoA,CD(:,2),'go',AoA,CD(:,3),'bo',AoA,
      CD(:,4),'mo',AoA,CD(:,5),'o','LineWidth',0.9) % SW1 - M1,M2
      ,M3,M4,M5
825 % plot(AoA,CD(:,6),'rv',AoA,CD(:,7),'gv',AoA,CD(:,8),'bv',AoA,
      CD(:,9),'mv',AoA,CD(:,10),'v','LineWidth',0.9) % SW2 - M1,
      M2,M3,M4,M5
826 % plot(AoA,CD(:,11),'r^',AoA,CD(:,12),'g^',AoA,CD(:,13),'b^',
      AoA,CD(:,14),'m^',AoA,CD(:,15),'^','LineWidth',0.9) % SW3 -
      M1,M2,M3,M4,M5
827 % plot(AoA,CD(:,16),'rs',AoA,CD(:,17),'gs',AoA,CD(:,18),'bs',
      AoA,CD(:,19),'ms',AoA,CD(:,20),'s','LineWidth',0.9) % SW4 -
      M1,M2,M3,M4,M5
828 % plot(AoA,CD(:,21),'rd',AoA,CD(:,22),'gd',AoA,CD(:,23),'bd',
      AoA,CD(:,24),'md',AoA,CD(:,25),'d','LineWidth',0.9) % SW5 -
      M1,M2,M3,M4,M5
829 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
      assigned is Orange (M5)
830 % grid on
831 % legend('Baseline','SW1 M1','SW1 M2','SW1 M3','SW1 M4','SW1
      M5','SW2 M1','SW2 M2','SW2 M3','SW2 M4','SW2 M5','SW3 M1',
      'SW3 M2','SW3 M3','SW3 M4','SW3 M5','SW4 M1','SW4 M2','SW4
      M3','SW4 M4','SW4 M5','SW5 M1','SW5 M2','SW5 M3','SW5 M4',
      'SW5 M5','Location','best')
832 % xlabel('\alpha (deg)')
833 % ylabel('C_{D Uncorrected} (-)')
834 % hold off
835 %
836 % figure ()
837 % hold on
838 % yline(CM_Base_24AoA, '--k')
839 % plot(AoA,CM(:,1),'ro',AoA,CM(:,2),'go',AoA,CM(:,3),'bo',AoA,
      CM(:,4),'mo',AoA,CM(:,5),'o','LineWidth',0.9) % SW1 - M1,M2
      ,M3,M4,M5
840 % plot(AoA,CM(:,6),'rv',AoA,CM(:,7),'gv',AoA,CM(:,8),'bv',AoA,
      CM(:,9),'mv',AoA,CM(:,10),'v','LineWidth',0.9) % SW2 - M1,
      M2,M3,M4,M5
841 % plot(AoA,CM(:,11),'r^',AoA,CM(:,12),'g^',AoA,CM(:,13),'b^',
      AoA,CM(:,14),'m^',AoA,CM(:,15),'^','LineWidth',0.9) % SW3 -
      M1,M2,M3,M4,M5
842 % plot(AoA,CM(:,16),'rs',AoA,CM(:,17),'gs',AoA,CM(:,18),'bs',
      AoA,CM(:,19),'ms',AoA,CM(:,20),'s','LineWidth',0.9) % SW4 -
      M1,M2,M3,M4,M5
843 % plot(AoA,CM(:,21),'rd',AoA,CM(:,22),'gd',AoA,CM(:,23),'bd',
      AoA,CM(:,24),'md',AoA,CM(:,25),'d','LineWidth',0.9) % SW5 -
      M1,M2,M3,M4,M5
844 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
      assigned is Orange (M5)
845 % grid on
846 % legend('Baseline','SW1 M1','SW1 M2','SW1 M3','SW1 M4','SW1
      M5','SW2 M1','SW2 M2','SW2 M3','SW2 M4','SW2 M5','SW3 M1',
      'SW3 M2','SW3 M3','SW3 M4','SW3 M5','SW4 M1','SW4 M2','SW4
      M3','SW4 M4','SW4 M5','SW5 M1','SW5 M2','SW5 M3','SW5 M4',

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        SW5 M5','Location','best')
847 % xlabel('\alpha (deg)')
848 % ylabel('C_{M Uncorrected} (-) (-)')
849 % hold off
850
851 %% Compare each Mach at each slot widths
852 % figure ()
853 % hold on
854 % subplot(1,5,1)
855 % yline(CL_Base_24AoA, '--k')
856 % plot(AoA,CL(:,1),'ro',AoA,CL(:,6),'r+',AoA,CL(:,11),'r*',AoA
      ,CL(:,16),'rs',AoA,CL(:,21),'rd','LineWidth',0.9)
857 % legend('Baseline','SW1 M1','SW2 M1','SW3 M1','SW4 M1','SW5
      M1','Location','northoutside')
858 % xlim([23 25])
859 % ylim([min(CL)-0.02 max(CL)+0.02])
860 % ylabel('Coeffiecient of Lift')
861 %
862 % subplot(1,5,2)
863 % yline(CL_Base_24AoA, '--k')
864 % plot(AoA,CL(:,2),'go',AoA,CL(:,7),'g+',AoA,CL(:,12),'g*',AoA
      ,CL(:,17),'gs',AoA,CL(:,22),'gd','LineWidth',0.9)
865 % legend('Baseline','SW1 M2','SW2 M2','SW3 M2','SW4 M2','SW5
      M2','Location','northoutside')
866 % xlim([23 25])
867 % ylim([min(CL)-0.02 max(CL)+0.02])
868 %
869 % subplot(1,5,3)
870 % yline(CL_Base_24AoA, '--k')
871 % plot(AoA,CL(:,3),'bo',AoA,CL(:,8),'b+',AoA,CL(:,13),'b*',AoA
      ,CL(:,18),'bs',AoA,CL(:,23),'bd','LineWidth',0.9)
872 % legend('Baseline','SW1 M3','SW2 M3','SW3 M3','SW4 M3','SW5
      M3','Location','northoutside')
873 % xlim([23 25])
874 % ylim([min(CL)-0.02 max(CL)+0.02])
875 % xlabel('Angle of Attack (deg)')
876 %
877 %
878 % subplot(1,5,4)
879 % yline(CL_Base_24AoA, '--k')
880 % plot(AoA,CL(:,4),'mo',AoA,CL(:,9),'m+',AoA,CL(:,14),'m*',AoA
      ,CL(:,19),'ms',AoA,CL(:,24),'md','LineWidth',0.9)
881 % legend('Baseline','SW1 M4','SW2 M4','SW3 M4','SW4 M4','SW5
      M4','Location','northoutside')
882 % xlim([23 25])
883 % ylim([min(CL)-0.02 max(CL)+0.02])
884 %
885 % subplot(1,5,5)
886 % yline(CL_Base_24AoA, '--k')
887 % plot(AoA,CL(:,5),'o',AoA,CL(:,10),'+',AoA,CL(:,15),'*',AoA,
      CL(:,20),'s',AoA,CL(:,25),'d','LineWidth',0.9,'Color
     ',[0.9290 0.6940 0.1250])
888 % legend('Baseline','SW1 M5','SW2 M5','SW3 M5','SW4 M5','SW5
      M5','Location','northoutside')
889 % xlim([23 25])
890 % ylim([min(CL)-0.02 max(CL)+0.02])
891 % hold off
892

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```

893 %% CL/CD/CM vs Cmu - Individual Points
894 % figure ()
895 % hold on
896 % yline(CL_Base_24AoA, '--k')
897 % plot(C_mu(:,1),CL(:,1),'ro',C_mu(:,2),CL(:,2),'go',C_mu(:,3),
      CL(:,3),'bo',C_mu(:,4),CL(:,4),'mo',C_mu(:,5),CL(:,5),'o',
      'LineWidth',0.9)
898 % plot(C_mu(:,6),CL(:,6),'r+',C_mu(:,7),CL(:,7),'g+',C_mu(:,8),
      CL(:,8),'b+',C_mu(:,9),CL(:,9),'m+',C_mu(:,10),CL(:,10),
      '+','LineWidth',0.9)
899 % plot(C_mu(:,11),CL(:,11),'r*',C_mu(:,12),CL(:,12),'g*',C_mu
      (:,13),CL(:,13),'b*',C_mu(:,14),CL(:,14),'m*',C_mu(:,15),CL
      (:,15),'*', 'LineWidth',0.9)
900 % plot(C_mu(:,16),CL(:,16),'rs',C_mu(:,17),CL(:,17),'gs',C_mu
      (:,18),CL(:,18),'bs',C_mu(:,19),CL(:,19),'ms',C_mu(:,20),CL
      (:,20),'s','LineWidth',0.9)
901 % plot(C_mu(:,21),CL(:,21),'rd',C_mu(:,22),CL(:,22),'gd',C_mu
      (:,23),CL(:,23),'bd',C_mu(:,24),CL(:,24),'md',C_mu(:,25),CL
      (:,25),'d','LineWidth',0.9)
902 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
      assigned is Orange (M5)
903 % legend({'Baseline','SW1 M1','SW1 M2','SW1 M3','SW1 M4','SW1
      M5','SW2 M1','SW2 M2','SW2 M3','SW2 M4','SW2 M5','SW3 M1','
      SW3 M2','SW3 M3','SW3 M4','SW3 M5','SW4 M1','SW4 M2','SW4
      M3','SW4 M4','SW4 M5','SW5 M1','SW5 M2','SW5 M3','SW5 M4','
      SW5 M5'},'Location','southeast')
904 % ylabel('Coeffiecient of Lift')
905 % xlabel('Momentum Coefficient')
906 % hold off
907
908 %% CL/CD/CM vs Cmu - Lines of Constant Slot Width
909 % figure ()
910 % hold on
911 % yline(CL_Base_24AoA, '--k')
912 % plot(C_mu(:,[1 2 4 5]),CL(:,[1 2 4 5]),'r','LineWidth',0.9)
913 % plot(C_mu(:,[6 8 9 10]),CL(:,[6 8 9 10]),'g','LineWidth
      ',0.9)
914 % plot(C_mu(:,[11 12 14 15]),CL(:,[11 12 14 15]),'b','
      LineWidth',0.9)
915 % plot(C_mu(:,[16 17 18 19 20]),CL(:,[16 17 18 19 20]),'m','
      LineWidth',0.9)
916 % plot(C_mu(:,[21 22 24 25]),CL(:,[21 22 24 25]),'LineWidth
      ',0.9,'Color',[0.9290 0.6940 0.1250])
917 % % plot(fit(C_mu(:,[1 2 3 4 5]),CL(:,[1 2 3 4 5])),',
      smoothingspline','SmoothingParam',[0.1]),'r--') %
      smoothingspline
918 % % plot(fit(C_mu(:,[6 7 8 9 10]),CL(:,[6 7 8 9 10])),',
      smoothingspline','SmoothingParam',[0.5]),'g--')
919 % % plot(fit(C_mu(:,[11 12 13 14 15]),CL(:,[11 12 13 14 15])
      ),',smoothingspline','SmoothingParam',[0.5]),'b--')
920 % % plot(fit(C_mu(:,[16 17 18 19 20]),CL(:,[16 17 18 19 20])
      ),',smoothingspline','SmoothingParam',[0.5]),'m--')
921 % % plot(fit(C_mu(:,[21 22 24 25]),CL(:,[21 22 24 25])),',
      smoothingspline','SmoothingParam',[0.5]),'--')
922 % ylim([min(CL)-0.01 max(CL)+0.02])
923 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
      assigned is Orange (M5)
924 % legend('Baseline','24^o \alpha: SW1','24^o \alpha SW2','24^o

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        \alpha SW3','24^o \alpha SW4','24^o \alpha SW5','SW1 Fit
        ','SW2 Fit','SW3 Fit','SW4 Fit','SW5 Fit','Location','
        southeast')
925 % ylabel('Coeffiecient of Lift')
926 % xlabel('Momentum Coefficient')
927 % hold off
928 %
929 % figure ()
930 % hold on
931 % yline(CD_Base_24AoA, '--k')
932 % plot(C_mu(:,[1 2 4 5]),CD(:,[1 2 4 5]),'r','LineWidth',0.9)
933 % plot(C_mu(:,[6 8 9 10]),CD(:,[6 8 9 10]),'g','LineWidth
        ',0.9)
934 % plot(C_mu(:,[11 12 14 15]),CD(:,[11 12 14 15]),'b','
        LineWidth',0.9)
935 % plot(C_mu(:,[16 17 18 19 20]),CD(:,[16 17 18 19 20]),'m','
        LineWidth',0.9)
936 % plot(C_mu(:,[21 22 24 25]),CD(:,[21 22 24 25]),'LineWidth
        ',0.9,'Color',[0.9290 0.6940 0.1250])
937 % legend('Baseline','24^o \alpha: SW1','24^o \alpha SW2','24^o
        \alpha SW3','24^o \alpha SW4','24^o \alpha SW5','SW1 Fit
        ','SW2 Fit','SW3 Fit','SW4 Fit','SW5 Fit','Location','
        southeast')
938 % ylabel('Coeffiecient of Drag')
939 % xlabel('Momentum Coefficient')
940 % hold off
941 %
942 % figure ()
943 % hold on
944 % yline(CM_Base_24AoA, '--k')
945 % plot(C_mu(:,[1 2 4 5]),CM(:,[1 2 4 5]),'r','LineWidth',0.9)
946 % plot(C_mu(:,[6 8 9 10]),CM(:,[6 8 9 10]),'g','LineWidth
        ',0.9)
947 % plot(C_mu(:,[11 12 14 15]),CM(:,[11 12 14 15]),'b','
        LineWidth',0.9)
948 % plot(C_mu(:,[16 17 18 19 20]),CM(:,[16 17 18 19 20]),'m','
        LineWidth',0.9)
949 % plot(C_mu(:,[21 22 24 25]),CM(:,[21 22 24 25]),'LineWidth
        ',0.9,'Color',[0.9290 0.6940 0.1250])
950 % legend('Baseline','24^o \alpha: SW1','24^o \alpha SW2','24^o
        \alpha SW3','24^o \alpha SW4','24^o \alpha SW5','SW1 Fit
        ','SW2 Fit','SW3 Fit','SW4 Fit','SW5 Fit','Location','
        southeast')
951 % ylabel('Pitching Moment Coeffiecient')
952 % xlabel('Momentum Coefficient')
953 % hold off
954
955
956 %% CL/CD/CM vs BR - Lines of Constant Slot Width
957 %
958 % figure ()
959 % hold on
960 % yline(CL_Base_24AoA, '--k')
961 % plot(BR(:,[1 2 4 5]),CL(:,[1 2 4 5]),'r','LineWidth',0.9)
962 % plot(BR(:,[1 3 4 5]),CL(:,[6 8 9 10]),'g','LineWidth',0.9)
963 % plot(BR(:,[1 2 4 5]),CL(:,[11 12 14 15]),'b','LineWidth
        ',0.9)
964 % plot(BR(:,[1 2 3 4 5]),CL(:,[16 17 18 19 20]),'m','LineWidth

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    ',0.9)
965 % plot(BR(:,[1 2 4 5]),CL(:,[21 22 24 25]),'LineWidth',0.9,'
    Color',[0.9290 0.6940 0.1250])
966 % legend('Baseline','24^o \alpha: SW1','24^o \alpha SW2','24^o
    \alpha SW3','24^o \alpha SW4','24^o \alpha SW5','SW1 Fit
    ','SW2 Fit','SW3 Fit','SW4 Fit','SW5 Fit','Location','
    northwest')
967 % ylabel('Coeffiecient of Lift')
968 % xlabel('Blowing Ratio (V_{slot}/V_{\infty})')
969 % hold off
970 %
971 % figure ()
972 % hold on
973 % yline(CD_Base_24AoA, '--k')
974 % plot(BR(:,[1 2 4 5]),CD(:,[1 2 4 5]),'r','LineWidth',0.9)
975 % plot(BR(:,[1 3 4 5]),CD(:,[6 8 9 10]),'g','LineWidth',0.9)
976 % plot(BR(:,[1 2 4 5]),CD(:,[11 12 14 15]),'b','LineWidth
    ',0.9)
977 % plot(BR(:,[1 2 3 4 5]),CD(:,[16 17 18 19 20]),'m','LineWidth
    ',0.9)
978 % plot(BR(:,[1 2 4 5]),CD(:,[21 22 24 25]),'LineWidth',0.9,'
    Color',[0.9290 0.6940 0.1250])
979 % legend('Baseline','24^o \alpha: SW1','24^o \alpha SW2','24^o
    \alpha SW3','24^o \alpha SW4','24^o \alpha SW5','SW1 Fit
    ','SW2 Fit','SW3 Fit','SW4 Fit','SW5 Fit','Location','
    southeast')
980 % ylabel('Coeffiecient of Drag')
981 % xlabel('Blowing Ratio (V_{slot}/V_{\infty})')
982 % hold off
983 %
984 % figure ()
985 % hold on
986 % yline(CM_Base_24AoA, '--k')
987 % plot(BR(:,[1 2 4 5]),CM(:,[1 2 4 5]),'r','LineWidth',0.9)
988 % plot(BR(:,[1 3 4 5]),CM(:,[6 8 9 10]),'g','LineWidth',0.9)
989 % plot(BR(:,[1 2 4 5]),CM(:,[11 12 14 15]),'b','LineWidth
    ',0.9)
990 % plot(BR(:,[1 2 3 4 5]),CM(:,[16 17 18 19 20]),'m','LineWidth
    ',0.9)
991 % plot(BR(:,[1 2 4 5]),CM(:,[21 22 24 25]),'LineWidth',0.9,'
    Color',[0.9290 0.6940 0.1250])
992 % legend('Baseline','24^o \alpha: SW1','24^o \alpha SW2','24^o
    \alpha SW3','24^o \alpha SW4','24^o \alpha SW5','SW1 Fit
    ','SW2 Fit','SW3 Fit','SW4 Fit','SW5 Fit','Location','north
    ')
993 % ylabel('Pitching Moment Coeffiecient')
994 % xlabel('Blowing Ratio (V_{slot}/V_{\infty})')
995 % hold off
996
997 %% Cmu VS Percent Gain with lines of Constant Slot Width
998
999 figure ()
1000 hold on
1001 %plot(0,CL_PerGain(:,[26]),'ko','LineWidth',2)
1002 % plot(0,CL_PerGain(:,[27]),'ks','Color',[0.25 0.80 0.54],',
    LineWidth',1.7) % BLF WT Gains
1003 %plot(C_mu(:,[1 2 3 4 5]),CL_PerGain(:,[28 29 30 31 32]),'k--h
    ',',LineWidth',0.9) %AFC WT Percent Gains

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```

1004 plot(C_mu(:,[1 2 4 5]),CL_PerGain(:,[1 2 4 5]),'r--o',',
      LineWidth',0.9)
1005 plot(C_mu(:,[6 8 9 10]),CL_PerGain(:,[6 8 9 10]),'g--v',',
      LineWidth',0.9)
1006 plot(C_mu(:,[11 12 14 15]),CL_PerGain(:,[11 12 14 15]),'b--^',',
      LineWidth',0.9)
1007 plot(C_mu(:,[16 17 18 19 20]),CL_PerGain(:,[16 17 18 19 20]),',
      m--s',',LineWidth',0.9)
1008 plot(C_mu(:,[21 22 24 25]),CL_PerGain(:,[21 22 24 25]),'--d',',
      LineWidth',0.9,'Color',[0.9290 0.6940 0.1250])
1009 grid on
1010 %legend('24^o \alpha: Baseline CFD','24^o \alpha: BLF CFD
      ','24^o \alpha: AFC WT','24^o \alpha: AFC CFD SW1','24^o \
      alpha: AFC CFD SW2','24^o \alpha: AFC CFD SW3','24^o \alpha
      : AFC CFD SW4','24^o \alpha: AFC CFD SW5','Location','east
      ')
1011 legend('AFC CFD SW1(0.037in), \alpha = 24^o','AFC CFD SW2
      (0.0296in), \alpha = 24^o','AFC CFD SW3(0.0222in), \alpha =
      24^o','AFC CFD SW4(0.0148in), \alpha = 24^o','AFC CFD SW5
      (0.0074in), \alpha = 24^o','Location','southeast')
1012 ylabel('C_L (% Gain)')
1013 xlabel('C_\mu (%)')
1014 xlim([0 14])
1015 ylim([0 40])
1016 hold off
1017
1018 % figure ()
1019 % hold on
1020 % plot(0,CD_PerRed(:,[26]),'k*',',LineWidth',1.5)
1021 % plot(0,CD_PerRed(:,[27]),'p',',Color',[0.25 0.80 0.54],',
      LineWidth',0.9)
1022 % plot(C_mu(:,[1 2 3 4 5]),CD_PerRed(:,[28 29 30 31 32]),'k--h
      ',',LineWidth',0.9)
1023 % plot(C_mu(:,[1 2 4 5]),CD_PerRed(:,[1 2 4 5]),'r--o',',
      LineWidth',0.9)
1024 % plot(C_mu(:,[6 8 9 10]),CD_PerRed(:,[6 8 9 10]),'g--v',',
      LineWidth',0.9)
1025 % plot(C_mu(:,[11 12 14 15]),CD_PerRed(:,[11 12 14 15]),'b
      --^',',LineWidth',0.9)
1026 % plot(C_mu(:,[16 17 18 19 20]),CD_PerRed(:,[16 17 18 19 20])
      ',m--s',',LineWidth',0.9)
1027 % plot(C_mu(:,[21 22 24 25]),CD_PerRed(:,[21 22 24 25]),'--d
      ',',LineWidth',0.9,'Color',[0.9290 0.6940 0.1250])
1028 % grid on
1029 % legend('24^o \alpha: Baseline WT','24^o \alpha: BLF WT','24^
      o \alpha: AFC WT','24^o \alpha: AFC CFD SW1','24^o \alpha:
      AFC CFD SW2','24^o \alpha: AFC CFD SW3','24^o \alpha: AFC
      CFD SW4','24^o \alpha: AFC CFD SW5','Location','east')
1030 % ylabel('C_D (% Reduction)')
1031 % xlabel('C_\mu (%)')
1032 % xlim([0 19])
1033 % hold off
1034 %
1035 % figure ()
1036 % hold on
1037 % plot(0,CM_PerRed(:,[26]),'k*',',LineWidth',1.5)
1038 % plot(0,CM_PerRed(:,[27]),'p',',Color',[0.25 0.80 0.54],',
      LineWidth',0.9)

```

```

1039 % plot(C_mu(:,[1 2 3 4 5]),CM_PerRed(:,[28 29 30 31 32]),'k--h
      ', 'LineWidth',0.9)
1040 % plot(C_mu(:,[1 2 4 5]),CM_PerRed(:,[1 2 4 5]),'r--o', '
      LineWidth',0.9)
1041 % plot(C_mu(:,[6 8 9 10]),CM_PerRed(:,[6 8 9 10]),'g--v', '
      LineWidth',0.9)
1042 % plot(C_mu(:,[11 12 14 15]),CM_PerRed(:,[11 12 14 15]),'b
      --^', 'LineWidth',0.9)
1043 % plot(C_mu(:,[16 17 18 19 20]),CM_PerRed(:,[16 17 18 19 20])
      , 'm--s', 'LineWidth',0.9)
1044 % plot(C_mu(:,[21 22 24 25]),CM_PerRed(:,[21 22 24 25]),'--d
      ', 'LineWidth',0.9, 'Color',[0.9290 0.6940 0.1250])
1045 % grid on
1046 % legend('24^o \alpha: Baseline WT','24^o \alpha: BLF WT','24^
      o \alpha: AFC WT','24^o \alpha: AFC CFD SW1','24^o \alpha:
      AFC CFD SW2','24^o \alpha: AFC CFD SW3','24^o \alpha: AFC
      CFD SW4','24^o \alpha: AFC CFD SW5','Location','east')
1047 % ylabel('C_M (% Reduction)')
1048 % xlabel('C_\mu (%)')
1049 % xlim([0 19])
1050 % hold off

```

## Appendix H. MATLAB Script: AFC Slot Extent Optimization

```
1 %% AFC Slot Extent Optimization
2 clear all; close all; clc; format compact; format short;
3 %% Baseline, Passive BLF and AFC Slot, Freestream M = 0.059,
   SW1, M1-M5 Wind Tunnel Uncorrected Data
4 alpha = 1;
5 Alpha_Baseline2=alpha+...
6 [-8.17894442052277;-7.16850773849801;-6.15464379090849;...
7 -5.04877209800816;-4.02932120636633;-3.00640352702020;...
8 -1.98382443346184;-0.870213403716582;0.153319187693818;...
9 1.17508365277160;2.19900159794485;3.30928370940170;...
10 4.32751503348324;5.34186930698045;6.44211101586254;...
11 7.45523765217682;8.46819102061274;9.56920569459411;...
12 10.6678210098701;11.6756459136262;12.7671846976348;...
13 13.7663130389622;14.8512817871214;15.9311893169993;...
14 17.0110707277628;18.0844673115262;19.1538944819053;...
15 20.2221014158863;21.3721215112022;22.4257937648188;...
16 23.5698166553147;24.6991922407033;25.7472428560031;...
17 26.8830239002552;28.0967117595190;29.2310840568254;...
18 30.4510280084815;31.6729762552610;32.9017417048610;...
19 34.2275325071614;35.4596797612262;36.7847709966838];...
20 CD_Base2=...
21 [0.0326396226315288;0.0273554591561591;0.02320762912...
22 52264;0.0184655617641355;0.0156734227994947;0.013931...
23 8232188933;0.0127460003513771;0.0110429698239139;0.0...
24 115328779992575;0.0132684007837646;0.01594624739861...
25 14;0.0186260816468254;0.0227511043823911;0.027425377...
26 8944443;0.0325465190807324;0.0391042044857320;0.0473...
27 291339011119;0.0578153893612589;0.0714274594986400;0...
28 .0882968225391222;0.107396801468250;0.12837527862316...
29 1;0.152008514898266;0.177050724527485;0.203713593209...
30 787;0.230608840670329;0.257527050009981;0.2850390953...
31 55441;0.311662701851170;0.335885212499362;0.35962757...
32 0078000;0.378102215918811;0.393975988177553;0.4094634...
33 43267234;0.422979456980625;0.438129375146260;0.452553...
34 360061481;0.469150907399056;0.488570671603892;0.51410...
35 4483039872;0.536274210618872;0.565069415967284];
36 CL_Base2=...
37 [-0.380686716946657,-0.335679522978898,-0.28809803698...
38 6591,-0.235205472140068,-0.180638051940071,-0.1234544...
39 23606297,-0.0655693172981972,-0.00446862170388157,0.0...
40 533671656873325,0.110388299123664,0.169693355141534,...
41 0.227263490287654,0.279476897333351,0.32863898256204...
42 2,0.375560539057904,0.422360052709387,0.4700363760260...
43 67,0.517777718341523,0.561913793013043,0.604151005786...
44 968,0.641842476206843,0.673795777863523,0.70451924645...
45 7192,0.729874924214394,0.754142327869694,0.7725926727...
46 70825,0.786833165496932,0.798718935717348,0.805103685...
47 529550,0.802634940849533,0.801598645011175,0.78608838...
48 7524569,0.776596912840933,0.767880111293073,0.7484587...
49 51498765,0.737187298271561,0.724400980387816,0.713740...
50 363550526,0.709249314247855,0.715390882106700,0.71448...
51 6482896382,0.719886109135885]';
52 CM_Base2=...
53 [-0.00241933648422381;-0.000994749356042714;0.00052513...
```

```

54 8889181397;0.000531995120895268;-0.000127610521605613;...
55 -0.00112181497128817;-0.00238738588975404;-0.004014823...
56 77348298;-0.00458591893002119;-0.00447507033838957;-0.0...
57 0570421624022764;-0.00639759228464273;-0.006060593543...
58 11681;-0.00452373994614179;-0.00254238263866779;-0.000...
59 802608455539601;0.000686585846786974;0.0019224715481...
60 3012;0.00305034068341110;0.00384085470805589;0.0046514...
61 9185638424;0.00533251814807207;0.00492217834961218;0.0...
62 0390892393185356;0.00131507381415635;-0.0018753227054...
63 2222;-0.00563731602852632;-0.0109907490359497;-0.016914...
64 9235037892;-0.0248236615415000;-0.0317363120696212;-0.0...
65 393746528162185;-0.0435606742506112;-0.043896906122957...
66 7;-0.0457089065451211;-0.0471099572765705;-0.04925656335...
67 62850;-0.0525805261396649;-0.0556579516727002;-0.0595181...
68 996791140;-0.0641550435894548;-0.0701361258272115];
69
70
71 Alpha_BLF_1=alpha+...
72 [-8.06594564259070;-7.14241231732519;-6.03905594741620;...
73 -5.01406378048430;-3.98721923601549;-2.87195351727540;...
74 -1.85058803650554;-0.831110322743736;0.275151806711067;...
75 1.29346471552093;2.31597900276951;3.42813304789199;...
76 4.45108375100950;5.55684707512697;6.57167414343638;...
77 7.58705903612775;8.69009006482263;9.70504580065541;...
78 10.7161174843277;11.2642436005670;11.8166774071110;...
79 12.2766843085277;12.8266085308312;13.3790159996166;...
80 13.8375751427264;14.3856475805125;14.9354617926899;...
81 15.3929723623862;15.9414105042531;16.4688861494385;...
82 16.9094889255359;17.4240418013865;17.9837233404080;...
83 18.4646453036484;18.9881016785306;19.5209239626320;...
84 20.0480920643511;20.4921008071506;21.0161537952655;...
85 21.5513155912465;21.9819661259102;22.4844514540255;...
86 23.0266031504895;23.4649469590941;23.9788010755111;...
87 24.4993216153161;24.9404098936923;25.4654301290090;...
88 25.9851110721517;26.4294113964856;26.9572368515206;...
89 27.4879036272060;27.9159749086103;28.4552397489093;...
90 28.9719941570135;29.4032901602970;29.9353877441201;...
91 30.4579590792370;30.8794429116547;31.4044874140582;...
92 31.9278672633083;32.3622515736385;32.8915967016012];
93 CD_BLF_1=...
94 [0.0331859562592513;0.0285589439023825;0.0225065331772370;...
95 0.0189468223940387;0.0158403087605802;0.0131311169034887;...
96 0.0122527914619488;0.0124686038531358;0.0121007596222725;...
97 0.01399411574444537;0.0168024120917713;0.0202655564151916;...
98 0.0245968486909978;0.0291105237603469;0.0348275369759939;...
99 0.0415565640185381;0.0491966039352059;0.0596374268695133;...
100 0.0712235463740903;0.0783859677428014;0.0880240892437888;...
101 0.0983355252004903;0.108101954523449;0.118749897647422;...
102 0.128576970063239;0.140223144052195;0.152845063683076;...
103 0.165098099722719;0.178263738604623;0.190669762413875;...
104 0.200917116172463;0.213283639422009;0.230302422336980;...
105 0.251856410673102;0.265348318598858;0.280169649171469;...
106 0.293079995746426;0.306468524342820;0.316087744265308;...
107 0.331153701240424;0.339352993468659;0.343805149187245;...
108 0.357367274638073;0.365487071651346;0.371746744842184;...
109 0.378965080879246;0.387348160309275;0.396148794017582;...
110 0.400919634435716;0.410355844881111;0.418992542285874;...
111 0.429377784632715;0.432161428908286;0.445358004857721;...

```

```

112 0.449511061662298;0.454432235165533;0.466615637205070;...
113 0.473488130419345;0.473825618553497;0.483262801297828;...
114 0.490134615871489;0.495193519187196;0.506592291154017];
115 CL_BLF_1=...
116 [-0.354173691100548,-0.309063999932849,-0.259899691306692,...
117 -0.201576490582196,-0.140228135605584,-0.0784330946201286,...
118 -0.0228956859968763,0.0306396081385506,0.0818251136500848,...
119 0.134125047245865,0.190880848861979,0.249375733204867,...
120 0.306594385654906,0.357250871754507,0.405853817460111,...
121 0.455048376575644,0.503867637134175,0.552607044125295,...
122 0.596166557862589,0.617511770875898,0.642365030513726,...
123 0.663583807519691,0.685775470178208,0.710600796703577,...
124 0.730284120516020,0.750511830740319,0.773647392520254,...
125 0.791158054932682,0.811773620986288,0.811217504491707,...
126 0.810796219594365,0.796534564440700,0.829074572567749,...
127 0.871414723998235,0.866595878432624,0.870649689280734,...
128 0.869767400527153,0.872958391535774,0.867711724905650,...
129 0.875307331477488,0.864330969244883,0.837270800264997,...
130 0.851219132828200,0.848402048276708,0.833399307819857,...
131 0.824406222320952,0.825560420849990,0.821339590367901,...
132 0.811456051420846,0.816016858774003,0.814771168240697,...
133 0.817599478203143,0.803887629919240,0.814774241132624,...
134 0.802847471376179,0.792555675655018,0.796901461921134,...
135 0.790083394307436,0.769385076296350,0.766250555705866,...
136 0.760289976252899,0.754334128100513,0.754700161457019]';
137 CM_BLF_1=...
138 [-0.00645565729432271;-0.00543366737074639;-0.00497230375830425;...
139 -0.00626840903527524;-0.00812639164827980;-0.00967798053293440;...
140 -0.00945309222782101;-0.00865038220961338;-0.00670502210461011;...
141 -0.00488751112138329;-0.00454480696604581;-0.00481732423437155;...
142 -0.00548800757156123;-0.00442664971617944;-0.00282825806744191;...
143 -0.00138620542503159;-0.000204421890390911;...
144 0.000817753587349030;0.00130240859034837;0.00109615288671430;
145 0.000464851194557061;-0.00149193626706634;-0.00380972808029311;...
146 -0.00533306500332433;-0.00620595983241655;-0.00759321564382312;...
147 -0.00870105692850148;-0.0108249745414312;-0.0129892457825265;...
148 -0.00516853422314401;-0.000189350755310846;-0.00462159855872107;...
149 -0.0191437591914945;-0.0261932152732147;-0.0251904959472022;...
150 -0.0378876638882588;-0.0478485428343769;-0.0499899927653833;...
151 -0.0545965073248441;-0.0540169594750646;-0.0642403701311685;...
152 -0.0678397210048976;-0.0669126861227226;-0.0711347448349583;...
153 -0.0673556117123620;-0.0649522888342130;-0.0668780318358190;...
154 -0.0603695865129550;-0.0637109281367164;-0.0621148519578112;...

```

```

155 -0.0619758111857658;-0.0662567712765227;-0.0668173655521368;...
156 -0.0655033106457927;-0.0660623006320958;-0.0655506777401585;...
157 -0.0645042350127906;-0.0634239194747829;-0.0619745103601840;...
158 -0.0628071667857057;-0.0612590184216668;-0.0608586271989955;...
159 -0.0620809601781004]+0.01;
160
161 Alpha_Slot_200_JD=alpha+...
162 [-8.13930569650318;-7.12694507515062;-6.02140811853273;...
163 -5.00170105594408;-3.98198111516462;-2.87036265170578;...
164 -1.84851324989122;-0.829147376904798;0.278405572171361;...
165 0.830926257583539;1.29568572893127;1.84718260035369;...
166 2.40197787987524;2.86990616314340;3.42386719604621;...
167 3.89045100146877;4.44232258507587;5.45367108933443;...
168 6.55597231268537;7.56639951144478;8.66928705589410;...
169 9.68113243597496;10.6947912580051;11.7961467191067;...
170 12.8093111578703;13.8364110334608;14.9500955001699;...
171 15.9579723471582;16.9664225058238;18.0282886988279;...
172 19.0036122250817;20.0556137860657;21.0148460077832;...
173 21.9702533986755;22.9384955211547;23.9902030711724;...
174 24.9551128961650;25.9233516796538;26.9910982455396;...
175 27.9409309963523;28.9897676706375;29.9562597573613;...
176 30.8989470972295;31.9683622607734;32.9188182156738];...
177 CD_Slot_200_JD=...
178 [0.0249842840892673;0.0195604134915005;0.0143834216638...
179 751;0.0108549143990608;0.00816881835012328;0.004879311...
180 46539239;0.00395781966804512;0.00365483992792561;0.004...
181 28241322482735;0.00474407790921938;0.0057582558648709...
182 8;0.00645273970293498;0.00751031094048318;0.0094122348...
183 9896528;0.0110575635340329;0.0132817317745282;0.015133...
184 5148856012;0.0188803112856184;0.0240003722774144;0.029...
185 4918706354342;0.0366716976789302;0.0443669347927839;0...
186 0532532582951283;0.0695916787031502;0.088008587337434...
187 5;0.108464773625040;0.136824436503663;0.16582820991150...
188 7;0.192436036579450;0.223461254556216;0.25112573246278...
189 7;0.280867767929434;0.301227165976154;0.32037888054629...
190 5;0.341135419249444;0.360932278333196;0.37833276340675...
191 3;0.395976505144352;0.419017614622716;0.43261089695018...
192 3;0.450796231404737;0.466349160853958;0.47795232912708...
193 8;0.500123088459546;0.510802744409361];
194 CL_Slot_200_JD=...
195 [-0.338646961351646,-0.292659862392328,-0.2411828826456...
196 14,-0.188464920242479,-0.134672726701926,-0.07674586574...
197 51916,-0.0206952235870607,0.0327214552553833,0.0852759...
198 690471117,0.111281942933680,0.136480593829496,0.161400...
199 738366892,0.188758512195716,0.217317919068340,0.244851...
200 486437686,0.271984976572820,0.297302530690163,0.341155...
201 632833166,0.389200881638037,0.433137445034258,0.481804...
202 530093597,0.527245178134752,0.573548540644765,0.620590...
203 739659397,0.667430345563330,0.729049497802401,0.789167...
204 505771261,0.829338662373363,0.871178430668242,0.876339...
205 382985236,0.883045943420430,0.877744734569981,0.866324...
206 720972384,0.851908768417901,0.851104984074884,0.845491...
207 955167970,0.841154026490747,0.839286128027530,0.850683...
208 644332506,0.830355379707657,0.821697577864173,0.819037...

```

```

209 753064181,0.790070686515306,0.803237872240048,0.783570...
210 560967676]';
211 CM_Slot_200_JD=...
212 [-0.00834979338577161;-0.00715681206848110;-0.0065466537...
213 4145752;-0.00688203234423188;-0.00779458060051240;-0.009...
214 27762017151896;-0.00966528705279758;-0.0095679478086160...
215 9;-0.00825205444560790;-0.00753024158239537;-0.006931591...
216 21437764;-0.00624167419865799;-0.00627780524635620;-0.00...
217 677685305657774;-0.00714047929698264;-0.00719647138574...
218 427;-0.00666526788181024;-0.00520675806074079;-0.0033756...
219 8081036960;-0.00182896399677014;-0.000752203860571932;...
220 -8.69837691748233e
    -05;0.000220931046794505;-0.00394263893098121;-0.01545796...

221 10548854;-0.0286247777470567;-0.0421161886578441;-0.0526...
222 581066968622;-0.0622903713117134;-0.0649164366029284;-0...
223 0679676602655533;-0.0710301613427541;-0.073605044751386...
224 5;-0.0757827756531143;-0.0801753059813129;-0.08113066871...
225 99231;-0.0827144357251951;-0.0846946079541785;-0.0854294...
226 231628424;-0.0841215861740769;-0.0841665989358836;-0.084...
227 2169756662313;-0.0831993253281970;-0.0831674320221782;...
228 -0.0852008474669002];
229
230 Alpha_Slot_400_JD=alpha+...
231 [-8.14107995734776;-7.12810380397329;-6.02294002587198;...
232 -5.00100829505852;-3.98065584668460;-2.87139441735438;...
233 -1.84952770602303;-0.829170803599483;0.280451313638561;...
234 0.832112928356729;1.29695570220239;1.84800350937919;...
235 2.40181187810453;2.86816341968855;3.42161042868440;...
236 3.88872287648642;4.43966731528486;5.45162906889796;...
237 6.55437032751475;7.56363601108004;8.66657245565575;...
238 9.67845705484742;10.6909516992006;11.7958743891732;...
239 12.8114141249747;13.8346778549107;14.9378776008161;...
240 15.9387749238412;16.9346122624383;18.0179820522858;...
241 18.9964023200859;20.0620812411592;21.0303959822269;...
242 22.0041179249296;22.9715615402812;24.0260517121405;...
243 24.9988278640787;25.9736340670725;27.0422333311487;...
244 27.9946973069450;29.0418733935211;29.9959334967865;...
245 30.9671914337833;32.0001766548288;32.9663708286242];...
246 CD_Slot_400_JD=...
247 [0.00569768908582134;0.000653616631782971;-0.0040173...
248 3492747906;-0.00742990193772587;-0.0102174497790087;...
249 -0.0133023270693763;-0.0142207914583933;-0.014594291...
250 7647373;-0.0142093229799219;-0.0138959193545874;-0.01...
251 26582858300000;-0.0117907234379582;-0.01058897412493...
252 04;-0.00846719539239434;-0.00710909653460416;-0.00465...
253 318894119242;-0.00296639088322539;0.001052522621462...
254 43;0.00651350808441484;0.0117933998076995;0.01891820...
255 08004069;0.0261482628131217;0.0342962335695831;0.043...
256 8656700474776;0.0552077756509481;0.0693740477420460;...
257 0.105172507392724;0.139528921009682;0.1679357319248...
258 90;0.199834155989705;0.226344669145139;0.25453057310...
259 9369;0.277085828367057;0.300568277707328;0.322077310...
260 429307;0.346829752414292;0.367124558895408;0.3862760...
261 86830406;0.412179568299533;0.427395948086337;0.44643...
262 3916573160;0.462425886927703;0.482117157303679;0.493...
263 772336860829;0.513431234800692];
264 CL_Slot_400_JD=...

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265 [-0.340528694281068,-0.293888778754073,-0.242807582020...
266 513,-0.187730196836646,-0.133267182896577,-0.077840128...
267 4080720,-0.0217711282459079,0.0326966095383901,0.08744...
268 56269616597,0.112540493770281,0.137827493036031,0.162...
269 271372214259,0.188582455220084,0.215469612627635,0.242...
270 458020182855,0.270152174087562,0.294486423567305,0.338...
271 989921342888,0.387501859615882,0.430206551500381,0.478...
272 925498707463,0.524407741473837,0.569476408715038,0.620...
273 301913918239,0.669660695436623,0.727211335640237,0.776...
274 209533096261,0.808978395884902,0.837441349306045,0.865...
275 408433204394,0.875399313732268,0.884603942028837,0.882...
276 816602113635,0.887824566473365,0.886173907128255,0.883...
277 512051474941,0.887516935802066,0.892614264341189,0.904...
278 916129219707,0.887378470447064,0.876959494318545,0.861...
279 114645048685,0.862448778909116,0.836979355690106,0.834...
280 003572518458]';
281 CM_Slot_400_JD=...
282 [-0.00959850700301111;-0.00874982906994464;-0.007907456...
283 16336122;-0.00881500204053227;-0.00980820493121330;-0.0...
284 110651682189337;-0.0113239431035566;-0.011840219262665...
285 1;-0.0108308275197412;-0.0103000706859604;-0.0095246466...
286 1322938;-0.00857190190790365;-0.00834770619569028;-0.00...
287 849964062857796;-0.00863106772547918;-0.00879291315863...
288 069;-0.00837630719200007;-0.00694002271937745;-0.005296...
289 62406811701;-0.00331477093293976;-0.00212958191237636;...
290 -0.00145238375830875;-0.000726417246053755;-0.00025042...
291 8208528577;-0.00158101230521345;-0.0119384093858803;-0...
292 .0278569646668860;-0.0391783362526073;-0.0469237967756...
293 573;-0.0566692689865733;-0.0616690489485235;-0.06525804...
294 91857559;-0.0682765276124359;-0.0731923881907869;-0.075...
295 6053897214873;-0.0829084605615219;-0.0854438243424612;...
296 -0.0882944149254450;-0.0890506385715564;-0.08978128770...
297 85074;-0.0915346082694105;-0.0921384186320555;-0.092891...
298 1886500812;-0.0935403064400923;-0.0928891979397311];...
299
300 Alpha_Slot_600_JD=alpha+...
301 [-8.15250305008806;-7.13851290714992;-6.03051364430308;...
302 -5.01117589838906;-3.99037918445528;-2.87932753037828;...
303 -1.85626236599775;-0.834814878555532;0.274142141001341;...
304 0.826066351573143;1.29116820600337;1.84275410005435;...
305 2.39770025991947;2.86382014537051;3.41749994600344;...
306 3.88381537566056;4.43571125667504;5.44782988317605;...
307 6.55176145418855;7.56357115087161;8.66644528646187;...
308 9.67834967266616;10.6916630962418;11.7982876029726;...
309 12.8131855970119;13.8340664829350;14.9467350593083;...
310 15.9674637590202;16.9845101257540;18.0875632637920;...
311 19.0966204643189;20.1633774635334;21.1396071845055;...
312 22.1110566367845;23.0677525891127;24.1201163602511;...
313 25.0488677017462;25.9941081509589;27.0518668176482;...
314 28.0270018230895;29.0770736345079;30.0501514516892;...
315 31.0001085712215;32.0467826847915;33.0096335195687];...
316 CD_Slot_600_JD=...
317 [-0.0130658913688246;-0.0180842416071628;-0.022456305...
318 0802255;-0.0257976158492426;-0.0287702976700154;-0.03...
319 20076226532163;-0.0324107936394564;-0.03261643771122...
320 30;-0.0319837811121743;-0.0315085156292136;-0.0299661...
321 090276477;-0.0291775542254593;-0.0280246271852704;-0...
322 0256038813179883;-0.0238580183687156;-0.021228450678...

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323 7270;-0.0191196323640248;-0.0149694630879372;-0.009078...
324 06619669437;-0.00304101045471653;0.00383001613165229...
325 ;0.0113398715173390;0.0197058169479430;0.030249908478...
326 1012;0.0403212498678895;0.0524337189708148;0.06698199...
327 27082439;0.0825577218736728;0.103000268644405;0.13377...
328 6722358127;0.185679142766743;0.238490168158967;0.2693...
329 60459893327;0.299375454581163;0.324196829528256;0.351...
330 115142779436;0.367985743075838;0.376515906340747;0.39...
331 9577001851152;0.422730003720431;0.444102434599543;0.4...
332 65101086216071;0.483472381511884;0.501379222405195;...
333 0.518553198817997];
334 CL_Slot_600_JD=...
335 [-0.352643716618924,-0.304928391262603,-0.250839956313...
336 286,-0.198513681158485,-0.143579491215208,-0.086253772...
337 9155831,-0.0289137259544743,0.0267106567212663,0.08075...
338 42895829787,0.106127658431716,0.131689431538560,0.156...
339 703991061284,0.184221784490254,0.210863253686253,0.23...
340 8098553737877,0.264947411815210,0.290290735103814,0.3...
341 34960608009534,0.384734959325207,0.430137762522489,0...
342 478790626509576,0.524293854844864,0.570230897122041,0...
343 .622861303021514,0.671539470632569,0.726562931104796,0...
344 .785603513336904,0.839404996363596,0.890361669785317,0...
345 .939204378913497,0.981687959342012,0.992035968075043,0...
346 .998643041172583,1.00124086382455,0.988191524579992,0...
347 983274465995295,0.940587830428161,0.914328522403276,0...
348 915133143717022,0.921639764091660,0.914291915191565,0...
349 918616737493617,0.897359802082030,0.886408446997923,0...
350 879886809143175]';
351 CM_Slot_600_JD=...
352 [-0.00723738933360987;-0.00620776301636090;-0.00619294...
353 458505423;-0.00651444951696916;-0.00743876910006222;-0...
354 .00861584790279979;-0.00966118845439566;-0.0105746532...
355 004899;-0.00980569395259948;-0.00916198942512294;-0.00...
356 848389612122977;-0.00782406485606092;-0.0076584206531...
357 9508;-0.00782905371730899;-0.00814129622862258;-0.0082...
358 4703629731736;-0.00807708135388103;-0.006707450540029...
359 11;-0.00524683155342631;-0.00386734839632959;-0.002368...
360 46368680112;-0.00158201749017828;-0.00111774076086887...
361 ;-0.000634937187145405;-0.00138717124650150;-0.0105812...
362 981760175;-0.0222199752206172;-0.0342678895374102;-0.0...
363 456083761608960;-0.057734448585022751;-0.06970409688556...
364 46;-0.0754547156471550;-0.0791776508059520;-0.08150487...
365 85559114;-0.0829557505717916;-0.0847154169596503;-0.08...
366 23035973940487;-0.0858402438505193;-0.084752948869612...
367 3;-0.0857334788596333;-0.0837092498012970;-0.085689331...
368 5450340;-0.0917963917474111;-0.0940930991685665;-0.097...
369 4335038708480];
370
371 Alpha_Slot_800_JD=alpha+...
372 [-8.16532994130786;-7.15071579092200;-6.04244860884083;...
373 -5.02099510922208;-4.00074350475546;-2.89013300970893;...
374 -1.86673672339860;-0.845557601359153;0.262744376454180;...
375 0.815668234712962;1.28098830005780;1.83392968241970;...
376 2.38963009158842;2.85600354947695;3.41124262157922;...
377 3.87728372488066;4.42928798070192;5.44207749788951;...
378 6.54701850023257;7.55851760590759;8.66181167361823;...
379 9.67231113504006;10.6858135558792;11.7945702669411;...
380 12.8095448979892;13.8303756931133;14.9434105377481;...

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381 15.9616233762802;16.9770125159476;18.0751112575024;...
382 19.0870816918115;20.1944651800602;21.2080328942639;...
383 22.1973387095223;23.1762140686440;24.2493579805815;...
384 25.2214289083073;26.1923382924692;27.2178579547376;...
385 28.1285669372076;29.1882477121527;30.1384264568971;...
386 31.0873604704253;32.0796152955456;33.0318609966642];...
387 CD_Slot_800_JD=...
388 [-0.00681050693390072;-0.0126543294087441;-0.0182495...
389 693770797;-0.0214166231427484;-0.0251674028323114;-0...
390 .0284813491243448;-0.0295284521703782;-0.0300352983...
391 439126;-0.0297999387101721;-0.0295720385414848;-0.02...
392 82132488021699;-0.0273310852132612;-0.026210383664...
393 1072;-0.0240278454672732;-0.0220435932508557;-0.0190...
394 684670650371;-0.0168993698727356;-0.01216566243845...
395 81;-0.00643704479454368;-0.000469991253904901;0.0068...
396 1634235048144;0.0143941708545328;0.022555795883598...
397 0;0.0335793770283875;0.0439463538650867;0.0560009143...
398 510980;0.0702808537518199;0.0848501778814416;0.10300...
399 2466782877;0.128061227791715;0.152144243602451;0.182...
400 336909797974;0.215148357201335;0.275067267157616;0.3...
401 20558261523750;0.362479685381631;0.396531037918776;...
402 0.429234176477427;0.457465813635064;0.4677768042418...
403 04;0.494369876697358;0.510196123102673;0.52428205263...
404 3874;0.518416110561748;0.533085621458722];
405 CL_Slot_800_JD=...
406 [-0.366247569549657,-0.317870438818895,-0.2634978559...
407 96289,-0.208927669846718,-0.154571608219602,-0.09771...
408 37712223667,-0.0400225453233562,0.0153172162849387,...
409 0.0686661296398034,0.0950996977124353,0.1208928993...
410 96894,0.147345053057996,0.175662782841257,0.2025731...
411 84086938,0.231462205167657,0.258020120152550,0.2834...
412 78382821840,0.328859784193542,0.379704711000120,0.4...
413 24778109798272,0.473876342402648,0.517889545618680...
414 ,0.564027033267523,0.618918797249851,0.667678243993...
415 874,0.722648579523156,0.782077615939359,0.833210844...
416 835199,0.882409908178346,0.925998118771882,0.971571...
417 395935769,1.02500675704765,1.07121349306802,1.09274...
418 928998711,1.10322282802753,1.12034462316562,1.12360...
419 156582039,1.12456603399776,1.09117884162421,1.02935...
420 696942839,1.03220012662585,1.01223881378076,0.98989...
421 6799890378,0.921229823462180,0.903460668486540]';
422 CM_Slot_800_JD=...
423 [-0.00271428206765456;-0.00189706750827400;-0.001585...
424 10093408801;-0.00257006623435670;-0.003639827594117...
425 15;-0.00377285117644621;-0.00528002084311486;-0.0060...
426 4783914821188;-0.00542639016919631;-0.0048547859236...
427 7664;-0.00467522918668672;-0.00464200994639661;-0.00...
428 484881943788308;-0.00517612644732052;-0.00576129489...
429 607823;-0.00558567933442236;-0.00544667475420462;-0...
430 00388856835124193;-0.00257735756993069;-0.001209129...
431 76751777;0.000188843218942158;0.00126966991609235;0...
432 .00194730019213918;0.00226867902786383;0.0020075243...
433 3835763;-0.00655633847238418;-0.0191938207372223;-0.0...
434 288876484116350;-0.0402225780133489;-0.0509736602055...
435 526;-0.0593875338193712;-0.0673592849128238;-0.074871...
436 3020188131;-0.0814793195538752;-0.0864569567583774;-0...
437 .0922018627535162;-0.0947708467128809;-0.09736442547...
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439 042960490281;-0.0905853919434668;-0.089976876926054...
440 0;-0.0848269056017114;-0.0859492228960141];
441
442 Alpha_Slot_1000_JD=alpha+...
443 [-8.19296176515518;-7.17933574587292;-6.07141593961330;...
444 -5.05068766637736;-4.01478390175705;-2.90376884270189;...
445 -1.88070289398938;-0.858610138673839;0.251892829170128;...
446 0.805045079373169;1.27096880298182;1.82550033419823;...
447 2.29328670403366;2.84752853218911;3.40257829519855;...
448 3.86968238230243;4.42287620882581;5.43862308343971;...
449 6.54573182715474;7.55713986284914;8.66098722550410;...
450 9.67236449623901;10.6852903591628;11.7936837267243;...
451 12.8112788281600;13.8329825727792;14.9471087553110;1...
452 5.9664578225023;16.9791398538928;18.0817616704432;...
453 19.0886948118036;20.1847033352771;21.2029090750168;...
454 22.2183661266420;23.2279674798223;24.3299915044846;...
455 25.3283955867359;26.3157875287581;27.3957186622302;...
456 28.3760532549829;29.4314555943111;30.3576518649962;...
457 31.2810950601421;32.2836331725416;33.2135410784349];
458 CD_Slot_1000_JD=...
459 [-0.0193797893655357;-0.0259114877416335;-0.03258667...
460 37823424;-0.0372877316448054;-0.0409895595179842;-0.0...
461 451211540031038;-0.0465323825799716;-0.046985848615...
462 9102;-0.0470235007266426;-0.0471019968699758;-0.04558...
463 46122476344;-0.0447892744155420;-0.0432186377043500;...
464 -0.0416831615990399;-0.0400375162366334;-0.037384285...
465 6392081;-0.0350786936687696;-0.0303777956122959;-0.02...
466 17416728583107;-0.0157560312384841;-0.00811648099009...
467 559;-0.000582397437687672;0.00780414749527014;0.0186...
468 951181907445;0.0294869235072628;0.0417640755961384;...
469 0.0566192455906378;0.0718139381421382;0.08864026042...
470 94024;0.109696609944029;0.131368096438492;0.15524846...
471 0024663;0.184343329546123;0.215847194077492;0.248784...
472 760521435;0.293162365698196;0.352499161384842;0.4063...
473 87379826736;0.458282454622353;0.500207681789809;0.54...
474 2355888075449;0.570273045623037;0.586548858269573;...
475 0.595084080898688;0.601632791661711];
476 CL_Slot_1000_JD=...
477 [-0.395553132478767,-0.348223986795931,-0.29421982134...
478 7971,-0.240418790630072,-0.169462472469212,-0.1121755...
479 65857211,-0.0548346870548746,0.00147404922605309,0.05...
480 71572729111181,0.0838330672852779,0.110266492551626,...
481 0.138405114959061,0.166814012293967,0.19358481061487...
482 2,0.222273055606256,0.249958342381286,0.2766782314731...
483 33,0.325196125920342,0.378340100431535,0.423316912878...
484 281,0.473001955093872,0.517946139059006,0.56347214502...
485 0504,0.617978556741035,0.669517203304557,0.7254133653...
486 91840,0.785999845181785,0.838338127376218,0.884666105...
487 104343,0.933051366361309,0.973282227247636,1.01465360...
488 923606,1.06577930934517,1.11505039826875,1.1581110922...
489 4280,1.20586235163683,1.23704752376115,1.255492945757...
490 42,1.27981308396896,1.29183424562026,1.29013981004425...
491 1.24474333567583,1.19536645118314,1.13760565033506,1.0...
492 9614563559966]';
493 CM_Slot_1000_JD=...
494 [0.00507017714348937;0.00614418826676139;0.006842971...
495 85030537;0.00699513112022954;0.00437741572681731;0.0...
496 0282945856269266;0.00113340818135327;0.000333189608...

```

```

497 933874;0.000586231571137447;0.000924799225952278;0.0...
498 00824185731205280;0.000767407000762050;0.0003493200...
499 57341334;-0.000162324801487116;-0.00074296932765326...
500 5;-0.00125212658580521;-0.00147376228469160;-0.001264...
501 98499510802;0.00179972763032268;0.00314076315957652...
502 ;0.00435342405830659;0.00526227344420236;0.006221210...
503 03062758;0.00675959969365219;0.00639421820758831;-0....
504 00220469951161398;-0.0136034339227159;-0.0230183035...
505 253696;-0.0325897625335028;-0.0410750732024380;-0.046...
506 7011262564439;-0.0522773449139122;-0.05960919917759...
507 88;-0.0671714951745267;-0.0740194214401699;-0.0823273...
508 039146220;-0.0909191500060944;-0.0970089485628756;...
509 -0.103913781913880;-0.108509186502984;-0.11207993050...
510 2852;-0.109408392847778;-0.105477991507032;-0.101058...
511 260651483;-0.0975542197429547];
512
513 %% Import Kestrel Data
514
515 [EX1] = importdata('EX1_forces.dat',' ',23);
516 [EX2] = importdata('EX2_forces.dat',' ',23);
517 [EX3] = importdata('EX3_forces.dat',' ',23);
518 [EX4] = importdata('EX4_forces.dat',' ',23);
519 [EX5] = importdata('EX5_forces.dat',' ',23);
520 [EX6] = importdata('EX6_forces.dat',' ',23);
521 [EX7] = importdata('EX7_forces.dat',' ',23);
522 [EX8] = importdata('EX8_forces.dat',' ',23);
523
524 SW_M = {EX1, EX2, EX3, EX4, EX5, EX6, EX7, EX8};
525 %% Axial Forces
526 Iter = 1000; %Number of iterations to average over
527 k = 0;
528 for i = 1:length(SW_M)
529     I = SW_M{i};
530     k=k+1;
531     fx_I = mean(I.data((length(I.data)-Iter:end)),33)); %
532         Time Avg at 33
533     fx(:,k) = fx_I;
534 end
535 fx_3_check = mean(EX3.data((length(EX3.data)-Iter:end)),33));
536
537 %% Vertical Forces
538 k = 0;
539 for j = 1:length(SW_M)
540     J = SW_M{j};
541     k=k+1;
542     fy_J = mean(J.data((length(J.data)-Iter:end)),34)); %
543         Time Avg at 34
544     fy(:,k) = fy_J;
545 end
546 fy_3_Check = mean(EX3.data((length(EX3.data)-Iter:end)),34));
547
548 %% Moment about the z-axis
549 x_cor = -1.28; % Correction for incorrect location of Moment
550         Reference point in CFD Settings
551 k = 0;
552 for e = 1:length(SW_M)
553     E = SW_M{e};
554     k=k+1;

```

```

552     Mz_E = mean(E.data(( [length(E.data)-Iter:end] ),38))/x_cor;
553     % Time Avg at 38
554     Mz(:,k) = Mz_E;
555 end
556 Mz_3_Check = mean(EX3.data(( [length(EX3.data)-Iter:end] ),38))
557 /x_cor;
558 %% Lift
559 AoA = 24;
560 k = 0;
561 for p = 1:length(SW_M)
562     FX_L = fx(p);
563     FY_L = fy(p);
564     k=k+1;
565     L_P = FY_L*cosd(AoA)-FX_L*sind(AoA);
566     L(:,k) = L_P;
567 end
568 L_3_Check = fy(:,3)*cosd(AoA)+fx(:,3)*sind(AoA);
569 %% Drag
570 k = 0;
571 for q = 1:length(SW_M)
572     FX_D = fx(q);
573     FY_D = fy(q);
574     k=k+1;
575     D_P = FX_D*cosd(AoA)+FY_D*sind(AoA);
576     D(:,k) = D_P;
577 end
578 D_3_Check = fx(:,3)*cosd(AoA)+fy(:,3)*sind(AoA);
579 %% Pitching Moment
580 x_cm = 1.3; % in - Estimated distance from Aero Center
581 MomRef_L = 1; % in - NA
582 % PM_0 = (Mz_0/MomRef_L)-(L_0*cosd(0)*x_cm)+(D_0*-sind(0)*
583 x_cm);
584 k = 0;
585 for z = 1:length(SW_M)
586     L_PM = L(z);
587     D_PM = D(z);
588     Mz_PM = Mz(z);
589     k=k+1;
590     PM_Z = (Mz_PM/MomRef_L)-(L_PM*cosd(AoA)*x_cm)+(D_PM*-sind(
591 AoA)*x_cm);
592     PM(:,k) = PM_Z;
593 end
594 PM_3_Check = (Mz(:,3)/MomRef_L)-(L(:,3)*cosd(AoA)*x_cm)+(D
595 (:,3)*-sind(AoA)*x_cm);
596 %% Coeffiecient of Lift
597 k = 0;
598 for v = 1:length(SW_M)
599     L_CL = L(v);
600     k=k+1;
601     CL_V = (L_CL*2)/(0.67764*0.0009518*((3751.5/12)^2));
602     CL(:,k) = CL_V;
603 end
604 CL_3_Check = (L(:,3)*2)/(0.67764*0.0009518*((3751.5/12)^2));

```

```

605 %% Coeffiecient of Drag
606 % CD_0 =(D_0*2)/(0.67764*0.0009518*((3751.5/12)^2));
607 k = 0;
608 for w = 1:length(SW_M)
609     D_CD = D(w);
610     k=k+1;
611     CD_W = (D_CD*2)/(0.67764*0.0009518*((3751.5/12)^2));
612     CD(:,k) = CD_W;
613 end
614 CD_3_Check = (D(:,3)*2)/(0.67764*0.0009518*((3751.5/12)^2));
615
616 %% Moment Coeffiecient
617 c_bar = 9.66;
618 % CM_0 =(PM_0*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
619 k = 0;
620 for x = 1:length(SW_M)
621     PM_CM = PM(x);
622     k=k+1;
623     CM_X = (PM_CM*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar)
624     ;
625     CM(:,k) = CM_X;
626 end
627 CM_3_Check =(PM(:,3)*2)/(0.67764*0.0009518*((3751.5/12)^2)*
628     c_bar);
629
630 %% Momentum Cefficient (C_mu) and Blowing Ratio (BR)
631     Calcualtion
632 V_inf = 3751.5; % in/s
633 C_mu = [7.332, 9.165, 5.499, 5.499, 3.666, 1.833, 7.332,
634     5.499];
635 V_slot = [18196.02];
636
637 BR = V_slot/V_inf;
638
639 %% Percent Gain/Reduction CL/CD/CM
640 CL_Base_24AoA = 0.8021; % <--CFD, WT =0.8021
641 CD_Base_24AoA = 0.3503; % <--CFD, WT =0.3478
642 CM_Base_24AoA = -0.03129; % <--CFD, WT =-0.028291
643
644 CL_BLF_24AoA = 0.8505; %WT
645 CD_BLF_24AoA = 0.3567; %WT
646 CM_BLF_24AoA = -0.06696; %WT
647
648 CL_AFC_WT = [0.8508, 0.8861, 0.98912, 1.10134, 1.14839,]; % 24
649     AoA Wind tunnel values in order of Cmu (M1, M2, M3, M4, M5)
650 CD_AFC_WT = [0.3423, 0.32275, 0.32244, 0.31237, 0.24135,]; %
651     24AoA Wind tunnel values in order of Cmu (M1, M2, M3, M4,
652     M5)
653 CM_AFC_WT = [-0.08023, -0.0758, -0.08285, -0.08556,
654     -0.07247,]; % 24AoA Wind tunnel values in order of Cmu (M1,
655     M2, M3, M4, M5)
656
657 CL_Combine = [CL, CL_Base_24AoA, CL_BLF_24AoA, CL_AFC_WT];
658 CD_Combine = [CD, CD_Base_24AoA, CD_BLF_24AoA, CD_AFC_WT];
659 CM_Combine = [CM, CM_Base_24AoA, CM_BLF_24AoA, CM_AFC_WT];
660
661 CL_PerGain = 100*((CL_Combine-CL_Base_24AoA)/abs(CL_Base_24AoA
662     ));

```

```

653
654 CD_PerRed = 100*((CD_Combine-CD_Base_24AoA)/abs(CD_Base_24AoA)
    );
655
656 CM_PerRed = 100*((CM_Combine-CM_Base_24AoA)/abs(CM_Base_24AoA)
    );
657
658 %% CD, CL, CM vs Alpha Plots
659 % figure()
660 % hold on
661 % plot(Alpha_Baseline2,CD_Base2, 'k', 'LineWidth',0.9)
662 % plot(Alpha_BLF_1,CD_BLF_1,'Color', [0.25 0.80 0.54], '
    LineWidth',0.9)
663 % plot(Alpha_Slot_200_JD,CD_Slot_200_JD, 'r', 'LineWidth
    ',0.9)
664 % plot(Alpha_Slot_400_JD,CD_Slot_400_JD, 'g', 'LineWidth
    ',0.9)
665 % plot(Alpha_Slot_600_JD,CD_Slot_600_JD, 'b', 'LineWidth
    ',0.9)
666 % plot(Alpha_Slot_800_JD,CD_Slot_800_JD, 'm', 'LineWidth
    ',0.9)
667 % plot(Alpha_Slot_1000_JD,CD_Slot_1000_JD, 'LineWidth',0.9)
668 % plot(AoA,CD(:,1),'ro',AoA,CD(:,2),'go',AoA,CD(:,3),'bo',AoA,
    CD(:,4),'mo',AoA,CD(:,5),'o',AoA,CD(:,6),'ko','LineWidth
    ',0.9)
669 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
    assigned is Orange (M5)
670 % xlim([23 25])
671 % xlabel('Angle of Attack (deg)')
672 % ylabel('Uncorrected Coefficient of Drag (-)')
673 % hold off
674 %
675 % title('Coefficient of Drag at 45 mph')
676 % legend('Baseline Model','Fence Model','Slot Model, C\mu
    =0.49%', 'Slot Model, C\mu=1.95%', 'Slot Model, C\mu=4.40%',
    'Slot Model, C\mu=7.82%', 'Slot Model, C\mu=12.22%', 'EX1', '
    EX2', 'EX3', 'EX4', 'EX5', 'EX6', 'Location', 'best')
677 % %legend('Windtunnel Basic Model','Fence Model','Slot Model,
    600 SLPM%')
678 % %legend('Windtunnel Basic Model','CFD Basic Model','Location
    ', 'best')
679 %
680 % figure()
681 % hold on
682 % plot(Alpha_Baseline2,CL_Base2, 'k', 'LineWidth',0.9)
683 % plot(Alpha_BLF_1,CL_BLF_1,'Color', [0.25 0.80 0.54], '
    LineWidth',0.9)
684 % plot(Alpha_Slot_200_JD,CL_Slot_200_JD, 'r', 'LineWidth
    ',0.9)
685 % plot(Alpha_Slot_400_JD,CL_Slot_400_JD, 'g', 'LineWidth
    ',0.9)
686 % plot(Alpha_Slot_600_JD,CL_Slot_600_JD, 'b', 'LineWidth
    ',0.9)
687 % plot(Alpha_Slot_800_JD,CL_Slot_800_JD, 'm', 'LineWidth
    ',0.9)
688 % plot(Alpha_Slot_1000_JD,CL_Slot_1000_JD, 'LineWidth',0.9)
689 % plot(AoA,CL(:,1),'ro',AoA,CL(:,2),'go',AoA,CL(:,3),'bo',AoA,
    CL(:,4),'mo',AoA,CL(:,5),'o',AoA,CL(:,6),'ko','LineWidth

```

```

    ',0.9)
690 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
    assigned is Orange (M5)
691 % xlim([23 25])
692 % xlabel('Angle of Attack (deg)')
693 % ylabel('Uncorrected Coefficient of Lift (-)')
694 % hold off
695 % legend('Baseline Model','Fence Model','Slot Model, C\mu
    =0.49%', 'Slot Model, C\mu=1.95%', 'Slot Model, C\mu=4.40%',
    'Slot Model, C\mu=7.82%', 'Slot Model, C\mu=12.22%', 'EX1', '
    EX2', 'EX3', 'EX4', 'EX5', 'EX6', 'Location', 'best')
696 % title('Coefficient of Lift at 45 mph')
697 % %legend('Windtunnel Basic Model','CFD Basic Model','Location
    ', 'best')
698 %
699 % figure()
700 % hold on
701 % plot(Alpha_Baseline2,CM_Base2, 'k', 'LineWidth',0.9)
702 % plot(Alpha_BLF_1,CM_BLF_1,'Color', [0.25 0.80 0.54], '
    LineWidth',0.9)
703 % plot(Alpha_Slot_200_JD,CM_Slot_200_JD, 'r', 'LineWidth
    ',0.9)
704 % plot(Alpha_Slot_400_JD,CM_Slot_400_JD, 'g', 'LineWidth
    ',0.9)
705 % plot(Alpha_Slot_600_JD,CM_Slot_600_JD, 'b', 'LineWidth
    ',0.9)
706 % plot(Alpha_Slot_800_JD,CM_Slot_800_JD, 'm', 'LineWidth
    ',0.9)
707 % plot(Alpha_Slot_1000_JD,CM_Slot_1000_JD, 'LineWidth',0.9)
708 % plot(AoA,CM(:,1),'ro',AoA,CM(:,2),'go',AoA,CM(:,3),'bo',AoA,
    CM(:,4),'mo',AoA,CM(:,5),'o',AoA,CM(:,6),'ko','LineWidth
    ',0.9)
709 % colororder([0.9290 0.6940 0.1250]) % Marker with no color
    assigned is Orange (M5)
710 % xlim([23 25])
711 % xlabel('Angle of Attack (deg)')
712 % ylabel('Uncorrected Pitch Moment Coefficient (-)')
713 % hold off
714 % legend('Baseline Model','Fence Model','Slot Model, C\mu
    =0.49%', 'Slot Model, C\mu=1.95%', 'Slot Model, C\mu=4.40%',
    'Slot Model, C\mu=7.82%', 'Slot Model, C\mu=12.22%', 'EX1', '
    EX2', 'EX3', 'EX4', 'EX5', 'EX6', 'Location', 'best')
715 % title('Pitch Moment Coefficient at 45 mph')
716 % %The coeffcient curves are superimposed, providng evidence
    that the data is good
717
718
719 %% CL/CD/CM vs BR - Lines of Constant Slot Width
720
721 % figure ()
722 % hold on
723 % yline(CL_Base_24AoA, '--k')
724 % plot(BR(:,[1]),CL(:,[1]),'ro','LineWidth',0.9)
725 % plot(BR(:,[1]),CL(:,[2]),'go','LineWidth',0.9)
726 % plot(BR(:,[1]),CL(:,[3]),'bo','LineWidth',0.9)
727 % plot(BR(:,[1]),CL(:,[4]),'mo','LineWidth',0.9)
728 % plot(BR(:,[1]),CL(:,[5]),'o','LineWidth',0.9,'Color',[0.9290
    0.6940 0.1250])

```

```

729 % plot(BR(:,[1]),CL(:,[6]),'ko','LineWidth',0.9)
730 % legend('Baseline','EX1','EX2','EX3','EX4','EX5','EX6',,
    Location','northwest')
731 % ylabel('Coeffiecient of Lift')
732 % xlabel('Blowing Ratio ( $V_{slot}/V_{\infty}$ )')
733 % hold off
734 %
735 % figure ()
736 % hold on
737 % yline(CD_Base_24AoA, '--k')
738 % plot(BR(:,[1]),CD(:,[1]),'ro','LineWidth',0.9)
739 % plot(BR(:,[1]),CD(:,[2]),'go','LineWidth',0.9)
740 % plot(BR(:,[1]),CD(:,[3]),'bo','LineWidth',0.9)
741 % plot(BR(:,[1]),CD(:,[4]),'mo','LineWidth',0.9)
742 % plot(BR(:,[1]),CD(:,[5]),'o','LineWidth',0.9,'Color',[0.9290
    0.6940 0.1250])
743 % plot(BR(:,[1]),CD(:,[6]),'ko','LineWidth',0.9)
744 % legend('Baseline','EX1','EX2','EX3','EX4','EX5','EX6',,
    Location','northwest')
745 % ylabel('Coeffiecient of Drag')
746 % xlabel('Blowing Ratio ( $V_{slot}/V_{\infty}$ )')
747 % hold off
748 %
749 % figure ()
750 % hold on
751 % yline(CM_Base_24AoA, '--k')
752 % plot(BR(:,[1]),CM(:,[1]),'ro','LineWidth',0.9)
753 % plot(BR(:,[1]),CM(:,[2]),'go','LineWidth',0.9)
754 % plot(BR(:,[1]),CM(:,[3]),'bo','LineWidth',0.9)
755 % plot(BR(:,[1]),CM(:,[4]),'mo','LineWidth',0.9)
756 % plot(BR(:,[1]),CM(:,[5]),'o','LineWidth',0.9,'Color',[0.9290
    0.6940 0.1250])
757 % plot(BR(:,[1]),CM(:,[6]),'ko','LineWidth',0.9)
758 % legend('Baseline','EX1','EX2','EX3','EX4','EX5','EX6',,
    Location','northwest')
759 % ylabel('Pitching Moment Coeffiecient')
760 % xlabel('Blowing Ratio ( $V_{slot}/V_{\infty}$ )')
761 % hold off
762
763 %% Cmu VS Percent Gain with lines of Constant Slot Width
764 figure ()
765 hold on
766 plot(C_mu(:,[1]),CL_PerGain(:,[1]),'ro','LineWidth',2)
767 plot(C_mu(:,[2]),CL_PerGain(:,[2]),'go','LineWidth',2)
768 plot(C_mu(:,[3]),CL_PerGain(:,[3]),'bo','LineWidth',2)
769 plot(C_mu(:,[4]),CL_PerGain(:,[4]),'mo','LineWidth',1.5)
770 plot(C_mu(:,[5]),CL_PerGain(:,[5]),'o','LineWidth',2,'Color',
    ,[0.9290 0.6940 0.1250])
771 plot(C_mu(:,[6]),CL_PerGain(:,[6]),'ko','LineWidth',2)
772 plot(C_mu(:,[7]),CL_PerGain(:,[7]),'yo','LineWidth',2)
773 plot(C_mu(:,[8]),CL_PerGain(:,[8]),'co','LineWidth',2)
774 %line([0 C_mu(:,[7])],[0,CL_PerGain(:,[7])])
775 %line([0 C_mu(:,[8])],[0,CL_PerGain(:,[8])])
776 grid on
777 %legend('24^o \alpha: AFC CFD SW3 M_{slot}=0.8731 EX1','24^o \
    alpha: AFC CFD SW3 M_{slot}=0.8731 EX2','24^o \alpha: AFC
    CFD SW3 M_{slot}=0.8731 EX3','24^o \alpha: AFC CFD SW3 M_{
    slot}=0.8731 EX4','24^o \alpha: AFC CFD SW3 M_{slot}=0.8731

```

```

EX5','24^o \alpha: AFC CFD SW3 M_{slot}=0.8731 EX6','24^o
\alpha: AFC CFD SW3 M_{slot}=0.8731 EX7','24^o \alpha: AFC
CFD SW3 M_{slot}=0.8731 EX8','Location','southeast')
778 legend('AFC CFD SW3 M5 EX1 = -0.25 to 0.75 x/c, \alpha = 24^o',
'AFC CFD SW3 M5 EX2 = -0.25 to 1.0 x/c, \alpha = 24^o',
'AFC CFD SW3 M5 EX3 = -0.25 to 0.5 x/c, \alpha = 24^o',
'AFC CFD SW3 M5 EX4 = 0 to 0.75 x/c, \alpha = 24^o',
'AFC CFD SW3 M5 EX5 = 0 to 0.5 x/c, \alpha = 24^o',
'AFC CFD SW3 M5 EX6 = 0 to 0.25 x/c, \alpha = 24^o',
'AFC CFD SW3 M5 EX7 = 0 to 1.0 x/c, \alpha = 24^o',
'AFC CFD SW3 M5 EX8 = 0.25 to 1.0 x/c, \alpha = 24^o',
'Location','southeast','Interpreter','tex')
779 ylabel('C_L (% Gain)')
780 xlabel('C_{\mu} (%)')
781 xlim([0 14])
782 ylim([0 40])
783 hold off
784 %
785 % figure ()
786 % hold on
787 % plot(C_mu(:, [1]), CD_PerRed(:, [1]), 'ro', 'LineWidth', 0.9)
788 % plot(C_mu(:, [2]), CD_PerRed(:, [2]), 'go', 'LineWidth', 0.9)
789 % plot(C_mu(:, [3]), CD_PerRed(:, [3]), 'bo', 'LineWidth', 0.9)
790 % plot(C_mu(:, [4]), CD_PerRed(:, [4]), 'mo', 'LineWidth', 0.9)
791 % plot(C_mu(:, [5]), CD_PerRed(:, [5]), 'o', 'LineWidth', 0.9, 'Color
', [0.9290 0.6940 0.1250])
792 % plot(C_mu(:, [6]), CD_PerRed(:, [6]), 'ko', 'LineWidth', 0.9)
793 % legend('EX1', 'EX2', 'EX3', 'EX4', 'EX5', 'EX6', 'Location', '
southeast')
794 % ylabel('Drag: Percent Reduction')
795 % xlabel('Momentum Coefficient')
796 % hold off
797 %
798 % figure ()
799 % hold on
800 % plot(C_mu(:, [1]), CM_PerRed(:, [1]), 'ro', 'LineWidth', 0.9)
801 % plot(C_mu(:, [2]), CM_PerRed(:, [2]), 'go', 'LineWidth', 0.9)
802 % plot(C_mu(:, [3]), CM_PerRed(:, [3]), 'bo', 'LineWidth', 0.9)
803 % plot(C_mu(:, [4]), CM_PerRed(:, [4]), 'mo', 'LineWidth', 0.9)
804 % plot(C_mu(:, [5]), CM_PerRed(:, [5]), 'o', 'LineWidth', 0.9, 'Color
', [0.9290 0.6940 0.1250])
805 % plot(C_mu(:, [6]), CM_PerRed(:, [6]), 'ko', 'LineWidth', 0.9)
806 % legend('EX1', 'EX2', 'EX3', 'EX4', 'EX5', 'EX6', 'Location', '
southeast')
807 % ylabel('Pitching Moment: Percent Reduction')
808 % xlabel('Momentum Coefficient')
809 % hold off
810
811
812
813 % figure ()
814 % hold on
815 % %plot(0, CL_PerGain(:, [26]), 'ko', 'LineWidth', 2)
816 % % plot(0, CL_PerGain(:, [27]), 'ks', 'Color', [0.25 0.80 0.54], '
LineWidth', 1.7) % BLF WT Gains
817 % %plot(C_mu(:, [1 2 3 4 5]), CL_PerGain(:, [28 29 30 31 32]), 'k
--h', 'LineWidth', 0.9) %AFC WT Percent Gains
818 % plot(C_mu(:, [1 2 4 5]), CL_PerGain(:, [1 2 4 5]), 'r--o', '

```

```

      LineWidth',0.9)
819 % plot(C_mu(:,[6 8 9 10]),CL_PerGain(:,[6 8 9 10]),'g--v',
      LineWidth',0.9)
820 % plot(C_mu(:,[11 12 14 15]),CL_PerGain(:,[11 12 14 15]),'b
      --^', 'LineWidth',0.9)
821 % plot(C_mu(:,[16 17 18 19 20]),CL_PerGain(:,[16 17 18 19 20])
      , 'm--s', 'LineWidth',0.9)
822 % plot(C_mu(:,[21 22 24 25]),CL_PerGain(:,[21 22 24 25]), '--d
      , 'LineWidth',0.9, 'Color',[0.9290 0.6940 0.1250])
823 % grid on
824 % %legend('24^o \alpha: Baseline CFD','24^o \alpha: BLF CFD
      ','24^o \alpha: AFC WT','24^o \alpha: AFC CFD SW1','24^o \
      alpha: AFC CFD SW2','24^o \alpha: AFC CFD SW3','24^o \alpha
      : AFC CFD SW4','24^o \alpha: AFC CFD SW5','Location','east
      ')
825 % legend('24^o \alpha: AFC CFD SW1','24^o \alpha: AFC CFD SW2
      ','24^o \alpha: AFC CFD SW3','24^o \alpha: AFC CFD SW4
      ','24^o \alpha: AFC CFD SW5','Location','southeast')
826 % ylabel('C_L (% Gain)')
827 % xlabel('C_\mu (%)')
828 % xlim([0 14])
829 % ylim([0 0.4])
830 % hold off

```

## Appendix I. MATLAB Script: Optimized AFC Slot Final Comparison

```

1 %% Final Comparison - Baseline WT, Passive BLF WT, AFC Cmu
  =12.22% WT, Optimal CFD Config
2 clear all; close all; clc; format compact; format short;
3 %% Baseline, Passive BLF and AFC Slot, Freestream M = 0.059,
  SW1, M1-M5 Wind Tunnel Uncorrected Data
4 alpha = 1;
5 Alpha_Baseline2=alpha+...
6 [-8.17894442052277;-7.16850773849801;-6.15464379090849;...
7 -5.04877209800816;-4.02932120636633;-3.00640352702020;...
8 -1.98382443346184;-0.870213403716582;0.153319187693818;...
9 1.17508365277160;2.19900159794485;3.30928370940170;...
10 4.32751503348324;5.34186930698045;6.44211101586254;...
11 7.45523765217682;8.46819102061274;9.56920569459411;...
12 10.6678210098701;11.6756459136262;12.7671846976348;...
13 13.7663130389622;14.8512817871214;15.9311893169993;...
14 17.0110707277628;18.0844673115262;19.1538944819053;...
15 20.2221014158863;21.3721215112022;22.4257937648188;...
16 23.5698166553147;24.6991922407033;25.7472428560031;...
17 26.8830239002552;28.0967117595190;29.2310840568254;...
18 30.4510280084815;31.6729762552610;32.9017417048610;...
19 34.2275325071614;35.4596797612262;36.7847709966838];...
20 CD_Base2=...
21 [0.0326396226315288;0.0273554591561591;0.02320762912...
22 52264;0.0184655617641355;0.0156734227994947;0.013931...
23 8232188933;0.0127460003513771;0.0110429698239139;0.0...
24 115328779992575;0.0132684007837646;0.01594624739861...
25 14;0.0186260816468254;0.0227511043823911;0.027425377...
26 8944443;0.0325465190807324;0.0391042044857320;0.0473...
27 291339011119;0.0578153893612589;0.0714274594986400;0...
28 .0882968225391222;0.107396801468250;0.12837527862316...
29 1;0.152008514898266;0.177050724527485;0.203713593209...
30 787;0.230608840670329;0.257527050009981;0.2850390953...
31 55441;0.311662701851170;0.335885212499362;0.35962757...
32 0078000;0.378102215918811;0.393975988177553;0.4094634...
33 43267234;0.422979456980625;0.438129375146260;0.452553...
34 360061481;0.469150907399056;0.488570671603892;0.51410...
35 4483039872;0.536274210618872;0.565069415967284];
36 CL_Base2=...
37 [-0.380686716946657,-0.335679522978898,-0.28809803698...
38 6591,-0.235205472140068,-0.180638051940071,-0.1234544...
39 23606297,-0.0655693172981972,-0.00446862170388157,0.0...
40 533671656873325,0.110388299123664,0.169693355141534,...
41 0.227263490287654,0.279476897333351,0.32863898256204...
42 2,0.375560539057904,0.422360052709387,0.4700363760260...
43 67,0.517777718341523,0.561913793013043,0.604151005786...
44 968,0.641842476206843,0.673795777863523,0.70451924645...
45 7192,0.729874924214394,0.754142327869694,0.7725926727...
46 70825,0.786833165496932,0.798718935717348,0.805103685...
47 529550,0.802634940849533,0.801598645011175,0.78608838...
48 7524569,0.776596912840933,0.767880111293073,0.7484587...
49 51498765,0.737187298271561,0.724400980387816,0.713740...
50 363550526,0.709249314247855,0.715390882106700,0.71448...
51 6482896382,0.719886109135885]';
52 CM_Base2=...

```

```

53 [-0.00241933648422381;-0.000994749356042714;0.00052513...
54 8889181397;0.000531995120895268;-0.000127610521605613;...
55 -0.00112181497128817;-0.00238738588975404;-0.004014823...
56 77348298;-0.00458591893002119;-0.00447507033838957;-0.0...
57 0570421624022764;-0.00639759228464273;-0.006060593543...
58 11681;-0.00452373994614179;-0.00254238263866779;-0.000...
59 802608455539601;0.000686585846786974;0.0019224715481...
60 3012;0.00305034068341110;0.00384085470805589;0.0046514...
61 9185638424;0.00533251814807207;0.00492217834961218;0.0...
62 0390892393185356;0.00131507381415635;-0.0018753227054...
63 2222;-0.00563731602852632;-0.0109907490359497;-0.016914...
64 9235037892;-0.0248236615415000;-0.0317363120696212;-0.0...
65 393746528162185;-0.0435606742506112;-0.043896906122957...
66 7;-0.0457089065451211;-0.0471099572765705;-0.04925656335...
67 62850;-0.0525805261396649;-0.0556579516727002;-0.0595181...
68 996791140;-0.0641550435894548;-0.0701361258272115];
69
70
71 Alpha_BLF_1=alpha+...
72 [-8.06594564259070;-7.14241231732519;-6.03905594741620;...
73 -5.01406378048430;-3.98721923601549;-2.87195351727540;...
74 -1.85058803650554;-0.831110322743736;0.275151806711067;...
75 1.29346471552093;2.31597900276951;3.42813304789199;...
76 4.45108375100950;5.55684707512697;6.57167414343638;...
77 7.58705903612775;8.69009006482263;9.70504580065541;...
78 10.7161174843277;11.2642436005670;11.8166774071110;...
79 12.2766843085277;12.8266085308312;13.3790159996166;...
80 13.8375751427264;14.3856475805125;14.9354617926899;...
81 15.3929723623862;15.9414105042531;16.4688861494385;...
82 16.9094889255359;17.4240418013865;17.9837233404080;...
83 18.4646453036484;18.9881016785306;19.5209239626320;...
84 20.0480920643511;20.4921008071506;21.0161537952655;...
85 21.5513155912465;21.9819661259102;22.4844514540255;...
86 23.0266031504895;23.4649469590941;23.9788010755111;...
87 24.4993216153161;24.9404098936923;25.4654301290090;...
88 25.9851110721517;26.4294113964856;26.9572368515206;...
89 27.4879036272060;27.9159749086103;28.4552397489093;...
90 28.9719941570135;29.4032901602970;29.9353877441201;...
91 30.4579590792370;30.8794429116547;31.4044874140582;...
92 31.9278672633083;32.3622515736385;32.8915967016012];
93 CD_BLF_1=...
94 [0.0331859562592513;0.0285589439023825;0.0225065331772370;...
95 0.0189468223940387;0.0158403087605802;0.0131311169034887;...
96 0.0122527914619488;0.0124686038531358;0.0121007596222725;...
97 0.0139941157444537;0.0168024120917713;0.0202655564151916;...
98 0.0245968486909978;0.0291105237603469;0.0348275369759939;...
99 0.0415565640185381;0.0491966039352059;0.0596374268695133;...
100 0.0712235463740903;0.0783859677428014;0.0880240892437888;...
101 0.0983355252004903;0.108101954523449;0.118749897647422;...
102 0.128576970063239;0.140223144052195;0.152845063683076;...
103 0.165098099722719;0.178263738604623;0.190669762413875;...
104 0.200917116172463;0.213283639422009;0.230302422336980;...
105 0.251856410673102;0.265348318598858;0.280169649171469;...
106 0.293079995746426;0.306468524342820;0.316087744265308;...
107 0.331153701240424;0.339352993468659;0.343805149187245;...
108 0.357367274638073;0.365487071651346;0.371746744842184;...
109 0.378965080879246;0.387348160309275;0.396148794017582;...
110 0.400919634435716;0.410355844881111;0.418992542285874;...

```

```

111 0.429377784632715;0.432161428908286;0.445358004857721;...
112 0.449511061662298;0.454432235165533;0.466615637205070;...
113 0.473488130419345;0.473825618553497;0.483262801297828;...
114 0.490134615871489;0.495193519187196;0.506592291154017];
115 CL_BLF_1=...
116 [-0.354173691100548,-0.309063999932849,-0.259899691306692,...
117 -0.201576490582196,-0.140228135605584,-0.0784330946201286,...
118 -0.0228956859968763,0.0306396081385506,0.0818251136500848,...
119 0.134125047245865,0.190880848861979,0.249375733204867,...
120 0.306594385654906,0.357250871754507,0.405853817460111,...
121 0.455048376575644,0.503867637134175,0.552607044125295,...
122 0.596166557862589,0.617511770875898,0.642365030513726,...
123 0.663583807519691,0.685775470178208,0.710600796703577,...
124 0.730284120516020,0.750511830740319,0.773647392520254,...
125 0.791158054932682,0.811773620986288,0.811217504491707,...
126 0.810796219594365,0.796534564440700,0.829074572567749,...
127 0.871414723998235,0.866595878432624,0.870649689280734,...
128 0.869767400527153,0.872958391535774,0.867711724905650,...
129 0.875307331477488,0.864330969244883,0.837270800264997,...
130 0.851219132828200,0.848402048276708,0.833399307819857,...
131 0.824406222320952,0.825560420849990,0.821339590367901,...
132 0.811456051420846,0.816016858774003,0.814771168240697,...
133 0.817599478203143,0.803887629919240,0.814774241132624,...
134 0.802847471376179,0.792555675655018,0.796901461921134,...
135 0.790083394307436,0.769385076296350,0.766250555705866,...
136 0.760289976252899,0.754334128100513,0.754700161457019]';
137 CM_BLF_1=...
138 [-0.00645565729432271;-0.00543366737074639;-0.00497230375830425;...
139 -0.00626840903527524;-0.00812639164827980;-0.00967798053293440;...
140 -0.00945309222782101;-0.00865038220961338;-0.00670502210461011;...
141 -0.00488751112138329;-0.00454480696604581;-0.00481732423437155;...
142 -0.00548800757156123;-0.00442664971617944;-0.00282825806744191;...
143 -0.00138620542503159;-0.000204421890390911;...
144 0.000817753587349030;0.00130240859034837;0.00109615288671430;
145 0.000464851194557061;-0.00149193626706634;-0.00380972808029311;...
146 -0.00533306500332433;-0.00620595983241655;-0.00759321564382312;...
147 -0.00870105692850148;-0.0108249745414312;-0.0129892457825265;...
148 -0.00516853422314401;-0.000189350755310846;-0.00462159855872107;...
149 -0.0191437591914945;-0.0261932152732147;-0.0251904959472022;...
150 -0.0378876638882588;-0.0478485428343769;-0.0499899927653833;...
151 -0.0545965073248441;-0.0540169594750646;-0.0642403701311685;...
152 -0.0678397210048976;-0.0669126861227226;-0.0711347448349583;...
153 -0.0673556117123620;-0.0649522888342130;-0.0668780318358190;...
154 -0.0603695865129550;-0.0637109281367164;-0.0621148519578112;...

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155 -0.0619758111857658;-0.0662567712765227;-0.0668173655521368;...
156 -0.0655033106457927;-0.0660623006320958;-0.0655506777401585;...
157 -0.0645042350127906;-0.0634239194747829;-0.0619745103601840;...
158 -0.0628071667857057;-0.0612590184216668;-0.0608586271989955;...
159 -0.0620809601781004]+0.01;
160
161 Alpha_Slot_800_JD=alpha+...
162 [-8.16532994130786;-7.15071579092200;-6.04244860884083;...
163 -5.02099510922208;-4.00074350475546;-2.89013300970893;...
164 -1.86673672339860;-0.845557601359153;0.262744376454180;...
165 0.815668234712962;1.28098830005780;1.83392968241970;...
166 2.38963009158842;2.85600354947695;3.41124262157922;...
167 3.87728372488066;4.42928798070192;5.44207749788951;...
168 6.54701850023257;7.55851760590759;8.66181167361823;...
169 9.67231113504006;10.6858135558792;11.7945702669411;...
170 12.8095448979892;13.8303756931133;14.9434105377481;...
171 15.9616233762802;16.9770125159476;18.0751112575024;...
172 19.0870816918115;20.1944651800602;21.2080328942639;...
173 22.1973387095223;23.1762140686440;24.2493579805815;...
174 25.2214289083073;26.1923382924692;27.2178579547376;...
175 28.1285669372076;29.1882477121527;30.1384264568971;...
176 31.0873604704253;32.0796152955456;33.0318609966642];...
177 CD_Slot_800_JD=...
178 [-0.00681050693390072;-0.0126543294087441;-0.0182495...
179 693770797;-0.0214166231427484;-0.0251674028323114;-0...
180 .0284813491243448;-0.0295284521703782;-0.0300352983...
181 439126;-0.0297999387101721;-0.0295720385414848;-0.02...
182 82132488021699;-0.0273310852132612;-0.026210383664...
183 1072;-0.0240278454672732;-0.0220435932508557;-0.0190...
184 684670650371;-0.0168993698727356;-0.01216566243845...
185 81;-0.00643704479454368;-0.000469991253904901;0.0068...
186 1634235048144;0.0143941708545328;0.022555795883598...
187 0;0.0335793770283875;0.0439463538650867;0.0560009143...
188 510980;0.0702808537518199;0.0848501778814416;0.10300...
189 2466782877;0.128061227791715;0.152144243602451;0.182...
190 336909797974;0.215148357201335;0.275067267157616;0.3...
191 20558261523750;0.362479685381631;0.396531037918776;...
192 0.429234176477427;0.457465813635064;0.4677768042418...
193 04;0.494369876697358;0.510196123102673;0.52428205263...
194 3874;0.518416110561748;0.533085621458722];
195 CL_Slot_800_JD=...
196 [-0.366247569549657,-0.317870438818895,-0.2634978559...
197 96289,-0.208927669846718,-0.154571608219602,-0.09771...
198 37712223667,-0.0400225453233562,0.0153172162849387,...
199 0.0686661296398034,0.0950996977124353,0.1208928993...
200 96894,0.147345053057996,0.175662782841257,0.2025731...
201 84086938,0.231462205167657,0.258020120152550,0.2834...
202 78382821840,0.328859784193542,0.379704711000120,0.4...
203 24778109798272,0.473876342402648,0.517889545618680...
204 ,0.564027033267523,0.618918797249851,0.667678243993...
205 874,0.722648579523156,0.782077615939359,0.833210844...
206 835199,0.882409908178346,0.925998118771882,0.971571...
207 395935769,1.02500675704765,1.07121349306802,1.09274...

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208 928998711,1.10322282802753,1.12034462316562,1.12360...
209 156582039,1.12456603399776,1.09117884162421,1.02935...
210 696942839,1.03220012662585,1.01223881378076,0.98989...
211 6799890378,0.921229823462180,0.903460668486540]';
212 CM_Slot_800_JD=...
213 [-0.00271428206765456;-0.00189706750827400;-0.001585...
214 10093408801;-0.00257006623435670;-0.003639827594117...
215 15;-0.00377285117644621;-0.00528002084311486;-0.0060...
216 4783914821188;-0.00542639016919631;-0.0048547859236...
217 7664;-0.00467522918668672;-0.00464200994639661;-0.00...
218 484881943788308;-0.00517612644732052;-0.00576129489...
219 607823;-0.00558567933442236;-0.00544667475420462;-0...
220 00388856835124193;-0.00257735756993069;-0.001209129...
221 76751777;0.000188843218942158;0.00126966991609235;0...
222 .00194730019213918;0.00226867902786383;0.0020075243...
223 3835763;-0.00655633847238418;-0.0191938207372223;-0.0...
224 288876484116350;-0.0402225780133489;-0.0509736602055...
225 526;-0.0593875338193712;-0.0673592849128238;-0.074871...
226 3020188131;-0.0814793195538752;-0.0864569567583774;-0...
227 .0922018627535162;-0.0947708467128809;-0.09736442547...
228 76938;-0.0959300891773638;-0.0898902740886361;-0.0917...
229 042960490281;-0.0905853919434668;-0.089976876926054...
230 0;-0.0848269056017114;-0.0859492228960141];
231
232 Alpha_Slot_1000_JD=alpha+...
233 [-8.19296176515518;-7.17933574587292;-6.07141593961330;...
234 -5.05068766637736;-4.01478390175705;-2.90376884270189;...
235 -1.88070289398938;-0.858610138673839;0.251892829170128;...
236 0.805045079373169;1.27096880298182;1.82550033419823;...
237 2.29328670403366;2.84752853218911;3.40257829519855;...
238 3.86968238230243;4.42287620882581;5.43862308343971;...
239 6.54573182715474;7.55713986284914;8.66098722550410;...
240 9.67236449623901;10.6852903591628;11.7936837267243;...
241 12.8112788281600;13.8329825727792;14.9471087553110;1...
242 5.9664578225023;16.9791398538928;18.0817616704432;...
243 19.0886948118036;20.1847033352771;21.2029090750168;...
244 22.2183661266420;23.2279674798223;24.3299915044846;...
245 25.3283955867359;26.3157875287581;27.3957186622302;...
246 28.3760532549829;29.4314555943111;30.3576518649962;...
247 31.2810950601421;32.2836331725416;33.2135410784349];
248 CD_Slot_1000_JD=...
249 [-0.0193797893655357;-0.0259114877416335;-0.03258667...
250 37823424;-0.0372877316448054;-0.0409895595179842;-0.0...
251 451211540031038;-0.0465323825799716;-0.046985848615...
252 9102;-0.0470235007266426;-0.0471019968699758;-0.04558...
253 46122476344;-0.0447892744155420;-0.0432186377043500;...
254 -0.0416831615990399;-0.0400375162366334;-0.037384285...
255 6392081;-0.0350786936687696;-0.0303777956122959;-0.02...
256 17416728583107;-0.0157560312384841;-0.00811648099009...
257 559;-0.000582397437687672;0.00780414749527014;0.0186...
258 951181907445;0.0294869235072628;0.0417640755961384;...
259 0.0566192455906378;0.0718139381421382;0.08864026042...
260 94024;0.109696609944029;0.131368096438492;0.15524846...
261 0024663;0.184343329546123;0.215847194077492;0.248784...
262 760521435;0.293162365698196;0.352499161384842;0.4063...
263 87379826736;0.458282454622353;0.500207681789809;0.54...
264 2355888075449;0.570273045623037;0.586548858269573;...
265 0.595084080898688;0.601632791661711];

```

```

266 CL_Slot_1000_JD=...
267 [-0.395553132478767,-0.348223986795931,-0.29421982134...
268 7971,-0.240418790630072,-0.169462472469212,-0.1121755...
269 65857211,-0.0548346870548746,0.00147404922605309,0.05...
270 71572729111181,0.0838330672852779,0.110266492551626,...
271 0.138405114959061,0.166814012293967,0.19358481061487...
272 2,0.222273055606256,0.249958342381286,0.2766782314731...
273 33,0.325196125920342,0.378340100431535,0.423316912878...
274 281,0.473001955093872,0.517946139059006,0.56347214502...
275 0504,0.617978556741035,0.669517203304557,0.7254133653...
276 91840,0.785999845181785,0.838338127376218,0.884666105...
277 104343,0.933051366361309,0.973282227247636,1.01465360...
278 923606,1.06577930934517,1.11505039826875,1.1581110922...
279 4280,1.20586235163683,1.23704752376115,1.255492945757...
280 42,1.27981308396896,1.29183424562026,1.29013981004425...
281 1.24474333567583,1.19536645118314,1.13760565033506,1.0...
282 9614563559966]';
283 CM_Slot_1000_JD=...
284 [0.00507017714348937;0.00614418826676139;0.006842971...
285 85030537;0.00699513112022954;0.00437741572681731;0.0...
286 0282945856269266;0.00113340818135327;0.000333189608...
287 933874;0.000586231571137447;0.000924799225952278;0.0...
288 00824185731205280;0.000767407000762050;0.0003493200...
289 57341334;-0.000162324801487116;-0.00074296932765326...
290 5;-0.00125212658580521;-0.00147376228469160;-0.001264...
291 98499510802;0.00179972763032268;0.00314076315957652...
292 ;0.00435342405830659;0.00526227344420236;0.006221210...
293 03062758;0.00675959969365219;0.00639421820758831;-0...
294 00220469951161398;-0.0136034339227159;-0.0230183035...
295 253696;-0.0325897625335028;-0.0410750732024380;-0.046...
296 7011262564439;-0.0522773449139122;-0.05960919917759...
297 88;-0.0671714951745267;-0.0740194214401699;-0.0823273...
298 039146220;-0.0909191500060944;-0.0970089485628756;...
299 -0.103913781913880;-0.108509186502984;-0.11207993050...
300 2852;-0.109408392847778;-0.105477991507032;-0.101058...
301 260651483;-0.0975542197429547];
302
303 %% Import Kestrel Data
304 AoA = [0 10 14 16 18 20 22 24 26 28 30 32];
305
306 [AoA_0] = importdata('0_forces.dat',' ',23);
307 [AoA_10] = importdata('10_forces.dat',' ',23);
308 [AoA_14] = importdata('14_forces.dat',' ',23);
309 [AoA_16] = importdata('16_forces.dat',' ',23);
310 [AoA_18] = importdata('18_forces.dat',' ',23);
311 [AoA_20] = importdata('20_forces.dat',' ',23);
312 [AoA_22] = importdata('22_forces.dat',' ',23);
313 [AoA_24] = importdata('24_forces.dat',' ',23);
314 [AoA_26] = importdata('26_forces.dat',' ',23);
315 [AoA_28] = importdata('28_forces.dat',' ',23);
316 [AoA_30] = importdata('30_forces.dat',' ',23);
317 [AoA_32] = importdata('32_forces.dat',' ',23);
318
319 Opt_Config = {AoA_0, AoA_10, AoA_14, AoA_16, AoA_18, AoA_20,
    AoA_22, AoA_24, AoA_26, AoA_28, AoA_30, AoA_32};
320 %% Axial Forces
321 Iter = 1000; %Number of iterations to average over
322 k = 0;

```

```

323 for i = 1:length(Opt_Config)
324     I = Opt_Config{i};
325     k=k+1;
326     fx_I = mean(I.data(([length(I.data)-Iter:end]),33)); %
        Time Avg at 33
327     fx(:,k) = fx_I;
328 end
329 fx_3_check = mean(AoA_14.data(([length(AoA_14.data)-Iter:end]),
    ,33));
330
331 %% Vertical Forces
332 k = 0;
333 for j = 1:length(Opt_Config)
334     J = Opt_Config{j};
335     k=k+1;
336     fy_J = mean(J.data(([length(J.data)-Iter:end]),34)); %
        Time Avg at 34
337     fy(:,k) = fy_J;
338 end
339 fy_3_Check = mean(AoA_14.data(([length(AoA_14.data)-Iter:end]),
    ,34));
340
341 %% Moment about the z-axis
342 x_cor = -1.28; % Correction for incorrect location of Moment
    Reference point in CFD Settings
343 k = 0;
344 for e = 1:length(Opt_Config)
345     E = Opt_Config{e};
346     k=k+1;
347     Mz_E = mean(E.data(([length(E.data)-Iter:end]),38))/x_cor;
        % Time Avg at 38
348     Mz(:,k) = Mz_E;
349 end
350 Mz_3_Check = mean(AoA_14.data(([length(AoA_14.data)-Iter:end
    ],38))/x_cor;
351
352 %% Lift
353 k = 0;
354 for p = 1:length(Opt_Config)
355     FX_L = fx(p);
356     FY_L = fy(p);
357     AoA_L = AoA(p);
358     k=k+1;
359     L_P = FY_L*cosd(AoA_L)-FX_L*sind(AoA_L);
360     L(:,k) = L_P;
361 end
362 L_3_Check = fy(:,3)*cosd(AoA(3))-fx(:,3)*sind(AoA(3));
363
364 %% Drag
365 k = 0;
366 for q = 1:length(Opt_Config)
367     FX_D = fx(q);
368     FY_D = fy(q);
369     AoA_D = AoA(q);
370     k=k+1;
371     D_P = FX_D*cosd(AoA_D)+FY_D*sind(AoA_D);
372     D(:,k) = D_P;
373 end

```

```

374 D_3_Check = fx(:,3)*cosd(AoA(3))+fy(:,3)*sind(AoA(3));
375
376 %% Pitching Moment
377 x_cm = 1.3; % in - Estimated distance from Aero Center
378 MomRef_L = 1; % in - NA
379 % PM_0 = (Mz_0/MomRef_L)-(L_0*cosd(0)*x_cm)+(D_0*-sind(0)*
    x_cm);
380 k = 0;
381 for z = 1:length(Opt_Config)
382     L_PM = L(z);
383     D_PM = D(z);
384     Mz_PM = Mz(z);
385     AoA_PM = AoA(z);
386     k=k+1;
387     PM_Z = (Mz_PM/MomRef_L)-(L_PM*cosd(AoA_PM)*x_cm)+(D_PM*-
        sind(AoA_PM)*x_cm);
388     PM(:,k) = PM_Z;
389 end
390 PM_3_Check = (Mz(:,3)/MomRef_L)-(L(:,3)*cosd(AoA(3))*x_cm)+(D
    (:,3)*-sind(AoA(3))*x_cm);
391
392 %% Coeffiecient of Lift
393 k = 0;
394 for v = 1:length(Opt_Config)
395     L_CL = L(v);
396     k=k+1;
397     CL_V = (L_CL*2)/(0.67764*0.0009518*((3751.5/12)^2));
398     CL(:,k) = CL_V;
399 end
400 CL_3_Check = (L(:,3)*2)/(0.67764*0.0009518*((3751.5/12)^2));
401
402 %% Coeffiecient of Drag
403 % CD_0 =(D_0*2)/(0.67764*0.0009518*((3751.5/12)^2));
404 k = 0;
405 for w = 1:length(Opt_Config)
406     D_CD = D(w);
407     k=k+1;
408     CD_W = (D_CD*2)/(0.67764*0.0009518*((3751.5/12)^2));
409     CD(:,k) = CD_W;
410 end
411 CD_3_Check = (D(:,3)*2)/(0.67764*0.0009518*((3751.5/12)^2));
412
413 %% Moment Coeffiecient
414 c_bar = 9.66;
415 % CM_0 =(PM_0*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar);
416 k = 0;
417 for x = 1:length(Opt_Config)
418     PM_CM = PM(x);
419     k=k+1;
420     CM_X = (PM_CM*2)/(0.67764*0.0009518*((3751.5/12)^2)*c_bar)
        ;
421     CM(:,k) = CM_X;
422 end
423 CM_3_Check =(PM(:,3)*2)/(0.67764*0.0009518*((3751.5/12)^2)*
    c_bar);
424
425 %% CD, CL, CM vs Alpha Plots
426 figure(1)

```

```

427 hold on
428 plot(Alpha_Baseline2,CD_Base2, 'k', 'LineWidth',0.9)
429 plot(Alpha_BLF_1,CD_BLF_1,'Color', [0.25 0.80 0.54], '
    LineWidth',0.9)
430 plot(Alpha_Slot_800_JD,CD_Slot_800_JD, 'm', 'LineWidth',0.9)
431 plot(Alpha_Slot_1000_JD,CD_Slot_1000_JD, 'LineWidth',0.9)
432 plot(AoA,CD,'b--o','LineWidth',0.9)
433 colororder([0.9290 0.6940 0.1250]) % Marker with no color
    assigned is Orange
434 grid on
435 xlabel('\alpha (deg)')
436 ylabel('C_D (-)')
437 xlim([0 32])
438 ylim([-0.06 0.6])
439 hold off
440 legend('Baseline WT','BLF WT','AFC Slot WT, C\mu=7.82%','AFC
    Slot WT, C\mu=12.22%','AFC Slot CFD Opt Config C\mu=7.33','
    Location','northwest')
441
442
443 figure(2)
444 hold on
445 plot(Alpha_Baseline2,CL_Base2, 'k', 'LineWidth',0.9)
446 plot(Alpha_BLF_1,CL_BLF_1,'Color', [0.25 0.80 0.54], '
    LineWidth',0.9)
447 plot(Alpha_Slot_800_JD,CL_Slot_800_JD, 'm', 'LineWidth',0.9)
448 plot(Alpha_Slot_1000_JD,CL_Slot_1000_JD, 'LineWidth',0.9)
449 plot(AoA,CL,'b--o','LineWidth',0.9)
450 colororder([0.9290 0.6940 0.1250]) % Marker with no color
    assigned is Orange
451 grid on
452 xlabel('\alpha (deg)')
453 ylabel('C_L (-)')
454 xlim([0 32])
455 ylim([0 1.4])
456 hold off
457 legend('Baseline WT','BLF WT','AFC Slot WT, C\mu=7.82%','AFC
    Slot WT, C\mu=12.22%','AFC Slot CFD Opt Config C\mu=7.33','
    Location','northwest')
458
459 figure(3)
460 hold on
461 plot(Alpha_Baseline2,CM_Base2, 'k', 'LineWidth',0.9)
462 plot(Alpha_BLF_1,CM_BLF_1,'Color', [0.25 0.80 0.54], '
    LineWidth',0.9)
463 plot(Alpha_Slot_800_JD,CM_Slot_800_JD, 'm', 'LineWidth',0.9)
464 plot(Alpha_Slot_1000_JD,CM_Slot_1000_JD, 'LineWidth',0.9)
465 plot(AoA,CM,'b--o','LineWidth',0.9)
466 colororder([0.9290 0.6940 0.1250]) % Marker with no color
    assigned is Orange
467 grid on
468 xlabel('\alpha (deg)')
469 ylabel('C_M (-)')
470 xlim([0 32])
471 % ylim([0 1.4])
472 hold off
473 legend('Baseline WT','BLF WT','AFC Slot WT, C\mu=7.82%','AFC
    Slot WT, C\mu=12.22%','AFC Slot CFD Opt Config C\mu=7.33',

```

```

        Location','southwest')
474
475 %% CL vs CD
476
477 figure(4)
478 hold on
479 plot(CD_Base2,CL_Base2, 'k', 'LineWidth',0.9)
480 plot(CD_BLF_1,CL_BLF_1, 'Color', [0.25 0.80 0.54], 'LineWidth',
    ,0.9)
481 plot(CD_Slot_800_JD,CL_Slot_800_JD, 'm', 'LineWidth',0.9)
482 plot(CD_Slot_1000_JD,CL_Slot_1000_JD, 'LineWidth',0.9)
483 plot(CD,CL, 'b--o','LineWidth',0.9)
484 colororder([0.9290 0.6940 0.1250]) % Marker with no color
    assigned is Orange
485 grid on
486 xlabel('C_D (-)')
487 ylabel('C_L (-)')
488 xlim([-0.05 0.51])
489 ylim([0 1.4])
490 hold off
491 legend('Baseline WT','BLF WT','AFC Slot WT, C\mu=7.82%','AFC
    Slot WT, C\mu=12.22%','AFC Slot CFD Opt Config C\mu=7.33','
    Location','southeast')
492 L_D_max = max(L./D);

```

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| <b>REPORT DOCUMENTATION PAGE</b>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |             |                                          |                                                                          |                                                                                                   | <i>Form Approved</i><br><b>OMB No. 0704-0188</b>                            |  |
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| <b>1. REPORT DATE</b> (DD-MM-YYYY)<br>25-03-2021                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |             | <b>2. REPORT TYPE</b><br>Master's Thesis |                                                                          |                                                                                                   | <b>3. DATES COVERED</b> (From — To)<br>Sept 2019 - Mar 2021                 |  |
| <b>4. TITLE AND SUBTITLE</b><br><br>Optimizing Design Parameters for Active Flow Control Boundary-Layer Fence Performance Enhancement on a Delta Wing                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |             |                                          |                                                                          | <b>5a. CONTRACT NUMBER</b>                                                                        |                                                                             |  |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |             |                                          |                                                                          | <b>5b. GRANT NUMBER</b>                                                                           |                                                                             |  |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |             |                                          |                                                                          | <b>5c. PROGRAM ELEMENT NUMBER</b>                                                                 |                                                                             |  |
| <b>6. AUTHOR(S)</b><br><br>Tedder, Nathan L., 1st Lt, USAF                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |             |                                          |                                                                          | <b>5d. PROJECT NUMBER</b>                                                                         |                                                                             |  |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |             |                                          |                                                                          | <b>5e. TASK NUMBER</b>                                                                            |                                                                             |  |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |             |                                          |                                                                          | <b>5f. WORK UNIT NUMBER</b>                                                                       |                                                                             |  |
| <b>7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)</b><br>Air Force Institute of Technology<br>Graduate School of Engineering and Management (AFIT/EN)<br>2950 Hobson Way<br>WPAFB OH 45433-7765                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |             |                                          |                                                                          |                                                                                                   | <b>8. PERFORMING ORGANIZATION REPORT NUMBER</b><br><br>AFIT-ENY-MS-21-M-322 |  |
| <b>9. SPONSORING / MONITORING AGENCY NAME(S) AND ADDRESS(ES)</b><br><br>Joint Aircraft Survivability Program Office                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |             |                                          |                                                                          |                                                                                                   | <b>10. SPONSOR/MONITOR'S ACRONYM(S)</b><br><br>JASPO                        |  |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |             |                                          |                                                                          |                                                                                                   | <b>11. SPONSOR/MONITOR'S REPORT NUMBER(S)</b>                               |  |
| <b>12. DISTRIBUTION / AVAILABILITY STATEMENT</b><br><br>DISTRIBUTION STATEMENT A:<br>APPROVED FOR PUBLIC RELEASE; DISTRIBUTION UNLIMITED.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |             |                                          |                                                                          |                                                                                                   |                                                                             |  |
| <b>13. SUPPLEMENTARY NOTES</b>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |             |                                          |                                                                          |                                                                                                   |                                                                             |  |
| <b>14. ABSTRACT</b><br>Utilizing CFD simulations, the study progressed the investigation of replicating and improving upon the performance of a NACA 0012 cropped delta-wing at high angles-of-attack with an AFC fluidic fence via wall-normal, steady blowing from an optimized single chordwise slot. Data was generated using CREATE-AV Kestrel CFD software on the DoD HPC systems. The flight regime was constant at Mach 1.18 with a Re of $5.0 \times 10^5$ , based on the $c_{root}$ , using angles-of-attack ranging from $0^\circ$ to $30^\circ$ . Experimental and CFD performance results of three configurations (baseline, passive BLF and AFC slot) were compared to validate the CFD models. Computational optimization of the AFC slot parameters (slot width, length, and jet velocity) utilized peak performance gains to justify slot enhancement. Surface flow visualization assessed the unique flow features that contribute to spanwise flow reduction and performance gains. The use of AFC techniques to replicate and improve passive flow control methods provides a solution for flow separation leading to wing stall and undesirable delta-wing moment characteristics. |             |                                          |                                                                          |                                                                                                   |                                                                             |  |
| <b>15. SUBJECT TERMS</b><br>active flow control (AFC), boundary layer fence (BLF) computational fluid dynamics (CFD), Computational Research and Engineering for Acquisition Tools and Environments-Air Vehicles (CREATE-AV), High Performance Computing (HPC), National Advisory Committee for Aeronautics (NACA), Reynolds Number (Re)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |             |                                          |                                                                          |                                                                                                   |                                                                             |  |
| <b>16. SECURITY CLASSIFICATION OF:</b>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |             |                                          | <b>17. LIMITATION OF ABSTRACT</b><br><br>UU                              |                                                                                                   | <b>18. NUMBER OF PAGES</b><br><br>179                                       |  |
| a. REPORT                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | b. ABSTRACT | c. THIS PAGE                             |                                                                          |                                                                                                   |                                                                             |  |
| U                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | U           | U                                        | <b>19a. NAME OF RESPONSIBLE PERSON</b><br>LtCol Michael Walker, AFIT/ENY |                                                                                                   |                                                                             |  |
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