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14. ABSTRACT
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15. SUBJECT TERMS
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a. REPORT UU	b. ABSTRACT UU	c. THIS PAGE UU	UU		Keith Schwab
					19b. TELEPHONE NUMBER 626-395-2986

**RPPR Final Report**  
as of 25-May-2021

Agency Code: 21XD

Proposal Number: 74781ELII

**Agreement Number: W911NF-19-1-0212**

**INVESTIGATOR(S):**

**Name:** Keith C Schwab  
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**Principal:** Y

Organization: **California Institute of Technology**

Address: Office of Sponsored Research, Pasadena, CA 911250001

Country: USA

DUNS Number: 009584210

EIN: 951643307

**Report Date:** 14-Jan-2020

Date Received: 20-May-2021

**Final Report** for Period Beginning 15-Mar-2019 and Ending 14-Dec-2019

**Title:** Investigation of Unexpected Transport of Superfluid Helium Through Graphene

**Begin Performance Period:** 15-Mar-2019

**End Performance Period:** 14-Dec-2019

**Report Term:** 0-Other

Submitted By: Keith Schwab

Email: schwab@caltech.edu

Phone: (626) 395-2986

**Distribution Statement:** 1-Approved for public release; distribution is unlimited.

**STEM Degrees:** 0

**STEM Participants:**

**Major Goals:** We have observed unexpected transport of superfluid helium-4 in an apparatus designed to study superflow through nanoporous membranes. This small award was to help fund further experiments to pin down if this superflow was in fact through graphene membranes, or some artifact of the measurement system. In the end, we have been unable to make a concrete conclusion and this requires further study. The student involved in the work abandoned the experiment and the PI is currently looking for a way to continue the study.

**Accomplishments:** We performed a number of experiments to attempt to identify if the superflow was through the graphene or around some other path in the apparatus. We were unable to make a concrete conclusion.

**Training Opportunities:** A Caltech PhD student worked on this experiment and received training in low temperature physics techniques.

**Results Dissemination:** Nothing to Report

**Honors and Awards:** Nothing to Report

**Protocol Activity Status:**

**Technology Transfer:** Nothing to Report

**PARTICIPANTS:**

**Participant Type:** PD/PI

**Participant:** Keith Schwab

**Person Months Worked:** 6.00

Project Contribution:

National Academy Member: N

**Funding Support:**

**Participant Type:** Graduate Student (research assistant)

**Participant:** Anthony Ardizzi

**RPPR Final Report**  
as of 25-May-2021

**Person Months Worked:** 6.00  
Project Contribution:  
National Academy Member: N

**Funding Support:**

**Partners**

,

I certify that the information in the report is complete and accurate:  
Signature: Keith Schwab  
Signature Date: 5/20/21 5:50PM



# Transport Through 2D-Materials

Superfluid Josephson Junction

# Caltech

Anthony Ardizzi

10/15/2018

Advisor: Keith Schwab

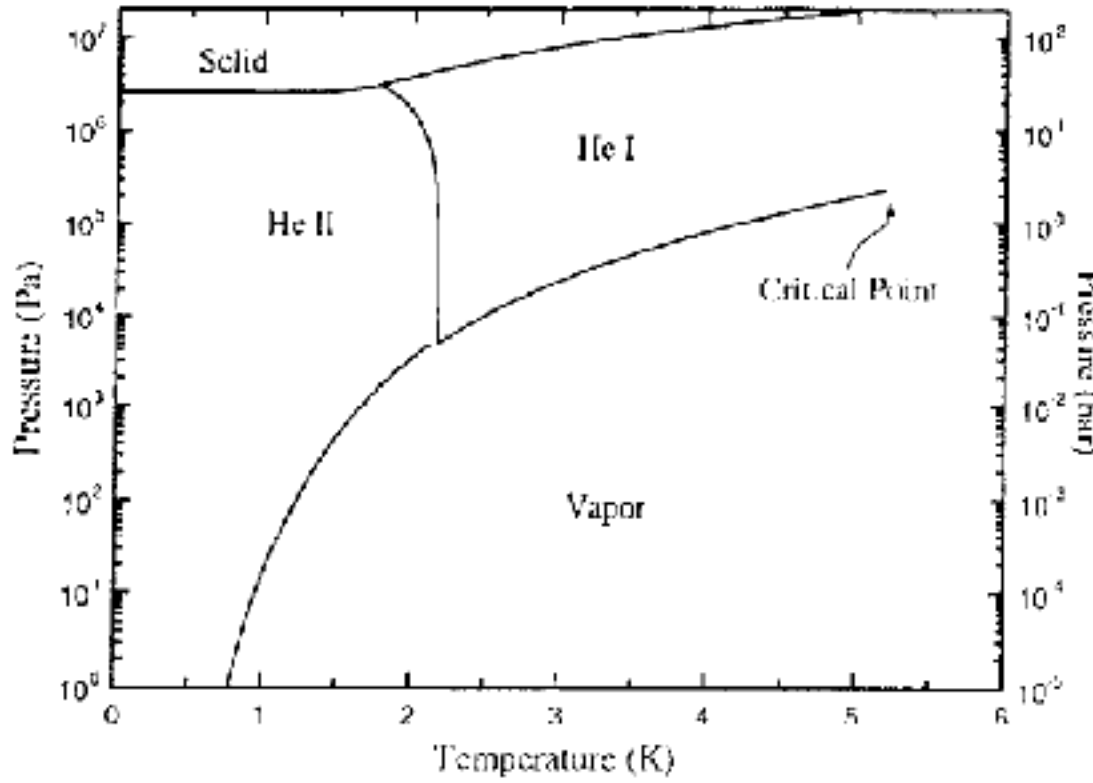
Committee Members: Keith Schwab, Stevan Nadj-Perge,  
Michael Roukes, Thomas Rosenbaum

# Outline

1. Background Physics
  - i. Helium
  - ii. Superfluids and Quantum Condensates
  - iii. Josephson Junctions
  - iv. Materials
2. Experimental Apparatus and Measurement Scheme
3. Superfluid transport data and Hydrodynamic Modelling
4. Future Directions

# Background Physics - Helium

4He Phase Diagram (Donnelly and Barenghi 1998)

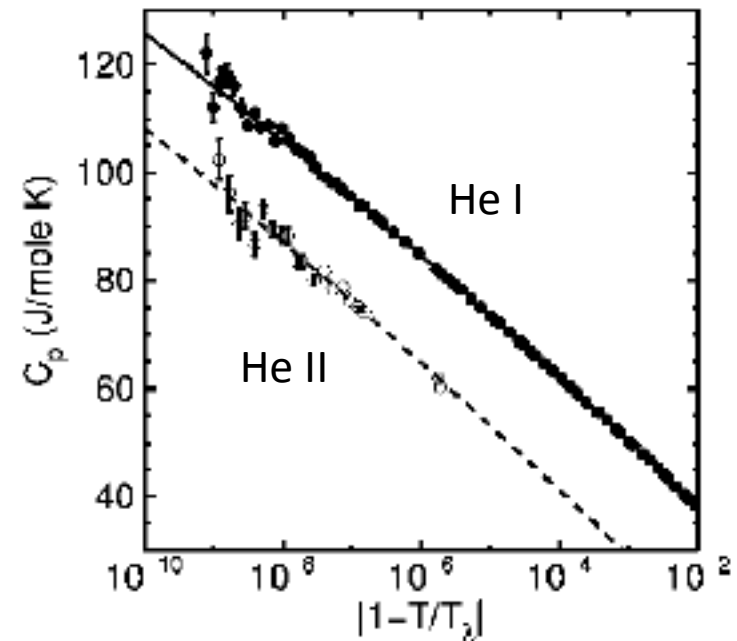
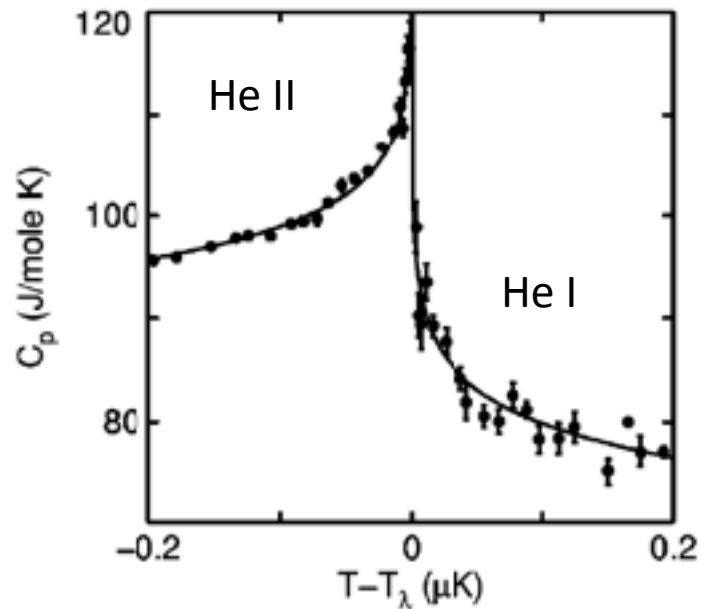


## BEC Condensation Estimate

$$T_b = \frac{2\pi\hbar^2}{m_4 k_b} \left( \frac{N}{2.612V} \right) \sim 3.1\text{K}$$

# Background Physics – Superfluids and Quantum Condensates

- $^4\text{He}$  condenses to a “superfluid” at  $T_\lambda=2.17\text{K}$



# Background Physics – Superfluids and Quantum Condensates

- Full hydrodynamic system of equations was first treated by (Landau 1941), (Landau and Lifshitz 1959) and (Khalatnikov 1965).

## Two-Fluid Model

$$\rho_s + \rho_n = \rho$$

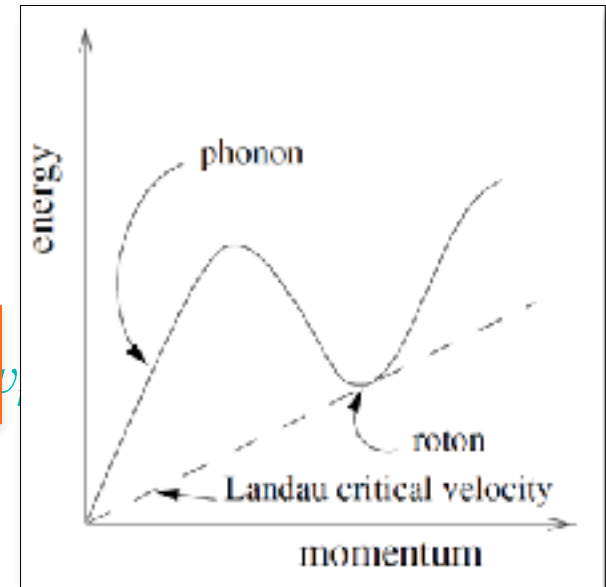
$$\rho_s \mathbf{v}_s + \rho_n \mathbf{v}_n = \mathbf{j}$$

$$\rho_s \left( \frac{\partial \mathbf{v}_s}{\partial t} + (\mathbf{v}_s \cdot \nabla) \mathbf{v}_s \right) = - \frac{\rho_s}{\rho} \nabla P + \rho_s \sigma \nabla T$$

$$\rho_n \left( \frac{\partial \mathbf{v}_n}{\partial t} + (\mathbf{v}_n \cdot \nabla) \mathbf{v}_n \right) = - \frac{\rho_n}{\rho} \nabla P - \rho_s \sigma \nabla T + \eta_n \nabla^2 \mathbf{v}_n$$

$$\text{curl}(\mathbf{v}_s) = 0$$

- The non-viscous flow was explained by the shape and sharpness of the dispersion spectrum derived by Landau



$$v_L \approx 60 \frac{\text{m}}{\text{s}}$$

# Background Physics – Superfluids and Quantum Condensates

- More complete microscopic description from (Onsager 1949), (London 1938 and 1954) and eventually Feynman (1955,1972) and (Anderson 1966).

$$\psi(\mathbf{r}, t) = \sqrt{\frac{\rho_s}{m_4}} e^{i\varphi(\mathbf{r}, t)}$$

$$v_s = \frac{\hbar}{m_4} \nabla \varphi$$

$$\hbar \frac{\partial \varphi}{\partial t} = - \frac{\partial H}{\partial N} \quad \hbar \frac{\partial N}{\partial t} = - \frac{\partial H}{\partial \varphi}$$

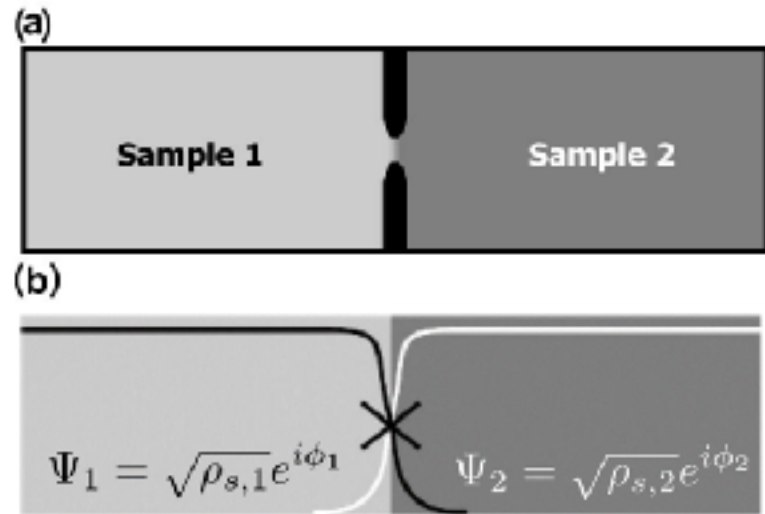
$$\frac{\partial \Delta \varphi}{\partial t} = - \frac{\Delta \mu}{\hbar}$$

Josephson Anderson Equation

# Background Physics – Josephson Junctions

- Quantum devices can follow when quantum phase can be measured -> Josephson Junction

$$\begin{aligned}\hbar \frac{\partial \psi_1}{\partial t} &= \mu_1 \psi_1 + K \psi_2 \\ \hbar \frac{\partial \psi_2}{\partial t} &= \mu_2 \psi_2 + K \psi_1\end{aligned}$$



DC Josephson Equation:  $I = I_0 \sin \Delta\phi$

Josephson Anderson Equation:  $\frac{d\Delta\phi}{dt} = -\frac{\Delta\mu}{\hbar}$

Josephson Frequency:

$$f_J = \frac{\Delta\mu}{\hbar}$$

# Background Physics – Josephson Junctions

## Superconductivity

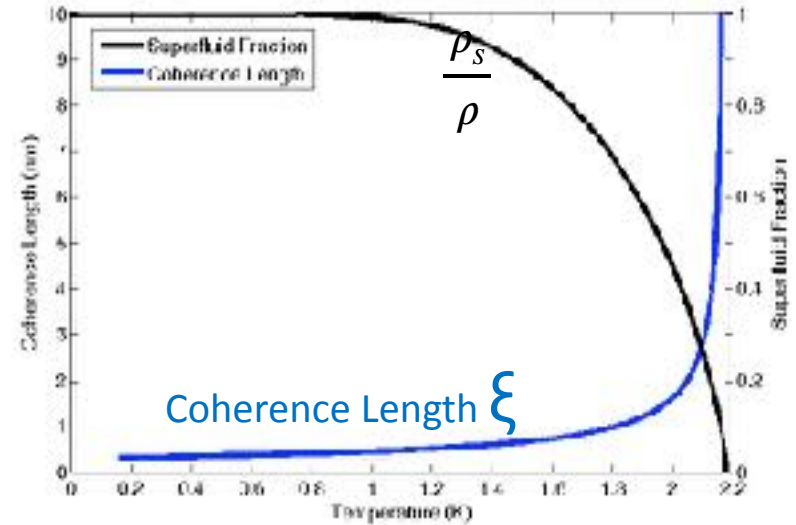
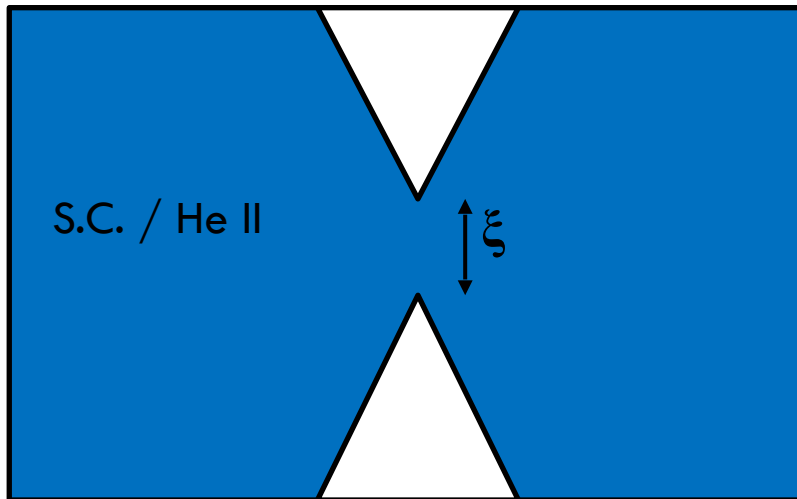
- Macroscopic Quantum System
- Zero Electrical Resistance
- Electrical Current
- Chemical Potential (Voltage)
- Critical Current Density
- **SQUIDs, Qubits**
- **Quantum Tunnelling of Cooper Pairs**
  - Cooper pair mass  $2m_e$
  - Barrier Energy  $E_b \approx 1\text{eV}$

## Superfluidity

- Macroscopic Quantum System
- Zero Viscosity
- Mass Current
- Chemical Potential (Pressure)
- Critical Flow Velocity
- **SHeQUIDS, Gyroscopes... Qubits?**
- **4He Particles too massive to tunnel**
  - Helium mass  $m_4 \approx 7000m_e$
  - Graphene barrier  $E_G \approx 20\text{eV}$

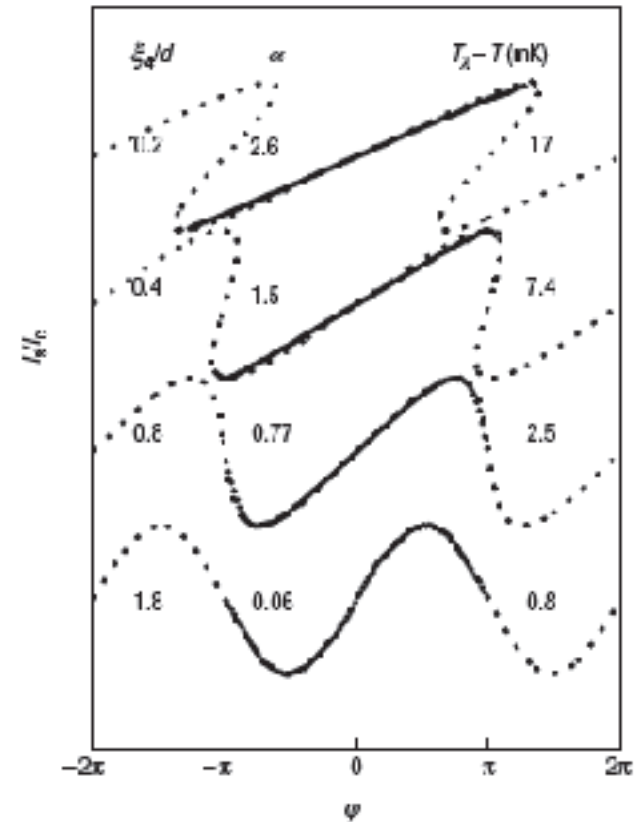
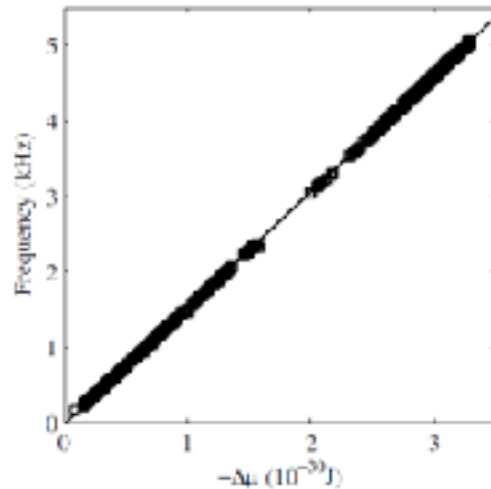
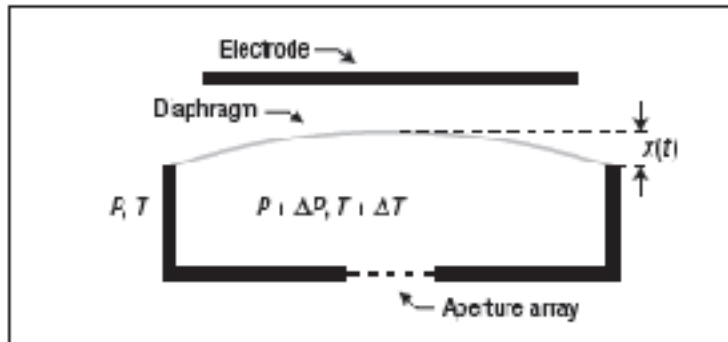
# Background Physics – Josephson Junctions

- Leads to “Dayem Bridge” junction design for superfluids



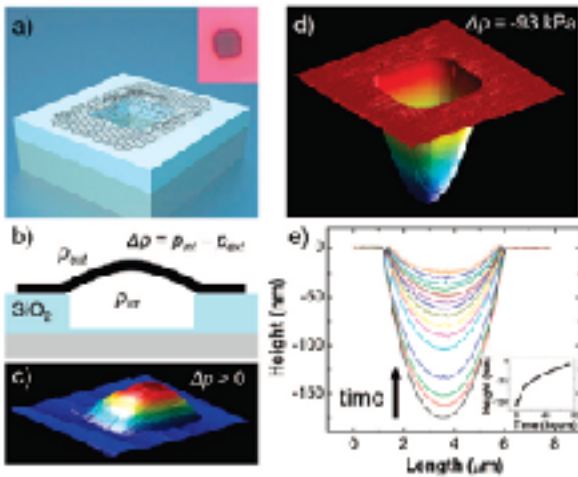
# Background Physics – Josephson Junctions

- Josephson oscillations have been observed in superfluid  $^4\text{He}$ , only within  $\sim 10\text{mK}$  of  $T_\lambda$



# Background Physics – Materials: Graphene

- Graphene appears to be completely impermeable to all atomic matter
  - WKB approximation, 20eV barrier  $\rightarrow$  tunneling suppression by  $\sim e^{-500}$  for conservative barrier parameters



(2008 Bunch et al)

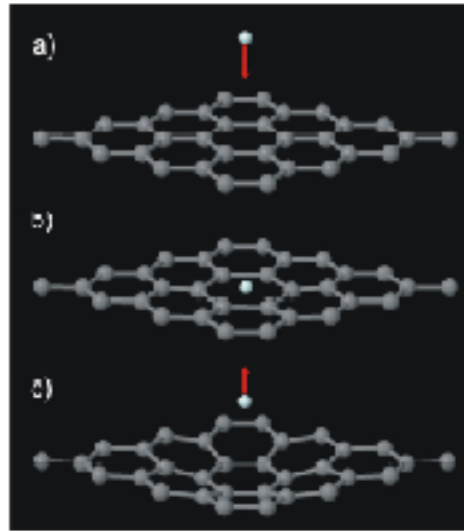
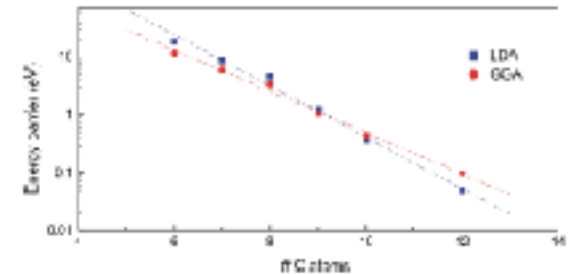
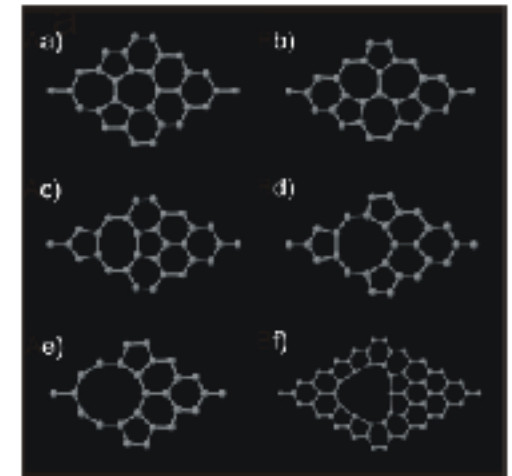


FIG. 2. (Color online) Reflection of a He atom with a kinetic energy of 18.0 eV from a graphene surface. a) The He atom approaches the perfect graphene layer. b) The He atom comes to rest before penetrating the graphene layer. Note that the relaxation of the graphene layer is very small at this moment. c) The He atom is reflected back and the surface starts to relax.



(2008 Leenaerts et al)

# Background Physics – Materials: Carboxy Fantrip

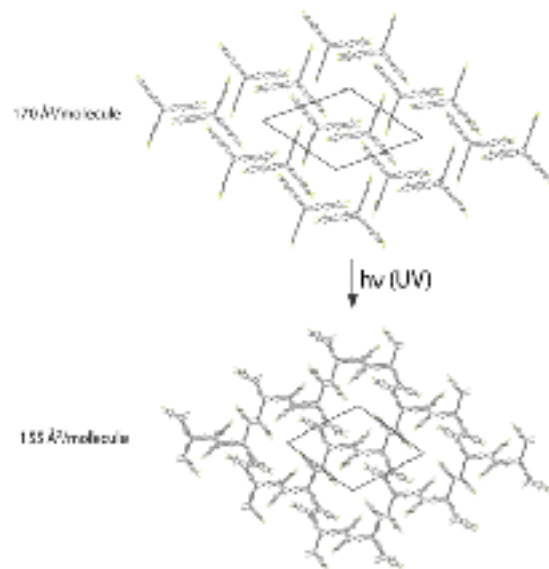


Figure 3.7. Change of MMA upon polymerization on carboxy fantrip.

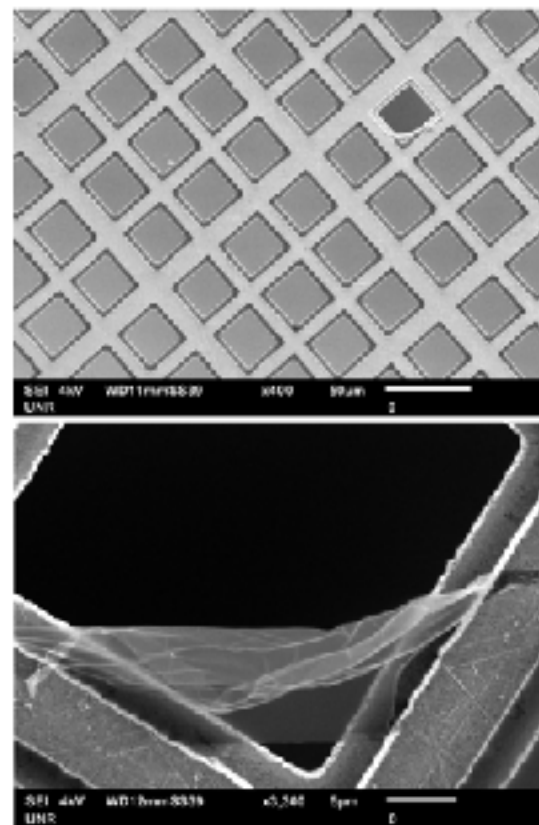
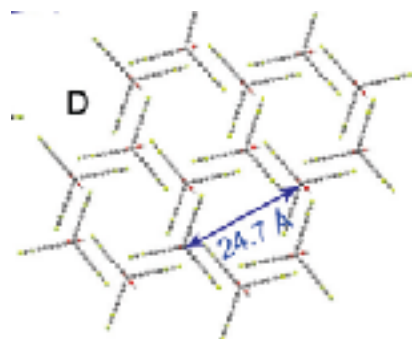
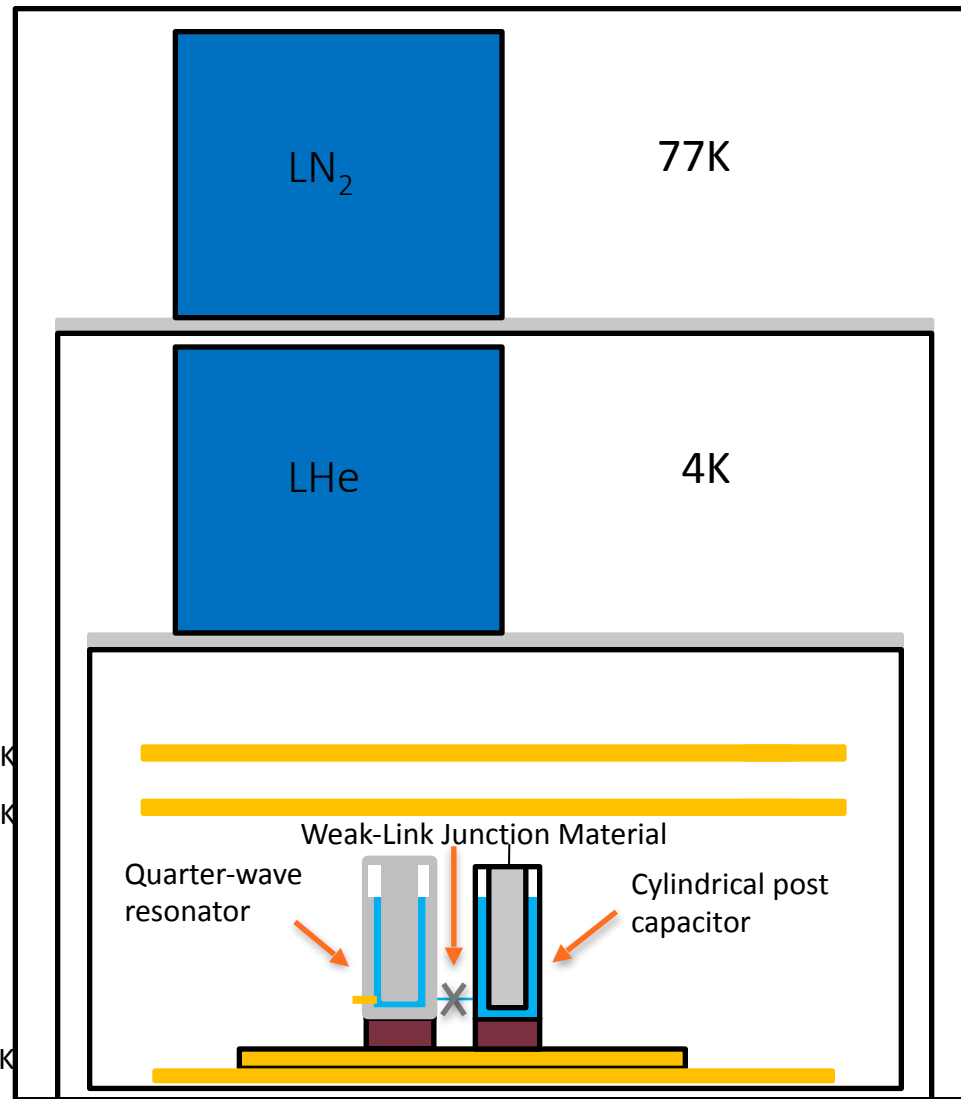


Figure 3.11. SEM images of poly(carboxy fantrip) spanning  $25 \times 25 \mu\text{m}^2$  holes on a TEM grid.

# Outline

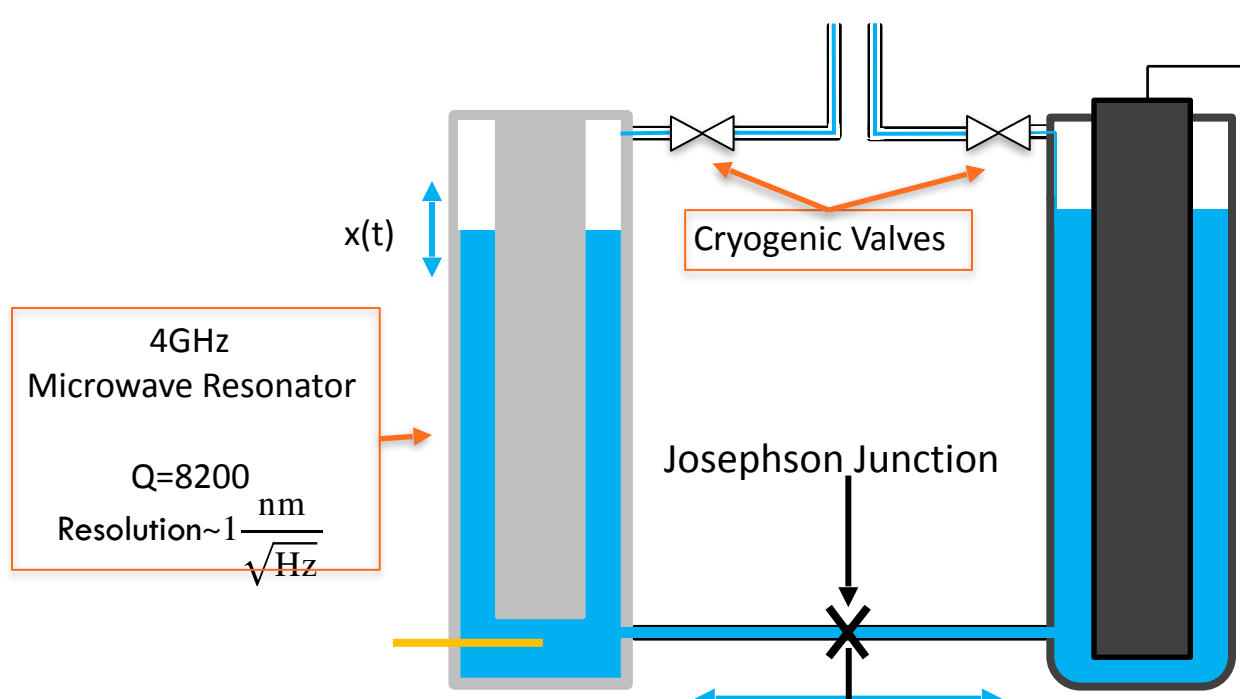
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# Experimental Apparatus and Measurement Scheme - Cryogenics



coiled  
pumped

# U-Tube Liquid Level Meter

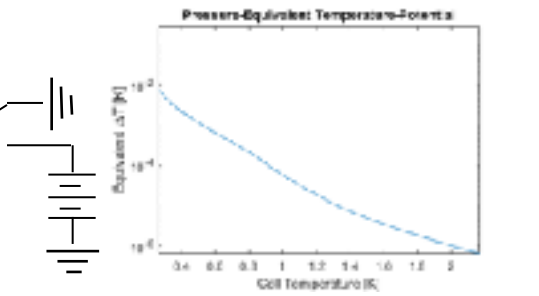


4GHz  
Microwave Resonator

$Q=8200$   
Resolution  $\sim 1 \frac{\text{nm}}{\sqrt{\text{Hz}}}$

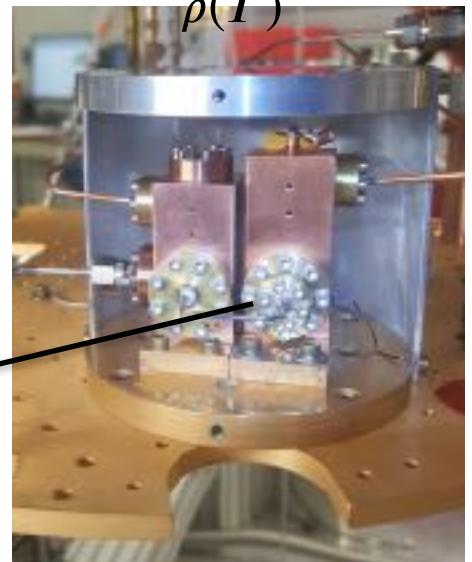
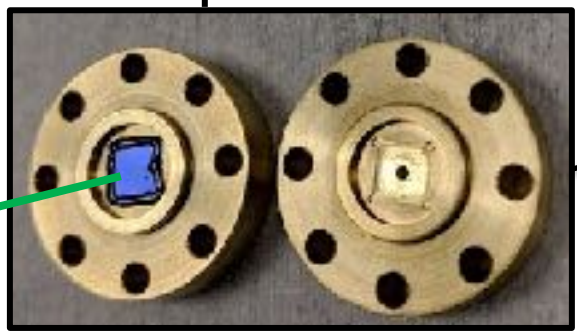
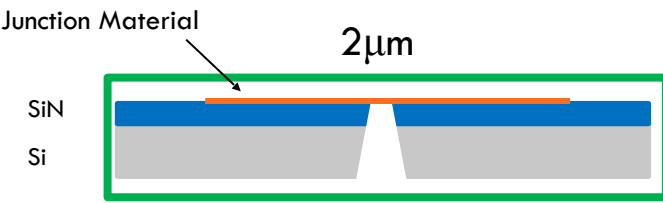
Cryogenic Valves

Josephson Junction



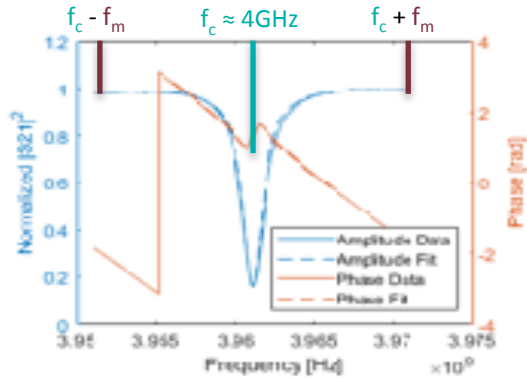
Capacitor  
 $V=100\text{V}$   $\longleftrightarrow$   $\Delta x=20\mu\text{m}$

$\Delta P=0.1\text{Pa}$   $\longleftrightarrow$   $\Delta T=1\mu\text{K}$   
When  $T=1.5\text{K}$

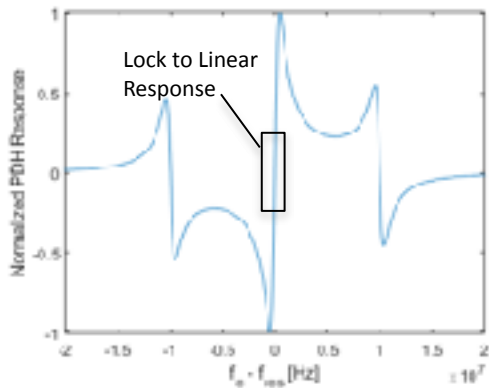
$$\frac{\Delta P}{\rho(T)} = s(T) \Delta T$$


# Experimental Apparatus and Measurement Scheme – PDH Microwave Scheme

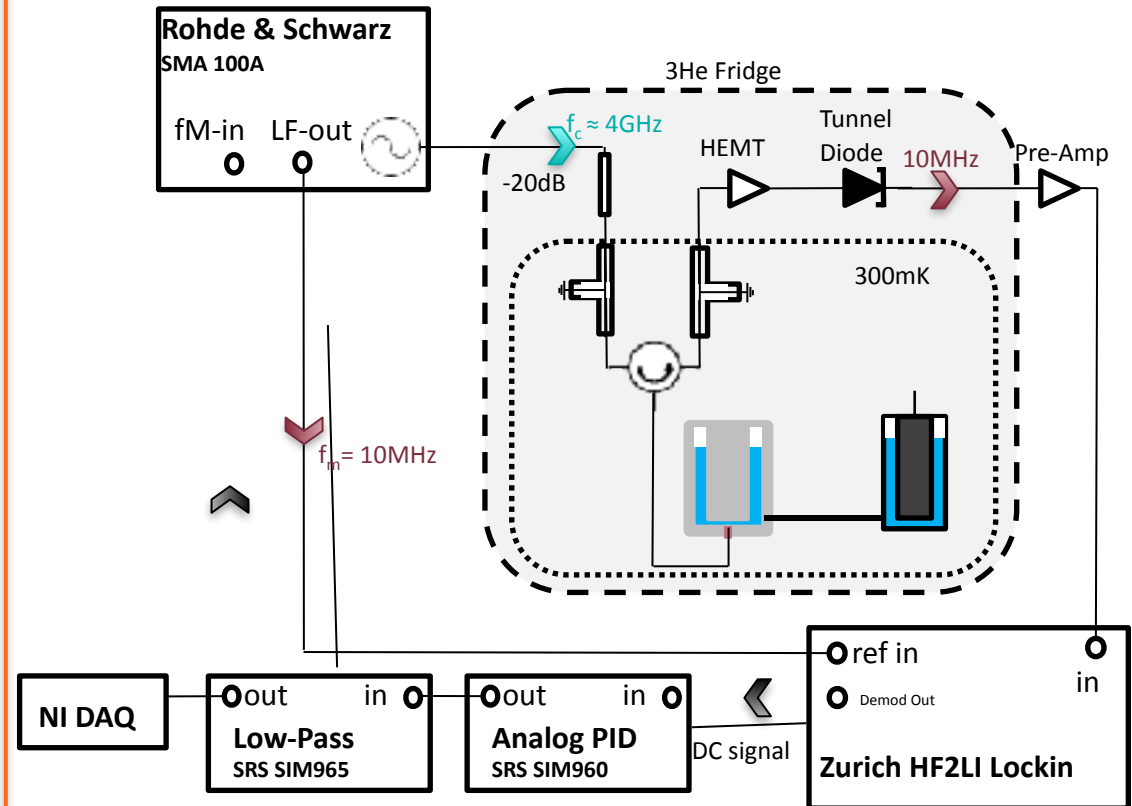
## Pound-Drever-Hall



## Typical PDH Response



## PDH PID Circuit

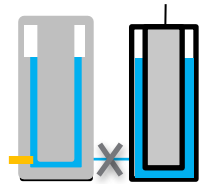
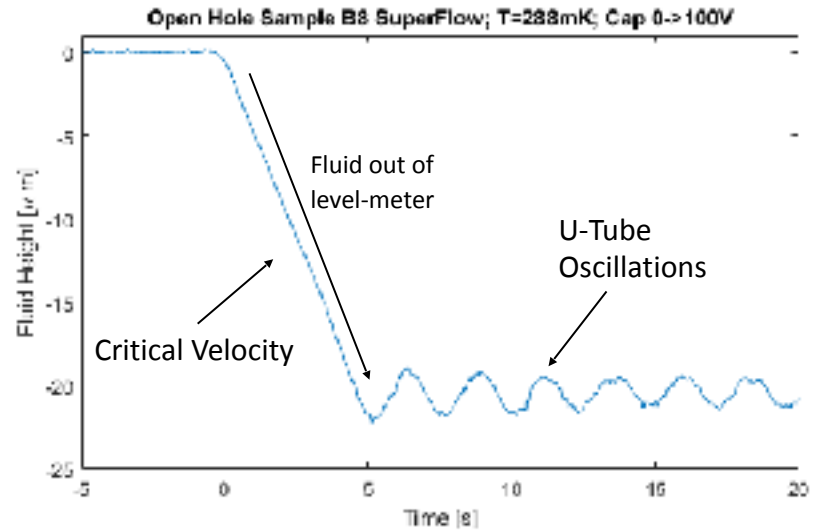
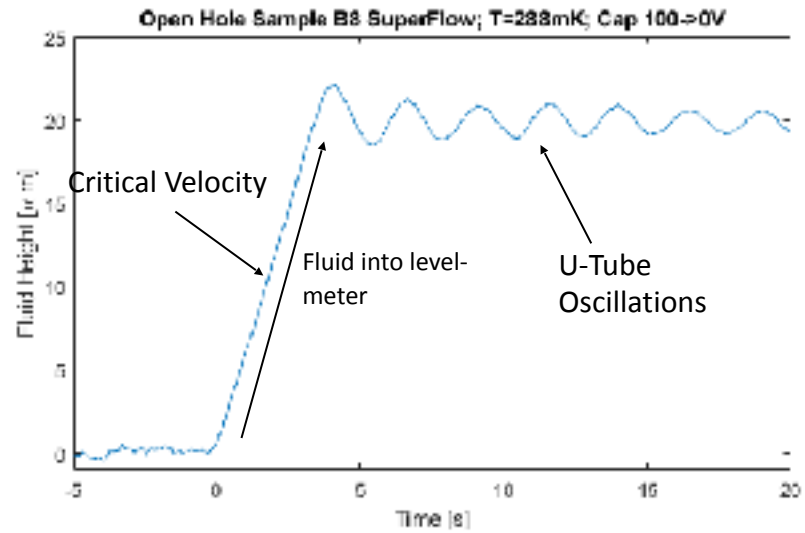
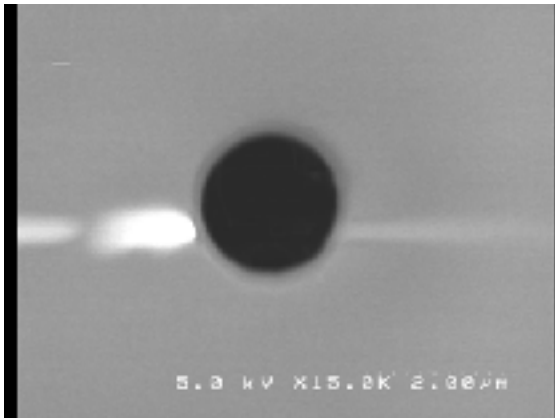
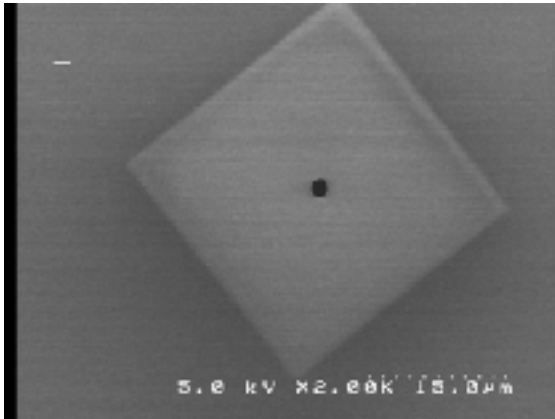


# Outline

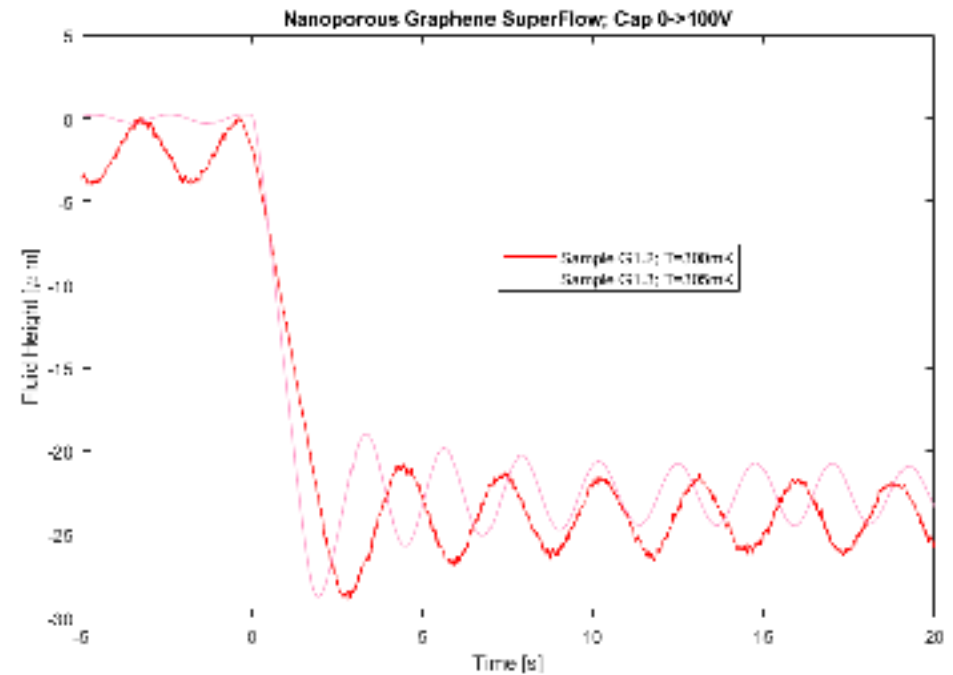
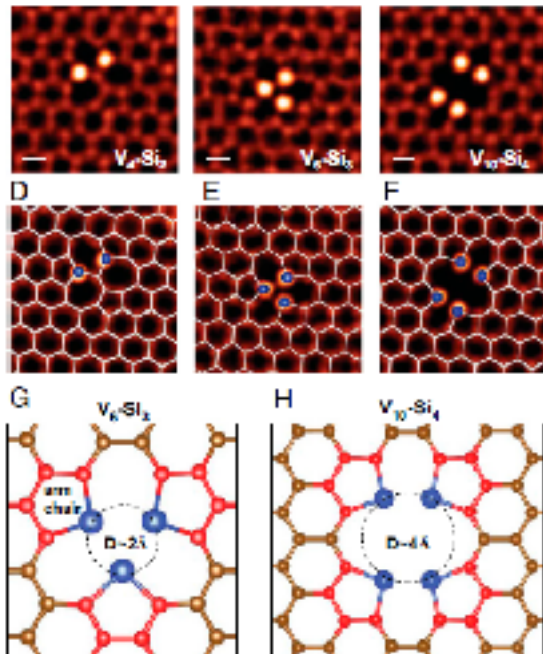
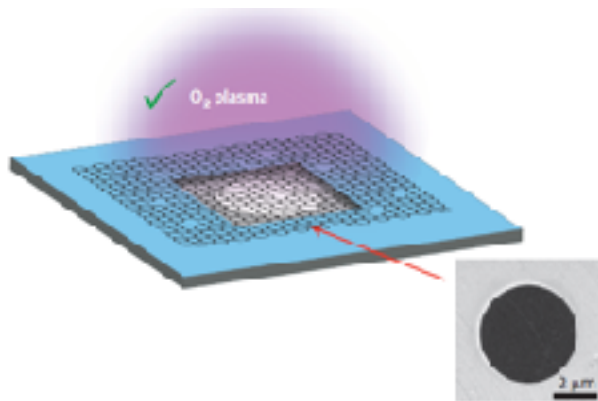
1. Background Physics
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# Transient Data - 2 $\mu\text{m}$ diameter hole

SEM Images



# Transient Data – Nanoporous Graphene



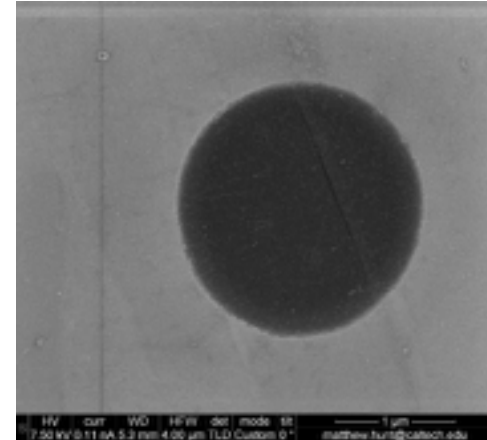
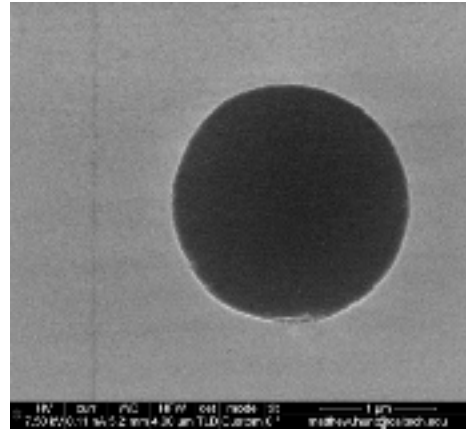
Lee et al, Proc Natl Acad Sci USA 2014  
Sumedh et al, Nature Nanotech 2015

# SEM Before and After Measurement (all at Caltech)

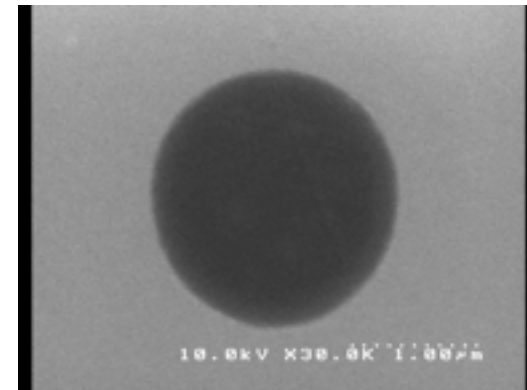
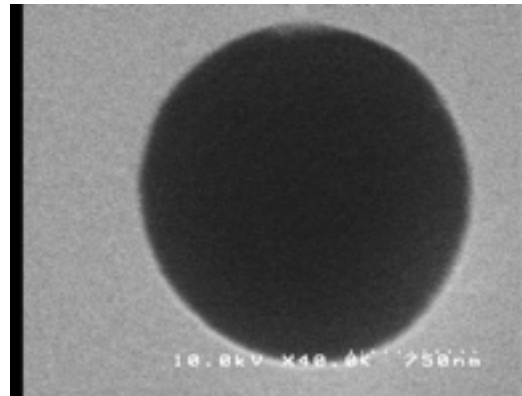
**Sample G1.2**

**Sample G1.3**

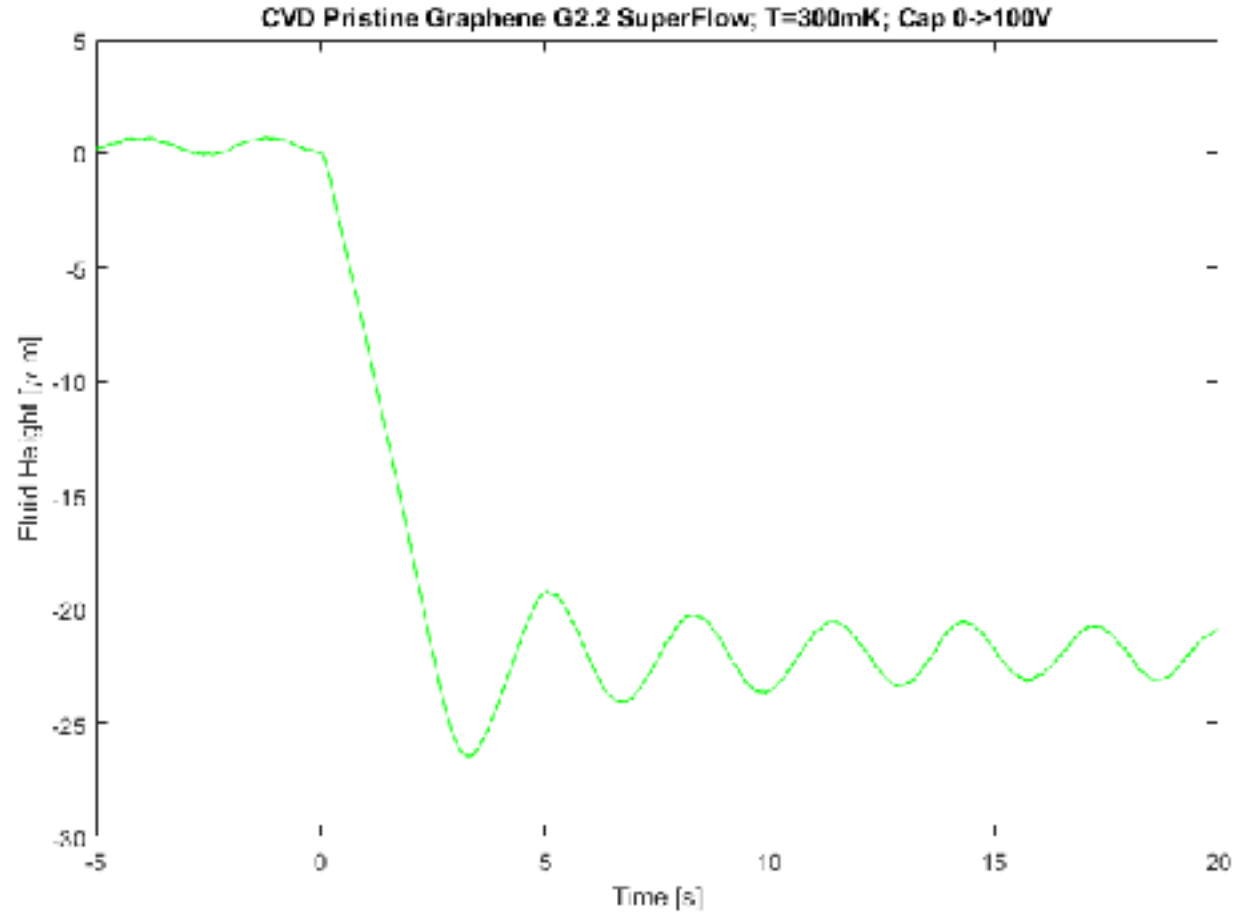
**Before Cooldown**



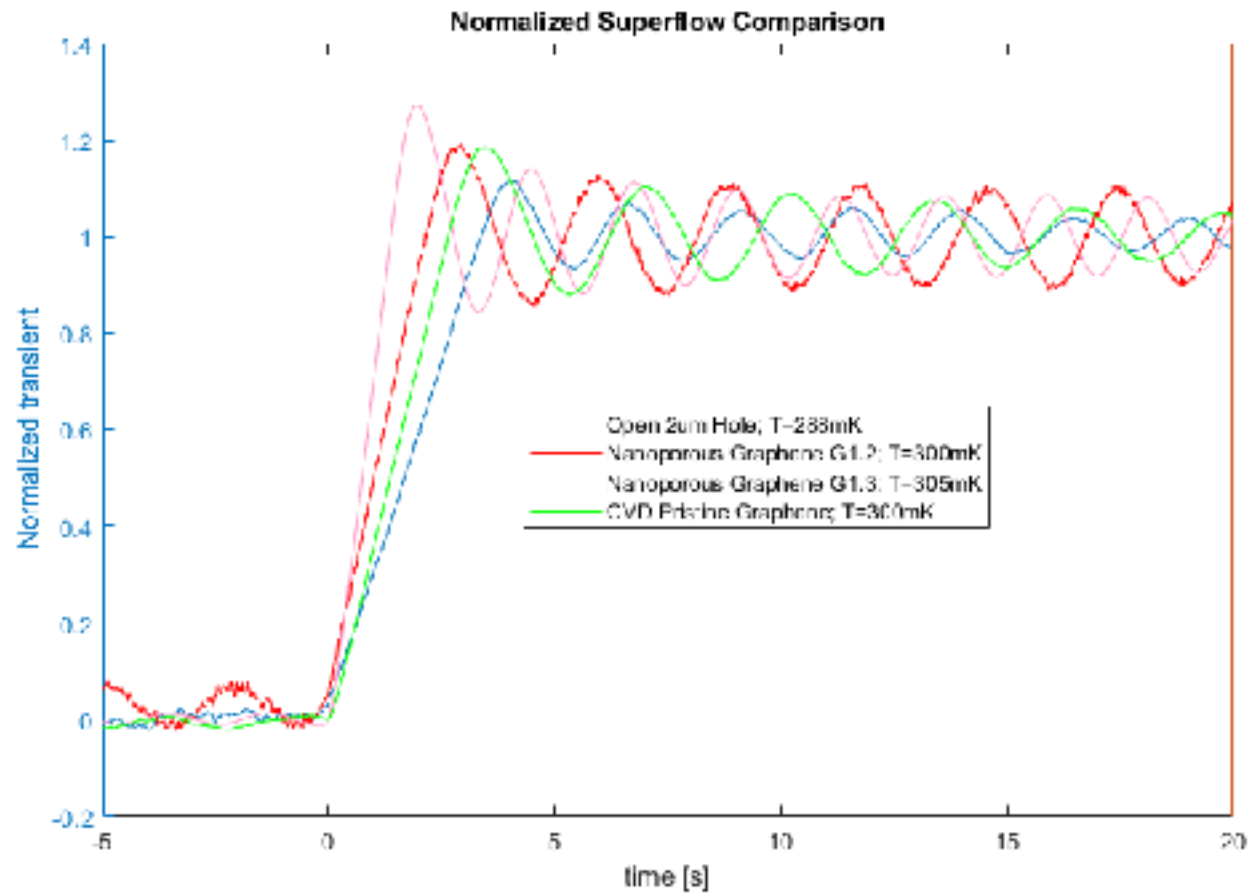
**After Cooldown**



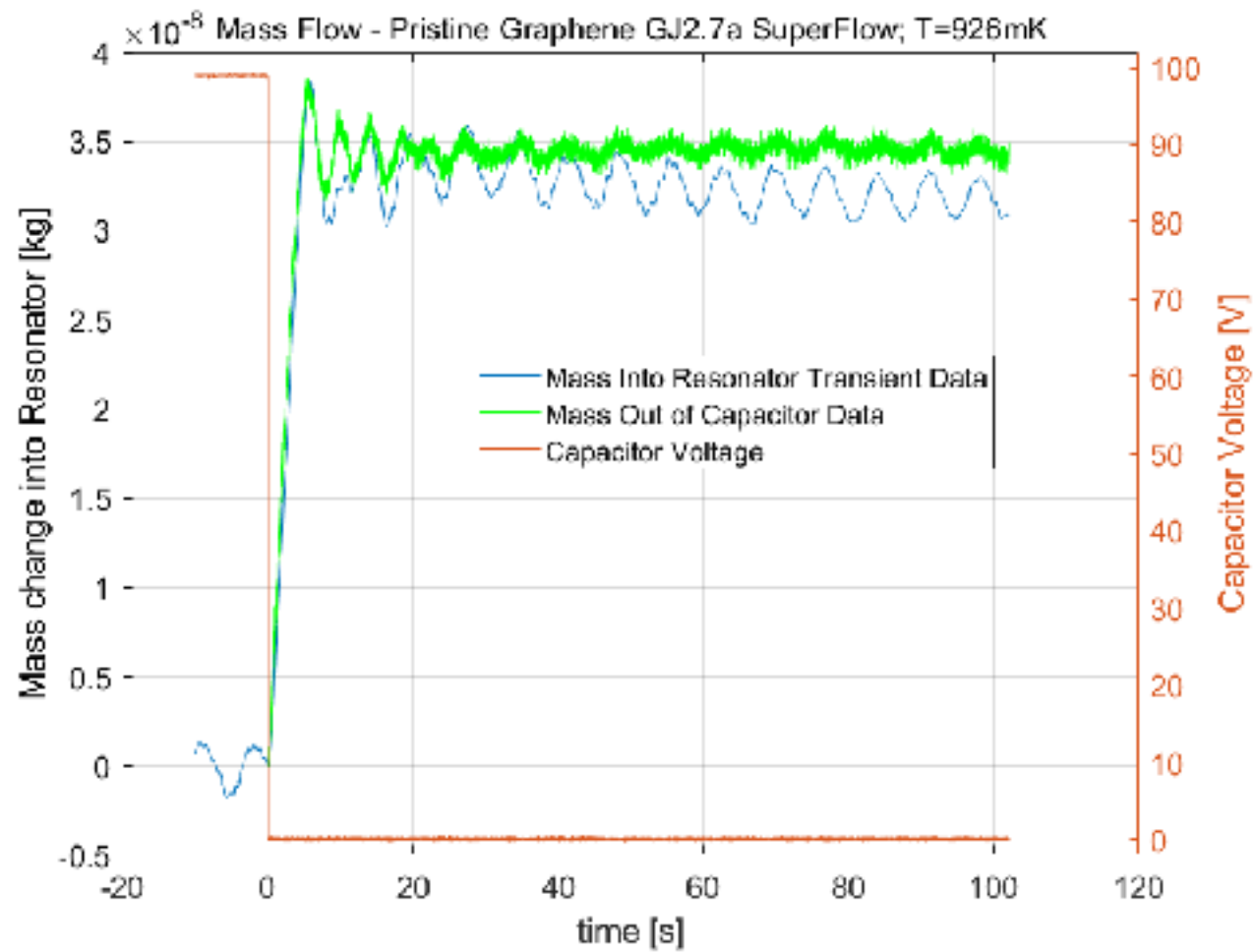
# Transient Data – Crystalline CVD Graphene



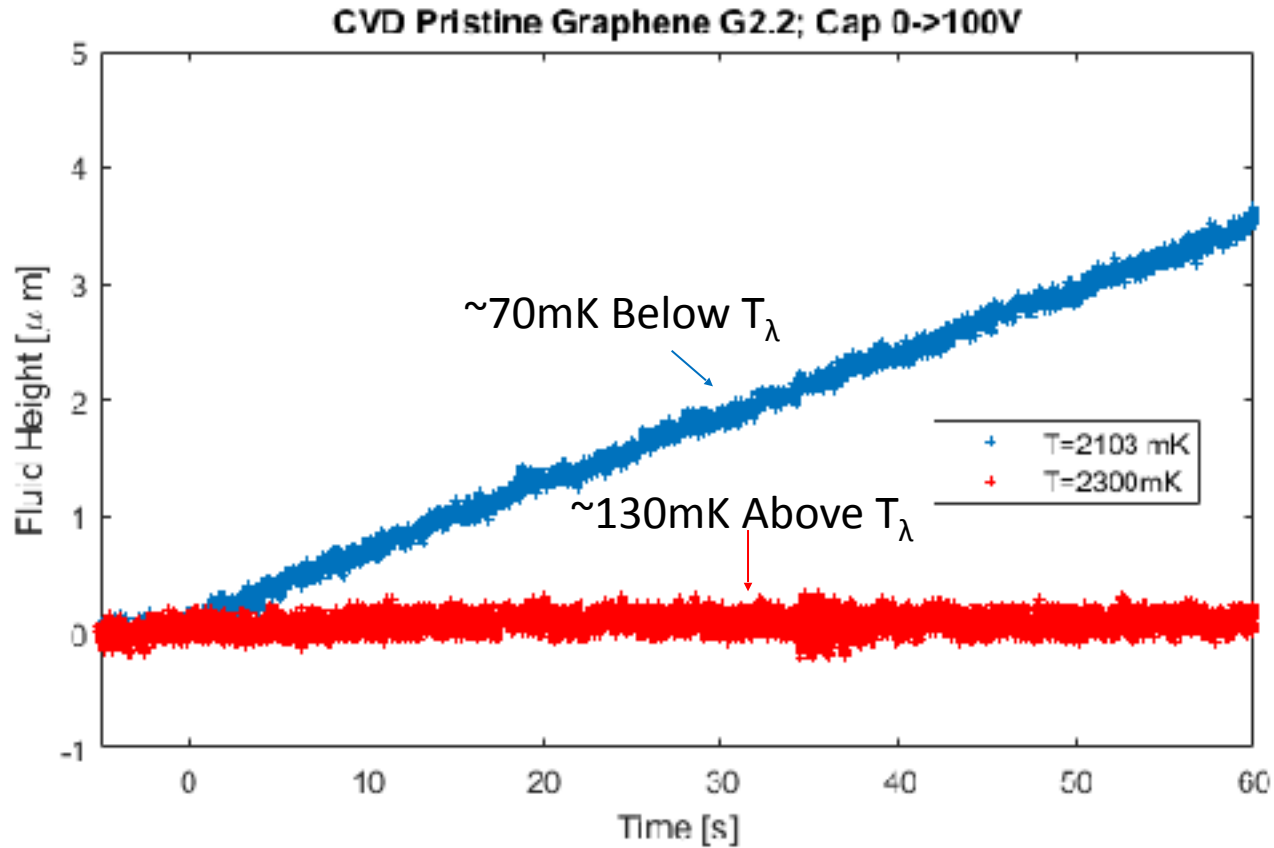
# Transient Data – Crystalline CVD Graphene



# Transient Data – Exfoliated Graphene

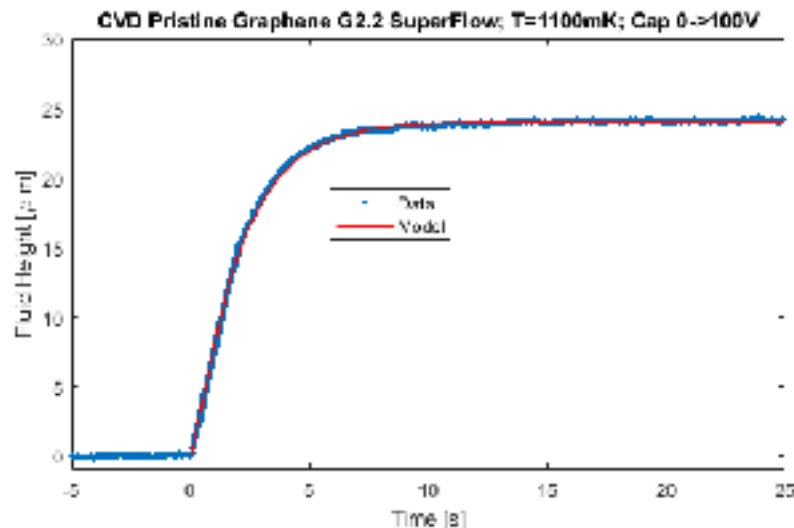
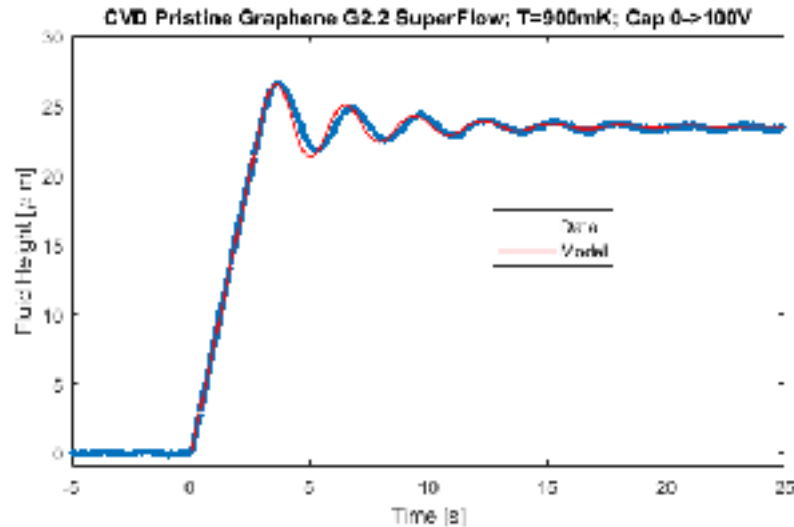


# Transient Data – Normal Fluid Through Graphene



Gas flow measurements at room temperature also show at least  $10^4$  reduction (limited by leak cart background)

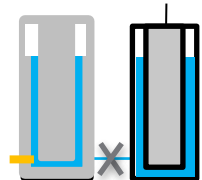
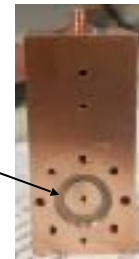
# Transient Data – Crystalline CVD Graphene – Superflow Model



## Relevant Model Parameters

- Junction Inductance
  - Consistent with 2μm hole
- Critical Velocity
  - Consistent with 2μm hole ~25m/s
- Kapitza Resistance
  - Consistent with approximate sinter area
- Capacitor Pressure
  - Consistent with estimate ~0.1Pa
- Resonator and PDH parameters
  - Taken from fitting

Silver Sinter



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# Future Directions

## **Immediate:**

- Final verification of graphene super-leak using sealed, exfoliated graphene flakes from Jim Hone
- Theoretical explanation of graphene super-leak phenomenon

## **Remainder of PhD:**

- Transport properties of multilayer graphene. Eventual weak-link?
- Transport through other 2D materials, such as MoS<sub>2</sub>, BN, Carboxy Fantrip, etc.
- Complete hydrodynamic modelling overall full temperature range, including Josephson effects

## **Time Permitting:**

- Implementation of a high-Q superconducting quarter-wave resonator as a fluid level-meter
- Theoretical investigation of Superfluid Qubits and other potential superfluid technologies

## **Next Generation of Students:**

- Building superfluid quantum devices

# Thank You

Professor Keith Schwab  
Dr. Jeffrey Bottimer

# Caltech

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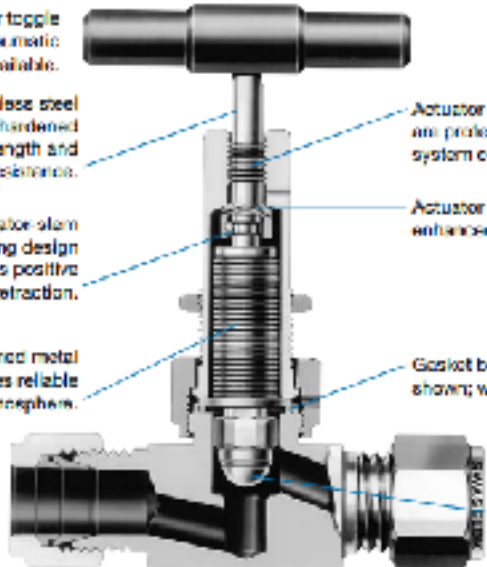
# Cryogenic Valves

Bar, round, or toggle handle, pneumatic actuation also available.

Stainless steel actuator is hardened for strength and wear resistance.

Actuator stem coupling design ensures positive stem retraction.

Precision-formed metal bellows provides reliable seal to atmosphere.



<https://www.swagelok.com/downloads/webcatalogs/en/MS-01-22.pdf>

# Superfluid Qubits

PRELIMINARY FORMALISM ON SUPERFLUID QUBIT EQUATIONS

THOUGHTS ON HOW TO IMPLEMENT AND COUPLE TO A SUPERFLUID QUBIT