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# RPPR Final Report

as of 12-May-2023

Agency Code: 21XD

Proposal Number: 74703PE

Agreement Number: W911NF-19-1-0172

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**Final Report** for Period Beginning 18-Mar-2019 and Ending 30-Sep-2022

**Title:** Quantum control and spectroscopy of a polyatomic molecular ion

**Begin Performance Period:** 18-Mar-2019

**End Performance Period:** 30-Sep-2022

**Report Term:** 0-Other

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**Distribution Statement:** 1-Approved for public release; distribution is unlimited.

## STEM Degrees:

## STEM Participants:

**Major Goals:** 1. Demonstrating quantum entanglement between an atomic ion and a molecular ion. Designing and constructing a cryogenic ion trapping apparatus,  
2. Increasing the experimental data rate with deterministic pure state preparation of CaH<sup>+</sup> in the room-temperature apparatus,  
3. Trapping Ca<sup>+</sup> in a cryogenic ion trap and characterizing the trap performance and cryocooler-induced vibrations. Applying the techniques to a polyatomic molecular ion N<sub>2</sub>H<sup>+</sup>.

**Accomplishments:** Year 1: Demonstrating quantum entanglement between an atomic ion and a molecular ion. We have demonstrated entanglement between an atomic ion qubit and a molecular ion qubit via Cirac-Zoller type interaction. Specifically, starting with both the Ca<sup>+</sup> and CaH<sup>+</sup> ions prepared in pure quantum states and one of their shared harmonic motional modes cooled near the ground state, a  $\pi/2$  pulse on the motion-exciting sideband of a molecular qubit transition prepares the CaH<sup>+</sup> and the motional mode in an entangled state. The motional state is then mapped to the atomic qubit with a  $\pi$  pulse on the motion-reducing sideband of the atomic qubit transition, thus entangling the Ca<sup>+</sup> and the CaH<sup>+</sup> ions. The atomic qubit consists of one level in the 4s S<sub>1/2</sub> state and one in the 3d D<sub>5/2</sub> state of Ca<sup>+</sup>, connected by a transition at ~411 THz. We had chosen two distinct sets of molecular levels as the molecular qubits. One set is within the J = 2 rotational manifold and connected by a transition with ~13 kHz frequency. The levels in the other set are in the J = 2 and J = 0 rotational manifolds, linked by a ~855 GHz transition. We aim to demonstrate the broad selection of transition frequencies offered by molecules. The entanglement is verified by measuring the population in the target basis states and the contrast of the parity scan where the phases of atomic and molecular analysis  $\pi/2$  pulses are varied. The fidelity between the produced states with the target Bell states can then be derived. For the case when both the qubit states are in the J = 2 rotational manifold, we attain a fidelity of 0.87(3). When the qubit states are in J = 2 and J = 0 manifolds, the fidelity can reach 0.76(4). In both cases, the fidelities indicate entanglement between the atom and the molecule. When

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investigating the sources of infidelity, we find that the state-preparation-and-measurement (SPAM) is the dominating source. The lower fidelity when the molecular qubit states are in two different rotational manifolds is mainly attributed to the extra pulses required and imperfect coherence in the frequency comb pulses.

Year 2: Increasing the experimental data rate with deterministic pure state preparation of  $\text{CaH}^+$  in the room-temperature apparatus.

Toward the goal of deterministic pure state preparation of  $\text{CaH}^+$ , the mechanisms that could affect the molecular states need to be well understood. In our work on precision rotational spectroscopy of  $\text{CaH}^+$  [chou2020], the trap rf electric field had been identified as the leading source of uncertainty. We performed systematic characterization of the trap rf electric field and developed an analytical model that describes the effect of such fields on the molecular levels. That allowed us to understand and control the effects of the fields. Equipped with better understanding of the effect of trap RF electric fields on the molecular levels and transitions, we have demonstrated Hertz-level resolution rotational spectroscopy and efficient population transfer between rotational manifolds of  $\text{CaH}^+$  by improving the coherence of our frequency comb. We have also incorporated a 285-GHz microwave source in the experimental setup and successfully driven the  $J = 0$  to  $J = 1$  transition in  $\text{CaH}^+$ . The frequency comb and the 285-GHz source enable reliable coherent transfer of molecular population between rotational manifolds with even and odd principal quantum number, which is essential for deterministic pure state preparation of  $\text{CaH}^+$ .

With the understanding of the effects of the rf electric field on the molecular levels, we decided to increase the bias magnetic field from 3.6 Gauss to 6.5 Gauss, which lifted degeneracy in some molecular levels and improved the efficiency of quantum-logic pumping. In place of a frequency comb, which requires significant upkeep, we have introduced a 570 GHz microwave source to move the population between  $J = 1$  and  $J = 2$  manifolds. Along with the 285-GHz microwave source, the molecular population can be controllably moved within the subspace consisting of  $J = 0, 1$ , and  $2$  manifolds. We have combined improved pumping within  $J = 1$  and  $J = 2$  rotational manifolds and the microwave sources to develop an experimental protocol track and trap the molecular state in the rotational manifolds with  $J$  smaller or equal to 2. After the molecular state is projectively prepared in  $J = 1$ , after some operations for control and/or spectroscopy purposes, the molecular state in  $J = 1$  is checked with nondestructive detection. A positive detection triggers operations moving the molecular population into the desired state and the experimental sequence carries on. If the detection results indicate that the molecular population is not in  $J = 1$  anymore, the control system will search for it in  $J = 2$  sublevels and then in the  $J = 0$  manifold. If the population is found in  $J = 0$  or  $J = 2$  manifolds, the 285 GHz or 570 GHz microwave source, respectively, will be used to move it back to the desired  $J = 1$  sublevel, after which the experimental sequence can resume. This procedure repeats until the population cannot be found in the  $J = 0, 1$  or  $2$  manifolds, at which point the control system switches to perform projective state preparation, with the state preparation success rate determined by the approximately blackbody radiation from the trap environment of the molecule.

The above sequence enabled significant improvement, from few percent to >50 percent, of the average fraction of time over which the experimental control system keeps track of the molecular population and experimental sequences can be performed. The increased data rate will greatly accelerate subsequent investigations.

Year 1: designing and constructing a cryogenic ion trapping apparatus; Year 3: Trapping  $\text{Ca}^+$  in a cryogenic ion trap and characterizing the trap performance and cryocooler-induced vibrations. Applying the techniques to a polyatomic molecular ion  $\text{N}_2\text{H}^+$ .

Toward studying  $\text{Ca}^+$  in the cryogenic ion trap, we have finished assembling the apparatus, tested operation of the trap at room temperature, and loaded  $\text{Ca}^+$  and various molecular species including ones with mass-to-charge ratio 28 (likely  $\text{N}_2^+$ ) and 29 (likely  $\text{N}_2\text{H}^+$ ). Testing and improvements of the molecular beam source took some time and the optimization for loading certain molecular species is still underway. For the ionization, we have tested pulsed lasers with wavelengths ranging from UV to near infrared, pulse energies from hundreds of microjoules to few millijoules, and pulse durations from hundreds of picoseconds to a few nanoseconds. The ion production using pulsed lasers was not efficient. Using loading success rate in a trap as the signal for ionization efficiency was not successful. With the guidance from Prof. Lewandowski at JILA, we introduced a multichannel plate (MCP) to detect ions produced by an electron gun. Such a setup allowed us to produce molecular ions and tune up the molecular flux from the molecular beam source. We are in the process of adding an ion detection chamber to the trap apparatus. The plan is to ionize neutral molecules from the beam source with an electron gun embedded in one of the endcaps on the trap. We are currently modifying the trap apparatus to accommodate cryogenic operations and the detection chamber for the molecular beam. After the system is tuned up for  $\text{Ca}^+$  and  $\text{CaH}^+$ , we will move on to studying  $\text{N}_2\text{H}^+$ .

**Training Opportunities:** Two graduate student, Dalton Chaffee and Zhimin Liu, and three postdoctoral researchers, Alejandra Collopy, Julian Schmidt, and Yu Liu worked on the project and received training on quantum state control of single trapped molecular ions.

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## as of 12-May-2023

**Results Dissemination:** Results of the project are presented in conferences and published to peer-reviewed journals as listed below.

Selected conference presentations:

1. Gordon conference on Atomic Physics, Newport, RI, 2019.
2. New frontiers in cold molecules, Cambridge, MA, 2019
3. The 50th Winter Colloquium on the Physics of Quantum Electronics, Snowbird, UT, 2020
4. Seminar on Precision Physics and Fundamental Symmetries, virtual, 2020
5. The European Conference on Trapped Ions (ECTI), virtual, 2021
6. Caltech Symposium on Frontiers in Chemical Physics, virtual 2021
7. The 8th International Conference on Trapped Charged Particles and Fundamental Physics (TCP), Glashütten, Germany, 2022

Publications:

[liu2023] Y. Liu et al., in preparation.

[collopy2023] A. L. Collopy, J. Schmidt, D. Leibfried, D. R. Leibbrandt, and C. W. Chou, Effects of an oscillating electric field on and dipole moment measurement of a single molecular ion, Phys. Rev. Lett. in press.

[lin2020] Y. Lin, D. R. Leibbrandt, D. Leibfried, and C. W. Chou, Quantum entanglement between an atom and a molecule, Nature 581, 273 (2020).

[chou2020] C. W. Chou, A. L. Collopy, C. Kurz, Y. Lin, M. E. Harding, P. N. Plessow, T. Fortier, S. Diddams, D. Leibfried, and D. R. Leibbrandt, Frequency-comb spectroscopy on pure quantum states of a single molecular ion, Science 367, 1458 (2020).

**Honors and Awards:** 2021 NIST BRONZE MEDAL AWARD

**Protocol Activity Status:**

**Technology Transfer:** Nothing to Report

### **PARTICIPANTS:**

**Participant Type:** Postdoctoral (scholar, fellow or other postdoctoral position)

**Participant:** Julian Schmidt

**Person Months Worked:** 6.00

**Funding Support:**

Project Contribution:

National Academy Member: N

**Participant Type:** Graduate Student (research assistant)

**Participant:** Dalton Chaffee

**Person Months Worked:** 6.00

**Funding Support:**

Project Contribution:

National Academy Member: N

**Participant Type:** Postdoctoral (scholar, fellow or other postdoctoral position)

**Participant:** Yu Liu

**Person Months Worked:** 6.00

**Funding Support:**

Project Contribution:

National Academy Member: N



**RPPR Final Report**  
as of 12-May-2023

**Partners**

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I certify that the information in the report is complete and accurate:

Signature: Chin-wen Chou

Signature Date: 5/5/23 6:23PM

## Major goals

1. Demonstrating quantum entanglement between an atomic ion and a molecular ion. Designing and constructing a cryogenic ion trapping apparatus,
2. Increasing the experimental data rate with deterministic pure state preparation of  $\text{CaH}^+$  in the room-temperature apparatus,
3. Trapping  $\text{Ca}^+$  in a cryogenic ion trap and characterizing the trap performance and cryocooler-induced vibrations. Applying the techniques to a polyatomic molecular ion  $\text{N}_2\text{H}^+$ .

## Accomplished under Goals

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