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APPROXIMATE ANALYSIS OF THE INITIAL PRESSURE  
DISTRIBUTION WITHIN A 105MM MUZZLE BRAKE

H. J. Sneck

August 1976



**BENET WEAPONS LABORATORY**  
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## TABLE OF CONTENTS

|                                                                                     | <u>PAGE</u> |
|-------------------------------------------------------------------------------------|-------------|
| REPORT DOCUMENTATION PAGE, DD FORM 1473                                             |             |
| INTRODUCTION                                                                        | 1           |
| ANALYSIS OF BLOW-BY                                                                 | 1           |
| ANALYSIS OF THE GAS FLOW BEHIND THE PROJECTILE                                      | 7           |
| ANALYSIS OF DIFFUSER UNCORKING                                                      | 8           |
| INITIAL PRESSURE DISTRIBUTION IN THE 4" LONG DIFFUSER SECTION                       | 13          |
| INITIAL PRESSURE DISTRIBUTION ON THE SIDE PLATES BETWEEN<br>THE DIFFUSER AND BAFFLE | 14          |
| INITIAL PRESSURE DISTRIBUTION ON THE BAFFLE                                         | 15          |
| SECOND STAGE ANALYSIS                                                               | 18          |
| ESTABLISHMENT OF STEADY FLOW                                                        | 24          |
| DISTRIBUTION LIST                                                                   |             |

## LIST OF FIGURES

|   |                                                               |    |
|---|---------------------------------------------------------------|----|
| 1 | PROJECTILE AND BRAKE AT MUZZLE UNCORKING                      | 2  |
| 2 | WAVE DIAGRAM FOR ANNULAR LEAKAGE AT UNCORKING                 | 4  |
| 3 | SHOCK WAVE PROPAGATION THROUGH THE BRAKE WINDOW               | 9  |
| 4 | WAVE DIAGRAM FOR SHOCK WAVE PROPAGATION THROUGH<br>THE WINDOW | 12 |
| 5 | LOCATION OF SIDE PLATE PRESSURE STATIONS                      | 16 |
| 6 | LOCATION OF BAFFLE PRESSURE STATIONS                          | 17 |
| 7 | WAVE DIAGRAM FOR SECOND BAFFLE                                | 19 |

## INTRODUCTION

This analysis will attempt to predict propellant pressures which act on various parts of a muzzle brake. These pressures will then serve as inputs to a stress analysis of the brake. The 105mm M68 gun and an experimental howitzer brake, fitted to the gun, were selected because the gun is being fired in a life test. For economy, pressures on the brake will be measured during a few of those rounds to check the analysis.

The internal pressures created in approximately the first 66 microseconds following the barrel uncorking are analyzed. The analysis is broken into two parts, one for the diffuser section of the brake, and one for the downstream portion through which the gases exhaust to the atmosphere. Both flows are modeled as one-dimensional during the short period of time which it takes for the uncorked gases to reach the end of the brake.

No attempt is made to predict the flow fields or the pressures produced by it at subsequent times, although approximate methods might be developed to do so, should the predictions of this analysis yield results in reasonable agreement with experiment.

## ANALYSIS OF BLOW-BY

At the instant that the projectile uncorks the barrel a shock wave is formed in the brake at the muzzle. This shock wave propagates down the diverging annular space between the projectile and the inside wall of the muzzle brake. The flow initiated by this shock wave represents a leakage of high pressure gas from behind the projectile. (See Figure 1).

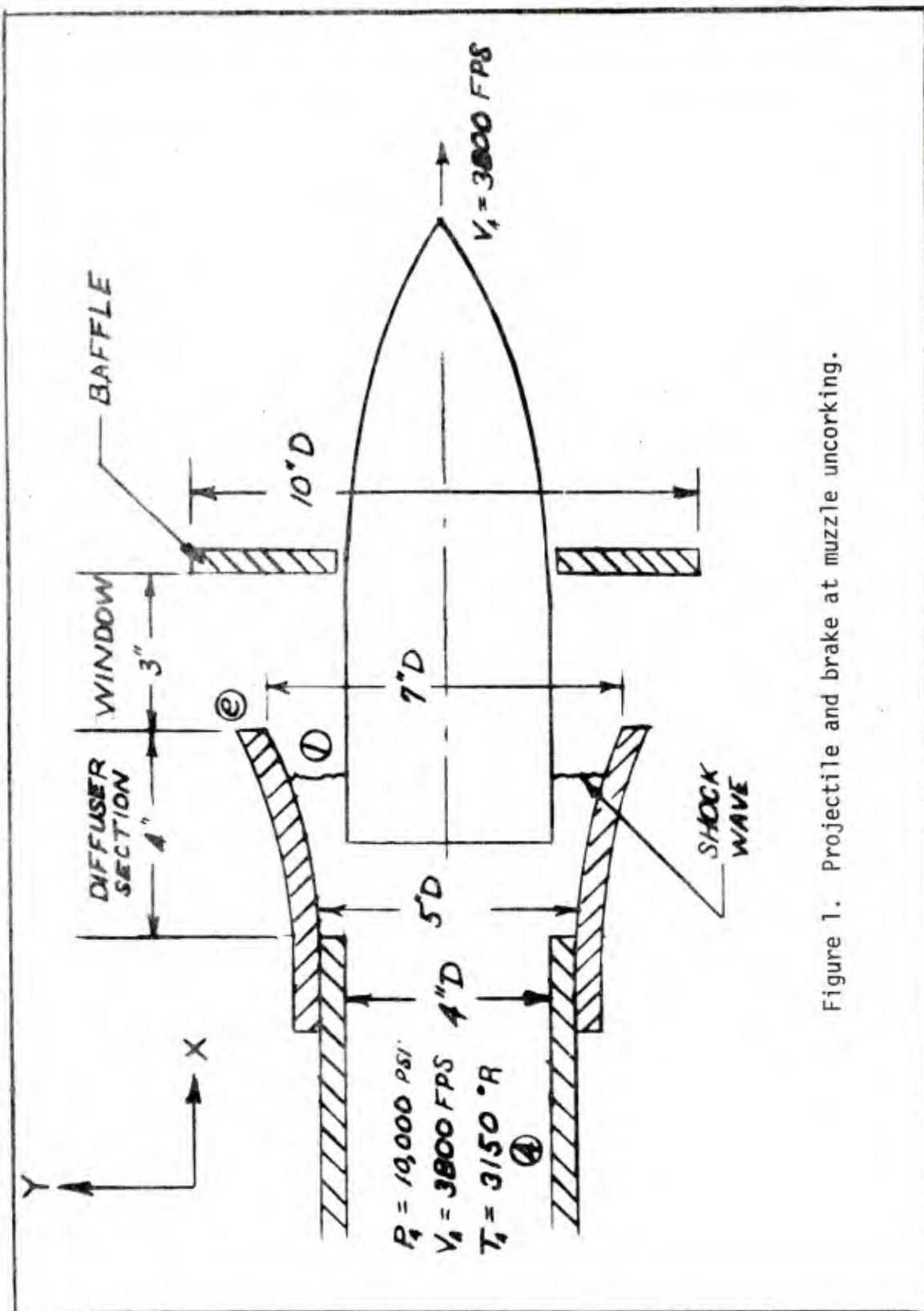


Figure 1. Projectile and brake at muzzle uncorking.

Figure 2 shows the various regions associated with the sudden release of high pressure gas into the annulus following the uncorking. The gas which escapes through this annulus traverses an area change with a ratio

$$(1) \quad \frac{A_1}{A_4} = \frac{(5)^2 - (4)^2}{(4)^2} = \frac{9}{16}$$

The equivalent diameter ratio for this area change is

$$(2) \quad \frac{D_1}{D_4} = \sqrt{\frac{A_1}{A_4}} = \frac{3}{4}$$

According to Alpher and White<sup>1</sup> the effect of an area change in a shock tube can be accounted for by introducing a factor (g) into the standard shock tube "burst" equation so that it takes the modified form

$$(3) \quad \frac{P_4}{P_1} = \frac{\frac{1}{g} \left[ \frac{2\gamma_1 M_s^2 - (\gamma_1 - 1)}{\gamma_1 + 1} \right]}{\left[ 1 - \left( \frac{\gamma_4 - 1}{\gamma_1 + 1} \right) \frac{C_1}{C_4} \left( M_s - \frac{1}{M_s} \right) \left( \frac{1}{g} \right) + \left( \frac{\gamma_4 - 1}{2} \right) \frac{V_4}{C_4} \right]^{\frac{\gamma_4 - 1}{2\gamma_4}}}$$

In this equation subscripts refer to the regions so numbered in Fig 2 and:

$$T_1 = 530^\circ\text{R}$$

$$T_4 = 3150^\circ\text{R}$$

$$\gamma_1 = 1.4 \text{ (air)}$$

$$\gamma_4 = 1.25 \text{ (combustion products)}$$

1. R. A. Alpher and D. R. White, "Ideal Theory of Shock Tubes with Area Change Near the Diaphragm" G. E. Rpt 57-RL-1664, Jan 1957

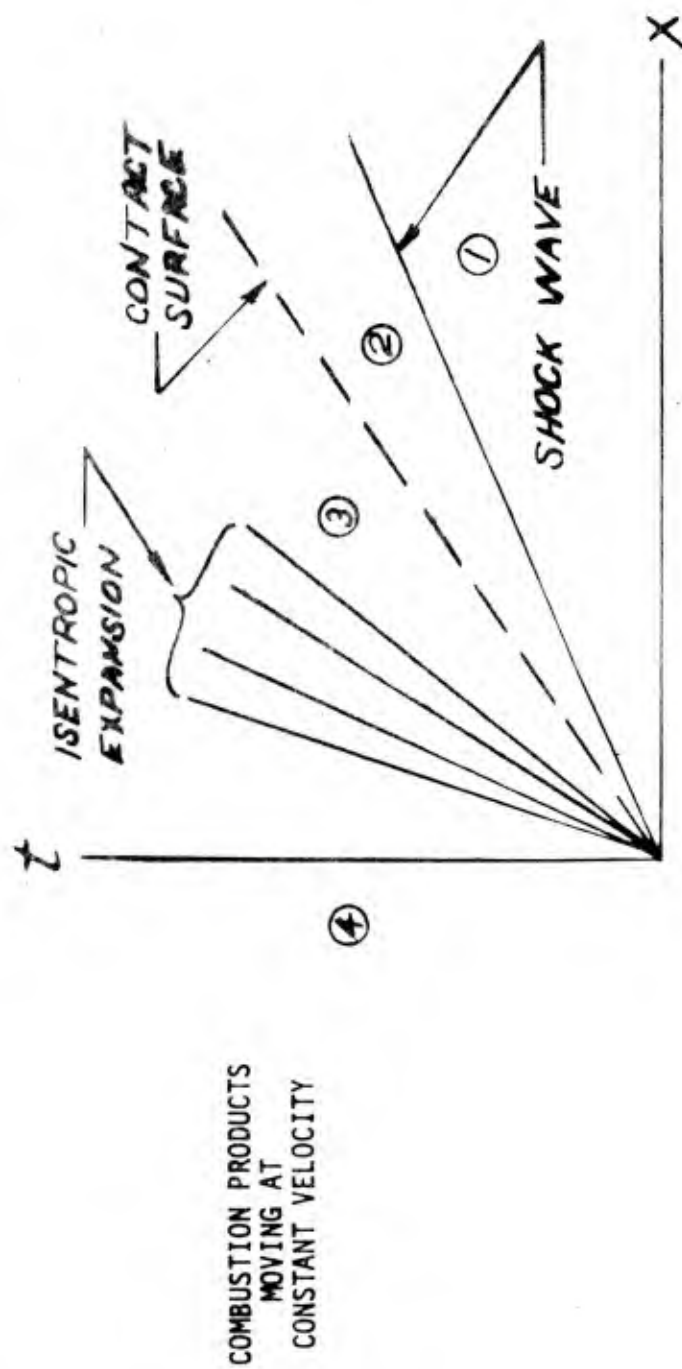


Figure 2. Wave diagram for annular leakage at uncorking.

$$\begin{aligned}
V_4 &= 3800 \text{ ft/sec (projectile velocity)} \\
g &= 1.25 \text{ for } D_4/D_1 = 4/3 \\
R_1 &= 53.3 \text{ ft-lbf/lbm } ^\circ\text{R (air)} \\
R_4 &= 67.0 \text{ ft-lbf/lbm } ^\circ\text{R (combustion products)} \\
\rho_4 &= 6.82 \text{ lbm/ft}^3 \\
g_c &= \text{gravitational constant} = 32.2 \text{ lbm ft/lbf sec}^2 \\
C_4 &= \sqrt{\gamma_4 g_c R_4 T_4} = 2918 \text{ ft/sec} \\
P_4/P_1 &= 10,000/15 = 667 \\
\frac{C_1}{C_4} &= \sqrt{\frac{1.4 (53.3) 530}{1.25 (67) 3150}} = 3.86
\end{aligned}$$

With these inputs, equation (3) becomes

(3a)

$$667 = \frac{0.933M_s^2 - 0.133}{[1.163 - 0.0393(M_s - 1/M_s)]^{10}}$$

Solving this equation (3a) for the initial shock Mach number ( $M_s$ ) yields a value of 9.2. The shock wave itself travels with a velocity of 9.2 (1130) = 10,396 ft/sec while the fluid which it sets into motion moves with a velocity given by

$$\begin{aligned}
(4) \quad v_2 &= \frac{2}{\gamma_1 + 1} C_1 \left( M_s - \frac{1}{M_s} \right) \\
&= \frac{2}{2.4} (1130) \left( 9.2 - \frac{1}{9.2} \right) \\
v_2 &= 85.61 \text{ ft/sec}
\end{aligned}$$

Obviously the shock wave and the fluid behind are traveling much faster than the projectile, reaching the end of the diffuser section of the brake (4" from the muzzle) before the base of the projectile does.

The propagation of a shock wave through an area change has been investigated by Whitman<sup>2</sup> who showed that

$$(5) \quad M_e = M_s \frac{(A_s)}{(A_e)} \frac{K_\infty}{2} \quad \text{where } K_\infty = .36$$

$$\approx 9.2 \left[ \frac{(5)^2 - (4)^2}{(7)^2 - (4)^2} \right]^{0.18}$$

$$M_e = 7.28$$

The conditions behind the shock wave at the exit of the diffuser are given by

$$(6) \quad \frac{P_e}{P_1} = \frac{2\gamma_1}{\gamma_1 + 1} M_e^2 - \frac{\gamma_1 - 1}{\gamma_1 + 1}$$

$$= \frac{2.8}{2.4} (7.28)^2 - \frac{0.4}{2.4}$$

$$\frac{P_e}{P_1} = 61.7$$

$$(7) \quad \frac{\rho_e}{\rho_1} = \frac{(\gamma_1 + 1) M_e^2}{(\gamma_1 - 1) M_e^2 + 2}$$

$$\frac{\rho_e}{\rho_1} = 5.48$$

$$(8) \quad T_e = \frac{P_e \rho_1}{P_1 \rho_e} T_1$$

$$T_e = \frac{(61.7)}{(5.48)} 530 = 5964^\circ R$$

2. G. B. Whitman, "On the Propagation of Shock Waves through Regions of Non-Uniform Area Flow," J. Fluid Mechanics, Vol. 2, P. 337 (1958)

$$(9) \quad v_e = \left( \frac{2}{\gamma + 1} \right) c_1 \left( M_e - \frac{1}{M_e} \right)$$

$$v_e = 6726 \text{ ft/sec}$$

The leakage passed by the projectile (blow-by) can be estimated from

$$(10) \quad \dot{m} = \rho_e A v_e$$

$$= \frac{5.48(0.075)}{144} \frac{(49-16)}{4} (6726) \pi$$

$$\dot{m} = 497.6 \text{ lbm/sec}$$

The time for the projectile base to reach the end of the diffuser is

$$\frac{x}{\dot{x}} = \frac{4/12}{3800} = 8.77 (10^{-5}) \text{ sec so that the total leakage during this period}$$

is 0.0436 lbm which is only a few percent of the total mass and therefore quite negligible.

#### ANALYSIS OF THE GAS FLOW BEHIND THE PROJECTILE

Since very little of the barrel gas is lost via blow-by as the projectile base moves through the diffuser section, most of the gas which was behind the projectile base at uncorking must still be behind the base when it reaches the diffuser exit (e).

If it is assumed that this gas undergoes an isentropic expansion, then the pressure at this point must be approximately

$$(11) \quad \frac{P_{41}}{P_4} = \left( \frac{V_4}{V_{41}} \right)^{\gamma_4}$$

$$\text{Therefore } P_{41} = 10,000 \left( \frac{16}{49} \right)^{1.25}$$

$$P_{41} = 2468 \text{ psia}$$

$$(12) \quad T_{41} = T_4 \left( \frac{P_{41}}{P_4} \right)^{\frac{\gamma_4 - 1}{\gamma_4}}$$

$$T_{41} = 3150 \left( \frac{2468}{10,000} \right)^{0.25} \quad T_{41} = 2381^\circ \text{R}$$

$$(13) \quad C_{41} = \sqrt{32.2 R_{41} T_{41} \gamma_4}$$

$$C_{41} = \sqrt{1.25(32.2)67(2381)}$$

$$C_{41} = 2534 \text{ ft/sec}$$

$$(14) \quad \rho_{41} = \rho_4 \frac{V_4}{V_{41}}$$

$$\rho_{41} = 6.82 \frac{(16)}{(49)} = 2.23 \text{ lbm/ft}^3$$

#### ANALYSIS OF DIFFUSER UNCORKING

Figure 3 illustrates the situation assumed to exist at the instant that the projectile base reaches the end of the diffuser. It will be assumed that the disk of fluid shown at the left of this figure propagates to the right with the projectile velocity  $\dot{x}$ , (3800 ft/sec) while expanding radially behind a radial shock wave. This assumption is analogous to that used in the report by Soifer<sup>3</sup> with the exception that the explosion does not emanate from a line source and is one-dimensional rather than cylindrical. The assumption of one-dimensional flow seems more realistic considering the presence of the brake side plates beyond the diffuser section. The burst of a finite size volume assumed here avoids the rather unrealistically low densities in the core of the burst which result from the assumption of a line source.

The shock Mach number for a shock wave propagating radially from the "window" of the muzzle brake is given by the equation

3. "Muzzle Brake Analysis," S & D Dynamics, Inc, TR # 73-6, Oct 73, Contr. No. DAAF 07-73-0541

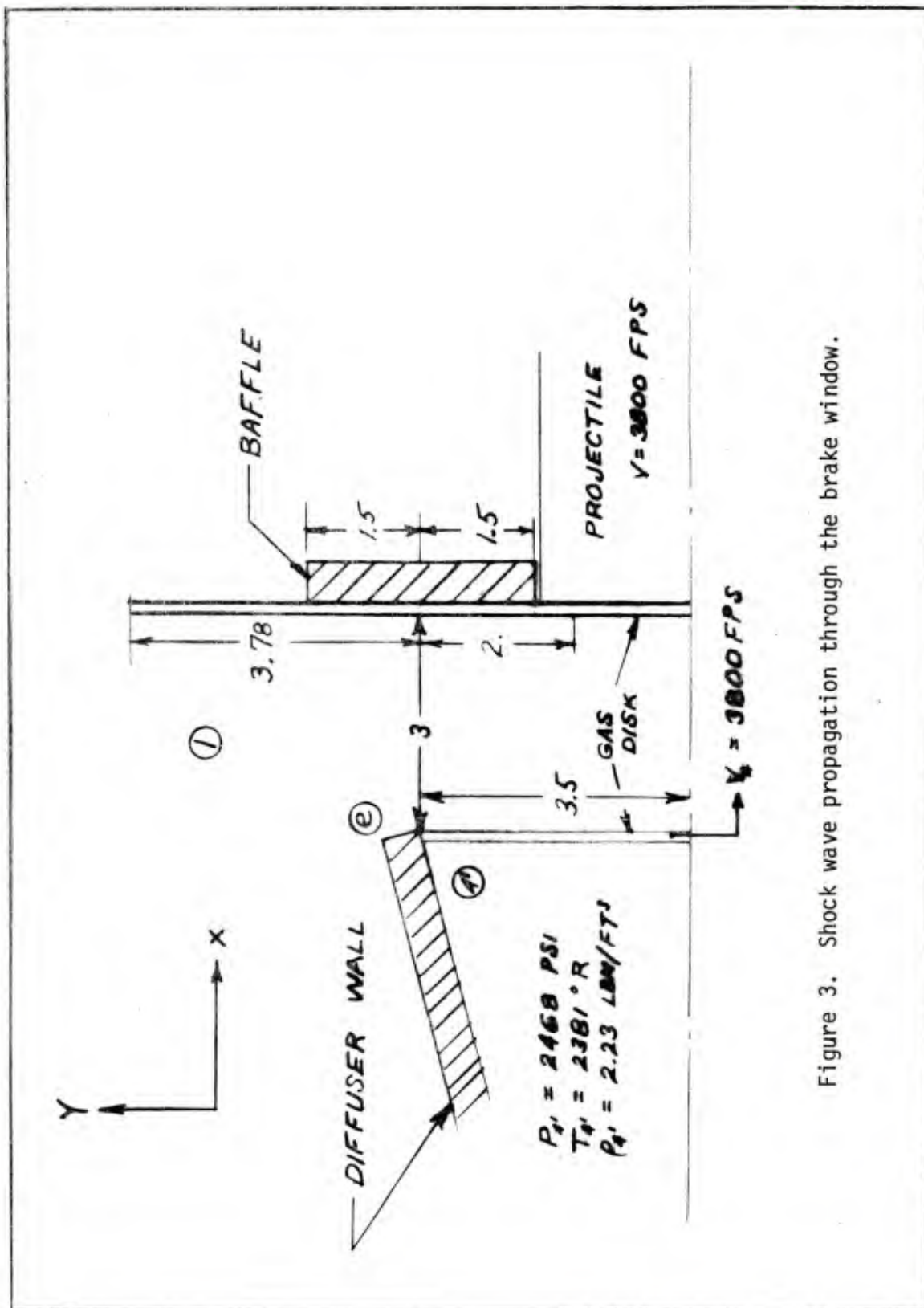


Figure 3. Shock wave propagation through the brake window.

$$(15) \quad \frac{P_4'}{P_1} = \frac{\frac{2\gamma_1 M_s^2 - (\gamma_1 - 1)}{\gamma_1 + 1}}{\left[ 1 - \left( \frac{\gamma_4' - 1}{\gamma_1 + 1} \right) \frac{C_1}{C_4'} \left( M_s - \frac{1}{M_s} \right) \right]^{\frac{2\gamma_4'}{\gamma_4' - 1}}}$$

$$(15a) \quad \frac{2468}{15} = \frac{1.167 M_s^2 - 0.167}{\left[ 1 - .0464 \left( M_s - \frac{1}{M_s} \right) \right]^{10}} = 164$$

This equation is the same as equation (3) without the factor (g). Furthermore, the last term in the denominator of (3) vanishes here because  $v_{41}$ , the radial velocity, is initially zero in this radially expanding shock.

The shock Mach number for this one-dimensional shock wave moving at a right angle to the flight path is  $M_s = 4.25$ . Behind this shock wave

$$(16) \quad v_{21} = \frac{2}{\gamma_1 + 1} C_1 \left( M_s - \frac{1}{M_s} \right) = 3774 \text{ ft/sec}$$

$$(17) \quad \frac{\rho_{21}}{\rho_1} = \frac{(\gamma_1 + 1) M_s^2}{(\gamma_1 - 1) M_s^2 + 2} = 5.40$$

$$(18) \quad \frac{P_{21}}{P_1} = \frac{2\gamma_1 M_s^2 - (\gamma_1 - 1)}{\gamma_1 + 1} = 20.9$$

$$(19) \quad T_{21} = \frac{P_{21}}{P_1} \frac{\rho_1}{\rho_{21}} T_1 = 2051^\circ\text{R}$$

The time required for the projectile base to move from the end of the diffuser to the baffle is  $\frac{x}{v} = \frac{3/12}{3800} = 6.58 (10^{-5})$  sec.

During this time the leading edge of the radial shock wave travels a distance

$$(20) \quad \Delta R = C_1 M_s \frac{x}{v}$$

$$\Delta R = \frac{(C_1 M_s)}{(3800)} 3 = 3.78 \text{ in}$$

as shown in Figure 3. The trailing edge of the centered expansion fan travels a distance

$$(21) \quad \Delta r = C_4 \frac{x}{x} = C_4 t$$

$$\Delta r = \left( \frac{2534}{3800} \right)^3 = 2.00 \text{ in}$$

Figure 4 shows the relative position of the characteristics and the shock front with respect to the baffle when the moving disk of gas impinges on it.

In order to find the pressure distribution on the baffle, the "backward" running characteristics (shown as a fan in Figure 4) are used to establish the location on the baffle while the forward running characteristics are used to carry the core conditions through the fan.

For example, the characteristic which intercepts the outer edge of the baffle has a slope of  $\frac{1.5/12}{6.58(10^{-5})} = 1900 \text{ ft/sec}$

therefore, the slope is equal to  $U_0 - C_0 = 1900$  where the subscript o refers to the outer edge of the end plate. Since along the "forward" running characteristic (not shown in Figure 4), the value  $u + \frac{2}{\gamma - 1} c = \text{constant} = 8C_4$ , i.e.,

$$(23) \quad U_0 + 8 C_0 = 8 C_4 = 8 (2534)$$

Combining these two equations yields

$$C_0 = 2041 \text{ ft/sec}$$

$$U_0 = 3941 \text{ ft/sec}$$

and

from (13)

$$T_0 = \frac{C_0^2}{32.2 \gamma R}$$

$$T_0 = \frac{(2041)^2}{(1.25)(67)(32.2)} = 1544^\circ R$$

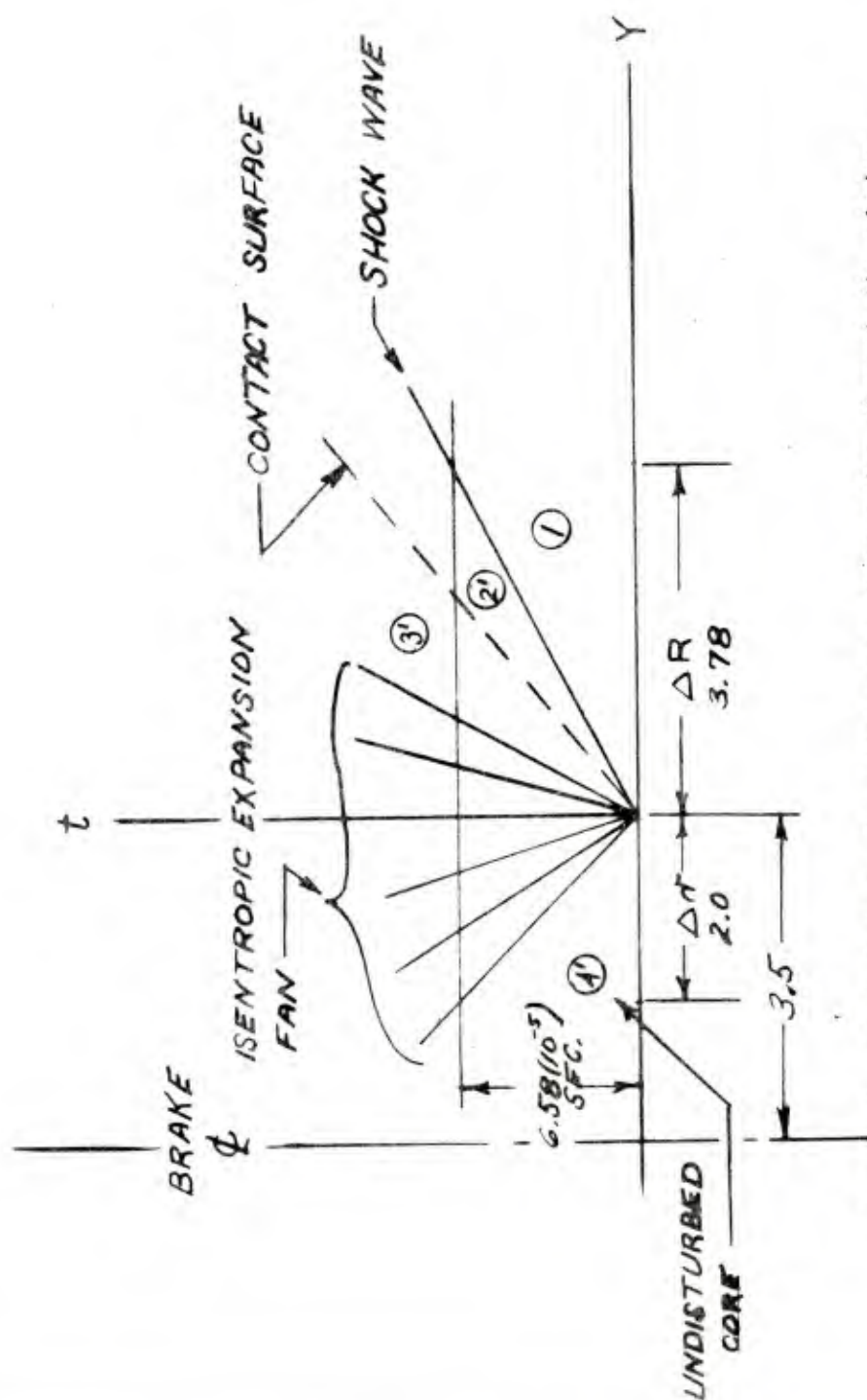


Figure 4. Wave diagram for shock wave propagation through the window.

from (12)

$$P_o = P_{4'} \left( \frac{T_o}{T_{4'}} \right)^{\frac{\gamma}{\gamma-1}}$$

$$P_o = 2468 \left( \frac{1544}{2381} \right)^5 = 283 \text{ psia}$$

(24)

$$P_o = P_{4'} \left( \frac{P_o}{P_{4'}} \right)^{\frac{1}{\gamma}}$$

$$P_o = 2.23 \left( \frac{283}{2468} \right)^{0.8} = 0.394 \frac{\text{lbm}}{\text{ft}^3}$$

The stagnation pressure rise due to momentum exchange as the disk impinges on the baffle is

(25)

$$\begin{aligned} (P_o)_s &= \frac{P_o V_{4'}^2}{g_o} \\ &= \frac{0.394 (3800)^2}{32.2 (144)} = 1227 \text{ PSI} \end{aligned}$$

The total pressure felt at the extremity of the baffle is therefore

(26)

$$P_o \text{ total} = 1227 + 283 = 1510 \text{ psi}$$

Using a similar procedure the distribution of total pressure can be mapped for the entire baffle. The following sections will describe the results of calculations for the pressure distribution throughout the brake interior.

#### INITIAL PRESSURE DISTRIBUTION IN THE 4" LONG DIFFUSER SECTION

The pressure distribution imposed radially upon the diverging diffuser section by the isentropic gas expansion directly behind the base of the projectile is computed from (11) and summarized in the following table.

Table 1

| <u>Diffuser Diameter (in)</u> | <u>Radial Pressure (Psi)</u> |
|-------------------------------|------------------------------|
| 5                             | 5724                         |
| 6                             | 3629                         |
| 7                             | 2468                         |

Following the "uncorking" of the diffuser by the projectile base, the diffuser pressures will decrease rapidly tending toward the steady values. As a consequence the values given in Table 1 should represent the maximum pressures experienced by the diffuser.

INITIAL PRESSURE DISTRIBUTION ON THE SIDE PLATES BETWEEN THE DIFFUSER AND BAFFLE

Following the uncorking of the diffuser the results of a one-dimensional shock expansion from the "windows" of the brake yield the following initial side plate pressure distributions:

Table 2  
(1" from Diffuser Exit)

| <u>Distance from Center Line (in)</u> | <u>Pressure (Psi)</u> |
|---------------------------------------|-----------------------|
| 0 - 2.83"                             | 2468                  |
| 3.0                                   | 1864                  |
| 3.5                                   | 759                   |
| 4.0                                   | 284                   |
| 4.5                                   | 95                    |
| 5.0                                   | 28                    |

Table 3  
(2" from Diffuser Exit)

| <u>Distance from Center Line (in)</u> | <u>Pressure (Psi)</u> |
|---------------------------------------|-----------------------|
| 0 - 2.17                              | 2468                  |
| 2.5                                   | 1860                  |
| 3.0                                   | 1202                  |
| 3.5                                   | 759                   |
| 4.0                                   | 470                   |
| 4.5                                   | 285                   |
| 5.0                                   | 167                   |

Table 4  
(3" from Diffuser Exit)

| <u>Distance from Center Line (in)</u> | <u>Pressure (Psi)</u> |
|---------------------------------------|-----------------------|
| 0 - 1.5                               | 2468                  |
| 2.0                                   | 1860                  |
| 2.5                                   | 1391                  |
| 3.0                                   | 1035                  |
| 3.5                                   | 759                   |
| 4.0                                   | 552                   |
| 4.5                                   | 399                   |
| 5.0                                   | 283                   |

The location of the pressure stations cited in Tables 2-4 are shown in Figure 5.

#### INITIAL PRESSURE DISTRIBUTION ON THE BAFFLE

The total pressures which are imposed initially by the arrival of the gases directly behind the projectile base are shown in Table 5. The location of the pressure stations used are shown in Figure 6. These are calculated by the method shown previously using equations (22) through (26).

Table 5

| <u>Distance from Center Plane (in)</u> | <u>Pressure (Psi)</u> |
|----------------------------------------|-----------------------|
| 0 - 1.5                                | 9413                  |
| 2.0                                    | 7397                  |
| 2.5                                    | 5782                  |
| 3.0                                    | 4501                  |
| 3.5                                    | 3462                  |
| 4.0                                    | 2648                  |
| 4.5                                    | 2015                  |
| 5.0                                    | 1510                  |

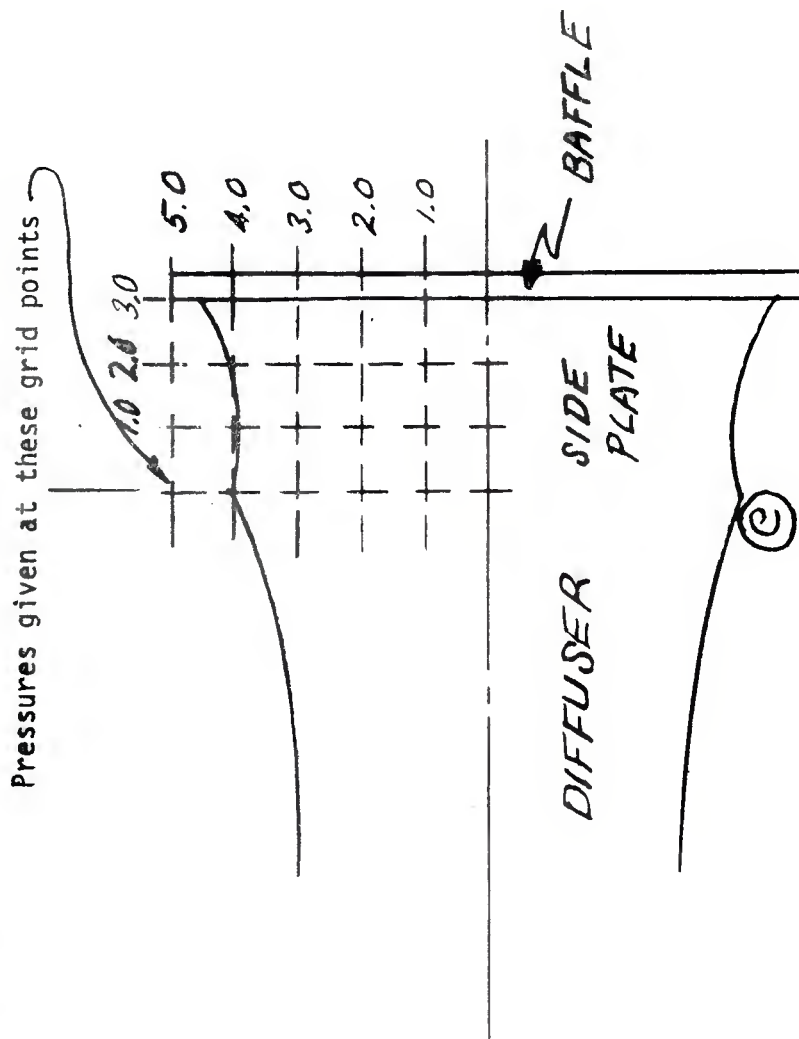


Figure 5. Location of side plate pressure stations.

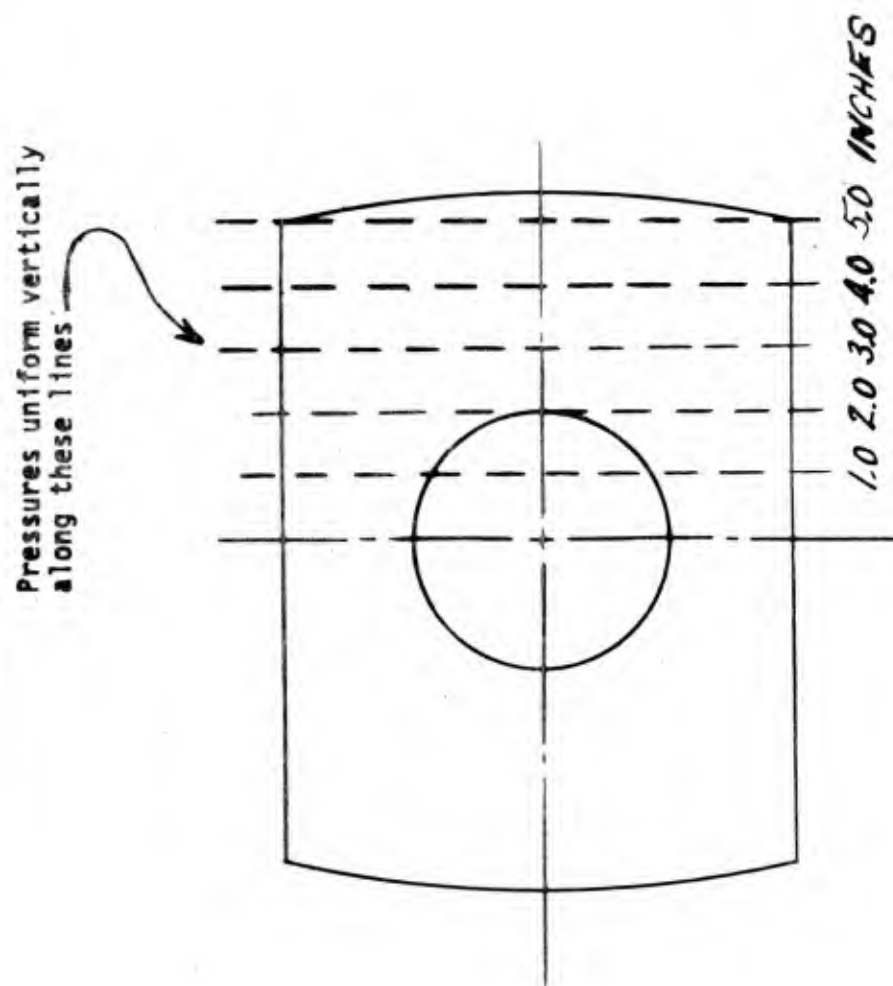


Figure 6. Location of baffle pressure stations.

These values are the stagnation pressures obtained by summing both the static and dynamic pressures.

All interior surfaces of the brake will experience some pressures prior to those listed above due to the precursor flow caused by blow-by. These pressures are expected, however, to be masked in time and amplitude by the almost simultaneous arrival of the uncorking flows.

#### SECOND STAGE ANALYSIS

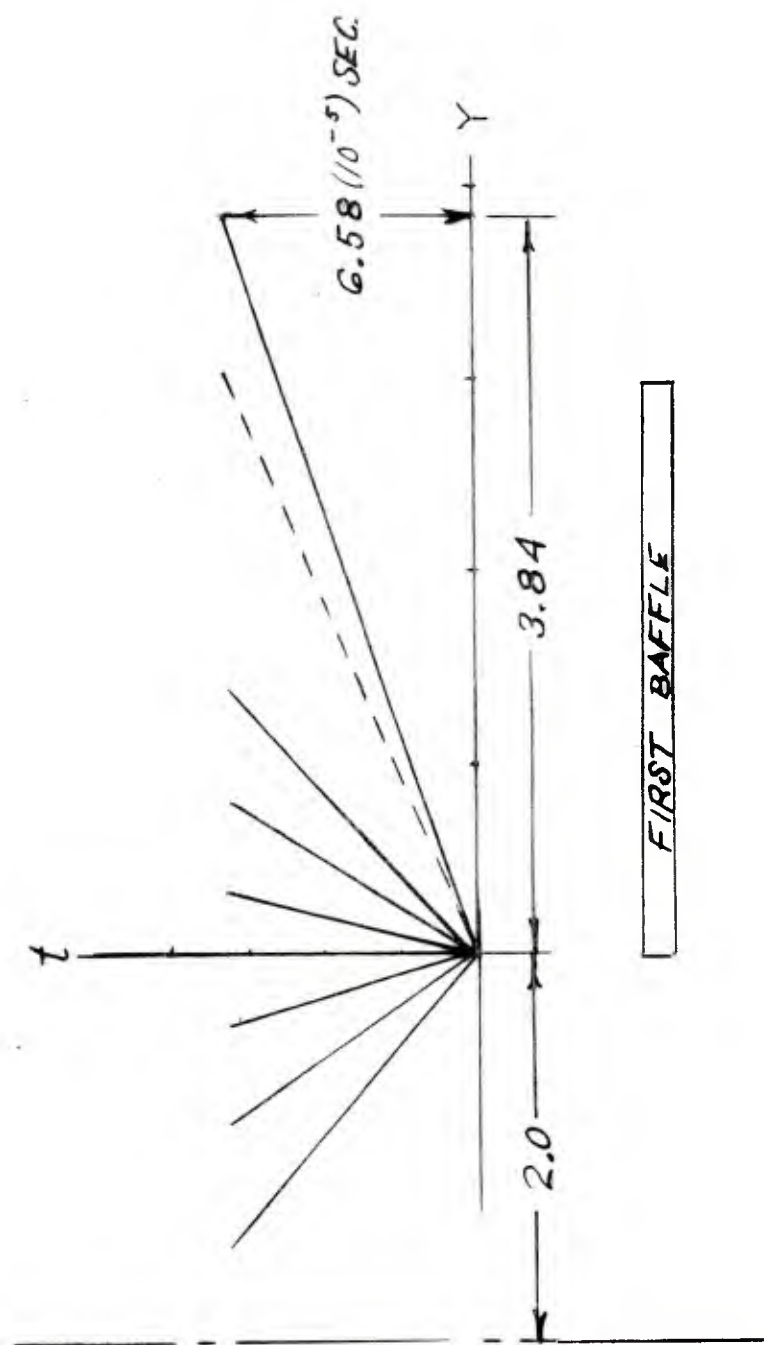
The techniques described above can be extended to the analysis of a second stage of the muzzle brake with some slight modifications.

Figure 7 shows the wave diagram for the radial motion of gas in the second stage as the disk of gas expands behind the projectile base. The only backward running characteristics generated in the first stage which pass into the second stage are those directly behind the projectile base when it passes through the first baffle. If it is assumed that this baffle is quite thin, then the burst of gases into the second stage gives rise to a new centered expansion fan as shown in Figure 7.

From the previous calculations of the values in Table 4, the conditions two inches from the center line at the moment that the projectile passes through the first baffle are

$$\begin{aligned} C_{4''} &= 2463 \text{ ft/sec} \\ T_{4''} &= 2250 \text{ }^{\circ}\text{R} \\ (27) \quad \rho_{4''} &= 1.778 \text{ lbm/ft}^3 \\ P_{4''} &= 1860 \text{ psia} \\ U_{4''} &= 563.6 \text{ ft/sec} \end{aligned}$$

The shock Mach number for the radial growth of the disk after it passes through the first baffle plate is given by (28) which is similar



FIRST BAFFLE

Figure 7. Wave diagram for second baffle.

to (3) and (15).

$$(28) \quad \frac{P_4''}{P_1} = \frac{\left[ \frac{2\gamma_1 M_s^2 - (\gamma_1 - 1)}{\gamma_1 + 1} \right]}{\left[ 1 - \left( \frac{\gamma_4 - 1}{\gamma_1 + 1} \right) \frac{C_1}{C_4} \left( M_s - \frac{1}{M_s} \right) + \left( \frac{\gamma_4 - 1}{2} \right) \frac{U_4''}{C_4''} \right]^{\frac{2\gamma_4}{\gamma_4 - 1}}}$$

$$124 = \frac{1.167 M_s^2 - 0.286}{\left[ 1.0286 - 0.0478 \left( M_s - \frac{1}{M_s} \right) \right]^{10}}$$

The shock Mach number which satisfies this equation is  $M_s = 4.3$ .

The velocity of the gas behind this shock wave is from (4)

$$(4) \quad \begin{aligned} U_{2''} &= \frac{2}{\gamma_1 + 1} C_1 \left( M_s - \frac{1}{M_s} \right) \\ &= \frac{2}{2.4} (1130) \left( 4.3 - \frac{1}{4.3} \right) \\ U_{2''} &= 3830 \text{ ft/sec} \end{aligned}$$

The pressure in this region is from (6).

$$(29) \quad \begin{aligned} \frac{P_{2''}}{P_1} &= \frac{2\gamma_1}{\gamma_1 + 1} M_s^2 - \frac{(\gamma_1 - 1)}{\gamma_1 + 1} = 21.4 \\ P_{2''} &= 321 \text{ psi} \end{aligned}$$

If the distance between the first and second baffles is assumed to be 3.0 inches, then the shock wave will have advanced radially a distance equal to

$$(30) \quad 3 \left( \frac{M_s C_1}{3800} \right) = 3 \left( \frac{1130(4.3)}{3800} \right) = 3.84''$$

which is 0.84" beyond the edge of the second baffle at this point, assuming that the second baffle is the same size as the first baffle.

The characteristic which forms the left side of the expansion fan coincides with characteristic along which  $U_4''$  and  $C_4''$  have constant values of

$$U_4'' = 563.6 \text{ ft/sec}$$

$$C_4'' = 2463 \text{ ft/sec}$$

from (27).

Regions 4'' and 3'' are connected by a forward running characteristic along which

$$(31) \quad U_4'' = \frac{2}{\gamma_4 - 1} C_4'' = U_3'' + \frac{2}{\gamma_4 - 1} C_3''$$

$$563.6 + 8(2463) = 3830 + 8C_3''$$

$$C_3'' = 2055 \text{ ft/sec}$$

Then from (13)

$$(32) \quad T_3'' = T_4'' \left( \frac{C_3''}{C_4''} \right)^2$$

$$T_3'' = 2250 \left( \frac{2055}{2463} \right)^2$$

$$T_3'' = 1566 \text{ } ^\circ\text{R}$$

from (12)

$$(33) \quad P_3'' = P_4'' \left( \frac{T_3''}{T_4''} \right)^{\frac{\gamma_4}{\gamma_4 - 1}}$$

$$P_3'' = 304 \text{ psia}$$

$$(34) \quad \text{from (8)} \quad \rho_3'' = \rho_4'' \frac{P_3''}{P_4''} \frac{T_4''}{T_3''}$$

$$= 1.778 \frac{304}{1860} \frac{2250}{1566}$$

$$\rho_3'' = 0.132$$

and from (25) the stagnation pressure is

$$(35) \quad (P_3'')_s = \frac{\rho_3'' \gamma^2}{g_0}$$

$$= \frac{0.132}{32.2} \left( \frac{3800}{12} \right)^2$$

$$P_{3''_s} = 411 \text{ psi}$$

The total pressure in the constant velocity region behind the shock wave is therefore

$$(36) \quad 304 + 411 = 715 \text{ psia}$$

The leading edge of the expansion fan has a slope

$$(37) \quad \begin{aligned} U_{3''} - C_{3''} &= U_{2''} - C_{3''} \\ &= 3830 - 2055 \\ &= 1775 \text{ ft/sec} \end{aligned}$$

The radial position of the leading edge of the fan at the second baffle is

$$(38) \quad \Delta R^1 = (1775)(6.58(10^{-5}))(12) = 1.40 \text{ in}$$

Referring to Figure 7 and (36) shows that the outer 1.6 inches of the second baffle plate has a constant total pressure of 715 psia impressed upon it.

The backward running characteristic coincident with the hole in the second baffle has a zero slope on the wave diagram so that  $U_i - C_i = 0$  or  $U_i = C_i$  along this characteristic. The forward running characteristic which connects the hole with the backward running characteristic at the edge of the fan carries a constant value of  $U + \frac{2}{\gamma-1} C$  so that

$$(39) \quad \begin{aligned} U_i + \left(\frac{2}{\gamma-1}\right) C_i &= U_{4''} + \left(\frac{2}{\gamma-1}\right) C_{4''} \text{ or} \\ U_i + \left(\frac{2}{\gamma-1}\right) C_i &= 563.6 + 8(2463) \end{aligned}$$

where  $U_i$  and  $C_i$  are the velocity and sound speed at the edge of the hole. Therefore

$$9U_i = 9C_i = 563.6 + 8(2463)$$

$$U_i = C_i = 2252 \text{ ft/sec}$$

Then as previously

$$\begin{aligned}
 (40) \quad T_i &= T_{4''} \left( \frac{C_i}{C_{4''}} \right)^2 \\
 &= 2250 \left( \frac{2252}{2463} \right)^2
 \end{aligned}$$

$$\begin{aligned}
 T_i &= 1881 \text{ } ^\circ\text{R} \\
 (41) \quad P_i &= P_{4''} \left( \frac{T_i}{T_{4''}} \right)^5 \\
 &= 1860 \left( \frac{1881}{2250} \right)^5
 \end{aligned}$$

$$\begin{aligned}
 P_i &= 760 \text{ psia} \\
 (42) \quad \rho_i &= \rho_{4''} \left( \frac{P_i}{P_{4''}} \right)^{\frac{1}{\gamma_4}} \\
 &= 1.778 \left( \frac{760}{1860} \right)^{.8} \\
 \rho_i &= 0.869 \text{ lbm/ft}^3
 \end{aligned}$$

The stagnation pressure at the hole's edge is then

$$\begin{aligned}
 (43) \quad (P_i)_s &= \frac{\rho_i}{g_0} V^2 \\
 &= \frac{0.869}{32.2} \left( \frac{3800}{12} \right)^2 \\
 (P_i)_s &= 2706 \text{ psi}
 \end{aligned}$$

The total pressure at the hole of the second baffle 2.0 inches from the center plane is  $2706 + 760 = 3466 \text{ psia}$ .

The pressure distribution throughout the fan can be computed in the same manner as for the first baffle. Comparing the pressures on the second baffle with those on the first (see Table 5) shows that the stagnation pressures on the second baffle at the hole and outside edge

are roughly one-half those experienced by the first baffle plate. The total force on the second baffle plate would, however, be somewhat less than one-half the force on the first baffle due to the fact that a large portion of the second baffle's area is exposed to a constant pressure of 715 psia.

The pressures on the side plates of the second stage are considerably lower than those on the first stage, ranging from 760 along the center plane to 304 just behind the shock wave.

Portions of the side plate behind the first baffle will be beyond the leading edge of the shock wave in the additional 66 microseconds covered by this analysis. Pressurization of these areas at future times will result from the complex flows which are established following the collision of the leading gas disk with the baffle.

#### ESTABLISHMENT OF STEADY FLOW

The condition of steady state flow will be attained when roughly the backward running characteristic (which is actually swept downstream in this case) reaches the end of the diffuser. The time at which this occurs can be estimated by examining

$$(44) \quad U_4 - C_4 = 3800 - 2918 = 882$$

which is roughly the speed with which pressure signals are swept downstream through the diffuser. Steady flow is attained in the time interval

$$(45) \quad \Delta t = \frac{4"/12}{882} = 33.3(10^{-5}) \text{ sec}$$

The projectile leaves the second stage baffle at

$$(46) \quad t = \frac{10"/12}{3800} = 22(10^{-5}) \text{ sec}$$

so that very shortly after the projectile clears the muzzle brake the diffuser flow becomes steady (assuming the muzzle conditions are quasi-steady).

Steady flow calculations through an area ratio 49/16, i.e., from the entrance to exit of the diffuser section show that the steady state exit conditions are as listed in Table 6 along with those for Region 4' immediately behind the projectile as it uncorks the diffuser. These latter are given by equations (11) through (13).

Table 6

|       | <u>Steady State</u> | <u>Behind Projectile Base</u> |
|-------|---------------------|-------------------------------|
| $T_e$ | 2068 °R             | 2381 °R                       |
| $C_e$ | 2364 fps            | 2534 fps                      |
| $V_e$ | 6146 fps            | 3800 fps                      |
| $P_e$ | 1220 psia           | 2468 psia                     |

The major changes which occur during the transition period to steady state occur in the exit velocity  $V_e$  and the exit pressure. As far as the side plates are concerned, this change is advantageous. Due to the increase in exit velocity, it is difficult to say whether the steady state is better or worse than the transient effects analyzed above.

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