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STATIC AND DYNAMIC BUCKLING OF SHALLOW SPHERICAL SHELLS SUBJECTED TO AXISYMMETRIC AND NEARLY AXISYMMETRIC STEP-PRESSURE LOADS USING SATANS-IIA, A MODIFIED VERSION OF SATANS-II

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THESIS

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by

Michael D. Shutt

December 1976

Thesis Advisor: Robert E. Ball

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20. (continued)

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ABSTRACT

②

A digital computer program for the geometrically nonlinear analysis of totally arbitrarily loaded shells of revolution (SATANS-II) was modified to more accurately account for the conditions at the pole of the shell. This program was used to determine the buckling load of shallow spherical shells of various sizes when subjected to static axisymmetric, dynamic axisymmetric, and dynamic nearly axisymmetric step-pressure loads of infinite duration. A comparison was made between the new buckling results and previous results obtained without the new pole routine. The comparison revealed a significant change in the buckling pressures, due solely to the change in the pole routine. The new static axisymmetric, dynamic axisymmetric, and even the dynamic asymmetric critical buckling pressure loads appear to be fairly reliable results for perfect, shallow shells.

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LIST OF SYMBOLS

b = nondimensional inplane stiffness

E = the modulus of elasticity of the shell

H = the rise of the spherical cap at the pole

h = the thickness of the shell

m = the mass density of the shell

M_s = the meridional bending moment per unit length

n = the Fourier index

P = a nondimensional applied load

P_{CRIT} = the nondimensional critical pressure

q_o = the classical buckling pressure of a complete sphere

$q^{(n)}$ = a column matrix containing the coefficients of the n^{th} term in the series expansion of the applied load

r = the normal distance from the axis of revolution to the surface of the cap

r_o = the normal distance from the axis to the cap in the base plane; the maximum value of r

R_s, R_θ = the radii of curvature in the s and θ directions, respectively

s = the meridional distance along the surface of the shell

t = the nondimensional time

T = the time

T_o = a reference time

U, V, W = the displacements in the s, θ and ζ directions, respectively

u, v, w = nondimensional series coefficients of U, V, W

$\bar{V}$ = a nondimensional measure of the volume of the shell deformation

$\bar{V}_{MAX}$ = the peak in the time history of the parameter $\bar{V}$

$W^{(n)}$ = the displacement in the ζ direction in the n^{th} harmonic

δt = the nondimensional time increment

= distance between stations

$\varepsilon^{(n)}$ = the nondimensional parameter governing the magnitude of the load applied in the asymmetric harmonics

ζ = the coordinate normal to the surface of the shell

θ = the circumferential angle measured about the axis of revolution

λ = a nondimensional geometric parameter used to describe the spherical cap

ν = Poisson's ratio

ξ = the normal distance from the base plane to the middle surface of the undeformed cap

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I. INTRODUCTION

In 1973 a digital computer study was presented by Ball and Burt [1] for the dynamic buckling load of clamped shallow spherical shells subjected to axisymmetric and nearly axisymmetric step-pressure loads. A static buckling analysis of the same spherical shells had been carried out in 1970 by Stilwell and Ball [2]. In these two studies the digital computer program SATANS-I [3] was used to calculate the critical buckling pressures for a large range of shell sizes. Other studies of the buckling of shallow shells have been conducted by Huang [4,5], by Stephens and Fulton [6], by Lock et al. [7], by Stricklin [8], and most recently by Akkas [9]. In Reference 1 the results from these other studies, except for those by Akkas, are compared with the results from SATANS-I for both static and dynamic buckling. In the axisymmetric static analysis the comparison with the results obtained by Huang [4] revealed that the SATANS-I results were higher than Huang's results for several shell sizes. In the dynamic, axisymmetric buckling analysis the SATANS-I results again either agreed closely with, or were somewhat higher than , the results by Huang [5], Stephens and Fulton [6], and Stricklin [8]. However, it was noted then that there was a general lack of consistent agreement among any of the sets of results. As a consequence, it appeared at that time that the axisymmetric buckling problem had not yet been totally resolved and that additional studies would be appropriate.

In the asymmetric dynamic buckling analysis of Reference 1 the few comparisons that could be made for the critical load also indicated that the SATANS-I results may be too high. A comparison of the recent estimates for the asymmetric dynamic buckling load obtained by Akkas [9] with the SATANS-I results also reveals the SATANS-I results to be well above those of Akkas [9]. However, it should be noted that the results obtained by Akkas were from his attempt to obtain a lower bound on the critical asymmetric load. This bound on the buckling load is obtained without the execution of a complete transient response analysis on the asymmetric part of the response of the shell, as is done in SATANS-I. In Akkas' analysis (Problem 1) the transient nonlinear axisymmetric response is computed, and a determinant is examined for possible bifurcation into asymmetric motion at each time step. The minimum load at which the determinant becomes zero is defined as the lower bound of the critical load.

As a consequence of the generally high buckling loads predicted by SATANS-I, a re-examination of the static and dynamic buckling of the shallow spherical shell was made in an attempt to determine the possible cause, or causes, of the high buckling loads. In our search we discovered that a modification of the manner in which the pole conditions are numerically approximated significantly lowered the buckling loads to values that are now in good agreement with the other results. The new procedure for handling the pole condition is given in section III of this thesis. The new buckling results are given in section V.

In addition to the pole condition modifications and the new buckling results the author has also made another significant change to the SATANS family of codes. In particular, the SATANS-II program for the geometrically nonlinear analysis of totally arbitrarily loaded shells of revolution, developed by Ryan [10] in 1972 to handle more complex and larger problems, was modified to make the computer memory requirement a variable quantity. This quantity is specified by the user to fit the particular problem being run. It eliminates the large core requirement of SATANS-II for small problems and allows for much larger problems to be solved than could be solved by SATANS-II. The new program with the pole condition and memory modifications will hereafter be called SATANS-IIA. It is described in section II.

II. DESCRIPTION OF SATANS-IIA

SATANS-II was developed by Ryan [10] from SATANS-I and incorporated the full trigonometric expansion of the applied load and solution vector, and introduced the handling of imperfections into the code. These modifications allow the analysis of shells under totally arbitrary loads, as well as imperfection studies on actual shells with measured imperfections [11]. Unfortunately, the original deck of cards for SATANS-II was destroyed. Professor Johann Arbocz of CALTECH had a listing of SATANS-II and punched a deck of cards with the changes to SATANS-I given in that listing. A copy of this deck was sent to Professor Ball. These cards have been added by the author to the original SATANS-I described by Ryan [10] and a complete version of SATANS-II has been reconstructed. SATANS-IIA is a modification by the author of the reconstructed SATANS-II program. A listing of SATANS-IIA can be found in Appendix A. The listing contains an example problem for the dynamic analysis of a clamped, truncated cone subjected to an impulsive loading which is uniform along the meridian and varies in a cosine distribution over one-half of the circumference. This problem is a sample problem suggested by the Lockeed Missiles and Space Corp. [12]. A condensed version of the output from the example problem is given in Appendix B. Input data preparation for SATANS-IIA can be found in Appendix C. The basic users manual, which includes preparation of input subroutines and the theory of the program, is contained in Reference 3, which can be obtained through COSMIC (M70-10098, LAR-10736), or ASIAC [13]. A users manual which includes preparation and handling of imperfection data within the SATANS programs can be found in

Ref. [10]. The above information, along with the following discussion, will inform the user on the capabilities and proper use of SATANS-IIA.

The modification of the SATANS-II program to make its core requirement variable was accomplished by putting in a single dimension statement at the beginning of the program, with subsequent dimensioning within the subroutines to only the first element of the vector or matrix. This is a convenient feature of the FORTRAN-IV language in which the program is written. The actual vector and matrix sizes are transmitted to the subroutines by an individual parameter list. Construction of the initial dimension statement and core request size is as follows:

The basic size of the program on the IBM-360/67 Digital Computer, without the initial dimension statement, is 272,000 bytes. This figure includes approximately 19,000 bytes of buffer space required for execution. Within the main dimension statement are fifteen variables. However, only three parameters are needed to specify the sizes of these fifteen variables.

Let a= The number of stations along the meridian of the shell times the number of harmonics considered.
Let b= a, plus two fictitious stations times the number of harmonics considered.
Let c= The number of harmonics considered.

The main dimension statement would then be constructed as,

```
DIMENSION P(4,4,a), DEE(4,4,a), DST(4,4,a), X(4,a),
          PHIXB(a), PHITB(a), Z(4,b), ZO(4,b),
          Z2(4,b), Z3(4,b), ZDOT(4,b), IS(99,c),
          JS(99,c), ID(99,c), JD(99,c)
```

The 99's above limit the user to 99 harmonics in any one run and an unlimited number of meridional stations. The core requirement for the general case would be,

272,000 + 216a + 80b + 1584c = bytes of core required.

For a sample calculation of the core requirements consider the example of a spherical cap with 40 stations along the meridian, and an asymmetric analysis with two harmonics. Therefore,

a= 40(stations) x 2(harmonics) = 80
b= 80 + 2 x 2(harmonics) = 84
c= 2(harmonics)

Thus, for the variables P, DEE, DST,
3 x (4x4x80) = 3840 (words) x 4 = 15,360 bytes

for the variable X,
4 x (80) = 320 (words) x 4 = 1280 bytes

for the varibles PHIXB, PHITB,
2 x (80) = 160 (words) x 4 = 640 bytes

for the varibles Z, ZO, Z2, Z3, ZDOT,
5 x (4x84) = 1680 (words) x 4 = 6720 bytes

lastly, for the varibles ID, JD, IS, JS,
4 x (99x2) = 792 (words) x 4 = 3168 bytes

Therefore, the total size of the main dimension statement would be 27,168 bytes. This figure would be rounded up to the nearest even thousand bytes, i.e. 28,000 bytes. Finally, the core requirement for this example problem would be

272,000 + 28,000 = 300,000 bytes.

III. IMPROVED POLE ROUTINE

The SATANS code is based upon Sander's geometrically nonlinear equations under the conditions of small strains and moderately small rotations. The formulation is in four second order nonlinear partial differential equations in terms of U, V, W, and M_s, where U, V, and W are the meridional, circumferential and normal displacements respectively, and M_s is the meridional bending moment. The nonlinear partial differential equations in the coordinates s, θ , and t are reduced to uncoupled sets of linear differential equations in s and t by expanding the variables in trigonometric series in the circumferential coordinate θ, and treating the nonlinear terms as pseudo loads. The first and second derivatives in the meridional coordinate s are replaced by the conventional central finite difference approximations, i.e.

$$\{z\}'_i = 1/2\Delta \ (\{z\}_{i+1} - \{z\}_{i-1}) \qquad (1)$$

and

$$\{z\}''_i = 1/\Delta^2 \ (\{z\}_{i+1} - 2\{z\}_i + \{z\}_{i-1}) \qquad (2)$$

where $\{z\}_i$ is the vector of U, V, W, and M_s at the i^{th} station, Δ is the uniform dimension between stations, and primes denote partial derivatives with respect to s. Applying these approximations to the governing set of domain equations leads to

$$[C]_i \{z\}_{i-1} + [B]_i \{z\}_i + [A]_i \{z\}_{i+1} = \{g\}_i \qquad (3)$$

When the shell does not have a pole, fictitious stations one increment off of the shell are introduced at each end. Both the governing domain equations and the boundary conditions are applied at the two boundary points. Thus, all finite difference approximations to the derivatives, including those of the boundary conditions, are of order Δ^2. However, prior to the development of SATANS-IIA, the treatment of the conditions to be applied at a pole at either end of a shell was handled by a simple Euler forward or backward difference approximation to the first derivative, with truncation error of order Δ. For example, for a pole at s= 0, where i= 1, the first derivative at the pole was approximated with

$$\{z\}'_1 = 1/\Delta \ (\{z\}_2 - \{z\}_1). \qquad (4)$$

At the time this procedure for handling the pole conditions was developed (1967) it was thought that this would not significantly alter the solution. However, it has since been discovered that such is not the case.

For the new pole routine, an expanded forward difference approximation of order Δ^2 is used at s= 0 which takes into account the two stations after the pole, instead of just one station after the pole as in the Euler scheme. This approximation is

$$\{z\}'_1 = 1/2\Delta \ (-3\{z\}_1 + 4\{z\}_2 - \{z\}_3). \qquad (5)$$

The conditions to be imposed upon the dependent variables at a pole are derived in Reference 14. They are :

For N= 0, $u_1 = v_1 = w'_1 = m'_{s1} = 0.$

Applying equation (5), these conditions can be put into the matrix form

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -3 & 0 \\ 0 & 0 & 0 & -3 \end{bmatrix} \begin{Bmatrix} u \\ v \\ w \\ m_s \end{Bmatrix}_1 + \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 4 & 0 \\ 0 & 0 & 0 & 4 \end{bmatrix} \begin{Bmatrix} u \\ v \\ w \\ m_s \end{Bmatrix}_2 + \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix} \begin{Bmatrix} u \\ v \\ w \\ m_s \end{Bmatrix}_3 = 0.$$

where the above 3 matrices are DL, DG, and DF within the SATANS programs.

For N= 1, $u_1 \pm v_1 = u' = w = m_s = 0,$

where the plus sign applies at an initial pole, and the minus sign at a final pole. The matrix form for these conditions is

$$\begin{bmatrix} -3 & 0 & 0 & 0 \\ 1 & \pm 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{Bmatrix} u \\ v \\ w \\ m_s \end{Bmatrix}_1 + \begin{bmatrix} 4 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \begin{Bmatrix} u \\ v \\ w \\ m_s \end{Bmatrix}_2 + \begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \begin{Bmatrix} u \\ v \\ w \\ m_s \end{Bmatrix}_3 = 0.$$

For N=2, $u = v = w = m'_s = 0$

the matrix form is

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -3 \end{bmatrix} \begin{Bmatrix} u \\ v \\ w \\ m_s \end{Bmatrix}_1 + \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 4 \end{bmatrix} \begin{Bmatrix} u \\ v \\ w \\ m_s \end{Bmatrix}_2 + \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix} \begin{Bmatrix} u \\ v \\ w \\ m_s \end{Bmatrix}_3 = 0.$$

For N > 2, $u = v = w = m_s = 0$

and DL= identity matrix, DG= DF= null matrices.

The sclution procedure in SATANS is an elimination scheme and starts with

$$\{z\}_1 = -[P]_1\{z\}_2 + \{x\}_1 , \tag{6}$$

where the values in $[P]_1$ based upon the Euler approximation are defined in Reference 14. The higher order approximation defines a new $[P]_1$. This new $[P]_1$ is obtained by simultaneously solving the pole conditions

$$[DL]\{z\}_1 + [DG]\{z\}_2 + [DF]\{z\}_3 = \{0\}, \tag{7}$$

and the domain equation at station 2 next to the pole

$$[C]_2\{z\}_1 + [B]_2\{z\}_2 + [A]_2\{z\}_3 = \{g\}_2 , \tag{8}$$

to eliminate $\{z\}_3$. Thus,

$$\{z\}_3 = [A]_2^{-1}(\{g\}_2 - [C]_2\{z\}_1 - [B]_2\{z\}_2). \tag{9}$$

Substituting equation (9) into equation (7) gives

$$[DL]\{z\}_1 + [DG]\{z\}_2 + [DF][A]_2^{-1}(\{g\}_2 - [C]_2\{z\}_1 - [B]_2\{z\}_2) = 0. \tag{10}$$

Combining like coefficients of the {z} vector leads to

$$([DL] - [DF][A]_2^{-1}[C]_2)\{z\}_1 + ([DG] - [DF][A]_2^{-1}[B]_2)\{z\}_2 = -[DF][A]_2^{-1}\{g\}_2. \tag{11}$$

Finally, solving for $\{z\}_1$ yields

$$\{z\}_1 = -[DL - DF \times A_2^{-1} \times C_2]^{-1} [DG - DF \times A_2^{-1} \times B_2] \{z\}_2$$

$$+ [DL - DF \times A_2^{-1} \times C_2]^{-1} [-DF \times A_2^{-1}] \{g\}_2. \qquad (12)$$

Thus, $[P]_1 = -[DL - DF \times A_2^{-1} \times C_2]^{-1} [DG - DF \times A_2^{-1} \times B_2]$ and $\{x\}_1 = [DL - DF \times A_2^{-1} \times C_2]^{-1} [-DF \times A_2^{-1}] \{g\}_2$. The new $[P]_1$ matrix has been placed into the "PMATRX" subroutine of SATANS-IIA and the new $\{x\}_1$ vector has been placed in the "FORCE" subroutine.

A listing of the pole routine may be found in Appendix D. To incorporate this new routine into a SATANS-I or-II program, first proceed to the "PMATRX" subroutine and remove the fifteen cards that are between, but not including, "IF(NN.GT.2) GO TO 90" and "11 CONTINUE". These cards are located after statement number "14" and just before statement number "11". Replace the cards removed by the ones listed in Appendix D which read from" C IN PMATRX " to " 90 M3=MN". Then proceed to the "FORCE" subroutine and remove statement number "10". Replace statement number "10" with the nine cards listed in Appendix D which read from " C IN FORCE" to "DO 11 I= 1,4" . Also place " COMMON /IBL5/IBCINL, IBCFNL " into the common area of the " FORCE " subroutine.

This completes the implementation of the new pole routine into either SATANS-I or II.

IV. PROBLEM DESCRIPTION

The geometry of the shallow spherical shell used in this study is identical to that used in Reference 1. Briefly, the shallow shell can be specified by the non-dimensional parameter λ , where

$$\lambda = 2[\,3\,(\,1 - \nu^{2}\,)\,]^{1/4}\,(\,H/\,h\,)^{1/2}. \tag{1}$$

H is the rise of the shell, h is the thickness, and ν is Poisson's ratio. The mass density of the shell is m. All shells analyzed had the following dimensions;

Radii of Curvature $R_s = R_\theta = 250$ inches

Thickness $h = 0.25$ inches

Modulus of Elasticity $E = 30{,}000{,}000$ psi

Poisson's Ratio $\nu = 0.3$

All buckling pressures obtained will be listed as a percent of the classical buckling pressure of a complete sphere, q_0, where

$$q_0 = [\,2\,E\,(\,h/R_s)^{2}\,]\,/\,[\,3\,(\,1 - \nu^{2}\,)\,]^{1/2} \tag{2}$$

Forty stations were used over the meridian. The nondimensional time increment δ t, where

$$t = T\,/\,(\,R_s^2 m\,/\,E)^{1/2}, \tag{3}$$

was taken as 0.05 for 3000 time steps, which is a total nondimensional time of 150. In addition, the axisymmetric analysis was repeated with a larger time step of $\delta t = 0.2$ for a total time of 600. In this study m was selected such that t is equal to T. The necessity for the long response time is explained in Reference 6.

In the axisymmetric analysis only the N= 0 harmonic is considered. However, in the asymmetric analysis a second harmonic is excited by applying an incremental load in that harmonic. In addition, analyses of the shells $\lambda = 6, 7.5,$ and 11 were made using five harmonics. The step pressure load for the axisymmetric harmonic is

$$\{q^{(0)}\} = P\, q_0 \, \{1\}, \tag{4}$$

and the step pressure load for the asymmetric second harmonic is

$$\{q^{(n)}\} = P\, q_0 \, \varepsilon^{(n)} \{1\}, \tag{5}$$

where $n > 0$, and $\varepsilon^{(n)}$ is taken as 0.0001. The value taken for the second harmonic in the asymmetric analysis was the same as the critical harmonic for the static buckling analysis presented by Stilwell and Ball [2]. When there was an uncertainty as to which was the critical static harmonic the two harmonics in question were both tested. Run times using SATANS-IIA with a two-harmonic analysis for 3000 time steps and 40 stations on the meridian took an average of 28 minutes on the IBM 360/67.

The parameter used to determine the minimum load at which dynamic buckling occurs is the peak value of $\bar{V}$, called

$\bar{V}_{MAX}$, where $\bar{V}$ is defined as

$$\bar{V} = \int_0^{r_0} r\, W^{(0)}\, dr \Big/ \int_0^{r_0} r\, \xi\, dr \qquad (6)$$

r is the normal distance from the axis to the shell, r_0 is the maximum value of r, $W^{(0)}$ is the normal displacement of the axisymmetric response and ξ is the vertical distance from the base plane to the undeformed shell. The $\bar{V}$ is a measure of the volume of the shell deformation. The Fortran statements computing $\bar{V}$ and $\bar{V}_{MAX}$ are given in Appendix E. When working a problem that requires these calculations the nineteen cards are inserted directly into the "DYNAMIC" subroutine right after the "IF" statement that calls the "OUTPUT" subroutine.

For convenience, the response in each asymmetric harmonic is also measured using equation (6), with $W^{(0)}$ replaced with $W^{(n)}$. The parameter $\bar{V}$ for the asymmetric harmonics does not represent a volume of deformation as it does for the axisymmetric harmonic. It can, however, be used to indicate the relative excitation of the asymmetric harmonics.

The buckling criterion for both the axisymmetric and the asymmetric dynamic buckling analysis defines the critical load as that load P where a very small increase in P causes a very large increase in $\bar{V}_{MAX}$. This is the same criterion as that used in Ref. [1].

V. RESULTS AND DISCUSSION

A. STATIC AXISYMMETRIC BUCKLING ANALYSIS

Table I presents the new results from the static axisymmetric buckling analyses for $\lambda = 4$ through 13 using the new pole routine. The two upper curves in Figure 1 present a comparison of the new results obtained by SATANS-IIA with those obtained by Stilwell and Ball [2] using the SATANS-I program. As can be seen in this figure, fairly significant changes in the buckling load occurred in the neighborhood of $\lambda = 4, 5$, and 9; and somewhat smaller differences occurred in the region $\lambda = 10$ through 13. The upper data points in Figure 2 present the comparison of the new results from SATANS-IIA with those obtained by Huang [4]. This comparison shows a very good agreement between the two sets of results, except for the largest values of λ. The new results have eliminated the differences that existed between the SATANS-I results and Huang's results.

B. DYNAMIC AXISYMMETRIC BUCKLING ANALYSIS

Figure 3 presents the new results for the peak value of $\bar{V}_{MAX}$ versus P for the various values of λ tested. Table II presents all of the new results for the dynamic axisymmetric buckling load. These loads are selected from figures constructed just like Figure 3. In every case, except for $\lambda = 4$, a value of P slightly above the P_{CRIT} value caused a $\bar{V}_{MAX}$ indicative of buckling, as well as a nonconvergence of the iterative solution procedure.

The lower two curves of Figure 1 present a comparison versus λ of the new axisymmetric dynamic buckling results with the previous buckling results obtained by Ball and Burt [1]. In every case the new critical pressure is lower than the critical pressure obtained using the Euler approximation at the pole.

The lower data points of Figure 2 present a comparison of the new results with those obtained by Huang [5], by Stephens and Fulton [6], and by Stricklin [8]. Just as in the case of the static axisymmetric buckling analysis, the new results compare much more favorably with the other results than did the results of Reference 1. It's interesting to note that the new results now tend to be slightly lower than the other results, whereas the results of Reference 1 were higher for almost all values of λ .

C. DYNAMIC ASYMMETRIC BUCKLING ANALYSIS

Table III presents the new results for the critical pressures obtained from the dynamic asymmetric analysis. The second harmonics, or critical static harmonics, used in the analyses are also presented in Table III. A comparison of the critical pressures from the asymmetric analyses, Table III, with the critical pressures from the axisymmetric analyses, Table II, reveals that only the shell $\lambda = 6$ buckled at a load below the axisymmetric buckling load. For the shell $\lambda = 7$ the critical buckling load was slightly larger when asymmetric motion was considered. In all other cases the buckling was not influenced by the presence of the second harmonic. These new buckling results and those by Ball and Burt [2] are plotted in Figure 4. The new results can be seen to be significantly different from the SATANS-I results, where the asymmetric buckling loads were lower than the axisymmetric loads for five out of the ten values of tested.

Except for λ = 6 and 7, the relationship between $\bar{V}_{MAX}$ and P for the N= 0 harmonic, in the two-harmonic analyses, was found to be essentially identical to the relationship found in the axisymmetric buckling analysis shown in Figure 3. Table IV A presents the $\bar{V}_{MAX}$ versus P data for both the N= 0 harmonic and the second harmonic, for all values of λ tested, except for λ = 6. Note that, except for λ =7 and 11, $\bar{V}_{MAX}$ for the asymmetric harmonic is generally very small, even when the $\bar{V}_{MAX}$ for the N= 0 harmonic indicates that the shell has buckled. Thus, except for the shells λ = 6 and 7, the presence of the asymmetric motion does not influence the axisymmetric motion, and except for the shells λ = 6, 7 and 11 the asymmetric motion is very small prior to buckling in the axisymmetric harmonic.

A more detailed analysis of the shell λ = 6 has been conducted since it was the only shell that revealed any significant axisymmetric sensitivity to asymmetric motion. This shell was studied using two two-harmonic analyses (N= 0, 1 and N= 0, 2) and a five-harmonic analysis (N= 0, 1, 2, 3, and 4). Figure 5 and Tables IV B and IV C contain values of $\bar{V}_{MAX}$ versus P for both of the asymmetric harmonics, N= 1 and N= 2, in the two two-harmonic analyses, as well as the values of $\bar{V}_{MAX}$ for the axisymmetric harmonic, N= 0. Figure 6 and Table IV D present the values of $\bar{V}_{MAX}$ versus P for the N= 0,1,2,3, and 4 harmonics from the five-harmonic study. A comparison of the critical buckling load predicted from the results of the two two-harmonic analyses in Figure 5 with the critical load from the five-harmonic analysis obtained from Figure 6 shows that the presence of the additional harmonics results in the shell buckling at a slightly lower load (0.50), with significant motion in the N= 1 harmonic instead of the N= 2 harmonic (see the nonconverged solution at P= 0.51), which is the critical harmonic for static asymmetric buckling. Studies using five harmonics have also been conducted for $\lambda = 7.5$ and $\lambda = 11$. As can be seen in Table IV D the critical harmonic for $\lambda = 7.5$ remained N= 3; however, significant motion occurred in that harmonic at P= .41 and .44. In the case of $\lambda = 11$, relatively large asymmetric motion occurred in the asymmetric mode of N= 5 vice 6 at a value of P= .46.

The comparison of the new results for the critical pressure for dynamic asymmetric buckling with those obtained analytically by Stricklin [8], by Akkas [9], and experimentally by Lock et al [7] is illustrated in Figure 7. The comparison reveals an agreement with Stricklin in every case, in general a higher value of P_{CRIT} than those obtained by Akkas, and most importantly a very good agreement with Lock's experimental results.

When making the comparison between the new results and those obtained by Akkas, it is necessary to look at the differences in the problem solution parameters used in the two studies. For example, buckling results obtained from SATANS-IIA using the same time increment as used by Akkas,

$\delta t = .2$ for 3000 time steps, were significantly higher than those using the time step of $\delta t = .05$ for many values of λ. Furthermore, the new results had , in some cases, instances of buckling occurring as far out in time as 130. Akkas, to shorten computer run times, observed the cap only for a time of less than 5. Furthermore, only the harmonics N= 1 or 2 or 3 were studied by Akkas for shells $\lambda = 5$ through 12. If the critical harmonic is not studied, the predicted load will be too high. Thus, it appears that Akkas' lower bound loads may not be true lower bounds.

Two additional features of the shell response should be noted. First, shells $\lambda = 6$, 7.5, and 11 exhibited a non-buckled response in the axisymmetric harmonic to a load larger than the defined critical buckling load. This can be seen in Tables IV A and IV C. Second, and most importantly, the buckling load proposed by Ball and Burt [1], and used here, defines buckling to occur when the $\bar{V}_{MAX}$ in the axisymmetric harmonic undergoes a large change due to a small change in P. Another criterion for dynamic buckling in the asymmetric analysis discussed in Reference 1 is to define the buckling load as that threshold load that initiates significant growth in the asymmetric harmonic. Re-examination of the $\bar{V}_{MAX}$ versus P data in Table IV A through D reveals that shells $\lambda = 6$, 7, and 11 exhibited relatively large asymmetric motion at loads smaller that the defined buckling load when compared with other $\bar{V}_{MAX}$ values for those shells, even though the numbers themselves were small when compared with the axisymmetric harmonic. Shells $\lambda = 7.5$ and 12 appear to be borderline cases. If the alternate criterion for buckling is used, the critical buckling loads for shells $\lambda = 6$, 7, and 11 become 0.47, 0.45, and 0.45, respectively. The shells $\lambda = 7.5$ and 12 could have buckling loads as low as 0.40 and 0.44, respectively. These values are more conservative than the definition based upon axisymmetric response. These five shells are the same five shells that exhibited an asymmetric buckling load lower than the axisymmetric buckling load in Reference 1.

VI. SUMMARY AND CONCLUSIONS

A digital computer program for the geometrically nonlinear analysis of totally arbitrarily loaded shells of revolution (SATANS-II) was modified to more accurately account for the conditions at the pole of the shell. This program, called SATANS-IIA, was used to determine the buckling load of shallow spherical shells of various sizes when subjected to static axisymmetric, dynamic axisymmetric, and dynamic nearly axisymmetric step-pressure loads of infinite duration. The cap sizes ranged from $\lambda = 4$ to 13 including $\lambda = 7.5$. A comparison was made between the new buckling results with the improved pole handling routine and the results that did not have the new pole routine. The comparison revealed a significant change in buckling pressures, due solely to the change from an order Δ finite difference approximation of the first derivatives at the pole to an approximation of order Δ^2. These new critical pressures are in very good agreement with the results from other studies of the same spherical shells. This good agreement with other results, which came about as a result of the modification of the pole handling routine, is a strong indication that the manner in which the pole condition is handled is vital to the accuracy of the solutions obtained.

In the asymmetric analysis, two harmonics were included for most of the shells; the axisymmetric harmonic and one asymmetric harmonic. Five-harmonic analyses were conducted for three of the shells. Two buckling criteria for the asymmetric analysis were considered. One defined buckling as that threshold load that caused a large increase in a deformation parameter, $\bar{V}_{MAX}$, in the axisymmetric harmonic. The other, more conservative than the first, defined buckling as that threshold load that caused a large increase in the $\bar{V}_{MAX}$ value for the asymmetric harmonic. Both values have been presented.

The new static axisymmetric, dynamic axisymmetric, and even the dynamic asymmetric critical buckling pressure loads appear to be fairly reliable results for perfect, shallow shells. The effect of realistic imperfections remains to be determined.

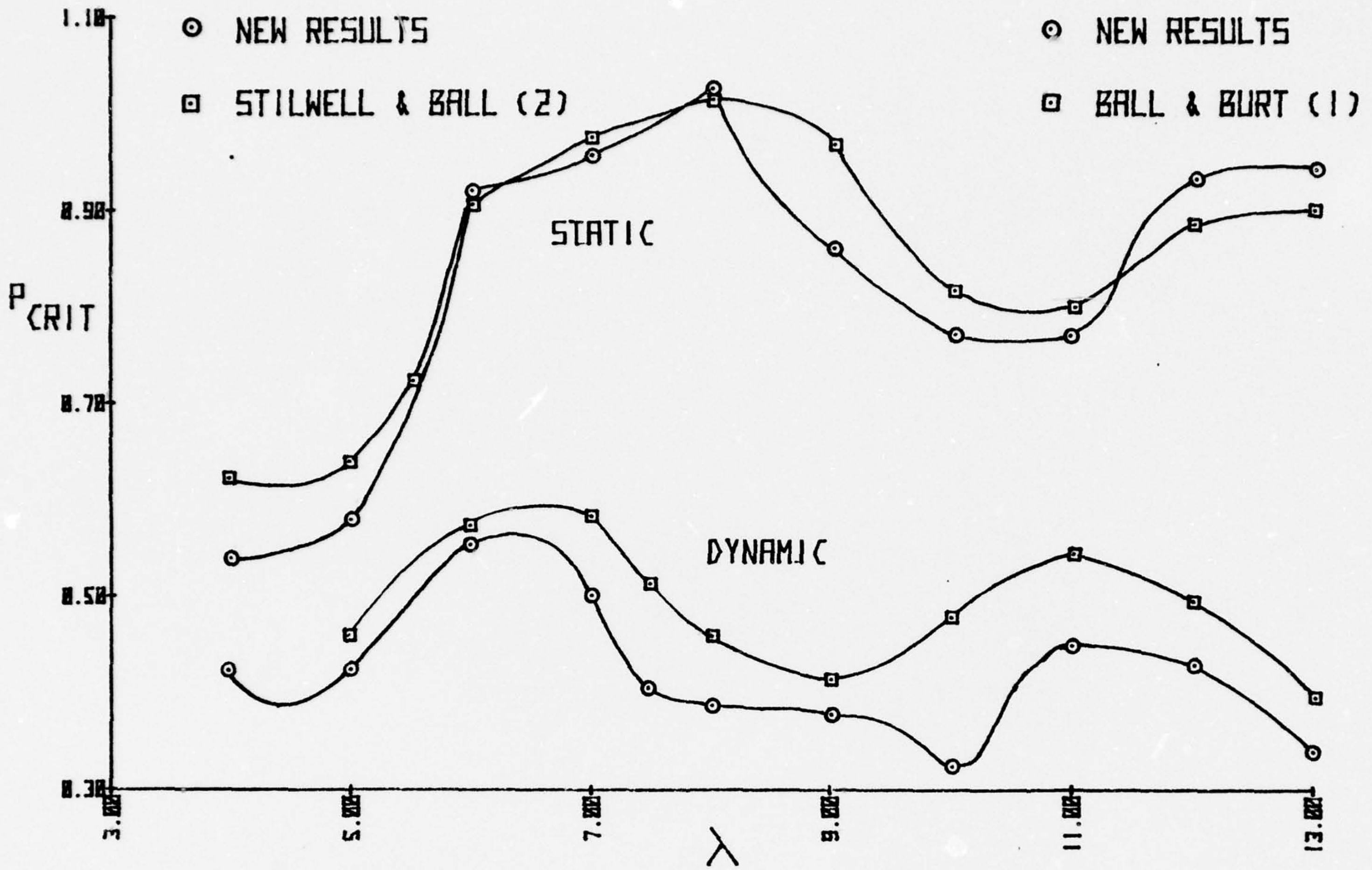

Figure 1 - CRITICAL STEP-PRESSURE LOAD VERSUS λ
AXISYMMETRIC (SATANS-I VERSUS SATANS-IIA)

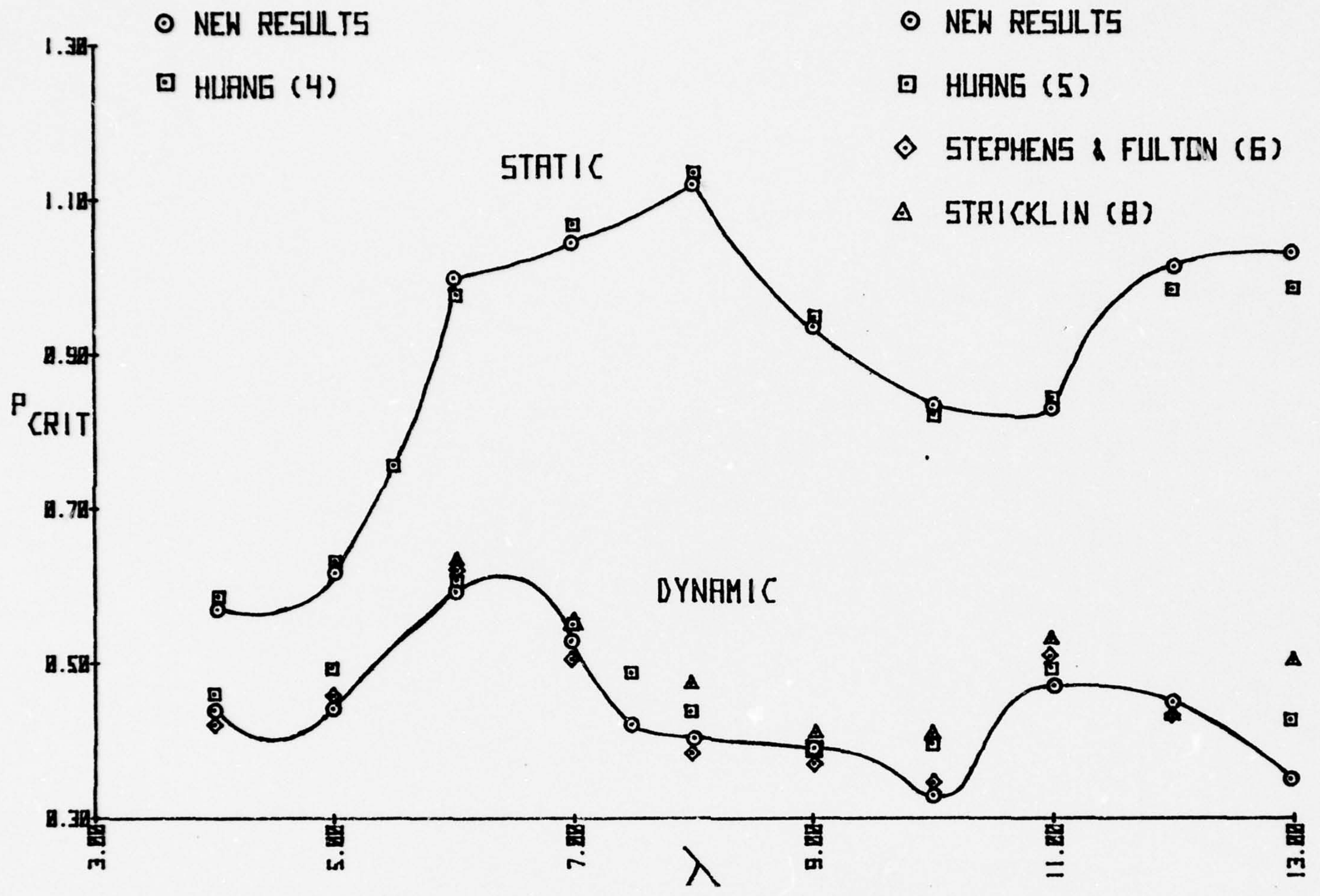

Figure 2 - CRITICAL STEP-PRESSURE LOAD VERSUS λ
AXISYMMETRIC (SATANS-IIA VERSUS ALL OTHERS)

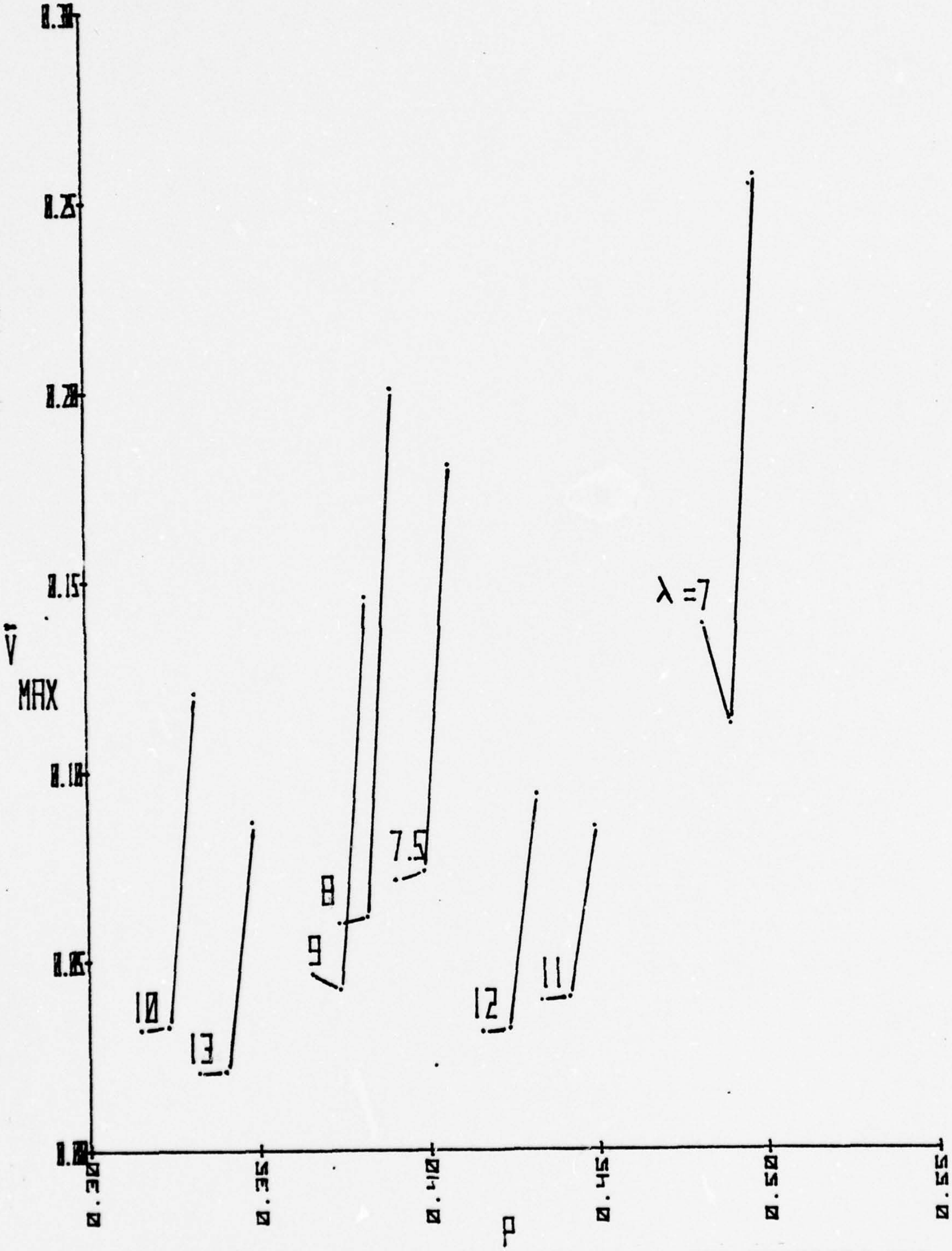

Figure 3 - PEAK DEFLECTION VERSUS P, AXISYMMETRIC AND ASYMMETRIC CASES FOR VARIOUS VALUES OF λ (SATANS-IIA)

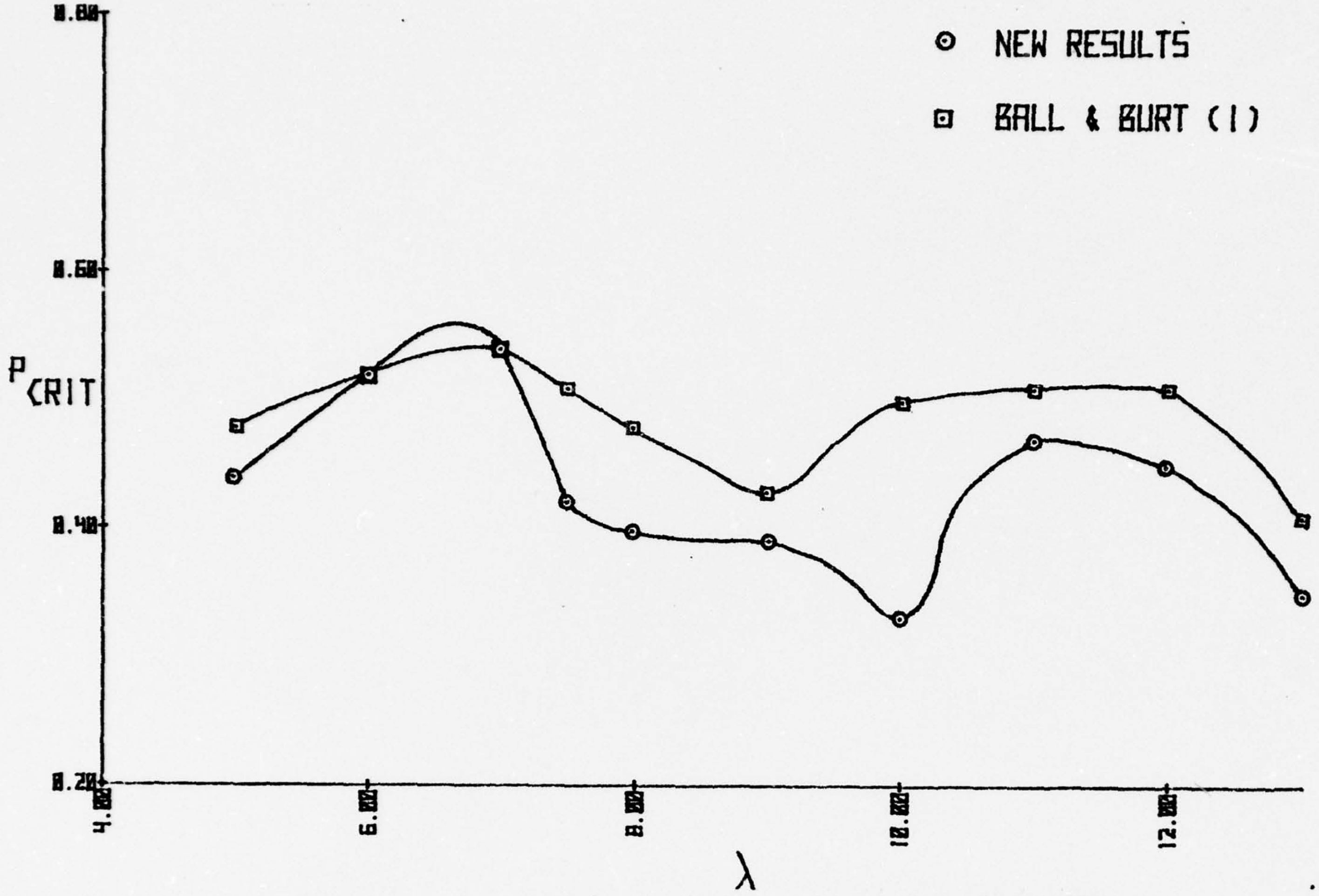

Figure 4 - CRITICAL STEP-PRESSURE LOAD VERSUS λ ASYMMETRIC ANALYSES (SATANS-I VERSUS SATANS-IIA)

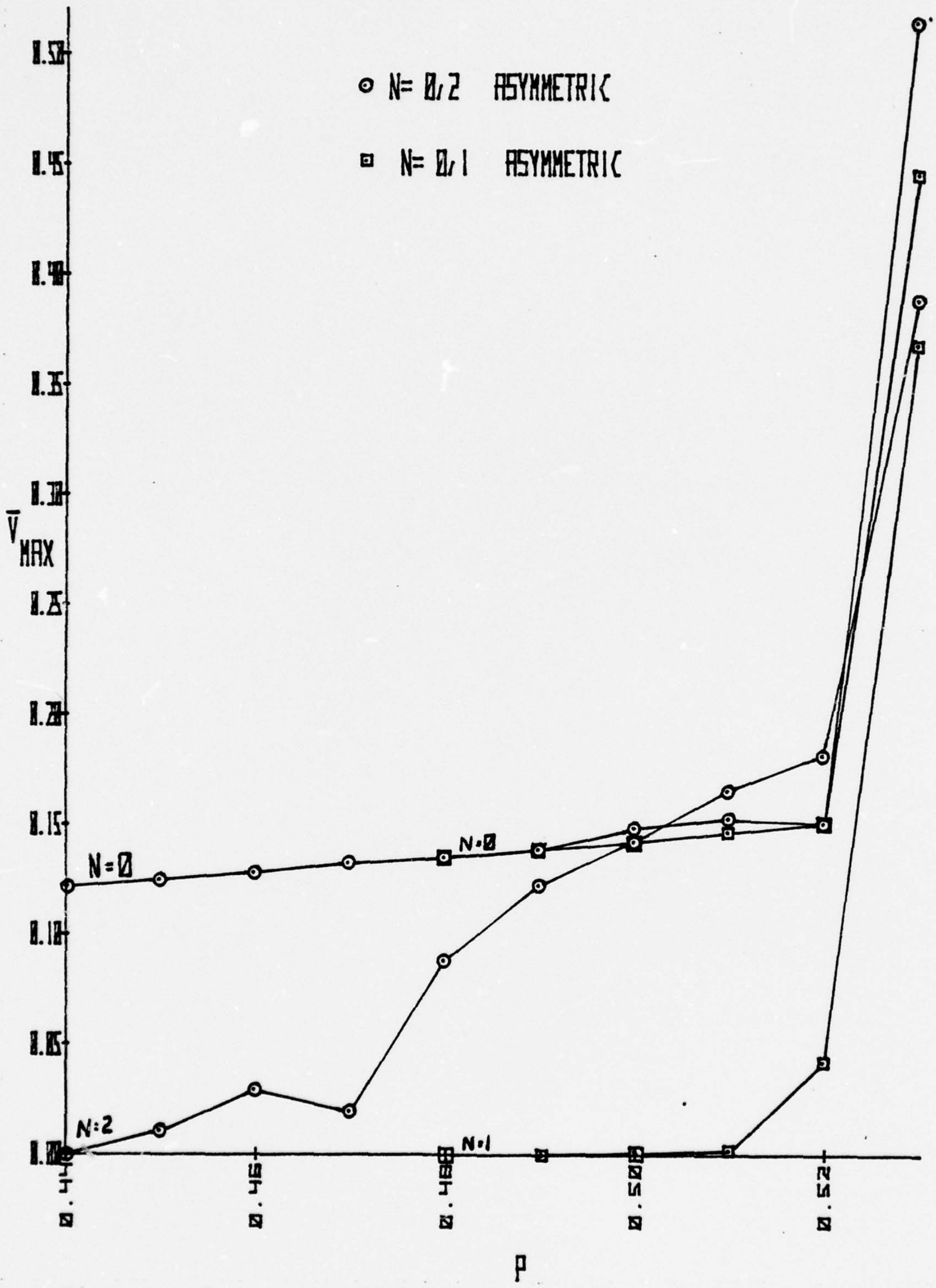

Figure 5 - PEAK DEFLECTION VERSUS P FOR THE ASYMMETRIC ANALYSES OF $\lambda = 6$ (N=0,1 AND N=0,2)

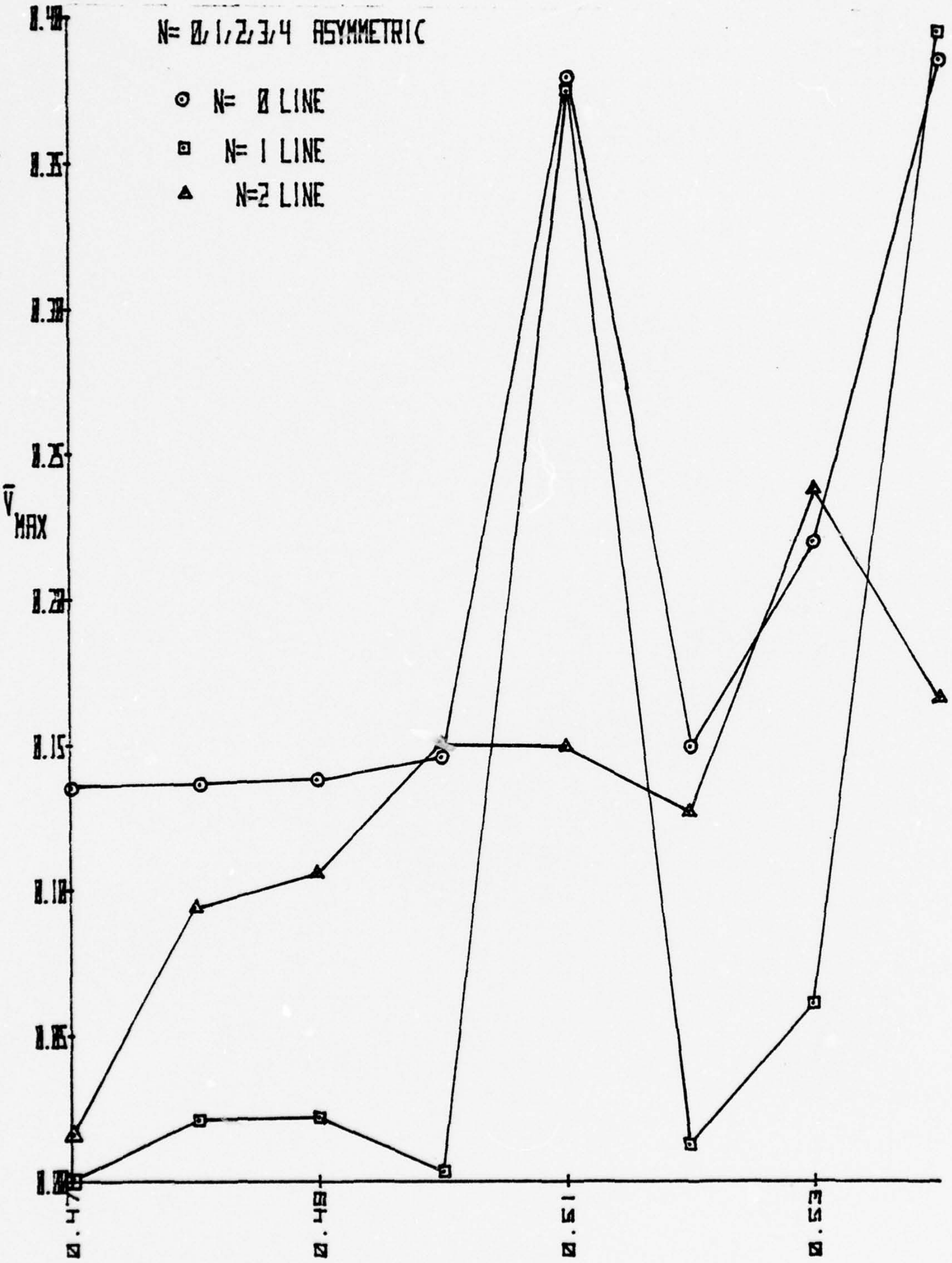

Figure 6 - PEAK DEFLECTION VERSUS P FOR THE ASYMMETRIC ANALYSES OF λ = 6 (N=0,1,2,3,AND4, ONLY N=0,1,AND2 PLOTTED)

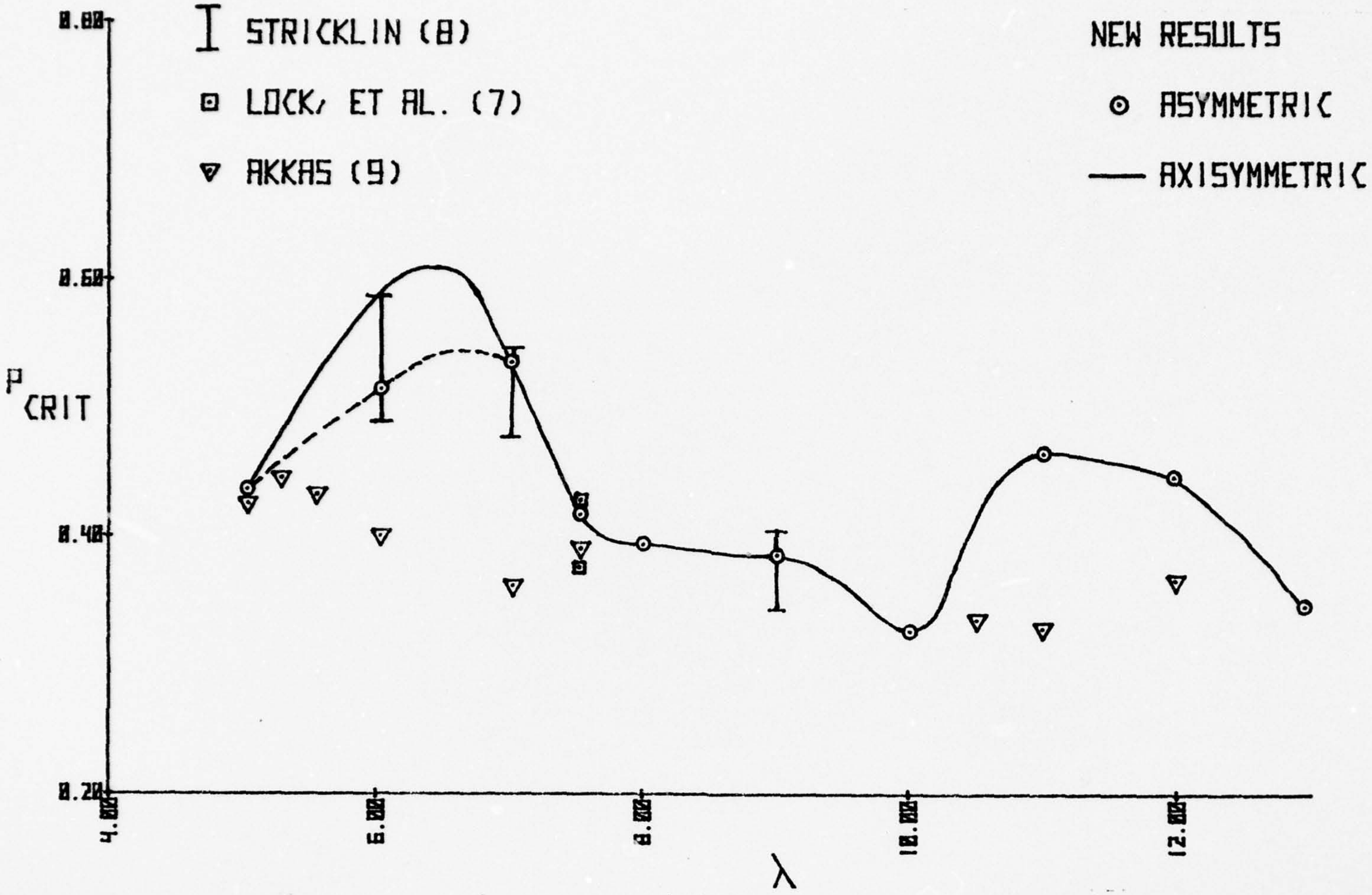

Figure 7 - CRITICAL STEP-PRESSURE LOAD VERSUS λ ASYMMETRIC ANALYSES (SATANS-IIA VERSUS ALL OTHERS)

A. TABLES

1. TABLE I Critical pressure loads from the static axisymmetric analyses.

λ	4	5	6	7	8	9	10	11	12	13
P_{CRIT}	.568	.616	1.0	1.048	1.12	.936	.832	.832	1.016	1.032

2. TABLE II Critical step-pressure loads from the axisymmetric dynamic analyses.

λ	4	5	6	7	7.5	8	9	10	11	12	13
P_{CRIT}	.45	.44	.59	.53	.42	.40	.39	.33	.47	.45	.35

3. TABLE III Critical step-pressure loads from the dynamic asymmetric analyses and critical asymmetric harmonics.

λ	5	6	7	7.5	8	9	10	11	12	13
P_{CRIT}	.44	.52	.54	.42	.40	.39	.33	.47	.45	.35
N_{CRIT}	1	2	3	3	4	5	6	7	8	9

4. TABLE IV Dynamic asymmetric analyses for $\bar{V}_{MAX}$ versus P.

1. TABLE IV A. Two-harmonic analyses for all values of λ exept $\lambda = 6$.

λ = 5 N= 0 and 2

P	.43	.44	.45
N= 0	.1659	.1676	.6606
N= 2	.0004787	.0000566	.0687

N= 0 and 1

P	.44	.45
N= 0	.1675	.6606
N= 1	.0003145	.0687

P	.46
N= 0	.7653
N= 1	.001092

λ = 7, N= 0 and 3

P	.45	.46	.47	.48	.49	.50	.52
N= 0	.09452	.09571	.09812	.1005	.1029	.1052	.1099
N= 3	.000889	.007456	.05052	.04323	.0279	.0335	.07488

P	.53	.54	.55
N= 0	.1122	.1146	.2709
N= 3	.05997	.06252	.03809

λ = 7.5, N= 0 and 3

P	.40	.41	.42	.43	.44	.45
N= 0	.0703	.07228	.07429	.2636	.07837	.2076
N= 3	.0001094	.001296	.0004304	.002754	.001188	.000338

P	.46
N= 0	.200
N= 3	.0003276

λ = 8, N= 0 and 4

P	.38	.39	.40	.41	.42	.43	.44
N= 0	.05893	.0607	.0624	.1964	.1713	.1957	.2297
N= 4	.0000566	.0000703	.0000364	.0000333	.0000274	.0000299	.0000326

λ = 9 N= 0 and 4

P	.38	.39	.40
N= 0	.04738	.04875	.1576
N= 4	.00003597	.00004635	.00004497

N= 0 and 5

P	.40
N= 0	.05012
N= 5	.00008385

λ = 10, N= 0 and 5

P	.32	.33	.34	.36	.38	.40
N= 0	.03239	.03347	.1086	.1217	.1288	.1235
N= 5	.0000281	.0000472	.00004125	.00002103	.0000449	.000114

λ = 11, N= 0 and 6

P	.45	.46	.46	.48	.49	.50
N= 0	.03910	.04004	.04099	.09814	.04241	.08824
N= 6	.004595	.01332	.02232	.02864	.03955	.02813

λ = 12, N= 0 and 7

P	.44	.45	.46
N= 0	.03236	.03316	.08633
N= 7	.00004214	.0004561	.00005158

λ = 13, N= 0 and 8

P	.34	.35	.36	.38	.40
N= 0	.02119	.02185	.06637	.07844	.07381
N= 8	.00001148	.00001134	.000006607	.000008245	.000119

2. TABLE IV B. Two-harmonic analyses with N= 0 and 1, λ = 6 only.

P	.48	.49	.50	.51	.52	.53
N= 0	.1350	.1385	.1421	.1460	.1499	.4453
N= 1	.0002797	.000195	.000245	.000926	.04081	.3668

3. TABLE IV C. Two-harmonic analyses with N= 0 and 2, λ = 6 only.

P	.44	.45	.46	.47	.48	.49	.50
N= 0	.1218	.1250	.1276	.1320	.1350	.1385	.1479
N= 2	.000239	.0101	.0293	.01976	.08768	.1223	.1419

P	.51	.52	.53	.54	.55	.56
N= 0	.1526	.1499	.5137	.5060	.2040	.5305
N= 2	.1654	.1816	.3878	.3996	.2156	.3617

4. TABLE IV D Five-harmonic analyses for selected shells.

λ = 6 N= 0,1,2,3, and 4

P	.47	.48	.49	.50	.51	.52	.53
N= 0	.1313	.1347	.1382	.1460	.3797	.1498	.2200
N= 1	.00021	.02108	.02215	.003676	.3743	.01276	.0616
N= 2	.0187	.0953	.1069	.1507	.1502	.1279	.2385
N= 3	.000181	.006237	.01437	.00163	.0405	.0123	.03978
N= 4	.0031	.04757	.05428	.04402	.05896	.0495	.064

P	.54
N= 0	.3854
N= 1	.3953
N= 2	.1671
N= 3	.05298
N= 4	.0613

λ = 7.5 N= 0,1,2,3,4 and 4

P	.40	.41	.42	.43	.44	.45
N= 0	.0703	.07228	.07429	.2592	.07837	.2544
N= 1	.00004855	.00004198	.00006093	.0002737	.0001167	.005952
N= 2	.0001164	.00007456	.0004184	.0000982	.000788	.0003188
N= 3	.0001277	.001187	.0004597	.0002853	.00107	.0003188
N= 4	.0008224	.0001898	.0002448	.0000526	.000280	.000134

λ = 11 N= 0,4,5,6, and 7

P	.45	.46	.47	.48	.49	.50
N= 0	.03910	.04004	.0499	.04195	.04291	.1040
N= 4	.0005759	.001263	.0009774	.001388	.002657	.001565
N= 5	.009568	.0140	.0124	.02239	.02759	.01548
N= 6	.002560	.007828	.02330	.02767	.02602	.02644
N= 7	.0001743	.0001486	.0002021	.01202	.02048	.02064

APPENDIX A

LISTING OF SATANS-IIA

```
C***********************************************************************SAT00010
C     THIS PROGRAM SERVES AS THE 'MAIN' PROGRAM, AND CALLS 'SATANS',    *SAT00020
C     AND CHECKS 'IRNAGN' TO SEE IF WE DESIRE ANOTHER RUN              *
C***********************************************************************SAT00030
      DIMENSION P(4,4,124),DEE(4,4,124),DST(4,4,124),X(4,124),Z(4,132),
     1ZO(4,132),Z2(4,132),Z3(4,132),ZDOT(4,132),IS(99,4),JS(99,4),
     2ID(99,4),JD(99,4),PHIXB(124),PHITB(124)
      COMMON /BLRUN/ IRNAGN
      COMMON /BLTHTA/ THETAM,COEFF
    1 CONTINUE
      CALL SATANS (P,DEE,DST,X,Z,ZO,Z2,Z3,ZDOT,IS,JS,ID,JD,PHIXB,PHITB)
      IF (IRNAGN.EQ.1) GO TO 1
      CALL FLYNVY                                                       SAT00080
      STOP                                                              SAT00090
      END                                                               SAT00100
                                                                        SAT00110
      SUBROUTINE GEOM                                                   SAT00120
C***********************************************************************SAT00130
C      THIS SUBROUTINE COMPUTES THE NONDIMENSIONAL GEOMETRY FUNCTIONS*SAT00140
C        OF THE SHELL                                                  *SAT00150
C***********************************************************************SAT00160
      REAL NU,LAM,LAM2,JAY,MT,LSD18,LSD1N,MASS                          SAT00170
      COMMON /IBL4/ KMAX,KL                                             SAT00180
      COMMON /BL8/  R(500),GAM(500),OMT(500)                            SAT00190
      COMMON /BL11/ OMXI(500),PHEE,TO,T2                                SAT00200
      COMMON /BL17/ DEL                                                 SAT00210
      COMMON /BL20/ DEOMX(500)                                          SAT00220
      COMMON /BL32/ TKN,ELAST,CHAR,SIGC                                 SAT00230
      COMMON /BL102/ DELOAD                                             SAT00240
      COMMON /BL103/ MASS(500)                                          SAT00250
      COMMON /BLTHTA/ THETAM
      AKX=KMAX-1
      DEL=1./AKX
      THET=ARSIN(2.2801/CHAR)
      DO 11 K=1,KMAX
      AK=K
      R(K)=(7.9459+(AK-1.)*(2.2801)/AKX)/CHAR
      GAM(K)=(2.2801/CHAR)/R(K)
      OMXI(K)=0.
      DEOMX(K)=0.
      OMT(K)=COS(THET)/R(K)
      MASS(K)=1.
   11 CONTINUE
      RETURN                                                            SAT00350
      END                                                               SAT00360
                                                                        SAT00370
      SUBROUTINE BDB(K,B,DB,D,DD)                                       SAT00380
C***********************************************************************SAT00390
```

```
C        THIS SUBROUTINE COMPUTES THE NONDIMENSIONAL IN-PLANE AND     *SAT00400
C        BENDING STIFFNESSES OF THE SHELL                              *SAT00410
C***********************************************************************SAT00420
      REAL NU,LAM,LAM2,JAY,MT,LSD18,LSD1N                               SAT00430
      COMMON /BL15/ NU,U1(99),V1(99),W1(99),V2(99),U2(99),W2(99),U3(99),SAT00440
     1              V3(99),W3(99)                                       SAT00450
      COMMON /BL17/ DEL                                                 SAT00460
      COMMON /BL32/ TKN,ELAST,CHAR,SIGC                                 SAT00470
      B=1.089082
      D=.09075683
      DE=0.
      DD=0.
      RETURN                                                            SAT00520
      END                                                               SAT00530
                                                                        SAT00540
      SUBROUTINE PLOAD(K,Z)                                             SAT00550
C***********************************************************************SAT00560
C        THIS SUBROUTINE ESTABLISHES THE NON-DIMENSIONAL FOURIER       *SAT00570
C        COEFFICIENTS OF THE LOADS APPLIED TO THE SHELL                *SAT00580
C***********************************************************************SAT00590
      REAL MASS                                                         SAT00600
      DIMENSION Z(4,1)                                                  SAT00610
      COMMON /IBL1/ MNMAX                                               SAT00620
      COMMON /IBL2/NN(99),MNINIT                                        SAT00630
      COMMON /IBL4/ KMAX,KL                                             SAT00640
      COMMON /IBL8/ LSTEP,ITR                                           SAT00650
      COMMON /BL3/  PR(99),PX(99),PT(99)                                SAT00660
      COMMON /BL6/  SOE,OSE,ALOAD                                       SAT00670
      COMMON /BL8/  R(500),GAM(500),OMT(500)                            SAT00680
      COMMON /BL32/ TKN,ELAST,CHAR,SIGC                                 SAT00690
      COMMON /BL102/ DELOAD                                             SAT00700
      COMMON /BL103/ MASS(500)                                          SAT00710
      COMMON /BL17/DEL/BL100/TEED,$DYNMC                                SAT00720
      COMMON /BLTHTA/ THETAM,COEFF
      RETURN                                                            SAT00910
      END                                                               SAT00920
      SUBROUTINE  INITL (Z,ZO,Z2,Z3,ZDOT)                               SAT01110
C***********************************************************************SAT01120
C     THIS SUBROUTINE DESCRIBES THE INITIAL CONDITIONS FOR DYNAMIC CASESSAT01130
C***********************************************************************SAT01140
      IMPLICIT LOGICAL*1 ($)                                            SAT01150
      DIMENSION Z(4,1),ZO(4,1),Z2(4,1),Z3(4,1),ZDOT(4,1)                SAT01160
      COMMON /IBL1/ MNMAX                                               SAT01170
      COMMON /IBL2/ NN(99),MNINIT                                       SAT01180
      COMMON /IBL4/ KMAX,KL                                             SAT01190
      COMMON /IBL9/ MAXM                                                SAT01200
      COMMON /IBL12/ KMAX1,KMAX2,NCONV                                  SAT01210
      COMMON /BL6/  SOE,OSE,ALOAD                                       SAT01220
```

```
      COMMON /BL32/ TKN,ELAST,CHAR,SIGO                                 SAT01230
      COMMON /BL100/ TEEO,$DYNMC                                        SAT01240
      COMMON /BL101/  DELSD                                             SAT01250
      NN(1)=0
      NN(2)=1
      NN(3)=2
      NN(4)=4
      PI=3.14159
      DO 2 M=1,MAXM
      IF(M.EQ.1) VEL=-444.08/PI
      IF(M.EQ.2) VEL=-444.08/2
      IF(M.EQ.3) VEL=-444.08*2./(3.*PI)
      IF(M.EQ.4) VEL=-444.08*2./(15.*PI)
      IF(M.EQ.4) VEL= 444.08*2./(15.*PI)
      DO 2 K=2,KL
      I=K+1+(M-1)*KMAX2
    2 ZCCT(3,I)=VEL*ELAST*TEEO/(CHAR*SIGO)*10
      RETURN                                                            SAT01260
      END                                                               SAT01270
      SUBROUTINE TLOAD(K,Z)                                             SAT00940
C***********************************************************************SAT00950
C     THIS SUBROUTINE DESCRIBES THE THERMAL LOADING ON THE SHELL       *SAT00960
C***********************************************************************SAT00970
      REAL NU                                                           SAT00980
      DIMENSION Z(4,1)                                                  SAT00990
      COMMON /IBL1/ MNMAX                                               SAT01000
      COMMON /IBL2/ NN(99),MNINIT                                       SAT01010
      COMMON /BL15/ NU,U1(99),V1(99),W1(99),V2(99),U2(99),W2(99),U3(99),SAT01020
     1              V3(99),W3(99)                                       SAT01030
      COMMON /BL32/ TKN,ELAST,CHAR,SIGO                                 SAT01040
      COMMON /IBL8/ LSTEP,ITR                                           SAT01050
      COMMON /BL5/  TT(99),EMT(99),DT(99),DMT(99)                       SAT01060
      COMMON /BL6/  SOE,OSE,ALOAD                                       SAT01070
      RETURN                                                            SAT01080
      END                                                               SAT01090
                                                                        SAT01100
      SUBROUTINE IMPERF (PHIXB,PHITB)                                   SAT01280
      DIMENSION PHIXB(1),PHITB(1)                                       SAT01290
      COMMON /IBL4/ KMAX,KL
      COMMON /IBL9/ MAXM
      KANDM=KMAX*MAXM
      DO 1 I=1,KANDM
      PHIXB(I)=0.
      PHITB(I)=0.
    1 CONTINUE
      RETURN                                                            SAT01300
      END                                                               SAT01310
      SUBROUTINE SATANS (P,CEE,DST,X,Z,ZD,Z2,Z3,ZCCT,IS,JS,ID,JD,PHIXB, SAT01320
```

```
     1PHITB)                                                            SATO1330
C***********************************************************************SATO1340
C     THIS SUBROUTINE READS ALL DATA, PRINTS THE OUTPUT TITLE PAGE,    *SATO1350
C     AND PASSES CONTROL TO ONE OF THE MAJOR CONTROLLING SUBROUTINES   *SATO1360
C***********************************************************************SATO1370
      IMPLICIT LOGICAL*1 ($)                                            SATO1380
      REAL*4 NU,LAM,LAM2,JAY,MT,LSD18,LSD1N,MASS                        SATO1390
      DIMENSION P(4,4,1),DEE(4,4,1),DST(4,4,1),X(4,1),Z(4,1),           SATO1400
     1ZC(4,1),Z2(4,1),Z3(4,1),ZDOT(4,1),IS(99,1),JS(99,1),IC(99,1),     SATO1410
     2JC(99,1),PHIXB(1),PHITB(1)                                        SATO1420
      COMMON /IBL1/ MNMAX                                               SATO1430
      COMMON /IBL4/ KMAX,KL                                             SATO1440
      COMMON /IBL5/ IBCINL,IBCFNL                                       SATO1450
      COMMON /IBL9/ MAXM                                                SATO1460
      COMMON /IBL10/ IFREQ,NTHMAX                                       SATO1470
      COMMON /IBL13/ ITRMAX,LSMAX                                       SATO1480
     1/IBLJ/ JUMP                                                       SATO1490
      COMMON /BL13/ OMEG1(4,4),CAPL1(4,4),OMEGL(4,4),CAPLL(4,4),        SATO1500
     1              UNIT(4,4)                                           SATO1510
      COMMON /BL15/ NU,U1(99),V1(99),W1(99),V2(99),U2(99),W2(99),U3(99),SATO1520
     1              V3(99),W3(99)                                       SATO1530
      COMMON /BL16/ EPS                                                 SATO1540
      COMMON /BL18/ EL1(4),ELL(4)                                       SATO1550
      COMMON /BL19/ TH(36)                                              SATO1560
      COMMON /BL32/ TKN,ELAST,CHAR,SIGO                                 SATO1570
      COMMON /BL100/ TEEO,$DYNMC                                        SATO1580
      COMMON /BL102/ DELOAD                                             SATO1590
      COMMON /BLPLOT/ IRADII,IGAMMA,IOMEGS,IOMEGT,ICEOMS,IBSTIF,IDSTIF, SATO1600
     1                IBBSTF,IDDSTF,IPR,IPS,IPT,ITT,IMT,IDTT,IDMT,INS,  SATO1610
     2                INTH,INSTH,IQS,IMS,IMTH,IMSTH,IU,IV,IW,IPHIS,     SATO1620
     3                IPHIT,IPHI,$PLOTS,$MODAL                          SATO1630
      COMMON /BLDATA/ TITLE,NO,IMODE,NDIMEN,IPRINT,LCHMAX,IC            SATO1640
      COMMON /BLRUN/ IRNAGN                                             SATO1650
      DIMENSION TITLE (18)                                              SATO1660
C***********************************************************************SATO1670
C     READ IN DATA FOR THIS RUN                                        *SATO1680
C***********************************************************************SATO1690
      READ (5,100) TITLE                                                SATO1700
      READ (5,101) NO,$DYNMC,IMODE,NDIMEN,NTHMAX,IFREQ,IPRINT,IBCINL,   SATO1710
     1             IBCFNL,KMAX,MNMAX,MAXM,LSMAX,LCHMAX,ITRMAX,IC        SATO1720
      READ (5,102) NU,SIGO,ELAST,TKN,CHAR,TEEO                          SATO1730
      READ (5,103) DELOAD,EPS                                           SATO1740
      READ(5,101) JUMP                                                  SATO1750
      IF (NTHMAX.EQ.0) GO TO 1                                          SATO1760
      READ (5,104) (TH(NTH),NTH=1,NTHMAX)                               SATO1770
      DO 2 NTH=1,NTHMAX                                                 SATO1780
    2 TH(NTH)=TH(NTH)*6.2831853/360.0                                   SATO1790
    1 IF (IBCINL.EQ.0) READ (5,105) OMEG1,CAPL1,EL1                     SATO1800
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      IF (IBCFNL.EQ.0) READ (5,105) OMEGL,CAPLL,ELL                     SAT01810
      READ (5,106) $PLOTS,$MODAL,IRADII,IGAMMA,IOMEGS,ICMEGT,ICECMS,    SAT01820
     1             IBSTIF,IDSTIF,IBBSTF,IDDSTF,IPR,IPS,IPT,ITT,IMT,IDTT,SAT01830
     2             IDMT,INS,INTH,INSTH,IQS,IMS,IMTH,IMSTH,IU,IV,IW,     SAT01840
     3             IPHIS,IPHIT,IPHI                                     SAT01850
      READ (5,107) IRNAGN                                               SAT01860
C***********************************************************************SAT01870
C     THIS CONCLUDES DATA READ-IN FOR THIS RUN.                        *SAT01880
C     PRINT OUT PERTINENT DATA.                                        *SAT01890
C***********************************************************************SAT01900
      WRITE (6,200) NO                                                  SAT01910
      WRITE (6,201) TITLE                                               SAT01920
      WRITE (6,202)                                                     SAT01930
      IF (IBCINL.LT.0) WRITE (6,203)                                    SAT01940
      IF (IBCINL.LT.0) GO TO 3                                          SAT01950
      WRITE (6,204)                                                     SAT01960
      WRITE (6,205) (OMEGI(1,J),J=1,4),(CAPLI(1,J),J=1,4),ELI(1)        SAT01970
      WRITE (6,206) (OMEGI(2,J),J=1,4),(CAPLI(2,J),J=1,4),ELI(2)        SAT01980
      WRITE (6,207) (OMEGI(3,J),J=1,4),(CAPLI(3,J),J=1,4),ELI(3)        SAT01990
      WRITE (6,208) (OMEGI(4,J),J=1,4),(CAPLI(4,J),J=1,4),ELI(4)        SAT02000
    3 IF (IBCFNL.LT.0) WRITE (6,209)                                    SAT02010
      IF (IBCFNL.LT.0) GO TO 4                                          SAT02020
      WRITE (6,210)                                                     SAT02030
      WRITE (6,205) (OMEGL(1,J),J=1,4),(CAPLL(1,J),J=1,4),ELL(1)        SAT02040
      WRITE (6,206) (OMEGL(2,J),J=1,4),(CAPLL(2,J),J=1,4),ELL(2)        SAT02050
      WRITE (6,207) (OMEGL(3,J),J=1,4),(CAPLL(3,J),J=1,4),ELL(3)        SAT02060
      WRITE (6,208) (OMEGL(4,J),J=1,4),(CAPLL(4,J),J=1,4),ELL(4)        SAT02070
    4 WRITE (6,211)                                                     SAT02080
      IF ($DYNMC) GO TO 5                                               SAT02090
      WRITE (6,212) KMAX,MAXM,DELOAD,LSMAX,ITRMAX,LCHMAX,EPS            SAT02100
      WRITE (6,213) CHAR,TKN,ELAST,SIGC,NU                              SAT02110
      IF (.NOT.$PLOTS) GO TO 6                                          SAT02120
      ICHCK1=IABS(IRADII)+IABS(IGAMMA)+IABS(IOMEGS)+IABS(ICMEGT)        SAT02130
     1      +IABS(IDEOMS)+IABS(IBSTIF)+IABS(IDSTIF)+IABS(IBBSTF)        SAT02140
     2      +IABS(IDDSTF)+IABS(IPR)+IABS(IPS)+IABS(IPT)+IABS(ITT)       SAT02150
     3      +IABS(IMT)+IABS(IDTT)+IABS(IDMT)                            SAT02160
      IF (ICHCK1.GT.0) WRITE (6,214)                                    SAT02170
      IF (ICHCK1.EQ.0) GO TO 8                                          SAT02180
      IF (IRADII.NE.0) WRITE (6,215)                                    SAT02190
      IF (IGAMMA.NE.0) WRITE (6,216)                                    SAT02200
      IF (IOMEGS.NE.0) WRITE (6,217)                                    SAT02210
      IF (ICMEGT.NE.0) WRITE (6,218)                                    SAT02220
      IF (ICECMS.NE.0) WRITE (6,219)                                    SAT02230
      IF (IBSTIF.NE.0) WRITE (6,220)                                    SAT02240
      IF (IDSTIF.NE.0) WRITE (6,221)                                    SAT02250
      IF (IBBSTF.NE.0) WRITE (6,222)                                    SAT02260
      IF (IDDSTF.NE.0) WRITE (6,223)                                    SAT02270
      IF (IPR   .NE.0) WRITE (6,224)                                    SAT02280
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      IF (IPS   .NE.0) WRITE (6,225)                                    SAT02290
      IF (IPT   .NE.0) WRITE (6,226)                                    SAT02300
      IF (ITT   .NE.0) WRITE (6,227)                                    SAT02310
      IF (IMT   .NE.0) WRITE (6,228)                                    SAT02320
      IF (ICTT  .NE.0) WRITE (6,229)                                    SAT02330
      IF (IDMT  .NE.0) WRITE (6,230)                                    SAT02340
    8 ICHCK1=IABS(INS)+IABS(INTH)+IABS(INSTH)+IABS(IQS)+IABS(IMS)       SAT02350
     1      +IABS(IMTH)+IABS(IMSTH)+IABS(IU)+IABS(IV)+IABS(IW)          SAT02360
     2      +IABS(IPHIS)+IABS(IPHIT)+IABS(IPHI)                         SAT02370
      IF((ICHCK1.GT.0).AND.$MCDAL) WRITE (6,231)                        SAT02380
      IF((ICHCK1.GT.0).AND..NOT.$MCDAL) WRITE (6,232)                   SAT02390
      IF (ICHCK1.EQ.0) GO TO 9                                          SAT02400
      IF (INS   .NE.0) WRITE (6,233)                                    SAT02410
      IF (INTH  .NE.0) WRITE (6,234)                                    SAT02420
      IF (INSTH.NE.0) WRITE (6,235)                                     SAT02430
      IF (IQS   .NE.0) WRITE (6,236)                                    SAT02440
      IF (IMS   .NE.0) WRITE (6,237)                                    SAT02450
      IF (IMTH  .NE.0) WRITE (6,238)                                    SAT02460
      IF (IMSTH.NE.0) WRITE (6,239)                                     SAT02470
      IF (IU    .NE.0) WRITE (6,240)                                    SAT02480
      IF (IV    .NE.0) WRITE (6,241)                                    SAT02490
      IF (IW    .NE.0) WRITE (6,242)                                    SAT02500
      IF (IPHIS.NE.0) WRITE (6,243)                                     SAT02510
      IF (IPHIT.NE.0) WRITE (6,244)                                     SAT02520
      IF (IPHI .NE.0) WRITE (6,245)                                     SAT02530
    9 GO TO 6                                                           SAT02540
    5 WRITE (6,246) KMAX,MAXM,DELOAD,LSMAX,ITRMAX,EPS                   SAT02550
      WRITE (6,247) CHAR,TKN,ELAST,SIGC,TEEO,NL                         SAT02560
    6 IF (NTHMAX.EQ.0) GO TO 7                                          SAT02570
      WRITE (6,248)                                                     SAT02580
      WRITE (6,249) (TH(NTH),NTH=1,NTHMAX)                              SAT02590
    7 IF (NDIMEN.EQ.1) WRITE (6,250)                                    SAT02600
      IF (NDIMEN.EQ.0) WRITE (6,251)                                    SAT02610
C***********************************************************************SAT02620
C     CALL APPROPRIATE CONTROLLING SUBPROGRAM                          *SAT02630
C***********************************************************************SAT02640
      IF ($DYNMC) CALL DYNAMC (P,CEE,DST,X,Z,ZC,Z2,Z3,ZDCT,IS,JS,ID,JD, SAT02650
     1PHIXB,PHITB)                                                      SAT02660
      IF (.NOT.$DYNMC) CALL STATIC (P,CEE,DST,X,Z,ZC,Z2,Z3,ZDCT,IS,JS,  SAT02670
     1ID,JD,PHIXB,PHITB)                                                SAT02680
C***********************************************************************SAT02690
C     READ STATEMENT FORMATS FOLLOW                                    *SAT02700
C***********************************************************************SAT02710
  100 FORMAT (18A4)                                                     SAT02720
  101 FORMAT (I5,L5,14I5)                                               SAT02730
  102 FORMAT (6E12.4)                                                   SAT02740
  103 FORMAT (2E12.4)                                                   SAT02750
  104 FORMAT (6E12.4)
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 1C5 FCRMAT (4E16.8)                                                    SAT02770
 1C6 FCRMAT (2L2,29I2)                                                  SAT02780
 1C7 FCRMAT (I2)                                                        SAT02790
C***********************************************************************SAT02800
C     WRITE STATEMENT FCRMATS FOLLOW                                   *SAT02810
C***********************************************************************SAT02820
 2C0 FCRMAT ('1',48X,'--PRCBLEM NUMBER',I5,'--',///)                    SAT02830
 2C1 FCRMAT (' ',38X,18A4,///)                                          SAT02840
 2C2 FCRMAT (' ',49X,'--INPUT DATA RECCRD--',//'      THE BCUNDARY CCNDISAT02850
     1TICNS ARE: ',//)                                                  SAT0286C
 2C3 FCRMAT (' ',T10,'THE SHELL HAS AN INITIAL PCLE',/)                 SAT02870
 2C4 FCRMAT (' ',T10,'AT THE INITIAL EDGE',//2X,'----------------CMEGA BSAT02880
     1AR---------------',15X,'---------------LAMDA BAR---------------',1SAT02890
     22X,'---EL-----',/)                                                SAT02900
 2C5 FCRMAT (' ','(',4E10.3,')  NS          (',4E10.3,')  U        ',E10SAT02910
     1.3)                                                               SAT02920
 2C6 FCRMAT (' ','(',4E10.3,')  NST    +    (',4E10.3,')  V    =   ',E10SAT02930
     1.3)                                                               SAT02940
 2C7 FCRMAT (' ','(',4E10.3,')  CS          (',4E10.3,')  W        ',E10SAT02950
     1.3)                                                               SAT02960
 2C8 FCRMAT (' ','(',4E10.3,')  PHIS        (',4E10.3,')  MS       ',E10SAT02970
     1.3)                                                               SAT02980
 209 FCRMAT (' ',T10,'THE SHELL HAS A FINAL PCLE',/)                    SAT02990
 21C FCRMAT (' ',T10,'AT THE FINAL ECGE',//2X,'----------------OMEGA BARSAT03000
     1----------------',15X,'----------------LAMCA BAR---------------',12SAT03010
     2X,'---EL-----',/)                                                 SAT03020
 211 FCRMAT (////)                                                      SAT03030
 212 FCRMAT (' ',4X,'NUMBER OF STATIONS-----------------------',I3/5X,'NSAT03040
     1UMBER OF MODES-------------------------',I3/5X,'INCREMENTAL LOAD FSAT03050
     2ACTCR-----------------',F6.3/5X,'MAXIMUM NUMBER CF LCAC STEPS-----SAT03060
     3-------',I3/5X,'MAXIMUM NUMBER OF ITERATICNS------------',I3/5X,'MSAT03070
     4AXIMUM NUMBER OF LOAD FACTOR CHANGES---',I3/5X,'CCNVERGENCE CRITERSAT03C80
     5ICN-------------------',F6.4//)                                   SAT03090
 213 FCRMAT (' ',4X,'CHARACTERISTIC SHELL DIMENSION-----------',E12.4/5XSAT03100
     1,'REFERENCE THICKNESS---------------------',E12.4/5X,'REFERENCE ELSAT03110
     2ASTICITY--------------------',E12.4/5X,'REFERENCE STRESS----------SAT03120
     3--------------',E12.4/5X,'PCISSCNS RATIO--------------------------SAT03130
     4',E12.4//)                                                        SAT03140
 214 FCRMAT (' ',T10,'PLCTS HAVE BEEN REQUESTED FOR THE BELCW LISTED GESAT03150
     1CMETRY, STIFFNESS OR LOADING QUANTITIES:'/)                       SAT03160
 215 FCRMAT ('+',T70,'RADIUS'/)                                         SAT03170
 216 FCRMAT ('+',T70,'GAMMA'/)                                          SAT03180
 217 FCRMAT ('+',T70,'CMEGA-S'/)                                        SAT03190
 218 FCRMAT ('+',T70,'GMEGA-THETA'/)                                    SAT03200
 219 FCRMAT ('+',T70,'DECMEGA-S'/)                                      SAT03210
 22C FCRMAT ('+',T70,'B-STIFFNESS'/)                                    SAT03220
 221 FCRMAT ('+',T70,'C-STIFFNESS'/)                                    SAT03230
 222 FCRMAT ('+',T70,'B-PRIME'/)                                        SAT03240
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223 FORMAT ('+',T70,'D-PRIME'/)                                         SAT03250
224 FORMAT ('+',T70,'PRESSURE LOADING - NORMAL'/)                        SAT03260
225 FORMAT ('+',T70,'PRESSURE LOADING - MERIDIONAL'/)                    SAT03270
226 FORMAT ('+',T70,'PRESSURE LOADING - CIRCUMFERENTIAL'/)               SAT03280
227 FORMAT ('+',T70,'THERMAL LOADING'/)                                  SAT03290
228 FORMAT ('+',T70,'THERMAL MOMENT'/)                                   SAT03300
229 FORMAT ('+',T70,'D-THERMAL LOADING'/)                                SAT03310
230 FORMAT ('+',T70,'D-THERMAL MOMENT'/)                                 SAT03320
231 FORMAT ('0',T20,'PLOTS HAVE BEEN REQUESTED FOR THE BELOW LISTED MOSAT03330
   1DAL QUANTITIES:'/)                                                  SAT03340
232 FORMAT ('0',T20,'PLOTS HAVE BEEN REQUESTED FOR THE BELOW LISTED SUSAT03350
   1MMED QUANTITIES:'/)                                                 SAT03360
233 FORMAT ('+',T70,'N-S'/)                                             SAT03370
234 FORMAT ('+',T70,'N-THETA'/)                                         SAT03380
235 FORMAT ('+',T70,'N-S-THETA'/)                                       SAT03390
236 FORMAT ('+',T70,'Q-S'/)                                             SAT03400
237 FORMAT ('+',T70,'M-S'/)                                             SAT03410
238 FORMAT ('+',T70,'M-THETA'/)                                         SAT03420
239 FORMAT ('+',T70,'M-S-THETA'/)                                       SAT03430
240 FORMAT ('+',T70,'U'/)                                               SAT03440
242 FORMAT ('+',T70,'W'/)                                               SAT03450
241 FORMAT ('+',T70,'V'/)                                               SAT03460
243 FORMAT ('+',T70,'PHI-S'/)                                           SAT03470
244 FORMAT ('+',T70,'PHI-THETA'/)                                       SAT03480
245 FORMAT ('+',T70,'PHI'/)                                             SAT03490
246 FORMAT (' ',4X,'NUMBER OF STATIONS----------------------',I3/5X,'NSAT03500
   1UMBER OF MODES------------------------',I3/5X,'INCREMENTAL TIME--SAT03510
   2--------------------',E9.4/5X,'MAXIMUM NUMBER OF TIME STEPS-----SAT03520
   3-------',I5/5X,'MAXIMUM NUMBER OF ITERATIONS------------',I3/5X,'CSAT03530
   4ONVERGENCE CRITERION-------------------',F6.4//)                  SAT03540
247 FORMAT (' ',4X,'CHARACTERISTIC SHELL DIMENSION----------',E12.4/5XSAT03550
   1,'REFERENCE THICKNESS---------------------',E12.4/5X,'REFERENCE ELSAT03560
   2ASTICITY-------------------',E12.4/5X,'REFERENCE STRESS----------SAT03570
   3--------------',E12.4/5X,'REFERENCE TIME-------------------------SAT03580
   4',E12.4/5X,'POISSONS RATIO--------------------',E12.4//)           SAT03590
248 FORMAT (' ',T20,'CIRCUMFERENTIAL COORDINATES FOR THE PRINT RECORD,SAT03600
   1 IN RADIAN MEASURE, ARE:'/)                                         SAT03610
249 FORMAT (' ',T10,6F16.10)                                            SAT03620
250 FORMAT (///' ',T20,'THE DATA PRINTED IS NON-DIMENSIONAL')           SAT03630
251 FORMAT (///' ',T20,'THE DATA PRINTED IS DIMENSIONAL')               SAT03640
    RETURN                                                              SAT03650
    END                                                                 SAT03660
    SUBROUTINE STATIC (P,DEE,DST,X,Z,ZC,Z2,Z3,ZDCT,IS,JS,ID,JD,PHIXB,   SAT03670
   1PHITB)                                                              SAT03680
C***********************************************************************SAT03690
C     THIS SUBROUTINE IS THE MAJOR CONTROLLING ROUTINE FOR ALL STATIC   *SAT03700
C     ANALYSIS PROBLEMS.  IT CONDUCTS INITIALIZATION, PREPARES INPUT    *SAT03710
C     MATERIAL FOR PLOTTING IF REQ'D, DETERMINES SHELL GEOMETRY, STIFF-*SAT03720
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C     NESSES,LOADING (PHYSICAL AND/OR THERMAL), AND INITIAL CONTIDIONS.*SAT03730
C     IT CONTROLS PROBLEM SOLUTION PROCEDURE.                          *SAT03740
C***********************************************************************SAT03750
      IMPLICIT LOGICAL*1 ($)                                            SAT03760
      REAL*4 NU,LAM,LAM2,JAY,MT,LSD18,LSD1N,MASS                        SAT03770
      DIMENSION P(4,4,1),DEE(4,4,1),DST(4,4,1),X(4,1),Z(4,1),           SAT03780
     1ZC(4,1),Z2(4,1),Z3(4,1),ZDOT(4,1),IS(99,1),JS(99,1),IC(99,1),     SAT03790
     2JC(99,1),PHIXB(1),PHITB(1)                                        SAT03800
      COMMON /IBL1/ MNMAX                                               SAT03810
      COMMON /IBL2/ N(99),MNINIT                                        SAT03820
C                   'N' APPEARS AS 'NN' IN SUBROUTINES FLOAD & EFG      SAT03830
      COMMON /IBL3/ M0,M1,M2,M3                                         SAT03840
      COMMON /IBL4/ KMAX,KL                                             SAT03850
      COMMON /IBL5/ IBCINL,IBCFNL                                       SAT03860
      COMMON /IBL6/ KLL                                                 SAT03870
      COMMON /IBL7/ MNMAXC,MAXD(99),MAXS(99),MAXSY(99),IJS(99)          SAT03880
      COMMON /IBL8/ LSTEP,ITR                                           SAT03890
      COMMON /IBL9/ MAXM                                                SAT03900
      COMMON /IBL10/ IFREQ,NTHMAX                                       SAT03910
      COMMON /IBL11/ ICORFL,IPASS                                       SAT03920
      COMMON /IBL12/ KMAX1,KMAX2,NCONV                                  SAT03930
      COMMON /IBL13/ ITRMAX,LSMAX                                       SAT03940
      COMMON /BL1/  A(4,4),BEE(4,4),C(4,4)                              SAT03950
      COMMON /BL3/  PR(99),PX(99),PT(99)                                SAT03960
      COMMON /BL4/  ZF1M(4,4,99),ZF2M(4,4,99),
     1              ZF3M(4,4,99),ZF4M(4,4,99)
      COMMON /BL5/  TT(99),MT(99),DT(99),DMT(99)                        SAT03990
C                   'MT' APPEARS AS 'EMT' IN SUBROUTINES INLPOL & FNLPOLSAT04000
      COMMON /BL6/  SOE,CSE,ALOAD                                       SAT04010
      COMMON /BL7/  D1,S1                                               SAT04020
      COMMON /BL8/  R(500),GAM(500),OMT(500)                            SAT04030
      COMMON /BL9/  FFS(4,99),EL1S(4),GEES(4,99)
      COMMON /BL10/ PHIX(99),PHIT(99),PHI(99)                           SAT04050
      COMMON /BL11/ OMXI(500),PHEE,T0,T2                                SAT04060
      COMMON /BL12/ TDLI,TDEL                                           SAT04070
      COMMON /BL13/ OMEG1(4,4),CAPL1(4,4),OMEGL(4,4),CAPLL(4,4),        SAT04080
     1              UNIT(4,4)                                           SAT04090
      COMMON /BL14/ LAM2,LSD18,LSD1N                                    SAT04100
      COMMON /BL15/ NU,U1(99),V1(99),W1(99),V2(99),U2(99),W2(99),U3(99),SAT04110
     1              V3(99),W3(99)                                       SAT04120
      COMMON /BL16/ EPS                                                 SAT04130
      COMMON /BL17/ DEL                                                 SAT04140
      COMMON /BL18/ EL1(4),ELL(4)                                       SAT04150
      COMMON /BL19/ TH(36)                                              SAT04160
      COMMON /BL20/ DEOMX(500)                                          SAT04170
      COMMON /BL23/ JAY(4,4),H(4,4)                                     SAT04180
      COMMON /BL24/ DL(4,4,99),DG(4,4,99),DF(4,4,99)
      COMMON /BL25/ E(4,4),F(4,4),G(4,4)                                SAT04200
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      COMMON /BL27/ BX3(99),BT3(99),BXT3(99),BE3(99)                    SAT04210
      COMMON /BL28/ EXX3(99),ETT3(99),ETX3(99),EXT3(99),EX3(99),ET3(99) SAT04220
      COMMON /BL29/ BX1(99),BT1(99),BXT1(99),BE1(99),BX2(99),BT2(99),   SAT04230
     1              BXT2(99),BE2(99)                                    SAT04240
      COMMON /BL30/ EXX1(99),ETT1(99),ETX1(99),EX1(99),ET1(99),EXX2(99),SAT04250
     1              ETT2(99),ETX2(99),EXT2(99),EX2(99),ET2(99)          SAT04260
      COMMON /BL31/ DELSQ,EXT1(99)                                      SAT04270
      COMMON /BL32/ TKN,ELAST,CHAR,SIGO                                 SAT04280
      COMMON /BL100/ TEEO,$DYNMC                                        SAT04290
      COMMON /BL101/ DELSD                                              SAT04300
      COMMON /BL102/ DELCAD                                             SAT04310
      COMMON /BL103/ MASS(500)                                          SAT04320
      COMMON /BL110/ TX(99),TTH(99),TXT(99),MX(99),MTH(99),MXT(99),     SAT04330
     1              QS(99)                                              SAT04340
      COMMON /BL111/ ABZ,ABZO,ABZN,ABZ3,CD2                             SAT04350
      COMMON /BLPHS/ PHX(99),PHT(99)
      COMMON /BLPLOT/  IRADII,IGAMMA,IOMEGS,IOMEGT,IDECMS,IBSTIF,IDSTIF, SAT04360
     1                 IBBSTF,IDDSTF,IPR,IPS,IPT,ITT,IMT,IDTT,IDMT,INS,  SAT04370
     2                 INTH,INSTH,IQS,IMS,IMTH,IMSTH,IU,IV,IW,IPHIS,     SAT04380
     3                 IPHIT,IPHI,$PLOTS,$MODAL                          SAT04390
      COMMON /BLPLT1/  XRADII(200),YGAMMA(200),YOMEGS(200),YOMEGT(200),  SAT04400
     1                 YDECMS(200),YBSTIF(200),YDSTIF(200),YBBSTF(200),  SAT04410
     2                 YDDSTF(200),YPR(200),YPS(200),YPT(200),YTT(200),  SAT04420
     3                 YMT(200),YDTT(200),YDMT(200),YNS(200),YNTH(200),  SAT04430
     4                 YNSTH(200),YQS(200),YMS(200),YMTH(200),YMSTH(200),SAT04440
     5                 YU(200),YV(200),YW(200),YPHIS(200),YPHIT(200),    SAT04450
     6                 YPHI(200),XSTATN(200)                             SAT04460
      COMMON /BLDATA/  TITLE,NO,IMODE,NDIMEN,IPRINT,LCHMAX,IC            SAT04470
      DIMENSION SIGT(2),SIGC(2),TITLE(18)                                SAT04480
C*******************************************************************SAT04490
      WRITE (6,8888)                                                     SAT04500
      DELSD=DELCAD*DELOAD                                                SAT04510
      KL=KMAX-1                                                          SAT04520
      KLL=KMAX-2                                                         SAT04530
      KMAX1=KMAX+1                                                       SAT04540
      KMAX2=KMAX+2                                                       SAT04550
      AK=KL                                                              SAT04560
      SIGT(1)=SIGO*TKN                                                   SAT04570
      SIGT(2)=SIGO/ELAST                                                 SAT04580
      SIGC(1)=SIGO*CHAR/ELAST                                            SAT04590
      SIGC(2)=SIGO*TKN**3/CHAR                                           SAT04600
      IF (IBCINL.LT.0) GO TO 14                                          SAT04610
      DO 98 I=1,4                                                        SAT04620
      DO 98 J=1,4                                                        SAT04630
      KKLM=J/4+1                                                         SAT04640
      OMEG1(I,J)=OMEG1(I,J)*SIGT(KKLM)                                   SAT04650
   98 CAPL1(I,J)=CAPL1(I,J)*SIGC(KKLM)                                   SAT04660
   14 IF(IBCFNL.LT.0) GO TO 17                                           SAT04670
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      DO 99 I=1,4                                                       SAT04680
      DO 99 J=1,4                                                       SAT04690
      KKLM=J/4+1                                                        SAT04700
      OMEGL(I,J)=OMEGL(I,J)*SIGT(KKLM)                                  SAT04710
   99 CAPLL(I,J)=CAPLL(I,J)*SIGC(KKLM)                                  SAT04720
   17 LAM=TKN/CHAR                                                      SAT04730
      SOE=SIGC/ELAST                                                    SAT04740
      OSE=.5*SOE                                                        SAT04750
      D1=1.0-NU                                                         SAT04760
      S1=1.0+NU                                                         SAT04770
      LAM2=LAM**2                                                       SAT04780
      IF(NDIMEN.LT.1) GO TO 228                                         SAT04790
      SIGC=1.0                                                          SAT04800
      ELAST=1.0                                                         SAT04810
      TKN=1.0                                                           SAT04820
      CHAR=1.0                                                          SAT04830
  228 DO 230 M=1,MAXM                                                   SAT04840
      PHX(M)=0.0
      PHT(M)=0.0
      N(M)=0.0                                                          SAT04850
      PX(M)=0.0                                                         SAT04860
      PT(M)=0.0                                                         SAT04870
      PR(M)=0.0                                                         SAT04880
      TT(M)=0.0                                                         SAT04890
      MT(M)=0.0                                                         SAT04900
      DT(M)=0.0                                                         SAT04910
      DMT(M)=0.0                                                        SAT04920
      MAXC(M)=0                                                         SAT04930
      MAXS(M)=0                                                         SAT04940
  230 MAXSY(M)=0                                                        SAT04950
      CALL GEOM                                                         SAT04960
      ICHCK1=IABS(IGAMMA)+IABS(IOMEGS)+IABS(IOMEGT)+IABS(IDEOMS)        SAT04970
     1       +IABS(IRADII)                                              SAT04980
      ICHCK2=IABS(IBSTIF)+IABS(IDSTIF)+IABS(IBBSTF)+IABS(IDDSTF)        SAT04990
      IF (.NOT.$PLOTS) GO TO 1001                                       SAT05000
      DO 2 K=1,KMAX                                                     SAT05010
    2 XSTATN(K)=FLOAT(K)                                                SAT05020
      IF (ICHCK1.EQ.0) GO TO 1001                                       SAT05030
      DO 1 K=1,KMAX                                                     SAT05040
      XRADII(K)=R(K)*CHAR                                               SAT05050
      YGAMMA(K)=GAM(K)/CHAR                                             SAT05060
      YOMEGS(K)=OMXI(K)/CHAR                                            SAT05070
      YOMEGT(K)=OMT(K)/CHAR                                             SAT05080
      YDEOMS(K)=DEOMX(K)/(CHAR*CHAR)                                    SAT05090
    1 CONTINUE                                                          SAT05100
 1001 CONTINUE                                                          SAT05110
      DO 86 K=1,KMAX                                                    SAT05120
   86 MASS(K)=0.                                                        SAT05130
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      WRITE(6,802)                                                      SAT05140
      DO 978 K=1,KMAX                                                   SAT05150
      RKK=R(K)*CHAR                                                     SAT05160
      CMXIK=CMXI(K)/CHAR                                                SAT05170
      GAMK=GAM(K)/CHAR                                                  SAT05180
      CMTK=CMT(K)/CHAR                                                  SAT05190
      CECMXK=CECMX(K)/(CHAR*CHAR)                                       SAT05200
  978 WRITE(6,803) K,RKK,GAMK,CMXIK,OMTK,DEOMXK                         SAT05210
  805 MC=0                                                              SAT05220
      M1=0                                                              SAT05230
      M2=0                                                              SAT05240
      M3=0                                                              SAT05250
      AEN=CHAR/SIGO/TKN                                                 SAT05260
      ZN=SIGO*TKN                                                       SAT05270
      WRITE(6,112)                                                      SAT05280
      DO 888 K=1,KMAX                                                   SAT05290
      CALL BCE(K,B,DB,D,DD)                                             SAT05300
      EST=ELAST*TKN                                                     SAT05310
      ZST=ELAST*TKN**3                                                  SAT05320
      B=B*BST                                                           SAT05330
      D=D*ZST                                                           SAT05340
      DB=DB/CHAR*BST                                                    SAT05350
      DD=DD/CHAR*ZST                                                    SAT05360
      WRITE (6,71) K,B,D,DB,DD                                          SAT05370
      IF (.NOT.$PLOTS.OR.(ICHCK2.EQ.0)) GO TO 888                       SAT05380
      YESTIF(K)=B                                                       SAT05390
      YDSTIF(K)=D                                                       SAT05400
      YBBSTF(K)=DB                                                      SAT05410
      YDDSTF(K)=DD                                                      SAT05420
  888 CONTINUE                                                          SAT05430
      CALL PLOAD(1,Z)                                                   SAT05440
      CALL TLOAD(1,Z)                                                   SAT05450
      DO 889 M=1,MNMAX                                                  SAT05460
      WRITE(6,113) N(M)                                                 SAT05470
      WRITE(6,114)                                                      SAT05480
      ICHCK3=IABS(IPR)+IABS(IPS)+IABS(IPT)+IABS(ITT)+IABS(IMT)          SAT05490
     1         +IABS(IDTT)+IABS(IDMT)                                   SAT05500
      DO 890 K=1,KMAX                                                   SAT05510
      CALL PLOAD(K,Z)                                                   SAT05520
      CALL TLOAD(K,Z)                                                   SAT05530
      PRM=PR(M)/ABN                                                     SAT05540
      PTM=PT(M)/ABN                                                     SAT05550
      PXM=PX(M)/ABN                                                     SAT05560
      TTM=TT(M)*ZN                                                      SAT05570
      EMTM=MT(M)/CHAR*ZN*TKN*TKN                                        SAT05580
      DTM=DT(M)/CHAR*ZN                                                 SAT05590
      DMTM=DMT(M)*ZN*TKN*TKN/(CHAR*CHAR)                                SAT05600
      WRITE (6,115) K,PRM,PXM,PTM,TTM,EMTM,DTM,DMTM                     SAT05610
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      IF (.NOT.$PLOTS.OR.(ICHCK3.EQ.0)) GO TO 890                       SAT05620
      YPR(K)=PRM                                                        SAT05630
      YPS(K)=PXM                                                        SAT05640
      YPT(K)=PTM                                                        SAT05650
      YTT(K)=TTM                                                        SAT05660
      YMT(K)=EMTM                                                       SAT05670
      YDTT(K)=DTM                                                       SAT05680
      YDMT(K)=DMTM                                                      SAT05690
  890 CONTINUE                                                          SAT05700
      IF (M.EQ.1) ICHCK3=ICHCK1+ICHCK2+ICHCK3                           SAT05710
      IF ($PLOTS.AND.(ICHCK3.GT.0)) CALL PLOT1(M)                       SAT05720
  899 CONTINUE                                                          SAT05730
      DELSQ=DEL**2                                                      SAT05740
      TCLI=.5/DEL                                                       SAT05750
      TDEL=2.0*DEL                                                      SAT05760
      MNINIT=1                                                          SAT05770
      MNMAXC=MNMAX                                                      SAT05780
      DO 20 I=1,4                                                       SAT05790
      DO 20 J=1,4                                                       SAT05800
      UNIT(I,J)=0.0                                                     SAT05810
   20 IF(I.EQ.J) UNIT(I,J)=1.0                                          SAT05820
      NMAX=MAXM*KMAX2                                                   SAT05830
      DO 22 K=1,NMAX                                                    SAT05840
      DO 22 I=1,4                                                       SAT05850
      ZDOT(I,K)=0.0                                                     SAT05860
      ZC(I,K)=0.0                                                       SAT05870
      Z2(I,K)=0.0                                                       SAT05880
      Z3(I,K)=0.0                                                       SAT05890
   22 Z(I,K)=0.0                                                        SAT05900
      ALOAD=DELOAD                                                      SAT05910
      CALL IMPERF (PHIXB,PHITB)                                         SAT05920
      CALL PMATRX (P,X,ZC,Z2,Z3,DEE,DST)                                SAT05930
      LSTEP=1                                                           SAT05940
      LCHANG=0                                                          SAT05950
      ITR=1                                                             SAT05960
      ICORFL=0                                                          SAT05970
      IF(MNMAX.EQ.MAXM) ICORFL=1                                        SAT05980
      IPASS=0                                                           SAT05990
  400 CALL XANDZ (P,DEE,DST,X,Z,ZC,Z2,Z3,ZDOT,IS,JS,ID,JD,PHIXB,PHITB)  SAT06000
      IF(ITRMAX.EQ.1) GO TO 50                                          SAT06010
      MNMAXC=MNMAX                                                      SAT06020
      IF(IPASS.LT.2) CALL MODES (IS,JS,ID,JD,P,X,ZC,Z2,Z3,DEE,DST)
      IF((NCONV.EQ.1).AND.(ITR.GT.1)) GO TO 50                          SAT06040
      IF(ITR.LT.ITRMAX) GO TO 23                                        SAT06050
      IF(LCHANG.LT.LCHMAX) GO TO 30                                     SAT06060
      WRITE(6,220) NO                                                   SAT06070
      GO TO 500                                                         SAT06080
   50 PL=LSTEP                                                          SAT06090
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      FI=IPRINT                                                         SAT06100
      LI=LSTEP/IPRINT                                                   SAT06110
      FLI=LI                                                            SAT06120
      FT=FLI-FL/FI                                                      SAT06130
      IF(FT.EQ.0.) CALL OUTPUT(IMODE,P,DEE,DST,X,Z,ZO,Z2,Z3,ZDOT,IS,JS, SAT06140
     1ID,JD,PHIXB,PHITB)                                                SAT06150
      IF(LSTEP.EQ.1) ITR=1                                              SAT06160
      IF(LSTEP.EQ.1) ITRPR=1                                            SAT06170
      IF(ITR.GT.ITRPR) ITRPR=ITR                                        SAT06180
      IF(LSTEP.GE.LSMAX) GO TO 360                                      SAT06190
   60 DO 61 MN=1,MNMAXO                                                 SAT06200
      DO 61 K=1,KMAX2                                                   SAT06210
      IK=K+(MN-1)*KMAX2                                                 SAT06220
      DO 61 I=1,4                                                       SAT06230
      ZN=2.0*Z(I,IK)-ZO(I,IK)                                           SAT06240
      ZO(I,IK)=Z(I,IK)                                                  SAT06250
   61 Z(I,IK)=ZN                                                        SAT06260
      IF(LSTEP.GE.LSMAX) GO TO 360                                      SAT06270
   62 ALOAD=ALOAD+DELOAD                                                SAT06280
      LSTEP=LSTEP+1                                                     SAT06290
      ITR=1                                                             SAT06300
      GO TO 400                                                         SAT06310
  360 WRITE(6,221) NO                                                   SAT06320
      GO TO 500                                                         SAT06330
   23 ITR=ITR+1                                                         SAT06340
      GO TO 400                                                         SAT06350
   30 IF(LSTEP-1) 310,310,320                                           SAT06360
  310 WRITE(6,223)                                                      SAT06370
      GO TO 500                                                         SAT06380
  320 WRITE(6,222)                                                      SAT06390
      LCHANG=LCHANG+1                                                   SAT06400
      LSTEP=LSTEP-1                                                     SAT06410
      ALOAD=ALOAD-DELOAD                                                SAT06420
      DELOAD=DELOAD/5.0                                                 SAT06430
      DO 32 MN=1,MNMAXO                                                 SAT06440
      DO 32 K=1,KMAX2                                                   SAT06450
      IK=K+(MN-1)*KMAX2                                                 SAT06460
      DO 32 I=1,4                                                       SAT06470
   32 Z(I,IK)=ZO(I,IK)                                                  SAT06480
      GO TO 62                                                          SAT06490
C***********************************************************************SAT06500
   71 FORMAT(20X,I3,4X,4E20.6)                                          SAT06510
  112 FORMAT(////17X,12H  STATION    20H       B STIFFNESS   20H      D STSAT06520
     1IFFNESS    20H       B PRIME        20H       D PRIME        //)  SAT06530
  113 FORMAT(///25X,44HPRESSURE AND TEMPERATURE COEFFICIENTS FOR N=I3,8HSAT06540
     1   FOLLOW//)                                                      SAT06550
  114 FORMAT(5X,7HSTATION,3X,15H        PR         15H       PX       15H SAT06560
     1  PT          15H       TT          15H      MT          15H      DTT     1SAT06570
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     25H      DMT     //)                                               SAT06580
  115 FORMAT(6X,I3,7X,7E15.4)                                           SAT06590
  220 FORMAT(1H1,80H          THE MAXIMUM NUMBER OF LOAD CHANGES HAVE BESAT06600
     1EN MADE.  END PROBLEM NUMBERI4)                                   SAT06610
  221 FORMAT(1H1,79H          THE MAXIMUM NUMBER OF LOAD STEPS HAVE BEENSAT06620
     1 TAKEN.  END PROBLEM NUMBERI4)                                    SAT06630
  222 FORMAT(1H1,119H         THE SOLUTION DID NOT CONVERGE WITHIN THE MSAT06640
     1AXIMUM NUMBER OF ITERATIONS.  THE LOAD FACTOR HAS BEEN DIVIDED BY SAT06650
     25.)                                                               SAT06660
  223 FORMAT(1H1,69H          THE SOLUTION DID NOT CONVERGE FOR THE FIRSSAT06670
     1T LOAD INCREMENT./11X,71HLOOK FOR AN ERROR IN THE INPUT DATA, OR TSAT06680
     2RY A SMALLER VALUE FOR DELOAD.)                                   SAT06690
  802 FORMAT(1H1,17X,15H STATION       16H     RADIUS     16H      GAMMA SAT06700
     1   16H       OMEGA S  16H     OMEGA THETA16H     DEOMEGA S  //)   SAT06710
  803 FORMAT(20X,I3, 9X,5E16.4)                                         SAT06720
 8888 FORMAT ('0',T20,'EXECUTING IN SUBROUTINE "STATIC"')               SAT06730
  500 RETURN                                                            SAT06740
      END                                                               SAT06750
      SUBROUTINE DYNAMC (P,CEE,DST,X,Z,ZD,Z2,Z3,ZDOT,IS,JS,ID,JD,PHIXB, SAT06760
     1PHITB)                                                            SAT06770
C***********************************************************************SAT06780
C     THIS SUBROUTINE IS ONE OF THE MAJOR CONTROLLING SUBROUTINES FOR  *SAT06790
C     ALL DYNAMIC ANALYSIS PROBLEMS.  IT OPERATES IN A FASHION SIMILAR *SAT06800
C     TO SUBROUTINE STATIC.                                            *SAT06810
C***********************************************************************SAT06820
      IMPLICIT LOGICAL*1 ($)                                            SAT06830
      REAL*4 NU,LAM,LAM2,JAY,MT,LSD18,LSDIN,MASS                        SAT06840
      DIMENSION P(4,4,1),CEE(4,4,1),DST(4,4,1),X(4,1),Z(4,1),           SAT06850
     1ZD(4,1),Z2(4,1),Z3(4,1),ZDOT(4,1),IS(99,1),JS(99,1),ID(99,1),     SAT06860
     2JD(99,1),PHIXB(1),PHITB(1)                                        SAT06870
      COMMON /IBL1/ MNMAX                                               SAT06880
      COMMON /IBL2/ N(99),MNINIT                                        SAT06890
C                   'N' APPEARS AS 'NN' IN SUBROUTINES PLOAD & EFG      SAT06900
      COMMON /IBL3/ M0,M1,M2,M3                                         SAT06910
      COMMON /IBL4/ KMAX,KL                                             SAT06920
      COMMON /IBL5/ IBCINL,IBCFNL                                       SAT06930
      COMMON /IBL6/ KLL                                                 SAT06940
      COMMON /IBL7/ MNMAXO,MAXD(99),MAXS(99),MAXSY(99),IJS(99)          SAT06950
      COMMON /IBL8/ LSTEP,ITR                                           SAT06960
      COMMON /IBL9/ MAXM                                                SAT06970
      COMMON /IBL10/ IFREQ,NTHMAX                                       SAT06980
      COMMON /IBL11/ ICORFL,IPASS                                       SAT06990
      COMMON /IBL12/ KMAX1,KMAX2,NCONV                                  SAT07000
      COMMON /IBL13/ ITRMAX,LSMAX                                       SAT07010
      COMMON /BL1/  A(4,4),BEE(4,4),C(4,4)                              SAT07020
      COMMON /BL3/  PR(99),PX(99),PT(99)                                SAT07030
      COMMON /BL4/  ZF1M(4,4,99),ZF2M(4,4,99),
     1              ZF3M(4,4,99),ZF4M(4,4,99)
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      COMMON /BL5/  TT(99),MT(99),DT(99),DMT(99)                       SAT07060
C                   'MT' APPEARS AS 'EMT' IN SUBROUTINES INLPOL & FNLPOLSAT07070
      COMMON /BL6/  SOE,CSE,ALOAD                                      SAT07080
      COMMON /BL7/  D1,S1                                              SAT07090
      COMMON /BL8/  R(500),GAM(500),OMT(500)                           SAT07100
      COMMON /BL9/  FFS(4,99),ELIS(4),GEES(4,99)
      COMMON /BL10/ PHIX(99),PHIT(99),PHI(99)                          SAT07120
      COMMON /BL11/ OMXI(500),PHEE,T0,T2                               SAT07130
      COMMON /BL12/ TDLI,TDEL                                          SAT07140
      COMMON /BL13/ OMEG1(4,4),CAPL1(4,4),OMEGL(4,4),CAPLL(4,4),       SAT07150
     1              UNIT(4,4)                                          SAT07160
      COMMON /BL14/ LAM2,LSD18,LSC1N                                   SAT07170
      COMMON /BL15/ NU,U1(99),V1(99),W1(99),V2(99),L2(99),W2(99),U3(99),SAT07180
     1              V3(99),W3(99)                                      SAT07190
      COMMON /BL16/ EPS                                                SAT07200
      COMMON /BL17/ DEL                                                SAT07210
      COMMON /BL18/ EL1(4),ELL(4)                                      SAT07220
      COMMON /BL19/ TH(36)                                             SAT07230
      COMMON /BL20/ DEOMX(500)                                         SAT07240
      COMMON /BL23/ JAY(4,4),H(4,4)                                    SAT07250
      COMMON /BL24/ DL(4,4,99),DG(4,4,99),DF(4,4,99)
      COMMON /BL25/ E(4,4),F(4,4),G(4,4)                               SAT07270
      COMMON /BL27/ BX3(99),BT3(99),BXT3(99),BE3(99)                   SAT07280
      COMMON /BL28/ EXX3(99),ETT3(99),ETX3(99),EXT3(99),EX3(99),ET3(99) SAT07290
      COMMON /BL29/ BX1(99),BT1(99),BXT1(99),BE1(99),BX2(99),BT2(99),  SAT07300
     1              BXT2(99),BE2(99)                                   SAT07310
      COMMON /BL30/ EXX1(99),ETT1(99),ETX1(99),EX1(99),ET1(99),EXX2(99),SAT07320
     1              ETT2(99),ETX2(99),EXT2(99),EX2(99),ET2(99)         SAT07330
      COMMON /BL31/ DELSQ,EXT1(99)                                     SAT07340
      COMMON /BL32/ TKN,ELAST,CHAR,SIGC                                SAT07350
      COMMON /BL100/ TEEC,$DYNMC                                       SAT07360
      COMMON /BL101/ DELSD                                             SAT07370
      COMMON /BL102/ DELOAD                                            SAT07380
      COMMON /BL103/ MASS(500)                                         SAT07390
      COMMON /BL110/ TX(99),TTH(99),TXT(99),MX(99),MTH(99),MXT(99),    SAT07400
     1              QS(99)                                             SAT07410
      COMMON /BL111/ ABZ,ABZ0,ABZN,ABZ3,CC2                            SAT07420
      COMMON /BLPHS/ PHX(99),PHT(99)
      COMMON /BLPLOT/ IRADII,IGAMMA,IOMEGS,IOMEGT,IDEOMS,IBSTIF,IDSTIF, SAT07430
     1                IBBSTF,IDDSTF,IPR,IPS,IPT,ITT,IMT,IDTT,IDMT,INS,  SAT07440
     2                INTH,INSTH,IQS,IMS,IMTH,IMSTH,IU,IV,IW,IPHIS,     SAT07450
     3                IPHIT,IPHI,$PLOTS,$MODAL                          SAT07460
      COMMON /BLPLT1/ XRADII(200),YGAMMA(200),YOMEGS(200),YOMEGT(200),  SAT07470
     1                YDEOMS(200),YBSTIF(200),YDSTIF(200),YBBSTF(200),  SAT07480
     2                YDDSTF(200),YPR(200),YPS(200),YPT(200),YTT(200),  SAT07490
     3                YMT(200),YDTT(200),YDMT(200),YNS(200),YNTH(200),  SAT07500
     4                YNSTH(200),YQS(200),YMS(200),YMTH(200),YMSTH(200),SAT07510
     5                YU(200),YV(200),YW(200),YPHIS(200),YPHIT(200),    SAT07520
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     6             YPHI(200),XSTATN(200)                                SAT07530
      COMMON /BLDATA/ TITLE,NC,IMODE,NDIMEN,IPRINT,LCHMAX,IC            SAT07540
      DIMENSION SIGT(2),SIGC(2),TITLE(18)                               SAT07550
      DIMENSION VBAR(99),AVB(99)                                        SAT07560
C***********************************************************************SAT07570
      WRITE (6,8888)                                                    SAT07580
      DELSD=DELOAD*DELCAD                                               SAT07590
      KL=KMAX-1                                                         SAT07600
      KLL=KMAX-2                                                        SAT07610
      KMAX1=KMAX+1                                                      SAT07620
      KMAX2=KMAX+2                                                      SAT07630
      AK=KL                                                             SAT07640
      SIGT(1)=SIGO*TKN                                                  SAT07650
      SIGT(2)=SIGO/ELAST                                                SAT07660
      SIGC(1)=SIGO*CHAR/ELAST                                           SAT07670
      SIGC(2)=SIGO*TKN**3/CHAR                                          SAT07680
      IF (IBCINL.LT.0) GO TO 14                                         SAT07690
      DO 98 I=1,4                                                       SAT07700
      DO 98 J=1,4                                                       SAT07710
      KKLM=J/4+1                                                        SAT07720
      OMEG1(I,J)=OMEG1(I,J)*SIGT(KKLM)                                  SAT07730
   98 CAPL1(I,J)=CAPL1(I,J)*SIGC(KKLM)                                  SAT07740
   14 IF(IBCFNL.LT.0) GO TO 17                                          SAT07750
      DO 99 I=1,4                                                       SAT07760
      DO 99 J=1,4                                                       SAT07770
      KKLM=J/4+1                                                        SAT07780
      OMEGL(I,J)=OMEGL(I,J)*SIGT(KKLM)                                  SAT07790
   99 CAPLL(I,J)=CAPLL(I,J)*SIGC(KKLM)                                  SAT07800
   17 LAM=TKN/CHAR                                                      SAT07810
      SCE=SIGO/ELAST                                                    SAT07820
      CSE=.5*SCE                                                        SAT07830
      D1=1.0-NU                                                         SAT07840
      S1=1.0+NU                                                         SAT07850
      LAM2=LAM**2                                                       SAT07860
      IF(NDIMEN.LT.1) GO TO 228                                         SAT07870
      SIGO=1.0                                                          SAT07880
      ELAST=1.0                                                         SAT07890
      TKN=1.0                                                           SAT07900
      CHAR=1.0                                                          SAT07910
  228 DO 230 M=1,MAXM                                                   SAT07920
      PHX(M)=0.0
      PHT(M)=0.0
      N(M)=0.0                                                          SAT07930
      PX(M)=0.0                                                         SAT07940
      PT(M)=0.0                                                         SAT07950
      PR(M)=0.0                                                         SAT07960
      TT(M)=0.0                                                         SAT07970
      MT(M)=0.0                                                         SAT07980
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      DT(M)=0.0                                                         SAT07990
      DMT(M)=0.0                                                        SAT08000
      MAXD(M)=0                                                         SAT08010
      MAXS(M)=0                                                         SAT08020
  230 MAXSY(M)=0                                                        SAT08030
      CALL GEOM                                                         SAT08040
      ICHCK1=IABS(IGAMMA)+IABS(IOMEGS)+IABS(IOMEGT)+IABS(IDEOMS)        SAT08050
     1        +IABS(IRADII)                                             SAT08060
      ICHCK2=IABS(IBSTIF)+IABS(IDSTIF)+IABS(IBBSTF)+IABS(IDDSTF)        SAT08070
      IF (.NOT.$PLOTS) GO TO 1001                                       SAT08080
      DO 2 K=1,KMAX                                                     SAT08090
    2 XSTATN(K)=FLOAT(K)                                                SAT08100
      IF (ICHCK1.EQ.0) GO TO 1001                                       SAT08110
      DO 1 K=1,KMAX                                                     SAT08120
      XRADII(K)=R(K)*CHAR                                               SAT08130
      YGAMMA(K)=GAM(K)/CHAR                                             SAT08140
      YOMEGS(K)=OMXI(K)/CHAR                                            SAT08150
      YOMEGT(K)=OMT(K)/CHAR                                             SAT08160
      YDEOMS(K)=DEOMX(K)/(CHAR*CHAR)                                    SAT08170
    1 CONTINUE                                                          SAT08180
 1001 CONTINUE                                                          SAT08190
  804 WRITE(6,810)                                                      SAT08200
      TEED=TEEO                                                         SAT08210
      IF(NDIMEN.EQ.1) TEED=1.0                                          SAT08220
      DO 979 K=1,KMAX                                                   SAT08230
      RKK=R(K)*CHAR                                                     SAT08240
      OMXIK=OMXI(K)/CHAR                                                SAT08250
      GAMK=GAM(K)/CHAR                                                  SAT08260
      OMTK=OMT(K)/CHAR                                                  SAT08270
      DEOMXK=DEOMX(K)/(CHAR*CHAR)                                       SAT08280
      AMSS=MASS(K)*TEED**2*ELAST*TKN/CHAR**2                            SAT08290
  979 WRITE(6,813) K,RKK,GAMK,OMXIK,OMTK,DEOMXK,AMSS                    SAT08300
  805 M0=0                                                              SAT08310
      M1=0                                                              SAT08320
      M2=0                                                              SAT08330
      M3=0                                                              SAT08340
      AEN=CHAR/SIGO/TKN                                                 SAT08350
      ZN=SIGO*TKN                                                       SAT08360
      WRITE(6,112)                                                      SAT08370
      DO 888 K=1,KMAX                                                   SAT08380
      CALL BDB(K,B,DB,D,DD)                                             SAT08390
      BST=ELAST*TKN                                                     SAT08400
      ZST=ELAST*TKN**3                                                  SAT08410
      B=B*BST                                                           SAT08420
      D=D*ZST                                                           SAT08430
      DB=DB/CHAR*BST                                                    SAT08440
      DD=DD/CHAR*ZST                                                    SAT08450
      WRITE (6,71) K,B,D,DB,DD                                          SAT08460
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      IF (.NOT.$PLOTS.OR.(ICHCK2.EQ.0)) GO TO 888                       SAT08470
      YESTIF(K)=B                                                       SAT08480
      YDSTIF(K)=D                                                       SAT08490
      YBBSTF(K)=DB                                                      SAT08500
      YDDSTF(K)=DD                                                      SAT08510
  888 CONTINUE                                                          SAT08520
      CALL FLOAD(1,Z)                                                   SAT08530
      CALL TLOAD(1,Z)                                                   SAT08540
      DELSQ=DEL**2                                                      SAT08550
      TDLI=.5/DEL                                                       SAT08560
      TDEL=2.0*DEL                                                      SAT08570
      MNINIT=1                                                          SAT08580
      MNMAXO=MNMAX                                                      SAT08590
      DO 20 I=1,4                                                       SAT08600
      DO 20 J=1,4                                                       SAT08610
      UNIT(I,J)=0.0                                                     SAT08620
   20 IF(I.EQ.J) UNIT(I,J)=1.0                                          SAT08630
      NMAX=MAXM*KMAX2                                                   SAT08640
      DO 22 K=1,NMAX                                                    SAT08650
      DO 22 I=1,4                                                       SAT08660
      ZDOT(I,K)=0.0                                                     SAT08670
      ZO(I,K)=0.0                                                       SAT08680
      Z2(I,K)=0.0                                                       SAT08690
      Z3(I,K)=0.0                                                       SAT08700
   22 Z(I,K)=0.0                                                        SAT08710
      IF(IC.EQ.0) GO TO 834                                             SAT08720
      CALL INITL (Z,ZO,Z2,Z3,ZDOT)                                      SAT08730
      ACO=CHAR*SIGO/ELAST                                               SAT08740
      ACM=SIGO*TKN**3/CHAR                                              SAT08750
      DO 830 M=1,MNMAX                                                  SAT08760
      MM=(M-1)*KMAX2                                                    SAT08770
      WRITE(6,126) N(M)                                                 SAT08780
      WRITE(6,127)                                                      SAT08790
      DO 831 K=2,KMAX1                                                  SAT08800
      MK=K+MM                                                           SAT08810
      TU=ACO*ZO(1,MK)                                                   SAT08820
      TV=ACO*ZO(2,MK)                                                   SAT08830
      TW=ACO*ZO(3,MK)                                                   SAT08840
      TM=ACM*ZO(4,MK)                                                   SAT08850
      KK=K-1                                                            SAT08860
  831 WRITE(6,71) KK,TU,TV,TW,TM                                        SAT08870
      WRITE(6,129)                                                      SAT08880
      DO 830 K=2,KMAX1                                                  SAT08890
      ACD=CHAR*SIGO/(ELAST*TEEO)                                        SAT08900
      AMD=SIGO*TKN**3/(CHAR*TEEO)                                       SAT08910
      MK=K+MM                                                           SAT08920
      TU=ACD*ZDOT(1,MK)                                                 SAT08930
      TV=ACD*ZDOT(2,MK)                                                 SAT08940
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      TW=ACD*ZDOT(3,MK)                                                 SAT08950
      TM=AMD*ZDOT(4,MK)                                                 SAT08960
      KK=K-1                                                            SAT08970
      WRITE(6,71) KK,TU,TV,TW,TM                                        SAT08980
      DO 830 I=1,4                                                      SAT08990
      Z(I,MK)=ZO(I,MK)+ZDOT(I,MK)*DELCAD                                SAT09000
      Z2(I,MK)=ZO(I,MK)-ZDOT(I,MK)*DELCAD                               SAT09010
  830 Z3(I,MK)=ZO(I,MK)-2.*ZDOT(I,MK)*DELOAD                            SAT09020
  834 CONTINUE                                                          SAT09030
      ALCAD=1.0                                                         SAT09040
      CALL IMPERF (PHIXB,PHITB)                                         SAT09050
      CALL FMATRX (P,X,ZO,Z2,Z3,DEE,DST)                                SAT09060
      LSTEP=1                                                           SAT09070
      LCHANG=0                                                          SAT09080
      ITR=1                                                             SAT09090
      ICORFL=0                                                          SAT09100
      IF(MNMAX.EQ.MAXM) ICORFL=1                                        SAT09110
      IPASS=0                                                           SAT09120
      ITTEST=0
  400 CALL XANDZ (P,DEE,DST,X,Z,ZO,Z2,Z3,ZDOT,IS,JS,ID,JD,PHIXB,PHITB)  SAT09130
      IF(ITRMAX.EQ.1) GO TO 50                                          SAT09140
      MNMAXO=MNMAX                                                      SAT09150
      IF(IPASS.LT.2) CALL MODES (IS,JS,ID,JD,P,X,ZO,Z2,Z3,DEE,DST)
      IF(NCONV.EQ.1) GO TO 50                                           SAT09170
      IF(ITR.LT.ITRMAX) GO TO 23                                        SAT09180
      GO TO 365                                                         SAT09190
   50 FL=LSTEP                                                          SAT09200
      FI=IPRINT                                                         SAT09210
      LI=LSTEP/IPRINT                                                   SAT09220
      FLI=LI                                                            SAT09230
      FT=FLI-FL/FI                                                      SAT09240
      IF(FT.EQ.0.) CALL OUTPUT(IMODE,P,DEE,DST,X,Z,ZO,Z2,Z3,ZDOT,IS,JS, SAT09250
     1ID,JD,PHIXB,PHITB)                                                SAT09260
      IF(LSTEP.GE.LSMAX) GO TO 360                                      SAT09300
      DO 65 MN=1,MNMAXO                                                 SAT09310
      DO 65 K=1,KMAX2                                                   SAT09320
      IK=K+(MN-1)*KMAX2                                                 SAT09330
      DO 65 I=1,4                                                       SAT09340
      ZN=3.0*(Z(I,IK)-ZO(I,IK))+Z2(I,IK)                                SAT09350
      Z3(I,IK)=Z2(I,IK)                                                 SAT09360
      Z2(I,IK)=ZO(I,IK)                                                 SAT09370
      ZO(I,IK)=Z(I,IK)                                                  SAT09380
   65 Z(I,IK)=ZN                                                        SAT09390
      ALCAD=1.0                                                         SAT09400
      LSTEP=LSTEP+1                                                     SAT09410
      ITR=1                                                             SAT09420
      GO TO 400                                                         SAT09430
   23 ITR=ITR+1                                                         SAT09440
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      GO TO 400                                                         SAT09450
  360 WRITE(6,271)                                                      SAT09460
      WRITE(6,188)(AVB(M),M=1,MAXM)                                     SAT09470
      WRITE(6,189) ITRPR                                                SAT09480
      GO TO 500                                                         SAT09490
  365 IF(LSTEP.EQ.1) GO TO 367                                          SAT09500
      WRITE(6,266) ITRMAX,LSTEP,NC                                      SAT09510
      WRITE(6,188)(AVB(M),M=1,MAXM)                                     SAT09520
      GO TO 500                                                         SAT09530
  367 WRITE(6,273)                                                      SAT09540
      GO TO 500                                                         SAT09550
C***********************************************************************SAT09560
   71 FORMAT(20X,I3,4X,4E20.6)                                          SAT09570
  112 FORMAT(////17X,12H  STATION   20H      B STIFFNESS   20H      D STSAT09580
     1IFFNESS   20H      B PRIME          20H      D PRIME        //)   SAT09590
  126 FORMAT(////5X,29HTHE INITIAL CONDITIONS FOR N=I3,8H  FOLLOW//)    SAT09600
  127 FORMAT(19X,7HSTATION,3X,20H         U                 20H      V  SAT09610
     1    20H        W              20H        M S               //)    SAT09620
  129 FORMAT(///19X,7HSTATION,3X,20H       U DOT              20H     V DOT  SAT09630
     1        20H        W DOT           20H        M S DOT        //)   SAT09640
  188 FORMAT(////' THE MAXIMUM VBAR FOR EACH MODE IS'/10E11.4)          SAT09650
  189 FORMAT(/'  THE MAXIMUMUM NUMBER OF ITERATIONS TAKEN IS   ',I3)     SAT09660
  266 FORMAT(1H1,35H    THE SOLUTION DID NOT CONVERGE INI3,24H ITERATIONSSAT09670
     1 AT TIME STEPI5,21H.  END PROBLEM NUMBERI4,1H.)                   SAT09680
  271 FORMAT(1H1,79H              THE MAXIMUM NUMBER OF TIME STEPS HAVE BEENSAT09690
     1 TAKEN.  END PROBLEM NUMBERI4)                                    SAT09700
  273 FORMAT(1H1,69H              THE SOLUTION DID NOT CONVERGE FOR THE FIRSSAT09710
     1T TIME INCREMENT./11X,71HLOCK FOR AN ERROR IN THE INPUT DATA, OR TSAT09720
     2RY A SMALLER VALUE FOR DELOAD.)                                   SAT09730
  810 FORMAT(1H1, 5X,15H STATION         16H     RADIUS     16H     GAMMA SAT09740
     1     16H     OMEGA S     16H     OMEGA THETA16H     DEOMEGA S  16H SAT09750
     2     MASS         //)                                             SAT09760
  813 FORMAT( 8X,I3, 9X,6E16.4)                                         SAT09770
 8888 FORMAT (' ',T10,'EXECUTING IN SUBROUTINE "DYNAMIC"')              SAT09780
  500 RETURN                                                            SAT09790
      END                                                               SAT09800
      SUBROUTINE PLOTIT(X,Y,NN,MODCUR)                                  SAT09810
C***********************************************************************SAT09820
C     THIS SUBROUTINE AND THE THREE THAT FOLLOW IT COMPRISE THE SELF-  *SAT09830
C     CONTAINED PLOTTING CAPABILITY OF PROGRAM SATANS.  THEY RECEIVE   *SAT09840
C     DATA TO BE PLOTTED, ROUND IT, SCALE IT, AND DRAW IS ON THE HIGH- *SAT09850
C     SPEED LINE PRINTER.                                              *SAT09860
C***********************************************************************SAT09870
      DIMENSION X( 1), Y( 1), RANGE(4)                                  SAT09880
      EQUIVALENCE (RANGE(1),XMAX), (RANGE(2),XMIN),(RANGE(3),YMAX),     SAT09890
     1            (RANGE(4),YMIN)                                       SAT09900
      KN=IABS(NN)                                                       SAT09910
      IF(MODCUR.GT.1) GO TO 5                                           SAT09920
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C***********************************************************************SAT09930
C     FIND MAX & MIN FOR SCALE COMPUTATIONS                            *SAT09940
C***********************************************************************SAT09950
      XMAX=-1.E20                                                       SAT09960
      XMIN=1.E20                                                        SAT09970
      YMAX=-1.E20                                                       SAT09980
      YMIN=1.E20                                                        SAT09990
      DO 1 I=1,KN                                                       SAT10000
      IF(X(I).LT.XMAX) GO TO 6                                          SAT10010
      XMAX=X(I)                                                         SAT10020
    6 IF(X(I).GT.XMIN) GO TO 7                                          SAT10030
      XMIN=X(I)                                                         SAT10040
    7 IF(Y(I).LT.YMAX) GO TO 8                                          SAT10050
      YMAX=Y(I)                                                         SAT10060
    8 IF(Y(I).GT.YMIN) GO TO 1                                          SAT10070
      YMIN=Y(I)                                                         SAT10080
    1 CONTINUE                                                          SAT10090
C***********************************************************************SAT10100
C     IF NOT AUTOSCALE GO TO CALL DRAWIT                               *SAT10110
C***********************************************************************SAT10120
      IF(NN.GT.0) GO TO 5                                               SAT10130
C***********************************************************************SAT10140
C     COMPUTE X-SCALE & NEW XMAX AND XMIN                              *SAT10150
C***********************************************************************SAT10160
      CALL SCALIT(XMAX,XMIN,4)                                          SAT10170
C***********************************************************************SAT10180
C     COMPUTE Y-SCALE & NEW YMAX AND YMIN                              *SAT10190
C***********************************************************************SAT10200
      CALL SCALIT(YMAX,YMIN,6)                                          SAT10210
C***********************************************************************SAT10220
C     PLOT CURVE                                                       *SAT10230
C***********************************************************************SAT10240
    5 CALL DRAWIT(X,Y,KN,RANGE,1,MODCUR)                                SAT10250
      IF(MODCUR. EQ.1.OR.MODCUR.EQ.2) RETURN                            SAT10260
C***********************************************************************SAT10270
C     PRINT SCALES WHEN LAST CURVE PLOTTED                             *SAT10280
C***********************************************************************SAT10290
      XS=(XMAX-XMIN)/80.                                                SAT10300
      YS=(YMAX-YMIN)/60.                                                SAT10310
      WRITE(6,100) XS,YS                                                SAT10320
  100 FORMAT(  15X,'X-SCALE:  "*"=',E10.3,' UNITS'//                    SAT10330
     1         15X,'Y-SCALE:  "*"=',E10.3,' UNITS')                     SAT10340
      RETURN                                                            SAT10350
      END                                                               SAT10360
C***********************************************************************SAT10370
      SUBROUTINE SCALIT(XMAX,XMIN,IDIV)                                 SAT10380
      DIV=IDIV                                                          SAT10390
C***********************************************************************SAT10400
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C     RCUND MAXIMUM TO NEXT HIGHEST 2 SIG FIGS                         *SAT10410
C***********************************************************************SAT10420
      XMAX=AMAX1(0.,XMAX)                                               SAT10430
      CALL RCUND(XMAX,IMX,FMX)                                          SAT10440
      IMX=IMX-1                                                         SAT10450
      FMX=FMX*10.                                                       SAT10460
    3 XMX=FMX*10.**IMX                                                  SAT10470
      IF(XMX.GE.XMAX) GC TO 2                                           SAT10480
      FMX=FMX+1.                                                        SAT10490
      IMM=FMX                                                           SAT10500
      FMX=IMM                                                           SAT10510
      GC TO 3                                                           SAT10520
C***********************************************************************SAT10530
C     RCUND MINIMUM TO NEXT LCWEST 2 SIG FIGS                          *SAT10540
C***********************************************************************SAT1055C
    2 XMIN=AMIN1(0.,XMIN)                                               SAT10560
      CALL RCUND(XMIN,IMN,FMN)                                          SAT10570
      IMN=IMN-1                                                         SAT10580
      FMN=FMN*10.                                                       SAT10590
   14 XMN=FMN*10.**IMN                                                  SAT10600
      IF(XMIN.GE.XMN) GC TO 11                                          SAT10610
      FMN=FMN-1.                                                        SAT10620
      IMM=FMN                                                           SAT10630
      FMN=IMM                                                           SAT10640
      GC TO 14                                                          SAT10650
C***********************************************************************SAT10660
C     RCUND MAX & MIN TC 1. OR .1 IF RANGE LARGE                       *SAT1C670
C***********************************************************************SAT10680
   11 XSC=XMX-XMN                                                       SAT10690
      IM=C                                                              SAT10700
      SM=1.                                                             SAT10710
    9 IF(XSC/CIV.LE.SM) GC TO 12                                        SAT10720
      IF(ABS(XMN).LT.SM.AND.ABS(XMN).GT.C.) XMN=SIGN(SM,XMN)            SAT10730
      IF(ABS(XMX).LT.SM.AND.ABS(XMX).GT.0.) XMX=SIGN(SM,XMX)            SAT10740
   12 IF(IM.GT.0) GO TO 19                                              SAT10750
      SM=.1                                                             SAT10760
      IM=IM+1                                                           SAT1C77C
      GC TO 9                                                           SAT10780
C***********************************************************************SAT10790
C     RCUND RANGE (MAX-MIN) TC 2 SIG FIGS                              *SAT10800
C***********************************************************************SAT10810
   19 XSC=XMX-XMN                                                       SAT10820
      CALL RCUND(XSC,ISIC,FACTX)                                        SAT1083C
C***********************************************************************SAT10840
C     FINC FACTCR WHICH IS MULTIPLE OF IDIV                            *SAT10850
C***********************************************************************SAT10860
      FACTX=FACTX*10.                                                   SAT10870
      CFAC=FACTX                                                        SAT10880
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      IS10=IS10-1                                                       SAT10890
      IFX=FACTX                                                         SAT10900
      FACTX=IFX                                                         SAT10910
   20 IF(MOD(IFX,IDIV).EQ.0.AND.FACTX.GE.OFAC) GO TO 10                 SAT10920
      IFX=IFX+1                                                         SAT10930
      FACTX=IFX                                                         SAT10940
      GO TO 20                                                          SAT10950
   10 IF(IDIV.GT.4) GO TO 15                                            SAT10960
C***********************************************************************SAT10970
C     IF X SCALE BETWEEN 8. AND 10., ROUND TO 10.                      *SAT10980
C***********************************************************************SAT10990
      FFX=ABS(FACTX/10.)                                                SAT11000
      IF(FFX.GT.8..AND.FFX.LT.10.) FFX=10.                              SAT11010
      IF(FACT X.LT.0.) FXX=-10.                                         SAT11020
      FACTX=FFX*10.                                                     SAT11030
   15 XSC=FACTX*10.**IS10                                               SAT11040
C***********************************************************************SAT11050
C     COMPUTE NEW MAX & MIN FROM ROUNDED SCALE                         *SAT11060
C***********************************************************************SAT11070
      IF(XM N*XM X.NE.0.) GO TO 4                                       SAT11080
      IF(XM N.LT.0.) XMIN=-XSC                                          SAT11090
      IF(XM X.GT.0.) XMAX=XSC                                           SAT11100
      RETURN                                                            SAT11110
    4 XMAX=XSC+XMN                                                      SAT11120
      XMIN=XMN                                                          SAT11130
      RETURN                                                            SAT11140
      END                                                               SAT11150
C***********************************************************************SAT11160
      SUBROUTINE ROUND(ANUM,IS,FACT)                                    SAT11170
C***********************************************************************SAT11180
C     EXPRESS ANUM IN SCIENTIFIC NOTATION WHERE                        *SAT11190
C           ANUM=FACT*10.**IS WHERE FACT IS BETWEEN 1. AND 9.9         *SAT11200
C***********************************************************************SAT11210
      IF(ANUM.EQ.0.) GO TO 15                                           SAT11220
      BNUM=ANUM                                                         SAT11230
      IF(BNUM.LT.0.) BNUM=-BNUM                                         SAT11240
      IS=ALOG(BNUM)*.43429448                                           SAT11250
      FACT=BNUM/10.**IS                                                 SAT11260
C***********************************************************************SAT11270
C     FIND POWER OF 10                                                 *SAT11280
C***********************************************************************SAT11290
      ICD=-3                                                            SAT11300
      R2=0                                                              SAT11310
      DO 10 II=1,5                                                      SAT11320
      ICD=ICD+1                                                         SAT11330
      R1=R2                                                             SAT11340
      R2=10.**(ICD+1)                                                   SAT11350
      IF(FACT.GE.R1.AND.FACT.LT.R2) GO TO 8                             SAT11360
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   10 CONTINUE                                                          SAT11370
    8 FACT=FACT*10.**(-IDD)                                             SAT11380
      IS=IS+IDD                                                         SAT11390
C***********************************************************************SAT11400
C     ROUND MANTISSA TO 2 SIG FIGS                                     *SAT11410
C***********************************************************************SAT11420
      IFAC=FACT*10.+.05                                                 SAT11430
      FACT=IFAC                                                         SAT11440
      FACT=FACT/10.                                                     SAT11450
      IF(FACT.LT.10.) GO TO 20                                          SAT11460
C***********************************************************************SAT11470
C     SET TO 1 IF LESS THAN 10.                                        *SAT11480
C***********************************************************************SAT11490
      FACT=1.                                                           SAT11500
      IS=IS+1                                                           SAT11510
C***********************************************************************SAT11520
C     IF INPUT NEGATIVE, SET MANTISSA NEGATIVE                         *SAT11530
C***********************************************************************SAT11540
   20 IF(ANUM.LT.0.) FACT=-FACT                                         SAT11550
      RETURN                                                            SAT11560
C***********************************************************************SAT11570
C     SET TO 0. IF 0.                                                  *SAT11580
C***********************************************************************SAT11590
   15 FACT=0.                                                           SAT11600
      IS=0                                                              SAT11610
      RETURN                                                            SAT11620
      END                                                               SAT11630
C***********************************************************************SAT11640
      SUBROUTINE DRAWIT(X,Y,NDATA,RANGE,KKZ,MODCUR)                     SAT11650
      DIMENSION GRID(61,81),XSCALE(5),YSCALE(7)                         SAT11660
      DIMENSION X(1),Y(1),RANGE(4)                                      SAT11670
      INTEGER*2 GRID,BLANK,DOT,XCHAR(4)/1H+,1H.,1H*,1HX/                SAT11680
      DATA DOT,BLANK/Z4B40,Z4040/                                       SAT11690
      KDATA=NDATA*KKZ                                                   SAT11700
      IF(MODCUR.GT.1) GO TO 444                                         SAT11710
C***********************************************************************SAT11720
C     GRID IS THE MATRIX USED TO PLOT THE POINTS                       *SAT11730
C***********************************************************************SAT11740
      IERR=0                                                            SAT11750
      XMAX=RANGE(1)                                                     SAT11760
      XMIN=RANGE(2)                                                     SAT11770
      YMAX=RANGE(3)                                                     SAT11780
      YMIN=RANGE(4)                                                     SAT11790
C***********************************************************************SAT11800
C     CHECKING X AND Y POINTS AND PLOTTING THOSE OUT OF RANGE          *SAT11810
C     AT THE MARGIN                                                    *SAT11820
C***********************************************************************SAT11830
      DO 30 I=1,KDATA,KKZ                                               SAT11840
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      IF(X(I).GT.XMAX.OR.X(I).LT.XMIN.OR.Y(I).GT.YMAX.OR.Y(I).LT.YMIN)  SAT11850
     1  IERR=IERR+1                                                     SAT11860
      IF(X(I).LE.XMAX) GO TO 205                                        SAT11870
      X   (I)=XMAX                                                      SAT11880
      GOTO 210                                                          SAT11890
  205 IF(X(I).GE.XMIN) GO TO 210                                        SAT11900
      X   (I)=XMIN                                                      SAT11910
  210 IF(Y(I).LE.YMAX) GO TO 215                                        SAT11920
      Y   (I)=YMAX                                                      SAT11930
      GOTO 30                                                           SAT11940
  215 IF(Y(I).GE.YMIN) GO TO 30                                         SAT11950
      Y   (I)=YMIN                                                      SAT11960
   30 CONTINUE                                                          SAT11970
C***********************************************************************SAT11980
C      PLOTTING X AND Y AXIS , IF NECESSARY                            *SAT11990
C***********************************************************************SAT12000
      JERR=0                                                            SAT12010
      XRANGE=XMAX-XMIN                                                  SAT12020
      YRANGE=YMAX-YMIN                                                  SAT12030
      IF (YRANGE.NE.0.)  GO TO 298                                      SAT12040
      IF(YMIN.EQ.0.) GO TO 889                                          SAT12050
      YMIN=0.                                                           SAT12060
      YRANGE=YMAX                                                       SAT12070
      GO TO 299                                                         SAT12080
  298 IF (XRANGE.NE.0.)  GO TO 299                                      SAT12090
      IF(XMIN.EQ.0.) GO TO 887                                          SAT12100
      XMIN=0.                                                           SAT12110
      XRANGE=XMAX                                                       SAT12120
C***********************************************************************SAT12130
C      BLANKING CUT MATRIX-(GRID)                                      *SAT12140
C***********************************************************************SAT12150
  299 DO 300 I=1,61                                                     SAT12160
      DO 301 JJ=1,81                                                    SAT12170
301   GRID(I,JJ)=BLANK                                                  SAT12180
  300 CONTINUE                                                          SAT12190
      IF(XMAX*XMIN.GE.0.) GO TO 222                                     SAT12200
      IYAXIS=80.*(-XMIN)/XRANGE+1.5                                     SAT12210
      DO 40 I=1,61                                                      SAT12220
   40 GRID(I,IYAXIS)=DOT                                                SAT12230
  222 IF(YMAX*YMIN.GE.0.) GO TO 333                                     SAT12240
      IXAXIS=60.*YMAX/YRANGE+1.5                                        SAT12250
      DO 60 I=1,81                                                      SAT12260
   60 GRID(IXAXIS,I)=DOT                                                SAT12270
C***********************************************************************SAT12280
C      COMPUTE PROPER SCALE NUMBERS                                    *SAT12290
C***********************************************************************SAT12300
  333 XINCR=XRANGE/4.                                                   SAT12310
      YINCR=YRANGE/6.                                                   SAT12320
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      XSCALE(1)=XMAX                                                    SAT12330
      XSCALE(5)=XMIN                                                    SAT12340
      DO 80 I=2,4                                                       SAT12350
      XSCALE(I)=XSCALE(I-1)-XINCR                                       SAT12360
      IF(ABS(XSCALE(I)).LT.1.E-4) XSCALE(I)=0.                          SAT12370
   80 CONTINUE                                                          SAT12380
      YSCALE(1)=YMAX                                                    SAT12390
      YSCALE(7)=YMIN                                                    SAT12400
      DO 81 I=2,6                                                       SAT12410
      YSCALE(I)=YSCALE(I-1)-YINCR                                       SAT12420
      IF(ABS(YSCALE(I)).LT.1.E-4) YSCALE(I)=0.                          SAT12430
   81 CONTINUE                                                          SAT12440
      DO 85 II=1,2                                                      SAT12450
      JJ=6-II                                                           SAT12460
      XT=XSCALE(JJ)                                                     SAT12470
      XSCALE(JJ)=XSCALE(II)                                             SAT12480
   85 XSCALE(II)=XT                                                     SAT12490
C***********************************************************************SAT12500
C***********************************************************************SAT12510
  444 IF(MODCUR.LT.2) JSET=0                                            SAT12520
      IF(JERR.GT.0) GO TO 885                                           SAT12530
      JSET=JSET+1                                                       SAT12540
      IF(JSET.GT.4) JSET=1                                              SAT12550
      DO 700 I=1,KDATA,KKZ                                              SAT12560
      IPTX=60.*(YMAX-Y(I))/YRANGE+1.5                                   SAT12570
      IPTY=80.*(X(I)-XMIN)/XRANGE+1.5                                   SAT12580
      IF(IPTX.GT.61.OR.IPTY.GT.81) GO TO 70                             SAT12590
      IF(IPTX.LE.0.OR.IPTY.LE.0)GO TO 70                                SAT12600
      GRID(IPTX,IPTY) = XCHAR(JSET)                                     SAT12610
      GO TO 700                                                         SAT12620
   70 IERR=IERR+1                                                       SAT12630
  700 CONTINUE                                                          SAT12640
C***********************************************************************SAT12650
C     OUTPUT SECTION WITH GRAPH                                        *SAT12660
C***********************************************************************SAT12670
      IF(MODCUR.EQ.1.OR.MODCUR.EQ.2) RETURN                             SAT12680
      AXR=ABS(XRANGE)                                                   SAT12690
      AYR=ABS(YRANGE)                                                   SAT12700
      IF(AXR.LT.1.E+8.AND.AXR.GE..95) GO TO 400                         SAT12710
      WRITE(6,17) XSCALE                                                SAT12720
   17 FORMAT(12X,1PE10.3,4(10X,E10.3)/15X,'**',8('+*********'),'+**')  SAT12730
      GO TO 401                                                         SAT12740
  400 WRITE(6,117) XSCALE                                               SAT12750
  117 FORMAT( 8X,F11.2,4( 9X,F11.2)/15X,'**',8('+*********'),'+**')     SAT12760
  401 II=1                                                              SAT12770
      DO 101 IK=1,61                                                    SAT12780
      IF(MOD(IK-1,10).NE.0) GO TO 92                                    SAT12790
      IF(AYR.LT.1.E+8.AND.AYR.GE..95) GO TO 404                         SAT12800
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      WRITE(6,18) YSCALE(II),(GRID(IK,IX),IX=1,81),YSCALE(II)           SAT12810
   18 FORMAT(3X,1PE10.3,2X,1H+,1X,81A1,1X,1H+,2X,E10.3)                 SAT12820
      GO TO 405                                                         SAT12830
  404 WRITE(6,118) YSCALE(II),(GRID(IK,IX),IX=1,81),YSCALE(II)          SAT12840
  118 FORMAT(2X,F11.2,'  + ',81A1,' +  ',F11.2)                         SAT12850
  405 II=II+1                                                           SAT12860
      GO TO 101                                                         SAT12870
   92 WRITE(6,19) (GRID(IK,IX),IX=1,81)                                 SAT12880
   19 FORMAT(15X,'* ',81A1,' *')                                        SAT12890
  101 CONTINUE                                                          SAT12900
      IF(AXR.LT.1.E+8.AND.AXR.GE..95) GO TO 402                         SAT12910
      WRITE(6,22) XSCALE                                                SAT12920
   22 FORMAT(15X,'**',8('+*********'),'+**'/12X,1PE10.3,4(10X,E10.3),//)SAT12930
      GO TO 403                                                         SAT12940
  402 WRITE(6,217) XSCALE                                               SAT12950
  217 FORMAT(15X,'**',8('+*********'),'+**'/ 8X,F11.2,4( 9X,F11.2),//)  SAT12960
  403 IF(IERR.GT.0) WRITE(6,20) IERR                                    SAT12970
   20 FORMAT(10X 'NUMBER OF POINTS OUT OF RANGE =', I4)                 SAT12980
 1000 RETURN                                                            SAT12990
  889 WRITE(6,888)                                                      SAT13000
  888 FORMAT(' ALL Y VALUES=0. CANNOT SETUP PLOT GRID. CHECK MAX & MIN YSAT13010
     1 WHEN MOCCUR=0 OR 1.')                                            SAT13020
      JERR=10                                                           SAT13030
      RETURN                                                            SAT13040
  887 WRITE(6,886)                                                      SAT13050
  886 FORMAT(' ALL X VALUES=0. CANNOT SETUP PLOT GRID. CHECK MAX & MIN XSAT13060
     1 WHEN MOCCUR=0 OR 1.')                                            SAT13070
      JERR=10                                                           SAT13080
      RETURN                                                            SAT13090
  885 WRITE(6,884)                                                      SAT13100
  884 FORMAT(' GRID NOT SETUP WHEN MOCCUR LAST 0 OR 1. NO PLOT UNTIL GRISAT13110
     1D PROPERLY SETUP')                                                SAT13120
      RETURN                                                            SAT13130
      END                                                               SAT13140
      SUBROUTINE OUTPUT(IMODE,P,DEE,DST,X,Z,Z0,Z2,Z3,ZDOT,IS,JS,ID,JD,  SAT13150
     1PHIXB,PHITB)                                                      SAT13160
C***********************************************************************SAT13170
C         THIS SUBROUTINE PREPARES THE PRINTOUT MATERIAL.  EVERY IPRINT *SAT13180
C         CONVERGED SOLUTION IS PRINTED.  THE FOURIER COEFFICIENTS OF THESAT13190
C         INPLANE FORCES, MERIDIONAL TRANSVERSE FORCE, CIRCUMFERENTIAL  *SAT13200
C         BENDING MOMENT, TWISTING MOMENT AND ROTATIONS CAN BE COMPUTED *SAT13210
C         AND PRINTED WITH THE SOLUTION Z FOR THE FOURIER COEFFICIENTS  *SAT13220
C         OF THE THREE DISPLACEMENTS AND MERIDIONAL BENDING MOMENT.  THISSAT13230
C         OUTPUT MATERIAL IS CONVERTED FROM DIMENSIONLESS FORM TO DIMEN-*SAT13240
C         SIONAL FORM HERE.  PROVISION IS MADE TO PRINT ONLY AT STATIONS*SAT13250
C         1, IFREQ+1, 2IFREQ+1, ETC.  THIS SUBROUTINE ALSO PERFORMS THE *SAT13260
C         SUMMATION PROCESS FOR COMPUTING THE TOTAL VALUES OF THE FORCES,SAT13270
C         MOMENTS, DISPLACEMENTS AND ROTATIONS AT THE NTHMAX POSITIONS  *SAT13280
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C        AROUND THE CIRCUMFERENCE PRESCRIBED IN THE INPUT DATA.         *SAT13290
C     DATA TO BE PLOTTED IS PREPARED HERE, IF REQ'D                     *SAT13300
C***********************************************************************SAT13310
      IMPLICIT LOGICAL*1 ($)                                             SAT13320
      REAL NU,MT,MX,MTH,MXT,MTS,KX,KT,KXT,LAM,LAM2,MASS                  SAT13330
      DIMENSION P(4,4,1),DEE(4,4,1),DST(4,4,1),X(4,1),Z(4,1),            SAT13340
     1ZC(4,1),Z2(4,1),Z3(4,1),ZDOT(4,1),IS(99,1),JS(99,1),IC(99,1),      SAT13350
     2JC(99,1),PHIXB(1),PHITB(1)                                         SAT13360
      COMMON /IBL2/ N(99),MNINIT                                         SAT13370
      COMMON /IBL3/ MO,M1,M2,M3                                          SAT13380
      COMMON /IBL4/ KMAX,KL                                              SAT13390
      COMMON /IBL5/ IBCINL,IBCFNL                                        SAT13400
      COMMON /IBL7/ MNMAXO,MAXD(99),MAXS(99),MAXSY(99),IJS(99)           SAT13410
      COMMON /IBL8/ LSTEP,ITR                                            SAT13420
      COMMON /IBL10/ IFREQ,NTHMAX                                        SAT13430
      COMMON /IBL12/ KMAX1,KMAX2,NCONV                                   SAT13440
      COMMON /IBL13/ ITRMAX,LSMAX                                        SAT13450
     1/IBLJ/ JUMP                                                        SAT13460
      COMMON /BL4/   ZF1M(4,4,99),ZF2M(4,4,99),
     1               ZF3M(4,4,99),ZF4M(4,4,99)
      COMMON /BL5/   TT(99),MT(99),DT(99),DMT(99)                        SAT13490
      COMMON /BL6/   SOE,OSE,ALOAD                                       SAT13500
      COMMON /BL7/   D1,S1                                               SAT13510
      COMMON /BL8/   R(500),GAM(500),OMT(500)                            SAT13520
      COMMON /BL10/  PHIX(99),PHIT(99),PHI(99)                           SAT13530
      COMMON /BL11/  OMXI(500),PHEE,TO,T2                                SAT13540
      COMMON /BL12/  TOLI,TDEL                                           SAT13550
      COMMON /BL14/  LAM2,LSD18,LSD1N                                    SAT13560
      COMMON /BL15/  NU,U1(99),V1(99),W1(99),V2(99),U2(99),W2(99),U3(99),SAT13570
     1               V3(99),W3(99)                                       SAT13580
      COMMON /BL17/  DEL                                                 SAT13590
      COMMON /BL19/  TH(36)                                              SAT13600
      COMMON /BL20/  DEOMX(500)                                          SAT13610
      COMMON /BL27/  BX3(99),BT3(99),BXT3(99),BE3(99)                    SAT13620
      COMMON /BL31/  DELSG,EXT1(99)                                      SAT13630
      COMMON /BL32/  TKN,ELAST,CHAR,SIGC                                 SAT13640
      COMMON /BL100/ TEEC,$DYNMC                                         SAT13650
      COMMON /BL101/ DELSD                                               SAT13660
      COMMON /BL102/ DELOAD                                              SAT13670
      COMMON /BL103/ MASS(500)                                           SAT13680
      COMMON /BL110/ TX(99),TTH(99),TXT(99),MX(99),MTH(99),MXT(99),      SAT13690
     1               QS(99)                                              SAT13700
      COMMON /BL111/ ABZ,ABZC,ABZN,ABZ3,CC2                              SAT13710
      COMMON /BLPLOT/  IRADII,IGAMMA,IOMEGS,IOMEGT,IDECMS,IBSTIF,IDSTIF, SAT13720
     1                 IBBSTF,IDDSTF,IPR,IPS,IPT,ITT,IMT,IDTT,IDMT,INS,  SAT13730
     2                 INTH,INSTH,IQS,IMS,IMTH,IMSTH,IU,IV,IW,IPHIS,     SAT13740
     3                 IPHIT,IPHI,$PLOTS,$MODAL                          SAT13750
      COMMON /BLPLT1/  XRADII(200),YGAMMA(200),YOMEGS(200),YOMEGT(200),  SAT13760
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     1                 YDECMS(200),YBSTIF(200),YCSTIF(200),YBBSTF(200),  SAT13770
     2                 YDDSTF(200),YPR(200),YPS(200),YPT(200),YTT(200),  SAT13780
     3                 YMT(200),YDTT(200),YDMT(200),YNS(200),YNTH(200),  SAT13790
     4                 YNSTH(200),YQS(200),YMS(200),YMTH(200),YMSTH(200),SAT13800
     5                 YU(200),YV(200),YW(200),YPHIS(200),YPHIT(200),    SAT13810
     6                 YPHI(200),XSTATN(200)                             SAT13820
      DIMENSION PTF(500),PF(500)                                         SAT13830
C***********************************************************************SAT13840
      ABZC=SIGO/ELAST                                                    SAT13850
      IF ($DYNMC) GO TO 181                                              SAT13860
      WRITE(6,101) LSTEP,ALOAD,ITR                                       SAT13870
      GO TO 182                                                          SAT13880
  181 TI=LSTEP*DELOAD                                                    SAT13890
      DTI=TI*TEEG                                                        SAT13900
      WRITE(6,151) LSTEP,TI,DTI,ITR                                      SAT13910
  182 LAM=TKN/CHAR                                                       SAT13920
      ENL=1.                                                             SAT13930
      ABZ=SIGO*TKN                                                       SAT13940
      ABZ3=ABZ*TKN*TKN/CHAR                                              SAT13950
      ABZN=CHAR*SIGO/ELAST                                               SAT13960
      IF(ITRMAX.EQ.1) ENL=0.                                             SAT13970
      DD2=1.-NU**2                                                       SAT13980
      D2I=1./DD2                                                         SAT13990
      DPI=1./S1                                                          SAT14000
      DNI=1./D1                                                          SAT14010
      TDLSQI=.5/DELSQ                                                    SAT14020
      ICHCK1=IABS(INS)+IABS(INTH)+IABS(INSTH)+IABS(IQS)+IABS(IMS)        SAT14030
     1          +IABS(IMTH)+IABS(IMSTH)                                  SAT14040
      ICHCK2=IABS(IU)+IABS(IV)+IABS(IW)+IABS(IPHIS)+IABS(IPHIT)          SAT14050
     1          +IABS(IPHI)                                              SAT14060
      IF(NTHMAX.EQ.0) GO TO 991                                          SAT14070
      DO 21 NTH=1,NTHMAX                                                 SAT14080
      DO 1 MN=1,MNMAXO                                                   SAT14090
      I1=1+(MN-1)*KMAX2                                                  SAT14100
      I2=I1+1                                                            SAT14110
      U1(MN)=Z(1,I1)                                                     SAT14120
      U2(MN)=Z(1,I2)                                                     SAT14130
      V1(MN)=Z(2,I1)                                                     SAT14140
      V2(MN)=Z(2,I2)                                                     SAT14150
      W1(MN)=Z(3,I1)                                                     SAT14160
    1 W2(MN)=Z(3,I2)                                                     SAT14170
      THET=TH(NTH)                                                       SAT14180
      WRITE(6,116) THET                                                  SAT14190
      DO 121 K=1,KMAX                                                    SAT14200
      K1=K+1                                                             SAT14210
      CALL BCB(K,BS,DB,CS,DD)                                            SAT14220
      IF(K.EQ.1.AND.IBCINL.LT.0) CALL PCLE(K,P,DEE,CST,X,Z,ZO,Z2,Z3,     SAT14230
     1ZDCT,IS,JS,ID,JD,PHIXB,PHITB)                                      SAT14240
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      IF(K.EQ.1.AND.IBCINL.LT.0) GO TO 999                              SAT14250
      IF(K.EQ.KMAX.AND.IBCFNL.LT.0) CALL POLE(K,P,CEE,DST,X,Z,ZO,Z2,Z3, SAT14260
     1ZCCT,IS,JS,ID,JD,PHIXB,PHITB)                                     SAT14270
      IF(K.EQ.KMAX.AND.IBCFNL.LT.0) GO TO 999                           SAT14280
      CALL PHIBET(K,Z,IS,JS,ID,JD,PHIXB,PHITB)                          SAT14290
      DEX=DEGMX(K)                                                      SAT14300
      RRA=1./R(K)                                                       SAT14310
      OX=CMXI(K)                                                        SAT14320
      OT=CMT(K)                                                         SAT14330
      GA=GAM(K)                                                         SAT14340
      DOXT=OX-OT                                                        SAT14350
      GDO=GA*DOXT                                                       SAT14360
      DD2D=DD2*DS                                                       SAT14370
      DO 3 MN=1,MNMAXO                                                  SAT14380
      EN=N(MN)                                                          SAT14390
      ENR=EN*RRA                                                        SAT14400
      CALL TLOAD(K,Z)                                                   SAT14410
      TTS=TT(MN)*ALOAD                                                  SAT14420
      EX=(U3(MN)-U1(MN))*TDLI+OX*W2(MN)+ENL*OSE*(EX3(MN)+BE3(MN))       SAT14430
      ET=ENR*V2(MN)+GA*U2(MN)+OT*W2(MN)+ENL*OSE*(ET3(MN)+BE3(MN))       SAT14440
      EXT=.5*((V3(MN)-V1(MN))*TDLI-ENR*U2(MN)-GA*V2(MN)+ENL*OSE*BXT3(MN)SAT14450
     1)                                                                 SAT14460
      KT=ENR*PHIT(MN)+GA*PHIX(MN)                                       SAT14470
      KXT=.5*(ENR*(-PHIX(MN)-GA*W2(MN)+(W3(MN)-W1(MN))*TDLI)+GDO*V2(MN) SAT14480
     1     +OT*(V3(MN)-V1(MN))*TDLI-GA*PHIT(MN)-DOXT*PHI(MN))           SAT14490
      TX(MN)=ES*(EX+NU*ET)-TTS                                          SAT14500
      TTH(MN)=BS*(ET+NU*EX)-TTS                                         SAT14510
      TXT(MN)=BS*D1*EXT                                                 SAT14520
      MK1=K1+(MN-1)*KMAX2                                               SAT14530
      MX(MN)=Z(4,MK1)                                                   SAT14540
      MTH(MN)=NU*MX(MN)+DD2D*KT-D1*MT(MN)*ALOAD                         SAT14550
      MXT(MN)=DS*D1*KXT                                                 SAT14560
      MK11=MK1+1                                                        SAT14570
      MKK1=MK1-1                                                        SAT14580
      CS(MN)=SIGO*TKN*LAM2*(GA*MX(MN)+(Z(4,MK11)-Z(4,MKK1))*TDLI        SAT14590
     1      +ENR*MXT(MN)-GA*MTH(MN))                                    SAT14600
      MX(MN)=MX(MN)*ABZ3                                                SAT14610
      MTH(MN)=MTH(MN)*ABZ3                                              SAT14620
      MXT(MN)=MXT(MN)*ABZ3                                              SAT14630
      TX(MN)=TX(MN)*ABZ                                                 SAT14640
      TTH(MN)=TTH(MN)*ABZ                                               SAT14650
      TXT(MN)=TXT(MN)*ABZ                                               SAT14660
      PHIX(MN)=PHIX(MN)*ABZO                                            SAT14670
      PHIT(MN)=PHIT(MN)*ABZO                                            SAT14680
      PHI(MN)=PHI(MN)*ABZO                                              SAT14690
      L1(MN)=L2(MN)                                                     SAT14700
      L2(MN)=L3(MN)                                                     SAT14710
      V1(MN)=V2(MN)                                                     SAT14720
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      V2(MN)=V3(MN)                                                     SAT14730
      W1(MN)=W2(MN)                                                     SAT14740
    3 W2(MN)=W3(MN)                                                     SAT14750
      FK=K-1                                                            SAT14760
      FIFREQ=IFREQ                                                      SAT14770
      KTST=(K-1)/IFREQ                                                  SAT14780
      FKTST=KTST                                                        SAT14790
      FKTEST=FK/FIFREQ-FKTST                                            SAT14800
      IF(K.EQ.1.OR.K.EQ.KMAX) GO TO 999                                 SAT14810
      IF(FKTEST.NE.0.) GO TO 2                                          SAT14820
  999 X(1,K)=0.                                                         SAT14830
      X(2,K)=0.                                                         SAT14840
      X(3,K)=0.                                                         SAT14850
      X(4,K)=0.                                                         SAT14860
      PTF(K)=0.                                                         SAT14870
      PF(K)=0.                                                          SAT14880
      AMX=0.                                                            SAT14890
      AMTH=0.                                                           SAT14900
      AMXTH=0.                                                          SAT14910
      ANX=0.                                                            SAT14920
      ANTH=0.                                                           SAT14930
      ANXTH=0.                                                          SAT14940
      AQS=0.                                                            SAT14950
      IF(JUMP.EQ.2) GO TO 73                                            SAT14960
      DO 72 MN=1,MNMAXO                                                 SAT14970
      EN=N(MN)                                                          SAT14980
      FC=EN*THET                                                        SAT14990
      SN=SIN(FC)                                                        SAT15000
      CS=COS(FC)                                                        SAT15010
      X(1,K)=X(1,K)+U1(MN)*CS*ABZN                                      SAT15020
      X(2,K)=X(2,K)+V1(MN)*SN*ABZN                                      SAT15030
      X(3,K)=X(3,K)+W1(MN)*CS*ABZN                                      SAT15040
      X(4,K)=X(4,K)+PHIX(MN)*CS                                         SAT15050
      PTF(K)=PTF(K)+PHIT(MN)*SN                                         SAT15060
      AMX=AMX+MX(MN)*CS                                                 SAT15070
      AMTH=AMTH+MTH(MN)*CS                                              SAT15080
      AMXTH=AMXTH+MXT(MN)*SN                                            SAT15090
      ANX=ANX+TX(MN)*CS                                                 SAT15100
      ANTH=ANTH+TTH(MN)*CS                                              SAT15110
      AQS=AQS+QS(MN)*CS                                                 SAT15120
      ANXTH=ANXTH+TXT(MN)*SN                                            SAT15130
   72 PF(K)=PF(K)+PHI(MN)*SN                                            SAT15140
C***********************************************************************SAT15150
      GO TO 429                                                         SAT15160
   73 DO 74 MN=3,MNMAXO,JUMP                                            SAT15170
      EN=N(MN)                                                          SAT15180
      FC=EN*THET                                                        SAT15190
      SN=SIN(FC)                                                        SAT15200
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      CS=COS(FC)                                                        SAT15210
      MNM=MN-1                                                          SAT15220
      X(1,K)=X(1,K)+(U1(MN)*CS+U1(MNM)*SN)*ABZN                         SAT15230
      X(2,K)=X(2,K)+(V1(MN)*SN+V1(MNM)*CS)*ABZN                         SAT15240
      X(3,K)=X(3,K)+(W1(MN)*CS+W1(MNM)*SN)*ABZN                         SAT15250
      X(4,K)=X(4,K)+PHIX(MN)*CS+PHIX(MNM)*SN                            SAT15260
      PTF(K)=PTF(K)+PHIT(MN)*SN+PHIT(MNM)*CS                            SAT15270
      AMX=AMX+MX(MN)*CS+MX(MNM)*SN                                      SAT15280
      AMTH=AMTH+MTH(MN)*CS+MTH(MNM)*SN                                  SAT15290
      AMXTH=AMXTH+MXT(MN)*SN+MXT(MNM)*CS                                SAT15300
      ANX=ANX+TX(MN)*CS+TX(MNM)*SN                                      SAT15310
      ANTH=ANTH+TTH(MN)*CS+TTH(MNM)*SN                                  SAT15320
      ANXTH=ANXTH+TXT(MN)*SN+TXT(MNM)*CS                                SAT15330
      AQS=AQS+QS(MN)*CS+QS(MNM)*SN                                      SAT15340
   74 PF(K)=PF(K)+PHI(MN)*SN+PHI(MNM)*CS                                SAT15350
      X(1,K)=X(1,K)+U1(1)*ABZN                                          SAT15360
      X(2,K)=X(2,K)+V1(1)*ABZN                                          SAT15370
      X(3,K)=X(3,K)+W1(1)*ABZN                                          SAT15380
      X(4,K)=X(4,K)+PHIX(1)                                             SAT15390
      PTF(K)=PTF(K)+PHIT(1)                                             SAT15400
      PF(K)=PF(K)+PHI(1)                                                SAT15410
      AMX=AMX+MX(1)                                                     SAT15420
      AMTH=AMTH+MTH(1)                                                  SAT15430
      AMXTH=AMXTH+MXT(1)                                                SAT15440
      ANX=ANX+TX(1)                                                     SAT15450
      ANTH=ANTH+TTH(1)                                                  SAT15460
      ANXTH=ANXTH+TXT(1)                                                SAT15470
      AQS=AQS+QS(1)                                                     SAT15480
C***********************************************************************SAT15490
  429 CONTINUE                                                          SAT15500
      IF(K.EQ.1) WRITE(6,117)                                           SAT15510
      WRITE(6,118) K,ANX,ANTH,ANXTH,AQS,AMX,AMTH,AMXTH                  SAT15520
      IF ($MODAL.OR.(ICHCK1.EQ.0)) GO TO 2                              SAT15530
      YNS(K)=ANX                                                        SAT15540
      YNTH(K)=ANTH                                                      SAT15550
      YNSTH(K)=ANXTH                                                    SAT15560
      YQS(K)=AQS                                                        SAT15570
      YMS(K)=AMX                                                        SAT15580
      YMTH(K)=AMTH                                                      SAT15590
      YMSTH(K)=AMXTH                                                    SAT15600
    2 CONTINUE                                                          SAT15610
  121 CONTINUE                                                          SAT15620
      DO 660 K=1,KMAX                                                   SAT15630
      FK=K-1                                                            SAT15640
      FIFREQ=IFREQ                                                      SAT15650
      KTST=(K-1)/IFREQ                                                  SAT15660
      FKTST=KTST                                                        SAT15670
      FKTEST=FK/FIFREQ-FKTST                                            SAT15680
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```
      IF(K.EQ.1.OR.K.EQ.KMAX) GO TO 661                                 SAT15690
      IF(FKTEST.NE.0.) GO TO 658                                        SAT15700
  661 IF(K.EQ.1) WRITE(6,217)                                           SAT15710
      WRITE(6,218) K,X(1,K),X(2,K),X(3,K),X(4,K),FTF(K),PF(K)           SAT15720
      IF ($MOCAL.OR.(ICHCK2.EQ.0)) GO TO 658                            SAT15730
      YL(K)=X(1,K)                                                      SAT15740
      YV(K)=X(2,K)                                                      SAT15750
      YW(K)=X(3,K)                                                      SAT15760
      YPHIS(K)=X(4,K)                                                   SAT15770
      YPHIT(K)=PTF(K)                                                   SAT15780
      YPHI(K)=PF(K)                                                     SAT15790
  658 DO 659 I=1,4                                                      SAT15800
  659 X(I,K)=0.                                                         SAT15810
  660 CONTINUE                                                          SAT15820
      IF ($PLOTS.AND..NOT.$MOCAL.AND.((ICHCK1.GT.0).OR.(ICHCK2.GT.0)))  SAT15830
     1    CALL PLOT2(NTH)                                               SAT15840
   21 CONTINUE                                                          SAT15850
  991 IF(IMODE.LE.0) RETURN                                             SAT15860
      DO 534 MN=1,MNMAXO                                                SAT15870
      WRITE(6,749) N(MN)                                                SAT15880
      DO 521 MM=1,MNMAXO                                                SAT15890
      I1=1+(MM-1)*KMAX2                                                 SAT15900
      I2=I1+1                                                           SAT15910
      U1(MM)=Z(1,I1)                                                    SAT15920
      U2(MM)=Z(1,I2)                                                    SAT15930
      V1(MM)=Z(2,I1)                                                    SAT15940
      V2(MM)=Z(2,I2)                                                    SAT15950
      W1(MM)=Z(3,I1)                                                    SAT15960
      W2(MM)=Z(3,I2)                                                    SAT15970
  521 CONTINUE                                                          SAT15980
      DO 445 K=1, KMAX                                                  SAT15990
      K1=K+1                                                            SAT16000
      CALL BCB(K,BS,DB,CS,DD)                                           SAT16010
      IF(K.EQ.1.AND.IBCINL.LT.0) CALL POLE(K,P,CEE,CST,X,Z,ZO,Z2,Z3,    SAT16020
     1ZCCT,IS,JS,ID,JD,PHIXB,PHITB)                                     SAT16030
      IF(K.EQ.KMAX.AND.IBCFNL.LT.0) CALL POLE(K,P,CEE,DST,X,Z,ZO,Z2,Z3, SAT16040
     1ZCCT,IS,JS,ID,JD,PHIXB,PHITB)                                     SAT16050
      TXZ=TX(MN)                                                        SAT16060
      TTHZ=TTH(MN)                                                      SAT16070
      TXTZ=TXT(MN)                                                      SAT16080
      AMXZ=MX(MN)                                                       SAT16090
      AMTHZ=MTH(MN)                                                     SAT16100
      AMXTZ=MXT(MN)                                                     SAT16110
      QSZ=QS(MN)                                                        SAT16120
      X(1,K)=PHIX(MN)                                                   SAT16130
      X(2,K)=PHIT(MN)                                                   SAT16140
      X(3,K)=PHI(MN)                                                    SAT16150
      IF(K.EQ.1.AND.IBCINL.LT.0) GO TO 583                              SAT16160
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      IF(K.EQ.KMAX.AND.IBCFNL.LT.0) GO TO 583                           SAT16170
      CALL PHIBET(K,Z,IS,JS,ID,JD,PHIXB,PHITB)                          SAT16180
      DEX=DECMX(K)                                                      SAT16190
      RRA=1./R(K)                                                       SAT16200
      OX=CMXI(K)                                                        SAT16210
      OT=CMT(K)                                                         SAT16220
      GA=GAM(K)                                                         SAT16230
      CCXT=OX-OT                                                        SAT16240
      GCO=GA*CCXT                                                       SAT16250
      DD2D=DD2*DS                                                       SAT16260
      EN=N(MN)                                                          SAT16270
      ENR=EN*RRA                                                        SAT16280
      CALL TLOAD(K,Z)                                                   SAT16290
      TTS=TT(MN)*ALOAD                                                  SAT16300
      EX=(U3(MN)-U1(MN))*TDLI+OX*W2(MN)+ENL*OSE*(BX3(MN)+BE3(MN))       SAT16310
      ET=ENR*V2(MN)+GA*U2(MN)+OT*W2(MN)+ENL*OSE*(BT3(MN)+BE3(MN))       SAT16320
      EXT=.5*((V3(MN)-V1(MN))*TDLI-ENR*U2(MN)-GA*V2(MN)+ENL*SOE*BXT3(MN)SAT16330
     1)                                                                 SAT16340
      KT=ENR*PHIT(MN)+GA*PHIX(MN)                                       SAT16350
      KXT=.5*(ENR*(-PHIX(MN)-GA*W2(MN)+(W3(MN)-W1(MN))*TDLI)+GCO*V2(MN) SAT16360
     1     +OT*(V3(MN)-V1(MN))*TDLI-GA*PHIT(MN)-CCXT*PHI(MN))           SAT16370
      TXZ=(BS*(EX+NU*ET)-TTS)*ABZ                                       SAT16380
      TTHZ=(BS*(ET+NU*EX)-TTS)*ABZ                                      SAT16390
      TXTZ=BS*D1*EXT*ABZ                                                SAT16400
      MK1=K1+(MN-1)*KMAX2                                               SAT16410
      AMXZ=Z(4,MK1)                                                     SAT16420
      AMTHZ=NU*AMXZ+DD2D*KT-D1*MT(MN)*ALOAD                             SAT16430
      AMXTZ=DS*D1*KXT                                                   SAT16440
      MK11=MK1+1                                                        SAT16450
      MKK1=MK1-1                                                        SAT16460
      CSZ=SIGO*TKN*LAM2*(GA*AMXZ+(Z(4,MK11)-Z(4,MKK1))*TDLI+ENR*AMXTZ   SAT16470
     1     -GA*AMTHZ)                                                   SAT16480
      AMXZ=AMXZ*ABZ3                                                    SAT16490
      AMTHZ=AMTHZ*ABZ3                                                  SAT16500
      AMXTZ=AMXTZ*ABZ3                                                  SAT16510
      X(1,K)=PHIX(MN)*ABZ0                                              SAT16520
      X(2,K)=PHIT(MN)*ABZ0                                              SAT16530
      X(3,K)=PHI(MN)*ABZ0                                               SAT16540
      DO 533 MM=1,MNMAX0                                                SAT16550
      U1(MM)=U2(MM)                                                     SAT16560
      U2(MM)=U3(MM)                                                     SAT16570
      V1(MM)=V2(MM)                                                     SAT16580
      V2(MM)=V3(MM)                                                     SAT16590
      W1(MM)=W2(MM)                                                     SAT16600
  533 W2(MM)=W3(MM)                                                     SAT16610
      FK=K-1                                                            SAT16620
      FIFREQ=IFREQ                                                      SAT16630
      KTST=(K-1)/IFREQ                                                  SAT16640
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      FKTST=KTST                                                        SAT16650
      FKTEST=FK/FIFREQ-FKTST                                            SAT16660
      IF(K.EQ.1.OR.K.EQ.KMAX) GO TO 583                                 SAT16670
      IF(FKTEST.NE.0.) GO TO 445                                        SAT16680
  583 CONTINUE                                                          SAT16690
      IF(K.EQ.1) WRITE(6,117)                                           SAT16700
      WRITE(6,118) K,TXZ,TTHZ,TXTZ,QSZ,AMXZ,AMTHZ,AMXTZ                 SAT16710
      IF (.NOT.$PLOTS.OR..NOT.$MODAL.OR.(ICHCK1.EQ.0)) GO TO 445        SAT16720
      YNS(K)=TXZ                                                        SAT16730
      YNTH(K)=TTHZ                                                      SAT16740
      YNSTH(K)=TXTZ                                                     SAT16750
      YQS(K)=QSZ                                                        SAT16760
      YMS(K)=AMXZ                                                       SAT16770
      YMTH(K)=AMTHZ                                                     SAT16780
      YMSTH(K)=AMXTZ                                                    SAT16790
  445 CONTINUE                                                          SAT16800
  446 WRITE(6,217)                                                      SAT16810
      DO 447 K=1,KMAX                                                   SAT16820
      FK=K-1                                                            SAT16830
      FIFREQ=IFREQ                                                      SAT16840
      KTST=(K-1)/IFREQ                                                  SAT16850
      FKTST=KTST                                                        SAT16860
      FKTEST=FK/FIFREQ-FKTST                                            SAT16870
      IF(K.EQ.1.OR.K.EQ.KMAX) GO TO 593                                 SAT16880
      IF(FKTEST.NE.0.) GO TO 447                                        SAT16890
  593 KZ=K+1+(MN-1)*KMAX2                                               SAT16900
      UP=Z(1,KZ)*ABZN                                                   SAT16910
      VP=Z(2,KZ)*ABZN                                                   SAT16920
      WP=Z(3,KZ)*ABZN                                                   SAT16930
      WRITE(6,218) K,UP,VP,WP,X(1,K),X(2,K),X(3,K)                      SAT16940
      IF (.NOT.$PLOTS.OR..NOT.$MODAL.OR.(ICHCK2.EQ.0)) GO TO 447        SAT16950
      YU(K)=UP                                                          SAT16960
      YV(K)=VP                                                          SAT16970
      YW(K)=WP                                                          SAT16980
      YPHIS(K)=X(1,K)                                                   SAT16990
      YPHIT(K)=X(2,K)                                                   SAT17000
      YPHI(K)=X(3,K)                                                    SAT17010
  447 CONTINUE                                                          SAT17020
      IF ($PLOTS.AND.$MODAL.AND.((ICHCK1.GT.0).OR.(ICHCK2.GT.0)))       SAT17030
     1   CALL PLOT2(1)                                                  SAT17040
  534 CONTINUE                                                          SAT17050
C***********************************************************************SAT17060
  101 FORMAT('1','           THE LOAD STEP NUMBER IS ',I2,'        THE LSAT17070
     1OAD FACTOR IS ',E11.4,'           THE SOLUTION CONVERGED IN ',I2,' SAT17080
     2ITERATIONS'////)                                                  SAT17090
  116 FORMAT('0','           THE SUMMED FORCES, MOMENTS, DISPLACEMENTS ANSAT17100
     1D ROTATIONS FOLLOW FOR THETA =',E15.6///)                         SAT17110
  117 FORMAT (/' STATION      N S              N THETA         N STHETA  SAT17120
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     1      Q S                 M S                 M THETA          M STHETA'//)
 118 FORMAT(1X,I3,3X,7E16.4)
 151 FORMAT('1','   THE TIME STEP NUMBER IS ',I4,'      THE TIME IS ',F5
     1.2,' OR ',E9.3,' SECONDS       THE SOLUTION CONVERGED IN ',I2,' ITE
     3RATIONS'////)
 217 FORMAT(//' STATION          U                V                    W
     1        PHI S            PHI THETA          PHI'/)
 218 FORMAT(1X,I3,3X,6E16.4)
 749 FORMAT('1',40X,' MODAL OUTPUT FOR MODE N = ',I3,' FOLLOWS')
C***********************************************************************
      RETURN
      END
      SUBROUTINE XANDZ (P,DEE,DST,X,Z,ZC,Z2,Z3,ZDOT,IS,JS,ID,JD,PHIXB,
     1PHITB)
C***********************************************************************
C        THIS SUBROUTINE COMPUTES THE X VECTOR USING THE P, PBAR, AND  *
C        P-HAT MATRICES AND SOLVES FOR THE Z VECTOR FOR THE APPLIED AND*
C        PSUEDO LOADS.  THE SUBROUTINES PHIBET(K) AND TEAETA(K) ARE    *
C        CALLED AND THE PREVIOUS SOLUTION FOR Z, OR THE ESTIMATED VALUE*
C        OF Z IS USED TO CALCULATE THE NON-LINEAR BETA AND ETA TERMS.  *
C        THE MATRICES FFS AND FLS ARE THE VALUES OF SMALL-F AT THE     *
C        INITIAL AND FINAL EDGES OF THE SHELL.  THE SUBROUTINE FORCE(K)*
C        IS CALLED TO CALCULATE THE LOAD VECTOR GEE, AND THE X VECTOR AT
C        EACH MERIDIAN STATION.  ONCE THE X VECTOR IS OBTAINED FOR ALL *
C        MERIDIAN STATIONS AND THE SOLUTION FOR Z(K+1) GIVEN BY EQUATION
C        (31B) IS OBTAINED, AND THE SOLUTION FOR Z(I) AT ALL THE OTHER *
C        MERIDIAN STATIONS DEFINED BY EQUATION (29B) IS OBTAINED.  THE *
C        SOLUTION Z AT THE IMAGINARY STATION OFF THE INITIAL EDGE OF   *
C        SHELL IS OBTAINED LAST.  THE TEST FOR CONVERGENCE OF THE SOLU-*
C        TION     IS MADE AS Z IS COMPUTED.  THE SPECIAL CONDITIONS FOR*
C        COMPUTING Z AT EITHER AN INITIAL OR A FINAL POLE ARE ALSO IN  *
C        THIS ROUTINE.                                                 *
C***********************************************************************
      IMPLICIT LOGICAL*1 ($)
      REAL NU,LAM2,MT,MASS
      DIMENSION P(4,4,1),DEE(4,4,1),DST(4,4,1),X(4,1),Z(4,1),
     1ZC(4,1),Z2(4,1),Z3(4,1),ZDOT(4,1),IS(99,1),JS(99,1),ID(99,1),
     2JD(99,1),PHIXB(1),PHITB(1)
      COMMON /IBL1/ MNMAX
      COMMON /IBL3/ MO,M1,M2,M3
      COMMON /IBL4/ KMAX,KL
      COMMON /IBL5/ IBCINL,IBCFNL
      COMMON /IBL6/ KLL
      COMMON /IBL7/ MNMAXO,MAXD(99),MAXS(99),MAXSY(99),IJS(99)
      COMMON /IBL8/ LSTEP,ITR
      COMMON /IBL12/ KMAX1,KMAX2,NCONV
      COMMON /IBL13/ ITRMAX,LSMAX
      COMMON /BL1/  A(4,4),BEE(4,4),C(4,4)
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      COMMON /BL3/  PR(99),PX(99),PT(99)                                 SAT17610
      COMMON /BL4/  ZF1M(4,4,99),ZF2M(4,4,99),
     1              ZF3M(4,4,99),ZF4M(4,4,99)
      COMMON /BL5/  TT(99),MT(99),DT(99),DMT(99)                         SAT17640
      COMMON /BL6/  SOE,CSE,ALOAD                                        SAT17650
      COMMON /BL7/  D1,S1                                                SAT17660
      COMMON /BL8/  R(500),GAM(500),OMT(500)                             SAT17670
      COMMON /BL9/  FFS(4,99),EL1S(4),GEES(4,99)
      COMMON /BL14/ LAM2,LSD18,LSD1N                                     SAT17690
      COMMON /BL15/ NU,U1(99),V1(99),W1(99),V2(99),U2(99),W2(99),U3(99),SAT17700
     1              V3(99),W3(99)                                        SAT17710
      COMMON /BL16/ EPS                                                  SAT17720
      COMMON /BL18/ EL1(4),ELL(4)                                        SAT17730
      COMMON /BL27/ BX3(99),BT3(99),BXT3(99),BE3(99)                     SAT17740
      COMMON /BL28/ EXX3(99),ETT3(99),ETX3(99),EXT3(99),EX3(99),ET3(99)  SAT17750
      COMMON /BL29/ BX1(99),BT1(99),BXT1(99),BE1(99),BX2(99),BT2(99),    SAT17760
     1              BXT2(99),BE2(99)                                     SAT17770
      COMMON /BL30/ EXX1(99),ETT1(99),ETX1(99),EX1(99),ET1(99),EXX2(99),SAT17780
     1              ETT2(99),ETX2(99),EXT2(99),EX2(99),ET2(99)           SAT17790
      COMMON /BL31/ DELSQ,EXT1(99)                                       SAT17800
      COMMON /BL100/ TEEC,$DYNMC                                         SAT17810
      COMMON /BL101/ DELSD                                               SAT17820
      COMMON /BL102/ DELOAD                                              SAT17830
      COMMON /BL103/ MASS(500)                                           SAT17840
      DIMENSION ELLS(4),FLS(4),ZT(4),IPIVOT(4),INDEX(4,2)                SAT17850
     1,CL0(4,4),CL1(4,4),CL2(4,4)                                        SAT17860
     2,TZMAX(4,99),ZDD(4)
      EQUIVALENCE (CL0(1),ZF1M(1)),(CL1(1),ZF2M(1)),(CL2(1),ZF3M(1))     SAT17880
C*********************************************************************SAT17890
      DO 201 I=1,4                                                       SAT17900
      DO 201 M=1,MNMAX                                                   SAT17910
      MJ=1+(M-1)*KMAX2                                                   SAT17920
      TZMAX(I,M)=ABS(Z(I,MJ))                                            SAT17930
      DO 201 K=2,KMAX2                                                   SAT17940
      KM=K+(M-1)*KMAX2                                                   SAT17950
      AZTST=ABS(Z(I,KM))                                                 SAT17960
      IF(AZTST.GT.TZMAX(I,M))  TZMAX(I,M)=AZTST                          SAT17970
  201 CONTINUE                                                           SAT17980
      NCONV=1                                                            SAT17990
      IF(ITRMAX.EQ.1) GO TO 66                                           SAT18000
      DO 1 M=1,MNMAXO                                                    SAT18010
      I=1+(KMAX+2)*(M-1)                                                 SAT18020
      U1(M)=Z(1,I)                                                       SAT18030
      V1(M)=Z(2,I)                                                       SAT18040
      W1(M)=Z(3,I)                                                       SAT18050
      I1=I+1                                                             SAT18060
      U2(M)=Z(1,I1)                                                      SAT18070
      V2(M)=Z(2,I1)                                                      SAT18080
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    1 W2(M)=Z(3,I1)                                                     SAT18090
      IF(IBCINL.LT.0) GO TO 100                                         SAT18100
      CALL PHIBET(1,Z,IS,JS,ID,JD,PHIXB,PHITB)                          SAT18110
      DO 2 M=1,MNMAX                                                    SAT18120
      BX1(M)=BX3(M)                                                     SAT18130
      BT1(M)=BT3(M)                                                     SAT18140
      BXT1(M)=BXT3(M)                                                   SAT18150
    2 BE1(M)=BE3(M)                                                     SAT18160
      CALL TEAETA(1,Z,IS,JS,ID,JD)                                      SAT18170
      DO 3 M=1,MNMAX                                                    SAT18180
      EXX1(M)=EXX3(M)                                                   SAT18190
      ETT1(M)=ETT3(M)                                                   SAT18200
      ETX1(M)=ETX3(M)                                                   SAT18210
      EXT1(M)=EXT3(M)                                                   SAT18220
      EX1(M)=EX3(M)                                                     SAT18230
    3 ET1(M)=ET3(M)                                                     SAT18240
  102  CALL PHIBET(2,Z,IS,JS,ID,JD,PHIXB,PHITB)                         SAT18250
      DO 4 M=1,MNMAX                                                    SAT18260
      BX2(M)=BX3(M)                                                     SAT18270
      BT2(M)=BT3(M)                                                     SAT18280
      BXT2(M)=BXT3(M)                                                   SAT18290
    4 BE2(M)=BE3(M)                                                     SAT18300
      CALL TEAETA(2,Z,IS,JS,ID,JD)                                      SAT18310
      DO 5 M=1,MNMAX                                                    SAT18320
      EXX2(M)=EXX3(M)                                                   SAT18330
      ETT2(M)=ETT3(M)                                                   SAT18340
      ETX2(M)=ETX3(M)                                                   SAT18350
      EXT2(M)=EXT3(M)                                                   SAT18360
      EX2(M)=EX3(M)                                                     SAT18370
    5 ET2(M)=ET3(M)                                                     SAT18380
      CALL PHIBET(3,Z,IS,JS,ID,JD,PHIXB,PHITB)                          SAT18390
      CALL TEAETA(3,Z,IS,JS,ID,JD)                                      SAT18400
   66 CONTINUE                                                          SAT18410
      IF(IBCINL.LT.0) GO TO 20                                          SAT18420
      CALL BDB(1,B1,DB,D,CD)                                            SAT18430
      GAM1=GAM(1)                                                       SAT18440
      CALL TLOAD(1,Z)                                                   SAT18450
      DO 8 M=1,MNMAX                                                    SAT18460
      IF(ITRMAX.EQ.1) GO TO 67                                          SAT18470
      FFS(1,M)=-TT(M)*ALOAD+OSE*(BX1(M)+BE1(M)+NU*(BT1(M)+BE1(M)))*B1   SAT18480
      FFS(2,M)=OSE*(B1   *D1      *BXT1(M)+EX1(M)+ET1(M))               SAT18490
      FFS(3,M)=LAM2*GAM1*D1*MT(M)*ALOAD-(EXX1(M)+ETX1(M))*SOE           SAT18500
      GO TO 8                                                           SAT18510
   67 FFS(1,M)=-TT(M)*ALOAD                                             SAT18520
      FFS(2,M)=0.                                                       SAT18530
      FFS(3,M)=LAM2*GAM1*D1*MT(M)*ALOAD                                 SAT18540
    8 FFS(4,M)=0.                                                       SAT18550
      DO 9 I=1,4                                                        SAT18560
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    9 ELLS(I)=ALOAD*ELL(I)                                                SAT18570
      CALL FORCE(1,P,X,DEE,DST,Z,Z0,Z2,Z3)
   20 CALL FORCE(2,P,X,DEE,DST,Z,Z0,Z2,Z3)
      DO 10 K=3,KLL                                                     SAT18600
      KP=K+1                                                            SAT18610
      IF(ITRMAX.EQ.1) GO TO 10                                          SAT18620
      CALL UPDATE                                                       SAT18630
      CALL PHIBET(KP,Z,IS,JS,ID,JD,PHIXB,PHITB)                         SAT18640
      CALL TEAETA(KP,Z,IS,JS,ID,JD)                                     SAT18650
   10 CALL FORCE(K,P,X,DEE,DST,Z,Z0,Z2,Z3)
      IF(ITRMAX.NE.1) CALL UPDATE                                       SAT18670
      IF(IBCFNL.LT.0) GO TO 120                                         SAT18680
      IF(ITRMAX.EQ.1) GO TO 11                                          SAT18690
      CALL PHIBET(KMAX,Z,IS,JS,ID,JD,PHIXB,PHITB)                       SAT18700
      CALL TEAETA(KMAX,Z,IS,JS,ID,JD)                                   SAT18710
   11 CALL FORCE(KL,P,X,DEE,DST,Z,Z0,Z2,Z3)
      CALL FORCE(KMAX,P,X,DEE,DST,Z,Z0,Z2,Z3)
      DO 12 I=1,4                                                       SAT18740
   12 ELLS(I)=ALOAD*ELL(I)                                              SAT18750
      CALL BCB(KMAX,BL,DB,D,DD)                                         SAT18760
      GAML=GAM(KMAX)                                                    SAT18770
      FLS(4)=0.                                                         SAT18780
      CALL TLOAD(KMAX,Z)                                                SAT18790
      DO 14 M=1,MNMAX                                                   SAT18800
      IF(M.GT.1) ELLS(1)=0.0                                            SAT18810
      IF(ITRMAX.EQ.1) GO TO 68                                          SAT18820
      FLS(1)=-TT(M)*ALOAD+OSE*(BX3(M)+BE3(M)+NU*(ET3(M)+BE3(M)))*BL    SAT18830
      FLS(2)   =OSE*(BL*D1*BXT3(M)+EX3(M)+ET3(M))                       SAT18840
      FLS(3)=LAM2*GAML*D1*MT(M)*ALOAD-(EXX3(M)+ETX3(M))*SOE             SAT18850
      GO TO 69                                                          SAT18860
   68 FLS(1)=-TT(M)*ALOAD                                               SAT18870
      FLS(2)=0.                                                         SAT18880
      FLS(3)=LAM2*GAML*D1*MT(M)*ALOAD                                   SAT18890
   69 CONTINUE                                                          SAT18900
      IK=KL+KMAX*(M-1)                                                  SAT18910
      IJ=KMAX*M                                                         SAT18920
      L=M*KMAX2                                                         SAT18930
      DO 14 I=1,4                                                       SAT18940
      SUMZ=0.                                                           SAT18950
      DO 15 J=1,4                                                       SAT18960
C***********************************************************************SAT18970
C     THE FOLLOWING CARD CAUSES BOUNDARY CONS TO EXIST FOR MODE 'O' ONLYSAT18980
C***********************************************************************SAT18990
      IF (M.NE.1) ELLS(J)=0                                             SAT19000
   15 SUMZ=SUMZ+ZF1M(I,J,M)*ELLS(J)+ZF2M(I,J,M)*X(J,IJ)+ZF3M(I,J,M)*    SAT19010
     1X(J,IK)+ZF4M(I,J,M)*FLS(J)                                        SAT19020
   14 Z(I,L)=SUMZ                                                       SAT19030
      LS=1                                                              SAT19040
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150 DO 16 M=1,MNMAX                                                       SAT19050
    DO 16 L=LS,KMAX                                                       SAT19060
    K=KMAX2-L                                                             SAT19070
    KPX=K-1                                                               SAT19080
    KZ=K+1                                                                SAT19090
    IJ=KPX+(M-1)*KMAX                                                     SAT19100
    JK=KZ+(M-1)*KMAX2                                                     SAT19110
    KK=JK-1                                                               SAT19120
    DO 17 I=1,4                                                           SAT19130
    SUMZ=0.                                                               SAT19140
    DO 18 J=1,4                                                           SAT19150
 18 SUMZ=SUMZ-P(I,J,IJ)*Z(J,JK)                                           SAT19160
    SUMZ=SUMZ+X(I,IJ)                                                     SAT19170
    ASUMZ=ABS(SUMZ)                                                       SAT19180
    IF(ASUMZ.GT.1.E+15) ITR=ITRMAX                                        SAT19190
    IF(NCONV.NE.1 .OR. ASUMZ .LT. 1.E-05) GO TO 17                        SAT19200
    DELZ=ABS(Z(I,KK)-SUMZ)                                                SAT19210
    ZTEST=EPS*TZMAX(I,M)                                                  SAT19220
    IF(DELZ.GT.ZTEST) NCONV=0                                             SAT19230
 17 Z(I,KK)=SUMZ                                                          SAT19240
 16 CONTINUE                                                              SAT19250
    IF(IBCINL.LT.0) GO TO 30                                              SAT19260
    DO 25 M=1,MNMAX                                                       SAT19270
    CALL EFG(1,M,Z0,Z2,Z3)                                                SAT19280
    CALL ABC                                                              SAT19290
    IJ=2+(M-1)*KMAX2
    IJ1=IJ+1                                                              SAT19310
    IJ2=IJ-1                                                              SAT19320
    DO 21 I=1,4                                                           SAT19330
    SUMZ=0.                                                               SAT19340
    DO 22 J=1,4                                                           SAT19350
 22 SUMZ=SUMZ-A(I,J)*Z(J,IJ1)-BEE(I,J)*Z(J,IJ)                            SAT19360
 21 ZT(I)=SUMZ+GEES(I,M)                                                  SAT19370
    CALL MATINV(C,4,ZT,1,DETERM,IPIVOT,INDEX,4,ISCALE)                    SAT19380
    DO 23 I=1,4                                                           SAT19390
 23 Z(I,IJ2)=ZT(I)                                                        SAT19400
 25 CONTINUE                                                              SAT19410
 30 RETURN                                                                SAT19420
100 CALL INLPOL (Z,PHIXB,PHITB)                                           SAT19430
    DO 101 M=1,MNMAXC                                                     SAT19440
    U1(M)=U2(M)                                                           SAT19450
    V1(M)=V2(M)                                                           SAT19460
    W1(M)=W2(M)                                                           SAT19470
    IJ=3+KMAX2*(M-1)                                                      SAT19480
    U2(M)=Z(1,IJ)                                                         SAT19490
    V2(M)=Z(2,IJ)                                                         SAT19500
101 W2(M)=Z(3,IJ)                                                         SAT19510
    GO TO 102                                                             SAT19520
```

```
  120 IF(ITRMAX.NE.1) CALL FNLPOL (Z,PHIXB,PHITB)                     SAT19530
      CALL FORCE(KL   ,P,X,DEE,DST,Z,ZC,Z2,Z3)
      IF(M2.EQ.0) GO TO 122                                           SAT19550
      L=KL+(M2-1)*KMAX                                                SAT19560
      L1=KMAX1+(M2-1)*KMAX2                                           SAT19570
      DO 130 I=1,4                                                    SAT19580
      SUM=0.                                                          SAT19590
      DO 131 J=1,4                                                    SAT19600
  131 SUM=SUM+CL2(I,J)*X(J,L)                                         SAT19610
      ASUMZ=ABS(SUM)                                                  SAT19620
      IF(NCONV.NE.1 .OR. ASUMZ.LT.1.E-05) GO TO 130                   SAT19630
      DELZ=ABS(Z(I,L1)-SUM)                                           SAT19640
      ZTEST=EPS*TZMAX(I,M2)                                           SAT19650
      IF(DELZ.GT.ZTEST) NCONV=0                                       SAT19660
  130 Z(I,L1)=SUM                                                     SAT19670
  122 IF(M1.EQ.0) GO TO 123                                           SAT19680
      L=KL+(M1-1)*KMAX                                                SAT19690
      L1=KMAX1+(M1-1)*KMAX2                                           SAT19700
      DO 132 I=1,4                                                    SAT19710
      SUM=0.                                                          SAT19720
      DO 133 J=1,4                                                    SAT19730
  133 SUM=SUM+CL1(I,J)*X(J,L)                                         SAT19740
      ASUMZ=ABS(SUM)                                                  SAT19750
      IF(NCONV.NE.1 .OR. ASUMZ .LT. 1.E-05) GO TO 132                 SAT19760
      DELZ=ABS(Z(I,L1)-SUM)                                           SAT19770
      ZTEST=EPS*TZMAX(I,M1)                                           SAT19780
      IF(DELZ.GT.ZTEST) NCONV=0                                       SAT19790
  132 Z(I,L1)=SUM                                                     SAT19800
  123 IF(M0.EQ.0) GO TO 124                                           SAT19810
      L=KL+(M0-1)*KMAX                                                SAT19820
      L1=KMAX1+(M0-1)*KMAX2                                           SAT19830
      DO 134 I=1,4                                                    SAT19840
      SUM=0.                                                          SAT19850
      DO 135 J=1,4                                                    SAT19860
  135 SUM=SUM+CL0(I,J)*X(J,L)                                         SAT19870
      ASUMZ=ABS(SUM)                                                  SAT19880
      IF(NCONV.NE.1 .OR. ASUMZ.LT.1.E-06) GO TO 134                   SAT19890
      DELZ=ABS(Z(I,L1)-SUM)                                           SAT19900
      ZTEST=EPS*TZMAX(I,M0)                                           SAT19910
      IF(DELZ.GT.ZTEST) NCONV=0                                       SAT19920
  134 Z(I,L1)=SUM                                                     SAT19930
  124 LS=2                                                            SAT19940
      GO TO 150                                                       SAT19950
      END                                                             SAT19960
                                                                      SAT19970
      SUBROUTINE PLOT2(NTH)                                           SAT19980
C*********************************************************************SAT19990
C     THIS SUBROUTINE CALLS PLOTTING ROUTINES FOR APPROPRIATE (USER  *SAT20000
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C     SPECIFIED) OUTPUT QUANTITIES                                     *SAT20010
C***********************************************************************SAT20020
      IMPLICIT LOGICAL*1 ($)                                            SAT20030
      COMMON /IBL4/ KMAX,KL                                             SAT20040
      COMMON /BL19/ TH(36)                                              SAT20050
      COMMON /BLPLOT/ IRADII,IGAMMA,IOMEGS,IOMEGT,IDEOMS,IBSTIF,IDSTIF, SAT20060
     1                IBBSTF,IDDSTF,IPR,IPS,IPT,ITT,IMT,IDTT,IDMT,INS,  SAT20070
     2                INTH,INSTH,IQS,IMS,IMTH,IMSTH,IU,IV,IW,IPHIS,     SAT20080
     3                IPHIT,IPHI,$PLOTS,$MOCAL                          SAT20090
      COMMON /BLPLT1/ XRADII(200),YGAMMA(200),YOMEGS(200),YOMEGT(200),  SAT20100
     1                YDEOMS(200),YBSTIF(200),YDSTIF(200),YBBSTF(200),  SAT20110
     2                YDDSTF(200),YPR(200),YPS(200),YPT(200),YTT(200),  SAT20120
     3                YMT(200),YDTT(200),YDMT(200),YNS(200),YNTH(200),  SAT20130
     4                YNSTH(200),YQS(200),YMS(200),YMTH(200),YMSTH(200),SAT20140
     5                YL(200),YV(200),YW(200),YPHIS(200),YPHIT(200),    SAT20150
     6                YPHI(200),XSTATN(200)                             SAT20160
C***********************************************************************SAT20170
      NGKMAX=-KMAX                                                      SAT20180
      IF ($MOCAL) GO TO 121                                             SAT20190
      IF (INS.EQ.0) GO TO 4                                             SAT20200
      WRITE (6,1000)                                                    SAT20210
      IF (INS.GT.0) CALL PLOTIT (XSTATN,YNS,KMAX,0)                     SAT20220
      IF (INS.LT.0) CALL PLOTIT (XSTATN,YNS,NGKMAX,0)                   SAT20230
      WRITE (6,1001)TH(NTH)                                             SAT20240
    4 IF (INTH.EQ.0) GO TO 5                                            SAT20250
      WRITE (6,1000)                                                    SAT20260
      IF (INTH.GT.0) CALL PLOTIT (XSTATN,YNTH,KMAX,0)                   SAT20270
      IF (INTH.LT.0) CALL PLOTIT (XSTATN,YNTH,NGKMAX,0)                 SAT20280
      WRITE (6,1002) TH(NTH)                                            SAT20290
    5 IF (INSTH.EQ.0) GO TO 6                                           SAT20300
      WRITE (6,1000)                                                    SAT20310
      IF (INSTH.GT.0) CALL PLOTIT (XSTATN,YNSTH,KMAX,0)                 SAT20320
      IF (INSTH.LT.0) CALL PLOTIT (XSTATN,YNSTH,NGKMAX,0)               SAT20330
      WRITE (6,1003) TH(NTH)                                            SAT20340
    6 IF (IQS.EQ.0) GO TO 7                                             SAT20350
      WRITE (6,1000)                                                    SAT20360
      IF (IQS.GT.0) CALL PLOTIT (XSTATN,YQS,KMAX,0)                     SAT20370
      IF (IQS.LT.0) CALL PLOTIT (XSTATN,YQS,NGKMAX,0)                   SAT20380
      WRITE (6,1004) TH(NTH)                                            SAT20390
    7 IF (IMS.EQ.0) GO TO 8                                             SAT20400
      WRITE (6,1000)                                                    SAT20410
      IF (IMS.GT.0) CALL PLOTIT (XSTATN,YMS,KMAX,0)                     SAT20420
      IF (IMS.LT.0) CALL PLOTIT (XSTATN,YMS,NGKMAX,0)                   SAT20430
      WRITE (6,1005) TH(NTH)                                            SAT20440
    8 IF (IMTH.EQ.0) GO TO 9                                            SAT20450
      WRITE (6,1000)                                                    SAT20460
      IF (IMTH.GT.0) CALL PLOTIT (XSTATN,YMTH,KMAX,0)                   SAT20470
      IF (IMTH.LT.0) CALL PLOTIT (XSTATN,YMTH,NGKMAX,0)                 SAT20480
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      WRITE (6,1006) TH(NTH)                                            SAT20490
    5 IF (IMSTH.EQ.0) GO TO 1211                                        SAT20500
      WRITE (6,1000)                                                    SAT20510
      IF (IMSTH.GT.0) CALL PLOTIT (XSTATN,YMSTH,KMAX,0)                 SAT20520
      IF (IMSTH.LT.0) CALL PLOTIT (XSTATN,YMSTH,NGKMAX,0)               SAT20530
      WRITE (6,1007) TH(NTH)                                            SAT20540
 1211 IF (IU.EQ.0) GO TO 10                                             SAT20550
      WRITE (6,1000)                                                    SAT20560
      IF (IU.GT.0) CALL PLOTIT (XSTATN,YU,KMAX,0)                       SAT20570
      IF (IU.LT.0) CALL PLOTIT (XSTATN,YU,NGKMAX,0)                     SAT20580
      WRITE (6,1010) TH(NTH)                                            SAT20590
   10 IF (IV.EQ.0) GO TO 11                                             SAT20600
      WRITE (6,1000)                                                    SAT20610
      IF (IV.GT.0) CALL PLOTIT (XSTATN,YV,KMAX,0)                       SAT20620
      IF (IV.LT.0) CALL PLOTIT (XSTATN,YV,NGKMAX,0)                     SAT20630
      WRITE (6,1009) TH(NTH)                                            SAT20640
   11 IF (IW.EQ.0) GO TO 12                                             SAT20650
      WRITE (6,1000)                                                    SAT20660
      IF (IW.GT.0) CALL PLOTIT (XSTATN,YW,KMAX,0)                       SAT20670
      IF (IW.LT.0) CALL PLOTIT (XSTATN,YW,NGKMAX,0)                     SAT20680
      WRITE (6,1008) TH(NTH)                                            SAT20690
   12 IF (IPHIS.EQ.0) GO TO 13                                          SAT20700
      WRITE (6,1000)                                                    SAT20710
      IF (IPHIS.GT.0) CALL PLOTIT (XSTATN,YPHIS,KMAX,0)                 SAT20720
      IF (IPHIS.LT.0) CALL PLOTIT (XSTATN,YPHIS,NGKMAX,0)               SAT20730
      WRITE (6,1011) TH(NTH)                                            SAT20740
   13 IF (IPHIT.EQ.0) GO TO 14                                          SAT20750
      WRITE (6,1000)                                                    SAT20760
      IF (IPHIT.GT.0) CALL PLOTIT (XSTATN,YPHIT,KMAX,0)                 SAT20770
      IF (IPHIT.LT.0) CALL PLOTIT (XSTATN,YPHIT,NGKMAX,0)               SAT20780
      WRITE (6,1012) TH(NTH)                                            SAT20790
   14 IF (IPHI.EQ.0) GO TO 21                                           SAT20800
      WRITE (6,1000)                                                    SAT20810
      IF (IPHI .GT.0) CALL PLOTIT (XSTATN,YPHI ,KMAX,0)                 SAT20820
      IF (IPHI .LT.0) CALL PLOTIT (XSTATN,YPHI ,NGKMAX,0)               SAT20830
      WRITE (6,1013) TH(NTH)                                            SAT20840
   21 RETURN                                                            SAT20850
  121 IF (INS.EQ.0) GO TO 15                                            SAT20860
      WRITE (6,1000)                                                    SAT20870
      IF (INS.GT.0) CALL PLOTIT (XSTATN,YNS,KMAX,0)                     SAT20880
      IF (INS.LT.0) CALL PLOTIT (XSTATN,YNS,NGKMAX,0)                   SAT20890
      WRITE (6,2001)                                                    SAT20900
   15 IF (INTH.EQ.0) GO TO 16                                           SAT20910
      WRITE (6,1000)                                                    SAT20920
      IF (INTH.GT.0) CALL PLOTIT (XSTATN,YNTH,KMAX,0)                   SAT20930
      IF (INTH.LT.0) CALL PLOTIT (XSTATN,YNTH,NGKMAX,0)                 SAT20940
      WRITE (6,2002)                                                    SAT20950
   16 IF (INSTH.EQ.0) GO TO 17                                          SAT20960
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      WRITE (6,1000)                                                    SAT20970
      IF (INSTH.GT.0) CALL PLOTIT (XSTATN,YNSTH,KMAX,0)                 SAT20980
      IF (INSTH.LT.0) CALL PLOTIT (XSTATN,YNSTH,NGKMAX,0)               SAT20990
      WRITE (6,2003)                                                    SAT21000
   17 IF (IQS.EQ.0) GO TO 18                                            SAT21010
      WRITE (6,1000)                                                    SAT21020
      IF (IQS.GT.0) CALL PLOTIT (XSTATN,YQS,KMAX,0)                     SAT21030
      IF (IQS.LT.0) CALL PLOTIT (XSTATN,YQS,NGKMAX,0)                   SAT21040
      WRITE (6,2004)                                                    SAT21050
   18 IF (IMS.EQ.0) GO TO 19                                            SAT21060
      WRITE (6,1000)                                                    SAT21070
      IF (IMS.GT.0) CALL PLOTIT (XSTATN,YMS,KMAX,0)                     SAT21080
      IF (IMS.LT.0) CALL PLOTIT (XSTATN,YMS,NGKMAX,0)                   SAT21090
      WRITE (6,2005)                                                    SAT21100
   19 IF (IMTH.EQ.0) GO TO 22                                           SAT21110
      WRITE (6,1000)                                                    SAT21120
      IF (IMTH.GT.0) CALL PLOTIT (XSTATN,YMTH,KMAX,0)                   SAT21130
      IF (IMTH.LT.0) CALL PLOTIT (XSTATN,YMTH,NGKMAX,0)                 SAT21140
      WRITE (6,2006)                                                    SAT21150
   22 IF (IMSTH.EQ.0) GO TO 231                                         SAT21160
      WRITE (6,1000)                                                    SAT21170
      IF (IMSTH.GT.0) CALL PLOTIT (XSTATN,YMSTH,KMAX,0)                 SAT21180
      IF (IMSTH.LT.0) CALL PLOTIT (XSTATN,YMSTH,NGKMAX,0)               SAT21190
      WRITE (6,2007)                                                    SAT21200
  231 IF (IU.EQ.0) GO TO 23                                             SAT21210
      WRITE (6,1000)                                                    SAT21220
      IF (IU.GT.0) CALL PLOTIT (XSTATN,YU,KMAX,0)                       SAT21230
      IF (IU.LT.0) CALL PLOTIT (XSTATN,YU,NGKMAX,0)                     SAT21240
      WRITE (6,2010)                                                    SAT21250
   23 IF (IV.EQ.0) GO TO 24                                             SAT21260
      WRITE (6,1000)                                                    SAT21270
      IF (IV.GT.0) CALL PLOTIT (XSTATN,YV,KMAX,0)                       SAT21280
      IF (IV.LT.0) CALL PLOTIT (XSTATN,YV,NGKMAX,0)                     SAT21290
      WRITE (6,2009)                                                    SAT21300
   24 IF (IW.EQ.0) GO TO 25                                             SAT21310
      WRITE (6,1000)                                                    SAT21320
      IF (IW.GT.0) CALL PLOTIT (XSTATN,YW,KMAX,0)                       SAT21330
      IF (IW.LT.0) CALL PLOTIT (XSTATN,YW,NGKMAX,0)                     SAT21340
      WRITE (6,2008)                                                    SAT21350
   25 IF (IPHIS.EQ.0) GO TO 26                                          SAT21360
      WRITE (6,1000)                                                    SAT21370
      IF (IPHIS.GT.0) CALL PLOTIT (XSTATN,YPHIS,KMAX,0)                 SAT21380
      IF (IPHIS.LT.0) CALL PLOTIT (XSTATN,YPHIS,NGKMAX,0)               SAT21390
      WRITE (6,2011)                                                    SAT21400
   26 IF (IPHIT.EQ.0) GO TO 27                                          SAT21410
      WRITE (6,1000)                                                    SAT21420
      IF (IPHIT.GT.0) CALL PLOTIT (XSTATN,YPHIT,KMAX,0)                 SAT21430
      IF (IPHIT.LT.0) CALL PLOTIT (XSTATN,YPHIT,NGKMAX,0)               SAT21440
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      WRITE (6,2012)                                                    SAT21450
   27 IF (IPHI.EQ.0) GO TO 28                                           SAT21460
      WRITE (6,1000)                                                    SAT21470
      IF (IPHI .GT.0) CALL PLOTIT (XSTATN,YPHI ,KMAX,0)                 SAT21480
      IF (IPHI .LT.0) CALL PLOTIT (XSTATN,YPHI ,NGKMAX,0)               SAT21490
      WRITE (6,2013)                                                    SAT21500
   28 RETURN                                                            SAT21510
C***********************************************************************SAT21520
 1000 FORMAT ('1')                                                      SAT21530
 1001 FORMAT ('0',T10,'"S"-MEMBRANE FORCE VS STATN,  MERIDIAN AT THETA =SAT21540
     1 ',F10.5,'  RADIANS')                                             SAT21550
 1002 FORMAT ('0',T10,'"THETA"-MEMBRANE FORCE VS STATN,  MERIDIAN AT THESAT21560
     1TA = ',F10.5,'  RADIANS')                                         SAT21570
 1003 FORMAT ('0',T10,'"S-THETA" MEMBRANE FORCE VS STATN,  MERIDIAN AT TSAT21580
     1HETA = ',F10.5,'  RADIANS')                                       SAT21590
 1004 FORMAT ('0',T10,'EFFECTIVE SHEAR VS STATN,  MERIDIAN AT THETA = ',SAT21600
     1F10.5,'  RADIANS')                                                SAT21610
 1005 FORMAT ('0',T10,'"S"-BENDING MOMENT VS STATN,  MERIDIAN AT THETA =SAT21620
     1 ',F10.5,' RADIANS')                                              SAT21630
 1006 FORMAT ('0',T10,'THETA-BENDING MOMENT VS STATN,  MERIDIAN AT THETASAT21640
     1 = ',F10.5,'  RADIANS')                                           SAT21650
 1007 FORMAT ('0',T10,'S-THETA BENDING MOMENT VS STATN,  MERIDIAN AT THESAT21660
     1TA = ',F10.5,'  RADIANS')                                         SAT21670
 1008 FORMAT ('0',T10,'NORMAL DEFLECTION VS STATN,  MERIDIAN AT THETA = SAT21680
     1',F10.5,'  RADIANS')                                              SAT21690
 1009 FORMAT ('0',T10,'CIRCUMFERENTIAL DEFLECTION VS STATN,  MERIDIAN ATSAT21700
     1 THETA = ',F10.5,'  RADIANS')                                     SAT21710
 1010 FORMAT ('0',T10,'MERIDIONAL DEFLECTION VS STATN,  MERIDIAN AT THETSAT21720
     1A = ',F10.5,'  RADIANS')                                          SAT21730
 1011 FORMAT ('0',T10,'MERIDIONAL ROTATION VS STATN,  MERIDIAN AT THETA SAT21740
     1= ',F10.5,'  RADIANS')                                            SAT21750
 1012 FORMAT ('0',T10,'CIRCUMFERENTIAL ROTATION VS STATN,  MERIDIAN AT TSAT21760
     1HETA = ',F10.5,'  RADIANS')                                       SAT21770
 1013 FORMAT ('0',T10,'MERIDIC-CIRCUMFERENTIAL ROTATION VS STATN,  MERIDSAT21780
     1IAN AT THETA = ',F10.5,'  RADIANS')                               SAT21790
 2001 FORMAT ('0',T10,'"S"-MEMBRANE FORCE VS STATION')                  SAT21800
 2002 FORMAT ('0',T10,'"THETA"-MEMBRANE FORCE VS STATION')              SAT21810
 2003 FORMAT ('0',T10,'"S-THETA" MEMBRANE FORCE VS STATION')            SAT21820
 2004 FORMAT ('0',T10,'EFFECTIVE SHEAR VS STATION')                     SAT21830
 2005 FORMAT ('0',T10,'"S"-BENDING MOMENT VS STATION')                  SAT21840
 2006 FORMAT ('0',T10,'THETA-BENDING MOMENT VS STATION')                SAT21850
 2007 FORMAT ('0',T10,'S-THETA BENDING MOMENT VS STATION')              SAT21860
 2008 FORMAT ('0',T10,'NORMAL DEFLECTION VS STATION')                   SAT21870
 2009 FORMAT ('0',T10,'CIRCUMFERENTIAL DEFLECTION VS STATION')          SAT21880
 2010 FORMAT ('0',T10,'MERIDIONAL DEFLECTION VS STATION')               SAT21890
 2011 FORMAT ('0',T10,'MERIDIONAL ROTATION VS STATION')                 SAT21900
 2012 FORMAT ('0',T10,'CIRCUMFERENTIAL ROTATION VS STATION')            SAT21910
 2013 FORMAT ('0',T10,'MERIDIO-CIRCUMFERENTIAL ROTATION VS STATION')    SAT21920
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C***********************************************************************SAT21930
      END                                                               SAT21940
      SUBROUTINE PLOT1(I)                                               SAT21950
C***********************************************************************SAT21960
C     THIS SUBROUTINE CALLS PLOTTING ROUTINES FOR APPROPRIATE (USER    *SAT21970
C     SPECIFIED) INPUT QUANTITIES                                      *SAT21980
C***********************************************************************SAT21990
      IMPLICIT LOGICAL*1 ($)                                            SAT22000
      COMMON /IBL4/ KMAX,KL                                             SAT22010
      COMMON /BLPLOT/ IRADII,IGAMMA,IOMEGS,IOMEGT,IDEOMS,IBSTIF,IDSTIF, SAT22020
     1                IBBSTF,IDDSTF,IPR,IPS,IPT,ITT,IMT,IDTT,IDMT,INS,  SAT22030
     2                INTH,INSTH,IQS,IMS,IMTH,IMSTH,IU,IV,IW,IPHIS,     SAT22040
     3                IPHIT,IPHI,$PLOTS,$MODAL                          SAT22050
      COMMON /BLPLT1/ XRADII(200),YGAMMA(200),YOMEGS(200),YOMEGT(200),  SAT22060
     1                YDEOMS(200),YBSTIF(200),YDSTIF(200),YBBSTF(200),  SAT22070
     2                YDDSTF(200),YPR(200),YPS(200),YPT(200),YTT(200),  SAT22080
     3                YMT(200),YDTT(200),YDMT(200),YNS(200),YNTH(200),  SAT22090
     4                YNSTH(200),YQS(200),YMS(200),YMTH(200),YMSTH(200),SAT22100
     5                YU(200),YV(200),YW(200),YPHIS(200),YPHIT(200),    SAT22110
     6                YPHI(200),XSTATN(200)                             SAT22120
C***********************************************************************SAT22130
      NGKMAX=-KMAX                                                      SAT22140
      IF (I.GT.1) GO TO 1                                               SAT22150
      IF (IRADII.EQ.0) GO TO 2                                          SAT22160
      WRITE (6,1000)                                                    SAT22170
      CALL PLOTIT (XSTATN,XRADII,NGKMAX,0)                              SAT22180
      WRITE (6,1001)                                                    SAT22190
    2 IF (IGAMMA.EQ.0) GO TO 4                                          SAT22200
      WRITE (6,1000)                                                    SAT22210
      CALL PLOTIT (XSTATN,YGAMMA,NGKMAX,0)                              SAT22220
      WRITE (6,1002)                                                    SAT22230
    4 IF (IOMEGS.EQ.0) GO TO 5                                          SAT22240
      WRITE (6,1000)                                                    SAT22250
      CALL PLOTIT (XSTATN,YOMEGS,NGKMAX,0)                              SAT22260
      WRITE (6,1003)                                                    SAT22270
    5 IF (IOMEGT.EQ.0) GO TO 6                                          SAT22280
      WRITE (6,1000)                                                    SAT22290
      CALL PLOTIT (XSTATN,YOMEGT,NGKMAX,0)                              SAT22300
      WRITE (6,1004)                                                    SAT22310
    6 IF (IDEOMS.EQ.0) GO TO 7                                          SAT22320
      WRITE (6,1000)                                                    SAT22330
      CALL PLOTIT (XSTATN,YDEOMS,NGKMAX,0)                              SAT22340
      WRITE (6,1005)                                                    SAT22350
    7 IF (IBSTIF.EQ.0) GO TO 8                                          SAT22360
      WRITE (6,1000)                                                    SAT22370
      CALL PLOTIT (XSTATN,YBSTIF,NGKMAX,0)                              SAT22380
      WRITE (6,1006)                                                    SAT22390
    8 IF (IDSTIF.EQ.0) GO TO 9                                          SAT22400
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      WRITE (6,1000)                                                    SAT22410
      CALL PLOTIT (XSTATN,YDSTIF,NGKMAX,0)                              SAT22420
      WRITE (6,1007)                                                    SAT22430
    9 IF (IBBSTF.EQ.0) GO TO 10                                         SAT22440
      WRITE (6,1000)                                                    SAT22450
      CALL PLOTIT (XSTATN,YBBSTF,NGKMAX,0)                              SAT22460
      WRITE (6,1008)                                                    SAT22470
   10 IF (IDDSTF.EQ.0) GO TO 1                                          SAT22480
      WRITE (6,1000)                                                    SAT22490
      CALL PLOTIT (XSTATN,YDDSTF,NGKMAX,0)                              SAT22500
      WRITE (6,1009)                                                    SAT22510
    1 IF (IPR.EQ.0) GO TO 11                                            SAT22520
      WRITE (6,1000)                                                    SAT22530
      CALL PLOTIT (XSTATN,YPR,NGKMAX,0)                                 SAT22540
      WRITE (6,1010)                                                    SAT22550
   11 IF (IPS.EQ.0) GO TO 12                                            SAT22560
      WRITE (6,1000)                                                    SAT22570
      CALL PLOTIT (XSTATN,YPS,NGKMAX,0)                                 SAT22580
      WRITE (6,1011)                                                    SAT22590
   12 IF (IPT.EQ.0) GO TO 13                                            SAT22600
      WRITE (6,1000)                                                    SAT22610
      CALL PLOTIT (XSTATN,YPT,NGKMAX,0)                                 SAT22620
      WRITE (6,1012)                                                    SAT22630
   13 IF (ITT.EQ.0) GO TO 14                                            SAT22640
      WRITE (6,1000)                                                    SAT22650
      CALL PLOTIT (XSTATN,YTT,NGKMAX,0)                                 SAT22660
      WRITE (6,1013)                                                    SAT22670
   14 IF (IMT.EQ.0) GO TO 15                                            SAT22680
      WRITE (6,1000)                                                    SAT22690
      CALL PLOTIT (XSTATN,YMT,NGKMAX,0)                                 SAT22700
      WRITE (6,1014)                                                    SAT22710
   15 IF (IDTT.EQ.0) GO TO 16                                           SAT22720
      WRITE (6,1000)                                                    SAT22730
      CALL PLOTIT (XSTATN,YDTT,NGKMAX,0)                                SAT22740
      WRITE (6,1015)                                                    SAT22750
   16 IF (IDMT.EQ.0) GO TO 17                                           SAT22760
      WRITE (6,1000)                                                    SAT22770
      CALL PLOTIT (XSTATN,YDMT,NGKMAX,0)                                SAT22780
      WRITE (6,1016)                                                    SAT22790
      WRITE (6,1000)                                                    SAT22800
   17 RETURN                                                            SAT22810
C***********************************************************************SAT22820
 1000 FORMAT ('1')                                                      SAT22830
 1001 FORMAT ('0',T10,'RADIUS VS STATION')                              SAT22840
 1002 FORMAT ('0',T10,'GAMMA VS STATION')                               SAT22850
 1003 FORMAT ('0',T10,'OMEGA-S VS STATION')                             SAT22860
 1004 FORMAT ('0',T10,'OMEGA-THETA VS STATION')                         SAT22870
 1005 FORMAT ('0',T10,'DOMEGA-S VS STATION')                            SAT22880
```

```
1006  FORMAT ('0',T10,'B-STIFFNESS VS STATION')                         SAT22890
1007  FORMAT ('0',T10,'D-STIFFNESS VS STATION')                         SAT22900
1008  FORMAT ('0',T10,'DB-STIFFNESS VS STATION')                        SAT22910
1009  FORMAT ('0',T10,'DC-STIFFNESS VS STATION')                        SAT22920
1010  FORMAT ('0',T10,'NORMAL LOADING VS STATION')                      SAT22930
1011  FORMAT ('0',T10,'MERIDIO-TANGENTIAL LOADING VS STATION')          SAT22940
1012  FORMAT ('0',T10,'CIRCUMFERENTIO-TANGENTIAL LOADING VS STATION')   SAT22950
1013  FORMAT ('0',T10,'THERMAL LOADING VS STATION')                     SAT22960
1014  FORMAT ('0',T10,'THERMAL BENDING LOADING VS STATION')             SAT22970
1015  FORMAT ('0',T10,'DE-THERMAL LOADING VS STATION')                  SAT22980
1016  FORMAT ('0',T10,'DE-THERMAL-BENDING LOADING VS STATION')          SAT22990
C***********************************************************************SAT23000
      END                                                               SAT23010
      SUBROUTINE FLYNVY                                                 00000010
      WRITE (6,111)                                                     00000020
      WRITE (6,1)                                                       00000030
      WRITE (6,2)                                                       00000040
      WRITE (6,3)                                                       00000050
      WRITE (6,4)                                                       00000060
      WRITE (6,5)                                                       00000070
      WRITE (6,6)                                                       00000080
      WRITE (6,7)                                                       00000090
      WRITE (6,8)                                                       00000100
      WRITE (6,9)                                                       00000110
      WRITE (6,10)                                                      00000120
      WRITE (6,11)                                                      00000130
      WRITE (6,12)                                                      00000140
      WRITE (6,13)                                                      00000150
      WRITE (6,14)                                                      00000160
      WRITE (6,15)                                                      00000170
      WRITE (6,16)                                                      00000180
      WRITE (6,17)                                                      00000190
      WRITE (6,18)                                                      00000200
      WRITE (6,19)                                                      00000210
      WRITE (6,20)                                                      00000220
      WRITE (6,21)                                                      00000230
      WRITE (6,22)                                                      00000240
      WRITE (6,23)                                                      00000250
      WRITE (6,24)                                                      00000260
      WRITE (6,25)                                                      00000270
      WRITE (6,26)                                                      00000280
      WRITE (6,27)                                                      00000290
      WRITE (6,28)                                                      00000300
      WRITE (6,29)                                                      00000310
      WRITE (6,30)                                                      00000320
      WRITE (6,31)                                                      00000330
      WRITE (6,32)                                                      00000340
      WRITE (6,33)                                                      00000350
```

```
      WRITE (6,34)                                                      00000360
      WRITE (6,35)                                                      00000370
      WRITE (6,36)                                                      00000380
      WRITE (6,37)                                                      00000390
      WRITE (6,38)                                                      00000400
      WRITE (6,39)                                                      00000410
      WRITE (6,40)                                                      00000420
  111 FORMAT ('1')                                                      00000430
    1 FORMAT (' ',T11,'                                                 00000440
     1       XXX')                                                      00000450
    2 FORMAT (' ',T11,'                                                 00000460
     1      XXXXX')                                                     00000470
    3 FORMAT (' ',T11,'                                                 00000480
     1    XXX  XXX')                                                    00000490
    4 FORMAT (' ',T11,'                                                 00000500
     1    XXX  XXX')                                                    00000510
    5 FORMAT (' ',T11,'                                                 00000520
     1      X@XXX')                                                     00000530
    6 FORMAT (' ',T11,'XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX     00000540
     1XXXXXXX@XXXXXXXXXXX     XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX00000550
     2XX')                                                              00000560
    7 FORMAT (' ',T11,'   XXXXXXXCOXXXXXXXOOXXXXXXXXXOCXXXXXXXXXXCX     00000570
     1XXXXXXX@XXXXXXXXXXX      XOXXXXXXXXXXOOXXXXXXXOOXXXXXXXOCXXXXXXXX'00000580
     2)                                                                 00000590
    8 FORMAT (' ',T11,'       XXXXXXOOXXXXXXXOOXXXXXXXXOCXXXXXXCX       00000600
     1      @XXX                XCXXXXXXCOXXXXXXXXOCXXXXXXXXOOXXXXXX')  00000610
    9 FORMAT (' ',T11,'           XXXXCCXXXXXXXXCCXXXXXXXCCXXXCXX       00000620
     1     XXXXXXXXX            XXOXXXCCXXXXXXXXOCXXXXXXXCCXXXX')       00000630
   10 FORMAT (' ',T11,'               XXXXXXXXXXXOCXXXXXXXXCOXXXXXXXXXXX00000640
     1XXXXXXOCCOOOOXXXXXXXXXXXXXXXXXXOCXXXXXXXOCXXXXXXXXXXX')           00000650
   11 FORMAT (' ',T11,'                   XXXXXXXXXXXXOOXXXXXXOOXXXXXXXO00000660
     1CCCCCCOCCOOCCOOCOCCCOXXXXXXXCOXXXXXXCOXXXXXXXXXXX')               00000670
   12 FORMAT (' ',T11,'                       XXXXXXXXXOCXXXXXOOXXXXXXOC00000680
     1CCCCOCOCCCCCCCOCCCCCOXXXXXOCXXXXXXCCXXXXXXXXX')                   00000690
   13 FORMAT (' ',T11,'                             XXXXXXXCCXXXXOCXXXXO00000700
     1CCCCCCCCCCCCCCOCOCCOXXXXOOXXXXOCXXXXXXX')                         00000710
   14 FORMAT (' ',T11,'                                   XXXXOCXXXCOXXX00000720
     1CX X X X X X X X XCCXXOCXXXCOXXXX')                               00000730
   15 FORMAT (' ',T11,'                                       XXOXXXXOOX00000740
     1CC X X X X X X X CCXOOXXXXOXX')                                   00000750
   16 FORMAT (' ',T11,'                                       CCCCCXXXXX00000760
     1CC X X X X X X X CCXXXXXCOOOO')                                   00000770
   17 FORMAT (' ',T11,'                                        CCC      00000780
     1XCCX X X X X X XOOX      OOC')                                    00000790
   18 FORMAT (' ',T11,'                                         CCC     00000800
     1 XCC X X X X X OOX      OOO')                                     00000810
   19 FORMAT (' ',T11,'                                          OOC    00000820
     1  XCOX X X X XOOX      OOO')                                      00000830
```

AD-A035 911 NAVAL POSTGRADUATE SCHOOL MONTEREY CALIF F/G 20/11
STATIC AND DYNAMIC BUCKLING OF SHALLOW SPHERICAL SHELLS SUBJECT--ETC(U)
DEC 76 M D SHUTT

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2 OF 2
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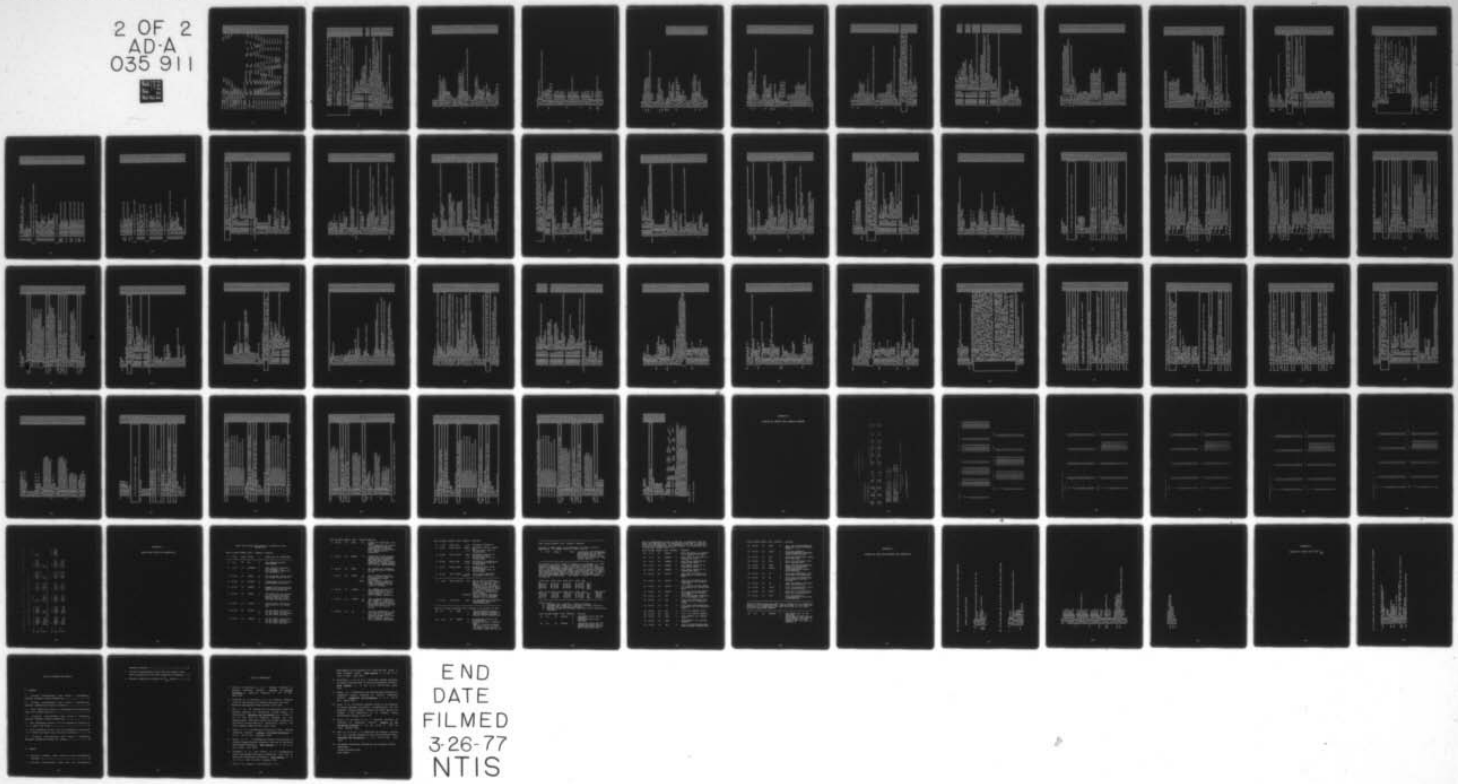

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```
   20 FORMAT (' ',T11,'                                           OCC   00000840
     1   XOO X X X OOX       OOO')                                      00000850
   21 FORMAT (' ',T11,'                                            CCCO 00000860
     1     XOC X OCX       OOOC')                                       00000870
   22 FORMAT (' ',T11,'                                             CCCC00000880
     1      XCOOCOX       OOOO')                                        00000890
   23 FORMAT (' ',T11,'                                               OO00000900
     1CCC  COCXCXOOO  COOOO')                                           00000910
   24 FORMAT (' ',T11,'                                                 00000920
     1 CCCCOCCCOCCCOOOO')                                               00000930
   25 FORMAT (' ',T11,'                                                 00000940
     1   COCCCCCCOOOO')                                                 00000950
   26 FORMAT (' ',T11,'                                                 00000960
     1     CCCCCCOO')                                                   00000970
   27 FORMAT (' ',T11,'                                                 00000980
     1        OOO')                                                     00000990
   28 FORMAT (' ',//////////)                                           00001000
   29 FORMAT (' ',T11,'     FFFFFFFFFFF  LLL       YYY         YYY      00001010
     1          NNN       NNN        A    VVV       VVV  YYY         YYY00001020
     2')                                                                00001030
   30 FORMAT (' ',T11,'     FFFFFFFFFFF  LLL        YYY       YYY       00001040
     1          NNNN      NNN       AAA   VVV       VVV   YYY       YYY'00001050
     2)                                                                 00001060
   31 FORMAT (' ',T11,'     FFF          LLL         YYY     YYY        00001070
     1          NNNNN     NNN      AAAAA   VVV     VVV     YYY     YYY')00001080
   32 FORMAT (' ',T11,'     FFF          LLL          YYY   YYY         00001090
     1          NNNNNN    NNN      AAAAA   VVV     VVV      YYY   YYY') 00001100
   33 FORMAT (' ',T11,'     FFF          LLL           YYY YYY          00001110
     1          NNNNNNN   NNN     AAA AAA   VVV   VVV        YYY YYY')  00001120
   34 FORMAT (' ',T11,'     FFFFFFFF     LLL            YYYYY           00001130
     1          NNN NNNN  NNN     AAA AAA   VVV   VVV         YYYYY')   00001140
   35 FORMAT (' ',T11,'     FFFFFFFF     LLL             YYY            00001150
     1          NNN  NNNN NNN    AAA   AAA   VVV  VVV          YYY')    00001160
   36 FORMAT (' ',T11,'     FFF          LLL             YYY            00001170
     1          NNN   NNNNNNN    AAAAAAAAA   VVV  VVV          YYY')    00001180
   37 FORMAT (' ',T11,'     FFF          LLL             YYY            00001190
     1          NNN    NNNNNN   AAAAAAAAAAA   VVVVV            YYY')    00001200
   38 FORMAT (' ',T11,'     FFF          LLL             YYY            00001210
     1          NNN     NNNNN   AAA     AAA   VVVVV            YYY')    00001220
   39 FORMAT (' ',T11,'     FFF          LLLLLLLLLLL     YYY            00001230
     1          NNN      NNNN  AAA       AAA   VVV             YYY')    00001240
   40 FORMAT (' ',T11,'     FFF          LLLLLLLLLLL     YYY            00001250
     1          NNN       NNN  AAA       AAA    V              YYY')    00001260
      RETURN                                                            00001270
      END                                                               00001280
      SUBROUTINE PMATRX (P.X,Z0,Z2,Z3,CEE,DST)                          00001290
C***********************************************************************00001300
C        THIS SUBROUTINE CALLS THE SUBRCUTINES FJ(K,MN), EFG(K,MN), ABC,00001310
```

```
C        AND PANDD(K,MN) TO SET UP THE P, P-BAR AND P-HAT MATRICES GIVEN00001320
C        BY EQUATIONS (30).                                            *00001330
C        INTERNALLY, MATRICES DL, DG AND DF ARE SET UP FOR THE CALCULA-*00001340
C        TION OF X(1) GIVEN BY EQUATION (31A), WHERE                   *00001350
C                                                                      *00001360
C        X(1) = DL*SMALL-L(1) + DG*SMALL-G(1) + DF*SMALL-F(1)          *00001370
C                                                                      *00001380
C        THE SPECIAL P MATRIX FOR A SHELL WITH AN INITIAL POLE IS ALSO *00001390
C        COMPUTED HERE.                                                *00001400
C        MATRICES ZF1M,ZF2M,ZF3M,ZF4M ARE SET UP FOR THE CALCULATION OF*00001410
C        Z(K+1) GIVEN BY EQUATION (31B), WHERE                         *00001420
C                                                                      *00001430
C        Z(K+1)=ZF1M*SMALL-L(K) + ZF2M*X(K) + ZF3M*X(K-1) + ZF4M*SMALL-F00001440
C                                                                      *00001450
C        IF THE SHELL HAS A FINAL POLE, THE MATRICES CL0,CL1,CL2 ARE   *00001460
C        PREPARED FOR THE CALCULATION OF Z(K)                          *00001470
C***********************************************************************00001480
      REAL JAY                                                          00001490
      DIMENSION P(4,4,1),DEE(4,4,1),DST(4,4,1),X(4,1),Z0(4,1),          00001500
     1Z2(4,1),Z3(4,1)                                                   00001510
      COMMON /IBL1/ MNMAX                                               00001520
      COMMON /IBL2/ N(99),MNINIT                                        00001530
      COMMON /IBL3/ M0,M1,M2,M3                                         00001540
      COMMON /IBL4/ KMAX,KL                                             00001550
      COMMON /IBL5/ IBCINL,IBCFNL                                       00001560
      COMMON /BL1/  A(4,4),BEE(4,4),C(4,4)                              00001570
      COMMON /BL4/  ZF1M(4,4,99),ZF2M(4,4,99),
     1              ZF3M(4,4,99),ZF4M(4,4,99)
      COMMON /BL13/ OMEG1(4,4),CAPL1(4,4),OMEGL(4,4),CAPLL(4,4),        00001600
     1              UNIT(4,4)                                           00001610
      COMMON /BL23/ JAY(4,4),H(4,4)                                     00001620
      COMMON /BL24/ DL(4,4,99),DG(4,4,99),DF(4,4,99)
      COMMON /BL25/ E(4,4),F(4,4),G(4,4)                                00001640
      DIMENSION PATA(4,4),PBTA(4,4),POTA(4,4),PJTA(4,4),DLL(4,4),PTR(4, 00001650
     14),DGG(4,4),ZF1(4,4),ZF2(4,4),ZFP0(4,4),ZFP1(4,4),ZFP2(4,4),IPIVO 00001660
     2T(4),INDEX(4,2),CL0(4,4),CL1(4,4),CL2(4,4),G1(4)                  00001670
      EQUIVALENCE (CL0(1),ZF1M(1)),(CL1(1),ZF2M(1)),(CL2(1),ZF3M(1)),   00001680
     1(ZFP0(1),PATA(1)),(ZFP1(1),PBTA(1)),(ZFP2(1),POTA(1))             00001690
     2,(ZF1(1),DLL(1)),(ZF2(1),PTR(1))                                  00001700
C***********************************************************************00001710
      IF(IBCINL.LT.0) GO TO 10                                          00001720
      DO 1 MN=MNINIT,MNMAX                                              00001730
      CALL HJ(1,MN)                                                     00001740
      CALL EFG(1,MN,Z0,Z2,Z3)                                           00001750
      CALL ABC                                                          00001760
      CALL MATINV(C,4,G1,0,DETERM,IPIVOT,INDEX,4,ISCALE)                00001770
      DO 3 I=1,4                                                        00001780
      DO 3 J=1,4                                                        00001790
```

```
      SUMA=0.
      SUMB=0.
      SUMC=0.
      SUMJ=0.
      DO 4 L=1,4
      SUMJ=SUMJ+OMEG1(I,L)*JAY(L,J)
      SUMA=SUMA+C(I,L)*A(L,J)
      SUMB=SUMB+C(I,L)*BEE(L,J)
    4 SUMC=SUMC+CMEG1(I,L)*H(L,J)
      FATA(I,J)=SUMA+UNIT(I,J)
      PBTA(I,J)=SUMB
      PCTA(I,J)=SUMC
    3 PJTA(I,J)=SUMJ
      DO 5 I=1,4
      DO 5 J=1,4
      SUMOB=0.
      SUMOA=0.
      SUMOC=0.
      DO 6 L=1,4
      SUMOB=SUMOB+POTA(I,L)*PBTA(L,J)
      SUMOA=SUMOA+POTA(I,L)*FATA(L,J)
    6 SUMOC=SUMOC+POTA(I,L)*C(L,J)
      DLL(I,J)=SUMOB+PJTA(I,J)+CAPL1(I,J)
      PTR(I,J)=SUMOA
    5 DGG(I,J)=SUMOC
      CALL MATINV(DLL,4,PTR,4,DETERM,IPIVOT,INDEX,4,ISCALE)
      DO 1 I=1,4
      DO 1 J=1,4
      SUMD=0.
      SUME=0.
      DO 7 L=1,4
      SUMD=SUMD+DLL(I,L)*DGG(L,J)
    7 SUME=SUME-DLL(I,L)*CMEG1(L,J)
      DL(I,J,MN)=DLL(I,J)
      DG(I,J,MN)=SUMD
      DF(I,J,MN)=SUME
      IJ=1+KMAX*(MN-1)
    1 P(I,J,IJ)=PTR(I,J)
      GO TO 20
   10 DO 11 MN=MNINIT,MNMAX
      NN=IABS(N(MN))
      IJ=1+KMAX*(MN-1)
      DO 14 I=1,4
      X(I,IJ)=0.
      DO 14 J=1,4
   14 P(I,J,IJ)=0.
      IF(NN.GT.3) GO TO 11
      IF(NN.GT.2) GO TO 90
```

```
C     IN FMATRX
      CALL EFG(2,MN,ZG,Z2,Z3)
      CALL ABC
      CALL MATINV(A,4,G1,0,DETERM,IPIVCT,INDEX,4,ISCALE)
      DO 901 II=1,4
      DO 901 JJ=1,4
      DL(II,JJ,MN)=0.
      DG(II,JJ,MN)=0.
  901 DF(II,JJ,MN)=0.
      IF(MN.GT.1) GO TO 12
      IF(MN.GT.0) GO TO 13
      MC=MN
      DL(1,1,MN)=1.
      DL(2,2,MN)=1.
      DL(3,3,MN)=-3.
      DL(4,4,MN)=-3.
      DG(3,3,MN)=4.
      DG(4,4,MN)=4.
      DF(3,3,MN)=-1.
      DF(4,4,MN)=-1.
      GO TO 902
   13 M1=MN
      DL(1,1,MN)=-3.
      DL(2,1,MN)=1.
      DL(2,2,MN)=1.
      IF(N(M1).LT.0)DL(2,2,MN)=-1.
      DL(3,3,MN)=1.
      DL(4,4,MN)=1.
      DG(1,1,MN)=4.
      DF(1,1,MN)=-1.
      GO TO 902
   12 M2=MN
      DL(1,1,MN)=1.
      DL(2,2,MN)=1.
      DL(3,3,MN)=1.
      DL(4,4,MN)=-3.
      DG(4,4,MN)=4.
      DF(4,4,MN)=-1.
  902 CONTINUE
      DO 903 II=1,4
      DO 903 JJ=1,4
      TTP=0.
      DO 904 L=1,4
  904 TTP=TTP+DF(II,L,MN)*A(L,JJ)
  903 CLO(II,JJ)=TTP
      DO 905 II=1,4
      DO 905 JJ=1,4
      TTP=0.
```

```
      TTQ=0.
      DO 906 L=1,4
      TTP=TTP+CLO(II,L)*C(L,JJ)
  906 TTQ=TTQ+CLO(II,L)*BEE(L,JJ)
      CL1(II,JJ)=DL(II,JJ,MN)-TTP
  905 CL2(II,JJ)=DG(II,JJ,MN)-TTQ
      CALL MATINV(CL1,4,G1,0,DETERM,IPIVOT,INDEX,4,ISCALE)
      DO 907 II=1,4
      DO 907 JJ=1,4
      TTP=0.
      TTQ=0.
      DO 908 L=1,4
      TTP=TTP+CL1(II,L)*CLO(L,JJ)
  908 TTQ=TTQ+CL1(II,L)*CL2(L,JJ)
      DL(II,JJ,MN)=-TTP
  907 P(II,JJ,IJ)=TTQ
      GO TO 11
   90 M3=MN
   11 CONTINUE                                                          00002430
   20 KLAST=KMAX                                                        00002440
      IF(IBCFNL.LT.0) KLAST=KL                                          00002450
      DO 23 K=2,KLAST                                                   00002460
      DO 23 MN=MNINIT,MNMAX                                             00002470
      CALL EFG(K,MN,Z0,Z2,Z3)                                           00002480
      CALL ABC                                                          00002490
   23 CALL PANDD(K,MN,P,CEE,DST,X)                                      00002500
      IF(IBCFNL.LT.0) GO TO 30                                          00002510
      DO 40 MN=MNINIT,MNMAX                                             00002520
      IKL=MN*KMAX-1                                                     00002530
      JKL=KMAX*MN                                                       00002540
      CALL FJ(KMAX,MN)                                                  00002550
      DO 41 I=1,4                                                       00002560
      DO 41 J=1,4                                                       00002570
      SUMO=0.                                                           00002580
      SUMP=0.                                                           00002590
      SUMJ=0.                                                           00002600
      DO 42 L=1,4                                                       00002610
      SUMO=SUMO+CMEGL(I,L)*H(L,J)                                       00002620
      SUMP=SUMP+P(I,L,IKL)*F(L,J,JKL)                                   00002630
   42 SUMJ=SUMJ+CMEGL(I,L)*JAY(L,J)                                     00002640
      PATA(I,J)=SUMO                                                    00002650
      PETA(I,J)=UNIT(I,J)-SUMP                                          00002660
   41 PJTA(I,J)=SUMJ+CAPLL(I,J)                                         00002670
      DO 43 I=1,4                                                       00002680
      DO 43 J=1,4                                                       00002690
      SUMCP=0.                                                          00002700
      SUMJP=0.                                                          00002710
      SUMCM=0.                                                          00002720
```

```
      DO 44 L=1,4                                                       00002730
      SUMOP=SUMOP+PATA(I,L)*PBTA(L,J)                                   00002740
      SUMJP=SUMJP+PJTA(I,L)*P(L,J,JKL)                                  00002750
   44 SUMOM=SUMOM-PATA(I,L)*P(L,J,IKL)                                  00002760
      ZF1(I,J)=SUMOP-SUMJP                                              00002770
   43 ZF2(I,J)=SUMOM-PJTA(I,J)                                          00002780
      CALL MATINV(ZF1,4,ZF2,4,DETERM,IPIVOT,INDEX,4,ISCALE)             00002790
      DO 45 I=1,4                                                       00002800
      DO 45 J=1,4                                                       00002810
      SZF3=0.                                                           00002820
      SZF4=0.                                                           00002830
      DO 46 L=1,4                                                       00002840
      SZF3=SZF3+ZF1(I,L)*PATA(L,J)                                      00002850
   46 SZF4=SZF4-ZF1(I,L)*OMEGL(L,J)                                     00002860
      ZF3M(I,J,MN)=SZF3                                                 00002870
      ZF4M(I,J,MN)=SZF4                                                 00002880
      ZF1M(I,J,MN)=ZF1(I,J)                                             00002890
   45 ZF2M(I,J,MN)=ZF2(I,J)                                             00002900
   40 CONTINUE                                                          00002910
      RETURN                                                            00002920
   30 DO 31 MN=MNINIT,MNMAX                                             00002930
      IKL=MN*KMAX-1                                                     00002940
      NN=N(MN)                                                          00002950
      NN=IABS(N(MN))                                                    00002960
      IF(NN    .GT.3) GO TO 31                                          00002970
      IF(NN.GT.2) GO TO 300                                             00002980
      IF(NN    .GT.1) GO TO 33                                          00002990
      IF(NN    .GT.0) GO TO 34                                          00003000
      MO=MN                                                             00003010
      DO 35 J=1,4                                                       00003020
      DO 35 I=1,4                                                       00003030
      CLO(I,J)=0.                                                       00003040
   35 ZFPO(I,J)=0.                                                      00003050
      ZFPO(1,1)=1.                                                      00003060
      ZFPO(2,2)=1.                                                      00003070
      ZFPO(3,1)=P(3,1,IKL)                                              00003080
      ZFPO(3,2)=P(3,2,IKL)                                              00003090
      ZFPO(3,3)=P(3,3,IKL)+1.                                           00003100
      ZFPO(3,4)=P(3,4,IKL)                                              00003110
      ZFPO(4,1)=P(4,1,IKL)                                              00003120
      ZFPO(4,2)=P(4,2,IKL)                                              00003130
      ZFPO(4,3)=P(4,3,IKL)                                              00003140
      ZFPO(4,4)=P(4,4,IKL)+1.                                           00003150
      CLO(3,3)=1.                                                       00003160
      CLO(4,4)=1.                                                       00003170
      CALL MATINV(ZFPO,4,CLO,4,DETERM,IPIVOT,INDEX,4,ISCALE)            00003180
      GO TO 31                                                          00003190
  300 M3=MN                                                             00003200
```

```
      GO TO 31
   34 M1=MN
      DO 60 J=1,4
      DO 60 I=1,4
      CL1(I,J)=0.
   60 ZFP1(I,J)=0.
      ZFP1(1,1)=P(1,1,IKL)+1.
      ZFP1(1,2)=P(1,2,IKL)
      ZFP1(1,3)=P(1,3,IKL)
      ZFP1(1,4)=P(1,4,IKL)
      ZFP1(2,1)=1.
      ZFP1(2,2)=-1.
      IF(N(MN).LT.0) ZFP1(2,2) = 1.
      ZFP1(3,3)=1.
      ZFP1(4,4)=1.
      CL1(1,1)=1.
      CALL MATINV(ZFP1,4,CL1,4,DETERM,IPIVOT,INDEX,4,ISCALE)
      GO TO 31
   33 M2=MN
      DO 70 J=1,4
      DO 70 I=1,4
      CL2(I,J)=0.
   70 ZFP2(I,J)=0.
      ZFP2(1,1)=1.
      ZFP2(2,2)=1.
      ZFP2(3,3)=1.
      ZFP2(4,1)=P(4,1,IKL)
      ZFP2(4,2)=P(4,2,IKL)
      ZFP2(4,3)=P(4,3,IKL)
      ZFP2(4,4)=P(4,4,IKL)+1.
      CL2(4,4)=1.
      CALL MATINV(ZFP2,4,CL2,4,DETERM,IPIVOT,INDEX,4,ISCALE)
   31 CONTINUE
      RETURN
      END
      SUBROUTINE FORCE (K,F,X,CEE,DST,Z,ZC,Z2,Z3)
C***********************************************************************
C        THIS SUBROUTINE COMPUTES THE GEE VECTOR IN EQUATION (28), AND *
C        THE X VECTOR IN EQUATION (29A) FOR A GIVEN MERIDIONAL STATION *
C        K.  THE VECTOR GEES IS THE NON-LINEAR VALUE OF GEE AT STA. 1. *
C***********************************************************************
      IMPLICIT LOGICAL*1 ($)
      REAL NU,MT,LAM2,MASS,MAS
      DIMENSION P(4,4,1),CEE(4,4,1),DST(4,4,1),Z(4,1),ZC(4,1),
     1Z2(4,1),Z3(4,1),X(4,1)
      COMMON /IBL1/ MNMAX
      COMMON /IBL2/ N(99),MNINIT
      COMMON /IBL4/ KMAX,KL
```

```
      COMMON /IBL5/ IBCINL,IBCFNL
      COMMON /IBL8/ LSTEP,ITR                                           00003690
      COMMON /IBL12/ KMAX1,KMAX2,NCONV                                  00003700
      COMMON /IBL13/ ITRMAX,LSMAX                                       00003710
      COMMON /BL3/   PR(99),PX(99),PT(99)                               00003720
      COMMON /BL4/   ZF1M(4,4,99),ZF2M(4,4,99),
     1               ZF3M(4,4,99),ZF4M(4,4,99)
      COMMON /BL5/   TT(99),MT(99),DT(99),DMT(99)                       00003750
      COMMON /BL6/   SOE,OSE,ALOAD                                      00003760
      COMMON /BL7/   D1,S1                                              00003770
      COMMON /BL8/   R(500),GAM(500),OMT(500)                           00003780
      COMMON /BL9/   FFS(4,99),EL1S(4),GEES(4,99)
      COMMON /BL11/  OMXI(500),PHEE,TO,T2                               00003800
      COMMON /BL12/  TDLI,TDEL                                          00003810
      COMMON /BL14/  LAM2,LSD1E,LSD1N                                   00003820
      COMMON /BL15/  NU,U1(99),V1(99),W1(99),V2(99),U2(99),W2(99),U3(99),00003830
     1               V3(99),W3(99)                                      00003840
      COMMON /BL17/  DEL                                                00003850
      COMMON /BL24/  DL(4,4,99),DG(4,4,99),DF(4,4,99)
      COMMON /BL27/  BX3(99),BT3(99),BXT3(99),BE3(99)                   00003870
      COMMON /BL28/  EXX3(99),ETT3(99),ETX3(99),EXT3(99),EX3(99),ET3(99) 00003880
      COMMON /BL29/  BX1(99),BT1(99),BXT1(99),BE1(99),BX2(99),BT2(99),  00003890
     1               BXT2(99),BE2(99)                                   00003900
      COMMON /BL30/  EXX1(99),ETT1(99),ETX1(99),EX1(99),ET1(99),EXX2(99),00003910
     1               ETT2(99),ETX2(99),EXT2(99),EX2(99),ET2(99)         00003920
      COMMON /BL31/  DELSC,EXT1(99)                                     00003930
      COMMON /BL100/ TEEO,$DYNMC                                        00003940
      COMMON /BL101/ DELSD                                              00003950
      COMMON /BL102/ DELOAD                                             00003960
      COMMON /BL103/ MASS(500)                                          00003970
      DIMENSION GEE(4)                                                  00003980
C*********************************************************************00003990
      FDIFF(A,B,C)=(-1.5*A+2.*B-.5*C)/DEL                               00004000
      RS=R(K)                                                           00004010
      RF=1./RS                                                          00004020
      GA=GAM(K)                                                         00004030
      CX=CMXI(K)                                                        00004040
      CT=CMT(K)                                                         00004050
      DL2=D1*LAM2                                                       00004060
      CALL BCB(K,BS,DBS,D,DD)                                           00004070
      CALL PLOAD(K,Z)                                                   00004080
      CALL TLOAD(K,Z)                                                   00004090
      MAS=MASS(K)                                                       00004100
      DO 4 M=1,MNMAX                                                    00004110
      I2=K+1+(M-1)*KMAX2                                                00004120
      IK=K+(M-1)*KMAX                                                   00004130
      IK1=IK-1                                                          00004140
      EN=N(M)                                                           00004150
```

```
      ENF=EN*RR                                                         00C04160
      EMT=MT(M)                                                         00004170
      GEE(1) =   (-PX(M)+DT(M)-DL2*GA*OX*EMT)*TCEL*ALCAD                00004180
     1   + MAS*(-5.*ZO(1,IZ  )+4.*Z2(1,IZ)-Z3(1,IZ))*TCEL/DELSD         00004190
      GEE(2) =   (-PT(M)-ENR*TT(M)-CL2*ENR*OT*EMT)*TCEL*ALCAC           00004200
     1   + MAS*(-5.*ZO(2,IZ  )+4.*Z2(2,IZ)-Z3(2,IZ))*TDEL/DELSD         00004210
      GEE(3) =   (-PR(M)-(CX+CT)*TT(M)-CL2*(GA*CMT(M)-(CX*CT-ENR**2)    00004220
     1*MT(M)))*TDEL*ALCAD                                               00004230
     1   + MAS*(-5.*ZO(3,IZ  )+4.*Z2(3,IZ)-Z3(3,IZ))*TDEL/DELSD         00004240
    1 GEE(4) =   MT(M)*TDEL*ALCAD                                       00004250
      IF(ITRMAX.EQ.1) GC TO 5C                                          00004260
      IF(K.GT.1) GC TO 6                                                00004270
      BX2T=BX1(M)                                                       00004280
      BT2T=BT1(M)                                                       00004290
      BXT2T=BXT1(M)                                                     00C04300
      BE2T=BE1(M)                                                       00004310
      EXX2T=EXX1(M)                                                     00004320
      ETT2T=ETT1(M)                                                     00004330
      ETX2T=ETX1(M)                                                     00004340
      EXT2T=EXT1(M)                                                     00C04350
      EX2T=EX1(M)                                                       00004360
      ET2T=ET1(M)                                                       00004370
      CBX= FDIFF(BX2T,BX2(M),BX3(M))                                    00004380
      CBT= FCIFF(BT2T,BT2(M),BT3(M))                                    00004390
      CEXT= FCIFF(BXT2T,BXT2(M),BXT3(M))                                00C04400
      CEE= FCIFF(BE2T,BE2(M),BE3(M))                                    00004410
      DET= FDIFF(ET2T,ET2(M),ET3(M))                                    00004420
      CEX= FCIFF(EX2T,EX2(M),EX3(M))                                    00C04430
      DEXX= FCIFF(EXX2T,EXX2(M),EXX3(M))                                00004440
      CETX= FCIFF(ETX2T,ETX2(M),ETX3(M))                                00004450
      GC TO 7                                                           00C04460
    6 IF(K.LT.KMAX) GO TC 8                                             00004470
      BX2T=BX3(M)                                                       00004480
      BT2T=BT3(M)                                                       0000449C
      BXT2T=BXT3(M)                                                     00004500
      BE2T=BE3(M)                                                       00004510
      EXX2T=EXX3(M)                                                     00004520
      ETT2T=ETT3(M)                                                     00004530
      ETX2T=ETX3(M)                                                     00004540
      EXT2T=EXT3(M)                                                     00004550
      EX2T=EX3(M)                                                       00004560
      ET2T=ET3(M)                                                       00C04570
      CEX=-FCIFF(BX2T,BX2(M),BX1(M))                                    00004580
      CET=-FCIFF(BT2T,BT2(M),BT1(M))                                    00004590
      CEXT=-FDIFF(BXT2T,BXT2(M),BXT1(M))                                00C04600
      CBE=-FDIFF(BE2T,BE2(M),BE1(M))                                    00004610
      CET=-FCIFF(ET2T,ET2(M),ET1(M))                                    00004620
      CEX=-FCIFF(EX2T,EX2(M),EX1(M))                                    00004630
```

```
      DEXX=-FDIFF(EXX2T,EXX2(M),EXX1(M))
      DETX=-FDIFF(ETX2T,ETX2(M),ETX1(M))
      GO TO 7
    8 DBX=TDLI*(BX3(M)-BX1(M))
      DBT=TDLI*(BT3(M)-BT1(M))
      DBE=TDLI*(BE3(M)-BE1(M))
      DBXT=TDLI*(BXT3(M)-BXT1(M))
      DET=TDLI*(ET3(M)-ET1(M))
      DEX=TDLI*(EX3(M)-EX1(M))
      DEXX=TDLI*(EXX3(M)-EXX1(M))
      DETX=TDLI*(ETX3(M)-ETX1(M))
      BX2T=BX2(M)
      BT2T=BT2(M)
      BXT2T=BXT2(M)
      BE2T=BE2(M)
      EXX2T=EXX2(M)
      ETT2T=ETT2(M)
      ETX2T=ETX2(M)
      EXT2T=EXT2(M)
      EX2T=EX2(M)
      ET2T=ET2(M)
    7 GEE(1)=GEE(1)-OSE*(BS*(DBX+DBE+GA*D1*(BX2T-ET2T)+NU*(DBT+DBE)
     1         +ENR*D1*BXT2T)+DBS*(BX2T+BE2T+NU*(BT2T+BE2T))-2.*CX*
     2              (EXX2T+ETX2T)-ENR*(EX2T+ET2T))*TDEL
      GEE(2)=GEE(2)+OSE*(BS*(ENR*(BT2T+BE2T+NU*(BX2T+BE2T))-D1*
     1      (DBXT+2.*GA*BXT2T))-D1*DBS*BXT2T+2.*CT*(ETT2T+EXT2T)
     2       -(DEX+DET))*TDEL
      GEE(3)=GEE(3)+OSE*(BS*((OX+NU*OT)*(BX2T+BE2T)+(OT+NU*OX)*
     1       (BT2T+BE2T))+2.*(GA*(EXX2T+ETX2T)+DEXX+DETX+ENR*
     2       (EXT2T+ETT2T)))*TDEL
   50 IF(K.GT.1) GO TO 10
      IF(M.GT.1) EL1S(1)=0.0
      DO 20 I=1,4
      GEES(I,M)=GEE(I)
      SUMX=0.
      DO 21 J=1,4
C***********************************************************************
C     FOLLOWING CARD CAUSES A SPECIFIED BOUNDARY CONDITION VALUE TO    *
C     EXISTS ONLY FOR MODE '0'                                          *
C***********************************************************************
      IF (M.NE.1) EL1S(J)=0.
   21 SUMX=SUMX+DL(I,J,M)*EL1S(J)+DG(I,J,M)*GEE(J)+DF(I,J,M)*FFS(J,M)
   20 X(I,IK)=SUMX
      GO TO 4
C     IN FORCE
   10 IF(K.NE.2.OR.(K.EQ.2.AND.IBCINL.GE.0)) GO TO 901
      DO 902 II=1,4
      SUMX=0.
```

```
      DO 903 L=1,4
  903 SUMX=SUMX+CL(II,L,M)*GEE(L)
  902 X(II,IK1)=SUMX
  901 CONTINUE
      DO 11 I=1,4
      SUMX=0.                                                           00005090
      DO 12 J=1,4                                                       00005100
   12 SUMX=SUMX+DEE(I,J,IK)*GEE(J)-DST(I,J,IK)*X(J,IK1)                 00005110
   11 X(I,IK)=SUMX                                                      00005120
    4 CONTINUE                                                          00005130
      RETURN                                                            00005140
      END                                                               00005150
      SUBROUTINE UPDATE                                                 00005160
C***********************************************************************00005170
C        THIS SUBROUTINE UPDATES THE STORAGE LOCATIONS OF THE BETA'S AND00005180
C        ETA'S.  IT IS CALLED IN SUBROUTINE XANDZ AFTER A MERIDIAN     *00005190
C        STATION CHANGE.                                               *00005200
C***********************************************************************00005210
      COMMON /IBL1/ MNMAX                                               00005220
      COMMON /BL27/ BX3(99),BT3(99),BXT3(99),BE3(99)                    00005230
      COMMON /BL28/ EXX3(99),ETT3(99),ETX3(99),EXT3(99),EX3(99),ET3(99) 00005240
      COMMON /BL29/ BX1(99),BT1(99),BXT1(99),BE1(99),BX2(99),BT2(99),   00005250
     1              BXT2(99),BE2(99)                                    00005260
      COMMON /BL30/ EXX1(99),ETT1(99),ETX1(99),EX1(99),ET1(99),EXX2(99),00005270
     1              ETT2(99),ETX2(99),EXT2(99),EX2(99),ET2(99)          00005280
      COMMON /BL31/ DELSQ,EXT1(99)                                      00005290
C***********************************************************************00005300
      DO 1 M=1,MNMAX                                                    00005310
      BX1(M)=BX2(M)                                                     00005320
      BT1(M)=BT2(M)                                                     00005330
      BXT1(M)=BXT2(M)                                                   00005340
      BE1(M)=BE2(M)                                                     00005350
      BX2(M)=BX3(M)                                                     00005360
      BT2(M)=BT3(M)                                                     00005370
      BXT2(M)=BXT3(M)                                                   00005380
      BE2(M)=BE3(M)                                                     00005390
      EXX1(M)=EXX2(M)                                                   00005400
      ETT1(M)=ETT2(M)                                                   00005410
      ETX1(M)=ETX2(M)                                                   00005420
      EXT1(M)=EXT2(M)                                                   00005430
      EX1(M)=EX2(M)                                                     00005440
      ET1(M)=ET2(M)                                                     00005450
      EXX2(M)=EXX3(M)                                                   00005460
      ETT2(M)=ETT3(M)                                                   00005470
      ETX2(M)=ETX3(M)                                                   00005480
      EXT2(M)=EXT3(M)                                                   00005490
      EX2(M)=EX3(M)                                                     00005500
    1 ET2(M)=ET3(M)                                                     00005510
```

```
      RETURN
      END
      SUBROUTINE MATINV(A,N,B,M,DETERM,IPIVOT,INDEX,NMAX,ISCALE)
C***********************************************************************
C        THIS SUBROUTINE SOLVES THE MATRIX EQUATION AX=B, WHERE A IS   *
C        A SQUARE COEFFICIENT MATRIX AND B IS A MATRIX OF CONSTANT VEC-*
C        TORS.                                                         *
C        A(INVERSE) IS ALSO OBTAINED AND THE DETERMINANT OF A IS AVAIL-*
C        ABLE.                                                         *
C        THE FOLLOWING MUST BE DIMENSIONED IN THE CALLING PROGRAM:     *
C        IPIVOT(N MAX), INDEX(N MAX,2), A(N MAX,N MAX), B(N MAX,N MAX) *
C        WHERE:                                                        *
C                   A = NAME OF 2-DIMENSIONAL ARRAY TO BE INVERTED     *
C                   N = ORDER OF A -  1<=N<=NMAX                       *
C                   B = NAME OF 2-DIMENSIONAL ARRAY TO BE MULTIPLIED   *
C                             BY A(INVERSE)                            *
C                   M = NUMBER OF COLUMN VECTORS IN B                  *
C                             NOTE: M = 0 SIGNALS INVERSION ONLY)      *
C                   IPIVOT = TEMPORARY STORAGE BLOCK                   *
C                   INDEX = TEMPORARY STORAGE BLOCK                    *
C                   NMAX = MAXIMUM ORDER OF A (AS DIMENSIONED IN THE   *
C                             CALLING PROGRAM)                         *
C                   DETERM= VALUE OF DETERMINANT AS GIVEN BELOW        *
C                   ISCALE = USED IN FORMULA BELOW                     *
C                                                                      *
C                   DETERMINANT(A) = (10**18)**ISCALE*(DETERM)         *
C                                                                      *
C                   A(INVERSE) IS STORED IN A                          *
C                   A(INVERSE)*B IS STORED IN B                        *
C***********************************************************************
      DIMENSION IPIVOT(N),A(NMAX,N),B(NMAX,M),INDEX(NMAX,2)
      EQUIVALENCE (IROW,JROW), (ICOLUM,JCOLUM), (AMAX, T, SWAP)
C***********************************************************************
C     INITIALIZATION
C
    5 ISCALE=0
    6 R1=10.0**18
    7 R2=1.0/R1
   10 DETERM=1.0
   15 DO 20 J=1,N
   20 IPIVOT(J)=0
   30 DO 550 I=1,N
C
C     SEARCH FOR PIVOT ELEMENT
C
   40 AMAX=0.0
   45 DO 105 J=1,N
   50 IF (IPIVOT(J)-1) 60, 105, 60
```

```
   60 DO 100 K=1,N                                                      00006000
   70 IF (IPIVOT(K)-1) 80, 100, 740                                     00006010
   80 IF (ABS(AMAX)-ABS(A(J,K)))85,100,100                              00006020
   85 IROW=J                                                            00006030
   90 ICOLUM=K                                                          00006040
   95 AMAX=A(J,K)                                                       00006050
  100 CONTINUE                                                          00006060
  105 CONTINUE                                                          00006070
  110 IPIVOT(ICOLUM)=IPIVOT(ICOLUM)+1                                   00006080
C                                                                       00006090
C       INTERCHANGE ROWS TO PUT PIVOT ELEMENT ON DIAGONAL               00006100
C                                                                       00006110
  130 IF (IROW-ICOLUM) 140, 260, 140                                    00006120
  140 DETERM=-DETERM                                                    00006130
  150 DO 200 L=1,N                                                      00006140
  160 SWAP=A(IROW,L)                                                    00006150
  170 A(IROW,L)=A(ICOLUM,L)                                             00006160
  200 A(ICOLUM,L)=SWAP                                                  00006170
  205 IF(M) 260, 260, 210                                               00006180
  210 DO 250 L=1, M                                                     00006190
  220 SWAP=B(IROW,L)                                                    00006200
  230 B(IROW,L)=B(ICOLUM,L)                                             00006210
  250 B(ICOLUM,L)=SWAP                                                  00006220
  260 INDEX(I,1)=IROW                                                   00006230
  270 INDEX(I,2)=ICOLUM                                                 00006240
  310 PIVOT=A(ICOLUM,ICOLUM)                                            00006250
C                                                                       00006260
C       SCALE THE DETERMINANT                                           00006270
C                                                                       00006280
 1000 PIVOTI=PIVOT                                                      00006290
 1005 IF(ABS(DETERM)-R1)1030,1010,1010                                  00006300
 1010 DETERM=DETERM/R1                                                  00006310
      ISCALE=ISCALE+1                                                   00006320
      IF(ABS(DETERM)-R1)1060,1020,1020                                  00006330
 1020 DETERM=DETERM/R1                                                  00006340
      ISCALE=ISCALE+1                                                   00006350
      GO TO 1060                                                        00006360
 1030 IF(ABS(DETERM)-R2)1040,1040,1060                                  00006370
 1040 DETERM=DETERM*R1                                                  00006380
      ISCALE=ISCALE-1                                                   00006390
      IF(ABS(DETERM)-R2)1050,1050,1060                                  00006400
 1050 DETERM=DETERM*R1                                                  00006410
      ISCALE=ISCALE-1                                                   00006420
 1060 IF(ABS(PIVOTI)-R1)1090,1070,1070                                  00006430
 1070 PIVOTI=PIVOTI/R1                                                  00006440
      ISCALE=ISCALE+1                                                   00006450
      IF(ABS(PIVOTI)-R1)320,1080,1080                                   00006460
 1080 PIVOTI=PIVOTI/R1                                                  00006470
```

```
      ISCALE=ISCALE+1
      GO TO 320
 1990 IF(ABS(PIVOTI)-R2)2000,2000,320
 2000 PIVOTI=PIVOTI*R1
      ISCALE=ISCALE-1
      IF(ABS(PIVOTI)-R2)2010,2010,320
 2010 PIVOTI=PIVOTI*R1
      ISCALE=ISCALE-1
  320 DETERM=DETERM*PIVOTI
C
C     DIVIDE PIVOT ROW BY PIVOT ELEMENT
C
  330 A(ICOLUM,ICOLUM)=1.0
  340 DO 350 L=1,N
  350 A(ICOLUM,L)=A(ICOLUM,L)/PIVOT
  355 IF(M) 380, 380, 360
  360 DO 370 L=1,M
  370 B(ICOLUM,L)=B(ICOLUM,L)/PIVOT
C
C     REDUCE NON-PIVOT ROWS
C
  380 DO 550 L1=1,N
  390 IF(L1-ICOLUM) 400, 550, 400
  400 T=A(L1,ICOLUM)
  420 A(L1,ICOLUM)=0.0
  430 DO 450 L=1,N
  450 A(L1,L)=A(L1,L)-A(ICOLUM,L)*T
  455 IF(M) 550, 550, 460
  460 DO 500 L=1,M
  500 B(L1,L)=B(L1,L)-B(ICOLUM,L)*T
  550 CONTINUE
C
C     INTERCHANGE COLUMNS
C
  600 DO 710 I=1,N
  610 L=N+1-I
  620 IF (INDEX(L,1)-INDEX(L,2)) 630, 710, 630
  630 JROW=INDEX(L,1)
  640 JCOLUM=INDEX(L,2)
  650 DO 705 K=1,N
  660 SWAP=A(K,JROW)
  670 A(K,JROW)=A(K,JCOLUM)
  700 A(K,JCOLUM)=SWAP
  705 CONTINUE
  710 CONTINUE
  740 RETURN
      END
      SUBROUTINE INLPOL (Z,PHIXB,PHITB)
```

```
C***********************************************************************
C        THIS SUBROUTINE COMPUTES THE NON-LINEAR TERMS BETA-SUB S,     *
C        -SUB THETA, -SUB S-THETA, ETA-SUB S-S AND -SUB THETA-S AT AN  *
C        INITIAL POLE.                                                 *
C***********************************************************************
      DIMENSION Z(4,1),PHIXB(1),PHITB(1)
      COMMON /IBL1/ MNMAX
      COMMON /IBL3/ MO,M1,M2,M3
      COMMON /IBL12/ KMAX1,KMAX2,NCONV
      COMMON /IBL13/ ITRMAX,LSMAX
     3/IBLJ/ JUMP
      COMMON /BL5/  TT(99),EMT(99),DT(99),DMT(99)
      COMMON /BL6/  SOE,CSE,ALOAD
      COMMON /BL7/  D1,S1
      COMMON /BL11/ OMXI(200),PHEE,TO,T2
      COMMON /BL11A/ PHEN,T2N
      COMMON /BL17/ DEL
      COMMON /BL29/ BX1(99),BT1(99),BXT1(99),BE1(99),BX2(99),BT2(99),
     1              BXT2(99),BE2(99)
      COMMON /BL30/ EXX1(99),ETT1(99),ETX1(99),EX1(99),ET1(99),EXX2(99),
     1              ETT2(99),ETX2(99),EXT2(99),EX2(99),ET2(99)
      COMMON /BL31/ DELSQ,EXT1(99)
C***********************************************************************
      DO 1 MN=1,MNMAX
      BX1 (MN)=0.
      BT1 (MN)=0.
      BXT1(MN)=0.
      BE1 (MN)=0.
      EX1 (MN)=0.
      ET1 (MN)=0.
      ETX1(MN)=0.
    1 EXX1(MN)=0.
      IF(M1.EQ.0) RETURN
      I2=2+(M1-1)*KMAX2
      I3=I2+1
      I4=I3+1
      IF(JUMP.EQ.2) GO TO 1000
      PHEE=(1.5*Z(3,I2)-2.*Z(3,I3)+.5*Z(3,I4))/DEL+OMXI(1)*Z(1,I2)
      BET=.5*PHEE**2
      IF(ITRMAX.EQ.1) BET=0.
      T2=0.
      IF(M2.EQ.0) GO TO 2
      CALL BDB(1,B,DB,D,DD)
      I2=2+(M2-1)*KMAX2
      I3=I2+1
      I4=I3+1
      T2=B*D1*((-1.5*Z(1,I2)+2.*Z(1,I3)-.5*Z(1,I4))/DEL+.5*SOE*BET)
      C1=.5*PHEE*T2
```

```
      BX1(M2)=BET
      BT1(M2)=-BET
      BXT1(M2)=-BET
      ETX1(M1)=Q1
      IF(M3.EQ.0) GO TO 2
      EXX1(M3)=Q1
      ETX1(M3)=-Q1
    2 TC=0.
      IF(MO.EQ.0) GO TO 3
      EX1(MO)=BET
      BT1(MO)=BET
      CALL BDE(1,B,DB,D,CC)
      CALL TLCAD(1,Z)
      I2=2+(MO-1)*KMAX2
      I3=I2+1
      I4=I3+1
      TC=B*S1*((-1.5*Z(1,I2)+2.*Z(1,I3)-.5*Z(1,I4))/DEL+CMXI(1)*Z(3,I2)
     1+.5*SOE*BET)-TT(MO)*ALCAD
    3 EXX1(M1)=PHEE*(TO+.5*T2)
      RETURN
 1000 CONTINUE
      PHEE=(1.5*Z(3,I2)-2.*Z(3,I3)+.5*Z(3,I4))/DEL+CMXI(1)*Z(1,I2)
      T2=C.
      IF(M2.EQ.0) GO TO 1002
      CALL BDE(1,B,DB,D,CC)
      I2=2+(M2-1)*KMAX2
      I3=I2+1
      I4=I3+1
      PHX1=PHIXB(KMAX+1)
      PHX2=PHIXB(2*KMAX+1)
      PHEN=(1.5*Z(3,I2-KMAX2)-2.*Z(3,I3-KMAX2)+.5*Z(3,I4-KMAX2))/DEL+
     1CMXI(1)*Z(1,I2-KMAX2)
      BX1(M2)=.5*(PHEE*(PHEE+2.*PHX1)-PHEN*(PHEN+2.*PHX2))
      IF(ITRMAX.EQ.1) BX1(M2)=0.
      BT1(M2)=-BX1(M2)
      BXT1(M2)=-BX1(M2)
      T2=B*D1*((-1.5*Z(1,I2)+2.*Z(1,I3)-.5*Z(1,I4))/DEL+.5*SOE*BX1(M2))
      M2L=M2-1
      BX1(M2L)=PHEE*(PHEN+PHX2)+PHX1*PHEN
      IF(ITRMAX.EQ.1) BX1(M2L)=0.
      BT1(M2L)=-BX1(M2L)
      BXT1(M2L)=BX1(M2L)
      T2N=B*D1*((-1.5*Z(1,I2-KMAX2)+2.*Z(1,I3-KMAX2)-.5*Z(1,I4-KMAX2))
     1  /DEL+.5*SOE*BX1(M2L))
 1002 TC=C.
      IF(MO.EQ.0) GO TO 1003
      BX1(MO)=.5*(PHEE*(PHEE+2.*PHX1)+PHEN*(PHEN+2.*PHX2))
      IF(ITRMAX.EQ.1) BX1(MO)=0.
```

```
      BT1(MO)=BX1(MO)                                                   00007920
      CALL BCB(1,B,DB,D,DC)                                             00007930
      CALL TLOAD(1,Z)                                                   00007940
      I2=2+(MC-1)*KMAX2                                                 00007950
      I3=I2+1                                                           00007960
      I4=I3+1                                                           00007970
      TC=B*S1*((-1.5*Z(1,I2)+2.*Z(1,I3)-.5*Z(1,I4))/DEL+CMXI(1)*Z(3,I2) 00007980
     1+.5*SOE*BX1(MO))-TT(MO)*ALOAD                                     00007990
 1003 IF(ITRMAX.EQ.1) GO TO 1001                                        00008000
      PHSS=PHEE+PHX1                                                    00008010
      PHSP=PHEN+PHX2                                                    00008020
      M1L=M1-1                                                          00008030
      EXX1(M1)=PHSS*T0+.5*(PHSS*T2+PHSP*T2N)                            00008040
      EXX1(M1L)=PHSP*T0-.5*(PHSP*T2-PHSS*T2N)                           00008050
      ETX1(M1)=.5*(PHSS*T2+PHSP*T2N)                                    00008060
      ETX1(M1L)=.5*(-PHSP*T2+PHSS*T2N)                                  00008070
      IF(M3.EQ.0) GO TO 1001                                            00008080
      M3L=M3-1                                                          00008090
      EXX1(M3)=.5*(PHSS*T2-PHSP*T2N)                                    00008100
      EXX1(M3L)=.5*(PHSS*T2N+PHSP*T2)                                   00008110
      ETX1(M3)=.5*(-PHSS*T2+PHSP*T2)                                    00008120
      ETX1(M3L)=.5*(-PHSP*T2-PHSS*T2N)                                  00008130
 1001 CONTINUE                                                          00008140
      RETURN                                                            00008150
      END                                                               00008160
      SUBROUTINE ABC                                                    00008170
C***********************************************************************00008180
C        THIS SUBROUTINE COMPUTES THE ELEMENTS OF THE A, BEE, AND C    *00008190
C        MATRICES.                                                     *00008200
C***********************************************************************00008210
      COMMON /BL1/  A(4,4),BEE(4,4),C(4,4)                              00008220
      COMMON /BL12/ TDLI,TDEL                                           00008230
      COMMON /BL17/ DEL                                                 00008240
      COMMON /BL25/ E(4,4),F(4,4),G(4,4)                                00008250
C***********************************************************************00008260
      D2=2./DEL                                                         00008270
      DO 1 I=1,4                                                        00008280
      DO 1 J=1,4                                                        00008290
      DEIJ=D2*E(I,J)                                                    00008300
      FIJ=F(I,J)                                                        00008310
      BEE(I,J)=-2.*DEIJ+TDEL*G(I,J)                                     00008320
      C(I,J)=DEIJ-FIJ                                                   00008330
    1 A(I,J)=DEIJ+FIJ                                                   00008340
      RETURN                                                            00008350
      END                                                               00008360
      SUBROUTINE PANDD(K,MN,P,DEE,DST,X)                                00008370
C***********************************************************************00008380
C        THIS SUBROUTINE COMPUTES THE ELEMENTS OF THE P, P-BAR, AND    *00008390
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C        P-HAT MATRICES FOR EACH MEDICIAN STATION K AND FOURIER MODE MN*00008400
C        THESE MATRICES ARE COMPUTED AND SAVED BECAUSE THEY DO NOT     *00008410
C        CHANGE DURING EITHER THE ITERATION PROCEDURE OR THE LOAD INCRE-00008420
C        MENT PROCEDURE - AS THEY ARE A FUNCTION OF THE SHELL'S INITIAL*00008430
C        GEOMETRY AND STIFFNESS.                                       *00008440
C**********************************************************************00008450
      DIMENSION P(4,4,1),DEE(4,4,1),DST(4,4,1),X(4,1)                   00008460
      COMMON /IBL4/ KMAX,KL                                             00008470
      COMMON /BL1/  A(4,4),BEE(4,4),C(4,4)                              00008480
      COMMON /BL4/  ZF1M(4,4,99),ZF2M(4,4,99),
     1              ZF3M(4,4,99),ZF4M(4,4,99)
      DIMENSION TM(4,4),IPIVOT(4),INDEX(4,2),X2(4)                      00008510
C**********************************************************************00008520
      IKL=K+KMAX*(MN-1)                                                 00008530
      KLI=IKL-1                                                         00008540
      DO 1 I=1,4                                                        00008550
      DO 1 J=1,4                                                        00008560
      SUM=0.                                                            00008570
      DO 2 L=1,4                                                        00008580
    2 SUM=SUM+C(I,L)*P(L,J,KLI)                                         00008590
    1 TM(I,J)=BEE(I,J)-SUM                                              00008600
      CALL MATINV(TM,4,X2,0,DETERM,IPIVOT,INDEX,4,ISCALE)               00008610
      DO 5 I=1,4                                                        00008620
      DO 5 J=1,4                                                        00008630
      SUMA=0.                                                           00008640
      SUMC=0.                                                           00008650
      DO 6 L=1,4                                                        00008660
      SUMA=SUMA+TM(I,L)*A(L,J)                                          00008670
    6 SUMC=SUMC+TM(I,L)*C(L,J)                                          00008680
      P(I,J,IKL)=SUMA                                                   00008690
      DEE(I,J,IKL)=TM(I,J)                                              00008700
    5 DST(I,J,IKL)=SUMC                                                 00008710
      RETURN                                                            00008720
      END                                                               00008730
      SUBROUTINE FNLPOL (Z,PHIXB,PHITB)                                 00008740
C**********************************************************************00008750
C        THIS SUBROUTINE COMPUTES THE NON-LINEAR TERMS BETA-SUB S,     *00008760
C        -SUB THETA, -SUB S-THETA, ETA-SUB S-S, AND -SUB THETA-S AT A  *00008770
C        FINAL POLE.                                                   *00008780
C**********************************************************************00008790
      DIMENSION Z(4,1),PHIXB(1),PHITB(1)                                00008800
      COMMON /IBL1/ MNMAX                                               00008810
      COMMON /IBL3/ MO,M1,M2,M3                                         00008820
      COMMON /IBL4/ KMAX,KL                                             00008830
      COMMON /IBL12/ KMAX1,KMAX2,NCONV                                  00008840
      COMMON /IBL13/ ITRMAX,LSMAX                                       00008850
      COMMON /IBLJ/ JUMP                                                00008860
      COMMON /BL5/  TT(99),EMT(99),DT(99),DMT(99)                       00008870
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      COMMON /BL6/  SOE,CSE,ALOAD                                       00008880
      COMMON /BL7/  D1,S1                                               00008890
      COMMON /BL11/ OMXI(500),PHEE,TO,T2                                00008900
      COMMON /BL11A/ PHEN,T2N                                           00008910
      COMMON /BL17/ DEL                                                 00008920
      COMMON /BL27/ BX3(99),BT3(99),BXT3(99),BE3(99)                    00008930
      COMMON /BL28/ EXX3(99),ETT3(99),ETX3(99),EXT3(99),EX3(99),ET3(99) 00008940
C***********************************************************************00008950
      DO 1 MN=1,MNMAX                                                   00008960
      BX3 (MN)=0.                                                       00008970
      BT3 (MN)=0.                                                       00008980
      BXT3(MN)=0.                                                       00008990
      BE3 (MN)=0.                                                       00009000
      EX3 (MN)=0.                                                       00009010
      ET3 (MN)=0.                                                       00009020
      ETX3(MN)=0.                                                       00009030
    1 EXX3(MN)=0.                                                       00009040
      CALL BCB(KMAX,B,DB,D,DB)                                          00009050
      IF(M1.EQ.0) RETURN                                                00009060
      KM=KMAX1+(M1-1)*KMAX2                                             00009070
      KM1=KM-1                                                          00009080
      KM2=KM-2                                                          00009090
      PHEE=-(1.5*Z(3,KM)-2.*Z(3,KM1)+.5*Z(3,KM2))/DEL+OMXI(KMAX)*Z(1,KM)00009100
      IF(JUMP.EQ.2) GO TO 1000                                          00009110
      BET=.5*PHEE**2                                                    00009120
      IF(ITRMAX.EQ.1) BET=0.                                            00009130
      T2=0.                                                             00009140
      IF(M2.EQ.0) GO TO 2                                               00009150
      KM=KMAX1+(M2-1)*KMAX2                                             00009160
      KM1=KM-1                                                          00009170
      KM2=KM-2                                                          00009180
      T2=B*D1*((1.5*Z(1,KM)-2.*Z(1,KM1)+.5*Z(1,KM2))/DEL+.5*SCE*BET)    00009190
      Q1=.5*PHEE*T2                                                     00009200
      BX3(M2)=BET                                                       00009210
      BT3(M2)=-BET                                                      00009220
      BXT3(M2)= BET                                                     00009230
      ETX3(M1)=Q1                                                       00009240
      IF(M3.EQ.0) GO TO 2                                               00009250
      EXX3(M3)=Q1                                                       00009260
      ETX3(M3)=-Q1                                                      00009270
    2 TO=0.                                                             00009280
      IF(MO.EQ.0) GO TO 3                                               00009290
      CALL TLOAD(KMAX,Z)                                                00009300
      KM=KMAX1+(MO-1)*KMAX2                                             00009310
      KM1=KM-1                                                          00009320
      KM2=KM-2                                                          00009330
      BX3(MO)=BET                                                       00009340
      BT3(MO)=BET                                                       00009350
```

```
      TC=B*S1*((1.5*Z(1,KM)-2.*Z(1,KM1)+.5*Z(1,KM2))/DEL+CMXI(KMAX)*     00009360
     1Z(3,KM)+.5*SOE*BET)-TT(MO)*ALOAD                                  00009370
     3 EXX3(M1)=PHEE*(TO+.5*T2)                                         00009380
      RETURN                                                            00009390
C*********************************************************************** 00009400
 1000 CONTINUE                                                          00009410
      T2=C.                                                             00009420
      IF(M2.EQ.0) GO TO 1002                                            00009430
      KM=KMAX1+(M2-1)*KMAX2                                             00009440
      KM1=KM-1                                                          00009450
      KM2=KM-2                                                          00009460
      J=KMAX*2                                                          00009470
      I=J+KMAX                                                          00009480
      PHX1=PHIXB(J)                                                     00009490
      PHX2=PHIXB(I)                                                     00009500
      PHEN=-(1.5*Z(3,KM-KMAX2)-2.*Z(3,KM1-KMAX2)+.5*Z(3,KM2-KMAX2))/DEL 00009510
     1+CMXI(KMAX)*Z(1,KM-KMAX2)                                         00009520
      BX3(M2)=.5*(PHEE*(PHEE+2.*PHX1)-PHEN*(PHEN+2.*PHX2))              00009530
      IF(ITRMAX.EQ.1) BX3(M2)=0.                                        00009540
      BT3(M2)=-BX3(M2)                                                  00009550
      BXT3(M2)=BX3(M2)                                                  00009560
      M2L=M2-1                                                          00009570
      BX3(M2L)=PHEE*(PHEN+PHX2)+PHX1*PHEN                               00009580
      IF(ITRMAX.EQ.1) BX3(M2L)=0.                                       00009590
      BT3(M2L)=-BX3(M2L)                                                00009600
      BXT3(M2L)=-BX3(M2L)                                               00009610
      T2=B*D1*((1.5*Z(1,KM)-2.*Z(1,KM1)+.5*Z(1,KM2))/DEL+.5*SOE*BX3(M2))00009620
      T2N=B*D1*((1.5*Z(1,KM-KMAX2)-2.*Z(1,KM1-KMAX2)+.5*Z(1,KM2-KMAX2)) 00009630
     1  /DEL+.5*SOE*BX3(M2L))                                           00009640
 1002 TC=C.                                                             00009650
      IF(MO.EQ.0) GO TO 1003                                            00009660
      CALL TLOAD(KMAX,Z)                                                00009670
      KM=KMAX1+(MO-1)*KMAX2                                             00009680
      KM1=KM-1                                                          00009690
      KM2=KM-2                                                          00009700
      BX3(MO)=.5*(PHEE*(PHEE+2.*PHX1)+PHEN*(PHEN+2.*PHX2))              00009710
      IF(ITRMAX.EQ.1) BX3(MO)=0.                                        00009720
      BT3(MO)=BX3(MO)                                                   00009730
      TC=B*S1*((1.5*Z(1,KM)-2.*Z(1,KM1)+.5*Z(1,KM2))/DEL+CMXI(KMAX)*     00009740
     1 Z(3,KM)+.5*SOE*BX3(MO))-TT(MO)*ALOAD                              00009750
 1003 IF(ITRMAX.EQ.1) GO TO 1001                                        00009760
      PHSS=PHEE+PHX1                                                    00009770
      PHSP=PHEN+PHX2                                                    00009780
      M1L=M1-1                                                          00009790
      EXX3(M1)=PHSS*TO+.5*(PHSS*T2+PHSP*T2N)                            00009800
      EXX3(M1L)=PHSP*TO-.5*(PHSP*T2-PHSS*T2N)                           00009810
      ETX3(M1)=.5*(PHSS*T2+PHSP*T2N)                                    00009820
      ETX3(M1L)=.5*(-PHSP*T2+PHSS*T2N)                                  00009830
```

```
      IF(M3.EQ.0) GO TO 1001
      M3L=M3-1
      EXX3(M3)=.5*(PHSS*T2-PHSP*T2N)
      EXX3(M3L)=.5*(PHSS*T2N+PHSP*T2)
      ETX3(M3)=.5*(-PHSS*T2+PHSP*T2N)
      ETX3(M3L)=.5*(-PHSP*T2-PHSS*T2N)
 1001 CONTINUE
      RETURN
      END
      SUBROUTINE PHIBET(K,Z,IS,JS,ID,JD,PHIXB,PHITB)
C***********************************************************************
C        THIS SUBROUTINE CALCULATES THE PHI'S AND CARRIES OUT THE      *
C        MULTIPLYING AND SUMMATION PROCEDURE FOR COMPUTING THE BETA    *
C        NON-LINEAR TERMS FOR A GIVEN MERIDIONAL STATION K.  THE ARRAYS*
C        IS, JS, ID, JS,IJS, MAXS, MAXD, MAXSY ARE PREPARED IN SUB-    *
C        ROUTINE MODES AND USED HERE.                                  *
C***********************************************************************
      DIMENSION Z(4,1),IS(99,1),JS(99,1),ID(99,1),JD(99,1),PHIXB(1),
     1PHITB(1)
      COMMON /IBL1/ MNMAX
      COMMON /IBL2/ N(99),MNINIT
      COMMON /IBL4/ KMAX,KL
      COMMON /IBL7/ MNMAXO,MAXD(99),MAXS(99),MAXSY(99),IJS(99)
      COMMON /IBL12/ KMAX1,KMAX2,NCONV
      COMMON /IBL13/ ITRMAX,LSMAX
      COMMON /IBLJ/ JUMP
      COMMON /BL6/  SOE,CSE,ALOAD
      COMMON /BL8/  R(500),GAM(500),OMT(500)
      COMMON /BL10/ PHIX(99),PHIT(99),PHI(99)
      COMMON /BL11/ OMXI(500),PHEE,TO,T2
      COMMON /BL12/ TDLI,TDEL
      COMMON /BL15/ NU,U1(99),V1(99),W1(99),V2(99),U2(99),W2(99),U3(99),
     1              V3(99),W3(99)
      COMMON /BL27/ BX3(99),BT3(99),BXT3(99),BE3(99)
      COMMON /BLPHS/ PHX(99),PHT(99)
C***********************************************************************
      CX=OMXI(K)
      CT=OMT(K)
      RRA=1./R(K)
      GA=GAM(K)
      KP2=K+2
      DO 1 M=1,MNMAXO
      EN=N(M)
      IK=KP2+(M-1)*KMAX2
      U3(M)=Z(1,IK)
      V3(M)=Z(2,IK)
      W3(M)=Z(3,IK)
      PHIX(M)=-TDLI*(W3(M)-W1(M))+CX*U2(M)
```

```
      PHIT(M)=EN*W2(M)*RRA+V2(M)*CT                                     00010320
    1 PHI(M)=(TDLI*(V3(M)-V1(M))+GA*V2(M)+EN*U2(M)*RRA)*.5              00010330
      IF(ITRMAX.EQ.1) RETURN                                            00010340
      IF(JUMP.EQ.2) GO TO 1111                                          00010350
      DO 9 M=1,MNMAX                                                    00010360
      SMO=0.                                                            00010370
      SMT=0.                                                            00010380
      SMR=0.                                                            00010390
      SMF=0.                                                            00010400
      IF(N(M).EQ.0) GO TO 20                                            00010410
      MAXL=MAXS(M)                                                      00010420
      IF(MAXL.EQ.0) GO TO 2                                             00010430
      DO 3 L=1,MAXL                                                     00010440
      I=IS(L,M)                                                         00010450
      J=JS(L,M)                                                         00010460
      SMO=SMO+PHIX(I)*PHIX(J)                                           00010470
      SMT=SMT-PHIT(I)*PHIT(J)                                           00010480
      SMR=SMR+PHIX(I)*PHIT(J)+PHIX(J)*PHIT(I)                           00010490
    3 SMF=SMF-PHI(I)*PHI(J)                                             00010500
    2 MAXL=MAXD(M)                                                      00010510
      IF(MAXL.EQ.0) GO TO 4                                             00010520
      DO 5 L=1,MAXL                                                     00010530
      I=ID(L,M)                                                         00010540
      J=JD(L,M)                                                         00010550
      SMO=SMO+PHIX(I)*PHIX(J)                                           00010560
      SMT=SMT+PHIT(I)*PHIT(J)                                           00010570
      SMR=SMR-PHIX(I)*PHIT(J)+PHIX(J)*PHIT(I)                           00010580
    5 SMF=SMF+PHI(I)*PHI(J)                                             00010590
    4 IF(MAXSY(M).EQ.0) GO TO 10                                        00010600
      I=IJS(M)                                                          00010610
      SMO=SMO+PHIX(I)**2/2.                                             00010620
      SMT=SMT-PHIT(I)**2/2.                                             00010630
      SMR=(SMR+PHIX(I)*PHIT(I))                                         00010640
      SMF=SMF-PHI(I)**2/2.                                              00010650
      GO TO 10                                                          00010660
   20 DO 21 L=1,MNMAXO                                                  00010670
      SMO=SMO+PHIX(L)**2                                                00010680
      SMT=SMT+PHIT(L)**2                                                00010690
   21 SMF=SMF+PHI(L)**2                                                 00010700
      IF(M.GT.MNMAXO) GO TO 11                                          00010710
      SMO=SMO+PHIX(M)**2                                                00010720
   11 EX3(M)=SMO*.5                                                     00010730
      ET3(M)=SMT*.5                                                     00010740
      EE3(M)=SMF*.5                                                     00010750
      EXT3(M)=0.                                                        00010760
      GO TO 9                                                           00010770
   10 EX3(M)=SMO                                                        00010780
      ET3(M)=SMT                                                        00010790
```

```
      EXT3(M)=SMR*.5                                                    00010800
      BE3(M)=SMF                                                        00010810
    5 CONTINUE                                                          00010820
      RETURN                                                            00010830
C***********************************************************************00010840
C                                                                      *00010850
C                                                                      *00010860
C     THIS SECTION HANDLES GENERAL LOADING AND IMPERFECTIONS           *00010870
C                                                                      *00010880
C                                                                      *00010890
C***********************************************************************00010900
 1111 CONTINUE                                                          00010910
      DO 60 M=1,MNMAXO                                                  00010920
      KP=K+(M-1)*KMAX                                                   00010930
      PHX(M)=PHIXB(KP)                                                  00010940
   60 PHT(M)=PHITB(KP)                                                  00010950
      DO 49 M=1,MNMAX                                                   00010960
      SMC=0.                                                            00010970
      SMT=0.                                                            00010980
      SMR=0.                                                            00010990
      SMF=0.                                                            00011000
C***********************************************************************00011010
C     TEST FOR ASYMMETRIC MODE                                         *00011020
C***********************************************************************00011030
      IF (N(M).LT.0) GO TO 101                                          00011040
C***********************************************************************00011050
C                                                                      *00011060
C     THIS SECTION HANDLES SYMMETRIC MODE COMBINATIONS ONLY            *00011070
C                                                                      *00011080
C***********************************************************************00011090
C     TEST FOR ZERO- TH MODE                                           *00011100
C***********************************************************************00011110
      IF(N(M).EQ.0) GO TO  420                                          00011120
      MAXL=MAXS(M)                                                      00011130
C***********************************************************************00011140
C     TEST FOR PRESENCE OF SYMMETRIC SUMMATION COMBINATIONS            *00011150
C***********************************************************************00011160
      IF(MAXL.EQ.0) GO TO 42                                            00011170
C***********************************************************************00011180
C     SET UP -COUPLING- MODES- INDICES AND TEST FOR MODE 1             *00011190
C***********************************************************************00011200
      DO 43 L=1,MAXL                                                    00011210
      I=IS(L,M)                                                         00011220
      J=JS(L,M)                                                         00011230
      II=I-1                                                            00011240
      JJ=J-1                                                            00011250
      IF (I.EQ.1) GO TO 43                                              00011260
C***********************************************************************00011270
```

```
C     COMPILE SUMS FOR SYMMETRIC SUMMATION COMBINATION MODES          *00011280
C***********************************************************************00011290
      SMC=SMC+PHIX(I)*PHIX(J)                                           00011300
     1    +PHX(I)*PHIX(J)+PHX(J)*PHIX(I)                                00011310
     2        -PHIX(II)*(PHIX(JJ)+PHX(JJ))-PHIX(JJ)*PHX(II)             00011320
      SMT=SMT-PHIT(I)*PHIT(J)                                           00011330
     1    -PHT(I)*PHIT(J)-PHT(J)*PHIT(I)                                00011340
     2        +PHIT(II)*(PHIT(JJ)+PHT(JJ))+PHIT(JJ)*PHT(II)             00011350
      SMR=SMR+PHIX(I)*PHIT(J)+PHIX(J)*PHIT(I)                           00011360
     1    +PHX(I)*PHIT(J)+PHX(J)*PHIT(I)+PHIX(I)*PHT(J)                 00011370
     2    +PHIX(J)*PHT(I)                                               00011380
     3        +PHIX(II)*(PHIT(JJ)+PHT(JJ))+PHIX(JJ)*(PHIT(II)           00011390
     4        +PHT(II))+PHX(II)*PHIT(JJ)+PHX(JJ)*PHIT(II)               00011400
      SMF=SMF-PHI(I)*PHI(J)                                             00011410
     1        +PHI(II)*PHI(JJ)                                          00011420
   43 CONTINUE                                                          00011430
   42 MAXL=MAXD(M)                                                      00011440
C***********************************************************************00011450
C     TEST FOR PRESENCE OF SYMMETRIC DIFFERENCE COMBINATIONS          *00011460
C***********************************************************************00011470
      IF(MAXL.EQ.0) GO TO 44                                            00011480
C***********************************************************************00011490
C     SET UP -COUPLING- MODES- INDICES AND TEST FOR MODE 1              00011500
C***********************************************************************00011510
      DO 45 L=1,MAXL                                                    00011520
      I=ID(L,M)                                                         00011530
      J=JD(L,M)                                                         00011540
      II=I-1                                                            00011550
      JJ=J-1                                                            00011560
      IF (J.EQ.1) GO TO 442                                             00011570
C***********************************************************************00011580
C     COMPILE SUMS FOR SYMMETRIC DIFFERENCE COMBINATION MODES         *00011590
C***********************************************************************00011600
      SMC=SMO+PHIX(I)*PHIX(J)                                           00011610
     1    +PHX(I)*PHIX(J)+PHX(J)*PHIX(I)                                00011620
     2        +PHIX(II)*(PHIX(JJ)+PHX(JJ))+PHIX(JJ)*PHX(II)             00011630
      SMT=SMT+PHIT(I)*PHIT(J)                                           00011640
     1    +PHT(I)*PHIT(J)+PHT(J)*PHIT(I)                                00011650
     2        +PHIT(II)*(PHIT(JJ)+PHT(JJ))+PHIT(JJ)*PHT(II)             00011660
      SMR=SMR-PHIX(I)*PHIT(J)+PHIX(J)*PHIT(I)                           00011670
     1    -PHX(I)*PHIT(J)+PHX(J)*PHIT(I)-PHIX(I)*PHT(J)                 00011680
     2    +PHIX(J)*PHT(I)                                               00011690
     3        +PHIX(II)*(PHIT(JJ)+PHT(JJ))-PHIX(JJ)*(PHIT(II)           00011700
     4        +PHT(II))+PHX(II)*PHIT(JJ)-PHX(JJ)*PHIT(II)               00011710
      SMF=SMF+PHI(I)*PHI(J)                                             00011720
     1        +PHI(II)*PHI(JJ)                                          00011730
      GO TO 45                                                          00011740
C***********************************************************************00011750
```

```
C     EXECUTE BELOW IF J=1 IN DIFFERENCE COMBINATIONS                 *00011760
C***********************************************************************00011770
  442 SMO=SMO+(PHIX(1)*PHIX(I)+PHX(1)*PHIX(I)+PHX(I)*PHIX(1))*2.0      00011780
      SMT=SMT+(PHIT(1)*(PHIT(II)+PHT(II))+PHIT(II)*PHT(1))*2.0          00011790
      SMR=SMR+(PHIX(1)*(PHIT(I)+PHT(I))+PHX(1)*PHIT(I)                  00011800
     1        +PHIT(1)*(PHIX(II)+PHX(II))+PHT(1)*PHIX(II))*2.0          00011810
      SMF=SMF+(PHI(1)*PHI(II))*2.0                                      00011820
   45 CONTINUE                                                          00011830
C***********************************************************************00011840
C     TEST FOR PRESENCE OF SAME-INDEX COMBINATION                     *00011850
C***********************************************************************00011860
   44 IF(MAXSY(M).EQ.0) GO TO 410                                       00011870
C***********************************************************************00011880
C     SET UP INDICES AND COMPILE SUMS                                 *00011890
C***********************************************************************00011900
      I=IJS(M)                                                          00011910
      II=I-1                                                            00011920
      SMO=SMO+PHIX(I)**2/2.                                             00011930
     1    +PHX(I)*PHIX(I)                                               00011940
     2        -PHIX(II)**2/2.0-PHIX(II)*PHX(II)                         00011950
      SMT=SMT-PHIT(I)**2/2.                                             00011960
     1    -PHT(I)*PHIT(I)                                               00011970
     2        +PHIT(II)**2/2.0+PHIT(II)*PHT(II)                         00011980
      SMR= SMR+PHIX(I)*PHIT(I)                                          00011990
     1    +PHX(I)*PHIT(I)+PHIX(I)*PHT(I)                                00012000
     2        +PHIX(II)*(PHIT(II)+PHT(II))+PHX(II)*PHIT(II)             00012010
      SMF=SMF-PHI(I)**2/2.                                              00012020
     2        +PHI(II)**2/2.0                                           00012030
      GO TO 410                                                         00012040
C***********************************************************************00012050
C     THIS SECTION HANDLES CASES WHERE MODE 0 IS INCLUDED             *00012060
C***********************************************************************00012070
  420 DO 421 L=1,MNMAXO                                                 00012080
      SMO=SMO+PHIX(L)**2                                                00012090
     1    +2.0*PHX(L)*PHIX(L)                                           00012100
      SMT=SMT+PHIT(L)**2                                                00012110
     1    +2.0*PHT(L)*PHIT(L)                                           00012120
  421 SMF=SMF+PHI(L)**2                                                 00012130
      SMO=SMO+PHIX(M)**2                                                00012140
     1    +2.0*PHX(M)*PHIX(M)                                           00012150
      SMF=SMF+PHI(1)**2                                                 00012160
      SMT=SMT+PHIT(1)*(PHIT(1)+2.0*PHT(1))                              00012170
      SMR=SMR+(PHIX(1)*(PHIT(1)+PHT(1))+PHX(1)*PHIT(1))*2.0             00012180
      DO 122 L=2,MNMAXO,2                                               00012190
  122 SMR=SMR+PHIX(L)*(PHIT(L+1)+PHT(L+1))+PHX(L)*PHIT(L+1)             00012200
      DO 121 L=3,MNMAXO,2                                               00012210
  121 SMR=SMR+PHIX(L)*(PHIT(L-1)+PHT(L-1))+PHX(L)*PHIT(L-1)             00012220
C***********************************************************************00012230
```

```
C     COMPILE BETA TERMS FOR THIS SPECIAL CASE                         *00012240
C***********************************************************************00012250
      BX3(M)=SMO*.5                                                     00012260
      BT3(M)=SMT*.5                                                     00012270
      BE3(M)=SMF*.5                                                     00012280
      BXT3(1)=SMR*0.5                                                   00012290
      GO TO 49                                                          00012300
C***********************************************************************00012310
C                                                                      *00012320
C     THIS SECTION HANDLES ASYMMETRIC MODES                            *00012330
C                                                                      *00012340
C***********************************************************************00012350
  101 MP=M+1                                                            00012360
      MAXL=MAXS(MP)                                                     00012370
C***********************************************************************00012380
C     TEST FOR PRESENCE OF SUMMATION COMBINATIONS                      *00012390
C***********************************************************************00012400
      IF (MAXL.EQ.0) GO TO 102                                          00012410
C***********************************************************************00012420
C     SET UP INDICES FOR SUMMATION COMBINATIONS                        *00012430
C***********************************************************************00012440
      DO 103 L=1,MAXL                                                   00012450
      I=IS(L,MP)                                                        00012460
      J=JS(L,MP)                                                        00012470
      II=I-1                                                            00012480
      JJ=J-1                                                            00012490
C***********************************************************************00012500
C     TEST FOR MODE 1 AND COMPILE SUMS                                 *00012510
C***********************************************************************00012520
      IF (I.EQ.1) GO TO 103                                             00012530
      SMO=SMO+PHIX(I)*(PHIX(JJ)+PHX(JJ))+PHIX(J)*(PHIX(II)+             00012540
     1    PHX(II))+PHIX(II)*PHX(J)+PHIX(JJ)*PHX(I)                      00012550
      SMT=SMT+PHIT(I)*(PHIT(JJ)+PHT(JJ))+PHIT(J)*(PHIT(II)+             00012560
     1    PHT(II))+PHIT(II)*PHT(J)+PHIT(JJ)*PHT(I)                      00012570
      SMR=SMR+PHIX(I)*(PHIT(JJ)+PHT(JJ))+PHIX(J)*(PHIT(II)+             00012580
     1    PHT(II))-PHIX(II)*(PHIT(J)+PHT(J))-PHIX(JJ)*                  00012590
     2    (PHIT(I)+PHT(I))+PHX(I)*PHIT(JJ)+PHX(J)*PHIT(II)-             00012600
     3    PHX(II)*PHIT(J)-PHX(JJ)*PHIT(I)                               00012610
      SMF=SMF+PHI(I)*PHI(JJ)+PHI(J)*PHI(II)                             00012620
  103 CONTINUE                                                          00012630
C***********************************************************************00012640
C     TEST FOR PRESENCE OF DIFFERENCE COMBINATIONS                     *00012650
C***********************************************************************00012660
  102 MAXL=MAXD(MP)                                                     00012670
      IF (MAXL.EQ.0) GO TO 104                                          00012680
C***********************************************************************00012690
C     SET UP INDICES FOR DIFFERENCE COMBINATIONS                       *00012700
C***********************************************************************00012710
```

```
      DC 105 L=1,MAXL
      I=IC(L,MP)
      J=JC(L,MP)
      I[illegible]I-1
      [illegible]-1
C**[illegible]***********************************************************
C     [illegible] FOR MODE 1 ANC CCMPILE SUMS                               *
C****[illegible]*********************************************************
      IF (J.EC.1) GO TO 123
      SMC=SMO-PHIX(I)*(PHIX(JJ)+PHX(JJ))+PHIX(J)*(PHIX(II)+
     1    PHX(II))+PHIX(II)*PHX(J)-PHIX(JJ)*PHX(I)
      SMT=SMT+PHIT(I)*(PHIT(JJ)+PHT(JJ))-PHIT(J)*(PHIT(II)+
     1    PHT(II))-PHIT(II)*PHT(J)+PHIT(JJ)*PHT(I)
      SMR=SMR+PHIX(I)*(PHIT(JJ)+PHT(JJ))+PHIX(J)*(PHIT(II)+
     1    PHT(II))+PHIX(II)*(PHIT(J)+PHT(J))+PHIX(JJ)*
     2    (PHIT(I)+PHT(I))+PHX(I)*PHIT(JJ)+PHX(J)*PHIT(II)+
     3    PHX(II)*PHIT(J)+PHX(JJ)*PHIT(I)
      SMF=SMF+PHI(I)*PHI(JJ)-PHI(J)*PHI(II)
      GC TO 1C5
C***********************************************************************
C     EXECUTE BELOW IF J=1 IN DIFFERENCE COMBINATIONS                  *
C***********************************************************************
  123 SMC=SMO+(PHIX(1)*(PHIX(II)+PHX(II))+PHIX(II)*PHX(1))*2.0
      SMT=SMT+(PHIT(I)*(PHIT(1)+PHT(1))+PHIT(1)*PHT(II))*2.C
      SMR=SMR+(PHIX(1)*(PHIT(II)+PHT(II))+PHIX(II)*(PHIT(1)+
     1    PHT(1))+PHX(1)*PHIT(II)+PHX(II)*PHIT(1))*2.0
      SMF=SMF+(PHI(I)*PHI(1))*2.0
  1C5 CCNTINUE
C***********************************************************************
C     TEST FOR PRESENCE CF SAME-INDEX CCMBINATICN                      *
C***********************************************************************
  1C4 IF (MAXSY(MP).EQ.0) GC TO 410
C***********************************************************************
C     SET UP INDICES AND CCMPILE SUMS                                  *
C***********************************************************************
      I=IJS(MP)
      II=I-1
      SMC=SMO+PHIX(I)*(PHIX(II)+PHX(II))+PHIX(II)*PHX(I)
      SMT=SMT+PHIT(I)*(PHIT(II)+PHT(II))+PHIT(II)*PHT(I)
      SMR=SMR+PHIX(I)*(PHIT(II)+PHT(II))-PHIX(II)*(PHIT(I)+
     1    PHT(I))+PHX(I)*PHIT(II)-PHX(II)*PHIT(I)
      SMF=SMF+PHI(I)*PHI(II)
C***********************************************************************
C     CCMPILE BETA TERMS                                               *
C***********************************************************************
  410 BX3(M)=SMO
      BT3(M)=SMT
      BXT3(M)=SMR*.5
```

```
      BE3(M)=SMF
   49 CONTINUE
      RETURN
      END
      SUBROUTINE HJ(K,MN)
C***********************************************************************
C       THIS SUBROUTINE COMPUTES THE ELEMENTS OF THE H AND JAY        *
C       MATRICES FOR BOTH BOUNDARIES OF THE SHELL                      *
C***********************************************************************
      REAL L2,LAM2,LSD1N,       LSD18,JAY,NU
      COMMON /IBL2/ N(99),MNINIT
      COMMON /IBL4/ KMAX,KL
      COMMON /BL8/  R(500),GAM(500),OMT(500)
      COMMON /BL11/ OMXI(500),PHEE,T0,T2
      COMMON /BL14/ LAM2,LSD18,LSD1N
      COMMON /BL15/ NU,U1(99),V1(99),W1(99),V2(99),L2(99),W2(99),U3(99),
     1              V3(99),W3(99)
      COMMON /BL17/ DEL
      COMMON /BL20/ DEOMX(500)
      COMMON /BL23/ JAY(4,4),H(4,4)
      EQUIVALENCE(L2,LAM2)
C***********************************************************************
      CALL BCB(K,B,DB,D,DD)
      YAH=1.
      IF(K.EQ.1.OR.K.EQ.KMAX)YAH=2.
      D1=(1.-NU)
      GA=GAM(K)
      OX=OMXI(K)
      RA=R(K)
      EN=N(MN)
      ENR=EN/RA
      REG=0.
      IF(YAH.EQ.2.) REG=1.
      OT=OMT(K)
      OXT=3.*OMXI(K)-OMT(K)
      OTX=3.*OMT(K)-OMXI(K)
      DL=D*L2*D1*ENR
      H(1,1)=B
      H(1,2)=0.
      H(1,3)=0.
      H(1,4)=0.
      H(2,1)=0.
      H(2,2)=B*D1/2.+L2*D*D1/8.*OTX**2*REG
      H(2,3)=DL/2.*OTX*REG
      H(2,4)=0.
      H(3,1)=0.
      H(3,2)=DL*OTX*YAH/4.
      ENR2=ENR**2
```

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      H(3,3)=L2*D*D1*(YAH*ENR2+(1.+NU)*GA**2)                           00013680
      GA2=GA**2                                                         00013690
      H(3,4)=L2                                                         00013700
      H(4,1)=0.                                                         00013710
      H(4,2)=0.                                                         00013720
      H(4,3)=-1.                                                        00013730
      H(4,4)=0.                                                         00013740
      JAY(1,1)=NU*GA*B                                                  00013750
      JAY(1,2)=NU*B*ENR                                                 00013760
      JAY(1,3)=B*(DX+NU*DT)                                             00013770
      JAY(1,4)=0.                                                       00013780
      JAY(2,1)=-B*D1*ENR/2.-DL/8.*DXT*CTX*REG                           00013790
      JAY(2,2)=-GA*H(2,2)                                               00013800
      JAY(2,3)=-GA*H(2,3)                                               00013810
      JAY(2,4)=0.                                                       00013820
      JAY(3,1)=-L2*D*D1*((1.+NU)*GA2*DX+ENR2/4.*DXT*YAH)                00013830
      JAY(3,2)=-GA*DL/2.*(     2.*CT*(1.+NU)+DTX/2.*YAH)                00013840
      JAY(3,3)=-L2*D*D1*(1.+NU+YAH)*GA*ENR2                             00013850
      JAY(3,4)=L2*D1*GA                                                 00013860
      JAY(4,1)=DX                                                       00013870
      JAY(4,2)=0.                                                       00013880
      JAY(4,3)=0.                                                       00013890
      JAY(4,4)=0.                                                       00013900
      DO 1 I=1,4                                                        00013910
      DO 1 J=1,4                                                        00013920
    1 H(I,J)=H(I,J)/2./DEL                                              00013930
      RETURN                                                            00013940
      END                                                               00013950
      SUBROUTINE EFG(K,MN,ZO,Z2,Z3)                                     00013960
C***********************************************************************00013970
C        THIS SUBROUTINE PREPARES THE ELEMENTS OF THE E, F, AND G      *00013980
C        FOR EACH MERIDIAN STATION K AND FOR EACH FOURIER MODE, MN.    *00013990
C***********************************************************************00014000
      IMPLICIT LOGICAL*1 ($)                                            00014010
      REAL NU,N,     LAM2,LSD18,LSD1N,MASS,MAS                          00014020
      DIMENSION ZO(4,1),Z2(4,1),Z3(4,1)                                 00014030
      COMMON /IBL2/NN(99),MNINIT                                        00014040
      COMMON /BL8/  R(500),GAM(500),OMT(500)                            00014050
      COMMON /BL11/ OMXI(500),PHEE,T0,T2                                00014060
      COMMON /BL14/ LAM2,LSD18,LSD1N                                    00014070
      COMMON /BL15/ NU,U1(99),V1(99),W1(99),V2(99),U2(99),W2(99),U3(99),00014080
     1              V3(99),W3(99)                                       00014090
      COMMON /BL20/ DEOMX(500)                                          00014100
      COMMON /BL25/ E(4,4),F(4,4),G(4,4)                                00014110
      COMMON /BL100/ TEEC,$DYNMC                                        00014120
      COMMON /BL101/ DELSD                                              00014130
      COMMON /BL102/ DELOAD                                             00014140
      COMMON /BL103/ MASS(500)                                          00014150
```

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C*************************************************************************************00014160
      N=NN(MN)                                                                          00014170
      MAS=MASS(K)                                                                       00014180
      CALL BCB(K,B,DB,D,CC)                                                             00014190
      E(1,1)=B                                                                          00014200
      E(1,2)=0.                                                                         00014210
      E(1,3)=0.                                                                         00014220
      E(1,4)=0.                                                                         00014230
      E(2,1)=0.                                                                         00014240
      C1=(1.-NU)                                                                        00014250
      RA=R(K)                                                                           00014260
      GA=GAM(K)                                                                         00014270
      CX=CMXI(K)                                                                        00014280
      CT=CMT(K)                                                                         00014290
      DEX=DEOMX(K)                                                                      00014300
      REX=(3.*OT-OX)                                                                    00014310
      GA2=GA**2                                                                         00014320
      RXE=(3.*OX-OT)                                                                    00014330
      CTX=OT*CX                                                                         00014340
      CNLR=LAM2*D*N*D1/(2.*RA)                                                          00014350
      CCNLR=CNLR*DD/D                                                                   00014360
      E(2,2)=B*C1/2.+LAM2*D*D1*REX**2/8.                                                00014370
      E(2,3)=CNLR*REX                                                                   00014380
      E(2,4)=0.                                                                         00014390
      E(3,1)=0.                                                                         00014400
      E(3,2)=E(2,3)                                                                     00014410
      RAN=(N/RA)**2                                                                     00014420
      E(3,3)=LAM2*D*D1*(2.*RAN+(1.+NU)*GA2)                                             00014430
      E(3,4)=LAM2                                                                       00014440
      E(4,1)=0.                                                                         00014450
      E(4,2)=0.                                                                         00014460
      E(4,3)=-D                                                                         00014470
      E(4,4)=0.                                                                         00014480
      F(1,1)=GA*B+DB                                                                    00014490
      F(1,2)=(1.+NU)*B*N/(2.*RA)+CNLR*REX*RXE/4.                                        00014500
      F(1,3)=B*(OX+NU*OT)+LAM2*D*D1*((1.+NU)*GA2*CX+RAN*RXE/2.)                         00014510
      F(1,4)=LAM2*OX                                                                    00014520
      F(2,1)=-F(1,2)                                                                    00014530
      F(2,2)=(D1/2.)*(GA*B+DB)-(LAM2*C*C1*REX/8.)*(2.*DEX-GA*(5.*OX                     00014540
     1-3.*OT))+LAM2*DD*C1*REX**2/8.                                                     00014550
      F(2,3)=CNLR*(2.*(1.+NU)*GA*OT-DEX+3.*GA*(CX-CT))+CCNLR*REX                        00014560
      F(2,4)=0.                                                                         00014570
      F(3,1)=-F(1,3)                                                                    00014580
      F(3,2)=CNLR*(3.*GA*OX-GA*OT*(5.+2.*NU)-DEX)+CCNLR*REX                             00014590
      F(3,3)=-LAM2*D*D1*((1.+NU)*(2.*GA*OX*OT+GA**3)+2.*GA*RAN)                         00014600
     1+LAM2*CC*D1*((1.+NU)*GA2+2.*RAN)                                                  00014610
      F(3,4)=LAM2*GA*(2.-NU)                                                            00014620
      F(4,1)=C*CX                                                                       00014630
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      F(4,2)=0.
      F(4,3)=-D*NU*GA
      F(4,4)=0.
      G(1,1)=NU*DB*GA-NU*B*OTX-B*GA2-D1*B*RAN/2.-LAM2*D*D1*((1.+NU)*GA2*
     1CX**2+RXE**2*RAN/8.)
     2  - 2.*MAS/DELSD
      G(1,2)=NU*N*DB/RA-(3.-NU)/(2.*RA)*GA*B*N-DNLR*2.*GA*(REX*RXE/8.
     1+(1.+NU)*OTX)
      G(1,3)=B*(DEX+GA*(OX-OT))+DB*(OX+NU*OT)-LAM2*D*D1*GA*RAN*(RXE/2.+(
     11.+NU)*OX)
      G(1,4)=LAM2*D1*GA*CX
      G(2,1)=-B*GA*N*(3.-NU)/(2.*RA)-D1*N*DB/(2.*RA)+DNLR*2.*(-1.*(1.+
     1NU)*GA*CTX+GA/8.*(6.*OTX-7.*OX**2-3.*OT**2)-DEX/4.*(5.*CT-3.*CX))
     2-DDNLR/4.*REX*RXE
      G(2,2)=-GA*F(2,2)+D1/2.*B*OTX-B*RAN-LAM2*D*D1*((1.+NU)*CT**2*RAN
     1-CTX/8.*REX**2)
     2  - 2.*MAS/DELSD
      G(2,3)=-B*N*(OT+NU*OX)/RA+DNLR*(GA*DEX-2.*GA2*OX-2.*(1.+NU)*CT
     1*RAN+REX*(GA2+OTX))-DDNLR*REX*GA
      G(2,4)=-NU*LAM2*OT*N/RA
      G(3,1)=-B*GA*(OT+NU*OX)+LAM2*D*D1*(GA*(1.+NU)*(-GA*DEX+GA2*OX
     1-CX*RAN+2.*OTX*CX)+RAN/2.*(GA*OX-GA*OT-3.*DEX))
     2-LAM2*DD*D1*((1.+NU)*GA2*OX+RAN/2.*RXE)
      G(3,2)=-B*N*(OT+NU*CX)/RA+DNLR*(2.*(1.+NU)*(OTX*OT-GA2*OX+2.*GA2
     1*CT-OT*RAN)+GA*DEX+3.*GA2*(CT-OX)+CTX*REX)-DDNLR*(2.*(1.+NU)*GA
     2*CT+GA*REX)
      G(3,3)=-B*(OX**2+2.*NU*OTX+OT**2)+LAM2*D*D1*RAN*((1.+NU)*(OTX-RAN
     1+2.*GA2)+2.*(GA2+CTX))-LAM2*DD*D1*RAN*(3.+NU)*GA
     2  - 2.*MAS/DELSD
      G(3,4)=-LAM2*(D1*CTX+NU*RAN)
      G(4,1)=D*(DEX+NU*GA*OX)
      G(4,2)=D*NU*N*OT/RA
      G(4,3)=D*NU*RAN
      G(4,4)=-1.
      RETURN
      END
      SUBROUTINE POLE(K,P,DEE,DST,X,Z,ZO,Z2,Z3,ZDOT,IS,JS,ID,JD,PHIXB,
     1PHITB)
C***********************************************************************
C        THIS SUBROUTINE PRINTS THE SOLUTION AT AN INITIAL AND A FINAL *
C        POLE.                                                         *
C***********************************************************************
      IMPLICIT LOGICAL*1 ($)
      REAL NU,MT,MX,MTH,MXT,MTS,KX,KT,KXT,LAM,LAM2,MASS
      DIMENSION P(4,4,1),DEE(4,4,1),DST(4,4,1),X(4,1),Z(4,1),ZO(4,1),
     1Z2(4,1),Z3(4,1),ZDOT(4,1),IS(99,1),JS(99,1),ID(99,1),JD(99,1),
     2PHIXB(1),PHITB(1)
      COMMON /IBL2/ N(99),MNINIT
```

```
      COMMON /IBL3/ MO,M1,M2,M3                                         00015120
      COMMON /IBL4/ KMAX,KL                                             00015130
      COMMON /IBL5/ IBCINL,IBCFNL                                       00015140
      COMMON /IBL7/ MNMAXO,MAXD(99),MAXS(99),MAXSY(99),IJS(99)          00015150
      COMMON /IBL8/ LSTEP,ITR                                           00015160
      COMMON /IBL10/ IFREQ,NTHMAX                                       00015170
      COMMON /IBL12/ KMAX1,KMAX2,NCONV                                  00015180
      COMMON /IBLJ/ JUMP                                                00015190
      COMMON /BL4/  ZF1M(4,4,99),ZF2M(4,4,99),
     1              ZF3M(4,4,99),ZF4M(4,4,99)
      COMMON /BL5/  TT(99),MT(99),DT(99),DMT(99)                        00015220
      COMMON /BL6/  SOE,CSE,ALOAD                                       00015230
      COMMON /BL7/  D1,S1                                               00015240
      COMMON /BL8/  R(500),GAM(500),CMT(500)                            00015250
      COMMON /BL10/ PHIX(99),PHIT(99),PHI(99)                           00015260
      COMMON /BL11/ OMXI(500),PHEE,TO,T2                                00015270
      COMMON /BL11A/ PHEN,T2N                                           00015280
      COMMON /BL12/ TDLI,TDEL                                           00015290
      COMMON /BL14/ LAM2,LSD18,LSC1N                                    00015300
      COMMON /BL15/ NU,U1(99),V1(99),W1(99),V2(99),U2(99),W2(99),U3(99),00015310
     1              V3(99),W3(99)                                       00015320
      COMMON /BL17/ DEL                                                 00015330
      COMMON /BL19/ TH(36)                                              00015340
      COMMON /BL20/ DEOMX(500)                                          00015350
      COMMON /BL27/ BX3(99),BT3(99),BXT3(99),BE3(99)                    00015360
      COMMON /BL31/ DELSQ,EXT1(99)                                      00015370
      COMMON /BL32/ TKN,ELAST,CHAR,SIGC                                 00015380
      COMMON /BL100/ TEEC,$DYNMC                                        00015390
      COMMON /BL101/ DELSD                                              00015400
      COMMON /BL102/ DELCAD                                             00015410
      COMMON /BL103/ MASS(500)                                          00015420
      COMMON /BL110/ TX(99),TTH(99),TXT(99),MX(99),MTH(99),MXT(99),     00015430
     1               QS(99)                                             00015440
      COMMON /BL111/ ABZ,ABZO,ABZN,ABZ3,DD2                             00015450
C***********************************************************************00015460
      CALL BCB(K,BS,DB,CS,DD)                                           00015470
      M1L=M1-1                                                          00015480
      M2L=M2-1                                                          00015490
      IF(K.EQ.KMAX) GO TO 301                                           00015500
      DO 202 MN=1,MNMAXO                                                00015510
      U1(MN)=U2(MN)                                                     00015520
      V1(MN)=V2(MN)                                                     00015530
      W1(MN)=W2(MN)                                                     00015540
      I3=3+(MN-1)*KMAX2                                                 00015550
      I2=I3-1                                                           00015560
      U2(MN)=Z(1,I3)                                                    00015570
      V2(MN)=Z(2,I3)                                                    00015580
      W2(MN)=Z(3,I3)                                                    00015590
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      PHIX(MN)=0.                                                       00015600
      PHIT(MN)=0.0                                                      00015610
      PHI(MN)=0.                                                        00015620
      MX(MN)=Z(4,I2)*ABZ3                                               00015630
      MTH(MN)=0.                                                        00015640
      MXT(MN)=0.                                                        00015650
      CS(MN)=0.                                                         00015660
      TX(MN)=0.                                                         00015670
      TTH(MN)=0.                                                        00015680
  202 TXT(MN)=0.                                                        00015690
      IF(M1.EQ.0) GO TO 203                                             00015700
      CALL INLPCL (Z,PHIXB,PHITB)                                       00015710
      PHIX(M1)=PHEE*ABZO                                                00015720
      PHIT(M1)=-PHEE*ABZO                                               00015730
      IF(JUMP.EQ.1) GO TO 1001                                          00015740
       PHIX(M1L)=PHEN*ABZO                                              00015750
      PHIT(M1L)=PHIX(M1L)                                               00015760
 1001 CONTINUE                                                          00015770
      II=3+(M1-1)*KMAX2                                                 00015780
      IP1=II+1                                                          00015790
      IM1=II-1                                                          00015800
      GA2=GAM(2)                                                        00015810
      CALL BCB(2,BS,DB,CS,DD)                                           00015820
      CALL TLCAD(2,Z)                                                   00015830
      PHIXX=-Z(3,IP1)*TDLI+CMXI(2)*Z(1,II)                              00015840
      PHITT=Z(3,II)/R(2)+CMT(2)*Z(2,II)                                 00015850
      PHII=((Z(2,IP1)-Z(2,IM1))*TDLI+GA2*Z(2,II)+Z(1,II)/R(2))/2.       00015860
      CS(M1)=SIGO*TKN*LAM2*((2.-NU)*Z(4,II)-DS*DC2*(PHITT/R(2)+PHIXX    00015870
     1    *GA2)+D1*MT(M1)*ALOAD+DS*D1*(-PHIXX/R(2)-GA2*PHITT+(CMT(2)-CMXI00015880
     2      (2))*PHII+(Z(3,IP1)*TDLI-GA2*Z(3,II))/R(2)+GA2*(CMXI(2)-CMT 00015890
     3     (2))*Z(2,II)+CMT(2)*(Z(2,IP1)-Z(2,IM1))*TDLI)*.5)/CEL        00015900
      IF(MO.EQ.0) GO TO 204                                             00015910
       TX(MO) =TO*ABZ                                                   00015920
      TTH(MO) =TO*ABZ                                                   00015930
      MTH(MO) =MX(MO)                                                   00015940
  204 IF(M2.EQ.0) GO TO 205                                             00015950
       TX(M2) = T2*ABZ                                                  00015960
      TTH(M2) =-T2*ABZ                                                  00015970
      TXT(M2)=-T2*ABZ                                                   00015980
      MTH(M2) =-MX(M2)                                                  00015990
      MXT(M2) =MTH(M2)                                                  00016000
      IF(JUMP.EQ.1) GO TO 205                                           00016010
      TX(M2L)=T2N*ABZ                                                   00016020
      TTH(M2L)=-TX(M2L)                                                 00016030
      TXT(M2L)=TX(M2L)                                                  00016040
      MTH(M2L)=-MX(M2L)                                                 00016050
      MXT(M2L)=MX(M2L)                                                  00016060
      GO TO 205                                                         00016070
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203  IF(MO.EQ.0) GO TO 206
     I3=3+(MO-1)*KMAX2
     I4=I3+1
     CALL TLOAD(1,Z)
     TX(MO)=BS*S1*((2.*Z(1,I3)-.5*Z(1,I4))/DEL+OMXI(1)*Z(3,I3-1))*ABZ
    1          -TT(MO)*ABZ*ALCAC
     TTH(MO)=TX(MO)
     MTH(MO)=MX(MO)
206  IF(M2.EQ.0) GO TO 205
     I3=3+(M2-1)*KMAX2
     I4=I3+1
     TX(M2)=BS*D1*(2.*Z(1,I3)-.5*Z(1,I4))/DEL
      TX(M2) = TX(M2)*ABZ
     TTH(M2) =-TX(M2)
     TXT(M2) =-TX(M2)
     MTH(M2) =-MX(M2)
     MXT(M2) =-MX(M2)
     IF(JUMP.EQ.1) GO TO 205
     TX(M2L)=BS*D1*(2.*Z(1,I3-KMAX2)-.5*Z(1,I4-KMAX2))/DEL
     TX(M2L)=TX(M2L)*ABZ
     TTH(M2L)=-TX(M2L)
     TXT(M2L)=TX(M2L)
     MTH(M2L)=-MX(M2L)
     MXT(M2L)=MX(M2L)
205  RETURN
301  CONTINUE
     DO 302 MN=1,MNMAXC
     U1(MN)=U2(MN)
     V1(MN)=V2(MN)
     W1(MN)=W2(MN)
     PHIX(MN)=0.
     PHIT(MN)=0.
     PHI(MN)=0.
     IK=KMAX1+(MN-1)*KMAX2
     MX(MN)=Z(4,IK)*ABZ3
     MTH(MN)=0.
     MXT(MN)=0.
     CS(MN)=C.
     TX(MN)=0.
     TTH(MN)=0.
302  TXT(MN)=0.
     IF(M1.EQ.0) GO TO 303
     CALL FNLPCL (Z,PHIXB,PHITB)
     PHIX(M1)=PHEE*ABZO
     PHIT(M1)= PHEE*ABZO
     IF(JUMP.EQ.1) GO TO 1002
     PHIX(M1L)=PHEN*ABZC
     PHIT(M1L)=-PHIX(M1L)
```

```
1002 CONTINUE
     II=KMAX+(M1-1)*KMAX2
     IP1=II+1
     IM1=II-1
     GAK=GAM(KL)
     CALL BCB(KL,BS,DB,CS,DD)
     CALL TLCAD(KL,Z)
     PHIXX=Z(3,IM1)*TDLI+OMXI(KL)*Z(1,II)
     PHITT=Z(3,II)/R(KL)+OMT(KL)*Z(2,II)
     PHII=((Z(2,IP1)-Z(2,IM1))*TDLI+GAK*Z(2,II)+Z(1,II)/R(KL))/2.
     CS(M1)=-SIGO*TKN*LAM2*((2.-NU)*Z(4,II)-DS*DC2*(PHITT/R(KL)+PHIXX
    1*GAK)+D1*MT(M1)*ALCAD-DS*D1*(-PHIXX/R(KL)-GAK*PHITT+(OMT(KL)-OMXI
    2      (KL))*PHII+(-Z(3,IM1)*TDLI-GAK*Z(3,II))/R(KL)+GAK*(OMXI(KL)
    3         -OMT(KL))*Z(2,II)+CMT(KL)*(Z(2,IP1)-Z(2,IM1))*TDLI)*.5)
    4      /DEL
     IF(MO.EQ.0) GO TO 304
      TX(MO) =TO*ABZ
     TTH(MO) =TO*ABZ
     MTH(MO) =MX(MO)
 304 IF(M2.EQ.0) GO TO 305
      TX(M2) = T2*ABZ
     TTH(M2) =-T2*ABZ
     TXT(M2) = T2*ABZ
     MTH(M2) =-MX(M2)
     MXT(M2) =MX(M2)
     IF(JUMP.EQ.1) GO TO 305
     TX(M2L)=T2N*ABZ
     TTH(M2L)=-TX(M2L)
     TXT(M2L)=-TX(M2L)
     MTH(M2L)=-MX(M2L)
     MXT(M2L)=-MX(M2L)
     GO TO 305
 303 IF(MO.EQ.0) GO TO 306
     IKM=KMAX+(MO-1)*KMAX2
     IM1=IKM-1
     CALL TLCAD(KMAX,Z)
     TX(MO)=BS*S1*((-2.*Z(1,IKM)+.5*Z(1,IM1))/DEL+CMXI(KMAX)*Z(3,IKM+1)
    1            )*ABZ-TT(MO)*ABZ*ALCAD
     TTH(MO) =TX(MO)
     MTH(MO) =MX(MO)
 306 IF(M2.EQ.0) GO TO 305
     IKM=KMAX+(M2-1)*KMAX2
     IM1=IKM-1
     TX(M2)=BS*D1*(-2.*Z(1,IKM)+.5*Z(1,IM1))/DEL
     TX(M2)=TX(M2)*ABZ
     TTH(M2) =-TX(M2)
     TXT(M2) = TX(M2)
     MTH(M2) =-MX(M2)
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```
      MXT(M2) = MX(M2)
      IF(JUMP.EQ.1) GO TO 305
      TX(M2L)=BS*D1*(-2.*Z(1,IKM-KMAX2)+.5*Z(1,IM1-KMAX2))/DEL
      TX(M2L)=TX(M2L)*ABZ
      TTH(M2L)=-TX(M2L)
      TXT(M2L)=-TX(M2L)
      MTH(M2L)=-MX(M2L)
      MXT(M2L)=-MX(M2L)
  305 RETURN
      END
      SUBROUTINE MODES (IS,JS,ID,JD,P,X,Z0,Z2,Z3,DEE,DST)
C***********************************************************************
C        IN THIS SUBROUTINE, ARRAYS THAT DEFINE THOSE SETS OF INDICES  *
C        THAT COMBINE TO EQUAL EACH VALUE OF N IN THE PROBLEM ARE DETER*
C        MINED.  MODES IS CALLED PRIOR TO THE FIRST ITERATION AND AFTER*
C        EVERY ITERATION UNTIL A SPECIFIED NUMBER OF FOURIER TERMS IS  *
C        REACHED.  EACH FOURIER INDEX IN THE PROBLEM IS SUBTRACTED FROM*
C        ALL OTHER FOURIER INDICES AND THE RESULT IS COMPARED WITH ALL *
C        FOURIER INDICES TO SEE IF THE NEW VALUE EXISTS IN THE PROGRAM.*
C        IF IT DOES, THE LOCATIONS OF THE TWO INDICES THAT MADE THE COM-
C        BINATION ARE STORED IN TWO SPECIAL 2-DIMENSIONAL ARRAYS, ID AND
C        JD.  ONE ARGUMENT OF EACH ARRAY IS THE VALUE OF THE NEW INDEX *
C        AND THE OTHER IS THE NUMBER OF COMBINATIONS OF INDICES THAT   *
C        ALSO GIVE THIS VALUE OF THE INDEX.  IF THERE IS NO INDEX IN THE
C        PROGRAM THAT MATCHES THE NEW ONE, THEN A NEW FOURIER TERM HAS *
C        BEEN GENERATED AND WILL BE CONSIDERED IN THE NEXT ITERATION FOR
C        SOLUTION.                                                     *
C        THE VARIABLE MAXD STORES THE TOTAL NUMBER OF SUCH COMBINATIONS*
C        FOR EACH VALUE OF THE FOURIER INDEX.  IN A SIMILAR MANNER, EACH
C        INDEX IS ADDED TO EVERY OTHER INDEX AND THE SUM COMPARED WITH *
C        ALL INDICES.  THIS RESULT IS STORED IN THE 2-DIMENSIONAL ARRAYS
C        IS AND JS, IN THE SAME MANNER AS WAS DONE FOR THE SUBTRACTION *
C        CASE.  THE VARIABLE MAXS STORES THE TOTAL NUMBER OF SUMMATION *
C        COMBINATIONS FOR EACH VALUE OF THE FOURIER INDEX.             *
C        A SPECIAL ROUTINE HANDLES THE CASES WHERE THE INDEX IS ADDED TO
C        AND SUBTRACTED FROM ITSELF.  THE 2-DIMENSIONAL ARRAY IJS STORES
C        THE LOCATION OF THE INDEX AND THE VARIABLE MAXSY STORES THE   *
C        TOTAL NUMBER OF SUCH COMBINATIONS.                            *
C        WITH THIS PROCEDURE, THE SERIES OF PRODUCTS THAT MAKE UP THE  *
C        BETA'S AND AETA'S CONTAIN NO ZERO TERM, AND THE SUMMATION IS  *
C        CARRIED OUT IN PHIBET(K) AND TEAETA(K) OVER SPECIFICALLY DE-  *
C        FINED LIMITS.                                                 *
C***********************************************************************
      DIMENSION P(4,4,1),DEE(4,4,1),DST(4,4,1),X(4,1),Z0(4,1),Z2(4,1),
     1Z3(4,1),IS(99,1),JS(99,1),ID(99,1),JD(99,1)
      COMMON /IBL1/ MNMAX
      COMMON /IBL2/ N(99),MNINIT
      COMMON /IBL7/ MNMAXC,MAXD(99),MAXS(99),MAXSY(99),IJS(99)
```

```
      COMMON /IBL9/ MAXM
      COMMON /IBL11/ ICORFL,IPASS
     7/IELJ/ JUMP
C***********************************************************************
C     DETERMINE IF NEED FOR MODAL COUPLING EXISTS                      *
C***********************************************************************
      IF(MAXM.EQ.1) RETURN
C***********************************************************************
C     SEE IF ENOUGH NEW MODES HAVE ALREADY BEEN GENERATED              *
C***********************************************************************
      IF(MNINIT.GT.MAXM) RETURN
C***********************************************************************
C                                                                      *
C                                                                      *
C     THIS SECTION HANDLES MODES GENERATED FROM THE DIFFERENCE         *
C     COMBINATIONS OF EXISTING MODES                                   *
C                                                                      *
C                                                                      *
C***********************************************************************
C     SET UP INITIAL LOOP FOR DIFFERENCE COMBINATIONS                  *
C***********************************************************************
      DO 1 MN=1,MNMAXO,JUMP
      NMN=N(MN)
      NNS=MN
      IF(MNINIT.GT.MN) NNS=MNINIT
C*******************************************Q********QQQ*Q4**********
C     SET UP SECOND LOOP - TO SUBTRACT PRESENT MODE FROM ALL OTHER     *
C     MODES                                                            *
C***********************************************************************
      DO 1 MM=NNS,MNMAXC,JUMP
      NMM=N(MM)
C***********************************************************************
C     CREATE DIFFERENCE                                                *
C***********************************************************************
      NTEST=IABS(NMN-NMM)
C***********************************************************************
C     SET UP 3RD LOOP - TO COMPARE DIFFERENCE WITH ALL OTHER MODES     *
C***********************************************************************
      DO 2 MMFT=1,MNMAX,JUMP
C***********************************************************************
C     IF WE SATISFY HERE, MODE EXISTS, GO TO INCREMENT -MAXC-          *
C***********************************************************************
      IF(NTEST.EQ.N(MMFT)) GO TO 10
    2 CONTINUE
C***********************************************************************
C     IF WE MAKE IT TO HERE, WE HAVE GENERATED A NEW MODE              *
C***********************************************************************
C     DO WE WANT ANY MORE NEW MODES                                    *
```

```
C***********************************************************************00018000
      IF(ICORFL.EQ.1) GO TO 1                                           00018010
C***********************************************************************00018020
C     FROM HERE TO -1-, WE INCREMENT COUNTERS AND MAKE APPROPRIATE    *00018030
C     ENTRIES IN -MAXD-,-IC- AND -JC-. TO SIMPLIFY USAGE OF -IC-       *00018040
C     AND -JC- IN TEAETA AND PHIBET, MODES ARE PLACED IN THESE         *00018050
C     ARRAYS SUCH THAT THE HIGHER MODE NUMBER IF ALWAYS FIRST          *00018060
C***********************************************************************00018070
      MNMAX=MNMAX+JUMP                                                  00018080
      N(MNMAX)=NTEST                                                    00018090
      IF (JUMP.GT.1) N(MNMAX-1)=-NTEST                                  00018100
      MMFT=MNMAX                                                        00018110
      IF(MNMAX.EQ.MAXM) ICORFL=1                                        00018120
   10 IF(NNN-NMM) 11,1,12                                               00018130
   11 LOCD=MAXD(MMFT)+1                                                 00018140
      MAXD(MMFT)=LOCD                                                   00018150
      IC(LOCD,MMFT)=MM                                                  00018160
      JC(LOCD,MMFT)=MN                                                  00018170
      GO TO 1                                                           00018180
   12 LOCD=MAXD(MMFT)+1                                                 00018190
      MAXD(MMFT)=LOCD                                                   00018200
      IC(LOCD,MMFT)=MN                                                  00018210
      JC(LOCD,MMFT)=MM                                                  00018220
    1 CONTINUE                                                          00018230
C***********************************************************************00018240
C                                                                      *00018250
C                                                                      *00018260
C     THIS SECTION HANDLES MODES GENERATED FROM THE SUMMATION          *00018270
C     COMBINATIONS OF EXISTING MODES                                   *00018280
C                                                                      *00018290
C                                                                      *00018300
C***********************************************************************00018310
C     NOW SET UP INITIAL LOOP FOR SUM COMBINATIONS                     *00018320
C***********************************************************************00018330
      DO 301 MN=1,MNMAXC,JUMP                                           00018340
      NNN=N(MN)                                                         00018350
      NNS=MN                                                            00018360
      IF(MNINIT.GT.MN) NNS=MNINIT                                       00018370
C***********************************************************************00018380
C     SET UP SECOND LOOP - TO ADD PRESENT MODE TO ALL OTHER MODES      *00018390
C***********************************************************************00018400
      DO 301 MM=NNS,MNMAXC,JUMP                                         00018410
      NMM=N(MM)                                                         00018420
C***********************************************************************00018430
C     CREATE SUM                                                       *00018440
C***********************************************************************00018450
      NTEST=NNN+NMM                                                     00018460
C***********************************************************************00018470
```

```
C      SET UP THIRD LOOP - TO COMPARE SUM WITH ALL OTHER MODES        *00018480
C***********************************************************************00018490
      DO 302 MMFT=1,MNMAX,JUMP                                          00018500
C***********************************************************************00018510
C      IF WE SATISFY HERE, MODE EXISTS, GO TO INCREMENT -MAXS- OR     *00018520
C      -MAXSY-)                                                       *00018530
C***********************************************************************00018540
      IF(NTEST.EQ.N(MMFT)) GO TO 310                                    00018550
  302 CONTINUE                                                          00018560
C***********************************************************************00018570
C      IF WE MAKE IT TO HERE, WE HAVE GENERATED A NEW MODE            *00018580
C***********************************************************************00018590
C      DO WE WANT ANY MORE NEW MODES                                  *00018600
C***********************************************************************00018610
      IF(ICORFL.EQ.1) GO TO 301                                         00018620
      IF(MNMAX.GE.MAXM) GO TO 301                                       00018630
C***********************************************************************00018640
C      INCREMENT -MNMAX- AND ESTABLISH NEW MODE NUMBER                *00018650
C***********************************************************************00018660
      MNMAX=MNMAX+JUMP                                                  00018670
      N(MNMAX)=NTEST                                                    00018680
      IF (JUMP.GT.1)  N(MNMAX-1)=-NTEST                                 00018690
      MMFT=MNMAX                                                        00018700
      IF(MNMAX.GE.MAXM) ICORFL=1                                        00018710
C***********************************************************************00018720
C      IF MODE WAS ADDED TO ITSELF, GO TO -MAXSY AND IJS- SECTION     *00018730
C***********************************************************************00018740
  310 IF(NMN.EQ.NMM) GO TO 360                                          00018750
C***********************************************************************00018760
C      MAKE ENTRIES IN -LOCS-,-IS- AND -JS-                           *00018770
C***********************************************************************00018780
      LOCS=MAXS(MMFT)+1                                                 00018790
      MAXS(MMFT)=LOCS                                                   00018800
      IS(LOCS,MMFT)=MN                                                  00018810
      JS(LOCS,MMFT)=MM                                                  00018820
      GO TO 301                                                         00018830
C***********************************************************************00018840
C      SEE IF THE SUM OF THE MODE WITH ITSELF WAS THE 0-TH MODE       *00018850
C***********************************************************************00018860
  360 IF(NMN.EQ.0) GO TO 301                                            00018870
C***********************************************************************00018880
C      IF HERE, IT WASN-T, MAKE ENTRIES IN -MAXSY- AND -IJS-          *00018890
C***********************************************************************00018900
      MAXSY(MMFT)=1                                                     00018910
      IJS(MMFT)=MN                                                      00018920
  301 CONTINUE                                                          00018930
      MNINIT=MNMAXO+JUMP                                                00018940
      IF(ICORFL.GT.0) IPASS=IPASS+1                                     00018950
```

```
      IF(IPASS.LT.2.AND.MNINIT.LE.MNMAX) CALL PMATRX (P,X,ZC,Z2,Z3,DEE,
     1DST)
      RETURN
      END
      SUBROUTINE TEAETA(K,Z,IS,JS,ID,JD)
C*********************************************************************
C         THIS SUBROUTINE CALCULATES THE INPLANE FORCES AND CARRIES OUT *
C         THE MULTIPLYING AND SUMMATION PROCEDURE FOR COMPUTING THE ETA *
C         NON-LINEAR TERMS FOR A GIVEN MERIDIONAL STATION K.  THE ARRAYS*
C         IS, JS, ID, JS, IJS, MAXS, MAXD, MAXSY PREPARED IN SUBROUTINE *
C         MODES ARE USED HERE                                           *
C*********************************************************************
      REAL NU,MT
      DIMENSION Z(4,1),IS(99,1),JS(99,1),ID(99,1),JD(99,1)
      COMMON /IBL1/ MNMAX
      COMMON /IBL2/ N(99),MNINIT
      COMMON /IBL7/ MNMAXO,MAXD(99),MAXS(99),MAXSY(99),IJS(99)
      COMMON /IBL8/ LSTEP,ITR
      COMMON /IBL13/ ITRMAX,LSMAX
     5/IBLJ/ JUMP
      COMMON /BL5/  TT(99),MT(99),DT(99),DMT(99)
      COMMON /BL6/  SOE,CSE,ALOAD
      COMMON /BL7/  D1,S1
      COMMON /BL8/  R(500),GAM(500),OMT(500)
      COMMON /BL10/ PHIX(99),PHIT(99),PHI(99)
      COMMON /BL11/ OMXI(500),PHEE,TO,T2
      COMMON /BL12/ TDLI,TDEL
      COMMON /BL15/ NU,U1(99),V1(99),W1(99),V2(99),U2(99),W2(99),U3(99),
     1              V3(99),W3(99)
      COMMON /BL27/ BX3(99),BT3(99),BXT3(99),BE3(99)
      COMMON /BL28/ EXX3(99),ETT3(99),ETX3(99),EXT3(99),EX3(99),ET3(99)
      COMMON /BLPHS/ PHX(99),PHT(99)
      DIMENSION TX(99),TTH(99),TXT(99)
C*********************************************************************
      RRA=1./R(K)
      GA=GAM(K)
      OX=OMXI(K)
      OT=OMT(K)
      CALL BDE(K,BS,DB,DS,DD)
      DO 1 M=1,MNMAXO
      PHIX(M)=PHIX(M)+PHX(M)
      PHIT(M)=PHIT(M)+PHT(M)
      EN=N(M)
      CALL TLOAD(K,Z)
      TTS=TT(M)*ALOAD
      EX=(U3(M)-U1(M))*TDLI+OX*W2(M)+CSE*(BX3(M)+BE3(M))
      ET= EN *V2(M)*RRA+GA*U2(M)+OT*W2(M)+OSE*(BT3(M)+BE3(M))
      EXT=.5*(TDLI*(V3(M)-V1(M))- EN *U2(M)*RRA-GA*V2(M))+CSE*EXT3(M)
```

```
      TX(M)=BS*(EX+NU*ET)-TTS                                           00019440
      TTH(M)=BS*(ET+NU*EX)-TTS                                          00019450
    1 TXT(M)=BS*C1*EXT                                                  00019460
      IF(JUMP.EQ.2) GO TO 1111                                          00019470
      DO 9 M=1,MNMAX                                                    00019480
      SMF=0.                                                            00019490
      SMS=0.                                                            00019500
      SMV=0.                                                            00019510
      SME=0.                                                            00019520
      SMN=0.                                                            00019530
      SMT=0.                                                            00019540
      IF(N(M).EQ.0) GO TO 20                                            00019550
      MAXL=MAXS(M)                                                      00019560
      IF(MAXL.EQ.0) GO TO 2                                             00019570
      DO 3 L=1,MAXL                                                     00019580
      I=IS(L,M)                                                         00019590
      J=JS(L,M)                                                         00019600
      SMF=SMF+TX(I)*PHIX(J)+TX(J)*PHIX(I)                               00019610
      SMS=SMS+TTH(I)*PHIT(J)+TTH(J)*PHIT(I)                             00019620
      SMV=SMV-PHIT(I)*TXT(J)-PHIT(J)*TXT(I)                             00019630
      SME=SME+PHIX(I)*TXT(J)+PHIX(J)*TXT(I)                             00019640
      SMN=SMN+TX(I)*PHI(J)+TX(J)*PHI(I)                                 00019650
    3 SMT=SMT+TTH(I)*PHI(J)+TTH(J)*PHI(I)                               00019660
    2 MAXL=MAXD(M)                                                      00019670
      IF(MAXL.EQ.0) GO TO 4                                             00019680
      DO 5 L=1,MAXL                                                     00019690
      I=ID(L,M)                                                         00019700
      J=JD(L,M)                                                         00019710
      SMF=SMF+TX(I)*PHIX(J)+TX(J)*PHIX(I)                               00019720
      SMS=SMS-TTH(I)*PHIT(J)+TTH(J)*PHIT(I)                             00019730
      SMV=SMV+PHIT(I)*TXT(J)+PHIT(J)*TXT(I)                             00019740
      SME=SME-PHIX(I)*TXT(J)+PHIX(J)*TXT(I)                             00019750
      SMN=SMN-TX(I)*PHI(J)+TX(J)*PHI(I)                                 00019760
    5 SMT=SMT-TTH(I)*PHI(J)+TTH(J)*PHI(I)                               00019770
    4 IF(MAXSY(M).EQ.0) GO TO 10                                        00019780
      I=IJS(M)                                                          00019790
      SMF=SMF+TX(I)*PHIX(I)                                             00019800
      SMS=SMS+TTH(I)*PHIT(I)                                            00019810
      SMV=SMV-PHIT(I)*TXT(I)                                            00019820
      SME=SME+PHIX(I)*TXT(I)                                            00019830
      SMN=SMN+TX(I)*PHI(I)                                              00019840
      SMT=SMT+TTH(I)*PHI(I)                                             00019850
      GO TO 10                                                          00019860
   20 DO 21 L=1,MNMAXO                                                  00019870
      SMF=SMF+TX(L)*PHIX(L)                                             00019880
   21 SMV=SMV+PHIT(L)*TXT(L)                                            00019890
      IF(M.GT.MNMAXO) GO TO 10                                          00019900
      SMF=SMF+TX(M)*PHIX(M)                                             00019910
```

```
   10 EXX3(M)=SMF*.5                                                    00019920
      ETT3(M)=SMS*.5                                                    00019930
      ETX3(M)=SMV*.5                                                    00019940
      EXT3(M)=SME*.5                                                    00019950
      EX3(M)=SMN*.5                                                     00019960
      ET3(M)=SMT*.5                                                     00019970
    9 CONTINUE                                                          00019980
      GO TO 2222                                                        00019990
C***********************************************************************00020000
C                                                                      *00020010
C                                                                      *00020020
C     THIS SECTION HANDLES GENERAL LOADING                             *00020030
C                                                                      *00020040
C                                                                      *00020050
C***********************************************************************00020060
 1111 DO 49 M=1,MMAX                                                    00020070
      SMF=0.0                                                           00020080
      SMS=0.0                                                           00020090
      SMV=0.0                                                           00020100
      SME=0.0                                                           00020110
      SMN=0.0                                                           00020120
      SMT=0.0                                                           00020130
C***********************************************************************00020140
C     TEST FOR ASYMMETRIC MODE                                         *00020150
C***********************************************************************00020160
      IF (N(M).LT.0) GO TO 101                                          00020170
C***********************************************************************00020180
C                                                                      *00020190
C     THIS SECTION HANDLES SYMMETRIC COMBINATIONS                      *00020200
C                                                                      *00020210
C***********************************************************************00020220
C     TEST FOR ZERO-TH MODE                                            *00020230
C***********************************************************************00020240
      IF (N(M).EQ.0) GO TO 420                                          00020250
      MAXL=MAXS(M)                                                      00020260
C***********************************************************************00020270
C     TEST FOR PRESENCE OF SYMMETRIC SUMMATION COMBINATIONS            *00020280
C***********************************************************************00020290
      IF (MAXL.EQ.0) GO TO 42                                           00020300
C***********************************************************************00020310
C     SET UP COUPLING MODES- INDICES AND TEST FOR MODE 1               *00020320
C***********************************************************************00020330
      DO 43 L=1,MAXL                                                    00020340
      I=IS(L,M)                                                         00020350
      J=JS(L,M)                                                         00020360
      II=I-1                                                            00020370
      JJ=J-1                                                            00020380
      IF (I.EQ.1) GO TO 43                                              00020390
```

```
C***********************************************************************00020400
C      COMPILE SUMS FOR SYMMETRIC SUM COMBINATION MODES                *00020410
C***********************************************************************00020420
      SMF=SMF+TX(I)*PHIX(J)+TX(J)*PHIX(I)-PHIX(II)*TX(JJ)               00020430
     1        -PHIX(JJ)*TX(II)                                          00020440
      SMS=SMS+TTH(I)*PHIT(J)+TTH(J)*PHIT(I)+PHIT(II)*TTH(JJ)            00020450
     1        +PHIT(JJ)*TTH(II)                                         00020460
      SMV=SMV-PHIT(I)*TXT(J)-PHIT(J)*TXT(I)+PHIT(II)*TXT(JJ)            00020470
     1        +PHIT(JJ)*TXT(II)                                         00020480
      SME=SME+PHIX(I)*TXT(J)+PHIX(J)*TXT(I)+PHIX(II)*TXT(JJ)            00020490
     1        +PHIX(JJ)*TXT(II)                                         00020500
      SMN=SMN+TX(I)*PHI(J)+TX(J)*PHI(I)+PHI(II)*TX(JJ)                  00020510
     1        +PHI(JJ)*TX(II)                                           00020520
      SMT=SMT+TTH(I)*PHI(J)+TTH(J)*PHI(I)+PHI(II)*TTH(JJ)               00020530
     1        +PHI(JJ)*TTH(II)                                          00020540
   43 CONTINUE                                                          00020550
   42 MAXL=MAXD(M)                                                      00020560
C***********************************************************************00020570
C      TEST FOR PRESENCE OF SYMMETRIC DIFFERENCE COMBINATIONS         *00020580
C***********************************************************************00020590
      IF (MAXL.EQ.0) GO TO 44                                           00020600
C***********************************************************************00020610
C      SET UP COUPLING MODES- INDICES AND TEST FOR MODE 1             *00020620
C***********************************************************************00020630
      DO 45 L=1,MAXL                                                    00020640
      I=IC(L,M)                                                         00020650
      J=JC(L,M)                                                         00020660
      II=I-1                                                            00020670
      JJ=J-1                                                            00020680
      IF (J.EQ.1) GO TO 442                                             00020690
C***********************************************************************00020700
C      COMPILE SUMS FOR SYMMETRIC DIFFERENCE COMBINATIONS               00020710
C***********************************************************************00020720
      SMF=SMF+TX(I)*PHIX(J)+TX(J)*PHIX(I)+PHIX(II)*TX(JJ)               00020730
     1        +PHIX(JJ)*TX(II)                                          00020740
      SMS=SMS-TTH(I)*PHIT(J)+TTH(J)*PHIT(I)-PHIT(II)*TTH(JJ)            00020750
     1        +PHIT(JJ)*TTH(II)                                         00020760
      SMV=SMV+PHIT(I)*TXT(J)+PHIT(J)*TXT(I)+PHIT(II)*TXT(JJ)            00020770
     1        +PHIT(JJ)*TXT(II)                                         00020780
      SME=SME-PHIX(I)*TXT(J)+PHIX(J)*TXT(I)+PHIX(II)*TXT(JJ)            00020790
     1        -PHIX(JJ)*TXT(II)                                         00020800
      SMN=SMN-TX(I)*PHI(J)+TX(J)*PHI(I)-PHI(II)*TX(JJ)                  00020810
     1        +PHI(JJ)*TX(II)                                           00020820
      SMT=SMT-TTH(I)*PHI(J)+TTH(J)*PHI(I)-PHI(II)*TTH(JJ)               00020830
     1        +PHI(JJ)*TTH(II)                                          00020840
      GO TO 45                                                          00020850
C***********************************************************************00020860
C      EXECUTE BELOW IF J=1 IN DIFF-COMB. (OR I=1 IN SUM COMB)       *00020870
```

```
C***********************************************************************00020880
  442 SMF=SMF+(PHIX(1)*TX(I)+PHIX(I)*TX(1))*2.0                         00020890
      SMS=SMS+(PHIT(I)*TTH(1)+PHIT(1)*TTH(II))*2.0                      00020900
      SMV=SMV+(PHIT(1)*TXT(II)+PHIT(II)*TXT(1))*2.0                     00020910
      SME=SME+(PHIX(II)*TXT(1)+PHIX(1)*TXT(I))*2.0                      00020920
      SMN=SMN+(PHI(I)*TX(1)+PHI(1)*TX(II))*2.0                          00020930
      SMT=SMT+(PHI(I)*TTH(1)+PHI(1)*TTH(II))*2.0                        00020940
   45 CONTINUE                                                          00020950
C***********************************************************************00020960
C     TEST FOR PRESENCE OF SAME-INDEX COMBINATIONS                     *00020970
C***********************************************************************00020980
   44 IF (MAXSY(M).EQ.0) GO TO 410                                      00020990
C***********************************************************************00021000
C     SET UP INDICES AND COMPILE SUMS                                  *00021010
C***********************************************************************00021020
      I=IJS(M)                                                          00021030
      II=I-1                                                            00021040
      SMF=SMF+TX(I)*PHIX(I)-PHIX(II)*TX(II)                             00021050
      SMS=SMS+TTH(I)*PHIT(I)+PHIT(II)*TTH(II)                           00021060
      SMV=SMV-PHIT(I)*TXT(I)+PHIT(II)*TXT(II)                           00021070
      SME=SME+PHIX(I)*TXT(I)+PHIX(II)*TXT(II)                           00021080
      SMN=SMN+TX(I)*PHI(I)+PHI(II)*TX(II)                               00021090
      SMT=SMT+TTH(I)*PHI(I)+PHI(II)*TTH(II)                             00021100
      GO TO 410                                                         00021110
C***********************************************************************00021120
C     HERE WE HANDLE CASES WHERE N(M)=0                                *00021130
C***********************************************************************00021140
  420 DO 421 L=1,MNMAXO                                                 00021150
      SMF=SMF+TX(L)*PHIX(L)                                             00021160
      SMV=SMV+TXT(L)*PHIT(L)                                            00021170
  421 CONTINUE                                                          00021180
      DO 422 L=3,MNMAXO,2                                               00021190
      LL=L-1                                                            00021200
      SMS=SMS+PHIT(LL)*TTH(L)+PHIT(L)*TTH(LL)                           00021210
      SME=SME+PHIX(L)*TXT(LL)+PHIX(LL)*TXT(L)                           00021220
      SMN=SMN+PHI(LL)*TX(L)+PHI(L)*TX(LL)                               00021230
      SMT=SMT+PHI(LL)*TTH(L)+PHI(L)*TTH(LL)                             00021240
  422 CONTINUE                                                          00021250
      SMF=SMF+TX(1)*PHIX(1)                                             00021260
      SMS=SMS+TTH(1)*PHIT(1)*2.0                                        00021270
      SMV=SMV+TXT(1)*PHIT(1)                                            00021280
      SME=SME+TXT(1)*PHIX(1)*2.0                                        00021290
      SMN=SMN+TX(1)*PHI(1)*2.0                                          00021300
      SMT=SMT+TTH(1)*PHI(1)*2.0                                         00021310
      GO TO 410                                                         00021320
C***********************************************************************00021330
C                                                                      *00021340
C     THIS SECTION HANDLES ASYMMETRIC MODE COMBINATIONS                *00021350
```

```
C                                                                      C00021360
C***********************************************************************00021370
  101 MF=M+1                                                            00021380
      MAXL=MAXS(MP)                                                     00021390
C***********************************************************************00021400
C     TEST FOR PRESENCE OF SUMMATION COMBINATIONS                      *00021410
C***********************************************************************00021420
      IF (MAXL.EQ.0) GO TO 102                                          00021430
C***********************************************************************00021440
C     SET UP COUPLING INDICES AND TEST FOR MODE 1                      *00021450
C***********************************************************************00021460
      DO 103 L=1,MAXL                                                   00021470
      I=IS(L,MP)                                                        00021480
      J=JS(L,MP)                                                        00021490
      II=I-1                                                            00021500
      JJ=J-1                                                            00021510
      IF (I.EQ.1) GO TO 103                                             00021520
C***********************************************************************00021530
C     COMPILE SUMS FOR ASYMMETRIC SUMMATION COMBINATIONS               *00021540
C***********************************************************************00021550
      SMF=SMF+PHIX(I)*TX(JJ)+PHIX(J)*TX(II)+PHIX(II)*TX(J)              00021560
     1         +PHIX(JJ)*TX(I)                                          00021570
      SMS=SMS-PHIT(I)*TTH(JJ)-PHIT(J)*TTH(II)+PHIT(II)*TTH(J)           00021580
     1         +PHIT(JJ)*TTH(I)                                         00021590
      SMV=SMV+PHIT(I)*TXT(JJ)+PHIT(J)*TXT(II)+PHIT(II)*TXT(J)           00021600
     1         +PHIT(JJ)*TXT(I)                                         00021610
      SME=SME+PHIX(I)*TXT(JJ)+PHIX(J)*TXT(II)-PHIX(II)*TXT(J)           00021620
     1         -PHIX(JJ)*TXT(I)                                         00021630
      SMN=SMN-PHI(I)*TX(JJ)-PHI(J)*TX(II)+PHI(II)*TX(J)                 00021640
     1         +PHI(JJ)*TX(I)                                           00021650
      SMT=SMT-PHI(I)*TTH(JJ)-PHI(J)*TTH(II)+PHI(II)*TTH(J)              00021660
     1         +PHI(JJ)*TTH(I)                                          00021670
  103 CONTINUE                                                          00021680
C***********************************************************************00021690
C     TEST FOR PRESENCE OF DIFFERENCE COMBINATIONS                     *00021700
C***********************************************************************00021710
  102 MAXL=MAXD(MP)                                                     00021720
      IF (MAXL.EQ.0) GO TO 104                                          00021730
C***********************************************************************00021740
C     SET UP COUPLING MODES- INDICES AND TEST FOR MODE 1               *00021750
C***********************************************************************00021760
      DO 105 L=1,MAXL                                                   00021770
      I=ID(L,MP)                                                        00021780
      J=JD(L,MP)                                                        00021790
      II=I-1                                                            00021800
      JJ=J-1                                                            00021810
      IF (J.EQ.1) GO TO 123                                             00021820
C***********************************************************************00021830
```

```
C     COMPILE SUMS FOR ASYMMETRIC DIFFERENCE COMBINATIONS              *
C***********************************************************************
      SMF=SMF-PHIX(I)*TX(JJ)+PHIX(J)*TX(II)+PHIX(II)*TX(J)
     1      -PHIX(JJ)*TX(I)
      SMS=SMS+PHIT(I)*TTH(JJ)+PHIT(J)*TTH(II)+PHIT(II)*TTH(J)
     1      +PHIT(JJ)*TTH(I)
      SMV=SMV+PHIT(I)*TXT(JJ)+PHIT(J)*TXT(II)+PHIT(II)*TXT(J)
     1      +PHIT(JJ)*TXT(I)
      SME=SME+PHIX(I)*TXT(JJ)+PHIX(J)*TXT(II)+PHIX(II)*TXT(J)
     1      +PHIX(JJ)*TXT(I)
      SMN=SMN+PHI(I)*TX(JJ)+PHI(J)*TX(II)+PHI(II)*TX(J)
     1      +PHI(JJ)*TX(I)
      SMT=SMT+PHI(I)*TTH(JJ)+PHI(J)*TTH(II)+PHI(II)*TTH(J)
     1      +PHI(JJ)*TTH(I)
      GO TO 105
C***********************************************************************
C     EXECUTE BELOW IF J=1 IN DIFF-COMB (OR I=1 IN SUM-COMB)          *
C***********************************************************************
  123 SMF=SMF+(PHIX(1)*TX(II)+PHIX(II)*TX(1))*2.0
      SMS=SMS+(PHIT(1)*TTH(I)+PHIT(II)*TTH(1))*2.0
      SMV=SMV+(PHIT(I)*TXT(1)+PHIT(1)*TXT(I))*2.0
      SME=SME+(PHIX(1)*TXT(II)+PHIX(I)*TXT(1))*2.0
      SMN=SMN+(PHI(1)*TX(I)+PHI(II)*TX(1))*2.0
      SMT=SMT+(PHI(1)*TTH(I)+PHI(II)*TTH(1))*2.0
  105 CONTINUE
C***********************************************************************
C     TEXT FOR PRESENCE OF SAME-INDEX COMBINATION                      *
C***********************************************************************
  104 IF (MAXSY(MP).EQ.0) GO TO 410
C***********************************************************************
C     SET UP COUPLING MODES- INDICES AND COMPILE SUMS                  *
C***********************************************************************
      I=IJS(MP)
      II=I-1
      SMF=SMF+PHIX(I)*TX(II)+PHIX(II)*TX(I)
      SMS=SMS-PHIT(I)*TTH(II)+PHIT(II)*TTH(I)
      SMV=SMV+PHIT(I)*TXT(II)+PHIT(II)*TXT(I)
      SME=SME+PHIX(I)*TXT(II)-PHIX(II)*TXT(I)
      SMN=SMN-PHI(I)*TX(II)+PHI(II)*TX(I)
      SMT=SMT-PHI(I)*TTH(II)+PHI(II)*TTH(I)
  410 CONTINUE
C***********************************************************************
C     PREPARE -AETA- TERMS                                             *
C***********************************************************************
      EXX3(M)=SMF*0.5
      ETT3(M)=SMS*0.5
      ETX3(M)=SMV*0.5
      EXT3(M)=SME*0.5
```

```
      EX3(M) =SMN*0.5                                                   00022320
      ET3(M) =SMT*0.5                                                   00022330
   49 CONTINUE                                                          00022340
 2222 CONTINUE                                                          00022350
C***********************************************************************00022360
C     UP-DATE U,V,W AND RETURN                                         *00022370
C***********************************************************************00022380
      DO 30 M=1,MNMAXO                                                  00022390
      U1(M)=U2(M)                                                       00022400
      V1(M)=V2(M)                                                       00022410
      W1(M)=W2(M)                                                       00022420
      U2(M)=U3(M)                                                       00022430
      V2(M)=V3(M)                                                       00022440
   30 W2(M)=W3(M)                                                       00022450
      RETURN                                                            00022460
      END                                                               00022470
      BLOCK DATA
      COMMON /BL27/ BX3      ,BT3      ,BXT3     ,BE3
      COMMON /BL28/ EXX3     ,ETT3     ,ETX3     ,EXT3     ,EX3      ,ET3
      COMMON /BL29/ BX1      ,BT1      ,BXT1     ,BE1      ,BX2      ,BT2     ,
     1              BXT2     ,BE2
      COMMON /BL30/ EXX1     ,ETT1     ,ETX1     ,EX1      ,ET1      ,EXX2     ,
     1              ETT2     ,ETX2     ,EXT2     ,EX2      ,ET2
      COMMON /BL31/ DELSQ,EXT1
      REAL BX3(99)/99*0./,BT3(99)/99*0./,BXT3(99)/99*0./,BE3(99)/99*0./,
     1EXX3(99)/99*0./,ETT3(99)/99*0./,ETX3(99)/99*0./,EXT3(99)/99*0./,
     2EX3(99)/99*0./,ET3(99)/99*0./,BX1(99)/99*0./,BT1(99)/99*0./,
     3BXT1(99)/99*0./,BE1(99)/99*0./,BX2(99)/99*0./,BT2(99)/99*0./,
     4BXT2(99)/99*0./,BE2(99)/99*0./,EXX1(99)/99*0./,ETT1(99)/99*0./,
     5ETX1(99)/99*0./,EX1(99)/99*0./,ET1(99)/99*0./,EXX2(99)/99*0./,
     6ETT2(99)/99*0./,ETX2(99)/99*0./,EXT2(99)/99*0./,EX2(99)/99*0./,
     7ET2(99)/99*0./,DELSQ/1*0./,EXT1(99)/99*0./
      END
//GO.SYSIN DD *

DATA CARDS GO HERE
```

APPENDIX B

LISTING OF OUTPUT FROM EXAMPLE PROBLEM

```
                                      --PROBLEM NUMBER     1--

                                LMSC TEST CASE, IMPULSIVELY LOADED CONE

                                        --INPUT DATA RECORD--
    THE BOUNDARY CONDITIONS ARE:

        AT THE INITIAL EDGE
  ---------------OMEGA BAR---------------          ----------------LAMDA BAR---------------            ---FL-----
  ( 0.0        0.0        0.0        0.0        )  NS        ( 0.100E 01 0.0        0.0        0.0        )  U         0.0
  ( 0.0        0.0        0.0        0.0        )  NST   +   ( 0.0        0.100E 01 0.0        0.0        )  V    =    0.0
  ( 0.0        0.0        0.0        0.0        )  QS        ( 0.0        0.0        0.100E 01 0.0        )  W         0.0
  ( 0.0        0.0        0.0        0.100E 01)  PHIS      ( 0.0        0.0        0.0        0.0        )  MS        0.0
        AT THE FINAL EDGE
  ---------------OMEGA BAR----------------          ----------------LAMDA BAR---------------            ---FL-----
  ( 0.0        0.0        0.0        0.0        )  NS        ( 0.100E 01 0.0        0.0        0.0        )  U         0.0
  ( 0.0        0.0        0.0        0.0        )  NST   +   ( 0.0        0.100E 01 0.0        0.0        )  V    =    0.0
  ( 0.0        0.0        0.0        0.0        )  QS        ( 0.0        0.0        0.100E 01 0.0        )  W         0.0
  ( 0.0        0.0        0.0        0.100E 01)  PHIS      ( 0.0        0.0        0.0        0.0        )  MS        0.0


    NUMBER OF STATIONS---------------------- 31
    NUMBER OF MODES------------------------- 4
    INCREMENTAL TIME------------------------.1824E-01
    MAXIMUM NUMBER OF TIME STEPS------------ 750
    MAXIMUM NUMBER OF ITERATIONS------------ 20
    CONVERGENCE CRITERION-------------------0.0100

    CHARACTERISTIC SHELL DIMENSION----------  0.1592E 02
    REFERENCE THICKNESS---------------------  0.5430E 00
    REFERENCE ELASTICITY--------------------  0.3520E 07
    REFERENCE STRESS------------------------  0.1000E 04
    REFERENCE TIME--------------------------  0.1095E-03
    POISSONS RATIO---------------------  0.2860E 00

              CIRCUMFERENTIAL COORDINATES FOR THE PRINT RECORD, IN RADIAN MEASURE, ARE:
        0.0            3.1415920258

              THE DATA PRINTED IS DIMENSIONAL
        EXECUTING IN SUBROUTINE "DYNAMIC"
```

```
STATION        RADIUS        GAMMA         OMEGA S       OMEGA THETA    DEOMEGA S     MASS

   1          0.7950E 01    0.1912E-01    0.0           0.1243E 00     0.0           0.1021E-03
   2          0.8026E 01    0.1893E-01    0.0           0.1231E 00     0.0           0.1021E-03
   3          0.8102E 01    0.1876E-01    0.0           0.1220E 00     0.0           0.1021E-03
   4          0.8178E 01    0.1858E-01    0.0           0.1209E 00     0.0           0.1021E-03
   5          0.8254E 01    0.1841E-01    0.0           0.1197E 00     0.0           0.1021E-03
   6          0.8330E 01    0.1824E-01    0.0           0.1187E 00     0.0           0.1021E-03
   7          0.8406E 01    0.1808E-01    0.0           0.1176E 00     0.0           0.1021E-03
   8          0.8482E 01    0.1792E-01    0.0           0.1165E 00     0.0           0.1021E-03
   9          0.8558E 01    0.1776E-01    0.0           0.1155E 00     0.0           0.1021E-03
  10          0.8634E 01    0.1760E-01    0.0           0.1145E 00     0.0           0.1021E-03
  11          0.8710E 01    0.1745E-01    0.0           0.1135E 00     0.0           0.1021E-03
  12          0.8786E 01    0.1730E-01    0.0           0.1125E 00     0.0           0.1021E-03
  13          0.8862E 01    0.1715E-01    0.0           0.1115E 00     0.0           0.1021E-03
  14          0.8938E 01    0.1700E-01    0.0           0.1106E 00     0.0           0.1021E-03
  15          0.9014E 01    0.1686E-01    0.0           0.1097E 00     0.0           0.1021E-03
  16          0.9090E 01    0.1672E-01    0.0           0.1087E 00     0.0           0.1021E-03
  17          0.9166E 01    0.1658E-01    0.0           0.1078E 00     0.0           0.1021E-03
  18          0.9242E 01    0.1644E-01    0.0           0.1069E 00     0.0           0.1021E-03
  19          0.9319E 01    0.1631E-01    0.0           0.1061E 00     0.0           0.1021E-03
  20          0.9394E 01    0.1618E-01    0.0           0.1052E 00     0.0           0.1021E-03
  21          0.9470E 01    0.1605E-01    0.0           0.1044E 00     0.0           0.1021E-03
  22          0.9546E 01    0.1592E-01    0.0           0.1035E 00     0.0           0.1021E-03
  23          0.9622E 01    0.1579E-01    0.0           0.1027E 00     0.0           0.1021E-03
  24          0.9698E 01    0.1567E-01    0.0           0.1019E 00     0.0           0.1021E-03
  25          0.9774E 01    0.1555E-01    0.0           0.1011E 00     0.0           0.1021E-03
  26          0.9850E 01    0.1543E-01    0.0           0.1003E 00     0.0           0.1021E-03
  27          0.9926E 01    0.1531E-01    0.0           0.9958E-01     0.0           0.1021E-03
  28          0.1000E 02    0.1519E-01    0.0           0.9882E-01     0.0           0.1021E-03
  29          0.1008E 02    0.1508E-01    0.0           0.9807E-01     0.0           0.1021E-03
  30          0.1015E 02    0.1497E-01    0.0           0.9734E-01     0.0           0.1021E-03
  31          0.1023E 02    0.1485E-01    0.0           0.9662E-01     0.0           0.1021E-03


          STATION        B STIFFNESS       D STIFFNESS       B PRIME          D PRIME

             1          0.208163E 07      0.511471E 05      0.0              0.0
             2          0.208163E 07      0.511471E 05      0.0              0.0
             3          0.208163E 07      0.511471E 05      0.0              0.0
             4          0.208163E 07      0.511471E 05      0.0              0.0
             5          0.208163E 07      0.511471E 05      0.0              0.0
             6          0.208163E 07      0.511471E 05      0.0              0.0
             7          0.208163E 07      0.511471E 05      0.0              0.0
             8          0.208163E 07      0.511471E 05      0.0              0.0
             9          0.208163E 07      0.511471E 05      0.0              0.0
            10          0.208163E 07      0.511471E 05      0.0              0.0
            11          0.208163E 07      0.511471E 05      0.0              0.0
            12          0.208163E 07      0.511471E 05      0.0              0.0
            13          0.208163E 07      0.511471E 05      0.0              0.0
            14          0.208163E 07      0.511471E 05      0.0              0.0
            15          0.208163E 07      0.511471E 05      0.0              0.0
            16          0.208163E 07      0.511471E 05      0.0              0.0
            17          0.208163E 07      0.511471E 05      0.0              0.0
            18          0.208163E 07      0.511471E 05      0.0              0.0
            19          0.208163E 07      0.511471E 05      0.0              0.0
            20          0.208163E 07      0.511471E 05      0.0              0.0
            21          0.208163E 07      0.511471E 05      0.0              0.0
            22          0.208163E 07      0.511471E 05      0.0              0.0
            23          0.208163E 07      0.511471E 05      0.0              0.0
            24          0.208163E 07      0.511471E 05      0.0              0.0
            25          0.208163E 07      0.511471E 05      0.0              0.0
            26          0.208163E 07      0.511471E 05      0.0              0.0
            27          0.208163E 07      0.511471E 05      0.0              0.0
            28          0.208163E 07      0.511471E 05      0.0              0.0
            29          0.208163E 07      0.511471E 05      0.0              0.0
            30          0.208163E 07      0.511471E 05      0.0              0.0
            31          0.208163E 07      0.511471E 05      0.0              0.0
```

```
THE INITIAL CONDITIONS FOR N=  0  FOLLOW

     STATION        U              V              W              M S

        1          0.0            0.0            0.0            0.0
        2          0.0            0.0            0.0            0.0
        3          0.0            0.0            0.0            0.0
        4          0.0            0.0            0.0            0.0
        5          0.0            0.0            0.0            0.0
        6          0.0            0.0            0.0            0.0
        7          0.0            0.0            0.0            0.0
        8          0.0            0.0            0.0            0.0
        9          0.0            0.0            0.0            0.0
       10          0.0            0.0            0.0            0.0
       11          0.0            0.0            0.0            0.0
       12          0.0            0.0            0.0            0.0
       13          0.0            0.0            0.0            0.0
       14          0.0            0.0            0.0            0.0
       15          0.0            0.0            0.0            0.0
       16          0.0            0.0            0.0            0.0
       17          0.0            0.0            0.0            0.0
       18          0.0            0.0            0.0            0.0
       19          0.0            0.0            0.0            0.0
       20          0.0            0.0            0.0            0.0
       21          0.0            0.0            0.0            0.0
       22          0.0            0.0            0.0            0.0
       23          0.0            0.0            0.0            0.0
       24          0.0            0.0            0.0            0.0
       25          0.0            0.0            0.0            0.0
       26          0.0            0.0            0.0            0.0
       27          0.0            0.0            0.0            0.0
       28          0.0            0.0            0.0            0.0
       29          0.0            0.0            0.0            0.0
       30          0.0            0.0            0.0            0.0
       31          0.0            0.0            0.0            0.0

     STATION        U DOT          V DOT          W DOT          M S DOT

        1          0.0            0.0            0.0            0.0
        2          0.0            0.0          -0.141355E 04    0.0
        3          0.0            0.0          -0.141355E 04    0.0
        4          0.0            0.0          -0.141355E 04    0.0
        5          0.0            0.0          -0.141355E 04    0.0
        6          0.0            0.0          -0.141355E 04    0.0
        7          0.0            0.0          -0.141355E 04    0.0
        8          0.0            0.0          -0.141355E 04    0.0
        9          0.0            0.0          -0.141355E 04    0.0
       10          0.0            0.0          -0.141355E 04    0.0
       11          0.0            0.0          -0.141355E 04    0.0
       12          0.0            0.0          -0.141355E 04    0.0
       13          0.0            0.0          -0.141355E 04    0.0
       14          0.0            0.0          -0.141355E 04    0.0
       15          0.0            0.0          -0.141355E 04    0.0
       16          0.0            0.0          -0.141355E 04    0.0
       17          0.0            0.0          -0.141355E 04    0.0
       18          0.0            0.0          -0.141355E 04    0.0
       19          0.0            0.0          -0.141355E 04    0.0
       20          0.0            0.0          -0.141355E 04    0.0
       21          0.0            0.0          -0.141355E 04    0.0
       22          0.0            0.0          -0.141355E 04    0.0
       23          0.0            0.0          -0.141355E 04    0.0
       24          0.0            0.0          -0.141355E 04    0.0
       25          0.0            0.0          -0.141355E 04    0.0
       26          0.0            0.0          -0.141355E 04    0.0
       27          0.0            0.0          -0.141355E 04    0.0
       28          0.0            0.0          -0.141355E 04    0.0
       29          0.0            0.0          -0.141355E 04    0.0
       30          0.0            0.0          -0.141355E 04    0.0
       31          0.0            0.0            0.0            0.0
```

```
THE INITIAL CONDITIONS FOR N=  1  FOLLOW

       STATION         U                V                W                M S

          1           0.0              0.0              0.0              0.0
          2           0.0              0.0              0.0              0.0
          3           0.0              0.0              0.0              0.0
          4           0.0              0.0              0.0              0.0
          5           0.0              0.0              0.0              0.0
          6           0.0              0.0              0.0              0.0
          7           0.0              0.0              0.0              0.0
          8           0.0              0.0              0.0              0.0
          9           0.0              0.0              0.0              0.0
         10           0.0              0.0              0.0              0.0
         11           0.0              0.0              0.0              0.0
         12           0.0              0.0              0.0              0.0
         13           0.0              0.0              0.0              0.0
         14           0.0              0.0              0.0              0.0
         15           0.0              0.0              0.0              0.0
         16           0.0              0.0              0.0              0.0
         17           0.0              0.0              0.0              0.0
         18           0.0              0.0              0.0              0.0
         19           0.0              0.0              0.0              0.0
         20           0.0              0.0              0.0              0.0
         21           0.0              0.0              0.0              0.0
         22           0.0              0.0              0.0              0.0
         23           0.0              0.0              0.0              0.0
         24           0.0              0.0              0.0              0.0
         25           0.0              0.0              0.0              0.0
         26           0.0              0.0              0.0              0.0
         27           0.0              0.0              0.0              0.0
         28           0.0              0.0              0.0              0.0
         29           0.0              0.0              0.0              0.0
         30           0.0              0.0              0.0              0.0
         31           0.0              0.0              0.0              0.0

       STATION         U DOT            V DOT            W DOT            M S DOT

          1           0.0              0.0              0.0              0.0
          2           0.0              0.0            -0.222040E 04      0.0
          3           0.0              0.0            -0.222040E 04      0.0
          4           0.0              0.0            -0.222040E 04      0.0
          5           0.0              0.0            -0.222040E 04      0.0
          6           0.0              0.0            -0.222040E 04      0.0
          7           0.0              0.0            -0.222040E 04      0.0
          8           0.0              0.0            -0.222040E 04      0.0
          9           0.0              0.0            -0.222040E 04      0.0
         10           0.0              0.0            -0.222040E 04      0.0
         11           0.0              0.0            -0.222040E 04      0.0
         12           0.0              0.0            -0.222040E 04      0.0
         13           0.0              0.0            -0.222040E 04      0.0
         14           0.0              0.0            -0.222040E 04      0.0
         15           0.0              0.0            -0.222040E 04      0.0
         16           0.0              0.0            -0.222040E 04      0.0
         17           0.0              0.0            -0.222040E 04      0.0
         18           0.0              0.0            -0.222040E 04      0.0
         19           0.0              0.0            -0.222040E 04      0.0
         20           0.0              0.0            -0.222040E 04      0.0
         21           0.0              0.0            -0.222040E 04      0.0
         22           0.0              0.0            -0.222040E 04      0.0
         23           0.0              0.0            -0.222040E 04      0.0
         24           0.0              0.0            -0.222040E 04      0.0
         25           0.0              0.0            -0.222040E 04      0.0
         26           0.0              0.0            -0.222040E 04      0.0
         27           0.0              0.0            -0.222040E 04      0.0
         28           0.0              0.0            -0.222040E 04      0.0
         29           0.0              0.0            -0.222040E 04      0.0
         30           0.0              0.0            -0.222040E 04      0.0
         31           0.0              0.0              0.0              0.0
```

```
THE INITIAL CONDITIONS FOR N=  2  FOLLOW

          STATION          U                    V                    W                    M S

             1             0.0                  0.0                  0.0                  0.0
             2             0.0                  0.0                  0.0                  0.0
             3             0.0                  0.0                  0.0                  0.0
             4             0.0                  0.0                  0.0                  0.0
             5             0.0                  0.0                  0.0                  0.0
             6             0.0                  0.0                  0.0                  0.0
             7             0.0                  0.0                  0.0                  0.0
             8             0.0                  0.0                  0.0                  0.0
             9             0.0                  0.0                  0.0                  0.0
            10             0.0                  0.0                  0.0                  0.0
            11             0.0                  0.0                  0.0                  0.0
            12             0.0                  0.0                  0.0                  0.0
            13             0.0                  0.0                  0.0                  0.0
            14             0.0                  0.0                  0.0                  0.0
            15             0.0                  0.0                  0.0                  0.0
            16             0.0                  0.0                  0.0                  0.0
            17             0.0                  0.0                  0.0                  0.0
            18             0.0                  0.0                  0.0                  0.0
            19             0.0                  0.0                  0.0                  0.0
            20             0.0                  0.0                  0.0                  0.0
            21             0.0                  0.0                  0.0                  0.0
            22             0.0                  0.0                  0.0                  0.0
            23             0.0                  0.0                  0.0                  0.0
            24             0.0                  0.0                  0.0                  0.0
            25             0.0                  0.0                  0.0                  0.0
            26             0.0                  0.0                  0.0                  0.0
            27             0.0                  0.0                  0.0                  0.0
            28             0.0                  0.0                  0.0                  0.0
            29             0.0                  0.0                  0.0                  0.0
            30             0.0                  0.0                  0.0                  0.0
            31             0.0                  0.0                  0.0                  0.0

          STATION          U DOT                V DOT                W DOT                M S DOT

             1             0.0                  0.0                  0.0                  0.0
             2             0.0                  0.0                 -0.942366E 03         0.0
             3             0.0                  0.0                 -0.942366E 03         0.0
             4             0.0                  0.0                 -0.942366E 03         0.0
             5             0.0                  0.0                 -0.942366E 03         0.0
             6             0.0                  0.0                 -0.942366E 03         0.0
             7             0.0                  0.0                 -0.942366E 03         0.0
             8             0.0                  0.0                 -0.942366E 03         0.0
             9             0.0                  0.0                 -0.942366E 03         0.0
            10             0.0                  0.0                 -0.942366E 03         0.0
            11             0.0                  0.0                 -0.942366E 03         0.0
            12             0.0                  0.0                 -0.942366E 03         0.0
            13             0.0                  0.0                 -0.942366E 03         0.0
            14             0.0                  0.0                 -0.942366E 03         0.0
            15             0.0                  0.0                 -0.942366E 03         0.0
            16             0.0                  0.0                 -0.942366E 03         0.0
            17             0.0                  0.0                 -0.942366E 03         0.0
            18             0.0                  0.0                 -0.942366E 03         0.0
            19             0.0                  0.0                 -0.942366E 03         0.0
            20             0.0                  0.0                 -0.942366E 03         0.0
            21             0.0                  0.0                 -0.942366E 03         0.0
            22             0.0                  0.0                 -0.942366E 03         0.0
            23             0.0                  0.0                 -0.942366E 03         0.0
            24             0.0                  0.0                 -0.942366E 03         0.0
            25             0.0                  0.0                 -0.942366E 03         0.0
            26             0.0                  0.0                 -0.942366E 03         0.0
            27             0.0                  0.0                 -0.942366E 03         0.0
            28             0.0                  0.0                 -0.942366E 03         0.0
            29             0.0                  0.0                 -0.942366E 03         0.0
            30             0.0                  0.0                 -0.942366E 03         0.0
            31             0.0                  0.0                  0.0                  0.0
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```
THE INITIAL CONDITIONS FOR N=  4  FOLLOW

        STATION         U                  V                  W                 M S

            1          0.0                0.0                0.0                0.0
            2          0.0                0.0                0.0                0.0
            3          0.0                0.0                0.0                0.0
            4          0.0                0.0                0.0                0.0
            5          0.0                0.0                0.0                0.0
            6          0.0                0.0                0.0                0.0
            7          0.0                0.0                0.0                0.0
            8          0.0                0.0                0.0                0.0
            9          0.0                0.0                0.0                0.0
           10          0.0                0.0                0.0                0.0
           11          0.0                0.0                0.0                0.0
           12          0.0                0.0                0.0                0.0
           13          0.0                0.0                0.0                0.0
           14          0.0                0.0                0.0                0.0
           15          0.0                0.0                0.0                0.0
           16          0.0                0.0                0.0                0.0
           17          0.0                0.0                0.0                0.0
           18          0.0                0.0                0.0                0.0
           19          0.0                0.0                0.0                0.0
           20          0.0                0.0                0.0                0.0
           21          0.0                0.0                0.0                0.0
           22          0.0                0.0                0.0                0.0
           23          0.0                0.0                0.0                0.0
           24          0.0                0.0                0.0                0.0
           25          0.0                0.0                0.0                0.0
           26          0.0                0.0                0.0                0.0
           27          0.0                0.0                0.0                0.0
           28          0.0                0.0                0.0                0.0
           29          0.0                0.0                0.0                0.0
           30          0.0                0.0                0.0                0.0
           31          0.0                0.0                0.0                0.0
  ------------------------------------------------------------------------------------------

        STATION        U DOT              V DOT              W DOT              M S DOT

            1          0.0                0.0                0.0                0.0
            2          0.0                0.0                0.188473E 03       0.0
            3          0.0                0.0                0.188473E 03       0.0
            4          0.0                0.0                0.188473E 03       0.0
            5          0.0                0.0                0.188473E 03       0.0
            6          0.0                0.0                0.188473E 03       0.0
            7          0.0                0.0                0.188473E 03       0.0
            8          0.0                0.0                0.188473E 03       0.0
            9          0.0                0.0                0.188473E 03       0.0
           10          0.0                0.0                0.188473E 03       0.0
           11          0.0                0.0                0.188473E 03       0.0
           12          0.0                0.0                0.188473E 03       0.0
           13          0.0                0.0                0.188473E 03       0.0
           14          0.0                0.0                0.188473E 03       0.0
           15          0.0                0.0                0.188473E 03       0.0
           16          0.0                0.0                0.188473E 03       0.0
           17          0.0                0.0                0.188473E 03       0.0
           18          0.0                0.0                0.188473E 03       0.0
           19          0.0                0.0                0.188473E 03       0.0
           20          0.0                0.0                0.188473E 03       0.0
           21          0.0                0.0                0.188473E 03       0.0
           22          0.0                0.0                0.188473E 03       0.0
           23          0.0                0.0                0.188473E 03       0.0
           24          0.0                0.0                0.188473E 03       0.0
           25          0.0                0.0                0.188473E 03       0.0
           26          0.0                0.0                0.188473E 03       0.0
           27          0.0                0.0                0.188473E 03       0.0
           28          0.0                0.0                0.188473E 03       0.0
           29          0.0                0.0                0.188473E 03       0.0
           30          0.0                0.0                0.188473E 03       0.0
           31          0.0                0.0                0.0                0.0
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THE TIME STEP NUMBER IS  250      THE TIME IS [illegible] OF 0.500E-03 SECONDS      THE SOLUTION CONVERGED IN  2 ITERATIONS

         THE SUMMED FORCES, MOMENTS, DISPLACEMENTS AND ROTATIONS FOLLOW FOR THETA =    0.0

STATION      N S            N THETA        N STHETA       Q S            M S            M THETA        M STHETA

   1      -0.3459E 04    -0.9571E 03     0.0           -0.2372E 04     0.2386E 03     0.5924E 02     0.0
  14       0.7629E 03     0.2451E 04     0.0            0.2591E 04     0.1838E 04     0.4448E 03     0.0
  27       0.3078E 04    -0.3224E 04     0.0           -0.2360E 04    -0.6155E 03    -0.1715E 03     0.0
  31       0.2631E 04     0.7875E 03     0.0            0.1322E 04    -0.9756E 02    -0.2790E 02     0.0

STATION      U              V              W              PHI S          PHI THETA      PHI

   1       0.0            0.0            0.2249E-09     0.1778E-08     0.0            0.0
  14      -0.6017E-02     0.0            0.1312E 00    -0.3545E-01     0.0            0.0
  27      -0.4079E-02     0.0            0.3927E-01     0.4481E-01     0.0            0.0
  31      -0.1578E-09     0.0           -0.6352E-10    -0.5080E-09     0.0            0.0
         THE SUMMED FORCES, MOMENTS, DISPLACEMENTS AND ROTATIONS FOLLOW FOR THETA =   0.314159E 01

STATION      N S            N THETA        N STHETA       Q S            M S            M THETA        M STHETA

   1       0.4580E 04     0.1275E 04    -0.3960E-02    -0.1934E 04     0.1454E 04     0.4158E 03    -0.1914E-04
  14      -0.6554E 04    -0.3291E 05    -0.1549E-02    -0.2561E 03    -0.8859E 03    -0.3320E 03     0.1056E-03
  27      -0.3568E 04    -0.6111E 04     0.4616E-02     0.3640E 03     0.5826E 03     0.1064E 03    -0.7260E-04
  31      -0.1638E 04    -0.5050E 03     0.3203E-02     0.5499E 03     0.1458E 04     0.4283E 03     0.1140E-04

STATION      U              V              W              PHI S          PHI THETA      PHI

   1       0.0            0.0           -0.4935E-09     0.3810E-08     0.1078E-15    -0.2666E-08
  14       0.5233E-02    -0.3805E-07    -0.2074E 00     0.2529E-01     0.1766E-07    -0.2672E-08
  27       0.2689E-02    -0.1181E-07    -0.4609E-01    -0.3238E-01     0.4166E-08     0.4195E-08
  31       0.3275E-10    -0.4139E-15    -0.3176E-10     0.2540E-09    -0.4097E-16     0.2155E-08
```

APPENDIX C

INPUT DATA GUIDE FOR SATANS-IIA

INPUT DATA GUIDE FOR SATANS-I, SATANS-II, AND SATANS-IIA

CARD	COLUMNS	FORMAT	ITEM	EXAMPLE	MEANING
1	1-72	18A4	TITLE	-	ENTER ANY 72 CHARACTERS
2	1-5	I5	NO	1	THE PROBLEM NUMBER, 0<NO<10000.
2	6-10	L5	$DYNAMC	F T	FOR A STATIC ANALYSIS, SET $DYNAMC = F. FOR A DYNAMIC ANALYSIS, SET $DYNAMC = T.
2	11-15	I5	IMODE	0 1	FOR NO MODAL OUTPUT DATA FOR MODAL OUTPUT DATA.
2	16-20	I5	NDIMEN	0 1	DIMENSIONAL OUTPUT DATA. NONDIMENSIONAL OUTPUT.
2	21-25	I5	NTHMAX	8	SUMMED SOLUTION WILL BE PRINTED AT NTHMAX MERIDIANS, 0<=NTHMAX<=36.
2	26-30	I5	IFREQ	2	SOLUTION WILL BE PRINTED AT THE FIRST STATION, EVERY SUBSEQUENT IFREQ STATION AND THE LAST STATION, 0<IFREQ<=KMAX.
2	31-35	I5	IPRINT	3	EVERY IPRINT CONVERGED SOLUTION WILL BE PRINTED.
2	36-40	I5	IBCINL	-1 0	IF THE SHELL HAS A POLE AT THE FIRST STATION. IF THE SHELL HAS NO POLE AT THE FIRST STATION.
2	41-45	I5	IBCFNL	-1 0	IF THE SHELL HAS A POLE AT THE LAST STATION. IF THE SHELL HAS NO POLE AT THE LAST STATION.

CARD	COLUMNS	FORMAT	ITEM	EXAMPLE	MEANING
2	46-50	I5	KMAX	35	NUMBER OF MERIDIONAL STATIONS. NOTE: KMAX<201 FOR SATANS-I WITHOUT PLOTS AND KMAX<101 FOR SATANS-I WITH PLOTS OR FOR SATANS-II. SATANS-IIA IS UNLIMITED.
2	51-55	I5	MNMAX	7	NUMBER OF SERIES COEFFICIENTS USED TO DESCRIBE THE INITIAL CONDITIONS, PRESSURE AND THERMAL LOADS (AND INITIAL IMPERFECTIONS IF USING SATANS-II OR IIA). MNMAX<=MAXM.
2	56-60	I5	MAXM	7	MAX NUMBER OF HARMONICS IN THE SOLUTION, LIMITED TO 99.
2	61-65	I5	LSMAX	1	FOR A LINEAR ANALYSIS.
				99	USE MANY LOAD STEPS FOR A NONLINEAR STATIC ANALYSIS.
				3000	FOR A DYNAMIC ANALYSIS, LSMAX IS THE NUMBER OF TIME INCREMENTS, WHERE LSMAX= T MAX/ΔT.
2	66-70	I5	LCHMAX	2	THE NUMBER OF LOAD STEP SIZE REDUCTIONS IN A STATIC ANALYSIS, RECOMMENDED RANGE = 2-4.
				0	FOR A DYNAMIC ANALYSIS.
2	71-75	I5	ITRMAX	1	FOR A LINEAR ANALYSIS.
				30	THE NUMBER OF ITERATIONS AT A LOAD OR TIME STEP. FOR A NONLINEAR ANALYSIS, SUGGESTED RANGE = 10-30, UP TO 50 FOR SPECIAL CASES.
2	76-80	I5	IC	0	INITIAL CONDITIONS. SET TO 0 FOR A STATIC ANALYSIS, OR FOR A DYNAMIC ANALYSIS WHERE THE SHELL IS AT REST AT T= 0.
				1	FOR A DYNAMIC ANALYSIS WITH INITIAL CONDITIONS.

CARD	COLUMNS	FORMAT	ITEM	EXAMPLE	MEANING
3	1-12	E12.3	NU	0.3	POISSON'S RATIO, ν.
3	12-24	E12.3	SIGO	1000.0	REFERENCE STRESS LEVEL, σ_0.
				1.0	IF THE INPUT DATA IS DIMENSIONAL.
3	24-36	E12.3	ELAST	.3E8	REFERENCE MODULUS OF ELASTICITY, E_0.
				1.0	IF THE INPUT DATA IS DIMENSIONAL.
3	37-48	E12.3	TKN	.4E-2	REFERENCE THICKNESS, h_0.
				1.0	IF THE INPUT DATA IS DIMENSIONAL.
3	49-60	E12.3	CHAR	8.16	CHARACTERISTIC SHELL DIMENSION, a.
				1.0	IF THE INPUT DATA IS DIMENSIONAL.
3	61-72	E12.3	TEEO	0.0	IF A STATIC ANALYSIS.
				.996E-5	REFERENCE TIME, T_0.

CARD	COLUMNS	FORMAT	ITEM	EXAMPLE	MEANING
4	1-12	E12.3	DELOAD	0.2	FOR A STATIC ANALYSIS, DELOAD IS THE LOAD INCREMENT. IT REMAINS UNCHANGED UNTIL THE SOLUTION FAILS TO CONVERGE IN ITERMAX ITERATIONS, WHEN IT IS REDUCED BY A FACTOR OF FIVE. A MAXIMUM OF LCHMAX SUCH REDUCTIONS WILL OCCUR.
				.1823E-6	FOR A DYNAMIC ANALYSIS, DELOAD IS THE NONDIMENSIONAL TIME INCREMENT.
4	13-24	E12.3	EPS	0.01	THE CONVERGENCE CRITERION RECOMMENDED RANGE OF 0.01<EPS<0.001.

CARD 4A IS ONLY INCLUDED FOR A SATANS-II OR SATANS-IIA RUN.

CARD	COLUMNS	FORMAT	ITEM	EXAMPLE	MEANING
4A	1-5	I5	JUMP	1	FOR AN ANALYSIS USING SINGLE SERIES EXPANSIONS.
				2	FOR AN ANALYSIS USING DOUBLE SERIES EXPANSIONS.
4A	5-10	I5	MPERFS	0	AN ANALYSIS WITHOUT IMPERFECTIONS.
				1	AN ANALYSIS WITH IMPERFECTIONS. NOTE: IF JUMP=2, MPERFS MAY BE 0 OR 1. IF JUMP =1, MPERFS MUST BE 0. IF MPERFS=1, JUMP MUST BE 2.

INCLUDE AS MANY CARDS 5 AS NECESSARY TO SPECIFY NTHMAX MERIDIANS. IF NTHMAX EQUALS 0, OMIT CARD 5.

CARD	COLUMN	FORMAT	ITEM	EXAMPLE	MEANING
5	1-72	6E12.3		10.0	A LIST OF CIRCUMFERENTIAL COORDINATES Θ, IN DEGREES AND TENTHS, WHERE THE SOLUTION PRINTOUT IS DESIRED. THE LIST MUST HAVE NTHMAX ENTRIES.

IF IBCINL= -1, OMIT CARDS 6 THROUGH 14. IF IBCFNL= -1, OMIT CARDS 15 THROUGH 23. CARDS 6 THROUGH 23 DESCRIBE THE BOUNDARY CONDITIONS AT THE FIRST, AND THEN AT THE LAST STATION. THE BOUNDARY CONDITIONS EXIST ON THE TOTAL VARIABLES, NOT ON THE INDIVIDUAL HARMONICS. LOADINGS APPLIED THROUGH SPECIFICATION OF BOUNDARY CONDITIONS ARE TAKEN IN THE ZEROETH HARMONIC (N=0) ONLY, AS THE COLUMN MATRIX $\{\ell\}$ IS SET TO ZERO FOR HARMONICS GREATER THAN ZERO. THE BOUNDARY CONDITIONS ARE DIMENSIONAL. THE FORMAT OF CARDS 6 THROUGH 23 IS 4E16.8.

$$\begin{array}{cccc} \text{CARD 6,15} & \text{CARD 7,16} & \text{CARD 8,17} & \text{CARD 9,18} \end{array}$$

$$\begin{bmatrix} \Omega(1,1) & \Omega(1,2) & \Omega(1,3) & \Omega(1,4) \\ \Omega(2,1) & \Omega(2,2) & \Omega(2,3) & \Omega(2,4) \\ \Omega(3,1) & \Omega(3,2) & \Omega(3,3) & \Omega(3,4) \\ \Omega(4,1) & \Omega(4,2) & \Omega(4,3) & \Omega(4,4) \end{bmatrix} \begin{bmatrix} N_s \\ N_{s\theta} \\ Q_s \\ \beta_s \end{bmatrix} +$$

$$\begin{array}{ccccc} \text{CARD 10,19} & \text{CARD 11,20} & \text{CARD 12,21} & \text{CARD 13,22} & \text{CARD 14,23} \end{array}$$

$$\begin{bmatrix} \Lambda(1,1) & \Lambda(1,2) & \Lambda(1,3) & \Lambda(1,4) \\ \Lambda(2,1) & \Lambda(2,2) & \Lambda(2,3) & \Lambda(2,4) \\ \Lambda(3,1) & \Lambda(3,2) & \Lambda(3,3) & \Lambda(3,4) \\ \Lambda(4,1) & \Lambda(4,2) & \Lambda(4,3) & \Lambda(4,4) \end{bmatrix} \begin{bmatrix} U \\ V \\ W \\ M_s \end{bmatrix} = \begin{bmatrix} \ell(1) \\ \ell(2) \\ \ell(3) \\ \ell(4) \end{bmatrix}$$

CARD 24 IS:

1. INCLUDED FOR A SATANS-I STATIC ANALYSIS.
2. INCLUDED BUT BLANK FOR A SATANS-I DYNAMIC ANALYSIS.
3. OMITTED FOR A SATANS-II ANALYSIS.
4. INCLUDED BLANK FOR DYNAMIC USED FOR STATIC SATANS-IIA ANALYSES.

CARD	COLUMN	FORMAT	ITEM	EXAMPLE	MEANING
24	1-2	L2	$PLOTS	F	INDICATES PLOTS ARE NOT DESIRED.
				T	INDICATES PLOTS ARE DESIRED.
24	3-4	L2	$MODAL	F	INDICATES PLOTS ARE FOR SUMMED SOLUTIONS ONLY.
				T	INDICATES PLOTS ARE FOR MODAL SOLUTIONS ONLY.

FOR THE REMAINDER OF CARD 24 ENTRIES, 0 INDICATES THAT NO PLOTS ARE DESIRED FOR THE PARTICULAR ITEM, AND 1 INDICATES THAT THEY ARE DESIRED. ALL GRAPHS ARE PLOTTED AS THE INDICATED ITEM VERSUS THE STATION NUMBER. IF A COMPLETE PLOT IS DESIRED, INSUTE IFREQ = 1.

CARD	COLUMN	FORMAT	ITEM	EXAMPLE	MEANING
24	5- 6	I2	IRADII	1	PLOT THE RADII AS COMPUTED BY SUBROUTINE GEOM.
24	7- 8	I2	IGAMMA	1	PLOT ρ'/ρ AS COMPUTED BY SUBROUTINE GEOM.
24	9-10	I2	IOMEGS	1	PLOT ω_s AS COMPUTED BY SUBROUTINE GEOM.
24	11-12	I2	IOMEGT	1	PLOT ω_θ AS COMPUTED BY SUBROUTINE GEOM.
24	13-14	I2	IDEOMS	1	PLOT ω_s' AS COMPUTED BY SUBROUTINE GEOM.
24	15-16	I2	IBSTIF	1	PLOT THE STIFFNESS B AS COMPUTED BY SUBROUTINE BDB.
24	17-18	I2	IDSTIF	1	PLOT THE STIFFNESS D AS COMPUTED BY THE SUBROUTINE BDB.
24	19-20	I2	IBBSTF	1	PLOT THE STIFFNESS db/ds AS COMPUTED BY SUBROUTINE BDB.
24	21-22	I2	IDDSTF	1	PLOT THE STIFFNESS dd/ds AS COMPUTED BY SUBROUTINE BDB.
24	23-24	I2	IPR	1	PLOT THE NORMAL COMPONENT OF THE PRESSURE LOAD.
24	25-26	I2	IPS	1	PLOT THE MERIDIONAL COMPONENT OF THE PRESSURE LOAD.
24	27-28	I2	IPT	1	PLOT THE CIRCUMFERENTIAL COMPONENT OF THE PRESSURE LOAD.
24	29-30	I2	ITT	1	PLOT THE THERMAL LOAD.
24	31-32	I2	IMT	1	PLOT THE THERMAL MOMENT.
24	33-34	I2	IDTT	1	PLOT d/ds OF THE THERMAL LOAD.
24	35-36	I2	IDMT	1	PLOT d/ds OF THE THERMAL MOMENT.
24	37-38	I2	INS	1	PLOT THE MERIDIONAL MEMBRANE FORCE DISTRIBUTION.

CARD	COLUMN	FORMAT	ITEM	EXAMPLE	MEANING
24	39-40	I2	INTH	1	PLOT THE CIRCUMFERENTIAL MEMBRANE FORCE DISTRIBUTION.
24	41-42	I2	INSTH	1	PLOT THE MERIDIO-CIRCUMFERENTIAL MEMBRANE FORCE DISTRIBUTION.
24	43-44	I2	IQS	1	PLOT THE TRANSVERSE FORCE DISTRIBUTION.
24	45-46	I2	IMS	1	PLOT THE MERIDIONAL MOMENT DISTRIBUTION.
24	47-48	I2	IMTH	1	PLOT THE CIRCUMFERENTIAL MOMENT DISTRIBUTION.
24	49-50	I2	IMSTH	1	PLOT THE MERIDIO-CIRCUMFERENTIAL MOMENT DISTRIBUTION.
24	51-52	I2	IU	1	PLOT THE MERIDIONAL DISPLACEMENT DISTRIBUTION.
24	53-54	I2	IV	1	PLOT THE CIRCUMFERENTIAL DISPLACEMENT DISTRIBUTION.
24	55-56	I2	IW	1	PLOT THE NORMAL DISPLACEMENT DISTRIBUTION.
24	57-58	I2	IPHIS	1	PLOT THE MERIDIONAL ROTATION DISTRIBUTION.
24	59-60	I2	IPHIT	1	PLOT THE CIRCUMFERENTIAL ROTATION DISTRIBUTION.
24	61-62	I2	IPHI	1	PLOT THE MERIDIO-CIRCUMFERENTIAL ROTATION DISTRIBUTION.

INCERT IMPERFECTION DATA HERE FOR A SATANS-II OR SATANS-IIA ANALYSIS WITH IMPERFECTIONS. INSURE FORMAT OF THE IMPERFECTION DATA IS COMPATIBLE WITH THAT SPECIFIED IN THE USER-WRITTEN SUBROUTINE IMPERF.

25	1-2	I2	IRNAGN	0	INDICATES THES IS THE ONLY RUN.
				1	INDICATES ANOTHER RUN IS TO BE MADE. ADD ANOTHER COMPLETE SET OF DATA CARDS AFTER THIS CARD IS IRNAGN= 1.

APPENDIX D

LISTING OF NEW POLE ROUTINE FOR SATANS-IIA

THE FOLLOWING CARDS ARE TO BE PLACED INTO THE FORCE SUBROUTINE

```
      COMMON /IBL5/IBCINL,IBCFNL
```

```
C    IN FORCE
   10 IF(K.NE.2.OR.(K.EQ.2.AND.IBCINL.GE.0)) GO TO 901
      DO 902 II=1,4
      SUMX=0.
      DO 903 L=1,4
  903 SUMX=SUMX+DL(II,L,M)*GEE(L)
  902 X(II,IK1)=SUMX
  901 CONTINUE
      DO 11 I=1,4
```

THE FOLLOWING CARDS ARE TO BE PLACED INTO THE PMATRX SUBROUTINE

```
C    IN PMATRX
      CALL EFG(2,MN)
      CALL ABC
      CALL MATINV(A,4,G1,0,DETERM,IPIVOT,INDEX,4,ISCALE)
      DO 901 II=1,4
      DO 901 JJ=1,4
      DL(II,JJ,MN)=0.
      DG(II,JJ,MN)=0.
  901 DF(II,JJ,MN)=0.
      IF(NN.GT.1) GO TO 12
      IF(NN.GT.0) GO TO 13
```

```
      M0=MN
      DL(1,1,MN)=1.
      DL(2,2,MN)=1.
      DL(3,3,MN)=-3.
      DL(4,4,MN)=-3.
      DG(3,3,MN)=4.
      DG(4,4,MN)=4.
      DF(3,3,MN)=-1.
      DF(4,4,MN)=-1.
      GO TO 902
   13 M1=MN
      DL(1,1,MN)=-3.
      DL(2,1,MN)=1.
      DL(2,2,MN)=1.
      IF(N(M1).LT.0) DL(2,2,MN)=-1
      DL(3,3,MN)=1.
      DL(4,4,MN)=1.
      DG(1,1,MN)=4.
      DF(1,1,MN)=-1.
      GO TO 902
   12 M2=MN
      DL(1,1,MN)=1.
      DL(2,2,MN)=1.
      DL(3,3,MN)=1.
      DL(4,4,MN)=-3.
      DG(4,4,MN)=4.
      DF(4,4,MN)=-1.
  902 CONTINUE
      DO 903 II=1,4
      DO 903 JJ=1,4
      TTP=0.
      DO 904 L=1,4
  904 TTP=TTP+DF(II,L,MN)*A(L,JJ)
  903 CLO(II,JJ)=TTP
      DO 905 II=1,4
      DO 905 JJ=1,4
      TTP=0.
      TTQ=0.
      DO 906 L=1,4
      TTP=TTP+CLO(II,L)*C(L,JJ)
  906 TTQ=TTQ+CLO(II,L)*BEE(L,JJ)
      CL1(II,JJ)=DL(II,JJ,MN)-TTP
  905 CL2(II,JJ)=DG(II,JJ,MN)-TTQ
      CALL MATINV(CL1,4,G1,0,DETERM,IPIVOT,INDEX,4,ISCALE)
      DO 907 II=1,4
      DO 907 JJ=1,4
      TTP=0.
      TTQ=0.
```

```
      DO 908 L=1,4
      TTP=TTP+CL1(II,L)*CL0(L,JJ)
  908 TTQ=TTQ+CL1(II,L)*CL2(L,JJ)
      CL(II,JJ,MA)=-TTP
  907 P(II,JJ,IJ)=TTQ
      GO TO 11
   90 M3=MN
```

APPENDIX E

LISTING OF CARDS FOR $\bar{V}$ AND $\bar{V}_{MAX}$

THE FOLLOWING CARDS ARE TO BE PLACED INTO THE DYNAMIC SUBROUTINE IF NEEDED

```
C     STATEMENTS FOR MAIN TO CALCULATE VBAR
  185 DENOM=.125*GMXI(KMAX)*R(KMAX)**4
      DO 186 M=1,MAXM
      DNUM=0.
      MM=(M-1)*KMAX2
      DO 184 K=2,KL
      KT=K+1+MM
  184 DNUM=DNUM+Z(3,KT)*R(K)
      DNUM=DNUM*DEL*SOE
  186 VBAR(M)=DNUM/DENOM
      ITTEST=ITTEST+1
      IF(ITTEST.NE.10) GO TO 963
      ITTEST=0
      WRITE(6,183)(LSTEP,(VBAR(M),M=1,MAXM))
  183 FORMAT(/5X,'VBAR AT TIME STEP ',I4,' FOR EACH MODE IS'/5E16.4)
  963 CONTINUE
      DO 187 M=1,MAXM
      IF(LSTEP.EQ.1) AVB(M)=0.
  187 IF(ABS(VBAR(M)).GT.AVB(M)) AVB(M)=ABS(VBAR(M))
```

LIST OF FIGURES AND TABLES

A. FIGURES

B. TABLES

LIST OF REFERENCES

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