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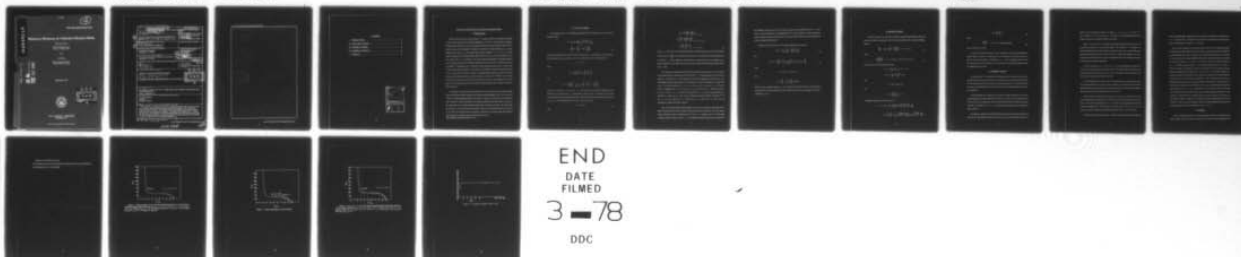
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NRL Memorandum Report 3614

Runaway Electrons In Collective Electric Fields

BERTRAM H. HUI

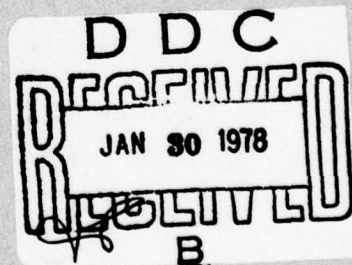
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RUNAWAY ELECTRONS IN COLLECTIVE ELECTRIC FIELDS

I INTRODUCTION

Recently, there have been numerous reports¹⁻⁶ of runaway electrons in tokamaks. The energy of runaway electrons observed in low density discharges ($n \leq 10^{13} \text{ cm}^{-3}$) is lower than that observed in higher density discharges. It has also been observed that the synchrotron radiation power often increases in steps, and is accompanied by radiation near and below the plasma frequency (ω_{pe}). As first pointed out by Coppi et. al.,⁷ the reduced plasma frequency radiation ($\omega_k = k_{||} / k \omega_{pe}$) in Alcator could be explained by an anomalous Doppler shifted mode,⁸ where ω_k is the wave frequency, k is the wave number, and $k_{||}$ is its component in the toroidal magnetic field direction. Pitch-angle scattering of the runaway electrons by the anomalous-Doppler-shifted mode can lead to an increase of synchrotron radiation.^{5,9} Papadopoulos et al.¹⁰ also show that pitch-angle scattering can cause a bump to form on the tail of the electron distribution. The bump-on-tail instability will then be excited and give rise to the ω_{pe} mode which is observed. Moreover, anomalous-Doppler-shifted and bump-on-tail modes may cause many runaway electrons to become trapped in local mirrors,¹¹ ∇B drift to the wall of the vacuum vessel, and destroy its liner. Such liner destruction may have been observed by the TFR group.² The macroscopic behavior of the anomalous-Doppler-shifted mode is described in detail by Choi and Horton.¹²

In this paper, we study the interactions between the runaway electrons and the collective modes using a Fokker-Planck model including a self-consistent quasilinear diffusion term. First, we show that if only the anomalous-Doppler-shifted mode is present, it gives rise to the bump-on-tail distribution. This is because of a velocity threshold for the anomalous-Doppler-shifted mode. Second, we show that the combination of the anomalous-Doppler-shifted mode, the bump-on-tail mode and a weak toroidal electric field $E_{||}$, can lead to synchrotron radiation similar to that experimentally observed. In section II, we review the analytical theory. In section III, we present the numerical model. The results are given in section IV, and these results are summarized in section V.

Note: Manuscript submitted September 14, 1977.

II ANALYTICAL MODEL

For electrostatic waves in a homogeneous magnetic field with immobile ions, we use the Harris dispersion relation:

$$k^2 = \omega_{pe}^2 \int dv \sum_l \frac{J_l^2(k_\perp v_\perp / \omega_{ce})}{k_\parallel v_\parallel - \omega_k - l\omega_{ce}} \times \left[k_\parallel v_\parallel \frac{\partial f_{oe}}{\partial v_\parallel^2} - l\omega_{ce} \frac{\partial f_{oe}}{\partial v_\perp^2} \right], \quad (1)$$

where J_l is the Bessel function of the first kind of order l , and ω_{ce} is the electron cyclotron frequency.

The initial distribution f_{oe} is given by a sum of a bulk equilibrium and a "tail" Maxwellian; i.e.,

$$f_{oe} = f_o + f_T,$$

where

$$f_o = n_o \left(\frac{m_e}{2\pi T_e} \right)^{3/2} \exp \left(-\frac{m_e v^2}{2T_e} \right),$$

and

$$f_T = n_T \left(\frac{m_e}{2\pi} \right)^{3/2} \frac{1}{T_{\perp T} T_{\parallel T}^{1/2}} \exp \left(-\frac{m_e v_\perp^2}{2T_{\perp T}} - \frac{m_e v_\parallel^2}{2T_{\parallel T}} \right),$$

with $n_T \ll n_o$ and $T_{\parallel T} \gg T_{\perp T}$ and $T_e \approx T_{\perp T}$. We expect that the dominant contributions to the growth rate γ_k^A come from $l = 0, -1$ gyroresonances because the $l = +1$ resonance is at the negative velocity side where the distribution function is relatively small. Solving the dispersion relation with $k_\perp v_\perp / \omega_{ce} \ll 1$ and keeping only the $l = 0$ and -1 terms, we obtain:

$$\omega_k \approx k_\parallel / k \omega_{pe} \quad (2)$$

and,

$$\begin{aligned}
\gamma_k^A \approx & \frac{\pi}{2} \frac{\omega_{pe}^3 k_{||}}{k^3} \frac{\partial \hat{f}_0}{\partial v_{||}} \bigg|_{v_{||} = \omega_k/k_{||}} \\
& + \frac{\pi}{4} \frac{k_{||}^3}{k^3} \frac{\omega_{pe}^3 v_{th\perp}^2}{\omega_{ce}^2} \frac{\partial \hat{f}_T}{\partial v_{||}} \bigg|_{v_{||} = (\omega_k + \omega_{ce})/k_{||}} \\
& + \frac{\pi}{4} \frac{k_{\perp}^2}{k^3} \frac{\omega_{pe}^3}{\omega_{ce}} \hat{f}_T \bigg|_{v_{||} = (\omega_k + \omega_{ce})/k_{||}}, \quad (3)
\end{aligned}$$

where $v_{th\perp} = (2T_e/m_e)^{1/2}$ is the perpendicular velocity of the bulk and also the tail of the distribution function, and $\hat{f} \equiv 2\pi \int_0^\infty dv_{\perp} v_{\perp} f$. The first and second term of (3) correspond to Landau damping by the $\ell = 0$ and $\ell = -1$ terms respectively. The third term is the driving term for the instability and is directly proportional to the density of the tail. The most unstable anomalous-Doppler-shifted mode¹³ has $k_{\perp} = \sqrt{2}k_{||}$.

Let us examine the circumstances under which these modes become important. We can estimate the resonance width in velocity space of the $\ell = 0$ and $\ell = -1$ resonances, given the maximum tail velocity v_m . In order for $\gamma_k^A > 0$, the third term of (3) has to be, bigger than the first term, i.e. Landau damping (the second term usually is not as important). To avoid Landau damping, we usually need $\omega_k/k_{||} > 3v_{th}$. But at resonance, $v_m = (\omega_{ce} + \omega_k)/k_{||}$, so $\omega_k/k_{||} \leq \omega_k v_m / (\omega_{ce} + \omega_k)$. Thus for the $\ell = 0$ resonance, $3v_{th} < v_{||} \leq \omega_k v_m / (\omega_{ce} + \omega_k)$, and for the $\ell = -1$ resonance, we have $3v_{th} (\omega_{ce} + \omega_k) / \omega_k < v_{||} \leq v_m$. In ATC, for example with $\omega_{ce} = \omega_{pe}$ and for runaway electron energy with $v_m = 10v_{th}$ and $k_{\perp} = \sqrt{2}k_{||}$ (which corresponds to maximum growth), we find for $\ell = 0$: $3v_{th} < v_{||} \leq 3.7v_{th}$, and for $\ell = -1$ we find: $8v_{th} < v_{||} \leq 10v_{th}$. For $T_e \approx 1\text{KeV}$, this will correspond to a runaway tail of about 140 KeV.

Once the anomalous-Doppler-shifted instability is excited, the self-consistent fluctuating electric fields will pitch-angle scatter the tail electrons. This process tends to isotropize the tail of the runaway electron distribution. Since a threshold exists for the $\ell = -1$ resonance, there is no pitch-angle scattering outside the resonant region of $v_{||}$. As the high-parallel-energy particles are continuously be-

ing isotropized, this causes an increase of electron density near the threshold of the $\ell = -1$ resonance. As was first pointed out by Papadopoulos¹⁰, this process modifies the runaway distribution function, forming a bump-on-tail distribution. This result is confirmed by both particle simulations and numerical Fokker-Planck solutions¹⁴.

The growth rate γ_k^B and ω_k^B for the two-dimensional bump-on-tail case are¹⁵:

$$\omega_k^B = \frac{1}{1 + \alpha^2} \left\{ \omega_{pi}^2 + \left(\frac{k_{||}}{k} \right)^2 \omega_{pe}^2 \right\}, \quad (4)$$

and

$$\gamma_k^B = -\omega_k^B \left[\pi^{1/2} \frac{n_T}{n_0} \frac{\omega_{pe}^2}{k^2 v_{th\perp}^2 (1 + \alpha^2)} \zeta \exp(-\zeta^2) \right], \quad (5)$$

where

$$\zeta = (\omega_k^B - k_{||} v_b) / k_{||} v_{th\perp},$$

and

$$\alpha^2 = \frac{\omega_{pe}^2}{\omega_{ce}^2} - \frac{n_T}{n_0} \frac{\omega_{pe}^2}{k^2 v_{th\perp}^2} \text{Re}Z'(\zeta),$$

where ω_{pi} is the ion plasma frequency, v_b is the velocity of the bump, and $\text{Re}Z'(\zeta)$ is the real part of the derivative of the Plasma Dispersion function. Depending on the angle of propagation, ω_k^B covers a range from ω_{pi} to ω_{pe} .

III NUMERICAL MODEL

The time evolution of the distribution function, anomalous-Doppler-shifted modes, and bump-on-tail modes is determined by the Fokker-Planck equation with a quasilinear diffusion operator:

$$\frac{\partial f_{oe}}{\partial t} - \frac{e}{m} \mathbf{E} \cdot \frac{\partial f_{oe}}{\partial \mathbf{v}} = \left(\frac{\partial f_{oe}}{\partial t} \right)_c + \nabla \cdot \mathbf{D} \cdot \nabla f_{oe} \quad (6)$$

where

$$\frac{1}{\Gamma_e} \left(\frac{\partial f_{oe}}{\partial t} \right)_c = -\nabla \cdot (f_e \nabla h_e) + \frac{1}{2} \nabla \nabla : (f_e \nabla \nabla g_e). \quad (7)$$

Here h_e and g_e are the "Rosenbluth potentials",

$$g_e(\mathbf{v}) = \sum_{b=e,i} \int d\mathbf{v}' f_{ob}(\mathbf{v}') |\mathbf{v} - \mathbf{v}'|,$$

$$h_e(\mathbf{v}) = \sum_{b=e,i} \frac{m_e + m_b}{2 m_b} \nabla^2 g_e,$$

with

$$\Gamma_e = (4\pi e^4 \ln D_e) / m_e^2,$$

and

$$D_e = \frac{3T_e}{2e^2} \left(\frac{T_e}{\pi n_e e^2} \right)^{1/2}.$$

The diffusion operation in Eq. (6) is given by¹⁷

$$\begin{aligned} \nabla \cdot \mathbf{D} \cdot \nabla f_{oe} = & 8\pi \frac{e^2}{m^2} \sum_{\mathbf{k}} \int d\mathbf{k} \frac{\mathcal{E}_{\mathbf{k}}(t)}{k^2} \left[\frac{-\mathbf{k} \omega_{ce}}{v_{\perp}} \frac{\partial}{\partial v_{\perp}} \right. \\ & \left. + k_{\parallel} \frac{\partial}{\partial v_{\parallel}} \right] \frac{J_{\perp}^2(k_{\perp} v_{\perp} / \omega_{ce})}{-i\omega_{\mathbf{k}} + ik_{\parallel} v_{\parallel} - i\mathbf{k} \omega_{ce} + \gamma_{\mathbf{k}}} \left[\frac{-\mathbf{k} \omega_{ce}}{v_{\perp}} \frac{\partial}{\partial v_{\perp}} \right. \end{aligned}$$

$$\left(+ k_{\parallel} \frac{\partial}{\partial v_{\parallel}} \right) f_{oe}, \quad (8)$$

where

$$\frac{\partial \mathcal{E}_k(t)}{\partial t} = 2 \gamma_k \mathcal{E}_k(t) + \text{thermal fluctuations} \quad (9)$$

and γ_k is given by (3) and (5).

Eq. (2)-(9) are solved numerically in polar coordinates using an alternating-direction-implicit method.^{18,19} Since it is impractical to cover all directions of the wave vector $\mathbf{k}$, we choose to solve the case where γ_k is maximum, i.e., $k_{\perp} = \sqrt{2} k_{\parallel}$. We hasten to point out that this does not mean we are restricting to one mode, because for this chosen propagation angle, the magnitude of k still varies.

IV NUMERICAL RESULTS

In previous work^{10,14} we examined the consequences of the bump-on-tail structure. Considerable interest has since been shown in the actual formation of this bump-on-tail distribution. We therefore present here two types of numerical experiments; one which shows how the bump-on-tail distribution forms, and one which shows the complete dynamics of the electron distribution.

We shall perform these calculations for Adiabatic Toroidal Compressor (ATC) experimental parameters. Our theory predicts that the electrons of interest are only mildly relativistic, so neither theory nor computation need be concerned with relativistic corrections. The Alcator experiment, in contrast, has $\omega_{ce} \gg \omega_{pe}$, and the bump-on-tail electrons are expected to be highly relativistic.

We begin by artificially removing the bump-on-tail process from the physical model, to show how the ADS modes can produce the bump on the tail of the distribution function. We

model the ATC experimental conditions as follows: $\omega_{ce} = \omega_{pe}$, $n_e = n_i = 2 \times 10^{13} \text{ cm}^{-3}$, $n_T/n_e = 0.03$, $T_e = T_i = 1 \text{ kev}$, and $v_m/v_{th\perp} = 10$. Here v_m is the maximum velocity of the runaway tail, and E_r is the runaway (Dreicer) electric field.

Figure 1 shows the initial, monotonically decreasing distribution function, and the one into which it evolves in 10^{-7} sec. Note the regions of $\ell = 0$ and $\ell = -1$ resonance. The pitch-angle scattering due to these resonances produces the bump. As we will see below, the bump-on-tail modes; when present, will quickly remove a bump of this magnitude. For now, our purpose is to show that such a bump can spontaneously form from a runaway distribution, and to examine its parametric dependence.

In Fig. 2, we change $\omega_{pe}/\omega_{ce} = 1$ to $\omega_{pe}/\omega_{ce} = 1.25$ which corresponds to higher density. We see that the threshold (the bump) gets closer to the thermal region. Eventually as the density increases the bump may get so close that it may merge with the thermal region, and the bump-on-tail modes could no longer be excited.

It is the flattening of the bump, and the resulting bump-on-tail modes, which accounts for the slowing down of the runaway electrons. Therefore, we expect that, in high density operations where the bump approaches the thermal distribution the runaway electron energy is higher, since the bump-on-tail modes provide less energy loss.

When we switch on the bump-on-tail mode, we do not expect to see the bump anymore, because the bump-on-tail mode occurs on a much faster time scale and flattens any bump. In Fig. 2, we show the time development of $\hat{f}(v_{\parallel})$ with both the anomalous-Doppler-shifted and bump-on-tail modes present. The parameters are the same as Fig. 1 except $n_T/n_o = 2\%$. The dotted curve shows the distribution function at steady state, about $1 \mu\text{sec.}$ after initiation.

Note that no bump is formed, and $\hat{f}(v_{\parallel})$ is flatter at the tail than initially. We find the

anomalous-Doppler-shifted instability dies down because of the depletion of particles by the $\ell = -1$ resonance. This is consistent with (3) which says the growth rate is directly proportional to the magnitude of $\hat{f}$ at the $\ell = -1$ resonance.

We have also calculated the synchrotron radiation power due to uncorrelated electrons and find that the power increases by about 75% in about 1 μ sec (See Fig. 4) and levels off after the instabilities die down. This is consistent with experimental observations.⁵ We conclude that the excitation of the anomalous-Doppler-shifted mode is definitely related to the increase of synchrotron radiation. If we follow $\hat{f}(v_{||})$ longer, we expect the resonance region of $\ell = -1$ to be filled up again, because $E_{||}$ can accelerate particles from low $v_{||}$ to high $v_{||}$. When this happens, the instability should be excited again and the synchrotron radiation should also increase. We have followed $\hat{f}(v_{||})$ up to 2.8×10^{-4} sec when the tail region is almost filled up again (see the circles of Fig. 2). We find the instability is not excited because the negative slope at $\ell = 0$ also increases tremendously. At first we believed this was due to $E_{||}$ pushing the bulk electrons, but we found this effect still remained after we switched off $E_{||}$. We conclude this must be due to isotropization. In fact it can be easily estimated that complete isotropization of $\hat{f}(v_{||})$ at $v_{||} = 3 v_{th}$ takes about 1 msec. Therefore in about a third of this time, the slope can increase enough to damp out the anomalous-Doppler-shifted mode. Experimentally it is observed that the synchrotron radiation increases in steps a few msec apart. If the increase in radiation is related to the excitation of anomalous-Doppler-shifted mode which we think it is, then v_m and the instability threshold for anomalous-Doppler-shifted mode must increase so that the $\ell = 0$ resonant region can reach $4 v_{th}$ or $5 v_{th}$.

V SUMMARY

We have developed the analytic tools for describing the effect of anomalous Doppler-shifted plasma waves and bump-on-tail modes upon the tokamak electron distribution func-

tion. These effects have been self-consistently incorporated in a numerical solution of the Fokker-Planck equation as a quasi-linear diffusion operator. Based on results using this model, we find the following general properties of the tokamak electron distribution:

1. The onset of the anomalous-Doppler-shifted modes gives rise both to a suprathermal synchrotron radiation spectrum and formation of a bump-on-tail distribution.
2. The combination of anomalous-Doppler-shifted and bump-on-tail modes are necessary to slow down the runaway electrons.

When comparing different experiments, our studies predict:

3. Experiments at higher electron number density should show lower-amplitude anomalous-Doppler-shifted modes, and higher mean runaway energy.
4. At any density, the threshold in v for onset of the anomalous-Doppler-shifted mode shifts outward with time.

Finally, the sudden reduction in $v_{||}$ caused by onset of the bump-on-tail modes and resultant flattening of the electron distribution function may cause voltage spikes. This loss in $v_{||}$ takes place with minimal loss of energy, breeding very hot electrons with large $v_{\perp}$ and small $v_{||}$. Such electrons would be trapped in poloidal magnetic field minima, and could drift to the outside of the system, leading to liner damage such as seen in TFR and Alcator.

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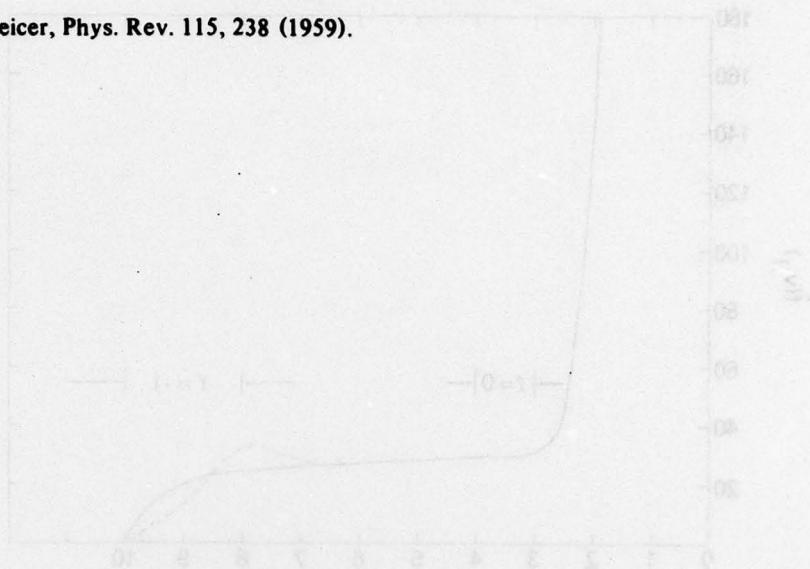


Figure 1 - Boltzmann distribution on the tail of the distribution function at $v = 10$ sec for an ionospheric plasma with $n = 10^{12} \text{ cm}^{-3}$, $T_e = 1 \text{ eV}$, $T_i = 1 \text{ eV}$. The dashed curve is the Boltzmann distribution at $v = 10$ sec for an ionospheric plasma with $n = 10^{12} \text{ cm}^{-3}$, $T_e = 1 \text{ eV}$, $T_i = 1 \text{ eV}$. The solid line is the Boltzmann distribution at $v = 10$ sec for an ionospheric plasma with $n = 10^{12} \text{ cm}^{-3}$, $T_e = 1 \text{ eV}$, $T_i = 1 \text{ eV}$.

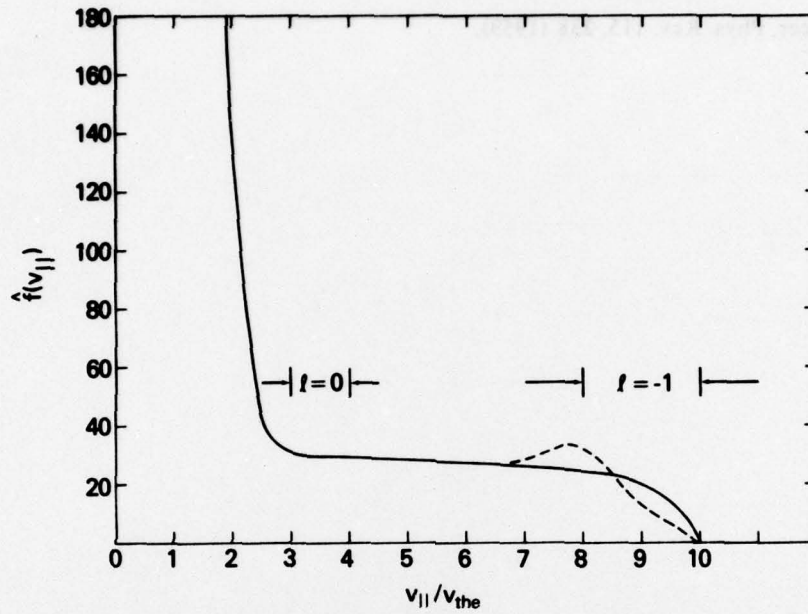


Figure 1 — Bump formation on the tail of the distribution function at $t = 10^{-7}$ sec due to anomalous-Doppler-shifted mode with $\omega_{ce}/\omega_{pe} = 1$, $n_o = 2 \times 10^{13} \text{ cm}^{-3}$, $T_e = 1 \text{ keV}$, $n_T/n_o = 3\%$, $E_{||}/E_R = 0.06$ and $v_M/v_{th\perp} = 10$. The resonance regions of $n = 0$ and $n = -1$ are indicated by arrows. $\hat{f}(v_{||})$ at $t = 0$ is given by solid line.

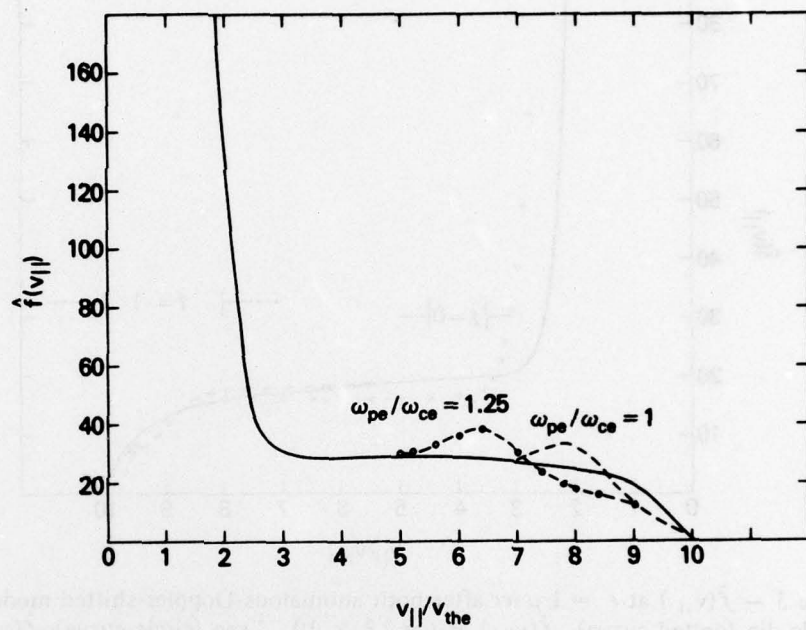


Figure 2 — Density dependence of bump formation

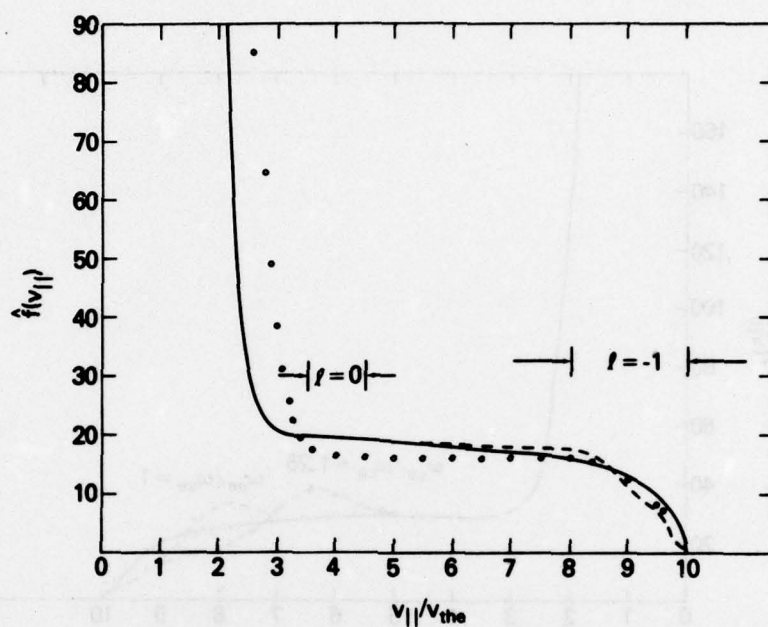


Figure 3 — $\hat{f}(v_{||})$ at $t = 1 \mu\text{sec}$ after both anomalous-Doppler-shifted mode and bump-on-tail mode die (dotted curve). $\hat{f}(v_{||})$ at $t = 2.8 \times 10^{-4} \text{ sec}$ (circle curve), $\hat{f}(v_{||})$ at $t = 0$ is given by solid line, $\omega_{ce}/\omega_{pe} = 1$, $n_o = 2 \times 10^{13} \text{ cm}^{-3}$, $T_e = 1 \text{ keV}$, $n_T/n_o = 2\%$, $E_{||}/E_R = 0.06$ and $v_M/v_{th\perp} = 10$.

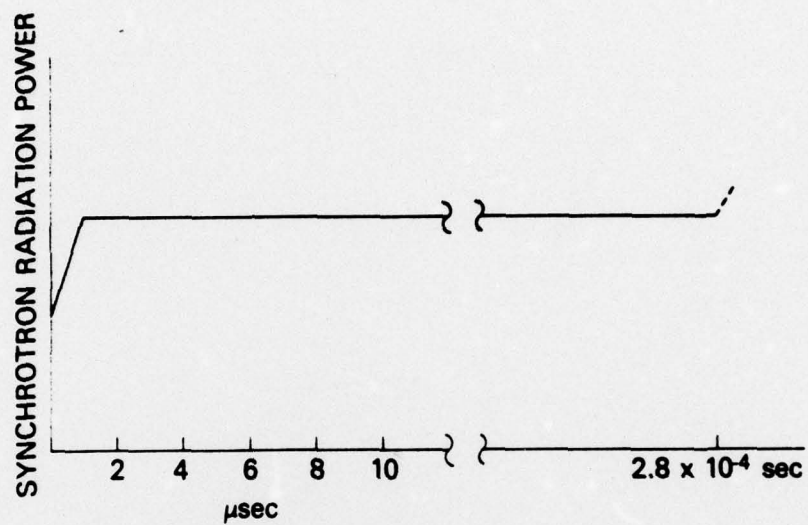


Figure 4 — Synchrotron radiation power vs time