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A GENERAL PURPOSE MULTIDIMENSIONAL FAST FOURIER TRANSFORM FOR U--ETC(U)
SEP 68 R L GORDON, N L OWSLEY
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A GENERAL PURPOSE MULTIDIMENSIONAL FAST FOURIER TRANSFORM FOR USE IN FORTRAN V PROGRAMS*

by

R. L. Gordon and N. L. Owsley

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INTRODUCTION

Fast Fourier Transform (FFT)

An external subroutine is available which performs the discrete Fourier Transform on a multidimensional array of floating point data. The data may be either real or complex. The transform values are always complex and are returned to the array used to carry the original data. The dimensionality of the input array is limited only by machine storage capacity. The number of input samples is not limited to a power of two and, in fact, can be prime in any or all dimensions. The subroutine is called by a one line, six argument call statement in the user program.

Procedure for FFT

The FFT subroutine is called with the following statement:

```
CALL FOURT(DATA,NN,NDIM,ISIGN,IFORM,WORK)
```

*The Program described in this memo has been adapted for the UNIVAC 1108 by the authors from a Lincoln Laboratory Technical Note "Three Programs That Perform the Cooley-Tukey Fourier Transform" by N. M. Brenner on 28 July 1967. The AD No. is AD 657019.

where:

DATA = An N-dimensional complex array used to hold the real and imaginary parts of the input data, and the real and imaginary parts of the transformed values. The real and imaginary parts of a datum must be stored in adjacent core locations as done by the complex array declarer in Fortran V. For real input data, the array DATA is a complex array with the imaginary part set to 0.0.

NN = A single dimensional integer array equal in length to the number of dimensions in the transform. The first element in the array is equal to the length of the first data dimension, the second element is equal to the length of the second data dimension, etc.

NDIM = The number of dimensions used for the array DATA.

ISIGN = { - 1 for a forward transform.
+ 1 for an inverse transform.

IFORM = { + 1 if data and transform are complex.
0 is data is real (zero imaginary values).
If it is "0" the imaginary parts of the data should be set to zero. (Transform will be complex).

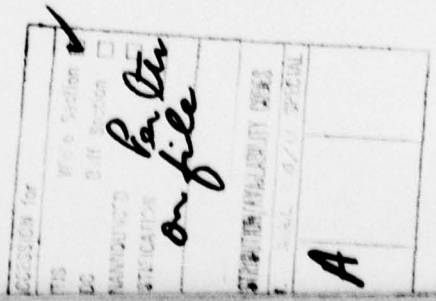
WORK = { "0" if all dimensions are equal to a power of two. If not it must be a single dimension floating point array equal to twice the length of the largest data array dimension not a power of two.

Special Notes:

1. There are no error messages, error halts or error returns in this subroutine. If NDIM or any NN(1) is less than one, the program returns immediately.

2. The data is assumed to form one cycle of a periodic function.[2]

3. The data is assumed to be equispaced in each dimension.[4] If the equispaced interval is DT, the resulting transform will be equispaced from 0 to $2\pi (N-1)/(NDT)$. The upper limit is identified with $-2\pi/(NDT)$ and all points above the foldover frequency π/NDT are identified with the corresponding negative frequency.



4. If an inverse transform is performed on an array of transformed data, the original data will reappear multiplied by N1*N2* . . .

5. The running time is extremely fast if the dimensions are rich in factors of two. The particular running time is dependent on the factorization of each dimension. Approximate times for a one dimensional complex transform are as follows:

N	Factorization	Time for Complex Transform (SEC)
4094	$2 \times 23 \times 89$	40
4096	$3^2 \times 5 \times 7 \times 13$	12
4096	2^{12}	3.1
4097	17×241	90
4098	$2 \times 3 \times 683$	240
4099	PRIME	1430
4100	$2^2 \times 5^2 \times 41$	20

6. For the use of real data input the designation IFORM = 0 can reduce running time by as much as forty percent.

7. A user must allow about 1750 core locations for the instructions.

8. The source and relocatable elements are on File 2 of Cur Tape U-183.

Examples of FFT Program

A. One dimensional forward transform of real data of length 64.

```
    COMPLEX D (64)                    @ Declare Data Array
    Do 10 I = 1, 64
 10 D(I) = (R, 0.0)                   @ Zero Imaginary Values
    - - - - - - - - -
    - - - - - - - - -
    - - - - - - - - -     Fortran Program
    - - - - - - - - -
    - - - - - - - - -
    CALL FOURT (D, 64, 1, -1, 0, 0)
```

where D = Data Array
64 = Length of Array
1 ~ One-Dimension
1 ~ Forward Transform
0 ~ Data is real
0 ~ No working array needed.

B. Three-dimensional forward Fourier transform of a complex array dimensioned 32 by 25 by 13.

```
DIMENSION WORK (50), NN (3)
COMPLEX D (32, 25, 13)              @ Declares Data  Array
DATA NN/32, 25, 13/                 @ Supplies Dimension Info to NN

- - - - - - - - -
- - - - - - - - -
- - - - - - - - -    Fortran Program
- - - - - - - - -
- - - - - - - - -

CALL FOURT (D, NN, 3, -1, 1, WORK)
```

where:

D = Data Array
NN = Integer Array of Length 3 to Supply Dimension Info
3 ~ Three Dimensional Transform
-1 ~ Forward Transform
1 ~ Complex Transform
WORK = Array of size 50 (2 x 25) since 25 is largest non power of two dimension.

Conclusions

The discrete Fourier Transform presented is extremely flexible in nature. Because of this flexibility considerable storage is required compared to some special purpose FFT's. It is felt that the main use of this FFT should be as an analytical tool as opposed to a "real time" processing technique.

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References

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2. Marsh, H. W., "Fast Fourier Transform - Theory and Application", Notes, April 3, 1967.

3. Haavind, R., "The FFT Computer: Designers 'Missing Link'", Electronic Design, Dec. 6, 1967.

4. Cooley, J. W. and Tukey, J. W., "An Algorithm for the Machine Calculation of Complex Fourier Series", Math. of Comput. XIX, April 1965, pp. 297-301.

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