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TI-59 MAGNETIC CARD CALCULATOR SOLUTIONS TO COMPOSITE MATERIALS--ETC(U)
APR 79 S W TSAI , H T HAHN

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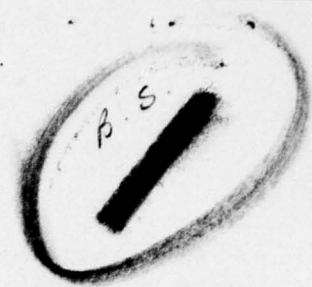


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LEVEL *II*



**TI-59 MAGNETIC CARD CALCULATOR SOLUTIONS
TO COMPOSITE MATERIALS FORMULAS**

*MECHANICS AND SURFACE INTERACTIONS BRANCH
NONMETALLIC MATERIALS DIVISION*

APRIL 1979

TECHNICAL REPORT AFML-TR-79-4040
Final Report for Period October 1977 to October 1978

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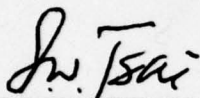
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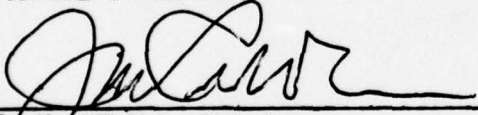
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This technical report has been reviewed and is approved for publication.



S. W. TSAI, Project Engineer & Chief
Mechanics & Surface Interactions Branch
Nonmetallic Materials Division

FOR THE COMMANDER



J. M. KELBLE, Chief
Nonmetallic Materials Division

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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) This volume contains the description and instructions of magnetic cards for TI-59 programmable calculators. These tapes contain the key calculations of the stiffness and strength of unidirectional and symmetrically laminated composites. Both in-plane and flexural loadings can be applied. The initial		

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stress and strain due to curing and moisture adsorption are also included in the strength calculation. With the aid of the magnetic cards, instant calculations can be made for practical use. The use of cards is also an effective teaching tool. The formulas used in the cards have been derived in another AFML report, entitled, "Introduction to Composite Materials", AFML-TR-78-201.

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FOREWORD

This report was prepared in the Mechanics and Surface Interactions Branch (AFML/MBM), Nonmetallic Materials Division, Air Force Materials Laboratory, Wright-Patterson AFB, Ohio. The work was performed under the support Project No. 2419, "Nonmetallic Structural Materials," Task No. 241903, "Composite Materials and Mechanics Technology." The time period covered by this effort was from October 1977 to October 1978. Stephen W. Tsai (AFML/MBM) was the laboratory project engineer. H. Thomas Hahn was a member of AFML/MBM until 1 August 1978.

The page numbers which appear in the flow charts refer to the pages of this report. The equation number, however, refer to those equations in AFML-TR-78-201, "Introduction to Composite Materials".

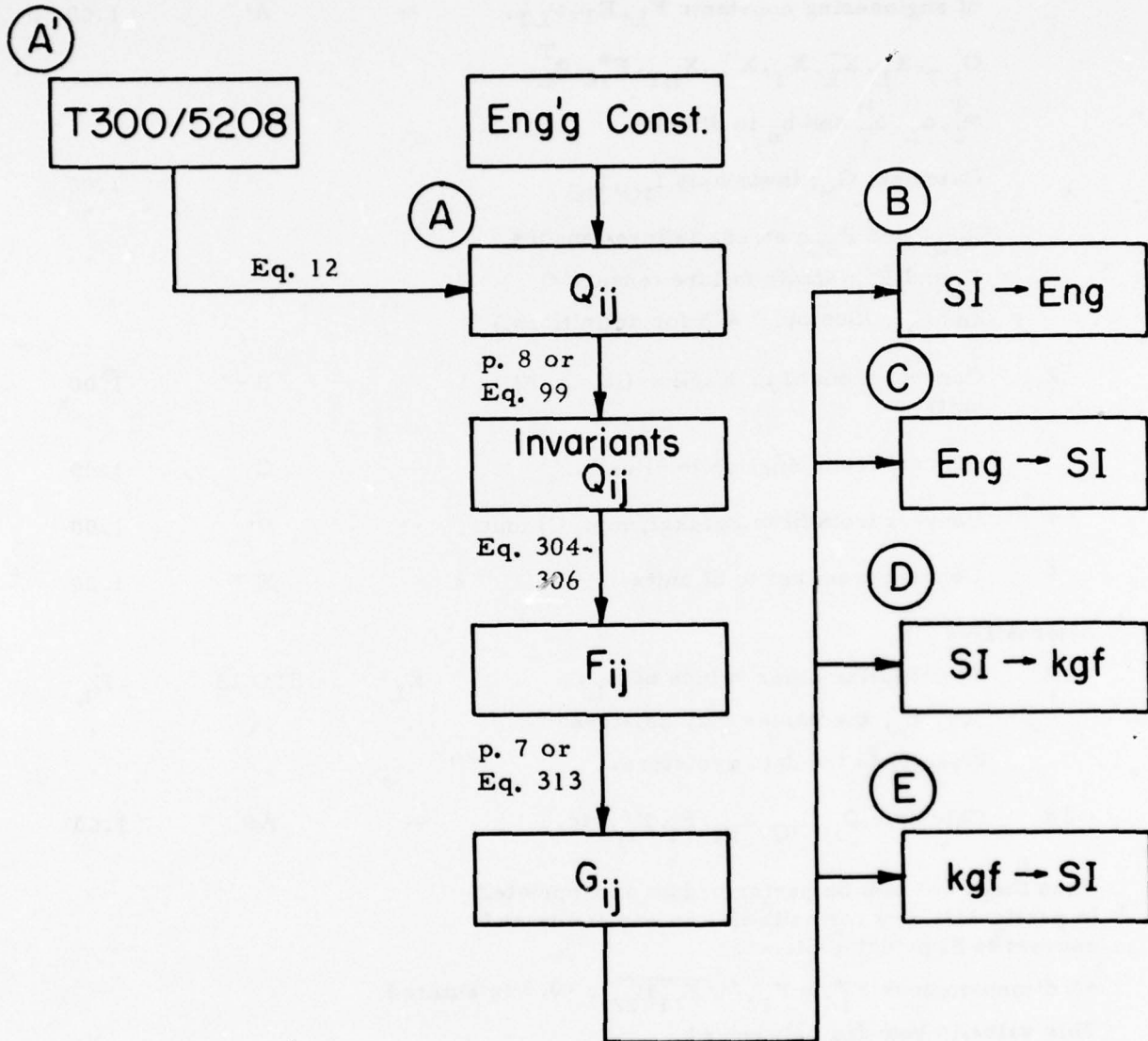
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TABLE OF CONTENTS

Tape #1	Properties of Unidirectional Composites . . .	1
Tape #2	Off-Axis Properties of Unidirectional Composites	9
Tape #3	In-Plane Stiffness of Symmetric Laminates	17
Tape #4	In-Plane Nonmechanical Strains of Symmetric Laminates	23
Tape #5	In-Plane Strength of Symmetric Laminates	31
Tape #6	Flexural Rigidity of Symmetric Sandwich Plates	39
Tape #7	Flexural Strength of Symmetric Sandwich Plates	45

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TAPE #1
PROPERTIES OF UNIDIRECTIONAL COMPOSITES



USER INSTRUCTIONS

TAPE #1: PROPERTIES OF UNIDIRECTIONAL COMPOSITES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
1	For T300/5208 plies, initialize values of engineering constants $E_L, E_T, \nu_{LT}, G_{LT}, X_L, X_L^-, X_T, X_T^-, X_{LT}, F_{12}^*, \alpha_L^T, \alpha_T^T, \alpha_L^H, \alpha_T^H$ and h_o in SI units. Calculate Q_{ij} ; invariants I_{1Q}, I_{2Q} R_{1Q} , and R_{2Q} ; stress failure tensors F_i and F_{ij} ; strain failure tensors G_i and G_{ij} . (See pp. 7 & 8 for definitions.)	--	A'	1.00
2	Convert from SI to English (lb, in, F) units.	--	B	1.00
3	Convert from English to SI units.	--	C	1.00
4	Convert from SI to kgf (kgf, mm, C) units.	--	D	1.00
5	Convert from kgf to SI units	--	E	1.00

Alternatives

1A	To initialize other values of E_L, \dots, h_o , the values may be stored directly in the data registers.	E_L . ' .	STO 18 . .	E_L . .
2A	Calculate $Q_{ij}, I_{iQ}, R_{iQ}, F_i, F_{ij}$, etc.	--	A	1.00

Then Steps 2-5 can be performed as appropriate. In particular, one can initialize in eng. units and convert to SI by using Step 3.

A dimensionless $F_{12}^ = F_{12} / \sqrt{F_{11} F_{22}} = -0.5$ is entered.

This value is bounded between ± 1 .

Computed ply data should be recorded in blocks 3 and 4 for future use. Tape #1 need not be run, unless a change in unit (e.g. from SI to Eng) or change in properties is desired.

Tape* 1Title PROPERTIES OF UNIDIRECTIONAL COMPOSITES
(T300/5208)

KEYS	STORAGE MEMORIES					
A Initialize(after entering Eng'g Constants)	0		20	ν_{LT}	40	
	1	Q_{11}	21	G_{LT}	41	h_o
A' Initialize T300/5208 (SI)	2	Q_{22}	22	α_L^T	42	I_{1Q}
	3	Q_{12}	23	α_T^T	43	I_{2Q}
B SI \rightarrow English (Pa) (psi)	4		24	α_L^H	44	R_{1Q}
	5		25	α_T^H	45	R_{2Q}
B'	6		26		46	F_{11}
	7		27	Q_{11}	47	F_1
C Eng \rightarrow SI (psi) (Pa)	8		28	Q_{22}	48	F_{22}
	9		29	Q_{12}	49	F_2
C'	10		30	Q_{66}	50	$F_{12}^* = F_{12} / \sqrt{F_{11} F_{22}}$
	11		31		51	F_{12}
D SI \rightarrow kgf (Pa) (kgf/mm ²)	12		32		52	
	13	X_L	33		53	
D'	14	X_L^-	34		54	G_{11}
	15	X_T	35		55	G_{22}
E kgf \rightarrow SI (kgf/mm ²) (Pa)	16	X_T^-	36		56	G_{12}
	17	X_{LT}	37		57	G_{66}
E'	18	E_L	38		58	G_1
	19	E_T	39	m	59	G_2

Tape #1 Properties of Unidirectional

T300-5208	000	76	LBL	080	93	160	75	-
	001	16	A'	081	06	161	43	RCL
	002	01	1	082	42	162	30	30
	003	08	8	083	25	163	95	=
	004	66	PAU	084	01	164	42	STD
	005	57	ENG	085	02	165	45	45
	006	01	1	086	05	166	43	RCL
	007	08	8	087	52	167	27	27
	008	01	1	088	94	168	85	+
	009	52	EE	089	06	169	43	RCL
	010	09	9	090	42	170	28	28
	011	42	STD	091	41	171	85	+
	012	18	18	092	76	172	02	2
	013	01	1	093	11	173	65	x
	014	00	0	094	57	174	43	RCL
	015	03	3	095	43	175	29	29
	016	52	EE	096	20	176	95	=
	017	08	8	097	33	177	55	-
	018	42	STD	098	65	178	04	4
	019	19	19	099	43	179	95	=
	020	93	.	100	19	180	42	STD
	021	02	2	101	55	181	42	42
	022	08	8	102	43	182	43	RCL
	023	42	STD	103	18	183	27	27
	024	20	20	104	75	184	75	-
	025	07	7	105	01	185	43	RCL
	026	01	1	106	95	186	28	28
	027	07	7	107	94	187	95	=
	028	52	EE	108	35	188	50	1/X
	029	07	7	109	42	189	55	-
	030	42	STD	110	39	190	02	2
	031	21	21	111	65	191	95	=
	032	01	1	112	43	192	42	STD
	033	05	5	113	18	193	44	44
	034	52	EE	114	95	194	43	RCL
	035	08	8	115	42	195	13	13
	036	42	STD	116	27	196	65	x
	037	13	13	117	42	197	43	RCL
	038	42	STD	118	01	198	14	14
	039	14	14	119	43	199	95	=
	040	04	4	120	39	200	35	1/X
	041	52	EE	121	65	201	42	STD
	042	07	7	122	43	202	46	46
	043	42	STD	123	19	203	65	x
	044	15	15	124	95	204	43	RCL
	045	02	2	125	42	205	14	14
	046	04	4	126	28	206	75	-
	047	06	6	127	42	207	43	RCL
	048	52	EE	128	02	208	14	14
	049	06	6	129	65	209	35	1/X
	050	42	STD	130	43	210	95	=
	051	16	16	131	20	211	42	STD
	052	06	6	132	95	212	47	47
	053	08	8	133	42	213	43	RCL
	054	52	EE	134	29	214	15	15
	055	06	6	135	42	215	65	x
	056	42	STD	136	03	216	43	RCL
	057	17	17	137	43	217	16	16
	058	93	.	138	21	218	95	=
	059	05	5	139	42	219	35	1/X
	060	94	+/-	140	30	220	42	STD
	061	42	STD	141	65	221	48	48
	062	50	50	142	04	222	65	x
	063	01	1	143	75	223	43	RCL
	064	52	EE	144	02	224	46	46
	065	94	+/-	145	65	225	95	=
	066	08	8	146	43	226	34	FX
	067	42	STD	147	29	227	65	x
	068	22	22	148	85	228	43	RCL
	069	01	1	149	43	229	50	50
	070	02	2	150	27	230	95	=
	071	05	5	151	85	231	42	STD
	072	52	EE	152	43	232	51	51
	073	94	+/-	153	28	233	43	RCL
	074	07	7	154	95	234	15	15
	075	42	STD	155	55	235	35	1/X
	076	23	23	156	08	236	75	-
	077	00	0	157	95	237	43	RCL
	078	42	STD	158	42	238	16	16
	079	24	24	159	43	239	35	1/X

Q_{ij}

F_{ij}

Tape #1 Properties of Unidirectional

240	95	=
241	42	STD
242	49	49
243	43	RCL
244	30	30
245	55	+
246	43	RCL
247	17	17
248	95	=
249	33	X ²
250	42	STD
251	57	57
252	43	RCL
253	46	46
254	65	X
255	43	RCL
256	27	27
257	33	X ²
258	85	+
259	00	2
260	00	X
261	43	RCL
262	51	51
263	65	X
264	43	RCL
265	27	27
266	65	X
267	43	RCL
268	29	29
269	00	+
270	43	RCL
271	48	48
272	65	X
273	43	RCL
274	29	29
275	33	X ²
276	00	=
277	42	STD
278	54	54
279	43	RCL
280	46	46
281	65	X
282	43	RCL
283	29	29
284	33	X ²
285	00	+
286	02	2
287	65	X
288	43	RCL
289	51	51
290	65	X
291	43	RCL
292	29	29
293	65	X
294	43	RCL
295	28	28
296	85	+
297	43	RCL
298	48	48
299	65	X
300	43	RCL
301	28	28
302	33	X ²
303	95	=
304	42	STD
305	55	55
306	43	RCL
307	46	46
308	65	X
309	43	RCL
310	27	27
311	65	X
312	43	RCL
313	29	29
314	85	+
315	43	RCL
316	51	51
317	65	X
318	43	RCL
319	27	27

320	65	X
321	43	RCL
322	28	28
323	85	+
324	43	RCL
325	51	51
326	65	X
327	43	RCL
328	29	29
329	33	X ²
330	85	+
331	43	RCL
332	48	48
333	65	X
334	43	RCL
335	28	28
336	65	X
337	43	RCL
338	29	29
339	95	=
340	42	STD
341	56	56
342	43	RCL
343	47	47
344	65	X
345	43	RCL
346	27	27
347	85	+
348	43	RCL
349	49	49
350	65	X
351	43	RCL
352	29	29
353	95	=
354	42	STD
355	58	58
356	43	RCL
357	47	47
358	65	X
359	43	RCL
360	29	29
361	85	+
362	43	RCL
363	49	49
364	65	X
365	43	RCL
366	28	28
367	95	=
368	42	STD
369	59	59
370	01	1
371	95	=
372	91	R/S
373	76	LBL
374	12	8
375	06	6
376	08	8
377	09	9
378	05	5
379	35	1/X
380	42	STD
381	40	40
382	05	5
383	55	+
384	09	9
385	95	=
386	49	PRD
387	22	22
388	49	PRD
389	23	23
390	03	3
391	09	9
392	93	.
393	04	4
394	49	PRD
395	41	41
396	71	SBR
397	34	FX
398	76	LBL
399	13	C

400	08	6
401	08	8
402	09	9
403	05	5
404	42	STD
405	40	40
406	09	9
407	55	+
408	05	5
409	95	=
410	49	PRD
411	22	22
412	49	PRD
413	23	23
414	03	3
415	09	9
416	93	.
417	04	4
418	35	1/X
419	49	PRD
420	41	41
421	71	SBR
422	34	FX
423	76	LBL
424	14	D
425	09	9
426	08	8
427	01	1
428	52	EE
429	04	4
430	35	1/X
431	42	STD
432	40	40
433	01	1
434	52	EE
435	03	3
436	49	PRD
437	41	41
438	76	LBL
439	34	FX
440	43	RCL
441	40	40
442	49	PRD
443	13	13
444	49	PRD
445	14	14
446	49	PRD
447	15	15
448	49	PRD
449	16	16
450	49	PRD
451	17	17
452	49	PRD
453	18	18
454	49	PRD
455	19	19
456	49	PRD
457	21	21
458	61	GTD
459	00	00
460	92	92
461	76	LBL
462	15	E
463	09	9
464	08	8
465	01	1
466	52	EE
467	04	4
468	42	STD
469	40	40
470	01	1
471	52	EE
472	03	3
473	35	1/X
474	49	PRD
475	41	41
476	71	SBR
477	34	FX
478	00	0
479	00	0

G_{ij}

SI →
kgf

Conversion

kgf →
SI

SI →
English

Eng → SI

Tape #1 Properties of Unidirectional/Sample Problems

T300/5208

AS/3501

SI

ENG.

SI

ENG.

0. 00	0. 00	00	0. 00	0. 00	00
181.81114 09	26.368548 06	01	138.78041 09	20.127688 06	01
10.346159 09	1.5005306 06	02	9.0162185 09	1.3076459 06	02
2.8969244 09	420.14858 03	03	2.7048656 09	392.29377 03	03
0. 00	0. 00	04	0. 00	0. 00	04
0. 00	0. 00	05	0. 00	0. 00	05
0. 00	0. 00	06	0. 00	0. 00	06
0. 00	0. 00	07	0. 00	0. 00	07
0. 00	0. 00	08	0. 00	0. 00	08
0. 00	0. 00	09	0. 00	0. 00	09
0. 00	0. 00	10	0. 00	0. 00	10
0. 00	0. 00	11	0. 00	0. 00	11
0. 00	0. 00	12	0. 00	0. 00	12
1.5 09	217.54895 03	13	1.44795 09	210. 03	13
1.5 09	217.54895 03	14	1.44795 09	210. 03	14
40. 06	5.8013053 03	15	51.7125 06	7.5 07	15
246. 06	35.678028 03	16	206.85 06	30. 03	16
68. 06	9.862219 03	17	93.0825 06	13.5 03	17
181. 09	26.250906 06	18	137.96895 09	20.01 06	18
10.3 09	1.4938361 06	19	8.9635 09	1.3 06	19
280. -03	280. -03	20	300. -03	300. -03	20
7.17 09	1.039884 06	21	7.10185 09	1.03 06	21
10. -09	5.5555556 -09	22	10. -09	5.5555556 -09	22
12.5 -06	6.9444444 -06	23	12.5 -06	6.9444444 -06	23
0. 00	0. 00	24	0. 00	0. 00	24
600. -03	600. -03	25	600. -03	600. -03	25
0. 00	0. 00	26	0. 00	0. 00	26
181.81114 09	26.368548 06	27	138.78041 09	20.127688 06	27
10.346159 09	1.5005306 06	28	9.0162185 09	1.3076459 06	28
2.8969244 09	420.14858 03	29	2.7048656 09	392.29377 03	29
7.17 09	1.039884 06	30	7.10185 09	1.03 06	30
0. 00	0. 00	31	0. 00	0. 00	31
0. 00	0. 00	32	0. 00	0. 00	32
0. 00	0. 00	33	0. 00	0. 00	33
0. 00	0. 00	34	0. 00	0. 00	34
0. 00	0. 00	35	0. 00	0. 00	35
0. 00	0. 00	36	0. 00	0. 00	36
0. 00	0. 00	37	0. 00	0. 00	37
0. 00	0. 00	38	0. 00	0. 00	38
1.0044814 00	1.0044814 00	39	1.0058815 00	1.0058815 00	39
0. 00	145.03263 -06	40	6.895 03	145.03263 -06	40
125. -06	4.92125 -03	41	133.24846 -06	5.2499895 -03	41
49.487787 09	7.177344 06	42	38.30159 09	5.5549804 06	42
26.880431 09	3.8985397 06	43	21.349287 09	3.0963433 06	43
85.73249 09	12.434009 06	44	64.882096 09	9.4100211 06	44
19.710431 09	2.8586557 06	45	14.247437 09	2.0663433 06	45
444.44444 -21	21.129344 -12	46	476.97198 -21	22.675737 -12	46
0. 00	-1. -18	47	-100. -24	0. 00	47
101.62602 -18	4.821405 -09	48	93.486509 -18	4.4444444 -09	48
20.934959 09	144.34654 -06	49	14.503263 -09	100. -06	49
-500. -03	-500. -03	50	-500. -03	-500. -03	50
-3.3603243 -18	-159.75326 -12	51	-3.3388039 -18	-158.73016 -12	51
0. 00	0. 00	52	0. 00	0. 00	52
0. 00	0. 00	53	0. 00	0. 00	53
12.004384 03	12.004384 03	54	7.3638004 03	7.3638004 03	54
10.680652 03	10.680652 03	55	7.4403621 03	7.4403621 03	55
3.0691032 03	-3.0691032 03	56	-1.7432239 03	-1.7432239 03	56
11.117842 03	11.117842 03	57	5.8211248 03	5.8211248 03	57
60.646995 00	60.646995 00	58	39.229377 00	39.229377 00	58
216.59641 00	216.59641 00	59	130.76459 00	130.76459 00	59

TAPE #1

TENSOR POLYNOMIAL FAILURE CRITERION IN STRAIN SPACE

Find: $G_{ij}e_i e_j + G_i e_i = 1$

From: $F_{ij}\sigma_i \sigma_j + F_i \sigma_i = 1$

and $\sigma_i = Q_{ij}e_j$

we have $G_{ij} = Q_{ik}Q_{jl}F_{kl}$

$$G_i = Q_{ik}F_k$$

For orthotropic materials: $Q_{16} = Q_{26} = 0$

$$G_{11} = F_{11}Q_{11}^2 + 2F_{12}Q_{11}Q_{21} + F_{22}Q_{12}^2$$

$$G_{22} = F_{11}Q_{12}^2 + 2F_{12}Q_{12}Q_{22} + F_{22}Q_{22}^2$$

$$G_{66} = F_{66}Q_{66}^2 = \left(\frac{Q_{66}}{X_{LT}} \right)^2$$

$$G_{12} = F_{11}Q_{11}Q_{12} + F_{12}(Q_{11}Q_{22} + Q_{12}^2) + F_{22}Q_{21}Q_{22}$$

$$G_{16} = G_{26} = 0$$

$$G_1 = F_1 Q_{11} + F_2 Q_{21}$$

$$G_2 = F_1 Q_{12} + F_2 Q_{22}$$

$$G_6 = 0$$

TAPE #1

DEFINITIONS OF INVARIANTS OF ELASTIC MODULUS

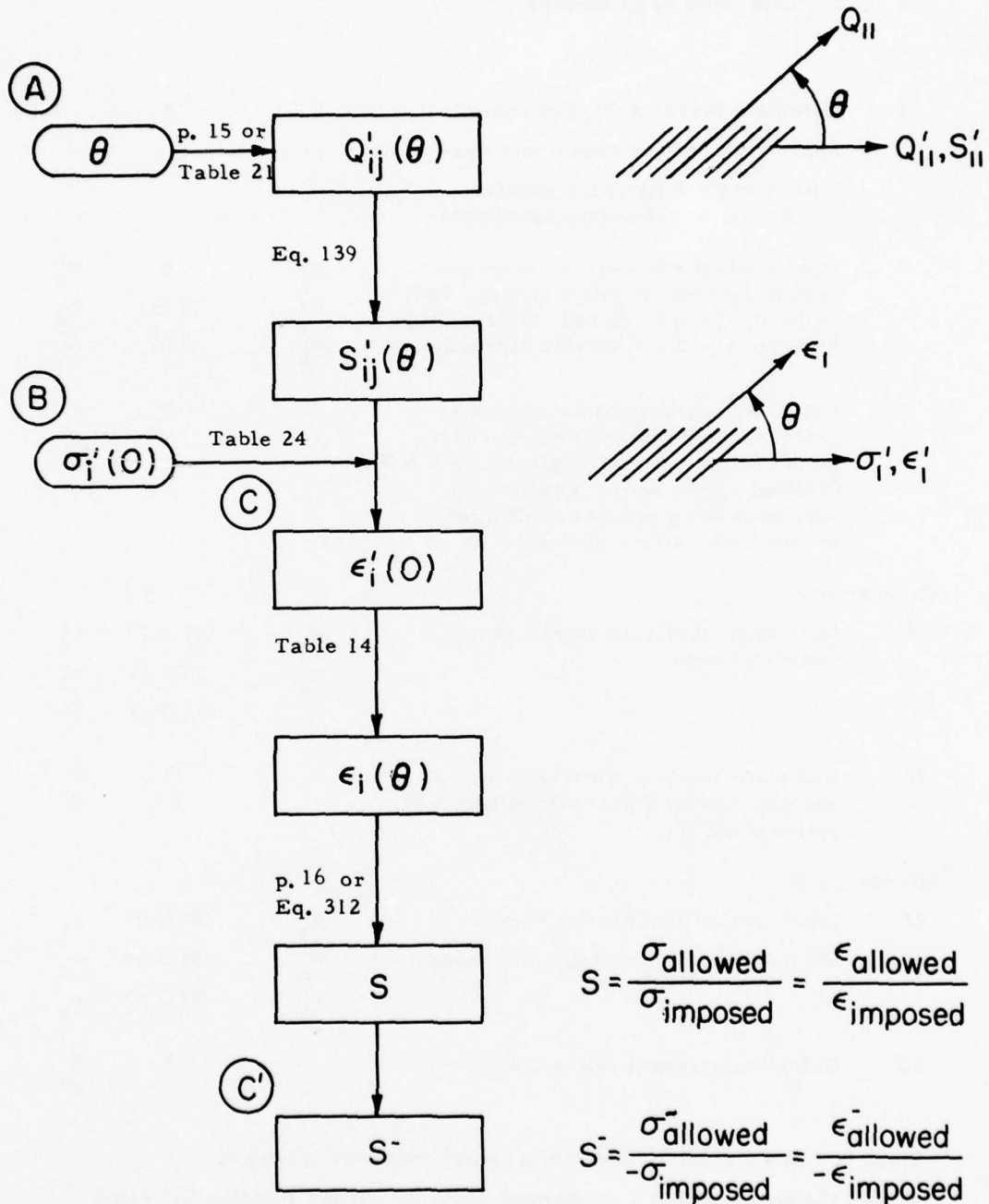
$$I_{1Q} = \frac{1}{2}(Q_{11} + Q_{22} - 2Q_{12}) = (U_1 + U_4) / 2$$

$$I_{2Q} = \frac{1}{4}(Q_{11} + Q_{22} - 2Q_{12} + 4Q_{66}) = U_5 = (U_1 - U_4) / 2$$

$$R_{1Q} = U_2$$

$$R_{2Q} = U_3$$

TAPE #2
OFF-AXIS PROPERTIES OF UNIDIRECTIONAL COMPOSITES



USER INSTRUCTIONS

TAPE #2: OFF-AXIS PROPERTIES OF UNIDIRECTIONAL COMPOSITES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
0	Ply data must be in storage			
1	Calculate modulus Q'_{ij} and compliance S'_{ij} in rotated coordinate system at angle θ (positive counter-clockwise) to reference coordinates	θ	A	1.00
2	Input applied stresses in reference coord. system. If unit stresses, such as [1, 0, 0], are entered, the resulting S values are the allowable strengths.	σ'_1 σ'_2 σ'_6	B R/S R/S	σ'_1 σ'_2 σ'_6
3*	Calculate corresponding strains in reference and material coord. systems and calculate strength ratios S & S^- . (defined as the ratios by which the applied loading must be multiplied to reach the failure surface).	-- --	C C'	S S^-

Alternative A

2A	Input applied strains in reference coord. system	e'_1 e'_2 e'_6	STO 10 STO 11 STO 12	e'_1 e'_2 e'_6
3A	Calculate strains in material coord. system, and calculate strength-strain ratios S and S^- .	-- --	D C'	S S^-

Alternative B

2B	Input strains in material coords. (Step 0 needed, but Step 1 not needed)	e_1 e_2 e_6	STO 07 STO 08 STO 09	e_1 e_2 e_6
3B	Calculate strength ratios S & S^- .	-- --	E C'	S S^-

* Steps 0, 1 and 2 must be executed at least once before Step 3.

If only the angle in Step 1 is changed while the stress remains the same Step 2 can be skipped. If the stress is changed while the angle remains constant, Step 1 can be omitted.

Tape* 2Title OFF-AXIS PROPERTIES OF UNIDIRECTIONAL COMPOSITES

KEYS	STORAGE MEMORIES					
A θ	0	θ	20	40	4θ	
	1	σ'_1	21	41	h_o	
A'	2	σ'_2	22	42	I_{1Q}	
	3	σ'_6	23	43	I_{2Q}	
B σ'_i	4		24	44	R_{1Q}	
	5		25	45	R_{2Q}	
B'	6		26	$ Q $	46	
	7	e_1	27	Q'_{11}	47	
C s	8	e_2	28	Q'_{22}	48	
	9	e_6	29	Q'_{12}	49	
C' s ⁻	10	e'_1	30	Q'_{66}	50	
	11	e'_2	31	Q'_{16}	51	
D S from e'_i	12	e'_6	32	Q'_{26}	52	... S
	13		33	S'_{11}	53	... S ⁻
D'	14		34	S'_{22}	54	G_{11}
	15		35	S'_{12}	55	G_{22}
E S from e_i	16		36	S'_{66}	56	G_{12}
	17		37	S'_{16}	57	G_{66}
E'	18		38	S'_{26}	58	G_1
	19		39	2θ	59	G_2

Tape #2 Off-Axis Properties

θ	000	76	LBL	080	38	SIN	160	95	=
	001	11	A	081	55	-	161	42	STD
	002	57	ENG	082	02	2	162	33	33
	003	42	STD	083	65	X	163	43	RCL
	004	00	00	084	43	RCL	164	27	27
	005	65	X	085	44	44	165	65	X
	006	02	2	086	95	=	166	43	RCL
	007	95	=	087	85	+	167	28	28
	008	42	STD	088	43	RCL	168	75	-
	009	39	39	089	40	40	169	43	RCL
	010	65	X	090	38	SIN	170	29	29
	011	02	2	091	65	X	171	33	X ²
	012	95	=	092	43	RCL	172	95	=
	013	42	STD	093	45	45	173	42	STD
	014	40	40	094	95	=	174	36	36
	015	01	1	095	42	STD	175	43	RCL
	016	06	6	096	31	31	176	27	27
	017	66	PAU	097	75	-	177	65	X
Q_{ij}	018	43	RCL	098	43	RCL	178	43	RCL
	019	42	42	099	39	39	179	30	30
	020	85	+	100	38	SIN	180	75	-
	021	43	RCL	101	65	X	181	43	RCL
	022	43	43	102	43	RCL	182	31	31
	023	85	+	103	44	44	183	33	X ²
	024	43	RCL	104	95	=	184	95	=
	025	39	39	105	94	+/-	185	42	STD
	026	39	CDS	106	42	STD	186	34	34
	027	65	X	107	32	32	187	43	RCL
	028	43	RCL	108	43	RCL	188	29	29
	029	44	44	109	27	27	189	65	X
	030	85	+	110	65	X	190	43	RCL
	031	43	RCL	111	43	RCL	191	32	32
	032	40	40	112	28	28	192	75	-
	033	39	CDS	113	65	X	193	43	RCL
	034	65	X	114	43	RCL	194	28	28
	035	43	RCL	115	30	30	195	65	X
	036	45	45	116	85	+	196	43	RCL
	037	95	=	117	43	RCL	197	31	31
	038	42	STD	118	29	29	198	95	=
	039	27	27	119	65	X	199	42	STD
	040	75	-	120	43	RCL	200	37	37
	041	43	RCL	121	31	31	201	43	RCL
	042	39	39	122	65	X	202	31	31
	043	39	CDS	123	43	RCL	203	65	X
	044	65	X	124	32	32	204	43	RCL
	045	02	2	125	65	X	205	32	32
	046	65	X	126	02	2	206	75	-
	047	43	RCL	127	75	-	207	43	RCL
	048	44	44	128	43	RCL	208	29	29
	049	95	=	129	28	28	209	65	X
	050	42	STD	130	65	X	210	43	RCL
	051	28	28	131	43	RCL	211	30	30
	052	43	RCL	132	31	31	212	95	=
	053	42	42	133	33	X ²	213	42	STD
	054	75	-	134	75	-	214	35	35
	055	43	RCL	135	43	RCL	215	43	RCL
	056	43	43	136	27	27	216	29	29
	057	75	-	137	65	X	217	65	X
	058	43	RCL	138	43	RCL	218	43	RCL
	059	40	40	139	32	32	219	31	31
	060	39	CDS	140	33	X ²	220	75	-
	061	65	X	141	75	-	221	43	RCL
	062	43	RCL	142	43	RCL	222	27	27
	063	45	45	143	30	30	223	65	X
	064	95	=	144	65	X	224	43	RCL
	065	42	STD	145	43	RCL	225	32	32
	066	29	29	146	29	29	226	95	=
	067	85	+	147	33	X ²	227	42	STD
	068	02	2	148	95	=	228	38	38
	069	65	X	149	42	STD	229	43	RCL
	070	43	RCL	150	26	26	230	26	26
	071	43	43	151	43	RCL	231	35	1/X
	072	75	-	152	28	28	232	49	FRD
	073	43	RCL	153	65	X	233	33	33
	074	42	42	154	43	RCL	234	49	FRD
	075	95	=	155	30	30	235	34	34
	076	42	STD	156	75	-	236	49	FRD
	077	30	30	157	43	RCL	237	35	35
	078	43	RCL	158	32	32	238	49	FRD
	079	39	39	159	33	X ²	239	36	36

IQI

S_{ij}^{1/2}

S_{ij}

Tape #2 Off-Axis Properties

240 49 PRD
 241 37 37
 242 49 PRD
 243 38 38
 244 01 1
 245 95 =
 246 91 R/S
 247 76 LBL
 248 12 B
 249 42 STD
 250 01 01
 251 91 R/S
 252 42 STD
 253 02 02
 254 91 R/S
 255 12 STD
 256 03 03
 257 91 R/S
 258 76 LBL
 259 13 C
 260 01 1
 261 04 4
 262 66 PHU
 263 43 RCL
 264 03 03
 265 65 x
 266 43 RCL
 267 37 37
 268 85 +
 269 43 RCL
 270 02 02
 271 65 x
 272 43 RCL
 273 35 35
 274 85 +
 275 43 RCL
 276 01 01
 277 65 x
 278 43 RCL
 279 33 33
 280 95 =
 281 42 STD
 282 10 10
 283 43 RCL
 284 01 01
 285 65 x
 286 43 RCL
 287 35 35
 288 85 +
 289 43 RCL
 290 02 02
 291 65 x
 292 43 RCL
 293 34 34
 294 85 +
 295 43 RCL
 296 03 03
 297 65 x
 298 43 RCL
 299 38 38
 300 95 =
 301 42 STD
 302 11 11
 303 43 RCL
 304 01 01
 305 65 x
 306 43 RCL
 307 37 37
 308 85 +
 309 43 RCL
 310 02 02
 311 65 x
 312 43 RCL
 313 38 38
 314 85 +
 315 43 RCL
 316 03 03
 317 65 x
 318 43 RCL
 319 36 36

320 95 =
 321 42 STD
 322 12 12
 323 76 LBL
 324 14 D
 325 43 RCL
 326 00 00
 327 39 COS
 328 33 X²
 329 65 x
 330 43 RCL
 331 10 10
 332 85 +
 333 43 RCL
 334 00 00
 335 38 SIN
 336 33 X²
 337 65 x
 338 43 RCL
 339 11 11
 340 85 +
 341 43 RCL
 342 00 00
 343 39 COS
 344 65 x
 345 43 RCL
 346 00 00
 347 38 SIN
 348 65 x
 349 43 RCL
 350 12 12
 351 95 =
 352 42 STD
 353 07 07
 354 75 -
 355 43 RCL
 356 10 10
 357 75 -
 358 43 RCL
 359 11 11
 360 95 =
 361 94 +/-
 362 42 STD
 363 08 08
 364 43 RCL
 365 11 11
 366 75 -
 367 43 RCL
 368 10 10
 369 95 =
 370 65 x
 371 43 RCL
 372 39 39
 373 38 SIN
 374 85 +
 375 43 RCL
 376 39 39
 377 39 COS
 378 65 x
 379 43 RCL
 380 12 12
 381 95 =
 382 42 STD
 383 09 09
 384 76 LBL
 385 15 E
 386 43 RCL
 387 54 54
 388 65 x
 389 43 RCL
 390 07 07
 391 33 X²
 392 85 +
 393 02 2
 394 65 x
 395 43 RCL
 396 56 56
 397 65 x
 398 43 RCL
 399 07 07

400 65 x
 401 43 RCL
 402 08 08
 403 85 +
 404 43 RCL
 405 55 55
 406 65 x
 407 43 RCL
 408 08 08
 409 33 X²
 410 85 +
 411 43 RCL
 412 57 57
 413 65 x
 414 43 RCL
 415 09 09
 416 33 X²
 417 95 =
 418 42 STD
 419 52 52
 420 43 RCL
 421 58 58
 422 65 x
 423 43 RCL
 424 07 07
 425 85 +
 426 43 RCL
 427 59 59
 428 65 x
 429 43 RCL
 430 08 08
 431 95 =
 432 42 STD
 433 53 53
 434 43 RCL
 435 52 52
 436 35 1/X
 437 42 STD
 438 52 52
 439 65 x
 440 43 RCL
 441 53 53
 442 55 +
 443 02 2
 444 95 =
 445 42 STD
 446 53 53
 447 33 X²
 448 85 +
 449 43 RCL
 450 52 52
 451 95 =
 452 34 1/X
 453 42 STD
 454 52 52
 455 85 +
 456 43 RCL
 457 53 53
 458 95 =
 459 94 +/-
 460 42 STD
 461 53 53
 462 85 +
 463 02 2
 464 65 x
 465 43 RCL
 466 52 52
 467 95 =
 468 42 STD
 469 52 52
 470 91 R/S
 471 76 LBL
 472 18 C
 473 43 RCL
 474 53 53
 475 91 R/S
 476 00 0
 477 00 0
 478 00 0
 479 00 0

Tape #2 Off-Axis Properties/Sample Problems

θ	0.00	15.00	30.00	45.00	00
α_1	1.00	1.00	1.00	1.00	01
	0.00	0.00	0.00	0.00	02
	0.00	0.00	0.00	0.00	03
	0.00	0.00	0.00	0.00	04
	0.00	0.00	0.00	0.00	05
	0.00	0.00	0.00	0.00	06
	0.00	0.00	0.00	0.00	07
	5.5248619-12	5.0511395-12	3.7569061-12	1.9889503-12	08
	-1.5469613-12	5.0602866-12	23.111624-12	47.770209-12	09
	0.00	-34.867503-12	-60.392288-12	-69.735007-12	10
	5.5248619-12	13.768628-12	34.746213-12	59.747083-12	11
	-1.5469613-12	-3.657202-12	-7.8776833-12	-9.987924-12	12
	0.00	-30.200717-12	-46.957821-12	-45.781258-12	13
	1.5 09	1.5 09	1.5 09	1.5 09	14
	1.5 09	1.5 09	1.5 09	1.5 09	15
	40.06	40.06	40.06	40.06	16
	246.06	246.06	246.06	246.06	17
	68.06	68.06	68.06	68.06	18
	181.09	181.09	181.09	181.09	19
	10.3 09	10.3 09	10.3 09	10.3 09	20
	280.-03	280.-03	280.-03	280.-03	21
	7.17 09	7.17 09	7.17 09	7.17 09	22
	10.-09	10.-09	10.-09	10.-09	23
	12.5-06	12.5-06	12.5-06	12.5-06	24
	0.00	0.00	0.00	0.00	25
	600.-03	600.-03	600.-03	600.-03	26
	13.426934 30	13.426934 30	13.426934 30	13.426934 30	27
	181.81114 09	160.46395 09	109.37925 09	56.657787 09	28
	10.346159 09	11.976919 09	23.646757 09	56.657787 09	29
	2.8969244 09	12.75214 09	32.462571 09	42.317787 09	30
	7.17 09	17.025216 09	36.735647 09	46.590862 09	31
	0.00	38.502857 09	54.192991 09	42.866245 09	32
	0.00	4.3633885 09	20.053523 09	42.866245 09	33
	5.5248619-12	13.768628-12	34.746213-12	59.747083-12	34
	97.087379-12	93.064094-12	80.527471-12	59.747083-12	35
	-1.5469613-12	-3.657202-12	-7.8776833-12	-9.987924-12	36
	139.47001-12	131.02905-12	114.14713-12	105.70616-12	37
	0.00	-30.200717-12	-46.957821-12	-45.781258-12	38
	0.00	-15.580541-12	-32.337645-12	-45.781258-12	39
	0.00	30.00	60.00	90.00	40
	0.00	60.00	120.00	180.00	41
	125.-06	125.-06	125.-06	125.-06	42
	49.487787 09	49.487787 09	49.487787 09	49.487787 09	43
	26.880431 09	26.880431 09	26.880431 09	26.880431 09	44
	85.73249 09	85.73249 09	85.73249 09	85.73249 09	45
	19.710431 09	19.710431 09	19.710431 09	19.710431 09	46
	444.44444-21	444.44444-21	444.44444-21	444.44444-21	47
	0.00	0.00	0.00	0.00	48
	101.62602-18	101.62602-18	101.62602-18	101.62602-18	49
	20.934959-09	20.934959-09	20.934959-09	20.934959-09	50
	-500.-03	-500.-03	-500.-03	-500.-03	51
	-3.3603243-18	-3.3603243-18	-3.3603243-18	-3.3603243-18	52
	1.5 09	222.22216 06	101.22462 06	64.536588 06	53
	1.5 09	322.82798 06	215.27228 06	198.9018 06	54
	12.004384 03	12.004384 03	12.004384 03	12.004384 03	55
	10.680652 03	10.680652 03	10.680652 03	10.680652 03	56
	-3.0691032 03	-3.0691032 03	-3.0691032 03	-3.0691032 03	57
	11.117842 03	11.117842 03	11.117842 03	11.117842 03	58
	60.646995 00	60.646995 00	60.646995 00	60.646995 00	59
	216.59641 00	216.59641 00	216.59641 00	216.59641 00	60

TAPE #2

TRANSFORMATION OF MODULUS COMPONENTS

	I_{1Q}	I_{2Q}	R_{1Q}	R_{2Q}
Q'_{11}	1	1	$\cos 2\theta$	$\cos 4\theta$
Q'_{22}	1	1	$-\cos 2\theta$	$\cos 4\theta$
Q'_{12}	1	-1		$-\cos 4\theta$
Q'_{66}		1		$-\cos 4\theta$
Q'_{16}			$\frac{1}{2}\sin 2\theta$	$\sin 4\theta$
Q'_{26}			$\frac{1}{2}\sin 2\theta$	$-\sin 4\theta$

$$Q'_{22} = Q'_{11} - 2R_{1Q} \cos 2\theta$$

$$Q'_{26} = Q'_{16} - 2R_{2Q} \sin 4\theta$$

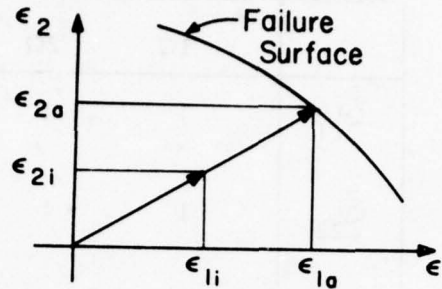
TAPE #2

STRENGTH RATIOS FOR UNIDIRECTIONAL COMPOSITES

Define $S = \frac{\epsilon_{\text{allowed}}}{\epsilon_{\text{imposed}}} = \frac{\epsilon_a}{\epsilon_i}$

Proportional loading is assumed; i.e.

$$\frac{\epsilon_{1a}}{\epsilon_{1i}} = \frac{\epsilon_{2a}}{\epsilon_{2i}} = \frac{\epsilon_{6a}}{\epsilon_{6i}} = S$$



Since linearly elastic behavior up to failure is also assumed,

$$S = \frac{\epsilon_a}{\epsilon_i} = \frac{\sigma_{\text{allowed}}}{\sigma_{\text{imposed}}}$$

Failure occurs when $\epsilon_{\text{imposed}} = \epsilon_{\text{allowed}}$, the failure criterion is satisfied:

$$G_{ij} \epsilon_i \epsilon_j + G_i \epsilon_i = 1$$

Then strength ratio $S = 1$.

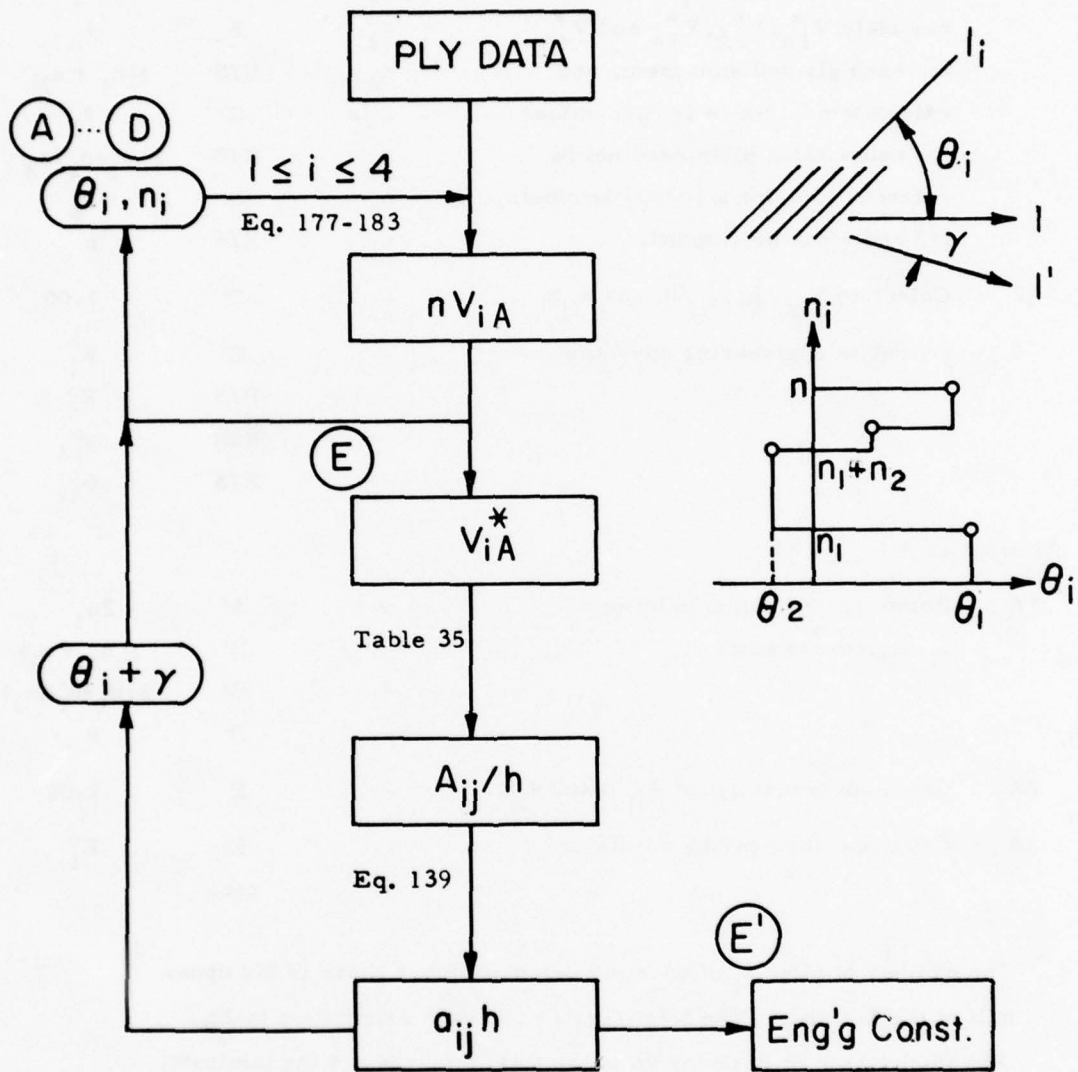
If $\epsilon_{\text{imposed}}$ is less than $\epsilon_{\text{allowed}}$, $S > 1$. The failure criterion is also satisfied:

$$G_{ij} \epsilon_i \epsilon_j S^2 + G_i \epsilon_i S = 1$$

where strains in this equation are $\epsilon_{\text{imposed}}$.

For a given state of imposed strains, we can solve for the quadratic equation for S ; the other real root is the strength ratio S^- which corresponds to that when all the imposed strains change signs. If original ϵ_i were all positive, the S^- is the strength ratio for opposite strains, or $-\epsilon_i$.

TAPE #3
 IN-PLANE STIFFNESS
 OF SYMMETRIC LAMINATES



USER INSTRUCTIONS

TAPE #3: IN-PLANE STIFFNESS OF SYMMETRIC LAMINATES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
0	Enter ply data.	--		
1	Enter ply angle θ_i , and number of plies at that angle, n_i^* , $i=1, 4$, and calculate V_{1A}^* , V_{2A}^* , V_{3A}^* and V_{4A}^* for each ply and sum them, and calculate n . Since $1 \leq i \leq 4$, values for nonexisting plies need not be entered, i.e. for a [0/90] laminate, $i=3$ and 4 can be skipped.	θ_1	A	θ_1
		n_1	R/S	$2n_1$
		θ_2	B	θ_2
		n_2	R/S	$2(n_1 + n_2)$
		θ_3	C	θ_3
		n_3	R/S	$2(n_1 + n_2 + n_3)$
		θ_4	D	θ_4
		n_4	R/S	n
2	Calculate V_{iA} , h , A_{ij}/h , and $a_{ij}h$.	--	E	1.00
3	Calculate engineering constants	--	E'	E_1^0
		--	R/S	E_2^0
		--	R/S	ν_{12}^0
		--	R/S	G_{12}^0

Alternative A

1A	Rotate entire laminate by γ ; ** n_i remain the same	γ	A'	$2n_1$
		--	B'	$2(n_1 + n_2)$
		--	C'	$2(n_1 + n_2 + n_3)$
		--	D'	n
2A	Calculate transformed A_{ij}/h and $a_{ij}h$,	--	E	1.00
3A	Calculate engineering constants	--	E'	E_1^0
		--	etc.	

* The number of plies n_i of each ply orientation are those in the upper half of the laminate. The total number for each orientation is $2n_i$. The thickness h in Register 26 is the total thickness of the laminate; the number in Register 46 is one half of the total ply number. For symmetric laminates, only the fraction of each orientation rather than the absolute number of plies is important.

** This is equivalent to rotating the reference coordinates in the clockwise or negative direction.

Tape* 3Title IN-PLANE STIFFNESS OF SYMMETRIC LAMINATES

KEYS	STORAGE MEMORIES		
A θ_1, n_1	0 γ	20 n_4	40 n_i
	1	21	41 h_o
A' $\theta_1 + \gamma, n_1$	2	22	42 I_{1Q}
	3	23	43 I_{2Q}
B θ_2, n_2	4	24	44 R_{1Q}
	5	25	45 R_{2Q}
B' $\theta_2 + \gamma, n_2$	6	26 h	46 $n/2$
	7	27 $Q_{11}, A_{11}/h$	47 V_{1A}^*
C θ_3, n_3	8	28 $Q_{22}, A_{22}/h$	48 V_{2A}^*
	9	29 $Q_{12}, A_{12}/h$	49 V_{3A}^*
C' $\theta_3 + \gamma, n_3$	10	30 $Q_{66}, A_{66}/h$	50 V_{4A}^*
	11	31 A_{16}/h	51
D θ_4, n_4	12	32 A_{26}/h	52
	13 θ_1	33 a_{11}^h	53
D' $\theta_4 + \gamma, n_4$	14 n_1	34 a_{22}^h	54
	15 θ_2	35 a_{12}^h	55
E $A_{ij}/h, a_{ij}^h$	16 n_2	36 a_{66}^h	56
	17 θ_3	37 a_{16}^h	57
E' Engineering Constants	18 n_3	38 a_{26}^h	58
	19 θ_4	39 $\theta_i, A $	59

Tape #3 In-Plane Stiffness

θ_1, n_1	000	76	LBL	080	39	CDS	160	43	RCL
	001	11	A	081	65	x	161	48	48
	002	57	ENG	082	43	RCL	162	65	x
	003	42	STD	083	40	40	163	43	RCL
	004	13	13	084	95	=	164	45	45
	005	00	0	085	44	SUM	165	95	=
	006	42	STD	086	47	47	166	42	STD
	007	46	46	087	43	RCL	167	27	27
	008	42	STD	088	39	39	168	75	-
	009	47	47	089	38	SIN	169	02	2
	010	42	STD	090	65	x	170	65	x
	011	48	48	091	43	RCL	171	43	RCL
	012	42	STD	092	40	40	172	47	47
	013	49	49	093	95	=	173	65	x
	014	42	STD	094	44	SUM	174	43	RCL
	015	50	50	095	49	49	175	44	44
	016	43	RCL	096	02	2	176	95	=
	017	13	13	097	49	PRD	177	42	STD
	018	91	R/S	098	39	39	178	28	28
	019	42	STD	099	43	RCL	179	43	RCL
	020	14	14	100	39	39	180	42	42
	021	42	STD	101	39	CDS	181	75	-
	022	40	40	102	65	x	182	43	RCL
	023	44	SUM	103	43	RCL	183	43	43
	024	46	46	104	40	40	184	75	-
	025	43	RCL	105	95	=	185	43	RCL
	026	13	13	106	44	SUM	186	48	48
	027	71	SBR	107	48	48	187	65	x
	028	33	X ²	108	43	RCL	188	43	RCL
θ_2, n_2	029	76	LBL	109	39	39	189	45	45
	030	12	B	110	38	SIN	190	95	=
	031	42	STD	111	65	x	191	42	STD
	032	15	15	112	43	RCL	192	29	29
	033	91	R/S	113	40	40	193	75	-
	034	42	STD	114	95	=	194	43	RCL
	035	16	16	115	44	SUM	195	42	42
	036	42	STD	116	50	50	196	85	+
	037	40	40	117	43	RCL	197	02	2
	038	44	SUM	118	46	46	198	65	x
	039	46	46	119	65	x	199	43	RCL
	040	43	RCL	120	02	2	200	43	43
	041	15	15	121	95	=	201	95	=
	042	71	SBR	122	91	R/S	202	42	STD
	043	33	X ²	123	76	LBL	203	30	30
θ_3, n_3	044	76	LBL	124	15	E	204	43	RCL
	045	13	C	125	01	1	205	49	49
	046	42	STD	126	03	3	206	65	x
	047	17	17	127	66	PAU	207	43	RCL
	048	91	R/S	128	43	RCL	208	44	44
	049	42	STD	129	46	46	209	55	+
	050	18	18	130	35	1/X	210	02	2
	051	42	STD	131	49	PRD	211	85	+
	052	40	40	132	47	47	212	43	RCL
	053	44	SUM	133	49	PRD	213	50	50
	054	46	46	134	48	48	214	65	x
	055	43	RCL	135	49	PRD	215	43	RCL
	056	17	17	136	49	49	216	45	45
	057	71	SBR	137	49	PRD	217	95	=
	058	33	X ²	138	50	50	218	94	+/-
θ_4, n_4	059	76	LBL	139	35	1/X	219	42	STD
	060	14	D	140	65	x	220	31	31
	061	42	STD	141	43	RCL	221	85	+
	062	19	19	142	41	41	222	02	2
	063	91	R/S	143	65	x	223	65	x
	064	42	STD	144	02	2	224	43	RCL
	065	20	20	145	95	=	225	50	50
	066	42	STD	146	42	STD	226	65	x
	067	40	40	147	26	26	227	43	RCL
	068	44	SUM	148	43	RCL	228	45	45
	069	46	46	149	42	42	229	95	=
	070	43	RCL	150	85	+	230	42	STD
	071	19	19	151	43	RCL	231	32	32
V_{iA}	072	76	LBL	152	43	43	232	43	RCL
	073	33	X ²	153	85	+	233	27	27
	074	65	x	154	43	RCL	234	65	x
	075	02	2	155	47	47	235	43	RCL
	076	95	=	156	65	x	236	28	28
	077	94	+/-	157	43	RCL	237	65	x
	078	42	STD	158	44	44	238	43	RCL
	079	39	39	159	85	+	239	30	30
				V_{iA}^*					
				A_{ij}/h					
							$ A $		

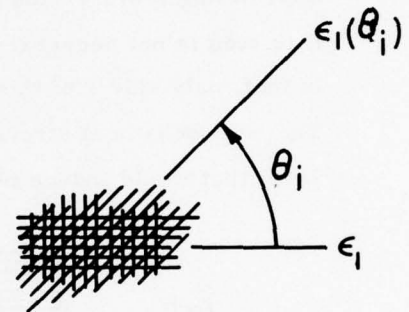
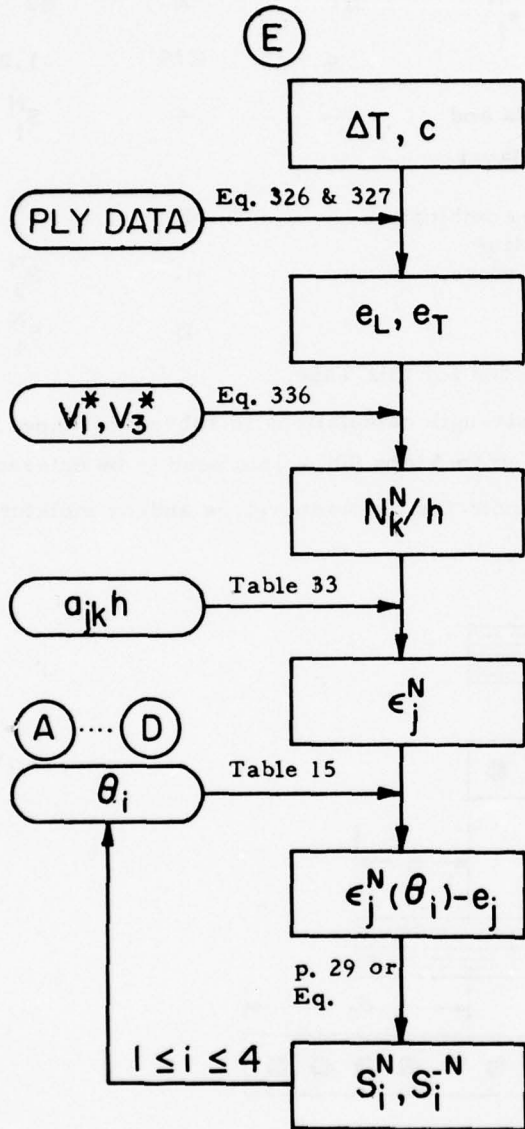
Tape #3 In-Plane Stiffness

240	85	+		320	43	RCL		400	15	15	
241	43	RCL		321	31	31		401	44	SUM	
242	29	29		322	95	=		402	17	17	
243	65	x		323	42	STD		403	44	SUM	
244	43	RCL		324	37	37		404	19	19	
245	31	31		325	43	RCL		405	00	0	
246	65	x		326	31	31		406	42	STD	
247	43	RCL		327	65	x		407	46	46	
248	32	32		328	43	RCL		408	42	STD	
249	65	x		329	32	32		409	47	47	
250	02	2		330	75	-		410	42	STD	
251	75	-		331	43	RCL		411	48	48	
252	43	RCL		332	29	29		412	42	STD	
253	28	28		333	65	x		413	49	49	
254	65	x		334	43	RCL		414	42	STD	
255	43	RCL		335	30	30		415	50	50	
256	31	31		336	95	=		416	43	RCL	
257	33	X ²		337	42	STD		417	14	14	
258	75	-		338	35	35		418	42	STD	
259	43	RCL		339	43	RCL		419	40	40	
260	27	27		340	29	29		420	44	SUM	
261	65	x		341	65	x		421	46	46	
262	43	RCL		342	43	RCL		422	43	RCL	
263	32	32		343	31	31		423	13	13	
264	33	X ²		344	75	-		424	71	SBR	
265	75	-		345	43	RCL		425	33	X ²	
266	43	RCL		346	27	27		<hr/>			
267	30	30		347	65	x		θ_2+r	426	76	LBL
268	65	x		348	43	RCL		427	17	B'	
269	43	RCL		349	32	32		428	43	RCL	
270	29	29		350	95	=		429	16	16	
271	33	X ²		351	42	STD		430	42	STD	
272	95	=		352	38	38		431	40	40	
273	42	STD		<hr/>				432	44	SUM	
274	39	39		a_{ij}	353	43	RCL	433	46	46	
275	43	RCL		354	39	39		434	43	RCL	
276	28	28		355	35	1/X		435	15	15	
277	65	x		356	49	PRD		436	71	SBR	
278	43	RCL		357	33	33		437	33	X ²	
279	30	30		358	49	PRD		<hr/>			
280	75	-		359	34	34		θ_3+r	438	76	LBL
281	43	RCL		360	49	PRD		439	18	C'	
282	32	32		361	35	35		440	43	RCL	
283	33	X ²		362	49	PRD		441	18	18	
284	95	=		363	36	36		442	42	STD	
285	42	STD		364	49	PRD		443	40	40	
286	33	33		365	37	37		444	44	SUM	
287	43	RCL		366	49	PRD		445	46	46	
288	27	27		367	38	38		446	43	RCL	
289	65	x		368	01	1		447	17	17	
290	43	RCL		369	95	=		448	71	SBR	
291	28	28		370	91	R/S		449	33	X ²	
292	75	-		<hr/>				<hr/>			
293	43	RCL		Eng'g	371	76	LBL	θ_4+r	450	76	LBL
294	29	29		Const.	372	10	E'	451	19	D'	
295	33	X ²		373	43	RCL		452	43	RCL	
296	95	=		374	33	33		453	20	20	
297	42	STD		375	35	1/X		454	42	STD	
298	36	36		376	91	R/S		455	40	40	
299	43	RCL		377	43	RCL		456	44	SUM	
300	27	27		378	34	34		457	46	46	
301	65	x		379	35	1/X		458	43	RCL	
302	43	RCL		380	91	R/S		459	19	19	
303	30	30		381	43	RCL		460	71	SBR	
304	75	-		382	35	35		461	33	X ²	
305	43	RCL		383	55	+		462	00	0	
306	31	31		384	43	RCL		463	00	0	
307	33	X ²		385	33	33		464	00	0	
308	95	=		386	95	=		465	00	0	
309	42	STD		387	94	+/-		466	00	0	
310	34	34		388	91	R/S		467	00	0	
311	43	RCL		389	43	RCL		468	00	0	
312	29	29		390	36	36		469	00	0	
313	65	x		391	35	1/X		470	00	0	
314	43	RCL		392	91	R/S		471	00	0	
315	32	32		<hr/>				472	00	0	
316	75	-		θ_1+r	393	76	LBL	473	00	0	
317	43	RCL		394	16	R'		474	00	0	
318	28	28		395	42	STD		475	00	0	
319	65	x		396	00	00		476	00	0	
				397	44	SUM		477	00	0	
				398	13	13		478	00	0	
				399	44	SUM		479	00	0	

Tape #3 In-Plane Stiffness/Sample Problems

	0.00	00	0.00	00	0.00	00	0.00	00
	181.81114	09 01	181.81114	09 01	181.81114	09 01	181.81114	09 01
	10.346159	09 02	10.346159	09 02	10.346159	09 02	10.346159	09 02
	2.8969244	09 03	2.8969244	09 03	2.8969244	09 03	2.8969244	09 03
	0.00	04	0.00	04	0.00	04	0.00	04
	0.00	05	0.00	05	0.00	05	0.00	05
	0.00	06	0.00	06	0.00	06	0.00	06
	0.00	07	0.00	07	0.00	07	0.00	07
	0.00	08	0.00	08	0.00	08	0.00	08
	0.00	09	0.00	09	0.00	09	0.00	09
	0.00	10	0.00	10	0.00	10	0.00	10
	0.00	11	0.00	11	0.00	11	0.00	11
	0.00	12	0.00	12	0.00	12	0.00	12
θ_i	0.00	13	45.00	13	0.00	13	0.00	13
τ_i	1.00	14	1.00	14	1.00	14	1.00	14
	90.00	15	-45.00	15	60.00	15	90.00	15
	1.00	16	1.00	16	1.00	16	1.00	16
	68.06	17	68.06	17	-60.00	17	45.00	17
	181.09	18	181.09	18	1.00	18	1.00	18
	10.3	09 19	10.3	09 19	10.3	09 19	-45.00	19
	280.-03	20	280.-03	20	280.-03	20	1.00	20
	7.17	09 21	7.17	09 21	7.17	09 21	7.17	09 21
	10.-09	22	10.-09	22	10.-09	22	10.-09	22
	12.5-06	23	12.5-06	23	12.5-06	23	12.5-06	23
	0.00	24	0.00	24	0.00	24	0.00	24
	600.-03	25	600.-03	25	600.-03	25	600.-03	25
R	500.-06	26	500.-06	26	750.-06	26	1.-03	26
A_{ij}/h	96.078649	09 27	56.657787	09 27	76.368218	09 27	76.368218	09 27
	96.078649	09 28	56.657787	09 28	76.368218	09 28	76.368218	09 28
	2.8969244	09 29	42.317787	09 29	22.607356	09 29	22.607356	09 29
	7.17	09 30	46.590862	09 30	26.880431	09 30	26.880431	09 30
	0.00	31	0.00	31	0.00	31	0.00	31
	0.00	32	0.00	32	0.00	32	0.00	32
a_{ij}/h	10.417611	-12 33	39.919255	-12 33	14.352198	-12 33	14.352198	-12 33
	10.417611	-12 34	39.919255	-12 34	14.352198	-12 34	14.352198	-12 34
	-314.10757	-15 35	-29.815752	-12 35	-4.2486946	-12 35	-4.2486946	-12 35
	139.47001	-12 36	21.463436	-12 36	37.201784	-12 36	37.201784	-12 36
	0.00	37	0.00	37	0.00	37	0.00	37
	0.00	38	0.00	38	0.00	38	0.00	38
	66.126864	30 39	66.126864	30 39	143.0311	30 39	143.0311	30 39
	1.00	40	1.00	40	1.00	40	1.00	40
	125.-06	41	125.-06	41	125.-06	41	125.-06	41
	49.487787	09 42	49.487787	09 42	49.487787	09 42	49.487787	09 42
	26.880431	09 43	26.880431	09 43	26.880431	09 43	26.880431	09 43
	85.73249	09 44	85.73249	09 44	85.73249	09 44	85.73249	09 44
	19.710431	09 45	19.710431	09 45	19.710431	09 45	19.710431	09 45
	2.00	46	2.00	46	3.00	46	4.00	46
	0.00	47	0.00	47	433.33333	-15 47	0.00	47
	1.00	48	-1.00	48	-733.33333	-15 48	0.00	48
	0.00	49	0.00	49	0.00	49	0.00	49
	0.00	50	0.00	50	0.00	50	0.00	50
	-3.3603243	-18 51	-3.3603243	-18 51	-3.3603243	-18 51	-3.3603243	-18 51
	0.00	52	0.00	52	0.00	52	0.00	52
	0.00	53	0.00	53	0.00	53	0.00	53
	12.004384	03 54	12.004384	03 54	12.004384	03 54	12.004384	03 54
	10.680652	03 55	10.680652	03 55	10.680652	03 55	10.680652	03 55
	-3.0691032	03 56	-3.0691032	03 56	-3.0691032	03 56	-3.0691032	03 56
	11.117842	03 57	11.117842	03 57	11.117842	03 57	11.117842	03 57
	60.646995	00 58	60.646995	00 58	60.646995	00 58	60.646995	00 58
	216.59641	00 59	216.59641	00 59	216.59641	00 59	216.59641	00 59

TAPE #4
 IN-PLANE NON MECHANICAL STRAINS
 OF SYMMETRIC LAMINATES



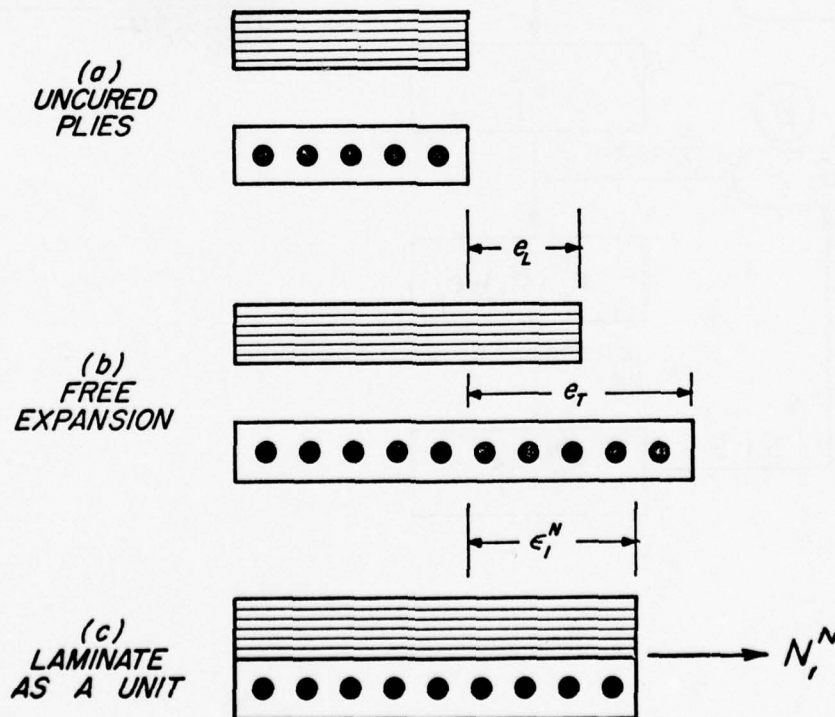
USER INSTRUCTIONS

TAPE #4: IN-PLANE NONMECHANICAL STRAINS OF SYMMETRIC LAMINATES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
0	Data from Tape #3 must be in storage.*	--		--
1	Enter ΔT , and c and calculate ϵ_j^N	ΔT c	E R/S	ΔT 1.00
2 **	Calculate nonmechanical strains and the strength ratios S_i^N for each layer, $i=1-4$. The strengths are based on the combination of environmentally induced strains from both temperature and moisture.	-- -- -- --	A B C D	S_1^N S_2^N S_3^N S_4^N

* Data in Registers 47 and 49 are needed for this Tape.

** This step is not necessary for the strength calculations in subsequent tapes. In fact, only side 1 of this tape (program steps 000 - 166) need to be entered. The nonmechanical strength ratio indicates the temperature and/or moisture level that would induce ply failures.



Tape* 4

Title IN-PLANE NONMECHANICAL STRAINS OF SYMMETRIC LAMINATES

KEYS		STORAGE MEMORIES					
A	S_1^N	0	γ	20	n_4	40	$q, \dots S_i^N, S_4^N$
		1	Q_{11}	21	$2\theta_i$	41	
A'		2	Q_{22}	22	α_L^T	42	I_{1Q}
		3	Q_{12}	23	α_T^T	43	I_{2Q}
B	S_2^N	4	N_1^N/h	24	α_L^H	44	R_{1Q}
		5	N_2^N/h	25	α_T^H	45	R_{2Q}
B'		6	N_6^N/h	26	h	46	n
		7	$e_1^N(\theta_i) - e_L$	27	S_1^{-N}	47	v_{1A}^*
C	S_3^N	8	$e_2^N(\theta_i) - e_T$	28	S_2^{-N}	48	$v_{2A}^*, \Delta T$
		9	$e_6^N(\theta_i)$	29	S_3^{-N}	49	v_{3A}^*
C'		10	e_1^N	30	S_1^N	50	v_{4A}^*, c
		11	e_2^N	31	S_2^N	51	
D	S_4^N	12	e_6^N	32	S_3^N	52	e_L
		13	θ_1	33	$a_{11} h$	53	e_T
D'		14	n_1	34	$a_{22} h$	54	G_{11}
		15	θ_2	35	$a_{12} h$	55	G_{22}
E	$\Delta T, c$	16	n_2	36	$a_{66} h$	56	G_{12}
		17	θ_3	37	$a_{16} h$	57	G_{66}
E'		18	n_3	38	$a_{26} h$	58	G_1
		19	θ_4	39	$p, A \dots S_4^{-N}$	59	G_2

Tape #4 In-Plane Nonmechanical

N/R	000	76	LRL	080	85	+			160	36	36
	001	15	E	081	43	RCL			161	95	=
	002	57	ENG	082	39	39			162	42	STD
	003	42	STD	083	95	=			163	12	12
	004	48	48	084	42	STD			164	01	1
	005	91	R/S	085	04	04			165	95	=
	006	42	STD	086	75	-			166	91	R/S
	007	50	50	087	02	2			S_1^N		
	008	65	x	088	65	x			167	76	LBL
	009	43	RCL	089	43	RCL			168	11	A
	010	24	24	090	47	47			169	43	RCL
	011	85	+	091	65	x			170	13	13
	012	43	RCL	092	43	RCL			171	71	SBR
	013	48	48	093	40	40			172	35	1/X
	014	65	x	094	95	=			173	42	STD
	015	43	RCL	095	42	STD			174	27	27
	016	22	22	096	05	05			175	43	RCL
	017	95	=	097	43	RCL			176	40	40
	018	42	STD	098	49	49			177	42	STD
	019	52	52	099	65	x			178	42	42
	020	08	8	100	43	RCL			179	91	R/S
	021	66	PAU	101	40	40			S_2^N		
	022	43	RCL	102	95	=			180	76	LBL
	023	48	48	103	94	+/-			181	12	B
	024	65	x	104	42	STD			182	43	RCL
	025	43	RCL	105	06	06			183	15	15
	026	23	23	106	65	x			184	71	SBR
	027	85	+	107	43	RCL	ϵ_j^N		185	35	1/X
	028	43	RCL	108	37	37			186	42	STD
	029	50	50	109	85	+			187	28	28
	030	65	x	110	43	RCL			188	43	RCL
	031	43	RCL	111	04	04			189	40	40
	032	25	25	112	65	x			190	42	STD
	033	95	=	113	43	RCL			191	43	43
	034	42	STD	114	33	33			192	91	R/S
	035	53	53	115	85	+			S_3^N		
	036	65	x	116	43	RCL			193	76	LBL
	037	43	RCL	117	05	05			194	13	C
	038	03	03	118	65	x			195	43	RCL
	039	85	+	119	43	RCL			196	17	17
	040	43	RCL	120	35	35			197	71	SBR
	041	52	52	121	95	=			198	35	1/X
	042	65	x	122	42	STD			199	42	STD
	043	43	RCL	123	10	10			200	29	29
	044	01	01	124	43	RCL			201	43	RCL
	045	95	=	125	04	04			202	40	40
	046	42	STD	126	65	x			203	42	STD
	047	39	39	127	43	RCL			204	44	44
	048	43	RCL	128	35	35			205	91	R/S
	049	52	52	129	85	+			S_4^N		
	050	65	x	130	43	RCL			206	76	LBL
	051	43	RCL	131	05	05			207	14	D
	052	03	03	132	65	x			208	43	RCL
	053	85	+	133	43	RCL			209	19	19
	054	43	RCL	134	34	34			210	71	SBR
	055	53	53	135	85	+			211	35	1/X
	056	65	x	136	43	RCL			212	42	STD
	057	43	RCL	137	06	06			213	30	30
	058	02	02	138	65	x			214	43	RCL
	059	95	=	139	43	RCL			215	40	40
	060	42	STD	140	38	38			216	42	STD
	061	40	40	141	95	=			217	45	45
	062	85	+	142	42	STD			218	91	R/S
	063	43	RCL	143	11	11			ϵ_j^N		
	064	39	39	144	43	RCL			219	76	LBL
	065	95	=	145	04	04			220	35	1/X
	066	55	-	146	65	x			221	65	x
	067	02	2	147	43	RCL			222	02	2
	068	95	=	148	37	37			223	95	=
	069	42	STD	149	85	+			224	42	STD
	070	39	39	150	43	RCL			225	21	21
	071	75	-	151	05	05			226	01	1
	072	43	RCL	152	65	x			227	00	0
	073	40	40	153	43	RCL			228	66	PAU
	074	95	=	154	38	38			229	43	RCL
	075	42	STD	155	85	+			230	10	10
	076	40	40	156	43	RCL			231	85	+
	077	65	x	157	06	06			232	43	RCL
	078	43	RCL	158	65	x			233	11	11
	079	47	47	159	43	RCL			234	95	=
									235	55	-
									236	02	2
									237	95	=
									238	42	STD
									239	39	39

Tape #4 In-Plane Nonmechanical

240	75		320	65	x	400	00	0
241	43	RCL	321	43	RCL	401	00	0
242	11	11	322	07	07	402	00	0
243	95	=	323	65	x	403	00	0
244	42	STD	324	43	RCL	404	00	0
245	40	40	325	08	08	405	00	0
246	65	x	326	85	+	406	00	0
247	43	RCL	327	43	RCL	407	00	0
248	21	21	328	55	55	408	00	0
249	39	CDS	329	65	x	409	00	0
250	85	+	330	43	RCL	410	00	0
251	43	RCL	331	08	08	411	00	0
252	39	39	332	33	X ²	412	00	0
253	85	+	333	95	=	413	00	0
254	53	(334	42	STD	414	00	0
255	43	RCL	335	39	39	415	00	0
256	12	12	336	43	RCL	416	00	0
257	65	x	337	58	58	417	00	0
258	43	RCL	338	65	x	418	00	0
259	21	21	339	43	RCL	419	00	0
260	38	SIN	340	07	07	420	00	0
261	54)	341	85	+	421	00	0
262	55	-	342	43	RCL	422	00	0
263	02	2	343	59	59	423	00	0
264	75	-	344	65	x	424	00	0
265	43	RCL	345	43	RCL	425	00	0
266	52	52	346	08	08	426	00	0
267	95	=	347	95	=	427	00	0
268	42	STD	348	55	-	428	00	0
269	07	07	349	43	RCL	429	00	0
270	75	-	350	39	39	430	00	0
271	43	RCL	351	55	-	431	00	0
272	10	10	352	02	2	432	00	0
273	75	-	353	95	=	433	00	0
274	43	RCL	354	42	STD	434	00	0
275	11	11	355	40	40	435	00	0
276	85	+	356	33	X ²	436	00	0
277	43	RCL	357	85	+	437	00	0
278	52	52	358	43	RCL	438	00	0
279	85	+	359	39	39	439	00	0
280	43	RCL	360	35	1/X	440	00	0
281	53	53	361	95	=	441	00	0
282	95	=	362	34	FX	442	00	0
283	94	+/-	363	42	STD	443	00	0
284	42	STD	364	39	39	444	00	0
285	08	08	365	75	-	445	00	0
286	43	RCL	366	43	RCL	446	00	0
287	12	12	367	40	40	447	00	0
288	65	x	368	95	=	448	00	0
289	43	RCL	369	42	STD	449	00	0
290	21	21	370	40	40	450	00	0
291	39	CDS	371	75	-	451	00	0
292	75	-	372	02	2	452	00	0
293	43	RCL	373	65	x	453	00	0
294	40	40	374	43	RCL	454	00	0
295	65	x	375	39	CDS	455	00	0
296	02	2	376	95	=	456	00	0
297	65	x	377	94	+/-	457	00	0
298	43	RCL	378	92	RTN	458	00	0
299	21	21	379	00	0	459	00	0
300	38	SIN	380	00	0	460	00	0
301	95	=	381	00	0	461	00	0
302	42	STD	382	00	0	462	00	0
303	09	09	383	00	0	463	00	0
304	33	X ²	384	00	0	464	00	0
305	65	x	385	00	0	465	00	0
306	43	RCL	386	00	0	466	00	0
307	57	57	387	00	0	467	00	0
308	85	+	388	00	0	468	00	0
309	43	RCL	389	00	0	469	00	0
310	54	54	390	00	0	470	00	0
311	65	x	391	00	0	471	00	0
312	43	RCL	392	00	0	472	00	0
313	07	07	393	00	0	473	00	0
314	33	X ²	394	00	0	474	00	0
315	85	+	395	00	0	475	00	0
316	02	2	396	00	0	476	00	0
317	65	x	397	00	0	477	00	0
318	43	RCL	398	00	0	478	00	0
319	56	56	399	00	0	479	00	0

Tape #4 In-Plane Nonmechanical / sample problems

0.00	00	0.00	00	0.00	00
181.81114	09 01	181.81114	09 01	181.81114	09 01
10.346159	09 02	10.346159	09 02	10.346159	09 02
2.8969244	09 03	2.8969244	09 03	2.8969244	09 03
-12.553922	06 04	19.864625	06 04	7.3107032	06 04
-12.553922	06 05	19.864625	06 05	7.3107032	06 05
0.00	06	0.00	06	0.00	06
-125.33858	-06 07	200.7023	-06 07	75.363712	-06 07
1.7481614	-03 08	-2.7992977	-03 08	-1.0511363	-03 08
0.00	09	0.00	09	0.00	09
-126.83858	-06 10	200.7023	-06 10	73.863712	-06 10
-126.83858	-06 11	200.7023	-06 11	73.863712	-06 11
0.00	12	0.00	12	0.00	12
0.00	13	0.00	13	0.00	13
1.00	14	1.00	14	1.00	14
90.00	15	90.00	15	90.00	15
1.00	16	1.00	16	1.00	16
68.06	17	68.06	17	68.06	17
181.09	18	181.09	18	181.09	18
10.3	09 19	10.3	09 19	10.3	09 19
280.	-03 20	280.	-03 20	280.	-03 20
180.00	21	180.00	21	180.00	21
10.	-09 22	10.	-09 22	10.	-09 22
12.5	-06 23	12.5	-06 23	12.5	-06 23
0.00	24	0.00	24	0.00	24
600.	-03 25	600.	-03 25	600.	-03 25
500.	-06 26	500.	-06 26	500.	-06 26
13.092402	00 27	1.395767	00 27	3.7170891	00 27
13.092402	00 28	1.395767	00 28	3.7170891	00 28
2.8969244	09 29	2.8969244	09 29	2.8969244	09 29
2.2350152	00 30	8.1762053	00 30	21.774182	00 30
2.2350152	00 31	8.1762053	00 31	21.774182	00 31
0.00	32	0.00	32	0.00	32
10.417611	-12 33	10.417611	-12 33	10.417611	-12 33
10.417611	-12 34	10.417611	-12 34	10.417611	-12 34
-314.10757	-15 35	-314.10757	-15 35	-314.10757	-15 35
139.47001	-12 36	139.47001	-12 36	139.47001	-12 36
0.00	37	0.00	37	0.00	37
0.00	38	0.00	38	0.00	38
7.6637088	00 39	4.7859861	00 39	12.745636	00 39
2.2350152	00 40	8.1762053	00 40	21.774182	00 40
125.	-06 41	125.	-06 41	125.	-06 41
49.487787	09 42	49.487787	09 42	49.487787	09 42
26.880431	09 43	26.880431	09 43	26.880431	09 43
85.73249	09 44	85.73249	09 44	85.73249	09 44
19.710431	09 45	19.710431	09 45	19.710431	09 45
2.00	46	2.00	46	2.00	46
0.00	47	0.00	47	0.00	47
ΔT -150.00	48	0.00	48	-150.00	48
0.00	49	0.00	49	0.00	49
c 0.00	50	5. -03	50	5. -03	50
-3.3603243	-18 51	-3.3603243	-18 51	-3.3603243	-18 51
-1.5	-06 52	0.00	52	-1.5	-06 52
-1.875	-03 53	3. -03	53	1.125	-03 53
12.004384	03 54	12.004384	03 54	12.004384	03 54
10.680652	03 55	10.680652	03 55	10.680652	03 55
-3.0691032	03 56	-3.0691032	03 56	-3.0691032	03 56
11.117842	03 57	11.117842	03 57	11.117842	03 57
60.646995	00 58	60.646995	00 58	60.646995	00 58
216.59641	00 59	216.59641	00 59	216.59641	00 59

TAPE #4

STRENGTH RATIOS FOR NONMECHANICAL STRAINS OF LAMINATES

Define
$$S^N = \left[\frac{\epsilon_{\text{allowed}}}{\epsilon_{\text{imposed}}} \right]^N$$

The strains that must satisfy the failure criterion are

$$\epsilon_i^N \Big|_{\text{allowed}} = \left[\epsilon_i^N - e_i \right]_{\text{all.}} = \left\{ \begin{array}{l} \epsilon_1^N - e_L \\ \epsilon_2^N - e_T \\ \epsilon_6^N \end{array} \right\} \Big|_{\text{allowed}}$$

where ϵ_i^N = nonmechanical strains

$$e_i = \{ e_L, e_T, 0 \} = \text{longitudinal, and transverse strains induced by temperature and moisture.}$$

Final failure criterion

$$G_{ij}(\epsilon_i^N - e_i)(\epsilon_j^N - e_j) + G_i(\epsilon_i^N - e_i) = 1$$

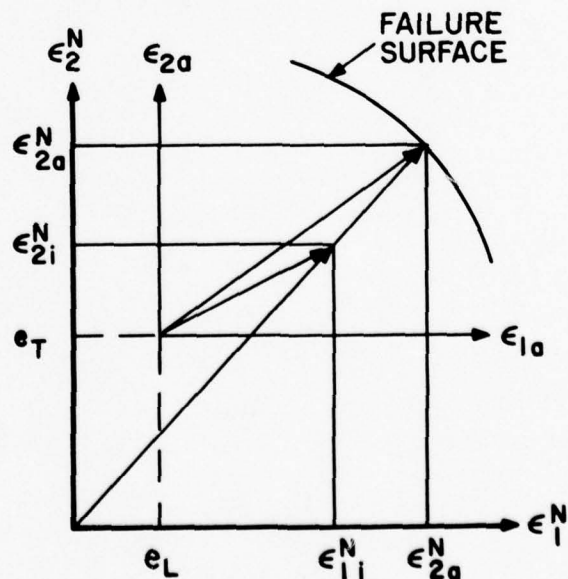
In terms of strength ratio S^N and imposed strain (nonmechanical):

$$G_{ij} S^N(\epsilon_i^N - e_i) S^N(\epsilon_j^N - e_j) + G_i S^N(\epsilon_i^N - e_i) = 1$$

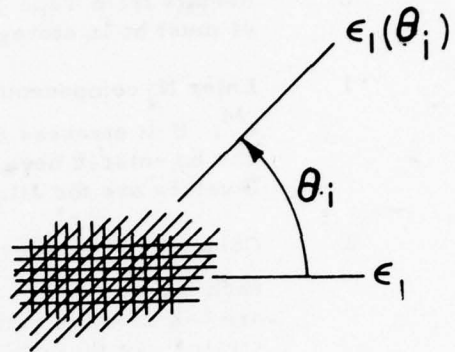
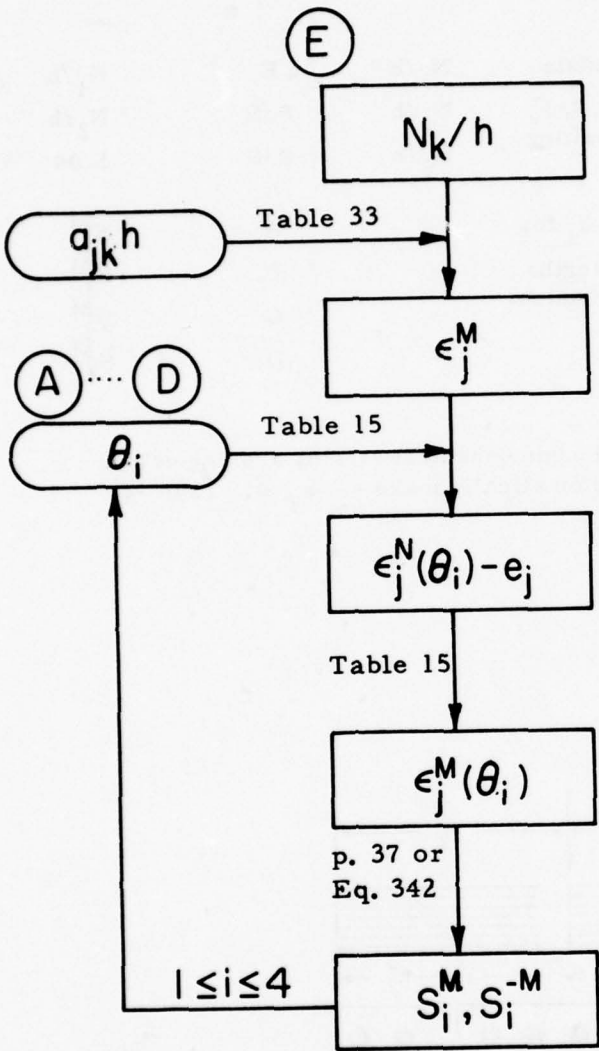
Expand this equation and solve for S^N :

$$a(S^N)^2 + bS^N + c = 0$$

The two roots are S^N and S^{-N} .



TAPE #5
 IN-PLANE STRENGTH OF SYMMETRIC LAMINATES



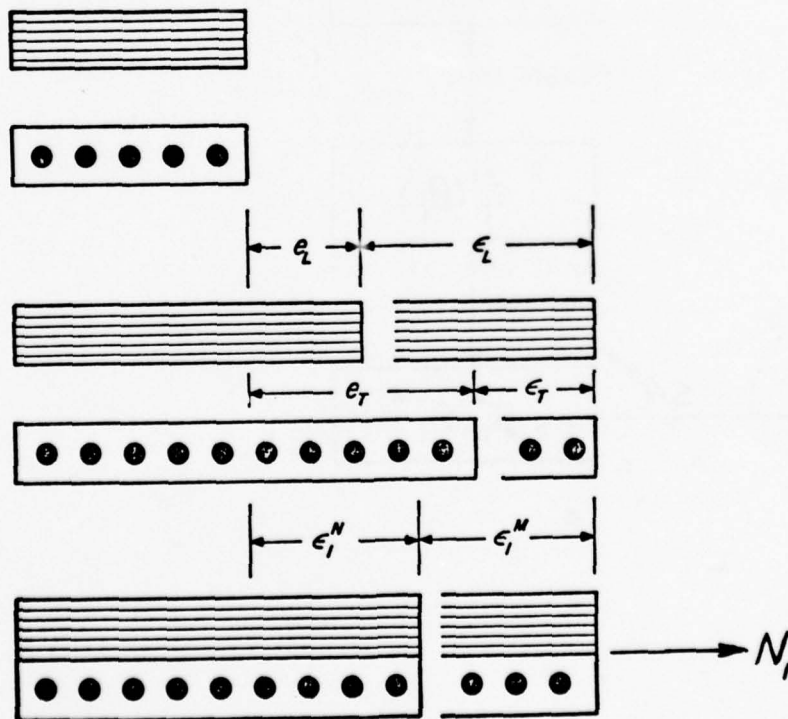
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USER INSTRUCTIONS

TAPE #5: IN-PLANE STRENGTH OF SYMMETRIC LAMINATES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
0	Results from Tape #3, c- #3 and #4 must be in storage*	--		--
1	Enter N_k components and calculate ϵ_i^M . Unit stresses such as [1, 0, 0] can be entered here. The resulting S values are the allowables.	N_1/h N_2/h N_6/h	E R/S R/S	N_1/h N_2/h 1.00
2	Calculate strength ratios S_i & S_i^M for each layer, $i=1-4$. These strengths are based on the ratios of mechanical strains; not the total strains.	-- -- -- --	A B C D	S_1^M S_2^M S_3^M S_4^M

*Tape #5 can be used following Tape #3 if nonmechanical strains are neglected. Ply data tape used in Step 0 of Tape #3 automatically make $\epsilon_L = \epsilon_T = 0$. Tape #4 need not be run for making $\Delta T = c = 0$.



KEYS	STORAGE MEMORIES		
A S_1^M	0	20	40
	1 N_1/h	21 $2\theta_i$	41
A'	2 N_2/h	22	42 S_1^M
	3 N_6/h	23	43 S_2^M
B S_2^M	4	24	44 S_3^M
	5	25	45 S_4^M
B'	6	26	46
	7 e_1^M	27 $e_1^M(\theta_i)$	47 S_1^{-M}
C S_3^M	8 e_2^M	28 $e_2^M(\theta_i)$	48 S_2^{-M}
	9 e_6^M	29 $e_6^M(\theta_i)$	49 S_3^{-M}
C'	10 e_1^N	30 $e_1^N(\theta_i) - e_L$	50 S_4^{-M}
	11 e_2^N	31 $e_2^N(\theta_i) - e_T$	51
D S_4^M	12 e_6^N	32 $e_6^N(\theta_i)$	52 e_L
	13 θ_1	33 a_{11}^h	53 e_T
D'	14	34 a_{22}^h	54 G_{11}
	15 θ_2	35 a_{12}^h	55 G_{22}
E $N_k/h, e_j^M$	16	36 a_{66}^h	56 G_{12}
	17 θ_3	37 a_{16}^h	57 G_{66}
E'	18	38 a_{26}^h	58 G_1
	19 θ_4	39	59 G_2

Tape #5 In-Plane Strength

N_x/R	000	76	LBL	080	40	40	160	65	x	
	001	15	E	081	42	STD	161	43	RCL	
	002	42	STD	082	42	42	162	21	21	
	003	01	01	083	91	R/S	163	38	SIN	
	004	91	R/S	084	76	LBL	164	55	-	
	005	42	STD	085	12	B	165	02	2	
	006	02	02	086	43	RCL	166	75	-	
	007	91	R/S	087	15	15	167	43	RCL	
	008	42	STD	088	71	SBR	168	52	52	
	009	03	03	089	35	1/X	169	95	=	
ϵ_j^M	010	65	x	090	42	STD	170	42	STD	
	011	43	RCL	091	48	48	171	30	30	
	012	37	37	092	43	RCL	172	75	-	
	013	85	+	093	40	40	173	43	RCL	
	014	43	RCL	094	42	STD	174	10	10	
	015	01	01	095	43	43	175	75	-	
	016	65	x	096	91	R/S	176	43	RCL	
	017	43	RCL	097	76	LBL	177	11	11	
	018	33	33	098	13	C	178	85	+	
	019	85	+	099	43	RCL	179	43	RCL	
	020	43	RCL	100	17	17	180	52	52	
	021	02	02	101	71	SBR	181	85	+	
	022	65	x	102	35	1/X	182	43	RCL	
	023	43	RCL	103	42	STD	183	53	53	
	024	35	35	104	49	49	184	95	=	
	025	95	=	105	43	RCL	185	94	+/-	
	026	42	STD	106	40	40	186	42	STD	
	027	07	07	107	42	STD	187	31	31	
	028	43	RCL	108	44	44	188	43	RCL	
	029	01	01	109	91	R/S	189	12	12	
	030	65	x	110	76	LBL	190	65	x	
	031	43	RCL	111	14	D	191	43	RCL	
	032	35	35	112	43	RCL	192	21	21	
	033	85	+	113	19	19	193	39	CDS	
	034	43	RCL	114	71	SBR	194	75	-	
	035	02	02	115	35	1/X	195	43	RCL	
	036	65	x	116	42	STD	196	40	40	
	037	43	RCL	117	50	50	197	65	x	
	038	34	34	118	43	RCL	198	02	2	
	039	85	+	119	40	40	199	65	x	
	040	43	RCL	120	42	STD	200	43	RCL	
	041	03	03	121	46	46	201	21	21	
	042	65	x	122	91	R/S	202	38	SIN	
	043	43	RCL	123	76	LBL	203	95	=	
	044	38	38	124	35	1/X	204	42	STD	
	045	95	=	125	65	x	205	32	32	
	046	42	STD	126	02	2	$\epsilon_j^M(\theta_i)$	206	43	RCL
	047	08	08	127	95	=		207	07	07
	048	43	RCL	128	42	STD		208	85	+
	049	01	01	129	21	21		209	43	RCL
	050	65	x	130	01	1		210	08	08
	051	43	RCL	131	08	8		211	95	=
	052	37	37	132	66	PAU		212	55	+
	053	85	+	133	43	RCL		213	02	2
	054	43	RCL	134	10	10		214	95	=
	055	02	02	135	85	+		215	42	STD
	056	65	x	136	43	RCL		216	39	39
	057	43	RCL	137	11	11		217	75	-
	058	38	38	138	95	=		218	43	RCL
	059	85	+	139	55	+		219	08	08
	060	43	RCL	140	02	2		220	95	=
	061	03	03	141	5	=		221	42	STD
	062	65	x	142	42	STD		222	40	40
	063	43	RCL	143	39	39		223	65	x
	064	36	36	144	75	-		224	43	RCL
	065	95	=	145	43	RCL		225	21	21
	066	42	STD	146	11	11		226	39	CDS
	067	09	09	147	95	=		227	85	+
	068	01	1	148	42	STD		228	43	RCL
	069	95	=	149	40	40		229	39	39
	070	91	R/S	150	65	x		230	85	+
ϵ_j^M	071	76	LBL	151	43	RCL		231	43	RCL
	072	11	A	152	21	21		232	09	09
	073	43	RCL	153	39	CDS		233	65	x
	074	13	13	154	85	+		234	43	RCL
	075	71	SBR	155	43	RCL		235	21	21
	076	35	1/X	156	39	39		236	38	SIN
	077	42	STD	157	85	+		237	55	+
	078	47	47	158	43	RCL		238	02	2
	079	43	RCL	159	12	12		239	95	=

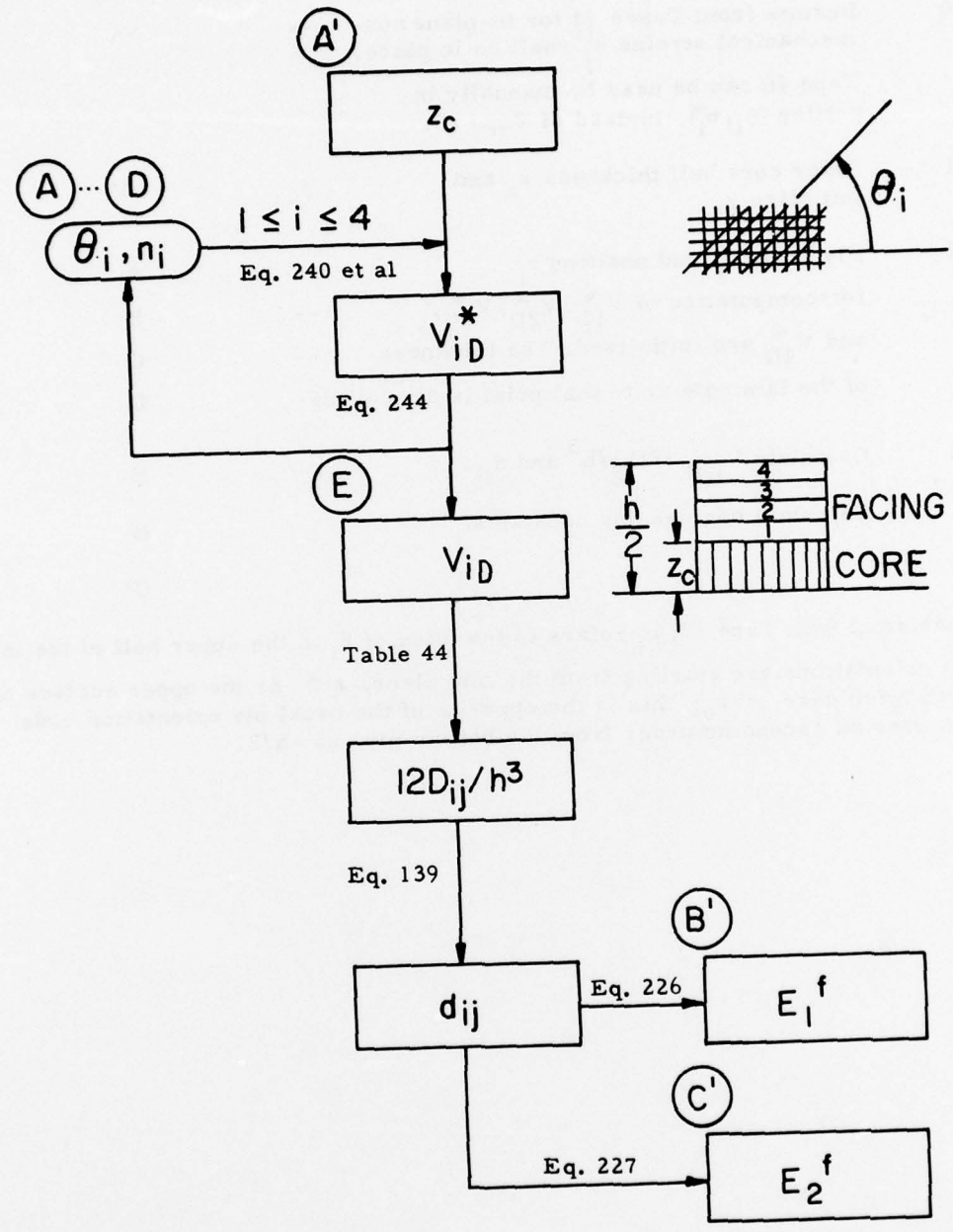
Tape #5 In-Plane Strength

240	42	STD	320	43	RCL	400	32	32
241	27	27	321	27	27	401	33	X ²
242	75	-	322	65	x	402	75	-
243	43	RCL	323	43	RCL	403	43	RCL
244	07	07	324	30	30	404	58	58
245	75	-	325	85	+	405	65	x
246	43	RCL	326	43	RCL	406	43	RCL
247	08	08	327	56	56	407	30	30
248	95	=	328	65	x	408	75	-
249	24	+/-	329	53	<	409	43	RCL
250	42	STD	330	43	RCL	410	59	59
251	28	28	331	27	27	411	65	x
252	43	RCL	332	65	x	412	43	RCL
253	09	09	333	43	RCL	413	31	31
254	65	x	334	31	31	414	95	=
255	43	RCL	335	85	+	415	55	+
256	21	21	336	43	RCL	416	43	RCL
257	39	ODS	337	28	28	417	39	39
258	75	-	338	65	x	418	85	+
259	43	RCL	339	43	RCL	419	43	RCL
260	40	40	340	30	30	420	40	40
261	65	x	341	54	>	421	33	X ²
262	02	2	342	85	+	422	95	=
263	65	x	343	43	RCL	423	34	FX
264	43	RCL	344	55	55	424	42	STD
265	21	21	345	65	x	425	39	39
266	38	SIN	346	43	RCL	426	75	-
267	95	=	347	28	28	427	43	RCL
268	42	STD	348	65	x	428	40	40
269	29	29	349	43	RCL	429	95	=
<i>S_i^M</i> 270	33	X ²	350	31	31	430	42	STD
271	65	x	351	85	+	431	40	40
272	43	RCL	352	43	RCL	432	75	-
273	57	57	353	57	57	433	02	2
274	85	+	354	65	x	434	65	x
275	43	RCL	355	43	RCL	435	43	RCL
276	54	54	356	29	29	436	39	39
277	65	x	357	65	x	437	95	=
278	43	RCL	358	43	RCL	438	94	+/-
279	27	27	359	32	32	439	92	RTN
280	33	X ²	360	95	=	440	00	0
281	85	+	361	55	+	441	00	0
282	02	2	362	43	RCL	442	00	0
283	65	x	363	39	39	443	00	0
284	43	RCL	364	55	+	444	00	0
285	56	56	365	02	2	445	00	0
286	65	x	366	95	=	446	00	0
287	43	RCL	367	42	STD	447	00	0
288	27	27	368	40	40	448	00	0
289	65	x	369	01	1	449	00	0
290	43	RCL	370	75	-	450	00	0
291	28	28	371	43	RCL	451	00	0
292	85	+	372	54	54	452	00	0
293	43	RCL	373	65	x	453	00	0
294	55	55	374	43	RCL	454	00	0
295	65	x	375	30	30	455	00	0
296	43	RCL	376	33	X ²	456	00	0
297	28	28	377	75	-	457	00	0
298	33	X ²	378	02	2	458	00	0
299	95	=	379	65	x	459	00	0
300	42	STD	380	43	RCL	460	00	0
301	39	39	381	56	56	461	00	0
302	43	RCL	382	65	x	462	00	0
303	58	58	383	43	RCL	463	00	0
304	65	x	384	30	30	464	00	0
305	43	RCL	385	65	x	465	00	0
306	27	27	386	43	RCL	466	00	0
307	85	+	387	31	31	467	00	0
308	43	RCL	388	75	-	468	00	0
309	59	59	389	43	RCL	469	00	0
310	65	x	390	55	55	470	00	0
311	43	RCL	391	65	x	471	00	0
312	28	28	392	43	RCL	472	00	0
313	85	+	393	31	31	473	00	0
314	02	2	394	33	X ²	474	00	0
315	65	x	395	75	-	475	00	0
316	53	<	396	43	RCL	476	00	0
317	43	RCL	397	57	57	477	00	0
318	54	54	398	65	x	478	00	0
319	65	x	399	43	RCL	479	00	0

Tape #5 In-Plane Strength/Sample Problems

	0. 00	0. 00	00	0. 00	0. 00	00
N_k	1. 00	1. 00	01	1. 00	1. 00	01
	0. 00	0. 00	02	0. 00	0. 00	02
	0. 00	0. 00	03	0. 00	0. 00	03
	7. 3107032 06	0. 00	04	-111. 69921 00	0. 00	04
	7. 3107032 06	0. 00	05	111. 69921 00	0. 00	05
	0. 00	0. 00	06	0. 00	0. 00	06
	10. 417611-12	10. 417611-12	07	39. 919255-12	39. 919255-12	07
	-314. 10757-15	-314. 10757-15	08	-29. 815752-12	-29. 815752-12	08
	0. 00	0. 00	09	0. 00	0. 00	09
	73. 863712-06	0. 00	10	-7. 7893455-09	0. 00	10
73. 863712-06	0. 00	11	7. 7893455-09	0. 00	11	
0. 00	0. 00	12	0. 00	0. 00	12	
0. 00	0. 00	13	45. 00	45. 00	13	
θ_i n_i	1. 00	1. 00	14	1. 00	1. 00	14
	90. 00	90. 00	15	-45. 00	-45. 00	15
	1. 00	1. 00	16	1. 00	1. 00	16
	68. 06	68. 06	17	68. 06	68. 06	17
	181. 09	181. 09	18	181. 09	181. 09	18
	10. 3 09	10. 3 09	19	10. 3 09	10. 3 09	19
	280. -03	280. -03	20	280. -03	280. -03	20
	180. 00	180. 00	21	-90. 00	-90. 00	21
	10. -09	10. -09	22	10. -09	10. -09	22
	12. 5-06	12. 5-06	23	12. 5-06	12. 5-06	23
0. 00	0. 00	24	0. 00	0. 00	24	
600. -03	600. -03	25	600. -03	600. -03	25	
500. -06	500. -06	26	500. -06	500. -06	26	
-314. 10757-15	-314. 10757-15	27	5. 0517515-12	5. 0517515-12	27	
10. 417611-12	10. 417611-12	28	5. 0517515-12	5. 0517515-12	28	
0. 00	0. 00	29	69. 735007-12	69. 735007-12	29	
75. 363712-06	0. 00	30	1. 5-06	0. 00	30	
-1. 0511363-03	0. 00	31	-1. 125-03	0. 00	31	
0. 00	0. 00	32	-15. 578691-09	0. 00	32	
10. 417611-12	10. 417611-12	33	39. 919255-12	39. 919255-12	33	
10. 417611-12	10. 417611-12	34	39. 919255-12	39. 919255-12	34	
-314. 10757-15	-314. 10757-15	35	-29. 815752-12	-29. 815752-12	35	
139. 47001-12	139. 47001-12	36	21. 463436-12	21. 463436-12	36	
0. 00	0. 00	37	0. 00	0. 00	37	
0. 00	0. 00	38	0. 00	0. 00	38	
1. 3193015 09	1. 3211072 09	39	150. 73203 06	136. 08024 06	39	
473. 81212 06	373. 39552 06	40	138. 67287 06	123. 2282 06	40	
125. -06	125. -06	41	125. -06	125. -06	41	
θ_3	739. 83225 06	681. 88201 06	42	138. 67287 06	123. 2282 06	42
	473. 81212 06	373. 39552 06	43	138. 67287 06	123. 2282 06	43
85. 73249 09	85. 73249 09	44	85. 73249 09	85. 73249 09	44	
19. 710431 09	19. 710431 09	45	19. 710431 09	19. 710431 09	45	
2. 00	2. 00	46	2. 00	2. 00	46	
θ_{-1}	1. 2360994 09	1. 1077053 09	47	162. 79119 06	148. 93229 06	47
	2. 1647909 09	2. 2688189 09	48	162. 79119 06	148. 93229 06	48
0. 00	0. 00	49	0. 00	0. 00	49	
5. -03	0. 00	50	5. -03	0. 00	50	
-3. 3603243-18	-3. 3603243-18	51	-3. 3603243-18	-3. 3603243-18	51	
-1. 5-06	0. 00	52	-1. 5-06	0. 00	52	
1. 125-03	0. 00	53	1. 125-03	0. 00	53	
12. 004384 03	12. 004384 03	54	12. 004384 03	12. 004384 03	54	
10. 680652 03	10. 680652 03	55	10. 680652 03	10. 680652 03	55	
-3. 0691032 03	-3. 0691032 03	56	-3. 0691032 03	-3. 0691032 03	56	
11. 117842 03	11. 117842 03	57	11. 117842 03	11. 117842 03	57	
60. 646995 00	60. 646995 00	58	60. 646995 00	60. 646995 00	58	
216. 59641 00	216. 59641 00	59	216. 59641 00	216. 59641 00	59	

TAPE #6
 FLEXURAL RIGIDITY OF SYMMETRIC SANDWICH PLATES



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USER INSTRUCTIONS

TAPE #6: FLEXURAL RIGIDITY OF SYMMETRIC SANDWICH PLATES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
0	Results from Tapes #4 for in-plane non-mechanical strains ϵ_j^N shall be in place. Tape #6 can be used by manually inputting (θ_i, n_i^*) , instead of Tape #3.	--	--	--
1	Enter core half thickness z_c and initialize z_i	z_c	A'	0.00
2	Ply angle θ_i^* and position z_i for computation of V_{1D}^* , V_{2D}^* , V_{3D}^* and V_{4D}^* are initialized. The thickness of the laminate up to that point is displayed:-	--	A B C D	$2z_1$ $2z_2$ $2z_3$ $2z_4$
3	Calculate V_{iD} , $12D_{ij}/h^3$ and d_{ij} .	--	E	1.00
4	Calculate engineering constants		B' C'	E_1^f E_2^f

* Consistent with Tape #3, n_i refers to the plies of θ_i in the upper half of the laminate.

** Ply orientations are starting from the mid plane, $z=0$, or the upper surface of the sandwich core, $z=z_c$; this is the opposite of the usual ply orientation code which uses an ascending order from the bottom ply, $z = -h/2$.

Tape* 6

FLEXURAL RIGIDITY OF SYMMETRIC SANDWICH
PLATES

KEYS	STORAGE MEMORIES			
A θ_1	0	20	$n_4, z_4 = \frac{h}{2}$	40
	1	21	z_c	41 h_o
A' z_c, z_i	2	22	v_{1D}	42 I_{1Q}
	3	23	v_{2D}	43 I_{2Q}
B θ_2	4	24	v_{3D}	44 R_{1Q}
	5	25	v_{4D}	45 R_{2Q}
B' E_1^f	6	26		46 $1 - \left(\frac{2z_c}{h}\right)^3$
	7	27	$12D_{11}/h^3$	47
C θ_3	8	28	$12D_{22}/h^3$	48
	9	29	$12D_{12}/h^3$	49 $2\theta_i$
C' E_2^f	10	e_1^N	$12D_{66}/h^3$	50 $z_i^3 - z_{i-1}^3$
	11	e_2^N	$12D_{16}/h^3$	51 $h/2, h^3/12$
D θ_4	12	e_6^N	$12D_{26}/h^3$	52 e_L
	13	θ_1	d_{11}	53 e_T
D'	14	n_1, z_1	d_{22}	54 G_{11}
	15	θ_2	d_{12}	55 G_{22}
E $12D_{ij}/h^3, d_{ij}$	16	n_2, z_2	d_{66}	56 G_{12}
	17	θ_3	d_{16}	57 G_{66}
E'	18	n_3, z_3	d_{26}	58 G_1
	19	θ_4	$ D $	59 G_2

Tape #6 Flexural Rigidity

ξ_i 000 76 LBL
 001 16 R*
 002 42 STD
 003 21 21
 004 85 +
 005 43 RCL
 006 14 14
 007 65 x
 008 43 RCL
 009 41 41
 010 95 =
 011 42 STD
 012 14 14
 013 85 +
 014 43 RCL
 015 16 16
 016 65 x
 017 43 RCL
 018 41 41
 019 95 =
 020 42 STD
 021 16 16
 022 85 +
 023 43 RCL
 024 18 18
 025 65 x
 026 43 RCL
 027 41 41
 028 95 =
 029 42 STD
 030 18 18
 031 85 +
 032 43 RCL
 033 20 20
 034 65 x
 035 43 RCL
 036 41 41
 037 95 =
 038 42 STD
 039 20 20
 040 00 0
 041 42 STD
 042 22 22
 043 42 STD
 044 23 23
 045 42 STD
 046 24 24
 047 42 STD
 048 25 25
 049 91 R/S

 ξ_1 050 76 LBL
 051 11 R
 052 43 RCL
 053 14 14
 054 42 STD
 055 51 51
 056 45 YX
 057 03 3
 058 75 -
 059 43 RCL
 060 21 21
 061 45 YX
 062 03 3
 063 95 =
 064 42 STD
 065 50 50
 066 43 RCL
 067 13 13
 068 71 SBR
 069 33 X²

 ξ_2 070 76 LBL
 071 12 B
 072 43 RCL
 073 16 16
 074 42 STD
 075 51 51
 076 45 YX
 077 03 3
 078 75 -
 079 43 RCL

080 14 14
 081 45 YX
 082 03 3
 083 95 =
 084 42 STD
 085 50 50
 086 43 RCL
 087 15 15
 088 71 SBR
 089 33 X²

 ξ_3 090 76 LBL
 091 13 0
 092 43 RCL
 093 18 18
 094 42 STD
 095 51 51
 096 45 YX
 097 03 3
 098 75 -
 099 43 RCL
 100 16 16
 101 45 YX
 102 03 3
 103 95 =
 104 42 STD
 105 50 50
 106 43 RCL
 107 17 17
 108 71 SBR
 109 33 X²

 ξ_4 110 76 LBL
 111 14 0
 112 43 RCL
 113 20 20
 114 42 STD
 115 51 51
 116 45 YX
 117 03 3
 118 75 -
 119 43 RCL
 120 18 18
 121 45 YX
 122 03 3
 123 95 =
 124 42 STD
 125 50 50
 126 43 RCL
 127 19 19

 V_{iD}^* 128 76 LBL
 129 33 X²
 130 65 x
 131 02 2
 132 95 =
 133 94 +/-
 134 42 STD
 135 49 49
 136 39 COS
 137 65 x
 138 43 RCL
 139 50 50
 140 95 =
 141 44 SUM
 142 22 22
 143 43 RCL
 144 49 49
 145 38 SIN
 146 65 x
 147 43 RCL
 148 50 50
 149 95 =
 150 44 SUM
 151 24 24
 152 02 2
 153 49 PRD
 154 49 49
 155 43 RCL
 156 49 49
 157 39 COS
 158 65 x
 159 43 RCL

160 50 50
 161 95 =
 162 44 SUM
 163 23 23
 164 43 RCL
 165 49 49
 166 38 SIN
 167 65 x
 168 43 RCL
 169 50 50
 170 95 =
 171 44 SUM
 172 25 25
 173 43 RCL
 174 51 51
 175 65 x
 176 02 2
 177 95 =
 178 91 R/S

 V_{iD} 179 76 LBL
 180 15 E
 181 01 1
 182 03 3
 183 66 PRD
 184 43 RCL
 185 51 51
 186 45 YX
 187 03 3
 188 95 =
 189 35 1/X
 190 49 PRD
 191 22 22
 192 49 PRD
 193 23 23
 194 49 PRD
 195 24 24
 196 49 PRD
 197 25 25
 198 65 x
 199 43 RCL
 200 21 21
 201 45 YX
 202 03 3
 203 75 -
 204 01 1
 205 95 =
 206 94 +/-
 207 42 STD
 208 46 46

 $\frac{12}{43} D_{ij}$ 209 43 RCL
 210 42 42
 211 85 +
 212 43 RCL
 213 43 43
 214 95 =
 215 65 x
 216 43 RCL
 217 46 46
 218 85 +
 219 43 RCL
 220 22 22
 221 65 x
 222 43 RCL
 223 44 44
 224 85 +
 225 43 RCL
 226 23 23
 227 65 x
 228 43 RCL
 229 45 45
 230 95 =
 231 42 STD
 232 27 27
 233 75 -
 234 02 2
 235 65 x
 236 43 RCL
 237 22 22
 238 65 x
 239 43 RCL

Tape #6 Flexural Rigidity

240	44	44	320	31	31	400	43	RCL	
241	95	=	321	65	x	401	31	31	
242	42	STD	322	43	RCL	402	65	x	
243	28	28	323	32	32	403	43	RCL	
244	43	RCL	324	65	x	404	32	32	
245	42	42	325	02	2	405	75	-	
246	75	-	326	75	-	406	43	RCL	
247	43	RCL	327	43	RCL	407	29	29	
248	43	43	328	28	28	408	65	x	
249	95	=	329	65	x	409	43	RCL	
250	65	x	330	43	RCL	410	30	30	
251	43	RCL	331	31	31	411	95	=	
252	46	46	332	33	X ²	412	42	STD	
253	75	-	333	75	-	413	35	35	
254	43	RCL	334	43	RCL	414	43	RCL	
255	23	23	335	27	27	415	29	29	
256	65	x	336	65	x	416	65	x	
257	43	RCL	337	43	RCL	417	43	RCL	
258	45	45	338	32	32	418	31	31	
259	95	=	339	33	X ²	419	75	-	
260	42	STD	340	75	-	420	43	RCL	
261	29	29	341	43	RCL	421	27	27	
262	75	-	342	30	30	422	65	x	
263	43	RCL	343	65	x	423	43	RCL	
264	42	42	344	43	RCL	424	32	32	
265	65	x	345	29	29	425	95	=	
266	43	RCL	346	33	X ²	426	42	STD	
267	46	46	347	95	=	427	38	38	
268	85	+	348	42	STD	428	43	RCL	
269	02	2	349	39	39	429	51	51	
270	65	x	350	43	RCL	430	45	Y ^x	
271	43	RCL	351	28	28	431	03	3	
272	43	43	352	65	x	432	65	x	
273	65	x	353	43	RCL	433	02	2	
274	43	RCL	354	30	30	434	55	-	
275	46	46	355	75	-	435	03	3	
276	95	=	356	43	RCL	436	95	=	
277	42	STD	357	32	32	437	42	STD	
278	30	30	358	33	X ²	438	51	51	
279	43	RCL	359	95	=	439	65	x	
280	24	24	360	42	STD	440	43	RCL	
281	65	x	361	33	33	441	39	39	
282	43	RCL	362	43	RCL	442	95	=	
283	44	44	363	27	27	443	35	1/X	
284	55	+	364	65	x	444	49	PRD	
285	02	2	365	43	RCL	445	33	33	
286	85	+	366	28	28	446	49	PRD	
287	43	RCL	367	75	-	447	34	34	
288	25	25	368	43	RCL	448	49	PRD	
289	65	x	369	29	29	449	35	35	
290	43	RCL	370	33	X ²	450	49	PRD	
291	45	45	371	95	=	451	36	36	
292	95	=	372	42	STD	452	39	PRD	
293	94	+/-	373	36	36	453	37	37	
294	42	STD	374	43	RCL	454	49	PRD	
295	31	31	375	27	27	455	38	38	
296	85	+	376	65	x	456	01	1	
297	02	2	377	43	RCL	457	95	=	
298	65	x	378	30	30	458	91	R/S	
299	43	RCL	379	75	-	459	76	LBL	
300	25	25	380	43	RCL	460	17	B'	
301	65	x	381	31	31	461	43	RCL	
302	43	RCL	382	33	X ²	462	33	33	
303	45	45	383	95	=	463	65	x	
304	95	=	384	42	STD	464	43	RCL	
305	42	STD	385	34	34	465	51	51	
306	32	32	386	43	RCL	466	95	=	
IDI	307	43	RCL	387	29	29	467	35	1/X
	308	27	27	388	65	x	468	91	R/S
	309	65	x	389	43	RCL	469	76	LBL
	310	43	RCL	390	32	32	470	18	C'
	311	28	28	391	75	-	471	43	RCL
	312	65	x	392	43	RCL	472	34	34
	313	43	RCL	393	28	28	473	65	x
	314	30	30	394	65	x	474	43	RCL
	315	85	+	395	43	RCL	475	51	51
	316	43	RCL	396	31	31	476	95	=
	317	29	29	397	95	=	477	35	1/X
	318	65	x	398	42	STD	478	91	R/S
	319	43	RCL	399	37	37	479	00	0

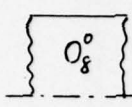

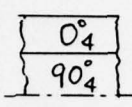
d_{ij}

d_{ij}*

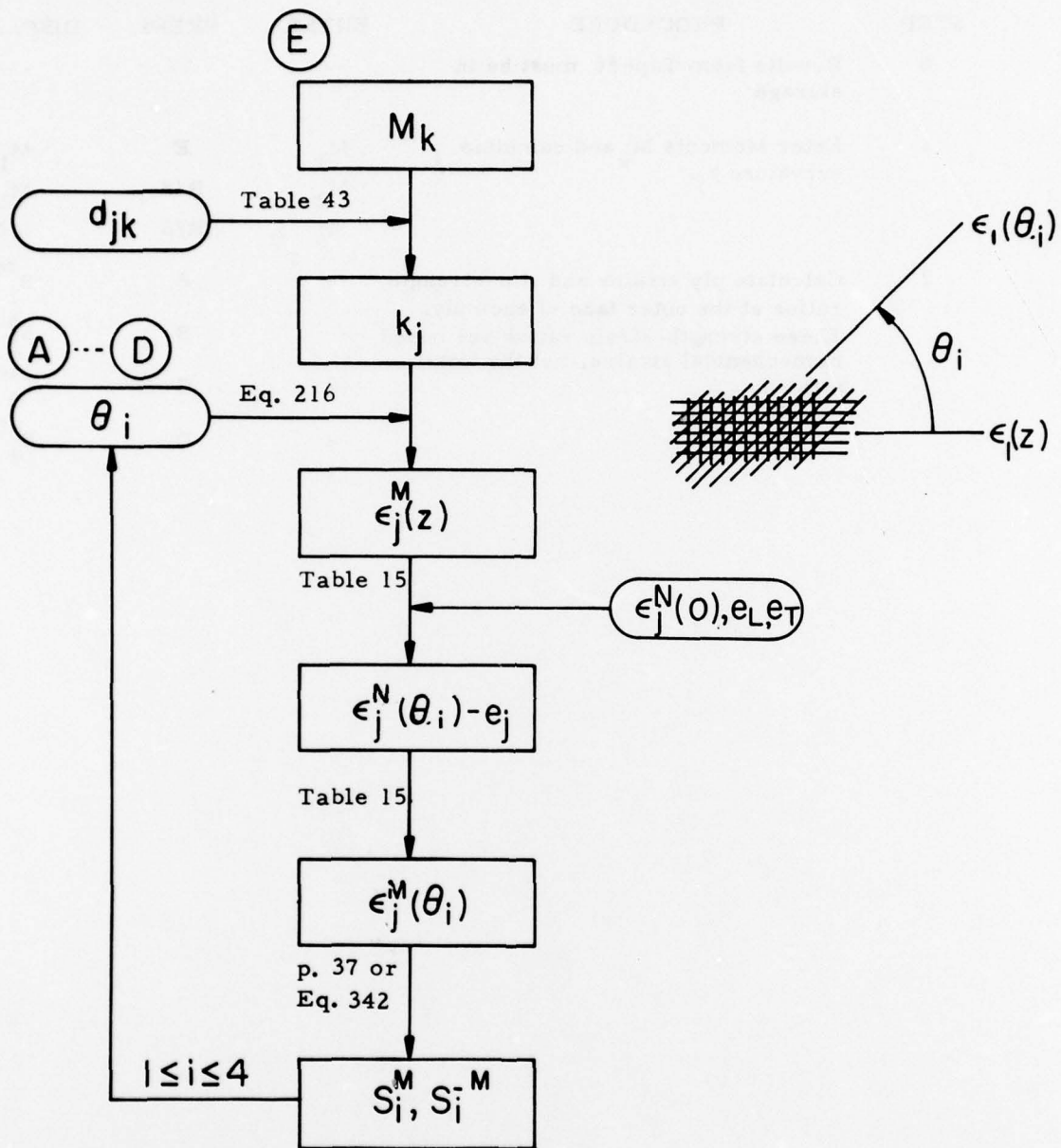
E_f

E_f

Tape #6 Flexural Rigidity / Sample Problems

	0. 00	0. 00	0. 00	0. 00	00
	181.81114 09	181.81114 09	181.81114 09	181.81114 09	01
	10.346159 09	10.346159 09	10.346159 09	10.346159 09	02
	2.8969244 09	2.8969244 09	2.8969244 09	2.8969244 09	03
	0. 00	0. 00	0. 00	0. 00	04
	0. 00		0. 00		0. 00
	0. 00	0. 00	0. 00	0. 00	05
	0. 00	0. 00	0. 00	0. 00	06
	0. 00	0. 00	0. 00	0. 00	07
	0. 00	0. 00	0. 00	0. 00	08
	0. 00	0. 00	0. 00	0. 00	09
	0. 00	0. 00	0. 00	0. 00	10
	0. 00	0. 00	0. 00	0. 00	11
	0. 00	0. 00	0. 00	0. 00	12
θ_1, β_1	0. 00	0. 00	90. 00	90. 00	13
	1. -03	1. -03	500. -06	750. -06	14
	40. 06	40. 06	0. 00	0. 00	15
	3.8447501 00	30.750001 03	θ_2, β_2	1. -03	16
	68. 06	68. 06	68. 06	68. 06	17
	2.8358135 03	22.65575 06	2.828126 03	22.625 06	18
	10.3 09	10.3 09	10.3 09	10.3 09	19
	5.6677823 03	22.65575 06	5.656251 03	22.625 06	20
z_c	0. 00	500. -06	0. 00	500. -06	21
	1. 00	875. -03	750. -03	281.25 -03	22
	1. 00	875. -03	1. 00	875. -03	23
	0. 00	0. 00	0. 00	0. 00	24
	0. 00	0. 00	0. 00	0. 00	25
	0. 00	0. 00	0. 00	0. 00	26
	181.81114 09	159.08475 09	160.37802 09	108.18108 09	27
	10.346159 09	9.0528889 09	31.779281 09	59.956555 09	28
	2.8969244 09	2.5348089 09	2.8969244 09	2.5348089 09	29
$\frac{12D_{ij}}{h^3}$	7.17 09	6.27375 09	7.17 09	6.27375 09	30
	0. 00	0. 00	0. 00	0. 00	31
	0. 00	0. 00	0. 00	0. 00	32
	8.2872928 -03	9.4711918 -03	9.3683286 -03	13.87939 -03	33
	145.63107 -03	166.43551 -03	47.278412 -03	25.042923 -03	34
	-2.320442 -03	-2.6519337 -03	-853.99478 -06	-586.78489 -06	35
d_{ij}	209.20502 -03	239.09145 -03	209.20502 -03	239.09145 -03	36
	0. 00	0. 00	0. 00	0. 00	37
	0. 00	0. 00	0. 00	0. 00	38
	13.426934 30	8.9949971 30	36.483153 30	40.652267 30	39
	0. 00	0. 00	0. 00	0. 00	40
	125. -06	125. -06	125. -06	125. -06	41
	49.487787 09	49.487787 09	49.487787 09	49.487787 09	42
	26.880431 09	26.880431 09	26.880431 09	26.880431 09	43
	85.73249 09	85.73249 09	85.73249 09	85.73249 09	44
	19.710431 09	19.710431 09	19.710431 09	19.710431 09	45
$1 - (\frac{z}{h})^2$	1. 00	875. -03	1. 00	875. -03	46
	0. 00	0. 00	0. 00	0. 00	47
	101.62602 -18	101.62602 -18	101.62602 -18	101.62602 -18	48
	0. 00	0. 00	0. 00	0. 00	49
$\frac{h^3}{12}$	1. -09	875. -12	875. -12	578.125 -12	50
	666.66667 -12	666.66667 -12	666.66667 -12	666.66667 -12	51
	0. 00	0. 00	0. 00	0. 00	52
	0. 00	0. 00	0. 00	0. 00	53
	12.004384 03	12.004384 03	12.004384 03	12.004384 03	54
	10.680652 03	10.680652 03	10.680652 03	10.680652 03	55
	-3.0691032 03	-3.0691032 03	-3.0691032 03	-3.0691032 03	56
	11.117842 03	11.117842 03	11.117842 03	11.117842 03	57
	60.646995 00	60.646995 00	60.646995 00	60.646995 00	58
	216.59641 00	216.59641 00	216.59641 00	216.59641 00	59

TAPE #7
 FLEXURAL STRENGTH OF SYMMETRIC SANDWICH PLATES



USER INSTRUCTION

TAPE #7: FLEXURAL STRENGTH OF SYMMETRIC SANDWICH PLATES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
0	Results from Tape #6 must be in storage	--	--	--
1	Enter Moments M_k and calculate curvature k_j .	M_1	E	M_1
		M_2	R/S	M_2
		M_6	R/S	1.00
2	Calculate ply strains and the strength ratios at the outer face of each ply. These strength-strain ratios are based on mechanical strains, not the total strains.	--	A	S_1^M
		--	B	S_2^M
		--	C	S_3^M
		--	D	S_4^M

KEYS		STORAGE MEMORIES					
A	S_1^M	0		20	z_4	40	$z_i, b, b/2a, S_i$
		1	M_1	21	z_c	41	h_o
A'		2	M_2	22		42	S_1^M
		3	M_6	23		43	S_2^M
B	S_2^M	4	k_1	24		44	S_3^M
		5	k_2	25		45	S_4^M
B'		6	k_6	26	M_6	46	$1 - \left(\frac{2z_c}{h}\right)^3$
		7	$e_1^M(z)$	27	$e_1^M(\theta_i)$	47	S_1^{-M}
C	S_3^M	8	$e_2^M(z)$	28	$e_2^M(\theta_i)$	48	S_2^{-M}
		9	$e_6^M(z)$	29	$e_6^M(\theta_i)$	49	S_3^{-M}
C'		10	e_1^N	30	$e_1^N(\theta_i) - e_L$	50	θ_i, S_4^{-M}
		11	e_2^N	31	$e_2^N(\theta_i) - e_T$	51	$h/2, h^3/12$
D	S_4^M	12	e_6^N	32	$e_6^N(\theta_i)$	52	e_L
		13	θ_1	33	d_{11}	53	e_T
D'		14	z_1	34	d_{22}	54	G_{11}
		15	θ_2	35	d_{12}	55	G_{22}
E	M_k	16	z_2	36	d_{66}	56	G_{12}
		17	θ_3	37	d_{16}	57	G_{66}
E'		18	z_3	38	d_{26}	58	G_1
		19	θ_4	39	$D, a, 1/a, \sqrt{S_i}$	59	G_2

Tape #7 Flexural Strength

M_k	000	76	LBL
	001	15	E
	002	42	STD
	003	01	01
	004	91	R/S
	005	42	STD
	006	02	02
	007	91	R/S
	008	42	STD
	009	03	03
k_j	010	65	x
	011	43	RCL
	012	37	37
	013	85	+
	014	43	RCL
	015	01	01
	016	65	x
	017	43	RCL
	018	33	33
	019	85	+
	020	43	RCL
	021	02	02
	022	65	x
	023	43	RCL
	024	35	35
	025	95	=
	026	42	STD
	027	04	04
	028	43	RCL
	029	01	01
	030	65	x
	031	43	RCL
	032	35	35
	033	85	+
	034	43	RCL
	035	02	02
	036	65	x
	037	43	RCL
	038	34	34
	039	85	+
	040	43	RCL
	041	03	03
	042	65	x
	043	43	RCL
	044	38	38
	045	95	=
	046	42	STD
	047	05	05
	048	43	RCL
	049	01	01
	050	65	x
	051	43	RCL
	052	37	37
	053	85	+
	054	43	RCL
	055	02	02
	056	65	x
	057	43	RCL
	058	38	38
	059	85	+
	060	43	RCL
	061	03	03
	062	65	x
	063	43	RCL
	064	36	36
	065	95	=
	066	42	STD
	067	06	06
	068	01	1
	069	95	=
	070	91	R/S
S_1^M	071	76	LBL
	072	11	A
	073	43	RCL
	074	13	13
	075	42	STD
	076	50	50
	077	43	RCL
	078	14	14
	079	71	SBR

	080	35	1/X
	081	42	STD
	082	47	47
	083	43	RCL
	084	40	40
	085	42	STD
	086	42	42
	087	91	R/S
S_2^M	088	76	LBL
	089	12	B
	090	43	RCL
	091	15	15
	092	42	STD
	093	50	50
	094	43	RCL
	095	16	16
	096	71	SBR
	097	35	1/X
	098	42	STD
	099	48	48
	100	43	RCL
	101	40	40
	102	42	STD
	103	43	43
	104	91	R/S
S_3^M	105	76	LBL
	106	13	C
	107	43	RCL
	108	17	17
	109	42	STD
	110	50	50
	111	43	RCL
	112	18	18
	113	71	SBR
	114	35	1/X
	115	42	STD
	116	49	49
	117	43	RCL
	118	40	40
	119	42	STD
	120	44	44
	121	91	R/S
S_4^M	122	76	LBL
	123	14	D
	124	43	RCL
	125	19	19
	126	42	STD
	127	50	50
	128	43	RCL
	129	20	20
	130	71	SBR
	131	35	1/X
	132	42	STD
	133	50	50
	134	43	RCL
	135	40	40
	136	42	STD
	137	45	45
	138	91	R/S
$S_5^M(z_i)$	139	76	LBL
	140	35	1/X
	141	42	STD
	142	40	40
	143	65	x
	144	43	RCL
	145	04	04
	146	95	=
	147	42	STD
	148	07	07
	149	01	1
	150	09	9
	151	66	PAU
	152	43	RCL
	153	40	40
	154	65	x
	155	43	RCL
	156	05	05
	157	95	=
	158	42	STD
	159	08	08

	160	43	RCL
	161	40	40
	162	65	x
	163	43	RCL
	164	06	06
	165	95	=
	166	42	STD
	167	09	09
$\epsilon_j^N(\theta_i)$	168	02	2
$-e_j$	169	49	PRD
	170	50	50
	171	43	RCL
	172	10	10
	173	85	+
	174	43	RCL
	175	11	11
	176	95	=
	177	55	-
	178	02	2
	179	95	=
	180	42	STD
	181	39	39
	182	75	-
	183	43	RCL
	184	11	11
	185	95	=
	186	42	STD
	187	40	40
	188	65	x
	189	43	RCL
	190	50	50
	191	39	CDS
	192	85	+
	193	43	RCL
	194	39	39
	195	85	+
	196	43	RCL
	197	12	12
	198	65	x
	199	43	RCL
	200	50	50
	201	38	SIN
	202	55	+
	203	02	2
	204	75	-
	205	43	RCL
	206	52	52
	207	95	=
	208	42	STD
	209	30	30
	210	75	-
	211	02	2
	212	65	x
	213	43	RCL
	214	39	39
	215	85	+
	216	43	RCL
	217	52	52
	218	85	+
	219	43	RCL
	220	53	53
	221	95	=
	222	94	+/-
	223	42	STD
	224	31	31
	225	43	RCL
	226	12	12
	227	65	x
	228	43	RCL
	229	50	50
	230	39	CDS
	231	75	-
	232	43	RCL
	233	40	40
	234	65	x
	235	02	2
	236	65	x
	237	43	RCL
	238	50	50
	239	38	SIN

Tape #7 Flexural Strength

$\epsilon_j^M(\theta_j)$

240	95	=
241	42	STD
242	32	32
243	43	RCL
244	07	07
245	85	+
246	43	RCL
247	08	08
248	95	=
249	55	+
250	02	2
251	95	=
252	42	STD
253	39	39
254	75	-
255	43	RCL
256	08	08
257	95	=
258	42	STD
259	40	40
260	65	x
261	43	RCL
262	50	50
263	39	COS
264	85	+
265	43	RCL
266	39	39
267	85	+
268	43	RCL
269	09	09
270	65	x
271	43	RCL
272	50	50
273	38	SIN
274	55	+
275	02	2
276	95	=
277	42	STD
278	27	27
279	75	-
280	43	RCL
281	07	07
282	75	-
283	43	RCL
284	08	08
285	95	=
286	94	+/-
287	42	STD
288	28	28
289	43	RCL
290	09	09
291	65	x
292	43	RCL
293	50	50
294	39	COS
295	75	-
296	43	RCL
297	40	40
298	65	x
299	02	2
300	65	x
301	43	RCL
302	50	50
303	38	SIN
304	95	=
305	42	STD
306	29	29
307	33	X ²
308	65	x
309	43	RCL
310	57	57
311	85	+
312	43	RCL
313	54	54
314	65	x
315	43	RCL
316	27	27
317	33	X ²
318	85	+
319	02	2

σ_i^M

320	75	x
321	43	RCL
322	56	56
323	65	x
324	43	RCL
325	27	27
326	65	x
327	43	RCL
328	28	28
329	85	+
330	43	RCL
331	55	55
332	65	x
333	43	RCL
334	28	28
335	33	X ²
336	95	=
337	42	STD
338	39	39
339	43	RCL
340	58	58
341	65	x
342	43	RCL
343	27	27
344	85	+
345	43	RCL
346	59	59
347	65	x
348	43	RCL
349	28	28
350	85	+
351	02	2
352	65	x
353	53	<
354	43	RCL
355	54	54
356	65	x
357	43	RCL
358	27	27
359	65	x
360	43	RCL
361	30	30
362	85	+
363	43	RCL
364	56	56
365	65	x
366	53	<
367	43	RCL
368	27	27
369	65	x
370	43	RCL
371	31	31
372	85	+
373	43	RCL
374	28	28
375	65	x
376	43	RCL
377	30	30
378	54	>
379	85	+
380	43	RCL
381	55	55
382	65	x
383	43	RCL
384	28	28
385	65	x
386	43	RCL
387	31	31
388	85	+
389	43	RCL
390	57	57
391	65	x
392	43	RCL
393	29	29
394	65	x
395	43	RCL
396	32	32
397	95	=
398	55	-
399	43	RCL

400	39	39
401	55	-
402	02	2
403	95	=
404	42	STD
405	40	40
406	01	1
407	75	-
408	43	RCL
409	54	54
410	65	x
411	43	RCL
412	30	30
413	33	X ²
414	75	-
415	02	2
416	65	x
417	43	RCL
418	56	56
419	65	x
420	43	RCL
421	30	30
422	65	x
423	43	RCL
424	31	31
425	75	-
426	43	RCL
427	55	55
428	65	x
429	43	RCL
430	31	31
431	33	X ²
432	75	-
433	43	RCL
434	57	57
435	65	x
436	43	RCL
437	32	32
438	33	X ²
439	75	-
440	43	RCL
441	58	58
442	65	x
443	43	RCL
444	30	30
445	75	-
446	43	RCL
447	59	59
448	65	x
449	43	RCL
450	31	31
451	95	=
452	55	+
453	43	RCL
454	39	39
455	85	+
456	43	RCL
457	40	40
458	33	X ²
459	95	=
460	34	FX
461	42	STD
462	39	39
463	75	-
464	43	RCL
465	40	40
466	95	=
467	42	STD
468	40	40
469	75	-
470	02	2
471	65	x
472	43	RCL
473	39	39
474	95	=
475	94	+/-
476	92	RTN
477	00	0
478	00	0
479	00	0

Tape #7 Flexural Strength / Sample Problems

	0. 00	0. 00	0. 00	0. 00	00
	1. 00	1. 00	1. 00	1. 00	01
M _k	0. 00	0. 00	0. 00	0. 00	02
	0. 00	0. 00	0. 00	0. 00	03
8. 2872928-03	9. 4711918-03	9. 3683286-03	13. 87939-03		04
-2. 320442-03	-2. 6519337-03	-853. 99478-06	-586. 78489-06		05
0. 00	0. 00	0. 00	0. 00		06
8. 2872928-06	9. 4711918-06	9. 3683286-06	13. 87939-06		07
-2. 320442-06	-2. 6519337-06	-853. 99478-09	-586. 78489-09		08
0. 00	0. 00	0. 00	0. 00		09
0. 00	0. 00	0. 00	0. 00		10
0. 00	0. 00	0. 00	0. 00		11
0. 00	0. 00	0. 00	0. 00		12
0. 00	0. 00	90. 00	90. 00		13
1. -03	1. -03	500. -06	750. -06		14
40. 06	40. 06	0. 00	0. 00		15
3. 8447501 00	30. 750001 03	1. -03	1. -03		16
68. 06	68. 06	68. 06	68. 06		17
2. 8358135 03	22. 65575 06	22. 625 06	22. 625 06		18
10. 3 09	10. 3 09	10. 3 09	10. 3 09		19
5. 6677823 03	22. 65575 06	22. 625 06	22. 625 06		20
0. 00	500. -06	0. 00	500. -06		21
1. 00	875. -03	750. -03	281. 25-03		22
1. 00	875. -03	1. 00	875. -03		23
0. 00	0. 00	0. 00	0. 00		24
0. 00	0. 00	0. 00	0. 00		25
0. 00	0. 00	0. 00	0. 00		26
8. 2872928-06	9. 4711918-06	9. 3683286-06	13. 87939-06		27
-2. 320442-06	-2. 6519337-06	-853. 99478-09	-586. 78489-09		28
0. 00	0. 00	0. 00	0. 00		29
0. 00	0. 00	0. 00	0. 00		30
0. 00	0. 00	0. 00	0. 00		31
0. 00	0. 00	0. 00	0. 00		32
8. 2872928-03	9. 4711918-03	9. 3683286-03	13. 87939-03		33
145. 63107-03	166. 43551-03	47. 278412-03	25. 042923-03		34
-2. 320442-03	-2. 6519337-03	-853. 99478-06	-586. 78489-06		35
209. 20502-03	239. 09145-03	209. 20502-03	239. 09145-03		36
0. 00	0. 00	0. 00	0. 00		37
0. 00	0. 00	0. 00	0. 00		38
1. 03	875. 00	964. 5143 00	667. 40582 00		39
1. 03	875. 00	791. 97978 00	516. 39171 00		40
SM	125. -06	125. -06	125. -06		41
1. 03	875. 00	835. 69432 00	374. 19028 00		42
26. 880431 09	26. 880431 09	791. 97978 00	516. 39171 00		43
85. 73249 09	85. 73249 09	85. 73249 09	85. 73249 09		44
19. 710431 09	19. 710431 09	19. 710431 09	19. 710431 09		45
1. 00	875. -03	1. 00	875. -03		46
SM	1. 03	875. 00	4. 8092482 03	2. 2499333 03	47
101. 62602-18	101. 62602-18	1. 1370488 03	818. 41992 00		48
0. 00	0. 00	0. 00	0. 00		49
0. 00	0. 00	0. 00	0. 00		50
666. 66667-12	666. 66667-12	666. 66667-12	666. 66667-12		51
0. 00	0. 00	0. 00	0. 00		52
0. 00	0. 00	0. 00	0. 00		53
12. 004384 03	12. 004384 03	12. 004384 03	12. 004384 03		54
10. 680652 03	10. 680652 03	10. 680652 03	10. 680652 03		55
-3. 0691032 03	-3. 0691032 03	-3. 0691032 03	-3. 0691032 03		56
11. 117842 03	11. 117842 03	11. 117842 03	11. 117842 03		57
60. 646995 00	60. 646995 00	60. 646995 00	60. 646995 00		58
216. 59641 00	216. 59641 00	216. 59641 00	216. 59641 00		59

DATE
ILMED
-8