

AFOSR-TR- 80 - 0005

Air Force Office of Scientific Research
Grant AFOSR-76-3073

AD A 079597

CURRENTS AND CHARGES ON CYLINDERS
IN A PARALLEL-PLATE TRANSMISSION LINE

Gordon McKay Laboratory
Harvard University
Cambridge, MA 02138

12
LEVEL II

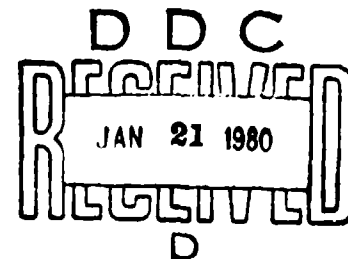
July 1979

Final Report

June 30, 1976 through June 30, 1979

Approved for public release; distribution unlimited

Prepared for
AIR FORCE OFFICE OF SCIENTIFIC RESEARCH (AFSC)
Bolling Air Force Base
Washington, DC 20332



80

1 16 074

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM	
1. REPORT NUMBER (18) AFOSR-TR-80-0005	2. GOVT ACCESSION NO.	3. REPORT TYPE CATALOG NUMBER	
4. TITLE (and Subtitle) CURRENTS AND CHARGES ON CYLINDERS IN A PARALLEL-PLATE TRANSMISSION LINE	5. TYPE OF REPORT & PERIOD COVERED Final Report June 30, 1976 - June 30, 1979		
6. AUTHOR(s) (10) T. T. Wu, M. Krook, R. W. P. King, D. J. Blejer, T. K. Sarkar, S. K. Wan, M. Owens, B. H. Sandler, J. E. Baum, and M. J. Miller	7. CONTRACT OR GRANT NUMBER(s) (15) AFOSR-76-3073		
8. PERFORMING ORGANIZATION NAME AND ADDRESS Harvard University Division of Applied Sciences Cambridge, Massachusetts 02138	10. PROGRAM ELEMENT, PROJECT, TASK AREA & ACQUISITION UNIT NUMBERS (16) 9751-64711F (17) 051		
11. CONTROLLING OFFICE NAME AND ADDRESS Air Force Office of Scientific Research/NP Bolling Air Force Base Washington, DC 20332	12. REPORT DATE (11) Jul 79	13. NUMBER OF PAGES 83	
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office) (12) 841	15. SECURITY CLASS. (of this report) Unclassified		
16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited.		15a. DECLASSIFICATION DOWNGRADING SCHEDULE	
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report) (9) Final Rept. 30 Jun 76-30 Jun 79		Accession For RTIS GRA&I ☒ DDC TAB ☐ Unannounced ☐ Justification ☐	
18. SUPPLEMENTARY NOTES		By _____ Distribution/_____ Availability Codes _____	
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Experimental study, model EMP simulator Electric field in simulator, at two different high frequencies Approximate theoretical representation; TEM, TM, and TE modes Surface charge density distributions Possible methods to improve field in simulator		Dist. Avail and/or special A ☐ ☐	
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) The final report summarizes the results of a 3-year model study to evaluate how well a parallel-plate transmission-line structure simulates an electromagnetic pulse with a plane-wave front. The amplitude and phase of the electric field inside the model simulator have been measured at two high frequencies for which transmission-line theory does not apply. An approximate theoretical representation of the field is used to interpret the measured data. Differences between the actual field and the desired traveling plane-wave field are discussed, and possible methods to improve the field in the simulator are offered.			

DD FORM 1 JAN 73 1473

EDITION OF 1 NOV 65 IS OBSOLETE

457 000

UNCLASSIFIED

SUMMARY

In order to determine the magnitudes and distributions of currents and charges induced on the surfaces of an aircraft when it encounters an electromagnetic pulse generated by a nuclear explosion, large simulators have been constructed in which the aircraft can be exposed to a hopefully comparable electromagnetic environment. One important type consists of a parallel-plate transmission line or open waveguide with tapered triangular ends, between the conductors of which a pulse with a plane wave front must travel. Since the relevant pulse contains a frequency spectrum with wavelengths that extend from very long to relatively short compared to the dimensions of the aircraft, the separation of the two conductors of the transmission-line simulator cannot be kept small compared to all of the wavelengths in the pulse as required for TEM transmission without propagating higher modes. It follows that TEM-mode transmission-line theory can be applied only to the very low frequency part of the spectrum, for which $kh = 2\pi h/\lambda \ll 1$.

The properties of the simulator at higher frequencies are difficult to determine accurately. One approach is to measure the electric field in a model simulator at one or more of the relevant higher frequencies, and then seek to interpret its distribution theoretically. This has been done in a carefully designed model simulator at two operating frequencies, $f = 626.5$ MHz ($\lambda = 48$ cm) and $f = 264$ MHz ($\lambda = 113.6$ cm). When the frequency is so high that kh is not small, as when $kh = 2\pi h/\lambda = 4.5\pi$ or $h = 2.25\lambda$ with $\lambda = 48$ cm and the height $h = 108$ cm, the electric field in the working volume is much more complicated than at low frequencies. This is true to a lesser degree when $kh = 1.32\pi$ or $h = 0.66\lambda$ for $\lambda = 113.6$ cm and $h = 75$ cm. Owing to the wide spacing, most of the energy supplied by the generator is now radiated into the surrounding space, and only a small fraction is dissipated in the load. The structure is essentially an antenna and not a transmission line.

Direct measurements have been made of both the amplitude and phase of the vertical (E_z) and longitudinal (E_y) components of the electric field throughout the working volume and adjacent regions of the simulator, and of E_z on the surfaces of both conducting plates where $E_y = 0$. In order to

interpret the measured results, the field in the working volume has been represented approximately in terms of the mode theory of the infinite parallel-plate waveguide. For the operating wavelength $\lambda = 48$ cm, four modes are well above cut-off. These are the TEM, TM_{01} , TM_{02} , and TM_{03} modes. Comparisons with the measured data indicate that the assumed approximate representation of the field by the superposition of ideal parallel-plate modes is a good one throughout the working volume of the simulator. It is also evident that the total E_z differs greatly from the part contributed by the TEM mode alone. This is true particularly near the top, where the difference between the incident spherical wave in the sloping sections and the plane wave in the working volume is greatest. There is no difference on the ground plane. TE modes contribute only negligibly and are ignored.

The components E_z and E_y in the working volume and adjacent regions were also measured with $f = 264$ MHz when $h = 75$ cm $= 0.66\lambda$ and $\lambda = 113.6$ cm. Now only the TEM and TM_{01} modes are above cut-off; TE modes are neglected. As with the higher frequency and greater height h of the working volume, the approximate representation of E_z and E_y by TEM and TM_{0n} modes is quite satisfactory.

The differences between the actual electromagnetic field in the working volume of the model simulator and the desired traveling plane wave are significant when $h = 108$ cm $= 2.25\lambda$ with $f = 626.5$ MHz, and considerably larger when $h = 75$ cm $= 0.66\lambda$ with $f = 264$ MHz. In the first place, the component E_z of the electric field is not uniform in either the transverse or vertical directions; secondly, there is a component E_y ; and thirdly, there is a significant standing wave. It follows that the electrical environment of a metallic obstacle placed in the working volume is necessarily quite different from what it would be if it were exposed to an incident plane wave. A sample set of measurements of the very sensitive charge density distribution on the surface of a tubular cylinder when located at the center of the working volume has been compared with earlier data taken at the same frequency and on the same cylinder when illuminated by a spherical wave. These are discussed in conjunction with theoretically determined distributions for an incident plane wave. The report closes with a discussion of possible methods of reducing the lateral and vertical nonuniformity of the field in the simulator as well as the standing-wave ratio.

CONTENTS

<u>Section</u>		<u>Page</u>
I	INTRODUCTION	9
II	THE HARVARD EMP SIMULATOR	10
III	PRELIMINARY MEASUREMENTS	16
IV	INTRODUCTORY DESCRIPTION OF THE FIELD IN THE WORKING VOLUME	23
V	THE FIELD IN THE PARALLEL-PLATE SECTION; TEM AND TM MODES	27
VI	THE MEASURED FIELD IN THE WORKING VOLUME: $h = 2.25\lambda = 108 \text{ cm}$, $f = 626.5 \text{ MHz}$	35
VII	THE MEASURED FIELD IN THE WORKING VOLUME: $h = 0.66\lambda = 75 \text{ cm}$, $f = 264 \text{ MHz}$	52
VIII	THE TRANSVERSE VARIATION OF THE ELECTRIC FIELD; TE MODES	56
IX	THE ACTUAL ELECTROMAGNETIC FIELD IN THE SIMULATOR AS AN APPROXIMATION OF A PLANE WAVE	68
X	POSSIBLE METHODS TO IMPROVE THE FIELD IN THE SIMULATOR AS AN APPROXIMATION OF A TRAVELING PLANE WAVE	78
	REFERENCES	81
	LIST OF PERSONNEL	82
	LIST OF PUBLICATIONS	83

AIR FORCE OFFICE OF SCIENTIFIC INFORMATION (AFOSI)
NOTICE OF REVISIONS
This report is approved for release and is
approved for distribution under E.O. 13526 (7b).
Distribution is unlimited.
A. D. BLOCH
Technical Information Officer

ILLUSTRATIONS

<u>Figure</u>		<u>Page</u>
1	Top view of simulator setup.	11
2	Simulator with (1) ground-plane probe, (2) top-plate probe, (3) space probe in working volume.	12
3	Diagrams of space probes.	14
4	Measured E_z along $\theta = 0^\circ$ on ground plane excited by monopole and corner reflector.	17
5	Theoretical electric field along $\theta = 0^\circ$ on ground plane for comparison with measured graphs in Figure 4.	18
6	Standing wave of $ E_z $ near load.	20
7	Measured E_z along $\theta = 0^\circ$ of ground plane of terminated simulator.	21
8	(a) Measured phase fronts in the simulator; (b) Phase angle θ_z along the line $y = -265$ cm; (c) $ E_z $ at $r = 55$ cm from the source.	22
9	Schematic diagrams of spherical wave incident on a plane. (a) Three-dimensional view. (b) Electric field in vertical plane. (c) Magnetic field in horizontal plane.	25
10a	Measured constant phase curves in the working volume; $h = 108$ cm, $b = 114.8$ cm, $f = 626.5$ MHz.	28
10b	Measured constant phase curves in the working volume; $h = 108$ cm, $b = 114.8$ cm, $f = 626.5$ MHz.	29
11	Electric field lines for four parallel-plate modes in working volume; $\lambda = 48$ cm.	32
12	Distribution of standing waves in working volume for each mode; $SWR = 1.36$, $\lambda = 48$ cm.	33
13	Measured magnitude of the vertical and longitudinal components of the electric field in the working volume.	36
14	Measured magnitude and phase of E_z in working volume of model simulator.	37
15	Measured magnitude and phase of E_z in working volume of model simulator.	38
16	Measured magnitude and phase of E_z in working volume of model simulator.	39

<u>Figure</u>		<u>Page</u>
17	Measured magnitude and phase of E_z on parallel plate of model simulator.	40
18	Measured magnitude and phase of E_y in working volume of model simulator.	41
19	Measured magnitude and phase of E_y in working volume of model simulator.	42
20	Measured magnitude and phase of E_y in working volume of model simulator.	43
21	Measured $ E_z $ near center ($x = 1.7$ cm) of working volume at four heights.	44
22	Measured electric field near central plane ($y = 0$) in working volume.	46
23	Amplitudes of TEM and TM_{0n} modes in forward half of working volume.	48
24a	Real part of vertical electric field in working volume. (Phase reference: $x = y = z = 0$.)	50
24b	Imaginary part of vertical electric field in working volume. (Phase reference: $x = y = z = 0$.)	51
25	Measured electric field in transverse plane $y = 0$ of working volume; $b = 114.8$ cm, $2a = 175$ cm, $h = 75$ cm, $f = 264$ MHz.	53
26	Real and imaginary parts of E_z in working volume and adjacent regions; phase referred to $x = y = z = 0$.	54
27	Graphs of the real and imaginary parts of $E_z(y) = A(y) + B(y)\cos(\pi z/h)$ and $E_y(y)$ as functions of y in and near the parallel-plate region.	55
28a	Measured constant phase curves in the working volume; $h = 108$ cm, $a = 87.5$ cm, $b = 114.8$ cm, $f = 626.5$ MHz.	57
28b	Measured constant phase curves in working volume; $h = 108$ cm, $a = 87.5$ cm, $b = 114.8$ cm, $f = 626.5$ MHz.	58
28c	Measured constant phase curves in working volume; $h = 108$ cm, $b = 114.8$ cm, $f = 626.5$ MHz.	59
29	Measured transverse distribution of E_z .	60
30	Transverse distributions of E_z and E_y .	62

<u>Figure</u>		<u>Page</u>
31	Schematic diagram of electric field lines in transverse plane showing fringing at the open side.	63
32a	Schematic diagram of TE_{01} and TE_{03} modes in working volume; solid lines, electric field E_z ; broken lines, magnetic field $H = \hat{x}H_x + \hat{y}H_y$.	66
32b	Schematic diagram of TE_{11} modes in working volume. Solid lines, electric field; broken lines, magnetic field.	67
33	Measured magnitude and phase of the transverse component of the magnetic field on the ground plane in the working volume; width $2a = 175$ cm, length $b = 114.8$ cm, height $h = 75$ cm.	69
34	Measured magnitude of the transverse magnetic field at a fixed position in the working volume as a function of frequency; $2a = 175$ cm, $b = 114.8$ cm, $h = 75$ cm, $P_f = 40$ W.	70
35	Measured surface density of charge on tubular cylinder in simulator.	72
36	Measured magnitude of surface density of outside charge on tubular cylinder; E-polarization, normal incidence.	73
37	Theoretical magnitude of surface density of outside charge on tubular cylinder; E-polarization, normal incidence.	74

TABLES

<u>Table</u>		<u>Page</u>
1	Coefficients referred to $y = 0, z = 0$, obtained from measured data.	47
2	Relative maxima of charge density on cylinder with $ka = 1, kh = 3.5\pi$. Theory for plane wave; measured in simulator; measured with spherical wave.	76

SECTION I

INTRODUCTION

The purpose of an EMP simulator is to provide an electromagnetic environment that approximates a traveling electromagnetic pulse composed of a spectrum of frequencies extending from very low to moderately high. For each component frequency, the electromagnetic field is a plane wave with mutually perpendicular electric and magnetic vectors that satisfy the relation $\vec{E} = \vec{c} \times \vec{B}$, where $\vec{c}$ is in the direction of propagation. It has the magnitude $c = 3 \times 10^8$ m/sec. One type of structure that is designed to generate an approximation of such a field is the guided-wave simulator which ideally has the properties of a uniform transmission line for the TEM mode at sufficiently low frequencies. That is, it has a characteristic impedance that is independent of the frequency and position along the direction of propagation and it can be terminated to provide a pure traveling wave at every cross section. Unfortunately, it is not obvious nor easily proved that the electromagnetic field in an actual simulator adequately approximates the desired properties at any or all frequencies in the pulse. The geometries of the different structures in actual use are such that a rigorous, quantitatively accurate analysis is very difficult. It follows that recourse must be had in numerical investigations or in direct measurements. Actually, an accurate and complete experimental study of the electromagnetic field in the working volume of a guided-wave simulator is faced with many difficulties. It is the purpose of this final report to summarize the results of such a study performed on the model simulator at Harvard University and, in order to make them meaningful, to interpret the measurements with the help of approximate, but instructive, theoretical results.

SECTION II

THE HARVARD EMP SIMULATOR

A detailed experimental study has been made of the electric field in the guided-wave simulator shown schematically in Figures 1 and 2. It consists of a rectangular metal plate between sloping triangular plates supported over a large aluminum ground plane (7.93×3.35 m) by dielectric cables and styrofoam blocks. It is driven at one end by the vertical extension of the inner conductor of a coaxial line connected to a CW power oscillator. It is terminated at the other end in standard two-watt resistors in parallel. The three-dimensional region under the rectangular plate is called the working volume. Its length b is 115 cm, its width $2a$ is 175 cm. Its height h above the ground plane is adjustable with the help of hinged joints between it and the sloping triangular plates combined with movable feed and load points. Two heights and frequencies have been used. They are $h = 108$ cm with $f = 625$ MHz or $\lambda = 48$ cm so that $h/\lambda = 2.25$, and $h = 75$ cm with $f = 264$ MHz or $\lambda = 113.6$ cm so that $h/\lambda = 0.66$. The altitude of each of the identical triangular plates is 331 cm and their projections on the ground plane when $h = 108$ cm are 311.5 cm, when $h = 75$ cm the projections are 322 cm. These dimensions provide a characteristic impedance of 100Ω when $h = 108$ cm, of 80Ω when $h = 75$ cm. A small corner reflector is placed behind the driven end; absorbing material completely surrounds the edges of the ground plane.

Cartesian coordinates are used to describe the location of a point in and near the working volume of the simulator. The origin is on the ground plane directly below the center of the parallel plate. The unit vectors $\hat{x}, \hat{y}, \hat{z}$ define, respectively, the transverse, longitudinal, and vertical directions, as indicated in Figure 2. Note that $\hat{y}$ points in the direction of propagation. For preliminary measurements the spherical coordinates (r, ϕ, θ) are also used with the origin ($r = 0$) on the ground plane at the driving point (see Figure 9). When $h = 108$ cm, the load is at $(r, \phi, \theta) = (738, 90^\circ, 0^\circ)$, where r is in centimeters.

In order to determine the electric field in the working volume and in the adjacent sections of the pyramidal regions as well as along the surfaces of the ground plane and the upper parallel plate, a system of movable probes

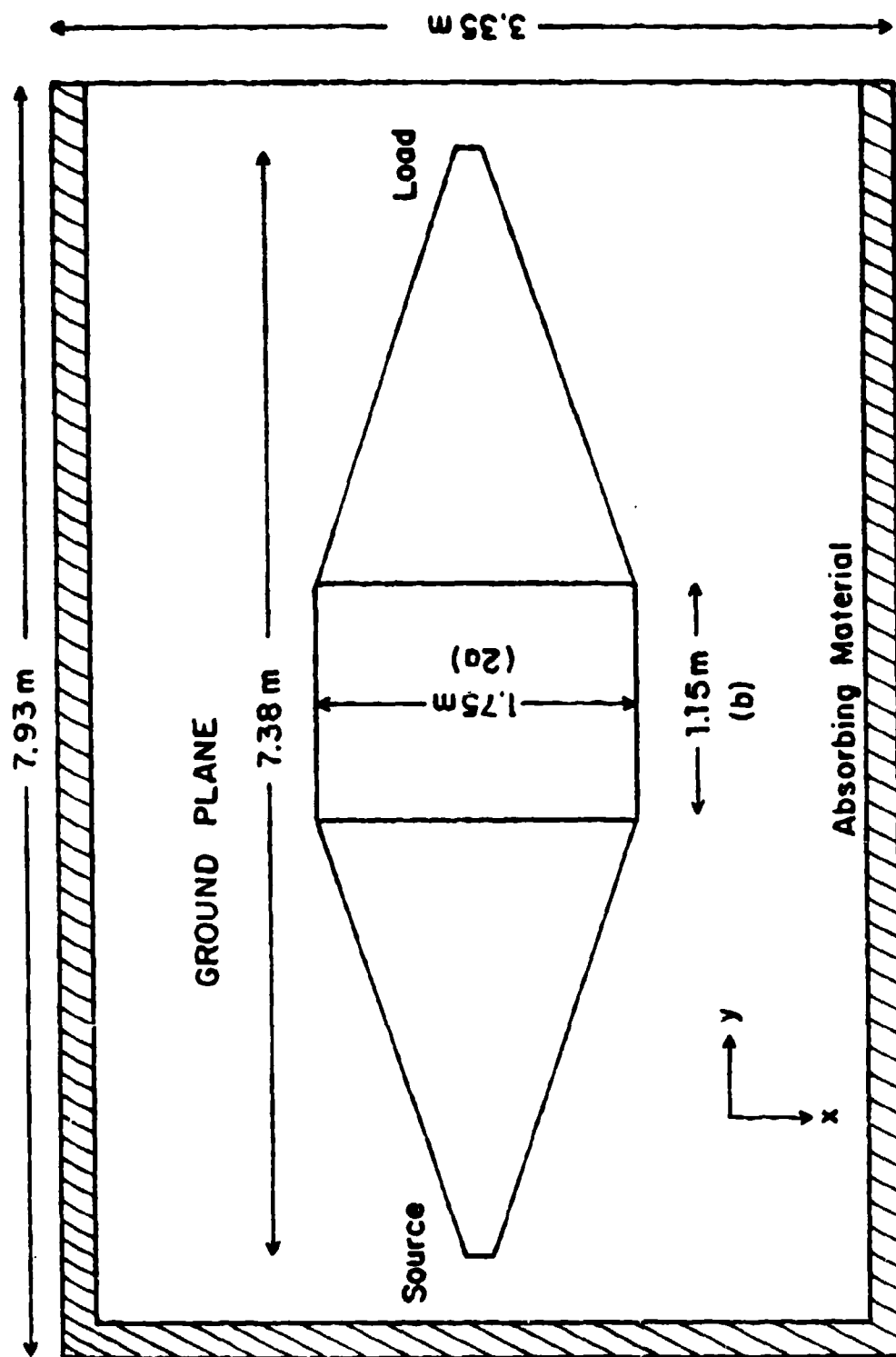
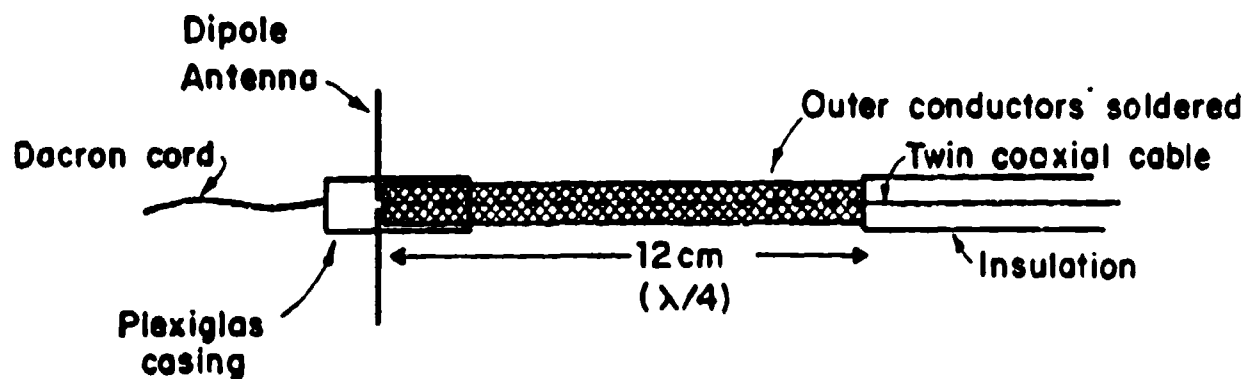


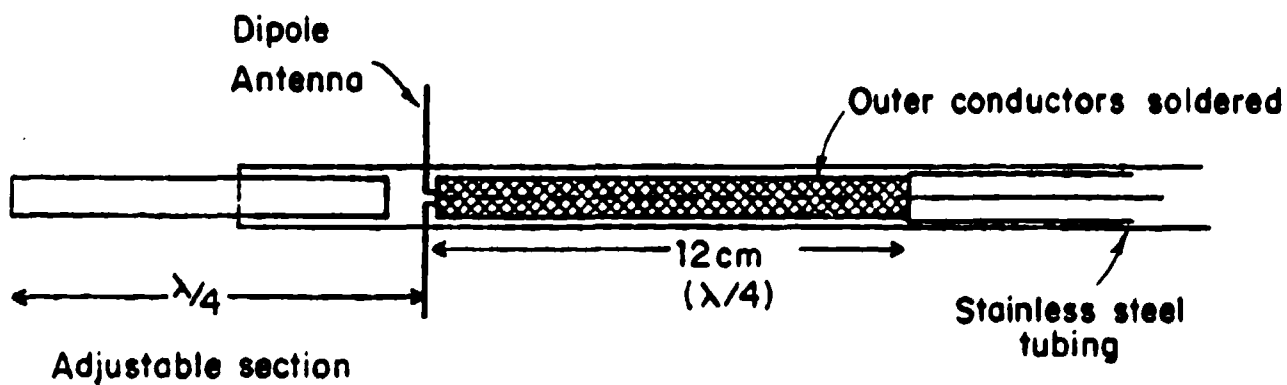
FIG. 1 TOP VIEW OF SIMULATOR SETUP

was designed and constructed for the direct measurement of both the amplitude and phase of E_y and E_z . As explained later, a small component E_x exists primarily near the open sides where fringing occurs, but this could not be measured. The component E_z on the ground plane was measured with a monopole probe 4 cm long, mounted on a brass disk 10 cm in diameter, and designed to slide along the ground plane when moved by means of a pulley system. The probe cable was constrained to lie flat on the ground plane and was, therefore, always perpendicular to the electric field. The measurement of E_z on the underside of the upper parallel plate was accomplished with a monopole probe that projects down into the working volume through longitudinal slots cut into the parallel plate. The probe was mounted on a brass block which was machined to slide in the slots. The output cable from the base of the probe was placed in a shielding tube constructed to lie along the upper surface of the sloping triangular plate leading to the load. The cable in its shielding tube extended beyond the load parallel to the ground plane and over its edge to the instrumentation below, as shown in Figure 2. The section over the ground plane constituted a transmission line with a characteristic impedance of 100 Ω . It was short-circuited at a distance of $\lambda/4$ from the load by a metal plate and so acted like an open circuit at the load.

The electric field throughout the working volume was measured with a dipole antenna that could be oriented vertically to measure E_z and horizontally to measure E_y . It was continuously movable in the working volume and adjacent sections below the triangular plates. The probe cable consisted of twin coaxial lines that were held parallel to the transverse x-axis as the probe was moved. This assured that they were perpendicular to both E_z and E_y , but necessarily parallel to E_x - which could excite axial standing-wave distributions of current and charge on their surfaces. Since these would have a charge maximum at the end adjacent to the terminals of the dipole, they could induce an undesired voltage across them if complete geometrical symmetry did not obtain. No such difficulty was encountered with $f = 626.5$ MHz, and the simple space probe (a) shown in Figure 3 was used to measure E_z and E_y throughout the working volume. At $f = 264$ MHz, an undesired voltage due to E_x was observed - presumably because the long twin cables from the probe in the working volume to the vector voltmeter under the ground plane happened to be near a resonant length. This difficulty was avoided by enclosing the twin cables in a metal tube provided



SPACE PROBE (a)



SPACE PROBE (b)

FIG. 3 DIAGRAMS OF SPACE PROBES

with an adjustable extension beyond the dipole, as shown in the diagram for space probe (b) in Figure 3. When the extension was adjusted to a quarter wavelength, the dipole was located at a charge minimum, instead of a charge maximum, in any standing wave induced on the tube by E_x . The undesired voltage across the terminals of the evidently not perfectly symmetrical dipole was thus reduced to an unobservable value.

SECTION III

PRELIMINARY MEASUREMENTS

Before measurements were made in the model simulator, the standing-wave pattern on the ground plane with its surrounding absorbing walls was investigated. The source was a short monopole at the location of the driving-point of the simulator ($r = 0$), backed by a small corner reflector. The frequency was $f = 626.5$ MHz or $\lambda = 48$ cm. By means of the movable monopole probe, the electric field E_z along the radial line $\theta = 0^\circ$ was measured in both amplitude and phase, as shown in Figure 4 in solid lines. It corresponds to the spherical traveling wave $E_z = Ae^{ikr}/r$ with a superimposed standing-wave ripple. In order to determine the predominant cause of the reflections that generate the standing wave, a reflecting plane was placed successively in three positions. For the first location normal to the direction of propagation at $r = s = 606$ cm, the field distribution shown in Figure 4 in dotted lines was obtained. This resembles the graphs in solid line, but with a substantially higher standing-wave ratio. For the second location, the reflecting plate was moved away from the source a distance of one quarter wavelength to $s = 618$ cm. The new field distribution was like the dotted one in Figure 4, but with the entire standing-wave pattern moved away from the source a distance of a quarter wavelength. A theoretical curve for the field when the reflecting plane at $s = 606$ cm is infinite in extent is shown in Figure 5 for comparison with the measured dotted graphs in Figure 4. The third location of the reflecting plane was normal to the x-direction and flat against the absorbing material on one side at $x = -136$ cm. The field measured in this case differed negligibly from that in the absence of any reflecting plane, shown in solid lines in Figure 4. These tests indicate that the reflections that produce the small standing wave shown by the solid-line graphs in Figure 4 originate at the rear edge and wall of the absorbing material. Their small amplitude shows that while there is some reflection from the edge of the ground plane and the absorbing material, this latter is generally effective in providing a predominantly traveling wave that closely approximates that over a plane of infinite extent.

The next set of preliminary measurements was carried out with the parallel rectangular and sloping triangular plates of the simulator in place,

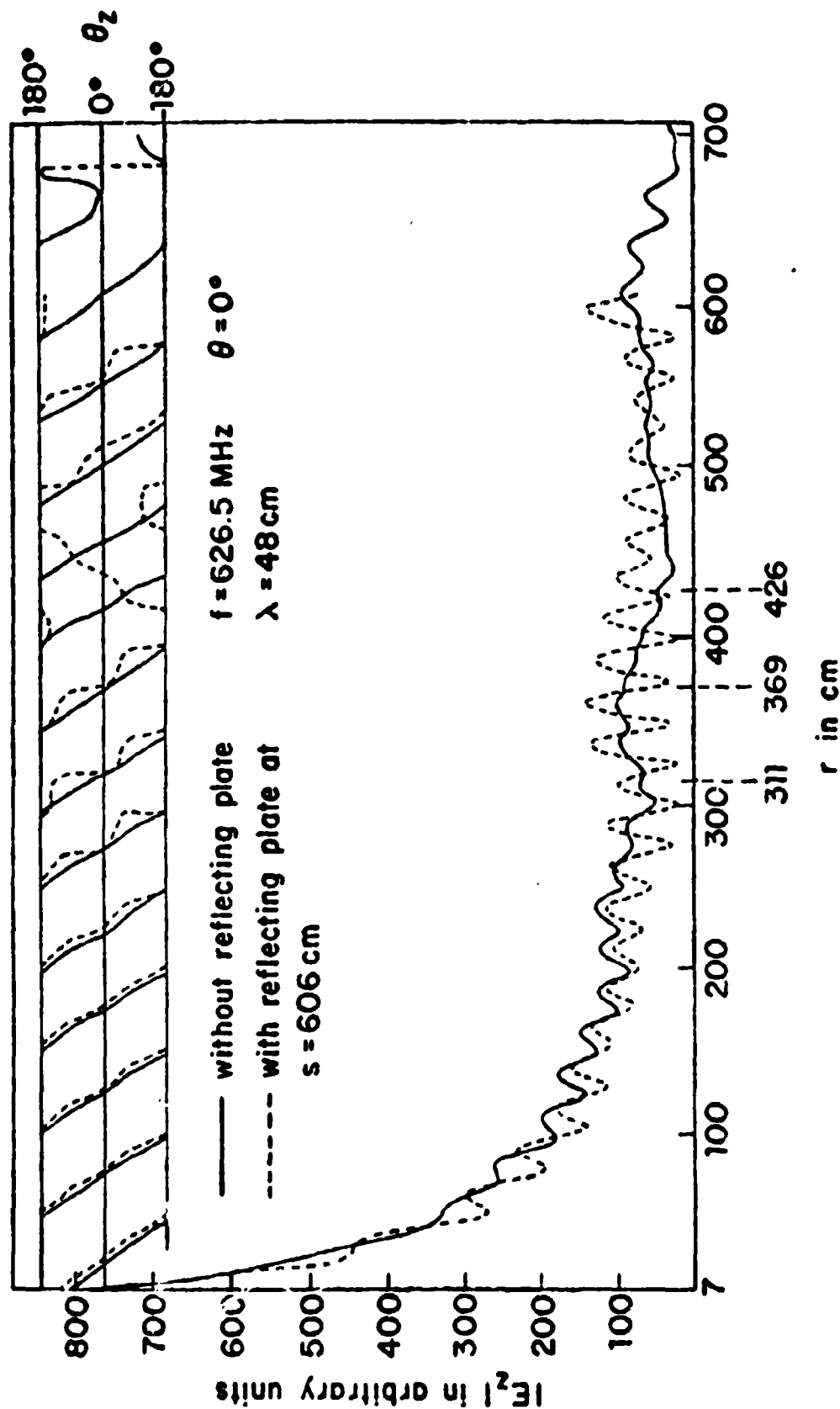


Fig. 4 Measured E_z along $\theta = 0^\circ$ on ground plane excited by monopole and corner reflector.

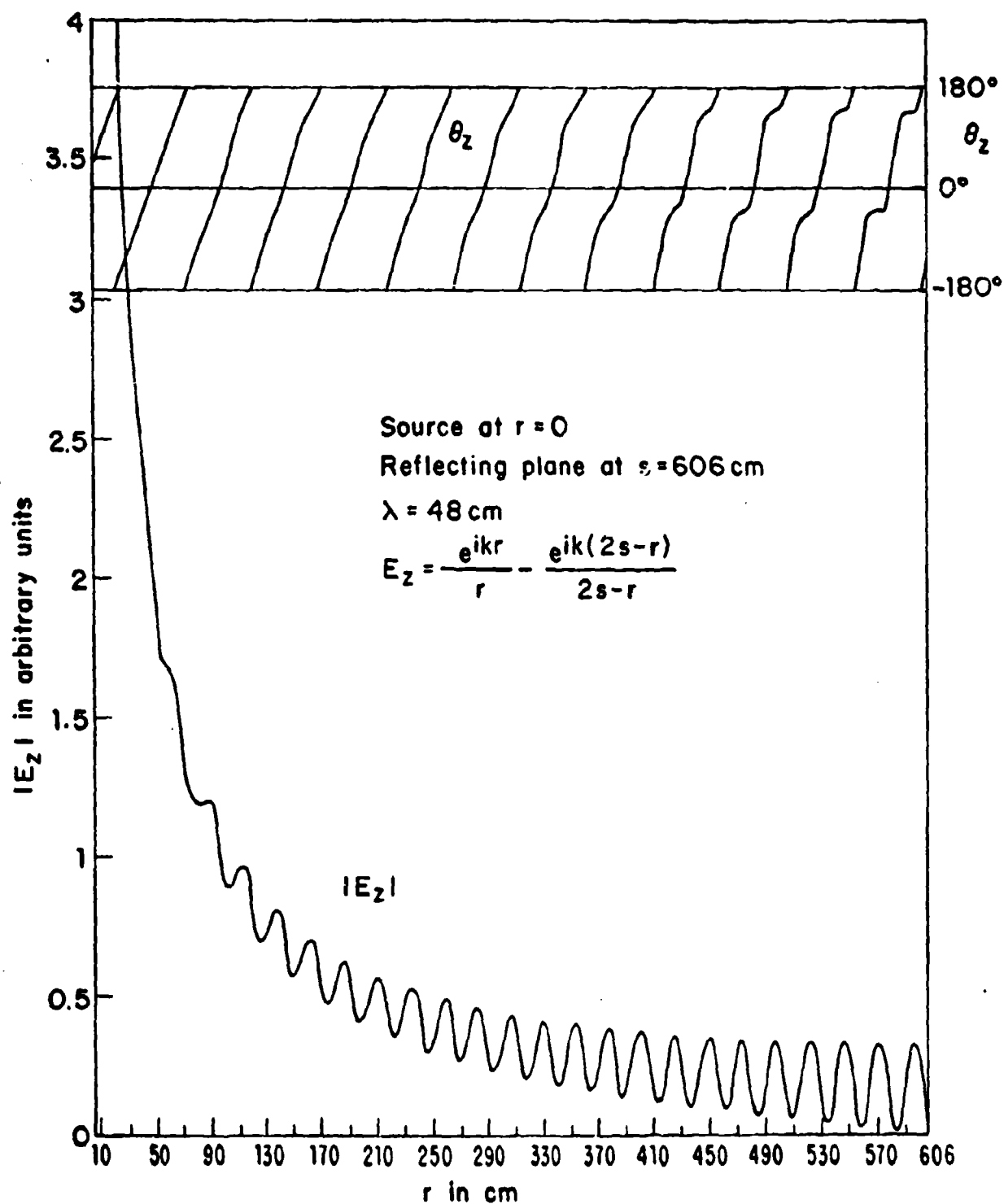


Fig. 5 Theoretical electric field along $\theta = 0^\circ$ on ground plane for comparison with measured graphs in Fig. 4.

and with a load of 105Ω as the termination. This value was chosen after measurements showed that it provided the lowest standing-wave ratio in the region near the load. Graphs of $|E_z|$ and θ_z are shown in Figure 6 for a distance of more than a wavelength adjacent to the 105Ω load. The standing-wave ratio of 3.7 shows that there is substantial reflection even with the best matched load. (It should be added that no really significant change in the standing-wave ratio was observed when the load was varied widely above and below 105Ω .) In Figure 7 are shown the graphs of $|E_z|$ and θ_z along the ground plane corresponding to those in solid lines in Figure 4, but now with the simulator plates in place. There is no dramatic difference. The main outline is still that of a traveling spherical wave with a superimposed standing wave. The latter is somewhat reduced near the source, somewhat enhanced near the load.

In Figure 8 are graphs in (a) of the measured phase fronts of E_z on the ground plane at four different radial distances between the source and the beginning of the working volume at $y = -57.5$ cm ($r = 311.5$ cm, $\theta = 0^\circ$). They are seen to be essentially circular with small oscillations near $\theta = 15^\circ$ due to edge effects from the sloping triangular plate above. The same information is conveyed in a different manner in (b) of Figure 8 which shows the phase along the line $y = -265$ cm between $x = 0$ and $x = -114.5$ cm. The solid line shows the measured phase, the broken line the theoretical phase for an ideal spherical wave with the wavelength $\lambda = 47.88$ cm. A graph of $|E_z|$ along a circular arc $r = 55$ cm is shown in (c) of Figure 8. It is constant within 1 dB under the sloping triangular plate where $0 \leq \theta \leq 15^\circ$. In the region beyond the projection of the edge of the triangular plate, i.e., $15^\circ < \theta \leq 30^\circ$, $|E_z|$ varies within a 3 dB range. It follows from Figure 7 that in the region beyond five wavelengths from the source, but not as far as the rear triangular plate, i.e., $250 \leq r \leq 400$ cm, $|E_z|$ is fairly constant in magnitude but with a superimposed standing-wave ripple. In this range the standing-wave ratio is relatively small, and the phase reasonably linear. Beyond the parallel-plate region, $r > 426$ cm, the standing-wave ratio is much higher, and the phase departs substantially from the linear.

It may be concluded from these preliminary measurements of E_z along the ground plane, that the field incident on the parallel-plate region is essentially a traveling spherical wave with a superimposed standing wave of relatively small amplitude.

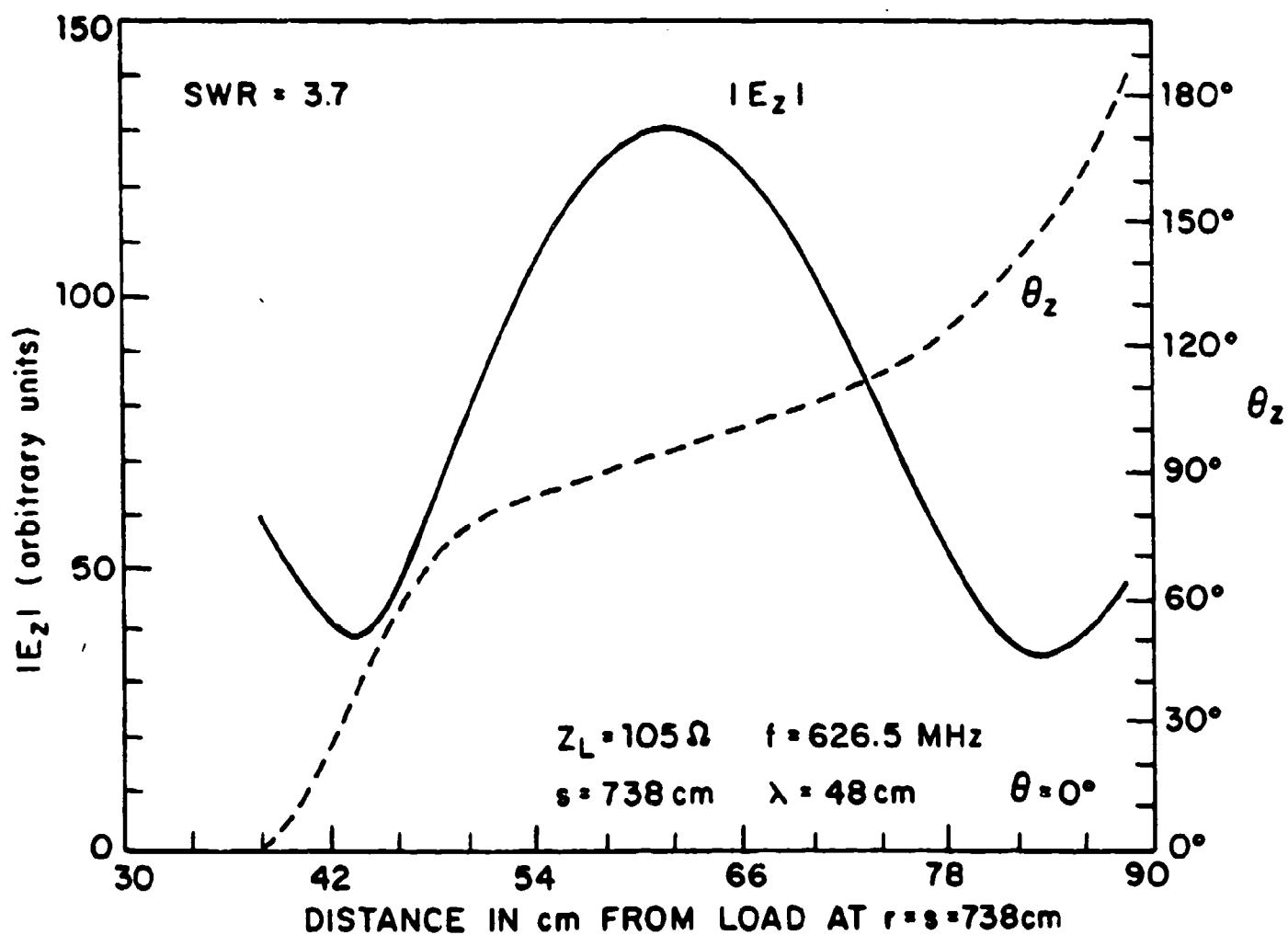


FIG. 6 STANDING WAVE OF $|E_z|$ NEAR LOAD

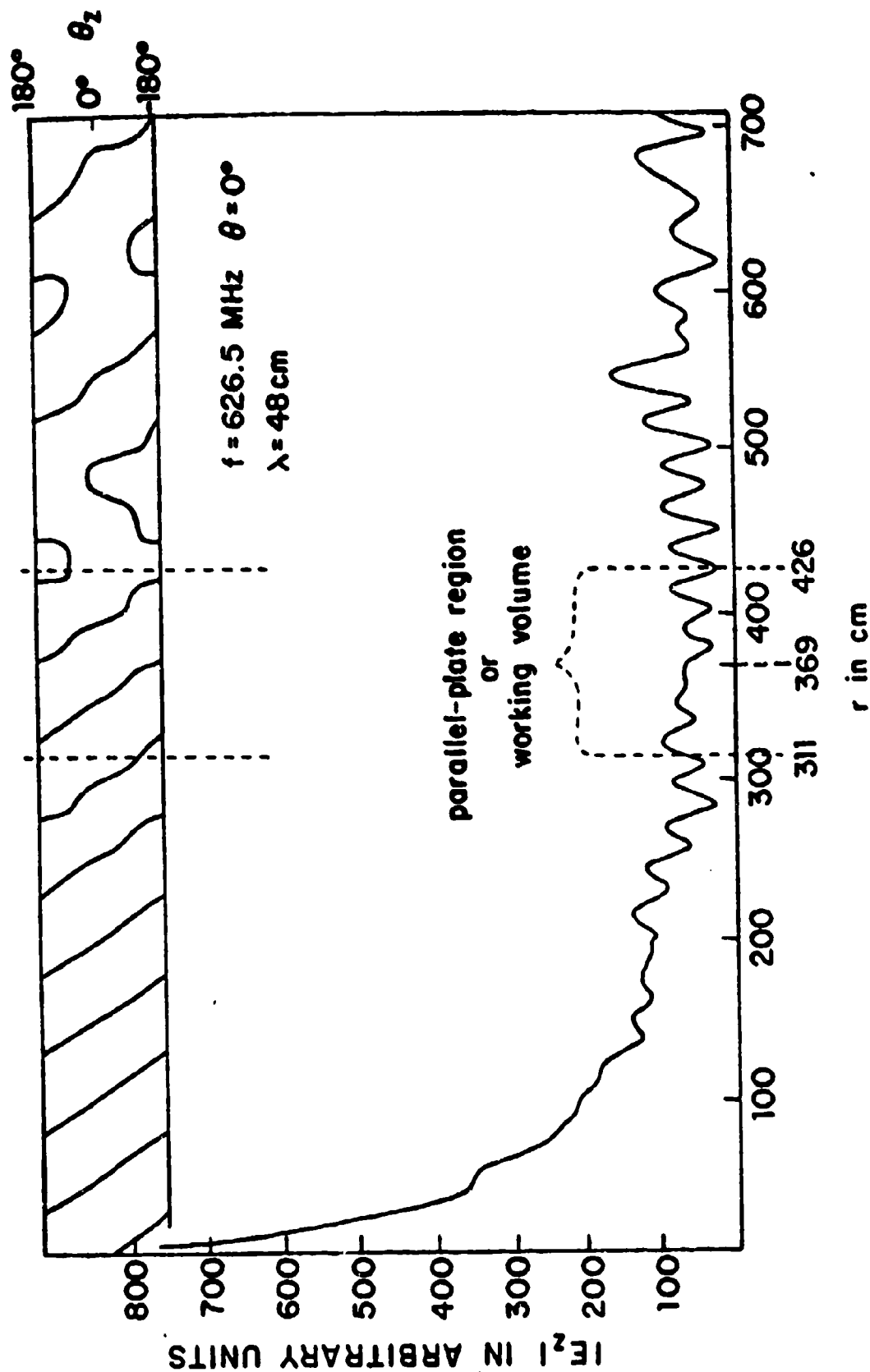


FIG. 7 MEASURED E_z ALONG $\theta = 0^\circ$ OF GROUND PLANE OF TERMINATED SIMULATOR

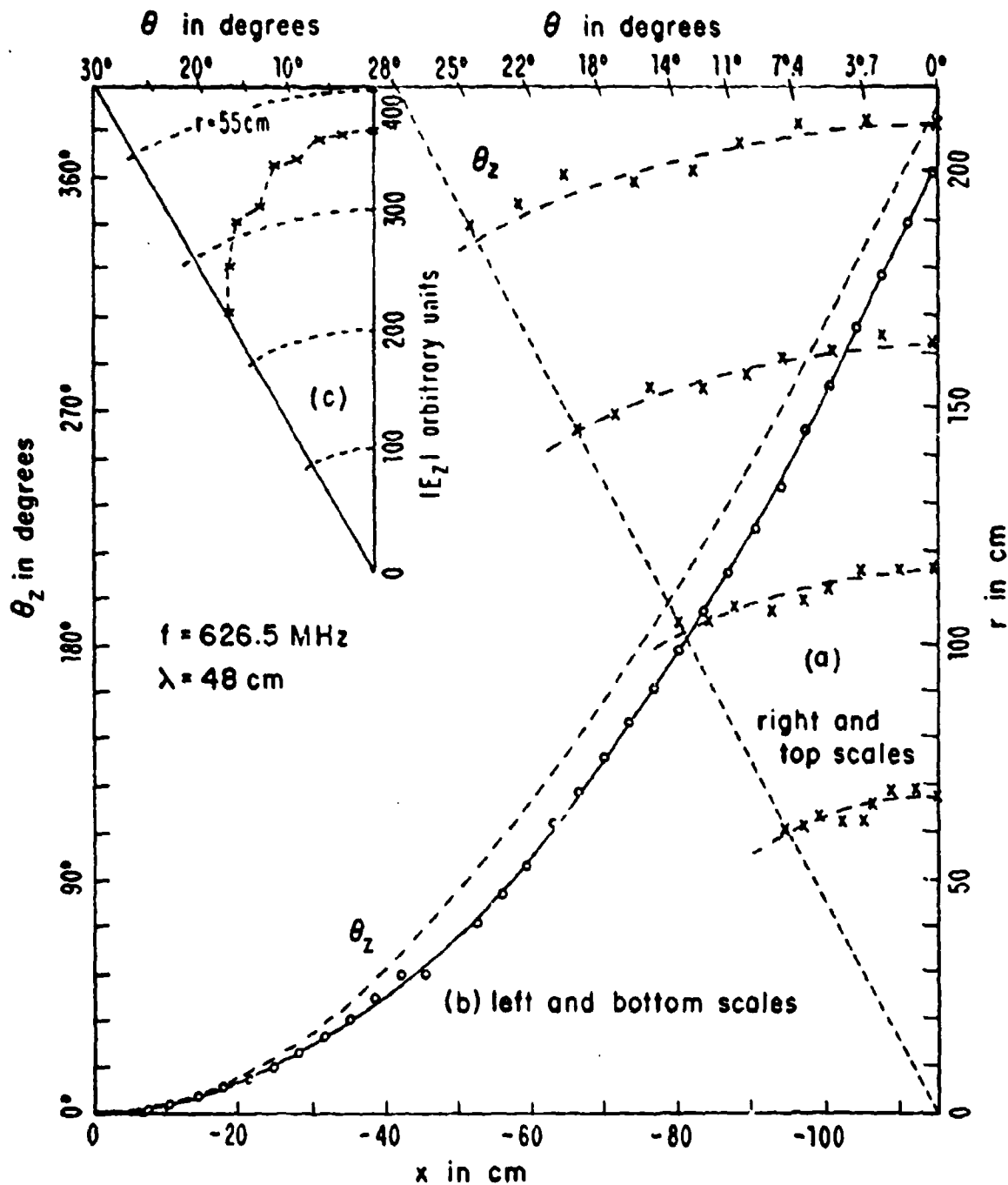


Fig. 8 (a) Measured phase fronts in the simulator; (b) Phase angle θ_z along the line $y = -265 \text{ cm}$; (c) $|E_z|$ at $r = 55 \text{ cm}$ from the source.

SECTION IV

INTRODUCTORY DESCRIPTION OF THE FIELD IN THE WORKING VOLUME

In order to provide a meaningful set of measurements of the electromagnetic field in the working volume of the simulator, that is, in the parallel-plate region and adjacent sections of the tapered ends, it is necessary to review briefly the elementary theoretical foundations. Consider first the field at frequencies that are sufficiently low to make the height h a negligible fraction of a wavelength, i.e., $kh = 2\pi h/\lambda \ll 1$. In this important range, the entire structure has the properties of an end-loaded transmission line operating in the TEM mode with negligible radiation, low line losses, a constant characteristic impedance, and a standing-wave ratio determined by the terminating load impedance. The TEM electric field in the working volume is vertically directed and approximately independent of the transverse coordinates x and z at points not too close to the side edges of the plates where fringing effects occur. That is, $\vec{E}(x,y,z) = \hat{z}E_z(y)$. $E_z(y)$ is proportional to $V(y)$, the transmission-line voltage across the conductors. The planes $y = \text{constant}$ are ideally surfaces of constant amplitude $|E_z|$ and phase θ_z . The incident wave travels in the positive y -direction, the reflected wave in the negative y -direction. With a proper termination $Z_L = Z_c$, the reflected wave from the load can be reduced to a negligible value. However, reflections do take place at the discontinuities at the junctions of the parallel plate and the sloping triangular end plates.

When the frequency is so high that kh is not small, in particular, when $kh = 2\pi h/\lambda = 4.5\pi$ or $h = 2.25\lambda$ as for the Harvard simulator at the operating wavelength $\lambda = 48$ cm and the height $h = 108$ cm, the electric field in the working volume is much more complicated. This is true to a lesser degree when $kh = 1.32\pi$ or $h = 0.66\lambda$ as for the Harvard simulator when $\lambda = 113.6$ cm and $h = 75$ cm. Owing to the wide spacing, most of the energy supplied by the generator is now radiated into the surrounding space, and only a small fraction is dissipated in the load. The structure is essentially an antenna and not a transmission line. This has been confirmed by K. M. SooHoo (ref. 1) in a numerical analysis of a comparable simulator. He concludes that in the high-frequency region, the radiated power approaches 80% of that supplied by the generator.

In order to understand the characteristics of the measured field and to relate them to the simple TEM field that dominates at low frequencies, it is advantageous to have an at least approximate theoretical representation of the field in the working volume. Owing to its finite size and connection to the sloping triangular driving and loading members, the working volume is not simply a section of an ideal parallel-plate waveguide of infinite length. No general analytical treatment of the complete simulator has been made. Analyses are available of infinitely long, parallel-plate waveguides with plates that have a finite width that is arbitrary (refs. 2 and 3), or that is very narrow (ref. 4), very wide (refs. 5 and 6), or infinitely wide (ref. 7). None of these provides any information on the fields in and the transmission-line properties of the long sloping triangular sections or of the junction region between them and the parallel-plate region. Unfortunately, they also provide primarily qualitative information about the fields in the parallel-plate section since this is only 115 cm long, but 175 cm wide and (with image) 216 cm (or 150 cm) high. Thus, the condition of infinite length (or at least great length compared with the transverse dimensions) implicit in all of the analyses of parallel-plate waveguides is not satisfied. Indeed, the parallel-plate section is relatively so short that end effects can be expected to be significant over much of its length. Even so, the theoretical representation of the field in an ideal parallel-plate waveguide in terms of propagating TEM, TM, and TE modes should provide the best available framework for interpreting the measured field in the working volume of the model simulator. Instead of reviewing these in general, it is expedient first to study the nature of the incident field in order to determine which of the many possible modes can actually be expected to be excited.

As has been demonstrated, the field incident on the parallel-plate region is essentially a spherical wave originating at the source with an electric field E_ϕ and magnetic field $H_\theta = B_\theta/\mu_0$ tangent to the surface of a sphere, as shown in Figure 9(a). The intersection of the spherical wave fronts with a vertical plane is shown in Figure 9(b). At points on the plane $y = \text{constant}$, $E_z = -E_\phi \sin \phi$, $E_y = E_\phi \cos \phi$. On the ground plane, $z = 0$ and $\phi = 90^\circ$ so that $E_z = -E_\phi$ and $E_y = 0$. Thus, along the plane corresponding to the input surface $y = -57.5$ cm of the working volume, there is a vertical component E_z of the electric field and also a longitudinal component E_y which increases from zero at the ground plane to a maximum at

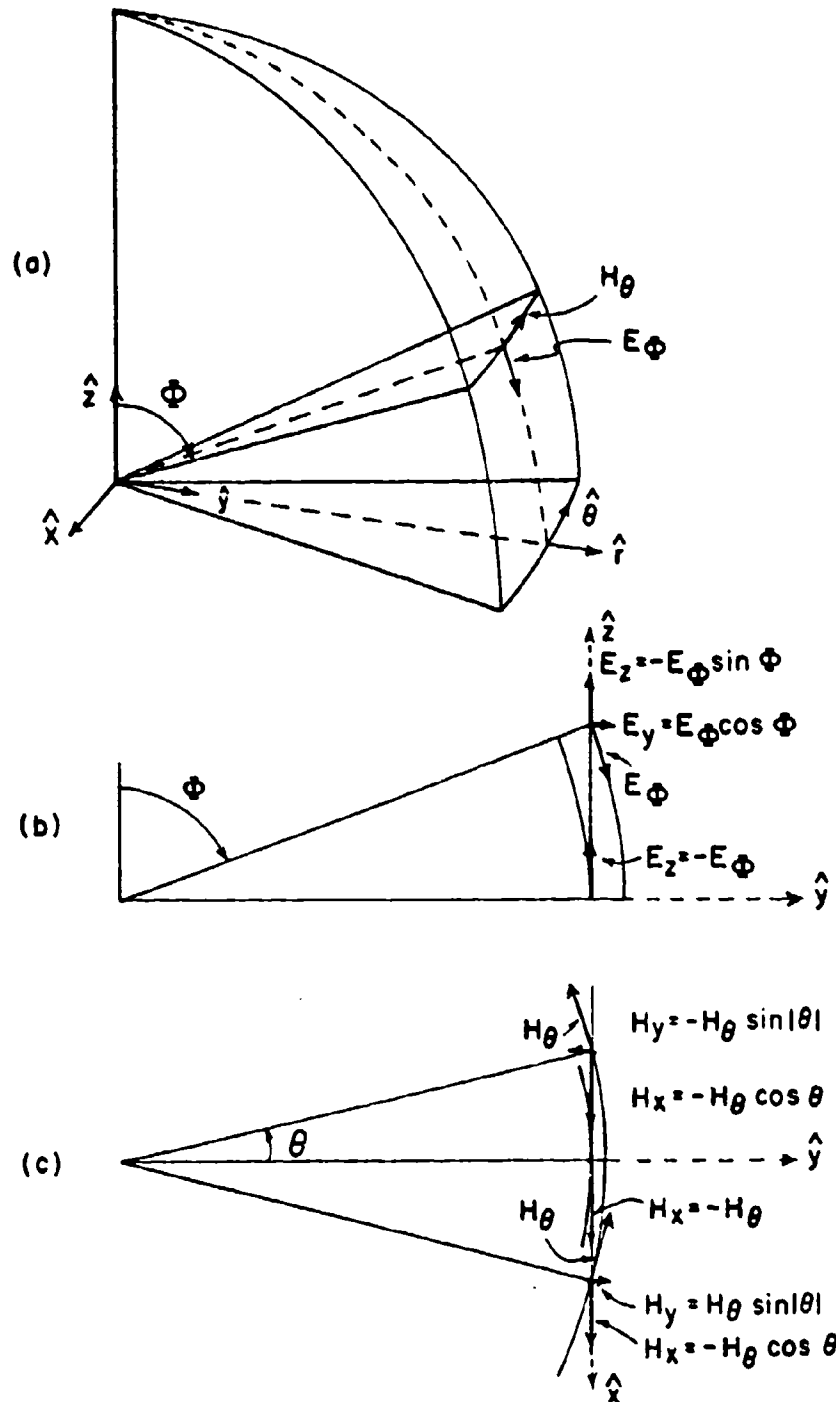


FIG. 9 SCHEMATIC DIAGRAMS OF SPHERICAL WAVE INCIDENT ON A PLANE. (a) THREE DIMENSIONAL VIEW (b) ELECTRIC FIELD IN VERTICAL PLANE (c) MAGNETIC FIELD IN HORIZONTAL PLANE.

the top plate. In the parallel-plate region these components can excite the TEM mode and those TM modes that are symmetric with respect to the transverse z coordinate.

The intersection of the spherical wave with a vertical plane in a horizontal section is shown in Figure 9(c). At points along the plane $y =$ constant, $H_x = -H_0 \cos \theta$, $H_y = -H_0 \sin \theta$; at $x = 0$ and $\theta = 0^\circ$, $H_x = -H_0$ and $H_y = 0$. Therefore, along the plane surface corresponding to the input surface $y = -57.5$ cm of the working volume, there is a transverse component H_x of the magnetic field and a longitudinal component H_y . The latter vanishes at $\theta = 0^\circ$, is positive for $\theta < 0^\circ$, negative for $\theta > 0^\circ$. In the parallel-plate region, these components are associated with the TEM mode and those TE modes that are antisymmetric with respect to the transverse x coordinate. Thus, E_z may include components in the TEM, TM, and TE modes, E_y consists exclusively of TM modes, and E_x may be composed of both TM and TE modes. Similarly, H_x may include components in the TEM, TM, and TE modes, H_y consists exclusively of TE modes, and H_z may be composed of both TE and TM modes.

SECTION V

THE FIELD IN THE PARALLEL-PLATE SECTION; TEM AND TM MODES

Since the field incident on the parallel-plate section of the simulator is a spherical wave, it is of interest to determine the nature of the phase fronts which characterize the electromagnetic field in that section. Measured graphs of the wave fronts or contours of constant phase, $\theta_z = \text{constant}$, of the vertical component E_z of the electric field in the parallel-plate region when $h = 108$ cm and $f = 626.5$ MHz are shown in Figures 10a and 10b in vertical yz planes at discrete values of x ranging from $x = 1.7$ cm near the center at $x = 0$ to $x = -70.3$ cm near the edge at $x = -87.5$ cm. Also shown are the wave fronts of a spherical wave originating at the driving point ($x = 0$, $y = -369$ cm, $z = 0$). Clearly the phase fronts throughout the parallel-plate region are essentially spherical with a superimposed oscillation due to reflections from the top plate.

It is not convenient to describe the field in a parallel-plate waveguide in terms of spherical wave fronts originating at an outside point. The natural representation is in terms of a superposition of plane waves known as parallel-plane modes. The simplest form is given by the mode theory of infinite parallel planes (ref. 7). Applicable to the parallel-plate section of the simulator are the TM modes symmetric in z supplemented, if desired, with the more complicated theory for plates of finite width (refs. 2 through 6). The significance of TE modes is considered in a later section. The relevant TM modes are given by: *

$$E_{yn} = -i\zeta I_n(y)(n\lambda/2h)(\epsilon_n/h)^{1/2} \sin(n\pi z/h) \quad (1)$$

$$E_{zn} = -V_n(y)(\epsilon_n/h)^{1/2} \cos(n\pi z/h) \quad (2)$$

$$H_{xn} = I_n(y)(\epsilon_n/h)^{1/2} \cos(n\pi z/h) \quad (3)$$

where $n = 0, 1, 2, \dots$; $\zeta = (\mu/\epsilon)^{1/2}$; $\epsilon_n = 1$ when $n = 0$, $\epsilon_n = 2$ when $n \neq 0$.

*When referred to the full height with image, h is replaced by $2h$, and $n = 0, 2, 4, 6, \dots$ instead of $0, 1, 2, 3, \dots$

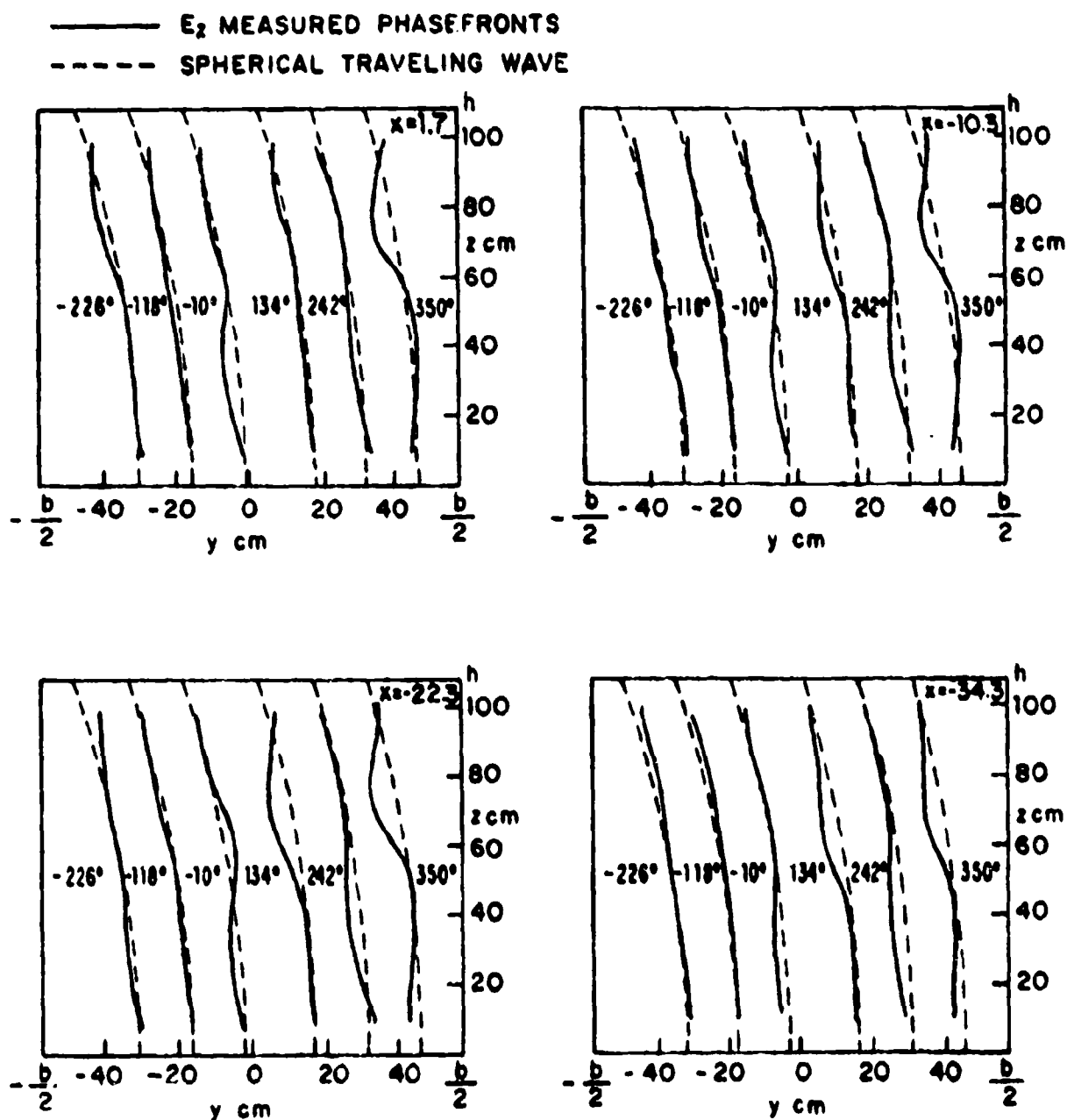


FIG. 100 MEASURED CONSTANT PHASE CURVES IN THE WORKING VOLUME;
 $h = 108$ cm, $b = 114.8$ cm, $f = 626.5$ MHz

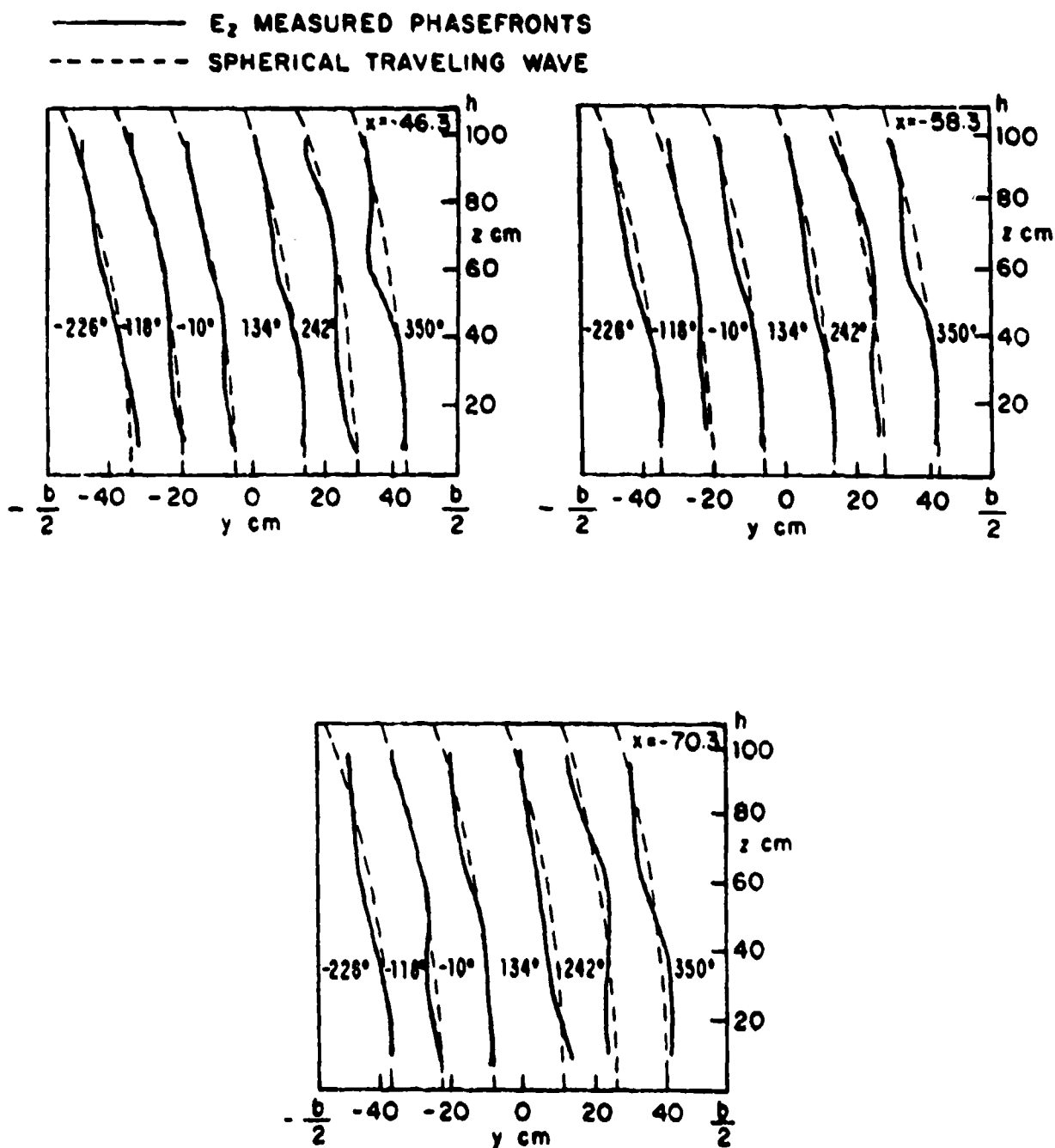


FIG. 10b MEASURED CONSTANT PHASE CURVES IN THE WORKING VOLUME;
 $h = 108$ cm, $b = 114.8$ cm, $f = 626.5$ MHz

The generalized voltage and current functions $V_n(y)$ and $I_n(y)$ satisfy the simple transmission-line equations:

$$\frac{dV_n(y)}{dy} = ik_{gn} Z_{cn} I_n(y) \quad (4)$$

$$\frac{dI_n(y)}{dy} = ik_{gn} Y_{cn} V_n(y) \quad (5)$$

where the guide wave number k_{gn} and characteristic impedance Z_{cn} are:

$$k_{gn} = (k^2 - k_{cn}^2)^{1/2}, \quad Z_{cn} = Y_{cn}^{-1} = \zeta k_{gn}/k \quad (6)$$

and the cut-off wave number k_{cn} is:

$$k_{cn} = 2\pi/\lambda_{cn}, \quad \lambda_{cn} = 2h/n \quad (7)$$

The guide wavelength is $\lambda_{gn} = 2\pi/k_{gn}$. The voltage and current functions for the TM_{0n} modes in the parallel-plane section, $-57.5 \text{ cm} \leq y \leq 57.5 \text{ cm}$, can be represented as the sums of incident and reflected waves, i.e.,

$$V_n(y) = V_n^{\text{inc}}(0)e^{ik_{gn}y} + V_n^{\text{ref}}(0)e^{-ik_{gn}y} \quad (8)$$

$$I_n(y)Z_{cn} = V_n^{\text{inc}}(0)e^{ik_{gn}y} - V_n^{\text{ref}}(0)e^{-ik_{gn}y} \quad (9)$$

where $V_n^{\text{inc}}(0)$ and $V_n^{\text{ref}}(0)$ are the complex amplitudes of the incident and reflected voltage waves in the transverse plane $y = 0$.

For the Harvard working volume and with the operating frequency at $f = 626.5 \text{ MHz}$, the TEM mode with $n = 0$ and three TM_{0n} modes with $n = 1, 2, 3$ can propagate. For the TEM mode, $k = k_{g0} = 0.1309 \text{ cm}^{-1}$, for the TM_{0n} modes, $k_{g1} = 0.977k = 0.128 \text{ cm}^{-1}$, $k_{g2} = 0.893k = 0.117 \text{ cm}^{-1}$, and $k_{g3} = 0.748k = 0.098 \text{ cm}^{-1}$. The corresponding guide wavelengths are $\lambda = \lambda_{g0} = 48 \text{ cm}$ for the TEM mode and $\lambda_{g1} = 49.1 \text{ cm}$, $\lambda_{g2} = 53.7 \text{ cm}$, and $\lambda_{g3} = 64.2 \text{ cm}$ for the TM_{0n} modes. The fields for the four modes are:

$$\text{TEM: } E_y = 0, \quad E_z = 0.096V_0(y), \quad H_x = 0.096I_0(y) \quad (10)$$

$$\begin{aligned} \text{TM}_{01}: \quad E_y &= -111.4I_1(y)\sin(.029z), \quad E_z = -0.136V_1(y)\cos(.029z) \\ H_x &= 0.136I_1(y)\cos(.029z) \end{aligned} \quad (11)$$

$$\begin{aligned} \text{TM}_{02}: \quad E_y &= -122.8I_2(y)\sin(.058z), \quad E_z = -0.136V_2(y)\cos(.058z) \\ H_x &= 0.136I_2(y)\cos(.058z) \end{aligned} \quad (12)$$

$$\begin{aligned} \text{TM}_{03}: \quad E_y &= -134.2I_3(y)\sin(.087z), \quad E_z = -0.136V_3(y)\cos(.087z) \\ H_x &= 0.136I_3(y)\cos(.087z) \end{aligned} \quad (13)$$

The relative amplitudes of the incident and reflected waves for each of these modes are not readily determined analytically. However, they can be estimated at any cross section of the working volume by comparison with the measured field.

The electric field lines characteristic of the TEM and first three TM_{0n} modes are shown in the yz-plane in Figure 11. At the upper left are the exclusively vertical field lines of the TEM mode. They have alternate upward and downward maxima at intervals of $\lambda/2 = 24$ cm. Note that there is no associated component E_y . At the upper right are the electric field lines for the TM_{01} mode. These resemble the TEM mode near the top conductor, but are oppositely directed near the ground plane since they are parts of closed loops with an E_y component in the region halfway between the conducting surfaces. The alternating upward and downward maxima now occur at intervals of $\lambda_{g1}/2 = 24.6$ cm. On the lower left are the E-lines for the TM_{02} mode, on the lower right those of the TM_{03} mode. These have additional closed loops in the vertical direction with associated E_y -components and a wider spacing between successive maxima in the horizontal direction. Thus, for the TM_{02} mode, the maxima occur at intervals of $\lambda_{g2}/2 = 26.8$ cm, for the TM_{03} mode at intervals of $\lambda_{g3}/2 = 32.1$ cm. Axial distributions of the four modes are shown in Figure 12 with an assumed standing-wave ratio of 1.36 for each. Note that for the TEM mode at the bottom, there are four half-wavelengths in

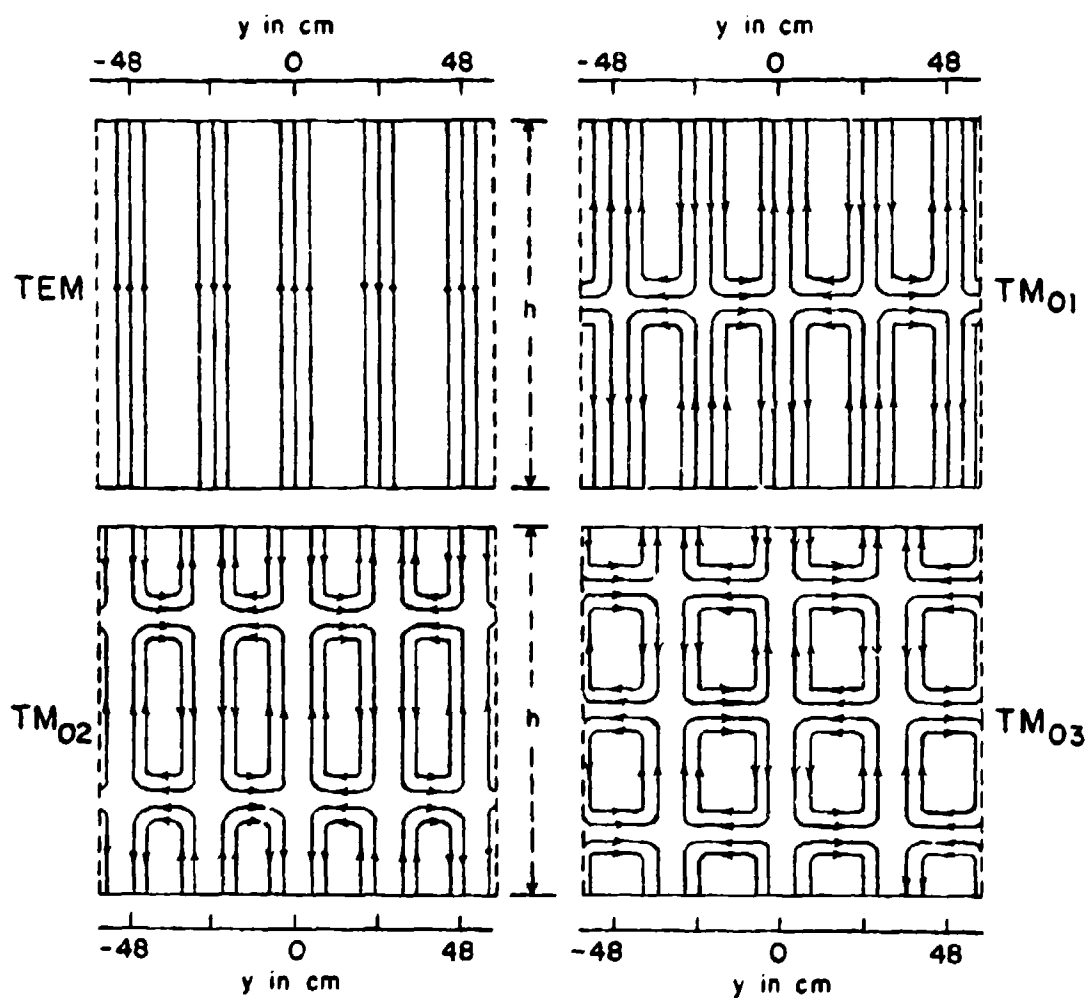


Fig. 11 Electric field lines for four parallel-plate modes in working volume $\lambda = 48$ cm.

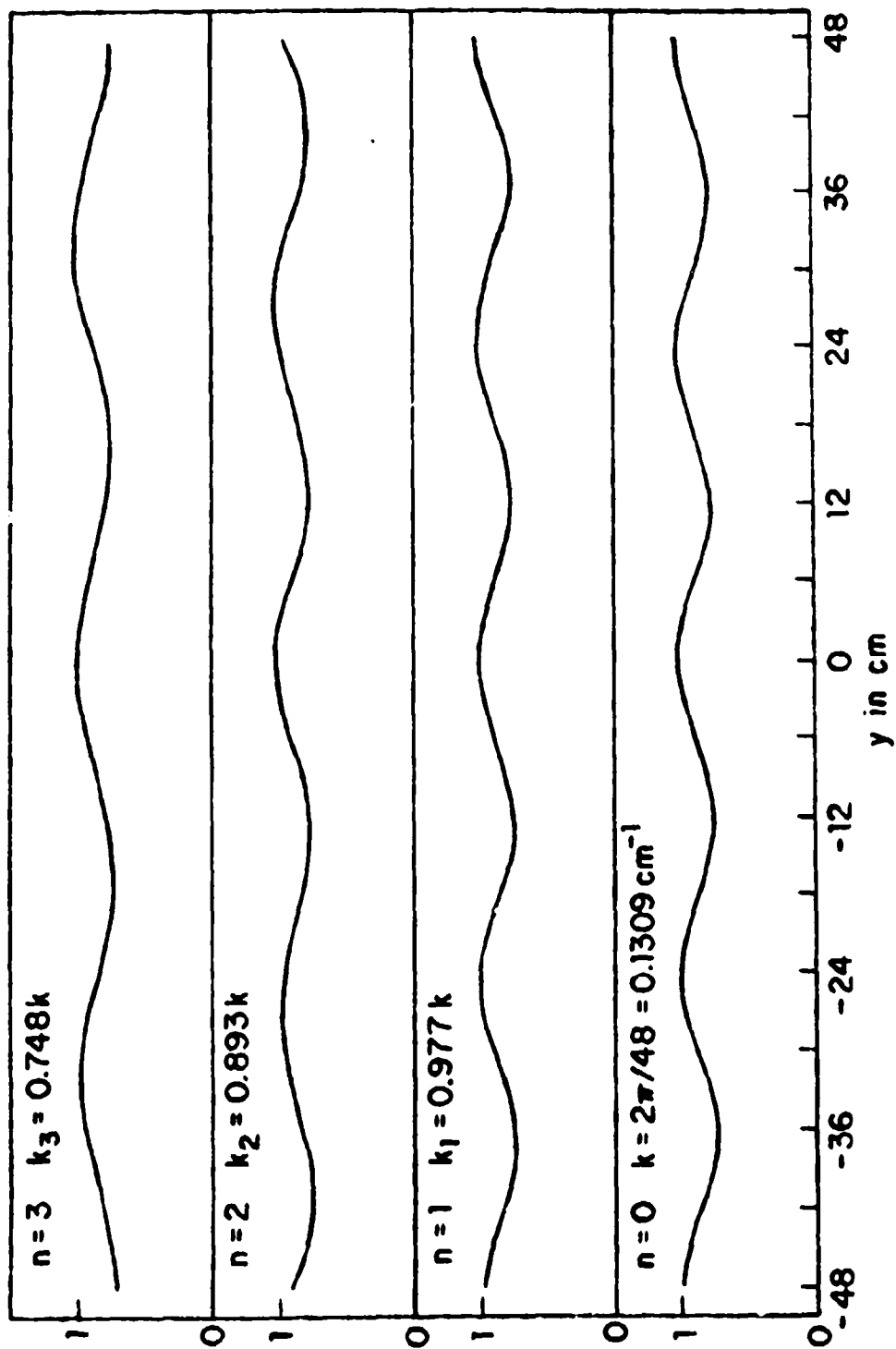


Fig. 12 Distribution of standing waves in working volume for each mode; SWR = 1.36
 $\lambda = 48 \text{ cm}$

the range $-48 \text{ cm} \leq y \leq 48 \text{ cm}$, whereas for the TM_{03} mode at the top, there are only three half-wavelengths in the same range.

When $h = 75 \text{ cm}$ and $f = 264 \text{ MHz}$ or $\lambda = 113.6 \text{ cm}$, the only propagating TM modes are the TEM mode and the TM_{01} mode. For the latter, the cut-off wavelength is $\lambda_{c1} = 2h = 150 \text{ cm}$, and the guide wavelength is $\lambda_{g1} = 174 \text{ cm}$. The formulas (1) - (3) apply with $n = 0$ for the TEM mode and $n = 1$ for the TM_{01} mode.

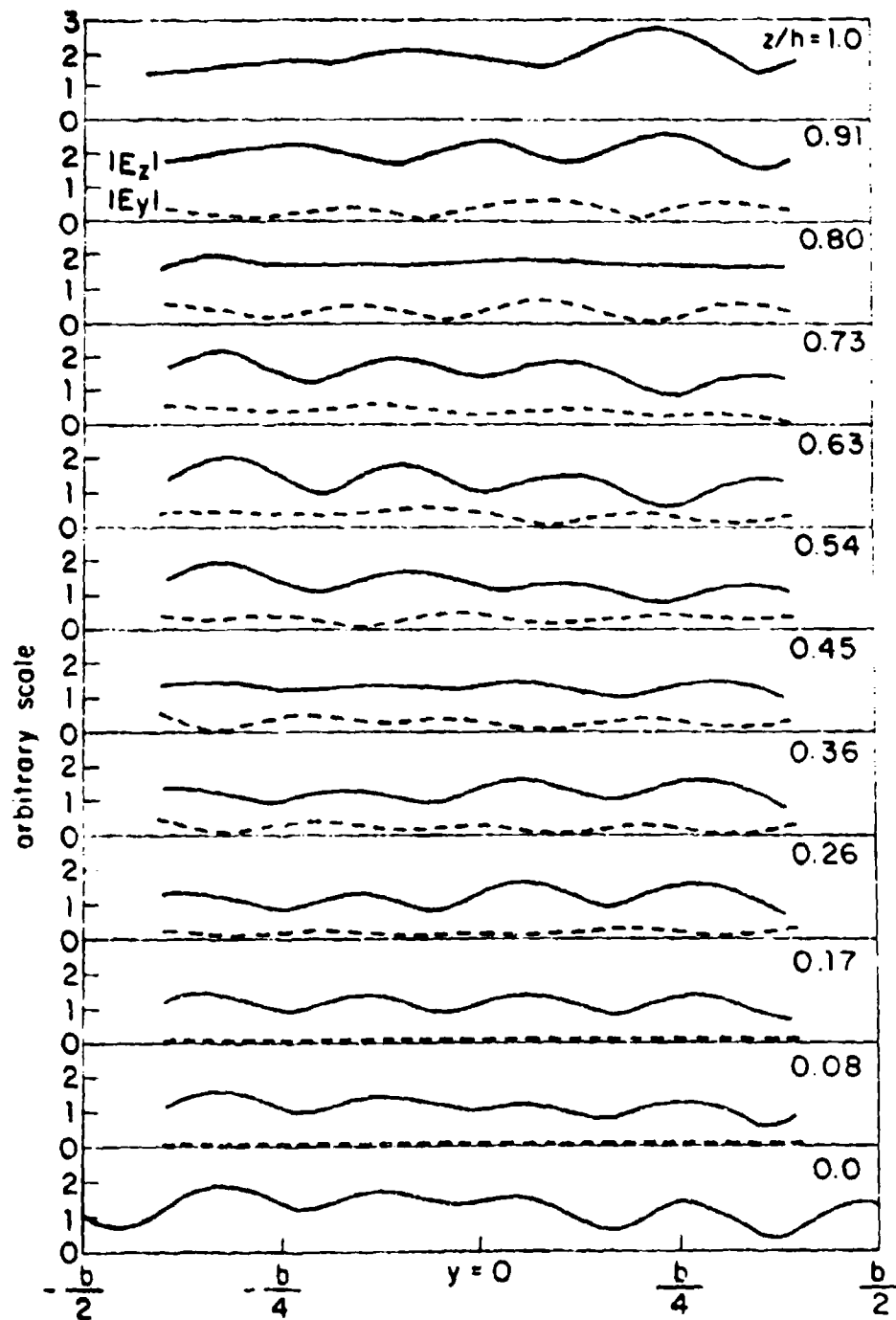
SECTION VI

THE MEASURED FIELD IN THE WORKING VOLUME: $h = 2.25\lambda = 108$ cm, $f = 626.5$ MHz

The principal components, E_z and E_y , of the electric field in the working volume were measured as functions of the longitudinal variable y with the transverse variables x and z as the parameters. Consider first the field with $f = 626.5$ MHz when $h = 108$ cm $= 2.25\lambda$ and $\lambda = 48$ cm. (The field with $h = 75$ cm $= 0.66\lambda$ with $\lambda = 113.6$ cm is studied in the next section.)

In Figure 13 are shown measured distributions of $|E_z|$ and $|E_y|$ in the yz -plane at $x = 1.7$ cm, i.e., very near the central plane $x = 0$ of the parallel-plate region. The parameter z/h ranges from 0 at the bottom to $z/h = 1$ at the top. The field along the ground plane $z/h = 0$ was measured with the monopole probe mounted on the movable metal disk; the field along the underside of the top plate was measured with the monopole probe that moves in longitudinal slots. The field at all other values of z/h was measured with the movable dipole space probe that is supported by a long tube parallel to the x -axis that moves laterally and vertically. The component E_z was measured with the dipole in the vertical position, the component E_y with the dipole in the horizontal position. Only the magnitudes $|E_z|$ and $|E_y|$ are shown in Figure 13. Actually, both magnitude and phase were measured. Furthermore, for each height z/h shown in Figure 13 except $z/h = 0$, the fields were measured at seven values of x covering one-half of the working volume.

Selected graphs at $z/h = 0.08$, 0.45 , and 0.91 as measured with the space probe and at $z/h = 1$ as measured by the monopole probe protruding from the top plate are shown in Figures 14 through 17 for E_z and in Figures 18 through 20 for E_y . Of particular interest are the four graphs of $|E_z|$ shown in Figure 21. They reveal the striking change in the standing-wave pattern in the plane $x = 1.7$ cm from near the top ($z/h = 0.91$) to near the bottom ($z/h = 0.079$). Clearly there are three standing-wave maxima at the top, four at the bottom. Actually, the standing-wave pattern for $|E_z|$ at $z/h = 0.08$ near the ground plane and shown at the bottom in Figure 21 is a good approximation of the TEM field shown at the bottom in Figure 12. The successive maxima are quite uniformly spaced at $\lambda/2 = 24$ cm and $|E_y| \neq 0$. On the other hand, the standing-wave pattern of $|E_z|$ at $z/h = 0.91$ near the



Longitudinal cross section of working volume y - z plane $x = 1.7 \text{ cm}$
 $b = 115 \text{ cm} = 2.4 \lambda$; $h = 108 \text{ cm} = 2.25 \lambda$

Fig. 13 Measured magnitude of the vertical and longitudinal components of the electric field in the working volume

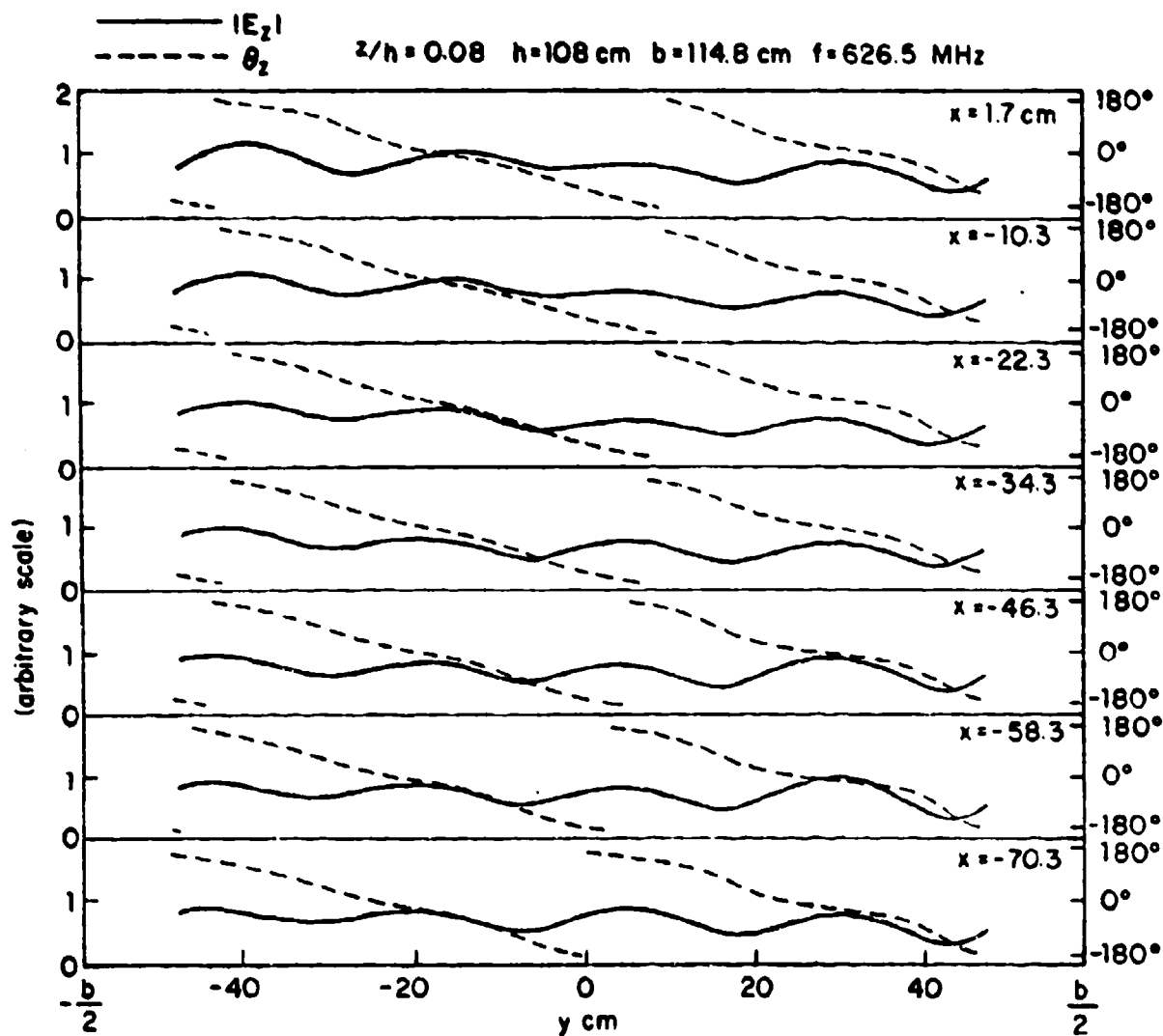


Fig. 14 Measured magnitude and phase of E_z in working volume of model simulator.

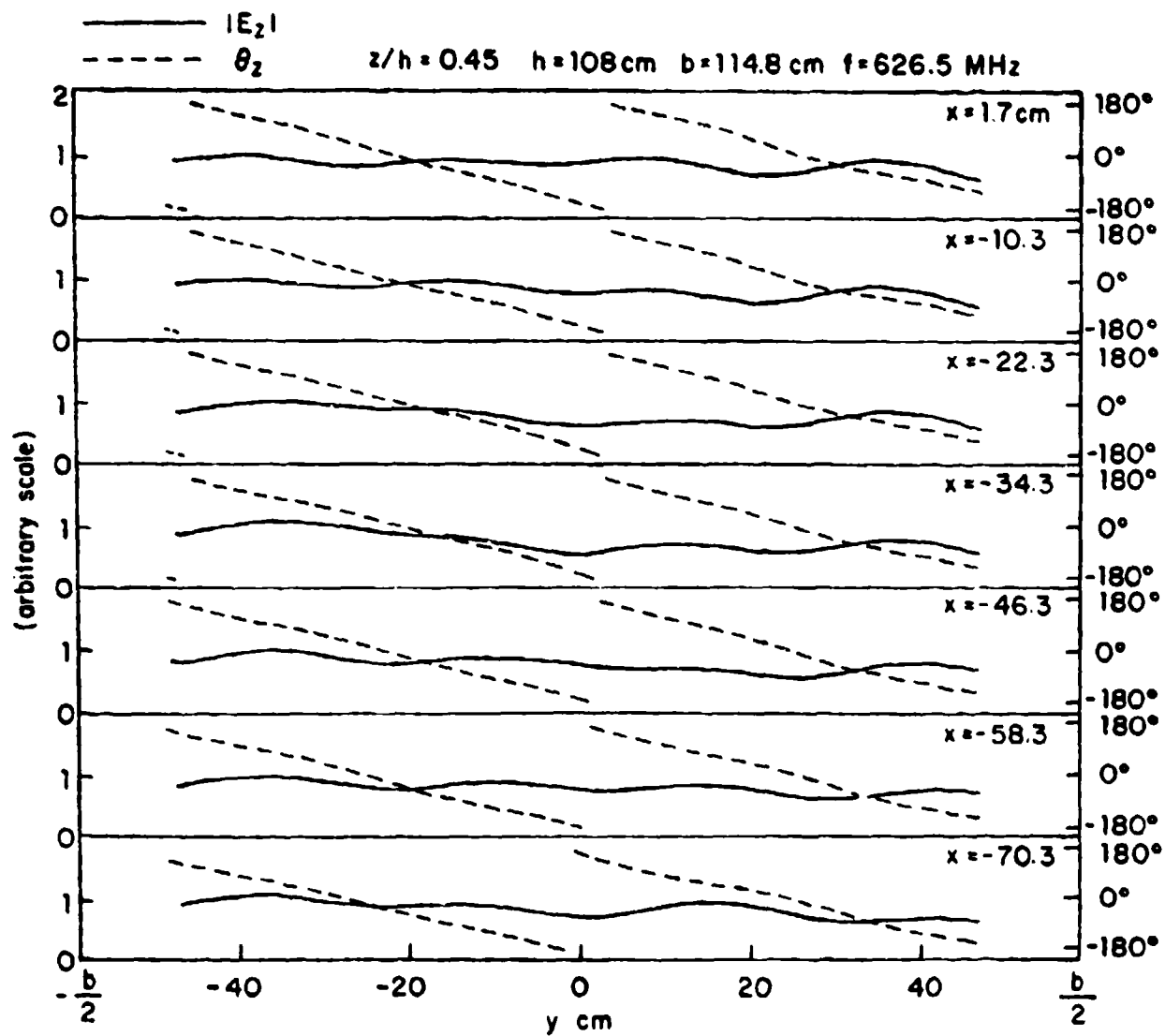


Fig. 15 Measured magnitude and phase of E_z in working volume of model simulator

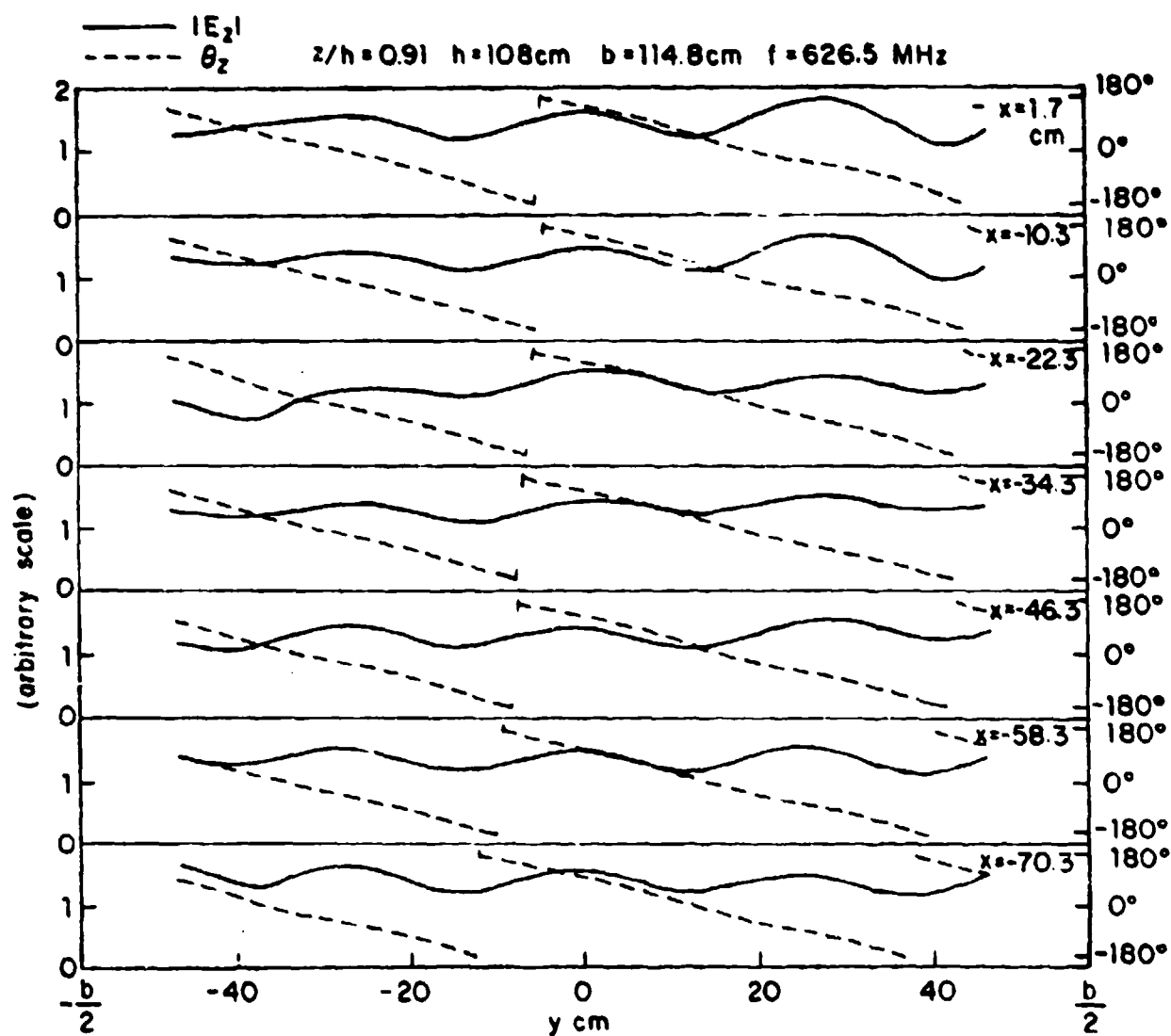


Fig. 16 Measured magnitude and phase of E_z in the working volume of model simulator

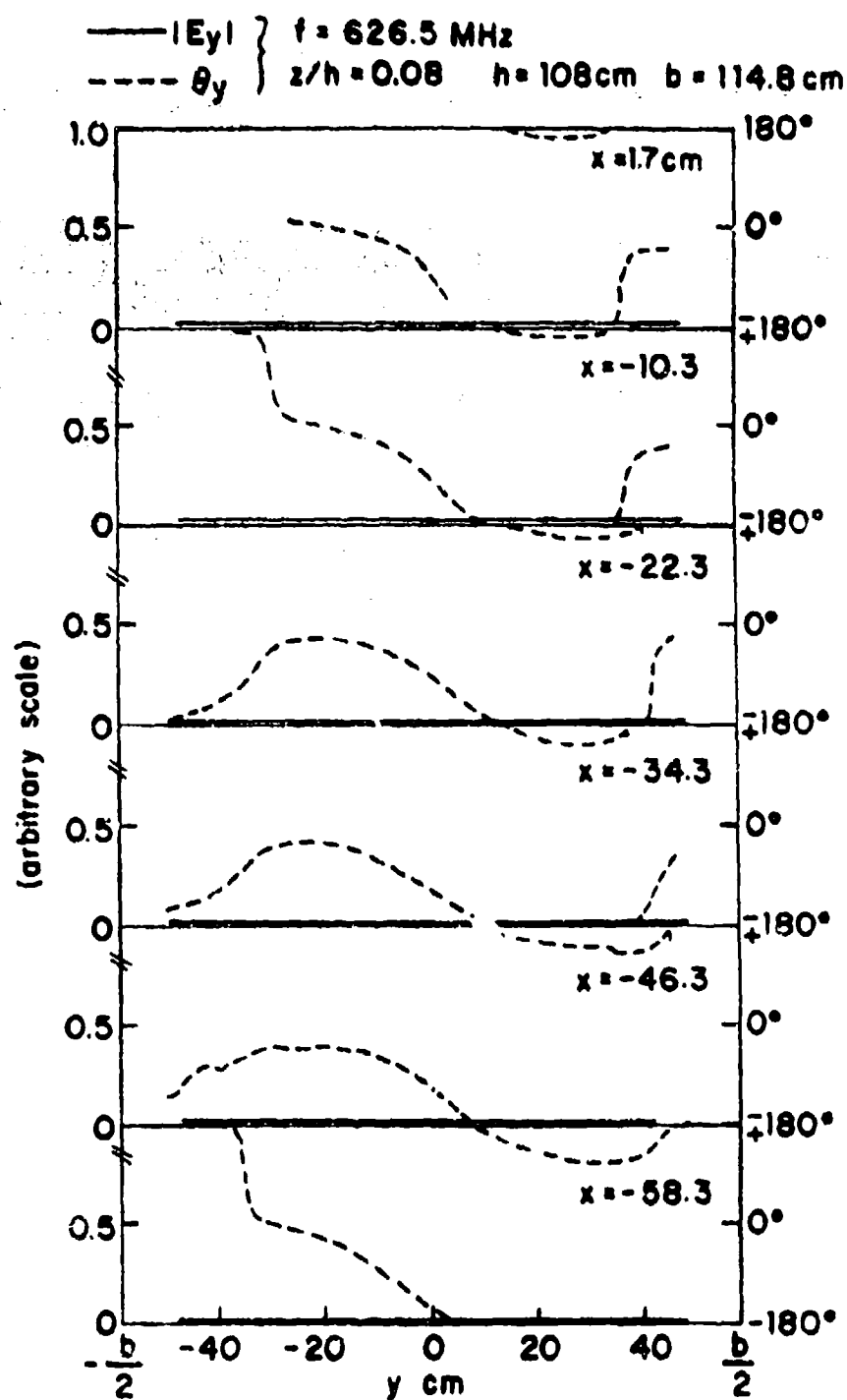


Fig. 18 Measured magnitude and phase of E_y in working volume of model simulator.

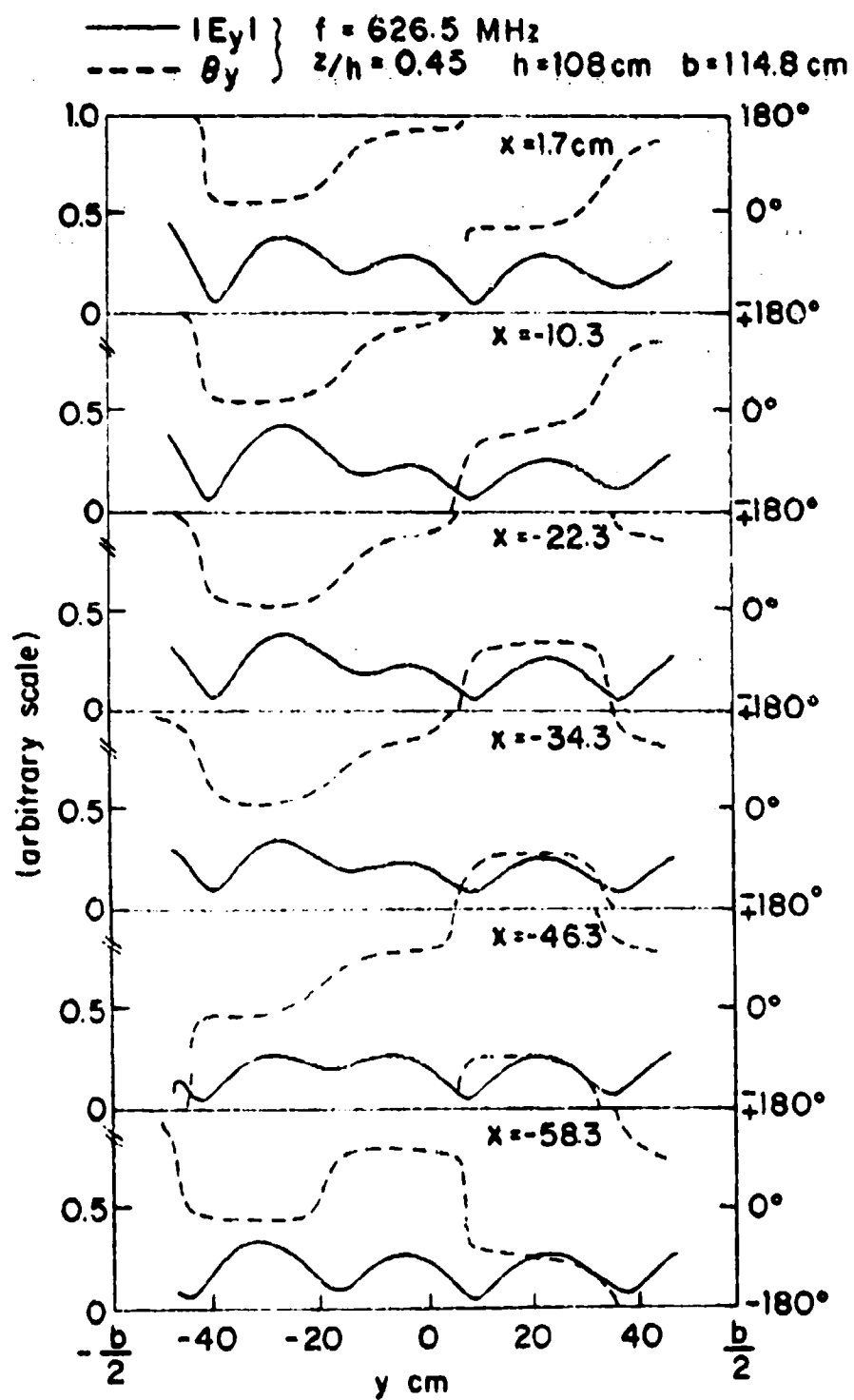


Fig. 19 Measured magnitude and phase of E_y in working volume of model simulator.

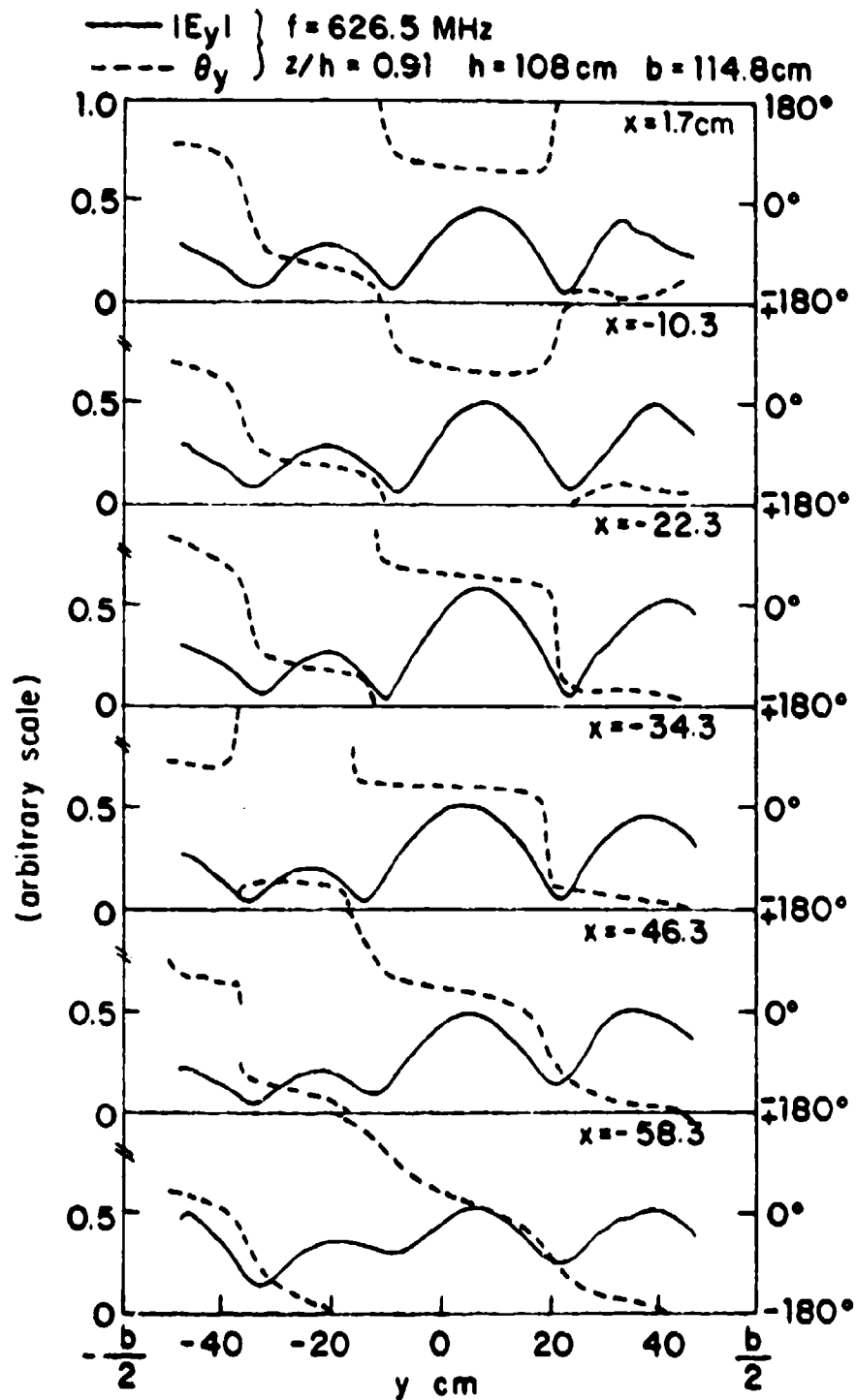


Fig. 20 Measured magnitude and phase of E_y in working volume of model simulator

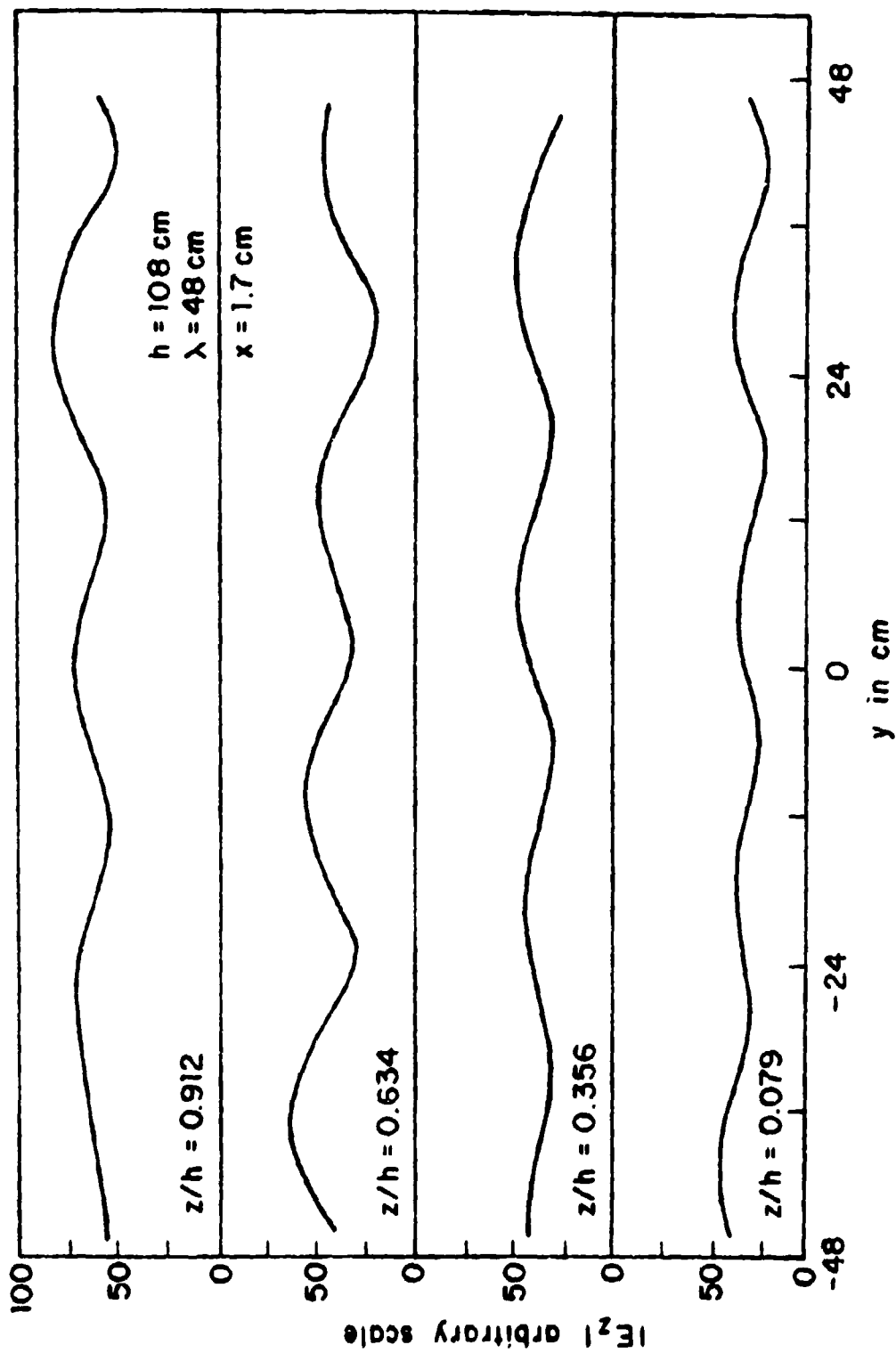


Fig. 21 Measured $|E_z|$ near center ($x = 1.7 \text{ cm}$) of working volume at four heights

top plate is quite different in that there are more nearly three instead of four standing half-wavelengths in the distance $-48 \text{ cm} \leq y \leq 48 \text{ cm}$. This is shown at the top in Figure 21. Thus, the measured graph at the top in Figure 21 resembles the graph at the top in Figure 12 for the standing-wave distribution of the $n = 3$ mode in the parallel-plate region. It is also evident from Figure 13 and Figures 18 through 20 that E_y is significant. It has a standing-wave distribution with a wavelength near λ_{g3} and is displaced from that of $|E_z|$ by nearly $\lambda_{g3}/4$.

In order to interpret the extensive data contained in the measured field in the working volume, the graphs shown in Figure 22 were constructed from the measured data. They show the measured $|E_z|$ as a function of the vertical coordinate z at seven different transverse positions x across the central plane ($y = 0$) of approximately one-half of the working volume. The distributions are seen to be quite comparable in magnitude and shape, thus indicating a field that is reasonably independent of the transverse coordinate x , as is implicit for the ideal TEM and TM_{0n} components. The fact that E_z is approximately independent of x also indicates that the contribution to $|E_z|$ by possible TE_{0l} modes is small. This is considered in a later section.

At each cross section ($y = \text{constant}$), E_z can be approximated by a superposition of the TEM and the three propagating TM_{0n} modes. The relative amplitudes of these modes cannot be determined theoretically, but can be obtained from the measured distribution of $E_z = E_{zR} + iE_{zI}$. Thus,

$$E_z(y) = A(y) + B(y)\cos(\pi z/h) + C(y)\cos(2\pi z/h) + D(y)\cos(3\pi z/h) \quad (14)$$

where $A(y) = A_R(y) + iA_I(y)$ is the complex amplitude of the TEM mode, $B(y) = B_R(y) + iB_I(y)$, $C(y) = C_R(y) + iC_I(y)$, and $D(y) = D_R(y) + iD_I(y)$ are, respectively, the complex amplitudes of the TM_{0n} modes, $n = 1, 2, 3$. The real amplitudes $A_R(y)$, $B_R(y)$, ..., $A_I(y)$, $B_I(y)$, ..., can be determined by fitting the distribution (14) to the corresponding measured curve at each cross section $y = \text{constant}$. Since E_z is approximately independent of x , it is sufficient to evaluate the amplitude coefficients at $x = 0$. The appropriate values are shown in Table 1 with all phases referred to the origin of coordinates $x = y = z = 0$. Graphs of the coefficients as functions of y are shown in Figure 23. It is seen that they form standing-wave patterns with

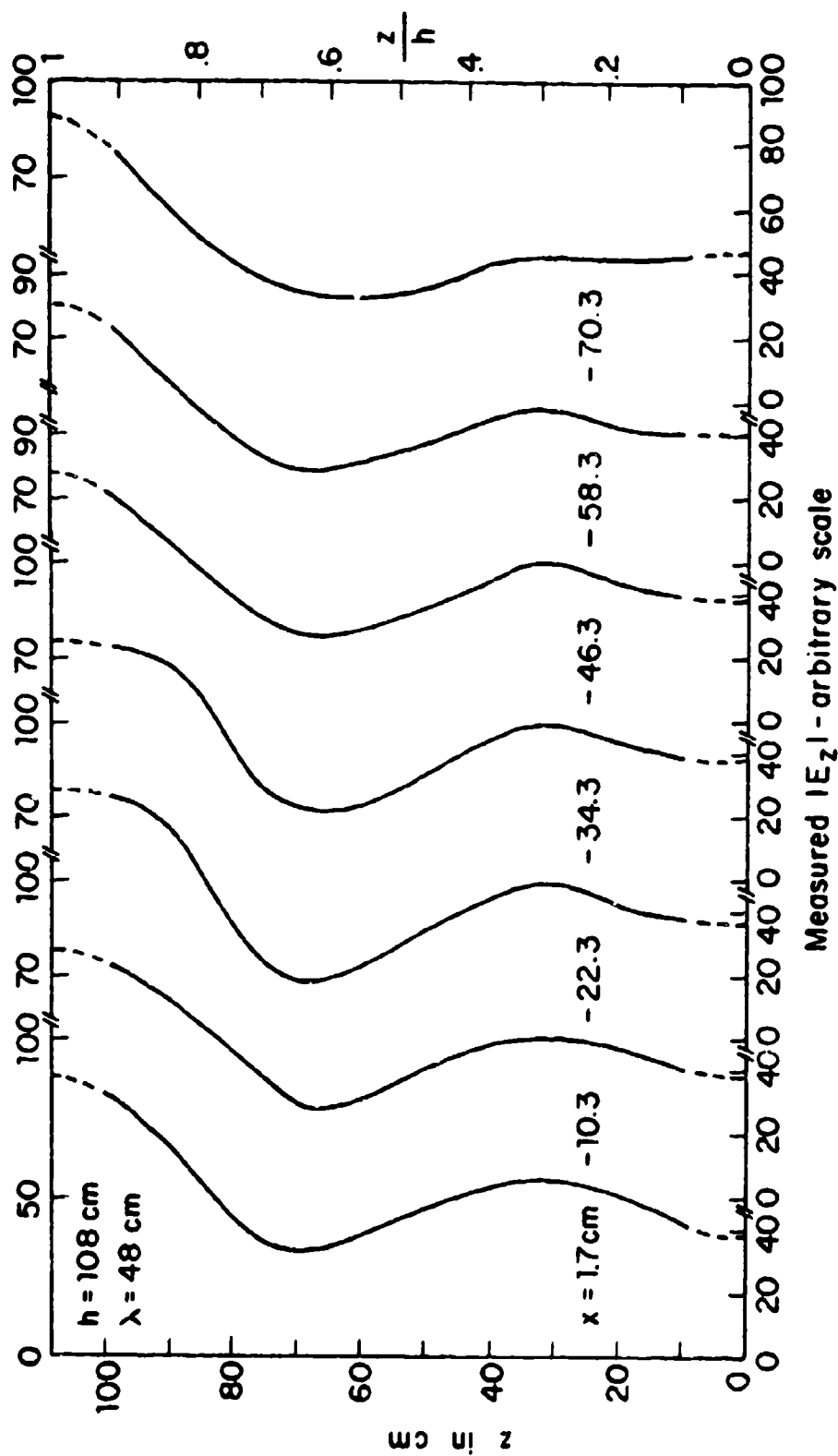


Fig. 22 Measured electric field near central plane ($y=0$) in working volume

TABLE 1

COEFFICIENTS REFERRED TO $y = 0$, $z = 0$, OBTAINED FROM MEASURED DATA

$y(\text{cm}) =$	0	-6	-12	-18	-24	-30	-36	-42	-46.5
$A_I(y)$	-41.2	-10.0	25.9	43	35	4.4	-34.7	-44	-40.2
$B_I(y)$	26.2	40.3	24.5	-0.2	-30	-37.3	-23.6	-1.5	19.6
$C_I(y)$	-3.5	-7.9	-5.1	-4	10.1	12.8	15.6	2.1	-6.4
$D_I(y)$	18.6	14.2	6.7	1.9	-9.0	-12.7	-15.3	-3.7	-3.2
$A_R(y)$	25.0	39.5	34.2	13.4	-19.8	-42.0	-33.4	-10.4	8.9
$B_R(y)$	16.7	-11.9	-35.3	-43.7	-18.8	16.4	45.5	46	23.1
$C_R(y)$	-2.1	-10.0	-4.7	2.7	2.5	7.0	-0.7	-4.8	-4.3
$D_R(y)$	1.0	7.6	5.8	4.1	1.6	-4.3	-6.2	-8.9	-6.9

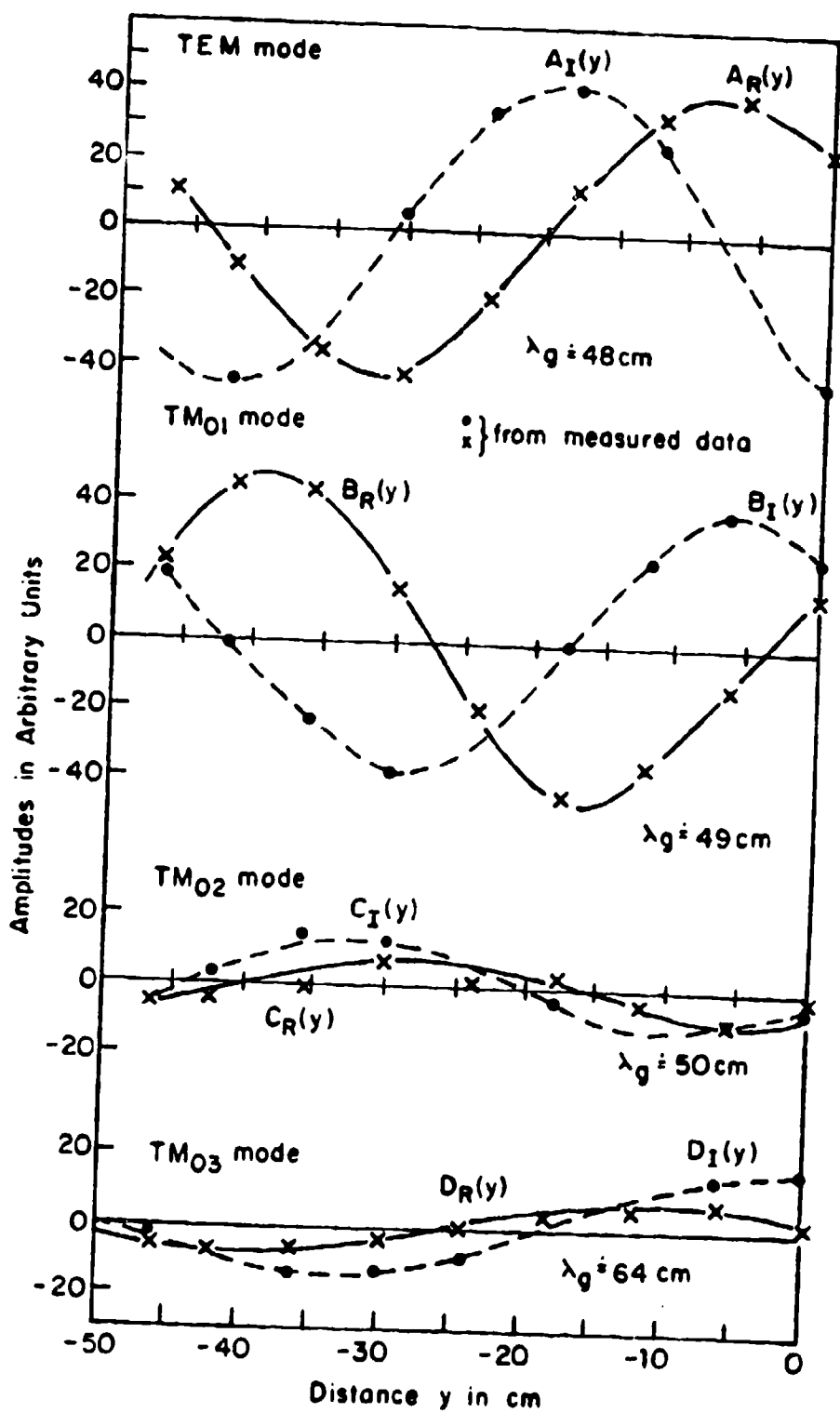


Fig. 23 Amplitudes of TEM and TM_{0n} modes in forward half of working volume

the wavelength $\lambda = 48$ cm for the A coefficients, $\lambda_{g1} = 49.1$ cm for the B coefficients, $\lambda_{g2} = 50$ cm for the C coefficients, and $\lambda_{g3} = 64$ for the D coefficients. These wavelengths are in good agreement with the ideal wavelengths, $\lambda = 48$ cm for the TEM mode, and $\lambda_{g1} = 49.2$ cm, $\lambda_{g2} = 53.7$ cm, and $\lambda_{g3} = 64.2$ cm for the TM_{0n} modes with $n = 1, 2, 3$.

When the coefficients in Table 1 are substituted in equation (14), E_z can be calculated as a function of z at any desired cross section. In Figures 24a and 24b are shown in broken lines the calculated vertical distributions of the real and imaginary parts of E_z at the center ($x = 0$, $y = 0$) of the working volume, and at $x = 0$ and successively $y = -6, -12, -18, -24, -30, -36$, and -42 cm toward the generator. Also shown in solid lines are the corresponding measured distributions. It is evident that the assumed approximate representation of the field as a superposition of the ideal parallel-plate TEM and TM_{0n} modes is a good one throughout the working volume of the model simulator. It is also evident that the total E_z differs greatly from the part contributed by the TEM mode alone, which is constant in z . Figure 23 shows that the amplitudes of the TEM and TM_{01} modes are almost the same. Their standing-wave distributions and phases are such that $|E_z|$ is substantially greater near the top plate, $z = h$, than near the ground plane, $z = 0$.

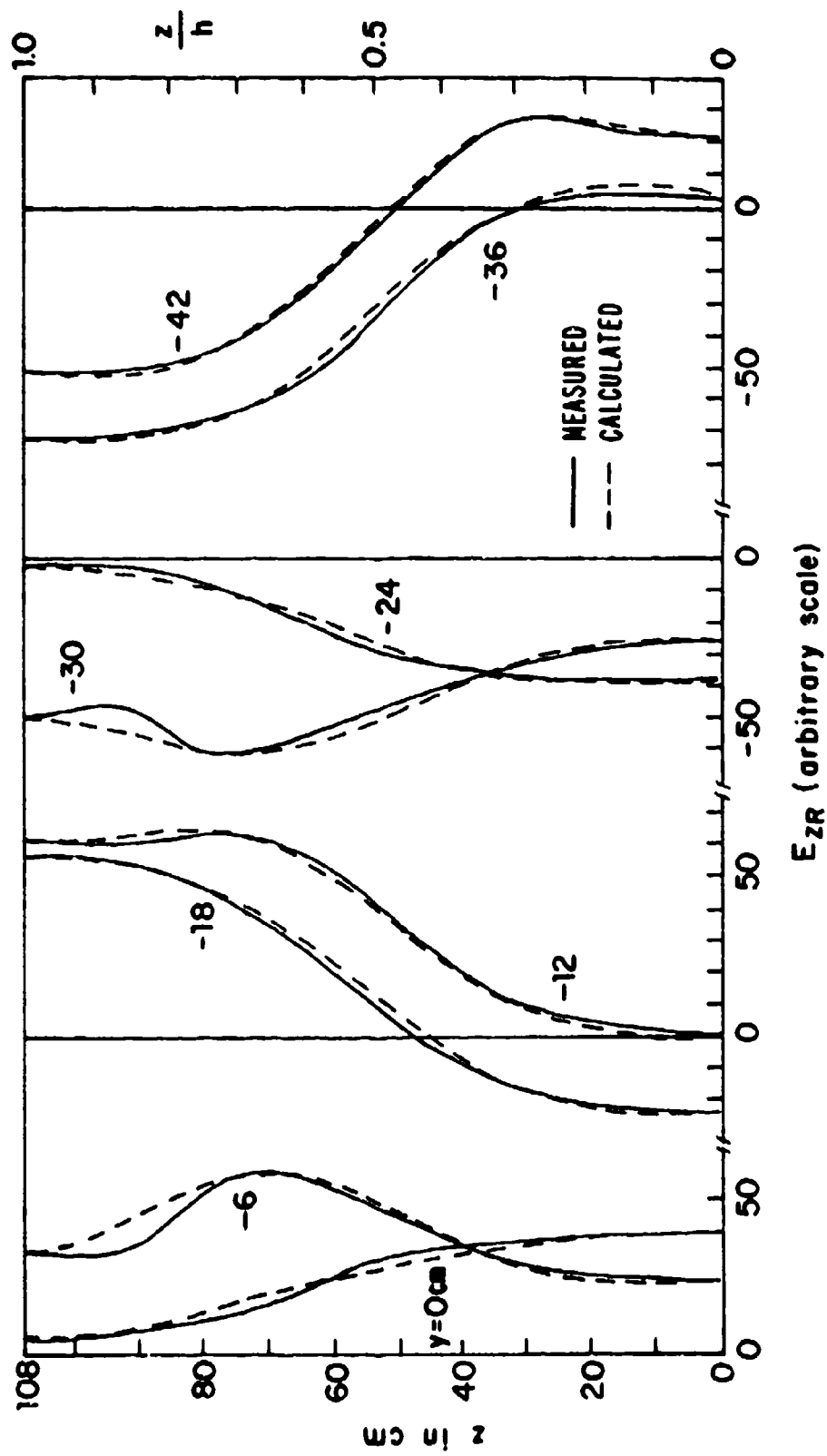


Fig. 24a Real part of vertical electric field in working volume. (Phase reference : $x = y = z = 0$)

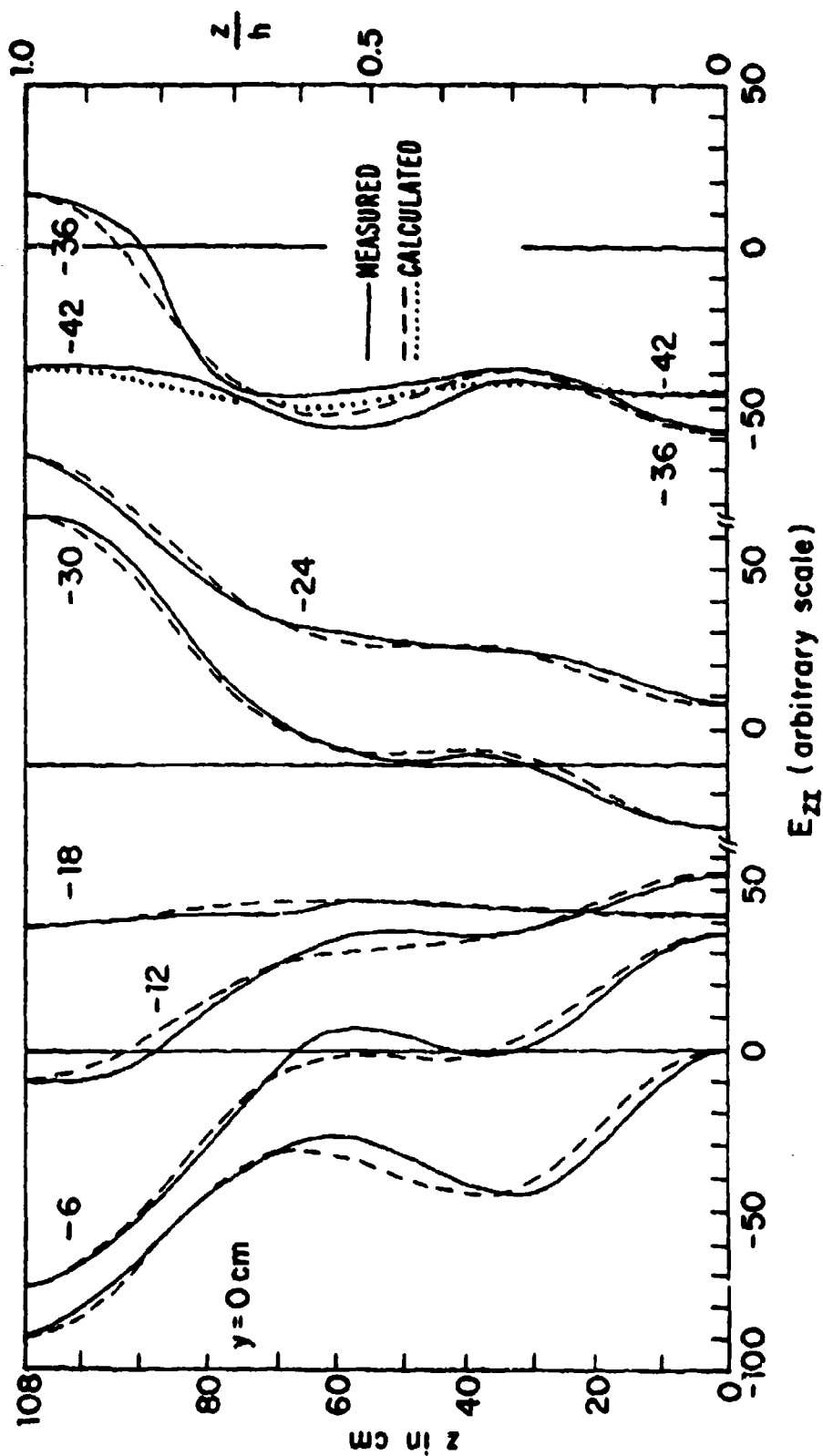


Fig. 24b Imaginary part of vertical electric field in working volume. (Phase reference: $x = y = z = 0$)

SECTION VII

THE MEASURED FIELD IN THE WORKING VOLUME: $h = 0.66\lambda = 75$ cm, $f = 264$ MHz

The components E_z and E_y in the working volume and adjacent regions were also measured with $f = 264$ MHz when $h = 75$ cm $= 0.66\lambda$ and $\lambda = 113.6$ cm. To simplify the presentation of the data, these components of the field were measured as functions of z/h with $y = 0$ and x as parameter. The measured graphs of $|E_z|$, $|E_y|$, θ_z , and θ_y are shown in Figure 25 for eight values of x . From them, the real and imaginary parts of E_z were determined, as shown in Figure 26.

Corresponding to equation (14), the vertical electric field is approximated by:

$$E_z(y) = A(y) + B(y)\cos(\pi z/h) \quad (15)$$

It follows that

$$A_R(y) + iA_I(y) = E_{zR}(y) + iE_{zI}(y), \quad \text{at } z = h/2 \quad (16)$$

Graphs of $A_R(y)$ and $A_I(y)$ as obtained from Figure 25 as functions of y are shown in the upper half of Figure 27. The half-wavelength is quite accurately $\lambda/2 = 56.8$ cm as determined from the graph of the large real part $A_R(y)$. Graphs of the amplitudes $B_R(y)$ and $B_I(y)$ of the part of $E_z(y)$ due to the TM_{01} mode are near the center of Figure 27; the associated graphs of the real and imaginary parts of $E_y(y)$, which is entirely TM_{01} , are at the bottom. Here the wavelength $\lambda_{g1} = 174$ cm is also confirmed by the standing-wave patterns of the imaginary parts. As with the higher frequency and greater height h of the working volume, the approximate representation of E_z and E_y by TEM and TM_{0n} modes is quite satisfactory.

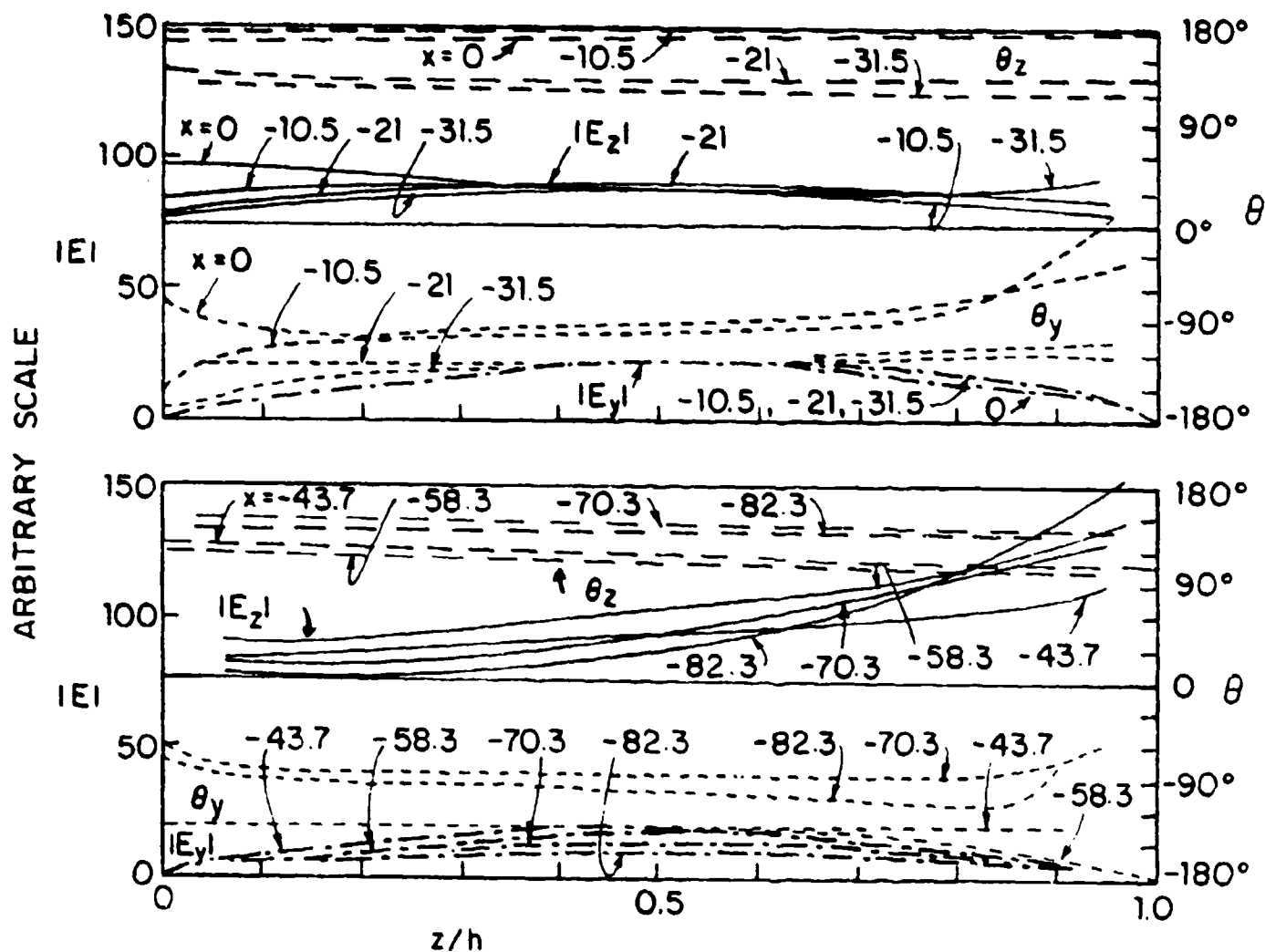


FIG. 25 MEASURED ELECTRIC FIELD IN TRANSVERSE PLANE $y=0$ OF WORKING VOLUME; $b = 114.8$ cm, $2a = 175$ cm, $h = 75$ cm, $f = 264$ MHz.

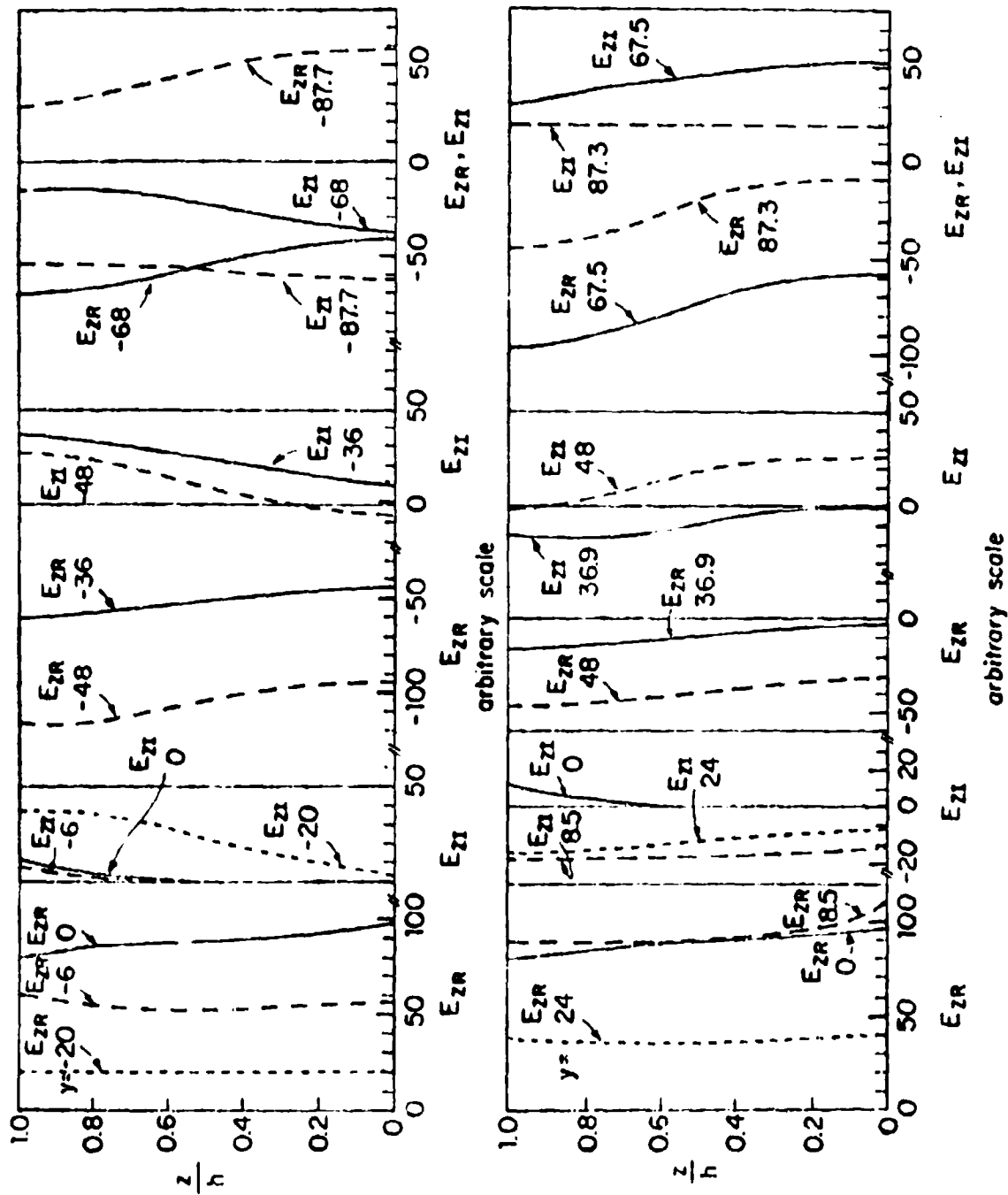


Fig. 26 Real and Imaginary Parts of E_z in Working Volume and Adjacent Regions; Phase Referred to $x=y=z=0$.

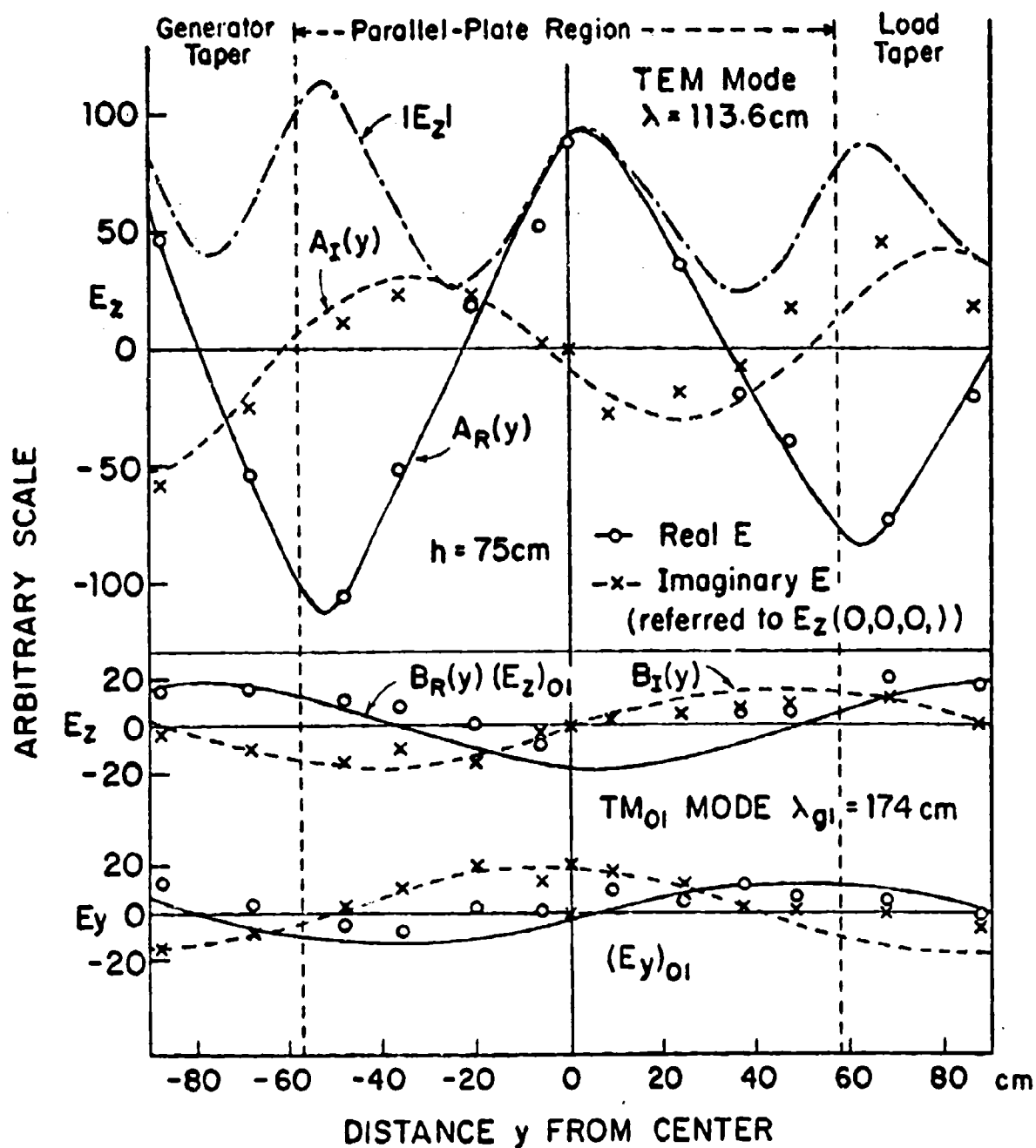


FIG. 27 GRAPHS OF THE REAL AND IMAGINARY PARTS OF $E_z(y) = A(y) + B(y)\cos(\pi z/h)$ AND $E_y(y)$ AS FUNCTIONS OF y IN AND NEAR THE PARALLEL PLATE REGION.

SECTION VIII

THE TRANSVERSE VARIATION OF THE ELECTRIC FIELD; TE MODES

The approximate representation of the electric field in the parallel-plate region of the simulator in terms of the TEM and TM_{0n} modes tacitly assumes that all of the components of the electromagnetic field are independent of the transverse variable x since all wave fronts are assumed to be planes perpendicular to the longitudinal y -axis. This was taken to be a good approximation because the electric field shown in Figure 22 changes relatively little as x is varied in steps from near the center of the working volume to near the edge at $x = \pm a = 87.5$ cm. It is now appropriate to examine the variation of the field with x in greater detail.

A useful starting point is the nature of the wave fronts - surfaces of constant phase - in the working volume. It is shown in conjunction with Figures 7 and 8 that the field incident on the parallel-plate region at $y = -b/2 = -57.5$ cm is essentially a traveling spherical wave. In Figures 28a, 28b, and 28c are shown the measured phase fronts of θ_z , the phase angle of E_z , in xy -planes at discrete values of z/h ranging from 1 to 0. With the measured curves are shown the phase fronts for ideal spherical traveling waves originating at the generator end of the simulator ($x = 0$, $y = -369$ cm, $z = 0$ when $h = 108$ cm). These graphs supplement those in Figures 10a and 10b which show the measured phase fronts of θ_z in yz -planes together with the phase fronts for the ideal spherical waves. It is seen from all of these diagrams that the measured phase fronts in transverse as well as in vertical planes are those of a spherical wave with superimposed oscillations due to standing waves. Clearly, the length and width of the parallel-plate region are inadequate to permit the development of plane wave fronts and the assumption that these are good approximations is acceptable only in the central part of the working volume, roughly in the range -50 cm $\leq x \leq 50$ cm, $z \leq h/2 = 54$ cm.

The measured transverse distributions of both $|E_z|$ and θ_z are shown in Figure 29 for a range of values of z from $z = 8.5$ cm $= 0.18\lambda$ near the ground plane at $z = 0$ to $z = 98.5$ cm or $h - z = 108 - 98.5$ cm $= 0.20\lambda$ from the top plate. The graphs of $|E_z|$ show a reasonably constant mean value for each value of z with a superimposed oscillation. This oscillation is a consequence

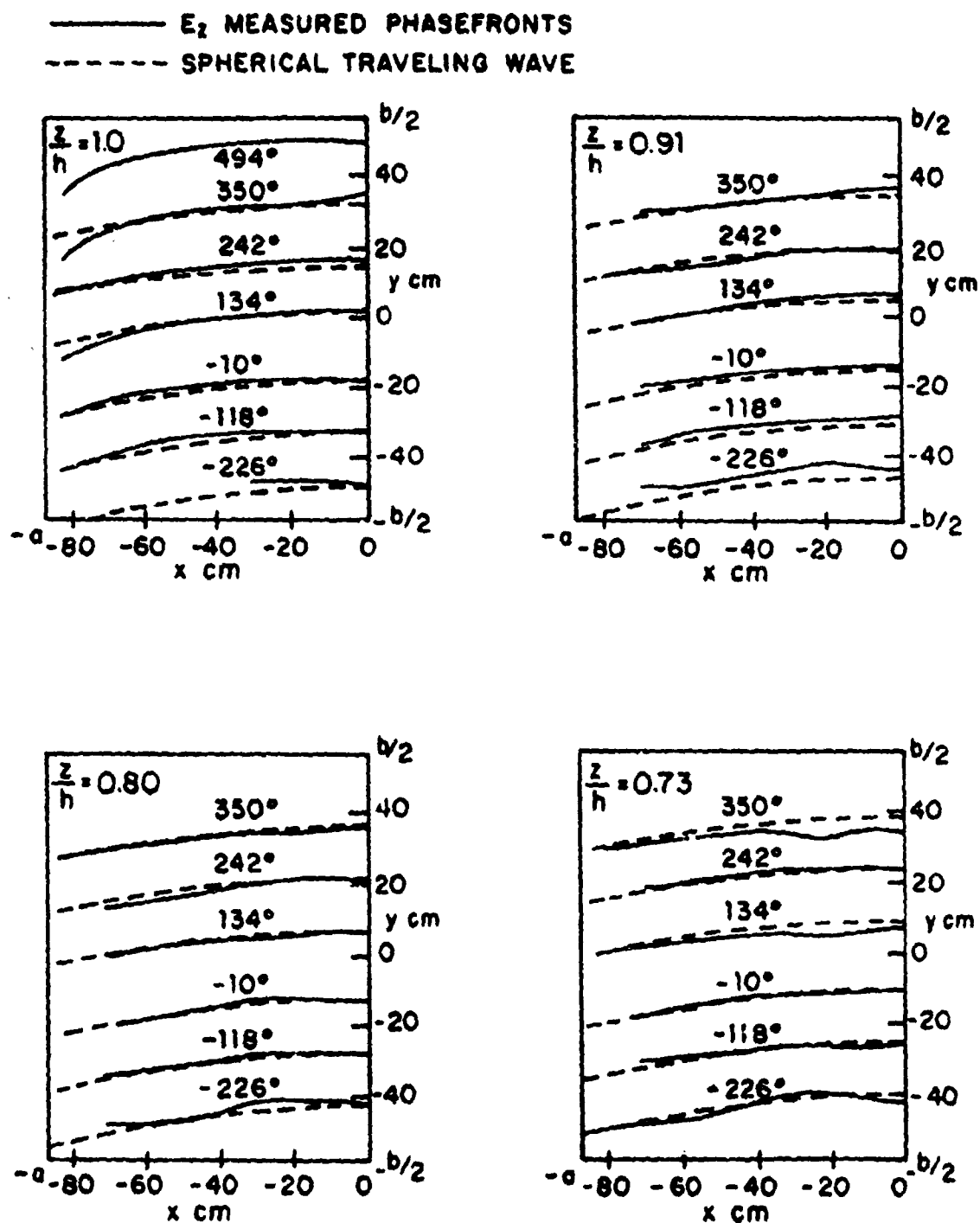


FIG. 28a MEASURED CONSTANT PHASE CURVES IN THE WORKING VOLUME;
 $h = 108$ cm, $a = 87.5$ cm, $b = 114.8$ cm, $f = 626.5$ MHz.

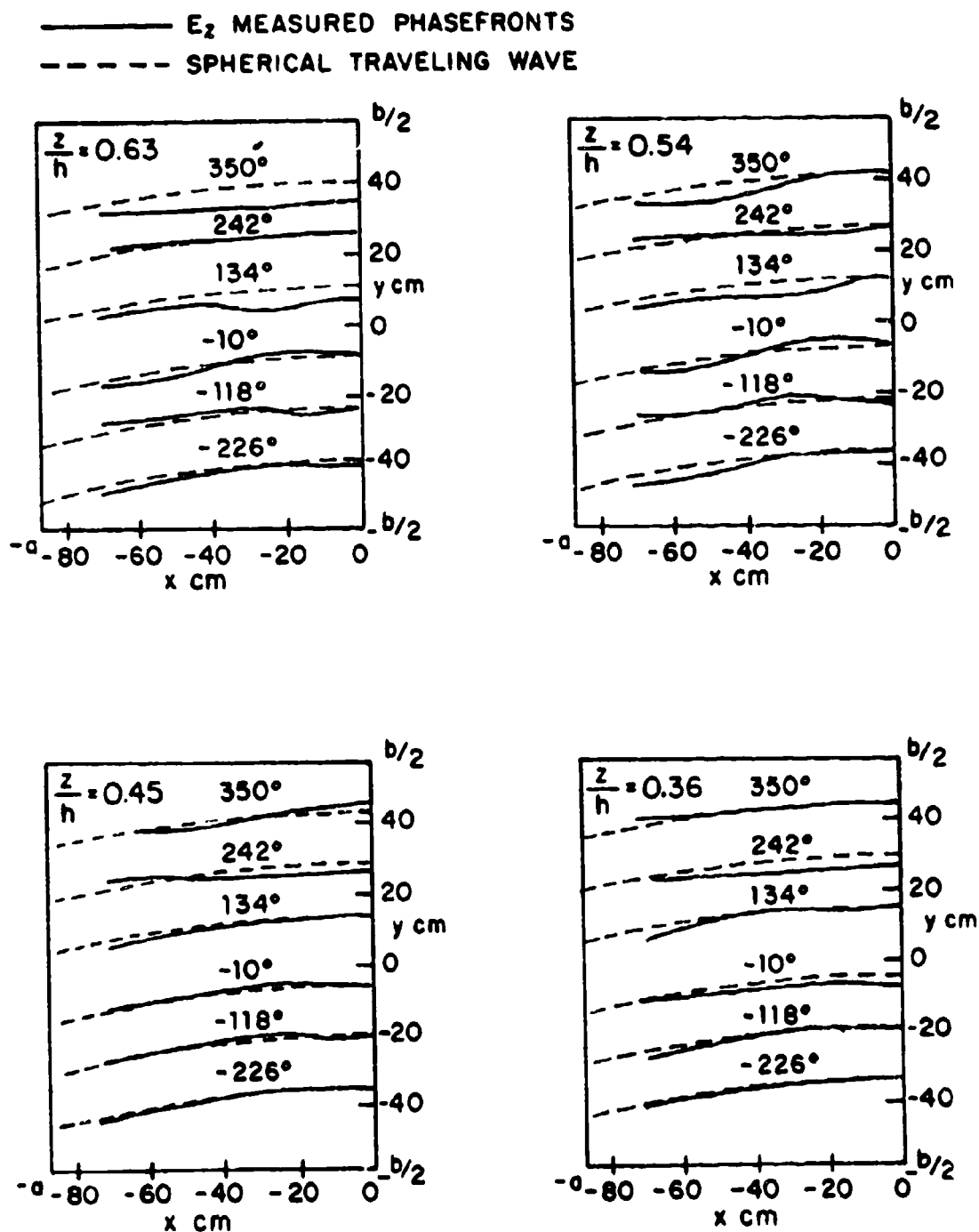


FIG. 28b MEASURED CONSTANT PHASE CURVES IN WORKING VOLUME;
 $h = 108$ cm, $a = 87.5$ cm, $b = 114.8$ cm, $f = 626.5$ MHz.

—— E_z MEASURED PHASEFRONTS
 ---- SPHERICAL TRAVELING WAVE

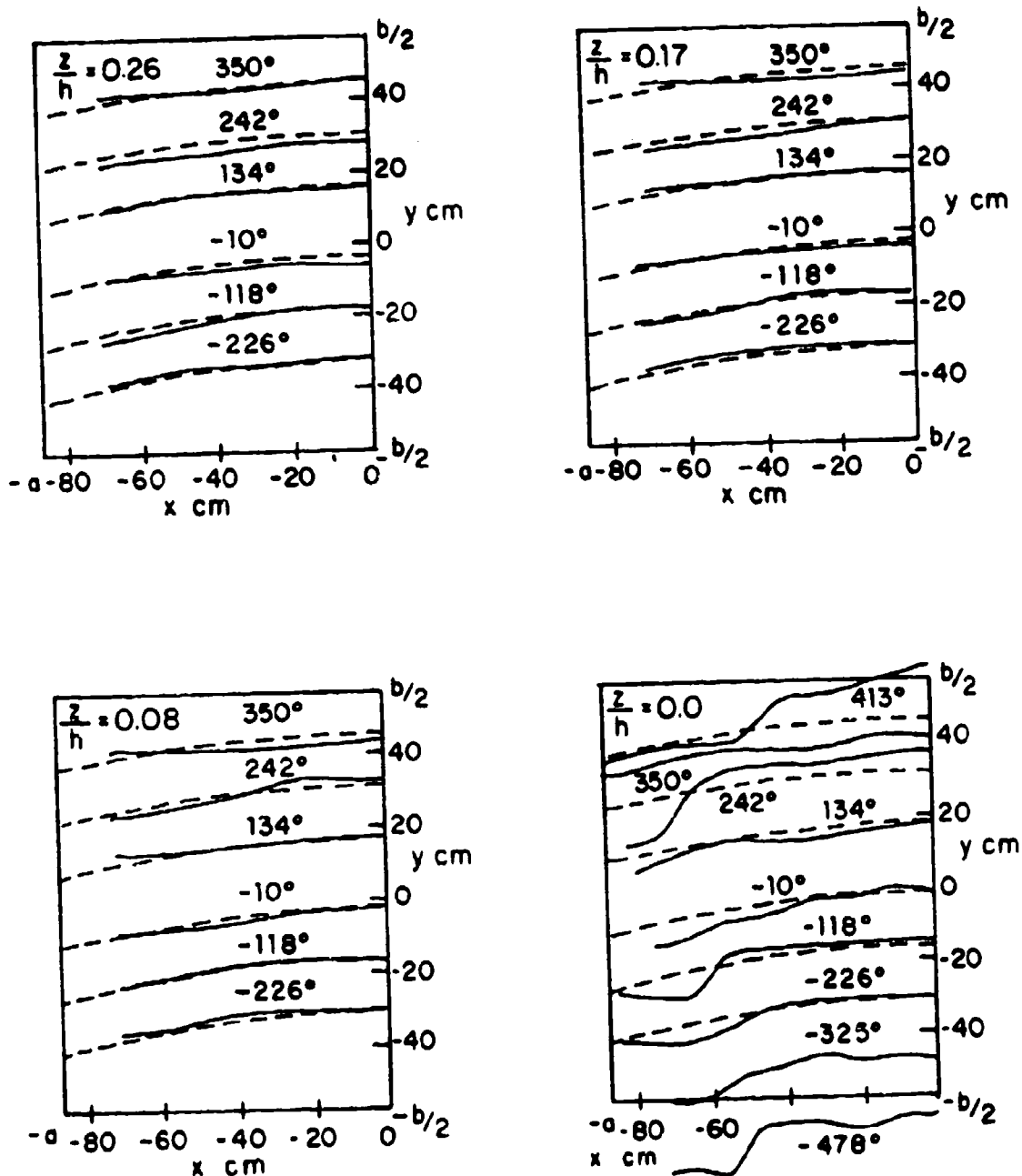


FIG. 28c MEASURED CONSTANT PHASE CURVES IN WORKING VOLUME;
 $h=108$ cm, $b=114.8$ cm, $f=626.5$ MHz.

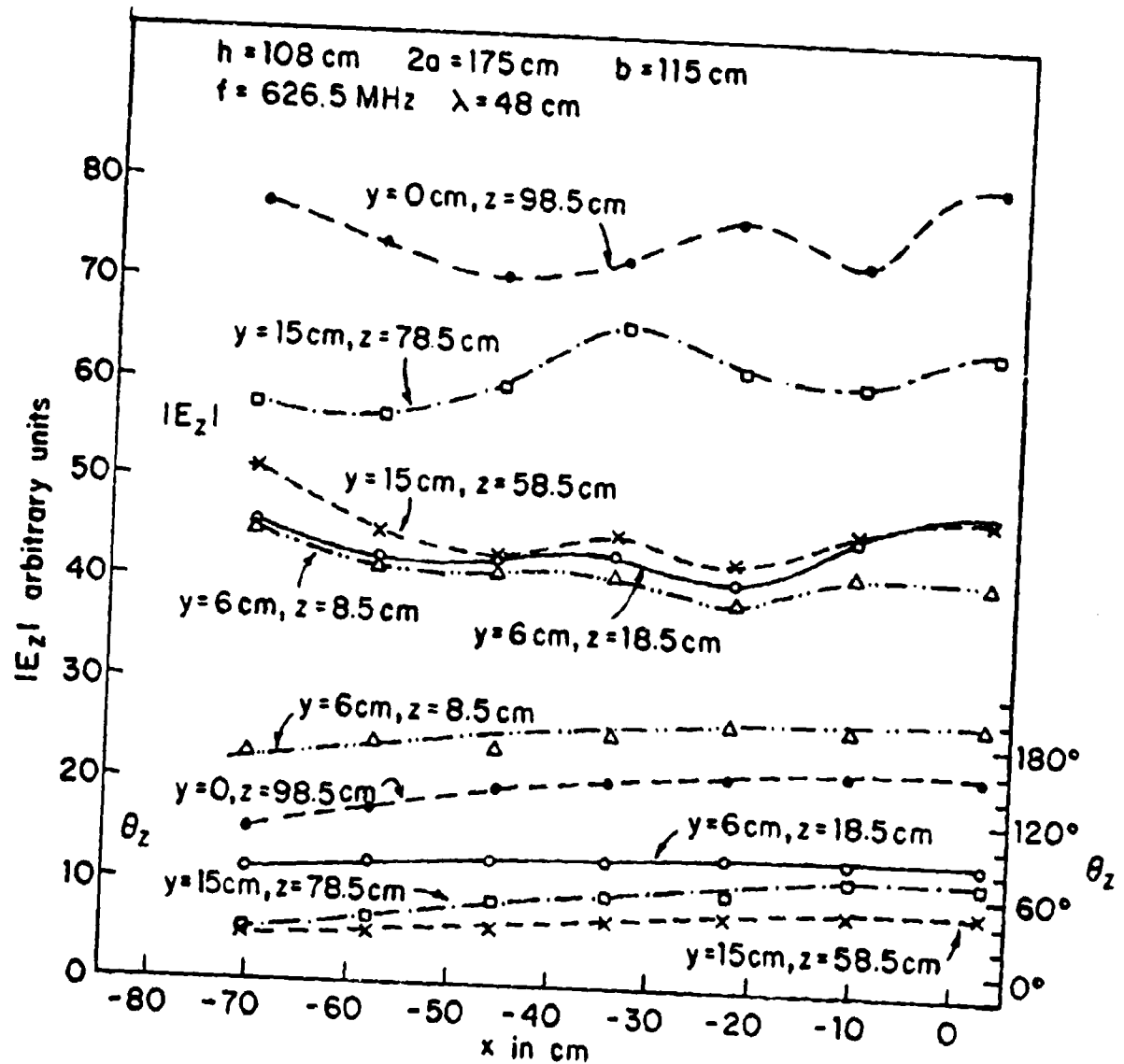


FIG. 29 MEASURED TRANSVERSE DISTRIBUTION OF E_2

of the fact that the wave fronts are actually spherical and not planar. The value of y selected for each z was the one at the maximum of $|E_z|$ nearest $y = 0$ in the standing-wave pattern with respect to the longitudinal coordinate y . The graphs of the phases θ_z are like those in Figures 28a, 28b, and 28c.

In Figure 30 are graphs similar to those in Figure 29, but for the smaller height $h = 75$ cm and the lower frequency 264 MHz. They range from $z = 10$ cm $= 0.09\lambda$ from the ground plane to $z = 70$ cm or $h - z = 5$ cm $= 0.04\lambda$ from the top plate. Since only TEM and TM_{01} modes are involved, it is possible also to show a graph of the transverse distribution of E_y at $z = 0.5h = 37.5$ cm where it is maximum. This is at the bottom of the figure. It is seen that E_y is quite constant from $x = 0$ to $x = -35$ cm where it begins to decrease to near half value at $x = -87.5$ cm, the edge of the upper plate. $|E_z|$ shown at the top is more complicated. Consider first the graph with $z = 37.5$ cm which shows the TEM mode only since E_z for the TM_{01} mode is zero at $z = h/2$. E_z as given by this graph is quite constant for -35 cm $\leq x \leq 35$ cm, but then experiences a significant oscillation. This is due to the spherical wave front which necessarily produces an oscillation along a planar surface. The average magnitude of E_z about which the oscillation takes place decreases from $x = 0$ outward at each value of z in the range $z < h/2 = 37.5$ cm; the magnitude increases when $z > h/2 = 37.5$ cm. As the edge of the upper plate at $x = -87.5$ cm, $z = h = 75$ cm is approached, $|E_z|$ increases rapidly and dominates over the relatively small oscillatory amplitude. The changes in $|E_z|$ as x is increased from zero are a consequence of the finite width of the upper plate. The electric lines of E_z that are vertical for infinitely wide plates are pushed outward near the ground plane and converge at and near the edge of the top plate, where there are large concentrations of electric charge on both the lower and upper surfaces, as shown schematically in Figure 31. The thinning of the electric lines near the ground plane corresponds to a reduction in $|E_z|$, the greater density of electric lines near the top plate corresponds to an increase in $|E_z|$.

As pointed out in conjunction with Figure 9(c), the excitation of the parallel-plate section of the simulator by an incident spherical wave provides antisymmetric components H_y of the magnetic field in the xz -plane at $y = -b/2 = -57.5$ cm. With metal plates of finite width, these can potentially excite antisymmetric TE_{m1} modes. A complete analysis of all possible TE

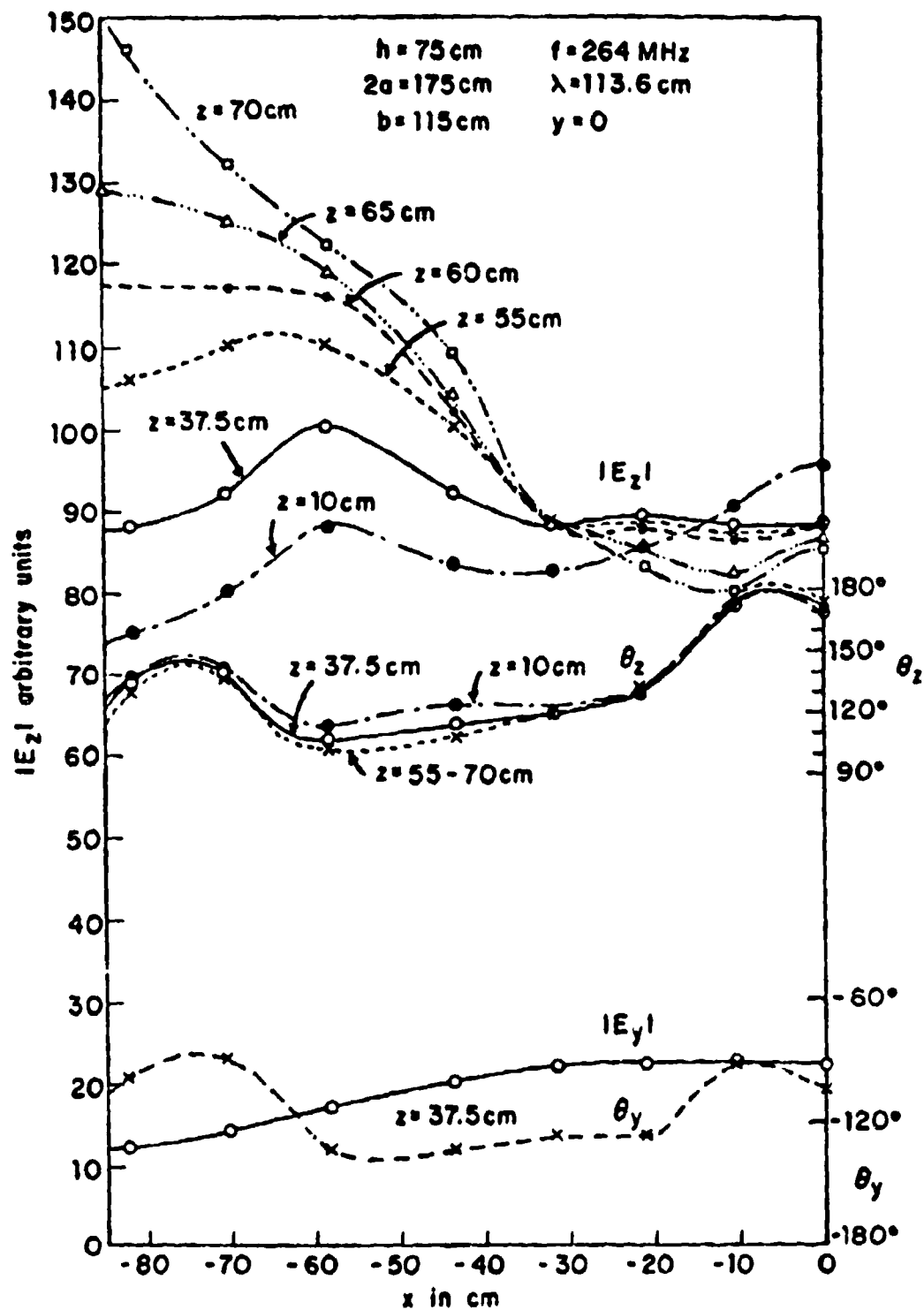


Fig. 30 Transverse distributions of E_2 and E_y

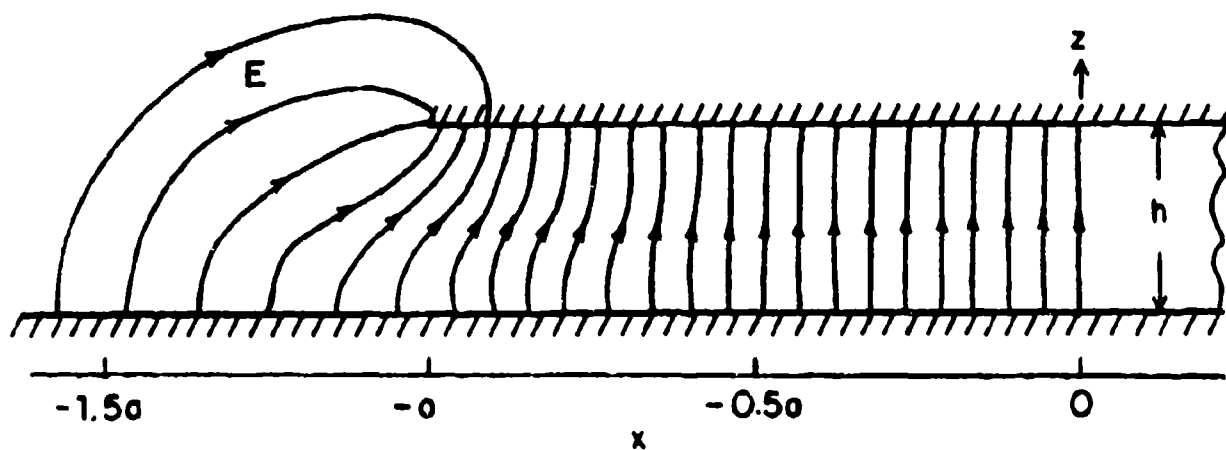


FIG. 31 SCHEMATIC DIAGRAM OF ELECTRIC FIELD LINES IN TRANSVERSE PLANE SHOWING FRINGING AT THE OPEN SIDE

modes without reference to any method of excitation has been given by Rushdi et al. (ref. 3). Those of possible interest in the parallel-plate section of the simulator are characterized by the following components of the electromagnetic field. They are antisymmetric in the transverse coordinate x . The antisymmetric $TE_{m\ell}$ modes that can be excited are given by:*

$$H_x^a \sim k_{x\ell} \cos(m\pi z/h) \cos(k_{x\ell} x) \quad (17)$$

$$H_y^a \sim \cos(m\pi z/h) \sin(k_{x\ell} x) \quad (18)$$

$$H_z^a \sim (m\pi/h) \sin(m\pi z/h) \sin(k_{x\ell} x) \quad (19)$$

$$E_x^a \sim (m\pi/h) \sin(m\pi z/h) \sin(k_{x\ell} x) \quad (20)$$

$$E_z^a \sim k_{x\ell} \cos(m\pi z/h) \cos(k_{x\ell} x) \quad (21)$$

where $m = 0, 1, 2, \dots$, $\ell = 1, 3, 5, \dots$. The most important are those with $m = 0$, for which

$$H_x^a \sim k_{x0\ell} \cos k_{x0\ell} x ; H_y^a \sim \sin k_{x0\ell} x ; H_z^a = 0 \quad (22)$$

$$E_x^a = 0 ; E_y^a = 0 ; E_z^a \sim k_{x0\ell} \cos k_{x0\ell} x \quad (23)$$

with $\ell = 1, 3, 5, \dots$. Also of possible interest are the $TE_{m\ell}$ modes with $m = 1$, for which

$$H_x^a \sim k_{x1\ell} \cos(\pi z/h) \cos(k_{x1\ell} x) ; E_x^a \sim (\pi/h) \sin(\pi z/h) \sin(k_{x1\ell} x) \quad (24)$$

$$H_y^a \sim \cos(\pi z/h) \sin(k_{x1\ell} x) ; E_y^a = 0 \quad (25)$$

$$H_z^a \sim (\pi/h) \sin(\pi z/h) \sin(k_{x1\ell} x) ; E_z^a \sim k_{x1\ell} \cos(\pi z/h) \cos(k_{x1\ell} x) \quad (26)$$

* When referred to the full height with image, h is replaced by $2h$, and $m = 0, 2, 4, 6, \dots$, instead of $0, 1, 2, 3, \dots$.

The amplitudes and wave numbers for the TE modes are given by Rusdhi et al. (ref. 3), and normalized amplitudes of the components of the field are evaluated for a parallel-plate region with $h/2a \ll 1$, specifically, $h/2a = 0.01$. This condition is not satisfied by the Harvard simulator, for which $h/2a = 108/175 = 0.62$ or $h/2a = 75/175 = 0.43$. A schematic representation of the TE_{01} and TE_{03} modes is in Figure 32a. It is seen that a superposition of the two modes to give $H_y = AH_{y1} + BH_{y2}$, where B is negative, will roughly approximate the antisymmetric distribution of H_y^{inc} due to the incident spherical wave shown in Figure 9(c). This shows a positive maximum of H_y^{inc} at the right edge of the working volume, a negative maximum of H_y^{inc} at the left edge. Thus, it seems reasonable to suppose that a superposition of TE_{0l} modes will approximate the difference $E_z(x,y,z) - E_z(0,y,z)$, where $E_z(0,y,z)$ is the field represented by TEM and TM_{0n} modes, and to assume that the TE_{11} mode shown in Figure 32b and other higher modes contribute negligibly. However, it is obvious from an examination of the distributions in Figure 32a of the TE_{01} and TE_{03} modes that many more than just these two are required to approximate the complicated transverse distributions shown in Figures 29 and 30. In this connection, it is well to note that the actual TE_{0l} distributions for a parallel-plate waveguide of finite width as formulated by Rusdhi et al. (ref. 3) take full account of the effects of the open sides of the waveguide. For the purposes of this report, the representation of the electromagnetic field in terms of TEM and TM_{0n} modes is adequate without the addition of a sum of TE_{0l} modes. As seen from Figures 29 and 30, the departure of $E_z(x,y,z)$ from $E_z(0,y,z)$ is quite small - of the order of 8% - in the central part of the simulator.

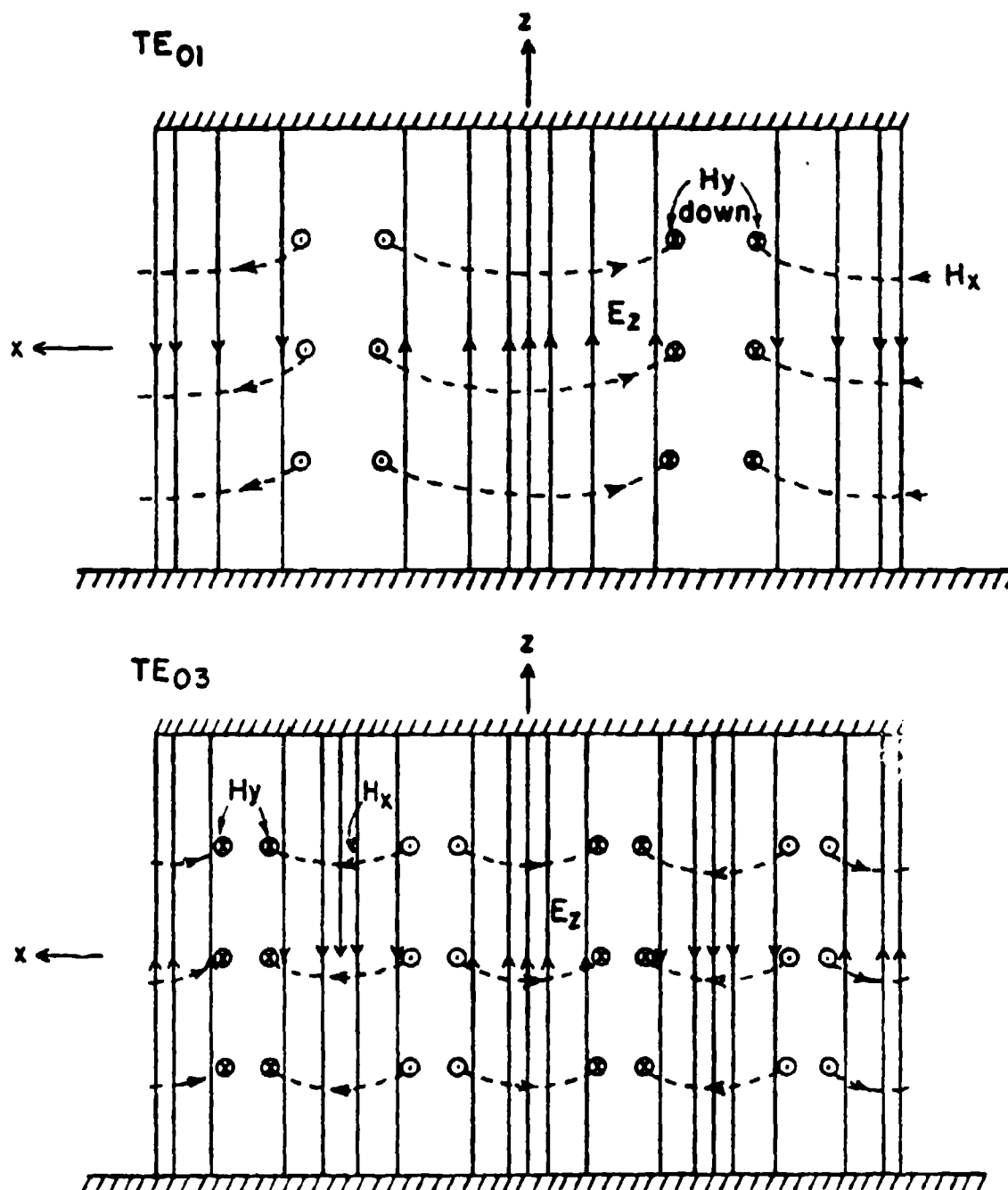


FIG. 320 SCHEMATIC DIAGRAM OF TE_{01} AND TE_{03} MODES IN WORKING VOLUME; SOLID LINES, ELECTRIC FIELD E_z ; BROKEN LINES, MAGNETIC FIELD $\vec{H} = \hat{x} H_x + \hat{y} H_y$.

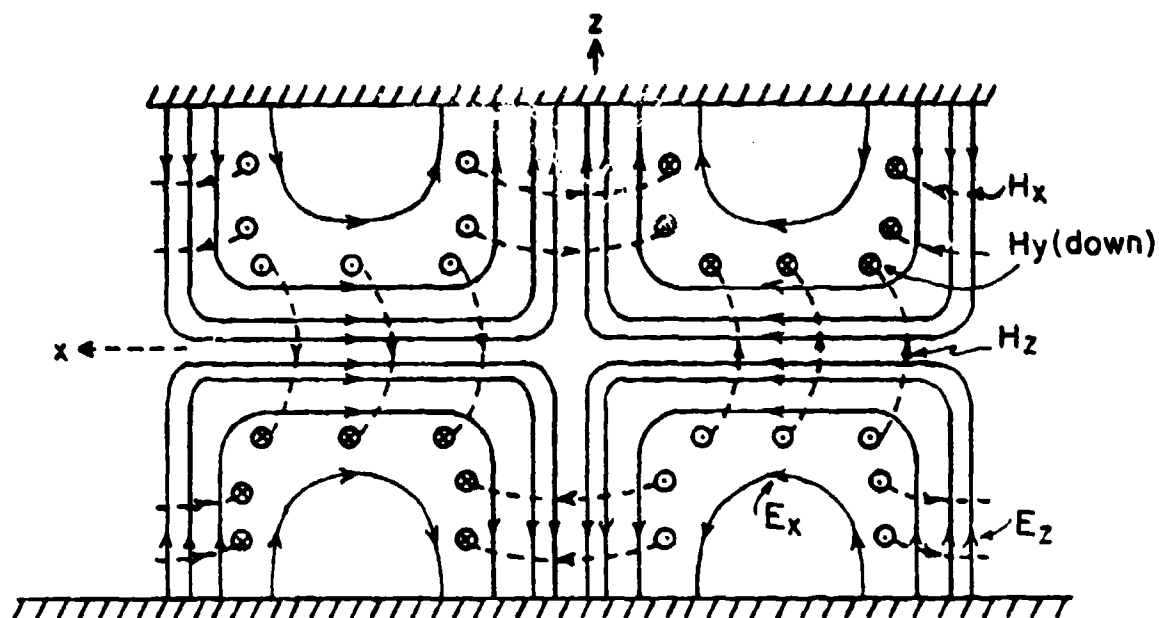


FIG. 32b SCHEMATIC DIAGRAM OF TE_{11} MODES IN WORKING VOLUME.
SOLID LINES, ELECTRIC FIELD; BROKEN LINES, MAGNETIC FIELD.

SECTION IX

THE ACTUAL ELECTROMAGNETIC FIELD IN THE SIMULATOR AS AN APPROXIMATION OF A PLANE WAVE

The electromagnetic field which is to be approximated in the working volume of the simulator is a plane wave traveling in the positive y-direction with the components $E_z(y,t) = E_z(0)e^{i(ky - \omega t)}$, $H_x(y,t) = E_z(y,t)/\zeta_0$, where $\zeta_0 = (\mu_0/\epsilon_0)^{1/2} = 120\pi$ ohms. The field is independent of the transverse coordinates x and z, and is distributed as shown in the upper left of Figure 11 at the instant $t = 0$. As time passes, the entire pattern moves in the positive y-direction with the speed $c = 3 \times 10^8$ m/sec.

The actual field in the parallel-plate section of the simulator is a spherical wave originating at the driving-point on the ground plane and modified by superimposed reflections from the top plate. The field can be approximated by a sum of appropriate parallel-plate modes, but this is merely a change in the representation and not in the nature of the field. Moreover, all of the modes are generated by the incident field and not by reflection at the load end.

As the cylindrical wave travels in the parallel-plate region, it experiences reflections at the edges $x = \pm a$ and at the end $y = b/2$. The former maintain the transverse standing waves shown in Figures 29 and 30, the latter the longitudinal standing waves shown in Figures 13 and 27. They can be decomposed into separate standing waves of the TEM and TM_{0n} modes, as shown in Figures 23 and 27. These graphs illustrate the standing-wave patterns of E_z and E_y . Measurements were also made of the standing-wave pattern of the magnetic field over a wide range of frequencies centering on $f = 264$ MHz with $h = 75$ cm. Selected graphs at $f = 250, 264$, and 270 MHz are shown in Figure 33. It is seen that as the frequency is varied, the entire standing-wave pattern moves. Simultaneously, the standing-wave ratio fluctuates. Note in Figure 33 how the depth of the minimum varies as its location moves. If the loop probe is fixed at $y = 0.074b = 8.5$ cm, which locates the minimum for $f = 264$ MHz shown in the middle figure in Figure 33, and the frequency is then varied, the graph shown in Figure 34 is obtained. This shows a succession of minima that occur at $y = 0.074b$ at different frequencies, but with that at $f = 264$ MHz the deepest and sharpest. The

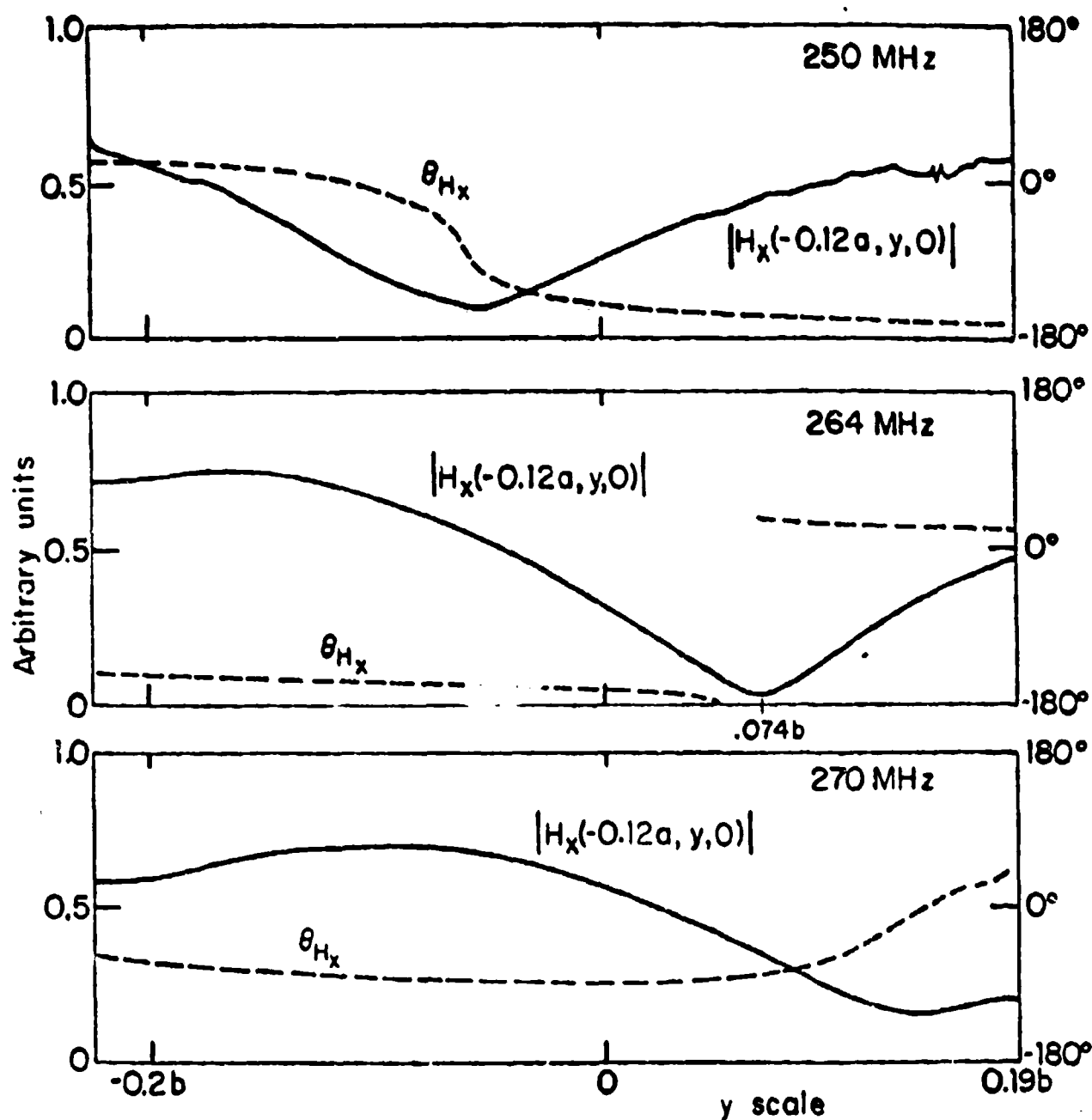


Fig 33 Measured magnitude and phase of the transverse component of the magnetic field on the ground plane in the working volume, width $2a = 175\text{cm}$, length $b = 114.8\text{cm}$, height $h = 75\text{cm}$.

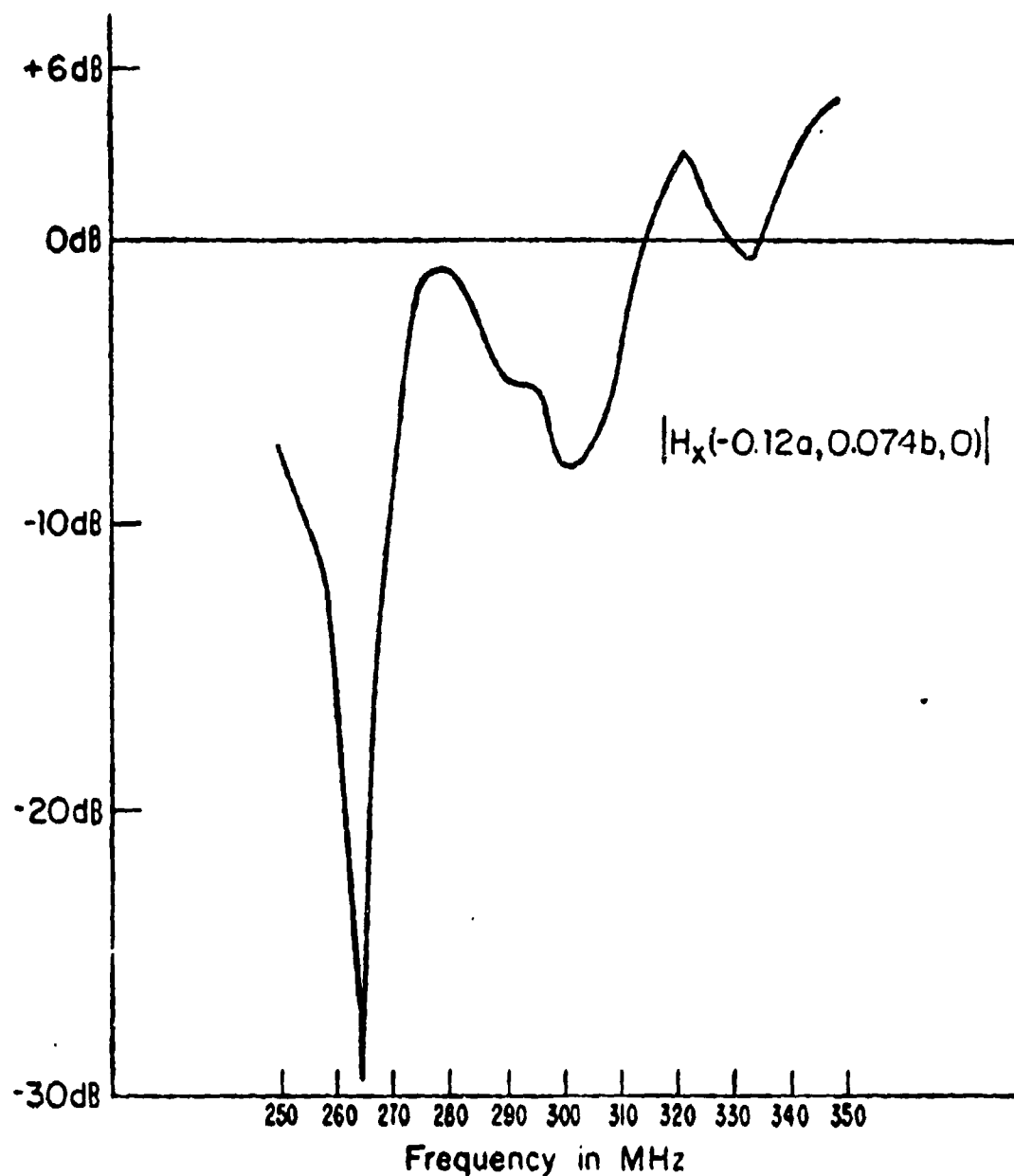


Fig. 34 Measured magnitude of the transverse magnetic field at a fixed position in the working volume as a function of frequency; $2a = 175$ cm, $b = 114.8$ cm, $h = 75$ cm, $p_f = 40$ W

maxima and minima in Figure 34 are a consequence of the standing waves generated in the working volume by reflections of the field at the ends $y = \pm b/2$ and the adjacent tapered sections. The standing-wave ratio varies somewhat with frequency so that the minimum amplitude at any fixed point increases and decreases with frequency. The deepest minimum at $y = 8.5$ cm occurs at $f = 264$ MHz. At another location of the probe, the frequency for and the depth of the minimum will be different.

The differences between the actual electromagnetic field in the working volume of the model simulator and a traveling plane wave are significant when $h = 108$ cm $= 2.25\lambda$ with $f = 626.5$ MHz, and considerably larger when $h = 75$ cm $= 0.66\lambda$ with $f = 264$ MHz. In the first place, the component E_z of the electric field is not uniform in either the transverse or vertical directions; secondly, there is a component E_y ; and thirdly, there is a significant standing wave. It follows that the electrical environment of a metallic obstacle placed in the working volume is necessarily quite different from what it would be if it were exposed to an incident plane wave. Therefore, it must be expected that currents and charges induced on the surface of an obstacle may also be quite different. A detailed comparison of the distributions of induced currents and charges on obstacles when in the simulator and when exposed to a plane wave is not yet available. However, a sample set of measurements has been made of the very sensitive charge density distribution on the surface of a tubular cylinder with electrical length $kh = 3.5\pi$ and electrical radius $ka = 1$ when located at the center of the parallel-plate section of the Harvard simulator with $h = 108$ cm and $f = 626.5$ MHz. This means that the axis of the cylinder is at a distance of 7.7λ from the source. Available from earlier measurements at the same frequency are the distributions of charge density along the same cylinder when illuminated by an incident spherical wave from a monopole at a distance of 7.5λ over an open ground plane. Theoretically determined distributions (ref. 8) are also available. The measured magnitudes of the charge density η are shown in Figure 35 for the simulator, in Figure 36 for the incident spherical wave. The theoretical distributions for an incident plane wave are in Figure 37. A comparison of the three figures shows that the general standing-wave nature of the distributions in both the longitudinal and transverse directions are comparable, but with significant differences in detail. These are most apparent in the relative magnitudes of the three standing-wave

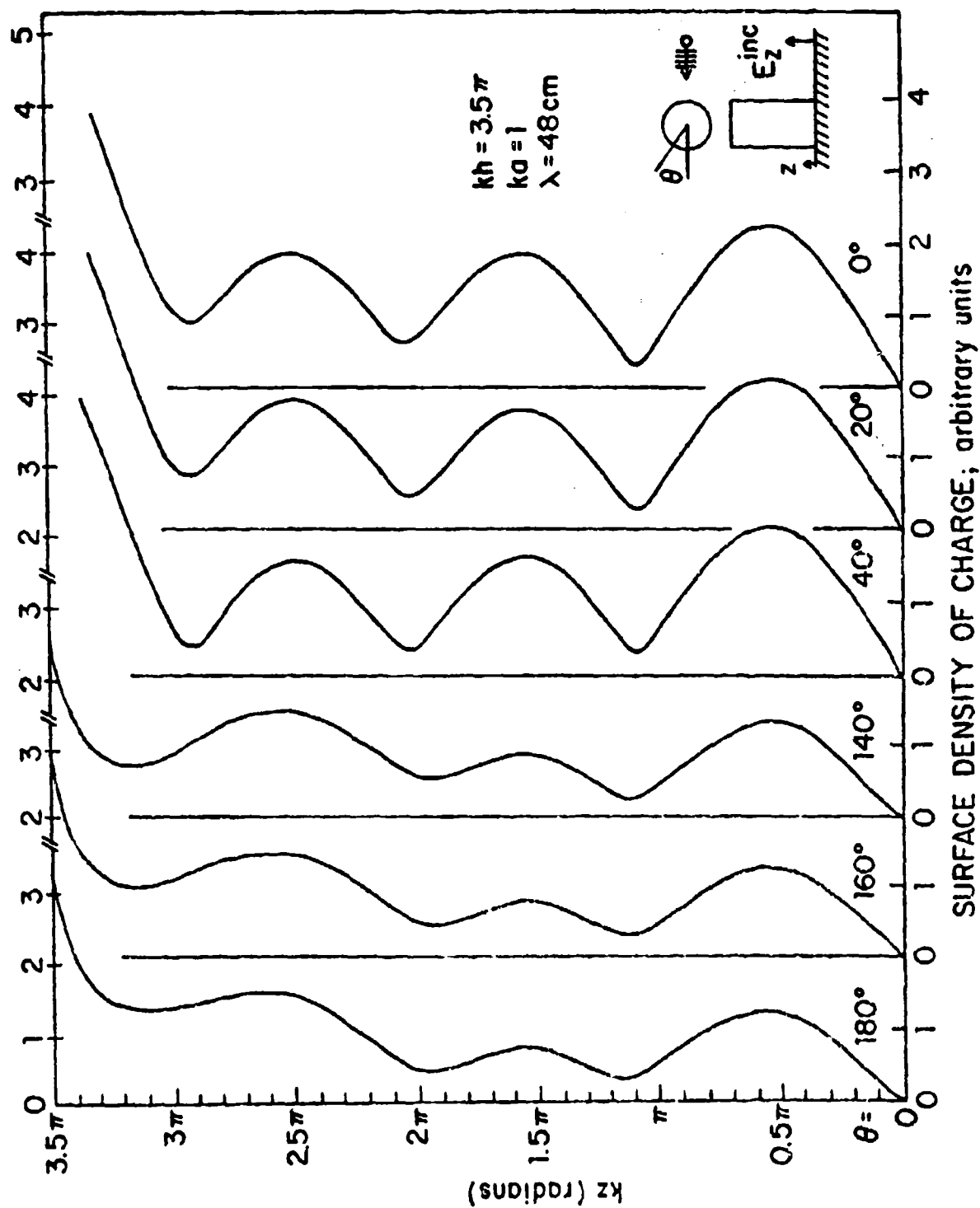


FIG. 35 MEASURED SURFACE DENSITY OF CHARGE ON TUBULAR CYLINDER IN SIMULATOR

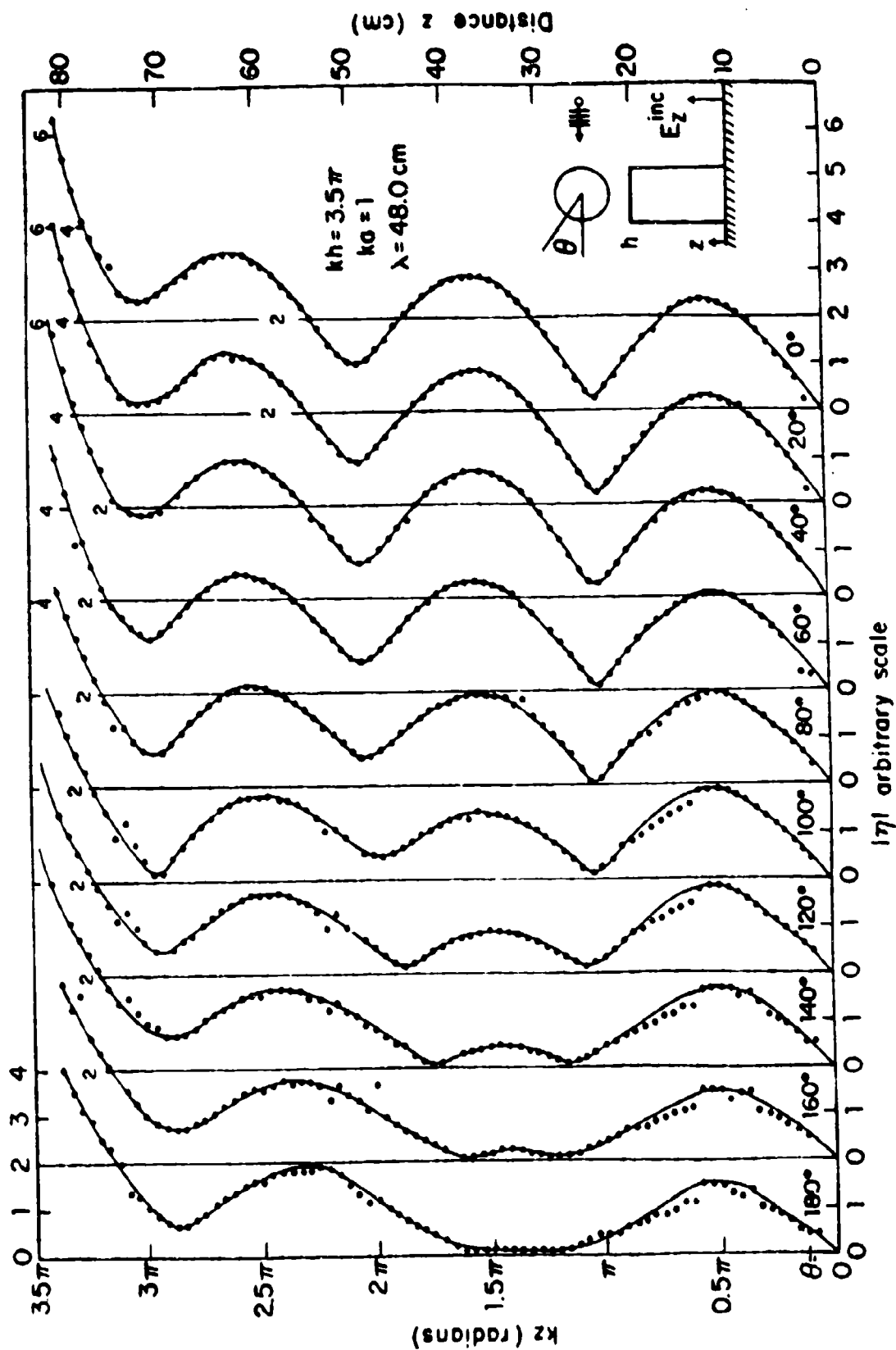


Fig. 36 Measured magnitude of surface density of outside charge on tubular cylinder; E-polarization, normal incidence.

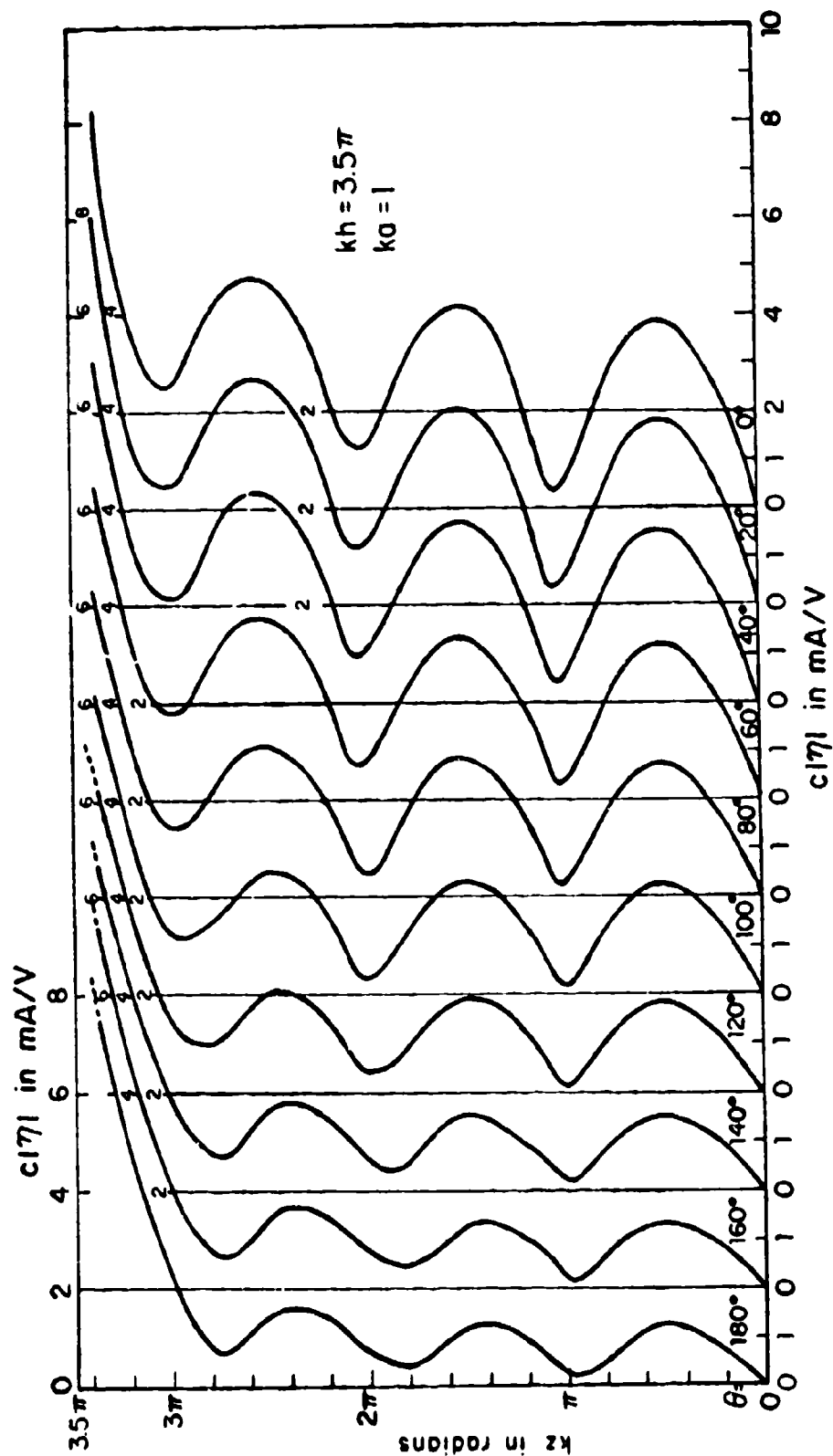


Fig. 37 Theoretical magnitude of surface density of outside charge on tubular cylinder; E-polarization, normal incidence.

maxima which occur near $kz = \pi/2, 3\pi/2$, and $5\pi/2$. These are listed side by side in Table 2 for ready quantitative evaluation. Thus, on the illuminated side ($\theta = 180^\circ$) the theoretical curve has maxima that increase from the ground plane ($z = 0$) upward in the proportions 1.00 : 1.04 : 1.27; the measured values for the simulator are 1.00 : 0.63 : 1.29; and those for the spherical wave are 1.00 : 0.08 : 1.23. Evidently, the second maximum is substantially lower in the simulator and almost completely absent with the spherical wave. It has been shown (ref. 8) that the virtual disappearance of the second maximum with an incident spherical wave is due to the presence of a component of the electric field perpendicular to the surface of the cylinder when the incident wave form is spherical instead of planar. The amplitude and phase relations are such that the second maximum is greatly reduced, the first and third somewhat increased. When the cylinder is in the simulator, the second maximum is reduced but much less than with the spherical wave. This is readily understood since the incident field in the simulator is a spherical wave modified by reflections from the top plate which act to reduce the curvature of the spherical wave.

On the shadowed side ($\theta = 0^\circ$), the ratio of maxima (normalized to the first maximum at $\theta = 180^\circ$) are for the plane wave 3.03 : 3.25 : 3.70; for the simulator 1.71 : 1.47 : 1.50; and for the spherical wave 1.61 : 1.97 : 2.23. Thus, both measured sets have substantially lower charge maxima in the shadow region than required by plane-wave theory. The maxima for the cylinder in the simulator decrease from the ground plane upward, those for the spherical wave and the plane wave increase substantially. Since the distributions on the shadowed side of the cylinder involve the excitation of the entire cylinder with rotational and axial resonance effects both active, it appears that the overall effect of the field in the simulator in inducing charges is less like that of a plane wave than that of the traveling spherical wave. This may be a consequence of the longitudinal standing waves in the simulator, although these have a standing-wave ratio of less than 2 when $h = 2.25\lambda$.

In the absence of more complete information on more complicated obstacles and especially those that have greater lateral dimensions, general conclusions about the adequacy of the field in the simulator are not possible. However, the measured data on an electrically long and thick cylinder do indicate

TABLE 2

RELATIVE MAXIMA OF CHARGE DENSITY ON CYLINDER WITH $ka = 1$, $kh = 3.5\pi$

THEORY FOR PLANE WAVE; MEASURED IN SIMULATOR; MEASURED WITH SPHERICAL WAVE

Max. Near kz =	Illuminated Side						Shadowed Side					
	$\theta = 180^\circ$						40°					
	Theory	Simul.	Spher.	Theory	Simul.	Spher.	Theory	Simul.	Spher.	Theory	Simul.	Spher.
2.5π	1.27	1.29	1.23	1.38	1.19	1.12	3.40	1.32	1.97	3.70	1.50	2.23
1.5π	1.04	0.63	0.08	1.23	0.73	0.31	2.90	1.32	1.80	3.25	1.47	1.97
0.5π	1.00	1.00	1.00	1.18	1.08	1.12	2.77	1.64	1.50	3.03	1.71	1.61

that the field in the simulator is sufficiently like that of a plane wave to produce the same general pattern of three-dimensional standing waves of charge density. The relative maxima and minima are observed substantially at the same locations as for a plane wave. However, the relative amplitudes of the individual maxima range from very close agreement to differences by factors up to 2.5. Extensive measurements on electrically thick cylinders have indicated that the distribution of the induced surface density of charge is more sensitive to the nature of the incident wave front than is the distribution of the induced surface density of current.

SECTION X

POSSIBLE METHODS TO IMPROVE THE FIELD IN THE SIMULATOR AS AN APPROXIMATION OF A TRAVELING PLANE WAVE

The lateral and vertical nonuniformity of the field in the simulator on the one hand and the existence of standing waves on the other hand constitute the principal departures from the desired traveling plane wave. Of these the first is a consequence of the spherical wave fronts that are incident on the parallel-plate section, the second is due to reflections at and beyond the junction of the parallel-plate region and the tapered section leading to the terminating impedance.

It might be supposed that the nonuniformity in the transverse distribution of the electric field is a problem only at high frequencies when modes other than the TEM can propagate in the parallel-plate section. The cut-off wavelength for the TM_{01} mode is $\lambda_{c1} = 2h$ so that at all wavelengths longer than $2h$, only the TEM mode can propagate. However, with the length b (≈ 115 cm) of the parallel-plate section substantially less than $2h$ (≈ 216 cm or 150 cm) and therefore less than λ when this is greater than $2h$, even nonpropagating modes may have significant amplitudes in the electrically rather short parallel-plate section. The obvious way to reduce the transverse variation in E_z in the parallel-plate section is to provide an incident field that more nearly approximates a plane wave than does the actual spherical wave. With the geometry of the input structure predetermined, this is not readily accomplished. It involves a modification of the phase velocity of the spherical wave in the tapered section from the generator by some kind of a collimating lens or its equivalent in the form of metal plates or corrugations on the ground plane so that the spherical wave front becomes more nearly planar as it reaches the parallel-plate section.

The existence of standing waves in the parallel-plate section is a consequence of the fact that the entire structure has the characteristics of a terminated transmission line only at low frequencies for which the condition $2\pi h/\lambda \ll 1$ is satisfied. This condition underlies the theory of all open transmission lines. It requires that radiation be negligible in determining the characteristics of the line. When it is satisfied, it is possible to design the transmission line so that virtually all of the power

supplied by the generator is transmitted along it to a matched load at the end. As the height h is increased, radiation becomes significant and, for sufficiently large values of h , dominant. The structure then acts like a traveling-wave antenna. Since the standing-wave ratio in the parallel-plate section is reasonably constant (see Figure 13), it is evident that the effective load on the open parallel-plate waveguide is at or beyond its junction with the sloping triangular plate at the load end. That is, most of the radiation takes place during reflection at or beyond the discontinuity formed by this sharp junction. (It is to be expected that radiation also takes place at the junction of the sloping triangular plate with the parallel plate at the generator end, but this does not affect the standing-wave ratio in the parallel-plate region.)

It is seen from Figure 23 that the amplitudes of the TEM and TM_{01} modes are about equal and those of the TM_{02} and TM_{03} modes negligible when $h = 2.25\lambda = 108$ cm with $f = 626.5$ MHz. In this case, the standing-wave ratio as obtained from Figure 13 is less than 2. On the other hand, Figure 27 shows that the amplitude of the TEM mode greatly exceeds that of the TM_{01} mode when $h = 0.66\lambda = 75$ cm with $f = 264$ MHz, and that in this case the standing-wave ratio is about 3. It, thus, appears that the standing-wave ratio in the working volume can be reduced significantly only by reducing the reflection at $y \geq b/2$ of the entire component E_z of the electric field between the parallel plates. The selective reduction of the TM_{0n} modes by attenuating E_y , even if 100% successful, would not significantly reduce the standing-wave ratio when it is greatest. There is no comparable way to attenuate separately the TE_{0l} modes since they have only an E_z component of the electric field. What is required to reduce the standing-wave ratio is a more frequency-independent termination for the parallel-plate section of the simulator than is provided by the sloping triangular plate with its resistive termination that is frequency independent only at sufficiently low frequencies. This is important primarily in the intermediate range of frequencies when h is of the order of a wavelength, and the standing-wave ratio is highest.

Recent measurements have shown that the very high standing-wave ratio shown in Figure 33 for the magnetic field at $f = 264$ MHz is reduced from about 20 to near 2 when the terminating resistance of the simulator is

greatly increased from the characteristic resistance of 80 ohms to between 600 and 800 ohms. It is to be anticipated that this change must increase the standing-wave ratio at very low frequencies, at which the simulator behaves like a nonradiating transmission line rather than like an antenna. Measurements at lower frequencies to verify this must be made. A systematic study is then in order to determine the optimum termination from the point of view of the entire frequency spectrum involved.

REFERENCES

1. Soohoo, K. M., "Numerical Analysis of a Transmission-Line EMP Simulator," Sensor and Simulation Note 209, 1974.
2. Dudley, D. G., and Quintenz, J. P., "Multi-Modal Transient Excitation Effects in an Infinite Parallel-Plate Waveguide," Canadian Jour. Physics, 50, pp. 2826-2835, 1972.
3. Rushdi, A. M., Mendez, R. C., Mittra, R., and Lee, S. W., "Leaky Modes in Parallel-Plate EMP Simulators," IEEE Trans. Electromagn. Compatib., EMC-20, pp. 443-453, 1978.
4. Marin, L., "Modes on a Finite Width, Parallel-Plate Simulator, I. Narrow Plates," Sensor and Simulation Note 201, 1974.
5. Marin, L., "Modes on a Finite Width, Parallel-Plate Simulator, II. Wide Plates," Sensor and Simulation Note 223, 1977; Revised, November 1977.
6. Marin, L., and Lewis, Jr., G. C., "Modes on a Finite Width, Parallel-Plate Simulator, III. Numerical Results for Modes on Wide Plates," Sensor and Simulation Note 227, 1977.
7. Marcuvitz, N., Wave Guide Handbook, McGraw-Hill Book Co., New York, 1951, p. 64.
8. Burton, R. W., King, R. W. P., and Blejer, D. J., "Surface Currents and Charges on an Electrically Thick and Long Conducting Tube in E- and H-Polarized, Normally Incident, Plane-Wave Fields," Radio Science, 13, pp. 75-91, 1978, Figure 16.

LIST OF PERSONNEL WHO PARTICIPATED IN RESEARCH

Professor Tai Tsun Wu, Principal Investigator
Professor Max Krook, Co-Principal Investigator
Professor Ronold W. P. King, Emeritus, Senior Scientist
Dr. Tapan K. Sarkar, Post-Doctoral Research Fellow
Mr. Dennis J. Blejer, Research Technician
Mr. S.-K. Wan, Research Technician
Mr. Mark J. Miller, Research Technician
Mr. J. E. Baum, Research Technician
Ms. M. Owens, Staff Assistant
Ms. B. H. Sandler, Programmer & Mathematician

LIST OF PUBLICATIONS

Papers to be Published:

"The Electromagnetic Field in an EMP Simulator at a High Frequency," by R. W. P. King and D. J. Blejer, scheduled to appear in IEEE Trans. on Electromagn. Compatibility, August 1979.

"Surface Currents and Charges on a Cross Formed by an Electrically Thick Cylinder and a Flat Plate in a Normally Incident, Plane-Wave Field," by R. W. P. King, D. J. Blejer, and R. W. Burton, scheduled to appear in Radio Science, September-October 1979.

"Current Induced on Single and Crossed Electrically Short and Thin Tubular Cylinders by a Normally Incident, Plane Electromagnetic Wave," by R. W. P. King, D. J. Blejer, and B. H. Sandler, scheduled to appear in the IEEE Transactions on Antennas and Propagation, September 1979.

Talks Presented:

"Current Induced on Single and Crossed Electrically Short and Thin Tubes by a Normally Incident, Plane Electromagnetic Wave," by R. W. P. King, D. J. Blejer, and B. H. Sandler, presented at the 1978 USNC/URSI Meeting, held at the University of Maryland, College Park, May 15-19, 1978.

"Measured Electric Fields in a Model Simulator," by D. J. Blejer and R. W. P. King, presented at the 1978 Nuclear EMP Meeting, held at the University of New Mexico, Albuquerque, June 6-8, 1978.

Interim Reports Issued:

"Currents and Charges on Cylinders in a Parallel-Plate Transmission Line: Description of Experimental Setup and Sample Measurements," by T. T. Wu, R. W. P. King, D. J. Blejer, and S.-K. Wan, AFOSR-76-3073 Annual Report, July 31, 1977.

"Electric Field in a Parallel-Plate EMP Simulator: Theoretical and Experimental Results," by M. Krook, R. W. P. King, D. J. Blejer, T. K. Sarkar, S.-K. Wan, AFOSR-76-3073 Annual Report, July 31, 1978.