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TECHNICAL REPORT RL-80-1

**STRESS INTENSITIES AROUND  
TRANSVERSE SURFACE FLAWS IN  
CYLINDRICAL SHELLS BY PHOTOELASTIC  
STRESS FREEZING**

John A. Schaeffel, Jr.  
✓ Ground Equipment and Missile Structures Directorate  
US Army Missile Laboratory

1 October 1979

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**U.S. ARMY MISSILE COMMAND**

**Redstone Arsenal, Alabama 35809**

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| 20. ABSTRACT (Continue on reverse side if necessary and identify by block number)<br>This report documents a set of seven tests for the determination of $K_I$ stress intensity factors for isotropic cylinders with transverse part-circular cracks loaded in combined uniaxial extension and internal pressure. Part-circular cracks were machined into birefringent Hysol CP5-4290 photoelastic cylinders. The cylinders were then subjected to combined loading while in a stress freezing cycle. Slices of the cracks were made at various angles and analyzed with a photoelastic polariscope. A least-squares curve fit of the photoelastic data was used to generate $K_I$ stress intensity factors. |                                                        |                                                                                                                                           |

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26.  $K_I$  data are plotted versus slice angle into the crack for various crack parameters. The results of the tests were compared with the results of previous tests in which the cylinders were loaded in either pure uniaxial tension or internal pressure.

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## I. INTRODUCTION

This work is a continuation of the efforts of Mullinix and Smith [1] and Vandiver et al. [2]. Their work involved the determination of stress intensity factors for homogeneous cylinders loaded under one of three conditions: internal pressure, bending, extension and having part circular longitudinal or transverse cracks in the outer wall. The present work considers the problem of finding stress intensity factors under the combined loading action of internal pressurization and extension. Transverse flaws in cylinders were considered for this effort.

Although flaws on the surface of cylinders usually occur as semi-elliptical in shape, the flaws in this work had to be made mechanically. This was accomplished by cutting part-circular flaws with circular saw blades to simulate an elliptical crack. The approximation has been made before and does not appear to offer any serious error. In this effort the assumed stress field at the crack tip border is defined as a 50-50 stress mixture derived from internal cylinder pressurization and extensional loading. Fifty percent of the applied stress was obtained from internal pressurization while the remaining fifty percent was obtained from extension.

## II. THEORY

The geometry for the part-circular transverse flaw may be described by the intersection of a circular element representing the flaw boundary with a hollow cylinder. *Figures 1 and 2* illustrate this geometry. For the opening mode of deformation, the stress distribution near the part-circular crack and in a plane perpendicular to the crackfront is given as [3,4,5]

$$\begin{aligned}\sigma_n &= \frac{K_I}{(2\pi r)^{1/2}} \cos \frac{\psi}{2} \left\{ 1 - \sin \frac{\psi}{2} \sin \frac{3\psi}{2} \right\} \\ \sigma_y &= \frac{K_I}{(2\pi r)^{1/2}} \cos \frac{\psi}{2} \left\{ 1 + \sin \frac{\psi}{2} \sin \frac{3\psi}{2} \right\} \\ \tau_{ny} &= \frac{K_I}{(2\pi r)^{1/2}} \sin \frac{\psi}{2} \cos \frac{\psi}{2} \cos \frac{3\psi}{2}\end{aligned}\tag{1}$$

In Equation (1),  $K_I$  is the stress intensity factor and the coordinates for the crack border are shown in *Figure 3*. The effect on the stress field of the crack border curvature as well as the

location and shape of other boundaries is reflected in the magnitude of  $K_I$ , the stress intensity factor. It is assumed that the stresses singular in  $r$  are much larger than terms regular in  $r$  very near the crack tip. Since experimental measurements must be made away from the crack tip where regular terms may make a significant contribution to the total stress field then another way of determining  $K_I$  must be found. Irwin [6] developed an approximation for the regular terms by assuming a uniform stress field,  $\sigma_{on}$ , was superimposed at the crack tip and parallel to the crack plane. With his approximation the local stress field is given as

$$\begin{aligned}\sigma_n &= \frac{K_I}{(2\pi r)^{1/2}} \cos \frac{\psi}{2} \left\{ 1 - \sin \frac{\psi}{2} \sin \frac{3\psi}{2} \right\} - \sigma_{on} \\ \sigma_y &= \frac{K_I}{(2\pi r)^{1/2}} \cos \frac{\psi}{2} \left\{ 1 + \sin \frac{\psi}{2} \sin \frac{3\psi}{2} \right\} \\ \tau_{ny} &= \frac{K_I}{(2\pi r)^{1/2}} \sin \frac{\psi}{2} \cos \frac{\psi}{2} \cos \frac{3\psi}{2}\end{aligned}\tag{2}$$

$\sigma_{on}$  does not affect the singular stress field but does alter the isochromatic fringe pattern which is proportional to the maximum in-plane shearing stress. The maximum shearing stress,  $\tau_{max}$ , is usually determined readily from photoelasticity.

From Irwin's stress equations, the maximum shearing stress in the plane perpendicular to the crack front, y-n, can be obtained from

$$\tau_{max}^2 = \frac{(\sigma_n - \sigma_y)^2}{2} + \tau_{ny}^2\tag{3}$$

as

$$\begin{aligned}\left\{ 2 \tau_{max} \right\}^2 &= \left\{ \frac{K_I}{(2\pi r)^{1/2}} \sin \psi + \sigma_{on} \sin \frac{3\psi}{2} \right\}^2 \\ &\quad + \left\{ \sigma_{on} \cos \frac{3\psi}{2} \right\}^2\end{aligned}\tag{4}$$

In photoelasticity, the maximum shearing stress from the stress optic law is

$$\tau_{\max} = \frac{fN}{2t} \quad (5)$$

where,

$t$   $\equiv$  thickness of the specimen measured parallel to the direction of light propagation.

$N$   $\equiv$  isochromatic fringe order.

$f$   $\equiv$  photoelastic fringe constant of the material.

In practice,  $\tau_{\max}$  is measured along the line  $\psi = \pi/2$  where the maximum shearing stress is known to be large. Simplification of Equation (4) with  $\psi = \pi/2$  results in the equation

$$4 \tau_{\max}^2 = \frac{K_I^2}{2\pi r} + \left\{ \frac{K_I}{(\pi r)^{1/2}} \right\} \sigma_{on} + \sigma_{on}^2 \quad (6)$$

Only the stress intensity factor  $K_I$  is used in fracture criteria. Smith et al. [7] found that by solving Equation (6) for  $\tau_{\max}$  and truncating the results to the same order in  $r$  as Equation (2) that

$$\tau_{\max} = \frac{K_I}{\sqrt{8\pi r}} + \sigma_{on} \quad (7)$$

If an apparent value of  $K$ ,  $K_{ap}$  is defined as,

$$K_{ap} = \sqrt{8\pi r} \tau_{\max} , \quad (8)$$

then Equation (7) can be written as

$$K_{ap} = K_I + \sqrt{8\pi r} \sigma_{on} \quad (9)$$

Equation (9) shows that in the region dominated by the singular stresses that there is a linear relationship between the apparent  $K$  and the square root of  $r$ . In determining  $K_I$ , the values of  $K_{ap}$  are plotted versus  $r^{1/2}$  for a photoelastic slice specimen. Data points which fall on a straight

line are selected while all others are rejected. A least-squares straight-line curve fit is then given to the selected points and the value of  $K_I$  is determined by taking the value of  $K_{ap}$  at  $r = 0$ , since  $K_{ap} = K_I$  at  $r = 0$ . *Figure 4* gives an example for a typical photoelastic slice specimen.

For clarity, the results of this experimental effort are compared with those of Reference [2]. To compute the overall stress level for experimentally subjecting a cylinder, Reference [5] was consulted. Thresher and Smith generated graphs of stress intensity factors for surface cracks in finite solids. Using their information along with the maximum allowable working stress in the photoelastic material a determination of  $\sigma_m$ , the nominal cylinder-wall stress, was made. From  $\sigma_m$ , the maximum working internal pressure  $P_i$  of the cylinder was obtained from

$$P_i = \frac{T}{R_c} \sigma_m \quad (10)$$

where

$T$  = Wall thickness of the cylinder.

$R_c$  = Radius of cylinder measured to the center of the cylinder wall.

For the case of pure internal pressure loading of a cylinder reported in [2],

$$P_i = 2 \frac{T}{R_c} \sigma_m \quad (11)$$

To compute the extensional loading  $P$  for the cylinder with a 50-50 stress mixture,

$$P = \frac{1}{2} \sigma_m A_c \quad (12)$$

while for the case reported for pure extensional loading in [2],

$$P = \sigma_m A_c \quad (13)$$

All stress levels were comparable since their ultimate determination was from the same source, Thresher and Smith [5].

### III. EXPERIMENTATION

The determination of stress intensity factors for cylinders loaded in internal pressure and extension followed the work given in References [1] and [2] which used three dimensional

photoelasticity. A series of seven combined loading tests were performed. The photoelastic material, Hysol CP5-4290, was cast by the Hysol Corporation, Olean, New York, and used in the experimentation. The cylinders are nominally 5.875 inch in outside diameter with a 0.75-inch wall thickness. All the specimens had flaws oriented transverse to the cylinder axis. These flaws were machined with a circular saw blade 0.006-inch thick. Blade radii of 0.875 and 1.500 inch were used to produce flaws of two different sizes.

For the seven tests, the internal pressure and extension loads were determined using Equations (10) and (12). *Figure 5* illustrates the apparatus for generating the internal gas pressure and extensional loading. The uniform tension load was supplied by hanging dead weights on the cylinder. The internal pressure load was supplied by compressed air passing through a regulator. The gas pressure was measured by a Mercury manometer.

After the surface flaw was machined, the cylinder was annealed by thermal soaking at 280 degrees Fahrenheit for six hours followed by cooling at the rate of one degree Fahrenheit per hour. The stress freezing of the models was accomplished using the same thermal cycle as for annealing except under loading conditions. After the stress freezing cycle, slices perpendicular to the crack border were removed from the model by means of band saw. *Figure 6* illustrates a few of the various angles at which slices were taken. The number of slices varied from test to test depending on the flaw size. Each slice was polished with sandpaper. The CP5-4290 material's fringe constant was obtained from previous beam tests.

To improve resolution for analysis, slices were placed in an oil bath consisting of 75.5 percent by volume of Halowax oil and 24.5 percent mineral oil. Since the indices of refraction of the oil and CP5-4290 were the same, light scatter was minimized. The slices were observed in a comparator polariscope at 10X magnification.

By means of an XY-table on the polariscope, points on the slices could be located to within  $\pm 0.0001$  inch. Fractional fringe orders were obtained using Tardy compensation.

#### IV. RESULTS AND DISCUSSION

The specimen test parameters and dimensions for the combined uniaxial tension and internal pressure loading tests are indicated in *Table 3*. *Tables 1* and *2* were reproduced from Reference [2] for comparison purposes and are for the separate loading cases. *Figures 7-10* are graphs of the non-dimensional stress intensity factor versus slice angle for transverse flawed cylinders loaded either in uniaxial tension or internal pressure. *Figures 11-17* are graphs of the non-dimensional stress intensity factor versus slice angle for transverse flawed cylinders

loaded in combined uniaxial tension and internal pressure. The combined loading case data compares favorably with the separate uniaxial and internal pressure load cases. In general, the data follows the same experimental trends and the stress intensity factors obtained for the combined loading case falls within the range of the individual load cases.

## V. SUMMARY AND CONCLUSIONS

A series of seven separate tests were conducted in which part circular flaws simulating natural elliptical cracks were machined into Hysol CP5-4290 cylinders. The cylinders were subjected to combined internal pressure and uniaxial tension loading. A photoelastic stress freezing cycle was conducted for each cylinder. Following the stress freezing cycle each cylinder was sliced and analyzed using a polariscope with Tardy compensation. The stress intensity factors were shown plotted versus slice angle and were compared with a previous set of tests reported in Reference [2]. The results indicate that the more complicated combined loading case produces results comparable to the separate loading cases. It appears that linear superposition of solutions for each stress intensity factor case (i.e., uniaxial loading or internal pressure loading) is valid.

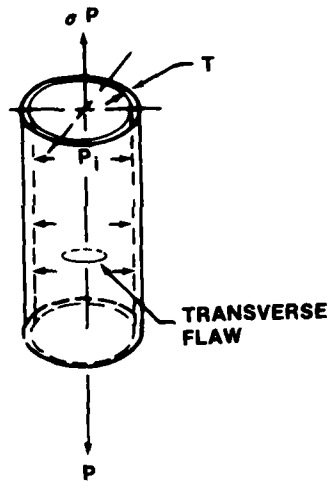


Figure 1. Transverse flaw loading geometry for a hollow cylinder.

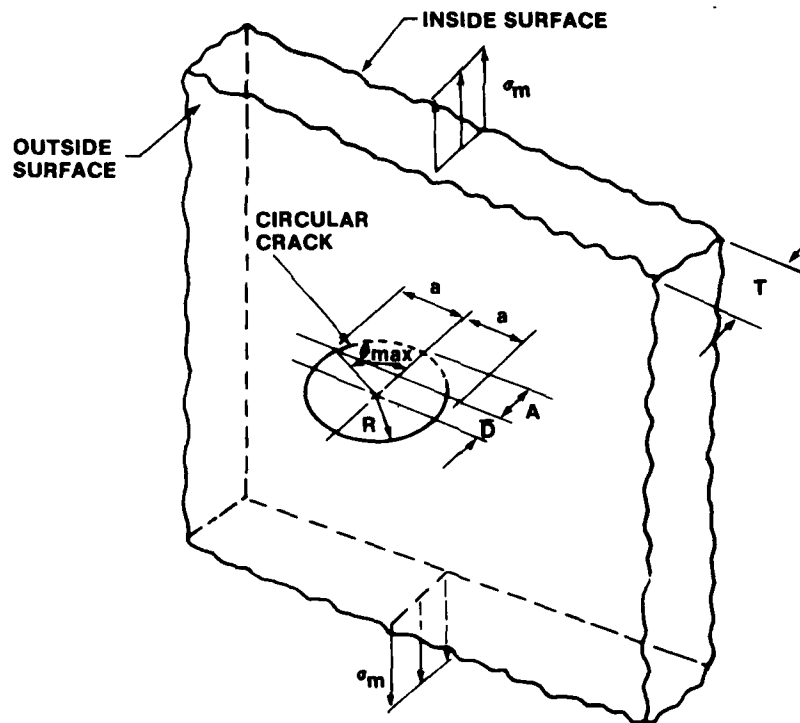


Figure 2. Notation for the part-circular surface flaw.

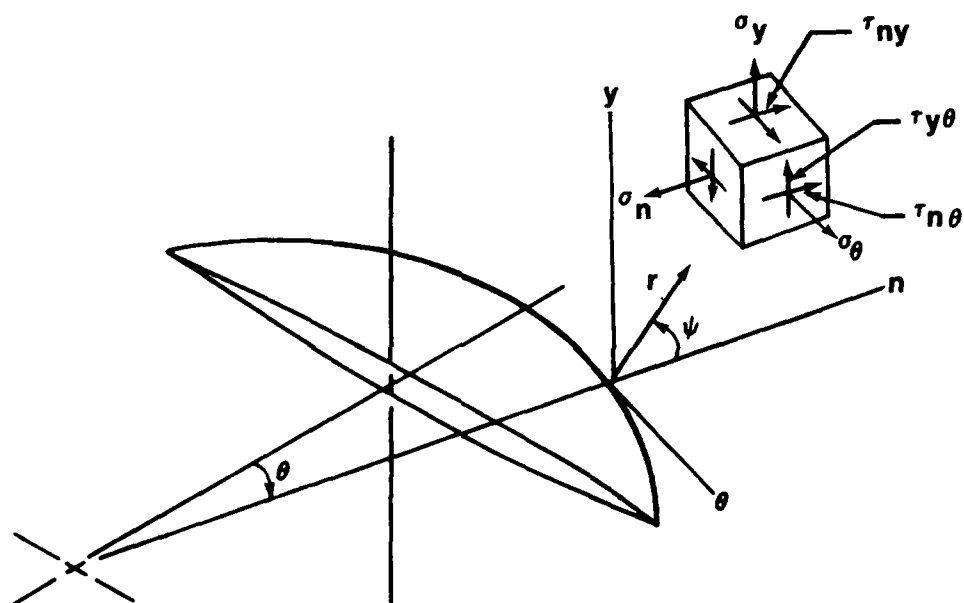


Figure 3. Sketch of crack-tip coordinates.

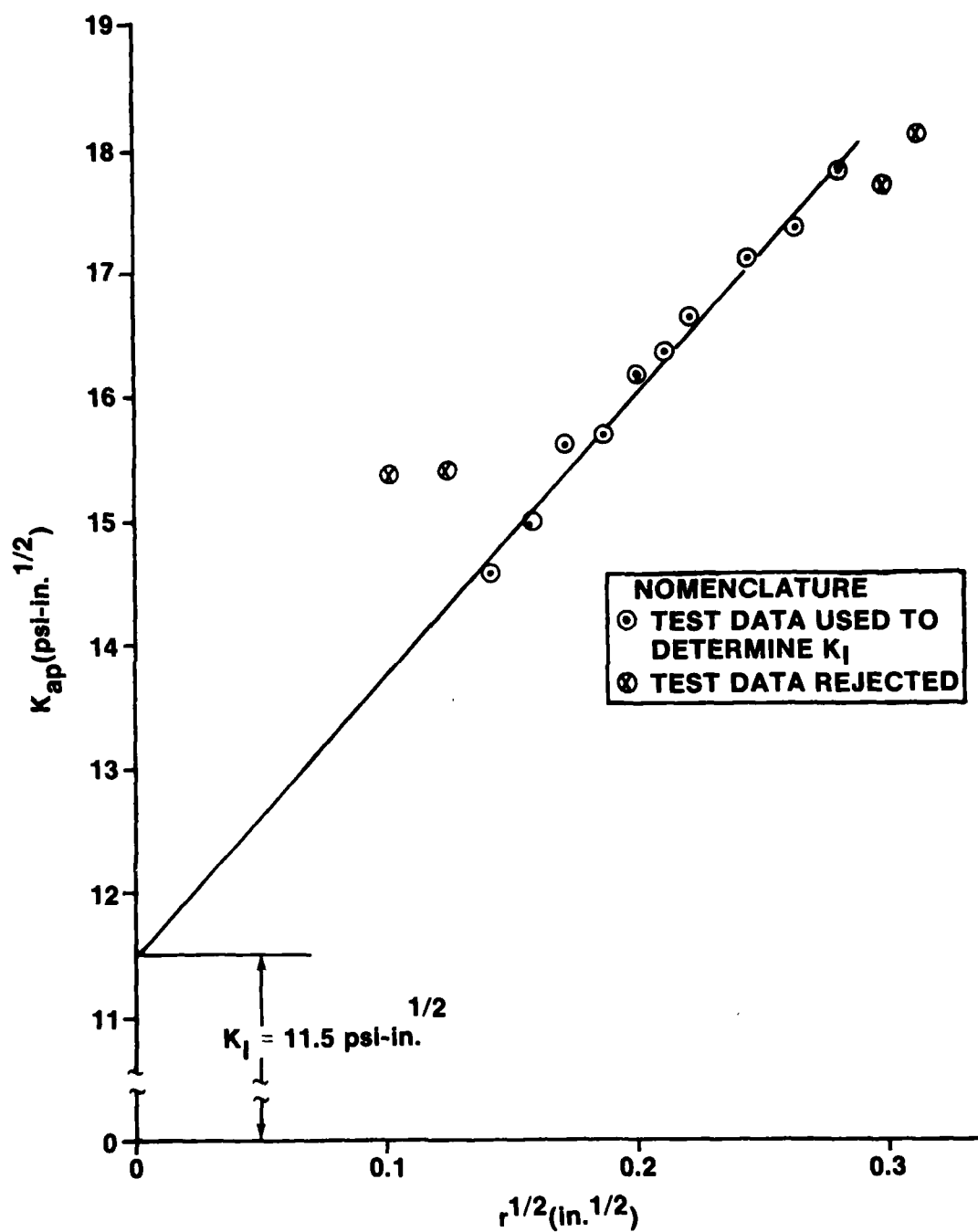


Figure 4. Typical set of slice data, illustrating the determination of  $K_I$ .

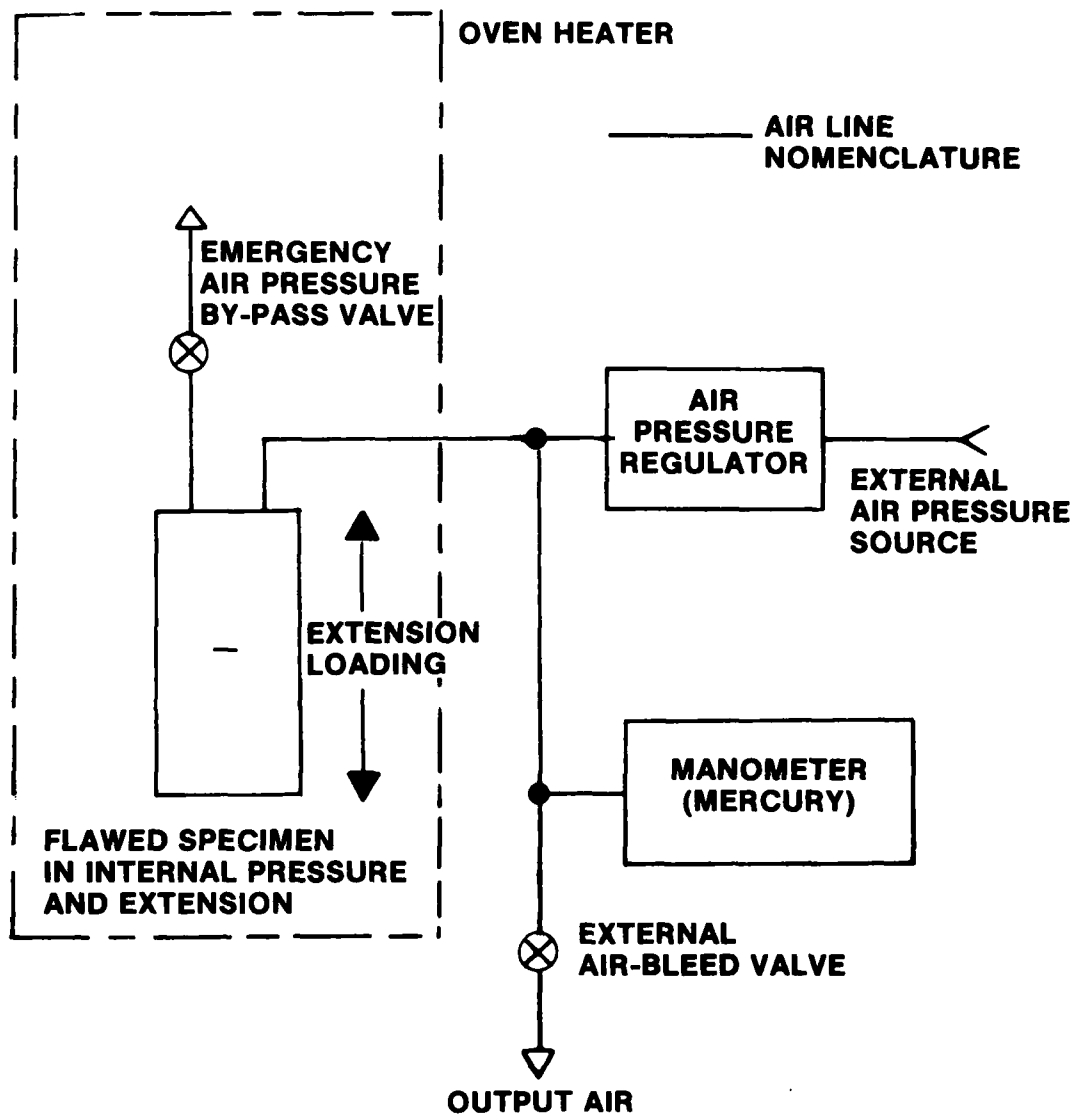


Figure 5. Schematic configuration for internal pressure and/or extension loading of cylinders.



**CIRCUMFERENTIAL FLAWS IN EXTENSION**  
(R = 0.875 INCH)

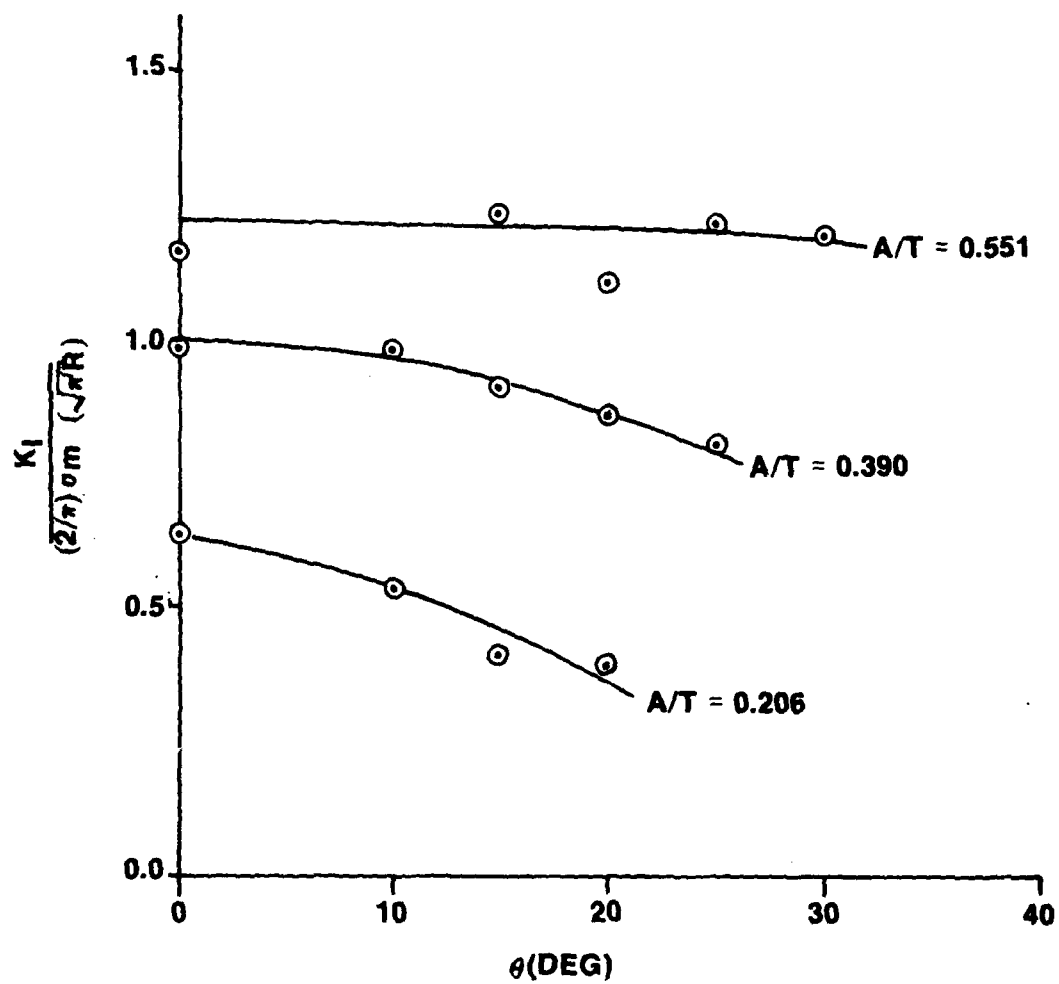


Figure 7. Stress intensity factor versus  $\theta$  for the transversely-flawed cylinder loaded in uniaxial tension (R = 0.875 inch).

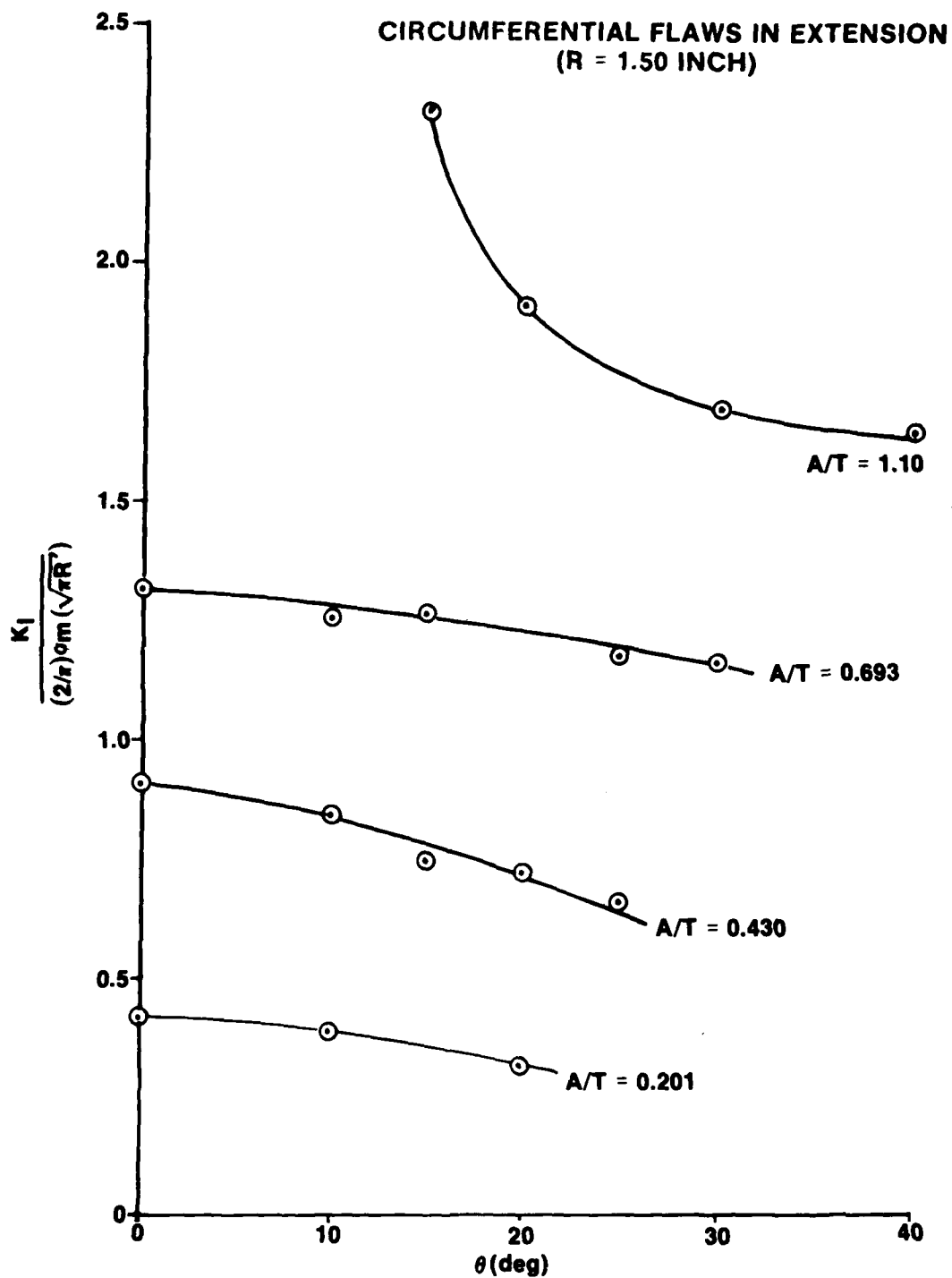


Figure 8. Stress intensity factor versus  $\theta$  for the transversely-flawed cylinder loaded in uniaxial tension (R = 1.500 inch).

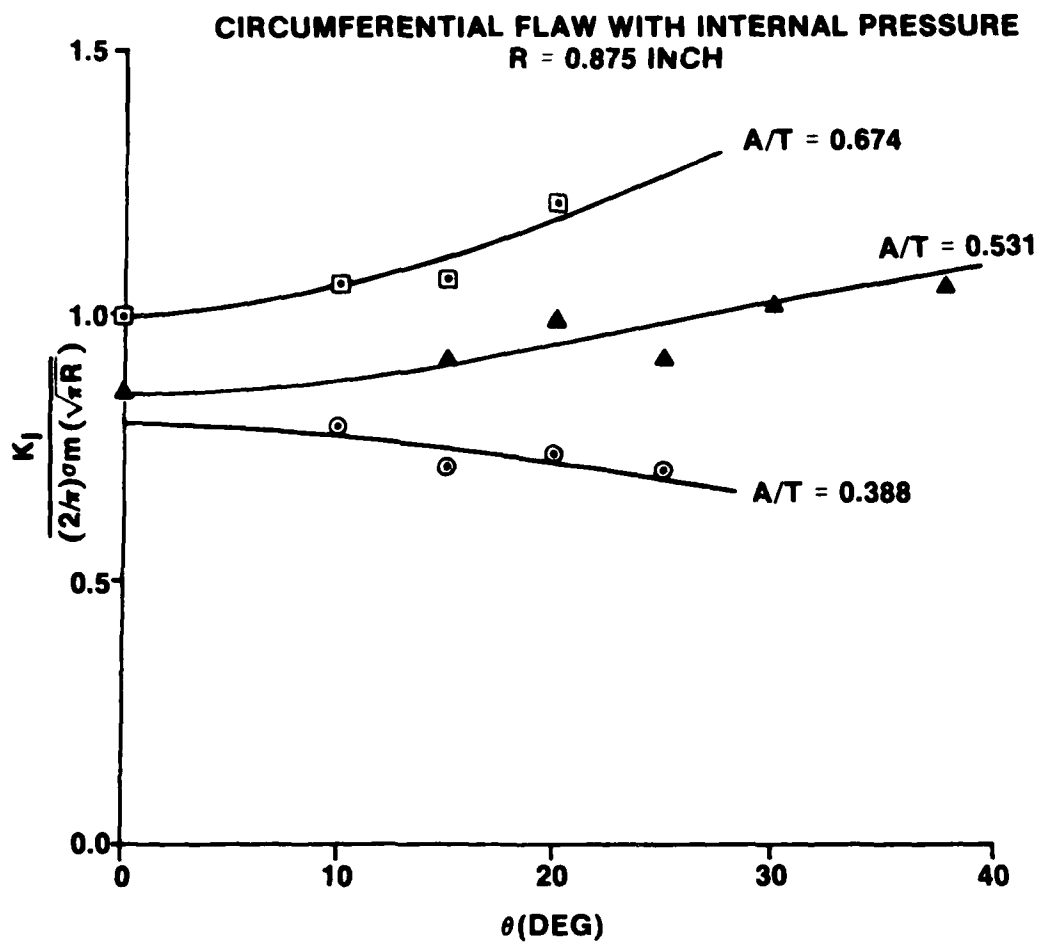
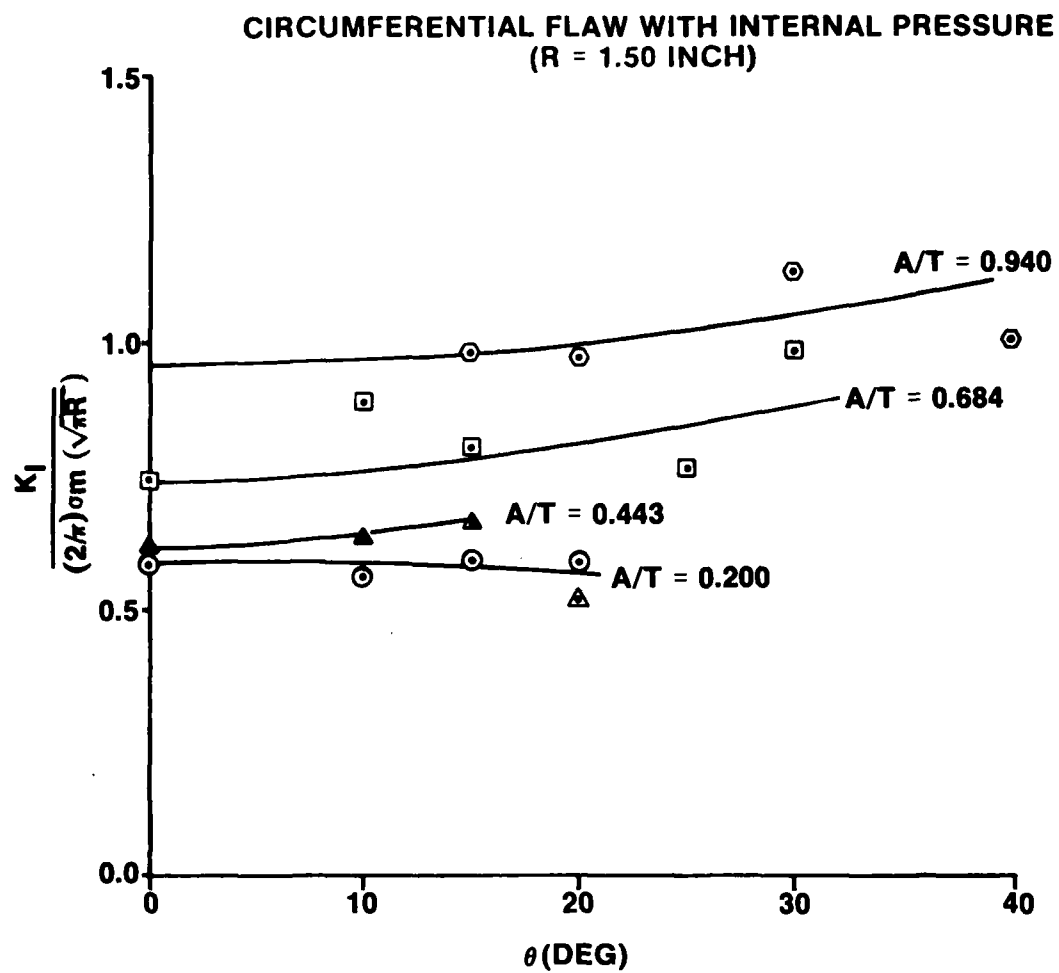
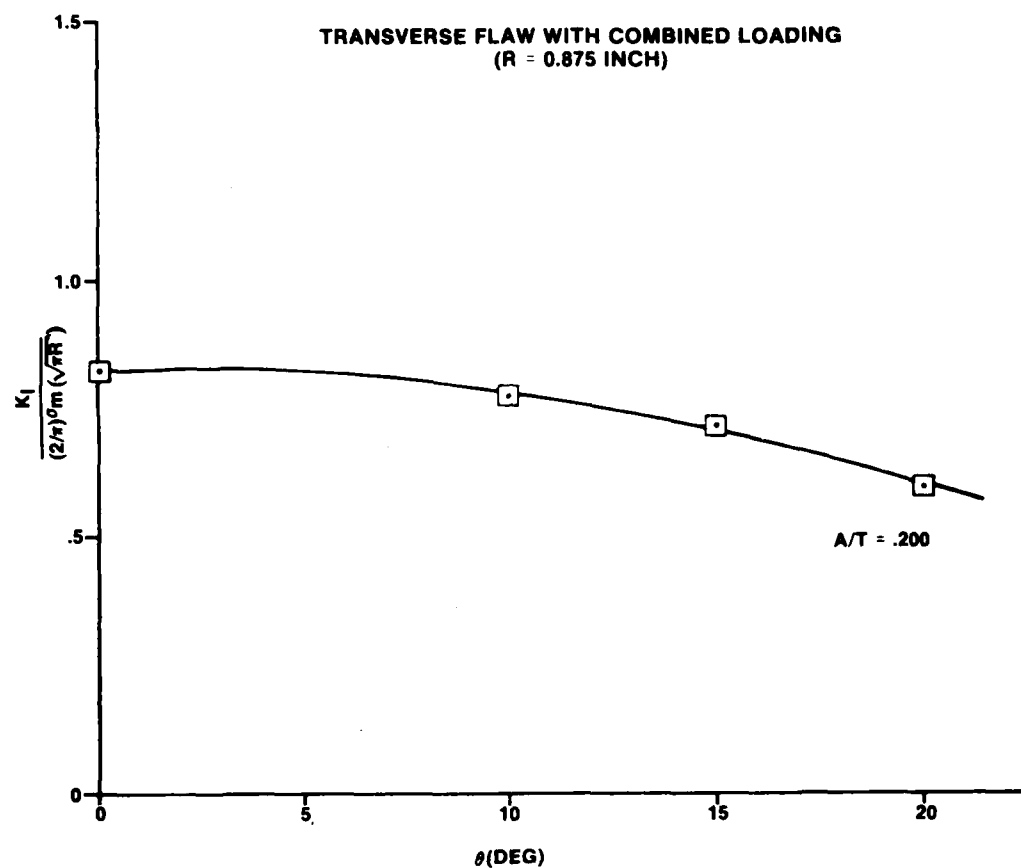


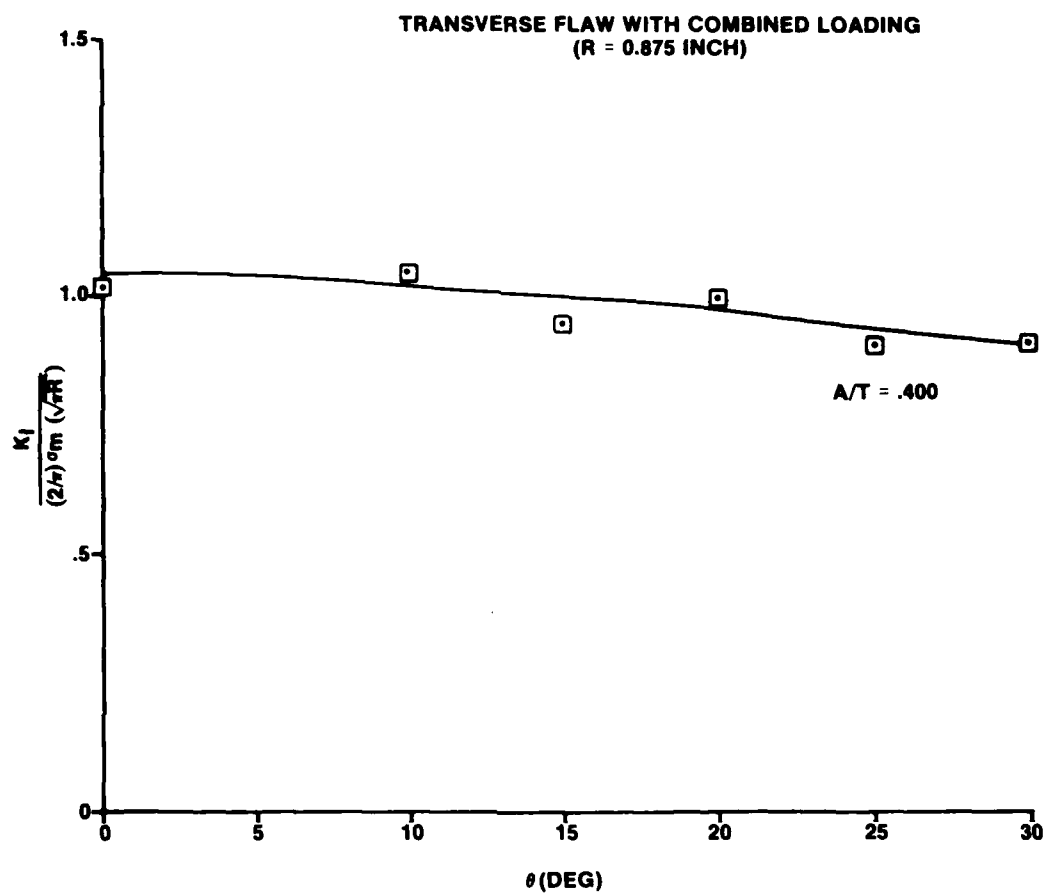
Figure 9. Stress intensity factor versus  $\theta$  for the transversely-flawed cylinder loaded with internal pressure (R = 0.875 inch).



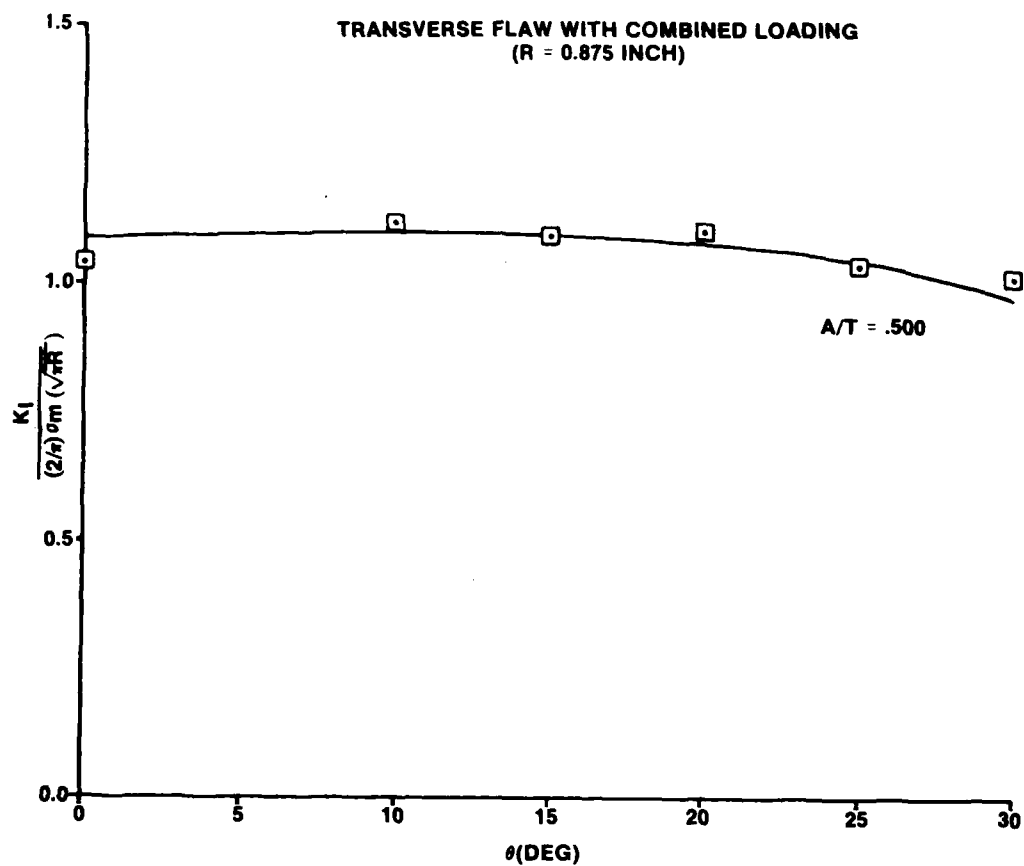
**Figure 10. Stress intensity factor versus  $\theta$  for the transversely-flawed cylinder loaded with internal pressure (R = 1.500 inch).**



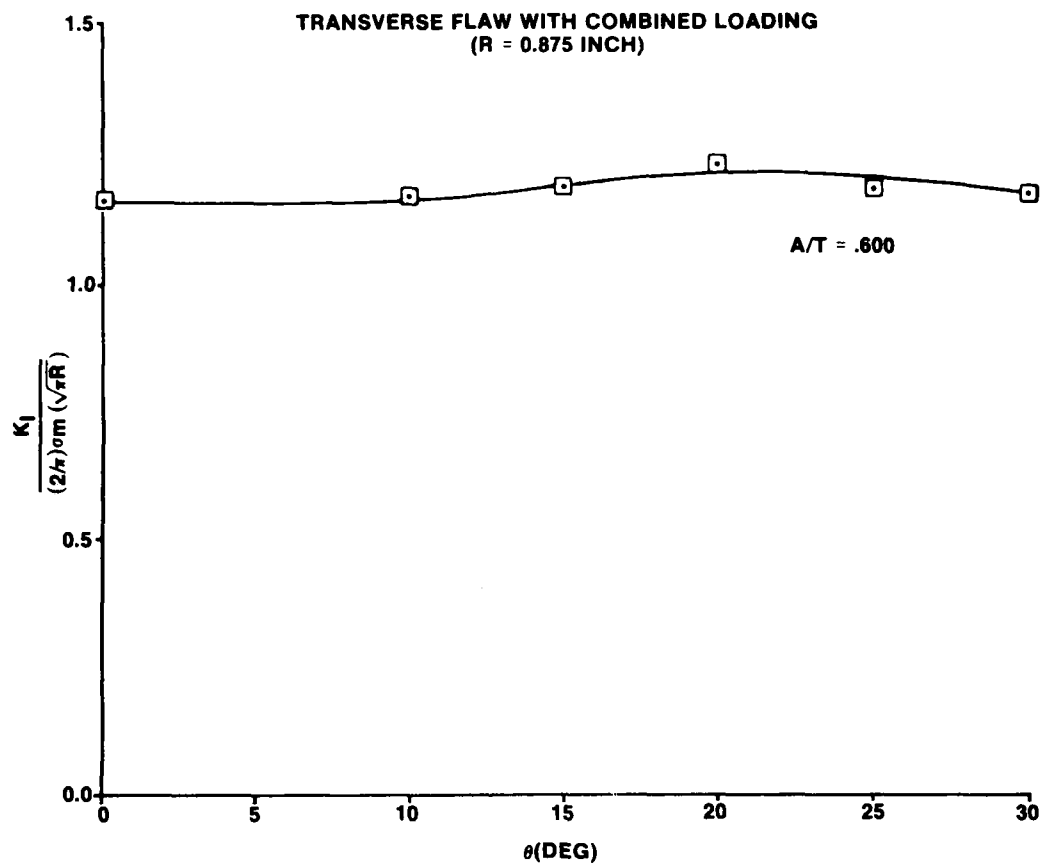
**Figure 11. Stress Intensity factor versus  $\theta$  for the transversely-flawed cylinder loaded with internal pressure and extension (R = 0.875 inch, A/T = .200).**



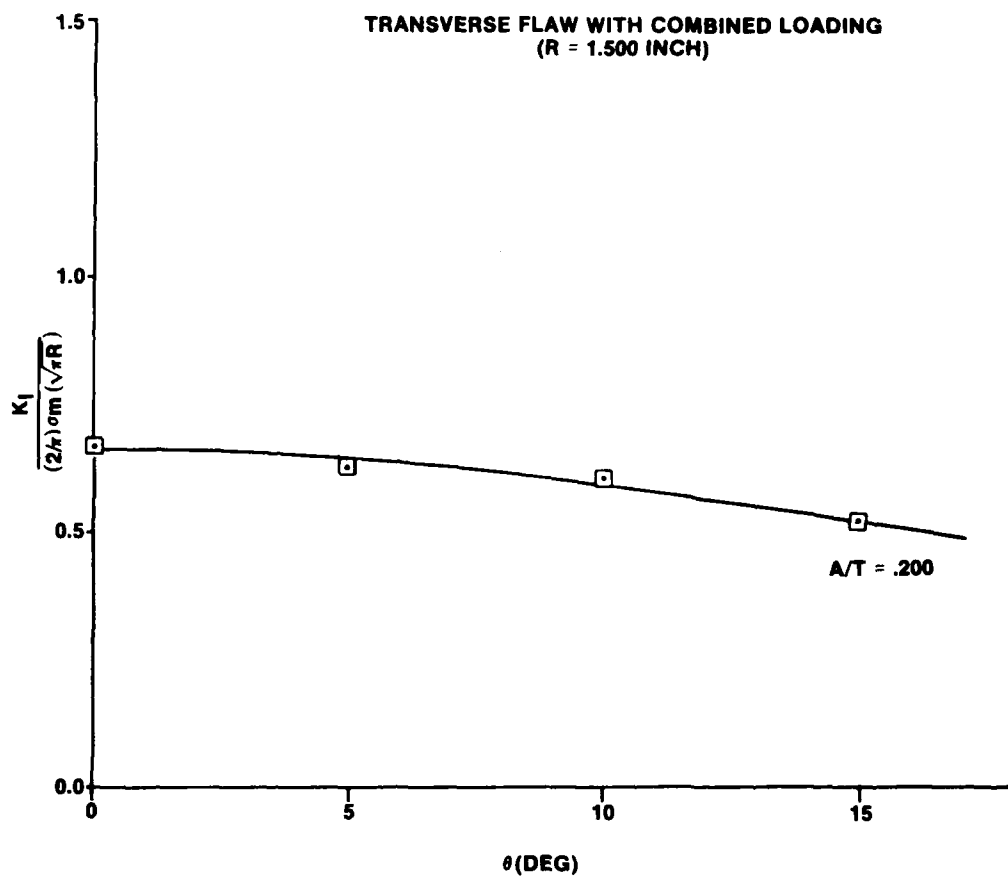
**Figure 12. Stress Intensity factor versus  $\theta$  for the transversely-flawed cylinder loaded with internal pressure and extension (R = 0.875 inch, A/T = .400).**



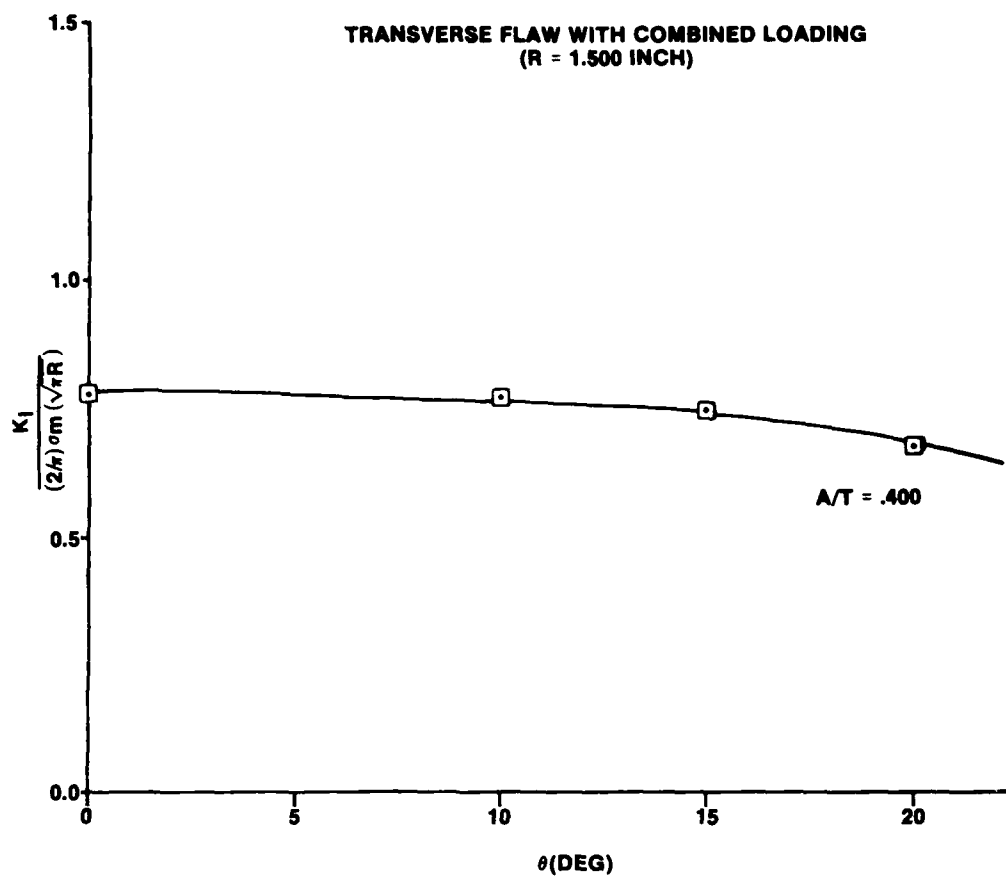
**Figure 13. Stress Intensity factor versus  $\theta$  for the transversely-flawed cylinder loaded with internal pressure and extension (R = 0.875 Inch, A/T = .500).**



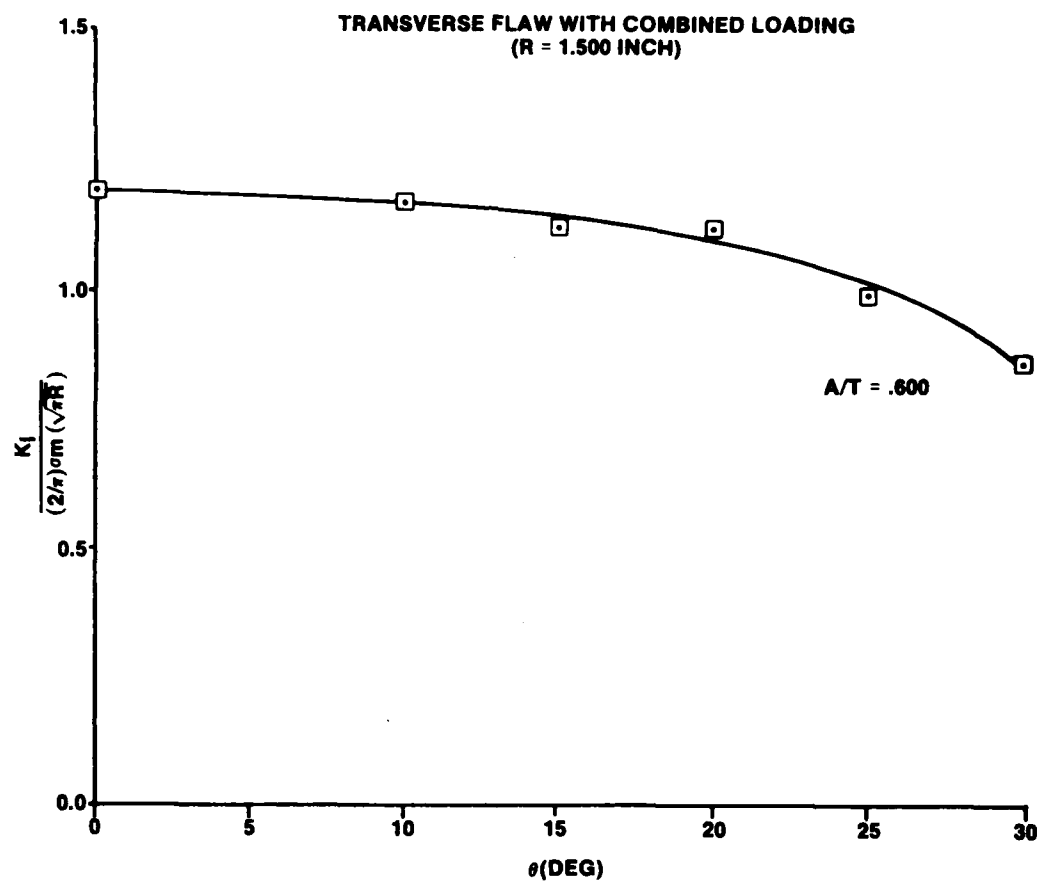
**Figure 14. Stress intensity factor versus  $\theta$  for the transversely-flawed cylinder loaded with internal pressure and extension (R = 0.875 inch, A/T = .600).**



**Figure 15. Stress Intensity factor versus  $\theta$  for the transversely-flawed cylinder loaded with internal pressure and extension (R = 1.500, inch, A/T = .200).**



**Figure 16. Stress intensity factor versus  $\theta$  for the transversely-flawed cylinder loaded with internal pressure and extension (R = 1.500 inch, A/T = .400).**



**Figure 17. Stress Intensity factor versus  $\theta$  for the transversely-flawed cylinder loaded with internal pressure and extension (R = 1.500 Inch, A/T = .600).**

TABLE 1. SPECIMEN DIMENSIONS AND TEST PARAMETERS FOR TRANSVERSELY-  
FLAWED CYLINDERS LOADED IN UNIAXIAL TENSION

| TEST PARAMETERS                                          | 1T     | 2T     | 3T     | 4T     | 5T     | 6T     | 7T     | 8T     |
|----------------------------------------------------------|--------|--------|--------|--------|--------|--------|--------|--------|
| R (inch)                                                 | 0.88   | 0.88   | 0.88   | 0.88   | 1.50   | 1.50   | 1.50   | 1.50   |
| T (inch)                                                 | 0.706  | 0.724  | 0.740  | 0.721  | 0.721  | 0.739  | 0.718  | 0.725  |
| A (inch)                                                 | 0.145  | 0.282  | 0.408  | 0.486  | 0.145  | 0.318  | 0.498  | 0.800  |
| D (inch)                                                 | 0.729  | 0.593  | 0.467  | 0.389  | 1.355  | 1.182  | 1.002  | 0.700  |
| OD (inch)                                                | 5.88   | 5.86   | 5.86   | 5.86   | 5.86   | 5.87   | 5.90   | 5.86   |
| $\theta_{max}$ (degree)                                  | 29.5   | 41.8   | 51.2   | 56.6   | 21.0   | 30.9   | 39.3   | 51.1   |
| 2a (inch)                                                | 0.865  | 1.175  | 1.376  | 1.480  | 1.080  | 1.560  | 1.935  | 2.400  |
| D (inch)                                                 | 0.834  | 0.678  | 0.534  | 0.444  | 0.903  | 0.788  | 0.668  | 0.467  |
| A/T                                                      | 0.206  | 0.390  | 0.551  | 0.674  | 0.201  | 0.430  | 0.693  | 1.100  |
| A/2a                                                     | 0.168  | 0.240  | 0.296  | 0.328  | 0.134  | 0.204  | 0.257  | 0.333  |
| d (inch)                                                 | 3.670  | 3.523  | 3.397  | 3.319  | 4.280  | 4.112  | 3.930  | 3.630  |
| Load (pound) P                                           | 125.33 | 120 ~3 | 112.38 | 115.03 | 110.38 | 100.06 | 94.34  | 80.37  |
| $\sigma_m$ (psi) = $P/A_c$                               | 10.74  | 10.32  | 9.72   | 9.84   | 9.48   | 8.42   | 8.13   | 5.16   |
| $2/\pi \sigma_m(\pi R)^{1/2}$ (psi-inch <sup>1/2</sup> ) | 11.34  | 10.90  | 10.26  | 10.39  | 13.12  | 11.63  | 11.24  | 7.14   |
| f (psi-inch)/(fringe)                                    | 1.56   | 1.56   | 1.56   | 1.56   | 1.56   | 1.56   | 1.56   | 1.56   |
| Crack Width (inch)                                       | 0.0082 | 0.0076 | 0.0082 | 0.0080 | 0.0060 | 0.0062 | 0.0065 | 0.0066 |

TABLE 2. SPECIMEN DIMENSIONS AND TEST PARAMETERS FOR TRANSVERSELY-  
FLAWED CYLINDERS LOADED WITH INTERNAL PRESSURE

| TEST PARAMETERS                                           | 1PC          | 2PC    | 3PC    | 4PC    | 5PC    | 6PC    | 7PC    | 8PC    |
|-----------------------------------------------------------|--------------|--------|--------|--------|--------|--------|--------|--------|
| R (Inch)                                                  | Test Failure | 0.875  | 0.875  | 0.875  | 1.500  | 1.500  | 1.500  | 1.500  |
| T (Inch)                                                  | Test Failure | 0.721  | 0.726  | 0.724  | 0.718  | 0.720  | 0.718  | 0.710  |
| A (Inch)                                                  | Test Failure | 0.279  | 0.385  | 0.488  | 0.144  | 0.319  | 0.491  | 0.668  |
| D (Inch)                                                  | Test Failure | 0.596  | 0.490  | 0.387  | 1.356  | 1.181  | 1.009  | 0.832  |
| OD (Inch)                                                 | Test Failure | 5.86   | 5.86   | 5.86   | 5.86   | 5.86   | 5.86   | 5.86   |
| $\theta$ max (Degree)                                     | Test Failure | 41.63  | 49.52  | 56.73  | 20.61  | 31.05  | 38.04  | 45.91  |
| 2a (Inch)                                                 | Test Failure | 1.17   | 1.34   | 1.46   | 1.06   | 1.55   | 1.89   | 2.18   |
| D (Inch)                                                  | Test Failure | 0.681  | 0.560  | 0.442  | 0.904  | 0.787  | 0.673  | 0.555  |
| A/T                                                       | Test Failure | 0.388  | 0.531  | 0.674  | 0.200  | 0.443  | 0.684  | 0.940  |
| A/2a                                                      | Test Failure | 0.238  | 0.287  | 0.334  | 0.136  | 0.205  | 0.280  | 0.306  |
| d (Inch)                                                  | Test Failure | 3.528  | 3.421  | 3.317  | 4.286  | 4.111  | 3.839  | 3.762  |
| P <sub>i</sub> (psi)                                      | Test Failure | 3.33   | 2.98   | 5.59   | 6.22   | 5.56   | 4.85   | 4.16   |
| $\sigma_m = (P_i R_o)/(2T)$ (psi)                         | Test Failure | 5.93   | 5.27   | 9.91   | 11.13  | 9.92   | 8.68   | 7.54   |
| $2/\pi \sigma_m (\pi R)^{1/2}$ (psi-Inch <sup>1/2</sup> ) | Test Failure | 6.26   | 5.56   | 10.46  | 15.39  | 13.71  | 11.99  | 10.43  |
| f (psi-Inch)/Inge                                         | Test Failure | 1.56   | 1.56   | 1.56   | 1.56   | 1.56   | 1.56   | 1.56   |
| Crack Width (Inch)                                        | Test Failure | 0.0058 | 0.0068 | 0.0074 | 0.0079 | 0.0071 | 0.0078 | 0.0081 |

TABLE 3. SPECIMEN DIMENSIONS AND TEST PARAMETERS FOR TRANSVERSELY-  
FLAWED CYLINDERS LOADED IN COMBINED UNIAXIAL TENSION AND  
INTERNAL PRESSURE

| TEST PARAMETERS         | 1PE   | 2PE   | 3PE   | 4PE   | 5PE   | 6PE   | 7PE   |
|-------------------------|-------|-------|-------|-------|-------|-------|-------|
| R (Inch)                | .875  | .875  | .875  | .875  | 1.500 | 1.500 | 1.500 |
| T (Inch)                | .7087 | .7308 | .7295 | .7341 | .7303 | .7351 | .7343 |
| A (Inch)                | .141  | .292  | .365  | .440  | .146  | .294  | .440  |
| D (Inch)                | .734  | .583  | .510  | .435  | 1.354 | 1.206 | 1.080 |
| OD (Inch)               | 5.86  | 5.86  | 5.86  | 5.86  | 5.86  | 5.86  | 5.86  |
| $\theta_{max}$ (Degree) | 29.05 | 42.66 | 48.20 | 53.51 | 20.77 | 29.78 | 36.82 |
| 2a (Inch)               | .850  | 1.166 | 1.304 | 1.407 | 1.062 | 1.490 | 1.798 |
| D                       | .939  | .866  | .583  | .497  | .903  | .804  | .707  |
| A/T                     | .200  | .400  | .500  | .600  | .200  | .400  | .600  |
| A/2a                    | .166  | .246  | .280  | .313  | .137  | .187  | .245  |
| d (Inch)                | 3.674 | 3.523 | 3.450 | 3.375 | 4.294 | 4.146 | 4.000 |
| Load (pound)            | 81.29 | 71.28 | 64.37 | 61.30 | 64.39 | 54.32 | 51.36 |
| $\sigma_m$ (psi)        | 13.93 | 11.88 | 11.17 | 10.26 | 10.98 | 9.94  | 8.69  |
| $P_i$ (psi)             | 3.808 | 3.370 | 3.160 | 2.930 | 3.11  | 2.93  | 2.48  |
| f (psi-Inch/fringe)     | 1.56  | 1.56  | 1.56  | 1.56  | 1.56  | 1.56  | 1.56  |
| Crack Width (Inch)      | .0071 | .0074 | .0064 | .0064 | .0213 | .0069 | .0061 |

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## APPENDIX A

### TEST DATA

This appendix contains a summary of all the test data presented in this report. The test nomenclature is as follows:

- T  $\equiv$  Extension loading test.  
 PC  $\equiv$  Internal pressure loading test.  
 PE  $\equiv$  Combined internal pressure and extension loading test.

The test nomenclature follows the test number. For example, 1PE refers to the first test run of a flaw in the transverse orientation subjected to combined internal pressure and extension loading.

### TEST NO. 1T

| A/T = 0.206 |             | R = 0.875 inch |                                             | $\sigma_m = 10.74 \text{ psi}$ |  |
|-------------|-------------|----------------|---------------------------------------------|--------------------------------|--|
| SLICE NO.   | ANGLE (DEG) | $K_I$          | $\frac{K_I}{2/\pi \sigma_m (\sqrt{\pi R})}$ |                                |  |
| 1           | 0           | 7.1788         | 0.633                                       |                                |  |
| 2           | 10          | 6.0309         | 0.532                                       |                                |  |
| 3           | 15          | 4.6534         | 0.410                                       |                                |  |
| 4           | 20          | 4.4673         | 0.394                                       |                                |  |

### TEST NO. 2T

| A/T = 0.390 |             | R = 0.875 inch |                                             | $\sigma_m = 10.32 \text{ psi}$ |  |
|-------------|-------------|----------------|---------------------------------------------|--------------------------------|--|
| SLICE NO.   | ANGLE (DEG) | $K_I$          | $\frac{K_I}{2/\pi \sigma_m (\sqrt{\pi R})}$ |                                |  |
| 1           | 0           | 10.7465        | 0.986                                       |                                |  |
| 2           | 10          | 10.6959        | 0.981                                       |                                |  |
| 3           | 15          | 9.9365         | 0.912                                       |                                |  |
| 4           | 20          | 9.3772         | 0.860                                       |                                |  |
| 5           | 25          | 8.7716         | 0.805                                       |                                |  |

### TEST NO. 3T

| A/T = 0.551 |             | R 0.875 Inch |                                            | $\sigma_m = 9.72 \text{ psi}$ |
|-------------|-------------|--------------|--------------------------------------------|-------------------------------|
| SLICE NO    | ANGLE (DEG) | $K_I$        | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |                               |
| 1           | 0           | 11.9434      | 1.164                                      |                               |
| 2           | 15          | 12.6552      | 1.233                                      |                               |
| 3           | 20          | 11.3063      | 1.102                                      |                               |
| 4           | 25          | 12.4901      | 1.217                                      |                               |
| 5           | 30          | 12.2604      | 1.195                                      |                               |

### TEST NO. 4T

| A/T = 0.674 |             | R = 0.875 inch |                                            | $\sigma_m = 9.84 \text{ psi}$ |  |
|-------------|-------------|----------------|--------------------------------------------|-------------------------------|--|
| SLICE NO    | ANGLE (DEG) | $K_I$          | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |                               |  |
| 1           | 0           | 12.0330        | 1.158                                      |                               |  |
| 3           | 20          | 14.8617        | 1.431                                      |                               |  |
| 4           | 20          | 13.7995        | 1.329                                      |                               |  |
| 5           | 30          | 13.1259        | 1.264                                      |                               |  |

### TEST NO. 5T

| A/T = 0.201 |             | R = 1.50 inch |                                            | $\sigma_m = 9.48 \text{ psi}$ |  |
|-------------|-------------|---------------|--------------------------------------------|-------------------------------|--|
| SLICE NO    | ANGLE (DEG) | $K_I$         | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |                               |  |
| 1           | 0           | 5.4174        | 0.413                                      |                               |  |
| 2           | 10          | 5.1066        | 0.389                                      |                               |  |
| 3           | 20          | 4.0967        | 0.312                                      |                               |  |

### TEST NO. 6T

| A/T = 0.430 |             | R = 1.50 inch |                                            | $\sigma_m = 8.416 \text{ psi}$ |  |
|-------------|-------------|---------------|--------------------------------------------|--------------------------------|--|
| SLICE NO    | ANGLE (DEG) | $K_I$         | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |                                |  |
| 1           | 0           | 10.5044       | 0.903                                      |                                |  |
| 2           | 10          | 9.8152        | 0.844                                      |                                |  |
| 3           | 15          | 8.6668        | 0.745                                      |                                |  |
| 4           | 20          | 8.5062        | 0.731                                      |                                |  |
| 5           | 25          | 7.6702        | 0.659                                      |                                |  |

### TEST NO. 7T

| A/T = 0.693 R = 1.50 inch $\sigma_m = 8.133 \text{ psi}$ |             |         |                                            |
|----------------------------------------------------------|-------------|---------|--------------------------------------------|
| SLICE NO                                                 | ANGLE (DEG) | $K_I$   | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |
| 1                                                        | 0           | 14.8162 | 1.318                                      |
| 2                                                        | 10          | 14.1479 | 1.258                                      |
| 3                                                        | 15          | 14.2745 | 1.270                                      |
| 4                                                        | 25          | 13.2439 | 1.178                                      |
| 5                                                        | 30          | 13.0841 | 1.164                                      |

### TEST NO. 8T

| A/T = 1.10 R = 1.50 inch $\sigma_m = 5.162 \text{ psi}$ |             |         |                                            |
|---------------------------------------------------------|-------------|---------|--------------------------------------------|
| SLICE NO.                                               | ANGLE (DEG) | $K_I$   | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |
| 1                                                       | 15          | 16.5615 | 2.321                                      |
| 2                                                       | 20          | 13.6390 | 1.912                                      |
| 3                                                       | 30          | 12.0614 | 1.691                                      |
| 4                                                       | 40          | 11.7697 | 1.649                                      |

### TEST NO. 2PC

| A/T = 0.388 R = 0.875 inch $\sigma_m = 5.93 \text{ psi}$ |             |        |                                            |
|----------------------------------------------------------|-------------|--------|--------------------------------------------|
| SLICE NO                                                 | ANGLE (DEG) | $K_I$  | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |
| 2                                                        | 10          | 4.9448 | 0.7899                                     |
| 3                                                        | 15          | 4.4775 | 0.7153                                     |
| 4                                                        | 20          | 4.6233 | 0.7385                                     |
| 5                                                        | 25          | 4.3932 | 0.7018                                     |

### TEST NO. 3PC

| A/T = 0.531 R = 0.875 inch $\sigma_m = 5.27 \text{ psi}$ |             |        |                                            |
|----------------------------------------------------------|-------------|--------|--------------------------------------------|
| SLICE NO                                                 | ANGLE (DEG) | $K_I$  | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |
| 1                                                        | 0           | 4.7515 | 0.8546                                     |
| 3                                                        | 15          | 5.0981 | 0.9169                                     |
| 4                                                        | 20          | 5.4732 | 0.9844                                     |
| 5                                                        | 25          | 5.0620 | 0.9104                                     |
| 6                                                        | 30          | 5.6509 | 1.0163                                     |
| 7                                                        | 38          | 5.8497 | 1.0521                                     |

**TEST NO. 4PC**

| A/T = 0.674 |             | R = 0.875 inch |                                             | $\sigma_m = 9.91 \text{ psi}$ |
|-------------|-------------|----------------|---------------------------------------------|-------------------------------|
| SLICE NO    | ANGLE (DEG) | $K_I$          | $\frac{K_I}{2/\pi \sigma_m (\sqrt{\pi R})}$ |                               |
| 1           | 0           | 10.3759        | 0.9920                                      |                               |
| 2           | 10          | 11.0626        | 1.0576                                      |                               |
| 3           | 15          | 11.1789        | 1.0687                                      |                               |
| 4           | 20          | 12.5803        | 1.2027                                      |                               |

**TEST NO. 5PC**

| A/T = 0.200 |             | R = 1.500 inch |                                             | $\sigma_m = 11.13 \text{ psi}$ |
|-------------|-------------|----------------|---------------------------------------------|--------------------------------|
| SLICE NO.   | ANGLE (DEG) | $K_I$          | $\frac{K_I}{2/\pi \sigma_m (\sqrt{\pi R})}$ |                                |
| 1           | 0           | 9.0737         | 0.5896                                      |                                |
| 2           | 10          | 8.6878         | 0.5645                                      |                                |
| 3           | 15          | 9.1832         | 0.5967                                      |                                |
| 4           | 20          | 9.0818         | 0.5901                                      |                                |

**TEST NO. 6PC**

| A/T = 0.443 |             | R = 1.500 inch |                                             | $\sigma_m = 9.92 \text{ psi}$ |
|-------------|-------------|----------------|---------------------------------------------|-------------------------------|
| SLICE NO.   | ANGLE (DEG) | $K_I$          | $\frac{K_I}{2/\pi \sigma_m (\sqrt{\pi R})}$ |                               |
| 1           | 0           | 8.4709         | 0.6179                                      |                               |
| 2           | 10          | 8.7018         | 0.6347                                      |                               |
| 3           | 15          | 9.1253         | 0.6656                                      |                               |
| 4           | 20          | 7.0955         | 0.5175                                      |                               |

**TEST NO. 7PC**

| A/T = 0.684 |             | R = 1.500 inch |                                             | $\sigma_m = 8.68 \text{ psi}$ |
|-------------|-------------|----------------|---------------------------------------------|-------------------------------|
| SLICE NO    | ANGLE (DEG) | $K_I$          | $\frac{K_I}{2/\pi \sigma_m (\sqrt{\pi R})}$ |                               |
| 1           | 0           | 8.9268         | 0.7445                                      |                               |
| 2           | 10          | 10.6402        | 0.8874                                      |                               |
| 3           | 15          | 9.6247         | 0.8027                                      |                               |
| 4           | 25          | 9.2004         | 0.7673                                      |                               |
| 5           | 30          | 11.8390        | 0.9874                                      |                               |

### TEST NO. 8PC

| A/T = 0.940 |             | R = 1.500 inch |                                            | $\sigma_m = 7.54 \text{ psi}$ |  |
|-------------|-------------|----------------|--------------------------------------------|-------------------------------|--|
| SLICE NO.   | ANGLE (DEG) | $K_I$          | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |                               |  |
| 1           | 15          | 10.2689        | 0.9845                                     |                               |  |
| 2           | 20          | 10.1580        | 0.9739                                     |                               |  |
| 3           | 30          | 11.8707        | 1.1381                                     |                               |  |
| 4           | 40          | 10.4856        | 1.0053                                     |                               |  |

### TEST NO. 1PE

| A/T = 0.200 |             | R = .875 inch |                                             | $\sigma_m = 13.93 \text{ psi}$ |  |
|-------------|-------------|---------------|---------------------------------------------|--------------------------------|--|
| SLICE NO.   | ANGLE (DEG) | $K_I$         | $\frac{K_I}{2/\pi \sigma_m (\sqrt{\pi R})}$ |                                |  |
| 1-1         | 0°          | 12.1381       | .826                                        |                                |  |
| 1-2         | 10°         | 11.3646       | .773                                        |                                |  |
| 1-3         | 15°         | 10.4009       | .707                                        |                                |  |
| 1-4         | 20°         | 8.7351        | .594                                        |                                |  |

### TEST NO. 2PE

| A/T = .400 |             | R = .875 inch |                                            | $\sigma_m = 11.88 \text{ psi}$ |  |
|------------|-------------|---------------|--------------------------------------------|--------------------------------|--|
| SLICE NO.  | ANGLE (DEG) | $K_I$         | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |                                |  |
| 2-1        | 0°          | 12.7124       | 1.014                                      |                                |  |
| 2-2        | 10°         | 13.1542       | 1.049                                      |                                |  |
| 2-3        | 15°         | 11.8315       | .944                                       |                                |  |
| 2-4        | 20°         | 12.5060       | .997                                       |                                |  |
| 2-5        | 25°         | 11.3443       | .905                                       |                                |  |
| 2-6        | 30°         | 11.3930       | .909                                       |                                |  |

### TEST NO. 3PE

| A/T = .500 |             | R = .875 inch |                                             | $\sigma_m = 11.165 \text{ psi}$ |  |
|------------|-------------|---------------|---------------------------------------------|---------------------------------|--|
| SLICE NO.  | ANGLE (DEG) | $K_I$         | $\frac{K_I}{2/\pi \sigma_m (\sqrt{\pi R})}$ |                                 |  |
| 3-1        | 0°          | 12.2987       | 1.044                                       |                                 |  |
| 3-2        | 10°         | 13.0904       | 1.111                                       |                                 |  |
| 3-3        | 15°         | 12.9064       | 1.095                                       |                                 |  |
| 3-4        | 20°         | 12.9740       | 1.101                                       |                                 |  |
| 3-5        | 25°         | 12.1957       | 1.035                                       |                                 |  |
| 3-6        | 30°         | 11.9617       | 1.015                                       |                                 |  |

### TEST NO. 4PE

| A/T .600 |             | R .875 inch |                                            | $\sigma_m = 10.28 \text{ psi}$ |
|----------|-------------|-------------|--------------------------------------------|--------------------------------|
| SLICE NO | ANGLE (DEG) | $K_I$       | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |                                |
| 4-1      | 0°          | 12.5119     | 1.153                                      |                                |
| 4-2      | 10°         | 12.6121     | 1.162                                      |                                |
| 4-3      | 15°         | 12.8565     | 1.185                                      |                                |
| 4-4      | 20°         | 13.3028     | 1.226                                      |                                |
| 4-5      | 25°         | 12.8078     | 1.180                                      |                                |
| 4-6      | 30°         | 12.7277     | 1.173                                      |                                |

### TEST NO. 5PE

| A/T .200  |             | R = 1.500 inch |                                            | $\sigma_m = 10.98 \text{ psi}$ |
|-----------|-------------|----------------|--------------------------------------------|--------------------------------|
| SLICE NO. | ANGLE (DEG) | $K_I$          | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |                                |
| 5-1       | 0°          | 10.0986        | .666                                       |                                |
| 5-2       | 5°          | 9.5187         | .627                                       |                                |
| 5-3       | 10°         | 9.1719         | .604                                       |                                |
| 5-4       | 15°         | 7.9137         | .522                                       |                                |

### TEST NO. 6PE

| A/T = .400 |             | R = 1.500 inch |                                            | $\sigma_m = 9.94 \text{ psi}$ |
|------------|-------------|----------------|--------------------------------------------|-------------------------------|
| SLICE NO.  | ANGLE (DEG) | $K_I$          | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |                               |
| 6-1        | 0°          | 10.6769        | .777                                       |                               |
| 6-2        | 10°         | 10.6978        | .779                                       |                               |
| 6-3        | 15°         | 10.2661        | .747                                       |                               |
| 6-4        | 20°         | 9.2705         | .675                                       |                               |

### TEST NO. 7PE

| A/T = .600 |             | R = 1.500 inch |                                            | $\sigma_m = 8.69 \text{ psi}$ |
|------------|-------------|----------------|--------------------------------------------|-------------------------------|
| SLICE NO.  | ANGLE (DEG) | $K_I$          | $\frac{K_I}{2/\pi \sigma_m(\sqrt{\pi R})}$ |                               |
| 7-1        | 0°          | 14.4033        | 1.199                                      |                               |
| 7-2        | 10°         | 13.8254        | 1.151                                      |                               |
| 7-3        | 15°         | 13.5577        | 1.129                                      |                               |
| 7-4        | 20°         | 13.5130        | 1.125                                      |                               |
| 7-5        | 25°         | 11.4605        | .954                                       |                               |
| 7-6        | 30°         | 10.3812        | .864                                       |                               |

APPENDIX B  
COMPUTER CODE

The computer code shown on the following pages was used to analyze the photoelastic data. The code uses the technique presented in Section II. With at least squares straight-line curve fit of the experimental data.

```

C-----PHOTOELASTICITY CODE-CYLINDERS
      DIMENSION AN(50),AR(50),AT(50),AK(50),ID(50)
      WRITE(5,22)
22      FORMAT(' NO. OF SLICES?')
      READ(5,1) N
1       FORMAT(I3)
      DO 19 I=1,N,1
      M=14
      F=1.56
      WRITE(5,25)
25      FORMAT(' SLICE THICKNESS?')
      READ(5,26) T
26      FORMAT(F10.0)
      WRITE(5,27)
27      FORMAT(' INPUT N-F6.0')
      DO 4 J=1,M,1
      READ(5,3) AN(J)
3       FORMAT(F6.0)
      IF(J.LE.9) AR(J)=FLOAT(J-1)*.005+.010
      IF(J.GT.9) AR(J)=FLOAT(J-9)*.010+.050
4       CONTINUE
      AMAX=0.
      DO 5 J=1,M,1
      AT(J)=F*AN(J)/(2.*T)
      AK(J)=AT(J)*SQRT(8.*3.14159*AR(J))
      IF(AK(J).GT.AMAX) AMAX=AK(J)
5       AR(J)=SQRT(AR(J))
6       CALL IPOKE('170410','1')
      CALL IPOKE('170410','0')
      DO 7 J=1,M,1
      IY=INT(AK(J)*1000./AMAX)
      IX=INT(AR(J)*1000./AR(M))
      CALL IPOKE('170412,IX)
      CALL IPOKE('170414,IY)
7       CALL IPOKE('170414','0')
      ITEST=IPEEK('177570)
      IF(ITEST.EQ.0) GOTO 6
      WRITE(5,8)

```

```

8      FORMAT(' NO. OF DELETE SAMPLES?')
      READ(5,9) ND
9      FORMAT(13)
      IF(ND.EQ.0) GOTO 20
      DO 11 J=1,ND,1
      READ(5,10) ID(J)
10     FORMAT(13)
11     CONTINUE
20     CONTINUE
      X1=0.
      X2=0.
      Y0=0.
      Y1=0.
      DO 14 J=1,M,1
      IF(ND.EQ.0) GOTO 21
      DO 13 K=1,ND,1
13     IF(J.EQ.ID(K)) GOTO 14
21     X1=X1+AR(J)
      X2=X2+AR(J)**2.
      Y0=Y0+AK(J)
      Y1=Y1+AK(J)*AR(J)
14     CONTINUE
      AK1=(X2*Y0-Y1*X1)/(FLOAT(M-ND)*X2-X1*X1)
      WRITE(5,15) 1
15     FORMAT(' SLICE NO. =',13)
      DO 18 J=1,M,1
      AR(J)=AR(J)**2.
      WRITE (5,16) AR(J),AN(J),AT(J),AK(J)
16     FORMAT(' R=',F10.4,5X,'N='F10.4,5X,
17           'TMAX=',F10.4,5X,'KAPP='F10.4)
18     CONTINUE
      WRITE(5,17) AK1
17     FORMAT(' K1=',F14.4)
19     CONTINUE
      STOP
      END

```

## LIST OF SYMBOLS

|                                             |                                                                        |
|---------------------------------------------|------------------------------------------------------------------------|
| $A$                                         | Crack depth at deepest point (semi-minor diameter for elliptical flaw) |
| $A_c$                                       | Nominal cross-sectional area of cylinder                               |
| $a$                                         | Half-length of crack on outside surface of wall                        |
| $\bar{D}$                                   | Distance from center of circular flaw to surface of the wall           |
| $D$                                         | Ratio of Distance $\bar{D}$ to radius of circular flaw $R$             |
| $d$                                         | Distance from center of cylinder to center of circular flaw            |
| $f$                                         | Photoelastic fringe constant                                           |
| $K_{I, SIF}$                                | Mode I stress intensity factor                                         |
| $N$                                         | Isochromatic fringe order                                              |
| $P$                                         | Total load on cylinder loaded in tension                               |
| $P_i$                                       | Internal cylinder pressure                                             |
| $R$                                         | Radius of circular flaw                                                |
| $R_c$                                       | Radius of cylinder measured to center of cylinder wall                 |
| $r, \psi$                                   | Polar coordinates centered at crack tip                                |
| $T$                                         | Wall thickness of the cylinder                                         |
| $t$                                         | Thickness of a slice analyzed                                          |
| $y, n, \theta$                              | Coordinate system shown in <i>Figure 3</i>                             |
| $\sigma_m$                                  | Nominal cylinder-wall stress                                           |
| $\sigma_{on}$                               | Uniform stress at the crack tip                                        |
| $\sigma_y, \sigma_n, \sigma_\theta$         | Normal stress components                                               |
| $\tau_{ny}, \tau_{n\theta}, \tau_{y\theta}$ | Shear stress components                                                |
| $\tau_{max}$                                | Maximum shearing stress in the plane perpendicular to the crack border |
| $\theta_{max}$                              | Maximum flaw angle ( <i>Figure 2</i> )                                 |

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