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**INVESTIGATION OF VIBRATION REDUCTION THROUGH
STRUCTURAL OPTIMIZATION**

H. W. Hanson
BELL HELICOPTER TEXTRON
P. O. Box 482
Fort Worth, Tex. 76101

July 1980

Final Report for Period August 1978 - March 1980

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APPLIED TECHNOLOGY LABORATORY POSITION STATEMENT

In the area of aircraft structural dynamic design, the existence of a reliable structural optimization method can be a valuable design tool, enabling a designer to perform rapid identification and evaluation of the most promising structural elements, which, upon modification of their modal properties, could minimize vibration response. In this program, a feasibility study was performed to evaluate two structural optimization methods, the Vincent circle and the forced response strain energy method for reducing vibration response, primarily via structural stiffness changes, using NASTRAN beam-element representation of the AH-1G with uniform damping. The forcing function consisted of a single main rotor 2 rev steady-state vertical excitation. The pilot's seat was selected as the location for dynamic response reduction.

The relative effectiveness of the methods to minimize the dynamic response at the selected location, subject to the constraints and considerations stated above, was based essentially on two factors: (a) selection of practical stiffness changes that an element can undergo, and (b) evaluation of the effectiveness of the groups of elements predicted by each method by calculating the response of the structure subject to practical stiffness changes.

The results obtained from the two methods, i.e., stiffness changes required and group of elements identified with high potential for reducing vibration, at best, do not agree. These results indicate that the forced response strain energy method is more suitable in attaining response reduction according to the investigative methodology used in this program.

The Vincent circle method was further investigated in conjunction with mass and damping changes. Also, the possibility that the Vincent circle method would indicate the optimum location of a fixed mass and damping dynamic absorber was investigated, yielding negative results.

The project engineer for this effort was Mr. N. J. Calapodas of the Aeronautical Technology Division, Structures Technical Area.

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The purpose of this program was to investigate structural optimization techniques for vibration reduction. The results of a practical evaluation of two such techniques, the Vincent circle method and the forced response strain energy method, are discussed. Initial comparison studies of the two methods based on stiffness parameter variations were conducted using an elastic-line NASTRAN

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model of the AH-1G helicopter. The forced response strain energy method was then applied to a large complex built-up NASTRAN AH-1G model. This application provided useful comparative data identifying the structural elements considered to be the primary contributors to the response. Realistic structural stiffness changes in these elements were assessed to determine their effect on vibration reduction. The Vincent circle method was further evaluated for mass tuning, damping, and dynamic absorber parameters using the elastic-line model.

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PREFACE

This investigation of vibration reduction through structural optimization was performed under Contract DAAK51-78-C-0011 for the Applied Technology Laboratory, U. S. Army Research and Technology Laboratories (AVRADCOM), Fort Eustis, Virginia. The program was implemented under the technical direction of Mr. Nicholas J. Calapodas of the Applied Technology Laboratory.

A literature survey of structural optimization techniques for vibration reduction was performed and two techniques - the Vincent circle method and the forced response strain energy method - were evaluated using a NASTRAN analysis of the Model AH-1G helicopter. Mr. Horace W. Hanson was the Bell Helicopter Textron Project Engineer.

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INTRODUCTION

In the development of a helicopter airframe structure, part of the design cycle must be concerned with keeping vibration to a minimum. The analysis and control of helicopter airframe dynamic characteristics are quite complex. The reasons are, in part:

- The large number of main rotor harmonic excitations simultaneously present, as well as excitations from secondary sources such as the tail rotor and shafting.
- The large variation in main rotor oscillatory hub forces and moments and phase relationships as a function of ship gross weight and center-of-gravity, airspeed, temperature, altitude, etc.
- The large number of locations at which vibrations must be controlled within the aircraft for reasons of crew and passenger comfort, system reliability, and service life of the airframe structure and components.
- Design changes for vibration control that must be accomplished within the framework of the overall design criteria, including many considerations such as size, strength, weight, and aerodynamic drag.

Vibration reduction is primarily accomplished through dynamic devices such as vibration isolation systems and dynamic absorbers, and/or through structural modifications that improve the vibratory elastic deformation characteristics of the airframe. Rapid and efficient techniques are needed for evaluating and optimizing these structural changes to minimize the vibration response. Two methods of reducing vibration through structural optimization were evaluated in this study - the Vincent circle method and the forced response strain energy method.

LITERATURE SURVEY

A brief search was conducted to locate and review existing literature applicable to vibration reduction by structural optimization techniques with emphasis on the Vincent circle and the forced response strain energy methods. Three data bases were used in the survey:

- The National Technical Information Service (NTIS)
- The Defense Technical Information Center (DTIC)
- The Engineering Index (COMPENDEX)

The information that is cataloged in the National Technical Information Service is derived from publications of the federal, state, and local government agencies; private industry; and universities, with emphasis placed on commercial applications. The information available from DTIC is obtained from many of the same sources as NTIS; however, the emphasis is placed on military and defense usage. The Engineering Index contains publications of the engineering societies, such as the proceedings of conferences, journals, and magazines.

Five documents applicable to the Vincent circle method were found (References 1 through 5). Only one report addressing

¹Vincent, A. H., A NOTE ON THE PROPERTIES OF THE VARIATION OF STRUCTURAL RESPONSE WITH RESPECT TO A SINGLE STRUCTURAL PARAMETER WHEN PLOTTED IN THE COMPLEX PLANE, Westland Helicopters Limited Report GEN/DYN/RES/010R, Yeovil, Somerset, England, September 1973.

²Done, G. T. S., and Hughes, A. D., THE RESPONSE OF A VIBRATING STRUCTURE AS A FUNCTION OF STRUCTURAL PARAMETERS, Journal of Sound and Vibration, Vol. 38, No. 2, 1975, pp. 255-266.

³Done, G. T. S., and Hughes, A. D., REDUCING VIBRATION BY STRUCTURAL MODIFICATION, Vertica, Vol. 1, No. 1, 1976, pp. 31-38, (paper presented at the First European Rotorcraft and Powered Lift Aircraft Forum at Southampton, September 22-24, 1975).

⁴Done, G. T. S., Hughes, A. D., and Webby, J., THE RESPONSE OF A VIBRATING STRUCTURE AS A FUNCTION OF STRUCTURAL PARAMETERS - APPLICATION AND EXPERIMENT, Journal of Sound and Vibration, Vol. 49, No. 2, 1976, pp. 149-159.

⁵Balmford, D. E. H., THE CONTROL OF VIBRATION IN HELICOPTERS, Aeronautical Journal, Vol. 81, No. 794, February 1977, pp. 63-67.

the forced response strain energy method was located (Reference 6).

The search did not disclose any other literature that dealt specifically with vibration reduction through structural optimization.

⁶Sciarra, J. J., USE OF THE FINITE ELEMENT DAMPED FORCED RESPONSE STRAIN ENERGY DISTRIBUTION FOR VIBRATION REDUCTION, Boeing-Vertol Company Report D210-10819-1, U.S. Army Research Office - Durham, Durham, North Carolina, July, 1974.

STRUCTURAL OPTIMIZATION METHODS UNDER EVALUATION

VINCENT CIRCLE METHOD

If a damped linear structure is excited by a constant sinusoidal force at a single location, the response of some other point in the structure can be shown to trace out a circular locus in the complex plane when any single structural element stiffness or mass parameter is continuously varied from minus infinity to plus infinity, as illustrated in Figure 1. This dynamic property of linear structures is known as the Vincent circle phenomenon (Reference 1). The phenomenon requires that some value of damping be present in order to develop the imaginary component of the response. The minimum response attainable, due to a particular stiffness or mass parameter, is indicated by the radius of the response circle and location of its center. Use of these circular properties will hereafter be referred to as the Vincent circle method.

The relevant mathematics of this circular response phenomenon, based on the theory originally established by Vincent, are given by Done and Hughes (Reference 2) and are summarized as follows:

The structure shown in Figure 1 has many degrees-of-freedom, and the response at point q due to a single sinusoidal force at point p is being examined. The amplitude of the displacement response vector, x , for the structure is given by

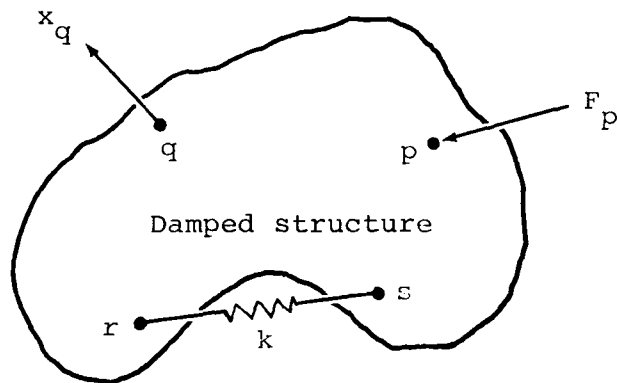
$$x = GF \quad (1)$$

where

$$G = [K - M\omega^2 + i\omega C]^{-1} \quad (2)$$

Consider two points, r and s , in the structure having mutually compatible degrees of freedom. A linear spring of stiffness, k , is inserted between these two points so as to exert zero force when the original structure is in equilibrium. Considering the structure as a free body, the forces exerted on it at points r and s by the spring are F_r and F_s , respectively, which have the relationship

$$F_r = k(x_s - x_r) = -F_s \quad (3)$$



Apply constant sinusoidal force of amplitude F at point p , vary spring stiffness k between points r and s , and measure response x at point q .

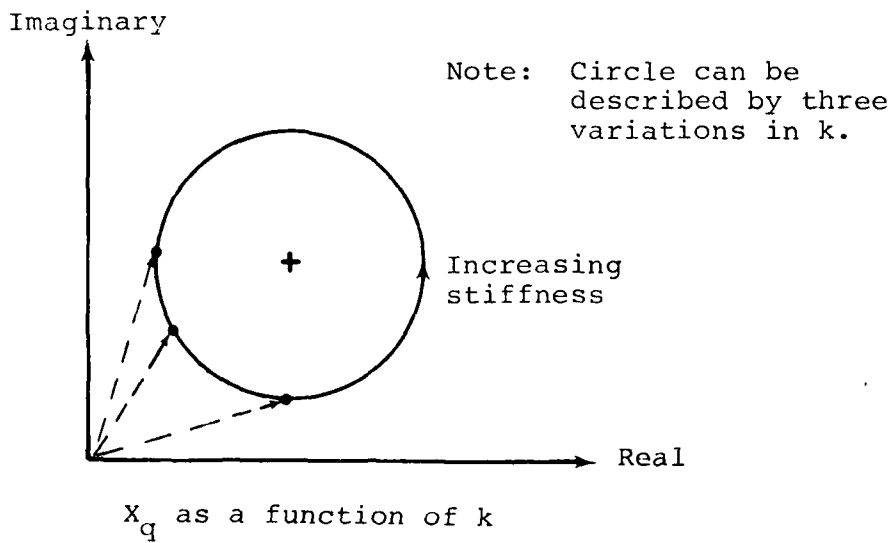


Figure 1. Vincent circle phenomenon.

The nonzero elements in the forcing vector F are F_r , F_s , and F_p . The response equations of interest are

$$x_q = G_{qp} F_p + G_{qr} F_r + G_{qs} F_s \quad (4)$$

$$x_r = G_{rp} F_p + G_{rr} F_r + G_{rs} F_s \quad (5)$$

$$x_s = G_{sp} F_p + G_{sr} F_r + G_{ss} F_s \quad (6)$$

where

G_{qp} is the complex receptance providing the displacement at point q due to a force at point p , etc.

Expressing F_r and F_s in terms of x_r and x_s from Equation (3), and subsequent elimination of x_r and x_s from Equations (4), (5), and (6), gives

$$\frac{x_q}{F_p} = G_{qp} + \frac{k(G_{sp} - G_{rp})(G_{qr} - G_{qs})}{1 + k(G_{rr} + G_{ss} - G_{rs} - G_{sr})} \quad (7)$$

This may now be rewritten in more general terms as

$$\xi + i\eta = (e + if) + \frac{k(a + ib)}{1 + k(c + id)} \quad (8)$$

where

$$\frac{x_q}{F_p} = \xi + i\eta \quad (9)$$

and a , b , c , d , e , and f are all real. The imaginary part of Equation (8) can be rearranged to the equation of a circle, being

$$\left[\xi - \left(e + \frac{b}{2d} \right) \right]^2 + \left[\eta - \left(f - \frac{a}{2d} \right) \right]^2 = \frac{a^2 + b^2}{4d^2} \quad (10)$$

It is important to note here that the radius of the circular response, as well as the complex coordinates of the center of the circle, may be obtained from these original complex

receptance matrix coupling terms of Equation (10). No iterations in k are necessary; in fact, k drops out of the solution when expressed in this form. Furthermore, it is clearly seen that these circular response properties are purely a function of the imaginary terms (i.e., damping).

Several papers have been published (References 2, 3, and 4) to both mathematically and experimentally substantiate this circular response region, and to employ these circular properties as a possible optimization technique for reducing structural vibration. In a more general sense, Balmford⁵ describes the Vincent circle as a method for providing a reduction of vibration in a local area by adjustment of airframe modes such that modal cancellation will take place to reduce the response for one frequency and one loading condition.

STRAIN ENERGY METHOD

Strain energy is an expression for the potential energy of a structural element and is most commonly expressed in matrix form for the static condition as

$$SE = 1/2 (\delta^T K_e \delta) \quad (11)$$

For the dynamic condition, structural elements possessing the highest strain energies in a given mode of vibration have been shown to be the best candidates for modification to reduce overall structural dynamic amplification.⁶ Two approaches are generally considered, as described in the following sections.

Modal Strain Energy Approach

This approach seeks to reduce vibration by detuning a structure natural frequency to a better position with respect to the forcing frequency. Modal strain energy is calculated for each structural element using the mode shape (eigenvector) for the natural frequency to be modified

$$SE = 1/2 (\phi^T K_e \phi) \quad (12)$$

Elements with the highest strain energies indicate the optimal structural elements to change in order to shift the natural frequency away from the forcing frequency, thereby reducing dynamic amplification.

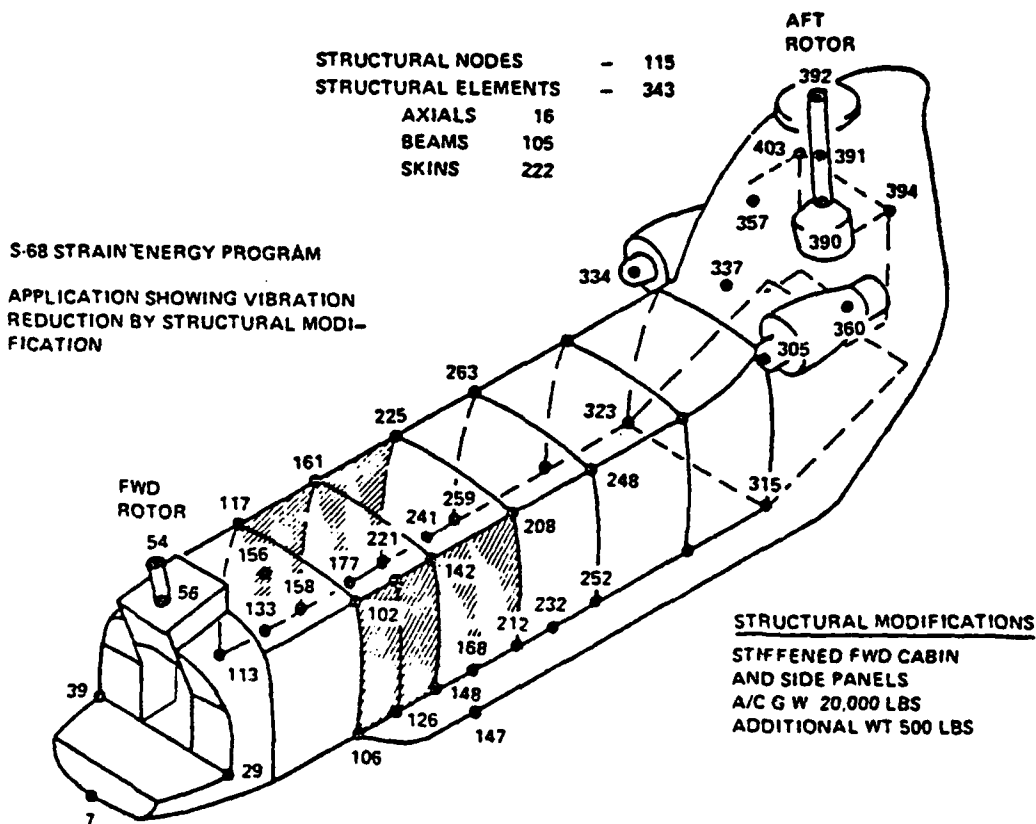
Forced Response Strain Energy Approach

This is an extension of the modal approach that takes into account the response participation of all modes for a particular load application and excitation frequency, including the effects of structural damping and combined forcing function phase relationships. Therefore, the resultant strain energy of each structural element will be a periodic function in time. Sciarra⁶ has done considerable work in this field and has arrived at an expression for the maximum damped forced response element strain energy within the period

$$\begin{aligned} 4(SE)_{\max} &= \delta_R^T K_e \delta_R + \delta_I^T K_e \delta_I \\ &+ [(\delta_I^T K_e \delta_I - \delta_R^T K_e \delta_R)^2 \\ &+ (\delta_R^T K_e \delta_I + \delta_I^T K_e \delta_R)^2]^{1/2} \end{aligned} \quad (13)$$

Elements with the highest strain energies indicate the elements that are most responsible for the structural dynamic amplification. Because the forced response strain energy approach gives direct information at the specific excitation frequency of interest, it was selected for comparison to the Vincent circle method.

Figure 2 illustrates an application of the strain energy technique. First, the modal strain energy approach was used to selectively stiffen the structure in order to move a fuselage natural frequency to a higher position above the excitation frequency, thereby reducing the dynamic amplification. A damped forced response analysis of the modified structure was then compared to the original structure, and it was confirmed that an overall vibration reduction had resulted in the fuselage area of interest.



Mode	Original Fuselage Hz	Modified Fuselage Hz	Excitation Frequency 11.45 Hz
7	6.687	6.703	
8	7.879	8.160	
9	8.442	8.494	
10	12.03	12.74	Natural Frequency Changed (Mode No. 10, 4th Elastic Mode) - Mode Amplification Factor Down From 9.1 to 5.0
11	12.52	12.79	
12	14.48	14.82	
13	15.69	16.02	
14	16.95	17.22	
15	18.94	19.06	

A damped forced response analysis comparison of the original and the modified fuselage resulted in a vibration reduction for 99 out of 123 degrees-of-freedom.

Figure 2. Boeing-Vertol CH-47A vibration reduction by structural modification (Reference 6).

PROGRAM OBJECTIVES

The purpose of this contracted study was to evaluate the practical applicability of the Vincent circle method, as compared to the forced response strain energy method, for reducing vibration through realistic structural stiffness optimization. The analytical study was performed on the Model AH-1G helicopter, and the effort was limited to application of a single steady-state main rotor 2/rev (10.8 Hz) vertical excitation force with a goal of minimizing the pilot's seat vertical response.

The Vincent circle method was further investigated for usefulness as applied to evaluating mass changes, damping, and ability to optimize dynamic absorber locations.

ANALYTICAL APPROACH

METHOD OF ANALYSIS

For evaluating the Vincent circle method, the receptance matrix technique previously described offers an attractive and direct means to obtain the response circle radius and center-of-location properties based on a single stiffness (or mass) parameter. However, for a feasibility study of this nature, several important disadvantages also exist in that the receptance matrix technique is not easily adapted for evaluation of the following:

- The sensitivity of the circular response region versus element stiffness (or mass) values.
- A coupled stiffness matrix between two points. In dealing with real structure, rarely are we concerned with a single uncoupled parameter like a simple spring, but rather structural elements behaving more like beams that have coupled stiffness matrices. For example, a single variation in the area moment of inertia (I) of a beam affects both the shear translational and rotational degrees-of-freedom between the two ends of the beam.
- Individual element damping variations while the damping for the remainder of the structure remains uniform.
- Tuning sensitivity of a dynamic absorber at different locations on the structure (i.e., effect of backup structure at absorber location).

Since the purpose of this contracted effort was not to evaluate the merits of the receptance matrix technique, and in order to use the same analytical tool for evaluating both the Vincent circle method and the forced response strain energy method, a straightforward linear NASTRAN⁷ analysis was selected for performing the study. Also, due to a unique situation at Bell Helicopter Textron wherein many NASTRAN computer runs can be accomplished quickly and at a low cost, the additional time and cost that would have been required to develop a special purpose receptance matrix manipulation computer program was avoided.

⁷THE NASTRAN USER'S MANUAL, NASA SP-222(03) National Aeronautics and Space Administration, Washington, D. C., July 1976.

As applied to the Vincent circle method, this straightforward NASTRAN approach required the evaluation of several iterations in the particular parameter under investigation to develop the circular response region, from which the response circle radius and center-of-location properties were subsequently determined. However, no restrictions were necessary on what parameters could be selected, and more in-depth information was provided as to the characteristics of the circular response region than if the receptance matrix technique had been employed.

The version of NASTRAN used at the time of this study was Level 16.0.5. This particular level of NASTRAN does support strain energy calculations, but only for static analysis. Although desirable, it was found that the NASTRAN internal modifications necessary to incorporate the complex damped forced response strain energy calculations (Equation 13) were beyond the scope of this study. However, by using the Direct Matrix Abstraction Program (DMAP) capability in NASTRAN, the static strain energy module was incorporated into the dynamics frequency response analysis with the following limitations:

- All applied oscillatory loads must be input at zero degrees phase.
- No damping can be included, thus the applied load and response vector have only real components.

These limitations were required because the statics format of the NASTRAN strain energy module is not compatible for processing complex numbers (i.e., only the real part of a complex number is considered). Therefore, the forced response strain energy expression for a structure element responding to a single resultant applied load with zero damping has now been reduced to

$$SE = 1/2 (\delta_R^T K_e \delta_R) \quad (14)$$

This results in a strain energy distribution that is a close approximation to the strain energy distribution obtained when a small amount of uniform structural damping is included. For the purposes of this study, this undamped strain energy distribution was acceptable for comparison to the Vincent circle results, wherein a small amount of damping must be included as previously explained.

MATHEMATICAL MODELS

Initial stiffness parameter investigations were conducted using a simple elastic-line NASTRAN model of the AH-1G helicopter (Figures 3 and 4). This elastic-line model was originally developed as an AH-1J (Reference 8) and was later modified into the AH-1G configuration (Reference 9). The structural optimization method showing the most potential for reducing vibration through realistic structural stiffness changes was then applied to minimize pilot's seat vertical response using a large complex built-up NASTRAN model of the AH-1G (Figure 5).¹⁰ The elastic-line model was also used to further evaluate the Vincent circle method as applied to mass, damping, and dynamic absorber parameters.

For use in this study, both the elastic-line and the built-up models of References 9 and 10, respectively, were updated to a basic mission-clean wing configuration. To show the similarity of the two models, a comparison of weight data and natural frequency placements is shown in Table 1. From the natural frequency comparisons, in addition to the obvious absence of landing gear skid modes, it is seen that the elastic-line model has no fuselage torsional modes in the zero to thirty hertz frequency range of interest. This is due to inadequate fuselage torsional mass inertia representation in the elastic-line model which, due to the torsional coupling, is also partially responsible for the differences in pylon roll and fuselage lateral bending modes. Note, however, the close agreement between the two models for the pylon pitch and the first and second fuselage vertical bending modes that are of primary importance in this study. Both the elastic-line and built-up models have the same elastic-line representations for the helicopter tailboom structure.

⁸Cronkhite, J. D., and Wilson, W. F., DYNAMIC ANALYSIS OF TWO-PER-REV VIBRATIONS IN THE MODEL AH-1J HELICOPTER - PIP Task No. AH-8-123, Bell Helicopter Textron Report 299-100-021, Fort Worth, Texas, 4 February 1972.

⁹Cronkhite, J. D., XM-97 (20MM) WEAPON ON THE AH-1G - PRELIMINARY DYNAMIC ANALYSIS, Bell Helicopter Textron Inter-office Memo 81:JDC:mb-054, Fort Worth, Texas, 29 May 1973.

¹⁰Cronkhite, J. D., Berry, V. L., and Brunken, J. E., A NASTRAN VIBRATION MODEL OF THE AH-1G HELICOPTER AIRFRAME, U.S. Army Armament Command Report No. R-TR-64-45, Research Directorate, Gen. Thomas J. Rodman Laboratory, Rock Island Arsenal, Rock Island, Illinois, June 1974.

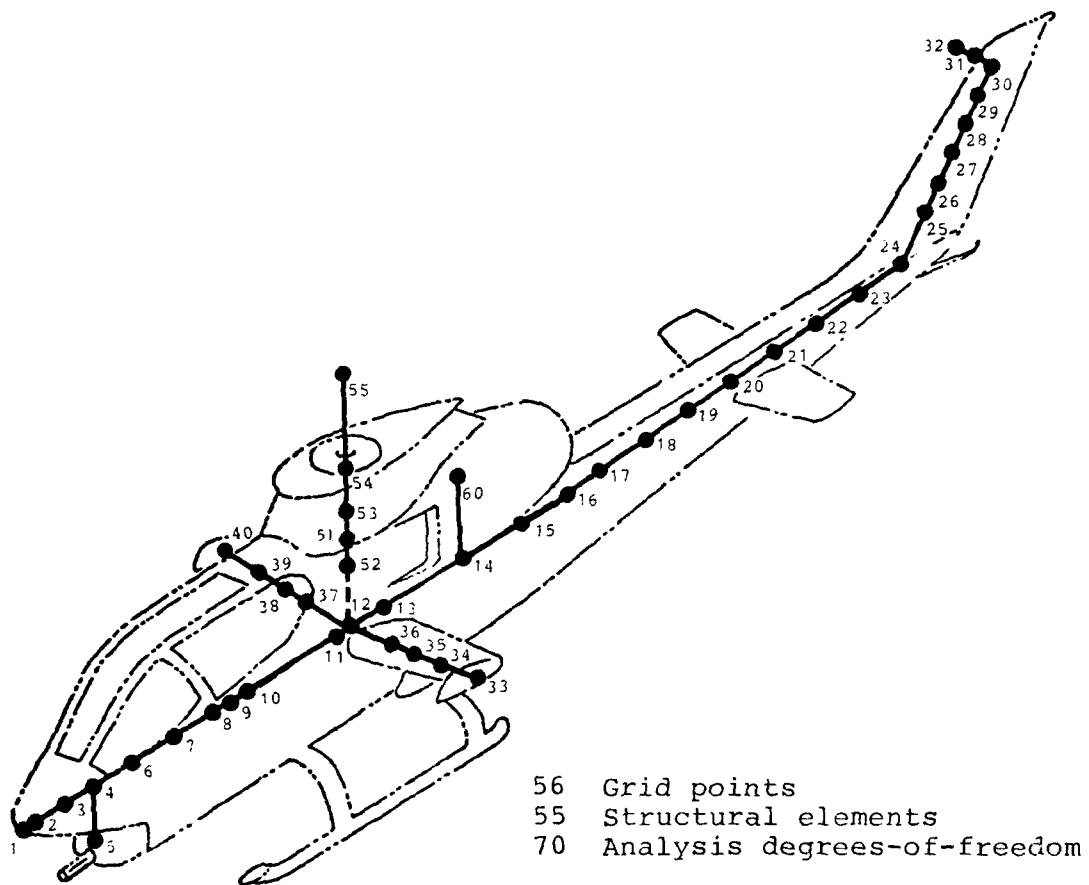


Figure 3. AH-1G elastic-line math model.

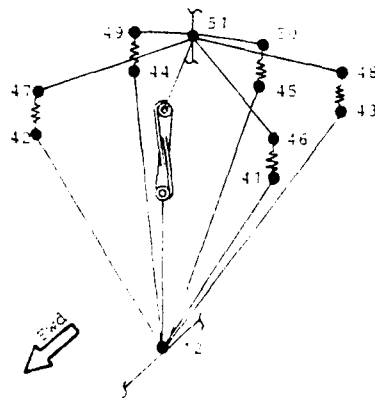
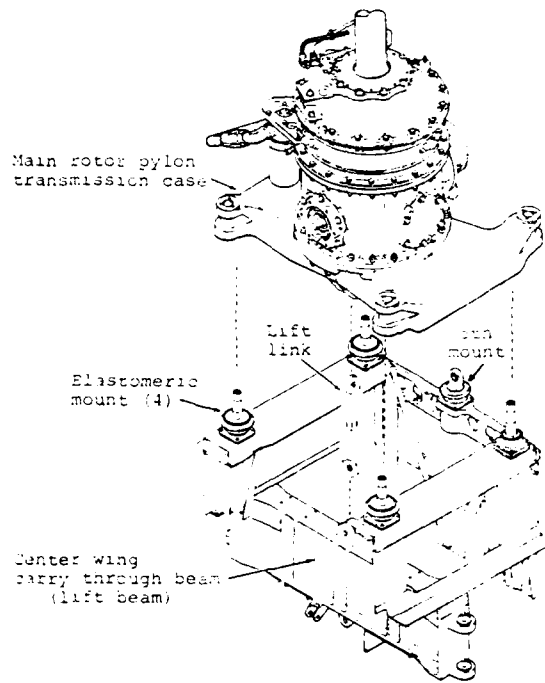


Figure 4. Elastic-line model main rotor pylon.

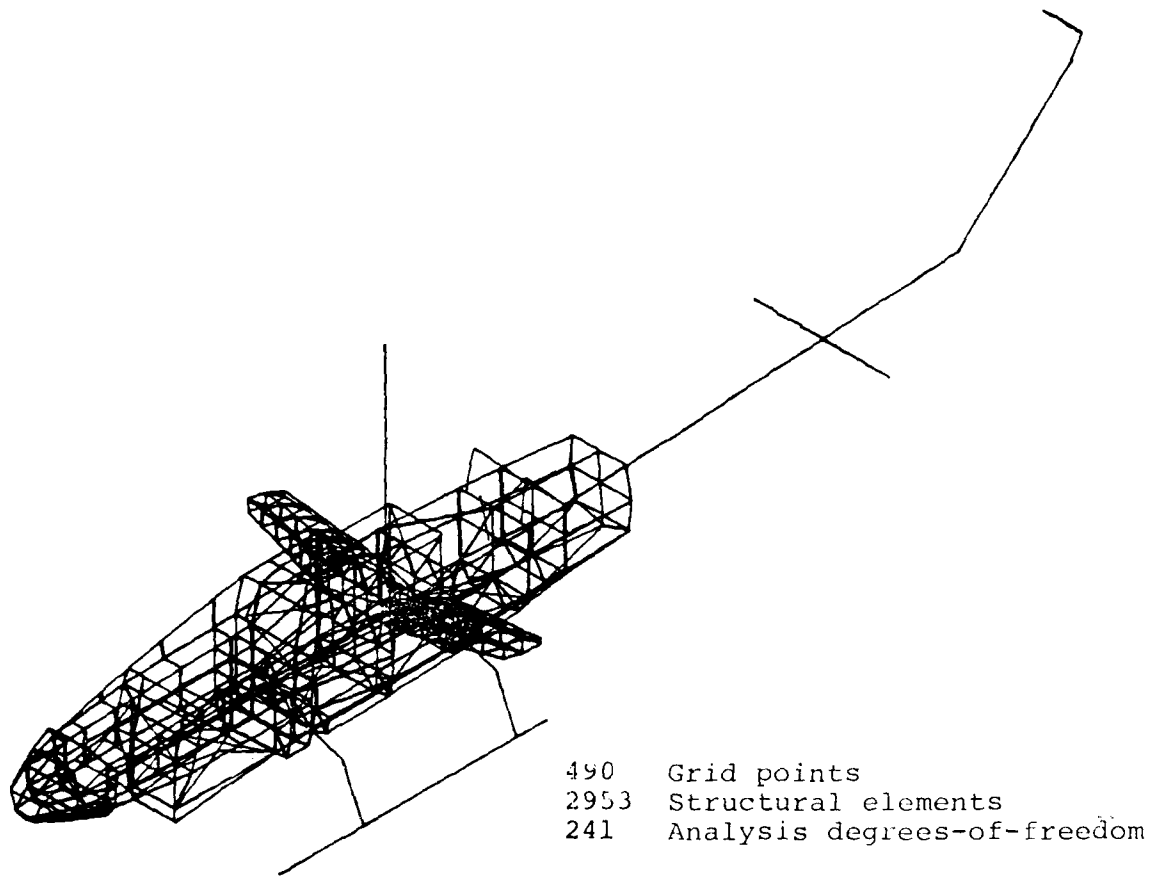


Figure 5. AH-1G built-up math model.

TABLE 1. AH-1G MODEL COMPARISON

Basic Mission-clean Wing	3-D Built-Up Model	Elastic Line Model	
Weight Data			
Gross weight (lb)	8394.	8394.	
Center-of-gravity	{ Sta (in.)	192.9	193.1
	{ BL (in.)	0.0	0.1
	{ WL (in.)	70.6	68.7
Inertias	{ Roll (lb-in. ²)	1.139×10^7	1.139×10^7
	{ Pitch (lb-in. ²)	6.193×10^7	6.200×10^7
	{ Yaw (lb-in. ²)	5.196×10^7	5.215×10^7
Natural Frequency Data			
Mode Description	(Hz)	(Hz)	
M/R pylon pitch	3.03	3.02	
M/R pylon roll	3.90	4.24	
1st Fuselage lateral bending	7.14	6.80	
1st Fuselage vertical bending	7.94	7.93	
1st Skid mode	14.57	-	
1st Fuselage torsion	15.66	-	
2nd Fuselage lateral bending	17.49	16.70	
2nd Fuselage vertical bending	17.49	17.86	
2nd Skid mode	18.76	-	
3rd Skid mode	19.84	-	
2nd Fuselage torsion	21.49	-	
4th Skid mode	23.43	-	
M/R mast lateral bending	25.28	24.79	
M/R mast F/A bending	24.97	25.80	
5th Skid mode	25.75	-	
3rd Fuselage vertical bending	26.96	29.47	
6th Skid mode	29.04	-	

The AH-1G elastic-line NASTRAN model (including the DMAP ALTER procedure developed for obtaining undamped forced response element strain energy output) is included as Appendix A.

PRACTICAL CRITERION FOR STRUCTURAL STIFFNESS CHANGES

A practical criterion for stiffness change limitations was developed by considering the classical single degree-of-freedom spring/mass/damper dynamic system that has a resonance dynamic amplification factor of 25 for 2 percent damping. This amplification factor can be reduced to 1.1 by either reducing the stiffness by a factor of 0.5, or by increasing the stiffness by a factor of 10, assuming the mass and damping parameters to remain constant. This 0.5 to 10 stiffness factor range seems to be within the limits of practical considerations even though, realistically speaking, structure designed for strength would not have its stiffness reduced by one-half or increased ten-fold without undergoing a considerable redesign effort (i.e., geometric shape factor, type materials, added weight penalties, etc.)

Based on this practical stiffness change criterion, the forced response strain energy and Vincent circle results were compared to determine which was the most promising method for vibration reduction through realistic structural stiffness optimization.

STIFFNESS PARAMETER INVESTIGATIONS

ELASTIC-LINE MODEL ANALYSIS

The forced response strain energy method was used to determine which structural members had the highest forced response strain energies. Using stiffness parameter variations, these members were then analyzed using the Vincent circle method.

Forced Response Strain Energy Results

Figure 6 is a NASTRAN-generated plot showing a side view of the elastic-line model forced response vertical deformation mode shape. The resultant forced response strain energy distribution is shown in Figure 7. The element identification numbers shown are related to the two-digit GRID numbers at each end of the element, as identified in Figures 3 and 4. The strain energy shown for each element is the total due to the resultant six degrees-of-freedom deflections at each end of the element and the element stiffness matrix as calculated by Equation (14). Since the elastic-line model is essentially symmetric and the applied load at the hub is in the vertical direction, only deflections in the vertical plane are contributing significantly to the strain energy calculation. Note how the strain energy distribution compares to what might be expected from examination of the elastic deformation mode shape of Figure 6.

The elastic-line model NASTRAN forced response strain energy output data are presented in Appendix B.

Vincent Circle Results

As previously shown, this circular response property is based on variations involving single parameters only. However, in this study the Vincent circle method was evaluated with respect to realistic element property changes such as AE axial stiffness and EI bending stiffness parameters, wherever applicable, so that the influence of all stiffness coupling terms would be included.

In all cases, a single 1000-pound 2/rev main rotor vertical excitation force was applied and the vertical response of the pilot's seat was calculated. Unless otherwise stated, all Vincent circle calculations were performed assuming 2-percent uniform structural damping.

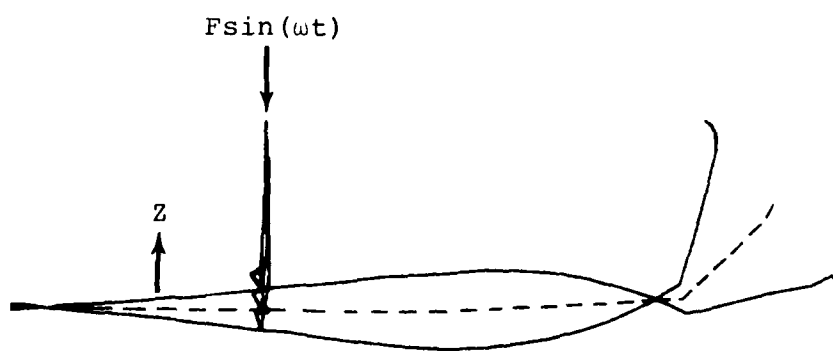


Figure 6. Elastic-line model 2/rev forced response mode shape.

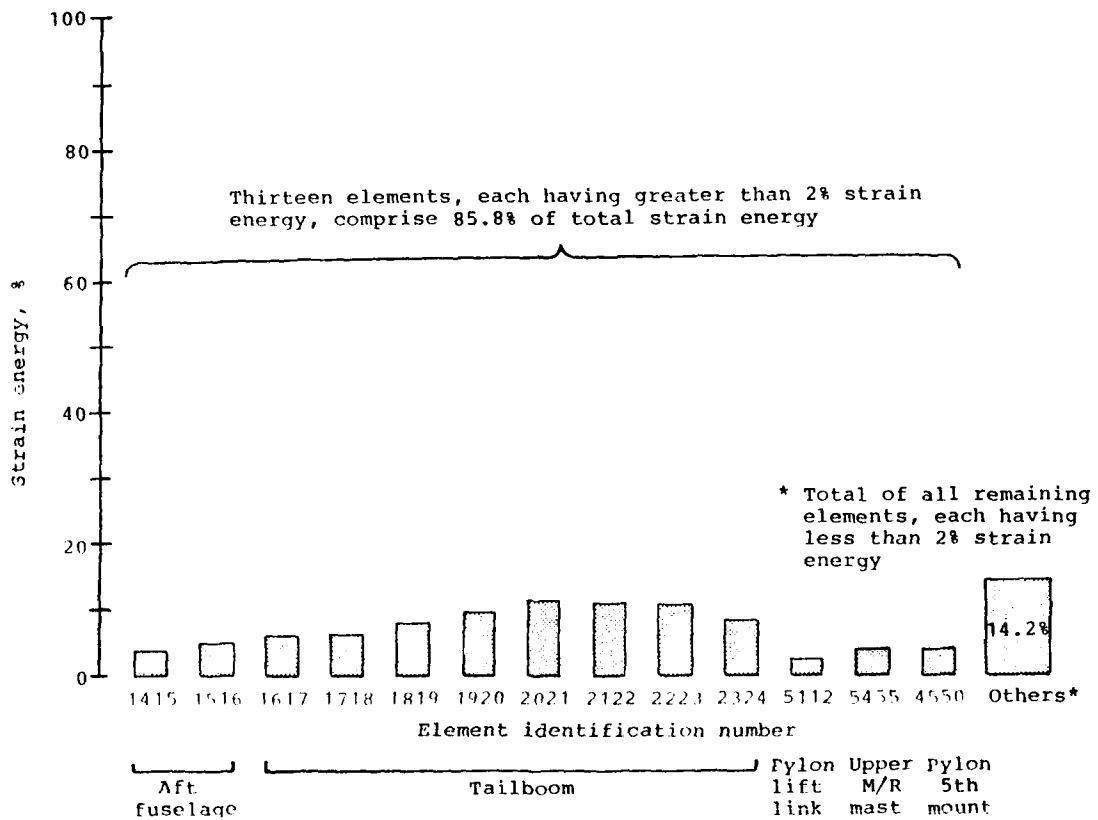


Figure 7. Elastic-line model forced response strain energy distribution.

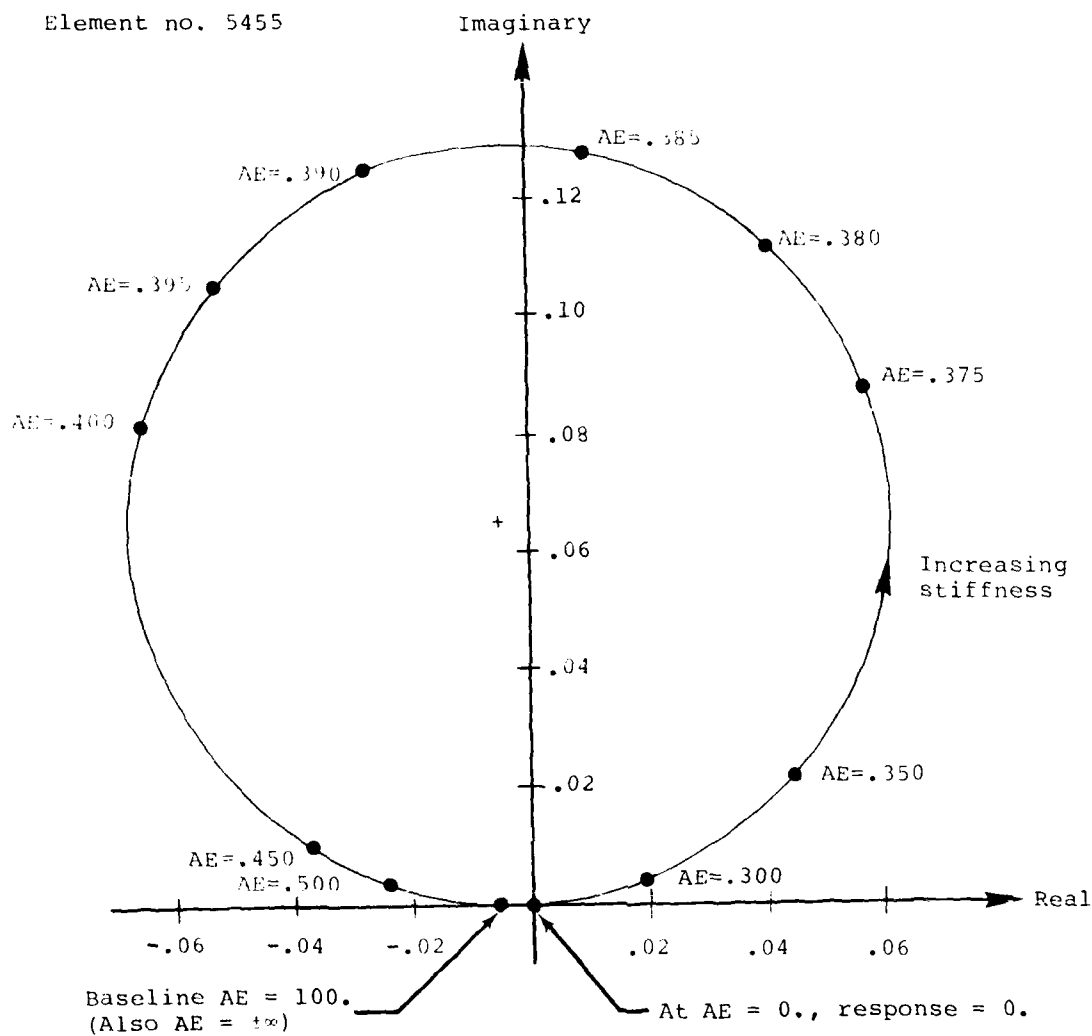
The first application of this method was to verify the circular response property using the elastic-line model. This was accomplished by evaluation of the AE axial stiffness parameter for the upper main rotor mast segment, as shown in Figure 8. Of particular significance are the zero response at zero stiffness and the sensitivity of response to stiffness variations. The zero response at zero stiffness occurs since the main rotor mast provides the only load path. The baseline stiffness value of the element indicates a low initial amplification factor, and the response is seen to be relatively insensitive to stiffness variations except for drastic changes over a very small range of values where, in reality, the element stiffness is the single parameter responsible for the resonance condition. Since the applied load was directed straight down the mast axis, only the mast AE stiffness parameter was evaluated.

With the circular response property thus verified, the remainder of the thirteen elements showing significant forced response strain energies were evaluated for Vincent circle properties of circle diameter and center location. In each case, all parameters were maintained at their original baseline values except for the particular stiffness parameter under investigation. Aft fuselage and tailboom elements were evaluated separately for both AE and vertical EI stiffness parameter variations. It was found that element AE parameter changes produced a response circle which included the baseline AE stiffness response point, as previously shown for element 5455 in Figure 8. Changes in the element EI parameter were found to produce another response circle, but one that was offset from the baseline EI stiffness response point. Further investigations showed that this offset of the EI response circle was due to the I associated stiffness coupling between beam transverse deflection and beam bending (slope change) degrees-of-freedom. This stiffness coupling offset effect was found to be most pronounced for element 1415 (Figure 9). The pylon lift link, element 5112, and the pylon 5th mount, element 4550, are analogous to axially loaded pin-ended rods so that only AE stiffness parameters were evaluated.

The response circle diameter indicates the maximum response change possible due to a particular element stiffness parameter. A normalized circle diameter distribution is shown in Figure 10. Figure 11 shows the maximum reduction in response due to each element stiffness parameter as determined from its circle diameter and center location. In the case of elements evaluated for both AE and EI stiffness parameters, the parameter providing the maximum reduction in response was selected. Note that the trend of element effectiveness established in Figure 10 is similar to that depicted in Figure 11.

Simple elastic line model with 2% uniform structural damping

Element no. 5455



pilot's seat response, inches

Figure 8. Vincent circle plot for upper main rotor mast segment.

Simple elastic line model with 2% uniform structural damping

Element no. 1415

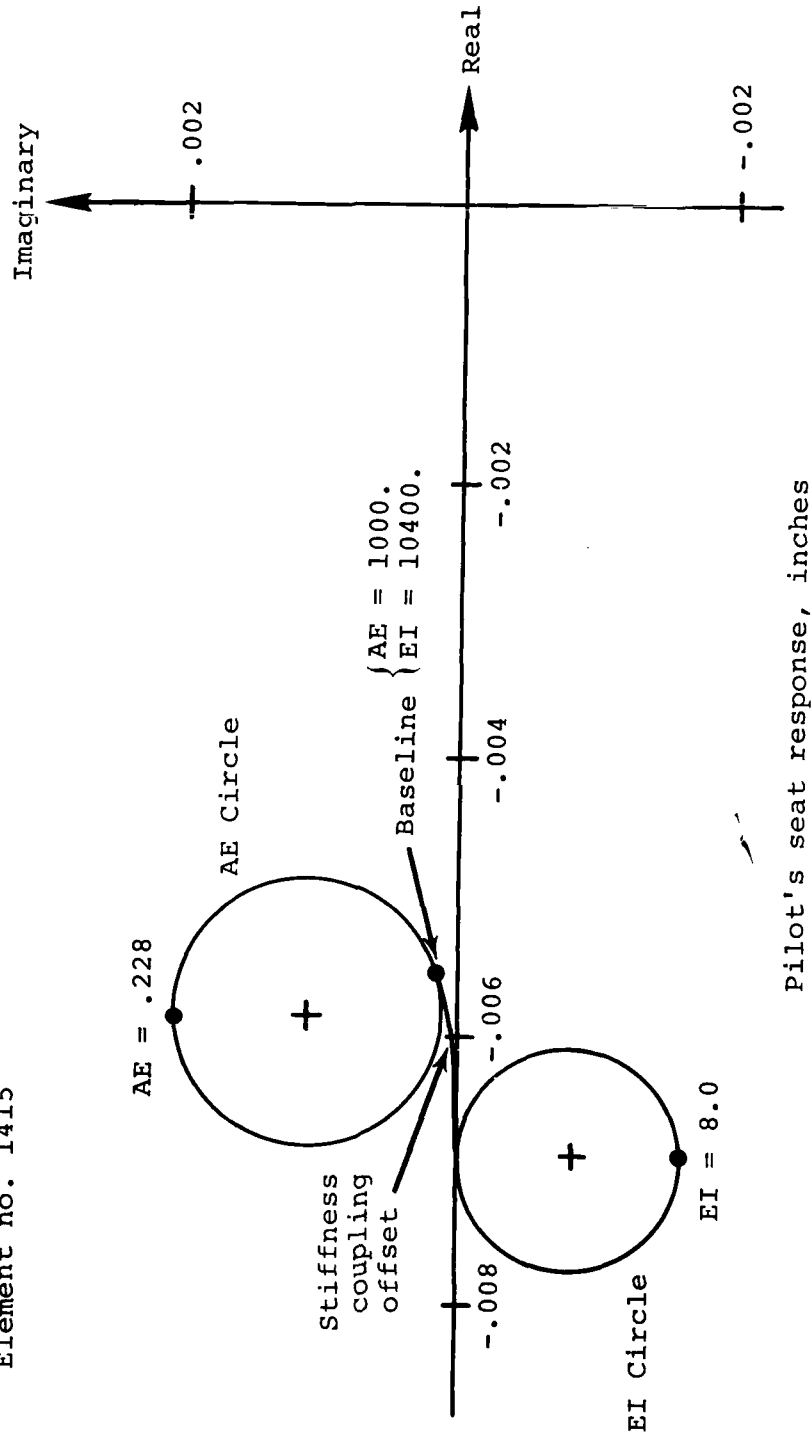


Figure 9. Vincent circle plots for aft fuselage segment.

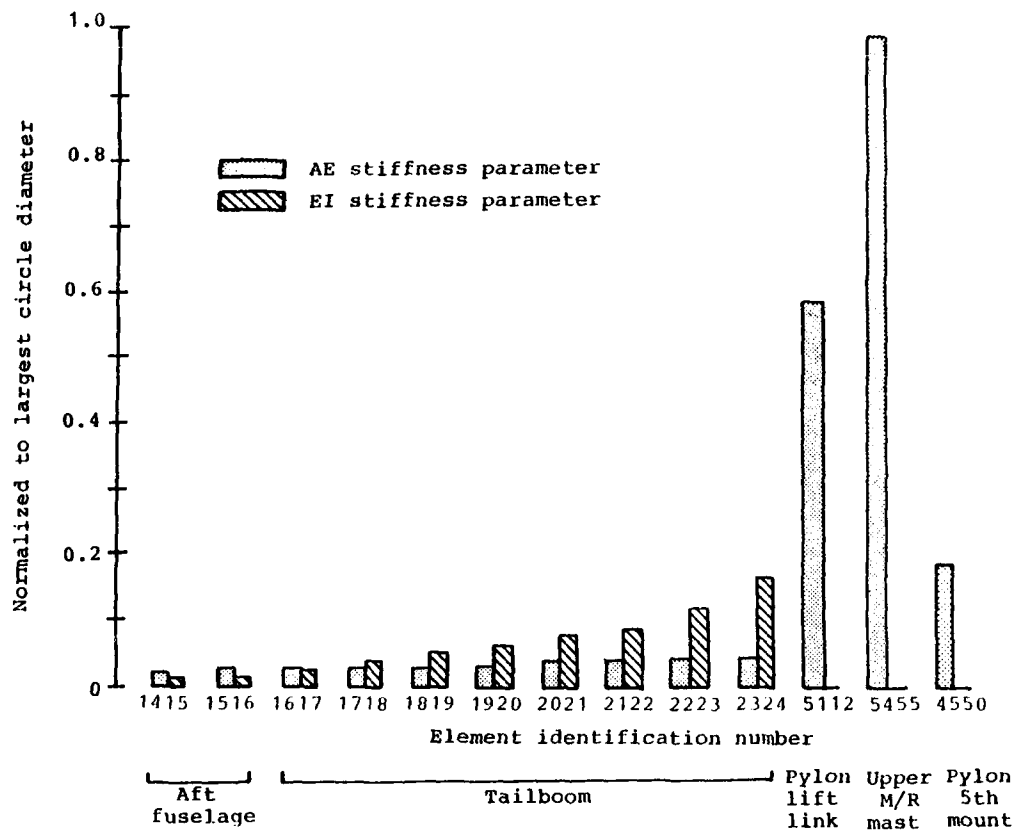


Figure 10. Elastic-line model Vincent circle diameter distribution for pilot's seat response.

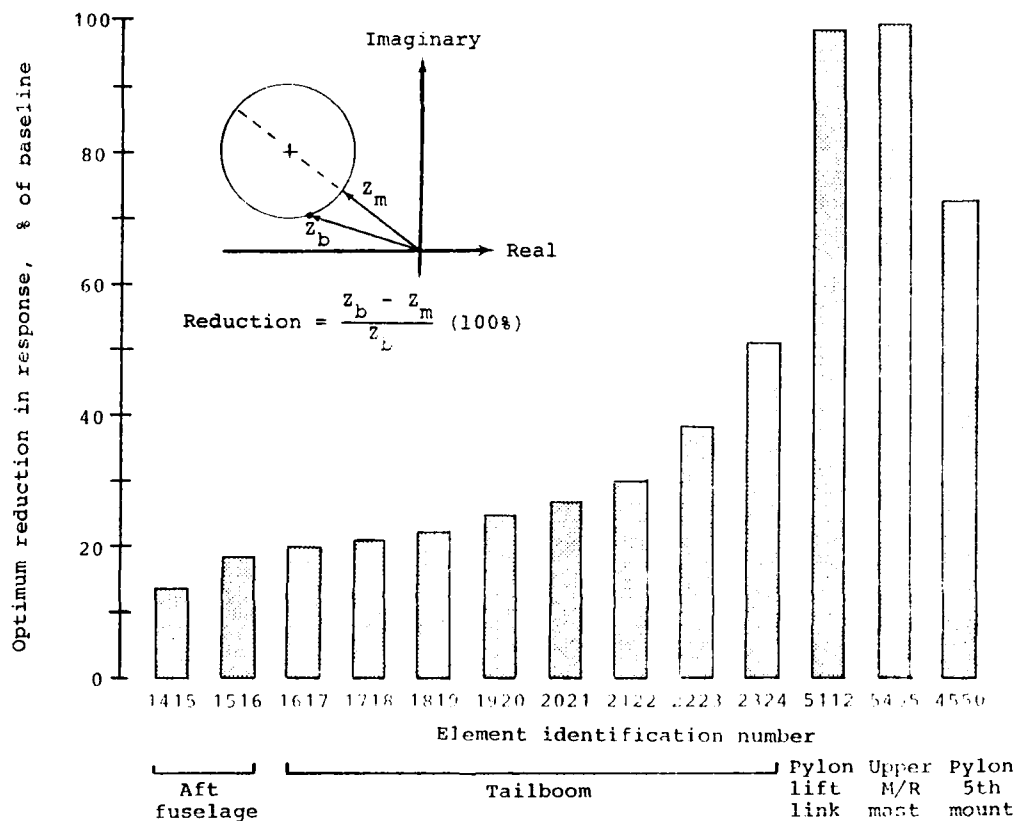


Figure 11. Elastic-line model optimum pilot's seat vibration reduction based on Vincent circle properties.

In other words, in this application the elements with the largest response circle diameters are also capable of achieving the minimum response; however, this is not to be construed as true in all cases.

The most important result to be pointed out is that the Vincent circle properties of circle diameter and center-of-location in the complex plane clearly can be used to determine the minimum response attainable for a particular stiffness parameter; however, no information is provided as to what stiffness value is required to achieve this minimum response. Table 2 shows the drastic and unrealistic stiffness values that were required to produce both the minimum and the maximum pilot's seat vertical response points on the response circle defined by each element stiffness parameter. The two cases where negative stiffnesses are indicated occurred because several elements provided parallel load paths so that a negative stiffness in one element was required to sufficiently reduce the combined elements positive stiffness resultant. In most cases, there is very little difference between the element stiffness values at minimum response and at maximum response (with exceptions for elements 1415, 1516, and 1617 due to their EI response circle offsets (see Figure 9)). Figure 12 further illustrates the stiffness nonlinearity around the response circle by depicting the typical stiffnesses generally found to describe the majority of the circular response region. This inherent property can be somewhat rationalized by considering a single degree-of-freedom model where the dynamic amplification is greatest for the resonance condition and decreases rapidly as the natural frequency is shifted either higher or lower than the excitation frequency.

Strain Energy/Vincent Circle Comparison

Figure 13 compares the undamped forced response strain energy distribution to the 2-percent damped Vincent circle diameter distribution for the same elements of the elastic-line model. Here again, where multiple stiffness parameters were evaluated for the same element, the stiffness parameter producing the largest circle diameter was chosen. It is seen that the Vincent circle method does not give the same distribution picture as the forced response strain energy method. The forced response strain energy method points to the tailboom as the area most responsible for dynamic amplification due to elastic deformation, while the Vincent

TABLE 2. ELASTIC-LINE MODEL ELEMENT STIFFNESS VALUES FOR MINIMUM AND MAXIMUM PILOT'S SEAT RESPONSE

Element No.	Stiffness Parameter Type	% of Baseline Stiffness	
		Minimum Response	Maximum Response
1415	AE	.021%	.024%
	EI	100%	.071%
1516	AE	.011%	.013%
	EI	100%	.027%
1617	AE	.190%	.213%
	EI	100%	.015%
1718	AE	.181%	.206%
	EI	.020%	.021%
1819	AE	.190%	.210%
	EI	.024%	.028%
1920	AE	.168%	.188%
	EI	.027%	.031%
2021	AE	.152%	.168%
	EI	.035%	.041%
2122	AE	.123%	.139%
	EI	.036%	.043%
2223	AE	.115%	.132%
	EI	.056%	.071%
2324	AE	.104%	.118%
	EI	.109%	.190%
5112	AE	-.775%	-.570%
5455	AE	0%	.387%
4550	AE	-167%	-147%

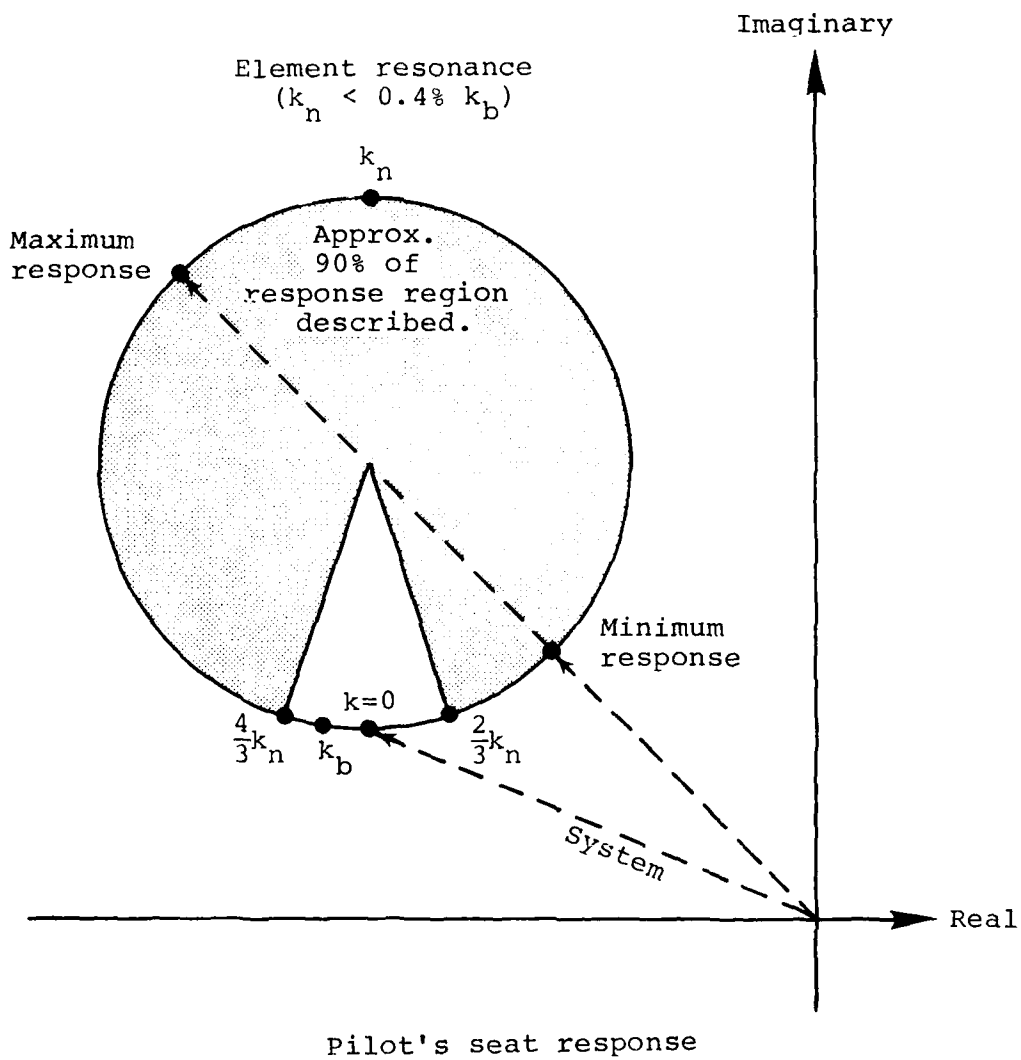


Figure 12. Typical sensitivity of Vincent circle response region.

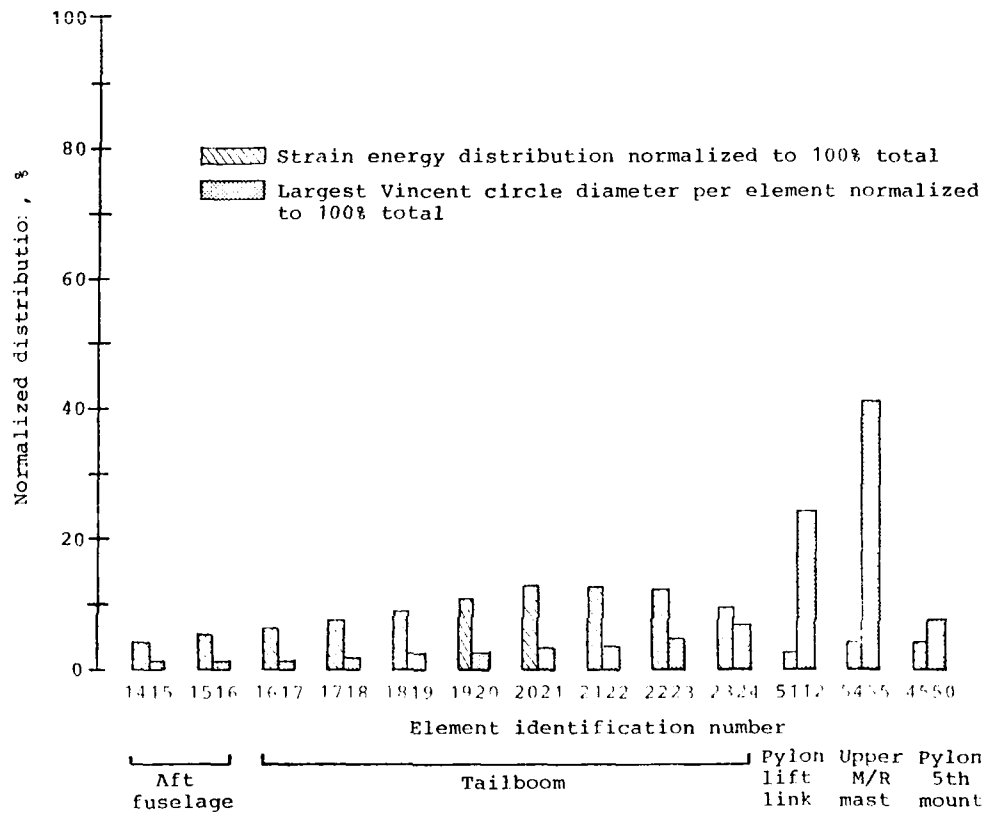


Figure 13. Forced response strain energy comparison to Vincent circle.

circle method points to the pylon as the area having the most potential for reducing vibration at the pilot's seat.

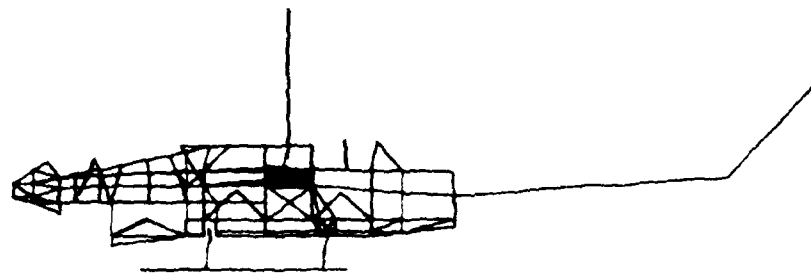
The pylon elements indicated by the Vincent circle method to have the greatest potential for reducing vibration were further evaluated. It was found, as might be strongly suspected from the previous discussion of results, that stiffness variations for these pylon elements within the established confines of the 0.5 to 10 stiffness factor range, even if done collectively, yielded virtually no substantial change in response at the pilot's seat. However, stiffness changes of this same magnitude applied to those tailboom elements initially undergoing substantial elastic deformation, as indicated by the forced response strain energy method, were found to produce significant changes in response at the pilot's seat. Therefore, the forced response strain energy method was determined to be better adapted for vibration reduction through structural stiffness optimization by indicating which structural elements are responsible for the initial dynamic amplification; it was also determined that realistic structural stiffness changes in these elements can efficiently alter the vibration characteristics of the structure.

BUILT-UP MODEL VIBRATION OPTIMIZATION

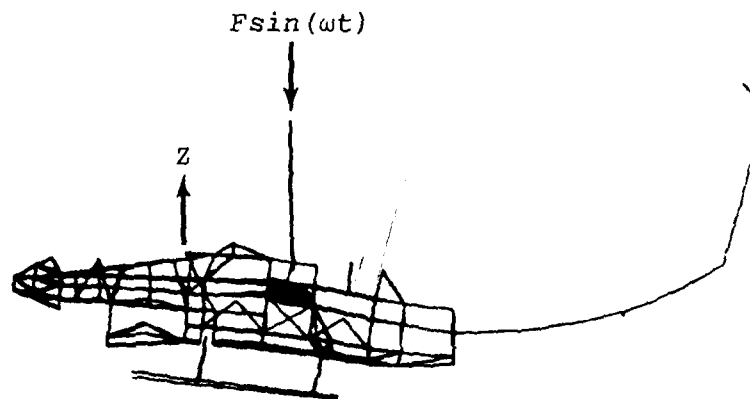
At this point in the investigations, the selected forced response strain energy method was applied to a large complex built-up NASTRAN model (Figure 5).

A NASTRAN-generated plot of a side view of the built-up model forced response vertical deformation mode shape is shown in Figure 14. The resultant undamped forced response strain energy distribution as compared to the distribution for the elastic-line model is shown in Figure 15. The elastic-line model element identification numbers were retained on the figure for reference. Note the similarity of the two distributions. In the case of the aft fuselage and main rotor mast elements, the single element representation of the elastic-line model has been replaced in the built-up model by more detailed modeling involving many elements more uniformly sharing the load, and each accounts for a smaller percentage of the total strain energy.

Previous analyses⁶ have verified that the most dynamically efficient structure for a given mode of vibration is one with a uniform energy distribution. Therefore, the most efficient structural stiffness modifications incorporated for pilot's seat vibration reduction should also result in a more uniform strain energy distribution.



Undeformed shape



Deformed shape

Figure 14. Built-up model 2/rev forced response mode shape.

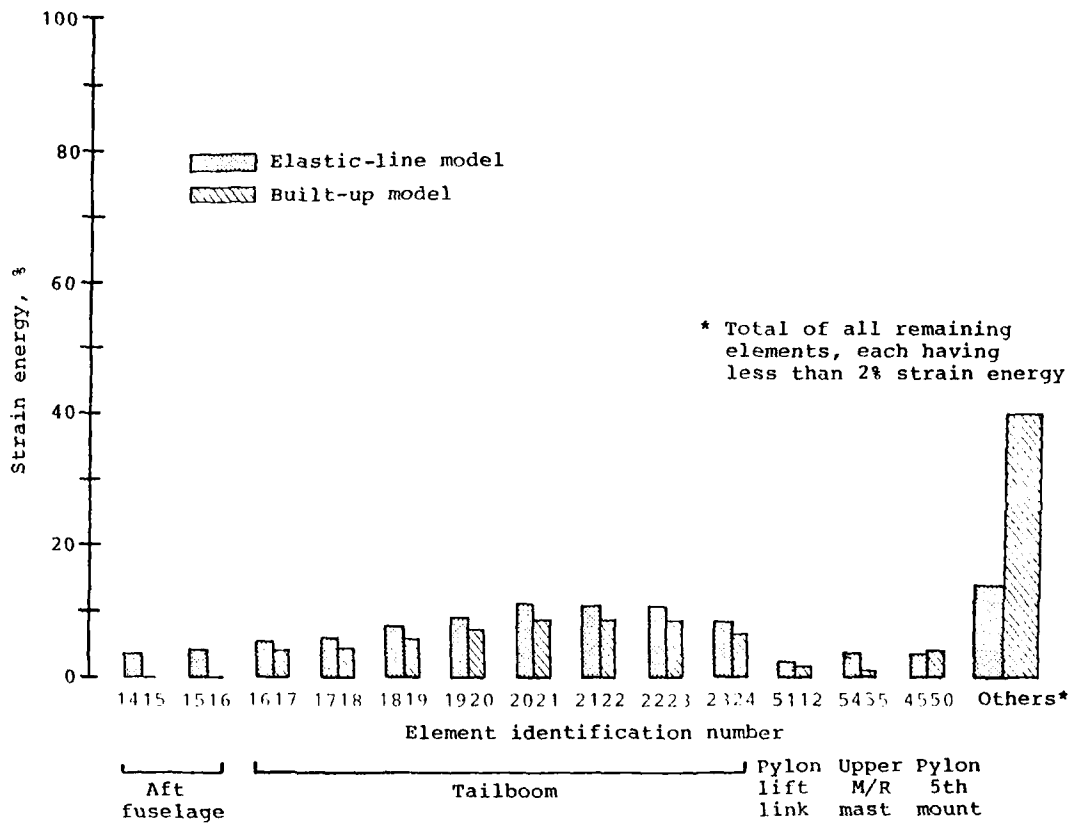


Figure 15. Comparison of forced response strain energy distributions.

From the baseline forced response strain energy distribution, the tailboom elements are seen to possess the most strain energy and were selected as the best candidates for stiffness modifications. The first step was to evaluate both extremes of the selected practical stiffness criterion range. For the stiffer case, the tailboom element with the most strain energy was made ten times stiffer, and the other tailboom elements were made stiffer according to their baseline strain energy ratio. For the softer case, the tailboom element with the least strain energy was made one-half as stiff, and the other tailboom elements were reduced in stiffness according to their baseline strain energy ratio (an additional criterion had to be imposed here - the resultant element stiffness could not be increased because of this strain energy ratio scheme used). The strain energy ratio scheme is shown in further detail in Table 3, along with the accompanying results. In both of these cases the resultant strain energies are more uniformly distributed. In both cases, the pilot's seat response increased in magnitude, but for the stiffer case the response changed phase. This result indicates that a proper stiffness increase, being within the selected practical stiffness criterion range, would result in an absolute zero response at the pilot's seat. Two additional stiffness iterations were required to achieve the desired results. In each case the selected stiffness ratio was applied to tailboom element number 4014220 (largest baseline strain energy) and the other tailboom elements were made stiffer according to their baseline strain energy ratio. As shown in Table 3, it was found that a maximum stiffness increase of 375 percent resulted in near zero response at the pilot's seat and reduced the total strain energy in the tailboom by 46 percent. This also resulted in a slight increase in the strain energies of the two tailboom elements nearest the fuselage. Additional selective stiffening of the tailboom could, no doubt, produce the same zero response results with a more uniform strain energy distribution; however, as it was not the purpose of this study to develop a general optimization procedure, further investigations in this area were not pursued.

A better interpretation of these results may be gained from examination of the simplified forced response mode shapes shown in Figure 16. Here it can easily be seen how the deformed mode shape was altered through the stiffness modifications to place the pilot's seat at a node point.

Although in the foregoing analysis it was possible to achieve zero dynamic response at a particular point under a unique set of circumstances, in no way should these results be interpreted as implying that zero response is always attainable

TABLE 3. BUILT-UP MODEL PILOT'S SEAT VIBRATION REDUCTION

Tailboom Element Identification Number	Baseline		Maximum (SE) _j Made 10X Stiffer		Minimum (SE) _j Made 0.5X Stiffer		Optimized For Minimum Response	
	Unitized Stiffness Ratio	Strain Energy (SE) _j (%)	Stiffness Ratio Applied S _j	Resulting Strain Energy (%)	Stiffness Ratio Applied S _j	Resulting Strain Energy (%)	Stiffness Ratio Applied S _j	Resulting Strain Energy (%)
(1617) 3-D Built-Up Model (Ref)	1.0	4.06	4.72	2.59	0.63	3.69	2.24	5.50
(1718)	1.0	4.50	5.23	2.11	0.70	4.00	2.49	4.61
(1819)	1.0	5.72	6.65	1.71	0.89	4.31	3.16	3.84
(1920)	1.0	7.10	8.26	1.41	1.0	5.03	3.92	3.27
(2021)	1.0	8.49	9.87	1.20	1.0	6.31	4.69	2.85
(2122)	1.0	8.60	10.0	1.02	1.0	6.68	4.75	2.50
(2223)	1.0	8.36	9.72	0.91	1.0	6.75	4.62	2.23
(2324)	1.0	3.23	3.76	0.80	0.50	5.36	1.78	2.04
	1.0	3.31	3.85	0.72	0.51	5.48	1.83	1.88
Totals =		53.37	12.47			47.61		28.77
1st Fus. vert. mode	7.94 hz		10.58 hz		7.49 hz		9.94 hz	
Pilot's seat response	-.005508 in		.022153 in		-.005874 in		-.000003 in	

$$S_j = \frac{(SE)_j}{8.60} (10.) \quad S_j = \frac{(SE)_j}{3.23} (0.5) \quad S_j = \frac{(SE)_j}{8.60} (4.75)$$

$$\{S_j = 1.0\}$$

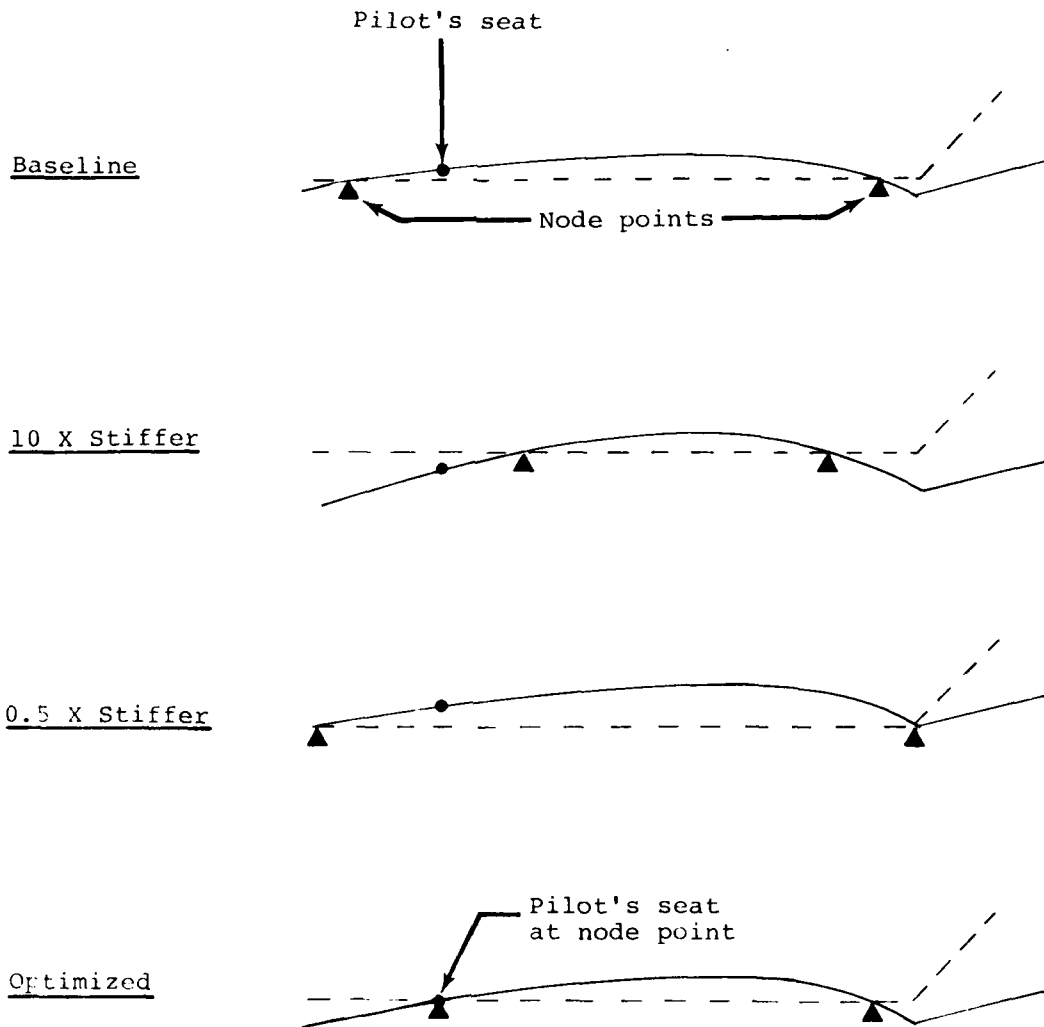


Figure 16. Simplified built-up model forced response mode shapes showing vibration optimization process.

through any type of structural modification. As previously explained in the introduction, many factors need to be considered. Also, for the purposes of this study, no change in mass was considered for any of the stiffness changes evaluated. One of the next most logical steps necessary for any realistic vibration optimization program would be to evaluate the combined effects of both stiffness and the associated weight change. The end product is, of course, a minimum vibration environment obtained through optimization of a structure within a given set of practical criteria.

FURTHER EVALUATION OF THE VINCENT CIRCLE

The Vincent circle phenomenon was further evaluated for mass tuning, damping, and dynamic absorber parameters using the elastic-line model and a simple add-on single degree-of-freedom spring-mass-damper system.

MASS PARAMETER RESULTS

Element mass parameter changes were found to describe the same circle that stiffness changes produce, only the increasing mass traced out the circle in the opposite direction. Data points on the example shown in Figure 17 have been somewhat exaggerated for clarity.

DAMPING PARAMETER RESULTS

Damping is usually not considered as a practical method of effectively altering airframe structural vibration. As shown in Figure 18, both the maximum amplification and the potential of the element for vibration control are greatly reduced by small increases in element damping.

DYNAMIC ABSORBER PARAMETER RESULTS

The adopted procedure for investigating dynamic absorber parameters was to evaluate the effectiveness of one absorber for attenuating 2/rev vertical vibration at the pilot's seat when placed at different locations on the structure; and then, to compare these results to the maximum reductions in pilot's seat response obtained from element stiffness Vincent circle properties at these same locations (as described in Figure 11). The adopted approach does not imply that any such relation between Vincent circle predictions and optimum dynamic absorber locations exists, or has been reported to exist.

The dynamic absorber energy absorption potential was kept constant by maintaining a 25-pound absorber mass and a 0.2% absorber damping coefficient. This required several absorber spring stiffness iterations to achieve the proper tuning of the dynamic absorber at each location due to the different boundary conditions (i.e., backup structure stiffness) which exists throughout the structure. In each case the dynamic absorber was positioned in the vertical direction for reducing pilot's seat vertical vibration. For this study seven dynamic absorber locations were evaluated and the results are shown in Figure 19 as compared to the maximum response reduction distribution obtained from the element stiffness Vincent circle properties.

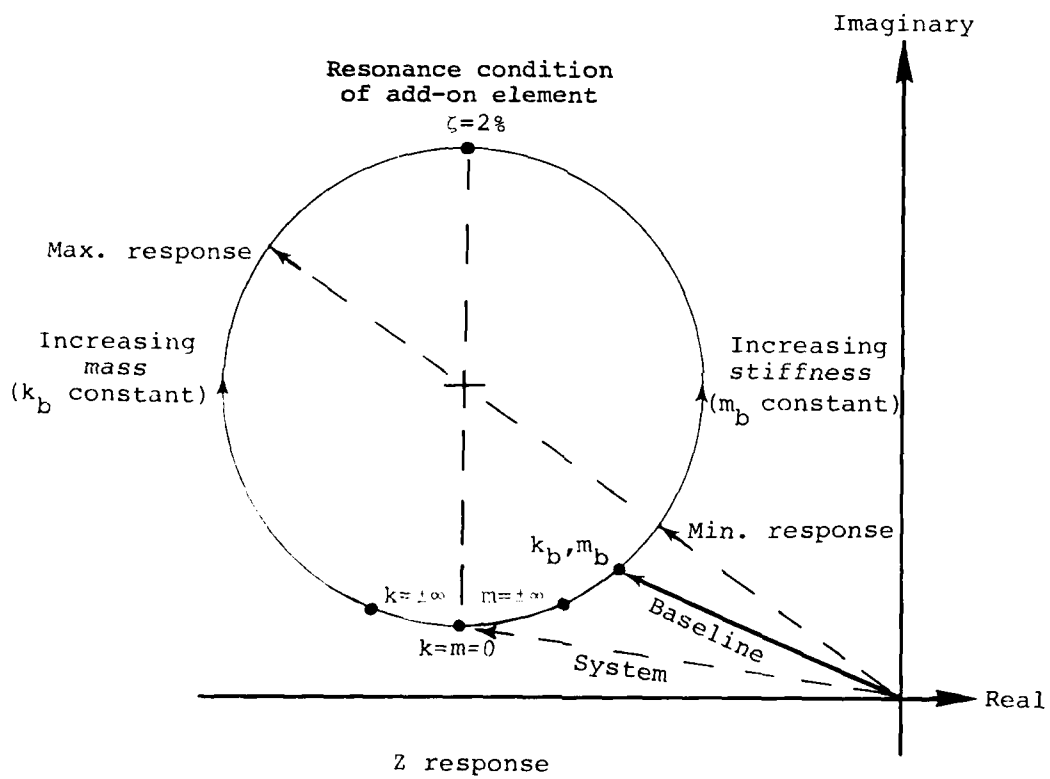
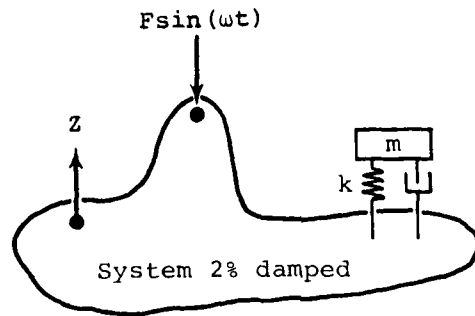


Figure 17. Typical Vincent circle stiffness/mass response region relationships.

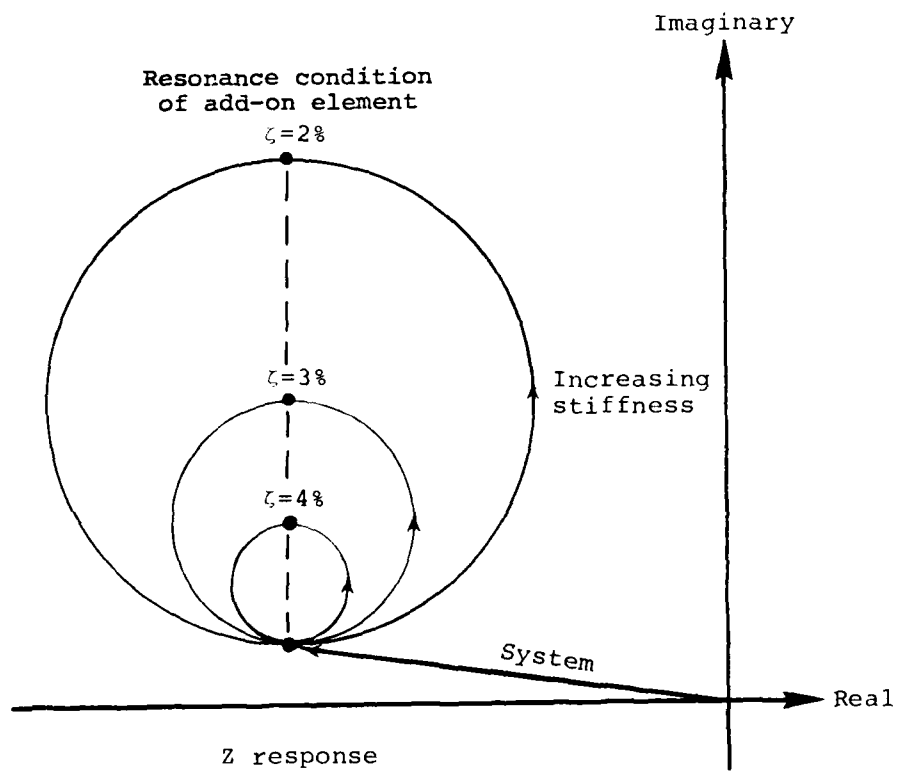
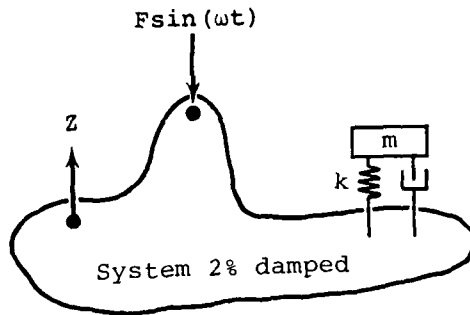


Figure 18. Effect of damping on typical Vincent circle response region.

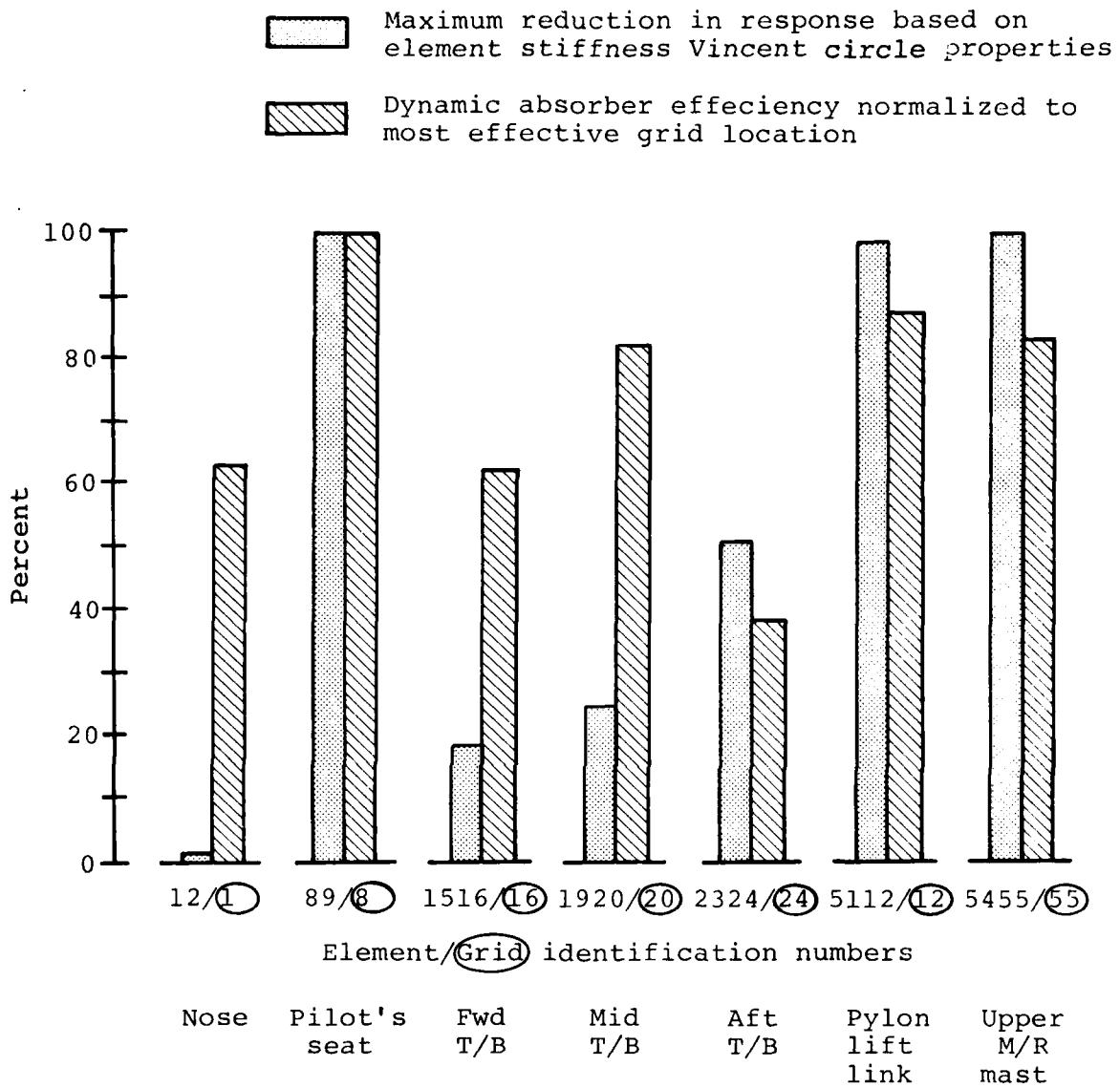


Figure 19. Comparison of Vincent circle properties to dynamic absorber location effectiveness for reducing pilot's seat vibration.

Examination of the dynamic absorber location effectiveness shows that the most efficient location for reducing pilot's seat vibration is at the pilot's seat; but, it also shows that a remote absorber located either at the top of the main rotor mast (grid 55), at the pylon lift link (grid 12), or at the middle of the tailboom (grid 20), would also be significantly effective for reducing vibration at the pilot's seat.

Use of the Vincent circle properties shows that both elements 89 and 5455 are capable of reducing the pilot's seat vibration by 100%. However, these results are inconclusive because any element providing the only load path is ultimately capable of reducing the pilot's seat response to zero if its stiffness is reduced to zero. Further examination of the comparisons shown in Figure 19 shows no definite trends to indicate that the Vincent circle method can be applied to predict optimum dynamic absorber locations.

CONCLUSIONS

The Vincent circle property of a circular response region has been examined and verified by straightforward linear analysis. This property would certainly be of value to the dynamicist for evaluation of a localized portion of structure known to be in, or very near, resonance and which could be controlled by changes involving only a few parameters.

However, for vibration reduction through optimization of an airframe structure where many elements are involved, the forced response strain energy method was found to be more suitable than the Vincent circle method by indicating which structural elements are most responsible for the elastic dynamic amplification. Practical parameter modifications of these elements will most significantly alter the airframe structural dynamic characteristics to reduce vibration. For the more detailed analysis involving complex applied loads, phasing, and damping, the damped forced response strain energy method has the potential benefit of rapid evaluation and optimization of structural vibratory response, which would be particularly beneficial in the predesign stages of an aircraft.

REFERENCES

1. Vincent, A. H., A NOTE ON THE PROPERTIES OF THE VARIATION OF STRUCTURAL RESPONSE WITH RESPECT TO A SINGLE STRUCTURAL PARAMETER WHEN PLOTTED IN THE COMPLEX PLANE, Westland Helicopters Limited Report GEN/DYN/RES/010R, Yeovil, Somerset, England, September 1973.
2. Done, G. T. S., and Hughes, A. D., THE RESPONSE OF A VIBRATING STRUCTURE AS A FUNCTION OF STRUCTURAL PARAMETERS, Journal of Sound and Vibration, Vol. 38, No. 2, 1975, pp. 255-266.
3. Done, G. T. S., and Hughes, A. D., REDUCING VIBRATION BY STRUCTURAL MODIFICATION, Vertica, Vol. 1, No. 1, 1976, pp. 31-38, (paper presented at the First European Rotorcraft and Powered Lift Aircraft Forum at Southampton, September 22-24, 1975).
4. Done, G. T. S., Hughes, A. D., and Webby, J., THE RESPONSE OF A VIBRATING STRUCTURE AS A FUNCTION OF STRUCTURAL PARAMETERS - APPLICATION AND EXPERIMENT, Journal of Sound and Vibration, Vol. 49, No. 2, 1976, pp. 149-159.
5. Balmford, D. E. H., THE CONTROL OF VIBRATION IN HELICOPTERS, Aeronautical Journal, Vol. 81, No. 794, February 1977, pp. 63-67.
6. Sciarra, J. J., USE OF THE FINITE ELEMENT DAMPED FORCED RESPONSE STRAIN ENERGY DISTRIBUTION FOR VIBRATION REDUCTION, Boeing-Vertol Company Report D210-10819-1, U.S. Army Research Office - Durham, Durham, North Carolina, July 1974.
7. THE NASTRAN USER'S MANUAL, NASA SP-222(03) National Aeronautics and Space Administration, Washington, D. C. July 1976.
8. Cronkhite, J. D., and Wilson, W. F., DYNAMIC ANALYSIS OF TWO-PER-REV VIBRATIONS IN THE MODEL AH-1J HELICOPTER - PIP Task No. AH-8-123, Bell Helicopter Textron Report 299-100-021, Fort Worth, Texas, 4 February 1972.
9. Cronkhite, J. D., XM-97 (20MM) WEAPON ON THE AH-1G - PRELIMINARY DYNAMIC ANALYSIS, Bell Helicopter Textron Inter-office Memo 81:JDC:mb-054, Fort Worth, Texas, 29 May 1973.

10. Cronkhite, J. D., Berry, V. L., and Brunken, J. E., A NASTRAN VIBRATION MODEL OF THE AH-1G HELICOPTER AIR-FRAME, U. S. Army Armament Command Report No. R-TR-64-45, Research Directorate, Gen. Thomas J. Rodman Laboratory, Rock Island Arsenal, Rock Island, Illinois, June 1974.

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GR ID	32	520.67	14.10	118.27					
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GR ID	34	196.575	-42.5	61.226					
GR ID	35	194.230	-30.0	60.498					
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GR ID	38	194.230	30.0	60.498					
GR ID	39	196.575	42.5	61.226					
GR ID	40	199.858	60.0	62.246					
GR ID	41	189.94	-12.375	77.57					
GR ID	42	189.94	12.375	77.57					
GR ID	43	211.72	-12.375	77.57					
GR ID	44	211.72	12.375	77.57					
GR ID	45	214.50	0.0	77.57					
GR ID	46	189.94	-12.375	77.57					
GR ID	47	189.94	12.375	77.57					
GR ID	48	211.72	-12.375	77.57					
GR ID	49	211.72	12.375	77.57					
GR ID	50	214.50	0.0	77.57					
GR ID	51	200.0	0.0	83.8					
GR ID	52	200.0	0.0	77.2					
GR ID	53	200.0	0.0	98.0					
GR ID	54	200.0	0.0	115.0					
GR ID	55	200.0	0.0	153.0					
GR ID	60	248.0	0.0	86.0					
CHAR	12	1	2	0.0	1.0	0.0	1		
CHAR	23	2	3	0.0	1.0	0.0	1		
CHAR	34	3	4	0.0	1.0	0.0	1		
CHAR	45	4	5	0.0	1.0	0.0	1		
CHAR	46	4	6	0.0	1.0	0.0	1		
CHAR	67	6	7	0.0	1.0	0.0	1		
CHAR	78	7	8	0.0	1.0	0.0	1		
CHAR	89	8	9	0.0	1.0	0.0	1		
CHAR	910	9	10	0.0	1.0	0.0	1		
CHAR	1011	10	11	0.0	1.0	0.0	1		
CHAR	1112	11	12	0.0	1.0	0.0	1		
CHAR	1213	12	13	0.0	1.0	0.0	1		
CHAR	1314	13	14	0.0	1.0	0.0	1		
CHAR	1415	14	15	0.0	1.0	0.0	1		
CHAR	1516	15	16	0.0	1.0	0.0	1		
CHAR	1617	16	17	0.0	1.0	0.0	1		
CHAR	1718	17	18	0.0	1.0	0.0	1		
CHAR	1819	18	19	0.0	1.0	0.0	1		
CHAR	1920	19	20	0.0	1.0	0.0	1		
CHAR	2021	20	21	0.0	1.0	0.0	1		
CHAR	2122	21	22	0.0	1.0	0.0	1		
CHAR	2223	22	23	0.0	1.0	0.0	1		
CHAR	2324	23	24	0.0	1.0	0.0	1		

20MM GUN

PILOT

T/R HUB

XMSN

M/R HUB
ENGINE

CBAR	2425	2425	24	25	0.0	1.0	0.0	1	
CBAR	2526	2526	25	26	0.0	1.0	0.0	1	
CBAR	2627	2627	26	27	0.0	1.0	0.0	1	
CBAR	2728	2728	27	28	0.0	1.0	0.0	1	
CBAR	2829	2829	28	29	0.0	1.0	0.0	1	
CBAR	2930	2930	29	30	0.0	1.0	0.0	1	+2930
+2930			0.0	0.0	0.0	-1.57	0.0	1	-5.21
CBAR	3031	3031	30	31	1.0	0.0	0.0	1	+3031
+3031	56								
CBAR	3132	3132	31	32	1.0	0.0	0.0	1	
CRIGD2	30310	30	31	33					
CBAR	3334	3334	33	34	1.0	0.0	0.0	1	
CBAR	3435	3435	34	35	1.0	0.0	0.0	1	
CBAR	3536	3536	35	36	1.0	0.0	0.0	1	
CBAR	3612	3612	36	12	1.0	0.0	0.0	1	+3612
+3612			0.0	0.0	0.0	-4.798	0.0	1	9.868
CBAR	1237	1237	12	37	1.0	0.0	0.0	1	+1237
+1237			-4.798	0.0	0.0	9.868	0.0	1	0.0
CBAR	3738	3738	37	38	1.0	0.0	0.0	1	
CBAR	3839	3839	38	39	1.0	0.0	0.0	1	
CBAR	3940	3940	39	40	1.0	0.0	0.0	1	
CRIGD1	1240	12	41	42	43	44	45		
CRIGD1	5140	51	46	47	48	49	50		
CBAR	5112	5112	51	12	0.0	1.0	0.0	1	+LIFTLNK
+LIFTLNK			-3.10	0.0	-7.90	-0.1	0.0	1	16.15
CELAS1	41461	1	41	1	46	2			
CELAS1	41462	2	41	2	46	3			
CELAS1	41463	3	41	3	46	3			
CELAS1	42471	1	42	1	47	1			
CELAS1	42472	2	42	2	47	2			
CELAS1	42473	3	42	3	47	3			
CELAS1	43481	1	43	1	48	1			
CELAS1	43482	2	43	2	48	2			
CELAS1	43483	3	43	3	48	3			
CELAS1	44491	1	44	1	49	1			
CELAS1	44492	2	44	2	49	2			
CELAS1	44493	3	44	3	49	3			
CELAS1	45503	33	45	3	50	3			
CRIGD2	515253	51	52	123456	53	12			
CBAR	5253	5253	52	53	0.0	1.0	0.0	1	+5253
+5253	56								
CBAR	5354	5354	53	54	0.0	1.0	0.0	1	
CBAR	5455	5455	54	55	0.0	1.0	0.0	1	
CRIGD1	1460	14	60						
PBAR	12	1	1000.	1650.	250.	200.			
PBAR	23	1	1000.	3300.	700.	200.			
PBAR	34	1	1000.	5350.	1100.	200.			
PBAR	45	1	1000.	5800.	1100.	225.			
PBAR	67	1	1000.	7300.	2750.	850.			
PBAR	78	1	1000.	7300.	3000.	850.			
PBAR	89	1	1000.	7300.	3200.	850.			
PBAR	910	1	1000.	9750.	8200.	2000.			
PBAR	1011	1	1000.	12750.	14710.	3250.			
PBAR	1112	1	1000.	18000.	14710.	3150.			
PBAR	1213	1	1000.	18000.	14710.	3150.			
PBAR	1314	1	1000.	13900.	11670.	2900.			
PBAR	1415	1	1000.	12100.	10400.	2650.			
PBAR	1516	1	1000.	8850.	9300.	2100.			
PBAR	1617	1	42.7403	5138.39	6244.61	3326.62			
PBAR	1718	1	47.4632	4686.89	6300.05	2387.82			
PBAR	1819	1	41.4892	3376.80	4650.61	1863.98			
PBAR	1920	1	38.7424	2797.46	3323.30	1422.92			
PBAR	2021	1	37.5606	2419.04	2301.92	1113.34			
PBAR	2122	1	36.7154	1919.77	1782.38	881.70			
PBAR	2223	1	34.7744	1418.76	1322.74	634.50			
PBAR	2324	1	35.5467	1008.00	1159.10	428.36			
PBAR	2425	1	38.50	182.6	5150.	113.5			
PBAR	2526	1	35.13	168.0	1900.	81.2			
PBAR	2627	1	32.70	152.0	1620.	69.0			
PBAR	2728	1	30.25	135.0	1540.	56.8			
PBAR	2829	1	27.85	100.0	1060.	48.5			
PBAR	2930	1	25.45	72.0	650.	43.7			
PBAR	3031	1	1000.	5.5	5.5	11.0			
PBAR	3132	1	1000.	3.5	3.5	7.0			
PBAR	3334	1	1000.	2600.	454.	230.			
PBAR	3435	1	1000.	4250.	1041.	380.			
PBAR	3536	1	1000.	8250.	1485.	560.			
PBAR	4112	1	1000.	9912.	1683.	5150.			
PBAR	1237	1	1000.	9912.	1683.	5150.			

PBAR	3738	1	1000.	8250.	1485.	560.
PBAR	3839	1	1000.	4250.	1031.	380.
PBAR	3940	1	1000.	2600.	454.	270.
PBAR	5112	1	25.R1			
PELAS	1	28125.				
PELAS	2	28125.				
PELAS	3	4500.				
PELAS	33	20000.				
PBAR	5253	1	100.	72.	72.	144.
PBAR	5354	1	100.	135.	135.	270.
PBAR	5455	1	100.	120.	120.	240.
MA11	1	1.0+6	1.0+6			
CONN2	1	1		12.029		
CONN2	2	2		34.965		
CONN2	3	3		66.882		
CONN2	4	4		198.829		
CONN2	5	5		253.4		
CONN2	6	6		439.371		
CONN2	7	7		561.594		
CONN2	8	8		355.019		
CONN2	9	9		189.893		
CONN2	10	10		714.319		
CONN2	11	11		686.484		
CONN2	12	12		125.393		
*N112	0.849+6					
CONN2	13	13		836.348		
CONN2	14	14		554.022		
CONN2	15	15		296.573		
CONN2	16	16		87.781		
CONN2	17	17		33.058		
CONN2	18	18		43.977		
CONN2	19	19		60.541		
CONN2	20	20		41.474		
CONN2	21	21		48.633		
CONN2	22	22		22.713		
CONN2	23	23		15.102		
CONN2	24	24		44.152		
CONN2	25	25		19.136		
CONN2	26	26		6.809		
CONN2	27	27		11.934		
CONN2	28	28		8.475		
CONN2	29	29		4.968		
CONN2	30	30		2.544		
CONN2	300	30		25.994		
CONN2	31	31		11.282		
CONN2	32	32		34.066		
CONN2	33	33		9.489		
CONN2	34	34		35.704		
CONN2	35	35		36.459		
CONN2	36	36		95.577		
CONN2	37	37		95.577		
CONN2	38	38		36.459		
CONN2	39	39		35.704		
CONN2	40	40		9.489		
CONN2	51	51		103.895		
CONN2	52	52		115.708		
CONN2	53	53		270.518		
CONN2	54	54		125.560		
CONN2	55	55		33.249		
CONN2	550	55		947.5		
CONN2	60	60		585.35		
*ENG	17800.		109500.		94700.	
PARAM	WTMASS	.00259				
PARAM	GRDPNT	0				
FREQ	10	10.7	10.8			
HLDAID	1000	55.3	0	0	99	0
DAHEA	55.3	55	3	1000.		
TABLED1	59					
*B(F)	0.0	1.0	200.0	1.0	ENDT	*B(F)

\$ THESE DMI MATRICES MUST BE INPUT FOR ELEMENT DYNAMIC STRAIN ENERGY						
\$ CALCULATIONS - CONSULT ALTER PACKAGE IN EXECUTIVE DECK FOR DETAILS.						
DMI	CP	0	2	1	1	1
DMI	CP	1	1	0.	2	1.
DMI	HP	0	2	1	1	1
DMI	HP	1	1	1.	2	0.

ENDATA						
END*						

*N112

*ENG

*B(F)

ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
PILOT SEAT RESPONSE TO 1000 LH 2/REV VERT HUR SHEAR

C A S E C O N T R O L D E C K E C H O

CARD COUNT	TITLE#	ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
1	SUBTITLE#	UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
2	LAHEL#	PILOT SEAT RESPONSE TO 1000 LH 2/REV VERT HUR SHFAR
3	ECHU#	10
4	FREQ#	10
5	OUTPUT	DISPXSURTI,REALK#ALL
6	ESE#	ALL
7	DLOAD#	1000
8	BEGIN	RUOK
9		
10		

CLASSIC LINE MODEL OF THE AH-1G HELICOPTER
 UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
 PILOT SEAT RESPONSE TO 1000 LB 2/REV VERT HUB SHAFT

1	2	3	4	5	6	7	8	9	10
GR10	1	1	1	1	1	1	1	1	1
GR10	2	1	1	1	1	1	1	1	1
GR10	3	1	1	1	1	1	1	1	1
GR10	4	1	1	1	1	1	1	1	1
GR10	5	1	1	1	1	1	1	1	1
GR10	6	1	1	1	1	1	1	1	1
GR10	7	1	1	1	1	1	1	1	1
GR10	8	1	1	1	1	1	1	1	1
GR10	9	1	1	1	1	1	1	1	1
GR10	10	1	1	1	1	1	1	1	1
GR10	11	1	1	1	1	1	1	1	1
GR10	12	1	1	1	1	1	1	1	1
GR10	13	1	1	1	1	1	1	1	1
GR10	14	1	1	1	1	1	1	1	1
GR10	15	1	1	1	1	1	1	1	1
GR10	16	1	1	1	1	1	1	1	1
GR10	17	1	1	1	1	1	1	1	1
GR10	18	1	1	1	1	1	1	1	1
GR10	19	1	1	1	1	1	1	1	1
GR10	20	1	1	1	1	1	1	1	1
GR10	21	1	1	1	1	1	1	1	1
GR10	22	1	1	1	1	1	1	1	1
GR10	23	1	1	1	1	1	1	1	1
GR10	24	1	1	1	1	1	1	1	1
GR10	25	1	1	1	1	1	1	1	1
GR10	26	1	1	1	1	1	1	1	1
GR10	27	1	1	1	1	1	1	1	1
GR10	28	1	1	1	1	1	1	1	1
GR10	29	1	1	1	1	1	1	1	1
GR10	30	1	1	1	1	1	1	1	1
GR10	31	1	1	1	1	1	1	1	1
GR10	32	1	1	1	1	1	1	1	1
GR10	33	1	1	1	1	1	1	1	1
GR10	34	1	1	1	1	1	1	1	1
GR10	35	1	1	1	1	1	1	1	1
GR10	36	1	1	1	1	1	1	1	1
GR10	37	1	1	1	1	1	1	1	1
GR10	38	1	1	1	1	1	1	1	1
GR10	39	1	1	1	1	1	1	1	1
GR10	40	1	1	1	1	1	1	1	1
GR10	41	1	1	1	1	1	1	1	1
GR10	42	1	1	1	1	1	1	1	1
GR10	43	1	1	1	1	1	1	1	1
GR10	44	1	1	1	1	1	1	1	1
GR10	45	1	1	1	1	1	1	1	1
GR10	46	1	1	1	1	1	1	1	1
GR10	47	1	1	1	1	1	1	1	1
GR10	48	1	1	1	1	1	1	1	1
GR10	49	1	1	1	1	1	1	1	1
GR10	50	1	1	1	1	1	1	1	1
GR10	51	1	1	1	1	1	1	1	1
GR10	52	1	1	1	1	1	1	1	1
GR10	53	1	1	1	1	1	1	1	1
GR10	54	1	1	1	1	1	1	1	1
GR10	55	1	1	1	1	1	1	1	1
GR10	56	1	1	1	1	1	1	1	1
GR10	57	1	1	1	1	1	1	1	1
GR10	58	1	1	1	1	1	1	1	1
GR10	59	1	1	1	1	1	1	1	1
GR10	60	1	1	1	1	1	1	1	1
CA02	1	1	1	1	1	1	1	1	1
CA03	1	1	1	1	1	1	1	1	1
CA04	1	1	1	1	1	1	1	1	1
CA05	1	1	1	1	1	1	1	1	1
CA06	1	1	1	1	1	1	1	1	1
CA07	1	1	1	1	1	1	1	1	1
CA08	1	1	1	1	1	1	1	1	1
CA09	1	1	1	1	1	1	1	1	1
CA10	1	1	1	1	1	1	1	1	1
CA11	1	1	1	1	1	1	1	1	1
CA12	1	1	1	1	1	1	1	1	1
CA13	1	1	1	1	1	1	1	1	1
CA14	1	1	1	1	1	1	1	1	1
CA15	1	1	1	1	1	1	1	1	1
CA16	1	1	1	1	1	1	1	1	1
CA17	1	1	1	1	1	1	1	1	1

20MM GUN
 PILOT
 T/R HUB
 XMSN
 W/R HUB ENGINE

CLASSIC LINE MODEL OF THE AH-1G HELICOPTER
UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD

PILOT SEAT RESPONSE TO 1000 1/2 REV VERT HOOD SHAK

1	2	3	4	5	6	7	8	9	10
CHAR	1718	17	14	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	1819	18	10	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	1920	19	20	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	2021	20	21	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	2122	21	22	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	2223	22	23	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	2324	23	24	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	2425	24	25	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	2526	25	26	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	2627	26	27	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	2728	27	28	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	2829	28	29	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	2930	29	30	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	3031	30	31	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	3132	31	32	1.0	0.0	0.0	0.0	0.0	0.0
CHAR	3233	32	33	1.0	0.0	0.0	0.0	0.0	0.0
CHAR	3334	33	34	1.0	0.0	0.0	0.0	0.0	0.0
CHAR	3435	34	35	1.0	0.0	0.0	0.0	0.0	0.0
CHAR	3536	35	36	1.0	0.0	0.0	0.0	0.0	0.0
CHAR	3637	36	37	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	3738	37	38	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	3839	38	39	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	3940	39	40	1.0	0.0	0.0	0.0	0.0	0.0
CHAR	4041	40	41	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	4142	41	42	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	4243	42	43	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	4344	43	44	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	4445	44	45	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	4546	45	46	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	4647	46	47	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	4748	47	48	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	4849	48	49	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	4950	49	50	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	5051	50	51	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	5152	51	52	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	5253	52	53	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	5354	53	54	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	5455	54	55	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	5556	55	56	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	5657	56	57	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	5758	57	58	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	5859	58	59	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	5960	59	60	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	6061	60	61	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	6162	61	62	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	6263	62	63	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	6364	63	64	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	6465	64	65	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	6566	65	66	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	6667	66	67	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	6768	67	68	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	6869	68	69	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	6970	69	70	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	7071	70	71	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	7172	71	72	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	7273	72	73	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	7374	73	74	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	7475	74	75	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	7576	75	76	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	7677	76	77	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	7778	77	78	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	7879	78	79	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	7980	79	80	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	8081	80	81	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	8182	81	82	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	8283	82	83	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	8384	83	84	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	8485	84	85	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	8586	85	86	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	8687	86	87	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	8788	87	88	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	8889	88	89	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	8990	89	90	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	9091	90	91	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	9192	91	92	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	9293	92	93	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	9394	93	94	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	9495	94	95	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	9596	95	96	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	9697	96	97	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	9798	97	98	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	9899	98	99	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	9900	99	100	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	10001	100	101	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	10102	101	102	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	10203	102	103	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	10304	103	104	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	10405	104	105	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	10506	105	106	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	10607	106	107	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	10708	107	108	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	10809	108	109	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	10910	109	110	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	11011	110	111	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	11112	111	112	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	11213	112	113	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	11314	113	114	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	11415	114	115	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	11516	115	116	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	11617	116	117	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	11718	117	118	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	11819	118	119	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	11920	119	120	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	12021	120	121	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	12122	121	122	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	12223	122	123	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	12324	123	124	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	12425	124	125	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	12526	125	126	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	12627	126	127	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	12728	127	128	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	12829	128	129	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	12930	129	130	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	13031	130	131	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	13132	131	132	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	13233	132	133	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	13334	133	134	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	13435	134	135	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	13536	135	136	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	13637	136	137	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	13738	137	138	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	13839	138	139	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	13940	139	140	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	14041	140	141	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	14142	141	142	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	14243	142	143	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	14344	143	144	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	14445	144	145	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	14546	145	146	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	14647	146	147	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	14748	147	148	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	14849	148	149	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	14950	149	150	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	15051	150	151	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	15152	151	152	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	15253	152	153	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	15354	153	154	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	15455	154	155	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	15556	155	156	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	15657	156	157	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	15758	157	158	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	15859	158	159	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	15960	159	160	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	16061	160	161	0.0	0.0	0.0	0.0	0.0	0.0
CHAR	16162	161	162	0.0	0.0	0			

ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
PILOT SEAT RESPONSE TO 1000 LH Z/REV VERT HUR SHEAR

		INPUT BULK DATA CHECK F C H O									
		1	2	3	4	5	6	7	8	9	10
PHAR	2324	1	1	1	35.54	1008.00	1150.10	428.36	11.5		
PHAR	2425	1	1	1	38.50	182.6	5150.	11.5			
PHAR	2526	1	1	1	35.13	169.0	1000.	11.2			
PHAR	2627	1	1	1	32.70	132.0	1620.	69.0			
PHAR	2728	1	1	1	27.83	105.0	1340.	36.8			
PHAR	2829	1	1	1	25.45	72.0	650.	43.7			
PHAR	3031	1	1	1	1000.	5.5	5.5	11.0			
PHAR	3132	1	1	1	1000.	3.5	3.5	7.0			
PHAR	3334	1	1	1	1000.	2600.	454.	230.			
PHAR	3435	1	1	1	1000.	4250.	1031.	360.			
PHAR	3536	1	1	1	1000.	8250.	1485.	560.			
PHAR	3612	1	1	1	1000.	9912.	1683.	5150.			
PHAR	3737	1	1	1	1000.	9912.	1683.	5150.			
PHAR	3838	1	1	1	1000.	8570.	1485.	560.			
PHAR	3939	1	1	1	1000.	4250.	1031.	360.			
PHAR	3940	1	1	1	1000.	4250.	1031.	360.			
PHAR	5112	1	1	1	25.81	2500.	434.	230.			
PELAS	1	1	1	1	28125.						
PELAS	2	1	1	1	28125.						
PELAS	3	1	1	1	4500.						
PELAS	33	1	1	1	20000.						
PHAR	5253	1	1	1	100.		72.	148.			
PHAR	5354	1	1	1	100.		135.	270.			
PHAR	5455	1	1	1	100.		120.	170.			
MATI	1	1	1	1	1.0E6						
CONM2	1	1	1	1	12.029						
CONM2	2	1	1	1	34.985						
CONM2	3	1	1	1	46.882						
CONM2	4	1	1	1	193.820						
CONM2	5	1	1	1	253.4						
CONM2	6	1	1	1	439.371						
CONM2	7	1	1	1	551.594						
CONM2	8	1	1	1	355.019						
CONM2	9	1	1	1	189.893						
CONM2	10	1	1	1	718.312						
CONM2	11	1	1	1	685.394						
CONM2	12	1	1	1	1.5E+06						
CONM2	13	1	1	1	836.348						
CONM2	14	1	1	1	554.622						
CONM2	15	1	1	1	296.573						
CONM2	16	1	1	1	87.781						
CONM2	17	1	1	1	33.058						
CONM2	18	1	1	1	43.977						
CONM2	19	1	1	1	60.541						
CONM2	20	1	1	1	41.475						
CONM2	21	1	1	1	29.713						
CONM2	22	1	1	1	15.102						
CONM2	23	1	1	1	44.152						
CONM2	24	1	1	1	19.136						
CONM2	25	1	1	1	6.409						
CONM2	26	1	1	1	11.934						
CONM2	27	1	1	1	4.768						
CONM2	28	1	1	1	4.768						
CONM2	29	1	1	1	5.594						
CONM2	30	1	1	1	11.282						
CONM2	31	1	1	1	34.066						
CONM2	32	1	1	1	9.489						
CONM2	33	1	1	1	31.704						
CONM2	34	1	1	1	16.459						
CONM2	35	1	1	1	22.577						
CONM2	36	1	1	1	30.459						
CONM2	37	1	1	1	14.763						
CONM2	38	1	1	1	18.419						
CONM2	39	1	1	1	11.763						
CONM2	40	1	1	1	27.014						
CONM2	41	1	1	1	13.540						
CONM2	42	1	1	1	27.014						
CONM2	43	1	1	1	13.540						
CONM2	44	1	1	1	27.014						
CONM2	45	1	1	1	13.540						

CWT12

ELASTIC LINE MODEL OF THE MAIN HELICOPTER
 UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
 PILOT SEAT RESPONSE TO 1000 LH 2/REV VERT HUB SHEAR

CARD COUNT	1	2	3	4	5	6	7	8	9	10
1-	CHAR	12	1	1	1	1	1	1	1	1
2-	CHAR	13	2	2	2	2	2	2	2	2
3-	CHAR	14	3	3	3	3	3	3	3	3
4-	CHAR	15	4	4	4	4	4	4	4	4
5-	CHAR	16	5	5	5	5	5	5	5	5
6-	CHAR	17	6	6	6	6	6	6	6	6
7-	CHAR	18	7	7	7	7	7	7	7	7
8-	CHAR	19	8	8	8	8	8	8	8	8
9-	CHAR	20	9	9	9	9	9	9	9	9
10-	CHAR	21	10	10	10	10	10	10	10	10
11-	CHAR	22	11	11	11	11	11	11	11	11
12-	CHAR	23	12	12	12	12	12	12	12	12
13-	CHAR	24	13	13	13	13	13	13	13	13
14-	CHAR	25	14	14	14	14	14	14	14	14
15-	CHAR	26	15	15	15	15	15	15	15	15
16-	CHAR	27	16	16	16	16	16	16	16	16
17-	CHAR	28	17	17	17	17	17	17	17	17
18-	CHAR	29	18	18	18	18	18	18	18	18
19-	CHAR	30	19	19	19	19	19	19	19	19
20-	CHAR	31	20	20	20	20	20	20	20	20
21-	CHAR	32	21	21	21	21	21	21	21	21
22-	CHAR	33	22	22	22	22	22	22	22	22
23-	CHAR	34	23	23	23	23	23	23	23	23
24-	CHAR	35	24	24	24	24	24	24	24	24
25-	CHAR	36	25	25	25	25	25	25	25	25
26-	CHAR	37	26	26	26	26	26	26	26	26
27-	CHAR	38	27	27	27	27	27	27	27	27
28-	CHAR	39	28	28	28	28	28	28	28	28
29-	CHAR	40	29	29	29	29	29	29	29	29
30-	CHAR	41	30	30	30	30	30	30	30	30
31-	CHAR	42	31	31	31	31	31	31	31	31
32-	CHAR	43	32	32	32	32	32	32	32	32
33-	CHAR	44	33	33	33	33	33	33	33	33
34-	CHAR	45	34	34	34	34	34	34	34	34
35-	CHAR	46	35	35	35	35	35	35	35	35
36-	CHAR	47	36	36	36	36	36	36	36	36
37-	CHAR	48	37	37	37	37	37	37	37	37
38-	CHAR	49	38	38	38	38	38	38	38	38
39-	CHAR	50	39	39	39	39	39	39	39	39
40-	CHAR	51	40	40	40	40	40	40	40	40
41-	CHAR	52	41	41	41	41	41	41	41	41
42-	CHAR	53	42	42	42	42	42	42	42	42
43-	CHAR	54	43	43	43	43	43	43	43	43
44-	CHAR	55	44	44	44	44	44	44	44	44
45-	CHAR	56	45	45	45	45	45	45	45	45
46-	CHAR	57	46	46	46	46	46	46	46	46
47-	CHAR	58	47	47	47	47	47	47	47	47
48-	CHAR	59	48	48	48	48	48	48	48	48
49-	CHAR	60	49	49	49	49	49	49	49	49
50-	CHAR	61	50	50	50	50	50	50	50	50
51-	CHAR	62	51	51	51	51	51	51	51	51
52-	CHAR	63	52	52	52	52	52	52	52	52
53-	CHAR	64	53	53	53	53	53	53	53	53
54-	CHAR	65	54	54	54	54	54	54	54	54
55-	CHAR	66	55	55	55	55	55	55	55	55
56-	CHAR	67	56	56	56	56	56	56	56	56
57-	CHAR	68	57	57	57	57	57	57	57	57
58-	CHAR	69	58	58	58	58	58	58	58	58
59-	CHAR	70	59	59	59	59	59	59	59	59
60-	CHAR	71	60	60	60	60	60	60	60	60
61-	CHAR	72	61	61	61	61	61	61	61	61
62-	CHAR	73	62	62	62	62	62	62	62	62
63-	CHAR	74	63	63	63	63	63	63	63	63
64-	CHAR	75	64	64	64	64	64	64	64	64
65-	CHAR	76	65	65	65	65	65	65	65	65
66-	CHAR	77	66	66	66	66	66	66	66	66
67-	CHAR	78	67	67	67	67	67	67	67	67
68-	CHAR	79	68	68	68	68	68	68	68	68
69-	CHAR	80	69	69	69	69	69	69	69	69
70-	CHAR	81	70	70	70	70	70	70	70	70
71-	CHAR	82	71	71	71	71	71	71	71	71
72-	CHAR	83	72	72	72	72	72	72	72	72

ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
 UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
 PILOT SEAT RESPONSE TO 1000 LB 2/REV VERT HUR SHEAR

CARD COUNT	1	2	3	4	5	6	7	8	9	10
74-	CONN2	12	12	12	12	12	12	12	12	12
75-	CONN2	13	13	13	13	13	13	13	13	13
76-	CONN2	14	14	14	14	14	14	14	14	14
77-	CONN2	15	15	15	15	15	15	15	15	15
78-	CONN2	16	16	16	16	16	16	16	16	16
79-	CONN2	17	17	17	17	17	17	17	17	17
80-	CONN2	18	18	18	18	18	18	18	18	18
81-	CONN2	19	19	19	19	19	19	19	19	19
82-	CONN2	20	20	20	20	20	20	20	20	20
83-	CONN2	21	21	21	21	21	21	21	21	21
84-	CONN2	22	22	22	22	22	22	22	22	22
85-	CONN2	23	23	23	23	23	23	23	23	23
86-	CONN2	24	24	24	24	24	24	24	24	24
87-	CONN2	25	25	25	25	25	25	25	25	25
88-	CONN2	26	26	26	26	26	26	26	26	26
89-	CONN2	27	27	27	27	27	27	27	27	27
90-	CONN2	28	28	28	28	28	28	28	28	28
91-	CONN2	29	29	29	29	29	29	29	29	29
92-	CONN2	30	30	30	30	30	30	30	30	30
93-	CONN2	31	31	31	31	31	31	31	31	31
94-	CONN2	32	32	32	32	32	32	32	32	32
95-	CONN2	33	33	33	33	33	33	33	33	33
96-	CONN2	34	34	34	34	34	34	34	34	34
97-	CONN2	35	35	35	35	35	35	35	35	35
98-	CONN2	36	36	36	36	36	36	36	36	36
99-	CONN2	37	37	37	37	37	37	37	37	37
100-	CONN2	38	38	38	38	38	38	38	38	38
101-	CONN2	39	39	39	39	39	39	39	39	39
102-	CONN2	40	40	40	40	40	40	40	40	40
103-	CONN2	41	41	41	41	41	41	41	41	41
104-	CONN2	42	42	42	42	42	42	42	42	42
105-	CONN2	43	43	43	43	43	43	43	43	43
106-	CONN2	44	44	44	44	44	44	44	44	44
107-	CONN2	45	45	45	45	45	45	45	45	45
108-	CONN2	46	46	46	46	46	46	46	46	46
109-	CONN2	47	47	47	47	47	47	47	47	47
110-	CONN2	48	48	48	48	48	48	48	48	48
111-	CONN2	49	49	49	49	49	49	49	49	49
112-	CONN2	50	50	50	50	50	50	50	50	50
113-	CRIGD1	1240	1240	1240	1240	1240	1240	1240	1240	1240
114-	CRIGD1	1460	1460	1460	1460	1460	1460	1460	1460	1460
115-	CRIGD1	5140	5140	5140	5140	5140	5140	5140	5140	5140
116-	CRIGD2	30310	30310	30310	30310	30310	30310	30310	30310	30310
117-	CRIGD2	51253	51253	51253	51253	51253	51253	51253	51253	51253
118-	DM1	253	253	253	253	253	253	253	253	253
119-	DM1	CP	CP	CP	CP	CP	CP	CP	CP	CP
120-	DM1	CP	CP	CP	CP	CP	CP	CP	CP	CP
121-	DM1	RP	RP	RP	RP	RP	RP	RP	RP	RP
122-	FREQ	10	10	10	10	10	10	10	10	10
123-	FREQ	10	10	10	10	10	10	10	10	10
124-	GRID	1	1	1	1	1	1	1	1	1
125-	GRID	2	2	2	2	2	2	2	2	2
126-	GRID	3	3	3	3	3	3	3	3	3
127-	GRID	4	4	4	4	4	4	4	4	4
128-	GRID	5	5	5	5	5	5	5	5	5
129-	GRID	6	6	6	6	6	6	6	6	6
130-	GRID	7	7	7	7	7	7	7	7	7
131-	GRID	8	8	8	8	8	8	8	8	8
132-	GRID	9	9	9	9	9	9	9	9	9
133-	GRID	10	10	10	10	10	10	10	10	10
134-	GRID	11	11	11	11	11	11	11	11	11
135-	GRID	12	12	12	12	12	12	12	12	12
136-	GRID	13	13	13	13	13	13	13	13	13
137-	GRID	14	14	14	14	14	14	14	14	14
138-	GRID	15	15	15	15	15	15	15	15	15
139-	GRID	16	16	16	16	16	16	16	16	16
140-	GRID	17	17	17	17	17	17	17	17	17
141-	GRID	18	18	18	18	18	18	18	18	18
142-	GRID	19	19	19	19	19	19	19	19	19
143-	GRID	20	20	20	20	20	20	20	20	20
144-	GRID	21	21	21	21	21	21	21	21	21

CLASS LINE MODEL OF THE A1-15 DELICATED
 UNDAMPED REDUCED RESPONSE STRAIN ENERGY METHOD
 PLASTIC AT RESPONSE TO 1000 LB 2/REV VERT HUB SPACR

CARD COUNT	1	2	3	4	5	6	7	8	9	10
145-	GRID	22	1.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
146-	GRID	23	425.24	0.000	57.20	0.000	0.000	0.000	0.000	0.000
147-	GRID	24	447.15	0.000	53.50	0.000	0.000	0.000	0.000	0.000
148-	GRID	25	464.10	0.000	50.80	0.000	0.000	0.000	0.000	0.000
149-	GRID	26	480.23	0.000	48.40	0.000	0.000	0.000	0.000	0.000
150-	GRID	27	497.77	0.000	46.32	0.000	0.000	0.000	0.000	0.000
151-	GRID	28	506.60	0.000	44.50	0.000	0.000	0.000	0.000	0.000
152-	GRID	29	515.43	0.000	42.90	0.000	0.000	0.000	0.000	0.000
153-	GRID	30	520.67	0.000	41.50	0.000	0.000	0.000	0.000	0.000
154-	GRID	31	520.67	7.20	118.27	0.000	0.000	0.000	0.000	0.000
155-	GRID	32	520.67	14.10	118.27	0.000	0.000	0.000	0.000	0.000
156-	GRID	33	107.858	-50.0	62.246	0.000	0.000	0.000	0.000	0.000
157-	GRID	34	146.574	-45.5	61.226	0.000	0.000	0.000	0.000	0.000
158-	GRID	35	194.230	-30.0	60.498	0.000	0.000	0.000	0.000	0.000
159-	GRID	36	195.202	19.19	57.868	0.000	0.000	0.000	0.000	0.000
160-	GRID	37	194.230	30.0	60.498	0.000	0.000	0.000	0.000	0.000
161-	GRID	38	196.575	42.5	61.226	0.000	0.000	0.000	0.000	0.000
162-	GRID	39	199.854	60.0	62.246	0.000	0.000	0.000	0.000	0.000
163-	GRID	40	199.94	-12.375	71.57	0.000	0.000	0.000	0.000	0.000
164-	GRID	41	199.94	12.375	71.57	0.000	0.000	0.000	0.000	0.000
165-	GRID	42	211.72	-12.375	77.57	0.000	0.000	0.000	0.000	0.000
166-	GRID	43	211.72	12.375	77.57	0.000	0.000	0.000	0.000	0.000
167-	GRID	44	189.94	-11.375	77.57	0.000	0.000	0.000	0.000	0.000
168-	GRID	45	189.94	11.375	77.57	0.000	0.000	0.000	0.000	0.000
169-	GRID	46	211.72	-11.375	77.57	0.000	0.000	0.000	0.000	0.000
170-	GRID	47	211.72	11.375	77.57	0.000	0.000	0.000	0.000	0.000
171-	GRID	48	214.50	0.0	77.57	0.000	0.000	0.000	0.000	0.000
172-	GRID	49	200.0	0.0	83.8	0.000	0.000	0.000	0.000	0.000
173-	GRID	50	200.0	0.0	77.2	0.000	0.000	0.000	0.000	0.000
174-	GRID	51	200.0	0.0	96.0	0.000	0.000	0.000	0.000	0.000
175-	GRID	52	200.0	0.0	113.0	0.000	0.000	0.000	0.000	0.000
176-	GRID	53	200.0	0.0	113.0	0.000	0.000	0.000	0.000	0.000
177-	GRID	54	200.0	0.0	113.0	0.000	0.000	0.000	0.000	0.000
178-	GRID	55	200.0	0.0	113.0	0.000	0.000	0.000	0.000	0.000
179-	GRID	56	200.0	0.0	113.0	0.000	0.000	0.000	0.000	0.000
180-	GRID	57	200.0	0.0	113.0	0.000	0.000	0.000	0.000	0.000
181-	PARAM	1	1.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
182-	PARAM	2	0.00250	0.000	0.000	0.000	0.000	0.000	0.000	0.000
183-	PARAM	12	1000.	1650.	250.	200.	200.	200.	200.	200.
184-	PARAM	23	1000.	3300.	700.	1100.	1100.	1100.	1100.	1100.
185-	PARAM	34	1000.	5400.	1100.	225.	225.	225.	225.	225.
186-	PARAM	47	1000.	7300.	1500.	350.	350.	350.	350.	350.
187-	PARAM	78	1000.	9200.	2000.	500.	500.	500.	500.	500.
188-	PARAM	89	1000.	11100.	2600.	700.	700.	700.	700.	700.
189-	PARAM	910	1000.	13000.	3300.	950.	950.	950.	950.	950.
190-	PARAM	1011	1000.	14900.	4100.	1200.	1200.	1200.	1200.	1200.
191-	PARAM	1112	1000.	16800.	5000.	1500.	1500.	1500.	1500.	1500.
192-	PARAM	1213	1000.	18700.	6000.	1800.	1800.	1800.	1800.	1800.
193-	PARAM	1314	1000.	20600.	7000.	2100.	2100.	2100.	2100.	2100.
194-	PARAM	1415	1000.	22500.	8000.	2400.	2400.	2400.	2400.	2400.
195-	PARAM	1516	1000.	24400.	9000.	2700.	2700.	2700.	2700.	2700.
196-	PARAM	1617	1000.	26300.	10000.	3000.	3000.	3000.	3000.	3000.
197-	PARAM	1718	1000.	28200.	11000.	3300.	3300.	3300.	3300.	3300.
198-	PARAM	1819	1000.	30100.	12000.	3600.	3600.	3600.	3600.	3600.
199-	PARAM	1920	1000.	32000.	13000.	3900.	3900.	3900.	3900.	3900.
200-	PARAM	2021	1000.	33900.	14000.	4200.	4200.	4200.	4200.	4200.
201-	PARAM	2122	1000.	35800.	15000.	4500.	4500.	4500.	4500.	4500.
202-	PARAM	2223	1000.	37700.	16000.	4800.	4800.	4800.	4800.	4800.
203-	PARAM	2324	1000.	39600.	17000.	5100.	5100.	5100.	5100.	5100.
204-	PARAM	2425	1000.	41500.	18000.	5400.	5400.	5400.	5400.	5400.
205-	PARAM	2526	1000.	43400.	19000.	5700.	5700.	5700.	5700.	5700.
206-	PARAM	2627	1000.	45300.	20000.	6000.	6000.	6000.	6000.	6000.
207-	PARAM	2728	1000.	47200.	21000.	6300.	6300.	6300.	6300.	6300.
208-	PARAM	2829	1000.	49100.	22000.	6600.	6600.	6600.	6600.	6600.
209-	PARAM	2930	1000.	51000.	23000.	6900.	6900.	6900.	6900.	6900.
210-	PARAM	3031	1000.	52900.	24000.	7200.	7200.	7200.	7200.	7200.
211-	PARAM	3132	1000.	54800.	25000.	7500.	7500.	7500.	7500.	7500.
212-	PARAM	3233	1000.	56700.	26000.	7800.	7800.	7800.	7800.	7800.
213-	PARAM	3334	1000.	58600.	27000.	8100.	8100.	8100.	8100.	8100.
214-	PARAM	3435	1000.	60500.	28000.	8400.	8400.	8400.	8400.	8400.
215-	PARAM	3536	1000.	62400.	29000.	8700.	8700.	8700.	8700.	8700.
216-	PARAM	3637	1000.	64300.	30000.	9000.	9000.	9000.	9000.	9000.

T/R HUB

XMSN

M/R HUB
ENGINE

ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
 UNDAMPED FORCED RESPONSES - STRAIN ENERGY METHOD
 PILOT SEAT RESPONSE TO 1000 C/P/R/V VERT HUH SHEAR

CARD	1	2	3	4	5	6	7	8	9	10
117-	PIAR	1612	1	1000.	9912.	1683.	5150.			
118-	PIAR	1738	1	1000.	4250.	1485.	560.			
119-	PIAR	3439	1	1000.	4250.	1031.	380.			
120-	PIAR	3940	1	1000.	2000.	454.	230.			
121-	PIAR	5112	1	25.41	72.	72.	144.			
122-	PIAR	3223	1	100.	135.	135.	270.			
123-	PIAR	2828	1	100.	120.	120.	240.			
124-	PIAR	3455	1							
225-	PELAS	1	24125.							
226-	PELAS	2	28125.							
227-	PELAS	3	4500.							
228-	PELAS	33	20000.							
229-	RLIAD2	1000	0	0	0	99	0			
230-	TATLDD1	99	0	200.0	1.0	ENDI				
231-	ENRPEC	0.0	1.0							GRMFC
	ENDDATA									

ELASTIC LINE MODEL OF THE MAIN HELICOPTER
 OPERATED FORCED RESPONSE STRAIN ENERGY METHOD
 PILOT SEAT RESPONSE TO 1000 TO 2 REV VERT HUB SHEAR
 LEVEL 2.0 NASTRAN DMAP COMPILER - SOURCE LISTING

```

31 PARAM //C,N,ADD//V,N,NOKGG,K/C,N,1/C,N,0 $
32 PARAM //C,N,ADD//V,N,NOMGG/C,N,1/C,N,0 $
33 PARAM //C,N,ADD//V,N,NURGG#-1/C,N,1/C,N,0 $
34 PARAM //C,N,ADD//V,N,NKAGG/C,N,1/C,N,0 $
35 *MS EST,CSTM,PT,DTI,GFUM2,KELM,KDICT,MELM,MDICT,HELM,DDICT,V,
    N,NOKGG,V,N,NOMGG,V,N,NURGG,V,N,NKAGG,V,N,CGY,CUPHASS,C,Y,
    CBTIAZ/C,Y,CPTU#Z,C,Y,CPOUAJ/C,Y,CPOUADZ/C,Y,CPTIAI/C,Y,
    CBTIBL/C,Y,CPTI#C $
36 SAVE NOKGG,NOMGG,NURGG,NKAGG $
37 CHKONT KELM,KDICT,MELM,MDICT,HELM,DDICT $
38 CEND LHLKGG,NKGG $
39 FMA GPECT,KDICT,KELM,KAGG,GPST $
40 CHKONT KGG,GPST $
41 LABEL LHLKGG $
42 CEND LHLMGG,NMGG $
43 FMA GPECT,MDICT,MELM,MDICT,C,N,-1/C,Y,PMASS#1,0 $
44 CHKONT MGG $
45 LABEL LHLMGG $
46 CEND LHLRGG,NURGG $
47 FMA GPECT,DDICT,MELM,MDICT $
48 CHKONT RGG $
49 LABEL LHLRGG $
50 CEND LHLKAGG,NKAGG $
51 FMA GPECT,KDICT,KELM,KAGG,V,N,NKAGG $
52 CHKONT KAGG $
53 LABEL LHLKAGG $
54 PURGE MGN,MEF,MAA,NMGG $
55 PURGE MNN,MEF,MAA,NURGG $
56 CHKONT MGG,MNN,MEF,MAA,NGG,MNN,MEF,MAA $
57 CEND LHLCHKONT $
58 CEND ERDRA,NMGG $
59 *MS *MPDT,CSTM,EUKIN,MGG/DG/AV,CGHPT#-1/C,Y,WTAKS $
60 *MS *MGG,***** $
61 LABEL LHL $
62 CEND KGG,KGG,NMGG,NL $
63 CHKONT KGG $
64 CEND LHLI,NDG,RL $
65 *MS *L,KGG,KGG,V,N,NURGG,C,N,1/C,N,1 $
    
```

ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
 UNIFORMED FORCED RESPONSE STRAIN ENERGY METHOD
 PILOT SEAT RESPONSE TO 1000 LB Z/REV VERT HUR SHEAR
 LEVEL 2.0 NASTRAN DMAP COMPILER - SOURCE LISTING

```

66 CHKDNT KGG $
67 LABEL LBL11 $
68 PARAM /C,N,MPY/V,N,NCKIP/C,N,O/C,N,O $
69 V04 CASECCAGE04,EFXIN,SILAGDT,GGPDT,CSTM/RG,USEI,ASET/ V,N:
LUSSET/V,N,MPCF1/V,N,MPCF2/V,N,SINGLE/V,N,OMIT/V,N,REACT/V,N:
NSKIP/V,N,REPEAT/V,N,NUSET/V,N,NOL/V,N,NOA/C,V,5URTD $
70 SAVE MPCFI,SINGLE,OMIT,NUSET,REACT,MPCF2,NSKIP,REPEAT,NOL,NOA $
71 PURGE GM,GMD/MPCF1/GD,GUD/OMIT/KFS,PSF,OPC/USSET $
72 CHKDNT GM,GMD,RG,GO,GUD,KFS,PSF,OPC,USSET $
73 CIND LBL4,GENEL $
74 CIND LBL4,NDSTMP $
75 GUP GPL,GPST,USSET,SIL,UGPST/V,N,MGPST $
76 SAVE NUGPST $
77 CIND LBL4,NDGPST $
78 DEP OGPST,//// $
79 LABEL LBL4 $
80 EQUIV KGG,KNN/MPCF1/MGG,MNN/MPCF1/ RGG,RNN/MPCF1/KAGG,KANN/MPCF1 $
81 CHKDNT KNN,MNN,RNN,KANN $
82 CIND LBL2,MPCF1 $
83 MCF1 USSET,RG/GM $
84 CHKDNT GM $
85 MCF2 USSET,GM,KGS,MGS,FGG,KAGG/KNN,MNN,RNN,KANN $
86 CHKDNT KNN,MNN,RNN,KANN $
87 LABEL LBL2 $
88 EQUIV KNN,KFF/SINGLE/MNN,MFF/SINGLE/RNN,RFF/SINGLE/KANN,KAFF/SINGLE $
89 CHKDNT KFF,MFF,DIFF,KAFF $
90 CIND LBL3,SINGLE $
91 MCF1 USSET,KNN,MNN,RNN,KANN/KFF,KFS,MFF,REF,KAFF $
92 CHKDNT KFS,KFF,MFF,REF,KAFF $
93 LABEL LBL3 $
94 EQUIV KFF,KAA/OMIT $
95 EQUIV MFF,MAA/OMIT $
96 EQUIV RFF,RAA/OMIT $
97 EQUIV KAFF,KAAA/OMIT $
98 CHKDNT KAA,MAA,RAA,KAAA $
99 CIND LBL5,OMIT $
100 MCF1 USSET,KFF,////GD,KAA,KDD,LJ,//// $
    
```


ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
 UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
 PILOT SEAT RESPONSE TO 1000 LB 2/REV VERT HUD SHIFR
 LEVEL 2.0 NASTRAN DMAP COMPILER - SOURCE LISTING

```

200 XYTRAN XYCOR,PSDF,AUTD,,,XYPLTR/C,N,RAND/C,N,PSET/V,N,PFILF/ V,N,
CARDNO $
201 SAVE PFILE,CARDNO $
202 XYPLUT XYPLTR// $
203 JUMP LBL16 $
204 LABEL LBL17 $
205 HFP OUPVCI,OPPC1,OPDCI,DEFCT,DEFSCI, //V,N,CARDNO $
206 SAVE CARDNO $
207 LABEL LBL16 $
208 CMD FINIS,REPEAT $
209 REPT LBL13,100 $
210 JUMP ERROR3 $
211 JUMP FINIS $
212 LABEL ERROR3 $
213 PRTPARM //C,N,-1/C,N,DIERRD $
214 LABEL ERRUR2 $
215 PRTPARM //C,N,-2/C,N,DIRERRD $
216 LABEL ERRUR1 $
217 PRTPARM //C,N,-1/C,N,DIERRD $
218 LABEL ERRUR4 $
219 PRTPARM //C,N,-4/C,N,DIERRD $
220 LABEL FINIS $
220 PARAM // C,N,MID / V,N,MINUS1#-1 $ <<<--- THIS MUST BE SET BY USER
220 PARAM // C,N,MID / V,N,INFORM1#1 $
220 LABEL ESEEDYN $
220 PARTN UPVC,CP, / UPVCI,UPVC2, / C,N,1 $
220 PARTN OPC,CP, / OPC1,OPC2, / C,N,1 $
220 GPFDR CASECC,UPVCI,KULM,KDICT,ECT,F,FXIN,GPCT,OPCI /
UNRGY1,DPDM1 / C,N,STATIC $
220 HFD UNRGY1,DPDM1, // $
220 PARTN CP,RP / CPI, // C,N,1 $
220 PARTN RP,CP / RPI, // C,N,1 $
220 JUTV UPVC2,UPVC / MINUS1 $
220 JUTV OPC2,OPC / MINUS1 $
220 JUTV CPI,CP / MINUS1 $
220 JUTV RPI,RP / MINUS1 $
220 JUTV ESEEDYN,RPDM1 $
    
```

ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
UNWEAHEED FORCED RESPONSE STRAIN ENERGY METHOD
PILOT SEAT RESPONSE TO 1000 L4 2PREV VERT HUH SHEAR
LEVEL 2.0 NASTRAN DMAP COMPILER SOURCE LISTING

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201 (4)

*** NO ERRORS FOUND - EXECUTE NASTRAN PROGRAM ***

*** SYSTEM INFORMATION MESSAGE 3113. FMGRP PROCESSING DOUBLE PRECISION ELEMENTS OF TYPE	3A	STARTING WITH ID	12
*** SYSTEM INFORMATION MESSAGE 3107. EMGOLD IS PROCESSING ELEMENTS OF TYPE # 3A.	BEGINNING WITH ELEMENT ID #		12
*** SYSTEM INFORMATION MESSAGE 3113. FMGRP PROCESSING DOUBLE PRECISION ELEMENTS OF TYPE	11	STARTING WITH ID	41461
*** SYSTEM INFORMATION MESSAGE 3113. FMGRP PROCESSING DOUBLE PRECISION ELEMENTS OF TYPE	30	STARTING WITH ID	1
*** SYSTEM INFORMATION MESSAGE 3107. EMGOLD IS PROCESSING ELEMENTS OF TYPE # 30.	BEGINNING WITH ELEMENT ID #		1

ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
UNDAMPED FORCED RESPONSE: STRAIN ENERGY METHOD
PILOT SEAT RESPONSE TO 1000 LBS PARV VERT HUB SHEAR

APR 81 09 1779 NAS 224N 17177Z PAGE 19

*** USER WARNING MESSAGE 3041
EXTERNAL GRID POINT 0 DOES NOT EXIST OR IS NOT A GEOMETRIC GRID POINT.
THE BASIC ORIGIN WILL BE USED.

ELASTIC LINK MODEL OF THE AIR-IG HELICOPTER
UNDAMPED FORCED RESPONSE - STRAIN ENERGY METHOD
PILOT SEAT RESPONSE TO 1000 LB Z-REV VERT HUB SHEAR

OUTPUT FROM GRID POINT WEIGHT GENERATOR
REFERENCE POINT # 0

```

***
R.39398E+03 0.0 0.0 0.0 0.0 0.0 5.764303E+05 5.615605E+02 ***
R.39398E+03 0.0 0.0 -5.764303E+05 0.0 0.0 1.620686E+06 ***
0.0 0.0 R.39398E+03 5.615605E+02 -1.620686E+06 0.0 0.0 2.00000E+00 ***
0.0 0.0 -5.764303E+05 1.620686E+06 -2.00000E+00 0.0 0.0 0.0 ***
5.764303E+05 0.0 0.0 -1.620686E+06 2.00000E+00 0.0 0.0 0.0 ***
-5.615605E+02 0.0 0.0 1.620686E+06 -2.00000E+00 0.0 0.0 0.0 ***
***
S - TRANSFORMATION MATRIX FOR SCALAR MASS PARTITION
***
1.000000E+00 0.0 0.0 0.0 ***
0.0 1.000000E+00 0.0 0.0 ***
0.0 0.0 1.000000E+00 0.0 ***
0.0 0.0 0.0 1.000000E+00 ***
***

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DIRECTION
MASS AXIS SYSTEM %K X-C.G. Y-C.G. Z-C.G.
X 8.39398E+03 1.930770E+02 6.620031E-02 6.867180E+01
Y 8.39398E+03 1.930770E+02 6.620031E-02 6.867180E+01
Z 8.39398E+03 1.930770E+02 6.620031E-02 6.867180E+01

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***
%K - INERTIAS RELATIVE TO C.G. ***
1.38890E+07 1.93763E+05 5.25083E+06 ***
1.38890E+07 1.93763E+05 5.25083E+06 ***
5.25083E+06 2.78324E+04 5.21459E+04 ***
***
%K - PRINCIPLE INERTIAS ***
1.07218E+07 5.23112E+07 ***
1.07218E+07 5.23112E+07 ***
0 - TRANSFORMATION MATRIX -- I(i) = 0I+1IS+0 ***
9.92056E-01 -1.25739E-01 4.10054E-01 ***
-1.25739E-01 9.92056E-01 4.10054E-01 ***
4.10054E-01 -1.25739E-01 9.92056E-01 ***

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ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
PILOT SEAT RESPONSE TO 1000 LB 2/REV VERT HUR SHEAR

*** UPPER WARNING MESSAGE 3017
DUE TO MORE POTENTIAL SINGULARITIES HAVE NOT BEEN REMOVED BY SINGLE OR MULTI-POINT CONSTRAINTS.

C.A. 3. LINE MODEL OF THE M-10 HELICOPTER
 UPDATED TO MODEL RESPONSE STRAIN ENERGY METHOD
 APRIL 4, 1979 NASTRAN 1/17/77 PAGE 22
 PILOT SEAT RESPONSE TO 1000 LB Z/REV VERT HUB SHEAR

POINT ID.	SINGULARITY ORDER	GRID POINT	SINGULARITY ORDER	TABLE	SPC	MPC
51	2	2	2	WEAKEST COMBINATION	1	0
51	2	4	4	STRONGEST COMBINATION	2	0
51	2	6	6	WEAKEST COMBINATION	1	0

***USER INFORMATION MESSAGE 30/3--PARAMETERS FOR SYMMETRIC DECOMPOSITION OF DATA BLOCK SCRATCH9 X N # 254 <
 THE ESTIMATE # 1 C AVG # 18 PC AVG # 0 SPILL GROUPS # 0 S AVG # 1
 ADDITIONAL CORE # -60050 C MAX # 29 PCMAX # 0 PC GROUPS # 0 PREFACE LINES # 1

ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
 UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
 PILOT SEAT RESPONSE TO 1000 L3 279EV VDOT HUR SHFAR
 FREQUENCY # 1.070000E+01

C O M P L E X		D I S P L A C E M E N T		V E C T O R		R E A L / I M A G I N A R Y	
POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
1	G	4.874033E-05	7.544494E-04	2.240049E-03	-1.990273E-05	8.833830E-05	-7.553022E-06
2	G	4.874029E-05	7.103570E-04	1.671908E-03	-1.990273E-05	8.831159E-05	-7.551654E-06
3	G	4.874026E-05	5.952402E-04	3.263431E-04	-1.990273E-05	8.810051E-05	-7.534421E-06
4	G	4.874023E-05	4.418425E-04	8.830251E-04	-1.990273E-05	8.776944E-05	-7.494312E-06
5	G	-1.774030E-03	7.018571E-05	-9.269097E-04	-1.990273E-05	8.776944E-05	-7.494312E-06
6	G	4.874012E-05	3.578717E-04	-2.444029E-03	-2.026291E-05	8.588457E-05	-7.370015E-06
7	G	4.874013E-05	2.094217E-04	-4.205648E-03	-2.035795E-05	8.642823E-05	-7.072649E-06
8	G	4.874034E-05	8.615702E-05	5.788453E-03	-2.045055E-05	8.621643E-05	-6.582316E-06
9	G	4.8740053E-05	3.152138E-05	-6.568957E-03	-2.049426E-05	8.308551E-05	-6.263381E-06
10	G	4.874006E-05	-2.054669E-05	-7.373322E-03	-2.051285E-05	8.256962E-05	-5.580552E-06
11	G	4.874008E-05	-2.346884E-04	-1.159485E-02	-2.056869E-05	1.105516E-04	-8.449787E-06
12	G	4.874020E-05	-2.700204E-04	-1.238336E-02	-2.057839E-05	1.148687E-04	-8.214764E-06
13	G	4.8740275E-05	-3.328014E-04	-1.429697E-02	-1.918181E-05	1.229342E-04	-3.621753E-06
14	G	4.874040E-05	-4.312445E-04	-1.880680E-02	-1.567381E-06	1.141520E-04	-1.676149E-06
15	G	4.874045E-05	-4.536966E-04	-2.150857E-02	-1.249843E-05	8.486643E-05	8.613956E-06
16	G	1.710694E-05	-4.837336E-04	-2.307774E-02	-9.257873E-06	5.398045E-05	1.816951E-06
17	G	3.2508163E-05	-3.724010E-04	-2.371792E-02	-7.470569E-06	1.649327E-05	4.270445E-06
18	G	7.897074E-06	-2.445758E-04	-2.362421E-02	-4.543251E-06	-2.538796E-05	7.184965E-06
19	G	-5.32741E-05	-5.185393E-05	-2.252059E-02	-7.466381E-07	-7.909637E-05	1.086600E-05
20	G	-2.201907E-04	2.101635E-04	-2.009551E-02	4.185483E-06	-1.511985E-04	1.490726E-05
21	G	-5.894944E-04	5.642807E-04	-1.594215E-02	1.059623E-05	-2.444503E-04	1.912507E-05
22	G	-9.200473E-04	9.940074E-04	-9.700742E-03	1.473024E-05	-3.500714E-04	2.387170E-05
23	G	-1.522230E-03	1.531104E-03	-1.580642E-03	3.008496E-05	-4.704936E-04	2.463072E-05
24	G	-2.2246421E-03	2.172197E-03	9.904901E-05	4.701066E-05	-2.8906156E-04	3.845504E-05

1.0 MODEL OF THE AIR-IG HELICOPTER
 2.0 REBOUND STRAIN ENERGY METHOD
 3.0 RESPONSE TO 1000 LB 2/REV VERT HUB SHAAR
 4.0 1.070000E+01

C O M P L E X D I S P L A C E M E N T V E C T O R
 XREAL/IMAGINARY

ID.	TYPE	T1	T2	T3	R1	R2	R3
25	G	-1.146940E-02	2.006275E-03	1.956331E-02	1.132648E-04	-6.027790E-04	9.704020E-05
26	G	-1.8560094E-02	1.842784E-03	2.490530E-02	1.633473E-04	-6.240611E-04	1.4422335E-04
27	G	-2.207655E-02	1.726395E-03	3.051125E-02	2.232180E-04	-6.8429157E-04	1.962540E-04
28	G	-2.762711E-02	1.533602E-03	3.625273E-02	2.956700E-04	-6.562183E-04	2.620050E-04
29	G	-3.328784E-02	1.295013E-03	4.210117E-02	3.806902E-04	-6.667869E-04	3.369232E-04
30	G	-3.918472E-02	4.388653E-04	4.560718E-02	4.202288E-04	-6.699718E-04	3.745395E-04
31	G	-4.188140E-02	4.388659E-04	4.863283E-02	4.834172E-04	-6.699718E-04	4.290626E-04
32	G	-4.540849E-02	4.388661E-04	5.262501E-02	6.261584E-04	-6.699718E-04	5.522270E-04
33	G	1.209431E-03	-4.540880E-05	-1.181537E-02	-1.303410E-05	1.154802E-04	-4.102123E-06
34	G	1.103442E-03	-4.538610E-05	-1.166707E-02	-1.348534E-05	1.153953E-04	-4.106071E-06
35	G	1.130901E-03	-4.578549E-05	-1.156693E-02	-1.424724E-05	1.152817E-04	-4.118327E-06
36	G	1.102926E-03	-4.673208E-05	-1.149504E-02	-1.543707E-05	1.150277E-04	-4.128995E-06
37	G	1.204941E-03	-4.673173E-05	-1.229203E-02	-2.837882E-05	1.150333E-04	-4.323740E-06
38	G	1.304352E-03	-3.841634E-05	-1.281920E-02	-2.776286E-05	1.153138E-04	-4.339963E-06
39	G	1.522762E-03	-2.801549E-05	-1.344364E-02	-2.866358E-05	1.154439E-04	-4.358093E-06
40	G	1.716947E-03	-1.272978E-05	-1.433104E-02	-2.921074E-05	1.155869E-04	-4.364634E-06
41	G	3.2164042E-03	3.270819E-04	-1.131773E-02	-2.057839E-05	1.148687E-04	-4.214764E-06
42	G	3.268408E-03	3.240819E-04	-1.182705E-02	-2.057839E-05	1.148687E-04	-4.214764E-06
43	G	3.104092E-03	2.8352043E-04	-1.381957E-02	-2.057839E-05	1.148687E-04	-4.214764E-06
44	G	3.268408E-03	2.8352043E-04	-1.432869E-02	-2.057839E-05	1.148687E-04	-4.214764E-06
45	G	3.276250E-03	2.8352043E-04	-1.433935E-02	-2.057839E-05	1.148687E-04	-4.214764E-06
46	G	3.335112E-03	3.347190E-04	-1.268246E-02	-5.070511E-05	1.111001E-05	-4.252120E-06
47	G	3.840435E-03	3.837196E-04	-1.240794E-02	-5.070511E-05	1.111001E-05	-4.252120E-06
48	G	3.335112E-03	2.471074E-04	-1.6009407E-02	-5.070511E-05	1.111001E-05	-4.252120E-06

UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD

PILLOT SEAT RESPONSE TO 1000 Lb Z/REV VERT HUR SHFAR

FREQUENCY # 1.070000E+01

COMPLEX DISPLACEMENT VECTOR

XPFAZ/IMAGINARY

JOINT ID.	TYPE	T1	T2	T3	R1	R2	R3
49	G	3.440352E-03 0.0	2.471078E-04 0.0	-1.082357E-02 0.0	-5.070511E-06 0.0	-7.111081E-05 0.0	-4.252120E-06 0.0
50	G	3.4467732E-03 0.0	2.352870E-04 0.0	-1.050753E-02 0.0	-5.070511E-06 0.0	-7.111081E-05 0.0	-4.252120E-06 0.0
51	G	2.8920113E-03 0.0	3.245320E-04 0.0	-1.182864E-02 0.0	-5.070511E-06 0.0	-7.111081E-05 0.0	-4.252120E-06 0.0
52	G	3.4421443E-03 0.0	2.950665E-04 0.0	-1.182864E-02 0.0	-5.070511E-06 0.0	-7.111081E-05 0.0	-4.252120E-06 0.0
53	G	1.528339E-03 0.0	4.005330E-04 0.0	-1.165854E-02 0.0	4.058259E-07 0.0	-8.140447E-05 0.0	-4.252120E-06 0.0
54	G	7.736734E-04 0.0	3.369586E-04 0.0	-1.151324E-02 0.0	6.826715E-06 0.0	-2.940244E-05 0.0	-4.252120E-06 0.0
55	G	4.574085E-04 0.0	-1.033943E-04 0.0	-1.118203E-02 0.0	1.396899E-08 0.0	2.228951E-06 0.0	-4.252120E-06 0.0
60	G	4.8157051E-03 0.0	1.363649E-04 0.0	-1.857850E-02 0.0	-1.567381E-05 0.0	1.141520E-04 0.0	-1.676149E-06 0.0

COMPLEX DISPLACEMENT VECTOR
REAL/IMAGINARY

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
1	G	3.039970E-05 0.0	7.374098E-04 0.0	1.544747E-03 0.0	-1.934840E-05 0.0	7.904487E-05 0.0	-7.352987E-06 0.0
2	G	3.039970E-05 0.0	6.896183E-04 0.0	1.030996E-03 0.0	-1.934840E-05 0.0	7.902614E-05 0.0	-7.351633E-06 0.0
3	G	3.039970E-05 0.0	5.776007E-04 0.0	-1.733632E-04 0.0	-1.934840E-05 0.0	7.888649E-05 0.0	-7.334588E-06 0.0
4	G	3.039970E-05 0.0	4.769487E-04 0.0	-1.256886E-03 0.0	-1.934840E-05 0.0	7.870367E-05 0.0	-7.299868E-06 0.0
5	G	-1.016378E-03 0.0	6.686249E-05 0.0	-1.296240E-03 0.0	-1.934840E-05 0.0	7.870367E-05 0.0	-7.299868E-06 0.0
6	G	3.039970E-05 0.0	3.405055E-04 0.0	-2.561204E-03 0.0	-1.968848E-05 0.0	7.764685E-05 0.0	-7.172140E-06 0.0
7	G	3.039970E-05 0.0	2.020785E-04 0.0	-4.263044E-03 0.0	-1.979106E-05 0.0	7.915303E-05 0.0	-6.678588E-06 0.0
8	G	3.039970E-05 0.0	8.225408E-05 0.0	-5.725712E-03 0.0	-1.968848E-05 0.0	8.423284E-05 0.0	-6.394771E-06 0.0
9	G	3.039970E-05 0.0	2.919475E-05 0.0	-6.458487E-03 0.0	-1.992354E-05 0.0	8.845895E-05 0.0	-6.080179E-06 0.0
10	G	3.039970E-05 0.0	-2.133229E-05 0.0	-7.219847E-03 0.0	-1.994160E-05 0.0	9.081292E-05 0.0	-5.801274E-06 0.0
11	G	3.039970E-05 0.0	-2.334603E-05 0.0	-1.126373E-02 0.0	-1.999889E-05 0.0	1.069764E-04 0.0	-4.293367E-06 0.0
12	G	3.039970E-05 0.0	-2.627100E-04 0.0	-1.202819E-02 0.0	-2.000833E-05 0.0	1.115734E-04 0.0	-4.062023E-06 0.0
13	G	3.039970E-05 0.0	-3.231217E-04 0.0	-1.389432E-02 0.0	-1.861382E-05 0.0	1.202979E-04 0.0	-3.478511E-06 0.0
14	G	3.039970E-05 0.0	-4.168444E-04 0.0	-1.534191E-02 0.0	-1.511645E-05 0.0	1.134100E-04 0.0	-1.566861E-06 0.0
15	G	3.039970E-05 0.0	-4.366846E-04 0.0	-2.104293E-02 0.0	-1.198725E-05 0.0	8.555621E-05 0.0	9.059426E-06 0.0
16	G	4.299838E-06 0.0	-4.186374E-04 0.0	-2.264039E-02 0.0	-8.735873E-06 0.0	5.560360E-05 0.0	1.865279E-06 0.0
17	G	2.266635E-05 0.0	-3.538299E-04 0.0	-2.332514E-02 0.0	-6.959906E-06 0.0	1.955825E-05 0.0	4.272573E-06 0.0
18	G	2.843362E-06 0.0	-2.272007E-04 0.0	-2.330878E-02 0.0	-4.051833E-06 0.0	-2.107554E-05 0.0	7.130619E-06 0.0
19	G	-8.379902E-05 0.0	-3.702281E-05 0.0	-2.231085E-02 0.0	-3.037886E-07 0.0	-7.413507E-05 0.0	1.073782E-05 0.0
20	G	-2.251880E-04 0.0	2.268255E-04 0.0	-2.002459E-02 0.0	4.019299E-06 0.0	-1.437334E-04 0.0	1.469434E-05 0.0
21	G	-5.231018E-04 0.0	5.080172E-04 0.0	-1.604917E-02 0.0	1.098687E-05 0.0	-2.349685E-04 0.0	1.882315E-05 0.0
22	G	-9.230770E-04 0.0	9.151994E-04 0.0	-1.002822E-02 0.0	1.906521E-05 0.0	-3.365027E-04 0.0	2.347003E-05 0.0
23	G	-1.497030E-03 0.0	1.510991E-03 0.0	-1.677037E-03 0.0	3.034134E-05 0.0	-4.267634E-04 0.0	2.911233E-05 0.0
24	G	-2.216615E-03 0.0	2.140461E-03 0.0	9.059130E-03 0.0	4.714845E-05 0.0	-2.670916E-04 0.0	3.030105E-05 0.0

PILLOT SEAT RESPONSE TO 1000 RPM STEADY STATE HUB SHEAR FREQUENCY = 1.08000E+01

POINT NO.	TYPE	T1	T2	T3	R1	R2	R3
26	G	-1.11739E-02	1.465181E-03	1.640864E-02	1.127584E-04	-5.869644E-04	4.547995E-05
27	G	-1.620717E-02	1.632145E-03	2.361178E-02	1.622661E-04	-6.079494E-04	1.400797E-04
28	G	-2.188809E-02	1.666117E-03	2.907395E-02	2.214033E-04	-6.265466E-04	1.934432E-04
29	G	-2.609807E-02	1.664866E-03	3.466991E-02	2.929114E-04	-6.396722E-04	2.584504E-04
30	G	-3.281081E-02	1.219792E-03	4.037144E-02	3.767423E-04	-6.501069E-04	3.345830E-04
31	G	-3.816655E-02	4.989358E-04	4.376986E-02	4.156823E-04	-6.532557E-04	3.698836E-04
32	G	-4.087972E-02	4.989377E-04	4.678277E-02	4.777317E-04	-6.532557E-04	4.240985E-04
33	G	-4.431935E-02	4.989391E-04	5.072388E-02	6.178971E-04	-6.532557E-04	5.465662E-04
34	G	-1.657101E-03	-6.653129E-05	-1.148170E-02	-1.253787E-05	1.121787E-04	-3.951713E-06
35	G	1.120442E-03	-4.449401E-05	-1.133553E-02	-1.209460E-05	1.120947E-04	-3.955556E-06
36	G	1.069066E-03	-4.488064E-05	-1.123883E-02	-1.373882E-05	1.119325E-04	-3.967531E-06
37	G	1.217054E-03	-4.580931E-05	-1.116608E-02	-1.491748E-05	1.117308E-04	-3.977905E-06
38	G	1.332711E-03	-3.758240E-05	-1.245458E-02	-2.711693E-05	1.120140E-04	-4.184475E-06
39	G	1.464774E-03	-2.729098E-05	-1.306318E-02	-2.800894E-05	1.121824E-04	-4.202487E-06
40	G	1.604886E-03	-1.216594E-05	-1.392817E-02	-2.853776E-05	1.122644E-04	-4.208870E-06
41	G	3.062717E-03	3.175149E-04	-1.049291E-02	-2.000533E-05	1.115734E-04	-4.062023E-06
42	G	3.132522E-03	3.175149E-04	-1.148804E-02	-2.000533E-05	1.115734E-04	-4.062023E-06
43	G	3.062717E-03	2.290441E-04	-1.342298E-02	-2.000533E-05	1.115734E-04	-4.062023E-06
44	G	3.132522E-03	2.290441E-04	-1.391811E-02	-2.000533E-05	1.115734E-04	-4.062023E-06
45	G	3.117904E-03	2.102360E-04	-1.342298E-02	-2.000533E-05	1.115734E-04	-4.062023E-06
46	G	3.221442E-03	3.102360E-04	-1.234160E-02	-2.000533E-05	1.115734E-04	-4.062023E-06
47	G	3.340921E-03	3.102360E-04	-1.294403E-02	-2.000533E-05	1.115734E-04	-4.062023E-06
48	G	3.221442E-03	2.409474E-04	-1.403110E-02	-2.000533E-05	1.115734E-04	-4.062023E-06

CLASSIC LINE MODEL OF THE AH-1G HELICOPTER
 UNGAUGED FORCED RESPONSE STRAIN ENERGY METHOD
 PILOT SEAT RESPONSE TO 1000 L/1 Z/REV VERT HOR SHFAP
 INPUT KEY # 1.000000E+01

C O M P L E X D I S P L A C E M E N T V E C T O R
 REAL/IMAGINARY

POINT NO.	TYPE	T1	T2	T3	R1	R2	R3
49	G	3.342921E-03 0.0	2.409487E-04 0.0	-1.043545E-02 0.0	-5.024988E-06 0.0	-9.323143E-05 0.0	-4.099636E-06 0.0
50	G	3.262186E-03 0.0	2.295517E-04 0.0	-1.011408E-02 0.0	-5.024988E-06 0.0	-9.323143E-05 0.0	-4.099636E-06 0.0
51	G	2.701357E-03 0.0	3.203021E-04 0.0	-1.146594E-02 0.0	-5.024988E-06 0.0	-9.323143E-05 0.0	-4.099636E-06 0.0
52	G	3.316689E-03 0.0	2.871372E-04 0.0	-1.146594E-02 0.0	-5.024988E-06 0.0	-9.323143E-05 0.0	-4.099636E-06 0.0
53	G	1.377471E-03 0.0	3.916568E-04 0.0	-1.129531E-02 0.0	3.405797E-07 0.0	-6.145172E-05 0.0	-4.099636E-06 0.0
54	G	6.458953E-04 0.0	3.302987E-04 0.0	-1.114966E-02 0.0	6.638950E-06 0.0	-2.703117E-05 0.0	-4.099636E-06 0.0
55	G	4.874486E-04 0.0	4.066260E-05 0.0	-1.081774E-02 0.0	1.365370E-05 0.0	7.273161E-06 0.0	-4.099636E-06 0.0
56	G	4.116551E-03 0.0	1.304774E-04 0.0	-1.811508E-02 0.0	-1.511448E-05 0.0	1.134100E-04 0.0	-1.504861E-06 0.0

*** USER WARNING MESSAGE 2354.
 GPMJRM01X01 IS UNABLE TO CONTINUE AND HAS BEEN TERMINATED DUE TO ERROR MESSAGE PRINTED ABOVE OR BELOW THIS MESSAGE.
 THIS ERROR OCCURRED IN GPFOR CODE #HERE THE VARIABLE -INPROR- WAS SET # 20

ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
PILOT SEAT RESPONSE TO 1000 L/S 2/REV VERT HUB SHEAR

APRIL 4 1979 NASTHAN 1/11/77 PAGE 29

*** SYSTEM WARNING MESSAGE 3002
EUF ENCOUNTERED WHILE READING DATA SET SCRATCH3XFILE 303K IN SUBROUTINE GPFDR

ELEMENT STRAIN ENERGIES * TOTAL FOR ALL TYPES # 4.3662823E+00

ELEMENT-ID	ELEMENT-TYPE #	STRAIN-ENERGY	PERCENT OF TOTAL
12		5.906181E-06	0.0001
23		3.840236E-06	0.0001
34		2.535050E-06	0.0001
67		1.435743E-06	0.0027
76		1.332600E-03	0.0314
69		2.341652E-03	0.0536
910		2.443716E-03	0.0559
1011		4.364190E-02	0.9991
1112		1.901396E-02	0.4353
1213		3.301403E-02	0.7556
1237		1.605901E-03	0.0368
1314		3.433401E-02	0.7900
1515		1.68059E-01	3.8154
1617		2.428470E-01	5.5601
1718		2.659352E-01	6.0879
1619		3.322464E-01	7.6054
1920		4.058198E-01	9.2901
2021		4.809279E-01	11.0095
2122		4.723912E-01	10.8515
2223		4.627764E-01	10.5940
2324		3.531978E-01	8.0855
2425		6.78239E-02	1.5464
2526		4.104621E-02	1.0252
2627		3.366378E-02	0.7752
2728		3.132105E-02	0.7170
2829		1.091245E-02	0.2498
2930		7.991073E-03	0.1827
3031		1.242663E-02	0.2753
3132		1.535723E-06	0.0000
3233		3.553541E-05	0.0008
3334		1.14821E-04	0.0027
3435		1.270350E-03	0.0291
3536		1.67222E-05	0.0039
3637		3.491257E-05	0.0007
3738		7.902715E-02	2.0000
3839		7.428759E-02	1.7006
5112		6.638360E-02	1.5197
5253		1.446560E-01	3.3551
5354			
5455			

LADJIC LINE MODEL OF THE AH-1G HELICOPTER
UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
PILOT SEAT RESPONSE TO 1000 LR Z/REV VERT HIUR SHFAR

ELEMENT STRAIN ENERGIES
ELEMENT-TYPE # ELAS1 * TOTAL FOR ALL TYPES # 4.3682823E+00

ELEMENT-ID	STRAIN-ENERGY	PERCENT OF TOTAL *
41401	4.112961E-04	0.0004
41462	2.245739E-06	0.0001
41463	4.110624E-03	0.0009
42471	4.137592E-04	0.0009
42472	2.245739E-06	0.0001
42473	2.164919E-03	0.0046
43481	4.112961E-04	0.0004
43482	1.402386E-06	0.0000
43483	4.112961E-04	0.0004
44491	1.965863E-06	0.0000
44492	1.965863E-06	0.0000
44493	2.764633E-02	0.6329
45503	1.510120E-01	3.4570

*** USER WARNING MESSAGE 235A.
GPFR MIXTURE IS UNABLE TO CONTINUE AND HAS BEEN TERMINATED DUE TO ERROR MESSAGE PRINTED ABOVE OR BELOW THIS MESSAGE.
THIS ERROR OCCURRED IN GPFR CODE WHERE THE VARIABLE -NERROR- WAS SET # 20

ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
PILOT SEAT RESPONSE TO 1000 U³ 2/REV VERT HUR SHEAR

*** SYSTEM WARNING MESSAGE 3002
EUF ENCOUNTERED WHILE READING DATA SET SCRATCHFILE 303K IN SUBROUTINE GPFDR

ELASTIC LINE MODEL OF THE A1-16 HELICOPTER
 UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
 PILOT SEAT RESPONSE TO 1000 LB Z-RAY VERT HUB SHEAR

E L E M E N T S T R A I N E N E R G I E S
 * TOTAL FOR ALL TYPES # 4.20V6100E+00

ELEMENT-ID	ELEMENT-TYPE #	STRAIN-ENERGY	PERCENT OF TOTAL
12	1	4.921822E-07	-0.0000
23	2	2.638168E-06	0.0001
34	3	-9.079813E-07	-0.0000
40	4	4.071328E-05	0.0011
57	2	2.231710E-04	0.0053
78	2	2.389228E-03	0.0565
66	3	3.055750E-03	0.0833
101	2	2.918608E-02	0.7404
111	2	2.110219E-02	0.5444
112	3	3.813657E-02	0.9959
1213	1	1.571460E-03	0.0373
1237	2	2.991120E-02	0.7105
1314	1	1.513309E-01	3.8449
1415	1	1.835668E-01	4.6365
1516	2	2.271718E-01	5.6385
1617	2	2.850487E-01	7.0480
1718	3	3.149040E-01	7.7496
1819	2	3.681069E-01	9.0072
2021	4	4.559377E-01	10.8522
2122	3	3.420211E-01	8.3827
2224	6	6.544316E-02	1.6546
2425	4	4.538817E-02	1.1732
2526	3	3.952727E-02	0.9990
2627	3	3.290632E-02	0.7817
2728	3	3.005998E-02	0.7481
2829	1	1.921770E-02	0.2427
2930	1	1.718948E-02	0.3946
3031	1	1.257398E-02	0.3000
3132	3	3.488512E-02	0.8808
3233	1	1.194205E-04	0.0028
3336	1	1.234347E-03	0.0293
3512	1	1.708630E-04	0.0041
3738	5	5.777416E-05	0.0014
3839	1	1.440337E-06	0.0000
3940	9	9.051341E-02	2.1897
5112	7	7.537621E-02	1.8906
5213	6	6.772234E-02	1.6993
5315	1	1.8778915E-01	4.6593

ELASTIC LINE MODEL OF THE AH-1G HELICOPTER
 UNDAMPED FORCED RESPONSE STRAIN ENERGY METHOD
 PILOT SEAT RESPONSE TO 1000 LB 2/REV VERT HUB SHFAR

ELEMENT-TYPE # ELAS1	E L E M E N T	S T R A I N	E N E R G Y	# TOTAL FOR ALL TYPES #	PERCENT OF TOTAL
41401	41401	4.003479E-04	4.0000	4.2096100E+00	0.0000
41462	41462	2.276618E-06	0.0000		0.0000
42471	42471	4.1193051E-03	0.0000		0.0000
42472	42472	4.119273E-04	0.0000		0.0000
43461	43461	2.276618E-06	0.0000		0.0000
43462	43462	2.152020E-03	0.0000		0.0000
44491	44491	4.003479E-04	0.0000		0.0000
44492	44492	1.992921E-06	0.0000		0.0000
44493	44493	2.178554E-02	0.0000		0.0000
45503	45503	4.04873E-04	0.0000		0.0000
		2.72011E-02	0.0000		0.0000
		1.449506E-01	0.0000		0.0000

SYMBOLS

A	Element cross-sectional area
C	Viscous damping matrix
E	Modulus of elasticity
F	Applied force
G	Complex receptance matrix
I	Element area moment of inertia
K	Stiffness matrix
k	Scalar spring
M	Mass matrix
m	Scalar mass
S	Stiffness ratio
SE	Strain energy
t	Time
x	Structural displacement response vector
Z	Pilot's seat vertical displacement response
δ	Element displacement response vector
ω	Circular frequency of the applied forces
ϕ	Element natural frequency mode shape (eigenvector)
ζ	Element structural damping coefficient

Subscripts

b	Baseline
e	Element
I	Imaginary component of response

j jth element
m At minimum response
n At resonance
R Real component of response

Superscripts

T Matrix transpose

**DATE
FILMED**

0-8