

AD-A095 471

LOWELL UNIV RESEARCH FOUNDATION MA

F/S 20/10

RESEARCH ON THE INVERSE SCATTERING PROBLEM FOR THE THREE-DIMENS--ETC(U)

DEC 80 H E MOSES

DAA629-78-6-0003

ML

UNCLASSIFIED

ULRF-411/CAR

ARO-14919.8-M

OR
AD-A
506-021



END

DATE

FILED

3-81

DTIC

LEVEL

ARO 14919.8-M

RESEARCH ON THE INVERSE SCATTERING PROBLEM
FOR THE

THREE-DIMENSIONAL SCHRÖDINGER EQUATION.

12

AD A095471

10 Harry E. Moses

DTIC
FEB 24 1981

Final Report.

(Period of Grant 1 Oct 1977-30 Sep 1980.)

11 15 Dec 1980

U.S. ARMY RESEARCH OFFICE

Grant No. DAAG29-78-G-0003

Project No. 14919-M

DBG FILE COPY

UNIVERSITY OF LOWELL
CENTER FOR ATMOSPHERIC RESEARCH
450 Aiken Street
Lowell, Massachusetts 01854

DISTRIBUTION STATEMENT A

Approved for public release;
Distribution Unlimited

81 2 18 226

409570

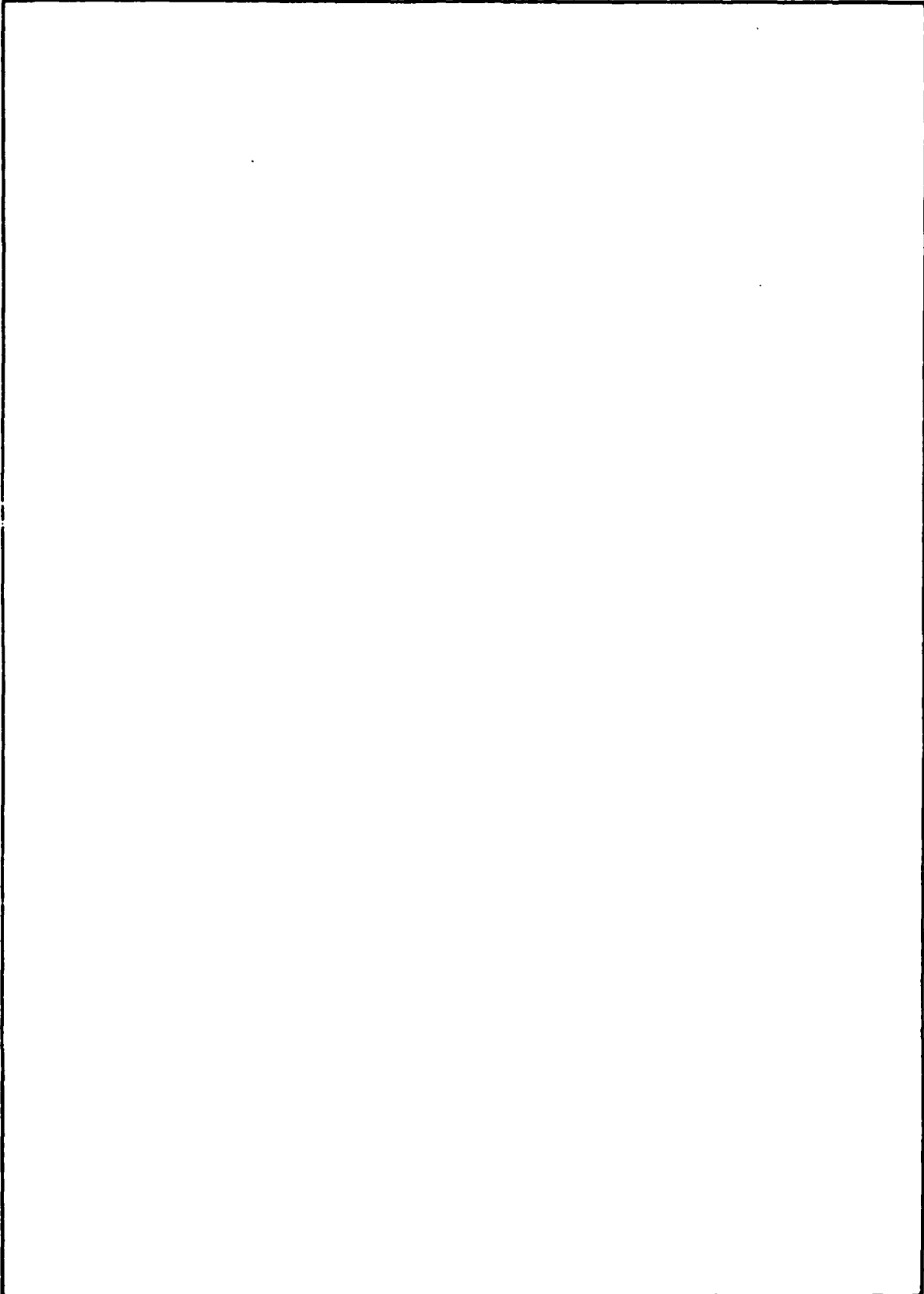
UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
	AD-A095471	
4. TITLE (and Subtitle) RESEARCH ON THE INVERSE SCATTERING PROBLEM FOR THE THREE-DIMENSIONAL SCHROEDINGER EQUATION		5. TYPE OF REPORT & PERIOD COVERED Final Oct. 1977-Sept. 1980
		6. PERFORMING ORG. REPORT NUMBER ULRF-411/CAR
7. AUTHOR(s) Harry E. Moses		8. CONTRACT OR GRANT NUMBER(s) DAAG29-78-G-0003
9. PERFORMING ORGANIZATION NAME AND ADDRESS University of Lowell, Center for Atmospheric Research, 450 Aiken Street, Lowell, Massachusetts 01854		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS Project No. 14919-M
11. CONTROLLING OFFICE NAME AND ADDRESS U.S. Army Research Office P. O. Box 12211 Research Triangle Park, NC 27709		12. REPORT DATE December 15, 1980
		13. NUMBER OF PAGES 4
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)		15. SECURITY CLASS. (of this report)
		15a. DECLASSIFICATION DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES The view, opinions, and/or findings contained in this report are those of the author and should not be construed as an official Department of the Army position, policy, or decision, unless so designated by other documentation.		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Inverse problem of scattering Inverse spectral theory for the three-dimensional problem Gelfand-Levitan equation		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) The work performed under the grant is summarize.		

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE(When Data Entered)



UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE(When Data Entered)

TABLE OF CONTENTS

	Page
1. Personnel Supported by the Grant	1
2. Direction of Research. Accomplishments.	1
3. Papers Published or Accepted for Publication	2
4. Papers which are Being Prepared for Submission	2

Accession For	☒
NTIS GRA&I	☐
DTIC TAB	☐
Unannounced	☐
Justification	
By —	
Distribution/	
Availability Codes	
Dist	
A	

1. Personnel Supported by the Grant

1. H. E. Moses, Principal Investigator.
2. G. Kaiser, Assistant Professor of Mathematics, University of Lowell, a nominal amount of support (less than \$4,000).
3. J. M. Cohen, Associate Professor of Physics, University of Pennsylvania, a nominal amount of support (less than \$5,000).

2. Direction of Research. Accomplishments.

The Principal Investigator's principal research direction has been to find appropriate triangularity conditions for the Gelfand-Levitan kernel in three-dimensions. The Gelfand-Levitan kernel for the one-dimensional problem has served as a model.

In this program we have proposed candidate for the Gelfand-Levitan kernel which we hope will give rise to local scattering potentials. A Jost wave function with appropriate completeness properties was given. Green's functions of a Jost type were also given.

We then broadened our attention to the consideration of non-local potentials in three dimensions. By introducing appropriate triangularity properties, we were able to obtain explicit non-local potentials for which the Schroedinger equation could be solved for exactly. A rich spectral theory results from the use of such potentials. Some have very unusual scattering properties, namely they do not scatter at all and thus could not be detected by a scattering experiment. These non-local potentials are the first potentials, non-local or local, which led to simple closed form solutions of the Schroedinger equations (energy-dependent potentials used by earlier workers are not really potentials, strictly speaking).

To understand the nature of triangularity better we considered the one-dimensional analogue of the non-local three-dimensional potentials. The potentials so obtained are the most general parity-dependent potentials and have very interesting scattering properties. These potentials may have technical applications. We are continuing to look into this matter. It was possible to show that a local and a non-local potential could give rise to the same scattering operator and point spectrum.

3. Papers Published or Accepted for Publication

1. "Jost Solutions and Green's Functions for the Three-Dimensional Schroedinger Equation," J. Math. Phys., 20, 1151 (1979).
2. "A Kernel of Gelfand-Levitan Type for the Three-Dimensional Schroedinger Equation," J. Math. Phys., 21, (1980).
3. "Exact Solutions for the Three-Dimensional Schroedinger Equation with Quasi-Local Potentials Obtained from a Three-Dimensional Gelfand-Levitan Equation. Examples of Totally Reflectionless Scattering," Mathematical Methods and Applications of Scattering Theory, Proceeding, Washington, D. C. 1979, Lecture Notes in Physics, Vol. 130, Springer Verlag (J. A. DeSanto, A. W. Saenz, and W. W. Zachary, Editors).
4. "An Explicit Example of a Local and a Non-Local Potential whose Hamiltonians are Unitarily Equivalent and whose Scattering Operators are Identical," accepted for publication by Studies in Applied Mathematics (with P. B. Abraham and B. DeFacio).

4. Papers which are Being Prepared for Submission

1. "Parity-Dependent Potentials in One Dimension," with P. B. Abraham and B. DeFacio.

DATE
ILME