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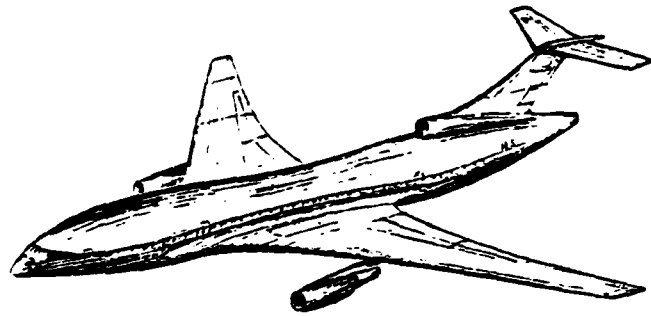


TRANSONIC FLUID DYNAMICS

Report TFD 81-06

K. Y. Fung, A. R. Seebass,
L. J. Dickson, C. F. Pearson

AN EFFECTIVE ALGORITHM
FOR SHOCK-FREE WING DESIGN



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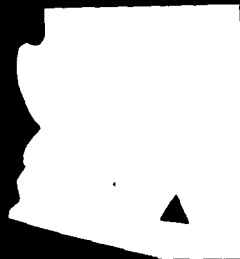
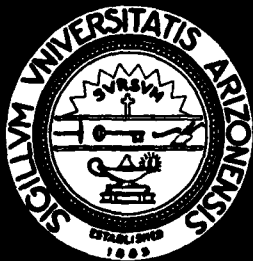
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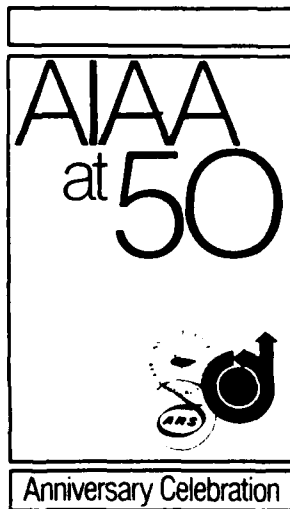
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AIAA-81-1236 An Effective Algorithm for Shock-Free Wing Design

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AN EFFECTIVE METHOD FOR SHOCK-FREE WING DESIGN

K.-Y. Fung, A. R. Seebass, L. J. Dickson, and C. F. Pearson

Abstract

This paper reviews the fictitious gas procedure of Sobieczky for finding shock-free airfoils and wings. Results for inviscid and viscous flows for airfoils and wings are described. The method is applied to a business jet planform resulting in a wing that should have good low speed characteristics as well as an $M_\infty L/D$ that is near the maximum achievable for the wing lift and thickness chosen for the study.

INTRODUCTION

There are a number of advancing technologies that should provide about a 40% improvement in transport aircraft fuel efficiency for the post 757/767 generation of aircraft. These include advances in the propulsion system, improved operations - including air traffic control, composite materials for primary as well as secondary structures, active flight control, and supercritical aerodynamics. More than half of this improvement will come from the use of composite materials and active control, in conjunction with aeroelastic tailoring of the wing structure to suppress flutter. This paper addresses a more modest contributor to this expected gain, viz., supercritical aerodynamics. Here we look for improvements in the "aerodynamic efficiency," $M_\infty L/D$, of about 5%. We must keep in mind that such small improvements are essential in obtaining the composite advance suggested above, and further, that each 1% increase in $M_\infty L/D$ of a single 300 passenger transport aircraft will save about \$100,000 in fuel costs per year at present prices.

The goal of maximizing $M_\infty L/D$ requires aircraft wings that have shock-free flow over them for as large a Mach number as possible for fixed lift, thickness, etc. Such flows are mathematically isolated from one another and have, in the past, been difficult to find. In the late 1960s and early 1970s methods for generating airfoils that were shock free at supercritical Mach numbers were developed by Nieuwland (1), Bauer, Garabedian and Korn (2), and Sobieczky (3). These investigations used different techniques to the same end, and will not be reviewed here. But even in their most advanced state they did not provide a rich selection of airfoils and none could be generalized to three dimensions. The application of these airfoil designs to swept, three-dimensional wings, required cut and try modifications of the wing in order to even come close to achieving shock-free flow. But Sobieczky (4), in a brilliant generalization of his earlier approach, saw that finding such designs in two dimensions would be routine, and that it seemed this generalization would apply to three-dimensional flows as well (5). We now know that while this generalization leads to an ill-posed boundary-value problem in three dimensions, this causes no serious difficulty for wings of moderate to large aspect ratio (6).

This paper reviews the fictitious gas method of designing shock-free wings, illustrating the procedure with several codes now in common use in the aircraft industry. The authors know little of the overall design process and our focus is more properly on the minor modifications to a wing that is already optimized for low speed and subcritical flight. The aerodynamic aspects of the design of commercial transports for aerodynamic efficiency have recently been reviewed by Lynch (7). We begin with the presumption that the designer has already chosen his basic airfoil section and wing planform and that he now wishes to maximize the $M L/D$ of the configuration using his existing computational tools, and that only a limited portion of the upper surface of the wing can be modified to achieve this goal without affecting the airfoil's low speed $(C_L)_{max}$. For our study we will use the GA(W)-2 airfoil and the Gates Learjet Century series planform.

AIRFOIL DESIGN

As noted above we begin by choosing a baseline airfoil. The GA(W)-2 has good low speed performance as well as some claim to being a relatively good supercritical airfoil (8). The numerical algorithm developed by Melnik (9) for computing the flow past airfoils in the presence of inviscid-viscous interactions, GRUMFOIL, has had early domestic dissemination. Nebeck (10) has modified this code for shock-free airfoil design in the presence of viscous interactions. N. Conley (private communication) reports that a modification of the Learjet wing section to obtain a shock-free flow at a freestream Mach number of 0.81 and a lift coefficient of $C_L = 0.50$ is desirable if this can be done with an airfoil such as the GA(W)-2 which has good low speed characteristics. Cosentino (private communication) has addressed the problem of design for an airfoil Mach number of 0.77 corresponding to a planform sweep of 15.7° . This process is not described here as the details may be found in Ref. 5, and our main concern is with wing design. With an appropriately chosen baseline airfoil based on the GA(W)-2, Cosentino was able to design an airfoil that was identical to the GA(W)-2 for the first 9% of its chord in order to retain the good low speed performance of the GA(W)-2, but had slight modifications to its upper surface in order to produce shock-free flow. Figure 1 compares the flow past the designed airfoil, GA(C)-250, as computed by GRUMFOIL, with that past a GA(W)-2 airfoil that has had its ordinates reduced to provide an 11.7% thick airfoil [GA(W)-2T]. The design point is $M_\infty = 0.7725$ and $C_L = 0.50$ with $Re = 6 \cdot 10^6$. Figure 2 compares the skin friction and boundary-layer displacement thickness on the two airfoils; note the small region of separation on the GA(W)-2T which has led to the lambda shock configuration responsible for the pressure distribution in Figure 1. We infer from these results that about a 100 count drag reduction has been achieved. The GA(W)-2, GA(C)-250, and the GA(W)-2T airfoils are compared in Figure 3. While there are only minor differences among the GA(W)-2T and GA(C)-250 airfoils, there are major differences in their supercritical performance indicating the great sensitivity of the flow to very minor changes in the upper surface. Since the GA(C)-250 is identical to the GA(W)-2 for the first 9% of the chord, we expect that it will also have a good low speed $(C_L)_{max}$.

WING DESIGN

Having selected our baseline airfoil, we now turn to wing design. We use this airfoil in the wing generator code of Sobieczky (11) to generate the wing input for a three-dimensional computation. We have chosen the FLO22 algorithm of Jameson and Caughey (12) for our wing studies. This code is well accepted by industry and is considerably faster than the conservative finite volume code used by Yu (13) to the same end. We note that while conservative differencing is important in the capture of shock waves, our design procedure computes the solution to an elliptic system and this can be done accurately with a nonconservative code. The basic tenets of the procedure have been described elsewhere (6,14). Because the changes we will make to our wing sections will be small, we must be careful to be sure they do not become obscured in the mapping from the physical plane to the computational plane. We have thus included a recomputation of the flow field after the design process in the computational variables in order to verify the results.

We remind the reader that in three-dimensions we solve an ill-posed boundary-value problem, and that any three-dimensional design must be confirmed by an analysis of the flow past this wing. The results of this computation are then compared with an analysis of the original wing shape, again using FLO22. Here, when there are shock waves present in the flow, this nonconservative calculation may overestimate their strength somewhat; however, the conservative potential approximation is even worse in this regard.

We begin our study with the candidate wing generated by the wing generator from the candidate baseline airfoil. Recall that this baseline airfoil was derived from the airfoil section of the wing we have designed to have optimum subcritical performance; it is not the airfoil we have designed to be shock free. We now repeat our fictitious gas study with a gas law that is close to that used in the airfoil design process. For conservative calculations we use a fictitious density, ρ_f , that depends on the flow speed q in a simple power law fashion, viz., $\rho_f / \rho_\infty = (q^*/q)^P$ for $q > q^*$, where $P < 1$, and is typically 0.9. In nonconservative calculations we prescribe a fictitious sound speed a , where $a = q(q/q^*)^L$ and $L > 0$. A value of $L = 5$ gives results similar to those of $P = 0.9$. Note that changing L (or P) results in a change in the size of the upper surface of the wing wetted by supersonic flow with the lower values of L (and higher values of P) reduce this area because they increase the mass flow through a unit area of the sonic surface.

Our goal, then, is to maximize $M_\infty L/D$ within the constraint that we maintain the features of the wing that optimized its subcritical performance. This we do by modifying the baseline airfoil and fictitious gas laws. We may even wish to employ an inverse design procedure like that of Henne (15) with the fictitious gas in order to help locate the fictitious supersonic domain where we wish it on the upper wing surface. Generally, the process of finding such a design requires several changes in the baseline section definition, additional changes in the twist variation to achieve an elliptic load distribution, and perhaps a half dozen Mach number and angle of attack

changes to determine the maximum M_∞ for which shock-free flow can be found for a given lift. Figure 4 depicts the pressures and corresponding wing sections for a non-shock-free wing design based on the GA(W)-2T airfoil. The wing has a lift coefficient of 0.375 at $M_\infty = 0.80$ and a nominal thickness of 11.7° . Also shown is a shock-free design that is derived from this wing that has somewhat less thickness. Figure 5 provides the same results for a wing that is the result of our shock-free wing design procedure. Here we have taken a baseline that is about .3% thicker than that desired. The designed wing has a lift coefficient of 0.439 at $M_\infty = 0.80$ and is 11.7° thick. The relative changes in the section drag coefficients are indicative of the inviscid improvement in the drag, but the individual magnitudes are obviously wrong. For the shock-free design the boundary layer will obviously not separate, but this is much less likely for the wing with the GA(W)-2T section. While these results are given for inviscid flow, they have been repeated with the section boundary-layer displacement thickness that, when used with the inviscid algorithm FLO6, gives essentially the same results as the GRUMFIDIL algorithm. Further improvements are no doubt possible, but these should serve to illustrate the effectiveness of the fictitious gas design method.

The design process in the presence of inviscid - viscous interactions that was successful in two dimensions is, as one would expect, also successful in three dimensions. We have used the algorithm developed by Stock (16) at Dornier for three-dimensional boundary layer calculations to provide the boundary layer displacement surface for the FLO22 computations. The two codes are interfaced with the PABLIM algorithm of C. L. Streett (private communication). Figure 6 shows the pressures on the original baseline wing used in the above study with those found on the wing designed to be shock free at $M_\infty = 0.76$ for a Reynolds number of $6 \cdot 10^6$. We are now in the process of repeating our inviscid design study to find an equivalent design when inviscid - viscous interactions are included.

CONCLUSION

It is clear that the fictitious gas method is capable of providing both airfoils and wings that are shock free. An experienced practitioner can push these designs to the natural barrier that seems to limit the maximum Mach number for fixed lift, or the maximum lift for fixed Mach number, for which shock-free designs are possible. Such studies can also be carried out successfully in the presence of viscous - inviscid interactions. Thus, the method can be used to provide very slight modifications to an already suitable design to maximize $M_\infty L/D$. We note that while a shock-free design point does not maximize this quantity, a shock-free design need only be used at a very slightly higher Mach number to achieve what must be near to the maximum possible for a given lift, Mach number, and thickness.

Acknowledgement

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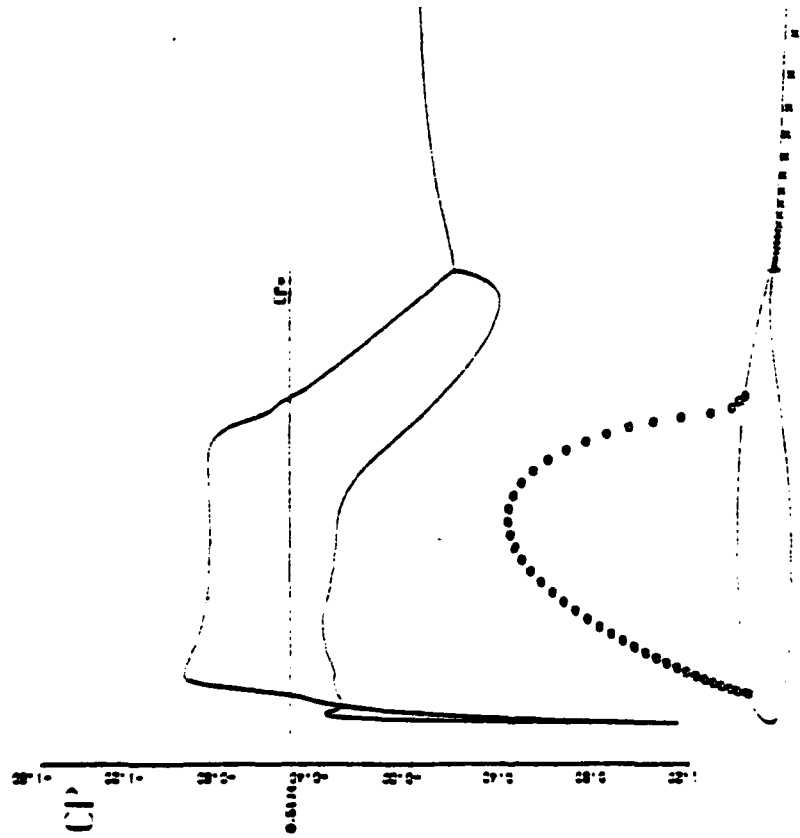
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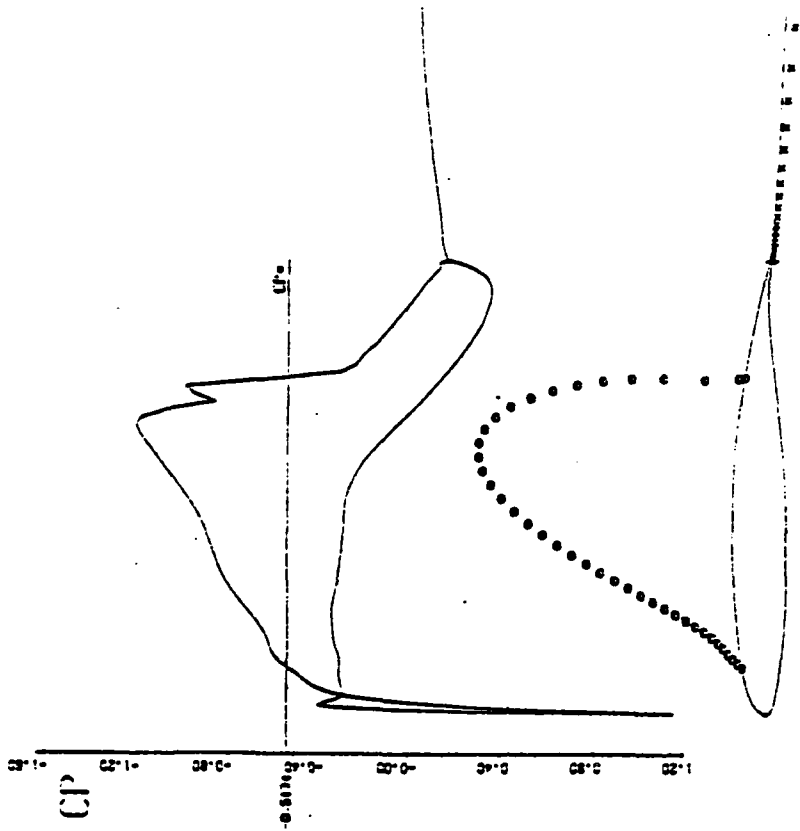
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 VARYING THE THICK WITH CURV CONSERVATIVE ANALYSIS
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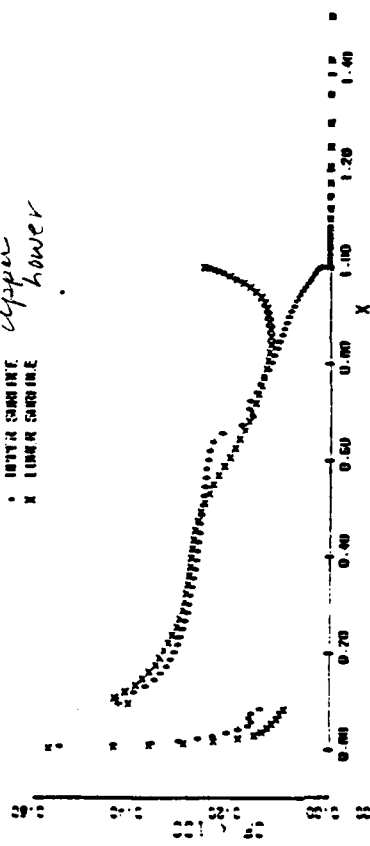
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Figure 1. Comparison on the pressures and sonic line shapes on the GA(C)
 -250 and GA(N)-2T airfoils at $M_\infty = 0.7725$, $C_L = 0.50$, and $Re = 6 \cdot 10^6$.

SKIN FRICTION

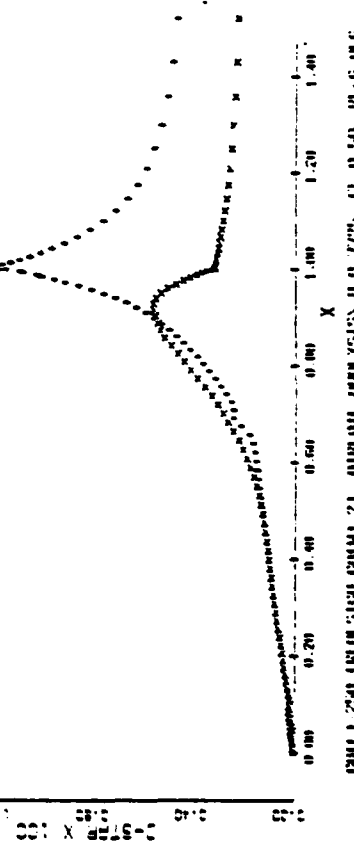
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 X LOWER SURFACE

upper
lower



DISPLACEMENT THICKNESS

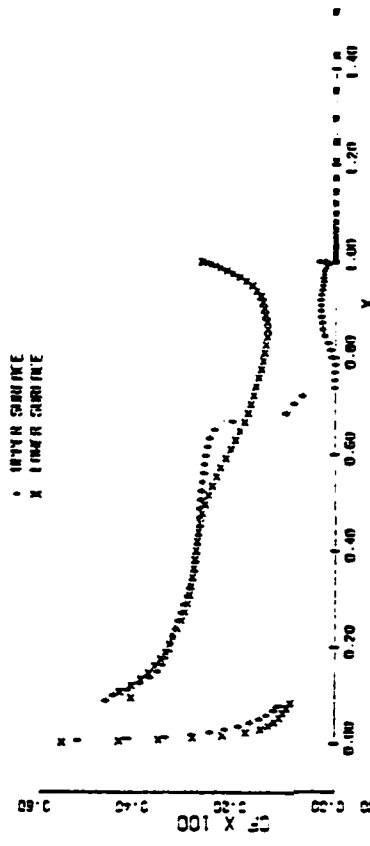
• WATER SURFACE
 X LOWER SURFACE



GA(C)-250 (111-7) UPPER SURFACE 0.0.7725, CI 0.50, RE 6.106
 0.0.7725 (111-7) LOWER SURFACE 0.0.7725, CI 0.50, RE 6.106
 X(111-7) 0.0.7725 (111-7) 0.0.7725 (111-7) 0.0.7725 (111-7)

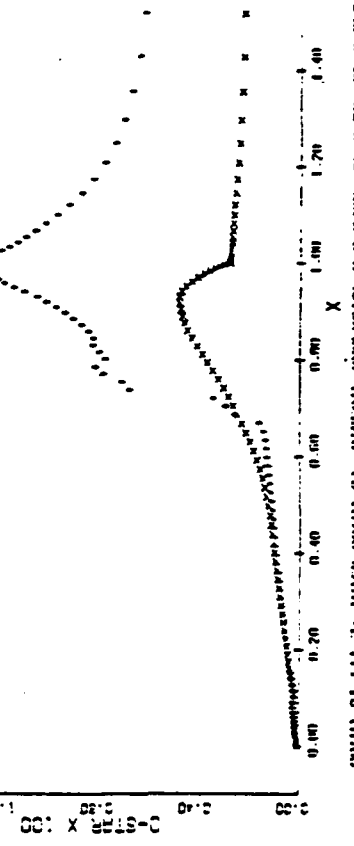
SKIN FRICTION

• WATER SURFACE
 X LOWER SURFACE



DISPLACEMENT THICKNESS

• WATER SURFACE
 X LOWER SURFACE



GA(W)-2T (111-7) UPPER SURFACE 0.0.7725, CI 0.50, RE 6.106
 0.0.7725 (111-7) LOWER SURFACE 0.0.7725, CI 0.50, RE 6.106
 X(111-7) 0.0.7725 (111-7) 0.0.7725 (111-7) 0.0.7725 (111-7)

Figure 2. Skin friction and boundary-layer displacement thickness on the GA(C)-250 and GA(W)-2T airfoils at $M_\infty = 0.7725$, $C_l = 0.50$, and $Re = 6.106$.

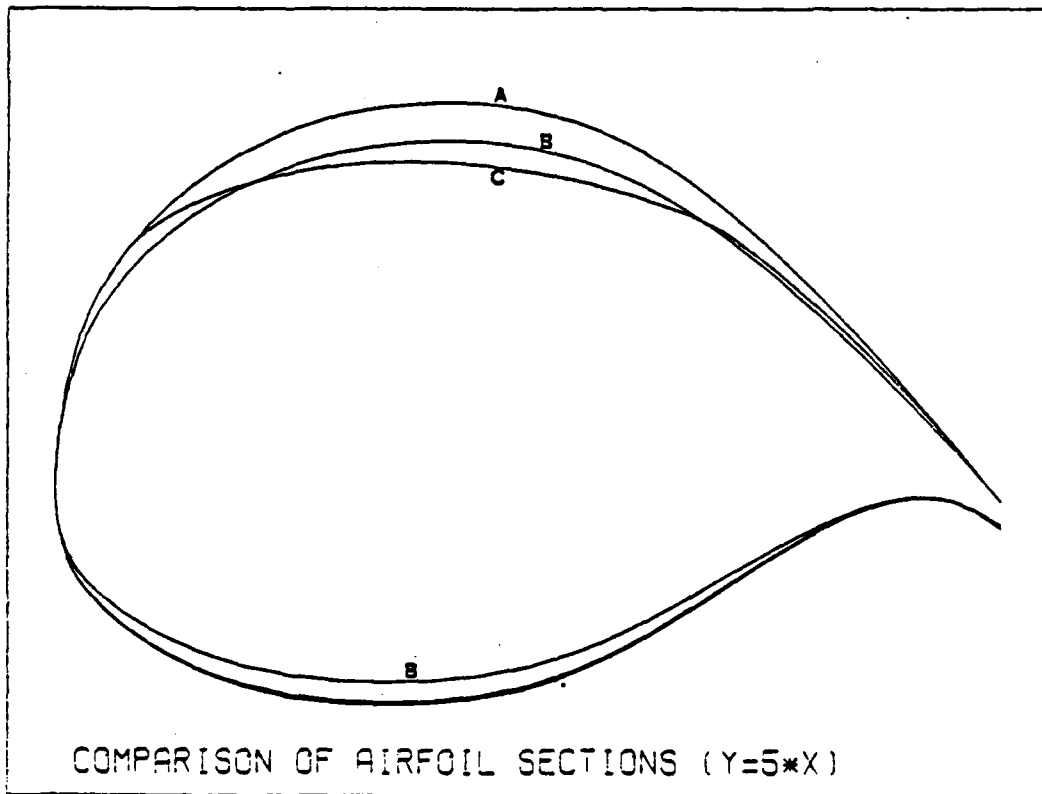
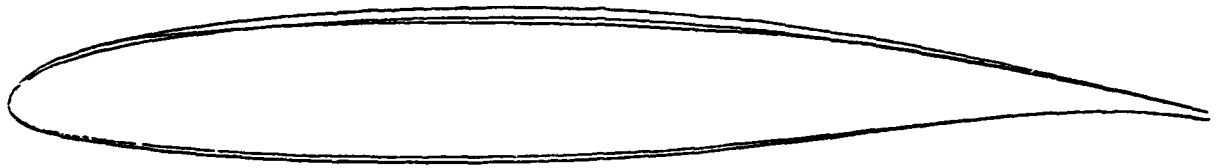


Figure 3. Comparison of the GA(W)-2 [A], GA(W)-2T [B], and GA(C)-250 [C] airfoils.

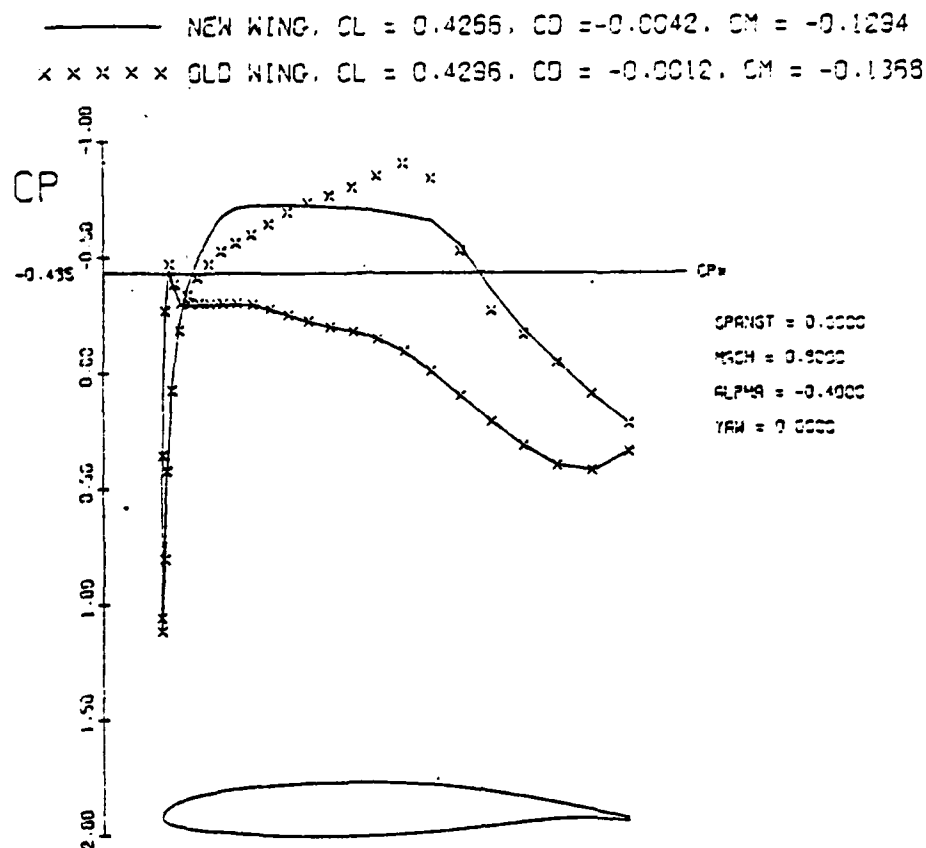


Figure 4. Pressures and wing section shapes for a wing derived from the GA(W)-2T airfoil and a shock-free design that results from this airfoil when used as a baseline. The lift coefficient of the non-shock free wing is 0.430 and the wing root is 11.7 per cent thick. The lift coefficient for the shock-free wing is 0.364 and this wing is about 11.4 per cent thick. The wing planform is shown at the end of the Figure.

— NEW WING. $C_L = 0.4504$, $C_D = -0.0026$, $C_M = -0.1432$
 x x x x x OLD WING. $C_L = 0.4545$, $C_D = 0.0012$, $C_M = -0.1528$

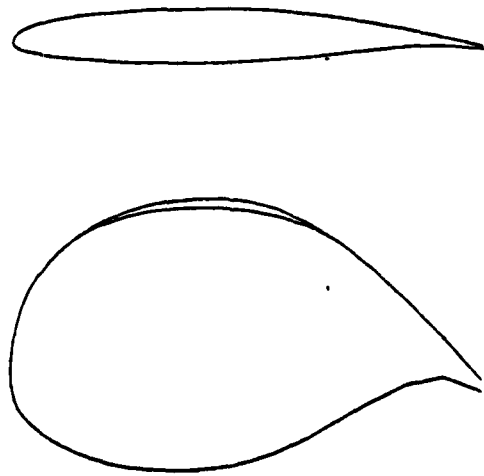
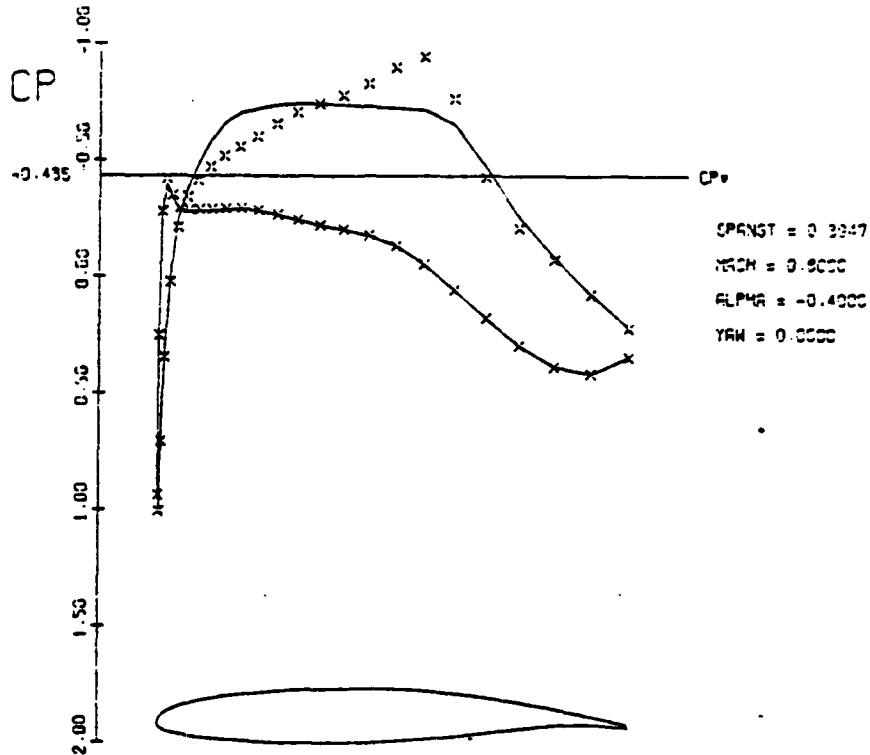


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Figure 4 (continued).

_____ NEW WING. $C_L = 0.4484$, $C_D = 0.0026$, $C_M = -0.1331$
 x x x x x OLD WING. $C_L = 0.4563$, $C_D = 0.0082$, $C_M = -0.1455$

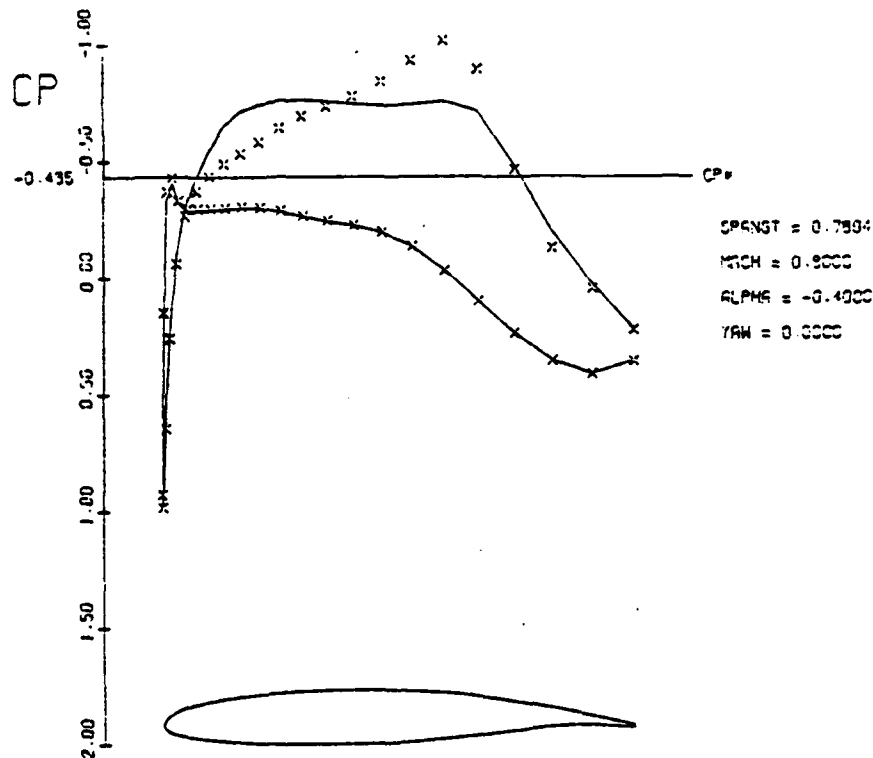


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Figure 4 (continued).

_____ NEW WING, $C_L = 0.4573$, $C_D = -0.0009$, $C_M = -0.1452$
 x x x x x OLD WING, $C_L = 0.4631$, $C_D = 0.0053$, $C_M = -0.1595$

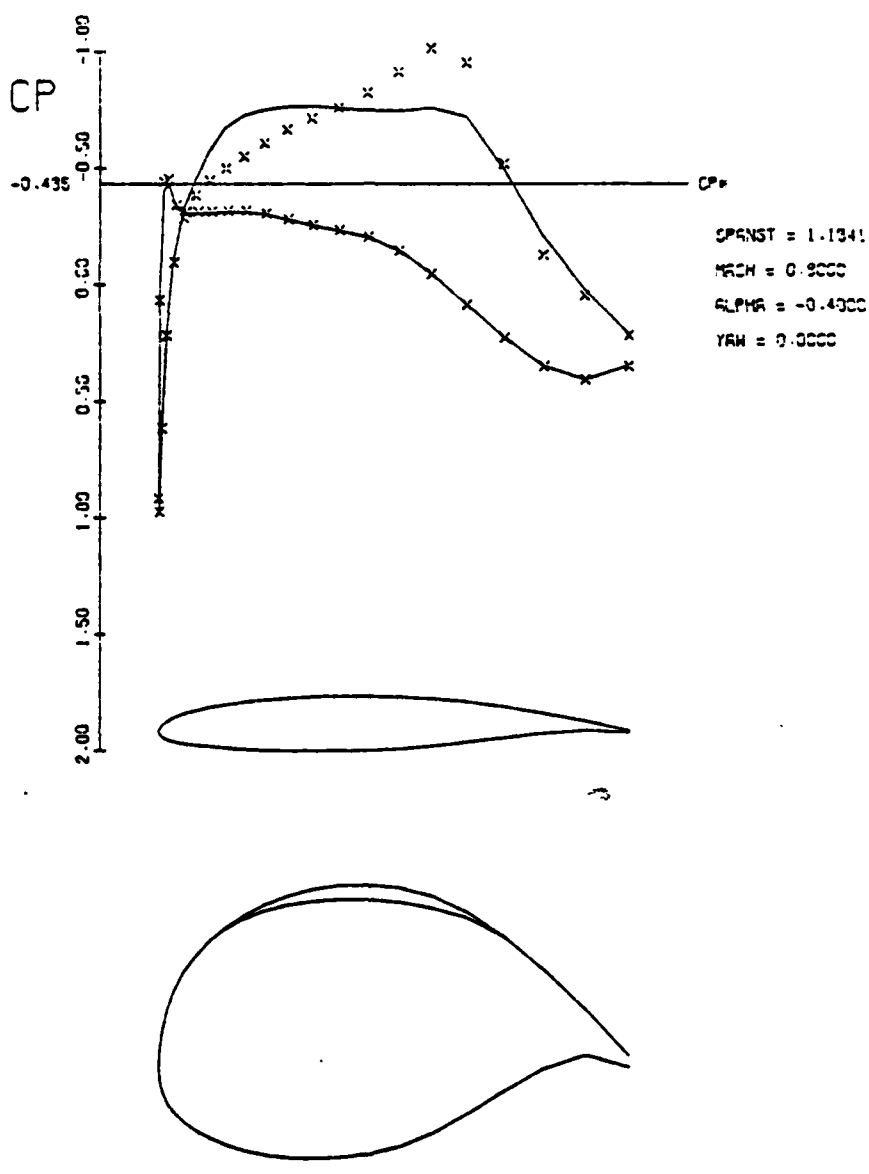


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Figure 4 (continued).

_____ NEW WING. $CL = 0.4510$. $CD = -0.0065$. $CM = -0.1598$
 x x x x x OLD WING. $CL = 0.4579$. $CD = -0.0007$. $CM = -0.1745$

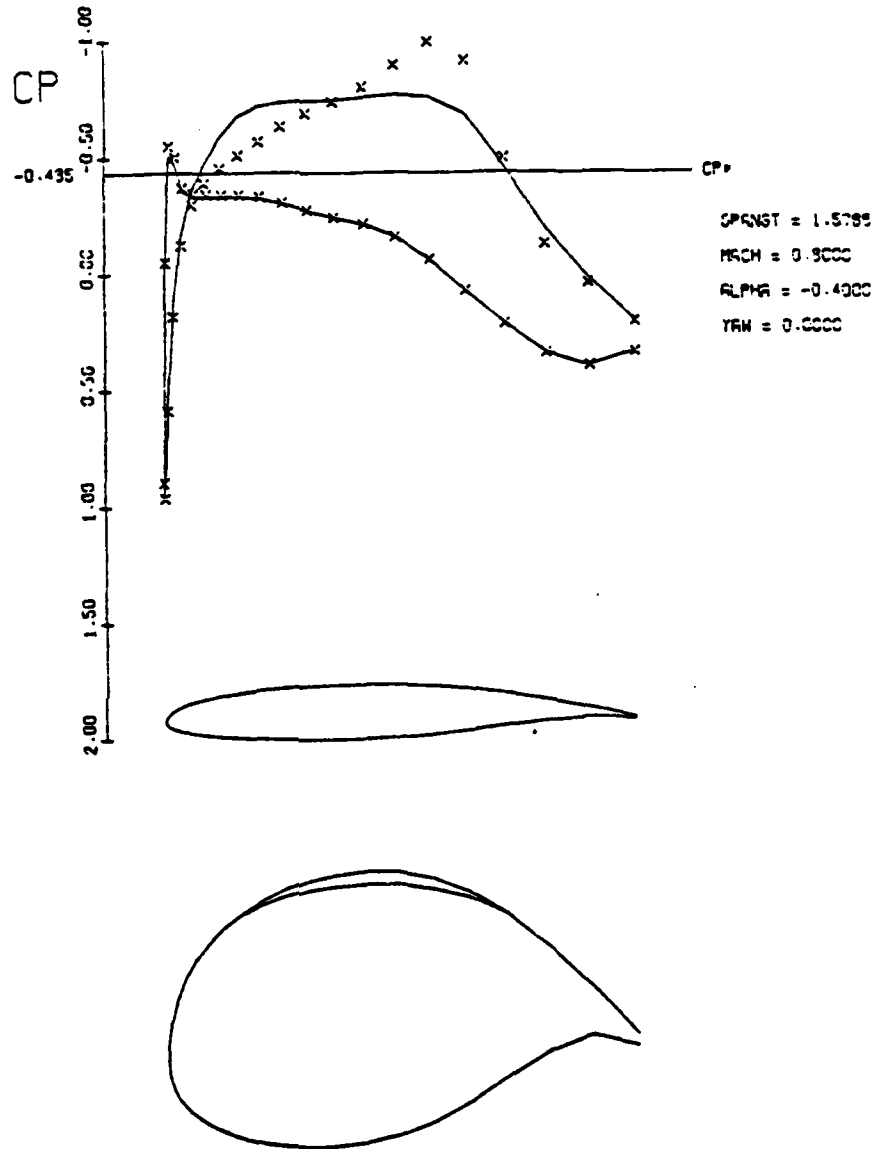


Figure 4. Pressures and wing section shapes for a wing derived from the GA(W)-2T airfoil and a shock-free design that results from this airfoil when used as a baseline. The lift coefficient of the non-shock free wing is 0.430 and the wing root is 11.7 per cent thick. The lift coefficient for the shock-free wing is 0.364 and this wing is about 11.4 per cent thick. The wing planform is shown at the end of the Figure.

————— NEW WING, $C_L = 0.3995$, $C_D = -0.0076$, $C_M = -0.1424$
 x x x x x OLD WING, $C_L = 0.4075$, $C_D = -0.0030$, $C_M = -0.1572$

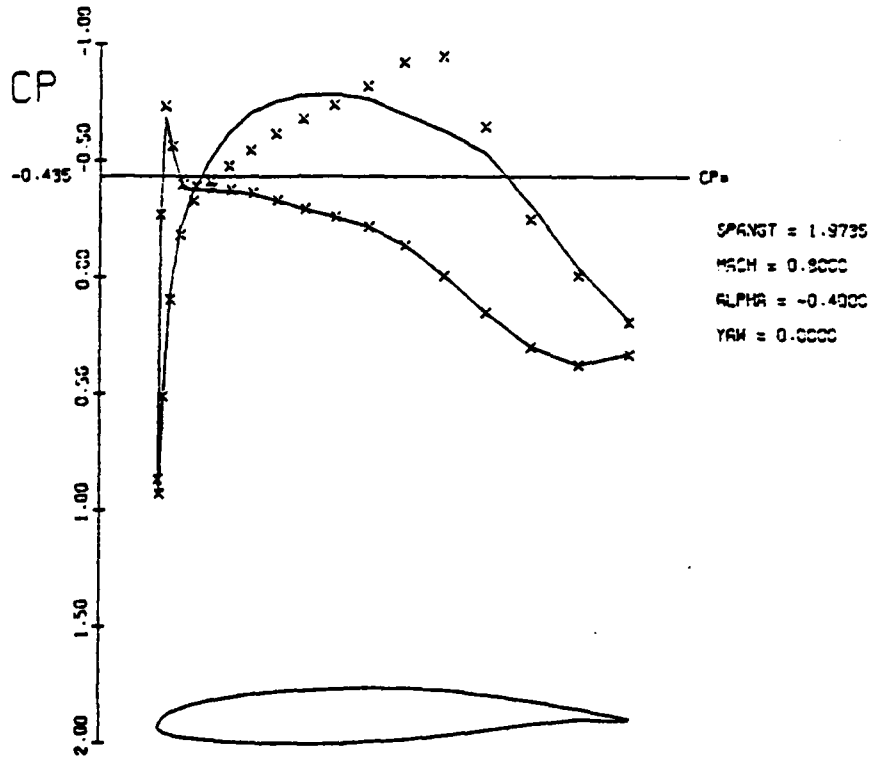


Figure 4. Pressures and wing section shapes for a wing derived from the GA(W)-2T airfoil and a shock-free design that results from this airfoil when used as a baseline. The lift coefficient of the non-shock free wing is 0.430 and the wing root is 11.7 per cent thick. The lift coefficient for the shock-free wing is 0.364 and this wing is about 11.4 per cent thick. The wing planform is shown at the end of the Figure.

Figure 4 (continued).

_____ NEW WING. $CL = 0.3095$, $CD = -0.0131$, $CM = -0.1219$
 x x x x x OLD WING. $CL = 0.3166$, $CD = -0.0104$, $CM = -0.1295$

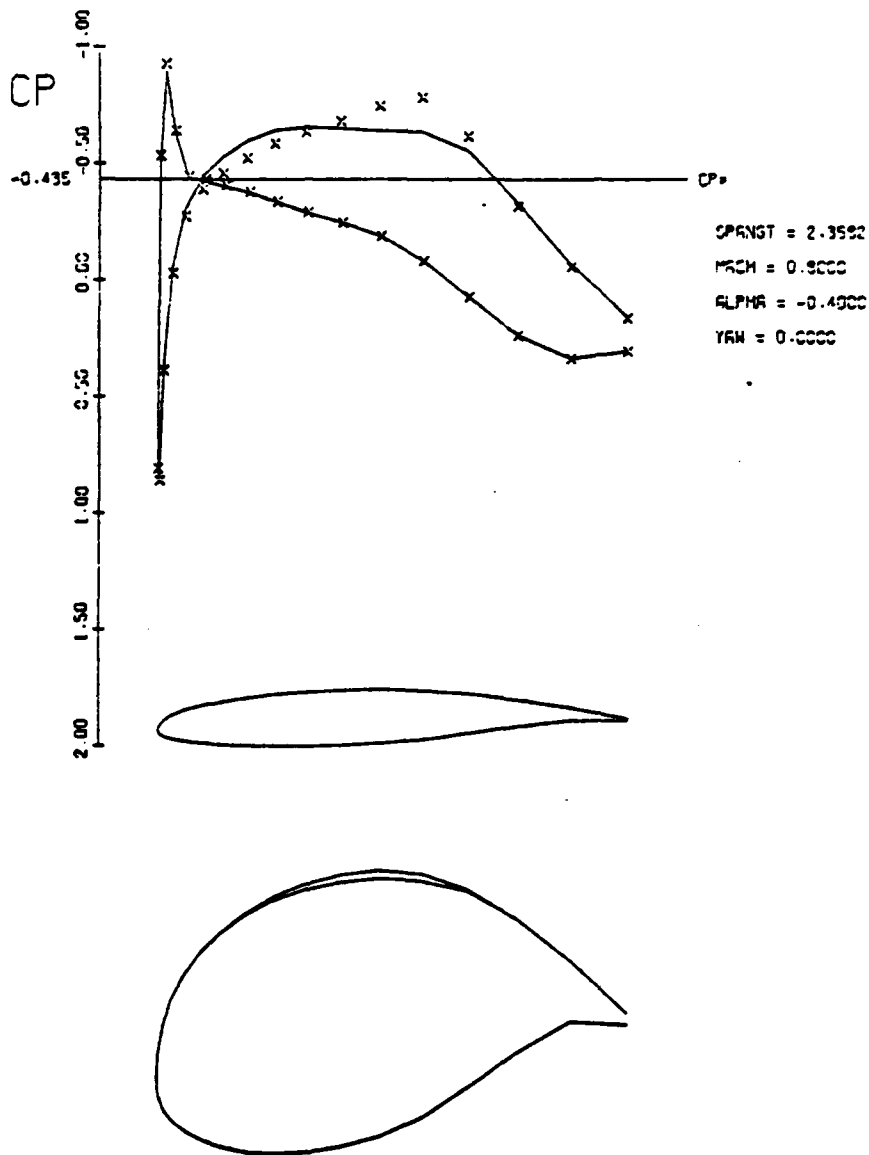
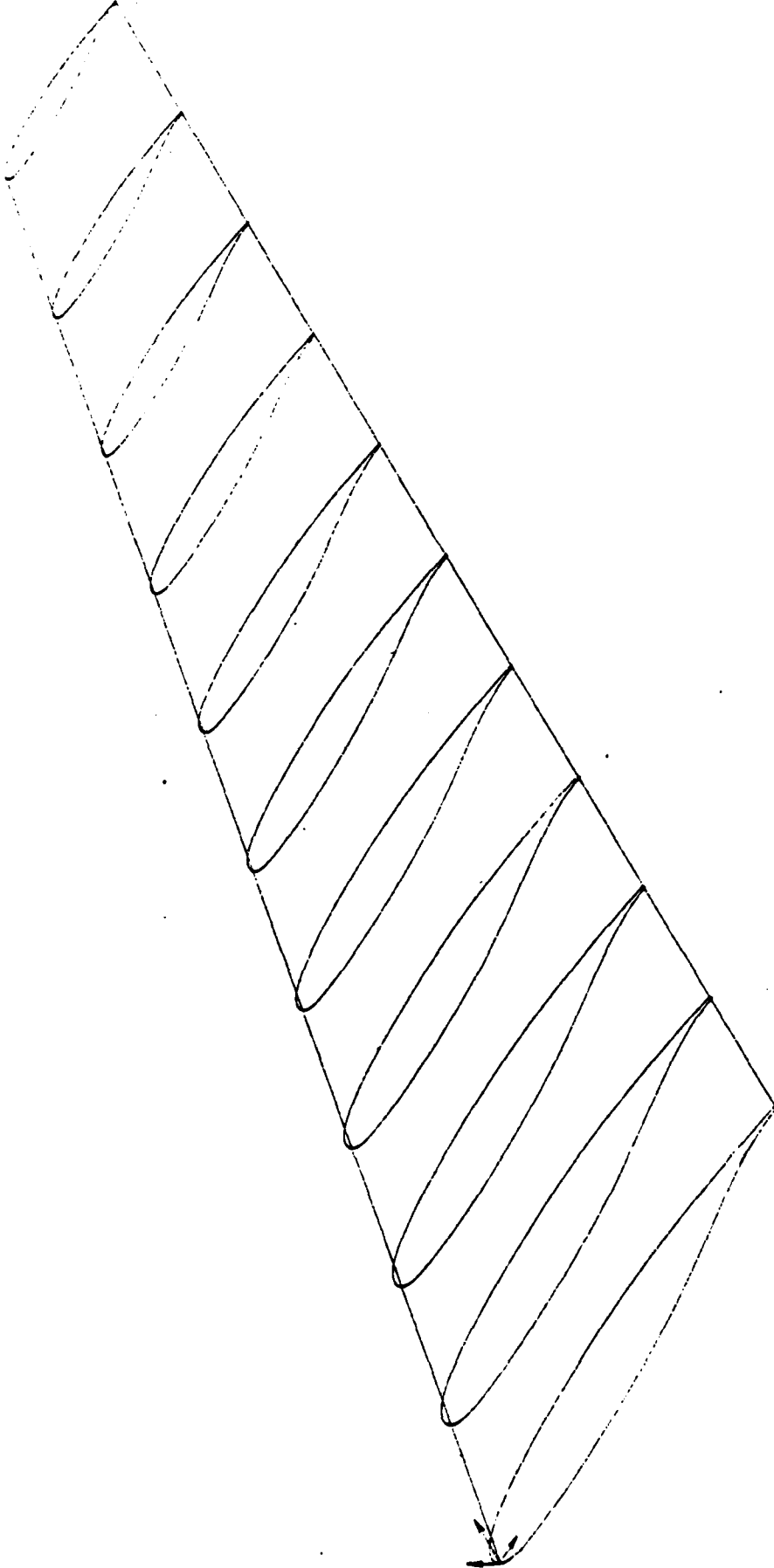


Figure 4. Pressures and wing section shapes for a wing derived from the GA(W)-2T airfoil and a shock-free design that results from this airfoil when used as a baseline. The lift coefficient of the non-shock free wing is 0.430 and the wing root is 11.7 per cent thick. The lift coefficient for the shock-free wing is 0.364 and this wing is about 11.4 per cent thick. The wing planform is shown at the end of the Figure.

Figure 4 (continued).



Figures 4&5. Learjet Century III wing planform with the baseline airfoil section that was used for the shock-free wing design of Figure 5.

— NEW WING. $CL = 0.4416$. $CD = -0.0043$. $CM = -0.1336$
 x x x x x OLD WING. $CL = 0.4451$. $CD = -0.0020$. $CM = -0.1394$

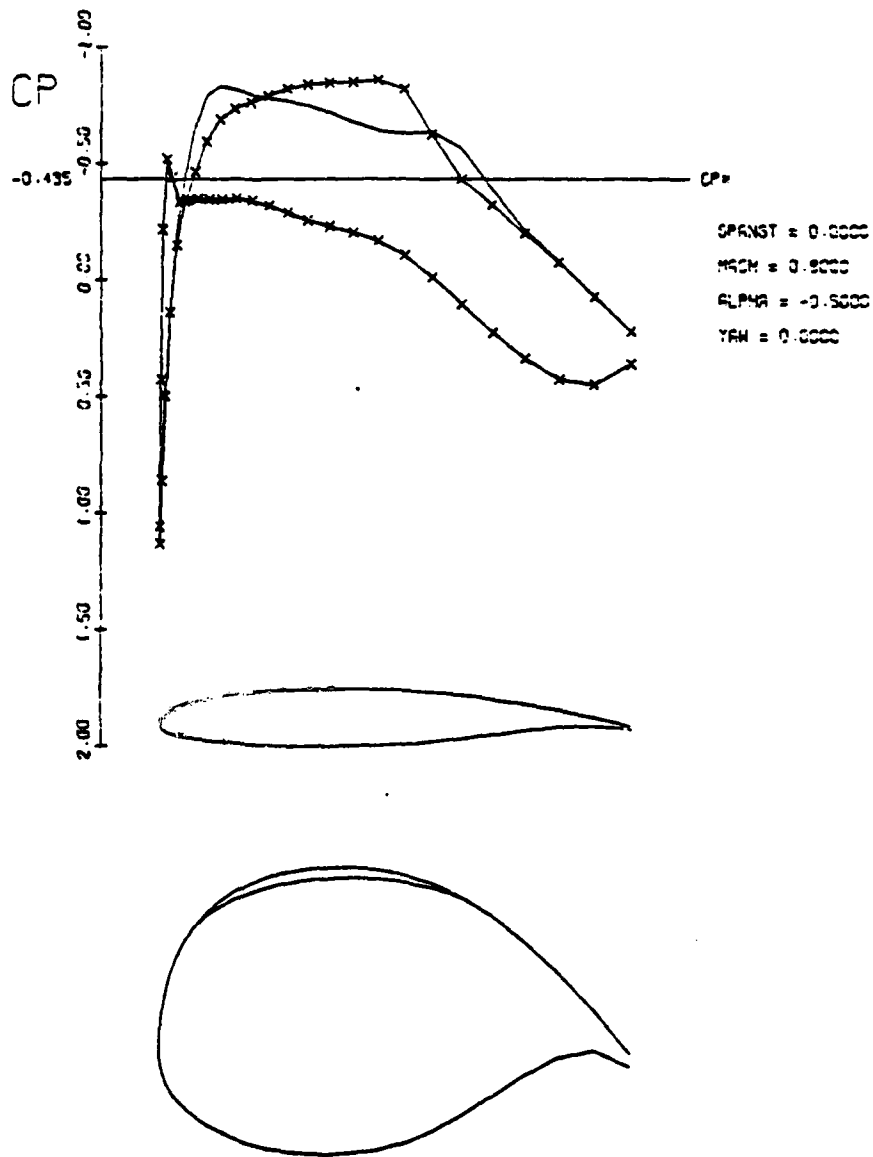


Figure 5. Pressures and wing section shapes for a wing derived from the baseline airfoil that gave the GA(C)-250 shock-free airfoil. Also shown are the pressures on this baseline airfoil. The lift coefficient of the shock-free design is 0.439; that for the baseline wing is 0.447. The proper comparison here is between this shock-free design and the old wing of Figure 4. These wings have the same thickness and nearly the same lift coefficient.

————— NEW WING. $CL = 0.4655$. $CD = -0.0032$. $CM = -0.1473$
 x x x x x OLD WING. $CL = 0.4717$. $CD = -0.0007$. $CM = -0.1534$

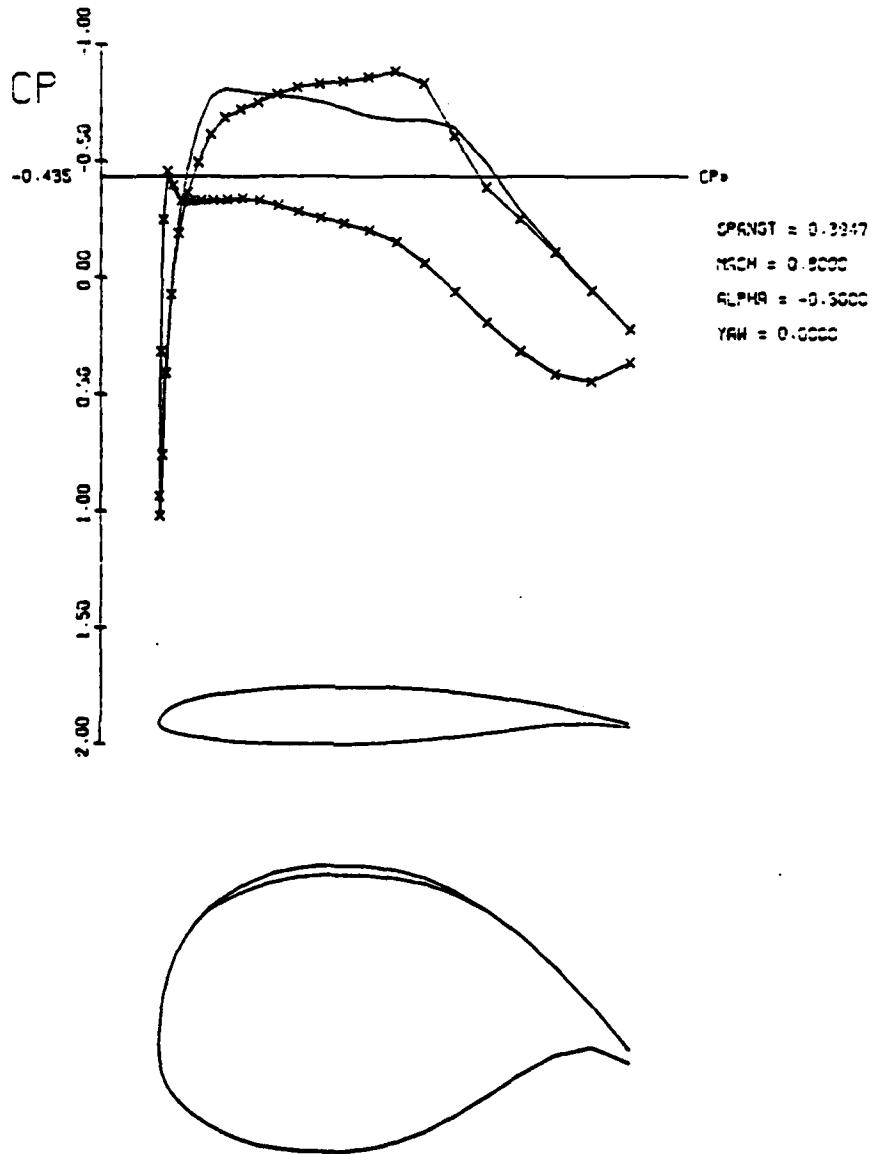


Figure 5. Pressures and wing section shapes for a wing derived from the baseline airfoil that gave the QA(C)-250 shock-free airfoil. Also shown are the pressures on this baseline airfoil. The lift coefficient of the shock-free design is 0.439; that for the baseline wing is 0.447. The proper comparison here is between this shock-free design and the old wing of Figure 4. These wings have the same thickness and nearly the same lift coefficient.

Figure 5 (continued).

_____ NEW WING. $CL = 0.4621$. $CD = 0.0020$. $CM = -0.1350$
 x x x x x OLD WING. $CL = 0.4693$. $CD = 0.0057$. $CM = -0.1448$

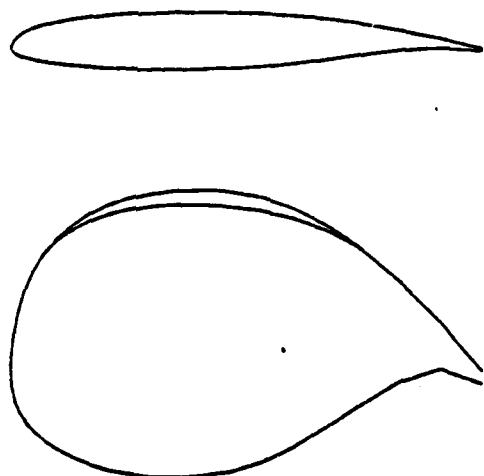
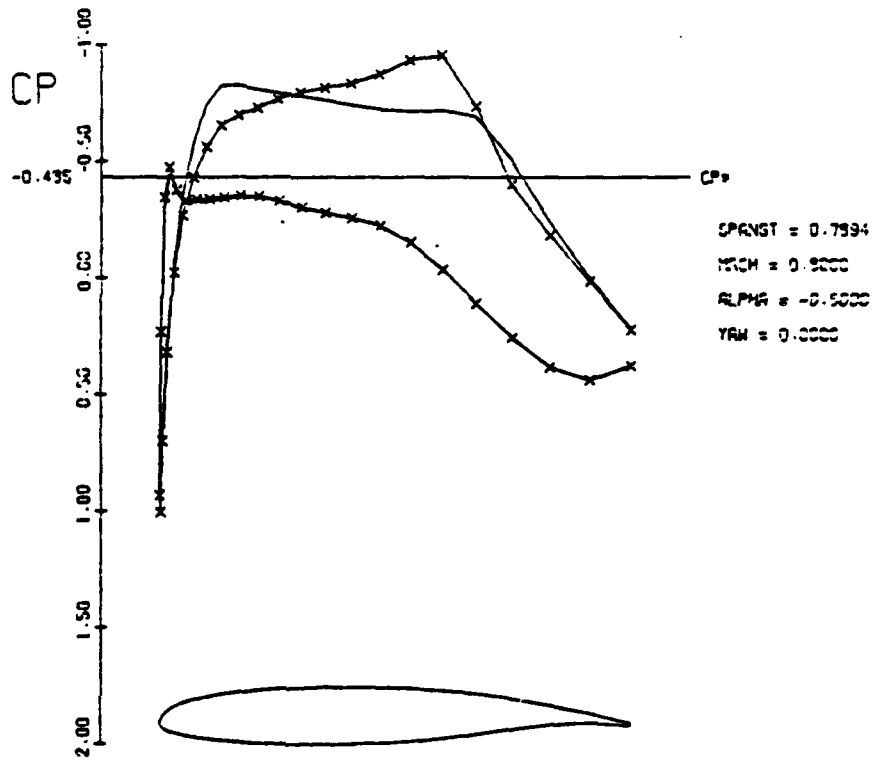


Figure 5. Pressures and wing section shapes for a wing derived from the baseline airfoil that gave the GA(C)-250 shock-free airfoil. Also shown are the pressures on this baseline airfoil. The lift coefficient of the shock-free design is 0.439; that for the baseline wing is 0.447. The proper comparison here is between this shock-free design and the old wing of Figure 4. These wings have the same thickness and nearly the same lift coefficient.

Figure 5 (continued).

_____ NEW WING. $C_L = 0.4721$, $C_D = -0.0017$, $C_M = -0.1495$
 x x x x x OLD WING. $C_L = 0.4805$, $C_D = 0.0025$, $C_M = -0.1591$

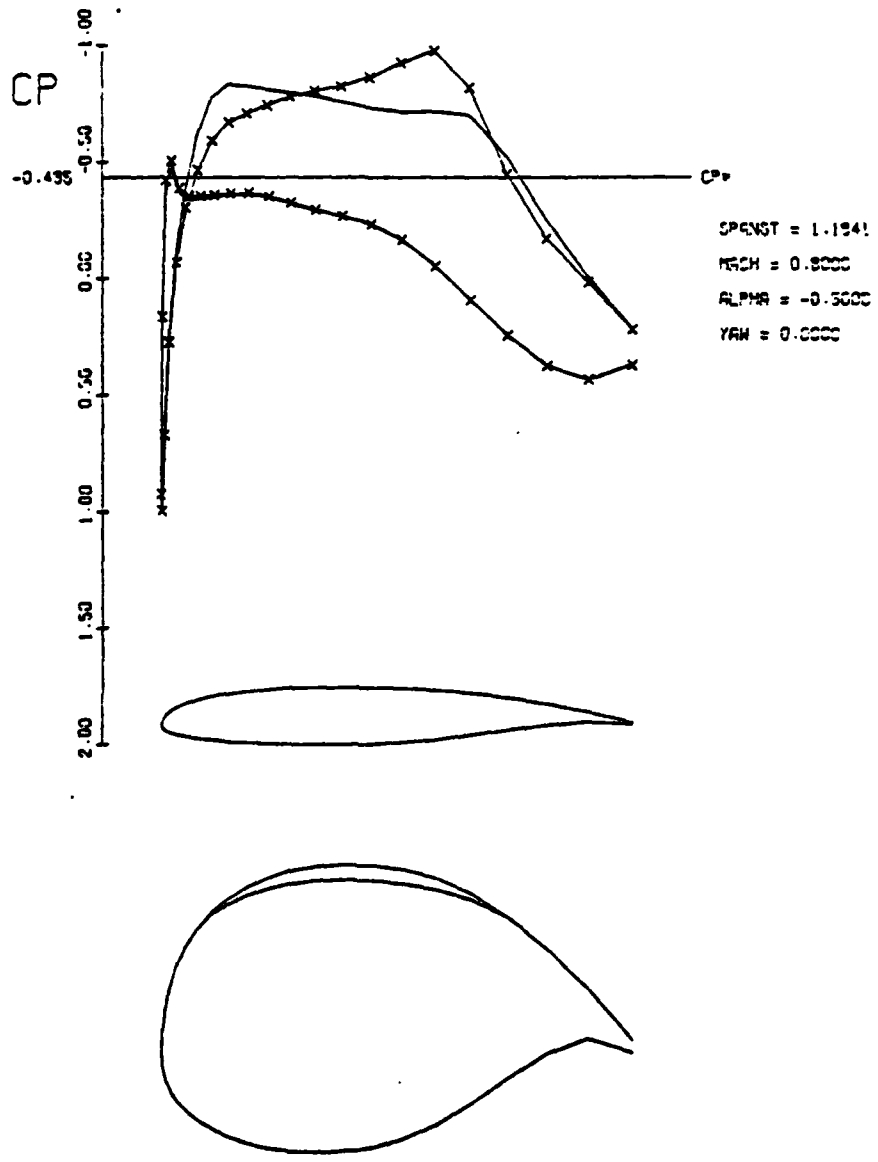


Figure 5. Pressures and wing section shapes for a wing derived from the baseline airfoil that gave the GA(C)-250 shock-free airfoil. Also shown are the pressures on this baseline airfoil. The lift coefficient of the shock-free design is 0.439; that for the baseline wing is 0.447. The proper comparison here is between this shock-free design and the old wing of Figure 4. These wings have the same thickness and nearly the same lift coefficient.

Figure 5 (continued).

— NEW WING. $C_L = 0.4140$. $C_D = -0.0090$. $C_M = -0.1457$
 x x x x x OLD WING. $C_L = 0.4250$. $C_D = -0.0063$. $C_M = -0.1556$

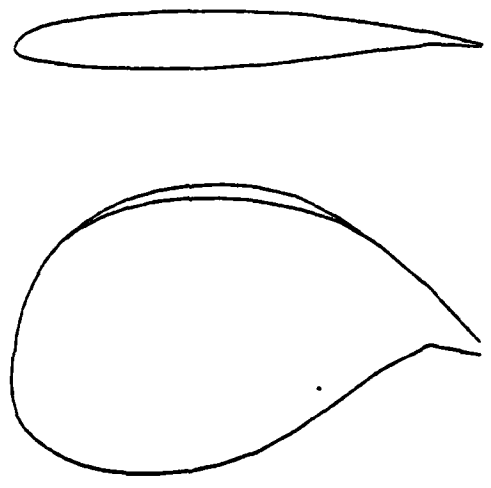
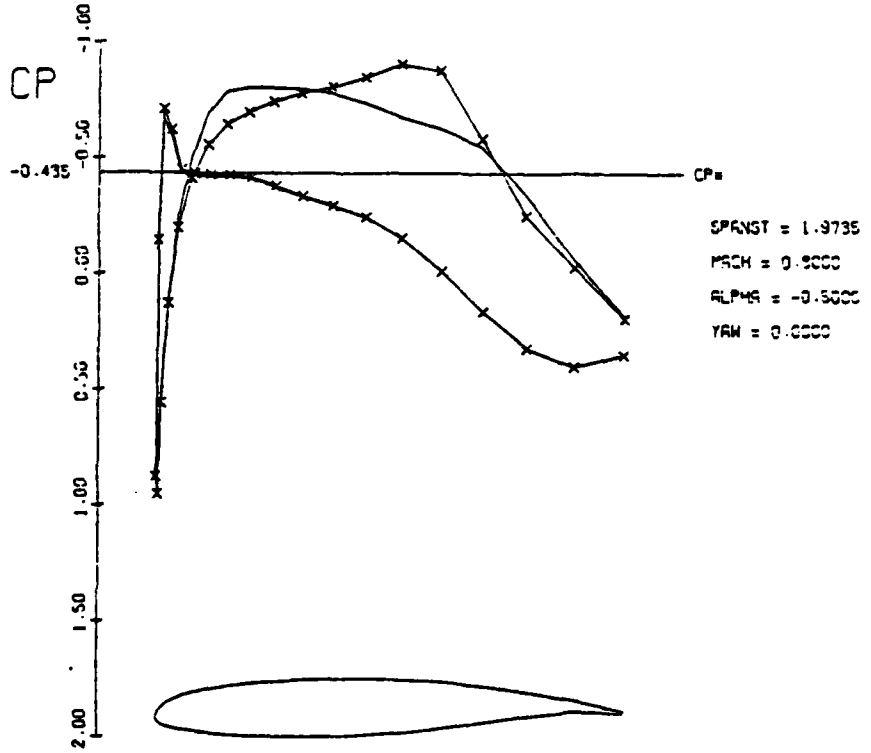


Figure 5. Pressures and wing section shapes for a wing derived from the baseline airfoil that gave the GA(C)-250 shock-free airfoil. Also shown are the pressures on this baseline airfoil. The lift coefficient of the shock-free design is 0.439; that for the baseline wing is 0.447. The proper comparison here is between this shock-free design and the old wing of Figure 4. These wings have the same thickness and nearly the same lift coefficient.

Figure 5 (continued).

————— NEW WING, $C_L = 0.3213$, $C_D = -0.0151$, $C_M = -0.1251$
 x x x x x OLD WING, $C_L = 0.3309$, $C_D = -0.0139$, $C_M = -0.1305$

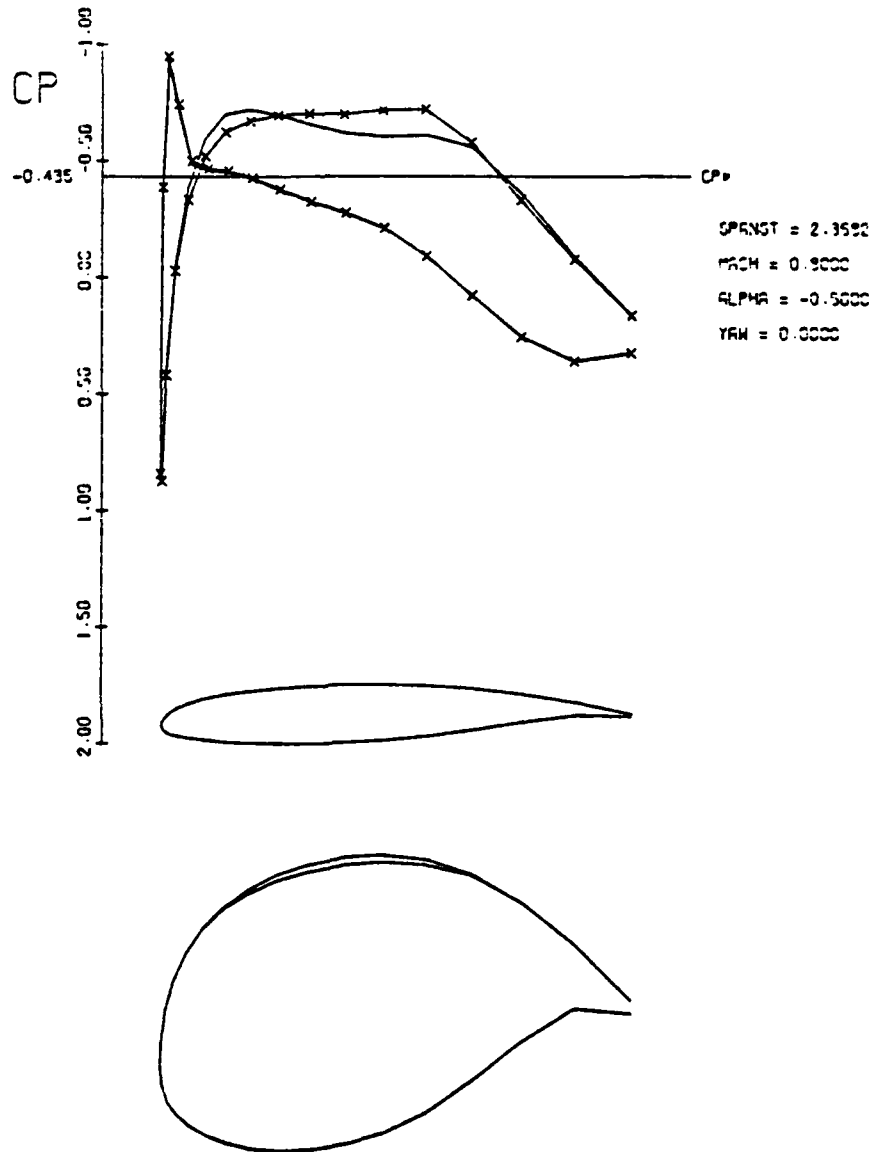
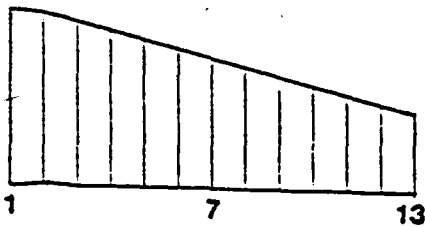
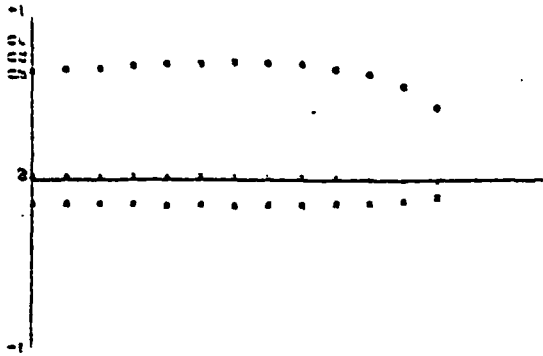


Figure 5. Pressures and wing section shapes for a wing derived from the baseline airfoil that gave the GA(C)-250 shock-free airfoil. Also shown are the pressures on this baseline airfoil. The lift coefficient of the shock-free design is 0.439; that for the baseline wing is 0.447. The proper comparison here is between this shock-free design and the old wing of Figure 4. These wings have the same thickness and nearly the same lift coefficient.

Figure 5 (concluded).

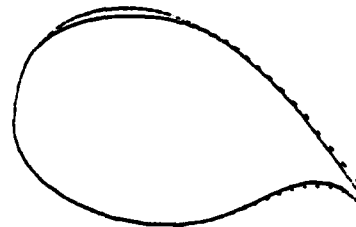
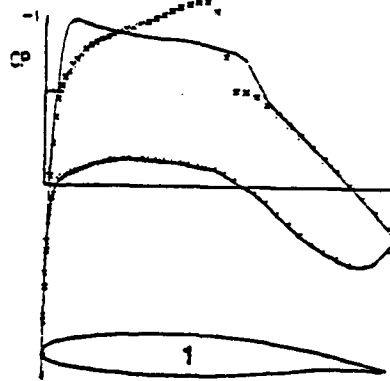
92455.21 / 92455.21 SWEEP WINGS

MACH = .7628 γ AW = .2823 ANG OF ATT. = -.4823
 ANGLE1 CL = .0566 CD = .0221 CY = -2.2557
 ANGLE2 CL = .0485 CD = .0131 CY = -2.2557



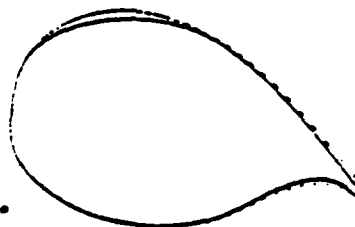
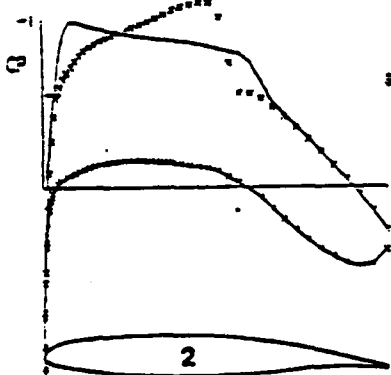
92455.21 / 92455.21 SWEEP WINGS

MACH = .7628 γ AW = .2823 ANG OF ATT. = -.4823
 ANGLE1 CL = .0592 CD = .0124 CY = -1.1353
 ANGLE2 CL = .0374 CD = .0167 CY = -1.1497



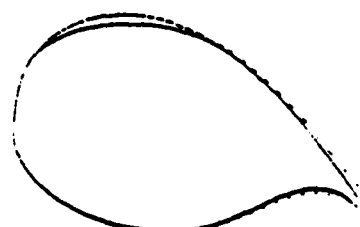
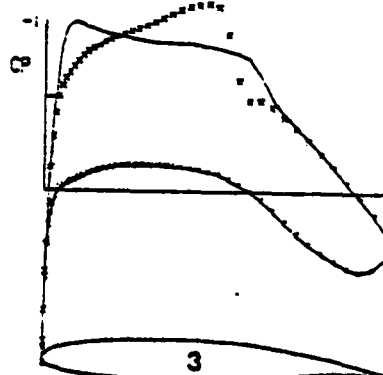
92455.21 / 92455.21 SWEEP WINGS

MACH = .7628 γ AW = .2823 ANG OF ATT. = -.4823
 ANGLE1 CL = .0596 CD = .0146 CY = -1.1383
 ANGLE2 CL = .0489 CD = .0182 CY = -1.1459



92455.21 / 92455.21 SWEEP WINGS

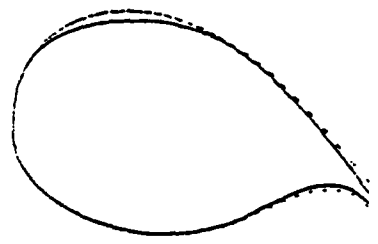
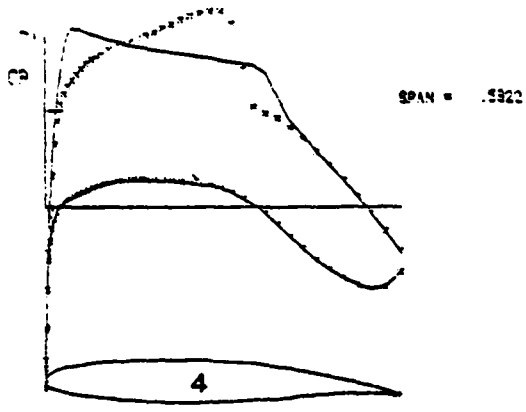
MACH = .7628 γ AW = .2823 ANG OF ATT. = -.4823
 ANGLE1 CL = .0582 CD = .0136 CY = -1.1288
 ANGLE2 CL = .0236 CD = .0124 CY = -1.1448



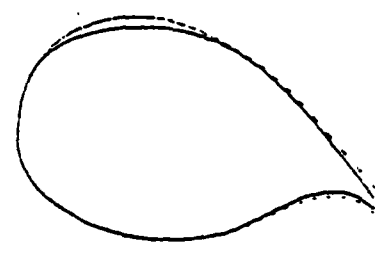
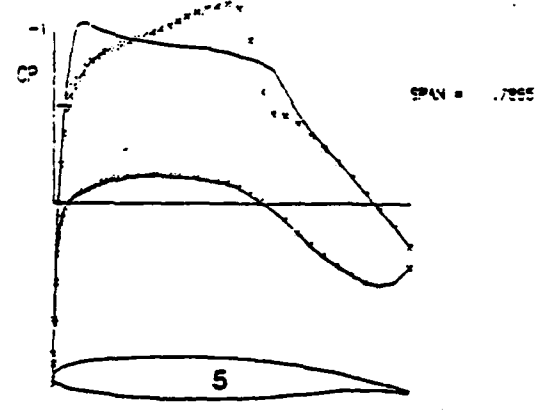
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Figure 6. Wing planform, section pressures, and section shapes for a wing that was designed to be shock free in the presence of inviscid-viscous interactions using FLO22 and the Stock 3D boundary - layer algorithm coupled by Streett's BLIM algorithm.

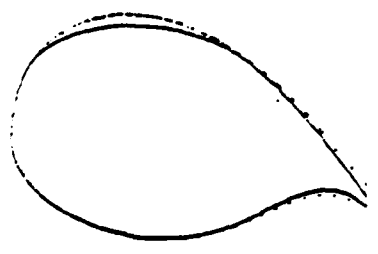
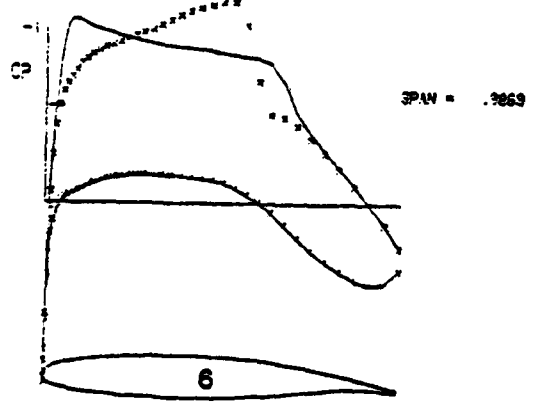
90455.01 / 90455.01 SWEEP WINGS
 MACH= .7600 γ_{AW} = .0220 ANG OF ATT.= -1.4200
 #IN61 C_L = .0792 C_D = .0120 C_M = -1.1440
 #IN62 C_L = .0792 C_D = .0177 C_M = -1.036



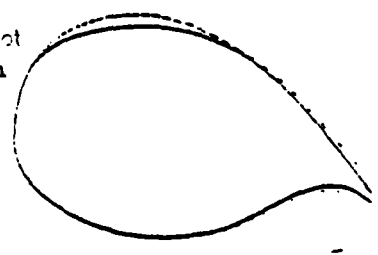
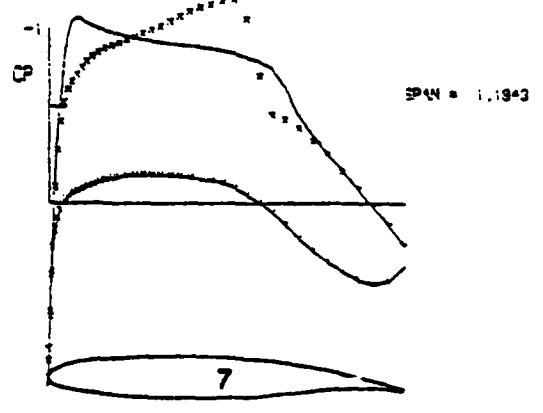
90455.01 / 90455.01 SWEEP WINGS
 MACH= .7600 γ_{AW} = .0220 ANG OF ATT.= -1.4200
 #IN61 C_L = .0395 C_D = .0120 C_M = -1.1492
 #IN62 C_L = .0391 C_D = .0158 C_M = -1.056



90455.01 / 90455.01 SWEEP WINGS
 MACH= .7600 γ_{AW} = .0220 ANG OF ATT.= -1.4200
 #IN61 C_L = .0900 C_D = .0120 C_M = -1.1439
 #IN62 C_L = .0892 C_D = .0130 C_M = -1.072



90455.01 / 90455.01 SWEEP WINGS
 MACH= .7600 γ_{AW} = .0220 ANG OF ATT.= -1.4200
 #IN61 C_L = .0363 C_D = .0144 C_M = -1.1475
 #IN62 C_L = .0360 C_D = .0144 C_M = -1.057

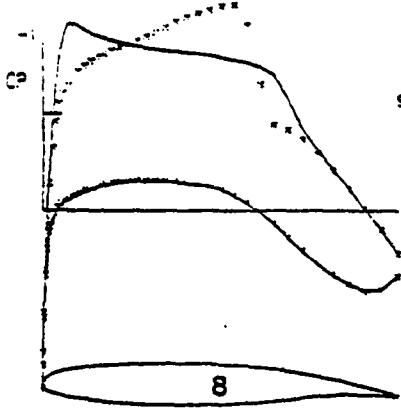


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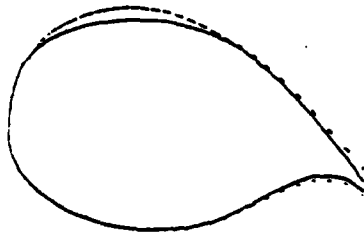
Figure 6 (continued).

33°455.01 / 30°455.01 SWEEP WINGS

MACH = .7633 YAW = .2222 ANG OF ATT. = -4.222
 #IN61 CL = .3371 CD = .3287 CM = -1.1497
 #IN62 CL = .3366 CD = .3153 CM = -1.525

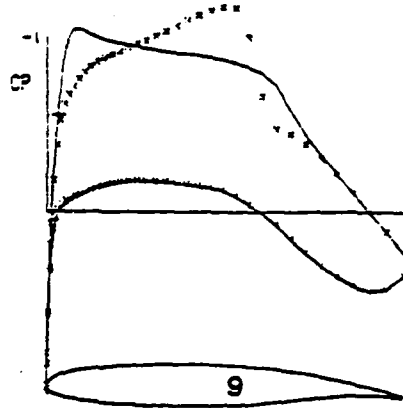


SPAN = 1.3817

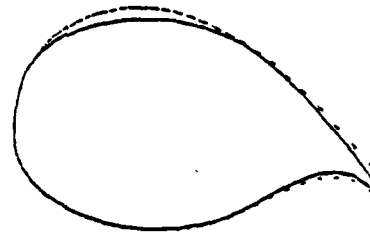


33°455.01 / 30°455.01 SWEEP WINGS

MACH = .7633 YAW = .2222 ANG OF ATT. = -4.222
 #IN61 CL = .3323 CD = .3228 CM = -1.1443
 #IN62 CL = .3322 CD = .3122 CM = -1.541

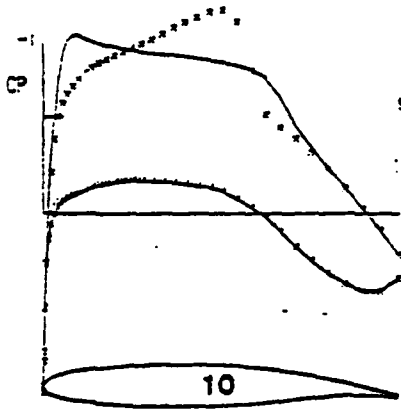


SPAN = 1.3791

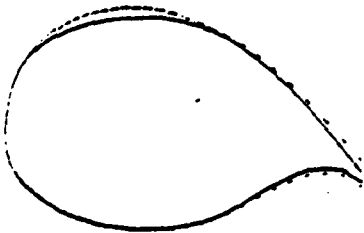


33°455.01 / 30°455.01 SWEEP WINGS

MACH = .7633 YAW = .2222 ANG OF ATT. = -4.222
 #IN61 CL = .3359 CD = .3238 CM = -1.1333
 #IN62 CL = .3358 CD = .3288 CM = -1.1452

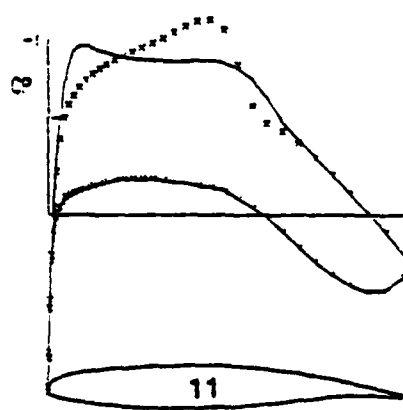


SPAN = 1.7765

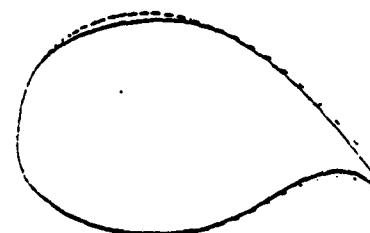


33°455.01 / 30°455.01 SWEEP WINGS

MACH = .7633 YAW = .2222 ANG OF ATT. = -4.222
 #IN61 CL = .3253 CD = .3221 CM = -1.1231
 #IN62 CL = .3272 CD = .3227 CM = -1.1452



SPAN = 1.3729



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Figure 6 (continued).

30455.31 / 30455.31 SWEEP WINGS
 TACH= .7522 YAW= .2222 ANG OF ATT= -.4222
 ANGI= .7522 CL= .7524 CD= -.2221 CP= -.1243
 ANG2= CL= .7533 CD= -.2227 CP= -.1282

30455.31 / 30455.21 SWEEP WINGS
 TACH= .7522 YAW= .2222 ANG OF ATT= -.4222
 ANGI= .7522 CL= .7523 CD= -.2228 CP= -.1243
 ANG2= CL= .7516 CD= -.2249 CP= -.1272

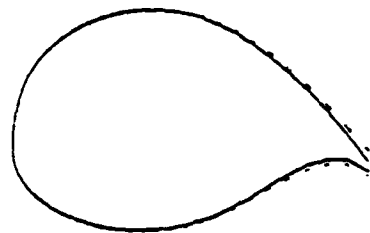
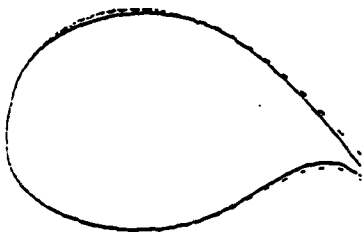
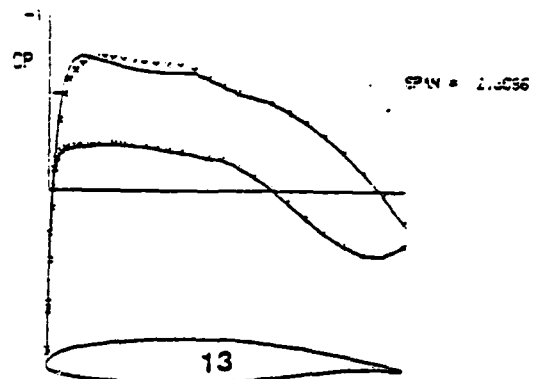
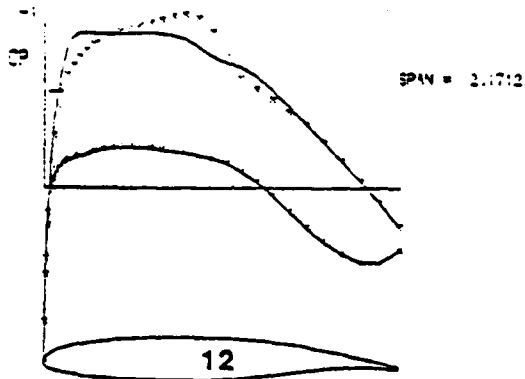


Figure 6 (concluded).

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