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FINAL REPORT

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Submitted by  
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Research has been carried out in two areas: first, the extension of Pisarenko's method to multidimensional (m-D) signals and arrays; second, the extension of the maximum entropy method (MEM) to non-uniformly sampled m-D signals and arrays. Most of this work has been of a theoretical nature.		

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**PI: James H. McClellan**

Research has been carried out in two areas: first, the extension of Pisarenko's method to multidimensional (m-D) signals and arrays; second, the extension of the maximum entropy method (MEM) to non-uniformly sampled m-D signals and arrays. Most of this work has been of a theoretical nature.

A procedure for calculating Pisarenko's estimate has been derived. The form of the estimate is that of sinusoids (or plane waves) in a background of noise with known spectral content, but unknown total power. The problem can be reduced to a linear program that is computationally similar to the one used for designing two-dimensional finite impulse response (FIR) digital filters.

In the process of deriving Pisarenko's spectral estimate, one is led naturally to consider the "extendibility" problem: Given a finite set of samples of a presumed autocorrelation function (acf), does there exist a positive power spectrum that exactly matches the given acf samples? This extendibility problem is important in practice. Often the autocorrelation function is estimated from data samples and it is necessary to have a test to determine whether such acf estimates are extendible. One possible test is to compute Pisarenko's estimate under the assumption that the background noise is white. In the course of the computation, the white noise power will be determined; if it turns out to be negative, the acf estimates are not extendible, if positive they are extendible. If the noise power were zero, then the power spectrum would consist only of impulses. Improvements on this test will be needed in the future.

The papers by Lang and McClellan [1,2,3] develop the theory of Pisarenko's method in detail. Connections to some practical array processing problems are also given. The review papers [4,5] by McClellan also discuss Pisarenko's method in the context of the general multidimensional spectral estimation problem.

The second major topic of research was the development of a general multidimensional MEM spectral estimation algorithm. A number of such algorithms have been proposed, but the research under this contract [6,7,8,9] is unique in that a rigorous mathematical approach was used to exploit fully the convex nature of the MEM optimization problem. In particular, a general necessary and sufficient condition for the existence of the m-D MEM spectral estimate has been obtained. This existence condition comes about when a dual entropy minimization problem is derived. The dual problem is particularly important because it is a finite-dimensional convex optimization problem; whereas, the original MEM problem is infinite-dimensional. Much of the previous work on MEM used some form of the dual problem, but not the

form derived in this work. A most important point is the convex nature of the problem which guarantees that traditional numerical optimization methods such as steepest descent or quasi-Newton will converge.

A final area of investigation is the use of the new m-D spectral estimation techniques in a practical setting. Some work [10,11] has been published on the comparison of MEM with interpolation for bearing estimation with non-uniform arrays. This research has shown the superiority of the general MEM algorithm for synthetic signals, consisting of sinusoids in noise. Work is presently underway to apply these algorithms to data from seismic arrays.

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