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EDUCATIONAL TESTING SERVICE PRINCETON NJ  
DEVELOPING A COMMON METRIC IN ITEM RESPONSE THEORY.(U)  
JUN 82 M L STOCKING, F M LORD  
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IN ITEM RESPONSE THEORY

Martha L. Stocking  
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| REPORT DOCUMENTATION PAGE                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                             | READ INSTRUCTIONS<br>BEFORE COMPLETING FORM |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------|---------------------------------------------|
| 1. REPORT NUMBER                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 2. GOVT ACCESSION NO.                                       | 3. RECIPIENT'S CATALOG NUMBER               |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | AD-A12872                                                   |                                             |
| 4. TITLE (and Subtitle)                                                                                                                                                                                                                                                                                                                                                                                                                                                         | 5. TYPE OF REPORT & PERIOD COVERED                          |                                             |
| Developing a Common Metric in Item Response Theory                                                                                                                                                                                                                                                                                                                                                                                                                              | Technical Report                                            |                                             |
| 6. AUTHOR(s)                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | 7. PERFORMING ORG. REPORT NUMBER                            |                                             |
| Virginia L. Stocking and Frederic M. Lord                                                                                                                                                                                                                                                                                                                                                                                                                                       | RR-82-25-ONR                                                |                                             |
| 8. PERFORMING ORGANIZATION NAME AND ADDRESS                                                                                                                                                                                                                                                                                                                                                                                                                                     | 9. CONTRACT OR GRANT NUMBER(s)                              |                                             |
| National Testing Service<br>Princeton, NJ 08541                                                                                                                                                                                                                                                                                                                                                                                                                                 | N00014-80-C-0402                                            |                                             |
| 10. CONTROLLING OFFICE NAME AND ADDRESS                                                                                                                                                                                                                                                                                                                                                                                                                                         | 11. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS |                                             |
| Personnel and Training Research Programs<br>Office of Naval Research (Code 458)<br>Arlington, VA 22217                                                                                                                                                                                                                                                                                                                                                                          | NR 150-453                                                  |                                             |
| 12. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)                                                                                                                                                                                                                                                                                                                                                                                                     | 13. REPORT DATE                                             |                                             |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | June 1982                                                   |                                             |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | 14. NUMBER OF PAGES                                         |                                             |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | 29                                                          |                                             |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | 15. SECURITY CLASS. (of this report)                        |                                             |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | Unclassified                                                |                                             |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | 16. DECLASSIFICATION/DOWNGRADING SCHEDULE                   |                                             |
| 17. DISTRIBUTION STATEMENT (of this Report)                                                                                                                                                                                                                                                                                                                                                                                                                                     |                                                             |                                             |
| Approved for public release; distribution unlimited.                                                                                                                                                                                                                                                                                                                                                                                                                            |                                                             |                                             |
| 18. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)                                                                                                                                                                                                                                                                                                                                                                                      |                                                             |                                             |
| 19. SUPPLEMENTARY NOTES                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                             |                                             |
| 20. KEY WORDS (Continue on reverse side if necessary and identify by block number)                                                                                                                                                                                                                                                                                                                                                                                              |                                                             |                                             |
| Item Response Theory, Common Metric, Scale Transformations, Item Banking, Equating, Item Bias                                                                                                                                                                                                                                                                                                                                                                                   |                                                             |                                             |
| 21. ABSTRACT (Continue on reverse side if necessary and identify by block number)                                                                                                                                                                                                                                                                                                                                                                                               |                                                             |                                             |
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## Developing a Common Metric in Item Response Theory

### Abstract

A common problem arises when independent estimates of item parameters from two separate data sets must be expressed in the same metric. This problem is frequently confronted in studies of horizontal and vertical equating and in studies of item bias. This paper discusses a number of methods for transforming one metric to another metric and presents a new method. Data are given comparing this new method with a current method and recommendations are made.

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## Developing a Common Metric in Item Response Theory\*

### Introduction

Suppose that item parameters for a given set of items have been independently estimated using data obtained from two different groups of examinees. These item parameter estimates will be different because the metric or scale defined by each independent calibration of the items is different. Many applications of item response theory (IRT) require that these item parameter estimates be expressed in the same metric. Such applications include vertical score-scale equating, horizontal score-scale equating, and item bias studies.

It is possible to transform item parameter estimates in one metric to another metric by a number of different methods. This paper will discuss the nature of these scale transformations, survey a number of current transformation methods, and present a new method and some results of its application.

### The Nature of Scale Transformations

Item response theory models  $P_i(\theta_a; \alpha_i, \beta_i, \gamma_i)$ , the probability of a correct response to item  $i$  by a person with ability level  $\theta_a$ . In typical models,  $P_i(\theta_a; \alpha_i, \beta_i, \gamma_i)$  is a function of  $\alpha_i(\theta_a - \beta_i)$ , where  $\alpha_i$  is the item discrimination,  $\beta_i$  is the item difficulty,

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and  $\gamma_i$  is the probability that an individual of very low ability answers the item correctly. When  $P_i(\theta_a; \alpha_i, \beta_i, \gamma_i)$  is a function of  $\alpha_i(\theta_a - \beta_i)$ , the origin and unit of measurement of the ability (and difficulty) metric are undetermined. That is to say, suppose  $\theta_a$  is transformed by a linear transformation, producing  $\theta_a^*$ . Suppose the same linear transformation is applied to  $\beta_i$  to produce  $\beta_i^*$ . Finally,  $\alpha_i$  is divided by the multiplicative constant of the linear transformation to produce  $\alpha_i^*$ . These transformations will not change the probability of a correct response:  $P_i(\theta_a^*; \alpha_i^*, \beta_i^*, \gamma_i) = P_i(\theta_a; \alpha_i, \beta_i, \gamma_i)$ . Notice that no transformation is necessary for the  $\gamma_i$  because  $\gamma_i$  is on the probability metric.

If an item is calibrated, i.e., its parameters are estimated, as part of one test, and then calibrated as part of a second test given to a different group, the actual values of the estimates of the parameters will differ because the scales established by the two calibrations differ. However, the relationship between these two scales will be linear since they differ only in origin and unit of measurement.

If  $b_{i1}$  is the estimate of item difficulty from the calibration of item  $i$  in test 1, and  $b_{i2}$  is the estimate of the same item difficulty from the calibration of test 2,  $b_{i2}^*$ , the value of  $b_{i2}$  transformed to the scale of test 1, is

$$b_{i2}^* = Ab_{i2} + B \quad , \quad (1)$$

where  $A$  and  $B$  are constants of the linear transformation of scale. If estimated item difficulties are transformed by a linear transformation, estimated abilities must be transformed by the same transformation, thus

$$\theta_{a2}^* = A\hat{\theta}_{a2} + B \quad . \quad (2)$$

If estimated item difficulty and ability are transformed by these linear expressions, then estimated item discrimination is transformed by

$$a_{i2}^* = a_{i2}/A \quad . \quad (3)$$

These transformations do not change  $a_{i2}(\hat{\theta}_{a2} - b_{i2})$ , consequently

$$P_i(\hat{\theta}_{a2}; a_{i2}, b_{i2}, c_{i2}) = P_i(\theta_{a2}^*, a_{i2}^*, b_{i2}^*, c_{i2}) \quad .$$

The problem of transforming the scales reduces to the problem of finding the appropriate  $A$  and  $B$  of the linear transformation. If we were dealing with true values of the parameters on their respective scales, it would be simple to find the correct values of  $A$  and  $B$ ; we could plot the values of two or more item difficulties and determine the line passing through them. But, we do not have true values; we have only estimates of them, and these estimates contain error. The estimated item difficulties will not fall into a straight line, but be scattered around some straight line. All methods of transforming scales attempt to estimate the parameters of this line by various techniques, and are applicable to any IRT model where  $P_i(\theta_a; \alpha_i, \beta_i, \gamma_i)$  is a function of  $a_i(\theta_a - \beta_i)$ .

### Current Methods

Superficially, the problem of finding the linear relationship between two sets of numbers might seem to call for simple regression techniques. The estimated item difficulties (or abilities) from one calibration might be used as the independent variable, and those obtained from the second calibration as the dependent variable. This approach would be incorrect. A regression approach assumes the independent variable is measured without error; we know this is not the case. But more important, a regression procedure is not symmetric with respect to its treatment of the two estimates of item difficulties. Since we have no reason for emphasizing or favoring one estimate of item difficulty over another estimate of the same item difficulty, we require a symmetric procedure.

A class of symmetric methods uses the first two moments of the distributions of estimated item difficulties. These methods find the parameters of the linear transformation,  $A$  and  $B$ , such that the mean and standard deviation of the transformed distribution of estimated item difficulties from the second calibration are equal to the mean and standard deviation of the estimated item difficulties from the first calibration.

A simple application of this method is found in Marco (1977) and in Cook, Eignor, and Hutten (1979). Poorly estimated item difficulties may have a serious impact on the computation of sample moments, however, producing a linear transformation that cannot be useful. Cook et al. (1979)

attempt to solve this by restricting the range of the difficulties used in computing moments.

Bejar and Wingersky (1981) use a more elaborate approach. Robust methods that give smaller weights to outlying points are used to estimate the moments. Linn, Levine, Hastings, & Wardrop (1980) attempt to reduce the influence of outliers by using weighted moments where the weights are inversely proportional to the estimated standard error of the estimates of the item difficulties.

The Bejar and Wingersky procedure treats all outliers in the same fashion, regardless of their standard error. The Linn et al. procedure treats all points with the same standard error in the same fashion, regardless of their outlier status. A procedure was developed by Lord and Stocking which attempts to overcome these potential problems. This procedure begins with a weighted estimate of the transformation exactly as in Linn et al. A robust procedure is then used to give small weights to those values whose perpendicular distance from this initial line is large, and a new line is estimated. The robust weighting is repeated until changes in the perpendicular distances become small. Details of this method are presented in the Appendix. Some results of this method will be described in subsequent sections of this paper.

A drawback of all of these "mean and sigma" transformation procedures is that they are typically applied only to the estimated item difficulties. That is, the  $A$  and  $B$  of the linear transformation of scale are estimated using only the  $b_i$ , and then applied to transform the  $\hat{\theta}_a$  and the  $a_i$ . While this is theoretically correct, better methods may exist which use more of the information available from the calibrations.

A class of methods, called "characteristic curve methods" in this paper, uses more information from calibrations. Each calibration of an item yields an estimated item response function or item characteristic curve  $P_i(\theta_a) \equiv P_i(\theta_a; a_i, b_i, c_i)$ . If estimates were error free, the proper choice of  $A$  and  $B$  for the linear transformation would cause these two curves to coincide. Haebara (1980) averages the squared difference between the individual item response functions over a suitable distribution of  $\theta$ , sums over the items common to the two calibrations, and chooses  $A$  and  $B$  to minimize this sum. Divgi (1980) chooses the  $A$  and  $B$  of the linear transformation to minimize the maximum difference between the sum of item response functions for the first calibration and the sum of the item response functions for the second calibration.

#### The New Method

This method falls into the class of characteristic curve methods. An examinee,  $a$ , with ability  $\theta_a$  has a true score  $\xi_a$  defined by

$$\xi_a \equiv \xi(\theta_a) \equiv \sum_{i=1}^n P_i(\theta_a; a_i, b_i, c_i) \quad , \quad (4)$$

where  $n$  is the number of items in the test. The correct linear transformation of scales from two different calibrations of the same test would

produce the same true scores for examinee  $a$  if the  $a_i$ ,  $b_i$ ,  $c_i$  were known. If  $\xi_a^*$  is the estimated true score obtained from the second calibration of the test after it has been transformed to the scale of the first, then

$$\xi_a^* \equiv \xi_a^*(\cdot) \equiv \sum_{i=1}^n P_i(\cdot; a_i^*, b_i^*, c_i) \quad (5)$$

For an examinee, the difference  $(\xi_a - \xi_a^*)$  should be small. In practice, we want to choose  $A$  and  $B$  such that for a suitable group of examinees, the average squared difference between true score estimates is as small as possible. The function to be minimized is

$$F = \frac{1}{N} \sum_{a=1}^N (\xi_a - \xi_a^*)^2, \quad (6)$$

where  $N$  is the number of examinees in the arbitrary group.

This function  $F$  considered as a function of  $A$  and  $B$  will be minimized when

$$\frac{\partial F}{\partial A} = \frac{-2}{N} \sum_{a=1}^N (\xi_a - \xi_a^*) \frac{\partial \xi_a^*}{\partial A} = 0, \quad (7)$$

and

$$\frac{\partial F}{\partial B} = \frac{-2}{N} \sum_{a=1}^N (\xi_a - \xi_a^*) \frac{\partial \xi_a^*}{\partial B} = 0. \quad (8)$$

Now, using the chain rule of differentiation,

$$\frac{\partial \hat{a}}{\partial A} = \sum_{i=1}^n \left( \frac{\partial P_i(a; a_{i2}^*, b_{i2}^*, c_{i2})}{\partial b_{i2}^*} \frac{\partial b_{i2}^*}{\partial A} + \frac{\partial P_i(a; a_{i2}^*, b_{i2}^*, c_{i2})}{\partial a_{i2}^*} \frac{\partial a_{i2}^*}{\partial A} \right) \quad (9)$$

Differentiating equations (1) and (3) gives  $\frac{\partial b_{i2}^*}{\partial A} = A$  and  $\frac{\partial a_{i2}^*}{\partial A} = \frac{-a_{i2}}{A^2}$ .

Substituting these derivatives into (9) gives the partial derivative

$$\frac{\partial \hat{a}}{\partial A} = \sum_{i=1}^n \left( b_{i2} \frac{\partial P_i(a; a_{i2}^*, b_{i2}^*, c_{i2})}{\partial b_{i2}^*} - \frac{a_{i2}}{A^2} \frac{\partial P_i(a; a_{i2}^*, b_{i2}^*, c_{i2})}{\partial a_{i2}^*} \right) \quad (10)$$

Also,

$$\frac{\partial \hat{a}}{\partial B} = \sum_{i=1}^n \frac{\partial P_i(a; a_{i2}^*, b_{i2}^*, c_{i2})}{\partial b_{i2}^*} \frac{\partial b_{i2}^*}{\partial B} \quad (11)$$

From equation (1),  $\frac{b_{i2}^*}{B} = 1$ , and substitution into (11) gives

$$\frac{\partial \hat{a}}{\partial B} = \sum_{i=1}^n \frac{\partial P_i(a; a_{i2}^*, b_{i2}^*, c_{i2})}{\partial b_{i2}^*} \quad (12)$$

The functional form of the partial derivatives of the item response function depends on the mathematical model chosen. Formulas for the partial derivatives for the three-parameter logistic item response function are given in Lord (1980, Chapter 4).

Once the functional form for the item response function is chosen, its derivatives are substituted into equations (10) and (12). These new expressions are then substituted into equations (7) and (8) to find the location of the minimum of  $F$  in equation (6).

In the applications described in the following section, the arbitrary group of examinees over which the function was minimized was chosen to be a spaced sample of about 200 examinees from the first calibration of a test. The parameters  $A$  and  $B$  of the linear transformation were found by minimizing  $F$  using the multivariate search technique by Davidon (1959) and Fletcher and Powell (1963).

## Results

### The Data and Analyses

Data from about 2000 examinees from each of 12 separate administrations of the Scholastic Aptitude Test (SAT) were selected for this study.

The SAT consists of six, 30-minute sections: two operational verbal sections, two operational mathematical sections, one Test of Standard Written English (TSWE) and one variable section containing equating or pretest items. The two verbal sections contain 40 and 45 items respectively; mathematical sections are 25 and 35 items respectively. Verbal equating or pretest sections are 40 items long; corresponding mathematical sections are 25 items long. TSWE data were not used in this study.

Each box in Exhibit 1 represents the operational sections, either verbal or mathematical, of a particular form of the SAT (upper case letters and numbers) and the equating section administered with that test form

(lower case letters). Each box contains items that are the same as items shown in boxes above and below it. For example, the second box in the verbal series contains items designated "X2fe." The "fe" items overlap with those contained in the box labeled "V4fe"; the "X2" items overlap with those contained in the box labeled "X2fm." The last box in each of the verbal and mathematical series contains items that overlap with the items in the first box, thus forming a closed chain.

Each box represents a separate calibration run using the computer program LOGIST (Wingersky, in press; Wingersky, Barton, Lord, 1982). For both the verbal chain and the mathematical chain, the scale established by the calibration of the items in the first box in the chain was arbitrarily chosen as the "base scale" for that chain. The estimates of item parameters for the overlapping items were then used to transform the scales established by the separate calibrations onto the appropriate base scale. For the verbal chain, for example, X2fe was transformed to the scale of V4fe using the item parameter estimates for the fe items that appear in both calibrations. Then X2fm was transformed to the scale of the transformed X2fe items, using the item parameter estimates for the X2 common items. This, of course, places the X2fm items on the V4fe scale. The next set of items, Y3fm, was transformed to the scale of the transformed X2fm items and so forth, until all items were placed on the scale of V4fe.

This sequential transformation process was performed in two ways:  
(1) the robust mean and sigma Lord and Stocking method described in

Verbal Chain

Mathematical Chain

V4 fe

V4 ff

fe X2

ff X2

X2 fm

X2 fn

fm Y3

fn Y3

Y3 fw

Y3 fx

fw B3

fx B3

B3 fk

B3 fl

fk Y2

fl Y2

Y2 fu

Y2 fv

fu Z5

fv Z5

Z5 et

Z5 eu

et V4

eu V4

Exhibit 1: Verbal and Mathematical Chains. Each box contains verbal or mathematical sections (capital letters and numbers) and an equating section (small letters).

the Appendix and (2) the new characteristic curve method described previously. This allows the comparison of the end results of the chaining process between the two transformation methods, but does not allow the comparison of the results of individual "links" in the chain.

To compare individual links in the chain, each link in the chain from the robust mean and sigma method was repeated exactly with the characteristic curve method. For example, in the verbal chain, X2fm was transformed to the scale of the (mean and sigma) transformed X2fe by the mean and sigma method as part of the sequential chaining using this method. This link was repeated exactly by using the characteristic curve method to transform X2fm to the scale of the (mean and sigma) transformed X2fe. In contrast to the chain of characteristic curve transformations, this series of characteristic curve transformations does not form a chain.

#### Results of Transformations for Verbal Items--Individual Links

A typical comparison of individual links is shown in Figures 1 and 2. In Figure 1, the horizontal axis is the (robust mean and sigma) transformed item difficulties for operational section X2 from the X2fe calibration. The vertical axis is the scale of the item difficulties for operational section X2 from the X2fm calibration. In Figure 2, the horizontal axis is the scale of the (robust mean and sigma) transformed item discriminations from X2 of X2fe. The vertical axis is the scale of the item discriminations of X2 from X2fm. The solid line through the

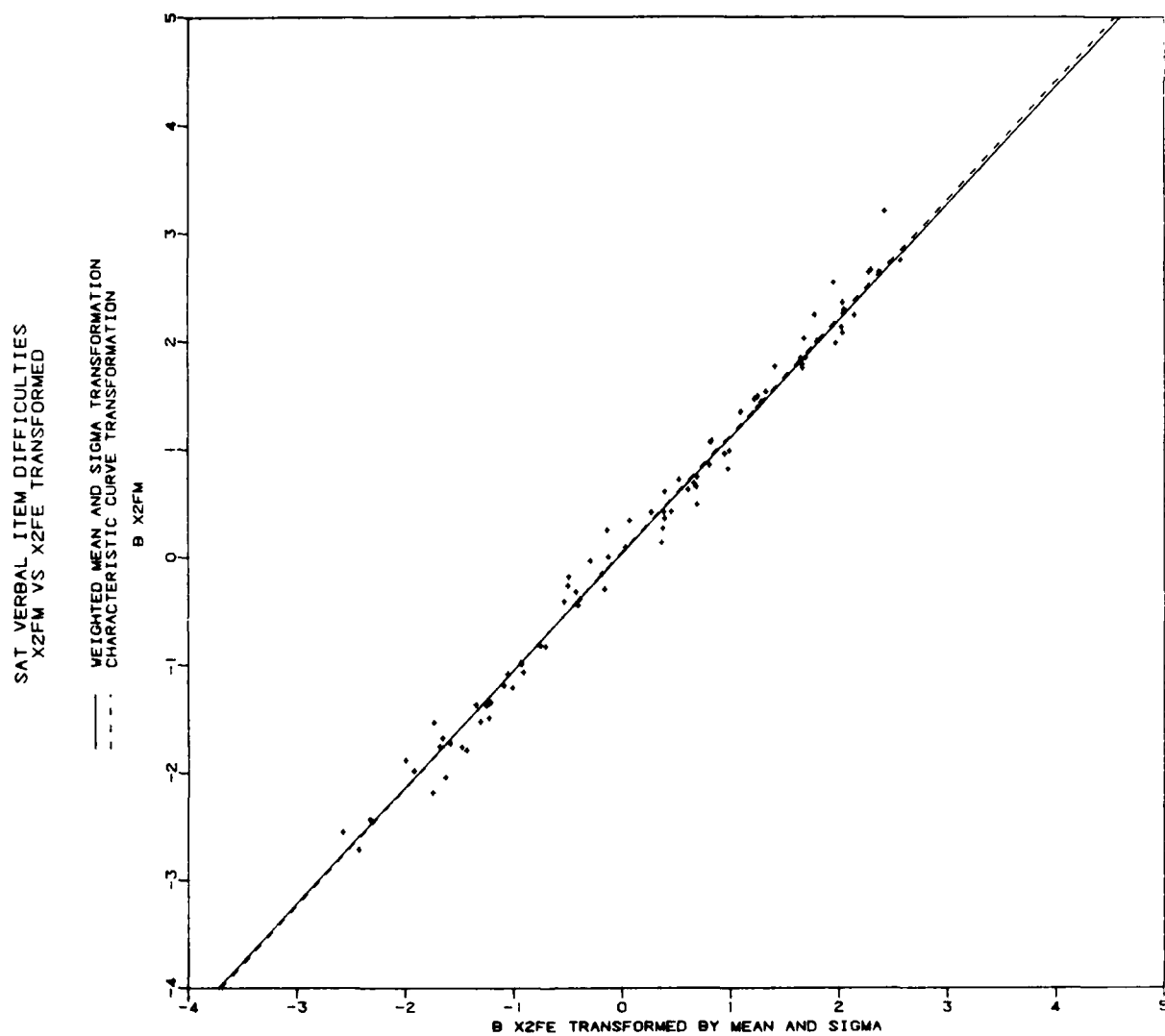


Figure 1. The two transformations for item difficulties compared for a typical verbal link.

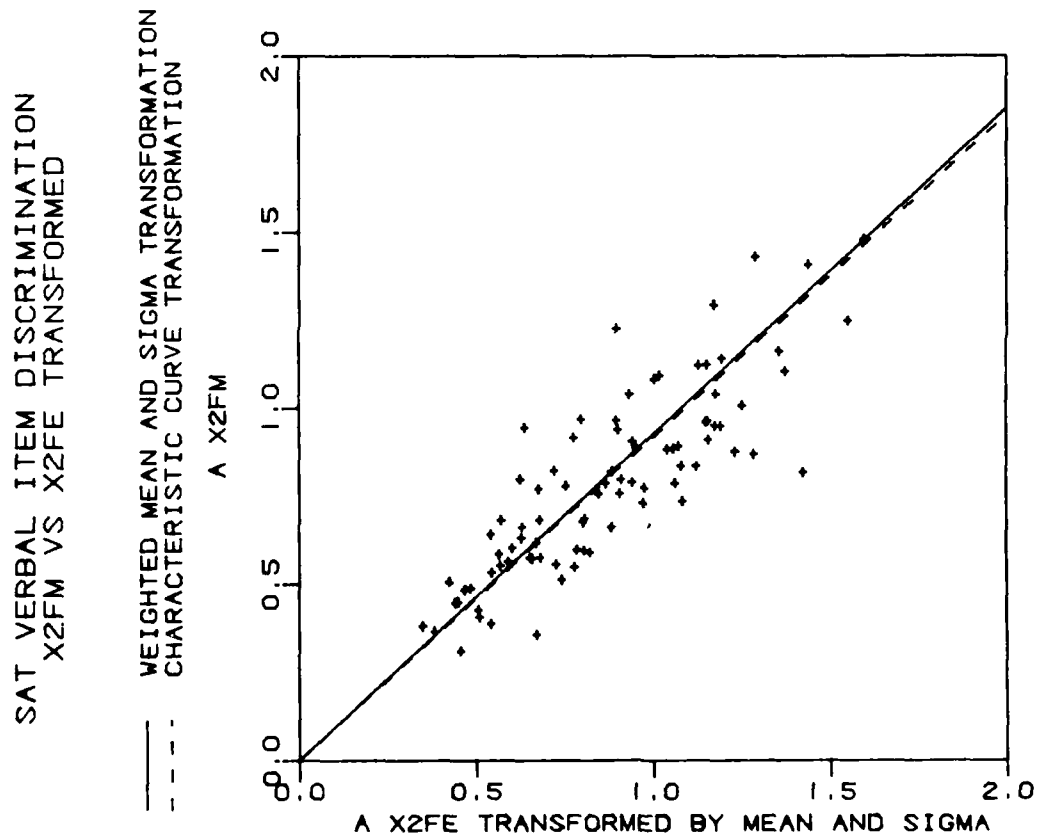


Figure 2. The two transformations for item discriminations compared for a typical verbal link.

the points in each figure is the linear transformation estimated by the robust mean and sigma method. The dashed line is the linear transformation estimated by the new characteristic curve method. The linear transformations do not differ much.

The largest difference found between the two methods for the verbal chain is shown in Figures 3 and 4. Figure 3 shows the presence of six points which could be considered outliers. The robust mean and sigma method explicitly tries to deal with these points, first by giving them low weights if the estimated standard errors are large, and then by giving them low weights if the perpendicular distance to the initial line is large. These points all ended up with weights which were very small or zero, thus some available information may have been discarded. The characteristic curve method does not discard any information. No other verbal link contained as many outliers as this one. It is possible that the difference between the two methods is due to their differential discarding of information.

On the whole, the direct comparison of individual links shows little difference between the two transformation methods for verbal data.

#### Results of Transformations for Mathematical Items--Individual Links

Most of the comparisons of the two transformation methods using mathematical data show little difference between the two methods. There are exceptions, one of which is shown in Figures 5 and 6. Inspection of Figure 5 shows the characteristic curve transformation is clearly a better fit to the data than the robust mean and sigma

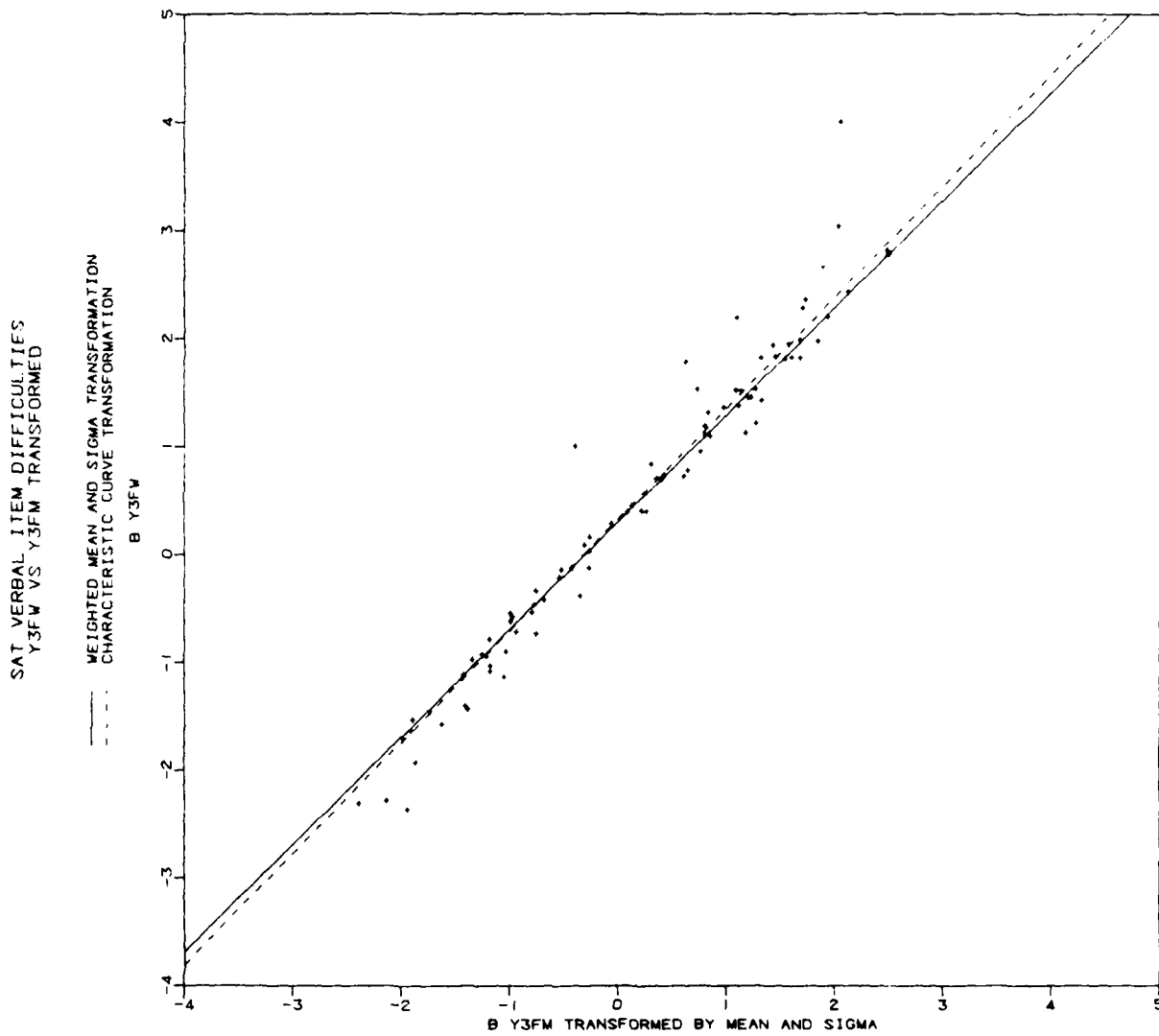


Figure 3. The two transformations for item difficulties compared for the worst verbal link.

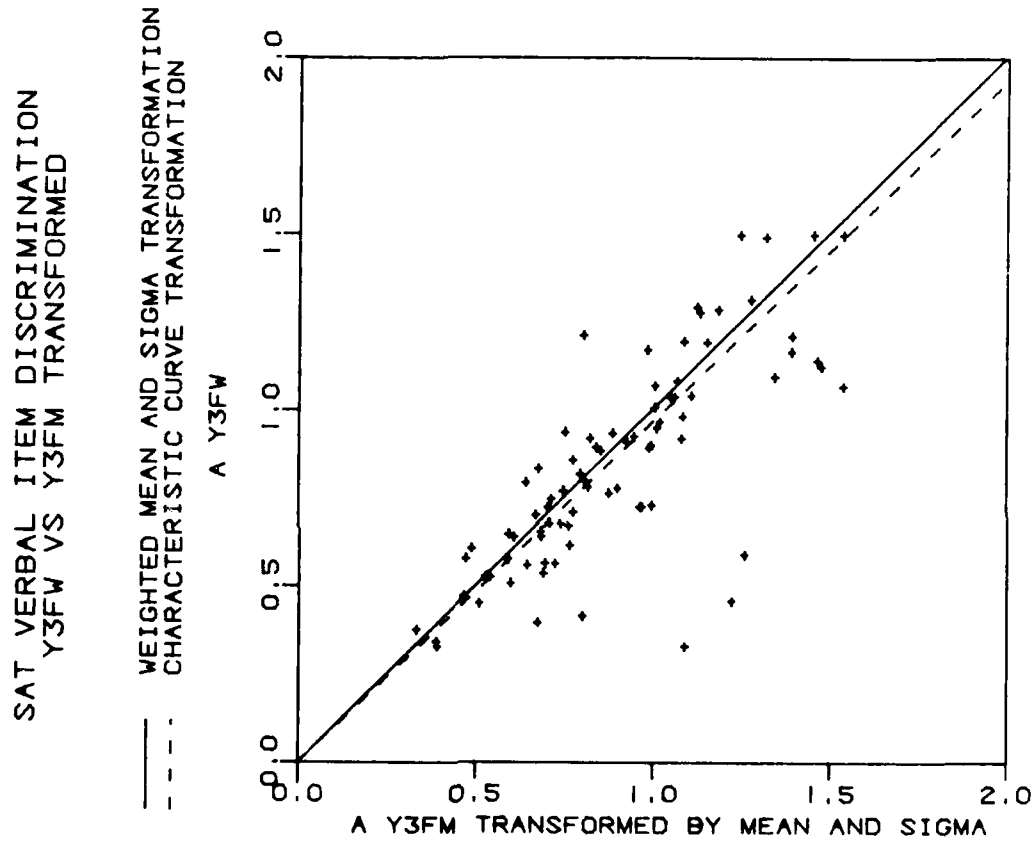


Figure 4. The two transformations for item discriminations compared for the worst verbal link.

transformation. This difference is more visible in Figure 6 where the robust mean and sigma transformation of the item discriminations produces unsatisfactory results. The line does not bisect the point cloud; there are only 18 out of 60 points below the line. The characteristic curve transformation was better; 31 out of 60 points are below the line.

There were two links which produced comparisons of this kind. That is, the characteristic curve transformation worked better than the mean and sigma transformation in both the fit to the item difficulties and the fit to the item discriminations. There were no links in which the mean and sigma transformation fit both the item difficulties and item discriminations better.

#### Chain Results

The cumulative results of chains of transformations may be evaluated by transforming the last (transformed) set of items in the chain directly to the base scale defined by the first set of items. Since the first and last sets of items are identical, this transformation should be an identity transformation. Figure 7 shows this comparison of each transformation method for the SAT verbal chain, and the identity transformation. The difficulties for items common to the first and last set of items are plotted on the horizontal axis. Figure 8 displays the same information for the SAT mathematical chain.

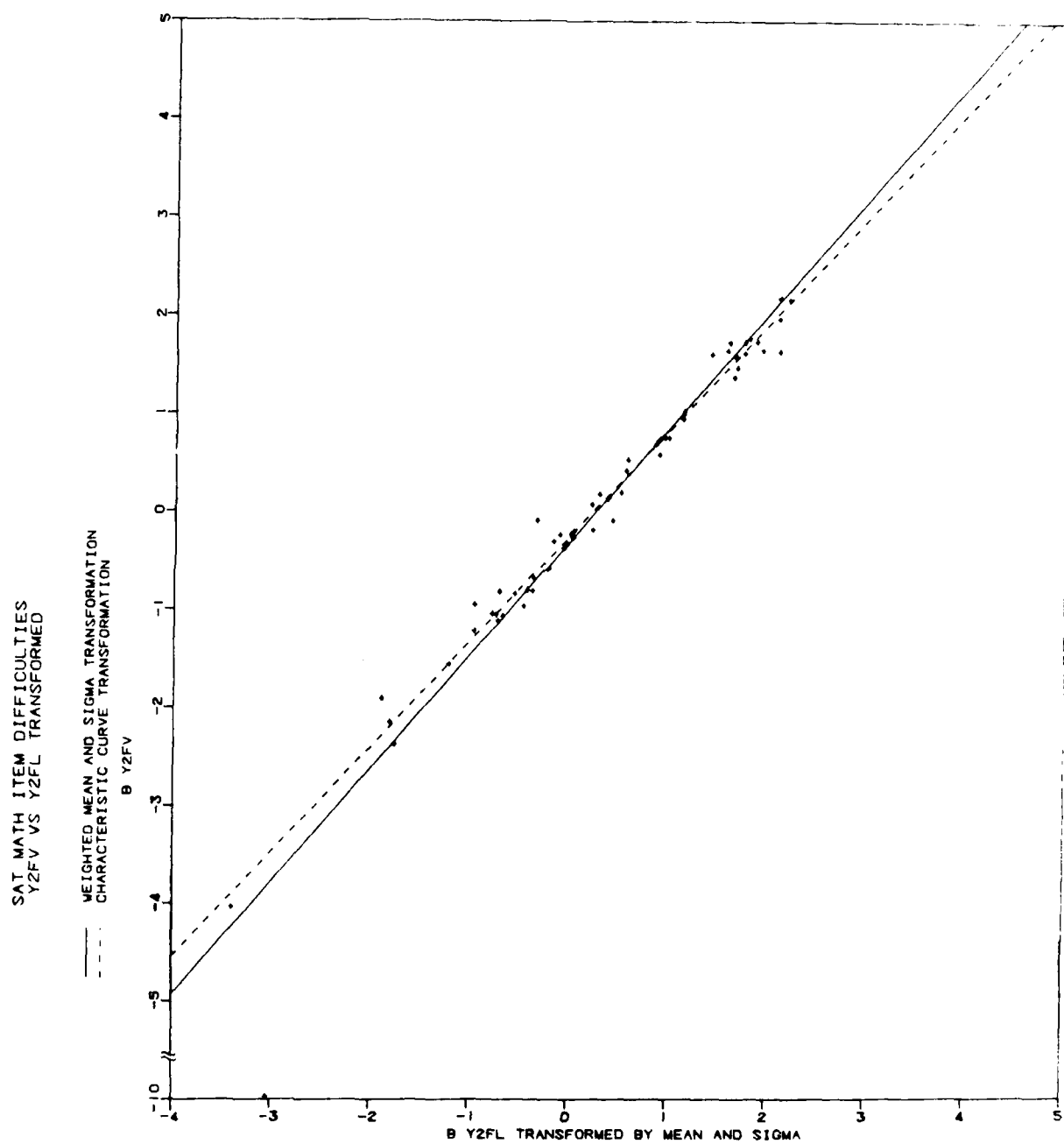


Figure 5. The two transformations for item difficulties compared for a bad mathematical link.

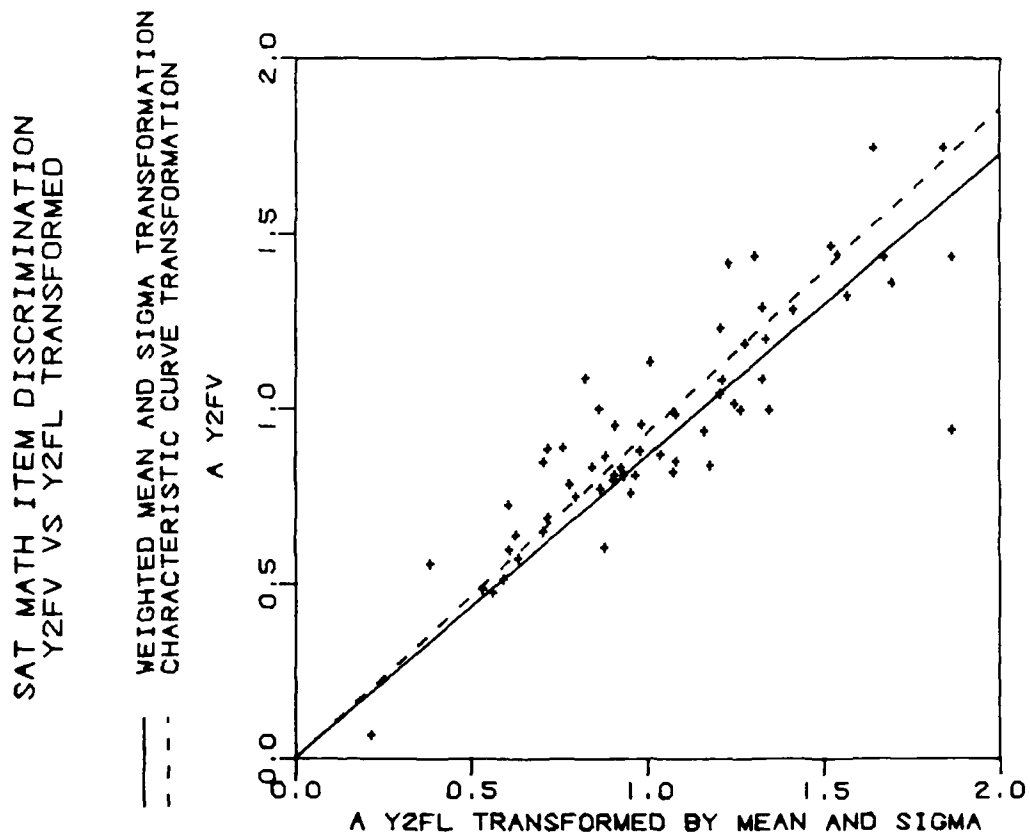


Figure 6. The two transformations for item discriminations compared for a bad mathematical link.

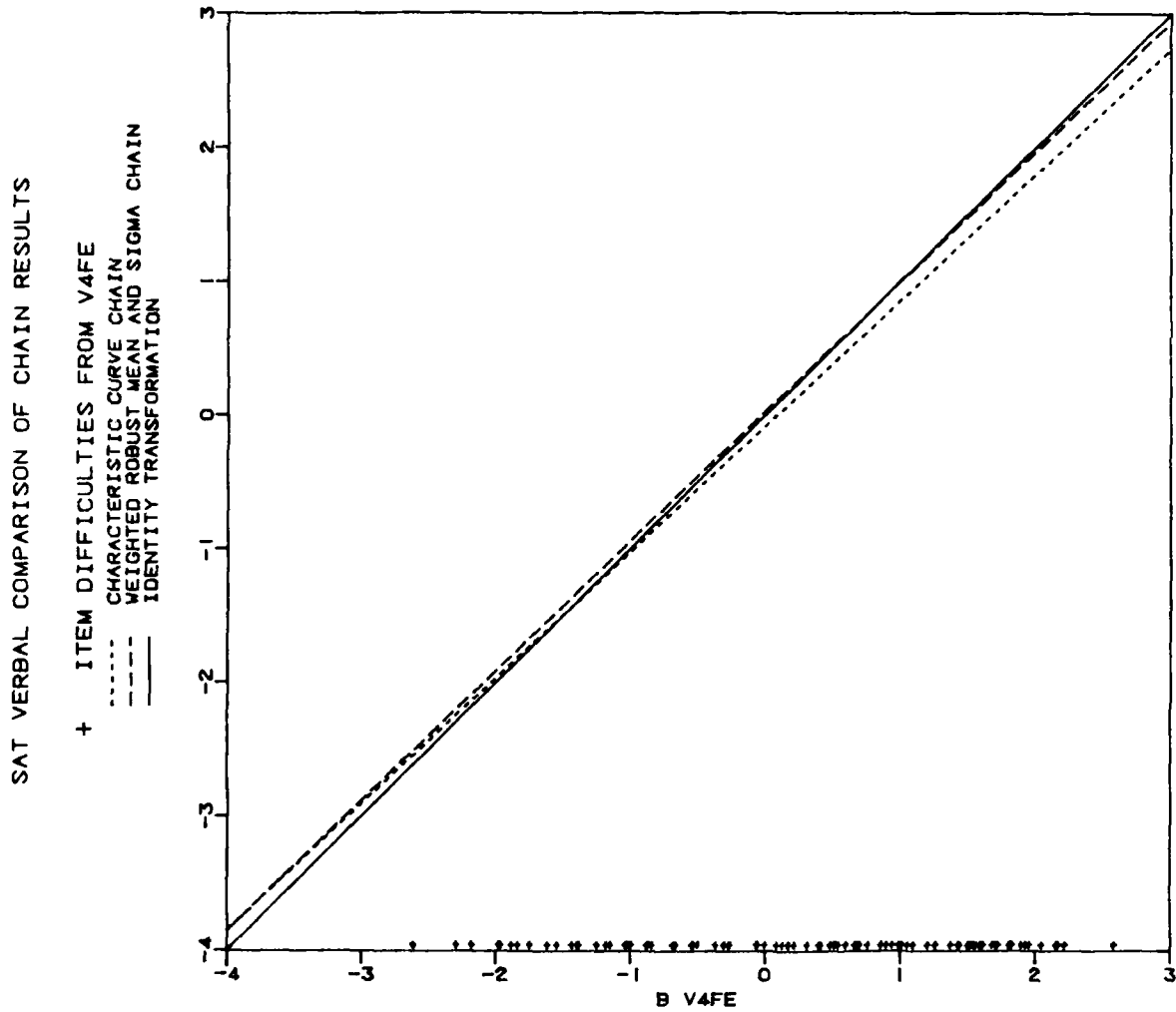


Figure 7. The final transformations for the SAT verbal chain.

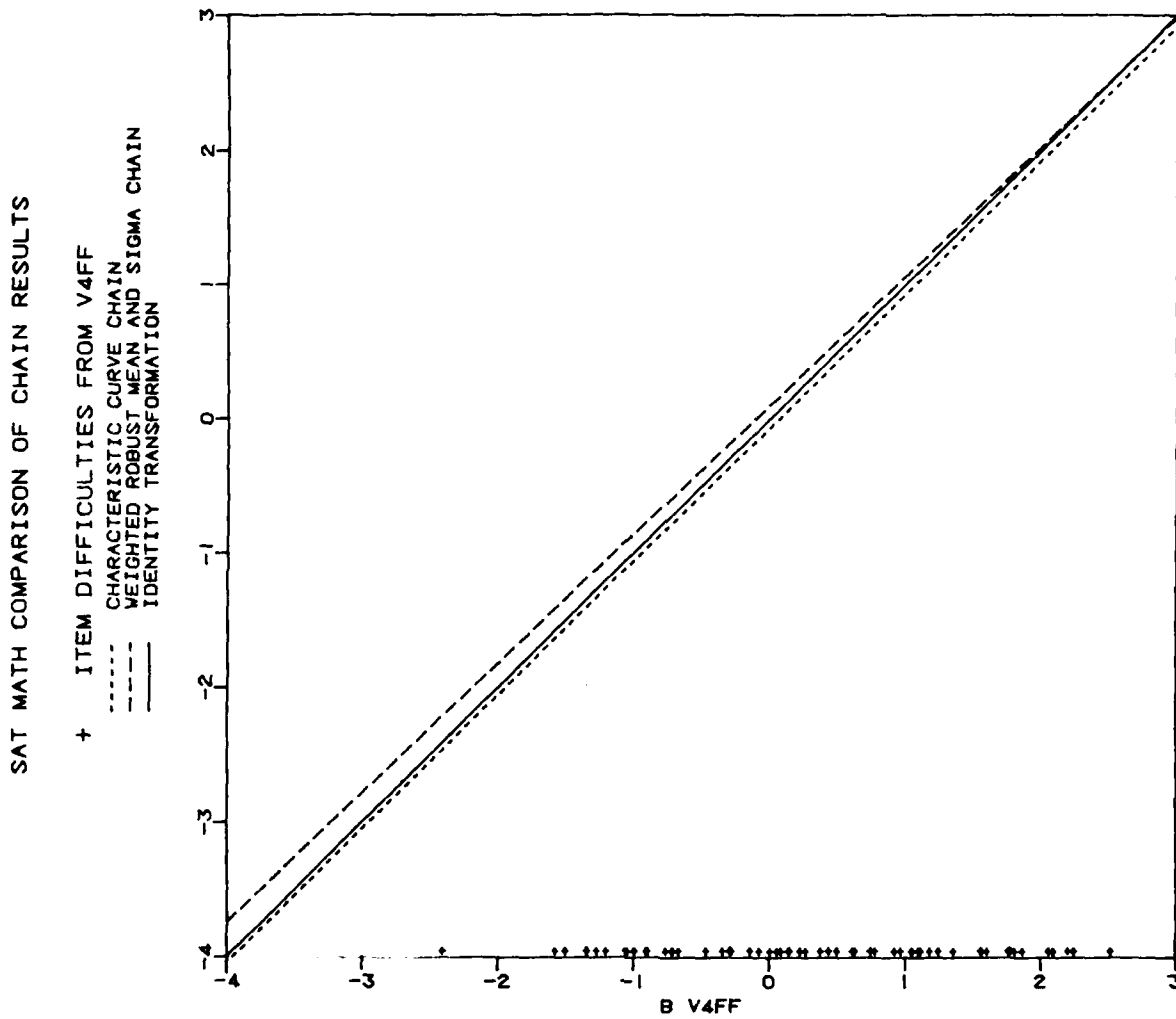


Figure 8. The final transformations for the SAT mathematical chain.

The robust mean and sigma method gives slightly better results than the characteristic curve method for verbal data. For mathematical data, the characteristic curve method worked better than the robust mean and sigma method.

### Conclusions

In situations where the robust mean and sigma transformation method worked well, as in the verbal data and most of the mathematical data, the characteristic curve method also worked well. However, the robust mean and sigma method sometimes produced unsatisfactory results. In these instances, the characteristic curve method worked much better. In particular, the characteristic curve method produced a much better transformation for the item discriminations (see Figure 6). If one is choosing a transformation method, the characteristic curve method, which uses more of the information available from each of the calibrations, would be recommended by the authors.

## Appendix

### Transforming Logistic Scales Using a Robust Iterative Weighted Mean and Sigma Method

This transformation method uses a function of the estimated standard errors of the estimated item difficulties for common items as weights to determine an initial transformation line based on mean and sigma equating of weighted estimates of item difficulties for the common items. A new set of weights is computed using a combination of the estimated standard error weights and robust (Tukey) weights based on perpendicular distances to the line. A new transformation line is computed and the procedure iterates until the maximum change in the perpendicular distances is less than some criterion.

#### Method

##### Computing the Standard Errors

The inverse of the information matrix  $I$  (p. 191 of Lord (1980)) is an approximation to the variance/covariance matrix for the item parameter estimates. The diagonal element of the inverse corresponding to the item difficulty is the estimated variance of the estimate of item difficulty. The square root of this quantity is the estimated standard error of the estimate of item difficulty.

Each item has two estimated item difficulties, one from each calibration. Therefore, each item has two estimated standard errors. The initial weight for an item to be used in the iterative procedure is the reciprocal of the larger estimated squared standard error of the estimated item difficulty.

The accuracy with which an estimated standard error of  $b$  is computed is the ratio of the determinant to the product of the diagonals of the information matrix. If this ratio is less than 0.0001, the estimated standard error is not accurate. The item is given a standard error weight of zero.

All people are included in the computation except those who did not reach the item.

#### Computing the Mean and Sigma Transformation

We have two distributions of weighted estimated item difficulties, one from each calibration. We let  $b_1$  be the distribution from the first calibration, and  $b_2$  be the distribution from the second calibration and compute

$$\begin{aligned} \bar{x}_{b_1} &, \text{ the mean of } b_1, \\ \sigma_{b_1} &, \text{ the standard deviation of } b_1, \\ \bar{x}_{b_2} &, \text{ the mean of } b_2, \\ \sigma_{b_2} &, \text{ the standard deviation of } b_2. \end{aligned}$$

The mean and sigma transformation (line) to put the second calibration estimated item difficulties onto the scale of the first is

$$b'_2 = A * b_2 + B,$$

where  $b'_2$  is the transformed distribution from the second calibration.

For this transformation,

$$\begin{aligned} A &= \sigma_{b_1} / \sigma_{b_2}, \\ B &= \bar{x}_{b_1} - A * \bar{x}_{b_2}. \end{aligned}$$

### Computing the Tukey Weights

Page 20 of Mosteller and Tukey (1977) gives a method of computing a robust estimate of location by weighting data with differential weights. We use only one piece of this process, namely the formula for the weights.

For our purposes,  $Y^*$  is the transformation line we have tentatively found. We replace Tukey's  $(Y(i) - Y^*)$  with the perpendicular distance of a point to the line.

Let  $D(i)$  equal the absolute value of the perpendicular distance. Then our weights,  $T(i)$ , are

$$T(i) = \begin{cases} \{1 - (D(i)/CS)^2\}^2 & \text{when } (D(i)/CS)^2 < 1 \\ 0 & \text{otherwise} \end{cases}$$

where  $S$  is the median of the  $D(i)$  and  $C$  is a constant equal to 6.

### The Iterative Procedure

The iterative procedure is as follows:

Step 1: For each item difficulty, for each common item, compute

$$W(i) = SE(B(i))^{-2} ,$$

where  $SE(B)$  is the larger of the two estimated standard errors.

Step 2: Compute a vector of scaled weights

$$W(i)' = W(i)/(\text{sum of } W(i)) .$$

Step 3: Compute the mean and sigma transformation line between the two sets of estimated item difficulties weighted by  $W'$ , and get the slope,  $A$ , and the intercept,  $B$ .

Step 4: Compute the perpendicular distances of each point to the line.

Step 5: Compute the Tukey weights,  $T(i)$  for each item, using these perpendicular distances.

Step 6: Reweight each point by a combined weight  $U(i)$ , where

$$U(i) = (W(i) * T(i)) / (\text{sum of } W(i) * T(i))$$

Step 7: Compute the weighted mean and sigma transformation line using these new weights.

Step 8: Repeat Steps 4, 5, and 6 until the maximum change in the perpendicular distances is less than 0.01.

#### Result

This procedure gives low weights to poorly determined item difficulties or to item difficulties which are outliers. Once the final transformation is found for the estimated item difficulties, the estimated item discriminations are transformed, as well as the ability estimates.

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