

AD-A117 377

ILLINOIS UNIV AT URBANA COMPUTER-BASED EDUCATION RESE--ETC F/6 5/9
RULE SPACE, THE PRODUCT SPACE OF TWO SCORE COMPONENTS IN SIGNED--ETC(U)
MAR 82 K K TATSUOKA, R BAILLIE N00014-79-C-0752

UNCLASSIFIED

CERL-RR-82-3-0NR

ML

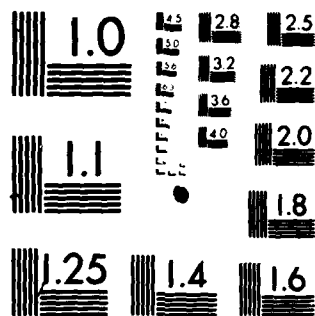
END

DATE

FILMED

82

DTIC



MICROCOPY RESOLUTION TEST CHART
NATIONAL BUREAU OF STANDARDS-1963-A

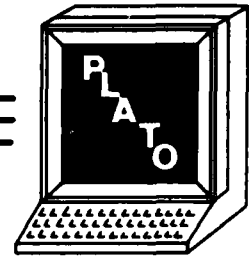
AD A117377

DTIC FILE COPY



Computer-based Education

Research Laboratory



University of Illinois

Urbana Illinois

RULE SPACE, THE PRODUCT SPACE OF TWO SCORE COMPONENTS IN SIGNED-NUMBER SUBTRACTION: AN APPROACH TO DEALING WITH INCONSISTENT USE OF ERRONEOUS RULES

KIKUMI K. TATSUOKA

ROBERT BAILLIE



Approved for public release; distribution unlimited.
Reproduction in whole or in part permitted for any
purpose of the United States Government.

This research was sponsored by the Personnel and Training
Research Program, Psychological Sciences Division, Office of
Naval Research, under Contract No. N000-14-79-C-0752.
Contract Authority Identification Number NR 150-415.

COMPUTERIZED ADAPTIVE TESTING AND MEASUREMENT

RESEARCH REPORT/82-3-ONR

MARCH 1982

82 07 23 009

Copies of this report may be
requested from:

Kikumi K. Tatsuoka
252ERL
103 S. Mathews
University of Illinois
Urbana, IL 61801

Acknowledgement

This research was sponsored by the Personnel and Training Research Program, Psychological Sciences Division, Office of Naval Research, under contract No. N00014-79-C-0752.

Several of the analyses presented in this report were performed on the PLATO[®] system. The PLATO[®] system is a development of the University of Illinois, and PLATO[®] is a service mark of Control Data Corporation.

The authors gratefully acknowledge the help of several people. First, thanks to Maurice Tatsuoka and Gerard Chevalaz for editing and careful proofreading. Louise Brodie did the typing and Roy Lipschutz did the artwork.



Accession For	
NTIS GRA&I	☒
DTIC TAB	☐
Unannounced	☐
Justification	
By	
Distribution/	
Availability Codes	
Avail and/or	
Dist	Special
A	

Unclassified

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER Research Report 82-3 ONR	2. GOVT ACCESSION NO. N00014-79-C-0752	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) Rule space, the product space of two score components in signed-number subtraction: An approach to dealing with inconsistent use of erroneous rules.		5. TYPE OF REPORT & PERIOD COVERED
7. AUTHOR(s) Kikumi K. Tatsuoka and Robert Baillie		6. PERFORMING ORG. REPORT NUMBER
9. PERFORMING ORGANIZATION NAME AND ADDRESS Computer-based Education Research Laboratory 103 S. Mathews, Rm. 252 ERL, U of Illinois Urbana, IL 61801		8. CONTRACT OR GRANT NUMBER(s) N00014-79-C-0752
11. CONTROLLING OFFICE NAME AND ADDRESS Personnel and Training Research Programs Office of Naval Research (Code 442) Arlington, VA 22217		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS 61153N: RR 042-04 NR 154-445
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)		12. REPORT DATE March 1982
		13. NUMBER OF PAGES
		15. SECURITY CLASS. (of this report)
		15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Extended Caution Index, aberrant response patterns, Item Response Theory erroneous rules of operation, signed-number arithmetic, simulation study, cluster, inconsistent and consistent misconceptions, rulespace		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) Students' responses to a 40-item test on signed-number subtraction are viewed as consisting of two different components, the sign and absolute value parts. Each component is scored zero-one for wrong or correct of the corresponding part of the answers. The traditional scoring yields a score		

of one only when both components have scores of one. By taking the values of the Extended Caution Index for the absolute value component as x-axis and those for sign component as y-axis, all pairs of component response patterns produced by consistent or inconsistent application of some kind of rules or random errors are mapped into the ECI product space. A simulation study showed that the response patterns generated by changing the binary score of any one item in the response patterns of an erroneous rule cluster together in the ECI product space. Moreover, the response patterns resulting from the same kind of misconceptions fall closer together than those resulting from very different kinds. This property of the ECI product space opens up a promising way to handle numerous numbers of "bugs" or rules quantitatively. But the ECIs are not defined in the cases of perfect scores and all zeros. There are often a considerable number of incomplete rules (e.g., all signs of the responses are right but absolute value parts are taken by some erroneous rule). The relationship between these incomplete, partially-right rules and the right rule or between other rules and the right rule cannot be discussed in this space at the present.

Abstract

Students' responses to a 40-item test on signed-number subtraction are viewed as consisting of two different components, the sign and absolute value parts. Each component is scored zero-one for wrong or correct of the corresponding part of the answer. The traditional scoring yields a score of one only when both components have scores of one. By taking the values of the extended caution index for the absolute value component as the x-axis and those for the sign component as the y-axis, all pairs of component response patterns produced by consistent or inconsistent application of various rules or random errors are mapped into the ECI product space. A simulation study showed that the response patterns generated by changing the binary score of any one item in the response patterns of an erroneous rule cluster together in the ECI product space. Moreover, the response patterns resulting from the same kind of misconceptions fall closer together than those resulting from very different kinds. This property of the ECI product space opens up a promising way to handle large numbers of "bugs" or rules quantitatively. But the ECIs are not defined in the cases of perfect or zero scores. Typically, there are many incomplete rules (e.g., all signs of the responses are right but absolute value parts are taken by some erroneous rule).

Introduction

Tatsuoka and Linn (1982) have recently introduced a group of new indices, extended caution indices for individual i (ECI_i), by extending Sato's original caution index (1975) into the context of item response theory (IRT). The caution index (C_i) is designed to identify anomalous binary response patterns to test items and to extract information not contained in the total score. Of course, several authors have developed appropriateness indices in conjunction with IRT (Wright, 1977; Levine and Rubin, 1979), but Tatsuoka and Linn's ECI_i has a unique feature different from appropriateness indices. When estimating the parameters of IRT models is not possible, C_i can be used instead of the ECI_i s, without loss of conceptual continuity. The item response curve, and test and group response curves used in defining ECI can be replaced by standard summary statistics based on observed item responses such as the number or proportion of people in a norm group answering an item correctly. C_i is designed for using such standard statistics based on sampling theory. Indeed, Harnisch and Linn (1981) used C_i for analyzing a NAEP dataset (National Assessment of Educational Progress) and successfully diagnosed curriculum differences and school differences within a school district. However, Rudner (1982) found that IRT-based indices detected aberrant response patterns more efficiently than those based on summary statistics. A recent paper by Tatsuoka and Tatsuoka (1982c) warns that there may be an upper limit to any personal indices' capability to detect aberrant response patterns. The detection rates by ECI s and one of the appropriateness measures are about 60% correct identification of aberrance, and 20% "false alarms," i.e., normal response patterns labelled aberrant. The result agrees with Rudner's

findings. It implies that further investigation of the behaviors of ECIs may be needed.

This paper introduces a new application of ECIs for studying a variety of students' misconceptions, which produce aberrant response patterns. By so doing, we may be able to uncover a different aspect of characteristics of ECIs. When tests are designed to measure the outcome of learning processes, looking into a whole response pattern to the test items often provides useful information to diagnose the student's state of knowledge (Birenbaum & Tatsuoka, 1980; Birenbaum & Tatsuoka, 1982a). The ECI values are determined by using response patterns and provide desirable information for diagnostic purposes.

An error diagnostic system for signed number arithmetic (SIGNBUG) has been developed by Tatsuoka and Baillie (1982) and it has successfully diagnosed quite a number of erroneous rules of operation. Similar diagnostic system for arithmetic such as whole number subtraction problems (Brown & Burton, 1978) have also found hundreds of erroneous rules resulting from incomplete knowledge or some kind of misconception ("bug") possessed by the students. But these systems are expensive and time consuming to construct. Besides, they can be used in only very specific domains of arithmetic. Tatsuoka and Linn (1982) briefly discussed using one of the five ECIs to detect the erroneous rules of operation in signed-number arithmetic. The ECIs have two possible advantages over previously considered approaches. First, unlike the individual consistency index (Tatsuoka & Tatsuoka, 1981, 1982b), ECIs do not require repeated measures. Second, application of ECIs is not restricted to specific content domains such as signed numbers computations or whole number arithmetic. Moreover, the number

of erroneous rules can sometimes become so large as to require some quantitative methods to classify them and to examine their relationships. Tatsuoka (1981) has tried to quantify the seriousness of misconceptions by ascertaining which level of the procedural steps it was that a student missed. Her approach is content specific and may be useful only for very simple problem domains.

This paper discusses a more general quantitative approach by utilizing the advantages of IRT-based ECIs. All erroneous rules of operation will be expressed as points in a geometric space (called "rule space"). Rule space is useful in handling large numbers of bugs and for examining their psychometric properties such as "stability" or "transitivity" of bugs (Tatsuoka, 1982). This new approach will be illustrated with the test data obtained from a 40-item test of signed-number subtraction problems. Moreover, the relationships between rules and their partially consistent application to the test items will be illustrated with simulated data in rule space.

Method and Procedure

A Brief Introduction of the Extended Caution Indices

The caution index for subject i is defined as the complement of the ratio of two covariances. The numerator of the ratio is the covariance of observed row vector, $y_i = (y_{i1}, \dots, y_{in})$ in the score matrix (y_{ij}) , [$i = 1, \dots, N$, $j = 1, \dots, n$ where N is the number of subjects and n the items], and the column-sum vector, $y_{\cdot} = (y_{\cdot 1}, y_{\cdot 2}, \dots, y_{\cdot n})$. The denominator is the covariance of the corresponding scores rearranged as a reverse Guttman vector $\underline{M}_1^s = (M_{11}, M_{12}, \dots, M_{1n})$ and the column-sum vector $y_{\cdot}$. Thus C_i is given by Equation (1).

$$(1) \quad C_1 = 1 - \frac{(\underline{y}_1 - \underline{P}_{1.}, \underline{y}_{.} - \underline{P}_{..})}{(\underline{M}_1^2 - \underline{P}_{1.}, \underline{y}_{.} - \underline{P}_{..})} = 1 - \frac{\text{cov}(\underline{y}_1, \underline{y}_{.})}{\text{cov}(\underline{M}_1^2, \underline{y}_{.})}$$

The values of ECIs are calculated by first constructing a probability matrix with elements P_{ij} . In practice, the P_{ij} can be replaced by $\hat{P}_{ij}$, whose values are obtained by substituting estimated item and person parameters in the logistic function.

One of the ECIs, ECI4, is defined by taking the ratio of two covariances of which the numerator is the covariance of the i th row vector in the score matrix (y_{ij}) and that in the probability matrix (P_{ij}), which are denoted by $\underline{y}_i$ and $\underline{P}_i$, respectively. The denominator is the covariance of the column-sum vector of (P_{ij}) which is denoted by $\underline{G} = (G.1, G.2, \dots, G.n)$, and $\underline{P}_i$. The following Equation (2) is the fourth index ECI4.

$$(2) \quad \text{ECI4} = 1 - \frac{\text{cov}(\underline{y}_i, \underline{P}_i)}{\text{cov}(\underline{G}, \underline{P}_i)}$$

The second ECI is ECI2 of which the denominator is the same as that of ECI4, but the numerator is the covariance of $\underline{y}_i$ and $\underline{G}$ and given in the following equation (3).

$$(3) \quad \text{ECI2} = 1 - \frac{\text{cov}(\underline{y}_i, \underline{G})}{\text{cov}(\underline{P}_i, \underline{G})}.$$

Unlike the caution index, the numerator of ECI4 is the covariance of the observed vector $\underline{y}_i$ and the probability vector $\underline{P}_i$ at the fixed level i ,

which is not a group dependent vector. As a result, ECI4 should be sensitive to the anomalous response patterns relative to the anomaly of response patterns in comparison with the row vector $\underline{P}_i$ at the level θ_i . On the other hand, the identical denominator, $(\underline{G}, \underline{P}_i)$ of ECI2 and ECI4 can be considered as a standardized scaling factor and the difference between the two indices comes from the numerators $\text{cov}(\underline{y}_i, \underline{P}_i)$ and $\text{cov}(\underline{y}_i, \underline{G})$. In other words, the numerator of ECI2 is proportional to the cosine of the angle between the two vectors $\underline{y}_i$ and $\underline{G}$ while the numerator of ECI4 is proportional to cosine of that between $\underline{y}_i$ and $\underline{P}_i$ in n items space. Therefore, the difference between ECI2 and ECI4 can be said to lie in whether the response pattern of the observed vector $\underline{y}_i$ conforms better to the pattern of vector $\underline{P}_i$ or that of the group average vector $\underline{G}$. Tatsuoka and Linn (1982) demonstrated briefly that ECI4 is moderately effective in spotting erroneous rules of operation. However, ECIs are θ -dependent measures and have a strong tendency to give inflated values at both the extremely high and low total scores. In order to avoid the undesired property of ECIs, Tatsuoka and Tatsuoka (1982c) derived the expectations and variances of ECI4 and ECI2 and standardized them. The standardized ECIs are given by Equations (4) and (5).

$$(4) \quad \text{ECI4}_z = \frac{\text{ncov}(\underline{P}_i - \underline{y}_i, \underline{P}_i)}{\left[\sum_{j=1}^n \sigma_{1j}^2 (\underline{P}_j - \underline{T}_j)^2 \right]^{1/2}}$$

$$(5) \quad \text{ECI2}_z = \frac{\text{ncov}(\underline{P}_i - \underline{y}_i, \underline{G})}{\left[\sum_{j=1}^n \sigma_{1j}^2 (\underline{G}_j - \underline{G})^2 \right]^{1/2}}$$

Regular response patterns: A new scoring procedure

A 40-item free response test that comprises four parallel subtests of signed-number subtraction problems was administered to 172 eighth graders at a local junior high school. The traditional scoring of right and wrong answers was decomposed into a two-component scoring procedure that separates the absolute-value and sign parts of the responses. The signs of the responses to n items were scored right or wrong and so were the absolute values. Therefore, a regular set of responses to n items was decomposed into two binary response patterns related to the sign component and the absolute-value component. The regular response patterns are element-wise multiplications of the two component response patterns. Suppose we have three responses to 10 items resulting from the following four rules.

Rule 1: The student uses the right rule for addition problems. In a subtraction problem, he/she changes the signs of the number in the parentheses first, then converts the subtraction into an addition problem and uses the right conversion.

$$-6 - (-10) = -6 - (+10) = -6 + (-10)$$

Rule 2: The student uses a wrong rule for addition. He/she always subtracts the smaller absolute value from the larger absolute value and takes the signs of the first number in the answer. The student converts subtraction to addition problems correctly, then consistently applies the same erroneous rule to the new addition problem.

Rule 3: The addition problems are answered by the right rule. Subtraction problems are converted by a wrong rule -- by simply changing the operation sign minus, $-$, to plus, $+$, except for L-S (e.g., $8-6$) and L (e.g., $6-8$) item types. The student knows how to get answers

for these two item types without converting them to addition problems. He/she uses the right addition rule for the new addition problems of the other eight item types.

Rule 4: The student always subtracts the smaller absolute value from the larger one and takes the sign of the number with the larger absolute value in the answer. The conversion of subtraction problems to addition is omitted and the difference between addition and subtraction of two signed numbers seems to be ignored.

Table 1 summarizes the four pairs of binary vectors and responses yielded by the four rules. As can be seen in Table 1, the elementwise

Insert Table 1 about here

multiplications of the two component score vectors yield the binary score vector of regular scoring. The response patterns scored by the regular scoring procedure of Rules 2 and 4 are identical but the sign component score vectors are different. Tatsuoka and Tatsuoka (1981) showed that all erroneous rules discovered so far are uniquely represented by the two component score vectors with the 10 items of subtraction problems. Therefore, the two component-response patterns are subjected to the estimation of item and person parameters separately by GETAB (Baillie, 1980).

Appendices I and II are summary lists of the estimated item parameters for the two sets of binary response patterns obtained from the 40-item subtraction test.

Table 1

The Binary Response Patterns of Three Different Scorings Generated by Three Erroneous Rules

Items	Rule 1			Rule 2			Rule 3			Rule 4		
	Responses	R	S A	Responses	R	S A	Responses	R	S A	Responses	R	S A
-3 - (-7) = +4	-10	0	0 0	-4	0	0 1	-10	0	0 0	-4	0	0 1
-2 - 8 = -10	-10	1	1 1	-6	0	1 0	-10	1	1 1	+6	0	0 0
5 - (-12) = +17	-7	0	0 0	+7	0	1 0	-7	0	0 0	-7	0	0 0
-11 - +8 = -19	-19	1	1 1	-3	0	1 0	-3	0	1 0	-3	0	1 0
9 - 4 = +5	+5	1	1 1	+5	1	1 1	+5	1	1 1	+5	1	1 1
-15 - (-9) = -6	-24	0	1 0	-6	1	1 1	-24	0	1 0	-6	1	1 1
-13 - 5 = -18	-18	1	1 1	-8	0	1 0	-18	1	1 1	-8	0	1 0
8 - (-6) = +14	+2	0	1 0	+2	0	1 0	+2	0	1 0	+2	0	1 0
-5 - +11 = -16	-16	1	1 1	-6	0	1 0	+6	0	0 0	+6	0	0 0
1 - 10 = -9	-9	1	1 1	+9	0	0 1	-9	1	1 1	+9	0	0 1
Total Scores		6	8 6		2	8 3		4	7 4		2	5 4

*R Regular Scores

*S Sign-Component Scores

*A Absolute-Value-Component-Scores

Rule Space

A rule space is defined as a geometric representation of the rules used by the students. Let $ECI4_{12}^s$, $i=1, \dots, N$ be the values of standardized ECIs obtained from the sign-component patterns and $ECI4_{12}^a$, $i=1, \dots, N$ be from the absolute-value component patterns. As a result, a pair of two real numbers is associated with each student. However, since ECIs are essentially a ratio of two covariances, they cannot be defined when the scores are either all ones or all zeros. It is impossible to assign a finite number to the response patterns yielded by using the right rule. So we omit the students who answered all the items right or all the items wrong in this study.

A plot of the values of ECI_{12}^a (hereafter the i will be omitted) against the absolute-component true scores for 100 students (excluding all zeros and all ones) and for the 21 most popular erroneous rules which are produced by a variety of misconceptions, is given in Figure 1.

Insert Figure 1 about here

The erroneous rules are marked by a small circle "o" while the real students are marked by "+". Each point in Figure 1 represents a absolute-component response pattern for the 40 items. If a student responds to the items by applying erroneous Rule 1 explained in Table 1 consistently throughout the test, then his component response patterns yield the same value of $ECI4_2^a$ and true score for the absolute value component as those produced by Rule 1 and his point in Figure 1 coincides with the point of Rule 1. If the student does not apply his or her rule perfectly consistently but answers one or two items randomly, then his or her component response pattern doesn't match that produced by applying the rule consistently. The values of the true

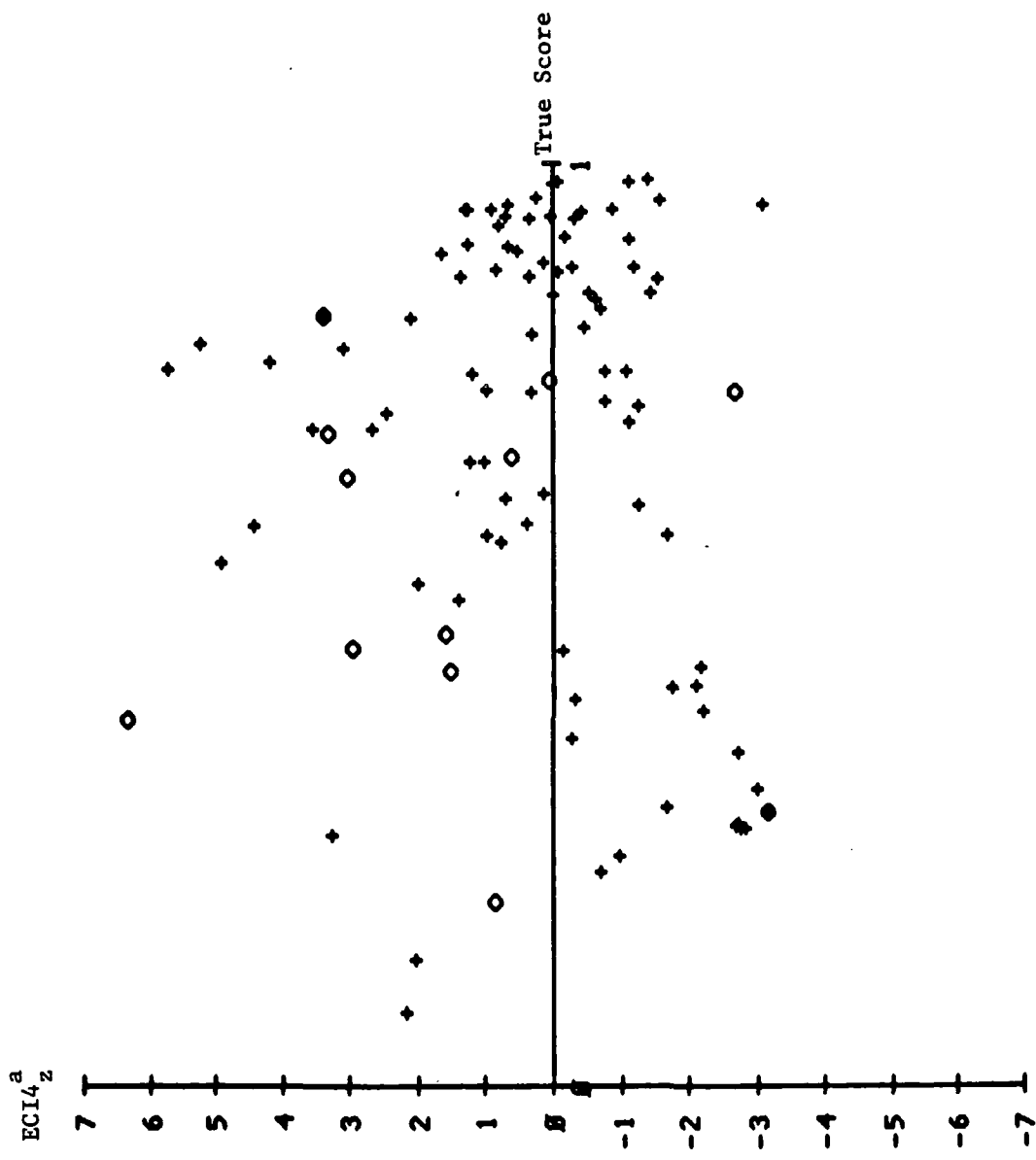


Figure 1: Plot of $ECI4_z^a$ Against True Scores for Absolute Value Component, Real Data ("+") and Erroneous Rules ("o").

scored and $ECI4_z^a$ associated with the student's inconsistent response patterns do not coincide with the values yielded by the rule. Given below in Figure 2 is the sign component, obtained by the same manner as for the absolute-value component patterns.

Insert Figure 2 about here

As can be seen in both the figures, some erroneous rules represented by "o" are found near the x-axis and a considerable number of aberrant response patterns produced by real students "+" is seen outside of erroneous rules "o". It yields the same result -- the low detection rates of aberrant response patterns by personal indices -- as Rudner (1982) and Tatsuoka and Tatsuoka (1982a) found in their studies.

Figure 3 is a plot of the sign-component true scores against absolute-value component true scores. The cluster near the top right corner in Figure 3 represents the students who executed the right rule for responding to the items with different extents of consistency as discussed in Tatsuoka and Tatsuoka (1981).

Insert Figure 3 about here

The ten points on the broken line perpendicular to the x-axis at $\theta = .292$ in Figure 3 have the same sign component response patterns. It means that their source of errors may be identical with respect to understanding of the absolute-value operation but not with respect to the sign operation. For example, since the distance of the two points (rules 16 and 32) is very small, their sources of misconception may be closely related with one another. In order to investigate this question, a simulation study was carried out.

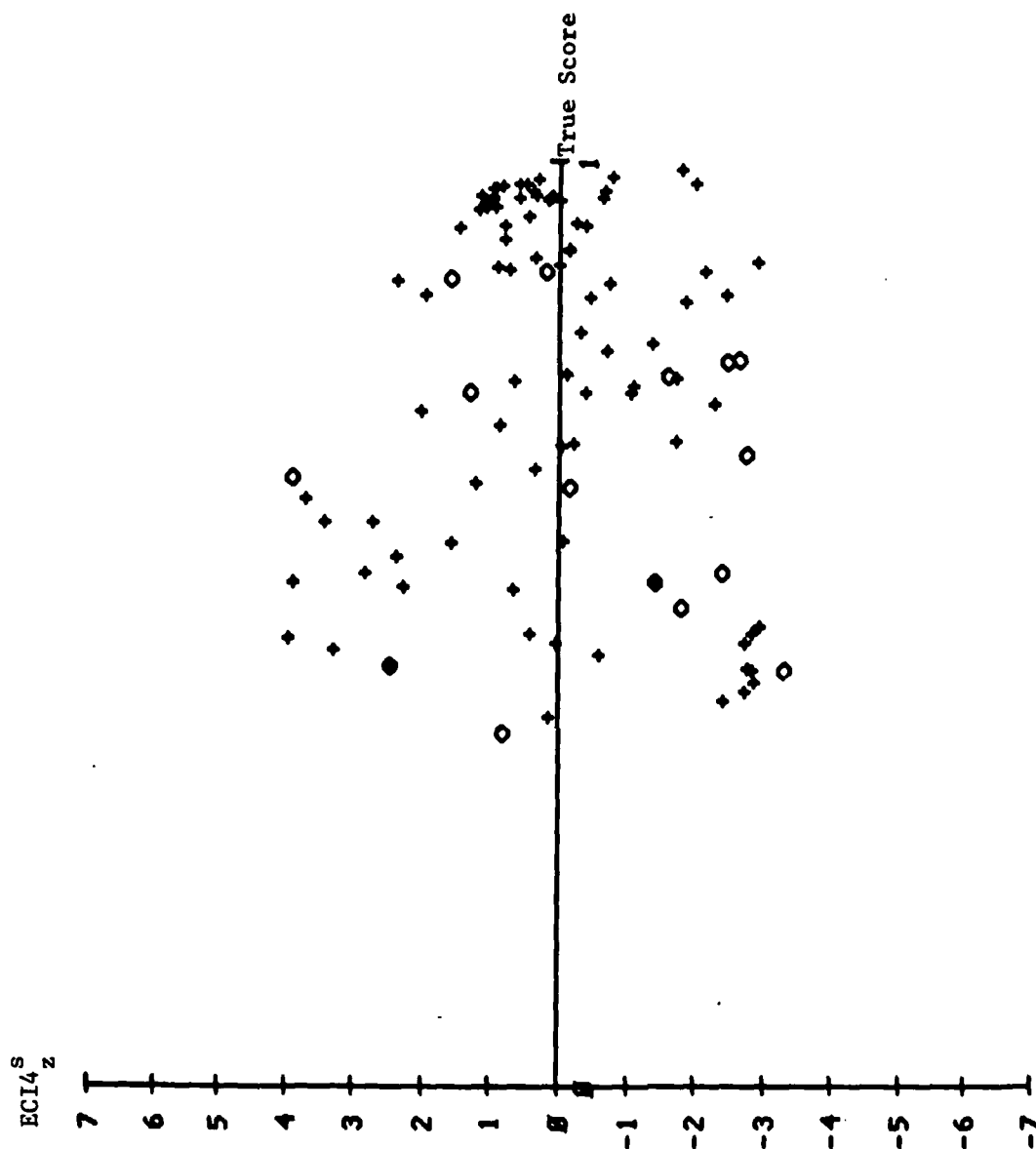


Figure 2: Plot of $ECI4_z^s$ Against True Score for Sign Component
Real Data ("+") and Erroneous Rule ("0").

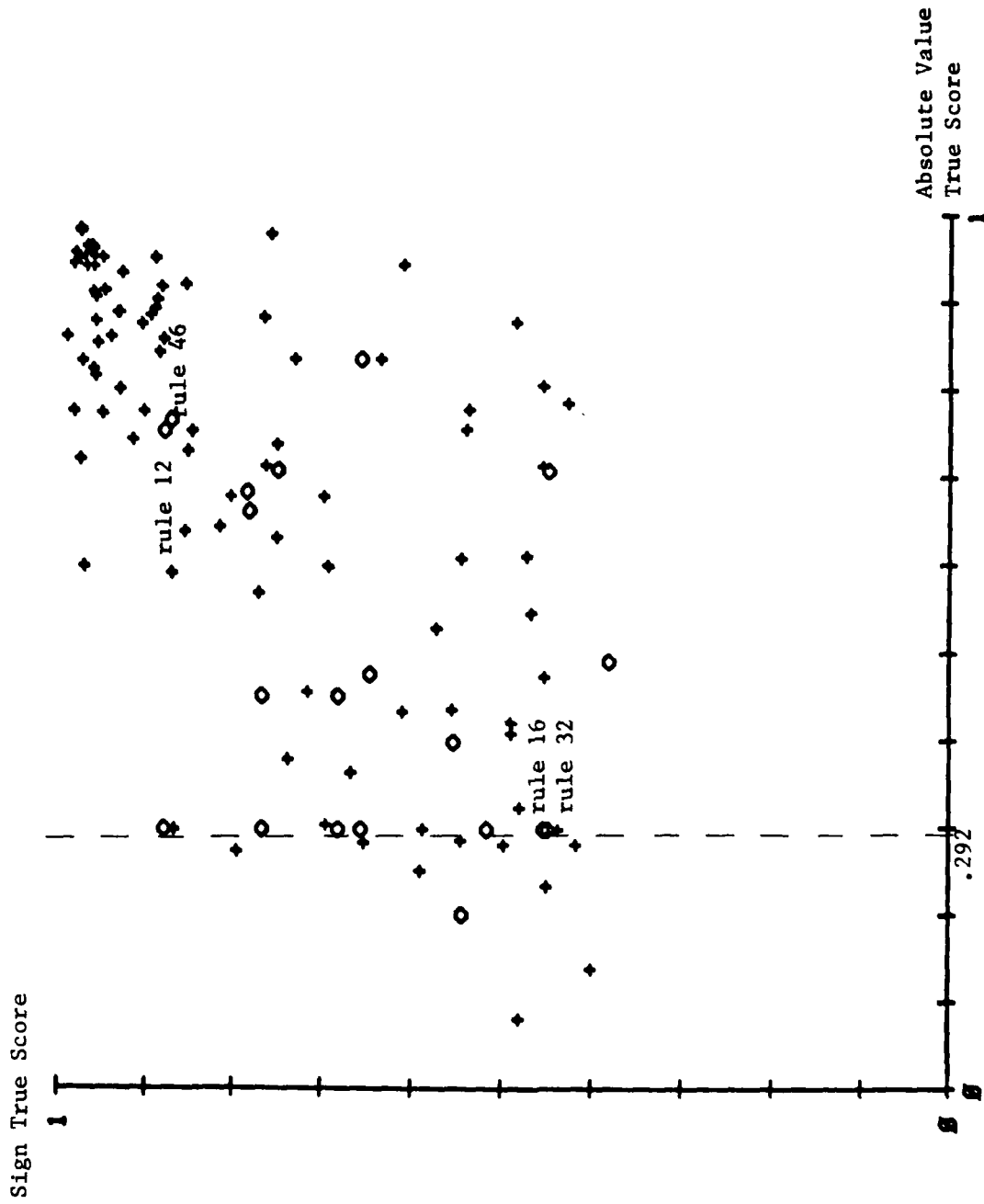


Figure 3: Plot of True Score for Absolute Value Component Against Sign Component, Real Data ("+" and "0") and Erroneous Rules ("0").

Procedures for Generating Simulated Inconsistent
Responses Around a Rule

The sign-component pattern of Rule 1 given in Table 1 is

$$\underline{s}^1 = [0101111111] \quad .$$

If the student uses Rule 1 inconsistently, then his/her responses to the 10 items in each parallel subtest will no longer match the response pattern $\underline{s}^1$. Depending on his/her degree of consistency, possibly one or two items out of the 10 will be off from $\underline{s}^1$ in at least one subtest. We generate 10 vectors in each of which exactly one element (the i th; $i=1,2,\dots,10$) is different from the corresponding element of $\underline{s}^1$ (i.e., is its complement) and call them $\underline{s}^1(i)$, $i=1,2,\dots,10$. If Rule 1 is consistently applied throughout the test, then the four response patterns from the four parallel subtests must be identical. Since a few items in the first subtest were deleted because of large standard errors of estimate by the maximum likelihood procedure used in the computer program GETAB (see Appendix I), the last three subsets were used for generating simulated data for the 31 students as follows:

The first "student's" responses to the four parallel blocks of 10 items each consist of four replications of $\underline{s}^1$ itself. The responses of the remaining 30 "students" to the first block of 10 items are likewise $\underline{s}^1$ without modification. However, the responses to the second through fourth blocks of 10 items are modified for the first, second and third subgroups of 10 "students" each in the following manner. For the first subgroup (i.e., "students" 2 through 11), the responses to the second block of 10 items are represented by $\underline{s}^1(1), \underline{s}^1(2), \dots, \underline{s}^1(10)$, while the third and fourth blocks remain "responded to" by Rule 1 to yield two

replications of $\underline{s}^1$. For the second subgroup ("students" 12 through 21), the responses to the third block of 10 items become $\underline{s}^1_{(1)}$, $\underline{s}^1_{(2)}, \dots, \underline{s}^1_{(10)}$, while those to the second and fourth blocks are $\underline{s}^1$ itself. For the third subgroup ("students" 22 through 31), the fourth-blocks responses become $\underline{s}^1_{(i)} [i=1, 2, \dots, 10]$ while the responses to blocks 2 and 3 remain as $\underline{s}^1$. Table 2 shows the 40-element response patterns generated for the 31 "students," for both the sign and absolute-value components. The 31 ECI4 values, including the perfect pattern by Rule 1 as the first vector, were calculated.

Insert Table 2 about here

The same procedure was repeated for the absolute-value component patterns. Thus, two sets of 31 ECI4, one for the sign component, the other for the absolute-value component patterns, are obtained. Figures

Insert Figures 4, 5 and 6 about here

4, 5, and 6 show that the 30 non-consistent (or partially consistent) response patterns plus the perfect pattern by a rule cluster together no matter which axes are chosen in plotting. This implies that each erroneous rule has in its vicinity its "non-consistent" response patterns -- the responses yielded by partially consistent application of the rule -- and they may form a unidimensional set of points like the cluster near the right rule in Figure 3. It confirms the results demonstrated in Tatsuoka and Tatsuoka (1981) and Birenbaum and Tatsuoka (1982a, b), which have investigated the effects of misconceptions on the dimensionality of a dataset and concluded that a unidimensional dataset in signed-number subtraction problems suggests a state of knowledge enabling a student to fairly consistently apply the right rule in responding to the test items. This can be interpreted to mean that a student at a certain state of knowledge produces a particular erroneous

Table 2

[illegible]

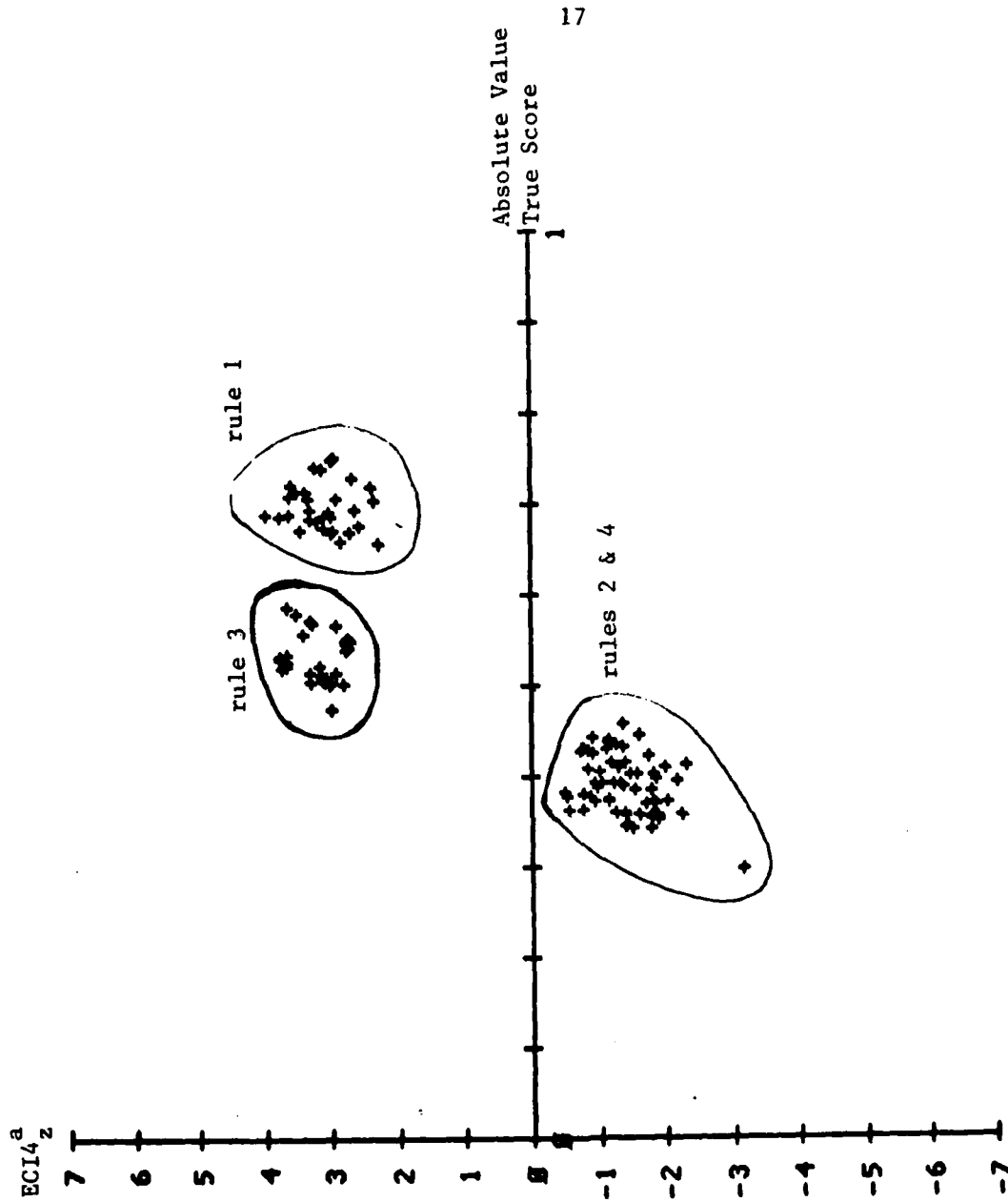


Figure 4: Plot of the Four Clusters Consisting of Inconsistent Responses Around Rules 1, 2, 3 and 4 in Table 1 for Absolute Value Component.

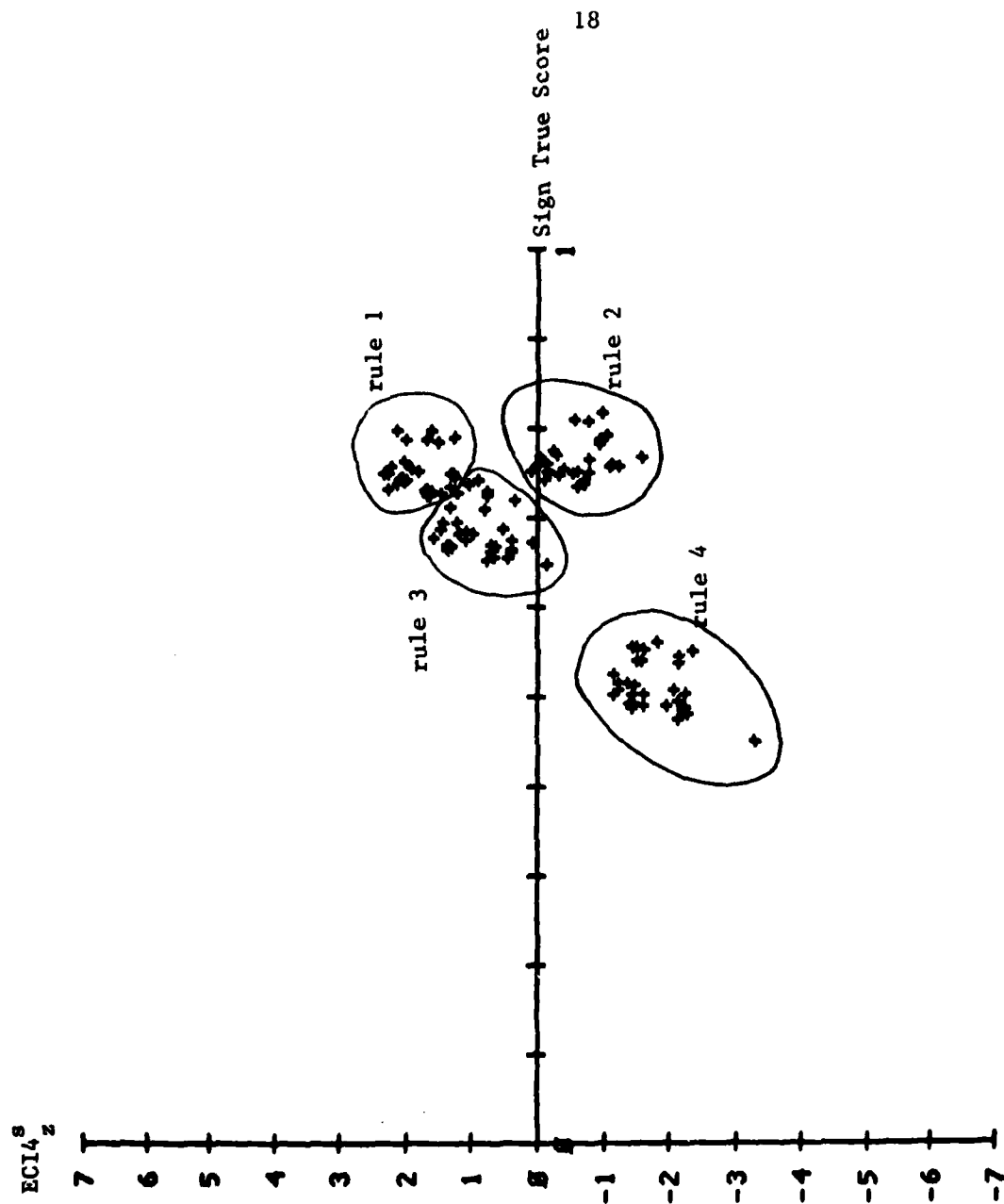


Figure 5: Plot of the Four Clusters Consisting of Inconsistent Responses Around Rules 1, 2, 3 and 4 in Table 1 for Sign Component.

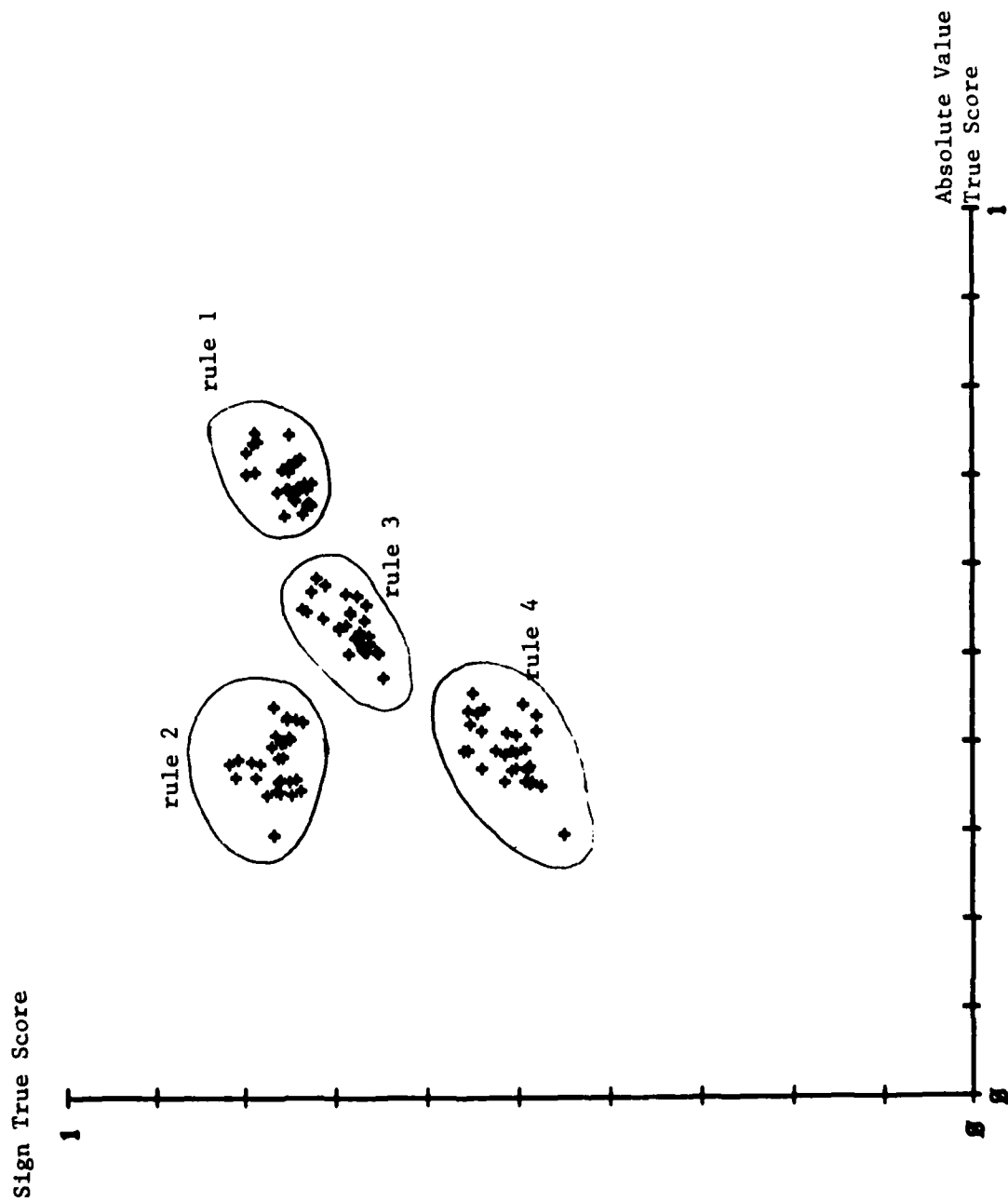


Figure 6: The Clusters of Inconsistent Responses Around Rules 1, 2, 3 and 4 in Table 1.

his knowledge level rises, he starts using the right rule
 consistency (Tatsuoka, 1982). Finally, his responses
 and more consistent and reach the right rule, represented by
 the corner in the plot in Figure 3. The phenomenon was
 observed in several datasets collected at various different
 time of a three year follow-up study of signed-number
 which is summarized in Tatsuoka (1982).

By placing Figure 1 on top of Figure 4, we are able to find a few
 whose absolute-value component patterns fall in one of the four
 The error analyses on these responses confirmed that they are
 produced by applying each rule with partial consistency.

Our erroneous rules given in Table 1 and the non-consistent
 neighboring each of them form four distinctly different
 can be seen in Figures 4, 5 and 6. However, Rules 12 and
 and 32 (for a more detailed description, see Tatsuoka &
 1981) marked in Figure 3 produce only two clusters as seen in
 the plot, when plotted in terms of the absolute-value and sign
 four distinctly different clusters are formed in the rule
 defined by the absolute value true scores and $ECI4_{12}^a$ as shown in

Insert Figures 7 & 8 about here

that the values of ECIs are capable of separating
 terms that have very close true scores.

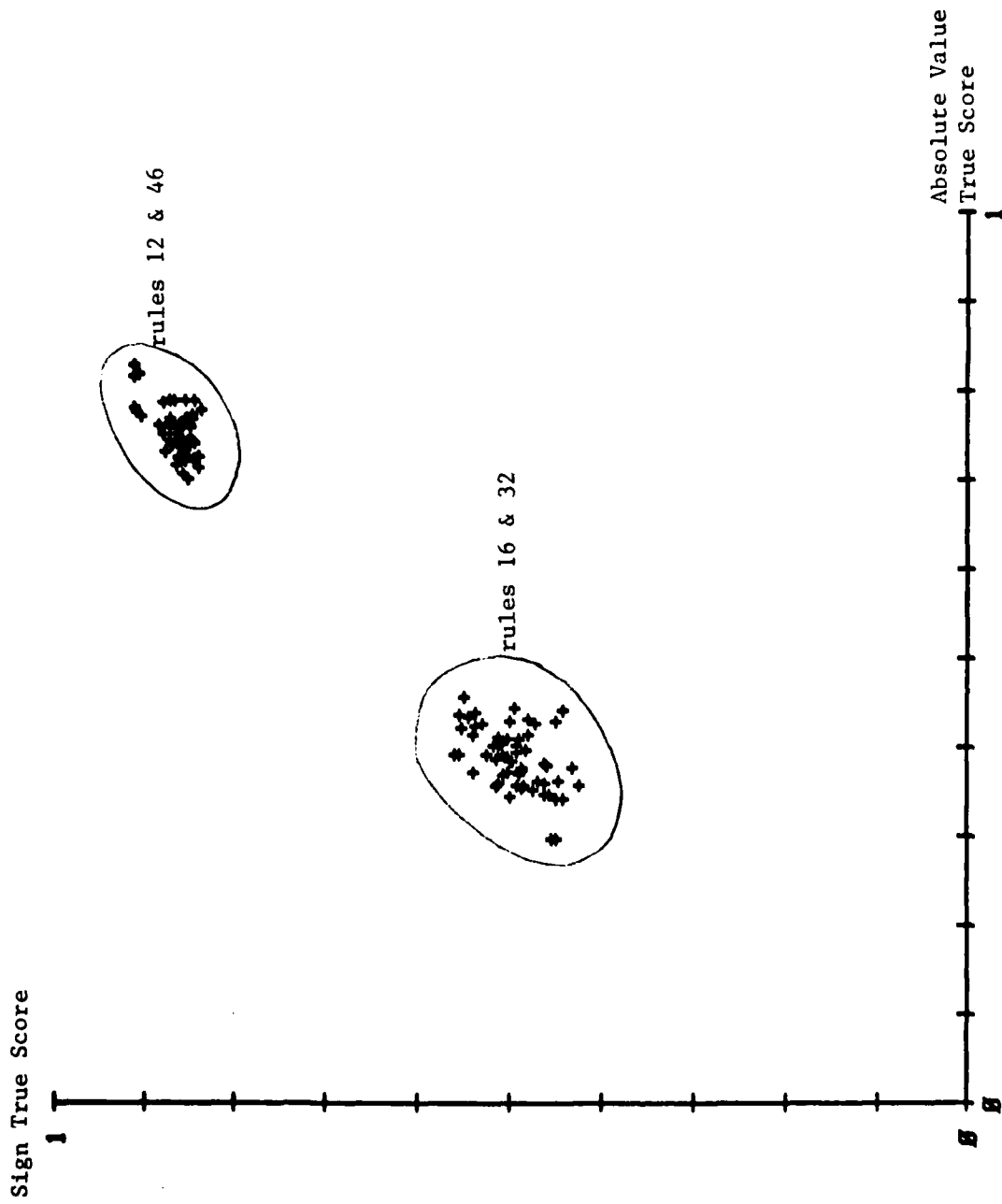


Figure 7: Plot of the Sign True Score Against Absolute Value for the Four Clusters Around Rules 12, 16, 32 and 46 in Figure 3.

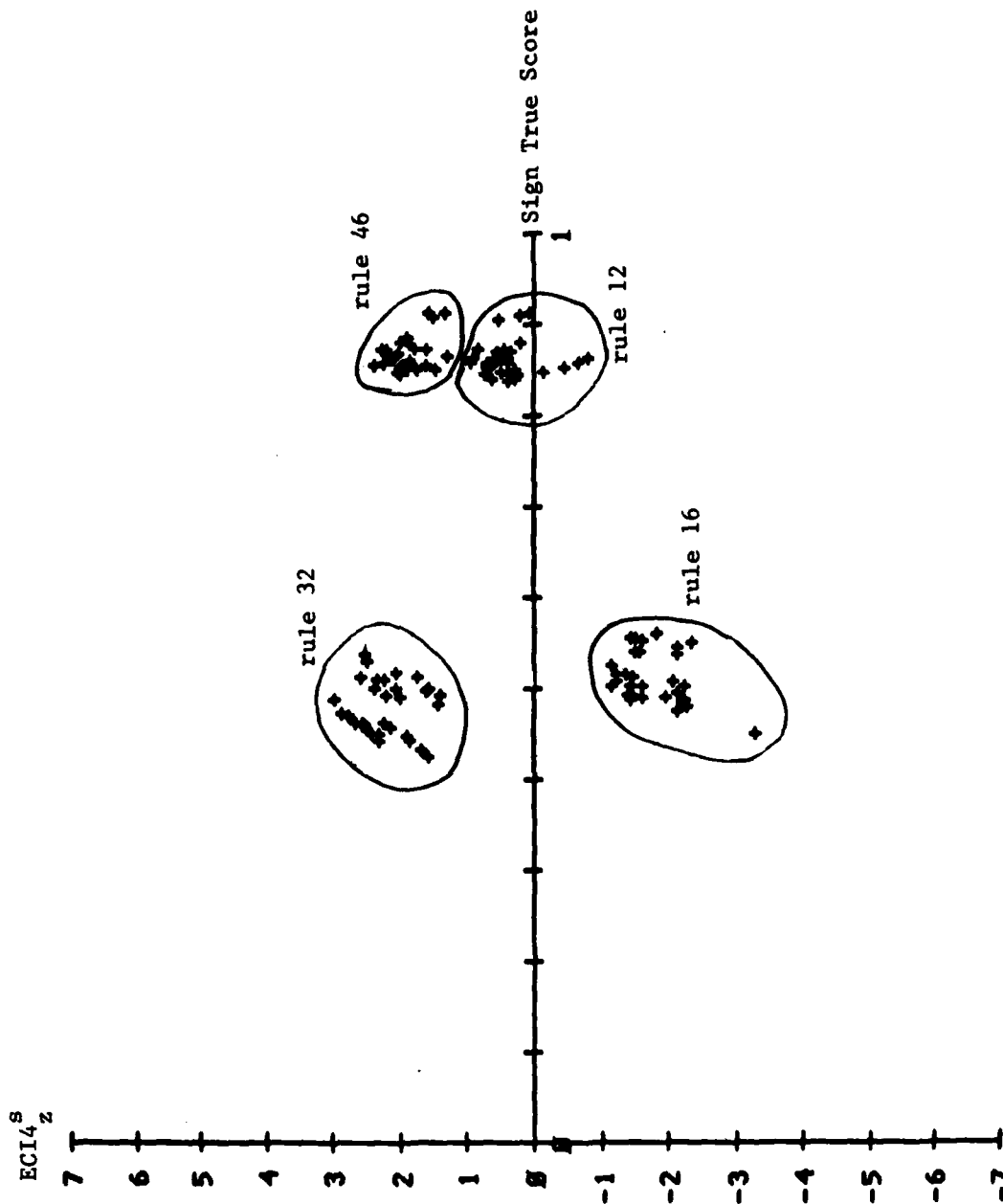


Figure 8: Plot of the Clusters Around Rules 12, 16, 32 and 46 in Figure 1, Sign True Score Against $ECI4_z^s$.

Summary and Discussion

A probabilistic model for dealing with a variety of misconceptions is developed and its useful properties are demonstrated with a 40-item signed-number subtraction test. The model is tentatively named "rule space" into which all response patterns are mapped. Rule space is defined as a cartesian product of estimated true scores and the values of standardized extended caution index, ECI_{4z} (Tatsuoka & Tatsuoka, 1982a). The advantage of using the standardized ECI is apparent from Figures 1, 2, 4 and 5 because ECI_z has the property of dispersing response patterns at the same fixed θ_i level. Therefore, if two response patterns from the same θ level are different, then their ECI_{iz} s have the two different values. As can be seen in Table 1, if we decompose the regular scoring into several components such as sign and absolute-value component scores in signed number arithmetic, then each rule has a much greater chance to be represented by a unique set of component response patterns. In the study of signed numbers, all erroneous rules discovered by SIGNBUG for over one thousand students have been uniquely represented so far by the two sets of response patterns. However, each subject matter may require a unique consideration of scoring procedures for the rule-space technique to be adapted. Then, by forming the rule spaces it may be possible to determine an individual student's state of knowledge by identifying a specific misconception, even when the responses are only partially consistent and cannot be diagnosed by the SIGNBUG approach.

References

- Baillie, R. GETAB: A computer program for estimating item and person parameters of the one- and two-parameter logistic model on the PLATO[®] system, 1980.
- Birenbaum, M., & Tatsuoka, K. K. The use of information from wrong responses in measuring students' achievement (Research Report 80-1-ONK). Urbana, Ill.: University of Illinois, Computer-based Education Research Laboratory, 1980. (AD A097715) (ERIC No. ED 202 915)
- Birenbaum, M., & Tatsuoka, K. K. On the dimensionality of achievement test data. Journal of Educational Measurement, in press, 1982a.
- Birenbaum, M., & Tatsuoka, K. K. The effect of a scoring system based on the algorithm underlying the students' response patterns on the dimensionality of achievement test data of the problem solving type. Journal of Educational Measurement, in press, 1982b.
- Brown, J. S., & Burton, R. R. Diagnostic models for procedural bugs in basic mathematical skills. Cognitive Science, 1978, 2, 155-192.
- Harnisch, D. L., & Linn, R. L. Identification of aberrant response patterns: application of caution index (Final Report). Urbana, Ill.: University of Illinois, Department of Educational Psychology, December 1981.
- Levine, M. V., & Rubin, D. B. Measuring the appropriateness of multiple-choice test scores. Journal of Educational Statistics, 1979, 4, 269-290.
- Rudner, L. M. Approaches for validating test performance. Paper presented at the meeting of the American Educational Researchers Association, New York, 1982.
- Sato, T. The construction and interpretation of S-P tables. Tokyo: Meiji Tosho, 1975 (in Japanese).
- Tatsuoka, K. K. An approach to assessing the seriousness of error types and predictability of future performance. (Research Report 81-1-ONK). Urbana, Ill.: University of Illinois, Computer-based Education Research Laboratory, February 1981. (ERIC No. ED 205 538)
- Tatsuoka, K. K. Effect of different instructional methods on error types and their consistency and change at different time points in learning. (Research Report 82-5-ONR). Urbana, Ill.: University of Illinois, Computer-based Education Research Laboratory, June 1982.
- Tatsuoka, K. K., & Baillie, R. SIGBUG: An error diagnostic computer program for signed-number arithmetic on the PLATO[®] system, 1982.

- Tatsuoka, K. K., & Linn, R. L. Indices for detecting unusual response patterns: Links between two general approaches and potential applications (Research Report 81-5-ONR). Urbana, Ill.: University of Illinois, Computer-based Education Laboratory, August 1981. Also in the Journal of Applied Psychology, 1982 (in press).
- Tatsuoka, K. K., & Tatsuoka, M. M. Detection of aberrant response patterns and their effect on dimensionality (Research Report 80-4-ONR). Urbana, Ill.: University of Illinois, Computer-based Education Research Laboratory, April 1980. (AD A091838) Also in Journal of Educational Statistics, 1982b (in press).
- Tatsuoka, K. K., & Tatsuoka, M. M. Spotting erroneous rules of operation by the individual consistency index (Research Report 81-4-ONR). Urbana, Ill.: University of Illinois, Computer-based Education Research Laboratory, 1981. Also in the Journal of Educational Psychology, 1982b (in press).
- Tatsuoka, K. K., & Tatsuoka, M. M. Standardized extended caution indices and comparison of their error detection rates (Research Report 82-4-ONR). Urbana, Ill.: University of Illinois, Computer-based Education Research Laboratory, March 1982c.
- Wright, B. D., & Stone, M. H. Best test design, Rasch Measurement. Chicago: The University of Chicago, Mesa Press, 1977.

21

Appendices

Appendix I

Estimated $\hat{a}$ s and $\hat{b}$ s of the Sign Component Scores
(N = 172)

Items	$\hat{a}$ s	$\hat{b}$ s	Items	$\hat{a}$ s	$\hat{b}$ s
11	1.1499	-1.0980	33	1.1922	-.9672
2	.7023	-1.1965	34	1.2023	-.8493
4*			36	1.3678	-.9408
6	.8025	-2.1632	38	1.0887	-1.6538
7*			39	.3135	-4.9597
8	.8057	-2.0711	40	.6888	-1.9455
9	.7383	-2.0964	41	.6432	-2.2016
12	.4391	-2.3949	44	.8380	-1.8726
13*			45	1.2010	- .6620
16	1.1973	-.4075	48	.8798	-.4871
17	1.2428	-1.1168	49	1.3178	-.9092
18	.9571	-.8658	50	1.3102	-.8352
20	1.5489	-1.0717	52	1.5050	-.7836
22	.8465	-2.0972	54	.9070	-1.7964
23	.2113	-6.8217	55	.3192	-3.8657
24	.6632	-1.9173	56	.8360	-1.4982
25	.5425	-2.4858	57	1.3123	-1.4005
28	1.0400	-1.6857	60	.6391	-2.5071
29	1.3690	-.8293	61	1.6311	-.8136
32	1.0638	-.5307	64	.6505	-.5665

*The maximum likelihood procedure did not converge

Appendix II

Estimated $\hat{a}_s$ and $\hat{b}_s$ of Absolute Value Component Scores
(N = 172)

Items	$\hat{a}_a$	$\hat{b}_a$	Items	$\hat{a}_a$	$\hat{b}_a$
1	.2703	-4.8475	33	.5805	-2.1912
2	1.1097	-.8180	34	1.4556	-.4256
4	1.4449	-.5630	36	1.5291	-.4390
6	.9975	-.7687	38	2.6000	-.5729
7	.5672	-2.0084	39	.6082	-1.5998
8*			40	.4443	-2.6204
9	1.2718	-.4632	41	1.2948	-.5126
12	1.3016	-.5674	44	1.4394	-.6516
13	2.0761	-.6438	45	1.4138	-.6880
16	.5965	-1.7412	48	.4394	-1.7471
17	.5658	-1.9440	49	.4538	-2.3231
18	.9642	-.6542	50	1.7342	-.5412
20	1.4535	-.6188	52	2.0177	-.5074
22	2.6207	-.4121	54	1.6602	-.6386
23	.4755	-2.3936	55	.6428	-1.8268
24	.3909	-2.2248	56	.4285	-2.3563
25	2.1031	0.3970	57	1.4859	-.3948
28	1.4988	-.9005	60	1.5030	-.6680
29	1.9786	-.6244	61	1.5419	-.7219
32	.6542	-1.6818	64	.4339	-1.9638

*The maximum likelihood procedure did not converge

Distribution List

Navy

1	Meryl Baker NPRDC Code P309 San Diego, CA 92152	1	Dr. James McBride Navy Personnel R&D Center San Diego, CA 92152
1	Dr. Jack R. Borsting Provost & Academic Dean U.S. Naval Postgrad Schl Monterey, CA 93940	1	Dr. William Montague Navy Personnel R&D Cent San Diego, CA 92152
1	Chief of Naval Education Liasan Office Air Force Human Resource Lab Flying Training Division Williams AFB, AZ 85224	1	Dr. William Nordbrook Instructional Program Dev. Bldg 90 NET-PDCD Great Lakes Naval Training Ctr Great Lakes, IL 60088
1	CDR Mike Curran Office of Naval Research 800 N. Quincy St. Code 270 Arlington, VA 22217	1	Ted M. I. Yellen Technical Information Office Code 201 Navy Personnel R&D Center San Diego, CA 92152
1	Dr. Pat Federico Navy Personnel R&D Center San Diego, CA 92152	1	Library, Code P201L Navy Personnel R&D Center San Diego, CA 92152
1	Mr. Paul Foley Navy Personnel R&D Center San Diego, CA 92152	6	Commanding Officer Naval Research Laboratory Code 2627 Washington, DC 20390
1	Dr. John Ford Navy Personnel R&D Center San Diego, CA 92152	1	Psychologist ONR Branch Office Bldg 114, Section D 666 Summer Street Boston, MA 02210
1	Dr. Norman Kerr Chief of Naval Technical Training Naval Air Station Memphis (75) Millington, TN 38054	1	Psychologist ONR West 1030 East Green St. Pasadena, CA 91106
1	Dr. William L. Maloy Principal Civilian Advisor for Education and Training Naval Training Command, Code 00A Pensacola, FL 32508	1	Office of Naval Research (442 PT) 800 N. Quincy Street Arlington, VA 22217
1	Cpt. Richard L. Martin, USN Prospective Commanding Officer USS Carl Vinson (CVN-70) Newport News Shipbuilding & Drydock Co. Newport News, VA 23607	5	Personnel & Training Research Programs (442 PT) Office of Naval Research Arlington, VA 22217

- 1 Chief of Naval Operations
Res. Devel. & Studies Branch
(OP-115)
Washington, DC 20350
- 1 Lt. Frank C. Petho, MSC, USN, Ph.D.
Selection and Training Res. Div.
Human Performance Sciences Department
Naval Aerospace Med. Res. Lab.
Pensacola, FL 32508
- 1 Dr. Bernard Rimland (03B)
Navy Personnel R&D Center
San Diego, CA 92152
- 1 Dr. Worth Scanland, Director
Research, Dev., Test, & Eval.
N-5
Naval Ed. & Training Command
NAS, Pensacola, FL 32508
- 1 Dr. Alfred F. Smode
Training Analysis & Ev. Grp.
(TAEG)
Dept. of the Navy
Orlando, FL 32813
- 1 Dr. Richard Sorensen
Navy Personnel R&D Center
San Diego, CA 92152
- 1 Dr. Ronald Weitzman
Code 54 WZ
Dpt. of Admin. Sci.
U.S. Naval Postgrad. Schl.
Monterey, CA 93940
- 1 Mr. John H. Wolfe
Code P310
Navy Personnel R&D Center
San Diego, CA 92152
- 1 Dr. Robert Wisher
Code 309
Navy Personnel R&D Center
San Diego, CA 92152
- 1 Dr. Martin F. Wiskoff
Navy Personnel R&D Center
San Diego, CA 92152

Army

- 1 Technical Director
Army Res. Inst.
5001 Eisenhower Ave.
Alexandria, VA 22333
- 1 James Baker
Systems Manning Tech
Army Res. Inst.
5001 Eisenhower Ave.
Alexandria, VA 22333
- 1 Dr. Beatrice Farr
Army Res. Inst.
5001 Eisenhower Ave.
Alexandria, VA 22333
- 1 Dr. Myron Fischl
Army Res. Inst.
5001 Eisenhower Ave.
Alexandria, VA 22333
- 1 Dexter Fletcher
US Army Res. Inst.
5001 Eisenhower Ave.
Alexandria, VA 22333
- 1 Dr. Michael Kaplan
Army Res. Inst.
5001 Eisenhower Ave.
Alexandria, VA 22333
- 1 Dr. Milton S. Katz
Training Tech. Area
Army Res. Inst.
5001 Eisenhower Ave.
Alexandria, VA 22333
- 1 Laurel Oliver
Army Res. Inst.
5001 Eisenhower Ave.
Alexandria, VA 22333
- 1 Dr. Harold F. O'Neil, Jr.
Attn. PERI-OK
Army Res. Inst.
5001 Eisenhower Ave.
Alexandria, VA 22333

1 Mr. Robert Ross
Army Res. Inst.
5001 Eisenhower Ave.
Alexandria, VA 22333

1 Dr. Robert Sasnor
Army Res. Inst.
5001 Eisenhower Ave.
Alexandria, VA 22333

1 Dr. Joseph Ward
Army Res. Inst.
5001 Eisenhower Ave.
Alexandria, VA 22333

Air Force

1 AF Human Resources Lab.
AFHRL/MPD
Brooks AFB, TX 78235

1 AF Office of Sci. Res.
Life Sciences Directorate, NL
Bolling AFB
Washington DC 20332

1 Dr. Earl A. Alluisi
HQ, AFHRL (AFSC)
Brooks AFB, TX 78235

1 Dr. Genevieve Haddad
Program Manager
Life Sciences Directorate
AFOSR
Bolling AFB,
Washington, DC 20332

1 Res. & Measurement Div.
Res. Branch, AFMPC/MPCYPR
Randolph AFB, TX 78148

1 Dr. Malcolm Ree
AFHRL/MP
Brooks AFB, TX 78235

1 Dr. Marty Rockway
Technical Director
AFHRL(OT)
Williams AFB, AZ 58224

Marines

1 H. William Greenup
Education Advisor (EO31)
Education Center, MCDEC
Quantico, VA 22134

1 Major Howard Langdon
HQ, Marine Corps
OTTI 31
Arlington Annex
Columbia Pike at Arlington Ridge Rd.
Arlington, VA 20380

1 Director, Off. of Manpwr Util.
HQ, Marine Corps (MPU)
BCB, Bldg. 2009
Quantico, VA 22134

1 HQ, Marine Corps
Code PMI-20
Washington, DC 20380

1 Special Ast. for Marine Corps
Code 100M
Office of Naval Research
800 N. Quincy St.
Arlington, VA 22217

1 Maj. Michael Patrow, USMC
HQ, Marine Corps
(Code MPI-20)
Washington DC 20380

1 Dr. A.L. Slafkosky
Scientific Advisor (Code RD-1)
HQ, Marine Corps
Washington, DC 20380

Coast Guard

1 Chief, Psych. Res. Branch
Coast Guard (G-P-1/2/TP42)
Washington, DC 20593

1 Thomas A. Warm
Coast Guard Inst.
P.O. Substation 18
Oklahoma City, OK 73169

Civil Government

- 1 Dr. Susan Chipman
Learning & Development
NIE
1200 19th St. NW
Washington, DC 20208
- 1 John Mays
National Inst. of Ed.
1200 19th St. NW
Washington, DC 20208
- 1 Richard McKillip
Personnel R&D Center
Personnel Management
1900 E. St. NW
Washington, DC 20415
- 1 William J. McLaurin
66610 Howie Court
Camp Springs, MD 20031
- 1 Dr. Arthur Melmed
National Inst. of Ed.
1200 19th St. NW
Washington, DC 20208
- 1 Dr. Andrew R. Molnar
Sci. Ed. Dev. & Res.
NSF
Washington, DC 20550
- 1 Dr. Joseph Psotka
NIE
1200 19th St. NW
Washington, DC 20208
- 1 Wallace Sinaiko
Program Director MRHS
Smithsonian Institution
801 N. Pitt Street
Alexandria, VA 22314
- 1 Dr. Vern W. Urry
Personnel R&D Center
Office of Personn. Mngmnt.
1900 E St. NW
Washington, DC 20415

- 1 Frank Withrow
US office of Ed.
400 Maryland Ave. SW
Washington, DC 20202
- 1 Dr. Joseph L. Young, Dir.
Memory & Cognitive Processes
NSF
Washington, DC 20550

Other Department of Defense

- 12 Defense Technical Information Center
Cameron Station, Bldg 5
Alexandria, VA 22314
Attn:TC
- 1 Dr. William Graham
Testing Directorate
MEPCOM/MEPCT-P
Ft. Sheridan, IL 60037
- 1 Military Assistant for
Training and Personnel Tech.
Office of the Under Secretary
of Defense for Res. & Eng.
Room 3D129, The Pentagon
Washington, DC 20301
- 1 Dr. Wayne Sellman
Office of the Asstnt. Sec.
of Defense (MRA & L)
Room 2B269, The Pentagon
Washington, DC 20301
- 1 DARPA
1400 Wilson Blvd.
Arlington, VA 22209

Non Government

- 1 Dr. James Algina
University of Florida
Gainsville, FL 32611
- 1 Dr. Erling B. Andersen
Dept. of Statistics
Studiestraede 6
1455 Copenhagen
DENMARK

- 1 Dr. John R. Anderson
Department of Psychology
Carnegie Mellon University
Pittsburgh, PA 15213
- 1 Dr. Thomas Anderson
CSR
174 Children's Res. Lab.
51 Gerty Drive
Champaign, IL 61820
- 1 Dr. John Annett
Dept. of Psychology
University of Warwick
Coventry CV4 7AL
ENGLAND
- 1 1Psych. Res. Unit
Dept. of Defense (Army)
Campbell Park Offices
Canberra ACT 2600
AUSTRALIA
- 1 Dr. Allan Baddeley
Medical Res. Council
Applied Psych. Unit
15 Chaucer Road
Cambridge CB2 2EF
ENGLAND
- 1 Dr. Patricia Baggett
Dept. of Psych.
University of Colorado
Boulder, CO 80309
- 1 Mr. Avron Barr
Department of Computer Science
Stanford University
Stanford, CA 94305
- 1 Dr. Issac Bejar
Educational Testing Serv.
Princeton, NJ 08450
- 1 Dr. Menucha Birenbaum
School of Ed.
Tel Aviv University
Ramat Aviv - Box 39040
Tel Aviv 69978
ISRAEL
- 1 Dr. Werner Birke
DezWPs im Streitkrafteamt
Postfach 20 50 03
D-5300 Bonn 2
WEST GERMANY
- 1 Dr. Darrel Bock
Dept. of Ed.
University of Chicago
Chicago, IL 60637
- 1 Liaison Scientists
Office of Naval Research
Branch Office, London
Box 39 FPO
New York, NY 09510
- 1 Dr. Lyle Bourne
Dept. of Psych.
University of Colorado
Boulder, CO 80309
- 1 Dr. Walter Bogan
4615 N. Park Ave, no. 1611
Chevy Chase, MD 20015
- 1 Dr. Robert Brennan
American College Testing Programs
P.O. Box 168
Iowa City, IA 52240
- 1 Dr. John S. Brown
XEROX Palo Alto Res. Cnt.
3333 Coyote Rd.
Palo Alto, CA 94304
- 1 Dr. C. Victor Bunderson
WICAT Inc.
University Plaza, Suite 10
1160 S. State St.
Orem, UT 84057
- 1 Dr. Leigh Burstein
Dept. of Education
University of California
Los Angeles, CA 90024
- 1 Dr. John B. Carroll
Psychometric Lab
Univ. of N. Carolina
Davie Hall 013A
Chapel Hill, NC 27514

William Chase
Psych.
Mellon University
Pittsburgh, PA 15213

William Clancey
Computer Sci.
University
Berkeley, CA 94305

William Coates
University
Michigan Ave. NE
Washington, DC 20064

William Cliff
Psychology
University of California
Berkeley, CA 94720

William E. Coffman
Iowa Testing Prog.
Lindquist Center
University of Iowa
Iowa City, IA 52242

William M. Collins
Beranek & Newman
Cambridge, MA 02138

William A. Cooper
University of Pittsburgh
Pittsburgh, PA 15213

William H. Crawford
Psych. Association
Washington, DC 20013

William H. Cronbach
Education
University
Berkeley, CA 94305

1 Dr. Evelyn Doody
Dept. of Psych
University of Oklahoma
529-D Stinson
Norman, OK 73069

1 Dr. Fritz Drasgow
Yale Schl. Organ. & Management
Yale University
Box 1A
New Haven, CT 06520

1 Dr. Leonard Feldt
Lindquist Center for Measurement
University of Iowa
Iowa City, IA 52242

1 Dr. Richard Ferguson
The Am. College Testing Prog.
P.O. Box 168
Iowa City, IA 52240

1 Mr. Wallace Feurzeig
Bolt Beranek & Newman, Inc.
50 Moulton St.
Cambridge, MA 02138

1 Dr. Victor Fields
Dept. of Psychology
Montgomery College
Rockville, MD 20850

1 Dr. Gerhard Fischer
Liebiggasse 5/3
A 1010 Vienna
AUSTRIA

1 Dr. Donald Fitzgerald
University of New England
Armidale, N. S. Wales 2351
AUSTRALIA

1 Dr. Edwin A. Fleishman
Advanced Research Resources Corp.
Suite 900
4330 E. West Highway
Washington, DC 20014

1 Dr. John Frederiksen
Bolt Beranek & Newman
50 Moulton St.
Cambridge, MA 02138

Dr. Paul Games
403D Carpenter
University Park, PA 16802

Dr. Robert Glaser
LRDC
University of Pittsburgh
3939 O'Hara St.
Pittsburgh, PA 15213

Dr. Bert Green
John Hopkins University
Dept. of Psychology
Charles & 34th St.
Baltimore, MD 21218

Dr. James Greeno
LRDC
3939 O'Hara St.
Pittsburgh, PA 15213

Dr. Ron Hambleton
School of Education
University of Massachusetts
Amherst, MA 01002

Dr. Delwyn Harnisch
ICBD
University of Illinois
51 Gerty Drive
Champaign, IL 61801

Dr. Chester Harris
School of Education
University of California
Santa Barbara, CA 93106

Dr. Barbara Hayes-Roth
The Rand Corporation
1700 Main St.
Santa Monica, CA 90406

Dr. Frederick Hayes-Roth
The Rand Corporation
1700 Main St.
Santa Monica, CA 90406

Dr. Dustin H. Heuston
Wicat, Inc.
Box 986
Orem, UT 84057

1 Dr. Kristina Hooper
Clark Kerr Hall
University of Calif.
Santa Cruz, CA 95060

1 Dr. Paul Holtzman
Decision Systems
MFI
100 S. Wacker Drive
Chicago, IL 60606

1 Dr. Lloyd Humphreys
421 Psychology
University of Illinois
Champaign, IL 61820

1 Prof. Raimo Konttinen or
Library
Institute for Ed Research
University of Jyväskylä
40100 Jyväskylä
FINLAND

1 Library
HumRRO/Western Division
27857 Berwick Drive
Carmel, CA 93921

1 Dr. Steven Hunka
Dept. of Education
University of Alberta
Edmonton, Alberta
CANADA

1 Dr. Earl Hunt
Dept. of Psychology
University of Washington
Seattle, WA 98105

1 Dr. Jack Hunter
2122 Coolidge St.
Lansing, MI 48906

1 Dr. Ed Hutchins
Navy Personnel R&D Center
San Diego, CA 92152

1 Dr. Huynh Huynh
College of Education
University of South Carolina
Columbia, SC 29208

- | | | | |
|---|---|---|--|
| 1 | Professor John A. Keats
University of Newcastle
AUSTRALIA 2308 | 1 | Dr. Robert Linn
210 Education
University of Illinois
Urbana, IL 61801 |
| 1 | Jeff Kelety
Dept. of Instr. Tech.
University of S. Calif.
Los Angeles, CA 92007 | 1 | Bob Loo, Ph.D.
Department of Psychology
The University of Calgary
2920 - 24th Ave. NW
Calgary, Alberta
CANADA T2N 1N4 |
| 1 | Dr. Walter Kintsch
Dept. of Psych.
University of Colorado
Boulder, CO 80302 | 1 | Dr. Frederick M. Lord
Educational Testing Ser.
Princeton, NJ 08540 |
| 1 | Dr. David Kieras
Dept. of Psych.
University of Arizona
Tucson, AZ 85721 | 1 | Dr. Drew Malizio
American Counc. on Ed.
No. 1 Pont Circle, #20
Washington, DC 20036 |
| 1 | Dr. Stephan Kosslyn
Harvard University
Dpt. of Psych.
33 Kirkland St.
Cambridge, MA 02138 | 1 | Dr. Gary Marco
Educational Testing Service
Princeton, NJ 08540 |
| 1 | Mr. Marlin Kroger
1117 Via Goleta
Palos Verdes Estates, CA 90274 | 1 | Dr. Scott Maxwell
Dpt. of Psych.
Univ. of Houston
Houston, TX 77004 |
| 1 | Dr. Marcy Lansman
Dpt. of Psych. NI 25
Univ. of Washington
Seattle, WA 98195 | 1 | Dr. David McArthur
CSE 145 Moor Hall
UCLA
Los Angeles, CA 90024 |
| 1 | Dr. Jill Larkin
Dpt. of Psych.
Carnegie Mellon Univ.
Pittsburgh, PA 15213 | 1 | Dr. Samuel T. Mayo
Loyola U. of Chicago
820 N. Michigan Av.
Chicago, IL 60611 |
| 1 | Dr. Alan Lesgold
LRDC
Univ. of Pittsburgh
Pittsburgh, PA 15260 | 1 | Dr. Erik McWilliams
Science Ed. Dev. & Res.
National Science Foundation
Washington, DC 20550 |
| 1 | Dr. Michael Levine
Dept. of Ed Psych
210 Education Bldg.
University of Illinois
Champaign, IL 61801 | 1 | Dr. Peter Mich
Ed Psych
Enderis Hall 719
University of Wisconsin
P.O. Box 413
Milwaukee, WI 53201 |
| 1 | Dr. Charles Lewis
Faculteit Sociale Wetenschappen
Rijksuniversiteit Groningen
Oude Boteringestraat 23
9712GC Groningen
NETHERLANDS | | |

- | | | | |
|---|--|---|--|
| 1 | Dr. David Miller
Graduate School of Ed.
UCLA
Los Angeles, CA 90024 | 1 | Dr. James Pellegrino
Univ. of Calif.
Dpt. of Psych.
Santa Barbara, CA 93106 |
| 1 | Dr. Mark Miller
TI Computer Sci. Lab
C/O 2824 Winterplace Circle
Plano, TX 75075 | 1 | Mr. Luigi Petrullo
2431 N. Edgewood St.
Arlington, VA 22207 |
| 1 | Dr. Allen Munro
Behvr. Tech. Lab.
1845 Elena Ave. 4th floor
Redondo Beach, CA 90277 | 1 | Dr. Martha Polson
Dpt. of Psych.
Campus Box 346
University of Colorado
Boulder, CO 80309 |
| 1 | Dr. Anthony J. Nitko
School of Ed.
Division of Ed. Studies
University of Pittsburgh
5C03 Forbes Quadrangle
Pittsburgh, PA 15260 | 1 | Dr. Peter Posner
Dpt. of Psych.
Univ. of Oregon
Eugene, OR 97403 |
| 1 | Dr. Donald A. Norman
Dpt. of Psych. C-009
Univ. of Calif.
La Jolla, CA 92093 | 1 | Dr. Peter Polson
Dpt. of Psych.
University of Colorado
Boulder, CO 80309 |
| 1 | Dr. Melvin Novick
356 Lindquist Cntr for Measur.
University of Iowa
Iowa City, IA 52242 | 1 | Dr. Diane M. Ramsey-Klee
R-K Res. & System Design
3947 Ridgmont Dr.
Malibu, CA 90265 |
| 1 | Dr. Jesse Orlansky
Inst. for Defense Analyses
400 Army Navy Drive
Arlington, VA 22202 | 1 | Minrat M. L. Rauch
P II 4
Bundesministerium der
Verteidigung
Postfach 1328
D-53 Bonn 1
GERMANY |
| 1 | Dr. Seymour A. Papert
MIT
Artific. Intelli. Lab.
545 Technology Square
Cambridge, MA 02139 | 1 | Dr. Mark D. Reckase
Ed Psych Dept.
University of Missouri
4 Hill Hall
Columbia, MO 65211 |
| 1 | Wayne M. Patience
American Council on Education
GED Testing Service, suite 20
One Dupont Circle, NW
Washington, DC 20036 | 1 | Dr. Lauren Resnick
LRDC
University of Pittsburgh
3939 O'Hara St.
Pittsburgh, PA 15213 |
| 1 | Dr. James A. Paulson
Portland State University
P.O. Box 751
Portland, OR 97207 | 1 | Dr. Mary Riley
LRDC
Univ. of Pittsburgh
3939 O'Hara St.
Pittsburgh, PA 15213 |

- 1 Dr. Andrew M. Rose
American Inst. for Res.
1055 Thomas Jefferson St. NW
Washington, DC 20007
- 1 Dr. Leonard L. Rosenbuan
Dept. of Psychology
Montgomery College
Rockville, MD 20850
- 1 Dr. Ernst Z. Rothkopf
Bell Laboratories
600 Mountain Ave.
Murry Hill, NJ 07974
- 1 Dr. Lawrence Rudner
403 Elm Ave.
Takoma Park, MD 20012
- 1 Dr. David Rumelhart
Cntr. for Human Info.
Univ. of Calif.
La Jolla, CA 92093
- 1 Dr. J. Ryan
Dept. of Ed.
University of S. Carolina
Columbia, SC 29208
- 1 Dr. Fumiko Samejima
Dept. of Psychology
U. of Tennessee
Knoxville, TN 37916
- 1 Dr. Alan Schoenfeld
Dpt. of Mathematics
Hamilton College
Clinton, NY 13323
- 1 Dr. Robert J. Seidel
Instr. Tech. Group
HUTMRRO
300 N. Washington St.
Alexandria, VA 22314
- 1 Dr. John Serber
University of Wisconsin
Dept. of Ed Psych
Milwaukee, WI 53201

- 1 Dr. Shigemasu
University of Tohoku
Dept. of Ed Psych
Kawauchi, Sendai 980
JAPAN
- 1 Dr. Edwin Shirkey
Dept. of Psychology
University of Centl Florida
Orlando, FL 32816
- 1 Dr. Ed Smith
Bolt Beranek & Newman, Inc.
50 Moulton St.
Cambridge, MA 02138
- 1 Dr. Richard Snow
School of Ed.
Stanford University
Stanford, CA 94305
- 1 Dr. Robert Sternberg
Dept. of Psychology
Yale University
Box 11A, Yale Station
New Haven, CT 06520
- 1 Dr. Albert Stevens
Bolt Beranek & Newman, Inc.
50 Moulton St.
Cambridge, MA 02138
- 1 Dr. David E. Stone
Hazeltine Corp.
7680 Old Springhouse Rd.
McLean, VA 22102
- 1 Dr. Patrick Suppes
Inst. for Math. Studies
in Soc. Sci.
Stanford University
Stanford, CA 94305
- 1 Dr. Hariharan Swaminathan
Lab. of Psychom. & Evi. Res.
School of Ed.
University of Massachusetts
Amherst, MA 01003
- 1 Dr. Brad Symson
Psychometric Research Group
Ed. Testing Service
Princeton, NJ 08541

Dr. David Thissen
Dept. of Psychology
U. of Kansas
Lawrence, KS 66044

Dr. John Thomas
IBM Thomas Watson
Res. Cnt.
P.O. Box 218
Yorktown Heights, NY 10598

Dr. Perry Thorndyke
The Rand Corp.
1700 Main St.
Santa Monica, CA 90406

Dr. Robert Tsutakawa
Dept. of Statistics
University of Missouri
Columbia, MO 65201

Dr. Howard Wainer
Division of Psychological Studies
Ed. Testing Service
Princeton, NJ 08540

Dr. Keith Wescourt
Information Sciences Dpt.
The Rand Corp.
1700 Main St.
Santa Monica, CA 90406

1 P.O. White
Dept. of Psychology
Institute of Psychiatry
DeCrespigny Park
London SE5 8AF
ENGLAND

1 Dr. Susan Whitely
Psychology Dept.
University of Kansas
Lawrence, KS 66044

1 Wolfgang Wildgrube
Streitdraefteamt
Box 20 50 03
D-5300 Bonn 2
WEST GERMANY

1 Dr. Steven Wise
Dept. of Guid. & Ed Psych
S. Illinois University
Carbondale, IL 62901