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Spectroscopic Parameters for Ozone From Infrared and Ultraviolet Techniques

S.M. ADLER-GOLDEN
R.A. ARMSTRONG

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Spectroscopic Parameters for Ozone From Infrared and Ultraviolet Techniques

1. INTRODUCTION

Ozone is an important source of infrared background radiation in the upper atmosphere. The spectral extent of this ozone emission is a function of the distribution of emitting vibrational levels. In the 80- to 120-km altitude region, high vibrational levels are populated via the $O + O_2 + M \rightarrow O_3^* + M$ recombination reaction, and it appears that a significant portion of these levels can emit prior to collisional relaxation. Thus, information concerning the population and relaxation of excited vibrational levels of ozone in the atmosphere is highly valuable.

Several approaches are currently under way to obtain information on the ozone recombination. One is the direct measurement of atmospheric IR radiance using rocket-borne probes.¹ Unfortunately, this approach is costly, and alternatives involving laboratory rather than field experiments are thus very appealing. The most sophisticated laboratory approach currently available utilizes the COCHISE

(Received for publication 11 August 1982)

1. Nadile, R. M., Stair, A. T., Jr., Wheeler, N. B., Frodsham, D. G., Wyatt, C. L., Baker, D. J., and Grieder, W. F. (1978) SPIRE-Spectral Infrared Rocket Experiment (Preliminary Results), AFGL-TR-78-0107, Air Force Geophysics Laboratory, Hanscom AFB, ADA058504; Degges, T. C., Stair, A. T., Jr., Nadile, R. M., and Hegblom, E. R. (1979) Altitude dependence and spectral character of atmospheric ozone long wavelength infrared emission, EOS Trans. AGU, 60:338.

(Cold Chemi-excited Infrared Simulation Experiment) apparatus at the Air Force Geophysics Laboratory (AFGL).² Ozone is formed under low pressure conditions similar to the upper atmosphere; the resulting chemiluminescence is measured in a cryogenic environment that enables high sensitivity and good spectral resolution. The ν_3 band emission has been investigated. Hot band emission has been observed, but the nascent distribution has not been directly measured, and its derivation must rely on estimated Einstein "A" coefficients for $\nu_3 > 1$.

Another method of obtaining information about the ozone recombination is based on time-resolved ultraviolet absorption measurements of ozone formed following pulsed excitation of oxygen or ozone-oxygen mixtures.^{3,4} Bair and co-workers have obtained extensive data in a system in which high pressures (about 0.1 to 1 atm) of O_2 to O_3 mixtures are flash-photolyzed, and the resultant O atoms recombine on a time scale of tens of microseconds.⁴ In these experiments the UV Hartley band of the freshly-formed ozone is seen to be altered from its normal appearance. Early workers³ attributed this effect to ozone being formed in a "precursor" state of an unspecified nature, which subsequently relaxes to ground-state ozone. Recent work has identified the precursor as vibrationally excited ozone.^{4,5} Bair and co-workers have indeed attempted to extract vibrational distributions and relaxation rates from their data.⁴ Although their spectral analysis method is not exact, their work demonstrates that quantitative information on the recombination can be extracted from UV spectra. A more careful analysis is definitely required.

This report is a result of our investigation of the ozone data base and consequent analysis of approaches to understanding atmospheric nonequilibrium radiative properties of ozone. The first two sections, the energy levels and Einstein "A" coefficients, are directly applicable to analysis of AFGL field and COCHISE results. The last section, an ultraviolet diagnostic for ozone, exemplifies an alternative approach that will supplement the analysis.

2. CALCULATIONS OF VIBRATIONAL LEVELS FOR OZONE

Chemiluminescence from high vibrationally-excited states of ozone resulting from the reaction $O + O_2 + M \rightarrow O_3^* + M$ has been observed in COCHISE. A full analysis of the signal requires knowledge of the emission frequencies, ν , given by

$$h\nu = E(\nu_1, \nu_2, \nu_3) - E(\nu_1, \nu_2, \nu_3 - 1) \quad (1)$$

(Due to the large number of references cited above, they will not be listed here. See References, page 21.)

as well as the Einstein coefficients (inverse lifetimes), denoted $A(v_1, v_2, v_3) \rightarrow (v_1, v_2, v_3 - 1)$, for all vibrational levels (v_1, v_2, v_3) that are appreciably populated in the ozone forming reaction.

The most extensive tabulation of energy levels $E(v_1, v_2, v_3)$ is found in Barbe.⁶ All levels having up to 3 quanta, (that is, $v_1 + v_2 + v_3 \leq 3$) are included. In addition, several 4-quantum levels are observed. Most of the data is derived from absorption measurements using a long optical pass ($l \times c = 2.5$ meter-atm) in a double beam spectrometer. The results are summarized in Table 1 in the "Exptal." column.

Spectroscopic constants for the energy levels were determined by the following procedure. First the formula

$$E_u = \sum_{i=1}^3 \omega_i (v_i + \frac{1}{2}) + \sum_{i \geq j=1}^3 x_{ij} (v_i + \frac{1}{2}) (v_j + \frac{1}{2}) \quad (2)$$

is used to find E_u , the energies of (hypothetical) unperturbed levels. Then a Darling-Dennison perturbation is added which couples the stretching motions and alters these levels. The resulting perturbed levels are obtained by diagonalizing the perturbation matrix. The appropriate matrix elements in the harmonic oscillator basis are given explicitly in Reference 6. (The matrix diagonalization is very straightforward, especially since for $v_1 + v_3 \leq 5$ it is at most a 3×3 .) The perturbed levels calculated by Barbe⁶ according to this prescription appear in Table 1 in the "Barbe Calc." column. Agreement with the experimental energy values is excellent, typically better than 1 cm^{-1} .

Clearly, the foregoing method for finding the energy levels can be extended to include those levels not already tabulated. We have performed the calculation on levels relevant to the COCHISE experiment for up to 5 quanta. The results are presented in Table 1 under "Current." To check the accuracy of the current work, the values may be compared with the "Barbe Calc." column. There are some minor discrepancies between the two columns, the source of which is unclear, but generally the agreement is good. It appears that the 4-quantum levels should agree with experiment to within about 1 cm^{-1} . The 5-quantum levels may be somewhat less accurate. Calculations on higher v -levels are not shown as it may be unrealistic to expect accurate results at such high energies. In fact, 5- and 6-quantum levels may lie in the quasi-continuum.⁷

6. Barbe, A., Secroun, C., and Jouve, P. (1974) Infrared spectra of $^{16}\text{O}_3$ and $^{18}\text{O}_3$: Darling and Dennison resonance and anharmonic potential function of ozone, *J. Mol. Spectros.* 49:171.

7. Hansel, K. D. (1979) On the dynamic of multiphoton dissociation of polyatomic molecules II. Application to O_3 : *Laser-Induced Processes in Molecules* (K. L. Kompa and S. D. Smith, Ed.), Springer Series in Chemical Physics, Vol. 6, Springer, Berlin.

Table 1. Ozone Energy Levels (cm^{-1})

Level	Exptal.	Barbe Calc.	Current
100	1103.15
010	700.93
*001	1042.096
200	2201.3	2201.6	2201.8
020
*002	2058.0	2057.8	2057.7
*101	2110.79	2110.5	...
*110	1795.3	1795.0	...
*011	1726.4	1726.0	...
300	...	3291.3	3291.3
030
*003	3046.0	3045.2	3045.0
210	...	2884.2	2884.0
201	3185.7	3186.5	3186.7
120
021	2409.5	2408.0	...
*102	3084.1	3085.2	3085.3
*012	2725.6	2725.5	2725.2
*111	2785.24	2785.3	...
400	4372.2
202	4142.7
*004	4000.4
301	...	4252.3	4252.3
*103	4026.0	4026.9	4026.9
310	3964.2
*112	3743.9
211	3849.4	3850.2	3850.7
*013	3697.1	3697.1	3696.7
220	3564.3
022	3390.6
121	3457.5	3458.1	3458.2
*104	4934.0
*005	4919.2
*014	4637.6
*113	4670.1

* Important for COCHISE

As already mentioned, the Table 1 listing is not complete, but restricted so as to concentrate on those levels relevant to the COCHISE experiment. The levels taken to be most significant for COCHISE are marked with an asterisk and consist of the following:

- a. levels $(0, 0, v_3)$, ≤ 5
- b. levels $(1, 0, v_3)$, ≤ 4
- c. levels $(0, 1, v_3)$, ≤ 4
- d. levels $(1, 1, v_3)$, ≤ 3

The rationale for choosing these levels is based on the assumption that the ν_1 and ν_3 modes are thermally equilibrated with each other (with a bath temperature of 80°K)² in COCHISE prior to observation of the emission; this is because the rate of exchange of quanta between the ν_1 and ν_3 modes is expected to be on the order of gas kinetic. Since this process occurs without gain or loss of quanta, we conclude that all levels having the same value of $(v_1 + v_3)$ are thermally equilibrated. From the computed energy levels, it is readily shown that levels having $v_1 \geq 2$ are negligibly populated given this condition. The levels having $v_2 = 0$ which are appreciably populated are thus type a and b levels. Similarly, the levels having $v_2 = 1$ which are of significance are the type c and type d levels. If necessary, the calculation may be extended to include levels having $v_2 \geq 2$.

The transition frequencies in cm^{-1} for the aforementioned levels are given in Figure 1. The figure also shows schematically the kinetic coupling between the levels, previously discussed, namely,

$$(1, v_2, n) \longleftrightarrow (0, v_2, n+1) . \quad (1)$$

The population ratio of these levels is fixed by the bath temperature. In Figure 1, the expected ratio for a bath temperature of 80°K is indicated. The adjustable parameters required to fit the COCHISE spectrum can be reduced to a manageable number by using fixed ratios between certain level populations.

3. EINSTEIN COEFFICIENTS FOR OZONE

The problem of calculating accurate Einstein coefficients for an anharmonic, coupled triatomic molecule, such as ozone, is a formidable one. Both a suitable potential surface and dipole moment function are required as a starting point. The full quantum mechanical solution may then be obtained in principle, using the variational method. In practice, however, due to necessary limitations on the size of the basis set, only the lower vibrational levels may be treated accurately. A new semiclassical approach may be a promising alternative to the full quantum treatment.⁸ The accuracy of this approach appears to be limited primarily by the uncertainty in the dipole moment function.

8. Noid, D. W., Koszykowski, M. L., and Marcus, R. A. (1977) A spectral analysis method of obtaining molecular spectra from classical trajectories, *J. Chem. Phys.* 67:404.

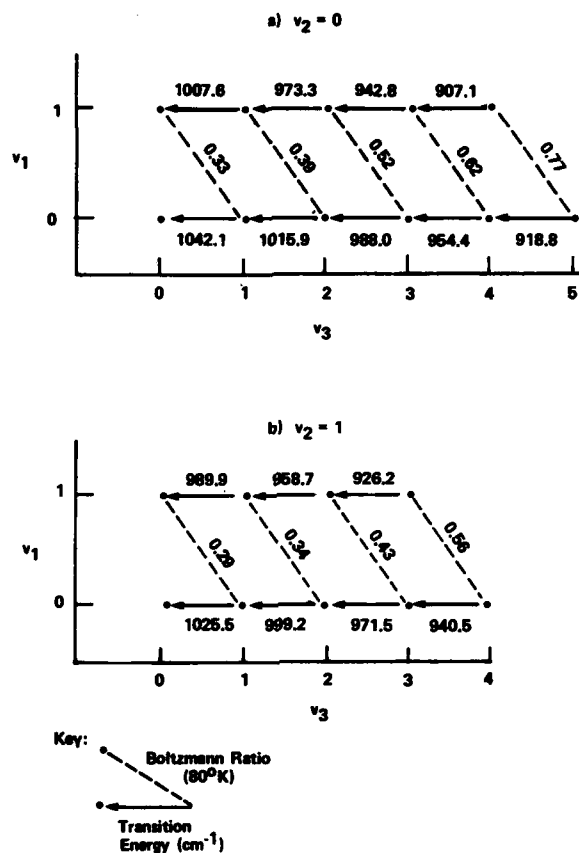


Figure 1. Ozone Transition Energies and Relative Boltzmann Populations

We consider here some approximate qualitative models. The simplest model, which is nonetheless adequate for many situations, utilizes a harmonic oscillator (that is, assumes "mechanical harmonicity"). We also assume, for the moment, "electrical harmonicity," which means that only the first order dipole matrix element $|\langle \Psi_f | q | \Psi_i \rangle|^2$ is considered (q is a vibrational coordinate). The behavior of the Einstein coefficient for this case is given by

$$\left(\frac{\nu_{001 \rightarrow 000}}{\nu} \right)^3 \frac{A_{v_3 \rightarrow v_3-1}}{A_{001 \rightarrow 000}} = v_3 \quad (4)$$

(independent of v_1 and v_2); $A_{001 \rightarrow 000}$ is known accurately,² and ν appears in Table 1. This formula was used in Reference 2 for a preliminary analysis of the COCHISE data.

An appreciably more accurate result is given by evaluating the first order matrix element in the basic set of wave functions that were obtained when the perturbation matrix was diagonalized. This procedure takes into account much of the mechanical anharmonicity actually present. The results are given in Table 2 in the column "Perturbed Harmonic." For comparison, Eq. (4) is given in the "Unperturbed Harmonic" column. It is seen that the Darling-Dennison perturbation has a significant, although not drastic, effect on the Einstein coefficients.

Table 2. (Matrix Element) $\times 2$ for $\Delta v_3 = -1$ Transitions

	Eq. (4) Unperturbed Harmonic	Perturbed Harmonic
000 \rightarrow 000	1	1
002 \rightarrow 001	2	1.93
101 \rightarrow 100	1	1
011 \rightarrow 010	1	1
003 \rightarrow 002	3	2.75
102 \rightarrow 101	2	1.89
012 \rightarrow 011	2	1.94
111 \rightarrow 110	1	1
004 \rightarrow 003	4	3.40
103 \rightarrow 102	3	2.69
013 \rightarrow 012	3	2.79
112 \rightarrow 111	2	1.91
005 \rightarrow 004	5	3.81
104 \rightarrow 103	4	3.41
014 \rightarrow 013	4	3.50
113 \rightarrow 112	3	2.73

A somewhat unexpected phenomenon results from the Darling-Dennison perturbation which may be of some importance. A small but nonnegligible intensity in the ($\Delta v_3 = -3, \Delta v_1 = 2$) sequence, lying to the red of the main ν_3 progression, is predicted. The quantity

$$\left(\frac{\nu_{001 \rightarrow 000}}{\nu} \right)^3 \frac{A_{(\nu_1, \nu_2, \nu_3) \rightarrow (\nu_1+2, \nu_2, \nu_3-3)}}{A_{001 \rightarrow 000}} \quad (5)$$

is presented in Table 3 along with the transition frequencies. These values are compared with Table 2 intensities in Figure 2. The important thing to note is the borrowing of intensity by the new sequence from the "allowed" $\Delta v_3 = -1$ progression, especially at high v . This is a general, qualitative feature of mechanically anharmonic systems.

Table 3. ($\Delta v_3 = -3, \Delta v_2 = 2$) Transitions

Transition	(Matrix Element) $\times 2$	$\nu(\text{cm}^{-1})$
003 \rightarrow 200	0.120	844.7
013 \rightarrow 210	0.100	812.9
103 \rightarrow 300	0.144	735.6
004 \rightarrow 201	0.476	814.7
014 \rightarrow 211	0.417	788.2
104 \rightarrow 301	0.467	681.7
005 \rightarrow 202	0.865	776.5

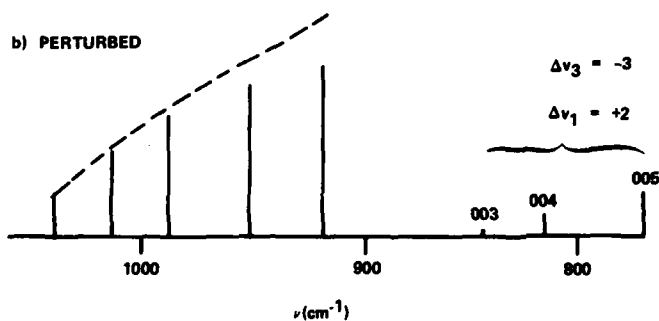
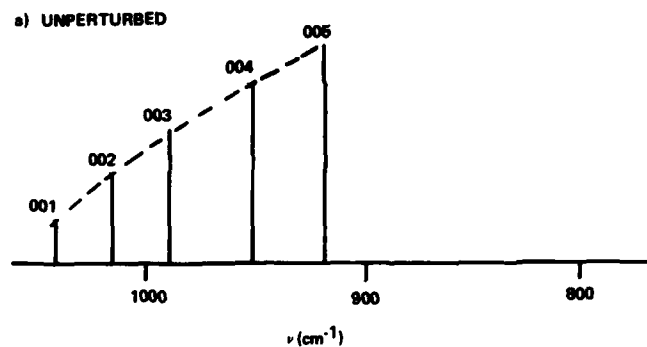


Figure 2. Relative Vibrational Intensities for Emitting Levels Using (a) Unperturbed Harmonic Oscillator and (b) Harmonic Oscillator Perturbed by Darling-Dennison Resonance

The important effect of electrical anharmonicity has not been included in the foregoing discussion. By analogy with diatomic molecules, it is expected that this will lead to a further decline in the value of the $\Delta v_3 = -1$ Einstein coefficient at high v . Consequently, the numerical values in Table 2 computed for the electrically harmonic case should be treated as a first approximation. In a qualitative sense, however, it does predict the general behavior of decreasing intensity with v relative to the simple scaling given in Eq. (4).

4. ULTRAVIOLET INVESTIGATIONS OF OZONE

It may at first appear that the conditions of high pressure used in the UV studies preclude their direct application to the study of the recombination in the upper atmosphere. The actual case is quite the contrary, however. Since the high pressure experiments provide accurately measured concentrations of O_2 , O and O_3 , fundamental rate coefficients for vibrational quenching may be extracted. Furthermore, the UV absorption spectra, unlike the IR emission spectra, show the population of the ground vibrational level as well as excited states. Finally, higher pressures can be actually more conducive, under some conditions to the observation of the nascent vibrational distribution. This is because in an initially pure oxygen experiment, ozone is formed in a three-body reaction whose rate is proportional to $[O_2]^2$ whereas the excited ozone is collisionally relaxed in a two-body interaction proportional to $[O_2]$.

We present here a preliminary analysis of the Hartley UV absorption spectrum based on a Franck-Condon synthesis. Both ab initio calculations and experimental data are used for verification of the results. Spectra of both ground and vibrationally excited levels are displayed, and a very simple application of the results to recombination data is also discussed. A full presentation of computational details will await further refinements.

Since only low v levels of the ground state are considered here, the shapes of the upper (1B_2) and lower (1A_1) potential surfaces in only a small localized Franck-Condon region control the UV spectrum. Quadratic approximation to the local surfaces has therefore been used. The relative activities of the three normal modes, q_1 , q_2 , and q_3 , can be estimated from ab initio calculations,⁹ absorption spectra¹⁰ and resonance Raman spectra.¹¹ The Raman data indicate that the bending mode, q_2 , is essentially inactive.¹¹ A similar conclusion was reached by considering the absorption spectrum.⁵ Accordingly, potential terms in q_2 may be removed, resulting in the following 2-dimensional, separable expressions for the local surfaces:

(Due to the length of References 9, 10 and 11, they will not be listed here. See References, page 21.)

$$V(^1B_2) = \frac{k_1'}{2} (q_1 - \delta)^2 + \frac{k_3'}{2} q_3^2 \quad (6)$$

$$V(^1A_1) = \frac{k_1''}{2} q_1^2 + \frac{k_3''}{2} q_3^2 \quad (7)$$

where q_1 and q_3 are symmetric and asymmetric stretch normal coordinates, respectively; k_1'' and k_3'' are the known force constants for the ground state; k_3' is known from the ab initio calculations⁹ and from the resonance Raman spectrum,¹¹ $k_3' \sim -3 k_3''$. The main determinants of the shape of the ground state spectrum are k_1' and δ . They can be adjusted for a best fit. In this preliminary work, $k_1' = 1.21 k_1''$, and $\delta = 2.507$ in dimensionless units. Franck-Condon factors resulting from Eqs. (6) and (7) may be readily evaluated by a convolution of 1-dimensional overlap integrals. The latter were evaluated for the (harmonic) q_1 coordinate, and numerically for the q_3 coordinate via integration of the Schrödinger equation to obtain q_3 wavefunctions. The model embodied in Eqs. (6) and (7) has also been discussed previously in connection with dissociation of triatomic molecules.^{12, 13} Although the surfaces given in Eqs. (6) and (7) using the parameter values specified are not ideal, the match between the observed and calculated ground state spectrum, ϵ_{000} (Figure 3) is still very good. Absorption spectra of the $1\nu_1$ and $1\nu_3$ levels are presented in Figure 4. The spectrum of $1\nu_2$ is assumed to be the same as the ground state spectrum.

It has been found experimentally that the $1\nu_1$ and $1\nu_3$ level populations equilibrate rapidly, reaching a population mixture determined by the bath translational temperature.^{4, 5, 14} The spectrum of this mixture ϵ^* , is therefore the experimentally relevant quantity characterizing the singly excited stretching modes. This point has been discussed more fully in connection with IR laser excitation experiments.⁵ In those experiments the determination of ϵ^* was hampered by inadequate knowledge of the amount of vibrationally excited ozone produced by the IR laser. However, a quantity proportional to $(\epsilon_{000} - \epsilon^*)$ was measured. Given a calculated ϵ^* spectrum, an experimentally determined ϵ^* spectrum can be matched to it by adjusting the constant of proportionality. In Figure 5, the laser data,⁵ adjusted as described, is compared to the current calculation of the room temperature ϵ^* . The agreement is very good, and within the experimental error of the measurements.

12. Pack, R. T. (1976) Simple Theory of Diffuse Vibrational Structure in Continuous UV Spectra of Polyatomic Molecules. 1. Collinear photodissociation of symmetric diatomics, *J. Chem. Phys.* **65**:4765.
13. Heller, E. J. (1978) Photofragmentation of symmetric triatomic molecules; Time dependent picture, *J. Chem. Phys.* **68**:3891.
14. Rosen, D. I., and Cool, T. A. (1975) Vibrational Deactivation of O₃ Molecules in Gas Mixtures, II, *J. Chem. Phys.* **62**:466.

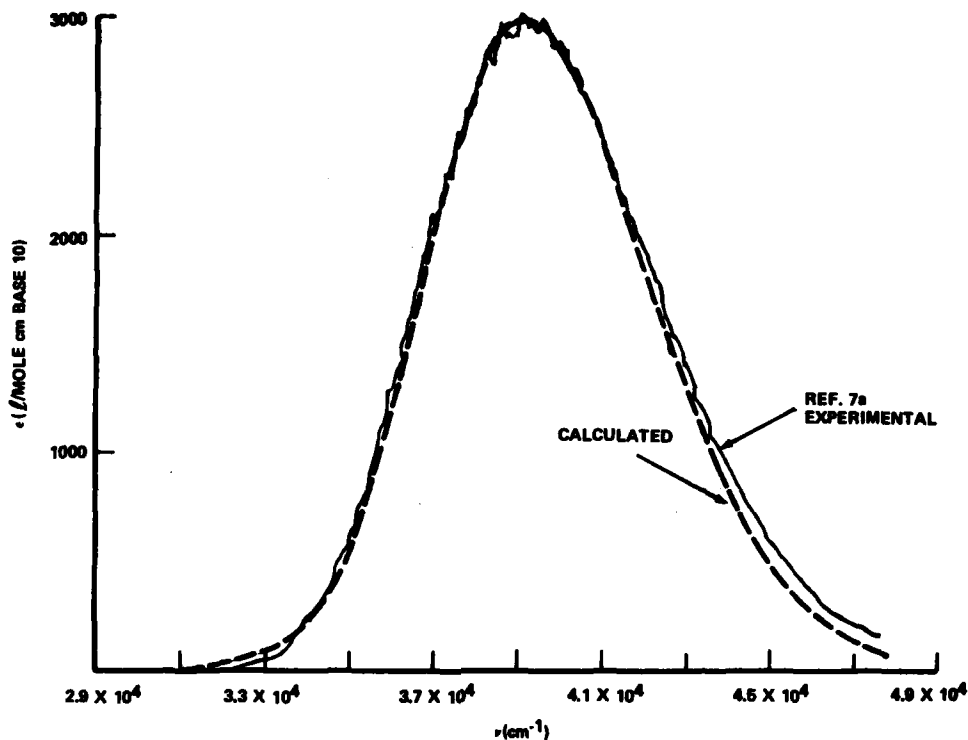


Figure 3. Ultraviolet Absorption Spectrum of Ground State Ozone

Analogous to the singly excited stretch spectrum, ϵ^* , is the doubly excited stretch spectrum, ϵ^{**} ; ϵ^{**} is broader and redder than ϵ^* , and essentially unstructured. It thus appears that ϵ_{000} , ϵ^* and ϵ^{**} are sufficiently distinctive in shape that the corresponding vibrational populations can be extracted accurately from the Reference 4 spectra.

Bair and co-workers^{4b, 4d} have demonstrated that the use of calculated UV spectra (similar to those in Figure 4) in modeling the observed ozone spectrum enables the extraction of vibrational level populations and relaxation rates during the recombination reaction. An improved analysis of Reference 4 data based on Franck-Condon calculations will be the subject of future work. Further refinements of the current Franck-Condon calculations are in progress; they are expected to yield more reliable spectra.

The type of information that a full UV analysis can yield may be demonstrated by the following simpler approach based on rough spectral shapes.^{4a, 15} Given a

15. Adler-Golden, S. M. (1982) Sum rules for molecular electronic spectra: Application to exact and reflection principle solutions, Chem. Phys. 64:421.

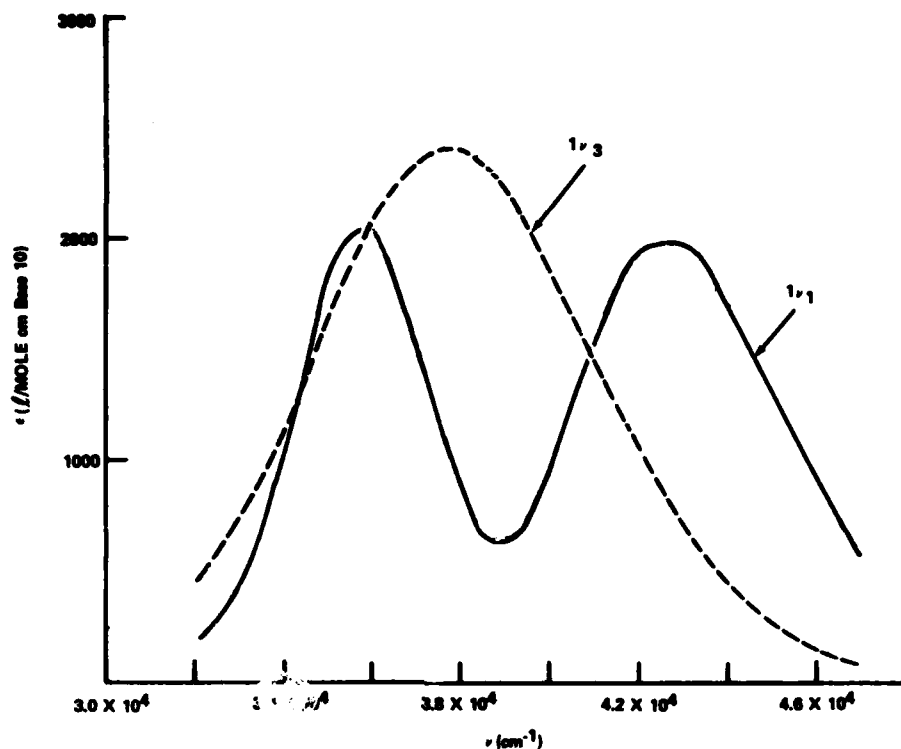


Figure 4. Calculated Ultraviolet Absorption Spectrum of Vibrationally Excited Ozone, $1\nu_1$ and $1\nu_3$

pair of potential surfaces, such as those specified by Eqs. (5) and (6), exact analytical expressions for the mean frequency $\overline{h\nu}$ and mean square frequency $\overline{(h\nu)^2}$ as a function of vibrational energy may be derived.¹⁵ These quantities are defined by

$$\overline{h\nu} = \frac{\int I(\nu)/\nu (h\nu) d\nu}{\int I(\nu)/\nu d\nu} \quad (8)$$

$$\overline{(h\nu)^2} = \frac{\int I(\nu)/\nu (h\nu)^2 d\nu}{\int I(\nu)/\nu d\nu} \quad (9)$$

where $I(\nu)$ is the absorption coefficient. The spectral variance σ^2 is given by

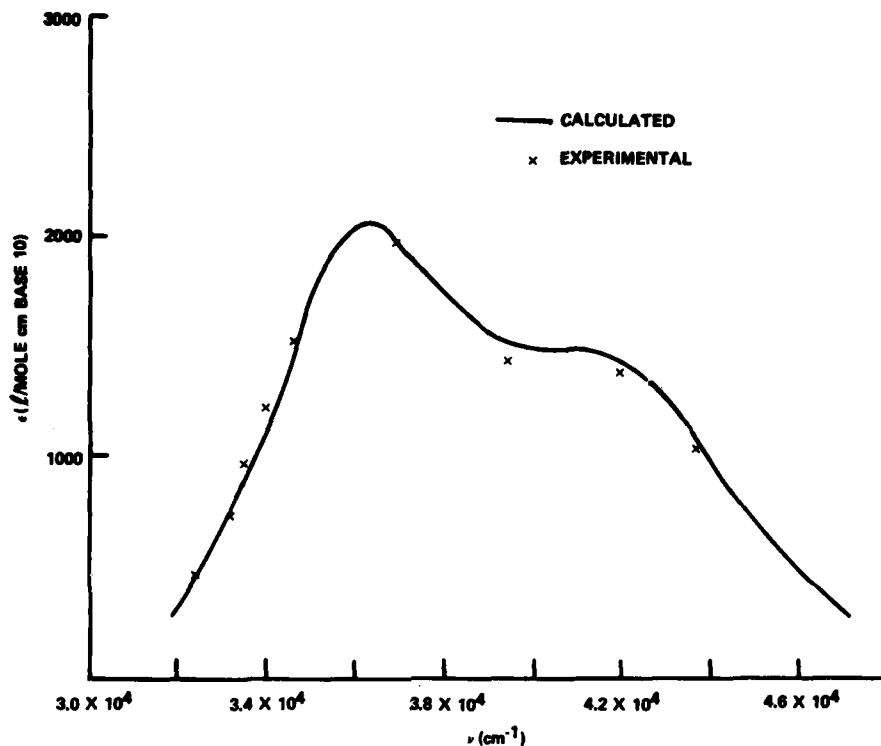


Figure 5. Ultraviolet Absorption Spectrum of Vibrationally Excited Ozone, ϵ^*

$$\sigma^2 = \overline{(h\nu)^2} - (\overline{h\nu})^2 . \quad (10)$$

The spectral "width" is defined by the square root of the variance. The spectral position and shape may be characterized by the quantities $\overline{h\nu}$ and σ^2 .

With use of Eqs. (6) and (7) for the potential surfaces, the following conclusions may be drawn:

1. The ozone UV absorption spectrum exhibits a red shift in proportion to the quantity of energy in the ν_3 mode, (E_3).
2. The spectrum exhibits an increase in variance proportional mainly to the quantity of energy in the ν_1 mode (E_1).
3. The spectrum is unaffected by the energy in the ν_2 mode.

The behavior described in the foregoing is seen in the Figure 4 calculated spectra, and is also consistent with available experimental data. Given reliable potential surfaces, the absolute quantities of energy present in the ν_1 and ν_3 modes may be deduced from an ozone recombination spectrum.

The amount of energy in ν_3 relative to ν_1 in nascent ozone is an important question arising from the COCHISE study,² and an issue that may be examined in the light of UV data. As explained previously, the relevant spectra are ϵ^* , ϵ^{**} , and so on, which are spectra of mixtures of levels having the same total number of stretching quanta. As collisional deactivation proceeds (following the initial ozone formation) the ratio $(E_3)/(E_1)$ should approach the value characteristic of the ϵ^* mixture. At earlier times, higher ν levels may be populated, in which case $\nu_3 \longleftrightarrow \nu_1$ equilibration yields higher $(E_3)/(E_1)$ values due to the details of the energy level spacings. Therefore, at short times after the ozone is formed, the quantity (red shift)/(change in σ^2), which is proportional to $(E_3)/(E_1)$, may be considerably higher than at longer times.

In Figure 6 the data of Reference 4a has been treated by the preceding method. The large value of $(E_3)/(E_1)$ at short times indeed suggests that most of the vibrational excitation is initially distributed in ν_3 , consistent with the expected population of high ν levels. However, after $\sim 50 \mu\text{sec}$ the vibrational manifold is sufficiently relaxed so that most of the stretching mode excitation is in singly excited levels.

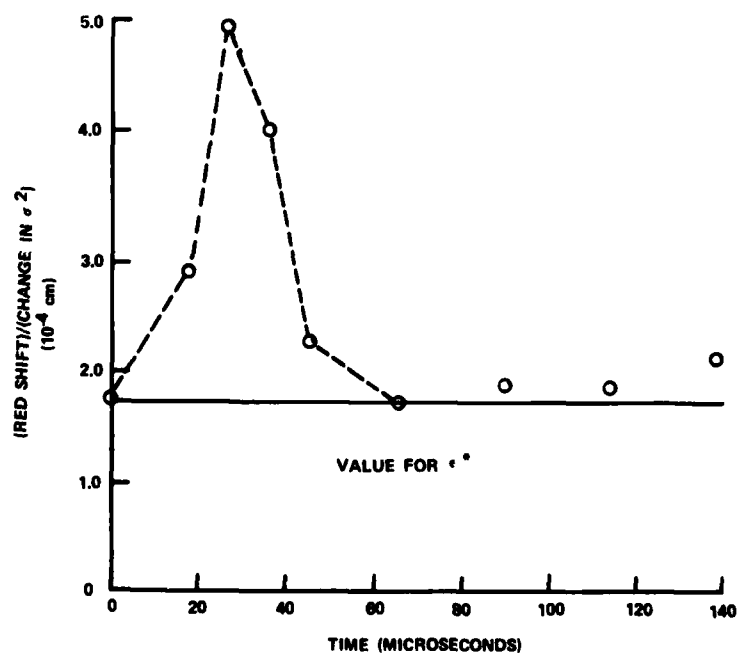


Figure 6. (Red Shift)/(Change in σ^2) vs Time After Photolysis of a 0.02 Torr O_3 /115 Torr O_2 Mixture

The present preliminary study suggests that a detailed analysis of UV data on the ozone recombination will yield the following information:

1. An estimate for the absolute amount of energy $(E_1) + (E_3)$ deposited in nascent ozone.
2. A rate constant for quenching of vibrational energy $(E_1) + (E_3)$ by molecular oxygen.
3. The temporal dependence of the populations in levels $1\nu_1$, $1\nu_3$, $2\nu_1$, $2\nu_3$, $1\nu_1 + 1\nu_3$, and the ground state, for the experimental conditions of Reference 4. Appropriate scaling to lower pressures for atmospheric applications should be possible.

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