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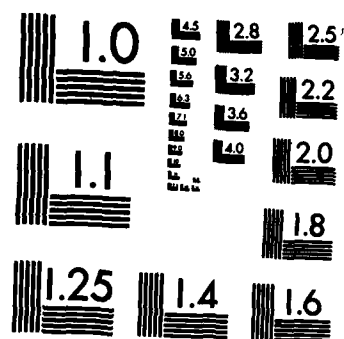
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THEORY OF GYROTRON AMPLIFIER IN A TAPE HELIX LOADED WAVEGUIDE

BY HAN S. UHM,
JOON Y. CHOE

RESEARCH AND TECHNOLOGY DEPARTMENT

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FOREWORD

Stability properties of the cyclotron maser instability in an annular electron beam propagating through a cylindrical waveguide loaded with a tape helix are investigated, in connection with applications on the gyrotron amplifier. Closed form of the dispersion relation for the cyclotron maser instability is obtained, including influence of the tape helix in stability behavior. It is shown that the bandwidth of the gyrotron amplifier for a tape helix is narrow in comparison with results for a sheath helix. However, the growth rate of the tape helix gyrotron is comparable to that of the sheath helix gyrotron.

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I. INTRODUCTION

In recent years, stability properties of the electron cyclotron maser instability¹⁻⁴ have been investigated in a great detail, in connection with applications on the gyrotron amplifiers. Particularly, motivated by a wide bandwidth microwave amplification, properties of the gyrotron amplifier in a sheath helix loaded waveguide have been also investigated in a previous study.⁵ Although a theoretical analysis in a sheath helix loaded waveguide is a reasonable simplifying assumption in many experiments, we expect a significant modification of the stability behavior when the sheath helix is replaced by a more practical tape helix. In this regard, this paper examines properties of the cyclotron maser instability in a hollow electron beam propagating through a tape helix loaded waveguide.

This paper extends the previous theory of the cyclotron maser instability, developed by the authors for a sheath helix loaded waveguide, to a tape helix loaded waveguide. The analysis is carried out within the framework of the Vlasov-Maxwell equations for an infinitely long hollow electron beam with radius R_0 , propagating parallel to a uniform magnetic field $B_0 \hat{e}_z$ with axial velocity $\beta_z c \hat{e}_z$. The radii of the helix and the grounded conducting wall are denoted by R_h and R_c , respectively. Equilibrium and stability properties are calculated for the electron distribution function [Equation (3)] in which all electrons have the same energy and the same canonical angular momentum but a Lorentzian distribution in the axial canonical momentum. We assume that the hollow beam is thin and very tenuous. The formal dispersion relation [Equation (31)] of the cyclotron maser instability is obtained in Section IV, including the important influence of the presence of a tape helix.

In Section IV, properties of the vacuum waveguide mode loaded with a tape helix are briefly investigated without including the influence of beam electrons. Stability properties of the cyclotron maser instability are numerically investigated in Section IV, in connection with application on the gyrotron amplifier. It is shown that the bandwidth of the tape helix gyrotron amplifier for a helix mode is narrow in comparison with results of the sheath helix gyrotron amplifier. However, the growth rate of the tape helix gyrotron is comparable to that of the sheath helix gyrotron. In addition, the growth rate and bandwidth of the gyrotron amplifier for tape helix are relatively less effected by the axial momentum spread than those for sheath helix.

II. LINEARIZED VLASOV-MAXWELL EQUATIONS FOR PERTURBATION

The equilibrium configuration consists of a relativistic annular electron beam propagating parallel to a strong, externally applied magnetic field $B_0 \hat{e}_z$. The mean radius of the electron beam is denoted by R_0 , and a grounded cylindrical conducting wall is located at radius $r = R_c$. Cylindrical polar coordinates (r, θ, z) are introduced in the analysis. A helix tape with width δ and zero thickness is located between the electron beam and conducting wall. The radius and pitch of the helix are denoted by R_h and L , respectively, thereby defining the pitch angle ϕ and the unit helix vector $\hat{e}_\phi$ by

$$\cot \phi = 2\pi R_h / L \quad (1)$$

and

$$\hat{e}_\phi = \cos \phi \hat{e}_\theta + \sin \phi \hat{e}_z \quad (2)$$

where $\hat{e}_\theta$ and $\hat{e}_z$ are unit vectors on the azimuthal and axial directions. Obviously, it is assumed $R_0 < R_h < R_c$.

In the analysis, we also assume that $v/\gamma \ll 1$, where $v = N_b e^2 / mc^2$ is Budker's parameter and γmc^2 is the electron energy. Here N_b is the total number of electrons per unit axial length, $-e$ and m are the charge and rest mass of electrons, respectively. Moreover, it is further assumed that the electron beam is thin, i.e., $(R_2 - R_1) \ll R_0$, where R_1 and R_2 are the inner

and outer radii, respectively, of the annular electron beam. In the present analysis, we investigate stability properties for the choice of equilibrium distribution function

$$f_b^0(H, P_\theta, P_z) = \frac{\hat{\omega}_c N_b \hat{p}_z \Delta}{4\pi^3 \gamma m c^2} \frac{\delta(\gamma - \hat{\gamma}) \delta(P_\theta - P_0)}{(\hat{p}_z - \hat{p}_z)^2 + \hat{p}_z^2 \Delta^2}, \quad (3)$$

Where $H = \gamma m c^2 = (m^2 c^4 + c^2 p^2)^{1/2}$ is the total energy, P_z is the axial momentum, $P_\theta = r \left[p_\theta - (e/2c) r B_0 \right]$ is the canonical angular momentum, $\hat{\omega}_c = e B_0 / m c$ is the non-relativistic electron cyclotron frequency, $P_0 = -(e/2c) (R_0^2 - r_L^2) B_0$ is the canonical angular momentum of an electron with Larmor radius $r_L = \left[(\gamma^2 - 1) c^2 / \hat{\omega}_c^2 - (\hat{p}_z / m \hat{\omega}_c)^2 \right]^{1/2}$, and $\hat{\gamma}$, $\hat{p}_z$ and Δ are constants.

Making use of Floquet's theorem,^{6, 7} we adopt a normal mode approach in which all perturbations are assumed to vary according to

$$\psi(x, t) = \sum_{n=-\infty}^{\infty} \hat{\psi}_n(r) \exp\{i(n\theta + k_n z - \omega t)\} \quad (4)$$

where

$$k_n = k - 2\pi(n-l)/L \quad (5)$$

is the axial wavenumber of the component n , ω and k are the oscillation frequency and the axial wavenumber, respectively, and l represents the primary azimuthal mode number. For example, for small k value, the electromagnetic field for $n = l$ azimuthal harmonic perturbation is dominant.⁶

In the present purposes, it is assumed that

$$|\omega - \hat{\omega}_c / \hat{\gamma} - (k + 2\pi s/L) \beta_z c| \ll \hat{\omega}_c / \hat{\gamma}, 2\pi \beta_z c/L \quad (6)$$

where $\beta_z = \hat{p}_z / \hat{\gamma} m c$, c is the speed of light in vacuo, and s is the space harmonic number. The Maxwell equations for the perturbed electric and magnetic field amplitudes can be expressed as

$$\begin{aligned} \nabla \times \hat{\underline{E}}(\underline{x}) &= i(\omega/c) \hat{\underline{B}}(\underline{x}) \\ \nabla \times \hat{\underline{B}}(\underline{x}) &= (4\pi/c) \hat{\underline{J}}(\underline{x}) - i(\omega/c) \hat{\underline{E}}(\underline{x}), \end{aligned} \quad (7)$$

where $\hat{\underline{E}}(\underline{x})$ and $\hat{\underline{B}}(\underline{x})$ are the perturbed electric and magnetic fields and $\hat{\underline{J}}(\underline{x})$ is the perturbed current density.

Within the content of a thin beam approximation and Eq. (6), the transverse components of the perturbed current density in Eq. (4) is expressed as⁵

$$\begin{aligned} \hat{J}_\theta(\underline{x}) &= i\hat{J}_r(\underline{x}) = \frac{c}{4\pi} \exp\{i(\alpha\theta + k_\alpha z)\} \\ &\times \left[\hat{E}_{\theta\alpha}(R_0) + i \hat{E}_{r\alpha}(R_0) \right] \chi(\omega, k) \delta(r - R_0) \end{aligned} \quad (8)$$

where the effective susceptibility $\chi(\omega, k)$ is defined by

$$\chi(\omega, k) = -i \frac{v\beta_z^2 c}{2\gamma\omega R_0} \frac{\omega^2 - k_\alpha^2 c^2}{(\Omega + i|k_\alpha| \beta_z c \hat{\gamma}_\Delta / \gamma_z^3)^2}, \quad (9)$$

$$\Omega = \omega - k_{\alpha} \beta_z c - \hat{\omega}_c / \gamma \quad (10)$$

is the Doppler-shifted eigenfrequency, $\beta_1 = p_1 / \gamma mc$, $\beta_z = \hat{p}_z / \gamma mc = (\gamma_z^2 - 1)^{1/2} / \gamma_z$,

$\nu = N_b e^2 / mc^2$ is the Budker's parameter and the integer α is defined by

$$\alpha = l - s. \quad (11)$$

As noted from Eq. (8), we emphasize that consistent with Eq. (6), the transverse current density is mainly originated from perturbations with $n = \alpha$ since the corrections associated with other perturbations with $n \neq \alpha$ are order $\Omega L / 2\pi \beta_z c$ ($\ll 1$) or smaller.⁵ Moreover, we can also approximate the perturbed charge and the axial component of the perturbed current density by

$$\hat{\rho}(r) = \hat{J}_z(r) = 0.$$

In this regard, from the Maxwell equation (7), we obtain

$$\left\{ \frac{1}{r} \frac{\partial}{\partial r} r \frac{\partial}{\partial r} - \frac{n^2}{r^2} + \frac{\omega^2}{c^2} - k_n^2 \right\} \hat{E}_{zn}(r) = 0 \quad (12)$$

for the axial component of the electric field with arbitrary n . Similarly, for the axial component of the magnetic field, the Maxwell equation (7) is expressed as

$$\left\{ \frac{1}{r} \frac{\partial}{\partial r} r \frac{\partial}{\partial r} - \frac{n^2}{r^2} + \frac{\omega^2}{c^2} - k_n^2 \right\} \hat{B}_{zn}(r) = 0 \quad (13)$$

for $n \neq \alpha$ and

$$\left\{ \frac{1}{r} \frac{\partial}{\partial r} r \frac{\partial}{\partial r} - \frac{\alpha^2}{r^2} + \frac{\omega^2}{c^2} - k_\alpha^2 \right\} \hat{B}_{z\alpha}(r) = - \frac{4\pi}{c} \left\{ \frac{1}{r} \frac{\partial}{\partial r} [r \hat{J}_{\theta\alpha}(r)] - i \frac{\alpha}{r} \hat{J}_{r\alpha}(r) \right\}, \quad (14)$$

where the r - and θ - components of the perturbed current density $\hat{J}_{r\alpha}(r)$ and $\hat{J}_{\theta\alpha}(r)$ are defined in Eq. (8)

The physically acceptable solution to Eq. (12) is

$$\hat{E}_{zn}(r) = a_n \begin{cases} J_n(p_n r), & 0 \leq r \leq R_h, \\ J_n(\eta_n) \frac{N_n(\zeta_n) J_n(p_n r) - J_n(\zeta_n) N_n(p_n r)}{J_n(\eta_n) N_n(\zeta_n) - J_n(\zeta_n) N_n(\eta_n)}, & R_h \leq r \leq R_c, \end{cases} \quad (15)$$

for all n . However, for the axial component of the magnetic field, we have

$$\hat{B}_{zn}(r) = \begin{cases} b_\alpha \left[J_\alpha(p_\alpha r) + g(\omega, k) N_\alpha(p_\alpha r) \right], & n = \alpha, \\ b_n J_n(p_n r), & n \neq \alpha, \end{cases} \quad (16)$$

for $R_0 < r < R_h$, and

$$\hat{B}_{zn}(r) = b_n J_n'(\eta_n) \frac{N_n'(\zeta_n) J_n(p_n r) - J_n'(\zeta_n) N_n(p_n r)}{J_n'(\eta_n) N_n'(\zeta_n) - J_n'(\zeta_n) N_n'(\eta_n)}, \quad (17)$$

for $R_n < r \leq R_c$ and for all n . In Eqs. (15) - (17), a_n and b_n are constants. $J_n(x)$ and $N_n(x)$ are the Bessel functions of the first and second kinds, respectively, of order n , the prime (') denotes $(d/dx) J_n(x)$ and $(d/dx) N_n(x)$, and the parameters η_n , ζ_n and p_n are defined by

$$\eta_n^2 = \zeta_n^2 R_h^2 / R_c^2 = p_n^2 R_h^2 = (\omega^2 / c^2 - k_n^2) R_h^2. \quad (18)$$

The boundary conditions of the magnetic field at $r=R_h$ for the tape helix are^{6, 7}

$$\hat{B}_z^i - \hat{B}_z^o = \frac{4\pi}{c} \hat{J}_{\parallel} \cos\phi, \quad (19)$$

$$\hat{B}_{\theta}^o - \hat{B}_{\theta}^i = \frac{4\pi}{c} \hat{J}_{\parallel} \sin\phi,$$

where the superscript i and o represent the magnetic field components at just inside and just outside, respectively, of the helix tape, $\hat{J}_{\parallel}$ is the surface current density along the helix direction with the unit vector $\hat{e}_{\phi}$. Assuming that the current in the tape flows only in the tape direction, and that it does not vary in phase or amplitude over the width of the tape, the surface current

density $\hat{J}_{\parallel}$ is reasonably expressed as^{6, 7}

$$\hat{J}_{\parallel} = \sum_n j_{\parallel n} \exp\{i(n\theta + k_n z)\} \quad (20)$$

where the component amplitude $j_{\parallel n}$

$$j_{\parallel n} = \hat{J} \exp(-ik_n \delta/2) \frac{\sin(k_n \delta/2)}{k_n \delta/2} \quad (21)$$

and δ is the width of the helix tape. Substituting Eqs. (15) - (17) and (20) into Eq. (19), it is straightforward to show that

$$a_n = -i \frac{p_n}{\omega} 2\pi^2 j_{\parallel n} \eta_n \cos\phi \left(\tan\phi - \frac{k_n}{\eta_n p_n} \right) \times \frac{J_n(\zeta_n) N_n(\eta_n) - J_n(\eta_n) N_n(\zeta_n)}{J_n(\zeta_n)} \quad (22)$$

and

$$b_n = \frac{2\pi^2}{c} j_{\parallel n} \cos\phi \eta_n \left[J'_n(\zeta_n) N'_n(\eta_n) - J'_n(\eta_n) N'_n(\zeta_n) \right] \times \begin{cases} \left[J'_\alpha(\zeta_\alpha) + g N'_\alpha(\zeta_\alpha) \right]^{-1}, & n = \alpha, \\ \left[J'_n(\zeta_n) \right]^{-1}, & n \neq \alpha. \end{cases} \quad (23)$$

At the helix surface, the electric field along the helix direction is given by

$$\hat{E}_{\parallel}(\underline{x}) = \sum_n \exp\{i(n\theta + k_n z)\} \left[\hat{E}_{\theta n}(R_h) \cos\phi + \hat{E}_{zn}(R_h) \sin\phi \right]. \quad (24)$$

Making use of the Maxwell equation (7), and Eqs. (15) and (16), we can show that Eq. (24) is expressed as

$$\hat{E}_{\parallel}(\underline{x}) = \cos\phi \sum_n \exp\{i(n\theta + k_n z)\} \times \left\{ a_n J_n(\eta_n) \left(\tan\phi - \frac{k_n}{\eta_n p_n} \right) - i \frac{\omega}{c p_n} b_n \left[J'_n(\eta_n) + g_n N'_n(\eta_n) \right] \right\}, \quad (25)$$

where $g_n = g$ for $n = \alpha$ and $g_n = 0$ otherwise. The coefficient function $g(\omega, k)$ in Eq. (25) can be expressed in terms of the helix and geometric parameters, assuming that the electric field in Eq. (25) is set equal to zero along the center line of the tape, i.e., at $z = (L\theta/2\pi) + (\delta/2)$. This assumption is a good approximation for narrow tapes. Substituting Eqs. (22) and (23) into Eq. (25), and carrying out a tedious but straightforward algebra, we obtain

$$g(\omega, k) = - \frac{J'_\alpha(\zeta_\alpha)}{N'_\alpha(\zeta_\alpha)} \frac{D(\omega, k)}{F(\omega, k)} \quad (26)$$

where the vacuum dispersion function $D(\omega, k)$ is defined by ⁷

$$D(\omega, k) = \sum_n \frac{\sin(k_n \delta/2)}{k_n \delta/2} \left\{ \eta_n^2 \left(\tan \phi - \frac{k_n}{\eta_n p_n} \right)^2 \frac{J_n(\eta_n)}{J_n(\zeta_n)} \right. \\ \times \left[J_n(\zeta_n) N_n(\eta_n) - J_n(\eta_n) N_n(\zeta_n) \right] \\ \left. + \frac{\omega^2 R_h^2}{c^2} \frac{J'_n(\eta_n)}{J'_n(\zeta_n)} \left[J'_n(\zeta_n) N'_n(\eta_n) - J'_n(\eta_n) N'_n(\zeta_n) \right] \right\} \quad (27)$$

and the function $F(\omega, k)$ is given by

$$F(\omega, k) = D(\omega, k) + \frac{\omega^2 R_h^2}{c^2} \frac{\sin(k_\alpha \delta/2)}{k_\alpha \delta/2} \\ \times \frac{\left[J'_\alpha(\zeta_\alpha) N'_\alpha(\eta_\alpha) - J'_\alpha(\eta_\alpha) N'_\alpha(\zeta_\alpha) \right]^2}{J'_\alpha(\zeta_\alpha) N'_\alpha(\zeta_\alpha)}, \quad (28)$$

where $k_n = k - 2\pi(n-\ell)/L$ defined in Eq. (5), and the parameters, η_n , ζ_n and p_n are given in Eq. (18).

Evidently from Eqs. (13) and (14), the axial component of the perturbed magnetic field is continuous across $r = R_0$ for all n except $n = \alpha$. For $n = \alpha$, the physically acceptable solution to Eq. (14) is given by

$$\hat{B}_{z\alpha}(r) = \begin{cases} b_{in} J_\alpha(p_\alpha r), & 0 \leq r < R_0, \\ b_\alpha [J_\alpha(p_\alpha r) + g N_\alpha(p_\alpha r)], & R_0 < r < R_h, \end{cases} \quad (29)$$

where b_{in} and b_a are constants. For convenience in the subsequent analysis, we introduce the normalized magnetic wave admittance $b_{\pm}$ defined at the inner and outer surfaces of the electron beam by

$$\begin{aligned} b_+ &= - \hat{B}_{za}(R_0^+) / [r(\partial/\partial r) \hat{B}_{za}]_{R_0^+} \\ b_- &= \hat{B}_{za}(R_0^+) / [r(\partial/\partial r) \hat{B}_{za}]_{R_0^-}. \end{aligned} \quad (30)$$

Making use of Eqs. (7), (8) and (30), we obtain the dispersion relation of the gyrotron amplifier in a tape helix waveguide

$$\Gamma(\omega, k) = - \frac{v \beta_1^2 c^2}{2 \gamma R_0^2 (\Omega + i |k_a| \beta_z c \gamma \Delta / \gamma_z^3)^2}, \quad (31)$$

where the admittance function $\Gamma(\omega, k)$ is defined by

$$\Gamma(\omega, k) = \frac{2g(\omega, k) / \pi \xi_{\alpha}^2 J_{\alpha-1}^2(\xi_{\alpha})}{1 + G(\omega, k)}, \quad (32)$$

$$G(\omega, k) = g \frac{N_{\alpha-1}(\xi_{\alpha})}{J_{\alpha-1}(\xi_{\alpha})} + \frac{k_a/p_{\alpha}}{\tan \phi - k_a/p_{\alpha} R_h^2} \frac{J'_{\alpha}(\eta_{\alpha}) + g N'_{\alpha}(\eta_{\alpha})}{J_{\alpha}(\eta_{\alpha})} \quad (33)$$

and the parameter ξ_{α} is defined by

$$\xi_{\alpha}^2 = \zeta_{\alpha}^2 R_0^2 / R_c^2 = (\omega^2 / c^2 - k_a^2) R_0^2 \quad (34)$$

The dispersion relation in Eq. (31), combined with Eqs. (32) and (33), is one of the main results of this paper and can be used to investigate gain and bandwidth of the gyrotron amplifier for a broad range of physical parameters.

III. VACUUM WAVEGUIDE MODES

Assuming no beam electrons ($v \rightarrow 0$) in this section, we obtain the vacuum dispersion relation

$$D(\omega, k) = 0 \quad (35)$$

from Eqs. (26), (31) and (32). In Eq. (35), the vacuum dispersion function $D(\omega, k)$ is defined in Eq. (27). Even though the dispersion relation is a very complicated transcendental function of ω and k , in the limiting case where the outer conducting wall is very close to the helix (i.e., $R_c/R_h \rightarrow 1$), the vacuum dispersion relation is simplified to three distinctive relations.⁷ These are the transverse electric like, the transverse magnetic like and the helix modes. Particularly, the helix mode is represented by a straight line

$$\omega = \pm [kc \sin\phi + l(c/R_c) \cos\phi] \quad (36)$$

in the (ω, k) parameter space. The characteristic electron beam mode in the gyrotron amplifier is given by

$$\omega = k\beta_z c + (2\pi s/L)\beta_z c + \hat{\omega}_c/\hat{\gamma} \quad (37)$$

from Eq. (6). In this regard, we conclude from Eqs. (36) and (37) that a super wideband microwave amplifier can be developed by a choice of beam parameters satisfying

$$\beta_z \simeq \sin\phi,$$

$$\hat{\omega}_c/\hat{\gamma} = (c/R_c) \cos\phi (l-s), \quad (38)$$

for $R_c/R_h \simeq 1$.

In general case where $R_c/R_h \neq 1$, the dispersion relation in Eq. (35) is numerically solved to find ω for specified k value. Shown in Fig. 1 is plots of the normalized oscillation frequency $\omega R_h/c \cos\phi$ versus the normalized axial wave number $kR_h \tan\phi$ for $\ell = 0$ helix mode, $\phi = \pi/6$, $\delta/L = 0.3$ and several values of the parameter R_c/R_h . It is noted from Fig. 1 that dispersion curves of the helix mode approach to the straight line defined by Eq. (36) as the parameter R_c/R_h is reduced to unity. Moreover, the helix mode dispersion curves wiggle more prominatly as the parameter R_c/R_h increases from unity to infinity. Obviously in the limit $R_c/R_h \rightarrow \infty$, every minimum points of ω in the dispersion curves are equal to zero. Detailed analytic and numerical investigation of the dispersion relation in Eq. (27) and (35) has been carried out in the previous literature⁷ by authers. For additional information of the vacuum dispersion properties, we urge the reader to review this literature.⁷

IV. CYCLOTRON MASER INSTABILITY

In this section, we investigate stability properties of the cyclotron maser instability in a hollow electron beam propagating through a tape helix loaded waveguide, by making use of the dispersion relation in Equation (31). The growth rate and bandwidth of the cyclotron maser instability are directly related to the gain and bandwidth of the tape helix gyrotron amplifier. Making use of the fact that the "Doppler-shifted" eigenfrequency in Equation (10) is well removed from the electron cyclotron resonance, i.e., $|\Omega| \ll \bar{\omega}_c/\bar{\gamma}$ and evaluating the wave admittance function $\Gamma(\omega, k)$ at $k = k_b = (\omega - \bar{\omega}_c/\bar{\gamma})/\beta_z c - 2\pi s/L$, the dispersion relation in Equation (31) can be approximated by

$$\left[\Gamma(\omega, k_b) - \frac{1}{\beta_z c} \left(\frac{\partial}{\partial k} \Gamma \right)_{k_b} \Omega \right] \left[\Omega + i \frac{|\omega - \bar{\omega}_c/\bar{\gamma}| \bar{\gamma} \Delta}{\gamma_z^3} \right]^2 = - \frac{\nu \beta_1^2 c^2}{2 \bar{\gamma} R_0^2} \quad (39)$$

In the remainder of this section, the growth rate $\Omega_i = -\text{Im}\Omega$ and the Doppler-shifted real oscillation frequency $\Omega_r = \text{Re}\Omega$ are numerically calculated from Equation (39) for the electron beam parameters $\nu = 0.002$, $\beta_1 = 0.4$ and $\bar{\gamma} = 1.118$ ($\beta_z = 0.2$). Obviously from Equation (10), the normalized gain $k_1 c/\bar{\omega}_c$ is expressed as

$$k_1 c/\bar{\omega}_c = -\Omega_i/\beta_z. \quad (40)$$

Shown in Figure 2 is plots of the normalized growth rate $k_1 c/\bar{\omega}_c$ versus $\omega/\bar{\omega}_c$ obtained from Equation (39) for the helix mode, $R_c/R_h = 1.1$, $R_0 = R_h - r_L$, $s = 0$,

$\delta/L = 0.3$, (a) $\Delta = 0.02$ and (b) $\Delta = 0.04$, and optimum values of the parameters $(R_h \bar{\omega}_c/c, \phi)$ for each azimuthal harmonic number ℓ . The optimum values of the parameter $(R_h \bar{\omega}_c/c, \phi)$ are given by $(1.06, 10.7^\circ)$ for $\ell = 1$, $(2.15, 11.4^\circ)$ for $\ell = 2$, $(3.2, 11^\circ)$ for $\ell = 3$ and $(4.2, 10^\circ)$ for $\ell = 4$. The bandwidth of the tape helix gyrotron amplifier for the helix mode in Figure 2 is narrow in comparison with results of the sheath helix gyrotron amplifier.⁵ However, the growth rate of the tape helix gyrotron for the helix mode is comparable to that of the sheath helix gyrotron. In addition, the growth rate and bandwidth in Figure 2 are relatively less effected by the axial momentum spread Δ than those of the sheath helix gyrotron.

In general, we can show⁵

$$\begin{aligned}\Gamma(\omega, k_b) &\approx 0, \\ [\partial \Gamma(\omega, k)/\partial k]_{k_b} &\approx 0,\end{aligned}\tag{41}$$

near the minimum oscillation frequency ω_0 in the hybrid vacuum waveguide mode and its corresponding wavenumber k_0 . Therefore, in order to correctly evaluate the gain of the gyrotron amplifier at $(\omega, k) = (\omega_0, k_0)$, we approximate Equation (31) by

$$\begin{aligned}\left[\Gamma(\omega, k_b) - \frac{1}{\beta_z c} \left(\frac{\partial}{\partial k} \Gamma \right)_{k_b} \Omega + \frac{1}{2\beta_z^2 c^2} \left(\frac{\partial^2}{\partial k^2} \Gamma \right)_{k_b} \Omega^2 \right] \\ \times \left[\Omega + i \frac{|\omega - \bar{\omega}_c/\bar{\gamma}| \bar{\gamma} \Delta}{\gamma_z^3} \right]^2 = - \frac{v \beta_{\perp}^2 c^2}{2\bar{\gamma} R_0^2}\end{aligned}\tag{42}$$

Of course, the dispersion relation in Equation (39) is used to obtain the gain for a broad range of physical parameters except near the point $(\omega, k) = (\omega_0, k_0)$ where use of Equation (42) is made to estimate the gain.

As a typical example of the gyrotron amplifier for the hybrid waves, which consist of the transverse electric and transverse magnetic modes, shown in Figure 3 are plots of the normalized gain $k_i c / \hat{\omega}_c$ versus $\omega / \hat{\omega}_c$ obtained from Equations (39) and (42) for $s = 0$, $R_c / R_h = 1.5$, $\delta / L = 0.3$, $\Delta = 0.04$, $R_0 = R_h - r_L$, $\phi = -30^\circ$ and $R_h \hat{\omega}_c / c = 1.86$ for $\ell = 0$, $R_h \hat{\omega}_c / c = 1.45$ for $\ell = 1$ and $R_h \hat{\omega}_c / c = 2.4$ for $\ell = 2$. The maximum gain in Figure 3 is considerably larger than that of the ordinary gyrotron amplifier. For example, the maximum growth rate for the $\ell = 1$ perturbation in Figure 3 is more than triple that of a smooth conducting waveguide without helix. As expected, the bandwidth of the tape helix gyrotron is narrower than that of the sheath helix gyrotron.⁵

In order to illustrate influence of the space harmonic number s on stability behavior, Figure 4 presents plots of the normalized growth rate versus $\omega / \hat{\omega}_c$ obtained from Equations (39) and (42) for $\ell = 2$, $R_c / R_h = 1.5$, $\delta / L = 0.3$, $\phi = -30^\circ$, and (a) $s = 1$ and corresponding optimum value $R_h \hat{\omega}_c / c = 2.15$, (b) $s = 0$ and $R_h \hat{\omega}_c / c = 2.4$ and (c) $s = -1$ and $R_h \hat{\omega}_c / c = 2.54$. As expected from the relation

$$\omega / \hat{\omega}_c = [1 + (c / R_h \hat{\omega}_c) \beta_z \gamma s \cot \phi] / \gamma, \quad (43)$$

the eigenfrequency corresponding to the maximum growth rate increases with decreasing value of the space harmonic number s for a negative pitch angle. However, the gain reduces drastically when the eigenfrequency of the maximum growth rate increases.

V. CONCLUSIONS

In this paper, we have examined the excitation of electromagnetic waveguide modes by the cyclotron maser instability in a hollow electron beam propagating through a waveguide loaded with a tape helix. Stability analysis was carried out within the framework of the linearized Vlasov-Maxwell equations, assuming that the electron beam is thin and tenuous. The formal dispersion relation of the cyclotron maser instability was obtained in Section II, including the important influence of the presence of a tape helix. Properties of the vacuum waveguide mode loaded with a tape helix were briefly investigated in Section III, without including the influence of beam electrons. Stability properties of the cyclotron maser instability were numerically investigated in Section IV, in connection with application on the gyrotron amplifier. It was shown that the bandwidth of the tape helix gyrotron amplifier for a helix mode is narrow in comparison with results of the sheath helix gyrotron amplifier. However, the growth rate of the tape helix gyrotron is comparable to that of the sheath helix gyrotron.

VI. ACKNOWLEDGEMENTS

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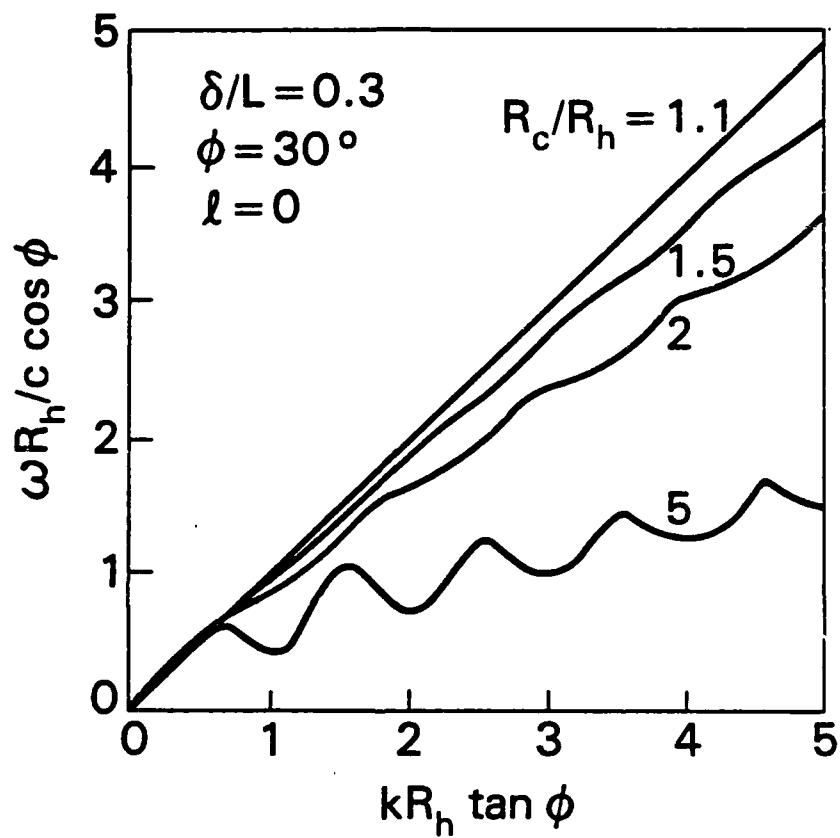


FIGURE 1. PLOTS OF THE NORMALIZED OSCILLATION FREQUENCY $\omega R_h / c \cos \phi$ VERSUS THE NORMALIZED AXIAL WAVE NUMBER $k R_h \tan \phi$ FOR $\ell = 0$ HELIX MODE, $\phi = \pi/6$, $\delta/L = 0.3$ AND SEVERAL VALUES OF THE PARAMETER R_c/R_h

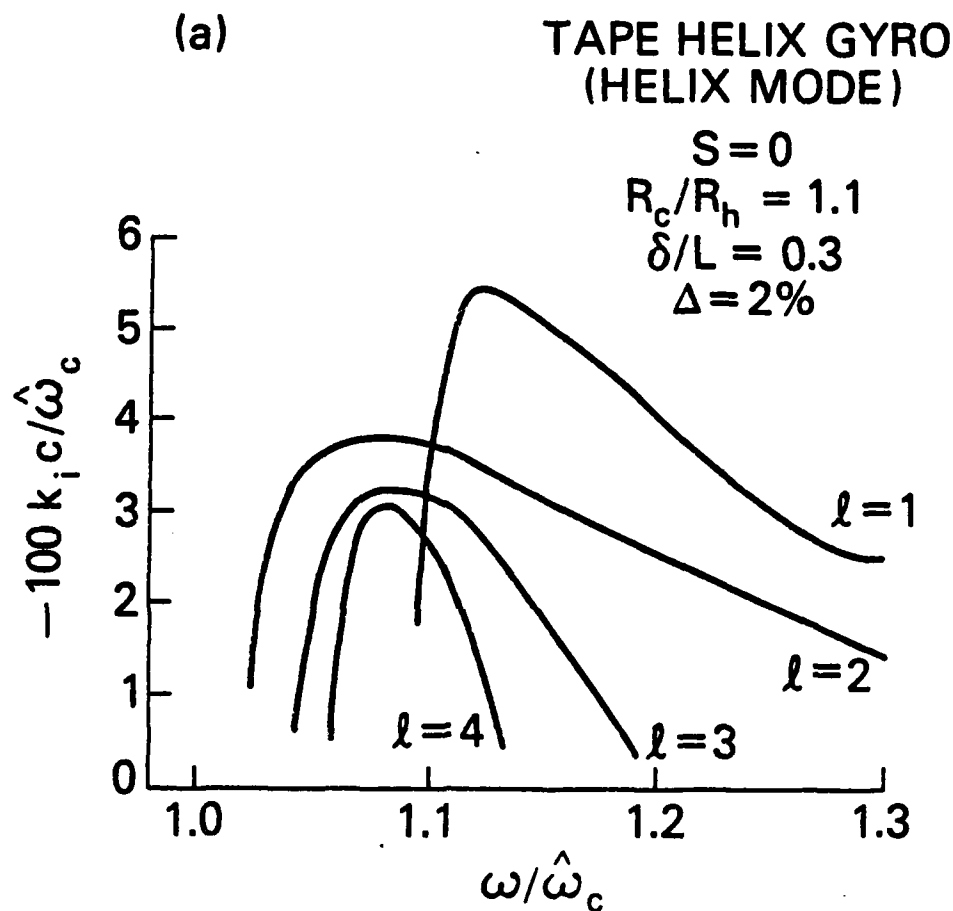


FIGURE 2. PLOTS OF THE NORMALIZED GROWTH RATE $k_i c / \hat{\omega}_c$ VERSUS $\omega / \hat{\omega}_c$ OBTAINED FROM EQUATION (39) FOR THE HELIX MODE, $R_c/R_h = 1.1$, $R_0 = R_h - r_L$, $s = 0$, $\delta/L = 0.3$, (a) $\Delta = 0.02$, (b) $\Delta = 0.04$, AND OPTIMUM VALUES OF THE PARAMETERS $(R_h \omega_c/c, \phi)$ GIVEN BY $(1.06, 10.7^\circ)$ FOR $l = 1$, $(2.15, 11.4^\circ)$ FOR $l = 2$, $(3.2, 11^\circ)$ FOR $l = 3$, AND $(4.2, 10^\circ)$ FOR $l = 4$

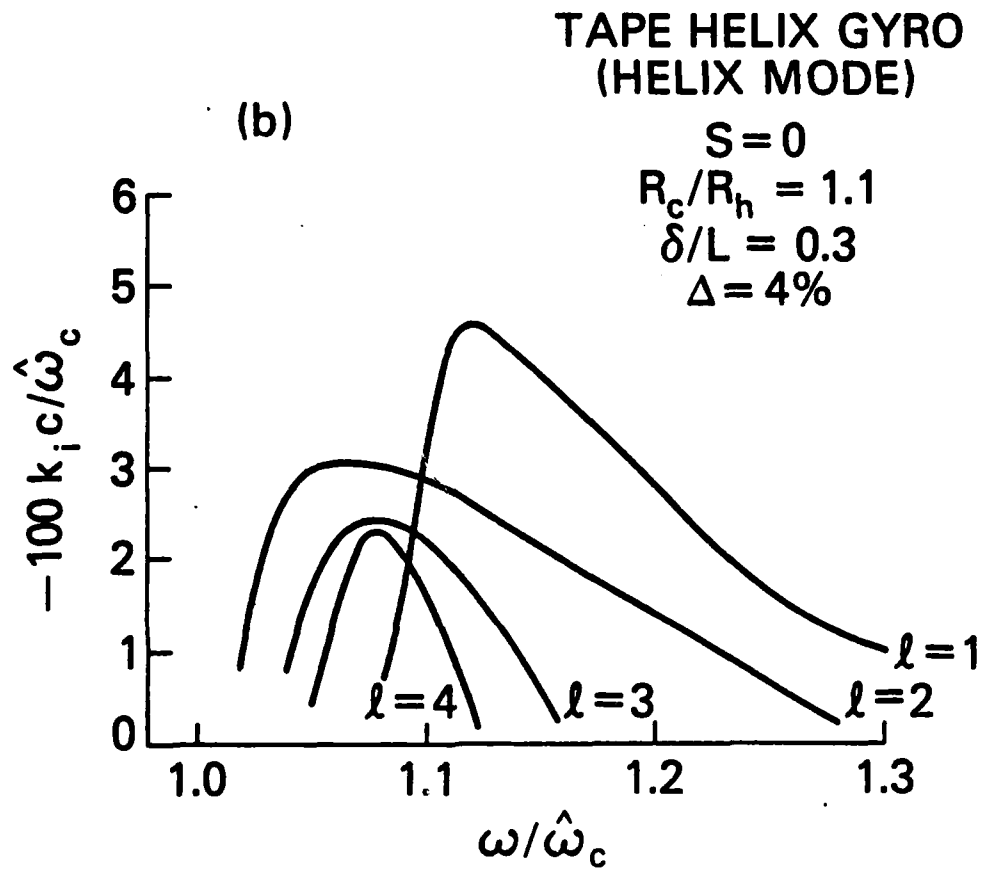


FIGURE 2 (CONTINUED)

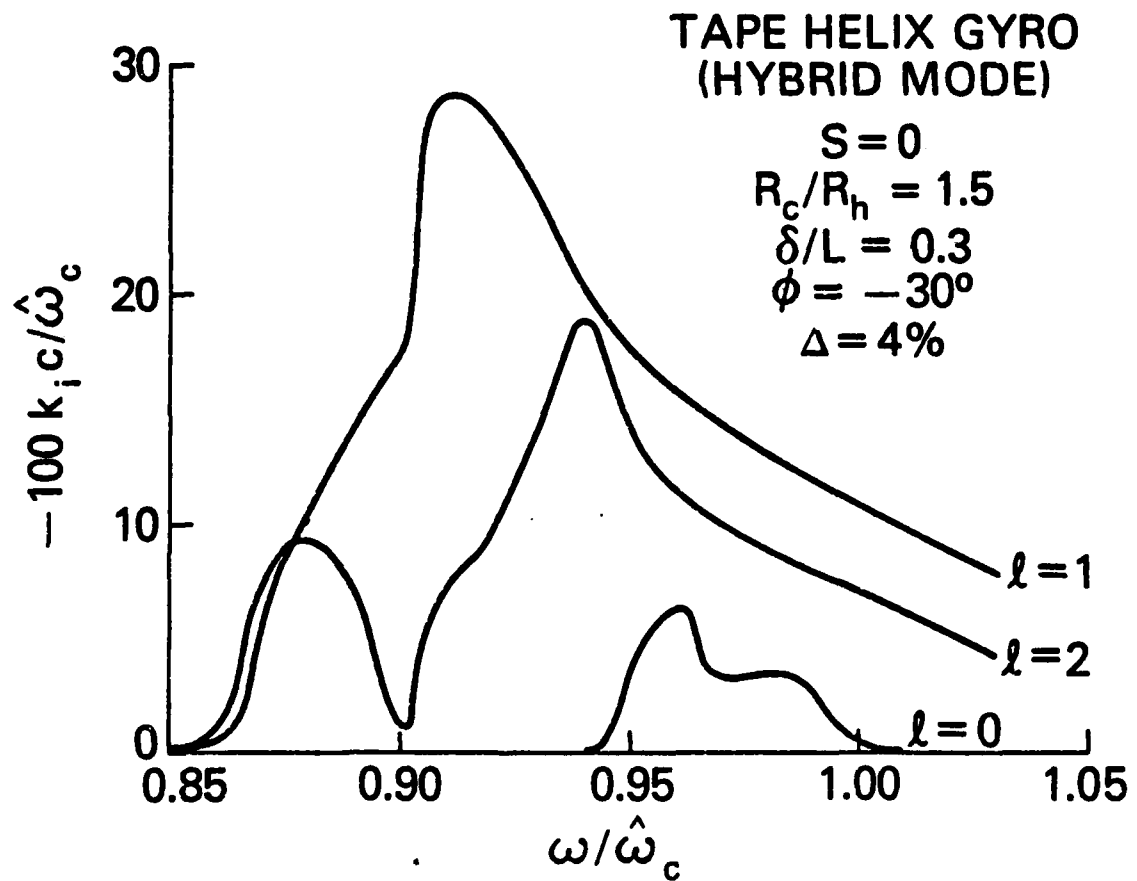


FIGURE 3. PLOTS OF THE NORMALIZED GAIN $k_i c / \hat{\omega}_c$ VERSUS $\omega / \hat{\omega}_c$ OBTAINED FROM EQUATIONS (39) AND (42) FOR $s = 0$, $R_c/R_h = 1.5$, $\delta/L = 0.3$, $\Delta = 0.04$, $R_0 = R_h - r_L$, $\phi = -30^\circ$ AND $R_h \hat{\omega}_c/c = 1.86$ FOR $l = 0$, $R_h \hat{\omega}_c/c = 1.47$ FOR $l = 1$, $R_h \hat{\omega}_c/c = 2.4$ FOR $l = 2$

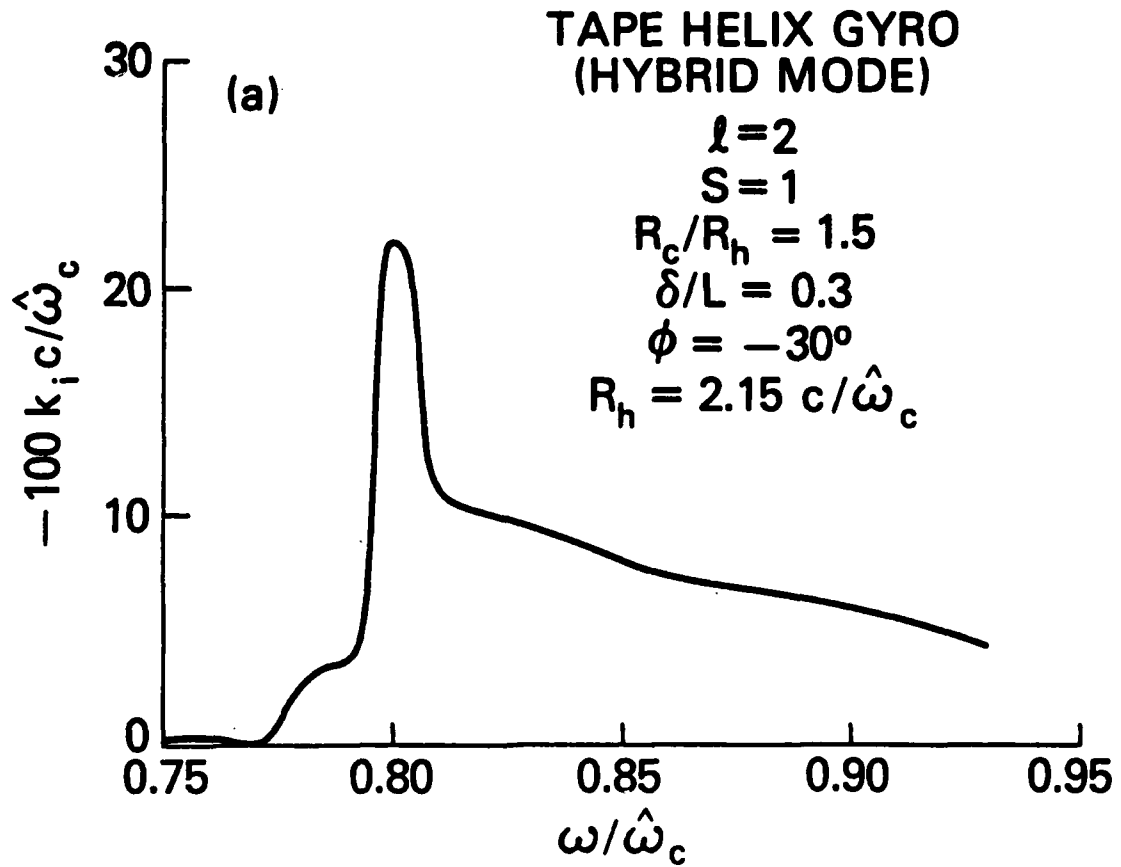


FIGURE 4. PLOTS OF THE NORMALIZED GROWTH RATE $k_i c / \hat{\omega}_c$ VERSUS $\omega / \hat{\omega}_c$ OBTAINED FROM EQUATIONS (39) AND (42) FOR $l=2$, $R_c/R_h = 1.5$, $\delta/L = 0.3$, $\phi = -30^\circ$, AND (a) $R_h \hat{\omega}_c / c = 2.15$ FOR $s=1$, (b) $R_h \hat{\omega}_c / c = 2.4$ FOR $s=0$ AND (c) $R_h \hat{\omega}_c / c = 2.54$ FOR $s=-1$

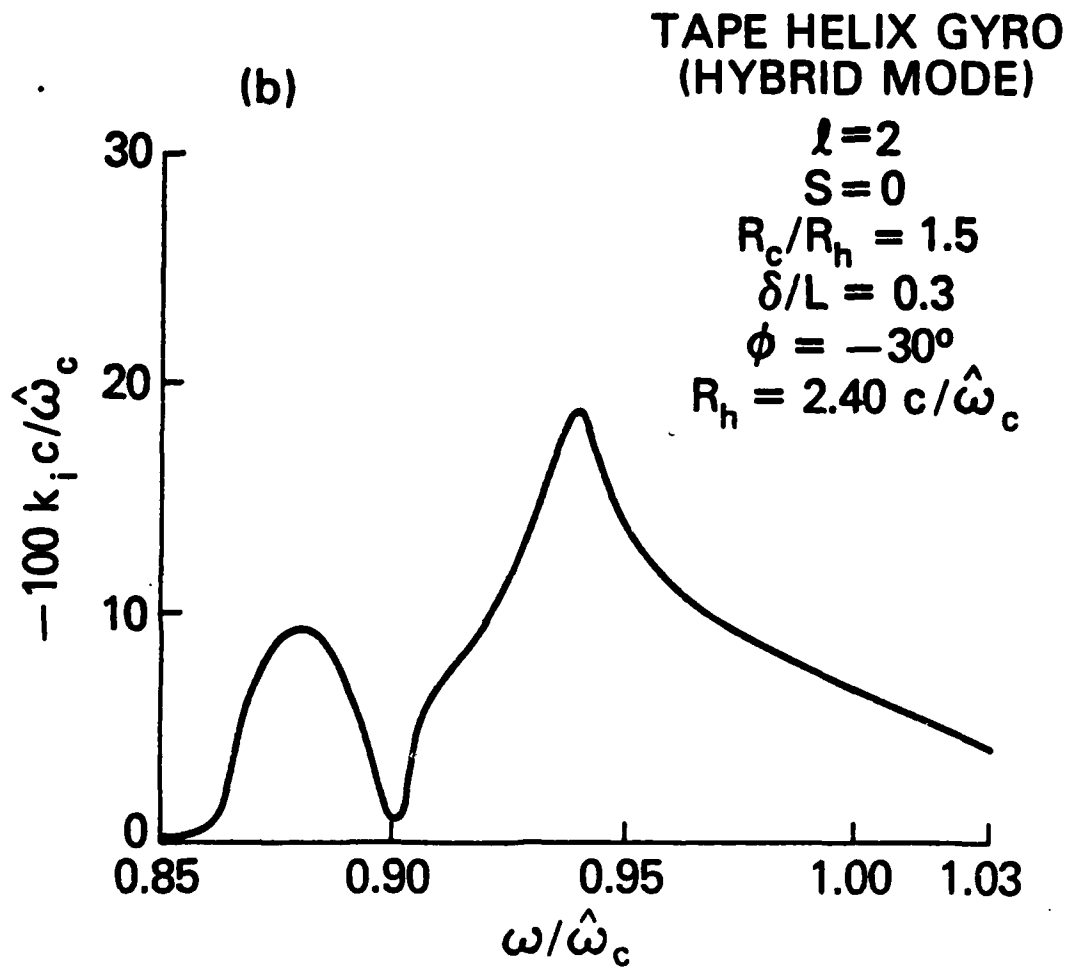


FIGURE 4. (CONTINUED)

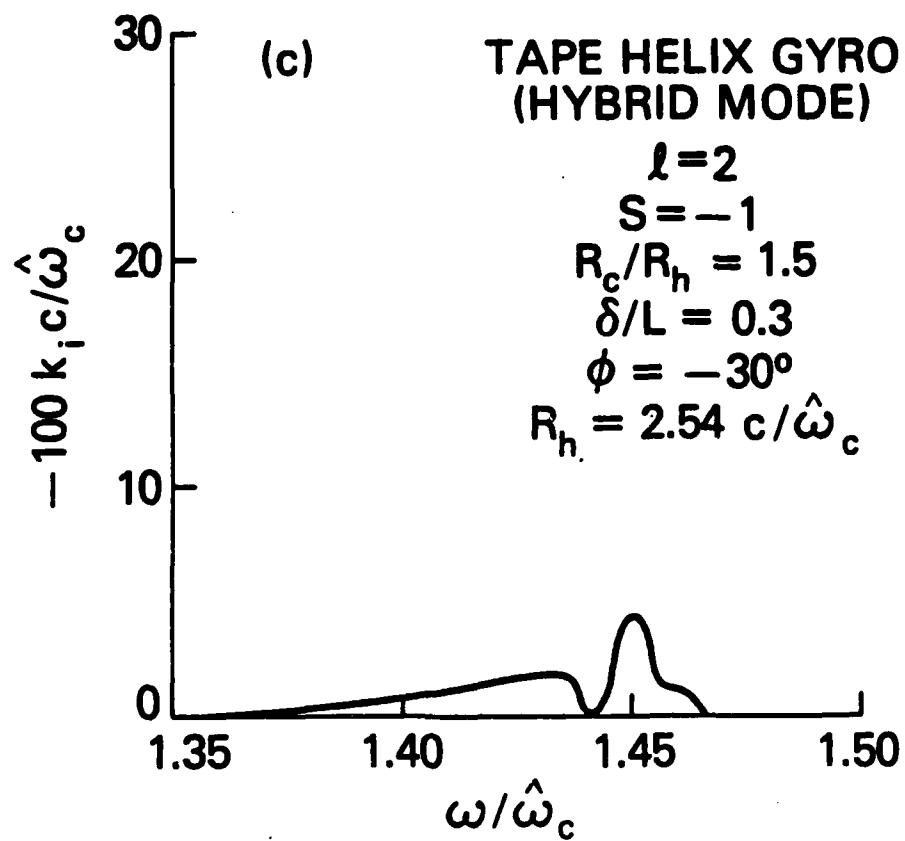


FIGURE 4. (CONTINUED)

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