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WHOLESALE PROVISIONING MODELS: MODEL OPTIMIZATION(U)
NAVAL POSTGRADUATE SCHOOL MONTEREY CA G T HOWARD
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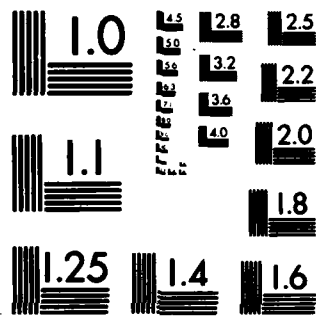
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Monterey, California



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WHOLESALE PROVISIONING MODELS:
MODEL OPTIMIZATION

by

G. T. Howard

October 1983

Final Report for Period April 1983 - September 1983

Approved for public release; distribution unlimited.

Prepared for:

Commanding Officer
Fleet Material Support Office
Mechanicsburg, PA 17055

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NAVAL POSTGRADUATE SCHOOL
Monterey, California


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Superintendent

David A. Schradly
Provost

The work reported herein was supported with funds provided by the Navy
Fleet Material Support Office, Mechanicsburg, Pennsylvania.


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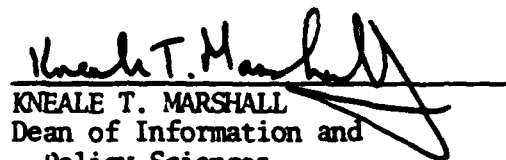
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SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER NPS55-83-028	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) WHOLESALE PROVISIONING MODELS: MODEL OPTIMIZATION	5. TYPE OF REPORT & PERIOD COVERED FINAL REPORT 1 April 83 - September 83	6. PERFORMING ORG. REPORT NUMBER
		8. CONTRACT OR GRANT NUMBER(s)
7. AUTHOR(s) G. T. Howard	9. PERFORMING ORGANIZATION NAME AND ADDRESS Naval Postgraduate School Monterey, CA 93943	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS N0036782PON3901
11. CONTROLLING OFFICE NAME AND ADDRESS Commanding Officer Fleet Material Support Office Mechanicsburg, PA 17055	12. REPORT DATE October 1983	13. NUMBER OF PAGES
	14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)	15. SECURITY CLASS. (of this report) Unclassified
16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Provisioning Availability Inventory Models Mean Supply Response Time Dynamic Programming		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) Wholesale provisioning models are considered. The performance measures used are: supply material availability, mean supply response time, and availability. These measures are optimized subject to a budget constraint. The performance constrained budget minimization problems are also solved for the optimal allocation. The basic method used is dynamic programming.		

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Abstract

Wholesale provisioning models are considered. The performance measures used are: supply material availability, mean supply response time, and availability. These measures are optimized subject to a budget constraint. The performance constrained budget minimization problems are also solved for the optimal allocation. The basic method used is dynamic programming.

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I. Introduction

A. Overview

The purpose of this report is to discuss solution methods for several problems arising in inventory provisioning. Two related types of problems are considered:

- 1) optimization of a performance measure subject to a budget constraint
- 2) minimization of cost subject to a constraint on performance.

The performance measures considered are Supply Material Availability (SMA), Mean Supply Response Time (MSRT), and "Pseudo-Availability" (PA). The basic approach to these problems is dynamic programming.

First the problems are formulated and solved using one recursive technique. Then a more efficient recursion is presented and discussed in the context of maximizing MSRT subject to a budget constraint.

These same budget constrained problems are formulated, discussed and solved using a marginal analysis approach in [2] and [3]. That method, although fast, does not guarantee that optimal solutions are obtained. This report provides a method of obtaining optimal solutions and thus provides a means of evaluating heuristic methods. In addition, this report shows how the performance constrained budget minimization problems can be solved directly. By contrast, reference [2] addresses this problem using generalized Lagrange Multipliers or by solving the budget constrained performance problem repeatedly for various budget levels.

The second recursion presented here is considerably faster than the first and it also guarantees an optimal solution in some cases. It is competitive in speed with the marginal analysis method for small and medium-sized

problems, but it is inefficient for problems with a large number of items or large budget values. Its virtue lies in its ability to get exact solutions to medium-sized problems.

B. Problem Formulations, budget constrained

This report considers three specific budget constrained optimization problems arising in inventory provisioning. These problems are formulated and discussed in detail elsewhere [2] and will be stated here without extensive explanation.

Following [2] we let

n = the total number of items considered for provisioning

C_i = the unit cost of item i

E_i = the essentiality code for item type i

λ_i = the demand rate for item i

T_i = the procurement leadtime for item i

S_i = the number of items of type i provided (the decision variables)

$Z_i(S_i)$ = the performance measure for item i when S_i units are stocked

$D_i(S_i) = Z_i(S_{i+1}) - Z_i(S_i)$

$p_i(x_i)$ = probability that demand for item i is x_i during the provisioning interval

$P_i(x_i)$ = cumulative probability of x_i or fewer demands during a provisioning interval

$MTTR_i$ = mean time to repair or replace item i

$MTBF_i$ = mean time between failures = $1/\lambda_i$

$MSRT_i(S_i)$ = mean supply response time when S_i units are stocked.

The three budget constrained problems considered are:

a) maximize Supply Material Availability (SMA), defined as

$$SMA(S_1, \dots, S_n) = \frac{\sum_{i=1}^n E_i \lambda_i T_i Z_i^{(1)}(S_i)}{\sum_{i=1}^n E_i \lambda_i T_i}$$

where

$$Z_i^{(1)}(S_i) = (1 - p_i(S_i)) + (S_i - \lambda_i T_i)(1 - P_i(S_i))/\lambda_i T_i .$$

b) minimize Mean Supply Response Time (MSRT), defined as

$$MSRT(S_1, \dots, S_n) = \frac{\sum_{i=1}^n E_i \lambda_i T_i Z_i^{(2)}(S_i)}{\sum_{i=1}^n E_i \lambda_i T_i}$$

where

$$Z_i^{(2)}(S_i) = (1 - p_i(S_i))(T_i/2 - S_i/\lambda_i) + \frac{S_i(S_i+1)}{2\lambda_i^2 T_i} \\ + p_i(S_i)(\lambda_i T_i - S_i)/2\lambda_i .$$

c) maximize Pseudo-Availability (PA), defined as

$$PA(S_1, \dots, S_n) = \prod_{i=1}^n Z_i^{(3)}(S_i)$$

where

$$Z_i^{(3)}(S_i) = MTBF_i / (MTBF_i + MTTR_i + Z_i^{(2)}(S_i)) .$$

In each of the budget constrained problems above the objective is to be optimized by selection of S_1, \dots, S_n subject to the constraints

$$\sum_{i=1}^n C_i S_i \leq B, \quad S_i \geq U \text{ integer}$$

where B is the specified budget level.

C. Problem Formulations, Performance Constrained

In addition to the three problems just stated, we consider three related problems in which the cost is to be minimized subject to a constraint on performance.

$$\begin{aligned} \text{a2) } \min \quad & \sum_{i=1}^n C_i S_i \\ \text{s.t.} \quad & \text{SMA}(S_1, \dots, S_n) \geq \text{SMA} \\ & S_i \geq 0 \text{ integer.} \end{aligned}$$

$$\begin{aligned} \text{b2) } \min \quad & \sum_{i=1}^n C_i S_i \\ \text{s.t.} \quad & \text{MSRT}(S_1, \dots, S_n) \leq \text{MSRT} \\ & S_i \geq 0 \text{ integer.} \end{aligned}$$

$$\begin{aligned} \text{c2) } \min \quad & \sum_{i=1}^n C_i S_i \\ \text{s.t.} \quad & \text{PA}(S_1, \dots, S_n) \geq \text{PA} \\ & S_i \geq 0 \text{ integer.} \end{aligned}$$

II. Solution Method and Examples

A. Dynamic Programming Approach

The computer program used to solve these problems is DP4, a general purpose program for performing dynamic programming tabular computations. Here we will describe the general nature of that program and those elements required to tailor it for use in the problems considered in this report.

The DP4 program deals with a problem consisting of n related stages each of which is characterized as shown in figure 1.

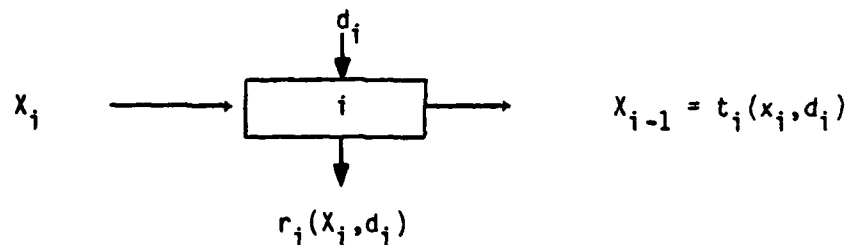


Figure 1. A single-stage decision problem.

In figure 1

x_i is the "state" variable

d_i is the decision variable

r_i is the stage return function

t_i is the stage transformation function.

In the overall problem consisting of n stages the output state variable from stage i , namely x_{i-1} , is the input to stage $i-1$. Thus, the n stage problem can be pictured as in figure 2.

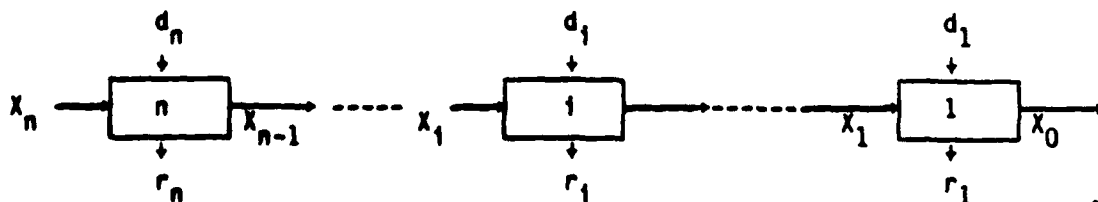


Figure 2. n -stage decision problem.

The state variable X_i can easily be understood in the context of the budget constrained problems as the amount of resource (money) remaining to be allocated to stages $i, i-1, \dots, 1$. The stages, of course, correspond to the items in the inventory problems.

At each stage i a decision d_i must be made. The decision has two effects. First, it yields a return r_i , the performance measure associated with the current item. Second, it yields a value of X_{i-1} which serves as the input to the remainder of the decision process. The decision d_i must be made with consideration both for the immediate return r_i and the future state X_{i-1} . The overall problem is to make the series of decisions d_n, \dots, d_1 to optimize some function of the individual stage returns.

In the problem (a1), where S_i is the decision variable, we can let the return functions be

$$r_i(X_i, S_i) = E_i \lambda_i T_i Z_i^{(1)}(S_i) / \sum_{i=1}^n E_i \lambda_i T_i \quad i = 1, \dots, n$$

and the stage transformation functions be

$$X_n = B$$

$$X_{i-1} = t_i(X_i, S_i) = X_i - C_i S_i \quad i = 1, \dots, n.$$

The overall return function is the sum of the individual return functions. Namely,

$$SMA(S_1, \dots, S_n) = \sum_{i=1}^n r_i(X_i, S_i).$$

The object remains to select S_1, \dots, S_n to optimize this return.

We let $f_i(x_i)$ = the optimal total return from stages $i, i-1, \dots, 1$
given that we enter stage i with state variable x_i .

Then we can write the recursive equations for this optimization as

$$f_i(x_i) = \max_{S_i} \{r_i(x_i, s_i) + f_{i-1}(x_{i-1})\}$$

$$\text{s.t. } x_{i-1} = x_i - C_i S_i$$

$$\text{and } 0 \leq S_i \leq x_i / C_i$$

$$\text{and } S_i = \text{integer}$$

for $i = 2, \dots, n$.

The equation at stage 1 is

$$f_1(x_1) = \max_{S_1} r_1(x_1, S_1)$$

$$\text{s.t. } 0 \leq S_1 \leq x_1 / C_1$$

$$\text{and } S_1 \text{ integer.}$$

The program DP4 performs this optimization provided the user supplies the following subroutines and data.

Required subroutines

1. STGRET - this subroutine defines the function $r_i(x_i, d_i)$
2. TRANFM - defines the stage transformation function $t_i(x_i, d_i)$
3. DLIMIT - defines the range of decision values d_i which can be considered for the particular value of x_i under consideration
4. STORE - allows the input of constants to be used in the other subroutines.

Required Data

1. n - the number of stages
2. For each stage i
 - XLOW - the lowest value of X_i to consider
 - XHIGH - the highest value of X_i to consider
 - DELX - the increment for X_i
 - XMODE - tells whether to maximize or minimize
 - XSTAGE - tells how this stage return relates to lower numbered stage returns (sum, product).

The methodology is essentially the same for the performance constrained problems. There the return functions $r_i(X_i, d_i) = c_i d_i$. The state variable X_i is interpreted as the portion of the performance measure to be attributed to stages $1, \dots, i$. The stage transformation functions in problem (a2) and (b2) are

$$X_{i-1} = X_i - Z_i(S_i) .$$

In problem (c2) the stage transformation is

$$X_{i-1} = X_i / Z^{(3)}(S_i) .$$

The program DP4 and the subroutines are shown in Appendix A. The subroutines are written to solve any of the problems (a1), (b1), (c1) or (a2), (b2), (c2). Thus they involve complications not needed for solving just one of these problems.

B. Examples

Several example problems were solved to illustrate the approach discussed here. All of the problems involved $n = 10$ items and all used the data shown in table 1.

Data

n	λ	Time	Cost	MTTR	E
1	5.0	1.0	1.0	.0137	1.0
2	2.0	1.0	2.0	.0274	1.0
3	3.0	1.0	5.0	.0137	1.0
4	5.0	1.0	10.0	.0822	1.0
5	10.0	1.0	20.0	.0274	1.0
6	25.0	1.0	5.0	.0027	1.0
7	1.0	1.0	1.0	.0054	1.0
8	1.0	1.0	100.0	.0411	3.0
9	0.5	1.0	50.0	.0082	1.0
10	2.0	1.0	10.0	.1370	3.0

Table 1: Data for Examples

1. The budget constrained problems.

Tables 2, 3, and 4 summarize the solutions for the example problems (a1), (b1), and (c1). These are the budget constrained problems.

B = Budget =	300	295	290	285	280
max SMA =	.750654	.746466	.741160	.736563	.732964
decision $S_1 =$	4	4	4	4	4
$S_2 =$	4	4	4	4	4
$S_3 =$	4	4	4	4	4
$S_4 =$	5	5	5	4	5
$S_5 =$	2	2	2	2	1
$S_6 =$	29	28	27	28	29
$S_7 =$	3	3	3	3	3
$S_8 =$	0	0	0	0	0
$S_9 =$	0	0	0	0	0
$S_{10} =$	3	3	3	3	3

Table 2: Solutions to example problem (a1)

B =	300	295	290	285	280
min MSRT =	.0838231	.0859625	.0878466	.0900560	.0927486
decision S_1	2	2	2	2	2
S_2	3	3	3	3	3
S_3	3	4	3	3	3
S_4	4	4	4	4	4
S_5	5	4	4	4	4
S_6	21	23	23	22	21
S_7	2	2	2	2	2
S_8	0	0	0	0	0
S_9	0	0	0	0	0
S_{10}	3	3	3	3	3

Table 3. Solutions to example problem (b1)

B =	300	295	290	285	280
max PA =	.0403727	.0387421	.037005	.0355446	.0341911
decision S_1	3	3	3	3	3
S_2	4	4	4	4	4
S_3	5	4	5	5	5
S_4	5	5	5	5	5
S_5	3	3	2	2	2
S_6	26	26	26	27	26
S_7	4	4	4	4	4
S_8	0	0	0	0	0
S_9	0	0	0	0	0
S_{10}	2	2	3	2	2

Table 4. Solutions to example problem (c1)

2. The performance constrained problems.

The related performance constrained problems were also solved for illustration. For example, the problem (a2) was solved using the data from Table 1 with the restriction that $SMA \geq .732964$. The solution to that problem is the same as the solution shown in the last column of Table 2 since the value .732964 is the (largest) value of SMA corresponding to a budget of 280.

III. Modifications to Basic Method

A. An Alternative Recursion

An alternative and more efficient approach is available for the budget constrained problems.

The approach is based on a different recursion from that used in Section 2 and is very similar to an approach used to solve the "cargo loading problem". See for example Dreyfus [1].

The cargo loading problem, stated as a maximization, is:

$$\begin{aligned} \max \quad & \sum_{j=1}^N v_j d_j \\ \text{s.t.} \quad & \sum_j c_j d_j \leq B \\ & d_j \geq 0 \text{ integer.} \end{aligned}$$

Although many methods are available for solving this problem, the one of interest to us is based on the following recursion

$$f(b) = \max_{j \in \{1, \dots, N\}} \{v_j + f(b - c_j)\}$$

where $f(b)$ is the optimal total return that can be obtained when a budget of b is available.

To illustrate this method consider the data in Table 5.

i	1	2	3 = N	
v_j	1	4	6	$B = 10$
c_j	1	3	4	

Table 5. Data for example using alternative recursion

The computation proceeds with increasing values of b until $b = B$ is reached. The process can be viewed as shown in figure 3 where a template

representing the available items is placed over the budget value of current interest. The template points back to previously determined optimal solution. Each of these previous solution is considered for updating by including one more item of the type inducted by the template. The updated solutions are compared and the best selected as the solution for the current value of b . The illustration shows the template at the budget value of 7. The optimal solutions for $b = 0, 1, \dots, 6$ have already been computed. The comparison at $B = 7$ is among the solution at 6 with an additional item 1 for a total return of 9, the solution at 4 with an additional item of type 2 for a total return of 10, and the solution at 3 with an additional item of type 3 for a return of 10. Either of the last two is chosen and recorded as an optimal solution at 7.

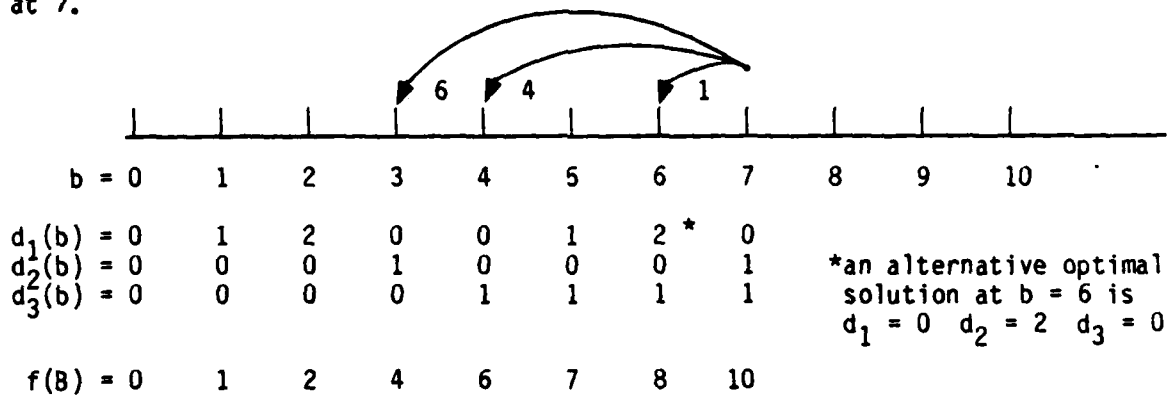


Figure 3: Illustration of solution method using the alternative recursion.

A very simple modification of this procedure can be used to solve the problems of the type discussed in this report. We consider

$$\begin{aligned} \max \quad & \sum_{j=1}^n r_j(d_j) \\ \text{s.t.} \quad & \sum_{j=1}^n c_j \cdot d_j \leq B \\ & d_j \geq 0 \text{ integer} \end{aligned}$$

where the return functions $r_j(d_j)$ are concave. The procedure below is not guaranteed to give the optimal solution for all $r_j(d_j)$ but is guaranteed if the $r_j(d_j)$ are points on a concave function.

In this case we will represent the return functions $r_j(d_j)$ as the sum of the marginal values of additional items of type j .

$$r_j(d) = + \sum_{i=1}^d m_j(i)$$

Thus $r_j(2) = m_j(0) + m_j(1) + m_j(2)$. These marginal values form a sequence with the properties that

$$m_j(i) > 0 \quad i$$

and

$$m_j(i) > m_j(k) \quad i < k .$$

The same algorithm as before was applied with the modification that the value term v_j , which was formerly constant, is replaced by $m_j(i)$ for the appropriate value of i . The program which implements this algorithm was called RECUR.

It should be noted that the discussion above treats the constraint as an inequality, but the function $f(b)$ in this section is computed for the constraint

$$\sum_{j=1}^N c_j x_j = b .$$

For this reason we may have in a maximization problem

$$f(b_1) > f(b_2)$$

although $b_1 < b_2$. That is, if we require the equality to be met exactly, it is not necessarily true that a larger budget is better. The program prints the values of $f(b)$ for several values of b so the optimal value of $b \leq B$ can be found visually.

B. Minimum Orders

1) RECMOD

A modification was made to the program RECUR to permit the user to specify minimum packaging quantities of each item. That is, item i is assumed to be packaged with q_i items per package. The provisioning can select only whole packages of each item. This modification resulted in the program RECMOD given in the Appendix.

2) Example

To illustrate the RECMOD program, consider the example problem (a2) solved previously. The optimal solution for budget $B = 300$ is repeated in Table 2 for the case in which all $q_i = 1$.

n	1	2	3	4	5	6	7	8	9	10	Objective
q_i	1	1	1	1	1	1	1	1	1	1	
d_i	2	3	3	4	5	21	2	0	0	3	.0838231
q_i	2	1	1	5	1	1	1	3	1	1	
d_i	2	3	3	5	4	23	2	0	0	3	.0847410

Table 6. Solution to Example using RECMOD.

The optimal solution is also shown for a modified problem in which not all q_i are equal to 1.

C. Discussion

The modified recursion just discussed has been implemented for the problem (a2) which is to minimize MSRT subject to a budget constraint. The method can also be applied to the other budget constrained problems, but this has not yet been done. All that is required is to modify the program to compute SMA or PA instead of MSRT and to maximize instead of minimize.

There is a difficulty in extending this method to problems in which the item costs are arbitrary values. The method is very effective when the costs are all integer and can be scaled so that the smallest cost is 1. If arbitrary costs are allowed, the algorithm can become ineffective for all except small values of B . Consider for example the costs of \$1.00, \$1.21, \$1.27 for three items. Let the budget be \$25.00. The problem could be solved by scaling the costs to be 100, 120, and 125 and the budget to be 2500, but then too many values of b must be considered when many of them are not possible. Alternatively the algorithm can step to the "next possible value" and will consider the following sequence of values

$b = 100, 121, 127, 200, 221, 227, 242, 248, 254, 300, 321, 327, \dots$

As the process continues, depending on the relative values of the costs, the sequence becomes more dense and may eventually include all possible values of b . This is ineffective and cumbersome for large values of B .

It is also not possible to apply the modified recursion for the performance constrained problems. On the other hand, the budget constrained problems are solved very rapidly and the relationship between cost and performance can easily be determined from solving the budget constrained problem using the first recursion. In fact, if MSRT is minimized for a budget of B , the solution is actually obtained for all values of b up to and including B . Those results reveal the relationship between performance and budget.

APPENDIX-PROGRAM LISTINGS

FILE: DPFILE EXEC A1 NAVAL POSTGRADJATE SCHOOL

FILEDEF 07 DISK (PERM
 FILEDEF 08 DISK RUSS10 DATA (PERM
 FILEDEF 06 TERM (LRECL 133 RECFM FB PERM
 FILEDEF 02 DISK (PERM

FILE: FILE FT07F001 A1 NAVAL POSTGRADUATE SCHOOL

10	1	10	NEW	0.	300.	1.	MIN	SUM	2
			300.		300.				
			CLD						
			295.		295.				
			OLD						
			290.		290.				
			OLD						
			285.		285.				
			OLD						
			280.		280.				
			CLD						
			275.		275.				

FILE: RUSS10 DATA A1 NAVAL POSTGRADUATE SCHOOL

2	0	10	300	(08,CON)	COST	1SMA	2MSRT	3AVAIL	-	DATA	ACEBD=LAM,COST,ESS,T,M??
		1.	1.	1.	1.	1.	1.	1.		.0137	
		2.	2.	2.	2.	2.	2.	2.		.0274	
		3.	3.	3.	3.	3.	3.	3.		.0137	
		5.	5.	5.	5.	5.	5.	5.		.0822	
		10.	10.	10.	10.	10.	10.	10.		.0274	
		25.	25.	25.	25.	25.	25.	25.		.0027	
		1.	1.	1.	1.	1.	1.	1.		.0054	
		1.	1.	1.	1.	1.	1.	1.		.0411	
		3.	3.	3.	3.	3.	3.	3.		.0082	
		5.	5.	5.	5.	5.	5.	5.		.1370	
		10.	10.	10.	10.	10.	10.	10.			

FOR RECUR THE LAST TWO LINE MUST BE PLACED FIRST INSTEAD OF THE CURRENT LINE. IT IS FOR DP4

DATA DESCRIPTION FOR CARD NUMBER 1

COLUMNS	JUSTIFY	VARIABLE NAME	MEANING
1 - 5	CJL 5	NMAX	THE NUMBER OF STAGES IN THE PROBLEM
6 - 10	CJL 10	MTAPE	LOGICAL TAPE NO OF THE MAIN TAPE IF THIS IS LEFT BLANK, THE COMPUTER WILL USE STANDARD SCRATCH TAPE 3
11 - 15	COL 15	SOLVE	= OLD IF THE OPTIMAL DECISION FUNCTIONS HAVE ALREADY BEEN CALCULATED AND ARE LOADED ON LOGICAL TAPE MTAPE = NEW IF THE OPTIMAL DECISION FUNCTIONS MUST BE CALCULATED AND STORED ON LOGICAL TAPE MTAPE BEFORE SOLVING THE PROBLEM

DATA DESCRIPTION FOR THE NEXT GROUP OF CARDS
 IF SOLVE = NEW ON CARD NUMBER 1, THEN EACH OF THE NMAX STAGES
 MUST BE DESCRIBED BY THE CARDS DISCUSSED BELOW. YOU CAN USE 1 CARD
 PER STAGE OR YOU CAN MAKE 1 CARD DESCRIBE MANY ADJACENT STAGES IF
 THEY ARE SIMILAR. THE STAGES MUST BE DESCRIBED IN NUMERICAL ORDER
 STARTING WITH STAGE 1 (I.E. STAGE 1 THEN 2, ... THEN NMAX)
 OMIT THIS PACK OF CARDS WHICH DESCRIBE THE STAGES IF SOLVE = OLD

COLUMNS	JUSTIFY	VARIABLE NAME	MEANING
1 - 5	CJL 5	NSTAGE	LOWEST NUMBERED STAGE FOR WHICH THIS CARD APPLIES
6 - 10	COL 10	NDITTO	HIGHEST NUMBERED STAGE FOR WHICH THIS CARD APPLIES. IF THESE COLUMNS ARE LEFT BLANK, THEN NDITTO WILL BE TAKEN AS EQUAL TO NSTAGE
11 - 20	ANY	XLOW	LOWEST VALUE OF XN FOR STAGE NSTAGE
21 - 30	ANY	XHIGH	HIGHEST VALUE OF XN FOR STAGE NSTAGE
31 - 40	ANY	DELX	INCREMENT IN XN FOR STAGE NSTAGE
41 - 46	COL 46	XMODE	= MIN IF STAGE NSTAGE IS TO BE MINIMIZED = MAX IF STAGE NSTAGE IS TO BE MAXIMIZED
47 - 52	COL 52	XSTAGE	= SUM IF THE COMPOSITION OPERATOR BETWEEN STAGES NSTAGE AND NSTAGE-1 IS ADDITION = MULT IF THE COMPOSITION OPERATOR BETWEEN STAGES NSTAGE AND NSTAGE-1 IS MULTIPLICATION = MINMAX IF THE COMPOSITION OPERATOR BETWEEN STAGES NSTAGE AND NSTAGE-1 IS TO MINIMIZE THE MAXIMUM INDIVIDUAL STAGE RETURN


```

1), AND STORE THEM ON LOGICAL TAPE I5)
REWIND NCALC
500 WRITE(MTAPE, NMAX)
304 WRITE(NOUTPE, 306) NMAX
306 FORMAT(16H THE PROBLEM HAS I5,7H STAGES)
314 IF(NSS2) 197,109,197
109 LINES = 6
WRITE(NOUTPE, 2006) NMAX, MTAP, SOLVE
2006 FORMAT(/// ' DATA CARD ', 2I7, A7)
121 DO 123 N=1, NMAX
    NM1=N-1
    IF(NDITTO-N) 241,132,132
241 READ(INTAPE, 124) NSTAGE, NDITTO, XLOW, XHIGH, DELX, XMODE, XSTAGE, MODES
124 FORMAT(2I5, 3E10.6, 2A6, I3)
    WRITE(NOUTPE, 2007) NSTAGE, NDITTO, XLOW, XHIGH, DELX, XMODE,
1 XSTAGE, MODES
2007 FORMAT(/// ' DATA CARD ', 2I5, 2X, 3F10.6, 2A6, I3)
    IF(LINES-41) 30,30,31
31 NPAGE=NPAGE+1
    WRITE(NOUTPE, 152) NPAGE
    LINES=1
30 LINES = LINES + 9
    ITOP=(XHIGH-XLOW)/DELX+1.001
    IF(MODES-1) 600,601,600
600 MODES=-1
601 IF(NSTAGE-N) 125,245,125
125 WRITE(NOUTPE, 127)
127 FORMAT(23H DATA CARD OUT OF ORDER)
    GO TO 2003
245 IF(NSTAGE-NDITTO) 246,126,126
246 WRITE(NOUTPE, 247) N, NSTAGE, NDITTO
247 FORMAT(/// 46H THE DESCRIPTION WHICH APPEARS BELOW FOR STAGE, I5, 17H
1 APPLIES TO STAGE, I5, 11H THRU STAGE, I5, 10H INCLUSIVE)
    LINES=LINES+4
    XMODE = XMODE - HOLMIN
    WRITE(6, 1001) XMODE
1001 FORMAT(1X, A6)
126 IF(XMODE-HOLMIN) 230,231,230
231 XMODE=1.0
    WRITE(NOUTPE, 232) N
232 FORMAT(//6H STAGE I5, 18H IS A MINIMIZATION)
    GO TO 520
230 XMODE=-1.0
    WRITE(NOUTPE, 234) N
234 FORMAT(//6H STAGE I5, 18H IS A MAXIMIZATION)
520 DO 129 I=1,4
    IF(XSTAGE-TAB(I)) 129,130,129
129 CONTINUE
521 NNFLAG=5
    GO TO 502
130 NNFLAG=1
502 IF(ITOP-MAX) 316,316,112
316 WRITE(NOUTPE, 110) XLOW, XHIGH, DELX
110 FORMAT(63H THE STATE VARIABLE IS BEING TREATED AS DISCRETE, GOING F
1 FROM XN=E14.5, 7H TO XN=E14.5, 13H IN STEPS OF E14.5)
    IF(MODES) 318,318,321
318 WRITE(NOUTPE, 510)
510 FORMAT(41H TOTAL ENUMERATION IS USED FOR THIS STAGE)
    GO TO 320
321 WRITE(NOUTPE, 511)
511 FORMAT(40H FIBONACCI SEARCH IS USED FOR THIS STAGE)
320 GO TO (11,12,13,14,132), NNFLAG
11 WRITE(NOUTPE, 16) NM1, N
16 FORMAT(40H THE COMPOSITION OPERATOR BETWEEN STAGES I6, 4H AND I6, 12H
1 IS ADDITION)
    GO TO 132
12 WRITE(NOUTPE, 17) NM1, N
17 FORMAT(40H THE COMPOSITION OPERATOR BETWEEN STAGES I6, 4H AND I6, 18H
1 IS MULTIPLICATION)
    GO TO 132
13 WRITE(NOUTPE, 18) NM1, N
18 FORMAT(40H THE COMPOSITION OPERATOR BETWEEN STAGES I6, 4H AND I6, 34H

```

```

1 IS TO MAXIMIZE THE MINIMUM RETURN)
GO TO 132
14 WRITE(NOUTPE,19) NMI,N
19 FORMAT(40H THE COMPOSITION OPERATOR BETWEEN STAGES I6,4H AND I6,34H
1 IS TO MINIMIZE THE MAXIMUM RETURN)
132 DO 136 I=1,ITOP
134 BEST=1.0E+35*XMODE
X=I-1
XN=XLOW+X*DELX
NUFF=1
CALL DLIMIT
IF(MODES) 602,602,603
603 CALL SEARCH(DLOW,DHIGH,DELD,XMODE,DNBEST,BEST)
GO TO 400
602 KTOP=(DHIGH-DLOW)/DELD+1.001
223 DO 137 J=1,KTOP
X=J-1
DN=DLOW+X*DELD
C JUMP MAY BE SET TO 1 IN TRANFM TO INDICATE AN INFEASIBLE XN-1
C JUMP=0
CALL TRANFM
CALL STGRET
C XMODE=1 FOR MIN, -1 FOR MAX
IF(JUMP.EQ.1)RN=999999*XMODE
IF(NUFF) 400,401,401
401 IF(N-1) 504,504,503
504 QN=RN
GO TO 143
503 K=(YN-YLOW)/DELY+1.001
IF(K) 212,212,209
212 WRITE(NOUTPE,210) N,XN,DN,YV
210 FORMAT(//9H AT STAGE I5,9H WITH XN=E15.8,8H AND DN=E15.8,12H XN-1
1EQUALSE16.8,21H AND IS OUT OF LIMITS//)
GO TO 2003
209 IF(K-JTOP) 205,206,212
206 RNMI=FNMI(JTOP)
GO TO 207
205 X=K-1
X=YLOW+X*DELY
RNMI=FNMI(K)+(FNMI(K+1)-FNMI(K))*(YN-X)/DELY
207 GO TO (21,22,23,24,248),NNFLAG
248 WRITE(NOUTPE,249) N
249 FORMAT(43H1C COMPOSITION OPERATOR NOT DEFINED FOR STAGE, I5)
GO TO 2003
21 QN=RN+RNMI
GO TO 143
22 QN=RN*RNMI
GO TO 143
23 IF(RN-RNMI) 141,141,142
141 QN=RN
GO TO 143
142 QN=RNMI
GO TO 143
24 IF(RN-RNMI) 145,145,146
145 QN=RNMI
GO TO 143
146 QN=RN
143 IF((QN-BEST)*XMODE) 144,137,137
144 BEST=QN
DNBEST=DN
137 CONTINUE
400 WRITE(NCALC) BEST,DNBEST
136 CONTINUE
REWIND NCALC
WRITE(NTAPE) XLOW,XHIGH,DELD,ITOP,XMODE
DO 404 I=1,ITOP
404 READ(NCALC) DUM,DNOFXN(I)
REWIND NCALC
WRITE(NTAPE) (DNOFXN(I),I=1,ITOP)
DO 402 I=1,ITOP
402 READ(NCALC) FN(I),DUM
REWIND NCALC

```

```

YLOW=XLOW
YHIGH=XHIGH
DELY=DELX
JTOP=ITOP
123 CONTINUE
WRITE(MTAPE) (FN(II),II=1,ITOP)
161 END FILE MTAPE
197 REWIND MTAPE
READ(MTAPE) NMAX
N=NMAX
J=N-1
IF(J) 407,407,201
201 DO 522 I=1,J
READ(MTAPE)
522 READ(MTAPE)
407 READ(MTAPE) XLOW,XHIGH,DELX,ITOP,XMODE
READ(MTAPE)
READ(MTAPE) (FN(I),I=1,ITOP)
BACKSPACE MTAPE
BACKSPACE MTAPE
READ(MTAPE,162) XN1,XN2
162 FORMAT(2E15.8)
NPAGE=NPAGE+1
WRITE(NOUTPE,152) NPAGE
WRITE(NOUTPE,2008) XN1, XN2
2008 FORMAT(/// ' DATA CARD ', 2F20.8 ///)
IF(XMODE) 323,323,324
324 WRITE(NOUTPE,325) N
325 FORMAT(29H THE PROBLEM IS TO MINIMIZE AI6,14H STAGE PROCESS)
GO TO 327
323 WRITE(NOUTPE,326) N
326 FORMAT(29H THE PROBLEM IS TO MAXIMIZE AI6,14H STAGE PROCESS)
327 WRITE(NOUTPE,328) XN1,XN2
328 FORMAT(42H XN IS TO BE CHOSEN OPTIMALLY BETWEEN XN=1PE14.5,8H AN
1D XN=1PE14.5)
171 IF(XLOW-XN1) 175,175,176
176 WRITE(NOUTPE,177) XLOW,XHIGH
177 FORMAT(47H THE PROGRAM ONLY HAS INFORMATION ON XN BETWEEN 16.8,4H
1ANDE16.8)
GO TO 240
175 IF(XN2-XHIGH) 181,181,176
181 IF(XN1-XN2) 178,178,176
178 IX1=(XN1-XLOW)/DELX+1.001
IX2=(XN2-XLOW)/DELX+1.001
BEST=1.0E+35*XMODE
DO 182 J=IX1,IX2
IF((FN(J)-BEST)*XMODE) 183,182,182
183 BEST=FN(J)
JSAVE=J
182 CONTINUE
X=JSAVE-1
XN=XLOW+X*DELX
WRITE(NOUTPE,184) XN,BEST
184 FORMAT(12H OPTIMAL XN=1PE14.5,164 OPTIMAL RETURN=1PE14.5)
READ(MTAPE) (DNOF XN(II),II=1,ITOP)
186 DN=DNOF XN(JSAVE)
CALL TRANFM
204 WRITE(NOUTPE,188)
188 FORMAT(7H0 N1 8X2H XN1 8X2HDN15X4HXN-1)
NN=0
203 WRITE(NOUTPE,189) N,XN,DN,YN
189 FORMAT(17,1P3E20.5)
NN=NN+1
N=N-1
IF(N-1) 244,193,193
244 GO TO 240
193 DO 406 I=1,4
406 BACKSPACE MTAPE
READ(MTAPE) XLOW,XHIGH,DELX,ITOP,XMODE
READ(MTAPE) (DNOF XN(II),II=1,ITOP)
L=(YN-XLOW)/DELX+1.001
IF(L) 214,214,215

```

```

214 L=1
219 NP1=N+1
   WRITE(NOUTPE,210) NP1,XN,DN,YN
   NN=NN+7
215 IF(L-ITOP) 218,216,217
216 DN=DN+FXN(L)
   XN=YN
   GO TO 196
217 L=ITOP
   GO TO 219
218 XN=YN
194 X=L-1
   X=XLOW+X*DELX
   DN=DN+FXN(L)+(DN+FXN(L+1)-DN+FXN(L))* (XN-X)/DELX
196 CALL TRANFM
   IF(NN-50) 203,203,220
220 NPAGE=NPAGE+1
   WRITE(NOUTPE,152) NPAGE
   GO TO 204
112 WRITE(NOUTPE,113) MAX,ITOP
113 FORMAT(72H THIS PROGRAM LIMITS THE NUMBER OF DISCRETE STEPS OF THE
1 STATE VARIABLE TO 16,26H AND THIS PROBLEM REQUIRES 16)
2002 FORMAT('1',, ' ERROR HALT')
2003 WRITE(6,2002)
   STOP
2000 WRITE(6,2001)
2001 FORMAT('1',, ' END OF DATA FILE')
   STOP
   END

```

CSEARCH DISCRETE FIBONACCI SEARCH SUBROUTINE
SUBROUTINE SEARCH(AA,BB,DELYY,XXMODE,YYBEST,BEST)
DIMENSION F(150)

```

CCCCCCCC
OPTIMIZE WITH RESPECT TO Y BETWEEN AA AND BB IN STEPS OF DELYY
STORE OPTIMUM Y IN YYBEST AND THE OPTIMUM VALUE OF THE OBJECTIVE
FUNCTION IN BEST
XXMODE=-1 FOR MAXIMIZE
XXMODE=1 FOR MINIMIZE
SUBROUTINE MUST BE INITIALIZED BY CALLING IT WITH DELYY=-1.0 AT
LEAST ONCE BEFORE IT IS USED FOR A SEARCH
DELY=DELYY
A=AA
B=BB
XMODE=XXMODE
IF(DELY) 100,100,101
100 F(1)=1.0
   F(2)=2.0
   DO 1 I=3,150
   F(I)=F(I-1)+F(I-2)+1.0
   IF(F(I)-1.0E+35) 1,2,2
   2 II=I
   RETURN
1 CONTINUE
   II=150
   RETURN
101 YHI=B
   YLO=A
   FNO=(YHI-YLO)/DELY+1.0
   DO 5 N=1,II
   IF(FNO-F(N)) 6,6,5
   5 CONTINUE
   WRITE(6,7)
   7 FORMAT(38H1ERROR, TOO MANY POINTS TO BE SEARCHED)
2002 FORMAT('1',, ' ERROR HALT')
2003 WRITE(6,2002)
   STOP
   6 IF(N-2) 42,41,40
   40 Y1=F(N-2)*DELY+YLO
   CALL FUNCTN(Y1,GY1)
   Y2=F(N-1)*DELY+YLO
   CALL FUNCTN(Y2,GY2)
   16 N=N-1

```

FILE: DP4 FORTRAN A1 NAVAL POSTGRADUATE SCHOOL

```
IF(N-1) 102,102,103
103 IF((GY2-GY1)*XMODE) 19,19,20
19 YLO=Y1+DELY
Y1=Y2
GY1=GY2
Y2=F(N-1)*DELY+YLO
IF(Y2-8) 104,104,105
105 GY2=1.0E+35*XMODE
GO TO 16
104 CALL FUNCTN(Y2,GY2)
GO TO 16
20 YHI=Y2-DELY
Y2=Y1
GY2=GY1
IF(N-2) 34,34,35
34 FNM2=0.0
GO TO 36
35 FNM2=F(N-2)
36 Y1=FNM2*DELY+YLO
CALL FUNCTN(Y1,GY1)
GO TO 16
102 IF((GY2-GY1)*XMODE) 110,111,111
110 YBEST=Y2
BEST=GY2
RETURN
111 YBEST=Y1
BEST=GY1
RETURN
41 Y1=A
CALL FUNCTN(Y1,GY1)
Y2=B
CALL FUNCTN(Y2,GY2)
GO TO 102
42 Y1=A
CALL FUNCTN(Y1,GY1)
GO TO 111
END
CFUNCTN
SUBROUTINE FUNCTN(Y,GY)
DIMENSION FN(10001),FNMI(10001),DNQFXN(10001)
REAL * 8 TAB(4)
COMMON /CON/TAB
COMMON XN,N,ON,YN,RN,SLW,XHIGH,DELX,DLOW,DHIGH,DELD,NUMBER
COMMON YLOW,YHIGH,DELY,NUFF,FN,JTOP,NNFLAG,NMAX,XLAM
COMMON A,B,C,D,E,SUMELT,KODE
EQUIVALENCE (FN(1),FNMI(1),DNQFXN(1))
DN=Y
NOUTPE=6
C JUMP MAY BE SET TO 1 IN TRANFM TO INDICATE AN INFEASIBLE XN-1
C JUMP=0
CALL TRANFM
CALL STGRET
C XMODE=1 FOR MIN, -1 FOR MAX
C IF(JUMP.EQ.1)RV=999999*XMODE
IF(N-1) 146,146,401
401 K=(YN-YLOW)/DELY+1.001
IF(K) 212,212,209
212 WRITE(NOUTPE,210) N,XN,ON,YN
210 FORMAT(///9H AT STAGE 15,9H WITH XN=E15.8,8H AND DN=E15.8,12H XN-1
1EQUALSE16.8,21H AND IS OUT OF LIMITS//)
2002 FORMAT('1',, ' ERROR HALT')
2003 WRITE(NOUTPE,2002)
STOP
209 IF(K-JTOP) 205,206,212
206 RNMI=FNMI(JTOP)
GO TO 207
205 X=K-1
X=YLOW+X*DELY
RNMI=FNMI(K)+(FNMI(K+1)-FNMI(K))*(YN-X)/DELY
207 GO TO (21,22,23,24),NNFLAG
21 QN=RN+RNMI
GO TO 137
```

FILE: DP4

FORTRAN A1 NAVAL POSTGRADUATE SCHOOL

```
22 QN=RN+RNM1
   GO TO 137
23 IF(RN-RNM1) 141,141,142
141 QN=RN
   GO TO 137
142 QN=RNM1
   GO TO 137
24 IF(RN-RNM1) 145,145,146
145 QN=RNM1
   GO TO 137
146 QN=RN
137 QY=QN
   RETURN
   END
```

CSTORE

```

SUBROUTINE STORE
DIMENSION FN(1000),FNM1(1000),,DNFXN(1000),A(101),B(101),C(101)
DIMENSION D(101),E(101)
REAL * 8 TAB(4)
COMMON /CON/TAB
COMMON XN,N,ON,YN,RN,SLOW,XHIGH,DELX,DLOW,DHIGH,DELD,NUMBER
COMMON YLOW,YHIGH,DELY,NUFF,FN,JTOP,VNFLAG,NMAX,XLAM
COMMON A,B,C,D,E,SUMELT,KODE1,KODE2
EQUIVALENCE (FN(1),FNM1(1),DNFXN(1))
INDATA=8
NOUTPE=6
808 READ (INDATA,808) KODE1,KODE2
FORMAT (2I3)
IF(KODE1.EQ.0) WRITE(NOUTPE,110)
IF(KODE1.EQ.1) WRITE(NOUTPE,101)
IF(KODE1.EQ.2) WRITE(NOUTPE,202)
IF(KODE1.EQ.3) WRITE(NOUTPE,303)
110 FORMAT (30H THE OBJECTIVE IS COST )
101 FORMAT (30H THE OBJECTIVE IS SMA )
202 FORMAT (30H THE OBJECTIVE IS MSRT )
303 FORMAT (30H THE OBJECTIVE IS AVAILABILITY )
IF(KODE2.EQ.0) WRITE(NOUTPE,900)
IF(KODE2.EQ.1) WRITE(NOUTPE,901)
IF(KODE2.EQ.2) WRITE(NOUTPE,902)
IF(KODE2.EQ.3) WRITE(NOUTPE,903)
900 FORMAT (30H CONSTRAINT ON COST )
901 FORMAT (30H CONSTRAINT ON SMA )
902 FORMAT (30H CONSTRAINT ON MSRT )
903 FORMAT (30H CONSTRAINT ON AVAILABILITY )
DO 333 K=1,NMAX
999 READ (INDATA,999) A(K),C(K),E(K),B(K),D(K)
FORMAT (5F10.4)
WRITE(NOUTPE,999) A(K),B(K),C(K),D(K),E(K)
333 CONTINUE
SUMELT=0.
DO 30 I=1,NMAX
30 SUMELT=SUMELT+E(I)*A(I)*B(I)
765 WRITE(6,765)SUMELT
765 FORMAT(F10.3)
RETURN
END
    
```

CSTGRET

```

SUBROUTINE STGRET
DIMENSION FN(1000),FNMI(1000),ONOFXN(1000),A(101),B(101),C(101)
DIMENSION D(101),E(101)
REAL * 8 TAB(4)
COMMON /CON/TAB
COMMON XN,N,JN,YN,RN,SLOW,XHIGH,DELX,DLOW,DHIGH,DELD,NUMBER
COMMON YLOW,YHIGH,DELY,NUFF,FN,JTOP,VNFLAG,NMAX,XLAM
COMMON A,B,C,D,E,SUMELT,KODE1,KODE2
EQUIVALENCE (FN(1),FNMI(1),ONOFXN(1))
IF(KODE1.EQ.0)GO TO 77
IDN=INT(DN)
AB=A(N)*B(N)
IS=IDN
TERM=0.
TEMP=0.
IF(IS.LT.0)GO TO 11
TERM=EXP(-AB)
TEMP=TERM
IF(IS.EQ.0)GO TO 11
DO 10 I=1,IS
TEMP=TEMP*AB/I
IF(TERM.GE..99999)GO TO 11
IF(TEMP.LE..00001)GO TO 11
10 TERM=TERM +TEMP
11 CDF=TERM
20 CONTINUE
IF(KODE1.NE.1)GO TO 40
C FOLLOWING CHANGED 120183
C SMA=(AB*(1.-TEMP)+(IDN-AB)*(1.-CDF))/AB
C SMA=(1.-TEMP)+(IDN-AB)*(1.-CDF)/AB
RN=E(N)*AB*SMA/SUMELT
RETURN
40 TWUS=(1.-CDF)*(AB*AB-2.*AB*IDN+IDN*(IDN+1))/(2.*A(N))
X+TEMP*B(N)*(AB-IDN)/2.
IF(KODE1.EQ.3)GO TO 50
RN=E(N)*TWUS/SUMELT
RETURN
50 CONTINUE
AMSRT=TWUS/AB
AMTBF=1./A(N)
AMTTR=D(N)
RN=(AMTBF)/(AMTBF+AMTTR+AMSRT)
RETURN
77 RN=C(N)*DN
C IF(KODE2.EQ.1.AND.N.EQ.1.AND.YN.LT.XN)RN=999999
RETURN
END

```

CDLIMIT

```

SUBROUTINE DLIMIT
DIMENSION FN(10001),FNMI(10001),DNOFXN(10001),A(101),B(101),C(101)
DIMENSION D(101),E(101)
REAL * 8 TAB(4)
COMMON /CON/TAB
COMMON XN,N,YN,YN,RN,SLOW,XHIGH,DELX,DLOW,DHIGH,DELD,NUMBER
COMMON YLOW,YHIGH,DELY,NUFF,FN,JTOP,VNFLAG,NMAX,XLAM
COMMON A,B,C,D,E,SUMELT,KODE1,KODE2
EQUIVALENCE (FN(1),FNMI(1),DNOFXN(1))
IF(KODE2.NE.3)GO TO 37
DLOW=0.
DELD=1.
DHIGH=AMIN1(XN/C(N),50.)
RETURN
37 AB=A(N)*B(N)
DO 555 ID=1,30
IS=ID-1
TERM=EXP(-AB)
TEMP=TERM
IF(IS.EQ.0)GO TO 11
DO 10 I=1,IS
TEMP=TEMP*AB/I
IF(TEMP.GE..99999)GO TO 11
IF(TEMP.LE..00001)GO TO 11
10 TERM=TERM +TEMP
11 CDF=TERM
40 TWUS=(1.-CDF)*(AB*AB-2.*AB*IS+IS*(IS+1))/(2.*A(N))
X+TEMP*B(N)*(AB-IS)/2.
C CHANGED FOLLOWING TO 555 FROM 556
IF(KODE2.EQ.2)GO TO 555
IF(KODE2.EQ.3)GO TO 554
SSS=(1.-TEMP)+(IS-AB)*(1.-CDF)/AB
RR=E(N)*AB*SSS/SUMELT
Y=XN-RR
DLOW=0.
C THE NUMBER IN THE NEXT LINE HAS A BIG EFFECT. IT SHOJLD NOT.
IF(N.EQ.1)DLOW=1000.
IF(N.EQ.1.AND.Y.GT.0..AND.ID.LT.30)GO TO 555
IF(N.EQ.1.AND.Y.LE.0.)DLOW=IS
136 DHIGH=30.+DLOW
IF(DLOW.EQ.1000.)DHIGH=1000.
DELD=1.
RETURN
554 AMSRT=TWUS/AB
AMTBF=1./A(N)
AMTTR=D(N)
AV=AMTBF/(AMTBF+AMTTR+AMSRT)
IF(AV.GE.XN)GO TO 556
555 CONTINUE
IS=30.
556 DLOW=IS
DELD=1.
DHIGH=50.
RETURN
END
BLOCK DATA
COMMON /CON/TAB
REAL * 8 TAB(4) / ' SUM', ' MULT', ' MAXMIN', ' MINMAX' /
END

```

FILE: TRANFM FORTRAN A1 NAVAL POSTGRADUATE SCHOOL

CTRANFM

```
SUBROUTINE TRANFM
DIMENSION FN(1000), FNM1(10001), DNOFXN(10001), A(101), B(101), C(101)
DIMENSION D(101), E(101)
REAL * 8 TAB(4)
COMMON /CON/TAB
COMMON XN, N, DN, YN, RN, SLOW, XHIGH, DELX, DLOW, DHIGH, DELD, NUMBER
COMMON YLOW, YHIGH, DELY, NUFF, FN, JTOP, VNFLAG, YMAX, XLAM
COMMON A, B, C, D, E, SUMELT, KODE1, KODE2
EQUIVALENCE (FN(1), FNM1(1), DNOFXN(1))
IF(KODE2.NE.0) GO TO 12
YN=XN-C(N)*DN
RETURN
12 IDN=INT(DN)
AB=A(N)*B(N)
IS=IDN
TERM=0.
TEMP=0.
IF(IS.LT.0) GO TO 11
TERM=EXP(-AB)
TEMP=TERM
IF(IS.EQ.0) GO TO 11
DO 10 I=1, IS
TEMP=TEMP*AB/I
IF(TERM.GE..99999) GO TO 11
IF(TEMP.LE..00001) GO TO 11
10 TERM=TERM+TEMP
11 CDF=TERM
40 TWUS=(1.-CDF)*(AB*AB-2.*AB*IDN+IDN*(IDN+1))/(2.*A(N))
X+TEMP*B(N)*(AB-IDN)/2.
IF(KODE2.EQ.2) GO TO 50
IF(KODE2.EQ.3) GO TO 51
SMA=(1.-TEMP)+(IDN-AB)*(1.-CDF)/AB
YN=XN-E(N)*AB*SMA/SUMELT

IF(YN.LT.0) YN=0.0

C IF(N.NE.1.AND.YN.LT.0.OR.N.NE.1.AND.YN.GT.1.) JUMP=1
C IF(N.EQ.1.AND.YN.GT.0) JUMP=1
C IF(JUMP.EQ.1) YN=0.
RETURN
51 AMSRT=TWUS/AB
AMTBF=1./A(N)
AMTR=D(N)
AV=(AMTBF)/(AMTBF+AMTR+AMSRT)
YN=XN/AV
C AV IS AVAIL
RETURN
50 YN=XN-E(N)*TWUS/SUMELT
IF(YN.LE.0.) YN=0.
RETURN
END
```

FILE: RECMOD FORTRAN A1 NAVAL POSTGRADUATE SCHOOL

```
DIMENSION A(20),B(20),C(20),D(20),E(20),MINQ(20)
DIMENSION T(10,30),F(1200),DX(10,1200),TN(10,31)
INTEGER BUDGET,BB,BBP1,DX
REAL*8 TIME,CTIME
INDATA=8
NOUTPE=6
888 READ(INDATA,888) NMAX,BUDGET
FORMAT(2I5)
777 READ(INDATA,777) (MINQ(I),I=1,NMAX)
FORMAT(20I5)
DO 333 K=1,NMAX
999 READ(INDATA,999) A(K),C(K),E(K),B(K),D(K)
FORMAT(5F10.4)
C 333 WRITE(NCUTPE,999) A(K),B(K),C(K),D(K),E(K)
CONTINUE
TIME=CTIME(1)
SUMELT=0.
DO 30 I=1,NMAX
30 SUMELT=SUMELT+E(I)*A(I)*B(I)

DO 10 I=1,NMAX
DX(I,1)=0
DO 110 KP1=1,31
K=KP1-1
AB=A(I)*B(I)
TERM=EXP(-AB)
TEMP=TERM
IF(K.EQ.0) GO TO 11
DO 14 JI=1,K
TEMP=TEMP*AB/JI
C 14 IF(TEMP.GE..999999) GO TO 11
C 11 IF(TEMP.LE..0000001) GO TO 11
TEMP=TEMP+TEMP
11 CDF=TERM

40 TWUS=(1.-CDF)*(AB*AB-2.*AB*K+K*(K+1))/(2.*A(I)
X+TEMP*B(I)*(AB-K)/2.
110 TN(I,KP1)=E(I)*TWUS/SUMELT
DO 70 K=1,30
70 T(I,K)=TN(I,K+1)-TN(I,K)
10 CONTINUE

C 456 DO 456 IJK=1,10
C 555 WRITE(6,555) (TN(KI,IJK),KI=1,NMAX)
C 555 FORMAT(5F12.7)

DO 80 I=1,NMAX
LIM=30/MINQ(I)
DO 85 K=1,LIM
TMOD=0.
MM=MINQ(I)
DO 90 J=1,MM
90 TMOD=TMOD+T(I,(K-1)*MINQ(I)+J)
T(I,K)=TMOD
85 CONTINUE
C(I)=MINQ(I)*C(I)
80 CONTINUE

IBD=BUDGET+1
DO 100 BBP1=1,IBD
BB=BBP1-1
XMIN=0.
ISTAR=0
TRY=0.
DO 210 I=1,NMAX
IF(BB-C(I).LT.0) GO TO 210
IF(BB-C(I).GT.0) GO TO 211
TRY=AMINI(TRY,T(I,1))
GO TO 212
```

```

211 TRY=T(I,DX(I,BBP1-C(I))+1)+F(BBP1-C(I))
212 IF (TRY.GT.XMIN) GO TO 210
XMIN=TRY
ISTAR=I
210 CONTINUE
F(BBP1)=XMIN

19 DO 21 I=1,NMAX
IF (ISTAR.EQ.0.OR.BB-C(ISTAR).LE.0) DX(I,BBP1)=0
IF (ISTAR.EQ.0.OR.BB-C(ISTAR).LE.0) GO TO 21
DX(I,BBP1)=DX(I,BBP1-C(ISTAR))
21 CONTINUE
IF(ISTAR.EQ.0)GO TO 100
IF(BBP1-C(ISTAR).LE.1) DX(ISTAR,BB+1)=1
IF(BBP1-C(ISTAR).LE.1) GO TO 100
DX(ISTAR,BBP1)=AMINO(DX(ISTAR,BBP1-C(ISTAR))+1,30)
100 CONTINUE
KLOW=IBD-5
KHIGH=IBD
DO 101 KBD=KLOW,KHIGH
TIME=TIME-CTIME(I)
WRITE(6,3456)TIME
C 3456 FORMAT('TIME=',F12.9)
WRITE(6,1000)(DX(I,KBD),I=1,NMAX)
WRITE(6,1000)(MINC(I),I=1,NMAX)
1000 FORMAT(10I5)
AMSRT=0.
DO 88 I=1,NMAX
88 AMSRT=AMSRT+TN(I,MINC(I)*DX(I,KBD))+1)
KBDM1=KBD-1
WRITE(6,2000) AMSRT,KBDM1
2000 FORMAT(1X,'MSRT= ',F10.8,' BUDGET= ',I7)
101 CONTINUE
RETURN
END
FUNCTION CTIME(I)
REAL*8 CTIME
DATA IFL/Q/
IF( IFL.NE.0 ) GO TO 10
IFL = 1
CTIME = 0.000
CALL SETIME
RETURN
10 CALL GETIME(ITIME)
CTIME = -ITIME*0.00002600
RETURN
END

```

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