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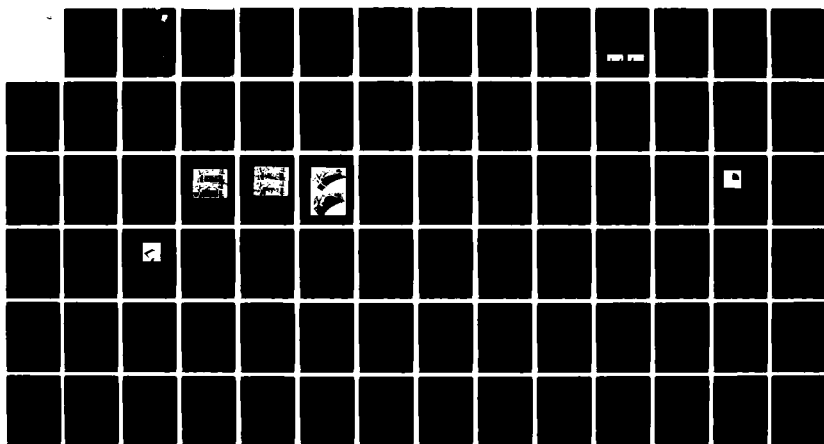
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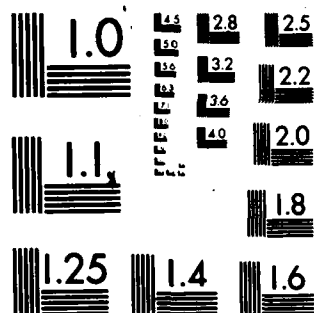


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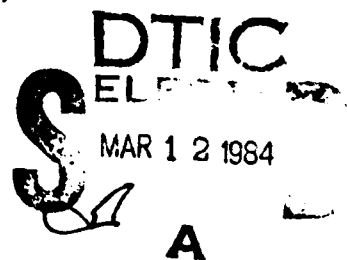
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Stanford University

Thomas O. Binford and H. Harlyn Baker

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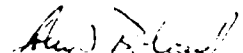
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1: Demonstration of Stereo Mapping Technology

1.1 Introduction

The focus of the research over this postdoctoral contract has been in augmenting and refining the specification of image matching strategies to be employed in an advanced stereo mapping system. Initially, our research task was to evaluate a preliminary design for a mapping system, and then by carrying out test implementations of elements of this proposed system, to iterate on the design process. As part of a continuing mapping program, this phase of the research would lead to more effective representations and improved matching strategies for surface reconstruction. The test implementations would build to provide a foundation on which we would develop an experimental rule-based stereo matching system. As part of this experimental system, we undertook to develop an interactive test facility to provide hand synthesized data for rule analysis. A change in the scope of the project occurred shortly after we had begun the research, and necessitated a redirection in the emphasis; rather than evaluating or continuing the design, we were to:

- a) experiment with an existing matching system (showing its capabilities and assessing its applicability to the planned system);
- b) demonstrate the design and the utility of the rule-based approach to surface inference from monocular information;
- c) develop tools to support an interactive test facility.

1.2 Scope of the Research

In a), we undertook to apply an existing stereo mapping system [Baker 1981] to some new imagery. This was designed to demonstrate its effectiveness, to expose its limitations, and to suggest both its role in an advanced mapping system and complementary research needed to improve its utility. Significant restructuring of the system was called for in enabling it to process this imagery. Details of these changes are described in section 5, which deals with the matching process. The modifications have now been implemented, enabling the system to:

- function on the output of an improved edge operator [Marimont 1982];
- use edge extent as one of its parameters in seeking optimized correspondence;
- exploit prepared transform information in processing images whose epipolar lines are not collinear with the scanning axes of the cameras.

Separate funding sources supported research in analysis and synthesis of rules for inference of three-dimensional shape from single images. This inference also has application in constraining search for matches in stereo correspondence. We will describe here some results of this research,

and, as part of the demonstration, will show its use in shape inference and search constraint in the domain of Orthogonal Trihedral Vertices (OTV's).

Our work in developing tools has centered on:

- a) a system for the hand construction of edge descriptions from hard copy imagery;
- b) an interactive system for determining the transform to bring image pairs into collinear epipolar registration.

Both of these systems make extensive use of interactive graphics, and the latter takes much advantage of previous stereo research from our laboratory ([Gennery 1980]).

These are the three principal areas to be covered in this report:

- experimentation with the automated mapping system;
- assessment of rule synthesis from manual and automated edge processes;
- development of test facility tools for edge extraction and image registration.

1.3 Specific Tasks

We will describe results in these areas of the research through discussion of the following:

- a) implementation of the digitizing test facility;
- b) the use of image edge descriptions produced using this facility and from an automated process [Marimont 1982] in synthesizing rules for stereo matching;
- c) examination of Orthogonal Trihedral Vertex (OTV) inference rules;
- d) development of a system for registration of image pairs;
- e) analysis of stereo imagery with an automated stereo process.

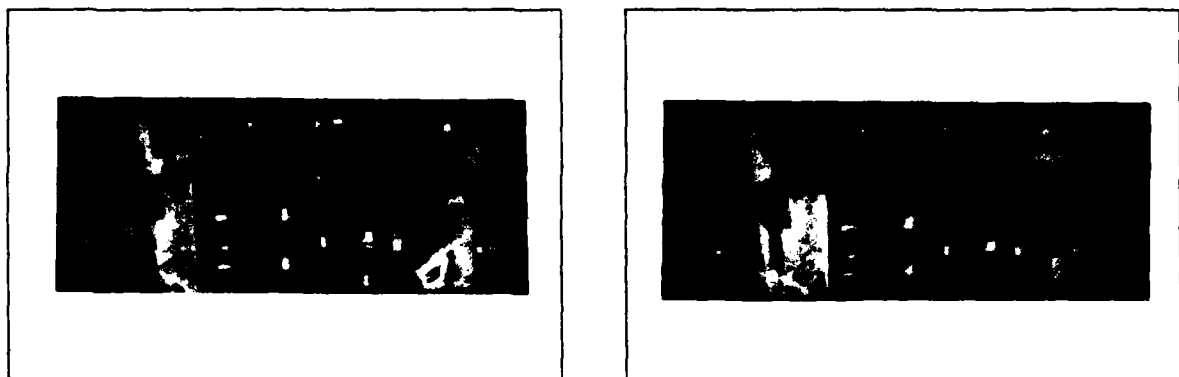
2: Digitizing Facility

2.1 Background

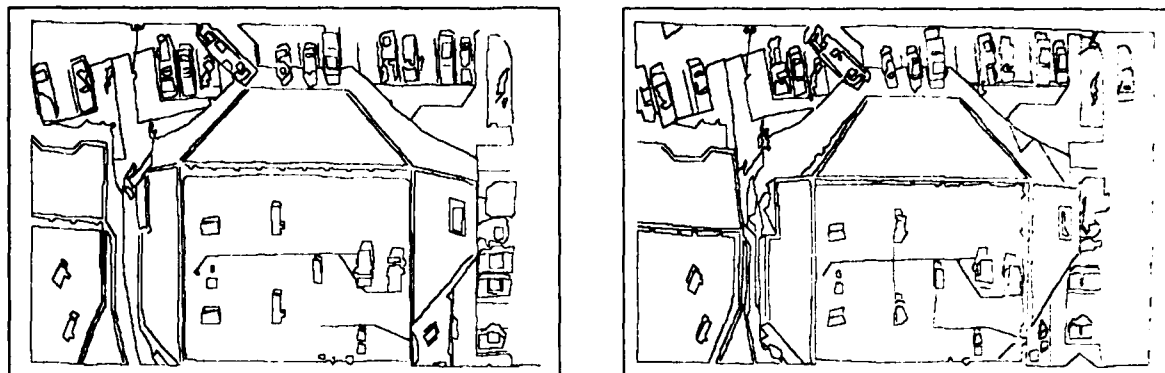
Our approach to rule development begins with hand synthesized and some automatically generated edge data. We have systems for the automatic generation of edge data (*i.e.* [Marimont 1982]). This data, extracted from a sufficiently wide selection of imagery types, gives good insight into the current capabilities of automated processes. Automated processes, however, are not able presently to give as meaningful a description of an image as we would like, and have not been designed to provide the aggregated abstractions research systems ([Lowe 1982]) will be soon supplying. To bridge this inadequacy, we work with both automatically generated data (the current state-of-the-art), and hand generated data (representative of the next generation of edge analysis processes). The hand generated data is obtained from a manually operated digitizing tablet. We have written a graphics-based digitizing and editing system to run with a GTCO tablet in producing these image descriptions. Section 6 lists instructions for the use of this program with the bitpad (GTCO tablet), and section 9 contains a source listing of the program.

2.2 Imagery Analysis with the Tablet

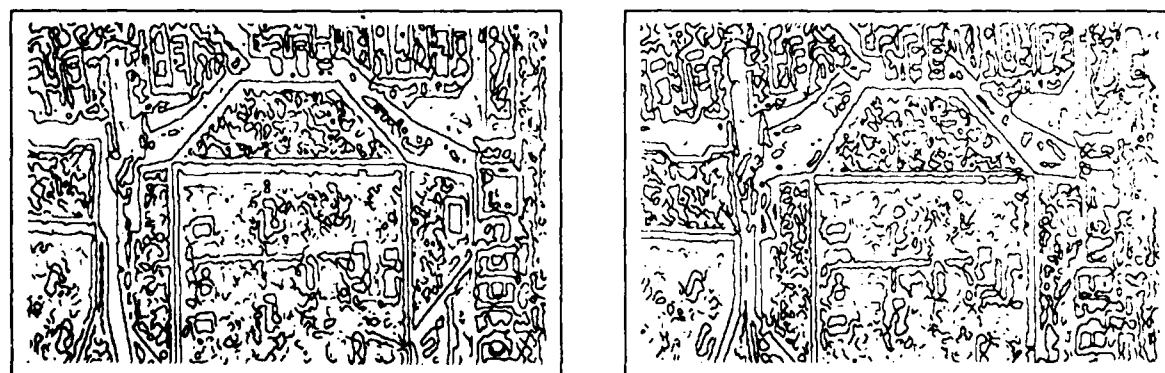
Figure 2-1 below shows an image pair of a building complex (referred to as the Sacramento imagery). Figure 2-2 shows the results of bitpad edge extraction on these images. Figure 2-3 shows the results of the Marimont operator [Marimont 1982] on the image pair. Manually generated edge data was produced using this facility for the analysis of rule synthesis of section 3. It was also used to digitize the building data of figures 2-1 for input to the OTV inference process, as figure 3-1.



Sacramento Imagery
Figure 2-1



Manually Extracted Edges
Figure 2-2



Automatically Produced Edges
Figure 2-3

3: Inference and Modelling

3.1 Introduction

We have been addressing inference of matching rules and the use of model-based analysis both with theoretical analyses and with hand and automated analyses of specific matching strategies; the latter applied to both real and synthesized imagery examples.

We have obtained extended edge data from hand and automated processing for use in synthesis of matching rules. Results from earlier work on OTV analysis (orthogonal transform vertices) have been exploited, and a demonstration of the use of such a rule for shape inference and in constraining search for correspondence has been prepared. Other funding has supported research in representation of generic structures. We have taken examples from this model-based research to produce ground and aerial views of a building complex, and have used this, as well as other data, in rule synthesis.

3.2 Geometric Modelling and Computer Vision

3.2.1 – Modelling, prediction and interpretation

Of course, one of the primary goals of research in computer vision is the development of systems that can recognize and locate objects in images. In order to identify such an object, it is clearly necessary to have some description of its characteristics that can be detected in an image. A *representation* of an object is the form this description takes.

One approach to representation is to provide the system with three-dimensional models of objects. Rotation of these models will allow objects to be observed, conceptually, from differing viewpoints. If parameters in a particular model are allowed to vary it is possible to have that single model represent a whole class of objects; constraining the parameters functions to delimit sub-classes. Further model manipulations, such as partitioning and projection, can be used to aid in mapping model to imagery data. The information contained in such object models may be used to determine possible interpretations of image features (*e.g.*, edges, ribbons, corners) and to provide feedback to predict the locations of such features in an image.

ACRONYM [Brooks 1981] is a three-dimensional rule-based modelling/vision system developed here at Stanford that provides, among other things, such feature prediction, model manipulation, and image interpretation. The rule-base operates on the models and on the sensed data to accomplish scene interpretation. Such a rule-based approach has been shown to be an effective form for constraint and search implementation, and allows easy modification and addition of new rules without the need of altering the underlying code.

Our group's intention over the next few years is to build a rule-based stereo system operating within ACRONYM whose functioning will include model-based prediction. Working toward this,

we have been carrying out experiments on scene inference and model-based prediction that will lead to a repertoire of stereo matching rules.

3.2.2 – Models and stereo matching

One of the major difficulties in determining stereo correspondence is in dealing with the large number of matches that are possible. Solution is generally found by search through a large parameter space, where possible correspondences are limited by geometric or photometric constraints. Search can be reduced even more dramatically by endowing the matcher with broad domain specific and domain independent knowledge. Such knowledge can be rule-based and model-based. Our proposition here is that the three-dimensional information in object models, along with inference and prediction mechanisms, can be used to interpret features in image pairs. These interpretations can then be used as filters to constrain the matching. We demonstrate this notion with the example of Orthogonal Trihedral Vertices, often referred to as cube corners or OTVs. Other rules synthesized from analysis of both manually extracted and automated edge processes follow.

The work on cube corners points to additional usefulness for a model-based approach. OTV orientation analysis (from matches across pairs of views) yields almost complete solution for camera parameters; constraints on sizes (again, from rules and models) could complete the camera solution. But the orientation information yielded by a match of a pair of vertices is valid only if the vertex is a cube corner; thus it is necessary to be able to distinguish between vertices that are cube corners and those that are not. If the models contain sufficient information to identify cube corners, then the problem of determining cube corners independently of the identification process is eliminated. In fact, both the search for cube corners and the search for identification are likely to be reduced when they are combined.

3.2.3 – OTV rule-based analysis

OTV theory

In cultural scenes, we find a large number of interior and exterior corners of cubes – typically when two walls at right angles meet the roof or the floor. The importance of utilizing this common structural element – the Orthogonal Trihedral Vertex (OTV) – has been emphasized earlier [Liebes 1981]. Since they provide a very tight constraint – the three edges are mutually orthogonal in space – it is possible to calculate the three dimensional orientations given the projections in the image. This can be done for both orthographic and perspective viewing.

If the eye is assumed to be focussed on the vertex of the cube corner, perspective can be ignored and the projection of a cube corner in XYZ space will simply be its orthogonal projection on the XY plane. Suppose that some 3 - star has angles between its rays a , b and c and also that the rays are represented by the unit vectors v_1 , v_2 , v_3 . We are interested in detecting whether there

are three vectors in XYZ space, which are mutually orthogonal and project, respectively to v_1 , v_2 , v_3 .

Since projection is accomplished by dropping the z -component, any 3 such vectors must be of the form $v_1 + \lambda_1 z$, $v_2 + \lambda_2 z$, and $v_3 + \lambda_3 z$ where z is the unit vector in the z -direction.

Requiring mutual orthogonality implies that the dot products of these vectors in pairs be zero. From these conditions and some simple manipulations we can calculate the formulas for

$$\lambda_1 = \pm \sqrt{-\frac{(\cos a)(\cos c)}{(\cos b)}}, \quad \lambda_2 = \pm \sqrt{-\frac{(\cos a)(\cos b)}{(\cos c)}}, \quad \lambda_3 = \pm \sqrt{-\frac{(\cos c)(\cos b)}{(\cos a)}}$$

Hence solutions exist if

- a) $\cos a$, $\cos b$, $\cos c$ are all non-zero and
- b) either one or three of $\cos a$, $\cos b$, $\cos c$ are negative, so that the quantities under the square root sign are positive.

These results were first derived in [Perkins 1968].

Thus we have a way of both eliminating false candidates for being OTVs and finding the 3-D orientations of valid OTV's. This algorithm has been implemented and run on data from the digitizing tablet.

OTV with/from models

Our analysis begins on both images, processing bottom up on the two images separately. As the rule system identifies likely OTVs in images (from its models), it proceeds to match them. The system should already have a tentative identification of the buildings containing the OTVs, so there should be relatively few possible matches at this point. Only OTVs that could be the same point on the same object need be compared. The analysis results in depths of matched objects, for all those objects having OTVs.

This requires that the modelling system handle point elements, and that it include both:

- inferring OTVs from models (volumes);
- accessing OTVs stored explicitly with the models.

3.3 Rule Synthesis

3.3.1 - Inference rules

We continue with the development of inference rules. This work is a logical extension of previous work [Binford 1981, Lowe 1982] done at Stanford in developing rules for inferring surface information from a single view. General assumptions about illumination, object geometry, the imaging process etc. have been used to derive rules for making specific inferences. For stereo vision Arnold and Binford [Arnold 1980] have developed conditions on correspondence of edge and surface intervals. We divide our rules into two categories: monocular rules, which enable surface inference from a single view; and stereo rules, which facilitate cross-image matching.

3.3.2 - Monocular and stereo rules.

1. Monocular rules - Rules which have been developed for inferences from monocular views can be utilised to provide a partial 3-dimensional interpretation which directs search in the second view. This category includes the rule for interpretation of Orthogonal Trihedral Vertices.

Another example is the T-junction rule [Binford 1981] which states that *'In absence of evidence to the contrary, the stem of a T is not nearer than the top, i.e. is coincident in space or further away'*. Application of this rule gives a set of nearer/farther relations. A hypothesized correspondence of edges which leads to inconsistent conclusions from the two views can be pruned from the search.

An image line which is straight must be the image of a straight space curve unless the curve is planar and the observer is coincidentally aligned with the plane of curvature. This enables us to dismiss correspondences between straight edges in one view and curves in the other view. If two image curves are projectively consistent with parallel, we assume they are images of curves which are parallel in space. That implies that their images in the other view would be parallel i.e. parallels map to parallels.

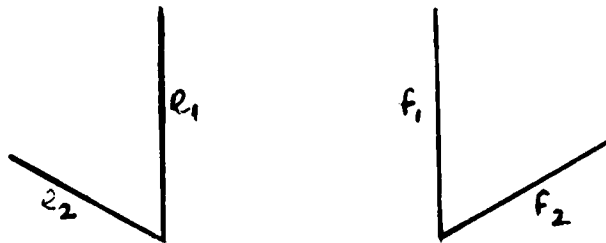
As these examples illustrate, most of the rules in [Binford 1981, Lowe 1982] and others developed by Malik and Binford have as direct corollaries stereo rules for checking the legality of a match. They can even direct the search process.

2. Stereo Rules – these are rules which have been derived from the stereo imaging process, and are a function of the imaging geometry.

An example rule in this class, which has long been used for finding stereo correspondences, is the epipolars rule – corresponding points must lie on corresponding epipolar lines. These rules have inherently no monocular analogs. Here are a few:

- a) Horizontal planes in one view get mapped to horizontal planes in the other view.
- b) Use of projective and quasi-projective invariants. This has not been examined in detail. Duda and Hart[Duda 1973] devote a chapter to this topic which has not really been exploited in stereo work.
- c) Conditions on correspondence of edges and surface intervals[Arnold 1980].
- d) Surface Occlusion rules:

Surfaces visible in one view can be occluded in the other view. We are interested in the conditions when this takes place. The basic idea is that if we cross a surface, an obscuration of edge occurs. A left surface visible in a right view is visible in the left view unless there is obscuration by a tall object. Similarly a right surface visible in a left view will be seen unless obscured by a tall object. These surface-obscuration rules can be formalized by the cross-product rule:

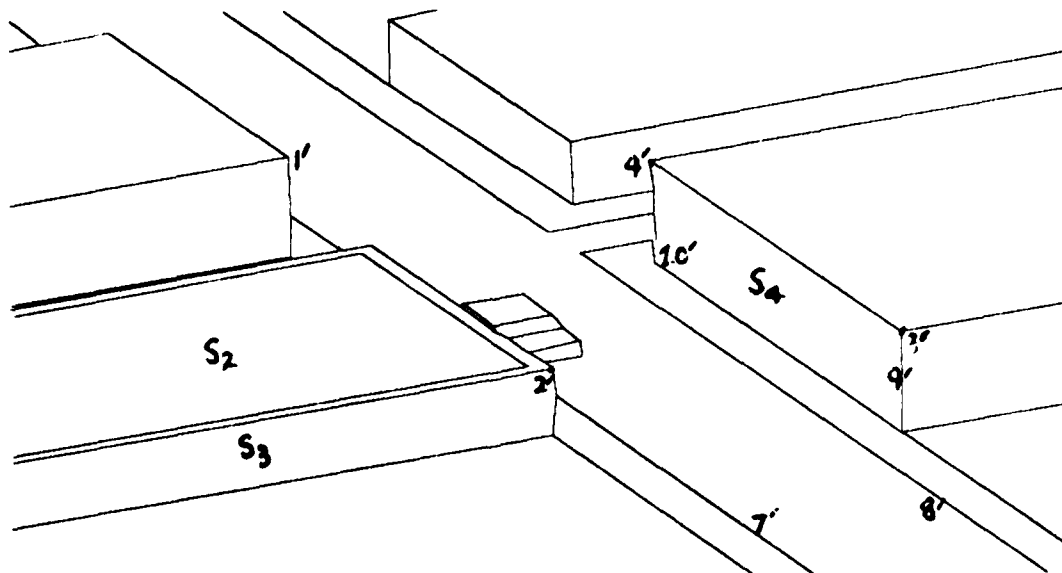


For the hypothesized edge match e_1 with f_1 and e_2 with f_2 , we compute the Z-component of the vector cross-product in the left image pair and the right image pair. If the z-components have opposite signs, we are seeing opposite sides of the surface. That implies that the object is not opaque.

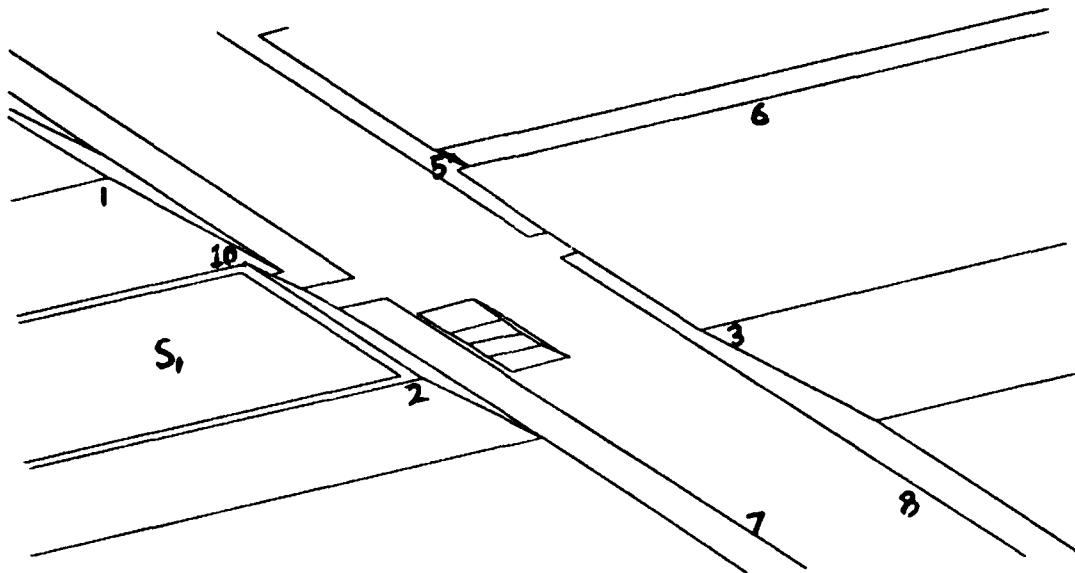
3.3.3 - Use of inference rules in a test analysis

Our preliminary results indicate good potential for the success of this approach. On hand simulations with line drawings of stereo pairs, the rules helped narrow down the choices considerably.

Consider the imagery shown in figures 3-1 and 3-2. Figure 3-1 is the right view and 3-2 the left view. Vertices 1, 2, 3 are orthogonal trihedral vertices. Using the formulae developed earlier, we can find the 3-D orientations of the edge vectors. These can be matched with the 3-D orientations of $1'$, $2'$, $3'$ to obtain a registering of these vertices when combined with the epipolar constraint. All OTV's in one view need not be visible in the other i.e. $4'$. Of the monocular constraints, the other major constraints which can be seen here are the T-junction rule and the parallels rule. In figure 3-2 edge 5 is behind edge 6. Edges 7 and 8 are parallel and so are $7'$ and $8'$. A match of 8 with $9'$ would not be accepted. Surfaces S_1 and S_2 are both horizontal planes (as can be deduced from the OTV analysis) and can be matched. Surface S_3 is not horizontal. Here of course, this does not provide any new information. Surface S_4 being a left face in a left view is not guaranteed to be visible in the other view - as in fact it is. The cross-product rule could be used to dismiss a match between 10 and $10'$.



Description of Left Image of Stereo Pair
Figure 3-1



*Description of Right Image of Stereo Pair
Figure 3-2*

4: Image Registration

4.1 Introduction to Epipolar Geometry

The search process in automated stereo mapping can be greatly restricted, and computation times significantly reduced, if information is available relating the relative camera geometries of a stereo pair. Often this information is available in the reconnaissance data (or at least a rough approximation to it). Other manual and automated schemes have been devised to provide the information when it is not present with the imagery ([Gennery 1980], [Hallert 1960]). This camera geometry information allows establishing epipolar correspondence of lines across images. When this has been done, search in one image for match points of a feature in the other image can be constrained along a single vector. More generally, any features lying along a particular vector in the one image may be found along a single vector in the other image. These image plane vectors are termed epipolar lines. Corresponding vectors are termed corresponding or conjugate epipolar lines.

In this section we detail an algorithm for determining conjugate epipolar lines in a set of imagery for which such camera geometry information is not explicitly available. Here, we rely upon an operator to select corresponding points in the two images. The system automatically improves the resolution of the correspondence through Fourier interpolation over a match window [Gennery 1980]. The set of such points is taken by an automated camera solver to produce the needed geometric information. This point selection is done with pan/zoom cursor control on a graphics device. If the camera information is available (as, for example, from reconnaissance data), then the point matching phase may be omitted (although this provision has not been enabled in the current system). Equally, rough camera geometry information, if available, may be used to partially automate the point selection phase, although again this is not implemented here. [Gennery 1980] and [Moravec 1980] have implemented totally automatic camera solvers in their stereo matching systems. Our next improvement to this system will be to incorporate the image sampling and feature matching of the [Gennery 1980] system, removing the need for manual point selection.

4.2 Glossary of Terms

Given two cameras C_1 and C_2 with origins θ_1 and θ_2 and focal planes P_1 and P_2 , we call:

Bundle of lines: A family of lines containing a common point.

Epipolar coordinates of a point: The number of the epipolar line it belongs to, and its distance to a fixed reference, like the epipole if it exists.

Epipolar direction: The direction of all epipolar lines if they are parallel.

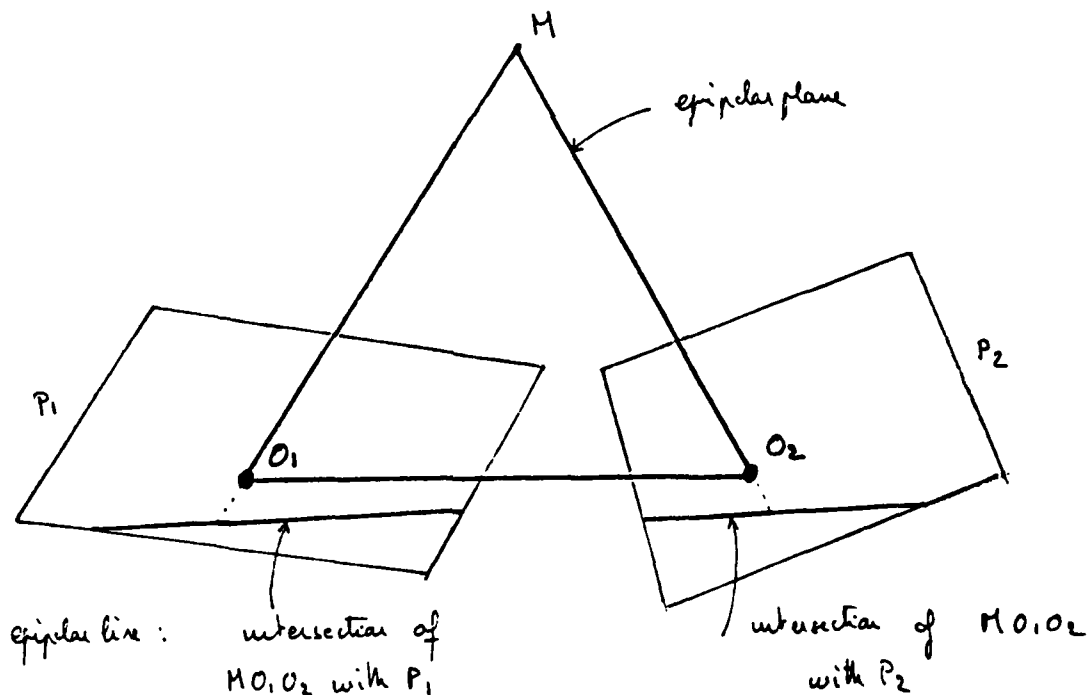
Epipolar line: The intersection of an epipolar plane with a focal plane. Alternate definition: the image in one camera of the pre-image of a point in the other camera's focal plane.

Epipolar plane: Any plane containing the two camera centers θ_1 and θ_2 .

Epipolar space: A space where the coordinates are the epipolar coordinates. In this space, a horizontal line is an epipolar line, and the epipole, if it exists, is a whole vertical line.

Epipole: The intersection, if it exists, of all epipolar lines in a focal plane.

Conjugate epipolar lines: the intersections of an epipolar plane with the two focal planes.



Epipolar Geometry
Figure 4-1

4.3 Background Theory

Given two stereo images P_1 and P_2 (the content of the focal planes P_1 and P_2 of the cameras), and two lines L_1 and L_2 contained in P_1 and P_2 , in general every point of L_1 maps to a line segment in P_2 , and there is no particular relationship between the line segments mapping to different points.

Fundamental property:

Every point in L_1 will map to a line segment contained in the same line L_2 if and only if L_1 and L_2 are a pair of conjugate epipolar lines.

Epipolar Geometry:

The family of epipolar lines in a focal plane is:

Either

- a) a set of parallel lines having a common epipolar direction,

or

- b) a bundle of lines, the intersection of which is the epipole.

4.4 Requirements of the System

Given a pair of stereo images, we want to:

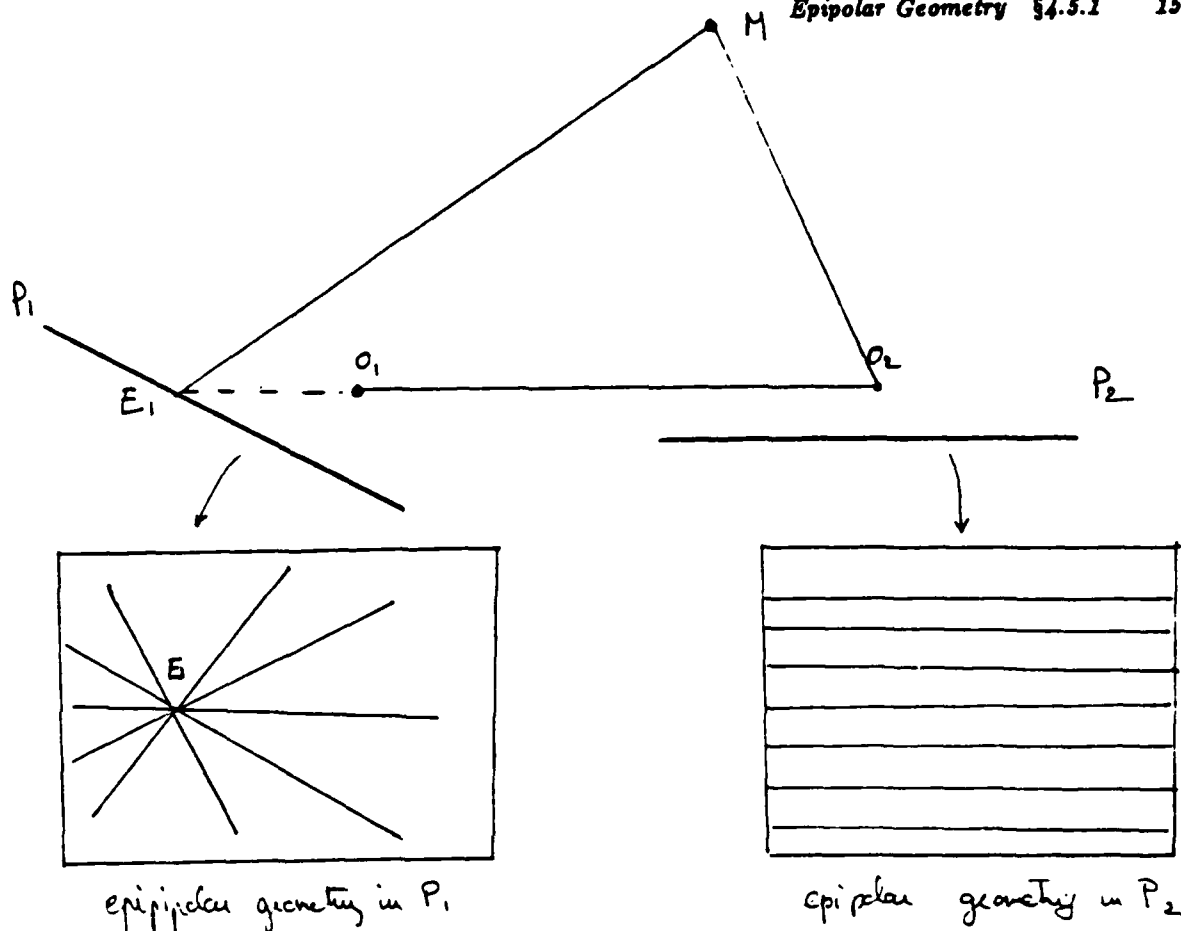
- 1) identify the kind of epipolar geometry present in the images;
- 2) explicitly show the epipolar lines belonging to each image;
- 3) for each image, compute the parameters which relate the original coordinates to the epipolar coordinates;
- 4) construct the image transforms in epipolar space.

Prior to these 4 steps, we will need to solve for the cameras, that is, to determine the 5 parameters describing their relative orientation. A procedure developed at Stanford [Gennery 1980] is used for this. We proceed as above, using simple analytic geometry for our calculations.

4.5 Algorithm Used

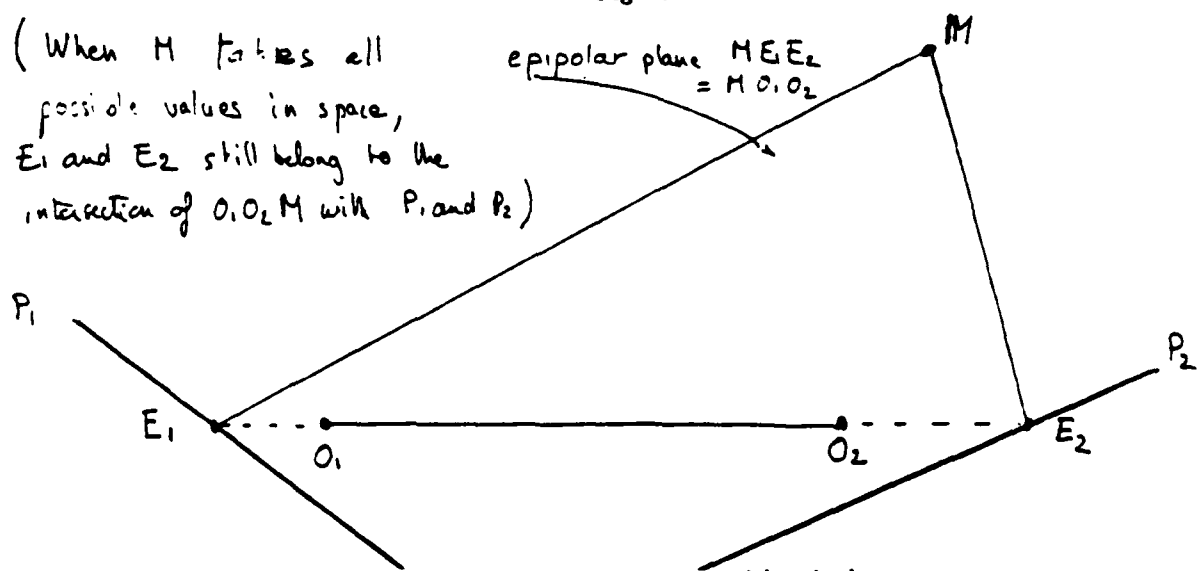
4.5.1 - Camera registration output

Each camera is viewed as a referential (θ_i, x, y, z) , $i \in \{1, 2\}$. The registration procedure yields *azimuth*, *elevation*, *pan*, *tilt*, and *roll* of one camera with respect to the other. From there, we compute:



Top view of a situation with only one epipole
Figure 4-2

(When M takes all possible values in space, E_1 and E_2 still belong to the intersection of $O_1 O_2 M$ with P_1 and P_2)



Top view of a situation with epipoles
Figure 4-3

- 1) the rotation matrix R between the two referentials:

$$R = \begin{pmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{pmatrix}$$

- 2) the translation unit vector t , the components of which are:

$$\begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix} \text{ in the base } \theta_1xyz, \quad \begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix} \text{ in the base } \theta_2xyz$$

Note that the magnitude of the translation vector cannot be determined from a pair of images.

4.5.2 - Epipolar geometry determination

The focal planes P_i are planes parallel to $\theta_i xy$, intersecting $\theta_i z$ at $z = f_i$, the focal distance. There is an epipole in plane P_i if and only if the translation vector intersects this plane, that is, if and only if its third component is not zero.

We thus determine the case we are working with:

- if $\gamma \neq 0$ and $\nu \neq 0$, there are two epipoles: CASE 1
- if $\gamma \neq 0$ and $\nu = 0$, there is one epipole E_1 : CASE 2
- if $\gamma = 0$ and $\nu \neq 0$, there is one epipole E_2 : CASE 3
- if $\gamma = 0$ and $\nu = 0$, there are no epipoles: CASE 4

Remarks:

- a) $\gamma = 0$ is replaced in the code by $|\gamma| < \text{threshold}$, where threshold is chosen as a function of the arithmetic precision of the machine: if we had infinite precision, then we could consider every case as being case 1. Here threshold = .0001 was found to be a good estimate.
- b) Most image pairs will belong to the first case, with γ and ν of the order of .1. The epipoles exist, are outside the picture frame, and, for the images worked with to date, tend to be at a distance of about 10 times the picture dimension.

4.5.3 – Epipoles and epipolar directions

If the epipole E_i exists, it is the extremity of the vector collinear to the translation vector, with a third component equal to f_i . If it does not, then the translation vector is the epipolar direction. Hence:

$$\text{Case 1: } E_1\left(\frac{\alpha f_1}{\gamma}, \frac{\beta f_1}{\gamma}\right) \quad E_2\left(\frac{\lambda f_2}{\nu}, \frac{\mu f_2}{\nu}\right)$$

$$\text{Case 2: } E_1\left(\frac{\alpha f_1}{\gamma}, \frac{\beta f_1}{\gamma}\right) \quad V_2(\lambda, \mu)$$

$$\text{Case 3: } V_1(\alpha, \beta) \quad E_2\left(\frac{\lambda f_2}{\nu}, \frac{\mu f_2}{\nu}\right)$$

$$\text{Case 4: } V_1(\alpha, \beta) \quad V_2(\lambda, \mu)$$

4.5.4 – Epipolar line calculation

4.5.5 – CASE 1: two epipoles

a) theory

Let $M_1(x_1, y_1, z_1)$ be a point in P_1 . E_1M_1 defines an epipolar line in P_1 , and the corresponding E_2M_2 defines the conjugate epipolar line in P_2 . The plane $(E_1, \theta_1, \theta_2, E_2, M_1, M_2)$ contains the translation vector t and E_1M_1 . Its normal is $E_1M_1 \times t$. The normal of P_2 is θ_2z . Hence the intersection of the two planes is given by the vector:

$$\theta_2z \times (E_1M_1 \times t) = (\theta_2z \cdot t)E_1M_1 - (\theta_2z \cdot E_1M_1)t$$

and E_2M_2 is collinear to this vector. Suppose that in θ_1xyz , $E_1M_1: (x_1, y_1, 0)$. In terms of components in θ_2xyz :

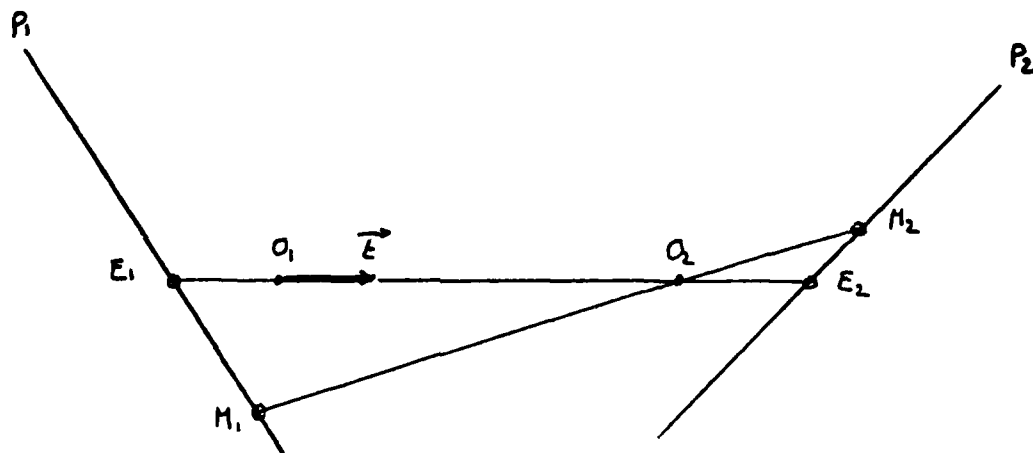
$$\theta_2z = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}, \quad t = \begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}, \quad E_1M_1 = \begin{pmatrix} x'_1 \\ y'_1 \\ z'_1 \end{pmatrix} = \begin{pmatrix} r_{11}x_1 + r_{12}y_1 \\ r_{21}x_1 + r_{22}y_1 \\ r_{31}x_1 + r_{32}y_1 \end{pmatrix}$$

$$E_2M_2 \text{ is collinear to } \begin{pmatrix} \nu x'_1 - \lambda z'_1 \\ \nu y'_1 - \mu z'_1 \end{pmatrix} = \begin{pmatrix} x_1(\nu r_{11} - \lambda r_{31}) + y_1(\nu r_{12} - \lambda r_{32}) \\ x_1(\nu r_{21} - \mu r_{31}) + y_1(\nu r_{22} - \mu r_{32}) \end{pmatrix}$$

If we let A be the matrix:

$$\begin{pmatrix} \nu r_{11} - \lambda r_{31} & \nu r_{12} - \lambda r_{32} \\ \nu r_{21} - \mu r_{31} & \nu r_{22} - \mu r_{32} \end{pmatrix}$$

Then we can write $E_2 M_2 = A E_1 M_1$ where $E_1 M_1$ is in base $\theta_1 xy$ and $E_2 M_2$ is in base $\theta_2 xy$.



Case 1
Figure 4-4

b) algorithm

Let N_1 be the number of epipolar lines that we want to determine. Each epipolar line is uniquely determined by the angle it makes with the x -axis. Let θ be this angle. Given k , the epipolar line number, $0 \leq k \leq n_1 - 1$, how can we determine θ ? If θ_0 and θ_1 are the lower and upper limits between which θ is allowed to vary, and $\theta_2 = \frac{(\theta_1 - \theta_0)}{N_1}$, then we will choose the middle of each interval: $\theta = \theta_0 + (k + .5)\theta_2$. But what are θ_0 and θ_1 ? We have to distinguish between three cases:

- The epipole is in the picture (very unlikely). Then θ can vary between 0 and 2π radians;

- The epipole is outside the image: there is a minimum and maximum angle under which the image is seen from this point. If we choose these angles in $[0, 2\pi]$, then most of the time every $\theta \in [\theta_0, \theta_1]$ will define a valid epipolar line in P_1 ;
- The exception from above is when the epipole is left of the image but on a same vertical level: then $[\theta_0, \theta_1]$ cannot be connected and still included in $[0, 2\pi]$. In this case we will choose the angles in $[-\frac{\pi}{2}, \frac{\pi}{2}]$.

Then L_1 will be defined by the point E_1 and the vector $V_1(\cos\theta, \sin\theta)$, and L_2 is defined by E_2 and $V_2 = AV_1$.

4.5.6 – CASE 2: one epipole E_1

a) theory

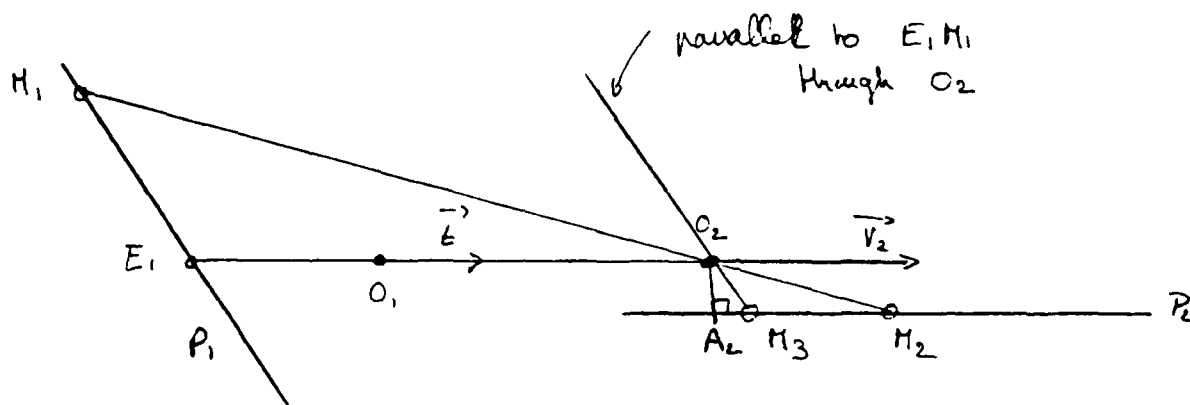
Given an epipolar line $\frac{L_1}{E_1 M_1}$, we already know that the corresponding epipolar line L_2 in P_2 is collinear to the vector $t = V_2(\lambda, \mu)$. Hence we just need to find a point belonging to L_2 . Clearly, L_2 is the intersection of P_2 with the plane (E_1, M_1, θ_2) . Thus any line contained in this plane will intersect P_2 at a point contained in L_2 . In particular, consider the parallel to L_1 driven through θ_2 . It intersects P_2 , thus L_2 , at M_3 such that, in base θ_2xyz :

$$E_1 M_1 = \begin{pmatrix} r_{11}x_1 + r_{12}y_1 \\ r_{21}x_1 + r_{22}y_1 \\ r_{31}x_1 + r_{32}y_1 \end{pmatrix}, \quad \text{hence} \quad \theta_2 M_3 = \begin{pmatrix} f_2 \frac{(r_{11}x_1 + r_{12}y_1)}{r_{31}x_1 + r_{32}y_1} \\ f_2 \frac{(r_{21}x_1 + r_{22}y_1)}{r_{31}x_1 + r_{32}y_1} \\ f_2 \end{pmatrix}$$

b) algorithm

In the same way as in case 1, we define $L_1(E_1, V_1)$ where $V_1(x_1 = \cos\theta_1, x_2 = \sin\theta_2)$. Then L_2 is defined by (M_3, V_2) , where the coordinates of M_3 are

$$\left(f_2 \frac{r_{11}x_1 + r_{12}y_1}{r_{31}x_1 + r_{32}y_1}, f_2 \frac{r_{21}x_1 + r_{22}y_1}{r_{31}x_1 + r_{32}y_1} \right)$$



Case 2
Figure 4-5

4.5.7 - CASE 3: one epipole E_2

a) theory

Let an epipolar line in P_1 be defined by the translation vector $t = V_1$ and by a point M_1 we pick. In P_2 , L_2 goes through E_2 and is collinear to a vector E_2M_2 , intersection of P_2 with the plane (θ_2, E_2, M_1) . This plane is orthogonal to $\theta_2 M_1 \times t$ and P_2 is orthogonal to $\theta_2 z$. Hence the intersection is collinear to $\theta_2 z \times (\theta_2 M_1 \times t)$

$$\begin{aligned} \text{since } \theta_2 M_1 &= \theta_2 \theta_1 + \theta_1 M_1 \\ &= kt + \theta_1 M_1, \end{aligned}$$

$$\theta_2 M_1 \times t = \theta_1 M_1 \times t,$$

$$\text{and } \theta_2 z \times (\theta_2 M_1 \times t) = (\theta_2 z \cdot t) \theta_1 M_1 - (\theta_2 z \cdot \theta_1 M_1) t.$$

Suppose $\theta_1 M_1 : (x_1, y_1, f_1)$ in $\theta_1 xyz$. Then in $\theta_2 xyz$:

$$\theta_2 z = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}, \quad t = \begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}, \quad \theta_1 M_1 = \begin{pmatrix} x'_1 \\ y'_1 \\ z'_1 \end{pmatrix} = \begin{pmatrix} r_{11}x_1 + r_{12}y_1 + r_{13}f_1 \\ r_{21}x_1 + r_{22}y_1 + r_{23}f_1 \\ r_{31}x_1 + r_{32}y_1 + r_{33}f_1 \end{pmatrix}$$

$E_2 M_2$ is thus collinear to:

$$\begin{pmatrix} \nu x'_1 - \lambda z'_1 \\ \nu y'_1 - \mu z'_1 \end{pmatrix} = \begin{pmatrix} x_1(\nu r_{11} - \lambda r_{31}) + y_1(\nu r_{12} - \lambda r_{32}) + f_1(\nu r_{13} - \lambda r_{33}) \\ x_1(\nu r_{21} - \mu r_{31}) + y_1(\nu r_{22} - \mu r_{32}) + f_1(\nu r_{23} - \mu r_{33}) \end{pmatrix}$$

Hence, if we let A be the same matrix as in CASE 1 and OF3 be the offset matrix:

$$\begin{pmatrix} \nu r_{13} - \lambda r_{33} \\ \nu r_{23} - \mu r_{33} \end{pmatrix}$$

Then we have: $E_2 M_2 = A \theta_1 M_1 + OF3$

Where $\theta_1 M_1$ is in base $\theta_1 xy$ and $E_2 M_2$ is in base $\theta_2 xy$

b) algorithm

Now, how do we pick M_1 in the first place? We want a set of N_1 equally spaced epipolar lines, and it appears convenient to pick points on the axes. If the epipolar lines are more horizontal, or the image stretched in height, then we will pick N_1 equally spaced points on the vertical axis, suitably located to cover the entire image. If the epipolar lines are more vertical or the image more stretched in width, then we pick them on the horizontal axis. Let L_x, L_y be the picture dimensions and (V_x, V_y) the epipolar direction:

If $V_x L_y < V_y L_x$, and $V_y < 0$, we pick $y_1 = (L_x | \frac{V_y}{V_x} | + L_y) (\frac{K+0.5}{N_1})$

If $V_x L_y < V_y L_x$, and $V_y > 0$, we pick $y_1 = (L_x | \frac{V_y}{V_x} | + L_y) (\frac{K+0.5}{N_1}) - L_x \frac{V_y}{V_x}$

If $V_y L_x < V_x L_y$, and $V_y < 0$, we pick $x_1 = (L_y | \frac{V_x}{V_y} | + L_x) (\frac{K+0.5}{N_1})$

If $V_y L_x < V_x L_y$, and $V_y > 0$, we pick $x_1 = (L_y | \frac{V_x}{V_y} | + L_x) (\frac{K+0.5}{N_1}) - L_y \frac{V_x}{V_y}$

Then we proceed as indicated above:

$$L_1(M_1, V_1 = t) \text{ is matched with } L_2(E_2, V_2 = F_2 M_2).$$

4.5.8 – CASE 4: no epipoles**a) theory**

Let an epipolar line in P_1 be defined by the translation vector $t = V_1$ and by a point M_1 we pick. In P_2 , L_2 goes through the image of M_1 , that is the extremity of a vector collinear to $\theta_1 M_1$ and whose third component is f_2 . In base $\theta_1 xyz$, $\theta_1 M_1 : (x_1, y_1, f_1)$. In base $\theta_2 xyz$:

$$\theta_1 M_1 = \begin{pmatrix} r_{11}x_1 + r_{12}y_1 + r_{13}f_1 \\ r_{21}x_1 + r_{22}y_1 + r_{23}f_1 \\ r_{31}x_1 + r_{32}y_1 + r_{33}f_1 \end{pmatrix} \quad \theta_2 M_2 = \begin{pmatrix} f_2 \frac{r_{11}x_1 + r_{12}y_1 + r_{13}f_1}{r_{31}x_1 + r_{32}y_1 + r_{33}f_1} \\ f_2 \frac{r_{21}x_1 + r_{22}y_1 + r_{23}f_1}{r_{31}x_1 + r_{32}y_1 + r_{33}f_1} \\ f_2 \end{pmatrix}$$

b) algorithm

We pick points E_1 in the same manner as in case 3. Then we calculate $\theta_2 M_2$ as indicated above and we match $L_1(E_1, t)$ with $L_2(E_2, t)$.

4.6 Transform Parameters

We want to output the minimum necessary parameters to do the following transformation:

given the coordinates of one point in one image, find its coordinates in epipolar space.

We treat the problem only in CASE 1, which is the most common case encountered. For this case, we will need:

- the coordinates of the epipoles;
- the number of epipolar lines;
- the minimum and maximum angle θ_0 and θ_1 under which picture 1 is viewed;
- the minimum distances D_{1min} and D_{2min} of the epipoles to the images;
- the matrix R , or rather its inverse R^{-1} .

For example, the images of figure 5-6 have transform parameters as follows:

Case = 1

$$N = 450$$

$$E_{11} = 358755.3$$

$$E_{12} = 166509.8$$

$$E_{21} = -7765.348$$

$$E_{22} = -3509.268$$

$$\theta_0 = 3.578705$$

$$\theta_1 = 3.577792$$

$$D_{1min} = 393249.0$$

$$D_{2min} = 8521.478$$

$$R_{11}^{-1} = 430.7463$$

$$R_{12}^{-1} = 2375.517$$

$$R_{21}^{-1} = 215.9756$$

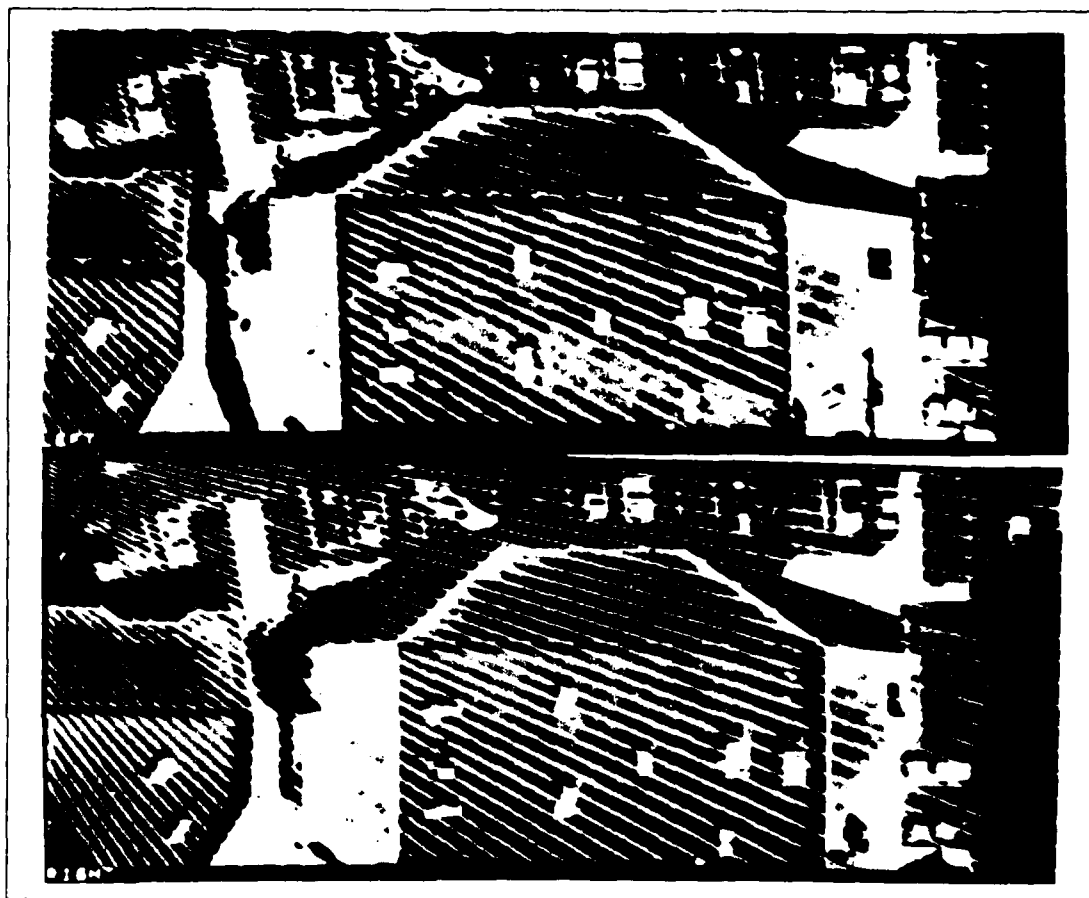
$$R_{22}^{-1} = 1075.811$$

4.7 Example of Epipolar Registration and Transformation

Figure 4-6 shows a stereo pair of a building complex. Figure 4-7 has this pair superpositioned with a set of corresponding epipolar lines. Figure 4-8 shows the imagery transformed such that epipolar lines are horizontal in the image, and conjugate epipolar lines have the same row coordinate.



Sacramento Building Image Pair
Figure 4-6



Epipolar Lines in this Imagery
Figure 4-7



Transformed Image

Figure 4-8

5: Analysis of Automated Stereo Mapping

5.1 Background

Results from our laboratory over the past few years [Quam 1971, Hannah 1974, Moravec 1980, Gennery 1980, Arnold 1980, Baker 1981, Arnold 1983], have demonstrated the possibilities of both area-based and feature-based stereo matching.

Area-based stereo matching uses windowing mechanisms to isolate parts of two images for cross-correlation. *Feature-based* stereo matching uses two-dimensional convolution operators (and perhaps grouping operators) to reduce an image to a depiction of its intensity boundaries, which can then be put into correspondence. Area-based cross-correlation techniques require distinctive texture within the area of correlation for successful operation. They break track:

- where there are ambiguous textures or featureless areas (roofs, sand and concrete);
- where the correlation area crosses surface discontinuities (at occlusions such as buildings, or thin objects (poles));
- where depth is ill-defined (such as through trees).

In general, these systems break track where there is no local correlation (zero signal, or where two images do not correspond) or where the correlation is ambiguous (where the signal is repetitive). The systems must be started manually and corrected when they break track.

Demands of mapping in cultural sites and in locales with surface discontinuity and ambiguous or non-existent texture make it essential that, if area-based analysis is to be done, it be done in conjunction with feature-based analysis. *Feature-based* analysis provides a solution to many of the problems of correlation. Principal among its advantages is that it operates on the most discriminable parts of an image: places that are distinctive in their intensity variation, and where localization is greatest. These are typically the boundaries between objects or between details on objects, or between objects and their backgrounds. The important point is that the features being put into correspondence for depth estimates are the boundaries of objects: area-based analysis is at its worst at object boundaries, yet determining boundaries can be said to be the most important part of mapping in 3-space.

Some other advantages of feature-based analysis are:

- a) *reduced combinatorics* — there are fewer features than pixels,
- b) *greater accuracy* — features can, in general, be positioned to sub-pixel precision, while area positioning precision is inversely proportional to window size, and considerably poorer, and
- c) *more realistic invariance assumptions* — area-based analysis presupposes that the *photometric* properties of a scene are invariant to viewing position, while feature-based analysis works with the assumption that it is the *geometric* properties that are invariant to viewing position.

The Baker system [Baker 1981] is the only current system that mixes these two matching modalities. We undertook in this postdoctoral work to demonstrate the capabilities of this system applied to new cultural imagery.

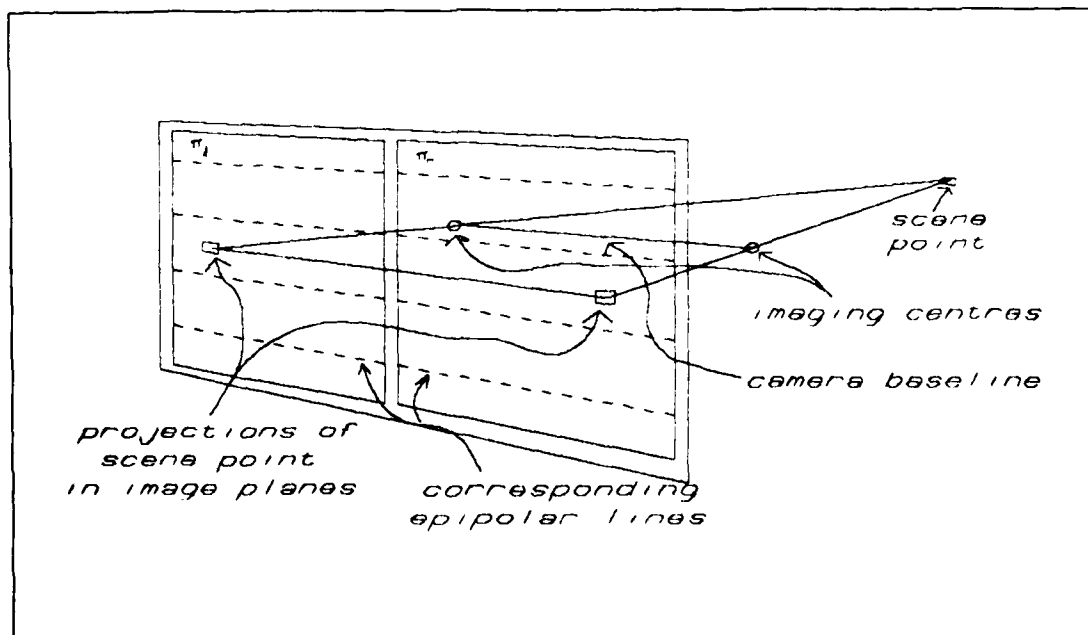
5.2 Baker System: before

In the Baker system, image *edges* are the features considered in stereo matching. These edges are located at positions in the image where a change in sign of second difference in intensity occurs. In the initial case a particular operator (one that was 1 by 7 pixels in size) measured the directional first difference in intensity at each pixel. Second differences were computed from these, and changes in sign of these second differences were used to interpolate zero crossings (i.e. peaks in first difference). Certain local properties other than *position* were measured and associated with each edge — *contrast*, *orientation*, and *intensity to either side* — and *links* were kept to nearest neighbors above, below, and to the sides. It is these properties that define an edge and provide the basis for the correspondence process.

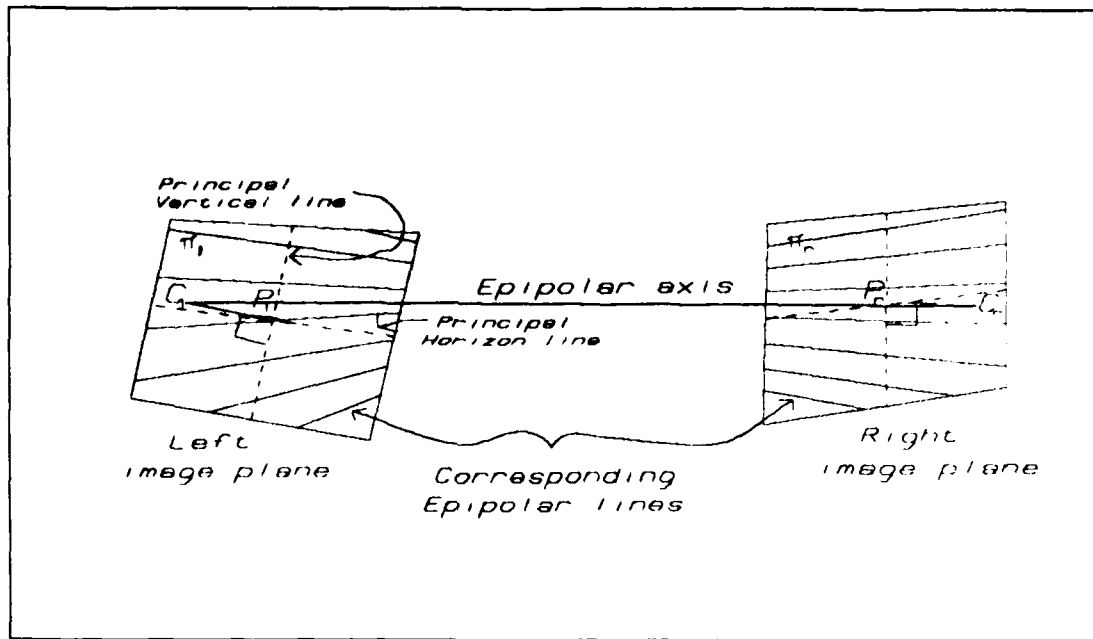
The correspondence is a search for *edge* matches across images. With no prior knowledge of the viewing situation, one could have any edge in one image matching any edge in the other. The combinatorics of a naive matching strategy clearly could be enormous. A lot of the analysis of a matching strategy goes into bounding this combinatorics and constraining the search for edge correspondences.

One of the principal constraints used in stereo analysis may be determined from a knowledge of the relative attitudes of the cameras. If two equivalent cameras are arranged with axes parallel, as shown in Figure 5-1, then they can be conceived of as sharing a single common image plane. Any point in the scene will project to two points on that joint image plane (one through each of the two lens centers), the connection of which will produce a line parallel to the baseline between the cameras. Thus corresponding edges in the two images must lie along the same line in the

joint image plane. This line is termed an *epipolar line* (see [Hallert 1960], and section 4). If the baseline between the two cameras happens to be parallel to the scanning axis of the cameras, then the correspondence only need consider edges lying along matched lines parallel to that axis in the two images. These lines are termed *conjugate*. Figure 5-1 indicates this camera geometry — a geometry which produces *collinear epipolar lines*. The algorithm described here assumed the stereo pair to have such a geometry, and if this was not the case then the appropriate transformation of the two images had to be made before any processing could be done. A less restrictive solution would be to have the correspondence process informed of the camera geometries, and have it solve for the more general epipolar situation as shown in figure 5-2. Incorporation of this capability is one of the enhancements we have made to the system over the past few months. Section 4 details the analysis for this solution.



Specialized Epipolar Geometry
Figure 5-1



General Epipolar geometry
Figure 5-2

The advantage of processing along epipolar lines is that the search for correspondence may be constrained to one dimension, along a single line-pair. It is then feasible to apply an efficient optimization process to the matching problem. The Viterbi algorithm [Forney 1973] is the optimization process used in this system. It is a dynamic programming technique used extensively in speech processing, and first used in vision research in some recent work at Control Data Corporation [Henderson 1979]. An earlier use of a dynamic programming technique for stereo matching is documented in [Gimel'farb 1972]. [Baker 1981] describes in detail the use of the Viterbi algorithm for stereo correspondence.

Other geometric and photometric constraints may be introduced both in limiting search and in bounding parameters for the evaluation function. [Arnold 1980] and [Baker 1981] provide discussions of these constraints in determining edge correspondences.

5.3 Baker System: enhancements

As stated, we undertook in this postdoctoral work to demonstrate the capabilities of the Baker system [Baker 1981] applied to some cultural scenes. Before carrying out these analyses we:

- a) enhanced the system with a capability to work with a better edge operator [Marimont 1982];
- b) enabled it to process images that are not graced with collinear epipolar geometry (*i.e.* most images);
- c) introduced an additional correspondence measure - edge extent.

To implement these enhancements required substantial redesign of the system, and redesign cycles with the Marimont process. Choosing useable data also presented difficulties, as the only imagery available was not of the correct geometry (see below). The two image pairs initially chosen (the Sacramento apartment complex and a section of some imagery of Moffett Field) proved, on closer examination, to require quite complex transformation, and could not be easily adjusted for epipolar processing. Obtaining useable data then tied the progress of this part of the demonstration to the progress of developing an image registration system.

In general, to bring imagery data into a properly transformed state could proceed in one of two ways:

- one could determine the transforms and then modify the imagery, producing an image pair having collinear epipolar geometry;
- or
- one could determine the transforms, and modify the output of an edge operator process that functions over the original imagery.

The latter is by far the superior approach, as it avoids resampling the image. This approach necessitates incorporating the transform computation into the stereo system, to follow edge finding and precede edge matching.

The second part of the stereo system's analysis is an intensity correlation process. This operates along epipolar lines as well, and clearly requires intensity information to be accessible along epipolar lines. One solution to this would be to take the original image pair and have the correlator rotate and change shape, size, and orientation as it moves around the image; this is an awkward and probably unnecessary complication. An alternative would be to access the transformed images, sampled as accurately as possible, and do the correlation in the rectangular space defined by collinear epipolar lines. The argument from edge accuracy indicated that transforming edges rather than resampling the image was the way to go; this argument from intensity correlation suggests that the resampled image can be useful.

Another implementation detail supported this use of both transformed edges and transformed imagery: it was found that the intensity information available from the Marimont process had too small a basis for useful correlation, and in fact, for transformed edges, had little relevance for the matching (it being measured not along epipolar lines). The transformed image had to be referenced again by the system to obtain more significant intensity estimates oriented along epipolar lines, and working with the image in epipolar space facilitated this.

The philosophy of the stereo matching process here had been to use edge analysis for, among other things, its higher accuracy, and to use intensity analysis for the continuity it provides. To be consistent with this, we wanted to have the highest possible accuracy for edges in epipolar space, and if sacrifice be needed for simplicity, to do it where it least degraded the analysis - in the intensity correlation. It is clear that transformed edges give higher accuracy than edges from transformed images (detectability might not change much, but localization is significantly reduced); and important simplifications could be obtained for little loss by doing the intensity correlation over the resampled image pair. This meant changes in our plans for the registration system: it had to produce not just transform information, but transformed images as well. Both forms are made available as output from the registration program described in section 4, and the enhanced Baker system uses them both. (However, the original edge finder of the stereo system has not been modified to use the transform information, and must work (at present) on the transformed images - with the limitations that brings.)

5.4 The Marimont Edge Operator

The Marimont edge operator has greater detection and reliability than the original Baker edge operator, and similar localization; earlier examples of its processing convinced us that its output would improve the quality of our stereo reconstruction. Its ability to track along zero signal areas in following zero-crossing edges leads to more coherent image descriptions. [Marimont 1982] provides details of the operator's functioning. Roughly, it works by convolving an $m \times m$ lateral inhibition function of $n \times n$ central window with an image. Zero crossings in this resultant image then indicate edges, and the edge position is determined by interpolating over the lateral inhibition surface. Section 7 details the content and format of the edge files produced by this process.

A few unanticipated problems became apparent once work with the edges was begun. One point, noted above, was that the intensity information stored at an edge (its left and right boundary values) had quite small support (a single pixel). This is in contrast with the original operator which interpolated for these values in an area 3 pixels wide and removed one pixel from the determined edge position. Another problem was that the edge connectivity produced by the Marimont system can be misleading, as figure 5-3 shows. Intensity significance was improved by sampling along epipolar lines in the transformed images. The connectivity problem has not been looked at yet.

Good connectivity is inherently difficult to achieve with zero crossing operators. Refinements to the process are being considered.

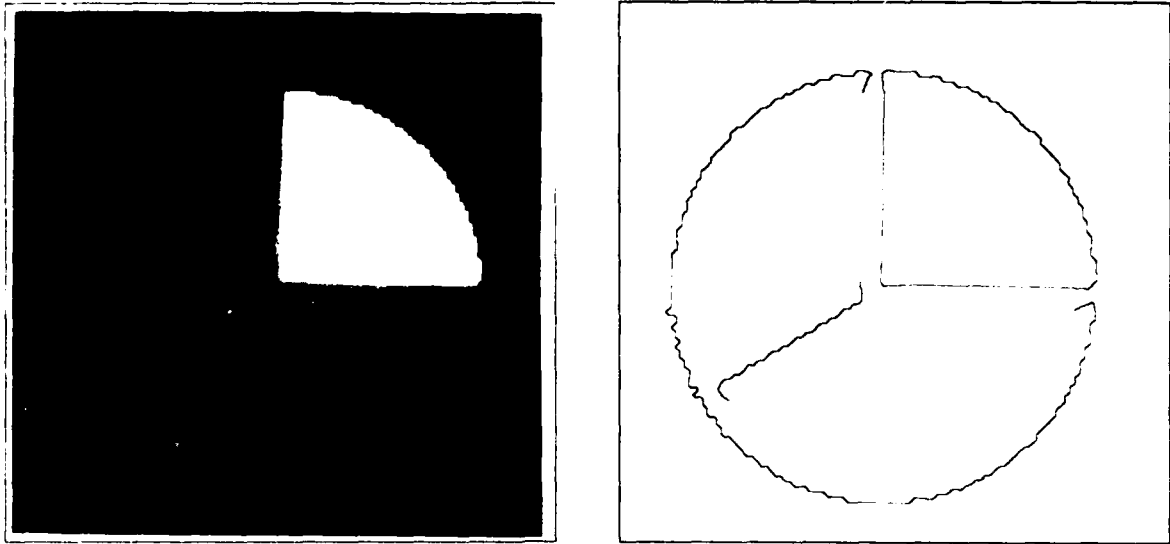


Image
Figure 5-3

The introduction of edge extent as a parameter in the dynamic programming solution was an obvious fallout from using the Marimont edges. Edges are output by that process as strings, with 2-connectedness. The maximum and minimum of some string, in transform space, is a measure of its (epipolar) extent. Prior to the use of this information the only way that global continuity entered the analysis was through a consistency enforcement relaxation process which ensured that edges connected in one view were interpreted as continuous in 3-space; all matching measures were quite local. With the modified approach, the correspondence measure is a function of (among other, more statistically based parameters) the ratio of edge extents. In particular, the likelihood of edge element a in the left image matching edge element b in the right image depends on the product of the ratios of the two upper extents (up from the edge elements) and the two lower extents (down from the two edge elements).

When image testing began with all of the above accomplished, another problem became apparent: the stereo system, bound into a machine architecture with a maximum of 256K words of memory, and always tightly wedged anyway, had grown with these changes to the point that only small portions of images could be worked on at once. Thus came to exist a windowing mechanism within the edge finding/loading and stereo matching processes.

5.5 Test Imagery

Our testing has been progressing on several sets of imagery: a synthetic image pair from Control Data Corporation, an aerial scene from the Engineering Topographic Laboratory, and a building scene of Sacramento. The latter imagery is the most relevant to the current postdoctoral contract, and we will be demonstrating the mapping system on this data. This imagery may be seen in figures 4-6 and 4-8.

6: Bitpad Instructions

6.1 Instructions for the Digitizing Tablet

6.1.1 - Introduction

The bitpad program is written in PASCAL to be run on a DEC KL-10 processor under WAITS at the Computer Science Department of Stanford University. It has an assembly code driver to handle input from the tablet over a normal RS-232 port (listing included also), and requires a graphics package available locally. Replacing this package for an intended use away from SAIL WAITS should be quite straightforward.

Locally, the bitpad may be run by typing DO TAB[S,HIB]. Figure 6 shows the digitizing tablet in use.

The initial preamble of questions deals with graphics options and line characteristics. You will usually want some sort of graphics output, so answer yes to the first question ("Want graphics output (y/n)?"). Graphics choices are DD or GOD (for later display). Say y to either or both of the questions about this. DD graphics go the Data Disc display while for viewing while you construct an edge file, while GOD graphics are for later Graphics Output Device device independent display. If you want little boxes drawn around the endpoints of lines, then answer y to ("Want boxes draw around vertices (y/n)?"). Box size refers to the size of the box to be drawn around vertices. Small is better for entry, large makes it easier to distinguish vertices from line nodes if you are trying to do deletions.

On the first digitizing pass over an image you will start directly from the bitpad; later sessions will involve adding to or editing an existing edge file. To enter an old file (or several old files), say Y to the question ("Want to read in a file (y/n)?"). This reads it in and displays it. For the moment there's a problem with reading strings into PASCAL, so it tries to read NEW.VRT[S,HIB]. If this file doesn't exist, it will give you the chance to enter another filename.. don't panic, just type in the new name.

When that file has been read in and displayed, it lets you choose another (ad infinitum). End with an answer of N (for NO) to the above question.

6.1.2 - Setting screen coordinates

Whether you've read in a file, or not, you now set up the bitpad to enter data. It asks for the TTYline of the tablet (50 is the current line number of the bitpad plug). You then define the screen area on the bitpad: select the four corners with the crosshairs (lower left, upper left, upper right, lower right) with any button, and confirm your selection by pushing button '2' ('8' says no, try for four more points).

6.1.3 - Adding segments and vertices

A 'segment' is made up of a start vertex, any number (even 0) of intermediate points, and an end vertex. Vertices may belong to any number of 'segments'. Adding vertices/points/segments is as follows:

Button: '1' defines a new vertex at the current crosshairs position, either starting a segment with it, or ending one there. '2' locates the nearest vertex (created by '1'), and begins or ends a segment there. '4' says add this point to the current segment list. '8' is a break. It lifts the pen. If it is followed by a '1' or '2', then that is all it does. If followed by a '4', it puts you in the delete cycle. If followed by another '8', you exit everything.

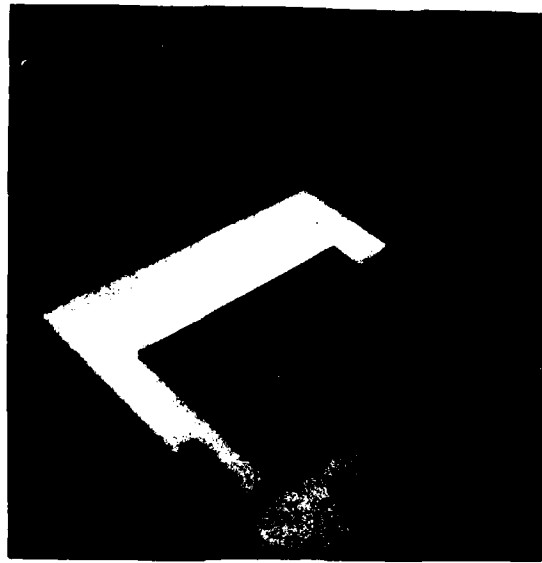
6.1.4 - Editing segments

You may enter the editor to delete segments at any point. You do this by keying '8' then '4' in the above entry loop.

To delete segments, first choose a vertex attached to the segment with '1' button. Then select either the other vertex (if there is no ambiguity) with a '1', or a point somewhere on the segment with a '4'. You then see it erased on the screen, and you push '2' to confirm that that's the one you want deleted, or '8' to say that its not the one you want deleted. Leave the delete cycle by keying '8'.

If you wish to add more to the file, run it again, and this time read in the VRT file produced on this previous pass.

At the moment, the GOD file is the sum of everything drawn on the screen during the run. To get just the current description, you have to pass the file once more through the program; making no changes, just reading it in and writing it out. Because of this, I recommend NOT producing a GOD file on the 1st through $n - 1$ st creation passes, saving it for the last run, when nothing will be altered.



*The Digitizing Tablet
Figure 6-1*

7: Marimont Edge File Format

This section describes the format of the edge files created by the Marimont edge process.

7.1 Header

The file is binary, and begins with an 128-word header, followed by a list of linked edge lists (ledgels); that is, after the header, there are a number of items called ledgels, each of which is a list of edges.

The format of the header is as follows:

word	interpretation
0	unused; ignore
1	unused; ignore
2	bits per pixel in input picture
3	bias of laterally inhibited picture
4	"nil-strength" flag
5	"end-of-list" flag
6	first row of picture window
7	first col of picture window
8	last row of picture window
9	last col of picture window
10	1 if contours of positive regions, -1 if those of negative regions.
11	format number of edge file (format 3 currently);
12-127	unused; ignore

7.2 Ledgels

Next come one or more ledgels, followed by a word containing the end of list flag (word 5 of the header above). Each ledgel has a two word header, a list of one or more edges, and a word after the last edge containing the end of list flag. Note that this word flags the ends of two kinds of list: the list of ledgels, and the list of edges that each ledgel contains.

Each ledgel has the following format:

word	interpretation
0	1 if the ledgel is closed, i.e. the last edge is linked (conceptually) to the first, else 0.
1	number of left turns less the number of right turns in the ledgel, as one traverses the ledgel from head to tail.
2	beginning of this ledgel's list of edges

. [one or more edges]

last end-of-list flag

7.3 Edgels

Each ledgel has a list of one or more edges. There are two kinds of edges, corresponding to "significant" and "insignificant" zero crossings in the laterally inhibited image. A significant zero crossing is a transition of the laterally inhibited signal from positive to negative. An insignificant zero crossing is a transition of the laterally inhibited signal from positive or negative (depending on the sign of the region whose encircling contours are being detected, see word 10 of the header above) to zero, and as such does not correspond to a likely edge in the original image. Their exclusion from linked edge lists, however, seems to destroy much useful connectivity. So, we include them as "links" and assume that one between two significant zero crossings is not a significant break in the edge. But at insignificant zero crossings we do not estimate the strength of the edge or image intensities to either side as we do for significant zero crossings. Since less information is thus associated with insignificant zero crossings, we use two edge formats to save space.

The format for an edge is as follows:

word interpretation

- 0 interpolated row coordinate of edge point (floating-point)
- 1 interpolated column coordinate of edge point (floating-point)
- 2 integer equal to 0 if edge is horizontal, 1 if vertical
- 3 two possible interpretations: if when interpreted as an integer, it equals the nil-strength flag, then this is an insignificant edge point, the edge strength is undefined, and this is the last field in the edge. Otherwise, this edge is significant, this field should be interpreted as a floating-point estimate of the edge strength, and the next two words are fields belonging to this edge. all edge files as of this writing were created by encircling positive regions (see word 10 of the header), and in that case the edge strength is always positive, and the brighter side of the edge is towards the left as one moves from the head of the ledgel to the tail.
- 4 (significant edges only!) estimate of original image intensity to the left
- 5 (significant edges only!) estimate of original image intensity to the right

7.4 Clarifications

The edge location coordinates are in picture coordinates, i.e. with respect to the original picture, NOT w.r.t. the window in which they were detected. Integral locations correspond to pixel centers, not boundaries, and the topmost, leftmost pixel center is taken to be $(0, 0)$, which means that an $m \times n$ picture has its upper left corner at $(-0.5, -0.5)$, and its lower right hand corner at $(m - 0.5, n - 0.5)$ (since the indices of the last row, col are $(m - 1, n - 1)$).

For the most part, edges are detected between horizontally or vertically adjacent pixels, which is why there are only two possible orientations for edges. An edge is detected between two such adjacent pixels if the laterally inhibited signal is positive at one and negative at the other. The edge location is estimated by the linearly interpolated zero crossing between these two values. Edge strength is the difference between laterally inhibited intensities one pixel to either side of estimated zero crossing (in the directions normal to that of the zero crossing); linear interpolation is used to estimate each of these intensities, since the points at which they're measured usually fall between pixels. The strength is scaled down to correspond to the difference between adjacent pixels (i.e. the strength measure is laterally inhibited contrast per pixel unit measure). Image intensities are estimated at these same points, i.e. one pixel to either side of the interpolated zero crossing, in an analogous way, by linearly interpolating between each pair of image intensities. However, both image intensities are retained.

The reason for the "for the most part" in the first line of the paragraph above is that "extended" zero crossings are detected in the current implementation. An extended zero crossing is three adjoining pixels in a row or column with one end pixel positive, one end pixel negative, and the middle pixel zero (values refer to the laterally inhibited signal). The estimates of edge location and strength and left and right image intensities are made just as in the above: the location of the edge is an interpolated zero-crossing, the edge strength is the (scaled) difference in (interpolated) laterally inhibited pixel values one pixel to either side of the estimated location, and the left and right image intensities are interpolated image intensities one pixel to either side of the estimated location.

8: Conclusions

8.1 Summary

A principal research interest of our group is in developing a rule-based advanced automated stereo mapping system to function within ACRONYM [Brooks 1981]. Current mapping techniques ignore much of the information available from inference on single views of a scene. This information can be useful for three-dimensional surface interpretation, and also provides extra parameters for stereo matching (i.e. surface orientation, occlusion cues). Our research effort is directed at establishing such monocular inference rules in a rule-base for stereo mapping.

In deriving these rules, we perform analysis of both hand extracted and automatically produced edge descriptions. A facility has been developed under the current postdoctoral contract for this manual edge extraction from hardcopy imagery. We have studied rule synthesis for several cases, including that of orthogonal trihedral vertices - features that dominate cultural scenes. This research is very promising, and has shown the utility of the rule-based approach to surface inference from monocular information. We will be continuing our research in rule synthesis under other funding.

Camera solving provides powerful constraint on the correspondence problem in stereo matching. We have developed a facility under this contract for interactively registering images, determining the parameters for transforming them (or their edge descriptions) into collinear epipolar space, and performing the actual image transformation. This determination is crucial to a mapping process. Incorporating an automated module to provide data for the camera solving is a very important next step.

We have experimented with an existing stereo mapping process, enhancing its flexibility with respect to image format and with respect to edge operator format, and have been preparing example outputs of its processing on new imagery. Our intent with this effort has been to show the capabilities of a local matching process and to assess its applicability to the planned rule-based system.

8.2 Demonstration

We will be demonstrating the following for RADC later in May:

- a) an interactive digitizing test facility;
- b) the use of image edge descriptions produced using this facility and from an automated process [Marimont 1982] in synthesizing rules for stereo matching;
- c) examination of Orthogonal Trihedral Vertex (OTV) inference rules;

- d) development of a system for registration of image pairs;
- e) analysis of stereo imagery with an automated stereo process.

Our demonstration will also present related equipment and system facilities that we use in support of this and other vision research.

9: Digitizing Program

See sections 2 and 6 for documentation on using this program.

```
-----
{$D+}{$M:20000}
Program Tablet(tty,vertfile);

CONST
  CHOP=100000;
  PI = 3.14159265;
  DDX = 432.0; DDY = 432.0; GDD = 512.0;
  lfx = 40.0;
  maxdifference=0.05; { one twentieth of screen away }

{ to hold the lines associated with a vertex. incoming lines are negative. }
TYPE
  LINESPTR=+linetype;
  linetype=record
    line:integer;
    nextline:linesptr;
  end;

{ to hold the vertices with their associated coordinates and lines }
  VERTLISTPTR=+vertlist;
  vertlist=record
    vertex:integer;
    x,y:real;
    header:linesptr;
    nextvert:vertlistptr;
  end;

{ to hold the points associated with a line }
  POINTPTR=+point;
  point=record
    xp,yp:real;
    nextpt:pointptr;
  end;

{ to hold the lines with their associated vertices and points }
  LINELISTPTR=+linelist;
  linelist=record
    linenum,initvert,finalvert:integer;
    header:pointptr;
    nextline:linelistptr;
  end;

  TEMPARRAY=array[1..20] of integer;
  STRNG=packed array[1:30] of char;

INTFILE= FILE OF INTEGER;           { For graphics }

Var  savex,savey,X1,Y1,X2,Y2,X3,Y3,X4,Y4,MINX,MINY:real;
      signold,oldvert,linenum,pich,picw,vertcount,linecount,verts,vertb:integer;
      dx,dy,gx,gy,lstx,lsty,ttyst,boxsize:integer;      { for drawing (x,y) }
      theta,REALX,REALY:real;
      B1,B2,answer,dumchar:char;
      TABLETIO,jump,finished,ddgraph,LAST4,BOXFLAG,boxgod,
        toconfirm,needconfirm,DDGRAPHX,GDDGRAPHX,T,readin,dotch:boolean;
```

```

vertfile,infile:text;
filename:string;
v1.startvert,tailvert,
  tptr,vptr:vertlistptr;          { vertex list }
newlptr,lptr,l,
  scanptr,lstscanptr:linesptr;    { lines of vertex list }
l1.startline,tailline,
  sptr,savsptr,lstsptr:linelistptr; { line list }
firstp,p,olddp,pptr:pointptr;    { points in line list }

godfile: INTFILE;      { GOD files for plotting }
SWITCH: RECORD         { Little hack for putting reals into integers }
CASE FOO:BOOLEAN OF
  TRUE: (I:INTEGER);   { for GOD files }
  FALSE: (R:REAL)
END;

{ external DD graphics procedures in GPAS.REL[TST,AAM] }
procedure ginit: extern;      { init }
procedure scrset: extern;    { clear screen }
procedure width(w:integer); extern; { no-op }
procedure drken: extern;     { make line dark }
procedure liten: extern;     { make line light }
procedure inven: extern;     { swap above }
procedure move(x,y:integer); extern; { invisible line to x,y }
procedure draw(x,y:integer); extern; { visible line to x,y }
procedure dpyup: extern;     { draw to screen }
procedure inchar(var key,ctlkey,metakey:integer); extern;
procedure bitini(line:integer); extern; { init tty for input }
procedure bitpad(var resul1,resul2,resul3:integer); extern; { tablet input }
function ttytab(var resul1,resul2,resul3:integer):boolean; extern; {tablet or tty test }
procedure ppset: extern;     { set page printer }
procedure ppdone: extern;    { release page printer }

```

```

{ READTABLET DISTANCE INITTEMPARRAY GRAPHICS (DD AND GOD) }

```

```

Procedure READTABLET(var B:char;var X,Y:real);
var T,IX,IY:integer;TA:real;

```

```

{ This procedure reads in data from either the terminal or the tablet.
  The data consists of which button was pressed, and the coordinates
  of the point at which it was pressed. The boolean TABLETIO indicates
  whether the procedure is reading from the tablet or from the terminal. }

```

```

  Begin
    if TABLETIO then
      begin
        bitpad(T,IX,IY);
        IF TTYTAB(T,IX,IY) THEN WRITELN(TTY,'tty activity');
        writeln(tty,t:0,' ',ix:0,' ',iy:0);
        B:=chr(48+T);X:=IX;Y:=IY;
      end
    else
      begin
        readln(tty);
        read(tty,B);read(tty,X);read(tty,Y);
      end;
  End;

```

```

PROCEDURE GETCOORDS;
  Begin
    READTABLET(31,X1,Y1);
  End;

```

```

REALX := (X1-MINX)/picw; REALY := (Y1-MINY)/pich;
IF REALX < 0.0 THEN REALX:=0.0
ELSE IF REALX > 1.0 THEN REALX:=1.0;
IF REALY < 0.0 THEN REALY:=0.0
ELSE IF REALY > 1.0 THEN REALY:=1.0;
( writeIn(tty,'B1=',B1, ' ', X1=',',X1:0,(' ',REALX:5:3,','), Y1=', ', Y1:0,(' ',REALY:5:3,',')); )
End;

```

```

FUNCTION ASK(N:integer): BOOLEAN;
VAR goodans:BOOLEAN;
Begin { ASK }
  goodans:=FALSE;
  Repeat
    case N of
      1:WRITE(TTY,'Want Tablet IO (y/n)?:');
      2:WRITE(TTY,'Want graphics output (y/n)?:');
      3:WRITE(TTY,' to the DD (y/n)?:');
      4:WRITE(TTY,' to the GODFILE (y/n)?:');
      5:WRITE(TTY,'Want to read in a file (y/n)?:');
      6:WRITE(TTY,'Happy with this frame (y/n)?:');
      7:WRITE(TTY,'Want to DELETE segments (y/n)?:');
      8:WRITE(TTY,'Do another deletion (y/n)?:');
      9:WRITE(TTY,'Is this the line to be deleted (y/n)?:');
      10:WRITE(TTY,' Want boxes draw around vertices (y/n)?:');
      11:WRITE(TTY,' Want frame drawn in GOD file (y/n)?:');
      12:WRITE(TTY,' Want to add to file from TABLET (y/n)?:');
    End;
    readln(tty);read(tty,answer); if(answer = 'y') or (answer = 'Y') then
      Begin ASK:=TRUE;goodans:=TRUE; End
    else Begin ASK:=FALSE;goodans:=TRUE; End;
  UNTIL goodans;
End; { ASK }

```

```

Function DISTANCE(X1, Y1, X2, Y2: Real):Real; {Finds the distance bet. 2 pts. }
begin
  distance:= Sqrt (Sqr (X2 - X1) + Sqr (Y2 - Y1));
end;

```

```

Procedure INITTEMPARRAY(var a:temparray);
var i:integer;
begin
  for i:= 1 to 20 do
    a[i]:=0;
  end;

```

```

Function MAX(a,b:integer): INTEGER;
Begin
  IF A > B THEN MAX := A ELSE MAX := B;
End;

```

{ Routines to make GOD files }

```

PROCEDURE OUT(N:INTEGER);
BEGIN
  GODFILE* := N; PUT(GODFILE)
END;

```

```

PROCEDURE OUTREAL(V:REAL);
BEGIN
  SWITCH.R := V;
  OUT(SWITCH.I)
END;

```

```

PROCEDURE PLOTLINE(X1,Y1,X2,Y2:REAL);
BEGIN
  OUT(7); { LINE }
  OUTREAL(X1); OUTREAL(Y1);

```

```

        OUTREAL(X2); OUTREAL(Y2);
        OUT(0)      { THICK }
    END;

{ Procedures to display graphics on the DD terminal. }

Procedure BOX;
Begin { BOX }
    IF BOXFLAG THEN
        Begin
            IF DDGRAFX THEN
                Begin
                    MOVE(dx-boxsize,dy-boxsize);DRAW(dx-boxsize,dy+boxsize);
                    DRAW(dx+boxsize,dy+boxsize);Draw(dx+boxsize,dy-boxsize);
                    Draw(dx-boxsize,dy-boxsize);MOVE(dx,dy);
                    IF NOT(READIN) THEN DPYUP;
                End;
            IF GODGRAFX THEN
                Begin
                    PLOTLINE(GX-boxsize,GY-boxsize,GX-boxsize,GY+boxsize);
                    PLOTLINE(GX-boxsize,GY+boxsize,GX+boxsize,GY+boxsize);
                    PLOTLINE(GX+boxsize,GY+boxsize,GX+boxsize,GY-boxsize);
                    PLOTLINE(GX+boxsize,GY-boxsize,GX-boxsize,GY-boxsize);
                End;
            End;
        End; { /OX }

procedure DARKDRAW;
Begin
    IF GODGRAFX THEN
        Begin
            gx:=round(realx*GDD);
            gy:= round(realx*GDD);
        End;
    IF DDGRAFX THEN
        Begin
            dx := round(realx*DDX+1fx);
            dy := round((1.0-realy)*DDY);
            MOVE(dx,dy);
            IF NOT(READIN) THEN DPYUP;
        End; { move if DD, nothing if GOD }
    End;

procedure LIGHTDRAW;
Begin
    IF GODGRAFX THEN
        Begin
            1stx:=gx; 1sty:=gy;
            gx:=round(realx*GDD);
            gy:= round(realx*GDD);
            PLOTLINE(1stx,1sty,gx,gy);
        End;
    IF DDGRAFX THEN
        Begin
            dx := round(realx*DDX+1fx);
            dy := round((1.0-realy)*DDY);
            DRAW(dx,dy);
            IF NOT(READIN) THEN DPYUP;
        End;
    End;

PROCEDURE FRAME;
Begin { FRAME }
    realx:=0.0;realy:=0.0;DARKDRAW; { DRAW FRAME AROUND SCREEN }
    realx:=0.0;realy:=1.0;LIGHTDRAW;
    realx:=1.0;realy:=1.0;LIGHTDRAW;
    realx:=1.0;realy:=0.0;LIGHTDRAW;
    realx:=0.0;realy:=0.0;LIGHTDRAW;

```

```

End:{ FRAME }

PROCEDURE GODINI;
Begin { GODINI }
  REWRITE(GODFILE,'TAB.GOD');
  OUT(97):          { DDINIT }
  OUT(1):           { SCREEN }
  OUTREAL(0.0);
  OUTREAL(0.0);
  OUTREAL(GDD);
  OUTREAL(GDD);
  OUT(4):           { LITEN }
  BOXGOD:=ASK(11);
  IF BOXGOD THEN FRAMEDRAW;
End: { GODINI }

PROCEDURE GODFINI;
VAR I:integer;
Begin { DPYUP and KILJOB }
  OUT(17):          { DPYUP }
  OUT(-1);
  OUT(-1);
  FOR I := 1 TO 32 DO OUT(0) { KILJOB }
End: { DPYUP and KILJOB }

PROCEDURE DDINI;
Begin { DDINI }
  PPSET:            { set up small page printer for text }
  ginit;
  scrset;
  DRKEN:            { dark here so's works like SUN }
  IF not(GODGRAFX) THEN FRAMEDRAW: { frame if just DO }
End: { DDINI }

PROCEDURE DDFINI;
Begin { page printer clear }
  PPDONE;
End: { page printer clear }

-----

{ INITLINELIST, INITVERTLIST, ENTERLINE, ENTERVERTEX, ADDLINEPTR }
Procedure INITLINELIST;
{this initializes the list of lines}
Begin
  new(l1);
  l1*.nextline:=nil;
  l1*.header:=nil;
  startline:=l1;
  tailline:=l1;
End:{INITLINELIST}

Procedure INITVERTLIST;
{this initializes the list of vertices}
Begin
  new(v1);
  v1*.nextvert:=nil;
  v1*.header:=nil;
  startvert:=v1;
  tailvert:=v1;
End:{INITVERTLIST}

Procedure ENTERLINE;
{this puts the line into linelist}

```

```

Begin
  linecount:=linecount+1;
  tailline+.linenum:=linecount;
  tailline+.initvert:=verta;
  tailline+.finalvert:=vertb;
  tailline+.header:=firstp;
  firstp:=nil;
  new(l1);
  tailline+.nextline:=l1;
  tailline:=l1;
  tailline+.nextline:=nil;
End; {ENTERLINE}

```

```

Procedure ENTERVERTEX;
{ starts a new vertex }

```

```

Begin
  tailvert+.x:=REALX;
  tailvert+.y:=REALY;
  vertcount:=vertcount+1;
  tailvert+.vertex:=vertcount;
  tailvert+.header:=nil;
  new(v1);
  tailvert+.nextvert:=v1;
  tailvert:=v1;
  tailvert+.nextvert:=nil;
End; { ENTERVERTEX }

```

```

Procedure ADDLINEPTR(line.vertnum:integer);
{ this adds a line to the linked list of lines associated with a vertex }

```

```

Begin
  v1:=startvert;
  while v1+.vertex <> vertnum do v1:=v1+.nextvert;
  lptr:=v1+.header;
  if lptr = nil then
    begin
      new(newlptr);
      v1+.header:=newlptr;
    end
  else
    begin
      while lptr+.nextline <> nil do lptr:=lptr+.nextline;
      new(newlptr);
      lptr+.nextline:=newlptr;
    end;
  newlptr+.line:=line;
  newlptr+.nextline:=nil;
End; {ADDLINEPTR}

```

```

Procedure FINDOLDVERTEX(var vptr:vertlistptr;var oldvert:integer;xold,yold:real);

```

```

{ This finds the old vertex which is nearest to the point at which B2 was
  pressed. If the nearest old vertex is further than maxdifference away, it
  tells how far away it is. }

```

```

var vertnum:integer;
    tptr:vertlistptr;

```

```

Begin
  tptr:=startvert;
  vptr:=startvert;
  while (tptr<>tailvert) do
    begin
      if DISTANCE(tptr+.x,tptr+.y,xold,yold)<DISTANCE(vptr+.x,vptr+.y,xold,yold) then

```



```

        vptr:=tptr;
        tptr:=tptr.nextvert;
    end;
    oldvert:=vptr.vertex;
    if (DISTANCE(vptr.x,vptr.y,xold,yold)>maxdifference) then
        writeln(tty,'the nearest old vertex is ',DISTANCE(vptr.x,vptr.y,xold,yold):4:
2,' away');
    End; {FINDOLDVERTEX}

```

```

PROCEDURE AIMVERT(vert:integer);
Begin
    tptr:=startvert;
    while tptr.vertex<>vert do
        tptr:=tptr.nextvert;
    REALX:=TPTR.X;REALY:=TPTR.Y;
End;

```

```

FUNCTION FINDOLDPOINT(var retsptr:linelistptr;TESTX,TESTY:real): BOOLEAN;
{ This finds the old point which is nearest to the point at which B2 was
pressed. If the nearest old point is further than maxdifference away, it
tells how far away it is. }

```

```

VAR OLDDIST:REAL;

```

```

PROCEDURE SEARCHPOINT(vlptr:linesptr;xold,yold:real);
Var tstsegnum:integer;
Begin
    tstsegnum:=ABS(vlptr.line); { get linenumber }
    sptr:=startline;
    while sptr.linenum<>tstsegnum do
        sptr:=sptr.nextline;
    pptr:=sptr.header;
    WHILE pptr<>NIL DO
        Begin
            IF DISTANCE(pptr.x,pptr.y,xold,yold) < OLDDIST THEN
                Begin
                    OLDDIST := DISTANCE(pptr.x,pptr.y,xold,yold);
                    savsptr:=sptr;
                End;
            pptr:=pptr.nextpt;
        End;
    End;

```

```

Begin
    AIMVERT(vert);
    savsptr:=nil;
    scanptr:=tptr.header;
    OLDDIST:=1.0;
    REPEAT
        SEARCHPOINT(scanptr,TESTX,TESTY);
        scanptr:=scanptr.nextline;
    UNTIL scanptr = nil;
    IF OLDDIST > maxdifference THEN
        Begin
            WRITELN(TTY, 'No such point on a line from that vertex');
            FINDOLDPOINT:=FALSE;
        End
    ELSE
        Begin
            verta:=savsptr.initvert;
            vertb:=savsptr.finalvert;
            retsptr:=savsptr; { copy back for return }
            FINDOLDPOINT:=TRUE;
        End;
    End; {FINDOLDPOINT}

```

```

PROCEDURE FINDOLDEST(savptr:linelistptr;procedure GRAPHIC; doit:boolean);

```

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```

Begin
  verta:=segptr+.initvert;
  vertb:=segptr+.finalvert;
  GRAPHIC;
  AIMVERT(verta); DARKDRAW: { start drawing }
  pptr:=segptr+.header; READIN:=TRUE;
  while pptr <> nil DO
    Begin
      REALX:=pptr+.xp; REALY:=pptr+.yp;
      pptr:=pptr+.nextpt;
      LIGHTDRAW;
    End;
  AIMVERT(vertb); LIGHTDRAW; READIN:=FALSE;
  DPYUP; DRKEN: { finishing drawing }
END;

FUNCTION CHECKOLDVERTEX(var retsptr:linelistptr): BOOLEAN;
Var tstsegnum,checksegnum:integer;
    tstvptr:vertlistptr;
    scnvlptr:linesptr;
    TSTT:BOOLEAN;

FUNCTION CHECKVERTSOFFLINE: BOOLEAN;
Begin
  tstsegnum:=ABS(scanptr+.line): { get linenumber }
  scnvlptr:=tstvptr+.header: { scan vertex line list }
  checksegnum:=+1;
  WHILE ((scnvlptr <> NIL) AND (tstsegnum <> checksegnum))
  DO Begin
    checksegnum:=ABS(scnvlptr+.line);
    scnvlptr:=scnvlptr+.nextline;
  End;
  IF tstsegnum <> checksegnum THEN
    Begin
      CHECKVERTSOFFLINE:=FALSE;
      scanptr:=scanptr+.nextline;
    End
  ELSE CHECKVERTSOFFLINE:=TRUE;
End;

Begin
  retsptr:=nil;
  FINDOLDVERTEX(tstvptr,vertb,REALX,REALY);
  savsptr:=nil: { tptr and tstvptr }
  scanptr:=tptr+.header;
  TSTT:=FALSE;
  WHILE ((scanptr <> NIL) AND NOT(TSTT))
  DO TSTT:=CHECKVERTSOFFLINE;
  IF TSTT THEN
    Begin
      sptr:=startline;
      while sptr+.linenum<>tstsegnum do
        sptr:=sptr+.nextline;
      retsptr:=sptr;
      CHECKOLDVERTEX := TRUE;
    End
  ELSE CHECKOLDVERTEX := FALSE
End: { CHECKOLDVERTEX }

PROCEDURE DELETESeg(segptr:linelistptr);

PROCEDURE DELSFROMV(vertnum:integer);
Begin
  AIMVERT(vertnum);
  scanptr:=tptr+.header;
  1stscanptr:=tptr+.header;
  while ABS(scanptr+.line) <> 11111111 DO
    Begin
      1stscanptr:=scanptr;

```

```

        scanptr:=scanptr+.nextline;
    End;
    IF scanptr=tptr.header then tptr.header:=scanptr+.nextline
    ELSE 1stscanptr+.nextline:=scanptr+.nextline;
End;

Begin
    verta:=segptr+.initvert;
    vertb:=segptr+.finalvert;
    linenum:=segptr+.linenum;
    DELSFROMV(verta);           { remove line from start vertex list}
    DELSFROMV(vertb);           { remove line from end vertex list}
    sptr:=startline;
    1stsptr:=nil;
    while sptr <> segptr DO
        Begin
            1stsptr:=sptr;
            sptr:=sptr+.nextline;
        End;
    IF 1stsptr=nil THEN startline:=sptr+.nextline
    ELSE 1stsptr+.nextline:=sptr+.nextline;
End; { DELETESEG }

PROCEDURE DELETEPHASE;
var segptr:line1stptr;

PROCEDURE SETDELETION;
Begin
    FINDOLDVERTEX(tptr,verta,REALX,REALY);
    GETCOORDS;           { select line or vertex point }
    T:=FALSE;
    CASE B1 of
        '1': T:= CHECKOLDVERTEX(segptr);
        '4': T:= FINDOLDPOINT(segptr,REALX,REALY);
        others: WriteLn(tty,'1 for vertex; 4 for point')
    End;
    IF T THEN
        Begin
            REMOVETEST(segptr,LITEN,TRUE);
            NEEDCONFIRM:=TRUE;
            writeLn(tty,'<B=2> for confirm, <B=8> for reject deletion');
        End
    ELSE writeLn(TTY,'Couldn't delete line (from vertex ',verta:0,')');
End; { SETDELETION }

PROCEDURE ERRMSG;
Begin
    writeLn(TTY,'B=1 or 4 for deletion, B=2 for confirm, B=8 for reject/quit');
End;

Begin { Deletes segments }
    PPSET;
    writeLn(TTY,'Select vertex <B=1>, then vertex <B=1> or point on line <B=4>; <B=8> quits. ');
    write(TTY,' Once selected, <B=2> confirms deletion, <B=8> cancels it. ');
    FINISHED:=FALSE;NEEDCONFIRM:=FALSE;
    REPEAT
        GETCOORDS;           { select vertex }
        CASE B1 OF
            '1': IF NOT(NEEDCONFIRM) THEN SETDELETION
                  ELSE ERRMSG;      { CHOSE THE LINE TO DELETE }
            '2': IF NEEDCONFIRM THEN      { THIS IS CONFIRMATION }
                Begin
                    DELETESEG(segptr);NEEDCONFIRM:=FALSE;
                    writeLn(tty,'For deletions B=1 then 1 or 4; B=8 is quit');
                End
            ELSE ERRMSG;
            '8': IF NEEDCONFIRM THEN      { THIS IS REJECTING THE DELETION }
                Begin
                    REMOVETEST(segptr,DRKEN,FALSE);NEEDCONFIRM:=FALSE;

```

```

        writeln(tty,'For deletions B=1 then 1 or 4; B=8 is quit');
      End
    ELSE Finished:=true;
  OTHERS: ERRMSG
  END; { OF CASE }

  UNTIL FINISHED;
  T:=TRUE;FINISHED:=FALSE;LAST4:=FALSE;
  writeln(tty,'Returning to entry mode');
End:{ Deletes segments }

PROCEDURE LASTDELETE: { last chance at deleting }
Begin
  PPSET;
  WriteIn(TTY,'DELETE? <B=2> for YES, <B=8> for NO');
  T:=FALSE;
  REPEAT
    READTABLET(B1, X4, Y4);
    CASE B1 of
      '2': DELETEPHASE: { do deletions }
      '8': T:=TRUE;
      others: writeln(TTY,'<B=2> for deletions or <B=8> for none')
    End;
  UNTIL T;
End;

```

Procedure STARTOLDVERTEX;

{ This procedure finds an old vertex, enters the number of the incoming line in the linked list of lines associated with it, enters the number of the old vertex in the line buffer, and calls ENTERLINE to move the contents of the buffer into the linked list of lines. It then draws a line to the old vertex. }

var llnenum,oldvert:integer;

```

Begin
  toconfirm:=false;LAST4:=FALSE;
  if jump then
    begin { jump }
      FINDOLDVERTEX(vptr,oldvert,REALX,REALY);
      REALX:=vptr+.x;REALY:=vptr+.y;
      verta:=oldvert;
      jump:=false;
      if ddgraph then DARKDRAW;
    end { jump }
  else
    begin { no jump }
      FINDOLDVERTEX(vptr,oldvert,REALX,REALY);
      vertb:=oldvert;
      REALX:=vptr+.x;REALY:=vptr+.y;
      ENTERLINE;
      ADDLINEPTR(llnenum,verta);
      ADDLINEPTR(-llnenum,vertb);
      if ddgraph then LIGHTDRAW;
      verta:=oldvert;
    end { no jump }
  End; {STARTOLDVERTEX}

```

Procedure STARTNEWVERTEX;

{ This procedure creates a new entry in the linked list of vertices

which contains the number and coordinates of the vertex, and adds the vertex number to the line buffer. If the vertex is at the end of the line (if B4 has been previously pressed to add points to that line), it calls ENTERLINE to add the contents of the line buffer to the linked list of lines. It also draws a line to the vertex. }

```
var linenum:integer;
```

```
Begin: {STARTNEWVERTEX}
```

```
  toconfirm:=false;LAST4:=FALSE;
  if jump then
    begin { jump }
      ENTERVERTEX;
      verta:=vertcount;
      jump:=false;
      if ddgraph then Begin DARKDRAW;BOX End;
    end { jump }
  else
    begin { no jump }
      ENTERVERTEX;
      vertb:=vertcount;
      ENTERLINE;
      ADDLINEPTR(linenum,verta);
      ADDLINEPTR(-linenum,vertb);
      if ddgraph then Begin LIGHTDRAW;BOX End;
      verta:=vertcount;
    end; { no jump }
  End; {STARTNEWVERTEX}
```

```
Procedure NEWPOINT;
```

{ This procedure adds the coordinates of a new point to the linked list of points which are associated with a vertex. }

```
Begin
  IF toconfirm then DELETEPHASE
  ELSE
    IF NOT(JUMP) THEN
      Begin
        if firstp=nil then
          begin
            new(p);
            firstp:=p;
            oldp:=p;
          end
        else begin
          new(p);
          oldp.nextpt:=p;
          oldp:=p;
        end
        pt.xp:=REALX;pt.yp:=REALY;
        pt.nextpt:=nil;
        if ddgraph then LIGHTDRAW;
        LAST4:=TRUE;
      End
    ELSE WRITELN(TTY,'Put the pen down first');
    toconfirm:=false;
  End; {NEWPOINT}
```

```
{ UTILITIES }
```

```
FUNCTION READINFILE:DOILEAN;
```

```
VAR baseline,basexent,i,numverts,curr,numlines,linum,oldj1no,QUANT: INTEGER;
```

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```
TVAL:BOOLEAN;
tptr:vertlistptr;
```

```
Procedure READVERTS;
{ This procedure reads the VERTICES from the vertfile }
```

```
Begin
  baseline:=linecount;basevert:=vertcount;
  read(infile,dumchar,dumchar,dumchar);
  read(infile,numverts); { get past 'V =' for N }
  readln(infile);
  FOR I:= 1 to numverts DO
    Begin
      read(infile,vnum,dumchar,dumchar,REALX,dumchar,REALY,dumchar,dumchar);
      { number, coorda, coordb }
      ENTERVERTEX;
      while not(eoln(infile)) DO
        Begin
          read(infile,oldline);
          IF oldline < 0 then signold:=-1 else signold:=1;
          oldline:=ABS(oldline); oldline:=(oldline+baseline)*signold;
          ADDLINEPTR(oldline,vnum+basevert);
        End;
      readln(infile);
    End;
  vertcount := basevert + numverts;
  linecount := baseline;
End; { READVERTS }
```

```
Procedure READLINES;
{ This procedure reads the LINES from the infile }
```

```
PROCEDURE FINDANDDRAW(vert:integer;procedure FUNC);
Begin
  tptr:=startvert;
  while tptr.vertex<>vert do
    tptr:=tptr.nextvert;
  REALX:=TPTR.X;REALY:=TPTR.Y;
  FUNC;BOX;
End;
```

```
Begin
  readln(infile,dumchar,dumchar,dumchar,numlines); { get past 'V =' for N }
  FOR I:= 1 to numlines DO
    Begin
      read(infile,lnum,dumchar,dumchar,verta,dumchar,vertb,dumchar,dumchar);
      verta:=verta+basevert;vertb:=vertb+basevert;
      IF ddgraph THEN FINDANDDRAW(verta,DARKDRAW);
      firstp:=nil;
      while not(eoln(infile)) DO
        Begin
          read(infile,dumchar,REALX,dumchar,REALY,dumchar);
          NEWPOINT;
        End;
      IF ddgraph THEN FINDANDDRAW(vertb,LIGHTDRAW);
      ENTERLINE;
      readln(infile);
    End;
  End;{READLINES}
```

```
Begin
  TVAL:=ASK(5);
  IF TVAL THEN
    Begin
      PPSET;
      { WRITE(TTY,'Filename:'); }
      { READLN(TTY,filename:QUANT:[ ]); }
      { WRITELN(TTY,QUANT:0); }
      { RESET(infile,'NEW.VRT'); }
```

```

        readin:=true;
        READVERTS;
        READLINES;
        IF (ddgraph and ddgrafx) THEN DPYUP;
        End;
        READINFILE:=TVAL;
    End; { READINFILE }

Function MAG(X1, Y1, X2, Y2: Real):INTEGER; { Finds the distance bet. 2 pts. }
BEGIN
    MAG:= round(Sqrt (Sqr (X2 - X1) + Sqr (Y2 - Y1)));
END;

Function ANGLE (X1, Y1, X2, Y2: Real): Real; { Finds angle theta bet. 2 lines }
VAR X,Y,xlt:real;
BEGIN
    X := X2 - X1;
    Y := Y2 - Y1;
    IF abs(X) > abs(y) THEN
        xLT := Arctan (Y/X)
    ELSE xLT := (PI/2) - Arctan (X/Y);
    angle := xlt;
END;

FUNCTION INITTABLE:BOOLEAN;
Begin
    WriteLn (tty, 'Lower-left corner: ');
        READTABLET(B1, X1, Y1);
    WriteLn (tty, 'Top-left corner: ');
        READTABLET(B1, X2, Y2);
    WriteLn (tty, 'Top-right corner: ');
        READTABLET(B1, X3, Y3);
    WriteLn (tty, 'Lower-right corner: ');
        READTABLET(B1, X4, Y4);
    { these calculations are dumb }
    minx := X1; miny := Y1;
    Theta := ((ANGLE(X1, Y1, X2, Y2) - Pi/2.0) + ANGLE(X2, Y2, X3, Y3) +
        (ANGLE(X4, Y4, X3, Y3) - Pi/2.0) + ANGLE(X1, Y1, X4, Y4)) /4.0;
    picw := MAX(MAG(X1, Y1, X2, Y2),MAG(X4, Y4, X3, Y3));
    pich := MAX(MAG(X1, Y1, X4, Y4),MAG(X2, Y2, X3, Y3));
    Write(tty, 'Theta=' ,theta:5:3, ' height=' ,pich:0, ' width=' ,picw:0);
    WriteLn(tty, ' <B=2> confirms, <B=8> rejects');
    READTABLET(B1, X4, Y4);
    CASE B1 of
        '2': INITTABLE:=TRUE; { make sure happy with this }
        '8': INITTABLE:=FALSE;
        others: writeLn(TTY, '2(confirm) or 8(reject)');
    End;
End;

PROCEDURE WRITEFILE;
TYPE bigarray=array[1..500] of integer;
VAR VTRAN,LTRAN:bigarray;
VCOUNT,LCOUNT:integer;

PROCEDURE BUILDVLTABLE;
Begin
    tptr:=start/ort;
    VCOUNT:=0;
    while (totr<>tailvert) do
        Begin
            verta:=tptr.vertex;
            IF tptr.header <> nil then
                Begin
                    VCOUNT:=VCOUNT+1;
                    VTRAN[verta]:=VCOUNT;
                End
            ELSE VTRAN[verta]:=-1; { null }
        End
    End;

```

```

    tptr:=tptr.nextvert;
  End;
  sptr:=startline;
  LCOUNT:=0;
  while sptr <> tailline do      { no nulls in segs.. they've been removed }
  Begin
    linenum:=sptr.linenum;
    LCOUNT:=LCOUNT+1;
    LTRAN[linenum]:=LCOUNT;
    sptr:=sptr.nextline;
  End;
End;

Begin { WRITE OUT VERTICES AND EDGES }
{ write file with entries:
    V = the number of vertices,
    <vertex entries> (N of them),
    L = number of lines,
    <line entries> (M of them).
  }
  BUILDVLTABLE; { make index transforms for vertices and lines }
  writeln(tty,'V = ',VCOUNT:0,' L = ',LCOUNT:0);
{ do Vertices }
  writeln(vertfil,'V = ',VCOUNT:0,' height = ',pich:0,' width = ',picw:0,' (mm)');
  vl:=startvert;
  repeat
    verta:=VTRAN[vl.vertex];
    IF verta > 0 then write(vertfil,verta:0,' (',vl.x:0:3,',',vl.y:0:3,')');
    l:=vl.header;
    if l<>nil then
      repeat
        linenum:=l.line;if linenum>0 then signold:=1 else signold:=-1;
        linenum:=signold*LTRAN[ABS(linenum)];
        write(vertfil,' ',linenum:0);
        l:=l.nextline;
      until l=nil;
      IF verta > 0 then writeln(vertfil);
      vl:=vl.nextvert;
    until vl=tailvert;
{ do Lines }
    writeln(vertfil,'L = ',LCOUNT:0);
    ll:=startline;
    repeat
      LINENUM:=LTRAN[ll.linenum];
      write(vertfil,LINENUM:0,' <',VTRAN[ll.initvert]:0,',',VTRAN[ll.finalvert]:0,'>');
      p:=ll.header;
      if p<>nil then
        repeat
          write(vertfil,' (',p.x:0:3,',',p.y:0:3,')');
          p:=p.nextpt;
        until p=nil;
        writeln(vertfil);
        ll:=ll.nextline;
      until ll=tailline;
  End; { WRITE VERTICES AND EDGES }

```

{MAIN PROGRAM STARTS HERE}

```

Begin
  writeln(tty,'Digitizing Tablet; Button Functions:');
  writeln(tty,' 1: start a new vertex (either fresh, or as the end of the current');
  writeln(tty,'      arced segment');
  writeln(tty,' 2: find the nearest vertex to this point, and treat it as the end');
  writeln(tty,'      (or start) of current arced segment');

```



```

writeln(tty,' 4: take this point');
writeln(tty,' 8: lift pen;');
writeln(tty,' if next is 1 or 2 then CONTINUE drawing');
writeln(tty,' if next is 4 then do a DELETION');
writeln(tty,' if next is 8 then QUIT');
DDGRAPH:=ASK(2);
IF DDGRAPH THEN
  BEGIN
    DDGRAFX:=ASK(3);
    GODGRAFX:=ASK(4);
    BOXFLAG:=ASK(10);
    IF BOXFLAG THEN
      Begin
        write(tty,' Box size(1,2):');
        readln(tty);read(TTY,boxsize);
      End;
    IF GODGRAFX THEN GODINI;
    IF DDGRAFX THEN DDINI;
  END;
Rewrite(verfile);
firstp:=nil;vptr:=nil;vertcount:=0;linecount:=0;
INITLINELIST;INITVERTLIST;
REPEAT T:= READINFILE UNTIL NOT(T);
TABLETIO:=TRUE;DOTAB:=TRUE;
IF READIN THEN DOTAB:=ASK(12);
IF DOTAB THEN
  Begin
    write(tty,'TTYline number:');
    readln(tty);read(tty,ttline);
    bitini(ttline);
    REPEAT T:=INITTABLET UNTIL T; { get corners of image }
    PPSET;
    writeln(tty,'*Ready*');
    readin:=false;finished:=false;toconfirm:=false;jump:=true;LAST4:=FALSE;
    firstp:=nil;
    repeat
      GETCOORDS;
      case B1 of
        '1':STARTNEWVERTEX;
        '2':STARTOLDVERTEX;
        '4':NEWPOINT;
        '8':Begin
          IF NOT(LAST4) THEN
            Begin
              if toconfirm then finished:=true
              else Begin
                toconfirm:=true;
                writeln(tty,'*Pen is UP*');
              End;
              jump:=true;
            End
          ELSE writeln(tty,'put the pen down first');
          End;
        others:WriteIn(tty,'Garbled data')
      end;
    until finished;
  End;
IF DDGRAPH THEN
  Begin
    IF GODGRAFX THEN GODFINI ELSE IF DDGRAFX THEN DCFINI;
  End;
WRITEFILE;
End. {MAIN}

```

```

:code to allow PASCAL to get BITPAD data from TTY other than job's TTY
: Macro-10 assembly code, with local code for TTY driver
title trace

```

```

-----

item==0
sc1==1
sc2==2
sc3==3
sc4==4
p==+017
MODE==0 :ASCII
JOBFF==+0121
chnsts==+0716000000000
ttyskp==+0047000400116
PPIOT==+0702000000000
DBEEP==+0047000400111 ;BEEP UO DEFN
DPYCLR==+0701000000000
INSKIP==+0051540000000
SLEEP==+0047000000031
OPDEF PPSEL[PPIOT 0.]
OPDEF PPACT[PPIOT 1.]
OPDEF DPYPOS[PPIOT 2.]
OPDEF DPYSIZ[PPIOT 3.]
OPDEF PPREL[PPIOT 4.]
OPDEF LEYPOS[PPIOT 6.]

radix 10

entry BITINI,BITPAD,PPSET,PPSET2,PPDONE,TTYTAB

BITINI: POP P.RETAD
MOVEM SC2,LINE ;LINE PARAMETER PASSED BY VALUE
MOVEI SC3,+017
BITLOP: HRRZ SC1,SC3 ;GET A CHAN TO TEST
LSH SC1,18+5
OR SC1,[CHNSTS SC2]
XCT SC1
TRNE SC2,+0400000 ;USED ALREADY?
SOJGE SC3,BITLOP ;TRY UNTIL NONE THERE
JUMPL SC3,NOCHMS
HRRZS SC3
LSH SC3,5
HRLZM SC3,CHAN ;THIS IS THE CHANNEL
MOVE ITEM,[TTYSKP]
IOR ITEM,CHAN
MOVEM ITEM,BITCHK
MOVE ITEM,LINE
SETZ SC2,
LINLOP: IDIVI ITEM,10 ;TREAT AS DECIMAL NUMBER (ALTHOUGH IT IS OCTAL)
ADDI SC1,+020
LSHC SC1,-6 ;SIDE IT OVER
JUMPN ITEM,LINLOP ;GO TILL DONE
HLRM SC2,BITDVC+1 ;LINE IN SIXBIT
BITOPN: MOVE ITEM,[OPEN BITDVC]
IOR ITEM,CHAN ;MAKE OPEN WORD
XCT ITEM
HALT BITOPN
MOVEI SC1,ITIBFS
EXCH SC1,JOBFF
MOVE ITEM,[I.BUF 2]
IOR ITEM,CHAN
XCT ITEM
MOVE SC1,JOBFF

```

```

        MOVE    ITEM,[INPUT]
        IOR     ITEM,CHAN
        MOVEM   ITEM,INCMD
        JRST   @RETAD          ;DONE INITING TTY LINE

NOCHNS: OUTSTR  [ASCIZ/
No channels left.. forget it
/]
        POPJ    P,

TTYSLP: MOVEI   0,0           ;SLEEP A JIFFY
        SLEEP   0,
TTYTAB: INSKIP  0,           ;has a char been typed?
        JRST   DOBTPD        ;NO
        SETOM   1(P)         ;return TRUE (SO CALLER GETS INPUT FROM TTY)
        POPJ    P,

DOBTPD: XCT     BITCHK        ;IF THERES A CHAR IN BITPAD BUFF, DO IT
        JRST   TTYSLP        ;ELSE SLEEP A BIT AND TRY AGAIN
        PUSHJ   P,BITPAD      ;GET INPUT FROM BITPAD
        SETZM   1(P)         ;return FALSE
        POPJ    P,

BITPAD: POP     P,RETAD
        HRRZM   SC2,RETVL1
        HRRZM   SC3,RETVL2
        HRRZM   SC4,RETVL3
FRC6:  MOVEI    ITEM,6        ;FIRST IS 6 DIGITS
        MOVEM   ITEM,COUNT
        PUSHJ   P,GETBYT
        JRST   FRC6          ;INSIST ON GOOD DATA
        MOVEM   SC1,FSTVAL
        MOVEI    ITEM,5        ;SECOND IS 5 DIGITS
        MOVEM   ITEM,COUNT
        PUSHJ   P,GETBYT
        JRST   FRC6          ;BAD DATA, LOOK FOR 6 BEFORE CONTINUING
INDON: MOVEM   SC1,@RETVL3     ;RETURN VALUE3 (Y VALUE)
        MOVE    SC1,FSTVAL     ;STRIP OFF BUTTON FROM FSTVAL
        IDIVI   SC1,*D100000
        MOVEM   SC1,@RETVL1     ;RETURN BUTTON (RETVL1)
        MOVEM   SC2,@RETVL2     ;RETURN VALUE2 (X VALUE)
        JRST   @RETAD

GETBYT: SETZ    SC1,          ;RETURN VALUE
BITILP: SOSG    IBF+2         ;COUNTER
        PUSHJ   P,REFBUF
        ILDB    SC2,IBF+1
        CAIG    SC2,"9"
        CAIGE   SC2,"0"
        JRST   BITILP
CNTLOP: IMULI   SC1,10
        ADDI    SC1,-*O60(SC2) ;SUM DIGITS
        SOSG    COUNT         ;DIGIT COUNTER
        JRST   GOTCNT
        SOSG    IBF+2         ;BUFF COUNTER
        PUSHJ   P,REFBUF
        ILDB    SC2,IBF+1
        CAIG    SC2,"9"
        CAIGE   SC2,"0"
        JRST   JITBAD         ;GARBLED .. LOOK FOR 6 AGAIN
        JRST   CNTLOP         ;GO FOR REST
GOTCNT: SOSG    IBF+2         ;BUFF COUNTER
        PUSHJ   P,REFBUF
        ILDB    SC2,IBF+1
        CAIG    SC2,"9"
        CAIGE   SC2,"0"
        JRST   BADCLR
BADCLR: SOSG    IBF+2         ;NOW FIELD CORRECT
        PUSHJ   P,REFBUF

```

```

      ILDB      SC2,IBF+1
BITBAD: CAIE    SC2,+016      ;CARRET
        JRST   BADCLR      ;NO, CLEAR THE CHARS
        MOVEI  SC1,-1
        DBEEP  SC1,
        OUTSTR [ASCIZ/Bad data/]
        POPJ   P,          ;YES, RETURN ERROR

GOODEND: AOS    (P)          ;GOOD ONE SKIPS BACK
        POPJ   P,

REFBUF: MOVE    ITEM,INCMD
        XCT     ITEM
        SOS     IBF+2
        POPJ   P,          ;GO BACK WITH NEW DATA

PPSET:  PPSEL   2            ;PAGE PRINTER 2 ON
        PPACT   +0100000     ;SEE 2, erase 0
        DPYPOS  -450
        DPYSIZ  +02001      ;2 LINES AT BOTTOM OF SCREEN. SCROLL CONTINUOUSLY
        LEYPOS  0            ;LINE EDITOR AT BOTTOM OF SCREEN
        PPACT   +0500000     ;SEE 2 and 0 (now cleared)
        POPJ   P,

PPSET2: PPSEL   2            ;PAGE PRINTER 2 ON
        PPACT   +0100000     ;SEE 2, erase 0
        DPYPOS  -400
        DPYSIZ  +04001      ;2 LINES AT BOTTOM OF SCREEN. SCROLL CONTINUOUSLY
        LEYPOS  0            ;LINE EDITOR AT BOTTOM OF SCREEN
        PPACT   +0500000     ;SEE 2 and 0 (now cleared)
        POPJ   P,

PPDOONE: PPACT  +0400000     ;SEE 0 (clear 2)
        DPYCLR
        POPJ   P,          ;FREE PP 2

BITDVC: EXP     MODE
        SIXBIT/TTY /
        EXP     IBF
IBF:    EXP     0,0,0
ITIBFS: BLOCK   100
        INTEGER INCMD,CHAN,LINE,RETAD,RETVL1,RETVL2,RETVL3,COUNT,FSTVAL,BITCHK

      END

```

10: Epipolar Registration Program

See section 4 for documentation on using this program.

Begin "epipolar determinations"

```

    REQUIRE "16A" COMPILER_SWITCHES; comment FIXR,FLTR,ADJSP;
    DEFINE  $\pi$ ="3.141592653";
    DEFINE UNLESS="WHILE -";
    DEFINE  $\alpha$ ="COMMENT ";
    DEFINE THRU="STEP 1 UNTIL";
    DEFINE TAB=" '11";
    DEFINE CR=" '15";
    DEFINE LF=" '12";
    DEFINE CRLF=" '15&'12";
    DEFINE CCRLF="&'15&'12";
    DEFINE NN=20;

    REQUIRE "CAMRAS.HDR[1,jfm]" SOURCE_FILE;
     $\alpha$  Gennery's camera solver;
    REQUIRE "MATRIX.HDR[1,JFM]" SOURCE_FILE;
     $\alpha$  Matrix operation utilities;
    REQUIRE "CHOSPT.HDR[S,HHB]" SOURCE_FILE;
     $\alpha$  Harlyn's point matcher;
    REQUIRE "PIXSAI[S,HE]" LIBRARY;
    REQUIRE "PIXFAI[S,HE]" LIBRARY;
     $\alpha$  Source files for image manipulation procedures: see below;
    EXTERNAL INTEGER PROCEDURE PIXEL(REFERENCE INTEGER PIX; INTEGER I,J);
     $\alpha$  gets the value PIX of a pixel of coordinates I,J;
    EXTERNAL PROCEDURE PUTEL(REFERENCE INTEGER PIX; INTEGER I,J,VALUE);
     $\alpha$  sets the value PIX of a pixel of coordinates I,J;
    EXTERNAL INTEGER PROCEDURE PFLDIM(STRING FILNAM);
     $\alpha$  gets the proper array dimension to represent the image called FILNAM;
    EXTERNAL INTEGER PROCEDURE GETPFL(STRING FILNAM; REFERENCE INTEGER PICTURE);
     $\alpha$  fills array starting at PICTURE ( for dimension see PFLDIM )
    with picture contained in file FILNAM;
    EXTERNAL INTEGER PROCEDURE
    PUTPFL(REFERENCE INTEGER PICTURE; STRING FILNAM; INTEGER MODE(1));
     $\alpha$  writes out a picture file FILNAM with data
    contained in array starting at PICTURE;
    EXTERNAL INTEGER PROCEDURE PIXDIM(INTEGER HEIGHT,WIDTH,BITS);
     $\alpha$  gets the proper array dimension to represent a HEIGHT x WIDTH image;
    EXTERNAL INTEGER PROCEDURE MAKPIX(INTEGER HEIGHT,WIDTH,BITS;
    REFERENCE INTEGER PICTURE);
     $\alpha$  creates an image array, starting at PICTURE, for a HEIGHT x WIDTH image;
    EXTERNAL PROCEDURE WIPE(REFERENCE INTEGER PIX; INTEGER value);
     $\alpha$  makes every pixel of the array equal to value;

     $\alpha$  Global variables;

    REAL ARRAY GG[1:5];
     $\alpha$  Adjusted values of the parameters (azimuth,elevation,pan,tilt,and roll);
    REAL ARRAY RM[1:3,1:3];
     $\alpha$  rotation matrix between base1 and base 2;
    REAL ALPHA,BETA,GAMMA,LAMDA,MU,NU;
     $\alpha$  translation vector components in base 1 and 2;
    INTEGER ECASE;
     $\alpha$  ECASE is a flag for the kind of geometry we have
    ECASE=1 : two epipoles ( most common case )

```

```

        ECASE=2 : one epipole in image 1
        ECASE=3 : one epipole in image 2
        ECASE=4 : no epipole;
INTEGER PBITS;
    a number of bits per pixel, returned by CHOSPT;
REAL ARRAY E1,E2[1:2];REAL ARRAY V1,V2[1:2];
    a points and vectors in images 1 & 2,
    epipoles or epipolar directions when they exist,
    else, generic points and vectors;
REAL FF1,FF2;
    a Focal distances in images 1 & 2;
REAL ARRAY M,MINV[1:2,1:2];
    a matrix A of the text and its inverse;
REAL K,N1;
    a generic and total epilines numbers: 0≤K≤N1;
REAL LOX,LOY,LNX,LNY;
    a dimensions of the images( output of CHOSPT) and of the transforms;
INTEGER IK,ILOX,ILOY,ILNX,ILNY;
    a the same, truncated, as integer variables;
REAL THETA,THETA0,THETA1,THETA2;
    a generic,minimum,maximum and increment
    angles under which image 1 is viewed from E1;
REAL PHI0,PHI1;
    a min and max angles for image 2;
REAL D1MIN,D1MAX,D2MAX,D2MIN,D;
    a minimum, maximum and generic distances from epipoles to images 1 & 2;
REAL ARRAY OF3[1:2];
    a offset for case 3, used in epilines calculation;
INTEGER I;
    a generic index;
BOOLEAN RIGHT1,RIGHT2;
    a true if epipole right of image, output of limits;
BOOLEAN DEBUG;
STRING P1,P2;
    a filenames for images P1 and P2;
INTEGER SIZEP,SIZES;
    a Size of the arrays that contain original and transformed image;

REAL ARRAY LX[1:NN]; a ARGUMENTS FOR CAMRAS;
REAL ARRAY LY[1:NN];
REAL ARRAY RX[1:NN];
REAL ARRAY RY[1:NN];

INTEGER NUM;

```

a I/O procedures:

```

INTEGER PROCEDURE GETANSWER;
    Begin INTEGER ANS; ANS=INCHRW LAND '137; PRINT(CRLF); RETURN(ANS) End;

BOOLEAN PROCEDURE ASK(STRING QUESTION);
    a ask a yes/no question;
    Begin "ask"
        INTEGER ASK;
        DO BEGIN print(question,"(Y or N)? ");
            ask=getanswer;
            END UNTIL ask="Y" v ask="N";
        return(if ask="Y" then TRUE else FALSE)
    End "ask";

PROCEDURE GETD(REFERENCE INTEGER NUM; STRING QUESTION; INTEGER EFAULT);
    Begin "GETD"
        PRINT(QUESTION);
        PTOSTR(0,CV(0,CV(L)));
        NUM ← CV(0,CV(L))
    End "GETD";

```

```

PROCEDURE SPACEPAUSE (STRING TEXT);
  BEGIN
    INTEGER T;
    PRINT(TEXT);
    DO T=INCHRW UNTIL T=" ";
    PRINT(CRLF);
  END;

PROCEDURE GETO (REFERENCE INTEGER NUM; STRING QUESTION; INTEGER DEFAULT);
  Begin "GETO"
    PRINT(QUESTION);
    PTOSTR(0,CVOS(DEFAULT));
    NUM ← CVO(INCHWL)
  End "GETO";

PROCEDURE GETF (REFERENCE REAL RNUM; STRING QUESTION; REAL DEFAULT);
  Begin "GETF"
    STRING NUMSTR; INTEGER BRCHAR;
    PRINT(QUESTION);
    PTOSTR(0,CVF(DEFAULT));
    RNUM ← REALSCAN(NUMSTR+INCHWL,BRCHAR);
  End "GETF";

```

a Arithmetic procedures:

```

SIMPLE PROCEDURE PROD2 (REAL ARRAY A,B,C);
  a multiplies 2*2 matrices;
  BEGIN
    REAL T;
    INTEGER I,J;
    FOR I=1 STEP 1 UNTIL 2 DO
      BEGIN
        T←0;
        FOR J=1 STEP 1 UNTIL 2 DO
          T ← T + B[I,J]*C[J];
        A[I]←T
      END
    END;

```

```

SIMPLE PROCEDURE PROD3 (REAL ARRAY A,B,C);
  a multiplies 3*3 matrices;
  BEGIN
    REAL T;
    INTEGER I,J;
    FOR I=1 STEP 1 UNTIL 3 DO
      BEGIN
        T←0;
        FOR J=1 STEP 1 UNTIL 3 DO
          T ← T + B[I,J]*C[J];
        A[I]←T
      END
    END;

```

```

PROCEDURE PARAMETERS;
  determines the rotation matrix R and the translation vector t in both bases;
  Begin "PARAMETERS"
    REAL ARRAY TM1[1:3,1:3],T1,T2[1:3];
    a TM1 is translation matrix (matrix A in Geometry)

```

```

      T1 and T2 are translation vectors in base 1 and base 2;
      REAL ARRAY A1,A2,B1,B2,B3,D[1:3,1:3];

      S1+S2+S3+3;
      ROTMAT(A1,D,GG[1],-2);
      ROTMAT(A2,D,GG[2],1);
      ROTMAT(B1,D,GG[3],2);
      ROTMAT(B2,D,GG[4],-1);
      ROTMAT(B3,D,GG[5],-3);
      MULT(TM1,A1,A2):  α translation matrix;
      MULT(D,B2,B1);
      MULT(RM,B3,D):  α rotation matrix;

      ALPHA+T1[1]+TM1[1,3]:  α translation vector is 3rd column of translation matrix;
      BETA+T1[2]+TM1[2,3];
      GAMMA+T1[3]+TM1[3,3];

      PROD3(T2,RM,T1):  α T2 is translation vector in second base;

      LAMDA+T2[1];
      MU+T2[2];
      NU+T2[3];

      PRINT("ROTATION MATRIX RM:",CRLF);
      PRINT(RM[1,1],RM[1,2],RM[1,3],CRLF);
      PRINT(RM[2,1],RM[2,2],RM[2,3],CRLF);
      PRINT(RM[3,1],RM[3,2],RM[3,3],CRLF);

      PRINT("TRANSLATION VECTOR t:",CRLF);
      PRINT(ALPHA,BETA,GAMMA,"IN BASE ONE",CRLF);
      PRINT(LAMDA,MU,NU,"IN BASE TWO",CRLF);

      end "PARAMETERS";

```

α Geometric procedures:

```

SIMPLE PROCEDURE RECT(REAL EX,EY,VX,VY,RO;REFERENCE REAL X,Y);

```

α rect returns the rectangular coordinates of a point with polar coordinates ro and α with respect to a shifted origin e(ex,ey).
 vx and vy are supposed proportional to cos α and sin α, but vx>0:
 α is always in $[-\pi/2, \pi/2]$, and RO should have a sign;

```

BEGIN "RECT"
  X=SQRT(VX*2+VY*2);
  VX=VX/X;
  VY=VY/X;
  X=EX+RO*VX;
  Y=EY+RO*VY;
END "RECT";

```

```

PROCEDURE POLAR( REAL EX,EY,X,Y; REFERENCE REAL THETA,RO);

```

α POLAR returns the polar coordinates of a point (x,y) with respect to a shifted origin (ex,ey)
 RO is always a positive number, and THETA is in the determination $[0, 2\pi]$;

```

Begin "POLAR"
  RO=SQRT((EX-X)*2+(EY-Y)*2);
  THETA=ATAN((EY-Y)/(EX-X));
  IF (X-EX)<0 THEN THETA=THETA+π;
  IF THETA < 0 THEN THETA=THETA+2*π;
END "POLAR";

```



```

SIMPLE PROCEDURE NEWX( REAL EX,EY,VX,VY;REFERENCE REAL NX);
  α A point E has the coordinates EX and EY in a plane where there is a vector V.
  If this plane is rotated so that V becomes the new X-axis, and shifted so
  that the old origin is anywhere on the new Y-axis, the new abscissa of
  E is just its projection onto V::
  BEGIN: NX=(EX*VX+EY*VY)/SQRT(VX*2+VY*2);END;

```

```

BOOLEAN PROCEDURE INPICTURE(REAL X,Y,LX,LY);
  RETURN( IF (0≤X≤LX ∧ 0≤Y≤LY) THEN TRUE ELSE FALSE);

```

```

PROCEDURE LIMITS( REAL LX,LY,EX,EY;REFERENCE REAL ALPHA0,ALPHA1,DMIN,DMAX;
  REFERENCE BOOLEAN RIGHT);

```

```

  α LIMITS returns:
  1) the minimum and maximum distances DMIN and DMAX from a point
  E to a rectangle of length LX and height LY with bottom left corner at
  origin.( typically, a picture and its epipole )
  2) The minimum and maximum angle through which the rectangle is viewed
  from point E. These angle ALPHA0 and ALPHA1 are in the determination
  [0,2π]( or occasionally, [-π/2,π/2] ) and the distances are consequently
  positive only.;

```

```

  BEGIN "LIMITS"
    REAL X,Y;
    REAL β1,β2,β3,β4;
    DMIN=SQRT(EX*2+EY*2); α initialize;
    DMAX=0;

    FOR X=1 THRU LX DO
      BEGIN
        α DESCRIBE HORIZONTAL SIDES OF RECTANGLE;
        DMAX=DMAX MAX SQRT((EX-X)*2+EY*2) MAX SQRT((EX-X)*2+(EY-LY)*2);
        DMIN=DMIN MIN SQRT((EX-X)*2+EY*2) MIN SQRT((EX-X)*2+(EY-LY)*2);
      END;
    FOR Y=1 THRU LY DO
      BEGIN
        α DESCRIBE VERTICAL SIDES OF RECTANGLE;
        DMAX=DMAX MAX SQRT(EX*2+(EY-Y)*2) MAX SQRT((EX-LX)*2+(EY-Y)*2);
        DMIN=DMIN MIN SQRT(EX*2+(EY-Y)*2) MIN SQRT((EX-LX)*2+(EY-Y)*2);
      END;

```

```

  α angle determination;
  α All angles are initially supposed in [0,2π];
  IF(0≤EX≤LX ∧ 0≤EY≤LY)THEN BEGIN
    α epipole is inside the image;
    ALPHA0=0;
    ALPHA1=2*π;
  END
  ELSE BEGIN
    α e1 is outside the image;
    determine the limit angles by inspecting the corners only;
    POLAR(EX,EY,0,0,β1,0);
    POLAR(EX,EY,LX,0,β2,0);
    POLAR(EX,EY,0,LY,β3,0);
    POLAR(EX,EY,LX,LY,β4,0);
    ALPHA1=(β1 MAX β2 MAX β3 MAX β4);
    ALPHA0=(β1 MIN β2 MIN β3 MIN β4);
    IF ALPHA1-ALPHA0>π THEN BEGIN
      α [0,2π] is not a convenient interval for our angles
      ( the epipole is left of the image, on the same vertical level);
      α Angles are in [-π/2,π/2];
      β1=ALPHA1;
      ALPHA1=ALPHA0;
      ALPHA0=β1-2*π;
    END
  END
  IF DEBUG THEN PRINT("EPIPOLE ON LEFT SIDE AND SAME VERTICAL LEVEL AS IMAGE:".CRLF);
  IF DEBUG THEN PRINT("FOR CONNEXITY, ANGLES ARE NOT CHOSEN IN [0,2π]");
  IF DEBUG THEN PRINT("IN LIMITS, α0= ",ALPHA0,CRLF);

```

```

IF DEBUG THEN PRINT("IN LIMITS,  $\alpha_1 =$ ", ALPHA1, CRLF);
END;
 $\alpha$  if epipole right of picture, set flag;
RIGHT $\leftarrow$ (EX>LX/2);
 $\alpha$  and invert scanning order by exchanging angles;
IF RIGHT THEN BEGIN
     $\beta_1 \leftarrow$  ALPHA1;
    ALPHA1 $\leftarrow$ ALPHA0;
    ALPHA0 $\leftarrow$  $\beta_1$ ;
END;
END;
END "LIMITS";

```

```

PROCEDURE FRAME( REAL EX,EY,VX,VY,LX,LY;REFERENCE REAL I1X,I1Y,I2X,I2Y;
REFERENCE BOOLEAN OUTFRAME);

```

α Given a point E and a vector V (they define a line), frame will determine, if they exist, the intersections of this line with the frame of the rectangle [0:LX,0:LY];

```

BEGIN "FRAME"
REAL X,Y;INTEGER FLAG;

```

```

PROCEDURE ASSIGN;
BEGIN "ASSIGN"
IF FLAG=0 THEN BEGIN I1X $\leftarrow$ X; I1Y $\leftarrow$ Y; END;
IF FLAG=1 THEN BEGIN I2X $\leftarrow$ X; I2Y $\leftarrow$ Y; END;
IF FLAG>1 THEN PRINT("ERROR IN PROCEDURE FRAME",CRLF);
FLAG $\leftarrow$ FLAG+1;
END "ASSIGN";

```

```
FLAG $\leftarrow$ 0;
```

```

IF VX=0 THEN BEGIN
X $\leftarrow$ 0;
Y $\leftarrow$ EY+(X-EX)*VY/VX;
IF INPICTURE(X,Y,LX,LY) THEN ASSIGN;
X $\leftarrow$ LX;
Y $\leftarrow$ EY+(X-EX)*VY/VX;
IF INPICTURE(X,Y,LX,LY) THEN ASSIGN;
END;

```

```

IF VY=0 THEN BEGIN
Y $\leftarrow$ 0;
X $\leftarrow$ EX+(Y-EY)*VX/VY;
IF INPICTURE(Y,X,LY,LX) THEN ASSIGN;
Y $\leftarrow$ LY;
X $\leftarrow$ EX+(Y-EY)*VX/VY;
IF INPICTURE(Y,X,LY,LX) THEN ASSIGN;
END;

```

```
OUTFRAME $\leftarrow$ (FLAG=0);
```

```

IF DEBUG THEN PRINT (" goes through : ",I1X,I1Y," and through: ",I2X,I2Y,CRLF);
END "FRAME";

```

```
PROCEDURE DETCASE;
```

α determines the nature of the epipolar geometry, according to the code:

```

case 1: two epipoles E1 and E2
case 2: one epipole E1
case 3: one epipole E2
case 4: no epipoles;

```

```

Begin "DETCASE"
  REAL THRESHOLD;  α MINIMUM POSITIVE NUMBER;
  GETF(THRESHOLD,"MINIMUM CONVERGENCE ALLOWED: ",0.0001);
  IF ABS(GAMMA)<THRESHOLD THEN
    IF ABS(NU)<THRESHOLD THEN ECASE=4
    ELSE ECASE=3
  ELSE IF ABS(NU)<THRESHOLD THEN ECASE=2
    ELSE ECASE=1;

  PRINT("                                CASE:",ECASE,CRLF);
end "DETCASE";

```

PROCEDURE EPIPOLES;
 α determines the epipoles and/or the epipolar directions
 It also calculates some parameters used by EPILINE (matrix M and offset OF3);

```

Begin "EPIPOLES"
  REAL DELTA; α Determinant of matrix M;

  IF (ECASE=1 ∨ ECASE=2) THEN BEGIN
    E1[1]=ALPHA*FF1/GAMMA;
    E1[2]=BETA*FF1/GAMMA;
    PRINT("EPIPOLE E1:",E1[1],E1[2],CRLF);
  END;

  IF (ECASE=1 ∨ ECASE=3) THEN BEGIN
    E2[1]=LAMDA*FF2/NU;
    E2[2]=MU*FF2/NU;
    PRINT("EPIPOLE E2:",E2[1],E2[2],CRLF);
    α M is the main conversion matrix;
    M[1,1]=NU*RM[1,1]-LAMDA*RM[3,1];
    M[1,2]=NU*RM[1,2]-LAMDA*RM[3,2];
    M[2,1]=NU*RM[2,1]-MU*RM[3,1];
    M[2,2]=NU*RM[2,2]-MU*RM[3,2];

    α Compute the inverse of matrix M for transformation P2→P1;
    DELTA=M[1,1]*M[2,2]-M[1,2]*M[2,1];
    IF DELTA=0 THEN PRINT("UNABLE TO INVERT MATRIX M : CAN'T DUMP

1") ELSE

      BEGIN
        MINV[1,1]= M[2,2]/DELTA;
        MINV[2,2]= M[1,1]/DELTA;
        MINV[1,2]= -M[1,2]/DELTA;
        MINV[2,1]= -M[2,1]/DELTA;
      END;

    IF ECASE=3 THEN BEGIN
      α and OF3 is an offset used in ECAE 3;
      OF3[1]=FF1*(NU*RM[1,3]-LAMDA*RM[3,3]);
      OF3[2]=FF1*(NU*RM[2,3]-MU*RM[3,3]);
    END;

  END;

  IF (ECASE=3 ∨ ECASE=4) THEN BEGIN
    V1[1]=ALPHA;
    V1[2]=BETA;
    IF V1[1]<0 THEN BEGIN V1[1]=-V1[1]; V1[2]=-V1[2] : 0;
    PRINT("EPIPOLAR DIRECTION V1:",V1[1],V1[2],CRLF);
  END;

  IF (ECASE=2 ∨ ECASE=4) THEN BEGIN
    V2[1]=LAMDA;
    V2[2]=MU;
    PRINT("EPIPOLAR DIRECTION V2:",V2[1],V2[2],CRLF);
  END;

```

End "EPIPOLES";

α more procedures;

PROCEDURE EPILINE;

Begin "EPILINE";

IF ECASE=1 THEN BEGIN

α This is an epipolar vector in P1;

THETA=THETA0+(K+0.5)*THETA2; α take middle of interval;

V1[1]=COS(THETA);

V1[2]=SIN(THETA);

α make v1 point to the right;

IF V1[1]<0 THEN BEGIN V1[1]=-V1[1];V1[2]=-V1[2] END;

α And this (V2) is the corresponding vector in P2;

PROD2(V2,M,V1);

α make v1 and v2 have consistent directions;

IF V1[1]*V2[1]<0 THEN BEGIN V2[1]=-V2[1];V2[2]=-V2[2];END;

END;

IF ECASE=2 THEN BEGIN

α This is an epipolar vector in P1;

THETA=THETA0+(K+0.5)*THETA2;

V1[1]=COS(THETA);

V1[2]=SIN(THETA);

α And this is a point belonging to the twin line in P2;

E2[1]=FF2*(RM[1,1]*V1[1]+RM[1,2]*V1[2])/(RM[3,1]*V1[1]+RM[3,2]*V1[2]);

E2[2]=FF2*(RM[2,1]*V1[1]+RM[2,2]*V1[2])/(RM[3,1]*V1[1]+RM[3,2]*V1[2]);

END;

IF (ECASE=3 ∨ ECASE=4) THEN

IF ABS(V1[2])*LOX≤V1[1]*LOY THEN BEGIN

α We pick a point on the Y axis;

E1[1]=0.0;

E1[2]=-(LOX*ABS(V1[2]/V1[1])+LOY)*(K+0.5)/N1;

IF V1[2]>0 THEN E1[2]=E1[2]-LOX*V1[2]/V1[1];

END

ELSE BEGIN

α We pick a point on the X axis;

E1[1]=-(LOY*ABS(V1[1]/V1[2])+LOX)*(K+0.5)/N1;

IF V1[2]>0 THEN E1[1]=E1[1]-LOY*V1[1]/V1[2];

E1[2]=0.0;

END;

IF ECASE=3 THEN BEGIN

α V2 directs the twin line in P2;

PROD2(V2,M,E1);

V2[1]=V2[1]+OF3[1];

V2[2]=V2[2]+OF3[2];

END;

IF ECASE=4 THEN BEGIN

α The twin line in P2 goes thru E2;

E2[1]=FF2*(RM[1,1]*E1[1]+RM[1,2]*E1[2]+RM[1,3]*FF1)

/(RM[3,1]*E1[1]+RM[3,2]*E1[2]+RM[3,3]*FF1);

E2[2]=FF2*(RM[2,1]*E1[1]+RM[2,2]*E1[2]+RM[2,3]*FF1)

/(RM[3,1]*E1[1]+RM[3,2]*E1[2]+RM[3,3]*FF1);

END;

End "EPILINE";

```

Begin "overhead";
  a DEBUG=ASK("DEBUG"); DEBUG=FALSE;
  IF DEBUG THEN SETPRINT("DEBUG","B");
  IF DEBUG THEN SETFORMAT(0,7) ELSE SETFORMAT(0,3);
  CHOSPTS(LX,LY,RX,RY,NUM,ILOY,ILOX,PBITS,P1,P2,TRUE);
  IF DEBUG THEN PRINT("NUM=",NUM,CRLF);
  IF DEBUG THEN SETFORMAT(0,7) ELSE SETFORMAT(0,3);
  LOY=ILOY;LOX=ILOX;
End "overhead";

```

PROCEDURE SOLVER;

a This procedure uses Gennery's code to do the camera registration from a set of corresponding points in the two images. It allows the user to pick the points on the images in an interactive way;

Begin "Solver"

```

REAL ARRAY X1[1:num],Y1[1:num],X2[1:num],Y2[1:num]; a chosen points;
REAL ARRAY SXX[1:num],SYY[1:num],SXY[1:num];
      GP[1:5],SP[1:5];
REAL ARRAY S[1:5,1:5]; a Covariance matrix of the errors in GG;
REAL ARRAY RESID[1:num,1:3];
REAL SD,ACC,Q,CONV;
INTEGER SDP,CORDST;
INTEGER SDF,MAXEDIT;
INTEGER NREJECT;
BOOLEAN ARRAY REJECT[1:num],FLAG[1:7];
BOOLEAN OUTPUT,RESOUT;

FOR I=1 THRU NUM DO
  Begin "copy values"
    X1[I]=LX[I];Y1[I]=LY[I];
    X2[I]=RX[I];Y2[I]=RY[I];
  End "copy values";
FOR I=1 THRU NUM DO
  SXX[I]=SXY[I]=SYY[I]=0;
  GETF(FF1,"Focal length :",320); FF2=FF1;
  GETD(MAXEDIT,"Number of points that can be rejected:",0);
  SDP=0.67;CORDST=0; SDF=0 ; OUTPUT=RESOUT=(1=1);
  GP[1]=1.57;GP[2]=GP[3]=GP[4]=GP[5]=0.0;

CAMERA(FF1,FF2,SDP,CORDST,SDF,NUM,MAXEDIT,OUTPUT,RESOUT,LX,LY,RX,RY,SXX,SYY,SXY,
      GP,SP,GG,S,RESID,SD,ACC,Q,CONV,NREJECT,REJECT,FLAG); a do the solving;

OUTSTR("Final values of parameters ~"&crlf);
PRINT(" azimuth:",CVF(GG[1]),crlf);
PRINT(" elevation:",CVF(GG[2]),crlf);
PRINT(" pan:",CVF(GG[3]),crlf);
PRINT(" tilt:",CVF(GG[4]),crlf);
PRINT(" roll:",CVF(GG[5]),crlf);

```

End "Solver";

PROCEDURE NEWDIM;

```

Begin "New_dimensions"
  PRINT(CRLF);
  GETF(N1,"NUMBER OF EPIPOLAR LINES: ",10);

```

CASE ECASE OF BEGIN "CASE 1"

BEGIN END;

BEGIN

```
LIMITS(LOX,LOY,E2[1],E2[2],PHI0,PHI1,D2MIN,D2MAX,RIGHT2);
IF INPICTURE(E2[1],E2[2],LOX,LOY) THEN LNX=D2MAX+D2MIN
ELSE LNX=D2MAX-D2MIN;
LIMITS(LOX,LOY,E1[1],E1[2],THETA0,THETA1,D1MIN,D1MAX,RIGHT1);
α theta2 is the incremental angle;
THETA2=(THETA1-THETA0)/N1;
α the epipole is either inside or outside;
IF INPICTURE(E1[1],E1[2],LOX,LOY) THEN LNX=D1MAX+D1MIN MAX LNX
ELSE LNX=D1MAX-D1MIN MAX LNX;
```

END;

BEGIN

```
NEWX(LOX,LOY,V2[1],V2[2],LNX);
LIMITS(LOX,LOY,E1[1],E1[2],THETA0,THETA1,D1MIN,D1MAX,RIGHT1);
IF INPICTURE(E1[1],E1[2],LOX,LOY) THEN LNX=D1MAX+D1MIN MAX LNX
ELSE LNX=D1MAX-D1MIN MAX LNX;
```

END;

BEGIN

```
NEWX(LOX,LOY,V1[1],V1[2],LNX);
LIMITS(LOX,LOY,E2[1],E2[2],PHI0,PHI1,D2MIN,D2MAX,RIGHT2);
IF INPICTURE(E2[1],E2[2],LOX,LOY) THEN LNX=D2MAX+D2MIN MAX LNX
ELSE LNX=D2MAX-D2MIN MAX LNX;
```

END;

BEGIN

```
NEWX(LOX,LOY,V2[1],V2[2],LNX);
NEWX(LOX,LOY,V1[1],V1[2],LNY);
LNX=LNX MAX LNY;
```

END;

END "CASE 1";

LNX=LNX+1;

LNY=LNY+1;

α prepare the integers to be used as indexes for arrays;

IK=K:ILOX+LOX;ILOY+LOY;ILNX=LNX;ILNY=LNY;

PRINT("THE DIMENSION OF THE NEW PICTURES WILL BE: ",ILNX,"(+4) X ",ILNY,CRLF);

END "New_dimensions";

PROCEDURE PRINTLINE;

BEGIN "PRINTLINE"

BOOLEAN OUTFRAME,MANUAL,PAUSE;

REAL X1,Y1,X2,Y2;

INTEGER IX1,IX2,IY1,IY2;

```
print(" If you chose the step-by-step option, the execution stops between",crlf);
print(" each line, waiting for you to type Y",crlf);
print(" If you do not chose this option, the execution proceeds automatically.",crlf);
print(" either in SLOW or FAST mode",crlf,crlf);
print("When printing is completed, type Y in both cases to return to the main program."
```

f);

MANUAL= ASK(" STEP-BY-STEP PRINTING ");

IF MANUAL THEN ELSE PAUSE=ASK("SLOW MOTION");

INITOVERLAY;

FOR K=0 THRU N1-1 DO

BEGIN "H'LOOP"

```

IF MANUAL THEN ASK(" LEFT ")
ELSE IF PAUSE THEN CALL (1,"SLEEP");
EPILINE;
FRAME(E1[1],E1[2],V1[1],V1[2],LOX,LOY,X1,Y1,X2,Y2,OUTFRAME);
IF OUTFRAME THEN PRINT("EPILINE # ".K," OFF PICTURE 1",CRLF)
ELSE BEGIN
    IX1←X1;IX2←X2;IY1←Y1;IY2←Y2;
    SETLEFT;
    OVERLINE(IX1,IY1,IX2,IY2);
END;

IF MANUAL THEN ASK("RIGHT ")
ELSE IF PAUSE THEN CALL (1,"SLEEP");
a PRINT ("      In picture 2. ");
FRAME(E2[1],E2[2],V2[1],V2[2],LOX,LOY,X1,Y1,X2,Y2,OUTFRAME);
IF OUTFRAME THEN PRINT("EPILINE # ".K," OFF PICTURE 2",CRLF)
ELSE BEGIN
    SETRIGHT;
    IX1←X1;IX2←X2;IY1←Y1;IY2←Y2;
    OVERLINE(IX1,IY1,IX2,IY2);
END;

END "MNLOOP";
SPACEPAUSE("Type <space> to continue: ");
FINIOVERLAY;

END "PRINTLINE";

```

PROCEDURE NEWC1(REAL X,Y;REFERENCE REAL Z;REFERENCE INTEGER N);

a X and Y are the coordinates of a point in picture 2.
 NEWC2 returns N and Z which are the number of the epipolar line(new ordinate)
 and the position of the point on this line (new abscissa).;

```

begin "newc1"
    IF ECASE=1 THEN BEGIN
        POLAR( E1[1],E1[2],X,Y,THETA,Z);
        IF(THETA0≤THETA+π≤THETA1) THEN THETA←THETA+π;
        IF(THETA0≤THETA-π≤THETA1) THEN THETA←THETA-π;
        Z←Z-D1MIN;
        N←N1*(THETA-THETA0)/(THETA1-THETA0)-0.5;
        END ELSE PRINT("SORRY, DEGENERATE CASE NOT YET DEVELOPPED");
    end "newc1";

```

PROCEDURE NEWC2(REAL X,Y;REFERENCE REAL Z;REFERENCE INTEGER N);

a NEWC2 does the same as newc2 in picture 2, but since the epilines are referenced
 by their position in picture 1, this involve some transformation first.;

```

begin "newc2"
    IF ECASE=1 THEN BEGIN
        POLAR(E2[1],E2[2],X,Y,THETA,Z);
        Z←Z-D2MIN;
        V2[1]←COS(THETA);
        V2[2]←SIN(THETA);
        a And this (V1) is the corresponding vector in P1;
        PROD2(V1,MINV,V2);
        a now we find which angle v2 correspond to and what epiline that is;
        THETA←ATAN(V1[2]/V1[1]);
        IF(THETA0≤THETA+π≤THETA1) THEN THETA←THETA+π;
    end "newc2";

```

```

      IF (THETA0 ≤ THETA - w ≤ THETA1) THEN THETA ← THETA - w;
      N ← N1 * (THETA - THETA0) / (THETA1 - THETA0) - 0.6;
    END ELSE PRINT("SORRY, DEGENERATE CASE NOT YET DEVELOPPED");
  end "newc2";

```

```

PROCEDURE TRANSFORM;
  BEGIN "TRANSFORM"

```

```

    BOOLEAN OUTFRAME;
    REAL X1,Y1,X2,Y2;
    INTEGER IX1,IX2,IY1,IY2,NX,NM1,VALUE;
    SAFE INTEGER ARRAY PP[0:SIZEP-1],SS[0:SIZE-1];  α INPUT AND OUTPUT ARRAYS;
    INTEGER XMIN,XMAX,N;      α Length info;
    STRING EP1,EP2; α transforms filenames;

```

```

PROCEDURE CLEARARRAY;
  BEGIN
    FOR IK ← 0 THRU N1-1 DO
      FOR I ← 0 THRU ILNX-1 DO
        PUTEL(SS[0],IK,I,0);
      END;
    END;

```

```

PROCEDURE TRLINE( INTEGER IM; REAL EX,EY,DMAX,DMIN; BOOLEAN INVERT );

```

```

  BEGIN "TRLINE"
    REAL LOWERD,UPPERD; α PICTURE BOUNDS;
    REAL VX,VY;
    IF DEBUG THEN PRINT("EPILINE # ",K,CRLF);
    EPILINE;
    IF IM=1 THEN BEGIN VX←V1[1];VY←V1[2];END
    ELSE BEGIN VX←V2[1];VY←V2[2];END;
    FRAME(EX,EY,VX,VY,LOX,LOY,X1,Y1,X2,Y2,OUTFRAME);
    IF OUTFRAME THEN PRINT("EPILINE # ",K," OFF PICTURE ",IM,CRLF)
    ELSE BEGIN
      IK←K;IX1←X1;IX2←X2;IY1←Y1;IY2←Y2;
      IF DEBUG THEN ELSE OVERLINE(IX1,IY1,IX2,IY2);
      XMIN←DMAX;XMAX←0;      α Initialize;
      IF INVERT THEN BEGIN UPPERD←DMIN;LOWERD←DMAX;END
      ELSE BEGIN UPPERD←DMAX; LOWERD←DMIN; END;
      FOR D← LOWERD THRU UPPERD DO
        BEGIN "pt-by-pt"
          RECT(EX,EY,VX,VY,D,X1,Y1);
          IF INPICTURE(X1,Y1,LOX,LOY) THEN
            BEGIN "transfer"
              IX1←X1;IY1←Y1; α coordinates on source image;
              VALUE←PIXEL(PP[0],IY1,IX1);
              IF DEBUG THEN OVERLINE(IX1,IY1,IX1,IY1);
              NX←D-LOWERD;
              XMIN←XMIN MIN NX;
              XMAX←XMAX MAX NX;
              PUTEL(SS[0],IK,NX+4,VALUE);
            END "transfer";
          END "pt-by-pt";

```

```

      N←XMIN LSH -8; α 8 MSBs of beginning of line;
      PUTEL(SS[0],IK,0,N);
      N←XMIN LSH 0 '377; α 8 LSBs of beginning of line;
      PUTEL(SS[0],IK,1,N);
      N←XMAX LSH -8; α 8 MSBs of end of line;
      PUTEL(SS[0],IK,2,N);
      N←XMAX LSH 0 '377; α 8 LSBs of end of line;
      PUTEL(SS[0],IK,3,N);

```



```
-----  
α Start of main program;  
BEGIN"Main"  
OVERHEAD;  
DO BEGIN  
  SOLVER;  
  PARAMETERS;  
  DETCASE;  
  EPIPOLES;  
  NEWDIM;  
  
  IF ASK("TRANSFORM THE IMAGES INTO EPIPOLAR SPACE ") THEN  
    IF ECASE=1 THEN BEGIN  
      SIZP=PFLDIM(P1);  
      SIZP=PFLDIM(P2) MAX SIZP;  
      ILNX=ILNX+4; α make space for line length info;  
      SIZS=PIXDIM(ILNY,ILNX,PBITS);  
      TRANSFORM;  
    END  
    ELSE PRINT("NO TRANSFORMATION FOR DEGENERATE CASE")  
  ELSE IF ASK("DRAW EPIPOLAR LINES ") THEN PRINTLINE;  
  
  IF ASK("DUMP THE PARAMETERS ") THEN DUMP;  
  
  END UNTIL ASK("ANOTHER TRY ")=FALSE;  
  
END "Main";  
  
End "epipolar determinations";
```

END;

END "TRLIN";

a body of procedure transform;

a DEBUG=ASK("DEBUG");

```

PRINT("NEW LEFT PICTURE: ");
EP1=INCHWL;
PRINT("NEW RIGHT PICTURE: ");
EP2=INCHWL;

PRINT("PICTURE 1:",CRLF);
INITOVERLAY;
SETLEFT;
GETPFL(P1,PP[0]);
MAKPIX(ILNY,ILNX,PBITS,SS[0]);
FOR K=0 THRU M1-1 DO TRLINE(1,E1[1],E1[2],D1MAX,D1MIN,RIGHT1);
PUTPFL(SS[0],EP1);
FINIOVERLAY;

INITOVERLAY;
PRINT("PICTURE 2:",CRLF);
SETRIGHT;
GETPFL(P2,PP[0]);
MAKPIX(ILNY,ILNX,PBITS,SS[0]);
CLEARARRAY;
FOR K=0 THRU M1-1 DO TRLINE(2,E2[1],E2[2],D2MAX,D2MIN,RIGHT2);
PUTPFL(SS[0],EP2);
SPACEPAUSE("Type <space> to continue: ");
FINIOVERLAY;

END "TRANSFORM";

```

PROCEDURE DUMP;

BEGIN "DUMP"

```

SETFORMAT(0.7);
SETPRINT(NULL,"B");

PRINT("ECASE= ",ECASE,CRLF);
PRINT("N1= ",N1,CRLF);
PRINT("E1[1]= ",E1[1],CRLF);
PRINT("E1[2]= ",E1[2],CRLF);
PRINT("E2[1]= ",E2[1],CRLF);
PRINT("E2[2]= ",E2[2],CRLF);
PRINT("THETA0= ",THETA0,CRLF);
PRINT("THETA1= ",THETA1,CRLF);
PRINT("D1MIN= ",D1MIN,CRLF);
PRINT("D2MIN= ",D2MIN,CRLF);
PRINT("MINV[1,1]= ",MINV[1,1],CRLF);
PRINT("MINV[1,2]= ",MINV[1,2],CRLF);
PRINT("MINV[2,1]= ",MINV[2,1],CRLF);
PRINT("MINV[2,2]= ",MINV[2,2],CRLF);

SETPRINT(NULL,"T");

END "DUMP";

```

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