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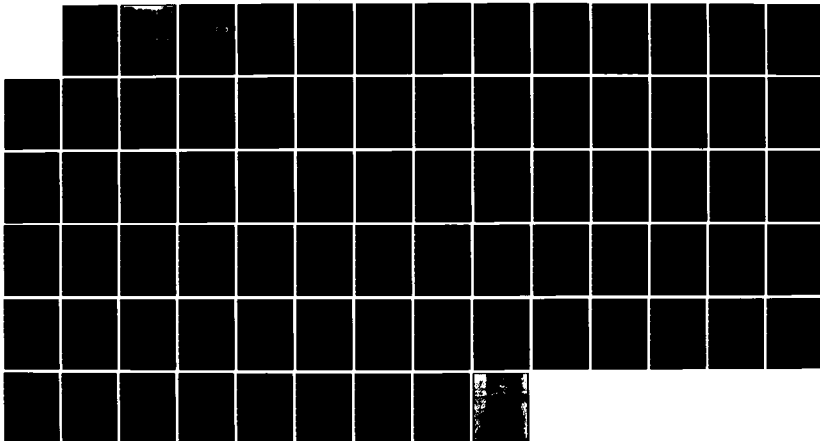
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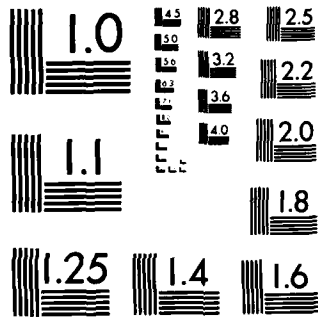
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ACHIEVING GENERALITY OVER CONDITIONS:  
COMBINING THE MULTITRAIT MULTIMETHOD MATRIX  
AND THE REPRESENTATIVE DESIGN OF EXPERIMENTS

Kenneth R. Hammond, Robert M. Hamm,  
and Janet Grassia

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Report No. 255  
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block 20

each concept. The criterion measures make it possible to complement Campbell and Fiske's internal validity matrix with an external validity matrix. Inclusion of the correlations among criteria in the external validity matrix is consistent with Brunswik's argument that generalization over conditions depends upon the representation of ecological relations among experimental conditions. Procedures are described for computing measures of convergent and discriminant validity for each matrix and for combining the data from both matrices.

ACHIEVING GENERALITY OVER CONDITIONS:  
COMBINING THE MULTITRAIT MULTIMETHOD MATRIX AND THE REPRESENTATIVE  
DESIGN OF EXPERIMENTS

Doubts about the generality of results produced by psychological research have been expressed with increasing frequency since Koch observed, after a monumental review of scientific psychology in 1959, that there is "a stubborn refusal of psychological findings to yield to empirical generalization" (1959, pp. 729-788). Brunswik (1952, 1956), Campbell and Stanley (1966), Cronbach (1975), Epstein (1979, 1980), Einhorn and Hogarth (1981), Greenwald (1975, 1976), Hammond (1966), Meehl (1978) and Simon (1979) among others, have also called attention to this situation and some (Epstein, 1980; Greenwald, 1976) have referred to it as a "crisis." All regard it as a fundamental, persistent problem in psychological research.

In an effort to develop a methodology that will provide generality without the loss of rigor, we build upon two previous methodological suggestions, (a) the multitrait multimethod matrix introduced by Campbell and Fiske (1959) and (b) the representative design of experiments introduced by Brunswik (1956). Data from a study of experts who were required to employ three modes of cognition in each of three judgment tasks (see Appendix A) provided a unique opportunity not only to make use of the multitrait multimethod matrix, but to extend it.

In their 1959 study of the field of individual differences, Campbell and Fiske convincingly demonstrated the faults of the conventional single-concept single-operation methodology. The overwhelming majority of studies they examined showed that results were more likely to be determined by the methods employed by the experimenters than by the traits hypothesized to account for the results. Although they showed that this failure to separate the effects of operation (method) from the effects of concept (trait) can be both demonstrated and avoided by use of the multitrait multimethod matrix, there has been little change in conventional research methodology.

The problem is not that Campbell and Fiske's work went unrecognized. It became a milestone in the methodological literature of psychology, and by 1983 had been cited over 1000 times. Yet in spite of the potential of the multitrait multimethod matrix for breaking the grip of a simpleminded operationism on psychological research, the method is for the most part simply not used. Presumably researchers have avoided it for tactical reasons, since it introduces conceptual complexity (which concepts and which methods should be compared?) and requires considerable additional labor and apparatus within a single study. Or perhaps there is general unawareness of the ephemeral character of results produced by single-concept single-method operationism. Whatever the reason, among tens of thousands of studies of individual differences, Turner (cited in Fiske, 1981) found only 70 published matrices between 1967 and 1980 (see Fiske, 1981, for a general review).

The multitrait multimethod matrix has probably never been used in experimental psychology, although its logic is equally applicable to that field (cf. Fiske, 1981). We examined the 62 articles in Volume 9 (1983) of the Journal of Experimental Psychology: Human Perception and Performance to ascertain whether researchers currently make a systematic effort to separate method variance from concept variance. The persistence of one-concept one-method operationism was evident: only 18 articles were found to employ more than one concept or more than one method; and of these, only four used more than one concept and more than one method. None, however, systematically separated method variance from concept variance; only one of the authors indicated cognizance of this methodological requirement. The multitrait multimethod approach was never mentioned.

In parallel fashion, Brunswik's (1943, 1952, 1956) argument that generalization over conditions requires the representation of ecological conditions in the design of experiments must be considered a milestone in the methodological literature of psychology; his work, too, has been cited over 1000 times, yet representative designs are seldom employed (see Hammond & Wascoe, 1980, for some examples). Representative design was never mentioned in the 62 articles examined in the volume cited above. The same reasons that led students of individual differences to forgo the use of the multitrait multimethod matrix also lead experimental psychologists to forgo the use of representative design; both are more difficult and time-consuming to execute than standard laboratory experiments.

### Plan of the Article

In what follows we first present a description of the Campbell/Fiske internal validity matrix; second, indicate our extension of it to an external validity matrix that incorporates the theory of representative design of experiments; third, show the complementarity of the two matrices; and fourth, illustrate how both matrices can be used to achieve generalization over conditions.

### The Campbell-Fiske Internal Validity Matrix

The internal validity multitrait multimethod matrix, presented in Table 1, is developed from a set of test scores taken from a group of subjects (Campbell & Fiske, 1959). The scores for each subject are correlated over several traits and methods. The authors describe the matrix as follows:

This illustration involves three different traits, each measured by three methods, generating nine separate variables. It will be convenient to have labels for various regions of the matrix, and such have been provided in Table [1]. The reliabilities will be spoken of in term of three reliability diagonals, one for each method. The reliabilities could also be designated as the monotrait-monomethod values. Adjacent to each reliability diagonal is the heterotrait-monomethod triangle. The reliability diagonal and the adjacent heterotrait-monomethod triangle make up a monomethod block. A heteromethod block is made up of a validity diagonal (which could also be designated as monotrait-heteromethod values) and the two

heterotrait-heteromethod triangles lying on each side of it. Note that these two heterotrait-heteromethod triangles are not identical.

In terms of this diagram, four aspects bear upon the question of validity. In the first place, the entries in the validity diagonal should be significantly different from zero and sufficiently large to encourage further examination of validity. This requirement is evidence of convergent validity. Second, a validity diagonal value should be higher than the values lying in its column and row in the heterotrait-heteromethod triangles. That is, a validity value for a variable should be higher than the correlations obtained between that variable and any other variables having neither trait nor method in common. This requirement may seem so minimal and so obvious as to not need stating, yet an inspection of the literature shows that it is frequently not met, and may not be met even when the validity coefficients are of substantial size. In Table [1], all the validity values meet this requirement. A third common-sense desideratum is that a variable correlate higher with an independent effort to measure the same trait than the measures designed to get at different traits which happen to employ the same method. For a given variable, this involves comparing its values in the validity diagonals with its values in the heterotrait-monomethod triangles. For variables A1, B1, and C1, this requirement is met to some degree. A fourth desideratum is that the same pattern of trait interrelationship be shown in all of the heterotrait triangles of both the monomethod and

heteromethod blocks. The hypothetical data in Table [1] meet this requirement to a very marked degree, in spite of the different general levels of correlation involved in the several heterotrait triangles. The last three criteria provide evidence for discriminant validity. (1959, pp. 82-83).

The value of this methodology is indisputable, and its application will yield definite and useful conclusions regarding the validity of psychological traits or theoretical concepts in general (see, e.g., Brewer & Collins, 1981; Fiske, 1981). The results from such a matrix will have populational and task generality insofar as the trait domain, the apparatus/method domain and the subject domain have been adequately sampled. The results, therefore, speak to the question of the construct validity of the traits investigated separate from the methods used, within the restraints chosen by the investigator.

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Insert Table 1 about here  
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#### Extension of the Campbell/Fiske Approach

Campbell and Fiske (1959) developed the multitrait multimethod matrix in order to evaluate the (a) internal validity of certain (b) traits within the study of (c) individual differences based on (d) group data. We extend their method by (a) adding an external validity matrix; (b) using both the internal and the external validity matrices to evaluate concepts in general instead of traits; (c) using both matrices to test propositions, in the tradition of experimental psychology; (d) making the behavior of the individual rather than of the group the fundamental unit of analysis, although group data can be analyzed as well. (See Hammond, McClelland, &

Mumpower, 1980, pp. 115-127 on the advantages of single-subject analysis; also Meehl, 1978, on the deficiencies of conventional between-group and within-group analyses.)

### The External Validity Matrix

Table 2 presents an external validity matrix that is based upon correlations between nine sets of engineers' judgments, made under three methods (cognitive modes) for each of three concepts, and three criteria. The three validity diagonals contain monoconcept correlations between each set of judgments (one for each method) and the criterion of the same concept against which the judgments are compared. The triangles consist of heteroconcept correlations between the judgments made in each condition (concept-method unit) and the criterion for a different concept. A method block consists of a validity diagonal and the heteroconcept triangles on either side of it.

The coefficients in the external validity matrix in Table 2 are different from those in the internal validity matrix in that each correlation in the external validity matrix is between judgments and measures of a criterion rather than between two responses. Aside from this very important difference, the interpretation of the coefficients with respect to the questions of convergent and discriminant validity is quite similar. As in the internal validity matrix, correlations in the external validity diagonal that are sufficiently large are evidence of convergent validity. In Table 2 the coefficients in the diagonals within each method block would show the external convergent validity of the judgment of each concept by that method. Comparison of the average of these diagonal values across the three concepts would indicate the relative external convergent

validity of each method. The heteroconcept triangles consist of the correlations of the expert's judgments of one concept (by a particular method) with the criterion measure of a different concept. Evidence of discriminant validity exists when a value in a validity diagonal is higher than the values lying in its column and row in the heteroconcept triangles. Further tests of external discriminant validity are described below.

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Insert Table 2 about here  
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The External Validity Matrix and the Representative Design of Experiments

The argument for the representative design of experiments is explicated in the external validity matrix because the naturally occurring intercorrelations among criterion variables are represented in the matrix (see Table 2). For example, if the correlation between criteria for c1 and c2 in Table 2 were .5, we would expect all correlations between judgments of c1 and the criterion for c2 (and vice versa) to be as high as but no higher than .5 if an engineer is performing appropriately. The intercorrelations among the criteria, or intraecological correlations, thus provide a standard for the heteroconcept correlations in the external validity matrix, and in the internal validity matrix as well. Without ecological representativeness as a standard, all such intercorrelations are changed by the experimenter to zero in the conventional systematic design of experiments. Therefore, generalization cannot be achieved on logical grounds, and indeed is not achieved empirically, as the psychologists cited above emphasized.

Complementarity of the Internal and External Validity Matrices: Evaluating Coherence, Performance, and Competence

The usefulness of analyzing the external validity matrix in conjunction with Campbell and Fiske's internal validity matrix is that the information provided by these matrices is complementary and makes possible an evaluation of cognitive coherence, performance, and competence. The distinction between coherence and performance is intended to parallel the traditional distinction between the coherence and correspondence theories of truth (see, e.g., White, 1967 and Prior, 1967). The coherence theory focuses on the extent to which statements of facts or judgments put forward cohere (or "hang together") with one another, that is, are related by logical implication. The internal validity matrix parallels the coherence theory of truth in the sense that it demands logical rather than external, empirical justification. Although the internal matrix does include empirical, factual material, no reference to empirical criteria outside the matrix itself is required to establish the internal validity of a set of psychological concepts. All that is required is that a logical criterion be met, namely, that convergent validities should be high and discriminant validities should be low.

The correspondence theory of truth, on the other hand, is concerned with the extent to which our beliefs about the world perform, or correspond, with respect to independently determined facts. Therefore an independent measure of the concepts in question is required in order to test the correspondence between what a theory predicts and what exists. The external validity matrix thus parallels the correspondence theory of truth in that it demands the evaluation of the empirical correspondence between psychological concepts and some independent measure of them.

Finally, because both matrices can be developed for a single subject (as we demonstrate below), it is possible to combine the results from each matrix into a single measure to provide a higher order indicator of each expert's judgment that we shall call "competence" (see also McClelland, 1973). Since we derive the measure of competence from measures of coherence and performance that are based on variations in both method and concept, our derivation copes directly with the problem of generalization. In the present case, for example, the conclusions about an expert's coherence and performance, and thus competence, are clearly based on, and thus limited to, his/her behavior over the three methods and three concepts employed in the study.

Summary of Similarities and Differences between Campbell and Fiske (1959) and the Present Approach

The two efforts are similar in that each provides comparisons of convergent validities and discriminant validities across concepts and methods (see Tables 1 and 2); but there are several differences. First, the internal validity matrix does not include test-criterion relations, but the external validity matrix does. Therefore it contains correlation coefficients that indicate the relation between measures of each subject's behavior and external, empirical criteria. As a result, the meaning of the entries in the cells is different in the two matrices. The correlation coefficient in each cell in the Campbell/Fiske internal validity matrix indicates the correlation between pairs of test measures, whereas the correlation coefficients in the external validity matrix indicate the correlation between a behavioral measure and an external criterion.

Second, the role of the individual subject in the two kinds of analysis is very different. Each correlation coefficient in the Campbell and Fiske (1959) multitrait multimethod matrix is across individuals, while in a multiconcept multimethod analysis each is across the objects of judgment, within a single individual. More specifically, in a multitrait multimethod analysis, each of  $n$  individuals is measured on  $j$  (traits) times  $k$  (methods) occasions, and one multitrait multimethod matrix is made for the whole set of individuals. In a multiconcept multimethod analysis, each of  $n$  individuals judges each of  $p$  objects on  $j$  (concepts) times  $k$  (methods) occasions, and a separate multiconcept multimethod matrix is constructed for each of the  $n$  individuals.

Third, because the external validity matrix must contain at least two criterion variables in order to separate concept from method, the relations between criteria in circumstances toward which the generalization is intended must be measured and taken into consideration when the subject's performance is evaluated. Conventional experimental psychology has been able to sidestep this matter only because of its persistent, implicit acceptance of single-concept single-method operationism. It is precisely at this point, however, that the external validity matrix is directly linked to Brunswik's (1956) representative design of experiments. In representative designs, intra-ecological correlations between criteria cannot be ignored and arbitrarily set to zero as is customary. This convention introduces a design feature that must, and has, frustrated generalization of results because the results are obtained under conditions seldom if ever present in the conditions of application. The use of representative design, however, means that correlations among criterion variables in the experiment will represent those in the circumstances to

which the results of the experiment are intended to generalize, or apply. In short, the same logic of inductive inference that we apply when generalizing from subject sample to subject population will apply to generalizing from experimental conditions to any other set of conditions (see, for example, Brunswik, 1943, 1952, 1956; Hammond, 1966; Hammond & Wascoe, 1980; Einhorn & Hogarth, 1981; Epstein, 1979, 1980).

Fourth is a difference in aims. Campbell and Fiske's principal aim was to enhance our methodological ability to evaluate the construct validity of traits (Cronbach & Meehl, 1955). We take that aim to have been achieved in principle (no one has challenged it), if not in practice. We aim therefore to build upon that achievement by showing that both matrices can be applied to experimental psychology as well as to the study of individual differences (cf. Cronbach, 1975). In addition, we intend to show that the internal validity matrix and the external validity matrix provide complementary information: (a) the internal validity matrix method can be used to evaluate the coherence of an expert's judgments, (b) the external validity matrix can be used to evaluate the performance of an expert's judgments, and (c) measures of coherence and performance can be combined to provide a measure of competence.

#### Illustrative Application

##### The Use of the Internal Validity Matrix in a Study of Expert Judgment

Data for an internal validity matrix based on a study of 20 highway engineers' judgments of the concepts of aesthetics, safety and capacity using intuitive, quasi-rational, and analytical methods (see Appendix A) are presented in Table 3. The data for the matrix were generated from the

mean of the 20 engineers' judgments for each of the 40 highways presented to them for each concept-method pair. Thus, the matrix illustrates the particulars of the behavior of an artificial engineer constructed from the mean judgments of this group. Data from the artificial engineer are presented mainly to illustrate the use of the method; no inferences can be drawn from the matrix in Table 3 to a matrix generated by any one engineer. Illustrations of individual matrices are provided below.

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Insert Table 3 about here  
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Each of the descriptions of the matrix presented by Campbell and Fiske (1959) apply to the matrix in Table 3. The three validity diagonals contain values that are high, relative to the heteroconcept triangles adjacent to them, thus providing evidence for internal convergent and discriminant validity.

#### Use of the External Validity Matrix in a Study of Expert Judgment

Table 4 presents the artificial engineer's external validity matrix, also based on the mean of 20 engineers' judgments.

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Insert Table 4 about here  
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Convergent validity of concepts. The external validity coefficient for the artificial engineer's aesthetics judgments made by the film strip method is .855, by the bar graph method is .945, and by the formula method is .951, thus producing a mean external convergent validity value across all three methods of .926 for aesthetic judgments. (Note: Fisher's z-transformation is used in the calculation of mean values.) Averaging

validity correlations pertaining to safety from the three method boxes, the mean convergent validity is .568; similarly, averaging the judgment-criterion correlations for capacity produces a mean convergent validity value of .530. In short, the data suggest that, irrespective of the method used, the artificial engineer judged highway aesthetics more accurately than highway safety or capacity, and judged safety and capacity with equal accuracy.

Convergent validity of methods. A measure of the external convergent validity for each method may be calculated by averaging the judgment-criterion correlations within each of the diagonals (.86, .70, .29; .95, .68, .83; .95, .23, .27), thus obtaining external validities for each method (.67, .85, .65). These results suggest that the artificial engineer judged these three concepts most accurately in the quasi-rational mode. Finally, the mean of the latter three coefficients is .74. This measure is informative because it may be used to compare one group of experts with another, to compare one individual with another (in the case when a matrix is constructed for each individual), or to evaluate the effect of a change in condition in either case. Moreover, the referential domain of this measure is clear; it is general over the three methods and three concepts employed in the study, as well as the group of engineers selected.

Measuring discriminant validity with reference to intra-ecological correlations. The intra-ecological correlations among empirical measures of the concepts permit an additional method for assessing discriminant validity. The correlation between the criterion measures of the concepts provides a standard against which to compare the heteroconcept correlations

between the expert's judgment of one concept and the criterion measure of a different concept. For example, if the correlation between aesthetics and safety is  $-.275$ , then it is appropriate for an engineer's judgments of aesthetics to be correlated  $-.275$  with safety (see Appendix B). Similarly, if the correlation between two criterion measures is low (as for safety and capacity,  $.180$ ), then the heteroconcept correlations should also be low. In short, the observed correlations between judgments of aesthetics, safety and capacity for an engineer are not to be compared to a standard of zero (an arbitrary demand for complete independence regardless of task conditions) but to a standard that is representative of task conditions, if we are properly to evaluate the discriminant validity of the judgments of these concepts with these methods.

To "untie" these variables, in other words to force zero intercorrelations among them, is (a) to invite the engineer to judge an unrepresentative set of conditions and thus (b) to extrapolate his results illegitimately from irrelevant conditions to the relevant ones. These two tactics have an embarrassingly long history in psychology; they are customarily explained away by arguments that "this is the best we can do" and/or "it doesn't matter, anyway." Neither argument is correct, but neither is necessary; the external validity form of the multiconcept multimethod matrix makes it possible to evaluate the competence of experts (or other subjects) in relation to the task conditions to which their judgments are to be applied.

The examples presented below illustrate the detailed application of both the internal and external validity matrices to the study of expert judgment. The first section describes the use of both matrices for testing

propositions in the context of experimental psychology, and the second describes the use of the matrices in connection with the study of individual differences.

### Application to Experimental Psychology

#### Internal Validity Matrix

The analyses to be reported in this section require that a matrix, similar to that for the artificial engineer of Table 3, above, be produced for each engineer, and that convergent or discriminant validities be determined for each.

It is possible to derive one criterion of convergent validity and four criteria of discriminant validity from the internal validity matrix. The criterion for convergent validity and one for discriminant validity are described below. The remaining criteria for internal discriminant validity are described in Appendix C.

Convergent validity. The convergent validity measure (monoconcept heteromethod correlations between judgments of the same concept using different methods) can be used to test hypotheses concerning the empirical status of each concept. For example,

H1: Each theoretical concept has empirical meaning, i.e., there is convergent validity for each concept across methods and within an appropriate sample of subjects.

Hypothesis 1 can be tested by asking whether, for each subject, judgments of the quantity of a concept covary, independently of the methods used to make the judgments. For example, for the artificial engineer (Table 3) the correlation between the film strip and bar graph methods for the aesthetics concept is .890; for the film strip and formula methods, .864; and for the bar graph and formula methods, .985. The overall convergent validity for aesthetics is the mean of these correlations (z-transformed), .938, which is significant at  $p < .001$ . A matrix was developed for each of the 20 engineers individually, and this procedure was carried out for each of the three concepts. All 20 engineers had significant positive convergent validities for aesthetics, 16 for safety, and 17 for capacity. Hence we conclude that each of the three concepts is capable of being measured by appropriate subjects independently of the method used; generality has been achieved over three methods.

More specific hypotheses may also be addressed. for example,

H2: No concept has higher or lower convergent validity than any other.

To test Hypothesis 2, the computed mean of the z-transforms of the three aesthetics convergent validities (indicated in the previous paragraph) is compared to the means of the safety and capacity convergent validities, for each engineer. The results indicate that 17 of the 20 engineers had greatest convergent validity when judging the aesthetics concept (Chi-squared = 21.75,  $p < .001$ ). A t-test analysis shows that, over the 20 engineers, the convergent validity score for aesthetics was significantly higher than the score for safety ( $t = 5.08$ ,  $p < .001$ ) and for

capacity ( $t = 5.66$ ,  $p < .001$ ). Again, the generality of the results is not contingent upon a single method; the domain of generality over concepts, methods and subjects is made evident.

Questions regarding the relative efficacy of methods over concepts may also be addressed. For example,

H3: No method pair has higher or lower convergent validity than any other method pair.

To test Hypothesis 3, we must consider the convergent validities related to each pair of methods. When the film strip and bar graph methods are applied to aesthetics, the convergent validity is .890, to safety, .713, and to capacity, .591 for the artificial engineer of Table 3. The mean (via z-transforms) of these correlations is .761. The mean for each of the possible method pairs is calculated through the development of a matrix for each engineer, and the order among pairs is determined, similar to the analysis used for testing Hypothesis 2. For 17 of the 20 engineers the bar graph and formula were the method pair that produced the highest convergent validity across the three concepts (Chi-squared = 21.754,  $p < .001$ ). This result tells us which pair of methods across the three concepts is best for achieving convergent validity with regard to these three concepts.

Discriminant validity. Convergent validity informs us about the covariance of judgments across methods, and thus about the status of a concept independent of the method used to measure it. In addition, however, we need to know whether the concept is discriminable from other

proposed theoretical entities. The first internal discriminant validity analysis employed in the examples below compares monoconcept heteromethod correlations to heteroconcept heteromethod correlations. Campbell and Fiske (1959) gave first priority to this test; for although many people would think it "so minimal and obvious as not to need stating," (p. 82) they observed that it often fails to be true. We therefore illustrate the test for the following hypothesis:

H4: All pairs of concepts are equally discriminable.

This hypothesis will be tested by calculating an index for each concept pair for each engineer, and looking for evidence of any concept being more, or less, discriminable than the others, for a statistically significant number of engineers. To illustrate the calculation of the index for the aesthetic and safety concepts, for the artificial engineer of Table 3, we compare the correlations from the validity (monoconcept heteromethod) diagonals that involve either aesthetics (.890, .864, .985) or safety (.713, .393, .422) with the correlations from the heteroconcept heteromethod triangles that involve both concepts (.283, .244, .360, .093, .548, and .209). (The sign on all heteroconcept correlations involving aesthetics was reversed because the intra-ecological correlations between the criterion measures of aesthetics and safety, and of aesthetics and capacity, were negative.) In order to aggregate these comparisons into an index, we subtract the mean of the z-transformations of the second set of correlations (.306) from the mean of the z-transformations of the first set (1.156), which produces an index (.850) of the discriminability of the aesthetics and safety concepts. The corresponding index for aesthetics and

capacity is .913; for safety and capacity,  $-.047$ . Thus, for the artificial engineer aesthetics and capacity are the easiest concepts to discriminate, and safety and capacity are most difficult to discriminate (a result which carries some practical implications).

This index of discriminant validity is calculated for each concept pair from each subject's matrix, and the order among concept pairs is determined. For all 20 engineers, the safety and capacity concepts were least discriminable (Chi-squared = 37.053,  $p < .001$ ). Therefore null hypothesis 4 is rejected, for the engineers' judgments of safety and capacity are more similar to each other than either is to their judgment of aesthetics. The remaining three indices of internal discriminant validity are described in Appendix C.

#### External Validity Analysis

One measure of convergent validity and three measures of discriminant validity can be derived from the external validity matrix. In addition, two measures of external discriminant validity can be produced using data from the internal validity matrix.

Convergent validity. The external convergent validity measure is based on the correlation between the engineer's judgments of a concept and the criterion measure of that concept. We examine first the relative convergent validity of each concept, thus:

H5: No concept has higher or lower external convergent validity than any other.

Hypothesis 5 is tested by averaging the z-transforms of the correlations for each concept across methods, and then comparing the averages for each concept. Thus the aesthetics concept had higher convergent validity than safety or capacity for all 20 engineers (Chi-squared = 37.053,  $p < .001$ ). Despite the counterintuitive nature of this result, it has a claim to our attention; it is general across three methods and stands against two other concepts.

Similar questions of external convergent validity can be addressed to methods. For example,

H6: No method has higher or lower external convergent validity than any other.

Hypothesis 6 is tested by averaging the z-transforms of the correlations for each method across concepts, and comparing methods. The film strip method was found to have the lowest convergent validity for 18 of the 20 engineers (Chi-squared = 26.404,  $p < .001$ ). It is least dependable in the context of this study. Methods and results for Hypotheses 5 and 6 are given in more detail in Hammond, Hamm, Grassia, and Pearson (1984).

Discriminant validity. The external validity matrix provides three ways of measuring external discriminant validity, and two additional measures can be produced from the internal validity matrix in combination with the criterion intercorrelations. These measures can be used to ask whether concepts can be discriminated accurately. For example,

H7: All pairs of concepts are equally discriminable.

The first external discriminant validity measure is analogous to the first internal discriminant validity measure, and is used to test Hypothesis 7 just as the latter was used to test Hypothesis 4: by calculating an index of discriminability for each concept pair for each engineer, comparing the concept pairs, and determining whether any particular order among the concept pairs occurred in a significant number of engineers. Thus, for the artificial engineer in Table 4, the discriminability of the aesthetics and safety concepts is measured by subtracting the mean of the z-transforms of the heteroconcept correlations involving aesthetics and safety (-.016, .362, .233, .497, .313, and .226) from the mean of the z-transformations of the achievement correlations involving aesthetics or safety (aesthetics: .855, .945, .951; safety: .702, .683, .226), a difference of .855. This figure is calculated for each concept pair for each engineer; the safety and capacity concepts were least discriminable for each of the 20 engineers ( $\text{Chi-squared} = 37.05$ ,  $p < .001$ ), a result that is consistent with that obtained in the internal validity matrices.

The availability of information about the intercorrelation among the measured criteria makes possible four additional procedures besides the first measure of external discriminant validity described above. The second and third procedures involve direct comparison of heteroconcept correlations with the correlations between the criterion measures of the two concepts, for the external and internal validity matrices respectively. The fourth and fifth procedures involve testing, for both matrices, whether the pattern of correlations in each heteroconcept triangle is identical to the pattern of correlations among the three criterion measures.

The second and third external discriminant validity measures allow us to ask whether there is systematic over- or underdiscrimination between concepts by testing the following hypothesis:

H8: Concepts are discriminated accurately.

The second external discriminant validity measure, which compares heteroconcept correlations from the external validity matrix with the corresponding correlations between the criterion measures, was used to test Hypothesis 8. A parallel test could be carried out with the third external discriminant validity index, which uses heteroconcept correlations from the internal validity matrix.

From each heteroconcept correlation in the external validity matrix, the corresponding criterion intercorrelation (intra-ecological correlation) is subtracted (after z-transformation). The mean of these differences for the set of heteroconcept correlations corresponding to a pair of concepts indicates the extent of the engineer's under- or overdiscrimination of the concepts. This procedure can be carried out for the safety and capacity concepts for the artificial engineer (Table 4). We subtract the z-transform of .180, the correlation between their criterion measures, from the mean of the z-transforms of the heteroconcept correlations involving aesthetics and safety (.683, .399, .516, .437, .199, .383), producing a difference of .302. The positive sign of this number indicates that, overall, the artificial engineer underdiscriminates between safety and capacity (confirming two prior results). This procedure was carried out for each concept pair, for each engineer. Fourteen of the 20 overdiscriminated between aesthetics and safety (Chi-squared = 2.45,

df = 1, NS), 15 over discriminated between aesthetics and capacity (Chi-squared = 4.05,  $p < .05$ ), and 19 underdiscriminated between safety and capacity (Chi-squared = 14.45,  $p < .001$ ).

The testing of a hypothesis using the fifth operation measuring external discriminant validity is described in Appendix C.

### Summary

In this section we have illustrated the application of the multiconcept multimethod validity analysis to topics typically of concern to experimental psychologists: testing theoretical propositions regarding the comparison of concepts and methods. This was done by using the internal validity matrix, which is concerned solely with the relations among different judgments of the concepts, obtained under different methods; and with the external validity matrix, concerned with the relation between the judgments and the criterion measures of the concepts.

Our illustration highlights the complementarity of these two analyses. We found in both the internal and external validity analyses that the aesthetics concept has the highest convergent validity; that the best pair of methods to use to obtain discriminant validity (in these conditions) is the quasi-rational, bar graph method and the analytical, formula-producing method; and that safety and capacity are least discriminable from each other. The external validity analysis was able to put this last finding in sharper perspective than could the internal validity analysis. It showed that the engineers underdiscriminate safety and capacity in comparison with the intercorrelation between the criterion measures of these concepts. The engineers' judgments of these two concepts are most highly correlated,

while in fact the criterion measures of these concepts have the lowest intercorrelation. This could have been otherwise; that is, if safety and capacity had actually been very highly correlated, the engineers might have overdiscriminated them even if the internal validity analysis had indicated that these two concepts are discriminated less than any other pairs of concepts. The external validity analysis provides the only way to determine which of these possibilities is true.

#### Application to Individual Differences

The multiconcept multimethod approach can be used to study individual differences in the competence of expert judgment. The need for individual comparisons is apparent from Tables 5, 6, 7, and 8, which show the internal and external validity matrices for two engineers. Engineer A's validity correlations are high (mean of 9 monoconcept heteromethod correlations from internal validity matrix = .705; mean of 9 monoconcept correlations from external validity matrix = .741), while Engineer B's are low (mean from internal matrix = .358; mean from external matrix = .609). Similar differences can be seen in their discriminant validities.

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Insert Tables 5, 6, 7, 8 about here  
-----

#### Indices of Coherence, Performance and Competence

Individual differences among engineers can be studied using numerical measures of convergent and discriminant validity derived from both the internal and external validity matrices. A procedure for evaluating validity can be converted into a numerical measure by adding (or subtracting, as appropriate) the means of the z-transforms of the

correlations in all the relevant cells in the matrix. The formulas for producing these indices are given in Table 9 and explained in Appendix D.

These measures can be combined into indices that measure overall internal validity (see Figure 1), which indicates the coherence of the engineer's judgments; the corresponding index of external validity indicates the engineer's performance, i.e., the correspondence between his judgments and reality. And the mean of these two indices provides a measure of the engineer's overall competence. Each index can be produced at different levels of aggregation (e.g., for each concept or for each pair of methods; see columns of Table 9), thus allowing numerical comparisons among these indices at each level.

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Insert Figure 1 and Table 9 about here  
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Measurements of coherence and performance are of special theoretical importance. The coherence of a person's judgments is the central characteristic of one of the traditional theories of knowledge, the coherence theory of truth. And the performance of a person's judgments is the central characteristic of a second traditional theory of knowledge, the correspondence theory of truth. Therefore, taken together, indices of internal and external validity inform us about a person's competence in the context of two historic theories of truth.

The methodology described here makes it possible to measure coherence and performance over several concepts and methods. Thus the generality of the behavior of each subject is explicated in terms of each theory of knowledge in the context of a different matrix of concepts and methods, each of which provides its own methodological justification for the generalization of results.

Among the experts in the example used here, a fairly high relation (.60) was found between coherence and performance. The treatment of coherence and performance as cognitive traits thus will allow us to examine empirically theoretical questions of importance to both philosophers and psychologists. For example:

1. Should competence always be a joint product of coherence and performance? Should these traits always be additive? Or is coherence a necessary but not a sufficient condition for performance? Common sense suggests that this should be so. But the relation between these traits may depend upon the complexity of the material and the degree of intellectual training required to master it. That is, variation in competence in, say, atomic physics may produce a very high correlation between coherence and performance, whereas variation in competence in financial forecasting may not. In short, coherence and performance may combine in different ways to provide competence, depending upon the nature of the material to be dealt with and the degree of training of the subject.
2. How should the measures of coherence and performance be combined into an overall measure of competence? Should they be weighted according to their relative importance and/or the quality of the measures? Common practice is to consider these measures separately. Moreover, different approaches to the study of cognition give greater consideration to one or the other of these aspects of competence. Studies within the framework of artificial intelligence and problem solving, for example, weight the experts'

coherence (and the coherence of the computer program that simulates the expert) very highly while placing less weight on performance. Judgment and decision researchers do the opposite (see Hammond, 1983). Explicating the concept of competence in terms of coherence and performance thus suggests that these two currently independent fields of research are investigating complementary aspects of competence among experts.

Comparison of the Competence of the Individual Experts and the Artificial Expert

Tables 3 and 4 (above) show the data for the artificially constructed engineer, produced by taking the mean of all the engineers' judgments of each highway, within each of the nine cells, and then performing a multiconcept multimethod analysis on these data. Would such an artificial expert, built upon aggregated judgments, provide more competent judgments than the individual experts?

Table 10 contrasts the validity indices and subindices for the artificial engineer with the corresponding indices for the lowest, mean, and best of the individual engineers. For all indices the artificial engineer's validity indices were better than the mean of the individual engineers' indices. Most important, for two indices (internal and external convergent validity) the artificial engineer's index was better than that of the best engineer. Finally, combining engineers' individual judgments produced judgments that were more competent than all but one engineer's judgments.

-----  
Insert Table 10 about here  
-----

### Summary

Individual differences were found in the quality of experts' judgment. Numerical measures were created for a number of procedures for measuring internal and external convergent and discriminant validity. These were combined into indices for the internal validity matrix (pertaining to the coherence of experts' judgment) and for the external validity matrix (pertaining to their performance). A correlation of .60 between coherence and performance was found among the engineers used in the illustrative example. The coherence and performance of the artificial engineer, created by averaging all individual engineers' judgments of each condition of the study, proved superior to that of the individual engineers.

### Discussion

As several noted psychologists have observed, psychological research lacks the cumulative character critical to the development of a science. In any such circumstance suspicion would arise that the scientific discipline in question is the captive of a flawed theoretical or methodological dogma. Since theories are numerous in psychology, but methodology is uniform throughout graduate schools and journal reviews, dogmatic methodology must be the prime suspect.

In an attempt to address the methodological problem of generalization we have extended and integrated the pioneering efforts of Campbell and Fiske (1959) and Brunswik (1956). Using individual experts' judgments of the safety, capacity and aesthetics of highways made under three

conditions, we first created a multiconcept multimethod matrix of internal validity for the judgment of concepts about highways, using different methods of eliciting judgments. This contrasts with Campbell and Fiske's multitrait multimethod matrix for the measurement of traits of persons, using different trait-measuring methods. Second, we used criterion measures for the concepts to create an external validity matrix. Measures of convergent and discriminant validity can be calculated from each of these matrices and used to address questions concerning, for example, how easily concepts can be discriminated or how well each method works. Taking full cognizance of the empirical relations among criteria in the determination of external discriminant validity conforms to Brunswik's demand for the representative design of experiments. Because the intercorrelations among the concepts are taken into account, the domain of the generality of the results is explicit.

The logic of the multiconcept multimethod matrix is based on what Feigl called "triangulation in logical space" (Feigl, 1958; see also Campbell & Fiske, 1959, p. 84). From a logical point of view, the methods and concepts selected for study should be completely independent; the "triangulation" should approximate a right triangle as nearly as possible. Thus, Campbell and Fiske (1959) discuss "convergence of the independent methods" and cite Cronbach and Meehl's argument that the use of "diverse criteria give[s] greater weight to the claim of construct validity than do . . . predictions of very similar behavior" (Cronbach & Meehl, 1955, p. 295). Brunswik, however, emphasized the fact that the ecological variables that so often serve as criteria for psychologists' concepts are not independent, i.e., orthogonal to one another. Therefore, from the researcher's point of view, Feigl's concept of "triangulation in logical

space" is not to be seen as a goal, but as a condition that serves didactic purposes, without regard to the demands of specific problems. The proper goal for the researcher (in contrast to the logician) is "triangulation in empirical space," in which the logician's worship of orthogonality is replaced by the researcher's worship of generalization. Informative as the logician's remarks undoubtedly are, the proper goal of basic research is generalization of results; and that goal can best be achieved through the use of "representative triangulation," in experiments as well as in studies of individual differences.

#### Addendum

Curiously, the literature of modern physics does not seem to include many treatises on methodological issues relating to reliability and validity of experiments, although there is a long history of treatises on measurement in physics (also apparent in psychology). A recent paper (Franklin & Howson, 1984) entitled "Why do scientists prefer to vary their experiments?" treats this topic as a contemporary one, thus suggesting that it does not have a long history (the oldest topical reference is 1979). Also, there appears to be no systematic treatment in physics of the problem of separation of method from concept such as carried out by Campbell and Fiske (1959). Personal communication with Allan Franklin confirms this conclusion. If psychology and physics are indeed beginning to recognize a common methodological problem of considerable importance, much might be gained from a joint consideration of "why scientists prefer to vary their experiments" (although it is not at all clear that all scientists do).

A comparison of the manner in which various experimental (physics, chemistry, biology) and nonexperimental (astronomy, archeology) disciplines treat the matter of repetition of experiments, the separation of reliability and validity, and/or the separation of concept from method is beyond the scope of the present article. Nevertheless, it is worth mentioning that our impression is that Campbell and Fiske's (1959) contribution, based on Feigl's (1958) original work, provides a more sophisticated, detailed examination of this matter than exists elsewhere (cf. Hacking, 1983).

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Footnotes

In constructing the internal validity matrix, repeated judgment reliabilities were not available from the data. Therefore they were estimated, using R from the linear best fit model of the engineer's judgments for the film strip and bar graph methods, and using the correlation between the judgments produced by corrected and uncorrected formulas for the formula method. Further details of these measures are available in Hammond, Hamm, Grassia, and Pearson (1984).

To determine whether the z-transformation of a correlation is significantly different from a zeta of zero (the expected correlation under the null hypothesis), the z-transformation is converted to a z-score by the formula (z-score minus zeta) divided by the variance of zeta (square root of  $[1/(N - 3)]$ ), and the probability of the z-score is determined from tables for the normal distribution. See Hays (1973, p. 662).

Table 1  
A Synthetic Multitrait-Multimethod Matrix

	Method 1			Method 2			Method 3																																																														
Traits	A <sub>1</sub>	B <sub>1</sub>	C <sub>1</sub>	A <sub>2</sub>	B <sub>2</sub>	C <sub>2</sub>	A <sub>3</sub>	B <sub>3</sub>	C <sub>3</sub>																																																												
Method 1	<table border="0" style="width: 100%; text-align: center;"> <tr> <td>A<sub>1</sub></td> <td colspan="2">(.89)</td> <td colspan="6"></td> </tr> <tr> <td>B<sub>1</sub></td> <td>.51</td> <td>(.89)</td> <td colspan="7"></td> </tr> <tr> <td>C<sub>1</sub></td> <td>.38</td> <td>.37</td> <td>(.76)</td> <td colspan="6"></td> </tr> </table>									A <sub>1</sub>	(.89)								B <sub>1</sub>	.51	(.89)								C <sub>1</sub>	.38	.37	(.76)																																					
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C <sub>1</sub>	.38	.37	(.76)																																																																		
Method 2	<table border="0" style="width: 100%; text-align: center;"> <tr> <td>A<sub>2</sub></td> <td>.57</td> <td>.22</td> <td>.09</td> <td colspan="6"></td> </tr> <tr> <td>B<sub>2</sub></td> <td>.22</td> <td>.57</td> <td>.10</td> <td colspan="6"></td> </tr> <tr> <td>C<sub>2</sub></td> <td>.11</td> <td>.11</td> <td>.46</td> <td colspan="6"></td> </tr> </table> <table border="0" style="width: 100%; text-align: center;"> <tr> <td></td> <td>(.93)</td> <td colspan="8"></td> </tr> <tr> <td></td> <td>.68</td> <td>(.94)</td> <td colspan="7"></td> </tr> <tr> <td></td> <td>.59</td> <td>.58</td> <td>(.84)</td> <td colspan="6"></td> </tr> </table>									A <sub>2</sub>	.57	.22	.09							B <sub>2</sub>	.22	.57	.10							C <sub>2</sub>	.11	.11	.46								(.93)										.68	(.94)									.59	.58	(.84)						
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Method 3	<table border="0" style="width: 100%; text-align: center;"> <tr> <td>A<sub>3</sub></td> <td>.56</td> <td>.22</td> <td>.11</td> <td>.67</td> <td>.42</td> <td>.33</td> <td colspan="3"></td> </tr> <tr> <td>B<sub>3</sub></td> <td>.23</td> <td>.57</td> <td>.12</td> <td>.43</td> <td>.66</td> <td>.34</td> <td colspan="3"></td> </tr> <tr> <td>C<sub>3</sub></td> <td>.11</td> <td>.11</td> <td>.45</td> <td>.34</td> <td>.32</td> <td>.58</td> <td colspan="3"></td> </tr> </table> <table border="0" style="width: 100%; text-align: center;"> <tr> <td></td> <td>(.94)</td> <td colspan="8"></td> </tr> <tr> <td></td> <td>.67</td> <td>(.92)</td> <td colspan="7"></td> </tr> <tr> <td></td> <td>.58</td> <td>.60</td> <td>(.85)</td> <td colspan="6"></td> </tr> </table>									A <sub>3</sub>	.56	.22	.11	.67	.42	.33				B <sub>3</sub>	.23	.57	.12	.43	.66	.34				C <sub>3</sub>	.11	.11	.45	.34	.32	.58					(.94)										.67	(.92)									.58	.60	(.85)						
A <sub>3</sub>	.56	.22	.11	.67	.42	.33																																																															
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	.58	.60	(.85)																																																																		

Table 2  
External Validity Matrix

Concepts	Method 1			Method 2			Method 3		
	C1	C2	C3	C1	C2	C3	C1	C2	C3
C1	.855	.362	-.473	.945	.479	-.311	.951	.226	.002
C2	.016	.702	.683	-.233	.683	.516	-.313	.226	.199
C3	-.172	.399	.291	-.298	.437	.833	-.316	.383	.266

Key:

○ monoconcept (validity)

⋯ heteroconcept

Table 3  
Internal Validity Multiconcept Multimethod Matrix for Artificial Engineer

		METHOD											
		Film Strip I				Bar Graph Q				Formula A			
Concepts		E	S	C	E	S	C	E	S	C	E	S	C
M	E	(.957)											
	S	.035	(.825)										
	C	-.117	.951	(.793)									
E	E	(.890)	-.283	-.364	(.996)								
	S	-.244	(.713)	.712	-.491	(.968)							
	C	-.051	.706	(.591)	-.282	.681	(.979)						
T	E	(.864)	-.360	-.452	(.985)	-.548	-.337	(.999)					
	S	-.093	(.393)	.427	-.209	(.422)	.452	-.232	(.415)				
	C	.176	.403	(.333)	.015	.270	(.340)	.004	.001	(.3:5)			
H	E												
	S												
	C												
O	E												
	S												
	C												
D	E												
	S												
	C												

Key:

( ) monoconcept monomethod (reliability)      E : Aesthetics



○ monoconcept heteromethod (validity)      S : Safety

△ heteroconcept monomethod      C : Capacity

⋯ heteroconcept heteromethod

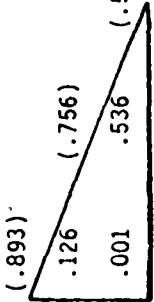
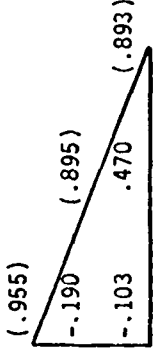
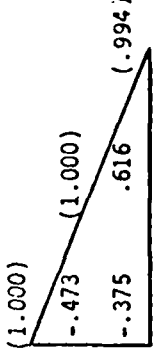
Table 4  
External Validity Multiconcept Multimethod Matrix for Artificial Engineer

		METHOD											
		Film Strip I				Bar Graph Q				Formula A			
Concepts		E	S	C	E	S	C	E	S	C	E	S	C
C	E	.855	.362	-.473	.945	-.479	-.311	.951	-.226	.002	.951	-.226	.002
R	S	.016	.702	-.683	-.233	.683	.516	-.313	.226	.199	-.313	.226	.199
I	C	-.172	.399	.291	-.298	.437	.833	-.316	.383	.266	-.316	.383	.266
T													
E													
R													
I													
A													

Key:  monoconcept (validity)  
 heteroconcept

Key: E : Aesthetics  
 S : Safety  
 C : Capacity

Table 5  
Internal Validity Matrix for Engineer A

		METHOD											
		Film Strip I				Bar Graph Q				Formula A			
Concepts		E	S	C	E	S	C	E	S	C	E	S	C
M	E												
	S												
	C												
E	E	(.793)	-.103	-.128	(.955)	-.190	(.895)	(.909)	-.359	-.095	(1.000)	-.473	(1.000)
	S	-.145	(.467)	.449	-.103	.470	(.893)	-.281	(.875)	.440	-.375	.616	(.994)
	C	-.010	.144	(.335)	-.103	.470	(.893)	-.335	.604	(.756)	-.375	.616	(.994)
T	E	(.786)	-.223	-.153	(.909)	-.359	-.095	(1.000)	-.473	(1.000)	-.375	.616	(.994)
	S	-.217	(.557)	.490	-.281	(.875)	.440	-.375	.616	(.994)	-.375	.616	(.994)
	C	-.172	.435	(.389)	-.335	.604	(.756)	-.375	.616	(.994)	-.375	.616	(.994)
H	E	(.786)	-.223	-.153	(.909)	-.359	-.095	(1.000)	-.473	(1.000)	-.375	.616	(.994)
	S	-.217	(.557)	.490	-.281	(.875)	.440	-.375	.616	(.994)	-.375	.616	(.994)
	C	-.172	.435	(.389)	-.335	.604	(.756)	-.375	.616	(.994)	-.375	.616	(.994)
O	E	(.786)	-.223	-.153	(.909)	-.359	-.095	(1.000)	-.473	(1.000)	-.375	.616	(.994)
	S	-.217	(.557)	.490	-.281	(.875)	.440	-.375	.616	(.994)	-.375	.616	(.994)
	C	-.172	.435	(.389)	-.335	.604	(.756)	-.375	.616	(.994)	-.375	.616	(.994)
D	E	(.786)	-.223	-.153	(.909)	-.359	-.095	(1.000)	-.473	(1.000)	-.375	.616	(.994)
	S	-.217	(.557)	.490	-.281	(.875)	.440	-.375	.616	(.994)	-.375	.616	(.994)
	C	-.172	.435	(.389)	-.335	.604	(.756)	-.375	.616	(.994)	-.375	.616	(.994)

Key:

( ) monoconcept monomethod (reliability)

○ monoconcept heteromethod (validity)

△ heteroconcept monomethod

△ heteroconcept heteromethod

Key:

E : Aesthetics

S : Safety

C : Capacity

Table 6  
External Validity Matrix for Engineer A

		METHOD											
		Film Strip I				Bar Graph Q				Formula A			
Concepts		E	S	C	E	S	C	E	S	C	E	S	C
E		.747	-.279	-.309	.843	-.286	-.101	.925	-.435	-.317			
S		.047	.583	.345	-.037	.538	.184	-.222	.691	.378			
C		-.194	.300	.268	-.326	.474	.769	-.358	.498	.873			

Key:

○ monoconcept (validity)

⋯ heteroconcept

Key:

E : Aesthetics

S : Safety

C : Capacity

Table 7  
Internal Validity Matrix for Engineer B

		METHOD											
		Film Strip I				Bar Graph Q				Formula A			
Concepts		E	S	C	E	S	C	E	S	C	E	S	C
M	E	(.716)											
	S	.355	(.694)										
	C	.511	.788	(.723)									
E	E	(-.005)	-.409	-.381	(.882)								
	S	-.094	(.287)	.332	-.267	(.717)							
	C	.092	.572	(.448)	-.461	.533	(.899)						
D	E	(.148)	-.307	-.343	(.770)	-.366	-.375				(.997)		
	S	.126	(.431)	.467	-.541	(.505)	.585				-.483	(.921)	
	C	.138	.155	(.058)	-.258	-.087	(.344)				-.028	.120	(.663)

Key:

( ) monoconcept monomethod (reliability)      E : Aesthetics

○ monoconcept heteromethod (validity)      S : Safety

△ heteroconcept monomethod      C : Capacity

⋯ heteroconcept heteromethod

Table 8  
External Validity Matrix for Engineer B

		METHOD											
		Film Strip I				Bar Graph Q				Formula A			
Concepts		E	S	C	E	S	C	E	S	C	E	S	C
C	E	.253	.377	.364	.742	.449	.461	.878	.469	.098			
R	S	.331	.500	.529	.261	.499	.336	.393	.518	.092			
I	C	.195	.475	.260	.364	.216	.783	.161	.487	.668			
T													
E													
R													
I													
A													

Key:

○ monoconcept (validity)

⋯ heteroconcept

Key:

E : Aesthetics

S : Safety

C : Capacity

Table 9

Measures of Validity

		For Each Concept-Method Unit (m, j)	For Each Concept (m)	For Each Concept Pair (m, n) m ≠ n
I N T E R N A L V A L I D I T Y	Reliability	$r_{m_j m_j}$	$r_{m_j m_j}$	
	C o n v e r g e n t V a l i d i t y	$M_{k \neq j} r_{m_j m_k}$	$M_{j \neq k} r_{m_j m_k}$	
		$M_{k \neq j} \left( r_{m_j m_k} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_j n_j} \right)$	$M_{j \neq k} \left( r_{m_j m_k} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_k n_j} \right)$	$M_{j \neq k} \left( \frac{r_{m_j m_k} + r_{m_k n_j}}{2} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_j n_j} \right)$
		$M_{k \neq j} \left( r_{m_j m_k} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_j n_j} \right)$	$M_{j \neq k} \left( r_{m_j m_k} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_k n_j} \right)$	$M_{j \neq k} \left( \frac{r_{m_j m_k} + r_{m_k n_j}}{2} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_j n_j} \right)$
E X T E R N A L V A L I D I T Y	Convergent Validity	$r_{m_j m_j}$	$r_{m_j m_j}$	
	D i s c r i m i n a n t	$M_{n \neq m} \left( r_{m_j n_j} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_j n_j} \right)$	$M_{j \neq k} \left( r_{m_j n_j} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_j n_j} \right)$	$M_{j \neq k} \left( \frac{r_{m_j n_j} + r_{m_k n_j}}{2} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_j n_j} \right)$
		$M_{n \neq m} \left( r_{m_j n_j} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_j n_j} \right)$	$M_{j \neq k} \left( r_{m_j n_j} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_k n_j} \right)$	$M_{j \neq k} \left( \frac{r_{m_j n_j} + r_{m_k n_j}}{2} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_j n_j} \right)$
		$M_{n \neq m} \left( r_{m_j n_j} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_j n_j} \right)$	$M_{j \neq k} \left( r_{m_j n_j} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_k n_j} \right)$	$M_{j \neq k} \left( \frac{r_{m_j n_j} + r_{m_k n_j}}{2} - \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} r_{m_j n_j} \right)$

\*Alternatively:  $r_{m_j m_j} - \frac{1}{2} \frac{M_{j \neq k} M_{k \neq j} n}{n \neq m} (r_{m_j n_j} + r_{m_k n_j})$

and similarly for all terms that are divided by two.

Table 9 (continued)

INTERNAL VALIDITY		For Each Method (j)	For Each Method Pair (j,k) j≠k	Overall
Reliability		M m $r_{m,jj}$	M K m j m $r_{m,jj}$	
Convergent Validity		M k m k≠j $r_{m,jk}$	M m $r_{m,jk}$	
	IDV1	M k m k≠j $r_{m,jk} - M_{k,m,n} \left( \frac{r_{m,jk} + r_{m,kj}}{2} \right)$	M m $r_{m,jk} - M_{m,n} \left( \frac{r_{m,jk} + r_{m,kj}}{2} \right)$	M m j k $r_{m,jk} - M_{m,n} \left( \frac{r_{m,jk} + r_{m,kj}}{2} \right)$
	IDV2	M m $r_{m,jj} - M_{m,n} \left( \frac{r_{m,jj}}{r_{m,jj}} \right)$	M m $r_{m,jj} - M_{m,n} \left( \frac{r_{m,jj}}{r_{m,jj}} \right)$	M m j $r_{m,jj} - M_{m,n} \left( \frac{r_{m,jj}}{r_{m,jj}} \right)$
IDV3	M k m k≠j $r_{m,jk} - M_{k,m,n} \left( \frac{r_{m,jk} + r_{m,kj}}{2} \right)$	M m $r_{m,jk} - M_{m,n} \left( \frac{r_{m,jk} + r_{m,kj}}{2} \right)$	M m j k $r_{m,jk} - M_{m,n} \left( \frac{r_{m,jk} + r_{m,kj}}{2} \right)$	
Convergent Validity		M m $r_{m,mj}$	M M m j m $r_{m,mj}$	
	EDV1	M m $r_{m,mj} - M_{m,n} \left( \frac{r_{m,mj} + r_{n,mj}}{2} \right)$	M m $r_{m,mj} - M_{m,n} \left( \frac{r_{m,mj} + r_{n,mj}}{2} \right)$	M m j $r_{m,mj} - M_{m,n} \left( \frac{r_{m,mj} + r_{n,mj}}{2} \right)$
	EDV2	M m,n m≠n $\left( \frac{r_{m,nj} - r_{m,n} + \left  r_{n,mj} - r_{m,n} \right }{2} \right)$	M m,n m≠n $\left( \frac{r_{m,nj} - r_{m,n} + \left  r_{n,mj} - r_{m,n} \right }{2} \right)$	M m,n j $\left( \frac{r_{m,nj} - r_{m,n} + \left  r_{n,mj} - r_{m,n} \right }{2} \right)$
EDV3	M k m,n m≠n $\left( \frac{r_{m,jk} - r_{m,n} + \left  r_{m,kj} - r_{m,n} \right }{2} \right)$	M m,n m≠n $\left( \frac{r_{m,jk} - r_{m,n} + \left  r_{m,kj} - r_{m,n} \right }{2} \right)$	M m,n j $\left( \frac{r_{m,jk} - r_{m,n} + \left  r_{m,kj} - r_{m,n} \right }{2} \right)$	
EXTERNAL VALIDITY				

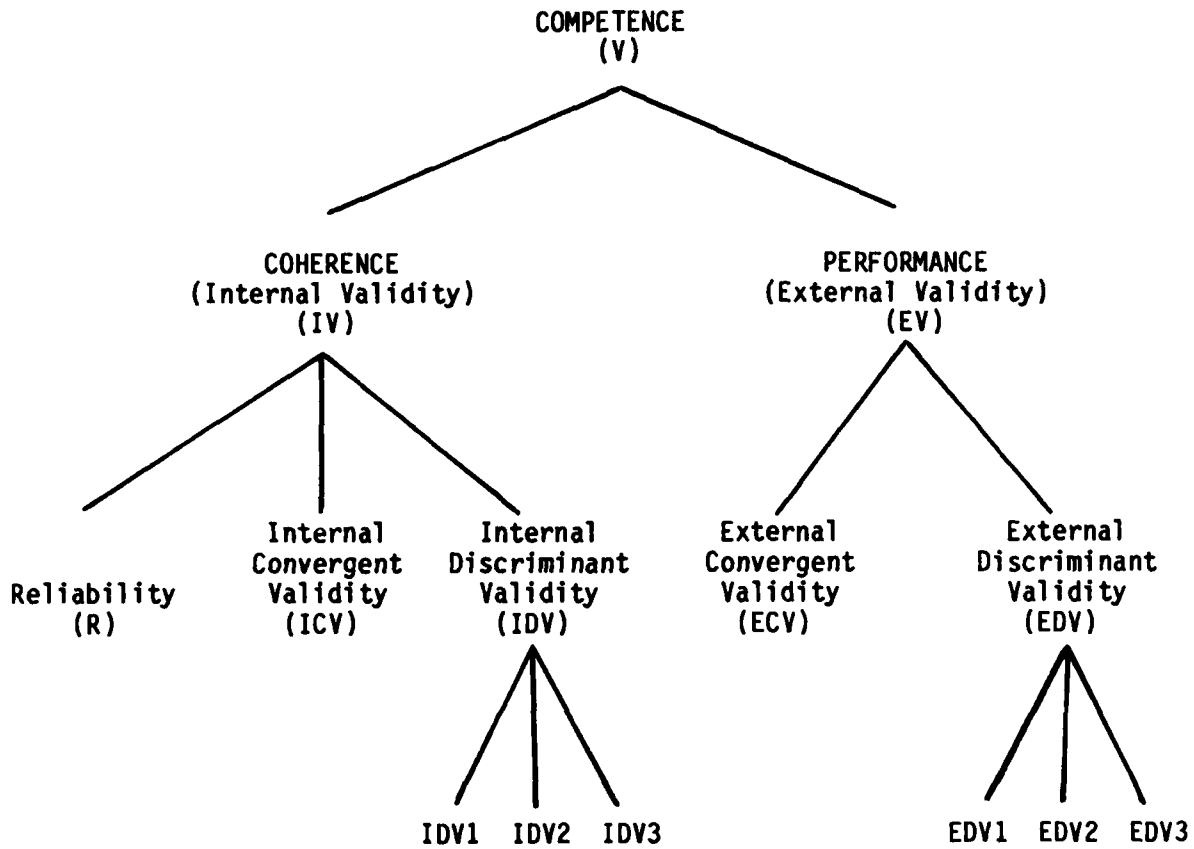
Table 10  
Comparison of Validity Indices (at Overall Level of Aggregation) for  
Artificial Engineer and Distribution of Validity Indices for Individual  
Engineers

Index	Artificial Engineer	Distribution of Individual Engineers		
		Low	Mean	High
Overall Validity (V)	.676	.371	.498	.706
Internal Validity (IV)	.853	.403	.619	.886
Reliability (R)	1.134	.706	.961	1.209
Convergent Validity (ICV)	.924	.346	.584	.877
Discriminant Validity (IDV)	.781	.432	.655	.894
External Validity (EV)	.499	.214	.376	.527
Convergent Validity (ECV)	.955	.510	.751	.953
Discriminant Validity (EDV)	.042	-.083	.001	.101

Figure Captions

Figure 1. The structure of indices representing coherence, performance and overall competence.

Figure A-1. Design of the highway engineers study.



		METHOD		
		Film Strip (Intuition Inducing) I	Bar Graph (Quasi Rationality Inducing) Q	Formula (Analysis Inducing) A
C O N C E P T	Aesthetics E			
	Safety S			
	Capacity C			

APPENDIX A

Context of Application

Whereas Campbell and Fiske (1959) directed their efforts toward ascertaining the validity of measures of constructs ("traits") about people, we attempted in a study of experts to ascertain the validity of expert judgments of concepts about highways. The purpose of this study was to examine the relative efficacy of intuitive, quasi-rational and analytical cognition. Twenty engineers judged the aesthetic value, safety, and capacity of 40 highways under three modes of cognition. Each engineer's judgments were studied in each cell of the diagram presented in Figure A-1. Intuition was induced by requiring each expert to judge each concept (aesthetics, safety, capacity) from film strips of 1-3 mile segments of each of the 40 highways. Quasi rationality was induced by requiring each expert to judge each concept from bar graphs that presented the values of nine attributes for each highway. Analytical cognition was induced by requiring each engineer to construct a mathematical formula for each concept. An empirical criterion was available for each concept. The criterion for the aesthetic value of each highway was derived from the mean judgment of 91 citizens who judged the same highway segments by rating the film strips, or by rating or ranking single frames from the film strips. The criterion for safety was the accident rate for each highway segment averaged over 7 years. The criterion for capacity was the figure calculated by using the procedure from the Highway Capacity Manual 1965 (Highway Research Board, 1965). Each expert devoted roughly 20 hours to the nine sessions, each of which was separated by two-week intervals. (See Hammond, Hamm, Grassia & Pearson, 1984, for details.)

-----  
Insert Figure A-1 about here  
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APPENDIX B

Correction for Attenuation

To use the intra-ecological correlations to estimate discriminant validity accurately in the external validity analysis, two new procedures are described:

1. Comparison of each heteroconcept correlation with the corresponding intra-ecological correlation.
2. Comparison of the order of pairwise heteroconcept correlations with the order of intra-ecological correlations.

These procedures risk being in error if the measures involved in one correlation are more noisy than the measures involved in another, because the true correlation of the noisily measured concepts would be underestimated. We would normally correct for such attenuation, using the formula:

$$rc(a,b) = \frac{r(a,b)}{\sqrt{r(a,a)*r(b,b)}}$$

where  $r(a,b)$  is the correlation between the measures of concepts a and b,  $rc(a,b)$  is the correlation corrected for attenuation, and  $r(a,a)$  is the reliability of the measure of a.

We have not corrected for attenuation in the illustrative analysis we present here because the reliabilities were not measured in the study by Hammond, Hamm, Grassia, and Pearson (1984). Although estimation procedures for the reliabilities of the engineers' judgments were used in creating the internal validity matrix (see Footnote 1), we hesitate to use these estimates in the above formula because the product would be an "estimate of an estimate". Also, the reliability of the criterion measures can not be similarly estimated because, for example, the capacity criterion was produced from a formula and thus has no measurement error, though it might still be "in error" in that the formula could be wrong.

Because of these problems with the measurement of reliability, the comparisons involved in producing external discriminant validity measures 2 through 5 use correlations that have not been corrected for attenuation. What are the possible effects of this?

1. If the amount of noise is identical for the judgments and the criterion measures, there is no problem; if (as is more likely) there is less noise in the criterion measures than in the engineer's judgments, then in testing Hypothesis 8 we will have underestimated the extent to which the engineers underdiscriminate among the concepts. Further, the measures of EDV2 and EDV3 will be especially noisy.
2. If the concepts are judged or measured with equal amounts of noise, then we have no problem in comparing them; if on the other hand one concept is judged or measured with more noise than another, then the comparison of the patterns in the heteroconcept triangles in Hypotheses C1 and C2 may be distorted.

To avoid such problems, it is important in planning research using the multiconcept multimethod methodology to directly measure the reliability of each judgment and each criterion measure, if possible.

## APPENDIX C

### Further Measures of Internal and External Discriminant Validity

This appendix explains and demonstrates the second, third and fourth measures of internal discriminant validity and the fifth measure of external discriminant validity.

#### Internal Discriminant Validity

The second measure compares the correlations on the reliability (monoconcept, monomethod) diagonal (see Table 3) with the correlations in the heteroconcept monomethod triangle. The third measure compares the correlations on the validity (monoconcept heteromethod) diagonal with the correlations in the heteroconcept monomethod triangle. The results of these measures with respect to Hypothesis 4 were identical to those determined by the first internal discriminant validity measure: the safety and capacity concept pair was least discriminable.

The fourth internal discriminant validity method, originally suggested by Campbell and Fiske (1959) in the passage quoted above, examines whether the correlations between judgments of different pairs of concepts have the same pattern regardless of the methods used in making the judgments.

Each of the 9 heteroconcept triangles contains correlations between judgments of each of the three possible pairs of concepts: aesthetics and safety (ES), aesthetics and capacity (EC), and safety and capacity (SC). There are six possible ways in which these correlations may be ordered. Similarity of the pattern of correlations in all nine heteroconcept triangles is evidence that for this set of concepts, this set of methods provides discriminant validity. The distribution of the heteroconcept

triangles among these orders can be tested with Chi-square against the expectation that 1.5 triangles would exhibit each of the 6 orders (cf. Delucchi, 1983).

For example, in the internal validity matrix for the artificial engineer (Table 3), there are 4 triangles with correlations in the order SC > ES > EC, 2 triangles with SC > EC > ES, 2 with ES > SC > EC, and 1 with EC > SC > ES. The Chi-square for the artificial engineer is not significant (Chi-squared = 7.667, df = 5, NS), and there is therefore no evidence for discriminant validity with this procedure, for the artificial engineer. For all engineers:

HC1: There is no predominant pattern among the hetero-concept correlations.

The analysis was carried out for each of the 20 engineers. Six engineers deviated significantly from the expected distribution; that is, showed evidence for discriminant validity. Four of these had the order SC > ES > EC.

#### External Discriminant Validity

The availability of the criterion measures and their intercorrelations allows us to look more directly at the question that was asked in Hypothesis C1 concerning the relative sizes of the correlations in the heteroconcept triangles. We will present this analysis using only data from the internal validity matrix; a parallel analysis could be done with data from the external validity matrix.

The correlation between the aesthetics and capacity criterion measures (.279) is larger than the correlation between aesthetics and safety (.275), which in turn is larger than the correlation between safety and capacity (.180). Accurate discriminant validity would require that this  $EC > ES > SC$  pattern occur in each heteroconcept triangle. (Note, however, that since the EC correlation is almost identical to the ES correlation in this particular data set, the  $ES > EC > SC$  pattern would also be expected to occur often.) Our hypothesis is:

HC2: Engineers' heteroconcept correlations have the same pattern as the criterion intercorrelations.

The null hypothesis is the same as for Hypothesis C1. To illustrate the analysis of this hypothesis, none of the artificial engineers' heteroconcept triangles exhibited the expected patterns  $EC > ES > SC$  or  $ES > EC > SC$ . The Chi-square test was used to determine, for each engineer individually, whether significantly more of his nine heteroconcept triangles had the expected pattern  $EC > ES > SC$  or its easily confused competitor  $ES > EC > SC$ . This is, of course, a more stringent test than for HC1. It was found that for only one engineer was the  $EC > ES > SC$  pattern predominant, and even this was not statistically significant. In fact, the reverse patterns were most common -- eight engineers had  $SC > ES > EC$ , and 7 had  $SC > EC > ES$ .

The fourth measure of internal discriminant validity, applied in testing Hypothesis C1, and the fifth measure of external discriminant validity, applied to Hypothesis C2, did not reveal any evidence for discriminant validity in this study. This contrasts with the findings

using the other discriminant validity measures. Although an explanation is available (the engineers judge safety and capacity to be more similar to each other than either is to aesthetics, when in fact aesthetics is more closely related to each than they are to each other), still it is clear that putting requirements on the pattern of heteroconcept correlations represents a stricter test of discriminant validity than the other procedures that Campbell and Fiske (1959) suggested for measuring it.

APPENDIX D

Procedure for Producing Indices of Validity

The various indices (e.g., of internal discriminant validity, external validity, or overall validity) are produced by taking the mean of the appropriate subindices (e.g., the first measure of internal discriminant validity, or external convergent validity) according to the pattern illustrated in Figure A-1. Each subindex is produced for each engineer by taking the mean of z-transformed correlations, from specific locations in the internal or external validity matrices, or the mean of the differences between such z-transformed correlations, corresponding to the comparisons that were illustrated above with Hypothesis 1-8. Table 9 displays the formulas for each of the 9 subindices, at each of 6 possible levels of aggregation. For example, the formula for the internal convergent validity index, at the concept level of aggregation, is:

$$\frac{M}{j,k} \quad r_{m m}$$
$$j \neq k$$

This index is calculated for each concept m. It is the mean, over all pairs of methods j and k where j is different from k, of the z-transformations of  $r_{m m}$ , which is the correlation between two judgments of concept m, using method j and method k. The correlations for the external validity matrix are (with one exception) of form  $r_{m n}$ ; that is, the correlation between the criterion measure of concept m and the engineer's judgment of concept n using method j. M is used as a "mean" symbol, representing a sum of correlations divided by the number of correlations summed over. The correlations involved in producing all the subindices in this table have been z-transformed.

Once the subindices are calculated as in Table 9, they combined as indicated in Figure A-1. Thus, the mean of the three internal discriminant validity subindices (IDV1, IDV2, and IDV3) is the index for internal discriminant validity (IDV); the mean of IDV and the internal convergent validity index (ICV) is the index for coherence or internal validity (IV); and the mean of IV and the index for performance or external validity (EV) is the index for overall competence (V).

In order that these indices be on a common scale, in which the meanings of the numbers are preserved when they are involved in the arithmetic operations of calculating means and differences, the indices consist only of those measures of reliability, convergent validity, and discriminant validity that are correlations or differences between correlations (after Fisher's z-transformation of the correlations). Therefore the procedures used for testing Hypotheses C1 and C2 (in Appendix C), which are not expressible as correlations, are not included in this index. Further, the second and third external discriminant validity measures used here are the absolute values of the differences between the engineer's heteroconcept correlation and the corresponding criterion intercorrelations (which addresses accuracy), while relative differences were used to test Hypothesis 7 (which addressed the question of over- or underdiscrimination). Finally, note that at some levels of aggregation specific subindices can not be created. For example, it is not possible to measure convergent validity at the level of concept pairs, because convergent validity deals, by definition, with only one concept. Similarly, it is not meaningful to create an index for the external validity of a pair of judgment methods, for the external validity matrix deals with only one judgment at a time. (A measure was possible for EDV3,

however, because it is derived from the internal validity matrix.) This means that the index should not be used for making comparisons between different levels of aggregation.

These indices are useful for a number of purposes. They can, for example, provide measures for evaluating:

1. Individual engineers' ability to discriminate among concepts (use individual IDV or EDV indices at the Overall level of aggregation in Table 9). In the present study, the engineers' individual internal discriminant validity indices range from .432 to .894, and their external discriminant validity indices range from -.083 to .101.
2. How well individual concepts can be judged (use mean V, IV, or EV indices at the Concept level of aggregation in Table 9). In the present study, aesthetics is judged best (internal validity = .93, external validity = .66), safety next (internal validity = .49, external validity = .23), and capacity third (internal validity = .45, external validity = .24).
3. How well pairs of concepts can be discriminated (use IDV or EDV indices at Concept Pair level of aggregation). In the present study, the aesthetics and capacity concepts are just as easily discriminable (IDV = .83, EDV = .07) as the aesthetics and safety concepts (IDV = .82, EDV = .08); safety and capacity are most readily confused (IDV = .32, EDV = -.16).

4. How well specific methods work (use indices at the Method level of aggregation). Both internal and external validity show that analysis is the best method for judging these concepts (internal validity = .80, external validity = .46), quasi rationality next (internal validity = .61, external validity = .45), and intuition third (internal validity = .44, external validity = .23).
  
5. How well pairs of methods work (use indices at the Method Pair level of aggregation). Consistent with the previous result, in case one wished to use only two of the three methods on a future project, one would choose the quasi-rational and analytical methods (IV = .63, EV = -.21) rather than the intuitive and quasi-rational (IV = .35, EV = -.23) or the intuitive and analytical (IV = .36, EV = -.24) methods.

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