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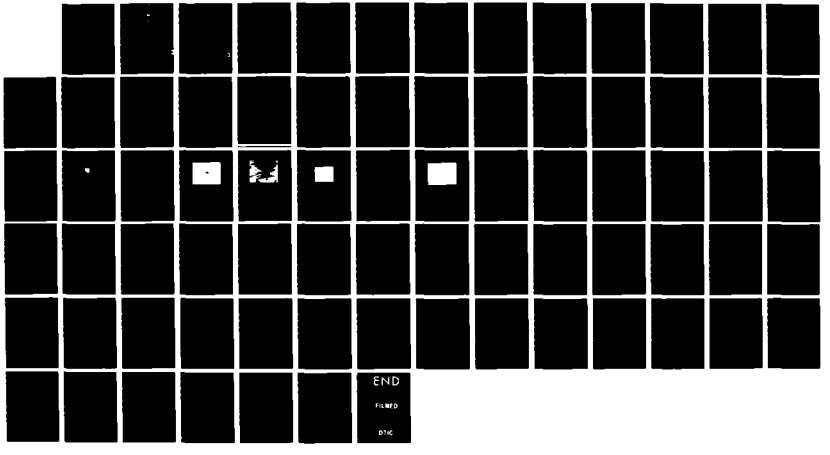

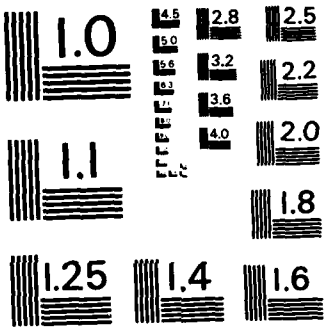

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Dall-Null Tester for

Spaceborne Applications

Thesis

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Dall-Null Tester for Spaceborne Applications

Thesis

Presented to the Faculty of the School of Engineering

of the Air Force Institute of Technology

Air University

In Partial Fulfillment of the

Requirements for the Degree of

Master of Science in Engineering Physics

Paul J. Wheeler, B.S.

Captain, USAF

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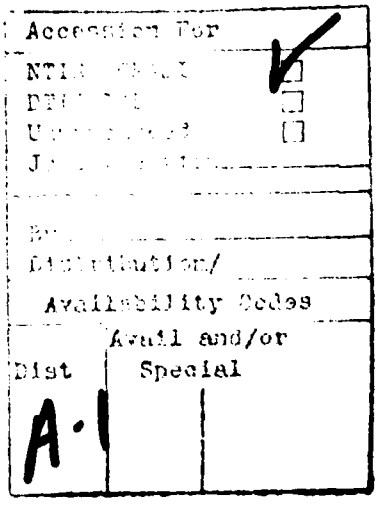

Preface

The purpose of this study was to design an adaptive optic system for a space based telescope. The design is built around a Dall-Hull tester. Much of the fine detail of the system was not researched because of the great difficulty and time required to correct all of the previous theory on which the design is based. However, the basis of a complete system is covered.

The making of the Focogram in the experimental section was very enjoyable and a nice break from the pitfalls of straight theory work. The results from the experiment showed the errors of the previous theories and paved the way to correcting them.

Several people have assisted me in this project. They are my advisor Dr. Dean Shankland, who always kept me headed in the right direction, but made me look and question every bend along the way; [illegible] Carthy, the librarian who tracked down all the references [illegible] requested; my class mate, Captain [illegible] tips on computer programming and [illegible]; [illegible] who helped me gather [illegible]

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Abstract

This is a study to design a self-correcting primary mirror system for a space telescope. The design is centered around a Dall-Null tester (a Foucault knife-edge tester with compensating lens). An in-depth study of the theory of the Foucault test from Foucault's original publications to current work is presented. Also shortcomings of the diffraction approach are shown. The findings of a simple experiment showed the way to the correct explanation as to the workings of the test. Based on this new explanation, a computer program to find the error in the surface of the mirror from the irradiance pattern provided by the Dall-Null tester was developed. The computer program with a sample run is included in the appendixes A and B.

The basic design of an adaptive optic system for a space-borne application is also presented in the paper. This design has the desired quality of being able to correct the mirror while the telescope is in use. The equations being independent of [illegible] the [illegible] can be applied to any [illegible] system as well as the [illegible].

Chapter 1

Introduction and Background

Ever since Galileo turned his telescope to the heavens, man has tried to improve this sky gazing instrument in order to gain more information from the skies. The best improvement that can be made in any telescope is to increase its light gathering capabilities. Increasing the size and improving the quality of the main optical element are the easiest ways to improve the light gathering capability of a telescope. The primary, or main optical element in a reflecting telescope, is the main mirror. And in a refracting telescope it is the large first lens. Since most large telescopes are reflectors, due mainly to more compact size and the lighter weight of the system, this paper will concern itself with improvements that are more suitable to reflecting telescopes.

Increasing the size of the primary lens in a telescope is the only way of increasing its light gathering capabilities. However, it is hard to say, for it may be either impossible or impractical to do so, or it could, however, be [illegible]

It is the reflective coating on the surface of the mirror that determines the reflectivity of the mirror. Therefore, any improvement in the reflectivity of the mirror is limited to the thickness and type of coating applied. Since the reflectivity is set in this manner, the only way left to improve the quality is to rid the surface of the mirror of defects. Most surface defects or imperfections are removed while the mirror is being fabricated.

Optical telescope mirrors are made by grinding glass into the desired shape and then coating them with a highly reflecting substance, like silver. As the glass is ground into the desired shape it is visually monitored for defects and imperfections. The most commonly used test for checking the mirror is the Foucault knife-edge test (or one of its derivatives). The Foucault test has one large [illegible]

the results of the usual test of a perfect spherical surface. This method of testing an optical surface using the proper lens in front of the Foucault tester now is known as the Dall-Null test. If the focal length of the mirror, the focal length of the desired lens, and the desired focal ratio of the mirror are known, then the proper compensating lens can be determined from a nomograph like the one found in Sky and Telescope (6:212).

Since the Dall-Null test is nothing more than a Foucault test with a lens in front of the knife-edge, all the theory that explains the Foucault test also explains the Dall-Null test. The theory of the Foucault test as it developed from Foucault's original publication, to the present, is presented in Chapter two. It is through the use of the theory as presented at the end of chapter two, that a way to detect and correct defects in the surface of a mirror can be determined.

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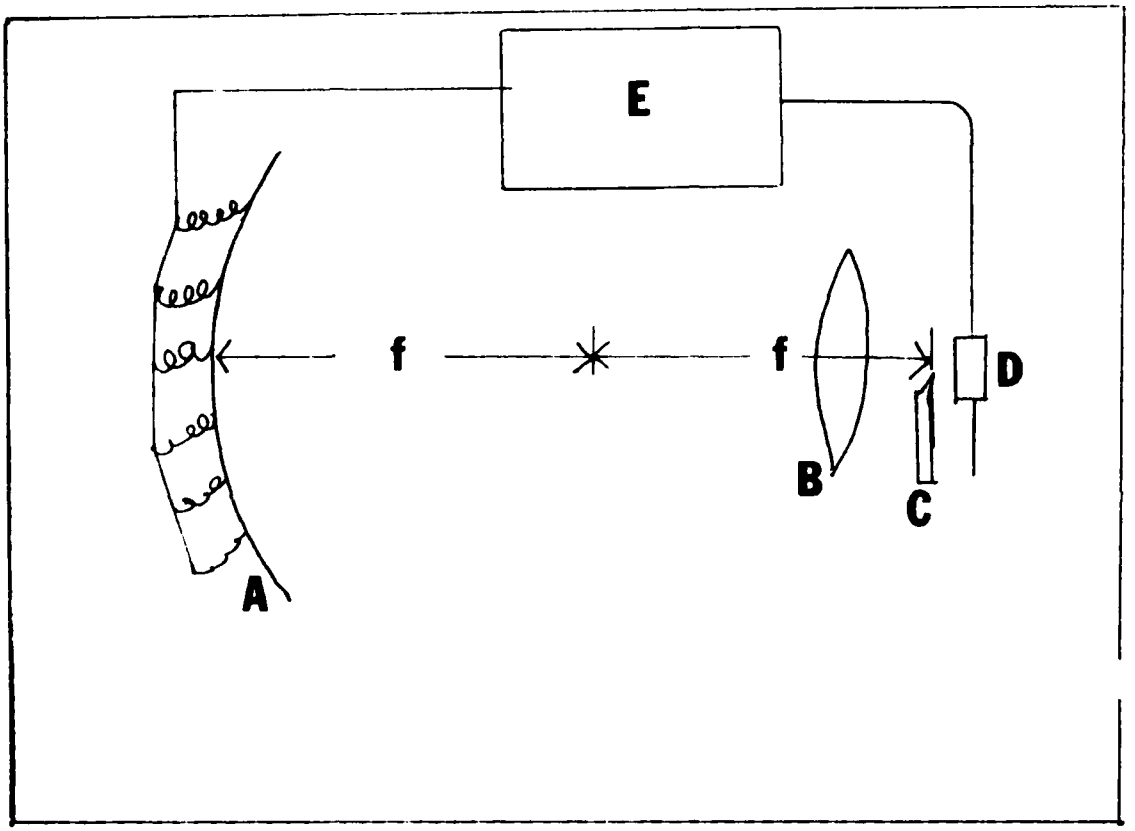


Figure 1 The basic layout of a Dall-Null tester
A is the deformable mirror with attached actuators
B is the compensating lens
C is the knife-edge
D is the detectorfor reading the irradiance
E is the computer and other electronic equipment

to escape the atmospheric limitations. This does cause some problems. One such problem is, "How can the surface of the mirror be tested to see if it has been twisted and warped out of shape by thermal and gravitational gradients as it spins around the earth?". This leads to the second question, "If surface defects do occur, how are they detected and corrected?".

One way to answer both of the above questions is to make the telescope with an adaptive optics system. This adaptive optics system consists of the following: a deformable main mirror with actuators, a computer, some electronics, a Dall compensating lens, and two Foucault testers. Figure 1 shows the basic layout of an adaptive optics system of a telescope. The deformable mirror is made by shaping a semiflexible material into the desired shape, and then coating it with a highly reflective substance (17,28). Then actuators (devices that can apply a push or pull force) are mounted on the back surface of the mirror. There are two major types of actuators. The first is the force type that uses either a stepping motor, or an electrodynamic voice coil to generate a push/pull force. The second is the piezoelectric type that contracts or expands with applied voltage (1). The computer's job is to calculate the error of the surface of the mirror from the irradiance of the images caused by each of the Foucault testers, and then to take the error information and correct the surface of the mirror through movement of the actuators. Two Foucault testers are needed to produce both a vertical and a horizontal scan. The two knife-edges are located approximately at the center of curvature, but orientated at 90 degrees from each other. The proper Dall compensating lens corrects the Foucault test for parabolic surfaces (6,7). The additional electronic equipment needed to complete a system consists of a sensor to read the irradiance, equipment to digitize the irradiance

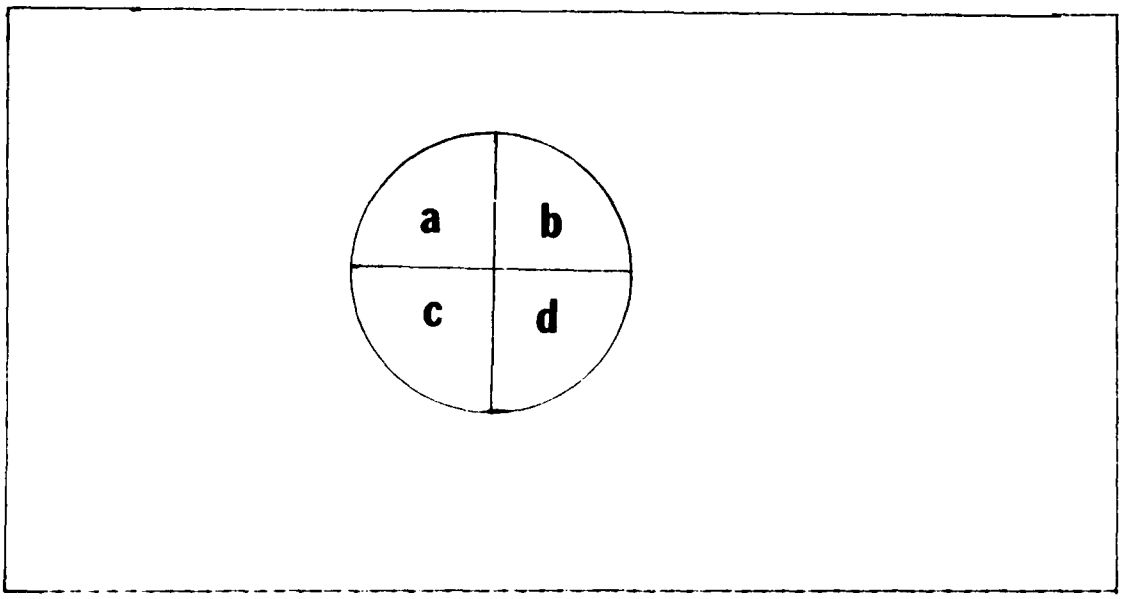


Figure 5. Mirror divided into four segments

pattern that is small ($\approx \lambda$). (Figure 4). These Airy patterns would either be passed by the knife-edge, or stopped completely, with just a few patterns left to straddle the knife-edge. It is these straddling patterns that would produce the effect of equation (2). But, because the light is incoherent, the irradiance of the waves add and not just their fields. This removes the singularities.

Now if the mirror was segmented into sections, as in Figure 5, each segment having a different local slope, the position of the light at the focus would be determined by the slope of each segment. Figure 6 shows the relative position of the light from each segment of the mirror relative to the knife-edge. If the slope is that of a perfect surface the knife-edge would split the image, case b, passing half and stopping half. If the slope was such that it raised the

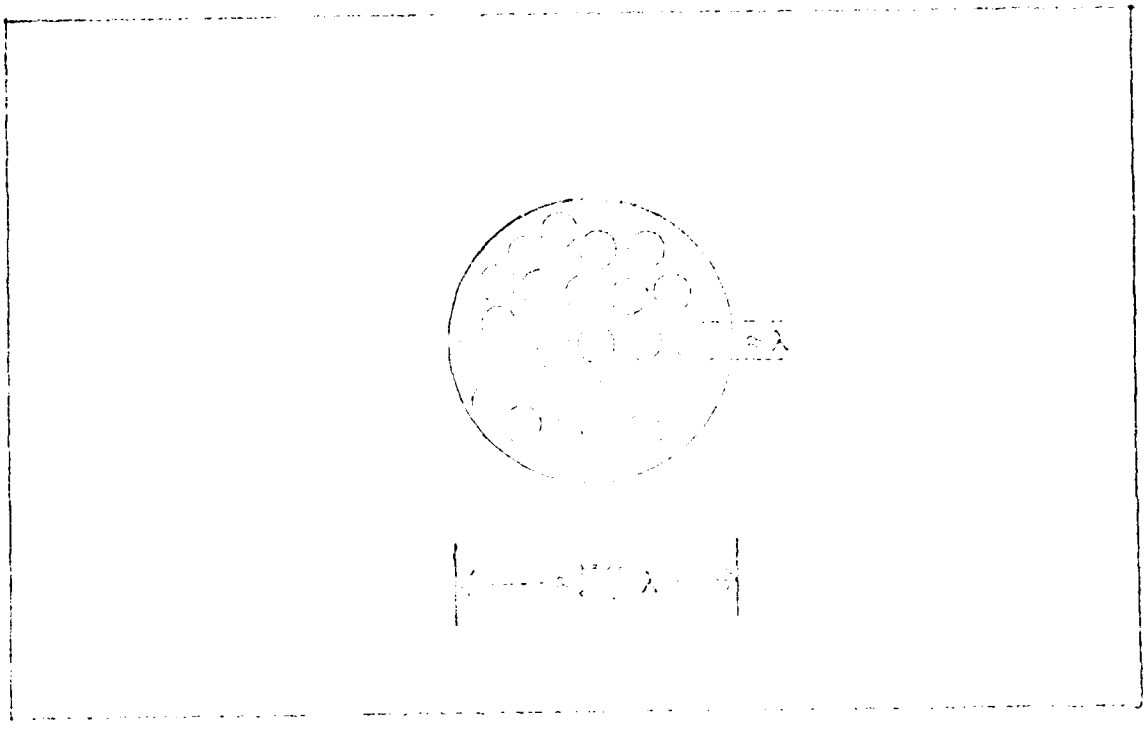


Figure 4 The Airy pattern of light, the image of the mirror at the focal point

$A(\underline{x})$ = the aperture function

$\underline{x} = (x_1, x_2)$

$\underline{y} = (y_1, y_2)$

$\underline{z} = (z_1, z_2)$

b = the distance the knife is displaced from the optic axis

But when equation 2 is used (being careful in expanding out all transforms and exponentials) to relate the irradiance of the image to the errors of the mirror, the resulting equations are so messy and complex they can not be solved. This is one of reasons the experiment described in chapter three was conducted.

The experiment described in Chapter Three was performed to verify what kind of results are obtained from an actual Foucault test, and to examine some of the operating parameters. The results of the experiment showed no existence of a bright rim around the image, and that the aperture did not affect the image at the screen as long as it does not intersect the beam. The experiment also showed that the light source had to be incoherent, and that monochromatic light was better than plain white for testing lenses due to the different focal length of each wavelength.

When using the laser as the source of radiation in the experiment, it became apparent that the diffraction theory of the Foucault test was inadequate to describe the results.

Where a = slit width

= MλR/b

n° = mλR/b

b = pupil radius

M = number of Airy patterns across slit

m = number of Airy patterns the lower edge is displaced from the center of the image

R = the radius out to the image from the knife-edge

λ = wavelength

The only real difference between this equation and that of Linfoot's is that the factor 1/(y-y') which gave the singularity is now replaced by the sinc function which has no singularity.

Welford's equation is basically the same result that the author, working in conjunction with Dr. Shealy, obtained upon applying Huygens' principle to the problem, (Figure 3). The resulting equation for the complex amplitude, $P(\underline{x})$, is

$$P(\underline{x}) = B \int_{\underline{\xi}} K(\underline{x},\underline{\xi})\, t(\underline{\xi}) \qquad (2)$$

where

$$K(\underline{x},\underline{\xi}) = \int_{\underline{\eta}} \cdots$$

$$r = (\quad)^{1/2}$$

$$\theta = \cdots$$

$$L = \cdots$$

$$\cdots = \cdots$$

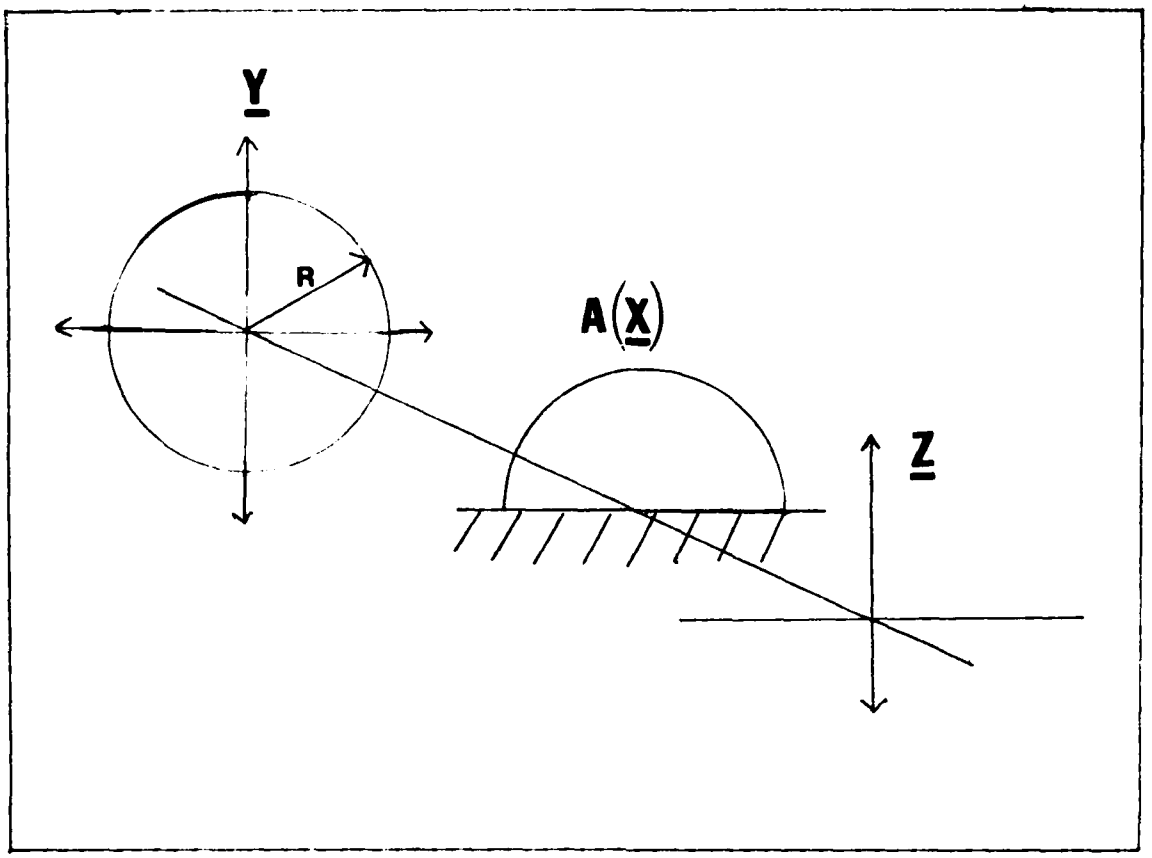


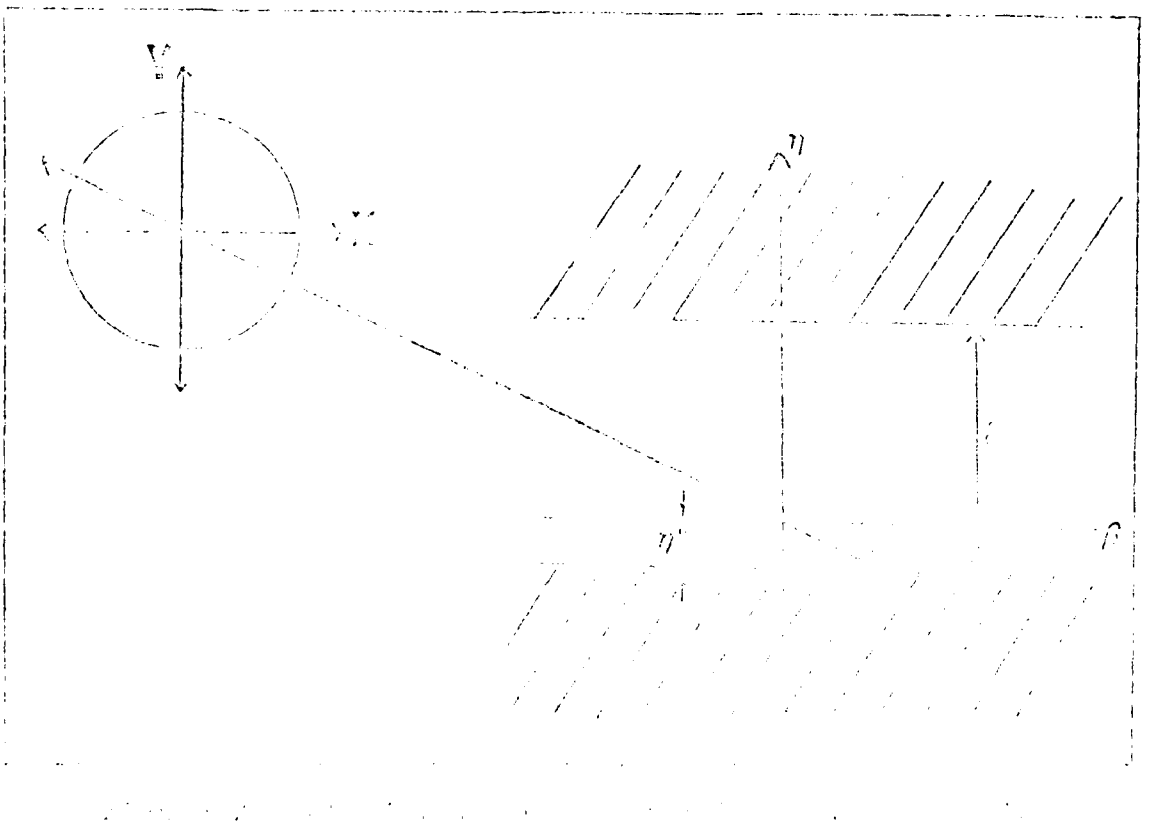
Figure 3 Orientation for the application of Huygens' Principle

disregard it as there could not be an actual infinity in the complex amplitude. Linfoot said that this infinity was due to the assumption of an infinite aperture. Welford decided to test this, and rederived Linfoot's work with a proper aperture function included. He used a very wide slit in the place of the knife-edge. Using Figure 2 as a reference, the equation Welford derived for the complex amplitude is:

$$U(x',y')=\int_{-\infty}^{\infty} a\ \mathrm{sinc}(M/b(y-y'))\exp(-\pi i/b(M+2m)(y-y'))F(x',y)dy$$

A plot of the perfect mirror's irradiance is found on page 140 of reference 23, and the plot of the perfect cassegrain mirror is on page 141. The point to note here is that the graphs and theory predict irradiance well out into the surrounding area outside of the mirror's boundary. This is not observed in practice.

W. T. Welford wrote an article (33) on the theory of the Foucault test in 1970, in which he noted that in Linfoot's, and his predecessors', computations a bright rim was predicted around the edge of the pupil of the system under test. Users of the test do not observe this bright ring, and



using a one inch diameter lens to expand the image; the "sec" term is less than one part in 100,000 at the edge of τ, where τ in this case is the semicircular edge corresponding to the value of $[u^2 + v^2]^{1/2}$ which is approximately $1300(\text{inch})^{-1}$. Disregarding the effects of the finite aperture of the viewing system, one can replace τ with infinity as the image is defined to be zero outside of the mirror. The complex amplitude now can be written,

$$D(x',y') = \frac{1}{2\pi} \int_0^{\infty} du \int_{-\infty}^{\infty} \exp(-iux'-ivy') \, W(u,v) \, dv$$

This reduces to the expression:

$$2\pi D(x',y') = \pi W(x',y') + i \int_{-\infty}^{\infty} \frac{W(\xi,\eta')}{\xi - x'} \, d\xi$$

and the observed irradiance is:

$$I(x',y') = 4\pi^2 \left| D(x',y') \right|^2$$

The [illegible]

$$I(x',y') = \pi^2 \left| \right|^2$$

This is saying the irradiance is uniform across the surface and zero outside the boundary of the mirror. If the surface of the actual mirror surface is labeled M, which is within a few wavelengths of a true spherical surface labeled M^o, then the wave at any point (x,y) is:

$$E(x,y) = |E(x,y)| \exp((-2\pi i/\lambda)\ \theta(x,y))$$

where $|E(x,y)|$ = the amplitude at the point (x,y)

$\theta(x,y)$ = the phase at the point (x,y)

λ = the wavelength

Now applying Huygens' principle along with the Paraxial approximation twice, once to the knife-edge and again to the image, results in the equation for the complex amplitude (the square of the amplitude is the irradiance) as:

$$O(x',y') = \frac{1}{2\pi} \int_{\gamma} \exp(-ixx'-iyy')\ V(u,v)\ \exp\frac{\lambda}{2\pi}(u^2+v^2)^{1/2}\ du dv$$

[illegible]

$$V(u,v) = \frac{1}{\pi^2} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} [illegible]\ dx'y$$

[illegible]

Where R is some retardation function

x = the position out from the center

(the radius has been normalized to one and y is just a variable of integration)

In the case of the perfect mirror, the retardation fuction, R, is equal to zero everywhere, and the equation reduces to Rayleigh's result, infinity at the edge of the mirror.

S. C. B. Gascoigne, working with H. H. Linfoot, took Zernike's work as his starting point and derived expressions for the irradiance that are valid for errors of arbitrary form and amount, in terms of definite integrals (Hilbert transforms). Gascoigne's equation for the irradiance of a perfect mirror is equivalent to Zernike's (equation 1). Gascoigne has tabulated his irradiance results on page 332 of reference 12 and plotted the results on page 334 of same reference.

It wasn't until Linfoot published his work in 1955, before anyone worked out the theory in [illegible] two or more dimensions (23). In the case of [illegible] under uniform illumination [illegible] the [illegible] could be expressed as:

[illegible]

[illegible]

was well out of the focal plane. His calculated irradiance ratios were then matched against photographic observed ratios with less than ten percent difference between corresponding points. Thus, Rayleigh's theory stood its ground, untouched until 1934.

In 1934, professor F. Zernike published his diffraction theory of the Foucault test(35). Zernike felt that the geometrical optic approach to the Foucault test did explain things well enough for the lens grinder to find the spots where more grinding was necessary, but in a test where wavelength defects could be detected, only wave optics and diffraction could completely describe the actual happenings and give the test's ultimate limit of sensitivity (35:377). He envisioned the surface of the mirror as a diffraction grating that would give first order spectra on both sides of the central image, which he called a phase grating. He built up his work by expressing everything in terms of this phase grating. From his phase grating expressions, he developed what is now called the method of phase contrast. This phase contrast method assigns phases to the different shades of irradiance in the image. Zernike's equation for the observed intensity, I(x), is:

$$I(x) = \pi^2 + \ln^2 \left| \frac{1 - x}{1 + x} \right| - 2\pi \int_{-1}^{1} \frac{R(y) - R(x)}{y - x} \, dy \qquad (1)$$

$$I(x) = \pi^2 + \ln^2 \left| \frac{D - x}{D + x} \right|$$

for the irradiance inside the edge of the mirror and

$$I(x) = \ln^2 \left| \frac{D - x}{D + x} \right|$$

for the irradiance outside the edge.

where D = the radius of the mirror

x = the position out from the center

At the edge of the mirror, when x = D, the logarithmic infinity that results is what Rayleigh said accounted for the bright ring around the image.

Sudhansukumar Banerji, in 1918, wrote that he had observed irradiance fluctuations of the entire surface when the knife-edge was considerably advanced and that there were no known repetings or explanations of this effect (2). He then proceeded to show that the fluctuations could be explained using Fourier's theory. Banerji then pointed out that Rayleigh had overlooked [illegible] the case where the knife-edge was exactly at the focus, and in particular, the position of the [illegible] and [illegible] this [illegible]

bright ring about the edge. The model also accounted for the bright line which appears at a step-discontinuity on the mirror surface.(27)

The theory of the Foucault test, as developed by Lord Rayleigh, gives irradiance of the field for the general case of any mirror, as viewed in the direction θ (relative to the optic axis) in terms of the Fresnel Cosine (Ci) and Sine (Si) integrals as:

$$I=\left[\mathrm{Si}\left[\frac{2\pi}{\lambda}\,\beta(1+\theta/\beta)\,\zeta_2\right]-\mathrm{Si}\left[\frac{2\pi}{\lambda}\,\beta(1+\theta/\beta)\,\zeta_1\right]+\mathrm{Si}\left[\frac{2\pi}{\lambda}\,\beta(1-\theta/\beta)\,\zeta_2\right]\right.$$

$$\left.-\mathrm{Si}\left[\frac{2\pi}{\lambda}\,\beta(1-\theta/\ )\,\zeta_1\right]\right]^2+\left[\mathrm{Ci}\left[\frac{2\pi}{\lambda}\,\beta(1-\theta/\beta)\right]_2\quad-\mathrm{Ci}\left[\frac{2\pi}{\lambda}\,\beta(1-\theta/\beta)\,\zeta_1\right]\right.$$

$$\left.-\mathrm{Ci}\left[\frac{2\pi}{\lambda}\,\beta(1+\theta/\beta)\,\zeta_2\right]+\mathrm{Ci}\left[\frac{2\pi}{\lambda}\,\beta(1+\theta/\beta)\,\zeta_1\right]\right]^2$$

where λ = Wavelength

ζ_2 = upper limit of aperture

ζ_1 = lower limit of aperture

θ = angular semi-aperture of the lens under test

Applying Rayleigh's irradiance equation for the special case of a perfect spherical mirror, tested at the center of curvature, with a change of variable in order to do the integration, the above equation for I(x) reduces to:

Chapter 2

The Tneory of the Foucault Test

After 1858 and 1859, when Leon Foucault published the first accounts of the Foucault knife-edge test, it rapidly became the optical test to verify the surface condition of a lens or a mirror (9,10,25:231). His first article described how to conduct the test, how to interpret the results, but not how or why it works (9). In his second article, he did attempt to explain the happenings in terms of geometric ray optics (10). This explanation worked well for extremely large errors but did not account for all of the observed effects. As Linfoot pointed out, the effects that are produced by the small errors (on the order of one to ten wavelengths) often caused trouble for the inexperienced mirror/lens grinder (24:128). One of these errors is the bright ring around the image of a properly ground lens. According to Foucault's original work, this bright ring could only be explained by saying it represented a steep narrow-turned edge, but there is no such edge on the surface of a properly ground lens.

In 1917, Lord Baron Rayleigh made the first attempt to derive a complete theory of how and why the Foucault test worked based on diffraction theory and wave optics. He used a simplified two-dimensional model (all equations and work were in one dimension) which qualitatively explained the

of the images for the computer, and equipment to provide the feedback between the actuators and the computer. Chapter four will discuss how the error in the surface height of the mirror is calculated from the irradiance pattern.

The complete system, deformable mirror, actuators, Dall-Null tester, computer, and the computer software for reading the focogram and controlling the actuators, comprised the necessary equipment to make up a self-correcting mirror system for a space-borne telescope application. This system has one big advantage over other possible systems for telescope applications. It works at the center of curvature and not at the focus. This allows the testing and correcting of the primary mirror to occur while the telescope is in use.

Chapter five will present conclusions of this study with recommendations for further study, the possible uses of such an adaptive optic in optical and other spectrum telescopes, and possible future thesis work.

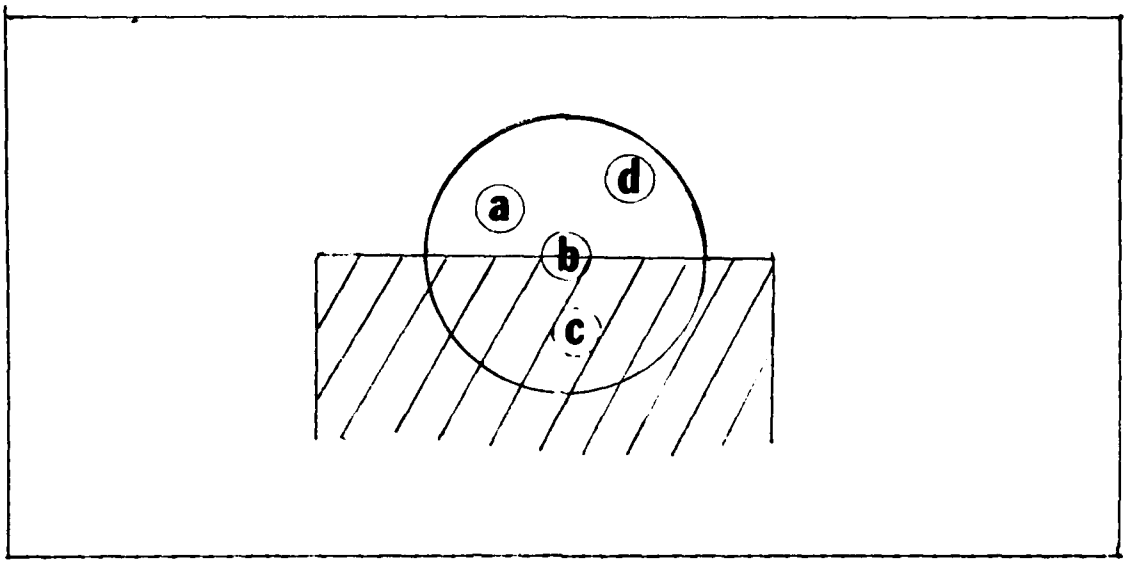


Figure 6. The relative poisition of the Ariy patterns at the knife-edge.

image, cases a and d, then all of the image will pass the knife-edge. But if the slope lowered the image, case c, the knife-edge would cut it off completely. Thus the irradiance of the resulting image would be determined by how much of each segment's image was passed by the knife-edge. Figure 7 shows the result for the current situtation.

Thus the correct theory of the Foucault test is revealed, and likewise, so is the theory of the Dall-Null test. And in chapter four this theory will be put to work to find the error in the height of the mirror surface.

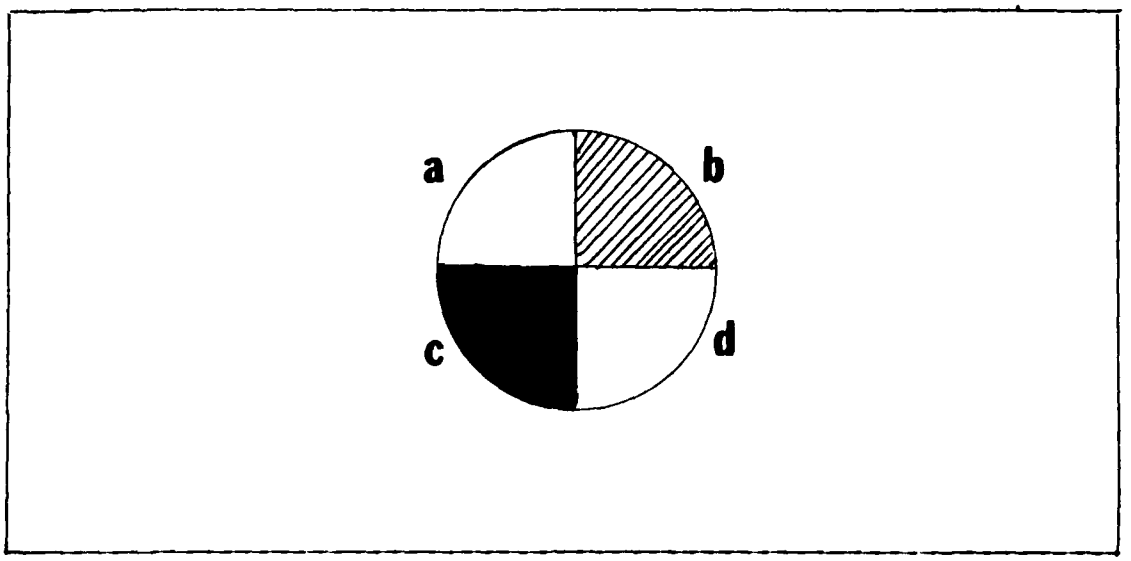


Figure 7. The image of the mirror

Chapter 3

An Experiment to Produce a Focogram

The Focograms presented in the literature (25:233-241, 20:390) did not show any bright rim about the edge that theory, according to Linfoot and his followers, says should be there. To answer the questions, "Is the theory right or is there something happening that is being missed?" and "Is Welford right in that it is the aperture function that will cure the infinity at the edge?", a simple experiment was set up to produce a Focogram of a lens.

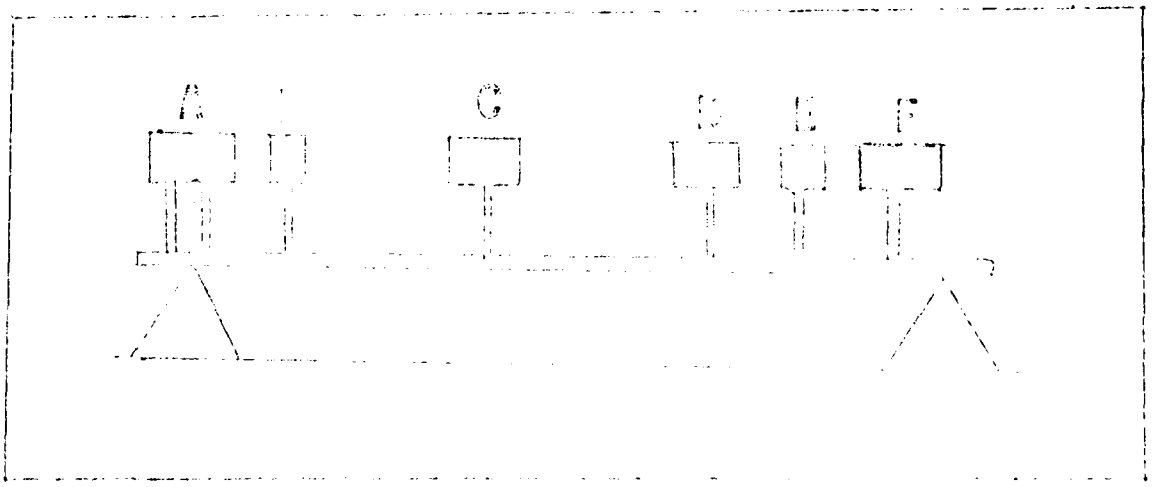


Figure 3

Figure 10 Foucault results from the HeNe laser

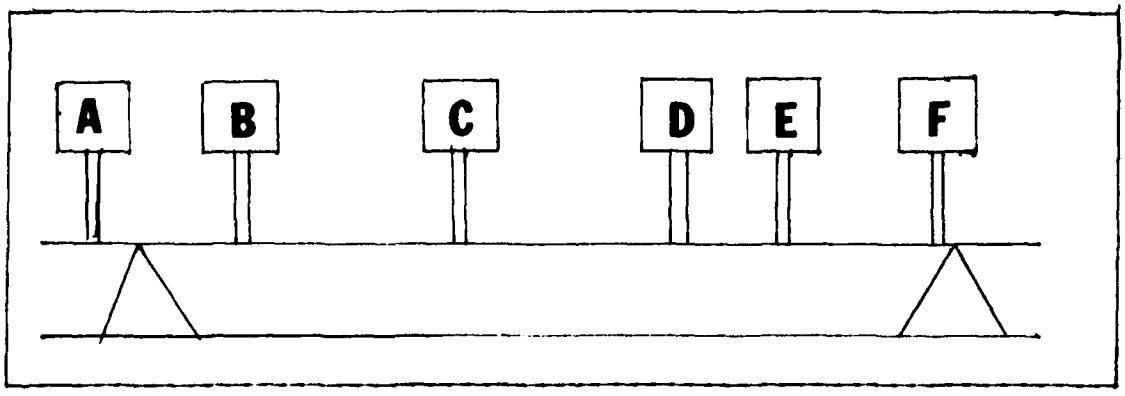


Figure 11 Experimental setup with the white light source
A is white light source
B is the pinhole
C is the lens under test
D is the knife-edge
E is the imaging lens
F is screen/camera

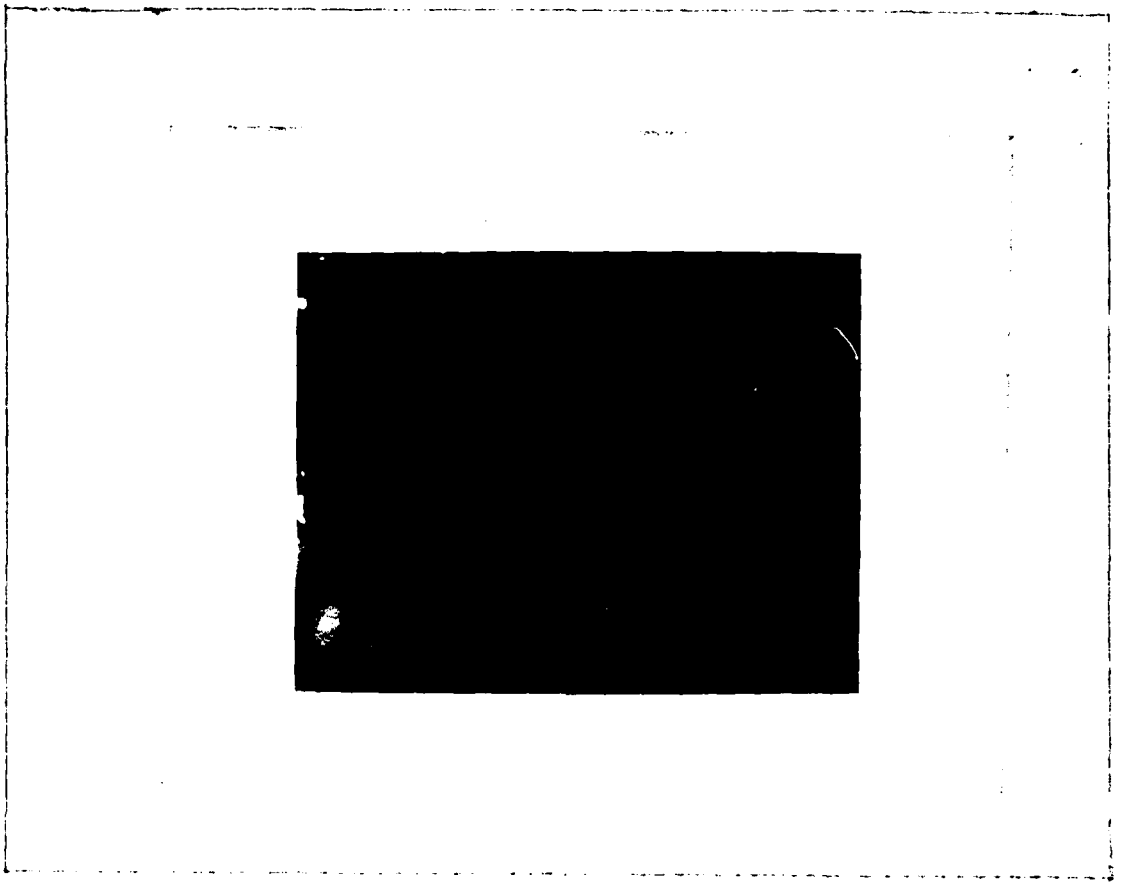


Fig. 12 Fourier results from the white light source

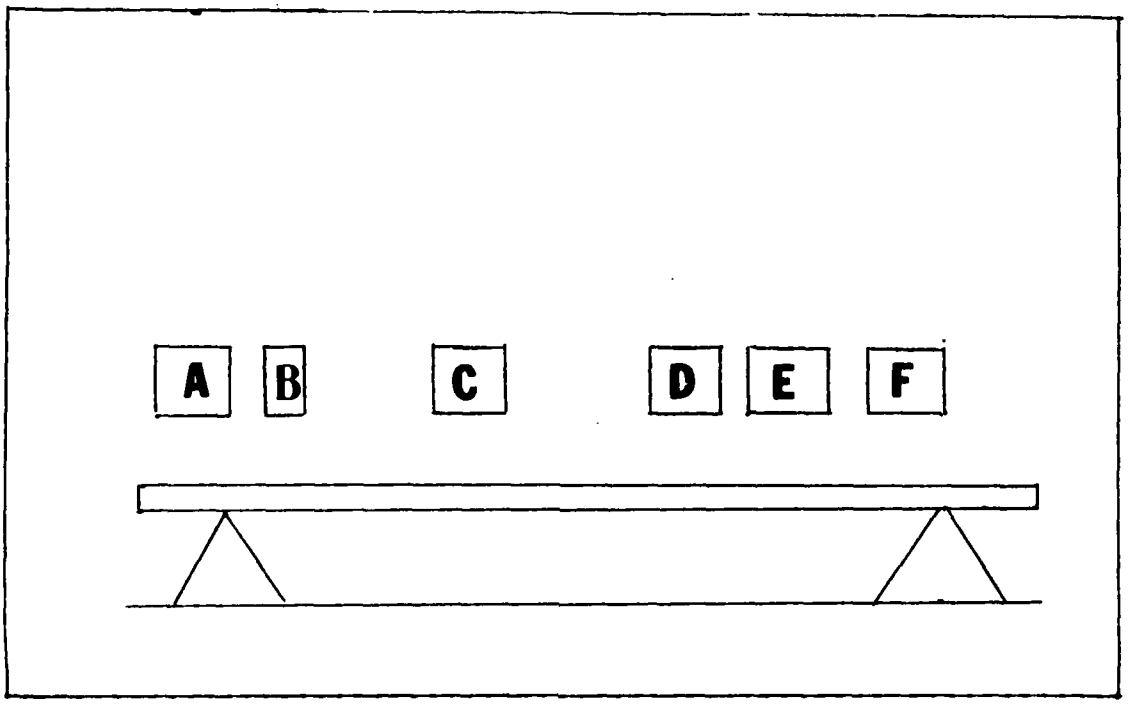
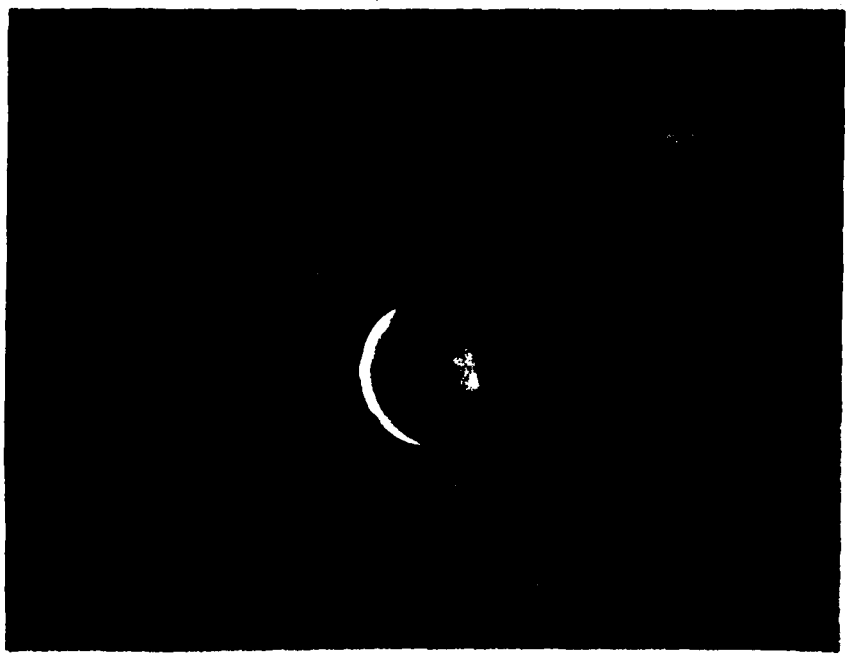


Figure 13 Experimental setup sodium source
A is the sodium lamp
B is the pin hole
C is the lens under test
D is the knife-edge
E is the imaging lens
F is the screen/camera

across the image at all times regardless of the amount of the beam the knife-edge cut off. The results that were obtained are presented in Figure 12.

The setup was then altered by the replacement of the white light source with a Sodium lamp as in Figure 13. The lenses' positions were adjusted for the wavelength with their order on the optic bench remaining the same. This setup gave the true Focogram that is presented as Figure 14.

A test to see how the aperture affects the image was conducted by inserting a 3 by 5 inch index card into the



the Foucault test. The actual explanation as to what is happening is presented in Chapter 2 pages 17-20.

Chapter 4

The Design a Ball-Null Tester

To interpret the information from the Foucault graph in an adaptive optical system, the theory that is presented in chapter two is used as the starting point. Each of the images of the knife-edge is scanned to yield the irradiance as a function of x and y. The irradiance is then divided by the background irradiance and run through a transformation to obtain the slope of the mirror surface. This slope of the mirror surface is then integrated to yield the height of the surface. Then the square of the differences of the integrated height for each direction at each point (x,y), is minimized to obtain the best height map of the mirror surface. The derivation of the equations to accomplish this task is as follows.

For a scan in the x-direction, the irradiance, I(x), is some function of x, I(x). The surface slope, r(x) is the derivative of the height with respect to x, or I(x). Now I(x) is measured, and it is desired, after integration, to

$$\int \int$$

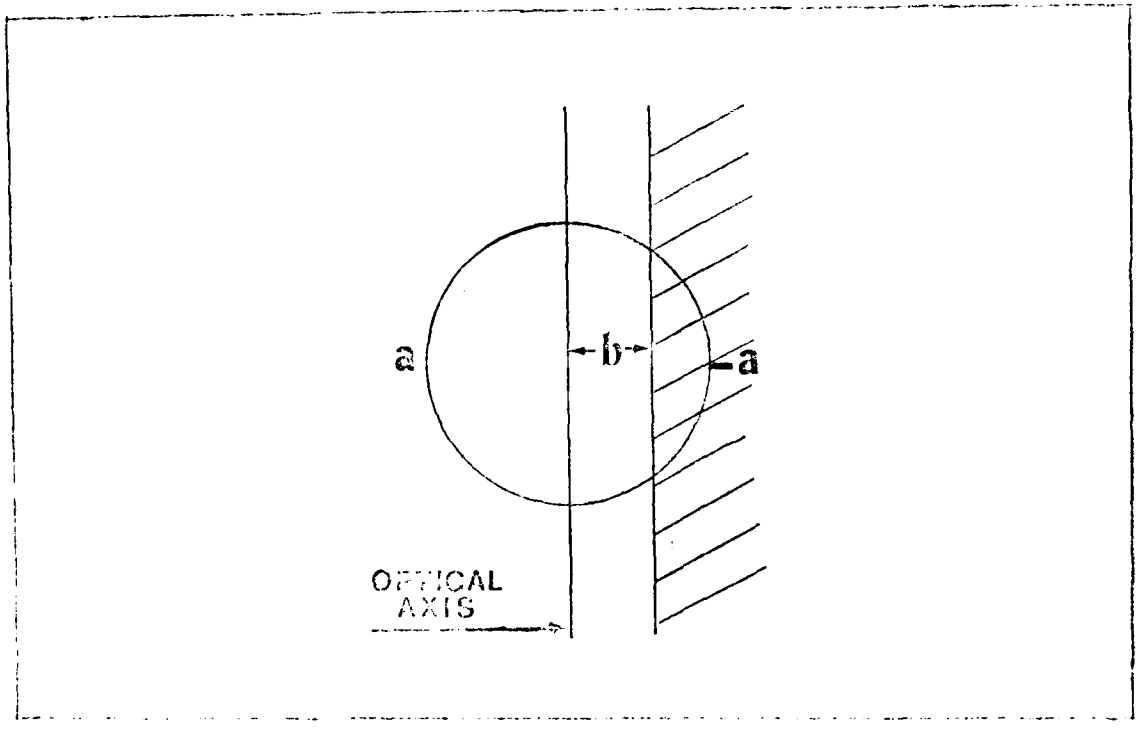


Figure 15 [illegible] for calculating the slope of the [illegible] b = [illegible] between tangent and center of [illegible]

where $b = 2Lm(x)$

L = distance between the mirror and knife-edge

$m(x)$= the local slope of the mirror

The irradiance, $I(x)$, is then:

$$I(x) = Io\ A$$

$$= Io\ (\pi/2 + \arcsin(b/a) - (b/a)(1-(b/a)^2)^{1/2})$$

where Io is the background irradiance.

Replacing b with 2Lm(x) yields:

$$I(x)/Io = \pi/2 + \arcsin(2Lm(x)/a) - (2Lm(x)/a)(1-(2Lm(x)/a)^2)^{1/2}$$

Since the y value has been a constant all through this discussion and implied, it can be inserted as part of the function to give:

$$I(x,y)/Io = \pi/2 + \arcsin(2Lm(x,y)/a) - (2Lm(x,y)/a)(1-(2Lm(x,y)/a)^2)^{1/2}$$

[illegible] the [illegible] of the [illegible] mirror slope, $m(x,y)$, where y [illegible] the [illegible]

$$I(x,y) = [illegible]$$

$$m(x,y) = dh(x,y)/dx$$

$$n(x,y) = dh(x,y)/dy$$

$$h'(x,y) = \int_0^x dx'\, m(x',y) + f(y)$$

$$h''(x,y) = \int_0^y dy'\, n(x,y') + g(x)$$

The mean difference squared between the slopes for each spot, S, can only be minimized by varying the functions $f(y)$ and $g(x)$ in the equation:

$$S = \frac{1}{A} \int\int_{A} dx\,dy\, (h'(x,y) - h''(x,y))^2$$

$$h'(x,y) = \int_0^x dx'\, m(x',y)$$

$$h''(x,y) = \int_0^y dy'\, n(x,y')$$

$$S = \frac{1}{A} \int\int_{A} dx\,dy\, \{ \quad - \quad \}^2$$

So that

$$\delta S/\delta\mu = 0 \qquad \text{when evaluated at } \mu = 0$$

$$= \int_0^1 dxdy \; (h'(x,y) - h''(x,y)) \, \tau(y)$$

$$\delta S/\delta\beta = 0 \qquad \text{when evaluated at } \beta = 0$$

$$= \int_0^1 dxdy \; (h'(x,y) - h''(x,y)) \, \mu(x)$$

$$0 = \int_0^1 dy \tau(y) \int_0^1 dx \; (h'(x,y) - h''(x,y))$$

Putting in the limits of integration:

$$0 = \int_x^a dx \mu(x) \int_{\tau^{-1}(x)}^{\tau^{-1}(y)} (h'(x,y) - h''(x,y))$$

$$0 = \int_{\tau^{-1}(x)}^{\tau^{-1}(y)} (h'(x,y) - h''(x,y))$$

```
 9    GOSUB 2000
 0 MX(I,J) = (RAD*SL(I,J))/(2*LE)
 1  IF IY(I,J)=0 THEN NX(I,J)=0:GOTO 100
 2   I(I,J)=IY(I,J)
 3    GOSUB 2000
 5 NX(I,J) = (RAD*SL(I,J))/(2*LE)
00     NEXT J
05  NEXT I
06 PRINT "Starting to integrate m(x,y)"
10 H = RAD/HOR
30 REM Intergrate mx
80 FOR A = 1 TO HOR STEP 1
90  FOR J = 1 TO VRT STEP 1
96    S=MX(A,J)
200     FOR I = 2 TO HOR STEP 2
210         FOR CON = 1 TO 2 STEP 1
220             IF CON = 1 THEN S = S + 4*MX(I,J)
230             IF CON = 2 THEN S = S + 2*MX(I+1,J)
240         NEXT CON
250        NEXT I
260      M(A,J) = H * S / 3
270   NEXT J
275 NEXT A
276 REM Intergrate n(x,y)
277 H=RAD/VRT
280 PRINT "starting to integrate n(x,y)"
```

```
14  INPUT"Input the distance between the mirror and knife-edge";LE
15  INPUT"Input the number of points in x direction"; HOR
16  INPUT"Input the number of points in y direction"; VRT
18  INPUT "Input the background intensity"; IO
19 INPUT"Input radius of the mirror";RAD
20  REM  Read Intensity in x direction
21 DIM IX(HOR,VRT),IY(HOR,VRT),MX(HOR,VRT),NX(HOR+1,VRT+1),P(VRT,HOR),G(HOR+1),
   F(VRT+1),M(HOR,VRT), N(HOR,VRT), ROY(VRT),ROX(HOR),H(HOR,VRT),FF(VRT+1),SL(V
   RT,HOR),I(VRT,HOR)
25   FOR I = 1 TO HOR
30     FOR J = 1 TO VRT
35         READ IX(I,J)
40     NEXT J
45   NEXT I
50  REM  Read Intensity in y direction
55   FOR I = 1 TO HOR
60      FOR J = 1 TO VRT
65       READ IY(I,J)
70      NEXT J
75   NEXT I
80  REM Make transformation from intensity to slope of mirror
81  PRINT "Starting to calculate the slopes at each point on the mirror."
85  FOR I = 1 TO HOR
86      FOR J = 1 TO VRT
87 IF IX(I,J)=0 THEN MX(I,J)=0:GOTO 91
88  I(I,J)=IX(I,J)
```

Appendix A

Computer program to find the error in the surface of a mirror

The following computer program is written in Rising Star's version of Basic for the Epson QX-10 personal computer. The program reads the irradiance from the data file. The slope of both directions is then calculated and integrated. After an arbitrary function for g(x) is chosen, an iteration is then set up and run to find the overall functions of each direction. Finally, the error in height is calculated and printed out.

The data file listed is from the case where it was assumed that the mirror had an height error function of $\cos(x^2/\quad)$, where $r = (\quad^2 + \quad^2)$ and a is the radius of the mirror. The [illegible] had been converted to one [illegible] δ [illegible] the [illegible] iteration point for [illegible] the [illegible] function is done equivalent to a [illegible] across [illegible]

checking out of mirrors in the infrared region, or examining microwave reflectors (antennae). And there are a vast number of possibilities in the visible region alone, for example, the automation of a lens/mirror grinding system, or the stabilization of a laser cavity. The basic design is the same for all cases, just a matter of proper scale.

Chapter 5

Conclusions and Recommendations

The work of this thesis has shown that all previous diffraction theory on the Foucault knife-edge test was inadequate to describe the actual results of the test. These inadequacies are: no bright ring is found around the image, no irradiance pattern is found outside of the mirror's boundary, coherent monochromatic light source does not produce a Focogram, and that it is not the fields of the waves that add at the focal point but their intensity to produce a Focogram. It has been shown that from the irradiance of the Focogram, the error of the surface on the mirror can be located and corrected. Also presented in this thesis are the design and [illegible] for components comprising an adaptive optical system built around the Ball-Hall test [illegible].

A possible follow-on [illegible] to the fine tuning of the computer code and the actual implementation into a control system, like that of the [illegible], as mentioned at the end of Chapter 4, [illegible] on the [illegible] but [illegible] from the surface heights as they are at the outset [illegible] by moving the [illegible]

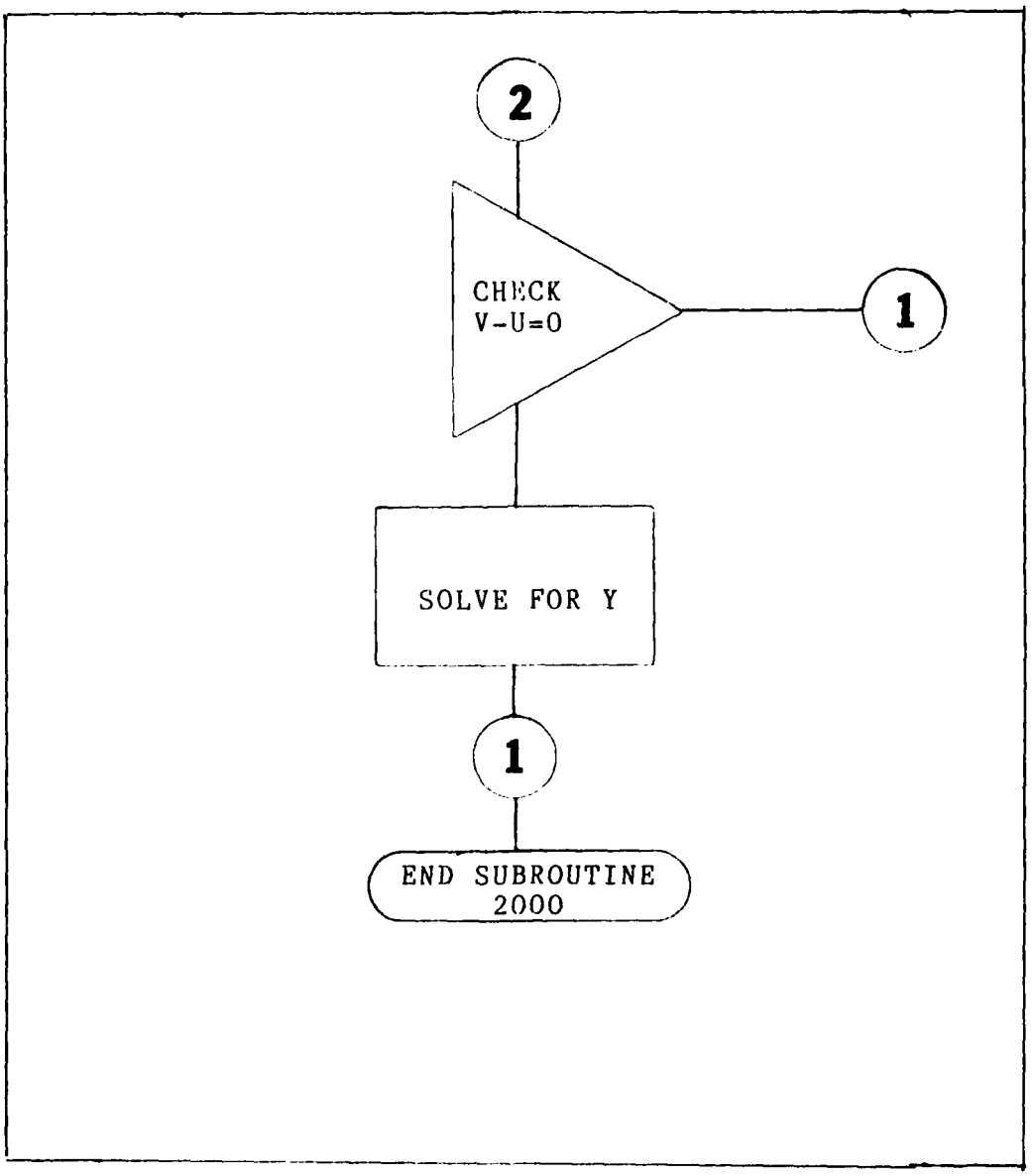


Figure 17d. The continuation of the flow chart.

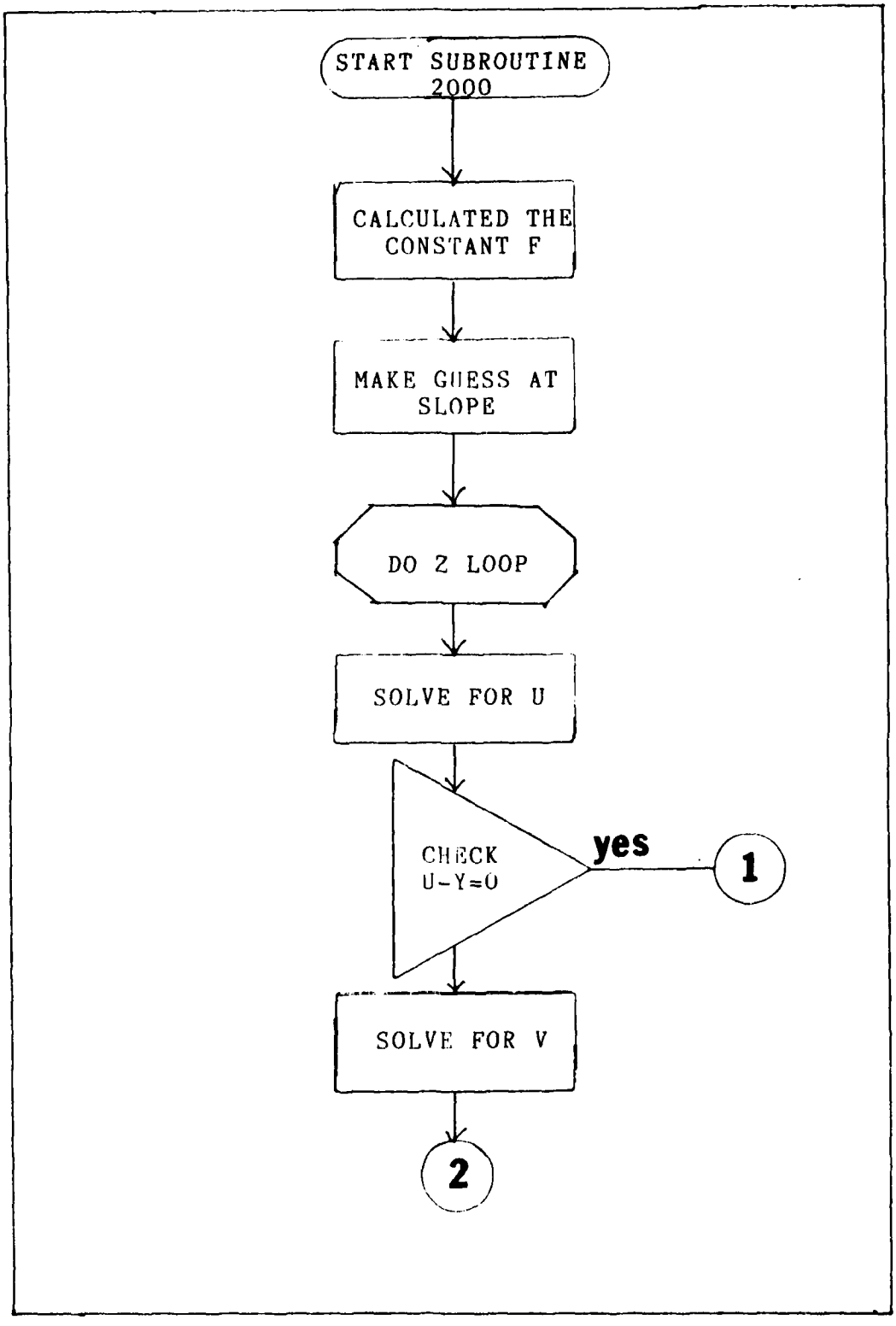


Figure 17c. The continuation of the flow chart.

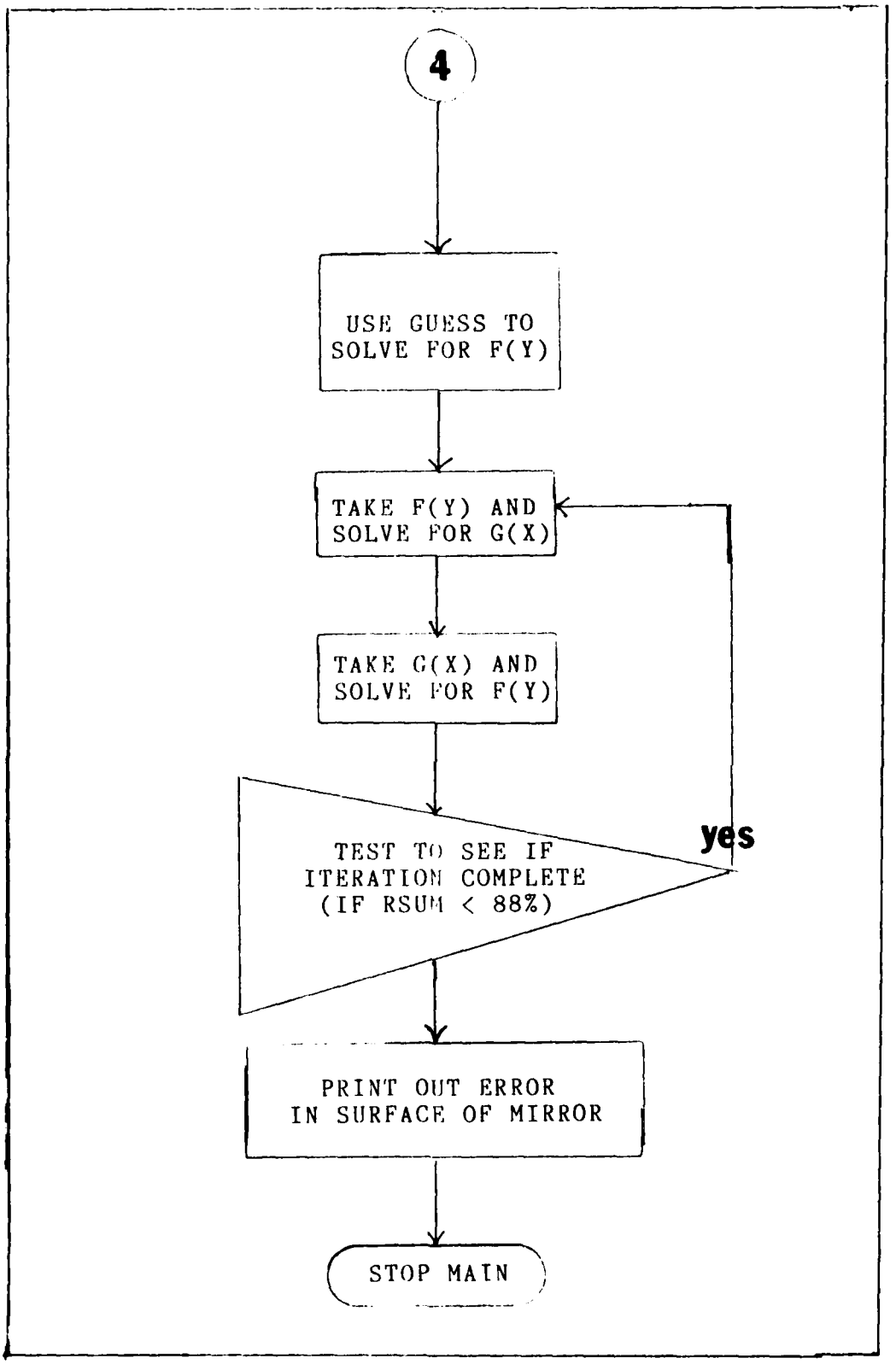


Figure 17b. The continuation of the flow chart.

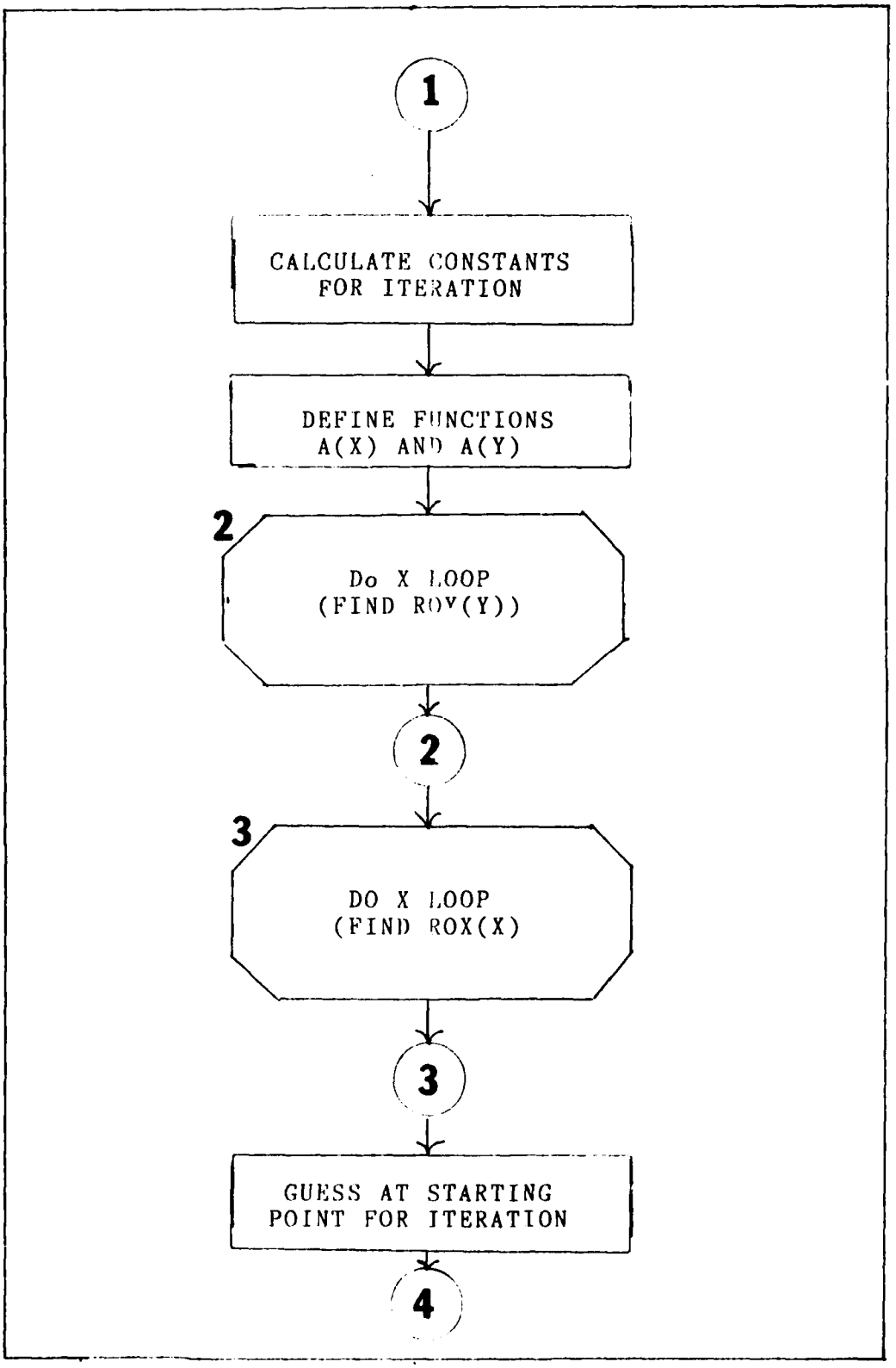


Figure 17a. The continuation of the flow chart.

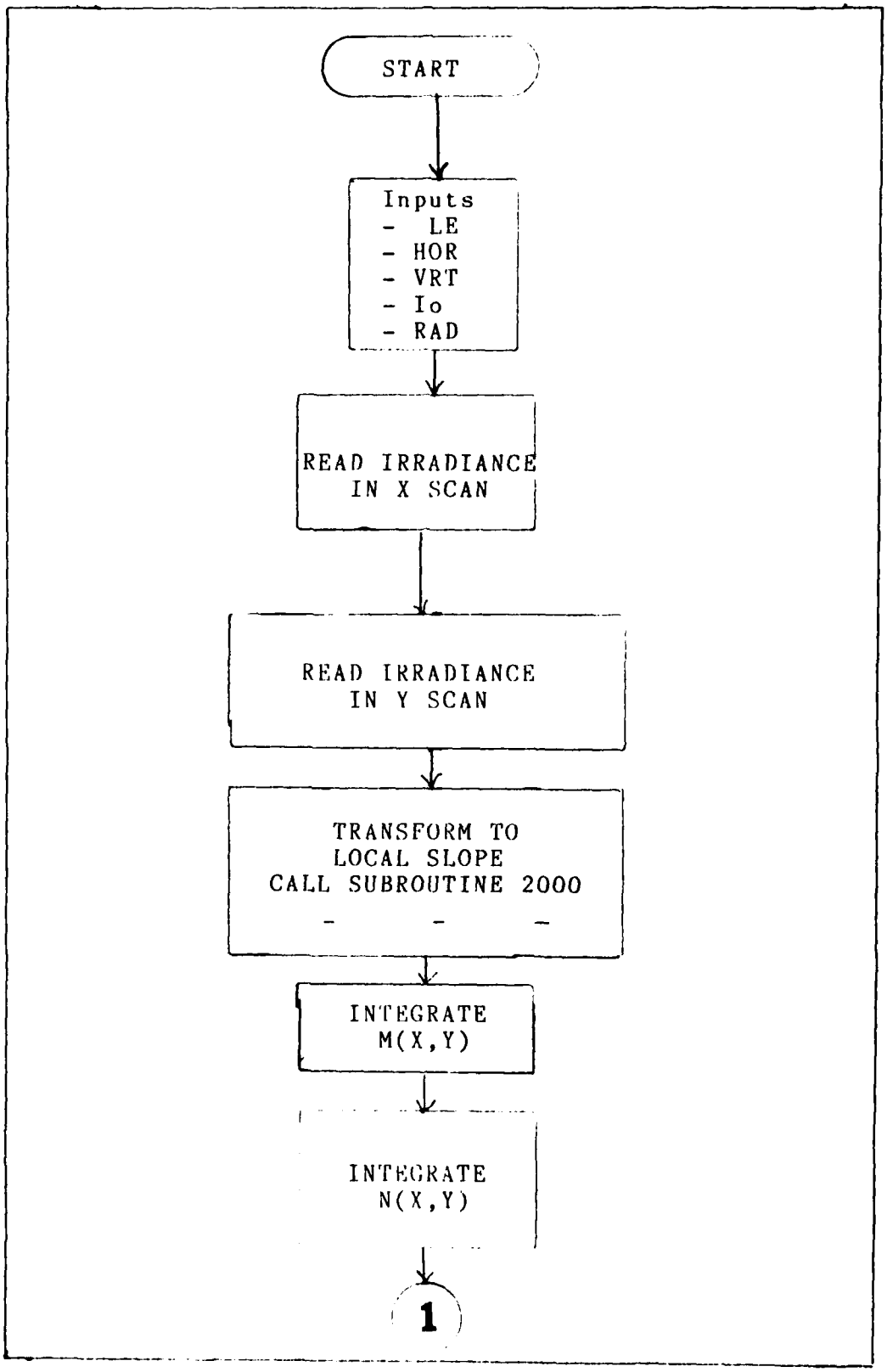


Figure 17. Flow chart of the computer program.

not using a system of this type because they are more concerned with wavefront sensing and controlling the wavefront on the out going wave, than with the surface of the mirror. They use fast acting actuators on the rear of the mirror to add imperfections to the wave front that cancel out the defects that occur during propagation to the target.

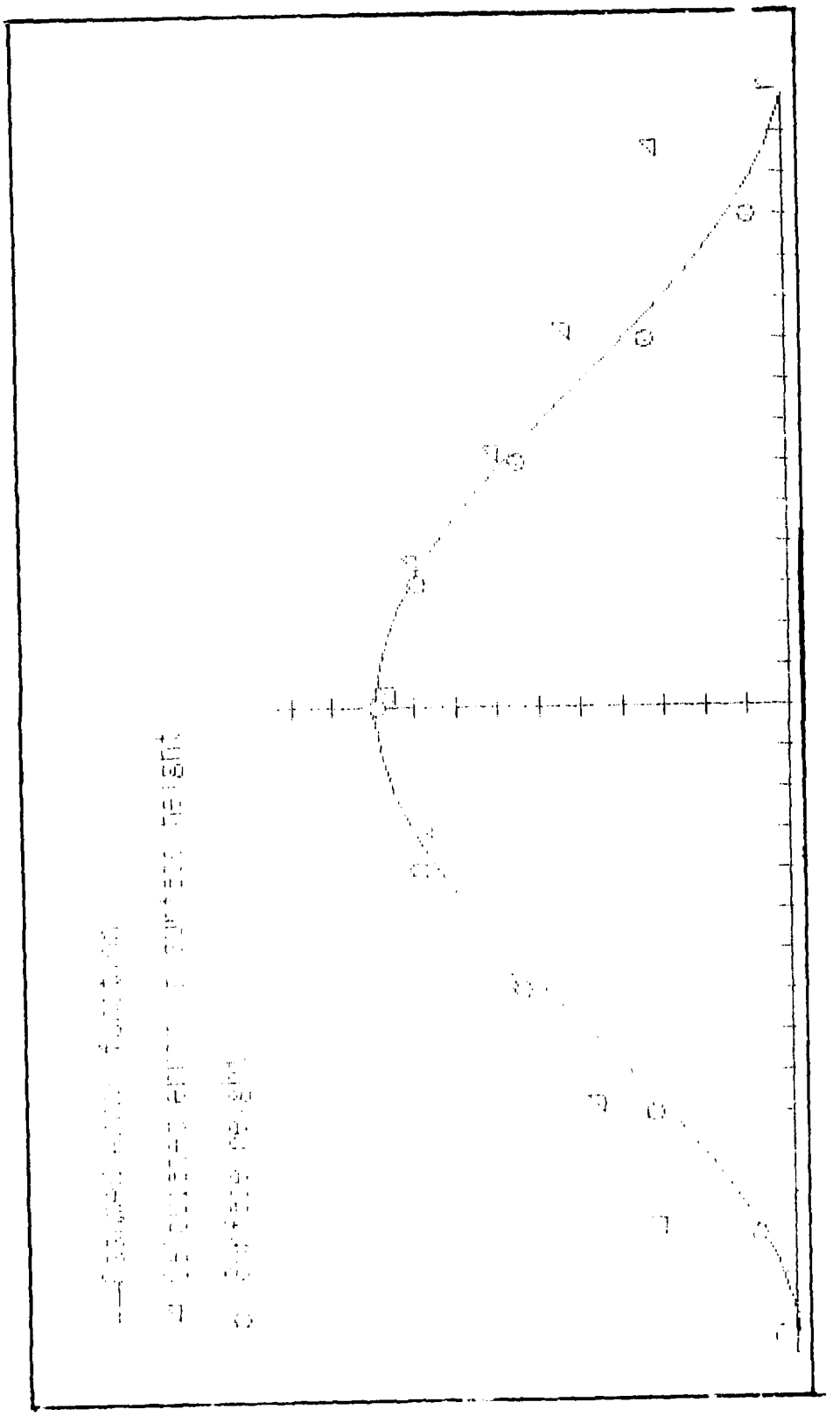


Figure 16. The graphed output across the mirror on the X-axis.

A computer program to solve for h(x,y) from the above approach is included as appendix A. Appendix B is an output from a sample run. Figure 16 shows the graphed results along the x axis of a run where it was assumed the surface had an error function of $1 + \cos(\pi r/a)$, where a was the radius and $r = (x^2 + y^2)^{1/2}$. The error function is represented as the solid curve. The height of the mirror at the points tested is shown as the circles, and the calculated error in the surface is shown as the triangles. The calculated error is close to the actual height except near the edge of the mirror. Upon close examination of the computer code it was found (under the condition that this might surface [illegible] contribution [illegible] mirror's surface. [illegible] is presented [illegible] the [illegible] the [illegible] the [illegible] program [illegible] ri[illegible].

$$0 = \int_{-a(x)}^{a(y)} dy\,(M(x,y) + f(y) - N(x,y) - g(x)) \text{ for any } x$$

$$0 = 2f(y)a(y) - \int_{-a(y)}^{a(y)} dx\, g(x) + \int_{-a(y)}^{a(y)} dx\,(M(x,y) - N(x,y))$$

$$0 = 2g(x)a(x) - \int_{-a(x)}^{a(x)} dy\, f(y) + \int_{-a(x)}^{a(x)} dy\,(M(x,y) - N(x,y))$$

$$\text{Let } p'(y) = \int_{-a(y)}^{a(y)} dx\,(M(x,y) - N(x,y)) \qquad (4)$$

$$p''(x) = \int_{-a(x)}^{a(x)} dy\,(M(x,y) - N(x,y)) \qquad (5)$$

$$f(y) = 1/2a(y)\left[p'(y) + \int_{-a(y)}^{a(y)} dx\, g(x)\right]$$

$$g(x) = 1/2a(x)\left[p''(x) + \int_{-a(x)}^{a(x)} dy\, f(y)\right]$$

The "Lock" is [illegible]:

$$L(\quad) = \int dx\,(\quad) + N(\quad) - f(\quad) - g(\quad))$$

[illegible] (7)

[illegible] (8)

[illegible]

```
290   FOR A = 1 TO VRT STEP 1
300  FOR I = 1 TO HOR STEP 1
306    S = NX(I,A)
310     FOR J = 2 TO VRT STEP 2
340         FOR CON = 1 TO 2 STEP 1
350             IF CON = 1 THEN S = S + 4 * NX(I,J)
360            IF CON = 2 THEN S =S + 2*NX(I,J+1)
370             NEXT CON
380      NEXT J
390     N(I,A) = H * S /3
395    NEXT I
396 NEXT A
397 REM Setting up constanst for the iterration phase.
400  FOR I = 1 TO HOR
410     FOR J = 1 TO VRT
420         P(I,J) = M(I,J) - N(I,J)
430         NEXT J
440      NEXT I
445 REM define functions a(y) and a(x)
450 DEF FN A(X) = SQR(RAD^2 -X^2)
460 DEF FN A(Y) = SQR(RAD^2 - Y^2)
465 REM solvinging the integrals for the constant functions of x and y
500  FOR Y=1 TO VRT STEP 1
505   S = P(1,Y)
510   FOR X = 1 TO (HOR/2-.5) STEP 2
530          S=S+4*P(X,Y)
```

```
540          S = S + 2*P(X+1,Y)
550        NEXT X
560      ROY(Y) = S*H/3
570    NEXT Y
620    FOR X=1 TO HOR
625      S=P(X,1)
630       FOR Y=2 TO (VRT/2-.5) STEP 2
640        S=S+4*P(X,Y)
650        S=S+2*P(X,Y+1)
660       NEXT Y
670       ROX(X)=S*H/3
680  NEXT X
685   REM Guess at what g(x) is, try 1-x^6
690  DEF FN G(X) = 1-(ABS(X))^6
695  DY = RAD/VRT
696   Y=0
699   REM Start point of iterration
700  FOR K = 1 TO VRT
710   Y=Y+DY
711  IF Y^2 => RAD^2 THEN GOTO 793
720  A=SQR(RAD^2-Y^2)
730  IN=0
740      FOR N=1 TO 11
750      X = -A + .2*A(N-1)
760     IN=IN+(.2*A)*FN G(X)
770      NEXT N
```

```
911 IF Y^2 => RAD THEN GOTO 992
920    A=SQR(RAD^2-Y^2)
930   IN=0
940    Z=INT(A/DX)
950     FOR N= 1 TO Z
960     IN=IN +DX*G(N)
970       NEXT N
980    FF(K)=(1/(2*A))*(ROY(K)+IN)
990   NEXT K
991 GOTO 997
992 FF(K)=0
993 GOTO 990
997 SUM=0
998  N=0
999 REM "Ready to check"
1000 FOR K= 1 TO HOR
1010     SUM=SUM+1
1020    DIF = FF(K)-F(K)
1030    IF DIF < 1E-03 THEN N=N+1
1040    F(K)=FF(K)
1050     NEXT K
1060    RSUM = N/SUM*100
1070   PRINT "The percent matched =",RSUM
1080    IF RSUM < 85 THEN 795
1090  REM if matched then print out f(y) and g(x) and find h(x,y)
1091  FOR X = 1TO HOR
```

```
780 F(K)=(1/(2*A))*(ROY(K)+IN)
785 W=W
790  NEXT K
791 GOTO 795
793 F(K)= 0
794 GOTO 790
795  DX = RAD/HOR
796  X=0
799 REM "ready to start 800 loop"
800  FOR K = 1 TO HOR
810      X=X+DX
811 IF X^2 => RAD^2 THEN GOTO 893
820      A=SQR(RAD^2 - X^2)
830     IN=0
840      Z=INT(A/DY)
850      FOR N = 1 TO Z
860       IN =IN + DY*F(Z)
870      NEXT N
880 G(K) = 1/((2*A))*(ROX(K)+IN)
890  NEXT K
891  GOTO 899
893  G(K) = 0
894 GOTO 890
899 Y=0
900  FOR K=1 TO VRT
910    Y=Y+DY
```

```
1092       PRINT F(X),G(X)
1093    NEXT X
1098      I=-1
1100  FOR X= 1 TO HOR
1105      J=-1
1110      FOR Y= 1 TO VRT
1115       IF (J^2+I^2) > RAD THEN H(X,Y)=0:GOTO 1130
1120         H(X,Y)=.5*(M(X,Y)+N(X,Y)+F(Y)+G(X))
1130  LPRINT X,Y,"Error is"H(X,Y)
1131       J=J+(2*(RAD/VRT))
1140       NEXT Y
1145       I=I+(2*(RAD/HOR))
1150     NEXT X
1160 GOTO 9999
1990 REM This is the subroutine to numericly solve for the slope of the mirror.
2000 F = I(I,J)/IO - PI/8
2100 Y=1E-03
2120 FOR Z = 1 TO 20
2200 U = SIN(F + SQR(ABS(1-Y*Y)))
2205 IF (U-Y) = 0 THEN GOTO 2300
2210 Y = 1/(U-Y)
2211 V=SIN(F+U*SQR(1-U*U))
2212 IF (V-U) = 0 THEN V=Y; GOTO 2300
2213 V=1/(V-U)
2214 IF (V-Y) = 0 THEN GOTO 2300
2215 Y=U+1/(V-Y)
```

```
 220 NEXT Z
2300 SL(I,J)=Y
2310 RETURN
3000 DATA 0,0,0,0,0,0,0,0,0,0,0,0,0,0,.914966,1.59555,1.84658,1.59556,.914966,0
     ,0
3010 DATA 0,0,0,1.01765,2.00827,2.72604,2.98783,2.72604,2.00827,1.01765,0,0,0,.
     45748,1.33885,2.1743,2.77137,2.98783,2.77137,2.17431,1.33885,.45748,0,0,.3
     9889,.90868,1.3856,1.72,1.847,1.72423,1.3857,.90868,.39889,0,0,0,0,0,0,0,0
     ,0,0,0,0,0,-.3989,-.9087,-1.3857
3020 DATA -1.72422,-1.846,-1.724,-1.3857,-.90868,-.39889,0,0,-.45748,-1.3388,-2
     .1743,-2.7714,-2.9878,-2.771,-2.174,-1.3388,-.45748,0,0,0,-1.0176,-2.0083,
     -2.726,-2.9878,-2.726,-2.0083,-1.01765,0,0,0,0,0,-.91497,-1.5955,-1.84658,
     -1.5955,-.91497,0,0
3030 DATA 0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,.457483,.398889,0
     ,-.398889,-.457483,0,0,0,0,0,1.01765,1.33884,.90868,0,-.90868,-1.33884,-1.
     01765,0,0,0,.914966,2.00826,2.17431,1.38568,0,-1.38568,-2.17431,-2.00826,-
     .914966,0,0,1.59555,2.72604
3040 DATA 2.77137,1.72422,0,-1.72422,-2.77137,-2.72604,-1.59555,0,0,1.84658,2.9
     8783,2.98783,1.84658,0,-1.84658,-2.98783,-2.98783,-1.84658,0,0,1.59555,2.7
     2604,2.77137,1.72422,0,-1.72422,-2.77137,-2.72064,-1.59555,0,0,.914966,2.0
     0826,2.17431,1.38568,0,-1.38568
3050 DATA -2.17431,-2.00826,-.914966,0,0,0,1.017654,1.338884,.90868,0,-.90868,-
     1.33884,-1.01765,0,0,0,0,0,.457483,.398889,0,-.398889,-.457483,0,0,0,0,0,0
     ,0,0,0,0,0,0,0,0,0
9999 END
```

	1	Error is 0
1	2	Error is 0
1	3	Error is 0
1	4	Error is 0
1	5	Error is 0
1	6	Error is 0
1	7	Error is 0
1	8	Error is 0
1	9	Error is 0
1	10	Error is 0
1	11	Error is 0
2	1	Error is 0
2	2	Error is 0
	3	Error is 0
2	4	Error is 1.1384639849
2	5	Error is 1.1372537323
2	6	Error is 1.1388195447
2	7	Error is 1.137878966
2	8	Error is 1.1374952983
2	9	Error is 1.1380261465
2	10	Error is 0
2	11	Error is 0
3	1	Error is 0
3	2	Error is 0
3	3	Error is 1.1388024637
3	4	Error is 1.1396093156

3	5	Error is 1.1383997087
3	6	Error is 1.1399658315
3	7	Error is 1.1390248203
3	8	Error is 1.1386402233
3	9	Error is 1.1391705686
3	10	Error is 1.1364436818
3	11	Error is 0
4	1	Error is 0
4	2	Error is 1.1399686284
4	3	Error is 1.1405416143
4	4	Error is 1.1413486153
4	5	Error is 1.1401383[illegible] 1
4	6	Error is 1.1417042413
4	7	Error is 1.1407631514
4	8	Error is 1.140378128
4	9	Error is 1.1409084712
4	10	Error is 1.1381820315
4	11	Error is 1.1151828256
5	1	Error is 0
5	2	Error is 1.1407981127
5	3	Error is 1.1413812201
5	4	Error is 1.1421781141
5	5	Error is 1.140966361
5	6	Error is 1.1425316291
5	7	Error is 1.1415906985
5	8	Error is 1.141205673
5	9	Error is 1.1417364446

5	10	Error is 1.1390109322
5	11	Error is 1.1160117263
6	1	Error is 0
6	2	Error is 1.1442853743
6	3	Error is 1.1448593163
6	4	Error is 1.1456654273
6	5	Error is 1.1444530782
6	6	Error is 1.146018696
6	7	Error is 1.1450772066
6	8	Error is 1.1446920279
6	9	Error is 1.1452228761
6	10	Error is 1.1424977963
6	11	Error is 1.1194985905
7	1	Error is 0
7	2	Error is 1.1402571981
7	3	Error is 1.1408306952
7	4	Error is 1.1416367275
7	5	Error is 1.1404245377
7	6	Error is 1.1419895967
7	7	Error is 1.1410488752
7	8	Error is 1.1406642864
7	9	Error is 1.1411953954
7	10	Error is 1.1384700051
7	11	Error is 1.1154707992
8	1	Error is 0
8	2	Error is 1.1388769069

8	3	Error is 1.1394494872
8	4	Error is 1.1402550931
8	5	Error is 1.1390429011
8	6	Error is 1.140607807
8	7	Error is 1.1396676754
8	8	Error is 1.1392846058
8	9	Error is 1.1398163441
8	10	Error is 1.13709031
8	11	Error is 1.1140911041
9	1	Error is 0
9	2	Error is 1.140134488
9	3	Error is 1.1407066998
9	4	Error is 1.1415123037
9	5	Error is 1.1403005402
9	6	Error is 1.1418655226
9	7	Error is 1.1409256518
9	8	Error is 1.1405432114
9	9	Error is 1.1410748048
9	10	Error is 1.138347918
9	11	Error is 1.1153487121
10	1	Error is 0
10	2	Error is 0
10	3	Error is 1.1330263727
10	4	Error is 1.1338326099
10	5	Error is 1.1326217736
10	6	Error is 1.1341871886

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Abstract

This is a study to design a self correcting primary mirror system for a space telescope. The design is centered around a Dall-Null tester (a Foucault knife-edge tester with compensating lens). An indepth study of the theory of the Foucault test from Foucault's original publications to current work is presented. Also short comings of the diffraction approach are shown. The findings of an simple experiment showed the way to the correct explanation as to the workings of the test. Based on this new explanation, a computer program to find the error in the surface of the mirror from the irradiance pattern provided by the Dall-Null tester was developed. The computer program with a sample run is included in the appendixes A and B.

The basic design of an adaptive optic system for a space-borne application is also presented in the paper. This design has the desired quality of being able to correct the mirror while the telescope is in use. The equations being independent of wavelength allows for the design to be applied to systems working outside of the visible spectrum as well as the systems working in the visible.

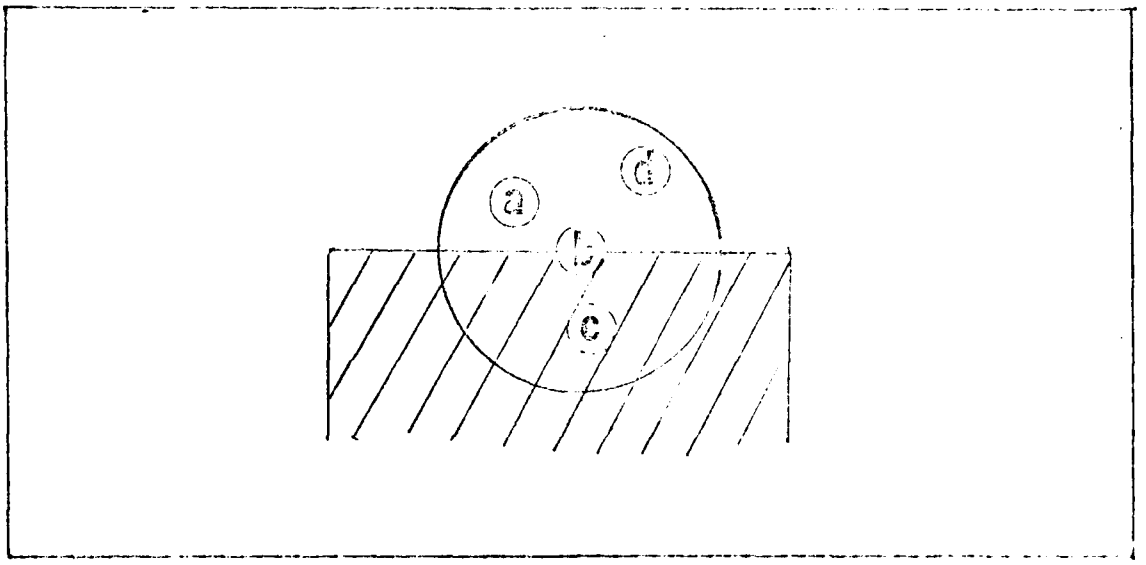

Figure 6. The relative poisition of the Airy patterns at the knife-edge.

image, cases a and d, then all of the image will pass the knife-edge. But if the slope lowered the image, case c, the knife-edge would cut it off completely. Thus the brightness of the resulting image would be determined by how much of each segment's image was passed by the knife-edge. Figure 7 shows the result for the current situation.

Thus the correct theory of the Foucault test is complete, and likewise, so is the theory of the Hull-Hull test. And in chapter four this theory will be put to work to find the error in the height of the mirror surface.

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