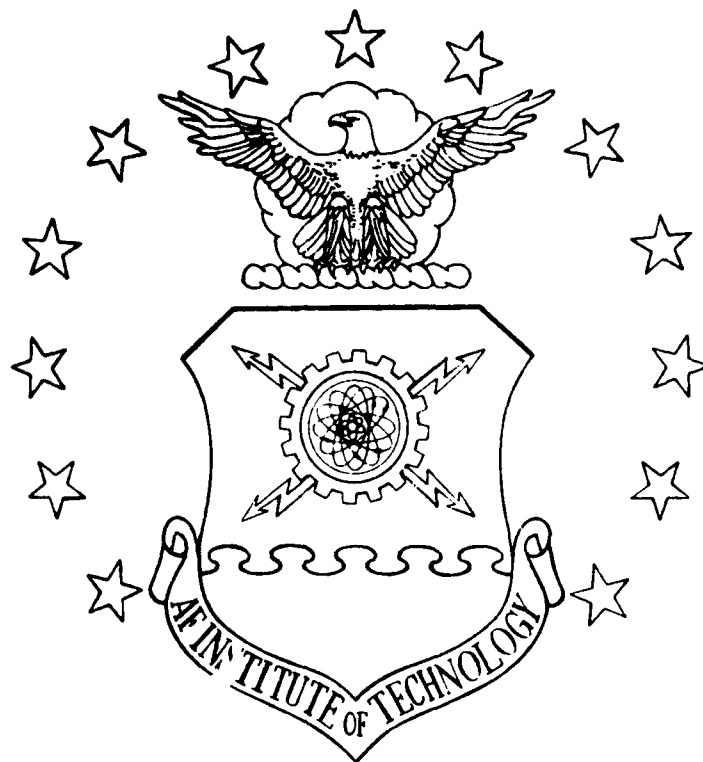


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ERROR PREDICTIONS IN  
 ACCOUNTING POPULATIONS  
 THESIS  
 Blaine F. Webber  
 Captain, USAF  
 AFIT/GSM/LSY/86S-23

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ERROR PREDICTIONS IN ACCOUNTING POPULATIONS

THESIS

Presented to the Faculty of the School of Systems and Logistics  
of the Air Force Institute of Technology  
Air University  
In Partial Fulfillment of the  
Requirements for the Degree of  
Master of Science in Systems Management

Blaine F. Webber, B.S.

Captain, USAF

September 1986

Approved for public release; distribution unlimited

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ABSTRACT

The purpose of this ~~research~~ was to examine robustness, mean relative tightness, coverage, and power of selected unmodified and modified Cox and Snell and Stringer error limit bounds. The simulation was performed by repetitive sampling from an accounting population with various known book value and error distributions. Additional modifications to the selected modified Cox and Snell bounds was done by incrementally loosening the bounds by 5, 10, and 20 percent in a search for bounds with better performance characteristics.

There were several conclusions that could be made from this research. The modified Cox and Snell bounds can achieve high coverages for accounting populations with low error amount intensity (EAI) with significant increases in mean relative tightness over unmodified Cox and Snell bounds. The Stringer and Cox and Snell bounds can still achieve high coverages with significant improvements in mean relative tightness when the nominal confidence level is lowered from 90% to 85%. Only minor changes in prior probability settings materially affect the performance of Cox and Snell bounds. And, in accounting populations with low EAI, the selected Cox and Snell bounds are conservative.

# ERROR PREDICTIONS IN ACCOUNTING POPULATIONS

## I. Introduction

### General Problem

Auditors are required to make statements about the accuracy of financial accounts by reviewing internal controls and empirical sampling. Through sampling and inferential statistics, auditors estimate as accurately as possible the maximum amount an account is likely to be in error. Their estimate is known as the upper error limit. The upper error limit is then compared to the material error, which is the limit of precision necessary for the account. Results of the comparison enable the auditor to state an opinion about the reasonable accuracy of the account (8:4,5).

The estimation of upper error limits depends on our ability to construct models incorporating two aspects of accounting: the error rate and the distribution of error sizes for those accounts in error [3:180].

Traditionally, to reduce risk, auditors have chosen upper error limit bounds which result in very broad confidence intervals, possibly far in excess of the actual error. This conservative approach is due to the fact that little is known about the characteristics of accounting populations (7:270). Conservatism leads to possible erroneous rejection of the hypothesis that the book value of the audited

population is reasonably accurate. Therefore, it is necessary to choose sampling plans and error limit bounds which are appropriate to the auditing situation.

Sampling should be done in such a way that a maximum amount of information can be obtained at a minimum cost.

When the auditor samples accounting populations, he encounters two key sets of problems. One is connected with low error rates in the accounting populations. The other pertains to the effectiveness of sampling procedures designed for either low or high error rates when the actual error rates are not of the anticipated magnitude [10:4].

Low error rates pose significant problems for auditors who use classical statistical estimators. Dollar-unit sampling (DUS) was "specifically developed for use in the auditing environment where low error rates in account balances are often encountered" (3:179). Bayesian procedures using prior subjective information about accounting populations have been used DUS to produce tighter upper error limits than those obtained with the DUS method and classical estimators (3:179). The Bayesian approach, though, has its own problems: (1) difficulty in assessing a prior probability judgment, and (2) measurement of utility in those decisions where the sums involved are large (1:115).

#### Definition of Key Terms

Confidence Interval: the range around a calculated sample mean in which the population mean is expected to lie at the given confidence level.

Nominal Confidence Level: the expected frequency of correct intervals or bounds in repeated samples.

Conservatism: larger upper error limits calculated than the nominal confidence level.

Error Taint: the error amount found in a sample unit divided by the true book value.

Rel Tightness: the magnitude of an upper error limit relative to the true error in the population.

Coverage: in repetitive sampling, the percentage of calculated upper error limits which are equal to or greater than the true dollar error in the population.

### Background

Upper Error Limits. When auditors first began using sampling techniques to estimate errors in accounting populations, they used classical sampling estimators: ratio and difference estimators.

Stringer (1963) cautioned that use of these estimators entails potential dangers because their estimated standard errors will equal zero when no errors are found in the sample. With classical large-sample confidence limits this would imply that the point estimate of the total audit amount or the total error amount is perfect, which, obviously is not a reasonable conclusion in an audit situation employing a moderately large sample size [9:77].

To overcome the observed shortcomings with ratio and difference estimators, Stringer developed his own method of calculating error limits (called the Stringer bound). Although the Stringer bound has been used extensively, it is not without its own problems. First of all, no general

theory has been published which supports the Stringer bound. This lack of theory occurs because the Stringer bound involves a combination of attributes and variables principles which makes theoretical analysis difficult. Second, the Stringer bound itself is very conservative, resulting in upper error limits far greater than the true error in populations (9:78).

In 1973, Anderson and Teitlebaum also identified potential dangers in using ratio and difference estimators for auditing when the error rate is small. They proposed using dollar-unit sampling together with the Stringer bound for estimating the total overstatement error in accounting populations. Dollar-unit sampling, which considers the individual dollar as the sample unit, requires no further stratification by book amount since all sampling units are exactly the same size in terms of book value without the need for stratification [8:78,79]. "Dollar-unit sampling can be thought of as employing the ultimate in stratification by book amount" [9:78].

In order to obtain more empirical evidence about the behavior of classical estimators, Neter and Loebbecke in 1975 conducted simulation studies with four actual accounting populations. They examined the performance of the mean-per-unit, ratio, and difference estimators each with simple, stratified random, and dollar-unit sampling. They found that, for the estimators under study, performance

varied significantly depending upon the error sizes and the distribution of errors within the populations. When the population error rate was small to moderate or the distribution of errors was highly skewed, the actual proportions of correct confidence intervals was far below the nominal level. Even under the most favorable conditions, Neter and Loebbecke found that there is the possibility that the nominal confidence coefficient based on the normal distribution differs somewhat from the actual confidence level [10:134,135].

In 1977 Neter, Leitch, and Fienberg proposed a different method of obtaining a bound for total population error. Basing their bound on the multinomial probability distribution, they named it the multinomial bound for overstatement errors. The multinomial bound has been found to be effective because:

- (1) it incorporates information about the magnitude of the sample errors;
- (2) it has distributional properties which are fully known;
- and (3) it does not require any assumptions about the distribution of the population or of the errors in the population [5:3].

When used with dollar-unit sampling, the multinomial bound has been shown to be significantly tighter than the Stringer bound, with actual confidence levels nearer to nominal levels (5:3).

While the use of monetary-unit sampling with either the Stringer bound or the multinomial bound avoids the problem of actual confidence levels far below the nominal level when there are few errors in an accounting population, neither the Stringer bound nor the multinomial bound permit a direct netting of

over- and understatement errors. Further, neither of these two bounds directly takes into account prior information which the auditor may have about the population error rate and/or the magnitude of the taintings in the population.

In contrast, a Bayesian approach to constructing bounds for the total error amount in an accounting population does enable the auditor to incorporate prior information into the estimation procedure, though there may be difficulties in making the needed assessments. The Bayesian approach also can provide bounds not only for the total overstatement and/or understatement error amounts in an accounting population separately, but for the net total error amount as well [5:3].

A great deal of support has been generated to integrate prior subjective knowledge of accounting populations into statistical calculations from statisticians as well as auditors.

Thus perhaps the strongest argument favoring the formal Bayesian decision process is that this intuition [prior subjective knowledge] is incorporated formally into the decision process. Moreover, by quantifying the intuition in the model, the Bayesian approach tends to prevent haphazard use of this experience [1:111].

My own view on the problem of estimating the money value of error is that a Bayesian approach is the only satisfactory one from a statistical viewpoint. The auditor's judgement on many issues is highly subjective and thus there is no reason why subjective ideas should not be introduced into the interpretation of his test results [12:279].

Cox and Snell (1979) proposed the use of "infinite population theory as a theoretical foundation for the development of a Bayesian upper bound for the total overstatement amount in the population" (5:499). A 1984 study done by Godfrey and Neter produced the following conclusions concerning the Cox and Snell bounds: (1) the

bounds are substantially affected by prior parameter assessments, (2) they are much tighter than the Stringer bound and have high coverage when the actual population contains low error rates, and (3) they are moderately tighter than the Stringer bound for populations whose error amount is large (5:520).

Godfrey and Andrews, in 1982, presented an alternative to classical and other Bayesian procedures. Their method, the finite Bayesian procedure, correctly assumes a finite population (which other Bayesian methods do not) and allows the integration of the auditor's prior information through a prior distribution. They found that their finite Bayesian model more closely approaches the actual population than other procedures and usually requires smaller sample sizes. As with other Bayesian models, the difficulty in the finite Bayesian procedure lies in determining a reasonably accurate prior assessment (4:304-315).

Several other Bayesian approaches have been proposed by statisticians and auditors. McCray, in 1982, assumed a discrete prior distribution for the total error amount and a multinomial distribution for the monetary unit taints. Garstka proposed a compound Poisson model which uses a discrete prior distribution for the mean error taint which is used to calculate an upper error bound for the total error amount. Vanacek's approach uses a beta prior

distribution for the population error rate, then obtains Bayesian posterior bounds for the population error rate (5:499).

In 1984, Dworin and Grimlund published a paper proposing a new method of statistical analysis for dollar-unit sampling. Their method was designed to overcome the conservative nature of previously applied upper error bounds. Their new bound, called the moment bound, holds considerable promise for inventory accounts. Results from their study indicate that, when the material limit of the population is less than four percent of book value, the moment bound will lead to the acceptance of more accounts than the multinomial bound. For populations where both understatement and overstatement errors are present, the moment bound provided significantly tighter bounds (2:219,236).

In 1985, Phillips examined modified and unmodified Stringer and Cox and Snell bounds for robustness using 96 accounting populations. He found that none of the modified Cox and Snell bounds were robust and that both the modified and unmodified Stringer bounds were robust at the 95 and 85 percent levels of confidence. The modified Stringer bound produced upper error limits which were approximately 19 percent tighter relative to the unmodified Stringer bound [11:105,106]. Phillips also found that decreasing, uniform, and increasing clustering of errors among line

items did not have a significant impact upon bound performance.

In a study done by Helton in 1985, modified and unmodified DUS-cell and Stringer bounds were examined for robustness at varied confidence levels. For the populations under study, he found that the only robust bounds were the unmodified Stringer bounds. However, all coverage failures occurred when a 50 percent line item error rate was introduced into the study population. Also, under certain error conditions, the unmodified Stringer and DUS-cell bounds produced tighter bounds relative to the respective modified bounds [6:4-1].

Characteristics of Accounting Populations. Auditors require knowledge of the frequency, magnitude, distribution, and the possible causes of errors in accounting populations to effectively and efficiently provide statements about the accuracy of the account (7:271). Prior to a study done by Johnson, Leitch, and Neter in 1981, little had been published about accounting population characteristics. Their study concentrated on accounts receivable and inventory audits and analyzed the magnitude of error rates, the susceptibility of individual items to error within the account, and the degree of overstatement and understatement errors (7:273,274). Highlights from the summary of their results are:

1. There is great variability in the error rates for both types of audits, with the inventory audits

tending to be substantially higher than those for accounts receivable.

2. There is some evidence from the 81 audits which suggests that the error rates in both types of audits may be higher for the larger accounts and for accounts with larger line items than for other accounts.

3. Most errors in receivables audits are overstatement errors, while inventory audits overstatement and understatement are more balanced in number.

4. The distribution of taintings are variable for both types of audits, especially those for inventory audits, and depart substantially from a normal distribution. Quite a few of the tainting distributions for inventories are negatively skewed [7:291].

These results verify that great care must be taken to choose the appropriate methods for sampling, estimating population means, and calculating upper error limits. Assuming a normal distribution is not appropriate for accounting populations. Results from the study indicate that dollar-unit sampling is the most beneficial method, in terms of gathering accurate information, of sampling accounting populations.

Conclusion. Auditors are faced with significant problems in choosing appropriate sampling techniques and upper error limits. Much research has been done trying to deal with these problems, but no clear solution currently exists. Further research in examining current methods and the development of new methods is needed. More efficient and effective auditing procedures will assist auditors in making more accurate and reliable decisions.

## SPECIFIC PROBLEM

Auditors must deal with two basic problems with accounting populations. First, accounting populations have relatively few errors. Sampling the populations may result in finding very few errors, which poses significant dilemmas when dealing with classical statistical estimators such as the mean-per-unit, ratio, or difference estimators. Using the sample results to construct confidence intervals for the population error may be unacceptable. The actual confidence intervals provided by classical estimators may be far less than their corresponding nominal levels. This leaves the auditor with no statistical foundation upon which to base his audit opinion. The second major problem facing auditors is determining an acceptable method of quantifying the judgment an auditor wants to make about an account. Classical statistics provide no way for auditors to explicitly incorporate subjective opinions into the final judgment. Bayesian statistical models provide a method by which auditors may introduce their professional judgments of particular accounting populations formally into upper error limit calculations and also help deal with the dilemma of low error rates. Proposed modifications to Cox and Snell Bayesian models have yet to be fully tested and formally reported.

## Purpose of the Research

Research Objective 1. The first objective of this research study is to examine robustness at the 90% confidence level for selected modified Cox and Snell upper error limit bounds using study populations with known mean book values, error rates, and error magnitude distributions. For the particular model to be robust, it should, with repetitive sampling, be correct at  $(1 - \alpha) \times 100$  percent of the time for each study population.

Research Objective 2. The second research objective is to examine the bound performance using measurements of coverage and rel tightness. Coverage is the proportion of the time, using repetitive sampling, an upper error limit equals or exceeds the true error in each study population. Rel tightness is a ratio of one conservative bound to another less conservative bound. For the purpose of this research, all modified Cox and Snell bounds will be compared to the unmodified Cox and Snell bounds (the conservative bound). If a bound can be found that has adequate coverage while providing tighter (greater rel tightness) upper error limits than the Stringer bound, then that bound would provide auditors a better tool with which to audit accounting populations.

Research Objective 3. The third objective is to examine the performance of the selected bounds by lowering the nominal confidence level to 85%. By lowering the

confidence level, it may be possible to achieve coverages equal to higher confidence levels but resulting in tighter bounds.

Research Objective 4. The fourth research objective is to incrementally loosen each of the calculated bounds by 5%, 10%, and 20% and then examine the resulting bounds for robustness, coverage, and rel tightness. By increasing the bounds in this manner, it may be possible to create a robust bound.

Research Objective 5. The fifth research objective is to examine the performance characteristic of power in the selected bounds to be tested. The power of a model is the percent of the time, in repetitive sampling, a bound correctly predicts that there is no material error in a given study population. The probability that the point estimate from an upper error limit model equaling the true error in an accounting population is small. An auditor controls the risk (Type I error) that the model does not predict a material error in the population when there actually is a material error by the chosen. In this study, the performance characteristics of robustness and coverage test the possibility of a Type I error. Also important to the auditor and what this research objective will measure is how well a particular bound avoids a Type II error, predicting a material error in the population when the actual error is not material.

## II. METHODOLOGY

### Introduction

This chapter presents the sampling approach, upper error limit models, the accounting and study populations, and the performance measurement procedures for the models. To remain consistent with previous research, notation in this research will be similar to that used by Phillips (1985). Much of the work in this research uses the Stringer and modified Stringer bounds for comparison purposes. The Stringer bound is used in practice, and past research has shown it to be extremely conservative. The main computer program, modified for use in this research, is provided in Appendix A.

### The Sampling Approach

Johnson, Leitch, and Neter (1981) showed that dollar-unit sampling is the most appropriate sampling method to use for accounting populations [7:291]. Dollar-unit sampling, by providing higher book value line items higher probability of being selected in an audit sample, gets more information out of accounting populations than classical sampling methods. Therefore, dollar-unit sampling will be used for this research. In dollar-unit sampling, the sampling unit is the individual dollar. The following steps outline the procedure for implementing a dollar-unit sample. First, the book value of each line item in the accounting population

must be placed into a cumulative list and summed to provide the total reported book value (T). A random sample of the proper size is then selected from the dollars one to T. Each number in the sample refers to a line item in the population. The entire line item to which the sampled dollar belongs is then audited. Lastly, the total error found in an audit unit is prorated proportionately to each dollar in the line item. For this research, a fortran computer program will be modified and used to draw 500 replications of systematic random sample size 200 dollar-units from each of the study populations.

#### Upper Error Limit Bounds

The upper error limit bound is a dollar figure in which an auditor would be confident at the nominal level that the total dollar error in a population would not exceed. Both Bayesian and non-Bayesian upper error methods in their modified form were included in this study. The non-Bayesian method was the modified Stringer bound which was the basis by which the modified Cox and Snell bounds, the Bayesian methods, were compared. The modified upper error methods involve adding dollar errors identified in the dollar-unit samples to the product of the bound's upper error limit and the number of unsampled dollars remaining in the study population. This method eliminates extrapolating probabalistic error limits to the errors in the sampled units and results in less conservative (tighter) upper error limits.

The Stringer Bound. The Stringer method was introduced by Kenneth W. Stringer in 1963 and uses a Poisson approximation to the binomial distribution. The Stringer upper error limit can be broken down into three components: basic precision, most likely error, and precision gap widening. The basic precision (BP) establishes a minimum upper error limit which an auditor would estimate if no errors were found in the sample. Each error found in a sample raises the upper error limit from this minimum using the most likely error and precision gap widening. The most likely error (MLE) is the auditors best estimate of the probable error in the population based on projecting the dollar-unit sample error onto the population [8:1]. Precision Gap Widening (PGW) represents the amount the total precision gap has widened as a result of finding errors in the sample. The sum of each of the components (BP+MLE+PGW) is known as the upper error limit (UEL) factor. Figure 2.1 provides an example of a Stringer upper error limit resulting from finding four errors of 100%, 80%, 40%, and 20% taintings in a sample of 200 dollar-units of a \$1,000,000 population evaluated at the 90% confidence level. For conservatism, it is important to list the errors in descending order by error tainting. This method gives larger value in estimating the upper error limits to the higher taints.

	Factor x Tainting	Average Sampling Interval	Dollar Conclusion	
Basic Precision	2.31	100%	\$5,000	\$11,550
Most Likely Error				
1st error	1.00	100	5,000	5,000
2nd error	1.00	80	5,000	4,000
3rd error	1.00	40	5,000	2,000
4th error	1.00	20	5,000	1,000
Precision Gap Widening				
1st error	0.58	100	5,000	2,900
2nd error	0.44	80	5,000	1,760
3rd error	0.36	40	5,000	720
4th error	0.31	20	5,000	310
Total Upper Error Limit				\$29,0

Figure 2.1 Example of the Stringer Method at the 90% Confidence Level.

Smith (1979) suggested modifying the Stringer method in order to provide a tighter bound. The modification consisted of applying the calculated upper error limit factor to the unsampled line items in the population and then adding the actual dollar error found in the sample to this result. The modified Stringer bound can be expressed as:

$$\text{MSTR} = (T_{\text{yus}}/n)(\text{UEL Factor}) + \sum e_i \quad (1)$$

where

$T_{\text{yus}}$  = the total book value of unsampled line items

$n$  = the sample size

UEL Factor = the same UEL Factor as found in the

unmodified Stringer method

$e_i$  = the dollar value of the error in the  $i$ th  
sample line item in error.

For illustration purposes, if the example in figure 2.1 were such that the total book value of the sampled line items is \$100,000 and the book value of the line item with the 100% taint is \$1,000, the 80% taint is 1,440, the 40% taint is \$840, the 20% taint is \$480, and the sample size is 200 dollar-units, the modified Stringer method could be calculated as follows:

$$\text{MSTR} = (\$900,000/200)(5.848) + \$1,460 = \$27,776$$

As can be seen, the modification to the Stringer bound reduces the upper error limit by \$1,464, thereby tightening the bound in this particular example by 5%.

The Cox and Snell Bound. Cox and Snell (1979) used infinite population theory to develop a Bayesian upper error method. The Cox and Snell bounds are differentiated by the prior parameter selections or settings of the dollar-unit error rate ( $\pi$ ), the mean taint ( $\mu_t$ ), and the prior probability distribution of  $\pi$  (designated as  $\sigma_\pi$ ) and  $\mu_t$  (designated as  $\sigma_\mu$ ). The following calculation is performed in developing an unmodified Cox and Snell upper error limit:

$$\text{UEL}_{\text{CS}} = \left\{ \frac{[m\bar{t} + (b-1)\mu_0]}{[a/\pi_0 + n]} \right\} \left\{ \frac{(m+a)}{(m+b)} \right\} \\ F[(1-\alpha); 2(m+a), 2(m+b)] \quad (2)$$

and

$$\text{CS} = (\text{UEL}_{\text{CS}})(T_y) \quad (3)$$

where

$\pi_0$  = the expected value of the error rate

$a = \pi_0^2 / \sigma_\pi^2$  where  $\sigma_\pi^2$  is the expected value of the variance of the population error rate

$\mu_0$  = the given expected value of the mean taint

$b = (\mu_0^2 / \sigma_\mu^2) + 2$  where  $\sigma_\mu^2$  is the expected value of the variance of the population mean taint

$n$  = the dollar-unit sample size

$m$  = observed number of sample dollar-units in error

$\bar{t}$  = the sample mean taint or simply the sum of the sample taints divided by  $m$

$F[(1-\alpha); 2(m+a), 2(m+b)]$  = the F distribution value at the nominal confidence level of  $(1-\alpha)$  with  $2(m+a)$  and  $2(m+b)$  degrees of freedom in the numerator and denominator respectively

$T_y$  = total population book value

For example, if a sample of 200 dollar-units has four errors with taints of .2, .4, .8, and 1.0 in a \$1,000,000 population, the resulting Cox and Snell upper error bound from prior parameter settings of  $\pi_0$  equals .20,  $\sigma_\pi$  equals .20,  $\mu_0$  equals .40, and  $\sigma_\mu$  equals .20, will be \$31,386 at the 90% nominal confidence level. If another error were found in a sample of the same population with the same taints as the previous example (meaning a taint of .6) and using the same prior parameter settings, the resulting 90% confidence level bound will be \$35,143. Thus, finding an additional error increases the bound by \$3,757. If, in the first example, a different Cox and Snell bound were chosen which

had prior parameter settings of  $\pi_0$  equals .20,  $\sigma_\pi$  equals .20,  $\mu_0$  equals .40, and  $\sigma_\mu$  equals .20, the resulting upper error limit bound at the 90% confidence level would be \$22,280.

The modified Cox and Snell bound is calculated in the same manner as the modified Stringer bound. It is obtained by statistically projecting the upper error limit to the total dollar value of the unsampled line items ( $T_{yus}$ ) then adding the total dollar value of the actual errors found in the sample ( $\sum e_i$ ). The modified Cox and Snell bound can be written as:

$$MCS = (UEL_{cs})(T_{yus}) + \sum e_i \quad (4)$$

If, in the first example given for the unmodified Cox and Snell bound, a modified Cox and Snell bound is calculated and the total dollar value of the sampled line items is \$100,000, then the resulting 90% confidence level bound will be \$29,447. The modification therefore reduced the upper error limit by \$1,939 or tightened the bound by 6.2 percent.

#### Prior Probability Parameter Settings

As previously explained, each Cox and Snell bound is distinguishable by the particular prior probability values for the dollar-unit error rate ( $\pi$ ), the mean taint ( $\mu_t$ ), and the standard deviations of both parameters ( $\sigma_\pi$  and  $\sigma_\mu$ ). The particular bounds to be examined in this study were selected

based upon the results of the Phillips (1985) research in which no modified Cox and Snell bounds were found to be robust. Five modified Cox and Snell bounds, each somewhat looser than the bounds in the Phillips (1985) research, were examined.

Prior expected values for the dollar-unit error rate ( $\pi_0$ ) included in this research were four bounds at .20 and one at .05 with each having the same standard deviation ( $\sigma_\pi$ ) of .20. Prior expected values for the mean taint ( $\mu_0$ ) ranged from small, .05, to medium, .10 and .20, to large, .40. The associated standard deviations ( $\sigma_\mu$ ) were selected to give variability and ranged from .10 to .20. Table 2.1 provides the specific prior expectation parameters for each of the modified Cox and Snell bounds examined in this research. Note that the different bounds are distinguished by A through E. This convention of identification will be maintained throughout this research and in every case refers to the particular probability parameter settings in Table 2.1. In order to accomplish the incremental modifications as specified in research objective 4, for every modified Cox and Snell bound calculated, three more bounds were calculated. The modified Cox and Snell bounds were multiplied by 1.05, 1.10, and 1.20 to provide 5, 10, and 20 percent loosening.

Table 2.1

Prior Probability Parameter Settings  
of Selected Cox and Snell Bounds

Bound	$\pi_0$	$\sigma_\pi$	$\mu_0$	$\sigma_\mu$	a	b
AMCS	.05	.20	.40	.10	.06	18.00
BMCS	.20	.20	.05	.20	1.00	2.06
CMCS	.20	.20	.10	.15	1.00	2.44
DMCS	.20	.20	.20	.20	1.00	3.00
EMCS	.20	.20	.40	.20	1.00	6.00

The Accounting Population

The main accounting population used for this research was acquired from the University of Michigan through Dr. James Godfrey. It consists of 8069 inventory accounts of a major pharmaceutical manufacturer. Account balances of \$100,000 and greater have been deleted on the presumption that they would be audited on a 100% basis in actual practice. Specific characteristics of the accounting population are listed in Table 2.2.

Table 2.2

Descriptive Statistics of  
Accounting Population Book Values

Number of Accounts	8069
Mean	\$1,191.39
Standard Deviation	\$5,739.53
Minimum	\$0.01
Maximum	\$99,328.32
Total	\$9,613,301.00
Variance	14,360,566.76
Skewness	11.4292
Kurtosis	189.927
Coefficient of Variation	3.18

### The Study Populations

In order to maintain a high degree of external validity, the study populations were created with extreme care. As noted previously in the background, Johnson, Leitch, and Neter (1981) found while inventory populations contain both overstatement and understatement errors, the majority of inventory populations still contained significant numbers of overstatement errors. Only overstatement errors were included in the population because the accounting population for this study is an inventory account and Cox and Snell bounds are not designed to deal with understatement errors.

A broad range of mean error rates ( $\pi_0$ ) were selected for this study to provide a rigorous test for the models examined. The six mean error rates are .80 (high), .25 and .10 (medium), and .5, .01, and .005 (low). If a model proves robust (ie, correct approximately  $(1-\alpha) \times 100$  percent of the time) for this range (favorable to unfavorable) of mean error rates, auditors need not be concerned about accurately predicting prior parameters for the accounting population they are auditing. They can be confident at the nominal level that no matter what error rate is encountered in the audited population, the actual error will not exceed the predicted upper error limit provided by the model.

Prior to seeding the population with errors, the population was sorted from low book values to high book

values. The population was then divided into two strata such that the total book values in each stratum were equal (total low book value = total high book value). The low book value accounts were identified as stratum 1 and the high book value accounts were stratum 2.

Four different combinations of mean taints were introduced into the population by strata as shown in Table 2.3. They were selected to provide significant contrasts among the study populations with a range from very high to very low mean taints.

Table 2.3

<u>Mean Taints</u>	
<u>Stratum 1</u>	<u>Stratum 2</u>
.8	.4
.4	.2
.2	.1
.1	.05

Errors were seeded into the population to reflect the findings of Johnson, Leitch, and Neter (1981). First, 10% of all errors in stratum 1 were randomly assigned 100% taints. Second, the other 90% of the errors in stratum 1 and all of the errors in stratum 2 were generated using an exponential distribution with the mean values shown in Table 2.2. In order to make the study populations more realistic, the exponential taint distributions were truncated at 1.0 in accordance with Godfrey and Neter (1984). Thus, (6 mean

error rates x 4 mean error taints) different study populations were created to examine the performance of the bounds. The particular characteristics of each study population are provided in Appendix B.

#### Performance Measurement Procedures

Performance of the modified Cox and Snell bounds was based upon robustness, coverage, rel tightness and power with respect to changes in error rate, mean taint, and error amount intensity. A robust bound must, with repetitive sampling, be correct  $(1 - \alpha) \times 100$  percent of the time for all study populations. Correctness is defined as a calculated upper error limit equaling or exceeding the actual error in the study population. Coverage is the percent of correct bounds out of 500 replications for each study population. The mean rel tightness measure constitutes the degree to which a calculated modified Cox and Snell bound reduced the projected error in a study population as compared to that indicated by the unmodified Cox and Snell bound. That is, with repetitive sampling in a given population, mean rel tightness is the ratio of the mean unmodified Cox and Snell bound to the mean modified Cox and Snell bound and can be written algebraically as

$$\text{Mean Rel Tightness} = (\sum CS_i / MCS_i) / 500$$

where

$CS_i$  = the unmodified Cox and Snell bound for

replication  $i$ ,  
 $MCS_i$  = the modified Cox and Snell bound for  
replication  $i$ , and  
 $i = 1, \dots, 500$ .

For measurement of mean rel tightness for the different nominal confidence level bounds, the conservative bound was the 90 percent nominal confidence level bound and can be written algebraically as

$$\text{Mean Rel Tightness} = (\sum MCS_{90_i} / MCS_{85_i}) / 500$$

where

$MCS_{90}$  = the modified Cox and Snell bound at the 90 percent nominal confidence level for replication  $i$

$MCS_{85}$  = the modified Cox and Snell bound at the 85 percent nominal confidence level for replication  $i$

$i = 1, \dots, 500$ .

In the context of an auditing situation, an auditor generally sets a level of error in a population at or above which the auditor will reject the population as being correct. This level of error is known as the level of materiality or simply the material error. When the true population total error amount is less than materiality and the correct decision is to accept the population, a bound which provides adequate coverage may provide bounds which

equal or exceed the material amount and cause the auditor to make the incorrect decision of rejecting the population. The probability of rejection performance or power of a particular upper error limit bound is determined by the level of materiality selected as criteria for measurement. In order to measure the selected bounds in this research for power, three levels of materiality were selected: five percent, two and one-half percent, and one-tenth of one percent of the total book value. The low materiality level of one-tenth of one percent was selected for accounting populations in which possibly a single high value item missing might be of significance or material. Therefore, for those study populations which do not contain a material error, probability of rejection performance can be measured as the percent of the time, in repetitive sampling, the bound equals or exceeds the selected level of materiality.

#### Analysis of Results

The study populations were sorted in ascending order based on the ratio of total dollar error ( $T_e$ ) to the total population book value ( $T_y$ ). This ratio is known as the error amount intensity (EAI) and can be expressed algebraically as the line item error rate times the mean taint or

$$EAI = T_{LI} \times T_t \quad (5)$$

where

$$T_{LI} = T_Y(e)/T_Y \quad \text{and}$$

$$T_t = T_e/T_Y(e)$$

$T_Y$  = total book value of all line items

$T_Y(e)$  = total book value of line items containing errors

$T_e$  = total population error amount

The study populations were then divided into four EAI categories, low, medium, high, and very high based on "logical breaks" in the EAI range. Table 2.4 identifies the EAI categories and their ranges while Table 2.5 identifies the specific EAI of each study population and the EAI category in which the study population lies. Each bound will be examined over all study populations for its performance in robustness and by each EAI category for its performance in coverage, mean rel tightness, and power.

TABLE 2.4  
 ERROR AMOUNT INTENSITY (EAI)\* CATEGORIES

Category	EAI Range	Number of Study Populations
Low	.00022 - .00170	6
Medium	.00442 - .04039	12
High	.06342 - .12081	4
Very High	.25091 - .37291	2

Total

Table 2.5  
 Study Populations (P) by Error Amount Intensity

Low (6)		Medium (12)		High (4)		Very High	
P	EAI	P	EAI	P	EAI	P	EAI
21	.00022	20	.00442	1	.06342	3	.25091
22	.00067	13	.00457	7	.07626	4	.37291
17	.00083	19	.00562	8	.11360		
23	.00121	9	.00707	2	.12081		
18	.00145	14	.00847				
24	.00170	15	.01364				
		10	.01375				
		16	.02045				
		5	.02177				
		11	.02608				
		12	.03839				
		6	.04039				

\* study population total dollar error as a proportion of total book value

### III. Results and Analysis

#### Introduction

This chapter contains the results of the analysis performed on the data generated from the research. The chapter is presented in the order of the research objectives and devotes a major section of the discussion to each. The first area discussed is bound robustness with respect to all the bounds including the unmodified and modified Stringer and Cox and Snell bounds. The discussion then transitions to mean coverage and mean rel tightness performance measures for each error amount intensity (EAI) category for the unmodified and modified Cox and Snell bounds. Analysis of bound performance when the nominal confidence level is lowered from 90 percent to 85 percent will follow with the discussion of power presented last.

Due to the large number of bounds, the reader needs to understand the bound nomenclature. The unmodified Stringer bounds are STR90 and STR85 meaning the unmodified Stringer bounds at the 90 and 85 percent nominal confidence levels, respectively. The last two numbers in the nomenclature refer to the bound's particular nominal confidence level which is either 90 or 85 percent. As stated in the previous chapter, the Cox and Snell bounds are distinguished by their particular prior probability parameter settings. There are five prior parameter settings (A through E) as identified in

Table 2.1. The unmodified, modified, and incrementally modified Cox and Snell bounds' first letter in the nomenclature will refer to these prior parameter settings. For example, ACS90 refers to the unmodified Cox and Snell bound at the 90 percent nominal confidence level with prior parameter settings of  $\pi_0$  is .05,  $\sigma_\pi$  is .20,  $\mu_0$  is .40, and  $\sigma_\mu$  is .10. AMCS90 refers to the modified Cox and Snell bound at the same nominal confidence level and with the same prior parameter settings. AM1M90 refers to the first incremental increase or 5 percent loosening of the modified Cox and Snell bound at the same nominal confidence level and with the same prior parameter settings. The second incremental increase or 10 percent loosening of the bound is AM2M90 and the third incremental increase or 20 percent loosening of the bound is AM3M90.

#### Measurement of Bound Robustness

The first research objective was to examine the bounds for robustness. A  $(1 - \alpha)$  upper error limit bound is robust if the bound is correct, with repetitive sampling from the population,  $(1 - \alpha) \times 100$  percent of the time. To meet this criterion in this research, the particular bound must attain actual coverage at the nominal confidence level or higher for all study populations.

The unmodified and modified Stringer bounds at both the 90 and the 85 percent nominal confidence levels were robust for all study populations. Table 3.1 presents the actual

mean coverages attained by each of the unmodified and modified Stringer bounds. All are well above the nominal confidence level which provides further evidence of the conservative nature of the Stringer bound. No unmodified or modified Cox and Snell bounds were robust.

Table 3.1  
Mean Coverage of the Stringer Bounds

<u>Bound</u>	<u>Mean Coverage</u>
STR90	.998
MSTR90	.990
STR85	.992
MSTR85	.973

Bound Performance in Coverage and Mean Rel Tightness

The second research objective was to examine bound performance in coverage and mean rel tightness and to identify those bounds which provided adequate mean coverage. Coverage is the percent of the time in repetitive sampling the calculated upper error limit equals or exceeds the actual error in each study population. Mean rel tightness of the modified Cox and Snell bounds was measured with respect to the corresponding unmodified Cox and Snell bound. Although there were no robust unmodified or modified Cox and Snell bounds, some bounds performed adequately in mean coverage for particular error amount intensity (EAI)

categories. Detailed information on each bounds performance in mean coverage and mean rel tightness by EAI category is provided in Appendix C.

Both unmodified Cox and Snell bounds D and E (DCS90 and ECS90) performed well in the low EAI category. These two bounds had adequate coverage for all six of the study populations in this EAI category both with mean coverages of 100 percent. The modified Cox and Snell bounds D and E (DMCS90 and EMCS90) also performed well in the low EAI category. DMCS90 and EMCS90 adequately covered all six study populations in this EAI category both with mean coverages of 100 percent while providing 18.3 percent and 20.7 percent (mean rel tightness measures of 118.3 percent and 120.7 percent) tighter bounds respectively than the unmodified Cox and Snell bounds. This finding indicates that the unmodified Cox and Snell bound performs in a relatively conservative fashion in populations with relatively low error amount intensities since the modified bounds tightened the unmodified bounds by 18.3 percent for the D bound and 20.7 percent for the E bound while not declining in actual mean coverage performance.

While both modified Cox and Snell bounds D and E (DMCS90 and EMCS90) had good mean coverage (100 percent) in the low EAI category, DMCS90 provided bounds which were 133.1 percent (mean rel tightness measure of 233.1 percent) tighter than EMCS90. The difference in the two bounds is in

the mean taint prior probability settings ( $\mu_0$ ). DMCS90 has a  $\mu_0$  of .20 while EMCS90 has a  $\mu_0$  of .40. This indicates that the bounds are very sensitive to the mean taint prior probability parameter settings when dealing with accounting populations with error amount intensities similar to those of the study populations in the low EAI category. Auditors, knowing they are dealing with populations with low EAI, would likely desire the tighter bound, DMCS90, since it provides actual mean coverages equivalent to EMCS90 but resulting in much tighter bounds.

In trying to determine what characteristics of DMCS90 and EMCS90 which made them perform well in the low EAI category, the prior probability parameter settings for the error rate and the mean taint appear to be significant. Figure 3.1 displays the modified Cox and Snell bound and their respective prior probability parameter settings. Bounds D and E are associated with a combination of high mean taint, error rate and distributions for both  $\theta_0$  and  $\theta_1$  relative to bounds A, B, and C. While bound A has a high mean taint, its low prior probability error rate setting may have detrimentally impacted its mean coverage performance. None of the unmodified or modified Cox and Snell bounds provided adequate mean coverage in any of the other three EAI categories (medium, high, or very high).

		$\pi_0$ .05	.20
		$\sigma_\pi$ .20	.20
$\mu_0$	$\sigma_\mu$		
.05	.20		Bound B
.10	.15		Bound C
.20	.20		Bound D
	.20		Bound E
.40	.10	Bound A	

Figure 3.2. Prior Parameter Settings of Selected Cox and Snell Bounds

Bound Performance at the 85 Percent Nominal Confidence Level

The third research objective was to examine the performance of the selected Cox and Snell bounds when the nominal confidence level is reduced from 90 percent to 85 percent. As with the bounds at the 90 percent nominal confidence level, only unmodified and modified Cox and Snell bounds D and E provided adequate coverage in the low EAI category and no bounds provided adequate coverage in any of the three other EAI categories. Table 3.2 presents the actual mean coverages at both nominal confidence levels for unmodified and modified Cox and Snell bounds D and E. Unmodified and modified Cox and Snell bound D (DCS85 and DMCS85) provided acceptable mean coverage for five of the six study populations with low EAI. Both bounds had actual

mean coverages of 91.2 percent with the modified bound (DMCS85) giving 17.6 percent (mean rel tightness measure of 117.6 percent) tighter bounds than the unmodified bound (DCS85). The study population not adequately covered by DCS85 and DMCS85 was study population number which had the highest EAI of the study populations in the low EAI category. Modified Cox and Snell bound D (DMCS85) at the 85 percent nominal confidence level provided actual mean coverages above 91 percent in the low EAI category and provided 23.4 percent (mean rel tightness measure of 123.4 percent) tighter bounds than the same bound at the 90 percent nominal confidence level.

Unmodified and modified Cox and Snell bound E at the 85 percent nominal level (ECS85 and EMCS85) adequately covered all six study populations in the low EAI category and both bounds had actual mean coverages of 100 percent. EMCS85 provided a 20.5 percent (mean rel tightness measure of 1.205) bound than the unmodified Cox and Snell bound (ECS85) at the same nominal confidence level and EMCS85 also tightened the modified Cox and Snell bound at the 90 percent nominal confidence level (EMCS90) by 20.5 percent. This finding is significant because much tighter (20.5 percent) upper error limits may be predicted at the 85 percent nominal confidence level with the same actual confidence levels as with the 90 percent nominal confidence level.

Table 3.2

Actual Mean Coverages of Cox and Snell  
Bounds D and E in the Low EAI Category\*

Nominal Level	Unmodified DCS	Bounds ECS	Modified DMCS	Bounds EMCS
90%	100	100	100	100
85%	91	100	91	100

\* all figures in percent

Although modified Cox and Snell bounds D and E at the 85 percent nominal confidence level performed well above the nominal level in mean coverage, bound D provided much tighter bounds than bound E. In the low EAI category, D bounds were 138.8 percent (mean rel tightness measure of 238.8 percent) tighter than the E bounds. This difference in tightness accounts for the decrease in mean tightness by the D bound. Therefore, if an auditor is dealing with populations known to have low EAI and he or she is willing to accept slightly more risk, then the modified Cox and Snell bound D at the 85 percent nominal confidence level (DMCS85) would be useful.

Bound Performance with the Incremental Modifications

The fourth research objective was to incrementally increase the modified Cox and Snell bounds by 5, 10, and 20 percent in order to possibly improve bound performance.

Since modified Cox and Snell bounds D and E performed well in the low EAI category, the incrementally modified bounds D and E also performed well in coverage. However, even with the third incremental modification (20 percent loosening of the modified Cox and Snell bound) there was no improvement in mean coverage in the low EAI category. The mean rel tightness measure deteriorated steadily for each incremental modification. This was the case for both 90 percent and 85 percent levels of confidence. Therefore, since the incremental modifications in the low EAI category provided no improvement in coverage and was detrimental to mean rel tightness, the incremental modifications to the modified Cox and Snell bounds were not successful in improving the modified Cox and Snell bounds in the low EAI category.

The incremental modifications in the medium and high EAI categories provided no improvement over the modified Cox and Snell bounds. In the very high EAI category, the third incremental modification to modified Cox and Snell bound A (AM3M90 and AM3M85) at both the 90 percent and the 85 percent nominal confidence level provided good mean coverage. These bounds covered both of the two study populations in the very high EAI category at the nominal levels or higher with a mean coverage well above the nominal levels at 94.6 percent and 88.6 percent respectively. These bounds, by loosening the modified Cox and Snell bound by 20 percent, resulted in a mean rel tightness measure looser

than the unmodified Cox and Snell bound with the same prior parameter settings. The 90 percent nominal confidence level bound (AM3M90) provided a mean rel tightness measure of 85.6 percent or 14.6 percent looser than the unmodified Cox and Snell bound. The 85 percent nominal confidence level bound (AM3M85) provided a mean rel tightness measure of 85.3 percent or 14.7 percent looser than the unmodified Cox and Snell bound at the same nominal confidence level. AM3M85 provided bounds which were 2.1 percent (mean rel tightness measure of 102.1 percent) tighter than the 90 percent nominal confidence level bound (AM3M90). Of the five bounds studied, bound A has the highest b value ( $|\mu_0^2/\sigma_\mu^2| + 2$ ) of 18.00 which, combined with the highest incremental modification, may have been the two factors which loosened the bound sufficiently to provide adequate mean coverage.

#### Measurement of Bound Power

The fifth research objective was to measure the probability of a bound rejecting the population when in actuality there was not a material error in the study population. The lowest level of materiality (.1 percent of total book value) was used to test modified Cox and Snell bounds D and E in the low EAI category. At this level of materiality, three study populations (17, 21, and 22) have actual errors intensities less than the material error. Modified Cox and Snell bounds D and E at both the 90 percent and 85 percent nominal confidence levels incorrectly

rejected the study populations 100 percent of the time. Further investigation into the cause for the bounds' high rejection rate revealed that the possibility of a lower limit to the bounds may exist. None of the unmodified or modified Cox and Snell bounds studied in this research could provide an upper error limit anywhere near the .1 percent of the total book value level of materiality; all the bounds were well above this level of materiality. This result indicates that the Cox and Snell bounds in this research may be too conservative for populations with low error amount intensities and where low levels of materiality are important.

#### IV. Summary, Conclusions, and Recommendations For Future Research

##### Summary

The results of this study extend research to find Bayesian approaches for auditing accounting populations. Five Cox and Snell bounds at both the 90 percent and the 85 percent nominal confidence levels and modifications to include known sample errors in bound calculations were examined. Incremental loosening of 5, 10, and 20 percent of each bound was accomplished to seek bound improvements. The power of each Cox and Snell bound found to provide adequate coverage was also tested. Performance of the unmodified and modified Stringer bounds was also tested using the same study populations.

The unmodified and modified Stringer bounds were robust at both confidence levels. Two of the unmodified and modified Cox and Snell bounds, D and E, at both confidence levels had adequate actual mean coverages in the low error amount intensity (EAI) study populations. In the low EAI category, modified Cox and Snell bound D at the 90 percent nominal confidence level provided 18.3 percent while bound E provided 20.7 percent tighter bounds than their corresponding unmodified bounds. Although bounds D and E had similar actual mean coverages, modified Cox and Snell bound D, with a mean taint ( $\mu_0$ ) of .20, provided bounds which were 133

percent tighter than bound E, with a  $\mu_0$  of .40.

At the 85 percent nominal confidence level, actual mean coverages of unmodified and modified Cox and Snell bound D exceeded 90 percent and reached 100 percent with bound E in the low EAI category. However, significant increases in bound tightness were noted for both bounds as the nominal level was decreased from 90 to 85 percent. Modified Cox and Snell bound D had 17.6 percent tighter bounds and modified bound E had 20.5 percent tighter bounds at the lower nominal confidence level. Although the mean coverages of modified Cox and Snell bound D at the 85 percent nominal level were lower than bound E, the increase in mean rel tightness of bound D was significant with 138.8 percent tighter bounds than bound E.

The only bound to provide adequate mean coverage in another EAI category was the third (20 percent) incremental loosening of modified Cox and Snell bound A at both the 90 and 85 percent nominal confidence levels in the high EAI category. This degree of loosening the modified Cox and Snell bound resulted in bounds which were more than 14 percent looser than the unmodified Cox and Snell bound.

With respect to power, no bounds were acceptable at the .1 percent of total book value level of materiality. Even Modified Cox and Snell bound D with its increases in mean rel tightness failed the power test providing 100 percent rejection of populations without a material error. This

finding indicates that even the Cox and Snell bounds examined in this research may be too conservative in low EAI populations.

### Conclusions

Even though the sensitivity of Cox and Snell bounds to their prior probability settings makes prediction of bound behavior difficult, this research has shown that modified Cox and Snell bounds D and E may provide auditors with a better tool with which to audit accounting populations with low error amount intensities than the Stringer bound. In the low EAI these two bounds, D and E, had good mean coverages while providing significant increases in rel tightness.

### Recommendations for Future Research

In this research, mean rel tightness was measured with respect to a more conservative bound. Further research might be done using the actual error in the study population as a basis. Although this method of calculating rel tightness would only be applicable in the laboratory situation where actual errors are known, it may provide a broader basis to compare bounds. Not only could one bound be compared to another for tightness, but the extent of the bound's conservatism is measured directly.

Auditors should consider the implementation of modified Cox and Snell bound D and E in accounting populations with low error amount intensities.

Further research should be done with other modified Cox and Snell bounds to determine those that may provide auditors with better upper error limit bounds.

Appendix A: Fortran Computer Program

```
*****
C
C   Author:  Lt Col J.J. Phillips
C
C   Revised: Capt Blaine F. Webber
C
C*****
C*****
C
C   MAIN PROGRAM
C
C*****
COMMON A(200),BMU(5),API(5),PI(5),TMU(5),B90(200)
COMMON B85(200),N,SKIP,BVARY(9000),AVARY(9000)
COMMON ERRARY(9000),TNTARY(9000),TOTARY(9000)
COMMON JZZ,CS90(5),MCS90(5),MMC190(5),MMC290(5)
COMMON MMC390(5),CS85(5),MCS85(5),MMC185(5),MMC285(5)
COMMON MMC385(5),IM,TOTANT,TBAR,STR90,STR85
COMMON MSTR90,MSTR85,BBVARY(300),INDEX(9000)
COMMON AAVARY(300),EERARY(300),TTNTRY(300)
COMMON IINDEX(300),PGW90,PGW85,BP90,BP85,TTOTRY(300)
COMMON XMLE,TELI,TEDV,TBR,IGY,ISDYPP,TYSKP,TETYY
COMMON SIMPER,BIGER,BIGBV,I,SAMPER,SAMPBV,ITOOT
COMMON TE,NX,M,FN,J,LER(6),TL(4),TH(4),MID,TYE
COMMON RANARY(9000),DSEED,TOT,ME,LE,CNTIT,CNTEM
OPEN(1,FILE='sampl.out ')
CALL FSEEK(1,0,2)
OPEN(4,FILE='bound.dat')
CALL FSEEK(4,0,2)
OPEN(9,FILE='info.out')
CALL FSEEK(9,0,2)
REWIND 1
REWIND 4
REWIND 9
WRITE(9,100)
100  FORMAT(//10X,'BEGIN SIMULATION.....')
CALL INITA
CALL ERRATE
STOP
END
C*****
C
C   Subroutine Errate
C
C*****
COMMON A(200),BMU(5),API(5),PI(5),TMU(5),B90(200)
COMMON B85(200),N,SKIP,BVARY(9000),AVARY(9000)
COMMON ERRARY(9000),TNTARY(9000),TOTARY(9000)
```

```

COMMON JZZ,CS90(5),MCS90(5),MMC190(5),MMC290(5)
COMMON MMC390(5),CS85(5),MCS85(5),MMC185(5),MMC285(5)
COMMON MMC385(5),IM,TOTANT,TBAR,STR90,STR85
COMMON MSTR90,MSTR85,BBVARY(300),INDEX(9000)
COMMON AAVARY(300),EERARY(300),TTNTRY(300)
COMMON IINDEX(300),PGW90,PGW85,BP90,BP85,TTOTRY(300)
COMMON XMLI,TELI,TEDV,TBR,IGY,ISDYPP,TYSKP,TETYY
COMMON SIMPER,BIGER,BIGBV,I,SAMPER,SAMPBV,ITOOT,TYE
COMMON TE,NX,M,FN,J,LERA(6),TL(4),TH(4),MID,CNTIT
COMMON RANARY(9000),DSEED,TOT,ME,LE,CNTEM
INTEGER CNTIT,CNTEM
REAL LERA(6),MID,X(1)
DOUBLE PRECISION DSEED
NR=0
I=0
CNTIT=0
ISDYPP=0
CNTEM=0
M=0
L=0
KK=0
IZZ=0
DSEED=123457.D0

```

C These are the study population line item error rates.

```

LERA(1)= 0.8
LERA(2)= 0.25
LERA(3)= 0.10
LERA(4)= 0.05
LERA(5)= 0.01
LERA(6)= 0.005

```

C These are the study population error taints.

```

TL(1)=.10
TL(2)=.2083
TL(3)=.8131
TL(4)=10.0
TH(1)=.0505
TH(2)=.10
TH(3)=.2083
TH(4)=.8131

```

C Read the actual accounting population values into arrays.

```

Open(unit=8, file='file3',status='old')
REWIND 8
TOTARY(1)=0.0
DO 55 i=1,8069
50 Read(8,*)BV,TOT,IND
   BVARY(I)=BV
   ERRARY(I)=0.0
   TOTARY(I)=totary(I-1)+bvary(i)
   AVARY(I)=0.0
   TNTARY(I)=0.0
   INDEX(I)=I
55 CONTINUE
CLOSE(8)
I = I-1

```

```

C Calculate the midpoint value of the accounting population.
  MID=Totary(I)/2
  K=1
C Calculate the number in the low book value stratum (CNTIT)
C and the number in the high book value stratum (CNTEM).
  57  If(MID.GE.Totary(K))then
      CNTIT=CNTEM+1
      K=K+1
      GO TO 57
  Else
      CNTEM=I-CNTIT
  END IF
C Create the study population by combining 6 error rates
C and 4 error taints.
  Do 2000 LE=1,6
C Call the subroutine to identify the line items with error.
  Call Errlin
C Identify 10 percent of the low book value items to receive
C 100 percent taints.
  IZZ = 0
  DO 500 KM = 1, CNTIT
    IF (RANARY(KM).EQ.0) then
      GO TO 500
    ELSE
      IZZ = IZZ+1
    END IF
  500  Continue
      IZZ = Int(IZZ*0.1)
c This do loop calculates study populations by combining
c each error rate with 4 mean error taints.
  DO 1000 ME=1,4
    KNT=0
    DO 650 KK=1,I
      If(Ranary(KK).NE.0)then
        If(KK.LE.CNTIT)then
          If(KNT.LE.IZZ)then
            AVARY(KK)=2*BVARY(KK)
            KNT=KNT+1
          Else
            550  Call GGUBS(DSEED,1,X)
                  EEXP=-TL(ME)*ALOG(X(1))
                  If(EEXP.GE.1.0)Go to 550
                  AVARY(KK)=BVARY(KK)*(1+EEXP)
            End if
            Go to 630
          Else
            560  Call GGUBS(DSEED,1,X)
                  EEXP=-TH(ME)*ALOG(X(1))
                  If(EEXP.GE.1.0)Go to 560
                  AVARY(KK)=BVARY(KK)*(1+EEXP)
            End if
            Go to 630
          End if
        End if
      End if
    End if
  End do

```

```

        Else
            AVARY(KK)=BVARY(KK)
        End if
630     ERRARY(KK)=AVARY(KK)-BVARY(KK)
        TNTARY(KK)=ERRARY(KK)/BVARY(KK)
650     Continue
        ISDYPP=ISDYPP+1
        Call Info
        CALL STRPOF
        Print*, 'Processing sample ... '
        ERK=TH(ME)
        CALL SAMPL
        Do 900 KL=1, I
            Avary(KL)=0.0
            Errary(KL)=0.0
            Tntary(KL)=0.0
900     Continue
1000    Continue
2000    Continue
        Close(4)
        END
C*****
        Subroutine Errlin
C*****
COMMON A(200), BMU(5), API(5), PI(5), TMU(5), B90(200)
COMMON B&5(200), N, SKIP, BVARY(9000), AVARY(9000)
COMMON ERRARY(9000), TNTARY(9000), TOTARY(9000)
COMMON JZZ, CS90(5), MCS90(5), MMC190(5), MMC290(5)
COMMON MMC390(5), CS85(5), MCS85(5), MMC185(5), MMC285(5)
COMMON MMC385(5), IM, TOTANT, TBAR, STR90, STR85
COMMON MSTR90, MSTR85, BBVARY(300), INDEX(9000)
COMMON AAVARY(300), EERARY(300), TTNTRY(300)
COMMON IINDEX(300), PGW90, PGW85, BP90, BP85, TTOTRY(300)
COMMON XMLI, TELI, TEDV, TBR, IGY, ISDYPP, TYSKP, TETYY
COMMON SIMPER, BIGER, BIGBV, I, SAMPER, SAMPBV, ITOOT, TYE
COMMON TE, NX, M, FN, J, LERA(6), TL(4), TH(4), MID, CNTIT
COMMON RANARY(9000), DSEED, TOT, ME, LE, CNTEM
INTEGER IX(9000), G, NSAMP, NPOP, IP, MPOP, MSAMP, IER
INTEGER CNTIT, CNTEM
REAL LERA(6), POP(1), SAMP(1), MID
DOUBLE PRECISION DSEED
J=0
K=0
KM=0
G=0
NSAMP=0
IP=0
NPOP=I
MPOP=NPOP
DO 5 KL=1, I
    IX(KL)=0
5     CONTINUE

```

```

        Do 10 J=1,I
            Ranary(J)=0.0
    10  Continue
C Calculate the number of line items to be in
C error(LERA(M)).
        NSAMP=I*LERA(LE)
C Call a random number generator which gives you NSAMP
C number of random numbers in array IX.
C Transfer the line items to be in error into array RANARY
    20  Call GGSRS(DSEED,0,NPOP,IP,MPOP,POP,NSAMP,MSAMP,
        * SAMP,IX,IER)
        Do 30 IG=1,NSAMP
            K=IX(IG)
            RANARY(K)=K
    30  Continue
        Return
        End
C*****
C
        SUBROUTINE SAMPL
C
C*****
COMMON A(200),BMU(5),API(5),PI(5),TMU(5),B90(200)
COMMON B85(200),N,SKIP,BVARY(9000),AVARY(9000)
COMMON ERRARY(9000),TNTARY(9000),TOTARY(9000)
COMMON JZZ,CS90(5),MCS90(5),MMC190(5),MMC290(5)
COMMON MMC390(5),CS85(5),MCS85(5),MMC185(5),MMC285(5)
COMMON MMC385(5),IM,TOTANT,TBAR,STR90,STR85
COMMON MSTR90,MSTR85,BBVARY(300),INDEX(9000)
COMMON AAVARY(300),EERARY(300),TNTRY(300)
COMMON IINDEX(300),PGW90,PGW85,BP90,BP85,TTOTRY(300)
COMMON XMLE,TELI,TEDV,TBR,IGY,ISDYPP,TYSKP
COMMON SIMPER,BIGER,BIGBV,I,SAMPER,SAMPBV,ITOOT,TYE
COMMON TE,NX,M,FN,J,LERA(6),TL(4),TH(4),MID,CNTIT
COMMON RANARY(9000),DSEED,TOT,ME,LE,TETYY,CNTEM
REAL MCS90(5),MMC190(5),MMC290(5),MMC390(5),MCS85(5)
REAL MMC185(5),MMC285(5),MMC385(5)
IGY=0
J=0
DO 100 JZZ=1,500
    SAMPBV=BIGBV
    SAMPER=BIGER
    XMLE=0.0
    PGW90=0.0
    PGW85=0.0
    X=0.0
    IM=0
    TOTANT=0.0
    ITOOT=0
    DO 10 ITO=1,200
        A(ITO)=0.00
10  CONTINUE

```

```

TZ=TOT
CALL STEP1
TOT=TZ
IGY=0
DO 20 IK=1,N
  SAMPER=SAMPER+EERARY(IK)
  SAMPBV=SAMPBV+BBVARY(IK)
  IF (TTNTRY(IK).NE.0.0) THEN
    ITOOT=ITOOT+1
    A(ITOOT)=TTNTRY(IK)
  ELSE
    GO TO 20
  END IF
20 CONTINUE
  IF (ITOOT.LE.1) GO TO 50
  CALL SORTA(A,200, ITOOT)
50 CONTINUE
  CALL BOUND1
  CALL BOUND2
  WRITE(4,60) ISDYPP,JZZ,N,TE, LERA(LE),TH(ME)
  WRITE(4,70) IM,TOT,SAMPBV,SAMPER,SIMPER
60 FORMAT(1X,3(I4,2X),3(F12.2,2X))
70 FORMAT(1X,I5,2X,4(F12.2,2X))
  WRITE(4,80)STR90,MSTR90,STR85,MSTR85
  WRITE(4,80)CS90(1),CS90(2),CS90(3),CS90(4),CS90(5)
  WRITE(4,80)MCS90(1),MCS90(2),MCS90(3),MCS90(4),
*   MCS90(5)
  WRITE(4,80)MMC190(1),MMC190(2),MMC190(3),
*   MMC190(4),MMC190(5)
  WRITE(4,80)MMC290(1),MMC290(2),MMC290(3),
*   MMC290(4),MMC290(5)
  WRITE(4,80)MMC390(1),MMC390(2),MMC390(3),
*   MMC390(4),MMC390(5)
  WRITE(4,80)CS85(1),CS85(2),CS85(3),CS85(4),CS85(5)
  WRITE(4,80)MCS85(1),MCS85(2),MCS85(3),MCS85(4),
*   MCS85(5)
  WRITE(4,80)MMC185(1),MMC185(2),MMC185(3),
*   MMC185(4),MMC185(5)
  WRITE(4,80)MMC285(1),MMC285(2),MMC285(3),
*   MMC285(4),MMC285(5)
  WRITE(4,80)MMC385(1),MMC385(2),MMC385(3),
*   MMC385(4),MMC385(5)
80 FORMAT(1X,5(F14.2,2X))
100 CONTINUE
  RETURN
  END

```

C\*\*\*\*\*

C

SUBROUTINE STEP1

C

C\*\*\*\*\*

COMMON A(200),BMU(5),API(5),PI(5),TMU(5),B90(200)

```

COMMON B85(200),N,SKIP,BVARY(9000),AVARY(9000)
COMMON ERRARY(9000),TNTARY(9000),TOTARY(9000)
COMMON JZZ,CS90(5),MCS90(5),MMC190(5),MMC290(5)
COMMON MMC390(5),CS85(5),MCS85(5),MMC185(5),MMC285(5)
COMMON MMC385(5),IM,TOTANT,TBAR,STR90,STR85
COMMON MSTR90,MSTR85,BBVARY(300),INDEX(9000)
COMMON AAVARY(300),EERARY(300),TTNTRY(300)
COMMON IINDEX(300),PGW90,PGW85,BP90,BP85,TTOTRY(300)
COMMON XMLE,TELI,TEDV,TBR,IGY,ISDYPP,TYSKP
COMMON SIMPER,BIGER,BIGBV,I,SAMPER,SAMPBV,ITOOT,TYE
COMMON TE,NX,M,FN,J,LEA(6),TL(4),TH(4),MID,CNTIT
COMMON RANARY(9000),DSEED,TOT,ME,LE,TETYY,CNTEM

```

C

```

REAL X(1)
DOUBLE PRECISION DSEED
14 CALL GGUBS(DSEED,1,X)
IF (X(1).EQ.0.0) GO TO 14
Y=X(1)*SKIP
DO 20 IMY=1,N
    TIJ=Y+(SKIP*(FLOAT(IMY)-1.0))
    CALL SEARCH(TIJ,LINEI)
    IGY=IGY+1
    BBVARY(IGY)=BVARY(LINEI)
    AAVARY(IGY)=AVARY(LINEI)
    EERARY(IGY)=ERRARY(LINEI)
    TTNTRY(IGY)=TNTARY(LINEI)
    TTOTRY(IGY)=TOTARY(LINEI)
    IINDEX(IGY)=INDEX(LINEI)
20 CONTINUE
C WRITE(1,50)JZZ,IGY
C50 FORMAT(10X,'ITERATION= ',I5,' SAMPLE SIZE= ',I5)
C DO 60 IGH=1,IGY
C WRITE(1,80)BBVARY(IGH),AAVARY(IGH),EERARY(IGH),
C * TTNTRY(IGH),TTOTRY(IGH),IINDEX(IGH)
C80 FORMAT(5X,5F12.3,I5)
C60 CONTINUE
RETURN
END

```

C\*\*\*\*\*

C

SUBROUTINE SEARCH(TIJ,LINEI)

C

C\*\*\*\*\*

```

COMMON A(200),BMU(5),API(5),PI(5),TMU(5),B90(200)
COMMON B85(200),N,SKIP,BVARY(9000),AVARY(9000)
COMMON ERRARY(9000),TNTARY(9000),TOTARY(9000)
COMMON JZZ,CS90(5),MCS90(5),MMC190(5),MMC290(5)
COMMON MMC390(5),CS85(5),MCS85(5),MMC185(5),MMC285(5)
COMMON MMC385(5),IM,TOTANT,TBAR,STR90,STR85
COMMON MSTR90,MSTR85,BBVARY(300),INDEX(9000)
COMMON AAVARY(300),EERARY(300),TTNTRY(300)
COMMON IINDEX(300),PGW90,PGW85,BP90,BP85,TTOTRY(300)

```

```

COMMON XMLE,TELI,TEDV,TBR,IGY,ISDYPP,TYSKP
COMMON SIMPER,BIGER,BIGBV,I,SAMPER,SAMPBV,ITOOT,TYE
COMMON TE,NX,M,FN,J,LER(6),TL(4),TH(4),MID,CNTIT
COMMON RANARY(9000),DSEED,TOT,ME,LE,TETYY,CNTEM
INTEGER MAXPT,MINPT,MIDPT
MINPT=1
MAXPT=I
10 MIDPT=(MAXPT-MINPT)/2+MINPT
IF ((MAXPT-MINPT).EQ.1) THEN
    LINEI=MAXPT
    RETURN
ELSE
    IF (TIJ.LE.TOTARY(MIDPT)) THEN
        MAXPT=MIDPT
    ELSE
        MINPT=MIDPT
    END IF
END IF
GO TO 10
END
C*****
C
C      SUBROUTINE SORTA(A,ND,NS)
C
C*****
REAL A(ND),TEMP
INTEGER I,LASTS,LASTI,SSTART
LOGICAL INSORT
SSTART=NS-1
LASTS=1
LASTI=LASTS
INSORT=.FALSE.
10 CONTINUE
IF (.NOT.INSORT) THEN
    INSORT=.TRUE.
    DO 20 I=SSTART,LASTI,-1
        IF (A(I).LT.A(I+1)) THEN
            TEMP=A(I)
            A(I)=A(I+1)
            A(I+1)=TEMP
            INSORT=.FALSE.
            LASTS=I
        END IF
    CONTINUE
    LASTI=LASTS+1
    GO TO 10
END IF
RETURN
END

```

```

C*****
C
      SUBROUTINE STRPOF
C
C*****
      COMMON A(200),BMU(5),API(5),PI(5),TMU(5),B90(200)
      COMMON B85(200),N,SKIP,BVARY(9000),AVARY(9000)
      COMMON ERRARY(9000),TNTARY(9000),TOTARY(9000)
      COMMON JZZ,CS90(5),MCS90(5),MMC190(5),MMC290(5)
      COMMON MMC390(5),CS85(5),MCS85(5),MMC185(5),MMC285(5)
      COMMON MMC385(5),IM,TOTANT,TBAR,STR90,STR85
      COMMON MSTR90,MSTR85,MSTR75,BBVARY(300),INDEX(9000)
      COMMON AAVARY(300),EERARY(300),TTNTRY(300),
      COMMON IINDEX(300),PGW90,PGW85,BP90,BP85TTOTRY(300)
      COMMON XMLI,TELI,TEDV,TBR,IGY,ISDYPP,TYSKP
      COMMON SIMPER,BIGER,BIGBV,I,SAMPER,SAMPBV,ITOOT,TYE
      COMMON TE,NX,M,FN,J,LERA(6),TL(4),TH(4),MID,CNTIT
      COMMON RANARY(9000),DSEED,TOT,ME,LE,TETYY,CNTEM
      N=200
      JJUMP=0
      IJUMP=0
      IBANG=0
      BIGBV=0.0
      IJACK=I
      BIGER=0.0
      SIMPER=0.0
      TYSKP=TOT
33      SKIP=TYSKP/N
      IBANG=0
      DO 10 LIP=1,IJACK
      IF (BVARY(LIP).GT.SKIP) THEN
          J=LIP
          IBANG=1
          GO TO 34
      END IF
10      CONTINUE
      IF (IBANG.EQ.0) GO TO 35
34      DO 20 K=J,IJACK
          IJUMP=IJUMP+1
          JJUMP=JJUMP+1
          BIGBV=BIGBV+BVARY(K)
          BIGER=BIGER+ERRARY(K)
          SIMPER=SIMPER+ERRARY(K)
20      CONTINUE
      TYSKP=TOT-BIGBV
      N=N-JJUMP
      IJACK=I-IJUMP
      JJUMP=0
      IF (IBANG.GT.0) GO TO 33
35      RETURN
      END

```

```

C*****
C
      SUBROUTINE INFO
C
C*****
COMMON A(200),BMU(5),API(5),PI(5),TMU(5),B90(200)
COMMON B85(200),N,SKIP,BVARY(9000),AVARY(9000)
COMMON ERRARY(9000),TNTARY(9000),TOTARY(9000)
COMMON JZZ,CS90(5),MCS90(5),MMC190(5),MMC290(5)
COMMON MMC390(5),CS85(5),MCS85(5),MMC185(5),MMC285(5)
COMMON MMC385(5),IM,TOTANT,TBAR,STR90,STR85
COMMON MSTR90,MSTR85,BBVARY(300),INDEX(9000)
COMMON AAVARY(300),EERARY(300),TTNTRY(300)
COMMON IINDEX(300),PGW90,PGW85,BP90,BP85,TTOTRY(300)
COMMON XMLE,TELI,TEDV,TBR,IGY,ISDYPP,TYSKP
COMMON SIMPER,BIGER,BIGBV,I,SAMPER,SAMPBV,ITOOT,TYE
COMMON TE,NX,M,FN,J,LER(6),TL(4),TH(4),MID,CNTIT
COMMON RANARY(9000),DSEED,TOT,ME,LE,TETYY,CNTEM
NX=0
TE=0.0
TOT=0.0
M=0
TYE=0.0
TELI=0.0
TEDV=0.0
TBR=0.0
TETYY=0.0
DO 1 JACK=1,I
NX=NX+1
TE=TE+ERRARY(JACK)
TOT=TOT+BVARY(JACK)
IF (ERRARY(JACK).NE.0.0) THEN
      M=M+1
      TYE=TYE+BVARY(JACK)
END IF
1 CONTINUE
TELI=FLOAT(M)/FLOAT(NX)
TEDV=TYE/TOT
TBR=TE/TYE
TETYY=TE/TOT
WRITE(9,20) ISDYPP,M,NX,TOT,TYE
WRITE(9,21) TE,TELI,TEDV,TBR,TETYY
20 FORMAT(1X,3(I5,2X),2(F14.4,2X))
21 FORMAT(1X,F14.2,4(F14.6,1X))
RETURN
END
C*****
C
      SUBROUTINE BOUND1
C
C*****
COMMON A(200),BMU(5),API(5),PI(5),TMU(5),B90(200)

```

```

COMMON B85(200),N,SKIP,BVARY(9000),AVARY(9000)
COMMON ERRARY(9000),TNTARY(9000),TOTARY(9000)
COMMON JZZ,CS90(5),MCS90(5),MMC190(5),MMC290(5)
COMMON MMC390(5),CS85(5),MCS85(5),MMC185(5),MMC285(5)
COMMON MMC385(5),IM,TOTANT,TBAR,STR90,STR85
COMMON MSTR90,MSTR85,BBVARY(300),INDEX(9000)
COMMON AAVARY(300),EERARY(300),TTNTRY(300)
COMMON IINDEX(300),PGW90,PGW85,BP90,BP85,TTOTRY(300)
COMMON XMLE,TELI,TEDV,TBR,IGY,ISDYPP,TYSKP
COMMON SIMPER,BIGER,BIGBV,I,SAMPER,SAMPBV,ITOOT,TYE
COMMON TE,NX,M,FN,J,LERA(6),TL(4),TH(4),MID,CNTIT
COMMON RANARY(9000),DSEED,TOT,ME,LE,TETYY,CNTEM
REAL STR90,STR85,MSTR90,MSTR85
BP90=2.31
BP85=1.90
DO 10 IZ=1,N
    XMLE=XMLE+A(IZ)
    PGW90=PGW90+(B90(IZ)*A(IZ))
    PGW85=PGW85+(B85(IZ)*A(IZ))
10 CONTINUE
    FN=FLOAT(N)
    STR90=(BP90+XMLE+PGW90)*TYSKP/FN+SIMPER
    STR85=(BP85+XMLE+PGW85)*TYSKP/FN+SIMPER
    MSTR90=(TOT-SAMPBV)*(BP90+XMLE+PGW90)/FN+SAMPER
    MSTR85=(TOT-SAMPBV)*(BP85+XMLE+PGW85)/FN+SAMPER
    RETURN
    END
C*****
C
SUBROUTINE BOUND2
C
C*****
COMMON A(200),BMU(5),API(5),PI(5),TMU(5),B90(200)
COMMON B85(200),N,SKIP,BVARY(9000),AVARY(9000)
COMMON ERRARY(9000),TNTARY(9000),TOTARY(9000)
COMMON JZZ,CS90(5),MCS90(5),MMC190(5),MMC290(5)
COMMON MMC390(5),CS85(5),MCS85(5),MMC185(5),MMC285(5)
COMMON MMC385(5),IM,TOTANT,TBAR,STR90,STR85
COMMON MSTR90,MSTR85,BBVARY(300),INDEX(9000)
COMMON AAVARY(300),EERARY(300),TTNTRY(300)
COMMON IINDEX(300),PGW90,PGW85,BP90,BP85,TTOTRY(300)
COMMON XMLE,TELI,TEDV,TBR,IGY,ISDYPP,TYSKP
COMMON SIMPER,BIGER,BIGBV,I,SAMPER,SAMPBV,ITOOT,TYE
COMMON TE,NX,M,FN,J,LERA(6),TL(4),TH(4),MID,CNTIT
COMMON RANARY(9000),DSEED,TOT,ME,LE,TETYY,CNTEM
REAL P,D1,D2,X,FIRST(5),MCS90(5),MMC190(5),MMC290(5)
REAL MMC390(5),MCS85(5),MMC185(5),MMC285(5),MMC385(5)
INTEGER IER
FN=FLOAT(N)
DO 12 IW=1,N
    IF (A(IW).GT.0.0) IM=IM+1
    TOTANT=TOTANT+A(IW)

```

```

12 CONTINUE
   IF (IM.EQ.0) THEN
       TBAR=0.0
   ELSE
       TBAR=TOTANT/FLOAT(N)
   END IF
   DO 13 IG=1,5
       FIRST(IG)=(((FLOAT(IM)*TBAR)+
* (BMU(IG)-1)*TMU(IG))/
* ((API(IG)/PI(IG))+FN))*(FLOAT(IM)+API(IG))/
* (FLOAT(IM)+BMU(IG)))
       D1=2*(FLOAT(IM)+API(IG))
       D2=2*(FLOAT(IM)+BMU(IG))
       P=.90
       CALL MDFI (P,D1,D2,X,IER)
       CS90(IG)=FIRST(IG)*X*TYSKP+SIMPER
       MCS90(IG)=FIRST(IG)*X*(TOT-SAMPBV)+SAMPER
       MMC190(IG)=MCS90(IG)*1.05
       MMC290(IG)=MCS90(IG)*1.10
       MMC390(IG)=MCS90(IG)*1.20
       P=.85
       CALL MDFI (P,D1,D2,X,IER)
       CS85(IG)=FIRST(IG)*X*TYSKP+SIMPER
       MCS85(IG)=FIRST(IG)*X*(TOT-SAMPBV)+SAMPER
       MMC185(IG)=MCS85(IG)*1.05
       MMC285(IG)=MCS85(IG)*1.10
       MMC385(IG)=MCS85(IG)*1.20
13 CONTINUE
   RETURN
   END
C*****
C
   SUBROUTINE INITA
C
C*****
COMMON A(200),BMU(5),API(5),PI(5),TMU(5),B90(200)
COMMON B85(200),N,SKIP,BVARY(9000),AVARY(9000)
COMMON ERRARY(9000),TNTARY(9000),TOTARY(9000)
COMMON JZZ,CS90(5),MCS90(5),MMC190(5),MMC290(5)
COMMON MMC390(5),CS85(5),MCS85(5),MMC185(5),MMC285(5)
COMMON MMC385(5),IM,TOTANT,TBAR,STR90,STR85
COMMON MSTR90,MSTR85,BBVAR(300),INDEX(9000)
COMMON AAVARY(300),EERARY(300),TTNTRY(300)
COMMON IINDEX(300),PGW90,PGW85,BP90,BP85,TTOTRY(300)
COMMON XMLI,TELI,TEDV,TBR,IGY,ISDYPP,TYSKP
COMMON SIMPER,BIGER,BIGBV,I,SAMPER,SAMPBV,ITOOT,TYE
COMMON TE,NX,M,FN,J,LER(6),TL(4),TH(4),MID,CNTIT
COMMON RANARY(9000),DSEED,TOT,ME,LE,TETYY,CNTEM
C
   B VALUES
   BMU(1)=18.00
   BMU(2)=2.0625
   BMU(3)=2.4444

```

BMU(4)=3.00  
BMU(5)=6.00  
C A VALUES  
API(1)=.0625  
API(2)=1.00  
API(3)=1.00  
API(4)=1.00  
API(5)=1.00  
C ERROR RATES  
PI(1)=.05  
PI(2)=.20  
PI(3)=.20  
PI(4)=.20  
PI(5)=.20  
C MEAN TAINTS  
TMU(1)=.40  
TMU(2)=.05  
TMU(3)=.10  
TMU(4)=.20  
TMU(5)=.40  
C PRECISION GAP WIDENING VALUES: 90% CONFIDENCE LEVEL  
B90(1)=.58  
B90(2)=.44  
B90(3)=.36  
B90(4)=.31  
B90(5)=.28  
B90(6)=.26  
B90(7)=.  
B90(8)=.22  
B90(9)=.21  
B90(10)=.20  
B90(11)=.19  
B90(12)=.19  
B90(13)=.17  
B90(14)=.17  
B90(15)=.17  
B90(16)=.16  
B90(17)=.15  
B90(18)=.15  
B90(19)=.15  
B90(20)=.14  
B90(21)=.14  
B90(22)=.13  
B90(23)=.14  
B90(24)=.13  
B90(25)=.13  
B90(26)=.14  
B90(27)=.12  
B90(28)=.12  
B90(29)=.12  
B90(30)=.12  
B90(31)=.12

```

B90(32)=.12
B90(33)=.12
B90(34)=.12
B90(35)=.12
B90(36)=.11
B90(37)=.11
B90(38)=.11
B90(39)=.11
DO 210 JC1=40,50
    B90(JC1)=.10
210 CONTINUE
DO 220 JC2=51,59
    B90(JC2)=.09
220 CONTINUE
DO 230 JC3=60,79
    B90(JC3)=.08
230 CONTINUE
DO 0 JC4=80,94
    B90(JC4)=.07
0 CONTINUE
DO 250 JC5=95,110
    B90(JC5)=.06
250 CONTINUE
DO 260 JC6=111,125
    B90(JC6)=.05
260 CONTINUE
DO 270 JC7=126,140
    B90(JC7)=.04
270 CONTINUE
DO 280 JC8=141,155
    B90(JC8)=.03
280 CONTINUE
DO 290 JC9=156,170
    B90(JC9)=.02
290 CONTINUE
DO 300 JC10=171,185
    B90(JC10)=.01
300 CONTINUE
DO 310 JC11=186,200
    B90(JC11)=0.00
310 CONTINUE
C PRECISION GAP WIDENING VALUES: 85% CONFIDENCE LEVEL
B85(1)=.48
B85(2)=.35
B85(3)=.29
B85(4)=.25
B85(5)=.23
B85(6)=.21
B85(7)=.19
B85(8)=.18
B85(9)=.17
B85(10)=.17

```

```

B85(11)=.15
B85(11)=.15
B85(12)=.14
B85(13)=.14
B85(14)=.13
B85(15)=.13
B85(16)=.13
B85(17)=.12
B85(18)=.12
B85(19)=.11
B85(20)=.11
B85(21)=.11
B85(22)=.11
B85(23)=.11
B85( )=.11
B85(25)=.10
B85(26)=.10
B85(27)=.10
B85(28)=.10
B85(29)=.10
DO 110 JA1=30,40
    B85(JA1)=.09
110 CONTINUE
DO 120 JA2=41,49
    B85(JA2)=.08
120 CONTINUE
DO 130 JA3=50,69
    B85(JA3)=.07
130 CONTINUE
DO 140 JA4=70,89
    B85(JA4)=.06
140 CONTINUE
DO 150 JA5=90,105
    B85(JA5)=.05
150 CONTINUE
DO 160 JA6=106,125
    B85(JA6)=.04
160 CONTINUE
DO 170 JA7=126,140
    B85(JA7)=.03
170 CONTINUE
DO 180 JA8=141,155
    B85(JA8)=.02
180 CONTINUE
DO 190 JA9=156,175
    B85(JA9)=.01
190 CONTINUE
DO 200 JA10=176,200
    B85(JA10)=0.00
200 CONTINUE
70 CONTINUE
RETURN
END

```

Appendix B: Study Population Characteristics

Study Pop	ER	L/H Taint	T <sub>LI</sub>	T <sub>t</sub>	Ty(e)	T <sub>e</sub>	EAI
1	.8	.1/.05	.80	.08	7,729,232	609,642	.06432
2	.8	.2/.1	.80	.15	7,729,232	1,161,342	.12081
3	.8	.4/.2	.80	.31	7,729,232	2,412,078	.25091
4	.8	.8/.4	.80	.46	7,729,232	3,584,906	.37291
5	.25	.1/.05	.25	.09	2,363,239	209,322	.02177
6	.25	.2/.1	.25	.16	2,363,239	388,310	.04039
7	.25	.4/.2	.25	.31	2,363,239	733,106	.07626
8	.25	.8/.4	.25	.46	2,363,239	1,092,029	.11360
9	.10	.1/.05	.08	.08	814,558	67,947	.00707
10	.10	.2/.1	.08	.16	814,558	132,154	.01375
11	.10	.4/.2	.08	.31	814,558	250,690	.02608
12	.10	.8/.4	.08	.45	814,558	369,018	.03839
13	.05	.1/.05	.05	.10	458,759	43,952	.00457
14	.05	.2/.1	.05	.18	458,759	81,393	.00847
15	.05	.4/.2	.05	.29	458,759	131,147	.01364
16	.05	.8/.4	.05	.43	458,759	196,598	.02045
17	.01	.1/.05	.02	.05	146,152	7,942	.00083
18	.01	.2/.1	.02	.10	146,152	13,951	.00145
19	.01	.4/.2	.02	.37	146,152	54,009	.00562
20	.01	.8/.4	.02	.29	146,152	42,460	.00442
21	.005	.1/.05	.004	.06	34,431	2,086	.00022
22	.005	.2/.1	.004	.19	34,431	6,433	.00067
23	.005	.4/.2	.004	.34	34,431	11,646	.00121
24	.005	.8/.4	.004	.48	34,431	16,365	.00170

Appendix C: Tables of Bound Results by EAI Category

EAI Category: Low (6 study populations)

Bound: CS90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Number of study populations adequately covered	mean coverage
		.05			.20
			.20		.20
.05	.20			1/6	.167
.10	.15			4/6	.705
.20	.20			6/6	1.00
.40	.20			6/6	1.00
	.10			1/6	.683

Key: Each number grouping represents--  
 study populations adequately covered      mean coverage

EAI Category: Low (6 study populations)

Bound: MCS90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Mean Coverage	Mean Rel Tightness
		.05	.20	1/6 .190	1.089
.05	.20				
				3/6 .668	1.145
.10	.15				
				6/6 1.00	1.183
.20	.20				
				6/6 1.00	1.207
.40	.20				
				0/6 .598	1.201
	.10				

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Low (6 study populations)

Bound: M1M90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Grouping	Mean Coverage
		.05			.20
		.20			.20
.05	.20			1/6	.205
					1.037
.10	.15			3/6	.685
					1.090
.20	.20			6/6	1.00
					1.127
.40	.20			6/6	1.00
					1.150
	.10			0/6	.598
					1.143

Key: Each number grouping represents--

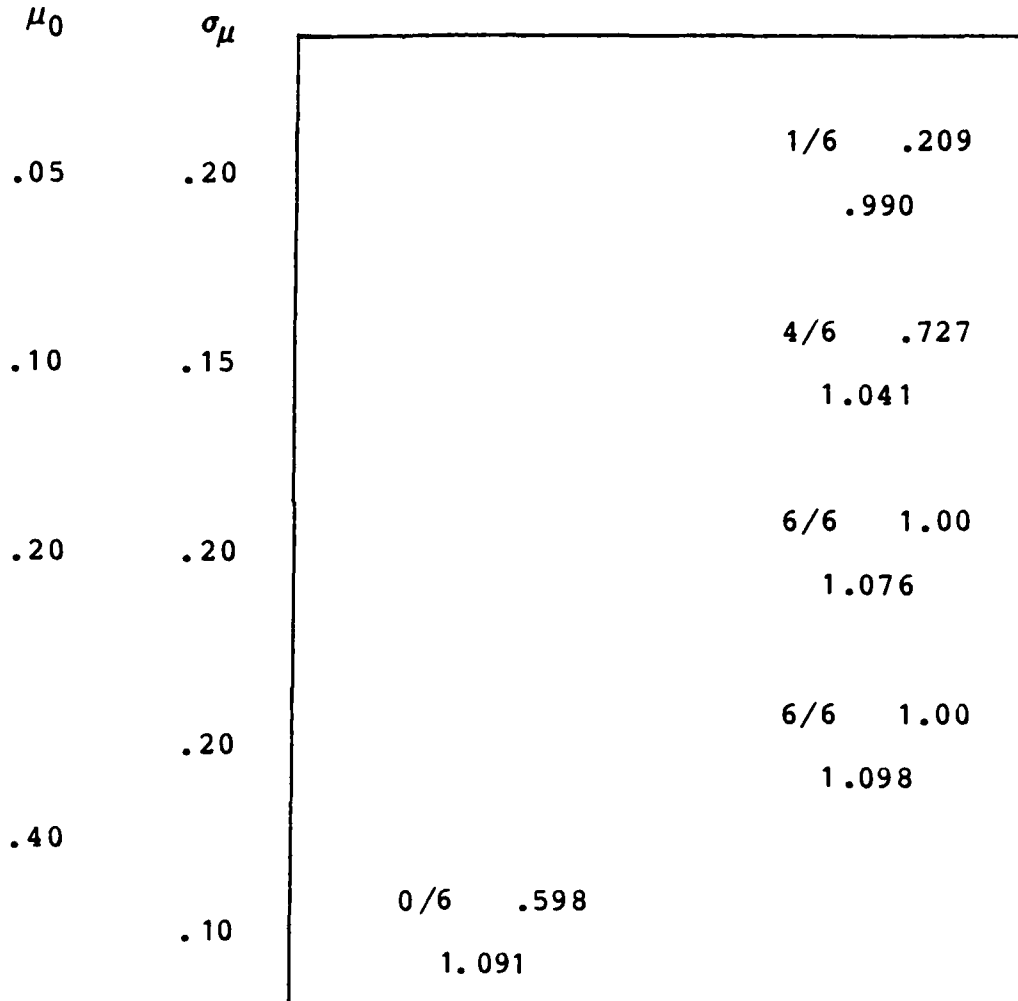
study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Low (6 study populations)

Bound: M2M90

$\pi_0$  .05 .20

$\sigma_\pi$  .20 .20



Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Low (6 study populations)

Bound: M3M90

$\pi_0$  .05 .20

$\sigma_\pi$  .20 .20

$\mu_0$	$\sigma_\mu$		
.05	.20	1/6	.235 .908
.10	.15	4/6	.750 .954
.20	.20	6/6	1.00 .986
.40	.20	6/6	1.00 1.006
	.10	1/6	.683 1.000

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
mean rel tightness wrt unmodified C&S bound

EAI Category: Low (6 study populations)

Bound: CS85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$		
		.05			.20
			.20		.20
.05	.20			1/6	.167
.10	.15			2/6	.595
.20	.20			5/6	.912
	.20			6/6	1.00
.40					
	.10			0/6	.598

Key: Each number grouping represents--  
 study populations adequately covered      mean coverage

EAI Category: Low (6 study populations)

Bound: MCS85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Study Populations Adequately Covered	Mean Coverage	Mean Rel Tightness wrt Unmodified C&S Bound
		.05	.20			
.05	.20			1/6	.187	1.073
.10	.15			1/6	.407	1.133
.20	.20			5/6	.912	1.176
.40	.20			6/6	1.00	1.205
	.10			0/6	.598	1.196

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Low (6 study populations)

Bound: M1M85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Study Populations Adequately Covered	Mean Coverage	Mean Rel Tightness wrt unmodified C&S bound
		.05	.20	1/6	.188	1.022
.05	.20			2/6	.559	1.079
.10	.15			5/6	.912	1.120
.20	.20			6/6	1.00	1.147
.40	.20					
	.10	0/6	.598			1.139

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Low (6 study populations)

Bound: M2M85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Grouping	Mean Coverage
		.05			.20
			.20		.20
.05	.20			1/6	.191
					.975
.10	.15			2/6	.613
					1.030
.20	.20			5/6	.912
					1.069
.40	.20			6/6	1.00
					1.095
	.10			0/6	.598
					1.087

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Low (6 study populations)

Bound: M3M85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Mean Coverage	Mean Rel Tightness
		.05	.20	1/6 .210	.894
.05	.20				
		.10	.15	2/6 .656	.944
.10	.15				
		.20	.20	5/6 .912	.980
.20	.20				
		.40	.20	6/6 1.00	1.004
.40	.20				
		.10	.10	0/6 .598	.997
.10	.10				

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Medium (12 study populations)

Bound: CS90

$\pi_0$  .05 .20

$\sigma_\pi$  .20 .20

$\mu_0$	$\sigma_\mu$		
.05	.20	0/12	.000
.10	.15	0/12	.000
.20	.20	0/12	.073
	.20	5/12	.431
.40	.10	6/12	.729

Key: Each number grouping represents--

study populations adequately covered

mean coverage

EAI Category: Medium (12 study populations)

Bound: MCS90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	
		.05	.20	
		.20	.20	
.05	.20			0/12 .000 .646
.10	.15			0/12 .000 .719
.20	.20			0/12 .038 .832
.40	.20			4/12 .415 1.017
	.10			5/12 .696 1.079

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Medium (12 study populations)

Bound: M1M90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Grouping	Mean Coverage
		.05	.20		
			.20		
.05	.20			0/12	.000
					.587
.10	.15			0/12	.000
					.653
.20	.20			0/12	.077
					.756
	.20			4/12	.437
.40					.924
	.10			6/12	.743
					.981

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Medium (12 study populations)

Bound: M2M90

$\pi_0$  .05 .20

$\sigma_\pi$  .20 .20

$\mu_0$	$\sigma_\mu$		
.05	.20	0/12	.000
			.587
.10	.15	0/12	.001
			.653
.20	.20	0/12	.082
			.756
.40	.20	5/12	.485
			.924
	.10	6/12	.784
			.981

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Medium (12 study populations)

Bound: M3M90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Grouping	Mean Coverage
		.05	.20		
		.20	.20		
.05	.20			0/12	.000
					.538
.10	.15			0/12	.008
					.599
.20	.20			1/12	.110
					.693
	.20			5/12	.566
.40					.847
	.10			7/12	.837
					.899

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Medium (12 study populations)

Bound: CS85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Study Populations Adequately Covered	Mean Coverage
		.05	.20		
		.20	.20		
.05	.20			0/12	.000
.10	.15			0/12	.000
.20	.20			0/12	.015
	.20			4/12	.404
.40	.10			7/12	.657

Key: Each number grouping represents--  
 study populations adequately covered      mean coverage

EAI Category: Medium (12 study populations)

Bound: MCS85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Study Populations Adequately Covered	Mean Coverage
.05	.20	.05	.20	0/12	.000
					.626
.10	.15			0/12	.000
					.697
.20	.20			0/12	.008
					.811
.40	.20			4/12	.400
					1.003
	.10			6/12	.639
					1.069

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Medium (12 study populations)

Bound: M1M85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Grouping	Mean Coverage
		.05	.20		
		.20	.20		
.05	.20			0/12	.000
					.596
.10	.15			0/12	.000
					.663
.20	.20			0/12	.029
					.772
	.20			4/12	.414
					.955
.40					
	.10			6/12	.680
					1.018

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Medium (12 study populations)

Bound: M2M85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Study Populations Adequately Covered	Mean Coverage
		.05	.20	0/12	.000
.05	.20				.569
		.20	.20	0/12	.000
.10	.15				.633
		.20	.20	0/12	.062
.20	.20				.737
		.20	.20	4/12	.432
.40	.20				.912
		.20	.10	7/12	.717
					.972

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Medium (12 study populations)

Bound: M3M85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Study Populations Adequately Covered	Mean Coverage
		.05	.20	0/12	.000
.05	.20				.521
		.20	.20	0/12	.006
.10	.15				.581
		.20	.20	1/12	.082
.20	.20				.676
		.20	.20	4/12	.504
.40	.20				.836
		.20	.10	8/12	.799
	.10				.891

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: High (4 study populations)

Bound: CS90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Mean Coverage
		.05	.20	
			.20	
.05	.20			0/4 .070
.10	.15			0/4 .077
.20	.20			0/4 .094
.40	.20			0/4 .269
	.10			
				2/4 .478

Key: Each number grouping represents--  
 study populations adequately covered      mean coverage

EAI Category: High (4 study populations)

Bound: MCS90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Mean Coverage	Mean Rel Tightness
.05	.20	.05	.20	0/4 .022	.915
.10	.15	.05	.20	0/4 .023	.917
.20	.20	.05	.20	0/4 .034	.924
.40	.20	.05	.20	0/4 .154	.957
	.10	.20	.20	1/4 .425	1.006

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: High (4 study populations)

Bound: M1M90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	mean coverage
		.05	.20	.20
		.20	.20	.20
.05	.20	0/4	.087	.872
.10	.15	0/4	.091	.874
.20	.20	0/4	.109	.880
.40	.20	0/4	.266	.911
	.10	1/4	.475	.958

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: High (4 study populations)

Bound: M2M90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	mean rel tightness wrt unmodified C&S bound	mean coverage
		.05	.20		.20
		.20	.20		.20
.05	.20			0/4	.177
					.832
.10	.15			0/4	.186
					.834
.20	.20			0/4	.200
					.840
	.20			0/4	.359
					.870
.40	.10			2/4	.497
					.915

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: High (4 study populations)

Bound: M3M90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Mean Coverage
		.05	.20	.339
.05	.20			.763
.10	.15			.347
				.764
.20	.20			.375
				.770
.40	.20			.469
				.797
	.10	2/4	.509	
				.839

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: High (4 study populations)

Bound: CS85

		$\pi_0$	.05		.20
		$\sigma\pi$	.20		.20
$\mu_0$	$\sigma\mu$				
.05	.20			0/4	.034
.10	.15			0/4	.036
.20	.20			0/4	.058
	.20			0/4	.205
.40					
	.10		1/4		.456

Key: Each number grouping represents--

study populations adequately covered

mean coverage

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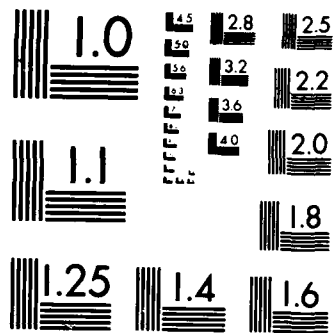
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EAI Category: High (4 study populations)

Bound: MCS85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	mean coverage
		.05	.20	.20
		.20	.20	.20
.05	.20	0/4	.013	.907
.10	.15	0/4	.013	.909
.20	.20	0/4	.018	.916
.40	.20	0/4	.118	.949
	.10	1/4	.397	1.000

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: High (4 study populations)

Bound: M1M85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Mean Coverage
		.05	.20	.20
		.20	.20	.20
.05	.20	0/4	.058	.864
.10	.15	0/4	.062	.866
.20	.20	0/4	.079	.872
.40	.20	0/4	.219	.904
	.10	1/4	.451	.952

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: High (4 study populations)

Bound: M2M85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Grouping	Mean Coverage
		.05	.20		
			.20		
.05	.20			0/4	.128
					.825
.10	.15			0/4	.133
					.827
.20	.20			0/4	.163
					.832
.40	.20			0/4	.315
					.863
	.10			2/4	.488
					.909

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: High (4 study populations)

Bound: M3M85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	
		.05	.20	
		.20	.20	
.05	.20			0/4 .297 .756
.10	.15			0/4 .308 .758
.20	.20			0/4 .330 .763
.40	.20			0/4 .446 .791
	.10			2/4 .505 .833

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Very High (2 study populations)

Bound: CS90

$\pi_0$  .05 .20

$\sigma_\pi$  .20 .20

$\mu_0$	$\sigma_\mu$		
.05	.20	0/2	.062
.10	.15	0/2	.061
.20	.20	0/2	.064
	.20	0/2	.084
.40			
	.10	0/2	.173

Key: Each number grouping represents--  
 study populations adequately covered      mean coverage

EAI Category: Very High (2 study populations)

Bound: MCS90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	0/2	mean coverage
		.05	.20		
.05	.20			0/2	.039
					1.020
.10	.15			0/2	.037
					1.020
.20	.20			0/2	.039
					1.021
.40	.20			0/2	.040
					1.023
	.10			0/2	.067
					1.028

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Very High (2 study populations)

Bound: M1M90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	0/2	mean coverage
		.05	.20		.20
		.20	.20		.20
.05	.20			0/2	.110
					.972
.10	.15			0/2	.108
					.972
.20	.20			0/2	.111
					.972
.40	.20			0/2	.138
					.974
	.10			0/2	.242
					.979

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Very High (2 study populations)

Bound: M2M90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	0/2	mean coverage
		.05	.20		
		.20	.20		
.05	.20			0/2	.320
					.928
.10	.15			0/2	.314
					.927
.20	.20			0/2	.320
					.928
	.20			0/2	.379
.40					.930
	.10			0/2	.546
					.934

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Very High (2 study populations)

Bound: M3M90

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Study Populations Adequately Covered	Mean Coverage	Mean Rel Tightness wrt unmodified C&S bound
		.05	.20	0/2	.795	.850
.05	.20			0/2	.794	.850
.10	.15			0/2	.801	.850
.20	.20			0/2	.852	.852
.40	.20			2/2	.946	.856
	.10					

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Very High (2 study populations)

Bound: CS85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Study Populations Adequately Covered	Mean Coverage
		.05	.20		
		.20	.20		
.05	.20			0/2	.036
.10	.15			0/2	.035
.20	.20			0/2	.035
	.20			0/2	.044
.40	.10			0/2	.097

Key: Each number grouping represents--  
 study populations adequately covered      mean coverage

EAI Category: Very High (2 study populations)

Bound: MCS85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	0/2	mean coverage
		.05	.20		
.05	.20			0/2	.013
					1.016
.10	.15			0/2	.013
					1.016
.20	.20			0/2	.013
					1.016
.40	.20			0/2	.020
					1.018
	.10			0/2	.034
					1.023

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Very High (2 study populations)

Bound: M1M85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Mean Coverage	Mean Rel Tightness
		.05	.20	.20	
		.20	.20	.20	
.05	.20	0/2	.067	.967	
.10	.15	0/2	.067	.967	
.20	.20	0/2	.068	.968	
.40	.20	0/2	.081	.970	
	.10	0/2	.140	.975	

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Very High (2 study populations)

Bound: M2M85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	0/2	mean coverage
		.05	.20		
		.20	.20		
.05	.20			0/2	.214
					.924
.10	.15			0/2	.212
					.923
.20	.20			0/2	.217
					.924
.40	.20			0/2	.263
					.926
	.10			0/2	.402
					.930

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

EAI Category: Very High (2 study populations)

Bound: M3M85

$\mu_0$	$\sigma_\mu$	$\pi_0$	$\sigma_\pi$	Mean Coverage
		.05	.20	.20
		.20	.20	.20
.05	.20	0/2	.699	.847
.10	.15	0/2	.699	.847
.20	.20	0/2	.706	.847
.40	.20	0/2	.771	.849
	.10	2/2	.886	.853

Key: Each number grouping represents--

study populations adequately covered      mean coverage  
 mean rel tightness wrt unmodified C&S bound

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VITA

Captain Blaine F. Webber was born on 7 December 1950 in Hartland, Maine. He grew up on a small farm in St. Albans and graduated from Nokomis Regional High School in 1969. After attending two years of engineering at the University of Maine, he enlisted in the Air Force and spent seven years as a ground radio technician. After receiving his Bachelors of Science Degree from the University of Tampa, Florida, he attended Officer Training School and received his Air Force commission in 1980. His first assignment as an officer was with the Reconnaissance and Electronic Warfare Program Office at Aeronautical Systems Division where he was financial analyst for the B-52 Tail Warning System and the EF-111 Tactical Jamming System. In 1983, Capt Webber was assigned to the 51st Tactical Fighter Wing, Osan AB, South Korea in the Cost and Management Analysis Branch. While at Osan AB, he completed course work for a Master of Arts Degree in Human Relations from Oklahoma University. In May 1985, he entered the School of Systems and Logistics, Air Force Institute of Technology.

Permanent address: 15511 Lakeshore Villas #3  
Tampa, Florida 33612

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The purpose of this research was to examine robustness, mean relative tightness, coverage, and power of selected unmodified and modified Cox and Snell and Stringer error limit bounds. The simulation was performed by repetitive sampling from an accounting population with various known book value and error distributions. Additional modifications to the selected Cox and Snell bounds was done by incrementally loosening the bounds by 5, 10, and 20 percent in a search for bounds with better performance characteristics.

There were several conclusions that could be made from this research. The modified Cox and Snell bounds can achieve high coverages for accounting populations with low error amount intensities (EAI) with significant increases in mean relative tightness over unmodified Cox and Snell bounds. The Stringer and Cox and Snell bounds can still achieve high coverages with significant improvements in mean relative tightness when the nominal confidence level is lowered from 90% to 85%. Only minor changes in prior probability parameter settings materially affect the performance of Cox and Snell bounds. And, in accounting populations with low EAI, the selected Cox and Snell bounds are conservative.

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