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A realistic description of EMP shielding by ferromagnetic materials was developed in this paper. The attenuation of three pulses by a typical ferromagnetic shield is described. Moreover, the form of this description readily allows for the inclusion of specific properties of ferromagnetic materials (e.g., magnetic relaxation, domain structure and magnetostriction) in calculations of shielding effectiveness.					
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Ferromagnetic Mitigation of Electromagnetic Pulse Effects

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CONTENTS

I. BACKGROUND AND MOTIVATION	1
II. THEORETICAL FORMALISM	2
III. RESULTS AND DISCUSSION	7
REFERENCES	14

FERROMAGNETIC MITIGATION OF ELECTROMAGNETIC PULSE EFFECTS

I. BACKGROUND AND MOTIVATION

Electronic equipment in regions up to 2000 miles in diameter can be made inoperative by electromagnetic pulses (EMP) generated during nuclear detonation. The EMP-induced transients produce electromagnetic fields having electric field magnitudes up to 50 kilovolts per meter. Such fields can produce permanent damage or malfunction, particularly to solid state devices. As a result, entire communications systems can be wiped out by a single nuclear burst. Moreover, EMP can produce currents as large as thousands of amperes in space and ground based electronics systems. Such currents, if not attenuated properly, can destroy any semiconductor device.

There are a number of techniques which can be employed for EMP mitigation. These include the use of extension shields, semiconductors (e.g., zener diodes), spark gaps, thermal and electromechanical devices and filters. Unfortunately, none of the presently used devices are adequate for systems requiring fast rise times and simultaneous large power handling capability.

Ferromagnetic shields may provide a solution to the EMP problem. They can be designed to reflect part of the energy and absorb the rest. Parameters associated with these mechanisms are adjustable within very broad ranges by selecting off-the-shelf materials and appropriate device configurations. Moreover, magnetic media specifically tailored for optimizing EMP mitigation should provide even further improvements. These improvements can be accomplished by tailoring parameters such as magnetic permeability, domain switching time, magnetic relaxation, saturation magnetization and electrical conductivity. New

materials like metglass (an amorphous ferromagnetic material) can be employed as a substitute to those used previously.

Earlier work has shown [1] that one can obtain a 42 db enhancement of the EMP shielding factor in off-the-shelf ferromagnetic conductors over that in nonferromagnetic conductors. Alternately, the use of ferromagnetic shielding can reduce the weight by an order of magnitude over that required for nonferromagnetic conductors having the same EMP shielding factor. Although this earlier work clearly demonstrates the utility of ferromagnetic shields devised from off-the-shelf materials, a realistic understanding of the behavior of such shields is indeed lacking. This deficiency is principally due to the nonlinear nature of the problem which led earlier workers [1-5] to analytic solutions which oversimplify the magnetization processes involved. Such oversimplifications include models which assume constant or a limiting value of the magnetic permeability. In contrast, realistic descriptions which incorporate actual material characteristics may be obtained with the use of computer solutions. The present report describes such a computer solution. In our approach, we have developed a theoretical model which allows for the inclusion of magnetic relaxation as well as other physical parameters.

II. THEORETICAL FORMALISM

Assume an electromagnetic pulse (Fig. 1) incident on a thin magnetic film with the geometry of Fig. 2.

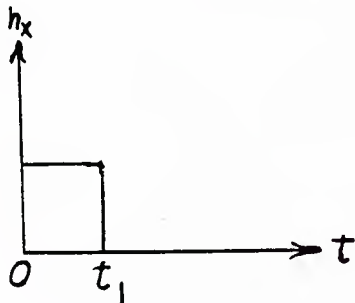


Fig. 1

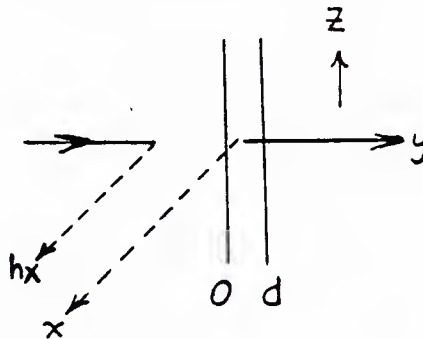


Fig. 2

We then have from Maxwell's equations

$$\nabla \times \vec{e} = -\mu \frac{d\vec{h}}{dt} \quad (1)$$

and

$$\nabla \times \vec{h} = \sigma \vec{e} \quad , \quad (2)$$

where μ and σ are the permeability and conductivity, respectively, of the magnetic film. At this time we also assume that μ is time independent. Using the geometry of Fig. 2 we get

$$\frac{\partial e_z}{\partial y} = -\mu \frac{\partial h_x}{\partial t} \quad (1a)$$

and

$$\frac{\partial h_x}{\partial y} = -\sigma e_z \quad . \quad (2a)$$

Finally, from Eqs. 1a and 2a, we find

$$\frac{\partial^2 h_x}{\partial y^2} = -\sigma \frac{\partial e_z}{\partial y} = \sigma \mu \frac{\partial h_x}{\partial t} = a^2 \frac{\partial h_x}{\partial t} \quad (3)$$

Taking the Laplace Transform of Eq. 3, we get

$$\frac{\partial^2 h_x(s)}{\partial y^2} = a^2 s h_x(s) \quad , \quad (4)$$

whose solution is of the form

$$h_x(s) = A(s) e^{-a \sqrt{s} y} + B(s) e^{a \sqrt{s} y} \quad (5)$$

To solve for A and B, we introduce the boundary conditions for the electric and magnetic fields at $y = 0$ and $y = d$.

$$h_i(t) + h_r(t) = h_x \Big|_{y=0} \quad , \quad (6a)$$

$$z_0 \left[h_i(t) - h_r(t) \right] = - \frac{1}{\sigma} \left. \frac{\partial h_x}{\partial y} \right|_{y=0} = 0, \quad (6b)$$

$$h_t(t - \frac{d}{c}) = h_x \quad y = d, \quad (6c)$$

and

$$z_0 h_t(t - \frac{d}{c}) = - \frac{1}{\sigma} \left. \frac{\partial h_x}{\partial y} \right|_{y=d}, \quad (6d)$$

where z_0 is the free space characteristic impedance. By simple algebraic "manipulations" we obtain

$$h_i(s) = \frac{1}{2} \left[h_x(s) - \frac{1}{z_0 \sigma} \frac{\partial h_x(s)}{\partial y} \right]_{y=0} \quad (7a)$$

and

$$\left[h_x(s) + \frac{1}{z_0 \sigma} \frac{\partial h_x(s)}{\partial y} \right]_{y=d} = 0 \quad (7b)$$

Substituting Eq. (5) into Eqs. (7a) and 7b) we get

$$\begin{aligned} h_x(s) &= h_i(s) \left[\frac{a_{22}(s) e^{-a \sqrt{s} y}}{\Delta(s)} - \frac{a_{21}(s) e^{a \sqrt{s} y}}{\Delta(s)} \right] \\ &= h_i(s) f(s). \end{aligned} \quad (8)$$

This relationship is very much analogous to a relationship found in circuit analysis. We define $f(s)$ as the transfer function of the magneto-conductive medium. We define

$$a_{11}(s) = \frac{1}{2} \left(1 + \frac{a \sqrt{s}}{z_0 \sigma} \right),$$

$$a_{12}(s) = \frac{1}{2} \left(1 - \frac{a \sqrt{s}}{z_0 \sigma} \right),$$

$$a_{21}(s) = e^{-a \sqrt{s} d} \left(1 - \frac{a \sqrt{s}}{z_0 \sigma} \right),$$

$$a_{22}(s) = e^{a \sqrt{s} d} \left(1 + \frac{a \sqrt{s}}{z_0 \sigma} \right),$$

and

$$\Delta(s) = a_{11}(s) a_{22}(s) - a_{12}(s) a_{21}(s).$$

We now wish to put $f(s)$ into a form which can be transformed back into the time domain. Substituting the above definitions into Eq. 8 we obtain, after some manipulations

$$\begin{aligned}
 f(s) &= 2 \sum_{n=0}^{\infty} \frac{(1 - c_1 \sqrt{s})^{2n}}{(1 + c_1 \sqrt{s})^{2n+1}} e^{-\sqrt{s}} (2nc_2 + ay) \\
 &\quad - \sum_{n=0}^{\infty} \frac{(1 - c_1 \sqrt{s})^{2n+1}}{(1 + c_1 \sqrt{s})^{2n+2}} e^{\sqrt{s}} (ay - 2c_2 - 2nc_2) \quad (9) \\
 &\equiv f_1(s) - f_2(s) ,
 \end{aligned}$$

where the summation comes from the expansion of the factor

$$1 - \frac{(1 - c_1 \sqrt{s})^2}{(1 + c_1 \sqrt{s})^2} e^{-2c_2 s} ,$$

which appears in the denominator of an earlier stage. Here we have let

$$c_1 = \frac{a}{z_0 \sigma}$$

and

$$c_2 = ad .$$

Finally, by expanding all the factors containing $\sqrt{s}$, we get

$$f_1(s) = 2 \left[\sum_{n=0}^{\infty} \sum_{m=0}^{2n} \sum_{p=0}^{\infty} \frac{(-1)^{m+p} c_1^{p+m} (2n+p)!}{(2n-m)! m! p!} s^{(p+m)/2} e^{-\sqrt{s}(2nc_2+ay)} \right] \quad (10a)$$

and

$$f_2(s) = 2 \left[\sum_{n=0}^{\infty} \sum_{m=0}^{2n+1} \sum_{p=0}^{\infty} \frac{(-1)^{m+p} c_1^{p+m} (2n+1+p)!}{(2n+1-m)! m! p!} s^{(p+m)/2} e^{-\sqrt{s}(2c_2+2nc_2-ay)} \right] \quad (10b)$$

From reference [6], Table 29.3.87, we have for the Laplace transform

$$\frac{s^{\frac{n-1}{2}}}{e^{-k\sqrt{s}}} = \frac{e^{-\frac{k^2}{4t}}}{2^n \sqrt{\pi t}^{n+1}} H_n\left(\frac{k}{2\sqrt{t}}\right)$$

where H_n is the n^{th} order Hermite Polynomial. Therefore, for the transform of $f(s)$, we have

$$f_1(t) = 2 \left[\sum_{n=0}^{\infty} \sum_{m=0}^{2n} \sum_{p=0}^{\infty} M_1 \frac{e^{-\frac{(2nc_2+ay)^2}{4t}}}{2^{p+m+1} \pi t (p+m+2)} H_{p+m+1}\left(\frac{2nc_2+ay}{2\sqrt{t}}\right) \right] \quad (11a)$$

and

$$f_2(t) = 2 \left[\sum_{n=0}^{\infty} \sum_{m=0}^{2n+1} \sum_{p=0}^{\infty} M_2 \frac{e^{-\frac{(2c_2+2nc_2-ay)^2}{4t}}}{2^{p+m+1} \pi t (p+m+2)} H_{p+m+1}\left(\frac{2c_2+2nc_2-ay}{2\sqrt{t}}\right) \right] \quad (11b)$$

where M_1 and M_2 are the numerical coefficients in Eqs. (10a) and (10b), respectively.

Also, we define

$$f(t) = f_1(t) - f_2(t) .$$

Now, we have to convolute the transfer function, $f(t)$ with the incident pulse to obtain the transmitted pulse, i.e.,

$$h(t) = \int_0^t f(t-\tau) h(\tau) d\tau \quad (12)$$

This completes the derivation.

III. RESULTS AND DISCUSSION

The convolution integral developed in the last section (Eq. 12) has been evaluated for three input pulses (a), a rectangular pulse, (b) a triangular pulse, and (c), a double exponential EMP pulse [7]. Each of these cases will be discussed in detail below following a description of the computer program used to evaluate the convolution integral.

A listing of the computer code is found in the Appendix. It consists of a main program, CONVEMP, and two function subroutines, FLAP and FLAP2. FLAP calculates the transfer function $f(t-\tau)$ and FLAP2 calculates the pulse $h(t)$. There are three versions of FLAP2 listed, one for each of the three pulses mentioned above. In addition to these user subroutines, several library routines are called to evaluate the integral and plot the results. D01AHF is a NAG [8] Library subroutine which integrates the function FLAP2 between the limits TMIN and TB to the relative accuracy EPSR. In our program, FLAP2 calls on FLAP to produce the function $FLAP2 = FLAP2 * FLAP$, and it is the product function which is integrated. The integral is evaluated repeatedly from $t = 0$ until some $t_{\max}$ when the intensity of the attenuated pulse approaches zero. EZXY and ANOTAT are NCAR [9] Library routines which plot K points of the function FP vs. T and are used in our program to plot the results of the above integrations.

A comment is necessary about the summations which appear in Eqs. 10 and 12. Our program does not contain the sum over l and m explicitly, but includes all terms up to $l + m = 1$. (Note that the s -dependent part of Eq. 10, the part that undergoes the transform, is dependent only on the sum $l + m$). Higher terms in the expansion are dependent on higher inverse powers of t and have a small effect near the origin and can be neglected. The sum over n is included explicitly and for most cases there was no significant improvement in increasing n from 10 to 100. However, for certain values of the parameters and at a sufficiently large t there was a small error which could be eliminated by increasing

n to 40. For all the cases discussed below, a value of $n = 10$ was used. Finally, the high precision (REAL*16) used in FLAP was needed because many of the terms are products of factors containing very large exponentials which exceed the range of lower precision variables.

The last step (before discussing the three pulses) is the evaluation of the constants c_1 and c_2 in terms of the material parameters. We list the appropriate definitions and values below:

$$c_1 = \frac{a}{Z_0 \sigma} ,$$

$$c_2 = ad ,$$

$$a = (\sigma \mu_R \mu_0)^{1/2} ,$$

$$Z_0 = (\mu_0 / \epsilon_0)^{1/2} ,$$

$$\mu_0 = 4\pi \times 10^{-9} \text{ henry/cm} ,$$

$$\epsilon_0 = \frac{1}{36\pi} \times 10^{-11} \text{ farad/cm} ,$$

$$\sigma = 5.8 \times 10^5 \text{ mhos/cm} ,$$

$$d = 1.0 \times 10^{-6} \text{ meter} ,$$

$$\mu_R = 500 ,$$

and therefore $c_1 = 0.866366 \times 10^{-8}$

and $c_2 = 1.9090 \times 10^{-4} .$

Furthermore, when $y = d$, the two factors which appear in the exponentials, $2nc_2 + ay$ and $2nc_2 + 2c_2 - ay$, become equal to $(2n + 1)c_2$. This makes both exponentials the same and greatly simplifies the calculation.

A plot of the transfer function appears in Fig. 3. The curve reaches a maximum of 1.48×10^4 at $t = 3.2 \times 10^{-9}$ sec. and falls to 14.6 at $t = 3.0 \times 10^{-8}$ sec.

PULL03

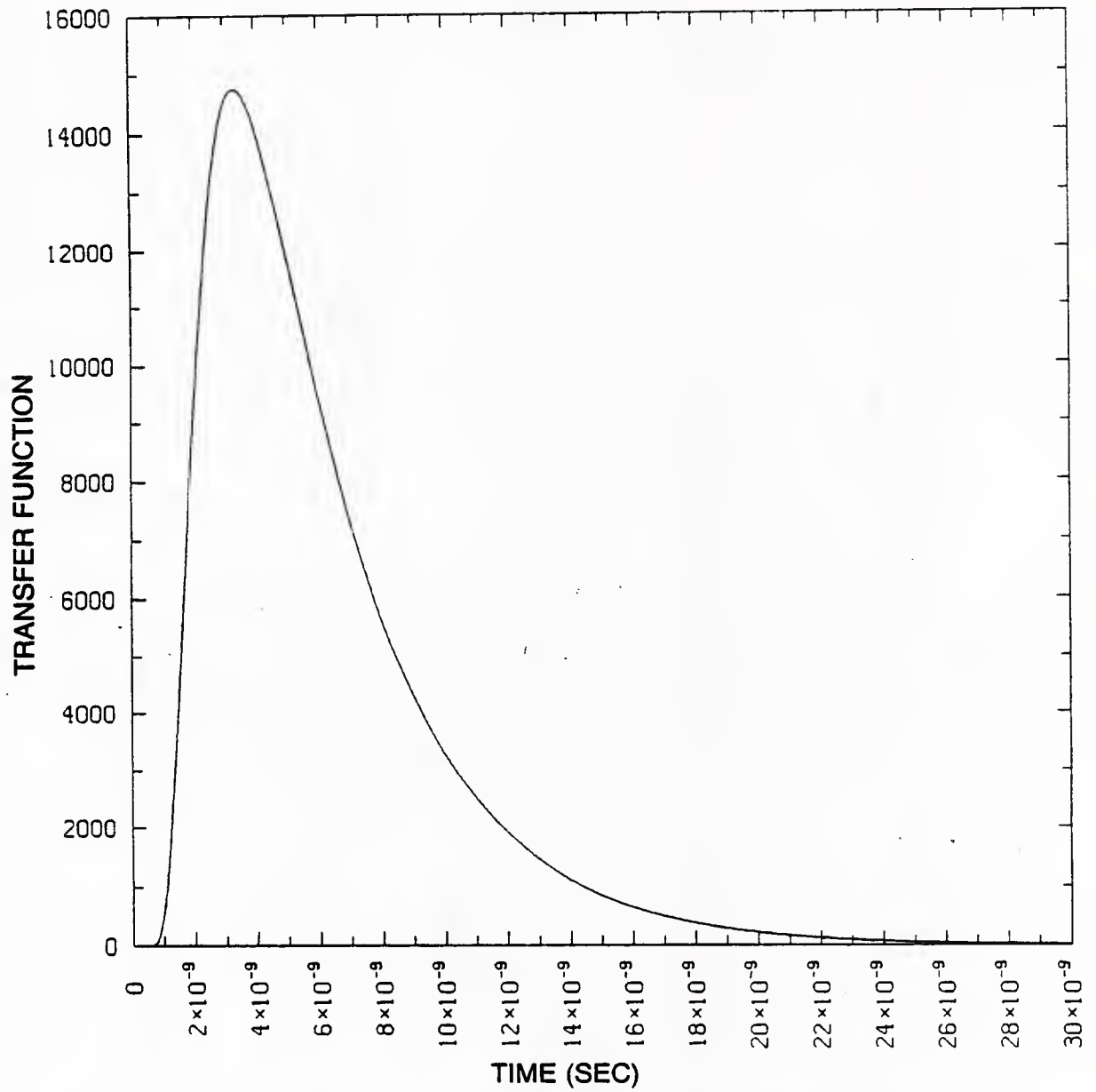


Fig. 3 Plot of Transfer Function vs. Time.

Now let us discuss the three cases. The rectangular and triangular pulses represent simple pulse shapes chosen to check out our program. The EMP pulse (see Eq. 13 below) is one usually used in the literature [7]. The rise time is related to the "unfolding time" of the fission of U^{235} and the decay time is related to the duration of the gamma rays. The widespread use of this curve makes it a suitable choice for the presentation of our calculations.

a) Rectangular Pulse

The incident pulse has the value $h = 1$ for $0 < t < 1.0 \times 10^{-7}$ and $h = 0$ for $t > 1.0 \times 10^{-7}$. Figure 4 shows the attenuated pulse plotted out to $t = 2.0 \times 10^{-7}$. The pulse rises to within one percent of its maximum value of 9.0×10^{-5} at $t = 2.0 \times 10^{-8}$ and falls to 8.0×10^{-7} at $t = 1.2 \times 10^{-7}$.

b) Triangular Pulse

The parameters for the incident pulse are $h = 0$ at $t = 0$, $h = 1.0$ at $t = 1.0 \times 10^{-8}$ and $h = 0$ at $t \geq 1.0 \times 10^{-7}$. Figure 5 shows the attenuated pulse plotted out to $t = 2.0 \times 10^{-7}$. As in the case a) above, the slope of the attenuated curve lags behind that of the incident curve. The pulse rises to a value of 8.25×10^{-5} at $t = 2.0 \times 10^{-8}$ and falls to 3.3×10^{-8} at $t = 1.2 \times 10^{-7}$.

c) EMP Pulse

The incident pulse has the form [7]

$$h = A(e^{-\alpha t} - e^{-\beta t}) \quad (13)$$

with $\alpha = 4.0 \times 10^6$ and $\beta = 476.0 \times 10^6$ (t in seconds). FLAP2 contains a routine to normalize the peak to unity. The maximum occurs at $t = 1.0 \times 10^{-8}$. Figure 6 shows the attenuated pulse plotted out to $t = 1.0 \times 10^{-6}$. The pulse rises to 8.8×10^{-5} at $t = 2.5 \times 10^{-8}$ and falls to 1.6×10^{-6} at $t = 1.0 \times 10^{-6}$.

C0PL01

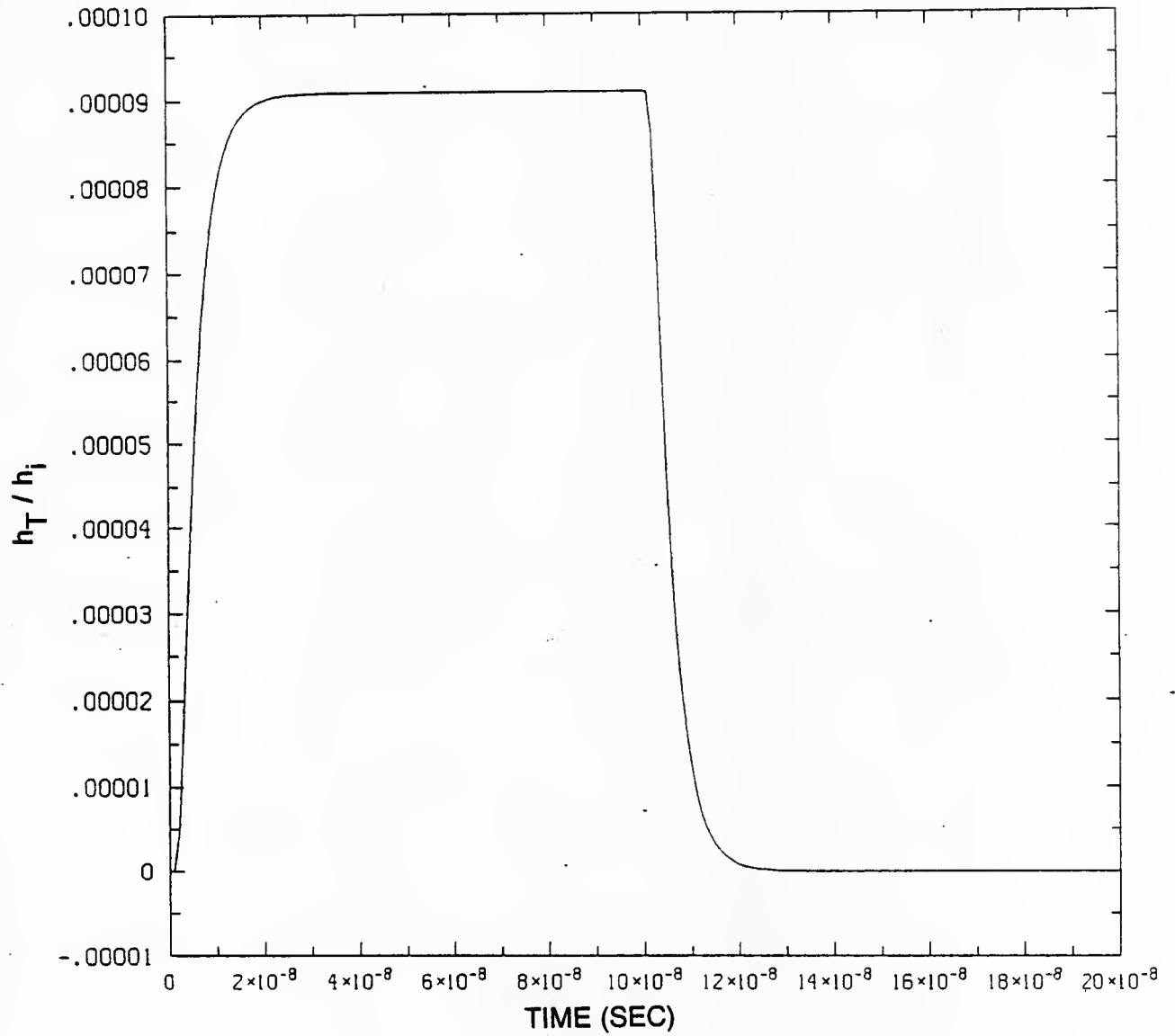


Fig. 4 Plot of h_T/h_i vs. Time for a Rectangular Pulse having an amplitude of 1 for $0 \leq T \leq 1.0 \times 10^{-7}$ sec. and 0 for $T > 1.0 \times 10^{-7}$ sec.

C0PL02

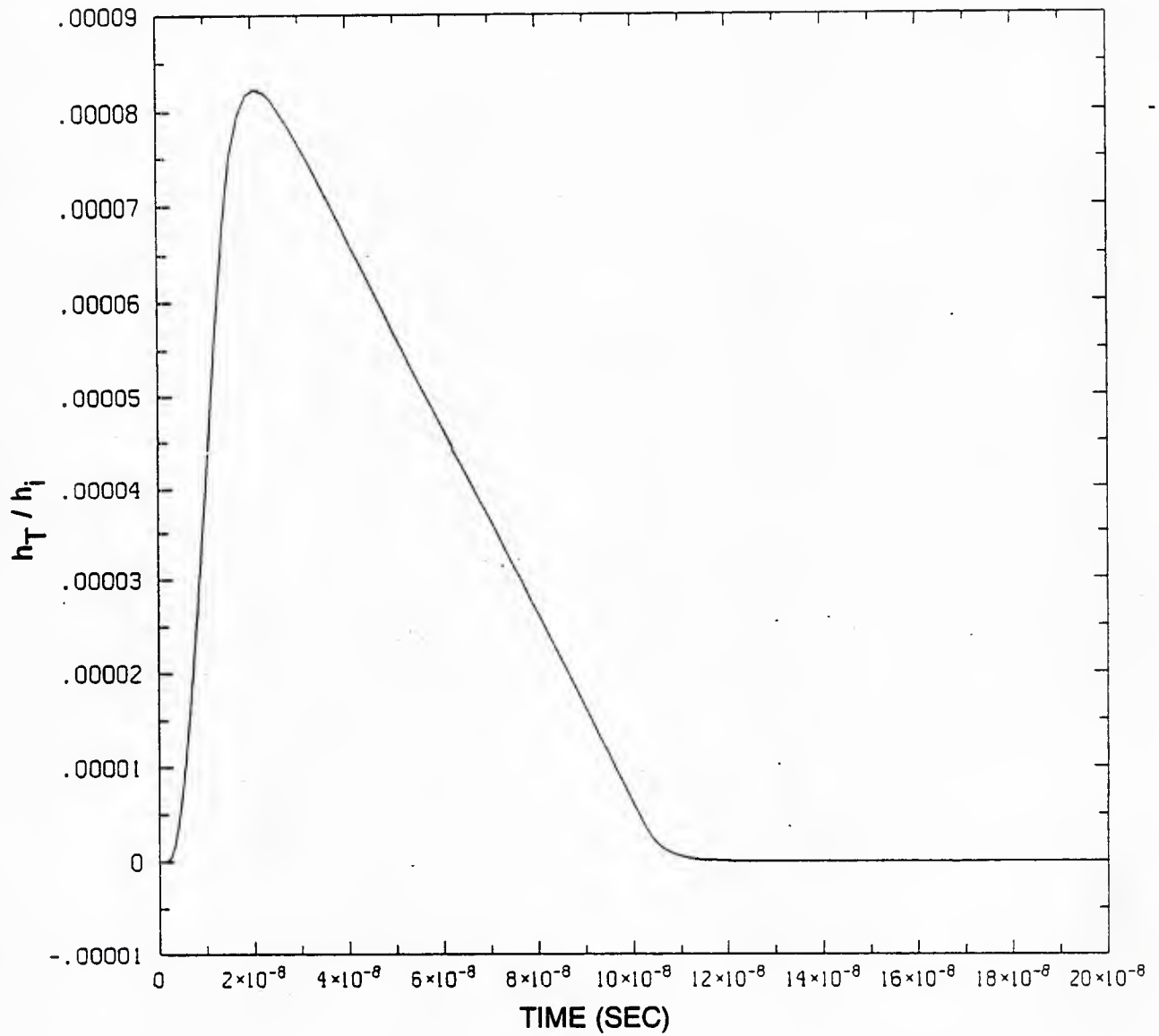


Fig. 5 Plot of h_T/h_i vs. Time for a Triangular Pulse having an amplitude of 1 for $T = 1.0 \times 10^{-8}$ sec. and 0 at $T = 0$ and $T > 1.0 \times 10^{-7}$ sec.

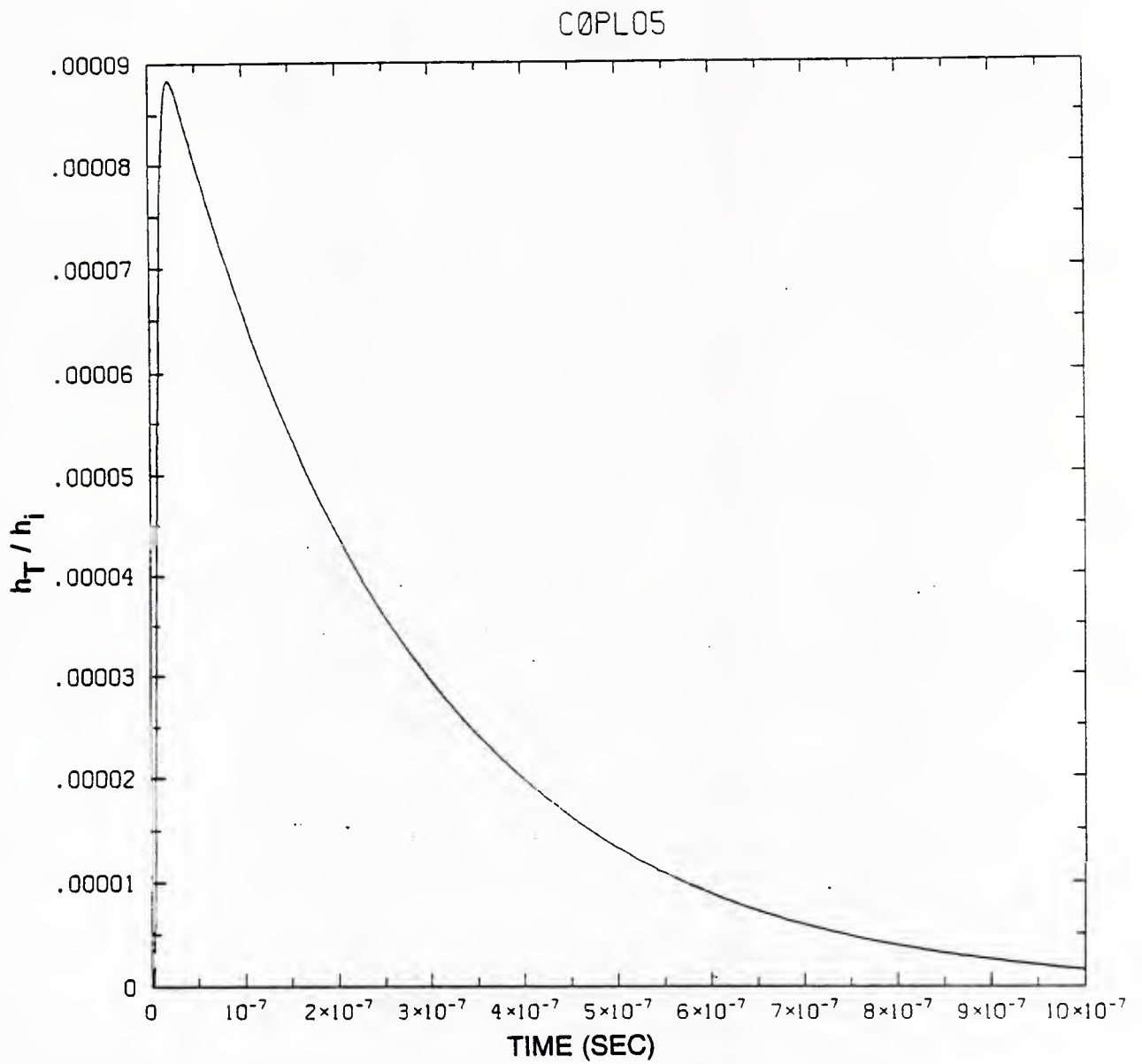


Fig. 6 Plot of h_T/h_i vs. Time for a pulse having the form $h_i = A(e^{-\alpha T} - e^{-\beta T})$ with $\alpha = 4.0 \times 10^6$, $\beta = 476.0 \times 10^6$ and A chosen so that $h_{\max} = 1$.

In all of these examples the transmitted pulse is not only attenuated but delayed and distorted. This is most easily seen in the transfer function itself, which shows the transmission of a delta function input pulse. The distortion results from the progressively greater attenuation of higher frequency components in the signal. The large attenuations obtained result primarily from reflection at the front surface, so that even very thin material can be an effective shield against radiation fields. With the method of calculation used, any influence of the back surface on this reflection is included.

As shown here, we have developed a realistic description of EMP shielding by ferromagnetic materials, including the attenuation of three pulses by a typical ferromagnetic shield. Moreover, the form of this description readily allows for the inclusion of specific properties of ferromagnetic materials (e.g., magnetic relaxation, domain structure and magnetostriction) in calculations of shielding effectiveness.

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```

PROGRAM CONVEMP
CHARACTER IDENT*8,YN*1,DUM*1
DIMENSION FP(2001),T(2001),DT(3),XLAB(2),IW(102),TN(10),NPI(10)
REAL*8 Y,Y0,FLAP2,D01AHF,EPSABS,EPSREL,ABSERR,W(800),TMIN,TI,
1FL(10),EPSR,RELERR,TB
REAL*16 PI,PIR2,XM1,F0
EXTERNAL FLAP2
COMMON /FBLK/C1,C2,PIR2,ALPHA,F0,NMAX,/FBLK3/TMIN,TI,FL12,
1NI,NPI,TN,FL,NF
DATA C1/8.8637E-9/,C2/1.9090E-4/,XLAB/'TIME','S',YLAB/'F','S'/
CALL DATE(DT)
TYPE*,'C1 = ',C1,' C2 = ',C2
5 TYPE*,'RUN IDENTIFICATION (FILENAME)?'
IDENT=' '
ACCEPT 135,IDENT
C EXPANSION OF DENOMINATOR
TYPE*,'HIGHEST VALUE OF N IN SUMMATION?'
ACCEPT*,NMAX
TYPE*,' INPUT FOR FLAP2'
NF=0
C ACCEPT INPUT FROM PULSE SUBROUTINE
Y0=FLAP2(0.)
PRINT 100,CHAR(27),CHAR(15)
PRINT 105,DT
PRINT 145,IDENT
PRINT 160,NI
PRINT 115,NMAX
NF=-1
C PRINT INPUT FROM PULSE SUBROUTINE
Y0=FLAP2(0.)
PRINT 130,CHAR(12),CHAR(18),CHAR(27)
NP=0
TYPE*,'SUPPRESS PRINTING (Y/N)?'
ACCEPT 140,YN
IF(YN.EQ.'Y') NP=1
TMAX=TMAX*1.E-6
IDENT(7:7)='S'
XM1=-1.
PI=QACOS(XM1)
PIR2=SQRT(PI)
T(1)=0.
IPT=IMAX+1
Y=0.
FP(1)=0.
EPSR=1.E-5
TMIN=0.
NLIMIT=0
IFAIL=0
IT1=1
T00=0.
IIT=0

```

```

C EVALUATE CONVOLUTION INTEGRAL AT POINT TI IN INTEGRATION REGION I
C NEXT I
    DO 20 I=1,NI
        T0=(TN(I+1)-TN(I))/NPI(I)
        IPT=NPI(I)+1
        IF(I.GT.1) IIT=IIT+NPI(I-1)
C NEXT TI
    DO 20 IT=2,IPT
        TI=TN(I)+T0*(IT-1)
        K=IIT+IT
        T(K)=TI
        ALPHA=-C2
        Y=0.
        NCJ=0
C PERFORM INTEGRATION OVER EACH INTEGRATION REGION J UP TO POINT TI
    DO 30 J=1,NI
        NF=J
        IF(NCJ.EQ.1) GO TO 30
        IF(FL(J+1).LT.0.) GO TO 30
        TMIN=TN(J)
        TB=TN(J+1)
        IF(TI.LE.TN(J+1)) THEN
            TB=TI
            NCJ=1
        ENDIF
        TYPE*,T0,TN(I),TI,TB
C NAG INTEGRATION ROUTINE
        Y0= D01AHF(TMIN,TB,EPSR,NPTS,RELERR,FLAP2,NLIMIT,IFAIL)
        Y=Y+Y0
30    CONTINUE
20    FP(K)=Y
C NCAR PLOTTING ROUTINES
        CALL ANOTAT(XLAB,YLAB,1,0,0,%REF(DUM))
        CALL EZXY(T,FP,K,%REF(IDENT))
        IF(NP.EQ.0) THEN
            PRINT 100,CHAR(27),CHAR(15)
            PRINT 120
C PRINT OUTPUT AT SELECTED POINTS ONLY
            DO 10 J=1,K,10
                IF(J.EQ.1)GO TO 10
                IF(MOD((J-1),40).EQ.0) PRINT 125,(T(I),FP(I),I=(J-30),J,10)
10            CONTINUE
                PRINT 130,CHAR(12),CHAR(18),CHAR(27)
                ENDIF
                TYPE*, 'ENTER ANOTHER SET OF DATA (Y/N)?'
                ACCEPT 140,YN
                IF(YN.EQ.'Y') GO TO 5
100           FORMAT(1X,A1,'[5i',A1)
105           FORMAT(' DATE = '2A4,A1)
115           FORMAT(' LAST TERM IN EXPANSION, N = ',I5)
120           FORMAT(5X,4(4X,'TIME',10X,'FCONV',7X))

```

```

125  FORMAT(5X,4(E12.4,2X,E14.5,2X))
130  FORMAT(1X,3A1,'[4i')
135  FORMAT(A8)
140  FORMAT(A1)
145  FORMAT(1X,A8)
160  FORMAT(' NO. OF INTEGRATION REGIONS = ',I5)
      STOP
      END

```

C THIS ROUTINE CALCULATES THE TRANSFER FUNCTION

```

      REAL*8 FUNCTION FLAP(TAU)
      REAL*16 CK1,X1,EX1,F,F1,F2,F3,F10,F1S,F2S,F3S,PIR2
      REAL*8 TI,FLAP2,TAU,TI0,TMIN
      COMMON /FBLK/C1,C2,PIR2,ALPHA,F,NMAX,/FBLK2/X1,EX1,CK1,F1S,F2S,F3S,
1/FBLK3/TMIN,TI0
      TI=TI0-TAU
      IF((TI**2).EQ.0..OR.TI.LT.0.) THEN
      FLAP=0.
      RETURN
      ENDIF
      F=0.
      F1S=0.
      F2S=0.
      F3S=0.
      CK1=1./(PIR2*TI**1.5)
      ALPHA=-C2
      DO 10 N=0,NMAX
      ALPHA=ALPHA+2.*C2
      ALPHA2=ALPHA*ALPHA
      X1=ALPHA2/(4.*TI)
      EX1=EXP(-X1)
      F10=C1*CK1*EX1
      F1=-2.*F10
      F2=C2*F10*(C2+6*C1)*(2*N+1)**2/TI
      F3=-C1*C2**3*F10*(2*N+1)**4/TI**2
      F=F+F1+F2+F3
      F1S=F1S+F1
      F2S=F2S+F2
      F3S=F3S+F3
10  CONTINUE
      FLAP=F
      RETURN
      END

```

```

C THIS ROUTINE GENERATES A RECTANGULAR PULSE
  REAL*8 FUNCTION FLAP2(TAU)
  REAL*8 TAU,TB,T,FL(10),TMIN,FLAP
  DIMENSION TN(10),NPI(10)
  COMMON /FBLK3/TMIN,TB,FL12,NI,NPI,TN,FL,NF
  DATA TN(1)/0./,FL(1)/1./
C INPUT PULSE PARAMETERS
  IF(NF.EQ.0) THEN
    TYPE*,'NUMBER OF INTEGRATION REGIONS?'
    ACCEPT*,NI
    TYPE*,'FOR EACH REGION, NUMBER OF POINTS, VALUE OF FUNCTION,
1AND END POINT?'
    DO 10,I=1,NI
      TYPE*,'REGION NO. 'I
      ACCEPT*,NPI(I),FL(I+1),TN(I+1)
10    TN(I+1)=TN(I+1)*1.E-6
      RETURN
    ENDIF
C PRINT PULSE PARAMETERS
  IF(NF.EQ.-1) THEN
    PRINT 110
    PRINT 115,(NPI(I),TN(I+1),FL(I+1),I=1,NI)
    RETURN
    ENDIF
C CALCULATE PULSE
  FLAP2=FL(2)
  FL12=FLAP2
  FLAP2=FLAP2*FLAP(TAU)
110  FORMAT(2X,'NPTS',4X,'TMAX',9X,'FL')
115  FORMAT(1X,I5,2E12.3)
  RETURN
  END

C THIS ROUTINE GENERATES A TRIANGULAR PULSE
  REAL*8 FUNCTION FLAP2(TAU)
  REAL*8 TAU,TB,T,FL(10),TMIN,FLAP
  DIMENSION TN(10),NPI(10)
  COMMON /FBLK3/TMIN,TB,FL12,NI,NPI,TN,FL,NF
  DATA TN(1)/0./,FL(1)/1./
C INPUT PULSE PARAMETERS
  IF(NF.EQ.0) THEN
    TYPE*,'NUMBER OF INTEGRATION REGIONS?'
    ACCEPT*,NI
    TYPE*,'FOR EACH REGION-NUMBER OF POINTS,VALUE OF FUNCTION,
1AND END POINT(MICROSECONDS)?'
    DO 5,I=1,NI
      TYPE*,'REGION NO. 'I
      ACCEPT*,NPI(I),FL(I+1),TN(I+1)
5    TN(I+1)=TN(I+1)*1.E-6
      RETURN
    ENDIF

```

```

C PRINT PULSE PARAMETERS
  IF(NF.EQ.-1) THEN
    PRINT 110
    PRINT 115,(NPI(I),TN(I+1),FL(I+1),I=1,NI)
    RETURN
  ENDIF
C CALCULATE PULSE AT POINT TAU IN REGION NF
  GO TO (10,20) NF
10  A1=FL(2)/TN(2)
    FLAP2=A1*TAU
    FL12=FLAP2
    FLAP2=FLAP2*FLAP(TAU)
    RETURN
20  DELT=TN(3)-TN(2)
    A2=-FL(2)/DELT
    B2=FL(2)*TN(3)/DELT
    FLAP2=A2*TAU+B2
    FL12=FLAP2
    FLAP2=FLAP2*FLAP(TAU)
110  FORMAT(2X,'NPTS',4X,'TMAX',9X,'FL')
115  FORMAT(1X,I5,2E12.3)
    RETURN
  END

C THIS ROUTINE GENERATES A DOUBLE EXPONENTIAL EMP PULSE
  REAL*8 FUNCTION FLAP2(TAU)
  REAL*8 TAU,TB,T,FL(10),TMIN,FLAP,GAMMA,GAMMA1,EX,C1,A
  DIMENSION TN(10),NPI(10)
  COMMON /FBLK3/TMIN,TB,FL12,NI,NPI,TN,FL,NF
  DATA TN(1)/0./,TN(2)/1.E-8/,TN(3)/1.E-7/,NI/3/,A0/1./
  SAVE A
C INPUT PULSE PARAMETERS
  IF(NF.EQ.0) THEN
    TYPE*, 'NUMBER OF POINTS, END POINT (MICROSECONDS)?'
    ACCEPT*,NPI(4),TN(4)
    TN(4)=TN(4)*1.E-6
    TYPE*, 'ALPHA, BETA?'
    ACCEPT*,FL(1),FL(2)
    DO 10,I=1,2
10   FL(I)=FL(I)*1.E6
    NPI(1)=25*NPI(4)/100
    NPI(2)=NPI(1)
    NPI(3)=2*NPI(1)
C NORMALIZE CURVE TO A0
    GAMMA=FL(2)/FL(1)
    GAMMA1=GAMMA-1
    TMAX=LOG(GAMMA)/(FL(1)*GAMMA1)
    EX=1.+1./GAMMA1
    C1=GAMMA1/GAMMA**EX
    A=A0/C1
    RETURN
  ENDIF

```

```

C PRINT PULSE PARAMETERS
  IF(NF.EQ.-1) THEN
    PRINT 105,NPI(4),TN(2)
    PRINT 100,FL(1),FL(2)
    PRINT 110,C1,TMAX
    RETURN
  ENDIF
C CALCULATE PULSE AT POINT TAU
  FLAP2=A*(EXP(-FL(1)*TAU)-EXP(-FL(2)*TAU))
  FL12=FLAP2
  FLAP2=FLAP2*FLAP(TAU)
100  FORMAT(' ALPHA = ',E12.3,' BETA = ',E12.3)
105  FORMAT(' NPTS = ',I5,' T = ',E12.3)
110  FORMAT(' E(MAX)/A = ',F7.5,' TMAX = ',E12.3)
    RETURN
  END

```

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