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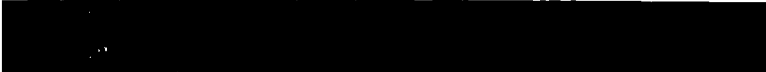
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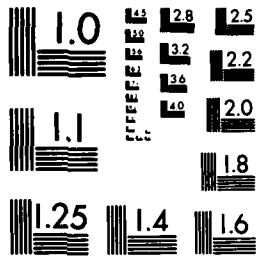
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REPORT

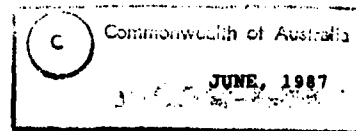
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EFFICIENCY ASPECTS OF SHORT, LOW
VELOCITY RAILGUNS

C. I. Sach

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MATERIALS RESEARCH LABORATORIES

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C. I. Sach



ABSTRACT

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The factors controlling the performance of short, low velocity railguns are studied and mathematical expressions defining the bounds of realizable efficiencies are obtained. The restrictions governing the validity of the expressions are discussed. The expressions are based on the proposition that during acceleration of the projectile in the railgun, the current falls almost linearly with time. Under the conditions discussed in this report it is shown that the maximum achievable efficiency is about 1.6%.

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SYMBOLS

C	primary storage capacitance
L_0	intermediate storage inductance
R_C	circuit resistance in pre-crowbar phase
R_1	incremental resistance of crowbar switch
R_2	incremental resistance of plasma armature
R_V	circuit resistance during post-crowbar phase
R_T	total effective resistance post-crowbar
R'	resistance per unit length of railgun
L'	inductance per unit length of railgun
V_1	total voltage across crowbar switch
V_2	total voltage across plasma armature
V_3	total voltage across main switch
E_1	basic (constant) breakdown potential, crowbar
E_2	basic (constant) breakdown potential, armature
I	circuit current
I_0	initial maximum current
I_E	effective current $(E_1 + E_2)/R_T$
I_M	current in ideal railgun at shot-out
I_1	second current maximum in uncrowbarred gun
x	position co-ordinate of projectile in barrel
l	length of barrel
v	projectile velocity
v_E	projectile exit velocity at muzzle
τ	circuit time constant (L_0/R_T)
T	time when current I reaches zero
t	time variable
t_E	time to shot-out from crowbarring

f scaling factor related to railgun inductance parameter L'

m_p mass of projectile

m_A mass of plasma armature

m combined mass of plasma armature and projectile ($m_A + m_p$)

u dimensionless time parameter (t_E/T)

w dimensionless railgun parameter

E_p kinetic energy of projectile at muzzle

$g(u)$ defined function of u

$h(w)$ defined function of w

η_T energy-transfer efficiency from capacitance to inductance energy store

η_I overall efficiency of ideal railgun

η overall efficiency of "practical" railgun

η_M overall upper bound efficiency of "practical" railgun

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EFFICIENCY ASPECTS OF SHORT, LOW
VELOCITY RAILGUNS

1. INTRODUCTION

For some years MRL carried out laboratory studies on small railguns. The aim of that work was to understand the basic physical processes involved in railgun operation and for that purpose small experimental railguns served very well. The experimental railguns were not designed to meet any military requirements and hence the need for high conversion efficiency was relatively unimportant. In fact the railguns used were inefficient with typically less than 2% of the input energy being converted to kinetic energy of the projectile. Nevertheless the question of efficiency has always been addressed in MRL's work and in particular the way in which input energy is distributed throughout the railgun system has been investigated in the experimental studies.

The background and results of MRL work have been reported previously [1-13]. Railguns with a 6 x 8 mm bore (RAPID and ERGS) [4] as well as a 10 x 10 mm bore (RIPPER) were used. Theoretical aspects of efficiency of the RAPID railgun were considered by Kowalenko [11] in his study of a firing series codenamed RPIP.

The work presented here examines some aspects of the efficiency question, taking into account most of the effects likely to occur in a practical system. The work relates to what is loosely termed a short railgun, the essential criterion defining a short gun being established in the report. The key to the study is the derivation of a simple mathematical expression for the current flow in the railgun during firing. This allows some useful expressions relating to the efficiency to be obtained. It is emphasised that the railgun configuration being considered here represents a specific class having limited applications; it would not be used to meet the more usual requirements of high velocity and high efficiency.

In this report various efficiency parameters are introduced. The efficiency with which electrical energy, initially stored in a capacitance, is transferred to a secondary inductance store is designated as η_T . For

reference purposes the overall efficiency, η_I , of an ideal railgun is then derived. A general expression for the overall efficiency, η , of a more practical railgun is then obtained together with an estimate of its upper bound η_M . Overall efficiency refers to the ratio of the kinetic energy of the railgun projectile as it leaves the gun to the energy initially stored in the primary capacitance store.

2. RAILGUN MODEL

2.1 General Description

In this study the conventional railgun model as shown in Fig. 1 is considered. A storage capacitance C is initially charged to a potential V_0 . During the pre-crowbar phase the main switch (a plasma-gap device or ignitron) is "closed", thus allowing the storage inductance L_0 to be charged via the plasma armature established behind the projectile in the railgun. When the current reaches its maximum value I_0 the crowbar switch isolates the capacitance from the inductance driving circuit. In practice the crowbarring is not achieved instantaneously and there is some minor ongoing interaction between the two circuits via the common crowbar path. It is emphasized that in this study the projectile is considered as initially at rest; the study does not cover injected railgun configurations [12].

2.2 Pre-crowbar Phase

The pre-crowbar phase starts with the closure of the main switch and consists of a short-duration energy transfer process in which the plasma armature is established and the inductance is fully charged to its maximum current. Although there is some movement of the projectile during this interval it will be considered negligible. The equivalent electrical circuit is as shown in Fig. 2. The voltage-drops V_2 and V_3 across the plasma armature and the main switch respectively are much smaller than the initial voltage V_0 on the capacitance. Under these conditions the only significant loss during energy transfer is due to the circuit resistance R_c . It has been shown [11,12] that the energy necessary to establish the arcs is negligible in comparison with the other energy-dissipating processes. As shown in any standard circuit analysis text covering lightly-damped tuned circuits, the maximum current I_0 built up in the inductance L_0 is given by

$$I_0 = V_0 \sqrt{\frac{C}{L_0}} \exp \left\{ -\frac{R_c}{4} \sqrt{\frac{C}{L_0}} \right\} \quad (1)$$

provided $R_c \sqrt{\frac{C}{L_0}} \ll 1$

This latter condition should be met for any well-designed system.

The efficiency of the energy transfer is defined as

$$\eta_T = \frac{\frac{1}{2} L_o I_o^2}{\frac{1}{2} C V_o^2} \quad (2)$$

which, by the use of equation (1), becomes

$$\eta_T = \exp \left\{ -\frac{R_C}{2} \sqrt{\frac{C}{L_o}} \right\} \quad (3)$$

In general one could expect that a railgun designed to meet high efficiency specifications would aim to achieve η_T values in the range $0.8 < \eta_T < 1$. However values as low as 0.6 have been observed experimentally in MRL work where efficiency has not been a major consideration.

2.3 Post-crowbar Phase

The situation at some general time in the post-crowbar phase is shown in Fig. 3. V_1 is the voltage across the crowbar switch and, as before V_2 is the voltage across the plasma armature in the railgun. The projectile of mass m_p , together with the armature which is assumed to have a constant mass m_a , has moved a distance x along the barrel whose length is l . In accordance with usual railgun analyses, the railgun is characterised by the two parameters L' and R' which are, respectively, the railgun barrel inductance and resistance per unit length. The circuit resistance R_V accounts for all resistive effects apart from those associated with the railgun armature and the crowbar switch.

An examination of the records of MRL railgun firings shows that the behaviour of the two plasma regions can be represented electrically by constant breakdown potentials E_1 and E_2 in association with small incremental resistances R_1 and R_2

$$\begin{aligned} \text{i.e.} \quad V_1 &= E_1 + R_1 I \text{ and} \\ V_2 &= E_2 + R_2 I, \end{aligned} \quad (4)$$

where I is the railgun current.

This matter is discussed in Section 3 of the report. The electrical equivalent circuit can then be redrawn as shown in Fig. 4. (The symbols for voltage break-down diodes have been used in the equivalent circuits to emphasize the electrical behaviour being attributed to the plasmas in this study).

The circuit equation for Fig. 4 is

$$L_0 \frac{dI}{dt} + L'x \frac{dI}{dt} + L'I \frac{dx}{dt} + E_1 + E_2 + (R_v + R_1 + R_2 + R'x) I = 0 \quad (5)$$

The second term in equation (5) may be neglected in comparison with the first if $L'x \ll L_0$. As the largest value of x will be the barrel length, ℓ , an appropriate condition is $\ell L' \leq L_0/10$. We are therefore limited in this study to railguns having an upper bound on length given by

$$\ell \leq \frac{1}{10} \frac{L_0}{L'} \quad (6)$$

The condition introduced above suggests that one possible way of classifying railgun systems for analysis purposes at least, is to use the system length parameter L_0/L' . Although this does not represent a physically measurable length as such, it may be used to classify a system as being short, medium or long according to whether $\ell \ll L_0/L'$, $\ell \sim L_0/L'$ or $\ell \gg L_0/L'$ respectively. In the present study we are concerned only with railguns which are short in the sense indicated above.

Returning to equation (5) the third term can be neglected in comparison with the first; a sufficient but probably over-conservative condition being

$$L'I_0 v_E \leq \frac{1}{10} \left| \frac{dI}{dt} \right|_{\max}, \quad (7)$$

where v_E is the muzzle, or exit, velocity of the projectile. It will further be considered that the maximum resistance of the rails, $R'\ell$, is much smaller than all other resistances combined, i.e. the condition

$$R'\ell \ll R_v + R_1 + R_2 \quad (8)$$

is satisfied. This is the case with the RAPID railgun.

Under the above conditions, the electrical equivalent circuit reduces to Fig. 5 and the system equation becomes

$$L_0 \frac{dI}{dt} + (E_1 + E_2) + R_I I = 0, \quad (9)$$

where R_T represents all the circuit resistances. If we consider this second phase starting at $t = 0$, then the initial condition for equation (9) is $I(0) = I_0$ where I_0 is given by equation (1).

The solution to equation (9) is

$$I = (I_0 + I_E) \exp\left(-\frac{t}{\tau}\right) - I_E, \quad (10)$$

where
$$I_E = \frac{E_1 + E_2}{R_T}, \quad (11)$$

and
$$\tau = \frac{L_0}{R_T} \quad (12)$$

The current variation defined above can be expressed in the normalized form

$$\frac{I}{I_0} = \left(1 + \frac{I_E}{I_0}\right) \exp\left[-\frac{t}{T} \ln\left(1 + \frac{I_0}{I_E}\right)\right] - \frac{I_E}{I_0}, \quad (13)$$

where T is the time at which the current reaches, and then remains at, zero level. T is given by

$$T = \tau \ln\left(\frac{I_0 + I_E}{I_E}\right) \quad (14)$$

Equation (13) is plotted for $I_E/I_0 = 1$ in Fig. 6A. For large values of I_E/I_0 , i.e. where $I_E/I_0 \rightarrow \infty$, equation (13) reduces to

$$I = I_0 \left[1 - \frac{t}{T}\right], \quad 0 \leq t \leq T \quad (15)$$

It is demonstrated in Fig. 6B that this linear relationship is a good approximation to equation (13) for a wide range of I_E/I_0 values, in particular for $I_E/I_0 \geq 1$. In the remainder of this report we will therefore regard $I_E \geq I_0$, i.e.

$$\frac{E_1 + E_2}{R_T} \geq I_0, \quad (16)$$

as a necessary and sufficient condition justifying the general use of the linear current relationship given by equation (15). The linear reduction of I with time as defined by equation (15) is clearly evident in the results of RAPID and RIPPER firings; in fact it was this unexpected linearity which led to the present analysis being undertaken. It should be noted that the analysis is valid only when $t \leq T$ and while the projectile and plasma armature remain within the railgun. In fact in all MRL firings the projectile left the muzzle at some time t_E less than T . In such cases the analysis is only valid for $t \leq t_E$. In many experimental firings, though not all, the linear current variation^E is observed beyond t_E down to the point where the current approaches zero. An example of this behaviour is shown in Fig. 7.

If the conditions introduced in the derivation of equation (10) are examined, it is seen that they amount, in effect, to neglecting the presence of the railgun except for the plasma parameters E_2 and R_2 . This means that effects relating to $R \cdot xI$, $L \cdot I (dx/dt)$ and $L \cdot x (dI/dt)$ are considered negligible. These are the terms which arise from railgun action and cause the difference between the breech voltage V_B and the muzzle voltage V_M (defined in Figs. 3 and 4). Representative data from a RAPID firing are shown in Fig. 8. Here the two voltages are seen to be essentially the same, i.e. the railgun, as far as electrical modelling purposes are concerned, can be considered to have the plasma armature located at the breech.

The important conclusion which follows directly is that the projectile's position and velocity within the railgun have negligible effect on the electrical driving circuit, i.e. the electrical circuit aspects of the gun system can be considered to be independent of mechanical aspects such as projectile position and velocity. The converse is not true.

3. EVALUATION OF REPRESENTATIVE RAILGUN PARAMETERS

3.1 Plasma Armature Parameters (E_2 , R_2)

A typical breech voltage record is shown in Fig. 9 and its corresponding current-voltage relationship in Fig. 10. (This result was taken using a RAPID gun in a series known as MRAP designed to test magnetic flux sensors.) Fig. 9 shows the characteristic slow run-down with the superimposed fluctuations up to shot-out and then the characteristic jump and more rapid run down until the arc is finally extinguished at the muzzle as the current reaches zero. Ignoring the randomlike fluctuations in Fig. 10, which are probably due to short-duration dynamic processes within the plasma volume, it is possible to represent the breech voltage V_B for the in-barrel phase as

$$V_B \approx 150 + 0.7 \times 10^{-3} I$$

from which, by equating V_B with V_2 and recalling that $V_2 = E_2 + R_2 I$ as discussed in section 2.3, we obtain $E_2 = 150$ V and $R_2 = 0.7 \times 10^{-3} \Omega$. As a matter of interest the breech voltage-current curve for the muzzle arc is also

shown in Fig. 10. This shows linear behaviour, also tending to $V_B = 150$ V, as the current approaches zero.

3.2 Combined Potential ($E_1 + E_2$) and Resistance R_T

A curve-fitting procedure was used to estimate ($E_1 + E_2$) and R_T . This involved plotting current-time data from experimental firings in the form (I/I_0) on a logarithmic scale versus time, as proposed by Kowalenko [11], and then comparing this with the theoretical curve (derived from equations (10), (11) and (12)),

$$\text{i.e.} \quad \frac{I}{I_0} = 1 - \frac{E_1 + E_2}{L_0} t \left(1 - \frac{R_T}{2L_0} t\right) \quad (17)$$

which was evaluated for assumed values of ($E_1 + E_2$) and R_T . This essentially trial-and-error procedure leads to unique values of ($E_1 + E_2$) and R_T for best fit.

A representative fit is shown in Fig. 11 where it is found that ($E_1 + E_2$) = 300 V and $R_T = 2.7 \times 10^{-3} \Omega$. The error in parameter estimation is probably about 10%.

3.3 Crowbar Breakdown Potential E_1

The first method used to evaluate E_1 involved direct measurement of the voltage across the crowbar switch during a railgun firing. The difficulty with this method is that when the main switch is closed during the pre-crowbar phase, the full capacitor voltage V_0 , which is typically 6 kV, appears across the crowbar switch. Experimental results show that during operation of the crowbar the potential reverses by approximately 1000 V before settling towards a value of about 200 V. In order to obtain these data a voltage divider (1000 times) was used to give the typical record shown in Fig. 12. The errors in the measurement are such that the value of $V_1 \approx 200$ V can only be regarded as approximate. The data are not sufficiently accurate to estimate E_1 or R_1 reliably.

A second method for determining E_1 was based on monitoring the current I during the operation of a railgun in which no projectile or foil was present but where a low resistance strap was placed across the muzzle. This arrangement effectively reduced the system to that shown in Fig. 13 during the post-crowbar phase. Although the resistance R will not correspond to R_T in the railgun circuit, the value E_1 should be the same as in a normal firing. The theoretical current relationship for the circuit proposed in Fig. 13 is

$$I = \left(I_0 + \frac{E_1}{R}\right) \exp\left(-\frac{tR}{L_0}\right) - \frac{E_1}{R} \quad (18)$$

and this was compared with experimental data. The parameter values best matching the experimental curve shown in Fig. 14 are $E_1 = 145$ V and $R = 1.67$ m Ω .

3.4 Pre-crowbar Circuit Resistance R_C

The most direct method for estimating R_C involves the use of equation (1) with measured values of V_o , I_o , C and L_o . Kowalenko [11] has drawn attention to some uncertainty in the calibration values for the current records obtained in the RAPID and RIPPER firings at MRL. An alternative method, using the results of a firing when the crowbar switch failed to operate, was therefore used. The waveform record, clipped on the negative-swing by limitations of the data-capture equipment, is shown in Fig. 15. The occurrence of the two successive current maxima I_o and I_1 , with the projectile still in bore, allows R_C to be estimated without the need for accurate current calibration. It can be readily shown that

$$R_C = -\frac{1}{\pi} \sqrt{\frac{L_o}{C}} \ln \left(\frac{I_1}{I_o} \right) \quad (19)$$

Substituting the following values which are representative of the RAPID railgun ($L_o = 6.3 \times 10^{-6}$ H, $C = 1600$ μ F and $I_1/I_o = 0.71$), equation (19) gives R_C as 7×10^{-3} Ω . The transfer efficiency η_T is then found from equation (3) to be 89%.

4. CONVERSION EFFICIENCY

4.1 The Ideal Railgun

An inductance L_o supplying current to a railgun with inductance per unit length L' and barrel length λ as shown in Fig. 16 is considered. The inductance, the rails and the armature are assumed to have zero resistance. Because the sum of the voltage drops around the circuit is zero, the circuit equation is

$$\frac{d}{dt} (L_o I + L' \lambda I) = 0 \quad (20)$$

Integrating equation (20) between shot-start and shot-out leads to

$$(L_o + L' \lambda) I_M = L_o I_o$$

where I_M is the railgun current at shot-out. It follows that

$$I_M = I_0 \frac{L_0}{L_0 + L'\ell} \quad (21)$$

Now if it is assumed that the reduction in stored magnetic energy corresponds to the increase in the kinetic energy E_p of the projectile, then

$$E_p = \frac{1}{2} L_0 I_0^2 - \frac{1}{2} (L_0 + L'\ell) I_M^2$$

i.e.

$$E_p = \frac{1}{2} \frac{L_0 L'\ell}{L_0 + L'\ell} I_0^2 \quad (22)$$

The conversion efficiency η_I is then given by

$$\eta_I = \frac{E_p}{\frac{1}{2} L_0 I_0^2} \quad (23)$$

which, with equation (22), yields

$$\eta_I = \frac{L'\ell}{L_0 + L'\ell} \quad (24)$$

This expression is quite general and, as would be expected, η_I approaches unity for $L'\ell \gg L_0$. For the case of short railguns, as discussed in Section 2.3 where $\ell \ll L_0/L'$, equation (24) becomes

$$\eta_I = \frac{L'\ell}{L_0} \quad (25)$$

As an example, for a railgun like RAPID, with $\ell = 0.5$ m, $L_0 = 6.3$ μ H and $L' \approx 0.5$ μ H/m the value of η_I is 0.04, i.e. the highest possible efficiency is 4%. It should be noted that this result is independent of the projectile mass, the current-time waveform and projectile motion providing only that equation (21) applies.

4.2 General Derivation - A More Realistic Model

In this section we consider the railgun discussed in Section 2 and in particular we will consider that the railgun current decreases linearly with time according to equation (15). The usual equation of motion is taken, i.e.

$$m \frac{dv}{dt} = \frac{1}{2} fL'I^2, \quad (26)$$

where $v = \frac{dx}{dt}$ is the projectile velocity, and

$$m = m_A + m_p$$

where m_p is the mass of the projectile, and m_A is the mass of the plasma armature and f is a factor ($f < 1$) introduced by Sadedin [13] to allow for the effect of leakage inductance. This results in a difference between the circuit magnetic flux and the effective flux contributing to the force acting on the plasma. The use of equation (26) implies that gas forces ahead of the projectile and friction forces are negligible, and that m_A is a constant. More specifically it means either that no material is picked up and expelled during armature motion or, if it is, it is ejected at the same mass rate as it is picked up and, additionally, is ejected at zero velocity relative to the armature.

Using equation (15) for the current I , integration of equation (26), leads to

$$mv = \frac{1}{6} fL'I_0^2 T \left[\left(\frac{t}{T}\right)^3 - 3\left(\frac{t}{T}\right)^2 + 3\left(\frac{t}{T}\right) \right] \quad (27)$$

which holds for $0 \leq t \leq T$ but only whilst the projectile remains in the barrel, i.e. $x \leq \ell$.

Using equation (27), the shot-out condition is

$$mv_E = \frac{1}{6} fL'I_0^2 [u^3 - 3u^2 + 3u], \quad 0 \leq u \leq 1 \quad (28)$$

where $u = \frac{t_E}{T}$, (29)

t_E is the time of projectile exit and

v_E is the exit velocity.

The condition $0 \leq u \leq 1$ in equation (28) means that the expression is only valid where the projectile reaches the muzzle before, or just as, the current reaches zero. The condition $u > 1$ (i.e. $t_E > T$) means the barrel is unnecessarily long because the current is zero for $t > T$.

The general expression defined by equation (27) can also be integrated to provide a relationship between barrel length ℓ and u as follows:

$$m\ell = \frac{1}{24} fL'I_0^2 T^2 [u^4 - 4u^3 + 6u^2] \quad (30)$$

The kinetic energy of the projectile at exit is given by

$$E_p = \frac{1}{2} m_p v_E^2$$

i.e.

$$E_p = \frac{1}{2} \frac{m_p \ell}{m_A + m_p} \frac{(mv_E)^2}{m\ell} \quad (31)$$

Using mv_E and $m\ell$ from equation (28) and (30) respectively then gives

$$E_p = \frac{1}{2} L' I_o^2 f \frac{m_p}{m_A + m_p} g(u), \quad (32)$$

where

$$g(u) = \frac{2[(u-1)^3 + 1]^2}{3u^2 [u^2 - 4u + 6]} \quad (33)$$

The efficiency of the railgun η which is the ratio of the exit kinetic energy to the original stored capacitor energy, is given by

$$\eta = \eta_T \frac{E_p}{\frac{1}{2} L_o I_o^2} \quad (34)$$

where η_T is the energy transfer efficiency discussed in Section 2. Using the expression for E_p obtained above

$$\eta = \eta_T \frac{m_p}{m_p + m_A} f \frac{L'\ell}{L_o} g(u) \quad (35)$$

The last expression is not directly useful as it stands. A more useful approach is to express efficiency in terms of a parameter

$$w = \frac{24(m_A + m_p)\ell}{fL'I_o^2 T^2} \quad (36)$$

which may also be expressed in terms of basic parameters in the form

$$w = \frac{24(m_A + m_P) \ell R_T^2}{fL'I_0^2 L_0^2 \ln^2 \left[1 + \frac{I_0 R_T}{E_1 + E_2} \right]} \quad (37)$$

The relationship between u and w follows from equation (30) as

$$u^2 (u^2 - 4u + 6) = w \quad (38)$$

This function is plotted in Fig. 17 where it is clear that the restriction $0 \leq u \leq 1$ leads to the corresponding restriction $0 \leq w \leq 3$. A function $h(w)$ can then be generated by combining equations (33) and (38) under the equality $g(u) = h(w)$ so that efficiency can be expressed in the form

$$\eta = \eta_T \frac{m_P}{m_P + m_A} f \frac{L' \ell}{L_0} h(w) \quad (39)$$

The function $h(w)$ is shown in Fig. 18.

Given the parameters of a short railgun, equations (37) and (39) can be used to evaluate the expected efficiency. If the value of w exceeds three it means the actual barrel length ℓ is longer than necessary. Its effective length will then be that value of ℓ which makes $w = 3$.

4.3 Summary of Restrictions

In deriving the efficiency expressions in the previous sections a number of conditions were imposed. These are not physical restrictions on railgun parameters as such but are conditions relating to the notion of short railguns as used in this report and relate to the validity of the mathematical expressions which have been derived. The first somewhat arbitrary, conditions are

$$\ell \leq \frac{1}{10} \frac{L_0}{L'} \quad \text{from equation (10),}$$

$$R' \ell \ll R_1 + R_2 + R_V \quad \text{from equation (8),}$$

$$\text{and} \quad \frac{E_1 + E_2}{R_T} \geq I_0 \quad \text{from equation (16).}$$

A third condition discussed in Section 4.2 is that the parameter w has a maximum value of 3. (It will be shown below that there is also a modified minimum permitted value greater than zero).

A fourth condition was introduced as equation (7), viz

$$L' I_0 v_E \leq \frac{1}{10} L_0 \left| \frac{dI}{dt} \right|_{\max}$$

This will now be examined more fully. From equation (15) it follows that dI/dt is a constant ($-I_0/T$). Substituting this in the above equation gives

$$v_E \leq \frac{1}{10T} \frac{L_0}{L'} \quad (40)$$

This value is, in effect, the upper limit on allowable muzzle velocity for which the present model applies. Now from equation (28) the maximum possible exit velocity, obtained for $u = 1$, is

$$v_{E \max} = \frac{fL' I_0^2 T}{6 (m_A + m_p)}$$

It then follows that the condition to be met is

$$\frac{fL' I_0^2 T}{6 (m_A + m_p)} \leq \frac{1}{10T} \frac{L_0}{L'} \quad (41)$$

which can be rearranged to give

$$w \geq \frac{40L'}{L_0} \quad (42)$$

where w is as defined previously. But it was also stipulated earlier that $w \leq 3$. Hence the maximum allowable value of L'/L_0 for which this present analysis can be considered valid is

$$\frac{L'}{L_0} = \frac{3}{40} \quad (43)$$

This condition is slightly more severe than $L'/L_0 \leq 1/10$ so it will now be used as the defining condition for a short railgun. For practical purposes of course the difference is of little consequence. An important conclusion is that the expression for efficiency η given in equation (39) is valid only in the range

$$40 \frac{L'}{L_0} \leq w \leq 3 \quad (44)$$

As an example of the use of the previous equations, consider a railgun with the following characteristics: $m_p = 10^{-3}$ kg, $l = 0.4$ m, $R_T = 3 \times 10^{-3}$ Ω , $I_0 = 10^5$ A, $E_1 + E_2 = 300$ V, $f = 0.6$, $L_0 = 5 \times 10^{-6}$ H, $L' = 0.5 \times 10^{-6}$ H/m and $\eta_T = 0.9$. It will be assumed that $m_A = 0$. The value of w from equation (37) is $w = 2.3$. Because $40 \frac{L'}{L_0} = 1.6$, the condition in equation (44) is met and hence the expressions given in the report can be used to determine $h(w)$ and η . From Fig. 17 $h(2.3) = 0.28$. From equation (39) we then obtain $\eta = 0.6\%$.

4.4 Maximum Achievable Efficiency

In the previous sections, mathematical expressions were obtained which allow the upper bound on efficiency of a short railgun ($\frac{L'}{L_0} \leq 3/40$) to be estimated. However it is evident from equation (39) that, for a given value of $\frac{L'}{L_0}$ it is necessary that $h(w)$ be made as large as possible if maximum efficiency is to be achieved. From Fig. 18 it is seen that this requires w to be minimized. But from equation (42) we know that this minimum value must be $40 \frac{L'}{L_0}$. Using these values we obtain an expression for maximum efficiency η_M using equation (39), which can be expressed as follows:

$$\frac{\eta_M}{\eta_T \left(\frac{m_p}{m_p + m_A} \right)} = \frac{L' l}{L_0} h\left(40 \frac{L'}{L_0}\right) \quad (45)$$

The function is plotted in Fig. 19. It is seen that the curve lies between the straight lines with slope 1 (corresponding to the ideal railgun) and slope 2/9. The important conclusion is that the maximum achievable efficiency is $2/9(\frac{L'}{L_0})$ as $\frac{L'}{L_0}$ approaches $3/40$, i.e. the maximum efficiency is 1.6%. For interest, the probable operating regime of the MRL RAPID railgun is shown in Fig. 19. Typical measured values of efficiency are 0.7% for RAPID [4] and 1.1 to 2.1% for ERGS I-M [6]. It should be noted that the experimental values will include gas-pressure propulsion effects which can be significant in short railguns [13].

4.5 Maximum Velocity Limit

An upper limit on the muzzle velocity for v_E for which the present model can be considered valid is given by equation (40) which, in conjunction with the expression for T derived at equation (14) earlier, gives

$$v_E \leq \frac{1}{10 \ln \left[1 + \frac{I_0 R_T}{E_1 + E_2} \right]} \left(\frac{R_T}{L'} \right) \quad (46)$$

The behaviour of this function is shown in Fig. 20 for circuit resistance values R_T in the range 0 to 5 m Ω and railgun currents I_0 in the range 25 to 200 kA. Values of $E_1 + E_2 = 300$ and $L' = 0.4$ μ H/m were used for all cases.

It is evident that even at the low peak current of 25 kA, the maximum velocity is only 3 km/s. This value lies at the low velocity end of the range of possible applications for which railguns are usually proposed. Further, it must be noted that low currents will, for barrels of practical lengths (e.g. 5 m), be incapable of propelling masses much above 0.1 g, i.e. the practical usefulness at low currents is very restricted. It is apparent therefore that the model and results developed here must be considered as appropriate only for low velocity guns.

5. DESIGN EQUATIONS FOR SMALL RAILGUNS

To complete this study a set of design equations will be obtained. Once again it must be emphasized that the results are only applicable to a restricted class of railgun applications where low velocities and low efficiencies are acceptable. It will be assumed that values of m_p and v_E have been specified and that a railgun giving maximum, albeit low, efficiency is to be designed. It will be taken that the values of f , $(E_1 + E_2)$ and L' are known for the railgun configuration proposed. The values of L_0 , l , I_0 and R_T are to be calculated. It will be assumed for convenience that $m_A \ll m_p$.

We know that maximum efficiency is achieved when $w = 3$ or, equivalently, $u = 1$. If $u = 1$ is substituted in equations (28) and (30) we obtain

$$m_p v_E = \frac{1}{6} f L' I_0^2 T \quad (47)$$

$$\text{and} \quad m_p l = \frac{1}{8} f L' I_0^2 T^2 \quad (48)$$

Combining (47) and (48) gives

$$l = \frac{9}{2} \frac{m_p v_E^2}{f L' I_0^2} \quad (49)$$

and then, using equation (43), we obtain

$$L_0 = 60 \frac{m_p v_E^2}{f I_0^2} \quad (50)$$

This means that l and L_0 are known once I_0 is determined. A value for I_0 can be evaluated as follows. From equation (47)

$$T = \frac{6 m v_E}{f L' I_0^2}$$

Combining this with an expression for T obtained from equation (12) and (14) we obtain

$$\frac{L_0}{R_T} \ln \left[\frac{I_0 + \frac{E_1 + E_2}{R_T}}{\frac{E_1 + E_2}{R_T}} \right] = \frac{6 m v_E}{f L' I_0^2} \quad (51)$$

Following the discussion in section 2.3 the convenient, though somewhat arbitrary design stipulation

$$R_T = \frac{E_1 + E_2}{I_0} \quad (52)$$

is introduced, equations (50) and (51) then providing the following expression for I_0 ,

$$I_0 = \frac{1}{10 \ln 2} \frac{E_1 + E_2}{L' v_E} \quad (53)$$

Equations (53), (52), (50) and (49), taken in turn, provide the required values of I_0 , R_T , L_0 and ℓ .

As an example, suppose $m_p = 10^{-3}$ kg, $v_E = 800$ m/s, $f = 0.6$, $\eta_T = 0.8$, $L' = 0.5 \times 10^{-6}$ H/m and $(E_1 + E_2) = 300$ V. Successive use of the above equations then gives $I_0 = 108$ kA, $R_T = 2.8$ m Ω , $L_0 = 5.5$ μ H and $\ell = 0.8$ m. The efficiency η_M is then 1.3%.

6. CONCLUSIONS

Expressions have been obtained for the current flow in, and efficiencies available from, small, low velocity railguns of the type used for experimental work at MRL. It is shown that in the context of this report the condition defining a short railgun is $\ell \leq 3/40 L_0/L'$. The maximum efficiency is achieved when the current drive reaches zero simultaneously with the projectile reaching the muzzle of the gun. Under these conditions the maximum efficiency is 2/9 of that for an ideal short rail gun whose efficiency is $\ell L'/L_0$, i.e. the best achievable efficiency is 1.6% when $\ell L'/L_0 = 3/40$.

The work has shown that the railgun current is controlled predominantly by the two constant voltage breakdown potentials E_1 and E_2 in

the plasma armature and in the (plasma) crowbar switch respectively and by the storage inductance L_0 and the total circuit resistance R_T . For typical small MRL railguns, the current decreases linearly with time, independent of projectile motion in the railgun. This effective decoupling of the electrical from the mechanical effects has enabled a simple analysis of the projectile behaviour to be carried out. For the configurations considered here, the efficiencies are very low, with approximately 98% of the energy which is initially transferred to the drive inductance being dissipated in the two plasma arcs and the circuit loss resistances.

The fundamental electrode potentials E_1 and E_2 were shown to be about 150 V. No opportunity has been available to study the factors affecting these values in other railgun configurations. From the RPIP firings it would appear that the value of E_2 is independent of the type and mass of metal foil used to establish the plasma armature.

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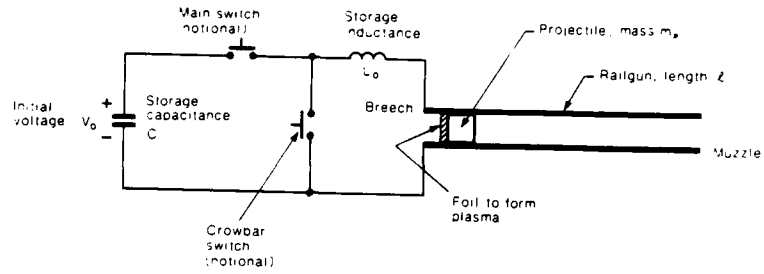


FIGURE 1 Railgun model.

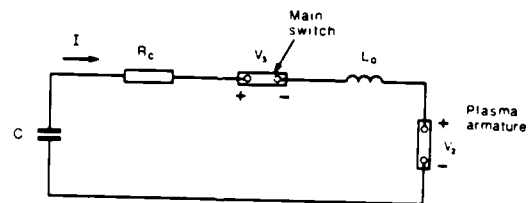


FIGURE 2 Pre-crowbar equivalent circuit.

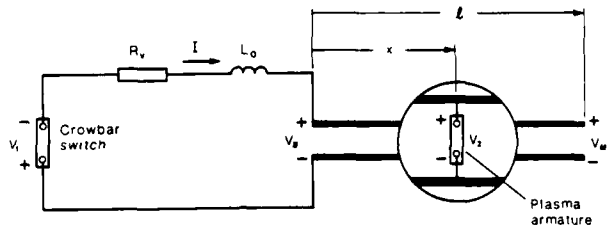


FIGURE 3 Post-crowbar equivalent circuit.

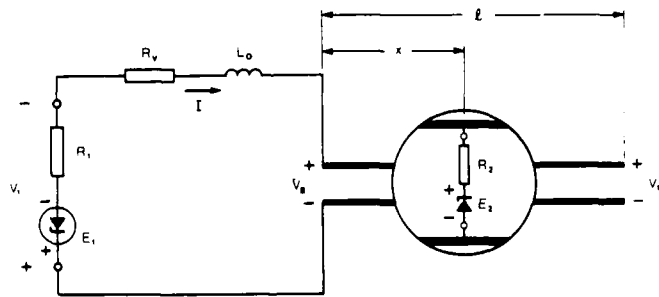


FIGURE 4 Post-crowbar equivalent circuit.

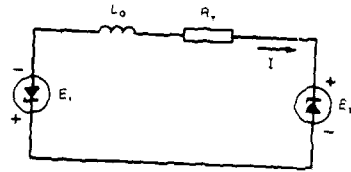


FIGURE 5 Simplified equivalent circuit.

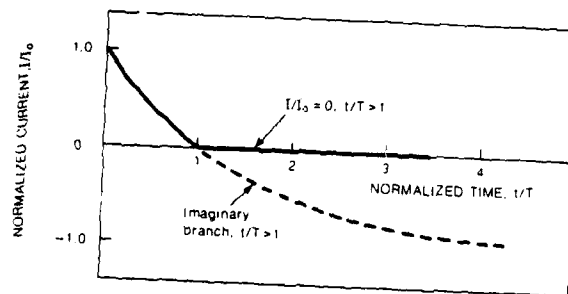


FIGURE 6A Current variation for $I_E/I_0 = 1$.

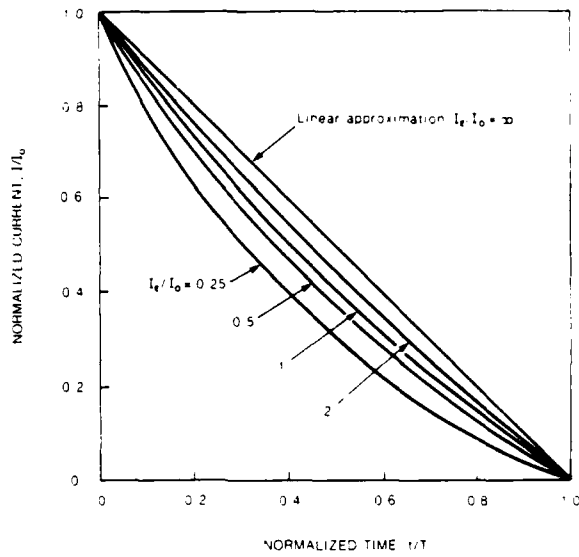


FIGURE 6B Current variation for different I_E/I_0 ratios.

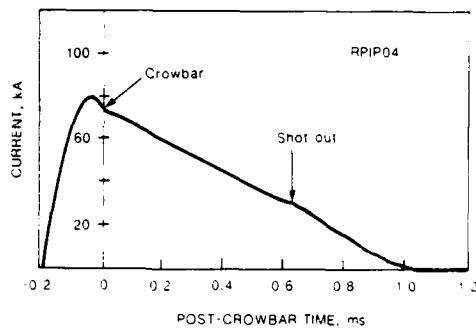


FIGURE 7 Experimental current record.

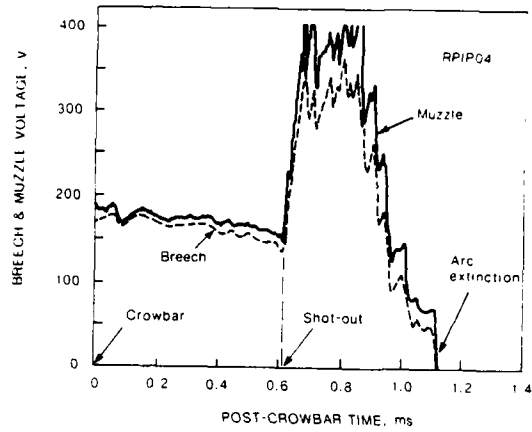


FIGURE 8 Experimental breech and muzzle voltage records.

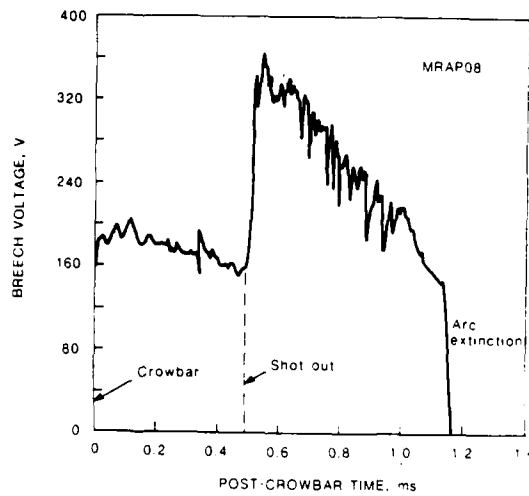


FIGURE 9 Post-crowbar breech voltage.

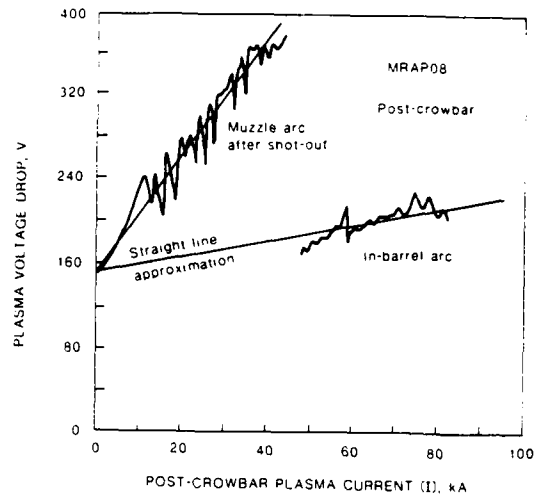


FIGURE 10 Plasma voltage-current relationships.

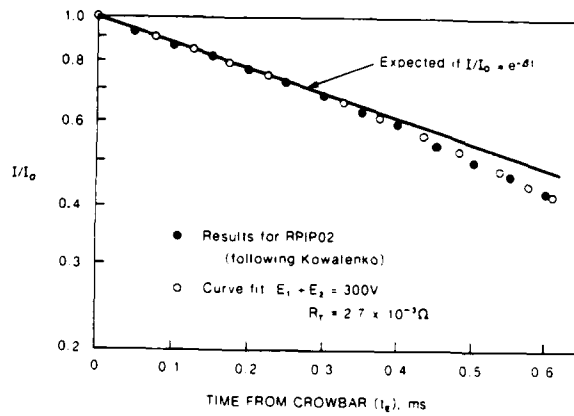


FIGURE 11 Parameter estimation by curve fitting.

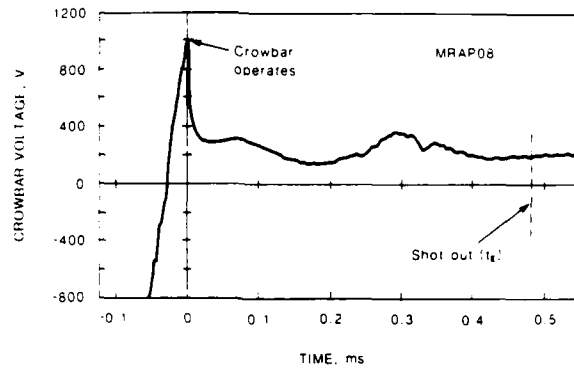


FIGURE 12 Crowbar switch voltage.

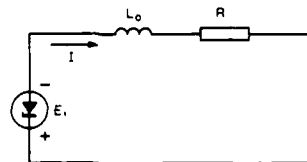


FIGURE 13 Equivalent circuit for low resistance muzzle strap with no projectile or plasma present.

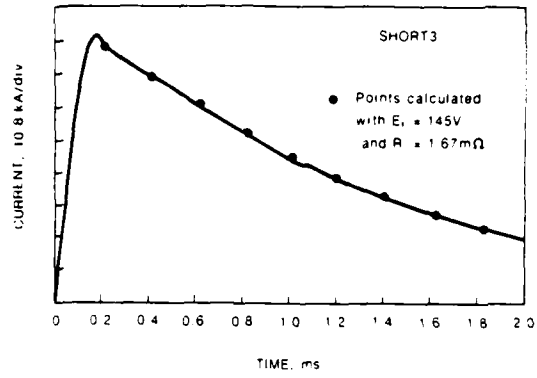


FIGURE 14 Experimental current record, no projectile and short-circuited muzzle.

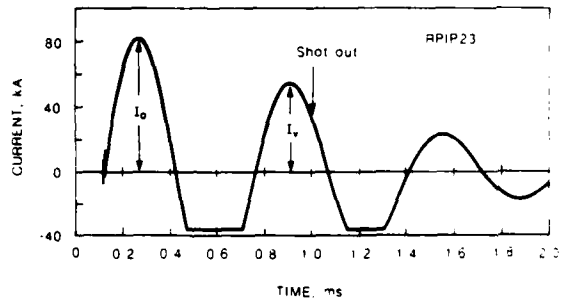


FIGURE 15 Experimental gun current with no crowbar switch.

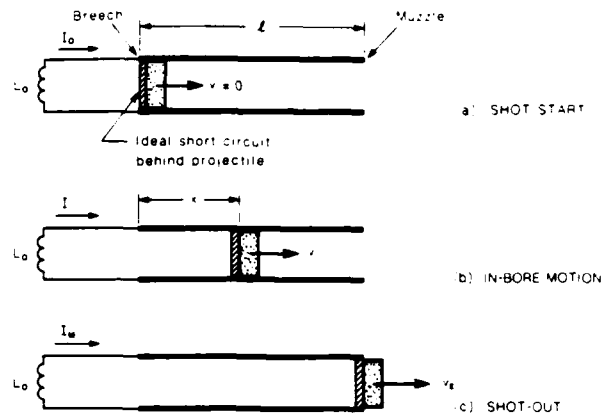


FIGURE 16 Stages in ideal railgun operation.

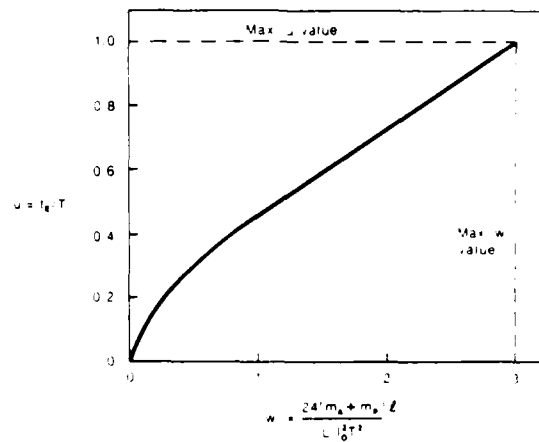


FIGURE 17 Relationship between u and w .

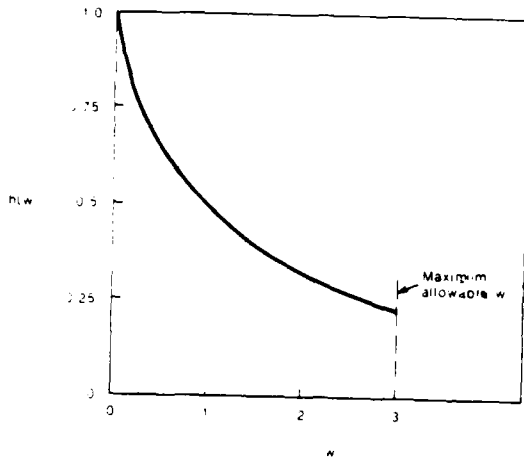


FIGURE 18 Plot of function $h(w)$.

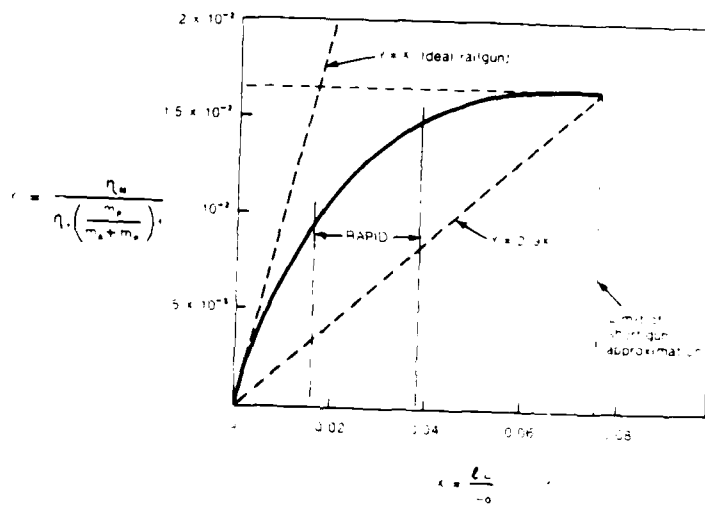


FIGURE 19 Maximum efficiency curve.

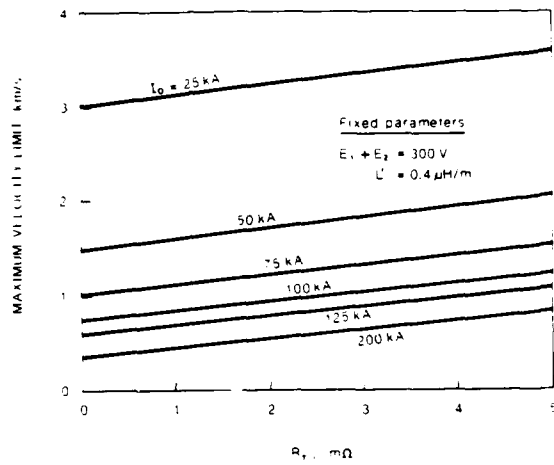


FIGURE 20 Maximum velocity limits on railgun model.

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ABSTRACT

The factors controlling the performance of short, low velocity railguns are studied and mathematical expressions defining the bounds of realizable efficiencies are obtained. The restrictions governing the validity of the expressions are discussed. The expressions are based on the proposition that during acceleration of the projectile in the railgun, the current falls almost linearly with time. Under the conditions discussed in this report it is shown that the maximum achievable efficiency is about 1.6%.

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