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SARLAC: A Relativistic Electron Beam Code

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→ SARLAC is a particle simulation code for studying the propagation of ultra-relativistic electron beams. It is used to study the nonlinear evolution of the resistive hose instability. We have developed a fast, semi-implicit, iterative field solver which allows us to include a large number of Fourier modes in the azimuthal direction. The solver iterates about a solution of the field equations dominated by the axisymmetric ($m = 0$) conductivity. This technique has proved to be quite successful. We compare some results of the code with those obtained from a linearized hose simulation code, and show differences when the hose oscillations reach large amplitude. <i>Keywords:</i>					
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SARLAC: A RELATIVISTIC ELECTRON BEAM CODE

We have recently written a number of simulation codes to test various aspects of the resistive hose instability in high energy electron beams propagating in resistive plasmas. Most methods used previously for treating the instability were restricted to small instability amplitudes. These are considered to be of practical interest because large amplitude hose-like oscillations quickly destroy the integrity of the the beam, and because, under appropriate circumstances, the instability "saturates" in the linear regime. That is to say, the hose instability is convective in the beam frame, and therefore, at any given point in the beam may reach a maximum which is still small followed by a decay of the instability as the disturbance convects past. Near term experiments, however, are frequently more unstable than can be treated by linear models, so we have developed a particle simulation code which can follow the evolution of an instability into the nonlinear regime¹⁻³. Similar codes have been written by Godfrey⁴ and Freeman⁵.

The nonlinear code has borrowed heavily from two of our previous codes, SIMMO⁶ and SIMM1⁷ which are particle simulation codes for axisymmetric beams and beams with small amplitude hose motions. The particle dynamics of those two codes are followed in Cartesian coordinates so the SARLAC code differs from these primarily in the calculation of the electromagnetic fields. We have developed a fast iterative field solver which allows us to include a large number of Fourier modes in the azimuthal direction.

The code employs many of the approximations found in most linearized propagation models⁸⁻¹⁰. The variables z and t are replaced by z and $\zeta = ct - z$ (the distance from the beam head), and all particles remain at constant ζ , since v_z is assumed to be the velocity of light. The frozen approximation is used in the field equations, and the same conductivity

model used in the VIPER⁸ code is employed. Beam dynamics are treated using standard particle simulation techniques. Current densities, fields, and conductivity are calculated on a polar grid (u, θ, ζ) with $u = \sqrt{r}$ as the radial variable. The lay-down scheme for the particles is quadratic in the radial and azimuthal variables and nearest grid point in the axial variable.

The ultra-relativistic approximations used in SARLAC lead to a code structure which is substantially different from "conventional" particle simulations. Information can only flow in one direction; toward larger ζ . Also, since individual particles always remain at the same axial position within the beam, the simulation can treat one slice at a time, thus reducing the number of particles in the simulation at any one time to $\sim 10^4$. Each beam slice is propagated forward in z until the maximum propagation range, $z_{\max}$ is reached. At this point, particles are loaded into the next slice, and the process is repeated. The current density J , conductivity σ , and potentials A and ϕ from the previous slice must be read from disk. The axial step $\Delta\zeta$ is variable, and the code has the option of subgridding the field and conductivity integrations on a finer axial mesh than is used for the particles. All diagnostics are done with post-processors. The dimensionless units used in VIPER and SIMM1 are employed throughout^{7,8}.

ELECTROMAGNETIC FIELDS

The frozen approximation to Maxwell's equations is performed in a gauge suggested by Lee¹¹. The equations are

$$\nabla_{\perp}^2(a + \phi) - \frac{\partial^2 a}{\partial \zeta^2} = -J_b + \sigma \frac{\partial a}{\partial \zeta}, \quad (1)$$

$$-\nabla_{\perp}^2 \frac{\partial a}{\partial \zeta} = -\nabla_{\perp} \cdot (\sigma \nabla_{\perp} \phi), \quad (2)$$

with the frozen condition

$$\frac{\partial}{\partial \zeta} \bar{A}_\perp = \frac{\partial a}{\partial z} = \frac{\partial \phi}{\partial z} = \frac{\partial \bar{A}_\perp}{\partial z} = 0 \quad (3)$$

and $a = A_z - \phi$.

The boundary conditions for a and ϕ are

$$a(r) = 0, \quad \zeta = 0$$

$$\phi(r) = 0, \quad \zeta = 0$$

$$a(\zeta) = 0, \quad r = R_{\max}$$

$$\phi(\zeta) = 0, \quad r = R_{\max}.$$

These conditions correspond to a beam propagating at the speed of light in a perfect conductor of radius $R_{\max}$.

The equations are similar in form to the EMPULSE¹² equations with an additional term $\partial^2 a / \partial \zeta^2$ in the first equation. A fully implicit method for solving these equations has been developed by Hui¹³. That field solver Fourier analyzes the azimuthal dependence of all quantities into a series of modes $\exp(im\theta)$ and performs a full complex matrix inversion, which is extremely time consuming and thus impractical for long simulation studies. The major advance of the SARLAC code is the development of a field solver which does not require a complete matrix inversion. The SARLAC field solver uses a predictor-corrector method which iterates about a solution obtained by assuming that the axi-symmetric ($m = 0$) conductivity dominates the solution. The $m = 0$ mode of any positive definite function is always larger than any other single mode and in the case of beam generated conductivity which is generated all along the beam axis, this mode is large compared to the other modes even for large excursions of the beam from axi-symmetry, as long as the front of the beam is on the axis.

Consider the first equation, and write it in the form

$$e^{-\int \sigma d\zeta'} \frac{\partial}{\partial \zeta} e^{\int \sigma d\zeta'} \frac{\partial a}{\partial \zeta} = \nabla_\perp^2 (a + \phi) + J_b. \quad (4)$$

Integrate this equation over the interval $\zeta_n \leq \zeta \leq \zeta_{n+1}$ to obtain

$$a^{n+1} = \left\{ a^n - a^{n-1} \frac{1}{2\sigma\Delta\zeta} (1 - e^{-\sigma\Delta\zeta}) + J_b \frac{1}{\sigma^2} (\sigma\Delta\zeta - (1 - e^{-\sigma\Delta\zeta})) \right. \\ \left. + \nabla_{\perp}^2 (a + \phi) \frac{1}{\sigma^2} (\sigma\Delta\zeta - (1 - e^{-\sigma\Delta\zeta})) \right\} / \left(1 - \frac{1}{2\sigma\Delta\zeta} (1 - e^{-\sigma\Delta\zeta}) \right), \quad (5)$$

where the superscript n represents the function evaluated at ζ_n . The conductivity, σ , is evaluated in the interval (ζ_n, ζ_{n+1}) . Rewrite Eq. (5) as

$$a^{n+1} = F(a^n, a^{n-1}; J_b, \sigma) \\ + \nabla_{\perp}^2 (a + \phi) f(\sigma), \quad (6)$$

where

$$F(a^n, a^{n-1}; J_b, \sigma) = \left\{ a^n - a^{n-1} \frac{1}{2\sigma\Delta\zeta} (1 - e^{-\sigma\Delta\zeta}) \right. \\ \left. + J_b \frac{1}{\sigma^2} (\sigma\Delta\zeta - (1 - e^{-\sigma\Delta\zeta})) \right\} / \left(1 - \frac{1}{2\sigma\Delta\zeta} (1 - e^{-\sigma\Delta\zeta}) \right) \quad (7)$$

and

$$f(\sigma) = \frac{(\sigma\Delta\zeta - (1 - e^{-\sigma\Delta\zeta})) / \sigma^2}{\left(1 - \frac{1}{2\sigma\Delta\zeta} (1 - e^{-\sigma\Delta\zeta}) \right)}. \quad (8)$$

Note that

$$f(\sigma) \longrightarrow \Delta\zeta / \sigma \quad \text{for } \sigma \text{ large}$$

$$f(\sigma) \longrightarrow (\Delta\zeta)^2 \quad \text{for } \sigma \text{ small.}$$

Equation (2) is simply differenced to give

$$-\nabla_{\perp}^2 \frac{a^{n+1} - a^n}{\Delta\zeta} = -\nabla_{\perp} \cdot (\sigma \nabla_{\perp} \phi). \quad (9)$$

Note that we have omitted the superscripts from some of the a and ϕ terms in Eqs. (6) and (9). By choosing these terms at the n th or $(n+1)$ th (or some combination of these levels), the differencing can be made explicit, or implicit to some formal accuracy. Our experience has been that the algorithms for these equations are numerically unstable if they are explicitly differenced. An implicit differencing can eliminate the instability, but at the expense of a complicated matrix inversion due to the azimuthal coupling of σ with the potentials. To avoid this, we have chosen instead to rewrite Eqs. (6) and (9) as

$$a^{n+1} - \nabla_{\perp}^2 (a + \phi) f_0(\phi) = F(a^n, a^{n-1}; J_b, \phi) + \nabla_{\perp}^2 (a + \phi) \left[f(\phi) - f_0(\phi) \right] \quad (10)$$

and

$$- \nabla_{\perp}^2 \frac{a^{n+1} - a^n}{\Delta \zeta} + \nabla_{\perp} \cdot (\sigma_0 \nabla \phi) = - \nabla_{\perp} \cdot (\sigma - \sigma_0) \nabla_{\perp} \phi, \quad (11)$$

where

$$f_0(\sigma) = \frac{1}{2\pi} \int_0^{2\pi} f(\sigma(\theta)) d\theta, \quad \sigma_0 = \frac{1}{2\pi} \int_0^{2\pi} \sigma(\theta) d\theta \quad (12)$$

Equations (10) and (11) are formally the same as Eqs. (6) and (9). However, since σ_0 does not vary in azimuth, the left-hand sides of these equations can be evaluated at the upper level without involving convolution sums, which leads to a tri-diagonal form for a^{n+1} and ϕ^{n+1} . The right-hand sides can be evaluated explicitly since the functions are known. The simplest differencing scheme leads to a first order algorithm. We have chosen a predictor-corrector method which is accurate to second order and quite stable. For the sake of brevity, we will not go into the details of

the differencing, but they are easily reproduced. We solve the equations in the Fourier transformed space (u, m, ζ) always keeping the right-hand sides explicit. The right-hand sides, then, can be evaluated in (u, θ, ζ) thus avoiding convolution sums on the right-hand sides as well. The method of adding and subtracting averaged terms to gain stability without full matrix inversions is similar to that used by Harned¹⁴ for a different set of equations.

NUMERICAL ISSUES

In SARLAC, the number of modes N_θ and radial mesh size Δu remain fixed throughout a run. Typically, $N_\theta = 16$ or 32 , and $\Delta u = 0.125 a_0^{1/2}$, where a_0 is a characteristic initial beam radius. The axial grid spacing $\Delta \zeta$ is specified for each slice at the beginning of the run. In general, $\Delta \zeta$ is allowed to increase with ζ since (at least in the linear regime) the ζ -variation is characterized by the dipole decay length, $\pi \sigma(r=0) a_0^2 / 2c^2$, which usually increases monotonically throughout the pulse. However, field solver tests have shown that the axial step size must often be reduced when the beam displacement is large. This is accomplished by subgridding the field and conductivity integrations. In most cases, $\Delta \zeta$ is chosen to be small enough that subgridding is rarely involved.

The beam current density J_b is intrinsically noisy because of the statistical fluctuations arising from the small number of particles in each $u-\theta$ grid cell. This is particularly troublesome near $u = 0$. Increasing the number of simulation particles per slice reduces noise problems but is computationally expensive. Other methods which we have employed include accumulating current densities on a coarser radial mesh than is used for the field solver and interpolating, averaging over the first few radial grid points, and using an azimuthal filtering technique near the origin.

Originally, we assigned random initial values of Θ to the particles but found that this procedure resulted in large initial noise levels for the hose instability and in substantial drifts in the beam head. The noise effects are reduced by loading the particles in pairs on opposite sides of the beam. If the velocities are also loaded symmetrically, the $m = 1$ azimuthal mode is eliminated in the initial stages of propagation. A small specified perturbation can be added to all particles in a given beam slice to start the hose instability in a controlled manner. Higher order Fourier modes can be suppressed by loading four or more particles with the appropriate symmetry. The elimination of higher order modes has not proven particularly useful since the nonlinear coupling of these modes is usually too weak to introduce significant hose growth.

The scattering of beam electrons by the neutral gas is known to play an important role in the evolution of the beam. SARLAC uses an algorithm originally developed by Chambers^{6,15} and modified by Hughes and Godfrey¹⁶ to provide a more accurate representation of the scattering process. Each beam particle is periodically scattered through a randomly chosen angle whose characteristic magnitude is determined by the energy and the gas density. After an initial transient phase, the beam reaches a quasi-static equilibrium. The beam radius then expands slowly due to scattering. If beam particles are loaded in pairs, a straightforward application of the scattering algorithm will eventually introduce significant noise and drifts at the beam head. These effects can be eliminated by scattering the particles in pairs. The random velocity $\Delta \vec{v}_i$ applied to a given particle at a given z step is balanced by adding $-\Delta \vec{v}_i$ to the particle with which it was originally paired. This technique has been highly successful in practice.

The simulation code is best suited for treating cases in which the hose displacement is a few times the nominal radius a_0 . The coordinate system is chosen to have the finest resolution in both the radial and azimuthal directions near the origin. For extremely large beam oscillations, when the beam displacement reaches a substantial fraction of the wall radius, the accuracy of the simulation is reduced, and the field solver is sometimes subject to numerical instabilities. The field solver instabilities appear to be triggered by conditions in which the local conductivity centroid gets far enough off the coordinate system axis that the conductivity is not dominated by the $m = 0$ mode. Usually this conductivity is generated by avalanche due to strong, localized, electric fields; such fields can arise when the hose motion is quite nonlinear¹. Evidence for very strong electric fields associated with nonlinear hose motion has been seen in the ETA experiments¹⁷, so the strong fields may be physical (up to a point). Considerable effort has been made to make the field solver more robust, and with careful differencing we have had some success. We have also found that these problems can be mitigated by using small ζ grids in regions where there are large hose amplitudes. Even so, we believe the code to be best suited for moderate hose oscillations.

NUMERICAL RESULTS

We have run the code under a variety of conditions. We show here the results of two runs; one for small perturbations in which the hose stays in the linear regime, saturates and decays, and one with moderate initial perturbations for which the hose grows and becomes nonlinear. The parameters for both sets of runs are

$a_0 = .5$ cm, the beam radius.

$I = 10$ kA, the beam current.

$\gamma = 100$, the beam energy.

$\zeta_r = 15$ cm, the beam current rise length.

$a_w = 81 a_0$, the outer radius of the simulation.

$y_{\text{pert}} = y_0 \sin 2\pi ((\zeta - \zeta_0)/\zeta_0)$, the initial perturbation over the

range

$$\zeta_0 < \zeta < 1.5 \zeta_0, \quad \zeta_0 = 10 \text{ cm.}$$

(Note, this perturbation is in the y direction.)

For the first run we used a very small initial hose amplitude $y_0 = 10^{-5} a_0$ which kept the hose oscillations linear over the length of the beam. For this case, the hose instability grows and saturates as seen in Fig. 1. Figure 2 shows a comparison of the saturation amplitude at various distances from the beam head with the results of the linearized VIPER code, which uses the multi-component model¹⁸ to represent the particle dynamics approximately. The oscillation frequency, growth rate, and saturation amplitude agree quite well with the VIPER code⁸.

The parameters chosen for the second run were the same except for a much larger initial amplitude $y_0 = 10^{-2} a_0$, so that the hose oscillations would become nonlinear. Figure 3 shows the growth of the hose through the x and y centroids of the beam. The dashed line is the y centroid which is

much larger than x because the perturbation is initialized in y . After the hose displacements reach the order of the beam radius, the frequency of the oscillation decreases. This is because the beam is spreading in radius and the wavelength of the oscillation scales as the radius. Figures 4-6 are beam particle plots at various distances of propagation.* We can see the development of the hose instability and the loss of the beam pinch as the instability becomes large.

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*To optimize the visual density of the plots, a randomly selected subset of the beam particles are plotted, rather than the entire beam.

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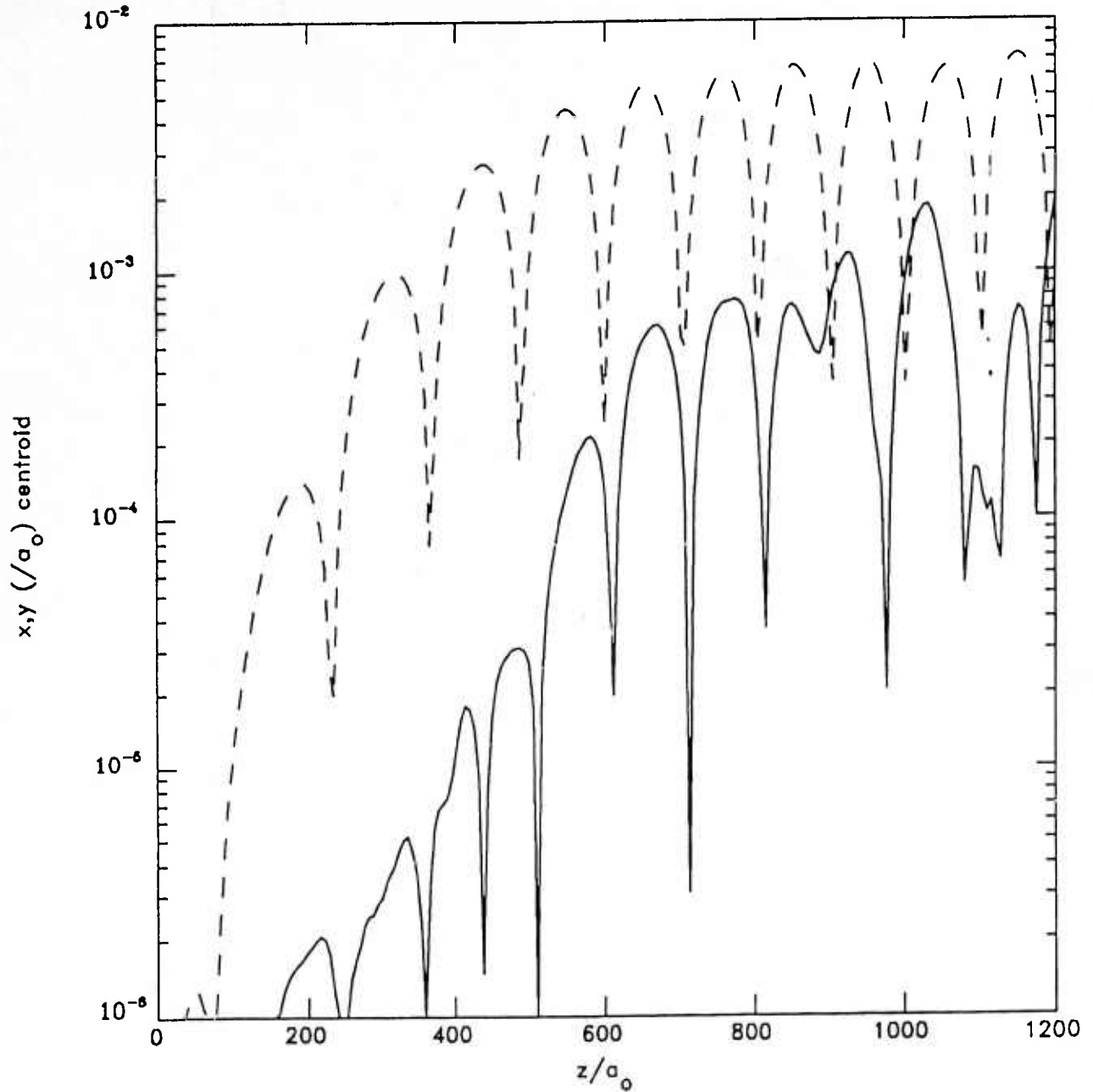


Figure 1. Plot of the beam x and y centroids at $\zeta = 50$ cm as a function of the beam propagation distance. The initial perturbation $y_0 = 10^{-5}$ so that saturation is reached while the hose instability is in the linear regime. The dashed line is the y centroid and the solid line is the x centroid. The initial perturbation is chosen in the y directions.

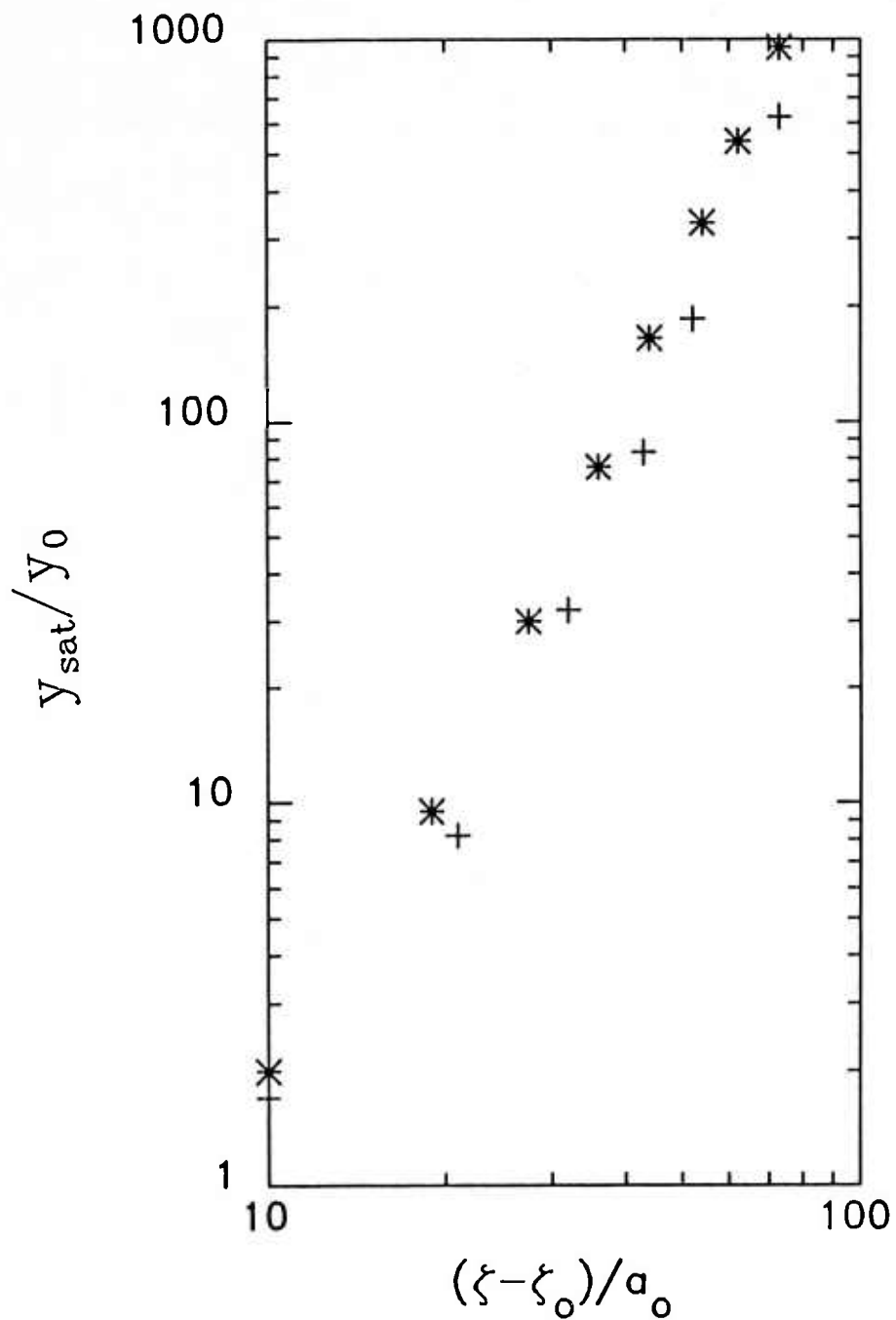


Figure 2. Plot of the saturated hose amplitude as a function of the distance back from the point of the initial perturbation. The SARLAC results are marked with *'s, while the VIPER results are marked with +'s.

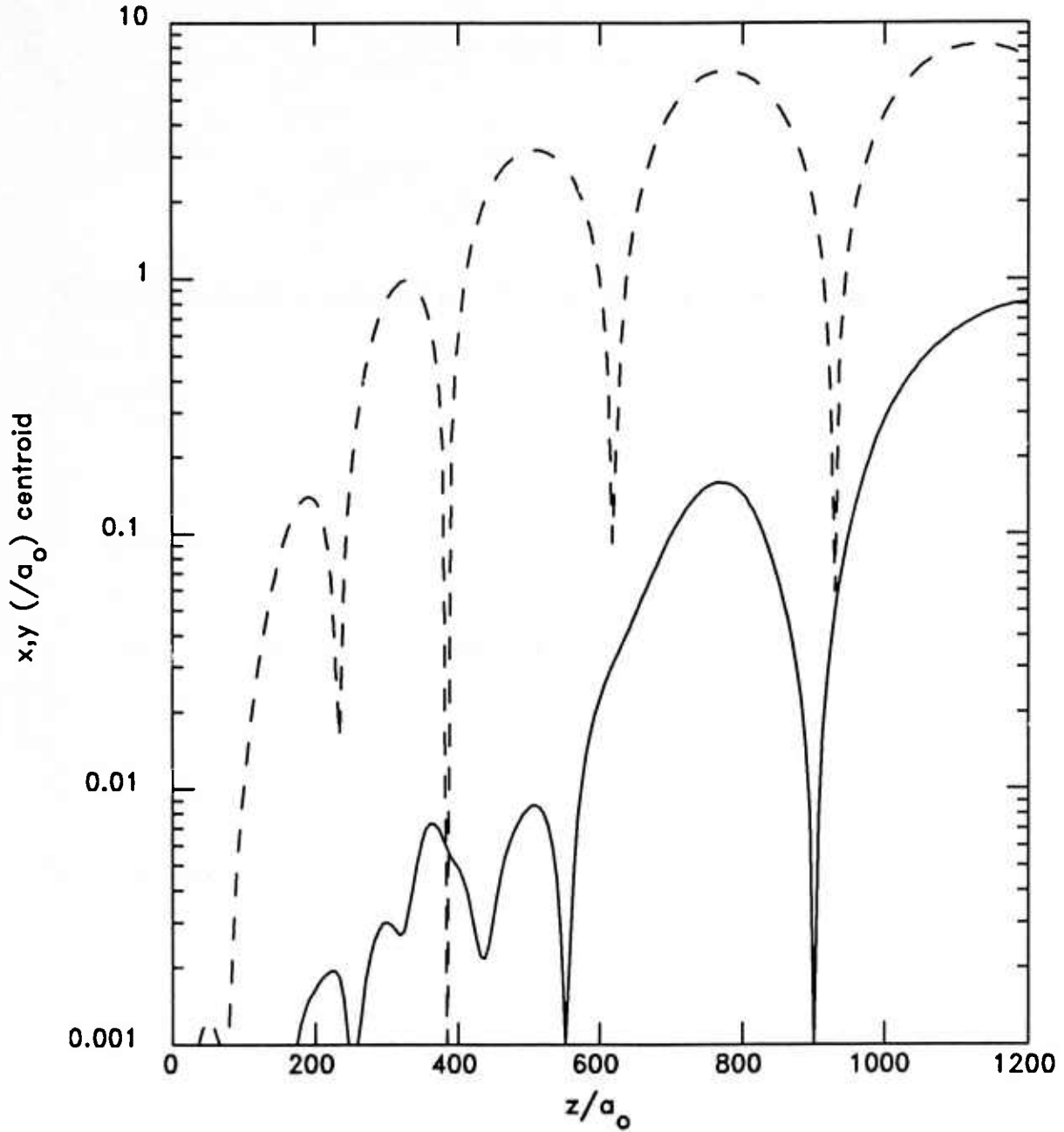


Figure 3. Plot of the beam x and y centroids at $\zeta = 50$ cm as a function of the beam propagation distance. The initial perturbation is $y_0 = 10^{-2}$ so that the hose instability becomes nonlinear. When the hose motion becomes large, the beam radius increases and the frequency of the oscillation decreases. Again, the dashed line is the y centroid and the solid line is the x centroid.

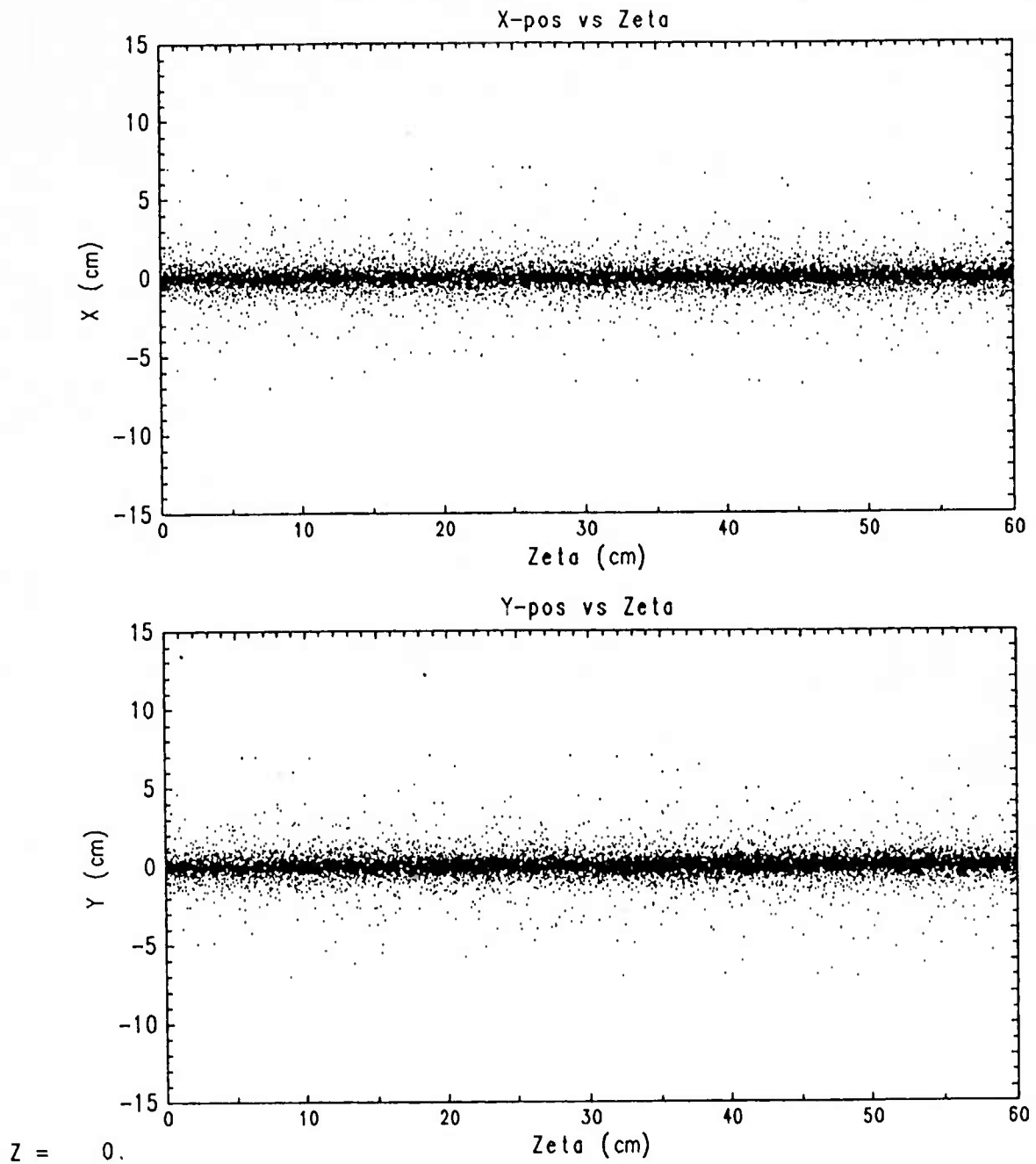
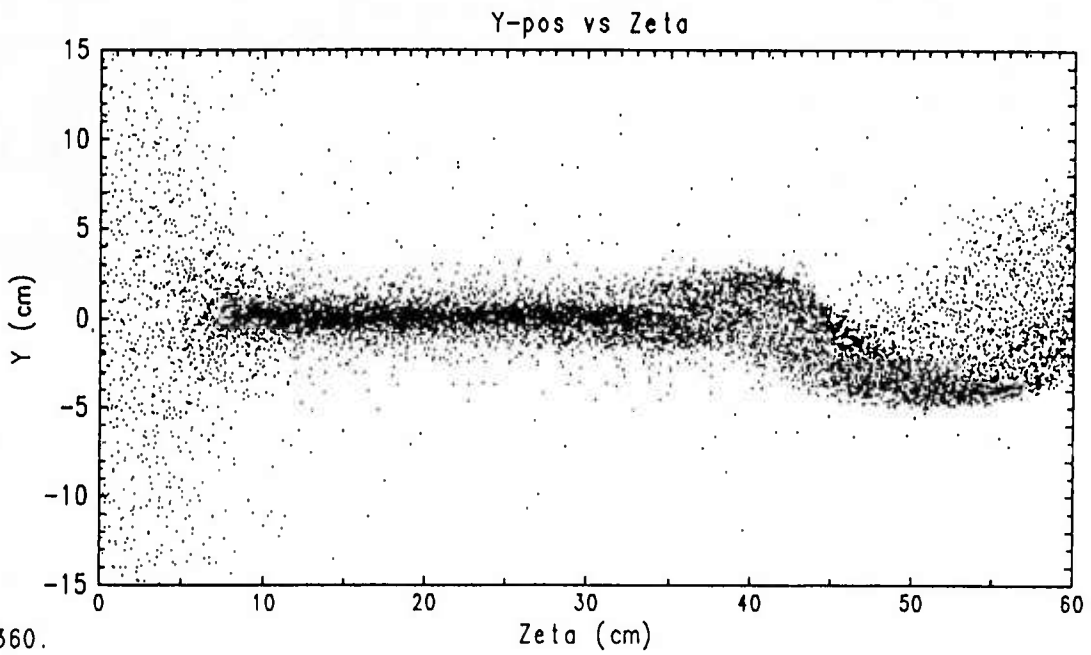
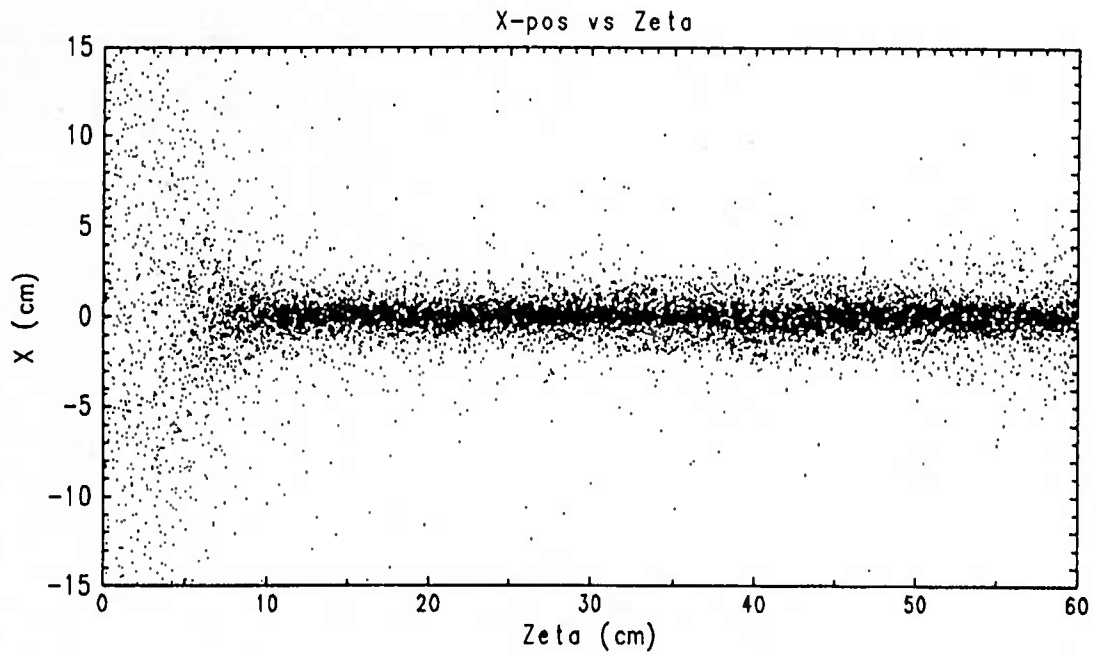
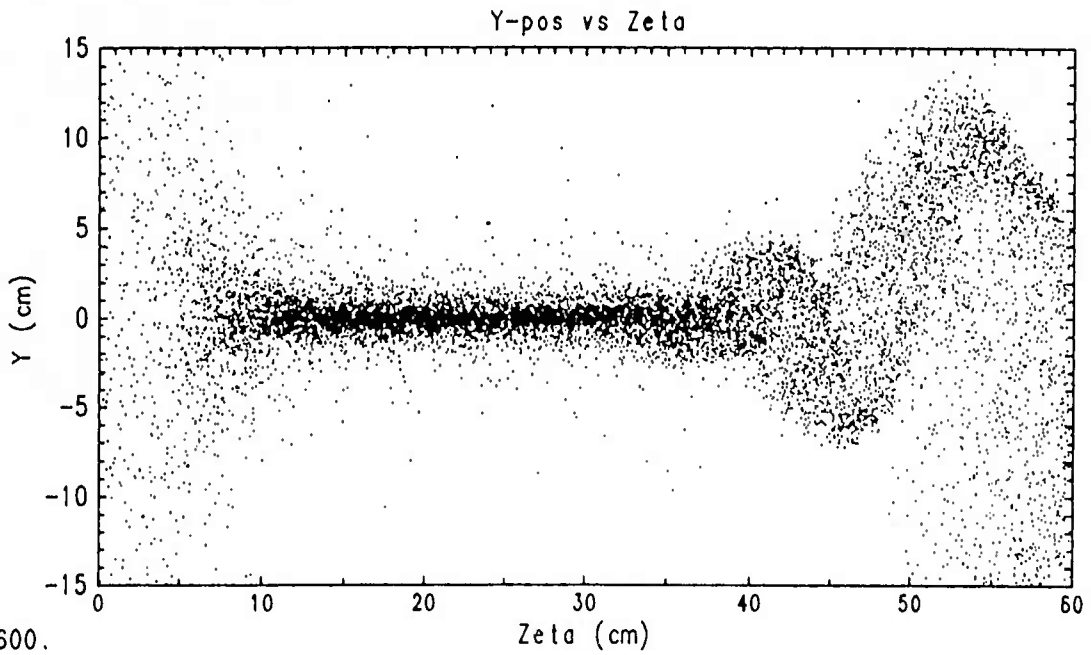
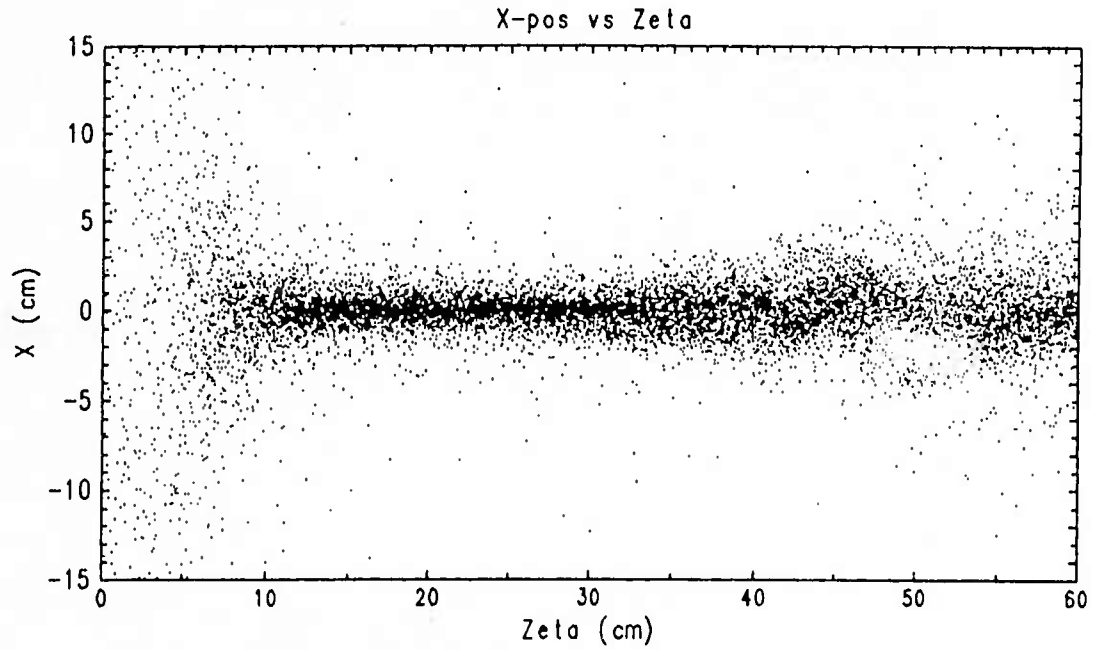


Figure 4. Plot of the beam particle positions at $z = 0$. The particles are loaded with a Bennett distribution. The beam current increases with increasing ζ but this is not indicated by increasing numbers of particles because the particles are weighted with the charge.



$z = 360.$

Figure 5. Plot of the beam particle positions at $z = 360$ cm. The beam head has begun to blow off and the hose perturbation has grown enough to be easily seen.



$Z = 600.$

Figure 6. Plot of the beam particle positions at $z = 600$ cm. The hose perturbation has grown so large that the tail of the beam is completely disrupted.

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