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REPORT NO. AFL 88-1-73

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AFOSR-TR- 88 - 0463

DIRECT-SOLUTION TECHNIQUES FOR VISCOUS FLOWS AND THEIR CONTROL

K.N. GHIA  
AND  
U. GHIA

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This research was supported by the Air Force Office of Scientific Research,  
under AFOSR Grant No. 87-0074.

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January 1988

88 5 32 180

REPORT DOCUMENTATION PAGE

1a. REPORT SECURITY CLASSIFICATION Unclassified		1b. RESTRICTIVE MARKINGS	
2a. SECURITY CLASSIFICATION AUTHORITY		3. DISTRIBUTION / AVAILABILITY OF REPORT Approved for Public Release; Distribution Unlimited.	
2b. DECLASSIFICATION / DOWNGRADING SCHEDULE			
4. PERFORMING ORGANIZATION REPORT NUMBER(S) AFL 88-1-73		5. MONITORING ORGANIZATION REPORT NUMBER(S) <b>AFOSR-TR- 88 - 0463</b>	
6a. NAME OF PERFORMING ORGANIZATION University of Cincinnati	6b. OFFICE SYMBOL (If applicable) --	7a. NAME OF MONITORING ORGANIZATION Air Force Office of Scientific Research/NA	
6c. ADDRESS (City, State, and ZIP Code) Dept. of Aerospace Engg. & Engg. Mechanics *Dept. of Mechanical & Industrial Engineering		7b. ADDRESS (City, State, and ZIP Code) Building 410 Bolling Air Force Base, DC 20332	
8a. NAME OF FUNDING / SPONSORING ORGANIZATION Air Force Office of Scientific Research	8b. OFFICE SYMBOL (If applicable) NA	9. PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER AFOSR 87-0074	
8c. ADDRESS (City, State, and ZIP Code) Building 410 Bolling Air Force Base		10. SOURCE OF FUNDING NUMBERS	
		PROGRAM ELEMENT NO. 61102F	PROJECT NO. 2307
		TASK NO. A1	WORK UNIT ACCESSION NO.
11. TITLE (Include Security Classification) Direct-Solution Techniques for Viscous Flows and Their Control			
12. PERSONAL AUTHOR(S) Kirti N. Ghia and Urmila Ghia*			
13a. TYPE OF REPORT Annual	13b. TIME COVERED FROM 10/15/86 TO 10/14/87	14. DATE OF REPORT (Year, Month, Day) January 1988	15. PAGE COUNT 37
16. SUPPLEMENTARY NOTATION --			
17. COSATI CODES		18. SUBJECT TERMS (Continue on reverse if necessary and identify by block number)	
FIELD	GROUP	SUB-GROUP	
			Unsteady Flow
			Temporally Deforming Geometry
			Active Control
			Direct Numerical Simulation
			Oscillating-flap Mechanism
			Unsteady Free Stream (over)
19. ABSTRACT (Continue on reverse if necessary and identify by block number)			
<p>The research performed under AFOSR Grant 87-0074 during the first year [October 1986-October 1987] of the Grant period is reviewed. Two main areas of research were pursued.</p> <p>In the area of active control of separated flows, the oscillating flap mechanism is examined by considering a backstep channel with an oscillating flap located in the primary reattachment region. A procedure has been developed for generating clustered conformal coordinates for this geometry with arbitrary orientations of the flap. Considerable effort was directed towards making the computational procedure efficient, so as to make it useful for repeated application needed for this temporally deforming geometry. The corresponding flow solution is presently being developed. Flow past an elliptic cylinder is studied with the objective of examining flow control via an unsteady free stream. (over)</p>			
20. DISTRIBUTION / AVAILABILITY OF ABSTRACT <input checked="" type="checkbox"/> UNCLASSIFIED/UNLIMITED <input type="checkbox"/> SAME AS RPT. <input type="checkbox"/> DTIC USERS		21. ABSTRACT SECURITY CLASSIFICATION Unclassified	
22a. NAME OF RESPONSIBLE INDIVIDUAL Dr. James D. Wilson		22b. TELEPHONE (Include Area Code) (202) 767-4935	22c. OFFICE SYMBOL NA

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K.N. GHIA\*

Department of Aerospace Engineering and Engineering Mechanics

U. GHIA\*

Department of Mechanical and Industrial Engineering

University of Cincinnati  
Cincinnati, Ohio

This research was supported by the Air Force Office of Scientific Research, Bolling Air Force Base, under AFOSR Grant No. 87-0074, with Dr. James D. Wilson as Technical Monitor.

Distribution of this report is unlimited.

\* Professor.

18. SUBJECT TERMS (Continued)

Elliptic Cylinder  
Conformal Mapping

Three-Dimensional Flows  
Large Data-Base Management

19. ABSTRACT (Continued)

*WFC*

The second area of research pursued deals with three-dimensional flows. An analysis and numerical solution procedure ~~have been~~ developed for the simulation of unsteady 3-D flows, using a self-consistent velocity-vorticity formulation. Considerable effort was also directed towards management of the large data-base associated with unsteady flows, especially ~~3-D~~ flows. This includes the consideration of concurrent I/O paging as well as appropriate output on the recently acquired IRIS superworkstation.

*Three dimensional*



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DTIC TAB	<input type="checkbox"/>
Unannounced	<input type="checkbox"/>
Justification	
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Distribution/	
Availability Codes	
Dist	Avail and/or Special
<i>A-1</i>	

## ABSTRACT

The research performed under AFOSR Grant 87-0074 during the first year [October 1986-October 1987] of the Grant period is reviewed. Two main areas of research were pursued.

In the area of active control of separated flows, the oscillating flap mechanism is examined by considering a backstep channel with an oscillating flap located in the primary reattachment region. A procedure has been developed for generating clustered conformal coordinates for this geometry with arbitrary orientations of the flap. Considerable effort was directed towards making the computational procedure efficient, so as to make it useful for repeated application needed for this temporally deforming geometry. The corresponding flow solution is presently being developed. Flow past an elliptic cylinder is studied with the objective of examining flow control via an unsteady free stream.

The second area of research pursued deals with three-dimensional flows. An analysis and numerical solution procedure have been developed for the simulation of unsteady 3-D flows, using a self-consistent velocity-vorticity formulation. Considerable effort was also directed towards management of the large data-base associated with unsteady flows, especially 3-D flows. This includes the consideration of concurrent I/O paging as well as appropriate output on the recently acquired IRIS superworkstation.

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## 1. RESEARCH OBJECTIVES

The objectives that were set for this grant consisted of the following:

- (i) To examine and achieve active control of two-dimensional (2-D) unsteady separated flows through direct numerical simulation using the unsteady Navier-Stokes (NS) equations,

and

- (ii) To study three-dimensional (3-D) unsteady, separated vortex-dominated flows by developing a direct implicit technique; this should also permit analysis of flow instabilities using model problems.

The research pursued in both of these areas since October 1986 and the progress achieved is described briefly in the next section.

## 2. RESEARCH PROGRESS

### 2.1 Control of Separated Flows

Active control/management of separated flows is studied by considering the flow in a backstep channel with an oscillating flap located near the downstream end of the primary separation bubble on the lower wall as shown in Fig. 1. Time-dependent boundary-oriented clustered conformal coordinates were generated, during the first half of this reporting period, using the Schwarz-Christoffel conformal mapping, followed by suitable contraction mappings to resolve the critical regions in this flow. A brief description of the method for developing the transformation and determining the coordinates for arbitrary orientations of the oscillating flap is given in Appendix. During the second half of this reporting period, effort has been focussed on determination of the flow in the temporally deforming domain of this flow.

### 2.1.1 Governing Equations

The problem is represented mathematically by the vorticity-stream function formulation of the time-dependent Navier-Stokes equations for 2-D incompressible flow. For a time-accurate solution of these equations for unsteady flow, the stream function  $\psi$  is obtained by a direct-solution method based on block-Gaussian elimination (BGE), for every time-step advance of the vorticity field  $\omega$ . With temporally deforming grids, even the linear differential equation for  $\psi$  takes on time-varying coefficients. Therefore, additional computational time is required not only for the evaluation of these coefficients but also for the solution of the corresponding partial differential equation by direct inversion. By contrast, for efficiency of the BGE procedure, the differential operator for  $\psi$  must remain time-invariant. Conformal mapping allows this to be achieved even in the presence of temporally deforming grids, as briefly described next.

In Cartesian coordinates, the stream-function equation has the form

$$\psi_{xx} + \psi_{yy} = -\omega \quad (1)$$

where the source function is the vorticity  $\omega$  which is a function of  $x$ ,  $y$  and  $t$ , i.e.,

$$\omega = \omega(x,y,t) \quad (2)$$

In conformal coordinates  $(\xi, \eta)$ , this equation can be represented as

$$\psi_{\xi\xi} + \psi_{\eta\eta} = -h^2\omega \quad (3)$$

where

$$h = h_1 = h_2 \quad (4)$$

is the scale factor of the conformal mapping

$$\xi + i\eta = f(x+iy) \quad (5)$$

In terms of complex variables, the conformal mapping and its scale factor become

$$z = f(\zeta) \quad , \quad h = \left| \frac{df}{d\zeta} \right| = \left| \frac{dz}{d\zeta} \right| \quad (6a,b)$$

where

$$\zeta = \xi + i\eta \quad \text{and} \quad z = x + iy \quad . \quad (7a,b)$$

For a temporally deforming boundary-aligned conformal coordinate system, the scale factor  $h$  varies with time, in addition to being spatially varying. However, by virtue of the special form of the stream function equation (3) that results with a conformal mapping, this time-varying  $h$  can be absorbed in the source function of this equation leading simply to the equation

$$\psi_{\xi\xi} + \psi_{\eta\eta} = G(\xi, \eta, t) \quad (8a)$$

where

$$G(\xi, \eta, t) \triangleq -h^2 \omega \quad . \quad (8b)$$

This leaves the stream-function equation with time-invariant coefficients. It is important to note that any clustering transformations, introduced in Eq. (8a) for the purpose of resolving the length scales of the problem, must be time-independent in order for the final form of the equation to possess time-independent coefficients. The clustering transformations used in the present work are of the form  $\xi = \xi(S)$  ,  $\eta = \eta(N)$  where  $(S, N)$  are the final computational coordinates.

The transport equation for the vorticity  $\omega$  for 2-D incompressible flow is written in vector form as

$$\omega_t + \bar{V} \cdot \nabla \omega = \frac{1}{\text{Re}} \nabla^2 \omega \quad (9)$$

Here,  $\bar{V}$  is the velocity vector with components  $u$  and  $v$  along the conformal-coordinate directions  $\xi$  and  $\eta$ , respectively, related to the stream function  $\psi$  as follows:

$$u = \frac{1}{h} \frac{\partial \psi}{\partial \eta} ; \quad v = -\frac{1}{h} \frac{\partial \psi}{\partial \xi} \quad (10)$$

The time-dependent conformal mapping can be expressed as

$$\xi = \xi(x, y, t)$$

$$\eta = \eta(x, y, t)$$

$$\tau = t$$

where  $\tau$  is the transformed time coordinate. Hence, the time derivative term  $\omega_t$  in Eq. (9) transforms as

$$\omega_t = \omega_\tau + \xi_t \omega_\xi + \eta_t \omega_\eta \quad (11)$$

or, finally, as

$$\omega_t = \omega_\tau + \frac{1}{h^2} [(x_\eta y_\tau - y_\eta x_\tau) \omega_\xi + (x_\xi y_\tau - y_\xi x_\tau) \omega_\eta] \quad (12)$$

The spatial derivatives of  $x, y$  are easily evaluated using the complex quantity  $dz/dz_c$ . The grid speed terms  $x_\tau, y_\tau$  are determined using the mapping at two successive levels of time.

### 2.1.2 Boundary Conditions

The wall boundary conditions are obtained from the condition of zero slip along the non-porous walls of the backstep channel. These are then expressed in terms of the stream function  $\psi$ , as follows:

Along  $\eta = \eta_{\min}$  and  $\eta = \eta_{\max}$ ,

$$\psi_\xi = -hv ; \quad \psi_\eta = hu \quad (13a,b)$$

For points on a stationary non-porous wall, these lead to the conditions that, at these points,

$$\psi|_{\eta_s} = 0 \quad \text{and} \quad \psi_{\eta}|_{\eta_s} = 0 \quad (14a,b)$$

where  $\eta_s$  denotes stationary-boundary points. Equation (14a) implies that the boundary is a streamline. For points on a moving boundary, the right-hand sides of either Eq. (13a) or Eq. (13b) or both may be non-zero, even when the boundary is non-porous. This is easily confirmed by examining the streamline pattern around a cylinder moving at a constant velocity in an otherwise stagnant fluid (Fig. 2). If, at points A and B on the cylinder,  $\psi = \psi_1$  at A and  $\psi = \psi_2$  at B, then  $\psi$  is not constant on the cylinder surface. Hence, for the present problem,  $\psi$  along the moving flap is no longer zero even though it is zero elsewhere on the lower boundary of the channel. The distribution of  $\psi$  along the moving flap is obtained by using Eq. (13) together with information about the flap motion, i.e.,

Along the flap:

$$u_F = 0 \quad \text{and} \quad v_F = r\dot{\theta} \quad (15a,b)$$

where  $r$  is the distance along the flap measured from its base (Fig. 3), and  $\dot{\theta}$  is the instantaneous rate of its rotation. The specified motion of the flap will provide  $\dot{\theta}$ , whereas  $r$  is obtained from  $\xi$  and  $h$  for the conformal mapping. Use of Eqs. (15a,b) in Eqs. (13a,b) leads to

$$\psi_2 - \psi_1 = - \int_{\xi_1}^{\xi_2} h v_F d\xi \quad \text{and} \quad \psi_{\eta}|_{\eta_F} = 0 \quad (16a,b)$$

As regards concerns about accuracy of the integration indicated in Eq. (16a), it is important to note that  $\psi = 0$  at points adjoining both sides of

the base of the flap. This provides a check on the integration accuracy and is used to formulate the discretized integration.

Another concern that needs to be dealt with is the following. The grid points in the computational plane are uniformly distributed and fixed for all time. With time-dependent clustering transformations, the grid-point distribution in the doubly-infinite straight-channel plane is also fixed for all time. The corresponding distributions along the flap in the physical plane at two successive time levels may not, in general, be related by the physical motion of the flap; see Fig. 4. For a straight flap, this can be treated without difficulty, using simple interpolation. For curved flap resulting from possible binding, this requires careful consideration.

All of the above analysis has been incorporated into the flow program and is being made operational. Some preliminary results are anticipated within the next few weeks, unless any additional problems are encountered and need to be resolved. Current plans are for a paper based on this work to be presented at the National Fluid Dynamics Congress scheduled for July, 1988, in Cincinnati, Ohio.

### 2.1.3 Flow Control for Axisymmetric Configurations

For 2-D rectangular configurations, the stream function equation possesses constant coefficients. This is not so for axisymmetric configurations where some of the coefficients in the equation governing the Stokes stream function contain the radius  $r$  in an essential manner. For a given computational point, the value of  $r$  changes with time as the boundary shape alters. This implies that the Schwarz-Christoffel mapping obtained directly as  $dz/d\zeta$  needs to be integrated at every time step. Furthermore, this implies that the elimination phase of the BGE method needs to be repeated at every time step. The time-consuming nature of this phase has a

large adverse effect on the efficiency of the overall procedure. The possible use of the MG-SI (Multi-Grid Strongly Implicit) procedure developed earlier by U. Ghia et al. [1983, 1987] is being explored for the stream function equation for the axisymmetric configuration of a pipe-orifice with bending of the orifice plate. The preliminary findings from this effort are summarized in Table I, and indicate that the MG-SI scheme is a viable procedure for solution of elliptic equations with time-dependent coefficients.

## 2.2 Unsteady Free Stream - A Control Mechanism

Aerodynamic forces can be significantly affected by the unsteady nature of the separation and reattachment phenomena on the suction surface of an aerodynamic body at high angle of attack. Present understanding of the underlying mechanisms is quite limited. A study of the flow past an elliptic cylinder at angle of attack was initiated around July 1987, with the objective of studying flow control by subjecting the elliptic cylinder to a time-dependent free stream.

As a first phase of this work, the flow past an elliptic cylinder is being studied, using the two-dimensional unsteady incompressible Navier-Stokes analysis of K. Ghia, Osswald and U. Ghia [1985]. Clustered conformal transformations are developed to obtain appropriate surface-oriented coordinates for an elliptic cylinder. The grid-clustering transformations implemented attempt to resolve the multiple disparate length scales of the unsteady separated flow; a typical grid consists of (229x45) mesh points.

The results of the present unsteady analysis are compared, qualitatively, with the experimental data of Izumi and Kuwahara [1983] in Figs. 5 and 6. For the case of an elliptic cylinder, with 50% thickness, angle of attack  $\alpha = 20^\circ$  and Reynolds number  $Re = 369$ . Before discussing

these figures, it is appropriate to point out the conditions under which the two sets of data are obtained, so the qualitative comparison carried out is in proper perspective. In the experiments, an electrolytic precipitation method was used to obtain flow visualization results; Taneda [1977] has shown that such an approach leads to visualization of 'integrated streaklines' which, in turn, show the 'vorticity' layers. Further, although the time scales are non-dimensionalized in the same way, the cylinder was accelerated over a finite amount of time in the experiment, whereas in the present analysis, the cylinder was impulsively started from rest. Finally, the orientation of the two sets of results shown is also different; the experimental photographs show a horizontal free stream and the cylinder at an angle of attack, but the present computational results are plotted with the axis of the cylinder being horizontal and the oncoming flow is at the appropriate angle of attack.

In Fig. 5, the instantaneous flow field results for "vorticity" as stated above, are shown for characteristic time  $T = 0.86$ . In the photograph as well as the plot, a counterclockwise rotating vortex is beginning to shed off of the lower surface near the trailing edge, while a clockwise rotating vortex sheet is reaching across the upper surface and curls down towards the trailing edge. In Fig. 6, the results are depicted at  $T = 1.69$ . Both sets of results show that the counterclockwise rotating vortex, that was initially seen being shed at  $T = 0.86$ , has moved downstream away from the cylinder. Figure 6 also shows the vortical structure positioned just over the upper portion of the trailing edge and the vortex sheet from the leading edge curling up and over this vortical structure in both the photograph as well as the plot of present results.

Preliminary results are obtained for flow past an elliptic cylinder with 25% thickness at an angle of attack  $\alpha = 15^\circ$  and  $Re = 1000$ . The flow solutions monitored showed that the cylinder, which is impulsively started from rest, goes through a highly unsteady phase until  $T \approx 17$ , after which the asymptotic state in the form of a limit cycle is reached. Further detailed examination of the limit cycle solution showed alternate shedding of vortices from the suction and pressure surfaces. The instantaneous stream function and vorticity are plotted in Fig. 7 (a-d) for the above configuration at  $T = 28.47$  corresponding to the maximum-lift instant and  $T = 29.106$  for the minimum-lift instant in the same cycle. The corresponding instantaneous velocity vectors for the two cases are depicted in Fig. 7 (e-f).

### 2.3 Three-Dimensional Incompressible Separated Flow

This study has continued using the model problem of the shear-driven flow within a 3-D rectangular cavity. Preliminary results using the direct inversion methodology for the unsteady Navier-Stokes equations were obtained during the first half of this report period culminating in the paper presented by Osswald, K. Ghia and U. Ghia [1987] at the 8th AIAA CFD Conference, Honolulu, Hawaii, appearing in the conference proceedings. Results obtained on the Department's Perkin Elmer 3250 using the serial research version of the code were presented for a (17x17x17) grid. This proved the formulation of the unsteady Navier-Stokes problem as well as the efficiency of the direct, inversion numerical procedures.

Since then the code has been fully vectorized for the CYBER 205 computer, resulting in efficient direct numerical simulation capabilities for highly unsteady 3-D viscous flows. Memory management considerations are currently being investigated using a two pronged approach.

Direct, inversion methodologies trade memory utilization (a relatively inexpensive resource) for CPU efficiency (still a scarce resource). For fine 3-D grids (33x33x33) to (65x65x65) the coefficient matrices employed to gain the efficiency of the direct inversion procedures exceed the in-core memory conveniently obtainable on the CYBER 205 at NASA/Langley. A two-pronged approach is being pursued to circumvent this difficulty. First, the strong numerical stability of the direct solution procedures, demonstrated in Osswald et al. [1987], permits the storage of these coefficient matrices in half-precision (32 bit) words rather than the full-precision (64 bit) words currently employed. This effectively doubles the in-core storage conveniently obtainable on the CYBER 205 system for holding the coefficient matrices without further recoding. In addition, use of the concurrent I/O capability of the CYBER 205 system is being investigated with the concept of implementing program controlled concurrent paging through this data base simultaneously with the solution calculations. This could greatly reduce the in-core storage requirement of the direct solution techniques placing the burden instead upon the concurrent I/O processor. Finally, access to the CRAY-2 facility at NASA/Ames is being pursued where significantly more memory is available to the single user.

Results of this memory management exercise as well as fine grid flow results for the driven cavity and 3-D backstep channel geometries has been submitted for presentation at the ICNMF '88 conference at Williamsburg, Virginia. The flow inside a backstep channel with finite spanwise extent will be examined next. For this geometry, careful laser-Doppler velocimetry results are available for the entire range of flow, i.e., for laminar, transition and turbulent flows.

### 3. RESEARCH FORECAST

As described in the preceding section, both areas of research pursued have progressed well to meet the objectives of this study. During the second year of the grant period, i.e. October 15, 1987 - October 14, 1988, effort will continue as follows:

- a. The active-flow reattachment-control study will be completed by carrying out a parametric study of the backstep channel flow with control flap to achieve optimum control. This effort will be coordinated with that of Nagib at the Illinois Institute of Technology. Various scenarios of flap geometry, location and motion will be examined in order to determine the optimum configuration of this flow-control mechanism. Control of unsteady separated flow will also be examined via the elliptic cylinder configuration with an unsteady free stream.
- b. Concurrently, the 3-D incompressible unsteady flow analysis and solution procedure will be applied to the flow in a rectangular cross-section duct with a backward facing step and verified by comparing the predictions with the corresponding laser-Doppler velocimetry (LDV) data available from the University of Karlsruhe and Stanford University in order to obtain insight into the mechanism of shear-layer instability, transition and the strange-attractor theory of turbulence.

Effort will also be directed towards gaining better familiarity with effective usage of the IRIS workstation. This equipment is especially useful in the present unsteady flow research, particularly, the 3-D work.

#### 4. REFERENCES

Note: Superscript (\*) designates work supported, in part, by AFOSR Grant 87-0074.

- Davis, R.T., (1983), "Numerical Methods for Coordinate Generation based on a Mapping Technique," in Computational Methods for Turbulent, Transonic and Viscous Flows, Editor: J.A. Essers, Hemisphere Publishing Corporation.
- Ghia, K.N., Osswald, G.A. and Ghia U., (1985), "Analysis of Two-Dimensional Incompressible Flow Past Airfoils Using Unsteady Navier-Stokes Equations," Numerical and Physical Aspects of Aerodynamic Flows: Vol. III, Editor: T. Cebeci, Springer-Verlag, New York, January 1985.
- Ghia, U., Ghia, K.N. and Ramamurti, R., (1983), "Multi-Grid Solution of Neumann Pressure Problem for Viscous Flows Using Primitive Variables," AIAA Paper 83-0557.
- Ghia, U., Ramamurti, R. and Ghia, K.N., (1988), "Solution of Neumann Pressure Problem in General Orthogonal Coordinates Using Multi-Grid Technique," to appear in AIAA Journal.
- \*Ghia, U., Zuo, L. and Ghia, K.N., (1988), "Towards Active Control of Flow Reattachment via Direct Simulation of Separated Flows in Temporally Deforming Geometries," paper under preparation.
- Izumi, K. and Kuwahara, K., (1983), "Unsteady Flow Field, Lift and Drag Measurements of Impulsively Started Elliptic Cylinder and Circular-Arc Airfoil," AIAA Paper No. 83-1711.
- \*Osswald, G.A., Ghia, K.N. and Ghia, U., (1987), "A Direct Algorithm for Solution of Incompressible Three-Dimensional Unsteady Navier-Stokes Equations," AIAA Paper 87-1139-CP, presented at AIAA 8th Computational Fluid Dynamics Conference, Honolulu, Hawaii, June 1987.
- Taneda, S., (1977), "Visual Study of Unsteady Separated Flows Around Bodies," Prog. Aerospace Sci., Vol. 17, pp. 287-348.
- \*Zuo, L., (1987), "Efficient Numerical Grid-Generation Method Based on Conformal Mapping," M.S. Thesis, Department of Aerospace Engineering and Engineering Mechanics, University of Cincinnati, Cincinnati, Ohio, December.

## 5. M.S. THESES COMPLETED

Collopy, G.B., "Determination of Flow, Including Discharge Coefficients, In a Pipe-Orifice Using Unsteady, Navier-Stokes Equations," M.S. Thesis, Department of Aerospace Engineering and Engineering Mechanics, University of Cincinnati, Cincinnati, Ohio, June 1987.

Liu, C.A., "Study of a Two-Dimensional Viscous Flow Past a Circular Cylinder Using Unsteady Navier-Stokes Equations," M.S. Thesis, Department of Aerospace Engineering and Engineering Mechanics, University of Cincinnati, Cincinnati, Ohio, June 1987.

Rocker, M., "Analysis and Development of Conformal Grid Generation Technique for Flow Past Arbitrary Airfoils at High Incidence," M.S. Thesis, Department of Aerospace Engineering and Engineering Mechanics, University of Cincinnati, Cincinnati, Ohio, June 1987.

Zuo, L., "Efficient Numerical Grid-Generation Methods Based on Conformal Mapping," M.S. Thesis, Department of Aerospace Engineering and Engineering Mechanics, University of Cincinnati, Cincinnati, Ohio, December 1987.

## 6. PAPERS AND REPORTS PUBLISHED

### BOOKS AND MONOGRAPHS

- Ghia, K.N., Ghia, U., Lamb, J.P., Editors; Unsteady Flow Separation, FED-Vol 52, ASME June 1987.
- Ghia, K.N., and Ghia, U., "Elliptic Systems: Finite-Difference Method," Chapter in Handbook on Numerical Heat Transfer, Editors: W.J. Minkowycz et al., John Wiley and Sons, 1988.
- Ghia, U. and Ghia, K.N., "Navier-Stokes Equations for Incompressible Flow," Section of Chapter in Handbook of Fluids and Fluid Machinery, Editor: A. Fuchs, McGraw Hill, 1987.
- Ghia, K.N., Osswald, G.A., and Ghia, U., "Analysis of Two-Dimensional Incompressible Flow Past Airfoils Using Unsteady Navier-Stokes Equations," Chapter in Numerical and Physical Aspects of Aerodynamic Flows: Vol. III, Editor: T. Cebeci, Springer-Verlag, New York, December 1986.

### PAPERS AND REPORTS

- Ghia, K.N., Osswald, G.A. and Ghia, U., "Analysis of Incompressible Massively Separated Viscous Flows Using Navier-Stokes Equations," accepted for publication in International Journal for Numerical Methods in Fluids, 1988.
- Ghia, U., Ramamurti, R. and Ghia, K.N., "Solution of Neumann Pressure Problem in General Orthogonal Coordinates Using Multi-Grid Technique," to appear in AIAA Journal, 1988.
- Ghia, K.N. and Ghia, U., "Analysis of Low-Speed Multidimensional Viscous Flows," Proceedings of AFOSR/FJSRL/DFAM/U. COLORADO Workshop II on Unsteady Separated Flows, Colorado Springs, Colorado, July 1987.
- Ghia, K.N., Ghia, U. and Shin, C.T., "Study of Fully Developed Incompressible Flow in Curved Ducts Using a Multigrid Technique," Journal of Fluids Engineering, Vol. 109, No. 3, 1987, pp. 318-338.
- Ghia, K.N., Liu, C.A., Ghia, U., Osswald, G.A., "Analysis of Unsteady Wake of a Circular Cylinder Using Navier-Stokes Equations," Unsteady Flow Separation, FED Vol. 52, pp. 187-190, 1987.
- Osswald, G.A., Ghia, K.N., and Ghia, U., "A Direct Algorithm for Solution of Incompressible Three-Dimensional Unsteady Navier-Stokes Equations," AIAA CP 874, pp. 408-421, 1987.
- Ghia, K.N., Ghia, U., Osswald, G.A. and Liu, C.A., "Simulation of Separated Flow Past a Bluff Body Using Unsteady Navier-Stokes Equations," Boundary Layer Separation, Editors: F.T. Smith and S. Brown, North Holland, pp. 251-267, 1987.
- Ghia, K.N. and Ghia, U., "Analysis of Three-Dimensional Viscous Internal Flows," Aerospace Engineering and Engineering Mechanics Report AFL 87-6-71, University of Cincinnati, June 1987.
- Ghia, K.N., "Specialized Instrumentation for Computational Fluid Dynamics Research," Aerospace Engineering and Engineering Mechanics Report AFL 87-6-72, University of Cincinnati, June 1987.
- Ghia, K.N. and Ghia, U., "Direct-Solution Technique for Viscous Flow and Their Control," Aerospace Engineering and Engineering Mechanics Report AFL 87-7-73, University of Cincinnati, July 1987.

- Oswald, G.A., Ghia, K.N. and Ghia, U., "Simulation of Buffeting Stall for a Cambered Joukowski Airfoil Using a Fully Implicit Method," Lecture Notes in Physics, Editors: F.G. Zhuang and Y.L. Zhu, Vol. 264, pp. 516-522, Springer-Verlag, 1986.
- Ghia, K.N., Oswald, G. A. and Ghia, U., "Simulation of Self-Induced Motion in the Near-Wake of a Joukowski Airfoil," Lecture Notes in Engineering, Edited by K. Kuwahara, R. Mendez and S. A. Orszag, Vol. 24, pp. 18-132, 1986.
- Ghia, U., Ramamurti, R. and Ghia, K.N., "A Semi-Elliptic Analysis of Internal Viscous Flows," Lecture Notes in Engineering, Edited by K. Kuwahara, R. Mendez and S. A. Orszag, Vol. 24, pp.108-117, 1986..

## 7. SCIENTIFIC INTERACTIONS - SEMINARS AND PAPER PRESENTATIONS

### Invited Lectures:

- Ghia, K.N., presented at the Second Nobeyama Workshop on Fluid Dynamics and Supercomputers, Tokyo, Japan, 1987.
- Ghia, U., presented at the Second Nobeyama Workshop on Fluid Dynamics and Supercomputers, Tokyo, Japan, 1987.
- Ghia, K.N. and Ghia, U., presented at International Symposium on Computational Fluid Dynamics, Sydney, Australia, August 1987.
- Ghia, K.N., presented Two Lectures in CFD Lecture Series at Indian Institute of Technology, Bombay, India, August 1987.
- Ghia, U., presented Two Lectures in CFD Lecture Series at Indian Institute of Technology, Bombay, India, August 1987.
- Ghia, K.N. and Ghia, U. presented at DARPA-URI Symposium on Periodic and Aperiodic Phenomenon Behind Circular Cylinders, Newport, RI, July 1987.
- Ghia, K.N. presented at Department of Mechanical Engineering and Applied Mechanics, University of Rhode Island, Providence, RI, July 1987.
- Ghia, K.N. presented at University of California at Davis, Davis, California, June 1987.

### Paper Presentations

- Ghia, K.N., Ghia, U. and Osswald, G.A., "Analysis of Low-Speed Multidimensional Unsteady Viscous Flows," presented at Workshop II on Unsteady Separated Flows, Colorado Springs, Colorado, July 1987.
- Ghia, U., Ramamurti, R. and Ghia, K.N., "Study of Viscous Flows with Upstream Interaction Using Interacting PNS Equations," presented at the R.T. Davis Symposium on Computational Mechanics, Cincinnati, Ohio, June 1987.
- Ghia, K.N., Liu, C.A., Ghia, U. and Osswald, G.A., "Analysis of Unsteady Wake of a Circular Cylinder Using Navier-Stokes Equations," presented at ASME Forum on Unsteady Flow Separation, Cincinnati, Ohio, June 1987.
- Osswald, G.A., Ghia, K.N., and Ghia, U., "A Direct Algorithm for Solution of Incompressible Three-Dimensional Unsteady Navier-Stokes Equation," AIAA 87-1139-CP, presented at AIAA 8th Computational Fluid Dynamics Conference, Honolulu, Hawaii, June 1987.
- Collopy, G., Ghia, K.N., Ghia, U. and Osswald, G.A., "Determination of Discharge Coefficients for a Pipe-Orifice Using the Navier-Stokes Equations," presented at AIAA 13th Annual Minisymposium on Aerospace Science and Technology, Dayton, Ohio, March 1987.
- Zuo, L., Ghia, U. and Ghia, K.N., "Efficient Numerical Grid Generation Methods Based on Conformal Mapping," presented at AIAA 13th Annual Minisymposium on Aerospace Science and Technology, Dayton, Ohio, March 1987.
- Rocker, M. and Ghia, K.N., "Analysis of High Incidence Aerodynamic Flow Past Arbitrary Lifting Airfoils Using Unsteady Navier-Stokes Equations," presented at AIAA 13th Annual Minisymposium on Aerospace Science and Technology, Dayton, Ohio, March 1987.
- Ghia, K.N., Ghia, U., Liu, C.A. and Osswald, G.A., "Study of Unsteady Wake Behind a Circular Cylinder Using Time-Dependent Simulation," Bull. Am. Phys. Soc., Vol. 31, No. 10, 1986, pp. 1746; presented at the 39th APS Meeting, Columbus, Ohio, November, 1986.

TABLE I

Computational Effort Units for BGE and MG-SI Solution of  
Stream-Function Equation for Axisymmetric Flow

<u>Method</u>	<u>Phase 1</u>	<u>Phase 2</u>	<u>Total</u>
BGE	6	1	7
MG-SI	2	2	4

Note 1: The effort quoted is referred to the CPU time required for Phase 2 of the BGE method for the axisymmetric orifice-pipe problem using a (257x33) grid.

Note 2: The test was conducted at the initial stage of the flow problem. During later stages, the MG-SI-phase 2 should require a reduced CPU time, whereas the BGE CPU time always remains fixed.

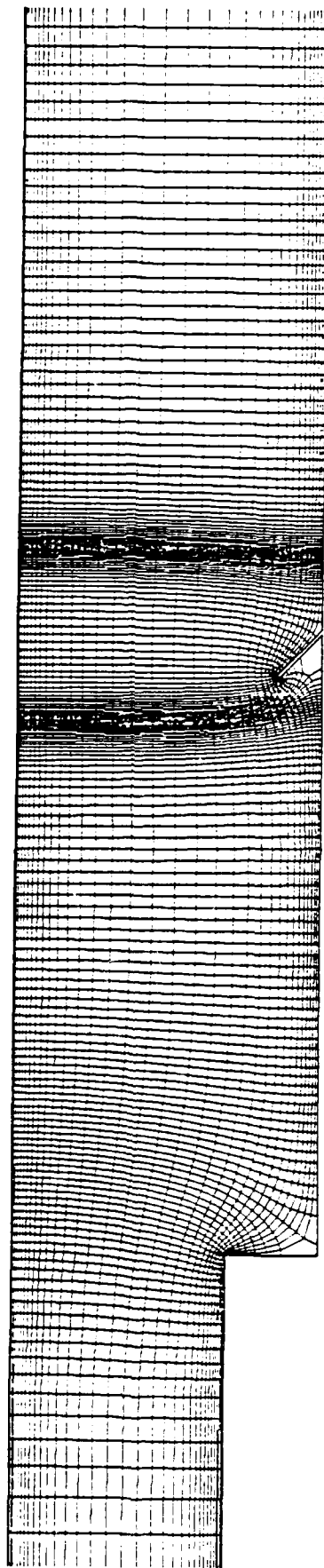


FIG. 1. CLUSTERED CONFORMAL BOUNDARY-ALIGNED GRID FOR BACKSTEP CHANNEL WITH OSCILLATING FLAP.

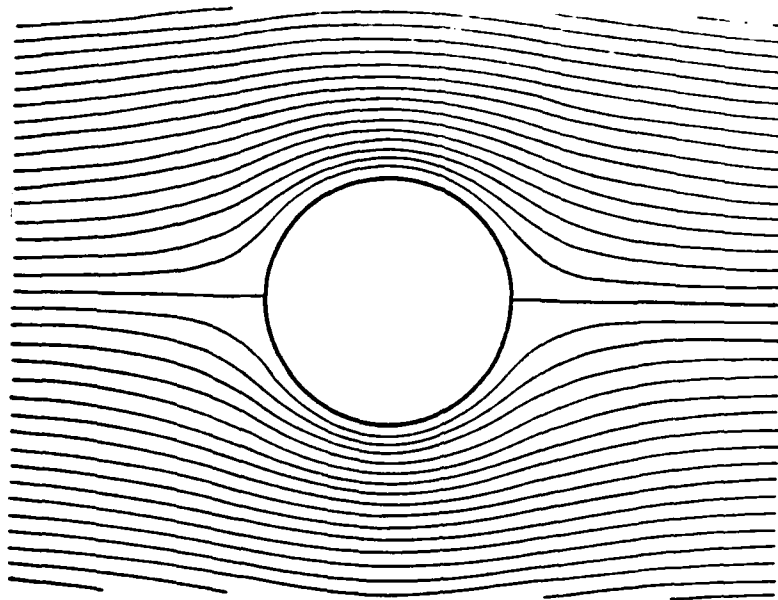


FIG. 2a. STREAMLINES FOR FLOW PAST STATIONARY CYLINDER IN A MOVING STREAM.

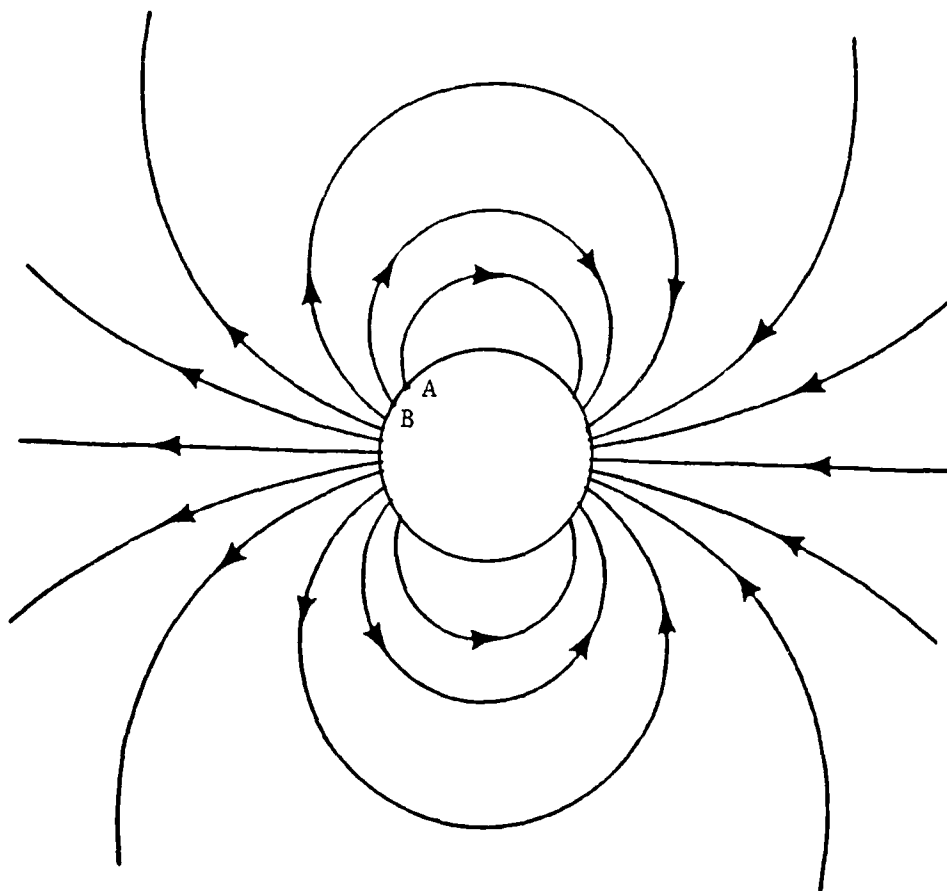


FIG. 2b. STREAMLINES FOR FLOW AROUND CYLINDER MOVING IN AN OTHERWISE STAGNANT FLUID.

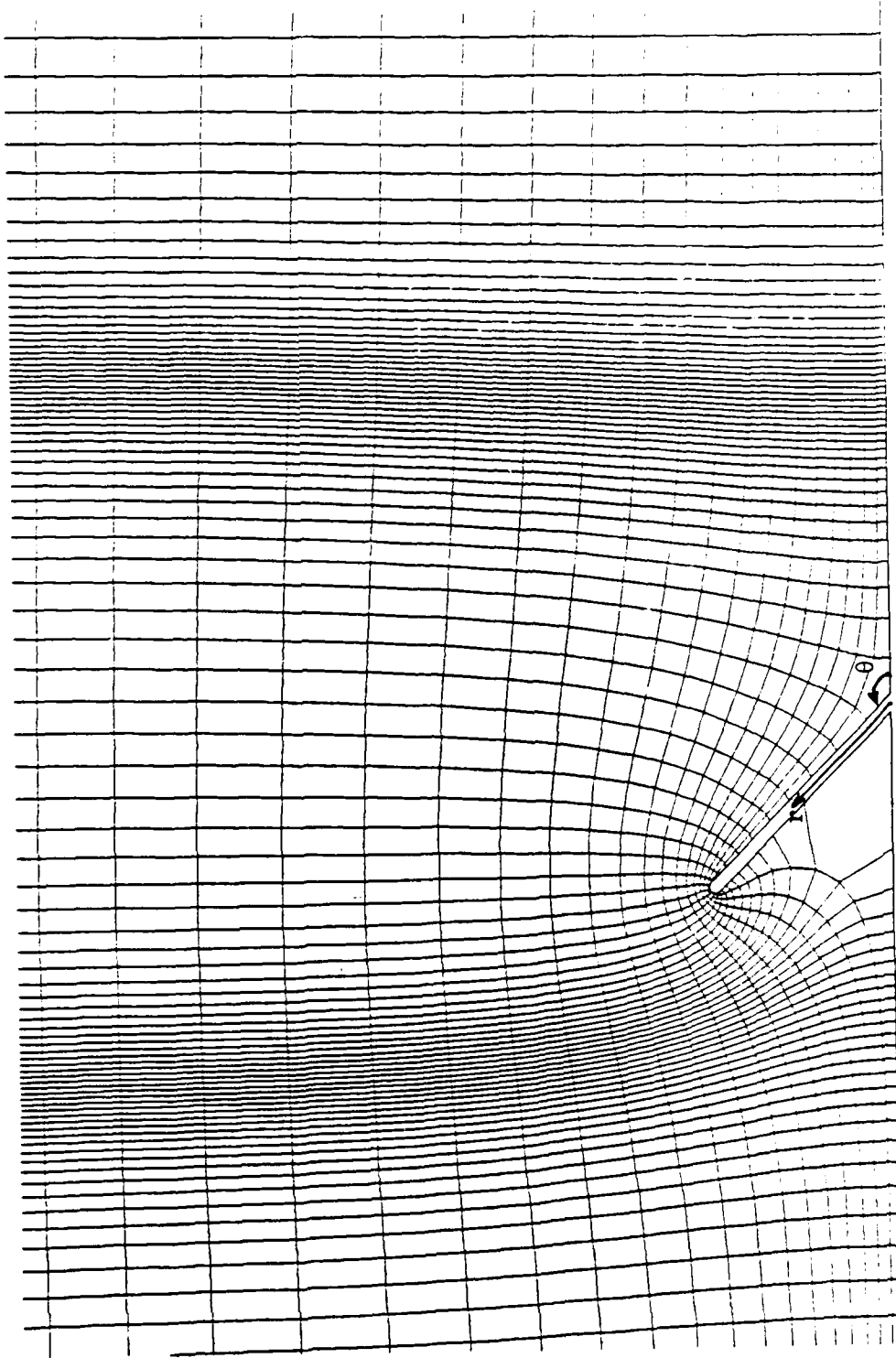


FIG. 3. LOCAL POLAR COORDINATES FOR OSCILLATING FLAP.

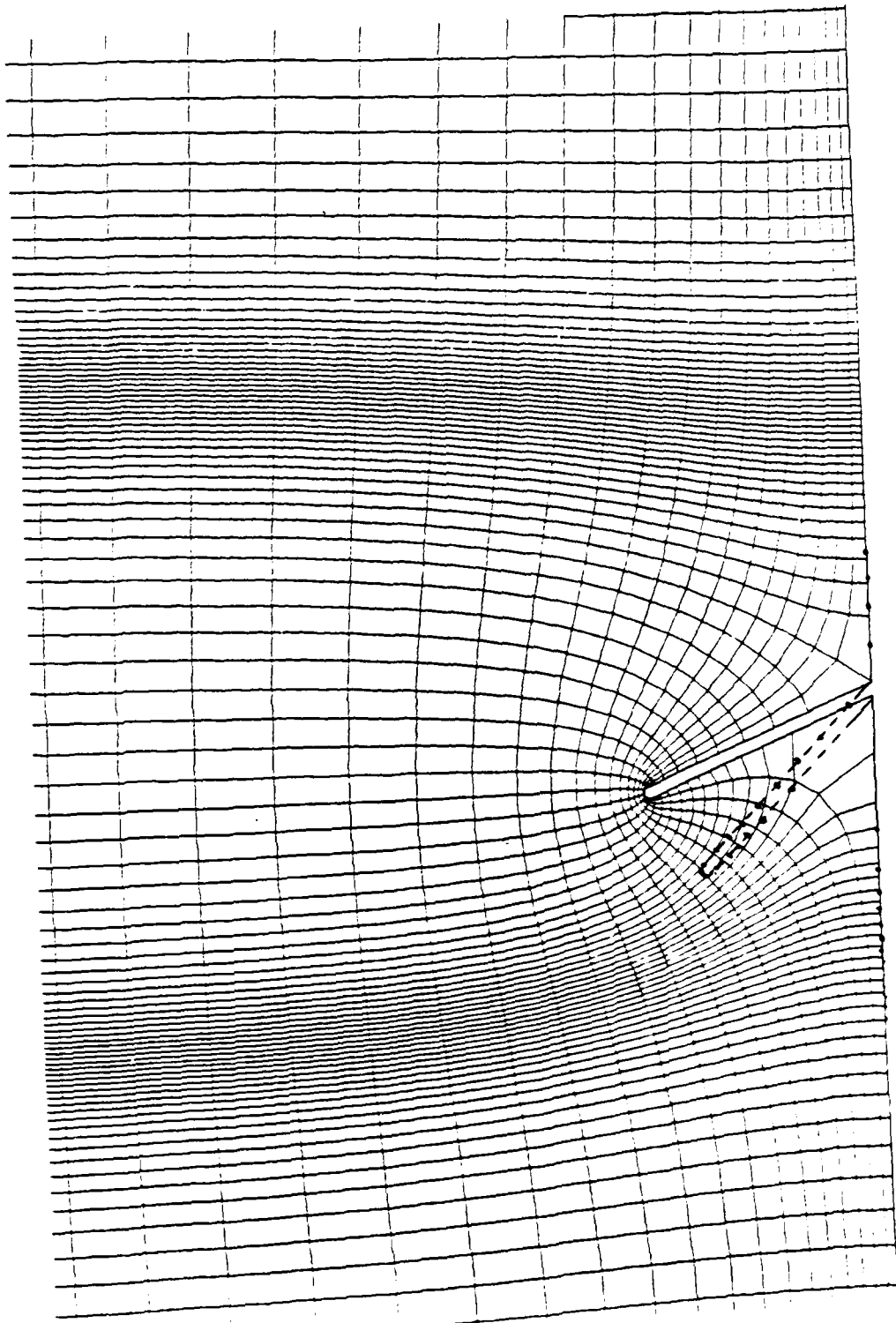


FIG. 4. LOCATIONS OF BOUNDARY POINTS ALONG FLAP IN TWO DIFFERENT ORIENTATIONS.

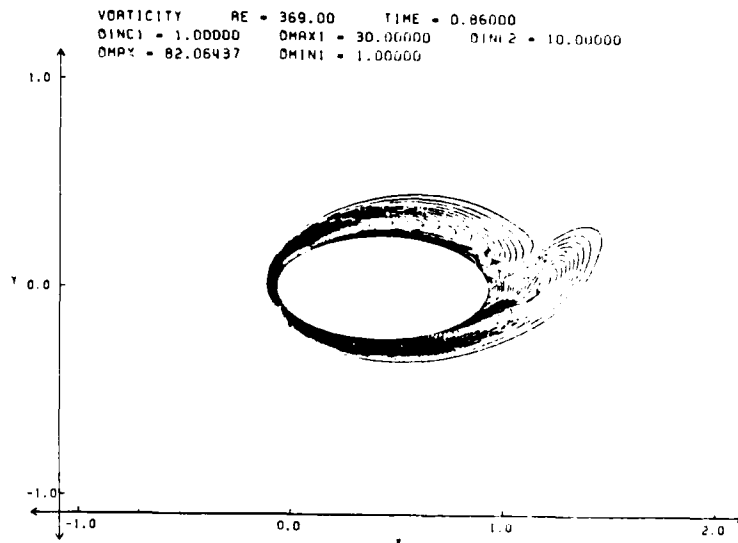


FIG. 5. COMPARISON OF "VORTICITY" CONTOURS AT  $Re = 369$ ,  $\alpha = 20^\circ$ ,  $T = 0.86$ ,  
 (a) DATA OF IZUMI AND KUWAHARA, (b) RESULTS OF PRESENT ANALYSIS.

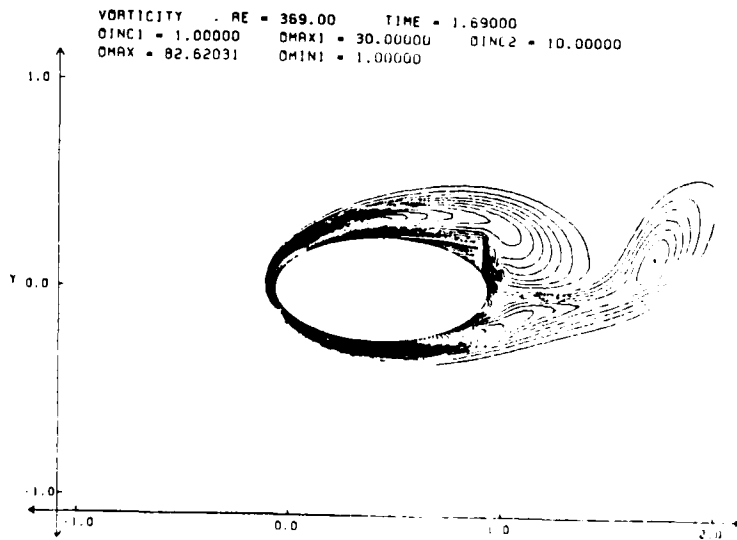


FIG. 6. COMPARISON OF "VORTICITY" CONTOURS AT  $Re = 369$ ,  $\alpha = 20^\circ$ ,  $T = 1.69$ ,  
 (a) DATA OF IZUMI AND KUWAHARA, (b) RESULTS OF PRESENT ANALYSIS.

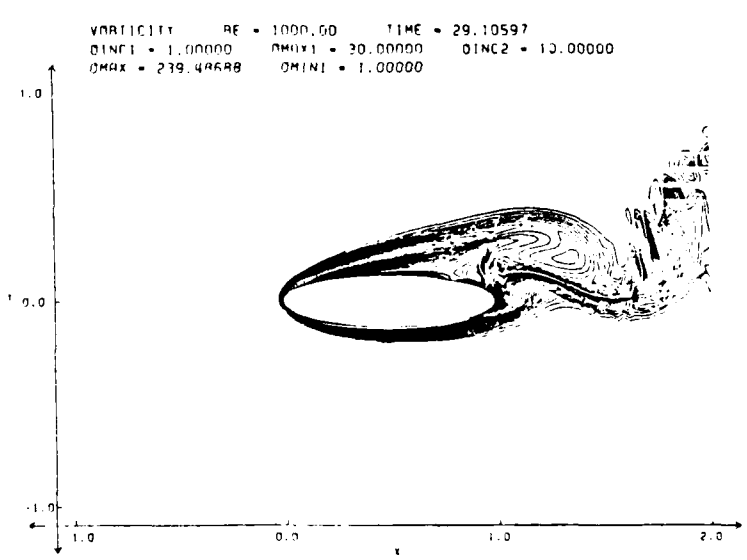
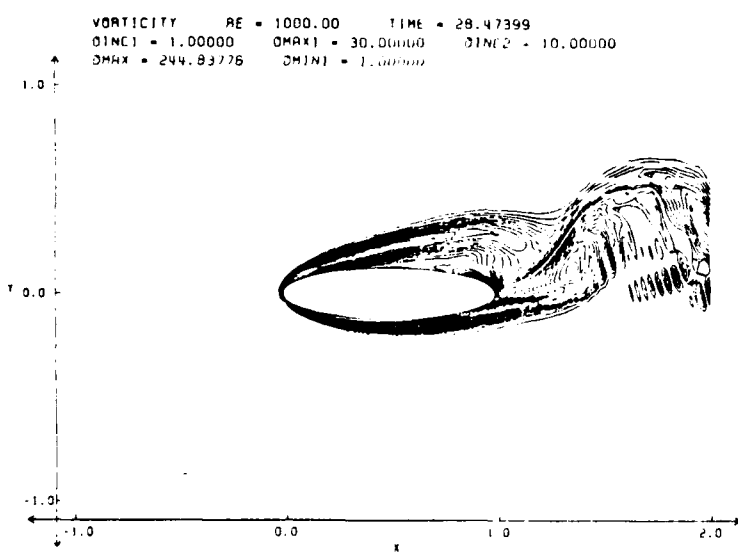
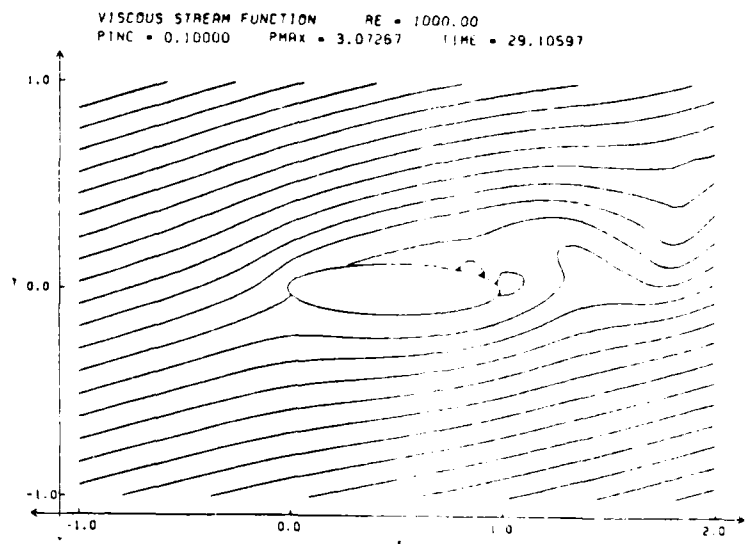
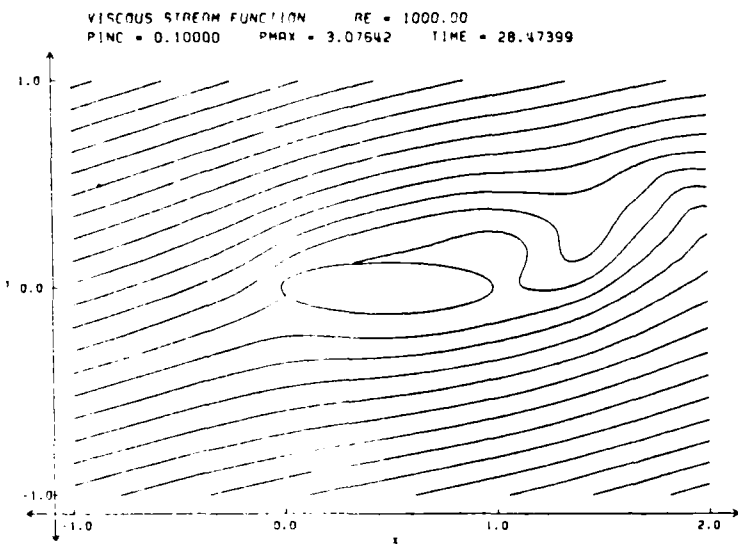


FIG. 7. FLOW FIELD RESULTS FOR  $Re = 1000$ ,  $\alpha = 15^\circ$ .  
 (a,b) INSTANTANEOUS STREAM FUNCTION ,  
 (c,d) INSTANTANEOUS VORTICITY CONTOURS

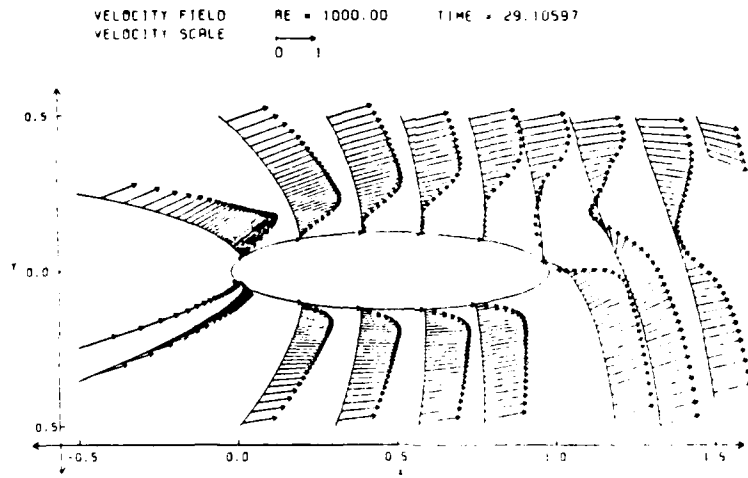
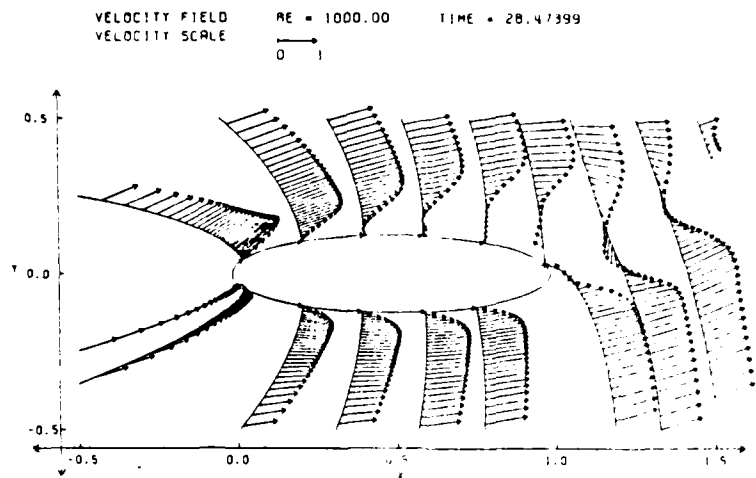


FIG. 7 (Cont'd.). FLOW FIELD RESULTS FOR  $Re = 1000$ ,  $\alpha = 15^\circ$ .  
 (e,f) INSTANTANEOUS VELOCITY VECTORS.

## APPENDIX

### EFFICIENT GENERATION OF CONFORMAL COORDINATES FOR ARBITRARY GEOMETRIES

#### A.1 Outline of Conformal Mapping Employed

Following the work of Davis [1983], the Schwarz-Christoffel conformal transformation given by the equation

$$\frac{dz}{d\zeta} = M \prod_{i=1}^n (\zeta - a_i)^{\alpha_i/\pi} \quad (\text{A.1})$$

is employed to map an n-sided polygon in the z-plane onto the upper half of the  $\zeta$ -plane as shown in Fig. A.1. In Eq. (A.1), the  $\alpha_i$ 's are known from the given geometry, while M and the  $a_i$ 's are unknown.

Since it is more appropriate to transform an arbitrary channel to a straight channel rather than to an upper-half plane, a further transformation is introduced which conformally maps the upper-half  $\zeta$ -plane to a straight channel in the T-plane. Clearly, this latter transformation is simply a special case of the Schwarz-Christoffel transformation [Eq. (A.1)] and is given as

$$\frac{d\zeta}{dT} = \pi \zeta \quad , \quad (\text{A.2a})$$

so that

$$T = \frac{1}{\pi} \ln(\zeta) \quad \text{or} \quad \zeta = \exp(\pi T) \quad . \quad (\text{A.2b})$$

Hence, the overall transformation is obtained as

$$\frac{dz}{dT} = \pi \zeta \left. \frac{dz}{d\zeta} \right|_{\zeta = \exp(\pi T)} \quad (\text{A.3})$$

with  $dz/d\zeta$  given by Eq. (A.1). Further details associated with the actual determination of this transformation are presently being documented in a paper (U. Ghia, Zuo and K. Ghia [1988]) to be submitted for publication in a technical journal. This work also constitute the basis of a Master's degree thesis (Zuo [1987]).

Figure A.2 shows typical grids obtained, using this analysis, for the backstep channel with an oscillating flap. Two representative positions of the flap are shown. The grid clustering occurring on the left of the flap is unnecessary for these positions of the flap. However, it is retained because the grid-clustering transformations are time-invariant and the clustering shown will be needed when the flap rotates to occupy a position in the second quadrant with reference to the axis of the flap motion. This is a small price to pay for the important advantage that the stream-function equation retains time-invariant coefficients and can continue to be solved efficiently by the BGE direct method.

#### A.2 Enhancement of Efficiency for Evaluation of Transformation

Since the transformation needs to be re-evaluated for every incremental change in orientation of the flap, considerable effort was focused on enhancing the efficiency of determination of the transformation. The results of this effort are summarized in Table A.1. Prior to commenting on these results, it is important to note the following. The Schwarz-Christoffel transformation directly provides the complex derivative  $dz/d\zeta$  or  $dz/dT$  and, hence, the scale factor  $h$  of this conformal mapping. The flow equations contain only  $h$  and its derivatives. Therefore, integration of  $dz/d\zeta$  itself is needed only when it is desired to view the grid. This may

not be necessary at each and every time step of the flow simulation; only  $h$  needs to be evaluated at every computational time level.

For channels, Eq. (A.3), together with Eq. (A.11), possesses a simple asymptotic form as  $\text{Re}(\zeta) \rightarrow \pm \infty$ . These equations approach this asymptotic form in an exponential manner, so that the simplified form constitutes an accurate representation of the actual transformation beyond relatively small distances away from the last deviation from the straight-channel configuration. As shown in Table A.1, implementation of this asymptotic form resulted in 66-80 percent saving of CPU time for the computation of  $h^2$ , while the CPU time saved in the grid calculation was almost 80-95 percent when the grid is obtained by integrating  $dz/dT$  in the T-plane, i.e., in the straight-channel plane. If the integration is done in the computational plane of the clustered coordinates (S,N), the CPU time saved is not nearly as large, but the grid clustering obtained in the physical plane is better.

In Table A.1, item B refers to the actual coding employed for evaluating the multi-exponential terms appearing in Eq. (A.1). After examining the manner in which such terms are actually evaluated in the computer, the coding was modified to reflect this manner of evaluation. This resulted in an additional 50 percent saving in the CPU time required to evaluate  $h^2$ . Hence, the implementation of both items A and B resulted in a total CPU time saving of almost 90 percent. It is believed that this level of efficiency is acceptable for proceeding on with the flow-control study.

A paper based on this efficient grid-generation study is presently under preparation by U. Ghia et al. [1988]. This study should also be very useful in various related areas such as those occurring in problems involving fluid-structure interactions and free surfaces, metal-forming problems as well as in bio-fluid mechanics involving flow through passages

with flexible walls. All of these problems encounter temporally deforming boundaries and may often require the consideration of more than one discipline of study. For example, in fluid-structure interaction problems, the fluid dynamics analysis provides the time-varying force distribution, while the structural analysis provides the boundary deformations (vibrations) occurring under the action of these unsteady forces. The high efficiency of the grid-generation method, together with the present formulation of the stream-function equation with constant coefficients even in the presence of temporally deforming geometry, paves the way for effectively examining the oscillating-flap flow-control mechanism.

TABLE A-1  
ENHANCEMENT OF EFFICIENCY

BY IMPLEMENTING	PERCENTAGE OF COMPUTATIONAL TIME SAVED	
	$h^2$ CALCULATION	GRID CALCULATION
ITEM 'A'	66 - 80	80 - 95* (66 - 80) <sup>+</sup>
ITEM 'B'	50	0
ITEMS 'A'+ 'B'	83 - 90	-- 80 - 95* (66 - 80) <sup>+</sup>

'A' : ASYMPTOTIC FORM FOR CHANNEL MAPPING.

'B' : TIME-SAVING TECHNIQUE FOR EVALUATING  
MULTI-EXPONENTIAL TERMS.

NOTE: CURVED BOUNDARIES ARE ALSO TREATED WITH  
COMPARABLE EFFICIENCY.

\* INTEGRATION DONE IN CHANNEL PLANE (T).

+ INTEGRATION DONE IN COMPUTATIONAL PLANE (S,N).

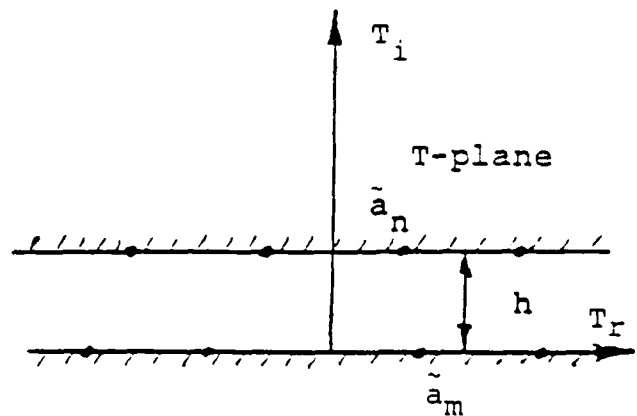
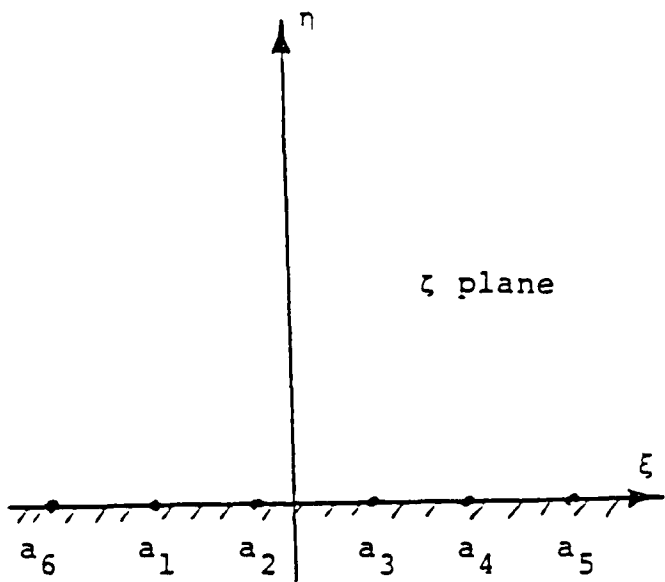
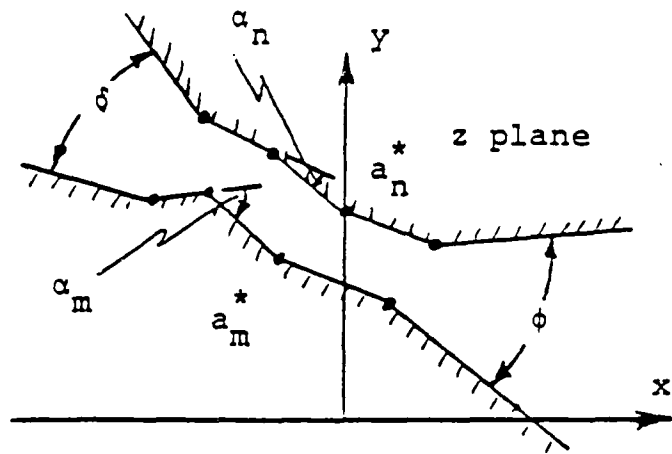


FIG. A-1 CONFORMAL MAPPING OF ARBITRARY CHANNEL TO STRAIGHT CHANNEL.

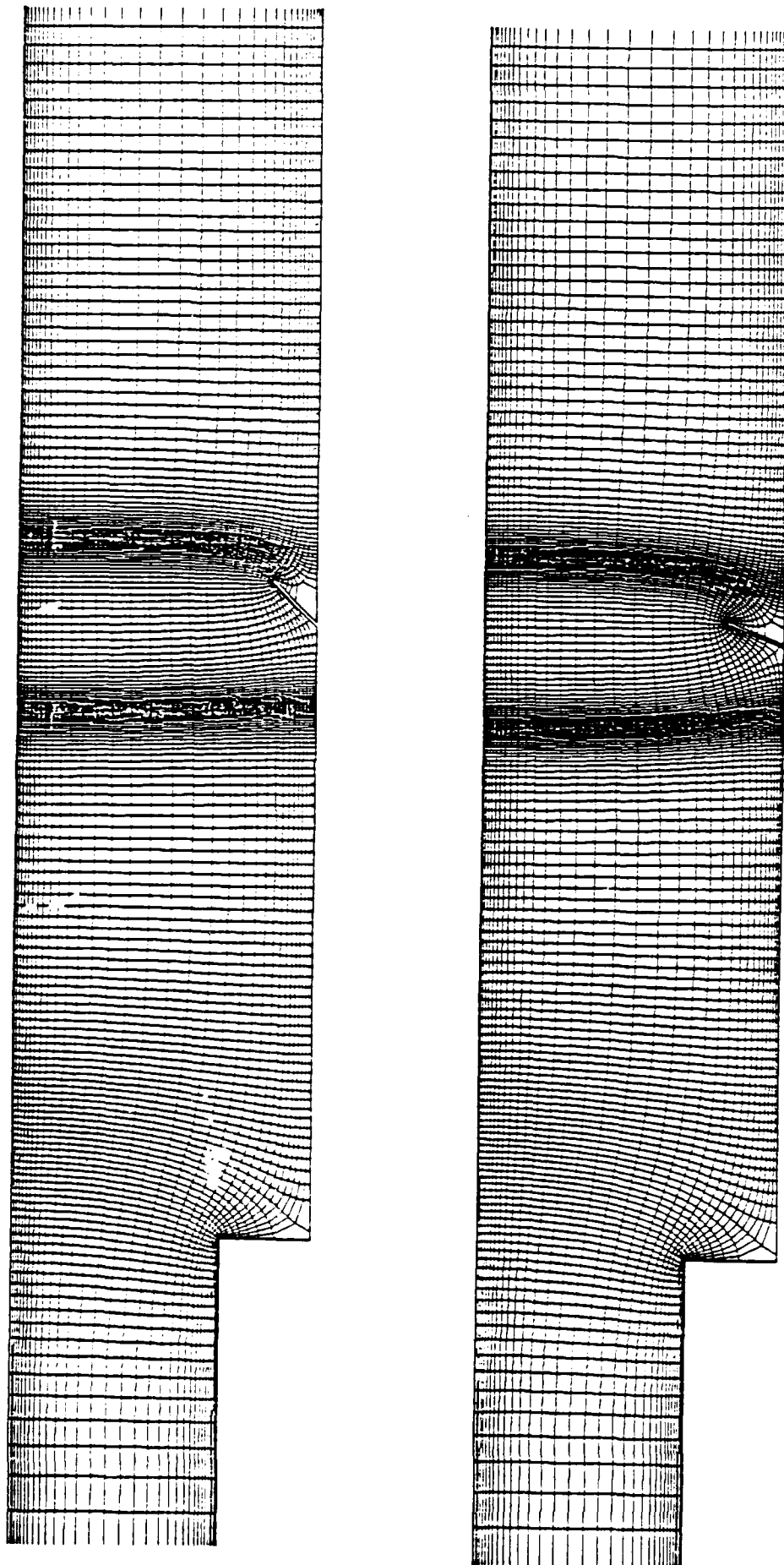


FIG. A-2 CLUSTERED CONFORMAL BOUNDARY-ALIGNED GRID FOR BACKSTEP CHANNEL WITH OSCILLATING FLAP IN TWO DIFFERENT POSITIONS.

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