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Optics and Symbolic Computing Semi-Annual Technical Report

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TABLE OF CONTENTS

<u>Section</u>	<u>Title</u>	<u>Page</u>
	INTRODUCTION	1
	SORTING WITH OPTICAL COMPARE-AND-EXCHANGE MODULES	5
	ALL-OPTICAL COMPARE-AND-EXCHANGE SWITCHES	35



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LIST OF FIGURES

<u>Figure</u>	<u>Title</u>	<u>Page</u>
SORTING WITH OPTICAL COMPARE-AND-EXCHANGE MODULES		
1	Compare-and-Exchange Module	13
2	Pipelined Bitonic Sorter on a Perfect Shuffle Connected Network	14
3	Time Evolution of Digital Compare and Exchange	18
4(a)	Transfer Function of a Latching AND Gate	20
4(b)	Latching AND Implementation of Compare Operation	20
5	Regenerative Exchange Circuit	26
6	Polarization Encoded Exchange	28
ALL-OPTICAL COMPARE-AND-EXCHANGE SWITCHES		
1	The compare-and-exchange module. E represents the exchange signal, A, B represent the two input numbers, and H, L represent the higher number and the lower number, respectively.	38
2	Compare circuit in which L indicates the latching logic gate.	38
3	The use of $A_i \bar{B}_i$ and $\bar{A}_i B_i$ to compare A and B. When $A < B$, $\bar{A}_i B_i = 1$ will appear first. When $A > B$, $A_i \bar{B}_i = 1$ will appear first.	40
4	Generation of $A_i \bar{B}_i$ and $\bar{A}_i B_i$ using a single bidirectional, reflection-mode Fabry-Perot etalon.	40
5	Experimental layout for all-optical compare and exchange with IF- ZnS interference filter, $\lambda/2$ -half-wave plate, $\lambda/4$ - quarter-wave plate. E represents the exchange signal, A, B represent	

LIST OF FIGURES (CONTINUED)

<u>Figure</u>	<u>Title</u>	<u>Page</u>
	the two binary encoded numbers, and H , L represent the outputs of the larger number and the smaller number, respectively.	42
6	Expected operation of compare-and-exchange circuits test set 1 and 2 on horizontal axis. All curves are drawn upside down consistent with the experimental photographs. The vertical axes are in arbitrary units.	43
7	Computer simulated transfer functions for the ideal interference filters. The horizontal axes are input power in arbitrary units and the vertical axes are reflectivity or transmissivity of the filters. (a). Reflectivity R_1 of the comparator IF_1 with $I_0=0$, $I_1=A_i$ (or B_i), and $I_2=A_i+B_i$; (b). Reflectivity R_2 of the latching NAND gate IF_2 with $I_1=\bar{R}_i$, and $I_2=\bar{R}_1+A_i\bar{B}_i$; (c). Transmissivity T_3 of the latching AND gate with $I_1=\bar{R}_2$, $I_2=\bar{R}_2 + \bar{R}_1A_i\bar{B}_i$ (or $\bar{R}_2+\bar{A}_iB_i$), and $I_3=\bar{R}_2+\bar{R}_1A_iB_i + \bar{A}_iB_i$; (d). Transmissivity T_4 of IF_4 with $I_0=0$, $I_0'=E$, $I_i=A_i+B_i+E$; (e). Reflectivity R_4 of IF_4 with definitions as in (d); (f). The sum of (d) and (e).	44
8	Experimental results of the inputs A , B and the logic outputs $\overline{AB}$, $\overline{AB}$. The input powers are 11 mW each, and the output power is about 5 mW.	47
9	Output of the exchange-prohibited signal $\overline{R_1AB}$. The upper two traces show the two groups of numbers coming into the system. In the first group A is larger than B and in the second one, B is larger than A . The power of the holding beam is 19 mW, and the output power is about 6 mW.	47
10	Output of the exchange signal E . The holding power is 20 mW, and the output power is 5 mW.	49
11	The high output and the low output of the system with $A>B$. The input power is 14.5 mW, and the output power is 6.5 mW.	49

LIST OF FIGURES (CONTINUED)

<u>Figure</u>	<u>Title</u>	<u>Page</u>
12	The high output and the low output of the system with $B > A$. The input power is 14.5 mW, and the output power is 6.5 mW.	50

INTRODUCTION

INTRODUCTION

Symbolic computation differs from its conventional numeric cousin in several fundamental ways. Foremost among the differences is the set of applications each intends to address. Typical symbolic computing applications include logical inference, information extraction, problem solving, and text/speech/image understanding. These applications typically require the processing of large amounts of information. In addition, many symbolic computing application environments are interactive and characterized by real-time performance requirements.

Using conventional serial hardware, however, the time it takes to process large amounts of symbolic information precludes real-time applications because the minimum time interval is fixed by practical considerations. For instance, multiplying two matrices takes $O(N^3)$ steps, where $N \times N$ is the number of elements in each matrix, and serial sorting can be done in no less than $O(N \log N)$ time steps, where N is the length of the list.¹ In addition, serial operations can only be pipelined to a limited degree: usually a memory fetch can occur while the cpu is processing another piece of data, but only one processing step can be performed at a time. Fortunately many symbolic computing operations have parallel algorithms that are pipelinable, and thus may run faster on parallel machines.

Symbolic computing applications that are parallelizable include calculating the transitive closure, shortest path or connected components of a relational graph. In addition, pruning a graph by consistent labeling with parallel matrix operations may reduce subsequent graph search times. Parallel algorithms for image and signal recognition include filtering and large kernel convolution and correlation. The logical set and relational algebra operations like intersection, union, division, projection, join, and cartesian product also can be speeded-up by parallel algorithms. In the rest of this report we will focus on sorting, which is common to both symbolic and conventional computation. We will begin by reviewing the existing parallel sorting algorithms. Parallel algorithms for the other symbolic computing operations will be the subject of future research.

Because of the real-time and large N constraints of symbolic computation, we will confine our discussions to parallel algorithms where the sorting time grows sublinearly with N : this immediately excludes linear arrays. Usually the uniform cost criterion is assumed when comparing algorithms, where all steps of the computation are of the same duration and processing, interconnect, and memory elements and operations are equally costly. Of course the uniform cost criterion is not applicable to systems with varying hardware

characteristics. In addition, all relative order arguments only apply for asymptotic values of N where constants and lower order terms are ignored.² However, N is bounded by technology constraints so the magnitude of the constants can be important when comparing real systems. Clearly technology and architecture dependent constants and relative costs are critical in a meaningful trade-off analysis between sorting systems. The following analysis will focus on these subtleties and result in the specification of optimal sorting systems with regard to the requirements of symbolic computing applications.

Sorting can be performed on 2-D array of processing elements in sublinear $O(N^{1/2})$ time.³ The nearest-neighbor communication of meshes allows the minimum temporal increment to be extremely small. Moreover, the 2-D topology makes them particularly well suited for implementation with 2-D technologies like electronics. While simple matrix operations can be pipelined for high throughput, most complex mesh algorithms like sorting are not pipelinable; and therefore, the system throughput equals the latency. In the high performance sorting applications found in symbolic computing, achieving a modest sublinear temporal complexity without pipelining is inadequate. Hence we must consider alternative sorting architectures.

The most powerful class of parallel algorithms are based on reconfigurable global communications between parallel processing elements and a common memory; hence they are called shared memory machines.⁴ The processing elements are fully connected through the memory and allow varying degrees of simultaneous memory reads and writes. Of the three general classes of parallel algorithms, shared memory computer algorithms can perform operations with the lowest number of time steps. For instance, sorting can be performed in $O(\log N)$ time and many graph problems benefit from shared memory. Abstract shared memory machines can also simulate both the mesh and network computers with no time delay.

While the temporal complexity of shared memory algorithms may be low, they usually require significantly more spatial resources than the mesh algorithms. In addition to limiting the size of the shared memory implementations, there is also a breakdown of the uniform cost criterion when comparing shared memory machines with meshes due to the globally reconfigurable interconnect. Global reconfiguration takes much more time in real systems than a simple nearest neighbor communication: the reconfiguration time increases substantially with N , the number of processing elements in the architecture. Thus shared memory implementations will be limited by practical

considerations to small-scale parallel architectures, which will not be optimal for sorting applications in symbolic computing.

Fortunately there is an alternative to the mesh and shared memory approaches to parallel computer architecture which we call network architectures. Network architectures are characterized by fixed, global communications between simple parallel processing elements. Sorting algorithms exist for network architectures that can be pipelined, have low delay $O(\log^2 N)$, and moderate spatial complexity $O(N \log^2 N)$.⁵ However in electronic network implementations, the global communications limit the maximum N and the minimum temporal interval from above and below respectively. Optical network implementations on the other hand are capable of building very large networks where the minimum temporal interval is limited by the propagation distance and the speed of light. At one nanosecond per foot, connection occurs quite rapidly in either fiber optic, bulk optical,⁶ or holographic⁷ systems. Thus the minimum temporal increment and N of optical networks can approach that of electronic meshes. The network architectures also obtain a low temporal complexity at the cost of reasonable spatial complexity while retaining the ability to pipeline the sorting operation.

From the preceding discussion it appears that network sorting algorithms are optimal for symbolic computing applications. In addition, optical networks are favored over their electronic counterparts because of their large size and bandwidth. The remainder of this report is devoted to issues concerning the optical implementation of network sorting algorithms. The first section details the design of optical implementations of the active portion of the network sorting algorithms, the compare-and-exchange operation. We propose using a distinctive feature of optical devices, namely bistability, that enables the construction of simple, hardwired circuits. At the end of this section we show how the properties of optical device families can be used to project the application domains of the resulting sorting networks. This paper has been accepted to a special issue of Applied Optics on optical computing.

In the second and last section we demonstrate an all-optical implementation of the compare-and-exchange operation using ZnS interference filters. This was a collaborative effort between BDM and the Optical Circuitry Cooperative of the Optical Sciences Center at the University of Arizona. This paper has been accepted to a special issue of the IEEE Journal of Selected Areas in Communications on photonic switching.

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SORTING WITH OPTICAL
COMPARE-AND-EXCHANGE MODULES

SORTING WITH OPTICAL COMPARE-AND-EXCHANGE MODULES

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ABSTRACT

Sorting is central to the solution of many knowledge-based and switching problems in advanced computation and communication systems. Parallel-pipelined sorting algorithms are appropriate for applications that demand high throughput, low delay and many data channels. One such algorithm, the bitonic sort, can be implemented with passive perfect shuffle interconnects between active stages of compare-and-exchange elements. In this paper we focus on optical hardware to implement the C&E operation and show that by taking advantage of a distinctive feature of optical logic, namely bistability, comparison circuits of remarkable simplicity are attainable. We describe implementations of C&E in a variety of optical device technologies capable of performing latching and nonlatching logic. Based on the device characteristics we outline potential application areas for each technology.

INTRODUCTION

In the early seventies it was estimated that 25% of all computer time was devoted to sorting.¹ With the widespread application of dedicated micro-controllers it is unlikely that this is still true; however, sorting remains one of the most common tasks in general-purpose computation. For instance, databases and expert systems often sort the elements of a data structure to simplify searching and the addition of new elements. Furthermore, data manipulation operations like projection, set union and intersection can be directly implemented by modified sorting algorithms.² Typically, knowledge-based systems operate on large numbers of related elements of information. As a general rule the number of parallel steps necessary to sort a data structure depends on the number of elements and the faster a sorting algorithm is, the more resources it requires. In other words the temporal complexity of the sorting problem is reduced at the expense of increased spatial complexity. Thus faced with a maximum amount of spatial resources and a minimum switching delay allowed by device-physics considerations, the time it takes to sort large structures in knowledge-based systems can prohibit real-time applications.

In addition to its widespread use in computation, sorting is also important in communications.³ In particular, parallel processor architectures can be interconnected by pipelined sorting networks

serving as message passing systems.⁴ Similarly, telecommunication packet switches can be based on sorting networks.⁵ Just as in knowledge-based systems, the hardware sorters for massively parallel architectures and subscriber loop communications must process large numbers of parallel channels with low delay. More importantly however, the sorting networks in communications must keep up with the data and packet generation rates--which can be considerable in large-grained parallel architectures and in trunk and video telecommunications. Hence, demands on the throughput of the sorting hardware mandate the use of parallel, pipelined sorting algorithms.

A sorting algorithm that fulfills the combined requirements of low temporal and spatial complexity along with high throughput is the bitonic network.³ The bitonic network can be pipelined in a multistage architecture that requires global interconnects and active compare-and-exchange (C&E) modules. It has been recognized that optical interconnects can provide the global connections needed between the stages.^{6,7,8} In addition, previous research described optical implementations of the exchange portion of the active modules using polarization switches,⁹ directional couplers¹⁰ and hybrid optoelectronic circuits.¹¹ In this paper we show the feasibility of simple, hardwired implementations of C&E in which all the processing is performed either optically or electrooptically. Specifically we propose using a family of devices for the comparison operation that employs bistability to combine logic and memory in a single device--obviating the need for external feedback as in flip-flops. In the next section we review the properties of the bitonic algorithm and its implications to electronic and optical implementations. In the last section we describe implementations of C&E using all-optical, hybrid optoelectronic and electrooptic logic devices. Based on the device characteristics, we outline the properties of the ensuing networks and their potential application domains.

PIPELINED BITONIC SORTING NETWORKS

A bitonic sequence of length N is composed of two sorted subsequences of length $N/2$. one monotonically increasing, the other decreasing. The bitonic merge combines the subsequences into a sorted sequence of length N using $\log N$ stages, each stage composed of compare-and-exchange modules and fixed interconnections between stages. The bitonic sorting algorithm for an arbitrarily ordered input list uses a divide-and-conquer strategy which begins by applying the bitonic merge to bitonic sequences of length 2, generating sorted sequences of length 2 and bitonic sequences of length 4. By repeated application of the bitonic merge, sorted and bitonic sequences of twice the length of those in the previous stage are formed. Thus, it takes $\log N$ applications of the bitonic merge to produce a sorted sequence of length N . Since the k th merge takes $\log k$ steps, the time complexity of the bitonic sort is $O(\log N)^2$. If we have a pipelined bitonic sorting network then there are $N/2$ compare-and-exchange modules per stage: thus, the spatial complexity is $O(N(\log N)^2)$.

Pipelined bitonic networks are difficult to implement with electronic technology for several reasons. Because of the length and complexity of the interstage interconnects, 2-D layouts of the networks require area and communication distances that grow faster than N , the number of data channels.¹² In such wire-limited architectures the signal propagation delays are dependent on the number of channels and contribute to the overall sorting delay. Similarly, the long wires require large, high-power drivers that dominate the total system power for large values of N . Moreover the maximum signal bandwidth, and thus the throughput, is proportional to the difference in length of the wires in a stage or their RC time constants, whichever is larger. With the addition of high-speed buffers the time-skew limited throughput can be increased at the expense of increased delay. In conclusion, pipelined bitonic sorting networks in electronics are limited to applications with small numbers of data channels and low signal bandwidths.

Optical technology, on the other hand, is well-suited to implement the interconnects needed in sorting networks.^{6,7,8} Each bitonic interstage connection pattern can be emulated by a number of perfect shuffles with global, space-variant communications.¹³ Free-space optical implementations of the perfect shuffle have been demonstrated^{14,15} that exploit the third dimension for non-interacting communication channels. Since the active devices must share area only

with the connections' input and output transducers rather than the connections themselves. sorters with large numbers of channels can be fit into small areas and volumes. Besides the area and volume advantages, 3-D interconnects permit the interstage delay to be independent of the number of channels. Thus in contrast to electronics, the overall sorting delay grows only with the number of stages. Moreover for the moderate distances present in these architectures, the optical drive power is independent of the communication distance. These passive optical systems also have minimal time skew and may communicate information at optical media bandwidths; thus, the sorting throughput can be quite large and is limited in practice by the response time of the active devices. Finally due to the prevalence of optical technology in mass storage and communication environments, the data to be sorted may already be in optical form. In conclusion, optical technology will be competitive for sorting applications with large numbers of channels and/or high bandwidth signals.

The limiting feature of optical multistage sorting networks, in contrast to electronic implementations, is not the passive interconnection network, but the active processing performed in parallel between each communication step. The advantages of optical interconnections for sorting that we outlined above are dependent on the existence of optically compatible 2-channel sorting elements. the

C&E module shown in Figure 1. The compare operation determines the relative magnitude of the information on the two input channels. Depending on the result of the comparison operation, the exchange operation directs the larger and smaller input data to the output channels marked high and low, respectively. A pipelined bitonic sorter on a perfect shuffle connected network is presented in Figure 2.

Condition 1) if $high \geq low$ then $high \rightarrow high$ and $low \rightarrow low$

Condition 2) if $high < low$ then $high \rightarrow low$ and $low \rightarrow high$

Fig. 1 Compare & Exchange Rules

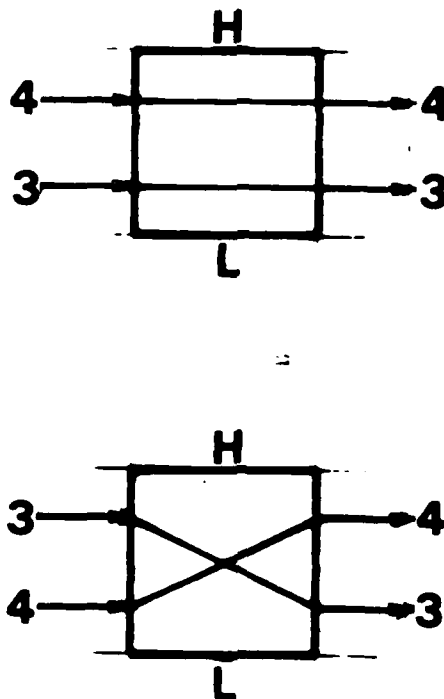


Figure 1. Compare-and-Exchange Module.

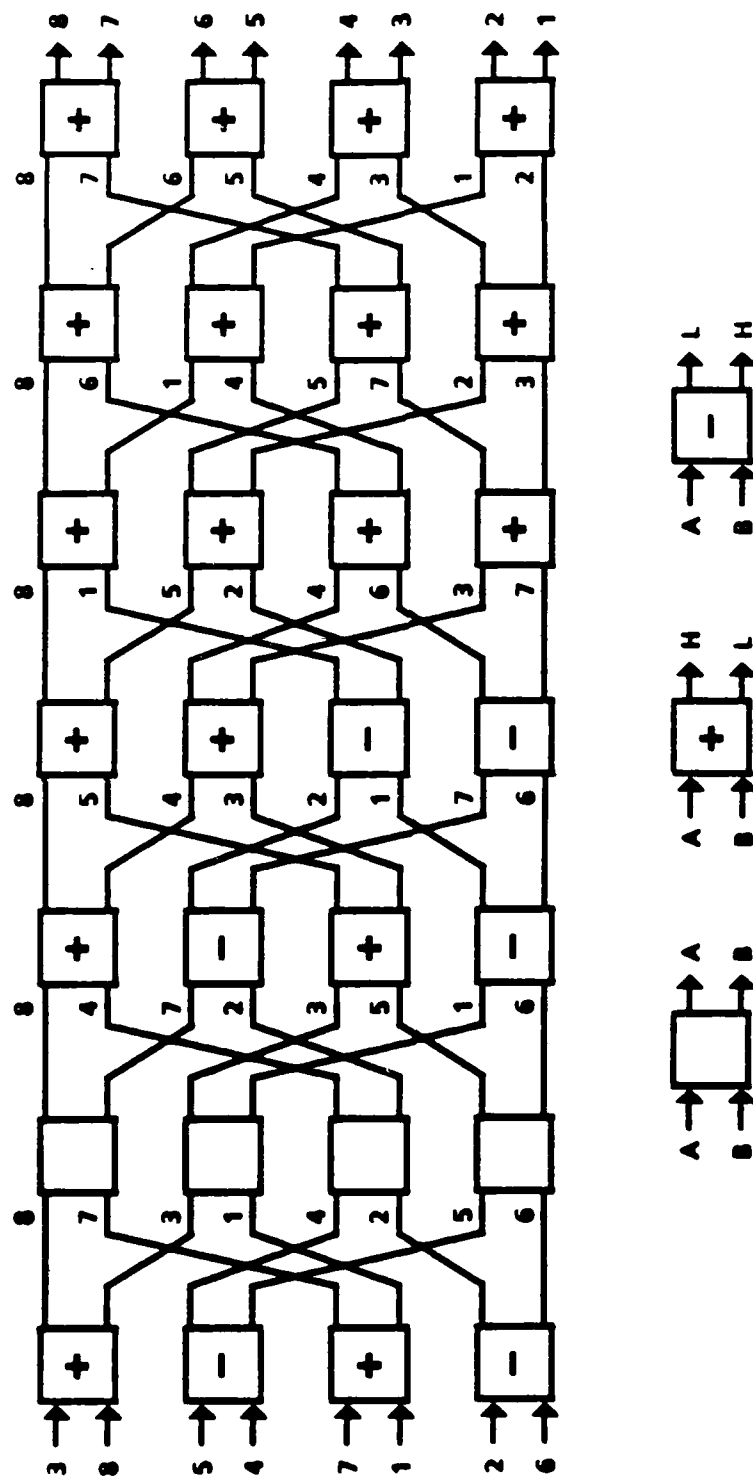


Figure 2. Pipelined Bitonic Sorter on a Perfect Shuffle Connected Network.

ANALOG IMPLEMENTATION OF COMPARE AND EXCHANGE MODULE:

Analog implementations of C&E have been proposed for associative memories and self-organizing systems ¹⁶. In this application, their role is to identify the element of a vector with the maximum value using a binary-tree architecture. Knowledge-based systems that do not involve high accuracy data could potentially use analog C&E and related operations for sorting and logical set operations. Unfortunately, analog sorting systems require system dynamic range much larger than the dynamic range of inputs. For the moment, let us assume that we desire error-free sorting by multistage analog C&E. Then the finite accuracy of each analog comparison calculation in the first stage places an initial upper bound on the allowable dynamic range of the inputs. In addition, multistage analog systems lacking signal restoration accumulate noise which further limits the useful dynamic range. Hence, noise introduced by non-uniform gain and crosstalk during or between the C&E processes is the most serious limiting factor since it will increase with each stage of the calculation. Clearly, the lowest signal-to-noise ratio is present at the last stage of the calculation and places the tightest restrictions on the allowable dynamic range of the inputs. If a specific dynamic range is desired for the inputs then the noise introduced by the system limits the number of possible stages. Since the number of stages is the logarithm or the logarithm squared of the number of inputs in deterministic sorting and selection networks, respectively,

noise also limits the number of data channels. Because of these apparent problems with analog approaches, we now turn to digital implementations of C&E.

DIGITAL IMPLEMENTATIONS OF COMPARE-AND-EXCHANGE MODULE:

Digital implementations of C&E have several advantages over analog approaches.¹⁷ A digital representation of data permits any finite dynamic range for the input values by simply specifying the number of bits. In addition digital logic can restore signal levels, and hence, the C&E units can be cascaded indefinitely. If crosstalk noise in the network is low and independent of the number of data channels, indefinite cascadability implies that the number of data channels is limited only by device-physics constraints like space and power. In contrast to analog implementations, for bit-serial data the internal complexity of the digital C&E modules remains constant regardless of the network size and the dynamic range of the inputs. Moreover, the low fan-in and -out of the bitonic network compensate for the low contrast and gain, respectively, in the active optical devices. Thus, the device requirements of the digital approach to multistage sorting networks appear to be compatible with the characteristics of optical and electrooptical technology. In this section we will show that C&E has simple, hardwired implementations that benefit from the bistable nature of many optical devices.

In a digital C&E module the comparison operation can be considered as a search for the most significant bit mismatch between the binary representations of the input data. The input word mismatch occurring closest to the most significant bit determines which datum is larger, and thus, the switch configuration. A rough outline of a serial algorithm for digital C&E schematically shown in Figure 1 is as follows:

- 1) input the data streams A and B most significant bit first into the high/low channels of the C&E module;
- 2) compare the two channels bit by bit; at the first occurrence of a mismatch between the strings, proceed to step 3 ;
- 3) if the mismatch is such that the A channel contains the larger datum, place the switch in the barred configuration (i.e. non-exchange position), otherwise the B channel contains the larger datum and place the switch in the crossed configuration (i.e. exchange position);

The time evolution of the switch position is illustrated in Figure 3 for typical input streams. The input data streams can be routed by the exchange switch subsequent to or even concurrent with comparison since up until the first mismatch the data streams are identical. Once the most significant mismatch has been detected and the exchange switch configuration determined, for correct operation the exchange switch must be insensitive to any subsequent mismatches. This property can be achieved in a number of ways, the most common

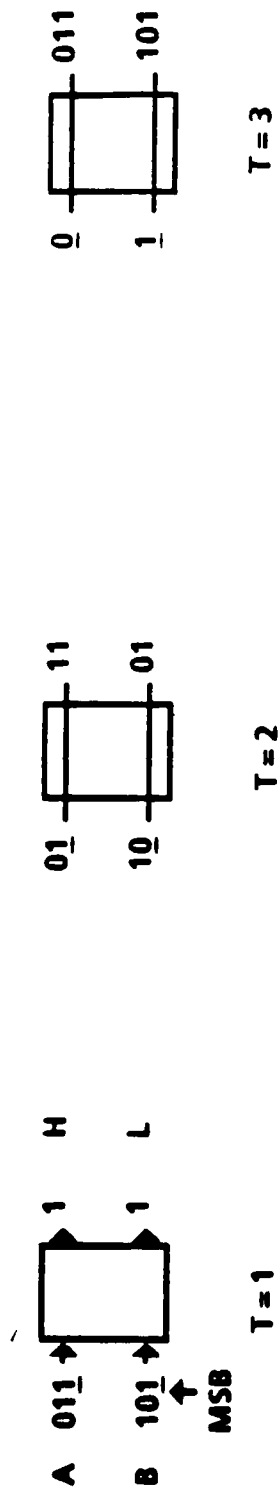


Figure 3. Time Evolution of Digital Compare and Exchange.

being feedback of the previous result of the comparison operation. Likewise, external flip-flops can record whether or not the mismatch has occurred and in which direction the switch should be set. Hence at the beginning of each word comparison the feedback signal or flip-flops must be reset to signify the mismatch has yet to occur.

LATCHING LOGIC DESIGN OF COMPARISON UNIT

Setting the exchange switch in a particular configuration until reset consists of remembering whether or not a mismatch has occurred and into which state, crossed or barred, the switch should be fixed. However, to reduce the complexity of the circuit we propose making the memory function inherent to the logic devices that perform comparison. This can be accomplished by using the bistability present in nonlinear logic devices with internal feedback. For example the transfer function of a latching AND gate is shown in Figure 4(a). While operating in latching mode, the device is biased up into the bistable loop. When the AND condition is first met, the state of the switch shifts to the upper part of the bistable loop. Since subsequent removal of all the inputs except for the bias does not change the output of the gate, the gate is effectively latched into the logical state true. Previously the only proposed uses for bistability in optical computers was for delay lines or memory elements.^{18,19} By extending the techniques we have presented here, it can be shown that latching NAND, OR, and NOR gates are possible with appropriate bistable loops and bias levels.

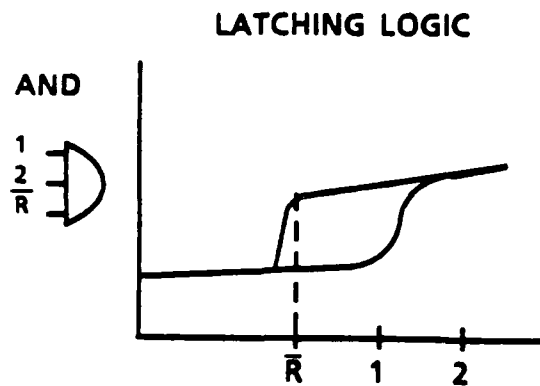


Figure 4(a). Transfer Function of a Latching and Gate.

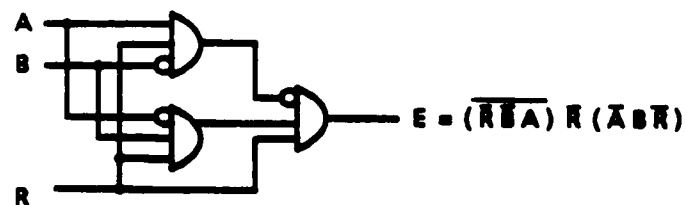


Figure 4(b). Latching and Implementation of Compare Operation.

Once one understands how latching logic works, the next task is to build latching logic circuits that perform a useful function. Unfortunately, we do not know of any general methods to design latching logic circuits based on a description of the intended circuit function. However, we succeeded in designing the latching AND circuit for comparison shown in Figure 4(b) that operates in the following manner. The top and bottom first layer AND gates are designed to latch at the first occurrence of the mismatches $(A_i > B_i)$ and $(B_i > A_i)$, respectively. If $(A_i > B_i)$ occurs before $(B_i > A_i)$ then the top gate latches to true while the output of the bottom gate is unlatched at false. The latched output of the top gate is then inverted to false, preventing the second layer gate from ever latching to the state (exchange = true), regardless of changes in the state of the bottom gate. Thus the output of the comparison module is effectively latched to the state (exchange = false). Conversely, if $(B_i > A_i)$ occurs before $(A_i > B_i)$ the bottom gate latches to true while the top gate remains unlatched at false. Thus the second layer gate and output of the comparison modules is directly latched to the state (exchange = true). Since removal of the bias causes all the latching gates to relax to the false state, the complement of the inter-word reset signal should be used as the bias to all of the latching gates. Since each gate latches at most once per word, the

switching duty cycle--and hence power dissipation in the comparison module--decreases with increasing word length. Other latching logic families, like those based on latching NAND gates, form the basis of alternative comparison circuits.²⁰

OPTICAL IMPLEMENTATIONS OF LATCHING LOGIC FOR COMPARISON

Latching logic gates can be fabricated using a variety of optical logic technologies. Each device technology has associated with it a set of performance characteristics that are crucial to the selection of the relevant application domain. Among the critical characteristics are switching speed, power, wavelength of operation, size and technological maturity. In this section, we will highlight a few of these device technologies and show how their individual characteristics limit their intended applications.

Bistable Fabry-Perot etalons can implement latching AND gates for the compare operation. The latching circuit we outlined above tolerates the low gain and contrast of etalons because the fan-out and -in required of the latching gates is at most one and three, respectively. Because of their high speed²¹ nonlinear etalons are well suited for switching broadband signals. The speed of the latching circuits based on etalons may be limited by the cavity build-up time required to reach the stable state. A device with a nonsymmetric cycle time²² (fast switch-on and slow switch-off) is useful if the packet frequency is small compared to the bit frequency.

Since at a fixed bandwidth the power dissipation in each comparison module decreases with increasing header length, large networks based on etalon comparison may be feasible. However as we shall see in the next section, large networks demand signal restoration whose total power dissipation grows with the bandwidth and network size. Anyhow, at a fixed bandwidth the power dissipation in the comparison module decreases with decreasing packet frequency. This is especially useful for applications that generate very long packets relatively infrequently such as inter-computer communications and video telecommunication.

Slightly slower speeds for comparison are possible with symmetric SEED devices serving as the latching AND gates.²³ Just as with bistable etalons, the latching SEED devices must wait for the positive feedback (in this case electrical) to build up to place the output in a stable state. Comparison units based on SEED devices offer a variable speed/power tradeoff:²⁴ therefore, higher levels of integration may be possible for low bandwidth signals before thermal dissipation becomes a problem. Thus, SEED arrays appear well suited for subscriber loop and intra-computer communications where the data rates are relatively lower but the number of channels is higher than the previous applications.

Bistable laser diodes also possess the necessary properties to implement latching logic. The high gain and contrast of laser diodes make them particularly well suited for environments where the

interstage connections create considerable losses and crosstalk. In addition, laser diode manufacturing technology has demonstrated its maturity, single mode fiber compatibility and ability to form 2-D arrays of devices. However the physical size and total power dissipation of the devices can be quite large, preventing their incorporation into very large integrated structures. Thus, they seem best suited for the trunk and inter-computer communications applications which involve a small number of high bandwidth channels.

There are alternatives for comparison implementation that are based on hybrid logic device designs. These designs detect the incoming light signals and then modulate one of the input signals or a bias signal to produce the desired logic operations.²⁵⁻²⁷ The primary advantage of this approach is that sophisticated electronic processing can be performed on the detected signal before it is applied to the modulator. For instance, complex switching nodes for store-and-forward packet switches may be attainable. The use of special modulating materials with intrinsic memory characteristics such as the Ferroelectric Liquid Crystals and other inorganic ferroelectric electrooptic materials will lead to latching logic devices. This technology is, however, immature and most device response times are on the order of milliseconds, making them too slow for the applications under consideration. New developments in

materials research to enhance the response time and successful incorporation of fast materials into functional devices will necessarily lead to a re-evaluation of this technology.

OPTICAL IMPLEMENTATION OF THE EXCHANGE UNIT

Spatial position encoded exchange units built with conventional non-latching logic can restore signal levels. Thus only signal to noise, crosstalk, uniformity, power and other systems engineering considerations limit the number of channels per stage and the total number of stages. Because noise does not propagate between stages, restoring exchange applies to deep networks. The schematic circuit diagram of the exchange unit is shown in Figure 5. The AND operation can be performed by any nonlinear optical device (all-optical or hybrid) with a sigmoidal input-output response and proper biasing. The two OR gates in the second stage receive signals that mutually exclusive, and hence can be implemented by passive combiners. As the logic expressions in Figure 5 indicate, the output H will be equivalent to A (and output L equivalent to B) if the exchange signal E is "0", and the signals at the output port will be interchanged if E is "1". Like the technology that is available for comparison, the networks based on restoring exchange devices span the spectrum from narrowband and large to broadband and small.

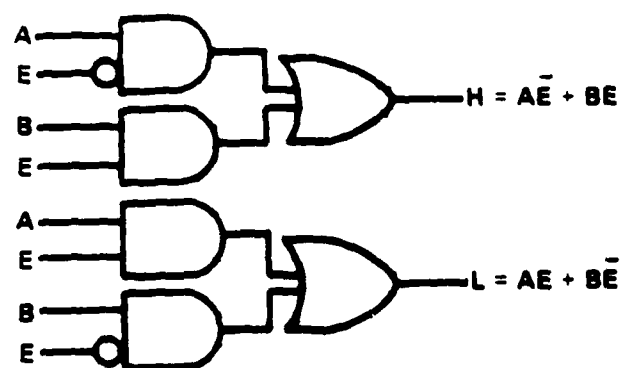


Figure 5. Regenerative Exchange Circuit.

The potential throughput per channel is greatly increased if the exchange module uses passive switches. In this case, the bandwidth of the message header is determined by the response time of the comparison logic while the trailing information can propagate at optical media bandwidths within the signal-to-noise limits imposed by losses in the passive switches. Polarization encoded switching using Wollaston prisms and controllable half-wave plates⁹ is one technology that performs passive routing. A photoactivated, polarization encoded exchange unit is shown in Figure 6. A photodiode, photoconductor or phototransistor receives the exchange signal and produces an electric field dependent change in the polarizability of the dynamic half-wave plate through the electrooptic effect. When activated, the dynamic half-wave plate rotates the polarization of the orthogonally polarized signal beams through 90°, thereby acting as a passive switch. The Wollaston prism or polarizing beamsplitter subsequently separates the high and low channels. The advantage of polarization switching, in addition to its passive nature, is that exchange occurs in one stage and the data may occupy the same spatial channel. Similarly, the data can be wavelength multiplexed for further increases in bandwidth. In addition, the fan-out of the previous comparison module only has to be one. However, the frame rate of optically controlled, dynamic half-wave device arrays is presently constrained to the millisecond regime by the material characteristics and the combined optical and electrical switching power dissipation limitations. Since exchange based on polarization-tagging is non-regenerative, the the number of

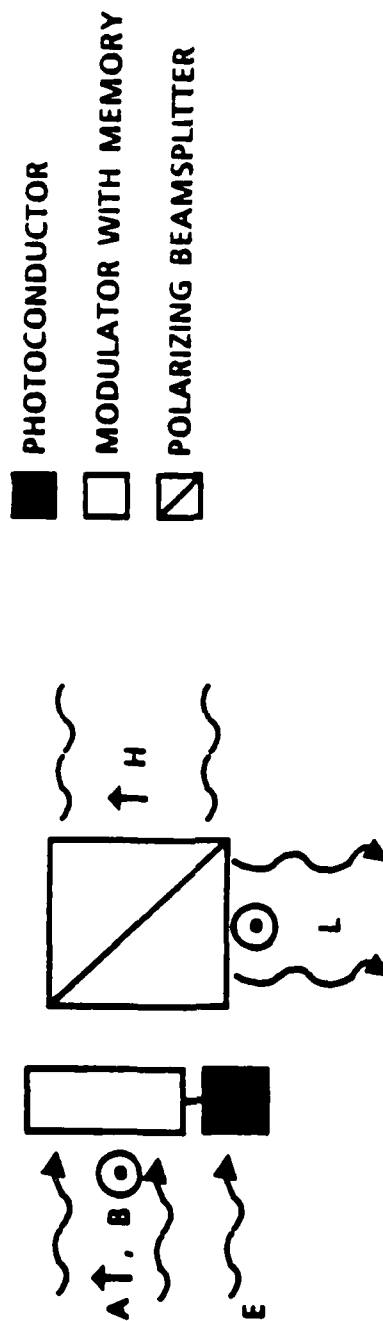


Figure 6. Polarization Encoded Exchange.

stages and thereby the number of inputs is primarily limited by absorptive, diffractive, sampling and scattering losses. Thus, they are limited to small networks with low packet frequency but high data rates like inter-computer communications or video telecommunications.

SUMMARY AND CONCLUSIONS

In this paper we reviewed why optical interconnects are appropriate to implement pipelined sorting networks for telecommunication and parallel-processing applications. We went on to propose optical implementations of the active compare-and-exchange operation that are essential to the sorting networks. In particular, we described a class of Boolean logic devices called latching logic which permits the design of simple, hardwired comparison modules. Latching logic significantly reduces the interconnect and gate complexity of the compare module over the non-latching logic approach. Based on the available device characteristics we outlined the application domains of sorters utilizing a variety of optical technology. Which technology one chooses depends on the requirements of the application of interest. One application where optics will compete most favorably with electronics is when the packets are long and infrequent, and where low delay and high throughput are paramount—for example video telecommunications and inter-processor message routing. Optics also appears competitive at the other extreme of intra-processor and subscriber-loop communication where the signals are much slower but involve very large numbers of channels.

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ALL-OPTICAL COMPARE-AND-EXCHANGE SWITCHES

All-Optical Compare-and-Exchange Switches

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Abstract—All-optical compare and exchange is experimentally demonstrated using ZnS bistable optical devices. The compare-and-exchange demonstration utilizes polarization multiplexing and filtering, and latching and bidirectional logic. The combination of 2-D arrays of compare-and-exchange modules with optical perfect-shuffle interconnections leads to pipelined optical sorting networks that can process large numbers of high-bandwidth signals in parallel. Optical sorting networks with these characteristics are applicable in telecommunication switches, parallel processor interconnections and database machines.

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I. Introduction

Sorting is one of the most common and well-understood topics in computer science. It is known that serial sorting algorithms require at least $O(N \log N)$ temporal complexity [1]. Hardware based on parallel sorting algorithms offers enhanced performance on problems that must rapidly sort large quantities of information. Since the number of clock cycles, devices and interconnects are limited resources in any processing environment, we need parallel algorithms with sublinear temporal and practical spatial complexity. In addition, the algorithms we choose must be optimum with respect to our specific implementation technology. For instance the mesh algorithms developed for VLSI require only nearest neighbor connections and are sublinear $O(N^{1/2})$ in temporal complexity [2]. Unfortunately, mesh algorithms must finish sorting one sequence before beginning another; thus their throughput is limited by their latency. On the other hand, the shared memory [3] and some network [4] algorithms have the lowest temporal complexity $O(\log N)$ of all sorting algorithms, but are not practical with current technology since they require globally reconfigurable interconnects and excessive spatial resources, respectively.

Network algorithms based on the bitonic sort [5] have sublinear temporal complexity $O(\log^2 N)$. Moreover, they can be pipelined in stages for high throughput; and thus, are useful in problems where throughput is as critical as latency. But the bitonic sorting network requires at least one globally-connected interstage communication pattern. For instance the perfect-shuffle [6] connection pattern transmits half the information present in the top half of a list to the bottom half and vice versa. Because VLSI is confined to the 2-D surface of a chip and electrons in wires are capacitively coupled, practical electronic perfect-shuffles are limited to small numbers of channels and low data rates. In contrast, the noninteracting nature of photons and 3-D connection capability of optics allows optical perfect-shuffle networks to have large numbers of parallel channels and high data rates [7]-[9]. Thus, optical sorting networks based on the perfect-shuffle interconnection and bitonic algorithm are desirable when the number of communication channels or the data rates exceed the capabilities of electronic systems.

In particular, optical sorting networks are applicable in telecommunication switches that route high-bandwidth optical data packets [10]. Telecommunication switches must handle many parallel channels, have low latency and keep up with the packet generation rates. Similarly, high-throughput sorters serve as the communication

fabric of electronic multiprocessors [11]. In these parallel processors the number of processing elements, and thereby the computational power, is governed by the number of parallel data channels. Furthermore, the throughput of each processing element is limited by the interconnection latency and throughput. In addition, sorting hardware may serve as dedicated subsystems for parallel database operations [12] in conjunction with optical memories [13]. Parallel and independent memory access can generate data rates beyond the capabilities of electronic systems.

Network sorting algorithms need, in addition to perfect-shuffle interconnections, 2x2 self-routing crossbar switches where each routing decision depends on the relative magnitude of the local information. Hence, we desire implementations of the 2x2 self-routing crossbars that are compatible with optical interstage connections and fulfill the requirements of bandwidth and parallelism in sorting applications. The function of such self-routing crossbars can be separated into the operations of comparison and exchange: comparison determines the relative magnitude of the local data; exchange configures the crossbar switch dependent on the outcome of the comparison.

In all subsequent discussions we assume a binary representation for the data. Overscores represent the invert operation; thus $\bar{R}_1$ and $\bar{R}_2$ are the logical complements of the system reset. Brackets "[]" contain a latching condition which we will explain shortly.

An algorithm for compare and exchange proceeds as follows: we label the synchronous input channels A and B, and operate serially from most to least significant bit. If $A_i > B_i$ occurs before $B_i > A_i$, where i represents the bit position, then the switch latches into the "don't-exchange" position. Conversely if $B_i > A_i$ occurs first then the switch latches into the exchange position (Fig.1). Latching implies that once an inequality has been detected, the exchange switch becomes set into one particular configuration until the system is reset.

Optical bistable devices have the potential for high-speed optical signal processing and computing [14]-[15]. ZnS and ZnSe bistable interference filters have already been used to demonstrate simple digital optical circuits, pattern recognition, symbolic substitution, and one-bit addition, because they can be operated in the visible spectrum and are relatively easy to fabricate [16]-[17]. In this paper we experimentally demonstrate a circuit that performs compare and exchange with ZnS interference filters as bistable devices. Here the ZnS interference filters are used in less common modes of operation including latching and bidirectional logic. In addition

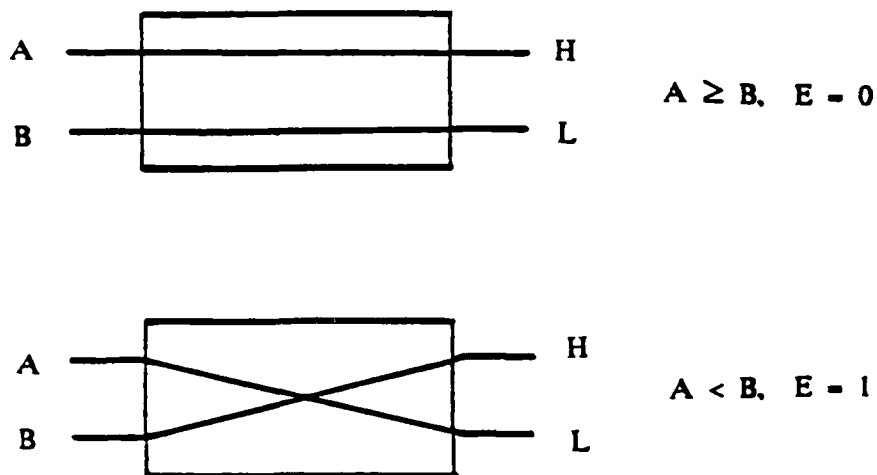


Figure 1. The compare-and-exchange module. E represents the exchange signal, A, B represent the two input numbers, and H, L represent the higher number and the lower number, respectively.

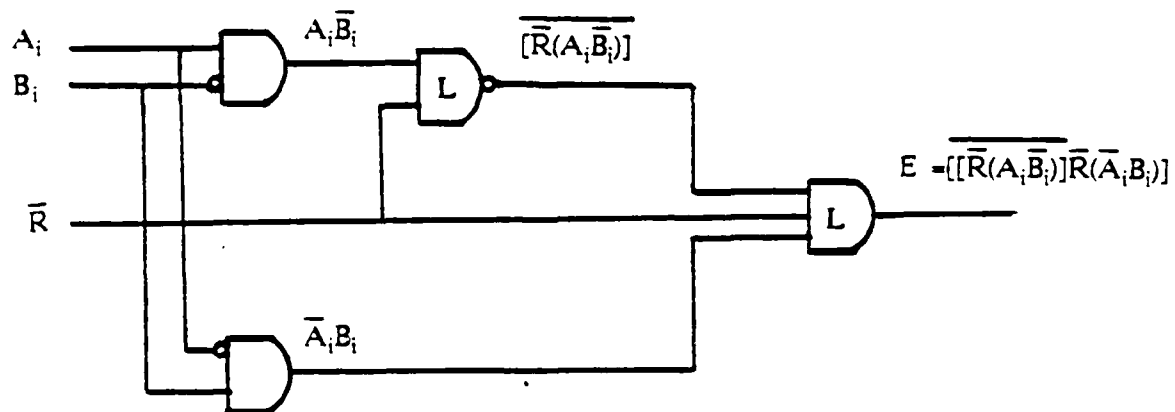


Figure 2. Compare circuit in which L indicates the latching logic gate.

we employ polarization multiplexing and filtering to achieve channel isolation, 4-port bidirectional devices and reduced feedback. In the next section we outline the design of one possible compare-and-exchange circuit without regard to the implementation technology. We also illustrate the expected operation of each part of the circuit. In the following section we present the general layout and operation of the compare-and-exchange design using ZnS interference filters along with polarization multiplexing and filtering. In the discussion section we compare the experimental and expected results. We conclude with some general comments.

II. Compare-and-Exchange Circuit Design

More than one circuit design is possible for comparison [18]. The circuit diagram for the comparison circuit demonstrated in this paper is shown in Fig.2. It consists of three parts. The first part is a comparator to distinguish between the cases where $A_i > B_i$ or $A_i < B_i$. Fig.3 shows how this can be done by generating $A_i \bar{B}_i$ and $\bar{A}_i B_i$. In the second and third parts, two latching gates are employed, so that when $A < B$, $\bar{A}_i B_i = 1$ comes first, and one latching gate will be switched-on to give an exchange signal $E = 1$. It remains in the on-state until all the bits of A and B are transmitted. Similarly, when $A > B$, $A_i \bar{B}_i$ comes first, and another latching gate will be switched-on to prevent the exchange. From Fig.3 we see that $A_i \bar{B}_i = 1$ and $\bar{A}_i B_i = 1$ never occur simultaneously, making it possible to separate the state of the latching gates.

Like comparison, however, there is more than one way to implement exchange. The appropriate choice depends on the application requirements, the technology characteristics and the corresponding comparison circuit. For demonstration purposes we will construct an active exchange module. If the exchange signal $E = 1$ is present, it sends B to the H-output and A to the L-output. Otherwise if the exchange signal is 0, it sends A to H-output and B to the L-output.

The above discussion shows that our circuit design needs a comparator, two latching gates, and an exchanger. Fig.4 shows that $A_i \bar{B}_i$ and $\bar{A}_i B_i$ can be generated from a single bistable etalon by using its reflections from both sides, so that a single bistable device can be used as a comparator. The latching operation is also natural for bistable devices, so that the two latching gates are just two bistable devices. Another bistable device is used as the exchanger with its transmission determined by the exchange signal. The details of their operations are discussed in the following section.

A_i	B_i	$A_i \bar{B}_i$	$\bar{A}_i B_i$
0	0	0	0
0	1	0	1
1	0	1	0
1	1	0	0

Figure 3. The use of $A_i \bar{B}_i$ and $\bar{A}_i B_i$ to compare A and B. When $A < B$, $\bar{A}_i B_i = 1$ will appear first. When $A > B$, $A_i \bar{B}_i = 1$ will appear first.

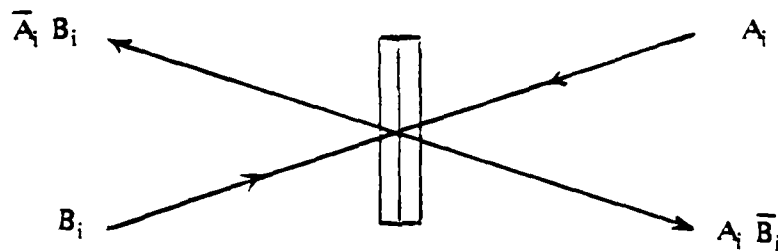


Figure 4. Generation of $A_i \bar{B}_i$ and $\bar{A}_i B_i$ using a single bidirectional, reflection-mode Fabry-Perot etalon.

III. Experimental Demonstration

The experimental layout for the compare-and-exchange circuit is shown in Fig.5. An Argon laser and a phase grating generate four optical beams, each having a peak power of about 40 mW. A chopper modulates beams A and B with the test sets, and blocks the holding beams $\bar{R}_1$ and $\bar{R}_2$ between each test set to allow the latching gates to reset. A half-wave plate gives the two holding beams $\bar{R}_1$ and $\bar{R}_2$ s polarization. A quarter-wave plate gives the beams A and B circular polarization.

For the experimental demonstration of all-optical compare and exchange we choose test vectors of $A = 110001$, $B = 101011$ and $A = 100011$, $B = 110101$. In the former set of test vectors $A_i > B_i$ occurs first; all four permutations of $A_i B_i$ follow to ensure that the switch is properly latched. Similarly, for the latter group of test vectors we find that $B > A$ and demonstrate the exchange stability to further permutations. Up until the first mismatch the position of the exchange switch is not important to first-order approximation since the output data streams are identical. In Fig.6 we depict the expected operation of the latching compare and passive circuits described above for both test sets. All data used in the simulations are based on the structure of each filter. The curves are drawn upside down to be consistent with the experimental photographs. We see that whether $A > B$ or $A < B$, the larger number always goes to the H-output. We did not fit the simulations with the experimental results because we wanted to show the ideal results with suitable devices. The transfer functions shown in Fig.7 used the same data.

The compare circuit operates in the following manner. The circularly polarized data beams, A and B, are incident on two polarizing beam splitters (PBS's). These PBS's serve two functions. One function is to sample the data beams for the compare operation: the p-polarization from the A channel propagates through the PBS for comparison, the s-polarization is reflected to the exchange switch; conversely, the s-polarization of the B beam is reflected for comparison and the p-polarization propagates through the PBS to the exchange switch while its polarization is rotated by the half-wave plate to match that of A. The orthogonally polarized data beams that were injected into the compare circuit are converted to circular polarization by two quarter-wave plates. The circularly polarized data beams are incident on the first interference filter (IF_1).

IF_1 operates in reflection mode as a bidirectional comparator. If B_i is zero and if A_i is one, then the circularly polarized A_i is reflected by IF_1 , converted to the s-polarization by the quarter-wave plate and reflected by the PBS to produce the signal

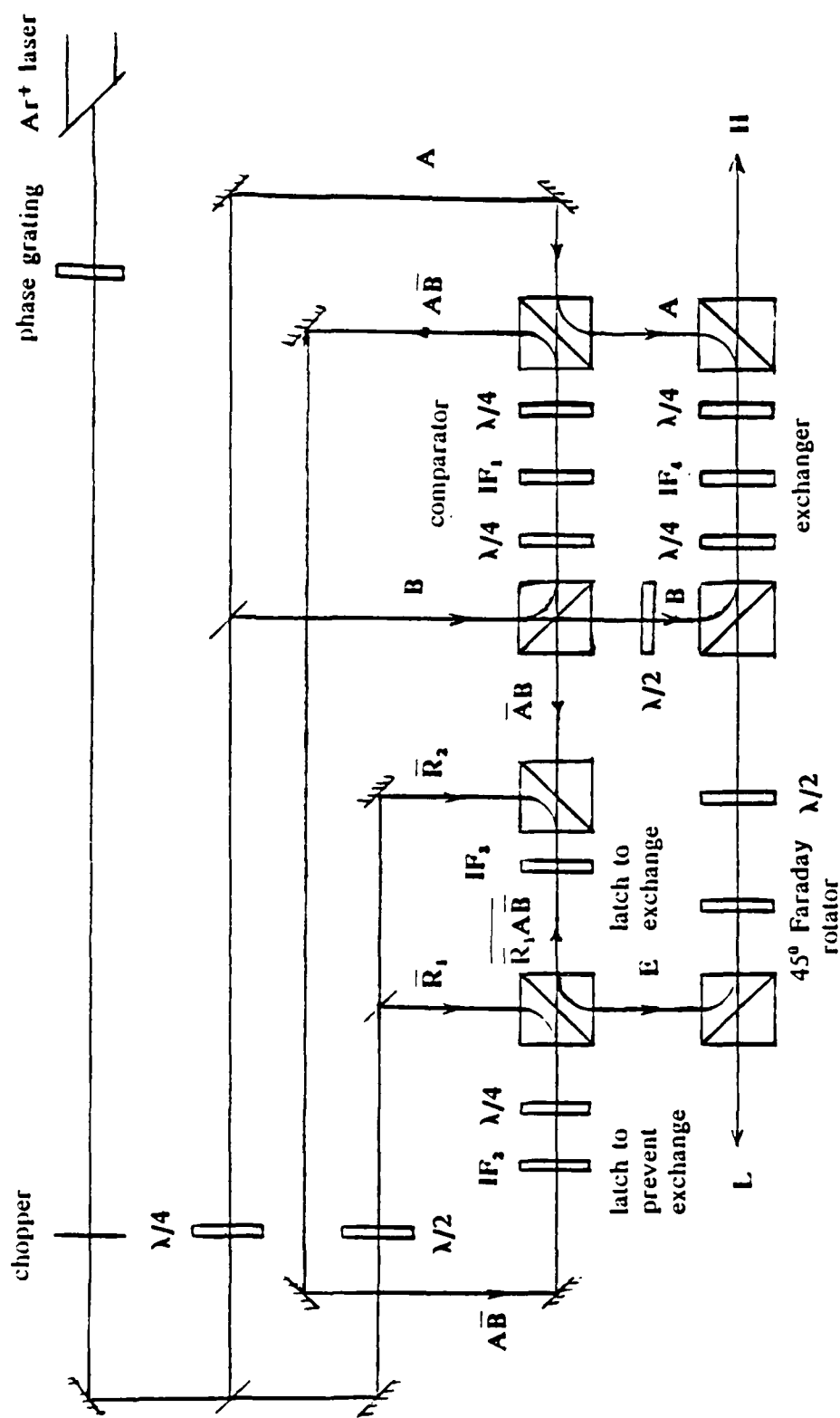


Figure 5. Experimental layout for all-optical compare and exchange with IF-ZnS interference filter, $\lambda/2$ -half-wave plate, $\lambda/4$ -quarter-wave plate. E represents the exchange signal, A, B represent the two binary encoded numbers, and H, L represent the outputs of the larger number and the smaller number, respectively.

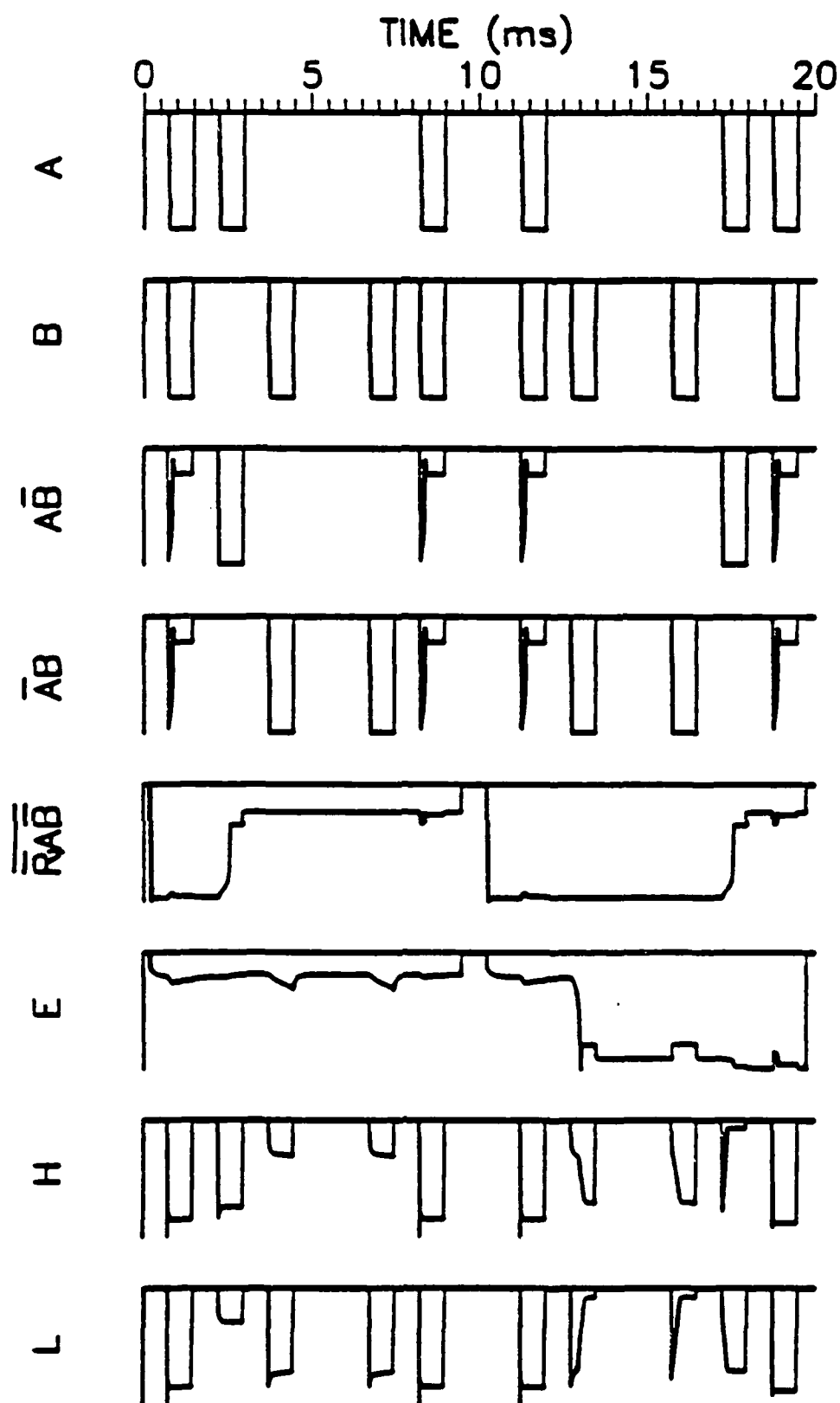


Figure 6. Expected operation of compare-and-exchange circuits test set 1 and 2 on horizontal axis. All curves are drawn upside down consistent with the experimental photographs. The vertical axes are in arbitrary units.

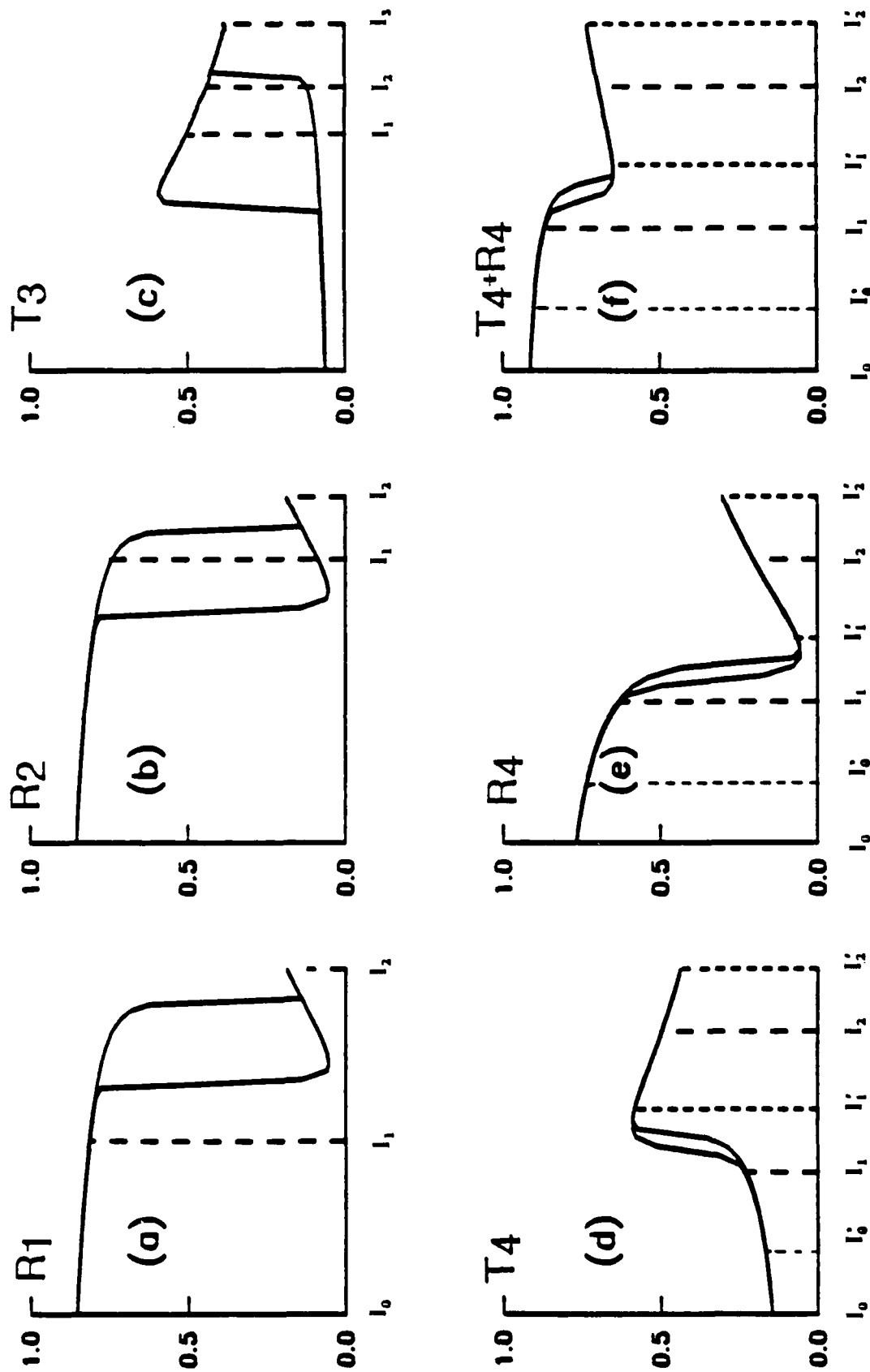


Figure 7. Computer simulated transfer functions for the ideal interference filters. The horizontal axes are input power in arbitrary units and the vertical axes are reflectivity or transmissivity of the filters. (a). Reflectivity R_1 of the comparator IF1 with $I_0=0$, $I_1=A_i$ (or B_i), and

$I_2 = A_i + B_i$; (b). Reflectivity R_2 of the latching **NAND** gate
 IF₂ with $I_1 = \bar{R}_i$, and $I_2 = \bar{R}_1 + A_i \bar{B}_i$; (c). Transmissivity
 T₃ of the latching **AND** gate with $I_1 = \bar{R}_2$, $I_2 = \bar{R}_2$
 + $\bar{R}_1 A_i \bar{B}_i$ (or $\bar{R}_2 + \bar{A}_i B_i$), and $I_3 = \bar{R}_2 + \bar{R}_1 A_i B_i$
 + $\bar{A}_i B_i$; (d). Transmissivity T₄ of IF₄ with $I_0 = 0$, $I'_0 = E$,
 $I_1 = A_i + B_i + E$; (e). Reflectivity R₄ of IF₄ with
 definitions as in (d); (f). The sum of (d) and (e).

$A_i \bar{B}_i$. In a similar fashion if A_i is zero and B_i is one, then the circularly polarized B_i is reflected by IF_1 , converted to the p-polarization by the quarter-wave plate and transmitted through the PBS to produce the signal $\bar{A}_i B_i$. Thus the PBS's also function as part of a bidirectional switch. Since the filter inputs are A_i and B_i and the outputs are both $\bar{A}_i B_i$ and $A_i \bar{B}_i$, IF_1 is a 4-port device.

$[\bar{R}_1 \bar{A} \bar{B}]$ is the exchange prohibited signal from IF_2 , which works in reflection mode as a latching NAND gate (See Fig.7b). As long as $A_i \bar{B}_i = 0$, the reflection of $\bar{R}_1$ is high, which has been polarization rotated so it passes through PBS helping IF_3 to switch on and latch to have a high transmission when $\bar{A}_i B_i$ becomes 1 (See Fig.7c). This is the exchange situation with $E = 1$. If $A_i \bar{B}_i$ becomes 1, IF_2 switches on and latches to have a low reflectivity; the reflection of $\bar{R}_1$ will be low thereafter. If this takes place before the first occurrence of $\bar{A}_i B_i$ equal to 1, IF_3 will never have enough input power to switch on, and the output of exchange signal E will always be low (See Fig.10).

The final filter IF_4 is the exchanger and works in both transmission and reflection modes (See Figs.7d-7f). If both A_i and B_i are 0, both outputs are 0 independent of the exchange signal. In the case that $E = 0$ and only one of A_i and B_i is 1, IF_4 will not switch on; beam A_i reflects to the high output on the right; beam B_i reflects to the low output on the left. If both A_i and B_i are 1, IF_4 switches on and has a high transmissivity and low reflectivity. Both sides have a high transmission independent of the exchange status. The exchange control signal E will move the transmission curve closer to the laser frequency. When $E = 1$, either signal (or both) can switch on the gate; then A_i and B_i are transmitted to the opposite sides, in other words they are exchanged.

Fig.8 shows the results of the comparator. It demonstrates clearly that as soon as there is a difference between A_i and B_i , the comparator has a high output to the following corresponding gate which makes the appropriate decision. At the first bit, numbers A_i and B_i are equal. The output goes from a high reflection rapidly to a low reflection and produces a sharp peak pulse at the rising edge of the output. If the signal pulse width is large enough compared to the width of the sharp pulse, this sharp pulse will not have enough power and would not switch the next stage. Before each comparison of the input numbers, $\bar{R}_1$ and $\bar{R}_2$ are reset to 1. When the compare and exchange is over, $\bar{R}_1$ and $\bar{R}_2$ are shut off. The system is waiting for the next operation. Fig.9 shows the exchange prohibited signal $[\bar{R}_1 \bar{A} \bar{B}]$. Upon the first occurrence of $A_i > B_i$, this signal latches to a low output. Fig.10 shows the exchange

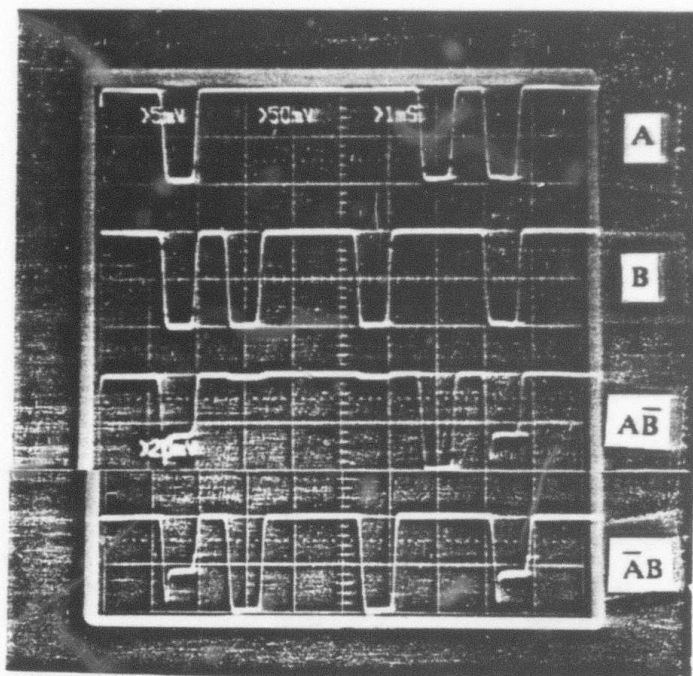


Figure 8. Experimental results of the inputs A, B and the logic outputs AB , $\overline{AB}$. The input powers are 11 mW each, and the output power is about 5 mW.

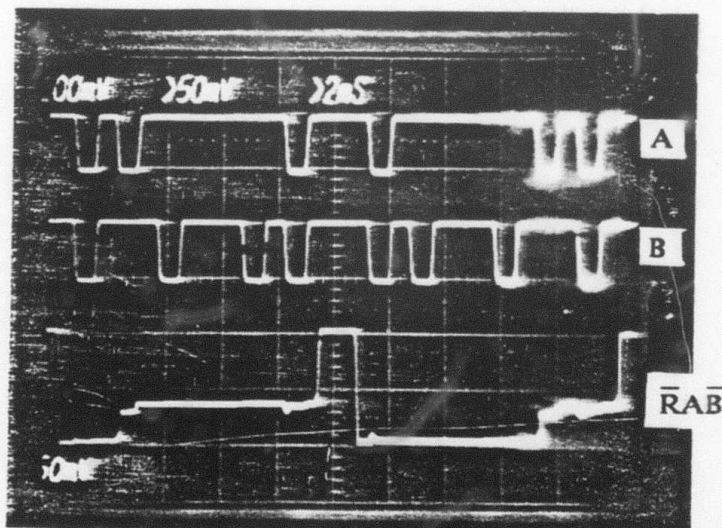


Figure 9. Output of the exchange-prohibited signal $\overline{R_1 AB}$. The upper two traces show the two groups of numbers coming into the system. In the first group A is larger than B and in the second one, B is larger than A. The power of the holding beam is 19 mW, and the output power is about 6 mW.

signal E which is the transmission of $\bar{R}_2$. On the left part of Fig.10, although two cases of $B_i > A_i$ occur, E remains in its low state because the earlier occurrence of $A_i > B_i$ latched the exchange prohibited signal to 0. On the right part of Fig.10, A is larger than B. Upon the first occurrence of $A_i > B_i$, E is latched to 1, and therefore all the following bits exchange their positions. The time delay at the rising edge of E is caused by the switching speed of the device. Figs.11 and 12 show the results of compare and exchange in the two cases of $A > B$ and $A < B$, respectively.

IV. Discussion

From the experimental results of the all-optical compare-and-exchange circuit one can see that the contrasts are not as good as those in the simulations. This is because the filters used in the experiment were not specially designed for reflection-mode operation. Therefore the low state of the reflection is higher than we expected. However even with such non-optimal filters, the system worked. The contrasts of the outputs could be better by using specially designed reflection-mode filters. This would also decrease the power required. Another bistable optical device, with its threshold set half way between the worst case levels 0 and 1, could amplify the outputs of the exchanger as well as enhance the contrast. Then the outputs could be used to drive the next compare-and-exchange module in a self-routing optical network.

It was not easy to obtain stable operations of all of the four interference filters simultaneously long enough to test the system, especially since the contrasts of the devices are not so good. The data in Figs.8-12 were taken with only the relevant section working. Figs.8-10 were taken from the compare unit consisting of IF_1 - IF_3 . And Figs.11-12 were the results from the exchange unit of IF_4 . While we were doing the exchange, we used a third beam having the power consistent with the exchange control signal E. Therefore, the experimental results do not show the delay as seen in the simulations. We also did the experiment with IF_1 and IF_3 producing a real exchange signal for the last gate to show that when $A < B$, the exchanger works.

It was also not easy to focus A, B and E onto IF_4 and have H and L come out without energy losses when the respective polarization directions are considered. A 45° Faraday rotation glass and a half-wave plate placed between the exchange control signal E and IF_4 might solve this problem. A plane-polarized light beam passing through the glass will have its polarization direction rotated through an angle θ relative to the polarization direction of the incident beam. A beam coming from the

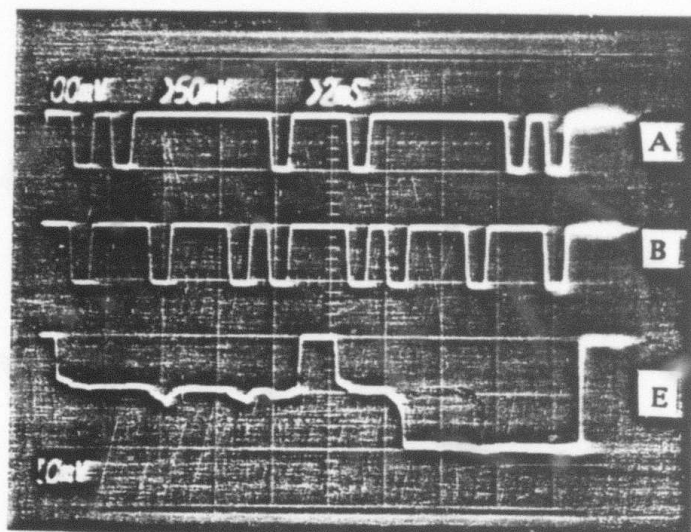


Figure 10. Output of the exchange signal E. The holding power is 20 mW, and the output power is 5 mW.

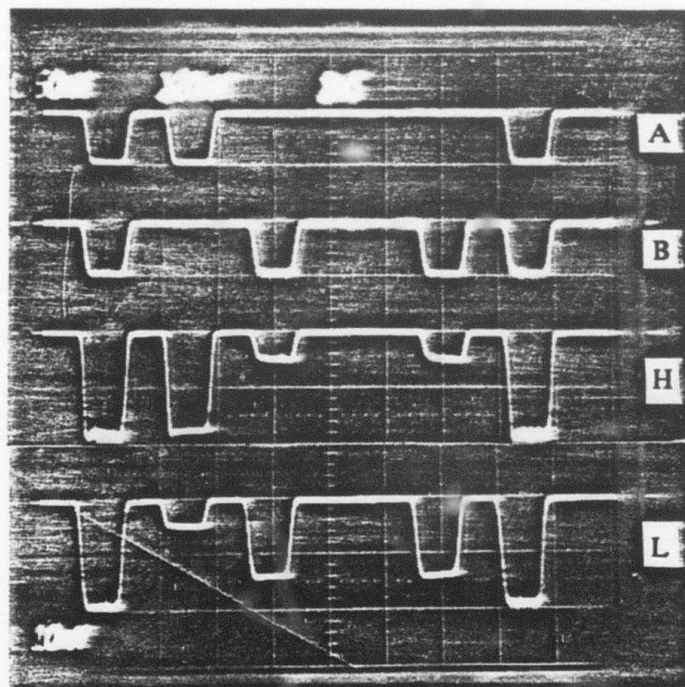


Figure 11. The high output and the low output of the system with $A > B$. The input power is 14.5 mW, and the output power is 6.5 mW.

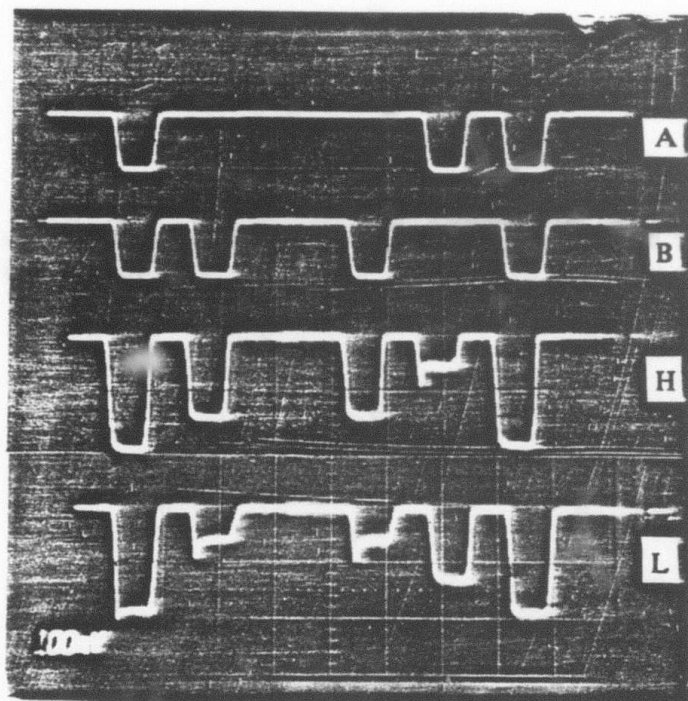


Figure 12. The high output and the low output of the system with $B > A$. The input power is 14.5 mW, and the output power is 6.5 mW.

opposite direction will have its polarization rotated in the same direction. Let θ be 45° and the fast axis of the half-wave plate be 67.5° with respect to the incident plane of vibration of E. Then the polarization direction of E propagating to the right will be rotated 90° , while that of L which propagates to the left will be unchanged. A Faraday rotator as shown in the experimental layout was not available during the experiment. Instead, only a half-wave plate was used to rotate the plane of the vibration of E by 90° and make E go to IF_4 , so that the system could work. By slightly detuning the half-wave plate, a small transmission of L is detected.

The power of the exchange control signal E in our experiment is small compared to those of numbers A and B. So the exchange operation in our case has to be active. That is when the exchanger is set to exchange status, it has to be switched on for each following bit. The operation speed is then limited by this switching speed. However, if E could be twice as large as A and B, the exchanger could operate as follows: While $E = 0$, IF_4 can not be switched on, and always keeps a high reflectivity, so that the input signals are reflected back, the exchanger operates like a mirror. While $E = 1$, IF_4 switches on and keeps a high transmissivity, so that the input signals are transmitted to the opposite sides and exchanged. The advantage is that after the exchanger is set, the following data could have a extremely high-speed transmission, since everything is linear after the exchange decision has been made.

The polarization encoding is the key to the compare-and-exchange realization. It not only reduces the energy losses in combining signals but also reduces the influences of crosstalk and feedback. The effect of the unused transmissions and reflections has been reduced to a minimum using polarization filtering. Transmissions of A and B through IF_1 and the transmission and reflection of E from IF_4 propagate back toward the source of A and B. The reflection of R_2 from IF_3 reflects directly back. Half of the high transmission of R_1 goes to IF_1 . But in this case, a decision has been made, and IF_1 is no longer used until the next operation begins. The transmission of $\bar{A}B$ through IF_3 can propagate to IF_2 which can only be high when an exchange decision is made. And half of the transmission of $A\bar{B}$ from IF_2 can propagate to IF_3 . But this can be eliminated with an additional Faraday rotator which also prevents $\bar{R}_1$ from feeding back to IF_1 .

The use of the on-axis, normal incidence makes the system extendable to operation on arrays, so that two-dimensional inputs could be compared and exchanged at the same time in parallel.

By using 2-D arrays of bistable devices and folded perfect-shuffle interconnections [18], optical sorting networks may be feasible for large numbers of channels, but first, system engineering issues must be addressed like cascadability, uniformity, crosstalk, reliability and heat dissipation.

The ZnS interference filters have relatively slow switching times (milliseconds) because they are based on thermal nonlinearities, making real-system applications unlikely. On the other hand, much faster compare-and-exchange modules based on GaAs Fabry-Perot etalons [19] may increase the throughput of the sorting networks. GaAs embodiments of the compare-and-exchange designs demonstrated here appear ideal for packet-switching telecommunication networks because GaAs etalons are diode-laser compatible [20] and allow rapid reconfiguration of very high-speed data channels.

V. Conclusions

All-optical compare and exchange has been demonstrated using bistable optical devices. The ZnS interference filters used required a speed of 3 ms per bit and a total four-filter power of about 100 mW. The experimental setup is extendable to operation on arrays and to other bistable optical devices. The switching times might be reduced to picoseconds using GaAs etalons, making the system more competitive with alternative approaches.

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