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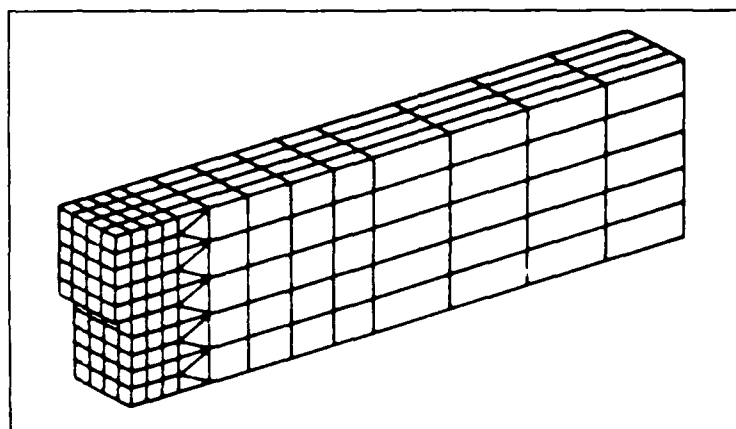
NCEL

Technical Report

By L.J. Malvar (UCLA) and
G.E. Warren (NCEL)Sponsored By Chief of
Naval Research

AD-A208 730

ANALYTICAL MODELING OF REINFORCED CONCRETE IN TENSION



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ABSTRACT A smeared crack approach to fracture of concrete in mode I was implemented in the finite element program ADINA. Nonlinear concrete elements with tensile cracking were modified to include tensile strain softening. When an element at an integration point cracks, the stiffness perpendicular to the crack is reduced to zero and the tensile stress across it is set as a function of the crack opening. Equilibrium iterations were implemented to redistribute stress. Two- and three-dimensional models of a single edge notched beam in three-point bending were analyzed and compared to experimental results with good agreement. The analytical representation of mixed mode fracture was also addressed. The mechanisms of shear transfer across a crack were detailed, and the rough crack model, relating shear stress to crack opening, is presented with discussions on orientation of successive crack planes, tensorial invariance, and snap-back phenomena. Problems are identified with modeling bond at the concrete/reinforcement interface and its effect on crack patterns.

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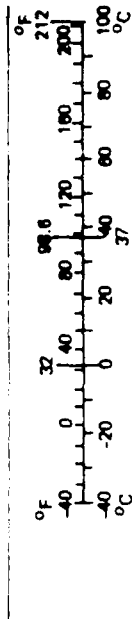
Approximate Conversions to Metric Measures

Symbol	When You Know	Multiply by	To Find	Symbol
LENGTH				
in	inches	2.54	centimeters	cm
ft	feet	30.48	centimeters	cm
yd	yards	0.9	meters	m
mi	miles	1.6	kilometers	km
AREA				
m ²	square inches	6.5	square centimeters	cm ²
ft ²	square feet	0.09	square meters	m ²
yd ²	square yards	0.8	square meters	m ²
ac	square miles	2.6	square kilometers	km ²
	acres	0.4	hectares	ha
MASS (weight)				
oz	ounces	28	grams	g
lb	pounds	0.45	kilograms	kg
	short tons (2,000 lb)	0.9	tonnes	t
VOLUME				
ts	teaspoons	5	milliliters	ml
T	tablespoons	15	milliliters	ml
fl oz	fluid ounces	30	milliliters	ml
c	cups	0.24	liters	l
pt	pints	0.47	liters	l
qt	quarts	0.95	liters	l
gal	gallons	3.8	liters	l
ft ³	cubic feet	0.03	cubic meters	m ³
yd ³	cubic yards	0.76	cubic meters	m ³
TEMPERATURE (exact)				
°F	Fahrenheit temperature	5/9 (after subtracting 32)	Celsius temperature	°C

Approximate Conversions from Metric Measures

When You Know	Multiply by	To Find	Symbol
LENGTH			
millimeters	0.04	inches	in
centimeters	0.4	inches	in
meters	3.3	feet	ft
meters	1.1	yards	yd
kilometers	0.6	miles	mi
AREA			
square centimeters	0.16	square inches	in ²
square meters	1.2	square yards	yd ²
square kilometers	0.4	square miles	mi ²
hectares (10,000 m ²)	2.5	acres	ac
MASS (weight)			
grams	0.035	ounces	oz
kilograms	2.2	pounds	lb
tonnes (1,000 kg)	1.1	short tons	
VOLUME			
milliliters	0.03	fluid ounces	fl oz
liters	2.1	pints	pt
liters	1.06	quarts	qt
liters	0.26	gallons	gal
cubic meters	35	cubic feet	ft ³
cubic meters	1.3	cubic yards	yd ³
TEMPERATURE (exact)			
Celsius temperature	9/5 (then add 32)	Fahrenheit temperature	°F

* 1 in. = 2.54 (exact). For other exact conversions and more detailed tables, see NBS Metric Publ. 286, Units of Weights and Measures, Price \$2.25, SD Catalog No. C13 10 286.



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CONTENTS

	Page
PURPOSE	1
PART 1: THREE-DIMENSIONAL MODE I CRACK PROPAGATION	2
INTRODUCTION	2
THE SMEARED CRACK APPROACH	2
STRESS - STRAIN LAWS	4
Linear Softening	4
Nonlinear Softening	4
TEST SERIES	6
FINITE ELEMENT ANALYSIS	7
FINITE ELEMENT RESULTS	10
Two-Dimensional Model	10
Three-Dimensional Model	10
DISCUSSION	10
Two-Dimensional Model	10
Three-Dimensional Model	11
PART 2. SHEAR TRANSFER	17
INTRODUCTION	17
SHEAR TRANSFER	17
EXPERIMENTAL BACKGROUND	17
ANALYTICAL BACKGROUND	18
THE ROUGH CRACK MODEL	18
IMPLEMENTATION IN ADINA	20
PRINCIPAL AXES ROTATION	20
The Rotating Crack Model	20
The Multiple Crack Model	21

	Page
ORTHOTROPIC VERSUS ANISOTROPIC MODELS	21
SNAP-BACK AND INSTABILITY	21
PART 3. BOND-SLIP	23
INTRODUCTION	23
INTERFACE ELEMENTS	23
BOND MECHANISMS	23
EMPIRICAL BOND-SLIP RELATIONSHIPS	24
EFFECT OF BOND ON CRACK PATTERN	24
CONCLUSIONS AND RECOMMENDATIONS	25
Mode I Fracture	25
Mixed Mode Fracture	25
Bond-Slip	25
REFERENCES	27
APPENDIXES	
A - Fictitious Crack Model	A-1
B - Crack Band Model, Two-Dimensional	B-1
C - Crack Band Model, Three-Dimensional	C-1



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PURPOSE

The Office of Naval Research (ONR) through the Naval Civil Engineering Laboratory (NCEL) has initiated a project to develop fracture mechanics methodology for design application of reinforced concrete elements in tensile and shear stress states. Since completion of an experimental program to establish the fracture energy parameters of plain concrete reported in Reference 1, efforts have been directed to the analytical formulation and modeling of tensile behavior of concrete. The purpose of this report is to present analytical modeling methodology of mode I (crack opening), mixed mode crack propagation (shear), and concrete reinforcing interface behavior (bond).

This report supports the project "Fatigue and Fracture of Concrete" in the ONR 6.1 Basic Research Program YR023.03.01B, Structural Modeling. In addition to design and analysis applications, concrete fracture mechanics methodology will eventually be incorporated into damage and condition assessment process of existing in service reinforced concrete facilities.

Concrete cracking in tension is the major factor contributing to the nonlinear behavior of reinforced concrete elements. The modeling of cracking in shear-critical members is most important since it will determine the ultimate resistance and post-failure behavior.

Crack propagation is facilitated when the material is in a state of plane strain. The material of thick members is in a state close to plane strain in the interior and in a state of plane stress along the edges. An accurate representation of the cracking will be obtained only if three-dimensional effects are considered. In the first part of this report a smeared crack representation is formulated and implemented in the two- and three-dimensional nonlinear concrete elements of the computer code ADINA (Ref 2). Experimental results from tests carried out on single edge notched beams show good agreement when compared to the analytical predictions.

Fracture of concrete may occur in three ways: Mode I (opening), II (shearing) and III (tearing). Although pure modes may be encountered, mixed mode propagation is more likely. In the second part of this report existing models of mode II and mixed mode constitutive relations are evaluated. Mixed mode crack propagation involves considering the transfer of shear forces across cracks. As a consequence, successive crack planes may form; these need not be orthogonal to each other. This report also addresses the analysis of shear transfer across cracks.

Crack distribution is greatly affected by the reinforcement-concrete interface behavior. Proper modeling of the bond stress-slip relationship is needed for an accurate prediction of the crack pattern. Bond-slip is addressed in the third part of the report.

The modifications implemented in ADINA in each case have been compiled in Appendixes A, B, and C.

PART 1. THREE-DIMENSIONAL MODE I CRACK PROPAGATION

INTRODUCTION

Finite element modeling of concrete fracture mechanics is a versatile tool for analysis. The implementation of a nonlinear discrete crack model has already been evaluated (Ref 1). However, discrete crack models present the difficulty of varying mesh topology to represent the crack advance. Modeling the crack advance is further complicated if the analysis is three-dimensional.

A smeared crack or crack band approach was implemented in the finite element program ADINA (Ref 2). The fracture zone was modeled as a band of uniformly distributed parallel microcracks having a blunt front. This concept was pioneered by Rashid (Ref 3), developed by Bazant et al. (Ref 4 through 7), and is also known as the Crack Band Model (CBM).

After implementation of the CBM approach into the two- and three-dimensional (2-D and 3-D) nonlinear concrete elements of ADINA, the performance of the models was evaluated by analyzing the results of the test series reported in Reference 1.

THE SMEARED CRACK APPROACH

Numerous experiments conducted on tensile specimens have shown that after crack formation, tensile stresses are transferred across the crack and their magnitude decreases with crack opening. Two stress-versus-crack width relationships have been formulated that are suitable for finite element applications. The Fictitious Crack Model (FCM) (Ref 8) represents a single crack development by separating the elements via introduction of new nodes and imposes nodal forces equivalent to the transferred stresses. The Crack Band Model transforms the crack opening, w , into strain, ϵ , dividing it by the element width and obtaining an equivalent stress versus strain ($\sigma - \epsilon$) relationship.

The CBM approach assumes that cracked elements show a strain softening behavior; i.e., the element stiffness is negative. This leads to a stiffness matrix not definitely positive, which would make the solution of finite element equations difficult and result in large errors. Strain softening in ADINA is included for concrete elements subjected to stresses beyond the maximum compressive stress. Upon reaching maximum compressive stress, zero (very small) stiffness is assigned coupled with isotropic conditions, and the stress increments are computed from a uniaxial stress-versus-strain law. A similar approach can be implemented in tension. Upon cracking at an integration point, a zero stiffness can be assigned across the crack and the stress increments can be derived from an equivalent, empirical stress-versus-strain law. The tensile model becomes orthotropic (Ref 9). Iterations are then required to satisfy equilibrium.

While transforming the stress-versus-crack-width relationship ($\sigma - w$) to stress-versus-strain ($\sigma - \epsilon$), the element width is included, resulting in a solution dependent on element size. In order to circumvent this condition, Bazant and Cedolin (Ref 5) suggested linking the relationship to the fracture energy, G_f , forcing the empirical $\sigma - \epsilon$ law to verify

$$G_f = h \int_0^{\epsilon_0} \sigma d\epsilon \quad (1)$$

where h is the band width, ϵ the strain and ϵ_0 the strain beyond which no stress is transferred. It is implied that the fracture energy (the energy needed to create a unit fracture area along the crack path) is uniformly distributed across the width of the fracture zone (band width).

Equation (1) is verified if

$$\sigma/f_t = f(w/w_0) \quad (2)$$

which satisfies

$$G_f = \int_0^{w_0} \sigma dw = w_0 f_t \int_0^1 \sigma/f_t d(w/w_0) \quad (3)$$

where

w = crack width or crack opening

w_0 = crack width beyond which no stress is transferred

f_t = tensile strength

and

$$w/w_c = \epsilon - \sigma/E$$

$$w_0/w_c = \epsilon_0$$

$$\begin{aligned} w/w_0 &= (\epsilon - \sigma/E)/\epsilon_0 = \epsilon/\epsilon_0 - (\sigma/f_t)(f_t/\epsilon_0 E) \\ &= \epsilon/\epsilon_0 - (\sigma/f_t)(\epsilon_p/\epsilon_0) \end{aligned} \quad (4)$$

where

w_c = element width

E = Young's modulus of concrete

ϵ_p = the strain corresponding to tensile strength

Substituting Equation (4) into Equation (2) yields:

$$\sigma/f_t = f(\epsilon/\epsilon_0, \sigma/f_t)$$

In general it is difficult to explicitly obtain stress.

In Reference 1, different $\sigma - w$ laws were evaluated. A more recent one has been presented by Cornelissen et al. (Ref 10) and used by others (Ref 11 and 12). This nonlinear relationship and one describing linear softening are described in following sections and have been implemented in ADINA.

STRESS - STRAIN LAWS

Linear Softening

In spite of numerous tests on tensile specimens (Ref 10, 13, and 14) showing a highly nonlinear softening, linear softening is sometimes used for computational simplicity. Typically the stress declines sharply upon crack initiation, up to an opening of approximately 15×10^{-3} mm beyond which the decline is not pronounced. The importance of the type of relationship used was pointed out in Reference 1 and will also be demonstrated in the present study.

A constant negative softening modulus, E_t , can be defined for linear softening and $\epsilon > \epsilon_p$ as

$$E_t = \frac{1}{\frac{1}{E} - \frac{2G_f}{w_c f_t^2}} \quad (5)$$

E_t and the $\sigma - \epsilon$ law are shown in Figure 1a.

Nonlinear Softening

The nonlinear $\sigma - w$ relationship defined in Reference 10 is shown in a nondimensional form in Figure 1b. It is an empirical formula derived by curve fitting the results of tensile tests.

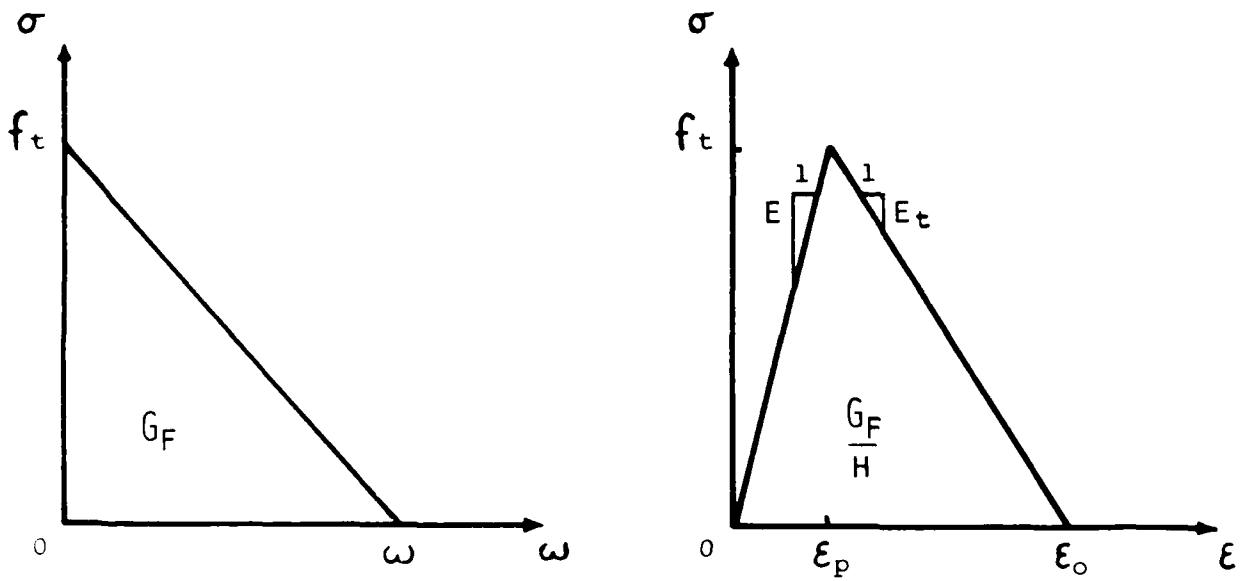
$$\sigma/f_t = \{1 + (C_1 w/w_0)^3\} e^{(-C_2 w/w_0)} - w/w_0 (1 + C_1^3) e^{(-C_2)} \quad (6)$$

where $C_1 = 3$ and $C_2 = 6.93$.

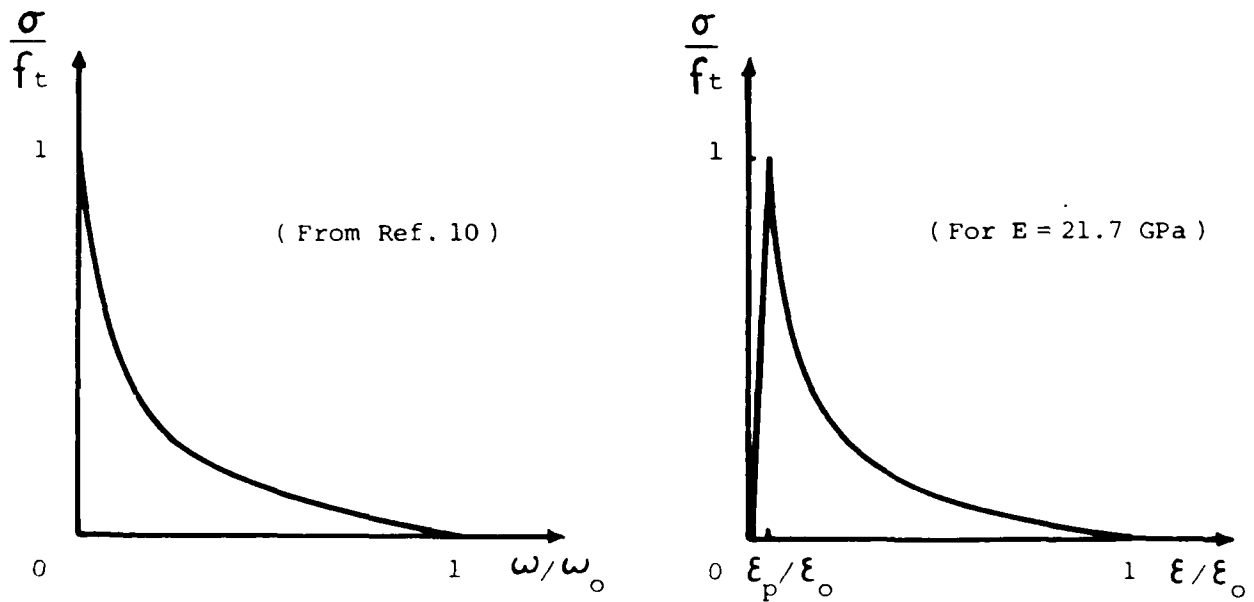
From Equation (3) w_0 can be found since G_f and f_t are known from experimental results as described in the following sections. From Equation (6):

$$\int_0^1 \frac{1}{\sigma/f_t} d(w/w_0) = 0.19470$$

To obtain a stress-versus-strain law, several points ($w/w_0, \sigma/f_t$) were chosen from Equation (6) (see Table 1) and transformed into $(\epsilon/\epsilon_0, \sigma/f_t)$. Linear interpolation was then performed between data points.



(A) LINEAR SOFTENING



(B) NONLINEAR SOFTENING

Figure 1. Stress versus crack width and stress versus strain relationships.

Table 1. Stress - Crack Width Relationship
(from Ref 10)

w/w_o	σ/f_t
0.00	1.0000
0.05	0.7082
0.10	0.5108
0.15	0.3817
0.20	0.2986
0.25	0.2446
0.30	0.2080
0.40	0.1596
0.60	0.0904
0.80	0.0361
1.00	0.0000

For the linear approximation:

$$\int_0^1 \sigma/f_t d(w/w_o) = 0.19704$$

Since $w_o = w \epsilon_o$ and $h = 2w_c$ (two elements were chosen across the crack band), ϵ_o is found from

$$G_f/2 = 0.19704 w_c \epsilon_o f_t$$

TEST SERIES

Twelve single edge notched beams with dimensions 102 mm by 102 mm (4 in. by 4 in.) cross section, 838 mm (33 in.) length and 788 mm (31 in.) span were tested in three point bending. The notch-to-depth ratio, a/W , was 0.5. The maximum aggregate size, d_a , was 9.5 mm (3/8 in.). The tests were carried out in displacement control.

Concrete properties are indicated in Table 2. The compressive strength was measured at 28 days on three 105 mm diameter by 305 mm (6 in. by 12 in.) standard cylinders. The tensile strength was obtained from splitting tensile tests conducted at 28 days on six similar cylinders. At the initiation of the compression tests strain readings at the cylinders' mid-height yielded the modulus of elasticity.

The results which have been reported in detail earlier (Ref 1) are summarized in Table 3. The fracture energy was obtained as the area under the load versus load-point deflection plot divided by the cross

Table 2. Concrete Properties

Ingredient	Amount
cement	279 kg/m ³
water	167 kg/m ³
9.5 mm gravel	1062 kg/m ³
sand	907 kg/m ³

Compressive strength at 28 days, $f'_c = 29.0$ MPa

Tensile strength at 28 days, $f_t = 3.1$ MPa

Modulus of elasticity, $E = 21.7$ GPa

sectional area at the notch. Also indicated are the mid-span displacements at peak load, d_p , and at the end of the test, d_0 (when the load carrying capacity of the beam vanishes). The set-up used is shown in Figure 2. An average of all experimental LLPD plots was used to compare with results from material modeling using the finite element method.

FINITE ELEMENT ANALYSIS

The average value of the fracture energy, G_f , was 0.0763 N/mm. Values obtained showed some variation with size and configuration.

Isoparametric elements and Gaussian integration were used. The smallest number possible of integration points was used (2 x 2 for two dimensions, 2 x 2 x 2 for three dimensions) to compensate for the excessive stiffness of these elements (Ref 15).

During crack propagation, the stiffness matrix had to be reformed periodically to reflect the changes of stiffness in the cracked elements (Ref 15 and 16). Stiffness was reformed at every equilibrium iteration for each loading step (a full Newton-Raphson procedure was employed). This approach inherently leads to a step-size dependency; that is if the loading steps are too large then too few reformations will be performed (Ref 17). Results appeared to remain practically constant for displacement steps below 0.0125 mm.

Although shear transfer across a crack can be modeled in ADINA through the use of a shear retention factor, β , no shear should be present in the center section of the symmetric specimen. To avoid energy consumption a very low value of β (0.0001) was adopted. It should be noted that recent research is drifting away from a constant shear retention factor towards a shear softening approach (Ref 12).

Table 3. Experimental Results

Specimen	G_f (N/m)	Peak load (N)	d_p (mm)	d_o (mm)
1	72.3	853	0.17	2.8
2	79.7	999	0.18	2.4
3	85.6	945	0.19	2.8
4	70.5	820	0.17	2.2
5	75.7	910	0.15	3.1
6	72.4	921	0.15	2.2
7	83.4	1011	0.16	2.5
8	75.3	950	0.17	2.9
9	68.1	883	0.13	2.4
10	68.6	950	0.16	2.6
11	84.1	950	0.16	2.7
12	79.8	997	0.15	2.0
Mean	76.3	932	0.16	2.6
Standard Deviation	6.1			

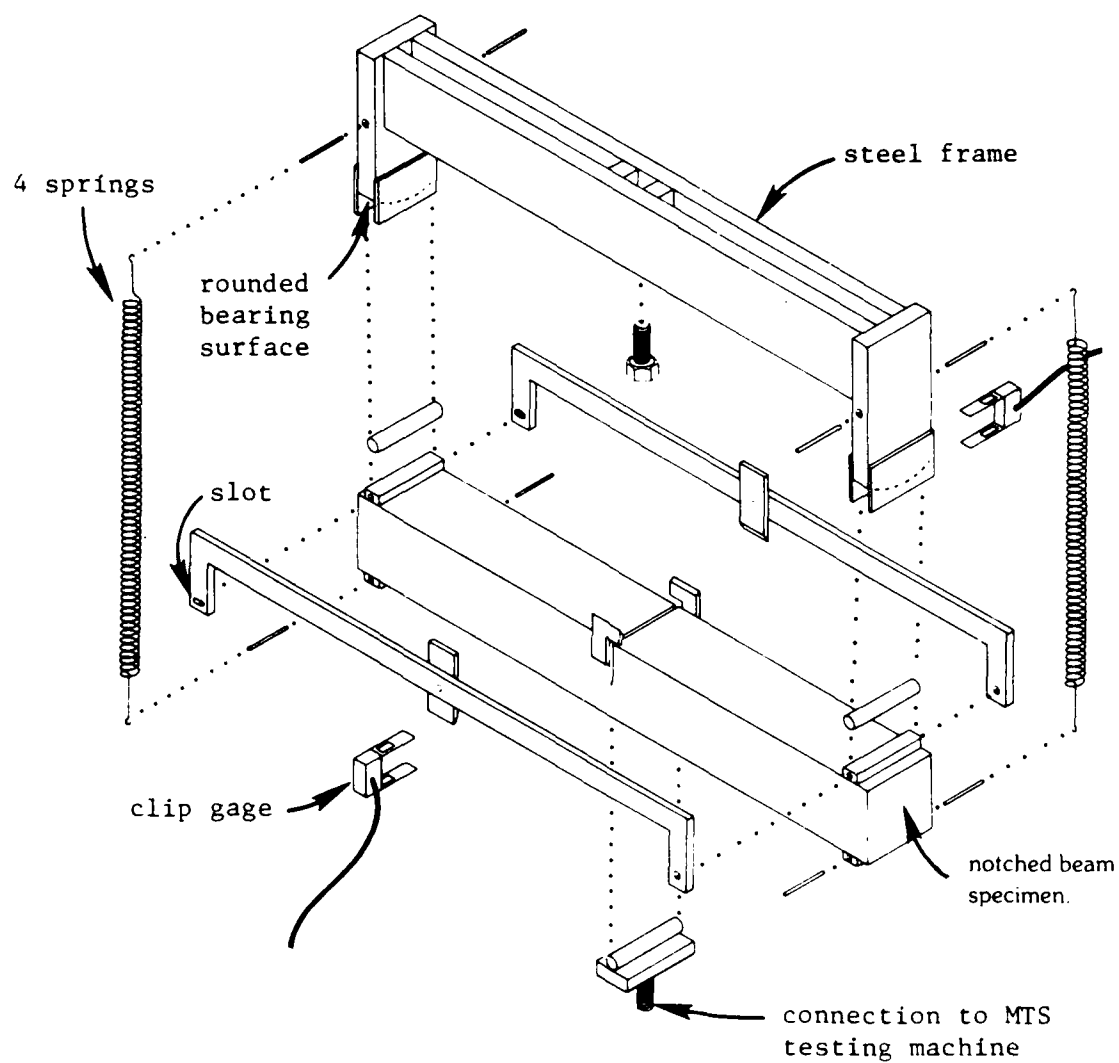


Figure 2. Test set-up.

Optimum configuration for a finite element is a square (2-D) or a cube (3-D). The element dimensions in the fracture zone were then chosen as 10 mm by 10 mm (2-D) or 10 mm by 10 mm by 10 mm (3-D). The crack band width was then 20 mm which is 2.1 times the maximum aggregate size d_a and is consistent with Reference 6, which found an optimum value of the crack band width to be around $3d_a$. Finite element meshes are shown in Figure 3.

The 2-D mesh used for the crack bond model is shown in Figure 3a. Only half of the specimen is discretized due to symmetry. In the C model, only nonlinear elements are used. In the LE model, only the five elements ahead of the notch are nonlinear concrete elements, all the others are linear elastic (LE model).

The 3-D mesh used is shown in Figure 3c. Only one quarter of the specimen is discretized due to the double symmetry. Two cases were again considered: LE, with 20 concrete and 500 elastic elements, and C, with all concrete elements.

FINITE ELEMENT RESULTS

Two-Dimensional Model

To compare with experimental observations (curve EXP of Figure 4), the LE model was first analyzed using a linear softening (LE-LS) and Cornelissen's relationship (LE-CS). Both load-load point deflation (LLPD) responses are shown on Figure 4. In addition, results using linear elastic elements, linear softening and the *Fictitious Crack Model* from Reference 1 are also shown (FCM-LE-LS). The mesh used with the FCM is shown in Figure 3b. Appendixes A and B detail the implementation of the FCM and the two-dimensional CBM.

The C model was then analyzed using Cornelissen's softening, and results are shown with the corresponding response from the others (C-CS). The magnified deformed shape is shown in Figure 5.

Three-Dimensional Model

LLPD plots for both LE and C three-dimensional models are shown in Figure 6 along with experimental response. Only nonlinear softening was used and the corresponding responses are marked LE-CS and C-CS. Numerical and graphic results shown in Figure 7 were obtained at peak load with the C-CS model. The magnified deformed shape of the cross section at the notch is shown in Figure 7a (due to symmetry only half of it is actually shown), while Figure 7b presents the stresses transferred across the cracked elements (at the integration points). Appendix C details the implementation of the three-dimensional CBM.

DISCUSSION

Two-Dimensional Model

Initial stiffness. It appears from Figure 4 that the CBM approach yields an initial stiffness which is about 10% lower than the experimental value. First cracking occurs at a load of about 600 N. Since

most of the elements are linear elastic, the initial response of the model is governed primarily by mesh geometry and element size. While the FCM analysis used a fine mesh (205 elements) with a zero notch width (Figure 3b), the CBM mesh is much coarser (90 elements) and shows a notch 20 mm wide (Figure 3a). A better match might be possible if the mesh was refined; however, the element should not be made smaller than the aggregate size. Another possible improvement would be to choose only one element across the whole crack band, cutting the notch size to 10 mm. However the latter would result in loss of model symmetry and the entire beam would have to be discretized.

Linear elastic elements with linear softening. Figure 4 indicates that the FCM and CBM yield essentially equivalent results (curves LE-LS and FCM-LE-LS). Both theories assume the total energy needed to fracture the specimen to be distributed uniformly along the fracture surface. A better match between them would be obtained if the meshes were equally refined. The simplification introduced by considering linear strain softening yields responses further from the experimental data than obtained with nonlinear softening.

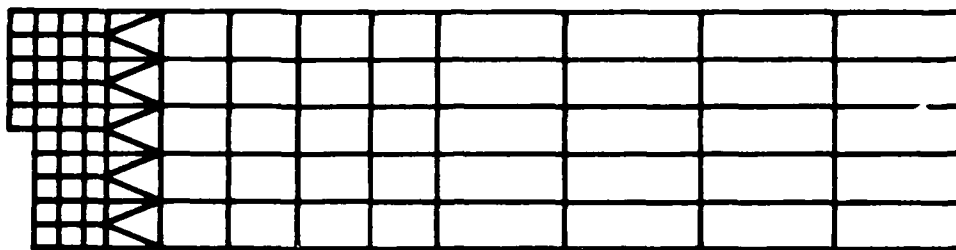
Nonlinear softening. Using linear elastic elements with Cornelissen's nonlinear stress versus displacement relationship yields a response closer to the experimental behavior (curve LE-CS). Further refinement with exclusive application of nonlinear concrete elements results in only a slight response change from the linear elastic case (curve C-CS).

Three-Dimensional Model

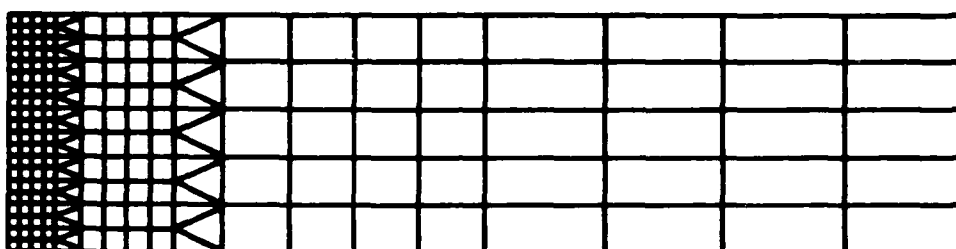
Three-dimensional isoparametric elements are stiffer than two-dimensional ones. As a consequence the initial behavior is closer to the experimental data as shown in Figure 6. After cracking, the load obtained for each displacement step is slightly lower than in the 2-D case.

The use of only nonlinear concrete elements (C-CS) increased the computing time threefold but did not affect substantially the response. The predicted peak load was in both cases lower than the experimental value (16% for C-CS versus 13% for LE-CS). It is reasonable to expect similarity since the nonlinear behavior concentrates near the fracture plane and the crack tip.

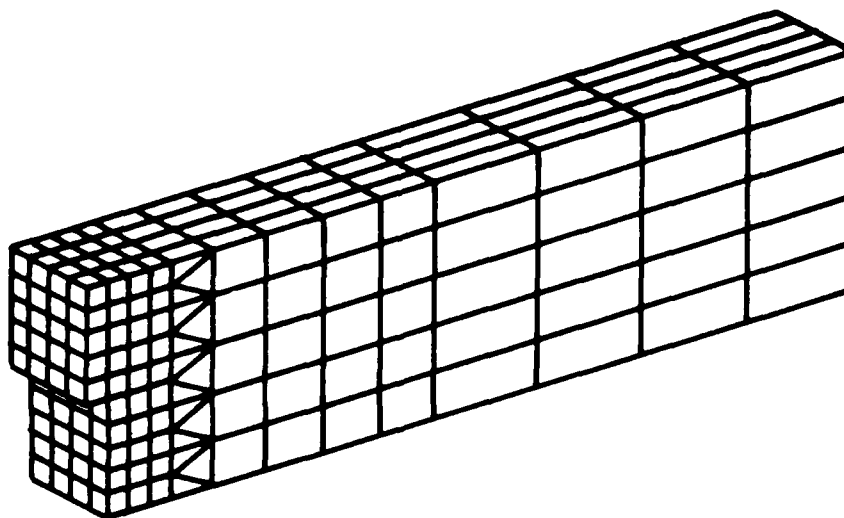
Figure 7b shows the stresses transferred across the cracked elements. It is apparent that more stress is transferred towards the beam's free edges. It is concluded that the crack at the edges does not open as wide and propagates slower than at the center (which typically occurs with metals). However, this deviation is small and the crack front can be assumed to be straight.



(A) CRACK BAND MODEL, 2-D MESH



(B) FICTITIOUS CRACK MODEL, 2-D MESH



(C) CRACK BAND MODEL, 3-D MESH

Figure 3. Two- and three-dimensional models.

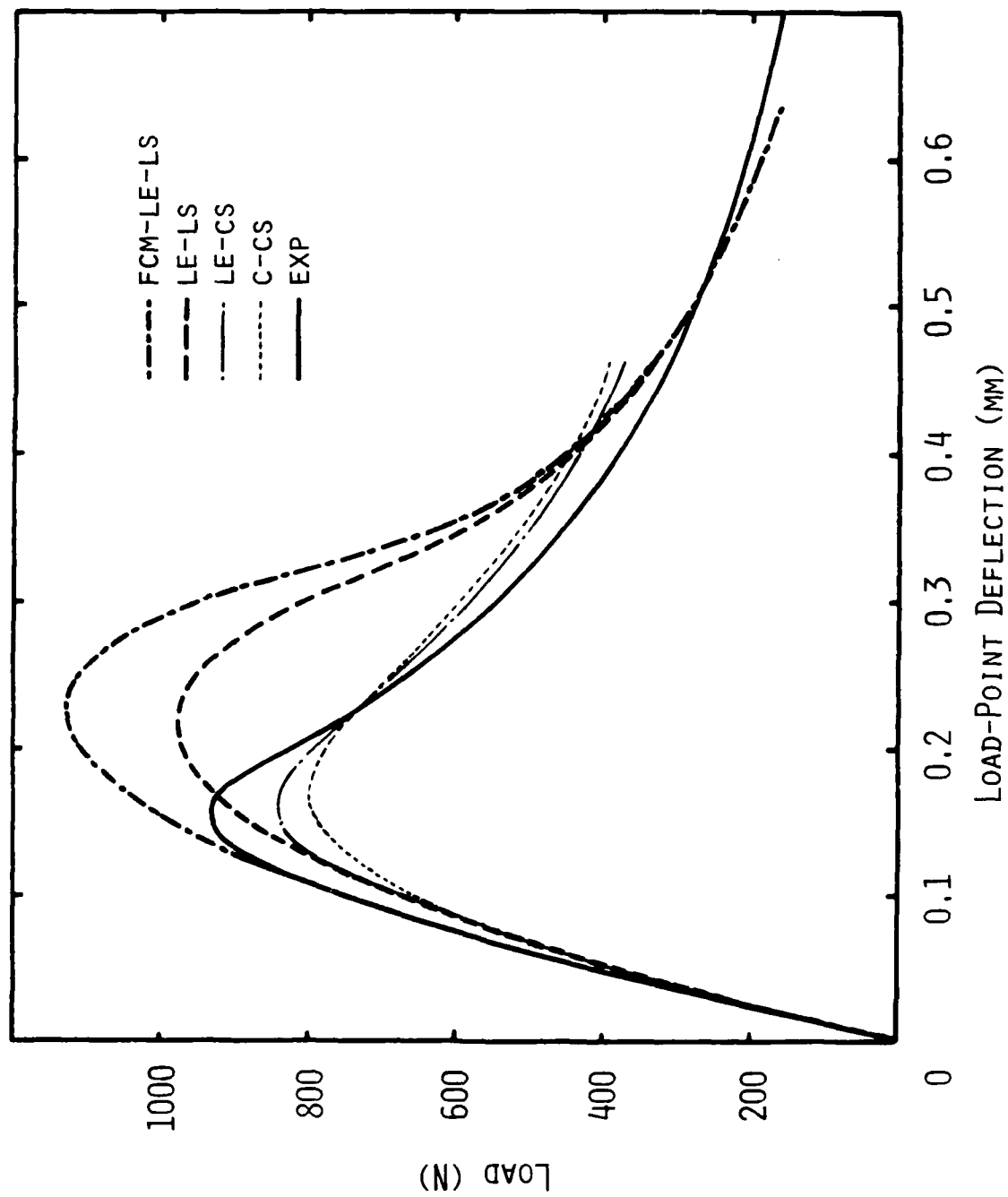


Figure 4. Load versus load-point deflection plots, 2-D model.

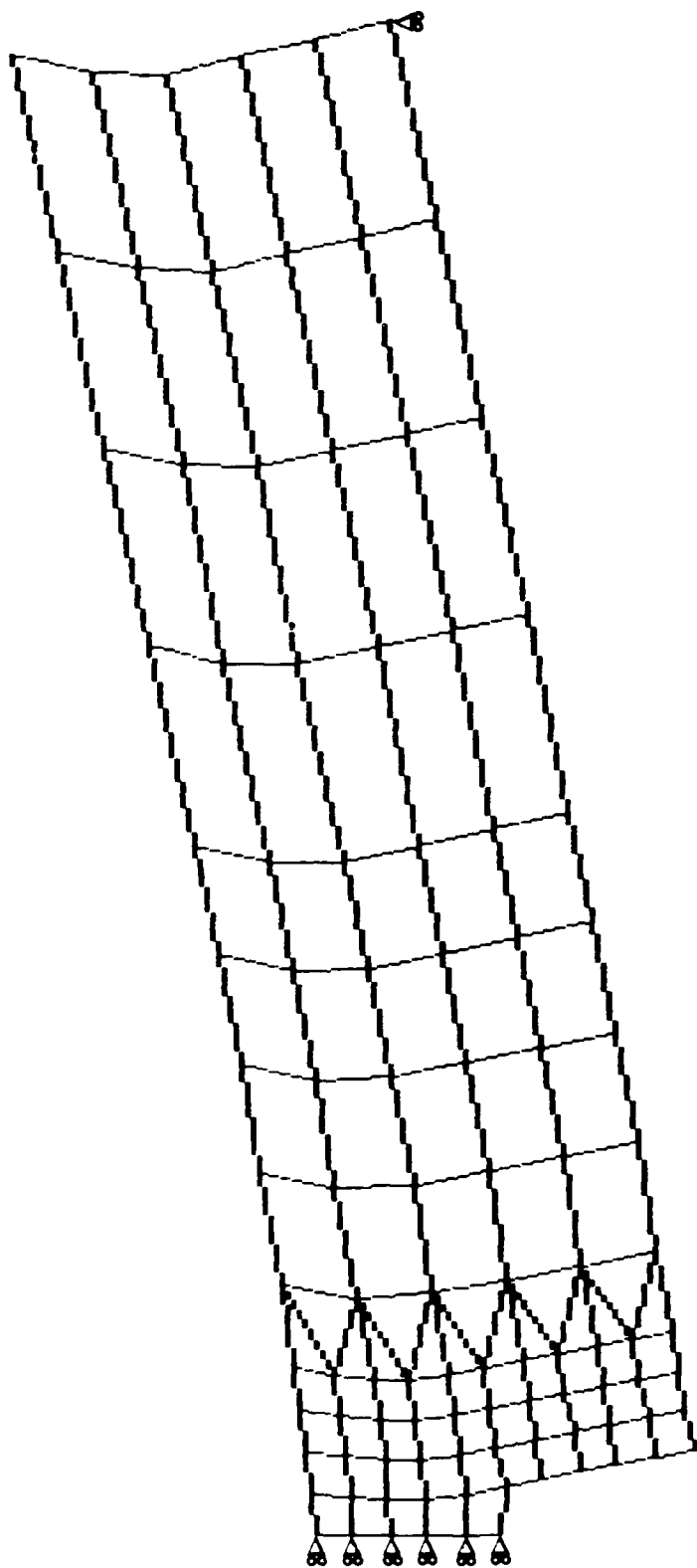


Figure 5. Deformed shape at peak load.

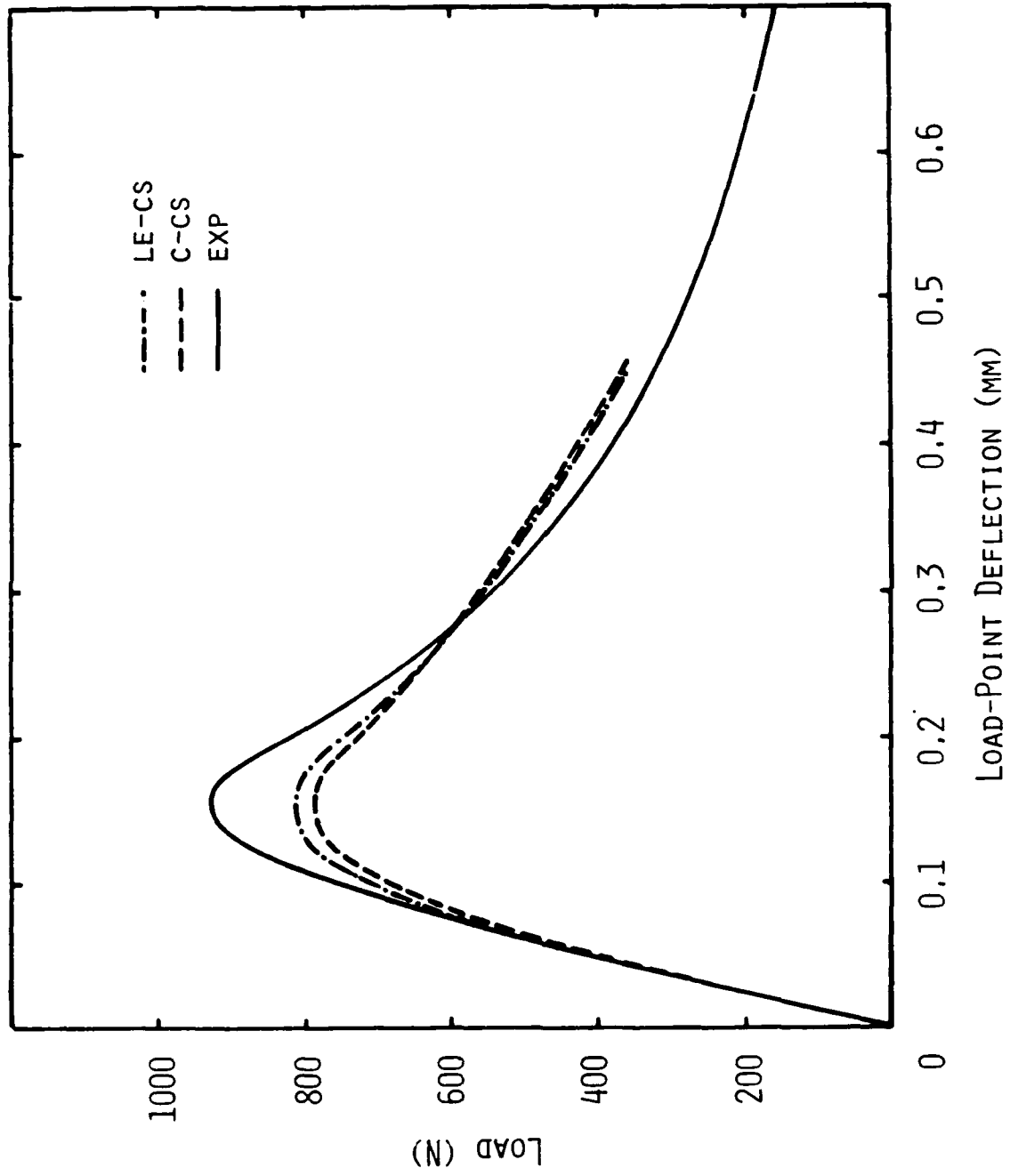
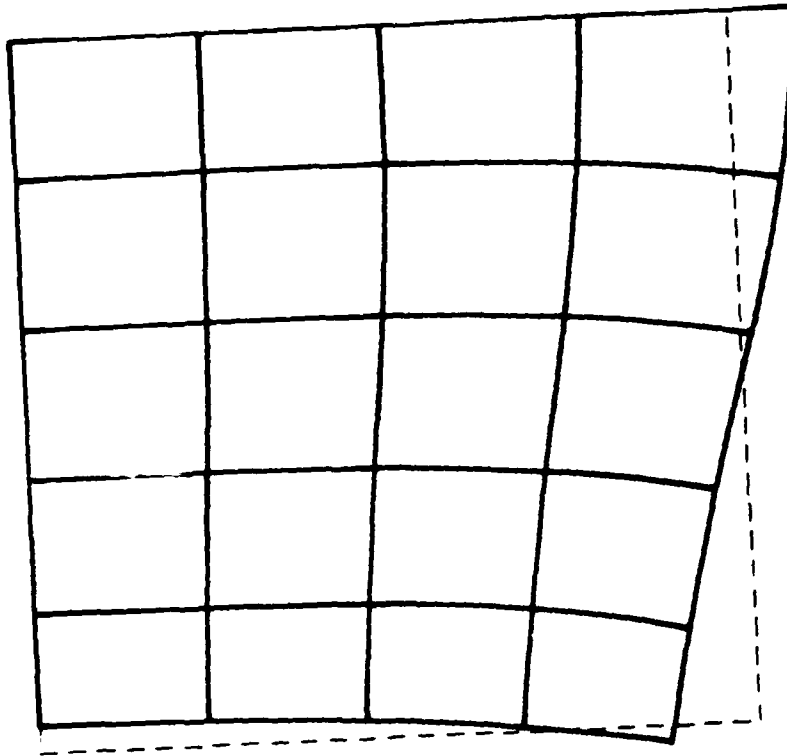


Figure 6. Load versus load-point deflection plots, 3-D model.



(A) CROSS SECTION -
DEFORMED SHAPE

238 238 243 243	239 239 243 243	240 241 244 244	244 250 247 251
201 201 210 210	201 202 210 211	202 203 211 212	205 210 213 217
158 158 166 166	158 159 166 167	159 161 167 169	163 167 170 173

GAUSS POINTS

4	8
2	6
3	7
1	5

(B) STRESSES ACROSS
CRACK ($.01 \text{ N/MM}^2$)

Figure 7. Fracture zone at peak load.

PART 2. SHEAR TRANSFER

INTRODUCTION

To model shear transfer across a crack, an adequate formulation of the constitutive relations representing the transferred stresses is needed. Shear transfer yields successive crack planes which need not be orthogonal to each other. Tensorial invariance is then addressed for the case of orthotropic models. Finally, as it happens in the case of tensile stress transfer, "snap-back" and instability may occur.

SHEAR TRANSFER

Cracks in reinforced concrete are able to transmit large shear forces. Traditionally this transfer has been neglected because of complexity and justified on the assumption that this would be a conservative simplification. In some cases this argument is erroneous (Ref 18 and 19). If a shear slip occurs along the crack, the crack will tend to dilate. If the crack dilatancy is prevented, forces normal to the crack faces will appear. These will have to be compensated by tensile forces on the reinforcement across the crack, increasing the potential for failure.

Shear stresses can be transferred across a crack in three different ways: (1) by aggregate interlock as a result of the roughness of the crack faces, (2) by dowel action or shear resistance of the reinforcement across the crack, (3) by the axial tensile force component in the reinforcement oblique to the plane of cracking.

For members with low reinforcement and for small crack widths, aggregate interlock is the main mechanism of shear transfer. Tests carried out on beams without web reinforcement showed that aggregate interlock accounted for up to 75% of the shear transfer (Ref 20). Hence most attention will be given to this first mechanism of transfer.

EXPERIMENTAL BACKGROUND

Numerous tests have been conducted to evaluate the contribution of each mechanism of shear transfer. To assess transfer by aggregate interlock, shear displacements were imposed on concrete specimens with a single crack. The crack width was maintained constant using a variable external constraint (Ref 20, 21, and 22), or unconstrained and monitored (Ref 23 through 26). In other cases the external constraining force was maintained constant (Ref 27 and 28). To eliminate the effect of dowel action, the concrete specimens were unreinforced (Ref 20) or had the reinforcement through oversized ducts next to the crack (Ref 23 through 26).

Most test results are presented as families of curves relating transferred shear stress to shear slip where each curve corresponds to a crack width (Figure 8). The shear stress is a function of shear slip and crack width (and, indirectly, of the normal stress).

ANALYTICAL BACKGROUND

In the early attempts at modeling shear transfer in finite element methods, the shear stiffness of a cracked element was taken as:

$$G_c = \beta G$$

where G is the shear stiffness of the uncracked element and β is called the shear stiffness reduction factor. This was implemented in ADINA. This model does not reflect the decrease in shear transfer capability when the crack width increases. Shear transfer eventually vanishes as the crack width approaches the aggregate size.

To overcome this difficulty, β has been linked to the crack width (Ref 29 through 32). For instance Cedolin and Dei Poli (Ref 30) used:

$$G_c = G \left(1 - \frac{\epsilon}{\epsilon_c} \right) \text{ for } 0 < \epsilon < \epsilon_c$$

$$G_c = 0 \quad \text{for } \epsilon > \epsilon_c$$

where

ϵ = strain normal to the crack

ϵ_c = value of ϵ after which there is no aggregate interlock

When the crack width is kept constant and the shear slip is increased, shear stress increases to a plateau independent of slip (Figure 8). Two analytical models which represent the nonlinear relationships between shear stress and slip are the Rough Crack Model of Bazant and Gambarova (Ref 19), and the Two-Phase Model of Walraven and Reinhardt (Ref 23 and 24). Both models will be more consistent with experimental behavior since they include general anisotropic properties.

THE ROUGH CRACK MODEL

The constitutive laws of the Rough Crack Model were simplified in Reference 33 as:

$$\sigma_{nn} = a_1 a_2 \frac{r}{(1+r^2)^{0.25}} \sqrt{\delta_n \sigma_{nt}}$$

$$\sigma_{nt} = \tau_0 \left(1 - \sqrt{\frac{2\delta_n}{d_a}} \right) r \frac{a_3 + a_4 |r|^3}{1 + a_4 r^4}$$

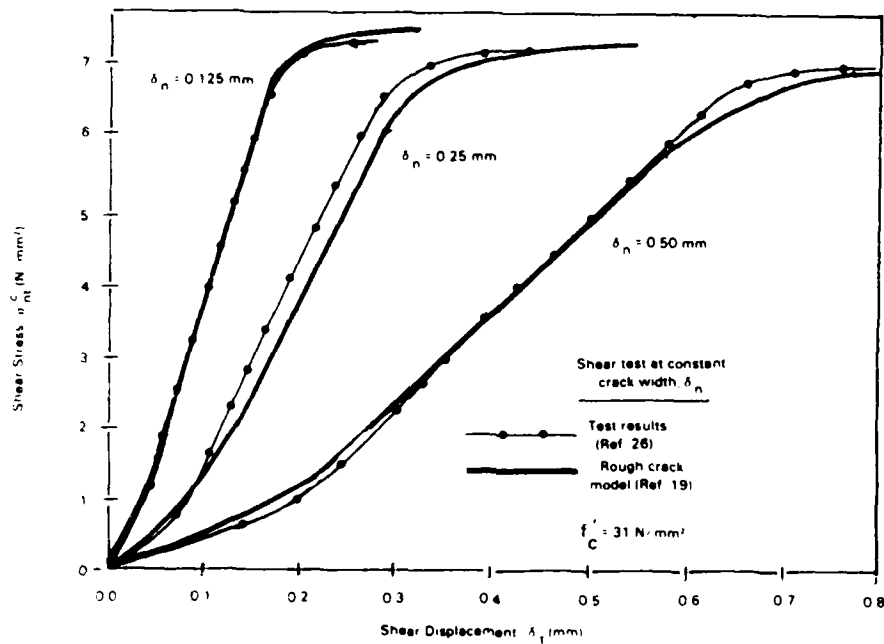


Figure 8. Shear stress versus shear slip.

in which δ_n = crack opening ($\delta_n \leq 0$)

δ_t = relative slip

σ_{nn} = interface normal stress

σ_{nt} = interface shear stress

$r = \delta_t / \delta_n$

$a_1 a_2 = 0.62$

$a_3 = 2.45 / \tau_0$

$a_4 = 2.4(1 - 4 / \tau_0)$

$\tau_0 = 0.25 f'_c$

These are empirical expressions based on Paulay and Loeber's tests results (Ref 26). The following assumptions were made:

- σ_{nn} is always compressive
- for $\delta_t = 0$ and $\delta_n > 0$ the crack faces cannot be in contact and therefore $\sigma_{nn} = 0$
- if $\delta_n = 0$ there is no crack and $\delta_t \neq 0$ cannot be obtained. Hence $\delta_t > 0$ when $\delta_n > 0$.

- for constant δ_t and increasing δ_n , both $|\sigma_{nn}|$ and $|\sigma_{nt}|$ decrease

As a consequence, if B is the crack stiffness matrix defined by

$$b_{ij} = \frac{\delta |\sigma_i|}{\delta \delta_j} \quad \text{with } \begin{matrix} i = nn, nt \\ j = n, t \end{matrix}$$

B is never positive definite which can cause numerical problems in finite element programs.

IMPLEMENTATION IN ADINA

The transfer of tensile stresses across a crack with a smeared crack approach and tension softening behavior resulted in a negative stiffness for the cracked element and was implemented using a residual load vector to redistribute the stresses during equilibrium iterations (Ref 1). This approach could also be followed to include the transfer of shear stresses by combining the Rough Crack Model and the Crack Band Model, discussed in Part 1. A similar approach for mixed-mode crack propagation appeared in Reference 34.

PRINCIPAL AXES ROTATION

In finite element implementations, cracking at a point occurs when one of the principal stresses reaches the tensile strength. A failure or cracking plane is defined upon cracking. Most computer programs, including ADINA, keep this plane constant and only allow successive planes to form perpendicular to the first one and to each other. However, when shear stress transfer across the crack is allowed, successive crack planes will generally not be perpendicular to each other (Ref 17).

In order to address this inconsistency, several recent approaches have been proposed, which are discussed below.

The Rotating Crack Model

It is assumed in the rotating crack model that the cracks are formed normal to the major principal tensile strain and rotate with it. Experiments carried out by Vecchio and Collins (Ref 35) on square, reinforced concrete panel sections support the assumption that the main crack formation is normal to the major principal tensile strain.

Cope et al. (Ref 36), first applied a rotating crack model, using a set of perpendicular axes, which followed the tensile strain rotation in a step-wise fashion. Gupta and Akbar (Ref 37) improved the model by considering a single crack which followed the tensile strain rotation in a continuous fashion. This method has been used by several researchers (Ref 38 through 41); however, the rotating crack model has been criticized (Ref 9, 42, and 43) for neglecting the previously formed cracks.

The Multiple Crack Model

An alternative approach to the rotating crack model was formulated by De Borst and Nauta (Ref 43, 44, and 45) and independently by Riggs and Powell (Ref 46), following the original development by Litton (Ref 47). They assumed that multiple, nonorthogonal cracks can form at an integration point. In this procedure the total strain increment is first decomposed into a solid concrete strain increment and a crack strain increment. Then, crack shear and normal strains are related to the corresponding stresses and an incremental crack stress-strain matrix is derived. In a similar fashion a solid concrete stress-strain matrix is formed. Finally, matrices of all cracks are assembled and an expression for the total stress-strain matrix is obtained.

The multiple crack model leads to excessive formation of new cracks, which led to the adoption of a threshold angle that allows new cracks to form only after the rotation of principal stresses reaches that angle (Ref 43). Numerical difficulties also are encountered because the crack stress-strain matrices are not positive definite.

ORTHOTROPIC VERSUS ANISOTROPIC MODELS

Numerous finite element analyses have been conducted using incrementally linear constitutive equations characterized by an orthotropic tangential stiffness. In the stress-free state isotropy is assumed and is replaced by stress-induced orthotropy when the tensile stress reaches the tensile strength. This scheme is also used in ADINA. In cases where the principal stresses rotate during the loading history, this model is not tensorially invariant; i.e., the predicted response is affected by the initial choice of axes (Ref 9). Dilatancy of the crack cannot be represented when orthotropy is assumed. Orthotropy assumes no relation between the shear strains and normal stresses. Invariance is maintained if general stress-induced anisotropy is assumed instead (Ref 9). An empirical anisotropic tangential stiffness matrix, such as the one derived from the Rough Crack Model, would be more suitable.

SNAP-BACK AND INSTABILITY

A general load-deflection response demonstrating the snap-back phenomenon is shown in Figure 9 (Ref 48). If load control were attempted to obtain this response, the path ABDEJ would be obtained since load control assumes a monotonic increment of the load. On the other hand, displacement control would yield a more complete response following the path ABCDEFHI. In either case the segment FGH representing the snap-back phenomenon could not be obtained since displacement is incremented monotonically.

To overcome the difficulty in obtaining a complete response, Riks (Ref 49) and Crisfield (Ref 41, 48, and 50) developed a procedure, known as Riks' or arc-length method, using a constraint equation fixing the step size in the load/deflection space.

Snap-back may occur in practice when strain softening is considered. Two simple examples are shown in References 41 and 51 for a bar in tension:

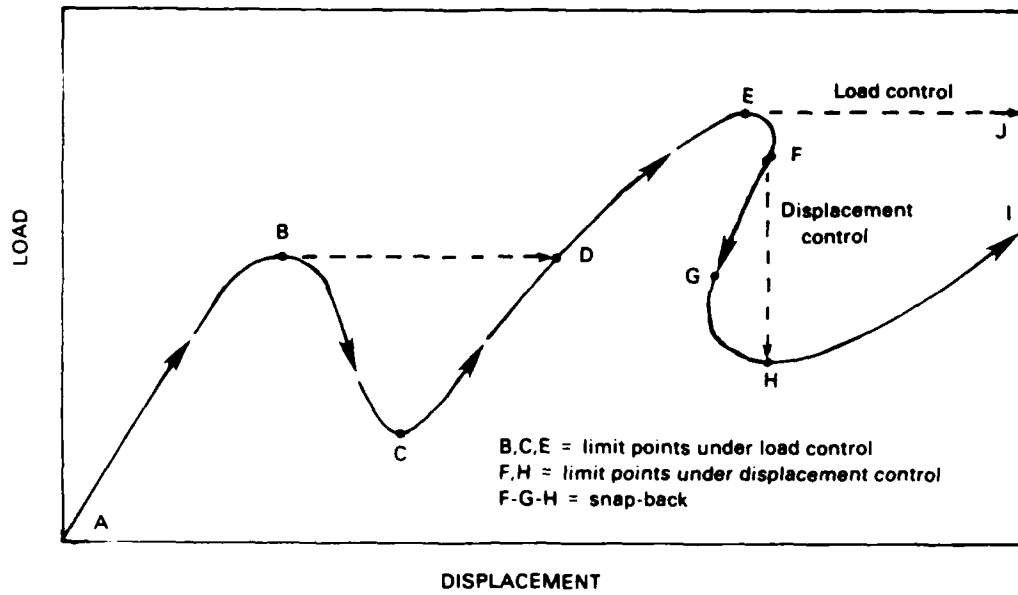


Figure 9. Snap-back phenomenon.

For a stress-strain law given by

$$\begin{aligned}
 \sigma &= E\varepsilon & \text{if } \varepsilon < \varepsilon_e & \quad \text{with } \varepsilon_e = f_t/E \\
 \sigma &= f_t [1 - (\varepsilon - \varepsilon_e)] & \text{if } \varepsilon_e < \varepsilon < \varepsilon_u & \quad \text{with } \varepsilon_u = n\varepsilon_e \\
 \sigma &= 0 & \text{if } \varepsilon > \varepsilon_u &
 \end{aligned}$$

where the bar is composed of m square elements in which one of the elements is strain softening and the other $(m-1)$ unloading, the bar will have an average strain increment of

$$\varepsilon = \frac{1}{m} \left[- (m-1) \frac{\Delta\sigma}{E} + \frac{\Delta\sigma}{E/(n-1)} \right] = \left[\frac{n}{m} - 1 \right] \frac{\Delta\sigma}{E}$$

It is observed that for $m > n$ the average strain in the post-peak regime is smaller than the peak load strain ε_e ; thus, a snap-back is originated. Riks' method has been implemented in ADINA (Ref 52) and applied to concrete cracking (Ref 41, 48, 49, and 53).

PART 3. BOND-SLIP

INTRODUCTION

In finite element analysis of reinforced concrete, bond-slip between reinforcement and concrete has been modeled using interface elements. Interface elements often use empirical, nonlinear bond stress-slip relationships.

INTERFACE ELEMENTS

The simplest interface element is the bond-link element developed by Ngo and Scordelis (Ref 54). This is a dimensionless element which connects two nodes with identical coordinates. It can be viewed as consisting of two orthogonal springs between the two nodes. De Groot et al. (Ref 55), generated a more complex element by combining the reinforcement and adjacent concrete into a finite bond-zone element. Hoshino (Ref 56) and Schafer (Ref 57) developed the dimensionless contact element, which gives a continuous connection between two elements. A comparison between these different models (Ref 58) showed that best results are obtained using contact elements with quadratic or higher order displacement functions.

An isoparametric contact element has been developed by Keuser, Mehlhorn et al. (Ref 59, 60, and 61), which is compatible with the two- and three-dimensional elements of ADINA. This contact element has been programmed in a modular structure to facilitate the input of user-supplied bond stress-slip relationship data.

BOND MECHANISMS

The mechanism of bond comprises three main components: chemical adhesion, friction, and mechanical interlock between bar ribs and concrete. Initially, for very small values of bond stress of up to 1 N/mm^2 chemical adhesion is the only resisting mechanism (Ref 62). If the bond stress is increased, chemical adhesion is destroyed and replaced by the wedging action of the ribs. This wedging action originates secondary internal radial cracks (Ref 63), longitudinal cracks, and crushing in front of the ribs. If inadequate confinement is provided, bond failure would occur as soon as the cracks spread across the concrete cover of the bar. With proper confinement, the bond stress reaches a maximum near $f'_c/3$ before decreasing as the concrete between ribs fails in shear and a frictional type of behavior ensues as shown in (Figure 10) (Ref 62).

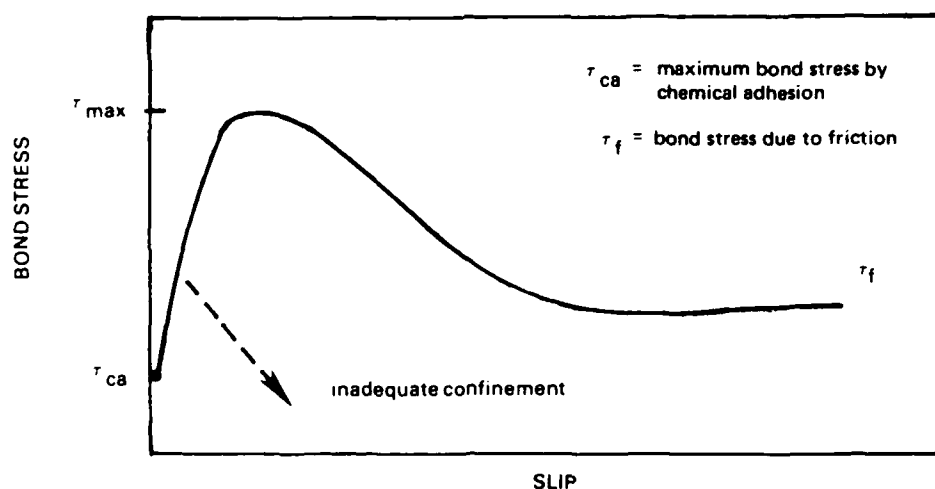


Figure 10. Typical bond-slip relationship.

EMPIRICAL BOND-SLIP RELATIONSHIPS

In order to obtain local bond stress-slip relationships for finite element modeling, the force to pull short lengths of embedded reinforcement out of concrete are measured. For embedment lengths of one to five lug spacings, consistent bond stress-slip relationships similar to the one depicted in Figure 10 have been obtained (Ref 62, 64, and 65). The use of longer embedment lengths leads to a nonuniform distribution of bond stress (Ref 66), difficulty in measuring local values without disturbing them, and different responses if the bar is pulled or pushed (Ref 67).

The parameters influencing bond-slip behavior are: load history, confinement, clear bar spacing, bar size and configuration, concrete strength, transverse pressure and loading rate. Experimental-based, local bond stress-slip relationships have been derived which are adequate for confined and unconfined bars to be used in the finite element methodology (Ref 65).

EFFECT OF BOND ON CRACK PATTERN

Bond-slip based on De Groot's model (Ref 55) has been implemented together with strain softening in the study of fracture of reinforced concrete (Ref 68). The inclusion of bond-slip produces a more realistic crack pattern, which is less diffuse and successfully represents primary and secondary cracking as observed by Goto (Ref 63).

CONCLUSIONS AND RECOMMENDATIONS

Mode I Fracture

A smeared crack approach has been implemented in ADINA for two and three dimensional nonlinear concrete elements in tension. The experimental results from tests on 12 single-edge notched beams were analyzed and good agreement was found. In particular it was shown that:

- the FCM and CBM approaches yielded similar results
- the bluntness of the crack front affected the model's behavior
- 3-D elements yielded a stiffer response than 2-D elements
- the crack front could be assumed straight.

In this application only mode I fracture occurs, and only tensile stress transfer across the crack needed to be modeled.

Mixed Mode Fracture

Mixed mode fracture including shear stress transfer is the general crack propagation mechanism. A benchmark problem in mixed mode fracture was presented by Arrea and Ingraffea (Figure 11) and studied in References 68 through 72. Initial attempts at modeling the shear transfer using a constant shear retention factor, β , and ADINA yielded results with almost no softening after peak load (Figure 12) and a crack pattern which contrasts with experimental observations (Figure 13). By considering a mode II fracture energy, Rots and De Borst successfully predicted an experimentally verified load-deflection response. However the model's crack pattern at ultimate residual load remained fixed and was inconsistent with physical observations.

It is expected that the consideration of an adequate shear transfer model, such as the Rough Crack Model that includes general anisotropy, will be more consistent with experimental observations and measurements. By considering the crack dilatancy, the initial crack next to the notch tip will tend to open further and propagate in the direction indicated by experiments.

Bond-Slip

It is proposed to update the current version of ADINA with an iso-parametric contact element for bond. The versatility of this model will allow for an easy updating of the bond stress-slip relationship. The empirical stress-strain relationship derived by Eligehausen, Popov and Bertero appears most complete and should be implemented in the contact element.

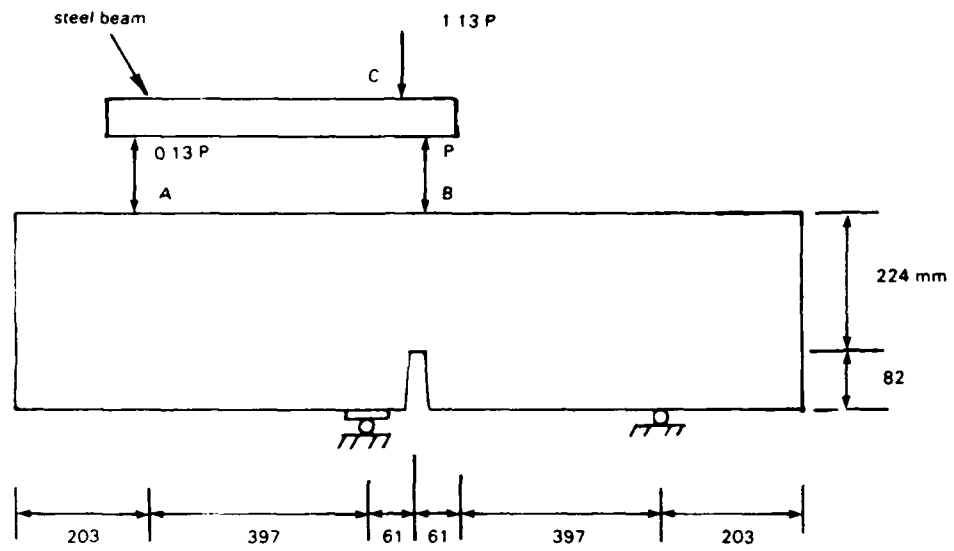


Figure 11. Single notch shear specimen.

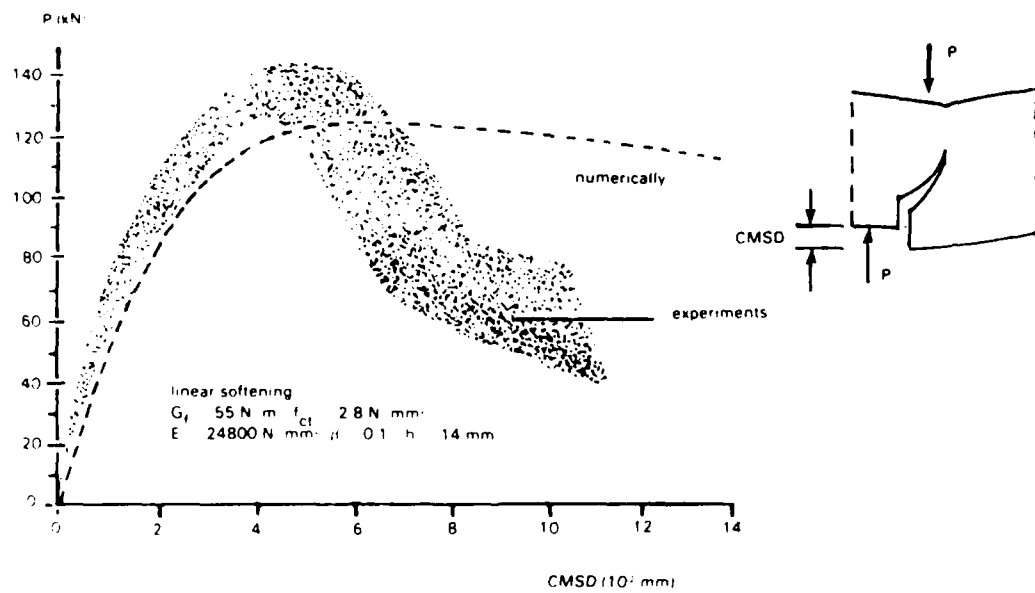


Figure 12. Load versus crack mouth sliding displacement.

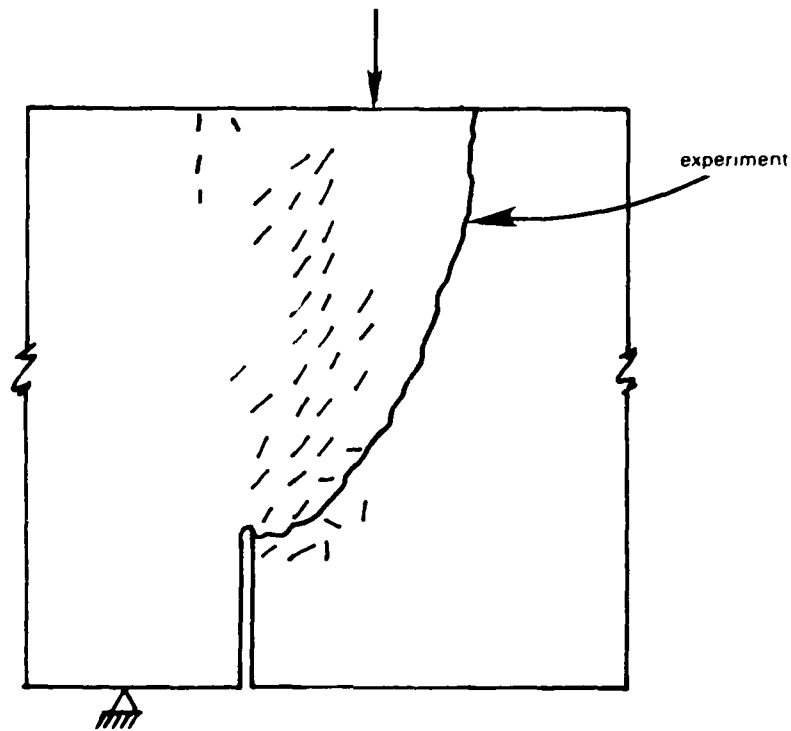


Figure 13. Crack pattern.

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Appendix A

FICTITIOUS CRACK MODEL

In the Fictitious Crack Model, crack propagation is accomplished by releasing successive nodes and inserting a residual force between them that is a function of the crack opening. In this example, nodes 7 to 21 are released. Since these nodes belong to the axis of symmetry of the specimen the coding is simplified. A bilinear strain softening is used.

CHANGES IN IUSER.F77

```

C*I   * * *   I N S E R T   U S E R - S U P P L I E D   C O D I N G   IUSER 58
C*I                                     IUSER 59
C*I   * * *   T O   S E T   M F L A G                               IUSER 60
C*I                                     IUSER 61
C*I                                     IUSER 62
      DO 100 I=7,21
      IF (M .EQ. 1) MFLAG = 1
100 CONTINUE
      RETURN                                                         IUSER 63
C*I                                     IUSER 64

```

CHANGES IN USERSL.F77

```

C*I   * * *   I N S E R T   U S E R - S U P P L I E D   C O D I N G   USERS109
C*I                                     USERS110
C*I                                     USERS111
      XWC = DD(2)*2.0
      IF (XWC .LE. 0.0) THEN
      RR(2) = 0.0
      ELSE IF (XWC .LE. 0.01840) THEN
      RR(2) = -500.0*(4.2-182.56*XWC)
      ELSE IF (XWC .LE. 0.09202) THEN
      RR(2) = -500.0*(1.05-11.41*XWC)
      ELSE
      RR(2) = 0.0
      END IF
      WRITE (6,*) 'M,DD(2),RR(2)',M,DD(2),RR(2)
      RETURN                                                         USERS112
C*I                                     USERS113
C*FILE END                                                         USERS114
      END                                                           USERS115

```


Appendix B

CRACK BAND MODEL, TWO-DIMENSIONAL

To implement a smeared crack approach, additional data has to be read by the program. The user must provide an additional card (2-D solid elements, material 5, card d) where the choice of softening is indicated, as well as band width, soft element width (usually same as band width), fracture energy and maximum aggregate size (format I5,4F10.0). The dimension of the vector CRKSTR is increased to memorize the unloading point from the virgin curve.

CHANGES IN TODMFE.F77

1 IDWAS/ 0, 0, 0,18,18, 0,10,15,15,33,33, 0, 0,26,6*0/,	TODMFE93
COMMON /SOFT/ ISCODE,WWCC,ELWW,GGFF,DDAA	TDFE 42
IF (MODEL.EQ.5) READ(IIN,1005) ISCODE,WWCC,ELWW,GGFF,DDAA	TDFE 101
1005 FORMAT (I5,4F10.0)	TDFE1219
COMMON /SOFT/ ISCODE,WWCC,ELWW,GGFF,DDAA	MATRT214
WRITE (6,2239) ISCODE,WWCC,ELWW,GGFF,DDAA	MATRT244
2239 FORMAT(/38H (BB) CODE FOR TENSILE STRESS TRANSFER,15,	MATRT726
1 /38H 1=LINEAR SOFTENING ,	
2 /38H 2=CORNELISSEN'S SOFTENING ,	
3 /38H SOFT BAND WIDTH (WWCC) ,F10.5,	
4 /38H SOFT ELEMENT WIDTH (ELWW) ,F10.5,	
5 /38H FRACTURE ENERGY (GGFF) ,F10.8,	
6 /38H MAXIMUM AGGREGATE SIZE (DDAA) ,F10.5)	

CHANGES IN ELT2D4.F77

IDW=18*ITWO	ELT2D438
DIMENSION PROP(1),WA(18,1),YZ(1),NOD5(1),NODS(1),TEMPV1(1)	ICDMOD16
DO 10 I=1,18	ICDMOD26

1	CRKSTR(6),STRESS(4),STRAIN(4),C(4,4),NODS(1),TEMPV1(1),	CDMOD 53
2	TEMPV2(1),YZ(1),NOD5(1),WA(1),DUMWA(18)	CDMOD 54
	DO 1 I=1,18	CDMOD 66
47	CALL DCRACK (C,SIG,ANGLE,MODEL,ITYP2D,NUMCRK,1,1,CRKSTR)	CDMOD270
	CALL DCRACK (C,STRESS,ANG,MODEL,ITYP2D,NUMCRK,1,2,CRKSTR)	CDMOD302
	CALL DCRACK (C,STRESS,ANGLE,MODEL,ITYP2D,NUMCRK,2,2,CRKSTR)	CDMOD350
	CALL DCRACK (C,STRESS,ANGLE,MODEL,ITYP2D,NUMCRK,1,2,CRKSTR)	CDMOD374
	CALL DCRACK (C,STRESS,ANGLE,MODEL,ITYP2D,NUMCRK,1,2,CRKSTR)	CDMOD422
	CALL DCRACK (C,STRESS,ANGPRI,MODEL,ITYP2D,NUMCRK,1,2,CRKSTR)	CDMOD427
	CALL DCRACK (C,STRESS,ANG,MODEL,ITYP2D,NUMCRK,2,1,CRKSTR)	CDMOD590
	DO 210 I=1,18	CDMOD596
	DIMENSION STR(4),EPS(4),CRKSTR(6),SP1(1),SP31(1),SP32(1),SP33(1),	CRAKID15
	DIMENSION C(4,4),SIG(4),D(4,4),T(4,4),DSIG(4),CRKSTR(6)	DCRACK 9
C	RELEASE APPROPRIATE STRESSES	DCRAC204
C		DCRAC205
98	NF=NUMCRK + 1	DCRAC206
	GO TO (140,120,110,155,100,100,100), NF	DCRAC207
100	CALL DSOF (4,SIGP,FALSTR,EP,CRKSTR,E,VNU,SIGMAT,SIGMAC)	DCRAC208
	IF (NUMCRK - 5) 140,120,110	DCRAC209
110	CALL DSOF (2,SIGP,FALSTR,EP,CRKSTR,E,VNU,SIGMAT,SIGMAC)	DCRAC210
120	SIGP(3)=SIGP(3)	DCRAC211
	CALL DSOF (1,SIGP,FALSTR,EP,CRKSTR,E,VNU,SIGMAT,SIGMAC)	DCRAC212
C		DCRAC213
C	ROTATE STRESSES TO GLOBAL AXES	DCRAC214

```

SUBROUTINE DSOF (IJ,SIGP,FALSTR,EP,CRKSTR,E,VNU,SIGMAT,SIGMAC)
IMPLICIT DOUBLE PRECISION ( A-H,O-Z )
COMMON /SOFT/ ISCODE,WWCC,GGFF,DDAA,ELWW
DIMENSION SIGP(4),EP(4),CRKSTR(6),CORN(11,3)
IF (CRKSTR(IJ).GT.0.D0) GOTO 5
SIGP(IJ)=FALSTR
RETURN
5 CONTINUE
C
DATA (CORN(1,1),I=1,11)/0.,.05,.1,.15,.2,.25,.3,.4,.6,.8,1.0/
DATA (CORN(1,2),I=1,11)/1.,.7082,.5108,.3817,.2986,.2446,
1      .2080,.1596,.0904,.0361,0.0/
JJ=IJ
IF (JJ.EQ.4) JJ=3
KK=JJ+3
EEPP=EP(IJ)
IF (EP(IJ).GT.CRKSTR(KK)) CRKSTR(KK)=EP(IJ)
IF (EP(IJ).LT.CRKSTR(KK)) EEPP=CRKSTR(KK)
ISS=ISCODE-2
IF (ISS) 10,20,30
C
10 CONTINUE
EETT=1/(1/E-(2*GGFF)/(SIGMAT**2*WWCC))
SIGP(IJ)=FALSTR+EETT*(EEPP-CRKSTR(JJ))
IF (EP(IJ).LT.CRKSTR(KK)) SIGP(IJ)=EP(IJ)/EEPP*SIGP(IJ)
IF (SIGP(IJ).GT.FALSTR) SIGP(IJ)=FALSTR
IF (SIGP(IJ).LT.0.D0) SIGP(IJ)=0.D0
SIGP(3)=0.D0
RETURN
C
20 CONTINUE
EO=GGFF/(WWCC*0.19704*SIGMAT)
DO 21 I=1,11
CORN(I,3)=CORN(I,1)+CORN(I,2)*CRKSTR(JJ)/EO
IF (EEPP/EO.LT.CORN(I,3)) GO TO 22
21 CONTINUE
22 AA=(CORN(I-1,2)-CORN(I,2))/(CORN(I-1,3)-CORN(I,3))
BB=CORN(I-1,2)-AA*CORN(I-1,3)
SIGP(IJ)=FALSTR*(AA*EEPP/EO+BB)
IF (EP(IJ).LT.CRKSTR(KK)) SIGP(IJ)=EP(IJ)/EEPP*SIGP(IJ)
IF (SIGP(IJ).GT.FALSTR) SIGP(IJ)=FALSTR
IF (SIGP(IJ).LT.0.D0) SIGP(IJ)=0.D0
SIGP(3)=0.D0
RETURN
C
30 CONTINUE
RETURN
C
END

```

Appendix C

CRACK BAND MODEL, THREE-DIMENSIONAL

An additional card is needed (3-D solid elements, material 5, card d) with the same information as for the 2-D case.

CHANGES IN THREDM.F77

	Change at or after: -----
1 IDWAS / 0, 0, 0, 25,25, 0,14,21,21,47,47,38,8*0/,	THRED100
COMMON /SOFT/ ISCODE,WWCC,ELWW,GGFF,DDAA	THDFE 46
IF (MODEL.EQ.5) READ(IIN,1009) ISCODE,WWCC,ELWW,GGFF,DDAA	THDFE102
1009 FORMAT (15,4F10.0)	THDF1190
COMMON /SOFT/ ISCODE,WWCC,ELWW,GGFF,DDAA	MATWRT14
WRITE (6,2239)	MATWR243
2239 FORMAT(/38H (BB) CODE FOR TENSILE STRESS TRANSFER,15,	MATWR596
1 /38H 1=LINEAR SOFTENING ,	
2 /38H 2=CORNELISSEN'S SOFTENING ,	
3 /38H SOFT BAND WIDTH (WWCC) ,F10.5,	
4 /38H SOFT ELEMENT WIDTH (ELWW) ,F10.5,	
5 /38H FRACTURE ENERGY (GGFF) ,F10.8,	
6 /38H MAXIMUM AGGREGATE SIZE (DDAA) ,F10.5)	

CHANGES IN ELT3D4.F77

IDW=25*ITWO	ELT3D444
DIMENSION PROP(1),WA(25,1),XYZ(1),NOD9(1),NODS(1),TEMPV1(1)	ICMOD316
DO 10 I=1,25	ICMOD326
1 CRKSTR(6),STRESS(6),STRAIN(6),C(6,6),RLMN(3,3),NODS(1),	CMOD3D54

1	TEMPV1(1),TEMPV2(1),XYZ(1),NOD9(1),WA(1),DUMWA(25)	CMOD3D55
	DO 1 I=1,25	CMOD3D67
47	CALL DCRAK3 (C,SIG,RLMN,MODEL,NUMCRK,1,1,CRKSTR)	CMOD3261
	CALL DCRAK3 (C,STRESS,RLMN,MODEL,NUMCRK,1,2,CRKSTR)	CMOD3286
	CALL DCRAK3 (C,STRESS,RLMN,MODEL,NUMCRK,2,2,CRKSTR)	CMOD3340
	CALL DCRAK3 (C,STRESS,RLMN,MODEL,NUMCRK,1,2,CRKSTR)	CMOD3363
159	CALL DCRAK3 (C,STRESS,RLMN,MODEL,NUMCRK,1,2,CRKSTR)	CMOD3414
	CALL DCRAK3 (C,STRESS,RLMN,MODEL,NUMCRK,1,2,CRKSTR)	CMOD3420
130	CALL DCRAK3 (C,SIG,RLMN,MODEL,NUMCRK,2,1,CRKSTR)	CMOD3561
	DO 210 I=1,25	CMOD3567
	DIMENSION STR(4),EPS(4),CRKSTR(6),SP1(1),SP31(1),SP32(1),SP33(1),	CRKID15
	DIMENSION C(4,4),SIG(4),D(4,4),T(4,4),DSIG(4),CRKSTR(6)	DCRACK 9
C	RELEASE APPROPRIATE STRESSES	DCRAK165
C		DCRAK166
	NF=IK + 1	DCRAK167
	GO TO (140,120,110,100,155), NF	DCRAK168
100	CALL DSOF3 (3,SIGP,FALSTR,EP,CRKSTR,E,VNU,SIGMAT,SIGMAC)	DCRAK169
110	SIGP(6)=SIGP(6)	DCRAK170
	CALL DSOF3 (2,SIGP,FALSTR,EP,CRKSTR,E,VNU,SIGMAT,SIGMAC)	DCRAK171
120	SIGP(5)=SIGP(5)	DCRAK172
	SIGP(4)=SIGP(4)	DCRAK173
	CALL DSOF3 (1,SIGP,FALSTR,EP,CRKSTR,E,VNU,SIGMAT,SIGMAC)	DCRAK174
C		DCRAK175
C	ROTATE STRESSES TO GLOBAL AXES	DCRAK176

```

SUBROUTINE DSOF3 (IJ,SIGP,FALSTR,EP,CRKSTR,E,VNU,SIGMAT,SIGMAC)  DSOF3  2
IMPLICIT DOUBLE PRECISION ( A-H,O-Z )
COMMON /SOFT/ ISCODE,WWCC,GGFF,DDAA,ELWW
DIMENSION SIGP(4),EP(4),CRKSTR(6),CORN(11,3)
IF (CRKSTR(IJ).GT.0.D0) GOTO 5
SIGP(IJ)=FALSTR
RETURN
5 CONTINUE

C
DATA (CORN(1,1),I=1,11)/0.,.05,.1,.15,.2,.25,.3,.4,.6,.8,1.0/
DATA (CORN(1,2),I=1,11)/1.,.7082,.5108,.3817,.2986,.2446,.2080,
1      .1596,.0904,.0361,0.0/
JJ=IJ
KK=JJ+3
EEPP=EP(IJ)
IF (EP(IJ).GT.CRKSTR(KK)) CRKSTR(KK)=EP(IJ)
IF (EP(IJ).LT.CRKSTR(KK)) EEPP=CRKSTR(KK)
ISS=ISCODE-2
IF (ISS) 10,20,30

C
10 CONTINUE
EETT=1/(1/E-(2*GGFF)/(SIGMAT**2*WWCC))
SIGP(IJ)=FALSTR+EETT*(EEPP-CRKSTR(JJ))
IF (EP(IJ).LT.CRKSTR(KK)) SIGP(IJ)=EP(IJ)/EEPP*SIGP(IJ)
IF (SIGP(IJ).GT.FALSTR) SIGP(IJ)=FALSTR
IF (SIGP(IJ).LT.0.D0) SIGP(IJ)=0.D0
IF (IJ-2) 12,11,11
11 SIGP(6)=0.D0
12 SIGP(5)=0.D0
SIGP(4)=0.D0
RETURN

C
20 CONTINUE
EO=GGFF/(WWCC*0.19704*SIGMAT)
DO 23 I=1,11
CORN(I,3)=CORN(I,1)+CORN(I,2)*CRKSTR(JJ)/EO
IF (EEPP/EO.LT.CORN(I,3)) GO TO 24
23 CONTINUE
24 AA=(CORN(I-1,2)-CORN(I,2))/(CORN(I-1,3)-CORN(I,3))
BB=CORN(I-1,2)-AA*CORN(I-1,3)
SIGP(IJ)=FALSTR*(AA*EEPP/EO+BB)
IF (SIGP(IJ).GT.FALSTR) SIGP(IJ)=FALSTR
IF (SIGP(IJ).LT.0.D0) SIGP(IJ)=0.D0
IF (IJ-2) 22,21,21
21 SIGP(6)=0.D0
22 SIGP(5)=0.D0
SIGP(4)=0.D0
RETURN

C
30 CONTINUE
RETURN

C
END

```

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- 19 Over-the-Beach operations (including containerization, materiel transfer, lighterage and cranes)
- 20 PCL storage, transfer and distribution

28 ENERGY/POWER GENERATION

- 29 Thermal conservation (thermal engineering of buildings, HVAC systems, energy loss measurement, power generation)
- 30 Controls and electrical conservation (electrical systems, energy monitoring and control systems)
- 31 Fuel flexibility (liquid fuels, coal utilization, energy from solid waste)
- 32 Alternate energy source (geothermal power, photovoltaic power systems, solar systems, wind systems, energy storage systems)
- 33 Site data and systems integration (energy resource data, energy consumption data, integrating energy systems)
- 34 ENVIRONMENTAL PROTECTION
- 35 Hazardous waste minimization
- 36 Restoration of installations (hazardous waste)
- 37 Waste water management and sanitary engineering
- 38 Oil pollution removal and recovery
- 39 Air pollution

44 OCEAN ENGINEERING

- 45 Seafloor soils and foundations
- 46 Seafloor construction systems and operations (including diver and manipulator tools)
- 47 Undersea structures and materials
- 48 Anchors and moorings
- 49 Undersea power systems, electromechanical cables, and connectors
- 50 Pressure vessel facilities
- 51 Physical environment (including site surveying)
- 52 Ocean-based concrete structures
- 54 Undersea cable dynamics

TYPES OF DOCUMENTS

- 85 Techdata Sheets
- 86 Technical Reports and Technical Notes
- 83 Table of Contents & Index to TDS

- 82 NCEL Guides & Abstracts
- 91 Physical Security

☐ None-
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