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EXTENSION OF AGGREGATION AND SHRINKAGE
TECHNIQUES USED IN THE ESTIMATION OF
MARINE CORPS OFFICER ATTRITION RATES

by

John M. Misiewicz

September 1989

Thesis Advisor:

Robert R. Read

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the Estimation of Marine Corps
Officer Attrition Rates

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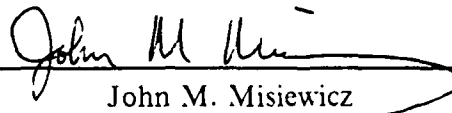
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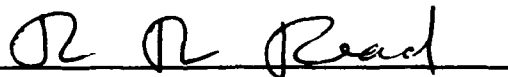
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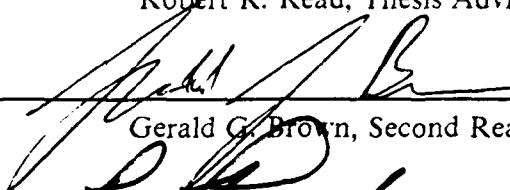
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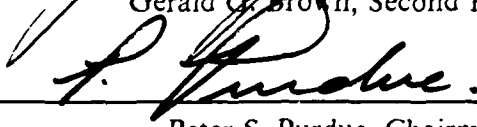
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ABSTRACT

In this thesis we treat the "small cell" problem encountered when building an attrition rate generator for large-scale manpower flow models, specifically for the USMC Officer Corps. Such models have a large number of low-inventory (i.e. small) personnel cells. This presents a dilemma: on one hand we want to preserve as much fidelity as possible in our work by preserving a great deal of detail in each cell; on the other hand our statistical estimation techniques require larger cell sample sizes than intrinsically occur cell-by-cell in actual sample data. Our approach to producing stable attrition rates for such cells involves two efforts: (i) the aggregation of cells into groups that exhibit homogeneity of attrition behavior, and (ii) the development of "shrinkage" estimation techniques for use in the individual groups. A heuristic algorithm is developed and tested to treat the aggregation problem. Empirical Bayes methods are developed to serve the multi-cell estimation requirements needed to preserve the fidelity. Cross validation techniques are used to verify these methods.

The present work builds upon the results of previous studies; we integrate what was learned into a coherent package that is ready for use.

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The reader is cautioned that computer programs developed in this research may not have been exercised for all cases of interest. While every effort has been made, within the time available, to ensure that the programs are free of computational and logic errors, they cannot be considered validated. Any application of these programs without additional verification is at the risk of the user.

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I. INTRODUCTION

A. GENERAL

The Officer Planning and Utility System (OPUS), a comprehensive and fully integrated manpower management system, is currently being implemented by the U.S. Marine Corps (Decision System Associates, 1986). This system contains a set of computer-based manpower planning models and is used by the Officer Plans Section (MPP-30), Headquarters, U.S. Marine Corps, to produce several manpower planning documents. The system must be able to accurately predict personnel attrition, i.e., officers leaving the service for purposes such as resignation, retirement, discharge, disability, or release. The forecasting of attrition is accomplished by the Marine Corps Officer Rate Projector (MCORP), developed by the Navy Personnel Research and Development Center (NPRDC), San Diego, California (NPRDC, 1985).

The attrition rate generator developed by NPRDC calculates empirical attrition rates using historical data with user-defined weights and threshold parameters (Siegel, 1983). This subjective input makes the current generator susceptible to unintentional misuse.

In support of MCORP, Professor Robert R. Read of the Naval Postgraduate School has been working on the "small cell" problem: applying multiparameter statistical estimation schemes to estimating attrition when there is low personnel inventory, or small cells, which generally exhibit unstable empirical rates.

A comment on terminology is in order. By attrition rate generator we mean methodology for estimating attrition probabilities for the various cells. The expression "empirical rates" refers to the ratio of leavers to inventory for each cell, unmodified by any information contained in "neighboring" cells. In contrast to this, the expression "empirical Bayes" refers to Bayes estimators whose prior parameters are estimated from data.

Accurate forecasting of losses is extremely important to the manpower planner. Overestimating losses causes excess accessions, promotion delays, underutilized personnel and increased costs, while underestimation causes personnel shortages and decreased readiness. The problem is compounded in that all but a few accessions must start at the bottom, i.e., Second Lieutenant, and work their way up to the higher ranks only after many years of service. For example, if a shortage of Lieutenant Colonels arises, it can

only be remedied by promoting more Majors, which has a rippling effect down the rank structure.

B. BACKGROUND

There have been seven Master's theses over the past four years which have studied various aspects of the attrition estimation problem. A concise summary of these works is given by Read (NPS Report NPS55-88-006, 1988, pp.16-23). These studies can be grouped into three general areas: shrinkage methods, cell aggregation and peripheral studies.

The application of a shrinkage method begins by identifying a number of personnel inventory cells, followed by the development of the empirical rates for individual cells and a weighted grand mean of these empirical rates. The final estimate for a cell is a convex combination of its empirical rate and the grand mean. There are numerous methods for accomplishing this, several of which have been applied in previous studies.

Tucker was the first to investigate the application of these methods to attrition estimation. He compared traditional estimators to the James-Stein estimator and the minimax estimator for a few selected grades and occupational fields. His results gave strong support to the James-Stein estimator; minimax was discarded as being too conservative for small cell use. However, there remained pockets of instability for which *goodness-of-fit tests failed*. (Tucker, 1985)

Following Tucker was Robinson, who introduced the Efron-Morris limited translation shrinkage alternative to augment the James-Stein estimator. These methods were evaluated with a broader set of test cases. Robinson was able to confirm Tucker's results, but the limited translation option failed to provide any consistent relief in the unstable areas. (Robinson, 1986)

The final application of shrinkage methods to estimating officer attrition rates was undertaken by Dickinson. He applied the previously used methods and an empirical Bayes estimator to a new and refined data base. Improved results were obtained, but the instability remained. Dickinson also performed some exploratory side studies dealing with the Freeman-Tukey transform and the use of empirical Bayes methods that allow non-uniform shrinkage, both of which provided the impetus for the present study. (Dickinson, 1988)

These three studies used ad hoc methods to deal with the second general area of study--cell aggregation. Aggregation of cells with low personnel inventory into sets of cells, often of larger inventory, is required when applying these shrinkage methods. The

desire is to use cells which exhibit similar attrition behavior. Two previous studies have investigated this area.

Amin Elseramegy used the Classification and Regression Trees (CART) program, which at the time was newly acquired by the Naval Postgraduate School, in an attempt to form aggregates of cells that exhibited homogeneous attrition behavior. Several difficulties in using this program were encountered, e.g., because of insufficient memory allocation he found it necessary to partition the data base into nine sets and apply CART to each. The resulting aggregations were generally unusable. (Amin Elseramegy, 1985)

Major breakthroughs in aggregation were made by Larsen. He applied a hierarchical clustering algorithm to the new data base. The resulting rules for building aggregates are well defined and especially viable from an intuitive point of view. Larsen's work provides the framework for the cell aggregation method developed in Chapter II of this thesis. (Larsen, 1987)

The remaining two theses of the seven were peripheral studies which applied alternate methods to attrition estimation. Hogan attempted multi-year forecasting using exponential smoothing; the smoothing constants were rather unusual and extreme and his results inconsistent (Hogan, 1986). Yacin applied logistic regression in the attempt to develop an attrition rate scheme; the only new results were the identification of some areas that exhibited similar attrition behavior (Yacin, 1987).

This thesis is the first to integrate the two main areas of study. Whereas previous studies of shrinkage methods have used ad hoc aggregation schemes, we now combine the implementation of a defensible aggregation method with empirical Bayes estimators. Moreover, these are applied to a larger and more refined data base. The results have been quite promising in that we have achieved greater stability in attrition rate estimation; we have defined guidelines for a heuristically appealing aggregation scheme; and we have acquired an increased understanding of the data base and developed more efficient ways to use it.

C. ORGANIZATION

The remainder of this introductory chapter provides a more detailed description of the small cell problem and the data base. The aggregation problem is discussed and the proposed aggregation method is presented in Chapter II.

The shrinkage estimation methods, generally classified as empirical Bayes type estimators, are described in Chapter III. Several variations are presented to allow

comparison and to gain further insight into their performance. Testing of these methods is important but for practical purposes must be carried out using sampling methods. The rationale used to select test cases, the cross validation techniques, and the measures of effectiveness used to evaluate the results are discussed in Chapter IV. A discussion of the results of the cross validation is also included in this chapter.

Finally, conclusions and recommendations based on these results are contained in Chapter V.

D. SMALL CELL PROBLEM

Marine Corps officers can be classified and thus partitioned by several attributes. The major partitioning of officers is by grade, years commissioned service (YCS), and military occupational specialty (MOS). Grade describes the position an officer holds in the service. The numbers of officers in each higher grade have a pyramid structure, i.e., there are more officers in the lower grades than in the higher grades. YCS is the total number of years served since becoming a commissioned officer. There is a strong correlation between grade and YCS since an officer generally moves up the grade structure as he gains in YCS. MOS is a four-digit code identifying the specific skill for which a Marine is trained. MOS need not remain constant over an officer's career, although most changes in MOS occur in the early years of commissioned service. An officer has a single primary MOS, however as he develops new job skills he may be assigned one or more additional MOSs.

For many purposes, partitioning by grade, YCS and MOS is sufficient. However in some applications additional refinement by service component, commissioning source, sex, race or education level may be necessary. Service component consists of three categories: regular officers, reserve officers, and reserves who have augmented to become regulars. It is strongly correlated with commissioning source, i.e., an officer receives a regular or reserve commission depending upon the commissioning source. Both affect an officer's initial service obligation, which is generally three to five years (except aviators, whose obligation is dependent upon the amount of flight training). Officers who receive a reserve commission normally serve three to four years active duty (except aviators), by the end of which they must have either augmented into the regular force or are then separated from active service.

These cross-classifications may be viewed as breaking the officer population into a multidimensional array, with each specific intersection of the classifications called a cell. The total number of possible cells is quite large, on the order of 10^6 . Many of these cells

are structurally infeasible in that no officer could possibly fit the cell characteristics, e.g., there are no Majors with two years commissioned service. The total officer inventory of approximately 20,000 officers is partitioned by the remaining feasible cells; some cells have inventory as large as 50, however most have less than five. An officer's characteristics are dynamic, i.e., as an officer moves through the grade, YCS and MOS structure he moves from one cell to another. As a result, the inventory of the feasible cells is also dynamic and fluctuates between zero and low inventory (less than five) over time.

These sparsely populated cells have very unstable empirical attrition rates. For example, a cell whose inventory is two officers of which one leaves the service during a given time period yields a 50% empirical attrition rate, whereas a cell whose inventory is one officer who remains in service during the same time period yields a 0% attrition rate. It is obvious that neither of these empirical estimations provides a usable attrition rate. Furthermore, these two rates could change dramatically during the next time period, typifying their instability.

Even when more modern estimation techniques (e.g. shrinkage) are applied, these small cells can still create statistical instability, thereby producing intolerably variable attrition rate estimates. The problem then is how to deal with these low inventory cells, or "small cells" in order to achieve stability.

E. DATA BASE

In this thesis we benefit from a refined data base compiled by NPRDC and made available to the Naval Postgraduate School in 1987. This data base, used by Larsen in his aggregation work (Larsen, 1987), was not available for the previous estimation studies at NPS.

The new data base provides more detailed information about the officer population. The grade structure now allows separation of Limited Duty Officers (LDO) as well as Warrant Officers (WO) from unrestricted officers. Officers who have failed selection to the next higher grade can also be identified. YCS is listed instead of length of service (LOS), which became ambiguous when dealing with officers who have prior enlisted service. MOS can now be broken out completely into 236 MOSs or summarized by the 39 occupational fields. Service component and commissioning source are both new categories. Other new categories that are not considered here are education level, race, additional MOSs, and military schools completed. Larsen gives a complete description of the classifications (Larsen, 1987, pp.66-82).

The data base also allows attrition to be broken out by retirement, release, discharge, resignation, etc., but for our immediate purpose we are only concerned with the total number of losses for any reason.

This refinement of the data presents a dichotomy: we can now break the data into more definitive cells to search for homogeneous attrition behavior and stability in estimation, but this leads to an even greater number of low inventory cells.

The new data base contains ten years of inventory and attrition data from the period 1977-1986, a significant improvement from the previous seven year data base covering the period 1977-1983. The inventory data is now obtained from quarterly vice yearly snap-shots of the officer population. The attrition data is annualized, i.e., the attrition count for a cell reflects the number of personnel who leave the service at any time during the year. Attritions are credited to the cell which the officer occupies at the time he leaves.

Two problems arise from this quarterly versus annualized data. First, it is possible for a cell to record zero inventory via the snap-shots, yet be credited with one or more attritions. To avoid this situation, the cell inventory used in all calculations is defined to be the larger of the inventory and the attrition count. This ensures that the inventory for a cell is at least as large as its recorded number of leavers. (This override occurs infrequently; a more sophisticated treatment would require significant model enhancement.) Second, to use the inventory and attrition data together we must divide the inventory data by four. This poses a philosophical problem when invoking a binomial model: the sample size may not be integral. However, for our application the usual mean and variance formulas are usable and can still serve in the interpolative sense.

II. CELL AGGREGATION

A. GENERAL

The aggregation problem takes on new meaning with the use of shrinkage estimators. Originally, aggregation had only one concern: how to pool cells together into a single cell in order to meet a user-defined minimum inventory threshold. This single aggregated cell was then used to determine the attrition rate estimate for the original, unaggregated cell. In this way an estimated value for a cell is obtained by using the grand mean for many cells.

The empirical Bayes multiparameter estimation techniques provide a way to compromise, using both the stability of a grand mean and the specific information of an individual cell. Now we pool cells together and obtain a **number** of cells that meet the user-defined minimum inventory threshold. It is important to note that we should be able to use a lower inventory threshold with empirical Bayes, thus retaining individual cell behavior to a greater extent. It is also important to use cells with homogeneous attrition behavior in the aggregation process.

B. BACKGROUND

The aggregation method currently used by MCORP is called the Small Cell Override Methodology (NPRDC, 1985, Appendix H). It is used to solve the original aggregation problem, i.e., if a cell is below the user-defined threshold, then cells are adjoined to the original cell until the threshold is met. The process for selecting cells for adjunction is rather crude, and large-scale with only a few levels (prior to using the entire officer corps). The attrition rate estimate for the original cell is the empirical rate from this aggregated cell.

To begin the process, the user defines a cell for which an attrition rate estimate is required by grade, YCS and MOS. The user also defines the minimum cell inventory threshold (and other parameters which are not relevant here). If the cell he identifies meets the threshold, no aggregation is required and the empirical attrition rate is determined. If the cell is below the threshold, additional cells must be added until the threshold is met.

This search for additional cells occurs by expanding by YCS and MOS, with grade remaining fixed throughout. Expanding in this sense means changing the YCS or MOS parameter to identify the additional cells to be added to the original cell. Initially, the

single cell is expanded by YCS. For example, if the original cell's grade/YCS/MOS was Capt/7/0802, the cells identified by Capt/6/0802, Capt/8/0802, etc., are added sequentially until the threshold is met. This YCS expansion has an upper bound at the 20 YCS point; an obvious boundary for attrition behavior due to retirement eligibility. If the original cell's YCS is above 20, then 20 would serve as the lower YCS bound.

If the threshold is not met after the YCS expansion, the override method starts over with the original cell and expands by MOS. Each MOS belongs to one of nine MOS groups which are defined along traditional Marine Corps functional areas, e.g., all helicopter pilot MOSs are grouped together as are all combat support MOSs. MOS expansion adds those cells identified by the MOSs in the same MOS group as the MOS of the original cell for the original YCS and grade. If the threshold is not met, all the MOSs in the MOS group are expanded by YCS in the same manner as the YCS expansion discussed previously.

If this MOS group and YCS expansion is unsuccessful, the override method starts over with the original cell and expands by all MOSs for the original grade and YCS. If necessary, all the MOSs are expanded by YCS as before.

Cell aggregation using this expansion method can potentially include all MOSs and YCS bounded only at the 20 year point. The desire to aggregate using cells with homogeneous attrition behavior is obviously compromised. Larsen provides a more comprehensive description of the current method (Larsen, 1987, pp.16-22).

Larsen examined attrition behavior in the MOS and YCS structure. He applied a hierarchical clustering algorithm in an attempt to find MOSs and YCSs that displayed homogeneous attrition behavior. He confirmed the belief that YCS is an important factor. The YCS expansion bounds he proposed reflect points at which officers reach the end of their initial service obligation as well as when they are eligible for retirement, which makes them especially viable from an intuitive point of view. Larsen also found that some MOSs did not cluster strictly by functional areas. This was especially significant in the aviation community. Whereas the previous data base allowed aviators to be considered only as one occupational field, the refined MOS information was able to identify six distinct homogeneous groups of aviators.

Larsen uses these results to define more refined MOS groups and YCS boundaries. To avoid the giant expansion leap from MOS group to all MOSs, he proposed a hierarchy of small MOS groups, large MOS groups and major MOS groups developed by observing which MOSs tend to exhibit similar attrition behavior. Homogeneity is greatest within the MOS group, and becomes successively worse as we move to the large

MOS group and then the major MOS group. Each MOS is assigned to a small MOS group. Small MOS groups combine to make a large MOS group, and large MOS groups combine to make a major MOS group.

Each small MOS group is assigned a set of YCS expansion bounds. Due to the different attrition behavior of the small MOS groups with respect to YCS, three different sets of YCS expansion bounds are proposed.

Initial expansion is by YCS within the specified boundaries, with grade and MOS held constant. If more expansion is required, we retain this aggregated cell and expand by small MOS group for the original grade and YCS. If the aggregated cell is still below the threshold, the MOSs in the small MOS group are expanded by YCS. Subsequent expansion to large MOS group and YCS, and major MOS group and YCS is accomplished until the threshold cell inventory is met.

Unlike the current expansion method, expansion using Larsen's proposed method will not cross defined MOS groups or YCS bounds to ever include all MOSs and YCSs bounded only at the 20 year point. Larsen provides a more detailed description of his recommended expansion rules (Larsen, 1987, pp.45-61).

C. EXPANSION METHOD

We now address the methods used to obtain the cells required for use with empirical Bayes estimation techniques. Expansion continues to mean finding more cells to be used, however we no longer simply add these cells to the original cell to form a single aggregated cell. The cells identified by the expansion process are now aggregated together to produce a number of cells. After the discussion of the expansion process in this section, an actual aggregation scheme is introduced in the next section.

To begin the estimation process, the manpower planner defines a specific cell by grade, YCS and MOS. The attributes service component and commissioning source are also included as possible cell descriptors for the purposes of this study. All other descriptors listed in the data base--sex, education level, additional MOSs, race and military schools--are ignored. Loss types are considered as a combined total, i.e., in this study we do not discriminate among the various types of losses. The first three user-defined descriptors--grade, YCS and MOS--are single-value inputs. The last two descriptors, service component and commissioning source, can be single values, or either one of them can be treated as a vector of values for each single cell. This vector is collapsed (total the components) during the aggregation process, i.e., all records which meet any of the vector's values are included in the same cell. As in the previously described expansion

methods, only YCS and MOS change during expansion, the remaining cell descriptors remain constant.

To use shrinkage techniques, the amount of expansion required not only depends upon the minimum cell inventory threshold but also upon a new input parameter: the threshold number of cells. These two parameters are denoted:

1. T_0 - cell inventory threshold. The minimum average inventory for a cell obtained by averaging the cell inventory over the ten years of data.
2. K_0 - threshold number of cells. The minimum number of aggregated cells whose inventory exceeds T_0 . These aggregated cells are the input cells for the empirical Bayes techniques.

For example, if $T_0 = 5.0$ and $K_0 = 10$, the expansion algorithm continues until at least ten aggregated cells, each with average inventory 5.0 or larger are obtained. Since we are concerned primarily with the small cell problem the values of T_0 and K_0 used are selected to range from five to 30. It is also presumed that T_0 is less than or equal to K_0 . These threshold values can certainly exceed 30 for other applications, however the resulting cells are not considered small and their attrition behavior most likely would not be as unstable, therefore not requiring special attention.

Prior to explaining the expansion process, we first define the MOS groups and YCS bounds. We have adopted much of Larsen's work in this area; many of the changes are minor but are necessary for implementation purposes.

The general idea of a hierarchy of MOS groups is repeated, as shown in Table 1. Each MOS belongs to a small MOS group, a large MOS group and a major MOS group. Listed are 14 small MOS groups, which combine to make six large MOS groups, which combine to make four major MOS groups. For example, small MOS groups one and two form large MOS group one, and small MOS groups three through six form large MOS group two. Large MOS groups one and two, which collectively contain small MOS groups one through six, make up major MOS group one. Major MOS group one contains only ground MOSs, and major MOS group two contains only aviation MOSs. Major MOS groups three and four are special cases as discussed below.

A subjective decision was made to keep the ground MOSs in groups defined along the more traditional functional areas. This is reflected in small MOS groups one through six. For estimation purposes it is advantageous if the cell inventories are not too variable in size (Carter and Rolph, 1974, p.882). It is also desirable to avoid having too many MOSs in each small MOS group. This allows the expansion to occur more gradually, and is especially important for small values of T_0 and K_0 . As a result, MOS 0302

Table 1. MOS GROUPS

Group Name	MOSs	Small MOS Group	Large MOS Group	Major MOS Group
Combat	0302	1	1	1
Combat Support	0802 1302 1802 1803	2		
Combat Service 1	0180 0202 2502 2602	3	2	
Combat Service 2	3415 4002 4302 5803	4		
Combat Logistics	0402 3002 3060 3502 6002	5		
Air Control	7204 7208 7210 7320	6		
Fixed Wing Pilots	7501 7511 7522 7542 7543 7545 7576	7	3	2
F-18 Pilots	7521 7523	8		
Rotary Wing Pilots +	7556 7557 7562 7564 7565 7566 7587	9	4	
Naval Flight Officers +	7508 7509 7563 7581 7583 7584 7585 7586 7588	10		
Basic Ground	0101 0201 0301 0401 0801 1301 1801 2501 2601 3001 3401 3501 4001 4301 4401 5801 6001 7201 7301 9901	11	5	3
Student Aviators	7580 7597 7598 7599	12		
Basic Pilots	7500 7510 7520 7540 7550 7560 7575	13		
Lawyers	4402	14	6	4

(infantry) is placed alone in a small MOS group. This MOS contains approximately 15% of the total officer population, and therefore its respective cells normally contain large inventory. The MOSs in small MOS group two also contain fairly large inventory, therefore are grouped together and their first expansion is with MOS 0302. The remaining ground MOSs in small MOS groups three through six have similarly small inventory.

The aviation small MOS groups (seven through ten) remain relatively unchanged from Larsen's recommendations. MOS 7564 (CH-53 pilot), was removed from a ground MOS group and added to small MOS group nine, which reflects its functional area. MOSs 7551 (C-9 pilot), 7552 (TC-4C pilot), 7555 (UC-12B pilot) and 7559 (CT-39 pilot)

were deleted since they are not primary MOSs. MOS 7530 (basic pilot VMFA (F-4)) was deleted since it is not a current MOS. (MCO P1200.7G, 1988)

Officers who have not acquired sufficient schooling or field experience to qualify for a primary MOS listed in small MOS groups one through ten are gathered together as basic officers or students in small MOS groups 11-13. These officers are generally second lieutenants or junior first lieutenants with three or fewer YCS. They are disregarded for the remainder of the study because their attrition rates are extremely low; probably because none of the officers in these groups have reached the end of their initial obligations.

MOS 4402 (lawyers) is considered a special case and is not addressed in this study.

All MOSs listed in Table 1 are primary MOSs for unrestricted officers as listed in the current Military Occupational Specialties Manual (MCO P1200.7G, 1988). It would be a logical and relatively simple extension of this table to create additional groups containing LDO and WO MOSs. These grades are not considered in this study and therefore their respective MOSs are excluded from the table.

Several of these seemingly ad hoc decisions to alter Larsen's recommended MOS groups are due to the YCS expansion bounds shown in Table 2. Every effort was made to group MOSs with similar YCS expansion bounds to allow for feasible implementation of the expansion algorithm. This is especially applicable when expanding to large and major MOS groups.

Table 2. YCS EXPANSION BOUNDS

MOS Group	Small MOS Groups	Bounded YCS Groups
Fixed Wing Pilots, F-18 Pilots, Lawyers	7, 8, 14	(1-6, 8-19) (7) (20-25) (26)
Rotary Wing Pilots, Naval Flight Officers	9, 10	(1-5, 8-19) (6,7) (20-25) (26)
All Others	1-6, 11-13	(1-3, 6-19) (4,5) (20-25) (26)

The YCS expansion bounds reflect the maximum expansion allowed from the initial YCS defined by the user. For example, if the original cell's grade/YCS/MOS is Capt/9/7501, we see from Table 1 that this MOS belongs to small MOS group seven. Thus its YCS expansion bounds are listed on the first line of Table 2. The value of nine

for YCS falls in the first YCS range, thus we could expand using all YCSs from one through 19, excluding seven. If the YCS for this original cell had been seven, no YCS expansion would be allowed.

These YCS expansion bounds are used with the MOS groups to define the additional cells which can be used with the original cell to obtain the required number of cells, K_0 , each with minimum average inventory, T_0 . The expansion stages are:

1. Stage 1 - Locate the small MOS group which contains the user-defined MOS. The initial cells are those specified by the MOSs in this group for the user-defined YCS, grade, service component and commissioning source (grade, service component and commissioning source remain fixed throughout the expansion process and thus are not repeated). These cells are aggregated to obtain cells with average inventory greater than or equal to T_0 . After aggregation, if the number of cells is greater than K_0 , stop, otherwise go to Stage 2.
2. Stage 2 - Expand by incrementing YCS (YCS-1, YCS+1, YCS-2, YCS+2, etc.) within the YCS bounds listed in Table 2 for all MOSs in the small MOS group. After each YCS increment, aggregate the cells to obtain cells with average inventory greater than or equal to T_0 . After aggregation, if the number of cells is greater than K_0 , stop, otherwise continue to increment by YCS. If the YCS bounds are reached before obtaining enough aggregated cells, retain the cells identified in Stages 1 and 2 and go to Stage 3.
3. Stage 3 - Expand to the large MOS group for the single user-defined YCS. Aggregate the cells to obtain cells with average inventory greater than or equal to T_0 . After aggregation, if the number of cells is greater than K_0 , stop, otherwise go to Stage 4.
4. Stage 4 - Expand by incrementing YCS for the large MOS group. After each YCS increment, aggregate the cells to obtain cells with average inventory greater than or equal to T_0 . After aggregation, if the number of cells is greater than K_0 , stop, otherwise continue to increment by YCS. If the YCS bounds are reached before obtaining enough aggregated cells, retain the cells identified in Stages 1 through 4 and go to Stage 5.
5. Stage 5 - Expand to the major MOS group for the single user-defined YCS. Aggregate the cells to obtain cells with average inventory greater than or equal to T_0 . After aggregation, if the number of cells is greater than K_0 , stop, otherwise go to Stage 6.
6. Stage 6 - Expand by incrementing YCS for the major MOS group. After each YCS increment, aggregate the cells to obtain cells with average inventory greater than or equal to T_0 . After aggregation, if the number of cells is greater than K_0 , stop, otherwise continue to increment by YCS. If the YCS bounds are reached before obtaining enough aggregated cells, stop. No more expansion is allowed. Inform the user that the thresholds are unattainable. Do not cross any major MOS group or YCS bounds.

Two points about the expansion process are emphasized. First, we retain the cells identified by all previous stages as we progress to the next stage. As stated before, the degree of homogeneity decreases as we move from small to large to major MOS groups.

Thus we want to locate as many cells from the small MOS group as possible before we expand to the large MOS group, and then locate as many cells from the large MOS group as possible before expanding to the major MOS group. The YCS expansion for each group may be different, e.g., the small MOS group may be expanded by all YCSs within the given YCS range, but the large MOS group may only be expanded by a few YCSs before the thresholds are attained.

The second point is that, when aggregating cells, any aggregation that was performed previously is discarded and all cells currently identified are pooled and made available for aggregation. This affords the aggregation algorithm greater flexibility and could create more aggregated cells than if the aggregated cells from previous stages were left intact, thereby keeping the amount of expansion to a minimum.

The aviation small MOS groups (seven through ten) make up the only major MOS group (two) that contains different YCS bounds, i.e., small MOS groups seven and eight have different YCS expansion with regard to year six than do small MOS groups nine and ten. To implement the expansion algorithm in a computer program, this difference is overcome by using the YCS bounds for the original user-defined MOS. For example, suppose MOS 7501 from small MOS group seven is the original MOS. If MOS expansion continues into the major MOS group, the MOSs in small MOS groups nine and ten would follow small MOS group seven's YCS expansion bounds.

In summary, this method of grouping MOSs should provide greater homogeneity among cells which are used in estimating attrition rates. Unlike the current method, ground and aviation MOSs are never used together. The YCS bounds provide a logical and effective way to treat periods of different attrition behavior. However, the greater the expansion the less homogeneous the cells become, which should be kept foremost in mind when setting the threshold parameters.

D. AGGREGATION METHOD

While the expansion steps are being undertaken in order to achieve the threshold levels specified by the user, those cells with inventory less than T_0 must be gathered up into larger, aggregated cells whose combined inventory exceeds T_0 . In order to limit the expansion to as few additional MOSs and YCSs as possible, we desire to maximize the number of aggregated cells obtained at any stage of the expansion.

The term maximization suggests the possible use of linear programming (LP). While an LP would ensure maximization, this would not be a trivial problem to solve, i.e., the LP relaxation would almost certainly fractionate cells, using their inventory in more than

one aggregated cell. This is not allowed since a cell may be assigned intact to only one aggregated cell. Thus an integer LP would be required which would typically contain 500 or more integer variables. This method would not be expedient in terms of computer usage, especially considering the potential number of integer LPs that may have to be solved for a single estimation cycle.

While we are trying to maximize the number of aggregated cells, it would be satisfactory to obtain close to the maximum if we could preclude the expense in computer time required by an integer LP. For this reason, a heuristic "greedy" algorithm was developed. Complete descriptions of the heuristic algorithm and the LP formulation are contained in Appendix A. The performance of this heuristic is discussed along with the results of the empirical Bayes methods in Chapter IV.

III. ESTIMATION METHODS

A. GENERAL

Once the cell aggregation phase is completed, we begin the attrition rate estimation process. The following notation is used to define the cell data

$$\begin{aligned} K &= \text{number of cells} \\ T &= \text{number of years of data.} \end{aligned} \tag{1}$$

Then for $i = 1, \dots, K$ and $t = 1, \dots, T$

$$\begin{aligned} N_i(t) &= \text{inventory of cell } i \text{ in year } t \\ Y_i(t) &= \text{number of attritions in cell } i \text{ in year } t. \end{aligned} \tag{2}$$

The cell data is assumed to be independent binomial, i.e., $Y_i(t) \sim \text{Bin}(N_i(t), p_i)$. A success is defined to be an attrition, i.e., an officer from that cell leaves the service during the year. The empirical attrition rate for cell i is given by the Maximum Likelihood Estimator (MLE)

$$\hat{p}_i = \frac{\sum_t Y_i(t)}{\sum_t N_i(t)}. \tag{3}$$

This estimate of p works well for cells with large inventory, but not those with small inventory, which is most often the case in our application.

The MLE has been shown to be dominated by shrinkage methods for $K \geq 3$ (Carter and Rolph, 1974; Efron and Morris, 1975; Casella, 1985). These methods find a grand mean or central attrition rate for the group of cells and a shrinkage factor for each cell. Previous theses have primarily used a common shrinkage factor for all cells; we now allow this shrinkage factor to vary from cell to cell. Each cell's MLE is shrunk towards the central rate by its shrinkage factor. In this way, attrition information from one cell "spills over" into other cells.

The shrinkage methods are developed under the theoretical assumption that the data is normally distributed. Most of the previous studies using empirical Bayes methods have used independent normal data with constant variance (Efron and Morris, 1972).

1973, 1975; Dickinson, 1988). Some applications have used binomial data, using a transformation to make it behave more like normal data (Carter and Rolph, 1974; Efron and Morris, 1975). In Carter and Rolph's estimation of fire alarm probabilities, transformation of the binomial data did not have a large effect on the results (Carter and Rolph, 1974). Our application allows us to investigate the impact of the transformation when applied with more extreme values of p .

Six variations of the empirical Bayes method are applied to the attrition rate estimation problem. The first four are similar in that they use the same iterative procedure to compute the amount of shrinkage for each cell. Of these four, two are on the transformed scale and two on the original scale. Each scale includes two methods of computing the cell variance: one method where the variance is time dependent and the other where it is time independent. The two variance calculations, if they produce like results, provide supporting evidence for the assumption that the data is independent and identically distributed over time. This assumption is certainly questionable, since an officer who remains in a given MOS will move through the YCS and grade cell structure in a predictable manner. As a result, variance that is constant in time (time independent) may not perform as well as one that allows for time variation. The fifth method uses a different iterative procedure to determine the amount of shrinkage and is addressed separately in paragraph III.C.. The final method breaks the cell data into its vector components (service component or commissioning source) before shrinkage techniques are applied and is addressed in paragraph III.D..

B. EMPIRICAL BAYES

1. Transformed Scale

We begin our application of empirical Bayes methods on the transformed scale in an effort to overcome some of the weaknesses in our assumptions. The transformation we use is the Freeman-Tukey transform, a modification of the basic arcsin transformation for binomial data. Its purpose is to stabilize the variance at one and make the data behave more like normal random variables. The form used is

$$X_i(t) = \frac{1}{2} \sqrt{N_i(t) + .5} \left\{ \arcsin\left(\frac{2Y_i(t)}{N_i(t)+1} - 1\right) + \arcsin\left(2\frac{Y_i(t)+1}{N_i(t)+1} - 1\right) \right\}. \quad (4)$$

Now, let

$$XT_i(t) = \frac{X_i(t)}{\sqrt{N_i(t) + .5}} \quad \text{for } t = 1, \dots, T_i \quad (5)$$

except when $N_i(t) = 0$ (no inventory in year t), in which case $XT_i(t)$ does not exist and we reduce T_i by one. The time average of the transformed values for cell i becomes

$$XTB_i = \frac{1}{T_i} \sum_t XT_i(t). \quad (6)$$

We now need to compute the variance of these time averages. Two methods are used: the first calculation is time dependent, i.e., the variance changes over time, the second is time independent.

The transform stabilizes the variance at one for large values of n and non-extreme values of p . These requirements on n and p are often violated in our application, therefore we have many combinations of n and p for which the variance is less than one. Dickinson was able to discover an interpolative formula which provides a good approximation for the variance of the transformed values, $X_i(t)$, for small values of n and p , and $K \geq 3$ (Dickinson, 1988, pp.8-11). This variance is given by

$$Var(X_i(t)) = \min\{1, V(X_i(t))\} \quad (7)$$

where $V(X_i(t))$ is found by solving

$$V(X_i(t)) = a(X_i(t) + C)^{b_1} (X_i(t) + C - 1)^{b_2} \quad (8)$$

with

$$C = \sqrt{N_i(t) + .5} \left(\frac{\pi}{2} \right) \quad (9)$$

and

$$a = 1.6835 \quad b_1 = -.8934 \quad b_2 = .9881. \quad (10)$$

Equation (8) obviously breaks down if $X_i(t) + C < 1$. When this occurs, we set $X_i(t) + C = 1.001$ and continue. The effect is to use a small but positive variance. The

value of one in Equation (7) dominates for about $X_i(t) + C \geq 2.2$. The variance of the time average is then

$$Var(XTB_i) = \frac{1}{T_i^2} \sum_t Var(XT_i(t)) = \frac{1}{T_i^2} \sum_t \frac{Var(X_i(t))}{N_i(t) + .5} . \quad (11)$$

The second method of computing the variance is the more familiar one. Continuing from Equation (6), the variance of the transformed values is given by

$$Var(XT_i) = \frac{1}{T_i - 1} \sum_t (XT_i(t) - XTB_i)^2 . \quad (12)$$

The variance of their average is therefore

$$Var(XTB_i) = \frac{1}{T_i} Var(XT_i) . \quad (13)$$

Regardless of which variance calculation we use, the same iterative algorithm is used to determine the empirical Bayes estimate for each cell. This estimate, XEB_i , is found by solving

$$XEB_i = \frac{A}{A + Var(XTB_i)} XTB_i + \frac{Var(XTB_i)}{A + Var(XTB_i)} XBB \quad (14)$$

where XEB_i , XTB_i and $Var(XTB_i)$ are cell specific, XBB is the (weighted) grand mean or central attrition rate, and A is the variance of the prior distribution of the cell means. These latter two values must be estimated simultaneously using the following iterative algorithm.

We initialize the algorithm with $A = 0$ and store the previous value of A by

$$A_0 \leftarrow A . \quad (15)$$

Now compute the (weighted) grand mean, XBB . Let

$$\alpha_i = \frac{1}{A + Var(XTB_i)} \quad (16)$$

and

$$\gamma_i = \frac{\alpha_i}{\sum_{j=1}^K \alpha_j} . \quad (17)$$

Then

$$XBB = \sum_{i=1}^K \gamma_i XTB_i . \quad (18)$$

The updated value of A becomes

$$A \leftarrow A - \frac{K - 1 - \sum_{i=1}^K \alpha_i (XTB_i - XBB)^2}{\sum_{i=1}^K \alpha_i^2 (XTB_i - XBB)^2} . \quad (19)$$

If $A \leq 0$, set $A = 0$ and exit. This represents the case when there is 100% shrinkage toward the grand mean. If $A > 0$, then check $|A - A_0| < \epsilon$ (e.g., $\epsilon = .0001$). If false, return to Equation (15) for another iteration. If true, the iterations have converged. Exit with the current values of A and XBB for use in Equation (14) to solve for the XEB_i .

Close study of Equation (14) shows that the amount of shrinkage changes from cell to cell since the variance terms are generally not equal. Specifically, cells with higher variance are shrunk more than those with lower variance. In addition, if A is small the shrinkage is greater towards XBB . As $A \rightarrow \infty$, the shrinkage is minimal and the individual cell means dominate.

Once the XEB_i are determined, these values must be transformed back to the original scale. We use

$$\hat{p}_i = \frac{1}{2} \{1 + \sin(XEB_i)\} . \quad (20)$$

2. Original Scale

We return to the assumption of binomial data for original scale calculations. As in the transformed scale, two methods to calculate the variance are used. We begin

with

$$XT_i(t) = \hat{p}_i(t) = \frac{Y_i(t)}{N_i(t)}. \quad (21)$$

As before, if $N_i(t) = 0$ (no inventory in year t), $XT_i(t)$ does not exist and we reduce T_i by one. This leads to the time average for cell i as

$$XTB_i = \frac{1}{T_i} \sum_t XT_i(t) = \frac{1}{T_i} \sum_t \hat{p}_i(t). \quad (22)$$

The variance calculation which is time dependent, i.e., changes over time, is given by

$$Var(XTB_i) = \frac{1}{T_i^2} \sum_t Var(XT_i(t)) = \frac{1}{T_i^2} \sum_t \frac{\hat{p}_i(t)(1 - \hat{p}_i(t))}{N_i(t)}. \quad (23)$$

We return to Equation (15) with these variance values to perform the iterative algorithm for finding the empirical Bayes estimate, XEB_i , given by Equation (14). Since we are already in the original scale, the transformation given in Equation (20) is ignored, i.e., $\hat{p}_i = XEB_i$.

A problem arises while performing the iterations if a cell has $Y_i(t) = 0 \forall t$ (zero attrition for every year). In this case, the variance given by Equation (23) equals zero. When this value is used in Equation (16), the formula for α_i becomes undefined. We resolve this problem using the Laplace Law of Succession. Assume that $Y_i(t) \sim Bin(N_i(t), p_i)$ and let

$$p_i^* = \frac{Y_i(t) + 1}{N_i(t) + 1} \quad \text{and} \quad q_i^* = \frac{N_i(t) - Y_i(t)}{N_i(t) + 1} \quad (24)$$

be the estimates as prescribed by this law, i.e., Bayes estimator using uniform prior. Then

$$Var\left(\frac{Y_i(t)}{N_i(t)}\right) = \frac{p_i^* q_i^*}{N_i(t)} = \frac{\left(\frac{Y_i(t) + 1}{N_i(t) + 1}\right)\left(\frac{N_i(t) - Y_i(t)}{N_i(t) + 1}\right)}{N_i(t)}. \quad (25)$$

If $Y_i(t) = 0$, then

$$\text{Var}\left(\frac{Y_i(t)}{N_i(t)}\right) = \frac{\left(\frac{1}{N_i(t)+1}\right)\left(\frac{N_i(t)}{N_i(t)+1}\right)}{N_i(t)} = \frac{1}{(N_i(t)+1)^2}. \quad (26)$$

This value is used as the summand in Equation (23) whenever $Y_i(t) = 0$ (zero attrition in any year).

For comparison purposes we again compute an alternate variance which is time independent. Continuing from Equation (22), let

$$\tilde{p}_i = \frac{\sum_t Y_i(t)}{\sum_t N_i(t)}. \quad (27)$$

The alternate variance is given by

$$\text{Var}(XTB_i) = \frac{1}{T_i^2} \sum_t \text{Var}(XT_i(t)) = \frac{\tilde{p}_i(1-\tilde{p}_i)}{T_i^2} \sum_t \frac{1}{N_i(t)}. \quad (28)$$

The problem with cells that have $Y_i(t) = 0 \forall t$ (zero attrition for every year) also occurs here, since the variance given by Equation (28) would equal zero. Using the same concept as before, we obtain the formula

$$\text{Var}(XTB_i) = \frac{\sum_t N_i(t)}{\left(1 + \sum_t N_i(t)\right)^2} \frac{1}{T_i^2} \sum_t \frac{1}{N_i(t)}. \quad (29)$$

However in this case, this variance formula is necessary only if all years have zero attrition.

As before, we return to Equation (15) to perform the iterative algorithm for finding the empirical Bayes estimate, XEB_i , given by Equation (14).

C. EFRON-MORRIS METHOD

This method is a modification of the iterative algorithm used to estimate A and XBB given by Efron and Morris (Efron and Morris, 1973, pp.127-129). It differs from the method given by Equations (14) through (19) in that it allows the variance of the prior, A , to change from cell to cell. It also gives greater weight to the cells with low variance, and reduces to the James-Stein estimator when the cell variances are constant.

Only one scenario for this method is considered, corresponding to the initial transformed scale, time dependent variance case. Thus, Equations (4) through (11) are repeated, and we begin from the point where we are entering the iterative algorithm. To simplify the following equations, let $D_i = Var(XTB_i)$ as given by Equation (11).

We initialize the algorithm with $A_i = 0$ and $SP_i = 0$ (previous values of S) for $i = 1, \dots, K$. Let

$$\alpha_i = \frac{1}{A_i + D_i} \quad (30)$$

and

$$\gamma_i = \frac{\alpha_i}{\sum_{j=1}^K \alpha_j} \quad (31)$$

Then

$$\hat{X} = \sum_{i=1}^K \gamma_i XTB_i \quad (32)$$

and

$$S_i = (XTB_i - \hat{X})^2 \quad (33)$$

Now set $i = 1$ and let

$$SN_i = \sum_{j \neq i} \frac{S_j - D_j}{(A_j + D_j)^2} \quad (34)$$

and

$$SD_i = \sum_{j \neq i} \frac{1}{(A_j + D_j)^2} . \quad (35)$$

We then use the Newton-Raphson iteration method to solve

$$A_i = \frac{(S_i - 3D_i) + (A_i + D_i)^2 SN_i}{3 + (A_i + D_i)^2 SD_i} = g(A_i) . \quad (36)$$

First set $AP_i \leftarrow A_i$ for $i = 1, \dots, K$ (previous values of A_i). The updated value for A_i becomes

$$A_i \leftarrow A_i - \frac{A_i - g(A_i)}{1 - g'(A_i)} . \quad (37)$$

If $A_i \leq 0$, set $A_i = 0$, let $i = i + 1$, and return to Equation (34). If $A_i > 0$, then test $|A_i - AP_i| > \varepsilon$. If true, return to Equation (36). If false, let $i = i + 1$ and return to Equation (34).

In either case after incrementing i , if $i = K + 1$, we exit and test $|S_i - SP_i| < \varepsilon \ \forall i$. If false, we update $SP_i \leftarrow S_i$ and return to Equation (30) with updated values of A_i . If true, the iterations have converged and we must finalize the estimators, XEM_i . Let

$$d_i^* = 3 + (A_i + D_i)^2 \sum_{j \neq i} \frac{1}{(A_j + D_j)^2} \quad (38)$$

and

$$B_i = \left(1 - \frac{4}{d_i^*}\right) \frac{D_i}{A_i + D_i} . \quad (39)$$

If $B_i > 1$, set $B_i = 1$, or if $B_i < 0$, set $B_i = 0$. Then

$$XEM_i = \hat{X} + (1 - B_i)(XTB_i - \hat{X}) . \quad (40)$$

This equation is comparable to Equation (14), which was used to determine the transformed scale estimates, XEB_i , using the previous iterative algorithm. The quantity B_i is

the amount of shrinkage toward the grand mean, $\hat{X}$. The corresponding quantity in Equation (14) is $\frac{Var(XTB_i)}{A + Var(XTB_i)}$.

To obtain $\hat{p}_i$, the XEM_i must be transformed back to the original scale using XEM_i in place of XEB_i in Equation (20).

D. VECTOR METHOD

This method is similar to the previous methods in the sense that it uses the aggregated cells produced to meet the defined threshold levels. However, prior to the estimation process, we now partition each aggregated cell by either service component or commissioning source, thus obtaining cells whose elements are vectors. The procedure given by Efron and Morris, modified to compensate for the assumed variance of the time averages, provides the framework for this method (Efron and Morris, 1972, pp.341-344).

The separation by service component or commissioning source requires us to define a third index: the components of the vector. Let

$$P = \text{number of service components/commissioning sources.} \quad (41)$$

Then for $i = 1, \dots, K, j = 1, \dots, P$ and $t = 1, \dots, T$

$$\begin{aligned} N_{ij}(t) &= \text{inventory of cell } i \text{ and vector component } j \text{ in year } t \\ Y_{ij}(t) &= \text{number of attritions in cell } i \text{ and vector component } j \text{ in year } t. \end{aligned} \quad (42)$$

Before we had K cells with scalar information, but now we need a $K \times P$ matrix where

$$\sum_{j=1}^P N_{ij}(t) = N_i(t) \quad \text{and} \quad \sum_{j=1}^P Y_{ij}(t) = Y_i(t). \quad (43)$$

A requirement for this method is that $K > P + 2$, for reasons that will soon become obvious.

We begin by defining $X_{ij}(t)$ as the transformed value for $N_{ij}(t)$ and $Y_{ij}(t)$ as given by Equation (4). Continuing in similar manner as the previous transformed scale methods, let

$$XT_{ij}(t) = \frac{X_{ij}(t)}{\sqrt{N_{ij}(t) + .5}} \quad \text{for } t = 1, \dots, T_{ij} \quad (44)$$

except when $N_{ij}(t) = 0$, in which case $XT_{ij}(t)$ does not exist and we reduce T_{ij} by one.

The time averages of the transformed values are then

$$XTB_{ij} = \frac{1}{T_{ij}} \sum_i XT_{ij}(t). \quad (45)$$

Here we obtain a vector of grand mean values, with each of the P grand means defined by

$$XBB_j = \frac{1}{K} \sum_{i=1}^K XTB_{ij}. \quad (46)$$

The transformed scale estimate, δ_{ji} , is then found by solving

$$\delta_{ji} = XBB_j + \{I_P - (K - P - 2)\tilde{S}^{-1}\}(XTB_{ji} - XBB_j) \quad (47)$$

where I_P is the identity matrix of order P , and $\tilde{S}^{-1}$ is found as discussed below. Reversal of the ij index in this and subsequent equations simply means the transpose of the $K \times P$ matrix to a $P \times K$ matrix.

To solve for $\tilde{S}^{-1}$, we begin by defining

$$\tilde{S} = X_{ji} X_{ji}^T \quad (48)$$

where

$$X_{ji} = (XTB_{ji} - XBB_j) \sqrt{V_{ji}}. \quad (49)$$

The V_{ji} matrix is the modification required by our application. (The multiplication in Equation (49) is element-wise as opposed to normal matrix multiplication.) The Efron and Morris method was developed under the assumption that $XTB_{ij} \sim N(\theta_{ij}, 1)$, whereas we are using

$$XTB_{ij} \sim N\left(\theta_{ij}, \frac{1}{T_{ij}^2} \sum_i \frac{1}{N_{ij}(t) + .5}\right) \quad (50)$$

provided that $XT_{ij}(t)$ has variance of one. Therefore

$$V_{ij} = \frac{1}{T_{ij}^2} \sum_i \frac{1}{N_{ij}(t) + .5} . \quad (51)$$

We use the requirement that the $P \times P$ matrix resulting from the operations within the brackets in Equation (47) must be nonnegative definite to solve for $\tilde{S}^{-1}$ without having to actually compute its inverse. We proceed by doing an eigenanalysis of $\tilde{S}$, which is seen by Equation (48) to be a real symmetric matrix. We form the diagonal matrix E , which has the eigenvalues, e_j , as its diagonal elements, and the matrix Γ , which has the corresponding eigenvectors as its columns. For any $e_j < (K - P - 2)$, we replace it with the value $(K - P - 2)$. The eigenanalysis provides us with the solution to

$$\begin{aligned} \tilde{S} \Gamma_j &= \Gamma_j e_j \\ \text{or } \tilde{S} \Gamma &= \Gamma E . \end{aligned} \quad (52)$$

Post-multiplying by Γ^T , we obtain

$$\tilde{S} = \Gamma E \Gamma^T \quad (53)$$

since Γ is ortho-normal and therefore $\Gamma \Gamma^T = I_p$. We then have

$$\tilde{S}^{-1} = (\Gamma E \Gamma^T)^{-1} = \Gamma E^{-1} \Gamma^T \quad (54)$$

which is easily solved since E^{-1} is found by replacing the diagonal elements of E by their reciprocal. This solution for $\tilde{S}^{-1}$ is then used in Equation (47) to solve for the transformed scale estimates, δ_{ji} . To obtain the attrition rate estimate for a cell, $\hat{p}_{ji}$, we use the inversion formula given by Equation (20) with δ_{ji} in place of XEB_i .

IV. CROSS VALIDATION

A. GENERAL

The six estimation methods discussed in Chapter III are evaluated using cross validation of the data base. This consists of successively holding out one year's data while the other nine years are used to estimate that year's attrition rates. Three measures of effectiveness (MOEs) are used to evaluate the validity of our assumptions and the performance of the estimation methods. Two of these are original scale MOEs--mean absolute deviation (MAD) and chi square statistic. The third is a transformed scale MOE--mean squared error (MSE). Test cases are chosen as input. The results of the cross validation are then discussed.

B. MEASURES OF EFFECTIVENESS

1. Mean Absolute Deviation

The MAD is probably the most useful MOE to the manpower planner. Our version is augmented to display overestimation and underestimation information. Along with the MAD we observe the magnitude of our errors in both directions, which is especially important since the cost of overestimating is generally not the same as the cost of underestimating. While it does not provide a specific value or standard to gauge the performance of our estimation methods, it does provide very useful insight into tendencies to consistently underestimate or overestimate.

For comparison of the estimation methods, we desire a MAD measure that does not depend upon cell inventories, yet still displays the overage/underage information. For these reasons, we use the attrition rate estimates, $\hat{p}_i$, as opposed to the estimated number of attritions, $(\hat{p}_i \cdot N_i(t))$ (where t = validation year), in our MAD calculations. For those estimates obtained in the transformed scale, the XEB_i are inverted back to the original scale using Equation (20) prior to calculating this MOE.

We define the empirical attrition rate for cell i in validation year t as

$$p_i^a = \frac{Y_i(t)}{N_i(t)} \quad (55)$$

except when $N_i(t) = 0$ (no inventory in cell i for the validation year). In this case we do not compute the cell's deviation from the estimated attrition rate since it would

artificially create an overage situation. Therefore, we reduce K by one and continue with the remaining cells (the reduced value of K is then used in the following formulas).

The MAD measures generated for each validation year are

$$\frac{K_u}{K} = \text{fraction of cells with underage} \quad (56)$$

where K_u is the number of cells which have underage,

$$\frac{\sum_i (p_i^a - \hat{p}_i)^+}{\sum_i |p_i^a - \hat{p}_i|} = \text{fraction of MAD due to underage} \quad (57)$$

and

$$MAD = \frac{1}{K} \sum_i |p_i^a - \hat{p}_i|. \quad (58)$$

We also calculate the average MAD over the validation years. Here we use a weighted average, since the number of cells may have been different in some validation years, i.e., a reduced value of K was used in these years. The weighted average takes the form

$$\text{Avg MAD} = \frac{\sum_t K_t MAD_t}{\sum_t K_t} \quad (59)$$

where K_t is the (possibly reduced) number of cells used in validation year t .

2. Chi Square

The chi square test is used as an indicator of how well the binomial model serves as a description of the attrition process. The test statistic is

$$X_{(K)}^2(t) = \sum_i \frac{(Y_i(t) - \hat{p}_i N_i(t))^2}{N_i(t) \hat{p}_i (1 - \hat{p}_i)} \quad (60)$$

where t is the validation year. As with the MAD calculations, if $N_i(t) = 0$ we reduce K by one and continue. Additionally, if $\hat{p}_i = 0$ or 1 , the denominator equals zero and the summand is undefined. The same course of action is used if this occurs--reduce K by one and continue. Those estimates obtained in the transformed scale are inverted back to the original scale prior to using Equation (60).

This MOE can be used as a gauge. The chi square statistic given by Equation (60) has expected value K and variance $2K$. We are looking for a X^2 value that is less than two standard deviations to the right of the mean, or

$$X_{(K)}^2 \leq K + 2\sqrt{2K} . \quad (61)$$

A weighted average chi square is computed in the same manner as the weighted average MAD in Equation (59). However, if the number of cells and thus the degrees of freedom, K , are different over the validation years a problem arises in determining the degrees of freedom for the weighted average. We solve this dilemma by assuming that the weighted average chi square has the original value of K degrees of freedom.

3. Mean Squared Error

The MSE is used to check the validity of our theoretical basis. It is the average squared deviation of the estimated rate from the actual rate, both rates on the transformed scale. The actual rate used is the transformed validation year data. The MSE is defined as

$$L(\delta, \mu) = \frac{1}{K} \sum_i (\delta_i - \mu_i)^2 \quad (62)$$

where

$$\begin{aligned} \delta_i &= XEB_i \\ \mu_i &= XT_i(t) \quad (t = \text{validation year}) . \end{aligned} \quad (63)$$

Again, if $N_i(t) = 0$, we reduce K by one and continue. A weighted average MSE is also computed similar to Equation (59).

The MSE also has a standard to gauge our model. Using Equations (5) and (12) we can compute a baseline variance for any given validation cell. The MSE for that cell, when compared to the baseline value, provides a figure to gauge the value of using shrinkage estimators instead of the cell averages, XTB_i . There is considerable variability

in these ratios, ranging from 20% to 100%, but 80% appears to be a fair median figure. For example, for cell variances computed from Equation (12) running about 0.15, the MSE hovers about 0.12.

4. Vector Method MOEs

The MOEs discussed above require slight modification before being applied to the vector method described in paragraph III.D.. Recall that this method uses K cells with service component or commissioning source broken out into a vector of length P . An attrition rate estimate, δ_{ij} , is obtained for each of the $K \times P$ matrix components. Thus now we have KP estimates which are compared to the corresponding empirical rates for the validation year. Equations (55) through (63) are modified by replacing all i subscripts with ij , replacing all summations over i by double summations over i and j , and replacing all instances of K by the product KP .

C. TEST CASES

The selection of test cases takes on great importance since they provide the foundation for comparison of these methods. It would be impossible to test every permutation of input parameters; therefore we seek a representative fraction of these which would give an accurate account of the performance of our aggregation and estimation methods. Because we are using a different data base from previous theses on estimation methods, no attempt to duplicate their test cases was made.

An approach based upon Latin square experimental design principles was used to select 30 test cases for the first five estimation methods. The test cases for the vector estimation method are addressed later. In determining the test cases, we randomized when possible and intervened to force pairings only when necessary. To begin, we selected values for the input parameters-- T_0 , K_0 , grade, YCS and MOS. Service component and commissioning source are ignored for these test cases, i.e., all classifications of both are accepted.

To ensure proper representation from small MOS groups one through ten, one MOS from each group was randomly selected: 0302, 1802, 2502, 4002, 3060, 7204, 7545, 7523, 7557 and 7563. Since YCS and grade are strongly correlated, these parameters were selected jointly. To ensure each YCS range within the bounded YCS groups was represented along with a fair representation of grades, four grade/YCS pairs were selected: 1Lt/4 YCS, Capt/7 YCS, LtCol/20 YCS and LtCol(failed select)/26 YCS. The two threshold parameters were also selected jointly, resulting in ten pairs (T_0/K_0): 30.0/30, 20.0/30, 20.0/20, 10.0/30, 10.0/20, 10.0/10, 5.0/30, 5.0/20, 5.0/10 and 5.0/5.

With these choices in place, it was necessary to combine them to define the actual test cases. It was decided to limit the grade/YCS pairs for these cases to 1Lt/4 YCS and Capt/7 YCS due to the large values for the first five threshold pairs. With ten MOSs specified, we sought ten test cases. Thus, each of the first five threshold pairs was listed twice. Each of the four aviation MOSs was randomly assigned to one of the five threshold pairs; the six ground MOSs were then randomly assigned to the remaining pairs. The two grade/YCS pairs were then randomly assigned within a set of common threshold pairs, e.g., for the two cases with T_0 / K_0 of 30.0/30, one was randomly assigned 1Lt/4 YCS, the other was then assigned Capt/7 YCS.

All four grade/YCS pairs would be used with the five remaining threshold pairs. Thus 20 more test cases were generated, with each of the five threshold pairs listed four times. Each MOS was randomly assigned to two distinct threshold pairs, ensuring that the large and major MOS groups were evenly spread throughout the pairs. The four grade/YCS pairs were assigned in random order to each set of common threshold pairs, ensuring that they were evenly spread across large and major MOS groups. The 30 test cases are summarized in Table 3.

The input parameters for six vector test cases were selected from the 30 test cases: Nos. 2, 3, 6, 10, 11 and 20. A small number of vector test cases was initially chosen to investigate the possible advantages of the vector method. If this method appeared to be favorable, then further testing would be conducted.

The six test cases contain a cross section of the input parameters. They include three ground and three aviation MOSs, and use each of the first three grade/YCS pairs twice. The grade/YCS pair of LtCol(FS)/26 YCS was not used because of its extremely low inventory numbers, which when broken out into a vector would have been of little exploratory use. These cases also include six different T_0 / K_0 pairs.

Each of the vector test cases is used twice: first with service component and then with commissioning source as the vector component. All three service components--regular, augmented regular and reserve--were used as vector components. Rather than use all 15 commissioning sources (these 15 are listed below Table 4) as vector components (many of them would contain little or no inventory) five commissioning sources for the ground test cases and five for the aviation test cases were chosen. These five were determined to be the sources which contain the largest percentage of inventory for the respective ground or aviation MOSs. The specific commissioning sources selected along with the other vector test case input parameters are summarized in Table 4.

Table 3. TEST CASES FOR METHODS 1-5

No.	T_0	K_0	MOS	S : L : M	YCS	Grade
1	30.0	30	0302	1 : 1 : 1	4	1Lt
2	30.0	30	7523	8 : 3 : 2	7	Capt
3	20.0	30	3060	5 : 2 : 1	7	Capt
4	20.0	30	7563	10 : 4 : 2	4	1Lt
5	20.0	20	2502	3 : 2 : 1	7	Capt
6	20.0	20	7557	9 : 4 : 2	4	1Lt
7	10.0	30	7204	6 : 2 : 1	4	1Lt
8	10.0	30	1802	2 : 1 : 1	7	Capt
9	10.0	20	7545	7 : 3 : 2	7	Capt
10	10.0	20	4002	4 : 2 : 1	4	1Lt
11	10.0	10	2502	3 : 2 : 1	20	LtCol
12	10.0	10	7557	9 : 4 : 2	26	LtCol(FS)
13	10.0	10	7545	7 : 3 : 2	7	Capt
14	10.0	10	0302	1 : 1 : 1	4	1Lt
15	5.0	30	4002	4 : 2 : 1	4	1Lt
16	5.0	30	0302	1 : 1 : 1	20	LtCol
17	5.0	30	7204	6 : 2 : 1	26	LtCol(FS)
18	5.0	30	7563	10 : 4 : 2	7	Capt
19	5.0	20	3060	5 : 2 : 1	7	Capt
20	5.0	20	7545	7 : 3 : 2	20	LtCol
21	5.0	20	1802	2 : 1 : 1	26	LtCol(FS)
22	5.0	20	7563	10 : 4 : 2	4	1Lt
23	5.0	10	7204	6 : 2 : 1	20	LtCol
24	5.0	10	4002	4 : 2 : 1	26	LtCol(FS)
25	5.0	10	7523	8 : 3 : 2	4	1Lt
26	5.0	10	1802	2 : 1 : 1	7	Capt
27	5.0	5	2502	3 : 2 : 1	7	Capt
28	5.0	5	7557	9 : 4 : 2	20	LtCol
29	5.0	5	3060	5 : 2 : 1	4	1Lt
30	5.0	5	7523	8 : 3 : 2	26	LtCol(FS)

(S : L : M = Small MOS Group : Large MOS Group : Major MOS Group)

Table 4. TEST CASES FOR VECTOR METHOD

No.	T_0	K_0	MOS	YCS	Grade	Service Comp	Comm Source
2	30.0	30	7523	7	Capt	1 2 3	(all)
2	30.0	30	7523	7	Capt	(all)	1 2 3 5 11
3	20.0	30	3060	7	Capt	1 2 3	(all)
3	20.0	30	3060	7	Capt	(all)	1 3 7 10 11
6	20.0	20	7557	4	1Lt	1 2 3	(all)
6	20.0	20	7557	4	1Lt	(all)	1 2 3 5 11
10	10.0	20	4002	4	1Lt	1 2 3	(all)
10	10.0	20	4002	4	1Lt	(all)	1 3 7 10 11
11	10.0	10	2502	20	LtCol	1 2 3	(all)
11	10.0	10	2502	20	LtCol	(all)	1 3 7 10 11
20	5.0	20	7545	20	LtCol	1 2 3	(all)
20	5.0	20	7545	20	LtCol	(all)	1 2 3 5 11

Service Component:

- 1 - regular
- 2 - augmented regular
- 3 - reserve

Commissioning Sources used:

- 1 - U.S. Naval Academy
- 2 - Platoon Leader Class-Aviation
- 3 - Platoon Leader Class-Ground
- 5 - Aviation Officer Candidate
- 7 - Officer Candidate Course-Ground
- 10 - Enlisted Commissioning Program
- 11 - NROTC-Scholarship

Commissioning Sources not used:

- 4 - Platoon Leader Class-Law
- 6 - Marine Aviation Cadet
- 8 - Officer Candidate Course-Law
- 9 - Officer Candidate Course-Women
- 12 - NROTC-Ground College
- 13 - NROTC-Aviation College
- 14 - NESEP
- 15 - All Other

D. RESULTS

For each test case, we apply the aggregation method to meet the threshold levels and then execute the estimation methods. While the ultimate use of these methods is to obtain an attrition rate estimate for the original cell, inspection of these estimates would be of little value in evaluating and comparing the estimation methods. Thus the output from the program takes the form of the MOEs.

The inclusion of the entire output from every test case would not only be cumbersome but would provide an inadequate means of comparing the methods. Therefore the output is summarized in Tables 5 through 7. They contain the output from the first five estimation methods only; the output from the vector test cases is presented later. Sample output for the six methods is contained in Appendix C.

The results summaries list the test case number, the cell inventory threshold, T_0 , and the actual number of cells used, K . The level of expansion required to achieve these parameter levels is also listed. For example, test case one had a cell inventory threshold of 30.0, and 24 aggregated cells were obtained by expanding the small, large and major MOS group by YCSs four and five. The value for K is often different from the threshold number of cells, K_0 , listed in Table 3. When K is less than K_0 , maximum expansion occurred and the threshold was unattainable. When K is greater than K_0 , the expansion was the least amount possible to remain above the thresholds. From these test cases we can see that it is difficult to meet the threshold number of cells exactly.

The results summaries then list the weighted average MOEs for each of the five estimation methods. The first row within each test case contains the MAD values, the second row the chi square values and the third row the MSE values. The maximum desired chi square value as given by Equation (61) is listed in parentheses, e.g., for test case one this value is 37.9. This affords easier comparison of the chi square values for the different methods. The values of MSE for both original scale methods are blank because MSE is a transformed scale MOE only.

Before discussing the results in general, some additional comments about specific test cases are necessary. Test case four could not be executed by the Efron-Morris method. This is because one of the aggregated cells contains zero attrition for all ten years of data. As a result, the iterative algorithm does not converge.

Test case 12 was not possible because not even one aggregated cell meeting the cell inventory threshold was obtained with maximum expansion in major MOS group two. This extremely low inventory problem was generally true for all test cases involving the LtCol(FS)/26 YCS pair. Test cases 17, 21 and 24 obtained only three aggregated cells

with maximum expansion in major MOS group one. Test case 30 was also from major MOS group two, and obtained only one aggregated cell meeting the cell inventory threshold. As a result, test case 30 was changed to Major(FS)/18 YCS so that results for these low thresholds could be obtained.

As the thresholds became low (test cases 23-30) cells with inventory much larger than T_0 were being obtained prior to any aggregation. This was especially true for the ILt/4 YCS and Capt/7 YCS pairs. To avoid masking the results of low inventory thresholds by actually using large inventory cells, the service component/commissioning source parameters for test cases 26, 27 and 29 were changed. Rather than accepting all classifications of these parameters, only one classification for each was accepted. Thus test case 26 was executed with regular/USNA, test case 27 was executed with augmented regular/PLC-ground, and test case 29 was executed with regular/NROTC-scholarship.

We now focus our attention on the results of these test cases with respect to the MOEs. The weighted average MAD figures vary little within each test case over the five methods. This suggests that the total deviation from the validation year empirical attrition rate was the same for all methods. However, this figure does not identify whether the deviations were overestimations or underestimations. The fraction of MAD from underage (not listed in the results summaries) was studied to gain more insight into this important consideration. For each of the 29 test cases (no results for test case 12), a weighted average fraction of MAD from underage was computed for each of the five estimation methods (weighted by the number of cells just as the weighted averages for the MOEs). A weighted average of these 29 values was then computed. This overall weighted average indicates the tendency of the method to underestimate or overestimate--averages above 0.5 indicate a tendency to underestimate; averages below 0.5 indicate a tendency to overestimate. The author is unaware of any information comparing the relative costs of underage and overage. Hence, as a default, we look for values of 0.5, which is a balance between overestimation and underestimation. The averages calculated were: TS1=0.426; TS2=0.436; OS1=0.481; OS2=0.512; and EM=0.452. Although the MAD figures were generally the same for all methods, these averages indicate that the tendencies to overestimate or underestimate may not be the same. The original scale methods seem to have achieved more balance than the transformed scale methods.

The chi square results were not entirely consistent across test cases nor across methods within a test case. These results are discussed first by comparisons between test cases; then by comparisons within test cases.

Of the first ten test cases, only three (Nos. 3, 5 and 8) had weighted average chi square values within the acceptable range. These three test cases expanded only into the large MOS group, whereas of the seven test cases which were unacceptable, all but one (No. 10) expanded into the major MOS group. Of the last 20 test cases, only four had chi square values outside the acceptable range (Nos. 13, 14, 15, and 18). Of these four, two expanded into the large MOS group, and two into the major MOS group. All the test cases with unacceptable values had either 1Lt/4 YCS or Capt/7 YCS pairs. They were fairly well spread across MOS groups. None of the test cases with lower thresholds (Nos. 19-30) had unacceptable chi square values. This suggests that lower thresholds, which result in less expansion, achieve more acceptable results with respect to this MOE.

To investigate this claim further, different combinations of threshold levels for test cases seven and nine were used. The results are contained in Table 8. These results reinforce the claim that lower thresholds are in fact better, since in both cases the chi square results improved as the thresholds, and therefore the level of expansion, were reduced. When comparing these extra test cases, keep in mind that the chi square values for each set of threshold values should be compared to the acceptable range for that specific number of cells; comparisons across test cases with different values of K are not valid. An important aspect of the argument for lower thresholds is that the thresholds must be considered jointly. For example, in test case seven, with a T_0/K pair of 10.0/6, the chi square values were nearly acceptable, whereas with 5.0/19 they were clearly unacceptable. Thus we should be most aware of the value $T_0 \times K_0$.

We now turn our attention to comparing the chi square values within a test case. Several test cases had chi square values that varied significantly over the estimation methods (Nos. 4, 6 and 22). These three all had 1Lt/4 YCS pairs and were large MOS group four. In test cases four and six the chi square values for the transformed scale methods were not too much larger than the desired maximum; the values for the original scale methods were significantly larger than the desired maximum. In test case 22 the chi square values for the transformed scale methods were acceptable, however the values for the original scale methods were again significantly larger than the desired maximum.

Several other test cases had varying chi square values, but to a lesser degree. In test case eight, only the transformed scale methods had acceptable chi square values, the original scale methods exceeded the desired maximum, although not by a significant margin. In test case 19, only the OS2 method exceeded the desired maximum. All methods for test cases 16, 25, and 27 were within the desired maximum, however the chi square values varied to a large degree over the five methods. Thus, using the chi square

MOE, it appears that the transformed scale methods were generally the same, and as a group outperformed the original scale methods.

The MSE was used only with the transformed scale methods, and thus no comparison with original scale methods can be made. The values for this MOE were generally equal between methods within a test case, and acceptable overall.

The results for the vector method test cases are summarized in Table 9. The table lists the value $K \times P$ (instead of K) because this is the number of estimates obtained and compared to the validation year empirical attrition rates with this method.

Test case two with commissioning source as the vector component had to be modified because only seven aggregated cells were obtained. As a result, $K = P + 2$, and the vector method could not be conducted. Therefore, commissioning source three (Platoon Leader Class-ground) was deleted as a vector component and the test case run with only four commissioning sources (1, 2, 5 and 11). Test case 20 with service component as the vector component was infeasible. By starting with a low cell inventory threshold (5.0), when the cells were broken out into the vector components their inventory became extremely low. As a result, when validating year five, two of the cells had zero inventory for all of the remaining nine years for service component three (reserve). Thus the value for XTB_j , given by Equation (45), becomes undefined and the method cannot be completed.

The results of the vector method with respect to the MOEs is similar to the results of the previous five estimation methods. This method produced acceptable MAD and MSE values, but its chi square values were fairly inconsistent. Test cases two and ten had unacceptable chi square values for both vector components; test case six had an unacceptable chi square value with service component as the vector component. Recall that these test cases also had unacceptable values with the vector component collapsed.

No fair comparison with the first five estimation methods can be made using the summarized results. Obviously the MAD and MSE quantities will be larger since we are comparing three to five times as many estimates to empirical rates with the vector method. Thus a different evaluation technique must be used.

The vector method is designed to take advantage of any correlation between the cells when broken out into vector components. To see if this is occurring we must look at the matrix $\tilde{S}^{-1}$ as given by Equation (54). In all of the vector test cases, this matrix was essentially diagonal, indicating little correlation between the vector components. In addition, all of the eigenvalues, which become the elements of the diagonal matrix E , were less than $(K - P - 2)$. Therefore, the eigenvalues were replaced by this quantity and the

matrix E always had $(K - P - 2)$ as its diagonal elements. Because these results indicated no worthwhile improvements over the first five methods, no further testing of the vector method was conducted.

Finally, the performance of the heuristic aggregation algorithm listed in Appendix A was also evaluated. For each test case, the total inventory of cells below T_0 was summed and this value divided by T_0 . The integer part of this number provides an upper bound on the number of aggregated cells that can be obtained by any aggregation technique. This upper bound was compared to the actual number of aggregated cells produced by the algorithm. The algorithm achieved the maximum in 71.4% (20 of 28) of the test cases. It achieved one less than the maximum in 21.4% (6 of 28) of the test cases, and two less than the maximum in 7.2% (2 of 28) of the test cases (only 28 test cases required aggregation: No. 12 was infeasible; No. 14 all cells were above T_0). This performance is acceptable for our application.

Table 5. SUMMARY OF RESULTS (CASES 1-10)

No.	T_0	K	Expansion Required	MOE	TS1	TS2	OS1	OS2	EM
1	30.0	24	S:(4,5) L:(4,5) M:(4,5)	MAD X(37.9) MSE	0.102 98.79 0.079	0.101 99.28 0.078	0.102 100.99	0.102 100.96	0.103 101.23 0.080
2	30.0	8	S:(7) L:(7) M:(7)	MAD X(16.0) MSE	0.091 28.16 0.077	0.090 27.68 0.076	0.092 28.71	0.091 28.68	0.091 27.73 0.076
3	20.0	31	S:(1-3,6-19) L:(6-8)	MAD X(46.7) MSE	0.056 37.49 0.062	0.056 37.80 0.062	0.055 39.58	0.055 42.85	0.055 38.38 0.062
4	20.0	23	S:(1-5,8-19) L:(1-5,8-19) M:(1-5,8-19)	MAD X(36.6) MSE	0.029 39.34 0.035	0.029 47.36 0.037	0.026 95.41	0.024 139.14	
5	20.0	20	S:(1-3,6-19) L:(7)	MAD X(32.6) MSE	0.048 20.75 0.048	0.049 20.83 0.049	0.047 24.34	0.047 24.20	0.048 21.41 0.049
6	20.0	22	S:(1-5,8-19) L:(1-5,8-19) M:(3-5)	MAD X(35.3) MSE	0.029 40.42 0.037	0.029 50.70 0.039	0.027 90.93	0.025 127.86	0.029 65.20 0.040
7	10.0	32	S:(4,5) L:(4,5) M:(4)	MAD X(48.0) MSE	0.129 111.67 0.137	0.130 113.23 0.137	0.130 112.64	0.130 113.64	0.133 114.28 0.140
8	10.0	28	S:(1-3,6-19) L:(1-3,6-11)	MAD X(43.0) MSE	0.039 34.37 0.039	0.038 34.70 0.040	0.039 45.16	0.038 49.60	0.039 35.54 0.040
9	10.0	14	S:(7) L:(7) M:(7)	MAD X(24.6) MSE	0.117 38.85 0.130	0.115 37.50 0.127	0.117 39.59	0.117 39.62	0.115 40.26 0.132
10	10.0	27	S:(4,5) L:(4,5)	MAD X(41.7) MSE	0.128 64.33 0.137	0.129 65.92 0.137	0.129 65.62	0.128 66.61	0.127 62.64 0.135

TS1 - Transformed scale, time dependent variance

TS2 - Transformed scale, time independent variance

OS1 - Original scale, time dependent variance

OS2 - Original scale, time independent variance

EM - Efron-Morris method

Table 6. SUMMARY OF RESULTS (CASES 11-20)

No.	T_0	K	Expansion Required	MOE	TS1	TS2	OS1	OS2	EM
11	10.0	11	S:(20-25) L:(20-25)	MAD X(20.4) MSE	0.109 18.79 0.141	0.106 19.75 0.142	0.108 19.96	0.107 20.53	0.107 18.99 0.139
12	10.0	0	S:(26) L:(26) M:(26)	MAD X(0.0) MSE					
13	10.0	14	S:(7) L:(7) M:(7)	MAD X(24.6) MSE	0.117 38.85 0.130	0.115 37.50 0.127	0.117 39.59	0.117 39.62	0.115 40.26 0.132
14	10.0	10	S:(4,5) L:(4,5)	MAD X(18.9) MSE	0.113 57.80 0.102	0.110 60.07 0.103	0.113 57.71	0.113 57.80	0.115 59.36 0.104
15	5.0	32	S:(4,5) L:(4,5)	MAD X(48.0) MSE	0.137 69.96 0.156	0.140 70.72 0.158	0.139 70.27	0.139 72.01	0.139 68.15 0.155
16	5.0	32	S:(20-25) L:(20-25) M:(20-22)	MAD X(48.0) MSE	0.122 39.41 0.146	0.122 40.38 0.146	0.121 44.35	0.121 47.84	0.121 42.27 0.148
17	5.0	3	S:(26) L:(26) M:(26)	MAD X(7.9) MSE	0.166 3.66 0.0189	0.166 3.57 0.188	0.168 3.88	0.168 3.78	0.168 4.02 0.202
18	5.0	29	S:(6,7) L:(6,7) M:(7)	MAD X(44.2) MSE	0.141 79.04 0.176	0.141 78.23 0.176	0.142 78.61	0.141 81.29	0.141 78.84 0.177
19	5.0	24	S:(2,3,6-10)	MAD X(37.9) MSE	0.085 28.95 0.122	0.082 29.28 0.123	0.080 30.91	0.084 43.36	0.080 35.44 0.132
20	5.0	19	S:(20-25) L:(20-25) M:(20)	MAD X(31.3) MSE	0.111 17.29 0.113	0.113 17.29 0.114	0.113 18.92	0.106 23.37	0.110 18.28 0.114

TS1 - Transformed scale, time dependent variance

TS2 - Transformed scale, time independent variance

OS1 - Original scale, time dependent variance

OS2 - Original scale, time independent variance

EM - Efron-Morris method

Table 7. SUMMARY OF RESULTS (CASES 21-30)

No.	T_0	K	Expansion Required	MOE	TS1	TS2	OS1	OS2	EM
21	5.0	3	S:(26) L:(26) M:(26)	MAD X(7.9) MSE	0.167 3.66 0.189	0.166 3.57 0.188	0.168 3.88	0.168 3.78	0.168 4.02 0.202
22	5.0	22	S:(1-5,8-19) L:(3,4)	MAD X(35.3) MSE	0.032 23.56 0.059	0.042 15.03 0.041	0.024 63.10	0.022 92.85	0.032 22.56 0.056
23	5.0	9	S:(20-25) L:(20)	MAD X(17.5) MSE	0.121 8.12 0.141	0.121 8.19 0.141	0.119 8.65	0.121 9.25	0.120 8.17 0.137
24	5.0	3	S:(26) L:(26) M:(26)	MAD X(7.9) MSE	0.166 3.66 0.189	0.166 3.57 0.188	0.168 3.88	0.168 3.78	0.168 4.02 0.202
25	5.0	10	S:(1-6,8-19) L:(1-6)	MAD X(18.9) MSE	0.050 5.09 0.044	0.051 4.78 0.037	0.020 15.35	0.020 16.54	0.048 4.85 0.039
26	5.0	11	S:(1-3,6-19) L:(6,7)	MAD X(20.4) MSE	0.138 13.61 0.184	0.138 13.65 0.186	0.138 14.09	0.135 16.10	0.135 14.28 0.189
27	5.0	6	S:(6-8)	MAD X(12.9) MSE	0.070 4.64 0.075	0.069 4.55 0.074	0.055 6.88	0.050 9.41	0.068 4.60 0.074
28	5.0	7	S:(20,21)	MAD X(14.5) MSE	0.114 7.59 0.140	0.116 7.67 0.143	0.118 7.99	0.113 8.74	0.116 8.37 0.147
29	5.0	5	S:(4,5)	MAD X(11.3) MSE	0.170 6.36 0.211	0.169 6.23 0.210	0.168 7.64	0.167 8.25	0.169 8.06 0.281
30	5.0	6	S:(1-6,8-19) L:(17-19)	MAD X(12.9) MSE	0.112 6.15 0.136	0.110 6.40 0.136	0.110 7.31	0.104 8.73	0.108 6.42 0.135

TS1 - Transformed scale, time dependent variance

TS2 - Transformed scale, time independent variance

OS1 - Original scale, time dependent variance

OS2 - Original scale, time independent variance

EM - Efron-Morris method

Table 8. SUMMARY OF RESULTS (CASES 7 AND 9 EXPANDED)

No.	T_0	K	Expansion Required	MOE	TS1	TS2	OS1	OS2	EM
7-1	10.0	32	S:(4,5) L:(4,5) M:(4)	X(48.0)	111.67	113.23	112.64	113.64	114.28
7-2	10.0	17	S:(4,5) L:(4)	X(28.7)	45.31	45.99	45.90	46.58	43.68
7-3	10.0	6	S:(4,5)	X(12.9)	13.08	12.98	13.41	13.53	13.03
7-4	5.0	19	S:(4,5) L:(4)	X(31.3)	49.28	49.53	49.23	50.84	46.91
7-5	5.0	7	S:(4,5)	X(18.9)	14.42	14.27	14.82	14.93	14.18
7-6	5.0	4	S:(4)	X(9.7)	9.20	8.88	9.22	9.20	9.49
9-1	10.0	14	S:(7) L:(7) M:(7)	X(24.6)	38.85	37.50	39.59	39.62	40.26
9-2	10.0	4	S:(7)	X(9.7)	10.35	10.14	10.58	10.57	10.11
9-3	5.0	17	S:(7) L:(7) M:(7)	X(28.7)	44.95	42.87	44.40	46.03	46.15
9-4	5.0	5	S:(7)	X(11.3)	11.91	11.69	12.16	12.15	11.64

TS1 - Transformed scale, time dependent variance

TS2 - Transformed scale, time independent variance

OS1 - Original scale, time dependent variance

OS2 - Original scale, time independent variance

EM - Efron-Morris method

Table 9. SUMMARY OF RESULTS (VECTOR METHOD)

No.	T_0	KP	Vector Component	MOE	Vector Method
2	30.0	24	SC	MAD X(37.9) MSE	0.149 61.03 0.229
2	30.0	28	CS	MAD X(43.0) MSE	0.222 115.34 0.398
3	20.0	93	SC	MAD X(120.3) MSE	0.158 110.96 0.219
3	20.0	155	CS	MAD X(190.2) MSE	0.157 132.37 0.201
6	20.0	66	SC	MAD X(89.0) MSE	0.062 109.19 0.074
6	20.0	100	CS	MAD X(128.3) MSE	0.083 58.58 0.081
10	10.0	81	SC	MAD X(106.5) MSE	0.212 251.63 0.368
10	10.0	120	CS	MAD X(151.0) MSE	0.321 707.85 0.625
11	10.0	42	SC	MAD X(60.3) MSE	0.193 44.86 0.214
11	10.0	60	CS	MAD X(81.9) MSE	0.222 53.55 0.225
20	5.0	72	SC	MAD X(0.0) MSE	
20	5.0	100	CS	MAD X(128.3) MSE	0.254 55.92 0.245

SC - service component

CS - commissioning source

V. CONCLUSIONS AND RECOMMENDATIONS

A. CONCLUSIONS

The results indicate that the desired stability in estimating attrition rates for low inventory cells has been achieved with the aggregation and estimation methods presented in this study. The use of "shrinkage" methods applied to well selected groups of cells allows for the achievement of quality estimates of attrition in the face of low inventory numbers for the individual cells.

None of the six estimation methods stood out as a clear favorite. The vector method did not provide any additional benefits using service component or commissioning source as vector components. Since it is a more complicated method and has the potential to become unsolvable with zero inventory vector components, it appears to be the least favorite. Perhaps more success would be obtained with alternative classifications for the vector component.

The Efron-Morris method also involves more computational effort than the first four empirical Bayes methods. Its performance was very much similar to the transformed scale, time dependent variance method since the only difference between them is the iterative algorithm used to determine the amount of shrinkage. The Efron-Morris method has the potential to become unsolvable when a cell has zero attrition for every year--a distinct possibility when dealing with low inventory cells. This suggests that it is the least favorite of the first five methods.

Of the remaining four methods, there seems to be only small difference between the time dependent variance and the time independent variance methods on the same scale. In test cases where the chi square values were marginal or unacceptable, the time dependent variance methods were usually better. In these same test cases, the transformed scale methods performed better than the original scale methods. Therefore, if one method was to be singled out as best, it would be the first method: transformed scale, time dependent variance.

The tendency to overestimate or underestimate as shown by the weighted average fraction of MAD from underage may also be a consideration when selecting a method. An analysis of this type must weigh the costs of overestimating versus the costs of underestimating, which generally are not the same. This type of an analysis is beyond

the scope of this study. In addition, further testing of the methods would be required to gain a more accurate estimate of this tendency.

The threshold levels also seem to strongly influence the performance of the estimation methods. It appears that expansion past the large MOS group begins to detract from homogeneous attrition behavior. While further study would be required to identify optimal threshold levels, it is apparent that both thresholds should not exceed 20.0, and the value of $T_0 \times K_0$ should not exceed 100.

A method for dealing with cells whose inventory is much greater than T_0 must be developed. In some test cases, cells with inventory three or more times as large as T_0 were obtained and used in the estimation process. This did not seem to affect the results, as they were present in almost all test cases. These cells could be disaggregated into multiple cells with inventory closer to the threshold, although the effect of this has not been determined.

B. RECOMMENDATIONS

The proposed aggregation method should be implemented as a method of identifying additional cells to be used in the attrition rate estimation process. This method provides greater homogeneity of attrition behavior among cells over the current method.

The empirical Bayes estimation methods developed in this study are recommended for use in estimating the attrition rates for low personnel inventory cells.

Overall, the empirical Bayes estimation methods when combined with the proposed aggregation method have achieved the stability in attrition rate estimation that is required to provide a foundation for manpower planning.

APPENDIX A. AGGREGATION ALGORITHMS

A. HEURISTIC ALGORITHM

The heuristic algorithm for aggregating cells is as follows:

1. Given a set of cells, S , and the (time average) inventory of each cell, INV_c , partition S into two subsets as follows:

$$S_1 = \{c : c \in S; INV_c \geq T_0\}$$

$$S_2 = \{c : c \in S; INV_c < T_0\}$$
2. Put the cells in S_1 into the set of aggregated cells, K .
3. Order the cells in S_2 according to size of their inventory:

$$INV_1 \leq INV_2 \leq \dots \leq INV_n \quad n = |S_2|$$
4. Start with c_n , the cell in S_2 with the largest inventory. Find the smallest cell in S_2 , c' , that when united with c_n the resulting total inventory will meet or exceed T_0 . Combine its data with c_n , put c_n into K , and remove c' from S_2 (the modified set S_2 will now be referred to as S_2^-). Repeat the procedure with c_{n-1} , and so forth.
5. If no cell in S_2^- when combined with the current largest cell, c_{n-i} , exceeds T_0 , use the next largest cell, c_{n-i-1} , and remove c_{n-i-1} from S_2^- . This will create an aggregated cell that is still below threshold. Return to the procedure in Step 4 of trying to find c' . If no such cell is contained in S_2^- , use c_{n-i-2} , and so forth.
6. Continue this procedure until the sum of all the cells remaining in S_2^- is less than T_0 . These cells are sequentially added to the aggregated cells in K in Step 7.
7. Add the largest cell in S_2^- to the smallest cell in K , and update its average inventory. Add the next largest cell in S_2^- to the current smallest cell in K , and update the inventory. Continue until all cells in S_2^- have been used.

We now have $|K|$ aggregated cells which exceed the threshold, T_0 , to use in the attrition rate estimation procedure.

B. INTEGER LINEAR PROGRAM

The formulation as an integer linear program is as follows:

Index Use

c	cell (before aggregation)
a	aggregated cell

Given Data

INV_c	average inventory of cell c
T_0	threshold cell inventory

Binary Variables

$X_{c,a}$ 1 indicates use cell c in aggregated cell a

Z_a 1 indicates use cell a for aggregation

Formulation

$$\text{MAX } \sum_a Z_a$$

subject to

$$\sum_a X_{c,a} \leq 1 \quad \forall c \quad (\text{each cell used at most once})$$

$$\sum_c INV_c \cdot X_{c,a} \geq T_0 \cdot Z_a \quad \forall a \quad (\text{aggregated cell must have size } \geq T_0)$$

$$X_{c,a}, Z_a \in \{0,1\}$$

APPENDIX B. COMPUTER PROGRAMS

A. GENERAL

A computer program written in FORTRAN is used to conduct the cross validation using the methods developed in this thesis. Although the program consists of 33 subroutines, 6 function subroutines, and over 2000 lines of code, it can be easily summarized by breaking it into the two areas of the thesis: cell aggregation and estimation methods.

The main program and aggregation subroutines (listed in paragraph B) read the input parameters and execute the expansion and aggregation methods discussed in Chapter II. An existing program written by Luis Uribe, an independent contractor under the direction of Professor Read, underwent extensive modification to fulfill these requirements. The input parameters-- T_0 , K_0 , MOS, YCS, grade, service component(s), and commissioning source(s)--are read by Subroutine GETPAR either in the interactive mode via the terminal or by using MC87 EXEC (listed in paragraph E). Uribe uses an innovative method to estimate the amount of expansion required to meet the threshold parameters. This approach precludes the requirement to read the data base after each step in the expansion process which would be extremely computer time intensive. Inventory information is extracted from the data base and stored in a separate data file for each pay grade (a sample data file and the program used to create it are listed in paragraph F). The data file is accessed via the user's A-disk which is significantly faster than accessing the data base through MVS. Subroutine READET reads the appropriate data file for the specified grade and constructs a table of cells for those records that are in the same major MOS group as the user defined MOS, and meet the service component and commissioning source parameters. All YCSs are accepted, since the extent of expansion is not yet determined. Function NCEVAL screens this table using the current level of expansion and estimates the number of aggregated cells with average inventory greater than or equal to T_0 that will be obtained. If this number is less than K_0 , Subroutine EXPAND begins the expansion stages as described in paragraph II.C.. After each increment of expansion, NCEVAL screens the table and estimates the number of aggregated cells that will be obtained. This loop through EXPAND and NCEVAL continues until the estimated number of aggregated cells meets the threshold, K_0 . The estimated number of cells and the level of expansion are then displayed on the terminal screen.

The user may elect to go forth and read the data base to determine the actual number of aggregated cells obtained, or may elect to change the level of expansion.

The level of expansion is changed through the variable AGGPCT. This variable estimates the effectiveness of the heuristic aggregation method listed in Appendix A. To estimate the number of aggregated cells that will be obtained, NCEVAL compares the cells which meet the expansion criteria to the minimum inventory threshold, T_0 . Those that are greater than T_0 will obviously produce one aggregated cell. The inventory of those that are less than T_0 is summed. The estimated number of cells is then the total of the number of cells greater than T_0 and AGGPCT times the sum of the cell inventory below T_0 divided by T_0 . The variable AGGPCT is initially set at 0.9, but can be interactively changed via the terminal. By increasing the value of AGGPCT we can decrease the level of expansion; by decreasing the value of AGGPCT we can increase the level of expansion.

Once we decide to go forth and read the actual data base, Subroutine READER extracts records meeting the expansion criteria developed using EXPAND and NCEVAL and pools them into cells. Subroutine AGGREG aggregates these cells to meet the average inventory threshold, T_0 . The actual number of aggregated cells obtained is then compared to the threshold number of cells, K_0 . Again, the user has the option of changing the level of expansion to obtain more or fewer cells, or continuing on to the estimation process.

The first five estimation methods are called by SUBROUTINE MC87BZ (listed in paragraph C). The estimation methods are contained in separate subroutines: EBTS1, EBTS2, EBOS1, EBOS2 and EMTS (EB-empirical Bayes; EM-Efron-Morris; TS-transformed scale; OS-original scale; 1-time dependent variance; 2-time independent variance). The iterations required by the first four methods are conducted in Subroutine EBITER; the Efron-Morris iterations are conducted in Subroutine EMITER. The MOEs are then computed by Subroutines MSE and OSMOE.

If the vector method is to be used, Subroutine BKDOWN then breaks the cells out by their vector components (a vector of length three for service component; a vector of length five for commissioning source). The vector estimation method is contained in Subroutine MC87V (listed in paragraph D). Since all of its computations are unique, this subroutine is self-contained with the exception of the transformation formula, which is contained in Function FTTV.

B. MAIN PROGRAM AND AGGREGATION SUBROUTINES

C --- PROGRAM TO CONDUCT AGGREGATION AND ESTIMATION METHODS	MC800010
C	MC800020
C --- PARAMETER MXY MUST BE UPDATED TO REFLECT EXACT NO. YEARS OF DATA	MC800030
C --- PARAMETER MXP IS MAX LENGTH OF 3RD DIMENSION P-VECTOR	MC800040
C --- PARAMETER MXK IS MAX NUMBER OF AGGREGATED CELLS (MAX NO)	MC800050
PARAMETER (MXX=600, MXY=10, MXP=6, MXK=50)	MC800060
PARAMETER (NMS=81, NG=14, NLG=6, NMG=4, NYB=4, NYE=18, NYEG=4)	MC800070
C	MC800080
INTEGER ST1,ST2,LYR	MC800090
INTEGER SYCS(31), NYCS	MC800100
INTEGER SYCSG(31),SYCSL(31),SYCSM(31),NYCSG,NYCSL,NYCSM	MC800110
INTEGER SMOS(30), NMOS	MC800120
INTEGER SVCMP(5), NSC	MC800130
INTEGER SCSRC(16),NCSR	MC800140
INTEGER SGRD	MC800150
INTEGER*2 MOSGR(2,NMS), YCSB(NYE,NYB,NYEG), VYC(NYE)	MC800160
INTEGER*2 LGRP(NG), MGRP(NLG)	MC800170
REAL INV(MXX,MXY),Y(MXX,MXY), SINV(MXX,MXY),SY(MXX,MXY)	MC800180
INTEGER DATA(MXY)	MC800190
C --- ARRAYS FOR MC87BZ	MC800200
REAL XTB(MXX),VXTB(MXX),XEB(MXX),A(MXX)	MC800210
C --- ARRAYS FOR MC87V	MC800220
REAL XTBJI(MXP,MXK), DELTA(MXP,MXK), X(MXP,MXK)	MC800230
REAL XVYR(MXP,MXK), VYRINV(MXP,MXK), VYRY(MXP,MXK)	MC800240
REAL BSTAR(MXP,MXP), S(MXP,MXP), GAMMA(MXP,MXP)	MC800250
REAL XBBJ(MXP), EVAL(MXP)	MC800260
C	MC800270
INTEGER*2 PTRTBL(MXX, 2), INDX(MXX), MKG(MXX), RETTBL(MXX,3)	MC800280
INTEGER*2 PTBL(MXX, 3), BKTBL(MXX,3)	MC800290
REAL AVINV(MXX), RETINV(MXX)	MC800300
DATA MKG/MXX*0/	MC800310
C --- ASSIGN MOS TO SMALL, LARGE AND MAJOR MOS GROUP	MC800320
DATA MOSGR/013,1, 020,2, 027,2, 038,2, 039,2,	MC800330
* 005,3, 007,3, 049,3, 052,3,	MC800340
* 074,4, 079,4, 085,4, 101,4,	MC800350
* 016,5, 060,5, 064,5, 076,5, 111,5, 116,5,	MC800360
* 132,6, 134,6, 135,6, 139,6,	MC800370
* 143,7, 147,7, 150,7, 153,7, 154,7, 155,7, 170,7,	MC800380
* 149,8, 151,8,	MC800390
* 160,9, 161,9, 164,9, 166,9, 167,9, 168,9, 178,9,	MC800400
* 173,10, 174,10, 175,10, 176,10, 177,10, 179,10, 144,10,	MC800410
* 145,10, 165,10,	MC800420
* 001,11, 006,11, 012,11, 015,11, 019,11, 026,11, 037,11,	MC800430
* 048,11, 051,11, 059,11, 070,11, 075,11, 078,11, 084,11,	MC800440
* 087,11, 100,11, 110,11, 115,11, 131,11, 138,11, 217,11,	MC800450
* 172,12, 187,12, 188,12, 189,12,	MC800460
* 142,13, 146,13, 148,13, 152,13, 156,13, 163,13, 169,13,	MC800470
* 088,14 /	MC800480
DATA LGRP/1,1,4*2,3,3,4,4,5,5,5,6/	MC800490
DATA MGRP/1,1,2,2,3,4/	MC800500
C --- CREATE YCS EXPANSION BOUNDS	MC800510
DATA YCSB/1,2,3,4,5,6, 8,9,10,11,12,13,14,15,16,17,18,19,	MC800520
* 7,17*0, 20,21,22,23,24,25,12*0, 26,17*0,	MC800530
* 1,2,3,4,5, 8,9,10,11,12,13,14,15,16,17,18,19,1*0,	MC800540

* 6,7,16*0, 20,21,22,23,24,25,12*0, 26,17*0,	MC800550
* 1,2,3,4,5,6, 8,9,10,11,12,13,14,15,16,17,18,19,	MC800560
* 7,17*0, 20,21,22,23,24,25,12*0, 26,17*0,	MC800570
* 1,2,3, 6,7,8,9,10,11,12,13,14,15,16,17,18,19,1*0,	MC800580
* 4,5,16*0, 20,21,22,23,24,25,12*0, 26,17*0 /	MC800590
C --- INITIALIZE INVENTORY AND ATTRITION ARRAYS	MC800600
DO 1 I=1,MXX	MC800610
DO 2 J=1,MXY	MC800620
SINV(I,J)=0	MC800630
SY(I,J)=0	MC800640
INV(I,J)=0	MC800650
Y(I,J)=0	MC800660
2 CONTINUE	MC800670
1 CONTINUE	MC800680
C --- DEFINE FILE FOR OUTPUT	MC800690
CALL EXCMS('FILEDEF 11 DISK MC87 OUTPUT A')	MC800700
C --- FIRST/LAST YEAR OF DATA ON TAPE. UPDATE WHEN NECESSARY	MC800710
ST1=77	MC800720
NYR=MXV	MC800730
LYR=ST1+NYR-1	MC800740
C --- INITIAL VALUE FOR AGGREGATION ESTIMATION PERCENTAGE	MC800750
AGGPCT=0.9	MC800760
ICYCLE=1	MC800770
C --- GET INPUT PARAMETERS	MC800780
CALL GETPAR(AIMIN,NO,NMOS,SMOS,NYCS,SYCS,SGRD,	MC800790
* NSC,SVCMP, NCSR,SCSRC, IGR,MOSGR,NMS, ISFLAG)	MC800800
C --- MAJOR GROUP IS MG, LARGE GROUP LG, GROUP IGR, YCS BLOCK IY	MC800810
LG=LGRP(IGR)	MC800820
MG=MGRP(LG)	MC800830
WRITE(6,*) ' '	MC800840
WRITE(6,*) '---- GR,LG,MG=',IGR,LG,MG	MC800850
WRITE(6,*) ' '	MC800860
C --- READ EVALUATION TABLE. SELECT ONLY RECS PASSING SELECTION CRITERIA	MC800870
CALL READET(RETTLB,RETINV,MXX,NRET,SGRD, NSC,SVCMP, NCSR,SCSRC,	MC800880
* MG,LGRP,MGRP, MOSGR,NMS)	MC800890
5 RC=0	MC800900
IGX=IGR	MC800910
LGX=0	MC800920
MGX=0	MC800930
NYCSG=1	MC800940
SYCSG(1)=SYCS(1)	MC800950
NYCSL=1	MC800960
SYCSL(1)=SYCS(1)	MC800970
NYCSM=1	MC800980
SYCSM(1)=SYCS(1)	MC800990
NCTOT=0	MC801000
NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSG,SYCSG,RETTLB,RETINV,NRET,MXX,	MC801010
* LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC801020
C --- DO WHILE NCTOT<NO & RC=0 (EXPAND AS LONG AS NO NOT MET)	MC801030
10 IF(NC .GE. NO) THEN	MC801040
WRITE(6,*) '\$GG EVAL NC,SYCSG=',NC,(SYCSG(II),II=1,NYCSG)	MC801050
GO TO 60	MC801060
ENDIF	MC801070
IF(NYCSG.EQ.1) THEN	MC801080
CALL GETVYC(SYCS(1),LG,YCSB,NYE,NYB,NYEG,VYC)	MC801090
WRITE(6,*) '== VYC=',(VYC(I),I=1,NYE)	MC801100

	ENDIF	MC801110
	CALL EXPAND(NYCSG,SYCSG,VYC,NYE,IGX,LGX,MGX,LG,MG,RC)	MC801120
	IF(IGX.EQ. 0) GO TO 20	MC801130
	NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSG,SYCSG,RETTBL,RETINV,NRET,MXX,	MC801140
	* LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC801150
	GO TO 10	MC801160
20	NCTOT=NC	MC801170
	WRITE(6,*) '\$\$G EVAL NC,SYCSG=',NCTOT,(SYCSG(II),II=1,NYCSG)	MC801180
C		MC801190
C ---	EXPAND TO LARGE MOS GROUP	MC801200
	WRITE(6,*) ' '	MC801210
	WRITE(6,*) '== EXPANDING BY LARGE GROUP: ',LGX	MC801220
	NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSL,SYCSL,RETTBL,RETINV,NRET,MXX,	MC801230
	* LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC801240
30	IF((NCTOT+NC).GE. NO) THEN	MC801250
	WRITE(6,*) '\$LL EVAL NC,SYCSL=',(NCTOT+NC),(SYCSL(II),II=1,NYCSL)	MC801260
	GO TO 60	MC801270
	ENDIF	MC801280
	IF(NYCSL.EQ. 1) CALL GETVYC(SYCS(1),LG,YCSB,NYE,NYB,NYEG,VYC)	MC801290
	CALL EXPAND(NYCSL,SYCSL,VYC,NYE,IGX,LGX,MGX,LG,MG,RC)	MC801300
	IF(LGX.EQ. 0) GO TO 40	MC801310
	NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSL,SYCSL,RETTBL,RETINV,NRET,MXX,	MC801320
	* LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC801330
	GO TO 30	MC801340
40	NCTOT=NCTOT+NC	MC801350
	WRITE(6,*) '\$\$L EVAL NC,SYCSL=',NCTOT,(SYCSL(II),II=1,NYCSL)	MC801360
C		MC801370
C ---	EXPAND TO MAJOR MOS GROUP	MC801380
	WRITE(6,*) ' '	MC801390
	WRITE(6,*) '== EXPANDING BY MAJOR GROUP: ',MGX	MC801400
	NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSM,SYCSM,RETTBL,RETINV,NRET,MXX,	MC801410
	* LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC801420
50	IF((NCTOT+NC).GE. NO .OR. RC.NE. 0) THEN	MC801430
	WRITE(6,*) '\$MM EVAL NC,SYCSM=',(NC+NCTOT),(SYCSM(II),II=1,NYCSM)	MC801440
	GO TO 60	MC801450
	ENDIF	MC801460
	IF(NYCSM.EQ. 1) CALL GETVYC(SYCS(1),LG,YCSB,NYE,NYB,NYEG,VYC)	MC801470
	CALL EXPAND(NYCSM,SYCSM,VYC,NYE,IGX,LGX,MGX,LG,MG,RC)	MC801480
	NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSM,SYCSM,RETTBL,RETINV,NRET,MXX,	MC801490
	* LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC801500
	GO TO 50	MC801510
C		MC801520
C ---	EXPANSION FINISHED	MC801530
60	IF(RC.NE. 0) THEN	MC801540
	WRITE(5,*) '*** REQUIRED NO MAY NOT BE MET: NO,NC=',NO,(NC+NCTOT)	MC801550
	ENDIF	MC801560
C ---	ALLOW USER TO CHANGE EXPANSION LEVEL	MC801570
	WRITE(5,*) 'ESTIMATED NUMBER OF CELLS = ',NC+NCTOT	MC801580
70	WRITE(5,*)	MC801590
	WRITE(5,*) 'ENTER 1 TO CALL READER, 0 TO CHANGE EXPANSION'	MC801600
	READ(5,*) NPICK1	MC801610
	IF(NPICK1.EQ. 1) THEN	MC801620
	GO TO 80	MC801630
	ELSE	MC801640
	WRITE(5,*) 'AGGPCT IS CURRENTLY = ', AGGPCT	MC801650
	WRITE(5,*) 'ENTER NEW VALUE FOR AGGPCT'	MC801660

READ(5,*) AGGPCT	MC801670
GO TO 5	MC801680
ENDIF	MC801690
80 WRITE(5,*) 'CALLING READER'	MC801700
C	MC801710
C --- USER ELECTS TO READ THE DATA BASE - DETERMINE MOS EXPANSION LEVEL	MC801720
CALL GETMOS(SMOS,NMOS,MGX,LGX,MG,LG,IGR,MOSGR,LGRP,MGRP,	MC801730
* NMS,NG,NLG)	MC801740
C --- READ THE DATA BASE AND CREATE THE CELLS	MC801750
CALL READER(DATA,INV,Y,MXX,NMOS,NYCSG,NYCSL,NYCSM,NSC,NCSR,NYR,	MC801760
* SMOS,SYCSG,SYCSL,SYCSM,SGRD,SVCMP,SCSRC,NRC,PTRTBL,LGX,MGX,IGR,	MC801770
* LG,MGRP,LGRP,MOSGR,NMS,NG,NLG,ICYCLE,NPT,PTBL,ISFLAG,SINV,SY)	MC801780
C --- PERFORM CELL AGGREGATION TO MEET INVENTORY THRESHOLD	MC801790
CALL AGGREG(INV,Y,MXX,NYR,SMOS,SYCSG,	MC801800
* NRC,NRCOLD,PTRTBL,INDX,AVINV,AIMIN,MKG)	MC801810
C --- ALLOW USER TO CHANGE EXPANSION LEVEL	MC801820
WRITE(5,*) 'NUMBER OF CELLS =' ,NRC	MC801830
90 WRITE(5,*)	MC801840
WRITE(5,*) 'ENTER 1 TO CONTINUE, 0 TO CHANGE EXPANSION'	MC801850
READ(5,*) NPICK2	MC801860
IF(NPICK2.EQ. 1) THEN	MC801870
GO TO 100	MC801880
ELSE	MC801890
WRITE(5,*) 'AGGPCT IS CURRENTLY =' , AGGPCT	MC801900
WRITE(5,*) 'ENTER NEW VALUE FOR AGGPCT'	MC801910
READ(5,*) AGGPCT	MC801920
ICYCLE=ICYCLE+1	MC801930
GO TO 5	MC801940
ENDIF	MC801950
C	MC801960
C --- USER ELECTS TO CONDUCT ESTIMATION	MC801970
100 CONTINUE	MC801980
WRITE(11,201)'EXPANSION INFORMATION: '	MC801990
WRITE(11,203)'ACTUAL NO. OF CELLS USED= ' ,NRC	MC802000
WRITE(11,202)'MOS GROUP #' ,IGR,' YCS' 'S USED= ',	MC802010
* (SYCSG(I),I=1,NYCSG)	MC802020
IF(LGX.GT. 0) THEN	MC802030
WRITE(11,204)'LARGE MOS GROUP #' ,LG,' YCS' 'S USED= ',	MC802040
* (SYCSL(I),I=1,NYCSL)	MC802050
ELSE IF(MGX.GT. 0) THEN	MC802060
WRITE(11,204)'LARGE MOS GROUP #' ,LG,' YCS' 'S USED= ',	MC802070
* (SYCSL(I),I=1,NYCSL)	MC802080
WRITE(11,204)'MAJOR MOS GROUP #' ,MG,' YCS' 'S USED= ',	MC802090
* (SYCSM(I),I=1,NYCSM)	MC802100
ENDIF	MC802110
C --- PERFORM ALL BUT VECTOR ESTIMATION METHODS IN MC87BZ	MC802120
CALL MC87BZ(INV,Y,NRC,NYR,XTB,VXTB,XEB,A,MXX,MXY)	MC802130
C --- VECTOR METHOD--BREAK CELLS INTO VECTOR, CONDUCT ESTIMATION	MC802140
IF(ISFLAG.GT. 0) THEN	MC802150
CALL BKDOWN(PTBL,NPT,PTRTBL,NRCOLD,INDX,MKG,MXX,MXY,	MC802160
* SINV,SY,INV,Y,BKTBL,NBK)	MC802170
CALL MC87V(INV,Y,MXX,NYR,NRC,XTBJI,DELTA,X,XVYR,VYRINV,VYRY,	MC802180
* BSTAR,S,GAMMA,XBBJ,EVAL,MXP,MXK,BKTBL,NBK,NSC,NCSR,ISFLAG)	MC802190
ENDIF	MC802200
C	MC802210
201 FORMAT(/1X,A)	MC802220

202	FORMAT(1X,A,I2,A/1X,18(I3))	MC802230
203	FORMAT(1X,A,I2)	MC802240
204	FORMAT(1X,A,I1,A/1X,18(I3))	MC802250
	END	MC802260
C		MC802270
	*****	MC802280
C		MC802290
	SUBROUTINE EXPAND(NYCSX,SYCSX,VYC,NYE,IGX,LGX,MGX,LG,MG,RC)	MC802300
C ---	EXPAND YCS IF FEASIBLE, ELSE EXPAND MOS TO LG/MG	MC802310
	INTEGER SYCSX(31), NYCSX	MC802320
	INTEGER*2 VYC(NYE)	MC802330
C ---	FIND POSITION OF ORIGINALLY REQUESTED SYCS(1)	MC802340
	IY=0	MC802350
	DO 10 I=1,NYE	MC802360
	IF(SYCSX(1) .EQ. VYC(I)) IY=I	MC802370
10	CONTINUE	MC802380
	IF(IY.EQ.0) GO TO 30	MC802390
C ---	FIND NEAREST NON-ZERO YCS TO USE FOR EXPANSION	MC802400
	DO 20 I=1,NYE	MC802410
	J=IY-I	MC802420
	IF(J.GE.1) THEN	MC802430
	IF(VYC(J).GT.0) GO TO 50	MC802440
	ENDIF	MC802450
	J=IY+I	MC802460
	IF(J.LE.NYE) THEN	MC802470
	IF(VYC(J).GT.0) GO TO 50	MC802480
	ENDIF	MC802490
20	CONTINUE	MC802500
30	CONTINUE	MC802510
C ---	NO MORE YCS EXPANSION POSSIBLE. SEE IF MOS EXP. FEASIBLE	MC802520
	IF(IGX.GT.0) THEN	MC802530
C ---	EXPAND FROM GROUPS TO LARGE GROUP LGX	MC802540
	IGX=0	MC802550
	LGX=LG	MC802560
	ELSE IF(LGX.GT.0) THEN	MC802570
C ---	EXPAND FROM LARGE GROUP LGX TO MAJOR GROUP MGX	MC802580
	LGX=0	MC802590
	MGX=MG	MC802600
	ELSE	MC802610
	RC=1	MC802620
	ENDIF	MC802630
	RETURN	MC802640
C		MC802650
C ---	EXPAND WITH YCS IN POSITION J & CLEAR VYC(J)	MC802660
50	CONTINUE	MC802670
	NYCSX=NYCSX+1	MC802680
	SYCSX(NYCSX)=VYC(J)	MC802690
	VYC(J)=0	MC802700
	END	MC802710
C		MC802720
	*****	MC802730
C		MC802740
	FUNCTION NCEVAL(AIMIN,IGX,LGX,MGX,NYCSX,SYCSX,RETTBL,RETINV,	MC802750
*	NRET,MXX,LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC802760
C ---	COMPUTE ESTIMATED NO. CELLS TO BE OBTAINED WITH CURRENT EXPANSION	MC802770
	INTEGER SYCSX(31),NYCSX	MC802780

	INTEGER*2 LGRP(14),MGRP(6)	MC802790
	INTEGER*2 RETTBL(MXX, 3)	MC802800
	REAL RETINV(MXX)	MC802810
	NCEVAL=0	MC802820
	IF(IGX.EQ.0 .AND. LGX.EQ.0 .AND. MGX.EQ.0) RETURN	MC802830
	TAINV=0.0	MC802840
	DO 100 I=1,NRET	MC802850
C ---	SCREEN ON YCS	MC802860
	DO 10 J=1,NYCSX	MC802870
	IF(RETTBL(I,2) .EQ. SYCSX(J)) GO TO 15	MC802880
10	CONTINUE	MC802890
	GO TO 100	MC802900
C ---	SCREEN ON MOS BY GROUP, L.GRP OR MG DEPENDING ON IGX,LGX,MGX	MC802910
15	CONTINUE	MC802920
	MOS=RETTBL(I,1)	MC802930
	IGP=RETTBL(I,3)	MC802940
	LGP=LGRP(IGP)	MC802950
	IF(MGX .GT. 0) THEN	MC802960
	IF(MGRP(LGP) .EQ. MGX) THEN	MC802970
	IF(LGP .NE. LG) GO TO 80	MC802980
	ENDIF	MC802990
	ELSE IF(LGX .GT. 0) THEN	MC803000
	IF(LGP .EQ. LGX) THEN	MC803010
	IF(IGP .NE. IGR) GO TO 80	MC803020
	ENDIF	MC803030
	ELSE	MC803040
	IF(IGP .EQ. IGX) GO TO 80	MC803050
	ENDIF	MC803060
	GO TO 100	MC803070
80	CONTINUE	MC803080
C ---	ACCEPTED	MC803090
	IF(RETINV(I) .GE. AIMIN) THEN	MC803100
	NCEVAL=NCEVAL+1	MC803110
	ELSE	MC803120
	TAINV=TAINV+RETINV(I)	MC803130
	ENDIF	MC803140
100	CONTINUE	MC803150
C ---	FINAL ESTIMATE IS NCEVAL	MC803160
	IF(AIMIN.GT.0) NCEVAL=NCEVAL + AGGPCT*TAINV/AIMIN	MC803170
	END	MC803180
C		MC803190
	*****	MC803200
C		MC803210
	SUBROUTINE GETVYC(SYCS, LG, YCSB,NYE,NYB,NYEG, VYC)	MC803220
	INTEGER*2 YCSB(NYE,NYB,NYEG), VYC(NYE), LGEX(6)	MC803230
	INIEGER SYCS	MC803240
	DATA LGEX/4,4,1,2,4,3/	MC803250
C ---	L INDICATES LAST DIMENSION IN YCS EXPANSION TABLE	MC803260
	L=LGEX(LG)	MC803270
C ---	FIND TO WHICH YCS BLOCK SYCS BELONGS AND MAKE COPY IN VYC	MC803280
	DO 10 J=1,NYB	MC803290
	DO 20 I=1,NYE	MC803300
	IF(SYCS .EQ. YCSB(I,J,L)) THEN	MC803310
	DO 30 K=1,NYE	MC803320
	VYC(K)=YCSB(K,J,L)	MC803330
30	CONTINUE	MC803340

	RETURN	MC803350
	ENDIF	MC803360
20	CONTINUE	MC803370
10	CONTINUE	MC803380
	WRITE(6,*) '***** YCS NOT FOUND IN YCSB TABLE YCS=',SYCS	MC803390
	END	MC803400
C		MC803410
	*****	MC803420
C		MC803430
	SUBROUTINE READET(RETTL,RETINV,MXX,NRET, SGRD, NSC,SVCMP,	MC803440
	* NCSR,SCSRC, MG,LGRP,MGRP, MOSGR,NMS)	MC803450
C ---	READ TABLE WITH ALL EXISTING COMBINATIONS FOR SELECTION CRITERIA	MC803460
C ---	ACCEPT RECS WITH MATCHING PG,MG,CS,SVC. ACCEPT ALL YCS	MC803470
	INTEGER SVCMP(5), NSC, SVC	MC803480
	INTEGER SCSRC(16),NCSR, CS	MC803490
	INTEGER SGRD, PG	MC803500
	INTEGER MOS,YCS	MC803510
	INTEGER*2 MOSGR(2,NMS), MGRP(*),LGRP(*)	MC803520
	INTEGER*2 RETTL(MXX, 3)	MC803530
	REAL RETINV(MXX), AI	MC803540
	NRET=0	MC803550
	DO 10 I=1,999999	MC803560
	READ(10+SGRD,100,END=999) PG,MOS,YCS,SVC,CS, NRECS,AI	MC803570
	IF(PG .NE. SGRD) GO TO 10	MC803580
	IGR=IGFIND(MOS, MOSGR,NMS)	MC803590
	LG=LGRP(IGR)	MC803600
	IF(MGRP(LG) .NE. MG) GO TO 10	MC803610
	DO 20 J=1,NSC	MC803620
	IF(SVC .EQ. SVCMP(J)) GO TO 21	MC803630
20	CONTINUE	MC803640
	GO TO 10	MC803650
21	CONTINUE	MC803660
	DO 30 J=1,NCSR	MC803670
	IF(CS .EQ. SCSRC(J)) THEN	MC803680
	CALL ACCEPT(MOS,YCS,IGR,RETTL,MXX,NRET,RETINV,AI)	MC803690
	GO TO 10	MC803700
	ENDIF	MC803710
30	CONTINUE	MC803720
C		MC803730
10	CONTINUE	MC803740
999	CONTINUE	MC803750
	IF(NRET .GT. MXX) THEN	MC803760
	WRITE(6,*) '***** ERROR - TOO MANY RECORDS IN RETTL'	MC803770
	STOP	MC803780
	ENDIF	MC803790
100	FORMAT(I2,I4,I3,I2,I3,I4,F7.2)	MC803800
	END	MC803810
C		MC803820
	*****	MC803830
C		MC803840
	SUBROUTINE ACCEPT(MOS,YCS,IGR, RETTL,MXX,NRET,RETINV,AI)	MC803850
C ---	ACCEPT ENTRY. ACCUMULATE IF ALREADY SAME COMBINATION IS PRESENT	MC803860
	INTEGER MOS,YCS	MC803870
	INTEGER*2 RETTL(MXX, 3)	MC803880
	REAL RETINV(MXX), AI	MC803890
	DO 10 I=1,NRET	MC803900

IF(MOS.EQ.RETTBL(I,1) .AND. YCS.EQ.RETTBL(I,2)) THEN	MC803910
RETINV(I)=RETINV(I) + AI	MC803920
RETURN	MC803930
ENDIF	MC803940
10 CONTINUE	MC803950
C --- NEW COMBINATION	MC803960
NRET=NRET+1	MC803970
RETTBL(NRET,1)=MOS	MC803980
RETTBL(NRET,2)=YCS	MC803990
RETTBL(NRET,3)=IGR	MC804000
RETINV(NRET)=AI	MC804010
END	MC804020
C	MC804030
*****	MC804040
C	MC804050
SUBROUTINE GETPAR(AIMIN,NO,NMOS,SMOS,NYCS,SYCS,SGRD,	MC804060
* NSC,SVCMP, NCSR,SCSRC, IGR,MOSGR,NMS, ISFLAG)	MC804070
C --- GET SELECTION CRITERIA FROM USER AND VALIDATE	MC804080
INTEGER SYCS(31), NYCS	MC804090
INTEGER SMOS(20), NMOS	MC804100
INTEGER SVCMP(5), NSC	MC804110
INTEGER SCSRC(16),NCSR	MC804120
INTEGER SGRD	MC804130
INTEGER*2 MOSGR(2,NMS)	MC804140
WRITE(5,*) ' ENTER THRESHOLD MIN. FOR AVERAGE INVENTORY'	MC804150
READ(5,*) AIMIN	MC804160
WRITE(5,*) ' ENTER THRESHOLD MIN. FOR NUMBER OF CELLS'	MC804170
READ(5,*) NO	MC804180
WRITE(5,*) ' THRESHOLDS TO USE AIMIN, NO= ',AIMIN,NO	MC804190
C	MC804200
WRITE(5,*) ' ENTER MOS (ONLY 1 ACCEPTED)'	MC804210
NMOS=1	MC804220
READ(5,*) SMOS(1)	MC804230
WRITE(6,*) ' MOS SELECTED: ', SMOS(1)	MC804240
IGR=IGFIND(SMOS(1), MOSGR,NMS)	MC804250
WRITE(6,*) ' GROUP TO USE: ', IGR	MC804260
IF(IGR.EQ.0) THEN	MC804270
WRITE(5,*) '***** ERROR - INVALID MOS SELECTED: ',SMOS(1)	MC804280
STOP	MC804290
ENDIF	MC804300
C	MC804310
WRITE(5,*) ' ENTER YCS (ONLY 1 ACCEPTED)'	MC804320
NYCS=1	MC804330
READ(5,*) SYCS(1)	MC804340
WRITE(6,*) ' YCS SELECTED: ', SYCS(1)	MC804350
C	MC804360
WRITE(5,*) ' ENTER GRADE'	MC804370
READ(5,*) SGRD	MC804380
WRITE(6,*) ' GRADE SELECTED', SGRD	MC804390
C	MC804400
WRITE(5,*) ' ENTER NO. OF SVC. COMPS & ARRAY (1-3, 4=1+2, 5=ALL)'	MC804410
READ(5,*) NSC, (SVCMP(I), I=1,NSC)	MC804420
C --- EXPAND 4 TO 1,2 AND 5 TO 1,2,3	MC804430
DO 10 I=1,NSC	MC804440
IF(SVCMP(I).EQ.4 .OR. SVCMP(I).EQ.5) THEN	MC804450
NSC=SVCMP(I)-2	MC804460

DO 15 J=1,NSC	MC804470
SVCMP(J)=J	MC804480
15 CONTINUE	MC804490
GO TO 11	MC804500
ENDIF	MC804510
10 CONTINUE	MC804520
11 CONTINUE	MC804530
WRITE(6,*) ' SERVICE COMPONENTS SELECTED', (SVCMP(I), I=1,NSC)	MC804540
C	MC804550
WRITE(5,*) ' ENTER NO. COMM. SOURCES AND ARRAY (1-15, 16=ALL)'	MC804560
READ(5,*) NCSR, (SCSRC(I), I=1,NCSR)	MC804570
C --- IF 16 IS SELECTED THEN EXPAND ARRAY TO COVER ALL 1-15	MC804580
DO 20 I=1,NCSR	MC804590
IF(SCSRC(I) .EQ. 16) THEN	MC804600
NCSR=15	MC804610
DO 25 J=1,NCSR	MC804620
SCSRC(J)=J	MC804630
25 CONTINUE	MC804640
GO TO 26	MC804650
ENDIF	MC804660
20 CONTINUE	MC804670
26 CONTINUE	MC804680
WRITE(5,*) ' COMM. SOURCES SELECTED:', (SCSRC(I), I=1,NCSR)	MC804690
C	MC804700
C --- FLAG TO DETERMINE WHICH OF SVC OR CS WILL BE USED AS 3RD DIMENSION	MC804710
WRITE(5,*) 'SELECT 3RD DIM. TO USE: 0=NONE, 1=SVC, 2=COMM. SOURCE'	MC804720
READ(5,*) ISFLAG	MC804730
C --- WRITE INPUT PARAMETER INFO TO OUTPUT FILE	MC804740
WRITE(11,101) 'TEST CASE INPUT PARAMETERS: '	MC804750
WRITE(11,102) 'INVENTORY THRESHOLD= ',AIMIN,	MC804760
* 'THRESHOLD NO. OF CELLS= ',NO	MC804770
WRITE(11,103) 'MOS= ',SMOS(1),'YCS= ',SYCS(1),'GRADE= ',SGRD	MC804780
WRITE(11,104) 'SERVICE COMPONENTS= ',(SVCMP(I),I=1,NSC)	MC804790
WRITE(11,104) 'COMM SOURCES= ',(SCSRC(I),I=1,NCSR)	MC804800
WRITE(6,*) '3RD DIMENSION= ',ISFLAG	MC804810
C	MC804820
101 FORMAT(1X,A)	MC804830
102 FORMAT(1X,A,F4.1,7X,A,I2)	MC804840
103 FORMAT(1X,A,I3,2(5X,A,I2))	MC804850
104 FORMAT(1X,A,15(I3))	MC804860
END	MC804870
C	MC804880
*****	MC804890
C	MC804900
SUBROUTINE GETMOS(SMOS,NMOS,MGX,LGX,MG,LG,IGR,MOSGR,LGRP,MGRP,	MC804910
* NMS,NG,NLG)	MC804920
C --- BUILD SMOS ARRAY BASED UPON EXPANSION	MC804930
INTEGER SMOS(30)	MC804940
INTEGER*2 MOSGR(2,NMS), LGRP(NG), MGRP(NLG)	MC804950
NMOS=0	MC804960
IF(MGX .GT. 0) THEN	MC804970
C --- HAVE EXPANDED TO MAJOR MOS GROUP	MC804980
DO 10 I=1,NMS	MC804990
IGP=MOSGR(2,I)	MC805000
LGP=LGRP(IGP)	MC805010
IF(MGRP(LGP) .EQ. MG) THEN	MC805020

	NMOS=NMOS+1	MC805030
	SMOS(NMOS)=MOSGR(1,I)	MC805040
	ENDIF	MC805050
10	CONTINUE	MC805060
	RETURN	MC805070
	ELSE IF(LGX .GT. 0) THEN	MC805080
C ---	HAVE EXPANDED TO LARGE MOS GROUP	MC805090
	DO 20 I=1,NMS	MC805100
	IGP=MOSGR(2,I)	MC805110
	IF(LGRP(IGP) .EQ. LG) THEN	MC805120
	NMOS=NMOS+1	MC805130
	SMOS(NMOS)=MOSGR(1,I)	MC805140
	ENDIF	MC805150
20	CONTINUE	MC805160
	RETURN	MC805170
	ELSE	MC805180
C ---	HAVE EXPANDED TO SMALL MOS GROUP	MC805190
	DO 30 I=1,NMS	MC805200
	IF(MOSGR(2,I) .EQ. IGR) THEN	MC805210
	NMOS=NMOS+1	MC805220
	SMOS(NMOS)=MOSGR(1,I)	MC805230
	ENDIF	MC805240
30	CONTINUE	MC805250
	RETURN	MC805260
	ENDIF	MC805270
	END	MC805280
C		MC805290
*****		MC805300
C		MC805310
	FUNCTION IGFIND(MOS, MOSGR,NMS)	MC805320
C ---	FIND LOCATION OF MATCHING MOS IN GROUP TABLE. RETURN GROUP NO	MC805330
	INTEGER*2 MOSGR(2,NMS)	MC805340
	DO 10 I=1,NMS	MC805350
	IF(MOSGR(1,I) .EQ. MOS) THEN	MC805360
		MC805370
	IGFIND=MOSGR(2,I)	MC805380
	RETURN	MC805390
	ENDIF	MC805400
10	CONTINUE	MC805410
	IGFIND=0	MC805420
	END	MC805430
C		MC805440
*****		MC805450
C		MC805460
	SUBROUTINE READER(DATA,INV,Y,MXX,NMOS,NYCSG,NYCSL,NYCSM,NSC,NCSR,	MC805470
	* NYR,SMOS,SYCSG,SYCSL,SYCSM,SGRD,SVCMP,SCSRC,NRC,PTRTBL,LGX,MGX,	MC805480
	* IGR,LG,MGRP,LGRP,MOSGR,NMS,NG,NLG,ICYCLE,NPT,PTBL,ISFLAG,SINV,SY)	MC805490
	REAL INV(MXX,NYR),Y(MXX,NYR), SINV(MXX,NYR),SY(MXX,NYR)	MC805500
	INTEGER*2 PTRTBL(MXX, 2), PTBL(MXX,3)	MC805510
	INTEGER SYCSG(*), SYCSL(*), SYCSM(*)	MC805520
	INTEGER SMOS(*), NMOS	MC805530
	INTEGER SVCMP(*), NSC	MC805540
	INTEGER SCSRC(*),NCSR	MC805550
	INTEGER SGRD	MC805560
	INTEGER TYPE,YCS,PG,MOS,SFX,CS,EDLV,SVC,MOS1,MOS2,RACE	MC805570
	INTEGER DATA(NYR)	MC805580
	CHARACTER*7 CITLS	

INTEGER*2 MOSGR(2,NMS),LGRP(NG),MGRP(NLG)	MC805590
C	MC805600
C --- REWIND DATA FILE AND RESET INV,Y IF CYCLING THRU READER	MC805610
IF(ICYCLE.GT. 1) THEN	MC805620
REWIND 1	MC805630
DO 6 I=1,MXX	MC805640
DO 5 J=1,NYR	MC805650
INV(I,J)=0.0	MC805660
Y(I,J)=0.0	MC805670
SINV(I,J)=0.0	MC805680
SY(I,J)=0.0	MC805690
5 CONTINUE	MC805700
6 CONTINUE	MC805710
ENDIF	MC805720
C --- READ RECORD AND STORE IN MATRIX	MC805730
ICR=0	MC805740
NRC=0	MC805750
NPT=0	MC805760
ICNT=0	MC805770
IYNO=0	MC805780
IYR=0	MC805790
C	MC805800
1 READ(1,101,END=999) TYPE,YCS,PG,MOS,SEX,CS,EDLV,SVC,MOS1,MOS2,	MC805810
* RACE,CITLS,DATA	MC805820
ICR=ICR+1	MC805830
C --- CHECK IF RECORD MEETS SELECTION CRITERIA. OTHERWISE REJECT.	MC805840
C --- COLLECT TYPES 0=INVENTORY, AND 1-5 ALL LOSSES	MC805850
IF(TYPE.GT.5) GO TO 999	MC805860
C	MC805870
C --- SCREEN FOR GRADE	MC805880
IF(PG.NE. SGRD) GO TO 1	MC805890
C	MC805900
C --- SCREEN FOR MOS	MC805910
IGP=IGFIND(MOS,MOSGR,NMS)	MC805920
IF(IGP.EQ.0) GO TO 1	MC805930
LGP=LGRP(IGP)	MC805940
IF(MGX.GT. 0) THEN	MC805950
C --- HAVE EXPANDED TO MAJOR MOS GROUP	MC805960
IF(LGP.EQ. LG) THEN	MC805970
DO 10 I=1,NYCSL	MC805980
IF(YCS.EQ. SYCSL(I)) THEN	MC805990
IY=I	MC806000
GO TO 60	MC806010
ENDIF	MC806020
10 CONTINUE	MC806030
GO TO 1	MC806040
ELSE IF(MGRP(LGP).EQ. MGX) THEN	MC806050
DO 20 I=1,NYCSM	MC806060
IF(YCS.EQ. SYCSM(I)) THEN	MC806070
IY=I	MC806080
GO TO 60	MC806090
ENDIF	MC806100
20 CONTINUE	MC806110
GO TO 1	MC806120
ELSE	MC806130
GO TO 1	MC806140

ENDIF	MC806150
ELSE IF(LGX .GT. 0) THEN	MC806160
C --- HAVE EXPANDED TO LARGE MOS GROUP	MC806170
IF(IGP .EQ. IGR) THEN	MC806180
DO 30 I=1,NYCSG	MC806190
IF(YCS .EQ. SYCSG(I)) THEN	MC806200
IY=I	MC806210
GO TO 60	MC806220
ENDIF	MC806230
30 CONTINUE	MC806240
GO TO 1	MC806250
ELSE IF(LGP .EQ. LGX) THEN	MC806260
DO 40 I=1,NYCSL	MC806270
IF(YCS .EQ. SYCSL(I)) THEN	MC806280
IY=I	MC806290
GO TO 60	MC806300
ENDIF	MC806310
40 CONTINUE	MC806320
GO TO 1	MC806330
ELSE	MC806340
GO TO 1	MC806350
ENDIF	MC806360
ELSE	MC806370
C --- HAVE EXPANDED TO SMALL MOS GROUP	MC806380
IF(IGP .EQ. IGR) THEN	MC806390
DO 50 I=1,NYCSG	MC806400
IF(YCS .EQ. SYCSG(I)) THEN	MC806410
IY=I	MC806420
GO TO 60	MC806430
ENDIF	MC806440
50 CONTINUE	MC806450
GO TO 1	MC806460
ELSE	MC806470
GO TO 1	MC806480
ENDIF	MC806490
ENDIF	MC806500
60 CONTINUE	MC806510
C	MC806520
DO 70 I=1,NMOS	MC806530
IF(MOS .EQ. SMOS(I)) THEN	MC806540
IM=I	MC806550
GO TO 80	MC806560
ENDIF	MC806570
70 CONTINUE	MC806580
WRITE(6,*) '*** ERROR IN MOS SCREENING ***',MOS	MC806590
WRITE(6,*) 'NMOS,SMOS=',NMOS,(SMOS(I),I=1,NMOS)	MC806600
GO TO 1	MC806610
C	MC806620
C --- SCREEN FOR SERVICE COMPONENT	MC806630
80 CONTINUE	MC806640
DO 90 I=1,NSC	MC806650
IF(SVC .EQ. SVCMP(I)) THEN	MC806660
IS=I	MC806670
GO TO 100	MC806680
END IF	MC806690
90 CONTINUE	MC806700

GO TO 1	MC806710
C	MC806720
C --- SCREEN FOR COMMISSIONING SOURCE	MC806730
100 CONTINUE	MC806740
DO 110 I=1,NCSR	MC806750
IF(CS .EQ. SCSRC(I)) THEN	MC806760
IR=I	MC806770
GO TO 120	MC806780
END IF	MC806790
110 CONTINUE	MC806800
GO TO 1	MC806810
C	MC806820
120 CONTINUE	MC806830
C	MC806840
C --- RECORD ACCEPTED - INSTALL IT IN INV,Y,SINV,SY, PTRTBL AND PTBL	MC806850
ICNT=ICNT+1	MC806860
IF(ISFLAG.EQ. 1) THEN	MC806870
IW=IS	MC806880
ELSE IF(ISFLAG.EQ. 2) THEN	MC806890
IW=IR	MC806900
ELSE	MC806910
IW=-99	MC806920
ENDIF	MC806930
MINV=GINV(PTRTBL, MXX,NRC, IM,IY,-99)	MC806940
MV=GINV(PTBL, MXX,NPT,IM,IY,IW)	MC806950
IF(TYPE.EQ. 0) THEN	MC806960
CALL INSINV(PTRTBL,MXX,NYR,NRC,MINV,IM,IY,-99,INV,DATA)	MC806970
CALL INSINV(PTBL, MXX,NYR,NPT,MV, IM,IY, IW,SINV,DATA)	MC806980
ELSE	MC806990
CALL INSY(MXX,NYR,MINV,Y,DATA)	MC807000
CALL INSY(MXX,NYR,MV, SY,DATA)	MC807010
IYR=IYR+1	MC807020
IF(MINV.EQ. 0) THEN	MC807030
WRITE(6,*) '*** ERROR IN DATA BASE. LOSS W/O INV. REC. '	MC807040
WRITE(6,122) 'Y**:', MOS,YCS,PG,EDLV,SVC,RACE,	MC807050
(DATA(IT), IT=1,NYR)	MC807060
* IYNO=IYNO+1	MC807070
ENDIF	MC807080
ENDIF	MC807090
C	MC807100
GO TO 1	MC807110
C	MC807120
999 CONTINUE	MC807130
WRITE(6,*) ' '	MC807140
WRITE(6,*) 'TOTAL RECORDS READ =',ICR	MC807150
WRITE(6,*) 'TOTAL INV. MOS/YCS COMBINATIONS=',NRC	MC807160
WRITE(6,*) 'TOTAL INV. MOS/YCS/IW COMBINATIONS=',NPT	MC807170
WRITE(6,*) 'TOTAL RECORDS ACCEPTED =',ICNT	MC807180
WRITE(6,*) 'TOTAL LOSS RECORDS ACCEPTED =',IYR	MC807190
WRITE(6,*) 'TOTAL LOSS RECORDS NOT MATCHED =',IYNO	MC807200
C --- TERMINATE IF NO DATA COLLECTED	MC807210
IF(NRC .EQ. 0) THEN	MC807220
WRITE(6,*) '***** NO DATA MEETS SELECTION REQS'	MC807230
STOP	MC807240
ENDIF	MC807250
C	MC807260

101	FORMAT(3I2,I3,I1,I2,2I1,2I3,I1,A7, 1X, 10I4)	MC807270
121	FORMAT(A8,13I6)	MC807280
122	FORMAT(A8,7I6, 5X, 12I6)	MC807290
131	FORMAT(I4, 2I6)	MC807300
132	FORMAT(I4, 3I6, 10F7.2)	MC807310
	END	MC807320
C		MC807330
*****		MC807340
C		MC807350
	FUNCTION GINV(P_TBL, MXX,NPT, IM,IY,IW)	MC807360
C ---	FIND LOCATION OF INVENTORY ENTRY FOR MOS,YCS,SVC/CS COMBINATIONS	MC807370
C ---	3RD DIMENSION CHECKED ONLY IN CASE IW>0	MC807380
	INTEGER*2 P_TBL(MXX, *)	MC807390
	DO 10 I=1,NPT	MC807400
	IF(P_TBL(I, 1) .EQ. IM .AND.	MC807410
*	P_TBL(I, 2) .EQ. IY) THEN	MC807420
	IF(IW.LT.0 .OR. (IW.GT.0 .AND. P_TBL(I, 3).EQ.IW)) THEN	MC807430
	GINV=I	MC807440
	RETURN	MC807450
	ENDIF	MC807460
	ENDIF	MC807470
10	CONTINUE	MC807480
	GINV=0	MC807490
	END	MC807500
C		MC807510
*****		MC807520
C		MC807530
	SUBROUTINE INSINV(PT,MXX,NYR,N,K,IM,IY,IW,INV,DATA)	MC807540
C ---	ACCUMM INTO KTH ENTRY. INSTALL IN POINTER TABLE IF NOT PRESENT	MC807550
	REAL INV(MXX, NYR)	MC807560
	INTEGER*2 PT(MXX, *)	MC807570
	INTEGER DATA(NYR)	MC807580
	IF(K .EQ. 0) THEN	MC807590
C ---	ADD NEW ENTRY	MC807600
	N=N+1	MC807610
	IF(N .GT. MXX) THEN	MC807620
	WRITE(6,*) '*** ERROR - TOO MANY INV. COMBINATIONS',N	MC807630
	STOP	MC807640
	ENDIF	MC807650
	K=N	MC807660
	PT(K, 1)=IM	MC807670
	PT(K, 2)=IY	MC807680
	IF(IW.GT.0) PT(K, 3)=IW	MC807690
	ENDIF	MC807700
	DO 130 IT=1,NYR	MC807710
	INV(K,IT)=INV(K,IT) + .25*FLOAT(DATA(IT))	MC807720
130	CONTINUE	MC807730
	END	MC807740
C		MC807750
*****		MC807760
C		MC807770
	SUBROUTINE INSY(MXX,NYR,K,Y,DATA)	MC807780
C ---	ACCUMM INTO KTH ENTRY FOR LOSS	MC807790
	REAL Y(MXX, NYR)	MC807800
	INTEGER DATA(NYR)	MC807810
	IF(K .EQ. 0) RETURN	MC807820

DO 10 IT=1,NYR	MC807830
Y(K,IT)=Y(K,IT) + DATA(IT)	MC807840
10 CONTINUE	MC807850
END	MC807860
C	MC807870
*****	MC807880
C	MC807890
SUBROUTINE AGGREG(INV,Y,MXX,NYR,SMOS,SYCSG,	MC807900
* NRC,NRCOLD,PTRTBL,INDX,AVINV, AIMIN,MKG)	MC807910
C --- COMP. AVERAGE INV. & SORT	MC807920
REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX)	MC807930
INTEGER*2 PTRTBL(MXX, 2), INDX(MXX),MKG(MXX)	MC807940
INTEGER SYCSG(*), SMOS(*)	MC807950
REAL*8 TINV,TY	MC807960
C	MC807970
C --- RESET MKG (NECESSARY WHEN CYCLING THRU AGGPCT VALUES)	MC807980
DO 10 I=1,MXX	MC807990
MKG(I)=0	MC808000
10 CONTINUE	MC808010
TINV=0	MC808020
TY=0	MC808030
DO 100 I=1,NRC	MC808040
C --- FIX INV. ENTRIES LOWER THAN CORRESP. LOSSES & COMP. AVG INV.	MC808050
AI=0	MC808060
DO 201 J=1,NYR	MC808070
TINV=TINV+INV(I,J)	MC808080
TY= TY+ Y(I,J)	MC808090
IF(INV(I,J).LT.Y(I,J)) INV(I,J)=Y(I,J)	MC808100
AI=AI+INV(I,J)	MC808110
201 CONTINUE	MC808120
AVINV(I)=AI/NYR	MC808130
INDX(I)=I	MC808140
100 CONTINUE	MC808150
WRITE(6,*) '==== TOTAL INV,Y=',TINV,TY	MC808160
C	MC808170
C --- SORT ASCENDING BY AVG INVENTORY	MC808180
CALL SORT2(AVINV,INDX,NRC)	MC808190
C	MC808200
NS1=0	MC808210
C --- DISPLAY TABLE IN SORT SEQUENCE	MC808220
CALL DSPTBL(INV,Y,AVINV,PTRTBL,INDX,AIMIN,NRC,MKG,MXX,NYR,	MC808230
* SYCSG,SMOS)	MC808240
C	MC808250
DO 200 K=NRC,1,-1	MC808260
IF(AVINV(K) .GE. AIMIN) THEN	MC808270
C --- MARK AS MEMBER OF SET S0	MC808280
MKG(K)=32767	MC808290
ELSE	MC808300
C --- INITIAL COUNT OF MEMBERS OF SET S1	MC808310
NS1=K	MC808320
GO TO 202	MC808330
ENDIF	MC808340
200 CONTINUE	MC808350
202 CONTINUE	MC808360
C --- DO AGGREGATIONS WITHIN SET S1 UNTIL NO MORE POSSIBLE (KF GE 0)	MC808370

KF=-1	MC808380
C --- DO WHILE KF<0	MC808390
300 IF(KF.GE.0) GO TO 310	MC808400
CALL AGG1(AVINV,INDX,MKG,NS1,INV,Y,MXX,NYR,AIMIN,KF)	MC808410
GO TO 300	MC808420
310 CONTINUE	MC808430
C --- DISPLAY TABLE AFTER 1ST AGGREGATION	MC808440
CALL DSPTBL(INV,Y,AVINV,PTRTBL,INDX,AIMIN,NRC,MKG,MXX,NYR,	MC808450
* SYCSG,SMOS)	MC808460
IF(NS1.EQ.NRC) THEN	MC808470
WRITE(6,*) '***** SET SO EMPTY. NO CELLS ABOVE THRESHOLD'	MC808480
STOP	MC808490
ENDIF	MC808500
C --- DO AGGREGATIONS FROM SET S1 INTO SET SO UNTIL NO MORE POSSIBLE	MC808510
KF=1	MC808520
C --- DO WHILE KF>0	MC808530
320 IF(KF.LE.0) GO TO 330	MC808540
CALL AGG2(AVINV,INDX,MKG,NS1,NRC,INV,Y,MXX,NYR, KF)	MC808550
GO TO 320	MC808560
330 CONTINUE	MC808570
C --- DISPLAY TABLE AFTER 2ND AGGREGATION	MC808580
CALL DSPTBL(INV,Y,AVINV,PTRTBL,INDX,AIMIN,NRC,MKG,MXX,NYR,	MC808590
* SYCSG,SMOS)	MC808600
C --- MOVE VALUES GE AIMIN TO BEGINNING OF ARRAYS	MC808610
CALL CMPRS(INV,Y,MXX,NYR,NRC,NRCOLD,AIMIN,AVINV)	MC808620
C --- DISPLAY TABLE AFTER MOVING VALUES.	MC808630
DO 400 K=1,NRC	MC808640
WRITE(6,122)K,AVINV(K), (INV(K,J),J=1,NYR)	MC808650
WRITE(6,123) (Y(K,J),J=1,NYR)	MC808660
400 CONTINUE	MC808670
122 FORMAT(/I5,14X,F8.3, 6X, 10F7.2)	MC808680
123 FORMAT(33X, 10F7.2)	MC808690
END	MC808700
C *****	MC808710
SUBROUTINE AGG1(AVINV,INDX,MKG,NS1,INV,Y,MXX,NYR,AIMIN,KF)	MC808720
C --- DO ONE PASS OF AGGREGATION	MC808730
REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX)	MC808740
INTEGER*2 INDX(MXX),MKG(MXX)	MC808750
KF=0	MC808760
CI=0	MC808770
DO 10 I=NS1,1,-1	MC808780
IF(MKG(I).EQ.0) THEN	MC808790
IF(KF.EQ.0) THEN	MC808800
C --- THIS WILL BE THE COLLECTING CELL	MC808810
KF=I	MC808820
CI=AVINV(I)	MC808830
ELSE	MC808840
IF(CI+AVINV(I).LT.AIMIN) THEN	MC808850
C --- ACCUM. WITH CELL KF TEMPORARILY. SET TEMP. POINTER -KF	MC808860
CI=CI+AVINV(I)	MC808870
MKG(I)=-KF	MC808880
ELSE	MC808890
C --- FIND SMALLEST CELL TO ADD	MC808900
CALL AGG1A(AVINV,MKG,I,CI,AIMIN,KF,MXX)	MC808910
ENDIF	MC808920

	IF(CI.GE.AIMIN) THEN	MC808930
C ---	MAKE THIS AGGREGATION PERMANENT AND EXIT	MC808940
	AVINV(KF)=CI	MC808950
	CALL AGG1B(INDX,MKG,KF,INV,Y,NYR,MXX)	MC808960
	NS1=NS1-1	MC808970
	MKG(KF)=32767	MC808980
	KF=-1	MC808990
	RETURN	MC809000
	ENDIF	MC809010
	ENDIF	MC809020
	ENDIF	MC809030
10	CONTINUE	MC809040
C		MC809050
	IF(KF.EQ.0) RETURN	MC809060
C ---	CLEAR TEMPORARY POINTERS LEFT. THIS WAS AN UNSUCCESSFUL AGGREG.	MC809070
	DO 20 I=1,NS1	MC809080
	IF(MKG(I).LT.0) MKG(I)=0	MC809090
20	CONTINUE	MC809100
	END	MC809110
C *****		MC809120
	SUBROUTINE AGG1A(AVINV,MKG,ILAST,CI,AIMIN,KF,MXX)	MC809130
C ---	FIND SMALLEST CELL TO ADD AND SET TEMPORARY POINTER	MC809140
	REAL AVINV(MXX)	MC809150
	INTEGER*2 MKG(MXX)	MC809160
	DO 10 I=1,ILAST	MC809170
	IF(MKG(I).EQ.0) THEN	MC809180
	IF(CI+AVINV(I).GE.AIMIN) THEN	MC809190
	CI=CI+AVINV(I)	MC809200
	MKG(I)=-KF	MC809210
	RETURN	MC809220
	ENDIF	MC809230
	ENDIF	MC809240
10	CONTINUE	MC809250
	WRITE(6,*) '**** ERROR IN AGG1A. NO VALUE FOUND ****'	MC809260
	STOP	MC809270
	END	MC809280
C *****		MC809290
	SUBROUTINE AGG1B(INDX,MKG,KF,INV,Y,NYR,MXX)	MC809300
C ---	MAKE AGGREGATION PERMANENT	MC809310
	REAL INV(MXX,NYR), Y(MXX,NYR)	MC809320
	INTEGER*2 INDX(MXX),MKG(MXX)	MC809330
	K=INDX(KF)	MC809340
	DO 10 I=1,KF-1	MC809350
	IF(MKG(I).LT.0) THEN	MC809360
	IF(MKG(I).NE.-KF) STOP 777	MC809370
	MKG(I)=KF	MC809380
	L=INDX(I)	MC809390
	DO 20 J=1,NYR	MC809400
	INV(K,J)=INV(K,J)+INV(L,J)	MC809410
	Y(K,J)= Y(K,J)+ Y(L,J)	MC809420
20	CONTINUE	MC809430
	ENDIF	MC809440
10	CONTINUE	MC809450
	END	MC809460
C *****		MC809470

	SUBROUTINE AGG2(AVINV,INDX,MKG,NS1,NRC,INV,Y,MXX,NYR, KF)	MC809480
C ---	DO ONE PASS OF AGGREGATION FROM SET S1 TO SET S0	MC809490
C ---	ON EACH PASS ONE ELEMENT OF S1 IS TAKEN & ADDED TO SMALLEST OF S0	MC809500
	REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX)	MC809510
	INTEGER*2 INDX(MXX),MKG(MXX)	MC809520
	KF=0	MC809530
C ---	FIND ELEMENT OF S1 (ONLY THOSE WITH POINTER MKG(I)=0)	MC809540
	DO 10 I=1,NS1	MC809550
	IF(MKG(I).EQ.0) THEN	MC809560
	KF=I	MC809570
	GO TO 12	MC809580
	ENDIF	MC809590
	10 CONTINUE	MC809600
	12 CONTINUE	MC809610
C ---	IF KF STILL 0 THEN NO MORE ELEMENTS IN S1 LEFT	MC809620
	IF(KF.EQ.0) RETURN	MC809630
C		MC809640
C ---	FIND SMALLEST ELEMENT OF S0 AND ADD TO IT. ONLY WITH MKG(I)=32767	MC809650
	ISM=NRC	MC809660
	SMALL=AVINV(ISM)	MC809670
	DO 20 I=1, NRC	MC809680
	IF(MKG(I).EQ.32767) THEN	MC809690
	IF(AVINV(I).LT.SMALL) THEN	MC809700
	ISM=I	MC809710
	SMALL=AVINV(I)	MC809720
	ENDIF	MC809730
	ENDIF	MC809740
	20 CONTINUE	MC809750
C ---	JOIN ELEMENT KF TO ELEMENT ISM	MC809760
	AVINV(ISM)=AVINV(ISM) + AVINV(KF)	MC809770
	MKG(KF)=ISM	MC809780
	L=INDX(KF)	MC809790
	K=INDX(ISM)	MC809800
	DO 30 J=1,NYR	MC809810
	INV(K,J)=INV(K,J)+INV(L,J)	MC809820
	Y(K,J)= Y(K,J)+ Y(L,J)	MC809830
	30 CONTINUE	MC809840
	END	MC809850
C *****		MC809860
	SUBROUTINE CMPRS(INV,Y,MXX,NYR,NRC,NRCOLD,AIMIN,AVINV)	MC809870
	REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX)	MC809880
C ---	COMPRESS INV,Y IN PLACE. MOVE ALL ROWS GE AIMIN TO TOP	MC809890
	NRCOLD=NRC	MC809900
	NRC=0	MC809910
	DO 10 I=1,NRCOLD	MC809920
	AI=CAINV(INV,I,MXX,NYR)	MC809930
	IF(AI .GE. AIMIN) THEN	MC809940
C ---	TRANSFER ACTIVE CELL I ---> NRC	MC809950
	NRC=NRC+1	MC809960
	AVINV(NRC)=AI	MC809970
	DO 20 J=1,NYR	MC809980
	INV(NRC,J)=INV(I,J)	MC809990
	Y(NRC,J)= Y(I,J)	MC810000
	20 CONTINUE	MC810010
	ENDIF	MC810020
	10 CONTINUE	MC810030

END	MC810040
C *****	MC810050
FUNCTION CAINV(INV,I,MXX,NYR)	MC810060
REAL INV(MXX, NYR)	MC810070
C --- COMPUTE AVERAGE INVENTORY FOR ROW I	MC810080
CAINV=0	MC810090
DO 10 J=1,NYR	MC810100
CAINV=CAINV+INV(I,J)	MC810110
10 CONTINUE	MC810120
CAINV=CAINV/NYR	MC810130
END	MC810140
C *****	MC810150
SUBROUTINE DSPTBL(INV,Y,AVINV,PTRTBL,INDX,AIMIN,NRC,MKG,MXX,NYR,	MC810160
* SYCSG,SMOS)	MC810170
C --- DISPLAY TABLE IN SORT SEQUENCE	MC810180
REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX)	MC810190
INTEGER*2 PTRTBL(MXX, 2), INDX(MXX),MKG(MXX)	MC810200
INTEGER SYCSG(*)	MC810210
INTEGER SMOS(*)	MC810220
INTEGER IATT(2)	MC810230
CHARACTER*1 STI	MC810240
WRITE(6,121)	MC810250
WRITE(6,*) 'INV. THRESHOLD MIN. VALUE=',AIMIN	MC810260
C	MC810270
WRITE(6,*) ' I INDX AVG MKG INVENTORY/LOSSES'	MC810280
DO 200 K=1,NRC	MC810290
STI=' '	MC810300
I=INDX(K)	MC810310
AI=AVINV(K)	MC810320
IF(AI .LT. AIMIN) STI='\$'	MC810330
IATT(1)=SMOS(PTRTBL(I,1))	MC810340
IATT(2)=SYCSG(PTRTBL(I,2))	MC810350
WRITE(6,122)K,I,AI,MKG(K),STI,(INV(I,J),J=1,NYR),(IATT(J),J=1,2),	MC810360
* PTRTBL(I,1),PTRTBL(I,2)	MC810370
WRITE(6,123) (Y(I,J),J=1,NYR)	MC810380
200 CONTINUE	MC810390
C	MC810400
121 FORMAT(///)	MC810410
122 FORMAT(/2I5,F8.3,I9,1X,A2, 10F7.2, 5X, 6I5)	MC810420
123 FORMAT(30X, 10F7.2)	MC810430
END	MC810440
C *****	MC810450
SUBROUTINE SORT2(Y,INDX, N)	MC810460
C --- INPLACE SORT USING SHELL ALGORITHM *****	MC810470
C --- SORTS ON Y AND DOES SAME REORDERING ON INDEXES INDX	MC810480
REAL Y(N),TEMP	MC810490
INTEGER GAP	MC810500
INTEGER*2 INDX(N), ITEMP	MC810510
LOGICAL EXCH	MC810520
C	MC810530
GAP=(N/2)	MC810540
5 IF (.NOT.(GAP.NE.0)) GO TO 500	MC810550
10 CONTINUE	MC810560
EXCH=.TRUE.	MC810570
K=N-GAP	MC810580
DO 200 I=1,K	MC810590

	KK=I+GAP	MC810600
	IF(.NOT.(Y(I).GT.Y(KK))) GO TO 100	MC810610
	TEMP=Y(I)	MC810620
	Y(I)=Y(KK)	MC810630
	Y(KK)=TEMP	MC810640
	ITEMP=INDX(I)	MC810650
	INDX(I)=INDX(KK)	MC810660
	INDX(KK)=ITEMP	MC810670
	EXCH=.FALSE.	MC810680
100	CONTINUE	MC810690
200	CONTINUE	MC810700
	IF (.NOT.(EXCH)) GO TO 10	MC810710
	GAP=(GAP/2)	MC810720
	GO TO 5	MC810730
500	CONTINUE	MC810740
	RETURN	MC810750
	END	MC810760
C		MC810770
	*****	MC810780
C		MC810790
	SUBROUTINE BKDOWN(PTBL,NPT,PTRTBL,NRC,INDX,MKG,MXX,MXY,	MC810800
	* SINV,SY,INV,Y,BKTBL,NBK)	MC810810
C ---	BREAKDOWN AGGREGATED VALUES BY THE 3RD DIMENSION SVC/CS	MC810820
	REAL INV(MXX,MXY),Y(MXX,MXY), SINV(MXX,MXY),SY(MXX,MXY)	MC810830
	INTEGER*2 PTRTBL(MXX, 2), INDX(MXX), MKG(MXX)	MC810840
	INTEGER*2 PTBL(MXX, 3), BKTBL(MXX,3)	MC810850
	REAL*8 TINV,TY	MC810860
	NBK=0	MC810870
C ---	TRAVERSE MKG ARRAY AND BUILD BKTBL	MC810880
	DO 10 I=1,NRC	MC810890
	IF(MKG(I).NE.32767) THEN	MC810900
	ICELL=MKG(I)	MC810910
	ELSE	MC810920
	ICELL=I	MC810930
	ENDIF	MC810940
	IX=INDX(I)	MC810950
	IM=PTRTBL(IX,1)	MC810960
	IY=PTRTBL(IX,2)	MC810970
	CALL BLDBK(ICELL,IM,IY,PTBL,NPT,MXX,BKTBL,NBK)	MC810980
10	CONTINUE	MC810990
C ---	DISPLAY BKTBL PRIOR TO SORTING	MC811000
	WRITE(6,101) (I,(BKTBL(I,J),J=1,3), I=1,NBK)	MC811010
	CALL SORT3(BKTBL,NBK,MXX)	MC811020
	WRITE(6,101) (I,(BKTBL(I,J),J=1,3), I=1,NBK)	MC811030
C ---	SUMMARIZE SINV,SY INTO INV,Y FOR MATCHING ENTRIES IN BKTBL	MC811040
	CALL SUMBK(BKTBL,NBK,MXX,SINV,SY,INV,Y,MXY)	MC811050
	WRITE(6,102) (I,(INV(I,J),J=1,MXY),(BKTBL(I,J),J=1,2), I=1,NBK)	MC811060
	WRITE(6,102) (I,(Y(I,J),J=1,MXY),(BKTBL(I,J),J=1,2), I=1,NBK)	MC811070
101	FORMAT(I4, 3I6)	MC811080
102	FORMAT(I4, 10F7.2,10X,2I4)	MC811090
103	FORMAT(/I5,10F7.2)	MC811100
104	FORMAT(5X,10F7.2)	MC811110
	END	MC811120
C	*****	MC811130
	SUBROUTINE BLDBK(ICELL,IM,IY,PTBL,NPT,MXX,BKTBL,NBK)	MC811140

	INTEGER*2 PTBL(MXX, 3), BKTBL(MXX,3)	MC811150
C ---	RECORD ALL ENTRIES IN PTBL WITH MATCHING IM,IY IN BKTBL	MC811160
	DO 10 I=1,NPT	MC811170
	IF(PTBL(I,1).EQ.IM .AND. PTBL(I,2).EQ.IY) THEN	MC811180
C ---	INSTALL WITH CELL ID, IW & POINTER	MC811190
	NBK=NBK+1	MC811200
	BKTBL(NBK,1)=ICELL	MC811210
	BKTBL(NBK,2)=PTBL(I,3)	MC811220
	BKTBL(NBK,3)=I	MC811230
	ENDIF	MC811240
10	CONTINUE	MC811250
	END	MC811260
C *****		MC811270
	SUBROUTINE SORT3(T,N,MXX)	MC811280
C ---	INPLACE SORT USING SHELL ALGORITHM *****	MC811290
C ---	SORTS ON 1ST 2 COLS. OF T & DOES SAME REORDERING ON 3RD COLUMN	MC811300
	INTEGER*2 T(MXX,3), ITEMP	MC811310
	INTEGER GAP	MC811320
	LOGICAL EXCH	MC811330
C		MC811340
	GAP=(N/2)	MC811350
5	IF (GAP.EQ.0) GO TO 500	MC811360
10	CONTINUE	MC811370
	EXCH=.FALSE.	MC811380
	K=N-GAP	MC811390
	DO 200 I=1,K	MC811400
	KK=I+GAP	MC811410
	IF(T(I,1).GT.T(KK,1) .OR.	MC811420
*	(T(I,1).EQ.T(KK,1) .AND. T(I,2).GT.T(KK,2))) THEN	MC811430
	IT1=T(I,1)	MC811440
	IT2=T(I,2)	MC811450
	IT3=T(I,3)	MC811460
	T(I,1)=T(KK,1)	MC811470
	T(I,2)=T(KK,2)	MC811480
	T(I,3)=T(KK,3)	MC811490
	T(KK,1)=IT1	MC811500
	T(KK,2)=IT2	MC811510
	T(KK,3)=IT3	MC811520
	EXCH=.TRUE.	MC811530
	ENDIF	MC811540
200	CONTINUE	MC811550
	IF (EXCH) GO TO 10	MC811560
	GAP=(GAP/2)	MC811570
	GO TO 5	MC811580
500	CONTINUE	MC811590
	RETURN	MC811600
	END	MC811610
C *****		MC811620
	SUBROUTINE SUMBK(BKTBL,NBK,MXX,SINV,SY,INV,Y,MXY)	MC811630
C ---	CREATE AGGREGATED ARRAYS INV,Y FROM CELL & 3RD DIM. INFO. IN BKTBL	MC811640
	REAL INV(MXX,MXY),Y(MXX,MXY), SINV(MXX,MXY),SY(MXX,MXY)	MC811650
	INTEGER*2 BKTBL(MXX,3)	MC811660
	REAL*8 TINV,TY	MC811670
	IP=0	MC811680
	I1=-1	MC811690
	I2=-1	MC811700

TINV=0	MC811710
TY=0	MC811720
DO 10 I=1,NBK	MC811730
IF(BKTBL(I,1).NE.I1 .OR. BKTBL(I,2).NE.I2) THEN	MC811740
C --- CHANGE OF CELL,IW IDENTIFIERS	MC811750
IP=IP+1	MC811760
I1=BKTBL(I,1)	MC811770
I2=BKTBL(I,2)	MC811780
DO 15 J=1,MXY	MC811790
INV(IP,J)=0	MC811800
Y(IP,J)=0	MC811810
15 CONTINUE	MC811820
BKTBL(IP,1)=I1	MC811830
BKTBL(IP,2)=I2	MC811840
ENDIF	MC811850
C --- ACCUMULATE	MC811860
I3=BKTBL(I,3)	MC811870
DO 20 J=1,MXY	MC811880
INV(IP,J)=INV(IP,J)+SINV(I3,J)	MC811890
Y(IP,J)= Y(IP,J)+ SY(I3,J)	MC811900
TINV=TINV+SINV(I3,J)	MC811910
TY= TY+ SY(I3,J)	MC811920
20 CONTINUE	MC811930
10 CONTINUE	MC811940
WRITE(6,*) '==== TOTAL INV,Y AFTER BREAKDOWN=',TINV,TY	MC811950
C	MC811960
NBK=IP	MC811970
C --- FIX INV. ENTRIES LOWER THAN CORRESP. LOSSES	MC811980
DO 40 I=1,NBK	MC811990
DO 30 J=1,MXY	MC812000
IF(INV(I,J).LT.Y(I,J)) INV(I,J)=Y(I,J)	MC812010
30 CONTINUE	MC812020
40 CONTINUE	MC812030
END	MC812040

C. ESTIMATION SUBROUTINES

	SUBROUTINE MC87BZ(INV,Y,NRC,NYR,XTB,VXTB,XEB,A,MXX,MXY)	MC800010
C ---	CONDUCTS FIRST FIVE ESTIMATION METHODS	MC800020
C		MC800030
	REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC800040
	REAL XTB(MXX), VXTB(MXX), A(MXX)	MC800050
C		MC800060
	CALL EBTS1(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC800070
	PRINT *, 'COMPLETED EBTS1'	MC800080
C		MC800090
	CALL EBTS2(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC800100
	PRINT *, 'COMPLETED EBTS2'	MC800110
C		MC800120
	CALL EBOS1(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC800130
	PRINT *, 'COMPLETED EBOS1'	MC800140
C		MC800150
	CALL EBOS2(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC800160
	PRINT *, 'COMPLETED EBOS2'	MC800170
C		MC800180
	CALL EMTS(INV,Y,NRC,NYR,XTB,VXTB,XEB,A,MXX,MXY)	MC800190
	PRINT *, 'COMPLETED EMTS'	MC800200
C		MC800210
	END	MC800220
C		MC800230
	*****	MC800240
C		MC800250
	SUBROUTINE EBTS1(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC800260
C ---	TRANSFORMED SCALE, TIME INDEPENDENT VARIANCE METHOD	MC800270
	REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC800280
	REAL XTB(MXX), VXTB(MXX)	MC800290
	REAL MAXL,MINL,L,MAXCHI,MINCHI	MC800300
	INTEGER T, VYR	MC800310
	DATA AA/1.6835/, B1/-.8934/, B2/.9881/	MC800320
	MAXL= -1000.0	MC800330
	MINL= 1000.0	MC800340
	SUML= 0.0	MC800350
	KLSUM=0	MC800360
	MAXCHI= -1000.0	MC800370
	MINCHI= 1000.0	MC800380
	SUMCHI= 0.0	MC800390
	KSUM=0	MC800400
	SUMMAD=0.0	MC800410
	KPSUM=0	MC800420
	WRITE(11,32)' '	MC800430
	WRITE(11,21)'EMP BAYES TRANS SCALE - TIME DEP VAR: '	MC800440
	WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE): '	MC800450
	WRITE(11,28)'FRACTION CELLS','FRACTION MAD'	MC800460
	WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD'	MC800470
	WRITE(11,30)	MC800480
C		MC800490
C ---	LOOP THROUGH VALIDATION YEARS	MC800500
	DO 280 VYR=1, NYR	MC800510
C ---	LOOP THROUGH CELLS	MC800520
	DO 260 IN=1, NRC	MC800530

T=0	MC800540
SUMXT=0	MC800550
SUMVAR=0	MC800560
C --- LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB)	MC800570
DO 200 IT=1, NYR	MC800580
IF(IT .NE. VYR) THEN	MC800590
IF(INV(IN,IT) .NE. 0) THEN	MC800600
X=FTT(INV(IN,IT), Y(IN,IT))	MC800610
C=SQRT(0.5+INV(IN,IT))	MC800620
XX=X+C*(3.141592654/2.0)	MC800630
XT=X/C	MC800640
T=T+1	MC800650
SUMXT=SUMXT+XT	MC800660
IF(XX .LT. 1.001) XX=1.001	MC800670
VARX=AA*(XX**B1)*(XX-1)**B2	MC800680
IF(VARX .GT. 1.0) VARX=1.0	MC800690
VARXT=VARX/(0.5+INV(IN,IT))	MC800700
SUMVAR=SUMVAR+VARXT	MC800710
ENDIF	MC800720
200 CONTINUE	MC800730
XTB(IN)=SUMXT/T	MC800740
VXTB(IN)=SUMVAR/T**2	MC800750
260 CONTINUE	MC800760
C	MC800770
C --- CONDUCT ALGORITHM TO FIND XEB	MC800780
CALL EBITER(NRC,XTB,VXTB,XEB,MXX,VYR)	MC800790
C	MC800800
C --- COMPUTE MEAN SQUARED ERROR	MC800810
CALL MSE(INV,Y,NRC,NYR,VYR,XEB,L,MXX,MXY,KL)	MC800820
IF(L .LT. MINL) THEN	MC800830
MINL=L	MC800840
MINLK=KL	MC800850
MINLYR=VYR	MC800860
ELSE IF(L .GT. MAXL) THEN	MC800870
MAXL=L	MC800880
MAXLK=KL	MC800890
MAXLYR=VYR	MC800900
ENDIF	MC800910
SUML=SUML+L*KL	MC800920
KLSUM=KLSUM+KL	MC800930
C	MC800940
C --- INVERT XEB TO ORIGINAL SCALE	MC800950
CALL INVERT(NRC,XEB,MXX)	MC800960
C	MC800970
C --- COMPUTE MAD AND CHI SQUARE	MC800980
CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,	MC800990
* FCELLU,FMADU,PMAD,KP)	MC801000
IF(CHI .LT. MINCHI) THEN	MC801010
MINCHI=CHI	MC801020
MNCHIK=K	MC801030
MNCHYR=VYR	MC801040
ELSE IF(CHI .GT. MAXCHI) THEN	MC801050
MAXCHI=CHI	MC801060
MXCHIK=K	MC801070
MXCHYR=VYR	MC801080
	MC801090

ENDIF	MC801100
SUMCHI=SUMCHI+CHI*K	MC801110
KSUM=KSUM+K	MC801120
KPSUM=KPSUM+KP	MC801130
SUMMAD=SUMMAD+PMAD*KP	MC801140
WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD	MC801150
280 CONTINUE	MC801160
C	MC801170
C --- WRITE RESULTS TO OUTPUT FILE	MC801180
AVGL=SUML/KLSUM	MC801190
AVGCHI=SUMCHI/KSUM	MC801200
AVGMAD=SUMMAD/KPSUM	MC801210
WRITE(11,19)'AVG MAD = ',AVGMAD	MC801220
WRITE(11,21)'CHI SQUARE (ORIG SCALE): '	MC801230
WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYR	MC801240
WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYR	MC801250
WRITE(11,26)'AVG CHI = ',AVGCHI	MC801260
WRITE(11,21)'MEAN SQUARED ERROR (TRANS SCALE): '	MC801270
WRITE(11,25)'MIN MSE = ',MINL,'K = ',MINLK,'VALID YR = ',MINLYR	MC801280
WRITE(11,25)'MAX MSE = ',MAXL,'K = ',MAXLK,'VALID YR = ',MAXLYR	MC801290
WRITE(11,27)'AVG MSE = ',AVGL	MC801300
19 FORMAT(38X,A,F5.3)	MC801310
21 FORMAT(/1X,A)	MC801320
25 FORMAT(1X,A,F6.3,5X,A,I3,5X,A,I2)	MC801330
26 FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)	MC801340
27 FORMAT(1X,A,F6.3/)	MC801350
28 FORMAT(17X,A,2X,A)	MC801360
29 FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A)	MC801370
30 FORMAT(1X,8(' '),2X,4(' '),2X,14(' '),2X,13(' '),2X,5(' '))	MC801380
31 FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)	MC801390
32 FORMAT(1X,A)	MC801400
RETURN	MC801410
END	MC801420
C	MC801430
*****	MC801440
C	MC801450
SUBROUTINE EBTS2(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC801460
C --- TRANSFORMED SCALE, TIME INDEPENDENT VARIANCE METHOD	MC801470
REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC801480
REAL XTB(MXX), VXTB(MXX)	MC801490
REAL MAXL,MINL,L,MAXCHI,MINCHI	MC801500
INTEGER T, VYR	MC801510
MAXL= -1000.0	MC801520
MINL= 1000.0	MC801530
SUML= 0.0	MC801540
KLSUM=0	MC801550
MAXCHI= -1000.0	MC801560
MINCHI= 1000.0	MC801570
SUMCHI= 0.0	MC801580
KSUM=0	MC801590
SUMMAD=0.0	MC801600
KPSUM=0	MC801610
WRITE(11,21)'EMP BAYES TRANS SCALE - TIME INDEP VAR: '	MC801620
WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE): '	MC801630
WRITE(11,28)'FRACTION CELLS','FRACTION MAD'	MC801640
WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD'	MC801650

WRITE(11,30)	MC801660
C	MC801670
C --- LOOP THROUGH VALIDATION YEARS	MC801680
DO 380 VYR=1, NYR	MC801690
C --- LOOP THROUGH CELLS	MC801700
DO 360 IN=1, NRC	MC801710
T=0	MC801720
SUMXT=0	MC801730
SUMXT2=0	MC801740
C --- LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB)	MC801750
DO 300 IT=1, NYR	MC801760
IF(IT .NE. VYR) THEN	MC801770
IF(INV(IN,IT) .NE. 0) THEN	MC801780
X=FTT(INV(IN,IT), Y(IN,IT))	MC801790
XT=X/SQRT(0.5+INV(IN,IT))	MC801800
T=T+1	MC801810
SUMXT=SUMXT+XT	MC801820
SUMXT2=SUMXT2+XT**2	MC801830
ENDIF	MC801840
ENDIF	MC801850
300 CONTINUE	MC801860
XTB(IN)=SUMXT/T	MC801870
VXTB(IN)=((T*SUMXT2)-(SUMXT**2))/((T-1)*T**2)	MC801880
360 CONTINUE	MC801890
C	MC801900
C --- CONDUCT ALGORITHM TO FIND XEB	MC801910
CALL EBITER(NRC,XTB,VXTB,XEB,MXX,VYR)	MC801920
C	MC801930
C --- COMPUTE MEAN SQUARED ERROR	MC801940
CALL MSE(INV,Y,NRC,NYR,VYR,XEB,L,MXX,MXY,KL)	MC801950
IF(L .LT. MINL) THEN	MC801960
MINL=L	MC801970
MINLK=KL	MC801980
MINLYR=VYR	MC801990
ELSE IF(L .GT. MAXL) THEN	MC802000
MAXL=L	MC802010
MAXLK=KL	MC802020
MAXLYR=VYR	MC802030
ENDIF	MC802040
SUML=SUML+L*KL	MC802050
KLSUM=KLSUM+KL	MC802060
C	MC802070
C --- INVERT XEB TO ORIGINAL SCALE	MC802080
CALL INVERT(NRC,XEB,MXX)	MC802090
C	MC802100
C --- COMPUTE MAD AND CHI SQUARE	MC802110
CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,	MC802120
* FCELLU,FMADU,PMAD,KP)	MC802130
IF(CHI .LT. MINCHI) THEN	MC802140
MINCHI=CHI	MC802150
MNCHIK=K	MC802160
MNCHYR=VYR	MC802170
ELSE IF(CHI .GT. MAXCHI) THEN	MC802180
MAXCHI=CHI	MC802190
MXCHIK=K	MC802200
MXCHYR=VYR	MC802210

ENDIF	MC802220
SUMCHI=SUMCHI+CHI*K	MC802230
KSUM=KSUM+K	MC802240
KPSUM=KPSUM+KP	MC802250
SUMMAD=SUMMAD+PMAD*KP	MC802260
WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD	MC802270
380 CONTINUE	MC802280
C	MC802290
C --- WRITE OUTPUT TO FILE	MC802300
AVGL=SUML/KLSUM	MC802310
AVGCHI=SUMCHI/KSUM	MC802320
AVGMAD=SUMMAD/KPSUM	MC802330
WRITE(11,19)'AVG MAD = ',AVGMAD	MC802340
WRITE(11,21)'CHI SQUARE (ORIG SCALE):'	MC802350
WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYR	MC802360
WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYR	MC802370
WRITE(11,26)'AVG CHI = ',AVGCHI	MC802380
WRITE(11,21)'MEAN SQUARED ERROR (TRANS SCALE):'	MC802390
WRITE(11,25)'MIN MSE = ',MINL,'K = ',MINLK,'VALID YR = ',MINLYR	MC802400
WRITE(11,25)'MAX MSE = ',MAXL,'K = ',MAXLK,'VALID YR = ',MAXLYR	MC802410
WRITE(11,27)'AVG MSE = ',AVGL	MC802420
19 FORMAT(38X,A,F5.3)	MC802430
21 FORMAT(/1X,A)	MC802440
25 FORMAT(1X,A,F6.3,5X,A,I3,5X,A,I2)	MC802450
26 FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)	MC802460
27 FORMAT(1X,A,F6.3/)	MC802470
28 FORMAT(17X,A,2X,A)	MC802480
29 FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A)	MC802490
30 FORMAT(1X,8(' '),2X,4(' '),2X,14(' '),2X,13(' '),2X,5(' '))	MC802500
31 FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)	MC802510
RETURN	MC802520
END	MC802530
C	MC802540
*****	MC802550
C	MC802560
SUBROUTINE EBOS1(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC802570
C --- ORIGINAL SCALE, TIME DEPENDENT VARIANCE METHOD	MC802580
REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC802590
REAL XTB(MXX), VXTB(MXX)	MC802600
REAL MAXCHI, MINCHI	MC802610
INTEGER T, VYR	MC802620
MAXCHI= -1000.0	MC802630
MINCHI= 1000.0	MC802640
SUMCHI= 0.0	MC802650
KSUM=0	MC802660
SUMMAD=0.0	MC802670
KPSUM=0	MC802680
WRITE(11,21)'EMP BAYES ORIG SCALE - TIME DEP VAR:'	MC802690
WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE):'	MC802700
WRITE(11,28)'FRACTION CELLS','FRACTION MAD'	MC802710
WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD'	MC802720
WRITE(11,30)	MC802730
C	MC802740
C --- LOOP THROUGH VALIDATION YEARS	MC802750
DO 480 VYR=1, NYR	MC802760
C --- LOOP THROUGH CELLS	MC802770

DO 460	IN=1, NRC	MC802780
	T=0	MC802790
	SUMXT=0	MC802800
	SUMVAR=0	MC802810
C ---	LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB)	MC802820
	DO 400 IT=1, NYR	MC802830
	IF(IT .NE. VYR) THEN	MC802840
	IF(INV(IN,IT) .NE. 0) THEN	MC802850
	PHAT=Y(IN,IT)/INV(IN,IT)	MC802860
	T=T+1	MC802870
	SUMXT=SUMXT+PHAT	MC802880
	IF(PHAT .GT. 0.0) THEN	MC802890
	SUMVAR=SUMVAR+PHAT*(1-PHAT)/INV(IN,IT)	MC802900
	ELSE	MC802910
	SUMVAR=SUMVAR+1/(INV(IN,IT)+1)**2	MC802920
	ENDIF	MC802930
	ENDIF	MC802940
	ENDIF	MC802950
400	CONTINUE	MC802960
	XTB(IN)=SUMXT/T	MC802970
	VXTB(IN)=SUMVAR/T**2	MC802980
460	CONTINUE	MC802990
C		MC803000
C ---	CONDUCT ALGORITHM TO FIND XEB	MC803010
	CALL EBITER(NRC,XTB,VXTB,XEB,MXX,VYR)	MC803020
C		MC803030
C ---	COMPUTE MAD AND CHI SQUARE	MC803040
	CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,	MC803050
	* FCELLU,FMADU,PMAD,KP)	MC803060
	IF(CHI .LT. MINCHI) THEN	MC803070
	MINCHI=CHI	MC803080
	MNCHIK=K	MC803090
	MNCHYR=VYR	MC803100
	ELSE IF(CHI .GT. MAXCHI) THEN	MC803110
	MAXCHI=CHI	MC803120
	MXCHIK=K	MC803130
	MXCHYR=VYR	MC803140
	ENDIF	MC803150
	SUMCHI=SUMCHI+CHI*K	MC803160
	KSUM=KSUM+K	MC803170
	KPSUM=KPSUM+KP	MC803180
	SUMMAD=SUMMAD+PMAD*KP	MC803190
	WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD	MC803200
480	CONTINUE	MC803210
C		MC803220
C ---	WRITE OUTPUT TO FILE	MC803230
	AVGCHI=SUMCHI/KSUM	MC803240
	AVGMAD=SUMMAD/KPSUM	MC803250
	WRITE(11,19)'AVG MAD = ',AVGMAD	MC803260
	WRITE(11,21)'CHI SQUARE (ORIG SCALE): '	MC803270
	WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYR	MC803280
	WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYR	MC803290
	WRITE(11,27)'AVG CHI = ',AVGCHI	MC803300
19	FORMAT(38X,A,F5.3)	MC803310
21	FORMAT(/1X,A)	MC803320
26	FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)	MC803330

27	FORMAT(1X,A,F9.3/)	MC803340
28	FORMAT(17X,A,2X,A)	MC803350
29	FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A)	MC803360
30	FORMAT(1X,8(' - '),2X,4(' - '),2X,14(' - '),2X,13(' - '),2X,5(' - '))	MC803370
31	FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)	MC803380
	RETURN	MC803390
	END	MC803400
C		MC803410
	*****	MC803420
C		MC803430
	SUBROUTINE EBOS2(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC803440
C ---	ORIGINAL SCALE, TIME INDEPENDENT VARIANCE METHOD	MC803450
	REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC803460
	REAL XTB(MXX), VXTB(MXX)	MC803470
	REAL MAXCHI, MINCHI	MC803480
	INTEGER T, VYR	MC803490
	MAXCHI= -1000.0	MC803500
	MINCHI= 1000.0	MC803510
	SUMCHI= 0.0	MC803520
	KSUM=0	MC803530
	SUMMAD=0.0	MC803540
	KPSUM=0	MC803550
	WRITE(11,21)'EMP BAYES ORIG SCALE - TIME INDEP VAR: '	MC803560
	WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE): '	MC803570
	WRITE(11,28)'FRACTION CELLS','FRACTION MAD'	MC803580
	WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD'	MC803590
	WRITE(11,30)	MC803600
C		MC803610
C ---	LOOP THROUGH VALIDATION YEARS	MC803620
	DO 580 VYR=1, NYR	MC803630
C ---	LOOP THROUGH CELLS	MC803640
	DO 560 IN=1 NRC	MC803650
	T=0	MC803660
	SUMXT=0	MC803670
	SUMVAR=0	MC803680
	SUMY=0	MC803690
	SUMINV=0	MC803700
C ---	LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB)	MC803710
	DO 500 IT=1, NYR	MC803720
	IF(IT.NE. VYR) THEN	MC803730
	IF(INV(IN,IT).NE. 0) THEN	MC803740
	PHAT=Y(IN,IT)/INV(IN,IT)	MC803750
	SUMXT=SUMXT+PHAT	MC803760
	SUMY=SUMY+Y(IN,IT)	MC803770
	SUMINV=SUMINV+INV(IN,IT)	MC803780
	T=T+1	MC803790
	SUMVAR=SUMVAR+1.0/INV(IN,IT)	MC803800
	ENDIF	MC803810
	ENDIF	MC803820
500	CONTINUE	MC803830
	XTB(IN)=SUMXT/T	MC803840
	IF(SUMY.GT. 0.0) THEN	MC803850
	PTILDE=SUMY/SUMINV	MC803860
	VXTB(IN)=(PTILDE*(1-PTILDE)*SUMVAR)/T**2	MC803870
	ELSE	MC803880
	VXTB(IN)=SUMINV*SUMVAR/(((1+SUMINV)**2)*T**2)	MC803890

ENDIF	MC803900
560 CONTINUE	MC803910
C	MC803920
C --- CONDUCT ALGORITHM TO FIND XEB	MC803930
CALL EBITER(NRC,XTB,VXTB,XEB,MXX,VYR)	MC803940
C	MC803950
C --- COMPUTE MAD AND CHI SQUARE	MC803960
CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,	MC803970
* FCELLU,FMADU,PMAD,KP)	MC803980
IF(CHI .LT. MINCHI) THEN	MC803990
MINCHI=CHI	MC804000
MNCHIK=K	MC804010
MNCHYR=VYR	MC804020
ELSE IF(CHI .GT. MAXCHI) THEN	MC804030
MAXCHI=CHI	MC804040
MXCHIK=K	MC804050
MXCHYR=VYR	MC804060
ENDIF	MC804070
SUMCHI=SUMCHI+CHI*K	MC804080
KSUM=KSUM+K	MC804090
KPSUM=KPSUM+KP	MC804100
SUMMAD=SUMMAD+PMAD*KP	MC804110
WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD	MC804120
580 CONTINUE	MC804130
C	MC804140
C --- WRITE OUTPUT TO FILE	MC804150
AVGCHI=SUMCHI/KSUM	MC804160
AVGMAD=SUMMAD/KPSUM	MC804170
WRITE(11,19)'AVG MAD = ',AVGMAD	MC804180
WRITE(11,21)'CHI SQUARE (ORIG SCALE): '	MC804190
WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYR	MC804200
WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYR	MC804210
WRITE(11,27)'AVG CHI = ',AVGCHI	MC804220
19 FORMAT(38X,A,F5.3)	MC804230
21 FORMAT(/1X,A)	MC804240
26 FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)	MC804250
27 FORMAT(1X,A,F9.3/)	MC804260
28 FORMAT(17X,A,2X,A)	MC804270
29 FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A)	MC804280
30 FORMAT(1X,8(' '),2X,4(' '),2X,14(' '),2X,13(' '),2X,5(' '))	MC804290
31 FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)	MC804300
RETURN	MC804310
END	MC804320
C	MC804330
*****	MC804340
C	MC804350
SUBROUTINE EMTS(INV,Y,NRC,NYR,XTB,VXTB,XEB,A,MXX,MXY)	MC804360
C --- EFRON-MORRIS METHOD	MC804370
REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC804380
REAL XTB(MXX), VXTB(MXX), A(MXX)	MC804390
REAL MAXL,MINL,L,MAXCHI,MINCHI	MC804400
INTEGER T, VYR	MC804410
DATA AA/1.6835/, B1/-.8934/, B2/.9881/	MC804420
MAXL= -1000.0	MC804430
MINL= 1000.0	MC804440
SUML= 0.0	MC804450

KLSUM=0	MC804460
MAXCHI= -1000.0	MC804470
MINCHI= 1000.0	MC804480
SUMCHI= 0.0	MC804490
KSUM=0	MC804500
SUMMAD=0.0	MC804510
KPSUM=0	MC804520
WRITE(11,21)'EFRON-MORRIS TRANS SCALE - TIME DEP VAR: '	MC804530
WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE): '	MC804540
WRITE(11,28)'FRACTION CELLS','FRACTION MAD'	MC804550
WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD'	MC804560
WRITE(11,30)	MC804570
C	MC804580
C --- LOOP THROUGH VALIDATION YEARS	MC804590
DO 280 VYR=1, NYR	MC804600
C --- LOOP THROUGH CELLS	MC804610
DO 260 IN=1, NRC	MC804620
T=0	MC804630
SUMXT=0	MC804640
SUMVAR=0	MC804650
C --- LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB)	MC804660
DO 200 IT=1, NYR	MC804670
IF(IT .NE. VYR) THEN	MC804680
IF(INV(IN,IT) .NE. 0) THEN	MC804690
X=FTT(INV(IN,IT), Y(IN,IT))	MC804700
C=SQRT(0.5+INV(IN,IT))	MC804710
XX=X+C*(3.141592654/2.0)	MC804720
XT=X/C	MC804730
T=T+1	MC804740
SUMXT=SUMXT+XT	MC804750
IF(XX .LT. 1.001) XX=1.001	MC804760
VARX=AA*(XX**B1)*(XX-1)**B2	MC804770
IF(VARX .GT. 1.0) VARX=1.0	MC804780
VARXT=VARX/(0.5+INV(IN,IT))	MC804790
SUMVAR=SUMVAR+VARXT	MC804800
ENDIF	MC804810
ENDIF	MC804820
200 CONTINUE	MC804830
XTB(IN)=SUMXT/T	MC804840
VXTB(IN)=SUMVAR/T**2	MC804850
260 CONTINUE	MC804860
C	MC804870
C --- CONDUCT ALGORITHM TO FIND XEB	MC804880
CALL EMITER(NRC,XTB,VXTB,XEB,A,MXX,VYR)	MC804890
C	MC804900
C --- COMPUTE MEAN SQUARED ERROR	MC804910
CALL MSE(INV,Y,NRC,NYR,VYR,XEB,L,MXX,MXY,KL)	MC804920
IF(L .LT. MINL) THEN	MC804930
MINL=L	MC804940
MINLK=KL	MC804950
MINLYR=VYR	MC804960
ELSE IF(L .GT. MAXL) THEN	MC804970
MAXL=L	MC804980
MAXLK=KL	MC804990
MAXLYR=VYR	MC805000
ENDIF	MC805010

SUML=SUML+I*KL	MC805020
KLSUM=KLSUM+KL	MC805030
C	MC805040
C --- INVERT XEB TO ORIGINAL SCALE	MC805050
CALL INVERT(NRC,XEB,MXX)	MC805060
C	MC805070
C --- COMPUTE MAD AND CHI SQUARE	MC805080
CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,	MC805090
* FCELLU,FMADU,PMAD,KP)	MC805100
IF(CHI.LT. MINCHI) THEN	MC805110
MINCHI=CHI	MC805120
MNCHIK=K	MC805130
MNCHYR=VYR	MC805140
ELSE IF(CHI.GT. MAXCHI) THEN	MC805150
MAXCHI=CHI	MC805160
MXCHIK=K	MC805170
MXCHYR=VYR	MC805180
ENDIF	MC805190
SUMCHI=SUMCHI+CHI*K	MC805200
KSUM=KSUM+K	MC805210
KPSUM=KPSUM+KP	MC805220
SUMMAD=SUMMAD+PMAD*KP	MC805230
WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD	MC805240
280 CONTINUE	MC805250
C	MC805260
C --- WRITE OUTPUT TO FILE	MC805270
AVGL=SUML/KLSUM	MC805280
AVGCHI=SUMCHI/KSUM	MC805290
AVGMAD=SUMMAD/KPSUM	MC805300
WRITE(11,19)'AVG MAD = ',AVGMAD	MC805310
WRITE(11,21)'CHI SQUARE (ORIG SCALE): '	MC805320
WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYR	MC805330
WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYR	MC805340
WRITE(11,26)'AVG CHI = ',AVGCHI	MC805350
WRITE(11,21)'MEAN SQUARED ERROR (TRANS SCALE): '	MC805360
WRITE(11,25)'MIN MSE = ',MINL,'K = ',MINLK,'VALID YR = ',MINLYR	MC805370
WRITE(11,25)'MAX MSE = ',MAXL,'K = ',MAXLK,'VALID YR = ',MAXLYR	MC805380
WRITE(11,27)'AVG MSE = ',AVGL	MC805390
19 FORMAT(38X,A,F5.3)	MC805400
21 FORMAT(/1X,A)	MC805410
25 FORMAT(1X,A,F6.3,5X,A,I3,5X,A,I2)	MC805420
26 FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)	MC805430
27 FORMAT(1X,A,F6.3)	MC805440
28 FORMAT(17X,A,2X,A)	MC805450
29 FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A)	MC805460
30 FORMAT(1X,8(' - '),2X,4(' - '),2X,14(' - '),2X,13(' - '),2X,5(' - '))	MC805470
31 FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)	MC805480
RETURN	MC805490
END	MC805500
C	MC805510
*****	MC805520
C	MC805530
SUBROUTINE EBITER(NRC,XTB,VXTB,XEB,MXX,VYR)	MC805540
C --- ITERATIVE ALGORITHM TO SOLVE FOR XEB	MC805550
REAL XTB(MXX), VXTB(MXX), XEB(MXX)	MC805560
INTEGER VYR	MC805570

A=0	MC805580
ITER=0	MC805590
100 CONTINUE	MC805600
ITER=ITER+1	MC805610
IF(ITER .GT. 100) PRINT *, 'EBITER GT 100'	MC805620
A0=A	MC805630
SUMALK=0	MC805640
C	MC805650
C --- SUM THE ALPHAS	MC805660
DO 200 I=1,NRC	MC805670
SUMALK=SUMALK+1/(A+VXTB(I))	MC805680
200 CONTINUE	MC805690
C	MC805700
C --- COMPUTE XBB	MC805710
XBB=0	MC805720
DO 300 I=1,NRC	MC805730
ALPHA=1/(A+VXTB(I))	MC805740
GAMMA=ALPHA/SUMALK	MC805750
XBB=XBB+GAMMA*XTB(I)	MC805760
300 CONTINUE	MC805770
C	MC805780
C --- UPDATE VALUE OF A	MC805790
SUMNUM=0	MC805800
SUMDEN=0	MC805810
DO 400 I=1,NRC	MC805820
ALPHA=1/(A+VXTB(I))	MC805830
SUMNUM=SUMNUM+ALPHA*(XTB(I)-XBB)**2	MC805840
SUMDEN=SUMDEN+((XTB(I)-XBB)**2)*ALPHA**2	MC805850
400 CONTINUE	MC805860
A=A-(NRC-1-SUMNUM)/SUMDEN	MC805870
IF(A .LE. 0) THEN	MC805880
A=0	MC805890
GO TO 500	MC805900
ENDIF	MC805910
IF(ABS(A-A0) .GT. 0.0001) GO TO 100	MC805920
500 CONTINUE	MC805930
C	MC805940
C --- ITERATIONS CONVERGED, COMPUTE XEB	MC805950
DO 600 I=1,NRC	MC805960
X=XTB(I)	MC805970
V=VXTB(I)	MC805980
XEB(I)=(A*X)/(A+V)+(V*XBB)/(A+V)	MC805990
600 CONTINUE	MC806000
RETURN	MC806010
END	MC806020
C	MC806030
*****	MC806040
C	MC806050
SUBROUTINE EMITER(NRC,XTB,VXTB,XEM,A,MXX,VYR)	MC806060
C --- ITERATIVE ALGORITHM TO SOLVE FOR XEB FOR EFRON-MORRIS METHOD	MC806070
REAL XTB(MXX), VXTB(MXX), XEM(MXX), A(MXX)	MC806080
INTEGER VYR	MC806090
DO 100 I=1,NRC	MC806100
A(I)=0	MC806110

100 CONTINUE	MC806120
C	MC806130
C --- SUM THE ALPHAS	MC806140
SUMALK=0	MC806150
DO 200 I=1,NRC	MC806160
SUMALK=SUMALK+1/(A(I)+VXTB(I))	MC806170
200 CONTINUE	MC806180
C	MC806190
C --- COMPUTE XHAT	MC806200
XHAT=0	MC806210
DO 300 I=1,NRC	MC806220
ALPHA=1/(A(I)+VXTB(I))	MC806230
GAMMA=ALPHA/SUMALK	MC806240
XHAT=XHAT+GAMMA*XTB(I)	MC806250
300 CONTINUE	MC806260
311 XHATP=XHAT	MC806270
I=1	MC806280
333 AP=A(I)	MC806290
S=(XTB(I)-XHAT)**2	MC806300
C	MC806310
C --- COMPUTE SN AND SD	MC806320
SN=0	MC806330
SD=0	MC806340
DO 400 J=1,NRC	MC806350
IF(J .NE. I) THEN	MC806360
DEN=(A(J)+VXTB(J))**2	MC806370
SN=SN+((XTB(J)-XHAT)**2-VXTB(J))/DEN	MC806380
SD=SD+1/DEN	MC806390
ENDIF	MC806400
400 CONTINUE	MC806410
C	MC806420
C --- NEWTON-RAPHSON ITERATIONS TO SOLVE FOR A	MC806430
444 AD=A(I)+VXTB(I)	MC806440
GNUM=S-3*VXTB(I)+SN*AD**2	MC806450
GDEN=3+SD*AD**2	MC806460
GPRM=2*AD*SN/GDEN-2*GNUM*AD*SD/GDEN**2	MC806470
G=GNUM/GDEN	MC806480
A(I)=A(I)-((A(I)-G)/(1-GPRM))	MC806490
IF(A(I) .LE. 0.) THEN	MC806500
A(I)=0.0	MC806510
I=I+1	MC806520
IF(I .LE. NRC) THEN	MC806530
GO TO 333	MC806540
ELSE	MC806550
GO TO 555	MC806560
ENDIF	MC806570
ENDIF	MC806580
IF(ABS(A(I)-AP) .LE. 0.0001) THEN	MC806590
I=I+1	MC806600
IF(I .LE. NRC) THEN	MC806610
GO TO 333	MC806620
ELSE	MC806630
GO TO 555	MC806640
ENDIF	MC806650
ELSE	MC806660
AP=A(I)	MC806670

GO TO 444	MC806680
ENDIF	MC806690
C	MC806700
C --- TEST FOR CONVERGENCE: ABS(S-SP) LT EPSILON	MC806710
555 SUMALK=0	MC806720
DO 600 J=1,NRC	MC806730
SUMALK=SUMALK+1/(A(J)+VXTB(J))	MC806740
600 CONTINUE	MC806750
XHAT=0	MC806760
DO 700 J=1,NRC	MC806770
ALPHA=1/(A(J)+VXTB(J))	MC806780
GAMMA=ALPHA/SUMALK	MC806790
XHAT=XHAT+GAMMA*XTB(J)	MC806800
700 CONTINUE	MC806810
DO 800 J=1,NRC	MC806820
S=(XTB(J)-XHAT)**2	MC806830
SP=(XTB(J)-XHATP)**2	MC806840
IF(ABS(S-SP) .GT. 0.0001) GO TO 311	MC806850
800 CONTINUE	MC806860
C	MC806870
C --- ITERATIONS CONVERGED, COMPUTE XEM	MC806880
DO 950 K=1,NRC	MC806890
SD=0	MC806900
DO 900 J=1,NRC	MC806910
IF(J .NE. K) SD=SD+1/(A(J)+VXTB(J))**2	MC806920
900 CONTINUE	MC806930
AD=A(K)+VXTB(K)	MC806940
DSTAR=3+(AD**2)*SD	MC806950
B=(1.-4./DSTAR)*VXTB(K)/AD	MC806960
IF(B .GT. 1.0) B=1.0	MC806970
IF(B .LT. 0.0) B=0.0	MC806980
XEM(K)=XHAT+(1-B)*(XTB(K)-XHAT)	MC806990
950 CONTINUE	MC807000
END	MC807010
C	MC807020
*****	MC807030
C	MC807040
SUBROUTINE MSE(INV,Y,NRC,NYR,VYR,XEB,L,MXX,MXY,KL)	MC807050
C --- COMPUTES MEAN SQUARED ERROR MOE	MC807060
REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC807070
REAL L,MU	MC807080
INTEGER VYR	MC807090
SUMSE=0	MC807100
KL=0	MC807110
DO 100 I=1,NRC	MC807120
IF(INV(I,VYR) .GT. 0.0) THEN	MC807130
X=FTT(INV(I,VYR),Y(I,VYR))	MC807140
MU=X/SQRT(0.5+INV(I,VYR))	MC807150
SUMSE=SUMSE+(XEB(I)-MU)**2	MC807160
KL=KL+1	MC807170
ENDIF	MC807180
100 CONTINUE	MC807190
L=SUMSE/KL	MC807200
RETURN	MC807210
END	MC807220
C	MC807230

*****		MC807240
C	SUBROUTINE OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,	MC807250
	* FCELLU,FMADU,PMAD,KP)	MC807260
C ---	COMPUTES MAD AND CHI SQUARE MOES	MC807270
	REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC807280
	INTEGER VYR	MC807290
	CHI=0.0	MC807300
	K=0	MC807310
	SUMPMO=0.0	MC807320
	SUMPMU=0.0	MC807330
	KPMO=0	MC807340
	KPMU=0	MC807350
	DO 100 I=1,NRC	MC807360
	P=XEB(I)	MC807370
	E=P*INV(I,VYR)	MC807380
	A=Y(I,VYR)	MC807390
C		MC807400
C ---	COMPUTE MAD FOR THIS CELL	MC807410
	IF(INV(I,VYR) .GT. 0.0) THEN	MC807420
	PA=A/INV(I,VYR)	MC807430
	IF(P .GT. PA) THEN	MC807440
	SUMPMO=SUMPMO+(P-PA)	MC807450
	KPMO=KPMO+1	MC807460
	ELSE	MC807470
	SUMPMU=SUMPMU+(PA-P)	MC807480
	KPMU=KPMU+1	MC807490
	ENDIF	MC807500
	ENDIF	MC807510
C		MC807520
C ---	COMPUTE CHI SQUARE FOR THIS CELL	MC807530
	IF(E .NE. 0.0 .AND. P .NE. 1.0) THEN	MC807540
	K=K+1	MC807550
	CHI=CHI+((A-E)**2)/(E*(1-P))	MC807560
	ENDIF	MC807570
	100 CONTINUE	MC807580
C		MC807590
C ---	COMPUTE WEIGHTED AVERAGES	MC807600
	KP=KPMO+KPMU	MC807610
	FCELLU=REAL(KPMU)/REAL(KP)	MC807620
	FMADU=SUMPMU/(SUMPMU+SUMPMO)	MC807630
	PMAD=(SUMPMU+SUMPMO)/KP	MC807640
	RETURN	MC807650
	END	MC807660
C		MC807670
		MC807680
*****		MC807690
C	SUBROUTINE INVERT(NRC,XEB,MXX)	MC807700
C ---	INVERT XEB TO ORIGINAL SCALE	MC807710
	REAL XEB(MXX)	MC807720
	DO 100 I=1, NRC	MC807730
	P=0.5*(1+SIN(XEB(I)))	MC807740
	IF (P .LT. 0.0) THEN	MC807750
	P=0.0	MC807760
	ELSE IF (P .GT. 1.0) THEN	MC807770
	P=1.0	MC807780
		MC807790

ENDIF	MC807800
XEB(I)=P	MC807810
100 CONTINUE	MC807820
RETURN	MC807830
END	MC807840
C	MC807850
*****	MC807860
C	MC807870
FUNCTION FTT(INV,Y)	MC807880
C --- CONDUCTS FREMAN-TUKEY TRANSFORM	MC807890
REAL INV,Y	MC807900
TEMP =-1. + 2.*Y/(1.+INV)	MC807910
TEMP1=-1. + 2.*(1.+Y)/(1.+INV)	MC807920
IF(ABS(TEMP).GT.1 .OR. ABS(TEMP1).GT.1) THEN	MC807930
WRITE(6,*) 'FTT ERROR INV,Y=',INV,Y,TEMP,TEMP1	MC807940
FTT=1	MC807950
RETURN	MC807960
ENDIF	MC807970
FTT=SQRT(.5+INV)*.5*(ASIN(TEMP) + ASIN(TEMP1))	MC807980
END	MC807990

D. VECTOR METHOD SUBROUTINE

	SUBROUTINE MC87V(INV,Y,MXX,NYR,NRC,XTBJI,DELTA,X,XVYR,VYRINV,	MC800010
	* VYRY,BSTAR,S,GAMMA,XBBJ,EVAL,MXP,MXK,BKTBL,NBK,NSC,NCSR,ISFLAG)	MC800020
C ---	VECTOR METHOD	MC800030
	REAL INV(MXX,NYR), Y(MXX,NYR)	MC800040
	REAL XTBJI(MXP,MXK), DELTA(MXP,MXK), X(MXP,MXK)	MC800050
	REAL XVYR(MXP,MXK), VYRINV(MXP,MXK), VYRY(MXP,MXK)	MC800060
	REAL BSTAR(MXP,MXP), S(MXP,MXP), GAMMA(MXP,MXP)	MC800070
	REAL XBBJ(MXP), EVAL(MXP)	MC800080
	INTEGER*2 BKTBL(MXX,3)	MC800090
C		MC800100
	REAL MAXL,MINL,L,MAXCHI,MINCHI,MO,MU,MAD	MC800110
	INTEGER T, VYR, P	MC800120
C		MC800130
	MAXL= -1000.0	MC800140
	MINL= 1000.0	MC800150
	SUML= 0.0	MC800160
	KPSUM=0	MC800170
	MAXCHI= -1000.0	MC800180
	MINCHI= 1000.0	MC800190
	SUMCHI= 0.0	MC800200
	KCSUM=0	MC800210
	WRITE(11,32)' '	MC800220
	WRITE(11,21)'EMP BAYES TRANS SCALE - VECTOR CASE:'	MC800230
	IF (ISFLAG.EQ. 1) THEN	MC800240
	P=NSC	MC800250
	WRITE(11,21)'VECTOR IS BY SERVICE COMPONENT'	MC800260
	ELSE	MC800270
	P=NCSR	MC800280
	WRITE(11,21)'VECTOR IS BY COMMISSIONING SOURCE'	MC800290
	ENDIF	MC800300
	WRITE(11,22)'K=',NRC,'P=',P,'KP= ',(NRC*P)	MC800310
	WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE):'	MC800320
	WRITE(11,28)'FRACTION CELLS','FRACTION MAD'	MC800330
	WRITE(11,29)'VALID YR','KP','WITH UNDERAGE','FROM UNDERAGE','MAD'	MC800340
	WRITE(11,30)	MC800350
	K=NRC	MC800360
	IF(K.LE. (P+2)) THEN	MC800370
	WRITE(6,*)'*** ERROR IN VECTOR CASE: P+2 GT K ***'	MC800380
	STOP	MC800390
	ENDIF	MC800400
C		MC800410
C ---	CONDUCT VALIDATION	MC800420
	DO 999 VYR=1, NYR	MC800430
	DO 90 J=1,MXP	MC800440
	DO 80 I=1,MXK	MC800450
	XTBJI(J,I)=0.0	MC800460
	DELTA(J,I)=0.0	MC800470
	XVYR(J,I)=0.0	MC800480
80	CONTINUE	MC800490
90	CONTINUE	MC800500
	KMKG=BKTBL(1,1)	MC800510
	NRC=1	MC800520
C ---	LOOP THROUGH CELLS IN VECTOR FORM	MC800530

DO 130	I=1,NBK	MC800540
	IF(BKTBL(I,1) .NE. KMKG) NRC=NRC+1	MC800550
DO 100	J=1,P	MC800560
	IF(BKTBL(I,2) .EQ. J) THEN	MC800570
	JP=J	MC800580
	GO TO 110	MC800590
	ENDIF	MC800600
100	CONTINUE	MC800610
	WRITE(6,*) '*** ERROR IN P VECTOR ASSIGNMENT ***'	MC800620
110	T=0	MC800630
	SUMXT=0	MC800640
	SUMVAR=0	MC800650
C ---	LOOP THROUGH YEARS OF DATA TO SOLVE FOR XTB AND VAR(XTB)	MC800660
	DO 120 IT=1, NYR	MC800670
	IF(IT .NE. VYR) THEN	MC800680
	IF(INV(I,IT) .NE. 0) THEN	MC800690
	XIJ=FTTV(INV(I,IT), Y(I,IT))	MC800700
	C=0.5+INV(I,IT)	MC800710
	XT=XIJ/SQRT(C)	MC800720
	SUMXT=SUMXT+XT	MC800730
	SUMVAR=SUMVAR+1/C	MC800740
	T=T+1	MC800750
	ENDIF	MC800760
	ENDIF	MC800770
120	CONTINUE	MC800780
	XTBJI(JP,NRC)=SUMXT/T	MC800790
C ---	STORE VARIANCE MATRIX IN DELTA MATRIX (TEMPORARY)	MC800800
	DELTA(JP,NRC)=SUMVAR/T**2	MC800810
C ---	GET VALIDATION YEAR ESTIMATE, INVENTORY AND ATTRITION INFO	MC800820
	IF(INV(I,VYR) .GT. 0.0) THEN	MC800830
	XIJ=FTTV(INV(I,VYR), Y(I,VYR))	MC800840
	XT=XIJ/SQRT(0.5+INV(I,VYR))	MC800850
	XVYR(JP,NRC)=XT	MC800860
	ENDIF	MC800870
	VYRINV(JP,NRC)=INV(I,VYR)	MC800880
	VYRY(JP,NRC)=Y(I,VYR)	MC800890
	KMKG=BKTBL(I,1)	MC800900
130	CONTINUE	MC800910
	IF(K .NE. NRC) THEN	MC800920
	WRITE(6,*) '*** ERROR IN VECTOR CASE: K NE NRC ***'	MC800930
	ENDIF	MC800940
C		MC800950
C ---	COMPUTE XBB SUB J	MC800960
	DO 210 J=1,P	MC800970
	SUMXTB=0.0	MC800980
	DO 200 I=1,K	MC800990
	SUMXTB=SUMXTB+XTBJI(J,I)	MC801000
200	CONTINUE	MC801010
	XBBJ(J)=SUMXTB/K	MC801020
210	CONTINUE	MC801030
C		MC801040
C ---	COMPUTE X SUB JI MATRIX, MAKE A COPY IN DELTA MATRIX (TEMPORARY)	MC801050
	DO 230 J=1,P	MC801060
	DO 220 I=1,K	MC801070
	X(J,I)=(XTBJI(J,I)-XBBJ(J))*SQRT(DELTA(J,I))	MC801080
	DELTA(J,I)=X(J,I)	MC801090

220	CONTINUE	MC801100
230	CONTINUE	MC801110
C		MC801120
C	--- COMPUTE S MATRIX	MC801130
	CALL MXYTF(P,K,X,MXP,P,K,DELTA,MXP,P,P,S,MXP)	MC801140
C		MC801150
C	--- DO EIGENANALYSIS OF S	MC801160
C	--- PUT EIGENVALUES INTO EVAL, EIGENVECTORS INTO GAMMA	MC801170
	CALL EVCSF(P,S,MXP,EVAL,GAMMA,MXP)	MC801180
C		MC801190
C	--- CREATE ESTAR INVERSE	MC801200
	KP2=K-P-2	MC801210
	DO 240 J=1,P	MC801220
	IF(EVAL(J).LT. KP2) THEN	MC801230
	EVAL(J)=KP2	MC801240
	ENDIF	MC801250
	EVAL(J)=1.0/EVAL(J)	MC801260
240	CONTINUE	MC801270
	DO 260 I=1,P	MC801280
	DO 250 J=1,P	MC801290
	IF(I.EQ. J) THEN	MC801300
	BSTAR(I,J)=EVAL(J)	MC801310
	ELSE	MC801320
	BSTAR(I,J)=0.0	MC801330
	ENDIF	MC801340
250	CONTINUE	MC801350
260	CONTINUE	MC801360
C		MC801370
C	--- CREATE BSTAR = I - (K-P-2) S TILDE INVERSE	MC801380
	CALL MRRRR(P,P,GAMMA,MXP,P,P,BSTAR,MXP,P,P,S,MXP)	MC801390
	CALL MXYTF(P,P,S,MXP,P,P,GAMMA,MXP,P,P,BSTAR,MXP)	MC801400
	DO 280 I=1,P	MC801410
	DO 270 J=1,P	MC801420
	BSTAR(I,J)=KP2*BSTAR(I,J)	MC801430
	IF(I.EQ. J) THEN	MC801440
	BSTAR(I,J)=1.0-BSTAR(I,J)	MC801450
	ELSE	MC801460
	BSTAR(I,J)=0.0-BSTAR(I,J)	MC801470
	ENDIF	MC801480
270	CONTINUE	MC801490
280	CONTINUE	MC801500
C		MC801510
C	--- COMPUTE DELTA SUB JI	MC801520
	DO 300 J=1,P	MC801530
	DO 290 I=1,K	MC801540
	X(J,I)=XTBJI(J,I)-XBBJ(J)	MC801550
290	CONTINUE	MC801560
300	CONTINUE	MC801570
	CALL MRRRR(P,P,BSTAR,MXP,P,K,X,MXP,P,K,XTBJI,MXP)	MC801580
	DO 320 J=1,P	MC801590
	DO 310 I=1,K	MC801600
	DELTA(J,I)=XBBJ(J)+XTBJI(J,I)	MC801610
310	CONTINUE	MC801620
320	CONTINUE	MC801630
C		MC801640
C	--- COMPUTE MSE	MC801650

KP=0	MC801660
SUMSE=0.0	MC801670
DO 340 J=1,P	MC801680
DO 330 I=1,K	MC801690
IF(INV(I,VYR) .GT. 0.0) THEN	MC801700
SUMSE=SUMSE+(DELTA(J,I)-XVYR(J,I))**2	MC801710
KP=KP+1	MC801720
ENDIF	MC801730
330 CONTINUE	MC801740
340 CONTINUE	MC801750
L=SUMSE/KP	MC801760
IF(L .LT. MINL) THEN	MC801770
MINL=L	MC801780
MINLKP=KP	MC801790
MINLYR=VYR	MC801800
ELSE IF(L .GT. MAXL) THEN	MC801810
MAXL=L	MC801820
MAXLKP=KP	MC801830
MAXLYR=VYR	MC801840
ENDIF	MC801850
SUML=SUML+L*KP	MC801860
KPSUM=KPSUM+KP	MC801870
C	MC801880
C --- INVERT DELTA SUB JI BACK TO ORIGINAL SCALE	MC801890
DO 360 J=1,P	MC801900
DO 350 I=1,K	MC801910
PHAT=0.5*(1+SIN(DELTA(J,I)))	MC801920
IF (PHAT .LT. 0.0) THEN	MC801930
PHAT=0.0	MC801940
ELSE IF (PHAT .GT. 1.0) THEN	MC801950
PHAT=1.0	MC801960
ENDIF	MC801970
DELTA(J,I)=PHAT	MC801980
350 CONTINUE	MC801990
360 CONTINUE	MC802000
C	MC802010
C --- COMPUTE CHI SQUARE AND MAD	MC802020
CHI=0.0	MC802030
KCHI=0	MC802040
SUMPMO=0.0	MC802050
SUMPMU=0.0	MC802060
KPMO=0	MC802070
KPMU=0	MC802080
DO 410 J=1,P	MC802090
DO 400 I=1,K	MC802100
PHAT=DELTA(J,I)	MC802110
E=PHAT*VYRINV(J,I)	MC802120
A=VYRY(J,I)	MC802130
IF(VYRINV(J,I) .GT. 0.0) THEN	MC802140
PACT=A/VYRINV(J,I)	MC802150
IF(PHAT .GT. PACT) THEN	MC802160
SUMPMO=SUMPMO+(PHAT-PACT)	MC802170
KPMO=KPMO+1	MC802180
ELSE	MC802190
SUMPMU=SUMPMU+(PACT-PHAT)	MC802200
KPMU=KPMU+1	MC802210

ENDIF	MC802220
ENDIF	MC802230
IF(E.NE.0.0 .AND. PHAT.NE.1.0) THEN	MC802240
KCHI=KCHI+1	MC802250
CHI=CHI+((A-E)**2)/(E*(1-PHAT))	MC802260
ENDIF	MC802270
400 CONTINUE	MC802280
410 CONTINUE	MC802290
KMAD=KPMO+KPMU	MC802300
FCELLU=REAL(KPMU)/REAL(KMAD)	MC802310
FMADU=SUMPMU/(SUMPMU+SUMPMO)	MC802320
PMAD=(SUMPMU+SUMPMO)/KMAD	MC802330
IF(CHI .LT. MINCHI) THEN	MC802340
MINCHI=CHI	MC802350
MNCHIK=KCHI	MC802360
MNCHYR=VYR	MC802370
ELSE IF(CHI .GT. MAXCHI) THEN	MC802380
MAXCHI=CHI	MC802390
MXCHIK=KCHI	MC802400
MXCHYR=VYR	MC802410
ENDIF	MC802420
SUMCHI=SUMCHI+CHI*KCHI	MC802430
KCSUM=KCSUM+KCHI	MC802440
WRITE(11,31) VYR,KMAD,FCELLU,FMADU,PMAD	MC802450
999 CONTINUE	MC802460
AVGL=SUML/KPSUM	MC802470
AVGCHI=SUMCHI/KCSUM	MC802480
WRITE(11,21)'CHI SQUARE (ORIG SCALE): '	MC802490
WRITE(11,26)'MIN CHI = ',MINCHI,'KP = ',MNCHIK,	MC802500
* 'VALID YR = ',MNCHYR	MC802510
WRITE(11,26)'MAX CHI = ',MAXCHI,'KP = ',MXCHIK,	MC802520
* 'VALID YR = ',MXCHYR	MC802530
WRITE(11,26)'AVG CHI = ',AVGCHI	MC802540
WRITE(11,21)'MEAN SQUARED ERROR (TRANS SCALE): '	MC802550
WRITE(11,25)'MIN MSE = ',MINL,'KP = ',MINLKP,'VALID YR = ',MINLYR	MC802560
WRITE(11,25)'MAX MSE = ',MAXL,'KP = ',MAXLKP,'VALID YR = ',MAXLYR	MC802570
WRITE(11,27)'AVG MSE = ',AVGL	MC802580
21 FORMAT(/1X,A)	MC802590
22 FORMAT(1X,3(A,I3,5X))	MC802600
25 FORMAT(1X,A,F6.3,5X,A,I3,5X,A,I2)	MC802610
26 FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)	MC802620
27 FORMAT(1X,A,F6.3/)	MC802630
28 FORMAT(17X,A,2X,A)	MC802640
29 FORMAT(1X,A,3X,A,3X,A,2X,A,3X,A)	MC802650
30 FORMAT(1X,8(' - '),2X,4(' - '),2X,14(' - '),2X,13(' - '),2X,5(' - '))	MC802660
31 FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)	MC802670
32 FORMAT(1X,A)	MC802680
WRITE(6,*)'COMPLETED VECTOR CASE'	MC802690
END	MC802700
C	MC802710
*****	MC802720
C	MC802730
FUNCTION FTTV(INV,Y)	MC802740
C --- CONDUCTS FREMAN-TUKEY TRANSFORM	MC802750
REAL INV,Y	MC802760
TEMP =-1. + 2.*Y/(1.+INV)	MC802770

```

TEMP1=-1. + 2.*(1.+Y)/(1.+INV)
IF(ABS(TEMP).GT.1 .OR. ABS(TEMP1).GT.1) THEN
    WRITE(6,*) 'FTT ERROR INV,Y=',INV,Y,TEMP,TEMP1
    FTT=1
    RETURN
ENDIF
FTTV=SQRT(.5+INV)*.5*(ASIN(TEMP) + ASIN(TEMP1))
END

```

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MC802780
MC802790
MC802800
MC802810
MC802820
MC802830
MC802840
MC802850

```

E. EXEC PROGRAM

```
CP LINK MVS 103 103 RR
ACC 103 K
*****
FIL * CLEAR
FIL 01 K DSN F0968 MCOR87 DATA (RECFM FB LRECL 69 BLOCK 17940
FIL 02 DISK MC87 TEMP
FIL 06 &1 (RECFM FBA LRECL 150
FIL 25 DISK MCLASS PG15 (RECFM F LRECL 25
FIL 27 DISK MCLASS PG17 (RECFM F LRECL 25
FIL 29 DISK MCLASS PG19 (RECFM F LRECL 25
FIL 30 DISK MCLASS PG20 (RECFM F LRECL 25
FIL 31 DISK MCLASS PG21 (RECFM F LRECL 25
FIL 32 DISK MCLASS PG22 (RECFM F LRECL 25
&BEGSTACK
30.0 /* AVG INV THRESHOLD T */
30 /* NO. CELLS THRESHOLD K */
13 /* MOS (ONLY 1) */
4 /* YCS (ONLY 1) */
15 /* GRADE (ONLY 1) */
3 1 2 3 /* NO. SVC COMPS AND ARRAY(1-REG,2-AUGREG,3-RES,4=1+2,5=ALL */
1 16 /* NO. COMM SRCS AND ARRAY(1-15, 16=ALL)
1 /* 3RD DIMENSION (0=NONE, 1=SVC, 2=CS)
&END
LOAD MC87 (START CLEAR
```

F. SAMPLE DATA FILE

1	2	3	4	5	6	7
--	-	-	-	--	-	----
15	0	1	1	15	1	0.02
15	0	3	2	9	5	0.42
15	0	3	3	9	6	0.75
15	0	3	2	10	4	0.15
15	0	3	1	11	1	0.10
15	0	3	3	10	2	0.15
15	0	3	3	3	1	0.02
15	0	3	3	4	1	0.02
15	0	4	2	9	6	0.87
15	0	4	2	10	2	0.20
15	0	4	3	9	2	0.07
15	0	4	1	11	1	0.10
15	0	4	3	4	2	0.05
15	0	4	3	10	1	0.10
15	0	5	2	9	3	0.27
15	0	5	2	10	2	0.20
15	0	5	1	11	1	0.07
15	0	6	2	9	1	0.02
15	1	2	3	15	1	0.05
15	1	3	1	1	2	0.20
15	1	3	3	15	1	0.05
15	1	3	3	10	1	0.10
15	1	3	3	7	3	0.12
15	1	3	3	3	5	0.30
15	1	3	3	5	2	0.65
15	1	3	3	2	5	0.45
15	1	3	3	9	3	0.12
15	1	3	2	15	1	0.05
15	1	3	1	11	3	0.12
15	1	3	1	10	2	0.10
15	1	3	2	7	1	0.02
15	1	3	3	6	1	0.10
15	1	4	3	5	2	0.12
15	1	4	3	2	5	0.40
15	1	4	2	3	2	0.12
15	1	4	1	1	1	0.02
15	1	4	2	9	2	0.07
15	1	4	3	9	1	0.02
15	1	4	3	7	5	0.25
15	1	4	3	10	1	0.02
15	1	4	3	3	2	0.05
15	1	4	1	10	1	0.02
15	1	4	3	12	1	0.02
15	1	4	2	12	1	0.07

(remaining entries omitted)

Column descriptions:

1 - grade	5 - commissioning source
2 - MOS	6 - number of records
3 - YCS	7 - total average inventory
4 - service component	

C --- PROGRAM TO CREATE INVENTORY DATA FILE BY GRADE	MC800010
PARAMETER (MXX=20000, MXY=10)	MC800020
C --- CLASSIF. TABLE: GRADE, MOS, YCS, SVC, CS	MC800030
INTEGER*2 PTRTBL(MXX, 5), NRECS(MXX)	MC800040
REAL AINV(MXX)	MC800050
INTEGER TYPE,YCS,PG,MOS,SEX,CS,EDLV,SVC,MOS1,MOS2,RACE	MC800060
INTEGER DATA(MXY), SPG	MC800070
CHARACTER*7 CITLS	MC800080
DATA AINV/MXX*0./, NRECS/MXX*0/	MC800090
C	MC800100
WRITE(5,*) 'ENTER PG'	MC800110
READ(5,*) SPG	MC800120
WRITE(5,*) 'PG TO USE=',SPG	MC800130
ICR=0	MC800140
NRC=0	MC800150
NG=0	MC800160
DO 10 I=1,999999	MC800170
READ(1,100,END=999) TYPE,YCS,PG,MOS,SEX,CS,EDLV,SVC,MOS1,MOS2,	MC800180
* RACE,CITLS,DATA	MC800190
ICR=ICR+1	MC800200
C --- CLASSIFY ALL RECORDS TYPE 0	MC800210
IF(TYPE.GT.0) GO TO 999	MC800220
C --- ADD NEW RECORD TO TABLE	MC800230
IF(PG.EQ.SPG) CALL ADDTBL(PG,MOS,YCS,SVC,CS, DATA,MXY, PTRTBL,	MC800240
* MXX, NRC,AINV,NRECS)	MC800250
IF(PG.EQ.SPG) NG=NG+1	MC800260
IF(MOD(ICR,5000).EQ.0) WRITE(6,*) 'ICR,NRC=',ICR,NRC	MC800270
10 CONTINUE	MC800280
C	MC800290
999 CONTINUE	MC800300
WRITE(6,*) ' '	MC800310
WRITE(6,*) 'TOTAL RECORDS READ =',ICR	MC800320
WRITE(6,*) 'TOTAL RECORDS ACCEPTED =',NG	MC800330
WRITE(6,*) 'TOTAL INVENTORY COMBINATIONS =',NRC	MC800340
DO 20 I=1,NRC	MC800350
WRITE(2,101) (PTRTBL(I,J),J=1,5), NRECS(I),AINV(I)	MC800360
20 CONTINUE	MC800370
100 FORMAT(3I2,I3,I1,I2,2I1,2I3,I1,A7, 1X, 10I4)	MC800380
101 FORMAT(I2,I4,I3,I2,I3, I4, F7.2)	MC800390
END	MC800400
C	MC800410
SUBROUTINE ADDTBL(PG,MOS,YCS,SVC,CS, DATA,MXY, PTRTBL,MXX, NRC,	MC800420
* AINV,NRECS)	MC800430
C --- SET INVENTORY POINTER FOR THIS ENTRY AND ACCUMULATE	MC800440
INTEGER*2 PTRTBL(MXX, 5), NRECS(MXX)	MC800450
REAL AINV(MXX)	MC800460
INTEGER YCS,PG,MOS,CS,SVC	MC800470
INTEGER DATA(MXY)	MC800480
MINV=GETINV(PTRTBL, MXX,NRC, PG,MOS,YCS,SVC,CS)	MC800490
IF(MINV.EQ.0) THEN	MC800500
C --- NEW COMBINATION	MC800510
NRC=NRC+1	MC800520
IF(NRC.GT.MXX) THEN	MC800530
WRITE(6,*) '*** ERROR - TOO MANY INV. COMBINATIONS',NRC	MC800540
STOP	MC800550
ENDIF	MC800560

MINV=NRC	MC800570
PTRTBL(MINV, 1)=PG	MC800580
PTRTBL(MINV, 2)=MOS	MC800590
PTRTBL(MINV, 3)=YCS	MC800600
PTRTBL(MINV, 4)=SVC	MC800610
PTRTBL(MINV, 5)=CS	MC800620
NRECS(MINV)=0	MC800630
ENDIF	MC800640
AI=0	MC800650
DO 110 IT=1, MXY	MC800660
AI=AI + FLOAT(DATA(IT))	MC800670
110 CONTINUE	MC800680
AINV(MINV)=AINV(MINV) + .25*AI/MXY	MC800690
NRECS(MINV)=NRECS(MINV) + 1	MC800700
END	MC800710
C ---	MC800720
FUNCTION GETINV(PTRTBL, MXX, NRC, PG, MOS, YCS, SVC, CS)	MC800730
C --- FIND LOCATION OF MATCHING INVENTORY ENTRY FOR A LOSS	MC800740
INTEGER*2 PTRTBL(MXX, 5)	MC800750
INTEGER YCS, PG, MOS, CS, SVC	MC800760
DO 10 I=1, NRC	MC800770
IF(PTRTBL(I, 1) .EQ. PG .AND.	MC800780
* PTRTBL(I, 2) .EQ. MOS .AND.	MC800790
* PTRTBL(I, 3) .EQ. YCS .AND.	MC800800
* PTRTBL(I, 4) .EQ. SVC .AND.	MC800810
* PTRTBL(I, 5) .EQ. CS) THEN	MC800820
	MC800830
	MC800840
	MC800850
10 CONTINUE	MC800860
GETINV=0	MC800870
END	MC800880

GETINV=I
RETURN

APPENDIX C. SAMPLE OUTPUT

A. GENERAL

This appendix contains sample output from the computer program. A sample output for test cases one through 30 which use the first five estimation methods is shown in paragraph B. A sample output for the vector test cases is shown in paragraph C. These examples show the output that is produced by the WRITE statements for file definition 11, e.g., WRITE(11,101). The program also contains several WRITE and PRINT statements that provide interactive information to the user via the terminal screen, e.g., WRITE(6,*), WRITE(5,*) and PRINT *. This interactive output is omitted.

B. SAMPLE OUTPUT (TEST CASES 1-30)

TEST CASE INPUT PARAMETERS:

```
INVENTORY THRESHOLD= 30.0      THRESHOLD NO. OF CELLS= 30
MOS= 13      YCS= 4      GRADE= 15
SERVICE COMPONENTS= 1 2 3
COMM SOURCES= 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
```

EXPANSION INFORMATION:

```
ACTUAL NO. OF CELLS USED= 24
MOS GROUP # 1 YCS'S USED=
  4  5
LARGE MOS GROUP #1 YCS'S USED=
  4  5
MAJOR MOS GROUP #1 YCS'S USED=
  4  5
```

EMP BAYES TRANS SCALE - TIME DEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION MAD FROM UNDERAGE	MAD
1	24	0.458	0.478	0.127
2	24	0.250	0.187	0.099
3	24	0.542	0.441	0.098
4	24	0.333	0.375	0.069
5	24	0.417	0.352	0.072
6	24	0.125	0.053	0.082
7	24	0.208	0.138	0.099
8	24	0.417	0.472	0.077
9	24	0.833	0.943	0.181
10	24	0.833	0.952	0.113
				AVG MAD = 0.102

CHI SQUARE (ORIG SCALE):

MIN CHI = 48.590 K = 24 VALID YR = 8
 MAX CHI = 329.334 K = 24 VALID YR = 9
 AVG CHI = 98.791

MEAN SQUARED ERROR (TRANS SCALE):

MIN MSE = 0.033 K = 24 VALID YR = 4
 MAX MSE = 0.205 K = 24 VALID YR = 9
 AVG MSE = 0.079

EMP BAYES TRANS SCALE - TIME INDEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION MAD FROM UNDERAGE	MAD
1	24	0.458	0.504	0.127
2	24	0.250	0.204	0.094
3	24	0.583	0.477	0.101
4	24	0.375	0.432	0.071
5	24	0.417	0.396	0.073
6	24	0.083	0.061	0.076
7	24	0.250	0.152	0.094
8	24	0.458	0.517	0.075
9	24	0.792	0.952	0.183
10	24	0.875	0.961	0.118

AVG MAD = 0.101

CHI SQUARE (ORIG SCALE):

MIN CHI = 45.452 K = 24 VALID YR = 6
 MAX CHI = 344.445 K = 24 VALID YR = 9
 AVG CHI = 99.284

MEAN SQUARED ERROR (TRANS SCALE):

MIN MSE = 0.036 K = 24 VALID YR = 4
 MAX MSE = 0.213 K = 24 VALID YR = 9
 AVG MSE = 0.078

EMP BAYES ORIG SCALE - TIME DEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION MAD FROM UNDERAGE	MAD
1	24	0.453	0.478	0.127
2	24	0.250	0.195	0.097
3	24	0.542	0.461	0.093
4	24	0.333	0.397	0.070
5	24	0.417	0.375	0.074
6	24	0.125	0.057	0.079
7	24	0.208	0.161	0.102
8	24	0.417	0.488	0.079
9	24	0.833	0.944	0.185
10	24	0.833	0.952	0.117

AVG MAD = 0.102

CHI SQUARE (ORIG SCALE):

MIN CHI =	49.207	K = 24	VALID YR = 6
MAX CHI =	340.035	K = 24	VALID YR = 9
AVG CHI =	100.985		

EMP BAYES ORIG SCALE - TIME INDEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION FROM UNDERAGE	MAD
1	24	0.458	0.479	0.127
2	24	0.250	0.196	0.097
3	24	0.542	0.462	0.093
4	24	0.333	0.399	0.070
5	24	0.417	0.377	0.075
6	24	0.125	0.056	0.079
7	24	0.208	0.161	0.101
8	24	0.417	0.490	0.079
9	24	0.833	0.945	0.185
10	24	0.833	0.953	0.117
				AVG MAD = 0.102

CHI SQUARE (ORIG SCALE):

MIN CHI =	48.836	K = 24	VALID YR = 6
MAX CHI =	339.835	K = 24	VALID YR = 9
AVG CHI =	100.960		

EFRON-MORRIS TRANS SCALE - TIME DEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION FROM UNDERAGE	MAD
1	24	0.458	0.475	0.126
2	24	0.250	0.172	0.095
3	24	0.583	0.451	0.102
4	24	0.375	0.365	0.076
5	24	0.333	0.348	0.076
6	24	0.083	0.046	0.082
7	24	0.208	0.135	0.098
8	24	0.458	0.469	0.076
9	24	0.708	0.938	0.185
10	24	0.875	0.960	0.115
				AVG MAD = 0.103

CHI SQUARE (ORIG SCALE):

MIN CHI =	46.301	K = 24	VALID YR = 8
MAX CHI =	340.712	K = 24	VALID YR = 9
AVG CHI =	101.231		

MEAN SQUARED ERROR (TRANS SCALE):

MIN MSE =	0.042	K = 24	VALID YR = 4
MAX MSE =	0.211	K = 24	VALID YR = 9
AVG MSE =	0.080		

C. SAMPLE OUTPUT (VECTOR TEST CASES)

TEST CASE INPUT PARAMETERS:

INVENTORY THRESHOLD= 30.0 THRESHOLD NO. OF CELLS= 30
 MOS= 151 YCS= 7 GRADE= 17
 SERVICE COMPONENTS= 1 2 3
 COMM SOURCES= 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15

EXPANSION INFORMATION:

ACTUAL NO. OF CELLS USED= 8
 MOS GROUP # 8 YCS'S USED= 7
 LARGE MOS GROUP #3 YCS'S USED= 7
 MAJOR MOS GROUP #2 YCS'S USED= 7

EMP BAYES TRANS SCALE - VECTOR CASE:

VECTOR IS BY SERVICE COMPONENT

K= 8 P= 3 KP= 24

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	KP	FRACTION CELLS WITH UNDERAGE	FRACTION MAD FROM UNDERAGE	MAD
1	24	0.375	0.219	0.186
2	24	0.458	0.375	0.179
3	24	0.458	0.417	0.130
4	24	0.458	0.422	0.127
5	24	0.542	0.708	0.146
6	24	0.292	0.310	0.142
7	24	0.250	0.193	0.126
8	24	0.375	0.434	0.092
9	24	0.458	0.705	0.161
10	24	0.792	0.912	0.202

CHI SQUARE (ORIG SCALE):

MIN CHI = 27.827 KP = 24 VALID YR = 8
 MAX CHI = 165.694 KP = 24 VALID YR = 10
 AVG CHI = 61.025

MEAN SQUARED ERROR (TRANS SCALE):

MIN MSE = 0.089 KP = 24 VALID YR = 8
 MAX MSE = 0.483 KP = 24 VALID YR = 10
 AVG MSE = 0.229

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