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**NONLINEAR STRESS ANALYSIS OF  
COMPOSITE-JACKETED STEEL CYLINDERS  
SUBJECTED TO HIGH INTERNAL PRESSURE**

PETER C.T. CHEN

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## INTRODUCTION

Weight reduction is a requirement for a majority of weapon systems being developed by the Army. The Army would like to design longer cannon and maintain the inertia characteristics of the shorter cannon. This accomplishment would allow current cannon mounts to be used. The longer cannon is expected to achieve higher muzzle velocity and greater accuracy than the standard cannon. The design under consideration is to replace a portion of the steel wall thickness with a lighter material. The inner portion, steel liner, maintains the tube projectile interface and shields the composite from the extremely hot gases. The outer portion, composite jacket, is made of a fiber-reinforced organic composite (graphite fiber and a bismaleimide matrix). A linear stress analysis for this problem under internal pressure in the elastic range was reported in a recent paper by M.D. Witherell and M.A. Scavullo (ref 1).

This report presents a nonlinear stress analysis of the compound tube problem. The loading ranges include elastic, elastic-plastic, and fully-plastic up to failure. Analytical expressions for the stresses, strains, and displacements are derived for all cases. Numerical results for the radial and hoop stresses in the nonlinear loading ranges are presented. The maximum value of internal pressure that the compound tube can contain without failure is predicted.

## PROBLEM AND ELASTIC ANALYSIS

Figure 1 shows a schematic of the compound tube problem. The compound tube consists of an inner steel "liner" and an outer composite "jacket." The steel liner of inside radius  $a$  and outer radius  $b$  is wrapped in the circumferential direction with a graphite-bismaleimide organic composite of outside radius  $c$ .

The elastic material constants for the composite and the steel are given in Table 1.

TABLE 1. ELASTIC CONSTANTS OF COMPOSITE JACKET AND STEEL LINER

Elastic Constants for IM6/Bismaleimide, 55% F.V.R.		
$E_r = 1.126 \text{ Mpsi}$ (7.758 Gpa)	$\nu_{r\theta} = 0.01524$	$\nu_{\theta r} = 0.3155$
$E_\theta = 23.31 \text{ Mpsi}$ (160.61 Gpa)	$\nu_{\theta z} = 0.3155$	$\nu_{z\theta} = 0.01524$
$E_z = 1.126 \text{ Mpsi}$ (7.758 Gpa)	$\nu_{zr} = 0.3991$	$\nu_{rz} = 0.3911$
Elastic Constants for Steel		
$E = 30.0 \text{ Mpsi}$ (206.7 Gpa)	$\nu = 0.3$	

When the composite tube is subjected to internal pressure  $p$  in the elastic range, the general solutions in the plane-strain condition for the isotropic liner ( $a \leq r \leq b$ ) are

$$\sigma_r \quad (1)$$

$$\sigma_\theta = \{ \mp(p-q) \left(\frac{b}{r}\right)^2 + p - q b^2/a^2 \} / \left(\frac{b^2}{a^2} - 1\right) \quad (2)$$

$$u/r = E^{-1}(1+\nu) [ (p-q)(b/r)^2 + (1-2\nu)(p-q b^2/a^2) ] / \left(\frac{b^2}{a^2} - 1\right) \quad (3)$$

and for the orthotropic jacket ( $b \leq r \leq c$ ),

$$\sigma_r = q \left[ - \left(\frac{c}{b}\right)^{k-1} \left(\frac{c}{r}\right)^{k+1} + \left(\frac{r}{b}\right)^{k-1} \right] / \left[ (c/b)^{2k} - 1 \right] \quad (4)$$

$$\sigma_\theta = kq \left[ (c/b)^{k-1} \left(\frac{c}{r}\right)^{k+1} + \left(\frac{r}{b}\right)^{k-1} \right] / \left[ (c/b)^{2k} - 1 \right] \quad (5)$$

$$u/r = \epsilon_\theta = \alpha_{12}\sigma_r + \alpha_{22}\sigma_\theta \quad (6)$$

where  $q$  is the pressure at the interface,  $k = (\alpha_{11}/\alpha_{22})^{1/2}$ ,

$$\alpha_{11} = (1-\nu_{rz}\nu_{zr})/E_r$$

$$\alpha_{12} = -(\nu_{\theta r} + \nu_{\theta z}\nu_{zr})/E_\theta$$

$$\alpha_{22} = (1-\nu_{\theta z}\nu_{z\theta})/E_\theta \quad (7)$$

By requiring the displacement to be continuous at the interface, the interface pressure  $q$  can be expressed as a linear function of internal pressure  $p$ ,

$$\frac{2p}{q} = \left(\frac{b^2}{a^2} - 1\right) \left[ AK \frac{(c/b)^{2k} + 1}{(c/b)^{2k} - 1} + B \right] + \frac{b^2}{a^2} + 1 \quad (8)$$

where

$$A = E\alpha_{22}/(1-\nu^2), \quad B = -E\alpha_{12}/(1-\nu^2) - \nu/(1-\nu) \quad (9)$$

Now all the stresses, strains, and displacements in the tube ( $a \leq r \leq c$ ) can be determined as functions of  $p$ . In particular, the expressions for the displacements at the bore ( $u_a$ ), interface ( $u_b$ ), and outside surface ( $u_c$ ) are

$$\left(\frac{b^2}{a^2} - 1\right) \frac{E}{p} \frac{u_a}{a} = (1+\nu) \frac{b^2}{a^2} + (1-\nu-2\nu^2) - \frac{4(1-\nu^2)(b^2/a^2)}{\left(\frac{b^2}{a^2} - 1\right) \left[ AK \frac{(c/b)^{2k} + 1}{(c/b)^{2k} - 1} + B \right] + \frac{b^2}{a^2} + 1} \quad (10)$$

$$\frac{u_b}{b} = q \left[ k\alpha_{22} \frac{(c/b)^{2k} + 1}{(c/b)^{2k} - 1} - \alpha_{12} \right] \quad (11)$$

$$\frac{u_c}{c} = \frac{2qk\alpha_{22}(c/b)^{k-1}}{(c/b)^{2k} - 1} \quad (12)$$

### ELASTIC-PLASTIC ANALYSIS

When the internal pressure  $p$  is large enough, part of the steel liner will become plastic. Using Tresca's yield criterion, the associated flow rule, and assuming linear strain-hardening, the elastic-plastic solution based on Bland can be used (refs 2,3). Let  $\rho$  be the elastic-plastic interface.

The solution can be written in the elastic portion ( $\rho \leq r \leq b$ ) as

$$\frac{E}{\sigma_0} \frac{u}{r} = \frac{1+\nu}{2} \frac{\rho^2}{r^2} + (1-\nu-2\nu^2) \left[ \frac{1}{2} \frac{\rho^2}{b^2} - \frac{q}{\sigma_0} \right] \quad (13)$$

$$\sigma_r/\sigma_0 \quad (14)$$

$$= \frac{1}{2} \left( \mp \frac{\rho^2}{r^2} + \frac{\rho^2}{b^2} \right) - \frac{q}{\sigma_0} \quad (15)$$

$$\sigma_z/\sigma_0 = \nu \rho^2/b^2 - 2\nu q/\sigma_0 \quad (16)$$

and in the plastic portion ( $a \leq r \leq \rho$ )

$$\frac{E}{\sigma_0} \frac{u}{r} = (1-\nu-2\nu^2) \frac{\sigma_r}{\sigma_0} + (1-\nu^2) \frac{\rho^2}{r^2} \quad (17)$$

$$\sigma_r/\sigma_0 \quad (18)$$

$$\sigma_\theta/\sigma_0 = \mp \frac{1}{2} (1-\eta\beta+\eta\beta \frac{\rho^2}{r^2}) + \frac{1}{2} \frac{\rho^2}{b^2} - (1-\eta\beta) \ln \frac{\rho}{r} - \frac{q}{\sigma_0} \quad (19)$$

$$\sigma_z/\sigma_0 = \nu \rho^2/b^2 - 2\nu(1-\eta\beta) \ln \frac{\rho}{r} - 2\nu q/\sigma_0 \quad (20)$$

$$\bar{\epsilon}^p = \beta(\rho^2/r^2-1) \quad , \quad \eta\beta = \frac{m}{m + \frac{3}{4} \frac{(1-m)}{(1-\nu)^2}} \quad (21)$$

$$\eta = \frac{2}{\sqrt{3}} \frac{E}{\sigma_0} \frac{m}{1-m} \quad , \quad m = \frac{E_t}{E} \quad , \quad \sigma = \sigma_0(1+\eta\epsilon^p) \quad (22)$$

where  $\sigma_0$  is the initial tensile yield stress, and  $E_t$  is the tangent modulus in the plastic range of the stress-strain curve.

Using Eqs. (11) and (13) and the requirement of displacement continuity at the interface, i.e.,  $u_{b-}$  (liner) =  $u_{b+}$  (jacket), we obtain the expression for the interface pressure  $q$  as

$$\frac{q}{\sigma_0} = \frac{(1-\nu^2)\rho^2/b^2}{(1+\nu)(1-2\nu) + E[\alpha_{22k} \frac{(c/b)^{2k} + 1}{(c/b)^{2k} - 1} - \alpha_{12}]} \quad (23)$$

Given any value of  $\rho$  in  $a \leq \rho \leq b$ , we can now determine  $q$ ,  $u$ , and all the stresses and strains in the tube. In particular, the expressions for internal pressure and for displacements at the bore and the interface are

$$\frac{p}{\sigma_0} = \frac{q}{\sigma_0} + \frac{1}{2} (1 - \frac{\rho^2}{b^2}) + (1-\eta\beta) \ln \frac{\rho}{a} + \frac{1}{2} \eta\beta (\frac{\rho^2}{a^2} - 1) \quad (24)$$

$$\frac{E}{\sigma_0} \frac{u}{a} = - (1-\nu-2\nu^2) \frac{p}{\sigma_0} + (1-\nu^2)\rho^2/a^2 \quad (25)$$

$$\frac{E}{\sigma_0} \frac{u}{b} = (1-\nu^2) \frac{\rho^2}{b^2} - (1-\nu-2\nu^2) \frac{q}{\sigma_0} \quad (26)$$

By letting  $p = a$  and  $b$ , we can determine the lower limits  $p^*$ ,  $q^*$ ,  $u_a^*$ ,  $u_b^*$ ,  $u_c^*$ , and the upper limits  $p^{**}$ ,  $q^{**}$ ,  $u_a^{**}$ ,  $u_b^{**}$ ,  $u_c^{**}$ , respectively.

### FULLY-PLASTIC ANALYSIS

When the internal pressure  $p$  is further increased, i.e.,  $p > p^{**}$ , the steel liner will become fully-plastic. The composite jacket remains elastic as long as the failure pressure is not reached. Using Tresca's yield criterion, the associated flow rule, and assuming linear strain-hardening, a fully-plastic solution can be obtained (ref 4). The result is presented here for completeness. The explicit expressions for the displacement, strains, and stresses in the plane-strain case, subject to  $\sigma_\theta \geq \sigma_z \geq \sigma_r$ , are

$$ru = E^{-1}(1-2\nu)(1+\nu)r^2\sigma_r + \phi b^2 \quad (27)$$

$$\sigma_r = -p + \sigma_0(1-\eta\beta)\ln\left(\frac{r}{a}\right) + \frac{1}{2} \frac{\eta\beta}{(1-\nu^2)} \left[ \frac{b^2}{a^2} - \frac{b^2}{r^2} \right] E\phi \quad (28)$$

$$\sigma_\theta = \sigma_r + \sigma_0(1+\eta\bar{\epsilon}^P) \quad (29)$$

where  $\sigma_0$ ,  $\eta$ ,  $\bar{\epsilon}^P$  are the initial yield stress, hardening parameter, and equivalent plastic strain, respectively, and

$$\bar{\epsilon}^P = \frac{-2}{\sqrt{3}} \left[ \phi b^2/r^2 - (1-\nu^2)\sigma_0/E \right] / \left[ 1 + \frac{2}{\sqrt{3}} (1-\nu^2)\eta\sigma_0/E \right] \quad (30)$$

$$\phi = \left[ E\alpha_{22k} \frac{(c/b)^{2k} + 1}{(c/b)^{2k} - 1} - E\alpha_{12} + (1-2\nu)(1+\nu) \right] q/E \quad (31)$$

$$p = \sigma_0(1-\eta\beta)\ln \frac{b}{a} + q \left\{ 1 + \frac{1}{2} \eta\beta \left( \frac{b^2}{a^2} - 1 \right) \left[ Ak \frac{(c/b)^{2k} + 1}{(c/b)^{2k} - 1} + B + 1 \right] \right\} \quad (32)$$

It is interesting to point out that  $p$  is a linear function of  $q$ . Similarly, when evaluating  $u$  at the bore from Eq. (27), we obtain

$$u_a/a = -(1-2\nu)(1+\nu)P/E + \phi b^2/a^2 \quad (33)$$

which can also be expressed as a linear function of  $q$  with the aid of Eqs. (31) and (32). Since the relation between  $q$  and  $u_b$  is linear from Eq. (11),  $p$  and  $u_a$ , given by Eqs. (32) and (33), respectively, can be expressed as linear functions of  $u_b$ .

## FAILURE ANALYSIS

Since the steel liner is ductile and failure precedes by plastic flows, a nonlinear stress analysis beyond the elastic limit is required. The liner is considered as failure when the maximum stress or maximum strain reaches the ultimate limit ( $\sigma_U$  or  $\epsilon_U$ ). The steel is assumed to be elastic-plastic, linear strain-hardening with  $\sigma_0 = 120$  Ksi,  $E_t = 120$  Ksi (826.8 Mpa), and  $\sigma_U$  (ultimate strength) = 140 Ksi (964.6 Mpa). The composite jacket is elastically-orthotropic, and brittle failure is considered with the maximum strain criterion (ref 5). The maximum strain from each simple test is either measured or computed from the measured strength divided by the elastic modulus. For the composite jacket used here, the maximum strain criterion is

$$-\epsilon_x^i \leq \epsilon_\theta \leq \epsilon_x^* \quad \text{and} \quad -\epsilon_y^i \leq \epsilon_r \leq \epsilon_y^* \quad (34)$$

where

$$\epsilon_x^* = X/E_\theta \quad , \quad \epsilon_x^i = X'/E_\theta \quad , \quad \epsilon_y^* = Y/E_r \quad , \quad \epsilon_y^i = Y'/E_r \quad (35)$$

and  $X, X', Y, Y' = 262, 225, 8.7, 21.8$  Ksi (1805, 1550, 60, 150 Mpa), respectively.

## DISCUSSION OF RESULTS

Given any value of internal pressure, we can obtain numerical results for the stresses and strains in the radial and tangential directions and also for the displacement at any radial position in a compound tube. The actual specimens were constructed (ref 1) using steel liners with two thicknesses and the

appropriate thickness of the composite circumferentially wound on the liner. The geometric dimensions (a,b,c) for the three composite tubes are (0.9, 1.0, 1.189), (0.9, 1.07, 1.189), and (0.9, 1.07, 1.391) inch. The pressure at the interface between the liner and jacket has been obtained as a function of internal pressure, and the results for three cases are shown in Figure 2. In this figure we also show the limits of internal pressure in the elastic-plastic range, i.e.,  $(p^*, p^{**}) = (20.48, 23.93), (23.06, 28.75), (27.47, 34.98)$  Ksi, respectively. The results of the hoop strains at the bore, the interface between the liner and jacket, and the outside surface for three cases are shown as functions of internal pressure in Figures 3, 4, and 5, respectively. The complete (including elastic, elastic-plastic, and fully-plastic) ranges of loadings up to failure have been considered. The maximum values of internal pressure that these compound tubes can contain without failure are  $p_f = 50.693, 48.483, \text{ and } 69.931$  Ksi for cases 1, 2, and 3, respectively, and the corresponding hoop strain is 1.12 percent. The results of hoop stresses at the bore ( $\sigma_{\theta/a}$ ) and at the interface ( $\sigma_{\theta/b_-}$  and  $\sigma_{\theta/b_+}$ ) are shown as functions of internal pressure in Figures 6, 7, and 8 for three cases. It should be noted that the hoop stresses at the interface are discontinuous with  $b_-$  and  $b_+$  representing the location in the liner and jacket, respectively. These figures show very clearly that the results change drastically when yielding occurs. The relation changes from linear to nonlinear when yielding sets in, and a more significant change occurs when the fully-plastic state is reached. The distributions of hoop stresses in the liner and jacket can be obtained at any given value of internal pressure. In Figures 9, 10, and 11, for cases 1, 2, and 3, respectively, we present the stress distributions for five values of internal pressure. The first three values correspond to initial yielding, 50 percent yielding, and 100 percent yielding. The percent yielding in the elastic-plastic range is defined

by  $(p-a)/(b-a) \times 100$  percent. After the fully-plastic state is reached, the stress distribution changes drastically as shown in the figures for the last three values of internal pressure. The hoop stresses in the liner decrease slightly, but those in the jacket increase elastically as internal pressure is increased.

#### CONCLUSION

The stresses, strains, and displacements in the liner and jacket can be obtained analytically for all loading ranges up to failure. The plastic deformation in the liner has a significant effect on the overall performance of the composite structure.

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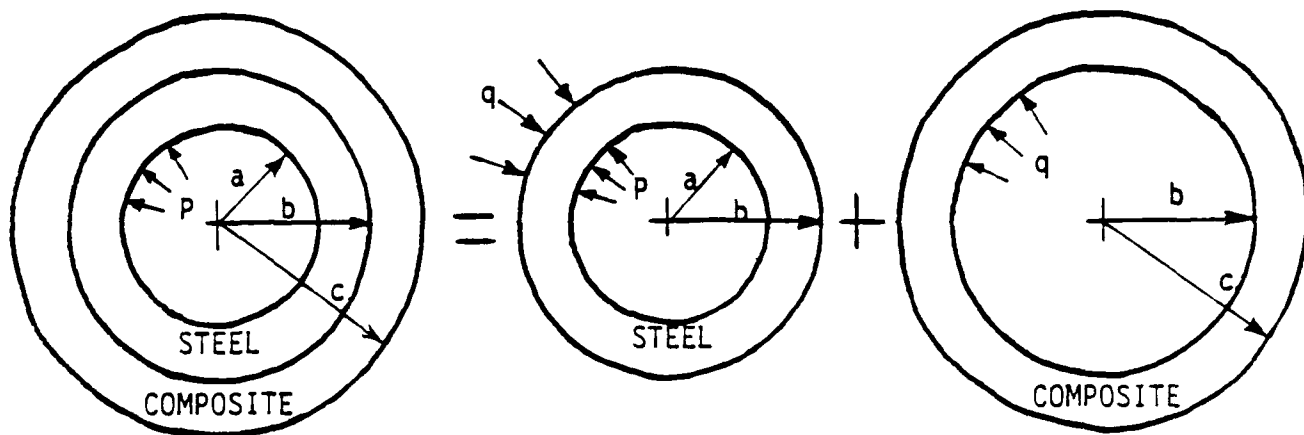


Figure 1. Schematic of a compound tube problem.

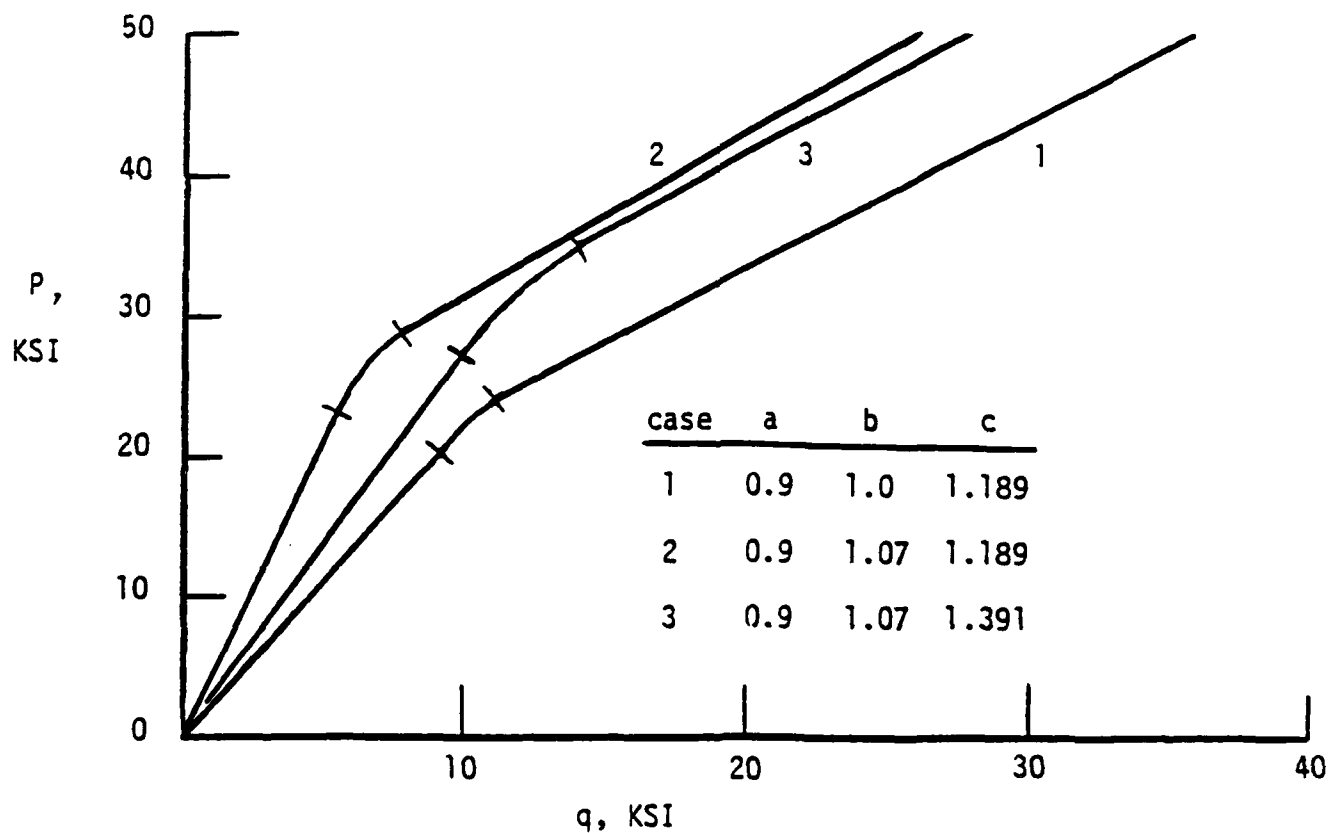


Figure 2. Interface pressure as a function of internal pressure.

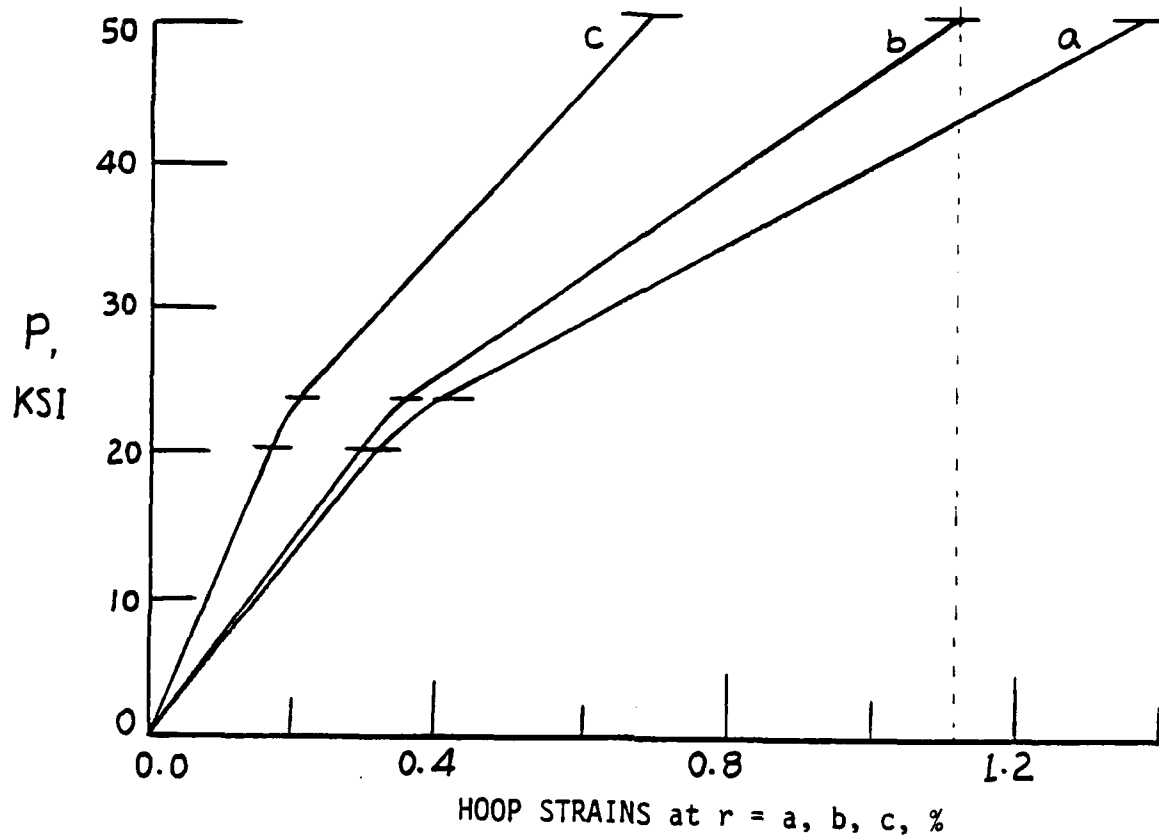


Figure 3. Hoop strains at the bore, interface, and outside surface as functions of internal pressure for case 1.

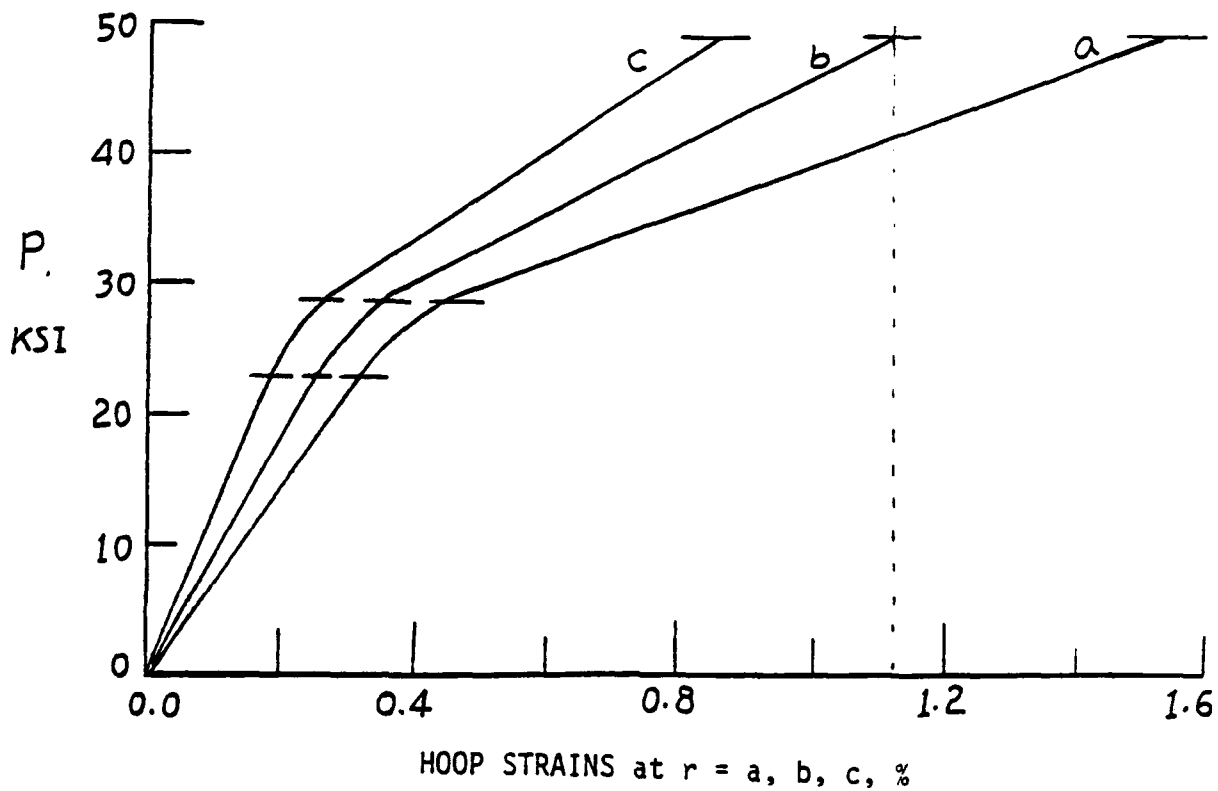


Figure 4. Hoop strains at the bore, interface, and outside surface as functions of internal pressure for case 2.

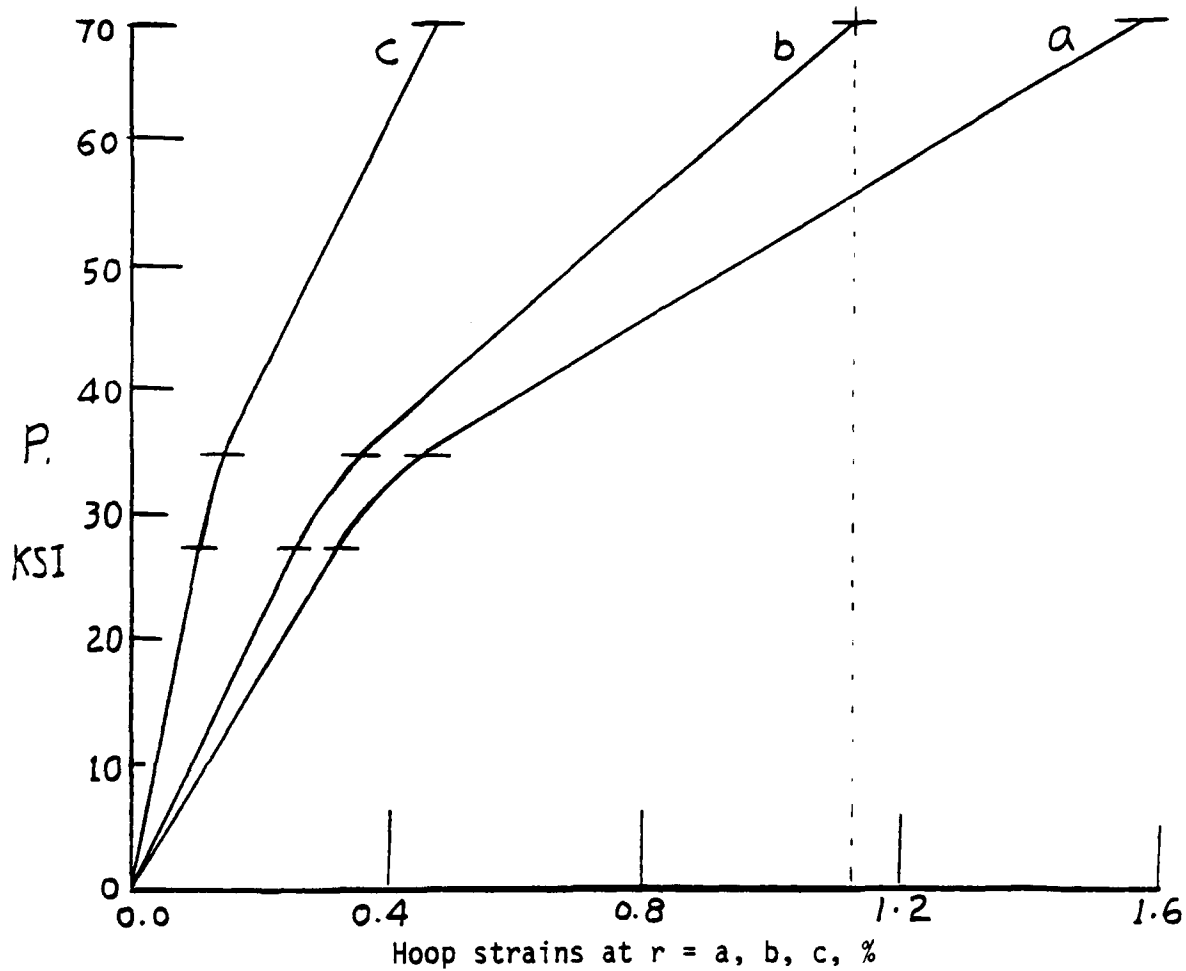


Figure 5. Hoop strains at the bore, interface, and outside surface as functions of internal pressure for case 3.

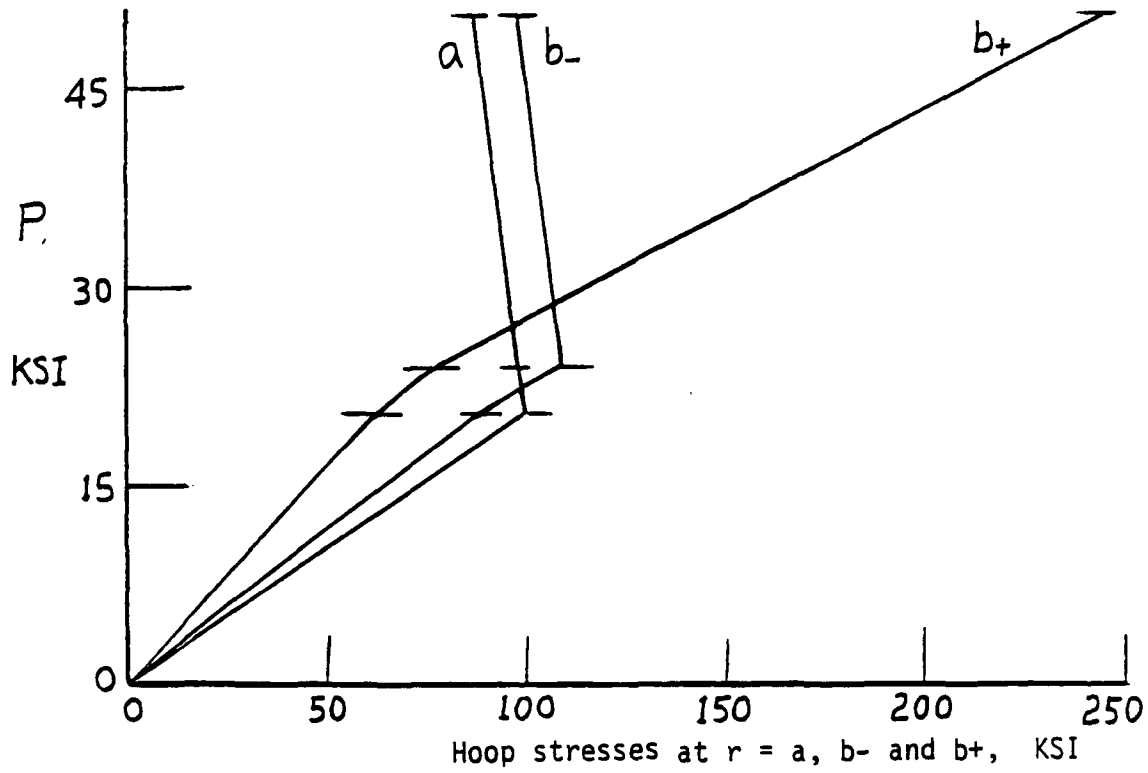


Figure 6. Hoop stresses at the bore and interface as functions of internal pressure for case 1.

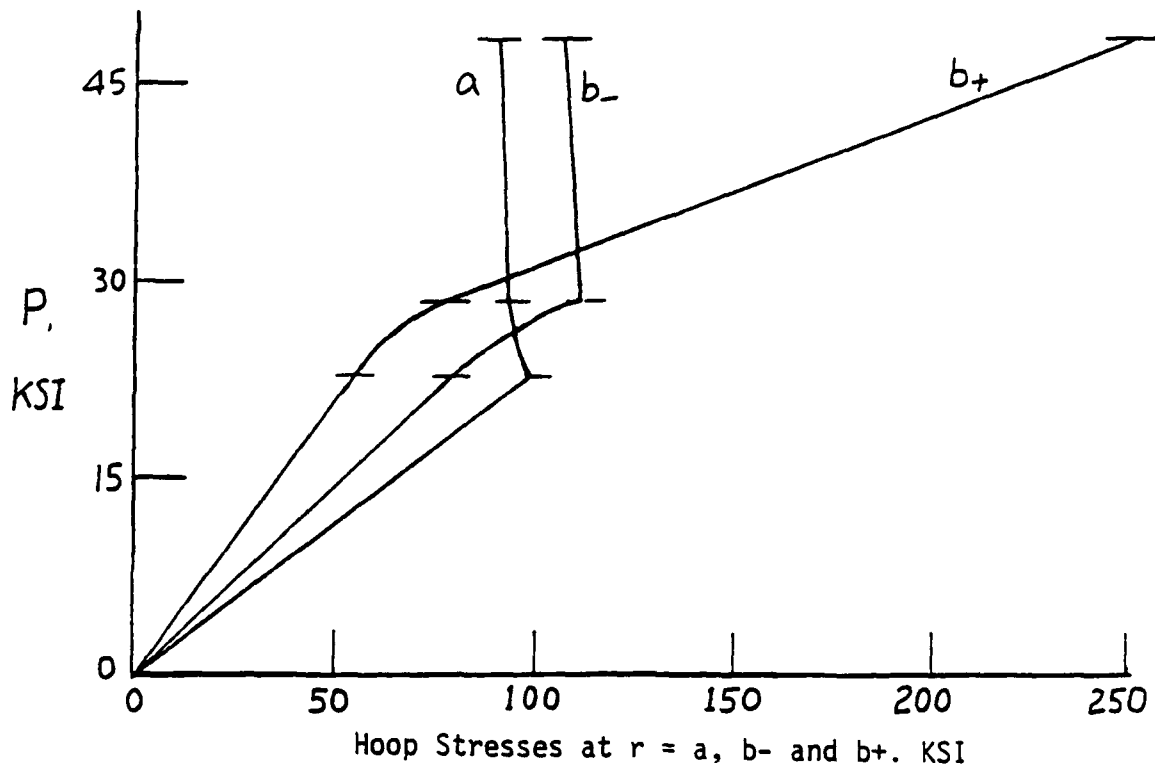


Figure 7. Hoop stresses at the bore and interface as functions of internal pressure for case 2.

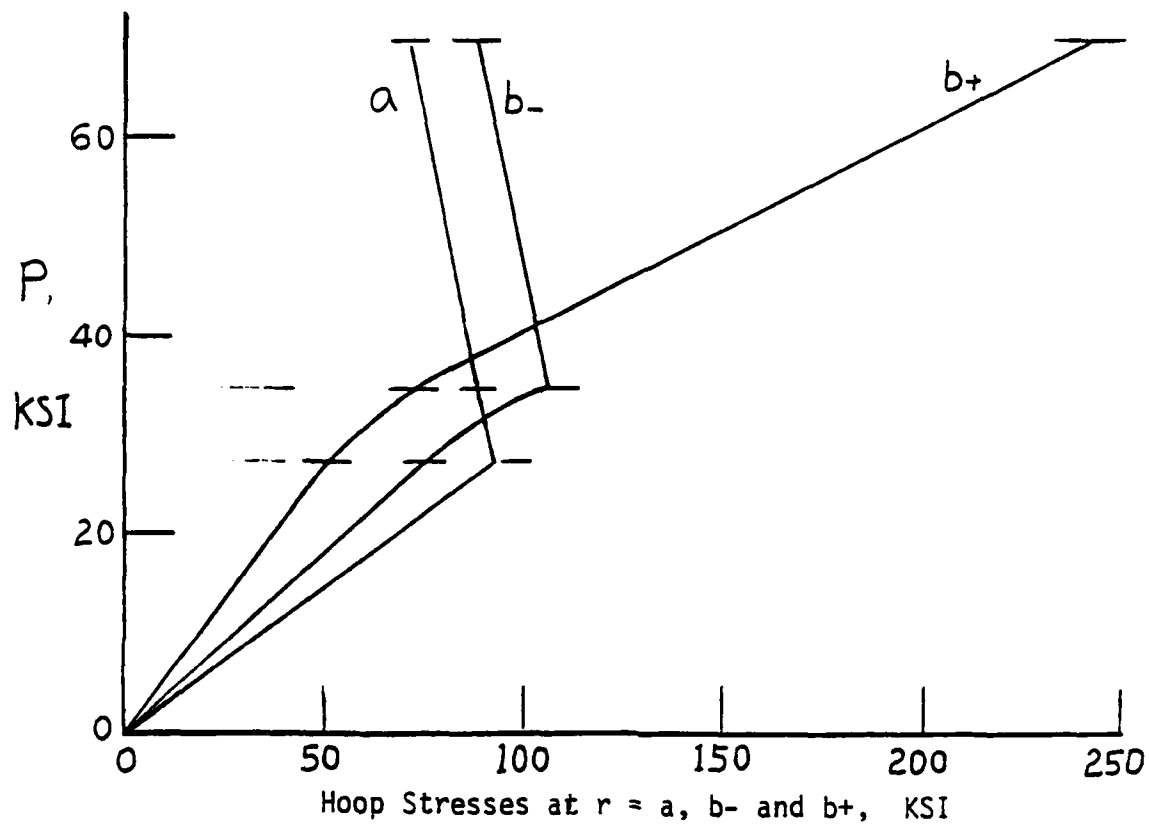


Figure 8. Hoop stresses at the bore and interface as functions of internal pressure for case 3.

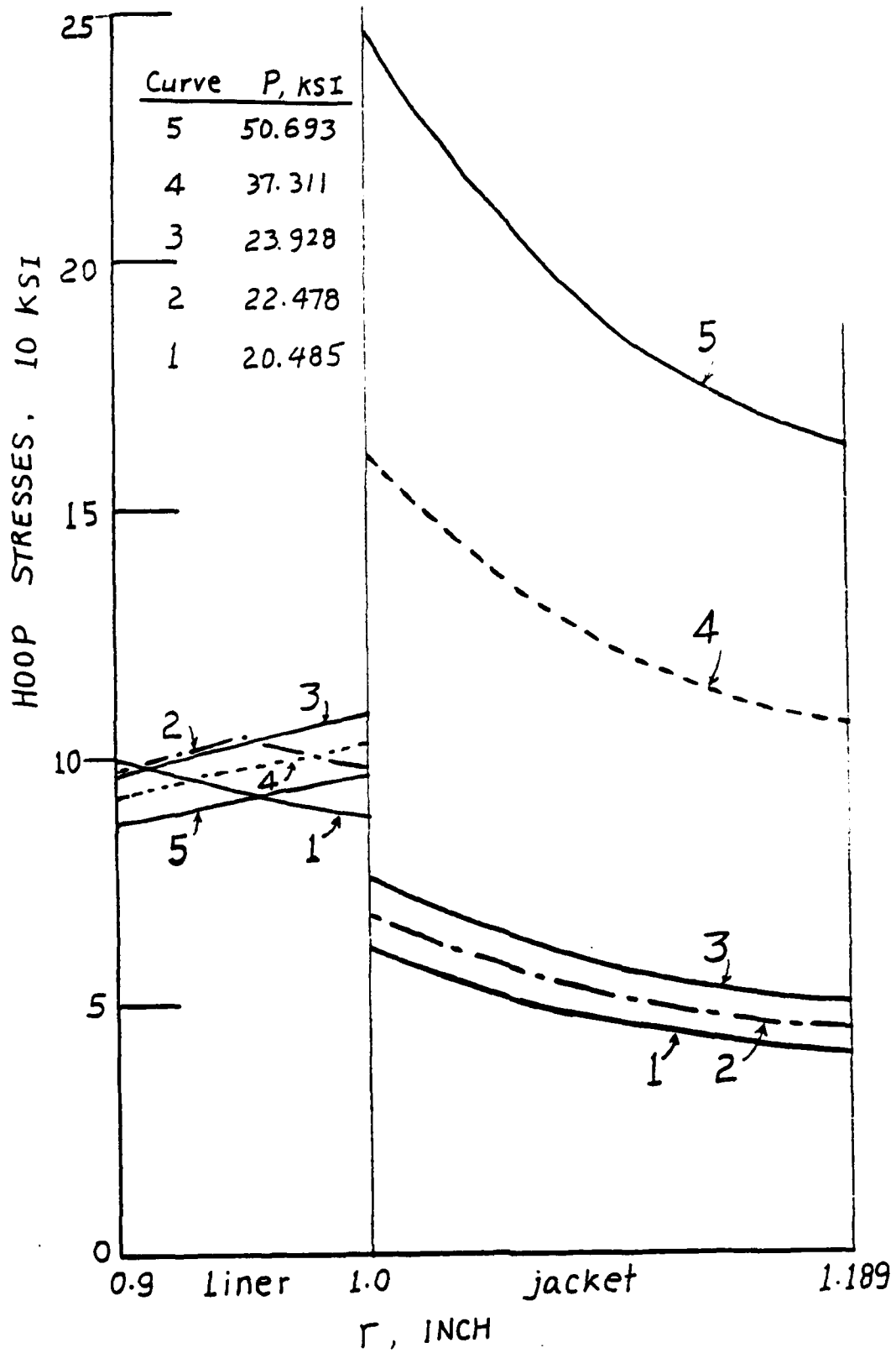


Figure 9. Distribution of hoop stresses in the liner and jacket for case 1.

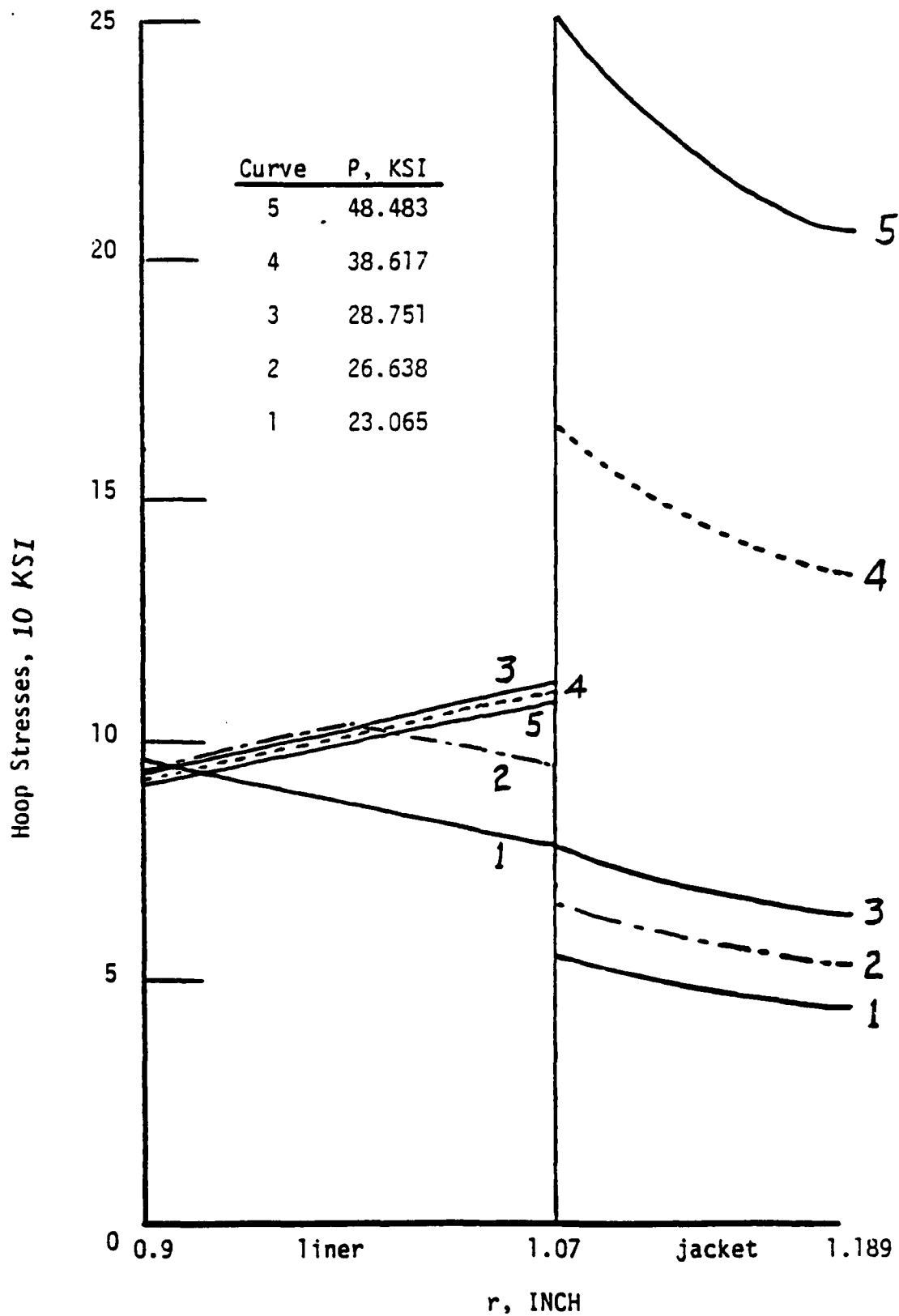


Figure 10. Distribution of hoop stresses in the liner and jacket for case 2.

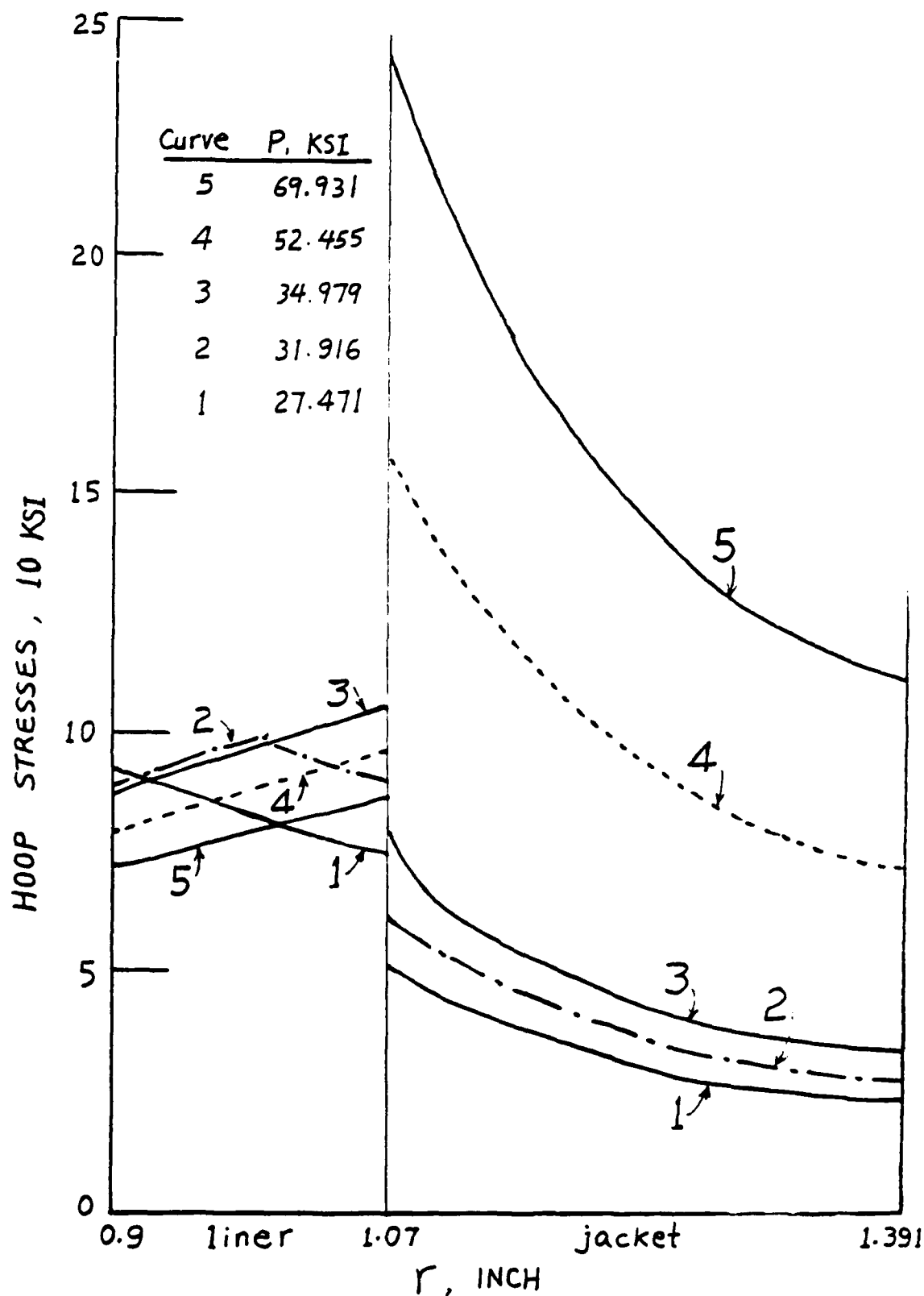


Figure 11. Distribution of hoop stresses in the liner and jacket for case 3.

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