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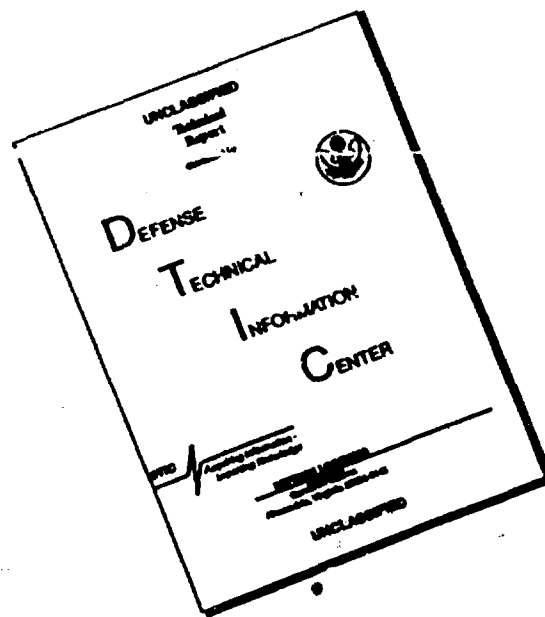
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A COMPARISON BETWEEN THEORETICAL PREDICTION AND EXPERIMENTAL MEASUREMENT OF THE DYNAMIC BEHAVIOUR OF SPUR GEARS

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ABSTRACT

A comparison was made between computer model predictions of gear dynamic behaviour and experimental results. The experimental data were derived from the NASA gear noise rig, which was used to record dynamic tooth loads and vibration. The experimental results were compared with predictions from the Australian Defence Science and Technology Organisation Aeronautical Research Laboratory's gear dynamics code, for a matrix of 28 load-speed points. At high torque the peak dynamic load predictions agree with experimental results with an average error of 5 percent in the speed range 800 to 6000 rpm. Tooth separation (or bounce), which was observed in the experimental data for light-torque, high-speed conditions, was simulated by the computer model. The model was also successful in simulating the degree of load sharing between gear teeth in the multiple-tooth-contact region.

INTRODUCTION

The dynamic behaviour of gears is important for a number of reasons—the dynamic load increment, the gear life, the gear noise, and the overall vibratory behaviour of the gear system. In aerospace applications, such as helicopter transmissions, all of these factors are relevant, and weight is also an important factor. A knowledge of dynamic load factors can assist in weight reduction.

The NASA gear noise rig was built to enable fundamental studies of gear dynamic behaviour to be carried out and to provide support to gear noise reduction programs. Oswald et al. (1991) compared dynamic load measurements from the NASA rig with predictions from the computer program DANST (Dynamic Analysis of Spur Gear Transmissions). This report continues that work, and compares the same experimental data with predictions from another model, developed at the Australian Defence Science and Technology Organisation (DSTO) Aeronautical Research Laboratory (ARL), designated ARL_DYN.

The two models differ significantly. DANST (Lin et al. 1989, 1987) has four torsional degrees of freedom representing the motor, the gears, and the load. The shaft stiffness elements are represented by linear stiffnesses, and the tooth compliance by a variable stiff-

ness. ARL_DYN (Rebbechi, 1991) models the gear in a way that allows the detailed contact conditions of each of the tooth pairs in contact to be separately represented. The model also includes shaft deflection. Although this has the disadvantage of increasing the complexity of the model, it has the advantage that the model parameters, such as the sliding friction coefficient, can be varied in a way that accords with the physical parameters.

The objectives of this work were (1) to evaluate predictions of dynamic load increment by using the ARL model and compare these with experimental results, and (2) to refine the model as necessary to match the predictions with the measured dynamic load curves.

APPARATUS AND PROCEDURES

The NASA Lewis gear noise rig (Fig. 1) was used for these tests. This rig features a single-mesh gearbox powered by a 150-kW (200-hp) variable-speed electric motor. An eddy-current dynamometer loads the output shaft. The gearbox can be operated at speeds up to 6000 rpm. The rig was built to carry out fundamental studies of gear noise and the dynamic behaviour of gear systems. It was designed to allow testing of various configurations of gears, bearings, dampers, and supports. The gearbox is extensively instrumented for strain and vibration measurements.

A poly-V belt drive was used as a speed increaser between the motor and the input shaft. A soft coupling was installed on the input shaft to reduce input torque fluctuations, which were caused by nonuniformity at the belt splice.

The test gears were identical spur gears (at 1:1 ratio) machined to American Gear Manufacturers Association (AGMA) class 13 accuracy. The gear profiles were modified with linear tip relief as shown in Fig. 2. Test gear parameters are shown in Table I.

Tooth root fillet strains were measured on the tensile and compressive sides of two successive teeth, at the 30° tangency location (Cornell, 1980), Fig. 3. Dynamic strains were recorded for the four gages at a matrix of 28 load-speed test conditions: four speeds (800, 2000, 4000, and 6000 rpm) and seven torque levels (16, 31, 47,

63, 79, 94, and 110 percent of the nominal torque of 71.8 N-m (635 lb-in.). The strain gage signals were transmitted through a slip-ring assembly to constant-current signal conditioners. The dynamic strain data were digitized by a digital data acquisition system, with sample rates of 50 kHz per channel at the 2000-, 4000-, and 6000-rpm speeds and 20 kHz at the 800-rpm speed. A once-per-revolution timing pulse provided an accurate angular position reference for digital resampling by linear interpolation. The resampled data were then synchronously averaged over several successive revolutions to reduce noise effects, such as the torque fluctuation from the drive belt.

The averaged strain data values were converted to normal tooth force (dynamic tooth load) by using calibration data measured under static conditions. The calibration apparatus and data reduction procedures are more fully described in Rebbechi et al. (1991) and Oswald et al. (1991).

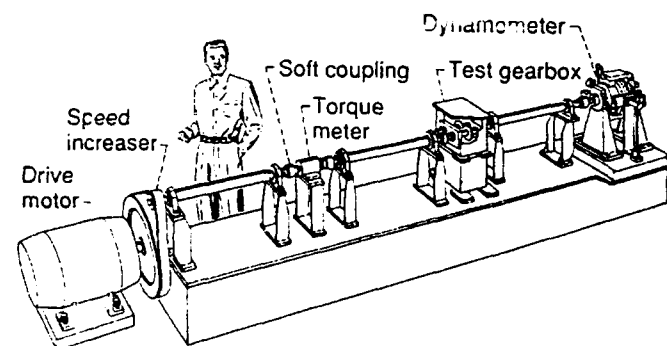
ANALYTICAL MODEL

ARL_DYN (Rebbechi, 1991), Fig. 4, considers both torsional and lateral displacements of the gears and can accommodate variable numbers of teeth in contact. The equations of motion were derived by considering dynamic equilibrium for moments and forces

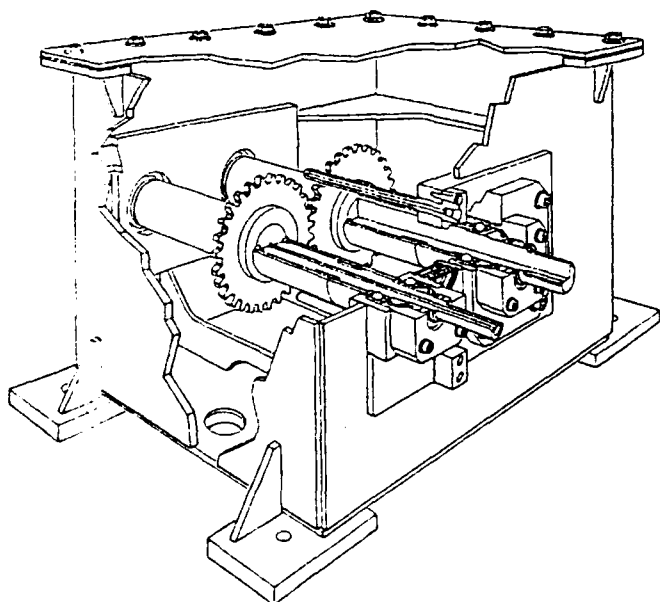
acting on the components of the system. Moments are taken about the axes of rotation. The mode of deflection of the gear teeth is taken as rotation about a point in the gear wheel at one tooth height below the base circle (see Rebbechi, 1983). The tooth stiffness, which varies with load position, is calculated according to a deflection equation in Merritt (1971). Forces acting through gear centers are resolved into coordinates x_1, y_1, x_2, y_2 . This results in $[8+2(t-1)]$ equations of motion, where t is the number of tooth pairs in contact. The set of equations can be reduced to $[7+(t-1)]$ equations by invoking the kinematic constraint equations for the gears in mesh.

To improve numerical accuracy, the equations involving gear body rotation θ_1, θ_2 were transformed to new coordinates $\Theta_1 = (\theta_1 + n\theta_2)/2$ (average rotation of gear pair) and $\Theta_2 = (\theta_1 - n\theta_2 - c)/2$ (relative rotation of gear pair), where θ_1 and θ_2 represent the rotation of the gear wheels, n is the gear ratio, and c is a constant used to make $\Theta_2 = 0$ if there are no errors. The new equations relate to (1) the absolute rotation, and (2) the relative rotation of the gear wheels. The gear dynamics code assembles the equations of motion in matrix form as shown in equation (1):

$$[M]\{\ddot{X}\} + [C]\{\dot{X}\} + [K]\{X\} = \{F\} \quad (1)$$

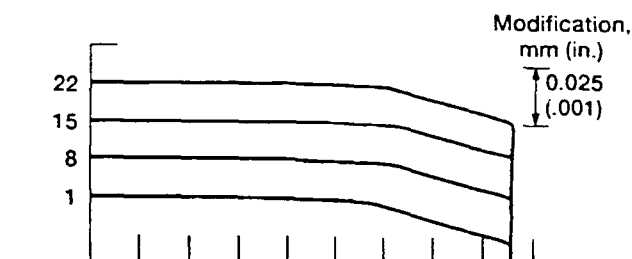


(a) Layout.

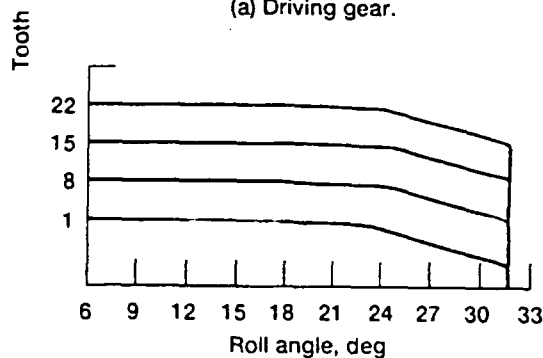


(b) Detail of gearbox.

Figure 1.—NASA gear noise rig.



(a) Driving gear.



(b) Driven gear.

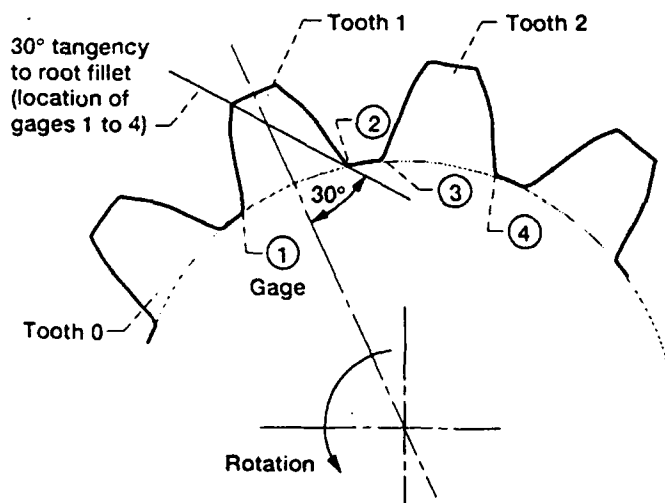
Figure 2.—Test gear profile traces.

TABLE 1.—TEST GEAR PARAMETERS

Gear type	Standard involute; full-depth tooth
Number of teeth	28
Module, mm (diametral pitch, in. ⁻¹)	3.175 (8)
Face width, mm (in.)	6.35 (0.25)
Pressure angle, deg	20
Theoretical contact ratio	1.64
Driver modification amount, mm (in.)	0.023 (0.0009)
Driven modification amount, mm (in.)	0.025 (0.0010)
Driver modification start, deg	24
Driven modification start, deg	24
Tooth-root radius, mm (in.)	1.35 (0.053)
Gear quality	AGMA class 13
Nominal (100 percent) torque, N-m (in.-lb)	71.77 (635.25)



(a) Gage installation.



(b) Gage location.

Figure 3.—Strain gage installation and location on test gear.

where M , C , and K are square coefficient matrices representing the mass (inertia), damping, and stiffnesses, and X and F are vectors of displacements and forces (torques), respectively. The order (number of degrees of freedom) of equation (1) is $(6+t)$, where t is the number of tooth pairs in contact. For low-contact-ratio gears, t normally varies between 1 and 2. If tooth separation (tooth bounce) occurs, t may also be zero. Therefore, the degrees of freedom vary

- θ_1 rotation of gear body 1
- θ_2 rotation of gear body 2
- θ_{3-6} rotation of gear teeth
- x_1 lateral displacement of gear wheel 1, transverse direction
- y_1 lateral displacement of gear wheel 1, radial direction
- x_2 lateral displacement of gear wheel 2, transverse direction
- y_2 lateral displacement of gear wheel 2, radial direction

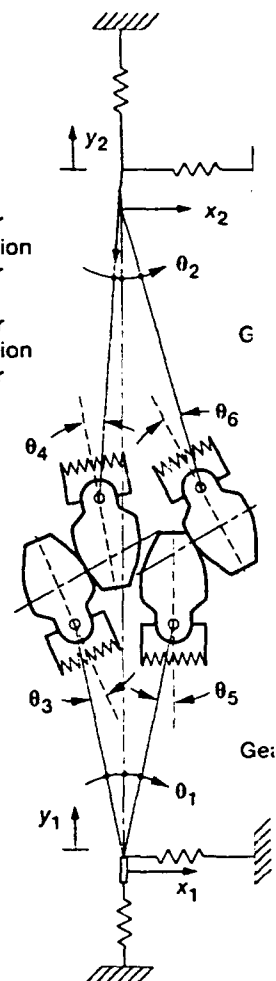


Figure 4.—Gear dynamics model.

between 6, 7, and 8, depending on whether there are zero, one, or two pairs of teeth in contact. The M , C , and K matrices contain a number of nonlinear terms owing to the nonlinear kinematic constraints.

The dynamics code allows prescription of such features as profile errors and modification, shaft deflection (including interaction effects with conditions of tooth contact), tooth deflection (including resulting change of contact position and common normal direction), and tooth sliding friction. The friction coefficient for the gear mesh (the friction force divided by the normal force) was taken to be 0.06. Values up to 0.10 were tried but made little difference in the results. Material damping in the gear tooth was modeled as viscous damping and expressed as the damping ratio (fraction of critical damping). Gear tooth material damping produces a significant effect. A damping ratio of 0.10 gave the best correlation with experimental data. The same damping ratio (0.10) was assumed for lateral bending of the shaft. The torsional shaft damping coefficient was 2.3×10^{-5} N-m/(rad/sec). Changing the shaft damping values had little effect.

For input and output boundary conditions, steady external torques were assumed. The code solves the equations of motion with a Newmark-Beta numerical integration technique. The profile modification measured for the test gears (Fig. 2) was specified for the analysis.

RESULTS AND DISCUSSION

Dynamic tooth loads computed from the strain gage readings were compared with the predictions of ARL_DYN for dynamic tooth force. Initial runs of the computer model, although producing good results at high loads (with an average error in maximum tooth load of 5 percent), did not successfully characterise dynamic behaviour at light loads and high speeds. An example is shown in Fig. 5, where at the roll angle of 21° , the predicted value is about 3.5 times the measured value.

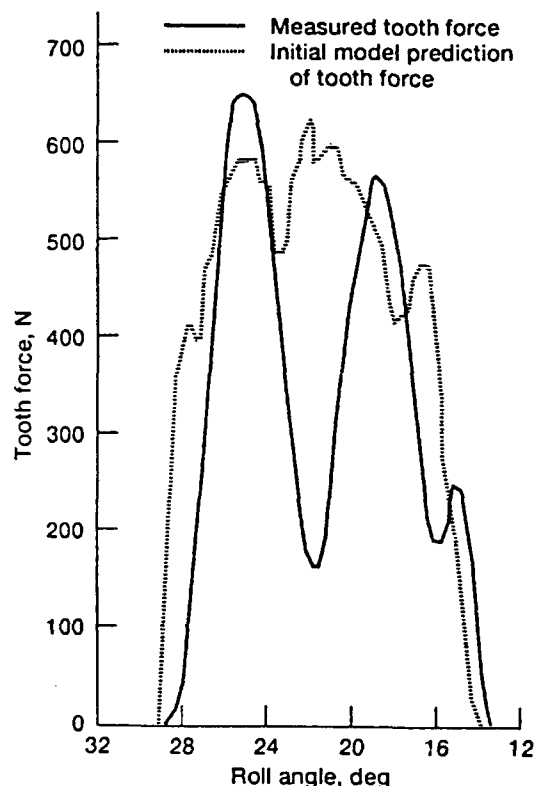


Figure 5.—Comparison between initial prediction of tooth force and measured result at 4000 rpm and 31-percent torque.

The experimental results were critically examined to evaluate reasons for the disagreement at light loads between analysis and experiment. A segment of these results is shown in Fig. 6. Here the dynamic tension strains at 31-percent torque are plotted for four speeds in the range 800 to 6000 rpm. Each curve has three parts: (1) a region where the strain increases rapidly as the load is taken up by the tooth of interest; (2) a region of slowly declining static strain (with dynamic effect superimposed) where the entire load is carried by a single tooth pair; this region lies approximately between points A and B in Fig. 6; and (3) a region where the load is passed to the following tooth. It can be seen that the load-sharing regions (1 and 3), and thus the effective contact ratio, were virtually unaffected by speed. Speed had little effect on the dynamic load until point A in Fig. 6 was reached. The higher speeds show an "overshoot." As this overshoot changed only in magnitude as the speed increased, and did not change in angular position, it most likely resulted from a predominantly inertial effect, and not from a combined mass/stiffness (resonance) effect, where we would expect a phase shift.

The approximate displacement error for this gear tooth profile when lightly loaded is as described by Munro (1989) and is sketched in Fig. 7. Munro terms this type of profile correction as "long profile relief," where the relief extends from below the high point of

single-tooth contact to the tooth tip. It appears that the overshoot in response evident in Fig. 6 arose from the inability of the gear pair to instantaneously adapt to the "separating mode" (where the driven gear leads the driving gear). As the gear speed increased, this effect became more marked. The dominant factors here are probably the gear wheel inertia, which relates to speed through the separating acceleration, and the external torque, which acts to reduce dynamic overshoot.

The effect of overshoot or tooth separation was reproduced in the computer model. Initially, the value used for gear wheel inertia did not include the inertias of the gear hub, shaft, spacers, or couplings. When these parts were accounted for, the inertia value increased by a factor of 4. The tooth forces for the "light" and the "standard" (corrected) gears are compared in Fig. 8. The measured tooth force data are also shown for comparison. This result closely accords with and confirms the hypothesis of Munro (1989), who described the tendency of gears with long relief to separate at light loads.

The influence of shaft deflection was also considered. Owing to the construction of this test gearbox (Fig. 1), where the gears are centrally mounted on relatively long supporting shafts, it was at one stage thought that lateral deflection may be a cause of the tooth bounce observed when light loads are combined with high speeds. Dynamic tooth strains at 4000 rpm are compared for seven torque levels in Fig. 9. The effect of tooth bounce can be seen in the curve for 16-percent torque. Here, the force vanishes around the pitch point, indicating that the teeth have lost contact. It is interesting to note that the tooth bounce shown here is not unique to the NASA gear noise rig but is also seen in the results of other researchers such as Tobe et al. (1977). Figure 10 compares the predicted dynamic tooth force for the normal gears with a case where the shaft stiffness is increased by a factor of 4. There is little difference in the character of these curves.

The shaft deflection in the radial direction (along the line joining the gear centers) for both normal and stiff shafts is plotted in Fig. 11. As expected, the mean deflection was less when the stiffness was increased, but surprisingly the dynamic displacement increased. This increase in dynamic displacement for a stiffer shaft was apparently a resonance effect (note the phase shift of approximately 90° between the curves). This indicates that shaft flexibility is not likely to be a contributing factor to the tooth bounce.

Dynamic load predictions for the model with the normal (heavier) gear wheels are compared with measured values in Fig. 12. Agreement is reasonable except in Fig. 12(c), at 6000 rpm and 31-percent torque. The prediction shows tooth separation at this condition, but tooth separation was actually recorded at the lower speed of 4000 rpm and the lighter torque of 16 percent (see Fig. 9). It is evident from these results that further refinement of the model is necessary to produce consistent results across the whole speed range. It is probable that the introduction of additional torsional degrees of freedom, representing the motor and the dynamometer, would aid in this regard, so that the dynamic load increments at different speeds could be magnified or reduced. The analysis was particularly successful in predicting the response in the load-sharing region (roll angle greater than 23° or less than 19°).

The peak values of the dynamic load from both measured and predicted data are compared at four speeds (800, 2000, 4000, and 6000 rpm) for the highest torque level (110 percent) in Fig. 13. The predicted and measured data show the same trend (i.e., a minimum at about 4000 rpm), and the values agree within an average error of 5 percent. The static load line drawn in Fig. 13 is calculated from the external applied torque of 110 percent. The resulting force of 1894 N (426 lb) is computed from the torque divided by the base circle radius.

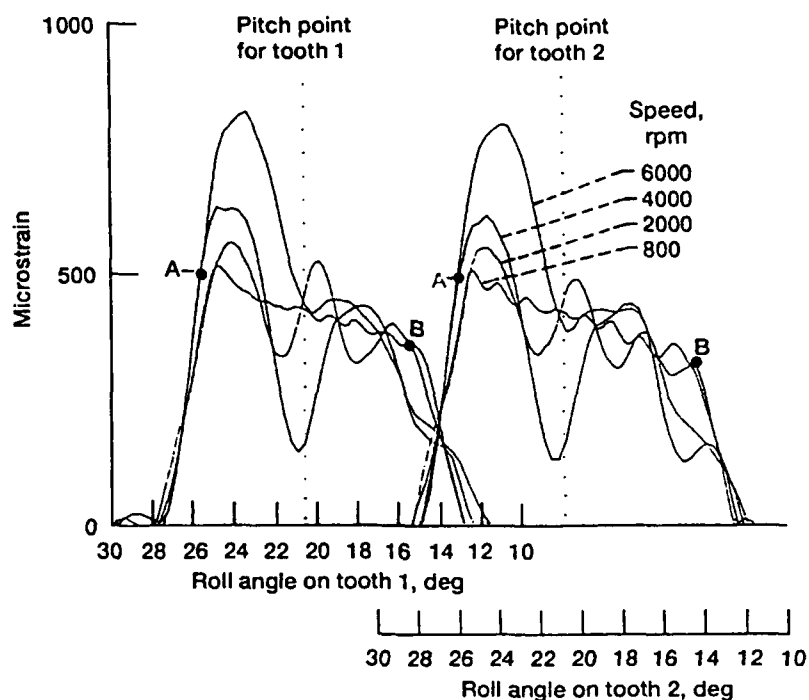


Figure 6.—Tension gage strain at 31-percent torque and four speeds.

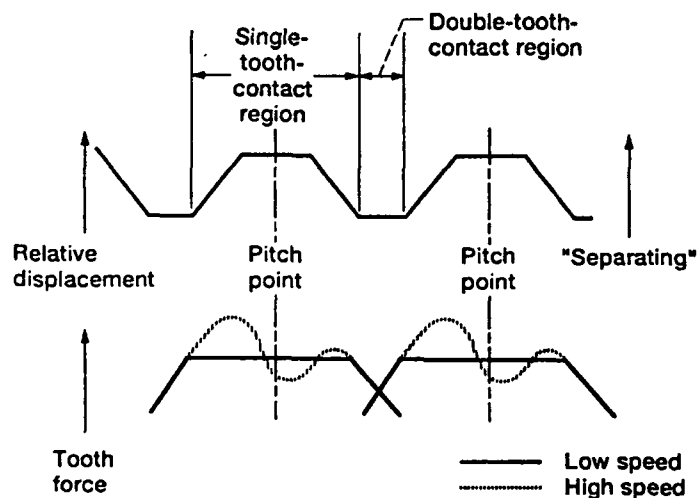


Figure 7.—Relative displacement in single- and double-tooth-contact regions and effect of speed on dynamic load.

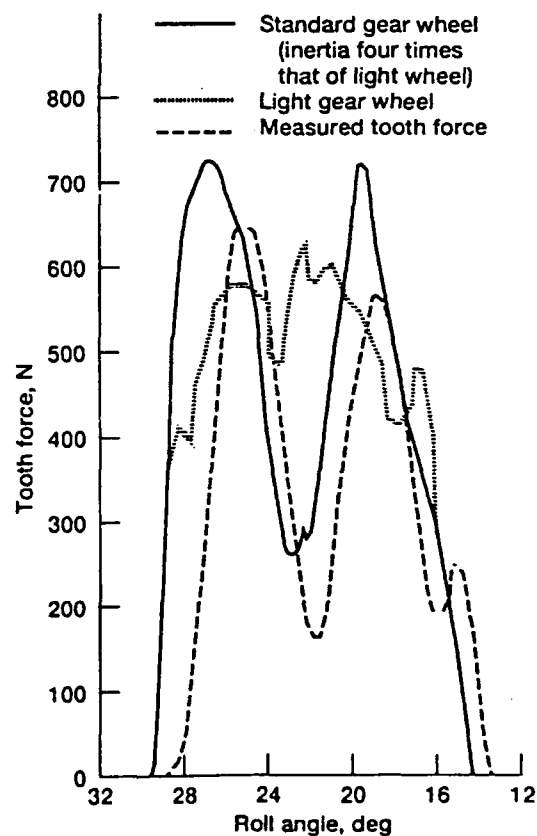


Figure 8.—Effect of gear wheel inertia on predicted dynamic tooth force at 4000 rpm and 31-percent torque.

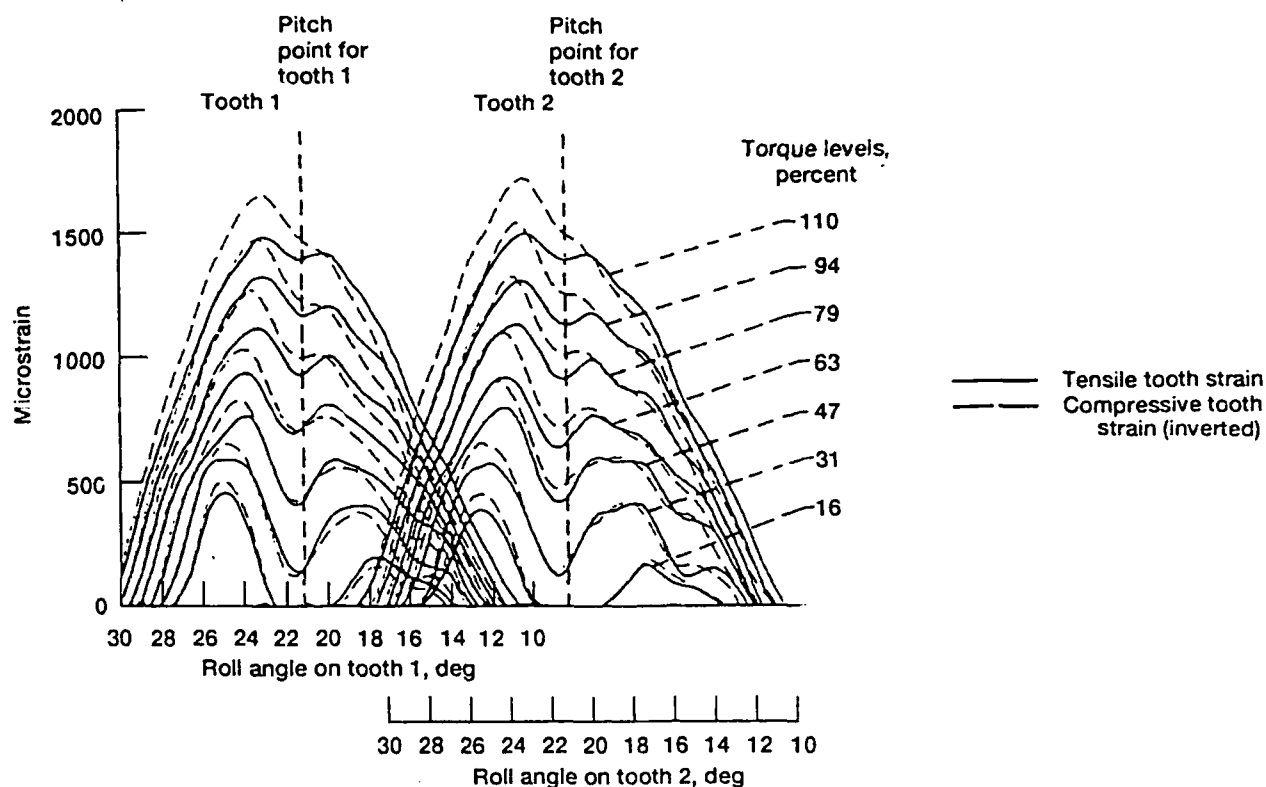


Figure 9.—Dynamic tooth strains at 4000 rpm and seven torque levels. Compressive strains are shown as positive for comparison with tensile data.

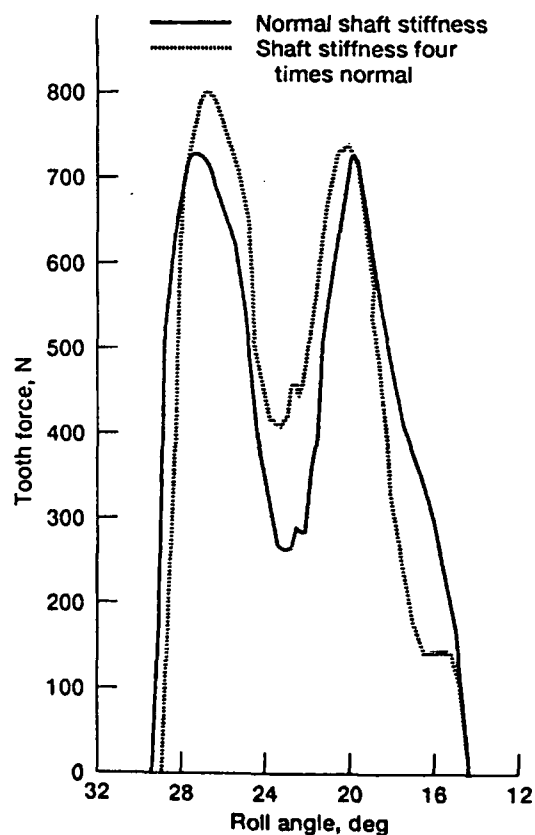


Figure 10.—Predicted dynamic tooth force at 4000 rpm and 31 percent torque. Comparison of results for two shaft stiffnesses.

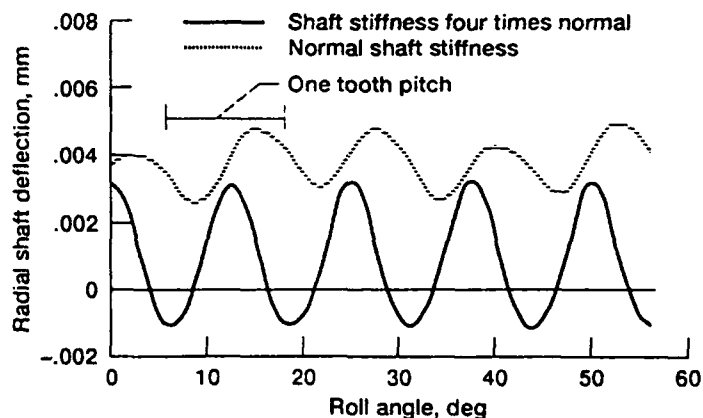


Figure 11.—Predicted radial shaft deflection at 4000 rpm and 31-percent torque. Comparison of results for two shaft stiffnesses.

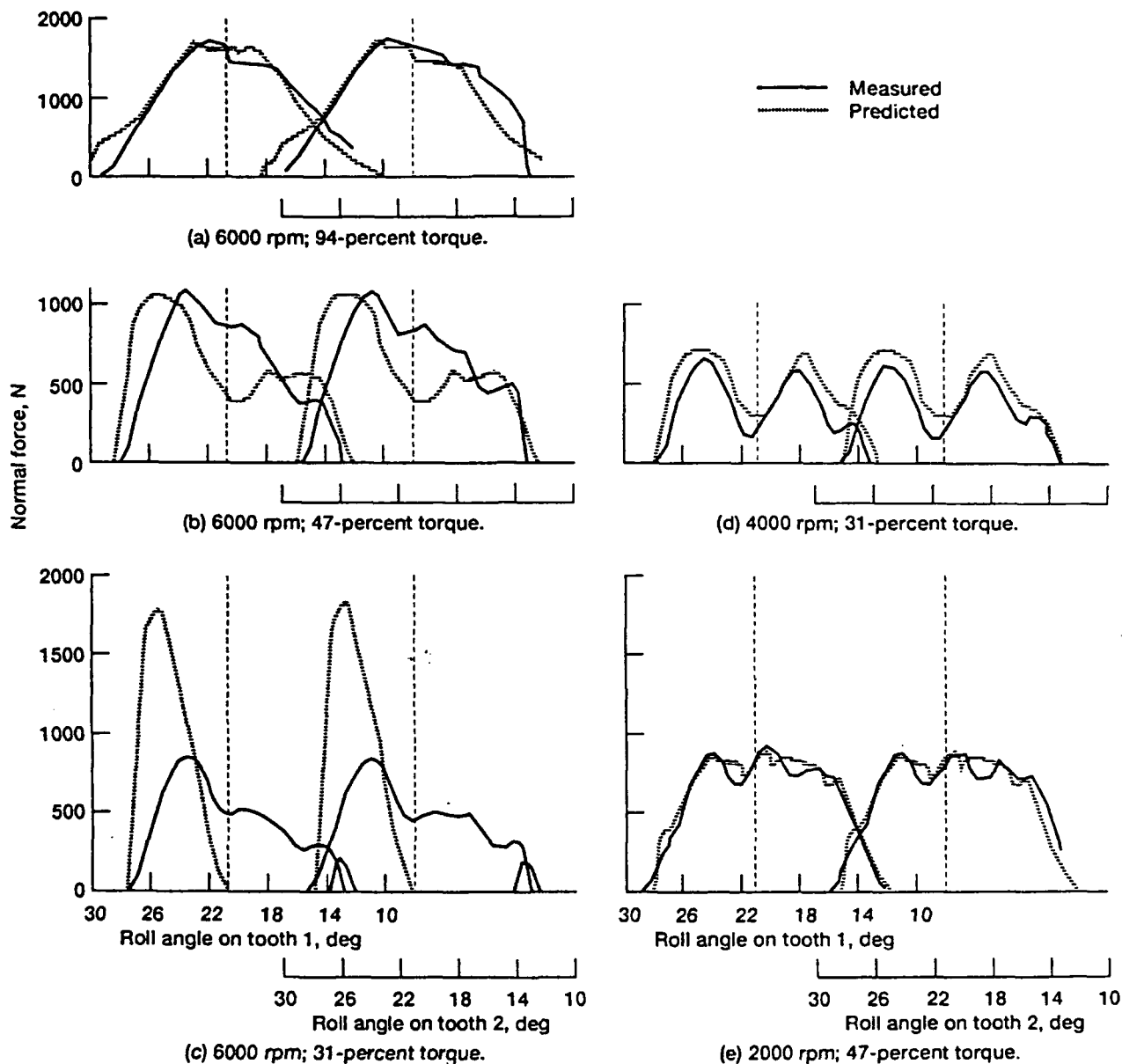


Figure 12.—Comparison between predicted and measured dynamic tooth loads for normal gear wheels.

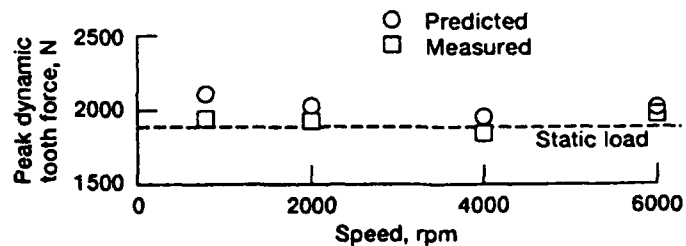


Figure 13.—Comparison between predicted and measured peak dynamic tooth load at 110-percent torque and four speeds.

CONCLUSIONS

Experimental data for gear tooth dynamic load were compared with predictions from the Australian Defence Science and Technology Organisation Aeronautical Research Laboratory's gear dynamics code. The effects of lateral shaft stiffness and gear body inertia were examined by using the computer model to improve predictions of gear tooth bounce as observed at light loads and high speeds. The following results were obtained:

(1) Peak dynamic load predictions agreed with measured data within an average error of 5 percent for 110-percent torque and speeds ranging between 800 and 6000 rpm.

(2) Tooth separation (or bounce) was observed in the experimental data for light-load, high-speed operation. The computer model predicted tooth separation under slightly different conditions. The model shows that this phenomenon is primarily dependent on the operating conditions of speed and load and the physical parameters of tooth profile and gear body inertia. An increase in gear wheel inertia increases the likelihood of tooth separation.

(3) The analytical model was successful in simulating the degree of load sharing between gear teeth in the multiple-tooth-contact region.

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