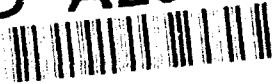


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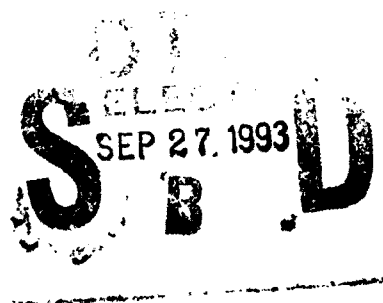


**SOME POTENTIAL ERRORS IN SATELLITE WIND ESTIMATES
USING THE GEOSTROPHIC APPROXIMATION
AND THE THERMAL WIND**

James Cogan

ARL-MR-36

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1. INTRODUCTION

Passive satellite sounders do not directly measure wind velocity; instead they derive it indirectly from the satellite temperature profile. The temperature profile is computed from radiances (infrared or microwave) emitted by volumes of atmosphere, each defined by a horizontal resolution area, and a vertical thickness according to a weighting function centered at some pressure level. The temperature profile is used to compute geopotential heights for the several pressure levels. The height field from many soundings for each pressure level is used to compute the geostrophic wind. The geostrophic wind is an approximation to the real wind that assumes frictionless flow parallel to "straight" height contours (along a great circle), where the pressure force balances the coriolis force. An alternative method involves the shear of the geostrophic wind, commonly referred to as the "thermal wind." For a given layer, thermal wind may be derived by using the gradient of mean layer temperature or the gradient of layer thickness. Since the thermal wind is really a shear, the wind velocity at some baseline level must be measured or computed (for example, geostrophic or measured wind at 800 hPa). Figure 1 illustrates the meaning of the thermal wind through a simple example. In the example the assumption is that the geostrophic wind at 700 hPa (1 hPa = 1 mbar) has a speed and direction of 20 ms^{-1} and 240° , and at 500 hPa the values are 20 ms^{-1} and 300° . The thermal wind speed and wind direction are 20 ms^{-1} and 360° , respectively. In this case the isotherms run from north to south, with the warm air to the west. Geostrophic wind and thermal wind are defined and derived in standard texts (Haltiner and Martin 1957, Holton 1979).

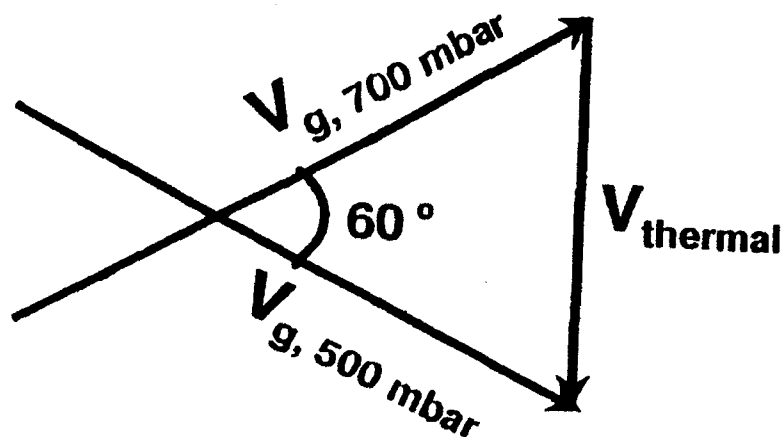


Figure 1. Illustration of the thermal wind for a layer from 700 to 500 hPa (see text).

This report presents some information and sample calculations on the types of errors that may be expected when geostrophic wind or thermal wind is used to estimate the actual wind from data gathered by passive satellite sensors. The assumption is that no additional data are available (that is, only satellite sounding data from sensors of the type found on present day environmental satellites). This report does not treat the improvements that should occur when data from other sources of data (for example, radar profilers, ground-based radiometers, unmanned aerial vehicles) are combined with the satellite data.

2. GEOSTROPHIC WIND

2.1 Basic Derivations

The equation for geostrophic wind along a constant pressure surface is given by

$$V_g = \frac{1}{f} \frac{\partial \phi}{\partial n} \quad (1)$$

where f is $2\Omega \sin \theta$ ($\Omega \sin \theta$ is the angular velocity of the earth about the local zenith at latitude θ , and Ω is the angular velocity at the poles), n is the horizontal distance, ϕ is geopotential height, and V_g is the geostrophic wind component perpendicular to the n direction. In general, geopotential height is $\phi = \int_0^z g dz$ where z is height and g = gravitational acceleration. For z in meters $\phi \approx 0.98z$.

The geostrophic wind also may be computed for a constant level (height) surface where

$$V_g = \frac{1}{\rho f} \frac{\partial p}{\partial n} \text{ where } \frac{1}{\rho} = \frac{R\bar{T}_v}{\bar{p}} \quad (\bar{T}_v = \text{mean virtual temperature along the distance } n \text{ on}$$

the surface, $\bar{p}$ = mean pressure along that same path, and R is the gas constant for dry air). The virtual temperature accounts for moisture in the air, which having a lower density than dry air causes $T_v > T$. However, at temperatures normally found above 4 or 5 km $T \approx T_v$ and for the purposes of this report one may consider $T \approx T_v$ at satellite heights $> 2 \text{ km}$ (generally true over land except in a moist summer or tropical atmosphere). This second form of the geostrophic wind equation can be used to check for changes caused by errors in $\bar{p}$ or $\bar{T}_v$ (or $\bar{T}$).

A similar type of "equilibrium" wind for curved parallel contours is referred to as the gradient wind. In this case, the tangential acceleration = 0. The scalar version of the

$$\text{equation is } V_g = \frac{rf}{2} \left(-1 + \left(1 + 4 \frac{V_g^2}{rf} \right)^{\frac{1}{2}} \right) \text{ where } r = R \tan \alpha \text{ (} R = \text{radius of earth, } \alpha$$

= angular radius of the equivalent small circle for r as seen from the center of the earth, and r = radius of curvature.) The equation may be rewritten for V and V_g in knots and nautical miles, or kilometers per hour and kilometers.

$$V = 1800rf \left(-1 + \left(1 + 4 \frac{V_g^2}{3600rf} \right)^{\frac{1}{2}} \right) \quad (2)$$

The parameter rf may be computed or extracted from standard tables to a sufficient accuracy (List 1984).

Heights of pressure levels are normally computed from the hydrostatic equation

$$z - z_o = - \frac{RT_v}{g} \ln \left(\frac{P}{P_o} \right) \quad (3)$$

where the subscript o refers to the surface or bottom of a layer. As before, $\bar{T}$ may be substituted for $\bar{T}_v$. Here the mean value is along a vertical path for a layer of atmosphere. Computation begins at the surface or a reference p level. The height differences or layer thicknesses ($z - z_o = \Delta z$) are "stacked" upon each other from bottom to top.

The real wind may be defined as the geostrophic wind plus an ageostrophic component. The horizontal part of this component consists of a pressure tendency term and a term involving the change in spacing of the contours (or isobars). To a sufficiently reasonable approximation (Haltner and Martin 1957), the pressure tendency $\left(\frac{\partial p}{\partial t} \right)$ term is given by

$$(V - V_g)_t = \frac{1}{\rho f^2} \frac{\partial}{\partial s} \left(\frac{\partial p}{\partial t} \right) = - \frac{1}{\rho f^2} \frac{\Delta}{\Delta s} \left(\frac{\partial p}{\partial t} \right) \quad (4)$$

where s consists of normal and tangential distances. The term for the change in contour spacing may be found by $(V - V_g)_s = \frac{V}{f} \frac{\partial V_g}{\partial s}$ where V is the real wind. To a fairly reasonable approximation, V on the right side may be approximated by V_g , the mean value along the distance s (in this case along a path equidistant from neighboring contours).

$$(V - V_g)_r \approx \frac{\overline{V_g}}{f} \left(\frac{\Delta V_g}{\Delta s} \right) \quad (5)$$

One may compute values that roughly estimate "typical" magnitudes of the possible errors in wind caused by the geostrophic approximation and errors in the geostrophic wind caused by errors in input values (for example, mean layer temperature). As a first step, wind speed only is considered.

2.2 Errors In V_g Caused By Mean Profile Temperature Error

The geostrophic wind for contours at 100 geopotential meters (gpm) in units of knots (List 1984) may be stated as $V_g = \frac{0.01712}{\Delta n}$ where Δn is in degrees of latitude. At 45° latitude and a contour interval of 30 gpm, and Δn expressed in kilometers,

$$V_g = \frac{5.701 \times 10^3}{\Delta n} \text{ in kn or } V_g = \frac{2.9387 \times 10^3}{\Delta n} \text{ in } ms^{-1} \quad (6)$$

For other contour intervals multiply by the ratio of "new interval"/30 gpm. For a typical midlatitude atmosphere (Jursa 1985), for the surface (assume at 1000 hPa) to 500 hPa layer, the possible error can be computed from net temperature profile error by using equations (3) and (6). The mean layer temperature for the April atmosphere at $45^\circ N$ (Jursa 1985) is used to compute the height of the 500 hPa level.

$$\Delta z = \frac{-287 \text{ K}^{-1} m^2 s^{-2} (265 \text{ K})}{9.81 \text{ ms}^{-2}} (-0.693) = 5373.6 \text{ m} \approx 5266.1 \text{ gpm}$$

Values are computed for differences of $\bar{T}$ of 1 and 2 K, or $\bar{T} = 264$ and 263 K.

$$\Delta z_{264} = 5353.3 \text{ m} \approx 5246.2 \text{ gpm}$$

$$\Delta z_{263} = 5333.1 \text{ m} \approx 5226.4 \text{ gpm}$$

For the case of a difference over the 1000 to 700 hPa layer for the same atmosphere,

$$\Delta z_{268} = \frac{-287 \text{ K}^{-1} m^2 s^{-2}}{9.81 \text{ ms}^{-2}} (268 \text{ K}) (-0.356675) = 2797.0 \text{ m} \approx 2741.1 \text{ gpm}$$

$$\Delta z_{267} = 2786.6 \text{ m} \approx 2730.9 \text{ gpm}$$

$$\Delta z_{266} = 2776.1 \text{ m} \approx 2720.6 \text{ gpm}$$

Similar computations may be made for other layers or sublayers, for example, in table 1. We now assume a "true" $\Delta\phi$ of 30 gpm between soundings 200 km apart. The differences in $\bar{T}$ errors between the soundings are assumed to be 1 and 2 K (for example, the first sounding has a $\bar{T}$ error of 2 K, and the second has an error of 3 K, for a difference in error of 1 K).

TABLE 1. DIFFERENCES IN GPM COMPUTED FOR THE LISTED LAYERS FOR THE LISTED DIFFERENCES IN $\bar{T}$ ERROR BETWEEN TWO SOUNDINGS 200 KM APART.

$\bar{T}$ Difference	Layer (hPa)				
(K)	1000-900	1000-800	1000-700	1000-600	1000-500
0	0	0	0	0	0
1	3.0	6.4	10.2	14.7	19.9
2	6.1	12.8	20.5	29.3	39.7

Equation (6) can be used to compute the V_g values for the "measured" difference (30 gpm) over 200 km, and V_g arising from the two $\bar{T}$ error differences (1 and 2 K), for both the entire 1000 to 500 hPa layer and the several sublayers. Table 1 shows the gpm differences and table 2 shows values of V_g .

TABLE 2. VALUE OF V_g IN ms^{-1} COMPUTED FOR THE LISTED LAYERS AND DIFFERENCES IN $\bar{T}$ ERROR BETWEEN TWO SOUNDINGS 200 KM APART. $\Delta\phi$ DIFFERENCES WERE ADDED TO THE "MEASURED" 30 GPM TO OBTAIN THE VALUES SHOWN.

$\bar{T}$ Difference	Layer (hPa)				
(K)	1000-900	1000-800	1000-700	1000-600	1000-500
0	14.7	14.7	14.7	14.7	14.7
1	16.2	17.8	19.7	21.9	24.4
2	17.7	21.0	24.7	29.0	34.1

Table 2 shows that the V_g differences are about 9.7, 5.0, and 1.5 ms^{-1} respectively for the layer and, for example, the 1000 to 700 hPa and 1000 to 900 hPa sublayers for a $\bar{T}$ error difference of 1 K. For a 2-K difference, the V_g differences are about 19.4, 10.0, and 3.0 ms^{-1} , respectively.

These differences in V_g are not small and may even result in a 180-degree change in direction (for example, subtracting 39.7 gpm from 30 gpm gives -9.7 ms^{-1} (reversed direction of the gradient) resulting in a small V_g in the opposite direction).

2.3 Errors Caused By Curved Flow

One may compute the difference in wind speed caused by the flow being curved instead of straight (along a great circle). For this comparison, the gradient wind for moderate geostrophic winds (15 and 30 ms^{-1}) is computed. From tables in List (1984) an rf parameter of 0.062 at a latitude of 45° is obtained for a radius of curvature (r) of about 600 nm (≈ 1110 km). For $V_g = 15$ ms^{-1} ,

$$V = 111.6sh^{-1}nms^{-1} \left(-1 + \left(1 + \frac{4(29.1nmh^{-1})}{3600sh^{-1}0.062nms^{-1}} \right)^{\frac{1}{2}} \right) = 26.1 \text{ kn} = 13.5 \text{ ms}^{-1}.$$

Also, for $V_g = 30$ ms^{-1} ,

$$V = 47.9 \text{ kn} = 24.7 \text{ ms}^{-1}$$

The two differences ($V - V_g$) computed above are 1.5 and 5.3 ms^{-1} .

2.4 Errors Caused by Mean Temperature Error

Another possible cause of error is an incorrect value of $\bar{T}$ but no difference in $\bar{T}$ error between the two soundings (same $\bar{T}$ error at both locations). The constant level surface version of equation (1) is used; that is, $V_g \approx \frac{R\bar{T}}{f\bar{p}} \frac{\Delta p}{\Delta n}$, where the assumption is that

$$\Delta p = 20 \text{ mbar}, \Delta n = 1000 \text{ km}, \bar{p} = 700 \text{ mbar}, \text{lat} = 45^\circ$$

For $\bar{T} = 270$ K,

$$V_g = \frac{(287 \text{ K}^{-1}m^2s^{-2}) 270 \text{ K} \left(\frac{20 \text{ mbar}}{10^6 \text{ m}} \right)}{1.03(10^{-4})s^{-1} 700 \text{ mbar}} = 21.5 \text{ ms}^{-1},$$

and for $\bar{T} = 267$ K,

$$V_g = 21.3 \text{ ms}^{-1}.$$

The difference in these moderate values of V_g is about 0.2 ms^{-1} . The likely error of a few tenths of a meter per second for moderate V_g is small relative to the other possible errors.

2.5 Errors From Ageostrophic Deviations

A significant potential source of error arises from not considering certain deviations from the geostrophic wind, which may be roughly approximated by the horizontal ageostrophic wind components. Equation (4) may be used to approximate the ageostrophic component arising from the pressure tendency.

Here a pressure tendency normal to the wind of -1 hPa over 1 h near 45° latitude is considered. One hPa = $10 \text{ kg m}^{-1}\text{s}^{-2}$ and the air density (ρ) = 1 kg m^{-3} .

$$(V - V_g)_t \approx \frac{-1}{1 \text{ kg m}^{-3}(1.03 \text{ s}^{-1})^2} \left(\frac{1}{2 \text{ m}} \right) \left(\frac{-10 \text{ kg m}^{-1}\text{s}^{-2}}{3600 \text{ s}} \right) \approx 1.3 \text{ ms}^{-1}$$

If the tangential component was the same size, the rough magnitude of the total pressure tendency term would be about 1.7 ms^{-1} .

Equation (5) expresses the ageostrophic component arising from a change in the spacing of contours on a constant pressure surface (or isobars on a constant height surface). A change of geostrophic wind of 2 ms^{-1} over a distance of 200 km is not unreasonable. For geostrophic wind speeds of 15 ms^{-1} and 30 ms^{-1} , at 45° latitude,

$$(V - V_g)_s \approx \frac{15 \text{ ms}^{-1}}{1.03(10^{-4})\text{s}^{-1}} \left(\frac{2 \text{ ms}^{-1}}{2(10^5)\text{m}} \right) \approx 1.5 \text{ ms}^{-1}$$

$$\text{and } (V - V_g)_t \approx 2.9 \text{ ms}^{-1}$$

Higher values of V_g or ΔV_g can occur, leading to higher values of this "contour spacing" component. When both components are combined, the ageostrophic part of the "real" horizontal wind may exceed 5 ms^{-1} (or $< 1 \text{ ms}^{-1}$ if the two terms tend to cancel or V_g is small).

2.6 Apparent Error From Direction Deviations

So far the error caused by incorrect orientation of the gradient has not been explicitly considered. Jedlovec (1985) reported on differences between gradients derived from data of the visible infrared spin scan radiometer (VISSR) atmospheric sounder (VAS) carried on the geostationary operational environmental satellite (GOES) and those computed using data from a special dense net of rawinsondes (50-km spacing). The differences ranged from a few degrees (almost parallel) to about 90° (nearly perpendicular). In the absence of other factors, an error in direction of the gradient (or contours) of around 30° could lead to a difference in V_g along the expected wind direction of about 2.0 and 4.0 ms^{-1} for V_g values of 15 and 30 ms^{-1} , respectively. A realistic high deviation in gradient near 45° could produce V_g differences of about 4.4 and 8.8 ms^{-1} for the aforementioned V_g values. While even good quality data from rawinsondes may contain wind velocity errors, the deviations in direction reported by Jedlovec (1985) may reflect real differences from the true direction of the gradient (or contours).

2.7 Net Error Values

Table 3 lists some of the potential causes of error in satellite-derived estimates of wind speed that use the geostrophic wind, along with possible magnitudes of those errors. A moderate wind speed is assumed (10 to 30 ms^{-1}).

TABLE 3. POSSIBLE MAGNITUDES OF ERROR IN WIND SPEED ARISING FROM LISTED CAUSES FOR SATELLITE-DERIVED GEOSTROPHIC WINDS.

Cause		Resultant Wind Speed Error (ms^{-1})
1	Incorrect $\bar{T}$	0.1 to 0.4
2	Gradient instead of Geostrophic Flow	1 to 5
3	Computed contour gradient incorrect (varying error in T sounding)*	5 to 20
4	Ageostrophic component Pressure tendency Contour spacing change	0.5 to 2 1 to 5
5	Incorrect direction of gradient (height or pressure)	Near 0 to 10 (Component in expected direction of wind)

*For the T sounding error (item 3) a layer of at least 300 hPa was assumed (for example, near sea level surface to about 3 km AGL, the region of largest satellite temperature error over land).

These values may tend to augment or cancel one another. For example, items 3 and 4 may result in errors of over 20 ms^{-1} or only 1 or 2 ms^{-1} . Miers et al. (1992) and their references report satellite geostrophic wind errors from ± 4 to $\pm 14 \text{ ms}^{-1}$, generally compared with wind speeds measured by rawinsondes. Rawinsonde data also may have errors, ranging from $< 1 \text{ ms}^{-1}$ for high quality equipment to $> 2.5 \text{ ms}^{-1}$ for older (now mostly obsolete) equipment (Fisher et al. 1987). Reasonable "middle of the road" errors (1 to 4 of table 3) from this analysis may lead to a "total error of about 15 to 20 ms^{-1} where the individual errors sum together or perhaps only 2 or 3 ms^{-1} where they largely cancel.

Deviations in direction of the gradient or contours from the actual direction (Miers et al. 1992, Jedlovec 1985) could result in apparent errors of up to 10 ms^{-1} . This "error" would be important for computing the wind speed for a specified direction. An example would be the cross or along trajectory wind speed for an artillery application. The apparent error (but a real component error) could either increase or decrease the "true" error. For example, an error in wind speed of 10 ms^{-1} combined with a deviation in gradient direction could result in a down range error of approximately 15 or 5 ms^{-1} .

The net errors shown in table 3 represent a range of "typical" values for moderate wind speeds (10 to 30 ms^{-1}). However, the reader may compute other values of potential errors for greater or lesser wind speeds, as well as for other parameters (for example, different radii of curvature, or differences in $\bar{T}$ error less than 0.5 K or greater than 2 K). The reader may elect to calculate new potential errors for one or more of the causes of table 3 to arrive at additional net error values. Appendix A contains a selection of tables from List (1984) that should suffice, along with the equations presented herein, for nearly all additional calculated errors.

3. THERMAL WIND

3.1 Basic Derivations

A number of texts provide information on formulations of the thermal wind (Haltiner and Martin 1957, Holton 1979). The form derived in Holton (1979) is used here. Given the horizontal components of the geostrophic wind in geopotential form,

$$u_g = -\frac{1}{f} \frac{\partial \phi}{\partial y} \quad \text{and} \quad v_g = \frac{1}{f} \frac{\partial \phi}{\partial x} \quad (7)$$

and

$$\frac{\partial \phi}{\partial p} = -\frac{1}{\rho} = \frac{RT}{p} \quad (8)$$

When equation (7) is differentiated with respect to p and equation (8) is applied, the results are

$$p \frac{\partial v_z}{\partial g} = \frac{\partial v_z}{\partial \ln p} = - \frac{R}{f} \left(\frac{\partial T}{\partial x} \right)_p$$

$$p \frac{\partial u_z}{\partial p} = \frac{\partial u_z}{\partial \ln p} = \frac{R}{f} \left(\frac{\partial T}{\partial y} \right)_p$$

or in vector form $\frac{\partial \mathbf{V}_z}{\partial \ln p} = - \frac{R}{f} \mathbf{k} \times (\nabla T)_p$

and $\mathbf{V}_T = \mathbf{V}_z(p_1) - \mathbf{V}_z(p_o) = - \frac{R}{f} \int_{p_o}^{p_1} (\mathbf{k} \times \nabla T) d \ln p$

where T = temperature, p = pressure, ρ = density, R = gas constant for dry air, ϕ = geopotential, and $\mathbf{V}_z$ = geostrophic wind. f is the coriolis parameter ($= 2 \Omega \sin \theta$ where Ω is the angular velocity of the earth at the poles and θ is latitude). In component form

$$u_T = - \frac{R}{f} \left(\frac{\partial \bar{T}}{\partial y} \right)_p \ln \left(\frac{p_o}{p_1} \right) \quad (9)$$

$$v_T = \frac{R}{f} \left(\frac{\partial \bar{T}}{\partial x} \right)_p \ln \left(\frac{p_o}{p_1} \right) \quad (10)$$

where $u_T = u_z(p_1) - u_z(p_o)$ and $v_T = v_z(p_1) - v_z(p_o)$ are the thermal wind components defined as the differences in the geostrophic components for the upper p surface, denoted with subscript 1, and the lower p surface, denoted by subscript o. $\bar{T}$ is the mean temperature for the layer from p_o to p_1 , and x and y are distances in the east-west and north-south directions, respectively. An alternative method is to use the geopotential form, or the equivalent "height" form.

$$u_T = - \frac{1}{f} \frac{\partial (\phi_1 - \phi_o)}{\partial y} = - \frac{g}{f} \frac{\partial (z_1 - z_o)}{\partial y}$$

$$v_T = \frac{1}{f} \frac{\partial (\phi_1 - \phi_o)}{\partial x} = \frac{g}{f} \frac{\partial (z_1 - z_o)}{\partial x}$$

Since this paper is concerned with errors in satellite temperature soundings, equations (9) and (10) will be used.

3.2 Errors From Incorrect Mean Temperatures

Equations (9) and (10) may be approximated in finite difference form to a sufficient accuracy.

$$u_T = - \frac{R(\Delta \bar{T})}{f(\Delta y)_p} \ln \left(\frac{P_0}{P_1} \right)$$

$$v_T = \frac{R(\Delta \bar{T})}{f(\Delta x)_p} \ln \left(\frac{P_0}{P_1} \right)$$

Taking differences in errors in $\bar{T}$ between soundings 200 km apart of 0.5, 1, and 2 K, one can compute potential discrepancies in thermal wind for given layers of atmosphere. The 700 to 300 hPa layer will be considered as a whole and subdivided into 100 hPa sublayers. Isotherms orientation will be assumed to be NE-SW (45°) and latitude to be 43° . For the entire layer, for a 2-K error in $\bar{T}$

$$u_T = - \frac{287 \text{ K}^{-1} \text{ m}^2 \text{ s}^{-2}}{10^{-4} \text{ s}^{-1}} \left(\frac{1.414 \text{ K}}{141.4 (10^3 \text{ m})} \right) (0.8473) = - 28.7(0.8473)$$

$$= - 24.3 \text{ ms}^{-1}$$

$$v_T = 24.3 \text{ ms}^{-1}$$

The magnitude (wind speed) from the standard formula is

$$V_T = (u_T^2 + v_T^2)^{\frac{1}{2}} = 34.4 \text{ ms}^{-1}$$

For a 1-K error in $\bar{T}$,

$$u_T = 12.15 \text{ ms}^{-1}$$

$$v_T = 12.15 \text{ ms}^{-1}$$

$$V_T = 17.2 \text{ ms}^{-1}$$

For 0.5-K error in $\bar{T}$,

$$V_T = 8.6 \text{ ms}^{-1}$$

Table 4 shows the values for individual sublayers (I) and the cumulative error (sum of errors from lowest to given layer, C). Slight differences between last cumulative values and values for entire 700 to 300 hPa layer appear because of round off of table values.

TABLE 4. THERMAL WIND VALUES (ms^{-1}) FOR LISTED LAYERS AND DIFFERENCES IN ERRORS IN MEAN TEMPERATURE ($\bar{T}$) BETWEEN SOUNDINGS 200 KM APART.

$\bar{T}$ Difference	Layers (hPa)							
	700-600		600-500		500-400		400-300	
	I	C	I	C	I	C	I	C
0.5	1.6	1.6	1.8	3.4	2.3	5.7	2.9	8.6
1	3.1	3.1	3.7	6.8	4.5	11.3	5.8	17.1
2	6.3	6.3	7.4	13.7	9.1	22.8	11.7	34.5

3.3 Net Potential Error

The results shown in table 4 do not include possible errors in the baseline wind field (for example, wind at 700 hPa), errors arising from not considering curvature, and ageostrophic components. Use of measured wind as the baseline value will reduce the total possible error. However, since the thermal wind itself makes use of the geostrophic approximation, the other sources of error may have an increasingly greater effect as height from the baseline level increases.

As a first estimate of potential errors, one can use the values of table 3, with the range of values from table 4 replacing item 3 (varying error in T sounding causing incorrect contour gradient). Table 5 repeats part of table 3 along with new results from table 4 for a 700 to 300 hPa layer. The values of item 1 of table 5 would be smaller for thinner layers (for example, a range of $< 1 \text{ ms}^{-1}$ to around 12 ms^{-1} for differences in $\bar{T}$ error of a few tenths of a degree to about 2 K for a 100 hPa thick layer).

These errors may tend to augment or cancel one another. For example, items 1 and 3 may result in errors of over 35 ms^{-1} , or only 1 or 2 ms^{-1} . For thinner layers (for example, 700 to 500 hPa) the value of item 1 would be much smaller (table 4), reducing

the overall potential error. However, the numbers in table 2 assume a "perfect" measured wind velocity at 700 hPa. The wind speed error of measured wind (rawinsonde or radar profiler) is likely to have a value near 1 to 2 ms^{-1} (Miers et al. 1992, Fisher et al. 1987). This error also may augment or diminish the "thermal wind" error. Some rough idea of potential error may be obtained by assuming "middle of the road" errors from table 5 (items 1 to 3). The potential total error may reach values over 25 ms^{-1} where the individual errors sum together, or perhaps less than 10 ms^{-1} where they largely cancel.

**TABLE 5. POTENTIAL MAGNITUDES OF ERROR IN THERMAL WIND
GIVEN POSSIBLE DIFFERENCES IN $\bar{T}$ ERROR BETWEEN
SOUNDINGS 200 KM APART.***

Cause		Potential Wind Speed Error (ms^{-1})
1	$\bar{T}$ gradient of layer (700-300 hPa) incorrect	5 to 35
2	Gradient instead of Geostrophic (curved flow)	1 to 5
3	Ageostrophic component	0.5 to 2 1 to 5
	Pressure tendency Contour spacing change	
4	Incorrect direction of temperature gradient	Near 0 to 10

*The assumption is that the difference in $\bar{T}$ error does not exceed 2 K for the 700 to 300 hPa layer. Baseline wind measured at 700 hPa.

Deviations in the temperature or height gradient from the actual direction (Miers et al. 1992, Jedlovec 1985) could result in apparent errors (but a real component error) of up to 10 ms^{-1} in geostrophic wind. These same deviations could cause errors in estimates of thermal wind of about the same size for thicker layers (for example, 700 to 300 hPa). Since thinner layers (for example, 700 to 600 hPa) normally would have smaller thermal wind values, the error from deviations from the true gradient direction would be smaller, perhaps less than 3 ms^{-1} . If a measured baseline wind was not available, the error could be considerably larger. For example, for a 700 to 300 mbar layer use of the geostrophic wind as the baseline wind could lead to errors of over 40 ms^{-1} if the net thermal wind error and the error in the baseline geostrophic wind tended to sum together.

4. CONCLUSION

Errors in satellite estimates of the real wind that use the geostrophic approximation or thermal wind may reach significant values. Net differences between the actual and geostrophic wind from a few to over 20 ms^{-1} are possible, with reasonable middle values of 10 or 12 ms^{-1} . The apparent wind speed error caused by differences in orientation of the geopotential height gradient may increase (or decrease) the component of the geostrophic wind in a specific direction, resulting in an augmentation or reduction in the effect of the other "real" errors. This effect may be especially important for artillery or aviation.

Net differences between the real wind and that derived from the thermal wind may range from a few to over 30 ms^{-1} for thick layers (for example, 700 to 300 hPa), with reasonable middle values around 15 to 18 ms^{-1} . For a thin layer of approximately 100 hPa thickness, the errors may range from 1 to over 10 ms^{-1} with reasonable middle values near 3 to 6 ms^{-1} . The apparent wind speed error caused by differences in temperature gradient orientation may increase (or decrease) the component of the estimated wind in a specific direction. As with the geostrophic wind, this apparent error may augment or reduce the effect of the other "real" errors.

The potential errors described in this report may occur when satellite data are used alone, without any additional data to "tie" down the appropriate satellite values. Some improvement should be possible through the use of new sources of data (Miers et al. 1992) such as radar wind profilers and accompanying radio acoustic sounding system (RASS), ground-based radiometers, and sensors on unmanned aerial vehicles, combined with processing techniques currently under development. In addition, new satellite sensors will eliminate many of the difficulties associated with current instruments. For example, new active sensors planned for early in the next century (for example, the laser atmospheric wind sounder) will measure wind velocity directly for cloud-free lines of sight, and new passive sounders (for example, atmospheric infrared sounder) will improve temperature profiles. In the interim the combination of additional sources of data, new processing techniques, and satellite sensors coming on line by the end of the 1990's (for example, special sensor microwave imager/sounder on Defense Meteorological Satellite Program satellites, and the advanced microwave sounding unit-A on National Oceanic and Atmospheric Administration satellites) may provide the best solution. Descriptions of these sensors may be found in NASA (1991), Patel (1992), and Swadley and Chandler (1992).

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APPENDIX A. TABLES FOR CALCULATING GEOSTROPHIC AND GRADIENT WINDS

This appendix presents a series of tables from List that may be used as an aid in calculating geostrophic and gradient winds. Accompanying explanations are included. For further details see List (1984),¹ Haltiner and Martin (1957),² and Holton (1979).³

¹G. Haltiner and F. Martin, 1957, Dynamical and Physical Met, McGraw-Hill Book Company, NY.

²J. R. Holton, 1979, An Introduction to Dynamic Meteorology, 2nd Edition, Academic Press, New York, NY.

³R. List (Ed), 1984, Smithsonian Met Tables, Smithsonian Institute Press, Washington, DC.

TABLE 37
GEOSTROPHIC WIND, CONSTANT PRESSURE SURFACE
 100 geopotential meter contours

The scalar equation for the geostrophic wind on a constant pressure surface is

$$V_g = \frac{1}{f} \frac{\partial \Phi}{\partial n}$$

where Φ is the geopotential in a constant-pressure surface, n is distance measured in the horizontal direction, f is the coriolis parameter, and V_g is the component of the geostrophic wind normal to the direction in which n is measured.

On a constant pressure surface with contours drawn for intervals of 100 geopotential meters (gpm.) this reduces to

$$V_g(\text{knots}) = \frac{0.017120}{f \Delta n}$$

(continued on next page)

Contour spacing				Latitude							
Degree of Latitude	Kilometers	Statute miles	Nautical miles	10°	15°	20°	25°	30°	35°	40°	45°
1.0	111	69	60	676.0	453.5	343.2	277.9	234.8	204.7	182.6	166.0
1.1	122	76	66	614.6	412.3	312.0	252.5	213.4	186.1	166.0	150.9
1.2	133	83	72	563.3	378.0	286.0	231.5	195.6	170.5	152.2	138.3
1.3	145	90	78	520.0	348.9	264.0	213.7	180.6	157.4	140.5	127.7
1.4	156	97	84	482.9	324.0	245.2	198.4	167.7	146.2	130.4	118.6
1.5	167	104	90	450.7	302.4	228.8	185.2	156.5	136.4	121.7	110.7
1.6	178	111	96	422.5	283.5	214.5	173.6	146.7	127.9	114.1	103.8
1.7	189	117	102	397.7	266.8	201.9	163.4	138.1	120.4	107.4	97.7
1.8	200	124	108	375.6	252.0	190.7	154.3	130.4	113.7	101.5	92.2
1.9	211	131	114	355.8	238.7	180.6	146.2	123.6	107.7	96.1	87.4
2.0	222	138	120	338.0	226.8	171.6	138.9	117.4	102.3	91.3	83.0
2.1	234	145	126	321.9	216.0	163.4	132.3	111.8	97.5	87.0	79.1
2.2	245	152	132	307.3	206.2	156.0	125.3	106.7	93.0	83.0	75.5
2.3	256	159	138	293.9	197.2	149.2	120.8	102.1	89.0	79.4	72.2
2.4	267	166	144	281.7	189.0	143.0	115.7	97.8	85.3	76.1	69.2
2.5	278	173	150	270.4	181.4	137.3	111.1	93.9	81.9	73.0	66.4
2.6	289	180	156	260.0	174.4	132.0	106.8	90.3	78.7	70.2	63.9
2.7	300	187	162	250.4	168.0	127.1	102.9	87.0	75.8	67.6	61.5
2.8	311	193	168	241.4	162.0	122.6	99.2	83.8	73.1	65.2	59.3
2.9	322	200	174	233.1	156.4	118.4	95.8	81.0	70.6	63.0	57.2
3.0	334	207	180	225.3	151.2	114.4	92.6	78.3	68.2	60.9	55.3
3.2	356	221	192	211.3	141.7	107.3	86.8	73.4	64.0	57.1	51.9
3.4	378	235	204	198.8	133.4	100.9	81.7	69.1	60.2	53.7	48.8
3.6	400	249	216	187.3	125.0	95.3	77.2	65.2	56.8	50.7	46.1
3.8	423	263	228	177.9	119.4	90.3	73.1	61.8	53.9	48.1	43.7
4.0	445	276	240	169.0	113.4	85.8	69.4	58.7	51.2	45.7	41.5
4.2	467	290	252	161.0	108.0	81.7	66.1	55.9	48.7	43.5	39.5
4.4	489	304	264	153.6	103.1	78.0	63.1	53.4	46.5	41.3	37.7
4.6	511	318	276	147.0	98.6	74.6	60.4	51.0	44.5	39.7	36.1
4.8	534	332	288	140.8	94.5	71.5	57.9	48.9	42.6	38.0	34.6
5.0	556	345	300	135.2	90.7	68.6	55.6	47.0	40.9	36.5	33.2
5.5	612	380	330	122.9	82.5	62.4	50.5	42.7	37.2	33.2	30.2
6.0	667	415	360	112.7	75.6	57.2	46.3	39.1	34.1	30.4	27.7
6.5	723	449	390	104.0	69.8	52.8	42.7	36.1	31.5	28.1	25.5
7.0	778	484	420	96.6	64.8	49.0	39.7	33.5	29.2	26.1	23.7
8.0	890	553	480	84.5	56.7	42.9	34.7	29.3	25.6	22.8	20.8
9.0	1001	622	540	75.1	50.4	38.1	30.9	26.1	22.7	20.3	18.4
10.0	1112	691	600	67.6	45.4	34.3	27.8	23.3	20.5	18.3	16.6

(To convert knots to other measures of speed see Table 35.)

(continued)

TABLE 37 (CONCLUDED)
GEOSTROPHIC WIND, CONSTANT PRESSURE SURFACE
100 geopotential meter contours

where Δs is the contour spacing measured in degrees of latitude (i.e., one unit of Δs has the length of one degree of latitude at the place for which the contour spacing is measured). Table 37 gives values of V , in knots as a function of Δs and latitude with auxiliary columns giving equivalents of Δs in kilometers, statute miles, and nautical miles. If the latter are measured by a map scale true at some other latitude the value should be corrected to the latitude at which the measurements are taken (see Table 165).

Since the geostrophic wind is inversely proportional to the contour spacing and directly proportional to the contour interval ($\Delta\phi$ gpm.), values of V , for 1/10 of the indicated spacing may be found by multiplying the tabular values by 10, etc., and for contour intervals that are multiples or submultiples of 100 gpm. by multiplying the tabular values by $\Delta\phi/100$ (e.g., for 200 gpm. contours multiply by 2, for 50 gpm. contours multiply by $\frac{1}{2}$, etc.).

Contour spacing				Latitude							
Degrees of Latitude	Kilometers	Statute miles	Nautical miles	50°	55°	60°	65°	70°	75°	80°	85°
1.0	111	69	60	133.2	143.3	155.5	129.5	124.9	121.5	119.2	117.8
1.1	122	76	66	139.3	150.3	163.2	117.7	113.6	110.3	108.4	107.1
1.2	133	83	72	127.7	119.4	113.0	107.9	104.1	101.3	99.3	98.2
1.3	145	90	78	117.9	110.2	104.3	99.6	96.1	93.5	91.7	90.6
1.4	156	97	84	109.3	102.4	96.8	92.3	89.2	86.8	85.1	84.2
1.5	167	104	90	102.2	95.5	90.4	86.3	83.3	81.0	79.3	78.6
1.6	178	111	96	95.3	89.6	84.7	81.0	78.1	75.0	74.3	73.9
1.7	189	117	102	90.1	84.3	79.7	76.2	73.5	71.3	70.1	69.3
1.8	200	124	108	85.1	79.6	75.3	72.0	69.4	67.3	66.2	65.5
1.9	211	131	114	80.7	75.4	71.3	68.2	65.7	64.0	62.7	62.0
2.0	222	138	120	76.5	71.7	67.8	64.8	62.5	60.8	59.6	58.9
2.1	234	145	126	73.0	68.2	64.3	61.7	59.5	57.9	56.8	56.1
2.2	245	152	132	69.7	65.1	61.6	58.9	56.8	55.2	54.2	53.6
2.3	256	159	138	66.6	62.3	58.9	56.3	54.3	52.8	51.8	51.2
2.4	267	166	144	63.8	59.7	56.3	54.0	52.1	50.6	49.7	49.1
2.5	278	173	150	61.3	57.3	54.2	51.8	50.0	48.6	47.7	47.1
2.6	289	180	156	58.9	55.1	52.1	49.8	48.0	46.7	45.8	45.3
2.7	300	187	162	56.8	53.1	50.2	48.0	46.3	45.0	44.1	43.6
2.8	311	193	168	54.7	51.2	48.4	46.3	44.6	43.4	42.6	42.1
2.9	322	200	174	52.8	49.4	46.7	44.7	43.1	41.9	41.1	40.6
3.0	334	207	180	51.1	47.8	45.2	43.2	41.6	40.5	39.7	39.3
3.2	356	221	192	47.9	44.8	42.4	40.3	39.0	38.0	37.2	36.8
3.4	378	235	204	45.1	42.1	39.9	38.1	36.7	35.7	35.1	34.7
3.6	400	249	216	42.5	39.8	37.7	36.0	34.7	33.8	33.1	32.7
3.8	423	263	228	40.3	37.7	35.7	34.1	32.9	32.0	31.4	31.0
4.0	445	276	240	38.3	35.8	33.9	32.4	31.2	30.4	29.8	29.5
4.2	467	290	252	36.3	34.1	32.3	30.8	29.7	28.9	28.4	28.1
4.4	489	304	264	34.8	32.5	30.8	29.4	28.4	27.6	27.1	26.8
4.6	511	318	276	33.3	31.2	29.5	28.2	27.2	26.4	25.9	25.6
4.8	534	332	288	31.9	29.9	28.2	27.0	26.0	25.3	24.8	24.5
5.0	556	345	300	30.6	28.7	27.1	25.9	25.0	24.3	23.8	23.6
5.5	612	380	330	27.9	26.1	24.6	23.5	22.7	22.1	21.7	21.4
6.0	667	413	360	25.3	23.9	22.6	21.6	20.8	20.3	19.9	19.6
6.5	723	449	390	23.6	22.0	20.9	19.9	19.2	18.7	18.3	18.1
7.0	778	484	420	21.9	20.5	19.4	18.5	17.8	17.4	17.0	16.8
8.0	890	553	480	19.2	17.9	16.9	16.2	15.6	15.2	14.9	14.7
9.0	1001	622	540	17.0	15.9	15.1	14.4	13.9	13.5	13.2	13.1
10.0	1112	691	600	15.3	14.3	13.6	13.0	12.5	12.2	11.9	11.8

(To convert knots to other measures of speed see Table 35.)

TABLE 40
GRADIENT WIND

The equation for the gradient wind speed V in cgs units is,

$$V = \frac{V_g}{2} \left(-1 + \sqrt{1 + \frac{4V_g^2}{r^2}} \right), \quad (1)$$

where

r = "radius of curvature" of the trajectory = $R \tan \alpha$ (see Table 166),

f = Coriolis parameter $2\omega \sin \phi$ (ω = angular velocity of rotation of the earth,
 ϕ = latitude),

V_g = geostrophic wind speed (see Tables 37-39).

Equation (1) can be rewritten in the following form

$$V = \frac{3600}{2} \frac{r}{f} \left(-1 + \sqrt{1 + \frac{4V_g^2}{3600 r^2}} \right) \quad (2)$$

for any of the following consistent combinations of units:

- V and V_g in miles per hour, r in statute miles,
- " " " " knots, r in nautical miles,
- " " " " kilometers per hour, r in kilometers.

V is a function of the parameter r/f and of the geostrophic wind speed V_g only. In applying equations (1) and (2) the following sign convention is necessary: for cyclonic curvature $r/f > 0$, for anticyclonic curvature $r/f < 0$.

Table 40 A gives values of the parameter r/f as a function of latitude, ϕ , and r . Table 40 B gives values of V for cyclonic curvature and Table 40 C for anticyclonic curvature as a function of the parameter r/f and the geostrophic wind speed V_g .

To find the gradient wind speed at a given point:

- Determine the latitude ϕ and the value r of the trajectory. (Table 166 indicates a method for finding r on a polar stereographic map projection; for other projections an estimate must be made.)
- From Table 40 A find the parameter r/f . (This parameter is linear in r so that values for other radii than those given may be readily determined from the table, e.g., if $r = 2300$, add the values for $r = 2000$ and $r = 300$.)
- Determine the geostrophic wind speed V_g at the given point (see Tables 37-39). (V_g and r must be in one of the consistent combinations of units given above.)
- Enter Table 40 B (cyclonic case) or Table 40 C (anticyclonic case) with the arguments r/f and V_g . The corresponding tabular value is the gradient wind V in the same units as V_g .

(continued)

TABLE 40 (CONTINUED)

GRADIENT WIND

TABLE 40 A.—Values of the parameter r/l

Radius of curvature r	Latitude																
	10°	15°	20°	25°	30°	35°	40°	45°	50°	55°	60°	65°	70°	75°	80°	85°	90°
100	0.002	0.004	0.005	0.006	0.007	0.008	0.009	0.010	0.011	0.012	0.013	0.013	0.014	0.014	0.014	0.015	0.015
200	.005	.008	.010	.012	.015	.017	.019	.021	.022	.024	.025	.026	.027	.028	.029	.029	.029
300	.008	.011	.015	.018	.022	.025	.028	.031	.034	.036	.038	.040	.041	.042	.043	.044	.044
400	.010	.015	.020	.025	.029	.033	.037	.041	.045	.048	.051	.053	.055	.056	.057	.058	.058
500	.015	.019	.025	.031	.036	.042	.047	.052	.056	.060	.063	.066	.069	.070	.072	.073	.073
600	.015	.023	.030	.037	.044	.050	.056	.062	.067	.072	.076	.079	.082	.085	.086	.087	.088
700	.018	.026	.035	.043	.051	.059	.066	.072	.078	.084	.088	.093	.096	.099	.101	.102	.102
800	.020	.030	.040	.049	.058	.067	.075	.083	.089	.096	.101	.106	.110	.113	.115	.116	.117
900	.023	.034	.045	.055	.066	.075	.084	.093	.101	.108	.114	.119	.123	.127	.129	.131	.131
1000	.025	.038	.050	.062	.073	.084	.094	.103	.112	.119	.126	.132	.137	.141	.144	.145	.146
1100	.028	.042	.055	.068	.080	.092	.103	.113	.123	.131	.139	.145	.151	.155	.158	.160	.160
1200	.030	.045	.060	.074	.088	.100	.112	.124	.134	.143	.152	.159	.164	.169	.172	.174	.175
1300	.033	.049	.065	.080	.095	.109	.122	.134	.145	.155	.164	.172	.178	.183	.187	.189	.190
1400	.035	.053	.070	.086	.102	.117	.131	.144	.156	.167	.177	.185	.192	.197	.201	.203	.204
1500	.038	.057	.075	.092	.109	.126	.141	.155	.168	.179	.189	.198	.206	.211	.215	.218	.219
1600	.041	.060	.080	.099	.117	.134	.150	.165	.179	.191	.202	.211	.219	.225	.230	.232	.233
1700	.043	.064	.085	.105	.124	.142	.159	.175	.190	.203	.215	.225	.233	.239	.244	.247	.248
1800	.046	.068	.090	.111	.131	.151	.169	.186	.201	.215	.227	.238	.247	.254	.259	.262	.263
1900	.048	.072	.095	.117	.139	.159	.178	.196	.212	.227	.240	.251	.260	.268	.273	.276	.277
2000	.051	.075	.100	.123	.146	.167	.187	.206	.223	.239	.253	.264	.274	.282	.287	.291	.292
2500	.063	.094	.125	.154	.182	.209	.234	.258	.279	.299	.316	.330	.343	.352	.359	.363	.365
3000	.076	.113	.150	.185	.219	.251	.281	.309	.335	.358	.379	.397	.411	.423	.431	.436	.438

(continued)

(continued)

SMITHSONIAN METEOROLOGICAL TABLES

TABLE 40. (CONTINUED)

GRADIENT WIND

TABLE 40 B.—Cyclonic curvature

$V, \text{ m/s}$	.02	.04	.06	.08	.10	.12	.14	.16	.18	.20	.30	.40	.50	.60
5	3	4	4	5	5	5	5	5	5	5	5	5	5	5
10	6	7	7	9	10	10	10	10	10	10	10	10	10	10
15	9	10	11	13	14	14	14	15	15	15	15	15	15	15
20	12	13	14	16	17	18	18	19	19	19	20	20	20	20
25	15	16	17	19	20	21	22	23	24	24	24	25	25	25
30	18	19	20	22	23	24	25	26	27	28	29	29	30	30
35	21	22	23	25	26	27	28	29	30	31	31	32	32	33
40	24	25	26	28	29	30	31	32	33	34	34	35	35	36
45	27	28	29	31	32	33	34	35	36	37	37	38	38	39
50	30	31	32	34	35	36	37	38	39	40	40	41	41	42
60	36	37	38	40	41	42	43	44	45	46	46	47	47	48
70	42	43	44	46	47	48	49	50	51	52	53	54	54	55
80	48	49	50	52	53	54	55	56	57	58	58	59	59	60
90	54	55	56	58	59	60	61	62	63	64	64	65	65	66
100	60	61	62	64	65	66	67	68	69	70	70	71	71	72
120	72	73	74	76	77	78	79	80	81	82	83	84	84	85
140	84	85	86	88	89	90	91	92	93	94	94	95	95	96
160	96	97	98	100	101	102	103	104	105	106	106	107	107	108
180	108	109	110	112	113	114	115	116	117	118	118	119	119	120
200	120	121	122	124	125	126	127	128	129	130	130	131	131	132
220	132	133	134	136	137	138	139	140	141	142	142	143	143	144
240	144	145	146	148	149	150	151	152	153	154	154	155	155	156
260	156	157	158	160	161	162	163	164	165	166	166	167	167	168
280	168	169	170	172	173	174	175	176	177	178	178	179	179	180
300	180	181	182	184	185	186	187	188	189	190	190	191	191	192
320	192	193	194	196	197	198	199	200	201	202	202	203	203	204
340	204	205	206	208	209	210	211	212	213	214	214	215	215	216
360	216	217	218	220	221	222	223	224	225	226	226	227	227	228
380	228	229	230	232	233	234	235	236	237	238	238	239	239	240
400	240	241	242	244	245	246	247	248	249	250	250	251	251	252
420	252	253	254	256	257	258	259	260	261	262	262	263	263	264
440	264	265	266	268	269	270	271	272	273	274	274	275	275	276
460	276	277	278	280	281	282	283	284	285	286	286	287	287	288
480	288	289	290	292	293	294	295	296	297	298	298	299	299	300
500	300	301	302	304	305	306	307	308	309	310	310	311	311	312

(continued)

UNITED STATES METEOROLOGICAL TABLES

TABLE 40 (CONCLUDED)

GRADIENT WIND

TABLE 40 C.—Anticyclonic curvature

V_c	r	.005	.007	.008	.009	.01	.02	.03	.04	.05	.06	.07	.08	.09	.10	.11	.12	.13	.14	.15	.16	.17	.18	.19	.20	.30	.40	.50	.60	
5	5	8	7	6	6	6	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5		
10	10						12	11	11	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	
15	15						21	18	17	16	16	16	16	16	16	16	16	16	16	15	15	15	15	15	15	15	15	15	15	
20	20							26	24	23	22	22	22	21	21	21	21	21	21	21	21	21	21	21	20	20	20	20	20	
25	25							39	32	30	29	28	28	27	27	27	27	26	26	26	26	26	26	26	26	25	25	25	25	
30	30								43	38	36	35	34	34	33	33	32	32	32	32	32	32	32	31	31	31	30	30	30	
35	35								60	48	44	42	41	40	39	39	38	38	38	38	37	37	37	37	36	36	36	36	36	
40	40									60	53	50	48	47	46	45	44	44	44	44	43	43	43	42	42	41	41	41	41	
45	45										64	59	56	54	53	52	51	50	50	50	49	49	48	48	47	46	46	46	46	
50	50										79	69	64	62	60	59	58	57	56	56	55	55	54	54	54	52	52	51	51	
60	60											98	85	80	76	74	72	71	70	69	68	67	67	66	66	63	63	62	62	
70	70											120	102	95	91	88	86	84	83	82	81	80	79	79	75	74	73	72	72	
80	80												144	120	111	106	102	100	98	96	95	94	92	92	87	85	84	83	83	
90	90														138	128	122	117	114	112	110	108	107	105	99	96	95	94	94	
100	100															157	145	138	132	129	126	124	122	120	112	108	106	105	105	
120	120																197	180	170	164	159	155	152	138	132	129	128	128	128	
140	140																		240	217	205	196	190	165	157	153	151	151	151	
160	160																				288	255	240	195	183	178	174	174	174	
180	180																							228	211	201	198	198	198	
200	200																							265	240	229	223	223	223	
220	220																								308	271	257	249	249	249
240	240																								360	304	285	275	275	275
260	260																								436	340	315	302	302	302
280	280																									381	347	331	331	331
300	300																									426	380	360	360	360
340	340																									550	455	423	423	423
380	380																										545	492	492	492
420	420																										668	668	668	668
460	460																											786	786	786
500	500																												786	786

NOTE.—The critical value of V in the anticyclonic case is defined as that value of V for which the radical in equation (2) is equal to zero.

Values of V are tabulated only when they are less than the critical value. For imaginary values of equation (2) no gradient wind can be specified; if such a condition existed, the wind would not flow along the isobars. At the critical value of V , the following apply:

$$V_{critical} = 2V_c$$
$$(r)_{critical} = -\frac{V_c}{900}$$

NOTE.—The critical value of V in the anticyclonic case is defined as that value of V for which the radical in equation (2) is equal to zero.

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$$V_{critical} = 2V_c$$

$$(r)_{critical} = -\frac{V_c}{900}$$

ANTICYCLONIC METEOROLOGICAL TABLES

TABLE 166

RADIUS OF CURVATURE ON A POLAR STEREOGRAPHIC PROJECTION

In computing gradient wind speeds (Table 40) and in other problems it is necessary to determine a factor r which depends on curvature of the trajectory. This factor arises in taking account of the horizontal component of the centrifugal force acting on a particle. The problem is twofold: (1) to determine the trajectory of the particle on a map, and (2) to determine the required value of r if the trajectory on the map is known. The first problem is of such nature that it cannot be treated adequately here. (NOTE.—In many cases an approximation is made from the curvature of the isobars or streamlines.) The second problem has been solved for the case of a polar stereographic projection, since on this projection a "small circle" on the earth projects as a circle on the map. Table 40 provides a means for computing the desired r for trajectories on a polar stereographic projection.

Let R be the radius of the earth, r' the true radius of the "small circle" on which the particle is assumed to be traveling at a given instant, and a its angular radius (as seen from the center of the earth). Then $r' = R \sin a$. Since we are concerned with the horizontal component of the centrifugal force, the effective horizontal radius of the curvature required in the gradient wind equation is given by $r = r' \sec a = R \tan a$. If an arc on a map representing the instantaneous trajectory of a particle of air is determined, this arc may be regarded as a portion of a "small circle."

To determine r for a given arc of a trajectory on the map:

1. Complete the circle by extending the arc (a set of circular templates will prove very useful).
2. Find the meridian which passes through the center of this circle.
3. Determine the latitudes ϕ_1 and ϕ_2 of the points where this meridian intersects the circle (extend the meridian across the pole if necessary).
- 4A. If the circle found in step 1 *does not* contain the pole, find the difference between ϕ_1 and ϕ_2 and enter part A of the table with this difference as the argument. The corresponding tabular value is the required radius r in statute miles, from the formula $r = R \tan \frac{1}{2}(\phi_1 - \phi_2)$.
- 4B. If the circle found in step 1 contains the pole, find the sum $(\phi_1 + \phi_2)$ and enter part B of the table with this sum as the argument. The corresponding tabular value is the required radius r in statute miles, from the formula $r = R \tan [90^\circ - \frac{1}{2}(\phi_1 + \phi_2)]$.

(continued)

TABLE 166

RADIUS OF CURVATURE ON A POLAR STEREOGRAPHIC PROJECTION

A. Circle not including pole.										
$\phi_1 - \phi_2$	0	1	2	3	4	5	6	7	8	9
	mi.	mi.	mi.	mi.	mi.	mi.	mi.	mi.	mi.	mi.
0°	0	35	69	104	138	173	207	242	277	311
10	346	381	416	451	486	521	556	591	627	662
20	653	733	769	805	841	877	914	950	987	1023
30	1060	1097	1135	1172	1210	1248	1286	1324	1363	1401
40	1440	1479	1519	1559	1599	1639	1680	1721	1762	1803
50	1845	1887	1930	1973	2016	2060	2104	2148	2193	2239
60	2235	2331	2373	2425	2473	2521	2570	2619	2669	2720
70	2771	2822	2875	2928	2982	3036	3092	3148	3204	3262
80	3320	3380	3440	3501	3563	3626	3690	3755	3821	3889
90	3957									
B. Circle including pole.										
$\phi_1 + \phi_2$	0	1	2	3	4	5	6	7	8	9
	mi.	mi.	mi.	mi.	mi.	mi.	mi.	mi.	mi.	mi.
0°		455433	226697	151110	113313	90631	75504	64697	56589	50278
10	45229	41693	37648	34730	32227	30057	28156	26477	24984	23646
20	22441	21350	20357	19449	18616	17849	17140	16482	15871	15301
30	14768	14249	13800	13358	12943	12550	12178	11825	11492	11174
40	10872	10583	10308	10045	9794	9553	9322	9100	8897	8683
50	8486	8256	8113	7937	7766	7601	7442	7288	7138	6994
60	6854	6718	6586	6457	6332	6211	6093	5978	5867	5757
70	5651	5547	5446	5347	5251	5157	5065	4975	4886	4800
80	4716	4633	4552	4473	4395	4318	4243	4170	4097	4027
90	3957	3889	3821	3755	3690	3626	3563	3501	3440	3380
100	3320	3262	3204	3148	3092	3036	2982	2928	2875	2822
110	2771	2720	2669	2619	2570	2521	2473	2425	2378	2331
120	2285	2239	2193	2148	2104	2060	2016	1973	1930	1887
130	1845	1803	1762	1721	1680	1639	1599	1559	1519	1479
140	1440	1401	1363	1324	1286	1248	1210	1172	1135	1097
150	1060	1023	987	950	914	877	841	805	769	733
160	698	662	627	591	556	521	486	451	416	381
170	346	311	277	242	207	173	138	104	69	35

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