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MILITARY HANDBOOK

METALLIC MATERIALS AND ELEMENTS FOR AEROSPACE VEHICLE STRUCTURES

Volume 2 of 2 Volumes

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FOREWORD

1. This military handbook is approved for use by all Departments and Agencies of the Department of Defense and the Federal Aviation Administration.

2. Beneficial comments (recommendations, additions, deletions) and any pertinent data which may be of use in improving this document should be addressed to: Chairman, MIL-HDBK-5 Coordination Activity (513-255-5128), WL/MLSE, Wright-Patterson AFB, OH 45433-6533, by using the self-addressed Standardization Document Improvement Proposal (DD Form 1426) appearing at the end of this document or by letter.

3. This document contains design information on the strength properties of metallic materials and elements for aerospace vehicle structures. All information and data contained in this handbook have been coordinated with the Air Force, Army, Navy, Federal Aviation Administration, and industry prior to publication, and are being maintained as a joint effort of the Department of Defense and the Federal Aviation Administration.

Custodians:
Army—AV
Navy—AS
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Army—ME, MI
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EXPLANATION OF NUMERICAL CODE

For chapters containing materials properties, a deci-numeric system is used to identify sections of text, tables, and illustrations. This system is explained in the examples shown below. Variations of this deci-numerical system are also used in Chapters 1, 8, and 9.

Example A

2.4.2.1.1

General material category (in this case, steel) .....

A logical breakdown of the base material by family characteristics (in this case, intermediate alloy steels); or for element properties .....

Particular alloy to which all data are pertinent. If zero, section contains comments on the family characteristics .....

If zero, section contains comments specific to the alloy; if it is an integer, the number identifies a specific temper or condition (heat treatment) .....

Type of graphical data presented on a given figure (see following description) .....

Example B

3.2.3.1.X

Aluminum .....

2000 Series Wrought Alloy .....

2024 Alloy .....

T3, T351, T3510, T3511, T4, and T42 Tempers .....

Specific Property as Follows .....

Tensile properties (ultimate and yield strength)	1
Compressive yield and shear ultimate strengths	2
Bearing properties (ultimate and yield strength)	3
Modulus of elasticity, shear modulus	4
Elongation, total strain at failure, and reduction of area	5
Stress-strain curves, tangent-modulus curves	6
Creep	7
Fatigue	8
Fatigue-Crack Propagation	9
Fracture Toughness	10

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Chapter 5

TITANIUM

5.1 General

This chapter contains the engineering properties and related characteristics of titanium and titanium alloys used in aircraft and missile structural applications.

General comments on engineering properties and the considerations relating to alloy selection are presented in Section 5.1. Mechanical- and physical-property data and characteristics pertinent to specific alloy groups or individual alloys are reported in Sections 5.2 through 5.5.

Titanium is a relatively lightweight, corrosion-resistant structural material that can be strengthened greatly through alloying and, in some of its alloys, by heat treatment. Among its advantages for specific applications are: good strength-to-weight ratio, low density, low coefficient of thermal expansion, good corrosion resistance, good oxidation resistance at intermediate temperatures, good toughness, and low heat-treating temperature during hardening, and others.

5.1.1 TITANIUM INDEX.—The coverage of titanium and its alloys in this chapter has been divided into four sections for systematic presentation. The system takes into account unalloyed titanium and three groups of alloys based on metallurgical differences which in turn result in differences in fabrication and property characteristics. The sections and the individual alloys covered under each are shown in Table 5.1.

5.1.2 MATERIAL PROPERTIES.—The material properties of titanium and its alloys are determined mainly by their alloy content and heat treatment, both of which are influential in determining the allotropic forms in which this material will be bound. Under equilibrium conditions, pure titanium has an "alpha" structure up to 1620 F, above which it transforms to a "beta" structure. The inherent properties of these two structures are quite different. Through alloying and heat treatment, one or the other or a combination of these two structures call be made to exist at service temperatures, and the properties of the material vary accordingly. References 5.1.2(a) and (b) provide general discussion of titanium microstructures and associated metallography.

TABLE 5.1 *Titanium Alloys Index*

Section	Alloy Designation
5.2	**Unalloyed Titanium**
5.2.1	Commercially Pure Titanium
5.3	**Alpha and Near-Alpha Titanium Alloys**
5.3.1	Ti-5A1-2.5Sn (Alpha)
5.3.2	Ti-8A1-1Mo-1V (Near-Alpha)
5.3.3	Ti-6A1-2Sn-4Zr-2Mo (Near-Alpha)
5.4	**Alpha-Beta Titanium Alloys**
5.4.1	Ti-6A1-4V
5.4.2	Ti-6A1-6V-2Sn
5.5	**Beta, Near-Beta, and Metastable Titanium Alloys**
5.5.1	Ti-13V-11Cr-3A1
5.5.2	Ti-15V-3Cr-3Sn-3A1
5.5.3	Ti-10V-2Fe-3A1

Titanium and titanium alloys of the alpha and alpha-beta type exhibit crystallographic textures in sheet form in which certain crystallographic planes or directions are closely aligned with the direction of prior working. The presence of textures in these materials lead to anisotropy with respect to many mechanical and physical properties. Poisson's ratio and Young's modulus are among those properties strongly affected by texture. Wide variations experienced in these properties both within and between sheets of titanium alloys have been qualitatively related to variations of texture. In general, the degree of texturing, and hence the variation of Young's modulus and Poisson's ratio, that is developed for alpha-beta alloys tends to be less than that developed in all alpha titanium alloys. Rolling temperature has a pronounced effect on the texturing of titanium alloys which may not in general be affected by subsequent thermal treatments. The degree of applicability of the effect of textural variations discussed above on the mechan-

ical properties of products other than sheet is unkown at present. The values of Young's modulus and Poisson's ratio listed in this document represent the usual values obtained on products resulting from standard mill practices. References 5.1.2(c) and (d) provide further information on texturing in titanium alloys.

5.1.2.1 *Mechanical Properties.*

5.1.2.1.1 *Fracture Toughness.*—The fracture toughness of titanium alloys is greatly influenced by such factors as chemistry variations, heat treatment, microstructure, and product thickness, as well as yield strength. For fracture critical applications, these factors should be closely controlled. Typical values of plane-strain fracture toughness for titanium alloys are presented in Table 5.1.2.1.1. Minimum average, and maximum values, as well as coefficient of variation are presented for various products for which valid data are available, but these values do not have the statistical reliability of the room-temperature mechanical properties.

5.1.3 MANUFACTURING CONSIDERATIONS.—Comments relating to formability, weldability, and final heat treatment are presented under individual alloys. These comments are necessarily brief and are intended only to aid the designer in the selection of an alloy for a specific application. In practice, departures from recommended practices are very common and are based largely on in-plant experience. Springback is nearly always a factor in hot or cold forming.

Final heat treatments that are indicated as "specified" heat treatments do not necessarily coincide with the producers' recommended heat treatments. Rather, these treatments, along with the specified room-temperature minimum tensile properties, are contained in the heat treating-capability requirements of applicable specifications, for example, MIL-H-81200. Departures from the specified aging cycles are often necessary to account for aging that may take place during hot working or hot sizing or to obtain more desirable mechanical properties, for example, improved fracture toughness. More detailed recommendations for specific applications are generally available from the material producers.

5.1.4 ENVIRONMENTAL CONSIDERATIONS.—Comments relating to temperature limitations in the application of titanium and titanium alloys are presented under the individual alloys.

Below about 300 F, as well as above about 700 F, creep deformation of titanium alloys can be expected at stresses below the yield strength. Available data indicate that room-temperature creep of unalloyed titanium may be significant (exceed 0.2 percent creep-strain in 1,000 hours) at stresses that exceed approximately 50 percent F_{ty}, room-temperature creep of Ti-5A1-1.5Sn ELI may be significant at stresses above approximately 60 percent F_{ty}, and room-temperature creep of the standard grades of titanium alloys may be significant at stresses above approximately 75 percent F_{ty}. References 5.1.4(a) through (c) provide some limited data regarding room-temperature creep of titanium alloys.

The use of titanium and its alloys in contact with either liquid oxygen or gaseous oxygen at cryogenic temperatures should be avoided, since either the presentation of a fresh surface (such as produced by tensile rupture) or impact may initiate a violent reaction [Reference 5.1.4(d)]. Impact of the surface in contact with liquid oxygen will result in a reaction at energy levels as low as 10 ft-lb. In gaseous oxygen, a partial pressure of about 50 psi is sufficient to ignite a fresh titanium surface over the temperature range from -250 F to room temperature or higher.

Titanium is susceptible to stress-corrosion cracking in certain anhydrous chemicals including methyl alcohol and nitrogen textroxide. Traces of water tend to inhibit the reaction in either environment. However, in N_2O_4, NO is preferred and inhibited N_2O_4 contains 0.4 to 0.8 percent NO. Red fuming nitric acid with less than 1.5 percent water and 10 to 20 percent NO_2 can crack the metal and result in a pyrophoric reaction.

Titanium alloys are also susceptible to stress corrosion by dry sodium chloride at elevated temperatures. This problem has been observed largely in laboratory tests at 450 to 500 F and higher and occasionally in fabrication shops. However, there have been no reported failures of

TABLE 5.1.2.1.1. *Values of Room Temperature Plaine-Strain Fracture Toughness of Titanium Alloys*[a]

									K_{Ic}, ksi $\sqrt{in.}$			
Alloy	Heat Treat Condition	Product Form	Orientation[b]	Yield Strength Range, ksi	Product Thickness Range, inches	Number of Sources	Sample Size	Specimen Thickness Range, inches	Max.	Avg.	Min.	Coefficient of Variation
Ti-6Al-4V	Mill Annealed	Forged Bar	L-T	121-143	<3.5	2	43	0.6-1.1	77	60	38	10.5
Ti-6Al-4V	Mill Annealed	Forged Bar	T-L	124-145	<3.5	2	64	0.5-1.3	81	57	33	11.7

[a]These values are for information only.
[b]Refer to Figure 1.4.12.3 for definition of symbols.

titanium components in service by hot salt stress corrosion. Cleaning with a nonchlorinated solvent (to remove salt deposits, including fingerprints) of parts used above 450 F is recommended.

In laboratory tests, with a fatigue crack present in the specimen, certain titanium alloys show an increased rate of crack propagation in the presence of water or salt water as compared with the rate in air. These alloys also may show reduced sustained load-carrying ability in aqueous environments in the presence of fatigue cracks. Crack growth rates in salt water are a function of sheet or section thickness. These alloys are not susceptible in the form of thin-gauge sheet, but become susceptible as thickness increases. The thickness at which susceptibility occurs varies over a visual range with the alloy and processing. Alloys of titanium found susceptible to this effect include some from alpha, alpha-beta, and beta-type microstructures. In some cases, special processing techniques and heat treatments have been developed that minimize this effect. References 5.1.4(e) through (g) present detailed summaries of corrosion and stress corrosion of titanium alloys.

Under certain conditions, titanium, when in contact with cadmium, silver, mercury, or certain of their compounds, may become embrittled. Refer to MIL-S-5002 and MIL-STD-1568 for restrictions concerning applications with titanium in contact with these metals or their compounds.

5.2 Unalloyed Titanium

Several grades of unalloyed titanium are offered and are classified on the basis of manufacturing method, degree of purity, or strength, there being a close relationship among these. The unalloyed titanium grades most commonly used are produced by the Kroll process, are intermediate in purity, and are commonly referred to as being of commercial purity.

5.2.1 COMMERCIALLY PURE TITANIUM

5.2.1.0 *Comments and Properties.*—Unalloyed titanium is available in all familiar product forms and is noted for its excellent formability. Unalloyed titanium is readily welded or brazed. It has been used primarily where strength is not the main requirement.

Manufacturing Considerations.—Unalloyed titanium is supplied in the annealed condition permitting extensive forming at room temperature. Severe forming operations also can be accomplished at elevated temperatures (300 to 900 F). Property degradation can be experienced after severe forming if as-received material properties are not restored by re-annealing.

Commercially pure titanium can be welded readily by the several methods employed for titanium joining. Atmospheric shielding is preferable although spot or seam welding may be accomplished without shielding. Brazing requires protection from the atmosphere which may be obtained by fluxing as well as by inert gas or vacuum shielding.

Environmental Considerations.—Titanium has an unusually high affinity for oxygen, nitrogen, and hydrogen at temperatures above 1050 F. This results in embrittlement of the material, thus usage should be limited to temperatures below that indicated. Additional chemical reactivity between titanium and selected environments such as methyl alcohol, chloride salt solutions, hydrogen, and liquid metal, can take place at lower temperatures, as discussed in Section 5.1.4 and its references.

Under certain conditions, titanium, when in contact with cadmium, silver, mercury, or certain of their compounds, may become embrittled. Refer to MIL-S-5002 and MIL-STD-1568 for restrictions concerning applications with titanium in contact with these metals or their compounds.

Heat Treatment.—Commercially pure titanium is fully annealed by heating to 1000 to 1300 F for 10 to 30 minutes. It is stress relieved by heating to 900 to 1000 F for 30 minutes. Commercially pure titanium cannot be hardened by heat treatment.

Specifications and Properties.—Some material specifications for commercially pure titanium are presented in Table 5.2.1.0(a). Room-temperature mechanical properties for commercially pure titanium are shown in Tables 5.1.2.0(b) and (c). The effect of temperature on physical properties is shown in Figure 5.2.1.0.

TABLE 5.2.1.0(a). *Material Specifications for Commercially Pure Titanium*

Specification	Form
AMS 4900	Sheet, strip, and plate
AMS 4901	Sheet, strip, and plate
AMS 4902	Sheet, strip, and plate
MIL-T-9046	Sheet, strip, and plate
MIL-T-9047	Bar
AMS 4921	Bar
MIL-T-81556	Extruded bars and shapes

5.2.1.1 *Annealed Condition.*—Elevated-temperature data for annealed commercially pure titanium are presented in Figures 5.2.1.1.1(a) through 5.2.1.1.3(b). Typical full-range stress-strain curves for the 40 and 70 ksi yield strength commercially pure titanium are shown in Figures 5.2.1.1.6(a) and (b).

TABLE 5.2.1.0(b). *Design Mechanical and Physical Properties of Commercially Pure Titanium*

Specification	MIL-T-9046	AMS 4902 and MIL-T-9046	AMS 4900 and MIL-T-9046	AMS 4901 and MIL-T-9046	AMS 4921 and MIL-T-9047	MIL-T-9047
Designation	CP-4	CP-3	CP-2	CP-1	CP-70	
Form	Sheet, strip, and plate				Bar	
Condition	Annealed				Annealed	
Thickness or diameter, in.	≤1.000				≤2.999[a]	3.000-4.000[a]
Basis	S	S	S	S	S	S
Mechanical Properties:						
F_{tu}, ksi:						
L	35	50	65	80	80	80
LT	35	50	65	80	80[b]	80
ST	...	...	...	...	...	80
F_{ty}, ksi:						
L	25	40	55	70	70	70
LT	25	40	55	70	70[b]	70
ST	...	...	...	...	...	70
F_{cy}, ksi:						
L	...	...	...	70	...	...
LT	...	...	...	70	...	...
F_{su}, ksi	...	...	...	42	...	...
F_{bru}, ksi:						
(e/D = 1.5)	...	...	...	120	...	...
(e/D = 2.0)	...	...	...	...	...	...
F_{bry}, ksi:						
(e/D = 1.5)	...	...	...	101	...	...
(e/D = 2.0)	...	...	...	...	...	...
e, percent:						
L	24[c]	20[c]	18[c]	15[c]	15	15
LT	24[c]	20[c]	18[c]	15[c]	15[b]	15
ST	...	...	...	...	...	15
RA, percent:						
L	...	...	...	...	30	30
LT	...	...	...	...	30[b]	30
ST	...	...	...	...	...	30
E, 10^3 ksi	15.5					
E_c, 10^3 ksi	16.0					
G, 10^3 ksi	6.5					
μ	...					
Physical Properties:						
ω, lb/in.^{3}	0.163					
C, K, and α	See Figure 5.2.1.0					

[a]Maximum of 16-square-inch cross-sectional area.

[b]Long transverse properties apply to rectangular bar only for thickness >0.500 inches and widths >3.000 inches. For AMS 4921, (*e*) (LT) = 12% and *RA* (LT) = 25%.

[c]Thickness of 0.025 inch and above.

TABLE 5.2.1.0(c). *Design Mechanical and Physical Properties of Commercially Pure Titanium Extruded Bars and Shapes*

Specification	MIL-T-81556			
	Comp. CP-4	Comp. CP-3	Comp. CP-2	Comp. CP-1
Form	Extruded bars and shapes			
Condition	Annealed			
Thickness or diameter, in.	0.188-3.000			
Basis	S	S	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	40	50	65	80
LT	...	...	...	...
F_{ty}, ksi:				
L	30	40	55	70
LT	...	...	...	...
F_{cy}, ksi:				
L	...	...	...	...
LT	...	...	...	...
F_{su}, ksi	...	...	...	...
F_{bru}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
F_{bry}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
e, percent:				
L	a	a	a	a
E, 10^3 ksi	15.5			
E_c, 10^3 ksi	16.0			
G, 10^3 ksi	6.5			
μ	...			
Physical Properties:				
ω, lb/in.^{3}	0.163			
C, K, and α	See Figure 5.2.1.0			

[a]Elongation in percent as follows:

Thickness, inches	Comp. CP-4	Comp. CP-3	Comp. CP-2	Comp. CP-1
0.188-1.000	25	20	18	15
1.001-2.000	20	18	15	12
2.001-3.000	18	15	12	10

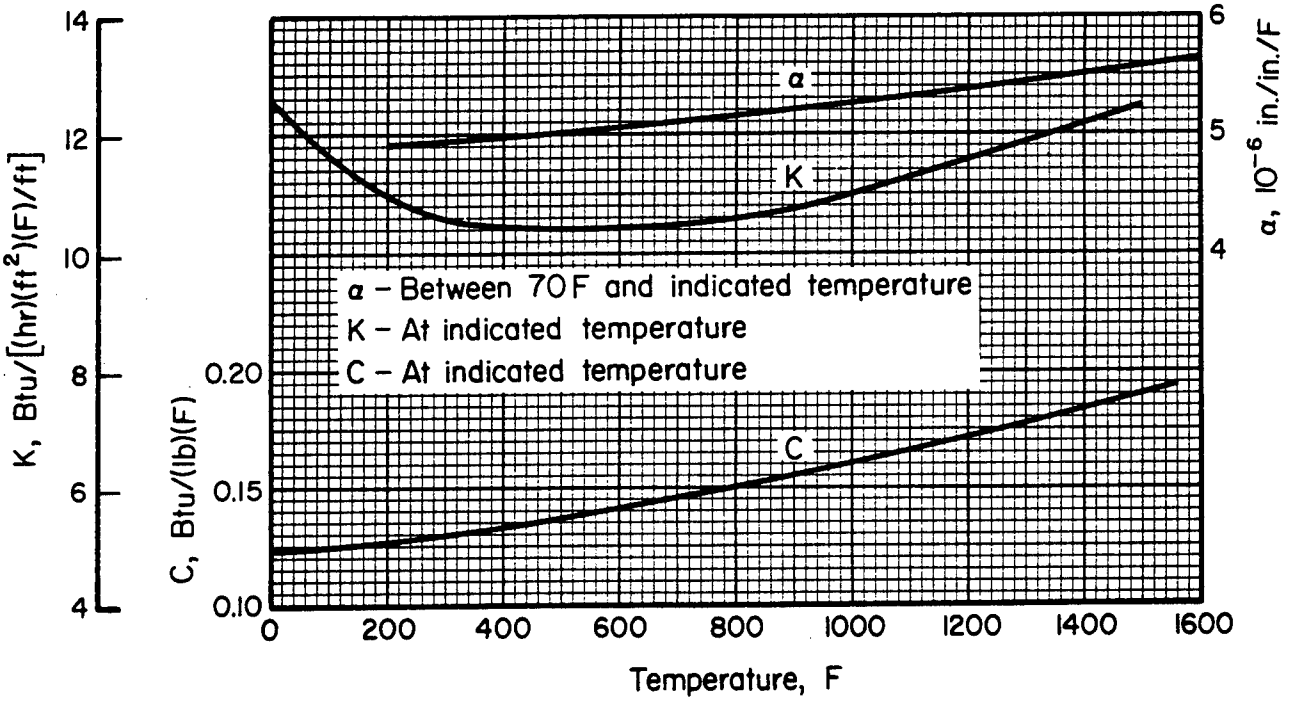


FIGURE 5.2.1.0. *Effect of temperature on the physical properties of commercially pure titanium.*

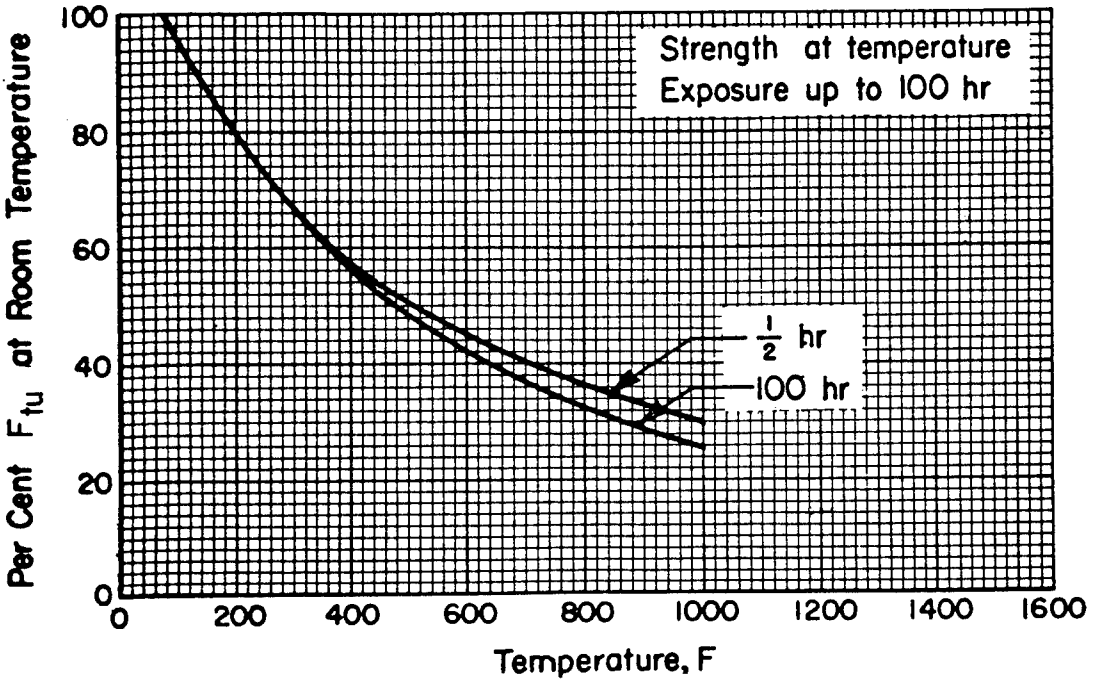


FIGURE 5.2.1.1.1(a). *Effect of temperature on the ultimate tensile strength (F_{tu}) of annealed commercially pure titanium.*

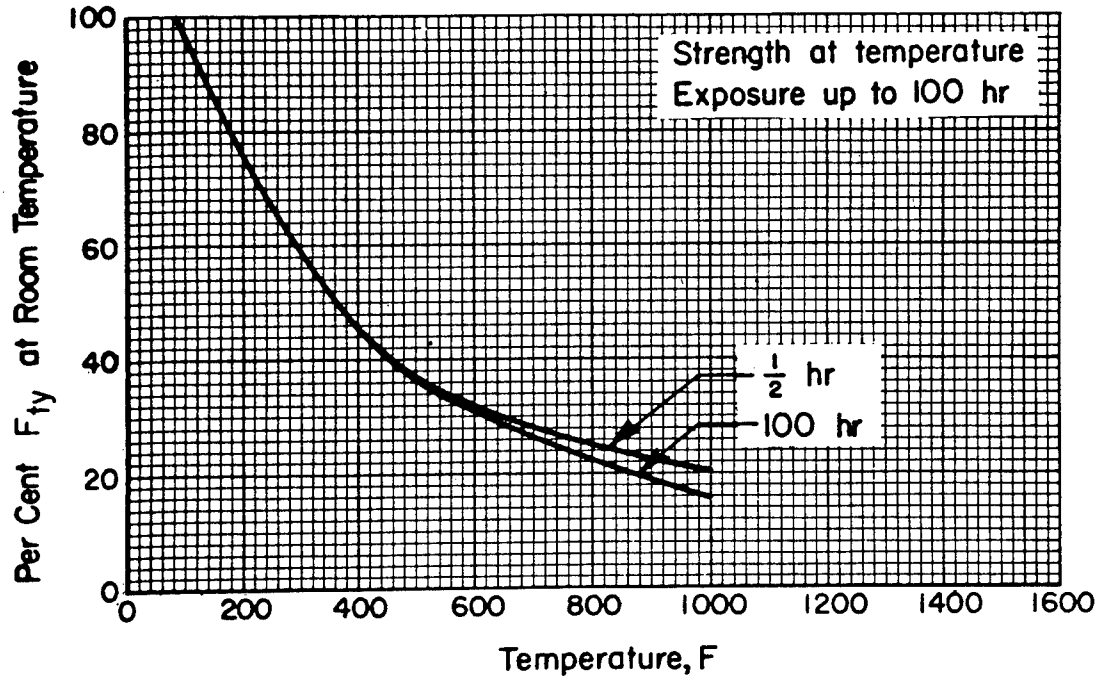


FIGURE 5.2.1.1.1(b). *Effect of temperature on the tensile yield strength (F_{ty}) of annealed commercially pure titanium.*

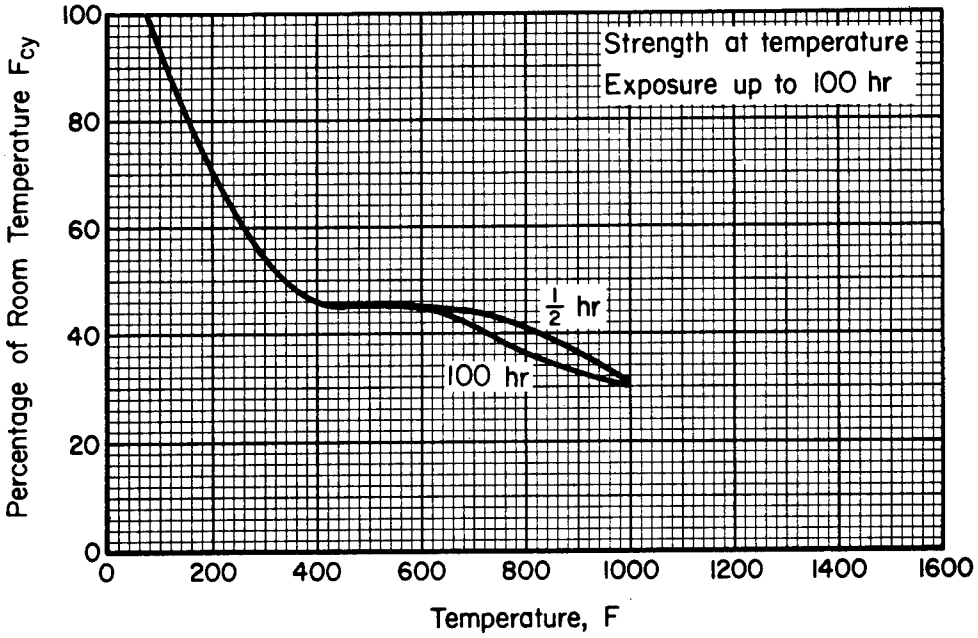


FIGURE 5.2.1.1.2(a). *Effect of temperature on the compressive yield strength (F_{cy}) of annealed commercially pure titanium.*

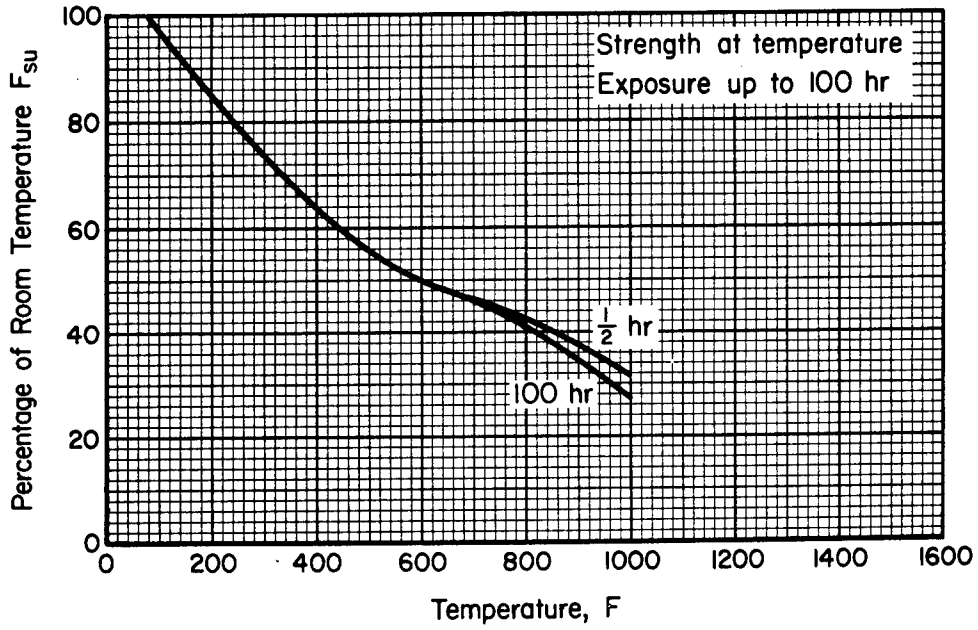


FIGURE 5.2.1.1.2(b). *Effect of temperature on the ultimate shear strength (F_{su}) of annealed commercially pure titanium.*

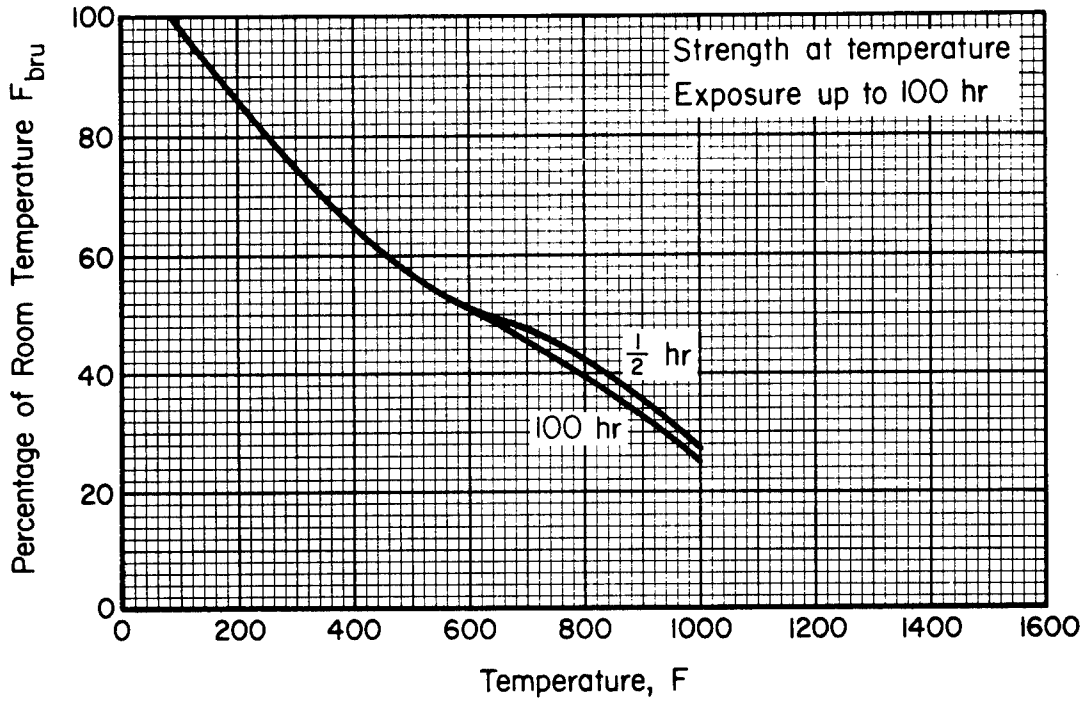


FIGURE 5.2.1.1.3(a). *Effect of temperature on the ultimate bearing strength (F_{bru}) of annealed commercially pure titanium.*

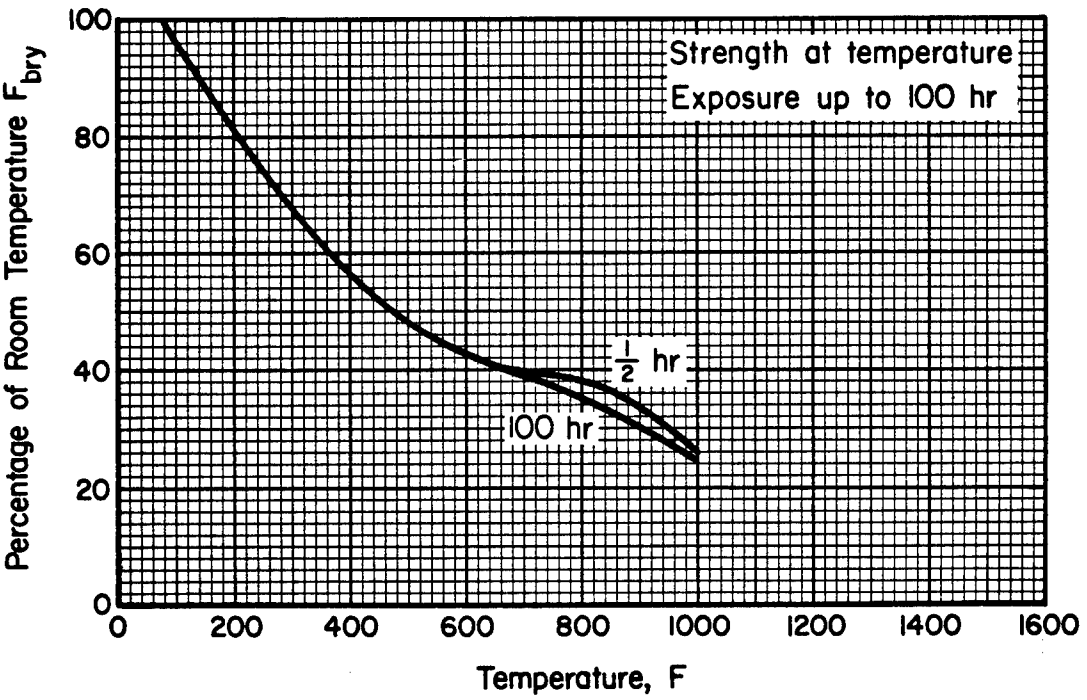


FIGURE 5.2.1.1.3(b). *Effect of temperature on the bearing yield strength (F_{bry}) of annealed commercially pure titanium.*

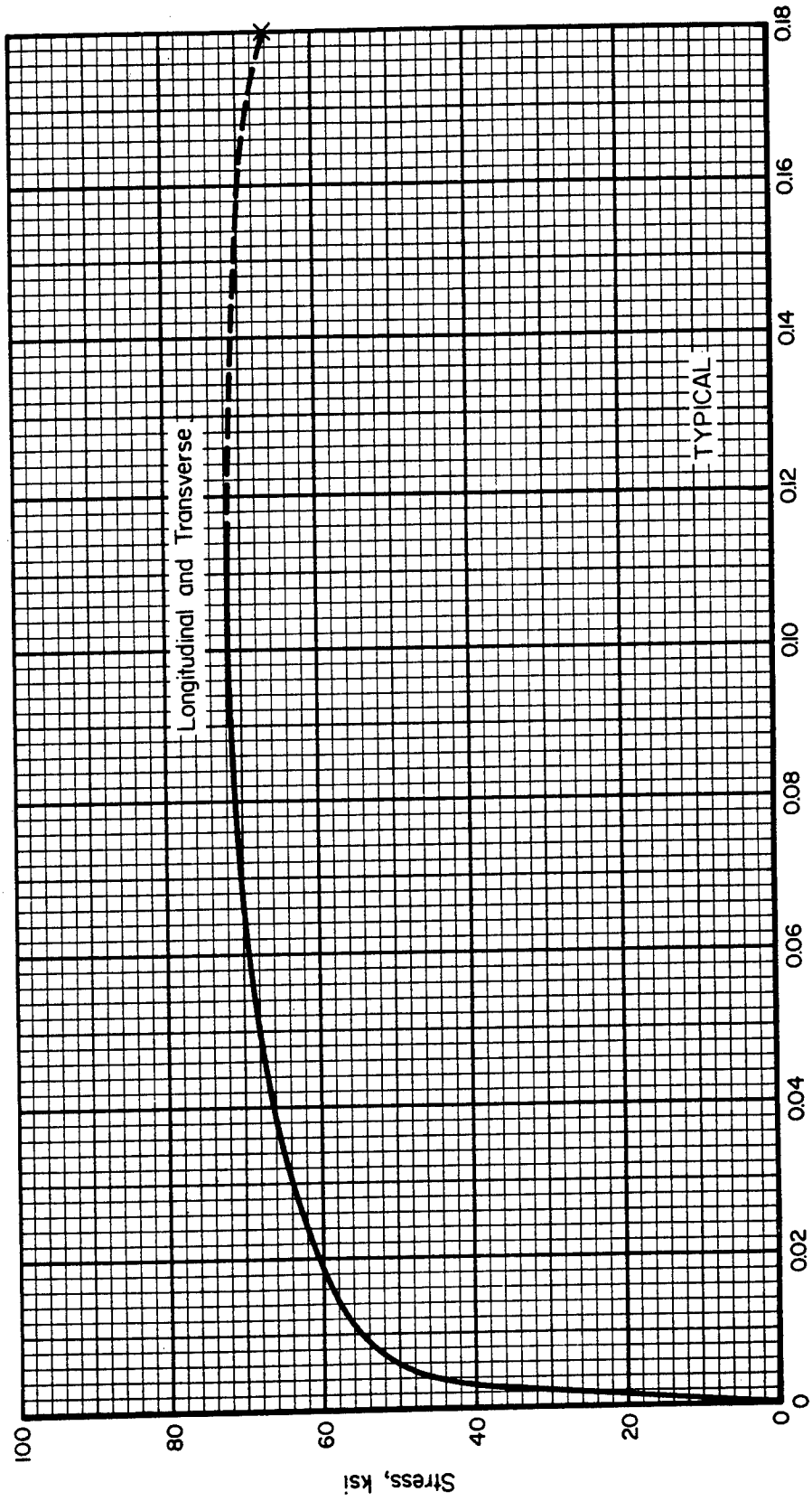


FIGURE 5.2.1.1.6(a). *Typical full-range tensile stress-strain curve for commercially pure titanium sheet (40 ksi yield at room temperature).*

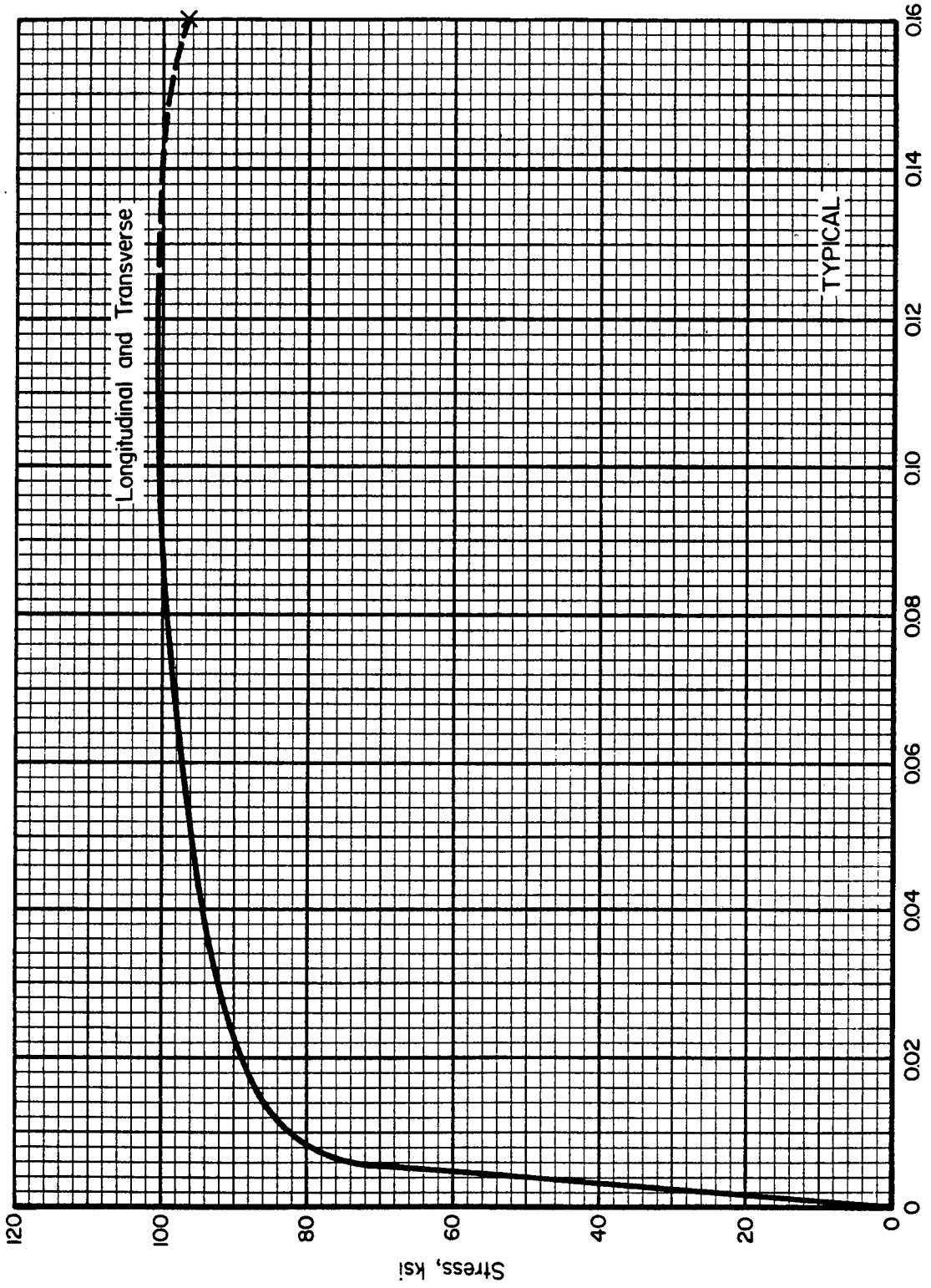


FIGURE 5.2.1.1.6(b). *Typical full range tensile stress-strain curve for commercially pure titanium sheet (70 ksi yield) at room temperature.*

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5.3 Alpha and Near-Alpha Titanium Alloys

The alpha titanium alloys contain essentially a single phase at room temperature, similar to that of unalloyed titanium. Alloys identified as near-alpha titanium have principally an all-alpha structure but contain small quantities of a beta phase because the composition contains some beta stabilizing elements. In both alloy types, alpha phase is stabilized by aluminum, tin, and zirconium. These elements, especially aluminum, contribute greatly to strength. The beta stabilizing additions (e.g., molybdenum and vanadium) improve fabricability and metallurgical stability of highly alpha-alloyed materials.

All alpha alloys have excellent weldability, toughness at low temperatures, and long-term elevated-temperature strength. They are well suited to cryogenic applications and to uses requiring good elevated-temperature creep strength. The characteristics of near-alpha alloys are predictably between those of all alpha and alpha-beta alloys in regard to fabricability, weldability, and elevated-temperature strength. The hot workability of both alpha and near-alpha alloys is inferior to that of the alpha-beta or beta alloys and the cold workability is very limited at the high-strength level of these grades. However, considerable forming is possible if correct forming temperatures and procedures are used.

5.3.1 Ti-5Al-2.5Sn

5.3.1.0 *Comments and Properties.*—Ti-5Al-2.5Sn is an all-alpha alloy available in many product forms and at two purity levels. The high purity grade of this composition is used principally for cryogenic applications and may be characterized as having lower strength but higher ductility and toughness than the standard grade. The normal purity grade also may be used at low temperatures but it is primarily suitable for room to elevated temperature applications (up to 900 F or to 1100 F for short times) where weldability is an important consideration.

Manufacturing Considerations.—Ti-5Al-2.5Sn is not so readily formed into complex shapes as other alloys with similar room-temperature properties, but far surpasses them in weldability. Except for some forging operations, fabrication of Ti-5Al-2.5Sn is conducted at temperatures where the structure remains all alpha. Severe forming operations may be accomplished at temperatures up to 1200 F. Moderately severe forming can be done at 300 to 600 F and simple forming may be done at room temperature. Most forming and welding operations are followed by an annealing treatment to relieve residual stresses imposed by the prior operation.

Ti-5Al-2.5Sn can be welded readily by inert-gas or vacuum-shielded arc methods or by spot or seam welding without atmospheric shielding. Brazing requires protection from the atmosphere; however, this is accomplished by fluxing as well as by inert gas or vacuum shielding.

Environmental Considerations.—Ti-5Al-2.5Sn is metallurgically stable at moderate elevated temperatures. The material is susceptible to hot-salt stress corrosion as well as aqueous chloride solution stress corrosion. Care should be exercised in applications involving such environments. The alloy has good oxidation resistance up to 1050 F. Standard grade material has been used at moderately low cryogenic temperatures; however, the ELI grade has higher toughness and has been used in cryogenic applications down to -423 F. Under certain conditions, titanium, when in contact with cadmium, silver, mercury, or certain of their compounds, may become embrittled. Refer to MIL-S-5002 and MIL-STD-1568 for restrictions concerning applications with titanium in contact with these metals or their compounds.

Heat Treatment.—This alloy is annealed by heating 1400 F for 60 minutes and 1600 F for 10 minutes and cooling in air. Stress relieving requires 1 or 2 hours at 1000 to 1200 F. Ti-5Al-2.5Sn cannot be hardened by heat treatment.

Specifications and Properties.—Some material specifications for Ti-5Al-2.5Sn are shown in Table 5.3.1.0(a). Room-temperature mechanical properties for Ti-5Al-2.5Sn are shown in Tables 5.3.1.0(b) through (d). The effect of temperature on physical properties is shown in Figure 5.3.1.0.

TABLE 5.3.1.0(a). *Material Specifications for Ti-5Al-2.5Sn*

Specification	Form
MIL-T-9046	Sheet, strip, and plate
AMS 4926	Bar
MIL-T-9047	Bar
MIL-T-81556	Extruded bar and shapes
AMS 4910	Sheet, strip, and plate
AMS 4966	Forging

5.3.1.1 *Annealed Condition.*—Elevated temperature curves for annealed Ti-5Al-2.5Sn are shown in Figures 5.3.1.1.1 through 5.3.1.1.5. Tensile properties cover the range -423 F to 1000 F; whereas other properties are for the range room temperature to 1000 F. Fatigue-crack-propagation data for sheet are shown in Figures 5.3.1.1.9(a) through (c).

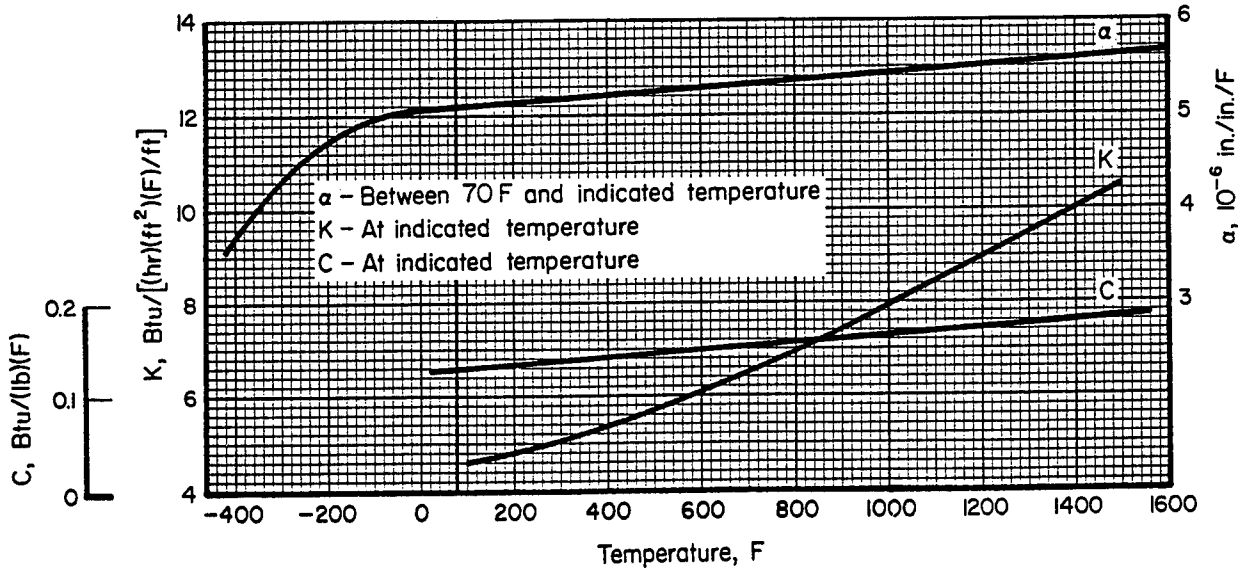


FIGURE 5.3.1.0. *Effect of temperature on the physical properties of Ti-5Al-2.5Sn alloy.*

TABLE 5.3.1.0(b). *Design Mechanical and Physical Properties of Ti-5Al-2.5Sn Sheet, Strip, and Plate*

Specification	AMS 4910 and MIL-T-9046, Comp. A-1								
Form	Strip	Sheet				Plate			
Condition	Annealed								
Thickness, in.	<0.187	0.015-0.079		0.080-0.187		0.188-0.250		0.251-1.500	1.501-4.000
Basis	S	A	B	A	B	A	B	S	S
Mechanical Properties:									
F_{tu}, ksi:									
L	120	120[b]	128	120[b]	131	120[b]	135	120	115
LT	120	120[b]	129	120[b]	132	120[b]	137	120	115
F_{ty}, ksi:									
L	113	110	115	113	118	113[b]	123	113	110
LT	113	113	118	113[b]	121	113[b]	125	113	110
F_{cy}, ksi:									
L	115	115	120	118	123	118	128	118	...
LT	118	118	123	118	126	118	130	118	...
F_{su}, ksi	75	75	80	75	82	75	85	75	...
F_{bru}, ksi:									
(e/D = 1.5)	167	167	179	167	183	167	190	167	...
(e/D = 2.0)	250	250	268	250	275	250	285	250	...
F_{bry}, ksi:									
(e/D = 1.5)	133	133	139	133	142	133	147	133	...
(e/D = 2.0)	190	190	198	190	203	190	210	190	...
e, percent (S-basis):									
L	10	10[a]	...	10	...	10	...	10	10
LT	10	10[a]	...	10	...	10	...	10	10
E, 10^3 ksi	15.5								
E_c, 10^3 ksi	15.5								
G, 10^3 ksi	...								
μ	...								
Physical Properties:									
ω, lb/in.^{3}	0.162								
C, K, and α	See Figure 5.3.1.0								

[a]Thickness 0.025 inch and above.
[b]S-basis. A values are higher than specification values as follows:

	0.015-0.079	0.080-0.187	0.188-0.250
F_{tu}			
L.....	123	126	130
LT.....	123	126	131
F_{ty}			
L.....	....	...	118
LT.....	....	115	120

TABLE 5.3.1.0(c). *Design Mechanical and Physical Properties of Ti-5Al-2.5Sn Bar and Forging*

Specification	AMS 4926[e] and MIL-T-9047			AMS 4966
Form	Bar			Forging
Condition	Annealed			Annealed
Thickness or diameter, in.	≤2.999[a]		3.000-4.000[a]	...
Basis	A	B	S	
Mechanical Properties:				
F_{tu}, ksi:				
L	115[b]	126	115	115
LT	115[c]	...	115	115[d]
ST	...	...	115	115[d]
F_{ty}, ksi:				
L	110[b]	120	110	110
LT	110[c]	...	110	110[d]
ST	...	...	110	110[d]
F_{cy}, ksi:				
L	...	...	...	...
LT	...	...	...	...
F_{su}, ksi	...	...	...	...
F_{bru}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
F_{bry}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
e, percent (S-basis):				
L	10	...	10	10
LT	10[c]	...	10	10[d]
ST	...	...	8	10[d]
RA, percent (S-basis):				
L	25	...	25	25
LT	25[c]	...	25	25[d]
ST	...	...	20	25[d]
E, 10^3 ksi	15.5			
E_c, 10^3 ksi	15.5			
G, 10^3 ksi	...			
μ	...			
Physical Properties:				
ω, lb/in.^{3}	0.162			
C, K, and α	See Figure 5.3.1.0			

[a]Maximum of 16-square-inch cross-sectional area.
[b]The A values are higher than S values as follows: F_{tu} = 117 ksi, F_{ty} = 113 ksi.
[c]S-basis. Applicable providing LT dimension is >3.000 inches.
[d]Applicable, providing LT or ST dimension is ≥2.500 inches.
[e]For AMS 4926, LT and ST values for *e* and *RA* may be different than those shown.

TABLE 5.3.1.0(d). *Design Mechanical and Physical Properties of Ti-5Al-2.5Sn Extrusion*

Specification	MIL-T-81556, Comp. A-1			
Form	Extruded bars and shapes			
Condition	Annealed			
Thickness or diameter, in.	0.188-1.000	1.001-2.000	2.001-3.000	3.001-4.000
Basis	S	S	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	120	115	115	115
LT	...	...	...	...
F_{ty}, ksi:				
L	115	110	110	110
LT	...	...	...	...
F_{cy}, ksi:				
L	...	...	...	...
LT	...	...	...	...
F_{su}, ksi	...	...	...	...
F_{bru}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
F_{bry}, ksi:				
(e/D = 1.5)				
(e/D = 2.0)				
e, percent:				
L	10	10	8	6
LT	...	...	...	...
E, 10^3 ksi	15.5			
E_c, 10^3 ksi	15.5			
G, 10^3 ksi	...			
μ	...			
Physical Properties:				
ω, lb/in.^{3}	0.162			
C, K, and α	See Figure 5.3.1.0			

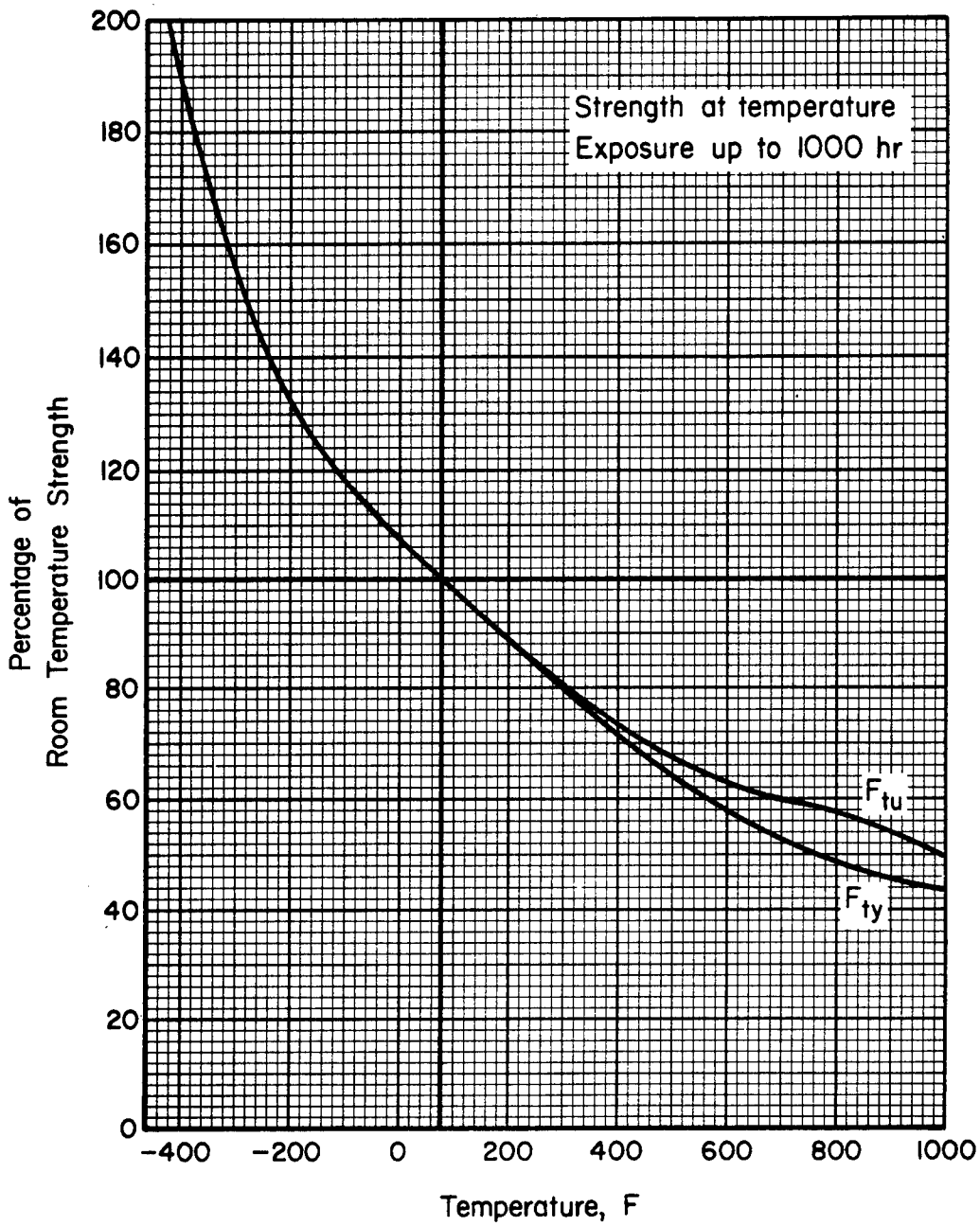


FIGURE 5.3.1.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of annealed Ti-5Al-2.5Sn alloy sheet.*

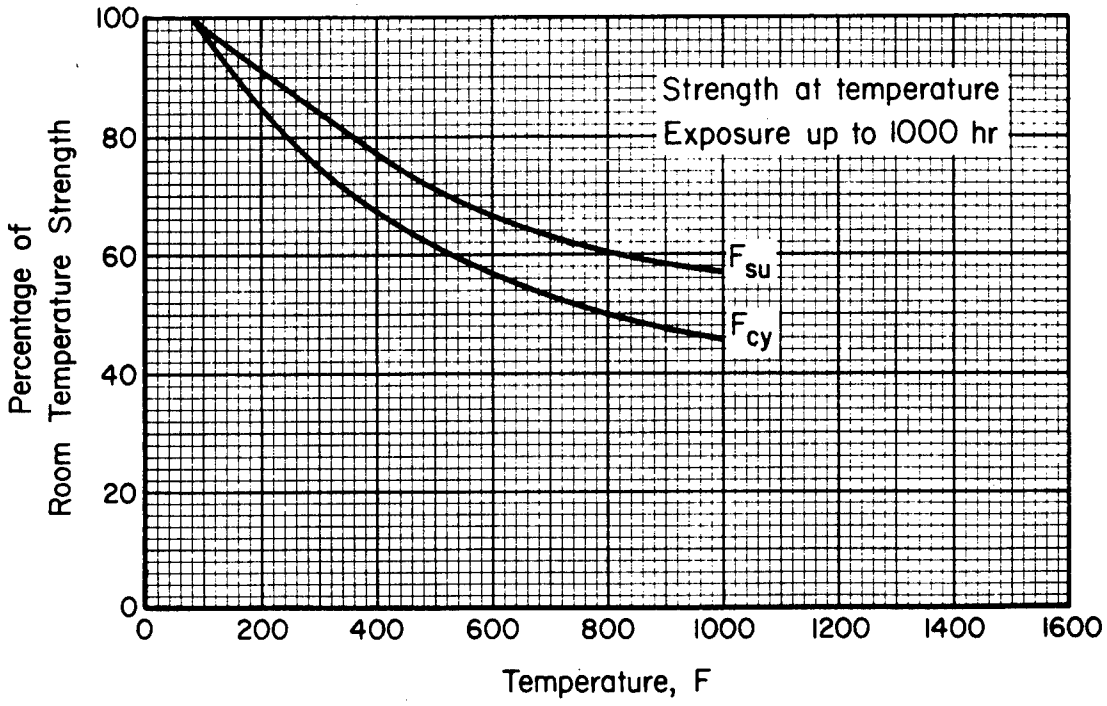


FIGURE 5.3.1.1.2. *Effect of temperature on the compressive yield strength (F_{cy}) and the shear ultimate strength (F_{su}) of annealed Ti-5Al-2.5Sn alloy sheet.*

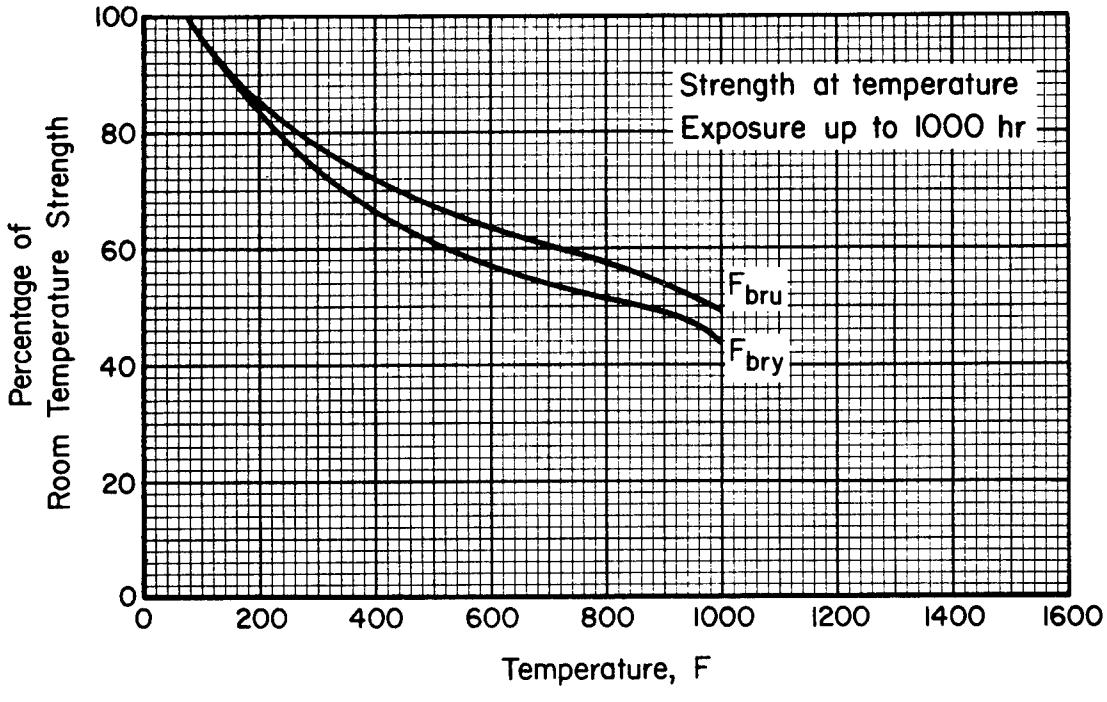


FIGURE 5.3.1.1.3. *Effect of temperature on the bearing ultimate strength (F_{bru}) and the bearing yield strength (F_{bry}) of annealed Ti-5Al-2.5Sn alloy sheet.*

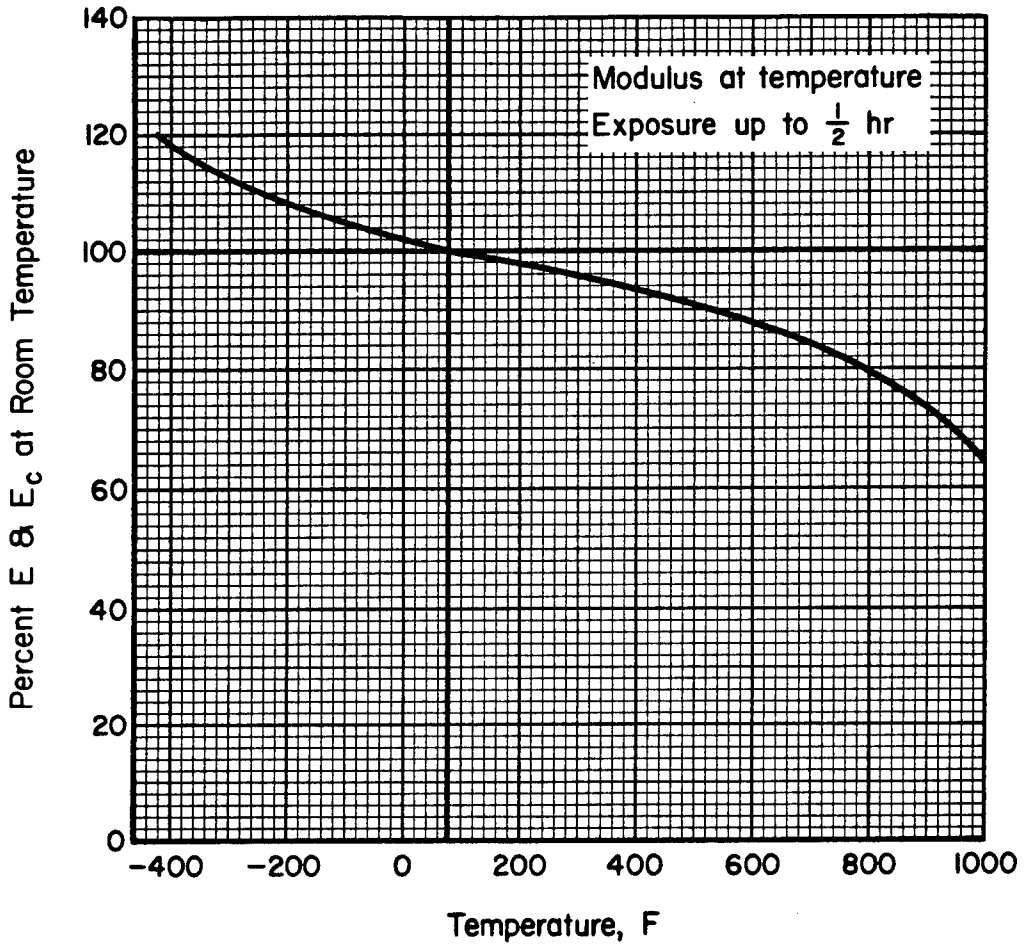


FIGURE 5.3.1.1.4. *Effect of temperature on the tensile and compressive moduli (E and E_c) of annealed Ti-5Al-2.5Sn alloy sheet.*

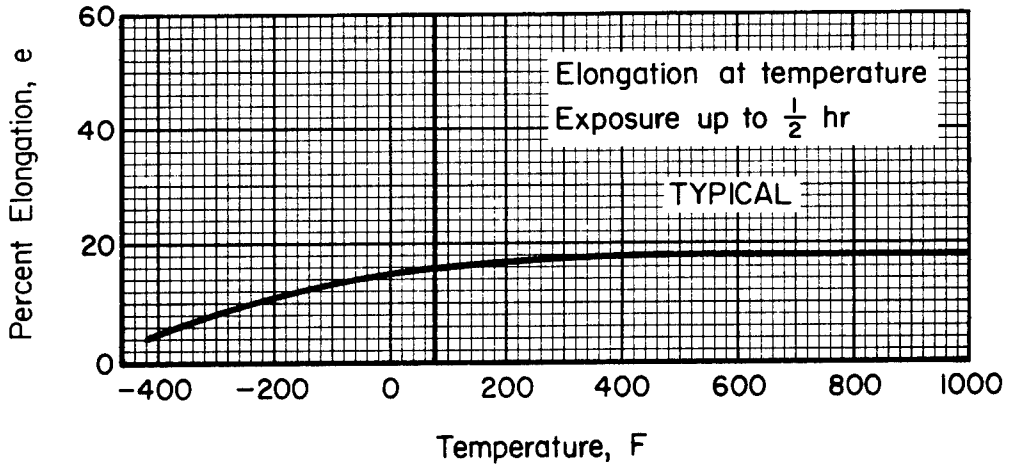


FIGURE 5.3.1.1.5. *Effect of temperature on the elongation (e) of annealed Ti-5Al-2.5Sn alloy sheet.*

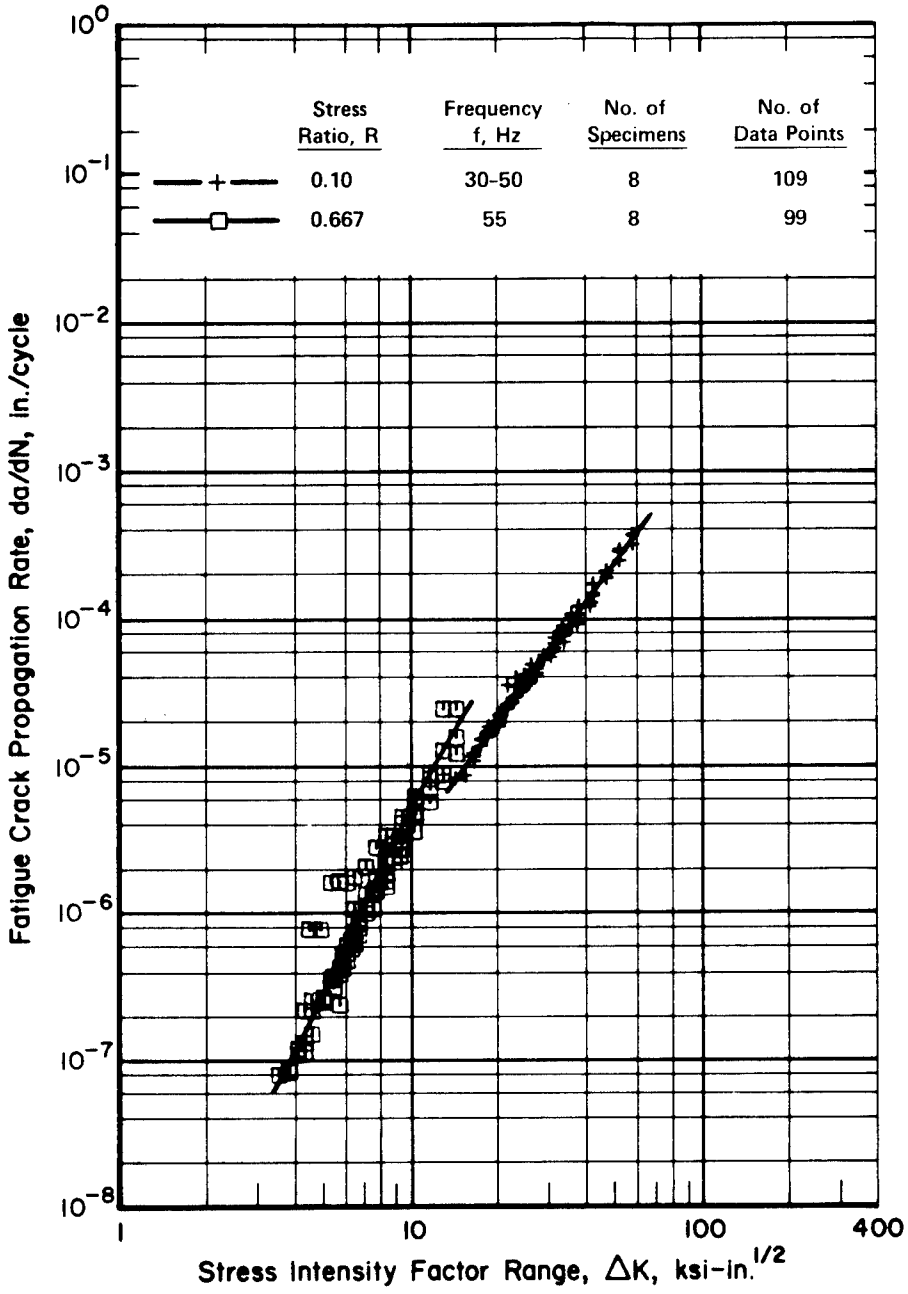


FIGURE 5.3.1.1.9(a). *Fatigue-crack-propagation data for 0.084 inch thick Ti-5Al-2.5Sn titanium alloy mill-annealed sheet. [Reference 5.3.1.1.9].*

Specimen Thickness: 0.08 inch	*Environment: Lab air*
Specimen Width: 2.76 inches	*Temperature: RT*
Specimen Type: CC	*Orientation: L-T and T-L*

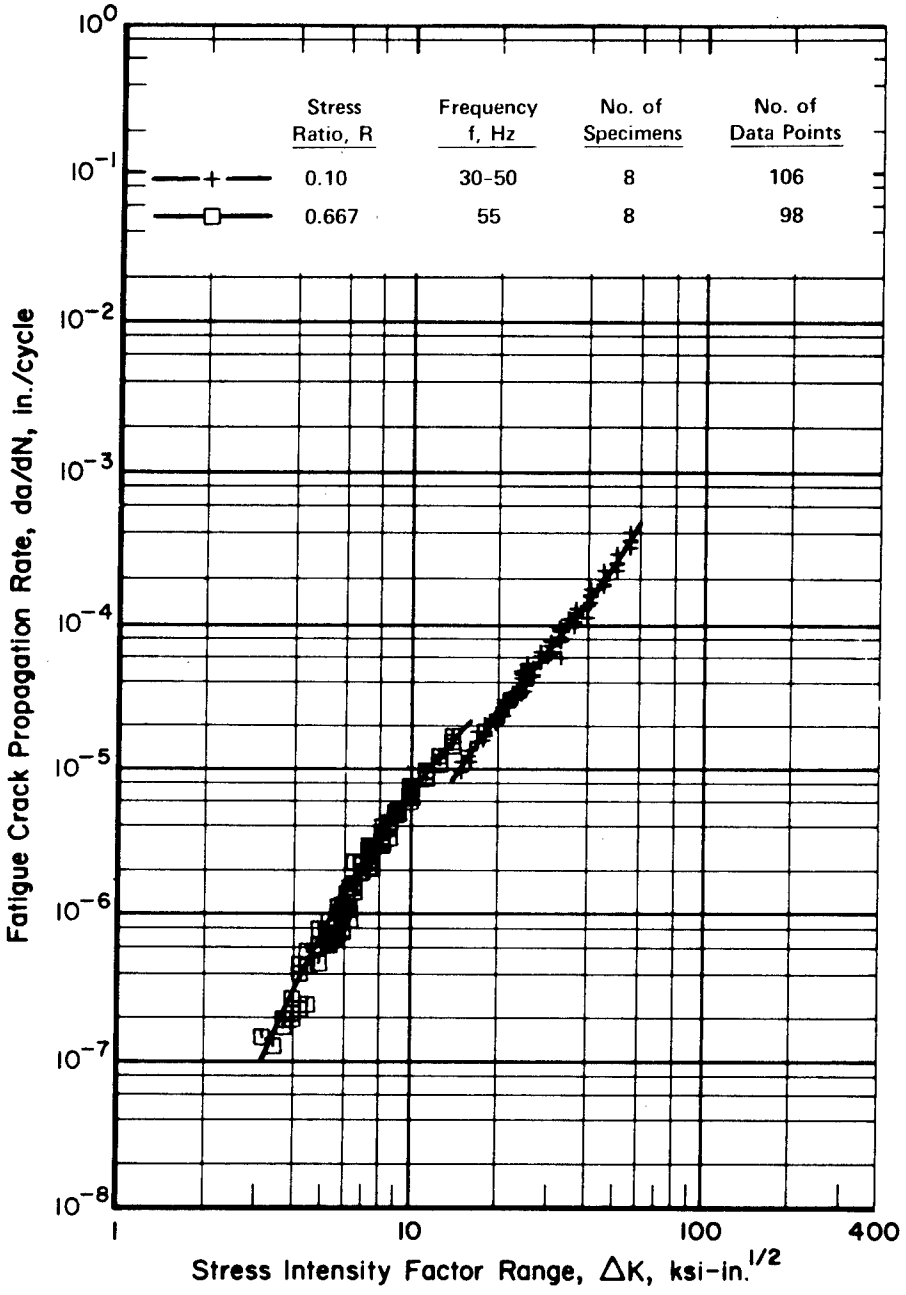


FIGURE 5.3.1.1.9(b). *Fatigue-crack-propagation data for 0.084 inch thick Ti-5A1-2.5Sn titanium alloy mill-annealed sheet.* [*Reference 5.3.1.1.9*].

Specimen Thickness: 0.08 inch
Specimen Width: 2.76 inches
Specimen Type: CC

Environment: Distilled water
Temperature: RT
Orientation: L-T and T-L

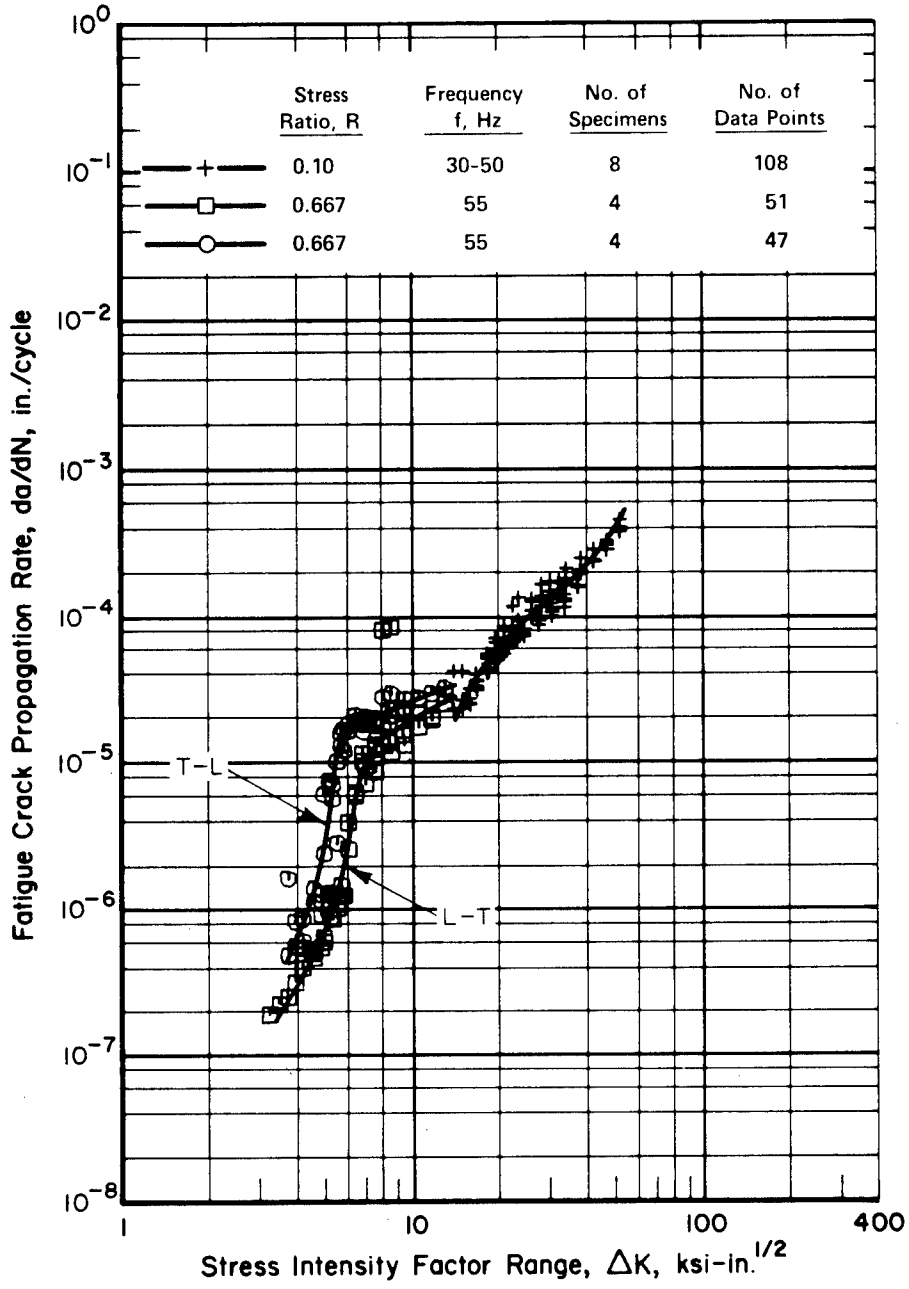


FIGURE 5.3.1.1.9(c). *Fatigue-crack propagation data for 0.084 inch thick Ti-5Al-2.5Sn titanium alloy mill-annealed sheet. [Reference 5.3.1.1.9].*

Specimen Thickness: 0.08 inch
Specimen Width: 2.76 inches
Specimen Type: CC

Environment: 3.5% NaCl
Temperature: RT
Orientation: L-T and T-L

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5.3.2 Ti-8Al-1Mo-1V

5.3.2.0 *Comments and Properties.*—Ti-8Al-1Mo-1V alloy is a near-alpha composition developed for improved creep resistance and thermal stability up to about 850 F. The alloy is available as billet, bar, plate, sheet, strip, extrusions, and forgings.

Manufacturing Considerations.—Room temperature forming of Ti-8Al-1Mo-1V sheet is somewhat more difficult than in Ti-6Al-4V, and for severe operations hot forming is required. Ti-8Al-1Mo-1V can be fusion welded readily with inert-gas protection or spot welding without atmospheric protection. Weld strengths are comparable to those of the parent metal although ductility is somewhat lower in the weldment.

Environmental Considerations.—Ti-8Al-1Mo-1V exhibits good oxidation resistance and thermal stability up to 850 F. A decrease in tensile elongation has been reported for single-annealed sheet following 150 hours stressed exposure at 1000 F. Extended exposure to temperatures exceeding 600 F adversely affects room-temperature spot-weld tension strength. This alloy is not recommended for structural applications at liquid-hydrogen temperatures (-423 F). The Ti-8Al-1Mo-1V alloy also is susceptible to chloride stress-corrosion attack in either elevated-temperature (hot-salt stress-corrosion) or ambient-temperature (aqueous stress-corrosion) chloride environments. Thus, care should be exercised in applying the material in chloride containing environments. Under certain conditions, titanium, when in contact with cadmium, silver, mercury, or certain of their compounds, may become embrittled. Refer to MIL-S-5002 and MIL-STD-1568 for restrictions concerning applications with titanium in contact with these metals or their compounds.

Heat Treatment.—Three treatments are used with Ti-8Al-1Mo-1V. These are:

Single Anneal: 1450 F for 8 hours, furnace cool.

Duplex Anneal: 1450 F for 8 hours, furnace cool, followed by 1450 F for 15 to 20 minutes, air cool.

Solution Treated and Stabilized: 1825 F for 1 hour, air cool, 1075 F for 8 hours, air cool.

As a general guide, the single anneal is used to obtain highest room-temperature mechanical properties and the duplex anneal to obtain highest fracture toughness. Both the single anneal and the duplex anneal are compatible with hot-forming operations. The solution treated and stabilized condition is used for forgings.

Specifications and Properties.—Material specifications for Ti-8Al-1Mo-1V are presented in Table 5.3.2.0(a). Room-temperature mechanical and physical properties for Ti-8AI-1Mo-1V are shown in Tables 5.3.2.0(b) and (c). The effect of temperature on physical properties is shown in Figure 5.3.2.0.

TABLE 5.3.2.0(a). *Material Specifications for Ti-8AI-1Mo-1V*

Specification	Form
MIL-T-9046	Sheet, strip, and plate
MIL-T-9047	Bar
AMS 4973	Forging
AMS 4915	Sheet, strip, and plate
AMS 4916	Sheet, strip, and plate

5.3.2.1 *Single-Annealed Condition.*—Cryogenic, room-temperature, and elevated temperature property curves for this condition are shown in Figures 5.3.2.1.1 and 5.3.2.1.4. Typical tensile and compressive stress-strain and tangent-modulus curves are shown in Figures 5.3.2.1.6(a) and (b) for room temperature and several elevated temperatures.

5.3.2.2 *Duplex-Annealed Condition.*—Cryogenic, room temperature, and elevated temperature curves for this condition are shown in Figure 5.3.2.2.1. Typical tensile and compressive stress-strain and tangent-modulus curves are shown in Figures 5.3.2.2.6(a) and (b) for room temperature and several elevated temperatures. Fatigue S/N curves for unnotched and notched specimens at room temperature and several elevated temperatures are shown in Figures 5.3.2.2.8(a) through (f).

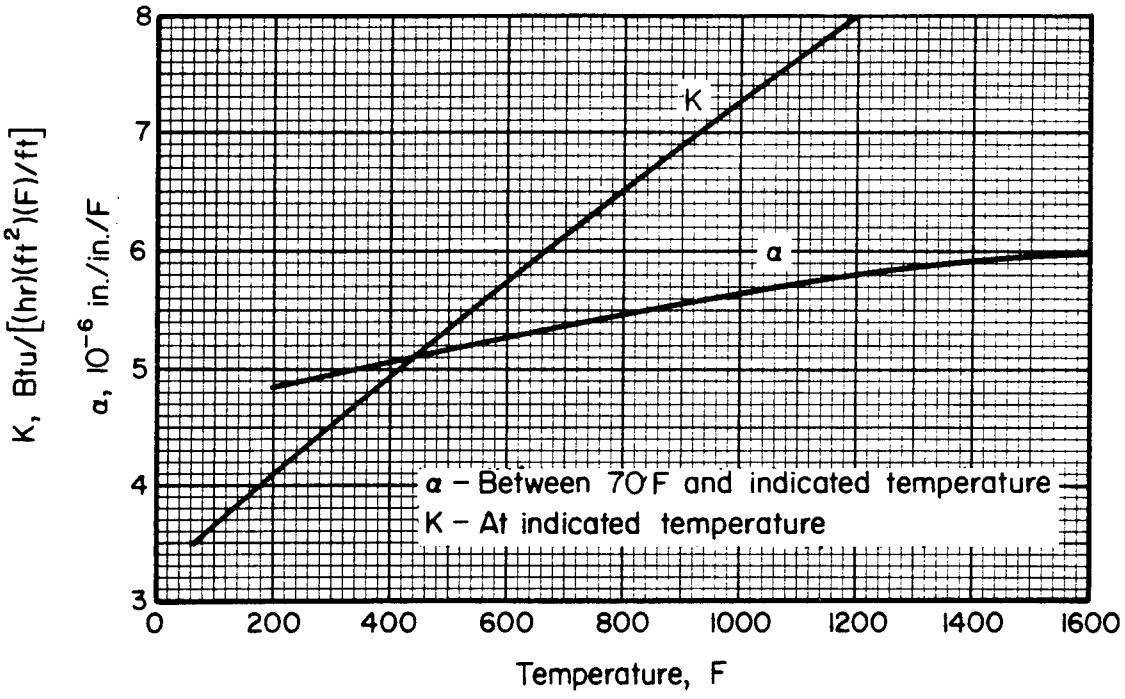


FIGURE 5.3.2.0. *Effect of temperature on the physical properties of Ti-8Al-1Mo-1V alloy.*

TABLE 5.3.2.0(b_1). *Design Mechanical and Physical Properties of Ti-8Al-1Mo-1V Sheet and Plate*

Specification	AMS 4915 and MIL-T-9046, Comp A-4				
Form	Sheet	Plate			
Condition	Single Annealed				
Thickness, in.	≤0.1875	0.1875-0.500	0.501-1.000	1.001-2.500	2.501-4.000
Basis	S	S	S	S	S
Mechanical Properties:					
F_{tu}, ksi:					
L	145	145	140	130	120
LT	145	145	140	130	120
ST	...	...	...	...	120[b]
F_{ty}, ksi:					
L	135	135	130	120	110
LT	135	135	130	120	110
ST	...	...	...	...	110[b]
F_{cy}, ksi:					
L	144	...	...	...	...
LT	149	...	...	...	...
ST	...	...	...	...	...
F_{su}, ksi	93	...	...	...	...
F_{bru}, ksi:					
(e/D = 1.5)	239	...	...	...	...
(e/D = 2.0)	294	...	...	...	...
F_{bry}, ksi:					
(e/D = 1.5)	196	...	...	...	...
(e/D = 2.0)	214	...	...	...	...
e, percent:					
L	a	10	10	10	8
LT	a	10	10	10	8
ST	...	...	...	...	8[b]
E, 10^3 ksi	17.5[c]				
E_c, 10^3 ksi	18.0[c]				
G, 10^3 ksi	6.7				
μ	0.32				
Physical Properties:					
ω, lb/in.^{3}	0.158				
C, Btu/(lb)(F)	0.12				
K and α	See Figure 5.3.2.0				

[a]0.008-0.014 in. thickness, 6 percent; 0.015-0.024 in. thickness, 8 percent; > 0.025 in. thickness, 10 percent.
[b]Applicable, providing ST dimension is >3.000 inches.
[c]Average, values may vary with test direction.

TABLE 5.3.2.0(b_2). *Design Mechanical and Physical Properties of Ti-8Al-1Mo-1V Sheet and Plate*

Specification	AMS 4916 and MIL-T-9046, Comp. A-4					
Form	Sheet		Plate			
Condition	Duplex Annealed					
Thickness, in.	0.015-0.024	0.025-0.1875	0.1875-0.500	0.501-1.000	1.001-2.000	2.001-4.000
Basis	S	S	S	S	S	S
Mechanical Properties:						
F_{tu}, ksi:						
L	135	135	130	130	125	120
LT	135	135	130	130	125	120
F_{ty}, ksi:						
L	120	120	120	120	115	110
LT	120	120	120	120	115	110
F_{cy}, ksi:						
L	126	126	...	...	...	...
LT	126	126	...	...	...	...
F_{su}, ksi	84	84	...	...	...	...
F_{bru}, ksi:						
(e/D = 1.5)	223	223	...	...	...	...
(e/D = 2.0)	269	269	...	...	...	...
F_{bry}, ksi:						
(e/D = 1.5)	174	174	...	...	...	...
(e/D = 2.0)	191	191	...	...	...	...
e, percent:						
L	8	10	10	10	10	8
LT	8	10	10	10	10	8
E, 10^3 ksi	17.5[a]					
E_c, 10^3 ksi	18.0[a]					
G, 10^3 ksi	6.7					
μ	0.32					
Physical Properties:						
ω, lb/in.^{3}	0.158					
C, Btu/(lb)(F)	0.12					
K and α	See Figure 5.3.2.0					

[a]Average, L and LT; values may vary with test direction.

TABLE 5.3.2.0(c). *Design and Physical Properties of Ti-8Al-1Mo-1V Bar and Forging*

Specification	MIL-T-9047		AMS 4973	
Form	Bar		Forging	
Condition	Duplex annealed		Solution treated and stabilized	
Thickness or diameter, in.	≤ 2.500[a]	2.501-4.000[a]	≤ 2.499	2.500-4.000
Basis	S	S	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	130	120	130	120
LT	130[b]	120[b]	130[c]	120
ST	...	120[b]	...	120
F_{ty}, ksi:				
L	120	110	120	110
LT	120[b]	110[b]	120[c]	110
ST	...	110[b]	...	110
F_{cy}, ksi:				
L	...	...	...	...
LT	...	...	...	...
ST	...	...	...	...
F_{su}, ksi	...	...	...	...
F_{bru}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
F_{bry}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
e, percent:				
L	10	10	10	10
LT	10[b]	10[b]	10[c]	10
ST	...	8[b]	...	10
E, 10^3, ksi	17.5[d]			
E_c, 10^3 ksi	18.0[d]			
G, 10^3 ksi	6.7			
μ	0.32			
Physical Properties:				
ω, lb/in.^{3}	0.158			
C, Btu/(lb)(F)	0.12			
K and α	See Figure 5.3.2.0			

[a]Maximum of 16 square-inch cross-sectional area.
[b]Applicable, providing LT or ST dimension is > 3.000 inches.
[c]Applicable, providing LT dimension is ≥ 2.500 inches.
[d]Average, values may vary with test direction.

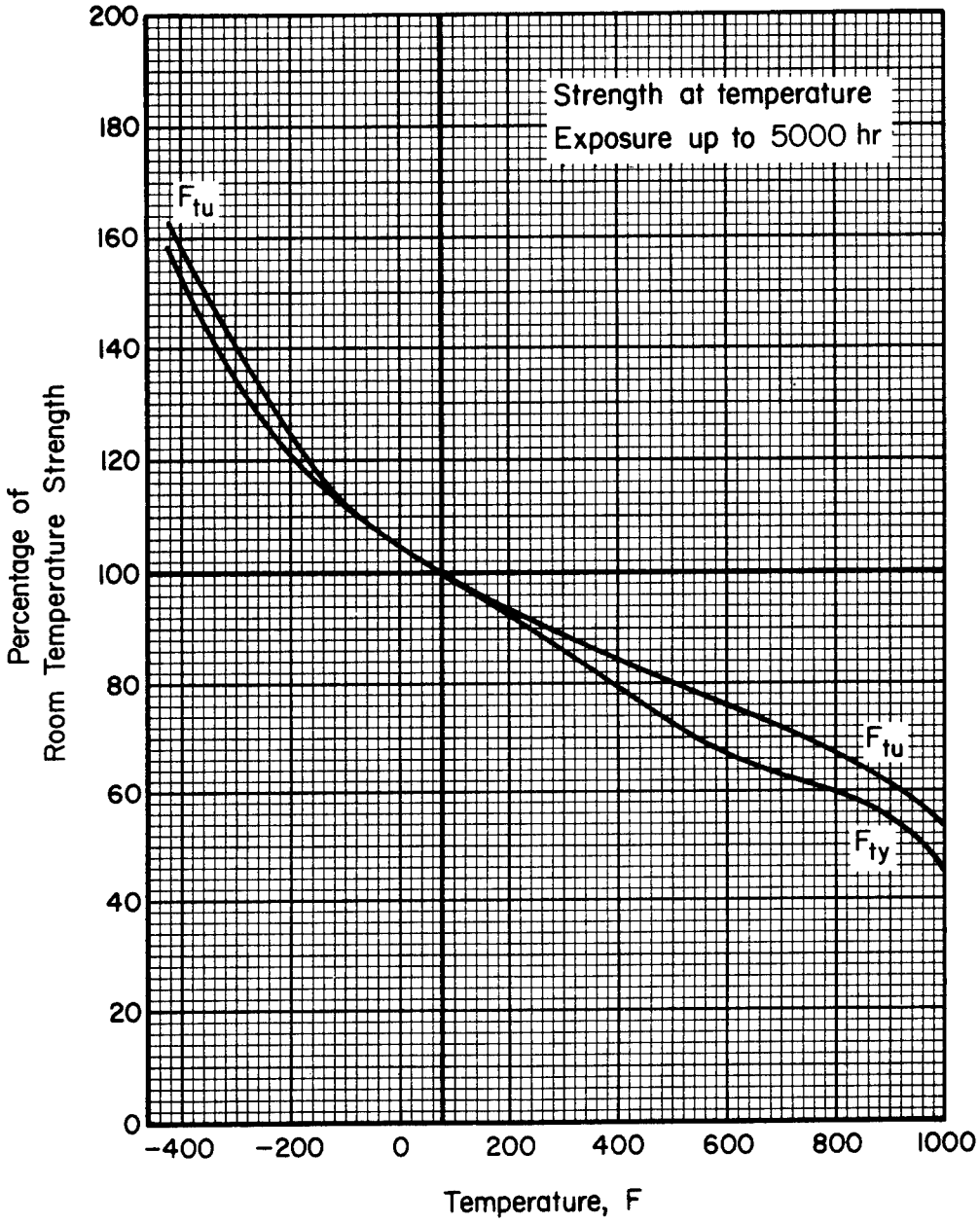


FIGURE 5.3.2.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of single-annealed Ti-8Al-1Mo-1V alloy sheet.*

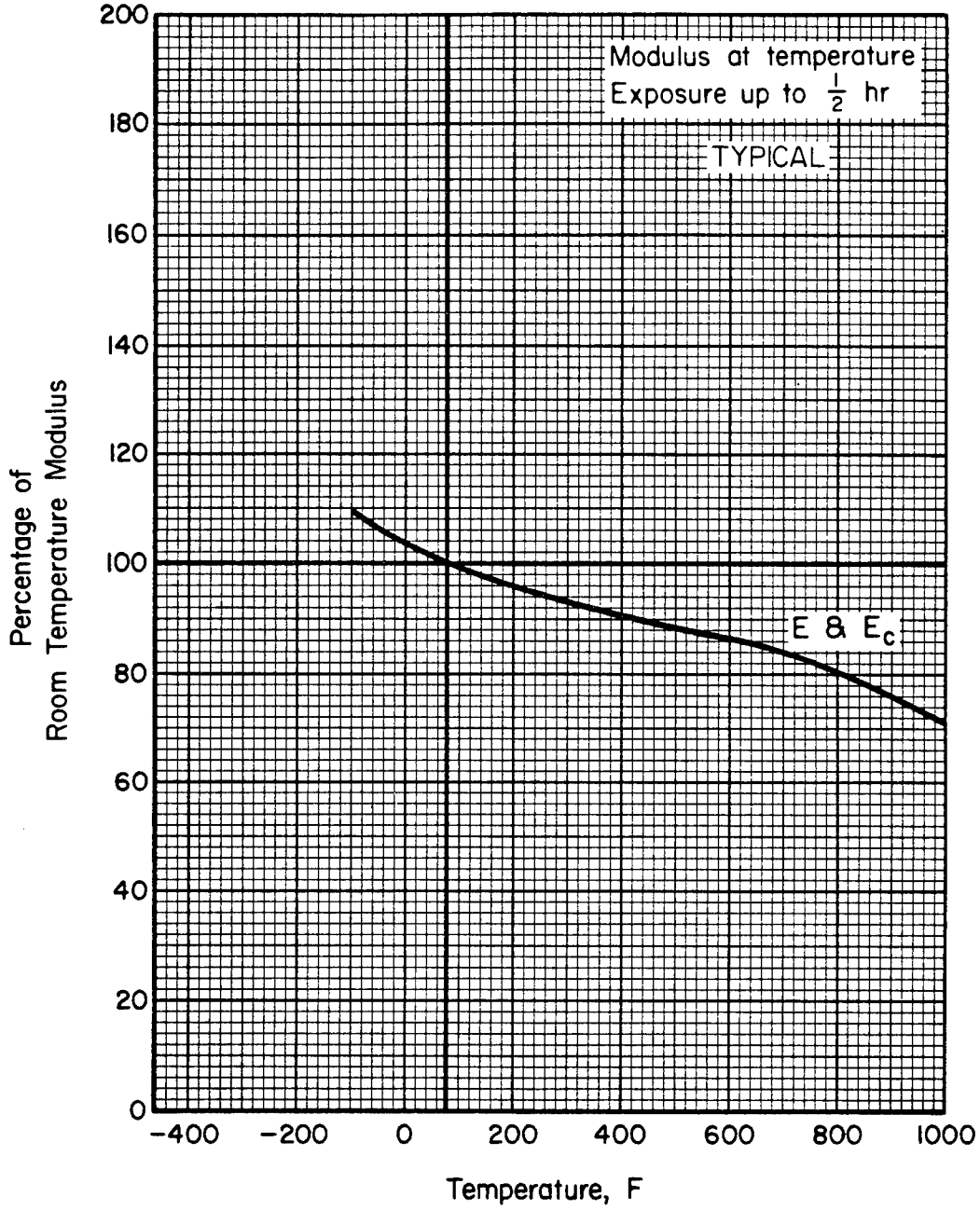


FIGURE 5.3.2.1.4. *Effect of temperature on the tensile and compressive moduli (E and E_c) of Ti-8Al-1Mo-1V alloy sheet.*

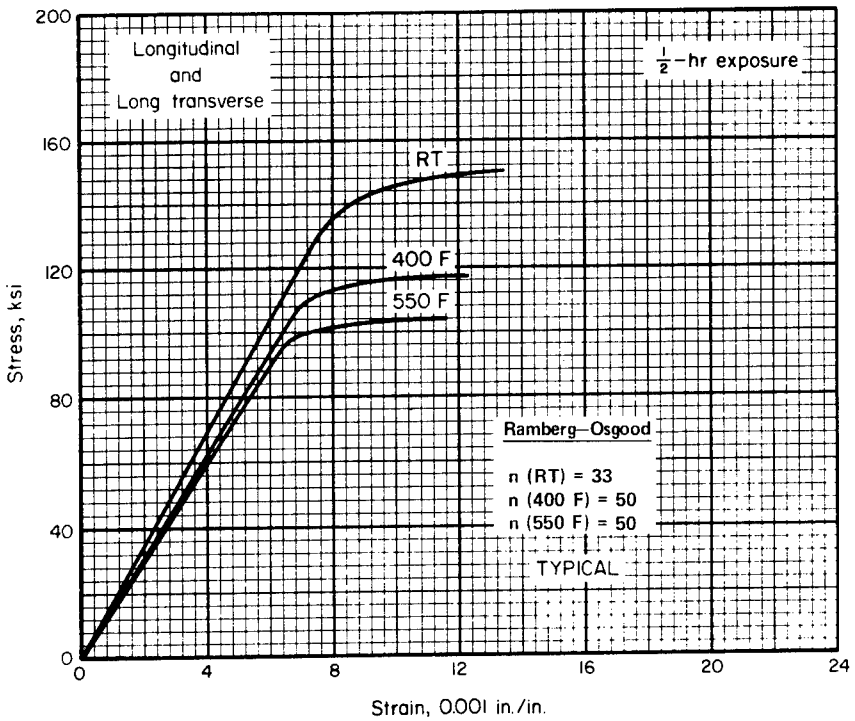


FIGURE 5.3.2.1.6(a). *Typical tensile stress-strain curves for single-annealed Ti-8Al-1Mo-1V alloy sheet at room and elevated temperatures.*

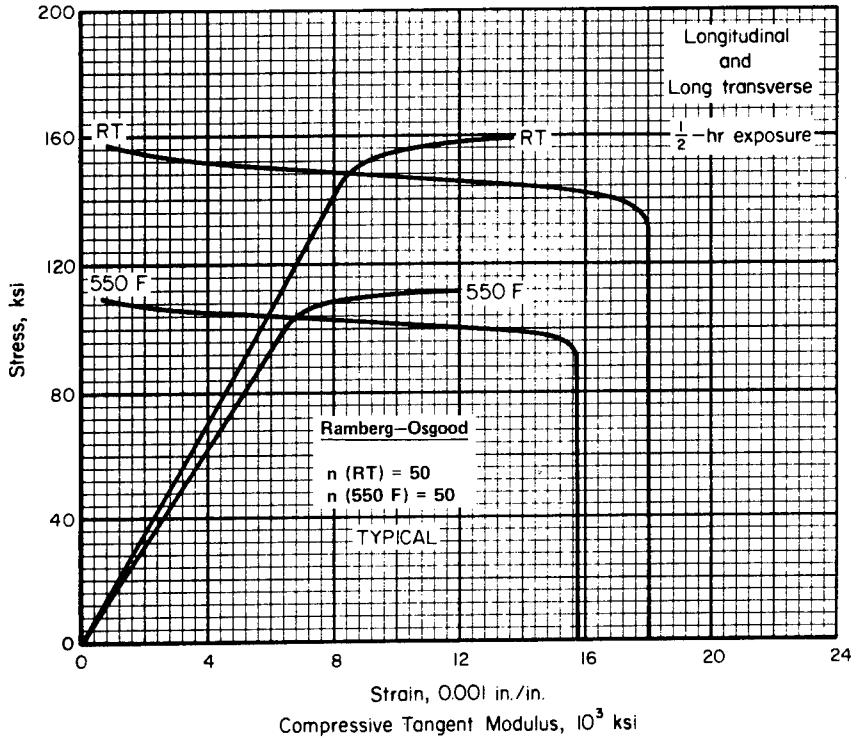


FIGURE 5.3.2.1.6(b). *Typical compressive stress-strain and compressive tangent-modulus curves for single-annealed Ti-8Al-1Mo-1V alloy sheet at room and elevated temperatures.*

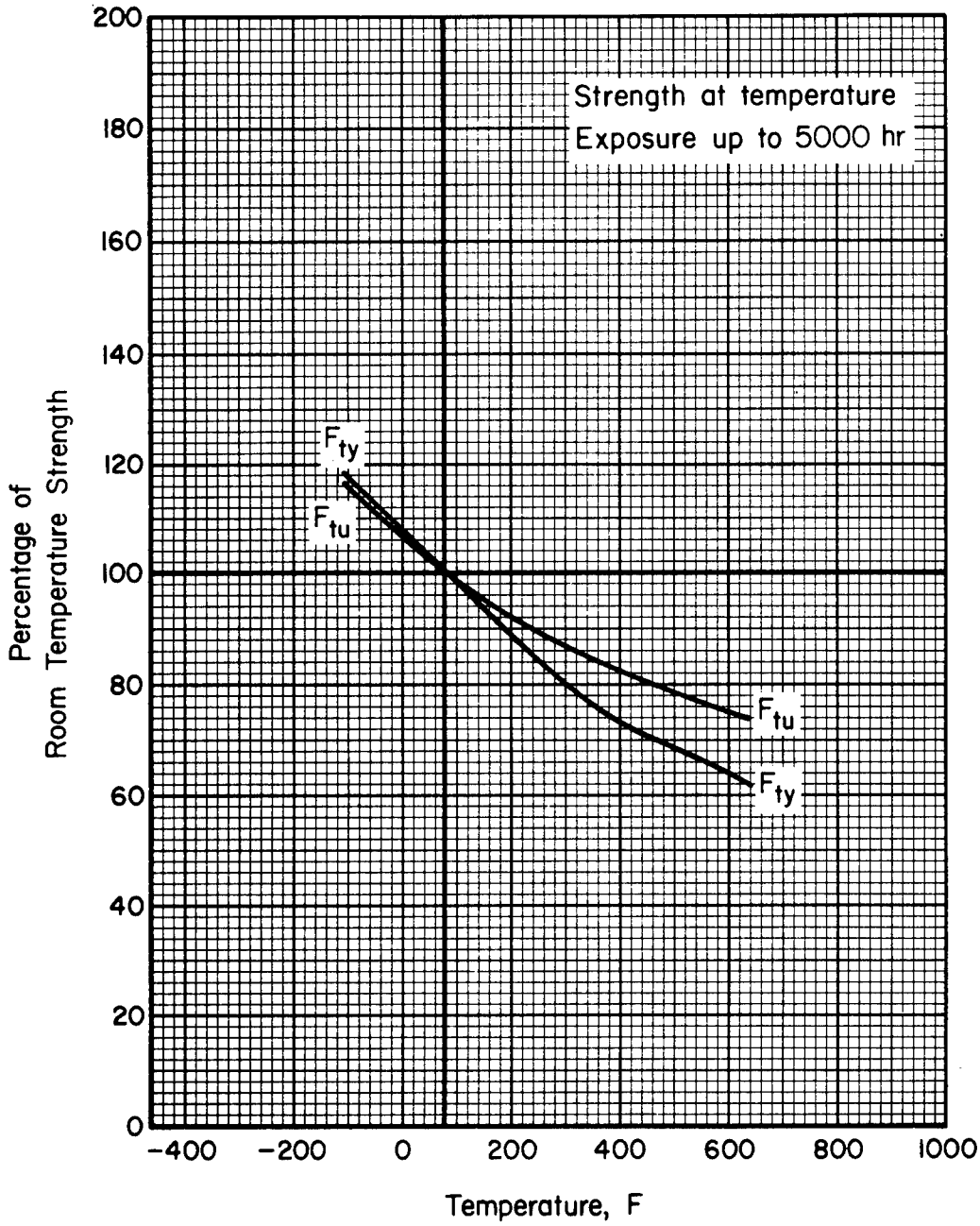


FIGURE 5.3.2.2.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of duplex-annealed Ti-8Al-1Mo-1V alloy sheet.*

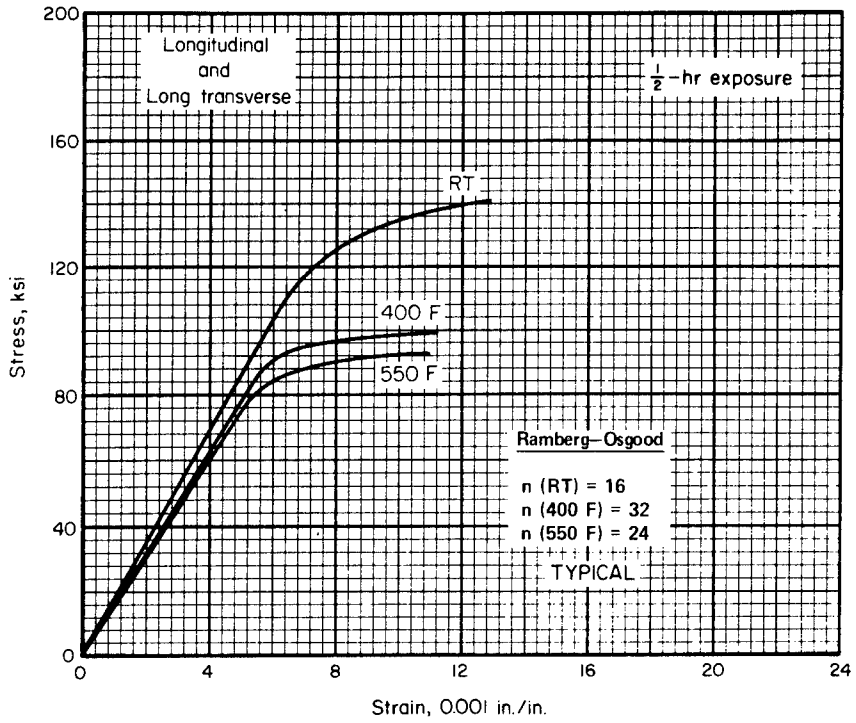


FIGURE 5.3.2.2.6(a). *Typical tensile stress-strain curves for duplex-annealed Ti-8Al-1Mo-1V alloy sheet at room and elevated temperatures.*

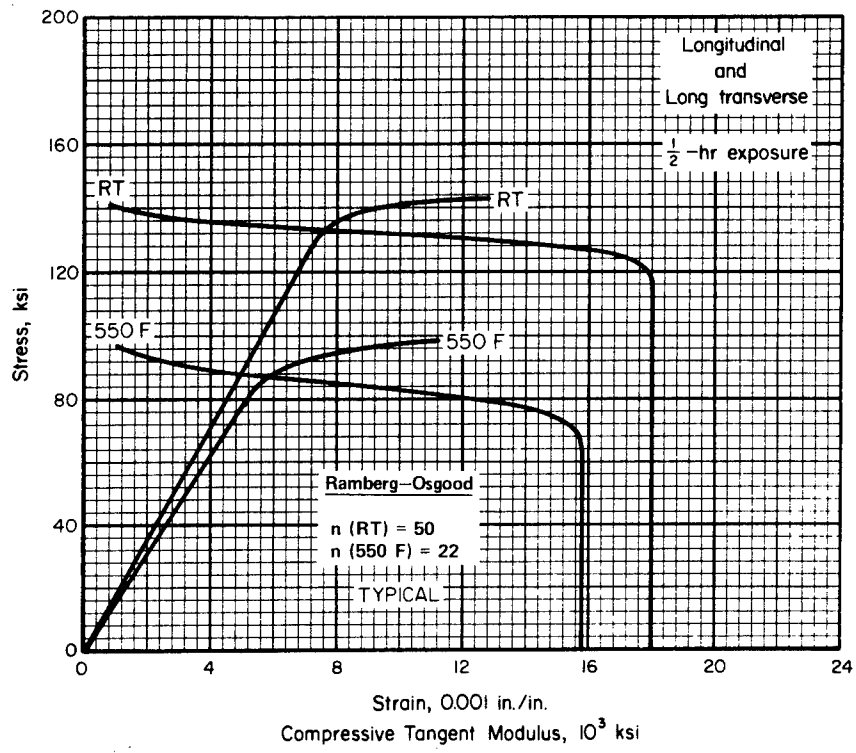


FIGURE 5.3.2.2.6(b). *Typical compressive stress-strain and compressive tangent-modulus curves for duplex-annealed Ti-8Al-1Mo-1V alloy sheet at room and elevated temperatures.*

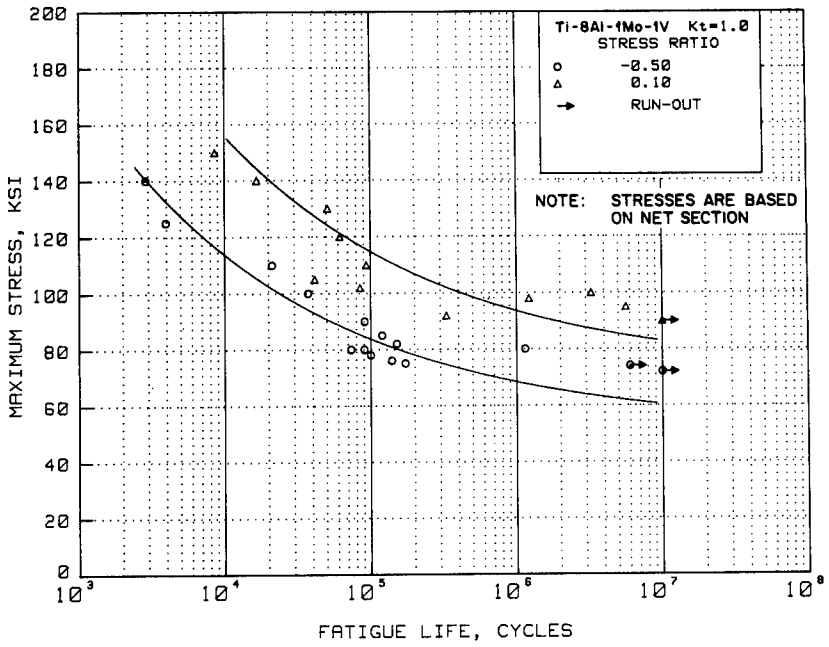


FIGURE 5.3.2.2.8(a). *Best-fit S/N curves for unnotched duplex annealed Ti-8Al-1Mo-1V sheet at room temperature, long transverse direction.*

Correlative Information for Figure 5.3.2.2.8(a)

Product Form: Sheet, 0.050-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	147.2	135.6	RT

Specimen Details: Unnotched
0.750-inch net width

Surface Condition: HNO_3/HF pickled

References: 5.3.2.2.8(a) and (b)

Test Parameters:

Loading — Axial
Frequency — 1800 cpm
Temperature — RT
Environment — Air

No. of Heats/Lots: 1

Equivalent Stress Equation

$\text{Log } N_f = 10.57 - 3.46 \log (S_{eq} - 66.7)$
$S_{eq} = S_{max} (1-R)^{0.61}$
Standard Error of Estimate = 0.47
Standard Deviation in Life = 0.81
$R^2 = 66.7\%$

Sample Size = 24

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

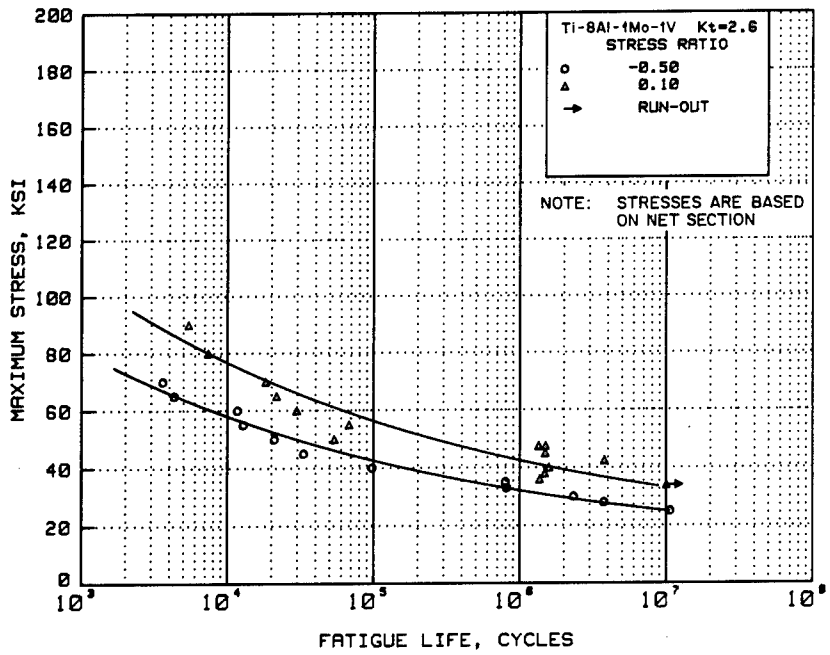


FIGURE 5.3.2.2.8(b). *Best fit S/N curves for notched, K_t = 2.6, duplex annealed Ti-8Al-1Mo-1V sheet at room temperature, long transverse direction.*

Correlative Information for Figure 5.3.2.2.8(b)

Product Form: Sheet, 0.050-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	147.2	135.6	RT Unnotched

Specimen Details: Notched, hole type, K_t = 2.6
1.500-inch, gross width
1.250-inch, net width
0.250-inch, diameter hole

Surface Condition: HNO_3/HF pickled

References: 5.3.2.2.8(a) and (b)

Test Parameters:

Loading — Axial
Frequency — 1800 cpm
Temperature — RT
Environment — Air

No. of Heats/Lots: 1

Equivalent Stress Equation

$\text{Log } N_f = 14.49 - 5.90 \log (S_{eq} - 12.7)$
$S_{eq} = S_{max} (1-R)^{0.55}$
Standard Error of Estimate = 0.33
Standard Deviation in Life = 1.10
R^2 = 90.9%

Sample Size = 26

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

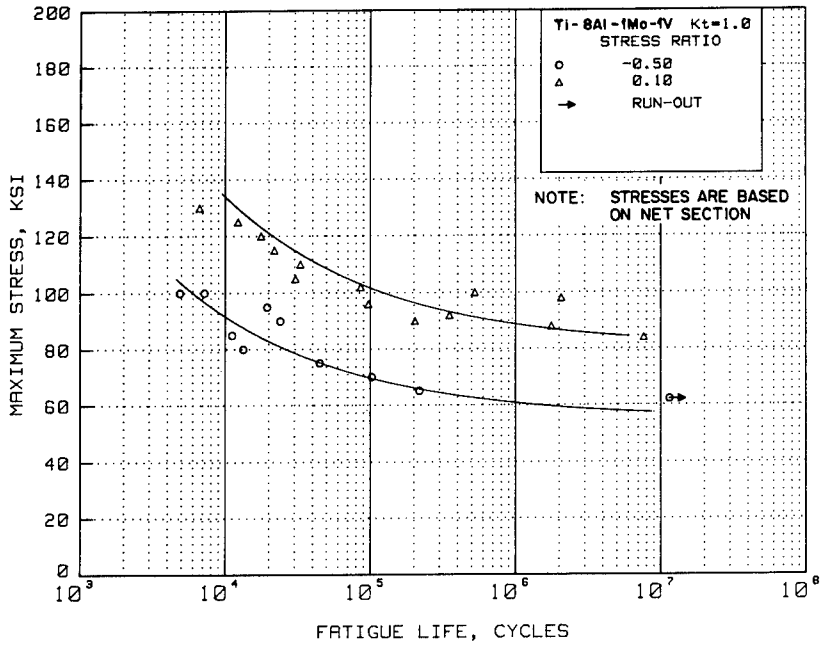


FIGURE 5.3.2.2.8(c). *Best-fit S/N curves for unnotched duplex annealed Ti-8Al-1Mo-1V sheet at 400 F, long transverse direction.*

Correlative Information for Figure 5.3.2.2.8(c)

Product Form: Sheet, 0.050-inch thick

Properties:

TUS, ksi	TYS, ksi	Temp., F
119.5	100.8	400

Specimen Details: Unnotched
0.750-inch net width

Surface Condition: HNO_3/ HF pickled

References: 5.3.2.2.8(a) and (b)

Test Parameters:

Loading — Axial
Frequency — 1800 cpm
Temperature — 400 F
Environment — Air

No. of Heats/ Lots: 1

Equivalent Stress Equation

$\text{Log } N_f = 8.30 - 2.53 \log (S_{eq} - 73.9)$
$S_{eq} = S_{max} (1-R)^{0.74}$
Standard Error of Estimate = 0.38
Standard Deviation in Life = 0.87
$R^2 = 80.9\%$

Sample Size = 23

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

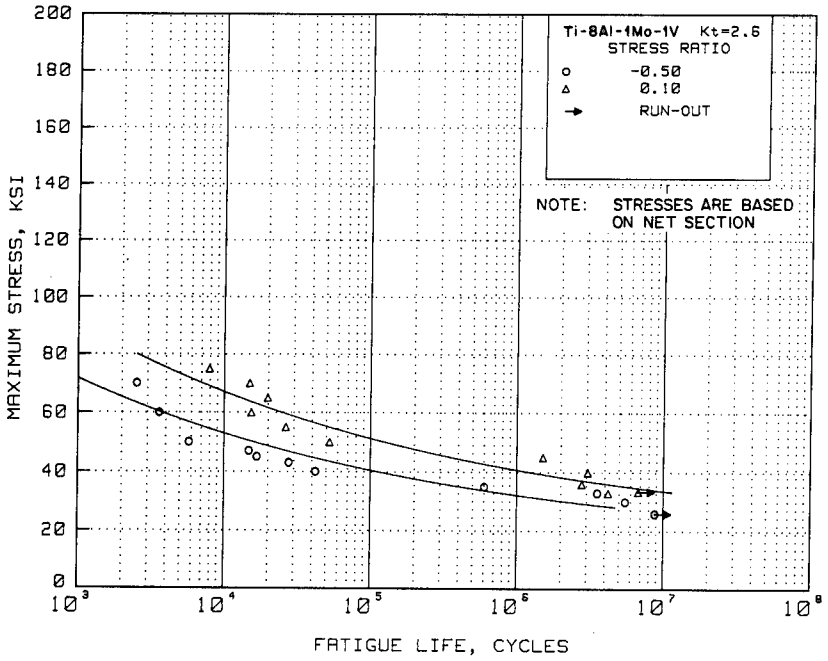


FIGURE 5.3.2.2.8(d). *Best-fit S/N curves for notched, $K_t = 2.6$, duplex annealed Ti-8Al-1 Mo-1V sheet at 400 F, long transverse direction.*

Correlative Information for Figure 5.3.2.2.8(d)

Product Form: Sheet, 0.050-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	119.5	100.8	400
			Unnotched

Specimen Details: Notched, hole type, $K_t = 2.6$
1.500-inch, gross width
1.250-inch, net width
0.250-inch, diameter hole

Surface Condition: HNO_3/HF pickled

References: 5.3.2.2.8(a) and (b)

Test Parameters:

Loading — Axial
Frequency — 1800 cpm
Temperature — 400 F
Environment — Air

No. of Heats/Lots: 1

Equivalent Stress Equation

$\text{Log } N_f = 13.39 - 5.68 \log (S_{eq} - 18.7)$
$S_{eq} = S_{max} (1-R)^{0.46}$
Standard Error of Estimate = 0.41
Standard Deviation in Life = 1.16
$R^2 = 87.2\%$

Sample Size = 20

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

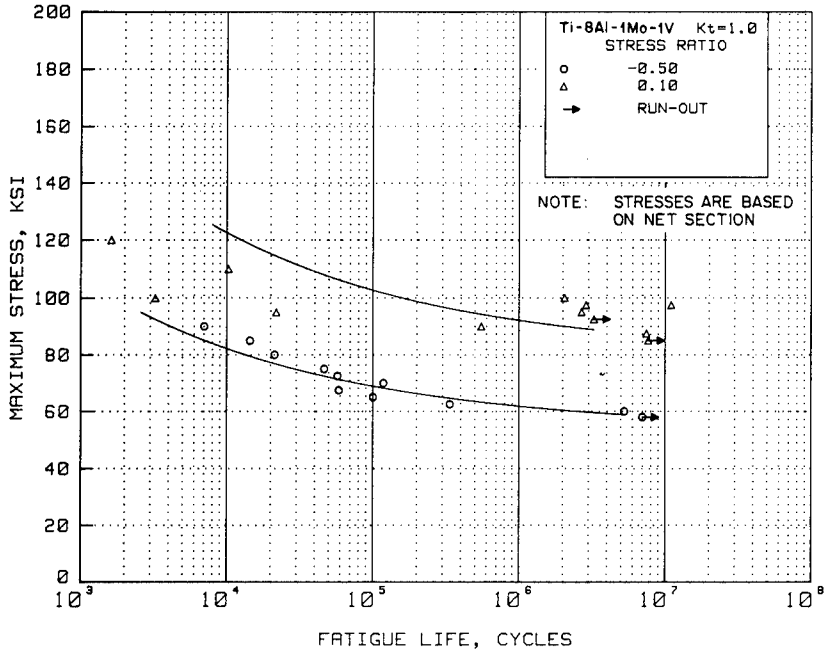


FIGURE 5.3.2.2.8(e). *Best-fit S/N curves for unnotched duplex annealed Ti-8Al-1Mo-1V sheet at 650 F, long transverse direction.*

Correlative Information for Figure 5.3.2.2.8(e)

Product Form: Sheet, 0.050-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	110.2	86.8	650

Specimen Details: Unnotched
0.750-inch net width

Surface Condition: HNO_3/HF pickled

References: 5.3.2.2.8(a) and (b)

Test Parameters:

Loading — Axial
Frequency — 1800 cpm
Temperature — 650 F
Environment — Air

No. of Heats/Lots: 1

Equivalent Stress Equation

$\text{Log } N_f = 9.83 - 3.66 \log (S_{eq} - 73)$
$S_{eq} = S_{max} (1-R)^{0.78}$
Standard Error of Estimate = 0.88
Standard Deviation in Life = 1.18
$R^2 = 44.3\%$

Sample Size = 20

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

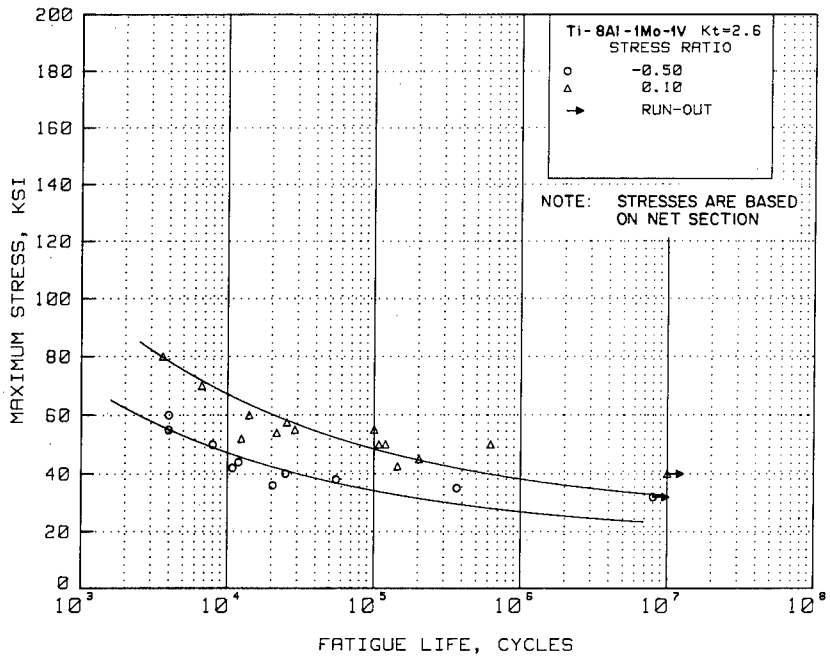


FIGURE 5.3.2.2.8(f). *Best-fit S/N curves for notched, K_t = 2.6, duplex annealed Ti-8Al-1Mo-1V sheet at 650 F, long transverse direction.*

Correlative Information for Figure 5.3.2.2.8(f)

Product Form: Sheet, 0.050-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	110.2	86.8	650 Unnotched

Specimen Details: Notched, hole type, K_t = 2.6
1.500-inch, gross width
1.250-inch, net width
0.250-inch, diameter hole

Surface Condition: HNO_3/HF pickled

References: 5.3.2.2.8(a) and (b)

Test Parameters:

Loading — Axial
Frequency — 1800 cpm
Temperature — 650 F
Environment — Air

No. of Heats/Lots: 1

Equivalent Stress Equation

$\text{Log } N_f = 10.16 - 3.88 \log (S_{eq} - 23)$
$S_{eq} = S_{max} (1-R)^{0.69}$
Standard Error of Estimate = 0.38
Standard Deviation in Life = 0.65
R^2 = 66.0%

Sample Size = 22

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

5.3.3 Ti-6Al-2Sn-4Zr-2Mo

5.3.3.0 *Comments and Properties.*—Ti-6Al-2Sn-4Zr-2Mo is a near-alpha titanium composition developed for improved elevated-temperature performance. The alloy has a titanium-aluminum base that is solid solution strengthened by additions of tin and zirconium. Molybdenum improves both room and elevated temperature strength, creep and thermal stability. Introduction of this alloy initially met the requirements for certain advanced performance gas turbine engine applications. Some of the more recent applications, however, require better creep strength than the alloy initially provided. Development work showed that a small addition of silicon, approximately 0.08 percent, substantially improved the creep strength of the alloy without significantly affecting the thermal stability. The alloy is creep resistant and relatively stable to about 1050 F. Creep and thermal stability of the alloy are further enhanced by solution treating high in the alpha-beta phase field. The alloy is available in bar, billet, plate, sheet, strip, and extrusions.

Manufacturing Conditions.—Forging of Ti-6Al-2Sn-4Zr-2Mo at temperatures below the beta transus temperature is recommended. For optimum creep properties beta forging or a modification of it is recommended with some loss in ductility to be expected. Elevated temperatures may be used for severe sheet forming operations while room-temperature forming may be used for mild contouring. Stress relief annealing may be combined with a final hot-sizing operation. The material can be welded using TIG or MIG fusion processes to achieve 100 percent joint efficiencies but with limited weld zone ductility. As in welding any titanium alloy, shielding from atmospheric contamination is required except for spot or seam welding.

Environmental Considerations.—Ti-6Al-2Sn-4Zr-2Mo is somewhat more resistant to hot-salt cracking than either Ti-8Al-1Mo-1V or Ti-6Al-4V alloys. The material is marginally susceptible to aqueous chloride solution stress-corrosion cracking. Surface oxides formed during exposure to service temperature (~950 F) do not adversely affect properties. Under certain conditions, titanium, when in contact with cadmium, silver, mercury, or certain of their compounds, may become embrittled. Refer to MIL-S-5002 and MIL-STD-1568 for restrictions concerning applications with titanium in contact with these metals or their compounds.

Heat Treatment.—Several different annealing treatments, which are described below, are available for Ti-6Al-2Sn-4Zr-2Mo.

For sheet and strip:

Duplex Anneal: 1650 F for ½ hour, air cool, followed by 1450 F for ¼ hour, and air cool.

Triplex Anneal: 1650 F for ½ hour, air cool, followed by 1450 F for ¼ hour, air cool, followed by 1100 F for 2 hours and air cool.

For plate:

Duplex Anneal: 1650 F for 1 hour, air cool, followed by 1100 F for 8 hours and air cool.

Triplex Anneal: 1650 F for ½ hour, air cool, followed by 1450 F for ¼ hour, air cool, followed by 1100 F for 2 hours and air cool.

For bars and forgings:

Duplex Anneal: Solution anneal 25 to 50 F below beta transus temperature for 1 hour, air cool or faster, followed by 1100 F for 8 hours and air cool.

Specifications and Properties.—Material specifications for Ti-6Al-2Sn-4Zr-2Mo are given in Table 5.3.3.0(a). Room-temperature mechanical and physical properties for Ti-6Al-2Sn-4Zr-2Mo are presented in Table 5.3.3.0(b) and (c). The effect of temperature on physical properties is shown in Figure 5.3.3.0.

TABLE 5.3.3.0(a). *Material Specifications for Ti-6Al-2Sn-4Zr-2Mo*

Specification	Form
MIL-T-9046	Sheet and strip
AMS 4975	Bar
AMS 4976	Forging
AMS 4919	Sheet, strip, and plate

5.3.3.1 *Single, Duplex, and Triplex Annealed.*—Room and elevated temperature property curves are shown in Figures 5.3.3.1.1, 5.3.3.1.2, and 5.3.3.1.4. Typical stress-strain curves at room and elevated temperatures are shown in Figures 5.3.3.1.6(a) and (b). Full range stress-strain curves at room and elevated temperatures are shown in Figure 5.3.3.1.6(c).

TABLE 5.3.3.0(b). *Design Mechanical and Physical Properties of Ti-6Al-2Sn-4Zr-2Mo*

Specification	AMS 4919								MIL-T-9046, Comp. AB-4
Form	Sheet								
Condition	Duplex annealed								Triplex annealed
Thickness or diameter, in. .	≤0.046		0.047-0.093		0.094-0.140		0.141-0.187		≤0.187
Basis	A	B	A	B	A	B	A	B	S[e]
Mechanical Properties:									
F_{tu}, ksi:									
L	135[a]	143	135[a]	143	135[a]	143	135[a]	143	145
LT	135[a]	143	135[a]	143	135[a]	143	135[a]	143	145
F_{ty}, ksi:									
L	125[b]	136	125[b]	136	125[b]	136	125[b]	136	135
LT	125[b]	134	125[b]	134	125[b]	134	125[b]	134	135
F_{cy}, ksi:									
L	132	142	132	142	132	142	132	142	...
LT	132	142	132	142	132	142	132	142	...
F_{su}, ksi	...	...	...	...	...	...	...	...	...
F_{bru}[d], ksi:									
(e/D = 1.5)	195	206	205	217	214	227	219	232	...
(e/D = 2.0)	217	230	243	258	266	282	279	295	...
F_{bry}[d], ksi:									
(e/D = 1.5)	171	183	171	183	171	183	171	183	...
(e/D = 2.0)	202	217	202	217	202	217	202	217	...
e, percent (S-basis):									
L	8[c]	...	c	...	10	...	10	...	c
LT	8[c]	...	c	...	10	...	10	...	c
E, 10^3 ksi	16.5								
E_c, 10^3 ksi	18.0								
G, 10^3 ksi	6.2								
μ	0.32								
Physical Properties:									
ω, lb/in.^{3}	0.164								
C, K, and α	See Figure 5.3.3.0								

[a]S-basis. The A values are as follows: F_{tu}(L & LT) = 139 ksi.
[b]S-basis. The A values are as follows: F_{ty}(L) = 131 ksi and F_{ty}(LT) = 129 ksi.
[c]8% for 0.025 through 0.062 inch and 10% for >0.062 inch.
[d]Bearing values are "dry pin" values per Section 1.4.7 1.
[e]S-basis values are representative of test specimens excised from duplex annealed material and thermally treated to triplex annealed condition in a laboratory furnace.

TABLE 5.3.3.0(c). *Design Mechanical and Physical Properties of Ti-6Al-2Sn-4Zr-2Mo*

Specification	AMS 4975		AMS 4976
Form	Bar		Forging
Condition	STA (Duplex annealed)		STA (Duplex annealed)
Cross-sectional area, in.^{2}	≤16		≤9
Thickness, or diameter, in.	≤3.000		≤3.000
Basis	A	B	S
Mechanical Properties:			
F_{tu}, ksi:			
L	130[a]	144	130
LT	130[b]	...	130[b]
ST	130[b]	...	130[b]
F_{ty}, ksi:			
L	120[a]	131	120
LT	120[b]	...	120[b]
ST	120[b]	...	120[b]
F_{cy}, ksi:			
L	...	...	...
LT	...	...	...
ST	...	...	...
F_{su}, ksi	...	...	...
F_{bru}, ksi:			
(e/D = 1.5)	...	...	...
(e/D = 2.0)	...	...	...
F_{bry}, ksi:			
(e/D = 1.5)	...	...	...
(e/D = 2.0)	...	...	...
e, percent (S basis):			
L	10	...	10
LT	10[b]	...	10[b]
ST	10[b]	...	10[b]
RA, percent (S basis):			
L	25	...	25
LT	25[b]	...	25[b]
ST	25[b]	...	25[b]
E, 10^3 ksi	16.5		
E_c, 10^3 ksi	18.0		
G, 10^3 ksi	6.2		
μ	0.32		
Physical Properties:			
ω, lb/in.^{3}	0.164		
C, K, and α	See Figure 5.3.3.0		

[a]S basis. The A values are as follows: F_{tu}(L) = 138 ksi and F_{ty}(L) = 125 ksi.

[b]S basis. Applicable providing transverse dimension is ≥2.500 in.

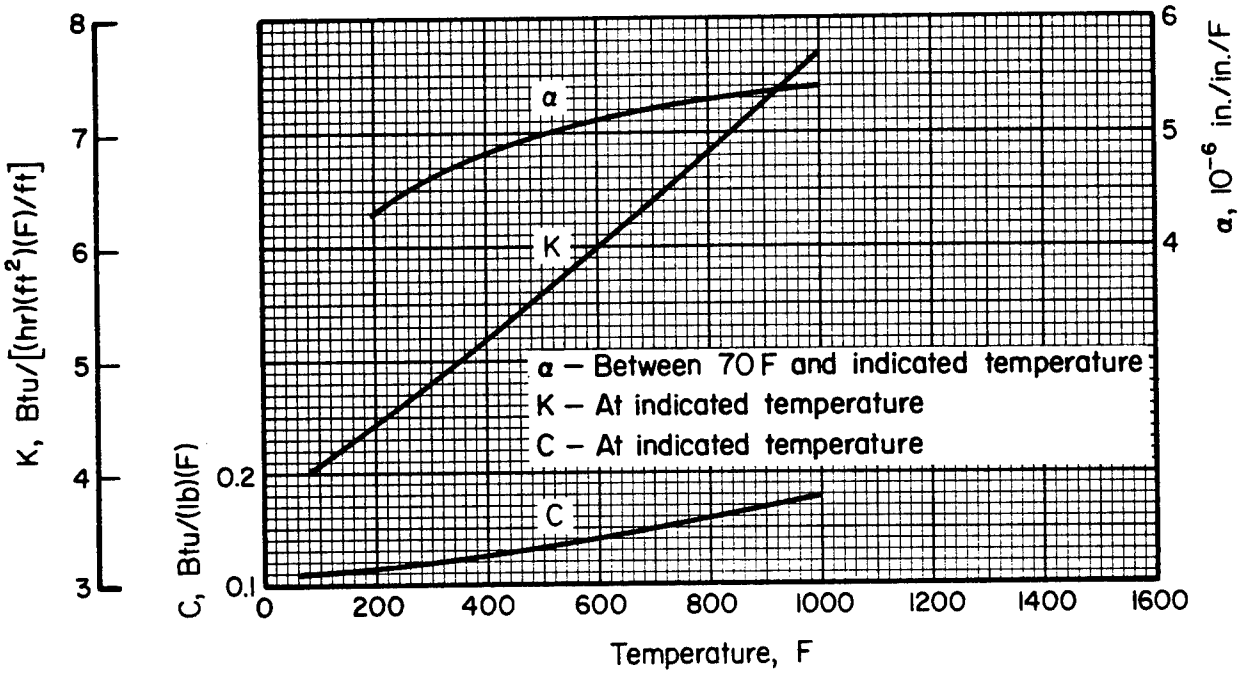


FIGURE 5.3.3.0. *Effect of temperature on the physical properties of Ti-6Al-2Sn-4Zr-2Mo alloy.*

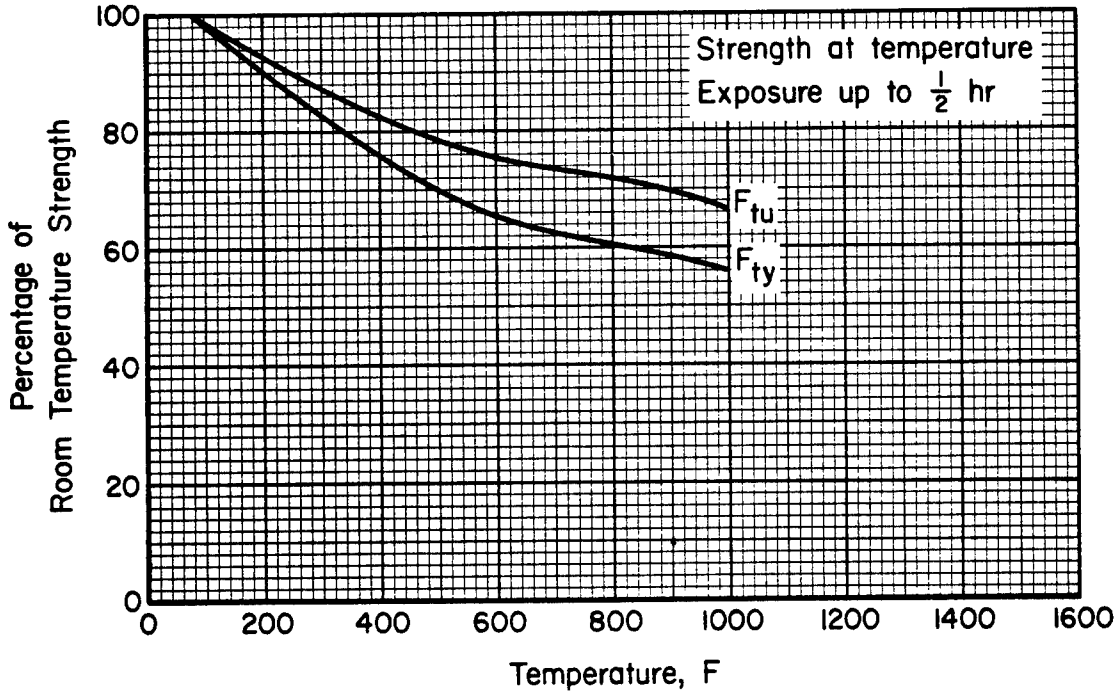


FIGURE 5.3.3.1.1. *Effect of temperature in the tensile ultimate strength (F_{tu}) and tensile yield strength (F_{ty}) of duplex- and triplex-annealed Ti-6Al-2Sn-4Zr-2Mo (all products).*

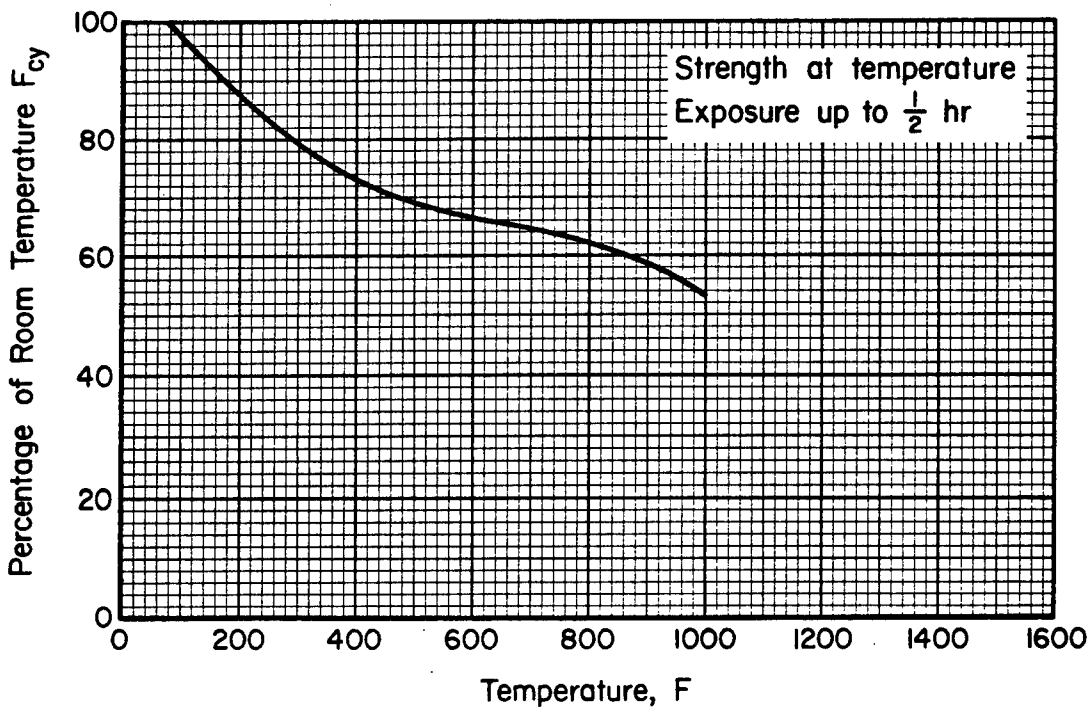


FIGURE 5.3.3.1.2. *Effect of temperature on the compressive yield strength (F_{cy}) of duplex annealed Ti-6Al-2Sn-4Zr-2Mo alloy sheet.*

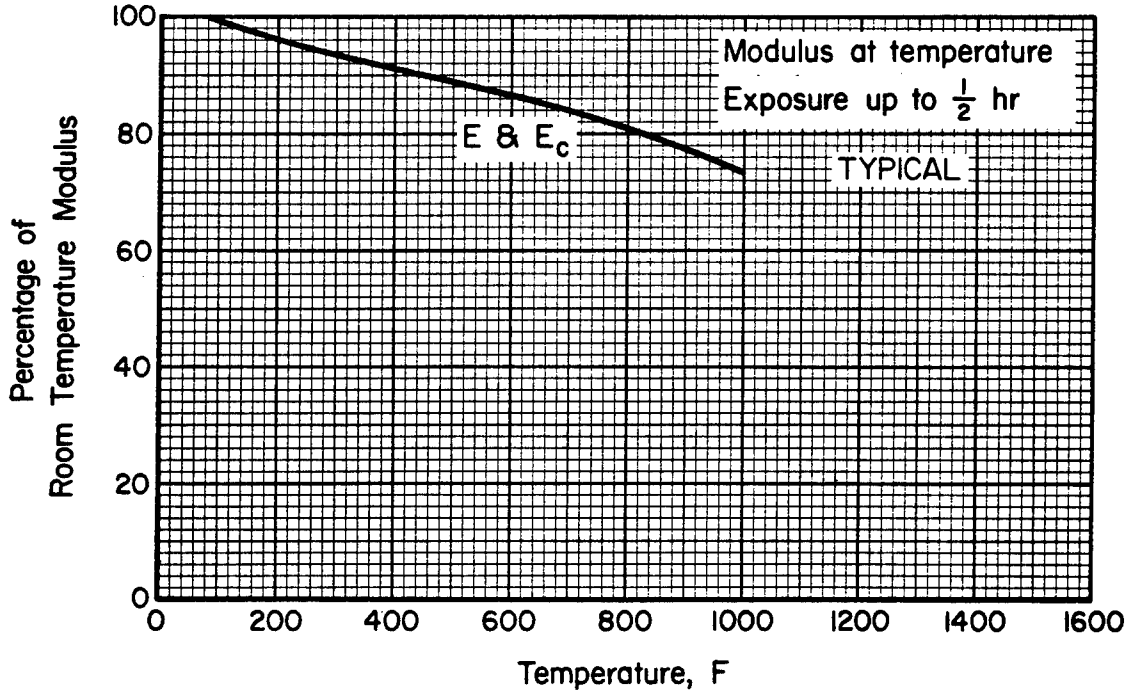


FIGURE 5.3.3.1.4. *Effect of temperature on the tensile and compressive moduli (E and E_c) of duplex- and triplex-annealed Ti-6Al-2Sn-4Zr-2Mo alloy.*

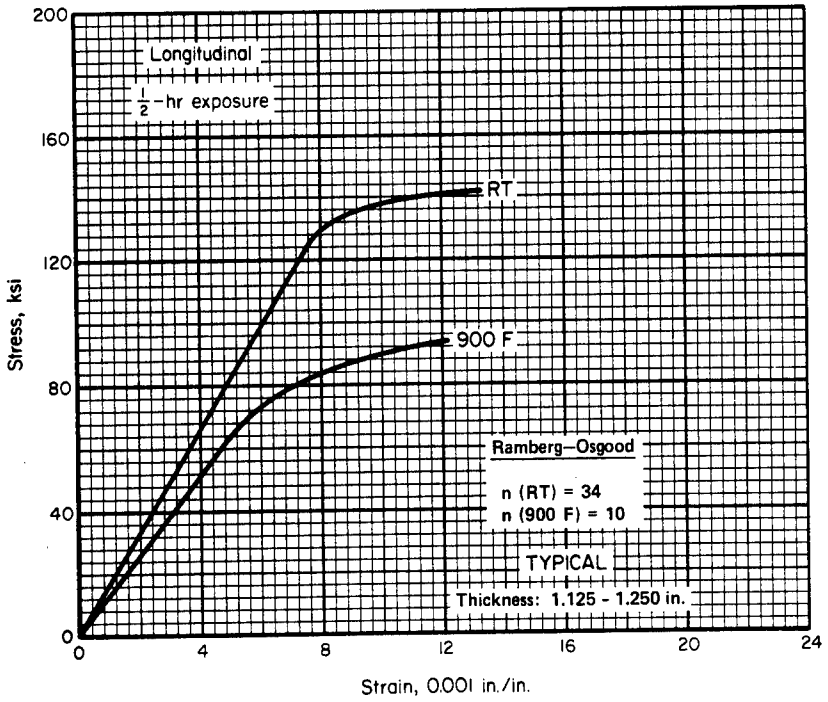


FIGURE 5.3.3.1.6(a). *Typical tensile stress-strain curves for duplex annealed Ti-6Al-2Sn-4Zr-2Mo alloy bar at various temperatures.*

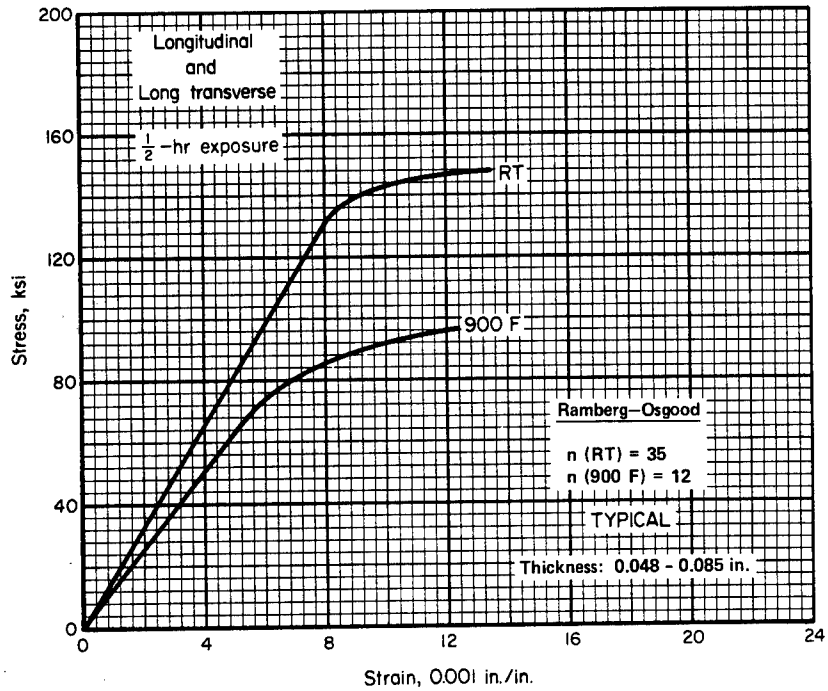


FIGURE 5.3.3.1.6(b). *Typical tensile stress-strain curves for duplex- and triplex-annealed Ti-6Al-2Sn-4Zr-2Mo alloy sheet at various temperatures.*

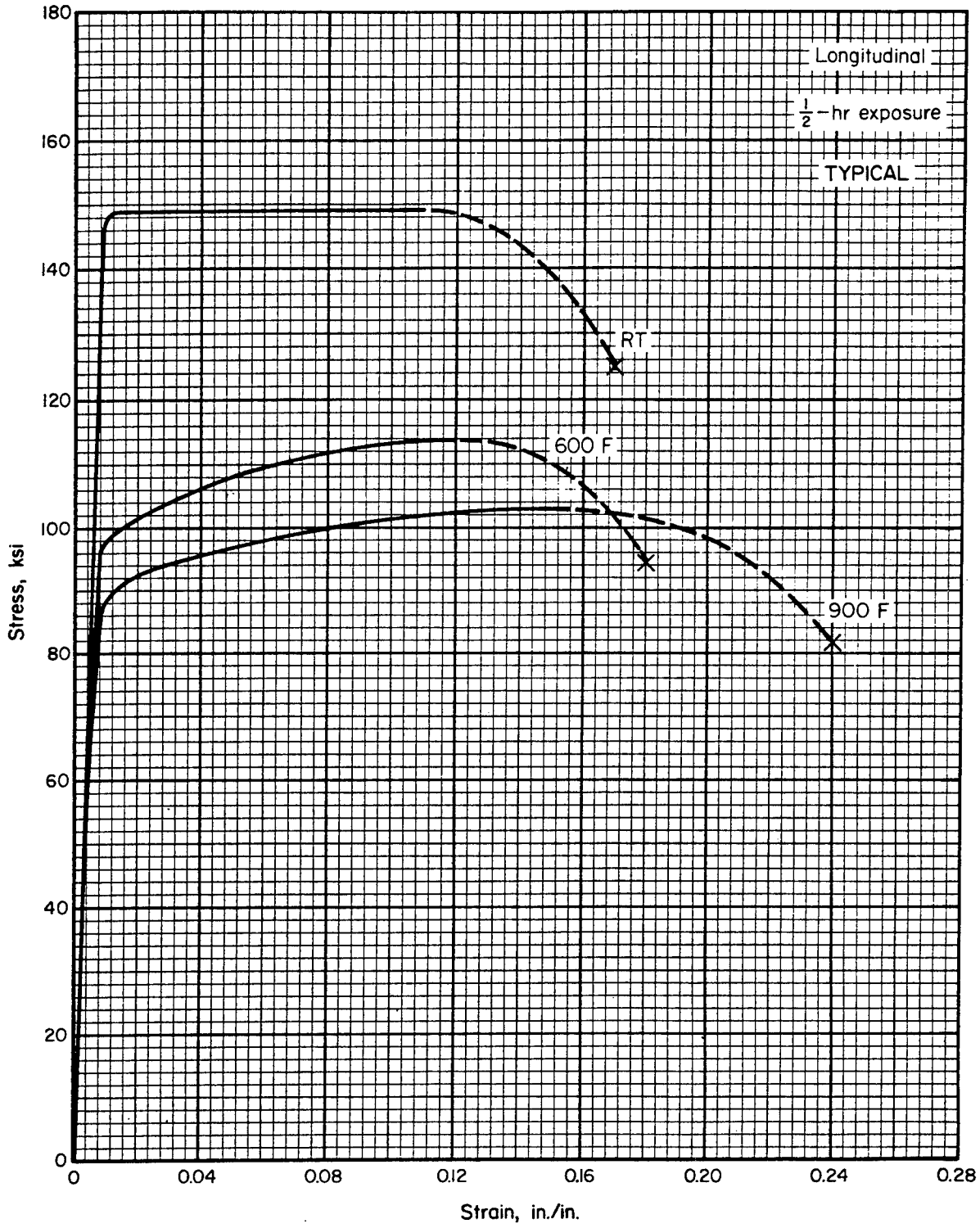


FIGURE 5.3.3.1.6(c). *Typical tensile stress-strain curves (full range) for duplex-annealed Ti-6Al-2Sn-4Zr-2Mo alloy sheet at room and elevated temperatures.*

5.4 Alpha-Beta Titanium Alloys

The alpha-beta titanium alloys contain both alpha and beta phases at room temperature. The alpha phase is similar to that of unalloyed titanium but is strengthened by alpha stabilizing additions (e.g., aluminum). The beta phase is the high-temperature phase of titanium but is stabilized to room temperature by sufficient quantities of beta stabilizing elements as vanadium, molybdenum, iron, or chromium. In addition to strengthening of titanium by the alloying additions, alpha-beta alloys may be further strengthened by heat treatment. The alpha-beta alloys have good strength at room temperature and for short times at elevated temperature. They are not noted for long-time creep strength. With the exception of annealed Ti-6Al-4V, these alloys are not recommended for cryogenic applications. The weldability of many of these alloys is poor because of the two-phase microstructure. However, some of them can be welded successfully with special precautions.

5.4.1 Ti-6Al-4V

5.4.1.0 *Comments and Properties.*—Ti-6Al-4V is available in all mill product forms as well as castings and powder metallurgy forms. It can be used in either the annealed or solution treated plus aged (STA) conditions and is weldable. Useful temperature range is from -320 to 750 F. For maximum toughness, Ti-6Al-4V should be used in the annealed or duplex-annealed conditions whereas for maximum strength, the STA condition is used. The full strength potential for this alloy is not available in sections greater than 1 inch.

Manufacturing Considerations.—Ti-6Al-4V alloy may be forged above the beta transus temperature using procedures to promote a high toughness material. The material is routinely finished below beta transus temperature for good combinations of fabricability, strength, ductility, and toughness. Elevated temperatures are usually used for form flat-rolled products although extensive forming may be accomplished at room temperature. Flat-rolled products are usually formed and used in the annealed condition although some forming in the STA condition is possible.

This alloy can be spot welded and is being fusion welded extensively in certain applications. Established titanium-welding techniques must be employed and special design considerations may be involved in fusion weldments. Stress-relief annealing after welding is recommended.

Environmental Considerations.—Ti-6Al-4V can withstand prolonged exposure to temperatures up to 750 F without loss of ductility. Its toughness in the annealed condition is adequate at temperatures down to -320 F. (A special low interstitial grade may be used down to -423 F.) Ti-6Al-4V is resistant to hot-salt stress corrosion to about its maximum use temperature depending on exposure time and exposure stress. The material is marginally susceptible to aqueous chloride solution stress corrosion, but is considered to have good resistance to this reaction compared with other commonly used alloys. Under certain conditions, titanium, when in contact with cadmium, silver, mercury, or certain of their compounds, may become embrittled. Refer to MIL-S-5002 and MIL-STD-1568 for restrictions concerning applications with titanium in contact with these metals or their compounds.

Heat Treatment.—This alloy is commonly specified in either the annealed condition or in the fully heat-treated condition. Annealing requires 1 hour at 1300 F followed by furnace cooling if maximum ductility is required.

The specified fully heat-treated, or solution-treated and aged condition for sheet is as follows:

Solution treat at 1700 F for 5 to 25 minutes, quench in water.

Age at 975 F for 4 to 6 hours, air cool.

For bars and forgings:

Solution treat at 1700 F for 1 hour, quench in water.

Age at 1000 F for 3 hours, air cool.

Specifications and Properties.—Some material specifications for Ti-6Al-4V are shown in Table 5.4.1.0(a). Room-temperature mechanical proper-

ties for Ti-6Al-4V are shown in Tables 5.4.1.0(b) through (f). The effect of temperature on physical properties is shown in Figure 5.4.1.0.

TABLE 5.4.1.0(a). *Material Specifications for Ti-6Al-4V*

Specificaion	Form
MIL-T-9046	Sheet, strip, and plate
MIL-T-9047	Bar
AMS 4934	Extrusion
AMS 4935	Extrusion
AMS 4967	Bar
AMS 4928	Bar and die forging
AMS 4911	Sheet, strip, and plate
AMS 4920	Die forging

5.4.1.1 *Annealed Condition.*—Elevated temperature curves for annealed Ti-6Al-4V are shown in Figures 5.4.1.1.1 through 5.4.1.1.5. Typical stress-strain curves at several temperatures are shown in Figures 5.4.1.1.6(a) through (c). Typical full-range stress-strain curves at room temperature are shown in Figure 5.4.1.1.6(d). Unnotched and notched fatigue data are shown in Figures 5.4.1.1.8(a) through (g). Fatigue crack-propagation data for plate are shown in Figure 5.4.1.1.9.

5.4.1.2 *Solution-Treated and Aged Condition.*—Elevated temperature curves for solution-treated and aged alloy are shown in Figures 5.4.1.2.1 through 5.4.1.2.4. Typical tensile and compressive stress-strain and tangent-modulus curves are shown in Figures 5.4.1.2.6(a) through (g). Typical full-range stress-strain curves at several temperatures up to 1000 F are shown in Figure 5.4.1.2.6(h). A nomograph of typical creep properties of solution-treated and aged sheet for the temperature range 600 F through 800 F is shown in Figure 5.4.1.2.7. Fatigue data at room and elevated temperatures are shown in Figures 5.4.1.2.8(a) through (i).

TABLE 5.4.1.0(b). *Design Mechanical and Physical Properties of Ti-6Al-4V Sheet, Strip, and Plate*

Specification	AMS 4911 and MIL-T-9046, Comp. AB-1					MIL-T-9046, Comp. AB-1			
Form	Sheet		Plate			Sheet, strip, and plate			
Condition	Annealed					Solution treated and aged			
Thickness, in.	≤ 0.1875		0.1875-2.000		2.001-4.000	≤ 0.1875	0.1875-0.750	0.751-1.000	1.001-2.000
Basis	A	B	A	B	S	S	S	S	S
Mechanical Properties:									
F_{tu}, ksi:									
L	134	139	130[a]	135	130	160	160	150	145
LT	134	139	130[a]	138	130	160	160	150	145
F_{ty}, ksi:									
L	126	131	120	125	120	145	145	140	135
LT	126	131	120[a]	131	120	145	145	140	135
F_{cy}, ksi:									
L	133	138	124	129	124	154	150	145	...
LT	135	141	130	142	130	162	...	...	...
F_{su}, ksi	87	90	79	84	79	100	93	87	...
F_{bru}, ksi:									
(e/D = 1.5)	213[b]	221[b]	206[b]	214[b]	206[b]	236	248	233	...
(e/D = 2.0)	272[b]	283[b]	260[b]	276[b]	260[b]	286	308	289	...
F_{bry}, ksi:									
(e/D = 1.5)	171[b]	178[b]	164[b]	179[b]	164[b]	210	210	203	...
(e/D = 2.0)	208[b]	217[b]	194[b]	212[b]	194[b]	232	243	235	...
e, percent (S-basis):									
L	8[c]	...	10	...	10	5[d]	8	6	6
LT	8[c]	...	10	...	10	5[d]	8	6	6
E, 10^3 ksi	16.0								
E_c, 10^3 ksi	16.4								
G, 10^3 ksi	6.2								
μ	0.31								
Physical Properties:									
ω, lb/in.^{3}	0.160								
C, K, and α	See Figure 4.5.1.0								

[a]The A values are higher than specification values as follows: F_{tu}(L) = 131 ksi, F_{tu}(LT) = 132 ksi, and F_{ty}(LT) = 123 ksi.
[b]Bearing values are "dry pin" values per Section 1.4.7.1.
[c]8%—0.025 to 0.062 in. and 10%—0.063 in. and above.
[d]5%—0.050 in. and above; 4%—0.033 to 0.049 in. and 3%—0.032 in. and below.

TABLE 5.4.1.0(c_1). *Design Mechanical and Physical Properties of Ti-6Al-4V Bar*

Specification	AMS 4928												
Form	Bar												
Condition	Annealed												
Thickness or diameter, in.	<0.500	0.500-1.000		1.001-2.000		2.001-3.000		3.001-4.000		4.001-5.000		5.001-6.000	
Basis	S	A	B	A	B	A	B	A	B	A	B	A	B
Mechanical Properties:													
F_{tu}, ksi:													
L	135	135[a]	142	134	140	130[a]	138	130	135	128	133	125	131
LT	135[b]	135[a]	144	135[a]	143	130[a]	142	130[a]	141	130[a]	139	130[a]	138
F_{ty}, ksi:													
L	125	125[a]	134	125[a]	131	120[a]	128	120	125	117	122	114	119
LT	125[b]	125[a]	134	125[a]	132	120[a]	131	120[a]	129	120[a]	127	119	125
F_{cy}, ksi:													
L	129	129	138	129	135	...	...	...	...	...	...	...	...
LT	...	...	...	...	...	...	...	...	...	...	...	...	...
F_{su}, ksi	83	83	87	82	86	...	...	...	...	...	...	...	...
F_{bru}, ksi:													
(e/D = 1.5)	201	201	212	200	209	...	...	...	...	...	...	...	...
(e/D = 2.0)	253	253	266	251	262	...	...	...	...	...	...	...	...
F_{bry}, ksi:													
(e/D = 1.5)	177	177	190	177	186	...	...	...	...	...	...	...	...
(e/D = 2.0)	205	205	220	205	215	...	...	...	...	...	...	...	...
e, percent (S-basis):													
L	10	10	...	10	...	10	...	10	...	10	...	10	...
LT	10[b]	10[b]	...	10[b]	...	10[b]	...	10	...	10	...	10	...
ST	...	...	...	...	...	10[b]	...	10	...	8	...	8	...
RA, percent (S-basis):													
L	25	25	...	25	...	25	...	25	...	20	...	20	...
LT	20[b]	20[b]	...	20[b]	...	20[b]	...	20	...	20	...	20	...
ST	...	...	...	...	...	15[b]	...	15	...	15	...	15	...
E, 10^3 ksi	16.0												
E_c, 10^3 ksi	16.4												
G, 10^3 ksi	6.2												
μ	0.31												
Physical Properties:													
ω, lb/in.^{3}	0.160												
C, K, and α	See Figure 5.4.1.0												

[a]S-basis. The A values are shown in Table 5.4.1.0(c_2).
[b]Applicable, providing LT or ST dimension is ≥ 2.500 inches.

TABLE 5.4.1.0(c_2). *A-Values for Tensile Yield and Ultimate Strength of Ti-6Al-4V Bar*

Thickness or diameter, in.	0.500-1.000	1.001-2.000	2.001-3.000	3.001-4.000	4.001-5.000	5.001-6.000
Mechanical Properties:						
F_{tu}, ksi:						
L	137	...	132	...	...	...
LT	140	139	138	136	135	134
F_{ty}, ksi:						
L	129	126	123	...	...	...
LT	129	127	127	123	121	...

TABLE 5.4.1.0(c_3). *Design Mechanical and Physical Properties of Ti-6Al-4V Bar*

Specification	MIL-T-9047												
Form	Bar												
Condition	Annealed												
Cross-sectional area, in.^{2}	≤48												
Thickness, in.	<0.500	0.500-1.000		1.001-2.000		2.001-3.000		3.001-4.000		4.001-5.000		5.001-6.000	
Basis	S	A	B	A	B	A	B	A	B	A	B	A	B
Mechanical Properties:													
F_{tu}, ksi:													
L	130	130[a]	142	130[a]	140	130[a]	138	130	135	128	133	125	131
LT	130[b]	130[a]	144	130[a]	143	130[a]	142	130[a]	141	130[a]	139	130[a]	138
F_{ty}, ksi:													
L	120	120[a]	134	120[a]	131	120[a]	128	120	125	117	122	114	119
LT	120[b]	120[a]	134	120[a]	132	120[a]	131	120[a]	129	120	127	119	125
F_{cy}, ksi:													
L	124	124	138	124	135	...	...	...	...	...	...	...	...
LT	...	...	...	...	...	...	...	...	...	...	...	...	...
F_{su}, ksi	80	80	87	80	86	...	...	...	...	...	...	...	...
F_{bru}, ksi:													
(e/D = 1.5)	194	194	212	194	209	...	...	...	...	...	...	...	...
(e/D = 2.0)	244	244	266	244	262	...	...	...	...	...	...	...	...
F_{bry}, ksi:													
(e/D = 1.5)	170	170	190	170	186	...	...	...	...	...	...	...	...
(e/D = 2.0)	197	197	220	197	215	...	...	...	...	...	...	...	...
e, percent (S basis):													
L	10	10	...	10	...	10	...	10	...	10	...	10	...
LT	10[b]	10[b]	...	10[b]	...	10[b]	...	10	...	10	...	10	...
ST	...	...	...	...	...	...	...	8	...	8	...	8	...
RA, percent (S-basis):													
L	25	25	...	25	...	25	...	25	...	20	...	20	...
LT	25[b]	25[b]	...	25[b]	...	25[b]	...	25	...	20	...	20	...
ST	...	...	...	...	...	...	...	15	...	15	...	15	...
E, 10^3 ksi	16.0												
E_c, 10^3, ksi	16.4												
G, 10^3, ksi	6.2												
μ	0.31												
Physical Properties:													
ω, lb/in.^{3}	0.160												
C, K, and α	See Figure 5.4.1.0												

[a]S-basis. The A values are shown in Table 5.4.1.0(c_4).
[b]Applicable, providing LT dimension is ≥3.000 inches.

TABLE 5.4.1.0(c_4). *A-Values for Tensile Yield and Ultimate Strength of Ti-6Al-4V Bar*

Thickness or diameter, in.	0.500-1.000	1.001-2.000	2.001-3.000	3.001-4.000	4.001-5.000	5.001-6.000
Mechanical Properties:						
F_{tu}, ksi:						
L	137	134	132	...	...	...
LT	140	139	138	136	135	134
F_{ty}, ksi:						
L	129	126	123	...	...	...
LT	129	127	125	123	121	...

TABLE 5.4.1.0(d). *Design Mechanical and Physical Properties of Ti-6Al-4V Bar*

Specification	AMS 4967[a] and MIL-T-9047									MIL-T-9047				
Form	Rectangular bar									Round, square, and hexagon bar				
Condition	Solution treated and aged													
Width, in.	0.501-8.000	1.001-4.000	4.001-8.000	1.501-4.000	4.001-8.000	2.001-4.000	4.001-8.000	3.001-8.000	4.001-8.000	...	...	...	...	...
Thickness, in.	≤0.500	0.501-1.000		1.001-1.500		1.501-2.000		2.001-3.000	3.001-4.000	≤0.500	0.501-1.000	1.001-1.500	1.501-2.000	2.001-3.000
Basis	S	S	S	S	S	S	S	S	S	S	S	S	S	S
Mechanical Properties:														
F_{tu}, ksi:														
L	160	155	150	150	145	145	140	135	130	165	160	155	150	140
LT	160	155	150	150	145	145	140	135	130	165	160	155	150	140
F_{ty}, ksi:														
L	150	145	140	140	135	135	130	125	120	155	150	145	140	130
LT	150	145	140	140	135	135	130	125	120	155	150	145	140	130
F_{cy}, ksi:														
L	...	...	...	...	...	...	...	...	...	...	...	...	...	...
LT	...	...	...	...	...	...	...	...	...	...	...	...	...	...
F_{su}, ksi	92	...	...	...	...	...	...	...	...	...	...	...	...	...
F_{bru}, ksi:														
(e/D = 1.5)	...	...	...	...	...	...	...	...	...	...	...	...	...	...
(e/D = 2.0)	...	...	...	...	...	...	...	...	...	...	...	...	...	...
F_{bry}, ksi:														
(e/D = 1.5)	...	...	...	...	...	...	...	...	...	...	...	...	...	...
(e/D = 2.0)	...	...	...	...	...	...	...	...	...	...	...	...	...	...
e, percent:														
L	10	10	10	10	10	10	10	10	8	10	10	10	10	10
LT	10	10	10	10	10	10	10	10	8	10	10	10	10	10
RA, percent:														
L	25	20	20	20	20	20	20	20	15	20	20	20	20	20
LT	25	20	20	20	20	20	20	20	15	20	20	20	20	20
E, 10^3 ksi	16.0													
E_c, 10^3 ksi	16.4													
G, 10^3 ksi	6.2													
μ	0.31													
Physical Properties:														
ω, lb/in.^{3}	0.160													
C, K, and α	See Figure 5.4.1.0													

[a]For AMS 4967, *e* and *RA* values may be different than those shown.

TABLE 5.4.1.0(e). *Design Mechanical and Physical Properties of Ti-6Al-4V Extrusion*

Specification	AMS 4935				AMS 4934							
Form	Extrusion											
Condition	Annealed				Solution treated and aged							
Thickness or diameter, in.	≤2.000		2.001-3.000		<0.500		0.501-0.750		0.751-1.000		1.001-2.000	2.001-3.000
Basis	A	B	A	B	A	B	A	B	A	B	S	S
Mechanical Properties:												
F_{tu}, ksi:												
L	130[a]	137	130[b]	135	155	163	151	157	147	153	140	130
LT[d]	130[a]	139	130[b]	139	155	163	151	157	147	155	140	130
F_{ty}, ksi:												
L	120	124	118	122	138	147	138	143	133	140	130	120
LT[d]	120[a]	128	120	125	138	147	138	145	133	142	130	120
F_{cy}, ksi:												
L	128	133	124	128	147	157	147	153	142	150	139	128
LT[d]	129	138	...	...	147	157	147	155	139	152	139	128
F_{su}, ksi	83	89	...	...	94	99	92	96	89	93	85	79
F_{bru}[c], ksi:												
(e/D = 1.5)	214	226	...	...	243	256	237	246	231	240	220	204
(e/D = 2.0)	264	278	...	...	311	327	303	315	295	307	281	261
F_{bry}[c], ksi:												
(e/D = 1.5)	180	186	...	...	208	222	208	216	201	212	196	182
(e/D = 2.0)	210	217	...	...	242	257	242	250	233	245	228	210
e, percent (S-basis):												
L	10	...	10	...	6	...	6	...	6	...	6	6
LT[d]	8	...	8	...	6	...	6	...	6	...	6	6
RA, percent (S-basis):												
L	20	...	20	...	12	...	12	...	12	...	12	12
LT[d]	15	...	15	...	12	...	12	...	12	...	12	12
E, 10^3 ksi	16.0											
E_c, 10^3 ksi	16.4											
G, 10^3 ksi	6.2											
μ	0.31											
Physical Properties:												
ω, lb/in.^{3}	0.160											
C, K, and α	See Figure 5.4.1.0											

[a]S-basis. The A values are higher than specification values as follows: F_{tu} (L) and (LT) = 132 ksi and F_{ty} (LT) = 121 ksi.
[b]S-basis. The A values are higher than specification values as follows: F_{tu} (L) = 132 ksi and F_{tu} (LT) = 136 ksi.
[c]Applicable, providing LT dimension is ≥2.500 inches.
[d]Bearing values are "dry pin" values per Section 1.4.7.1.

TABLE 5.4.1.0(f). *Design Mechanical and Physical Properties of Ti-6Al-4V Die Forging*

Specification	AMS 4928			AMS 4920	
Form	Die Forging				
Condition	Alpha-beta processed, annealed			Alpha-beta or beta processed, annealed	
Thickness, in.	≤2.000	2.001-4.000	4.001-6.000	≤2.000	2.001-6.000
Basis	S	S	S	S	S
Mechanical Properties:					
F_{tu}, ksi:					
L	135	130	130	130	130
LT	135[a]	130[a]	130	130[a]	130[a]
ST	...	130[a]	130	...	130[a]
F_{ty}, ksi:					
L	125	120	120	120	120
LT	125[a]	120[a]	120	120[a]	120[a]
ST	...	120[a]	120	...	120[a]
F_{cy}, ksi:					
L	...	123	123	...	123
LT	...	128	128	...	128
ST	...	...	...	...	...
F_{su}, ksi	...	79	79	...	79
F_{bru}, ksi:					
(e/D = 1.5)	...	203	203	...	203
(e/D = 2.0)	...	257	257	...	257
F_{bry}, ksi:					
(e/D = 1.5)	...	171	171	...	171
(e/D = 2.0)	...	201	201	...	201
e, percent:					
L	10	10	10	8	8
LT	10[a]	10[a]	10	8[a]	8[a]
ST	...	10[a]	8	...	8[a]
RA, percent:					
L	25	25	20	15	15
LT	20[a]	20[a]	20	15[a]	15[a]
ST	...	15[a]	15	...	15[a]
E, 10^3 ksi	16.0				
E_c, 10^3	16.4				
G, 10^3 ksi	6.2				
μ	0.31				
Physical Properties:					
ω, lb/in.^{3}	0.160				
C, K, and α	See Figure 5.4.1.0				

[a]Applicable providing LT or ST dimension is ≥2.500 inches.

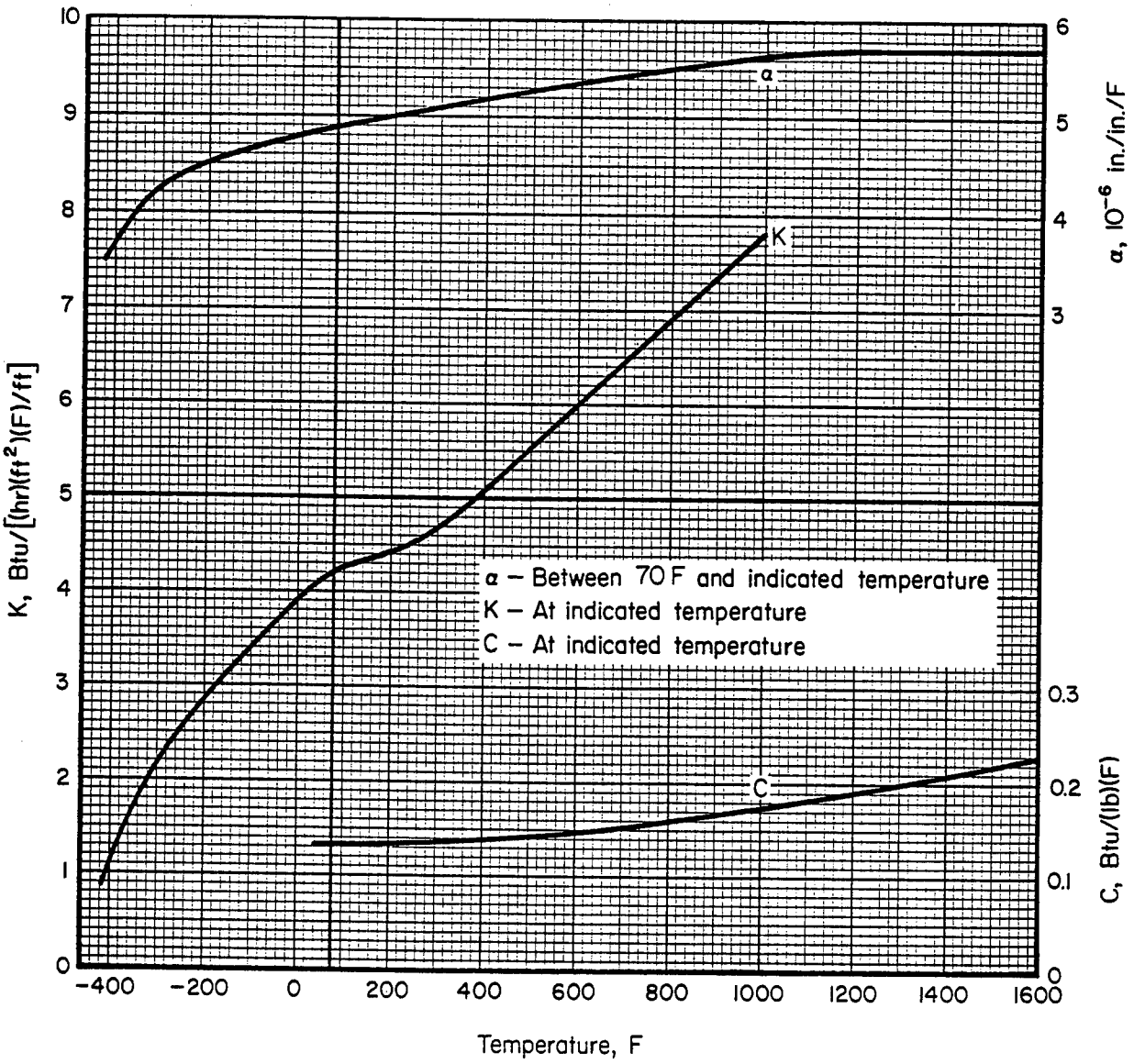


FIGURE 5.4.1.0. *Effect of temperature on the physical properties of Ti-6Al-4V alloy.*

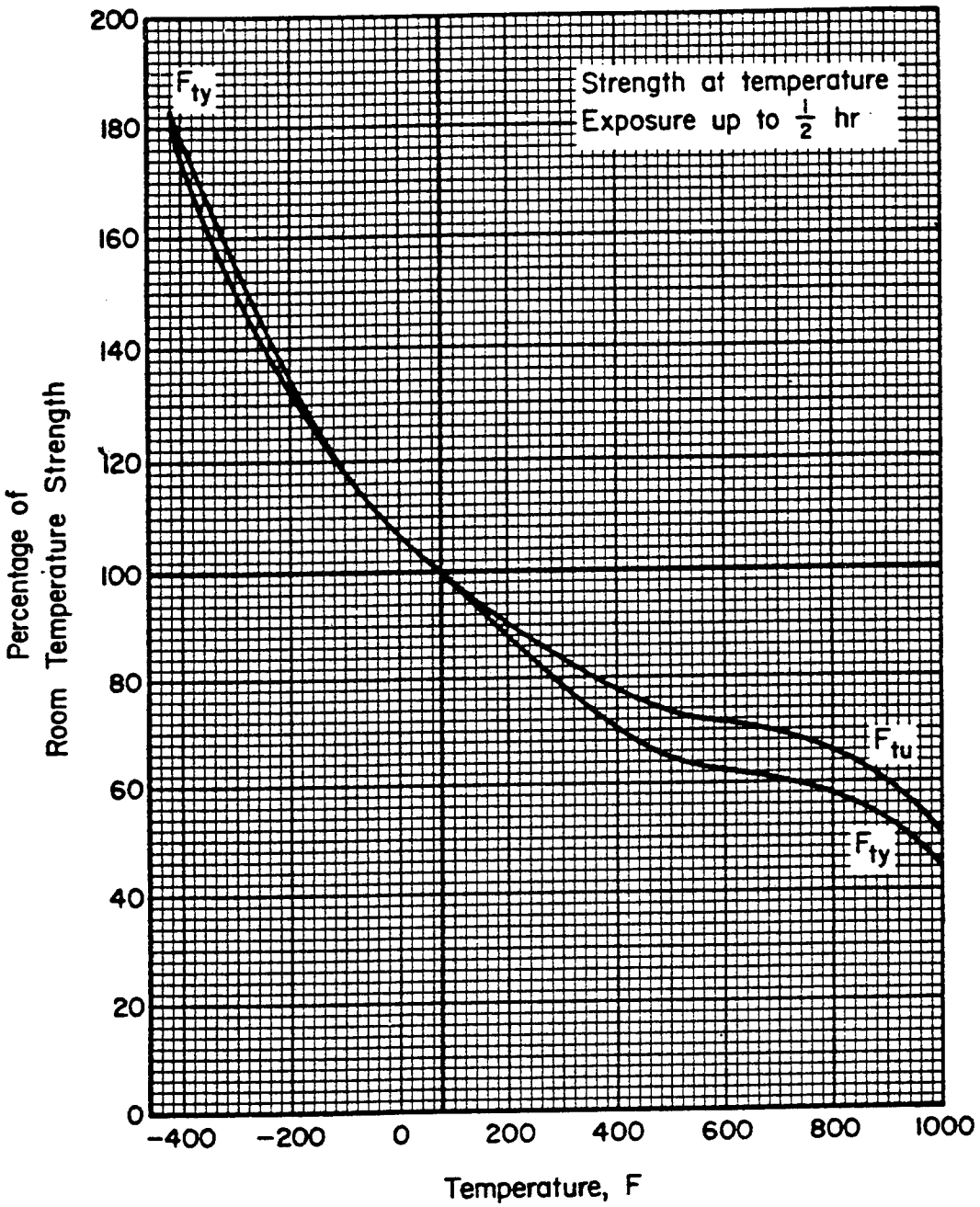


FIGURE 5.4.1.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of annealed Ti-6Al-4V alloy (all products).*

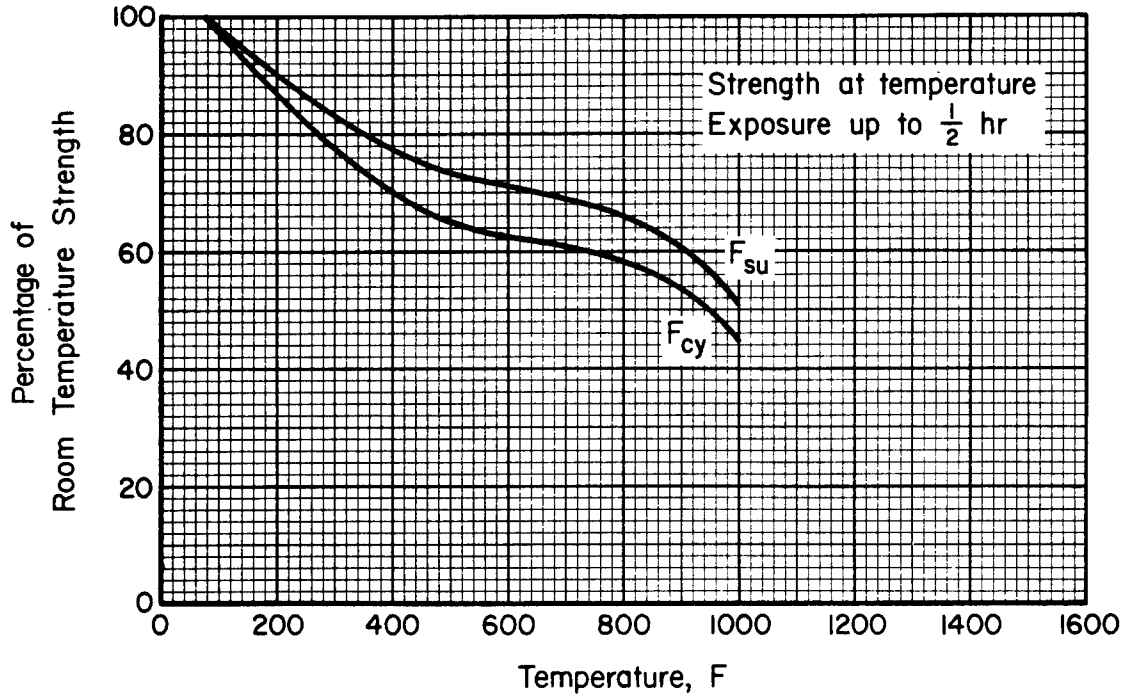


FIGURE 5.4.1.1.2. *Effect of temperature on the compressive yield strength (F_{cy}) and the shear ultimate strength (F_{su}) of annealed Ti-6Al-4V alloy (all products).*

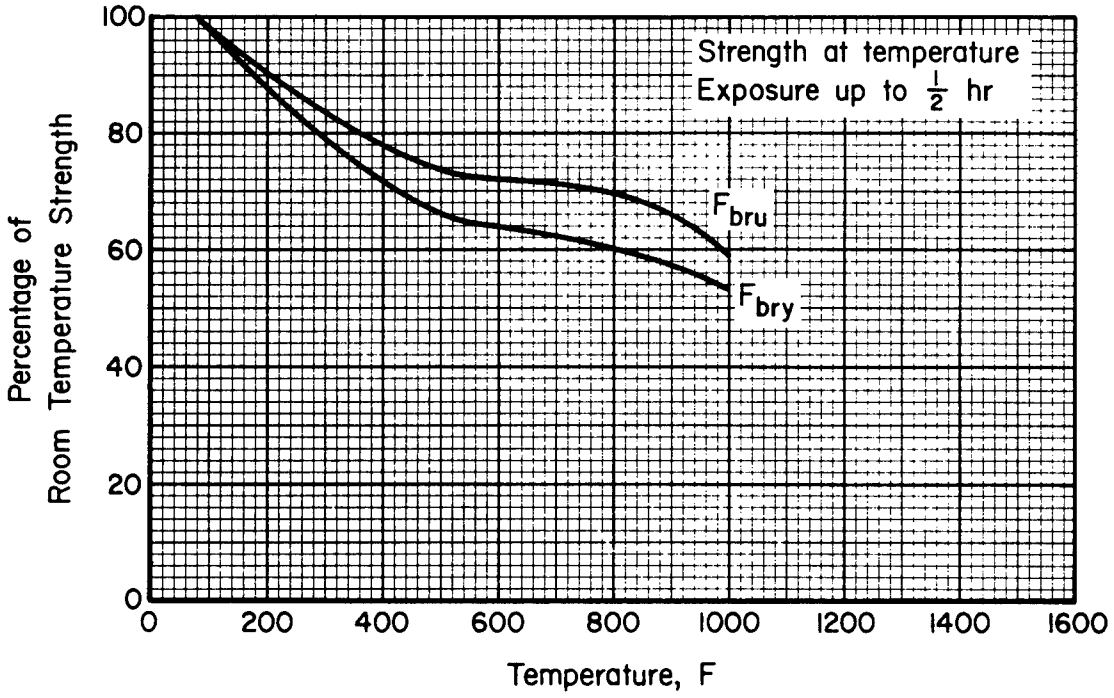


FIGURE 5.4.1.1.3. *Effect of temperature on the bearing ultimate strength (F_{bru}) and the bearing yield strength (F_{bry}) of annealed Ti-6Al-4V alloy (all products).*

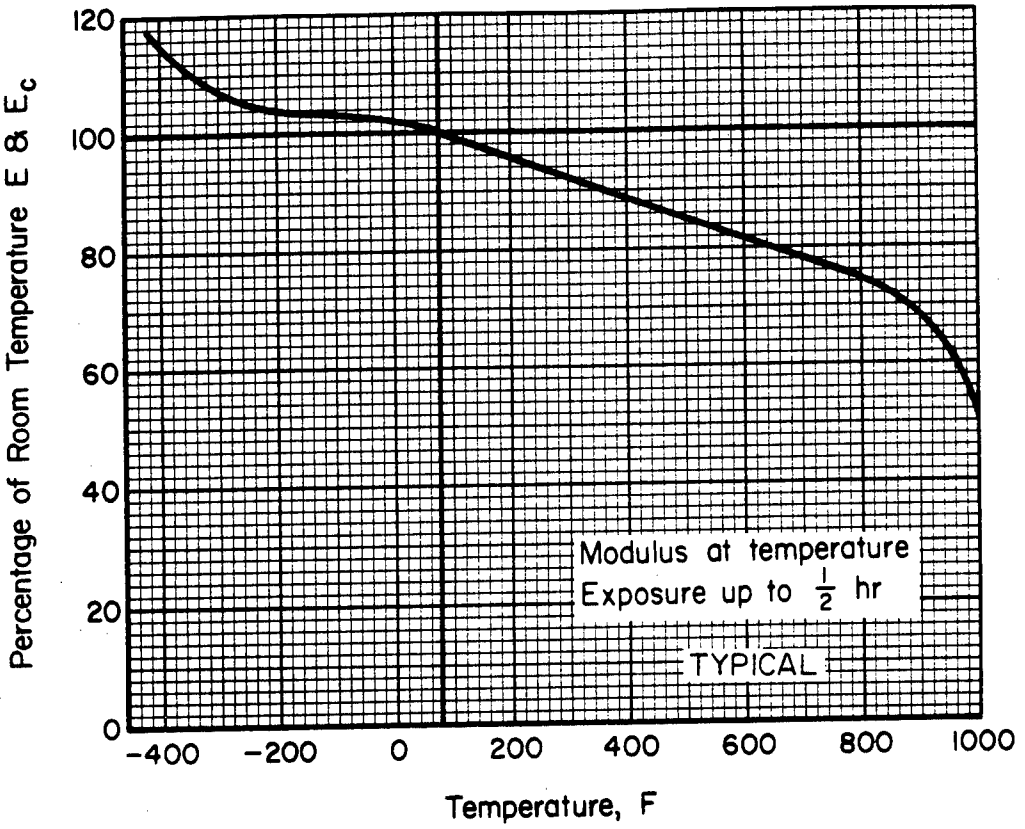


FIGURE 5.4.1.1.4. *Effect of temperature on the tensile and compressive moduli (E and E_c) of annealed Ti-6Al-4V alloy sheet and bar.*

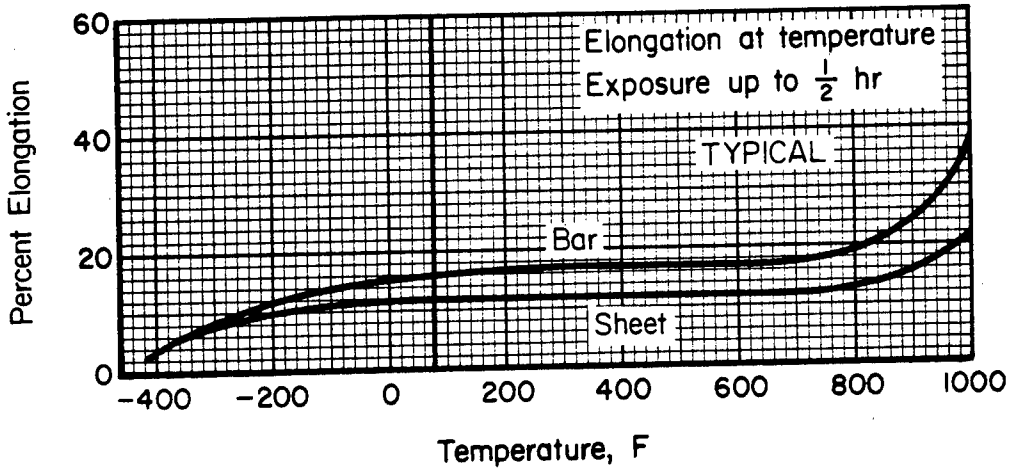


FIGURE 5.4.1.1.5. *Effect of temperature on the elongation of annealed Ti-6Al-4V alloy sheet and bar.*

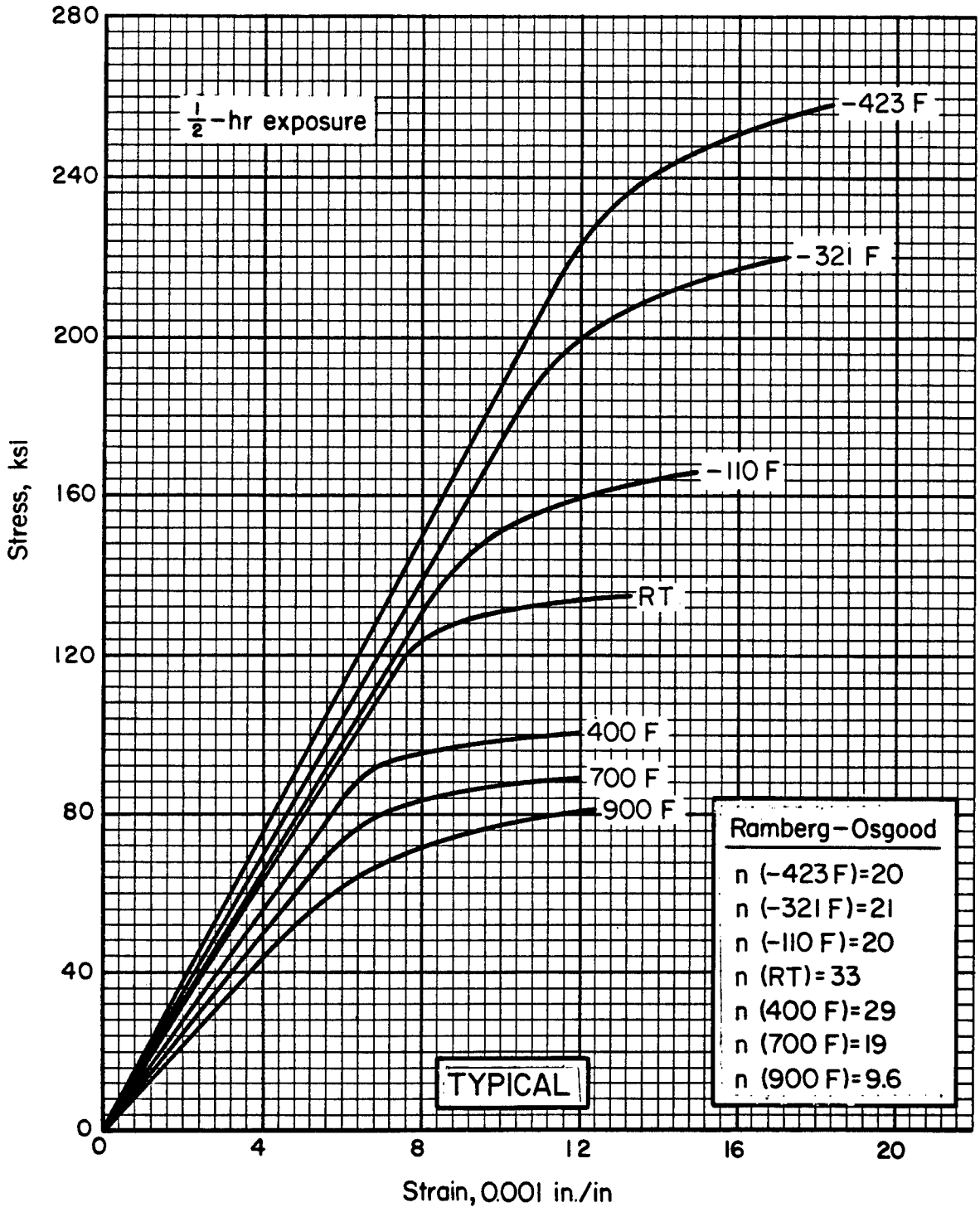


FIGURE 5.4.1.1.6(a). *Typical tensile stress-strain curves at cryogenic, room, and elevated temperatures for annealed Ti-6Al-4V alloy extrusion.*

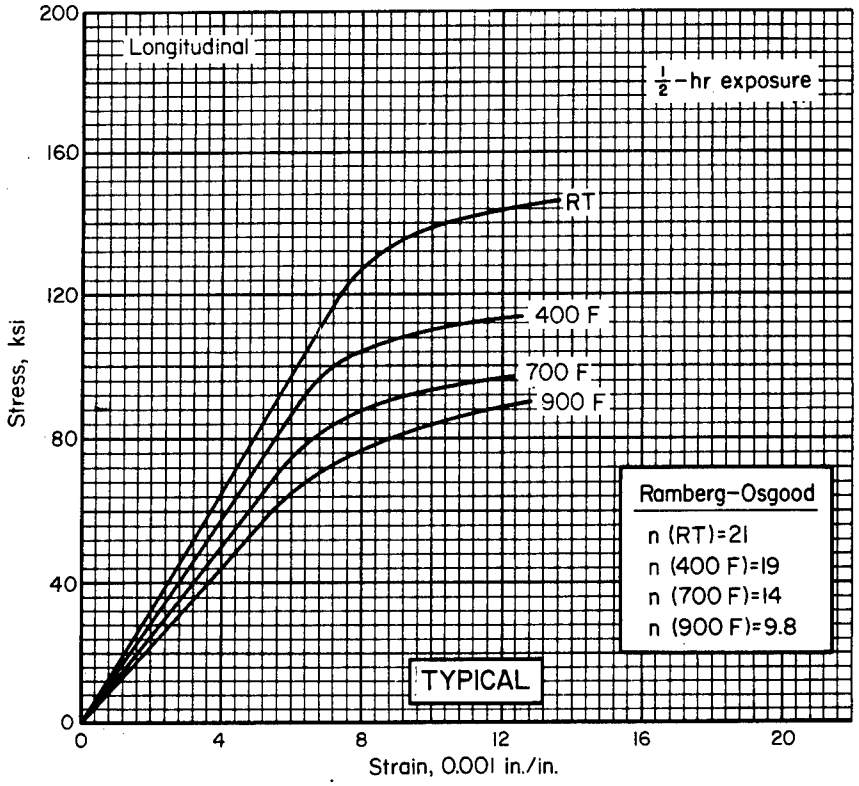


FIGURE 5.4.1.1.6(b). *Typical compressive stress-strain curves at room and elevated temperatures for annealed Ti-6Al-4V alloy extrusion.*

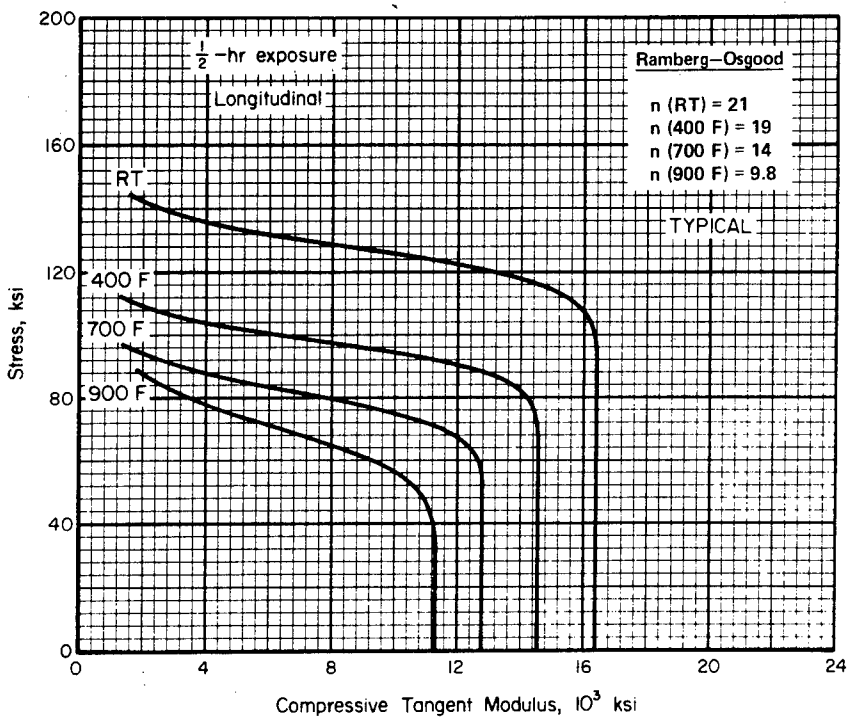


FIGURE 5.4.1.1.6(c). *Typical compressive tangent-modulus curves at room and elevated temperatures for annealed Ti-6Al-4V alloy extrusion.*

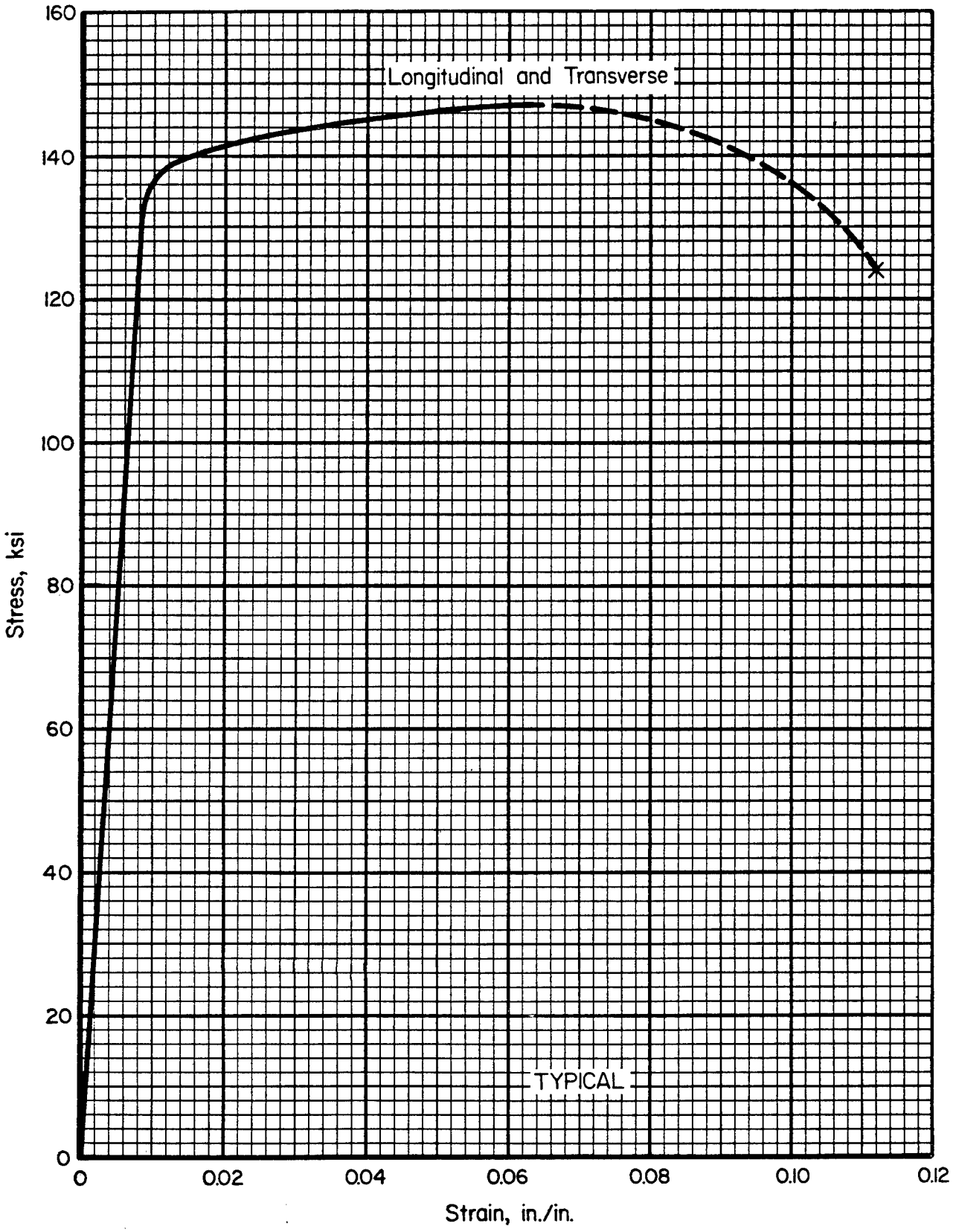


FIGURE 5.4.1.1.6(d). *Typical tensile stress-strain curves (full range) for annealed Ti-6Al-4V sheet at room temperature.*

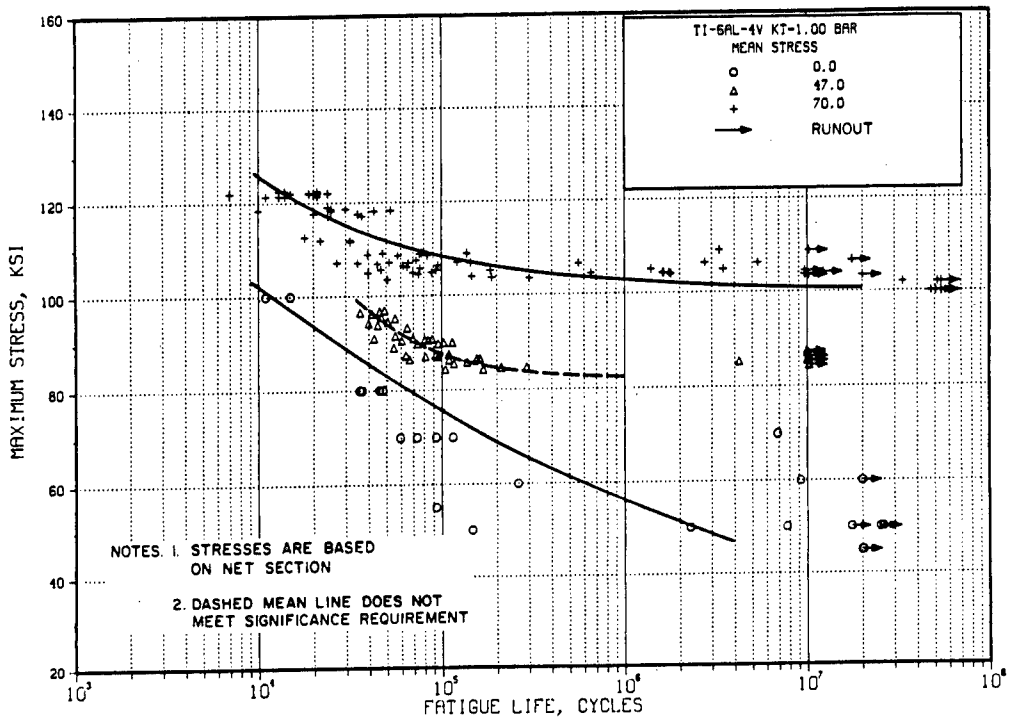


FIGURE 5.4.1.1.8(a). *Best-fit S/N curves for unnotched Ti-6Al-4V annealed bar, longitudinal direction.*

Correlative Information for Figure 5.4.1.1.8(a)

Product Form: Bar, 1-1/4-inch diameter

Properties:	TUS, ksi	TYS, ksi	Temp., F
	137	129	RT

Specimen Details: Unnotched
0.280-inch diameter

Surface Condition:

0 ksi mean stress—32 RMS ground
47 ksi mean stress—100 RMS machined
70 ksi mean stress—32 RMS ground and 100 RMS machined

Reference: 5.4.1.1.8(a)

Test Parameters:

Loading - Axial
Frequency - 1800 cpm
Temperature - RT
Environment - Air

No. of Heats/Lots: Not specified

Maximum Stress Equations:

Log N_f = 19.18–7.55 log S_{max}, S_m = 0

= 5.70–0.94 Log (S_{max}–82.3), S_m = 47
= 7.08–2.18 Log (S_{max}–99.6), S_m = 70

Sample Size = 134

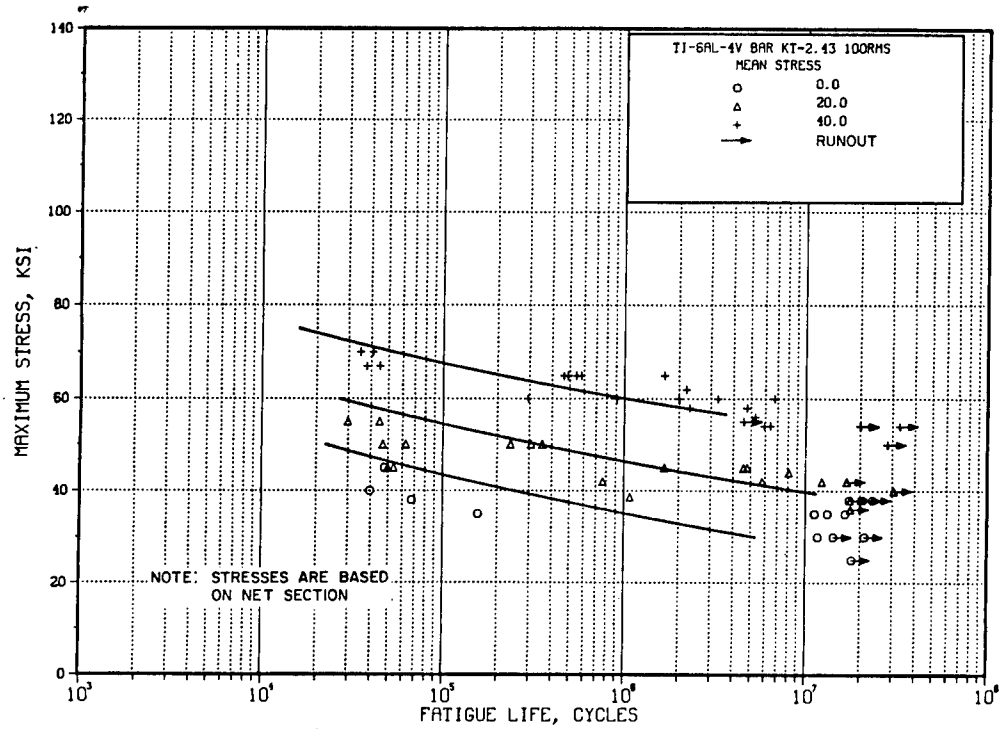


FIGURE 5.4.1.1.8(b). *Best-fit S/N curves for notched, K_t = 2.43, Ti-6Al-4V annealed bar, longitudinal direction.*

Correlative Information for Figure 5.4.1.1.8(b)

Product Form: Bar, 1-inch diameter

Properties:	TUS, ksi	TYS, ksi	Temp., F
	150	143	RT

Specimen Details: 60° V-notch
0.025-inch notch radius
0.260-inch test section diameter at notch

Surface Condition: RMS 100 machined

Reference: 5.4.1.1.8(a)

Test Parameters:

Loading – Axial
Frequency – 1800 cpm
Temperature – RT
Environment – Air

No. of Heats/Lots: Not specified

Equivalent Stress Equation:

$\log N_f = 24.1 - 10.7 \log S_{eq}$

$S_{eq} = S_{max} (1-R)^{0.49}$
Standard Error of Estimate = 0.677
Standard Deviation in Life = 0.920
R^2 = 46%

Sample Size = 46

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

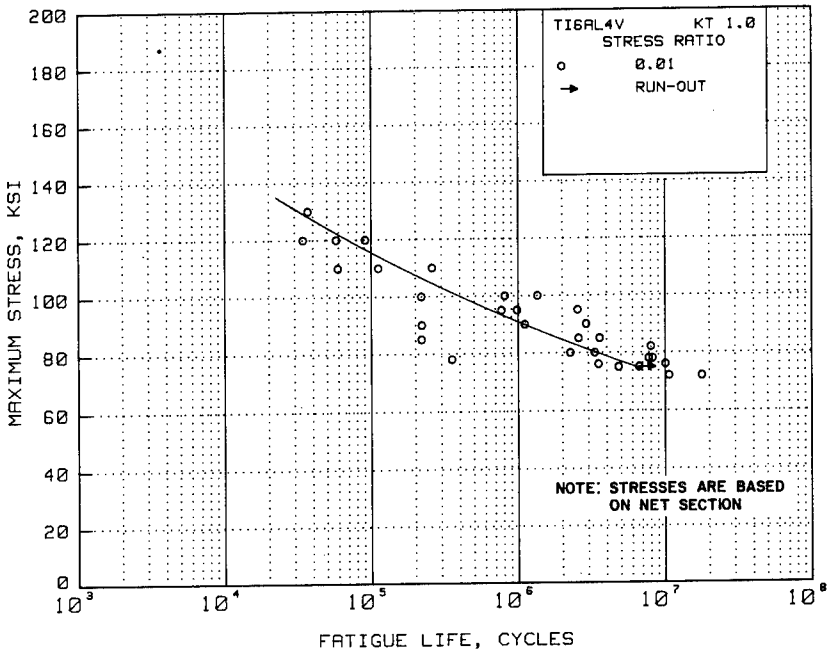


FIGURE 5.4.1.1.8(c). *Best-fit S/N curves for unnotched annealed Ti-6Al-4V extrusion at room temperature, longitudinal direction.*

Correlative Information for Figure 5.4.1.1.8(c)

Product Form: Extrusion, 0.300- and 0.560-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	143	127	RT

Specimen Details: Unnotched
1.50-inch gross width
0.75-inch net width
4.00-inch net section radius

Surface Conditions: RMS 63

Reference: 5.4.1.1.8(b)

Test Parameters:

Loading — Axial
Frequency — 1800 cpm
Temperature — RT
Environment — Air

No. of Heats/Lots: Not specified.

Equivalent Stress Equation:

$\log N_f = 24.8 - 9.6 \log (S_{max})$
Standard Error of Estimate = 0.41
Standard Deviation in Life = 0.81
$R^2 = 75\%$

Sample Size = 30

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

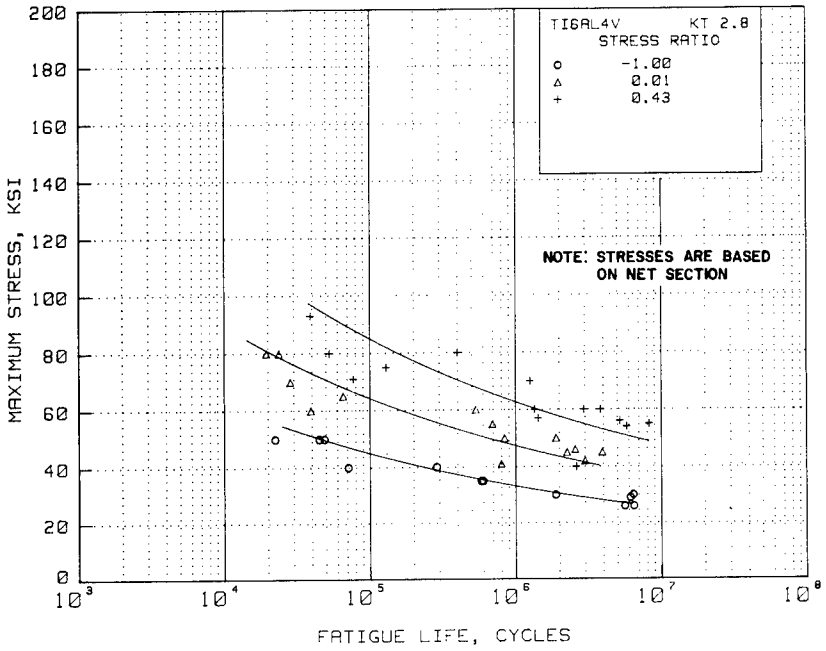


FIGURE 5.4.1.1.8(d). *Best-fit S/N curves for notched, K_t = 2.8, annealed Ti-6Al-4V extrusion at room temperature, longitudinal direction.*

Correlative Information for Figure 5.4.1.1.8(d)

Product Form: Extrusion, 0.300- and 0.560-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	143	127	RT

Specimen Details: Notched, hole type, K_t = 2.8
0.250-inch hole diameter
1.500-inch gross width
1.750-inch net width

Surface Conditions: RMS 63

Reference: 5.4.1.1.8(b)

Test Parameters:

Loading — Axial
Frequency — 1800 cpm
Temperature — RT
Environment — Air

No. of Heats/Lots: Not specified.

Equivalent Stress Equation:

$\text{Log } N_f = 14.8 - 5.8 \log (S_{eq})$
$S_{eq} = S_{max}(1-R)^{0.50}$
Standard Error of Estimate = 0.41
Standard Deviation in Life = 0.86
R^2 = 78%

Sample Size = 40

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

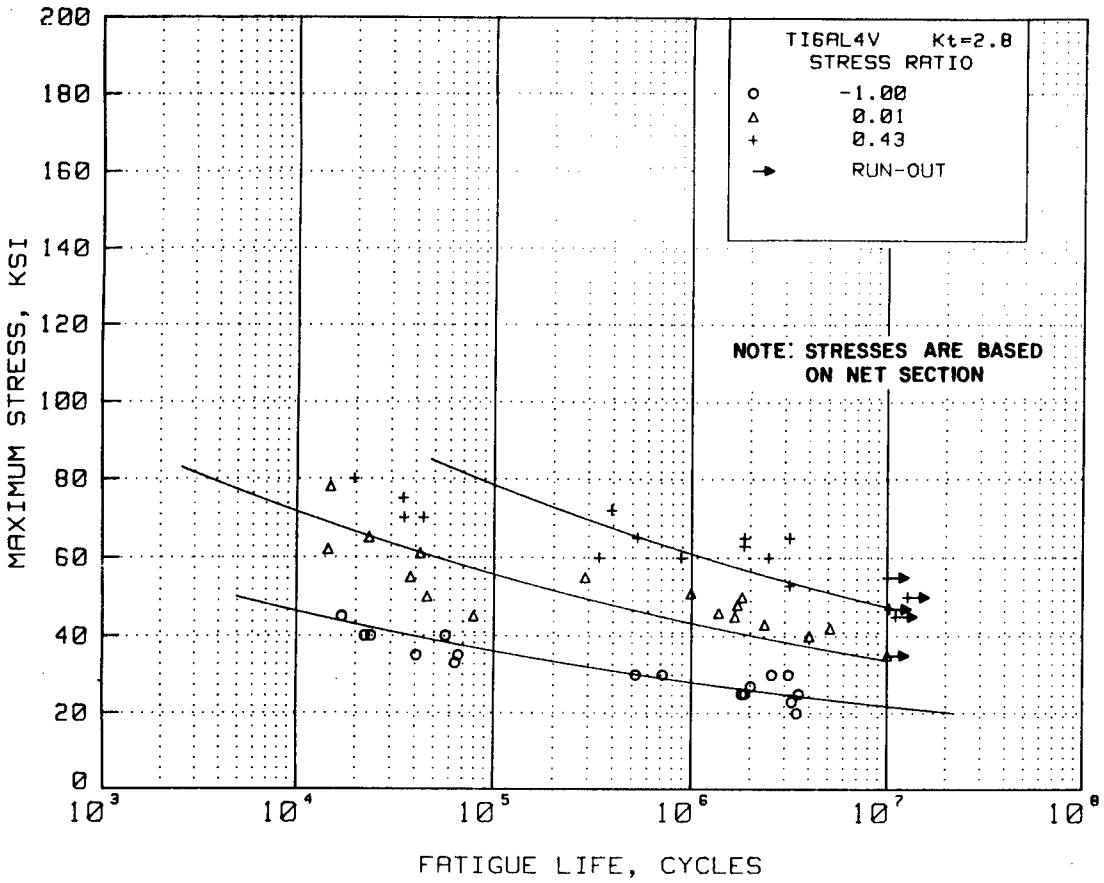


FIGURE 5.4.1.1.8(e). *Best-fit S/N curves for notched, K_t = 2.8, annealed Ti-6Al-4V extrusion at 400 and 600 F, longitudinal direction.*

Correlative Information for Figure 5.4.1.1.8(e)

Product Form: Extrusion, 0.300- and 0.560-inch thick

Properties:

TUS, ksi	TYS, ksi	Temp., F
112	92	400
101	77	600

Specimen Details: Notched, hole type, K_t = 2.8
0.250-inch hole diameter
1.250-inch net width
1.500-inch gross width

Surface Condition: RMS 63

Reference: 5.4.1.1.8(b)

Test Parameters:
Loading - Axial
Frequency - 1800 cpm
Temperature - 400 F and 600 F
Environment - Air

No. of Heats/Lots: Not specified

Equivalent Stress Equation:
$\text{Log } N_f = 21.0\text{-}9.18 \log (S_{eq})$
$S_{eq} = S_{max}(1\text{-}R)^{0.62}$
Standard Error of Estimate = 0.50
Standard Deviation in Life = 0.89
R^2 = 68%

Sample Size: 47

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

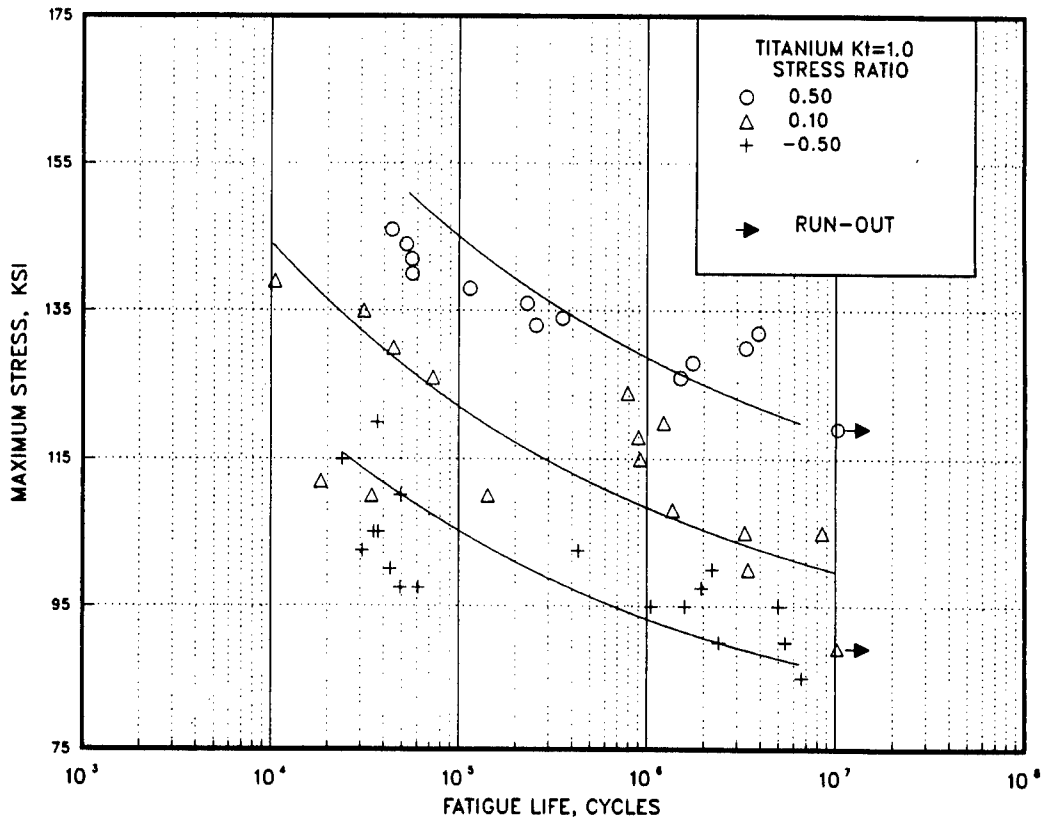


FIGURE 5.4.1.1.8(f). *Best-fit S/N curves for unnotched Ti-6Al-4V annealed sheet, long transverse direction.*

Correlative Information for Figure 5.4.1.1.8(f)

Product Form: Sheet, 0.063, 0.070, 0.078-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	147-152	136-143	RT

Specimen Details: Unnotched, 0.375-inch width

Surface Condition: Machined to 32 RMS, lightly polished with 400 grit emery paper

Reference: 5.4.1.1.8(c)

Test Parameters:
Loading - Axial
Frequency - 10-95 Hz
Temperature - RT
Environment - Air

No. of Heats/Lots: 3

Equivalent Strain Equation:
$\text{Log } N_f = 12.59 - 4.89 \log (S_{eq} - 82.8)$
$S_{eq} = S_{max}(1\text{-}R)^{0.29}$
Standard Deviation of Log Life = 0.62
Adjusted R^2 = 50.6%

Sample Size: 47

[Caution: The equivalent strain model may provide unrealistic life predictions for strain ratios and ranges beyond those represented above]

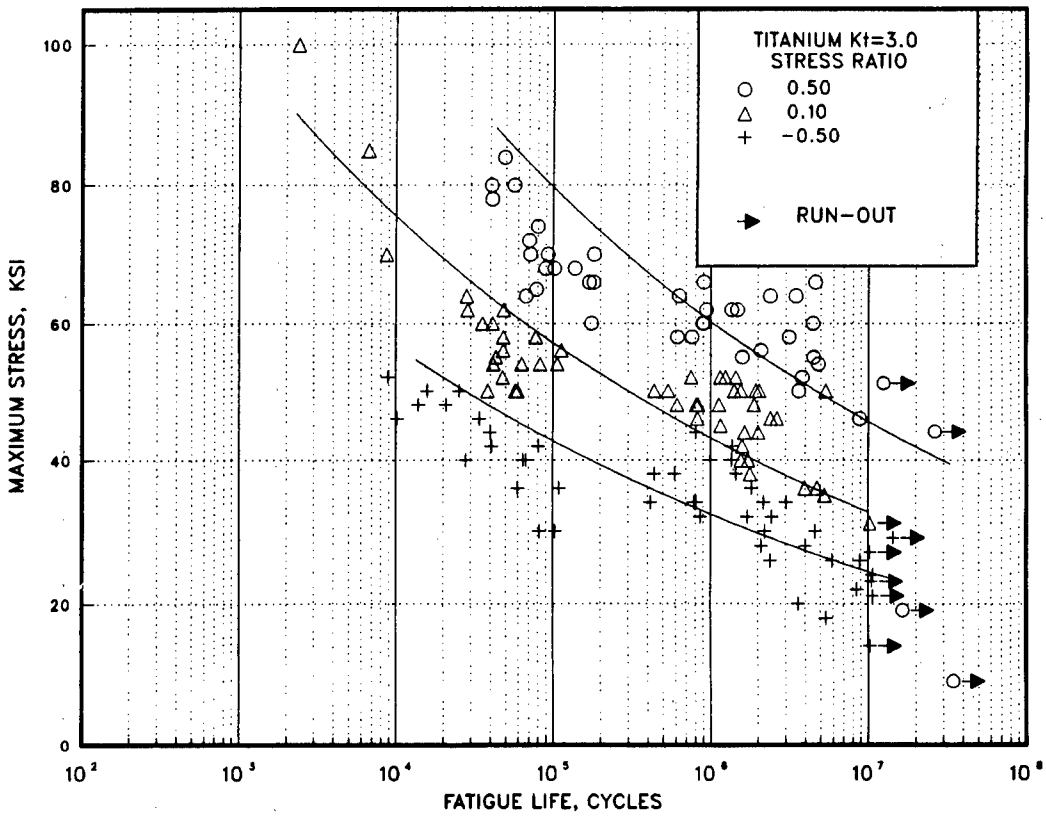


FIGURE 5.4.1.1.8(g). *Best-fit S/N curves for notched, K_t=3.0, Ti-6Al-4V annealed sheet, longitudinal and long transverse direction.*

Correlative Information for Figure 5.4.1.1.8(g)

Product Form: Sheet, 0.063, 0.070, 0.078-inch thick

Properties:

TUS, ksi	TYS, ksi	Temp., F
145-152	136-146	RT

Specimen Details: Notched, K_t = 3.0
0.487-inch net section

Surface Condition: Machined to 32 RMS, lightly polished with 400 grit emery paper

Reference: 5.4.1.1.8(c)

Test Parameters:
Loading - Axial
Frequency - 10-95 Hz
Temperature - RT
Environment - Air

No. of Heats/Lots: 3

Equivalent Strain Equation:
$\text{Log } N_f = 19.28 - 8.25 \log (S_{eq})$
$S_{eq} = S_{max}(1\text{-}R)^{0.57}$
Standard Deviation of Log Life = 0.53
Adjusted R^2 = 62.5%

Sample Size: 141

[Caution: The equivalent strain model may provide unrealistic life predictions for strain ratios and ranges beyond those represented above]

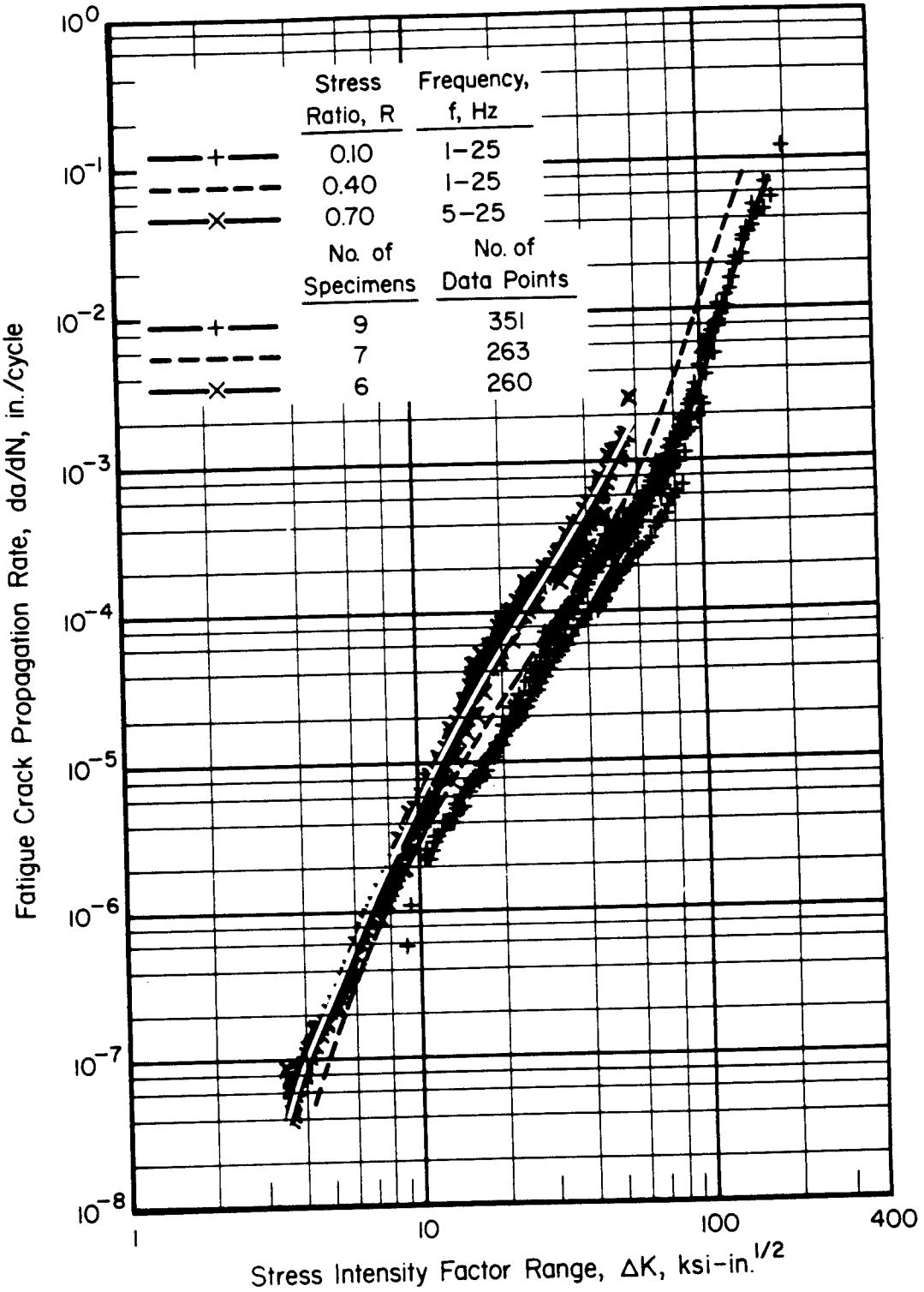


FIGURE 5.4.1.1.9. *Fatigue-crack-propagation data for 0.250 inch thick Ti-6Al-4V mill-annealed titanium alloy plate with buckling restraint. (Reference 5.4.1.1.9.)*

Specimen Thickness:	*0.250 inch*	*Environment:*	*50% R.H.*
Specimen Width:	*9.6, 16, 32 inches*	*Temperature:*	*RT*
Specimen Type:	*CC*	*Orientation:*	*L-T*

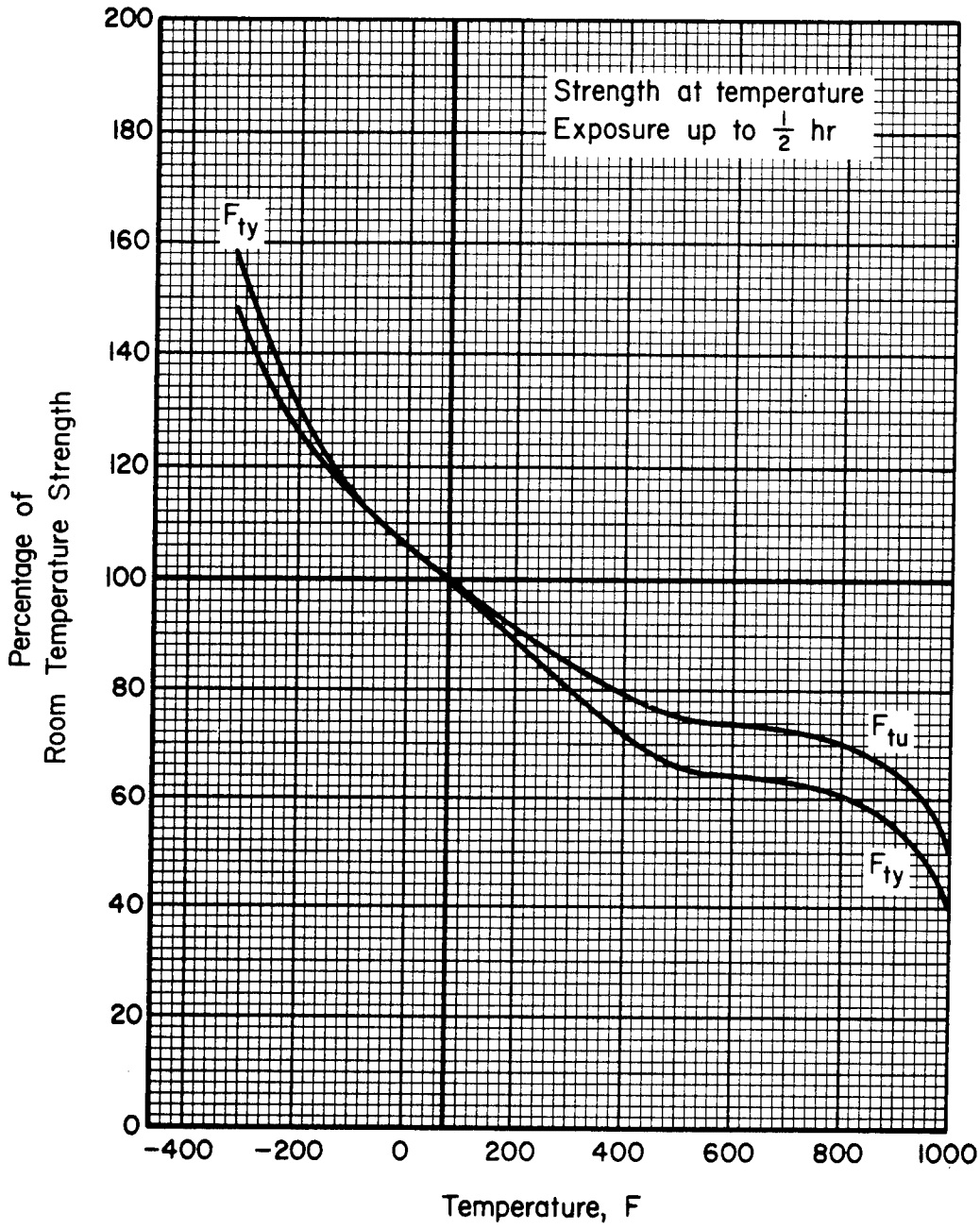


FIGURE 5.4.1.2.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of solution-treated and aged Ti-6Al-4V alloy (all products).*

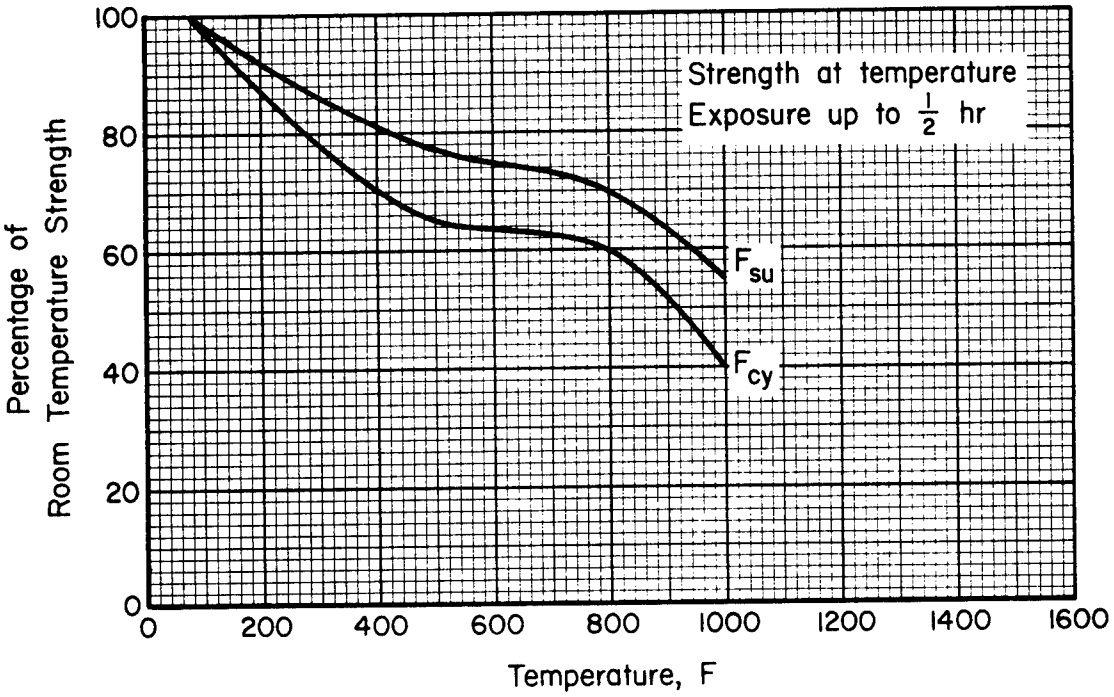


FIGURE 5.4.1.2.2. *Effect of temperature on the compressive yield strength (F_{cy}) and the shear ultimate strength (F_{su}) of solution-treated and aged Ti-6Al-4V alloy (all products).*

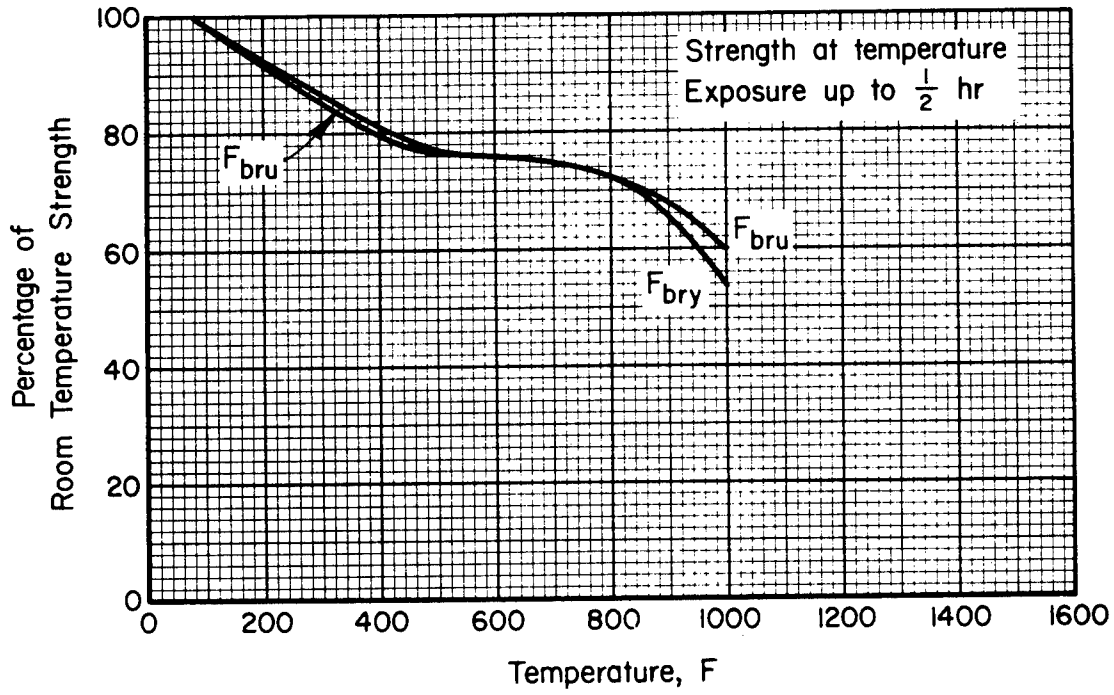


FIGURE 5.4.1.2.3. *Effect of temperature on the bearing ultimate strength (F_{bru}) and the bearing yield strength (F_{bry}) of solution-treated and aged Ti-6Al-4V alloy (all products).*

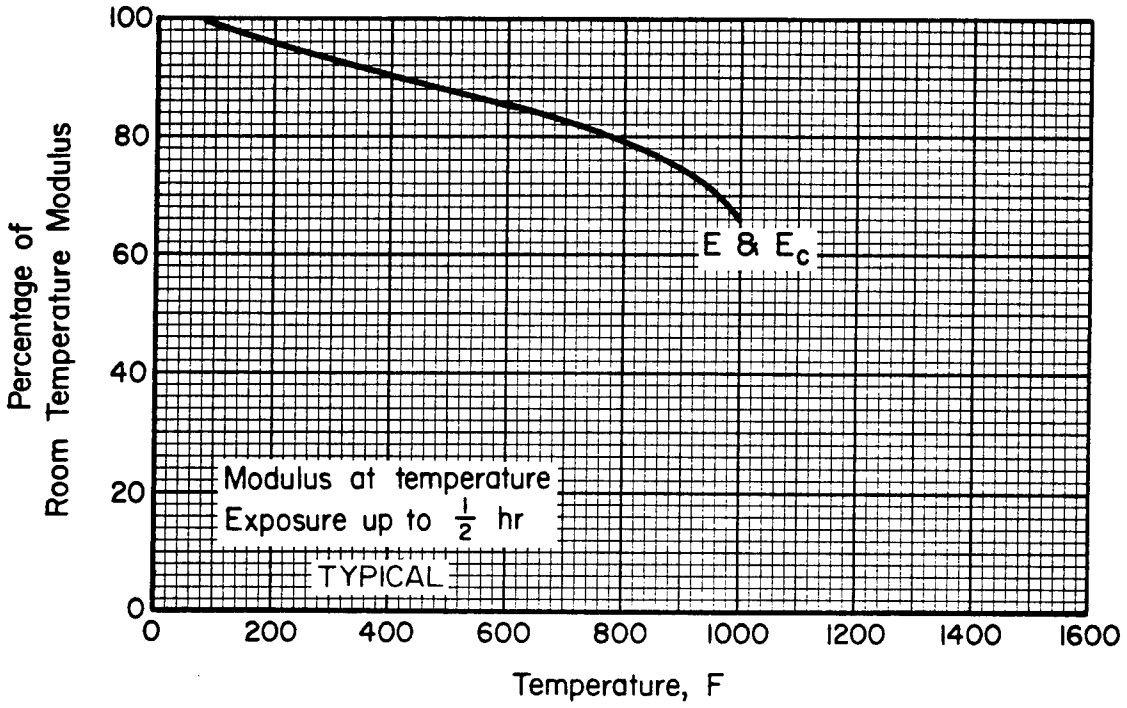


FIGURE 5.4.1.2.4. *Effect of temperature on the tensile and compressive moduli (E and E_c) of solution-treated and aged Ti-6Al-4V alloy.*

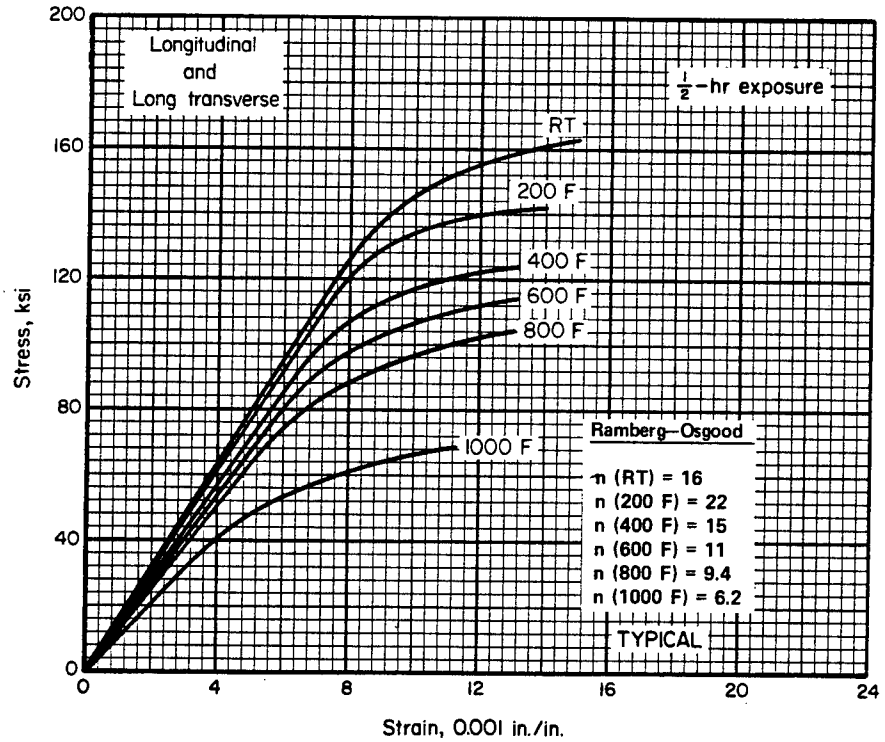


FIGURE 5.4.1.2.6(a). *Typical tensile stress-strain curves for solution-treated and aged Ti-6Al-4V alloy sheet at room and elevated temperatures.*

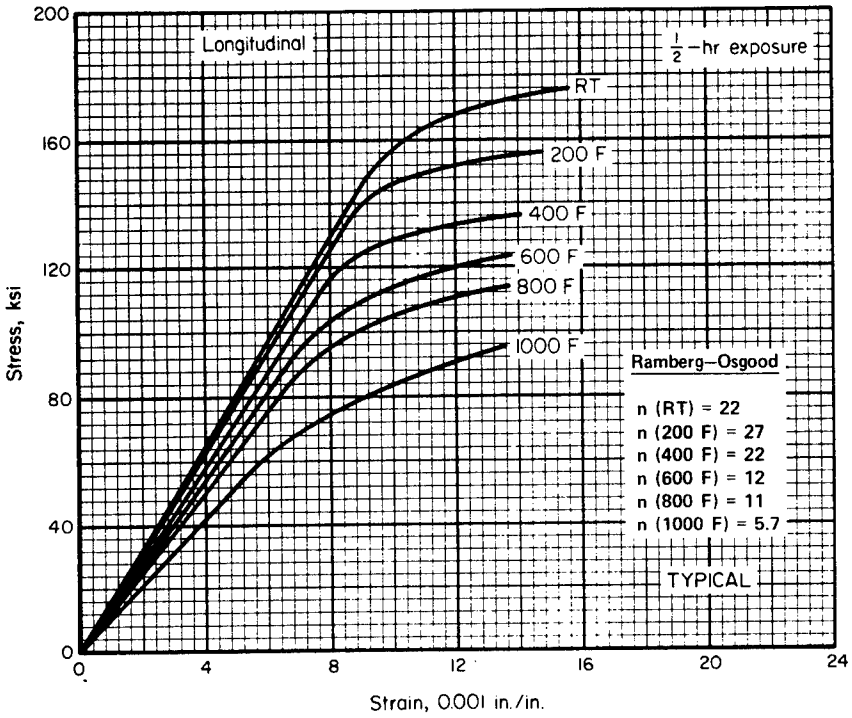


FIGURE 5.4.1.2.6(b). *Typical compressive stress-strain curves for solution-treated and aged Ti-6Al-4V alloy sheet at room and elevated temperatures.*

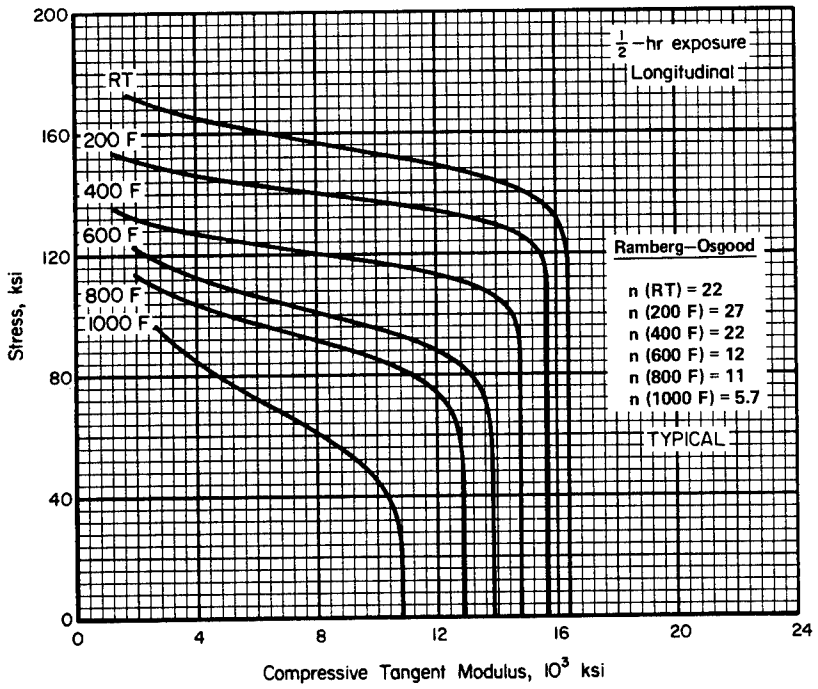


FIGURE 5.4.1.2.6(c). *Typical compressive tangent-modulus curves for solution-treated and aged Ti-6Al-4V alloy sheet at room and elevated temperatures.*

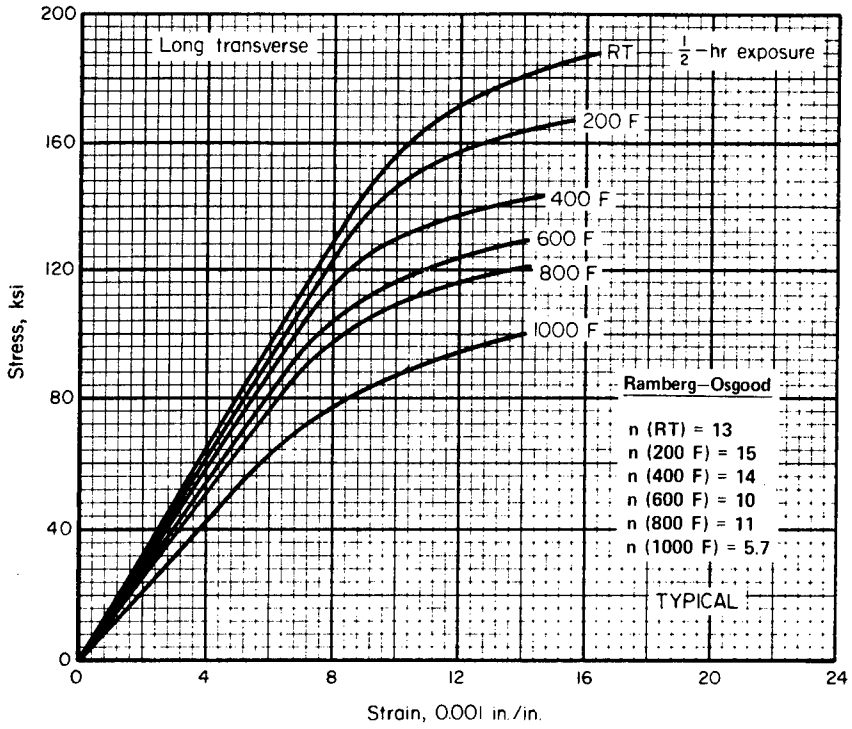


FIGURE 5.4.1.2.6(d). *Typical compressive stress-strain curves for solution-treated and aged Ti-6Al-4V alloy sheet at room and elevated temperatures.*

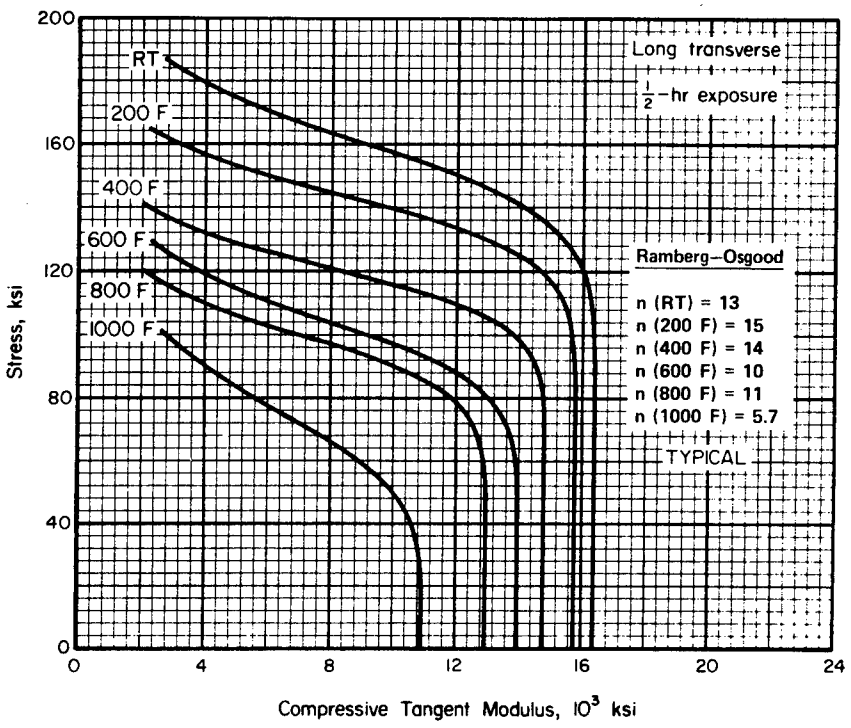


FIGURE 5.4.1.2.6(e). *Typical compressive tangent-modulus curves for solution-treated and aged Ti-6Al-4V alloy sheet at room and elevated temperatures.*

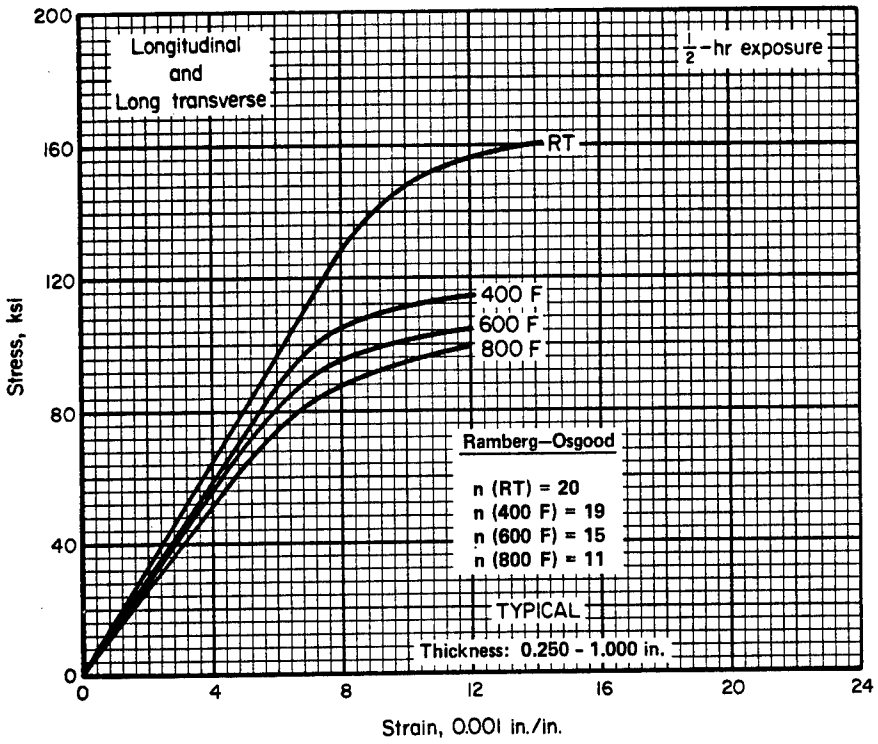


FIGURE 5.4.1.2.6(f). *Typical tensile stress-strain curves for solution-treated and aged Ti-6Al-4V alloy plate at room and elevated temperature.*

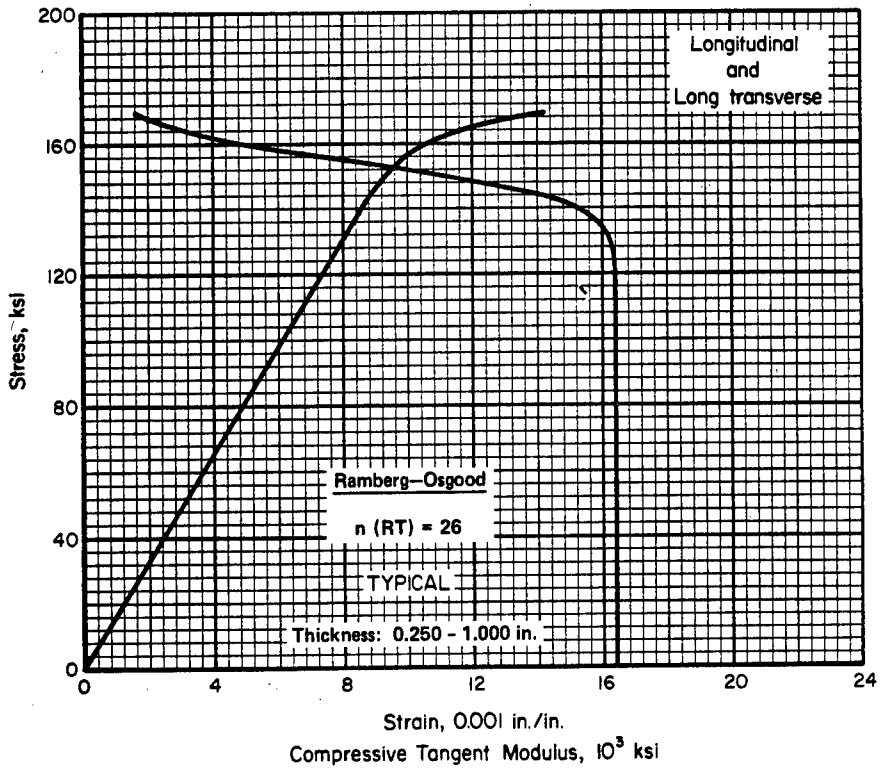


FIGURE 5.4.1.2.6(g). *Typical compressive stress-strain and tangent-modulus curves for solution-treated and aged Ti-6Al-4V alloy plate at room temperature.*

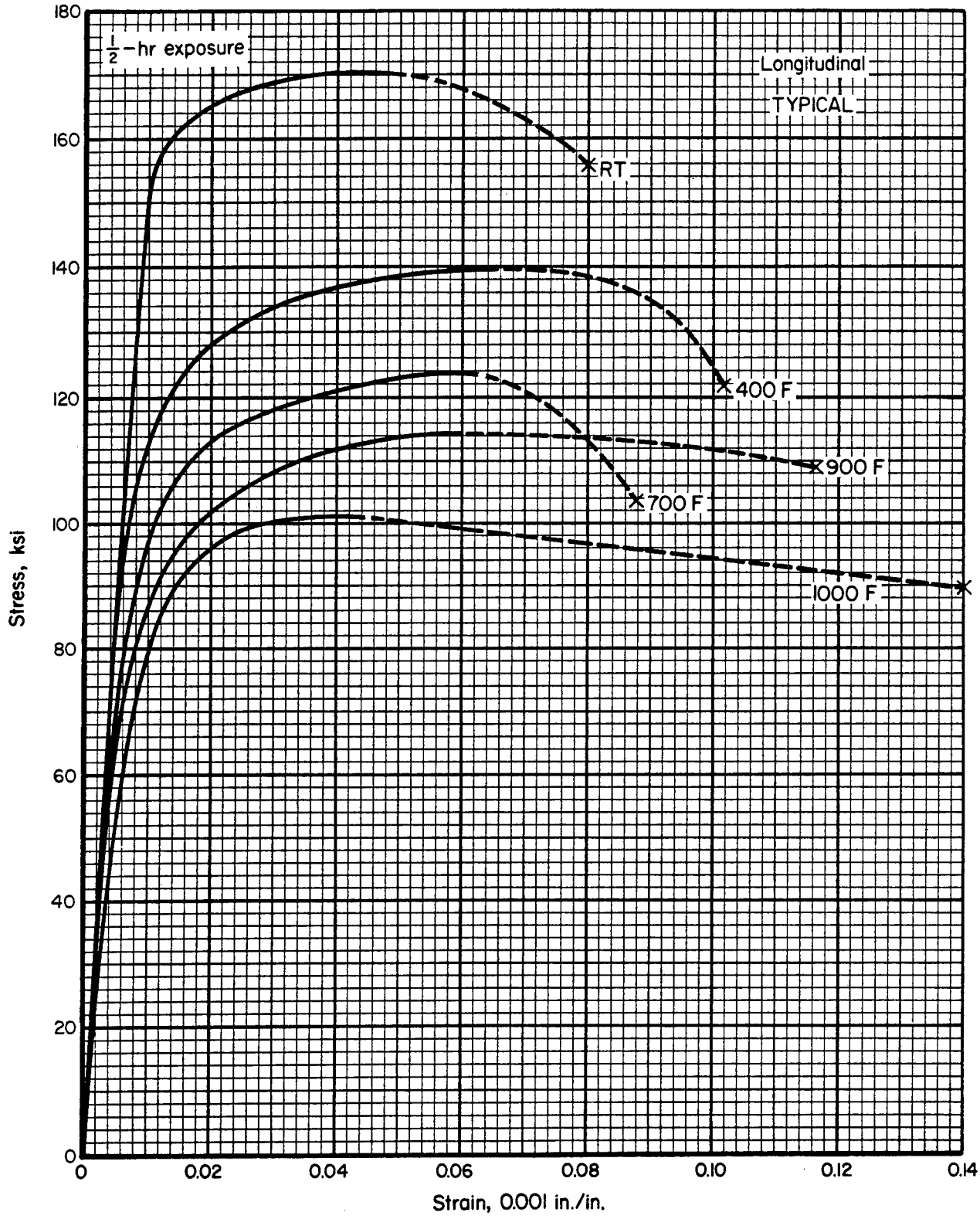


FIGURE 5.4.1.2.6(h). *Typical tensile stress-strain curves (full range) for solution-treated and aged Ti-6Al-4V alloy at room and elevated temperatures.*

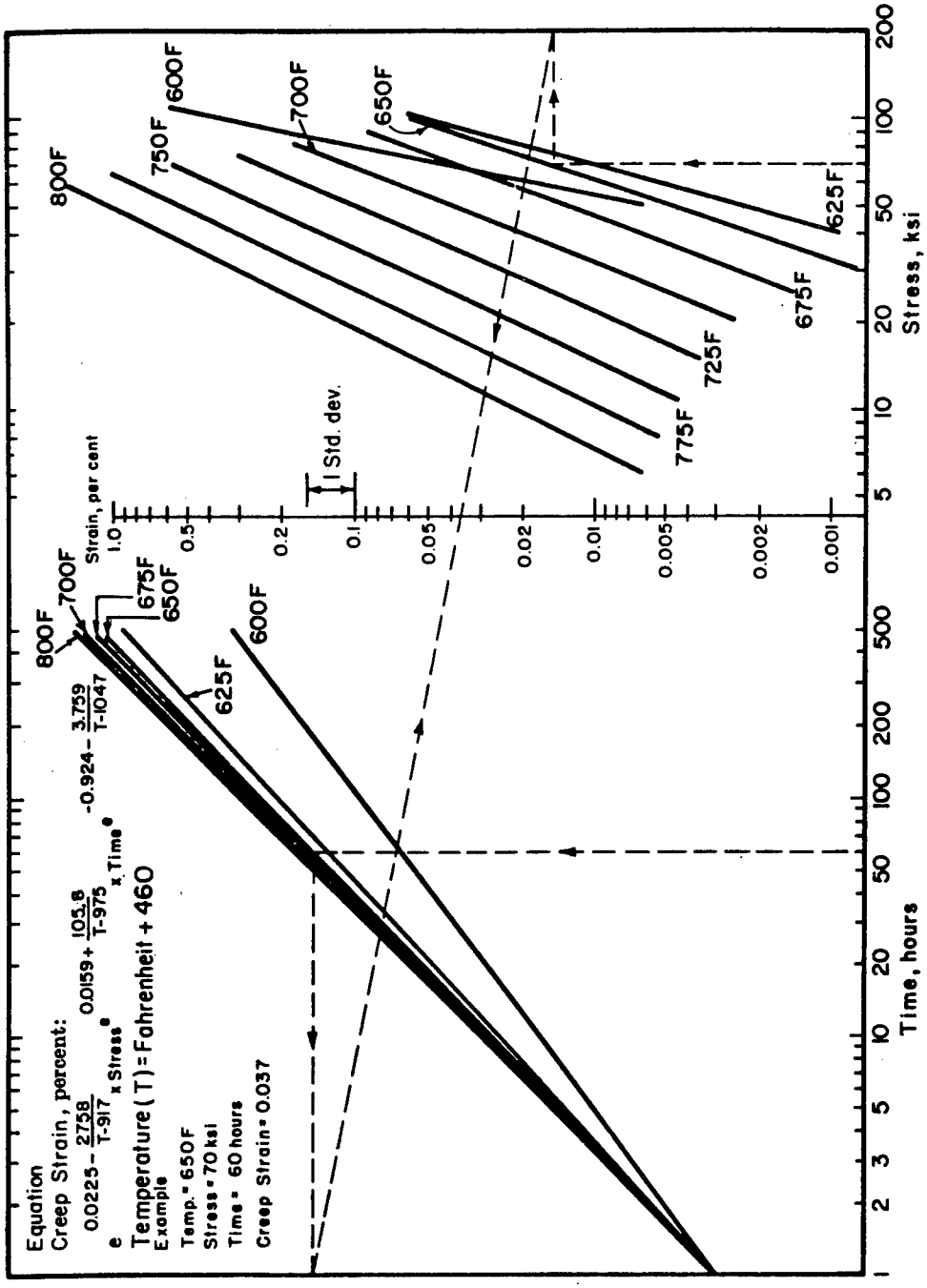


FIGURE 5.4.1.2.7. *Typical creep properties of solution-treated and aged Ti-6Al-4V alloy sheet for temperature range 600 F through 800 F.*

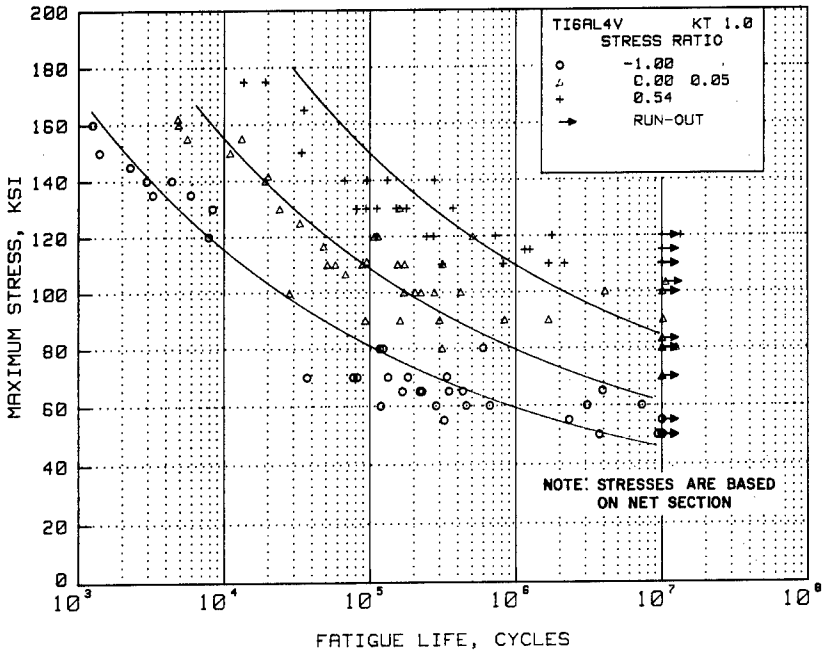


FIGURE 5.4.1.2.8(a). *Best-fit S/N curves for unnotched solution-treated and aged Ti-6Al-4V sheet at room temperature, longitudinal direction.*

Correlative Information for Figure 5.4.1.2.8(a)

Product Forms: Sheet, 0.063-inch and 0.125-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	166–177	153–167	RT

Specimen Details: Unnotched
Ref. 5.4.3.2.8(a)
Specimen details not available
Ref. 5.4.3.2.8(b)
1.000-inch net width
8.000-inch test section radius
3.00-inch gross width

Surface Condition:

Ref. 5.4.3.2.8(a). Edges finished with a crocus cloth
Ref. 5.4.3.2.8(b). Machined specimens were cleaned with methyl ethyl ketone. Edges polished with number 1 and 00 grit emery paper, recleaned with methyl ethyl ketone.

References: 5.4.1.2.8(a),(b)

Test Parameters:

Loading — Axial
Frequency —
Ref. 5.4.3.2.8(a), not specified
Ref. 5.4.3.2.8(b), 1500–2200 cpm
Temperature — RT
Environment — Air

No. of Heats/Lots: 4

Equivalent Stress Equation:

$\text{Log } N_f = 14.29 - 4.91 \log (S_{eq} - 30.6)$
$S_{eq} = S_{max}(1-R)^{0.42}$
Standard Error of Estimate = 0.48
Standard Deviation in Life = 0.90
$R^2 = 72\%$

Sample Size = 99

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

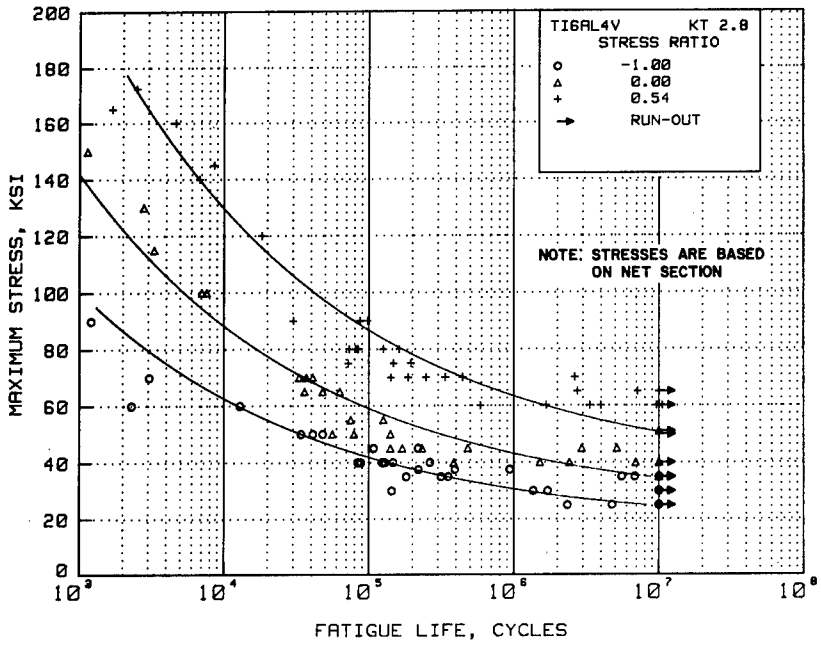


FIGURE 5.4.1.2.8(b). *Best-fit S/N curves for notched, K_t = 2.8, solution-treated and aged Ti-6Al-4V sheet at room temperature, longitudinal direction.*

Correlative Information for Figure 5.4.1.2.8(b)

Product Form: Sheet, 0.063-inch and 0.125-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	166–177	153–167	RT

Specimen Details: Notched, hole type, K_t = 2.8
0.9375-inch net width
1.000-inch gross width
8.000-inch test section radius
0.0625-inch-diameter hole

Surface Conditions: Machined specimens were cleaned with methyl ethyl ketone. Edges polished with number 1 and 00 grit emery paper and recleaned with methyl ethyl ketone.

Reference: 5.4.1.2.8(b)

Test Parameters:

Loading — Axial
Frequency — 1500–2200 cpm
Temperature — RT
Environment — Air

No. of Heats/Lots: 3

Equivalent Stress Equation:

$\text{Log } N_f = 10.87 - 3.80 \log (S_{eq} - 24.0)$
$S_{eq} = S_{max}(1-R)^{0.50}$
Standard Error of Estimate = 0.43
Standard Deviation in Life = 0.98
R^2 = 81%

Sample Size = 87

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

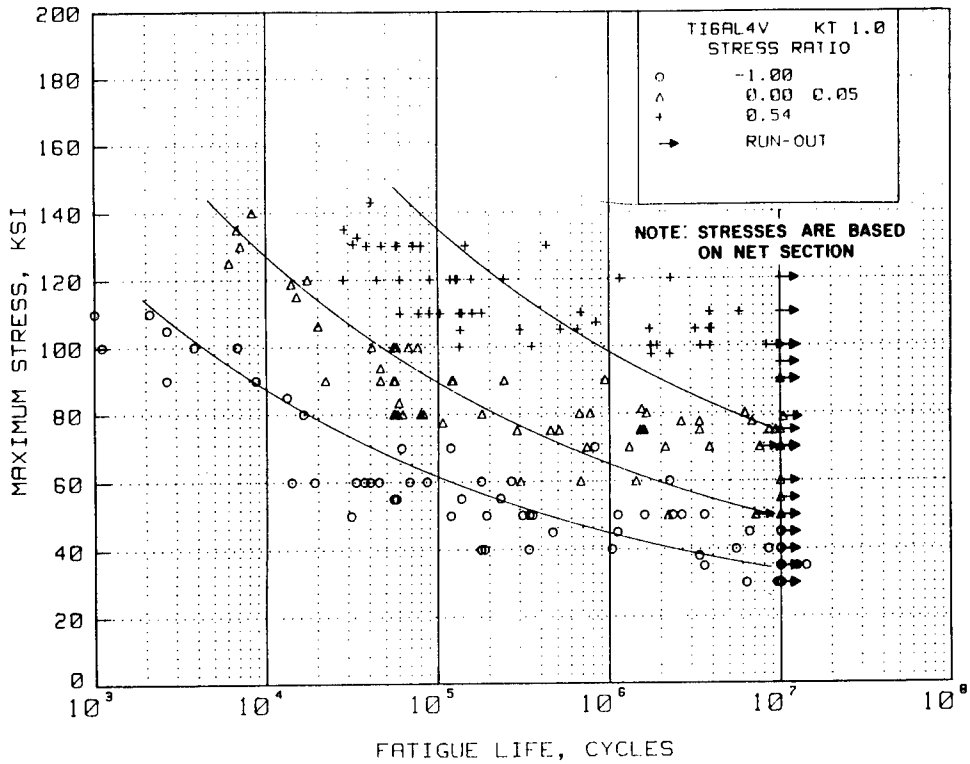


FIGURE 5.4.1.2.8(c). *Best-fit S/N curves for unnotched solution-treated and aged Ti-6Al-4V sheet at 400 F and 600 F, longitudinal direction.*

Correlative Information for Figure 5.4.1.2.8(c)

Product Forms: Sheet, 0.063-inch and 0.125-inch thick

Properties:

TUS, ksi	TYS, ksi	Temp., F
142-143	117-121	400 F
125-134	102-113	600 F

Specimen Details: Unnotched
Ref. 5.4.3.2.8(a)
Specimen details not available
Ref. 5.4.3.2.8(b)
1.000-inch gross width
8.000-inch test section radius
3.00-inch gross width
0.9375-inch net width

Surface Condition:
Ref. 5.4.3.2.8(a). Edges finished with a crocus cloth
Ref. 5.4.3.2.8(b). Machined specimens were cleaned with methyl ethyl ketone. Edges polished with number 1 and 00 grit emery paper, recleaned with methyl ethyl ketone.

References: 5.4.1.2.8(a) and (b)

Test Parameters:
Loading - Axial
Frequency -
Ref. 5.4.3.2.8(a), not specified
Ref. 5.4.3.2.8(b), 1500-2200 cpm
Temperature - 400 F and 600 F
Environment - Air

No. of Heats/Lots: 4

Equivalent Stress Equation:
$\text{Log } N_f = 14.7 - 5.31 \log (S_{eq} - 21.8)$
$S_{eq} = S_{max}(1\text{-}R)^{0.54}$
Standard Error of Estimate = 0.58
Standard Deviation in Life = 0.93
$R^2 = 61\%$

Sample Size: 163

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

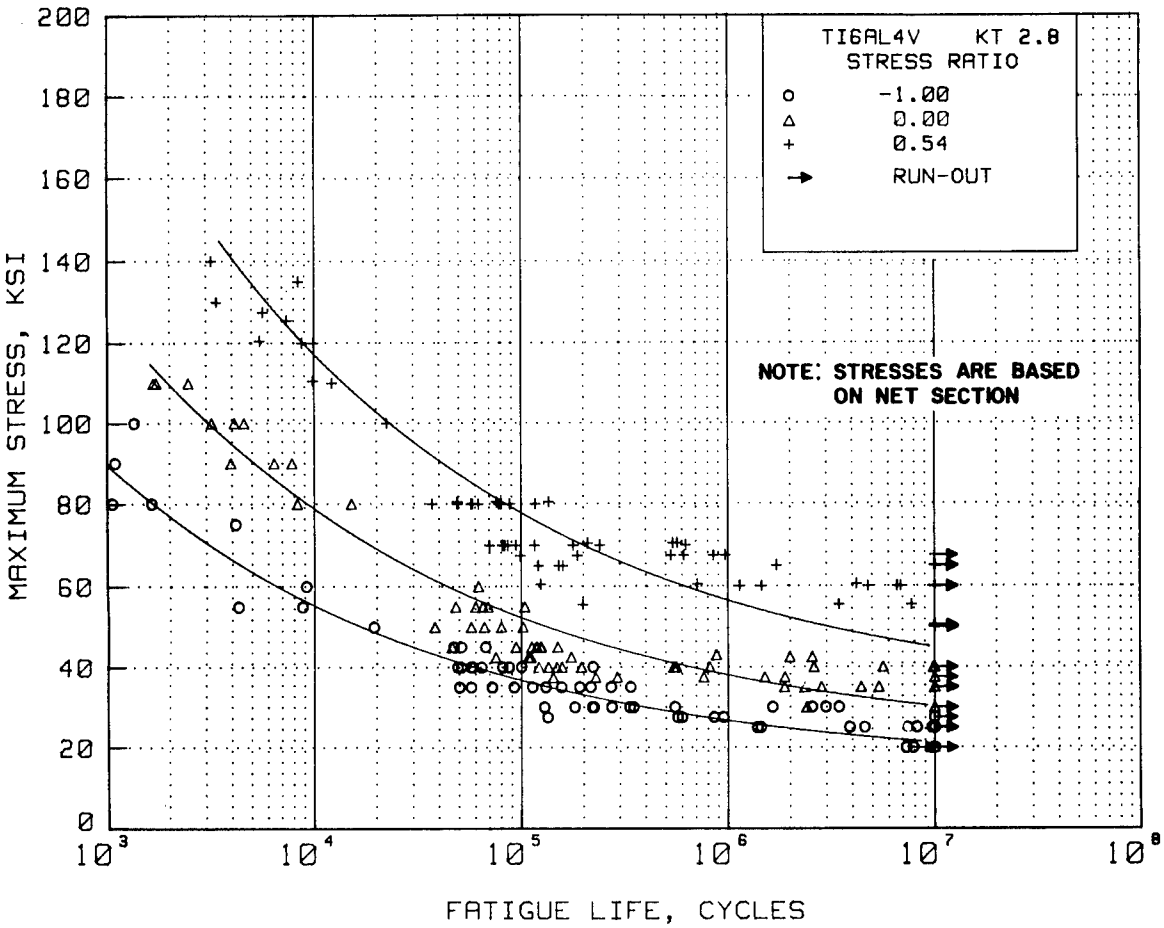


FIGURE 5.4.1.2.8(d). *Best-fit S/N curves for notched, K_t = 2.8, solution-treated and aged Ti-6Al-4V sheet at 400 F and 600 F, longitudinal direction.*

Correlative Information for Figure 5.4.1.2.8(d)

Product Forms: Sheet, 0.063-inch and 0.125-inch thick

Properties:

TUS, ksi	TYS, ksi	Temp., F
142-143	117-121	400 F
129-133	103-105	600 F

Specimen Details: Notched, hole type, K_t = 2.8
1.000-inch gross width
8.000-inch test section radius
0.0625-inch-diameter hole
0.9375-inch net width

Surface Condition: Machined specimens were cleaned with methyl ethyl ketone. Edges polished with number 1 and 00 grit emery paper and recleaned with methyl ethyl ketone.

Reference: 5.4.1.2.8(b)

Test Parameters:
Loading - Axial
Frequency - 1500-2200 cpm
Temperature - 400 F and 600 F
Environment - Air

No. of Heats/Lots: 3

Equivalent Stress Equation:
$\text{Log } N_f = 10.64 - 3.77 \log (S_{eq} - 20.9)$
$S_{eq} = S_{max}(1\text{-}R)^{0.51}$
Standard Error of Estimate = 0.42
Standard Deviation in Life = 0.93
R^2 = 80%

Sample Size: 175

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

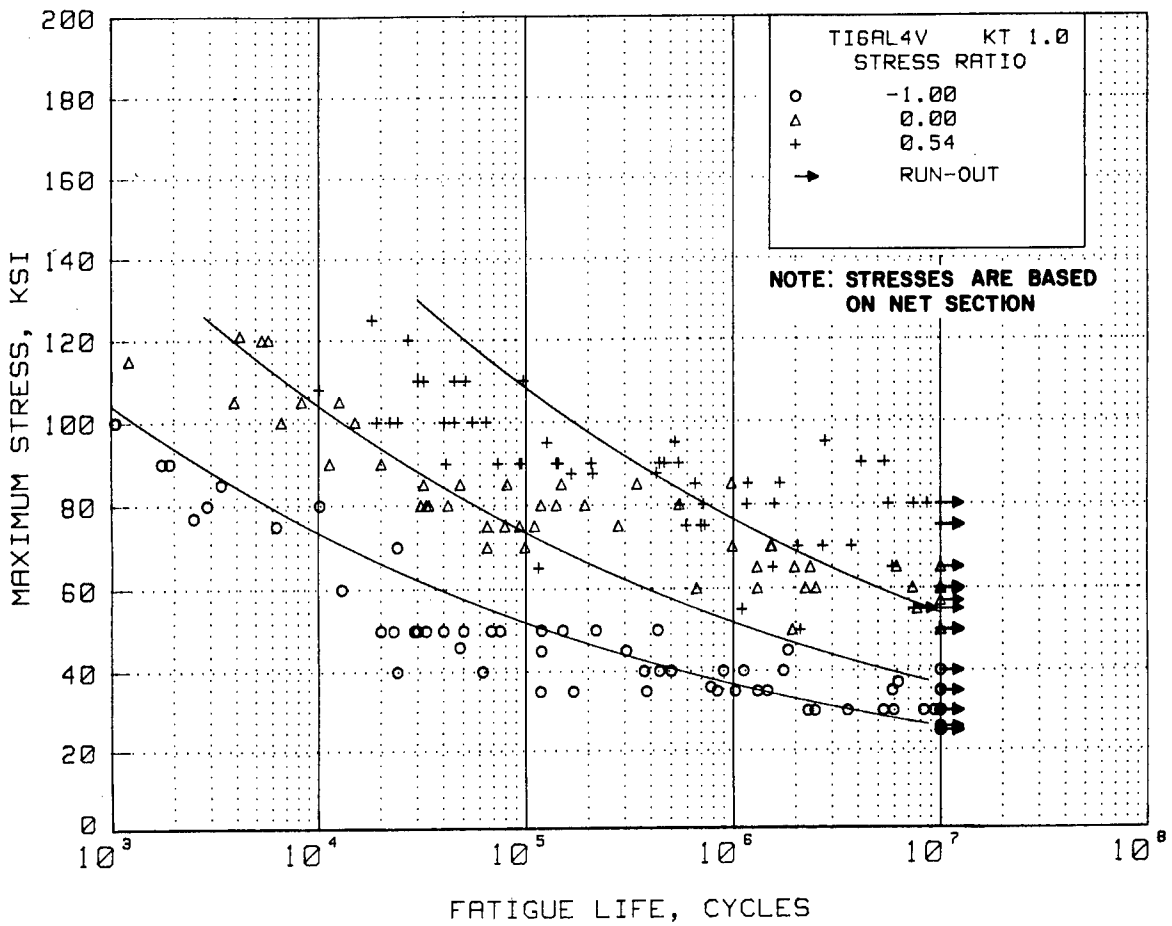


FIGURE 5.4.1.2.8(e). *Best-fit S/N curves for unnotched solution-treated and aged Ti-6Al-4V sheet at 800 F and 900 F, longitudinal direction.*

Correlative Information for Figure 5.4.1.2.8(e)

Product Forms: Sheet, 0.063-inch and 0.125-inch thick

Properties:

TUS, ksi	TYS, ksi	Temp., F
120-125	93-96	800 F
110-111	84-86	900 F

Specimen Details: Unnotched
1.000-inch gross width
8.000-inch test section radius
3.00-inch gross width
0.9375-inch net width

Surface Condition: Machined specimens were cleaned with methyl ethyl ketone. Edges polished with number 1 and 00 grit emery paper and recleaned with methyl ethyl ketone.

Reference: 5.4.1.2.8(b)

Test Parameters:
Loading - Axial
Frequency - 1500-2200 cpm
Temperature - 800 F and 900 F
Environment - Air

No. of Heats/Lots: 3

Equivalent Stress Equation:
$\text{Log } N_f = 17.34 - 6.61 \log (S_{eq})$
$S_{eq} = S_{max}(1-R)^{0.50}$
Standard Error of Estimate = 0.58
Standard Deviation in Life = 0.99
$R^2 = 73\%$

Sample Size: 154

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

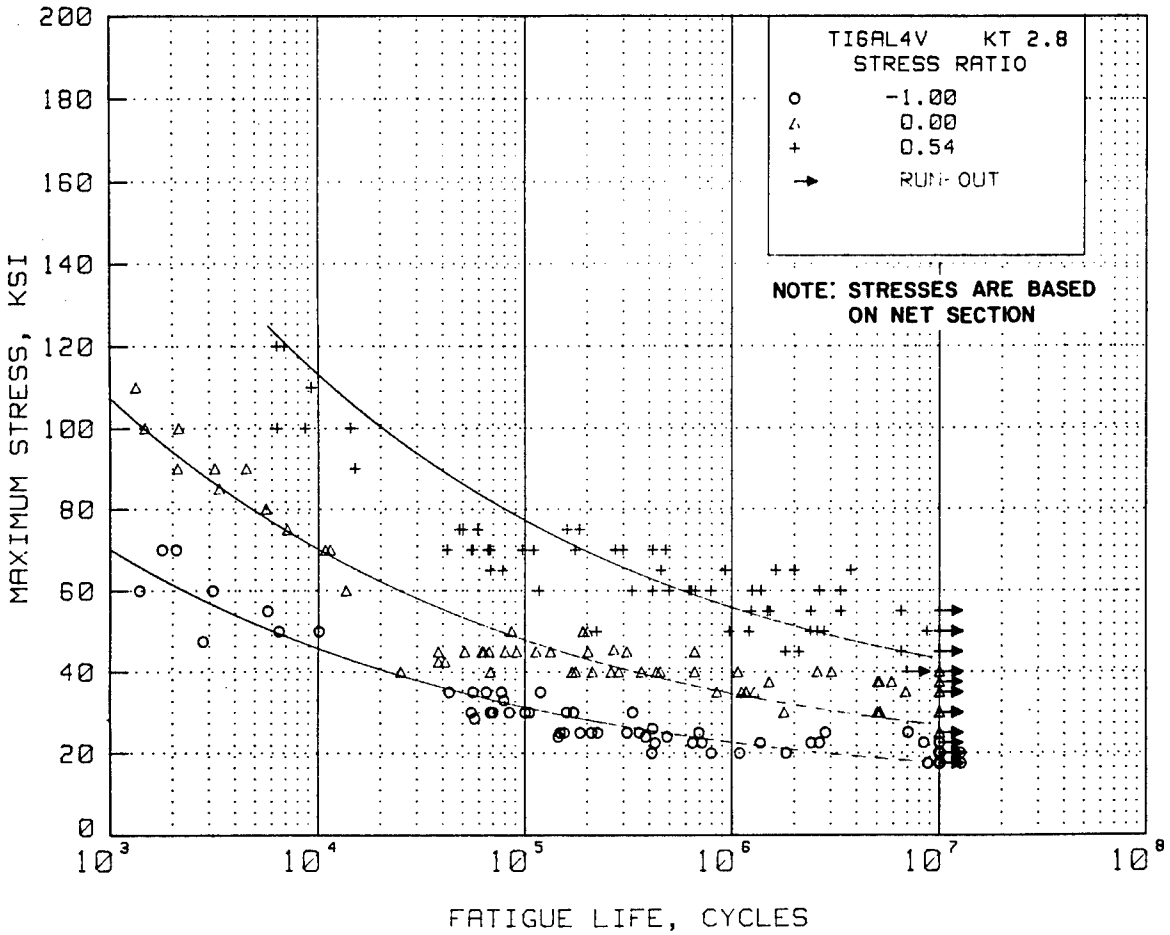


FIGURE 5.4.1.2.8(f). *Best-fit S/N curves for notched, $K_t = 2.8$, solution-treated and aged Ti-6Al-4V sheet at 800 F and 900 F, longitudinal direction.*

Correlative Information for Figure 5.4.1.2.8(f)

Product Forms: Sheet, 0.063-inch and 0.125-inch thick

Properties:

TUS, ksi	TYS, ksi	Temp., F
120-124	93-96	800 F
110-111	84-88	900 F

Specimen Details: Notched, hole type, $K_t = 2.8$
1.000-inch gross width
8.000-inch test section radius
0.0625-inch-diameter hole
0.9375-inch net width

Surface Condition: Machined specimens were cleaned with methyl ethyl ketone. Edges polished with number 1 and 00 grit emery paper and recleaned with methyl ethyl ketone.

Reference: 5.4.1.2.8(b)

Test Parameters:
Loading - Axial
Frequency - 1500-2200 cpm
Temperature - 800 F and 900 F
Environment - Air

No. of Heats/Lots: 3

Equivalent Stress Equation:
$\text{Log } N_f = 11.75 - 4.45 \log (S_{eq} - 15.0)$
$S_{eq} = S_{max}(1\text{-}R)^{0.62}$
Standard Error of Estimate = 0.43
Standard Deviation in Life = 0.96
$R^2 = 79\%$

Sample Size: 173

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

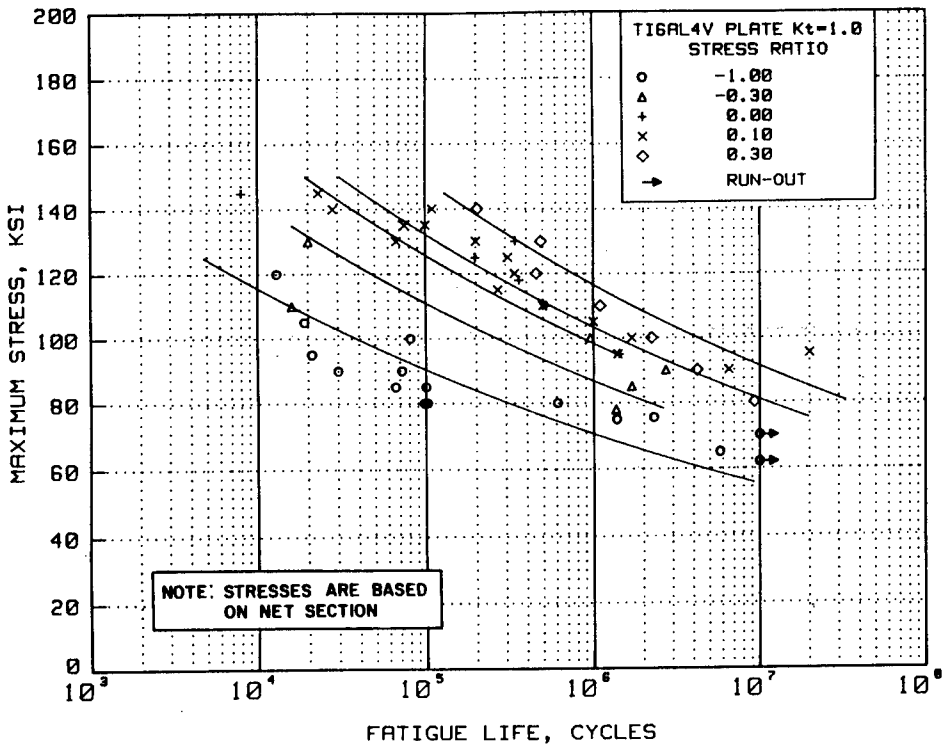


FIGURE 5.4.1.2.8(g). *Best-fit S/N curves for unnotched, solution-treated and aged Ti-6Al-4V plate at room temperature, longitudinal direction.*

Correlative Information for Figure 5.4.1.2.8(g)

Product Form: Plate, 1.00-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	158	149	RT
	155	145	RT

Specimen Details: Unnotched, round

Uniform Gage	Hourglass	
———	3.25	Reduced section radius of curvature, inch
0.195	0.250	Diameter, inch

Surface Condition: Longitudinally polished with No. 000 emery paper removing all circumferential marks.

Reference: 5.4.1.2.8(c) and (d)

Test Parameters:

Loading - Axial
Frequency - 1,800 to 18,000 cpm
Temperature - RT
Environment - air

No. of Heats/Lots: 2

Equivalent Stress Equation:

$\text{Log } N_f = 24.6\text{-}9.35 \log (S_{eq})$
$S_{eq} = S_{max} (1\text{-}R)^{0.48}$
Standard Error of Estimate =0.39
Standard Deviation in Life = 0.83
$R^2 = 79\%$

Sample Size = 49

[Caution: the equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

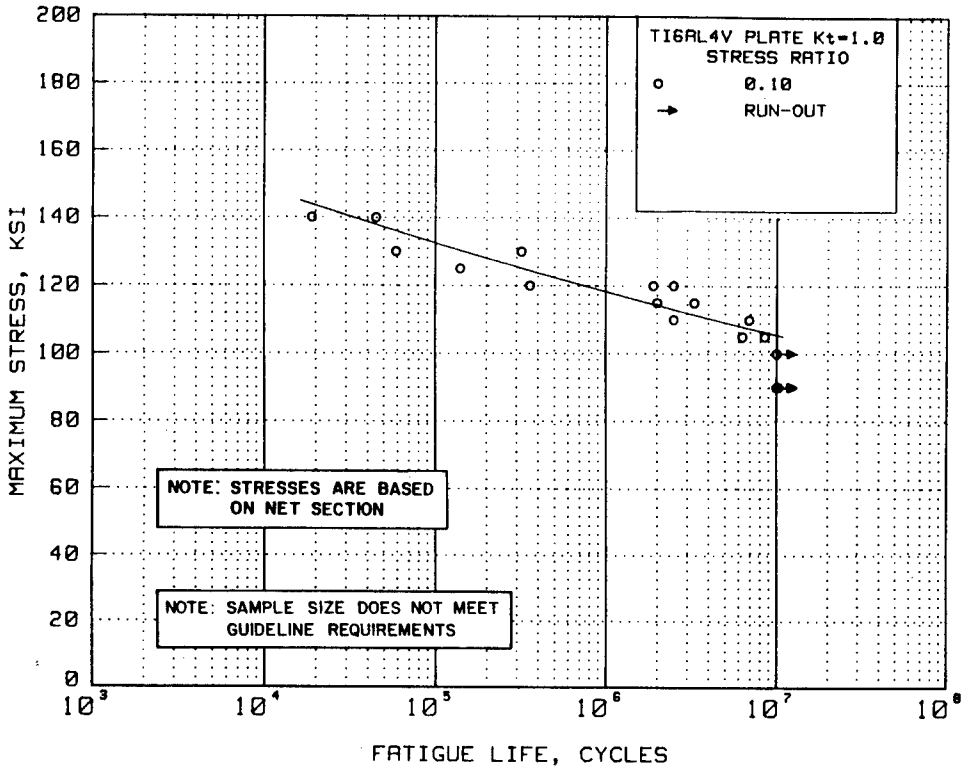


FIGURE 5.4.1.2.8(h). *Best-fit S/N curves for unnotched, solution-treated and aged Ti-6Al-4V plate at room temperature, long transverse direction.*

Correlative Information for Figure 5.4.1.2.8(h)

Product Form: Plate, 0.50-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	173	164	RT

Specimen Details: Unnotched, flat hourglass
10-inch reduced section radius of curvature
1-inch net section width
0.156-inch net section thickness

Surface Condition: Machined to 63 RMS

Reference: 5.4.1.2.8(d)

Test Parameters:

Loading - Axial
Frequency - unspecified
Temperature - RT
Environment - air

No. of Heats/Lots: 1

Equivalent Stress Equation:

Log N_f = 47.9-20.2 log (S_{max})
Standard Error of Estimate =0.33
Standard Deviation in Life = 0.89
R^2 = 87%

Sample Size = 14

[Caution: the equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

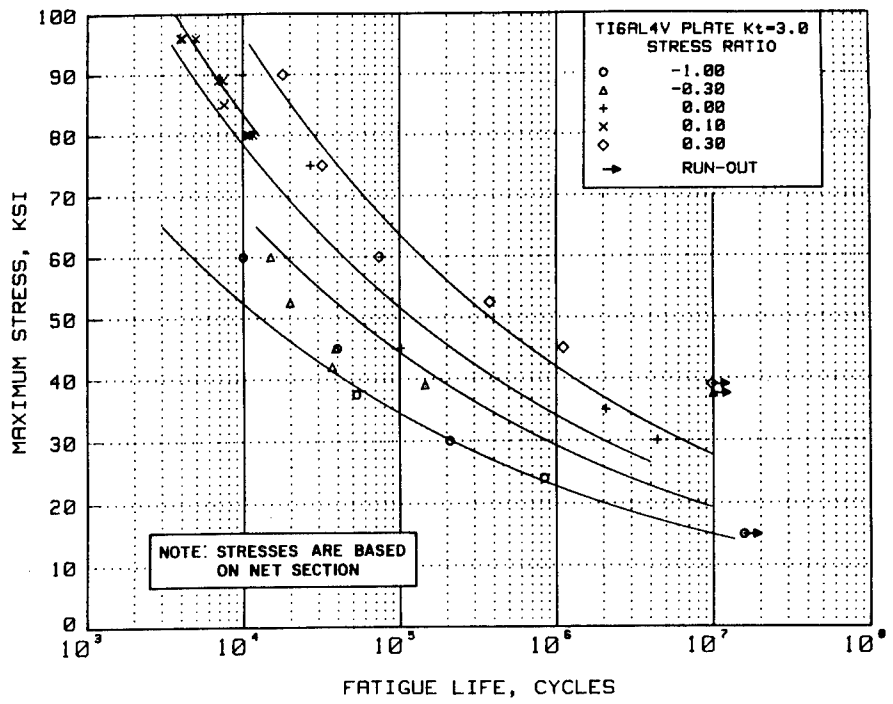


FIGURE 5.4.1.2.8(i). *Best-fit S/N curves for notched, K_t = 3.0, solution-treated and aged Ti-6Al-4V plate at room temperature, longitudinal direction.*

Correlative Information for Figure 5.4.1.2.8(i)

Product Form: Plate, 1.025 and 0.750-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	155	145	RT (unnotched)
	187	———	RT (notched)

Specimen Details: Circumferentially notched, K_t = 3.0

Ref (c)	Ref (e)	
0.195	0.430	Gross diameter, inch
0.136	0.300	Net section, inch
0.005	0.016	Notch radius, r, inch
60°	60°	Flank angle, ω

Surface Condition:

Ref. (c) notch made with light finishing cuts
Ref. (e) notch polished in lathe

Reference: 5.4.1.2.8(c) and (e)

Test Parameters:

Loading - Axial
Frequency - 1,800 to 18,000 cpm
Temperature - RT
Environment - air

No. of Heats/Lots: 2

Equivalent Stress Equation:

$\text{Log } N_f = 14.4\text{-}5.51 \log (S_{eq})$
$S_{eq} = S_{max} (1\text{-}R)^{0.58}$
Standard Error of Estimate =0.24
Standard Deviation in Life = 0.81
R^2 = 92%

Sample Size = 31

[Caution: the equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

5.4.2 Ti-6Al-6V-2Sn

5.4.2.0 *Comments and Properties.*—Ti-6Al-6V-2Sn alloy is similar to Ti-6Al-4V alloy in many respects but has higher strength and deeper hardenability (i.e., use of thicker sections possible). A variety of mill product forms are available including billet, bar, plate, sheet, strip, and extrusions and these may be used in either the annealed or the solution-treated and aged (STA) conditions. The maximum strength is developed in the STA condition in sections up to about 2 inches in thickness.

Manufacturing Considerations.—To insure optimum mechanical properties in Ti-6Al-6V-2Sn forgings, at least 50 percent reduction should be done at temperatures below the beta transus temperature (i.e., <1735 F). The Ti-6Al-6V-2Sn is readily formable in the annealed condition. In the sheet or plate forms the alloy is generally used in the annealed condition, although the alloy is capable of heat treatment to higher strength levels with some loss of toughness. When the Ti-6Al-6V-2Sn sheet and plate are hot formed at any temperature over 1000 F and air cooled, the material should be stabilized by reheating to 1000 F followed by air cooling. Welding is not usually recommended although limited weld joining operations are possible if the assembly is amenable to post-weld thermal treatments for the restoration of ductility to the weld and heat-affected zones.

Environmental Considerations.—While the short-time elevated-temperature properties and stability of Ti-6Al-6V-2Sn alloy are good, creep strength above 650 F and long-term stability at temperatures above 800 F are not. The material ages during prolonged exposures around 800 F and above, particularly when under stress. Oxidation resistance of Ti-6Al-6V-2Sn is satisfactory in short-term exposures to 1000 F. The material is nearly equivalent to the Ti-6Al-4V alloy in terms of hot-salt and aqueous chloride solution stress-corrosion resistance. Under certain conditions, titanium, when in contact with cadmium, silver, mercury, or certain of their compounds, may become embrittled. Refer to MIL-S-5002 and MIL-STD-1568 for restrictions concerning applications with titanium in contact with these metals or their compounds.

Heat Treatment.—This alloy is commonly specified in either the annealed condition or the solution-treated and aged condition. The solution-treated and aged condition is as follows:

Solution treat at 1625 F for ½ to 1 hour, quench in water.

Age at 1000 ± 25 F for 4 to 8 hours, air cool.

Specifications and Properties.—Material specifications for Ti-6Al-6V-2Sn are shown in Table 5.4.2.0(a). Room-temperature mechanical properties are shown in Tables 5.4.2.0(b) through (e). The effect of temperature on physical properties is shown in Figure 5.4.2.0.

TABLE 5.4.2.0(a). *Material Specifications for Ti-6Al-6V-2Sn*

Specifications	Form
MIL-T-9046	Sheet, strip, and plate
AMS 4979	Bar and forging
MIL-T-81556	Extruded bar and shapes
AMS 4971	Bar and forging
AMS 4978	Bar and forging
AMS 4918	Sheet, strip, and plate

5.4.2.1 *Annealed Condition.*—Elevated temperature curves for annealed condition are shown in Figures 5.4.2.1.1(a) through 5.4.2.1.3(b). Typical stress-strain and tangent-modulus curves for this condition are shown in Figures 5.4.2.1.6(a) and (b). A typical full range tensile stress-strain curve is shown in Figure 5.4.2.1.6(c). Unnotched and notched fatigue data are presented in Figures 5.4.2.1.8(a) and (b).

5.4.2.2 *Solution-Treated and Aged Condition.*—Elevated temperature curves are shown in Figures 5.4.2.2.1 and 5.4.2.2.2.

TABLE 5.4.2.0(b). *Design Mechanical and Physical Properties of Ti-6Al-6V-2Sn Sheet, Strip, and Plate*

Specification	MIL-T-9046, Comp. AB-3, and AMS 4918							MIL-T-9046, Comp. AB-3			
Form	Sheet, strip, and plate										
Condition	Annealed							Solution treated and aged			
Thickness, in.	<0.1875		0.1875-0.500	0.501-1.000	1.001-1.500	1.501-2.000	2.001-4.000	≤0.1875	0.1875-1.500	1.501-2.500	2.501-4.000
Basis	A	B	S	S	S	S	S	S	S	S	S
Mechanical Properties:											
F_{tu}, ksi:											
L	155	160	150	150	150	150	145	170	170	160	150
LT	155	150	150	150	150	150	145	170	170	160	150
F_{ty}, ksi:											
L	145[a]	152	140	140	140	140	135	160	160	150	140
LT	145[a]	154	140	140	140	140	135	160	160	150	140
F_{cy}, ksi:											
L	...	...	139	142	146	148	...	...	170	...	...
LT	...	...	151	147	141	136	...	...	170	...	...
F_{su}, ksi	...	...	91	93	95	95	...	...	101	...	...
F_{bru}, ksi:											
(e/D = 1.5)	...	...	236	241	247	250	...	...	264	...	...
(e/D = 2.0)	...	...	294	303	312	317	...	...	324	...	...
F_{bry}, ksi:											
(e/D = 1.5)	...	...	193	196	199	202	...	...	237	...	...
(e/D = 2.0)	...	...	215	223	234	240	...	...	266	...	...
e, percent (S-basis):											
L	10[b]	...	10	10	10	10	8	8	8	6	6
LT	8[b]	...	8	8	8	8	6	6	8	6	6
E, 10^3 ksi	16.0										
E_c, 10^3 ksi	16.4										
G, 10^3 ksi	6.2										
μ	0.31										
Physical Properties:											
ω, lb/in.^{3}	0.164										
C, K, and α	See Figure 5.4.2.0										

[a]The A values are higher than specification values as follows: F_{ty} (L) = 147 ksi, F_{ty} (LT) = 149 ksi.

[b]Longitudinal <0.025 in. = 8 percent. Long transverse < 0.025 in. = 6 percent.

TABLE 5.4.2.0(c). *Design Mechanical and Physical Properties of Ti-6Al-6V-2Sn Bar*

Specification	AMS 4978						AMS 4971 and AMS 4979			
Form	Bar						Bar and forging			
Condition	Air-cool annealed[a]						Solution treated and aged			
Thickness or diameter, in.	≤1.500		1.501-3.000		3.001-4.000		≤1.000	1.001-2.000	2.001-3.000	3.001-4.000
Basis	A	B	A	B	A	B	S	S	S	S
Mechanical Properties:										
F_{tu}, ksi:										
L	144	150	139	145	136	142	175	170	155	150
LT[b]	147	152	143	148	140	145	175	170	155	150
ST[b]	...	...	...	...	...	...	...	...	155	150
F_{ty}, ksi:										
L	131	138	126	132	123	129	160	155	145	140
LT[b]	136	141	131	136	127	132	160	155	145	140
ST[b]	...	...	...	...	...	...	...	...	145	140
F_{cy}, ksi:										
L	...	...	...	...	...	...	...	...	...	...
LT[b]	...	...	...	...	...	...	...	...	...	...
ST[b]	...	...	...	...	...	...	...	...	...	...
F_{su}, ksi	...	...	...	...	...	...	...	...	...	...
F_{bru}, ksi:										
(e/D = 1.5)	...	...	...	...	...	...	...	...	...	...
(e/D = 2.0)	...	...	...	...	...	...	...	...	...	...
F_{bry}, ksi:										
(e/D = 1.5)	...	...	...	...	...	...	...	...	...	...
(e/D = 2.0)	...	...	...	...	...	...	...	...	...	...
e, percent (S-basis):										
L	10	...	10	...	10	...	8	8	8	8
LT[b]	8	...	8	...	8	...	6	6	6	6
ST[b]	...	...	8	...	8	...	...	...	6	6
RA, percent (S-basis):										
L	20	...	20	...	15	...	20	20	20	20
LT[b]	15	...	15	...	15	...	15	15	15	15
ST[b]	...	...	15	...	15	...	...	...	15	15
E, 10^3 ksi	16.0									
E_c, 10^3 ksi	16.4									
G, 10^3 ksi	6.2									
μ	0.31									
Physical Properties:										
ω, lb/in.^{3}	0.164									
C, K, and α	See Figure 5.4.2.0									

[a]1300 to 1350 F for 1-3 hours, air cool to room temperature.
[b]Applicable, providing LT or ST dimension is ≥2.500 inches.

TABLE 5.4.2.0(d). *Design Mechanical and Physical Properties of Ti-6Al-6V-2Sn Forging*

Specification	AMS 4978	
Form	Forging	
Condition	Annealed	
Thickness or diameter, in.	≤2.000	2.001-4.000
Basis	S	S
Mechanical Properties:		
F_{tu}, ksi:		
L	150	145
LT[a]	150	145
ST[a]	...	145
F_{ty}, ksi:		
L	140	135
LT[a]	140	135
ST[a]	...	135
F_{cy}, ksi:		
L	...	...
LT[a]	...	...
ST[a]	...	...
F_{su}, ksi	...	...
F_{bru}, ksi:		
(e/D=1.5)	...	...
(e/D=2.0)	...	...
F_{bry}, ksi:		
(e/D=1.5)	...	...
(e/D=2.0)	...	...
e, percent:		
L	10	10
LT[a]	8	8
ST[a]	...	7
RA, percent:		
L	20	20
LT[a]	15	15
ST[a]	15	15
E, 10^3 ksi	16.0	
E_c, 10^3 ksi	16.4	
G, 10^3 ksi	6.2	
μ	0.31	
Physical Properties:		
ω, lb/in.^{3}	0.164	
C, K, and α	See Figure 5.4.2.0	

[a]Applicable, providing LT or ST dimension is ≥2.500 inches.

TABLE 5.4.2.0(e). *Design Mechanical and Physical Properties of Ti-6Al-6V-2Sn Extruded Bar and Shapes*

Specification	MIL-T-81556, Comp. AB-3							
Form	Extruded bar and shapes							
Condition	Annealed				Solution treated and aged			
Thickness or diameter, in. .	≤2.000		2.001-3.000	3.001-4.000	0.188-0.500	0.501-1.500	1.501-2.500	2.501-4.000
Basis	A	B	S	S	S	S	S	S
Mechanical Properties:								
F_{tu}, ksi:								
L	142	148	145	140	170	165	160	150
LT	141	148	145	140	170	165	160	150
F_{ty}, ksi:								
L	129	135	135	130	160	155	150	140
LT	128	135	135	130	160	155	150	140
F_{cy}, ksi:								
L	137	144	140	135	165	160	155	145
LT	136	142	140	135	165	160	155	145
F_{su}, ksi	93	97	...	...	...	...	...	...
F_{bru}[a], ksi:								
(e/D=1.5)	218	229	...	...	...	...	...	...
(e/D=2.0)	268	281	...	...	...	...	...	...
F_{bry}[a], ksi:								
(e/D=1.5)	196	203	...	...	...	...	...	...
(e/D=2.0)	227	235	...	...	...	...	...	...
e, percent (S-basis):								
L	10	...	10	10	8	8	8	8
LT	8	...	8	8	6	6	6	6
RA, percent (S-basis):								
L	20	...	20	20	15	15	15	15
LT	15	...	15	15	12	12	12	12
E, 10^3 ksi	16.0							
E_c, 10^3 ksi	16.4							
G, 10^3 ksi	6.2							
μ	0.31							
Physical Properties:								
ω, lb/in.^{3}	0.164							
C, K, and α	See Figure 5.4.2.0							

[a]Bearing values are "dry pin" values per Section 1.4.7.1.

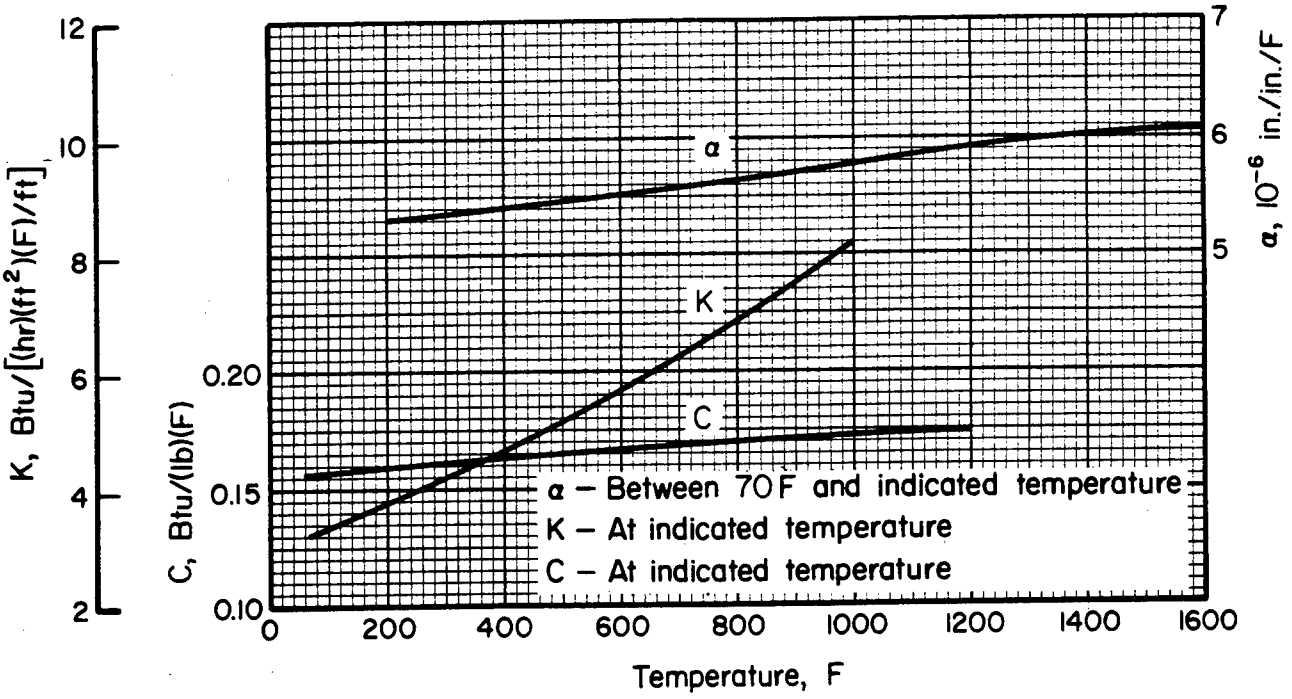


FIGURE 5.4.2.0. *Effect of temperature on the physical properties of Ti-6Al-6V-2Sn alloy.*

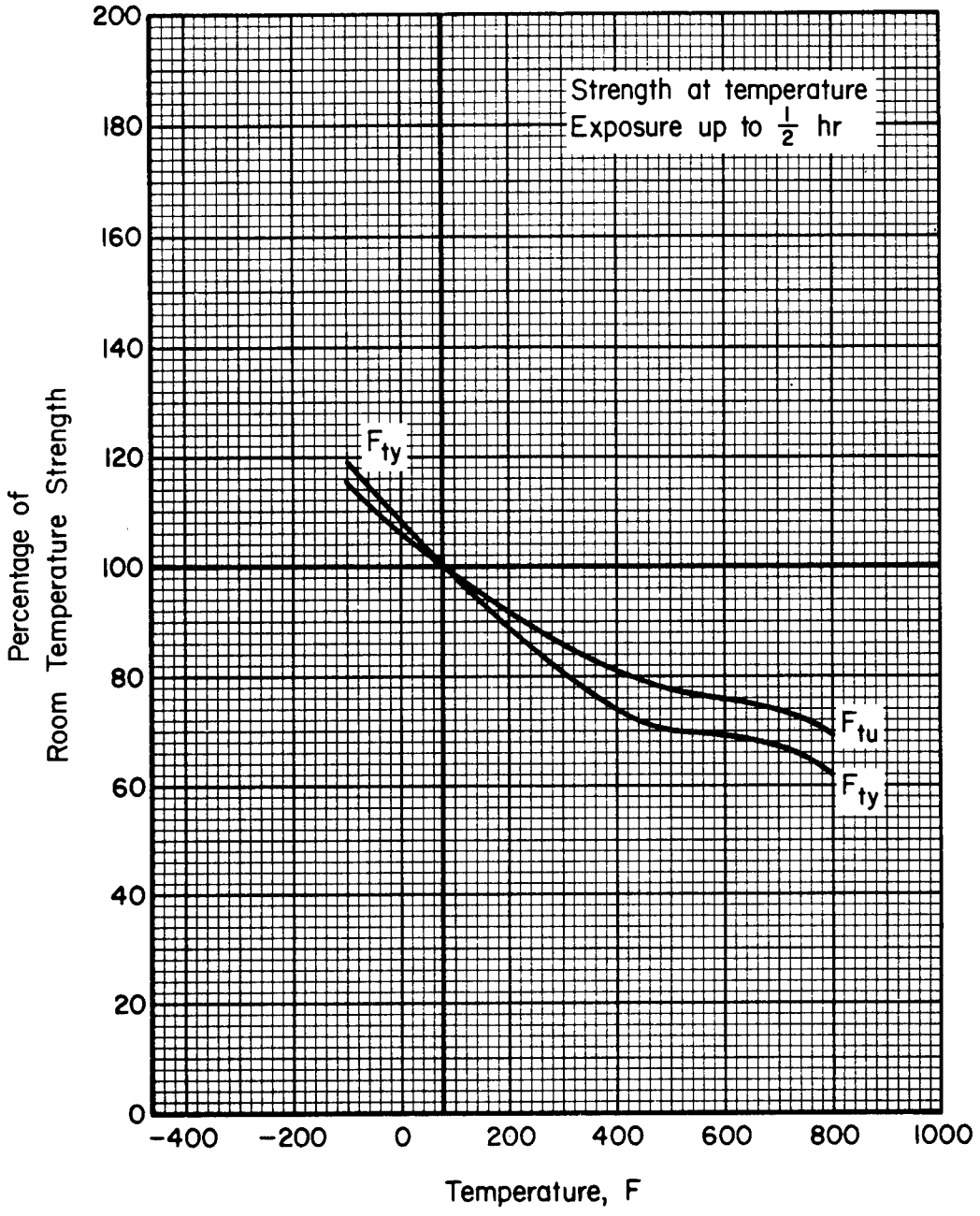


FIGURE 5.4.2.1.1(a). *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of annealed Ti-6Al-6V-2Sn extrusion.*

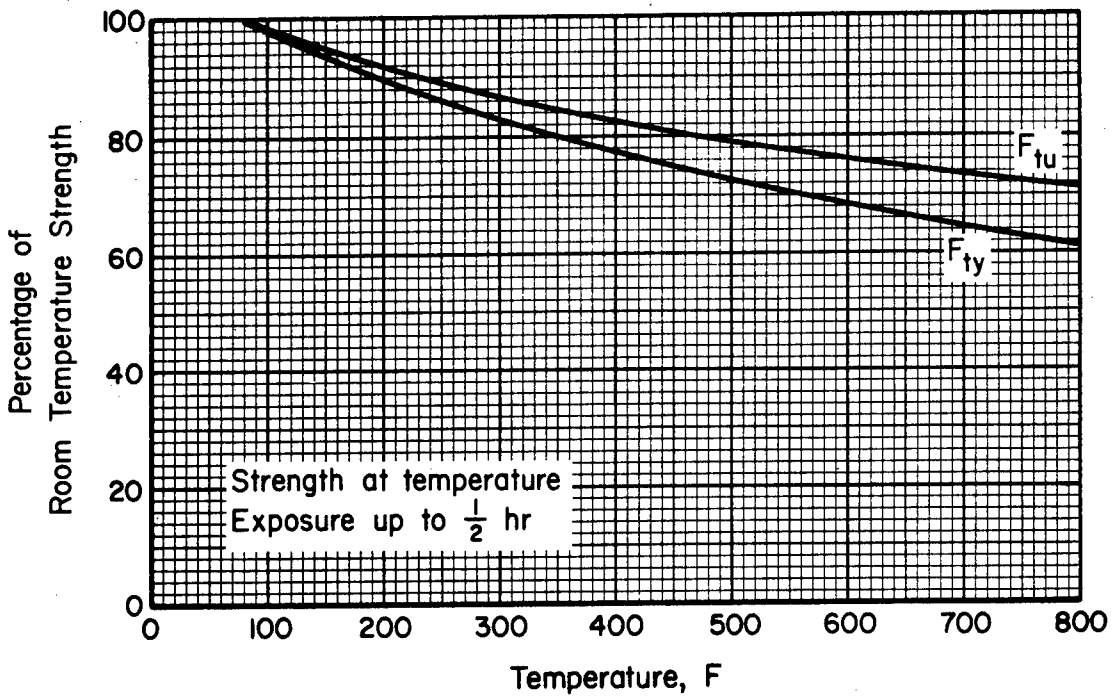


FIGURE 5.4.2.1.1(b). *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of annealed Ti-6Al-6V-2Sn plate.*

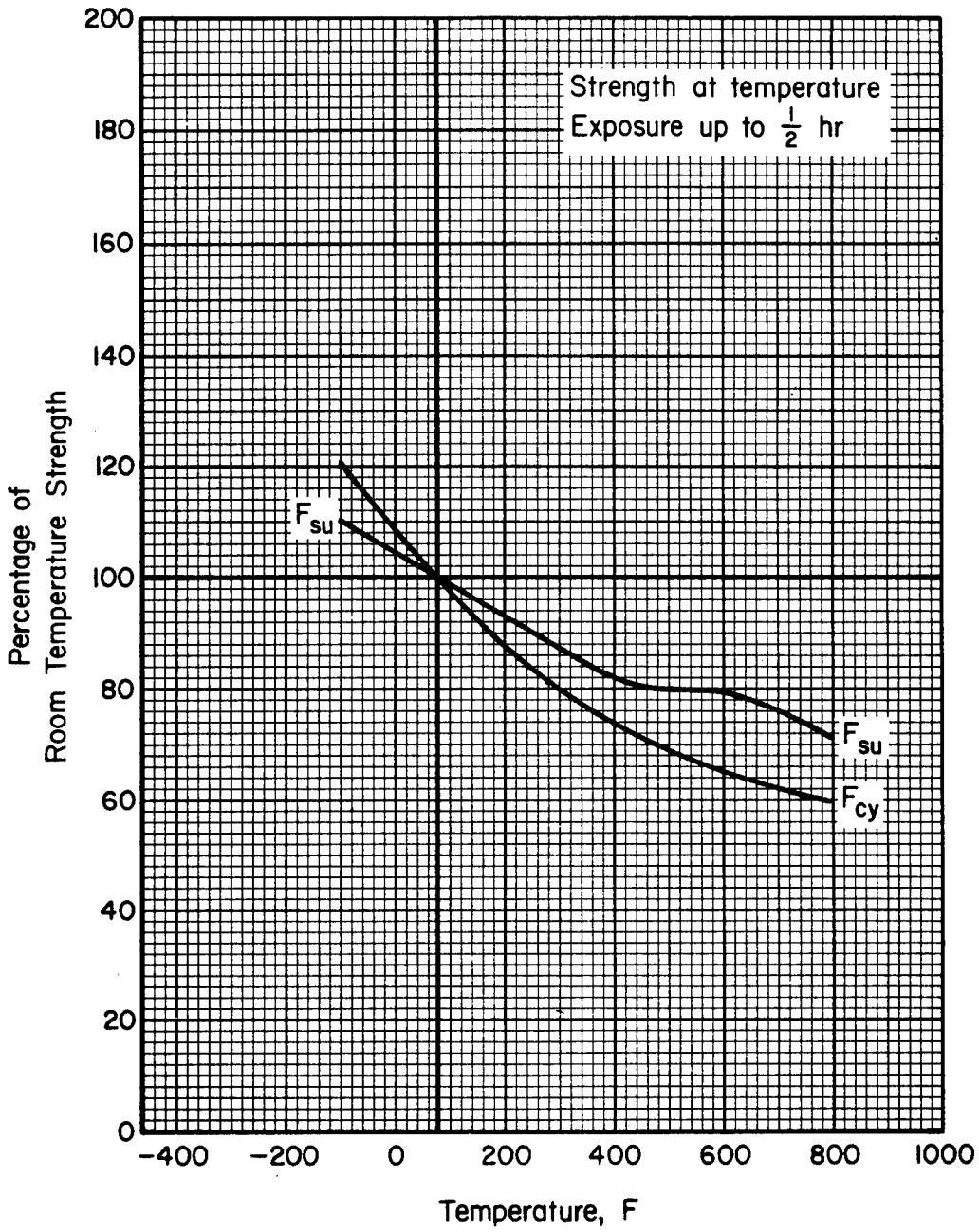


FIGURE 5.4.2.1.2(a). *Effect of temperature on the compressive yield strength (F_{cy}) and the shear ultimate strength (F_{su}) of annealed Ti-6Al-6V-2Sn extrusion.*

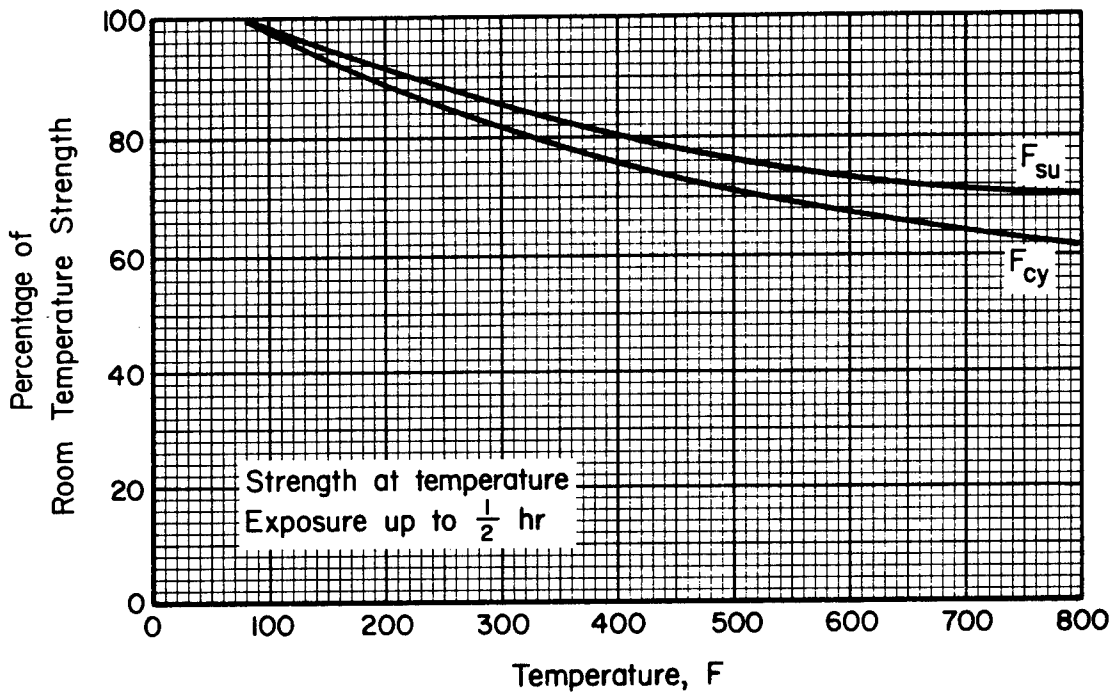


FIGURE 5.4.2.1.2(b). *Effect of temperature on the compressive yield strength (F_{cy}) and the shear ultimate strength (F_{su}) of annealed Ti-6Al-6V-2Sn plate.*

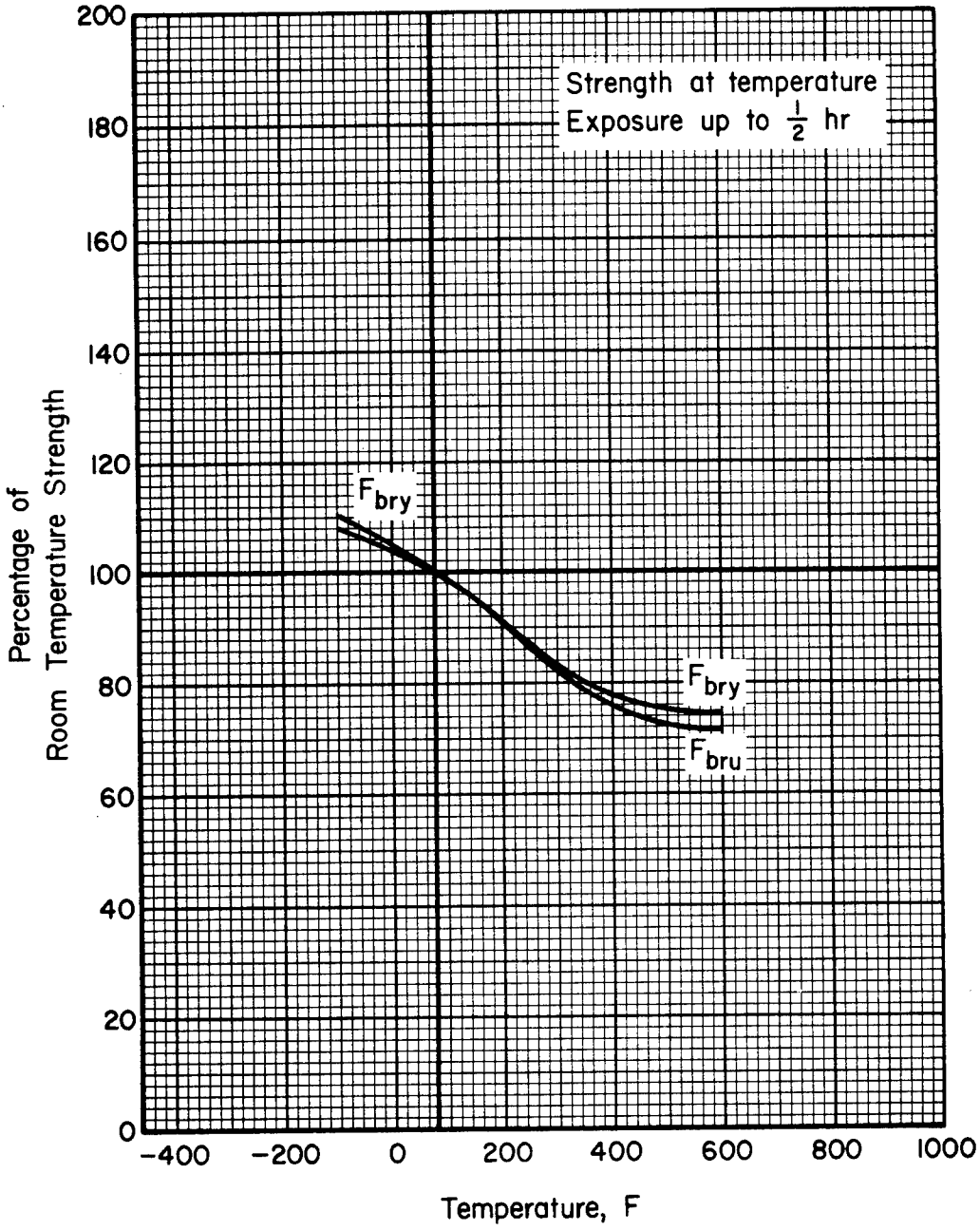


FIGURE 5.4.2.1.3(a). *Effect of temperature on the bearing ultimate strength (F_{bru}) and the bearing yield strength (F_{bry}) of annealed Ti-6Al-6V-2Sn extrusion.*

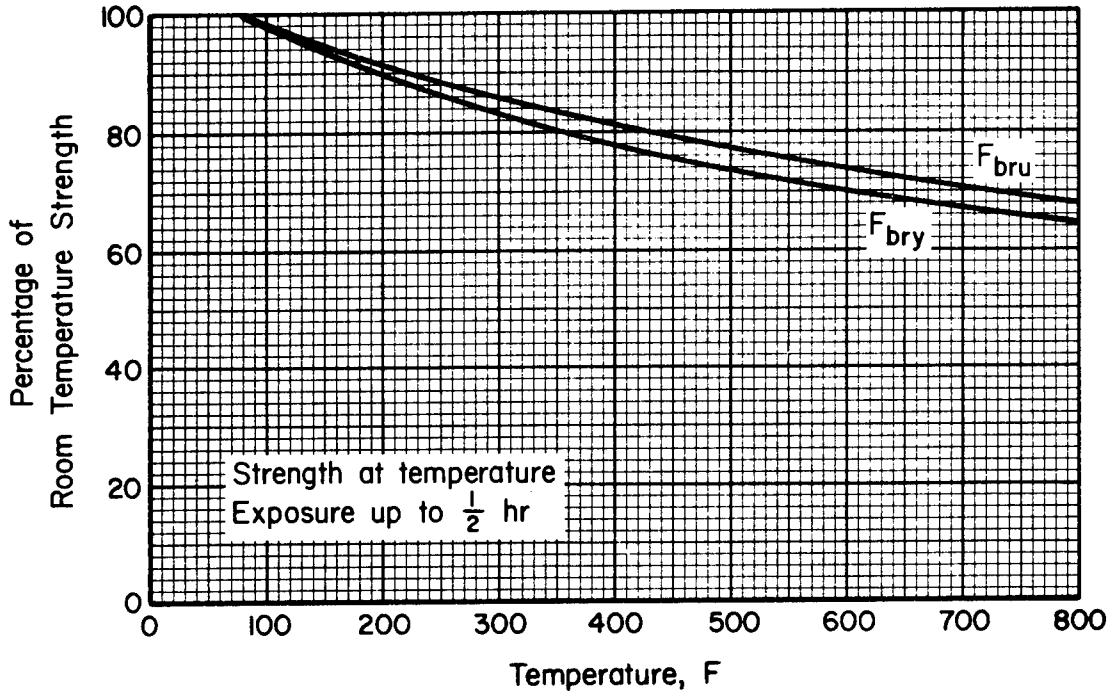


FIGURE 5.4.2.1.3(b). *Effect of temperature on the bearing ultimate strength (F_{bru}) and the bearing yield strength (F_{bry}) of annealed Ti-6Al-6V-2Sn plate.*

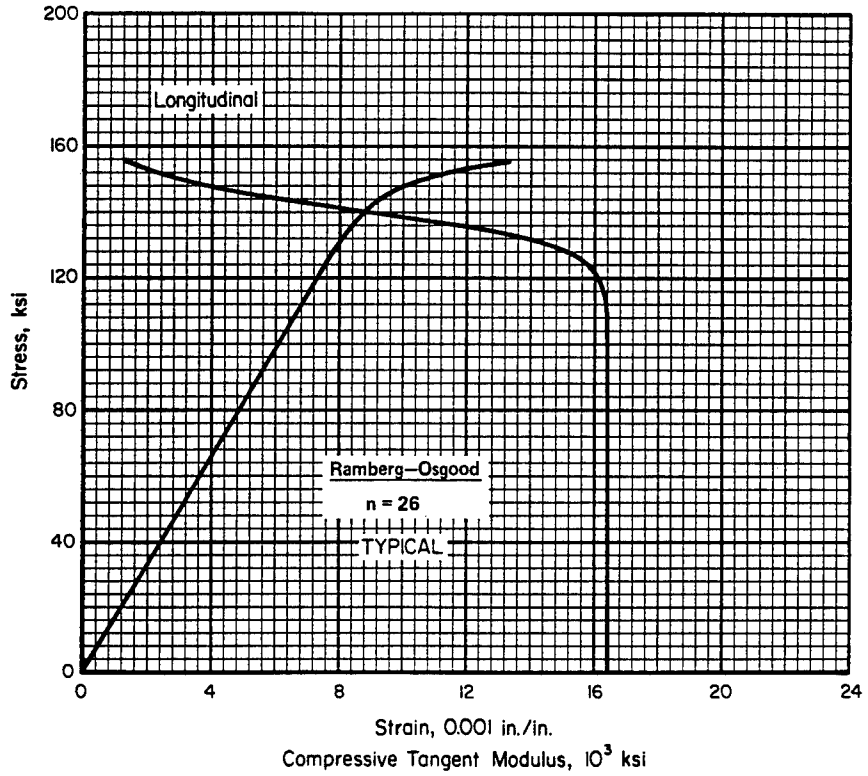


FIGURE 5.4.2.1.6(a). *Typical compressive stress-strain and tangent-modulus curves at room temperature for annealed Ti-6Al-6V-2Sn extrusion.*

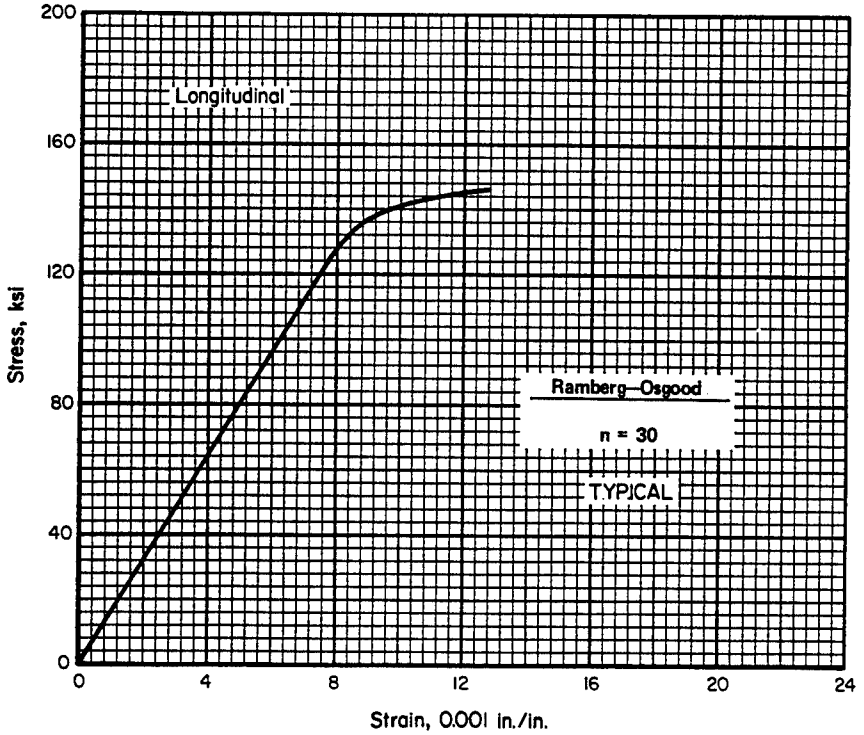


FIGURE 5.4.2.1.6(b). *Typical tensile stress-strain curve at room temperature for annealed Ti-6Al-6V-2Sn extrusion.*

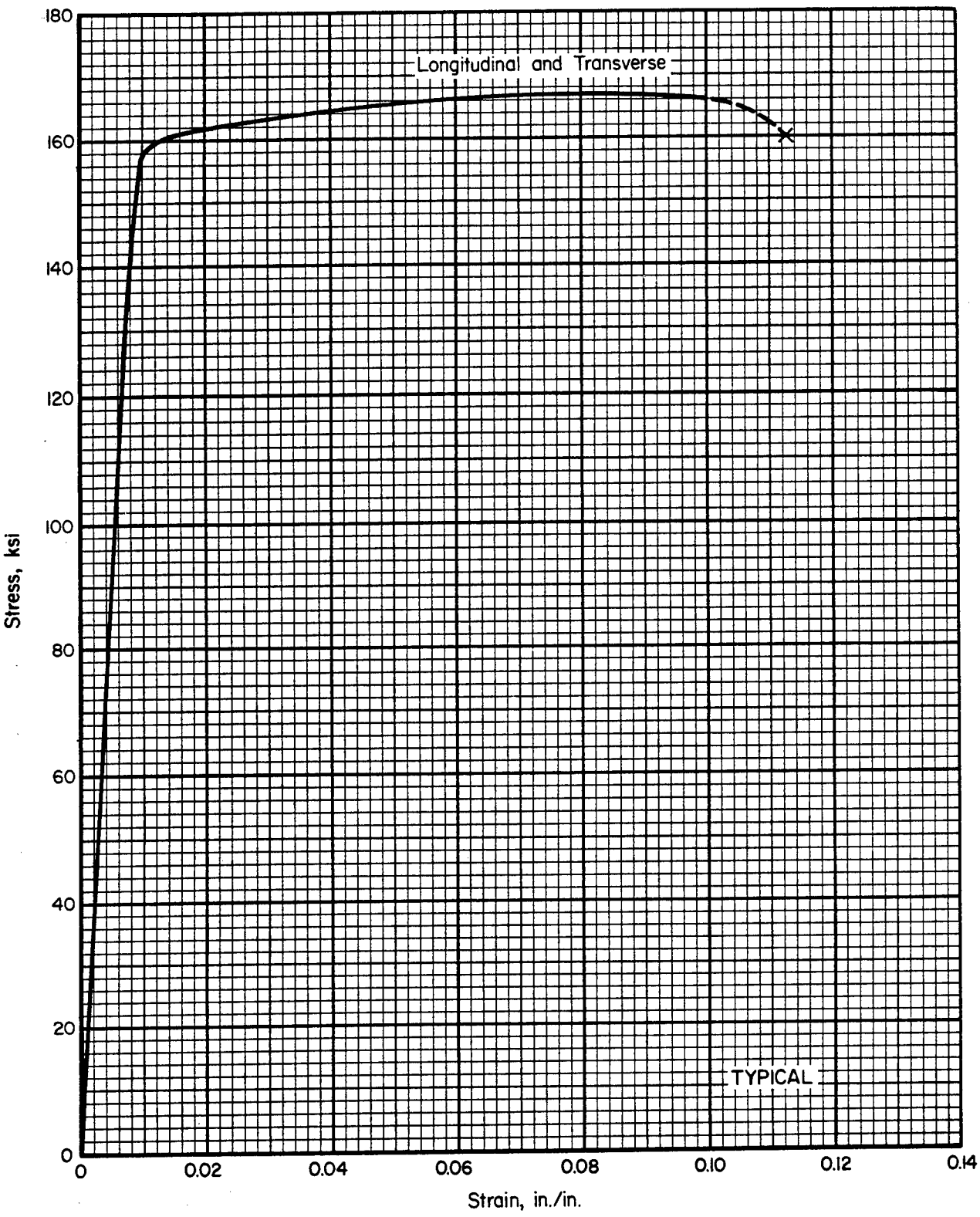


FIGURE 5.4.2.1.6(c). *Typical tensile stress-strain curve (full range) for annealed Ti-6Al-6V-2Sn sheet at room temperature.*

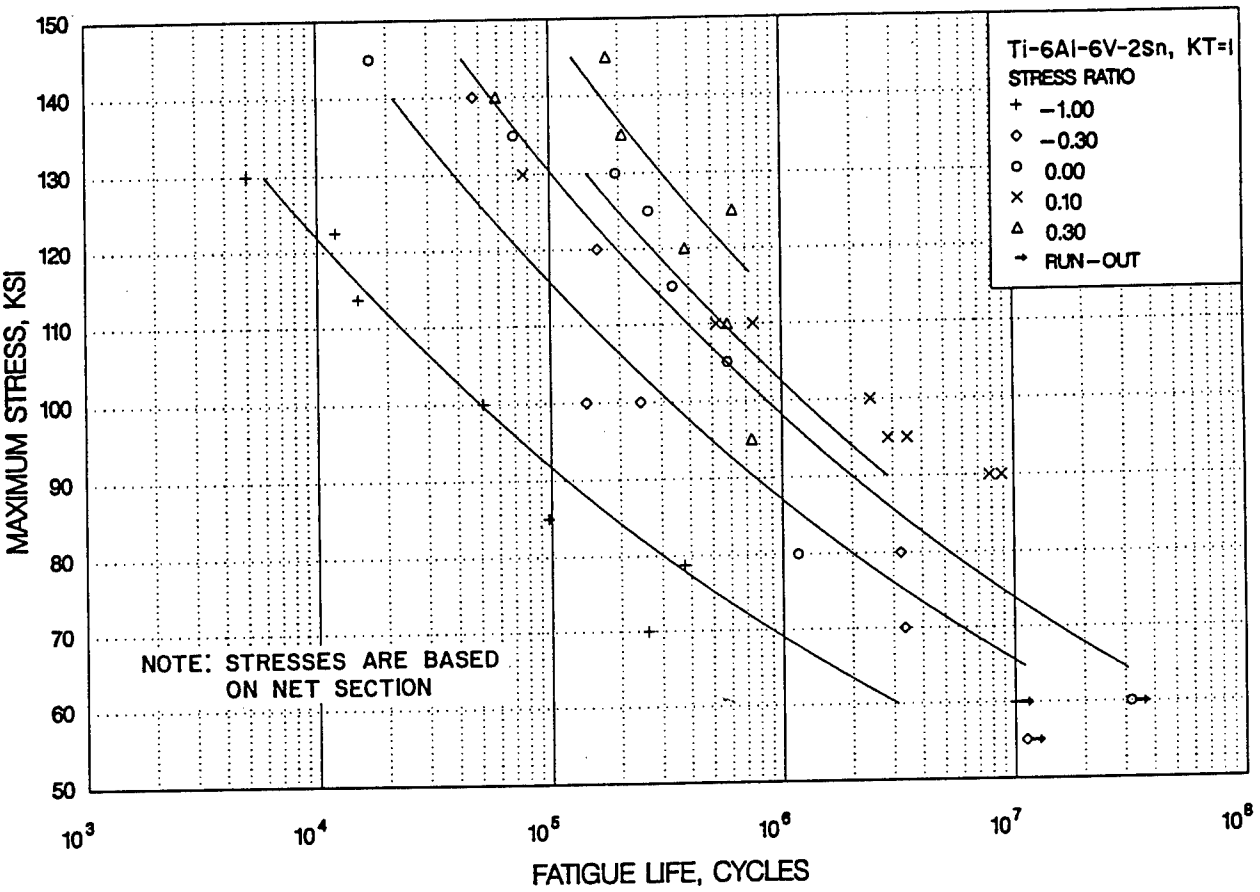


FIGURE 5.4.2.1.8(a). *Best-fit S/N curves for annealed Ti-6Al-6V-2Sn plate and die forging, K_t = 1.0, longitudinal direction.*

Correlative Information for Figure 5.4.2.1.8(a)

Product Form: Plate, 1.57-inch thick; die forging, thickness not specified

Properties:	TUS, ksi	TYS, ksi	Temp, F
	154.5	148.5	RT
	159.9	151.5	RT

Specimen Details:
Unnotched
0.195-inch diameter
Unspecified diameter from forging

Surface Condition:
RMS 32
Unspecified from forging

References: 5.4.1.2.8(c) and 5.4.2.1.8

Test Parameters:
Loading—Axial
Frequency—Unspecified
Temperature—RT
Atmosphere—Air

No. of Heats/Lot: 3

Equivalent Stress Equation:

$\text{Log } N_f = 20.90 - 8.10 \log (S_{eq})$

$S_{eq} = S_a + 0.41\ S_m$

Standard deviation in log(Life) = $23.5\ (1/S_{eq})$

Adjusted R^2 = 89%

Sample Size = 38

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

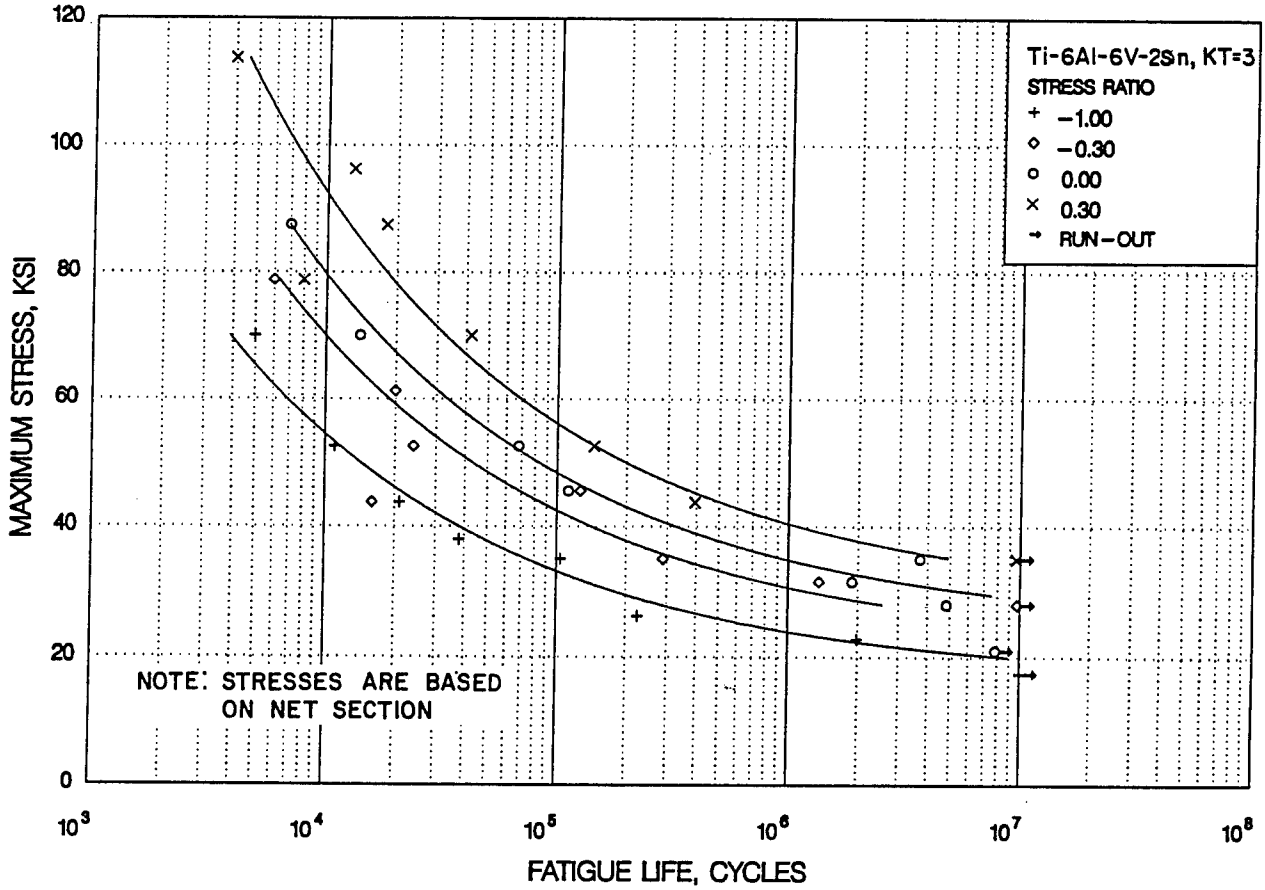


FIGURE 5.4.2.1.8(b). *Best-fit S/N curves for annealed Ti-6Al-6V-2Sn plate, K_t = 3.0, longitudinal direction.*

Correlative Information for Figure 5.4.2.1.8(b)

Product Form: Plate, 1.57-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp, F
	154.6	148.5	RT

Specimen Details:
V-Groove, K_t = 3.0
0.195-inch gross diameter
0.136-inch net diameter
0.005-inch root radius
60° flank angle

Surface Condition: RMS 32

References: 5.4.1.2.8(c)

Test Parameters:
Loading—Axial
Frequency—Unspecified
Temperature—RT
Atmosphere—Air

No. of Heats/Lot: 1

Equivalent Stress Equation:

$\text{Log } N_f = 8.31 - 2.73 \log (S_{eq} - 16.9)$
$S_{eq} = S_a + 0.37\ S_m$

Standard deviation in log(Life) = $8.87\ (1/S_{eq})$

Adjusted R^2 = 92%

Sample Size = 32

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

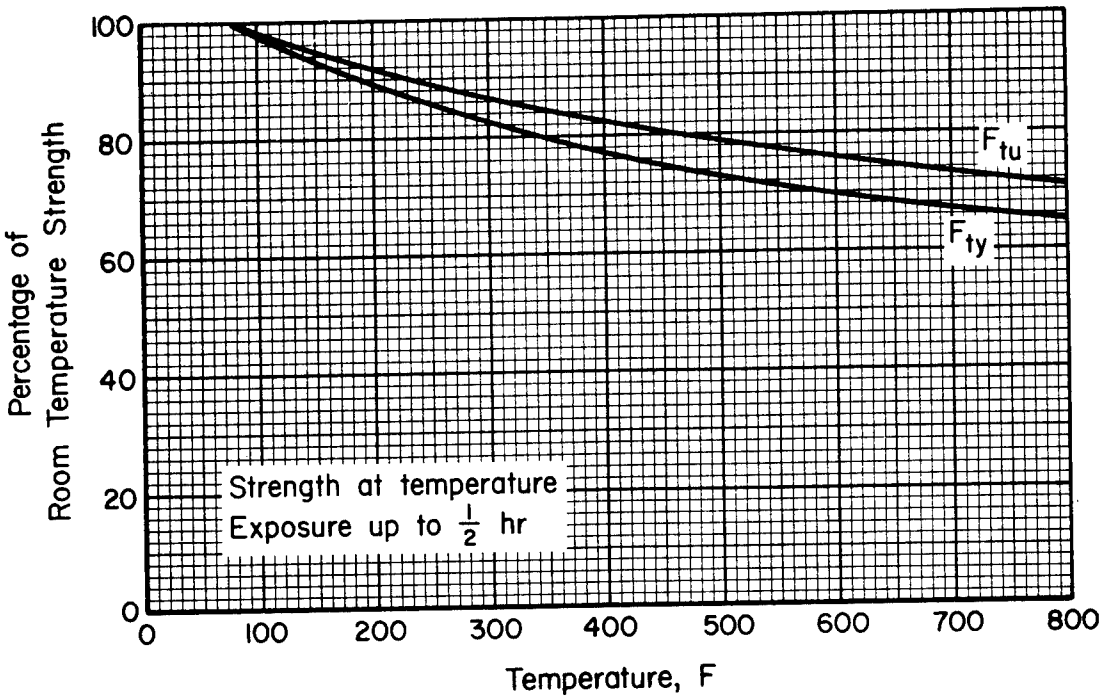


FIGURE 5.4.2.2.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of solution-treated and aged Ti-6Al-6V-2Sn plate.*

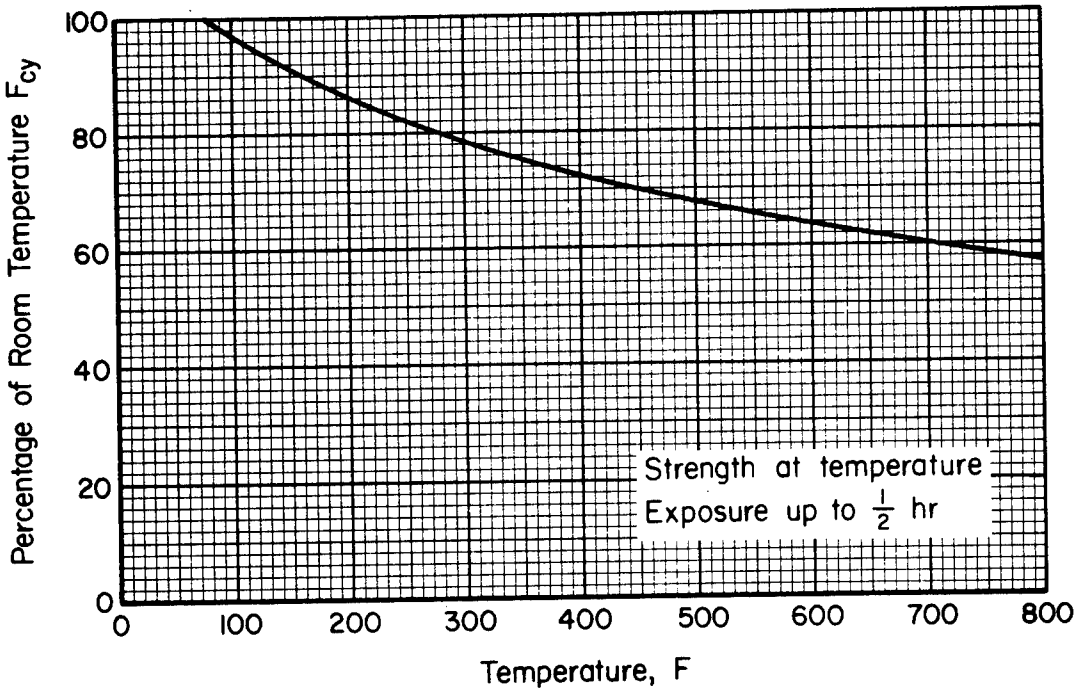


FIGURE 5.4.2.2.2. *Effect of temperature on compressive yield strength (F_{cy}) of solution-treated and aged Ti-6Al-6V-2Sn plate.*

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5.5 Beta, Near-Beta, and Metastable-Beta Titanium Alloys

There is no clear-cut definition for beta titanium alloys. Conventional terminology usually refers to near-beta alloys and metastable-beta alloys as classes of beta titanium alloys. A near-beta alloy is generally one which has appreciably higher beta stabilizer content than a conventional alpha-beta alloy such as Ti-6Al-4V, but is not quite sufficiently stabilized to readily retain an all-beta structure with an air cool of thin sections. For such alloys, a water quench even of thin sections is required. Due to the marginal stability of the beta phase in these alloys, they are primarily solution treated below the beta transus to produce primary alpha phase which in turn results in an enriched, more stable beta phase. This enriched beta phase is more suitable for aging. The Ti-10V-2Fe-3Al alloy is an example of a near-beta alloy.

On the other hand, the metastable-beta alloys are even more heavily alloyed with beta stabilizers than near-beta alloys and, as such, readily retain an all-beta structure upon air cooling of thin sections. Due to the added stability of these alloys, it is not necessary to heat treat below the beta transus to enrich the beta phase. Therefore, these alloys do not normally contain primary alpha since they are usually solution treated above the beta transus. These alloys are termed "metastable" because the resultant beta phase is not truly stable—it can be aged to precipitate alpha for strengthening purposes. Alloys such as Ti-15-3, B120VCA, Beta C, and Beta III are considered metastable-beta alloys.

Unfortunately, the classification of an alloy as either near-beta or metastable beta is not always obvious. In fact, the "metastable" terminology is not precise since a near-beta alloy is also metastable—i.e., it also decomposes to alpha plus beta upon aging.

There is one obvious additional category of beta alloys—the stable beta alloys. These alloys are so heavily alloyed with beta stabilizers that the beta phase will not decompose to alpha plus beta upon subsequent aging. There are no such alloys currently being produced commercially. An example of such an alloy is Ti-30Mo.

The interest in beta alloys stems from the fact that they contain a high volume fraction of beta phase which can be subsequently hardened by alpha precipitation. Thus, these alloys can generate quite high strength levels (in excess of 200 ksi) with good ductilities. Also, such alloys are much more deep hardenable than alpha-beta alloys such as Ti-6Al-4V. Finally, many of the more heavily alloyed beta alloys exhibit excellent cold formability and as such offer attractive sheet metal forming characteristics.

5.5.1 Ti-13V-11Cr-3Al

5.5.1.0 *Comments and Properties.*—Ti-13V-11Cr-3Al is a heat-treatable alloy possessing good workability and toughness in the annealed condition and high strength in the heat-treated condition. It is noted for its exceptional ability to harden in heavy sections (up to 6-inch diameter or greater) to tensile strength of 170 ksi F_{tu}.

Manufacturing Considerations.—This alloy possesses very good formability at room temperature; stretch forming is usually conducted at 500 F. Ti-13V-11Cr-3Al is readily fusion or spot welded. Arc-welded joints are very ductile in the as-welded condition, but have low strengths.

Environmental Considerations.—Ti-13V-11Cr-3Al is stable for times up to 1000 hours in the annealed condition at 550 F and in the solution treated and aged condition up to 600 F. Prolonged exposure above these temperatures may result in ductility losses. If welding is employed, the stability of the weld should be investigated under the particular exposure conditions to be encountered. While the material is not noted for good creep performance, Ti-13V-11Cr-3Al has exceptional short-time strength at temperatures to 1200 F and above. Oxidation resistance is satisfactory at such temperatures for short-time exposure and for long-time exposure at the lower elevated temperatures. Hot-salt stress corrosion has been shown to be possible in this alloy at temperatures as low as 500 F in highly stressed applications (e.g., rivet heads). It is generally thought that the material is moderately susceptible to aqueous chloride solu-

tion stress corrosion. Ti-13V-11Cr-3Al is not noted for good fracture toughness in the aged or high-strength condition and is not recommended in any condition for cryogenic temperature applications. Under certain conditions, titanium, when in contact with cadmium, silver, mercury, or certain of their compounds, may become embrittled. Refer to MIL-S-5002 and MIL-STD-1568 for restrictions concerning applications with titanium in contact with these metals or their compounds.

Heat Treatment.—This alloy is commonly specified in either the annealed condition or in the fully heat-treated condition. The specified fully heat-treated, or solution-treated and aged, condition is as follows:

> Solution treat at 1450 F for 15 to 60 minutes, air cool (water quench if material is over 2 inches thick).
>
> Age at 900 F for 2 to 60 hours, dependent on strength level. (Note: typical aging time to achieve F_{tu} = 170 ksi is 24 to 36 hours.)

Specifications and Properties.—Material specifications for Ti-13V-11Cr-3Al are shown in Table 5.5.1.0(a). Room-temperature mechanical and physical properties for Ti-13V-11Cr-3Al are shown in Table 5.5.1.0(b). The effect of temperature on physical properties is shown in Figure 5.5.1.0.

TABLE 5.5.1.0(a). *Material Specifications for Ti-13V-11Cr-3Al*

Specifications	Form
MIL-T-9046	Sheet, strip, and plate
MIL-T-9047	Bar

5.5.1.1 *Annealed Condition.*—Elevated temperature curves for annealed Ti-13V-11Cr-3Al are shown in Figures 5.5.1.1.1 through 5.5.1.1.4. Typical tensile stress-strain curves for annealed material at temperatures ranging from room temperature to 1000 F are shown in Figure 5.5.1.1.6. Unnotched and notched fatigue data at room and elevated temperatures for annealed sheet are shown in Figures 5.5.1.1.8(a) through (d).

5.5.1.2 *Solution-Treated and Aged Condition.*—Elevated temperature curves for solution-treated and aged Ti-13V-11Cr-3Al are shown in Figures 5.5.1.2.1 through 5.5.2.1.4. Typical tensile stress-strain curves at various temperatures are shown in Figure 5.5.1.2.6. Unnotched fatigue data at room and elevated temperatures for solution-treated and aged sheet are shown in Figures 5.5.1.2.8(a) through (c).

TABLE 5.5.1.0(b). *Design Mechanical and Physical Properties of Ti-13V-11Cr-3Al*

Specification	MIL-T-9046, Comp. B-1			MIL-T-9047	
Form	Sheet, strip, and plate			Bar	
Condition	Annealed		Solution treated and aged	Annealed	Solution treated and aged
Thickness or diameter, in.	0.012-0.049	0.050-4.000	≤4.000	≤7.000[a]	≤4.000[a]
Basis	S	S	S	S	S
Mechanical Properties:					
F_{tu}, ksi:					
L	132	125	170	125	170
LT	132	125	170	125[c]	170[c]
ST	...	125	170	125[c]	170[c]
F_{ty}, ksi:					
L	126	120	160	120	160
LT	126	120	160	120[c]	160[c]
ST	...	120	160	120[c]	160[c]
F_{cy}, ksi:					
L	...	120	162	...	...
LT	...	120	162	...	...
ST	...	120	162	...	...
F_{su}, ksi	...	92	105	...	...
F_{bru}, ksi:					
(e/D = 1.5)	...	207	248	...	...
(e/D = 2.0)	...	270	313	...	...
F_{bry}, ksi:					
(e/D = 1.5)	...	169	217	...	...
(e/D = 2.0)	...	200	247	...	...
e, percent:					
L	8	10	4[b]	10	6
LT	8	10	4[b]	10[c]	2[c]
ST	...	10	4[b]	10[c]	2[c]
RA, percent:					
L	...	...	...	25	10
LT	...	...	...	25[c]	5[c]
ST	...	...	...	25[c]	5[c]
E, 10^3 ksi	14.5		15.5	14.5	15.5
E_c, 10^3, ksi	...		...	...	...
G, 10^3, ksi	...		...	...	...
μ	...		...	...	...
Physical Properties:					
ω, lb/in.^{3}	0.174				
C, K, and α	See Figure 5.5.1.0				

[a]Maximum of 16 square-inch cross-sectional area.
[b]Thickness 0.025 inch and above: 3 percent below 0.025 inch.
[c]Applicable, providing LT or ST dimension is ≥3.000 inches.

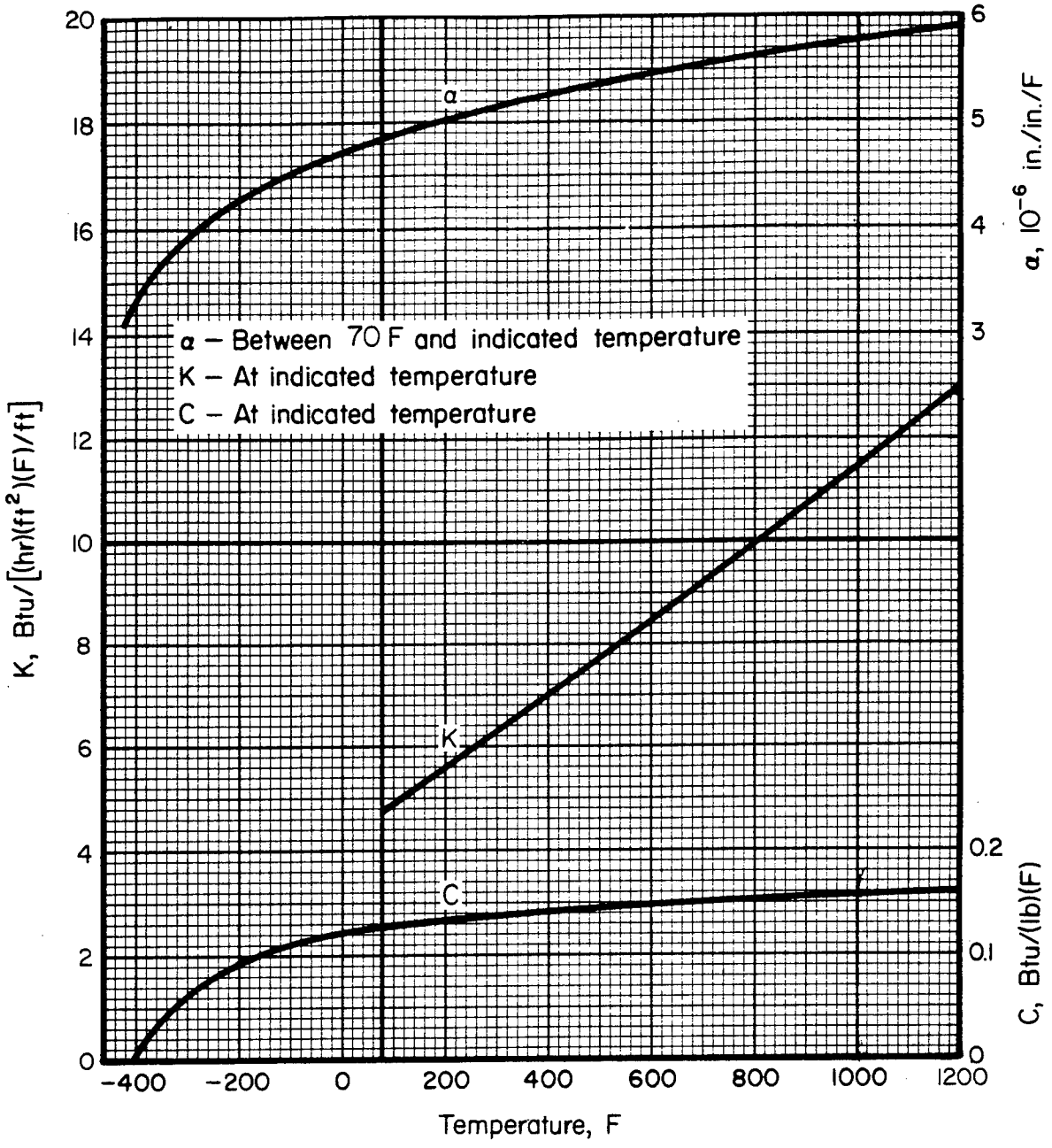


FIGURE 5.5.1.0. *Effect of temperature on the physical properties of Ti-13V-11Cr-3Al alloy.*

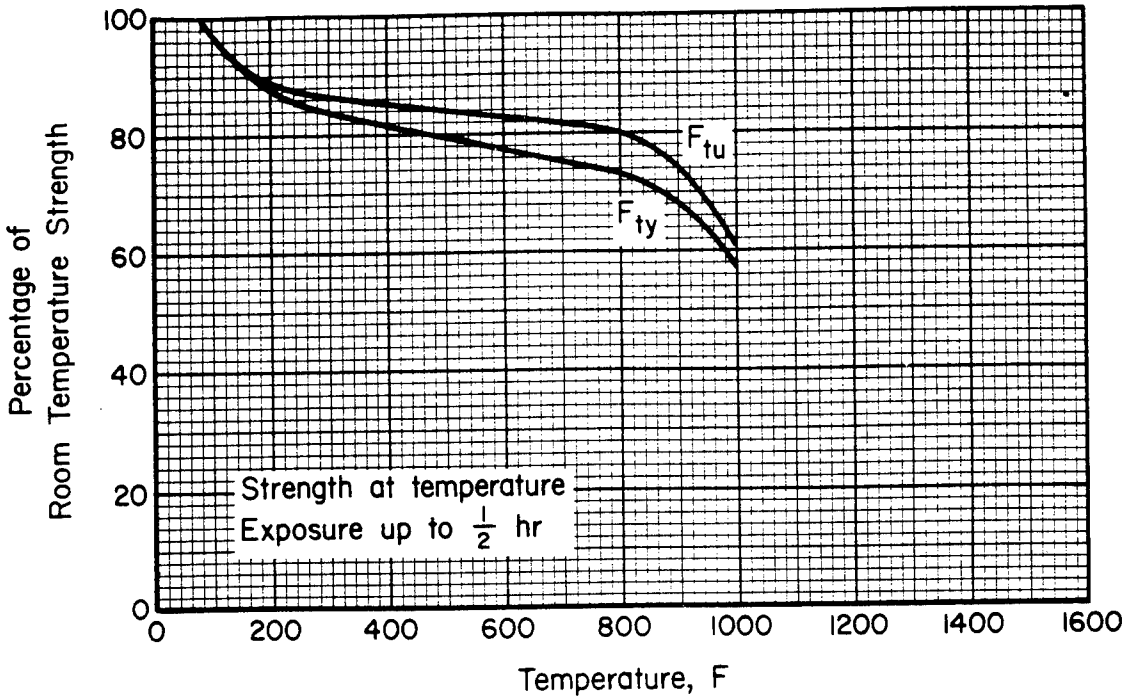


FIGURE 5.5.1.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of annealed Ti-13V-11Cr-3Al alloy sheet.*

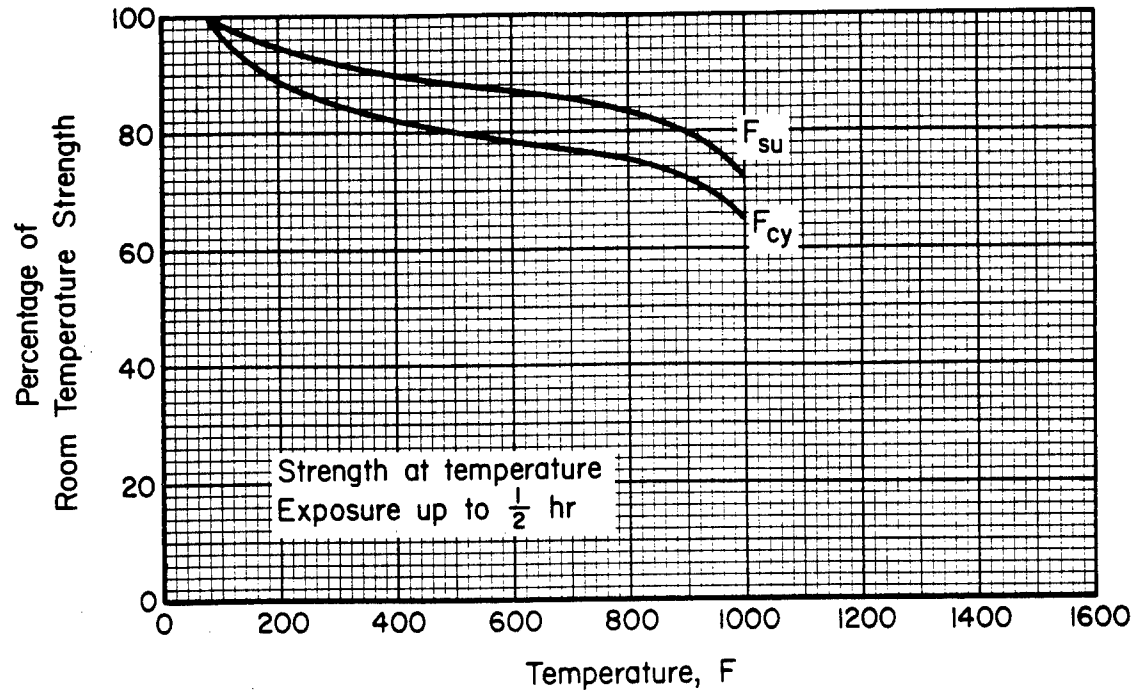


FIGURE 5.5.1.1.2. *Effect of temperature on the compressive yield strength (F_{cy}) and the shear ultimate strength (F_{su}) of annealed Ti-13V-11Cr-3Al alloy sheet.*

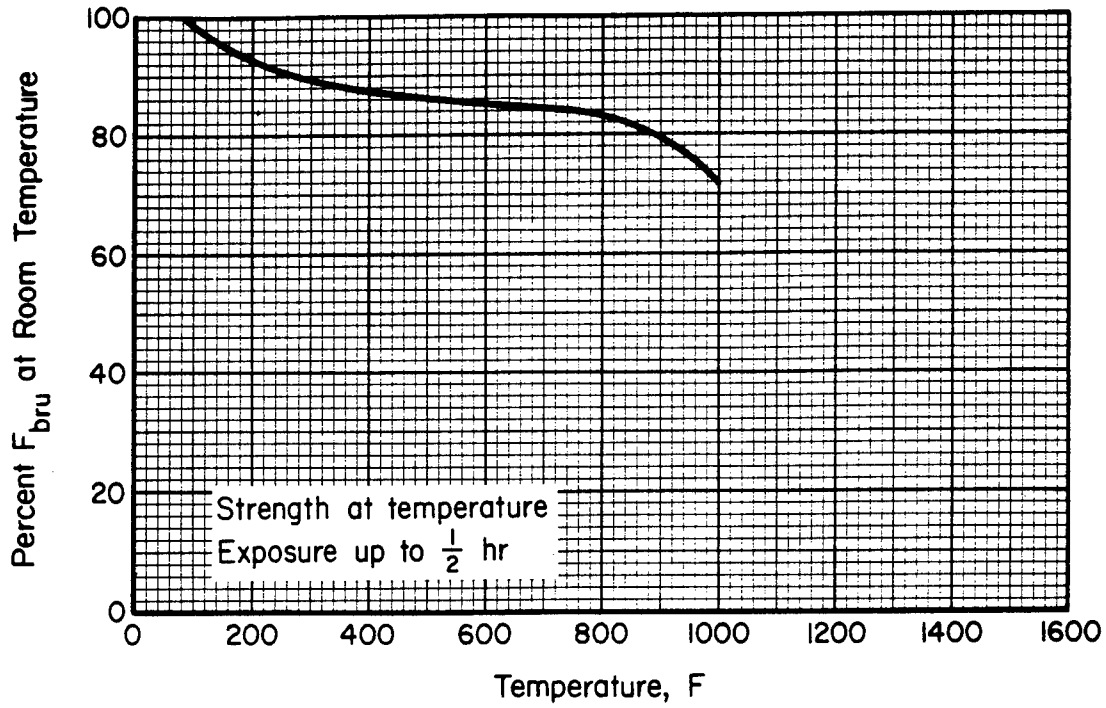


FIGURE 5.5.1.1.3(a). *Effect of temperature on the ultimate bearing strength (F_{bru}) of annealed Ti-13V-11Cr-3Al alloy sheet.*

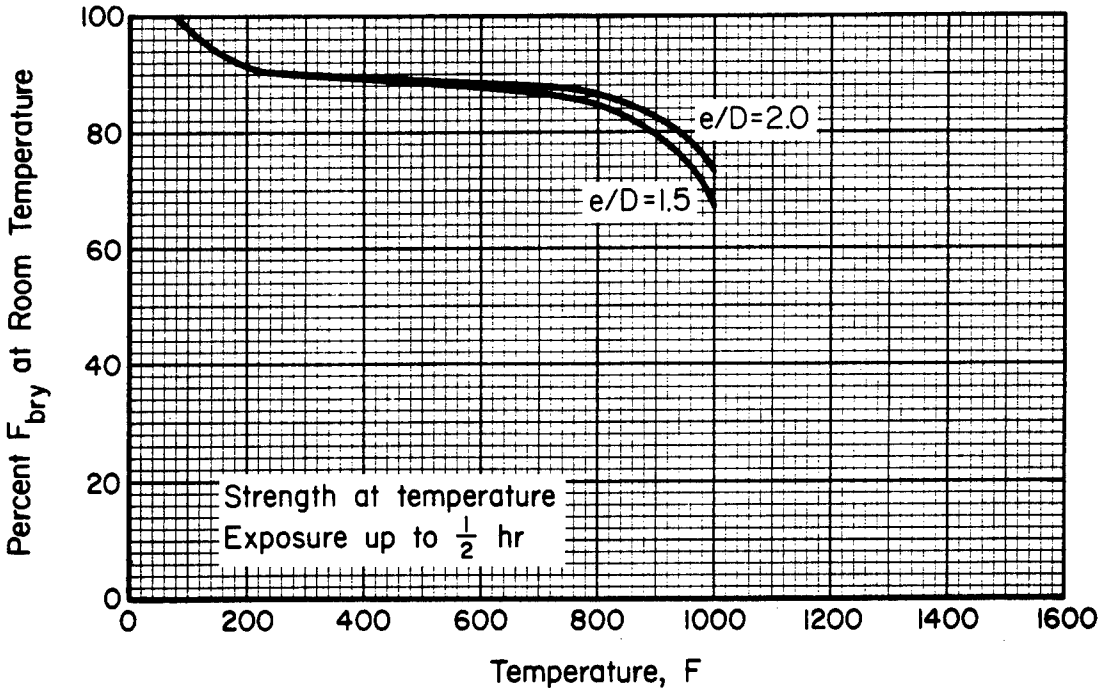


FIGURE 5.5.1.1.3(b). *Effect of temperature on the bearing yield strength (F_{bry}) of annealed Ti-13V-11Cr-3Al alloy sheet.*

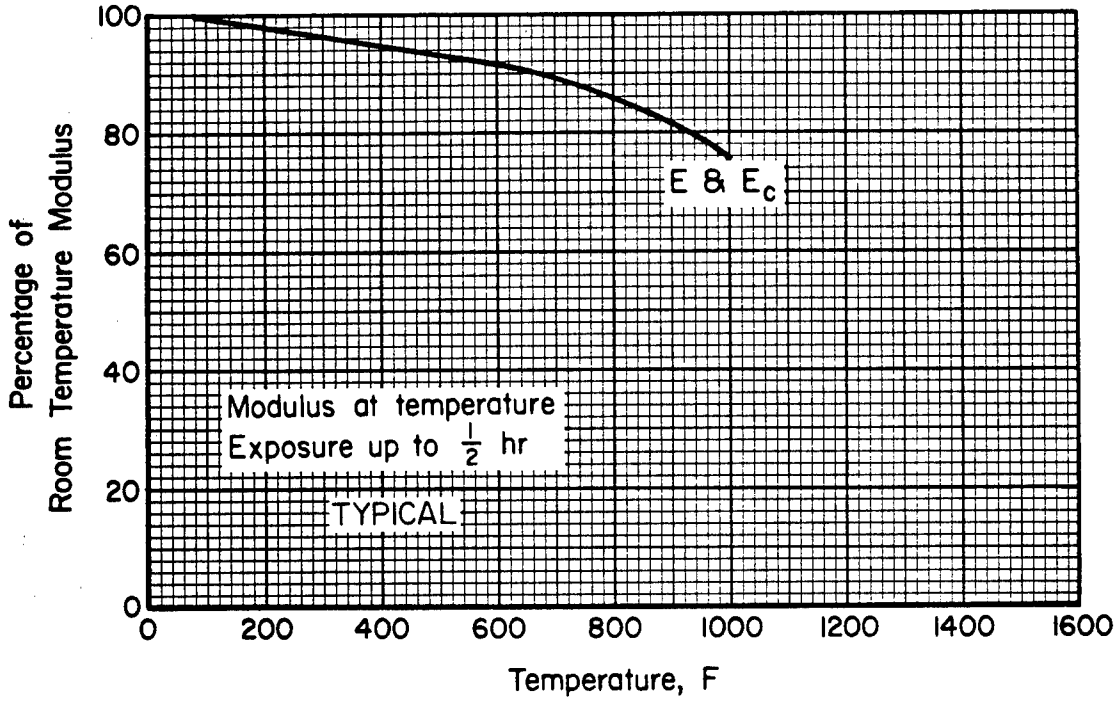


FIGURE 5.5.1.1.4. *Effect of temperature on the tensile and compressive moduli (E and E_c) of annealed Ti-13V-11Cr-3Al alloy sheet.*

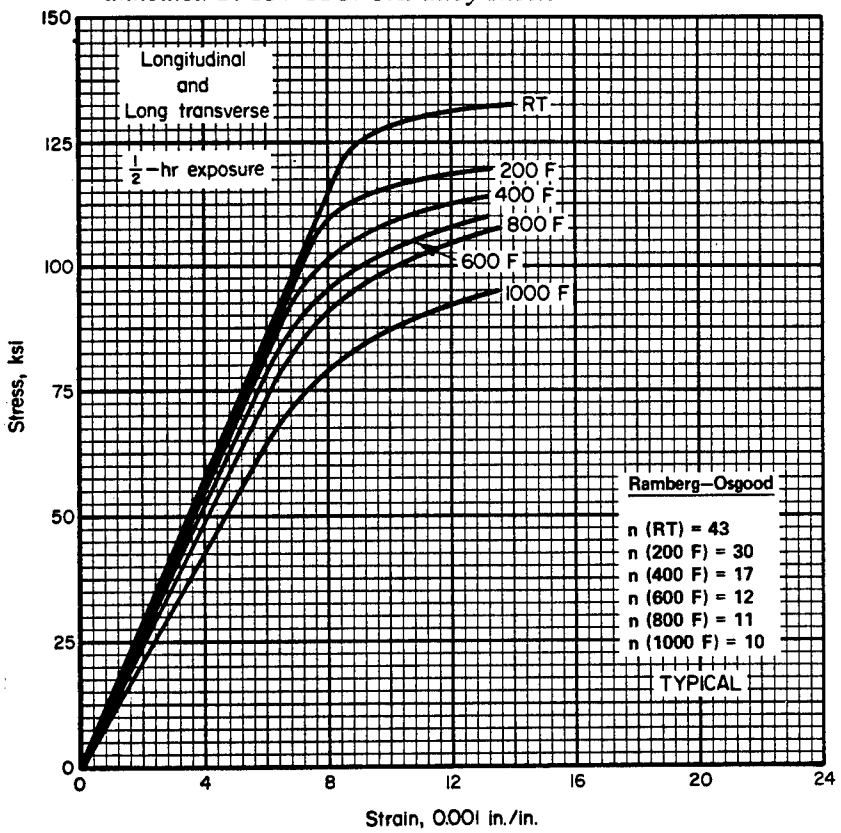


FIGURE 5.5.1.1.6. *Typical tensile stress-strain curves for annealed Ti-13V-11Cr-3Al alloy sheet at room and elevated temperatures.*

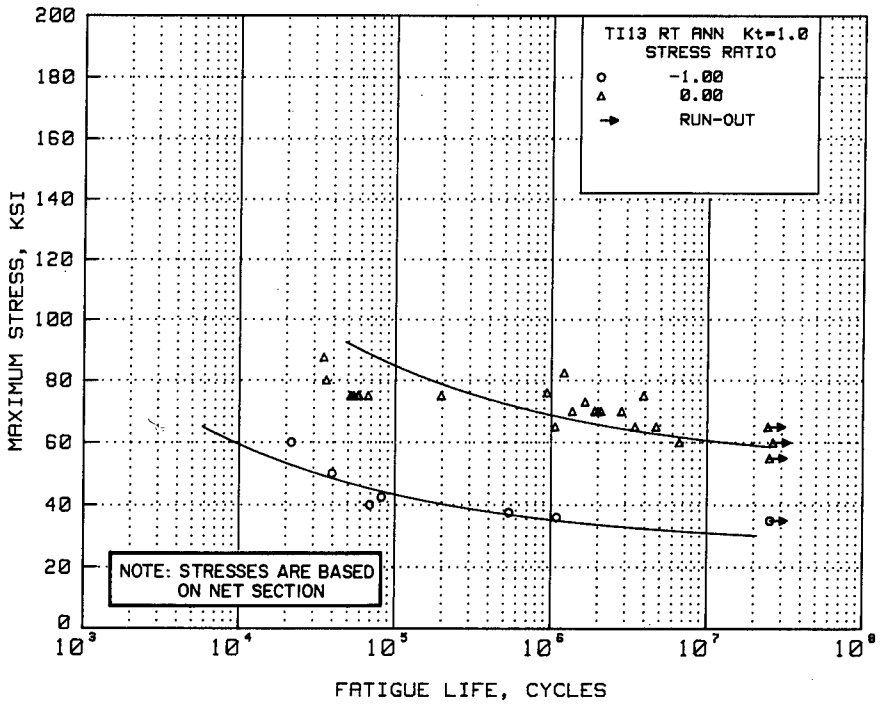


FIGURE 5.5.1.1.8(a). *Best-fit S/N curves for unnotched, annealed Ti-13V-11Cr-3Al alloy sheet, longitudinal direction.*

Correlative Information for Figure 5.5.1.1.8(a)

Product Form: Sheet, 0.043-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	138.50	132.80	RT

Specimen Details: Unnotched, 0.30-inch wide

Surface Condition: As machined, edges polished with emery paper.

Reference: 5.5.1.1.8

Test Parameters:

Loading — Axial
Frequency — 3600 cpm
Temperature — RT
Environment— Air

No. of Heats/Lots: Not specified

Equivalent Stress Equation

$\text{Log } N_f = 10.15\text{-}3.41 \log (S_{eq}\text{-}52.2)$
$S_{eq} = S_{max} (1\text{-}R)^{0.97}$
Standard Error of Estimate = 0.58
Standard Deviation in Life = 0.82
R^2 = 50%

Sample Size = 27

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

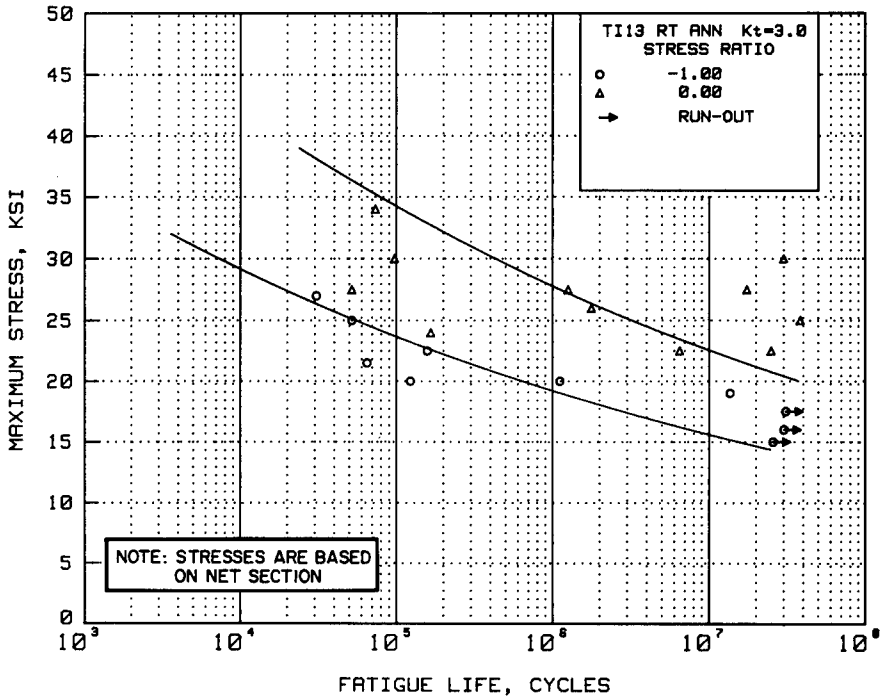


FIGURE 5.5.1.1.8(b). *Best-fit S/N curves for notched, K_t = 3.0, annealed Ti-13V-11Cr-3Al alloy sheet, longitudinal direction.*

Correlative Information for Figure 5.5.1.1.8(b)

Product Form: Sheet, 0.043-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	138.50	132.8	RT

Specimen Details: Notched, Edge, K = 3.0
0.448-inch gross width
0.300-inch net width
0.022-inch root radius, r
60° flank angle, ω

Surface Condition: As machined, edges polished with emery paper.

Reference: 5.5.1.1.8

Test Parameters:

Loading — Axial
Frequency — 3600 cpm
Temperature — RT
Environment— Air

No. of Heats/Lots: Not specified

Equivalent Stress Equation

$\text{Log } N_f = 21.93\text{-}11.03 \log (S_{eq})$
$S_{eq} = S_{max} (1\text{-}R)^{0.53}$
Standard Error of Estimate = 0.91
Standard Deviation in Life = 1.11
R^2 = 33%

Sample Size = 19

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

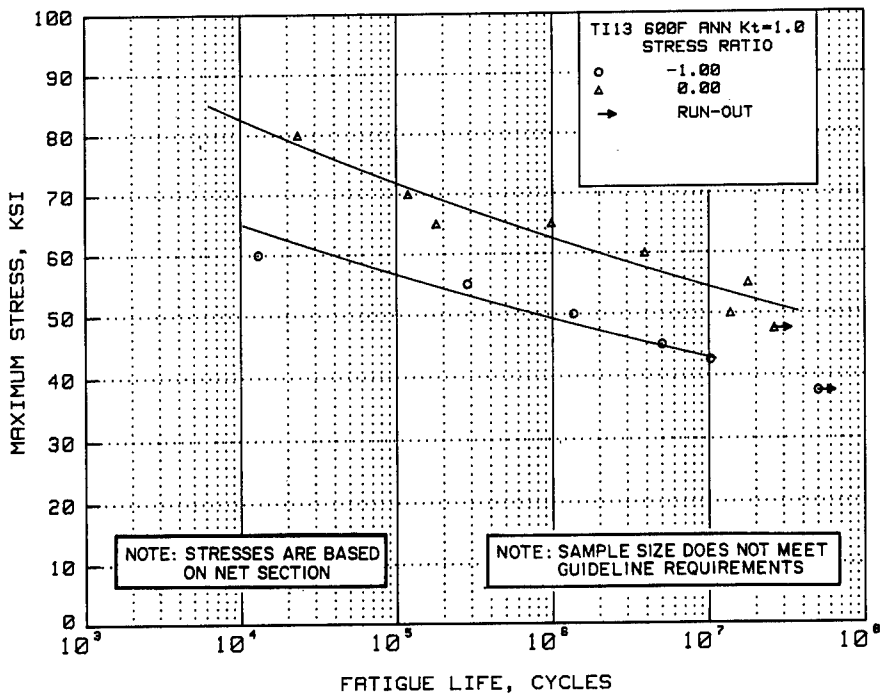


FIGURE 5.5.1.1.8(c). *Best-fit S/N curves for unnotched, annealed Ti-13V-11Cr-3Al alloy sheet at 600 F, longitudinal direction.*

Correlative Information for Figure 5.5.1.1.8(c)

Product Form: Sheet, 0.043-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	116.00	102.61	600 F

Specimen Details: Unnotched, 0.300-inch width

Surface Condition: As machined, edges polished with emery paper.

Reference: 5.5.1.1.8

Test Parameters:

Loading — Axial
Frequency — 3600 cpm
Temperature — 600 F
Environment— Air

No. of Heats/Lots: Not specified

Equivalent Stress Equation

$\text{Log } N_f = 35.63\text{-}16.50 \log (S_{eq})$
$S_{eq} = S_{max} (1\text{-}R)^{0.34}$
Standard Error of Estimate = 0.35
Standard Deviation in Life = 1.07
$R^2 = 90\%$

Sample Size = 12

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

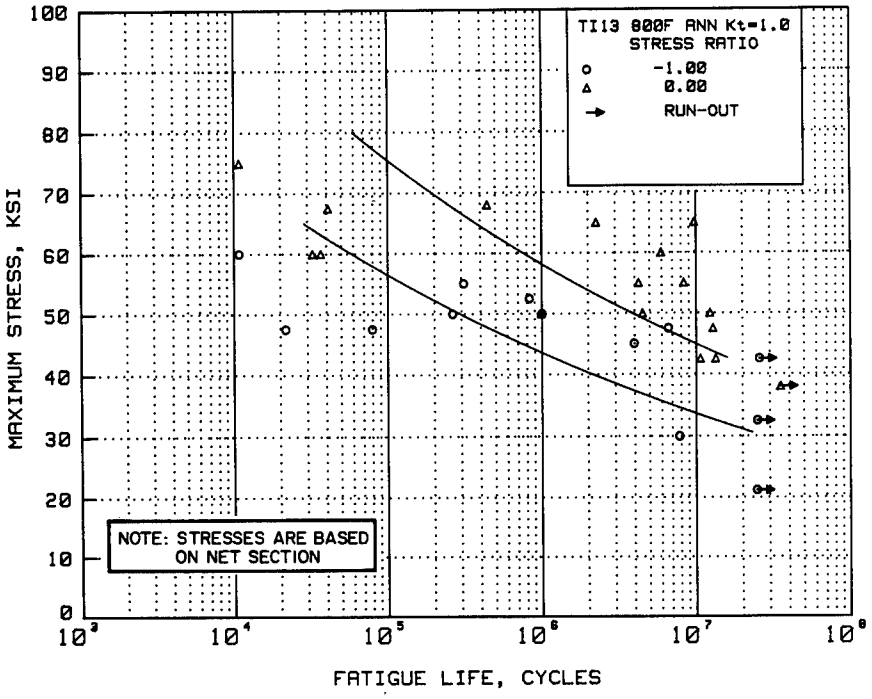


FIGURE 5.5.1.1.8(d). *Best-fit S/N curves for unnotched annealed Ti-13V-11Cr-3Al alloy sheet at 800 F, longitudinal direction.*

Correlative Information for Figure 5.5.1.1.8(d)

Product Form: Sheet, 0.043-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	115.80	98.61	800 F

Specimen Details: Unnotched, 0.300-inch wide

Surface Condition: As machined, edges polished with emery paper.

Reference: 5.5.1.1.8

Test Parameters:

Loading — Axial
Frequency — 3600 cpm
Temperature — 800 F
Environment— Air

No. of Heats/Lots: Not specified

Equivalent Stress Equation

$\text{Log } N_f = 21.67\text{-}8.88 \log (S_{eq})$
$S_{eq} = S_{max} (1\text{-}R)^{0.42}$
Standard Error of Estimate = 0.84
Standard Deviation in Life = 1.07
$R^2 = 39\%$

Sample Size = 26

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

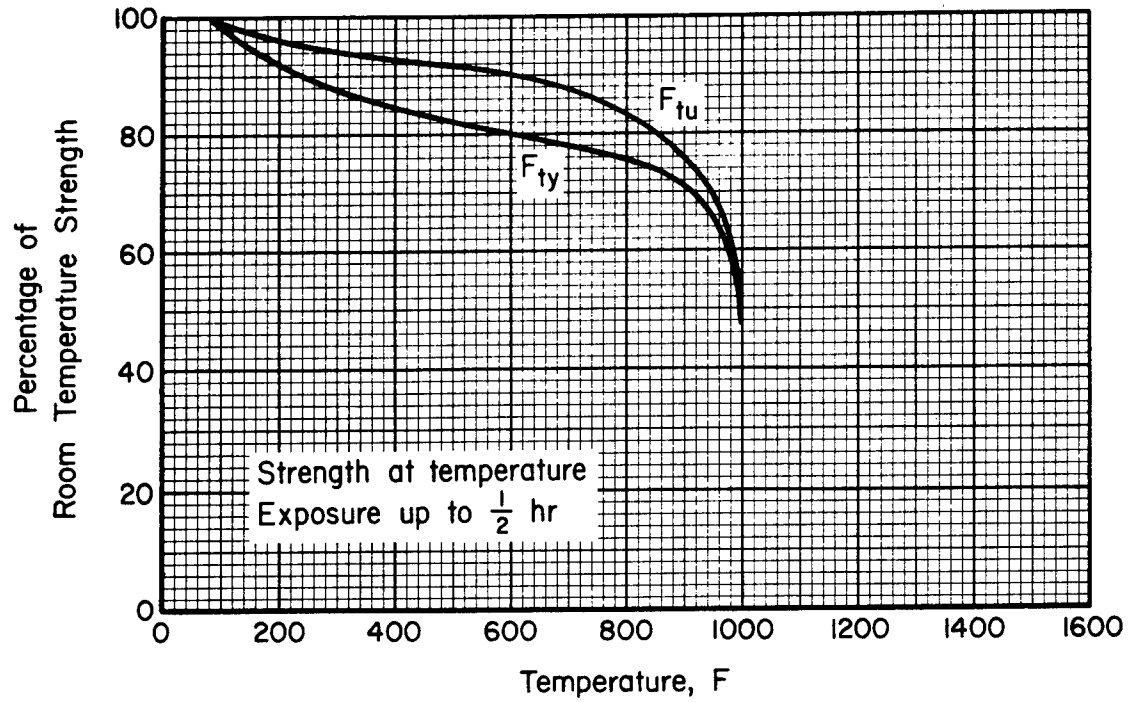


FIGURE 5.5.1.2.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of solution-treated and aged Ti-13V-11Cr-3Al alloy sheet.*

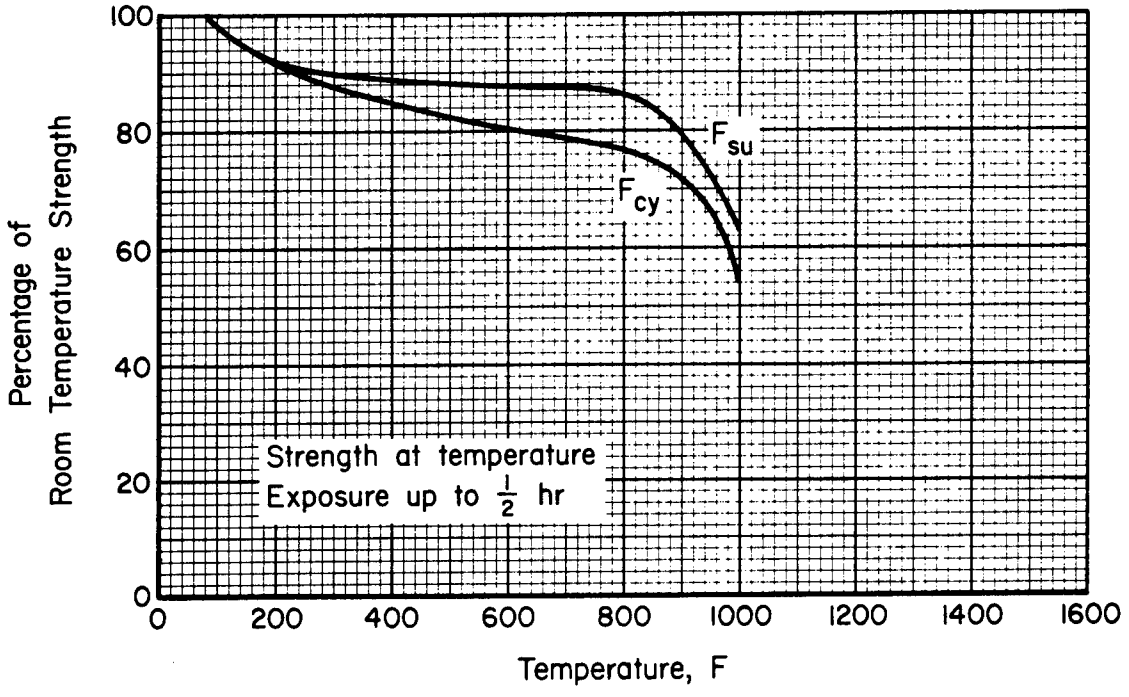


FIGURE 5.5.1.2.2. *Effect of temperature on the compressive yield strength (F_{cy}) and the shear ultimate strength (F_{su}) of solution-treated and aged Ti-13V-11Cr-3Al alloy sheet.*

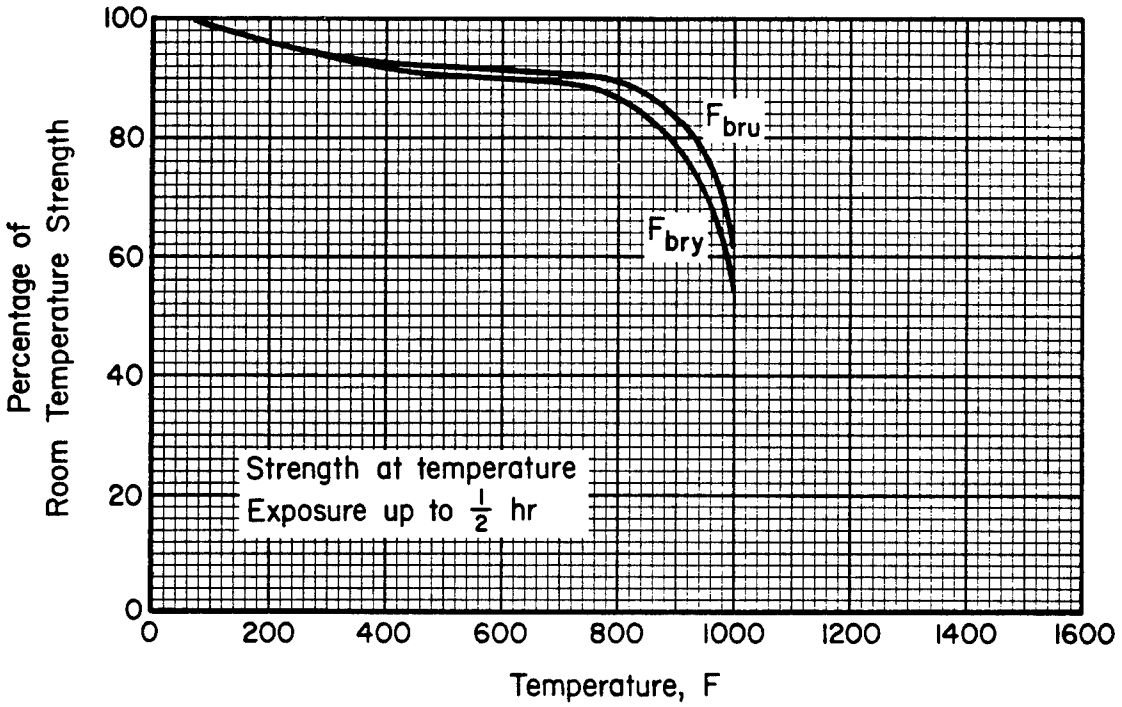


FIGURE 5.5.1.2.3. *Effect of temperature on the bearing ultimate strength (F_{bru}) and the bearing yield strength (F_{bry}) of solution-treated and aged Ti-13V-11Cr-3Al alloy sheet.*

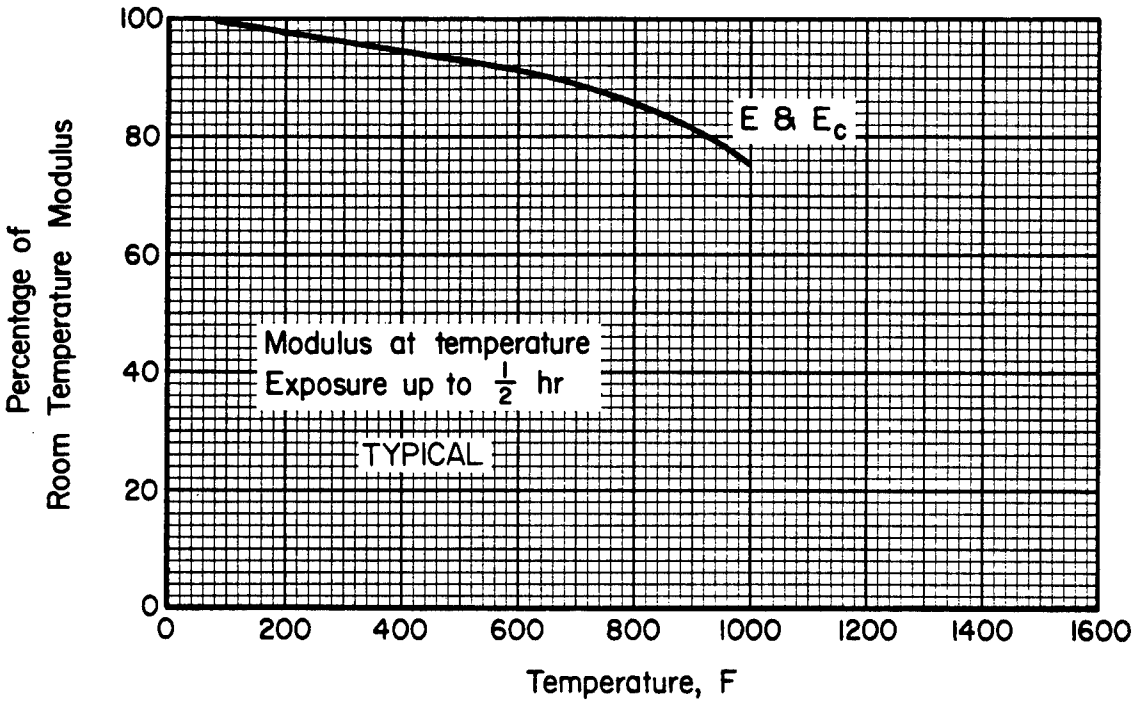


FIGURE 5.5.1.2.4. *Effect of temperature on the tensile and compressive moduli (E and E_c) of solution-treated and aged Ti-13V-11Cr-3Al alloy sheet.*

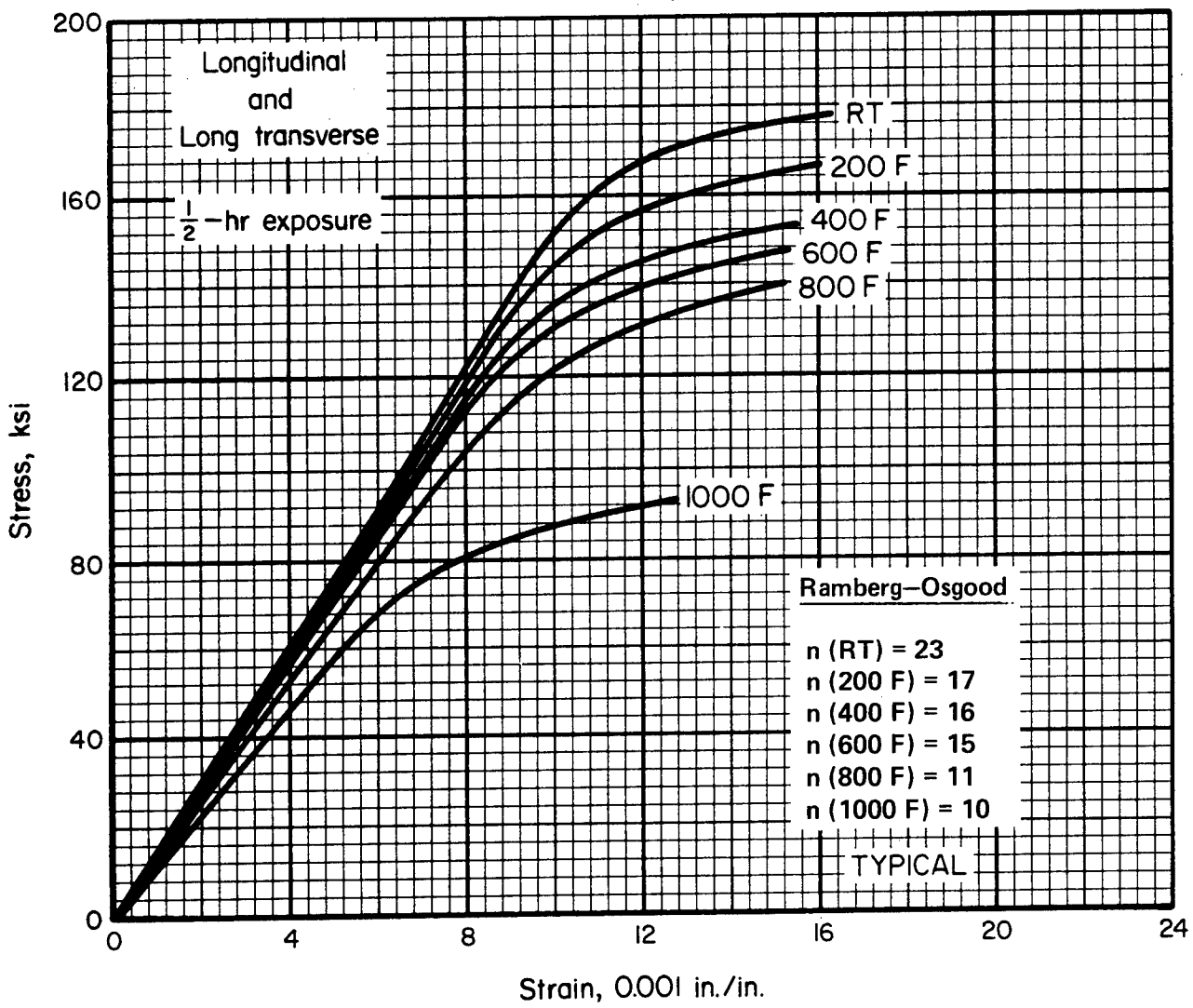


FIGURE 5.5.1.2.6. *Typical tensile stress-strain curves for solution-treated and aged Ti-13V-11Cr-3Al alloy sheet at room and elevated temperatures.*

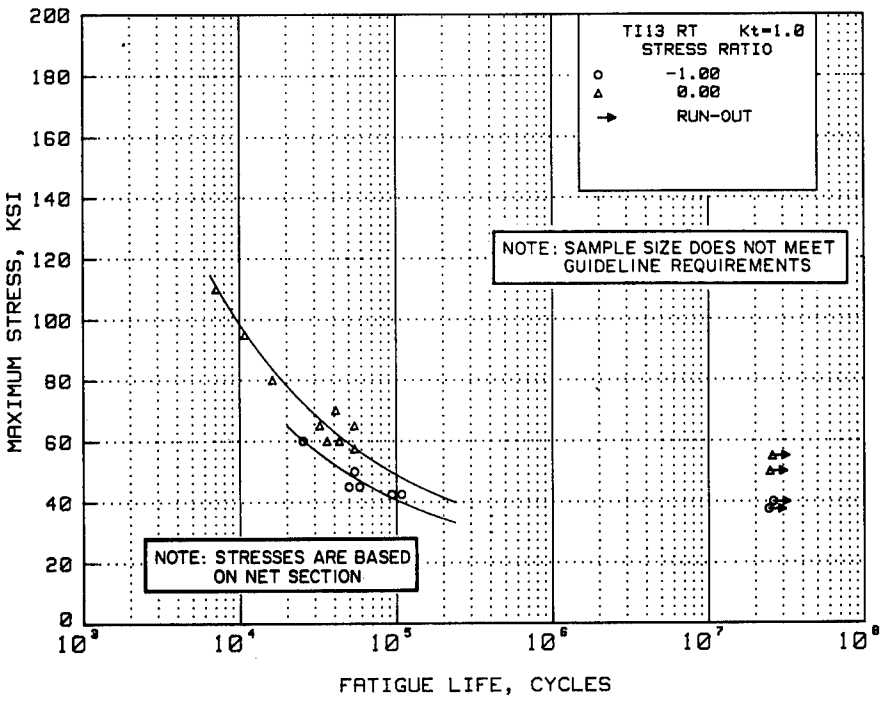


FIGURE 5.5.1.2.8(a). *Best-fit S/N curves for unnotched, solution treated and aged Ti-13V-11Cr-3Al alloy sheet and plate, longitudinal direction.*

Correlative Information for Figure 5.5.1.2.8(a)

Product Form: Sheet, 0.043-inch thick and plate, 1.00-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	174.5	156.7	RT

Specimen Details: Unnotched, 0.30-inch wide
Unnotched, 0.20-inch wide

Surface Condition: As machined, edges polished with emery paper.

As machined, edges were hand-polished.

References: 5.5.1.1.8 and 5.5.1.2.8

Test Parameters:

Loading — Axial
Frequency — 3600 cpm, 10,000 cpm
Temperature — RT
Environment— Air

No. of Heats/Lots: Not specified

Equivalent Stress Equation

$\text{Log } N_f = 8.37\text{-}2.30 \log (S_{eq}\text{-}20)$
$S_{eq} = S_{max} (1\text{-}R)^{0.27}$
Standard Error of Estimate = 0.093
Standard Deviation in Life = 0.31
$R^2 = 91\%$

Sample Size = 17

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

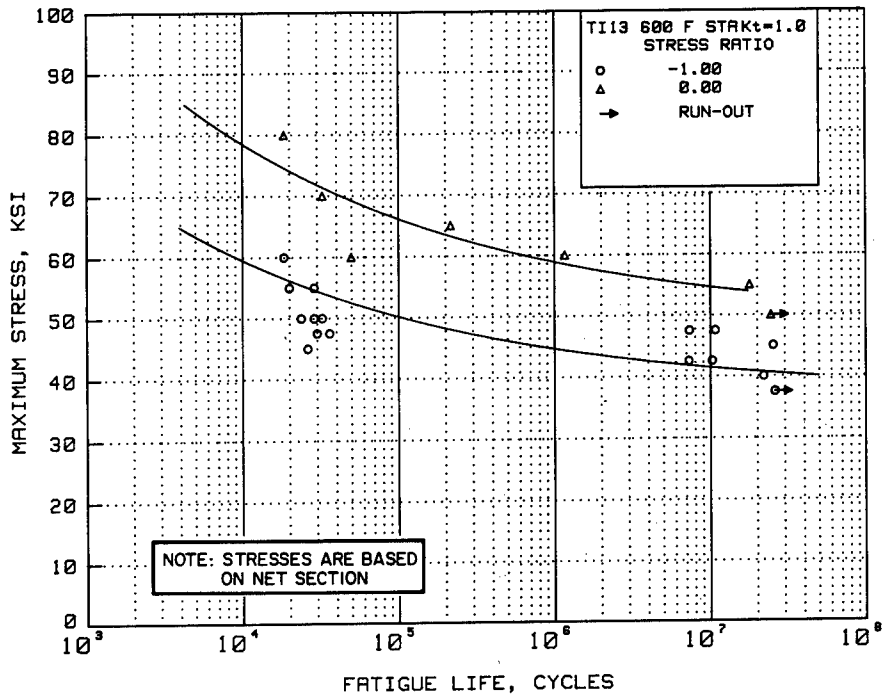


FIGURE 5.5.1.2.8(b). *Best-fit S/N curves for unnotched, solution treated and aged Ti-13V-11Cr-3Al alloy sheet at 600 F, longitudinal direction.*

Correlative Information for Figure 5.5.1.2.8(b)

Product Form: Sheet, 0.043-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	156.30	127.0	600 F

Specimen Details: Unnotched, 0.310-inch wide

Surface Condition: As machined, edges polished with emery paper.

Reference: 5.5.1.1.8

Test Parameters:

Loading — Axial
Frequency — 3600 cpm
Temperature — 600 F
Environment— Air

No. of Heats/Lots: Not specified

Equivalent Stress Equation

$\text{Log } N_f = 10.39\text{-}4.33 \log (S_{eq}\text{-}48.5)$
$S_{eq} = S_{max}\,(i\text{-}R)^{0.40}$
Standard Error of Estimate = 0.90
Standard Deviation in Life = 1.27
$R^2 = 50\%$

Sample Size = 21

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

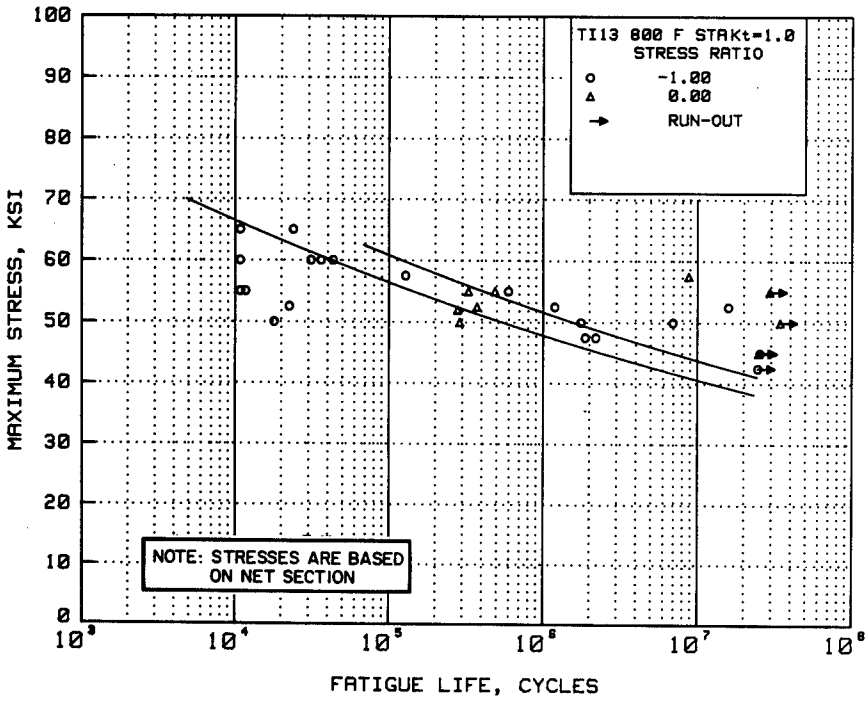


FIGURE 5.5.1.2.8(c). *Best-fit S/N curves for unnotched, solution treated and aged Ti-13V-11Cr-3Al alloy sheet at 800 F, longitudinal direction.*

Correlative Information for Figure 5.5.1.2.8(c)

Product Form: Sheet, 0.043-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp., F
	149.40	122.30	800 F

Specimen Details: Unnotched, 0.30-inch wide

Surface Condition: As machined, edges polished with emery paper.

Reference: 5.5.1.1.8

Test Parameters:

Loading — Axial
Frequency — 3600 cpm
Temperature — 800 F
Environment— Air

No. of Heats/Lots: Not specified

Equivalent Stress Equation

$\text{Log } N_f = 30.03\text{-}14.03 \log (S_{eq})$
$S_{eq} = S_{max} (1\text{-}R)^{0.11}$
Standard Error of Estimate = 0.85
Standard Deviation in Life = 1.01
$R^2 = 29\%$

Sample Size = 24

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

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5.5.2 Ti-15V-3Cr-3Sn-3Al (Ti-15-3)

5.5.2.0 *Comments.*—Ti-15V-3Cr-3Sn-3Al is a solute rich (metastable) beta titanium alloy. It was developed primarily to lower the cost of titanium sheet metal parts by reducing materials and processing cost. Contrary to conventional alpha-beta alloys, this alloy is strip producible and has excellent room temperature formability characteristics. It can also be aged to a wide range of strength levels to meet a variety of application needs. Although this alloy was originally developed as a sheet alloy, it has expanded into other areas such as fasteners, foil, plate, tubing, castings, and forgings.

Manufacturing Considerations.—Ti-15V-3Cr-3Sn-3Al is usually supplied in the solution-annealed condition. In this condition, the alloy has a single phase (beta) structure and, hence, is readily cold formed. After cold forming, the alloy can be resolution-treated in the 1450 F to 1550 F range and subsequently aged in the 900 F to 1100 F range, depending upon desired strength. Care should be exercised to ensure that no surface contamination results from the solution treatment. The alloy can be directly aged after forming; however, strength will vary depending upon the amount of cold work in the part. The alloy can also be hot formed. Heating times prior to hot forming should be minimized in order to prevent appreciable aging prior to forming. Ti-15V-3Cr-3Sn-3Al alloy is readily welded by standard titanium welding techniques.

Environmental Considerations.—In the aged condition, Ti-15V-3Cr-3Sn-3Al appears to be immune to hot-salt stress corrosion cracking below the 500 F to 440 F range. However, some susceptibility has been noted after 100-hour stressed exposures at 600 F. The presence of salt water does not appear to affect the room temperature crack growth behavior of aged material. Alloy Ti-15V-3Cr-3Sn-3Al should not be used in the solution treated condition. Long time exposure of solution treated and cold worked material to service temperatures above approximately 300 F or solution treated material to service temperatures above approximately 400 F can result in low ductility. Under certain conditions, titanium, when in contact with cadmium, silver, mercury, or certain of their compounds, may become embrittled. Refer to MIL-S-5002 and MIL-STD-1568 for restrictions concerning such applications.

Heat Treatment.—This alloy should be solution treated for 10-30 minutes in the 1450 F to 1550 F range, cooled at a rate approximating an air cool of 0.125 inch thick sheet and subsequently aged. Aging is generally conducted in the 900 F to 1100 F range, followed by an air cool. Aging times will vary depending upon aging temperature. The material can be used in service in the solution treated condition subject to the temperature limitations described above.

Specifications and Properties.—A material specification for Ti-15V-3Cr-3Sn-3Al is shown in Table 5.5.2.0(a). Room-temperature mechanical properties for Ti-15V-3Cr-3Sn-3Al are shown in Table 5.5.2.0(b). The effect of temperature on physical properties is shown in Figure 5.5.2.0.

TABLE 5.5.2.0(a). *Material Specification for Ti-15V-3Cr-3Sn-3Al*

Specification	Form
AMS 4914	Sheet and strip

5.5.2.1 *Solution-Treated and Aged (1000 F) Condition.*—Typical tensile and compressive stress-strain and compressive tangent-modulus curves are presented in Figures 5.5.2.1.6(a) and (b).

TABLE 5.5.2.0(b). *Design Mechanical and Physical Properties of Ti-15V-3Cr-3Sn-3Al Sheet*

Specification	AMS 4914
Form	Sheet
Condition	STA (1000 F/8 Hrs.)
Thickness, in.	≤0.125
Basis	S
Mechanical Properties:	
F_{tu}, ksi:	
L	145
LT	145
F_{ty}, ksi:	
L	140
LT	140
F_{cy}, ksi:	
L	139
LT	144
F_{su}, ksi	92
F_{bru}[a], ksi:	
(e/D = 1.5)	216
(e/D = 2.0)	276
F_{bry}[a], ksi:	
(e/D = 1.5)	203
(e/D = 2.0)	233
e, percent:	
L	7
LT	7
E, 10^3 ksi:	
L	15.2
LT	15.7
E_c, 10^3, ksi:	
L	15.3
LT	16.0
G, 10^3, ksi	...
μ	...
Physical Properties:	
ω, lb/in.^{3}	0.172
C, *K*, and α	See Figure 5.5.2.0

[a]Bearing values are "dry pin" values per Section 1.4.7.1.

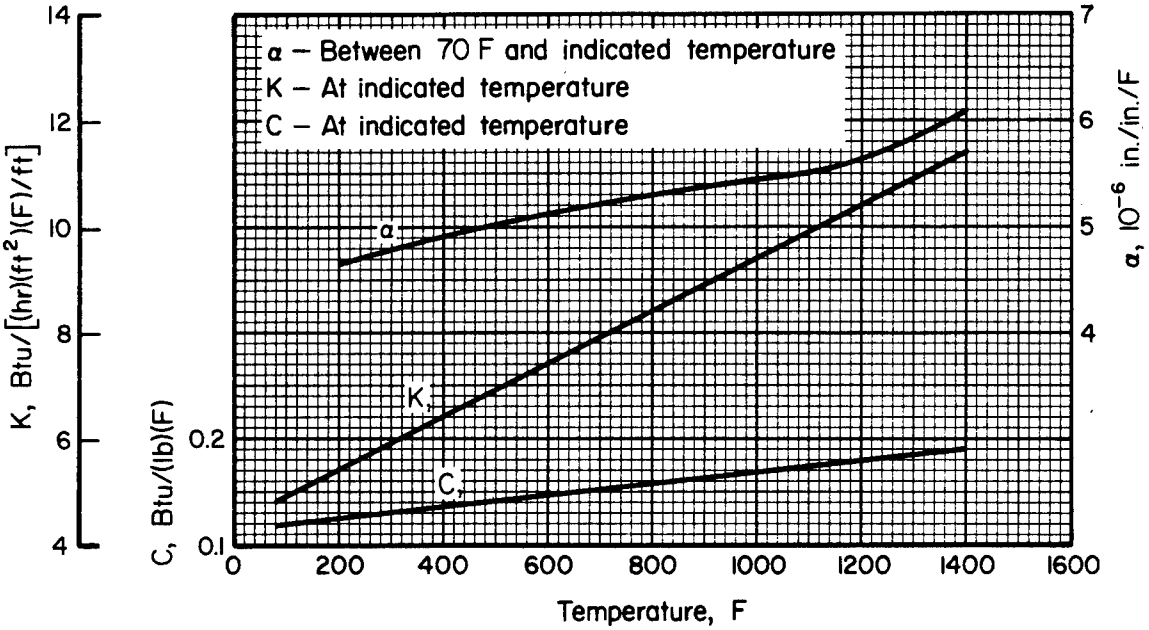


FIGURE 5.5.2.0. *Effect of temperature on the physical properties of Ti-15V-3Cr-3Sn-3Al alloy.*

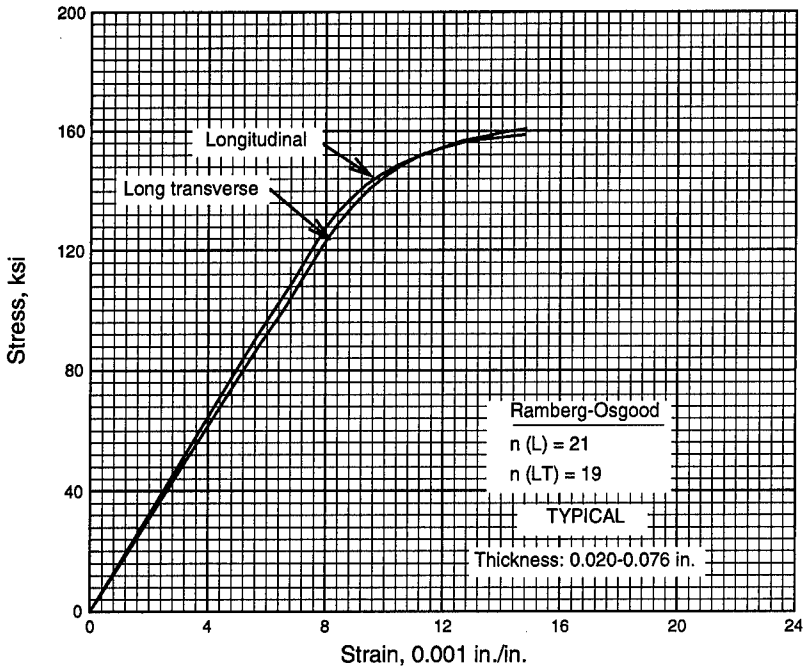


FIGURE 5.5.2.1.6(a). *Typical tensile stress-strain curves at room temperature for solution treated and aged (1000 F) Ti-15V-3Cr-3Sn-3Al alloy sheet.*

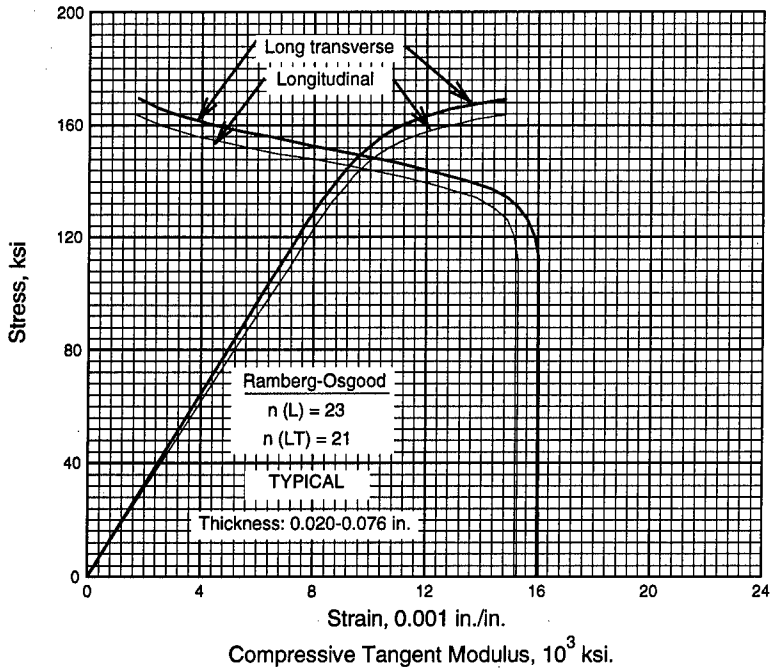


FIGURE 5.5.2.1.6(b). *Typical compressive stress-strain and compressive tangent-modulus curves at room temperature for solution treated and aged (1000 F) Ti-15V-3Cr-3Sn-3Al alloy sheet.*

5.5.3 Ti-10V-2Fe-3Al (Ti-10-2-3)

5.5.3.0 Comments and Properties.—Ti-10V-2Fe-3Al is a solute lean beta (near beta) titanium alloy that was developed primarily as a high strength forging alloy. It has excellent forging characteristics, possessing flow properties at 1500 F similar to Ti-6Al-4V at 1700 F. This characteristics provides advantages, such as lower die cost and better die fill capability. This alloy also provides the best combination of strength and toughness of any of the commercially available titanium alloys. For example, at the 180 ksi tensile ultimate strength level, the alloy has a K_{Ic} value of 40 ksi-in.$^{1/2}$ minimum.

In addition to this high strength condition, the alloy can also be processed to intermediate strength levels for higher fracture toughness. This alloy has also been reported to exhibit a shape-memory effect.

Manufacturing Considerations.—Ti-10V-2Fe-3Al is usually supplied as bar or billet product which has been finish forged (or rolled) in the alpha-beta field. In order to optimize the microstructure for the high strength condition, the forging is usually given a pre-form forge above the beta transus, followed by a 15 to 25 percent reduction below the beta transus. Ideally, the beta forging operation is finished through the beta transus, followed by a quench. The intent of the two-step forging process is to develop a structure without grain boundary alpha, but with elongated primary alpha needles in an aged beta matrix. The alloy is considered to be deep hardenable, capable of generating high strengths in section thicknesses up to approximately 5 inches. The alloy is also readily weldable by conventional titanium welding techniques.

Environmental Consideration.—In the solution treated plus aged condition, the material exhibits excellent resistance to stress corrosion cracking, typically exhibiting a $K_{Iscc} > 0.8\ K_{Ic}$, In the solution-treated condition, the material should not be subjected to long term exposure in the 500 to 800 F range, since such exposure could result in high strength, low ductility conditions. Exposure to cadmium, silver, mercury, or certain other compounds should be avoided. Refer to MIL-STD-1568 and MIL-S-5002.

Heat Treatment.—For the high strength condition, the alloy is generally solution treated approximately 65 F below the beta transus (which is typically 1460 to 1480 F), followed by a water quench and an 8-hour age at 900 to 950 F. Overaging in the 950 F to 1150 F range may also be used to obtain lower strength levels.

Beta Flecks.—Ti-10V-2Fe-3Al is a segregation prone alloy which can exhibit a microstructural phenomenon known as "beta-flecks". Certain areas may possess a lower beta transus than the matrix (due primarily to beta stabilizer enrichment) and, as such, can fully transform during heat treatment just below the matrix transus. In severe cases, this condition can lead to lower ductility and a reduction in fatigue strength due to grain boundary alpha formation in the "flecked" region. Care should be exercised to procure only material which has been melted under strict control to prevent severe "fleck" formation.

Specifications and Properties.—Material specifications for Ti-10V-2Fe-3Al are shown in Table 5.5.3.0(a). Room temperature mechanical properties for Ti-10V-2Fe-3Al are presented in Table 5.5.3.0(b).

TABLE 5.5.3.0(a). *Material Specifications for Ti-10V-2Fe-3Al*

Specification	Form
AMS 4983	Forging
AMS 4984	Forging
AMS 4986	Forging

5.5.3.1 *Solution Treated and Aged (900 to 950 F) Condition.*—Typical tensile and compressive stress-strain and compressive tangent-modulus curves are presented in Figure 5.5.3.1.6.

5.5.3.2 *Solution Treated and Aged (950 to 1000 F) Condition.*—Typical tensile and compressive stress-strain and compressive tangent-modulus curves are shown in Figure 5.5.3.2.6.

TABLE 5.5.3.0(b). *Design Mechanical and Physical Properties of Ti-10V-2Fe-3Al Die Forging*

Specification	AMS 4983	AMS 4984
Form	Conventional die forging	
Condition	Solution treated and aged (900-950 F)	
Thickness, in.	<1.000	≤3.000
Basis	S	S
Mechanical Properties:		
F_{tu}, ksi:		
L	180	173
LT	180[b]	173[b]
ST	...	173[b]
F_{ty}, ksi:		
L	160	160
LT	160[b]	160[b]
ST	...	160[b]
F_{cy}, ksi:		
L	168	168
LT	166	166
ST	...	166
F_{su}, ksi	101	97
F_{bru}[a], ksi:		
(e/D = 1.5)	244	234
(e/D = 2.0)	295	284
F_{bry}[a], ksi:		
(e/D = 1.5)	227	227
(e/D = 2.0)	261	261
e, percent:		
L	4	4
LT	4[b]	4[b]
ST	...	4[b]
E, 10^3 ksi	15.9	
E_c, 10^3, ksi	16.3	
G, 10^3, ksi	...	
μ	...	
Physical Properties:		
ω, lb/in.^{3}	0.168	
a, 10^{-6} in./in./F	5.4 (68-800 F)	
C and K	...	

[a]Bearing values are "dry pin" values per Section 1.4.7.1.
[b]Applicable providing LT or ST dimension is ≥2.500 inches.

TABLE 5.5.3.0(c). *Design Mechanical and Physical Properties of Ti-10V-3Al Hand Forging*

Specification	AMS 4986	
Form	Hand forging	
Condition	Solution treated and aged (950-1000 F)	
Thickness, in.	≤3.000	3.001-4.000
Basis	S	S
Mechanical Properties:		
F_{tu}, ksi:		
L	160	160
LT	160[a]	160
F_{ty}, ksi:		
L	145	145
LT	145[a]	145
F_{cy}, ksi:		
L	154	...
LT	...	...
F_{su}, ksi	97[b]	...
F_{bru}[c], ksi:		
(e/D = 1.5)	241	...
(e/D = 2.0)	293	...
F_{bry}[c], ksi:		
(e/D = 1.5)	218	...
(e/D = 2.0)	245	...
e, percent:		
L	6	6
LT	6[a]	6
RA, percent:		
L	10	10
LT	10[a]	10
E, 10^3 ksi	15.9	
E_c, 10^3 ksi	16.3	
G, 10^3 ksi	...	
μ	...	
Physical Properties:		
ω, lb/in.^{3}	0.168	
a, 10^{-6} in./in./F	5.4 (68-800 F)	
C and K	...	

[a]Applicalbe providing LT dimension is ≥2.500 inches.
[b]Shear strength determined in accordance with ASSTM B 769.
[c]Bearing values are "dry pin" per Section 1.4.7.1.

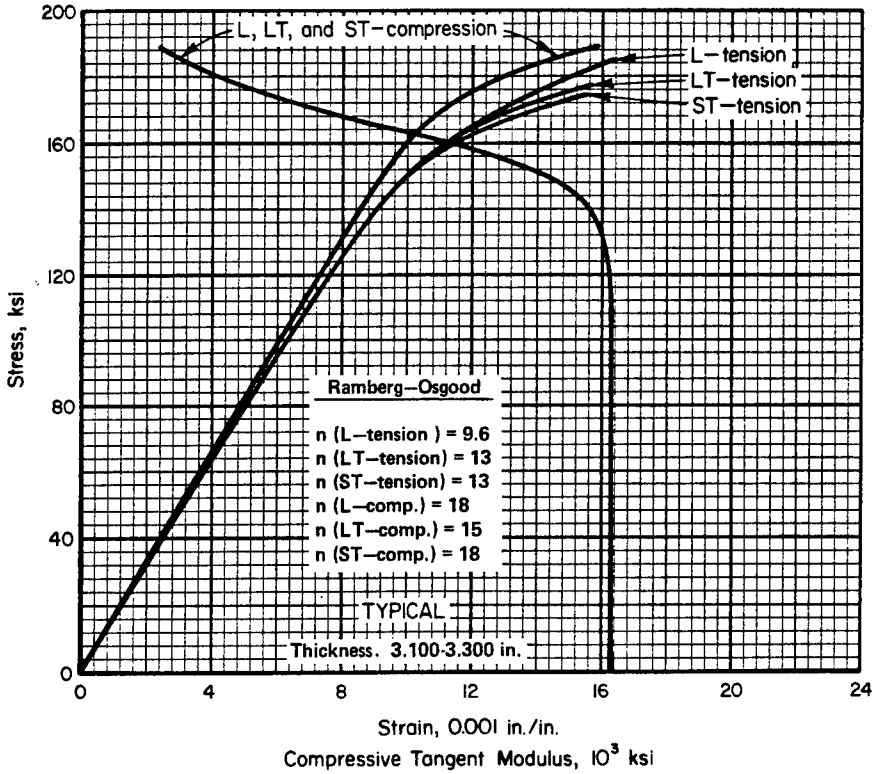


FIGURE 5.5.3.1.6. *Typical tensile stress-strain, compressive stress-strain, and compressive tangent-modulus curves for solution treated and aged (900-950 F) Ti-10V-2Fe-3Al die forging.*

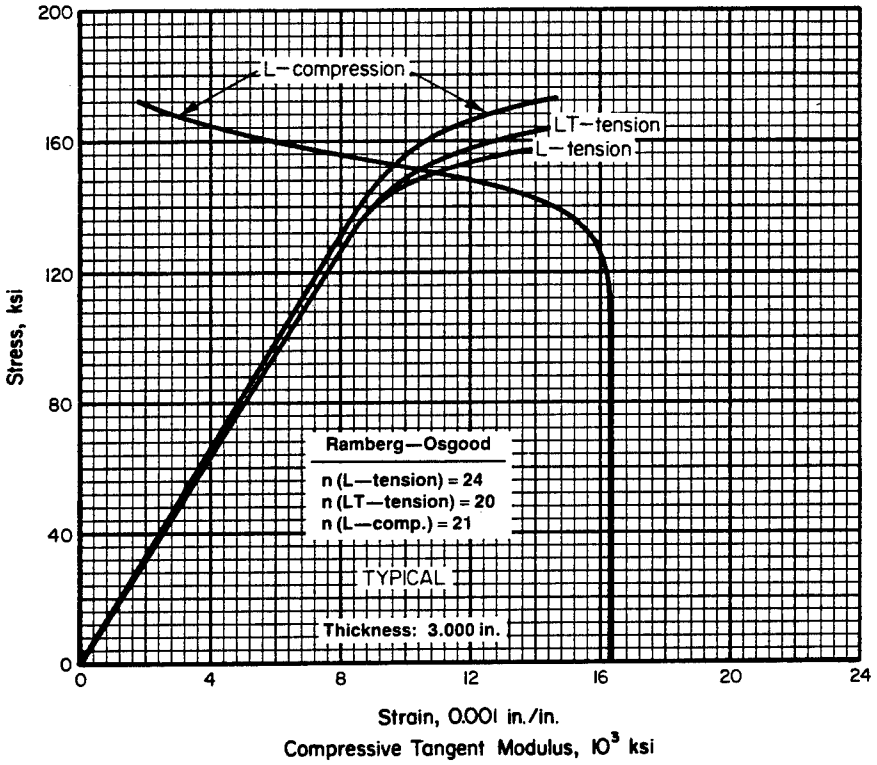


FIGURE 5.5.3.2.6. *Typical stress-strain, compressive stress-strain, and compressive tangent-modulus curves for solution treated and aged (950-1000 F) Ti-10V-2Fe-3Al hand forging.*

5.6 Element Properties

5.6.1 BEAMS.—See Equation 1.3.2.3, Section 1.5.2.5, and References 1.7.1(a) and (b) for general information on stress analysis of beams.

5.6.1.1 *Simple Beams.*—Beams of solid, tubular, or similar cross sections can be assumed to fail through exceeding an allowable modulus of rupture in bending (F_b). In the absence of specific data, the ratio F_b/F_{tu} can be assumed to be 1.25 for solid sections.

5.6.1.1.1 Round Tubes.—For round tubes, the value of F_b will depend on the D/t ratio as well as the ultimate tensile stress. The bending modulus of rupture of 6Al-4V titanium alloy is given in Figure 5.6.1.1.1.

5.6.1.1.2 Unconventional Cross Sections.—Sections other than solid or tubular should be tested to determine the allowable bending stress.

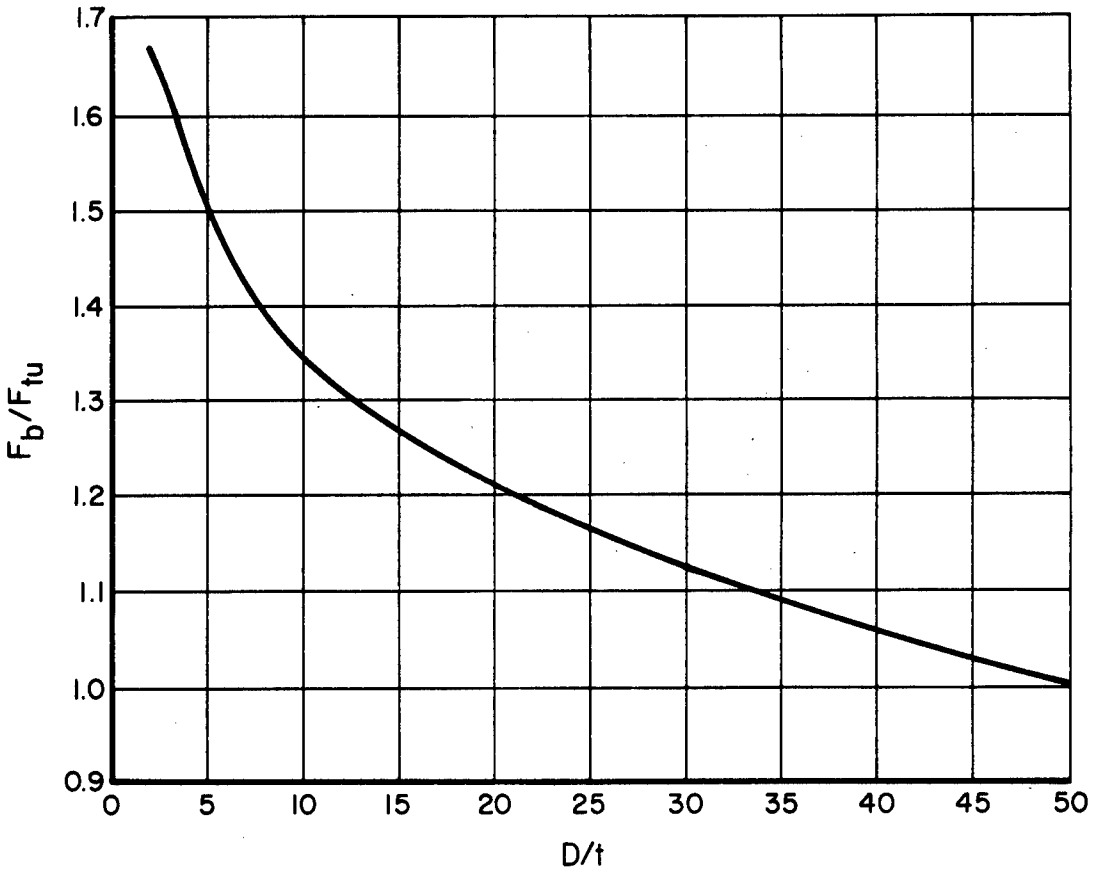


FIGURE 5.6.1.1.1. *Bending modulus of rupture for solution-treated and aged Ti-6Al-4V alloy round tubing manufactured from bar material.*

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REFERENCES

5.1.2(a) Jaffe, R. I., "The Physical Metallurgy of Titanium Alloys", Progress in Metal Physics, Vol. 7, Pergammon Press, Oxford, England, pp 65-167 (1958).

5.1.2(b) "Aircraft Designer's Handbook for Titanium and Titanium Alloys", AFML-TR-67-142 (March 1967).

5.1.2(c) Larson, F. R., "Anisotropy in Titanium Sheet in Uniaxial Tension", *ASM Transactions*, **57**, pp 620-631 (1964).

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Chapter 6

HEAT-RESISTANT ALLOYS

6.1 General

Heat-resistant alloys are arbitrarily defined as iron alloys richer in alloy content than the 18 percent chromium, 8 percent nickel types, or as alloys with a base element other than iron and which are intended for elevated-temperature service. These alloys have adequate oxidation resistance for service at elevated temperatures and are normally used without special surface protection. So-called "refractory" alloys that require special surface protection for elevated-temperature service are not included in this chapter.

This chapter contains strength properties and related characteristics of wrought heat-resistant alloy products used in aerospace vehicles. The strength properties are those commonly used in structural design, such as tension, compression, bearing, and shear. The effects of elevated temperature are presented. Factors such as metallurgical considerations influencing the selection of metals are included in comments preceding the specific properties of each alloy or alloy group. Data on creep, stress-rupture, and fatigue strength, as well as crack-growth characteristics are presented in the applicable alloy section.

There is no standardized numbering system for the alloys in this chapter. For this reason, each alloy is identified by its most widely accepted trade designation.

For convenience in presenting these alloys and their properties, the heat-resistant alloys have been divided into three groups, based on alloy composition. These groups and the alloys for which specifications and properties are included as shown in Table 6.1.

TABLE 6.1. *Heat-Resistant Alloys Index*

Section	Designation
6.2	**Iron-Chromium-Nickel-Base Alloys**
6.2.1	A-286
6.2.2	N-155
6.3	**Nickel-Base Alloys**
6.3.1	Hastelloy X
6.3.2	Inconel Alloy 600 (Inconel)
6.3.3	Inconel 625
6.3.4	Inconel 706
6.3.5	Inconel 718
6.3.6	Inconel Alloy X-750 (Inconel X)
6.3.7	René 41
6.3.8	Waspaloy
6.4	**Cobalt-Base Alloys**
6.4.1	L-605
6.4.2	Alloy 188

The heat treatments applied to the alloys in this chapter vary considerably from one alloy to another. For uniformity of presentation, the heat-treating terms are defined as follows:

Stress-Relieving.—Heating to a suitable temperature, holding long enough to reduce residual stresses, and cooling in air or as prescribed.

Annealing.—Heating to a suitable temperature, holding, and cooling at a suitable rate for the purpose of obtaining minimum hardness or strength.

Solution-Treating.—Heating to a suitable temperature, holding long enough to allow one or more constituents to enter into solid solution, and cooling rapidly enough to hold the constituents in solution.

Aging, Precipitation-Hardening.—Heating to a suitable temperature and holding long enough to obtain hardening by the precipitation of a constituent from the solution-treated condition.

The actual temperatures, holding times, and heating and cooling rates used in these treatments vary from alloy to alloy and are described in the applicable specifications.

6.1.1 MATERIAL PROPERTIES

6.1.1.1 *Mechanical Properties.*—The mechanical properties of the heat-resistant alloys are affected by relatively minor variations in chemistry, processing, and heat treatment. Consequently, the mechanical properties shown for the various alloys in this chapter are intended to apply only to the alloy, form (shape), size (thickness), and heat treatment indicated. When statistical values are shown, these are intended to represent a fair cross section of all mill production within the indicated scope.

Strength Properties.—Room-temperature strength properties for alloys in this chapter are based primarily on minimum tensile property requirements of material specifications. Values for nonspecification strength properties are derived. The variation of properties with temperature and other data of interest are presented in figures or tables, as appropriate.

The strength properties of the heat-resistant alloys generally decrease with increasing temperatures or increasing time at temperature. There are exceptions to this statement, particularly in the case of age-hardening alloys; these alloys may actually show an increase in strength with temperature or time, within a limited range, as a result of further aging. In most cases, however, this increase in strength is temporary and, furthermore, cannot usually be taken advantage of in service. For this reason, this increase in strength has been ignored in the preparation of elevated temperature curves as described in Chapter 9.

At cryogenic temperatures, the strength properties of the heat-resistant alloys are generally higher than at room temperature, provided some ductility is retained at the low temperatures. For additional information on mechanical properties at cryogenic temperatures, other references, such as the Cryogenic Materials Data Handbook (OTS PB 161093), should be consulted.

Ductility.—Specified minimum ductility requirements are presented for these alloys in the room-temperature property tables. The variation in ductility with temperature is somewhat erratic for the heat-resistant alloys. Generally, ductility decreases with increasing temperature from room temperature up to about 1200 to 1400 F, where it reaches a minimum value, then it increases with higher temperatures. Prior creep exposure may also affect ductility adversely. Below room temperature, ductility decreases with decreasing temperature for some of these alloys.

Stress-Strain Relationships.—The stress-strain relationships presented are typical curves prepared as described in Section 9.3.2.

Creep.—Data covering the temperatures and times of exposure and the creep deformations of interest are included as typical information in individual material sections. These presentations may be in the form of creep stress-lifetime curves for various deformation criteria as specified in Chapter 9 or as a creep nomographs.

Fatigue.—Fatigue S/N curves for unnotched and notched specimens at room temperature and elevated temperatures are shown in each alloy section. Fatigue crack propagation data are also presented.

6.1.1.2 *Physical Properties.*—Selected physical-property data are presented for these alloys. Processing variables and heat treatment have only a slight effect on these values; thus, the properties listed are applicable to all forms and heat treatments.

6.2 Iron-Chromium-Nickel-Base Alloys

6.2.0 GENERAL COMMENTS.—The alloys in this group, interms of cost and in maximum service temperature, generally fall between the austenitic stainless steels and the nickel- and cobalt-base alloys. They are used in airframes, principally, in the temperature range 1000 to 1200 F, in those applications in which the stainless steels are inadequate and service requirements do not justify the use of the more costly nickel or cobalt alloys.

6.2.0.1 *Metallurgical Considerations.*

Composition.—The complex-base alloys comprising this group range from those in which iron is considered the base element to those which border on the nickel-base alloys. All of them contain sufficient alloying elements to place them in the "Superalloy" category, yet contain enough iron to reduce their cost considerably.

Chromium, in amounts ranging from 10 to 20 percent or higher, primarily increases oxidation resistance and contributes to strengthening of these alloys. Nickel and cobalt strengthen and toughen these materials. Molybdenum, tungsten, and columbium contribute to hardness and strength, particularly at elevated temperatures. Titanium and aluminum are added to provide age-hardening.

Heat Treatment.—The complex-base alloys are heat treated with conventional equipment and fixtures such as would be used for austenitic stainless steels. Since these alloys are susceptible to carburization during heat treatment, it is good practice to remove all grease, oil, cutting lubricant, etc., from the surface before heating. A low-sulfur and neutral or slightly oxidizing furnace atmosphere is recommended for heating.

6.2.0.2 *Manufacturing Considerations.*—The iron-chromium-nickel-base alloys closely resemble the austenitic stainless steels insofar as forging, cold forming, machining, welding, and brazing are concerned. Their higher strength may require the use of heavier forging or forming equipment, and machining is somewhat more difficult than for the stainless steels. Pertinent comments are included under the individual alloys.

6.2.1 A-286

6.2.1.0 *Comments and Properties.*—A-286 is a precipitation-hardening iron-base alloy designed for parts requiring high strength up to 1300 F and oxidation resistance up to 1500 F. It is used in jet engines and gas turbines for parts such as turbine buckets, bolts, and discs, and sheet metal assemblies. A-286 is available in the usual mill forms.

A-286 is somewhat harder to hot or cold work than the austenitic stainless steels. Its forging range is 2150 to 1800 F; when finishing below 1800 F, light reductions (under 15 percent) must be avoided to prevent grain coarsening during subsequent heat treatment. A-286 is readily machined in the partially or fully aged condition but is soft and "gummy" in the solution-treated condition. A-286 should be welded in the solution-treated condition. Fusion welding is difficult for large section sizes and moderately difficult for small cross sections and sheet. Cracking may be encountered in the welding of heavy sections or parts under high restraint. A dimensional contraction of 0.0008 inch per inch is experienced during aging. Oxidation resistance of A-286 is equivalent to that of Type 310 stainless steel up to 1800 F.

Some material specifications for A-286 alloy are presented in Table 6.2.1.0(a). Room-temperature mechanical and physical properties are shown in Table 6.2.1.0(b). The effect of temperature on physical properties is shown in Figure 6.2.1.0.

6.2.1.1 *Solution-Treated and Aged Condition.*—Elevated-temperature data are presented in Figures 6.2.1.1.1, 6.2.1.1.3, and 6.2.1.1.4(a) through (c). Stress rupture properties are specified at 1200 F; the appropriate specifications should be consulted for detailed requirements. Figures 6.2.1.1.8(a) through (e) are fatigue S/N curves for several elevated temperatures.

TABLE 6.2.1.0(a). *Material Specifications for A-286 Alloy*

Specification	Form	Condition
AMS 5525	Sheet, strip, and plate	Solution treated (1800 F)
AMS 5731	Bar, forging, tubing, and ring	Solution treated (1800 F)
AMS 5732	Bar, forging, tubing, and ring	Solution treated (1800 F) and aged
AMS 5734	Bar, forging, and tubing	Solution treated (1650 F)
AMS 5737	Bar, forging, and tubing	Solution treated (1650 F) and aged

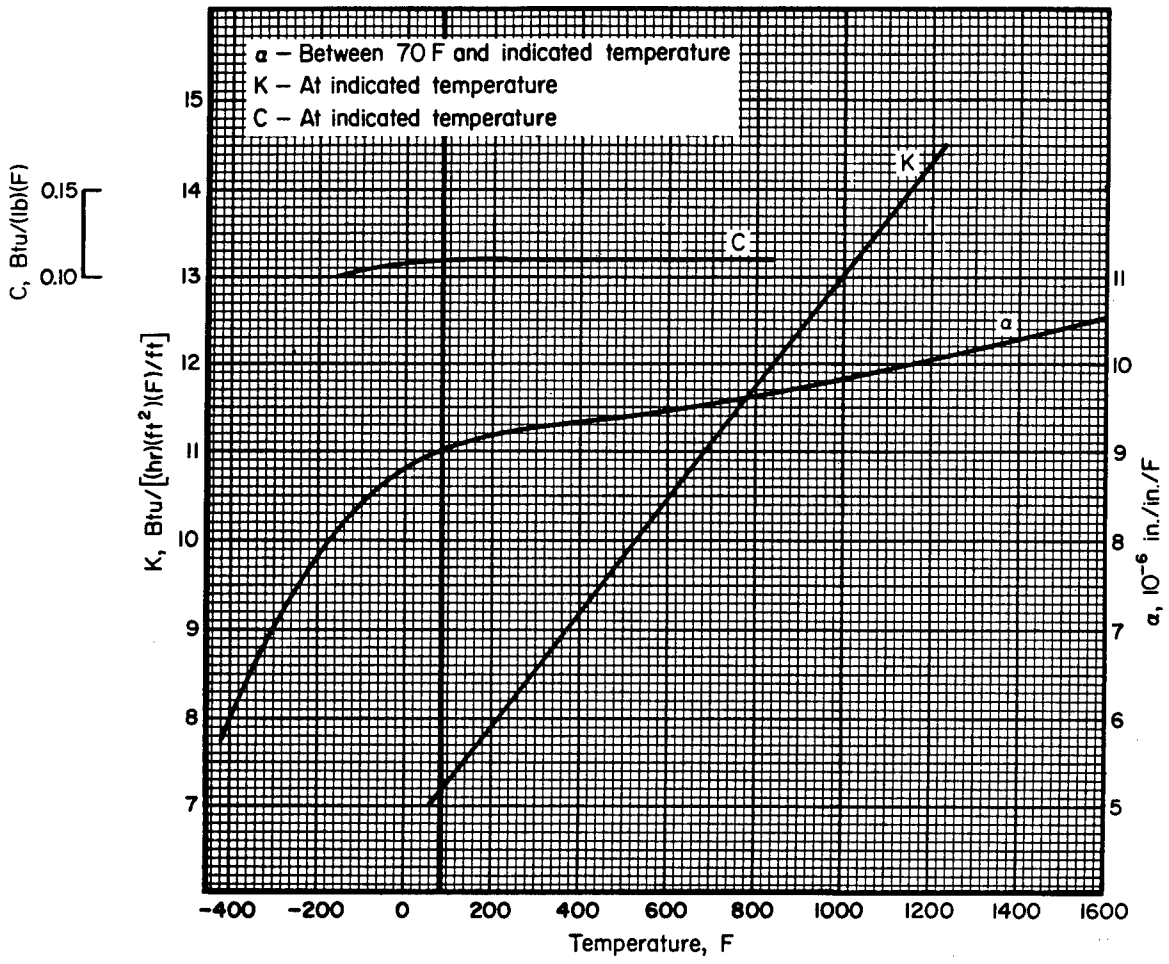


FIGURE 6.2.1.0. *Effect of temperature on the physical properties of A-286.*

TABLE 6.2.1.0(b). *Design Mechanical and Physical Properties of A-286 Alloy*

Specification	AMS 5525	AMS 5731 AMS 5732	AMS 5734 AMS 5737		
Form	Sheet, strip, and plate	Bar			
Condition	Solution treated and aged				
Thickness or diameter, in.	>0.004	≤2.499	2.500-5.000	≤2.499	2.500-5.000
Basis	S[a]	S	S	S	S
Mechanical Properties:					
F_{tu}, ksi:					
L	...	130	130	140	140
LT	140	130[b]	130	140[b]	140
ST	...	...	130	...	140
F_{ty}, ksi:					
L	...	85	85	95	95
LT	95	85[b]	85	95[b]	95
ST	...	...	85	...	95
F_{cy}, ksi:					
L	...	85	85	95	95
LT	95	...	...	...	...
F_{su}, ksi	91	85	85	91	91
F_{bru}, ksi:					
(e/D = 1.5)	210	195	195	210	210
(e/D = 2.0)	266	247	247	266	266
F_{bry}, ksi:					
(e/D = 1.5)	142	127	127	142	142
(e/D = 2.0)	171	153	153	171	171
e, percent:					
L	...	15	15	12	12
LT	15	15[b]	15	12[b]	12
ST	...	...	15	...	12
RA, percent:					
L	...	20	20	15	15
LT	...	20[b]	20	15[b]	15
ST	...	...	20	...	15
E, 10^3 ksi	29.1				
E_c, 10^3 ksi	29.1				
G, 10^3 ksi	11.1				
μ	0.31				
Physical Properties:					
ω, lb/in.^{3}	0.287				
C, K, and α	See Figure 6.2.1.0				

[a]Test direction longitudinal for widths less than 9 inches; transverse for widths 9 inches and over.
[b]Applicable to widths ≥2.500 inches only.

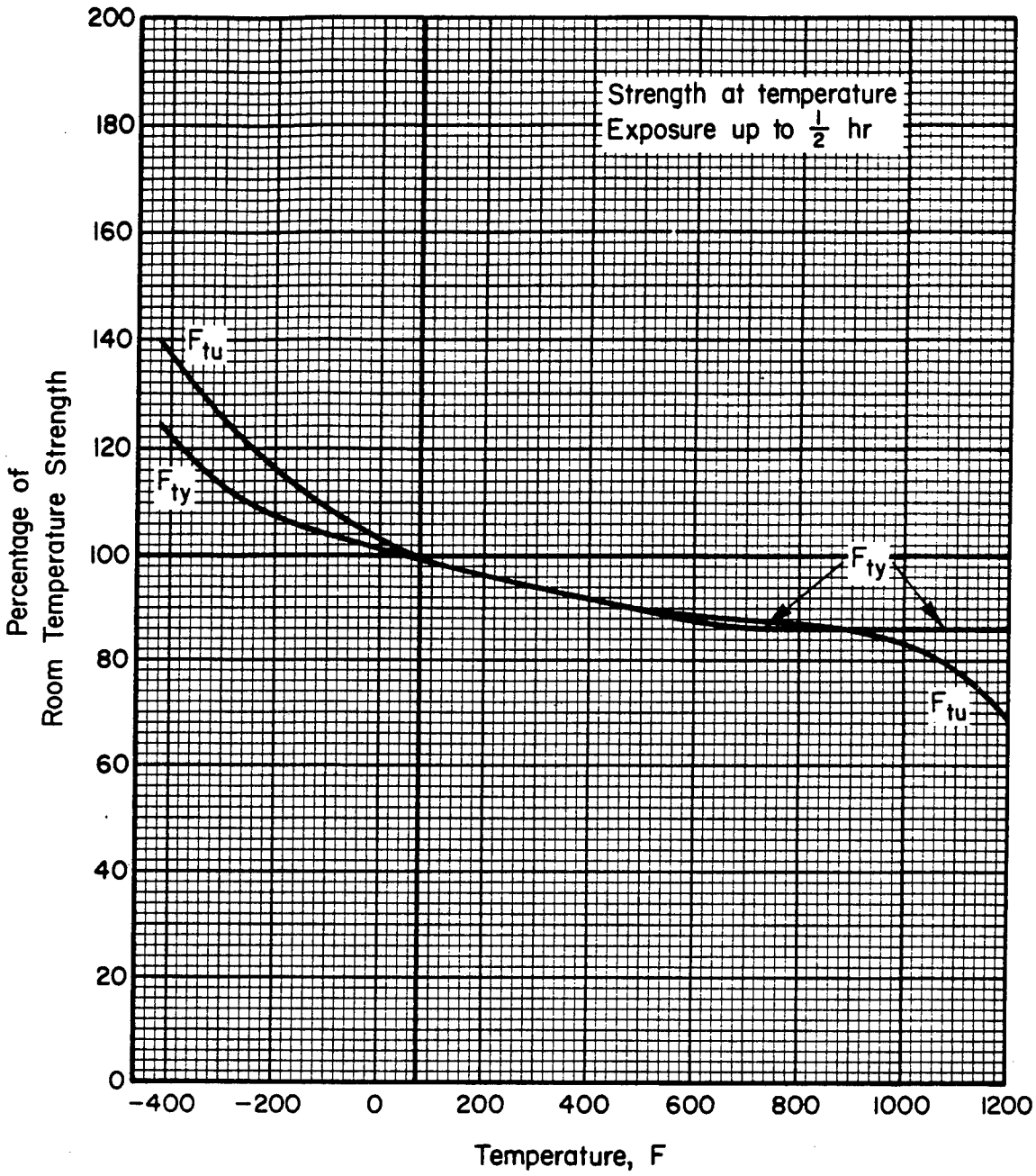


FIGURE 6.2.1.1.1. *Effect of temperature on the tensile yield strength (F_{ty}) and tensile ultimate strength (F_{tu}) of A-286 alloy (1800 F solution treatment temperature).*

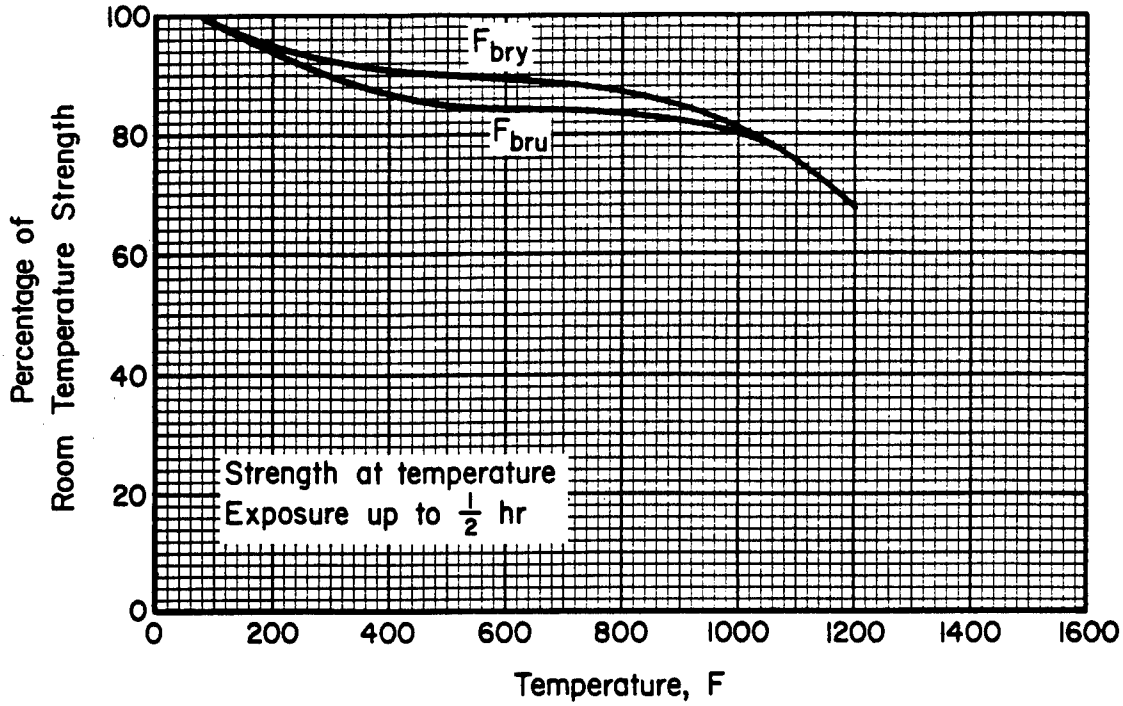


FIGURE 6.2.1.1.3. *Effect of temperature on the bearing ultimate strength (F_{bru}) and the bearing yield strength (F_{bry}) for A-286 alloy (1800 F solution treatment temperature).*

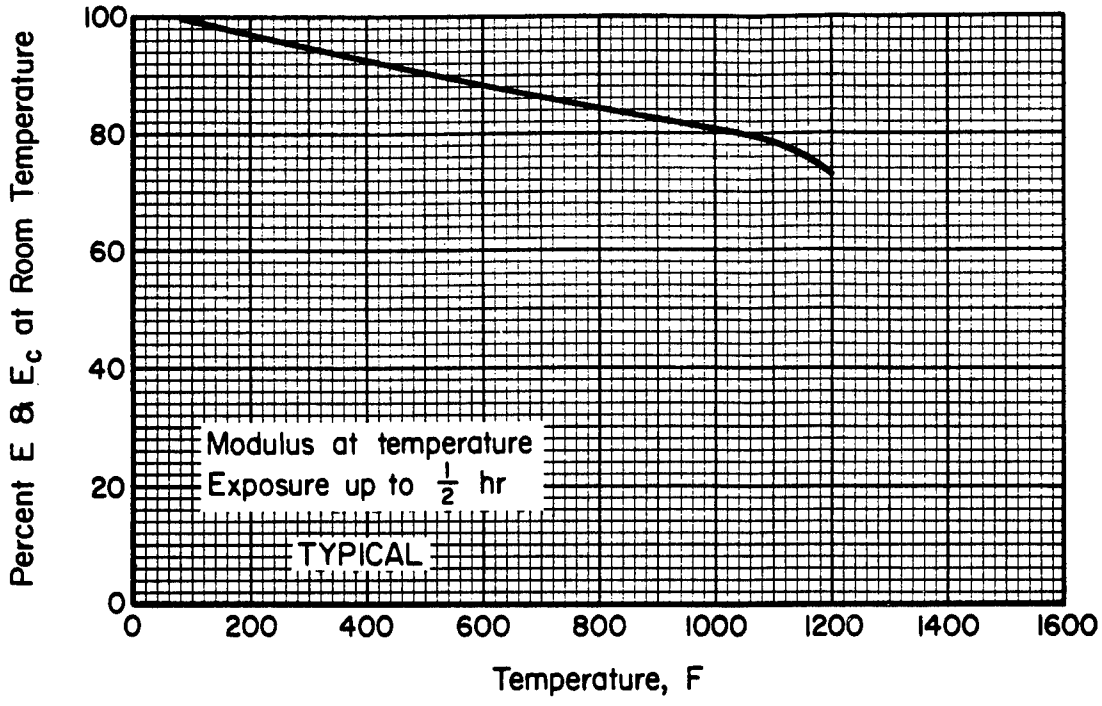


FIGURE 6.2.1.1.4(a). *Effect of temperature on the tensile and compressive moduli (E and E_c) for A-286 alloy (1800 F solution treatment temperature).*

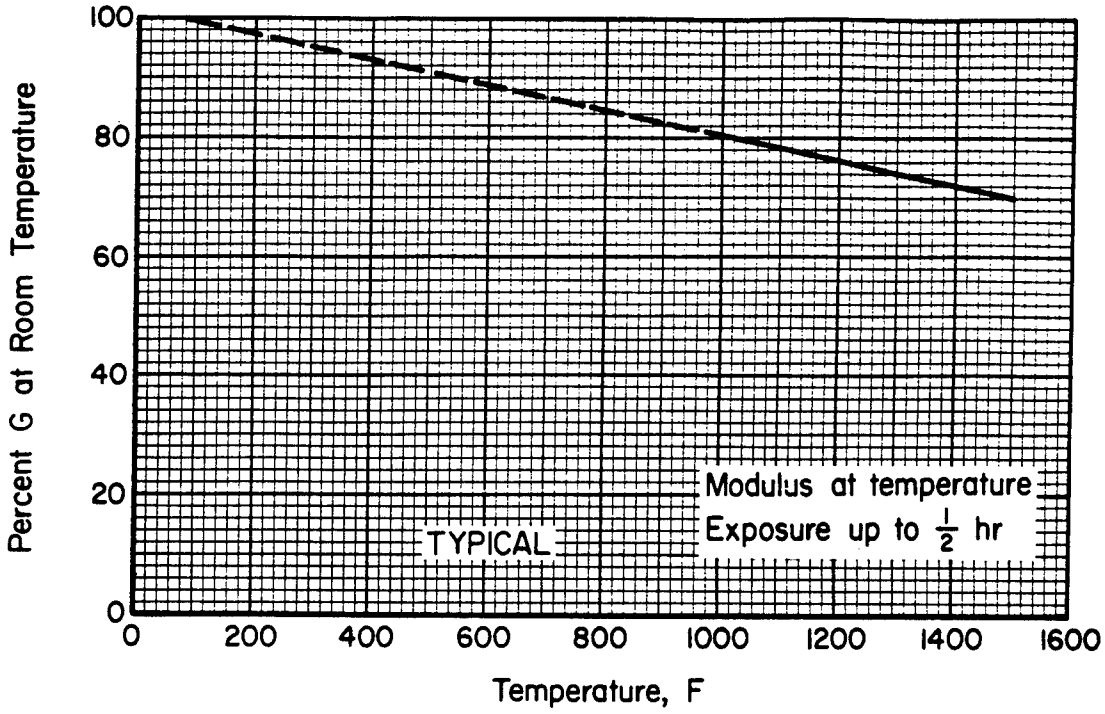


FIGURE 6.2.1.1.4(b). *Effect of temperature on the shear modulus (G) of A-286 alloy.*

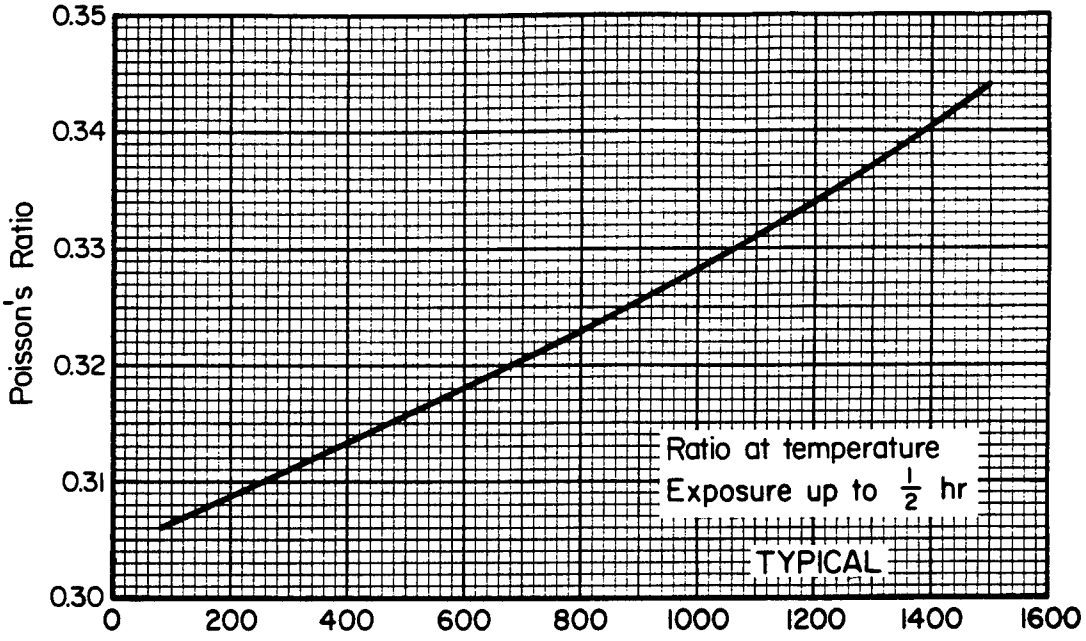


FIGURE 6.2.1.1.4(c). *Effect of temperature on Poisson's ratio (μ) for A-286 alloy.*

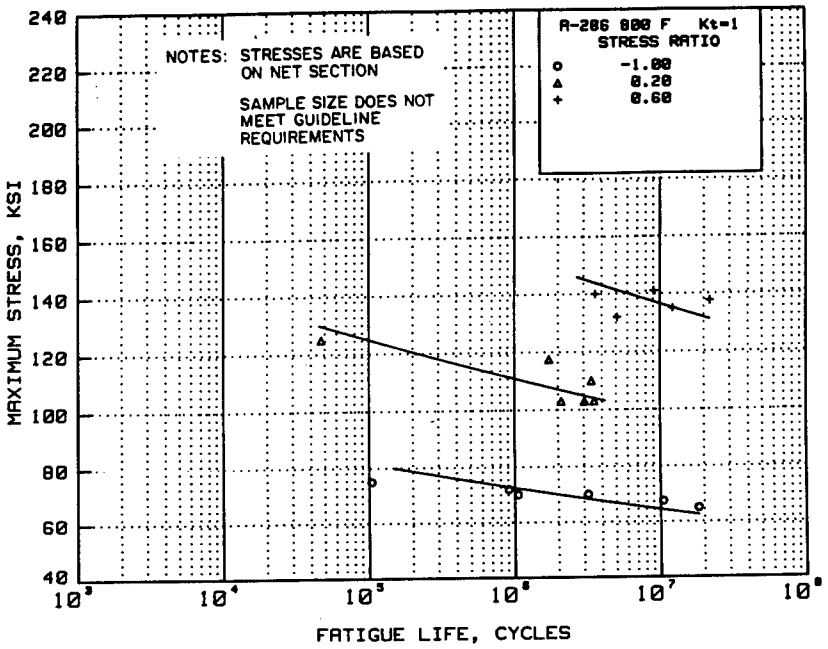


FIGURE 6.2.1.1.8(a). *Best-fit S/N curves for unnotched A-286 bar at 800 F, longitudinal direction.*

Correlative Information for Figure 6.2.1.1.8(a)

Product Form: Bar, air melted

Properties:	TUS, ksi	TYS, ksi	Temp., F
	141.4	95.3	800

Specimen Details: Unnotched
0.250-inch diameter

Heat Treatment: 1650 F for 2 hours, oil quenched and 1300 F for 16 hours, air cooled.

Surface Condition: Not given

Reference: 6.2.1.1.8

Test Parameters:

Loading — Axial
Frequency — 3600 cpm
Temperature — 800 F
Environment — Air

No. of Heats/Lots: 1

Equivalent Stress Equation:

$\text{Log } N_f = 45.1 - 19.5 \log (S_{eq})$
$S_{eq} = S_{max}(1-R)^{0.47}$
Standard Error of Estimate = 0.418
Standard Deviation in Life = 0.717
$R^2 = 65.9\%$

Sample Size = 17

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

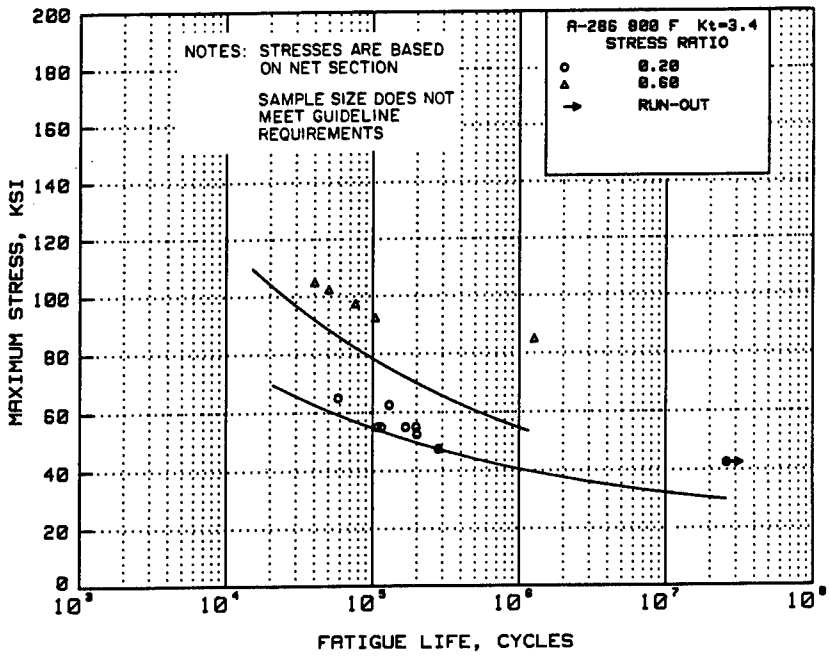


FIGURE 6.2.1.1.8(b). *Best-fit S/N curves for notched, K_t = 3.4, A-286 alloy bar at 800 F, longitudinal direction.*

Correlative Information for Figure 6.2.1.1.8(b)

Product Form: Bar, air melted

Properties:	TUS, ksi	TYS, ksi	Temp., F
	141.4	95.3	800 Unnotched

Specimen Details: Notched, V-Groove, K_t = 3.4
0.375-inch gross diameter
0.250-inch net diameter
0.010-inch root radius, r
60° flank angle, ω

Heat Treatment: 1650 F for 2 hours, oil quenched and 1300 F for 16 hours, air cooled.

Surface Condition: As machined

Reference: 6.2.1.1.8

Test Parameters:

Loading — Axial
Frequency — 3600 cpm
Temperature — 800 F
Environment — Air

No. of Heats/Lots: 1

Equivalent Stress Equation:

$\text{Log } N_f = 11.4 - 4.4 \log (S_{eq} - 20)$
$S_{eq} = S_{max}(1-R)^{0.75}$
Standard Error of Estimate = 0.271
Standard Deviation in Life = 0.387
R^2 = 50.9%

Sample Size = 13

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

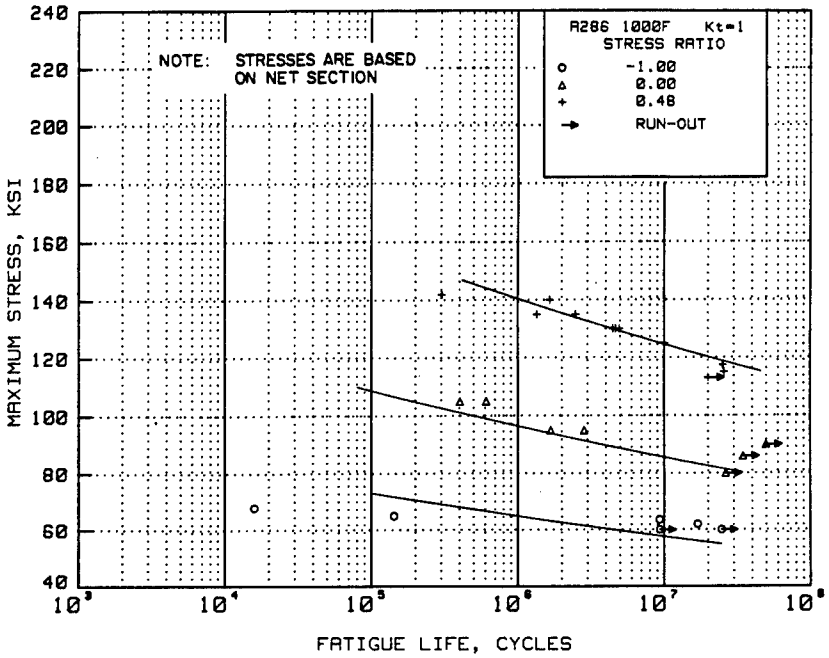


FIGURE 6.2.1.1.8(c). *Best-fit S/N curves for unnotched A-286 bar at 1000 F, longitudinal direction.*

Correlative Information for Figure 6.2.1.1.8(c)

Product Form: Bar, air melted

Properties:	TUS, ksi	TYS, ksi	Temp., F
	137.2	100.6	1000

Specimen Details: Unnotched
0.250-inch diameter

Heat Treatment: 1650 F for 2 hours, oil quenched and 1300 F for 16 hours, air cooled.

Surface Condition: Not given

Reference: 6.2.1.1.8

Test Parameters:

Loading — Axial
Frequency — 3600 cpm
Temperature — 1000 F
Environment — Air

No. of Heats/Lots: 1

Equivalent Stress Equation:

$\text{Log } N_f = 44.2 - 19.3 \log (S_{eq})$
$S_{eq} = S_{max}(1-R)^{0.57}$
Standard Error of Estimate = 0.566
Standard Deviation in Life = 0.835
$R^2 = 54.0\%$

Sample Size = 18

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

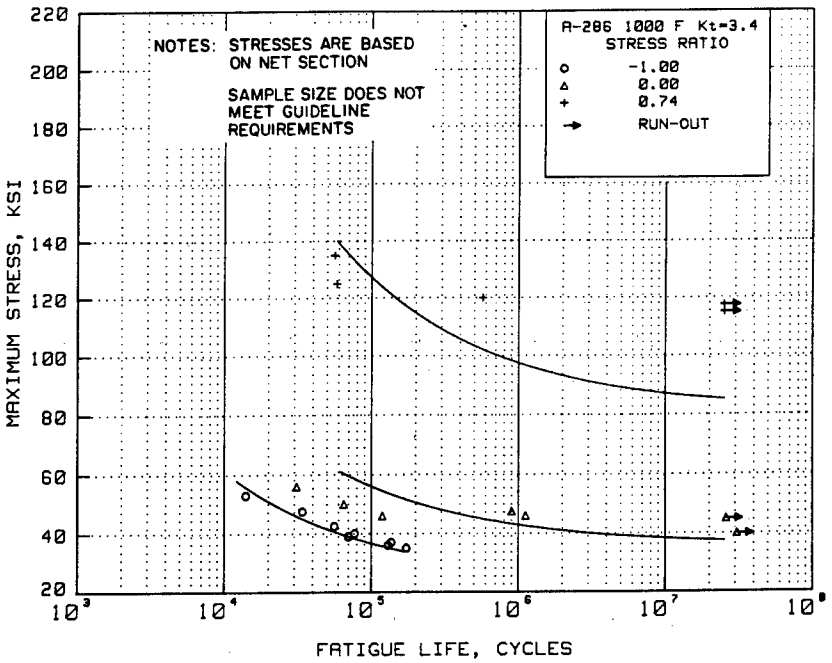


FIGURE 6.2.1.1.8(d). *Best-fit S/N curves for notched, K_t = 3.4, A-286 bar at 1000 F, longitudinal direction.*

Correlative Information for Figure 6.2.1.1.8(d)

Product Form: Bar, air melted

Properties:	TUS, ksi	TYS, ksi	Temp., F
	137.2	100.6	1000 Unnotched

Specimen Details: Notched, V-Groove, K_t = 3.4
0.375-inch gross diameter
0.250-inch net diameter
0.010-inch root radius, r
60° flank angle, ω

Heat Treatment: 1650 F for 2 hours, oil quenched and 1300 F for 16 hours, air cooled.

Surface Condition: As machined

Reference: 6.2.1.1.8

Test Parameters:
Loading — Axial
Frequency — 3600 cpm
Temperature — 1000 F
Environment — Air

No. of Heats/Lots: 1

Equivalent Stress Equation:

$\text{Log } N_f = 7.86 - 2.19 \log (S_{eq} - 35.8)$
$S_{eq} = S_{max}(1-R)^{0.61}$
Standard Error of Estimate = 0.365
Standard Deviation in Life = 0.510
R^2 = 48.7%

Sample Size = 17

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

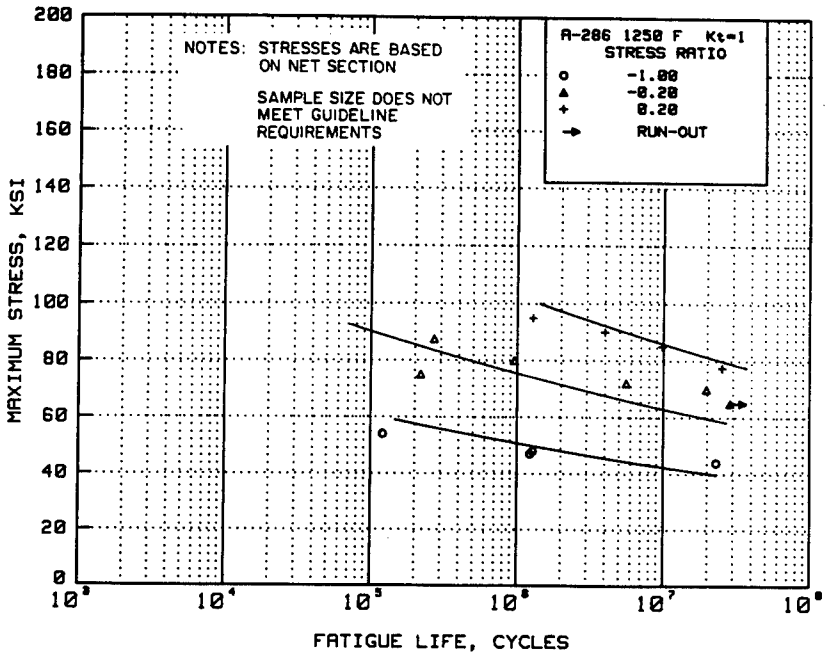


FIGURE 6.2.1.1.8(e). *Best-fit S/N curves for unnotched A-286 bar at 1250 F, longitudinal direction.*

Correlative Information for Figure 6.2.1.1.8(e)

Product Form: Bar, air melted

Properties:	TUS, ksi	TYS, ksi	Temp., F
	109.6	96.5	1250

Specimen Details: Unnotched
0.250-inch diameter

Heat Treatment: 1650 F for 2 hours, oil quenched and 1300 F for 16 hours, air cooled.

Surface Condition: Not given

Reference: 6.2.1.1.8

Test Parameters:

Loading — Axial
Frequency — 3600 cpm
Temperature — 1250 F
Environment — Air

No. of Heats/Lots: 1

Equivalent Stress Equation:

$\text{Log } N_f = 30.8 - 12.8 \log (S_{eq})$
$S_{eq} = S_{max}(1-R)^{0.77}$
Standard Error of Estimate = 0.513
Standard Deviation in Life = 0.788
$R^2 = 57.6\%$

Sample Size = 13

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above]

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6.2.2 N-155 Alloy

6.2.2.0 *Comments and Properties.*—N-155 alloy, also known as Multimet, is designed for applications involving high stress up to 1500 F. It has good oxidation properties and good ductility and can be fabricated readily by conventional methods. This alloy has been used in many aircraft applications, including afterburner components, combustion chambers, exhaust assemblies, turbine components, and bolts.

N-155 is forged readily between 2200 and 1650 F. It is easily formed by conventional methods; intermediate anneals may be required to restore its ductility. This alloy is machinable in all conditions; low cutting speeds and ample flow of coolant are required. The weldability of N-155 is comparable to that of the austenitic stainless steels. The oxidation resistance of N-155 sheet is good up to 1500 F.

Some materials specifications for N-155 are presented in Table 6.2.2.0(a). Room-temperature mechanical and physical properties for N-155 sheet and tubing in the solution-treated (annealed) condition are presented in Table 6.2.2.0(b). Bars and forgings are not specified by room-temperature properties but have specific elevated-temperature requirements. The effect of temperature on physical properties is shown in Figure 6.2.2.0.

TABLE 6.2.2.0(a). *Material Specifications for N-155 Alloy*

Specification	Form	Condition
AMS 5532	Sheet	Solution treated
AMS 5585	Tubing (welded)	Solution treated
AMS 5768	Bar and forging	Solution treated and aged
AMS 5769	Bar and forging	Solution treated

6.2.2.1 *Solution-Treated Condition.*—Elevated-temperature curves are presented in Figures 6.2.2.1.1(a) and (b), as well as 6.2.2.1.4(a) and (b). Stress-rupture properties are specified at 1500 F for sheet and at 1350 F for bars and forgings; the appropriate specifications should be consulted for detailed requirements.

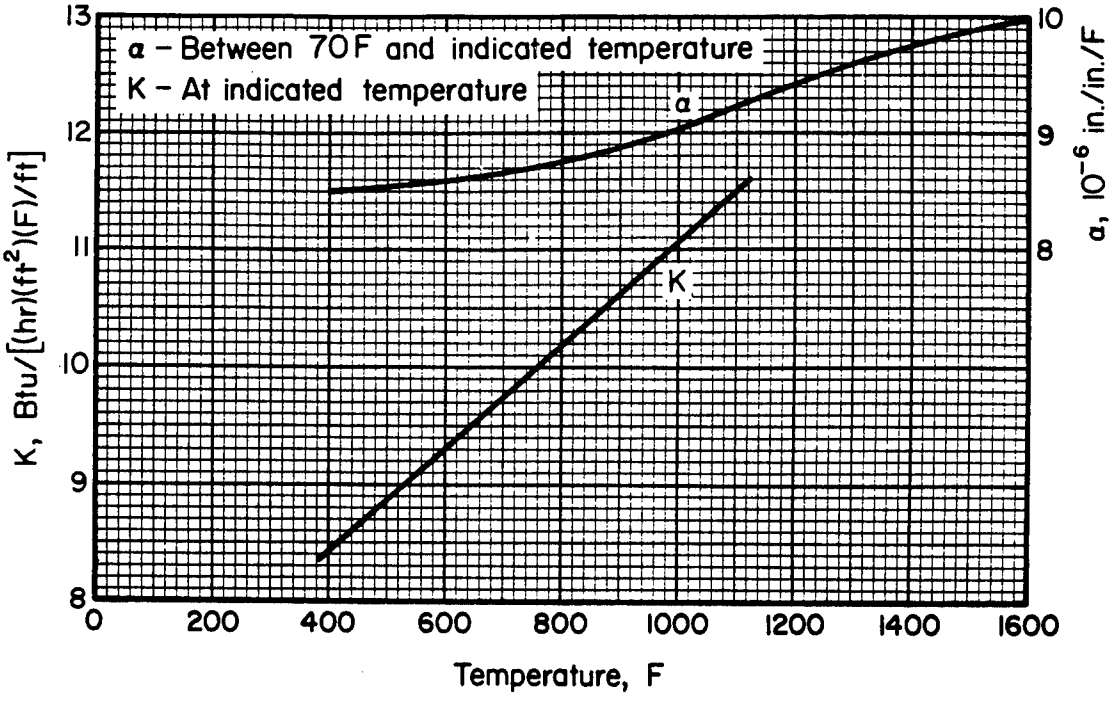


FIGURE 6.2.2.0. *Effect of temperature on the physical properties of N-155 alloy.*

TABLE 6.2.2.0(b). *Design Mechanical and Physical Properties of N-155 Alloy*

Specification	AMS 5532		AMS 5585
Form	Sheet	Strip and plate	Tubing
Condition	Solution treated		
Thickness, in.	≤0.187	...	...
Basis	S[a]	S[a]	S
Mechanical Properties:			
F_{tu}, ksi:			
L	...	...	100
LT	100	100	...
F_{ty}, ksi:			
L	...	...	49[b]
LT	49[b]	...	...
F_{cy}, ksi:			
L	...	...	...
LT	...	...	...
F_{su}, ksi	...	...	...
F_{bru}, ksi:			
(e/D = 1.5)	...	...	...
(e/D = 2.0)	...	...	...
F_{bry}, ksi:			
(e/D = 1.5)	...	...	...
(e/D = 2.0)	...	...	...
e, percent:			
L	...	...	[c]
LT	40	40	...
E, 10^3 ksi	29.2		
E_c, 10^3 ksi	29.2		
G, 10^3 ksi	11.2		
μ	See Figure 6.2.2.1.4(b)		
Physical Properties:			
ω, lb/in.^{3}	0.300		
C, Btu/(lb)(F)	0.103 (70 to 212 F)		
K, Btu/[(hr)(ft^2)(F)/ft]	See Figure 6.2.2.0		
α, 10^{-6} in./in./F	See Figure 6.2.2.0		

[a]Test direction longitudinal for widths less than 9 inches: transverse for widths 9 inches and over.
[b]Typical value reduced to minimum.
[c]Strip = 35.
Full section 0.625 thick = 40.
Full section >0.625 thick = 30.

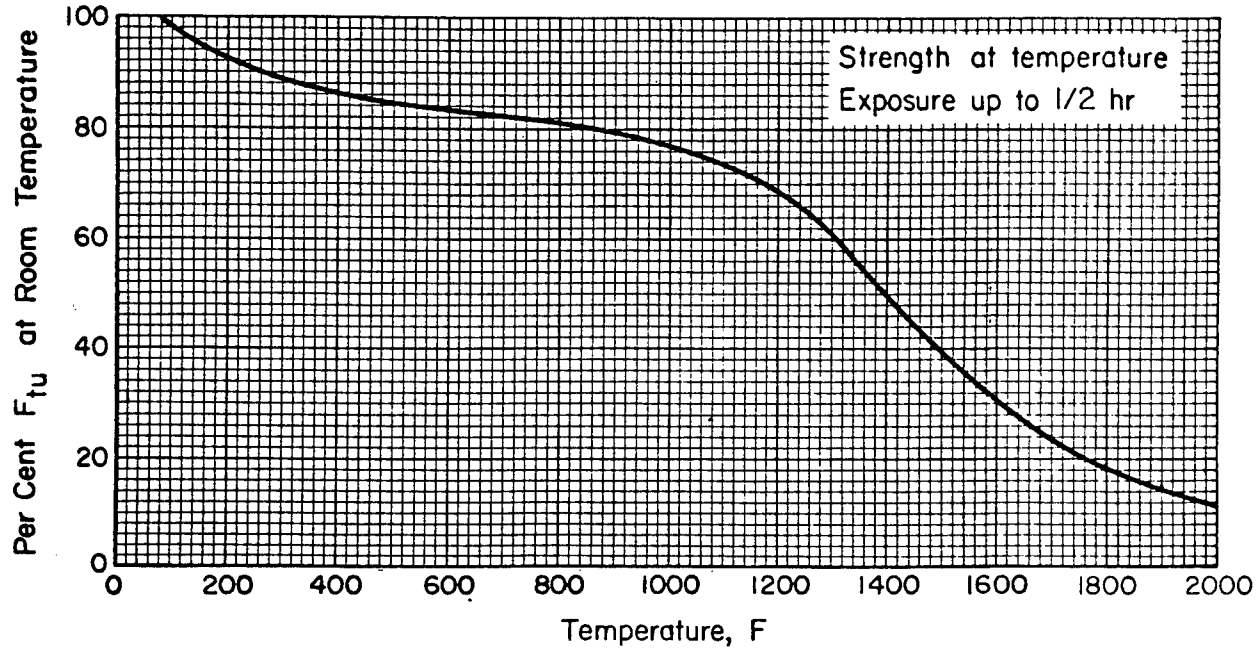


FIGURE 6.2.2.1.1(a). *Effect of temperature on the ultimate tensile strength (F_{tu}) of N-155 alloy.*

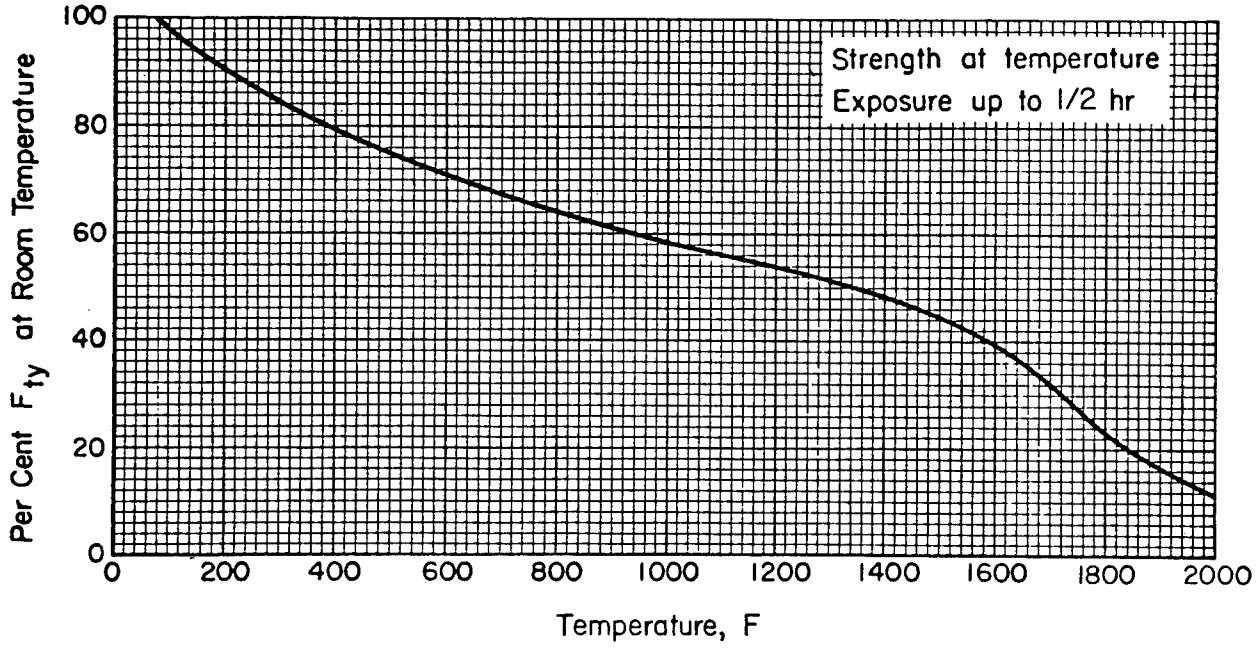


FIGURE 6.2.2.1.1(b). *Effect of temperature on the tensile yield strength (F_{ty}) of N-155 alloy.*

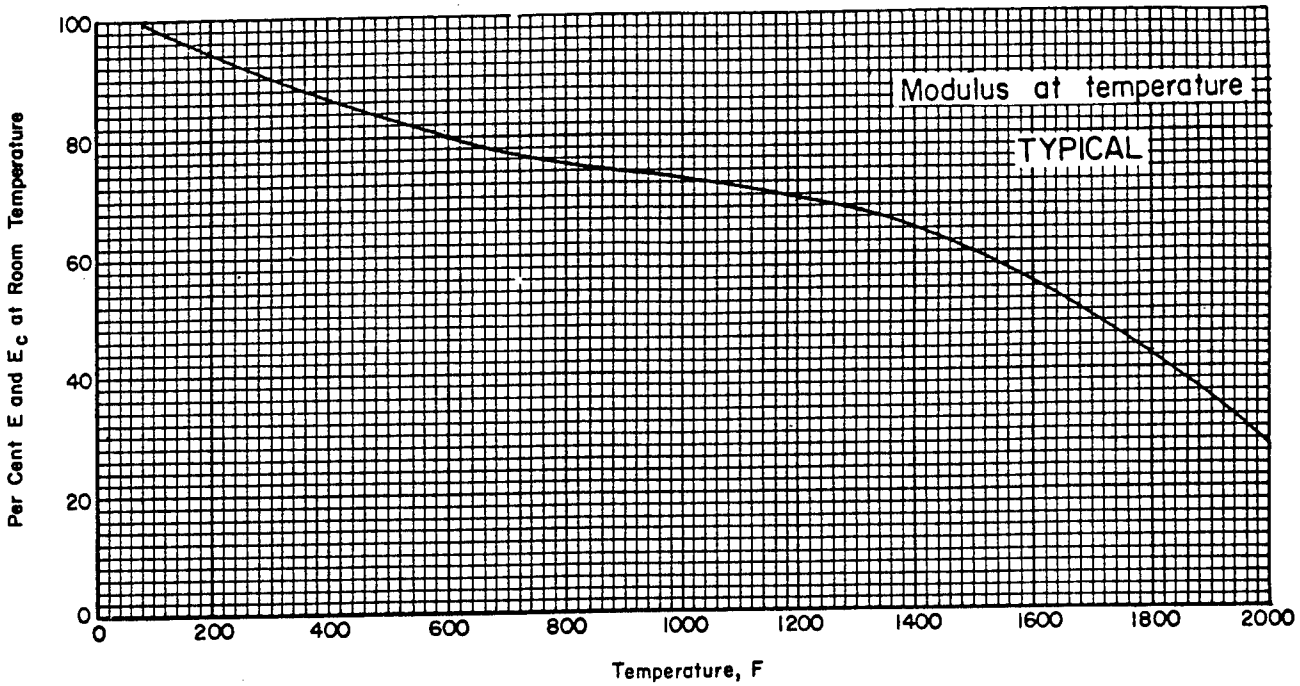


FIGURE 6.2.2.1.4(a). *Effect of temperature on the tensile and compressive moduli (E and E_c) of N-155 alloy.*

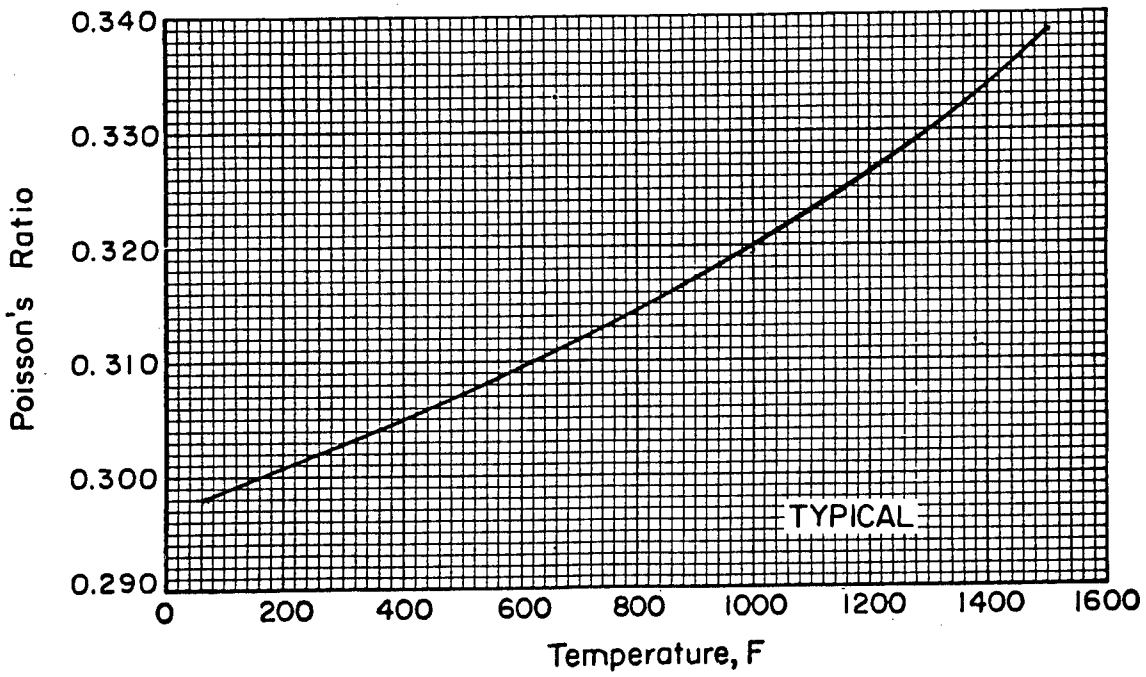


FIGURE 6.2.2.1.4(b). *Effect of temperature on Poisson's ratio (μ) for N-155 alloy.*

6.3 Nickel-Base Alloys

6.3.0 GENERAL COMMENTS.—Nickel is the base element for most of the higher temperature heat-resistant alloys. While it is more expensive than iron, nickel provides an austenitic structure that has greater toughness and workability than ferritic structures of the same strength level.

6.3.0.1 *Metallurgical Considerations.*

Composition.—The common alloying elements for nickel are cobalt, iron, chromium, molybdenum, titanium, and aluminum. Cobalt, when substituted for a portion of the nickel in the matrix, improves high-temperature strength; small additions of iron tend to strengthen the nickel matrix and reduce the cost; chromium is added to increase strength and oxidation resistance at very high temperatures; molybdenum contributes to solid solution strengthening. Titanium and aluminum are added to most nickel-base heat resistant alloys to permit age-hardening by the formation of Ni_3 (Ti, Al) precipitates; aluminum also contributes to oxidation resistance.

The nature of the alloying elements in the age-hardenable nickel-base alloys makes vacuum melting of these alloys advisable, if not mandatory. However, the additional cost of vacuum melting is more than compensated for by the resulting improvements in elevated-temperature properties.

Heat Treatment.—The nickel-base alloys are heat treated with conventional equipment and fixtures such as would be used with austenitic stainless steels. Since nickel-base alloys are more susceptible to sulfur embrittlement than are iron-base alloys, it is essential that sulfur-bearing materials such as grease, oil, cutting lubricants, marking paints, etc., be removed before heat treatment. Mechanical cleaning, such as wire brushing, is not adequate and if used should be followed by washing with a suitable solvent or by vapor degreasing. A low-sulfur content furnace atmosphere should be used. Good furnace control with respect to time and temperature is desirable since overheating some of the alloys as little as 35 F impairs strength and corrosion resistance.

When it is necessary to anneal the age-hardenable-type alloys, a protective atmosphere (such as argon) lessens the possibility of surface contaminations or depletion of the precipitation-hardening elements. This precaution is not so critical in heavier sections since the oxidized surface layer is a smaller percentage of the cross section. After solution annealing, the alloys are generally quenched in water. Heavy sections may require air cooling to avoid cracking from thermal stresses.

In stress-relief annealing of a structure or assembly composed of an aluminum-titanium hardened alloy, it is vitally important to heat the structure rapidly through the age-hardening temperature range, 1200 to 1400 F (which is also the low ductility range) so that stress relief can be achieved before any aging takes place. Parts which are to be used in the fully heat-treated condition would have to be solution treated, air cooled, and subsequently aged. In this case the stress-relief treatment would be conducted in the solution-temperature range. Little difficulty has been encountered with distortion under rapid heating conditions, and distortion of weldments of substantial size has been less than that observed with conventional slow heating methods.

6.3.0.2 *Manufacturing Considerations.*

Forging.—All of the alloys considered, except for the casting compositions, can be forged to some degree. The matrix-strengthened alloys can be forged with proper consideration of cooling rates, atmosphere, etc. Most of the precipitation-hardenable grades can be forged, although heavier equipment is required and a smaller range of reductions can be safely attained.

Cold Forming.—Almost all of the wrought-nickel-base alloys in sheet form are cold formable. The lower strength alloys offer few problems, but the higher strength alloys require higher forming pressures and more frequent anneals.

Machining.—All of the alloys in this section are readily machinable, provided the optimum conditions of heat treatment, type of tool speed, feed, depth of cut, etc., are achieved. Specific

recommendations on these points are available from various producers of these alloys.

Welding.—The matrix-strengthening-type alloys offer no serious problems in welding. All of the common resistance- and fusion-welding processes (except submerged arc) have been successfully employed. For the age-hardenable type of alloy, it is necessary to observe some further precautions:

(1) Welding should be confined to annealed material where design permits. In full age-hardened material, the hazard of cracking in weld and/or parent metal is great.

(2) If design permits joining some portions only after age hardening, the parts to be joined should be "safe ended" with a matrix-strengthened-type alloy (with increased cross section) and then age hardened; welding should then be carried out on the "safe ends."

(3) Parts severely worked or deformed should be annealed before welding.

(4) After welding, the weldment will often require stress relieving before aging.

(5) Material must be heated rapidly to the stress-relieving temperature.

(6) In a number of the age-hardenable alloys, fusion welds may exhibit only 70 to 80 percent of the rupture strength of the parent metal. The deficiency can often be minimized by design, such as locating welds in areas of lowest temperature and/or stress. The use of special filler wires to improve weld-rupture properties is under investigation.

Brazing.—The solid-solution-type chromium-containing alloys respond well to brazing, using techniques and brazing alloys applicable to the austenitic stainless steels. Generally, it is necessary to braze annealed material and to keep stresses low during brazing, especially when brazing with low melting alloys, to avoid embrittlement. As with the stainless steels, dry hydrogen, argon, or helium atmospheres (-80 F dew point or lower) are used successfully, and vacuum brazing is now receiving increasing attention.

The aluminum-titanium age-hardened nickel-base alloys are difficult to braze, even using extremely dry reducing- and inert-gas atmospheres, unless some method of fluxing, solid or gaseous, is used. An alternative technique which is commonly used is to preplate the areas to be brazed with ½ to 1 mil of nickel. For some metal combinations, a few fabricators prefer to apply an iron preplate. In either case, the plating prevents the formation of aluminum or titanium oxide films and results in better joints.

Most of the high-temperature alloys of the nickel-base type are brazed with Ni-Cr-Si-B and Ni-Cr-Si types of brazing alloy. Silver brazing alloys can be used for lower temperature applications. However, since the nickel-base alloys to be brazed are usually employed for higher temperature applications, the higher melting point, stronger, and more oxidation-resistant brazing alloys of the Nicrobraz type are generally used. Some of the gold-base and palladium-base brazing alloys may be useful under some circumstances in intermediate-temperature applications.

6.3.1 HASTELLOY X

6.3.1.0 *Comments and Properties.*—Hastelloy X is a nickel-base alloy used for burner-liner parts, turbine-exhaust weldments, afterburner parts, and other parts requiring oxidation resistance and moderately high strength above 1450 F. It is not hardenable except by cold working and is used in the solution-treated (annealed) condition. Hastelloy X is available in all the usual mill forms.

Hastelloy X is somewhat difficult to forge; forging should be started at 2150 to 2200 F and continued as long as the material flows freely. It should be in the annealed condition for optimum cold forming, and severely formed detail parts should be solution treated at 2150 F for 7 to 10 minutes and cooled rapidly after forming. Machinability of Hastelloy X is similar to that of austenitic stainless steel; the alloy is tough and requires low cutting speeds and ample cutting fluids. Hastelloy X can be resistance or fusion welded or brazed; large or complex fusion weldments require stress relief at 1600 F for 1 hour. Hastelloy X has good oxidation resistance up to 2100 F. It age hardens somewhat during long exposure between 1200 and 1800 F, but this is not a serious problem.

Some material specifications for Hastelloy X are presented in Table 6.3.1.0(a). Room-temperature mechanical and physical properties for Hastelloy X sheet are presented in Table 6.3.1.0(b). AMS 5754 does not specify tensile properties for bars and forgings. Figure 6.3.1.0 shows the effect of temperature on physical properties.

TABLE 6.3.1.0(a). *Material Specifications for Hastelloy X*

Specification	Form	Condition
AMS 5536	Sheet and plate	Solution heat treated (annealed)
AMS 5754	Bar and forging	Solution heat treated (annealed)

6.3.1.1 *Annealed Condition.*—The effect of temperature on various mechanical properties is presented in Figures 6.3.1.1.1 and 6.3.1.1.4. In addition, certain stress-rupture requirements at 1500 F are specified in AMS 5536 and 5754 for Hastelloy X. Typical tensile stress-strain curves at room and elevated temperatures are presented in Figure 6.3.1.1.6(a). Typical compressive stress-strain and tangent-modulus curves at room and elevated temperatures are presented in Figure 6.3.1.1.6(b).

TABLE 6.3.1.0(b). *Design Mechanical and Physical Properties of Hastelloy X Sheet and Plate*

Specification	AMS 5536						
Form	Sheet[a] and plate						
Condition	Solution treated (annealed)						
Thickness, in.	<0.010	0.010-0.019	0.020-0.100		0.101-0.187	0.188-2.000	>2.000
Basis	S	S	A	B	S	S	S
Mechanical Properties:							
F_{tu}, ksi:							
L	...	...	...	...	...	...	...
LT	105	105	102	106	105	100	95
F_{ty}, ksi:							
L	...	...	...	...	...	...	...
LT	45	45	44	47	45	40	40
F_{cy}, ksi:							
L	...	...	...	...	...	...	...
LT	...	...	...	...	...	...	...
F_{su}, ksi	...	...	...	...	...	...	...
F_{bru}, ksi:							
(e/D = 1.5)	...	...	...	...	...	...	...
(e/D = 2.0)	...	...	...	...	...	...	...
F_{bry}, ksi:							
(e/D = 1.5)	...	...	...	...	...	...	...
(e/D = 2.0)	...	...	...	...	...	...	...
e, percent (S-basis):		...					
L	...	...	...	...	...	...	...
LT	...	29	35	...	35	35	35
E, 10^3 ksi	29.8						
E_c, 10^3 ksi	29.8						
G, 10^3 ksi	11.3						
μ	0.32						
Physical Properties:							
ω, lb/in.^{3}	0.297						
C, Btu/(lb)(F)	See Figure 6.3.1.0						
K, Btu/[(hr)(ft^2)(F)/ft]	See Figure 6.3.1.0						
α, 10^{-6} in./in./F	See Figure 6.3.1.0						

[a]Test direction longitudinal for widths less than 9 inches: transverse for widths 9 inches and over.

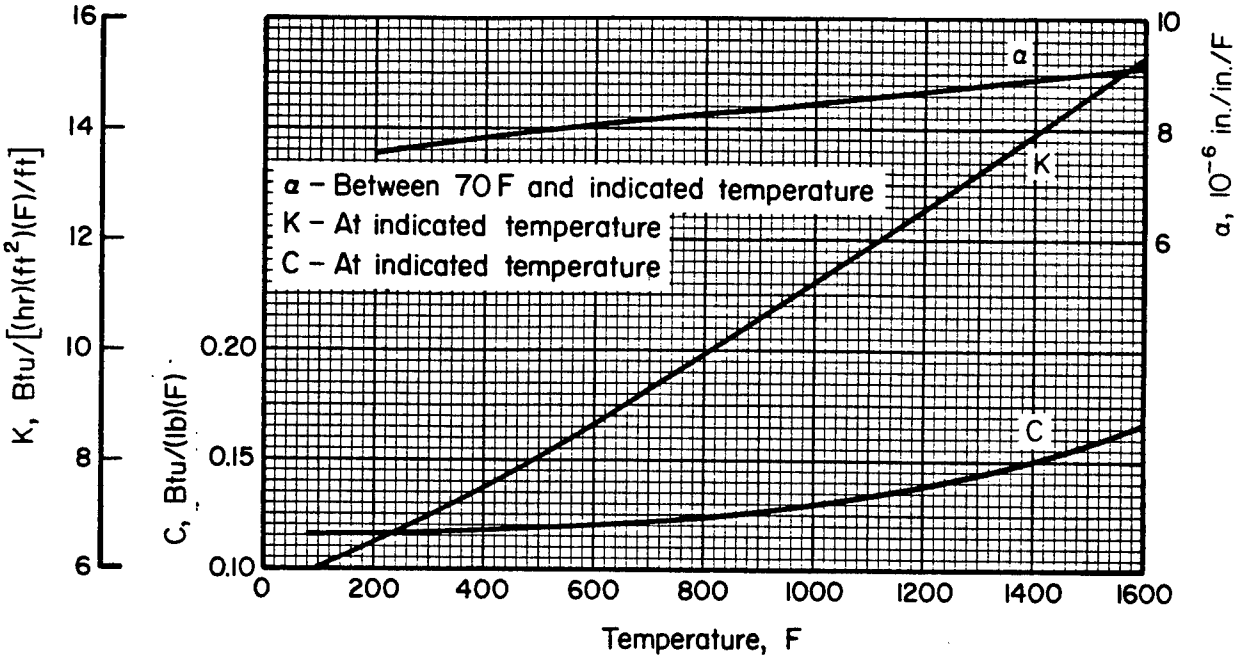


FIGURE 6.3.1.0. *Effect of temperature on the physical properties of Hastelloy X.*

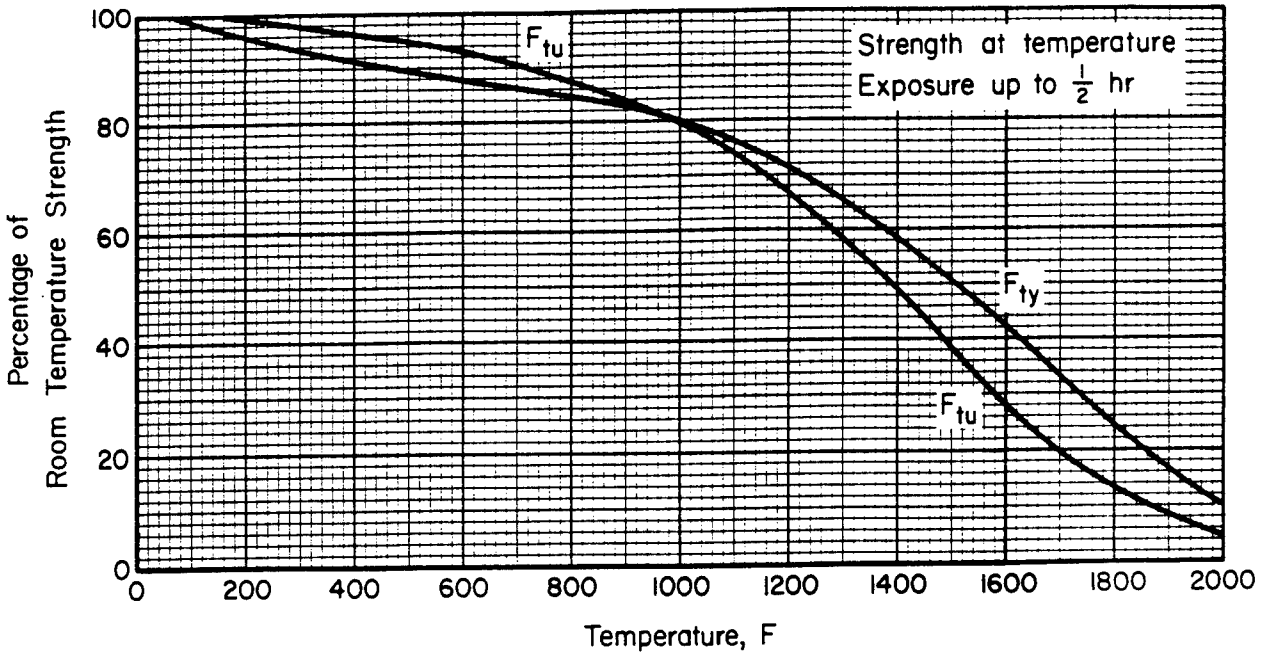


FIGURE 6.3.1.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of Hastelloy X sheet.*

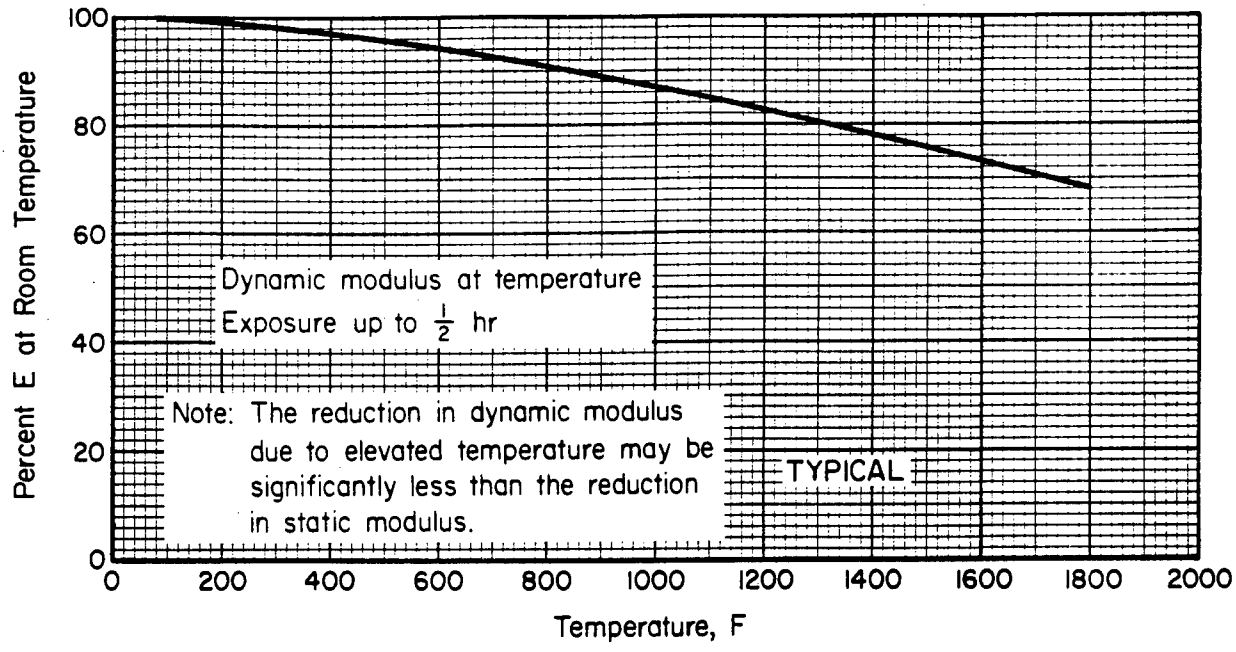


FIGURE 6.3.1.1.4. *Effect of temperature on dynamic modulus (E) of Hastelloy X sheet.*

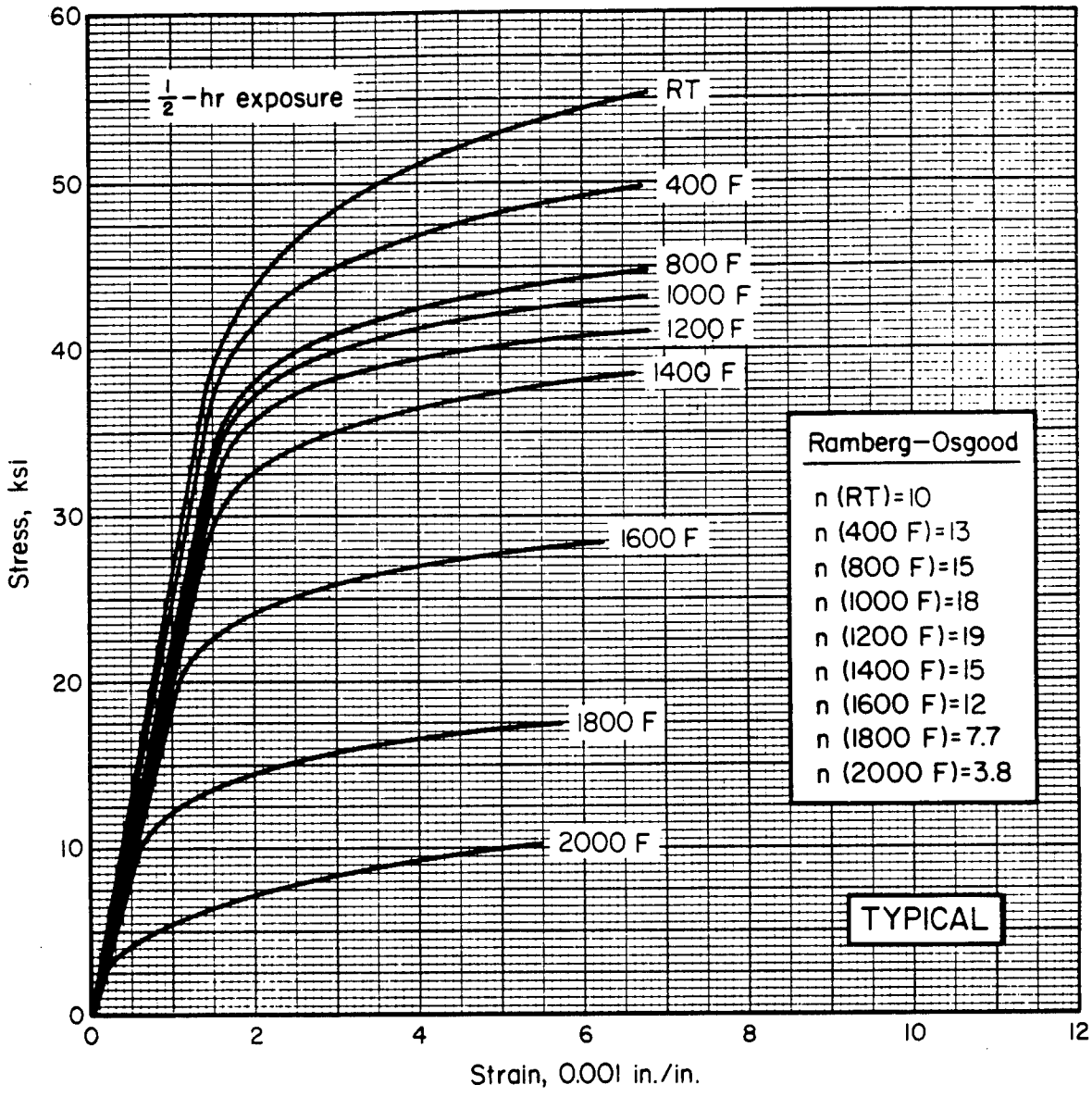


FIGURE 6.3.1.1.6(a). *Typical tensile stress-strain curves for Hastelloy X sheet at room and elevated temperatures.*

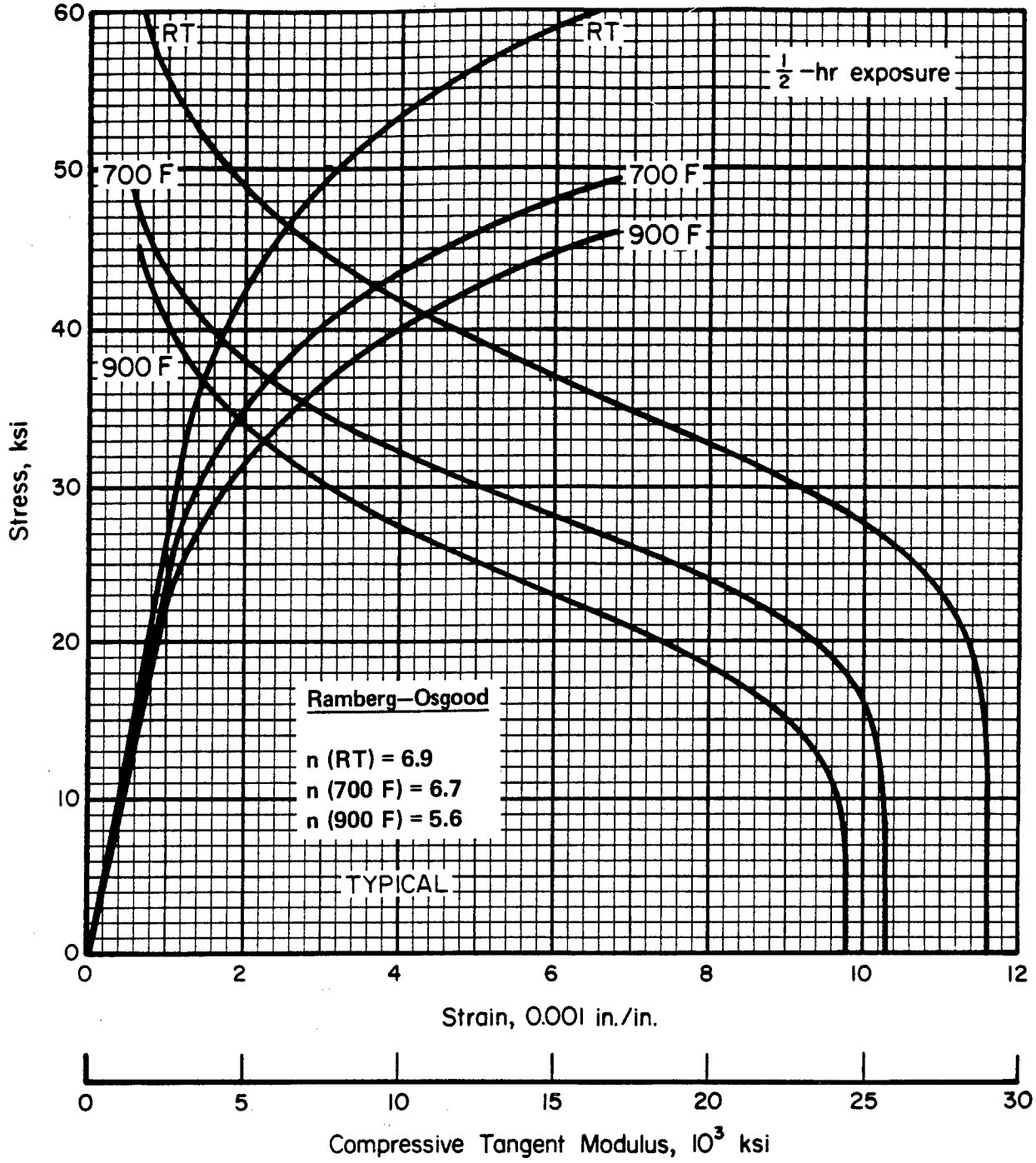


FIGURE 6.3.1.1.6(b). *Typical compressive stress-strain and compressive tangent-modulus curves for Hastelloy X bar at room and elevated temperatures.*

6.3.2 INCONEL 600 ALLOY

6.3.2.0 *Comments and Properties.*—Inconel 600 Alloy is a corrosion- and heat-resistant nickel-base alloy used for low-stressed parts operating up to 2000 F. It is not hardenable except by cold working and is usually used in the annealed condition. Inconel is available in all the usual mill forms.

Inconel 600 Alloy is readily forged between 2250 and 1900 F; "hot-cold" working between 1600 and 1200 F is harmful and should be avoided; cold working below 1200 F results in improved properties. This alloy is readily formed but should be annealed after severe forming operations. The maximum annealing temperature is 1800 F if minimum yield-strength requirements are to be met consistently. Inconel 600 Alloy is susceptible to rapid grain growth at 1800 F or higher, and exposures at these temperatures are necessarily brief if large grain size is objectionable.

Inconel 600 Alloy is somewhat difficult to machine because of its toughness and capacity for work hardening; high-speed steel or cemented-carbide tools should be used, and tools should be kept sharp. This alloy can be resistance or fusion welded or brazed (using nonsilver containing brazing alloy); large or complex fusion weldments should be stress relieved at 1600 F for 1 hour. Oxidation resistance of Inconel 600 Alloy is excellent up to 2000 F in sulfur-free atmospheres. This alloy is subject to attack in sulfur-containing atmospheres.

TABLE 6.3.2.0(a). *Material Specifications for Inconel 600 Alloy*

Specification	Form	Condition
AMS 5540	Plate, sheet, and strip	Annealed
AMS B166	Bar and rod	Various
AMS 5580	Tubing, seamless	Annealed
ASTM B564	Forging	Annealed

Some material specifications for Inconel 600 Alloy are presented in Table 6.3.2.0(a). Room-temperature mechanical and physical properties are shown in Tables 6.3.2.0(b), (c), and (d). Figure 6.3.2.0 shows the effect of temperature on the physical properties.

6.3.2.1 *Annealed Condition.*—Elevated-temperature data for this condition are shown in Figures 6.3.2.1.1 through 6.3.2.1.4.

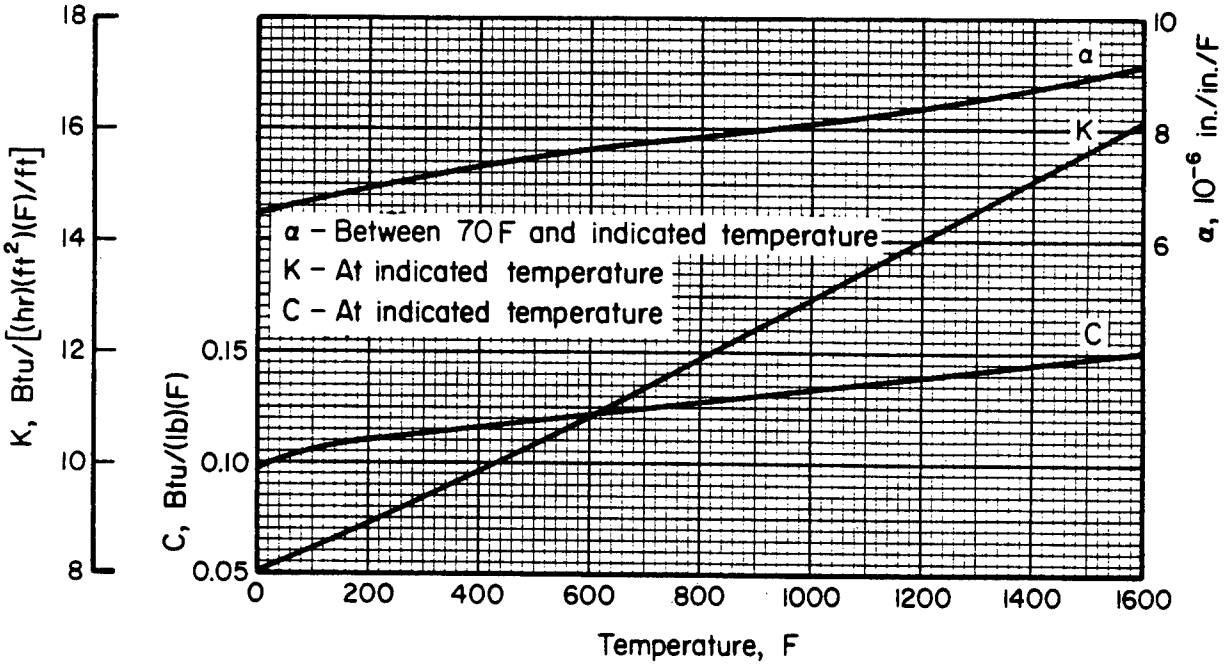


FIGURE 6.3.2.0. *Effect of temperature on the physical properties of Inconel 600.*

TABLE 6.3.2.0(b). *Design Mechanical and Physical Properties of Inconel 600 Alloy*

Specification	AMS 5540	AMS 5580		ASTM B564
Form	Sheet, strip, and plate	Tubing		Forging
Condition	Annealed	Cold drawn		Annealed
Thickness, in.	0.020-2.000	...		...
Outside Diameter, in.	...	≤5.000	5.001-6.625	...
Basis	S	S	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	...	80	80	80
LT	80	...	...	...
F_{ty}, ksi:				
L	...	35	30	35
LT	35	...	...	...
F_{cy}, ksi:				
L	...	35	30	35
LT	35	...	...	...
F_{su}, ksi	51	51	51	51
F_{bru}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	152	152	152	152
F_{bry}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
e, percent:				
L	...	30	35	30
LT	30	...	...	...
E, 10^3 ksi	30.0			
E_c, 10^3 ksi	30.0			
G, 10^3 ksi	11.0			
μ	0.29			
Physical Properties:				
ω, lb/in.^{3}	0.304			
C, K, and α	See Figure 6.3.2.0			

TABLE 6.3.2.0(c). *Design Mechanical and Physical Properties of Inconel 600 Alloy Bar and Rod*

Specification	ASTM B166				
Form	Round			Square, hexagon, and rectangle	
Condition	Cold-worked				
Thickness, in.	≤0.499	0.500-1.000	1.001-2.500	≤0.250	0.251-0.499
Basis	S	S	S	S	S
Mechanical Properties[a]:					
F_{tu}, ksi:					
L	120	110	105	100	95
LT	...	...	...	...	...
F_{ty}, ksi:					
L	90	85	80	80	70
LT	...	...	...	...	...
F_{cy}, ksi:					
L	...	...	...	...	...
LT	...	...	...	...	...
F_{su}, ksi	...	...	...	...	...
F_{bru}, ksi:					
(e/D = 1.5)	...	...	...	...	...
(e/D = 2.0)	...	...	...	...	...
F_{bry}, ksi:					
(e/D = 1.5)	...	...	...	...	...
(e/D = 2.0)	...	...	...	...	...
e, percent:					
L	7[b]	10	12	5[b]	7
E, 10^3 ksi	30.0				
E_c, 10^3 ksi	30.0				
G, 10^3 ksi	11.0				
μ	0.29				
Physical Properties:					
ω, lb/in.^{3}	0.304				
C, K, and α	See Figure 6.3.2.0				

[a]Mechanical property requirements apply only when specified by purchaser.
[b]Not applicable to thickness <0.094 inch.

TABLE 6.3.2.0(d). *Design Mechanical and Physical Properties of Inconel 600 Alloy Bar and Rod*

Specification	ASTM B166				
Form	Round			Square, hexagon, and rectangle	Bar and rod
Condition	Hot-worked				Annealed
Thickness, in.	0.250-0.500	0.501-3.000	>3.000	All	All
Basis	S	S	S	S	S
Mechanical Properties[a]:					
F_{tu}, ksi:					
L	95	90	85	85	80
LT	...	...	...	...	...
F_{ty}, ksi:					
L	45	40	35	35	35
LT	...	...	...	...	...
F_{cy}, ksi:					
L	...	...	...	...	35
LT	...	...	...	...	...
F_{su}, ksi	...	...	...	...	51
F_{bru}, ksi:					
(e/D = 1.5)	...	...	...	...	...
(e/D = 2.0)	...	...	...	...	152
F_{bry}, ksi:					
(e/D = 1.5)	...	...	...	...	...
(e/D = 2.0)	...		...	...	...
e, percent:					
L	20	25	30	...	30[b]
E, 10^3 ksi	30.0				
E_c, 10^3 ksi	30.0				
G, 10^3 ksi	11.0				
μ	0.29				
Physical Properties:					
ω, lb/in.^{3}	0.304				
C, K, and α	See Figure 6.3.2.0				

[a]Mechanical property requirements apply only when specified by purchaser.
[b]Not applicable to thickness >0.094 inch.

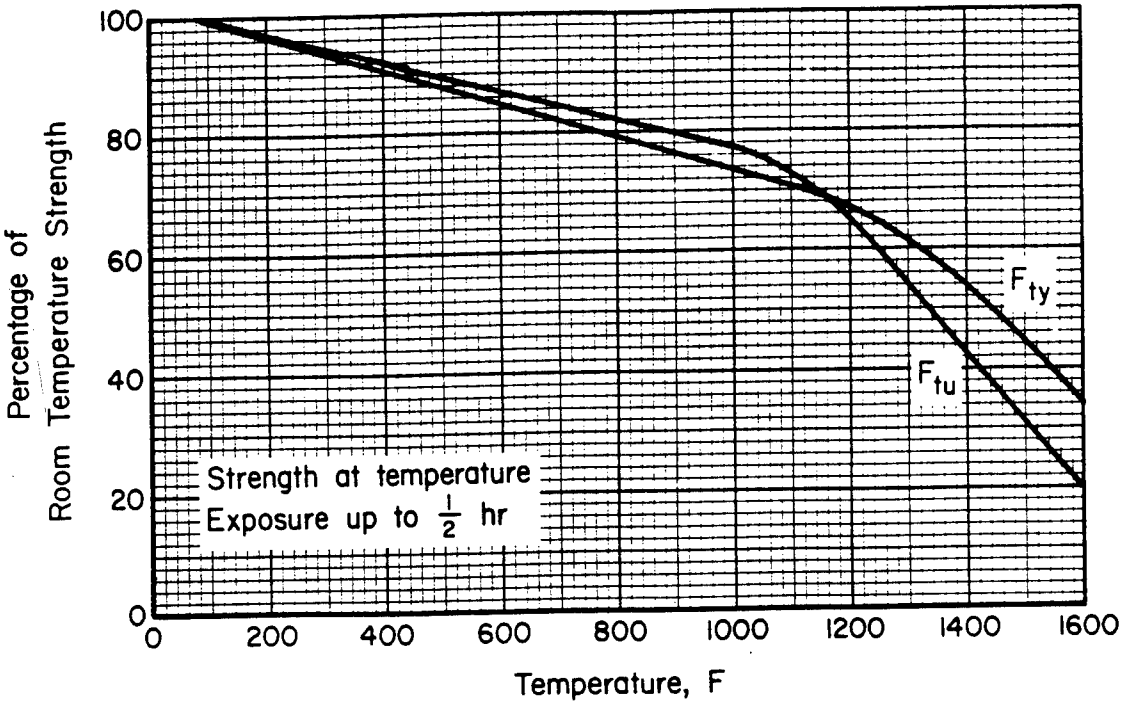


FIGURE 6.3.2.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of Inconel Alloy 600.*

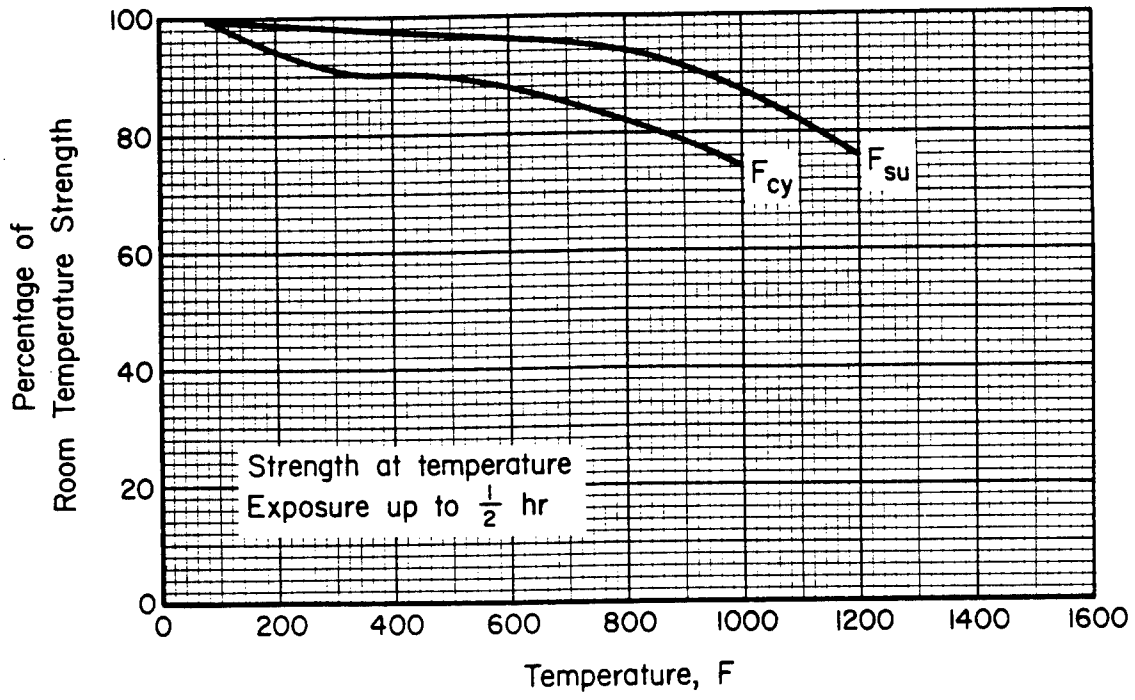


FIGURE 6.3.2.1.2. *Effect of temperature on the compressive yield strength (F_{cy}) and the shear ultimate strength (F_{su}) of Inconel Alloy 600.*

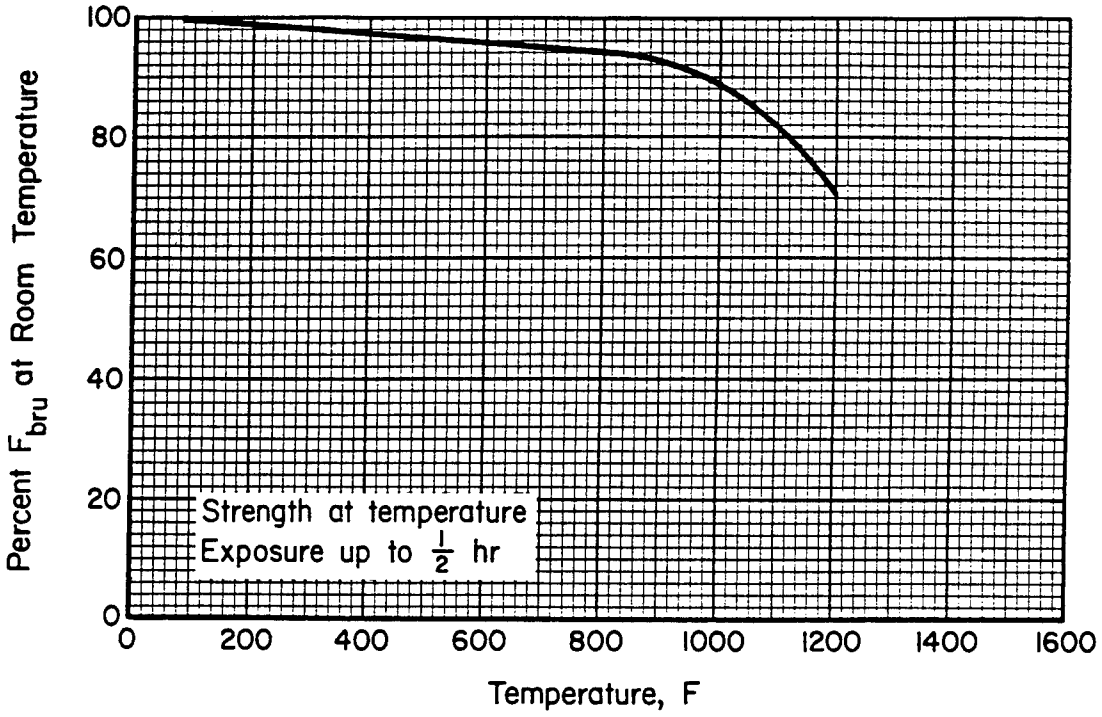


FIGURE 6.3.2.1.3(a). *Effect of temperature on the ultimate bearing strength (F_{bru}) of Inconel Alloy 600.*

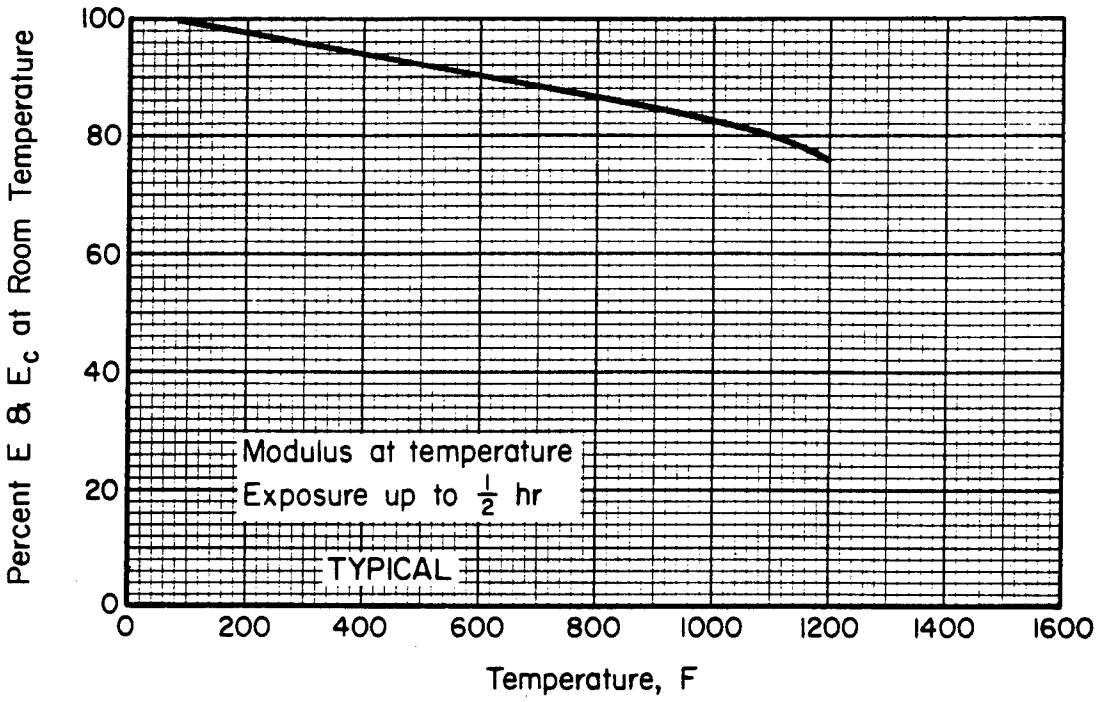


FIGURE 6.3.2.1.4. *Effect of temperature on the tensile and compressive moduli (E and E_c) of Inconel Alloy 600.*

6.3.3 INCONEL 625 ALLOY

6.3.3.0 *Comments and Properties.*—Inconel 625 is a solid-solution, matrix strengthened nickel-base alloy primarily for applications requiring good corrosion and oxidation resistance at temperatures up to approximately 1800 F and also where such parts may require welding.

The strength of the alloy is derived from the strengthening effect of molybdenum and columbium; thus, precipitation hardening is not required and the alloy is used in the annealed condition. The strength is greatly affected by the amount of cold work prior to annealing and by the annealing temperature. The material is usually annealed at 1700 to 1900 F for time commensurate with thickness. The properties in this section are restricted to that annealing range.

Because the alloy was developed to retain high strength at elevated temperatures, it resists deformation at hot working temperatures but can be readily fabricated with adequate equipment. The combination of strength, corrosion resistance, and ability to be fabricated, including welding by common industrial practices, are the alloy's outstanding features.

Some material specifications for Inconel 625 Alloy are listed in Table 6.3.3.0(a). Room-temperature mechanical and physical properties for Inconel 625 Alloy are listed in Tables 6.3.3.0(b) and (c). Figure 6.3.3.0 shows the effect of temperature on the physical properties.

TABLE 6.3.3.0(a). *Material Specifications for Inconel 625 Alloy*

Specification	Form	Condition
AMS 5599	Sheet, strip, and plate	Annealed
AMS 5666	Bar, forging, and ring	Annealed

6.3.3.1 *Annealed Condition.*—Elevated-temperature curves for tensile ultimate strength, tensile yield strength, tensile and compressive moduli, and Poisson's ratio are presented in Figures 6.3.3.1.1(a) and (b), as well as 6.3.3.1.4(a) and (b). Typical stress-strain and tangent-modulus curves are shown in Figures 6.3.3.1.6(a) through (d). Fatigue S/N curves are presented in Figures 6.3.3.1.8(a) through (d).

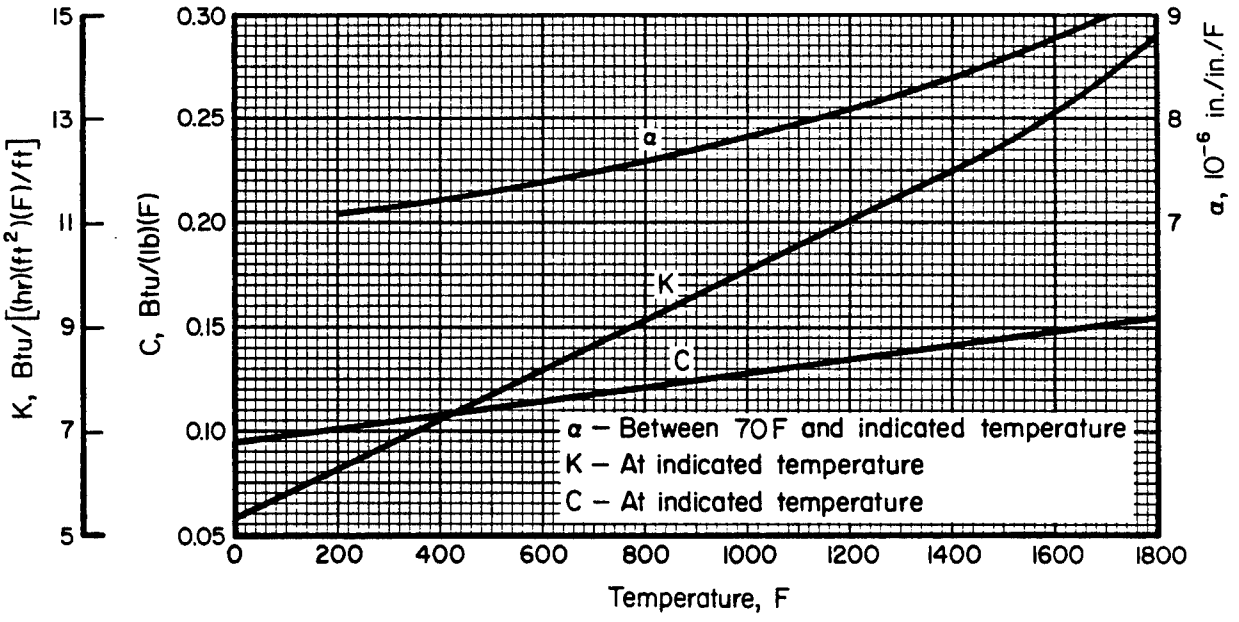


FIGURE 6.3.3.0. *Effect of temperature on the physical properties of Inconel 625 Alloy.*

TABLE 6.3.3.0(b). *Design Mechanical and Physical Properties of Inconel 625 Alloy Sheet and Plate*

Specification	AMS 5599									
Form	Sheet and plate									
Condition	Annealed									
Thickness, in.	≤0.062		0.063-0.109		0.110-0.140		0.141-0.187		0.188-0.250	0.251-1000
Basis	A	B	A	B	A	B	A	B	S	S
Mechanical Properties:										
F_{tu}, ksi:										
L	119	127	119	126	119	125	118	123	119	...
LT	120[a]	128	120[a]	127	120[a]	126	119	124	120	120
F_{ty}, ksi:										
L	56	62	55	61	54	60	53	59	59	...
LT	57	63	56	62	55	61	54	60	60	60
F_{cy}, ksi:										
L	59	65	58	64	57	63	55	62	62	...
LT	59	66	58	65	57	64	56	63	63	...
F_{su}, ksi	79	84	79	84	79	83	79	82	79	..
F_{bru}, ksi:										
(e/D = 1.5)	202	216	202	214	202	212	201	209	202	...
(e/D = 2.0)	263	281	263	279	263	276	261	272	263	...
F_{bry}[b], ksi:										
(e/D = 1.5)	88	97	86	95	84	94	83	92	92	...
(e/D = 2.0)	109	121	107	119	105	117	103	115	115	...
e, percent (S basis):										
LT	30	...	30	...	30	...	30	...	30	30
E, 10^3 ksi	29.8									
E_c, 10^3 ksi	29.8									
G, 10^3 ksi	1.8									
μ	0.28									
Physical Properties:										
ω, lb/in.^{3}	0.305									
C, K, and α	See Figure 6.3.4.0									

[a]S-basis. The A values are higher than specification values as follows: F_{tu}(≤0.062) = 123 ksi, F_{tu} (0.063-0.109) = 122 ksi, and F_{tu} (0.110-0.140) = 121 ksi.
[b]Bearing values are "dry pin" values per Section 1.4.7.1.

TABLE 6.3.3.0(c). *Design Mechanical and Physical Properties of Inconel 625 Alloy Bar*

Specification	AMS 5666			
Form	Bar			
Condition	Annealed			
Thickness or diameter, in.	0.500-0.999	1.000-1.999	2.000-2.999	3.000-3.999
Basis	S	S	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	120	120	120	120
ST	...	...	118	118
F_{ty}, ksi:				
L	60	60	60	60
ST	...	...	57	57
F_{cy}, ksi:				
L	60	59	56	53
ST	...	...	60	60
F_{su}, ksi	79	79	79	79
F_{bru}[a], ksi:				
(e/D = 1.5)	192	192	192	192
(e/D = 2.0)	234	234	234	234
F_{bry}[a], ksi:				
(e/D = 1.5)	88	88	88	88
(e/D = 2.0)	102	102	102	102
e, percent (S-basis):				
L	30	30	30	30
E, 10^3 ksi	29.8			
E_c, 10^3 ksi	29.8			
G, 10^3 ksi	11.8			
μ	0.28			
Physical Properties:				
ω, lb/in.^{3}	0.305			
C, K, and α	See Figure 6.3.4.0			

[a]Bearing values are "dry pin" values per Section 1.4.7.1.

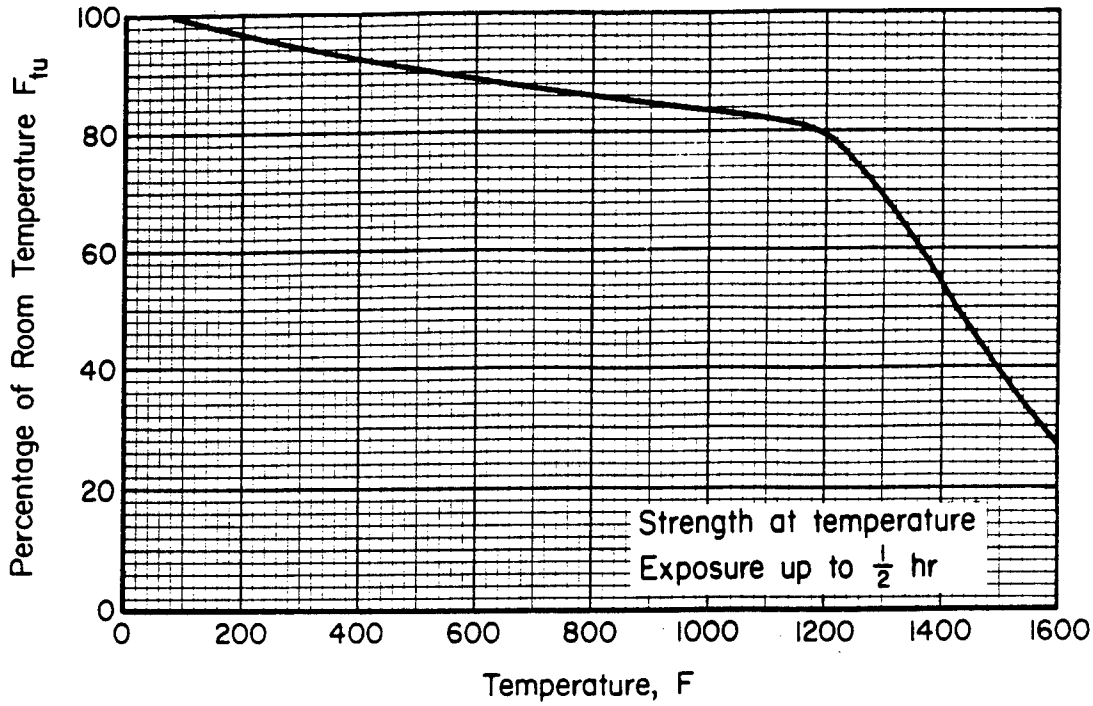


FIGURE 6.3.3.1.1(a). *Effect of temperature on the ultimate tensile strength (F_{tu}) of annealed Inconel Alloy 625 sheet and bar.*

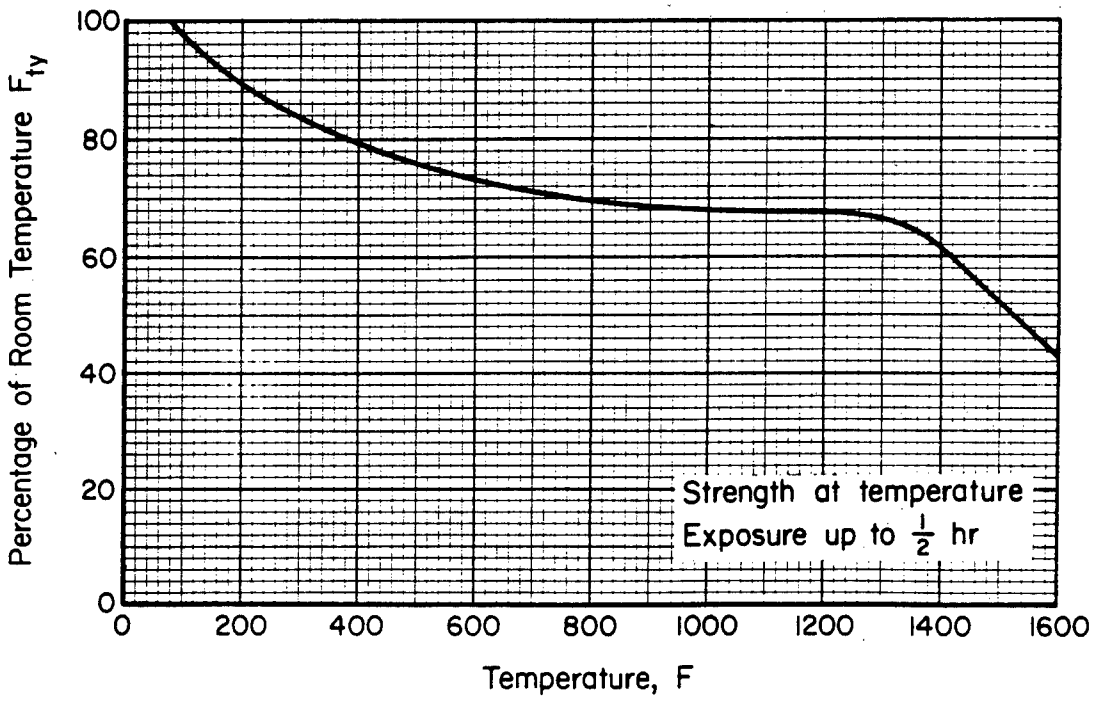


FIGURE 6.3.3.1.1(b). *Effect of temperature on the tensile yield strength (F_{ty}) of annealed Inconel Alloy 625 sheet and bar.*

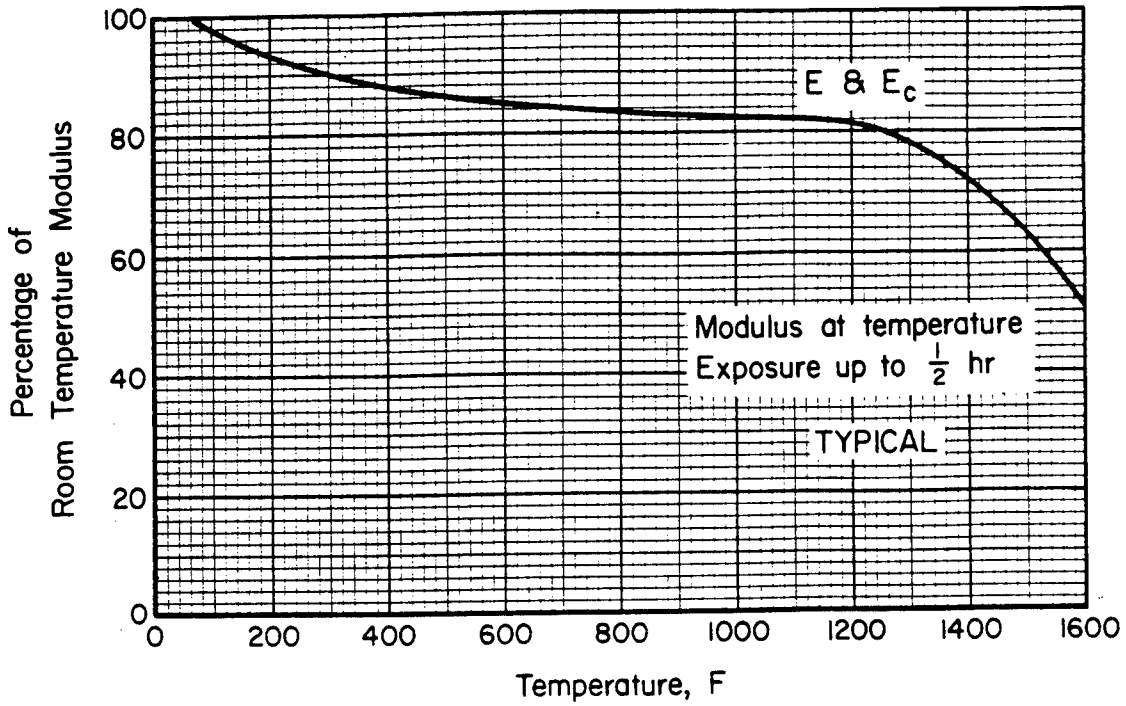


FIGURE 6.3.3.1.4(a). *Effect of temperature on the tensile and compressive moduli (E and E_c) of annealed Inconel Alloy 625.*

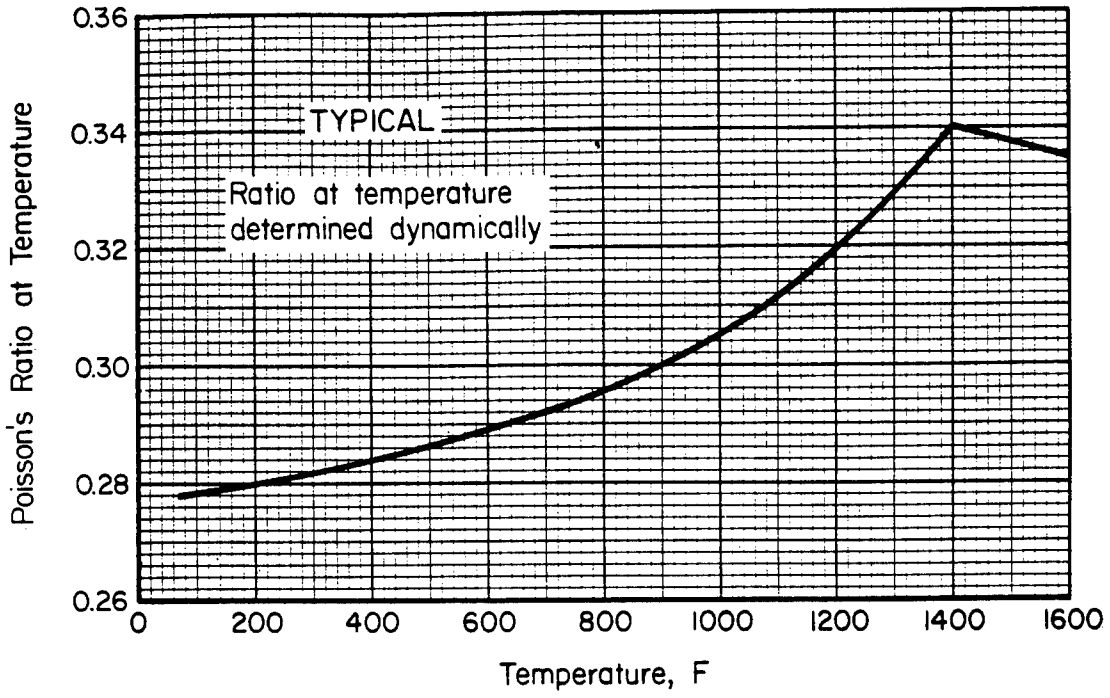


FIGURE 6.3.3.1.4(b). *Effect of temperature on Poisson's ratio (μ) for annealed Inconel Alloy 625 bar.*

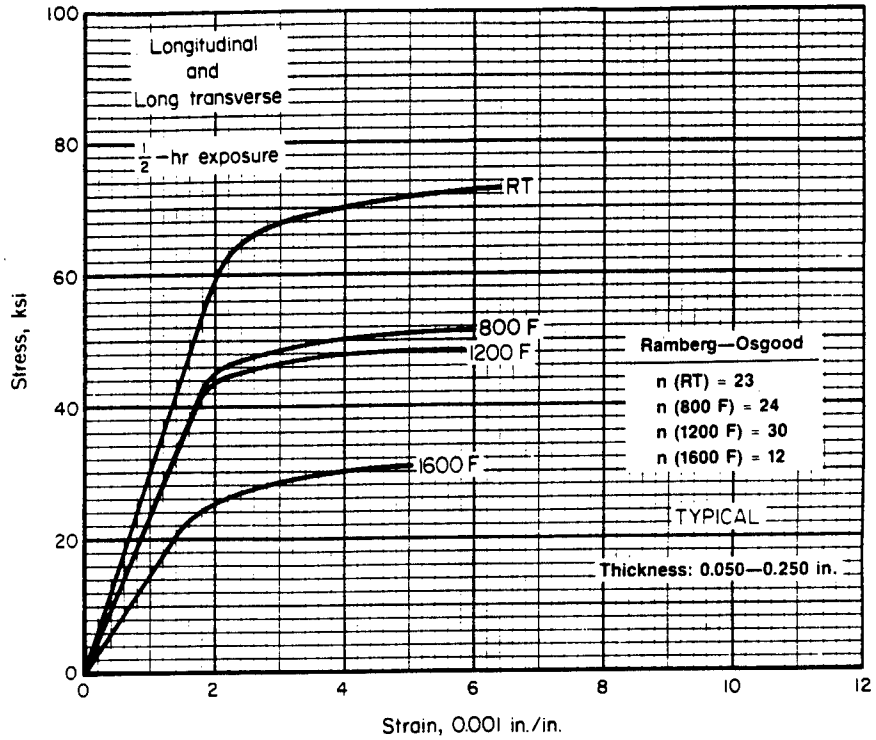


FIGURE 6.3.3.1.6(a). *Typical tensile stress-strain curves for annealed Inconel Alloy 625 sheet at room and elevated temperatures.*

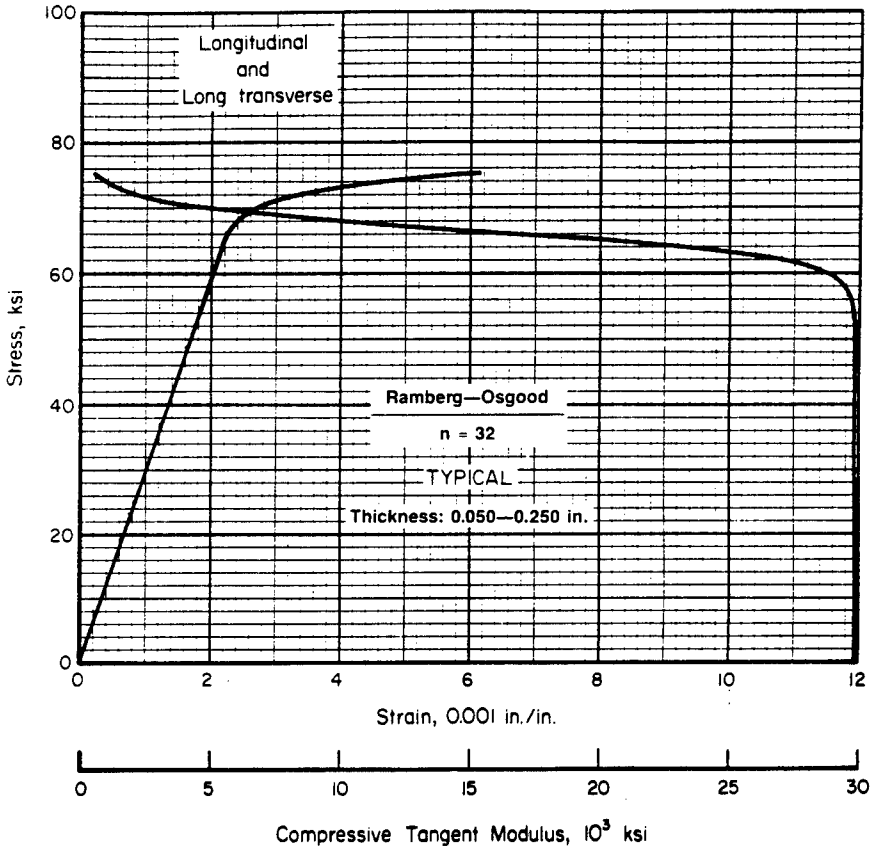


FIGURE 6.3.3.1.6(b). *Typical compressive stress-strain and compressive tangent-modulus curves for annealed Inconel Alloy 625 sheet at room temperature.*

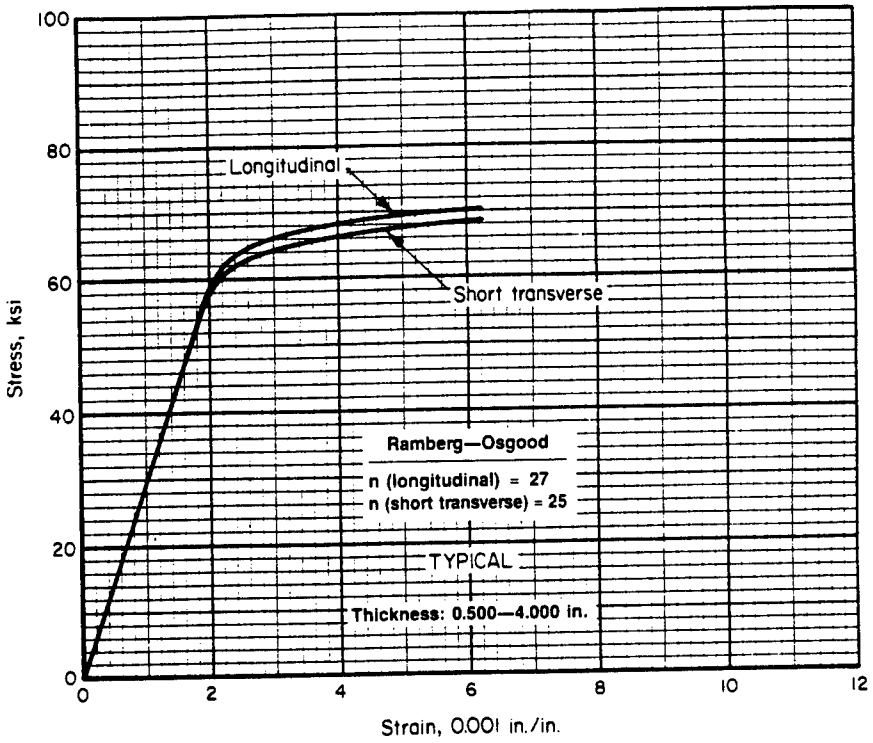


FIGURE 6.3.3.1.6(c). *Typical tensile stress-strain curves for annealed Inconel Alloy 625 bar at room temperature.*

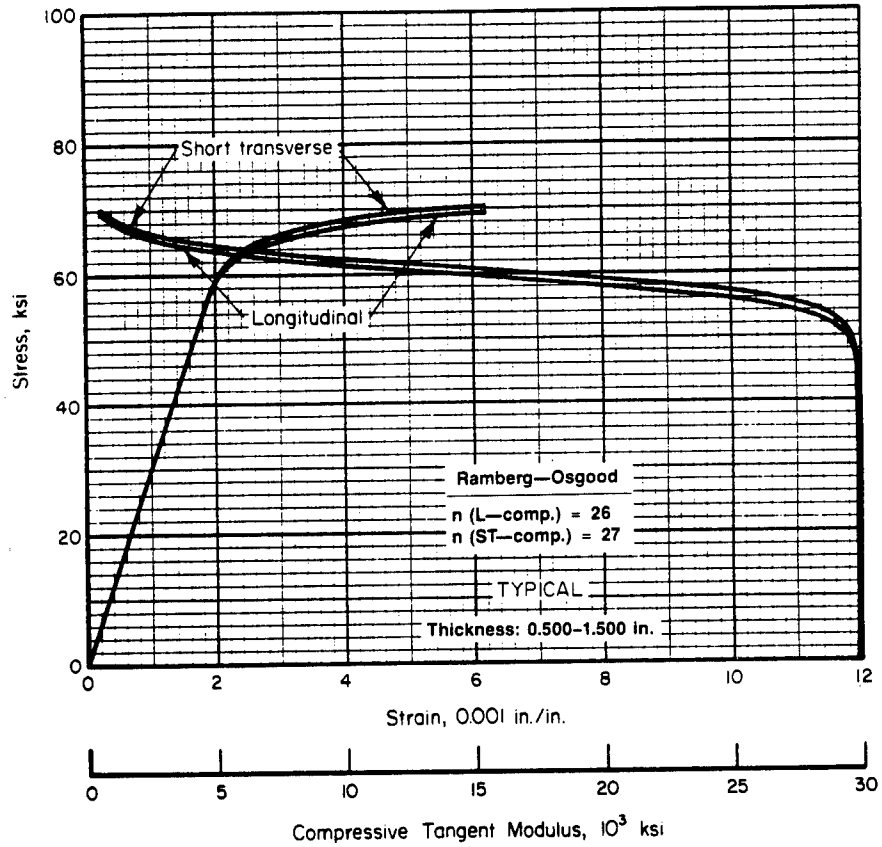


FIGURE 6.3.3.1.6(d). *Typical compressive stress-strain and compressive tangent-modulus curves for annealed Inconel Alloy 625 bar at room temperature.*

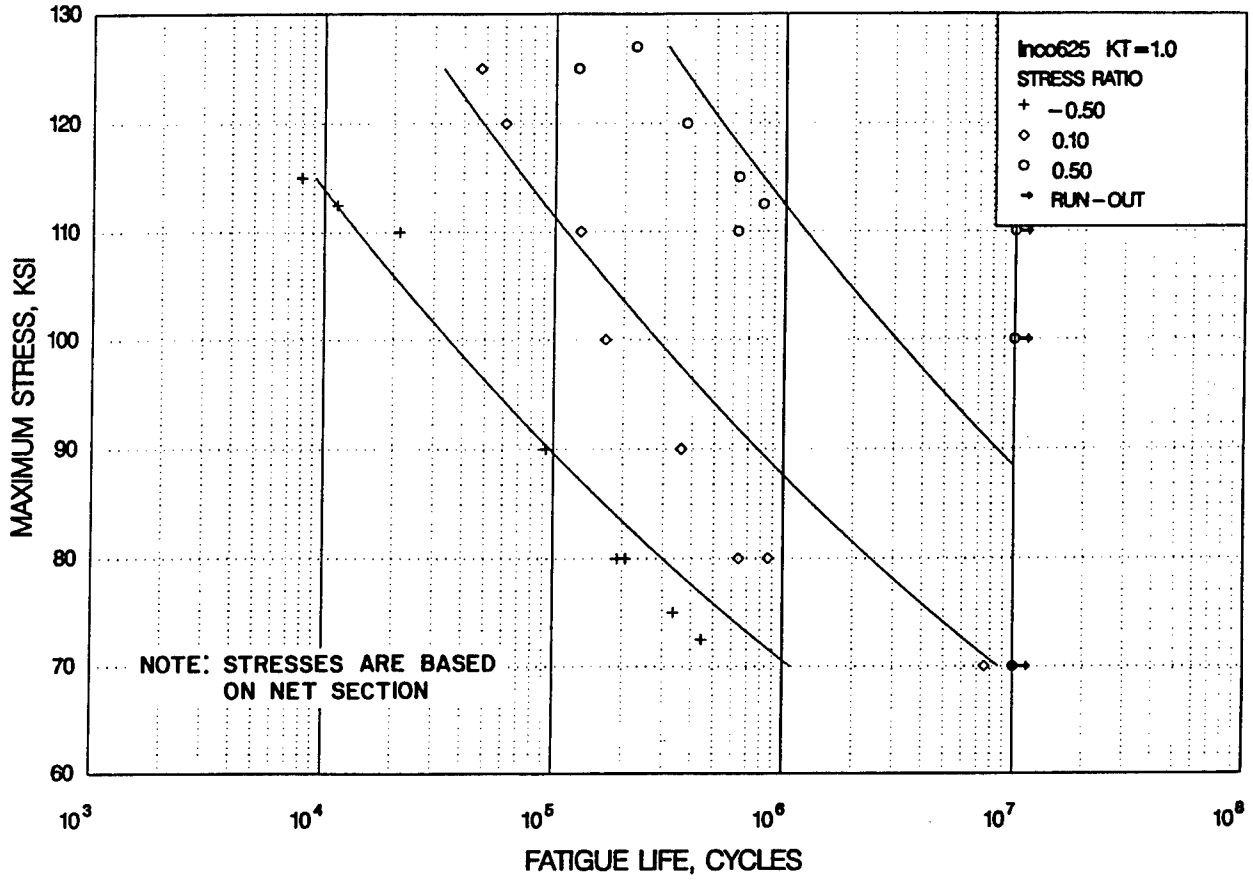


FIGURE 6.3.3.1.8(a). *Best-fit S/N curves for annealed unnotched Inconel 625 bar, longitudinal direction.*

Correlative Information for Figure 6.3.3.1.8(a)

Product Form: Bar, 3/4-inch diameter

Properties:

TUS, ksi	TYS, ksi	Temp., F
133.2	73.8	RT

Specimen Details: Unnotched
0.250-inch diameter

Surface Condition: Longitudinally polished

Reference: 6.3.3.1.8(a)

Test Parameters:
Loading - Axial
Frequency - Unspecified
Temperature - RT
Atmosphere - Air

No. of Heats/Lots: 1

Equivalent Stress Equation:

$$\text{Log } N_f = 24.49 - 9.62 \text{ Log } (S_{eq})$$

$$S_{eq} = S_{max}(1\text{-}R)^{.42}$$

Standard Deviation in log(life) = 22.71 $(1/S_{eq})$

Adjusted R^2 = 90%

Sample Size = 27

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

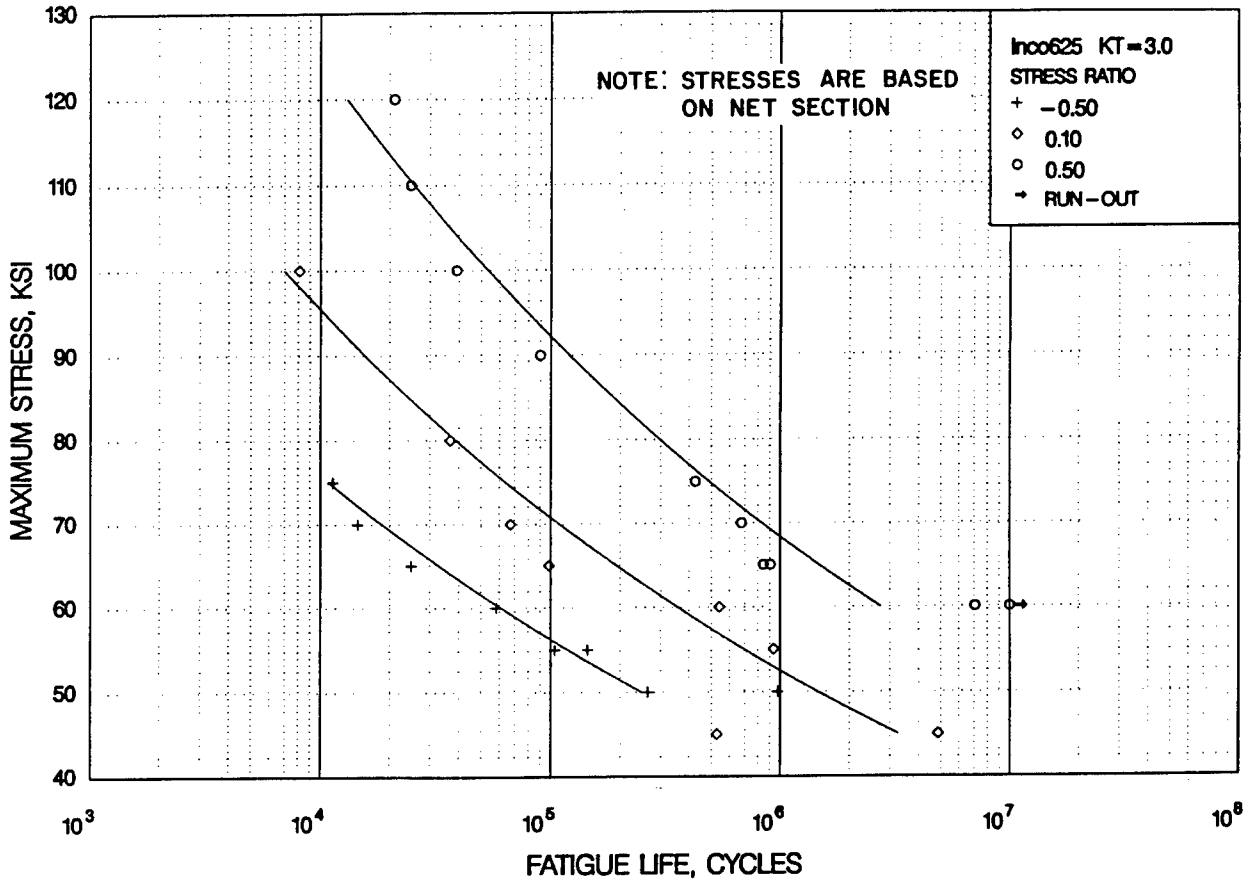


FIGURE 6.3.3.1.8(b). *Best-fit S/N curves for annealed notched Inconel 625 bar, K_t = 3.0, longitudinal direction.*

Correlative Information for Figure 6.3.3.1.8(b)

Product Form: Bar, 3/4-inch diameter

Properties:

TUS, ksi	TYS, ksi	Temp., F
133.2	73.8	RT

Specimen Details: V-Groove, K_t = 3.0
0.375-inch gross diameter
0.250-inch net diameter
0.013-inch root radius
60° flank angle

Surface Condition: Polished

Reference: 6.3.3.1.8(a)

Test Parameters:
Loading - Axial
Frequency - Unspecified
Temperature - RT
Atmosphere - Air

No. of Heats/Lots: 1

Equivalent Stress Equation:

$$\text{Log } N_f = 19.08 - 7.70 \text{ Log } (S_{eq})$$

$$S_{eq} = S_{max}(1\text{-}R)^{.45}$$

Standard Deviation in log(life) = $14.31\ (1/S_{eq})$

Adjusted R^2 = 92%

Sample Size = 26

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

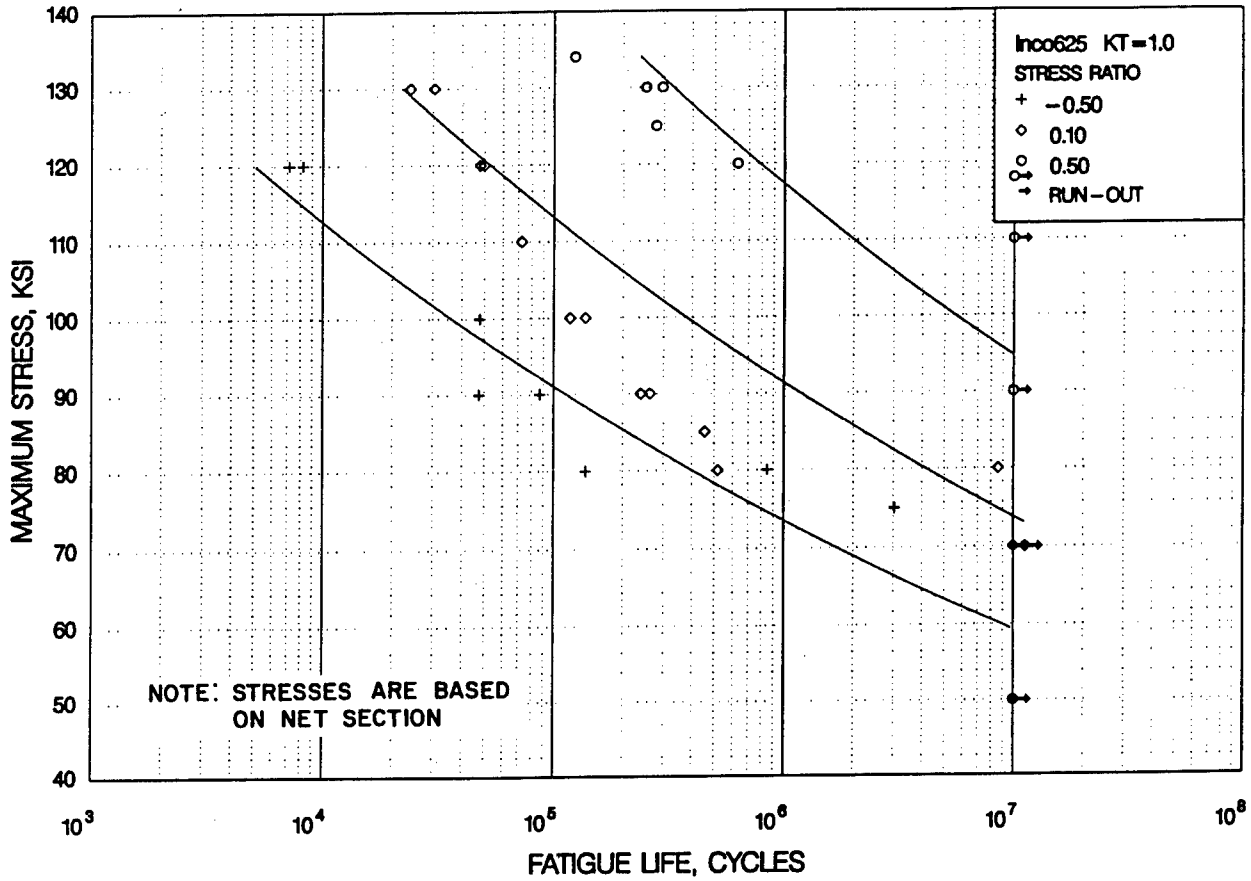


FIGURE 6.3.3.1.8(c). *Best-fit S/N curves for annealed unnotched Inconel 625 sheet, long-transverse direction.*

Correlative Information for Figure 6.3.3.1.8(c)

Product Form: Sheet, 0.093- and 0.125-inch thick

Properties:

TUS, ksi	TYS, ksi	Temp., F
135.4, 136.7	74.6, 69.8	RT

Specimen Details: Unnotched
0.500-inch wide
0.250-inch wide

Surface Condition: As ground

References: 6.3.3.1.8(a) and (b)

Test Parameters:
Loading - Axial
Frequency - Unspecified
Temperature - RT
Atmosphere - Air

No. of Heats/Lots: 2

Equivalent Stress Equation:

$$\text{Log } N_f = 26.91 - 10.77 \text{ Log } (S_{eq})$$

$$S_{eq} = S_{max}(1-R)^{.43}$$

Standard Deviation in log(life) = $37.39\ (1/S_{eq})$

Adjusted R^2 = 75%

Sample Size = 34

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

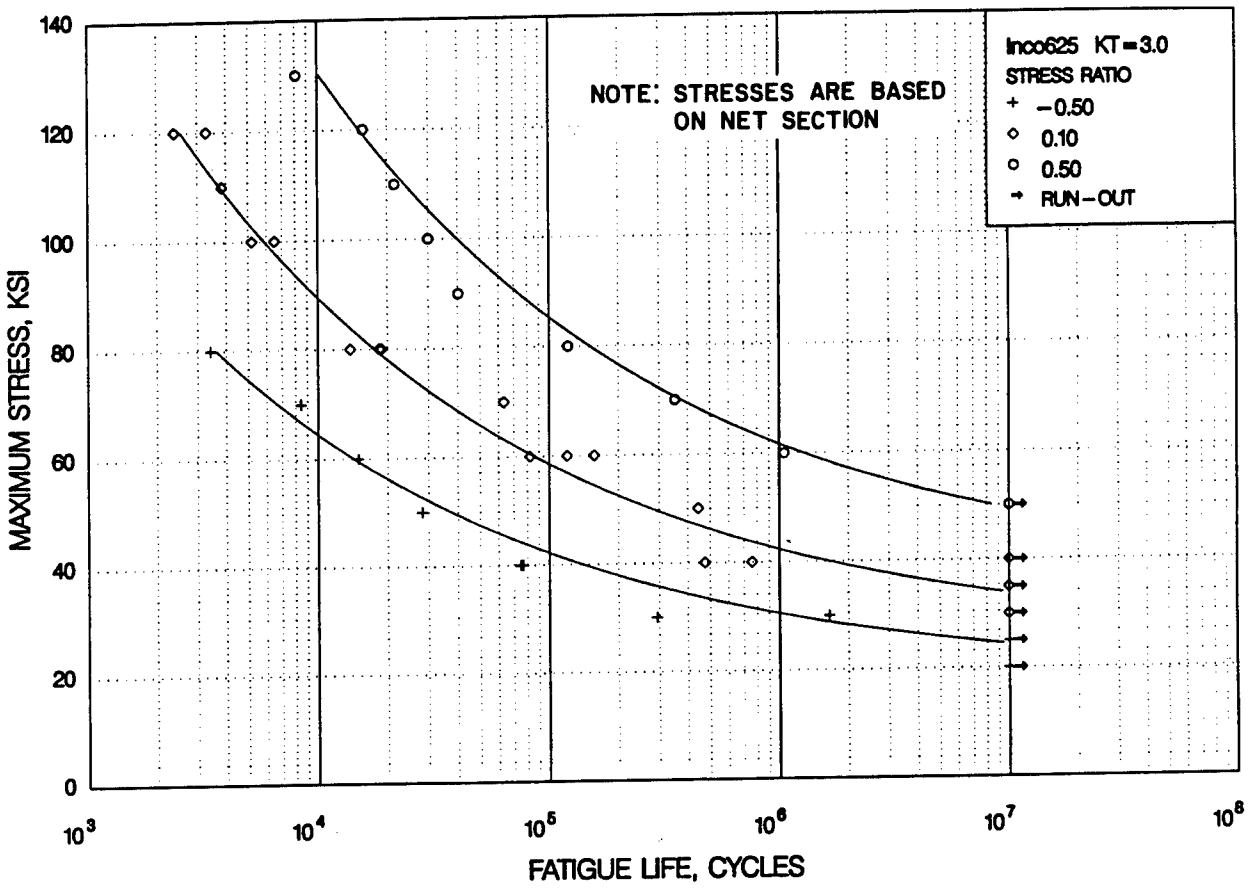


FIGURE 6.3.3.1.8(d). *Best-fit S/N curves for annealed notched Inconel 625 sheet, K_t = 3.0, long transverse direction.*

Correlative Information for Figure 6.3.3.1.8(d)

Product Form: Sheet, 0.093- and 0.125-inch thick

Properties:

TUS, ksi	TYS, ksi	Temp., F
135.4, 136.7	74.6, 69.8	RT

Specimen Details: Edge notched, K_t = 3.0
0.625-inch gross width
0.030-inch root radius
0.375-inch net width
60° flank angle

Surface Condition: As ground

References: 6.3.3.1.8(a) and (b)

Test Parameters:
Loading - Axial
Frequency - Unspecified
Temperature - RT
Atmosphere - Air

No. of Heats/Lots: 2

Equivalent Stress Equation:

$$\text{Log } N_f = 10.35 - 3.56 \text{ Log } (S_{eq} - 22.89)$$

$$S_{eq} = S_{max}(1-R)^{.64}$$

Standard Deviation in log(life) = $10.52\ (1/S_{eq})$

Adjusted R^2 = 96%

Sample Size = 37

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

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6.3.4 INCONEL 706 ALLOY

6.3.4.0 *Comments and Properties.*—Inconel 706 Alloy is a vacuum-melted precipitation-hardened, nickel-base alloy with characteristics similar to Inconel 718 Alloy except that Inconel Alloy 706 has greatly improved machinability. The alloy has good formability and weldability. Like Inconel 718 Alloy, Inconel 706 has excellent resistance to postweld strain-age cracking.

Depending upon choice of heat treatment, this alloy may be used for applications requiring either (1) high resistance to creep and stress rupture up to 1300 F or (2) high-tensile strength at cryogenic temperatures or elevated temperatures for short times. The creep-resistant heat treatment is characterized by an intermediate stabilizing treatment before precipitation hardening. Inconel 706 Alloy also has good resistance to oxidation and corrosion over a broad range of temperatures and environments.

Because of close relationship between heat treatment properties and application, the form and applications are listed with specifications in Table 6.3.4.0(a). Room-temperature mechanical and physical properties are in Table 6.3.4.0(b). The effect of temperature on physical properties is shown in Figure 6.3.4.0.

TABLE 6.3.4.0(a). *Material Specifications for Inconel 706 Alloy*

Specification	Form	Application
AMS 5605	Sheet, strip, and plate	Tensile 1800 F solution treated
AMS 5606	Sheet, strip, and plate	Creep-rupture 1750 F solution treated
AMS 5701	Bar, forging, and ring	Tensile 1800 F solution treated
AMS 5702	Bar, forging, and ring	Creep-rupture 1750 F solution treated
AMS 5703	Bar, forging, and ring	Creep-rupture 1750 F solution treated, stabilized and precipitation treated

6.3.4.1 *Solution-Treated and Aged Condition (Creep Rupture Heat Treatment).*—Effect of temperature on mechanical properties is shown in Figures 6.3.4.1.1, 6.3.4.1.4, and 6.3.4.1.5. Typical tensile stress-strain curves are shown in Figure 6.3.4.1.6(a) and typical compressive stress-strain and tangent-modulus curves in Figure 6.3.4.1.6(b). A full-range tensile stress-strain curve is shown in Figure 6.3.4.1.6(c). Stress-rupture properties are specified at 1200 F; the appropriate specification should be consulted for detailed requirements.

TABLE 6.3.4.0(b). *Design Mechanical and Physical Properties of Inconel 706 Alloy*

Specification	AMS 5605		AMS 5606	AMS 5701		AMS 5702 and AMS 5703	
Form	Sheet, strip, and plate			Bar and forging			
Condition	Heat treated per indicated specification						
Thickness or diameter, in.	≤0.187	0.188-1.000	All	<2.500	2.500-4.000	<2.500	2.500-4.000
Basis	S	S	S	S	S	S	S
Mechanical Properties:							
F_{tu}, ksi:							
L	...	...	...	170	170	170	165
LT	175	170	170	...	...	...	...
F_{ty}, ksi:							
L	...	...	...	140	135	130	130
LT	145	140	135	...	...	...	...
F_{cy}, ksi:							
L	...	...	...	146	141	136	136
LT	152	146	141	...	...	...	...
F_{su}, ksi	109	106	106	106	106	106	103
F_{bru}[a], ksi:							
(e/D = 1.5)	271	263	263	263	263	263	256
(e/D = 2.0)	344	334	334	334	334	334	325
F_{bry}, ksi:							
(e/D = 1.5)	202	195	188	195	188	181	181
(e/D = 2.0)	243	234	226	234	226	218	218
e, percent:							
L	...	...	...	12	12	12	12
LT	12	12	12	...	...	...	...
RA, percent:							
L	...	...	...	15	15	15	15
E, 10^3 ksi	30.4						
E_c, 10^3 ksi	30.4						
G, 10^3 ksi	11.0						
μ	0.38						
Physical Properties:							
ω, lb/in.^{3}	0.292						
C, *K*, and α	See Figure 6.3.4.0						

[a]Bearing values are "dry pin" values per Section 1.4.7.1.

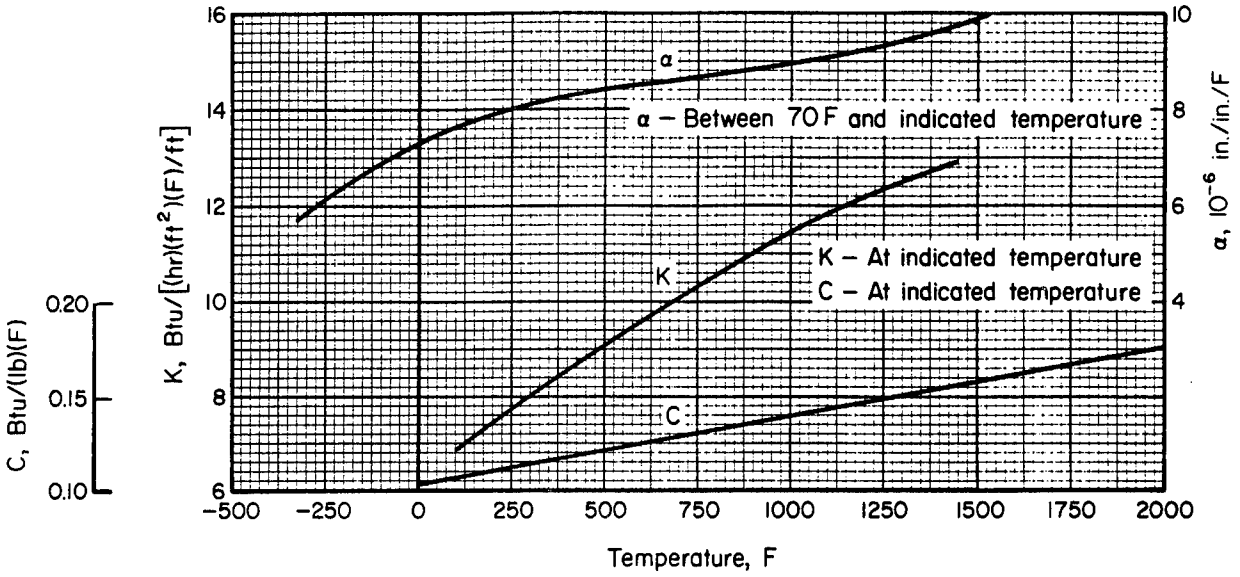


FIGURE 6.3.4.0. *Effect of temperature on the physical properties of solution-treated and aged Inconel 706 Alloy.*

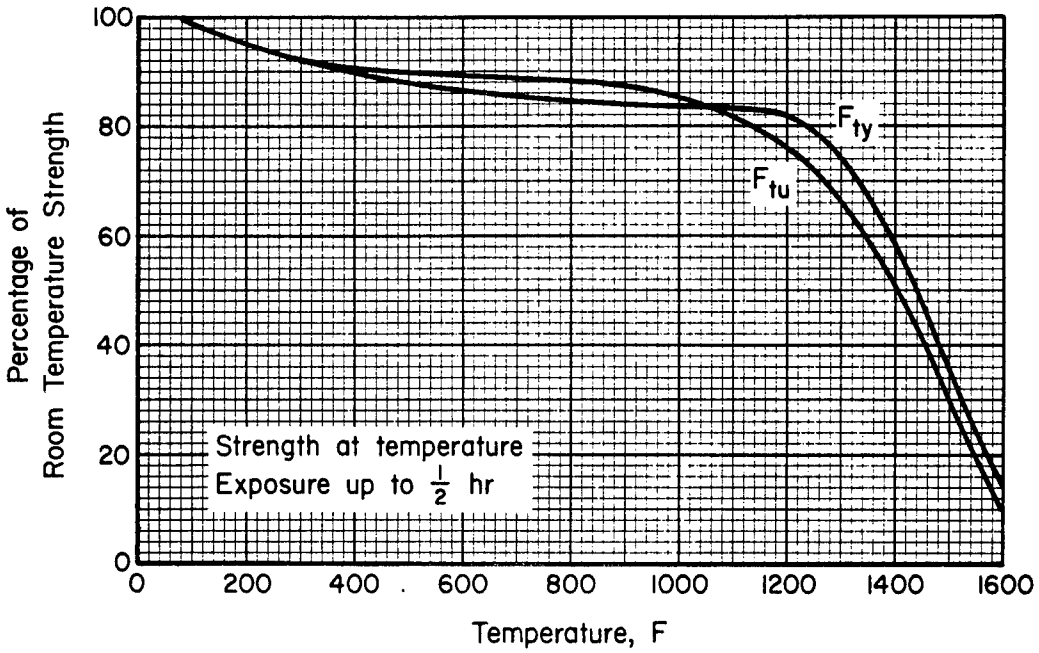


FIGURE 6.3.4.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of solution treated and aged (creep rupture heat treatment)*

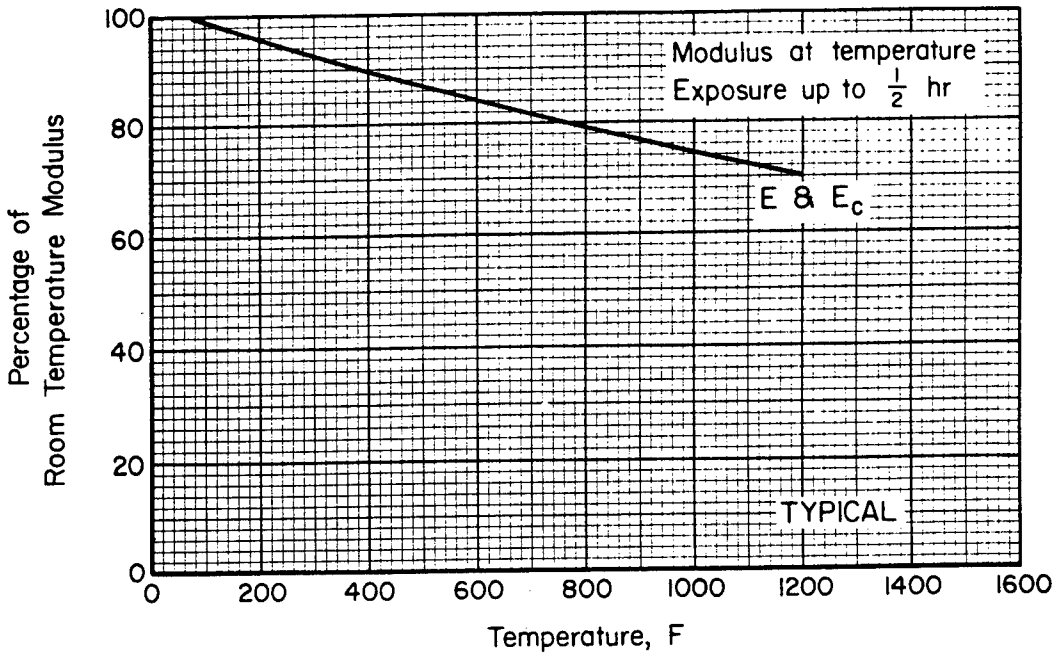


FIGURE 6.3.4.1.4. *Effect of temperature on the tensile and compressive moduli (E and E_c) of Inconel 706 Alloy.*

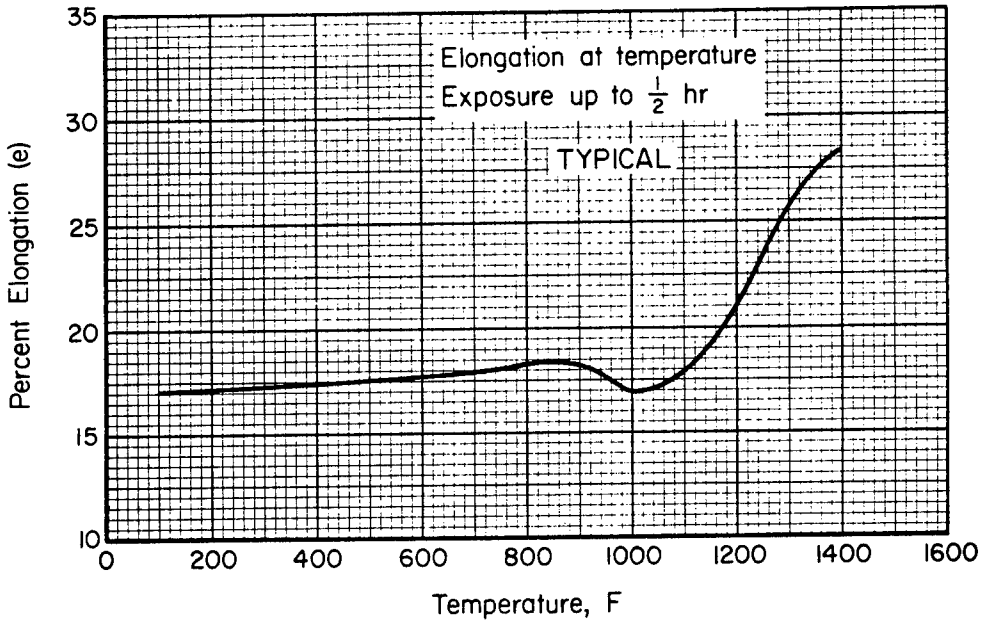


FIGURE 6.3.4.1.5. *Effect of temperature on the elongation (e) of solution treated and aged Inconel 706 Alloy (creep rupture heat treatment).*

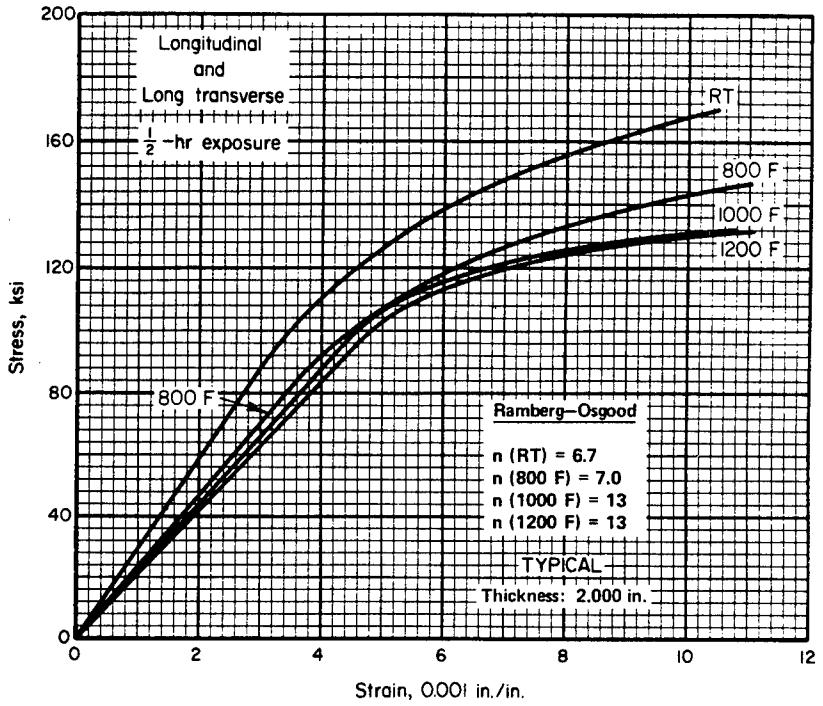


FIGURE 6.3.4.1.6(a). *Typical tensile stress-strain curves for solution-treated and aged Inconel Alloy 706 (creep rupture heat treatment) forged bar.*

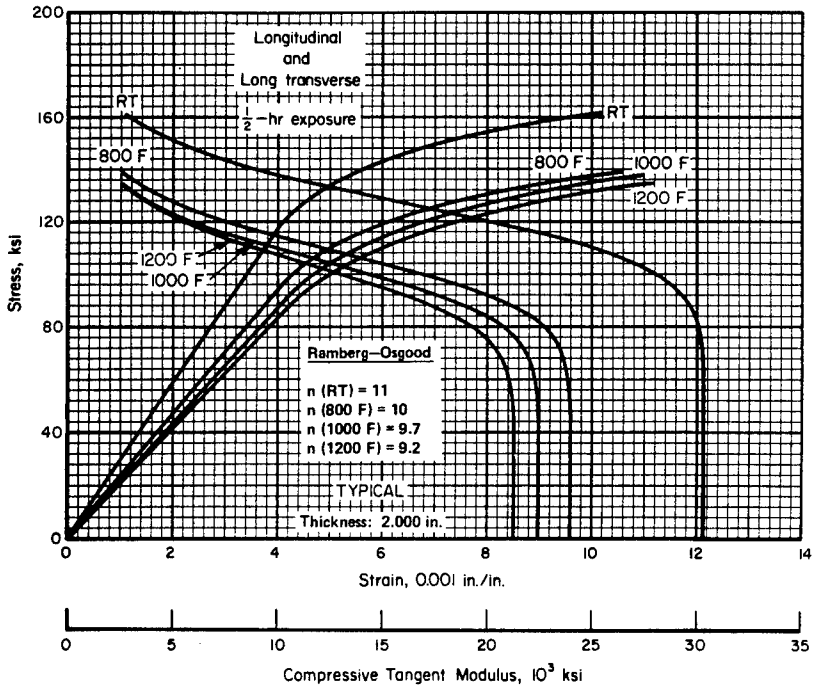


FIGURE 6.3.4.1.6(b). *Typical compressive stress-strain and compressive tangent-modulus curves for solution-treated and aged Inconel Alloy 706 (creep rupture heat treatment) forged bar.*

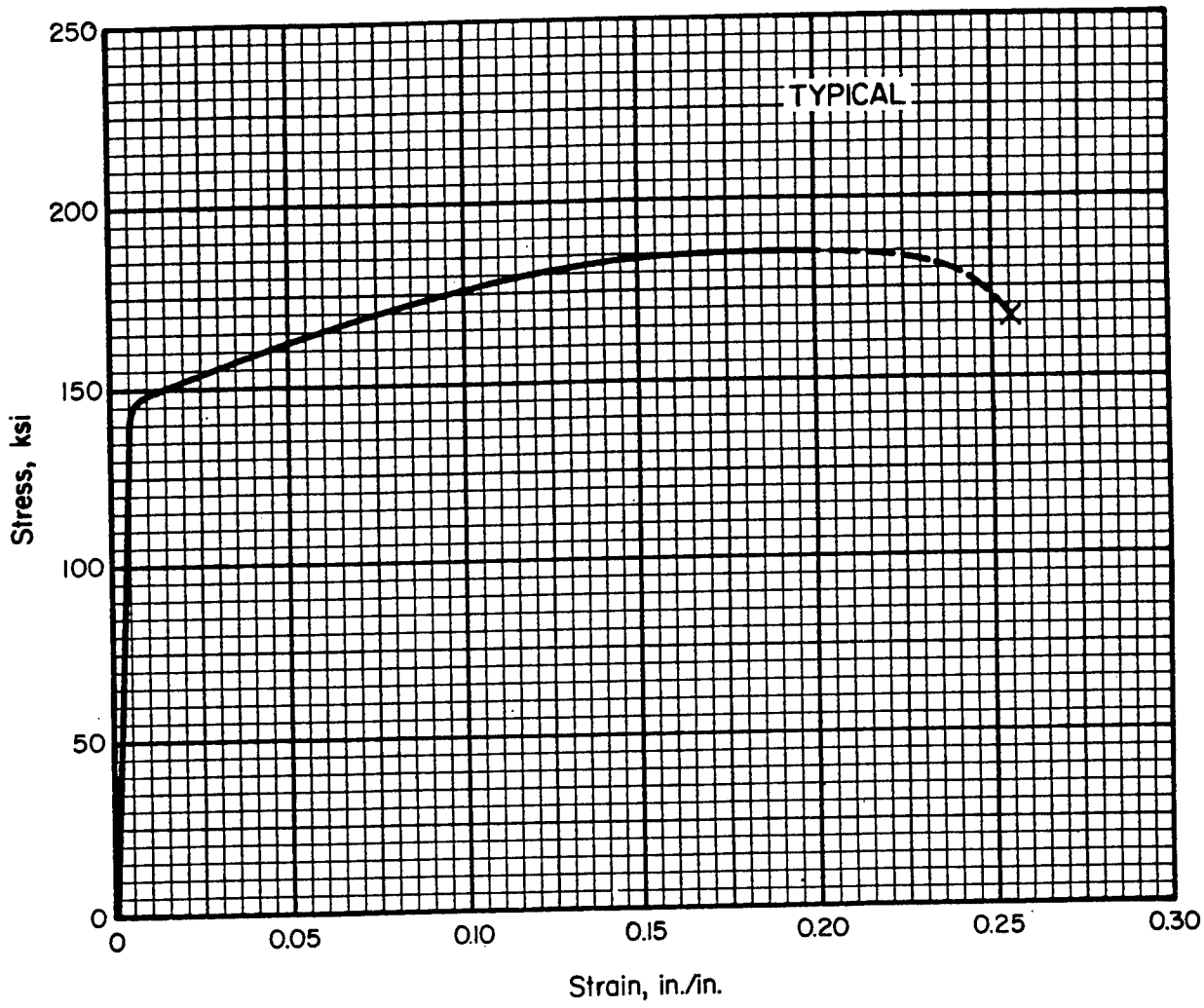


FIGURE 6.3.4.1.6(c). *Typical tensile stress-strain curve (full range) for Inconel Alloy 706 bar and sheet at room temperature (creep rupture heat treatment).*

6.3.5 INCONEL 718

6.3.5.0 *Comments and Properties.*—Inconel 718 is a vacuum-melted, precipitation-hardened nickel-base alloy. It can be welded easily and excels in its resistance to strain-age cracking. It is also readily formable. Depending on choice of heat treatments, this alloy finds applications requiring either (1) high resistance to creep and stress rupture to 1300 F or (2) high strength at cryogenic temperatures for short-time use up to 1000 F. It also has good oxidation resistance up to 1800 F. Inconel 718 is available in all wrought forms and investment castings.

Because of the close relationship between heat treatment, properties, and applications, both the product form and application are listed with the specifications in Table 6.3.5.0(a). Room-temperature mechanical and physical properties are presented in Tables 6.3.5.0(b) through (d). The effect of temperature on physical properties is presented in Figure 6.3.5.0.

6.3.5.1 *Solution-Treated and Aged Condition.*—Elevated-temperature curves are presented in Figures 6.3.5.1.1 and 6.3.5.1.4(a) through (c). Typical tensile and compressive stress-strain curves as well as typical compressive tangent-modulus curves for sheet and castings are shown in Figures 6.3.5.1.6(a) through (c). Figure 6.3.5.1(a) is a typical (full-range) stress-strain curve for Inconel 718 investment casting.

TABLE 6.3.5.0(a). *Material Specifications for Inconel 718 Alloy*

Specification	Form	Application
AMS 5589	Tubing	Creep-rupture
AMS 5590	Tubing	Short-time
AMS 5596	Sheet, strip, plate	Creep-rupture
AMS 5597	Sheet, strip, plate	Short-time
AMS 5662, 5663	Bar, forging	Creep-rupture
AMS 5664	Bar, forging	Short-time
AMS 5383	Investment castings	Short-time

Creep and stress-rupture curves for forging are shown in Figures 6.3.5.1.7(a) through (e). Supplemental creep and stress-rupture information for forging is presented in Table 6.3.5.1.7(f). Fatigue S/N curves are presented in Figures 6.3.5.1.8(a) through (g). Fatigue-crack-propagation data for die forging and plate are presented in Figures 6.3.5.1.9(a) through (c).

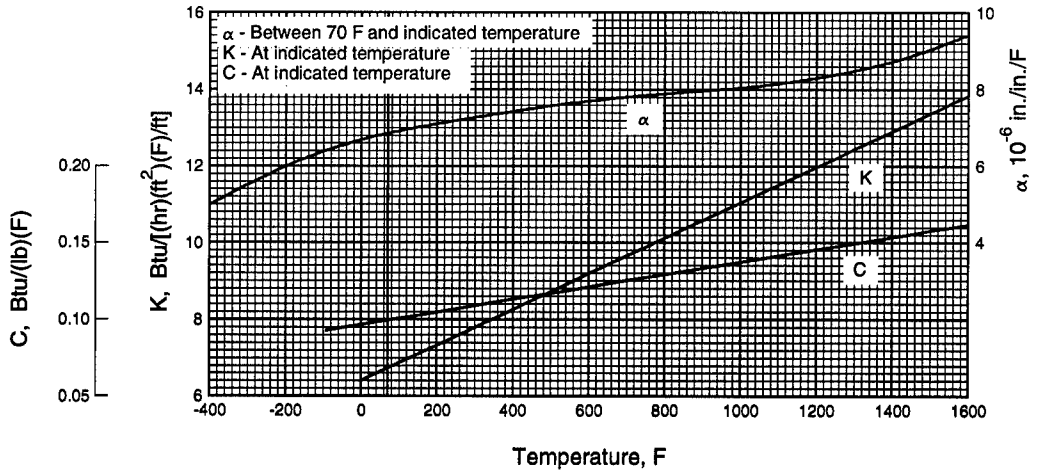


FIGURE 6.3.5.0. *Effect of temperature on the physical properties of Inconel 718 Alloy.*

TABLE 6.3.5.0(b). *Design Mechanical and Physical Properties of Inconel 718 Alloy*

Specification	AMS 5596				AMS 5597	AMS 5589	AMS 5590
Form	Sheet		Plate		Sheet and plate	Tubing	
Condition	Solution treated and aged per indicated specification						
Thickness, in.	0.010-0.187		0.188-0.249	0.250-1.000	0.010-1.000	O.D. > 0.125 Wall > 0.015	
Basis	A	B	S	S	S	S	S
Mechanical Properties[a]:							
F_{tu}, ksi:							
L	180	192	180	...	...	185	170
LT	180[c]	191	180	180	180	...	...
F_{ty}, ksi:							
L	145	156	148	...	...	150	145
LT	147	158	150	150	150	...	...
F_{cy}, ksi:							
L	155	167	158	...	...	...	...
LT	158	170	161	...	...	...	...
F_{su}, ksi	124	132	124	...	...	...	...
F_{bru}[b], ksi:							
(e/D = 1.5)	291	309	291	...	...	...	...
(e/D = 2.0)	380	403	380	...	...	...	...
F_{bry}[b], ksi:							
(e/D = 1.5)	208	223	212	...	...	...	...
(e/D = 2.0)	241	259	246	...	...	...	...
e, percent (S-basis):							
L	...	...	...	...	...	12	15
LT	12	...	12	12	12	...	...
E, 10^3 ksi	29.4						
E_c, 10^3 ksi	30.9						
G, 10^3 ksi	11.4						
μ	0.29						
Physical Properties:							
ω, lb/in.^{3}	0.297						
C, K, and α	See Figure 6.3.5.0						

[a]Design allowables were based upon data from samples of material, supplied in the solution treated condition, which were aged to demonstrate heat treatment response by suppliers. Properties obtained by the user may be different, if the material has been formed or otherwise cold worked.
[b]Bearing values are "dry pin" values per Section 1.4.7.1.
[c]S-basis. The A value is 183 ksi.

TABLE 6.3.5.0(c). *Design Mechanical and Physical Properties of Inconel 718 Alloy Bar and Forging*

Specification	AMS 5662 and AMS 5663								AMS 5664	
Form	Bar							Forging	Bar	Forging
Condition	Solution treated and aged per indicated specification									
Thickness, in.	0.250-1.000	1.001-1.500	1.501-2.000	2.001-2.500	2.501-3.000	3.001-4.000	4.001-5.000	≤5.000	≤10.000	≤10.000
Basis	S	S	S	S	S	S	S	S	S	S
Mechanical Properties:										
F_{tu}, ksi:										
L	185	185	185	185	185	185	185	185	185	180
LT[b]	180	180	180	180	180	180	180	180	180	180
ST[b]	...	...	...	...	180	180	180	...	...	180
F_{ty}, ksi:										
L	150	150	150	150	150	150	150	150	150	150
LT[b]	150	150	150	150	150	150	150	150	150	150
ST[b]	...	...	...	...	146	150	150	...	...	150
F_{cy}, ksi:										
L	156	156	156	156	156	156	156	...	...	...
ST	...	...	...	156	156	156	156	...	...	...
F_{su}, ksi	111	114	116	118	119	121	123	...	...	...
F_{bru}[a], ksi:										
(e/D = 1.5)	309	309	309	309	309	309	309	...	...	...
(e/D = 2.0)	394	394	394	394	394	394	394	...	...	...
F_{bry}[a], ksi:										
(e/D = 1.5)	216	216	216	216	216	216	216	...	...	...
(e/D = 2.0)	257	257	257	257	257	257	257	...	...	...
e, percent:										
L	12	12	12	12	12	12	12	12	10	12
LT[b]	6	6	6	6	6	6	6	10	10	12
ST[b]	...	...	...	...	6	6	6	...	10	12
RA, percent:										
L	15	15	15	15	15	15	15	15	12	15
LT[b]	8	8	8	8	8	8	8	12	12	15
ST[b]	...	...	...	...	8	8	8	...	12	15
E, 10^3 ksi:										
L										
LT										
E_c, 10^3 ksi:										
L										
LT										
G, 10^3 ksi										
μ										
Physical Properties:										
ω, lb/in.^{3}	0.297									
C, K, and α	See Figure 6.3.5.0									

[a]Bearing values are dry pin values per Section 1.4.7.1.
[b]Applicable providing LT or ST direction is ≥2.500 inches.

TABLE 6.3.5.0(d). *Design Mechanical and Physical Properties of Inconel 718 Alloy Investment Castings*

Specification	AMS 5383
Form	Investment Casting
Condition	STA
Location within casting	Any
Thickness, in.	≤0.500
Basis	S
Mechanical Properties:	
F_{tu}, ksi	120
F_{ty}, ksi	105
F_{cy}, ksi	105
F_{su}, ksi	88[a]
F_{bru}[b], ksi:	
(e/D = 1.5)	202
(e/D = 2.0)	248
F_{bry}[b], ksi:	
(e/D = 1.5)	161
(e/D = 2.0)	188
e, percent	3
RA, percent	8
E, 10^3 ksi	29.4
E_c, 10^3 ksi	30.9
G, 10^3 ksi	11.4
μ	0.29
Physical Properties:	
ω, lb/in.^{3}	0.297
C, K, and α	See Figure 6.3.5.0

[a]Determined in accordance with ASTM Procedure B769.
[b]Bearing values are "dry pin" values per Section 1.4.7.1.

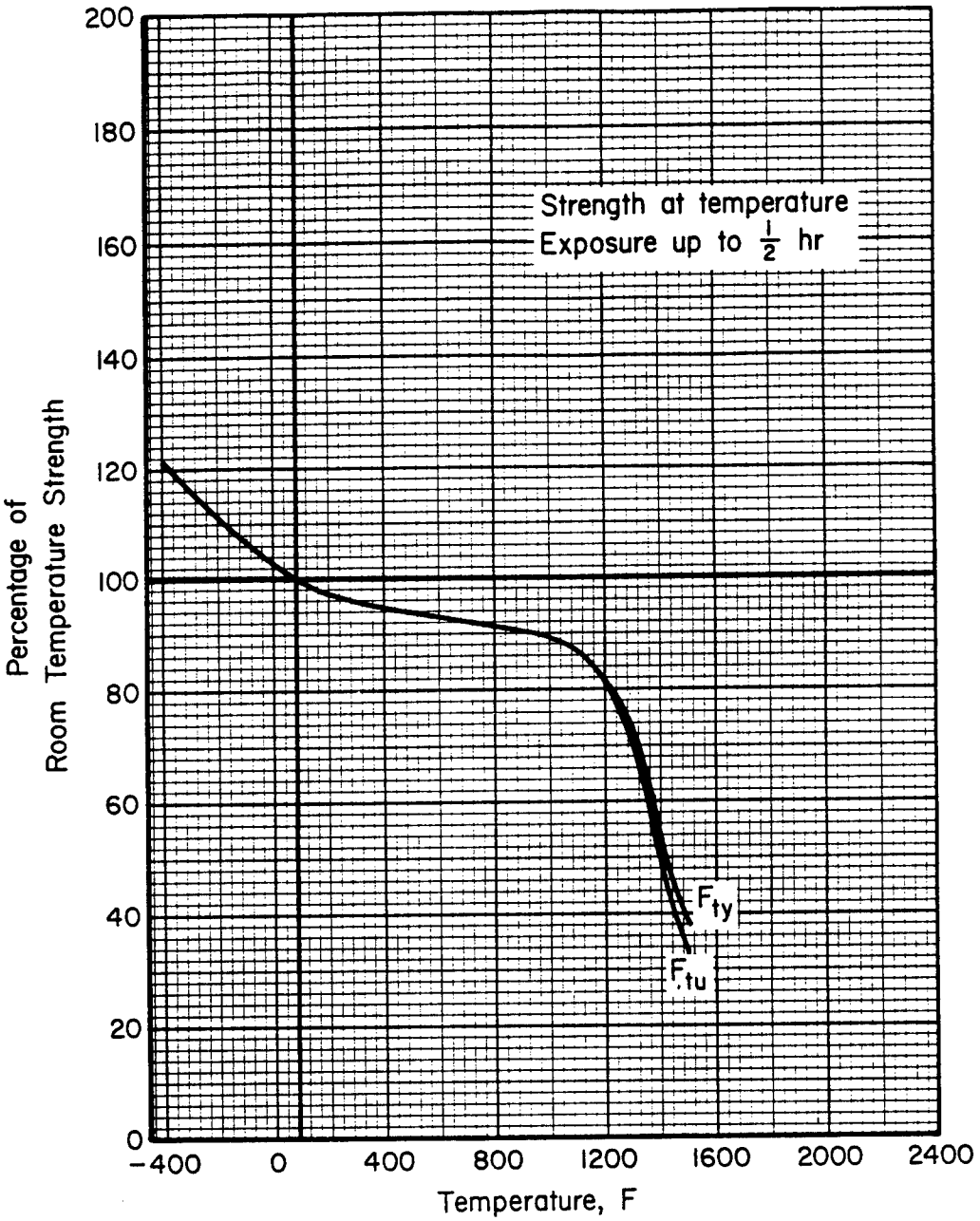


FIGURE 6.3.5.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and tensile yield strength (F_{ty}) of solution-treated and aged Inconel 718 alloy.*

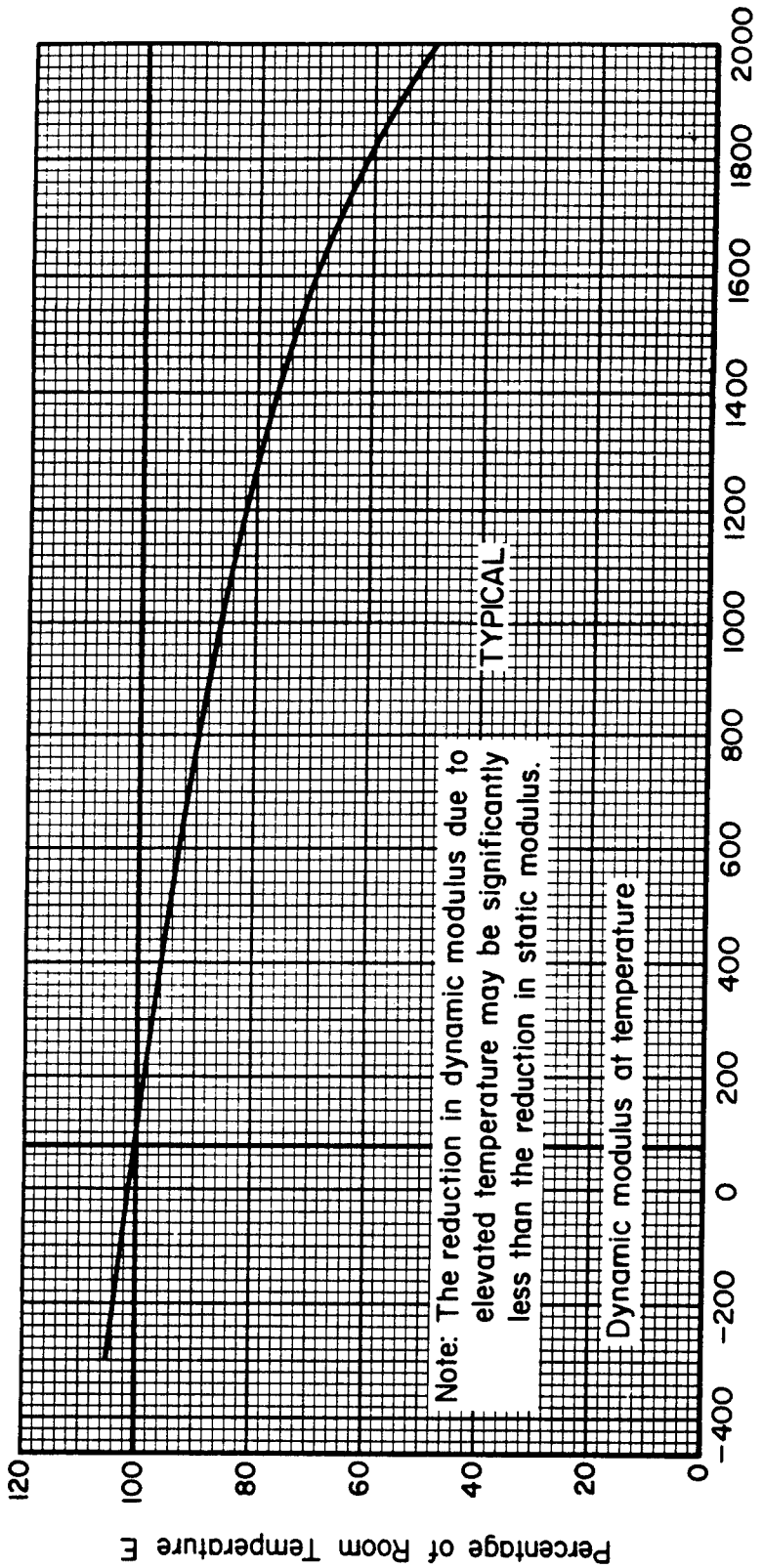


FIGURE 6.3.5.1.4(a). *Effect of temperature on dynamic tensile modulus (E) of solution-treated and aged Inconel 718 alloy.*

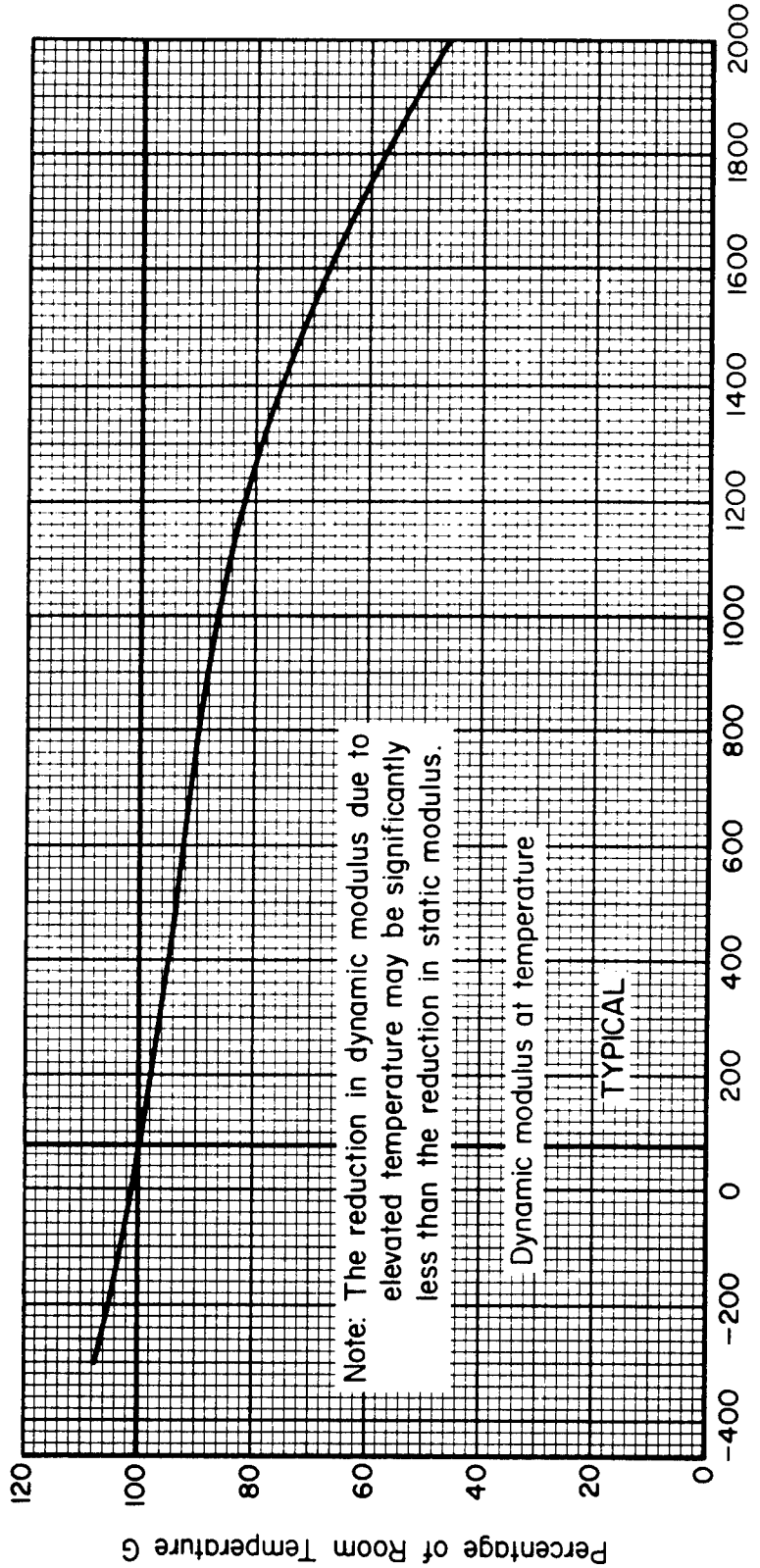


FIGURE 6.3.5.1.4(b). *Effect of temperature on dynamic shear modulus (G) of solution treated and aged Inconel 718 alloy.*

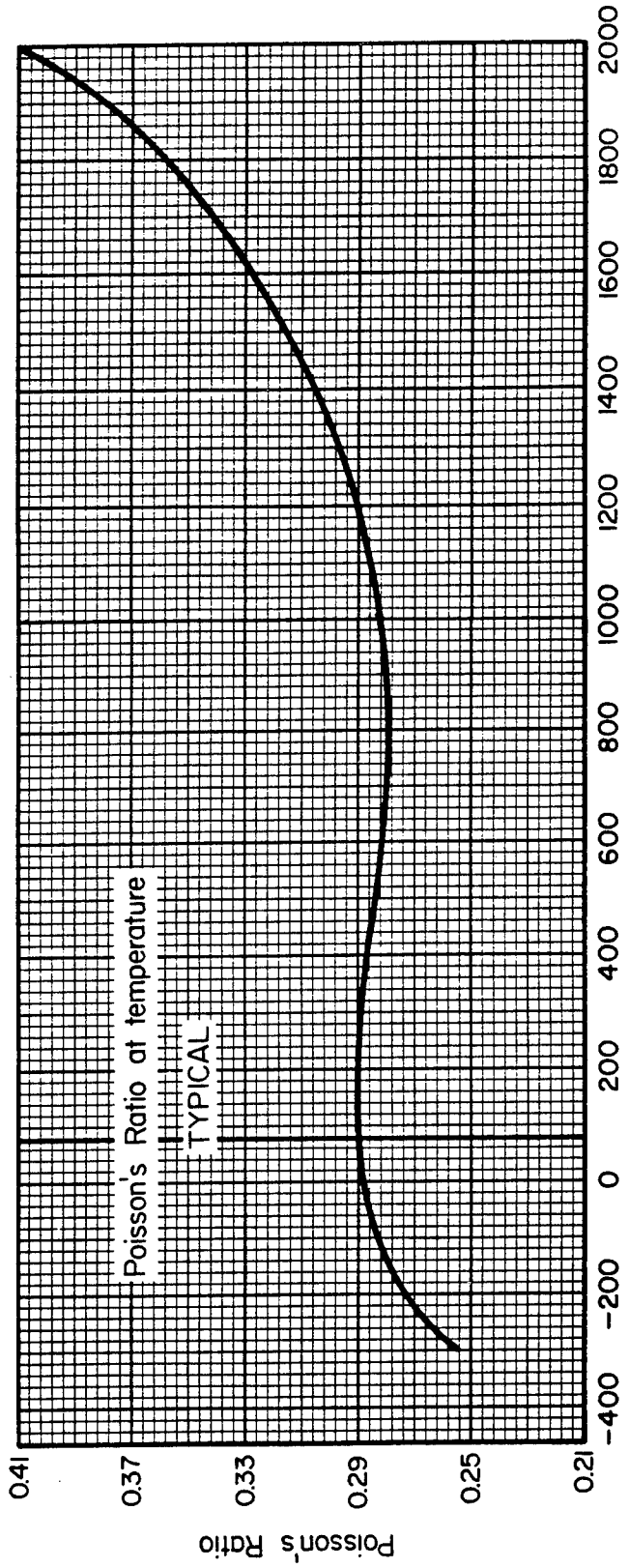


FIGURE 6.3.5.1.4(c). *Effect of temperature on Poisson's ratio (μ) for solution-treated and aged Inconel 718 alloy.*

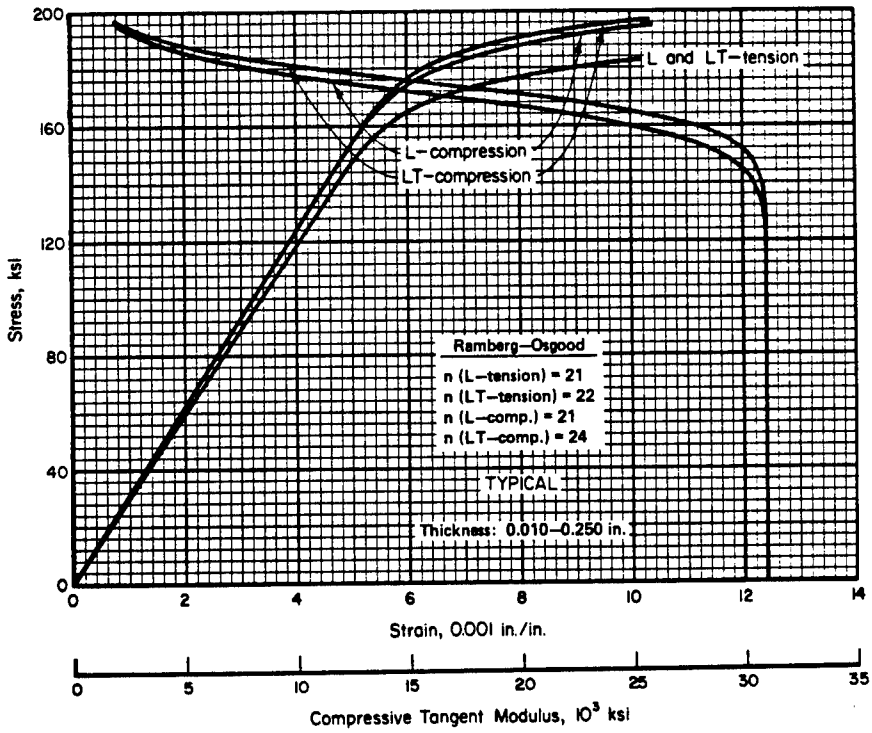


FIGURE 6.3.5.1.6(a). *Typical tensile stress-strain, compressive stress-strain, and compressive tangent-modulus curves for solution-treated and aged Inconel 718 sheet (AMS 5596) at room temperature.*

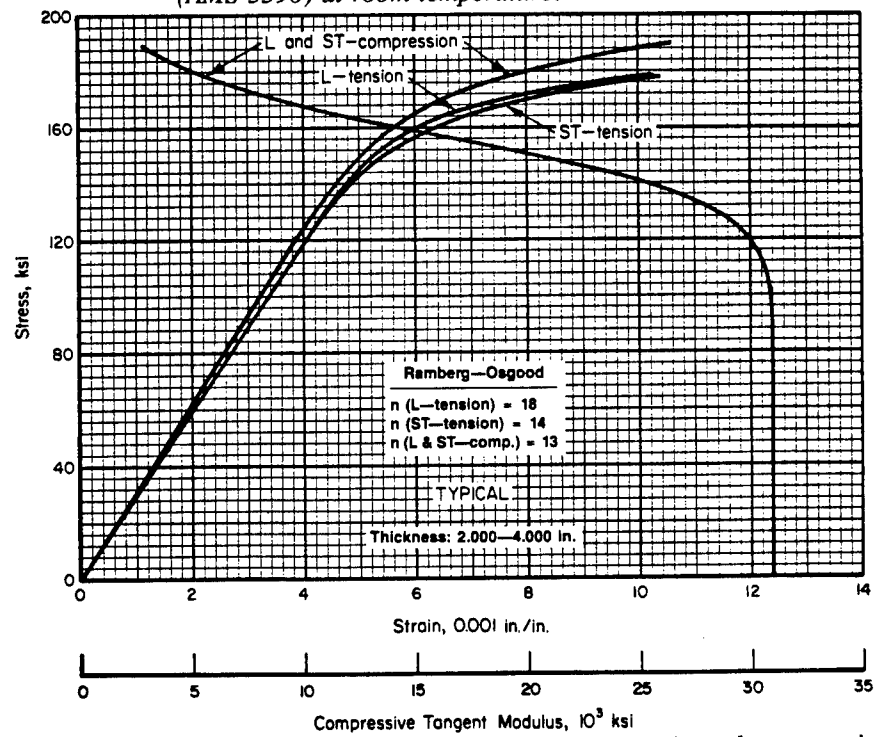


FIGURE 6.3.5.1.6(b). *Typical tensile and compressive stress-strain and compressive tangent-modulus curves for solution treated and aged (creep-rupture application) Inconel 718 alloy bar (AMS 5662 and AMS 5663) at room temperature.*

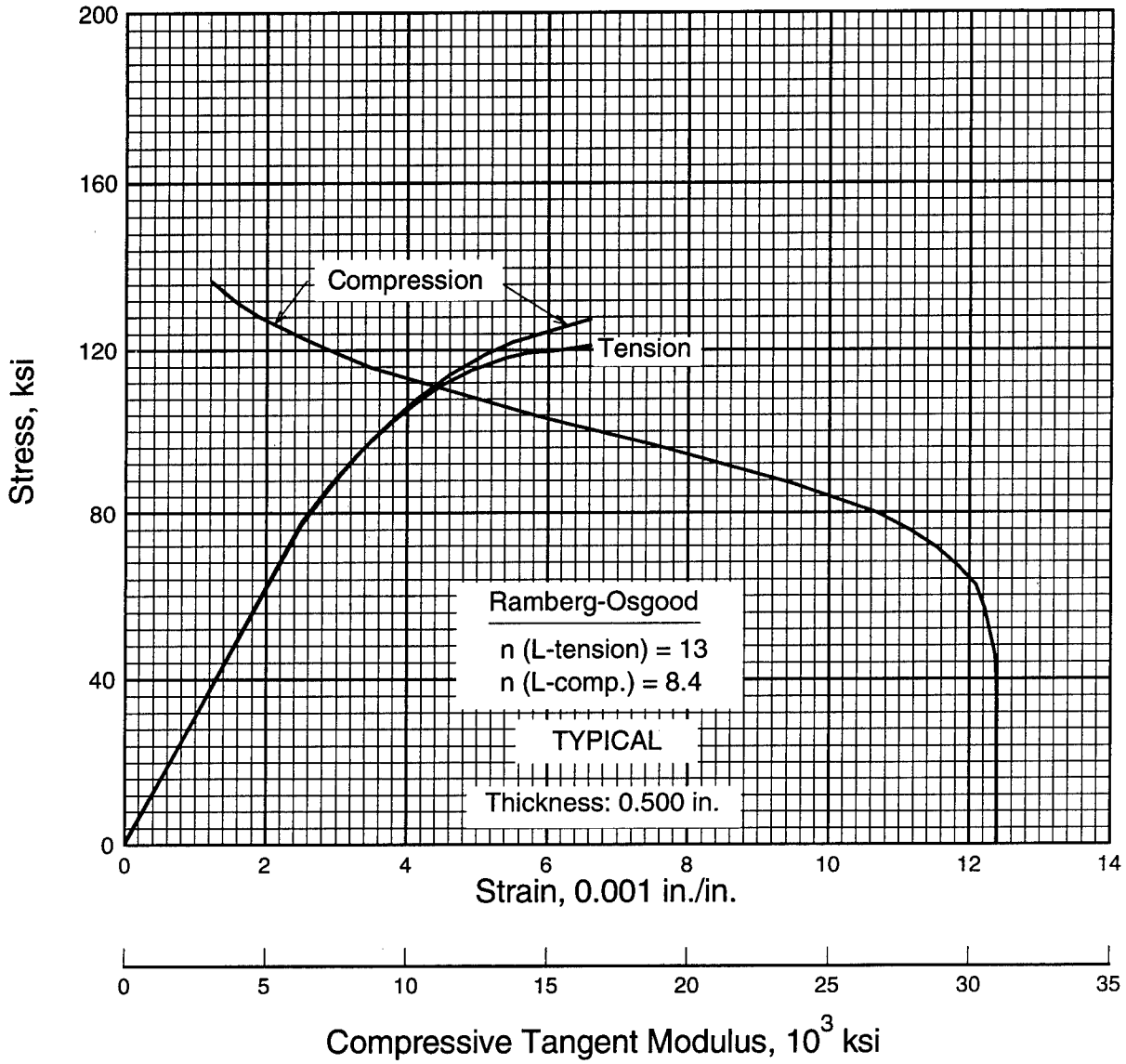
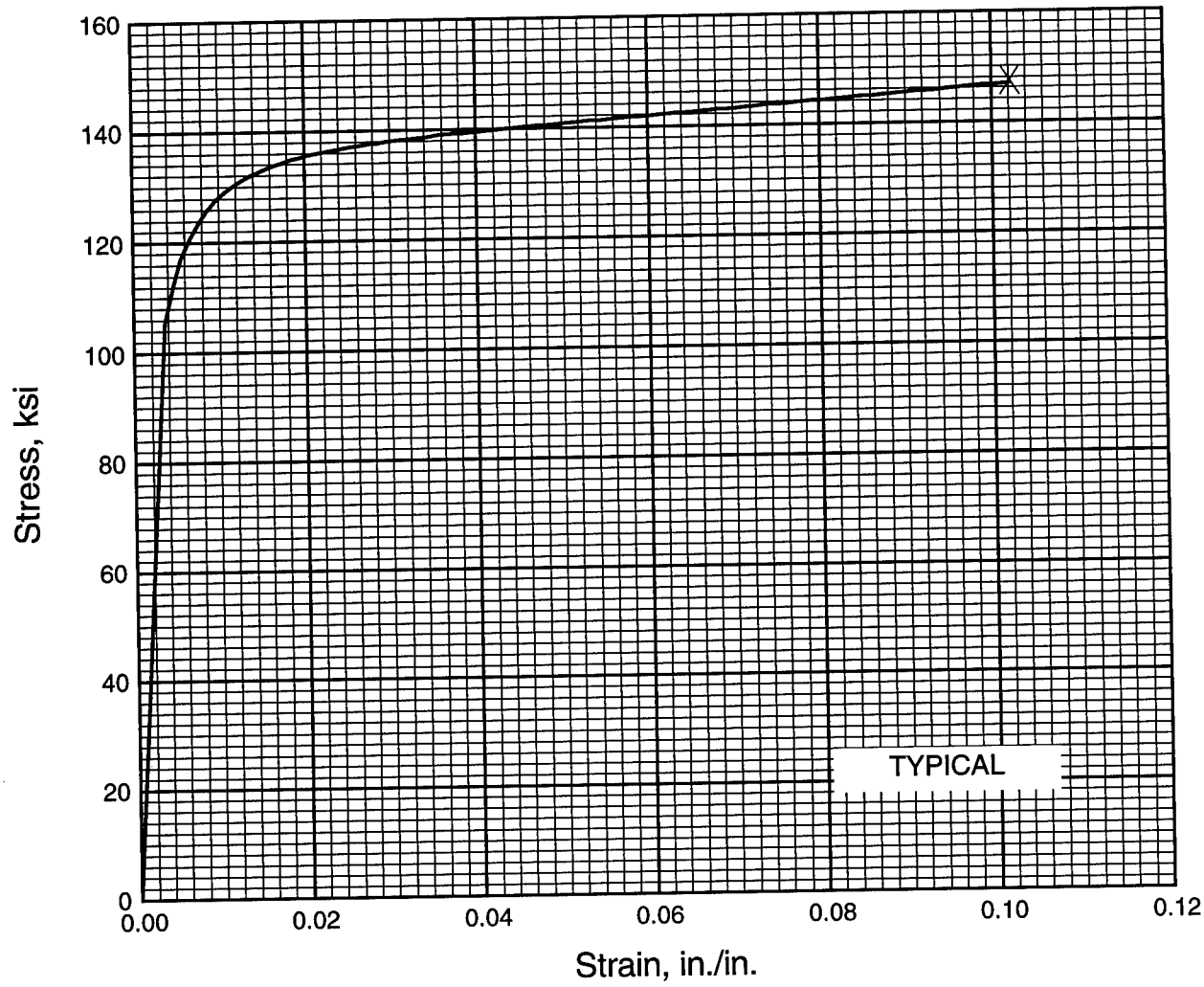


FIGURE 6.3.5.1.6(c). *Typical tensile stress-strain, compressive stress-strain, and compressive tangent-modulus curves for solution treated and aged Inconel 718 alloy investment casting (AMS 5383)at room temperature.*



FIGUR E 6.3.5.1.6(d). *Typical tensile stress-strain curve (full range) for solution treated and aged Inconel 718 investment casting (AMS 5383) at room temperature.*

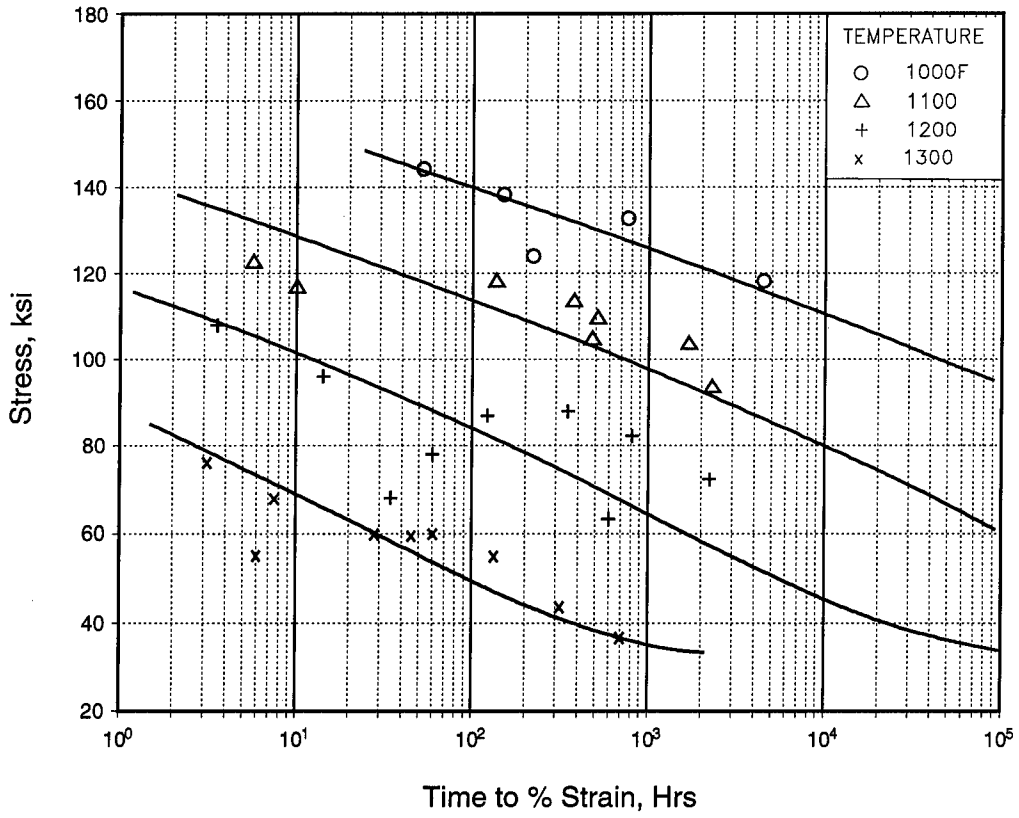


FIGURE 6.3.5.1.7(a). *Average isothermal 0.10% creep curves for Inconel 718 alloy forging.*

Correlative Information for Figure 6.3.5.1.7(a)

Makeup of Data Collection:

Heat Treatment: 2 [See Table 6.3.5.1.7(f)]
Number of Vendors = Unknown
Number of Lots = 2
Number of Test Laboratories = 1
Number of Tests = 32

Specimen Details:

Type - Unnotched round bar
Gage Length - N.A.
Gage Thickness - 1/4" - 3/8"

0.10 Percent Creep Equation:

$\text{Log } t = c + b_1 T + b_2 X + b_3 X^2 + b_4 X^3$

T= °R
X= log (stress, ksi)
c = 185.16
b_1= 0.01778
b_2= -255.25
b_3= 146.28
b_4= -28.65

Analysis Details:

Inverse Matrix = [See Table 6.3.5.1.7(f)]
Standard Deviation = 0.99
Standard Error of Estimate = 0.56

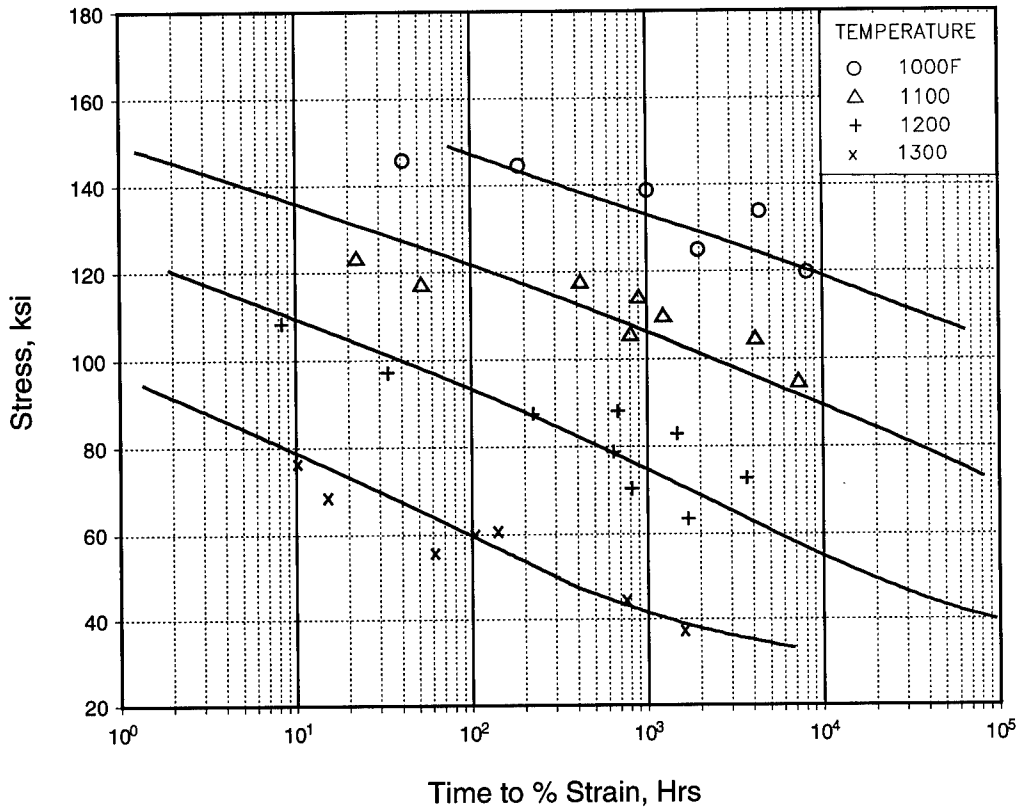


FIGURE 6.3.5.1.7(b). *Average isothermal 0.20% creep curves for Inconel 718 forging.*

Correlative Information for Figure 6.3.5.1.7(b)

Makeup of Data Collection:

Heat Treatment: 2 [See Table 6.3.5.1.7(f)]
Number of Vendors = Unknown
Number of Lots = 2
Number of Test Laboratories = 1
Number of Tests = 31

Specimen Details:

Type - Unnotched round bar
Gage Length - N.A.
Gage Thickness - 1/4" - 3/8"

0.20 Percent Creep Equation:

$\text{Log } t = c + b_1 T + b_2 X + b_3 X^2 + b_4 X^3$

T= °R
X= log (stress, ksi)
c = 185.67
b_1= -0.01778
b_2= -255.25
b_3= 146.28
b_4= -28.65

Analysis Details:

Inverse Matrix = [See Table 6.3.5.1.7(f)]
Standard Deviation = 0.98
Standard Error of Estimate = 0.41

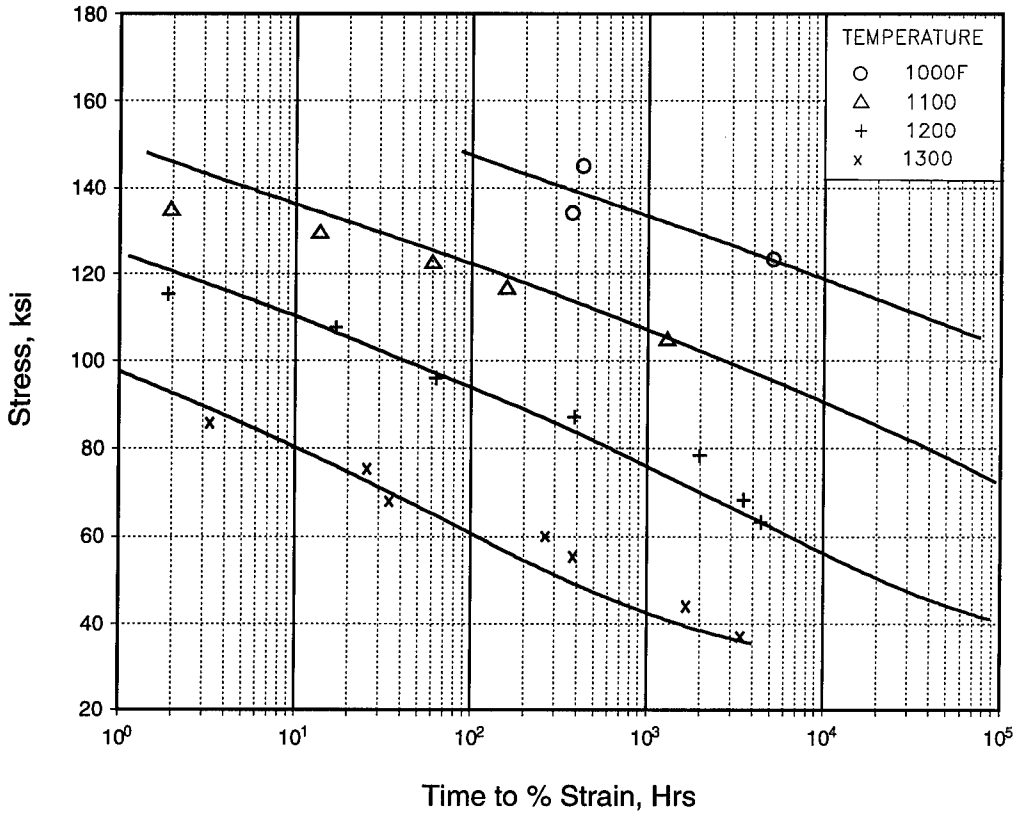


FIGURE 6.3.5.1.7(c). *Average isothermal 0.50% creep curves for Inconel 718 forging.*

Correlative Information for Figure 6.3.5.1.7(c)

Makeup of Data Collection:

Heat Treatment: 2 [See Table 6.3.5.1.7(f)]
Number of Vendors = Unknown
Number of Lots = 2
Number of Test Laboratories = 1
Number of Tests = 22

Specimen Details:

Type - Unnotched round bar
Gage Length - N.A.
Gage Thickness - 1/4" - 3/8"

0.50 Percent Creep Equation:

$\text{Log } t = c + b_1 T + b_2 X + b_3 X^2 + b_4 X^3$

T= °R
X= log (stress, ksi)
c = 185.75
b_1= -0.01778
b_2= -255.25
b_3= 146.28
b_4= -28.65

Analysis Details:

Inverse Matrix = [See Table 6.3.5.1.7(f)]
Standard Deviation = 1.10
Standard Error of Estimate = 0.34

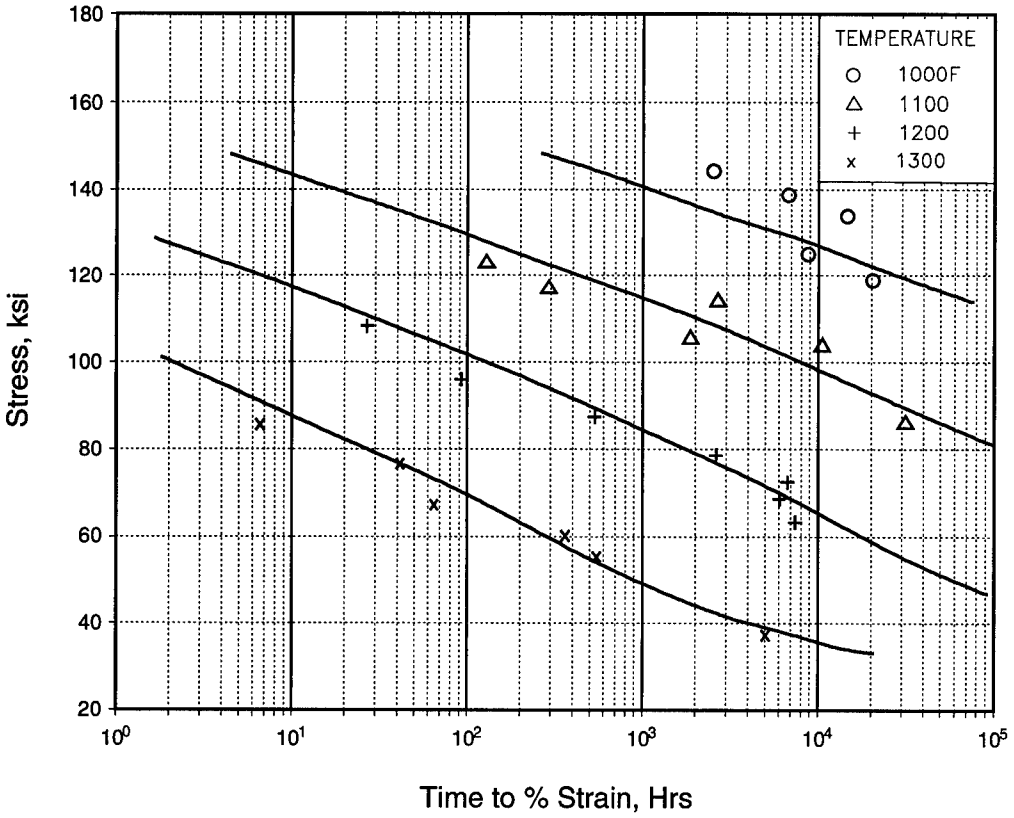


FIGURE 6.3.5.1.7(d). *Average isothermal 5.00% creep curves for Inconel 718 forging.*

Correlative Information for Figure 6.3.5.1.7(d)

Makeup of Data Collection:

Heat Treatment: 2 [See Table 6.3.5.1.7(f)]
Number of Vendors = Unknown
Number of Lots = 2
Number of Test Laboratories = 1
Number of Tests = 24

Specimen Details:

Type - Unnotched round bar
Gage Length - N.A.
Gage Thickness - 1/4" - 3/8"

5.00 Percent Creep Equation:

$\text{Log } t = c + b_1 T + b_2 X + b_3 X^2 + b_4 X^3$

T= °R
X= log (stress, ksi)
c = 186.16
b_1= -0.01778
b_2= -255.25
b_3= 146.28
b_4= -28.65

Analysis Details:

Inverse Matrix = [See Table 6.3.5.1.7(f)]
Standard Deviation = 1.02
Standard Error of Estimate = 0.37

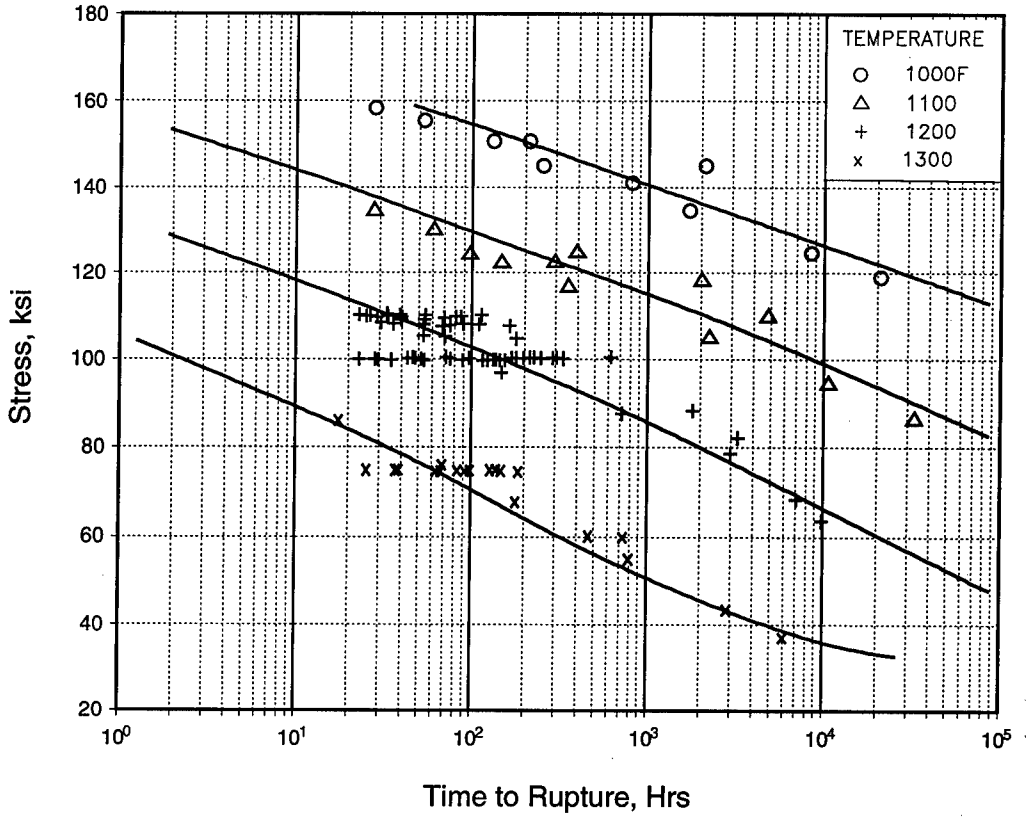


FIGURE 6.3.5.1.7(e). *Average isothermal stress rupture curves for Inconel 718 forging.*

Correlative Information for Figure 6.3.5.1.7(e)

Makeup of Data Collection:

Heat Treatment: 2 [See Table 6.3.5.1.7(f)]
Number of Vendors = Unknown
Number of Lots = 7
Number of Test Laboratories = 2
Number of Tests = 162

Specimen Details:

Type - Unnotched round bar
Gage Length - N.A.
Gage Thickness - 1/4" - 3/8"

Stress Rupture Creep Equation:

$\text{Log } t = c + b_1 T + b_2 X + b_3 X^2 + b_4 X^3$

T= °R
X= log (stress, ksi)
c = 186.27
b_1= -0.01778
b_2= -255.25
b_3= 146.28
b_4= -28.65

Analysis Details:

Standard Deviation = 0.63
Standard Error of Estimate = 0.29
Within Heat Treatment Variance = 0.071
Ratio of Between to Within Heat Treatment Variance = (at spec pt.) <0.10

TABLE 6.3.5.1.7(f) *Supplemental Information on the Creep and Stress Rupture Properties of Inconel 718 Forging.*

Heat Treatment Details

Heat Treatment Number	Cycle Number	Temperature, °F	Time, Hours	Cool
2	1	1800	1	AC, WQ
	2	1325	8	FC (100 F/hr)
	3	1150	8	AC
21	1	1700–1850	1	AC
	2	1325	8	FC (100 F/hr)
	3	1150	8	AC

Stress Rupture Equation and Inverse Matrix for the Creep Stress = 0.10, 0.20, 0.50, and 5.00% and Stress Rupture Conditions

$$\log t = c + b_1T + b_2X + b_3X^2 + b_4X^3 + b_5Y_1 + b_6Y_2 + b_7Y_3 + b_8Y_4 + b_9Y_5$$

where $Y_1 = 1$; $Y_2, Y_3, Y_4, Y_5 = 0$ for Creep Strain = 0.10% Data
$Y_2 = 1$; $Y_1, Y_3, Y_4, Y_5 = 0$ for Creep Strain = 0.20% Data
$Y_3 = 1$; $Y_1, Y_2, Y_4, Y_5 = 0$ for Creep Strain = 0.50% Data
$Y_4 = 1$; $Y_1, Y_2, Y_3, Y_5 = 0$ for Creep Strain = 5.00% Data
$Y_1, Y_2, Y_3, Y_4\ Y_5 = 0$ for Stress Rupture Data

Column / Row	1	2	3	4	5	6	7	8	9
1	1.809E+00	-1.108E-03	-1.978E+00	6.499E-01	-5.748E-02	-1.606E+00	-1.444E+00	-1.015E+00	-9.777E-01
2	-1.108E-03	6.834E-07	1.212E-03	-3.979E-04	3.517E-05	9.843E-04	8.852E-04	6.219E-04	5.993E-04
3	-1.978E+00	1.212E-03	3.482E+00	-1.657E+00	2.032E-01	1.634E+00	1.359E+00	6.886E-01	5.921E-01
4	6.499E-01	-3.979E-04	-1.657E+00	9.145E-01	-1.220E-01	-4.892E-01	-3.610E-01	-6.305E-02	3.594E-03
5	-5.748E-02	3.517E-05	2.032E-01	-1.220E-01	1.697E-02	3.801E-02	2.248E-02	-1.245E-02	-2.618E-02
6	-1.606E+00	9.843E-04	1.634E+00	-4.892E-01	3.801E-02	1.471E+00	1.303E+00	9.401E-01	9.124E-01
7	-1.444E+00	8.852E-04	1.359E+00	-3.610E-01	2.248E-02	1.303E+00	1.222E+00	8.806E-01	8.600E-01
8	-1.015E+00	6.219E-04	6.886E-01	-6.305E-02	-1.245E-02	9.401E-01	8.806E-01	7.491E-01	6.987E-01
9	-9.777E-01	5.993E-04	5.921E-01	3.594E-03	-2.618E-02	9.124E-01	8.600E-01	6.987E-01	1.195E+00

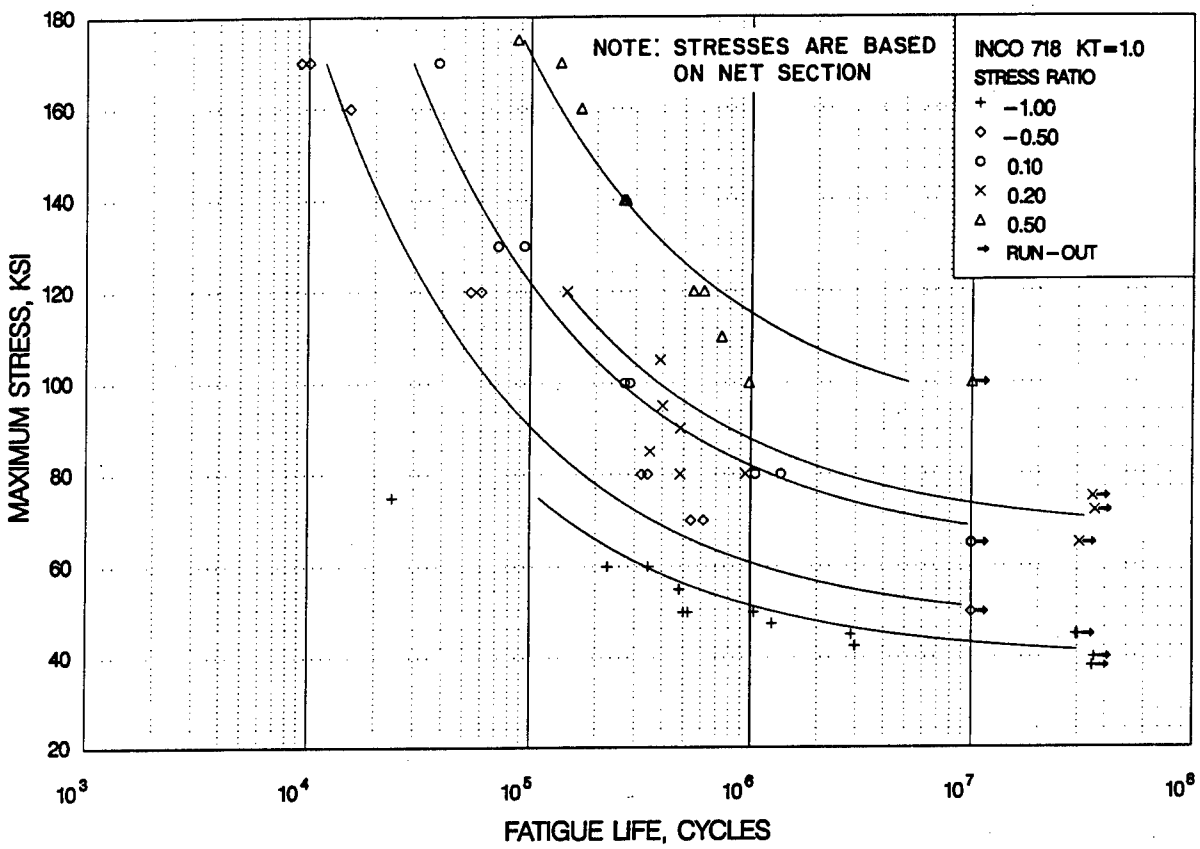


FIGURE 6.3.5.1.8(a). *Best-fit S/N curves for unnotched Inconel 718 sheet at room temperature, long transverse direction.*

Correlative Information for Figure 6.3.5.1.8(a)

Product Form: Sheet, 0.066-inch and 0.109-inch

Properties:	TUS, ksi	TYS, ksi	Temp, F
	197.0	164.0	RT
	208.7	184.2	RT

Specimen Details: Unnotched
0.30-inch net width
0.5-inch net width

Heat Treatment: See AMS 5596

Surface Condition: #400 grit belt polished

Reference: 6.2.1.1.8 and 6.3.5.1.8(a)

Test Parameters:

Loading—Axial
Frequency—Unspecified
Temperature—RT
Environment—Air

No. of Heats/Lots: 2

Equivalent Stress Equation

$\text{Log } N_f = 8.63 - 2.07 \text{ Log } (S_{eq} - 58.48)$

$S_{eq} = S_{max}(1\text{-}R)^{.58}$

Standard Deviation in Log (Life) = $26.73\ (1/S_{eq})$

$R^2 = 90.3$

Sample Size = 53

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

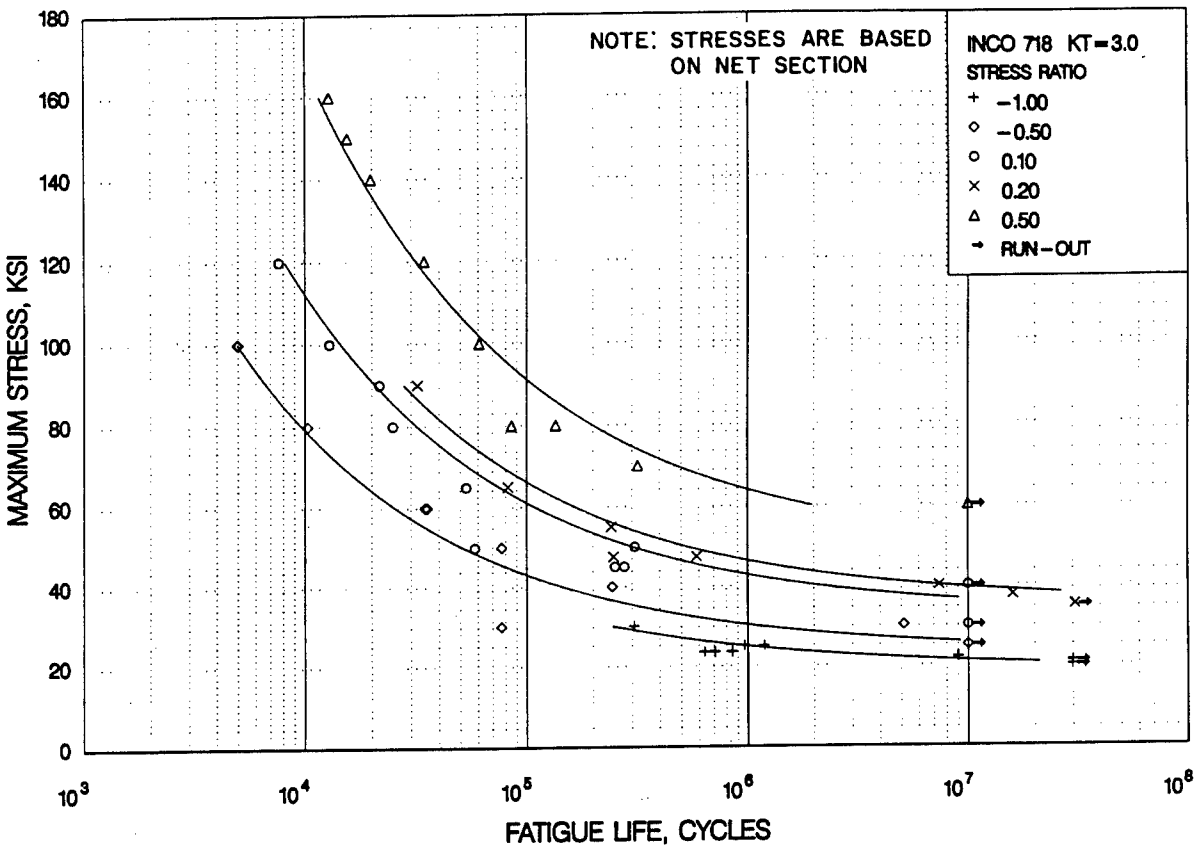


FIGURE 6.3.5.1.8(b). *Best-fit S/N curves for notched, K_t = 3.0, Inconel 718 sheet at room temperature, long transverse direction.*

Correlative Information for Figure 6.3.5.1.8(b)

Product Form: Sheet, 0.066-inch and 0.109-inch

Properties:	TUS, ksi	TYS, ksi	Temp, F
	197.0	164.0	RT
	208.7	184.2	RT

Specimen Details: Notched 60° V-Groove
K_t = 3.0
0.30-inch net width
0.22-inch root width
0.625-inch net width
0.030-inch root radius

Heat Treatment: See AMS 5596

Surface Condition: As machined

Reference: 6.2.1.1.8 and 6.3.5.1.8(a)

Test Parameters:

Loading—Axial
Frequency—Unspecified
Temperature—RT
Environment—Air

No. of Heats/Lots: 2

Equivalent Stress Equation
$\text{Log } N_f = 8.17 - 2.23 \text{ Log } (S_{eq} - 30.58)$
$S_{eq} = S_{max}(1\text{-}R)^{.68}$
Standard Deviation in Log (Life) = $14.07\ (1/S_{eq})$
$R^2 = 93.7$

Sample Size = 49

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

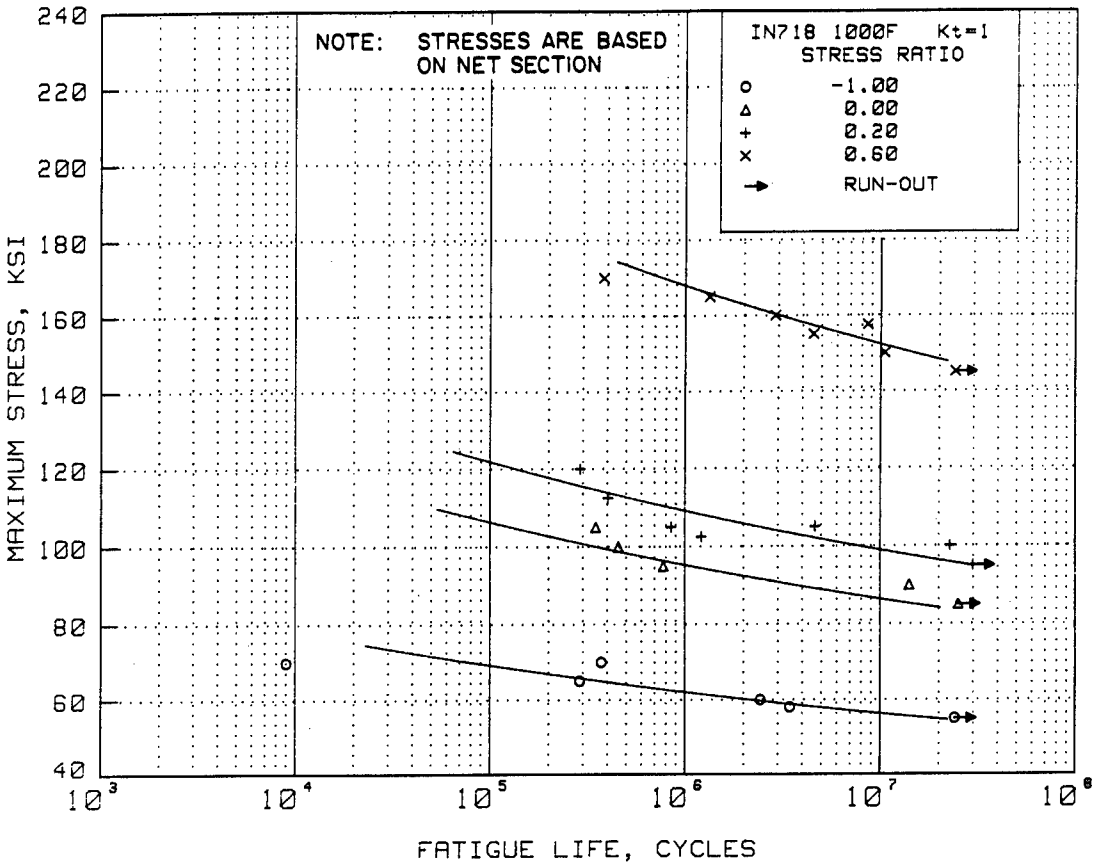


FIGURE 6.3.5.1.8(c). *Best-fit S/N curves for unnotched Inconel 718 sheet at 1000 F, long transverse direction.*

Correlative Information for Figure 6.3.5.1.8(c)

Product Form: Sheet, 0.066-inch

Properties:	TUS, ksi	TYS, ksi	Temp, F
	165.0	141.8	1000

Specimen Details: Unnotched
0.30-inch net width

Heat Treatment: See AMS 5596

Surface Condition: #400 grit belt polished

Reference: 6.2.1.1.8

Test Parameters:

Loading—Axial
Frequency—60 Hz
Temperature—1000 F
Environment—Air

No. of Heats/Lots: 1

Equivalent Stress Equation

$\text{Log } N_f = 23.51 - 10.57 \text{ Log } (S_{eq} - 50)$

$S_{eq} = S_{max}(1\text{-}R)^{0.62}$

Standard Error of Estimate = 0.414
Standard Deviation in Life = 0.776
$R^2 = 71.5\%$

Sample Size = 21

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

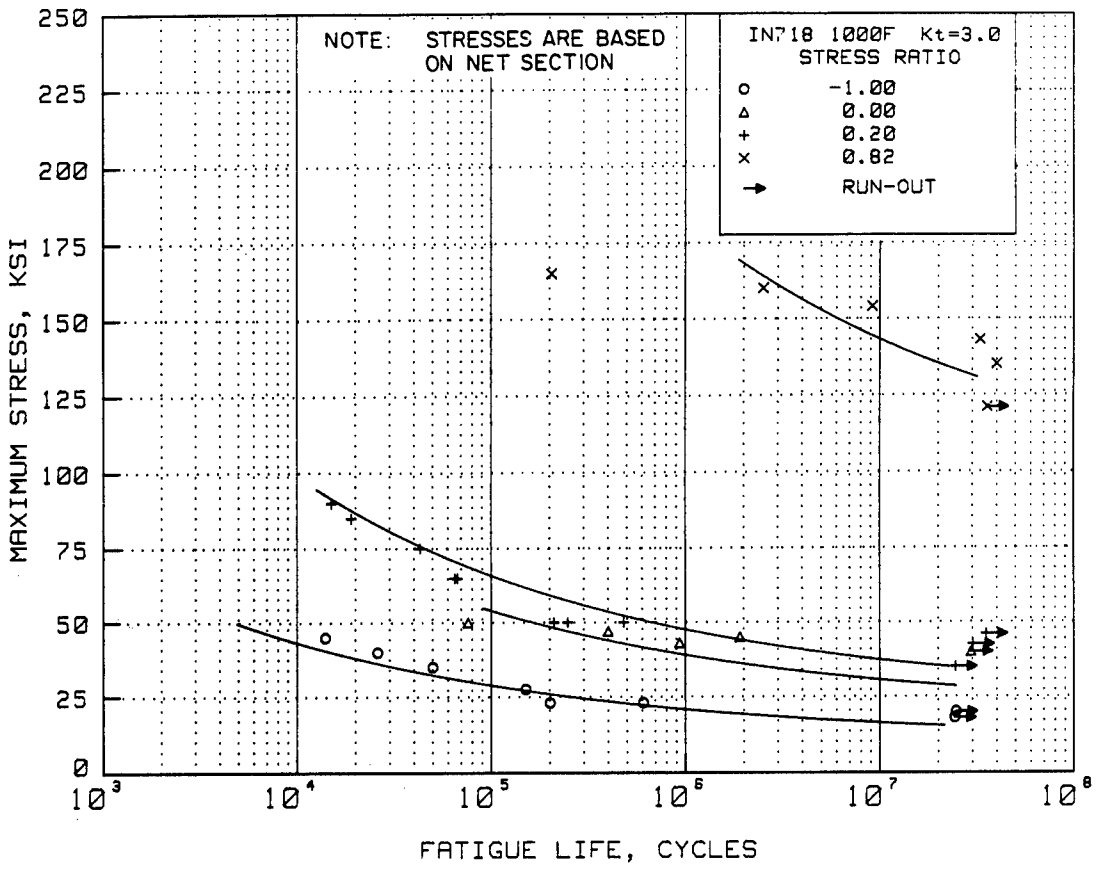


FIGURE 6.3.5.1.8(d). *Best-fit S/N curves for notched, K_t = 3.0, Inconel 718 sheet at 1000 F, long transverse direction.*

Correlative Information for Figure 6.3.5.1.8(d)

Product Form: Sheet, 0.066-inch

Properties:	TUS, ksi	TYS, ksi	Temp, F
	165.0	141.8	1000 Unnotched

Specimen Details: Notched, V-Groove, K_t = 3.0
0.448-inch gross width
0.30-inch net width
0.022-inch root radius, r
60° flank angle, ω

Heat Treatment: See AMS 5596

Surface Condition: As machined

Reference: 6.2.1.1.8

Test Parameters:

Loading—Axial
Frequency—60 Hz
Temperature—1000 F
Environment—Air

No. of Heats/Lots: 1

Equivalent Stress Equation
$\text{Log } N_f = 11.02 - 3.93 \text{ Log } (S_{eq} - 20)$
$S_{eq} = S_{max}(1\text{-}R)^{0.91}$
Standard Error of Estimate = 0.404
Standard Deviation in Life = 0.988
R^2 = 83.3%

Sample Size = 23

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

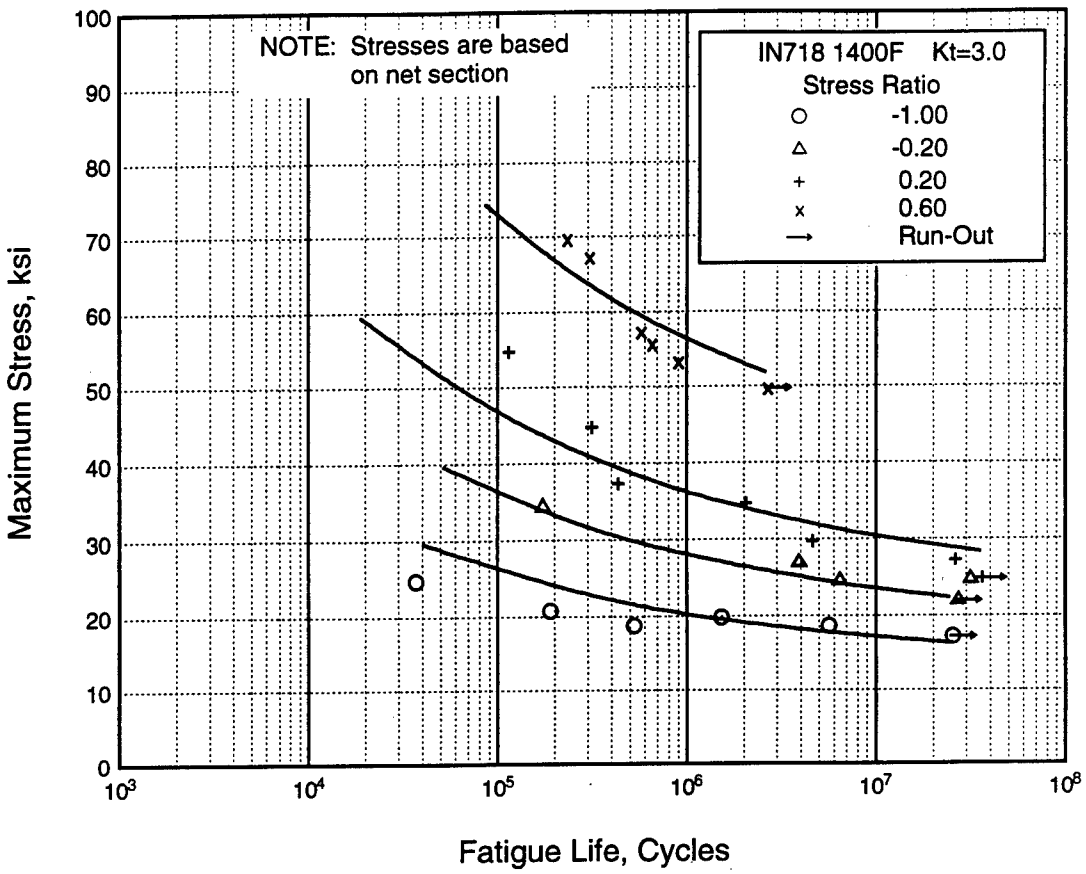


FIGURE 6.3.5.1.8(e). *Best-fit S/N curves for notched, K_t = 3.0, Inconel 718 sheet at 1400 F, long transverse direction.*

Correlative Information for Figure 6.3.5.1.8(e)

Product Form: Sheet, 0.066-inch

Properties:

TUS, ksi	TYS, ksi	Temp, F
113.0	100.1	1400 Unnotched

Specimen Details: Notched, V-Groove, K_t = 3.0
0.448-inch gross width
0.30-inch net width
0.022-inch root radius, r
60° flank angle, ω

Heat Treatment: See AMS 5596

Surface Condition: As machined.

Reference: 6.2.1.1.8

Test Parameters:

Loading—Axial
Frequency—60 Hz
Temperature—1400 F
Environment—Air

No. of Heats/Lots: 1

Equivalent Stress Equation
$\text{Log } N_f = 10.29 - 4.02 \text{ Log } (S_{eq} - 20)$
$S_{eq} = S_{max}(1\text{-}R)^{0.62}$
Standard Error of Estimate = 0.442
Standard Deviation in Life = 0.717
R^2 = 62.0%

Sample Size = 20

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

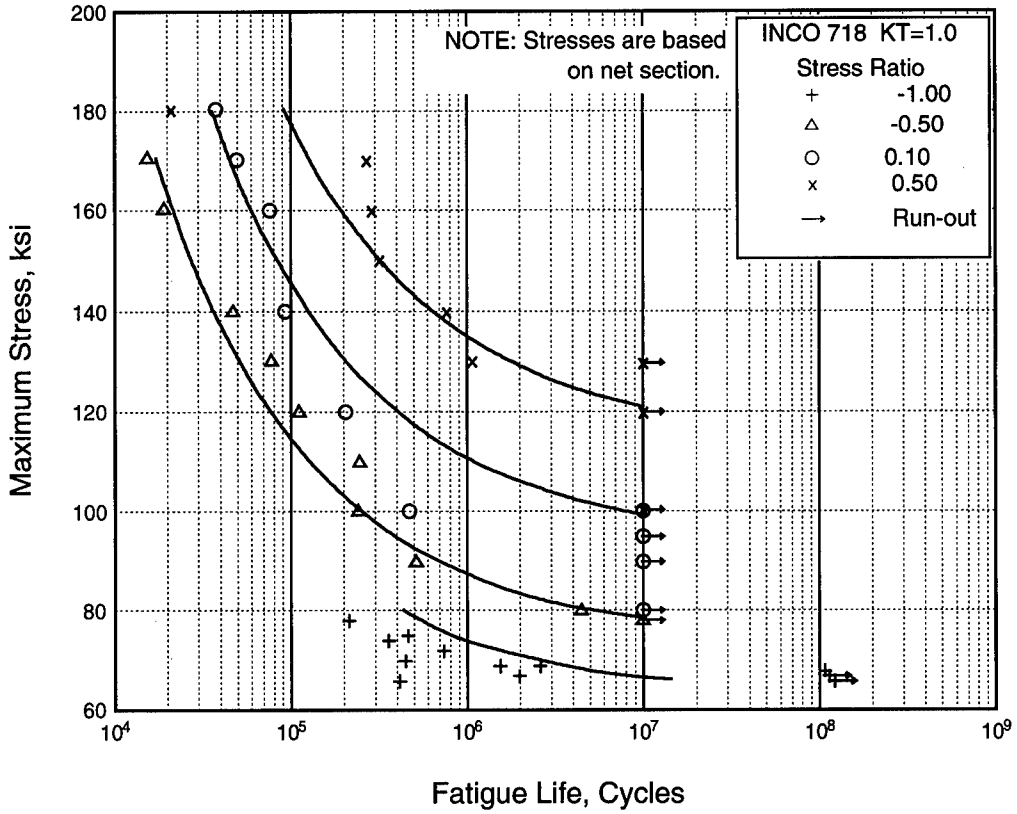


FIGURE 6.3.5.1.8(f). *Best-fit S/N curves for unnotched Inconel 718 bar and plate at room temperature, longitudinal direction.*

Correlative Information for Figure 6.3.5.1.8(f)

Product Form: Bar, 0.75-inch diameter; plate, 0.5-, 0.75-, and 1.0-inch thick

Properties:	TUS, ksi	TYS, ksi	Temp, F
	204.4	177.7	RT
	200.0	166.7	RT

Specimen Details: Unnotched
0.250-inch diameter
0.200-inch diameter

Heat Treatment: See AMS 5662 and AMS 5596

Surface Condition: Unspecified, RMS 8-11

Reference: 6.3.3.1.8(a) and 6.3.5.1.8(b)

Test Parameters:
Loading - Axial
Frequency - Unspecified
Temperature - RT
Environment - Air

No. of Heats/Lots: 4

Equivalent Stress Equation
$\text{Log } N_f = 8.18 - 2.07 \log (S_{eq} - 63.0)$
$S_{eq} = S_a + 0.40\ S_m$
Standard Deviation in Log (Life) = $38.56\ (1/S_{eq})$
$R^2 = 67.7$

Sample Size = 44

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

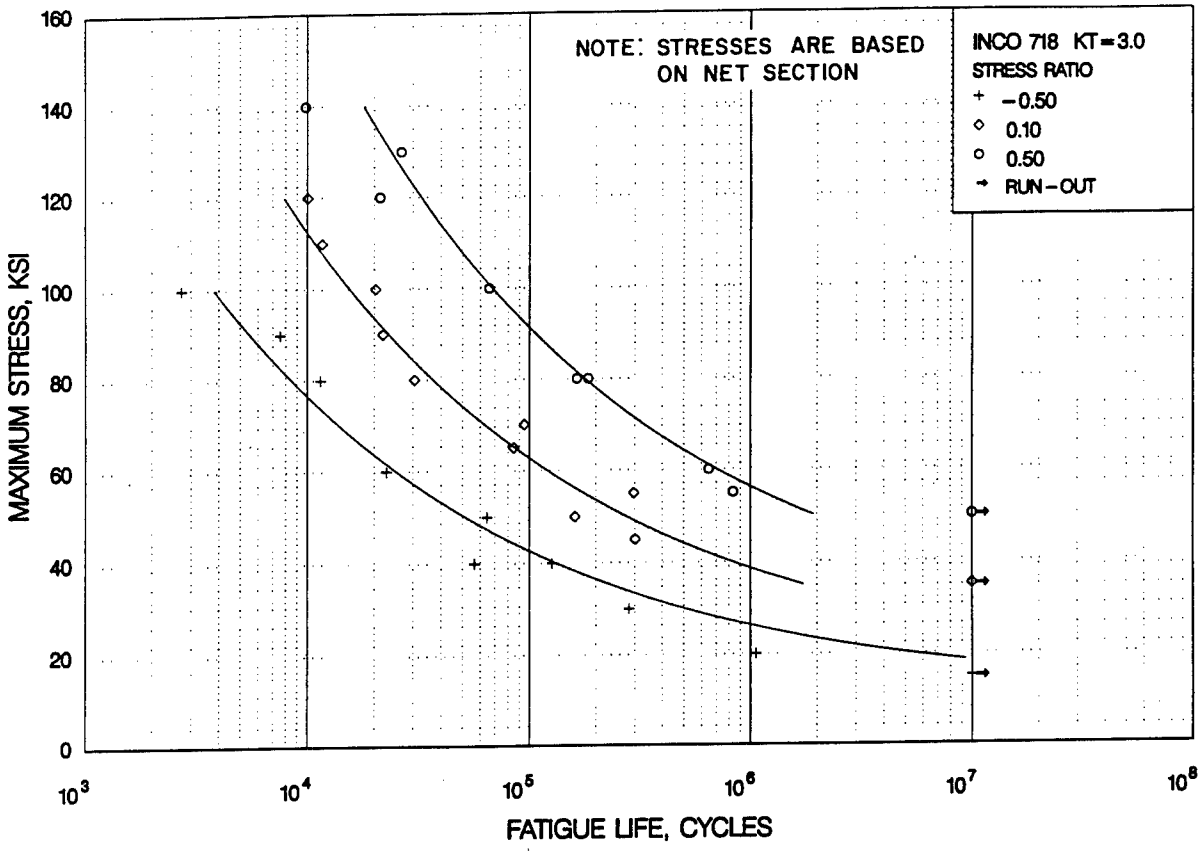


FIGURE 6.3.5.1.8(g). *Best-fit S/N curves for notched, K_t = 3.0, Inconel 718 bar at room temperature, longitudinal direction.*

Correlative Information for Figure 6.3.5.1.8(g)

Product Form: Bar, 0.75-inch diameter

Properties:	TUS, ksi	TYS, ksi	Temp, F
	204.4	177.7	RT

Specimen Details: Notched, 60° V Notch
0.252-inch diameter
0.013-inch diameter

Heat Treatment: See AMS 5662 and AMS 5596

Surface Condition: Unspecified

Reference: 6.3.3.1.8(a)

Test Parameters:

Loading—Axial
Frequency—Unspecified
Temperature—RT
Environment—Air

No. of Heats/Lots: 1

Equivalent Stress Equation
Log N_f = 9.45 - 3.17 Log (S_{eq} - 8.6)
$S_{eq} = S_a + 0.16\ S_m$
Standard Deviation in Log (Life) = 6.97 ($1/S_{eq}$)
R^2 = 93.6

Sample Size = 31

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

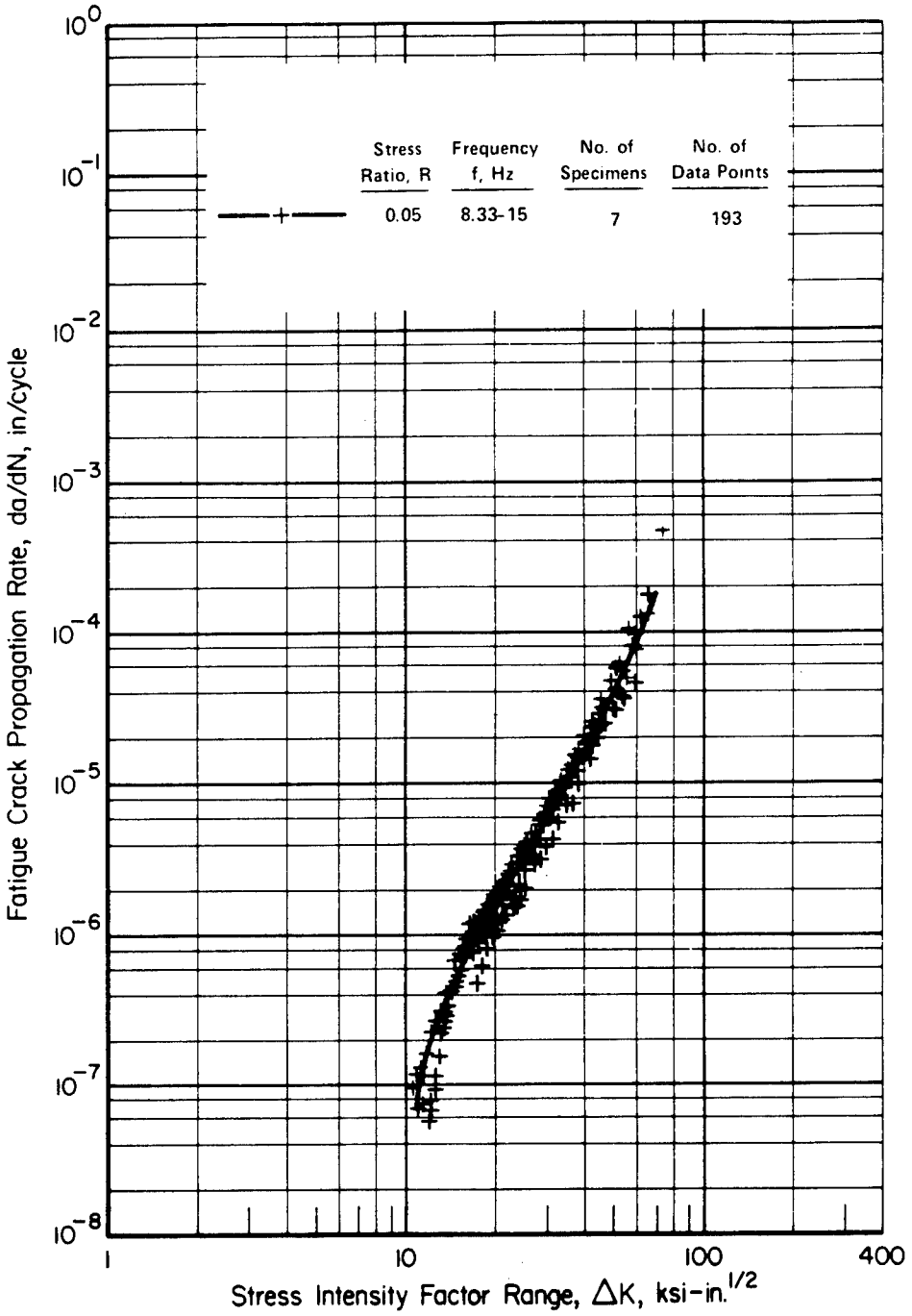


FIGURE 6.3.5.1.9(a). *Fatigue-crack-propagation data for Inconel 718 die forging (upset ratio = 5) and 0.5-inch thick plate. [References—6.3.5.1.9(a) through (e).]*

Specimen Thickness:	*0.298-0.502 inch*	*Environment:*	*Lab air*
Specimen Width:	*1.153-2.000 inches*	*Temperature:*	*RT*
Specimen Type:	*CT*	*Orientation:*	*L-T and T-L*

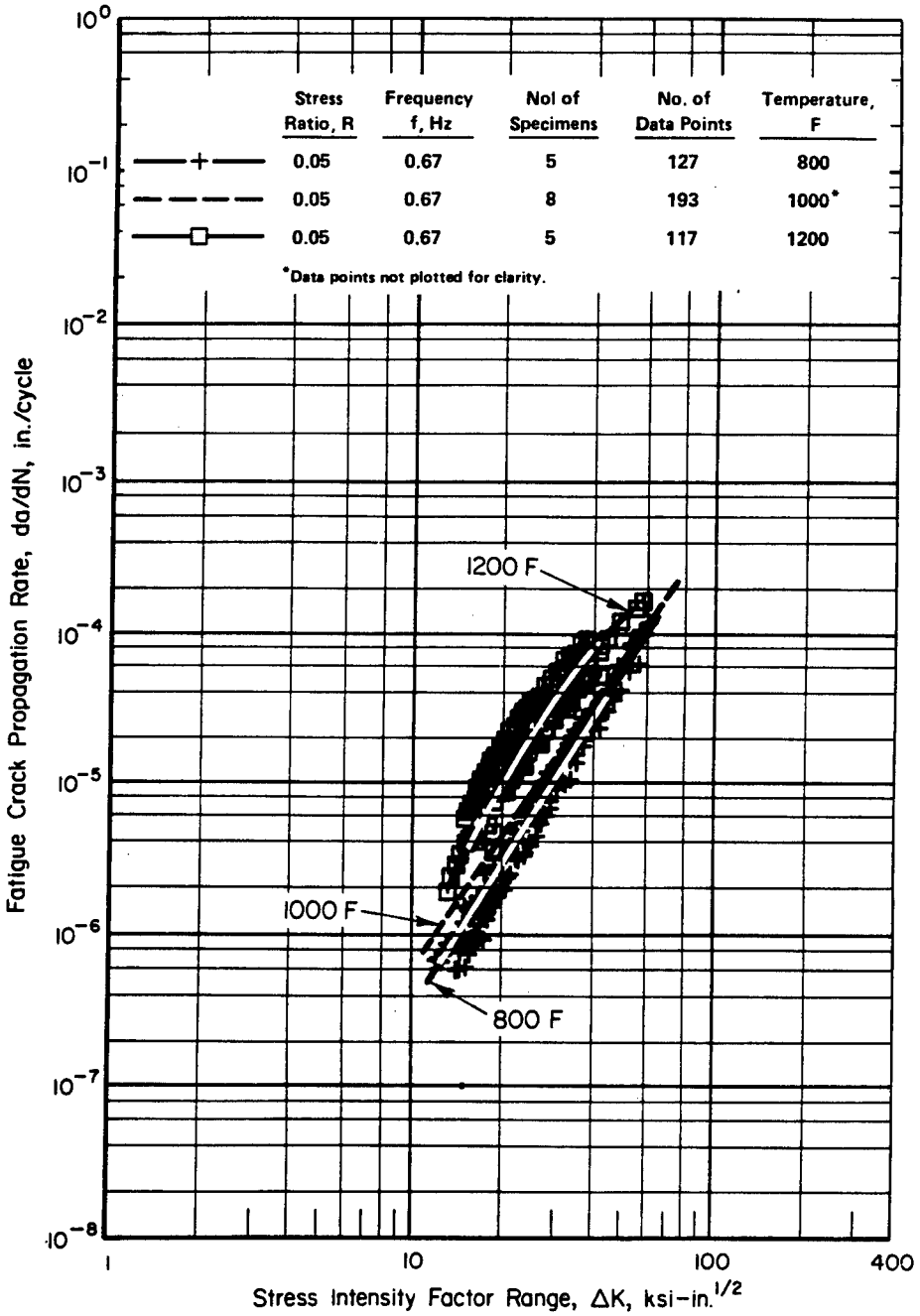


FIGURE 6.3.5.1.9(b). *Fatigue-crack-propagation data for Inconel 718 die forging (upset ratio = 5) and 0.5-inch thick plate. [References--6.3.5.1.9(b) and 6.3.5.1.9(d) through (g).]*

Specimen Thickness:	*0.298–0.502 inch*	*Environment:*	*Lab air*
Specimen Width:	*1.157–2.001 inches*	*Temperature:*	*800–1200 F*
Specimen Type:	*CT*	*Orientation:*	*L-T and T-L*

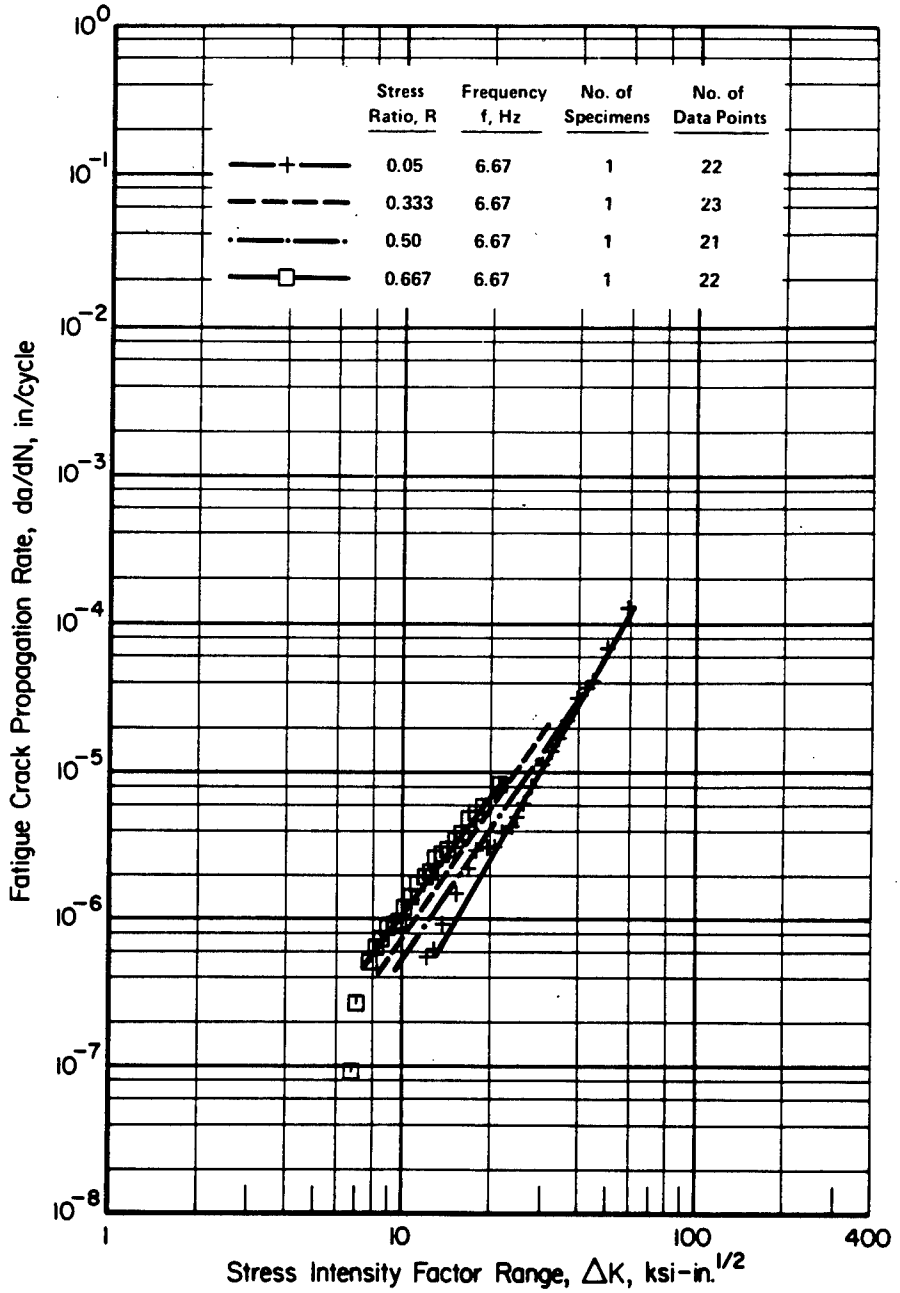


FIGURE 6.3.5.1.9(c). *Fatigue-crack-propagation data for Inconel 718 0.5-inch thick plate. [Reference--6.3.5.1.9(f).]*

Specimen Thickness:	*0.298–0.479 inch*	*Environment:*	*Lab air*
Specimen Width:	*1.151–1.993 inches*	*Temperature:*	*1000 F*
Specimen Type:	*CT*	*Orientation:*	*L-T and T-L*

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6.3.6 INCONEL X-750 ALLOY

6.3.6.0 *Comments and Properties.*—Inconel X-750 Alloy is a high-strength oxidation-resistant nickel-base alloy. It is used for parts requiring high strength up to 1000 F or high creep strength up to 1500 F and for low-stressed parts operating up to 1900 F. It is hardenable by various combinations of solution treatment and aging, depending on its form and application. Inconel X-750 Alloy is available in all the usual wrought mill forms.

Inconel X-750 Alloy can be readily forged between 2225 and 1900 F; "hot-cold" working between 1600 and 1200 F is harmful and should be avoided. This alloy is readily formed but should be solution treated at 1925 F for 7 to 10 minutes after severe forming operations. It is somewhat more difficult to machine than austenitic stainless steels. Rough machining is easier in the solution-treated condition; finish machining in the partly or fully aged condition. Fusion welding is difficult for large section sizes and moderately difficult for small cross sections and sheet. It must be welded in the annealed or solution-treated condition; weldments should be stress relieved at 1650 F for 2 hours before aging. Nickel brazing, followed by precipitation heat treatment of the brazed assembly, results in strength nearly equal to fully heat-treated material.

Oxidation resistance of Inconel X-750 Alloy is good to 1900 F; but the beneficial effects of aging are lost above 1500 F. This alloy is subject to attack in sulfur-containing atmospheres.

A variety of heat treatments has been developed for Inconel X-750. Each provides special properties and renders the material in the best metallurgical condition for the intended application. Only two of these heat treatments, for applications requiring high strength up to 1100 F, are described below.

Annealed and Aged for Sheet, Strip, and Plate.—Mill annealed plus 1300 F for 20 hours, and A.C. per AMS 5542.

Equalized and Aged for Bar and Forging.—1625 F for 4 hours, A.C., plus 1300 F for 24 hours, and A.C. per AMS 5667.

Other heat treatments are available for maximum creep-rupture strength.

Some material specifications for Inconel X-750 Alloy are shown in Table 6.3.6.0(a). Room-temperature mechanical and physical properties are shown in Table 6.3.6.0(b).

TABLE 6.3.6.0(a). *Material Specifications for Inconel X-750 Alloy*

Specification	Form	Condition
AMS 5542	Sheet, strip, and plate	Annealed
AMS 5667	Bar and forging	Equalized

The effect of temperature on the physical properties of this alloy is shown in Figure 6.3.6.0.

6.3.6.1 *Annealed and Aged.*—Elevated-temperature curves for tensile and yield ultimate strengths are shown in Figures 6.3.6.1.1 through 6.3.6.1.3.

6.3.6.2 *Equalized and Aged.*—Elevated-temperature curves are presented in Figures 6.3.6.2.1(a) and (b), as well as 6.3.6.2.4(a) and (b).

TABLE 6.3.6.0(b). *Design Mechanical and Physical Properties of Inconel X-750 Alloy*

Specification	AMS 5542				AMS 5667	
Form	Strip		Sheet	Plate	Bars and forgings	
Condition	Annealed and aged				Equalized and aged	
Thickness or diameter, in.	≤0.009	≥0.010	0.010-0.187	0.188-4.000	<4.000	4.000-10.000
Basis	S	S	S	S	S	S
Mechanical Properties:						
F_{tu}, ksi:						
L	...	...	...	...	165	160
LT	150	155	165	155	...	...
F_{ty}, ksi:						
L	...	...	...	...	105	100
LT	...	...	105	100	...	...
F_{cy}, ksi:						
L	...	...	...	...	105	100
LT	...	...	105	100	...	...
F_{su}, ksi	...	...	107	100	102	99
F_{bru}, ksi:						
(e/D = 1.5)	...	...	247	232	247	240
(e/D = 2.0)	...	...	313	294	313	304
F_{bry}, ksi:						
(e/D = 1.5)	...	...	157	150	157	150
(e/D = 2.0)	...	...	189	180	189	180
e, percent:						
L	...	...	...	...	20	15
LT	...	15	20	20	...	...
RA, percent:						
L	...	...	...	...	25	17
E, 10^3 ksi	30.6					
E_c, 10^3 ksi	30.6					
G, 10^3 ksi	11.8					
μ	0.30					
Physical Properties:						
ω, lb/in.^{3}	0.298					
C, K, and α	See Figure 6.3.6.0					

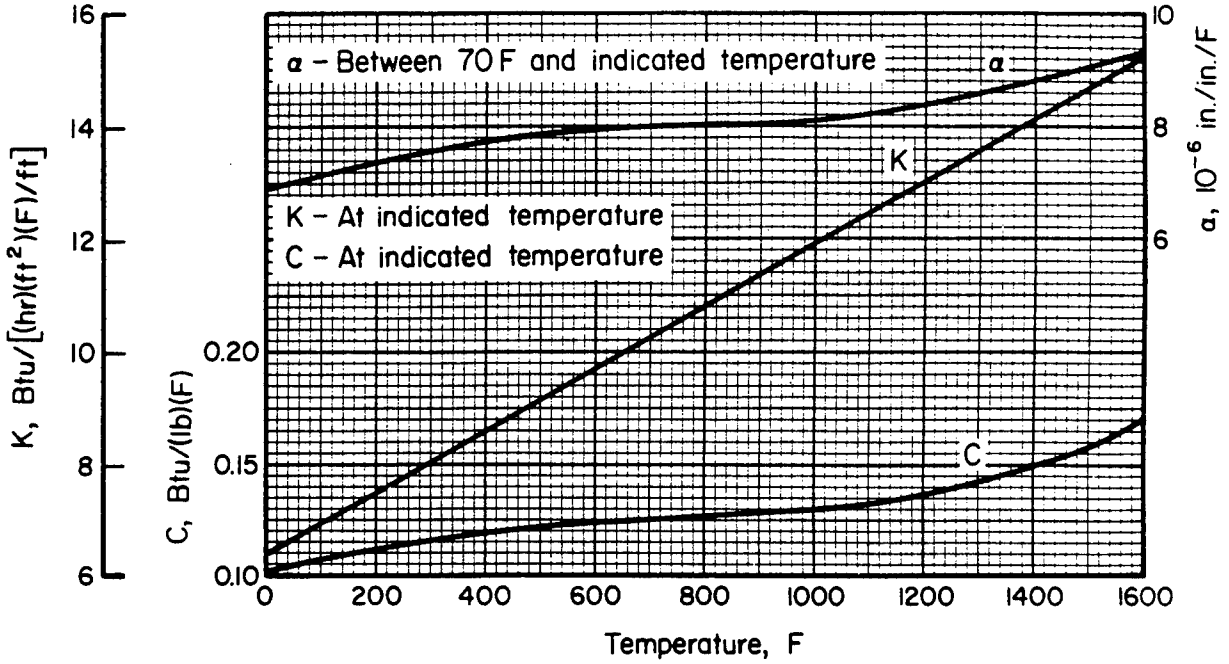


FIGURE 6.3.6.0. *Effect of temperature on the physical properties of Inconel Alloy X-750.*

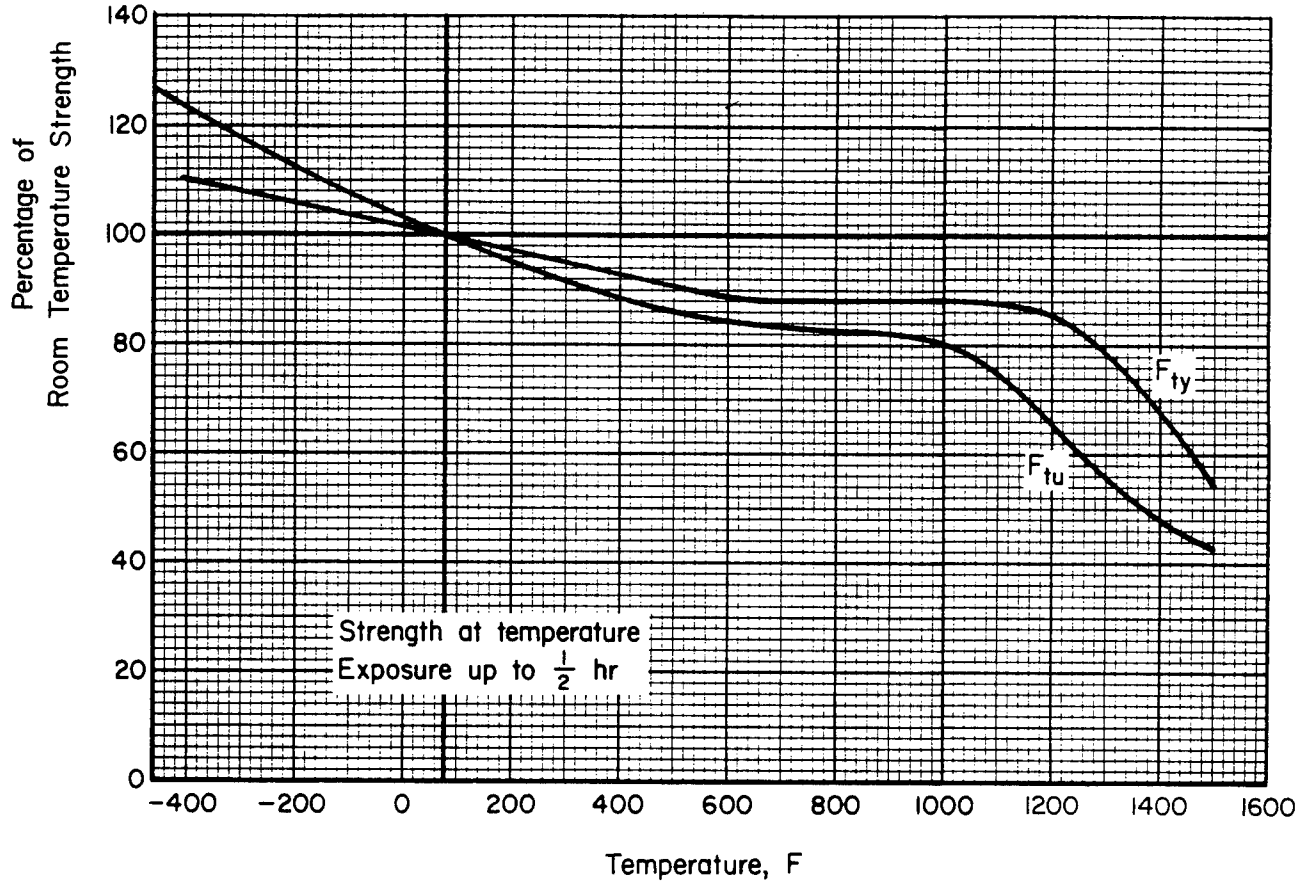


FIGURE 6.3.6.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and tensile yield strength (F_{ty}) of Inconel X-750 alloy sheet and plate (AMS 5542).*

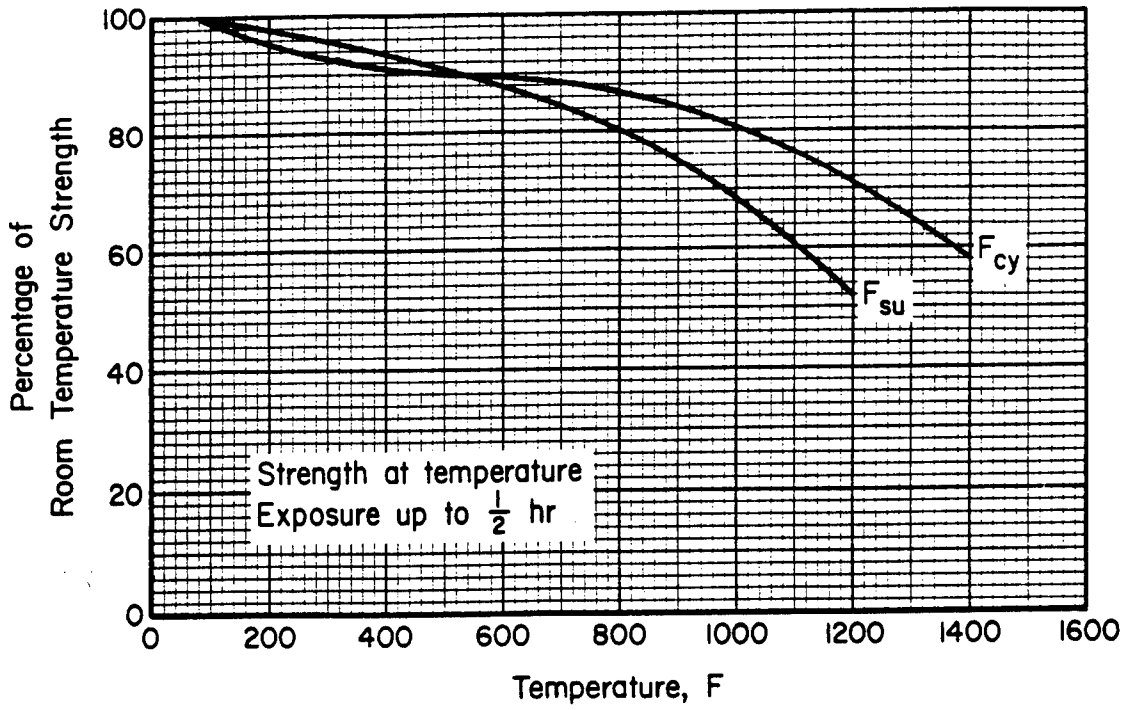


FIGURE 6.3.6.1.2. *Effect of temperature on the compressive yield strength (F_{cy}) and the shear ultimate strength (F_{su}) of Inconel X-750 alloy.*

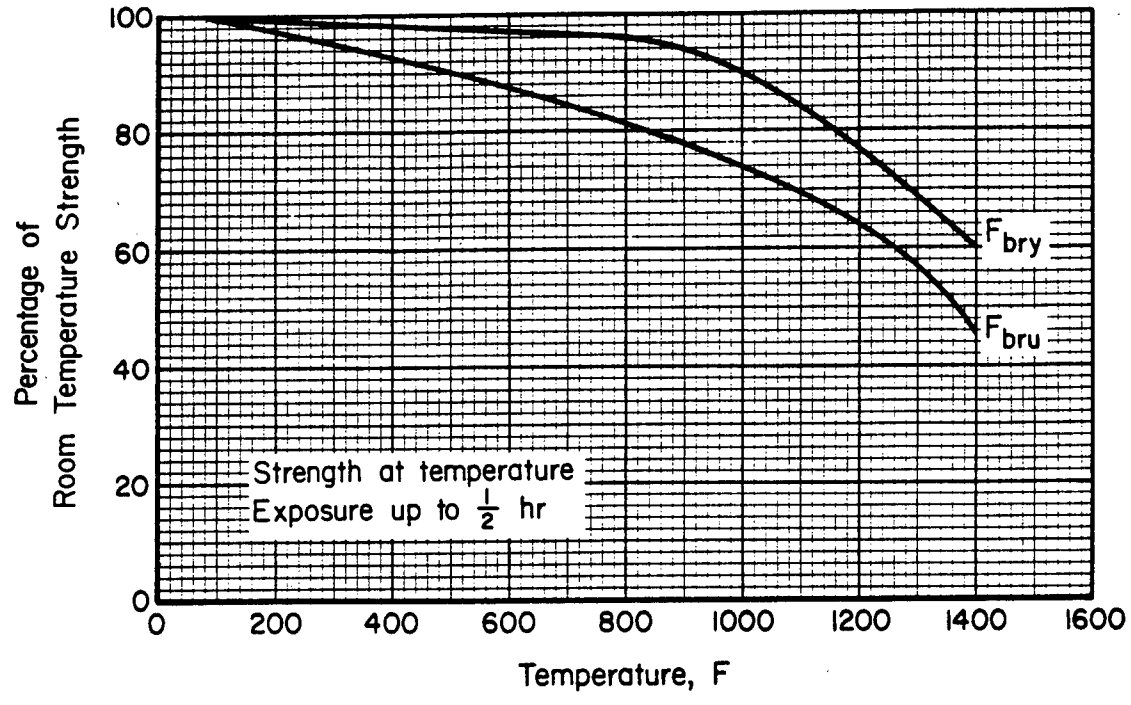


FIGURE 6.3.6.1.3. *Effect of temperature on the bearing ultimate strength (F_{bru}) and the bearing yield strength (F_{bry}) of Inconel X-750 alloy.*

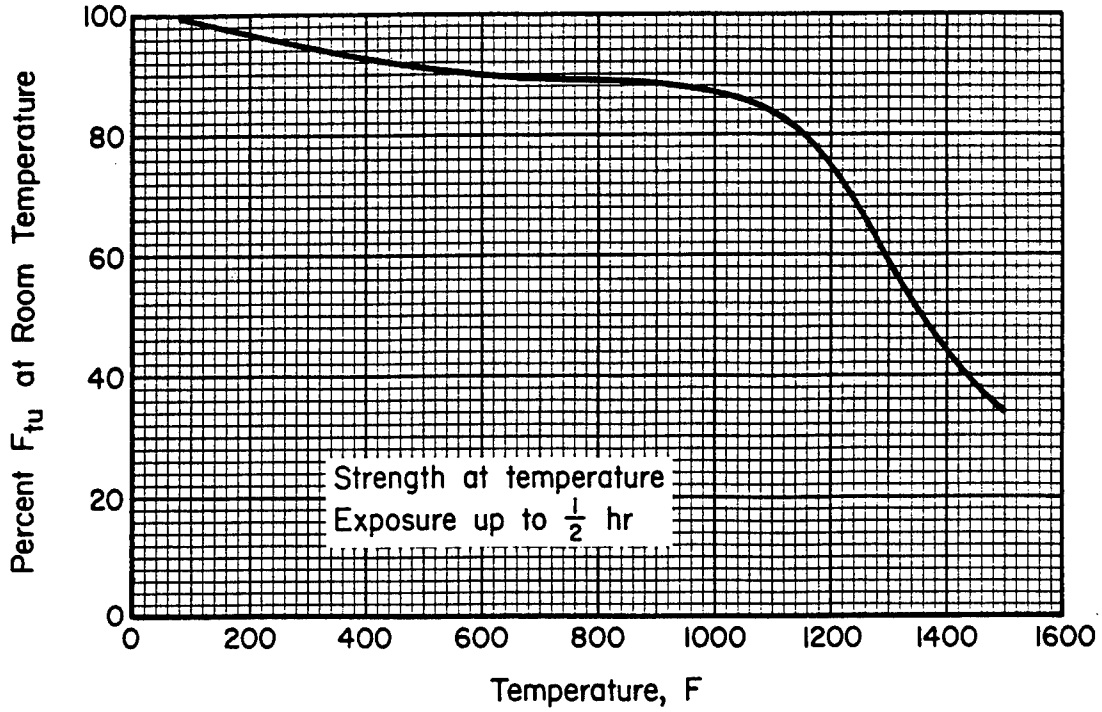


FIGURE 6.3.6.2.1(a). *Effect of temperature on the tensile ultimate strength (F_{tu}) of Inconel X-750 alloy bar (AMS 5667).*

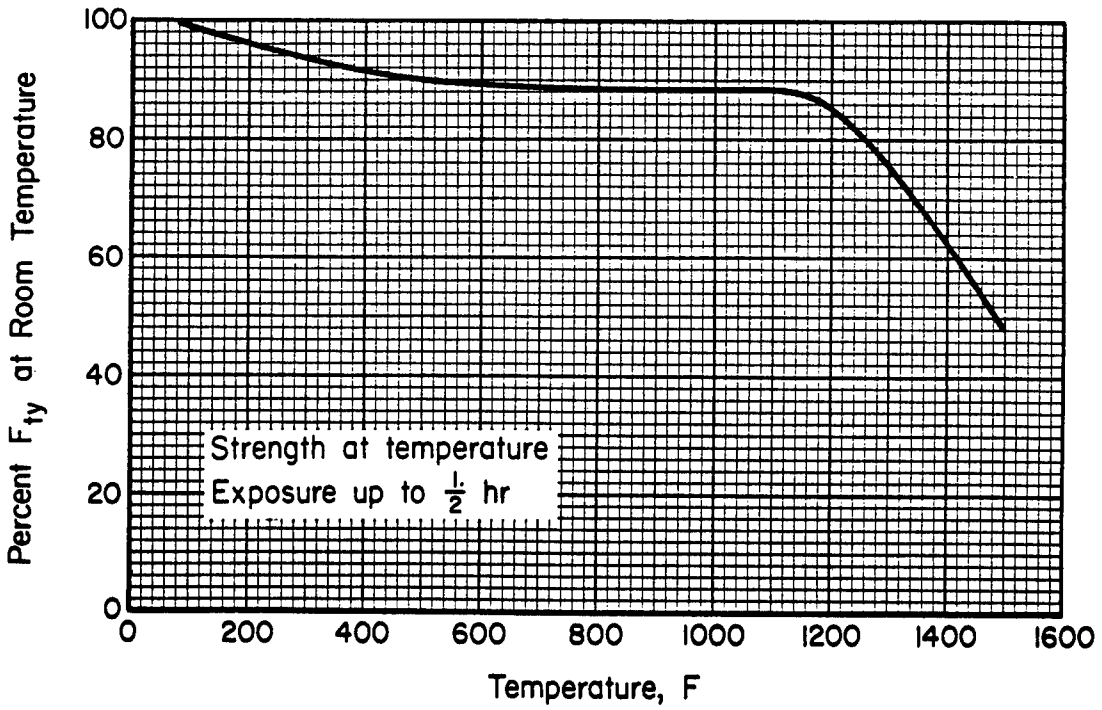


FIGURE 6.3.6.2.1(b). *Effect of temperature on the tensile yield strength (F_{ty}) of Inconel X-750 alloy bar (AMS 5667).*

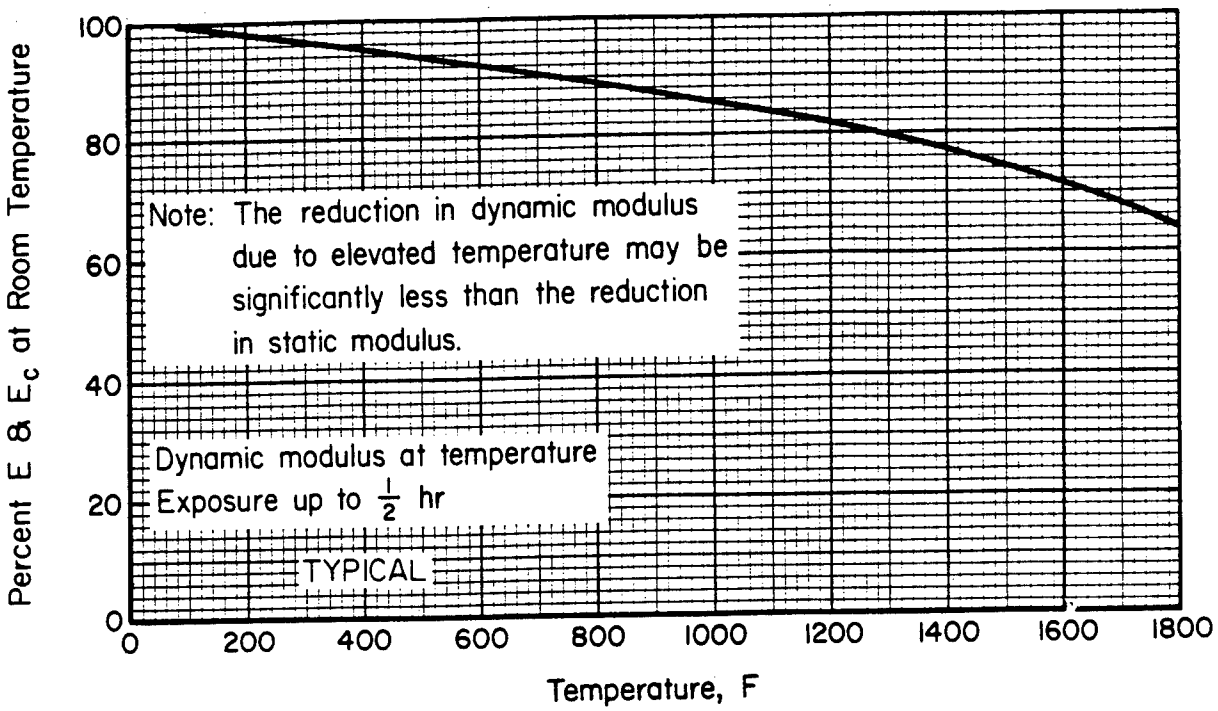


FIGURE 6.3.6.2.4(a). *Effect of temperature on the tensile and compressive moduli (E and E_c) of Inconel X-750 alloy.*

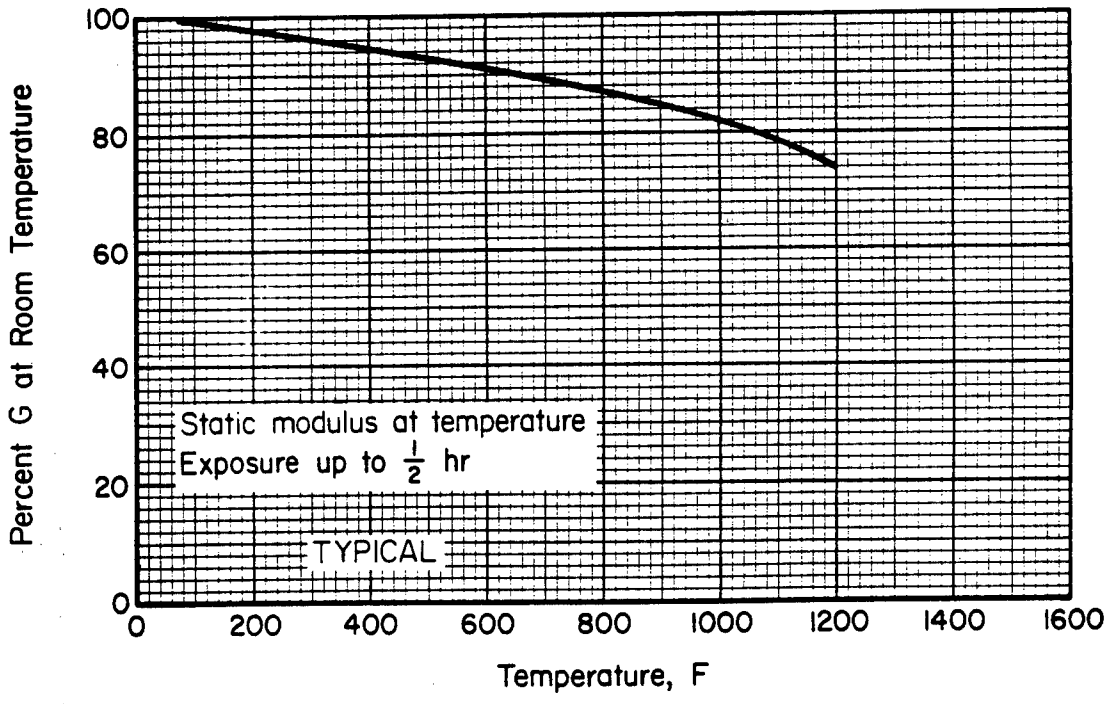


FIGURE 6.3.6.2.4(b). *Effect of temperature on the shear modulus (G) of Inconel X-750 alloy.*

6.3.7 René 41

6.3.7.0 *Comments and Properties.*—René 41 is a vacuum-melted precipitation-hardening nickel-base alloy designed for highly stressed parts operating between 1200 and 1800 F. Its applications include afterburner parts, turbine castings, wheels, buckets, and high-temperature bolts and fasteners. René 41 is available in the form of sheet, bars, and forgings.

René 41 is forged between 2150 and 1900 F; small reductions must be made when breaking up an as-cast structure; cracking may be encountered in finishing below 1850 F. René 41 work hardens rapidly, and frequent anneals are required; to anneal, heat rapidly to 1950 F for 30 minutes and quench.

René 41 is difficult to machine. In the soft solution-annealed condition it is gummy; therefore, it should be in the fully aged condition for optimum machinability, and tungsten carbide cutting tools should be used. René 41 can be welded satisfactorily in the solution-treated condition; after welding, the parts should be solution treated for stress relief.

René 41 should not be exposed to temperatures above 2050 F during latter stages of hot working or during subsequent operations, otherwise severe intergranular cracking may be encountered.

The oxidation resistance of René 41 is good to 1800 F. Lengthy exposure above the aging temperature (1400 to 1650 F) results in loss of strength and room-temperature ductility.

Some material specifications for René 41 are shown in Table 6.3.7.0(a). Room temperature mechanical and physical properties are shown in Table 6.3.7.0(b). The effect of temperature on physical properties is shown in Figure 6.3.7.0.

TABLE 6.3.7.0(a). *Material Specifications for for René 41 Alloy*

Specification	Form	Condition
AMS 5545	Plate, sheet, and strip	Vacuum melted, solution treated
AMS 5712	Bar and forging	Vacuum melted, solution treated and aged
AMS 5713	Bar and forging	Vacuum melted, solution treated and aged

6.3.7.1 *Solution Treated at 1975 F and Aged at 1400 F Condition.*—Tensile and stress-rupture requirements at elevated temperatures are specified for René 41. The appropriate specification should be consulted for detailed requirements. Other elevated-temperature data for René 41 in this condition are presented in Figures 6.3.7.1.1 through 6.3.7.1.5. A creep nomograph for René 41 alloy sheet is shown in Figure 6.3.7.1.7.

TABLE 6.3.7.0(b). *Design Mechanical and Physical Properties of René 41 Alloy*

Specification	AMS 5545				AMS 5712 and AMS 5713
Form	Sheet			Plate	Bar and forging
Condition	Solution treated and aged (1400 F)				
Thickness or diameter, in.	≤0.020	0.021-0.187		0.188-0.375	≤1.000
Basis	S	A[a]	B[a]	S	S
Mechanical Properties:					
F_{tu}, ksi:					
L	...	170[b]	185	...	170
LT	160	170[b]	185	170	...
F_{ty}, ksi:					
L	...	123	132	...	130
LT	120	123	132	130	...
F_{cy}, ksi:					
L	...	132	142	...	133
LT	...	135	145	...	...
F_{su}, ksi	...	105	114	105	110
F_{bru}, ksi:					
(e/D = 1.5)	...	244	266	244	...
(e/D = 2.0)	...	310	338	310	...
F_{bry}, ksi:					
(e/D = 1.5)	...	197	211	208	...
(e/D = 2.0)	...	245	263	259	...
e, percent (S-basis):					
L	...	...	...	...	8
LT	6	10	...	10	...
RA, percent (S-basis):					
L	...	...	...	...	10
E, 10^3 ksi	31.6				
E_c, 10^3 ksi	31.6				
G, 10^3 ksi	12.1				
μ	0.31				
Physical Properties:					
ω, lb/in.^{3}	0.298				
C, *K*, and α	See Figure 6.3.7.0				

[a]Design allowables were based upon data from samples of material, supplied in solution treated condition, which were aged to demonstrate heat treat response by suppliers. Properties obtained by the user may be different if the material has been formed or otherwise cold worked.
[b]S-basis. The A value is 178 ksi.

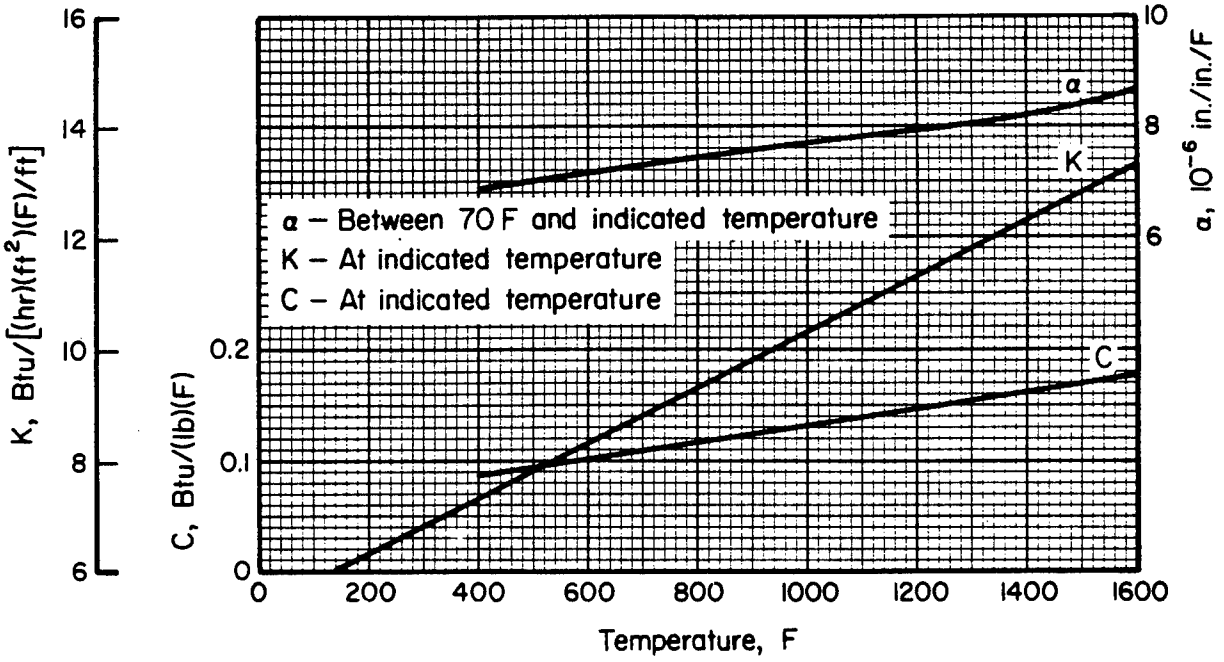


FIGURE 6.3.7.0. *Effect of temperature on the physical properties of Rene´41 alloy.*

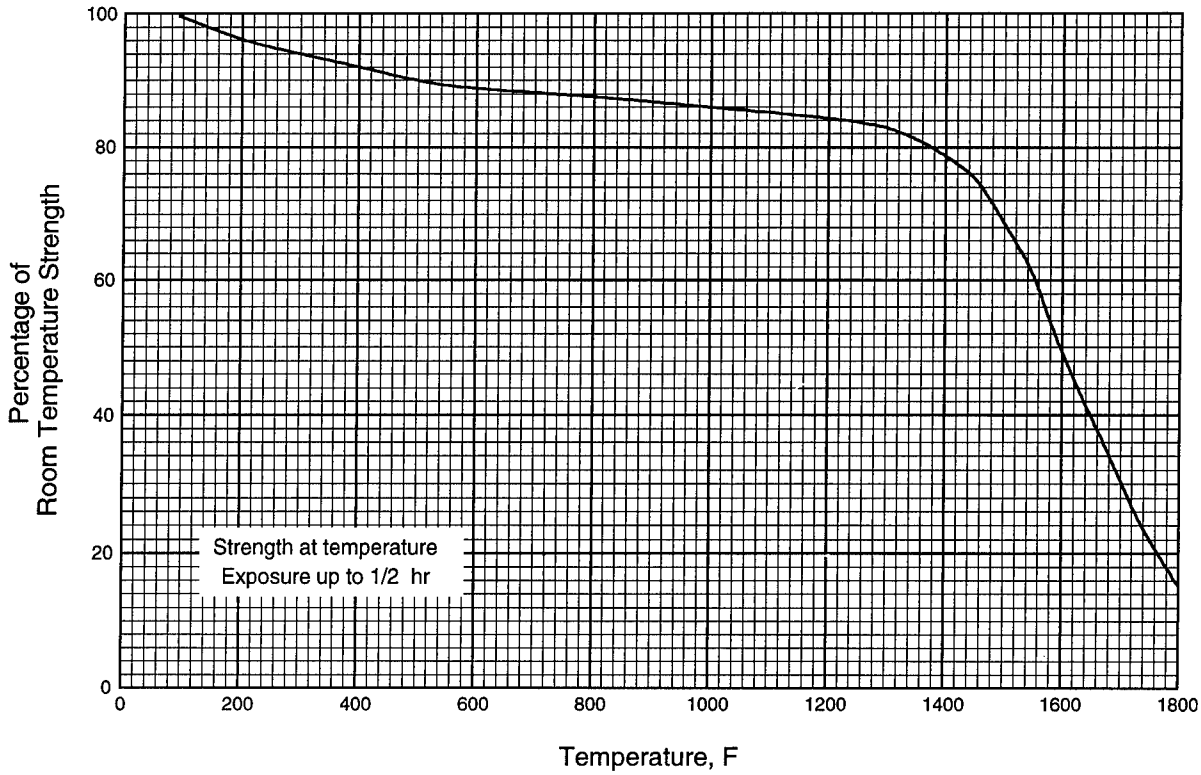


FIGURE 6.3.7.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of René 41 alloy.*

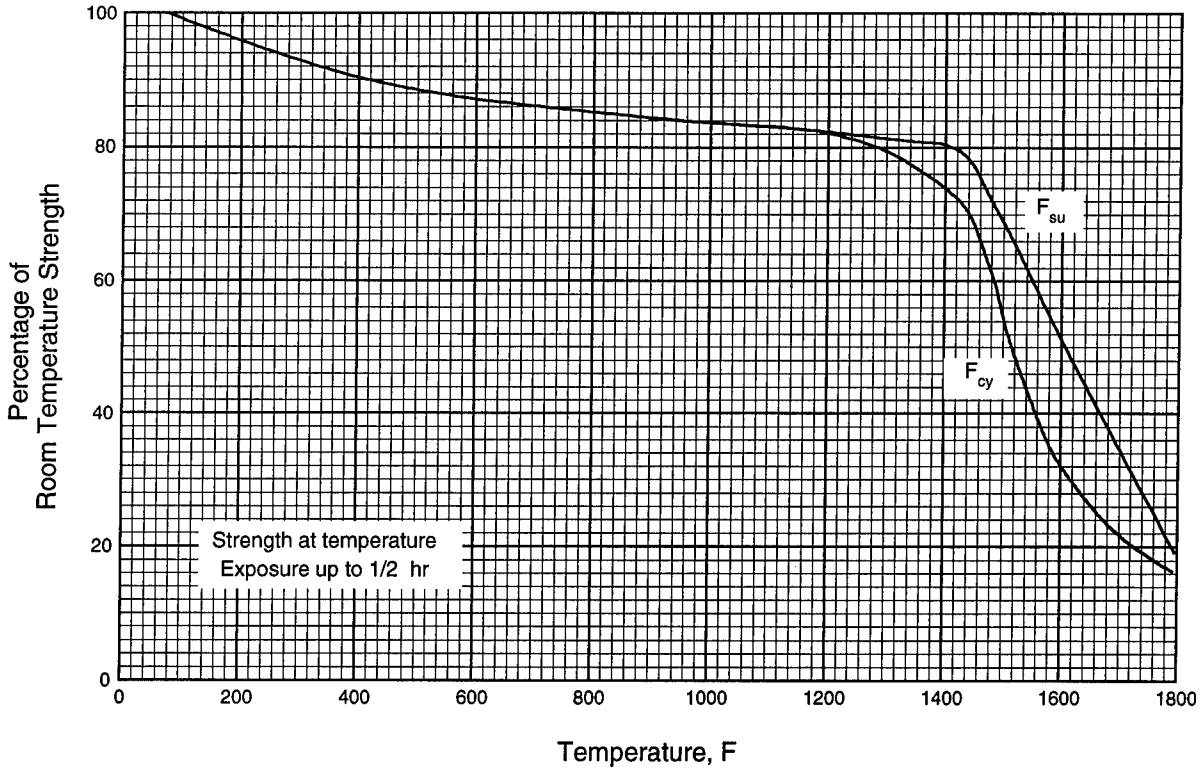


FIGURE 6.3.7.1.2. *Effect of temperature on the compressive yield strength (F_{cy}) and the shear ultimate strength (F_{su}) of René 41 alloy.*

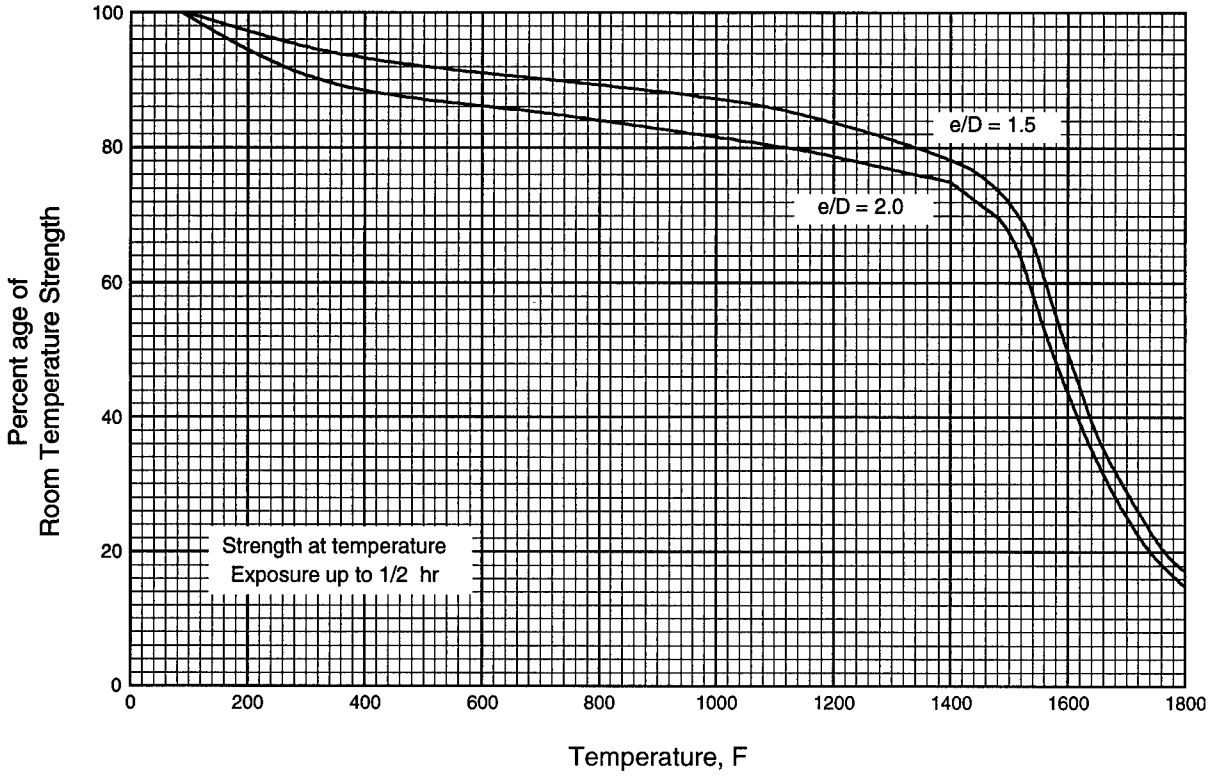


FIGURE 6.3.7.1.3(a). *Effect of temperature on the ultimate bearing strength (F_{bru}) of René 41 alloy.*

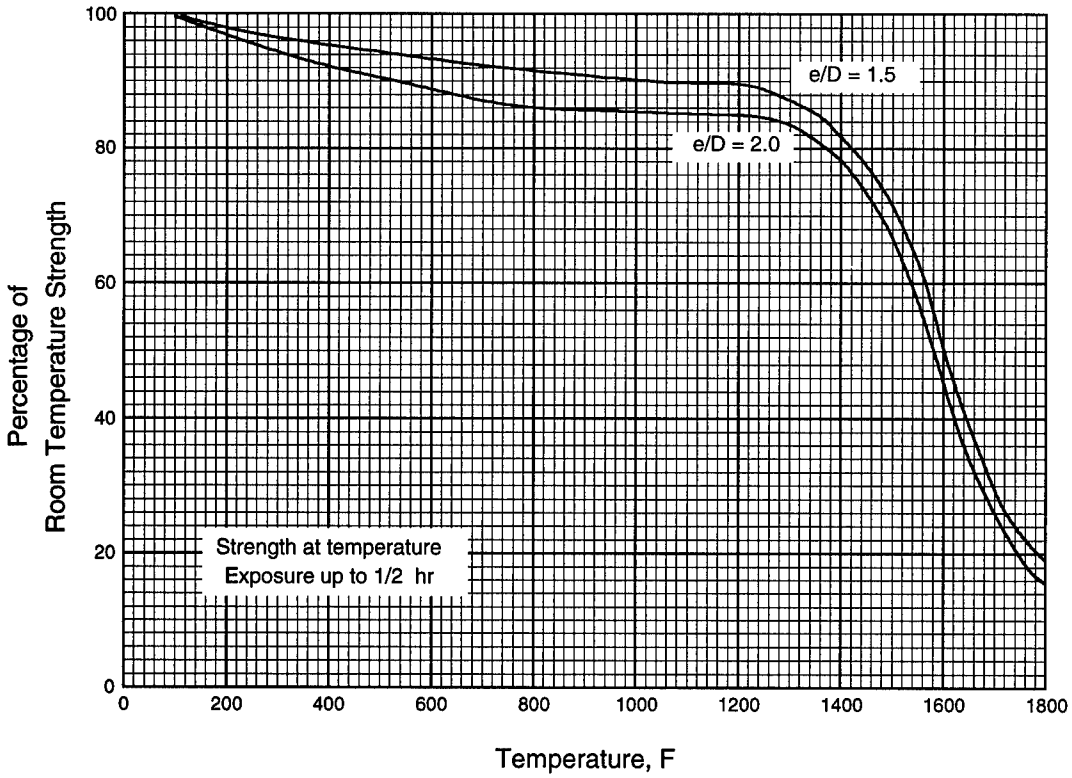


FIGURE 6.3.7.1.3(b). *Effect of temperature on the bearing yield strength (F_{bry}) of René 41 alloy.*

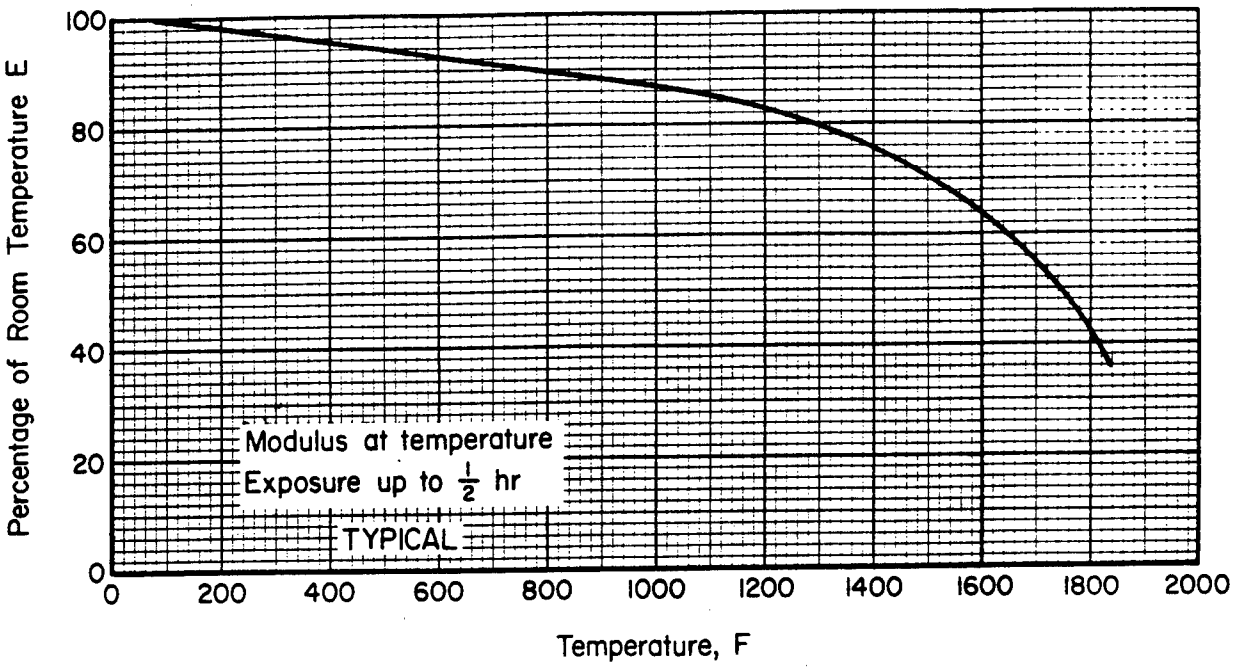


FIGURE 6.3.7.1.4. *Effect of temperature on the tensile modulus (E) of René 41 alloy.*

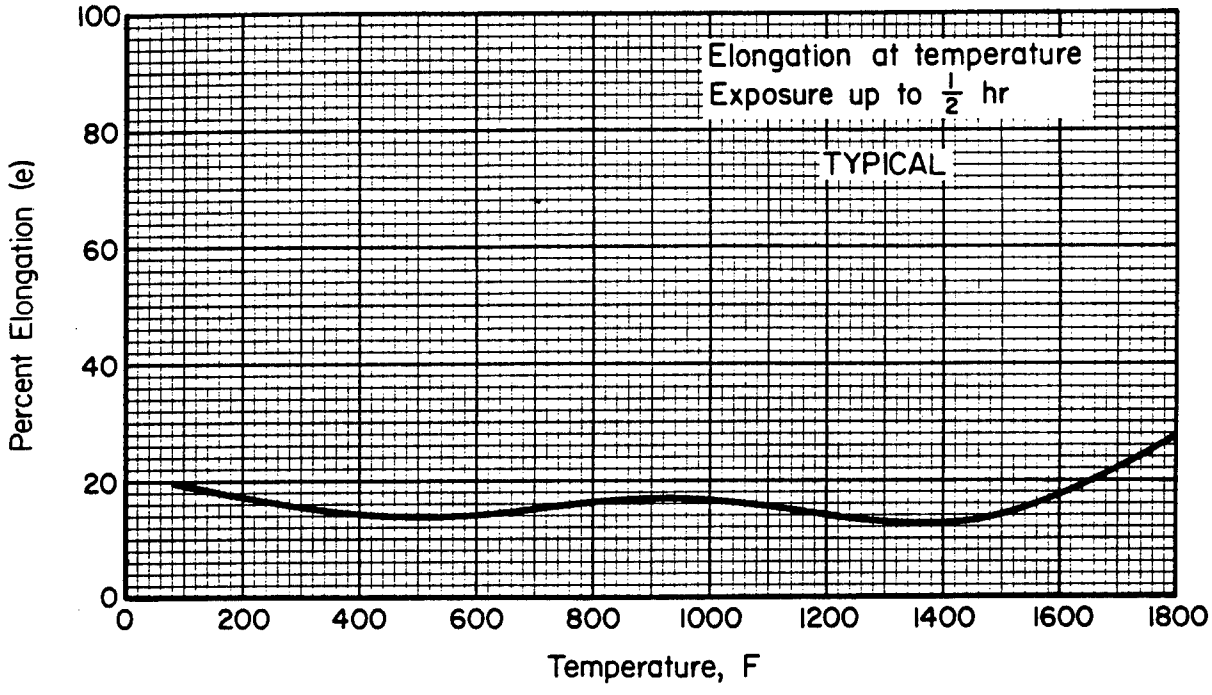


FIGURE 6.3.7.1.5. *Effect of temperature on the elongation (e) of René 41 alloy (>0.020 thickness) sheet.*

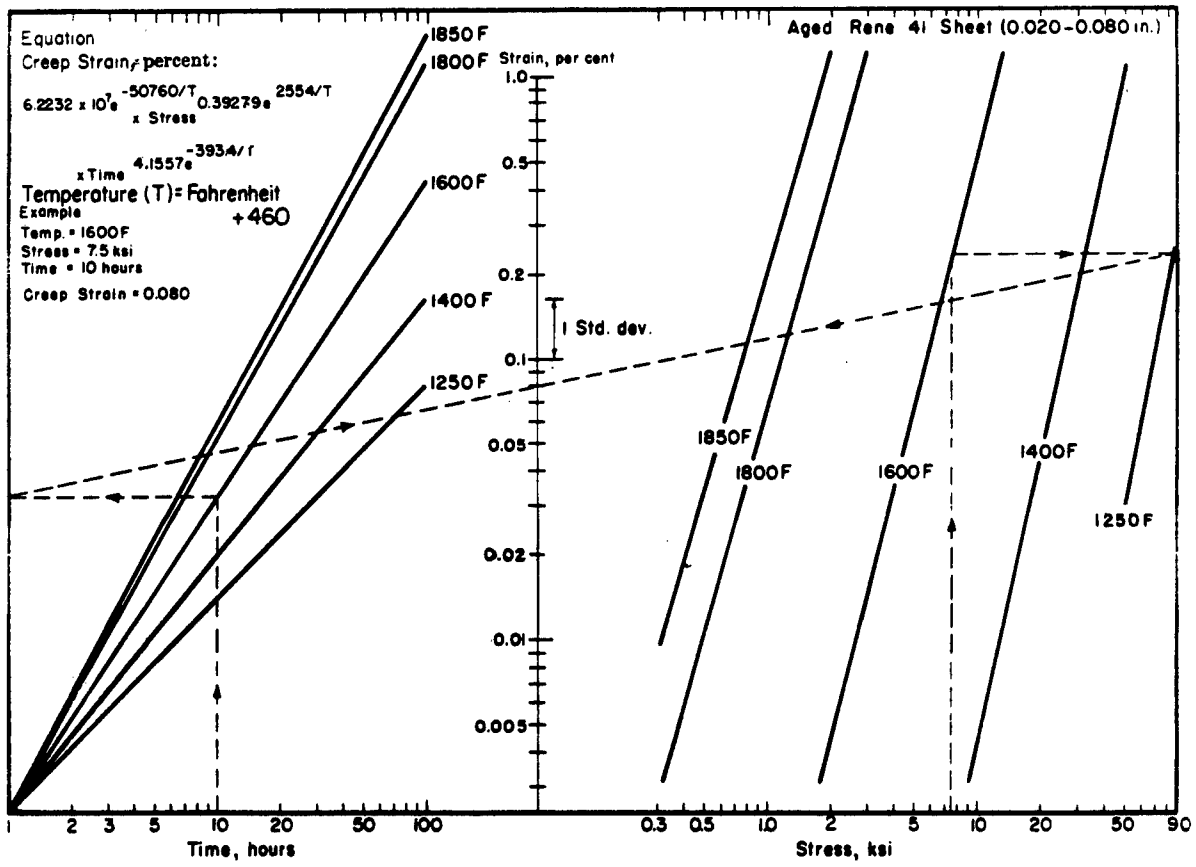


FIGURE 6.3.7.1.7. *Typical creep properties of Rene 41 alloy sheet.*

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6.3.8 WASPALOY

6.3.8.0 *Comments and Properties.*—Waspaloy is a vacuum-melted precipitation-hardened nickel-base alloy which is strengthened by the precipitation of titanium and aluminum compounds and the solid-solution strengthening effects of chromium, molybdenum, and cobalt. The alloy is designed for highly stressed parts operating at temperatures up to 1550 F, such as aircraft gas turbine blades and discs and rocket engine parts. It is available in all the usual mill forms.

The optimum range for forging is 2050 to 1900 F. Avoid working the alloy below 1900 F due to danger of cracking and also decreasing the stress-rupture life. Sufficient soaking time between heating is necessary to ensure complete recrystallization; however, avoid excessive long-time soaking at the high forging temperature. Furnace atmospheres should be either neutral or slightly oxidizing to prevent carburization and to minimize scaling.

Waspaloy is relatively difficult to machine. Drilling, turning, etc., can best be accomplished in solution-treated and partially aged condition. Generally, carbine tools are preferred, and positive feeds are required to avoid work hardening. For finish machining, grinding is preferable.

Waspaloy is susceptible to hot cracking or "hot-shortness" above 2150 F, therefore, extreme care should be exercised in the design of weldments so that restraint can be minimized. Waspaloy should be welded in the annealed condition, with minimum heat input, and with rapid cooling by means of chill bars and gas backup. This alloy has good resistance to oxidation at temperatures up to 1750 F and to combustion products encountered in aircraft gas turbines.

Two heat treatments are used for this material. One is for optimum tensile strength (solution treated 1825 to 1900 F, stabilize 1550 F, 24 hours air cool, and age 16 hours at 1400 F air cool), and the other for stress-rupture properties (solution treated 1975 F, stabilized 1550 F, 24 hours air cool, age 1400 F, 16 hours air cool).

Some material specifications for Waspaloy are shown in Table 6.3.8.0(a). Room-temperature mechanical properties are shown in Table 6.3.8.0 (b). Physical properties at room and elevated temperatures are shown in Figure 6.3.8.0.

TABLE 6.3.8.0(a). *Material Specifications for Waspaloy*

Specification	Form
AMS 5544	Plate, sheet, and strip
AMS 5704	Forgings
AMS 5706	Bar, forging, ring
AMS 5707	Bar, forging, ring
AMS 5708	Bar, forging, ring
AMS 5709	Bar, forging, ring[a]

[a]Primarily for applications requiring high stress-rupture strength.

6.3.8.1 Aged Condition.—Stress rupture requirements at elevated temperatures are specified in material specifications. The appropriate specification should be consulted for detailed requirements. The effect of temperature on various mechanical properties is shown in Figures 6.3.8.1.1, 6.3.8.1.4, as well as 6.3.8.1.5(a) and (b). The effect of temperature on the Ramberg-Osgood parameter, n (tension), is shown in Figure 6.3.8.1.6(a). Typical tensile stress-strain curves are shown in Figure 6.3.8.1.6(b).

TABLE 6.3.8.0(b). *Design Mechanical and Physical Properties of Waspaloy*

Specification	AMS 5544		AMS 5704	AMS 5706 and AMS 5707
Form	Sheet, strip, and plate		Forging	Bar, forging, and ring
Condition	Solution, stabilization, and precipitation heat treated			
Thickness, in.	≤0.020	>0.020	≤3.500	≤3.500
Basis	S	S	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	...	...	175	160
LT	170	175	...	...
F_{ty}, ksi:				
L	...	...	120	110
LT	110	115	...	...
F_{cy}, ksi:				
L	...	...	...	...
LT	...	...	...	...
F_{su}, ksi	...	...	...	...
F_{bru}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
F_{bry}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
e, percent:				
L	...	...	15	15
LT	15	20	...	...
RA, percent:				
L	...	...	18	18
E, 10^3 ksi	30.6			
E_c, 10^3 ksi	...			
G, 10^3 ksi	...			
μ	...			
Physical Properties:				
ω, lb/in.^{3}	0.298			
C, Btu/(lb)(F)	See Figure 6.3.8.0			
K, Btu/[(hr)(ft^2)(F)/ft]	See Figure 6.3.8.0			
α, 10^{-6} in./in./F	See figure 6.3.8.0			

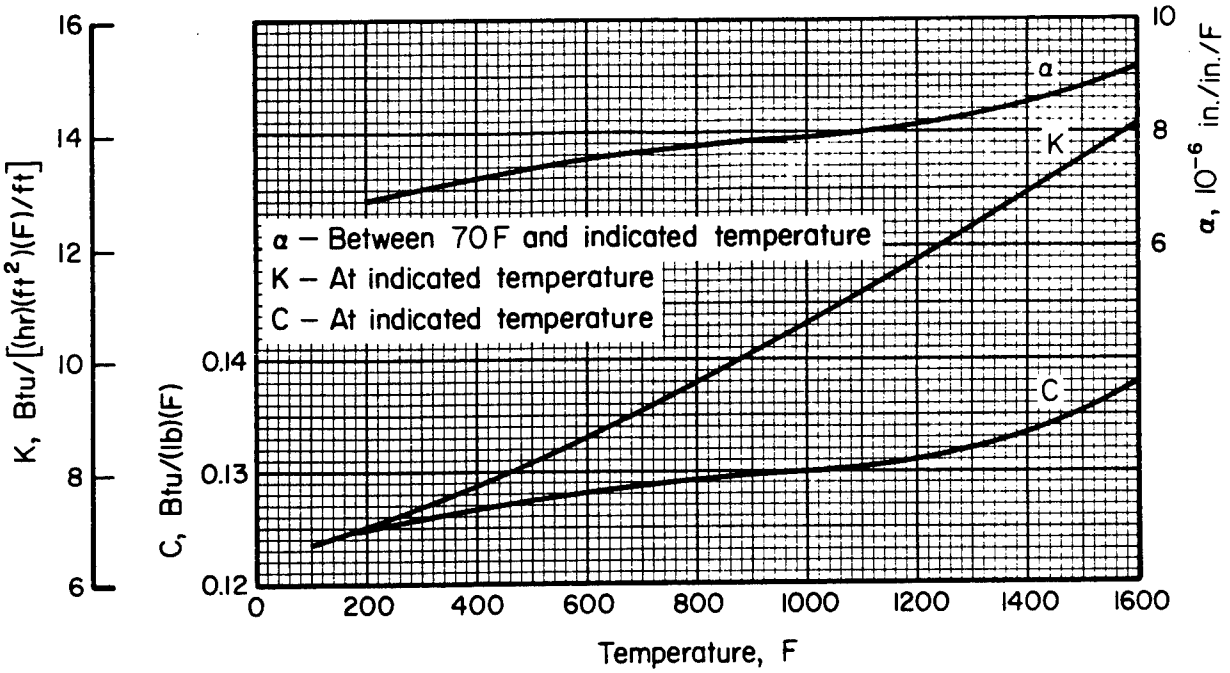


FIGURE 6.3.8.0. *Effect of temperature on the physical properties of Waspaloy.*

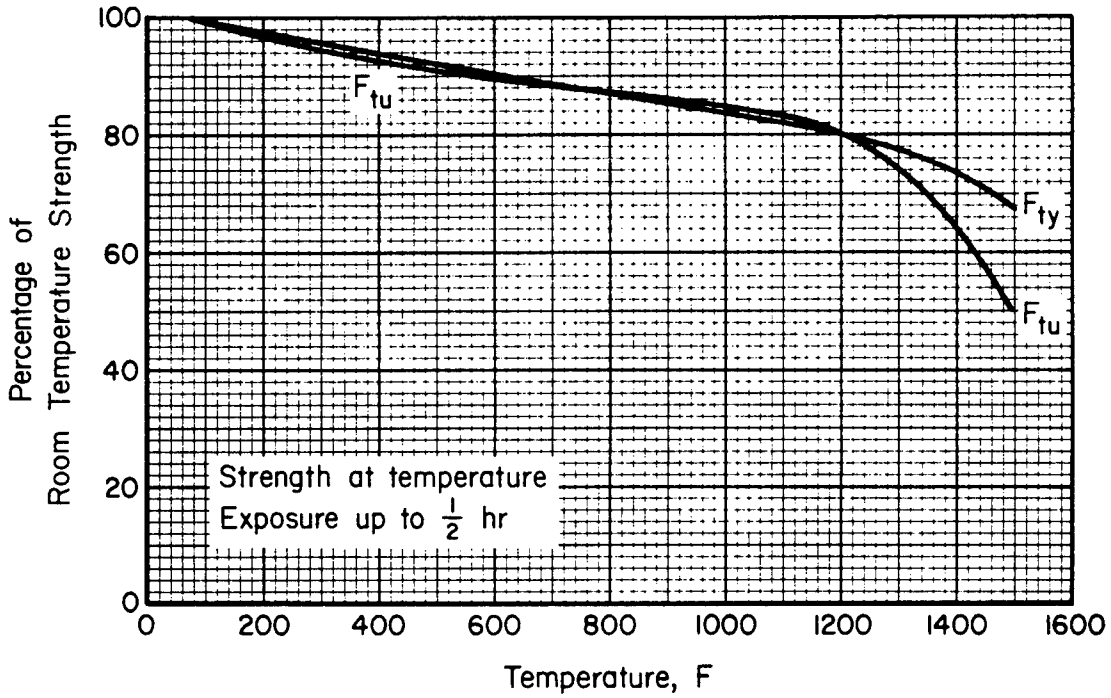


FIGURE 6.3.8.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of Waspaloy.*

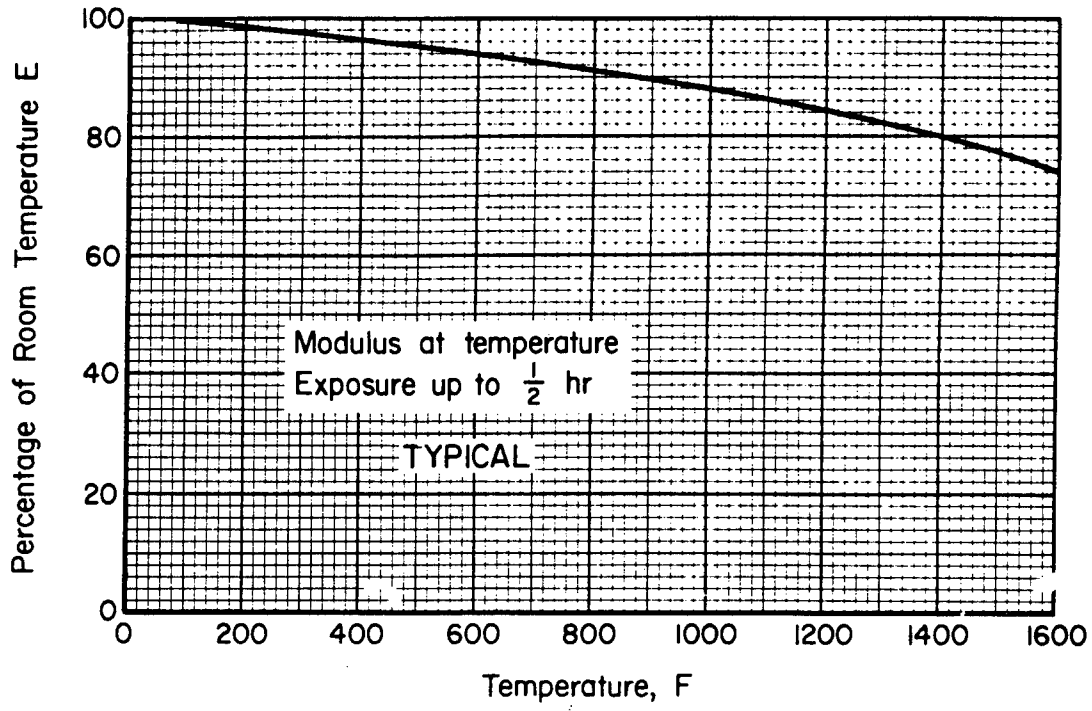


FIGURE 6.3.8.1.4. *Effect of temperature on the modulus of elasticity (E) of Waspaloy.*

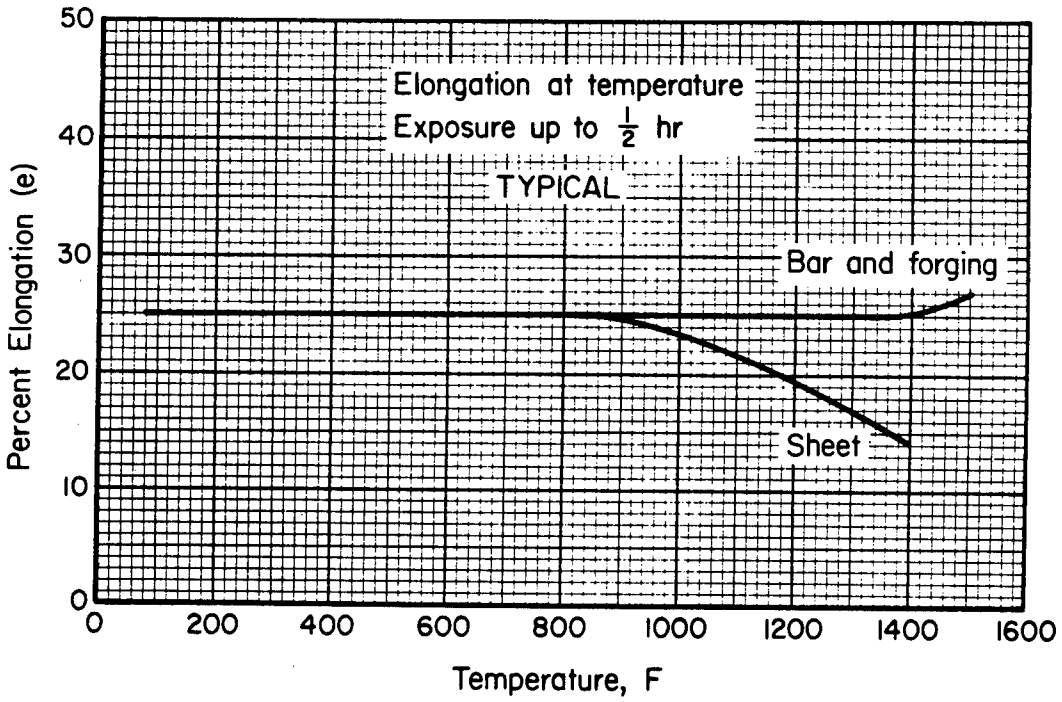


FIGURE 6.3.8.1.5(a). *Effect of temperature on elongation (e) of Waspaloy.*

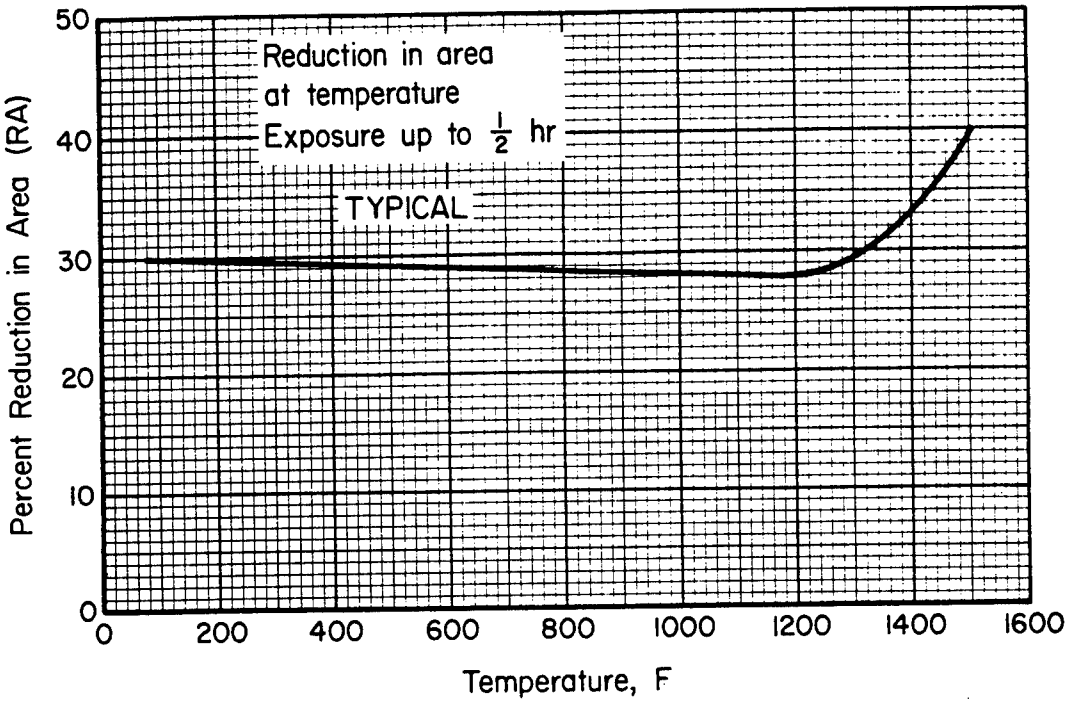


FIGURE 6.3.8.1.5.(b) *Effect of temperature on reduction in area (RA) of Waspaloy bar and forging.*

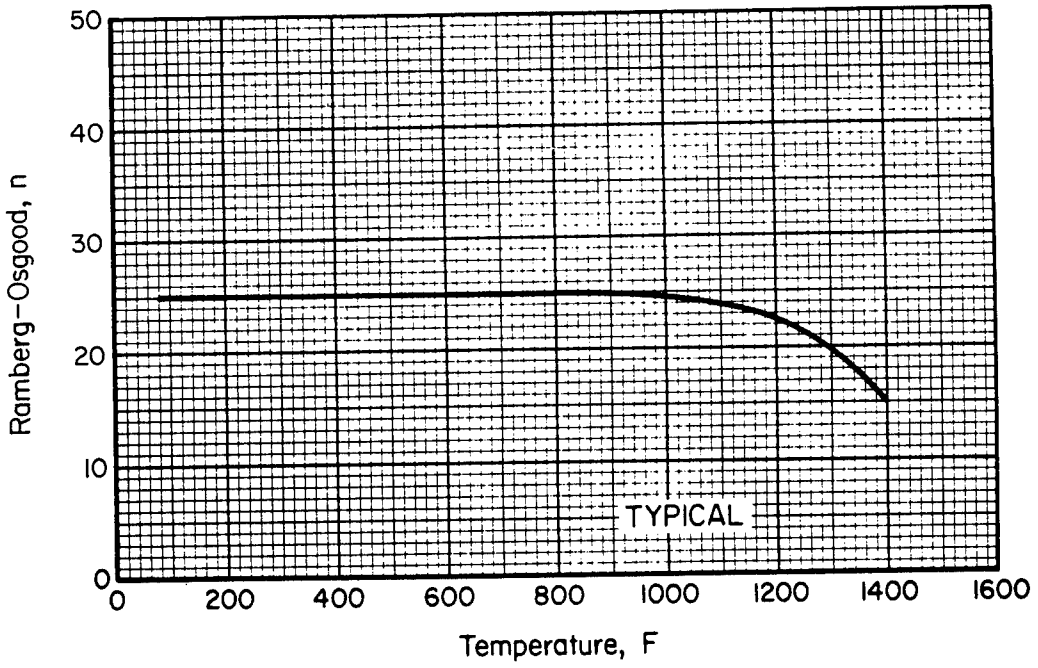


FIGURE 6.3.8.1.6(a). *Effect of temperature on Ramberg-Osgood parameter (n in tension) of Waspaloy.*

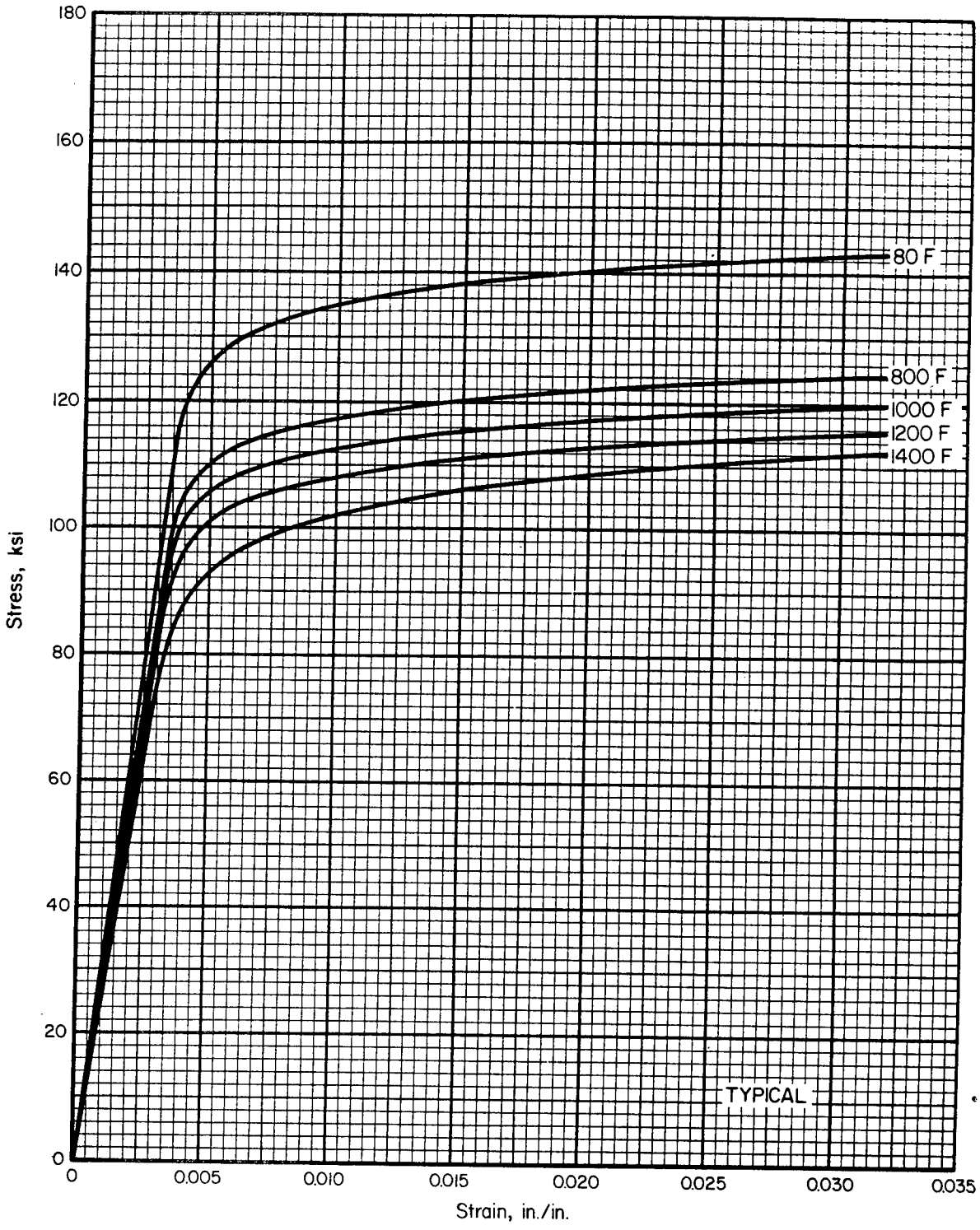


FIGURE 6.3.8.1.6.(b) *Typical tensile stress-strain curves for Waspaloy at room and elevated temperatures (all products).*

6.4 Cobalt-Base Alloys

6.4.0 GENERAL COMMENTS.—The use of cobalt in wrought heat-resistant alloys is usually limited to additions of cobalt to alloys of other bases. Very few of the heat-resistant alloys can be considered as cobalt base, since cobalt is seldom the predominating element. For airframe applications, some workability is usually required; the alloys considered in this section are limited to those available in wrought form.

6.4.0.1 *Metallurgical Considerations.*

Composition.—The common alloying elements for cobalt are chromium, nickel, carbon, molybdenum, and tungsten. Chromium is added to increase strength and oxidation resistance at very high temperatures; nickel to increase toughness; carbon to increase the hardness and strength, especially when combined with chromium and the other carbide formers, molybdenum and tungsten; molybdenum and tungsten also contribute to solid-solution strengthening.

Vacuum melting is not required for these alloys. For this reason, the cobalt-base alloys are often competitively priced with vacuum-melted nickel-base alloys although the price of cobalt is higher than that of nickel.

Heat Treatment.—The cobalt-base alloys are heat treated with conventional equipment and fixtures such as those used with austenitic stainless steels. The use of good heat-treating practices is recommended, although this is not so critical as in the case of the nickel-based alloys.

6.4.0.2 *Manufacturing Considerations.*

Forging.—Because these alloys are designed to have very high strength at temperatures near the forging range, they require the use of heavy forging equipment. However, the forgeability of these alloys is good over a fairly wide range of temperatures. Hot-cold working is neither required nor recommended for these alloys.

Cold Forming.—These alloys, when in the solution-treated condition, have excellent ductility and are readily cold formed. Because of their capacity for work hardening, they require higher forming pressures and frequent anneals.

Machining.—These alloys are tough and they work harden rapidly; consequently, heavy-duty vibration-free machine tools, sharp cutting tools (high-speed steel or carbide tipped), and low cutting speeds are required.

Welding.—The weldability of the cobalt-base alloys is comparable with that of the austenitic stainless steels. Welding may be accomplished by all commonly used welding processes. Large or complex weldments require stress relief.

Brazing.—These alloys can be brazed using the same techniques and precautions applicable to stainless steels and nickel-base alloys. Alloys which contain aluminum or titanium require extremely dry, inert gas atmospheres, very high vacuum or a thin (0.002 to 0.0010-inch thick) nickel plating to prevent surface oxidation. It is also necessary to braze the material in the annealed condition and to keep the stresses low during brazing to avoid embrittlement, especially when brazing with low melting alloys.

6.4.0.3 *Special Precautions.*—If the cobalt--base alloys have not been exposed to neutron radiation, no special safety precautions in handling are required. However, neutron irradiation creates a very dangerous radioactive isotope, cobalt 60, which has a half life of about 5.2 years. Special precautions must be employed to protect personnel from the radioactive material.

6.4.1 L-605

6.4.1.0 *Comments and Properties.*—L-605, also known as Haynes Alloy 25, is a corrosion and heat-resistant cobalt-base alloy used for moderately stressed parts operating between 1000 and 1900 F. Its applications include gas turbine blades and rotors, combustion chambers, and afterburner parts. L-605 is not hardenable except by cold working and is usually used in the annealed condition. It is available in all the usual mill forms.

L-605 forges moderately well between 2250 and 1900 F. In the annealed condition, it has excellent formability at room temperature; severely

formed parts should be annealed at 2225 F for 7 to 10 minutes. L-605 is difficult to machine. Its toughness and capacity for work hardening necessitate the use of sharp tools and low cutting speeds; high-speed steel or carbide cutting tools are recommended. L-605 can be fusion or resistance welded or brazed; large or complex fusion weldment should be stress relieved at 1300 F for 2 hours. This alloy has excellent oxidation resistance up to 1900 F.

Some material specifications for L-605 are shown in Table 6.4.1.0(a). Room-temperature mechanical and physical properties are shown in Table 6.4.1.0(b). The effect of temperature on physical properties is shown in Figure 6.4.1.0.

TABLE 6.4.1.0(a). *Material Specifications for L-605 Alloy*

Specification	Form	Condition
AMS 5537	Sheet	Solution treated (annealed)
AMS 5759	Bar and forging	Solution treated (annealed)

6.4.1.1 *Solution Treated Condition.*—Elevated temperature properties for this condition are shown in Figures 6.4.1.1.1 through 6.4.1.1.5. A creep nomograph is shown in Figure 6.4.1.1.7. Stress-rupture requirements at elevated temperatures are specified in material specifications. The appropriate specification should be consulted for detailed requirements.

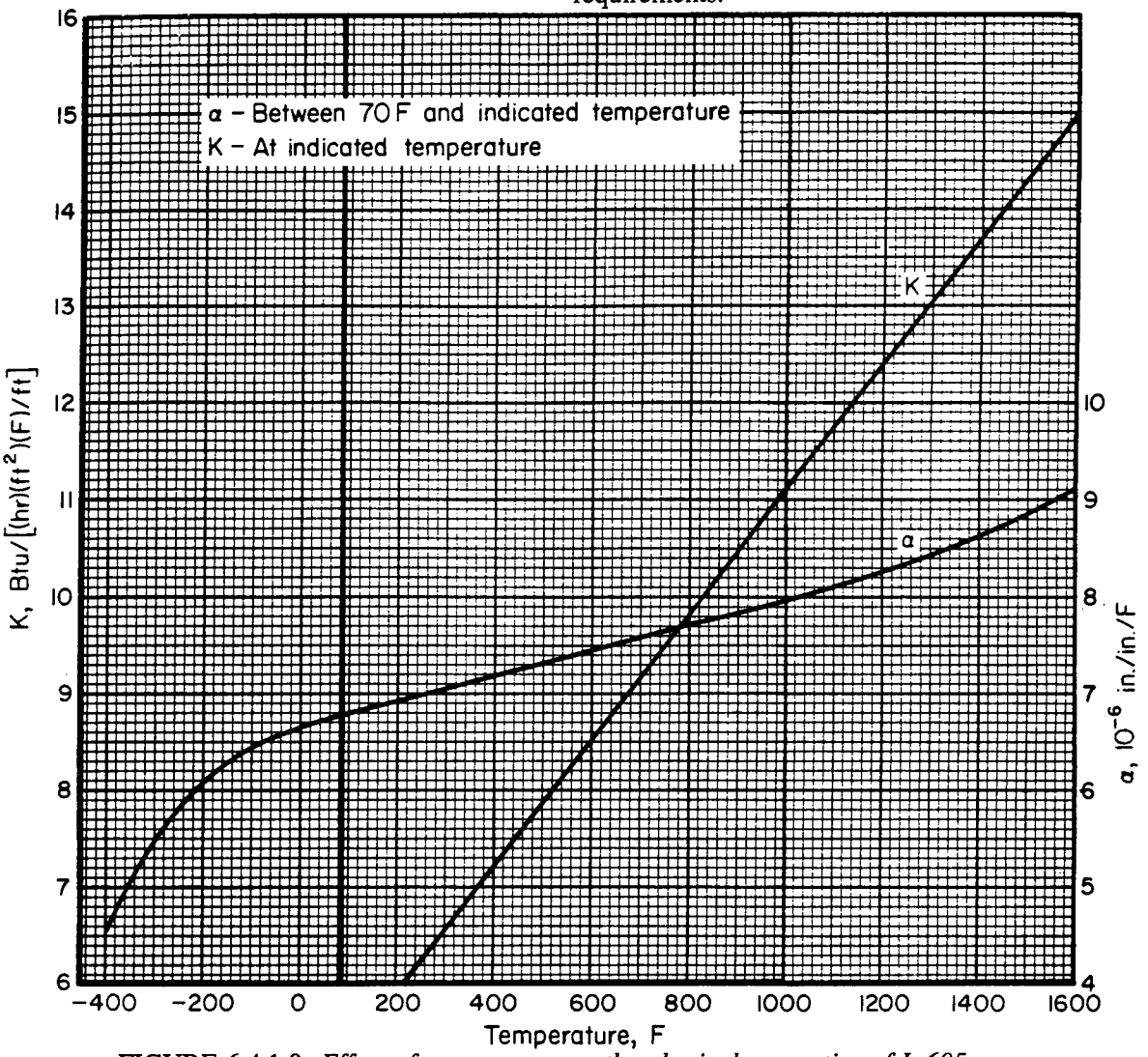


FIGURE 6.4.1.0 *Effect of temperature on the physical properties of L-605.*

TABLE 6.4.1.0(b). *Design Mechanical and Physical Properties of L-605 Alloy*

Specification	AMS 5537			AMS 5759
Form	Sheet		Plate	Bar and forging
Condition	Solution treated			
Thickness, in.	0.010-0.187		0.188-0.375	≤1.000
Basis	A	B	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	126	131	...	125
LT	130	135	130	...
F_{ty}, ksi:				
L	57	62	...	45
LT	55[a]	60	55	...
F_{cy}, ksi:				
L	41	45	...	42
LT	56	61	...	...
F_{su}, ksi	91	95	91	88
F_{bru}, ksi:				
(e/D = 1.5)	186	193	186	...
(e/D = 2.0)	232	241	232	...
F_{bry}, ksi:				
(e/D = 1.5)	88	96	88	...
(e/D = 2.0)	113	123	113	...
e, percent (S-basis):				
L	...	...	...	30
LT	[b]	...	45	...
E, 10^3 ksi	32.6			
E_c, 10^3 ksi	32.6			
G, 10^3 ksi	12.6			
μ	0.29			
Physical Properties:				
ω, lb/in.^{3}	0.330			
C, Btu/(lb)(F)	0.090 (70-212 F)			
C, K, and α	See Figure 6.4.1.0			

[a]The A value is higher than specification value as follows: F_{ty} = 56 ksi.
[b]30 - ≤0.020; 35 - 0.021 to 0.032; 40 - 0.033 to 0.043; 45 - 0.043.

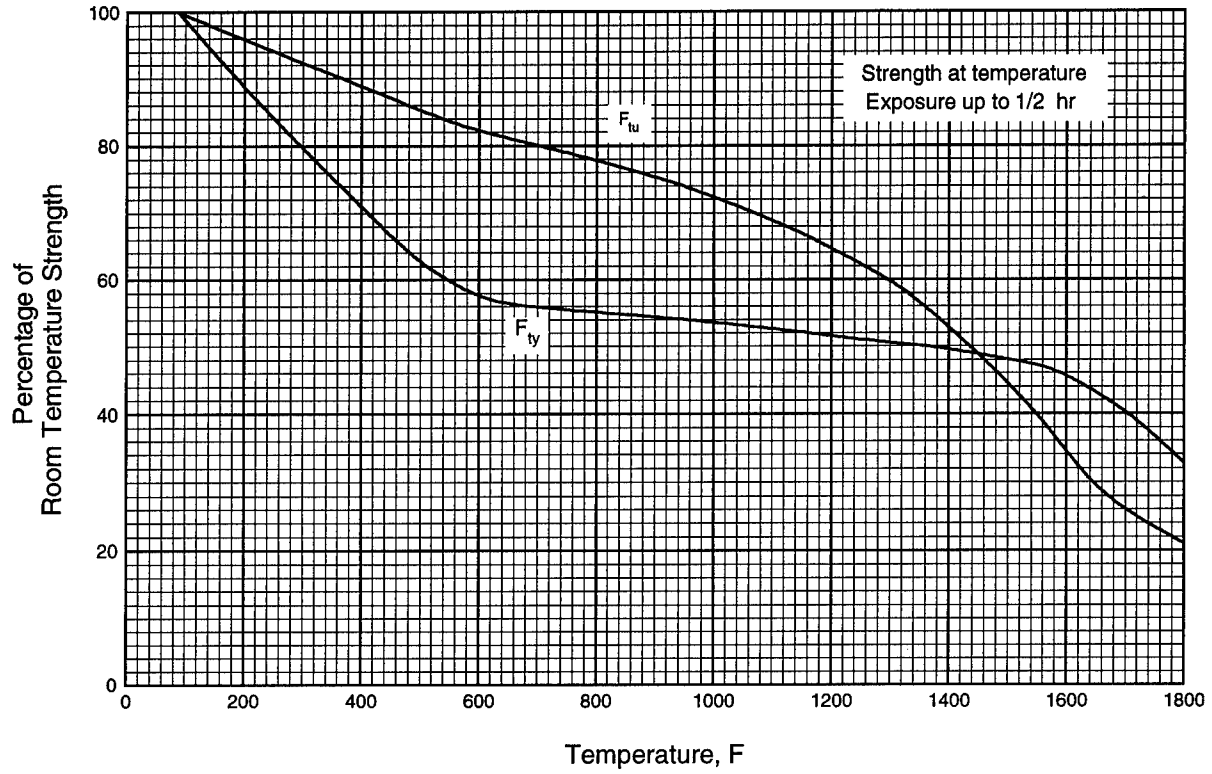


FIGURE 6.4.1.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield strength (F_{ty}) of L-605 alloy.*

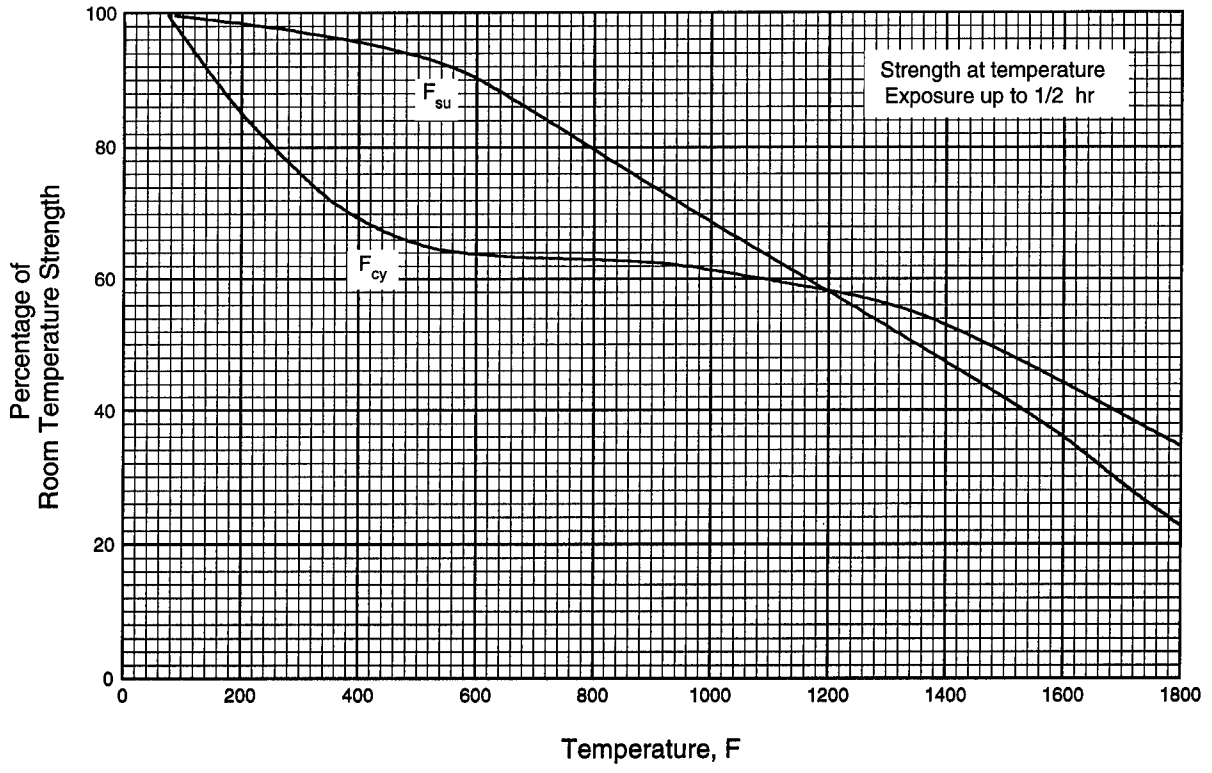


FIGURE 6.4.1.1.2. *Effect of temperature on the compressive yield strength (F_{cy}) and the shear ultimate strength (F_{su}) of L-605 alloy.*

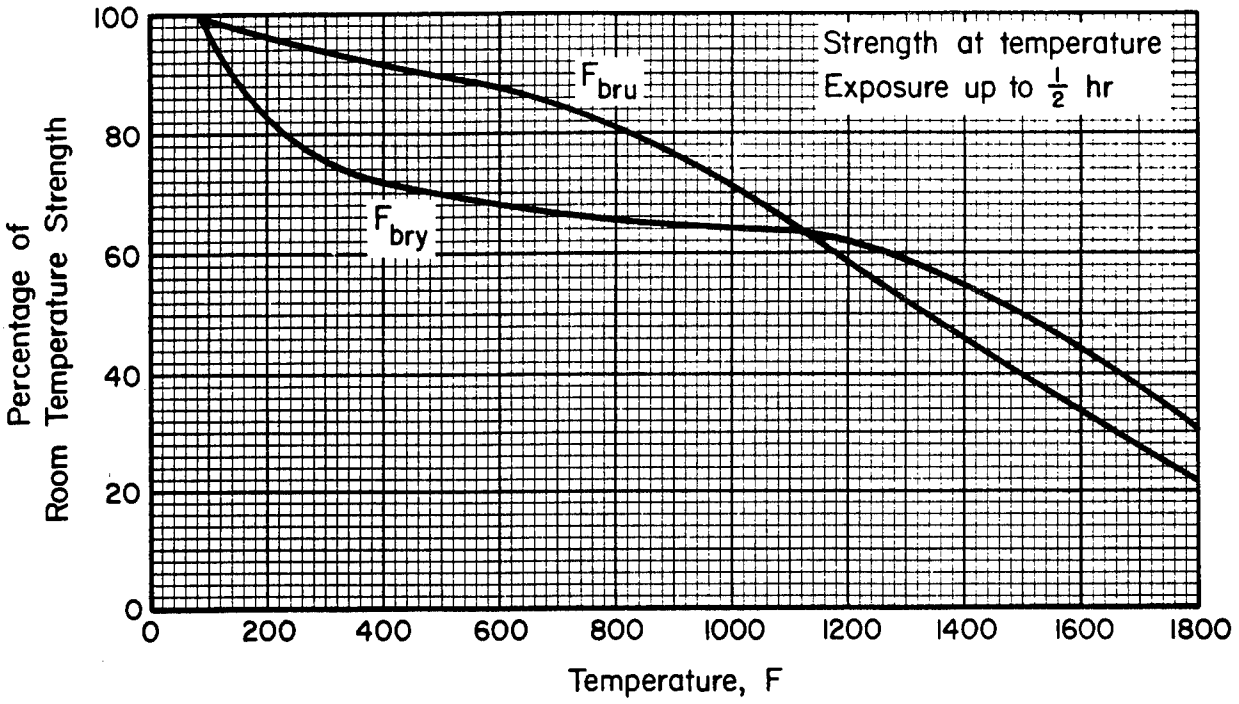


FIGURE 6.4.1.1.3. *Effect of temperature on the bearing ultimate strength (F_{bru}) and the bearing yield strength (F_{bry}) of L-605 alloy sheet.*

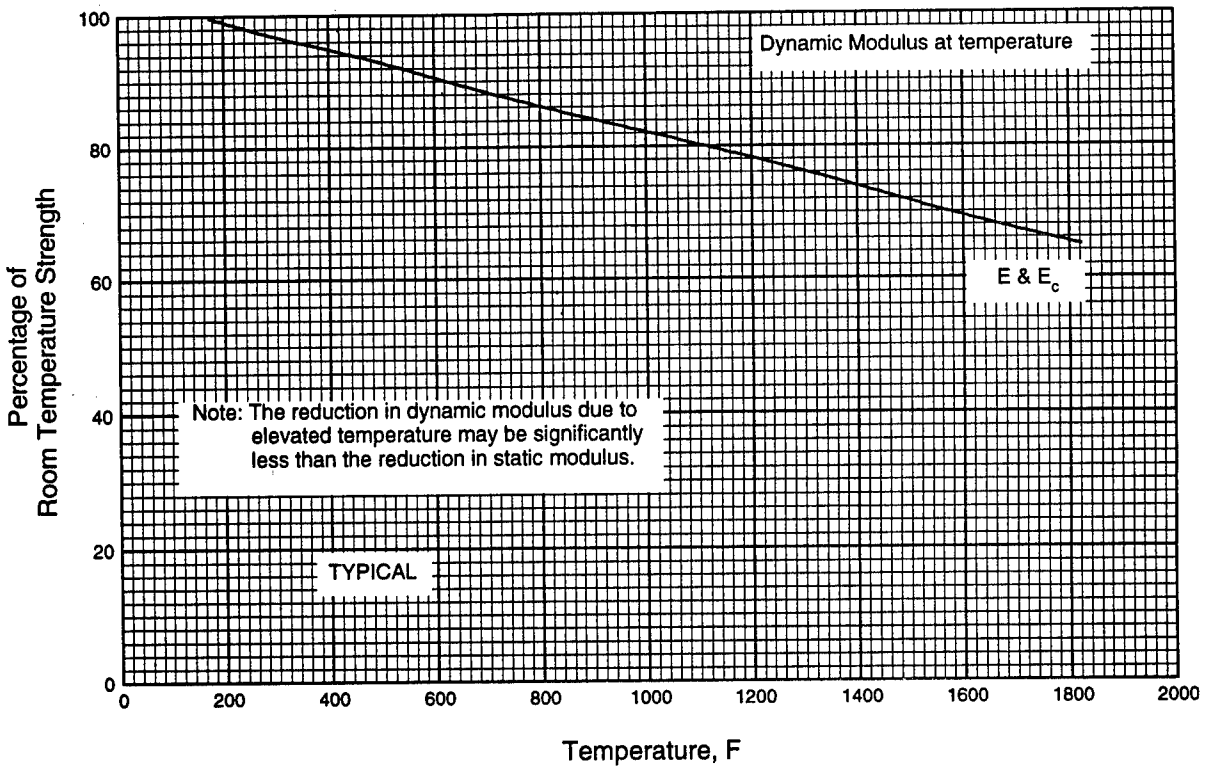


FIGURE 6.4.1.1.4(a). *Effect of temperature on dynamic moduli (E and E_c) of L-605 sheet.*

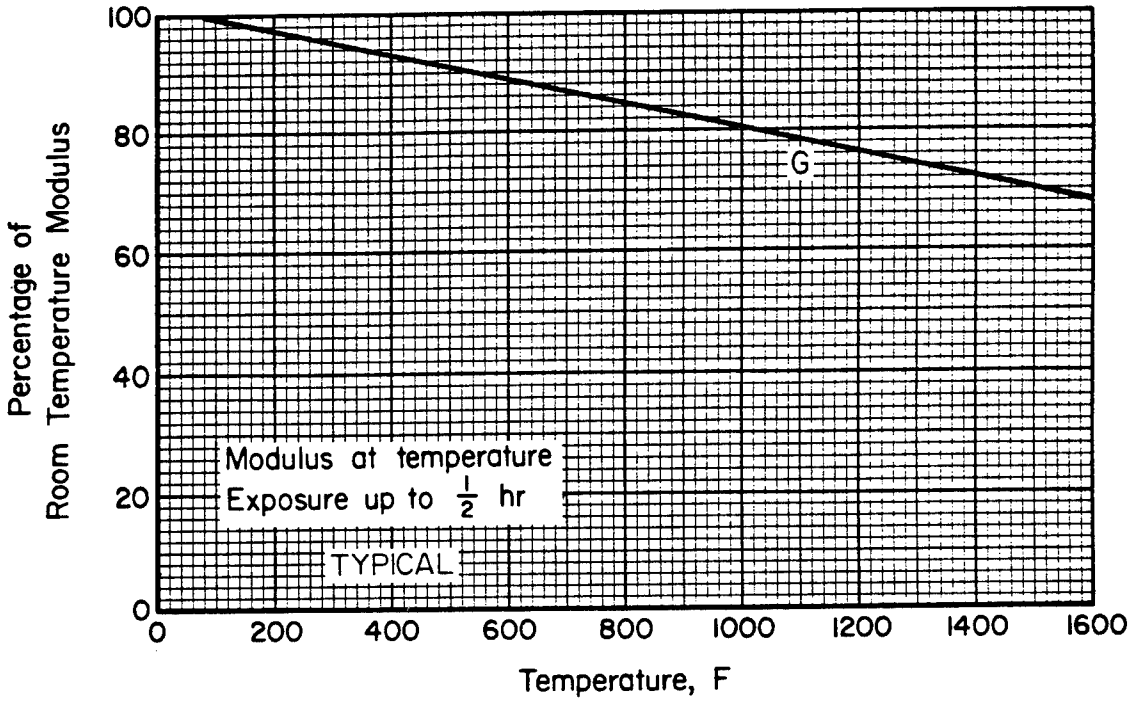


FIGURE 6.4.1.1.4(b). *Effect of temperature on the shear modulus (G) of L-605 sheet.*

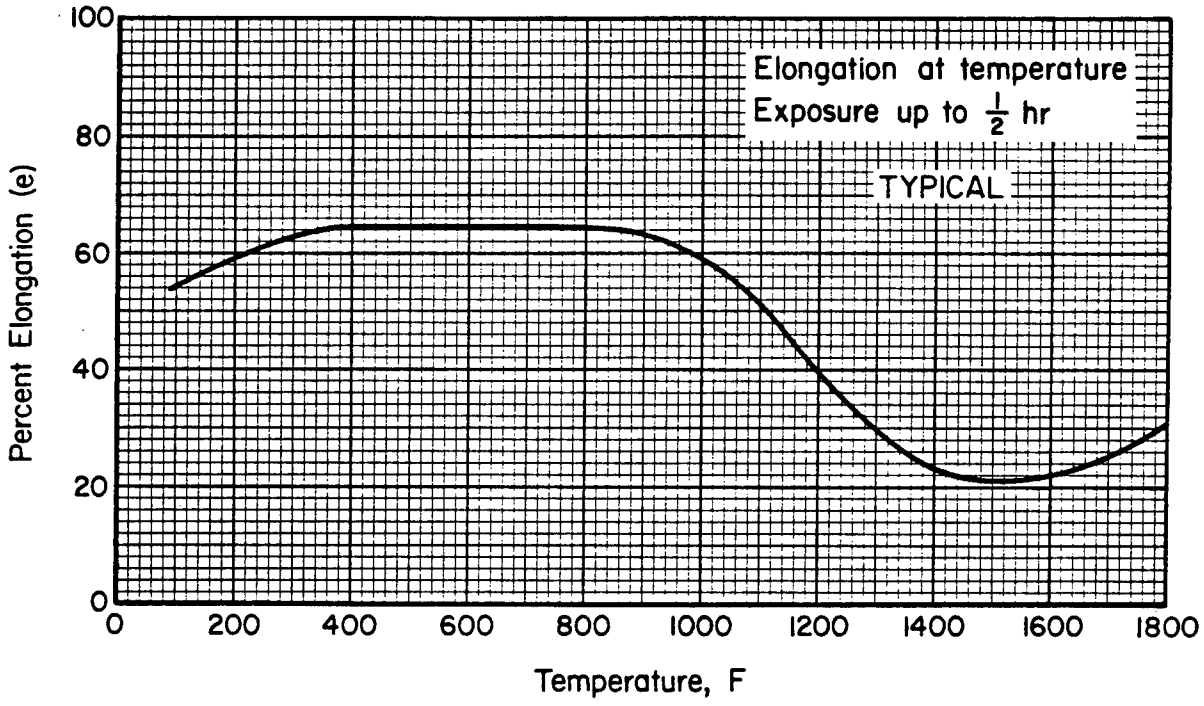


FIGURE 6.4.1.1.5. *Effect of temperature on the elongation (e) of L-605 alloy (> 0.020 thickness) sheet.*

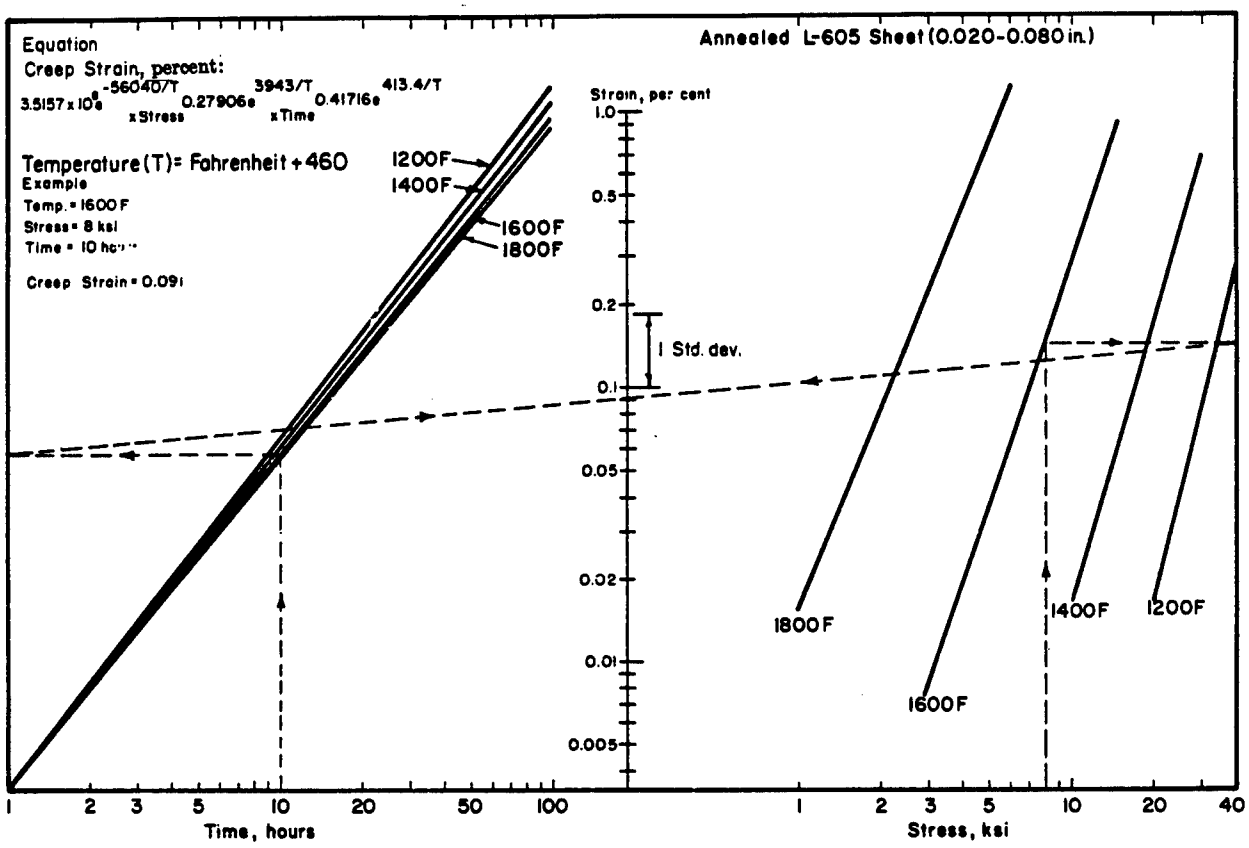


FIGURE 6.4.1.1.7. *Typical creep properties of L-605 alloy sheet.*

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6.4.2 ALLOY 188

6.4.2.0 *Comments and Properties.*—Alloy 188 is a corrosion- and heat-resistant cobalt-base alloy used for moderately stressed parts up to 2100 F. The alloy exhibits outstanding oxidation resistance up to 2100 F resulting from the addition of minute amounts of lanthanum to the alloy system. The alloy exhibits excellent post-aged ductility after prolonged heating of 1000 hours at temperatures up to 1600 F inclusive.

Alloy 188 is not hardenable except by cold working and is used in the solution-treated condition. The alloy can be forged and welded. Welding can be accomplished by both manual and automatic welding methods including electron beam, gas tungsten air, and resistance welding. Like other cobalt base alloys, machining is difficult necessitating the use of sharp tools and low cutting speeds; high speed steel or carbide cutting tools are recommended. Gas turbine applications include transition ducts, combustion cans, spray bars, flame-holders, and liners.

Material specifications for Alloy 188 are presented in Table 6.4.2.0(a). Room-temperature mechanical and physical properties are shown in Table 6.4.2.0(b). The effect of temperature on physical properties is shown in Figure 6.4.2.0.

TABLE 6.4.2.0(a). *Material Specifications for Alloy 188*

Specification	Form	Condition
AMS 5608	Sheet and plate	Solution treated (annealed)
AMS 5772	Bar and forging	Solution treated (annealed)

6.4.2.1 *Solution-Treated Condition.*—Elevated-temperature properties are presented in Figures 6.4.2.1.1(a) and (b), 6.4.2.1.2, 6.4.2.1.4(a) through (c), and 6.4.2.1.5. Typical tensile stress-strain curves at room temperature are presented in Figure 6.4.2.1.6(a). Typical compressive stress-strain and tangent-modulus curves at room and elevated temperatures are presented in Figure 6.4.2.1.6(b). Strain control fatigue data for bar are presented in Figures 6.4.2.1.8(a) through (d).

TABLE 6.4.2.0(b). *Design Mechanical and Physical Properties of Alloy 188 Sheet*

Specification	AMS 5608	
Form	Sheet	
Condition	Solution Treated	
Thickness, in.	<0.020	0.020-0.187
Basis	S	S
Mechanical Properties:		
F_{tu}, ksi:		
L	125	125
LT	125	125
F_{ty}, ksi:		
L	57	57
LT	55	55
F_{cy}, ksi:		
L	...	...
LT	55	55
F_{su}, ksi	111	111
F_{bru}, ksi:		
(e/D = 1.5)	...	...
(e/D = 2.0)	...	...
F_{bry}, ksi:		
(e/D = 1.5)	...	...
(e/D = 2.0)	...	...
e, percent:		
LT	40	45
E, 10^3 ksi	33.6	
E_c, 10^3 ksi	33.6	
G, 10^3 ksi	12.8	
μ	0.31	
Physical Properties:		
ω, lb/in.^{3}	0.324	
C, *K*, and α	See Figure 6.4.2.0	

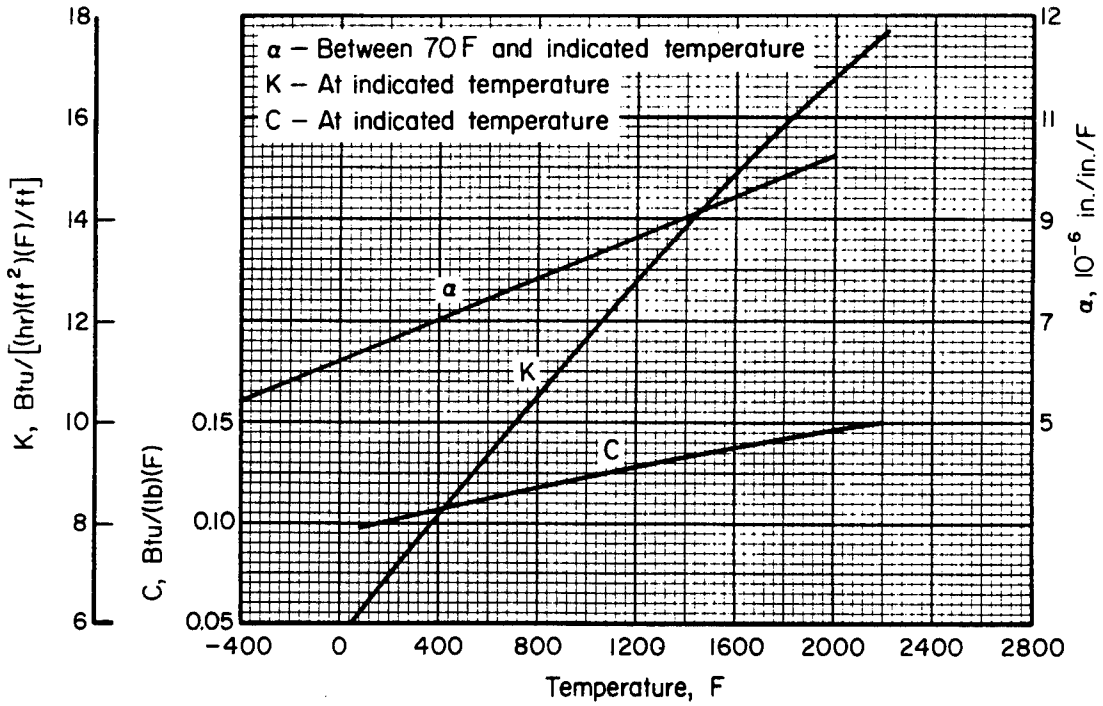


FIGURE 6.4.2.0. *Effect of temperature on the physical properties of Alloy 188.*

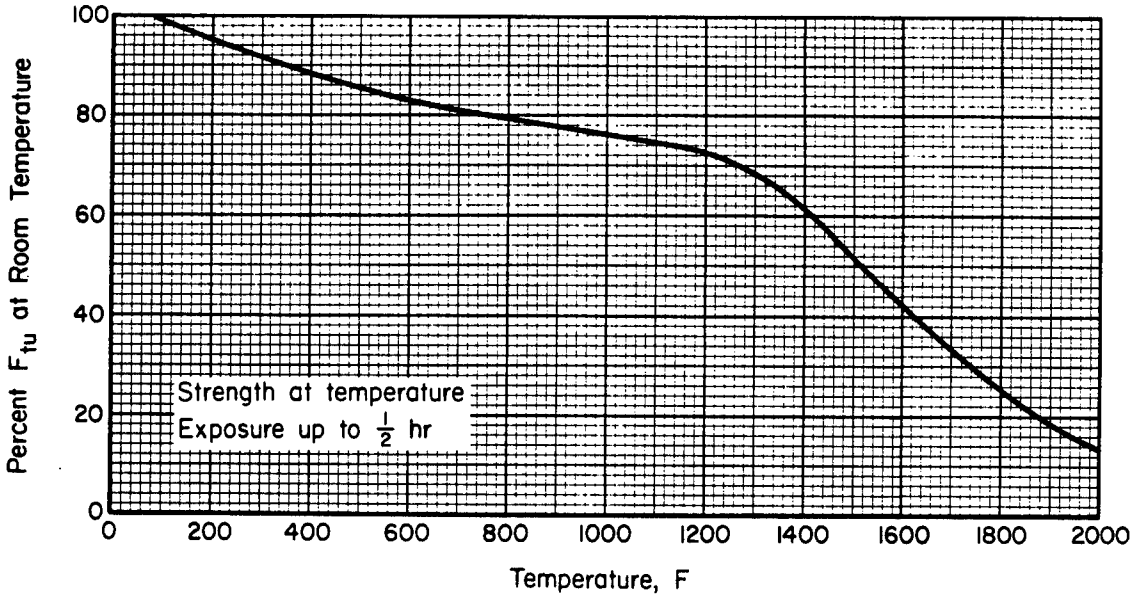


FIGURE 6.4.2.1.1(a). *Effect of temperature on ultimate tensile strength (F_{tu}) of Alloy 188 sheet.*

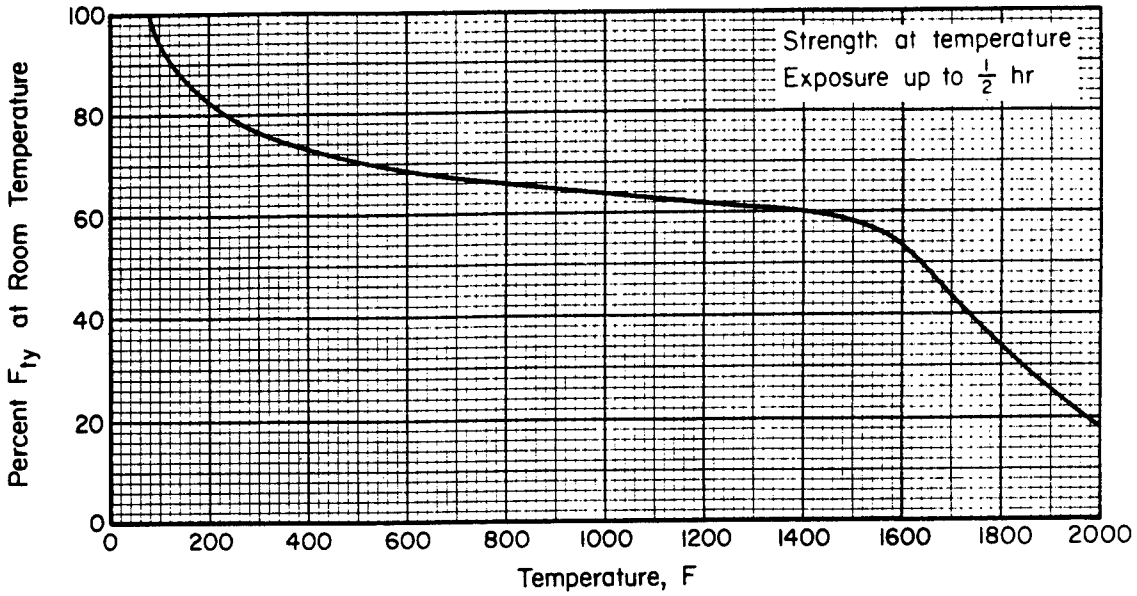


FIGURE 6.4.2.1.1(b). *Effect of temperature on tensile yield strength (F_{ty}) of Alloy 188 sheet.*

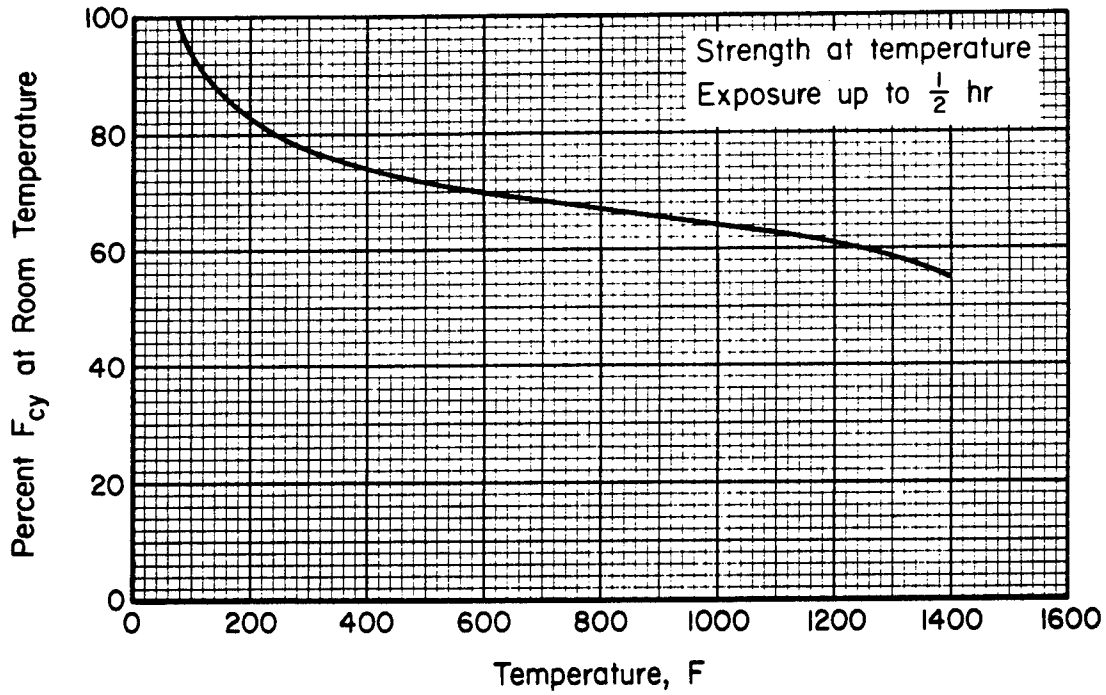


FIGURE 6.4.2.1.2. *Effect of temperature on compressive yield strength (F_{cy}) of Alloy 188 sheet.*

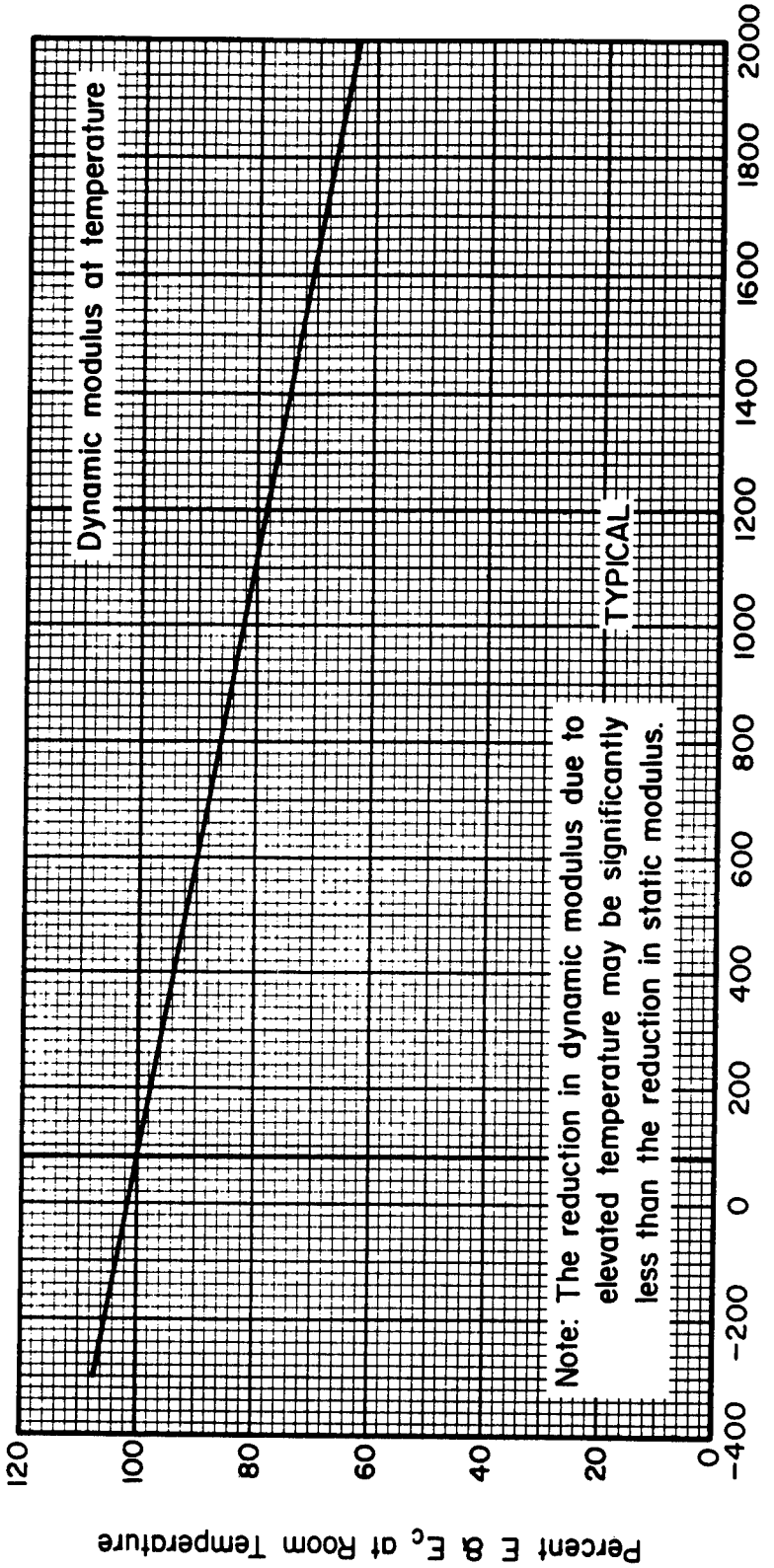


FIGURE 6.4.2.1.4(a). *Effect of temperature on dynamic moduli (E and E_c) of Alloy 188.*

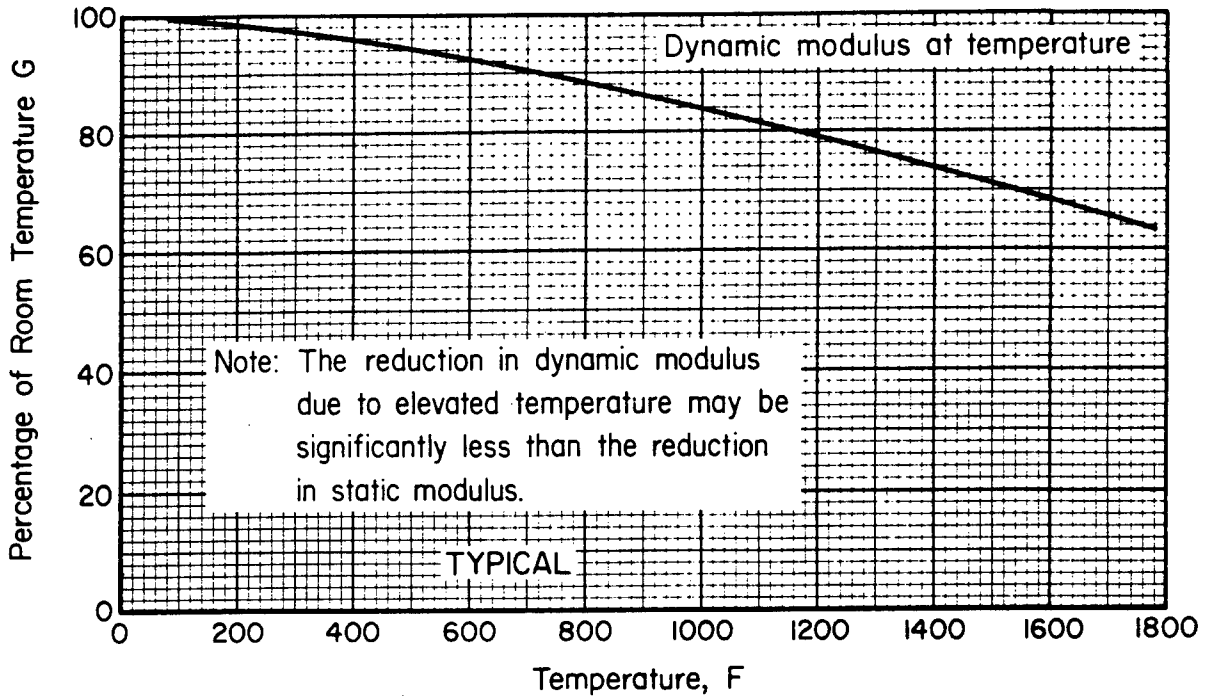


FIGURE 6.4.2.1.4(b). *Effect of temperature on dynamic shear modulus (G) for Alloy 188.*

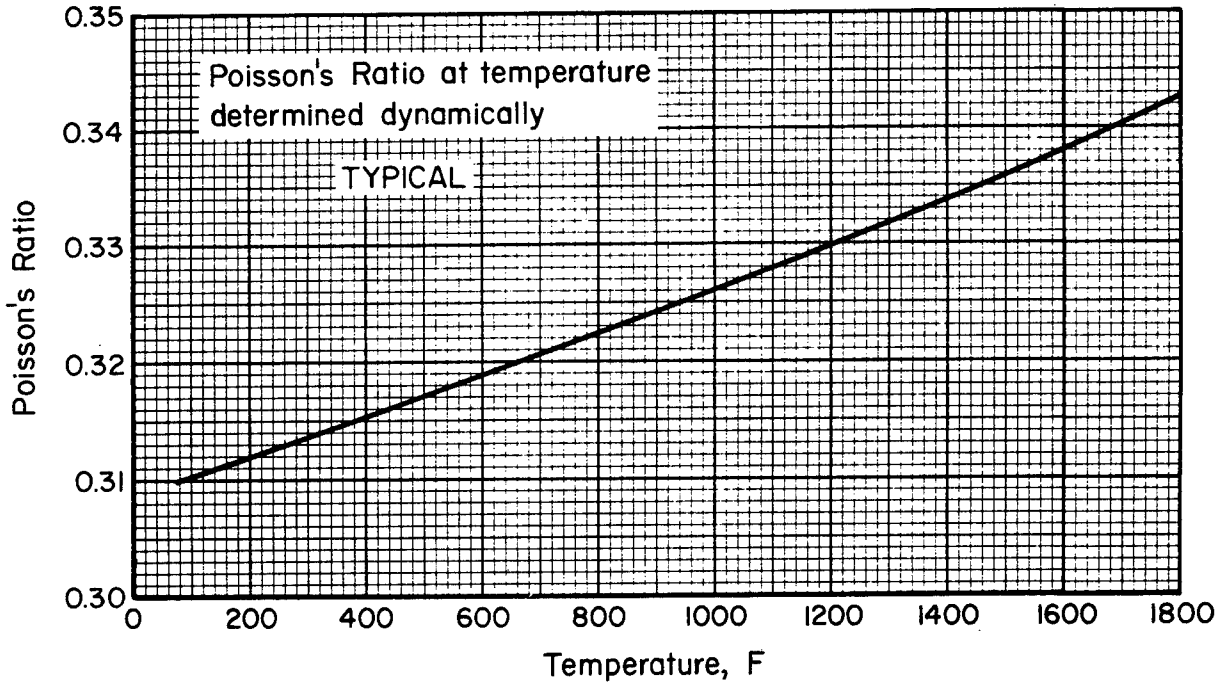


FIGURE 6.4.2.1.4(c). *Effect of temperature on Poisson's ratio (μ) for Alloy 188.*

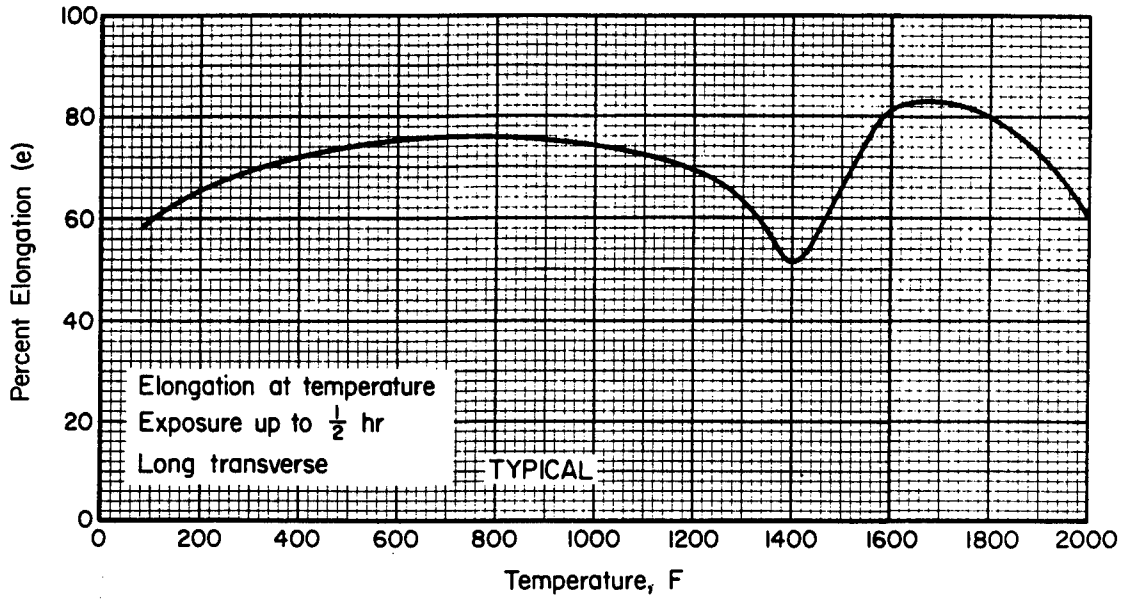


FIGURE 6.4.2.1.5. *Effect of temperature on elongation (e) of Alloy 188 sheet.*

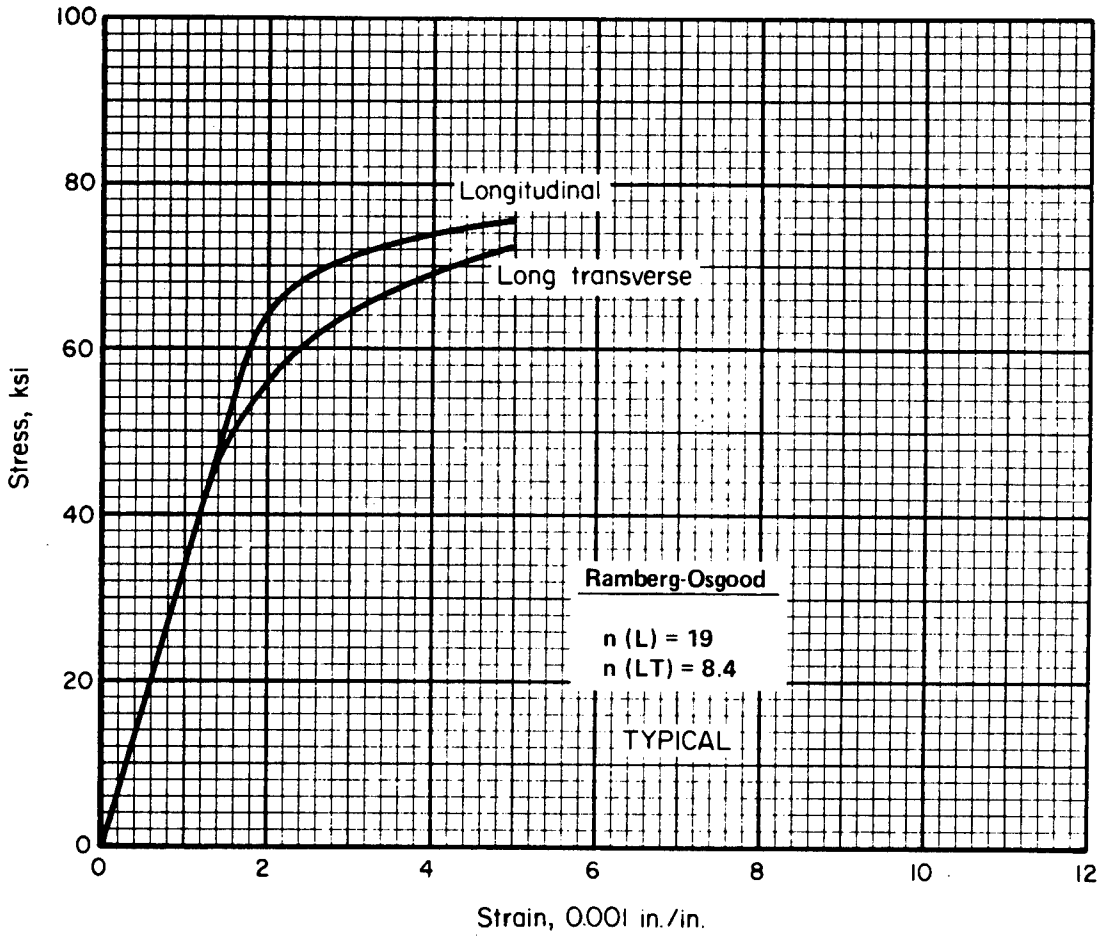


FIGURE 6.4.2.1.6(a). *Typical tensile stress-strain curves for Alloy 188 sheet at room temperature.*

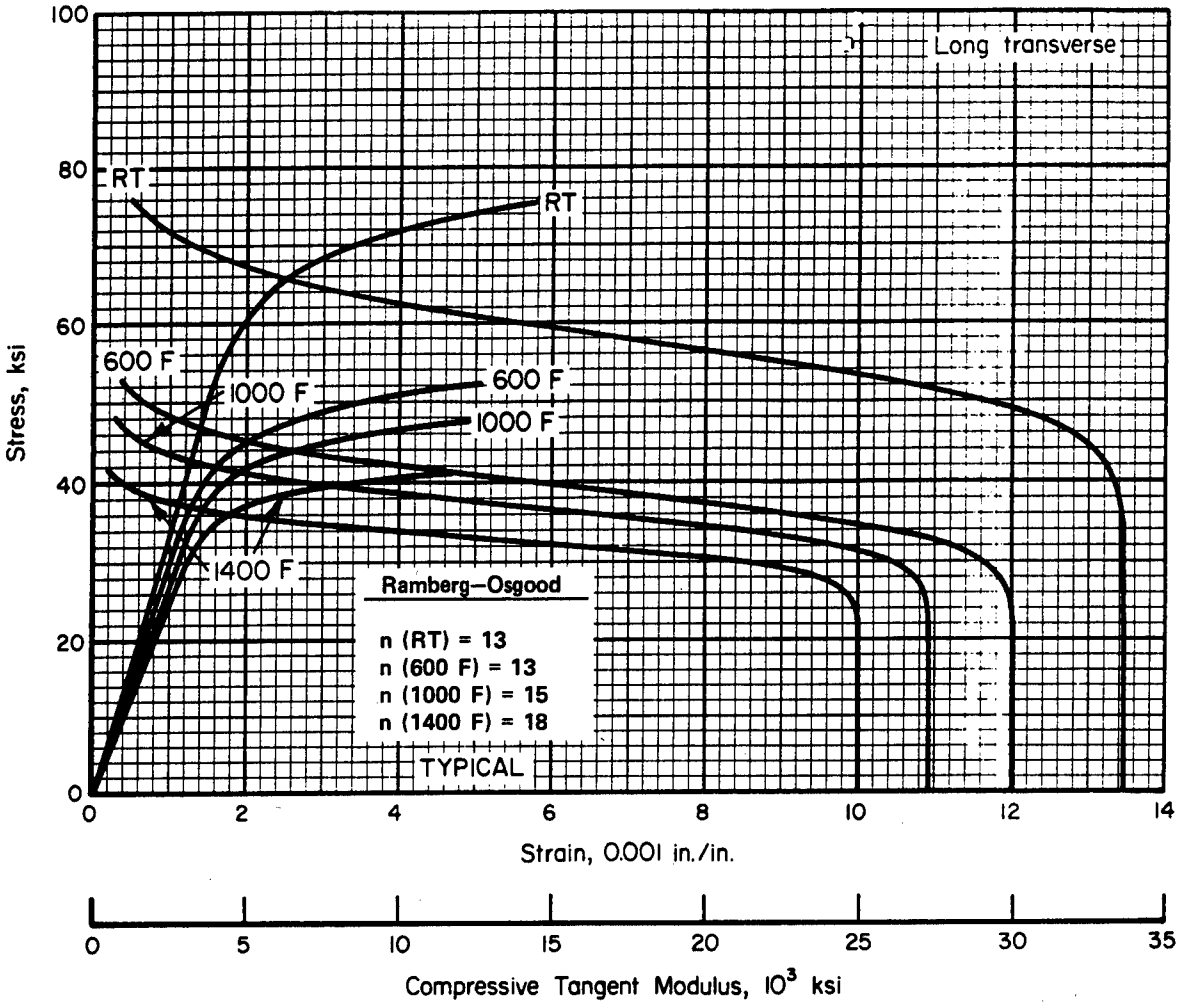


FIGURE 6.4.2.1.6(b). *Typical compressive stress-strain and compressive tangent-modulus curves for Alloy 188 sheet at various temperatures.*

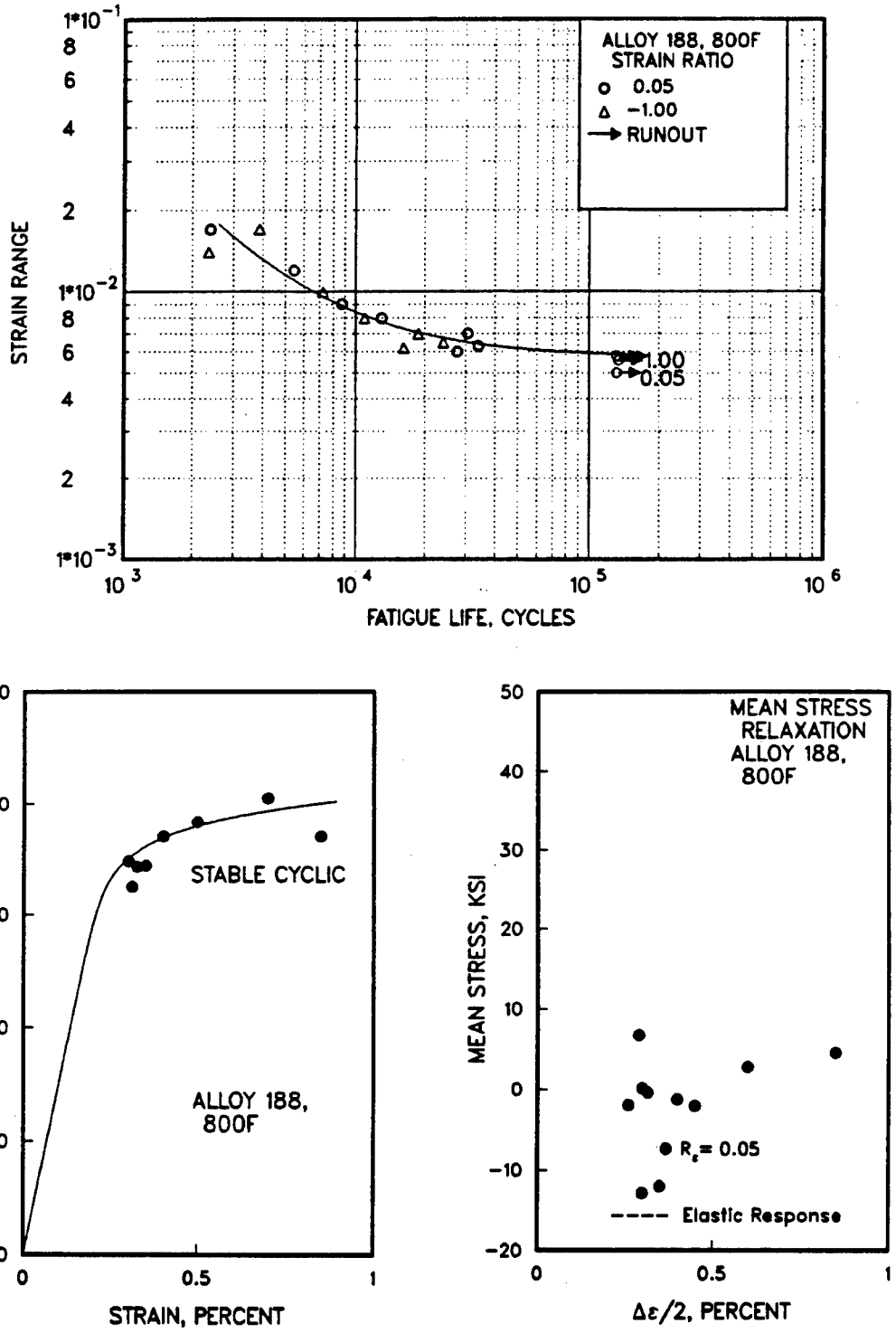


FIGURE 6.4.2.1.8(a). *Best-fit ε/N curve, cyclic stress-strain curve, and mean stress relaxation curve for Alloy 188 bar, longitudinal orientation at 800 F.*

Correlative Information for Figure 6.4.2.1.8(a)

Product Form/Thickness:
Bar/0.5-inch-thick diameter

Thermal Mechanical Processing History:

Solution annealed (AMS 5772)

Properties:	TUS,ksi	TYS, ksi	E, ksi	Temp., F
	102*	55*		75
			29,766	800

Stress-Strain Equations:

Cyclic (Companion Specimens)
Proportional Limit = 60 ksi

$(\Delta\sigma/2) = 109\ (\Delta\varepsilon_p/2)^{0.06}$
Mean Stress Relaxation

Inadequate data at low strain range values

Specimen Details:
Uniform gage test section
0.250-inch diameter

Reference: 3.8.1.1.8

Test Parameters:

Strain Rate/Frequency - 20 cpm
Wave Form - Triangular
Temperature - 800 F
Atmosphere - Air

No. of Heat/Lots: 2

Equivalent Strain Equation:

$\text{Log } N_f = 1.678 - 0.905 \log(\Delta\varepsilon\text{-}0.00572)$

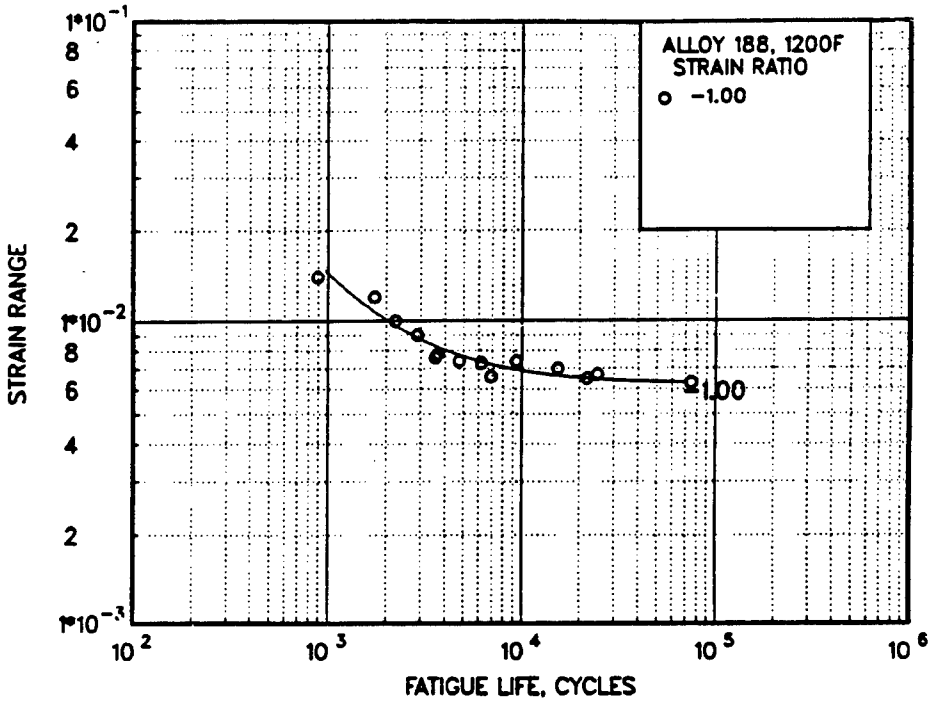
Standard Deviation of log(Life) = $0.00176\ (1/\varepsilon_{eq})$

Adjusted R^2 Statistic = 82%

Sample Size = 18

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

*Minimum values from AMS 5772.



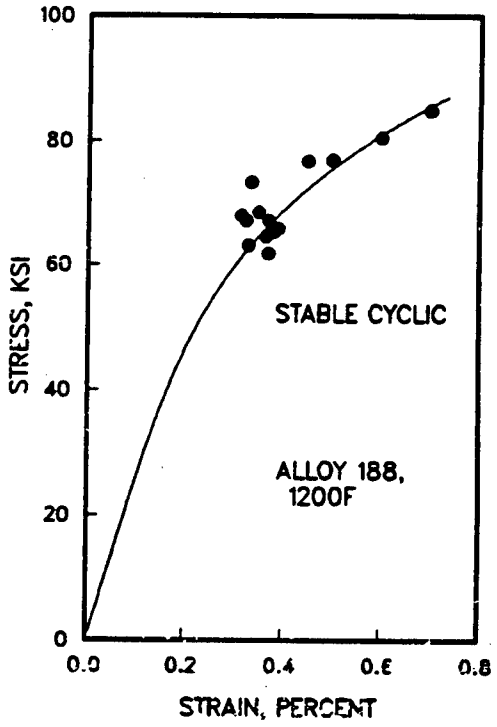


FIGURE 6.4.2.1.8(b). *Best-fit ε/N curve and cyclic stress-strain curve for Alloy 188 bar, longitudinal orientation at 1200 F.*

Correlative Information for Figure 6.4.2.1.8(b)

Product Form/Thickness:
Bar/1.5-inch-thick

Thermal Mechanical Processing History:

Solution annealed (AMS 5772)

Properties:	TUS,ksi	TYS, ksi	E, ksi	Temp., F
	120*	55*		75
			20,050	1200

Stress-Strain Equations:

Cyclic (Companion Specimens)
Proportional Limit = 45 ksi

$(\Delta\sigma/2) = 293\ (\Delta\varepsilon_p/2)^{0.22}$

Specimen Details:
Uniform gage test section
0.250-inch diameter

Reference: 3.8.1.1.8

Test Parameters:

Strain Rate/Frequency - 20 cpm
Wave Form - Triangular
Temperature - 1200 F
Atmosphere - Air

No. of Heat/Lots: 1

Equivalent Strain Equation:

$\text{Log } N_f = 1.073 - 0.925 \log(\Delta\varepsilon - 0.00622)$

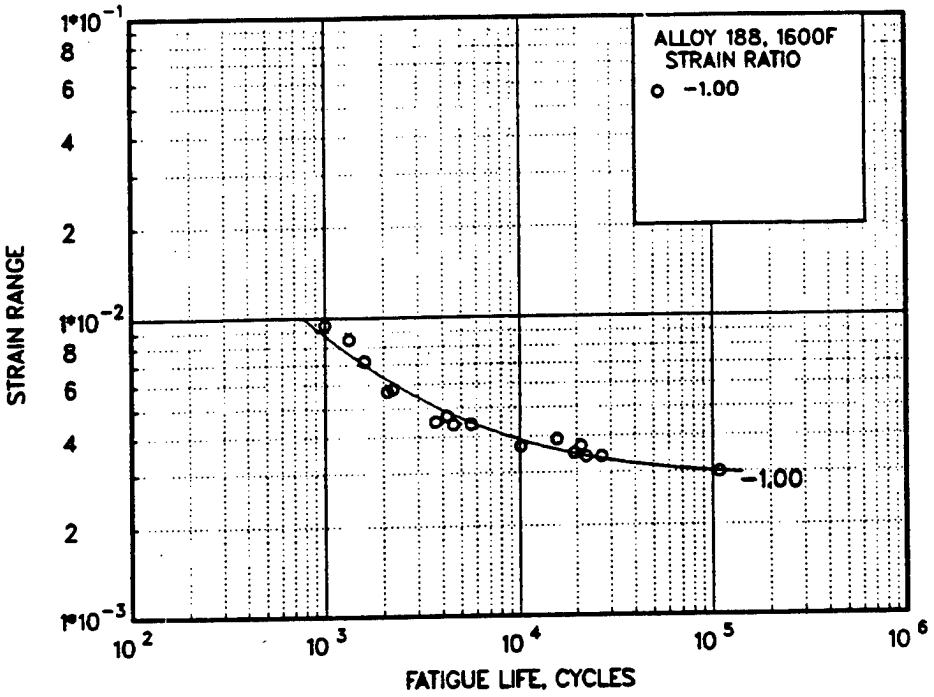
Standard Deviation of log(Life) = $0.00134\ (1/\varepsilon_{eq})$

Adjusted R^2 Statistic = 91%

Sample Size = 14

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

*Minimum values from AMS 5772.



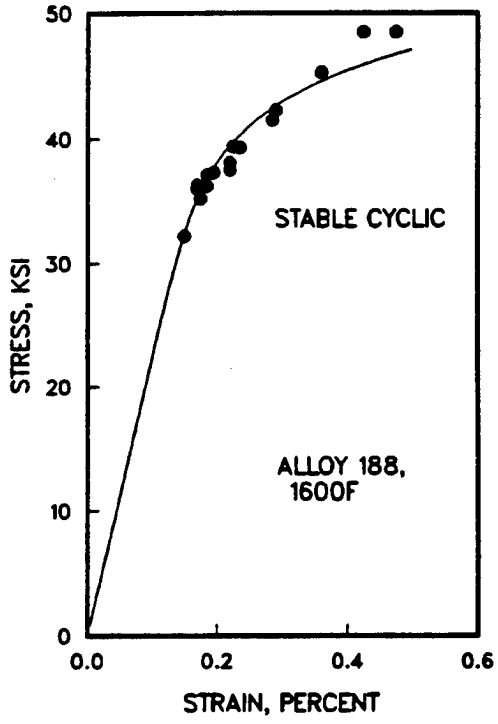


FIGURE 6.4.2.1.8(c). *Best-fit ε/N curve and cyclic stress-strain curve for Alloy 188 bar, longitudinal orientation at 1600 F.*

Correlative Information for Figure 6.4.2.1.8(c)

Product Form/Thickness:
Bar/1.5-inch-thick

Thermal Mechanical Processing History:

Solution treated, water quenched (AMS 5772)

Properties:	TUS, ksi	TYS, ksi	E, ksi	Temp., F
	120*	55*		75
			22,406	1600

Stress-Strain Equations:

Cyclic (Companion Specimens)
Proportional Limit = 36 ksi

$(\Delta\sigma/2) = 81.6\ (\Delta\varepsilon_p/2)^{0.094}$

Specimen Details:
Uniform gage test section
0.250-inch diameter

Reference: 3.8.1.1.8

Test Parameters:

Strain Rate/Frequency - 20 cpm
Wave Form - Triangular
Temperature - 1600 F
Atmosphere - Air

No. of Heat/Lots: 1

Equivalent Strain Equation:

$\text{Log } N_f = 0.011 - 1.343 \log(\Delta\varepsilon - 0.00283)$

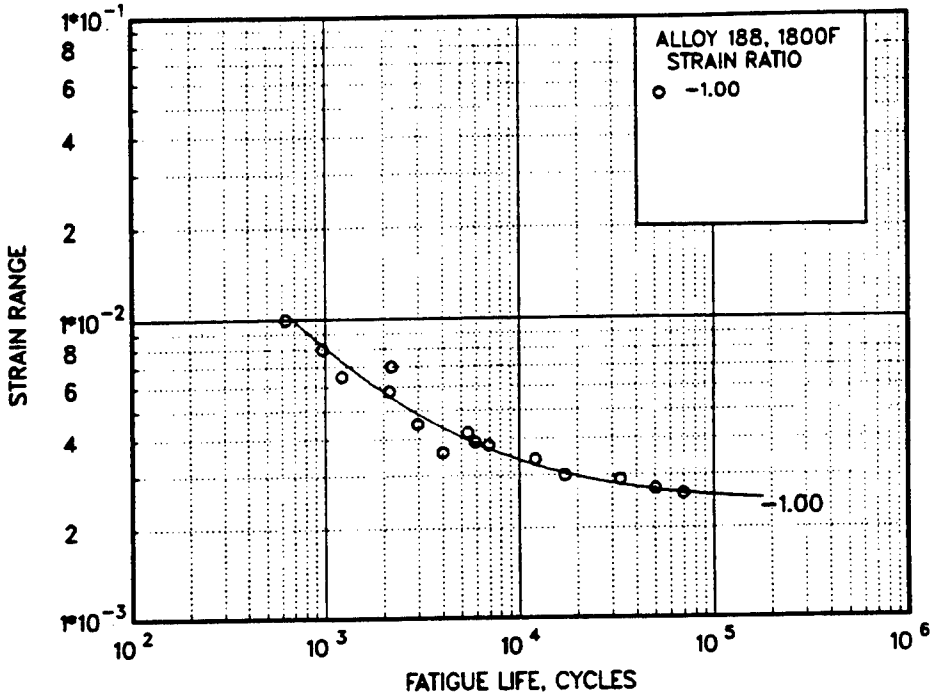
Standard Deviation of log(Life) = 0.116

Adjusted R^2 Statistic = 96%

Sample Size = 16

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

*Minimum values from AMS 5772.



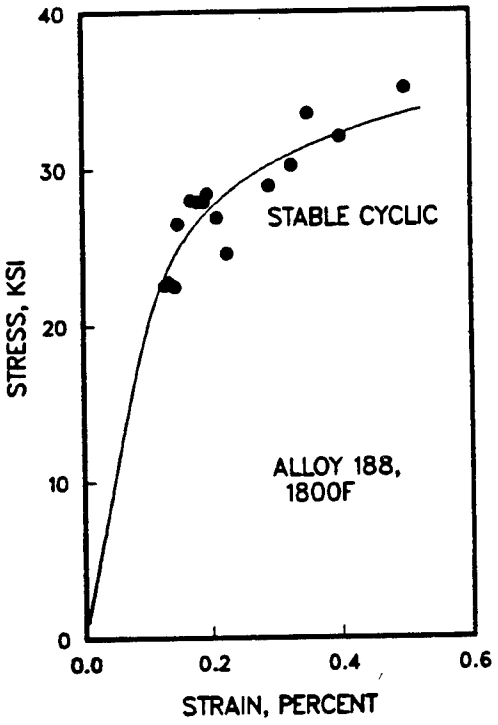


FIGURE 6.4.2.1.8(d). *Best-fit ε/N curve and cyclic stress-strain curve for Alloy 188 bar, longitudinal orientation at 1800 F.*

Correlative Information for Figure 6.4.2.1.8(d)

Product Form/Thickness:
Bar/1.5-inch-thick

Thermal Mechanical Processing History:

Solution treated, water quenched (AMS 5772)

Properties:	TUS,ksi	TYS, ksi	E, ksi	Temp., F
	120*	55*		75
			20,353	1800

Stress-Strain Equations:

Cyclic (Companion Specimens)
Proportional Limit = 23 ksi

$(\Delta\sigma/2) = 66.3\ (\Delta\varepsilon_p/2)^{0.12}$

Specimen Details:
Uniform gage test section
0.250-inch diameter

Reference: 3.8.1.1.8

Test Parameters:

Strain Rate/Frequency - 20 cpm
Wave Form - Triangular
Temperature - 1800 F
Atmosphere - Air

No. of Heat/Lots: 1

Equivalent Strain Equation:

$\text{Log } N_f = 0.047 - 1.317 \log(\Delta\varepsilon - 0.00239)$

Standard Deviation in log(Life) = 0.0126

Adjusted R^2 Statistic = 96%

Sample Size = 15

[Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios beyond those represented above.]

*Minimum values from AMS 5772.

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6.2.1.1.8 Blatherwick, A. A. and Cers, A., "Fatigue, Creep and Stress-Rupture Properties of Nicrotung, Super A-286, and Inconel 718", AFML-TR-65-4447 (June 1966) (MCIC 65927).

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6.3.3.1.8(b) Deel, O. L., and Mindlin, H., "Engineering Data on New Aerospace Structural Materials", AFML-TR-71-249, Battelle (December 1971) (MIL-HDBK-5 Source M-465).

6.3.5.1.8(a) Ruff, P. E., "Effect of Manufacturing Processes on Structural Allowables—Phase I," AFWAL-TR-85-4128, Battelle (January 1986) (MIL-HDBK-5 Source M-654).

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6.3.5.1.9(b) Mills, W. J. and James, L. A., "Effect of Heat-Treatment on Elevated Temperature Fatigue-Crack Growth Behavior of Two Heats of Alloy 718", ASME Paper 78-WA-PVP-3 (December 1978).

6.3.5.1.9(c) James, L. A., "Investigation of Potential Product Form Effects Upon the Fatigue-Crack Growth Behavior of Alloy 718", Mechanical Properties Test Data for Structural Materials, Semiannual Progress Report for Period Ending July 31, 1979, Report ORNL/BRP-79/5, pp. 5.1-5.4, Oak Ridge National Laboratory (October 1979).

6.3.5.1.9(d) James, L. A., "The Effect of Product Form Upon Fatigue-Crack Growth Behavior in Alloy 718", Report HEDL-TME-80-11, Hanford Engineering Development Laboratory (March 1980).

6.3.5.1.9(e) James, L. A. and Mills, W. J., "Effect of Heat-Treatment and Heat-to-Heat Variations in the Fatigue-Crack Growth Response of Alloy 718—Phase I: Macroscopic Variation", Report HEDL-TME-80-9, Hanford Engineering Development Laboratory (March 1980).

6.3.5.1.9(f) James, L. A., "Fatigue-Crack Propagation Behavior of Inconel 718", Report HEDL-TME-75-80, Hanford Engineering Development Laboratory (September 1975).

6.3.5.1.9(g) James, L. A., "Heat-to-Heat and/or Melt Practice Variations in Crack Growth Behavior of Alloy 718", Mechanical Properties Test Data for Structural Materials, Quarterly Progress Report for Period Ending January 31, 1978, Report ORNL-5380, pp. 153-160, Oak Ridge National Laboratory (March 1978).

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Chapter 7

MISCELLANEOUS ALLOYS AND HYBRID MATERIALS

7.1 General

This chapter contains the engineering properties and related characteristics of miscellaneous alloys and hybrid materials. In addition to the usual properties, some characteristics relating to the special uses of these alloys are described. For example, the electrical conductivity is reported for the bronzes and information is included on toxicity of particles of beryllium and its compounds, such as beryllium oxide.

The organization of this chapter is in sections by base metal and subdivided as shown in Table 7.1.

TABLE 7.1. *Miscellaneous Alloys Index*

Section	Designation
7.2	**Beryllium**
7.2.1	Standard Grade Beryllium
7.3	**Copper and Copper Alloys**
7.3.1	Manganese Bronzes
7.3.2	Copper Beryllium
7.4	**Multiphase Alloys**
7.4.1	MP35N Alloy
7.4.2	MP159 Alloy
7.5	**Aluminum Alloy Sheet Laminates**
7.5.1	2024-T3 Aramid Fiber Reinforced Sheet Laminate
7.5.2	7475-T761 Aramid Fiber Reinforced Sheet Laminate

7.2 Beryllium

7.2.0 GENERAL

This section contains the engineering properties and related characteristics of beryllium used in aerospace structural applications. Beryllium is a lightweight, high modulus, moderate temperature metal which is used for specific aerospace applications. Structural designs utilizing beryllium sheet should allow for anisotropy, particularly the very low short transverse properties. Additional information on the fabrication of beryllium may be found in References 7.2.0(a) through (i).

7.2.1 STANDARD GRADE BERYLLIUM

7.2.1.0 *Comments and Properties.*—Standard grade beryllium bars, rods, tubing, and machined shapes are produced from vacuum hot-pressed powder with 1½ percent maximum beryllium oxide content. These products are also available in numerous other compositions for special purposes but are not covered in this document. Sheet and plate are fabricated from vacuum hot-pressed powder with 2 percent maximum beryllium oxide content.

7.2.1.1 *Manufacturing Considerations.*—

Hot Shaping.—Beryllium hot-pressed block can be forged and rolled but requires temperatures of 700 F and higher because of brittleness. A temperature range of 1000 to 1400 F is recommended. Hot shaping procedures are given in more detail in Reference 7.2.0(b).

Forming.—Beryllium sheet should be formed at 1300 to 1350 F, holding at temperature no more than 1.5 hours, for minimum springback. Forming above 1450 F will result in a reduction in strength.

Machining.—Carbide tools are most often used in machining beryllium. Mechanical metal removal techniques generally cause microcracks and metallographic twins. Finishing cuts are usually 0.002 to 0.005 inch in depth to minimize surface damage. Although most machining operations are performed without coolant, to avoid, as far as possible, contamination of the chips, the use of coolant can reduce, in some cases. The depth of damage and give longer tool life. See Reference 7.2.0(c) for more information. Finish machining should be followed by chemical etching to remove machining damage, normally 0.002-inch minimum, from parts. See References 7.2.0(h) and (i). A combination of 1350 F stress relief followed by an 0.0005-inch etch may be necessary

for close tolerance parts. Damage-free metal removal techniques include chemical milling and electrochemical machining. The drilling of sheet may lead to delamination and breakout unless the drillhead is of the controlled torque type and the drills are carbide burr type.

Joining.—Parts may be joined mechanically by riveting, but only by squeeze riveting to avoid damage to the beryllium, by bolting, threading, or by press fitting specifically designed to avoid damage. Parts also may be joined by brazing, soldering, braze welding, adhesive bonding, and diffusion bonding. Fusion welding is not recommended. Brazing may be accomplished with zinc, aluminum-silicon, or silver-base filler metals. Many elements, including copper, may cause embrittlement when used as brazing filler metals. However, specific manufacturing techniques have been developed by various beryllium fabricators to use many of the common braze materials. For each method of joining specific detailed procedures must be followed, Reference 7.2.0(f).

Surface Treatment.—A surface treatment such as chemical etching to remove the machined surface of metal is recommended to ensure the specified properties. All design allowables herein represent material so treated. This surface treatment is especially important when beryllium is to be mechanically joined. References 7.2.0(d), (h), and (i) contain information on etching solutions and procedures.

Toxicity Hazard.—Particles of beryllium and its compounds, such as beryllium oxide, are toxic, so special precautions to prevent inhalation must be taken. References 7.2.1.1(a) through (e) outline the hazard and methods to control it.

Specifications and Properties.—Material specifications for standard grade beryllium are presented in Table 7.2.1.0(a).

TABLE 7.2.1.0(a). *Material Specifications for Standard Grade Beryllium*

Specification	Form
AMS 7906	Bar, rod, tubing, and mechanical shapes
AMS 7902	Sheet and plate

Room-temperature mechanical and physical properties are shown in Tables 7.2.1.0(b) and (c). Notch tensile test data are available in Reference 7.2.1.1(g). The effect of temperature on physical properties is shown in Figure 7.2.1.0.

7.2.1.1 *Hot-Pressed Condition.*—The effect of temperature on the mechanical properties of hot-pressed beryllium is presented in Figures 7.2.1.1.1 and 7.2.1.1.4.

TABLE 7.2.1.0(b). *Design Mechanical and Physical Properties of Beryllium Bar, Rod, Tubing, and Mechanical Shapes*

Specification	AMS 7906
Form	Bar, rod, tubing, and machined shapes
Condition	Hot pressed (ground and etched)
Thickness or diameter, in.	...
Basis	S
Mechanical Properties:	
F_{tu}, ksi:	
L	47
LT	47
F_{ty}, ksi:	
L	35
LT	35
F_{cy}, ksi:	
L	...
LT	...
F_{su}, ksi	...
F_{bru}, ksi:	
(e/D = 1.5)	...
(e/D = 2.0)	...
F_{bry}, ksi:	
(e/D = 1.5)	...
(e/D = 2.0)	...
e, percent:	
L	2
LT	2
E, 10^3 ksi	42
E_c, 10^3 ksi	42
G, 10^3 ksi	20
μ	0.10
Physical Properties:	
ω, lb/in.^{3}	0.067
C, *K*, and α	See Figure 7.2.1.0

TABLE 7.2.1.0(c). *Design Mechanical and Physical Properties of Beryllium Sheet and Plate*

Specification	AMS 7902			
Form	Sheet	Plate		
Condition	Stress relieved (ground and etched)			
Thickness or diameter, in.	0.020-0.250	0.251-0.450	0.451-0.600	≥0.601
Basis	S	S	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	70	65	60	40
LT	70	65	60	40
F_{ty}, ksi:				
L	50	45	40	30
LT	50	45	40	30
F_{cy}, ksi:				
L	...	...	...	...
LT	...	...	...	...
F_{su}, ksi	...	...	...	...
F_{bru}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
F_{bry}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
e, percent:				
L	10	4	3	1
LT	10	4	3	1
E, 10^3 ksi	42.5			
E_c, 10^3 ksi	42.5			
G, 10^3 ksi	20.0			
μ	0.10 (L and LT)			
Physical Properties:				
ω, lb/in.^{3}	0.067			
C, K, and α	See Figure 7.2.1.0			

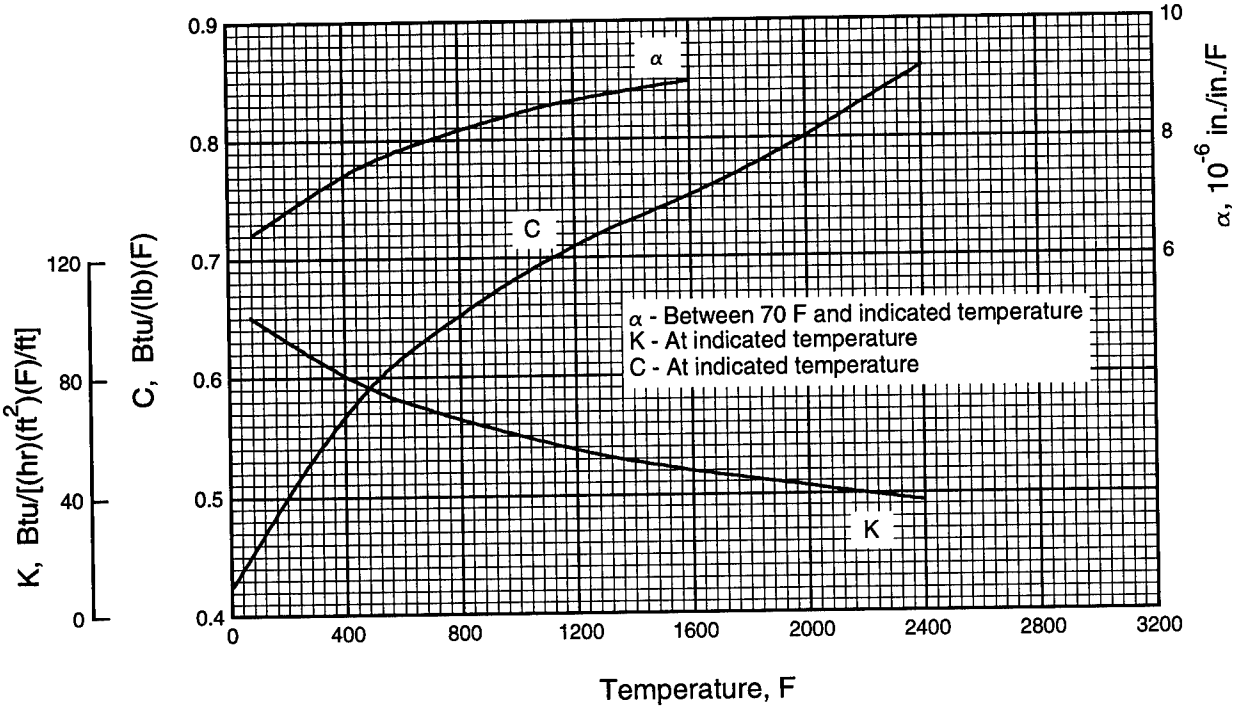


FIGURE 7.2.1.0. *Effect of temperature on the physical properties of beryllium (2% maximum BeO).*

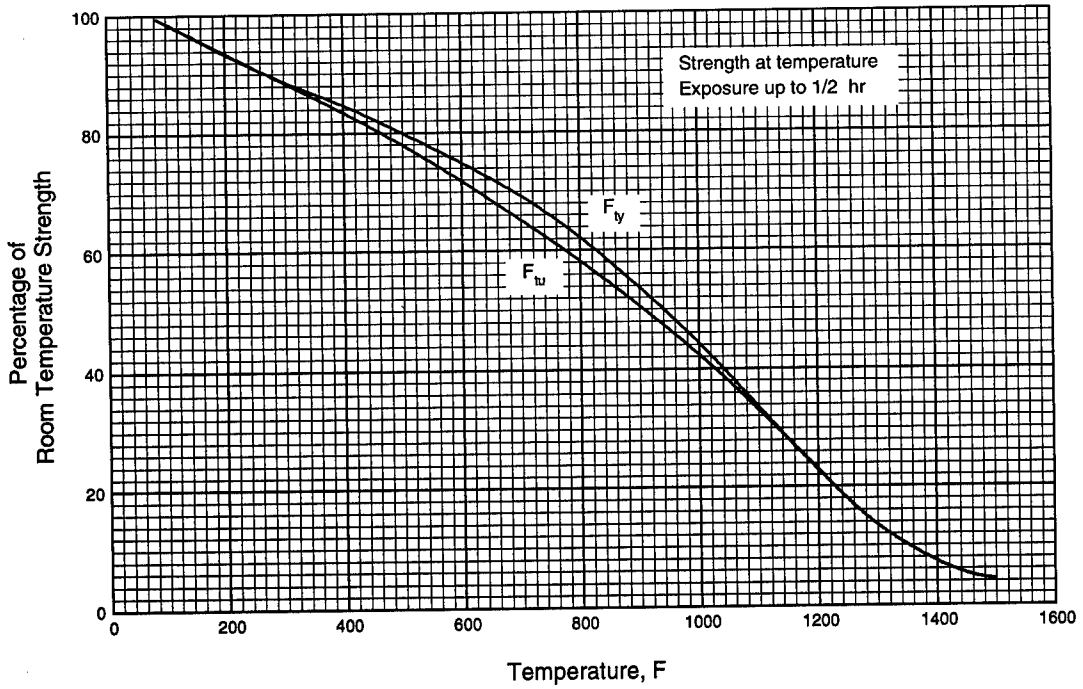


FIGURE 7.2.1.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and tensile yield strength (F_{ty}) of hot-pressed beryllium bar, rod, tubing, and machined shapes.*

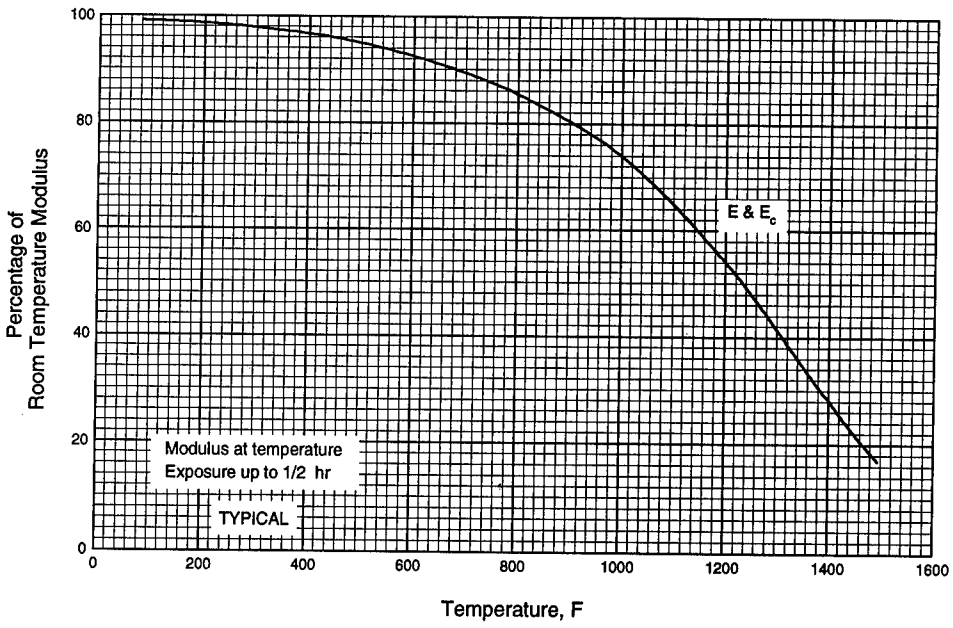


FIGURE 7.2.1.1.4. *Effect of temperature on the tensile and compressive moduli (E and E_c) of hot-pressed beryllium bar, rod, tubing, and machined shapes.*

7.3 Copper and Copper Alloys

7.3.0 GENERAL

The properties of major significance in designing with copper and copper alloys are electrical and thermal conductivity, corrosion resistance, and good bearing qualities (antigalling). Copper and copper alloys are non-magnetic and can be readily joined by welding, brazing and soldering. The use of copper alloys is usually predicated upon two or more of the above properties plus the ease of casting and hot and cold working into desirable shapes.

The thermally unstable range for copper and copper alloys generally begins somewhat above room temperature (150 F). Creep, stress relaxation and diminishing stress rupture strength are factors of concern above 150 F. Copper alloys frequently are used at temperatures up to 480 F. The range between 480 and 750 F is considered very high for copper alloys, since copper and many of its alloys begin to oxidize slightly above 350 F and protection may be required. Bronzes containing Al, Si, and Be oxidize to a lesser extent than the red copper alloys. Precipitation hardened alloys such as copper beryllium retain strength up to their aging temperatures of 500 to 750 F.

Copper alloys used for bearing and wear resistance applications include, in the order of their increasing strength and load-carrying capacity, copper-tin-lead, copper-tin, silicon bronze, manganese bronze, aluminum bronze, and copper beryllium. Copper beryllium and manganese bronzes are included in MIL-HDBK-5.

Copper-base bearing alloys are readily cast by a number of techniques: statically sand cast, centrifugally cast into tubular shapes, and continuously cast into various shapes. Tin bronze, sometimes called phosphor bronze because phosphorous is used to deoxidize the melt and improve castability, is a low strength alloy. It is generally supplied as a static (sand) casting or centrifugal casting (tubular shapes from rotating graphite molds). Manganese bronze is considerably stronger than tin bronze, is easily cast in the foundry, has good toughness and is not heat treated. Aluminum bronze alloys, especially those with nickel, silicon, and manganese over 2 percent, respond to heat treatment, resulting in greater strength, and higher galling and fatigue limits than manganese bronze. Aluminum bronze is used in the static and centrifugal cast form or parts may be machined from wrought rod and bar stock. Copper beryllium is the highest strength copper-base bearing material, due to its response to precipitation hardening. Copper beryllium is also available in static and centrifugal cast form but is generally used as wrought shapes, such as extrusions, forgings, and mill shapes.

Copper beryllium, because of its high strength, is also useful as a spring material. In this application its high elastic limit, high fatigue strength as well as good electrical conductivity are significant. Copper beryllium resists softening up to 500 F, which is higher than other common copper alloys. Copper beryllium springs are usually fabricated from strip or wire. Consult References 7.3.0(a) through (c) for more information.

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7.3.1 MANGANESE BRONZES

7.3.1.0 *Comments and Properties.*—The manganese bronzes are also known as the high strength yellow brasses and leaded high-strength yellow brasses. These alloys contain zinc as the principal alloying element with smaller amounts of iron, aluminum, manganese, nickel, and lead present. These bronzes are easily cast.

Some material specifications for manganese bronzes are presented in Table 7.3.1.0(a). A cross index to CDA and former QQ-C-390 designations is presented in Table 7.3.1.0(b). Room-temperature mechanical properties are shown in Tables 7.3.1.0(c) and (d).

TABLE 7.3.1.0(a). *Material Specifications for Manganese Bronzes*

Specification	Form
AMS 4860	Casting
AMS 4862	Casting

TABLE 7.3.1.0(b). *Cross Index*

Copper Alloy UNS No.	CDA Alloy No.	Former QQ-C-390 Alloy No.
C86300	863	C7
C86500	865	C3

TABLE 7.3.1.0(c). *Design Mechanical and Physical Properties of C86500 Manganese Bronze*

Specification	AMS 4860
Form	Sand and centrifugal casting
Condition	As cast
Location within casting	Any area
Basis	S
Mechanical Properties:	
F_{tu}, ksi	65[a]
F_{ty}, ksi	25[a]
F_{cy}, ksi	...
F_{su}, ksi	...
F_{bru}, ksi:	
(e/D = 1.5)	...
(e/D = 2.0)	...
F_{bry}, ksi:	
(e/D = 1.5)	...
(e/D = 2.0)	...
e, percent	20[a]
E, 10^3 ksi	15.0
E_c, 10^3, ksi	...
G, 10^3, ksi	...
μ	...
Physical Properties:	
ω, lb/in.^{3}	0.301
C, Btu/(lb)(F)	0.09 (at 68 F)
K, Btu/[(hr)(ft^2)(F)/ft]	50 (at 68 F)
α, 10^{-6} in./in/F	11.3 (68 to 212 F)
Electrical conductivity, % IACS	22.0

[a]When specified, conformance to tensile property requirements is determined by testing specimens cut from casting.

TABLE 7.3.1.0(d). *Design Mechanical and Physical Properties of C86300 Manganese Bronze*

Specification	AMS 4862
Form	Sand and centrifugal casting
Condition	As cast
Location within casting	Any area
Basis	S
Mechanical Properties:	
F_{tu}, ksi	110[a]
F_{ty}, ksi	60[a]
F_{cy}, ksi	...
F_{su}, ksi	...
F_{bru}, ksi:	
(e/D = 1.5)	...
(e/D = 2.0)	...
F_{bry}, ksi:	
(e/D = 1.5)	...
(e/D = 2.0)	...
e, percent	12[a]
E, 10^3 ksi	14.2
E_c, 10^3, ksi	...
G, 10^3, ksi	...
μ	...
Physical Properties:	
ω, lb/in.^{3}	0.283
C, Btu/(lb)(F)	0.09 (at 68 F)
K, Btu/[(hr)(ft^2)(F)/ft]	20.5 (at 68 F)
α, 10^{-6} in./in/F	12.0 (68 to 500 F)
Electrical conductivity, % IACS	8.0

[a]When specified, conformance to tensile property requirements is determined by testing specimens cut from casting.

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7.3.2 COPPER BERYLLIUM

7.3.2.0 *Comments and Properties.*—Copper beryllium refers to a family of copper-base alloys containing beryllium and cobalt or nickel which cause the alloys to be precipitation hardenable. Data for only one high-strength alloy, designated C17200, which contains 1.90 percent (nominal) beryllium, are presented in this section. This alloy is suitable for parts requiring high strength, good wear, and corrosion resistance. Alloy C17200 is available in the form of rod, bar, shapes, mechanical tubing, strip, and casting.

Manufacturing Considerations.—Rod and bar are available in the solution-treated (TB00) (AMS 4650) or solution-treated plus cold worked (TD04) (AMS 4651) condition. After fabrication operations, the material may be strengthened by precipitation heat treatment (aging). Rod and bar are also available from the mill in the TF00 (AMS 4533) and TH04 (AMS 4534) conditions. Mechanical tubing is available from the mill in TF00 condition (AMS 4535). Machining operations on rod, bar, and tubing are usually performed on material in the TF00 or TH04 conditions. This eliminates the volumetric shrinkage of 0.02 percent, which occurs during precipitation hardening, as a factor in maintaining final dimensional tolerances. This material has good machinability in all conditions.

Strip is also available in the heat treatable condition. Parts are stamped or formed in a heat treatable temper and subsequently precipitation heat treated. For strip, the heat treatable tempers are designated TB00 (AMS 4530, ASTM B194), TD01 (ASTM B194), TD02 (AMS 4532, ASTM B194), and TD04 (ASTM B194), indicating a progressively greater amount of cold work by the mill. When parts produced from these tempers are precipitation heat treated by the user, the designations become TF00, TH01, TH02, and TH04, respectively. Strip is also available from the mill for the hardened conditions. Design values for these conditions are not included.

Environmental Considerations.—The copper beryllium alloys have good corrosion resistance and are not susceptible to hydrogen embrittlement. The maximum service temperature for C17200 copper beryllium products is 500 F for up to 100 hours.

Specifications and Properties.—A cross-index to previous and current temper designations for C17200 alloy is presented in Table 7.3.2.0(a).

TABLE 7.3.2.0(a). *Cross-Index to Previous and Current Temper Designations for C17200 Copper Beryllium*

Previous Temper	Current ASTM Temper
A	TB00
AT	TF00
¼H	TD01
¼HT	TH01
½H	TD02
½HT	TH02
H	TD04
HT	TH04

Material specifications for alloy C17200 are presented in Table 7.3.2.0(b). Room-temperature mechanical properties are shown in Tables 7.3.2.0(c) through (g). The effect of temperature on physical properties is depicted in Figure 7.3.2.0.

TABLE 7.3.2.0(b). *Material Specifications for C17200 Copper Beryllium Alloy*

Specification	Form
ASTM B194	Strip (TB00, TD01, TD02, TD04)
AMS 4530	Strip (TB00)
AMS 4532	Strip (TD02)
AMS 4650	Bar, rod, shapes, and forgings (TB00)
AMS 4533	Bar and rod (TF00)
AMS 4535	Mechanical tubing (TF00)
AMS 4651	Bar and rod (TD04)
AMS 4534	Bar and rod (TH04)

The temper index for C17200 alloy is as follows:

Section	Temper
7.3.2.1	TF00
7.3.2.2	TH04

7.3.2.1 *TF00 Temper.*—Typical tensile and compressive stress-strain and tangent modulus curves are presented in Figures 7.3.2.1.6(a) and (b).

7.3.2.2 *TH04 Temper.*—Typical tensile and compressive stress-strain and tangent modulus curves are presented in Figure 7.3.2.2.6.

TABLE 7.3.2.0(c). *Design Mechanical and Physical Properties of Copper Beryllium Strip*

Specification	ASTM B194 AMS 4530	ASTM B194	ASTM B194 AMS 4532	ASTM B194
Form	Strip			
Condition	TF00	TH01	TH02	TH04
Thickness, in.	≤0.188	≤0.188	≤0.188	≤0.188
Basis	S	S	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	165	175	185	190
LT	...	...	...	...
F_{ty}, ksi:				
L	140	150	160	165
LT	...	...	...	...
F_{cy}[a], ksi:				
L	140	150	160	165
LT	140	150	160	165
F_{su}[a], ksi	90	90	92	95
F_{bru}[a], ksi:				
(e/D = 1.5)	214	227	240	247
(e/D = 2.0)	280	297	314	323
F_{bry}[a], ksi:				
(e/D = 1.5)	196	210	224	231
(e/D = 2.0)	210	225	240	247
e, percent:				
L	3	2.5	1	1
E, 10^3 ksi	18.5			
E_c, 10^3 ksi	...			
G, 10^3 ksi	7.3			
μ	0.27			
Physical Properties:				
ω, lb/in.^{3}	0.298			
C, K, and α	See Figure 7.3.2.0 for TF00 temper			

[a]These properties do not represent values derived from tests, but are estimates.

TABLE 7.3.2.0(d). *Design Mechanical and Physical Properties of C17200 Copper Beryllium Rod and Bar*

Specification	AMS 4650 and AMS 4533				
Form	Rod and bar				
Condition	TF00				
Thickness, in.	≤1.500	1.501-2.000	2.001-3.000	3.001-3.500	3.501-4.000
Basis	S	S	S	S	S
Mechanical Properties:					
F_{tu}, ksi:					
L	165	165	165	165	165
ST	...	158	158	158	158
F_{ty}, ksi:					
L	140	140	140	140	140
ST	...	137	137	137	137
F_{cy}, ksi:					
L	150	149	145	143	139
ST	...	142	142	142	142
F_{su}, ksi	...	94	94	94	94
F_{bru}[a], ksi:					
(e/D = 1.5)	226	226	226	226	226
(e/D = 2.0)	290	290	290	290	290
F_{bry}[a], ksi:					
(e/D = 1.5)	200	200	200	200	200
(e/D = 2.0)	225	225	225	225	225
e, percent:					
L	4[b]	4[b]	4[b]	3	3
E, 10^3 ksi	18.5				
E_c, 10^3 ksi	18.7				
G, 10^3 ksi	7.3				
μ	0.27				
Physical Properties:					
ω, lb/in.^{3}	0.298				
C, K, and α	See Figure 7.3.2.0				

[a]Bearing values are "dry pin" values per Section 1.4.7.1.
[b]AMS 4650 specifies e = 3 percent.

TABLE 7.3.2.0(e). *Design Mechanical and Physical Properties of C17200 Copper Beryllium Rod and Bar*

Specification	AMS 4651			
Form	Rod and bar			
Condition	TH04			
Thickness, in.	≤0.375	0.376-1.000	1.001-1.500	1.501-2.000
Basis	S	S	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	185	180	175	175
ST	...	...	...	169
F_{ty}, ksi:				
L	145	145	145	145
ST	...	...	...	140
F_{cy}, ksi:				
L	...	148	148	148
ST	...	...	...	154
F_{su}, ksi	...	89	90	93
F_{bru}[a], ksi:				
(e/D = 1.5)	...	242	235	235
(e/D = 2.0)	...	306	298	298
F_{bry}[a], ksi:				
(e/D = 1.5)	...	207	207	207
(e/D = 2.0)	...	225	225	225
e, percent:				
L	1	1	2	2
E, 10^3 ksi	18.5			
E_c, 10^3 ksi	18.7			
G, 10^3 ksi	7.3			
μ	0.27			
Physical Properties:				
ω, lb/in.^{3}	0.298			
C, K, and α	...			

[a]Bearing values are "dry pin" values per Section 1.4.7.1.

TABLE 7.3.4.0(f). *Design Mechanical and Physical Properties of C17200 Copper Beryllium Rod and Bar*

Specification	AMS 4534											
Form	Rod and bar											
Condition	TH04											
Thickness, in.	≤0.375		0.376-0.999		1.000-1.499		1.500-1.999		2.000-2.499		2.500-3.000	
Basis	A	B	A	B	A	B	A	B	A	B	A	B
Mechanical Properties:												
F_{tu}, ksi:												
L	182	188	180	186	177[a]	184	177	183	175	181	172	178
ST	...	...	...	...	...	...	167	173	168	174	167	173
F_{ty}, ksi:												
L	157	165	154	162	150[a]	162	150	158	147	155	145	152
ST	...	...	...	...	...	...	145	153	142	150	140	147
F_{cy}, ksi:												
L	...	...	157	166	153	164	153	162	150	158	148	155
ST	...	...	...	...	...	...	160	168	156	165	154	162
F_{su}, ksi	...	...	89	92	91	95	94	97	95	98	94	96
F_{bru}[b], ksi:												
(e/D = 1.5)	...	...	242	250	238	247	238	246	235	243	231	239
(e/D = 2.0)	...	...	306	317	302	313	302	312	298	308	293	303
F_{bry}[b], ksi:												
(e/D = 1.5)	...	...	220	231	214	228	214	226	210	221	207	217
(e/D = 2.0)	...	...	239	251	233	248	233	245	228	240	225	236
e, percent (S-basis):												
L	3	...	3	...	3	...	3	...	3	...	3	...
E, 10^3 ksi	18.5											
E_c, 10^3 ksi	18.7											
G, 10^3 ksi	7.3											
μ	0.27											
Physical Properties:												
ω, lb/in.^{3}	0.298											
C, K, and α	...											

[a]S-basis. A values are F_{tu}(L) = 178 ksi and F_{ty} = 152 ksi.
[b]Bearing values are "dry pin" values per Section 1.4.7.1.

TABLE 7.3.2.0(g). *Design Mechanical and Physical Properties of C17200 Copper Beryllium Mechanical Tubing*

Specification	AMS 4535			
Form	Mechanical tubing			
Condition	TF00			
Outside Diameter, in.	≤2.499		2.500-12.000	
Wall Thickness, in.	≤0.749		0.750-2.000	
Basis	A	B	A	B
Mechanical Properties:				
F_{tu}, ksi:				
L	161	167	161	167
LT	...	...	157	163
F_{ty}, ksi:				
L	126	136	126	136
LT	...	...	124	134
F_{cy}, ksi:				
L	134	145	134	145
LT	...	...	135	146
F_{su}, ksi	92	95	92	95
F_{bru}[a], ksi:				
(e/D = 1.5)	228	237	228	237
(e/D = 2.0)	287	298	287	298
F_{bry}[a], ksi:				
(e/D = 1.5)	183	197	183	197
(e/D = 2.0)	206	222	206	222
e, percent (S-basis):				
L	3	...	3	...
E, 10^3 ksi	18.5			
E_c, 10^3 ksi	18.7			
G, 10^3 ksi	7.3			
μ	0.27			
Physical Properties:				
ω, lb/in.^{3}	0.298			
C, Btu/(lb)(F)	See Figure 7.3.4.0			

[a]Bearing values are "dry pin" values per Section 1.4.7.1.

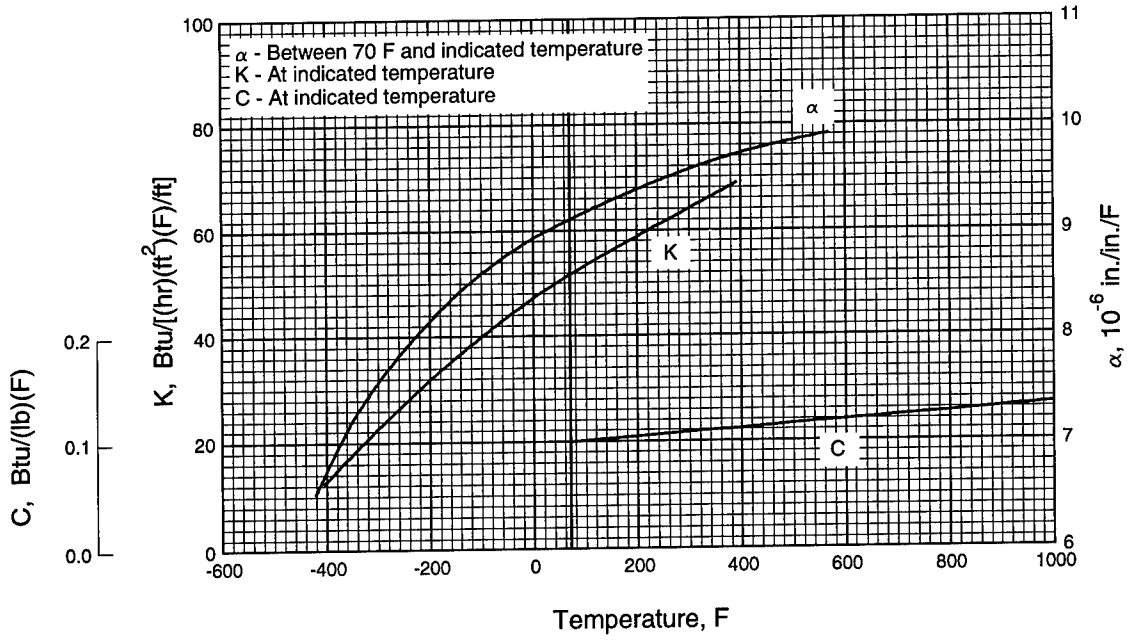


FIGURE 7.3.2.0. *Effect of temperature on the physical properties of copper beryllium (TF00).*

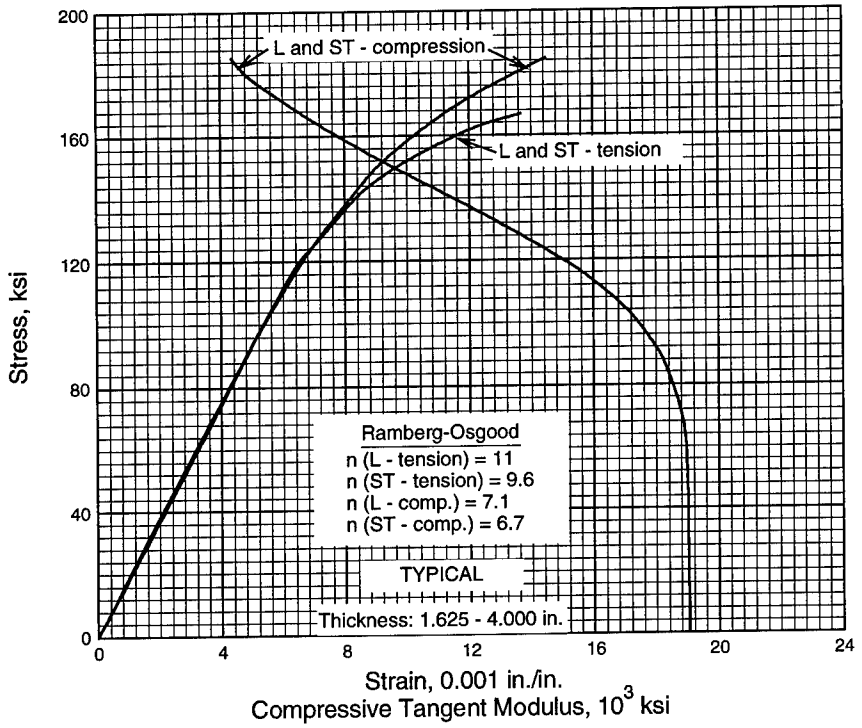


FIGURE 7.3.2.1.6(a). *Typical tensile and compressive stress-strain and compressive tangent-modulus curves for C17200 copper beryllium bar and rod in TF00 temper.*

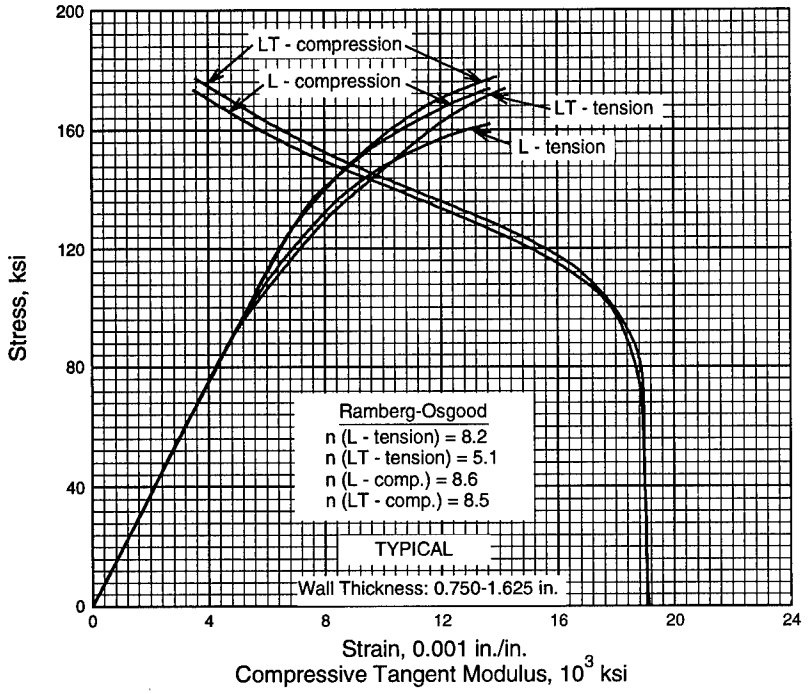


FIGURE 7.3.2.1.6(b). *Typical tensile and compressive stress-strain and compressive tangent-modulus curves for C17200 copper beryllium mechanical tubing in TF00 temper.*

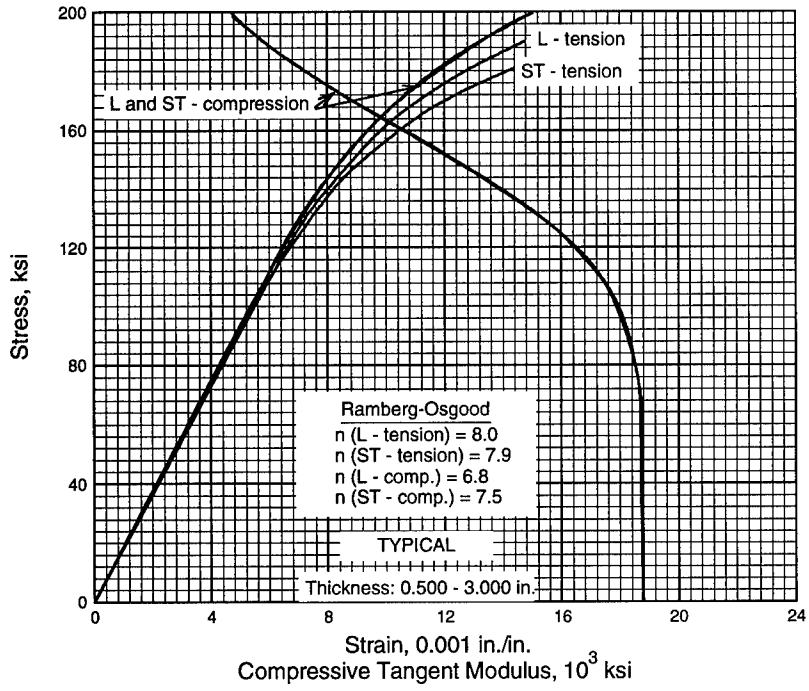


FIGURE 7.3.2.2.6. *Typical tensile and compressive stress-strain and compressive tangent-modulus curves for C17200 copper beryllium bar and rod in TH04 temper.*

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7.4 Multiphase Alloys

7.4.0 GENERAL

This section contains the engineering properties of the "Multiphase" alloys. These alloys, based on the quaternary of cobalt, nickel, chromium, and molybdenum, can be work-strengthened and aged to ultrahigh strengths with good ductility and corrosion resistance.

7.4.1 MP35N ALLOY

7.4.1.0 *Comments and Properties.*—MP35N is a vacuum induction, vacuum arc remelted alloy which can be work-strengthened and aged to ultrahigh strengths. This alloy is suitable for parts requiring ultrahigh strength, good ductility and excellent corrosion and oxidation resistance up to 700 F.

Manufacturing Considerations.—The work hardening characteristics of MP35N are similar to 304 stainless steel. Drawing, swaging, rolling, and shear forming are excellent deforming methods for work strengthening the alloy. The machinability of MP35N is similar to the nickel-base alloys.

Environmental Considerations.—MP35N has excellent corrosion, crevice corrosion and stress corrosion resistance in seawater. Due to the passivity of MP35N, a galvanically active coating, such as aluminum or cadmium, may be required to prevent galvanic corrosion of aluminum joints. Initial tests have indicated that MP35N does not appear to be susceptible to hydrogen embrittlement.

Short time exposure to temperatures above 700 F causes a decrease in ductility (elongation and reduction of area) at temperature. Mechanical properties at room temperature are not affected significantly by unstressed exposure to temperatures up to 50 degrees below the aging temperature (1000 to 2000 F) for up to 100 hours.

Heat Treatment.—After work strengthening, MP35N is aged at 1000 to 1200 F for 4 to 4½ hours and air cooled.

Material specifications for MP35N are presented in Table 7.4.1.0(a). The room-temperature mechanical and physical properties for MP35N are presented in Tables 7.4.1.0(b) and (c). The effect of temperature on physical properties is shown in Figure 7.4.10.

Table 7.4.1.0(a). *Material Specifications for MP35N Alloy*

Specification	Form
AMS 5844	Bar (solution treated, and cold drawn)
AMS 5845	Bar (solution treated, cold drawn and aged)

7.4.1.1 *Cold Worked and Aged Condition.*—Elevated temperature curves for various mechanical properties are shown in Figures 7.4.1.1.1, 7.4.1.1.4 (a) and (b), and 7.4.1.1.5. Typical tensile stress-strain curves at room and elevated temperatures are shown in Figure 7.4.1.1.6.

TABLE 7.4.1.0(b). *Design Mechanical and Physical Properties of MP35N Alloy Bar*

Specification	AMS 5845			
Form	Bar			
Condition	Solution treated, cold drawn, and aged			
Diameter, in.[c]	≤0.800		0.801-1.000	1.001-1.750
Basis	A	B	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	260[a]	275	260	260
LT	...	...	...	...
F_{ty}, ksi:				
L	230[b]	266	230	230
LT	...	...	...	...
F_{cy}, ksi:				
L	...	...	...	...
LT	...	...	...	...
F_{su}, ksi	145	147	145	...
F_{bru}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
F_{bry}, ksi:				
(e/D = 1.5)	...	...	...	...
(e/D = 2.0)	...	...	...	...
e, percent (S basis):				
L	8	...	8	8
RA, percent (S basis):				
L	35	...	35	35
E, 10^3 ksi	34.0			
E_c, 10^3 ksi	...			
G, 10^3 ksi	11.7			
μ	...			
Physical Properties:				
ω, lb/in.^{3}	0.304			
C, Btu/(lb)(F)	0.18 (32 to 70 F)			
K and α	See Figure 7.4.1.0			

[a]The A value of 266 ksi is higher than specification minimum.
[b]The A value of 256 ksi is higher than specification minimum.
[c]Tensile specimens are located at T/2 location for bars 0.800 inch and under in diameter or distance between parallel sides and at T/4 location of larger size bars. The strength of bar, especially large diameter, may vary significantly from center to surface; consequently, caution should be exercised in machining parts from bars over 0.800 inch in diameter since strengths may be lower than design values depending on depth of material removed from surface.

TABLE 7.4.1.0(c). *Design Mechanical and Physical Properties of MP35N Alloy Bar*

Specification	AMS 5844	
Form	Bar	
Condition	Solution treated, cold drawn, and aged	
Diameter, in.[a]	≤1.000	1.001-1.750
Basis	S	S
Mechanical Properties:		
F_{tu}, ksi:		
L	260	260
LT	...	...
F_{ty}, ksi:		
L	230	230
LT	...	...
F_{cy}, ksi:		
L	...	...
LT	...	...
F_{su}, ksi	145	...
F_{bru}, ksi:		
(e/D = 1.5)	...	...
(e/D = 2.0)	...	...
F_{bry}, ksi:		
(e/D = 1.5)	...	...
(e/D = 2.0)	...	...
e, percent:		
L	8	8
RA, percent:		
L	35	35
E, 10^3 ksi	34.0	
E_c, 10^3 ksi	...	
G, 10^3 ksi	11.7	
μ	...	
Physical Properties:		
ω, lb/in.^{3}	0.304	
C, Btu/(lb)(F)	0.18 (32 to 70 F)	
K and α	See Figure 7.4.1.0	

[a]Tensile specimens are located at T/2 location for bars 0.800 inch and under in diameter or distance between parallel sides and at T/4 location for larger size bars. The strength of bar, especially large diameter may vary significantly from center to surface; consequently, caution should be exercised in machining parts from bars over 0.800 inch in diameter since strengths may be lower than design values depending on depth of material removed from surface.

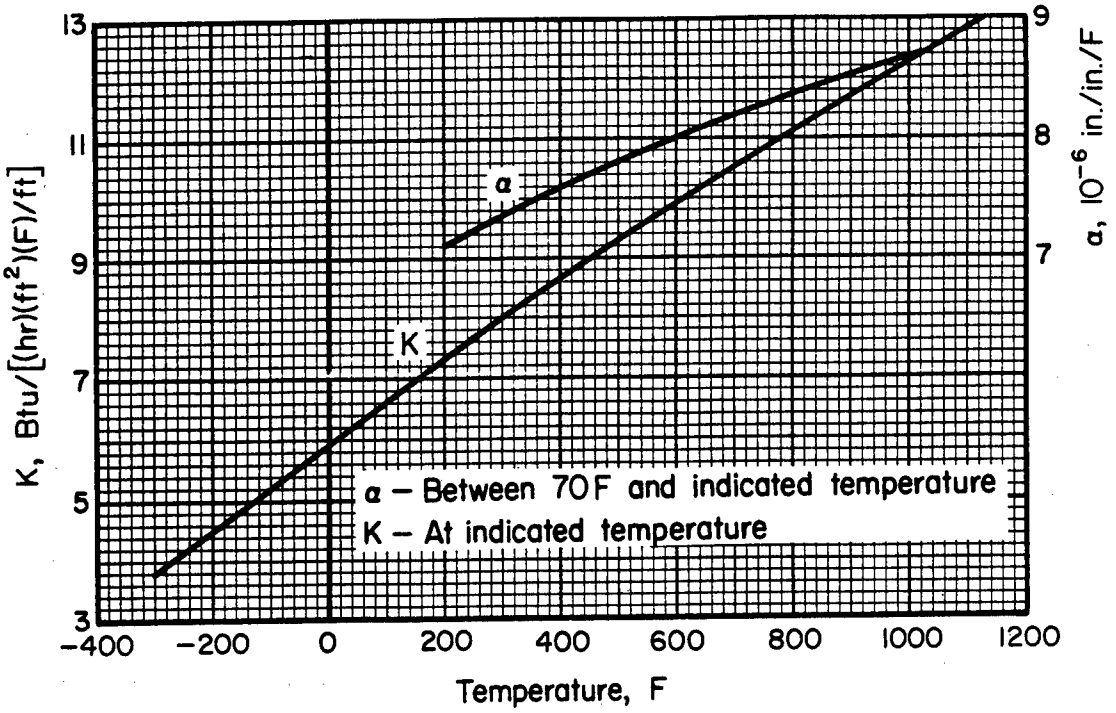


FIGURE 7.4.1.0. *Effect of temperature on the physical properties of MP35N alloy.*

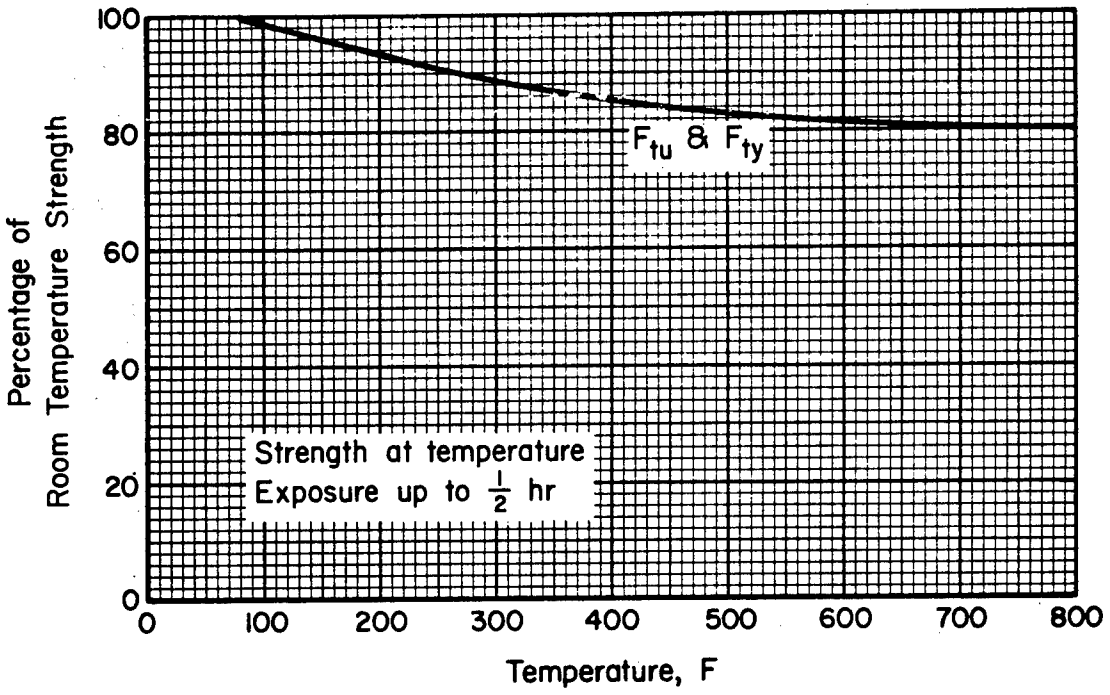


FIGURE 7.4.1.1.1. *Effect of temperature on the tensile ultimate strength (F_{tu}) and the tensile yield* strength *(F_{ty}) of cold worked and aged MP35N bar, F_{tu} = 260 ksi.*

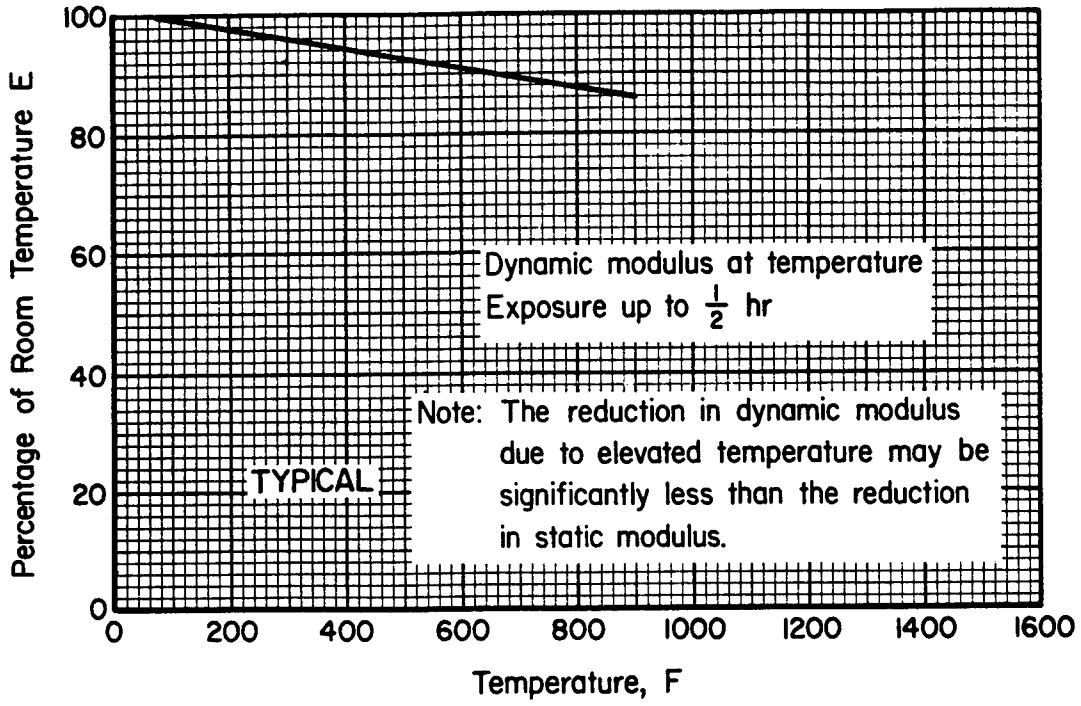


FIGURE 7.4.1.1.4(a). *Effect of temperature on the dynamic tensile modulus (E) of MP35N alloy bar.*

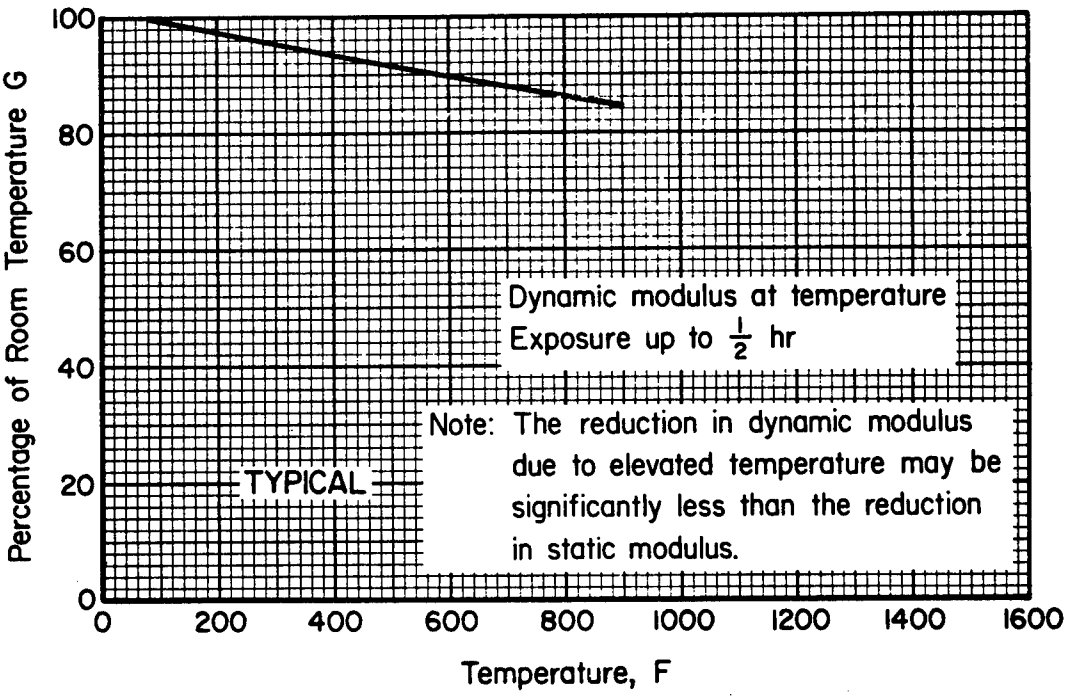


FIGURE 7.4.1.1.4(b). *Effect of temperature on the dynamic shear modulus (G) of MP35N alloy bar.*

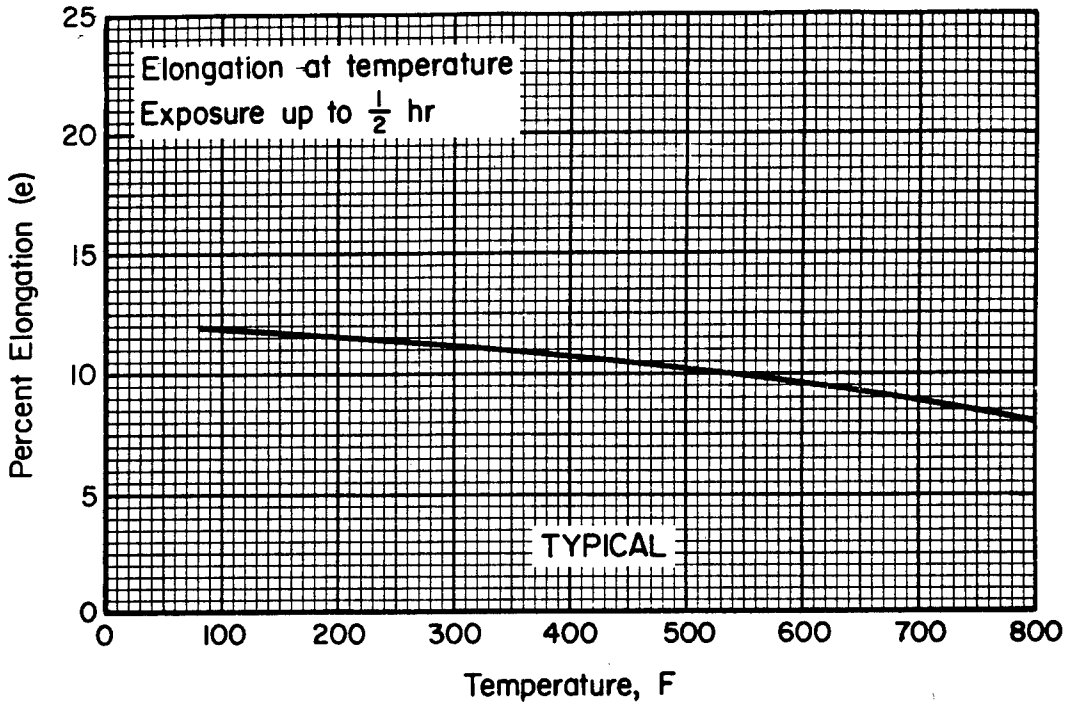


FIGURE 7.4.1.1.5. *Effect of temperature on the elongation (e) of cold worked and aged MP35N bar, F_{tu} = 260 ksi.*

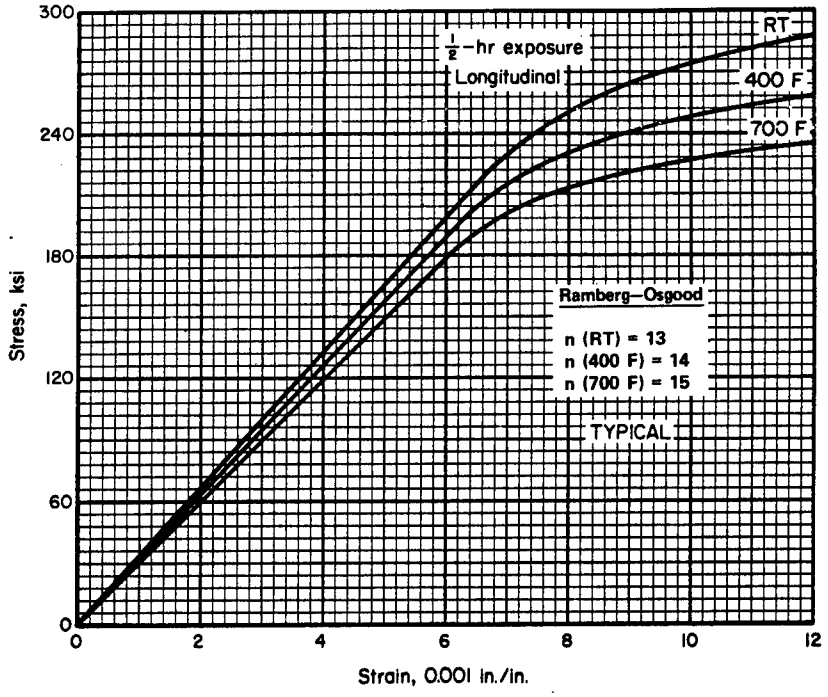


FIGURE 7.4.1.1.6. *Typical tensile stress-strain curves at room and elevated temperatures for cold worked and aged MP35N bar, F_{tu} = 260 ksi.*

7.4.2 MP159 ALLOY

7.4.2.0 *Comments and Properties.*—MP159 is a vacuum induction, vacuum arc remelted alloy, based on cobalt, nickel, chromium, iron, and molybdenum, which can be work-strengthened and aged to ultrahigh strength. This alloy is suitable for parts requiring ultrahigh strength, good ductility, and excellent corrosion and oxidation resistance up to 1100 F. The alloy maintains its ultrahigh strength very well at temperatures up to 1100 F.

Manufacturing Considerations.—The work hardening characteristics of MP159 are similar to MP35N and 304 stainless steel. Drawing, swaging, rolling, and shear forming are excellent deforming methods for work strengthening the alloy. The machinability of MP159 is similar to MP35N and the nickel-base alloys.

Environmental Considerations.—MP159 has excellent corrosion, crevice corrosion, and stress corrosion resistance in various hostile environments. Due to the passivity of MP159, a galvanically active coating, such as aluminum or cadmium, may be required to prevent galvanic corrosion of aluminum joints. Initial tests have indicated that MP159 does not appear to be susceptible to hydrogen embrittlement.

Heat Treatment.—After work strengthening, MP159 is aged at 1200 to 1250 F ± 25 F for 4 to 4½ hours and air cooled.

Material specifications for MP159 are presented in Table 7.4.2.0(a). The room temperature mechanical and physical properties for MP159 and presented in Tables 7.4.2.0(b) and (c). The effect of temperature on thermal expansion is shown in Figure 7.4.2.0.

TABLE 7.4.2.0(a). *Material Specifications for MP159 Alloy*

Specification	Form
AMS 5842	Bar (solution treated and cold drawn)
AMS 5843	Bar (solution treated, cold drawn, and aged)

7.4.2.1 *Cold Worked and Aged Condition.*—The effect of temperature on tension modulus of elasticity and shear modulus is presented in Figure 7.4.2.1.4. A typical stress-strain curve at room temperature is shown in Figure 7.4.2.1.6.

TABLE 7.4.2.0(b). *Design Mechanical and Physical Properties of MP159 Alloy Bar*

Specification	AMS 5843				
Form	Bar				
Condition	Solution treated, cold drawn, and aged				
Diameter, in.[a]	≤0.500		0.501-0.800		0.801-1.750
Basis	A	B	A	B	S
Mechanical Properties:					
F_{tu}, ksi:					
L	260[b]	269	260[b]	269	260
LT	...	...	...	...	...
F_{ty}, ksi:					
L	250[c]	262	250[c]	262	250
LT	...	...	...	...	...
F_{cy}, ksi:					
L	...	...	...	...	...
LT	...	...	...	...	...
F_{su}, ksi	131	144	...	...	...
F_{bru}, ksi:					
(e/D = 1.5)	...	...	...	...	...
(e/D = 2.0)	...	...	...	...	...
F_{bry}, ksi:					
(e/D = 1.5)	...	...	...	...	...
(e/D = 2.0)	...	...	...	...	...
e, percent (S basis):					
L	6	...	6	...	6
RA, percent (S basis):					
L	32	...	32	...	32
E, 10^3 ksi	35.3				
E_c, 10^3 ksi	...				
G, 10^3 ksi	11.3				
μ	0.37 (solution treated condition)				
Physical Properties:					
ω, lb/in.^{3}	0.302				
C and K	...				
α, 10^{-6} in./in./F	See Figure 7.4.2.0				

[a]Tensile specimens are located at T/2 location for bars 0.800 inch and under in diameter or distance between parallel sides and at T/4 location for larger size bars. The strength of bar, especially large diameter, may vary machining parts from bars over 0.800 inch in diameter since strengths may be lower than design values depending on depth of material removed from surface.
[b]S-basis. The A value of 265 ksi is higher than specification minimum.
[c]S-basis. The A value of 253 ksi is higher than specification minimum.

TABLE 7.4.2.0(c). *Design Mechanical and Physical Properties of MP159N Alloy Bar*

Specification	AMS 5842	
Form	Bar	
Condition	Solution treated, cold drawn, and aged	
Diameter, in.[a]	≤0.500	0.501-1.750
Basis	S	S
Mechanical Properties:		
F_{tu}, ksi:		
L	260	260
LT	...	...
F_{ty}, ksi:		
L	250	250
LT	...	...
F_{cy}, ksi:		
L	...	...
LT	...	...
F_{su}, ksi	131	...
F_{bru}, ksi:		
(e/D = 1.5)	...	...
(e/D = 2.0)	...	...
F_{bry}, ksi:		
(e/D = 1.5)	...	...
(e/D = 2.0)	...	...
e, percent:		
L	6	6
RA, percent:		
L	32	32
E, 10^3 ksi	35.3	
E_c, 10^3 ksi	...	
G, 10^3 ksi	11.3	
μ	0.37 (solution treated condition)	
Physical Properties:		
ω, lb/in.^{3}	0.302	
C and K	...	
α, 10^{-6} in./in./F	See Figure 7.4.2.0	

[a]Tensile specimens are located at T/2 location for bars 0.800 inch and under in diameter or distance between parallel sides and at T/4 location for larger size bars. The strength of bar, especially large diameter may vary significantly from center to surface; consequently, caution should be exercised in machining parts from bars over 0.800 inch in diameter since strengths may be lower than design values depending on depth of material removed from surface.

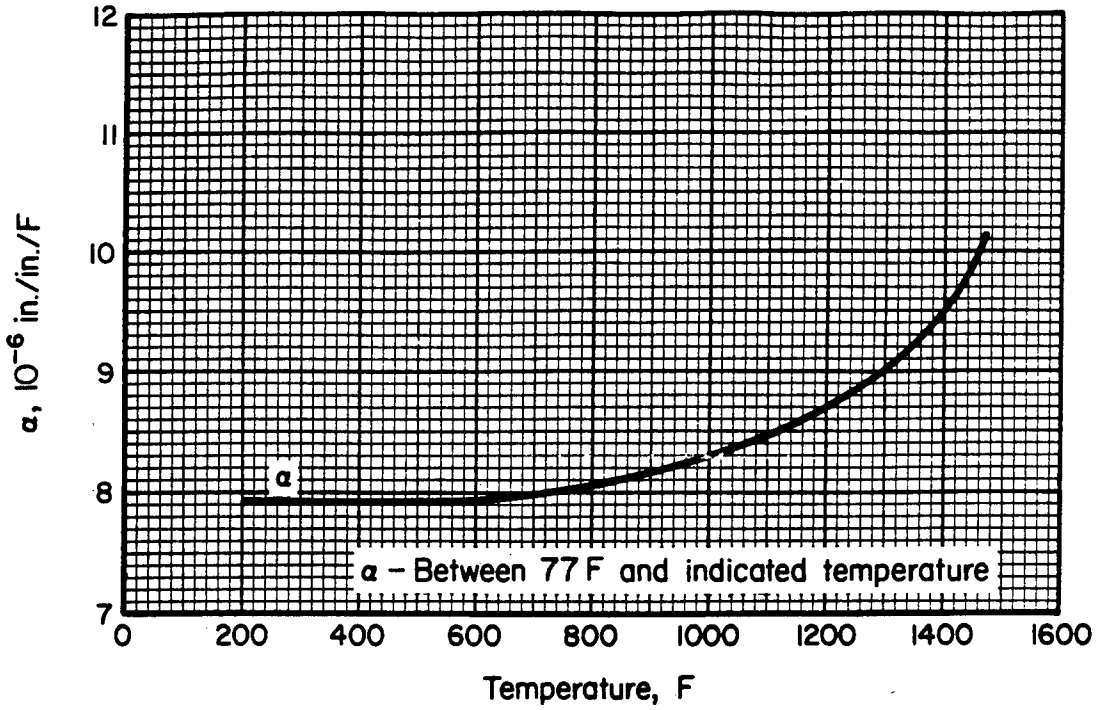


FIGURE 7.4.2.0. *Effect of temperature on thermal expansion (α) of MP159 alloy bar.*

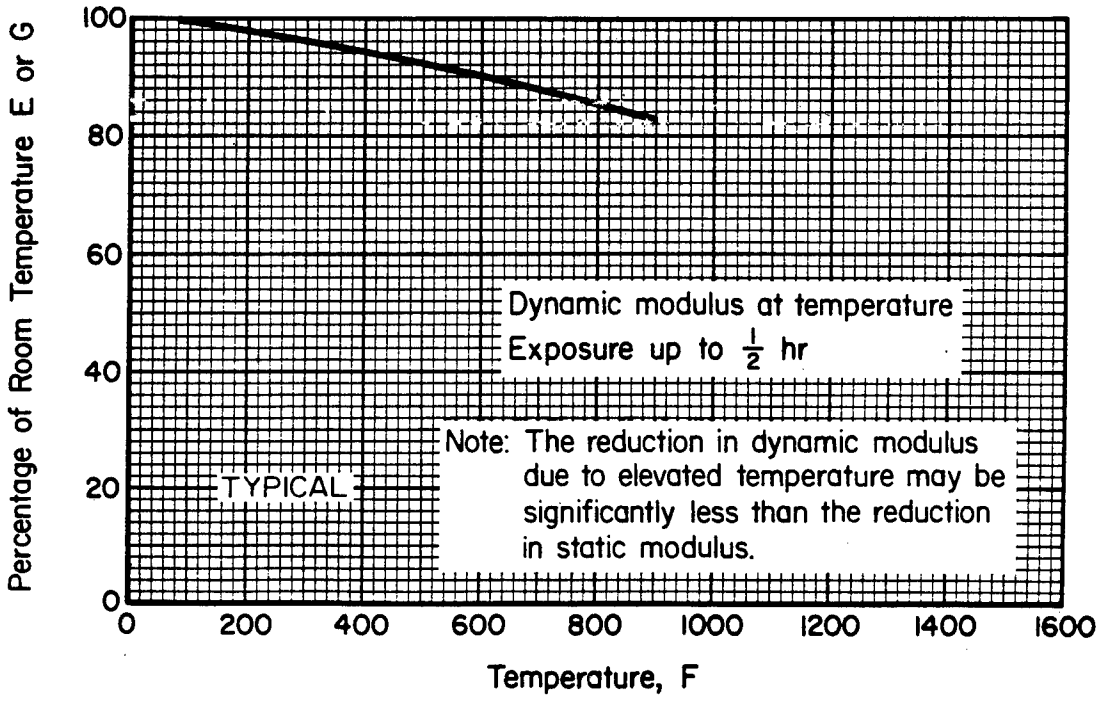


FIGURE 7.4.2.1.4. *Effect of temperature on the tensile modulus (E) and shear modulus (G) of MP159 alloy bar.*

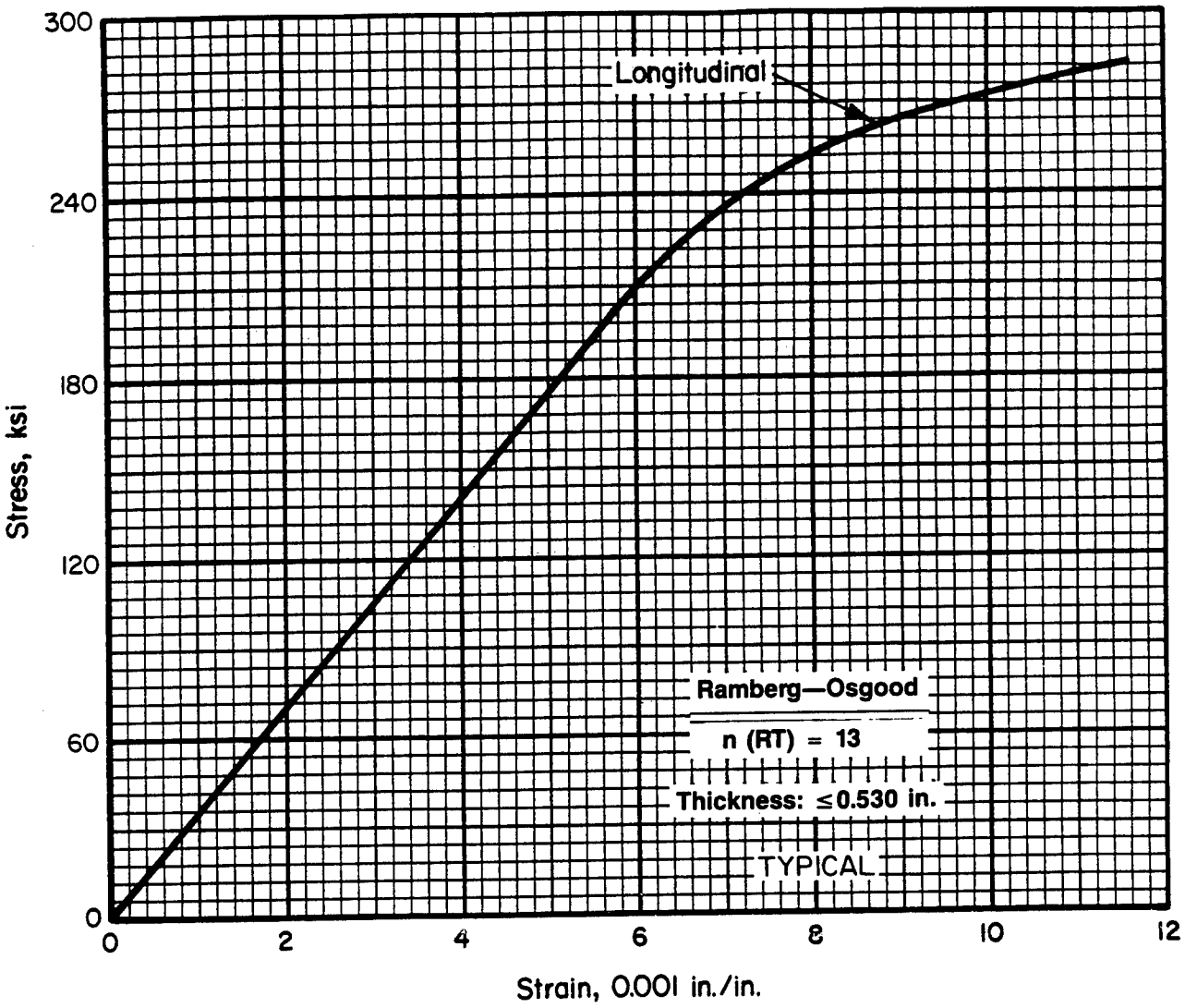


FIGURE 7.4.2.1.6. *Typical tensile stress-strain curve at room temperature for cold worked and aged MP159 alloy bar.*

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7.5 Aluminum Alloy Sheet Laminates

7.5.0 GENERAL.—This section contains the engineering properties of aluminum alloy sheet laminates. These products consist of thin high-strength aluminum alloy sheets alternating with fiber layers impregnated with adhesive. These sheet laminates provide a very efficient structure for certain applications and exhibit excellent fatigue resistance.

Tensile and compressive properties for the aluminum alloy sheet laminates were determined using test specimens similar to those used for testing conventional aluminum alloy sheet with one exception. The Iosipescu shear specimen was the most appropriate configuration for the determination of shear strength. Shear yield strength and shear ultimate strength were determined using the Iosipescu test procedure. Shear yield strength was determined at 0.2% offset from load-deformation curves. Bearing tests were conducted according to ASTM E 238, which is applicable to conventional aluminum alloy products. Bearing specimens exhibited several different types of failure and bearing strength was influenced by failure mode. Consequently, a more suitable bearing test procedure for aramid fiber reinforced aluminum alloy sheet laminates is currently being developed. However, the design values for bearing strength determined according to ASTM E 238 are conservative and are considered suitable for design. These sheet laminates exhibit low elongation as measured by the tensile test. Consequently, a more realistic measure of ductility is total strain at failure, ε_t, defined as the measure of strain determined from the tensile load-deformation curve at specimen failure. This measurement includes both elastic and plastic strains. The minimum total strain at failure value from the material specification shall be presented in the room temperature design allowable table. These sheet laminates are generally anisotropic. Therefore, design values for each grain orientation of the aluminum alloy sheet shall be presented for all mechanical properties, except F_{su} and F_{sy}. The longitudinal direction is parallel to the rolling direction of the aluminum alloy sheet or length of sheet laminate, while the long transverse direction is 90° to the longitudinal direction or parallel to the width of the sheet laminate. The design values for F_{cy}, F_{sy}, F_{su}, F_{bry}, and F_{bru} were derived conventionally in accordance with the guidelines.

7.5.1 2024-T3 ARAMID FIBER REINFORCED SHEET LAMINATE

7.5.1.0 *Comments and Properties.*—This product consists of thin 2024-T3 sheets alternating with aramid fiber layers embedded in a special resin. Nominal thickness of aluminum sheet is 0.012 inch with a prepreg nominal thickness of 0.0085 inch. The primary advantage of this product is the significant improvement in fatigue and fatigue crack growth properties compared to conventional aluminum alloy structures. The product also has good damping capacity and resistance to impact. Compared to 7475-T761 aramid fiber-reinforced sheet laminate, this product has better formability and damage tolerance characteristics.

Manufacturing Considerations.—This product can be fabricated by conventional metal practices for machining, sawing, drilling, joining with fasteners and can be inspected by conventional procedures.

Environmental Considerations.—This product has good corrosion resistance. The maximum service temperature is 200 F.

Specification and Properties.—A material specification is presented in Table 7.5.1.0(a). Room-temperature mechanical properties are presented in Table 7.5.1.0(b).

TABLE 7.5.1.0(a). *Material Specifications for 2024-T3 Aramid Fiber Reinforced Sheet Laminate*

Specification	Form
AMS 4254	Sheet laminate

7.5.1.1 *T3 Temper.*—Typical tensile and compressive stress-strain and tangent-modulus curves are shown in Figures 7.5.1.1.6(a) through (b).

TABLE 7.5.1.0(b). *Design Mechanical and Physical Properties of 2024-T3 Aluminum Alloy, Aramid Fiber Reinforced, Sheet Laminate*

Specification	AMS 4254			
Form	Aramid fiber reinforced sheet laminate			
Laminate lay-up	2/1	3/2	4/3	5/4
Nominal thickness, in.	0.032	0.053	0.074	0.094
Basis	S	S	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	90	96	101	101
LT	48	44	43	42
F_{ty}, ksi:				
L	48	49	49	49
LT	33	30	30	30
F_{cy}, ksi:				
L	35	35	34	33
LT	33	30	30	30
F_{su}[a], ksi	d	d	d	d
F_{sy}[a], ksi	16	15	14	14
F_{bru}[b], ksi:				
L (e/D = 1.5)	78	73	73	68
LT (e/D = 1.5)	89	84	80	75
L (e/D = 2.0)	93	86	83	77
LT (e/D = 2.0)	95	89	81	76
F_{bry}[b], ksi:				
L (e/D = 1.5)	53	52	51	50
LT (e/D = 1.5)	56	52	52	52
L (e/D = 2.0)	63	63	61	59
LT (e/D = 2.0)	66	61	61	60
ε_t[c], percent:				
L	2	2	2	2
LT	12	12	12	14
E, 10^3 ksi:				
L	9.9	9.9	9.7	9.6
LT	8.1	7.5	7.1	7.0
E_c, 10^3, ksi:				
L	9.5	9.4	9.3	9.1
LT	8.0	7.5	7.2	7.0
G, 10^3, ksi:				
L	2.7	2.5	2.4	2.2
LT	2.6	2.4	2.4	2.2
μ:				
L	0.33	0.34	0.34	0.32
LT	0.29	0.27	0.26	0.25
Physical Properties:				
ω, lb/in.^{3}	0.086	0.084	0.082	0.081
C, K, and α	...	...	...	...

[a]Shear values determined from data obtained using Iosipescu shear specimens.
[b]Bearing values are "dry pin" values per Section 1.4.7.1 determined in accordance with ASTM E238.
[c]Total (elastic plus plastic) strain at failure determined from stress-strain curve.
[d]Shear ultimate strengths not determinable due to excessive deflection of specimen.

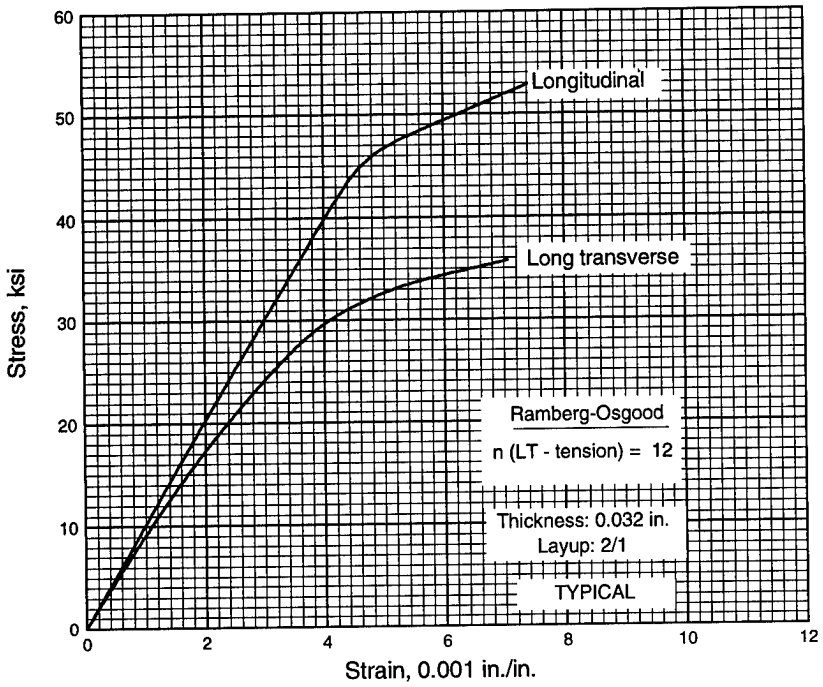


FIGURE 7.5.1.1.6(a). *Typical tensile stress-strain curves for 2024-T3 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

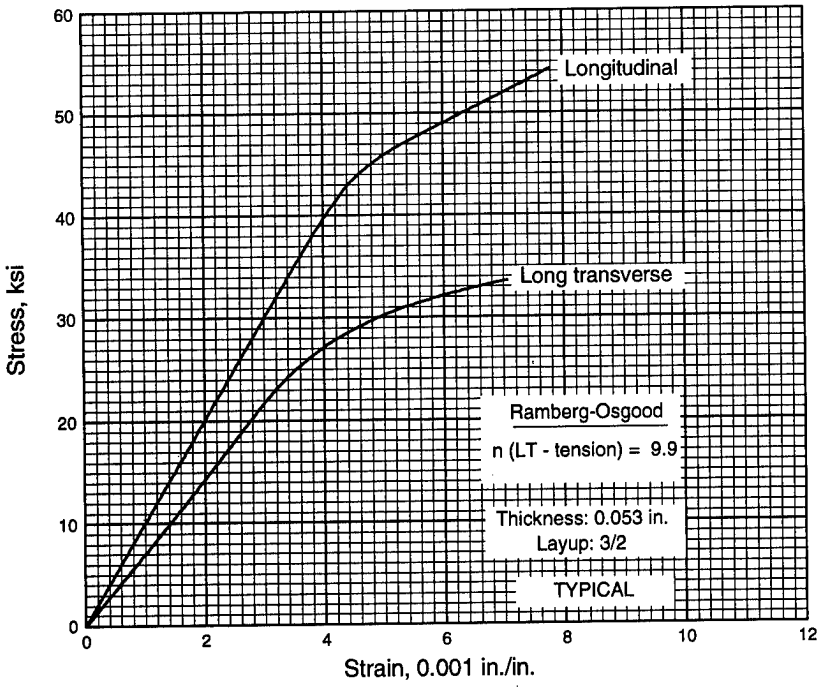


FIGURE 7.5.1.1.6(b). *Typical tensile stress-strain curves for 2024-T3 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

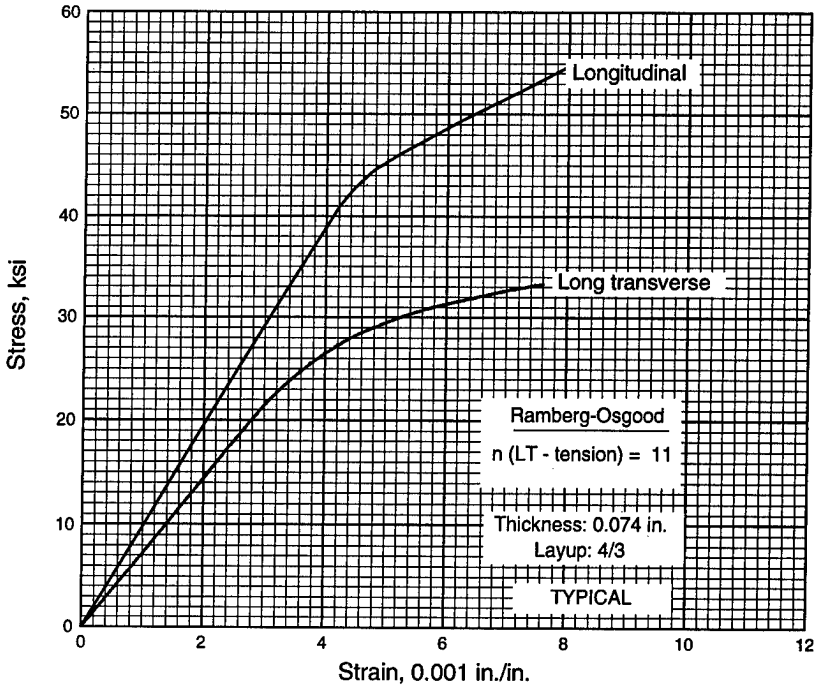


FIGURE 7.5.1.1.6(c). *Typical tensile stress-strain curves for 2024-T3 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

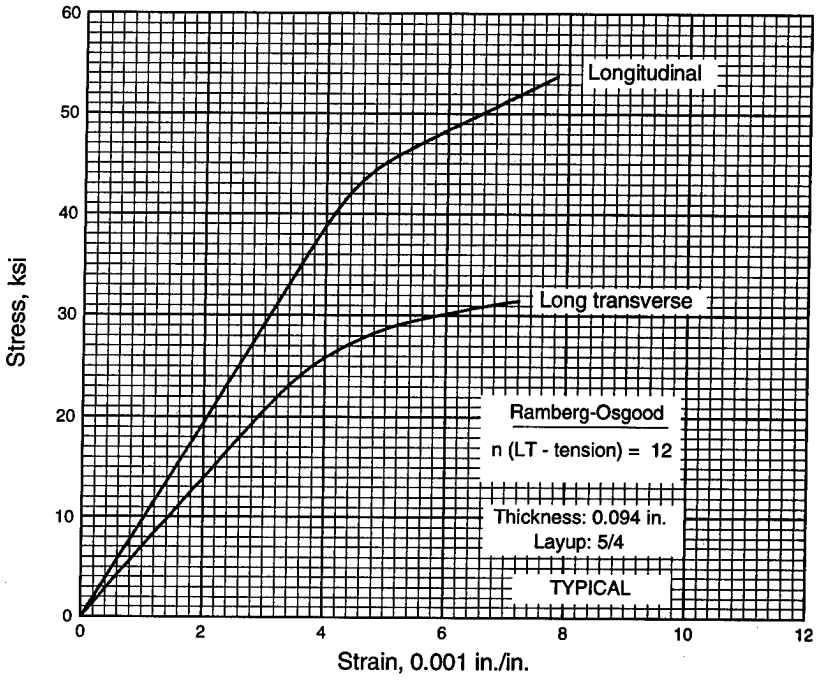


FIGURE 7.5.1.1.6(d). *Typical tensile stress-strain curves for 2024-T3 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

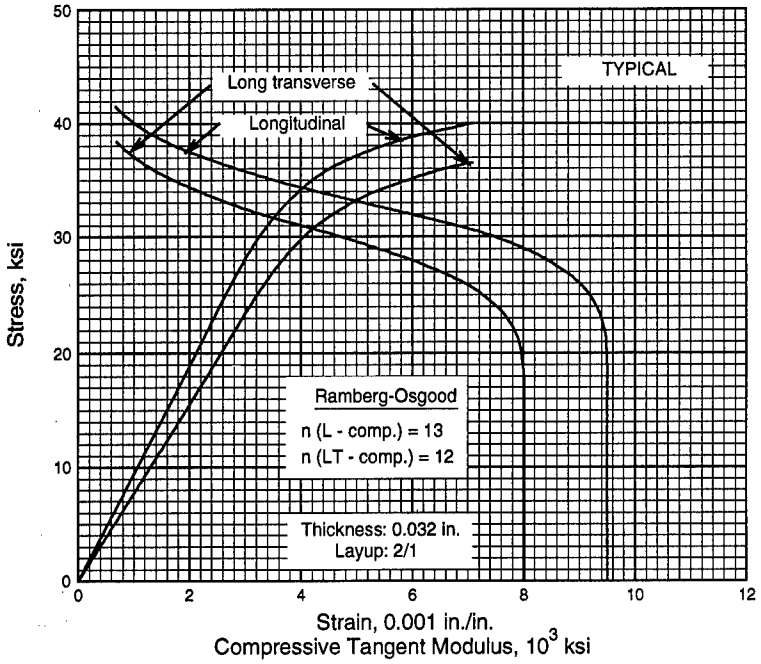


FIGURE 7.5.1.1.6(e). *Typical compressive stress-strain and compressive tangent-modulus curves for 2024-T3 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

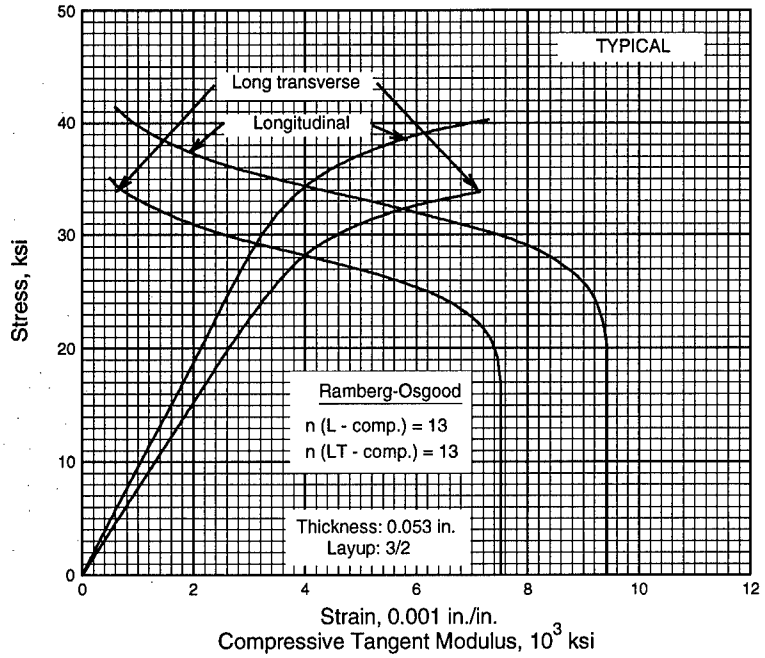


FIGURE 7.5.1.1.6(f). *Typical compressive stress-strain and compressive tangent-modulus curves for 2024-T3 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

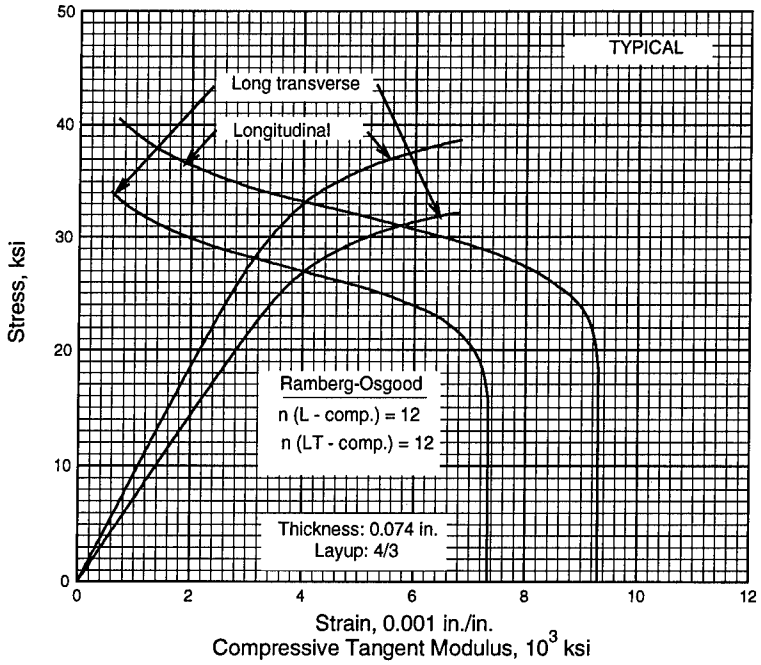


FIGURE 7.5.1.1.6(g). *Typical compressive stress-strain and compressive tangent-modulus curves for 2024-T3 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

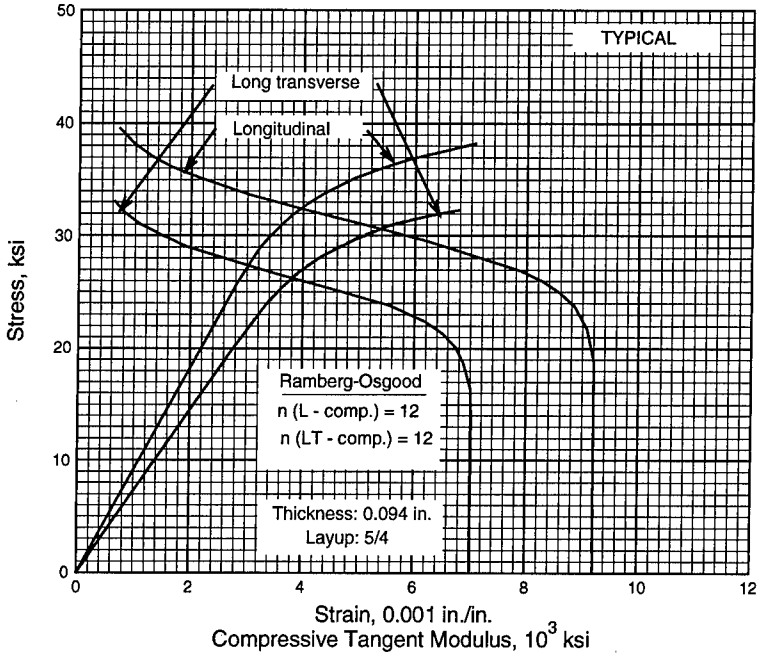


FIGURE 7.5.1.1.6(h). *Typical compressive stress-strain and compressive tangent-modulus curves for 2024-T3 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

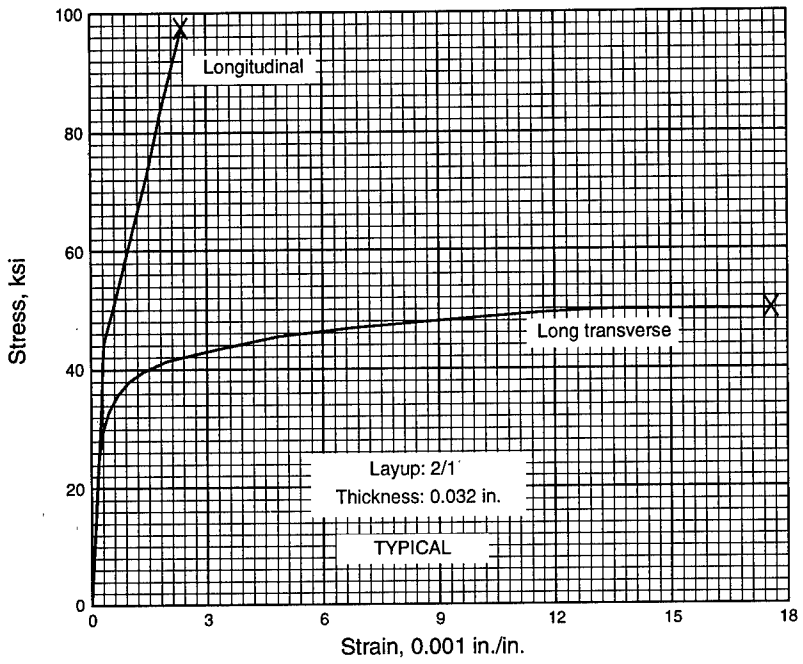


FIGURE 7.5.1.1.6(i). *Typical tensile stress-strain curves (full-range) for 2024-T3 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

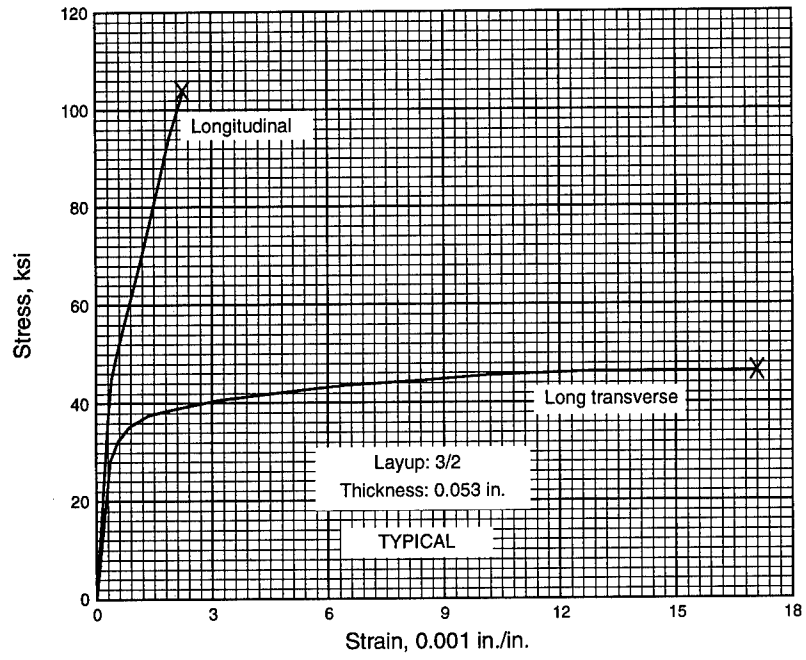


FIGURE 7.5.1.1.6(j). *Typical tensile stress-strain curves (full-range) for 2024-T3 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

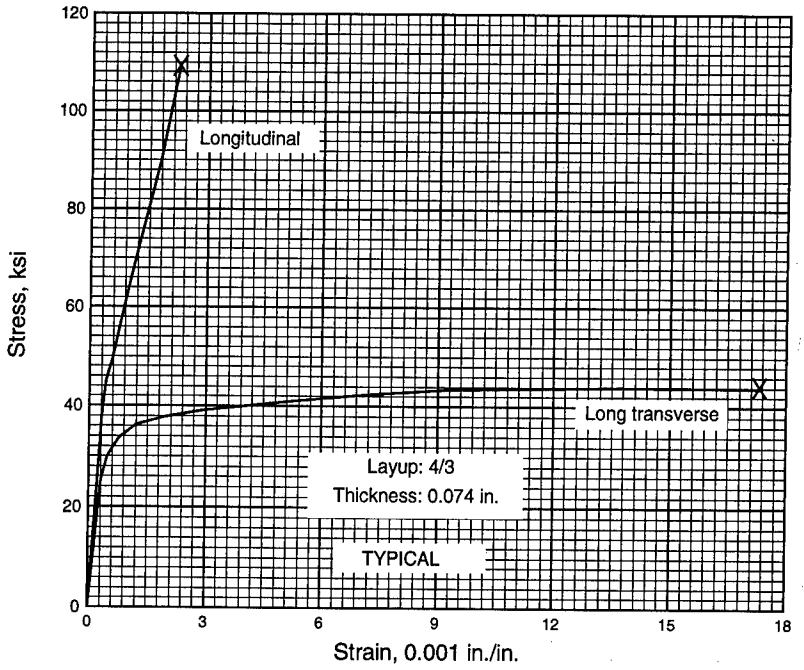


FIGURE 7.5.1.1.6(k). *Typical tensile stress-strain curves (full-range) for 2024-T3 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

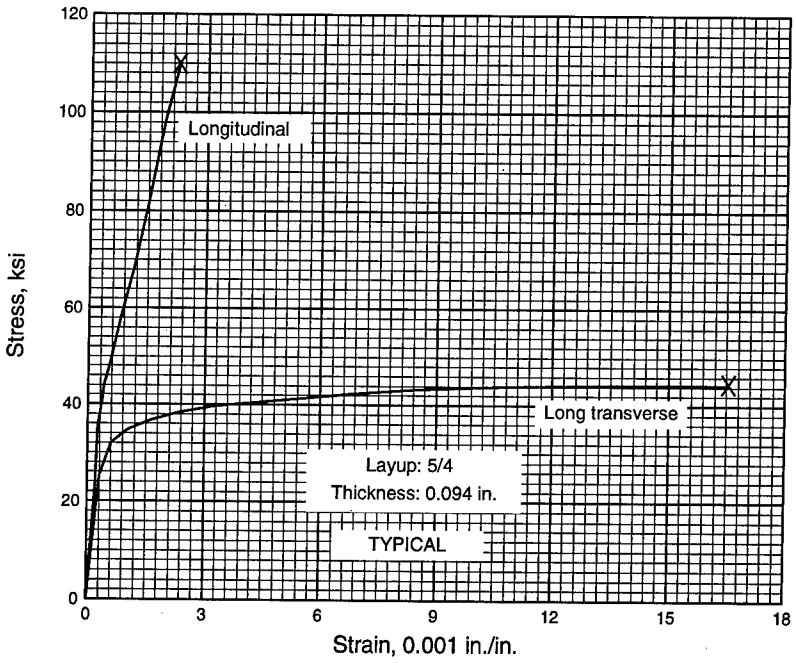


FIGURE 7.5.1.1.6(l). *Typical tensile stress-strain curves (full-range) for 2024-T3 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

7.5.2 7475-T761 ARAMID FIBER REINFORCED SHEET LAMINATE

7.5.2.0 *Comments and Properties.*—This product consists of thin 7475-T761 sheets alternating with aramid fiber layers embedded in a special resin. Nominal thickness of aluminum sheet is 0.012 inch with a prepreg nominal thickness of 0.0085 inch. The primary advantage of this product is the significant improvement in fatigue and fatigue crack growth properties compared to conventional aluminum alloy structures. The product also has good damping capacity and resistance to impact.

Manufacturing Considerations.—This product can be fabricated by conventional metal practices for machining, sawing, drilling, joining with fasteners and can be inspected by conventional procedures.

Environmental Considerations.—This product has good corrosion resistance. The maximum service temperature is 200 F.

Specifications and Properties.—A material specification is presented in Table 7.5.2.0(a). Room-temperature mechanical properties are presented in Table 7.5.2.0(b).

TABLE 7.5.2.0(a). *Material Specifications for 7475-T761 Aramid Fiber Reinforced Sheet Laminate*

Specification	Form
AMS 4302	Sheet laminate

7.5.2.1 *T761 Temper.*—Tensile and compressive stress-strain and tangent modulus curves are shown in Figures 7.5.2.1.6(a) through (f). Full-range tensile stress-strain curves are presented in Figures 7.5.2.1.6(g) through (j).

TABLE 7.5.2.0(b). *Design Mechanical and Physical Properties of 7475-T761 Aluminum Alloy, Aramid Fiber Reinforced, Sheet Laminate*

Specification	AMS 4302			
Form	Aramid fiber reinforced sheet laminate			
Laminate lay-up	2/1	3/2	4/3	5/4
Nominal thickness, in.	0.032	0.053	0.074	0.094
Basis	S	S	S	S
Mechanical Properties:				
F_{tu}, ksi:				
L	103	111	114	116
LT	56	51	50	48
F_{ty}, ksi:				
L	76	82	82	84
LT	48	43	42	40
F_{cy}, ksi:				
L	46	46	44	44
LT	51	48	47	45
F_{su}[a], ksi	35	33	33	32
F_{sy}[a], ksi	24	23	22	21
F_{bru}[b], ksi:				
L (e/D = 1.5)	91	83	84	82
LT (e/D = 1.5)	96	85	86	80
L (e/D = 2.0)	104	87	88	84
LT (e/D = 2.0)	108	88	86	80
F_{bry}[b], ksi:				
L (e/D = 1.5)	73	70	66	69
LT (e/D = 1.5)	76	69	69	67
L (e/D = 2.0)	83	81	77	79
LT (e/D = 2.0)	84	76	75	72
e_t[c], percent:				
L	1.5	1.8	1.7	1.8
LT	6.1	6.4	6.3	6.6
E, 10^3 ksi:				
L	9.8	9.9	10.0	9.8
LT	7.7	7.1	6.7	6.7
E_c, 10^3 ksi:				
L	9.6	9.6	9.6	9.7
LT	7.8	7.3	7.0	6.9
G, 10^3 ksi:				
L	2.8	2.6	2.3	2.3
LT	2.6	2.4	2.3	2.3
μ:				
L	0.35	0.35	0.35	0.35
LT	0.25	0.25	0.25	0.25
Physical Properties:				
ω, lb/in.^{3}	0.085	0.083	0.082	0.081
C, K, and α	...	...	...	...

[a]Shear values determined from data obtained using Iosipescu shear specimens.
[b]Bearing values are "dry pin" values per Section 1.4.7.1 determined in accordance with ASTM E 238.
[c]Total (elastic plus plastic) strain at failure determined from stress-strain curve. Values are minimum but not included in AMS 4302.

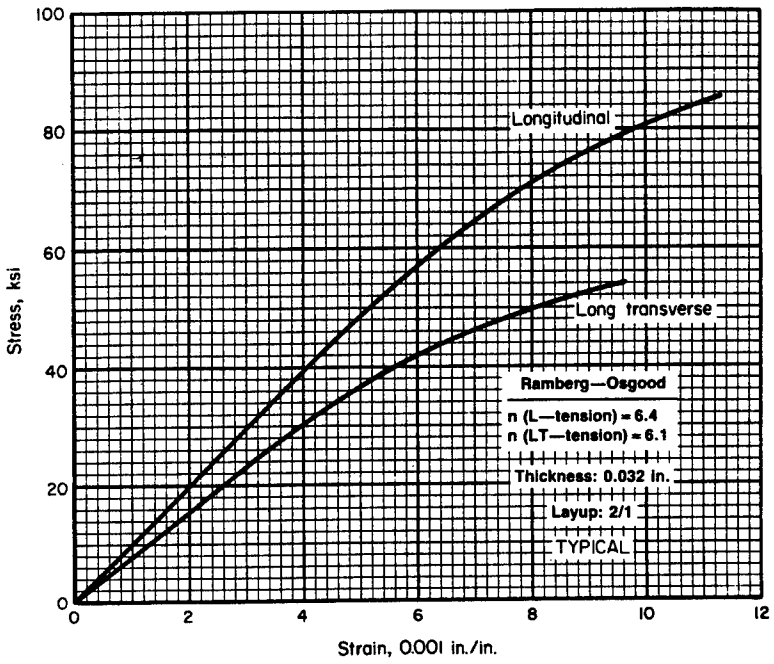


FIGURE 7.5.2.1.6(a). *Typical tensile stress-strain curves for 7475-T761 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

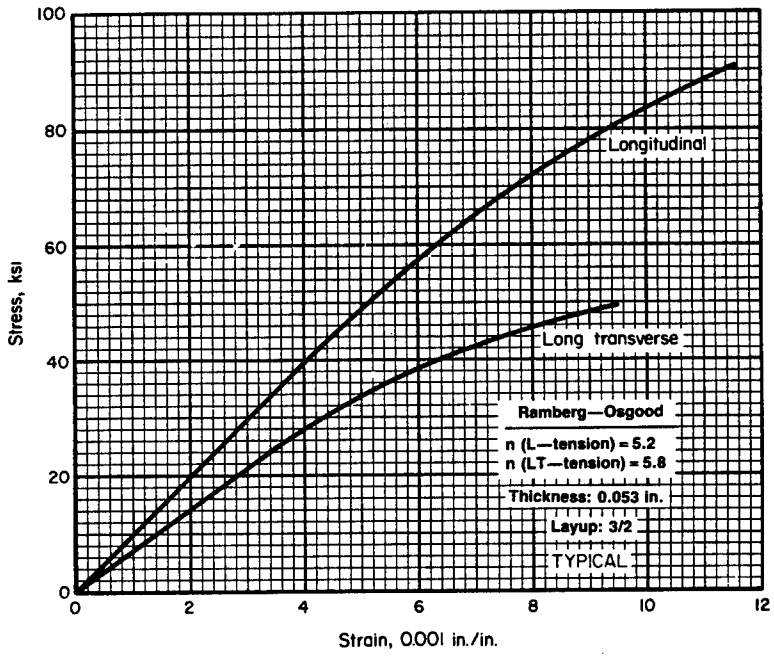


FIGURE 7.5.2.1.6(b). *Typical tensile stress-strain curves for 7475-T761 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

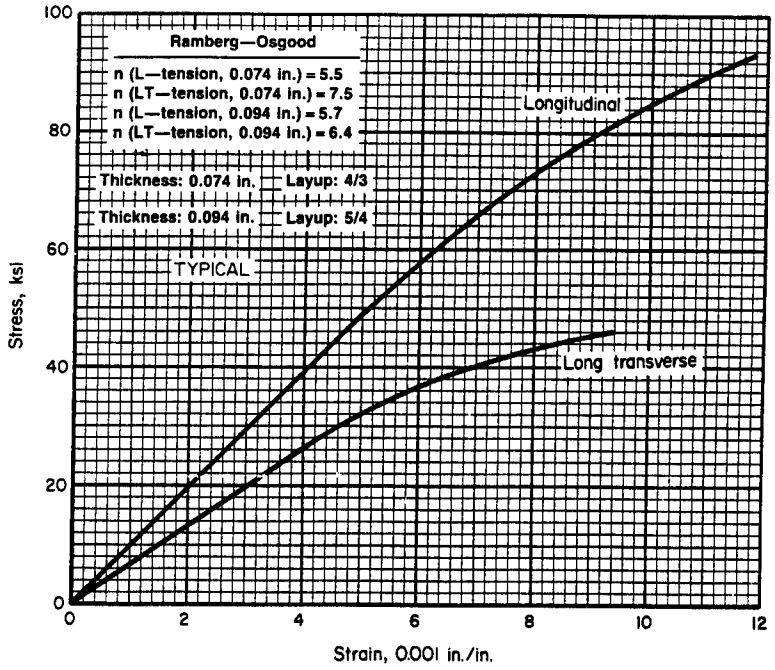


FIGURE 7.5.2.1.6(c). *Typical tensile stress-strain curves for 7475-T761 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

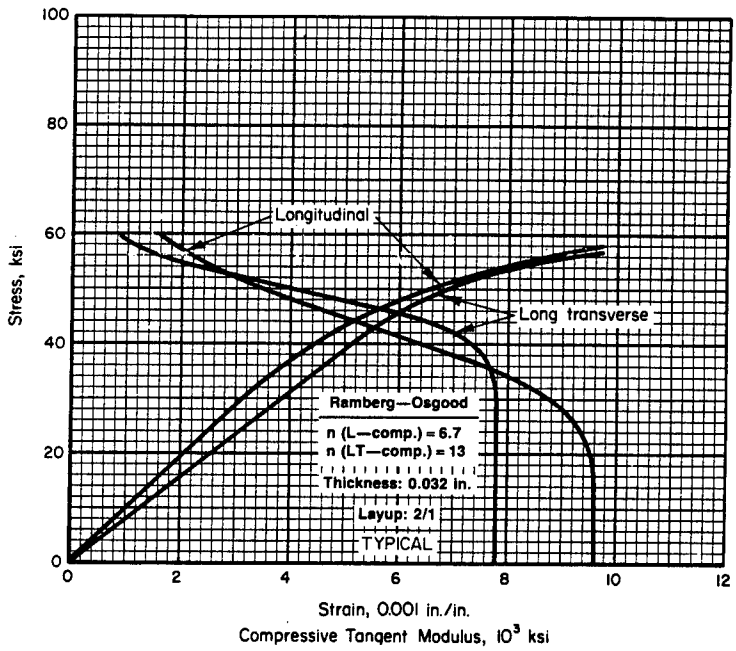


FIGURE 7.5.2.1.6(d). *Typical compressive stress-strain and compressive tangent-modulus curves for 7475-T761 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

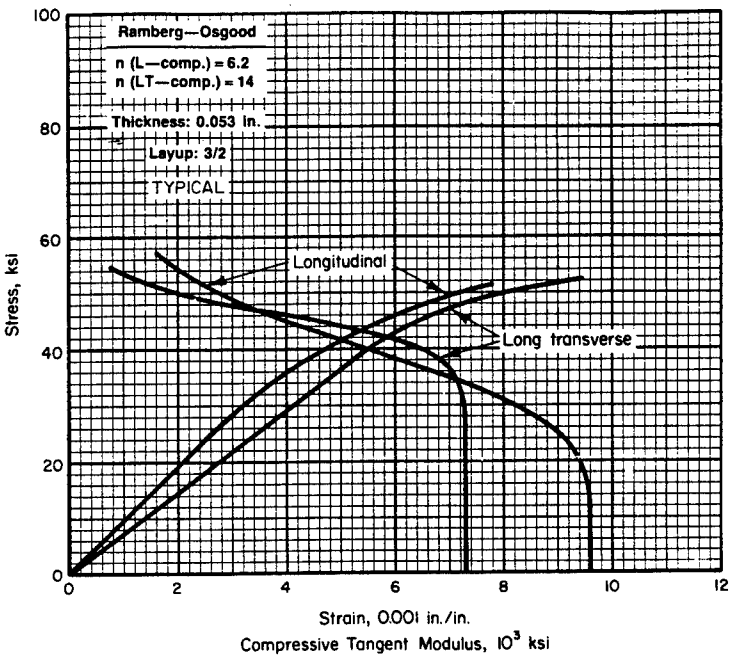


FIGURE 7.5.2.1.6(e). *Typical compressive stress-strain and compressive tangent-modulus curves for 7475-T761 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

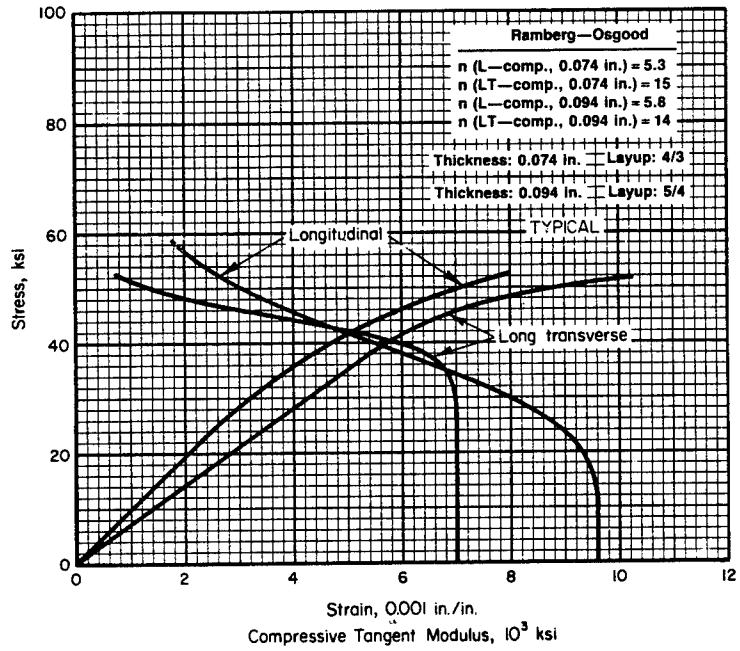


FIGURE 7.5.2.1.6(f). *Typical compressive stress-strain and compressive tangent-modulus curves for 7475-T761 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

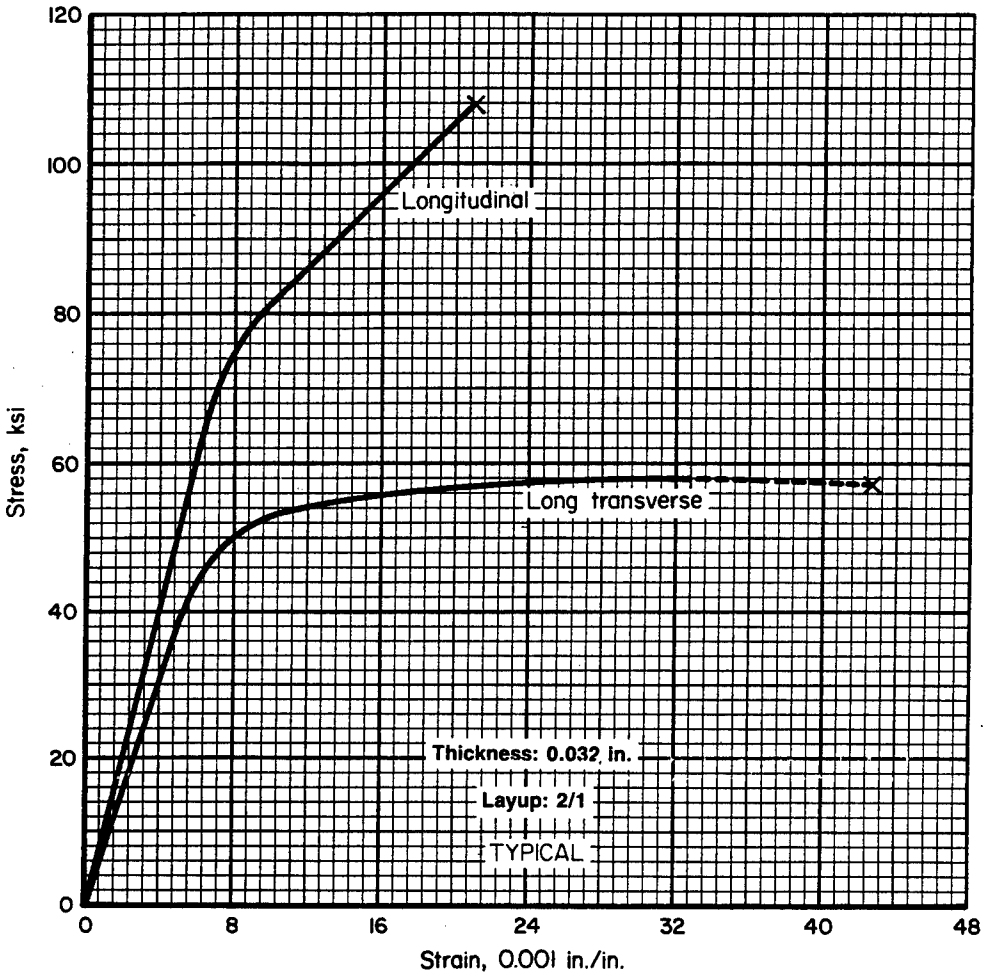


FIGURE 7.5.2.1.6(g). *Typical tensile stress-strain curves (full-range) for 7475-T761 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

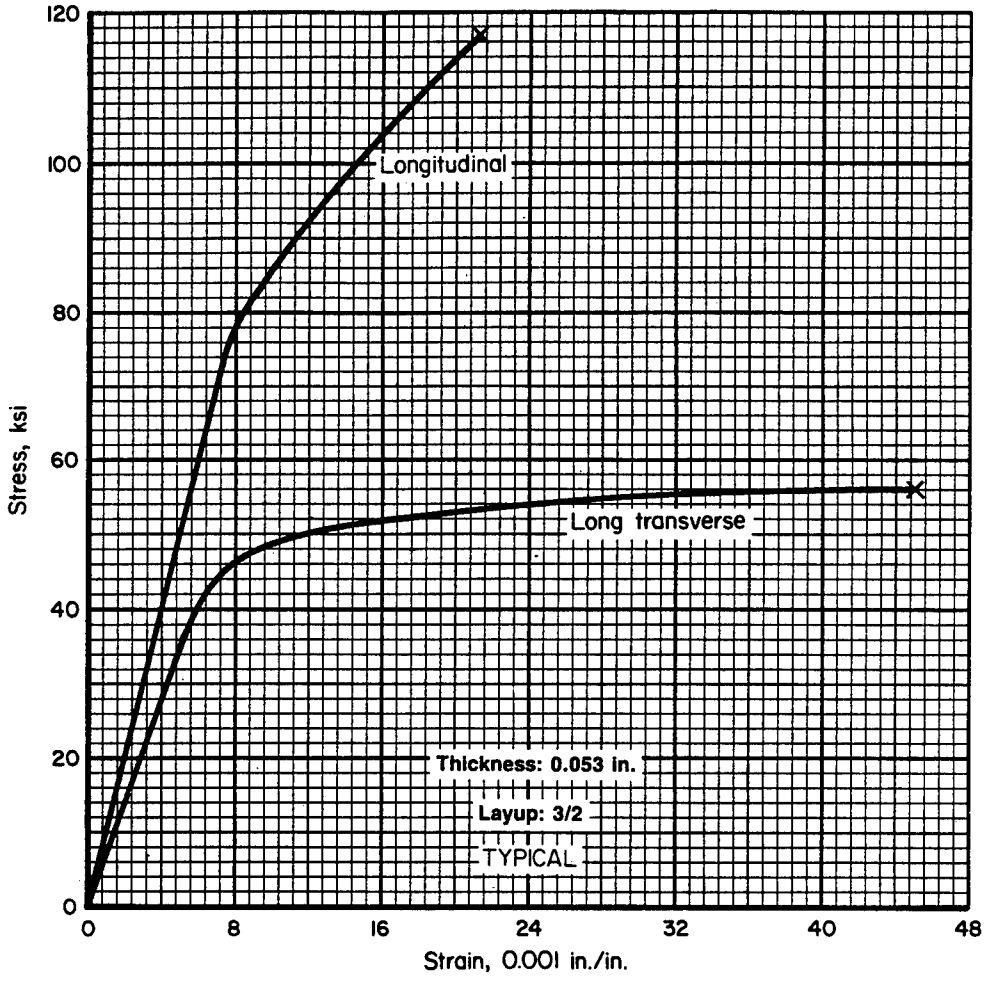


FIGURE 7.5.2.1.6(h). *Typical tensile stress-strain curves (full-range) for 7475-T761 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

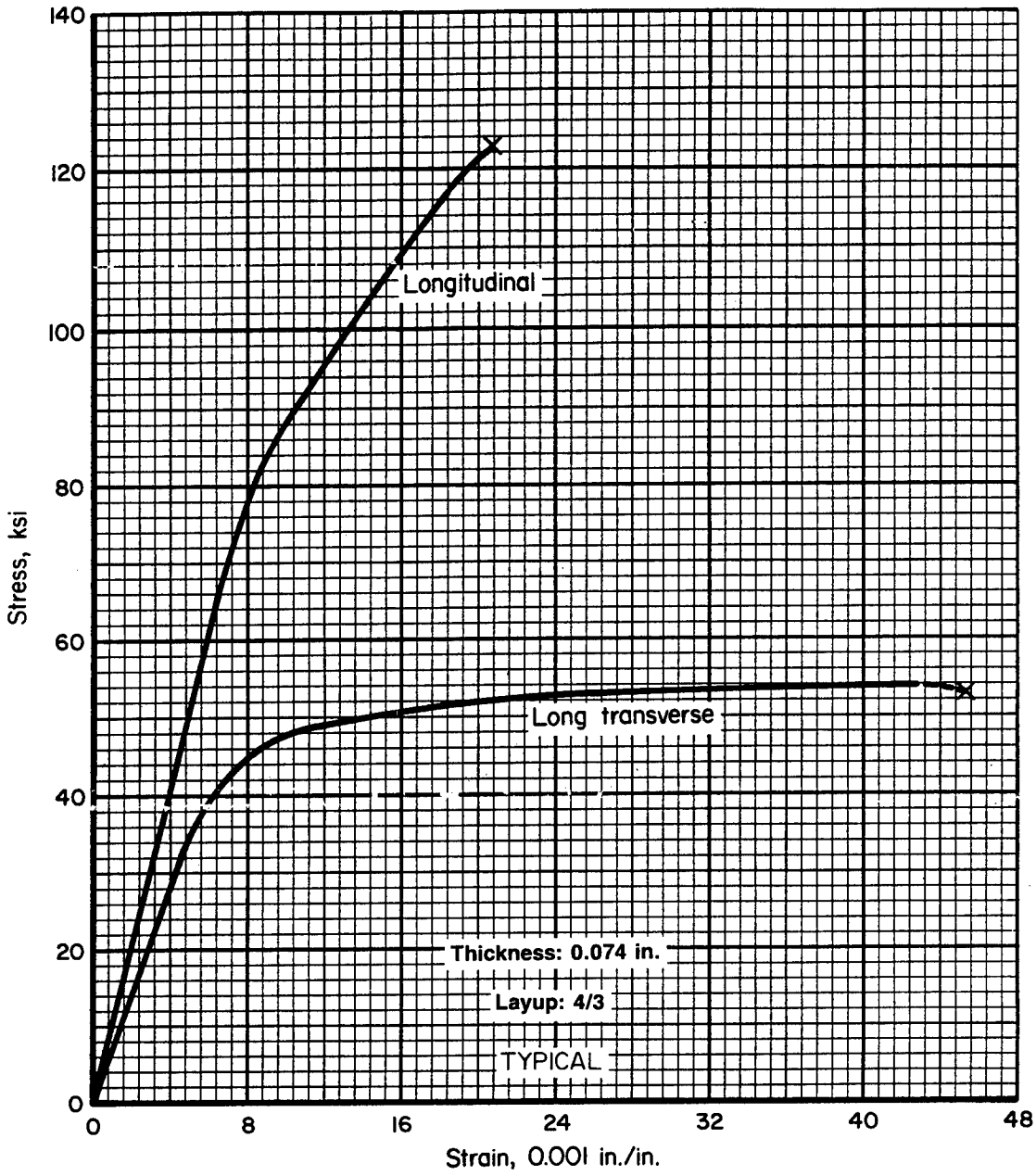


FIGURE 7.5.2.1.6(i). *Typical tensile stress-strain curves (full-range) for 7475-T761 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

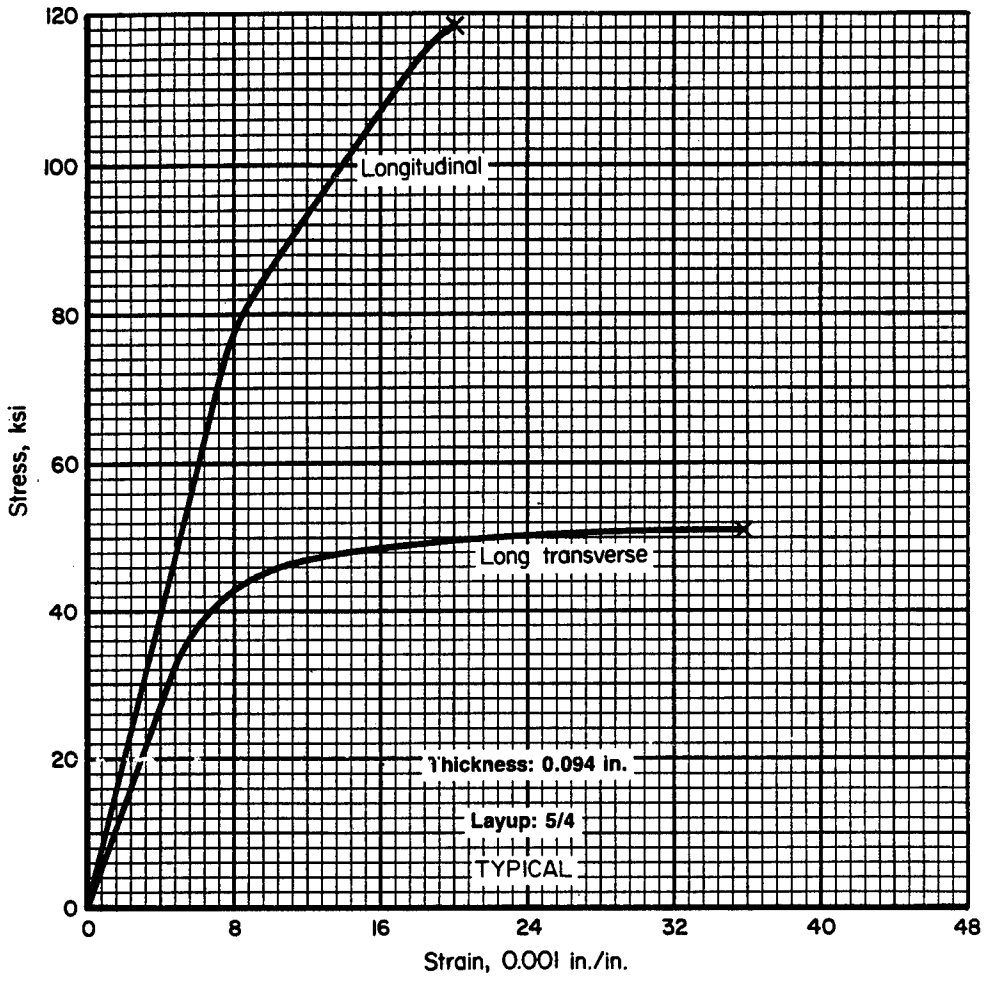


FIGURE 7.5.2.1.6(j). *Typical tensile stress-strain curves (full-range) for 7475-T761 aluminum alloy, aramid fiber-reinforced, sheet laminate.*

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7.2.0(c) Williams, R. F., and Ingels, S. E., "The Fabrication of Beryllium—Volume III: Metal Removal Techniques," NASA TM X-53453 (August 1966).

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7.3.0(b) "The Selection and Application of Copper Alloy Castings," by the ASM Committee on Copper Alloy Castings, ASM Metals Handbook, Vol. 1, 8th Edition, pp. 972-983 (1961).

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Chapter 8

STRUCTURAL JOINTS

This chapter, while comprising three major sections, primarily is concerned with joint allowables. Section 8.1 is concerned with mechanically fastened joints; Section 8.2, with metallurgical joints (various welding and brazing processes). Section 8.3 contains information for structural component data; it is concerned with bearings, pulleys, and cables.

With particular reference to Section 8.1, the introductory section (8.1.1) contains fastener indexes that can be used as a quick reference to locate a specific table of joint allowables. Following this introductory section are five sections comprising the five major fastener categories, as shown in Table 8.0.1.

TABLE 8.0.1. *Structural Joints Index (Fastener Type)*

Section	Fastener Type
8.1.2	Solid Rivets
8.1.2.1	Protruding head
8.1.2.2	Flush head
8.1.3	Blind fasteners
8.1.3.1	Protruding head
8.1.3.2	Flush head
8.1.4	Swaged collar fasteners
8.1.4.1	Protruding head
8.1.4.2	Flush head
8.1.5	Threaded fasteners
8.1.5.1	Protruding head
8.1.5.2	Flush head
8.1.6	Special fasteners
8.1.6.1	Fastener sleeves

In each of the five major sections, there are subsections that describe the factors to be considered in determining the strength of fasteners and joints. After each major section, pertinent tables are presented.

Similarly, Section 8.2 has an introductory section (8.2.1), followed by two major sections comprising different metallurgical joints as shown in Table 8.0.2.

TABLE 8.0.2. *Structural Joints Index (Joining Methods)*

Section	Joining Methods
8.2.2	Welded joints
8.2.2.1	Fusion
8.2.2.2	Flush and
8.2.2.3	pressure
	Spot and seam
8.2.3	Brazing
8.2.3.1	Copper
8.2.3.2	Silver

Following each 4-digit section, applicable tables and figures for the particular section are presented.

8.1 Mechanically Fastened Joints

To determine the strength of mechanically fastened joints, it is necessary to know the strength of the individual fasteners (both by itself, and when installed in various thicknesses of the various materials). In most cases, failures in such joints occur by tensile failure of the fasteners, shearing of the fasteners and by bearing and/or tearing of the sheet or plate.

8.1.1 INTRODUCTION AND FASTENER INDEXES.—Five categories of mechanical fasteners are presently contained in this handbook, generically defined as follows:

Solid Rivets.—Solid rivets are defined as one piece fasteners installed by mechanically upsetting one end.

Blind Fasteners.—Blind fasteners are usually multiple piece devices that can be installed in a joint which is accessible from one side only. When a blind fastener is being installed, a self-contained mechanical, chemical, or other feature forms an upset on its inaccessible or blind side. These fasteners must be destroyed to be removed. This fastener category includes such fasteners as blind rivets, blind bolts, etc.

Swaged Collar Fasteners.—Swaged collar fasteners are multiple piece fasteners, usually consisting of a solid pin and a malleable collar which is swaged or formed onto the pin to clamp the joint. This fastener usually is permanently installed. This fastener class includes such fasteners as "Hi-Shear" rivets, "Lockbolts", and "Cherrybucks".

Threaded Fasteners.—Fasteners in this category are considered to be any threaded part (or parts) that after assembly in a joint can be easily removed without damage to the fastener or to the material being joined. This classification includes bolts, screws, and a wide assortment of proprietary fasteners.

Special Fasteners.—As the name implies, this category of fastener is less commonly used in primary aircraft structure than the four categories listed above. Examples of such fastening systems are sleeves, inserts, panel fasteners, etc.

In the following 3-digit sections, descriptive information is presented relative to the establishment of design allowables in joints containing these four categories of fasteners. Following each such section are the various tables of joint allowables or associated information for computing joint allowables as described.

Tables 8.1.1(a) through (d) are fastener indexes that list the joint allowables tables for each fastener category. These indexes are provided to make it easier to locate the allowables table for a given fastener and sheet material combination. Each of the indexes generally is similarly structured in the following manner. The left-hand column describes the fastener by referring to the MS or NAS part number or to a vendor part number, when the fastener is not covered by either series. The second column contains the table number for the allowables table for each fastener. The fastener column has been so arranged that when protruding head and countersunk head fasteners are included in a given fastener index table, the protruding head tables appear first in the second column. The third column identifies generally the base material of the fastener. Generic terms usually are used, such as steel, aluminum, titanium, etc. The fourth column identifies the specific sheet or plate material.

It is recommended that Section 9.4.1 be reviewed in its entirety since it contains detailed information on the generation and analysis of joint data that results in the joint allowables tables contained in this section.

8.1.1.1 *Fastener Shear Strengths.*—Fastener shear strengths accepted and documented by the aerospace industry and government agencies are listed in Table 8.1.1.1. Some existing tables in MIL-HDBK-5 may reflect other values; however, new fastener proposals will be classified in accordance with the above-noted table.

TABLE 8.1.1(a). *Fastener Index for Solid Rivets*

Fastener Identification[a]	Table Number	Rivet Material	Sheet Material	Page No.
Rivet Hole Size	8.1.2(a)	...	...	8-10
Shear Strength of Solid Rivets	8.1.2(b)	...	...	8-10
Unit Bearing Strength	8.1.2.1(a)	...	...	8-11
Shear Strength Corection Factors	8.1.2.1(b)	Aluminum	...	8-12
NAS1198 (MC)[b]	8.1.2.1(c)	A-286	A-286	8-13
MS20427M (MC)	8.1.2.2(a)	Monel	AISI 301/302	8-14
MS20427M (D)[b]	8.1.2.2(b)	Monel	AISI 301/302	8-15
MS20426AD (D)	8.1.2.2(c)	Aluminum	Aluminum	8-16
MS20426D (D)	8.1.2.2(d)	Aluminum	Aluminum	8-17
MS20426DD (D)	8.1.2.2(e)	Aluminum	Aluminum	8-18
MS20426 (MC)	8.1.2.2(f)	Aluminum	Clad 2024-T42	8-19
MS20426B (MC)	8.1.2.2(g)	Aluminum	AZ31B-H24	8-20
MS20427M (MC)	8.1.2.2(h)	Monel	Com Pure Titanium	8-21
BRFS-D (MC)	8.1.2.2(i)	Aluminum	Clad 2024-T3	8-22
BRFS-AD (MC)	8.1.2.2(j)	Aluminum	Clad 2024-T3	8-23
BRFS-DD (MC)	8.1.2.2(k)	Aluminum	Clad 2024-T3	8-24
BRFS-T (MC)	8.1.2.2(l)	Ti-45Cb	Clad 7075-T6/Ti-6Al-4V	8-25
MS14218E	8.1.2.2(m)	Aluminum	Clad 2024-T3	8-26
NAS1097E (MC)	8.1.2.2(n)	Aluminum	Clad 2024-T3/7075-T6	8-27
MS14218AD (MC)	8.1.2.2(o)	Aluminum	Clad 2024-T3	8-28
MS14219E (MC)	8.1.2.2(p)	Aluminum	Clad 2024-T3	8-29
MS14219E (MC)	8.1.2.2(q)	Aluminum	Clad 7075-T6	8-30
MS20426E	8.1.2.2(r)	Aluminum	Clad 2024-T3	8-30a
MS20426E	8.1.2.2(s)	Aluminum	Clad 7075-T3	8-30b

[a]In some case entries in this table identify the subject matter in certain tables.
[b]MC, machine countersunk holes; D, dimpled holes.

TABLE 8.1.1(b). Fastener Index for Blind Fasteners

Fastener Identification	Table Number	Fastener Sleeve Material	Sheet or Plate Material	Page No.
	Protruding-head, Friction-Lock Blind Rivets			
CR 6636	8.1.3.1.1(a)	A-286	Various	8-32
MS20600M	8.1.3.1.1(b)	Monel	AISI 301	8-33
MS20600M	8.1.3.1.1(c)	Monel	Clad 2024-T3/7075-T6	8-34
MS20600AD and MS 20602AD	8.1.3.1.1(d)	Aluminum	Clad 2024-T3	8-35
MS20600B	8.1.3.1.1(e)	Aluminum	AZ31B-H24	8-36
	Protruding-head, Mechanical-Lock Blind Rivets			
NAS1398C	8.1.3.1.2(a)	A-286	Alloy Steel	8-37
CR 2643	8.1.3.1.2(a)	A-286	Alloy Steel	8-37
NAS1398 MS or MW	8.1.3.1.2(b)	Monel	AISI 301-½ Hard	8-38
NAS1398 MS or MW	8.1.3.1.2(c)	Monel	Clad 7075-T6	8-39
NAS1398B	8.1.3.1.2(d_1)	Aluminum	Clad 2024-T3	8-40
NAS1398D	8.1.3.1.2(d_1)	Aluminum	Clad 2024-T3	8-40
NAS1738B and NAS1738E	8.1.3.1.2(d_2)	Aluminum	Clad 2024-T3	8-41
NAS1398B	8.1.3.1.2(e)	Aluminum	AZ31B-H24	8-42
NAS1738B and NAS1738E	8.1.3.1.2(e)	Aluminum	AZ31B-H24	8-42
CR 2A63	8.1.3.1.2(f)	Aluminum	Clad 2024-T81	8-43
CR 4623	8.1.3.1.2(g)	A-286	Clad 7075-T6	8-44
CR 4523	8.1.3.1.2(h)	Monel	Clad 7075-T6	8-45
NAS1720KE and NAS1720KE ( ) L	8.1.3.1.2(i)	Aluminum	Clad 7075-T6	8-46
NAS1720C and NAS1720C ( ) L	8.1.3.1.2(j)	A-286	Clad 2024-T3	8-47
M7885/2	8.1.3.1.2(k)	Aluminum	Clad 7075-T6	8-48
M7885/6	8.1.3.1.2(l)	Aluminum	Clad 2024-T3	8-49
AF3243	8.1.3.1.2(m)	Aluminum	Clad 2024-T3	8-50
HC3213	8.1.3.1.2(n)	Aluminum	Clad 2024-T3	8-51
	Flush-head, Friction-Lock Blind Rivets			
CR 6626 (MC)[a]	8.1.3.2.1(a)	A-286	Various	8-52
MS20601M (MC)	8.1.3.2.1(b)	Monel	17-7PH (TH1050)	8-53
MS20601M (D)[a]	8.1.3.2.1(c)	Monel	AISI 301	8-54
MS20601M (MC)	8.1.3.2.1(d_1)	Monel	AISI 301-Ann	8-55
MS20601M (MC)	8.1.3.2.1(d_2)	Monel	AISI 301-¼ Hard	8-56
MS20601M (MC)	8.1.3.2.1(d_3)	Monel	AISI 301-½ Hard	8-57
MS20601M (MC)	8.1.3.2.1(e)	Monel	7075-T6	8-58
MS20601AD and MS20603AD (MC)	8.1.3.2.1(f)	Aluminum	Clad 2024-T3	8-59
MS20601B (MC)	8.1.3.2.1(g)	Aluminum	AZ31B-H24	8-60

TABLE 8.1.1(b). Fastener Index for Blind Fasteners—Continued

Fastener Identification	Table Number	Fastener Sleeve Material	Sheet or Plate Material	Page No.
Flush-head, Mechanical-Lock Spindle Blind Rivets				
NAS1399C (MC)	8.1.3.2.2(a)	A-286	Alloy Steel	8-61
CR 2642 (MC)	8.1.3.2.2(a)	A-286	Alloy Steel	8-61
NAS1399 MS or MW (MC)	8.1.3.2.2(b)	Monel	AISI 301-½ Hard	8-62
NAS1291C (MC)	8.1.3.2.2(c)	A-286	Clad 7075-T6	8-63
NAS1399 MS or MW (MC)	8.1.3.2.2(d)	Monel	Clad 7075-T6	8-64
NAS1921M (MC)	8.1.3.2.2(e)	Monel	Clad 7075-T6	8-65
CR 2A62 (MC)	8.1.3.2.2(f)	Aluminum	Clad 2024-T81	8-66
NAS1921B (MC)	8.1.3.2.2(g)	Aluminum	Clad 7075-T6	8-67
NAS1399B (MC)	8.1.3.2.2(h)	Aluminum	Clad 2024-T3	8-68
NAS1399D (MC)	8.1.3.2.2(h)	Aluminum	Clad 2024-T3	8-68
NAS1739B and NAS1379E (MC)	8.1.3.2.2(i)	Aluminum	Clad 2024-T3	8-69
NAS1739B and NAS1739E (D)	8.1.3.2.2(i)	Aluminum	Clad 2024-T3	8-69
NAS1399B (MC)	8.1.3.2.2(j)	Aluminum	AZ31B-H24	8-70
NAS1739B and NAS1739E (MC)	8.1.3.2.2(j)	Aluminum	AZ31B-H24	8-70
CR 4622 (MC)	8.1.3.2.2(k)	A-286	Clad 7075-T6	8-71
CR 4522 (MC)	8.1.3.2.2(l)	Monel	Clad 7075-T6/T651	8-72
NAS1721KE and NAS1721KE ( )L (MC)	8.1.3.2.2(m)	Aluminum	Clad 2024-T3	8-73
NAS1721C and NAS1721C ( )L (MC)	8.1.3.2.2(n)	A-286	Clad 7075-T6	8-74
M 7885/3 (MC)	8.1.3.2.2(o)	Aluminum	Clad 2024-T3	8-75
M 7885/7 (MC)	8.1.3.2.2(p)	Aluminum	Clad 2024-T3	8-76
HC3212 (MC)	8.1.3.2.2(q)	Aluminum	Clad 2024-T3	8-77
MBC 4807 and MBC 4907	8.1.3.2.2(r)	Aluminum	Clad 2024-T3	8-77a
MBC 4801 and MBC 4901	8.1.3.2.2(s)	Aluminum	Clad 2024-T3	8-77b

TABLE 8.1.1(b). *Fastener Index for Blind Fasteners—Continued*

Fastener Identification	Table Number	Fastener Sleeve Material	Sheet or Plate Material	Page No.
	Flush-head Blind Bolts			
MS21140 (MC)	8.1.3.2.3(a)	A-286	Clad 7075-T6/T651	8-78
MS90353 (MC)	8.1.3.2.3(b_1)	Alloy Steel	Clad 2024-T3/T351	8-79
MS90353 (MC)	8.1.3.2.3(b_2)	Alloy Steel	Clad or Bare 7075-T6 or T651	8-80
FF-200, FF-260 and FF-312 (MC)	8.1.3.2.3(c)	Alloy Steel	Clad 2024-T42/ 7075-T6	8-81
NS 100 (MC)	8.1.3.2.3(d)	Alloy Steel	Clad 7075-T6	8-82
SSHFA-200 and SSHFA-260(MC)	8.1.3.2.3(e)	Aluminum	Clad 2024-T42/ 7075-T6	8-83
PLT-150 (MC)	8.1.3.2.3(f)	Alloy Steel	Clad 7075-T6/T651	8-84
NAS1670L (MC)	8.1.3.2.3(g)	Alloy Steel	Clad 7075-T6/T651	8-85
NAS1674L (MC)	8.1.3.2.3(h)	Aluminum	Clad 7075-T6	8-86

[a]MC, machine countersunk holes; D, dimpled holes.

TABLE 8.1.1(c). *Fastener Index for Swaged-Collar/Upset-Pin Fasteners*

Fastener Identification	Table Number	Fastener Pin Material	Sheet or Plate Material	Page No.
Ultimate Single-Shear and Tensile Strengths	8.1.4	Alloy Steel and Alum.	...	8-88
CSR 925	8.1.4.1(a)	Titanium	Clad 7075-T6	8-89
CSR 925	8.1.4.1(b)	Titanium	Clad 2024-T3	8-90
NAS1436-NAS1442 (MC)[a]	8.1.4.2(a)	Alloy Steel	Clad 7075-T6/T651	8-91
NAS7024-NAS7032 (MC)	8.1.4.2(b)	Alloy Steel	Clad 7075-T6/T651	8-92
CSR 924 (MC)	8.1.4.2(c)	Titanium	Clad 7075-T6	8-93
CSR 924 (MC)	8.1.4.2(d)	Titanium	Clad 2024-T3	8-94
HSR 201 (MC)	8.1.4.2(e)	A-286	Clad 7075-T6	8-95
HSR 101 (MC)	8.1.4.2(f)	Titanium	Clad 7075-T6	8-96
GPL 3SC-V (MC)	8.1.4.2(g)	Titanium	Clad 7075-T6	8-97
GPL 3SC-V (MC)	8.1.4.2(h)	Titanium	Clad 2024-T3	8-98
LGPL 2SC-V (MC)	8.1.4.2(i)	Titanium	Clad 7075-T6	8-99
LGPL 2SC-V (MC)	8.1.4.2(j)	Titanium	Clad 2024-T3	8-100

[a]MC, machine countersunk holes.

TABLE 8.1.1(d). *Fastener Index for Threaded Fasteners*

Fastener Identification[a]	Table Number	Fastener Sleeve Material	Sheet	Page No.
Single Shear Strength	8.1.5(a)	Steel	...	8-103
Tensile Strength	8.1.5(b_1)	Steel	...	8-104
Tensile Strength	8.1.5(b_2)	...	...	8-105
Unit Bearing Strength	8.1.5.1	Alloy Steel	...	8-106
AN 509 Screws (MC)[b]	8.1.5.2(a_1)	Alloy Steel	Clad 2024-T3	8-107
AN 509 Screws (MC)	8.1.5.2(a_2)	CRES	Clad 7075-T6	8-108
PBF 11 (MC)	8.1.5.2(b)	Alloy Steel	Ti-6Al-4V	8-109
TL 100 (MC)	8.1.5.2(c)		Clad 7075-T6	8-110
TLV 100 (MC)	8.1.5.2(d)	Titanium	Clad 7075-T6	8-111
HPB-V (MC)	8.1.5.2(e)	Titanium	Clad 7075-T6	8-112
KLBHV with KFN 600 (MC)	8.1.5.2(f)	Titanium	Clad 7075-T6	8-113
HL-61-70 (MC)	8.1.5.2(g)	CRES	Clad 7075-T6	8-114
HL-719-79 (MC)	8.1.5.2(h)	Alloy Steel	Clad 7075-T6	8-115
HL-11 (MC)	8.1.5.2(i)	Titanium	Clad 7075-T6	8-116
HL-911 (MC)	8.1.5.2(j)	Titanium	Clad 7075-T6	8-117
NAS4452S and KS 100-FV with NAS4445DD (MC)	8.1.5.2(k)	Alloy Steel or Titanium	Clad 7075-T6	8-118
HPG-V (MC)	8.1.5.2(l)	Titanium	Clad 7075-T6	8-119
NAS4452V with NAS4445 DD (MC)	8.1.5.2(m)	Titanium	Clad 7075-T6	8-120
HL18Pin, HL70 Collar (MC)	8.1.5.2(n)	Alloy Steel	Clad 7075-T6	8-121
HL19 Pin, HL70 Collar (MC)	8.1.5.2(o)	Alloy Steel	Clad 7075-T6	8-122

[a]In some cases entreis in this table identify the subject matter in certain tables.
[b]MC, machine countersunk holes; D, dimpled holes.

TABLE 8.1.1(e). *Fastener Index for Special Fasteners*

Fastener Identification	Table Number	Fastener Pin Material	Sheet or Plate Material	Page No.
ACRES Sleeves	...	A-286	Clad 7075-T6	8-123
MIL-B-8831/4 (MC)[a]	8.1.6.2(a)	Steel Pin, Aluminum Sleeve	Clad 7075-T6	8-124
MIL-B-8831/4 (MC)	8.1.6.2(b)	Steel Pin, Aluminum Sleeve	Clad 2024-T3	8-125

[a]MC, machine countersunk holes.

TABLE 8.1.1.1. *Fastener Shear Strengths*

F_{su}, ksi	Examples of Current Alloys Which Meet Level[a]	Current Usage		
		Driven Rivets	Blind Fasteners	Solid Shank Fasteners
28	5056	X	X	
30	2117	X	X	
34	2017	X	X	
36	2219	X	X	
38	2017	X	X	
41	2024 and 7050-T73	X		
43	7050-T731	X	X	X
46	7075		X	
49	Monel	Undriven		
50	Ti/Cb	X		
55	Monel		X	
75	Alloy Steel and CRES		X	X
78	A-286			X
90	A-286	Undriven		
95	Alloy Steel, A-286, Ti-6Al-4V	X	X	X
108	Alloy Steel and Ti-6Al-2Sn			X
110	A-286			X
112	Alloy Steel		X	X
125	Alloy Steel and CRES			X
132	Alloy Steel			X
145	MP35N			X
156	Alloy Steel			X
180	Alloy Steel			X

[a]Different tempers and thermal treatments are used to obtain desired fastener shear strengths.

8.1.2 SOLID RIVETS.—The recommended diameter dimensions of the upset head on solid rivets shall be at least 1.3 times the nominal shank diameter except for 7050 rivets which shall be at least 1.4 times the nominal shank diameter. Head heights shall be a minimum of 0.3 diameter. Shear strengths for driven rivets may be based on areas corresponding to the nominal hole diameter provided that the nominal hole diameter is not larger than the values listed in Table 8.1.2(a). If the nominal hole diameter is larger than the listed value, the listed value shall be used. Shear strength values for solid rivets of a number of rivet materials are given in Table 8.1.2(b).

8.1.2.1 *Protruding-Head Solid Rivet Joints.*— The unit load at which shear or bearing type of failure occurs is calculated separately and the lower of the two governs the design.

The design bearing stress for various materials at both room and elevated temperatures is given in the strength properties stated for each alloy or group of alloys and is applicable to riveted joints wherein cylindrical holes are used and where t/D is greater than or equal to 0.18; where t/D is less than 0.18, tests to substantiate yield and ultimate bearing strengths must be performed. These bearing stresses are applicable only for the design of rigid joints where there is no possibility of relative motion of the parts joined without deformation of such parts. Design bearing stresses at low temperatures will be higher than those specified for room temperature; however, no quantitative data are available.

For convenience, "unit" sheet bearing strengths for rivets, based on a bearing stress of 100 ksi and nominal hole diameters, are given in Table 8.1.2.1(a).

In computing protruding-head rivet design shear strengths, the shear strength values obtained from Table 8.1.2(b) should be multiplied by the correction factors given in Table 8.1.2.1(b). This compensates for the reduction in rivet shear strength resulting from high bearing stresses on the rivet at t/D ratios less than 0.33 for single-shear joints and 0.67 for double-shear joints.

For those rivet material sheet material combinations where test data shows the above to be unconservative or for rivet materials other than those shown in Table 8.1.2(b), joint allowables should be established by test in accordance with Section 9.4. From such tests tabular presentation of ultimate load and yield load allowables are made.

Unless otherwise specified, yield load is defined in Section 9.4.1.3.3 as the load which results in a joint permanent set equal to 0.04D, where D is the decimal equivalent of the hole diameter defined in Table 9.4.1.2(a).

Table 8.1.2.1(c) provides ultimate and yield strength data on protruding-head A-286 solid rivets in aged A-286 sheet, for a variety of conditions of exposure.

8.1.2.2 *Flush-Head Solid Rivet Joints.*— Tables 8.1.2.2(a) through (q) contain joint allowables for various flush-head solid rivet/sheet material combinations. The allowable ultimate loads were established from test data using the average ultimate test load divided by a factor of 1.15. (See Section 9.4 for possible variations.) This factor is not applicable to shear strength cutoff values. Shear strength cutoff values may be either the procurement specification shear strength (S value) of the fastener, or if no specification exists, a statistical value determined from test results as described in Section 9.4.

Yield load allowables are established from test data. Unless otherwise specified, the yield load is defined in Section 9.4.1.3.3 as the load which results in a joint permanent set equal to 0.04D, where D is the decimal equivalent of the hole diameter defined in Table 9.4.1.2(a).

For machine countersunk joints, the sheet gage specified in the tables is that of the countersunk sheet. When the noncountersunk sheet is thinner than the countersunk sheet, the bearing allowable for the noncountersunk sheet-fastener combination should be computed, compared to the table value, and the lower of the two values selected. Increased attention should be paid to detail design in cases where $t/D < 0.25$ because of possibly greater incidence of difficulty in service life.

TABLE 8.1.2(a). *Standard Rivet-Hole Drill Sizes and Nominal Hole Diameters*

Rivet Size, in.	1/16	3/32	1/8	5/32	3/16	1/4	5/16	3/8
Drill No.	51	41	30	21	11	F	P	W
Nominal Hole Diameter, in.	0.067	0.096	0.1285	0.159	0.191	0.257	0.323	0.386

TABLE 8.1.2(b). *Shear Strength of Solid Rivets*

Rivet Diameter, in.	1/16	3/32	1/8	5/32	3/16	1/4	5/16	3/8
Designation	Shear Strength, lbs[a]							
Rivet Material:								
5056-H321 F_{su} = 28 ksi[b] ..... B	99	203	363	556	802	1450	2295	3275
2117-T3 F_{su} = 30 ksi[b] ..... AD	106	217	388	596	862	1555	2460	3510
2017-T31 F_{su} = 34 ksi[b] ..... D	120	247	442	675	977	1765	2785	3980
2017-T3 F_{su} = 38 ksi[b] ..... D	134	275	494	755	1090	1970	3115	4445
2024-T31 F_{su} = 41 ksi[b] ..... DD	145	296	531	814	1175	2125	3360	4800
7050-T73 F_{su} = 41 ksi[c] ..... E, KE	145	296	531	814	1175	2125	3360	4800
7050-T731 F_{su} = 43 ksi[b] .... E, KE	152	311	558	854	1230	2230	3525	5030
Monel F_{su} = 49 ksi	173	355	635	973	1405	2540	4015	5735
Ti-45Cb F_{su} = 53 ksi	187	384	687	1050	1520	2750	4340	6200
A-286 F_{su} = 90 ksi	317	651	1170	1790	2580	4670	7370	10500

[a]Based on nominal hole diameter specified in Table 8.1.2(a).

[b]Values are for the as driven condition, on a probability basis (B values). The third digit (1) of the temper designation indicates recognition of strengthening derived from driving.

[c]Undriven S value; driven B value has not been demonstrated.

TABLE 8.1.2.1(a). *Unit Bearing Strength of Sheet on Rivets, F_{br} = 100 ksi*

Sheet thickness, in.	Unit Bearing Strength for Indicated Rivet Diameter, lbs							
	1/16	3/32	1/8	5/32	3/16	1/4	5/16	3/8
0.012	80	...	...	...	...	...	...	...
0.016	107	...	...	...	...	...	...	...
0.018	121	173	...	...	...	...	...	...
0.020	134	192	...	...	...	...	...	...
0.025	168	240	321	...	...	...	...	...
0.032	214	307	411	509	...	...	...	...
0.036	241	346	462	572	688	...	...	...
0.040	268	384	514	636	764	...	...	...
0.045	302	432	578	716	860	...	...	...
0.050	335	480	642	795	955	1285	...	...
0.063	422	605	810	1002	1203	1619	2035	...
0.071	476	682	912	1129	1356	1825	2293	2741
0.080	536	768	1028	1272	1528	2056	2584	3088
0.090	603	864	1156	1431	1719	2313	2907	3474
0.100	670	960	1285	1590	1910	2570	3230	3860
0.125	838	1200	1606	1988	2388	3212	4038	4825
0.160	1072	1536	2056	2544	3056	4112	5168	6176
0.190	1273	1824	2442	3021	3629	4883	6137	7334
0.250	1670	2400	3210	3975	4775	6425	8075	9650

TABLE 8.1.2.1(b). *Shear Strength Correction Factors for Solid Protruding Head Rivets*[a]

Rivet Diameter, in.	1/16	3/32	1/8	5/32	3/16	1/4	5/16	3/8
	Single-Shear Rivet Strength Factors							
Sheet thickness, in.:								
0.016	0.964	...	...	...	...	...	...	...
0.018	0.981	0.912	...	...	...	...	...	...
0.020	0.995	0.933	...	...	...	...	...	...
0.025	1.000	0.970	0.920	...	...	...	...	...
0.032	...	1.000	0.964	0.925	...	...	...	...
0.036	...	...	0.981	0.946	0.912	...	...	...
0.040	...	...	0.995	0.964	0.933	...	...	...
0.045	...	...	1.000	0.981	0.953	...	...	...
0.050	...	...	...	0.995	0.970	0.920	...	...
0.063	...	...	...	1.000	1.000	0.961	0.922	...
0.071	...	...	...	...	...	0.979	0.944	0.909
0.080	...	...	...	...	...	0.995	0.964	0.933
0.090	...	...	...	...	...	1.000	0.981	0.953
0.100	...	...	...	...	...	...	0.995	0.972
0.125	...	...	...	...	...	...	1.000	1.000
	Double-Shear Rivet Strength Factors							
Sheet thickness, in.:								
0.016	0.687	...	...	...	...	...	...	...
0.018	0.744	0.518	...	...	...	...	...	...
0.020	0.789	0.585	...	...	...	...	...	...
0.025	0.870	0.708	0.545	...	...	...	...	...
0.032	0.941	0.814	0.687	0.560	...	...	...	...
0.036	0.969	0.857	0.744	0.630	0.518	...	...	...
0.040	0.992	0.891	0.789	0.687	0.585	...	...	...
0.045	1.000	0.924	0.834	0.744	0.653	...	...	...
0.050	...	0.951	0.870	0.789	0.708	0.545	...	...
0.063	...	1.000	0.937	0.872	0.808	0.679	0.550	...
0.071	...	...	0.966	0.909	0.852	0.737	0.622	0.508
0.080	...	...	0.992	0.941	0.891	0.789	0.687	0.585
0.090	...	...	1.000	0.969	0.924	0.834	0.744	0.653
0.100	...	...	...	0.992	0.951	0.870	0.789	0.708
0.125	...	...	...	1.000	1.000	0.935	0.870	0.805
0.160	...	...	...	...	...	0.992	0.941	0.891
0.190	...	...	...	...	...	1.000	0.981	0.939
0.250	...	...	...	...	...	...	1.000	1.000

[a]Sheet thickness is that of the thinnest sheet in single-shear joints and the middle sheet in double-shear joints. Values based on tests of aluminum rivets, Reference 8.1(a).

TABLE 8.1.2.1(c). Static Joint Strength of Protruding Head A-286 Solid Rivets in A-286 Alloy Sheet at Various Temperatures

Rivet Type	NAS1198 (F_{su} = 90 ksi)								
Sheet Material	A-286, solution treated and aged, F_{tu} = 140 ksi								
Temperature	Room Temperature			1200 F, Stabilized 15 Minutes			1200 F, Rapid Heating in 20 Seconds, Tested in 15 Seconds		
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)
Sheet thickness, in.:	Ultimate Strength[a], lbs.								
0.020	478	...	...	331	...	...	470[b]	...	...
0.025	590	740	...	426	626	...	587[b]	726[b]	...
0.032	745	932	1132	560	801	962	752[b]	930[b]	1117[b]
0.040	923	1152	1397	682	1002	1204	783	1164[b]	1397[b]
0.050	1023	1428	1677	...	1044	1505	...	1198	1729[b]
0.063	1131	1578	1821	...	...	1507	...	...	...
0.071	1170	1660	1909	...	...	...	...	...	...
0.080	...	1752	2008	...	...	...	...	...	...
0.090	...	1790	2118	...	...	...	...	...	...
0.100	...	...	2229	...	...	...	...	...	...
0.125	...	...	2504	...	...	...	...	...	...
0.160	...	...	2580	...	...	...	...	...	...
Rivet shear strength[c]	1170	1790	2580	682	1044	1507	783	1198	1729
Sheet thickness, in.:	Yield Strength[a,d], lbs.								
0.020	447	...	...	300	...	...	300	...	...
0.025	590	695	...	374	464	...	374	464	...
0.032	745	932	974	479	593	713	478	593	712
0.040	867	1152	1167	598	741	890	598	740	889
0.050	938	1331	1407	...	925	1112	...	924	1110
0.063	1031	1447	1649	...	...	1400	...	...	...
0.071	1089	1518	1723	...	...	...	...	...	...
0.080	...	1597	1806	...	...	...	...	...	...
0.090	...	1686	1898	...	...	...	...	...	...
0.100	...	...	1990	...	...	...	...	...	...
0.125	...	...	2221	...	...	...	...	...	...
0.160	...	...	2543	...	...	...	...	...	...

[a]Test data from which the yield and ultimate strengths were derived can be found in reference 8.1.2.1.
[b]Yield value is less than 2/3 of indicated ultimate.
[c]Rivet shear strength is documented in NAS1198 as 90 ksi.
[d]Permanent set at yield load: 0.005 inch.
Note: Because of difficulties encountered upsetting countersunk head rivets in thin A-286 sheet, such conditions should be avoided in design.

TABLE 8.1.2.2(a). *Static Joint Strength of 100° Flush Head Monel Solid Rivets in Machine-Countersunk Stainless Steel Sheet*

Rivet Type	MS20427M (F_{su} = 49 ksi)									
Sheet Material	AISI 302-Annealed			AISI 301-¼ Hard			AISI 301-½ Hard AISI 301-Full Hard			
Rivet Diameter, in.	1/8	5/32	3/16	1/8	5/32	3/16	3/32	1/8	5/32	3/16
(Nominal Hole Diameter, in.)	(0.1285)	(0.159)	(1.191)	(0.1285)	(0.159)	(0.191)	(0.096)	(0.1285)	(0.159)	(0.191)
	Ultimate Strength, lbs									
Sheet thickness, in.:										
0.040	439[a]	...	...	439	...	...	251	439	...	...
0.050	526[a]	[b] 673[a]	...	468	[b] 673	...	322	447	[b] 673	...
0.063	635[a]	820[a]	[b] ...	595	732	[b] ...	355	538	688	[b] ...
0.071	...	915[a]	1110[a]	635	830	990	...	615	741	984
0.080	...	973[a]	1246[a]	[b] ...	936	1118	[b] ...	635	850	995 [b]
0.090	...	...	1380[a]	...	973	1255	...	...	973	1132
0.100	...	...	1400	...	...	1400	...	...	...	1280
0.125	...	...	...	...	...	...	...	...	...	1400
Rivet shear strength[c]	635	973	1400	635	973	1400	355	635	973	1400
	Yield Strength[d], lbs									
Sheet thickness, in.:										
0.040	259	...	...	368	...	...	212	324	...	...
0.050	324	402	...	442	570	...	293	360	498	...
0.063	408	506	...	492	686	...	355	480	557	...
0.071	...	570	685	561	714	958	...	561	630	780
0.080	...	643	771	...	764	1012	...	635	765	848
0.090	...	...	865	...	893	1062	...	...	893	1000
0.100	...	...	965	...	...	1160	...	...	...	1160
0.125	...	...	...	...	...	...	...	...	...	1400
Head height (ref.), in.	0.048	0.061	0.077	0.048	0.061	0.077	0.042	0.048	0.061	0.077

[a]Yield value is less than 2/3 of the indicated ultimate strength value.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Rivet shear strength is documented in MS20427M.
[d]Permanent set at yield load: 0.005 inch.

TABLE 8.1.2.2(b). Static Joint Strength of 100° Flush Head Monel Solid Rivets in Dimpled Stainless Steel Sheet

Rivet Type	MS20427M (F_{su} = 49 ksi)										
Sheet Material	AISI 302 - annealed				AISI 301 - 1/4 hard			AISI 301 - 1/2 hard			
Rivet Diameter, in.	1/8	5/32	3/16	1/4	1/8	5/32	3/16	3/32	1/8	5/32	3/16
(Nominal Hole Diameter, in.)	(0.1285)	(0.159)	(0.191)	(0.257)	(0.1285)	(0.159)	(0.191)	(0.096)	(0.1285)	(0.159)	(0.191)
	Ultimate Strength, lbs.										
Sheet thickness, in.:											
0.020	348	...	...	...	497	...	...	348	497	...	...
0.025	441	536	...	...	595	766	...	355	595	766	...
0.032	568	698	846	...	635	931	1163	...	635	931	1163
0.040	635	884	1046	1370	...	973	1382	...	...	973	1382
0.050	...	973	1320	1730	...	...	1405	...	...	...	1405
0.063	...	...	1405	2240	...	...	...	...	...	...	...
0.071	...	...	...	2490	...	...	...	...	...	...	...
0.080	...	...	...	2540	...	...	...	...	...	...	...
Rivet shear strength[a]	635	973	1405	2540	635	973	1405	355	635	973	1405
	Yield Strength[b], lbs.										
Sheet thickness, in.:											
0.020	336	...	...	...	449	...	...	329	449	...	...
0.025	427	518	...	...	533	681	...	355	533	681	...
0.032	550	679	801	...	635	842	1049	...	635	842	1049
0.040	635	856	1020	1326	...	973	1252	...	...	973	1252
0.050	...	973	1280	1678	...	...	1405	...	...	...	1405
0.063	...	...	1405	2140	...	...	...	...	...	...	...
0.071	...	...	...	2420	...	...	...	...	...	...	...
0.080	...	...	...	2540	...	...	...	...	...	...	...
Head height (max.), in.	0.048	0.061	0.077	0.103	0.048	0.061	0.077	0.042	0.048	0.061	0.077

[a]Rivet shear strength from Table 8.1.2(b).
[b]Permanent set at yield load: 0.005 inch.

TABLE 8.1.2.2(c). Static Joint Strength of 100° Flush Head Aluminum Alloy (2117-T3) Solid Rivets in Dimpled Aluminum Alloy Sheet[a,b]

Rivet Type	MS20426AD (F_{su} = 30 ksi)								
Sheet Material	2024-T3 2024-T42 2024-T62 2024-T81		2024-T3 2024-T42		2024-T62 2024-T81		2024-T86 7075-T6		
Rivet Diameter, in.	3/32	1/8	5/32	3/16	5/32	3/16	1/8	5/32	3/16
(Nominal Hole Diameter, in.)	(0.096)	(0.1285)	(0.159)	(0.191)	(0.159)	(0.191)	(0.1285)	(0.159)	(0.191)
	Ultimate Strength, lbs.								
Sheet thickness, in.:									
0.016	177	...	...	...	...	...	...	...	...
0.020	209	299	...	...	...	...	302	...	...
0.025	217	360	474	...	462	...	383	462	...
0.032	...	388	568	722	596	725	388	596	725
0.040	...	...	596	839	...	862	...	...	862
0.050	...	...	...	862	...	...	...	...	...
Rivet shear strength[c]	217	388	596	862	596	862	388	596	862
	Yield Strength[d], lbs.								
Sheet thickness, in.:									
0.016	154	...	...	...	...	...	...	...	...
0.020	184	257	...	...	...	...	257	...	...
0.025	209	315	324	...	324	...	315	410	...
0.032	...	367	430	512	430	512	367	525	640
0.040	...	...	506	644	...	644	...	...	782
0.050	...	...	...	757	...	...	...	...	...
Head height (max.),in.	0.036	0.042	0.055	0.070	0.055	0.070	0.042	0.055	0.070

[a]These allowables apply to double dimpled sheets and to the upper sheet dimpled into a machine-countersunk lower sheet. Sheet gage is that of the thinnest sheet for double dimpled joints and of the upper dimpled sheet for dimpled, machine-countersunk joints. The thickness of machine-countersunk sheet must be at least one tabulated gage thicker than the upper sheet. In no case shall allowables be obtained by extrapolation for gages other than those shown.
[b]Test data from which the yield strengths listed were derived and can be found in Reference 8.1.2.2.
[c]Rivet shear strength from Table 8.1.2(b).
[d]Permanent set a yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.2.2(d). Static Joint Strength of 100° Flush Head Aluminum Alloy (2017-T3) Solid Rivets in Dimpled Aluminum Alloy Sheet[a,b]

Rivet Type	MS20426D (F_{su} = 38 ksi)								
Sheet Material	2024-T3 and 2024-T42			2024-T86 and 7075-T6			2024-T62 and 2024-T81		
Rivet Diameter, in.	5/32	3/16	1/4	5/32	3/16	1/4	5/32	3/16	1/4
(Nominal Hole Diameter, in.)	(0.159)	(0.191)	(0.257)	(0.159)	(0.191)	(0.257)	(0.159)	(0.191)	(0.257)
	Ultimate Strength, lbs.								
Sheet thickness, in.:									
0.025	419	...	...	530	...	...	419	...	...
0.032	600	681	...	672	822	...	600	681	...
0.040	738	905	845	755	1000	1108	738	905	1108
0.050	755	1090	1332	...	1090	1508	755	1090	1508
0.063	...	...	1695	...	...	1803	...	...	1803
0.071	...	...	1853	...	...	1930	...	...	1930
0.080	...	...	1970	...	...	1970	...	...	1970
Rivet shear strength[c]	755	1090	1970	755	1090	1970	755	1090	1970
	Yield Strength[d], lbs.								
Sheet thickness, in.:									
0.025	336	...	...	450	...	...	336	...	...
0.032	483	546	...	581	...	...	483	546	...
0.040	589	730	845	675	705	978	589	730	845
0.050	681	888	1187	...	867	1508	681	888	1187
0.063	...	...	1415	...	1007	1803	...	...	1415
0.071	...	...	1656	...	...	1930	...	...	1656
0.080	...	...	1870	...	...	1970	...	...	1870
Head height (max.), in.	0.055	0.070	0.095	0.055	0.070	0.095	0.055	0.070	0.095

[a]These allowables apply to double dimpled sheets and to the upper sheet dimpled into a machine-countersunk lower sheet. Sheet gage is that of the thinnest sheet for double dimpled joints and of the upper dimpled sheet for dimpled, machine-countersunk joints. The thickness of machine-countersunk sheet must be at least one tabulated gage thicker than the upper sheet. In no case shall allowables be obtained by extrapolation for gages other than those shown.
[b]Test data from which the yield strengths listed were derived and can be found in Reference 8.1.2.2.
[c]Rivet shear strength from Table 8.1.2(b).
[d]Permanent set a yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.2.2(e). *Static Joint Strength of 100° Flush Head Aluminum Alloy (2024-T31) Solid Rivets in Dimpled Aluminum Alloy Sheet*[a,b]

Rivet Type	MS20426DD (F_{su} = 41 ksi)					
Sheet Material	2024-T3 2024-T42		2024-T62 2024-T81		2024-T86 7075-T6	
Rivet Diameter, in.	3/16	1/4	3/16	1/4	3/16	1/4
(Nominal Hole Diameter, in.)	(0.191)	(0.257)	(0.191)	(0.257)	(0.191)	(0.257)
	Ultimate Strength, lbs.					
Sheet thickness, in.:						
0.032	744	...	786	...	786	...
0.040	941	879	982	1300	982	1300
0.050	1110	1359	1152	1705	1152	1705
0.063	1175	1727	1175	2010	1175	2010
0.071	...	1883	...	2125	...	2125
0.080	...	2025	...	...	...	...
0.090	...	2125	...	...	...	...
Rivet shear strength[c]	1175	2125	1175	2125	1175	2125
	Yield Strength[d], lbs.					
Sheet thickness, in.:						
0.032	582	...	649	...	786	...
0.040	666	879	816	962	982	978
0.050	738	1308	961	1308	1152	1543
0.063	925	1564	1068	1564	1175	1958
0.071	...	1711	...	1711	...	2125
0.080	...	1928	...	...	...	...
0.090	...	2121	...	...	...	...
Head height (max.), in.	0.070	0.095	0.070	0.095	0.070	0.095

[a]These allowables apply to double dimpled sheets and to the upper sheet dimpled into a machine-countersunk lower sheet. Sheet gage is that of the thinnest sheet for double dimpled joints and of the upper dimpled sheet for dimpled, machine-countersunk joints. The thickness of machine-countersunk sheet must be at least one tabulated gage thicker than the upper sheet. In no case shall allowables be obtained by extrapolation for gages other than those shown.
[b]Test data from which the yield strengths listed were derived and can be found in Reference 8.1.2.2.
[c]Rivet shear strength from Table 8.1.2(b).
[d]Permanent set a yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.2.2(f). *Static Joint Strength of 100° Flush Head Aluminum Alloy Solid Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	MS20426AD (2117-T3) (F_{su} = 30 ksi)				MS20426D (2017-T3) (F_{su} = 38 ksi)			MS20426DD (2024-T31) (F_{su} = 41 ksi)	
Sheet Material	Clad 2024-T42								
Rivet Diameter, in. (Nominal Hole Diameter, in.)	3/32 (0.096)	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	5/32 (0.159)	3/16 (0.191)	1/4 (0.257)	3/16 (0.191)	1/4 (0.257)
	Ultimate Strength[a], lbs								
Sheet thickness, in.:									
0.032	178	...	...	...	...	...	...	...	...
0.040	193	[c] 309	...	...	...	...	...	...	...
0.050	206	340	[c] 479	...	580[b]	...	...	...	...
0.063	216	363	523	[c] 705	657[b]	[c] 859[b]	...	886	...
0.071	...	373	542	739	[c] 690	917[b]	[c] ...	942	[c] ...
0.080	...	...	560	769	720	969[b]	...	992	...
0.090	...	...	575	795	746	1015	1552[b]	1035	1647[b]
0.100	...	...	...	818	...	1054	1640[b]	[c] 1073	1738[b] [c]
0.125	...	...	...	853	...	1090	1773	1131	1877
0.160	...	...	...	...	...	...	1891	...	2000
0.190	...	...	...	...	...	...	1970	...	2084
Rivet shear strength[d]	217	388	596	862	755	1090	1970	1175	2125
	Yield Strength[a,e], lbs								
Sheet thickness, in.:									
0.032	132	...	...	...	...	...	...	...	...
0.040	153	231	...	...	...	...	...	...	...
0.050	188	261	321	...	345	...	...	...	...
0.063	213	321	402	471	401	515	...	614	...
0.071	...	348	453	538	481	557	...	669	...
0.080	...	...	498	616	562	623	...	761	...
0.090	...	...	537	685	633	746	861	842	1053
0.100	...	...	...	745	...	854	1017	913	1115
0.125	...	...	...	836	...	1018	1313	1021	1357
0.160	...	...	...	...	...	...	1574	...	1694
0.190	...	...	...	...	...	...	1753	...	1925
Head height (ref.), in.	0.036	0.042	0.055	0.070	0.055	0.070	0.095	0.070	0.095

[a]Test data from which the yield and ultimate strength listed were derived can be found in Reference 8.1.2.2.
[b]Yield value is less than 2/3 of the indicated ultimate strength value.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Rivet shear strength is documented in MS20426.
[e]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.2.2(g). *Static Joint Strength of 100° Flush Head Aluminum Alloy (5056-H321) Solid Rivets in Machine-Countersunk Magnesium Alloy Sheet*

Rivet Type	MS20426B (F_{su} = 28 ksi)				
Sheet Material	AZ31B-H24				
Rivet Diameter, in.	3/32	1/8	5/32	3/16	1/4
(Nominal Hole Diameter, in.)	(0.096)	(0.1285)	(0.159)	(0.191)	(0.257)
	Ultimate Strength, lbs				
Sheet thickness, in.:					
0.032	172[a]	...	...	...	...
0.040	180	[b] 304[a]	...	...	...
0.050	190	318	[b] 467[a]	...	...
0.063	203	337	490	[b] 679[a]	...
0.071	...	348	503	697[a]	[b] ...
0.080	...	360	519	715	...
0.090	...	363	536	737	1244
0.100	...	...	554	757	1271 [b]
0.125	...	...	556	802	1343
0.160	...	...	...	...	1440
0.190	...	...	...	...	1450
Rivet shear strength[c]	203	363	556	802	1450
	Yield Strength[d], lbs				
Sheet thickness, in.:					
0.032	104	...	...	...	...
0.040	127	172	...	...	...
0.050	152	214	268	...	...
0.063	186	259	334	409	...
0.071	...	287	369	459	...
0.080	...	318	406	504	...
0.090	...	353	450	555	792
0.100	...	...	491	606	856
0.125	...	...	556	735	1030
0.160	...	...	...	...	1273
0.190	...	...	...	...	1450
Head height (ref.), in.	0.036	0.042	0.055	0.070	0.095

[a]Yield value is less than 2/3 of the indicated ultimate strength value.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Rivet shear strength is documented in MS20426.
[d]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.2.2(h). *Static Joint Strength of 100° Flush Head Monel Solid Rivets in Machine-Countersunk Titanium Alloy Sheet*

Rivet Type	MS20427M (F_{su} = 49 ksi)			
Sheet Material	Commercially Pure Titanium, F_{su} = 80 ksi			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	1/4 (0.257)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.040	531	...	...	...
0.050	573	[a] 818	...	...
0.063	626	885	[a] ...	...
0.071	635	926	1242	...
0.080	...	973	1302	[a] ...
0.090	...	...	1360	...
0.100	...	...	1400	2260
0.125	...	...	...	2460 [a]
0.160	...	...	...	2540
Rivet shear strength[b]	635	973	1400	2540
	Yield Strength[c], lbs			
Sheet thickness, in.:				
0.040	376	...	...	...
0.050	472	582	...	...
0.063	598	736	...	...
0.071	635	835	933	...
0.080	...	945	1130	...
0.090	...	...	1268	...
0.100	...	...	1400	1860
0.125	...	...	...	2340
0.160	...	...	...	2540
Head height (max.), in.	0.048	0.061	0.077	0.103

[a]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[b]Rivet shear strength is documented in MS20427.
[c]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.2.2(i). *Static Joint Strength of 120° Flush Shear Head Aluminum Alloy (2017-T3) Solid Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	BRFS-D[a] (F_{su} = 38 ksi)				
Sheet Material	Clad 2024-T3				
Rivet Diameter, in. (Nominal Hole Diameter, in.)[b]	3/32 (0.096)	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	1/4 (0.257)
	Ultimate Strength, lbs				
Sheet thickness, in.:					
0.020	139	...	...	...	...
0.025	176	233	...	...	...
0.032	226	300	367	...	...
0.040	275	378	465	552	...
0.050	...	477	585	697	930
0.063	...	494	741	886	1182
0.071	...	...	755	1005	1338
0.080	...	...	...	1090	1513
0.090	...	...	...	...	1711
0.100	...	...	...	...	1902
0.125	...	...	...	...	1970
Rivet shear strength[c]	275	494	755	1090	1970
	Yield Strength[d], lbs				
Sheet thickness, in.:					
0.020	137	...	...	...	...
0.025	171	229	...	...	...
0.032	207	294	359	...	...
0.040	231	357	453	547	...
0.050	...	398	550	680	918
0.063	...	451	614	814	1149
0.071	...	...	655	857	1295
0.080	...	...	...	914	1430
0.090	...	...	...	...	1513
0.100	...	...	...	...	1592
0.125	...	...	...	...	1790
Head height (ref.), in.	0.018	0.023	0.030	0.039	0.049

[a]Data supplied by Briles Rivet Corp.
[b]Fasteners installed in hole diameters of 0.0975, 0.1285, 0.1615, 0.1945, 0.257, +0.0005, -0.001, respectively.
[c]Shear strength based on Table 8.1.2(b) and F_{su} = 38 ksi.
[d]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.2.2(j). *Static Joint Strength of 120° Flush Shear Head Aluminum Alloy (2117-T3) Solid Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	BRFS-AD[a] (F_{su} = 30 ksi)				
Sheet Material	Clad 2024-T3				
Rivet Diameter, in. (Nominal Hole Diameter, in.)[b]	3/32 (0.096)	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	1/4 (0.257)
	Ultimate Strength, lbs				
Sheet thickness, in.:					
0.020	119	...	...	...	...
0.025	144	201	...	...	...
0.032	171	250	316	...	...
0.040	204	292	386	474	...
0.050	217	343	451	571	806
0.063	...	388	536	675	987
0.071	...	...	596	737	1073
0.080	...	...	...	812	1169
0.090	...	...	...	862	1278
0.100	...	...	...	...	1371
0.125	...	...	...	...	1550
Rivet shear strength[c]	217	388	596	862	1550
	Yield Strength[d], lbs				
Sheet thickness, in.:					
0.020	119	...	...	...	...
0.025	144	201	...	...	...
0.032	171	250	316	...	...
0.040	204	292	386	474	...
0.050	217	343	451	571	806
0.063	...	388	536	675	987
0.071	...	...	596	737	1073
0.080	...	...	...	812	1169
0.090	...	...	...	862	1278
0.100	...	...	...	...	1371
0.125	...	...	...	...	1550
Head height (ref.), in.	0.018	0.023	0.030	0.039	0.049

[a]Data supplied by Briles Rivet Corp.
[b]Fasteners installed in hole diameters of 0.0975, 0.1285, 0.1615, 0.1945, 0.257, +0.0005, -0.001, respectively.
[c]Shear strength based on Table 8.1.2(b) and F_{su} = 38 ksi.
[d]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.2.2(k). *Static Joint Strength of 120° Flush Shear Head Aluminum Alloy (2024-T31) Solid Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	BRFS-DD[a] (F_{su} = 41 ksi)	
Sheet Material	Clad 2024-T3	
Rivet Diameter, in.	3/16	1/4
(Nominal Hole Diameter, in.)[b]	(0.191)	(0.257)
	Ultimate Strength, lbs	
Sheet thickness, in.:		
0.040	598	...
0.050	772	1000
0.063	994	1300
0.071	1130	1480
0.080	1180	1690
0.090	...	1920
0.100	...	2120
Rivet shear strength[c]	1180	2120
	Yield Strength[d], lbs	
Sheet thickness, in.:		
0.040	598	...
0.050	772	1000
0.063	949	1300
0.071	1000	1480
0.080	1060	1680
0.090	...	1760
0.100	...	1850
Head height (ref.), in.	0.039	0.049

[a]Data supplied by Briles Rivet Corp.
[b]Fasteners installed in hole diameters of 0.1935 and 0.257, ±0.0005.
[c]Shear strength based on Table 8.1.2(b) and F_{su} = 41 ksi.
[d]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.2.2(l). *Static Joint Strength of 120° Flush Shear Head Ti-45 Cb Solid Rivets in Machine-Countersunk Aluminum Alloy and Titanium Sheet*

Rivet Type	BRFS-T[a] (F_{su} = 53 ksi)					
Sheet Material	Clad 7075-T6			Annealed Ti-6Al-4V		
Rivet Diameter, in. (Nominal Hole Diameter, in.)[b]	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)
	Ultimate Strength, lbs					
Sheet thickness, in.:						
0.025	288	...	...	400	...	...
0.032	369	456	...	513	635	...
0.040	461	572	685	564	796	952
0.050	577	713	858	602	867	1190
0.063	610	891	1080	650	927	1270
0.071	628	914	1220	680	964	1310
0.080	649	939	1300	687	1005	1360
0.090	671	967	1330	...	1050	1420
0.100	687	996	1370	...	...	1470
0.125	...	1050	1450	...	...	1520
0.160	...	...	1520	...	...	...
Rivet shear strength[c]	687	1050	1520	687	1050	1520
	Yield Strength[d], lbs					
Sheet thickness, in.:						
0.025	288	...	...	400	...	...
0.032	369	456	...	513	635	...
0.040	461	572	685	564	796	952
0.050	577	713	858	602	867	1190
0.063	610	891	1080	650	927	1270
0.071	628	914	1220	680	964	1310
0.080	649	939	1300	687	1005	1360
0.090	671	967	1330	...	1050	1420
0.100	687	996	1370	...	...	1470
0.125	...	1050	1450	...	...	1520
0.160	...	...	1520	...	...	...
Head height (ref.), in.	0.023	0.030	0.039	0.023	0.030	0.039

[a]Data supplied by Briles Rivet Corp.
[b]Allowables developed from tests with hole diameters noted, except 5/32 and 3/16 diameters were 0.161 and 0.1935 ±0.0005, respectively.
[c]Rivet shear strength based on Table 8.1.2(b) and F_{su} = 53 ksi.
[d]Permanent set at yield load: 4% of nominal hole diameter (Ref. 9.4.1.3.3).

TABLE 8.1.2.2(m). *Static Joint Strength of 120° Flush Shear Head Aluminum Alloy (7050-T731) Solid Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	MS14218E[a] (F_{su} = 43 ksi)						
Sheet Material	Clad 2024-T3						
Rivet Diameter, in. (Nominal Hole Diameter, in.)[b]	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	7/32 (0.228)	1/4 (0.257)	9/32 (0.290)	5/16 (0.323)
	Ultimate Strength, lbs						
Sheet thickness, in.:							
0.025	215	...	...	...	...	...	...
0.032	307	[c] 346	...	...	...	...	...
0.040	434	478	[c] 529	...	...	...	...
0.050	508	673	732	[c] 806	...	...	...
0.063	536	781	1045	1135	[c] 1200	1285	...
0.071	554	803	1110	1365	1445	1530	[c] 1630
0.080	558	827	1140	1565	1735	1835	1930 [c]
0.090	...	854	1175	1605	1990	2200	2320
0.100	...	...	1205	1645	2030	2525	2725
0.125	...	...	1230	1740	2140	2650	3205
0.160	...	...	...	1755	2230	2820	3400
0.190	...	...	...	...	...	2840	3525
Rivet shear strength[d]	558	854	1230	1755	2230	2840	3525
	Yield Strength[e], lbs						
Sheet thickness, in.:							
0.025	215	...	...	...	...	...	...
0.032	307	346	...	...	...	...	...
0.040	388	478	529	...	...	...	...
0.050	487	601	721	806	...	...	...
0.063	536	760	912	1085	1200	1285	...
0.071	552	803	1030	1225	1377	1530	1630
0.080	558	827	1140	1385	1554	1755	1930
0.090	...	854	1175	1560	1750	1970	2200
0.100	...	...	1205	1645	1950	2200	2445
0.125	...	...	1230	1735	2140	2650	3060
0.160	...	...	...	1755	2230	2810	3400
0.190	...	...	...	...	...	2840	3525
Head height (ref.), in.	0.027	0.035	0.044	0.053	0.061	0.069	0.077

[a]Data supplied by Briles Rivet Corp.
[b]Allowables developed from tests with hole diameters noted, except 5/32, 3/16, and 5/16 diameters were 0.161, 0.1935, and 0.316, respectively. Hole tolerances were +0.0005-0.001 inch.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Shear strength based on Table 8.1.2(b) and F_{su} = 43 ksi.
[e]Permanent set at yield load: 4% of nominal hole diameter (Ref. 9.4.1.3.3).

TABLE 8.1.2.2(n). *Static Joint Strength of 100° Flush Shear Head Aluminum Alloy (7050-T73) Solid Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	NAS1097-E[a] (F_{su} = 41 ksi)							
Sheet Material	Clad 2024-T3				Clad 7075-T6			
Nominal Rivet Diameter, in. ... (Nominal Hole Diameter, in.)[b]	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	1/4 (0.257)	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	1/4 (0.257)
	Ultimate Strength, lbs							
Sheet thickness, in.:								
0.025	227	...	...	...	278	...	...	...
0.032	326	[c] 367	...	...	354	[c] 441	...	...
0.040	437	505	[c] 561	...	439	547	[c] 661	...
0.050	466	679	773	[c] 908	456	674	823	[c] 1120
0.063	485	717	1005	1275	477	700	980	1330 [c]
0.071	497	731	1025	1500	490	716	999	1570
0.080	507	747	1045	1750	505	734	1020	1760
0.090	521	765	1065	1840	520	754	1045	1790
0.100	531	781	1085	1870	531	774	1070	1825
0.125	...	814	1135	1935	...	814	1130	1905
0.160	...	...	1175	2030	...	...	1175	2020
0.190	...	...	...	2110	...	...	...	2115
0.250	...	...	...	2125	...	...	...	2125
Rivet shear strength[d]	531	814	1175	2125	531	814	1175	2125
	Yield Strength[e], lbs							
Sheet thickness, in.:								
0.025	192	...	...	...	222	...	...	...
0.032	283	311	...	...	307	356	...	...
0.040	349	439	479	...	372	475	542	...
0.050	398	538	674	767	398	572	724	894
0.063	462	617	799	1105	431	612	836	1205
0.071	497	665	857	1310	451	638	867	1400
0.080	507	720	921	1400	474	666	900	1490
0.090	521	765	995	1500	499	698	938	1540
0.100	531	781	1065	1595	525	729	976	1595
0.125	...	814	1135	1835	...	808	1070	1720
0.160	...	...	1175	2030	...	...	1175	1895
0.190	...	...	...	2110	...	...	...	2050
0.250	...	...	...	2125	...	...	...	2125
Head height (ref.), in.	0.029	0.037	0.046	0.060	0.029	0.037	0.046	0.060

[a]Data supplied by Lockheed-Georgia Company.
[b]Fasteners installed in hole diameters of 0.130, 0.158, 0.191, and 0.254 ± 0.003 inch, respectively.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Shear strength based on Table 8.1.2(b) and F_{su} = 41 ksi.
[e]Permanent set at yield load: 4% of nominal hole diameter (Ref. 9.4.1.3.3).

TABLE 8.1.2.2(o). *Static Joint Strength of 120° Flush Shear Head Aluminum Alloy (2117-T3) Solid Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	MS14218AD[a] (F_{su} = 30 ksi)					
Sheet Material	Clad 2024-T3					
Rivet Diameter, in. (Nominal Hole Diameter, in.)[b]	3/32 (0.096)	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	7/32 (0.228)	1/4 (0.257)
	Ultimate Strength, lbs					
Sheet thickness, in.:						
0.020	125	...	...	...	...	...
0.025	153	[c] 212	...	...	...	...
0.032	188	263	[c] 334	...	...	...
0.040	216	322	408	[c] 498	...	...
0.050	217	380	498	609	[c] 740	849
0.063	...	388	588	751	910	1040 [c]
0.071	...	...	596	817	1015	1155
0.080	...	...	...	862	1125	1290
0.090	...	...	...	...	1205	1425
0.100	...	...	...	...	1225	1520
0.125	...	...	...	...	...	1555
Rivet shear strength[d]	217	388	596	862	1225	1555
	Yield Strength[e], lbs					
Sheet thickness, in.:						
0.020	125	...	...	...	...	...
0.025	153	212	...	...	...	...
0.032	188	263	334	...	...	...
0.040	216	319	408	498	...	...
0.050	217	370	492	609	740	849
0.063	...	388	574	733	910	1040
0.071	...	...	596	794	1005	1155
0.080	...	...	...	842	1090	1275
0.090	...	...	...	862	1180	1380
0.100	...	...	...	...	1225	1480
0.125	...	...	...	...	...	1555
Head height (ref.), in.	0.022	0.027	0.035	0.044	0.053	0.061

[a]Data supplied by Briles Rivet Corp.
[b]Load allowables developed from tests with hole diameters noted, except 3/32, 5/32, and 3/16 diameters were 0.098, 0.161, and 0.1935, respectively. Hole tolerance was +0.0005-0.001 inch.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Shear strength based on Table 8.1.2(b) and F_{su} = 30 ksi.
[e]Permanent set at yield load: 4% of nominal hole diameter (Ref. 9.4.1.3.3).

TABLE 8.1.2.2(p). *Static Joint Strength of 120° Flush Tension Type Head Aluminum Alloy (7050-T731) Solid Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	MS14219 E[a] (F_{su} = 43 ksi)							
Sheet Material	Clad 2024-T3							
Rivet Diameter, in. (Nominal Hole Diameter, in.)[b]	3/32 (0.096)	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	7/32 (0.228)	1/4 (0.257)	9/32 (0.290)	5/16 (0.523)
	Ultimate Strength, lbs							
Sheet thickness, in.:								
0.032	210	...	...	...	...	...	...	...
0.040	279	[c] 339	...	...	...	...	...	...
0.050	310	473	[c] 527	...	...	...	...	...
0.063	311	538	743	[c] 819	...	...	...	...
0.071	...	558	788	979	[c] 1065	...	...	...
0.080	...	...	834	1105	1280	[c] ...	...	...
0.090	...	...	854	1165	1520	1625	...	...
0.100	...	...	...	1230	1605	1890	[c] 2020	2120
0.125	...	...	...	...	1755	2145	2580	2965 [c]
0.160	...	...	...	...	...	2230	2840	3415
0.190	...	...	...	...	...	...	...	3525
Rivet shear strength[d]	311	588	854	1230	1755	2230	2840	3525
	Yield Strength[e], lbs							
Sheet thickness, in.:								
0.032	210	...	...	...	...	...	...	...
0.040	277	339	...	...	...	...	...	...
0.050	301	468	527	...	...	...	...	...
0.063	309	538	728	819	...	...	...	...
0.071	...	543	788	979	1065	...	...	...
0.080	...	...	823	1100	1280	...	...	...
0.090	...	...	833	1165	1490	1625	...	...
0.100	...	...	...	1190	1605	1875	2020	2120
0.125	...	...	...	...	1705	2145	2580	2945
0.160	...	...	...	...	...	2200	2765	3390
0.190	...	...	...	...	...	...	...	3455
Head height (ref.), in.	0.034	0.041	0.053	0.068	0.077	0.090	0.100	0.104

[a]Data supplied by Briles Rivet Corp.
[b]Load allowables developed from tests with hole diameters noted, except 5/32, 3/16, and 5/16 diameter were 0.161, 0.1935, and 0.316, respectively. Hole tolerances were + 0.0005, -0.001 inch.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Rivet shear strength based on Table 8.1.2(b) and F_{su} = 43 ksi.
[e]Permanent set at yield load: 4% of nominal hole diameter (Ref. 9.4.1.3.3).

TABLE 8.1.2.2(q). *Static Joint Strength of 120° Flush Tension Type Head Aluminum Alloy (7050-T731) Solid Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	MS14219 E[a] (F_{su} = 43 ksi)							
Sheet Material	Clad 7075-T6							
Rivet Diameter, in. (Nominal Hole Diameter, in.)[b]	3/32 (0.096)	1/8 (0.1285)	5/32 (0.159)	3/16 (0.191)	7/32 (0.228)	1/4 (0.257)	9/32 (0.290)	5/16 (0.523)
	Ultimate Strength, lbs							
Sheet thickness, in.:								
0.032	272	...	...	...	...	...	...	...
0.040	297	[c] 455	...	...	...	...	...	...
0.050	311	522	[c] 704	...	...	...	...	...
0.063	...	558	803	[c] 1065	...	...	...	...
0.071	...	...	832	1140	[c] 1435	...	...	...
0.080	...	...	854	1180	1600	[c] ...	...	...
0.090	...	...	...	1220	1650	2030	...	...
0.100	...	...	...	1230	1700	2090	[c] 2565	2860
0.125	...	...	...	...	1755	2230	2740	3295 [c]
0.160	...	...	...	...	...	...	2840	3525
Rivet shear strength[d]	311	558	854	1230	1755	2230	2840	3525
	Yield Strength[e], lbs							
Sheet thickness, in.:								
0.032	272	...	...	...	...	...	...	...
0.040	296	455	...	...	...	...	...	...
0.050	308	522	704	...	...	...	...	...
0.063	...	550	802	1065	...	...	...	...
0.071	...	...	823	1140	1435	...	...	...
0.080	...	...	845	1170	1600	...	...	...
0.090	...	...	...	1205	1650	2030	...	...
0.100	...	...	...	1220	1685	2090	2565	2860
0.125	...	...	...	...	1740	2195	2715	3295
0.160	...	...	...	...	...	...	2815	3480
Head height (ref.), in.	0.034	0.041	0.053	0.068	0.077	0.090	0.100	0.104

[a]Data supplied by Briles Rivet Corp.
[b]Allowables developed from tests with hole diameters noted, except 3/32, 5/32, 3/16, and 5/16 diameters were 0.098, 0.161, 0.1935, and 0.316, respectively. Hole tolerances were +0.0005, -0.001 inch.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Rivet shear strength based on Table 8.1.2(b) and F_{su} = 43 ksi.
[e]Permanent set at yield load: 4% of nominal hole diameter (Ref. 9.4.1.3.3).

Table 8.1.2.2(r). *Static Joint Strength of Solid 100° Flush Head Aluminum Alloy (7050-T73) Solid Rivets in Machine Countersunk Aluminum Alloy Sheet*

Rivet Type	MS20426E (Fsu = 41 ksi)[a]			
Sheet Material	Clad 2024-T3			
Rivet Diameter, in.	1/8	5/32	3/16	1/4
(Nominal Hole Diameter, in.)[b]	(0.1285)	(0.159)	(0.191)	(0.257)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.040	386	…	…	…
0.050	419	592	…	…
0.063	463	647	870	…
0.071	491	680	910	…
0.080	521	718	955	…
0.090	531	760	1005	1610
0.100	…	802	1055	1680
0.125	…	814	1175	1845
0.160	…	…	…	2085
0.190	…	…	…	2125
Rivet shear strength[d]	531	814	1175	2125
	Yield Strength, lbs			
Sheet thickness, in.:				
0.040	262	…	…	…
0.050	327	404	…	…
0.063	412	510	612	…
0.071	464	574	690	…
0.080	517	647	777	…
0.090	531	728	875	1175
0.100	…	794	972	1310
0.125	…	814	1160	1635
0.160	…	…	…	2070
0.190	…	…	…	2125
Head Height (ref.), in.	0.042	0.055	0.070	0.095

(a) Data supplied by Lockheed Ga. Co. and Air Force Materials Laboratory.
(b) Load allowables developed from tests with hole diameters of 0.130, 0.158, 0.191, and 0.256 ± 0.003 inch.
(c) The values in the table above the horizontal line in each column are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires the specific approval of the procuring activity.
(d) Shear strength based on area computed from nominal hole diameters in Table 8.1.2(b) and F_{su}=41 ksi.
(e) Permanent set at yield load: 4% of the nominal hole diameter.

Table 8.1.2.2 (s). *Static Joint Strength of Solid 100° Flush Head Alumunim Alloy (7050-T73) Solid Rivets in Machine Countersunk Aluminum Alloy Sheet*

Rivet Type	MS20426E (Fsu = 41 ksi)[a]			
Sheet Material	Clad 7075-T6			
Rivet Diameter, in.	1/8	5/32	3/16	1/4
(Nominal Hole Diameter, in.)[b]	(0.1285)	(0.159)	(0.191)	(0.257)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.040	318	...	...	...
0.050	393	c 492	...	...
0.063	440	606	c 745	...
0.071	469	642	840	c ...
0.080	502	683	898	...
0.090	531	728	952	1430
0.100	...	773	1005	1570 c
0.125	...	814	1140	1755
0.160	...	...	1175	2010
0.190	...	...	...	2125
Rivet shear strength[d]	531	814	1175	2125
	Yield Strength, lbs			
Sheet thickness, in.:				
0.040	257	...	...	...
0.050	330	399	...	...
0.063	423	515	607	...
0.071	469	586	693	...
0.080	502	666	789	...
0.090	531	728	896	1175
0.100	...	773	1005	1320
0.125	...	814	1140	1680
0.160	...	...	1175	2010
0.190	...	...	...	2125
Head Height (ref.), in.	0.042	0.055	0.070	0.095

(a) Data supplied by Lockheed Ga. Co., Air Force Materials Laboratory, Allfast, Cherry Fasteners, Douglas Aircraft Co., and Huck Mfg. Co.

(b) Load allowables developed from tests with hole diameters of 0.130, 0.158, 0.191, and 0.256 ± 0.003 inch.

(c) The values in the table above the horizontal line in each column are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires the specific approval of the procuring activity.

(d) Shear strength based on area computed from nominal hole diameters in Table 8.1.2(b) and F_{su} = 41 ksi.

(e) Permanent set at yield load: 4% of the nominal hole diameter.

8.1.3 BLIND FASTENERS.—The strengths shown in the following tables are applicable only for the grip lengths and hole tolerances recommended by the respective fastener manufacturers. For some fastener systems, permanent set at yield load may be increased if hole sizes greater than those listed in the applicable table are used. This condition may exist even though the test hole size lies within the manufacturer's recommended hole size range (Reference 9.4.1.3.3).

The strength values were established from test data and are applicable to "joints" with e/D ≥ 2.0. For joints with e/D ratios less than 2.0, tests to substantiate the use of yield and ultimate strength allowables must be made. Ultimate strength values of protruding- and flush-head blind fasteners were obtained as described in Section 9.4. The analyses included dividing the average ultimate load from test data by 1.15. This factor is not applicable to shear strength cutoff values which may be either the procurement specification shear strength (S values) of the fastener, or if no specification exists, a statistical value determined from test results as described in Section 9.4.

Unless otherwise specified, yield load is defined in Section 9.4.1.3.3 as the load which results in a joint permanent set equal to 0.04D, where D is the decimal equivalent of the hole or fastener shank diameter, as defined in Table 9.4.1.2(a). Some tables are footnoted to show the previous criteria used for those particular tables.

For machine countersunk joints, the sheet gage specified in the tables is that of the countersunk sheet. When the noncountersunk sheet is thinner than the countersunk sheet, the bearing allowable for the noncountersunk sheet-fastener combination should be computed, compared to the table value, and the lower of the two values selected. Increased attention should be paid to detail design in cases where t/D < 0.25 because of the possibility of unsatisfactory service life.

Joint allowable strengths of blind fasteners in double-dimpled or dimpled into machine countersunk applications should be established on the basis of specific tests acceptable to the procuring or certifying agency. In the absence of such data, allowables for blind fasteners in machine countersunk sheet may be used.

Reference should be made to the requirements of the applicable procuring or certifying agency relative to the use of blind fasteners such as the limitations of usage in design standard MS33522.

8.1.3.1 *Protruding-Head Blind Fasteners*

8.1.3.1.1 *Friction-Lock Blind Rivets.*—Tables 8.1.3.1.1(a) through 8.1.3.1.1(e) contain joint allowables for various protruding-head, friction-lock blind rivet/sheet material combinations.

8.1.3.1.2 *Mechanical-Lock Spindle Blind Rivets.*—Tables 8.1.3.1.2(a) through (n) contain joint allowables for various protruding-head, mechanical-lock spindle blind rivet/sheet material combinations.

8.1.3.2 *Flush-Head Blind Fasteners*

8.1.3.2.1 *Friction-Lock Blind Rivets.*—Tables 8.1.3.2.1(a) through (g) contain joint allowables for various flush-head, friction-lock blind rivet/sheet material combinations.

8.1.3.2.2 *Mechanical-Lock Spindle Blind Rivets.*—Tables 8.1.3.2.2(a) through (q) contain joint allowables for various flush-head, mechanical-lock spindle blind rivet/sheet material combinations.

8.1.3.2.3 *Flush-Head Blind Bolts.*—Tables 8.1.3.2.3(a) through (h) contain joint allowables for various flush-head blind bolt/sheet material combinations.

TABLE 8.1.3.1.1(a). *Static Joint Strength of Blind Protruding Head A-286 Rivets in Alloy Steels, Titanium Alloy and A-286 Alloy Sheet*

Rivet Type	CR 6636[a] (F_{su} = 75 ksi)			
Sheet Material	Alloy Steel, F_{tu} = 125 ksi, Titanium Alloys, F_{tu} = 120 ksi, and A-286 Alloy, F_{tu} = 140 ksi			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength[b], lbs			
Sheet thickness, in.:				
0.008	169	...	...	...
0.012	290	341	...	...
0.016	412	493	566	...
0.020	532	645	748	924
0.025	688	816	967	1221
0.032	796	1050	1278	1650
0.040	879	1233	1570	2129
0.050	945	1354	1807	2673
0.063	970	1461	1980	3168
0.071	...	1490	2062	3350
0.080	...	...	2150	3515
0.090	...	...	...	3663
0.100	...	...	...	3779
0.112	...	...	...	3890
Rivet shear strength[c]	970	1490	2150	3890

[a]Data supplied by Cherry Fasteners.
[b]Yield strength is in excess of 80% of ultimate. This is based on a previous Navy "BuAer" definition that yield strength would not be considered to be critical if it exceeded 1.15 x 2.3 of design ultimate strength. There was no requirement for submission of the yield data for inclusion in ANC-5.
[c]Shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 75 ksi.

TABLE 8.1.3.1.1(b). *Static Joint Strength of Protruding Head Monel Rivets in Stainless Steel Sheet*

Rivet Type	MS20600M (F_{su} = 55 ksi)							
Sheet Material	ANSI 301-Annealed				AISI 301-½ Hard			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.154)	1/4 (0.258)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs							
Sheet thickness, in.:								
0.010	...	...	...	...	195	...	...	...
0.012	...	...	...	...	225	287	...	...
0.016	...	...	...	...	290	367	453	...
0.020	332[a]	...	...	...	358	450	552	774
0.025	396[a]	494[a]	...	...	440	552	675	940
0.032	472[a]	627[a]	768[a]	...	522	690	1040	1163
0.040	526[a]	729[a]	942[a]	1290[a]	580	810	1200	1430
0.050	594[a]	810[a]	1070[a]	1585[a]	635	903	1325	1760
0.063	681[a]	919[a]	1280[a]	1875[a]	678	980	1385	2090
0.071	700[a]	984[a]	1370[a]	1980[a]	701	1013	1438	2220
0.080	713	1055[a]	1470[a]	2110[a]	713	1050	1486	2340
0.090	...	1080[a]	1530[a]	2240[a]	...	1081	1540	2450
0.100	...	1090	1580	2380[a]	...	1090	1580	2540
0.125	...	...	...	2700[a]	...	...	...	2710
0.160	...	...	...	2855	...	...	...	2855
Rivet shear strength[b]	713	1090	1580	2855	713	1090	1580	2855
	Yield Strength[c], lbs							
Sheet thickness, in.:								
0.010	...	...	...	...	195	...	...	...
0.012	...	...	...	...	225	287	...	...
0.016	...	...	...	...	290	367	453	...
0.020	128	...	...	...	358	450	551	774
0.025	160	199	...	...	440	552	675	940
0.032	205	254	306	...	522	690	836	1163
0.040	257	318	382	514	580	810	1040	1430
0.050	321	397	477	642	635	903	1200	1760
0.063	405	501	601	810	678	980	1325	2090
0.071	456	564	678	912	701	1013	1385	2220
0.080	514	635	764	1025	713	1050	1438	2340
0.090	...	715	860	1155	...	1081	1486	2450
0.100	...	795	955	1285	...	1090	1540	2540
0.125	...	...	...	1605	...	...	...	2710
0.160	...	...	...	2055	...	...	...	2855

[a]Yield value is less than 2/3 of the indicated ultimate strength value.
[b]Rivet shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 55 ksi.
[c]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.1.1(c). *Static Joint Strength of Blind Protruding Head Monel Rivets in Aluminum Alloy Sheet*

Rivet Type	MS20600M (F_{su} = 55 ksi)							
Sheet Material	2024-T3				7075-T6			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs							
Sheet thickness, in.:								
0.025	268	...	...	...	297	...	...	...
0.032	365	429	...	...	405	472	...	...
0.040	478	569	650	...	485	631	720	...
0.050	545	738	860	1070	545	747	955	1190
0.063	622	844	1110	1430	622	844	1110	1590
0.071	652	903	1180	1665	652	903	1180	1840
0.080	684	968	1255	1910	684	968	1255	1940
0.090	713	1010	1345	2060	713	1010	1345	2060
0.100	...	1050	1415	2180	...	1050	1415	2180
0.125	...	1090	1545	2480	...	1090	1545	2480
0.160	...	...	1580	2735	...	...	1580	2735
0.190	...	...	...	2855	...	...	...	2855
Rivet shear strength[a]	713	1090	1580	2855	713	1090	1580	2855
	Yield Strength[b], lbs							
Sheet thickness, in.:								
0.025	234	...	...	...	272	...	...	...
0.032	297	370	...	...	343	430	...	...
0.040	368	460	556	...	425	533	644	...
0.050	458	570	688	936	492	657	797	1090
0.063	529	715	863	1170	529	759	996	1350
0.071	552	786	970	1315	552	786	1075	1520
0.080	577	818	1090	1470	577	818	1110	1700
0.090	605	853	1155	1650	605	853	1155	1915
0.100	...	888	1200	1830	...	888	1200	1970
0.125	...	976	1300	2110	...	976	1300	2110
0.160	...	...	1450	2310	...	...	1450	2310
0.190	...	...	...	2480	...	...	...	2480

[a]Shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 55 ksi.
[b]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.1.1(d). *Static Joint Strength of Blind Protruding Head Alloy (2117-T3) Rivets in Aluminum Alloy Sheet*

Rivet Type	MS20600AD and MS20602AD (F_{su} = 30 ksi)			
Sheet Material	Clad 2024 T3			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.025	233	...	...	...
0.032	277	368	...	...
0.040	321	425	544	...
0.050	388	506	643	961
0.063	...	596	753	1110
0.071	...	...	823	1200
0.080	...	...	862	1305
0.090	...	...	...	1415
0.100	...	...	...	1550
Rivet shear strength[a]	388	596	862	1550
	Yield Strength[b], lbs			
Sheet thickness, in.:				
0.025	226	...	...	...
0.032	264	356	...	...
0.040	304	406	523	...
0.050	362	475	610	925
0.063	388	560	709	1058
0.071	...	596	771	1135
0.080	...	...	862	1230
0.090	...	...	...	1330
0.100	...	...	...	1450

[a]Rivet shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 30 ksi.
[b]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.1.1(e). *Static Joint Strength of Blind Protruding Head Aluminum Alloy (5056) Rivets in Magnesium Alloy Sheet*

Rivet Type	MS20600B (F_{su} = 28 ksi)			
Sheet Material	AZ31B-H24			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength[a], lbs			
Sheet thickness, in.:				
0.025	178	...	...	...
0.032	218	282	...	...
0.040	256	339	420	...
0.050	290	392	502	714
0.063	330	449	584	870
0.071	352	481	627	942
0.080	363	512	667	1025
0.090	...	550	714	1090
0.100	...	556	757	1160
0.125	...	...	802	1315
0.160	...	...	...	1450
Rivet shear strength[b]	363	556	802	1450

[a]Yield strength is in excess of 80% of ultimate. This is based on a previous Navy "BuAer" definition that yield strength was not considered to be critical if it exceeded 1.15 x 2/3 of design ultimate strength. There was no requirement for submission of the yield data for inclusion in ANC-5.

[b]Shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 28 ksi.

TABLE 8.1.3.1.2(a). *Static Joint Strength of Blind Protruding Head Locked Spindle A-286 Rivets in Alloy Steel Sheet*

Rivet Type	NAS1398C[a] and NAS1398C, Code A[b] (F_{su} = 75 ksi)			CR 2643[a] (F_{su} = 95 ksi)		
Sheet Material	Alloy Steel F_{tu} = 180 ksi					
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
	Ultimate Strength[c], lbs					
Sheet thickness, in.:						
0.025	697	...	...	697	...	...
0.032	785	1112	...	807	1112	...
0.040	860	1211	1628	911	1246	1639
0.050	956	1325	1772	1043	1406	1833
0.063	970	1480	1958	1215	1615	2090
0.071	...	1490	2070	1230	1748	2240
0.080	...	...	2150	...	1885	2420
0.090	...	...	...	...	...	2610
0.100	...	...	...	...	...	2720
Rivet shear strength	970[d]	1490[d]	2150[d]	1230[e]	1885[e]	2720[e]

[a]Data supplied by Cherry Fasteners.
[b]Confirmatory data supplied by Olympic Fastening Systems, Inc.
[c]Yield strength is in excess of 80% of ultimate. This is based on a previous Navy "BuAer" definition that yield strength would not be considered to be critical if it exceeded 1.15 x 2/3 of design ultimate strength. There was no requirement for submission of the yield data for inclusion in ANC-5.
[d]Rivet shear strength is documented in NAS1400.
[e]Shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 95 ksi.

TABLE 8.1.3.1.2(b). *Static Joint Strength of Blind Protruding Head Locked Spindle Monel Rivets in Stainless Steel Sheet*

Rivet Type	NAS1398 MS or MW[a] and NAS1398 MS or MW, Code A[b] (F_{su} = 55 ksi)		
Sheet Material	AISI 301-½ Hard		
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
	Ultimate Strength[c], lbs		
Sheet thickness, in.:			
0.025	462	...	...
0.032	568	734	...
0.040	594	870	1094
0.050	632	915	1270
0.063	678	971	1335
0.071	706	1009	1380
0.080	710	1048	1428
0.090	...	1090	1532
0.100	...	...	1580
Rivet shear strength[d]	710	1090	1580

[a]Data supplied by Cherry Fasteners.
[b]Confirmatory data supplied by Olympic Fastening Systems, Inc.
[c]Yield strength is in excess of 80% of ultimate strength. This is based on a previous Navy "BuAer" definition that yield strength was not considered to be critical if it exceeded 1.15 x 2/3 of design ultimate strength. There was no requirement for submission of the yield strength data for inclusion in ANC-5.
[d]Rivet shear strength is documented in NAS1400.

TABLE 8.1.3.1.2(c). *Static Joint Strength of Blind Protruding Head Locked Spindle Monel Rivets in Aluminum Alloy Sheet*

Rivet Type	NAS1398 MS or MW[a] and NAS1398 MS or MW, Code A[b] (F_{su} = 55 ksi)		
Sheet Material	Clad 7075-T6		
Rivet Diameter, in. (Nominal Hole Diameter, in.) ..	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
	Ultimate Strength[c], lbs		
Sheet thickness, in.:			
0.025	318	...	...
0.032	404	506	...
0.040	466	624	774
0.050	546	720	922
0.063	647	845	1072
0.071	710	921	1168
0.080	...	1009	1272
0.090	...	1090	1387
0.100	...	...	1507
0.125	...	...	1580
Rivet shear strength[d]	710	1090	1580

[a]Data supplied by Cherry Fasteners.
[b]Confirmatory data supplied by Olympic Fastening Systems, Inc.
[c]Yield strength is in excess of 80% of ultimate. This is based on a previous Navy "BuAer" definition that yield strength would not be considered to be critical if it exceeded 1.15 x 1/3 of design ultimate strength. There was no requirement for submission of the yield data for inclusion in ANC-5.
[d]Rivet shear strength is documented in NAS1400.

TABLE 8.1.3.1.2(d_1). *Static Joint Strength of Blind Protruding Head Locked Spindle Aluminum Alloy Rivets in Aluminum Alloy Sheet*

Rivet Type	NAS1398B[a] (F_{su} = 30 ksi)				NAS1398D[a] (F_{su} = 38 ksi)			
Sheet Material	Clad 2024-T3							
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
Sheet thickness, in.:	Ultimate Strength, lbs.							
0.025	228	...	...	...	228	...	...	...
0.032	289	364	412	...	304	364	...	...
0.040	337	448	553	670	355	470	553	...
0.050	388	521	662	914	418	548	696	914
0.063	...	596	781	1145	494	647	816	1205
0.071	...	...	854	1240	...	710	894	1303
0.080	...	...	862	1350	...	755	975	1420
0.090	...	...	...	1475	...	...	1069	1545
0.100	...	...	...	1550	...	...	1090	1670
0.125	...	...	...	...	...	...	...	1970
Rivet shear strength[b]	388	596	862	1550	494	755	1090	1970

[a]Data supplied by Cherry Fasteners.
[b]Rivet shear strength documented in NAS1400.

TABLE 8.1.3.1.2(d_2). *Static Joint Strength of Blind Protruding Head Locked Spindle Aluminum Alloy Rivets in Aluminum Alloy Sheet*

Rivet Type	NAS1738B and NAS1738E[a] (F_{su} = 34 ksi)		
Sheet Material	Clad 2024-T3		
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.144)	5/32 (0.178)	3/16 (0.207)
	Ultimate Strength, lbs		
Sheet thickness, in.:			
0.025	267	305	330
0.032	368	428	473
0.040	427	567	636
0.050	480	650	815
0.063	547[b]	735	912
0.071	554[b]	785[b]	976
0.080	...	837[b]	1042[b]
0.090	...	...	1115[b]
0.100	...	...	1128[b]
Rivet shear strength[c]	554	837	1128
	Yield Strength[d], lbs		
Sheet thickness, in.:			
0.020	185	213	228
0.025	242	285	317
0.032	298	386	433
0.040	321	453	568
0.050	336	489	625
0.063	336	508	680
0.071	336	508	684
0.080	...	508	684
0.090	...	...	684
0.100	...	...	684

[a]Data supplied by Cherry Fasteners.
[b]Yield value is less than 2/3 of the indicated ultimate.
[c]Rivet shear strength was documented in NAS1740 prior to Revision (1), dated January 15, 1974.
[d]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.1.2(e). *Static Joint Strength of Blind Protruding Head Locked Spindle Aluminum Alloy Rivets in Magnesium Alloy Sheet*

Rivet Type	NAS1398B[a] (F_{su} = 30 ksi)				NAS1738B and NAS1738E[a] (F_{su} = 34 ksi)		
Sheet Material	AZ31B-H24						
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)	1/8 (0.144)	5/32 (0.178)	3/16 (0.207)
	Ultimate Strength, lbs.						
Sheet thickness, in.:							
0.025	163	...	...	...	202	...	...
0.032	208	256	310	...	261	321	372
0.040	255	324	388	519	325	401	465
0.050	298	394	485	654	372	501	579
0.063	352	461	588	822	425	570	708
0.071	385	501	639	924	458	609	756
0.080	388	550	695	1020	495	656	809
0.090	...	596	755	1109	536[b]	709	866
0.100	...	...	820	1191	554[b]	759	925
0.125	...	...	862	1397	...	837[b]	1072[b]
0.160	...	...	...	1550	...	...	1128[b]
Rivet shear strength	388[c]	596[c]	862[c]	1550[c]	554[d]	837[d]	1128[d]
	Yield Strength[e], lbs.						
Sheet thickness, in.:							
0.025	...	...	...	...	155	...	...
0.032	...	...	...	...	198	243	282
0.040	...	...	...	...	248	304	353
0.050	...	...	...	...	302	380	441
0.063	...	...	...	...	325	460	556
0.071	...	...	...	...	336	478	614
0.080	...	...	...	...	336	499	638
0.090	...	...	...	...	336	508	664
0.100	...	...	...	...	336	508	684
0.125	...	...	...	...	...	508	684
0.160	...	...	...	...	...	...	684

[a]Data supplied by Cherry Fasteners.
[b]Yield value is less than 2/3 of the indicated ultimate strength value.
[c]Rivet shear strength is documented in NAS1400.
[d]Rivet shear strength was documented in NAS1740 prior to Revision (1), dated January 15, 1974.
[e]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.1.2(f). *Static Joint Strength of Blind Protruding Head Locked Spindle Aluminum Alloy (2219) Rivets in Aluminum Alloy Sheet*

Rivet Type	CR 2A63[a] (F_{su} = 36 ksi)		
Sheet Material	Clad 2024-T81		
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
	Ultimate Strength, lbs		
Sheet thickness, in.			
0.025	256	...	...
0.032	295	404	...
0.040	340	458	592
0.050	395	527	675
0.063	467	617	783
0.071	478	672	848
0.080	...	734	922
0.090	...	741	1005
0.100	...	...	1063
Rivet shear strength[b]	478	741	1063
	Yield Strength[c], lbs		
Sheet thickness, in.:			
0.025	256	...	...
0.032	295	404	...
0.040	336	458	592
0.050	383	521	675
0.063	440	598	770
0.071	445	646	827
0.080	...	683	890
0.090	...	690	963
0.100	...	...	984

[a]Data supplied by Cherry Fasteners.
[b]Shear strength values based on indicated nominal hole diameters and F_{su} = 36 ksi.
[c]Permanent set at yield load: 4% of nominal hole diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.1.2(g). *Static Joint Strength of Blind Protruding Head Locked Spindle A-286 Rivets in Aluminum Alloy Sheet*

Rivet Type	CR4623[a] (F_{su} = 75 ksi)			
Sheet Material	Clad 7075-T6			
Rivet Diameter, in. (Nominal Hole Diameter, in.)[b]	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
Sheet thickness, in.:	Ultimate Strength, lbs.			
0.020	237	...	...	...
0.025	298	367	...	...
0.032	385	478	566	...
0.040	486	601	714	939
0.050	610	757	902	1185
0.063	772	958	1145	1505
0.071	856	1080	1290	1705
0.080	903	1220	1455	1925
0.090	956	1340	1645	2175
0.100	995	1405	1830	2425
0.125	...	1545	2055	3035
0.160	...	...	2215	3570
0.190	...	...	...	3885
0.250	...	...	...	3920
Rivet shear strength[c]	995	1545	2215	3920
Sheet thickness, in.:	Yield Strength[d], lbs.			
0.020	237	...	...	...
0.025	296	367	...	...
0.032	381	475	565	...
0.040	478	594	709	938
0.050	596	745	890	1180
0.063	690	932	1125	1490
0.071	747	1005	1270	1680
0.080	812	1085	1385	1895
0.090	857	1175	1495	2140
0.100	879	1265	1600	2360
0.125	...	1365	1870	2715
0.160	...	...	1995	3215
0.190	...	...	...	3425
0.250	...	...	...	3690

[a]Data supplied by Cherry Fasteners.

[b]Allowable loads developed from test with hole diameters as listed.

[c]Fastener shear strength based on nominal hole diameters and F_{su} = 75 ksi from data analysis.

[d]Permanent set at yield load: 4% of nominal hole diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.1.2(h). *Static Joint Strength of Blind Protruding Head Locked Spindle Monel Rivets in Aluminum Alloy Sheet*

Rivet Type	CR 4523[a] (F_{su} = 65 ksi)			
Sheet Material	Clad 7075-T6			
Rivet Diameter, in. (Nominal Hole Diameter, in.)[b]	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.020	221	...	...	...
0.025	284	344	...	...
0.032	373	456	533	...
0.040	475	582	684	878
0.050	602	740	875	1130
0.063	701	945	1120	1455
0.071	729	1055	1270	1655
0.080	760	1095	1440	1885
0.090	796	1140	1540	2135
0.100	831	1180	1590	2390
0.125	863	1290	1725	2760
0.160	...	1340	1905	3005
0.190	...	...	1920	3215
0.250	...	...	...	3400
Rivet shear strength[c]	863	1340	1920	3400
	Yield Strength[d], lbs			
Sheet thickness, in.:				
0.020	221	...	...	...
0.025	279	344	...	...
0.032	360	447	530	...
0.040	453	561	667	878
0.050	569	706	841	1110
0.063	659	893	1065	1405
0.071	707	965	1205	1590
0.080	729	1035	1340	1795
0.090	752	1105	1430	2030
0.100	776	1135	1520	2260
0.125	834	1205	1645	2590
0.160	...	1305	1765	2880
0.190	...	...	1870	3015
0.250	...	...	...	3290

[a]Data supplied by Cherry Fasteners.
[b]Allowable loads developed from test with hole diameters as listed.
[c]Fastener shear strength based on nominal hole diameters and F_{su} = 65 ksi from data analysis.
[d]Permanent set at yield load: 4% of nominal hole diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.1.2(i). *Static Joint Strength of Blind Protruding Head Locked Spindle Aluminum Alloy (7050) Rivets in Aluminum Alloy Sheet*

Rivet Type	NAS 1720KE and NAS 1720KE( )L[a,b] (F_{su} = 33 ksi)		
Sheet Material	Clad 2024-T3		
Rivet Diameter, in. (Nominal Hole Diameter, in.)[c]	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
Sheet thickness, in:	Ultimate Strength, lbs.		
0.020	174	...	...
0.025	219	272	...
0.032	282	350	417
0.040	354	440	525
0.050	376	552	659
0.063	392	585	816
0.071	402	597	831
0.080	413	611	847
0.090	425	626	866
0.100	437	641	884
0.125	450	680	929
0.160	...	700	950
Rivet shear strength[d]	450	700	950
Sheet thickness, in.:	Yield Strength[e], lbs.		
0.020	174	...	...
0.025	215	272	...
0.032	261	340	417
0.040	314	406	504
0.050	366	489	603
0.063	382	570	732
0.071	391	582	809
0.080	402	595	825
0.090	414	610	843
0.100	426	625	861
0.125	450	662	905
0.160	...	700	950

[a]Data supplied by Avdel Corp.
[b]Fasteners should not be used for structural applications where the t/D is less than 0.15.
[c]Loads developed from tests with hole diameters of 0.130, 0.162, and 0.194, +0.0005, -0.0000 inch.
[d]Rivet shear strength is documented in NAS 1722.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.1.2(j). *Static Joint Strength of Blind Protruding Head Locked Spindle A-286 Rivets in Aluminum Alloy Sheet*

Rivet Type	NAS1720C and NAS1720C( )L[a,b] (F_{su} = 75 ksi)		
Sheet Material	Clad 7075-T6		
Rivet Diameter, in. (Nominal Hole Diameter, in.)[c]	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
Sheet thickness, in:	Ultimate Strength, lbs.		
0.025	329	...	...
0.032	399	528	...
0.040	499	621	799
0.050	625	778	930
0.063	789	982	1170
0.071	847	1105	1320
0.080	870	1245	1490
0.090	896	1320	1680
0.100	921	1350	1865
0.125	985	1430	1955
0.160	1000	1500	2090
0.190	...	...	2200
Rivet shear strength[d]	1000	1500	2200
Sheet thickness, in.:	Yield Strength[e], lbs.		
0.025	329	...	...
0.032	390	386	...
0.040	453	607	779
0.050	531	704	895
0.063	632	831	1045
0.071	687	909	1140
0.080	701	996	1245
0.090	717	1070	1360
0.100	733	1090	1475
0.125	773	1140	1575
0.160	829	1210	1655
0.190	...	...	1730

[a]Data supplied by Avdel Corp.
[b]Fasteners should not be used for structural applications where the t/D is less than 0.15.
[c]Loads developed from tests with hole diameters of 0.130, 0.162, and 0.194, ±.0001 inch.
[d]Rivet shear strength is documented in NAS1722.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.1.2(k). *Static Joint Strength of Blind Protruding Head Locked Spindle Aluminum Alloy Rivets in Aluminum Alloy Sheet*

Rivet Type	M 7885/2[a] (F_{su} = 51 ksi approx.)		
Sheet Material	Clad 2024-T3		
Rivet Diameter, in.	1/8	5/32	3/16
(Nominal Hole Diameter, in.)[b]	(0.130)	(0.162)	(0.194)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.025	249	...	...
0.032	314	397	...
0.040	387	489	593
0.050	414	603	730
0.063	443	644	882
0.071	461	667	909
0.080	481	692	939
0.090	504	720	973
0.100	526	748	1005
0.125	582	818	1090
0.160	661	916	1205
0.190	664	1000	1305
0.250	...	1030	1480
Rivet shear strength[c]	664	1030	1480
	Yield Strength, lbs.[d]		
Sheet thickness, in.:			
0.025	222	...	...
0.032	275	353	...
0.040	294	428	525
0.050	312	457	628
0.063	336	487	664
0.071	351	505	686
0.080	368	526	711
0.090	386	549	738
0.100	405	572	766
0.125	451	629	834
0.160	515	709	931
0.190	570	778	1010
0.250	...	916	1175

[a]Data supplied by Allfast Fastening Systems, Cherry Textron, and Huck International Inc.
[b]Loads developed from tests with hole diameters of 0.130, 0.162, and 0.194, ± 60.001 inch.
[c]Rivet shear strength is documented in MIL-R-7885D.
[d]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.1.2(l). *Static Joint Strength of Blind Protruding Head Locked Spindle Aluminum Alloy Rivets in Aluminum Alloy Sheet*

Rivet Type	M 7885/6[a] (F_{su} = 51 ksi approx.)		
Sheet Material	Clad 2024-T3		
Rivet Diameter, in.	1/8	5/32	3/16
(Nominal Hole Diameter, in.)[b]	(0.144)	(0.178)	(0.207)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.032	306	386	...
0.040	376	473	557
0.050	493	581	683
0.063	527	758	847
0.071	548	783	948
0.080	571	812	1050
0.090	597	844	1085
0.100	623	876	1120
0.125	688	956	1215
0.160	778	1065	1345
0.190	814	1160	1455
0.250	...	1245	1680
0.312	...	...	1685
Rivet shear strength[c]	814	1245	1685
	Yield Strength, lbs.[d]		
Sheet thickness, in.:			
0.032	306	386	...
0.040	359	473	557
0.050	412	553	683
0.063	479	637	784
0.071	492	719	844
0.080	505	736	913
0.090	521	755	989
0.100	536	774	1010
0.125	575	822	1065
0.160	628	888	1140
0.190	675	946	1210
0.250	...	1060	1340
0.312	...	...	1480

[a]Data supplied by Allfast Fastening Systems, Cherry Textron, and Huck International, Inc.
[b]Loads developed from tests with hole diameters of 0.144, 0.178, and 0.207, ± 0.001 inch.
[c]Rivet shear strength is documented in MIL-R-7885D.
[d]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.1.2(m). *Static Joint Strength of Blind Protruding Head Locked Spindle Aluminum Alloy Rivets in Aluminum Alloy Sheet*

Rivet Type	AF3243[a] (F_{su} = 51 ksi approx.)		
Sheet Material	Clad 2024-T3		
Rivet Diameter, in.	1/8	5/32	3/16
(Nominal Hole Diameter, in.)[b]	(0.144)	(0.178)	(0.207)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.032	306	386	...
0.040	376	473	557
0.050	493	581	683
0.063	527	758	847
0.071	548	783	948
0.080	571	812	1050
0.090	597	844	1085
0.100	623	876	1120
0.125	688	956	1215
0.160	778	1065	1345
0.190	814	1160	1455
0.250	...	1245	1680
0.312	...	...	1685
Rivet shear strength[c]	814	1245	1685
	Yield Strength, lbs.[d]		
Sheet thickness, in.:			
0.032	306	386	...
0.040	376	473	557
0.050	493	581	683
0.063	527	758	847
0.071	548	783	948
0.080	571	812	1050
0.090	597	844	1085
0.100	623	876	1120
0.125	688	956	1215
0.160	778	1065	1345
0.190	814	1160	1455
0.250	...	1245	1680
0.312	...	...	1685

[a]Data supplied by Allfast Fastening Systems.
[b]Loads developed from tests with hole diameters of 0.144, 0.178, and 0.207, ± 0.001 inch.
[c]Rivet shear strength is documented in MIL-R-7885D.
[d]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.1.2(n). *Static Joint Strength of Blind Protruding Head Locked Spindle Aluminum Alloy Rivets in Aluminum Alloy Sheet*

Rivet Type	HC3213[a] (F_{su} = 51 ksi approx.)		
Sheet Material	Clad 2024-T3		
Rivet Diameter, in.	1/8	5/32	3/16
(Nominal Hole Diameter, in.)[b]	(0.130)	(0.162)	(0.194)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.025	249	...	...
0.032	314	397	...
0.040	387	489	593
0.050	479[e]	603	730
0.063	538[e]	753[e]	908
0.071	558[e]	812[e]	1015
0.080	581[e]	840[e]	1140[e]
0.090	607[e]	872[e]	1180[e]
0.100	632[e]	904[e]	1220[e]
0.125	664[e]	983[e]	1315[e]
0.160	...	1030[e]	1450[e]
0.190	...	...	1480[e]
Rivet shear strength[c]	664	1030	1480
	Yield Strength, lbs.[d]		
Sheet thickness, in.:			
0.025	222	...	...
0.032	275	353	...
0.040	294	428	525
0.050	312	457	628
0.063	336	487	664
0.071	351	505	686
0.080	368	526	711
0.090	386	549	738
0.100	405	572	766
0.125	451	629	834
0.160	...	709	931
0.190	...	...	1010

[a]Data supplied by Huck International Inc.
[b]Loads developed from tests with hole diameters of 0.130, 0.162, and 0.194, ±0.001 inch.
[c]Rivet shear strength is documented in MIL-R-7885D.
[d]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).
[e]Yield is less than 2/3 of indicated ultimate.

TABLE 8.1.3.2.1(a). *Static Joint Strength of Blind 100° Flush Head A-286 Rivets in Machine-Countersunk Alloy Steel, Titanium Alloy, and A-286 Alloy Sheet*

Rivet Type	CR 6626[a] (F_{su} = 75 ksi)			
Sheet Material	Alloy Steel, F_{tu} = 125 ksi, Titanium Alloy, F_{tu} = 120 ksi, and A-286 Alloy, F_{tu} = 140 ksi			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.040	582[b]	...	...	...
0.050	693	[c] 898[b]	...	...
0.063	842	1082	[c] 1351[b]	...
0.071	891	1189	1478	[c] ...
0.080	949	1303	1633	...
0.090	970	1379	1798	2558[b]
0.100	...	1461	1916	2772 [c]
0.112	...	1490	2026	3036
0.125	...	...	2150	3333
0.140	...	...	...	3531
0.160	...	...	...	3795
0.190	...	...	...	3890
Rivet shear strength[d]	970	1490	2150	3890
	Yield Strength[e], lbs			
Sheet thickness, in.:				
0.040	355	...	...	...
0.050	499	557	...	...
0.063	681	784	858	...
0.071	771	923	1031	...
0.080	858	1082	1223	...
0.090	920	1202	1424	1700
0.100	...	1297	1643	1997
0.112	...	1417	1779	2327
0.125	...	...	1925	2690
0.140	...	...	...	3053
0.160	...	...	...	3432
0.190	...	...	...	3845
Head height (ref.), in.	0.042	0.055	0.070	0.095

[a]Data supplied by Cherry Fasteners.
[b]Yield value is less than 2/3 of the indicated ultimate strength value.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Rivet shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 75 ksi.
[e]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.2.1(b). *Static Joint Strength of Blind 100° Flush Head Monel Rivets in Machine-Countersunk Stainless Steel*

Rivet Type	MS20601M (R.T. F_{su} = 55 ksi)											
Sheet Material	17-7PH, TH 1050											
Temperature	Room				500 F				700 F			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs											
Sheet thickness, in.:												
0.040	373[a]	...	...	...	373[a]	...	...	...	373[a]	...	...	...
0.050	429	[b] 574[a]	...	...	429	[b] 574[a]	...	...	429	[b] 574[a]	...	...
0.063	495	664	[b] 866[a]	...	495	664	[b] 866[a]	...	495	664	[b] 866[a]	...
0.071	535	714	924	[b] ...	535	714	924	[b] ...	535	714	924	[b] ...
0.080	579	771	991	...	579	771	991	...	574	771	991	...
0.090	630	833	1065	1615[a]	625	833	1065	1615[a]	590	833	1065	1615[a]
0.100	...	896	1140	1720	[b] ...	896	1140	1720	[b] ...	884	1140	1720 [b]
0.125	...	...	1325	1970	...	...	1325	1970	...	904	1290	1970
0.160	...	...	...	2320	...	...	...	2320	...	...	1305	2300
0.180	...	...	...	2520	...	...	...	2500	...	...	...	2360
Rivet shear strength[c]	713	1090	1580	2855	648	993	1430	2590	590	904	1305	2360
	Yield strength[d], lbs											
Sheet thickness, in.:												
0.040	213	...	...	...	213	...	...	...	213	...	...	...
0.050	303	332	...	...	303	332	...	...	303	332	...	...
0.063	439	476	518	...	439	476	518	...	439	476	518	...
0.071	528	569	621	...	528	569	621	...	528	569	621	...
0.080	579	696	741	...	579	696	741	...	574	696	741	...
0.090	630	833	910	1030	625	833	910	1030	590	833	910	1030
0.100	...	896	1075	1212	...	896	1075	1212	...	884	1075	1212
0.125	...	...	1325	1731	...	...	1325	1731	...	904	1290	1731
0.160	...	...	...	2320	...	...	...	2320	...	...	1305	2300
0.180	...	...	...	2520	...	...	...	2500	...	...	...	2360
Head height (ref.), in.	0.042	0.055	0.070	0.095	0.042	0.055	0.070	0.095	0.042	0.055	0.070	0.095

[a]Yield value is less than 2/3 of the indicated ultimate strength value.

[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.

[c]Rivet shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} values at 55 ksi, 50 ksi, and 45 ksi at room temperature, 500 F and 700 F, respectively.

[d]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.2.1(c). *Static Joint Strength of Blind 100° Flush Head Monel Rivets in Dimpled Stainless Steel Sheet*

Rivet Type	MS20601M (F_{su} = 55 ksi)							
Sheet Material	AISI 301-Annealed				AISI 301-1/4 Hard			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs.							
Sheet thickness, in.:								
0.010	224	...	...	...	277	377	...	...
0.012	254	338	...	...	302	428	560	...
0.016	313	412	519	...	358	485	632	...
0.020	375	486	610	...	415	542	705	1135
0.025	447	576	722	1045	482	642	808	1230
0.032	516	705	876	1255	543	750	963	1400
0.040	536	793	1055	1490	585	833	1110	1660
0.050	565	825	1150[a]	1790	628	910	1240	1930
0.063	...	868	1200[a]	2065	...	964	1330	2175
0.071	...	...	...	2100	...	973	1375	2275
0.080	...	...	...	2150	...	...	1405	2340
0.090	...	...	...	2200	...	...	...	2440
0.100	...	...	...	...	...	...	...	2510
Rivet shear strength[b]	635	973	1405	2540	635	973	1405	2540
	Yield Strength[a], lbs.							
Sheet thickness, in.:								
0.010	188	...	...	...	244	291	...	...
0.012	214	281	...	...	259	335	423	...
0.016	270	352	438	...	333	428	535	...
0.020	328	422	518	...	398	528	639	896
0.025	397	506	627	873	443	612	774	1080
0.032	498	627	770	1070	505	689	912	1330
0.040	536	772	939	1310	576	779	1015	1590
0.050	565	825	1150	1590	619	883	1145	1770
0.063	...	868	1200	1970	...	954	1305	2000
0.071	...	...	...	2100	...	973	1350	2140
0.080	...	...	...	2150	...	...	1400	2305
0.090	...	...	...	2200	...	...	...	2395
0.100	...	...	...	...	...	...	...	2475
Head height (ref.), in.	0.042	0.055	0.070	0.095	0.042	0.055	0.070	0.095

[a]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.
[b]Rivet shear strength from Table 8.1.2(b).

TABLE 8.1.3.2.1(d_1). *Static Joint Strength of Blind 100° Flush Head Monel Rivets in Machine-Countersunk Stainless Steel Sheet*

Rivet Type	MS20601M (F_{su} = 55 ksi)			
Sheet Material	AISI 301-Annealed			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.040	469[a]	...	...	...
0.050	555[a]	[b] 721[a]	...	...
0.063	...	864[a]	[b] 1075[a]	...
0.071	...	...	1187[a]	[b] ...
0.080	...	...	...	...
0.090	...	...	...	2040
Rivet shear strength[c]	713	1090	1580	2855 [b]
	Yield Strength[d], lbs			
Sheet thickness, in.:				
0.040	231	...	...	...
0.050	321	359	...	...
0.063	...	500	566	...
0.071	...	...	678	...
0.080	...	...	...	...
0.090	...	...	...	1135
Head height (ref.), in.	0.042	0.055	0.070	0.095

[a]Yield value is less than 2/3 of the indicated ultimate strength value.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Rivet shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 55 ksi.
[d]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.2.1(d_2). *Static Joint Strength of Blind 100° Flush Head Monel Rivets in Machine-Countersunk Stainless Steel Sheet*

Rivet Type	MS20601M (R.T. F_{su} = 55 ksi)											
Sheet Material	AISI 301-¼ Hard											
Temperature	Room				500 F				700 F			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs											
Sheet thickness, in.:												
0.040	373[a]	...	...	...	373[a]	...	...	...	373[a]	...	...	...
0.050	450	[b] 574[a]	...	...	450[a]	[b] 574[a]	...	...	450[a]	[b] 574[a]	...	...
0.063	538	704	[b] 866[a]	...	538	704[a]	[b] 866[a]	...	538	704[a]	[b] 866[a]	...
0.071	584	773	960	[b] ...	584	773	960[a]	[b] ...	584	773	960[a]	[b] ...
0.080	637	838	1065	...	637	838	1065[a]	...	590	838	1065[a]	...
0.090	695	910	1155	1645	648	910	1155	1645[a]	...	904	1155	1645[a]
0.100	713	984	1240	1800	[b] ...	984	1240	1800[a]	[b] ...	...	1240	1800[a] [b]
0.125	...	1090	1460	2135	...	993	1430	2135	...	...	1305	2135
0.160	...	...	1580	2550	...	...	...	2550	...	...	...	2360
0.180	...	...	...	2780	...	...	...	2590	...	...	...	...
Rivet shear strength[c]	713	1090	1580	2855	648	993	1430	2590	590	904	1305	2360
	Yield Strength[d], lbs											
Sheet thickness, in.:												
0.040	231	...	...	...	192	...	...	...	192	...	...	...
0.050	336	359	...	...	279	298	...	...	279	298	...	...
0.063	459	531	566	...	425	440	471	...	425	440	471	...
0.071	530	625	698	...	525	546	576	...	525	546	576	...
0.080	607	725	835	...	607	683	690	...	590	683	690	...
0.090	693	832	966	1135	648	832	872	945	...	832	872	945
0.100	713	943	1095	1345	...	943	1060	1115	...	...	1060	1115
0.125	...	1090	1420	1815	...	993	1420	1670	...	...	1305	1670
0.160	...	...	1580	2430	...	...	...	2430	...	...	...	2360
0.180	...	...	...	2775	...	...	...	2590	...	...	...	...
Head height (ref.), in.	0.042	0.055	0.070	0.095	0.042	0.055	0.070	0.095	0.042	0.055	0.070	0.095

[a]Yield value is less than 2/3 of the indicated ultimate strength value.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Rivet shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 55 ksi at R.T., F_{tu} = 50 ksi at 500 F, and F_{su} = 45 ksi at 700 F.
[d]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.2.1(d_3). *Static Joint Strength of Blind 100° Flush Head Monel Rivets in Machine-Countersunk Stainless Steel Sheet*

Rivet Type	MS20601M (R.T. F_{su} = 55 ksi)											
Sheet Material	AISI 301-½ Hard											
Temperature	Room				500 F				700 F			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs											
Sheet thickness, in.:												
0.040	350[a]	...	...	...	350[a]	...	...	...	350[a]	...	...	...
0.050	444	[b] 540[a]	...	...	444	[b] 540[a]	...	...	444	[b] 540[a]	...	...
0.063	538	694	[b] 821	...	538	694	[b] 821	...	538	694	[b] 821	...
0.071	584	773	935	[b] ...	584	773	935	[b] ...	575	773	935	[b] ...
0.080	637	838	1065	...	624	838	1065	...	586	838	1065	...
0.090	695	910	1155	1585	648	910	1155	1585	590	886	1155	1585
0.100	713	984	1240	1780	[b] ...	962	1240	1780	[b] ...	904	1240	1780 [b]
0.125	...	1090	1460	2135	...	993	1410	2135	...	...	1305	2135
0.160	...	...	1580	2550	...	...	1430	2500	...	...	...	2345
0.180	...	...	...	2780	...	...	...	2590	...	...	...	2360
Rivet shear strength[c]	713	1090	1580	2855	648	993	1430	2590	590	904	1305	2360
	Yield Strength[d], lbs											
Sheet thickness, in.:												
0.040	231	...	...	...	231	...	...	...	231	...	...	...
0.050	336	359	...	...	336	359	...	...	336	359	...	...
0.063	459	531	566	...	459	531	566	...	459	531	566	...
0.071	530	625	698	...	530	625	698	...	530	625	698	...
0.080	607	725	835	...	607	725	835	...	586	725	835	...
0.090	693	832	966	1135	648	832	966	1135	590	832	966	1135
0.100	713	943	1095	1345	...	943	1095	1345	...	904	1095	1345
0.125	...	1090	1420	1815	...	993	1410	1815	...	...	1305	1815
0.160	...	...	1580	2430	...	...	1430	2430	...	...	...	2345
0.180	...	...	...	2775	...	...	...	2590	...	...	...	2360
Head height (ref.), in.	0.042	0.055	0.070	0.095	0.042	0.055	0.070	0.095	0.042	0.055	0.070	0.095

[a]Yield value is less than 2/3 of the indicated ultimate strength value.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Rivet shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 55 ksi at R.T., F_{su} = 50 ksi at 500 F, and F_{su} = 45 ksi at 700 F.
[d]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.2.1(e). *Static Joint Strength of Blind 100° Flush-Head Monel Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	MS20601M (F_{su} = 55 ksi)			
Sheet Material	7075-T6			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.040	320[a]	[b] ...	...	...
0.050	393	494[a]	[b] ...	...
0.063	487	612[a]	747[a]	[b] ...
0.071	545	684	832[a]	...
0.080	565	766	930[a]	...
0.090	587	840	1040	1425[a] [b]
0.100	610	867	1150	1570[a]
0.125	...	937	1270	1940
0.160	...	...	1385	2260
0.190	...	...	...	2390
Rivet shear strength[c]	713	1090	1580	2855
	Yield Strength[d], lbs			
Sheet thickness, in.:				
0.040	146	...	...	...
0.050	228	226	...	...
0.063	395	369	343	...
0.071	496	495	444	...
0.080	526	640	615	...
0.090	561	769	806	660
0.100	595	811	1000	912
0.125	...	918	1195	1560
0.160	...	...	1375	2105
0.190	...	...	...	2310
Head height (ref.), in.	0.042	0.055	0.070	0.095

[a]Yield value is less than 2/3 of the indicated ultimate strength value.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Rivet shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 55 ksi.
[d]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.2.1(f). *Static Joint Strength of Blind 100° Flush Head Aluminum Alloy (2117-T3) Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	MS20601AD and MS20603AD (F_{su} = 30 ksi)			
Sheet Material	Clad 2024-T3			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.040	159	...	...	...
0.050	236	[a] 258	...	...
0.063	327	369	[a] 398	...
0.071	360	439	485	[a] ...
0.080	388	511	577	...
0.090	...	561	684	795
0.100	...	596	768	945 [a]
0.125	...	...	862	1270
Rivet shear strength[b]	388	596	862	1550
	Yield Strength[c], lbs			
Sheet thickness, in.:				
0.040	110	...	...	...
0.050	198	185	...	...
0.063	300	308	296	...
0.071	336	384	391	...
0.080	377	468	497	...
0.090	...	524	614	621
0.100	...	592	709	973
0.125	...	...	862	1150
Head height (ref.), in.	0.042	0.055	0.070	0.095

[a]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[b]Shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 30 ksi.
[c]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.2.1(g). *Static Joint Strength of Blind 100° Flush Head Aluminum Alloy (5056-H321) Rivets in Machine-Countersunk Magnesium Alloy Sheet*

Rivet Type	MS20601B (F_{su} = 28 ksi)			
Sheet Material	AZ31B-H24			
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.040	167	...	...	...
0.050	208	[a] 257	...	...
0.063	262	324	[a] 390	...
0.071	295	366	440	[a] ...
0.080	333	413	495	...
0.090	363	464	557	749
0.100	...	516	620	833 [a]
0.125	...	556	774	1040
0.160	...	...	802	1332
0.190	...	...	...	1450
Rivet shear strength[b]	363	556	802	1450
	Yield Strength[c], lbs			
Sheet thickness, in.:				
0.040	158	...	...	...
0.050	197	244	...	...
0.063	248	308	370	...
0.071	279	346	417	...
0.080	315	391	469	...
0.090	354	440	527	710
0.100		489	587	789
0.125	...	556	734	986
0.160	...	...	802	1262
0.190	...	...	...	1450
Head height (ref.), in.	0.042	0.055	0.070	0.095

[a]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[b]Rivet shear strength based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 28 ksi.
[c]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.2.2(a). *Static Joint Strength of Blind 100° Flush Head Locked Spindle A-286 Rivets in Machine-Countersunk Alloy Steel Sheet*

Rivet Type	NAS1399C[a] (F_{su} = 75 ksi)			CR 2642[a] (F_{su} = 95 ksi)		
Sheet Material	Alloy Steel, F_{tu} = 180 ksi					
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
	Ultimate Strength, lbs.					
Sheet thickness, in.:						
0.040	380[b]	...	...	380[b]	...	...
0.050	475[b]	[c] 588[b]	...	475	[c] 588[b]	...
0.063	698	741[b]	[c] 890[b]	698	741	[c] 890[b]
0.071	840	908	1004[b]	[c] 840	908	1004[b] [c]
0.080	970	1108	1171[b]	1002	1108	1171
0.090	...	1333	1438	1185	1333	1438
0.100	...	1490	1710	1230	1559	1710
0.125	...	...	2150	...	1885	2380
0.160	...	...	...	...	...	2720
Rivet shear strength	970[d]	1490[d]	2150[d]	1230[e]	1885[e]	2720[e]
	Yield Strength[f], lbs.					
Sheet thickness, in.:						
0.040	137	...	...	180	...	...
0.050	292	219	...	320	278	...
0.063	494	468	387	536	513	432
0.071	614	620	570	665	675	628
0.080	755	793	776	816	860	847
0.090	...	983	1003	981	1063	1090
0.100	...	1176	1236	1144	1267	1337
0.125	...	...	1809	...	1777	1950
0.160	...	...	...	...	...	2720
Head height (ref.), in.	0.042	0.055	0.070	0.042	0.055	0.070

[a]Data supplied by Cherry Fasteners.
[b]Yield value is less than 2/3 of the indicated ultimate strength value.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Rivet shear strength is documented in NAS1400.
[e]Shear strength is based on areas computed from nominal hole diameters in Table 8.1.2(a) and F_{su} = 95 ksi.
[f]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.2.2(b). *Static Joint Strength of Blind 100° Flush Head Locked Spindle Monel Rivets in Machine-Countersunk Stainless Steel Sheet*

Rivet Type	NAS1399 MS or MW[a] (F_{su} = 55 ksi)		
Sheet Material	AISI 301-1/2 Hard		
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.040	287[b]	...	...
0.050	363	[c] 445[b]	...
0.063	491	569	[c] 671[b]
0.071	569	668	755[b] [c]
0.080	657	776	886
0.090	710	898	1032
0.100	...	1019	1182
0.125	...	1090	1580
Rivet shear strength[d]	710	1090	1580
	Yield Strength[e], lbs.		
Sheet thickness, in.:			
0.040	163	...	...
0.050	243	253	...
0.063	348	384	401
0.071	413	463	496
0.080	487	554	606
0.090	568	655	726
0.100	...	753	846
0.125	...	1004	1156
Head height (ref.), in.	0.042	0.055	0.070

[a]Data supplied by Cherry Fasteners.
[b]Yield value is less than 2/3 of the indicated ultimate strength value.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Rivet shear strength is documented in NAS1400.
[e]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.2.2(c). *Static Joint Strength of 100° Flush Head Locked Spindle A-286 Blind Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	NAS1921C[a] (F_{su} = 80 ksi)		
Sheet Material	Clad 7075-T6		
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
	Ultimate Strength, lbs		
Sheet thickness, in.			
0.050	612[b]	...	...
0.063	749[b]	956[b]	...
0.071	831[b]	1060[b]	...
0.080	923[b]	1180[b]	1450[b]
0.090	1110[b]	1305[b]	1605[b]
0.100	1090[b]	1435[b]	1755[b]
0.125	...	1670[b]	2130[b]
0.160	...	...	2400[b]
Rivet shear strength[c]	1090	1670	2400
	Yield Strength[d], lbs		
Sheet thickness, in.:			
0.050	365	...	...
0.063	466	571	...
0.071	528	649	...
0.080	598	737	873
0.090	639	835	990
0.100	686	931	1105
0.125	804	1065	1325
0.160	...	...	1605
Head height (ref.), in.	0.042	0.055	0.070

[a]Data supplied by Huck Manufacturing Company.
[b]Yield value is less than 2/3 of indicated ultimate strength value.
[c]Rivet shear strength is documented in NAS1900.
[d]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3) (revised May 1, 1985 from the greater of 0.012 inch or 4% of nominal diameter).

TABLE 8.1.3.2.2(d). *Static Joint Strength of Blind 100° Flush Head Locked Spindle Monel Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	NAS1399 MS or MW[a] (F_{su} = 55 ksi)		
Sheet Material	Clad 7075-T6		
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.040	323[b]	...	...
0.050	404[b]	[c] 499[b]	...
0.063	500[b]	631[b]	[c] 757[b]
0.071	557	703[b]	855[b] [c]
0.080	610	784	958[b]
0.090	636	873	1065[b]
0.100	662	937	1175
0.125	710	1015	1370
0.160	...	1090	1505
0.190	...	...	1580
Rivet shear strength[d]	710	1090	1580
	Yield Strength[e], lbs.		
Sheet thickness, in.:			
0.040	139	...	...
0.050	223	218	...
0.063	331	353	351
0.071	397	436	451
0.080	472	529	563
0.090	556	633	687
0.100	562	737	811
0.125	574	873	1120
0.160	...	894	1260
0.190	...	...	1280
Head height (ref.), in.	0.042	0.055	0.070

[a]Data supplied by Cherry Fasteners.
[b]Yield value is less than 2/3 of the indicated ultimate strength value.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Rivet shear strength is documented in NAS1400.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3) (revised May 1, 1985, from the greater of 0.005 inch or 2.5% of nominal diameter).

TABLE 8.1.3.2.2(e). *Static Joint Strength 100° Flush Head Locked Spindle Monel Blind Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	NAS 1921 M[a] (F_{su} = 75 ksi)		
Sheet Material	Clad 7075-T6		
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.050	595[b]	...	...
0.063	732[b]	927[b]	...
0.071	816[b]	1035[b]	...
0.080	913[b]	1158[b]	1400[b]
0.090	946[b]	1289[b]	1570[b]
0.100	980[b]	1415[b]	1720[b]
0.125	1020	1525[b]	2055[b]
0.160	...	1565[b]	2245[b]
0.190	...	...	2260
Rivet shear strength[c]	1020	1565	2260
	Yield Strength[d], lbs.		
Sheet thickness, in.:			
0.050	354	...	...
0.063	447	554	...
0.071	504	625	...
0.080	569	707	843
0.090	607	796	952
0.100	626	885	1060
0.125	686	972	1265
0.160	...	1080	1430
0.190	...	...	1540
Head height (ref.), in.	0.042	0.055	0.070

[a]Data supplied by Huck Manufacturing Company.
[b]Yield value is less than 2/3 of indicated ultimate value.
[c]Rivet shear strength is documented in NAS 1900.
[d]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3) (revised May 1, 1985 from the greater of 0.012 inch or 4% of nominal diameter).

TABLE 8.1.3.2.2(f). *Static Joint Strength of Blind 100° Flush Head Aluminum Alloy (2219) Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	CR 2A62[a] (F_{su} = 36 ksi)		
Sheet Material	Clad 2024-T81		
Nominal Rivet Diameter, in.	1/8	5/32	3/16
(Nominal Hole Diameter, in.)	(0.130)	(0.162)	(0.194)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.050	203	...	...
0.063	289	319	...
0.071	342	385	...
0.080	393	461	503
0.090	416	542	603
0.100	439	610	701
0.125	478	682	894
0.160	...	741	1013
0.190	...	...	1063
Rivet shear strength[b]	478	741	1063
	Yield Strength[c], lbs.		
Sheet thickness, in.:			
0.050	169	...	...
0.063	247	267	...
0.071	295	326	...
0.080	349	394	423
0.090	409	468	514
0.100	424	544	603
0.125	448	658	827
0.160	...	670	960
0.190	...	...	1002
Head height (ref.), in.	0.042	0.055	0.070

[a] Data supplied by Cherry Fasteners.
[b] Shear strength values are based on indicated nominal hole diameters and F_{su} = 36 ksi.
[c] Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.2.2(g). *Static Joint Strength of Blind 100° Flush Head Locked Aluminum Alloy Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	NAS1921B[a] (F_{su} = 36 ksi)		
Sheet Material	Clad 7075-T6		
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.040	171	...	...
0.050	232	[b] 267	...
0.063	313	366	[b] 411
0.071	360	427	484 [b]
0.080	416	498	566
0.090	477	571	658
0.100	494	647	748
0.125	...	755	978
0.160	...	...	1090
Rivet shear strength[c]	495	755	1090
	Yield Strength[d], lbs.		
Sheet thickness, in.:			
0.040	110	...	...
0.050	161	171	...
0.063	247	254	270
0.071	303	315	330
0.080	354	395	399
0.090	373	484	506
0.100	393	549	611
0.125	...	610	803
0.160	...	...	906
Head height (ref.), in.	0.042	0.055	0.070

[a]Data supplied by Huck Manufacturing Company.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Rivet shear strength is documented in NAS1900.
[d]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3) (revised May 1, 1985, from the greater of 0.005 inch or 2.5% of nominal diameter).

TABLE 8.1.3.2.2(h). *Static Joint Strength of Blind 100° Flush Head Locked Spindle Aluminum Alloy Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	NAS1399B[a] (5056) (F_{su} = 30 ksi)			NAS1399D[a] (2017) (F_{su} = 36 ksi)		
Sheet Material	Clad 2024-T3					
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
	Ultimate Strength, lbs.					
Sheet thickness, in.:						
0.040	149[b]	...	...	149[b]	...	...
0.050	223[b]	[c] 230[b]	...	223[b]	[c] 230[b]	...
0.063	310[b]	349[b]	[c] 356[b]	319[b]	349[b]	[c] 356[b]
0.071	366	415[b]	448[b]	[c] 379[b]	420[b]	448[b] [c]
0.080	388	492[b]	544[b]	423	506[b]	547[b]
0.090	...	578	646[b]	459	600[b]	660[b]
0.100	...	596	751[b]	494	652	775[b]
0.125	...	...	862	...	755	969
0.160	...	...	...	...	...	1090
Rivet shear strength[d]	388	596	862	494	755	1090
	Yield Strength[e], lbs.					
Sheet thickness, in.:						
0.040	72	...	...	72	...	...
0.050	114	113	...	114	113	...
0.063	197	182	170	197	182	170
0.071	247	245	220	247	245	220
0.080	304	316	304	304	316	304
0.090	...	396	399	367	396	399
0.100	...	473	493	431	473	493
0.125	...	...	729	...	672	729
0.160	...	...	...	...	...	1060
Head height (ref.), in.	0.042	0.055	0.070	0.042	0.055	0.070

[a]Data supplied by Cherry Fasteners.
[b]Yield value is less than 2/3 of the indicated ultimate strength value.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Rivet shear strength is documented in NAS1900.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3) (revised May 1, 1985, from the greater of 0.005 inch or 2.5% of nominal diameter).

TABLE 8.1.3.2.2(i). *Static Joint Strength of Blind 100° Flush Head Locked Spindle Aluminum Alloy Rivets in Machine-Countersunk and Dimpled Aluminum Alloy Sheet*

Rivet Type	NAS1739B[a] and NAS1739E[a,c] (F_{su} = 34 ksi)			NAS1739B[b] and NAS1739E[b,c] (F_{su} = 34 ksi)		
Sheet Material	Clad 2024-T3					
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.144)	5/32 (0.178)	3/16 (0.207)	1/8 (0.144)	5/32 (0.178)	3/16 (0.207)
	Ultimate Strength, lbs.					
Sheet thickness, in.:						
0.020	...	...	...	246	334	418
0.025	...	...	...	281	376	465
0.032	212	...	...	330	436	536
0.040	266	[d] 326	...	386	506	616
0.050	344	410	[d] ...	456	592	716
0.063	441	533	606	546	703	845
0.071	504	608	696	[d] ...	771	926
0.080	554	693	794	...	837	1015
0.090	...	787	900	...	...	1110
0.100	...	837	1015	...	...	...
0.125	...	...	1128	...	...	...
Rivet shear strength[e]	554	837	1128	554	837	1128
	Yield Strength[f], lbs.					
Sheet thickness, in.:						
0.020	...	...	...	...	...	...
0.025	...	...	...	...	...	...
0.032	159	...	...	...	...	...
0.040	212	247	...	...	...	...
0.050	279	331	...	...	...	...
0.063	365	437	492	...	...	...
0.071	418	503	568	...	...	...
0.080	448	577	654	...	...	...
0.090	...	659	750	...	...	...
0.100	...	689	845	...	...	...
0.125	...	...	960	...	...	...
Head height (ref.), in.	0.035	0.047	0.063	0.035	0.047	0.063

[a]Machine-countersunk holes.
[b]Dimpled holes. These allowables apply to double dimpled sheets and to the upper sheet dimpled into a machine-countersunk lower sheet. Sheet gauge is that of the thinnest sheet for double dimpled joints and of the upper dimpled, machine-countersunk joints. The thickness of the machine-countersunk sheet must be at least one tabulated gauge thicker than the upper sheet. In no case shall allowables be obtained by extrapolation for gauges other than those shown.
[c]Data supplied by Cherry Fasteners. Confirmatory data for machine-countersunk holes provided by Allfast Fastening Systems, Inc.
[d]The values in the table above the horizontal line in each column are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[e]Rivet shear strength is documented in NAS1740.
[f]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3) (revised May 1, 1985, from the greater of 0.005 inch or 2.5% of nominal diameter).

TABLE 8.1.3.2.2(j). *Static Joint Strength of Blind 100° Flush Head Locked Spindle Aluminum Alloy Rivets in Machine-Countersunk Magnesium Alloy Sheet*

Rivet Type	NAS1399B[a] (F_{su} = 30 ksi)				NAS1739B and NAS 1739E[a] (F_{su} = 34 ksi)		
Sheet Material	AZ31B-H24						
Rivet Diameter, in. (Nominal Hole Diameter, in.)	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)	1/8 (0.144)	5/32 (0.178)	3/16 (0.207)
	Ultimate Strength, lbs.						
Sheet thickness, in.:							
0.032	...	...	...	...	188[b]	...	...
0.040	178[b]	...	...	...	235[b]	[c] 292[b]	...
0.050	223[b]	[c] 274[b]	...	...	295	362[b]	[c] ...
0.063	292[b]	349[b]	[c] 418[b]	...	371	457	530[b]
0.071	334[b]	399[b]	471[b]	[c] ...	418	514	600[b] [c]
0.080	383[b]	459[b]	536[b]	...	471	580	671
0.090	388	526[b]	613[b]	803[b]	531	651	756
0.100	...	593[b]	693[b]	892[b]	[c] 554	725[b]	843
0.125	...	596	862	1153[b]	...	837[b]	1052[b]
0.160	...	...	...	1532[b]	...	...	...
Rivet shear strength	388[d]	596[d]	862[d]	1550[d]	554[e]	837[e]	1128[e]
	Yield Strength[f], lbs.						
Sheet thickness, in.:							
0.032	...	...	...	...	106	...	...
0.040	49	...	...	...	147	164	...
0.050	94	76	...	...	197	227	...
0.063	158	152	128	...	262	307	340
0.071	197	200	186	...	300	355	399
0.080	242	254	250	...	314	414	462
0.090	291	315	323	277	330	459	534
0.100	...	375	396	376	336	478	608
0.125	...	530	580	621	...	508	667
0.160	...	...	...	968	...	...	...
Head height (ref.), in.	0.042	0.055	0.070	0.095	0.035	0.047	0.063

[a]Data supplied by Cherry Fasteners.
[b]Yield value is less than 2/3 of the indicated ultimate strength value.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Rivet shear strength is documented in NAS1400.
[e]Rivet shear strength is documented in NAS1740 dated March 1968.
[f]Permanent set at yield load: the greater of 0.005 inch or 2.5% of nominal diameter.

TABLE 8.1.3.2.2(k). *Static Joint Strength of Blind 100° Flush Head Locked Spindle A-286 Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	CR 4622[a] (F_{su} = 75 ksi)			
Sheet Material	Clad 7075-T6			
Rivet Diameter (Nominal Hole Diameter, in.)[b]	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.050	595[c]	...	...	...
0.063	733[c]	932[c]	...	...
0.071	817[c]	1035[c]	...	...
0.080	913	1160[c]	1410[c]	...
0.090	947	1290[c]	1570[c]	...
0.100	982	1420	1725[c]	2360[c]
0.125	995	1525	2060	2880[c]
0.160	...	1545	2215	3605
0.190	...	...	...	3810
0.250	...	...	...	3920
Rivet shear strength[d]	995	1545	2215	3920
	Yield Strength[e], lbs			
Sheet thickness, in.:				
0.050	211	...	...	...
0.063	348	339	...	...
0.071	489	470	...	...
0.080	608	620	574	...
0.090	664	787	774	...
0.100	720	947	970	853
0.125	860	1120	1400	1505
0.160	...	1365	1695	2410
0.190	...	...	...	2740
0.250	...	...	...	3405
Head height (ref.), in.	0.041	0.054	0.069	0.095

[a]Data supplied by Cherry Fasteners.
[b]Allowable loads developed from test with nominal hole diameters as listed.
[c]Yield value is less than 2/3 of the indicated ultimate strength value.
[d]Fastener shear strength based upon nominal hole diameters and F_{su} = 75 ksi from data analysis.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.2.2(l). *Static Joint Strength of Blind 100° Flush Head Locked Spindle Monel Rivets in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Rivet Type	CR 4522[a] (F_{su} = 65 ksi)			
Sheet and Plate Material	Clad 7075-T6 and T651			
Rivet Diameter (Nominal Hole Diameter, in.)[b]	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)	1/4 (0.258)
	Ultimate Strength, lbs			
Sheet or plate thickness, in.:				
0.050	529[c]	...	...	...
0.063	632[c]	828[c]	...	...
0.071	694[c]	906[c]	...	...
0.080	754	995[c]	1240[c]	...
0.090	776	1095	1360[c]	...
0.100	797	1170	1475[c]	...
0.125	852	1240	1695	2485[c]
0.160	863	1335	1810	2975
0.190	...	1340	1910	3105
0.250	...	...	1920	3365
0.312	...	...	...	3400
Rivet shear strength[d]	863	1340	1920	3400
	Yield Strength[e], lbs			
Sheet or plate thickness, in.:				
0.050	169	...	...	...
0.063	346	273	...	...
0.071	454	408	...	...
0.080	561	562	483	...
0.090	621	732	688	...
0.100	682	874	888	...
0.125	833	1060	1300	1355
0.160	863	1325	1615	2225
0.190	...	1340	1885	2585
0.250	...	...	1920	3300
0.312	...	...	...	3400
Head height (ref.), in.	0.042	0.055	0.070	0.095

[a]Data supplied by Cherry Fasteners.
[b]Allowable loads developed from test with nominal hole diameters as listed.
[c]Yield value is less than 2/3 of the indicated ultimate strength value.
[d]Fastener shear strength based upon nominal hole diameters and F_{su} = 65 ksi from data analysis.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.2.2(m). *Static Joint Strength of Blind 100° Flush Head Locked Spindle Aluminum Alloy (7050) Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	NAS1721KE and NAS1721KE ( )L[a] (F_{su} = 33 ksi)		
Sheet Material	Clad 2024-T3		
Rivet Diameter, in. (Nominal Hole Diameter, in.)[b]	1/8 (0.130)	5/32 (0.162)	3/16 (0.194)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.040	221[d]	...[c]	...
0.050	277[d]	342[d]	...[c]
0.063	351	435[d]	518[d]
0.071	396	491[d]	586[d]
0.080	448	555	662[d]
0.090	450	626	747
0.100	...	697	832
0.125	...	700	950
Rivet shear strength[e]	450	700	950
	Yield Strength[f], lbs.		
Sheet thickness, in.:			
0.040	62	...	...
0.050	150	99	...
0.063	263	240	182
0.071	333	327	287
0.080	386	425	404
0.090	403	534	534
0.100	...	600	665
0.125	...	653	874
Head height (ref.), in.	0.042	0.055	0.070

[a]Data supplied by Avdel Corp.
[b]Loads developed from tests with hole diameters of 0.130, 0.162, and 0.194, ±0.001 inch.
[c]The values in the table above the horizontal line in each column are for knife-edge conditions, and the use of fasteners in this condition is undesirable. The use of knife-edge conditions in the design of military aircraft requires the specific approval of the procuring activity.
[d]Yield value is less than 2/3 of indicated ultimate value.
[e]Rivet shear strength is documented in NAS1722.
[f]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.2.2(n). *Static Joint Strength of Blind 100° Flush Head Locked Spindle A-286 Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	NAS1721C and NAS1721C( )L[a] (F_{su} = 75 ksi)		
Sheet Material	Clad 7075-T6		
Rivet Diameter, in.	1/8	5/32	3/16
(Nominal Hole Diameter, in.)	(0.130)	(0.162)	(0.194)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.040	454[d]	...[c]	...
0.050	585[d]	707[d]	...[c]
0.063	751[d]	919[d]	1075[d]
0.071	853[d]	1045[d]	1230[d]
0.080	881[d]	1190[d]	1405[d]
0.090	896	1345[d]	1595[d]
0.100	912	1365[d]	1785[d]
0.125	951	1415	1970
0.160	1000	1485	2055
0.190	...	1500	2125
0.250	...	...	2200
Rivet shear strength[e]	1000	1500	2200
	Yield Strength[f], lbs.		
Sheet thickness, in.:			
0.040	77	...	...
0.050	220	122	...
0.063	375	352	246
0.071	470	471	425
0.080	578	604	585
0.090	615	753	763
0.100	641	902	942
0.125	707	997	1330
0.160	799	1110	1470
0.190	...	1210	1585
0.250	...	...	1820
Head height (ref.), in.	0.042	0.055	0.070

[a]Data supplied by Avdel Corp.
[b]Loads developed from tests with hole diameters of 0.130, 0.162, and 0.194, ±0.001 inch.
[c]The values in the table above the horizontal line in each column are for knife-edge conditions and the use of fasteners in this condition is undesirable. The use of knife-edge conditions in the design of military aircraft requires the specific approval of the procuring activity.
[d]Yield value is less than 2/3 of indicated ultimate value.
[e]Rivet shear strength is documented in NAS1722.
[f]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.2.2(o). *Static Joint Strength of Blind 100° Flush Head Locked Spindle Aluminum Alloy Rivets in Machine Countersunk Aluminum Alloy Sheet*

Rivet Type	M7885/3[a] (F_{su} = 51 ksi approx.)		
Sheet Material	Clad 2024-T3		
Rivet Diameter, in.	1/8	5/32	3/16
(Nominal Hole Diameter, in.)[b]	(0.130)	(0.162)	(0.194)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.040	241[f]	...	...
0.050	290	[c] 375[f]	...
0.063	355	455	[c] 561[f]
0.071	394	505	620 [c]
0.080	439	560	686
0.090	471	622	760
0.100	491	683	834
0.125	543	764	1015
0.160	616	855	1125
0.190	664	932	1220
0.250	...	1030	1405
0.312	...	...	1480
Rivet shear strength[d]	664	1030	1480
	Yield Strength, lbs.[e]		
Sheet thickness, in.:			
0.040	155	...	...
0.050	197	242	...
0.063	252	310	366
0.071	286	352	417
0.080	325	400	474
0.090	367	453	537
0.100	390	506	600
0.125	434	607	758
0.160	495	683	897
0.190	548	749	975
0.250	...	880	1130
0.312	...	...	1290
Head height (ref.), in.	0.042	0.055	0.070

[a]Data supplied by Allfast Fastening Systems, Cherry Textron, and Huck Manufacturing Company.
[b]Loads developed from tests with hole diameters of 0.130, 0.162, and 0.194, ± 0.001 inch.
[c]The values of the table above the horizontal line in each column are for knife-edge conditions, and the use of fasteners in this condition is undesirable. The use of knife-edge conditions in the design of military aircraft requires the specific approval of the procuring activity.
[d]Rivet shear strength is documented in MIL-R-7885D.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).
[f]Yield is less than 2/3 of indicated ultimate.

TABLE 8.1.3.2.2(p). *Static Joint Strength of Blind 100° Flush Head Locked Spindle Aluminum Alloy Rivets in Machine Countersunk Aluminum Alloy Sheet*

Rivet Type	M7885/7[a] (F_{su} = 51 ksi approx.)		
Sheet Material	Clad 2024-T3		
Rivet Diameter, in.	1/8	5/32	3/16
(Nominal Hole Diameter, in.)[b]	(0.144)	(0.178)	(0.207)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.032	204	...	...
0.040	249	[c] 315	...
0.050	304	384	[c] ...
0.063	376	472	557
0.071	420	527	621 [c]
0.080	469	588	692
0.090	525	656	771
0.100	580	725	851
0.125	691	895	1049
0.160	769	1072	1327
0.190	814	1154	1462
0.250	...	1245	1652
0.312	...	...	1685
Rivet shear strength[d]	814	1245	1685
	Yield Strength, lbs.[e]		
Sheet thickness, in.:			
0.032	162	...	...
0.040	202	250	...
0.050	252	312	...
0.063	318	393	457
0.071	358	443	515
0.080	400	499	580
0.090	435	561	653
0.100	470	615	725
0.125	557	723	876
0.160	679	875	1052
0.190	784	1004	1203
0.250	...	1264	1504
0.312	...	...	1685
Head height (ref.), in.	0.035	0.047	0.063

[a]Data supplied by Allfast Fastening Systems, Cherry Textron, and Huck Manufacturing Company.
[b]Loads developed from tests with hole diameters of 0.144, 0.178, and 0.207, ± 0.001 inch.
[c]The values of the table above the horizontal line in each column are for knife-edge conditions, and the use of fasteners in this condition is undesirable. The use of knife-edge conditions in the design of military aircraft requires the specific approval of the procuring activity.
[d]Rivet shear strength is documented in MIL-R-7885D.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.2.2(q). *Static Joint Strength of Blind 100° Flush Head Locked Spindle Aluminum Alloy Rivets in Machine Countersunk Aluminum Alloy Sheet*

Rivet Type	HC3212[a] (F_{su} = 51 ksi approx.)		
Sheet Material	Clad 2024-T3		
Rivet Diameter, in.	1/8	5/32	3/16
(Nominal Hole Diameter, in.)[b]	(0.130)	(0.162)	(0.194)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.040	241	...	...
0.050	290	[c] 375	...
0.063	355	455	[c] 561
0.071	394	505	620 [c]
0.080	439	560	686
0.090	488	622	760
0.100	538	683	834
0.125	631	837	1015
0.160	664	999	1260
0.190	...	1030	1420
0.250	...	...	1480
Rivet shear strength[d]	664	1030	1480
	Yield Strength, lbs.[e]		
Sheet thickness, in.:			
0.040	169	...	...
0.050	250	265	...
0.063	355	395	417
0.071	394	475	513
0.080	427	560	621
0.090	450	622	741
0.100	473	664	834
0.125	529	735	970
0.160	609	834	1090
0.190	...	919	1190
0.250	...	...	1395
Head height (ref.), in.	0.042	0.055	0.070

[a]Data supplied by Huck International Inc.
[b]Loads developed from tests with hole diameters of 0.130, 0.162, and 0.194, ± 0.001 inch.
[c]The values of the table above the horizontal line in each column are for knife-edge conditions, and the use of fasteners in this condition is undesirable. The use of knife-edge conditions in the design of military aircraft requires the specific approval of the procuring activity.
[d]Rivet shear strength is documented in MIL-R-7885D.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

Proposed Table 8.1.3.2.2 (r). Static Joint Strength of Blind 100 Flush Head Locked Spindle 2014 Aluminum Alloy Rivets in Machine Countersunk Aluminum Alloy Sheet

Rivet Type	MBC 4807 and 4907 (F_{su} = 33 ksi approx.)[a]		
Sheet Material	Clad 2024-T3		
Rivet Diameter, in.	1/8	5/32	3/16
(Nominal Hole Diameter, in.)[b]	(0.130)	(0.162)	(0.194)
	Ultimate Strength, lbs.		
Sheet Thickness, in.:			
0.040	183 [c]	---	---
0.050	243	286 [c]	---
0.063	320	382	437 [c]
0.071	368	441	508
0.080	412	508	588
0.090	435	582	677
0.100	450	641	766
0.125	---	700	937
0.160	---	---	950
Rivet Shear Strength[d]	450	700	950
	Yield Strength, lbs.[e]		
Sheet Thickness, in.:			
0.040	102	---	---
0.050	173	160	---
0.063	264	274	263
0.071	309	345	347
0.080	333	423	441
0.090	360	486	546
0.100	387	519	651
0.125	---	602	765
0.160	---	---	904
Head Height (ref.), in.	0.041	0.053	0.068

(a) A product of Avdel Systems Ltd.
(b) Loads developed from tests with hole diameters of 0.130, 0.162, and 0.194, +/- 0.001 inch.
(c) The values in the table above the horizontal line in each column are for knife-edge conditions, and the use of fasteners in this condition is undesirable. The use of knife-edge conditions in the design of military aircraft requires the specific approval of the procuring activity.
(d) Rivet shear strength is documented in NAS 1722, and rivets meet the requirements of NAS 1721.
(e) Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

Table 8.1.3.2.2 (s). Static Joint Strength of Blind Protruding Head Locked Spindle 2014 Aluminum Alloy Rivets in Aluminum Alloy Sheet

Rivet Type	MBC 4801 and 4901 (F_{su} = 33 ksi approx.)[a]		
Sheet Material	Clad 2024-T3		
Rivet Diameter, in.	1/8	5/32	3/16
(Nominal Hole Diameter, in.)[b]	(0.130)	(0.162)	(0.194)
	Ultimate Strength, lbs.		
Sheet Thickness, in.:			
0.025	247	---	---
0.032	284	389	---
0.040	326	441	571
0.050	378	507	650
0.063	415	589	751
0.071	437	617	814
0.080	450	649	864
0.090	---	684	906
0.100	---	700	948
0.125	---	---	950
Rivet Shear Strength[c]	450	700	950
	Yield Strength, lbs.[d]		
Sheet Thickness, in.:			
0.025	238	---	---
0.032	277	375	---
0.040	321	431	552
0.050	368	500	635
0.063	381	572	743
0.071	389	583	810
0.080	399	594	828
0.090	---	607	843
0.100	---	619	858
0.125	---	---	896

(a) A product of Avdel Systems Ltd.
(b) Loads developed from tests with hole diameters of 0.130, 0.162, and 0.194, ±0.001 inch.
(c) Rivet shear strength is documented in NAS 1722, and rivets meet the requirements of NAS 1720.
(d) Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.2.3(a). *Static Joint Strength of Blind 100° Flush Head A286 Bolts in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	MS21140[a] (F_{su} = 95 ksi)				
Sheet and Plate Material	Clad 7075-T6 and T651				
Fastener Diameter, in. (Nominal Shank Diameter, in.)	5/32 (0.163)	3/16 (0.198)	1/4 (0.259)	5/16 (0.311)	3/8 (0.373)
	Ultimate Strength, lbs				
Sheet or plate thickness, in.:					
0.071	1165[b]	...	...	...	...
0.080	1330[b]	[c] 1600[b]	...	...	...
0.090	1515[b]	1805[b]	[c] ...	...	...
0.100	1700[b]	2020[b]	2615[b]	...	...
0.125	1980[b]	2595[b]	3295[b]	[c] 3935[b]	...
0.160	...	2925[b]	4335[b]	5080[b]	[c] 6010[b]
0.190	...	...	5005[b]	6150[b]	7205[b] [c]
0.200	...	...	...	6520[b]	6580[b]
0.250	...	...	...	7215[b]	9810[b]
0.312	...	...	...	...	10380[b]
Fastener shear strength[d]	1980	2925	5005	7215	10380
	Yield Strength[e], lbs				
Sheet or plate thickness, in.:					
0.071	478	...	...	...	...
0.080	584	627	...	...	...
0.090	702	730	...	...	...
0.100	819	901	1025	...	...
0.125	1115	1260	1435	1540	...
0.160	...	1760	2090	2285	2430
0.190	...	...	2655	2965	3235
0.200	...	...	...	3190	3510
0.250	...	...	...	4320	4860
0.312	...	...	...	...	6460
Head height (ref.), in.	0.074	0.082	0.108	0.140	0.168

[a]Data supplied by Huck Manufacturing Company.
[b]Yield value is less than 2/3 of the indicated ultimate strength value.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Fastener shear strength is documented in MIL-F-8975.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3) (revised May 1, 1986, from the greater of 0.012 inch or 4% of nominal diameter).

TABLE 8.1.3.2.3(b_1). *Static Joint Strength of Blind 100° Flush Head Alloy Steel Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	MS90353, MS90353S, and MS90353U[a] (F_{su} = 112 ksi)				
Sheet and Plate Material	Clad 2024-T3 and T351				
Fastener Diameter, in. (Nominal Shank Diameter, in.)	5/32 (0.163)	3/16 (0.198)	1/4 (0.259)	5/16 (0.311)	3/8 (0.373)
	Ultimate Strength, lbs				
Sheet or plate thickness, in.:					
0.071	1120[b]	...	...	...	...
0.080	1305[b]	[c] 1480[b]	...	...	...
0.090	1510[b]	1735[b]	[c] ...	...	...
0.100	1740[b]	2000[b]	2380[b]	...	...
0.125	2080[b]	2670[b]	3210[b]	[c] 3625[b]	...
0.160	2340[b]	3195[b]	4440[b]	5060[b]	[c] 5700[b]
0.190	...	3450[b]	5090[b]	6310[b]	7180[b] [c]
0.250	...	...	5900[b]	7860[b]	9890[b]
0.312	...	...	...	8500[b]	11600[b]
0.375	...	...	...	...	12200[b]
Fastener shear strength[d]	2340	3450	5900	8500	12200
	Yield Strength[e], lbs				
Sheet or plate thickness, in.:					
0.071	403	...	...	...	...
0.080	513	501	...	...	...
0.090	636	652	...	...	...
0.100	759	799	1045	...	...
0.125	989	1170	1525	1620	...
0.160	1170	1510	2200	2430	2610
0.190	...	1700	2700	3120	3440
0.250	...	...	3330	4170	5095
0.312	...	...	...	4955	6175
0.375	...	...	...	...	7135
Head height (ref.), in.	0.072	0.080	0.105	0.137	0.165

[a]Data supplied by Huck Manufacturing Company.
[b]Yield strength value is less than 2/3 of indicated ultimate strength value.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Fastener shear strength is documented in MIL-F-81177.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.2.3(b_2). *Static Joint Strength of Blind 100° Flush Head Alloy Steel Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Rivet Type	MS90353[a] (F_{su} = 112 ksi)				
Sheet and Plate Material	Clad or Bare 7075-T6 and T651				
Fastener Diameter, in. (Nominal Hole Diameter, in.)	5/32 (0.163)	3/16 (0.198)	1/4 (0.259)	5/16 (0.311)	3/8 (0.373)
	Ultimate Strength, lbs				
Sheet or plate thickness, in.:					
0.071	1360[c]	...	...	...	...
0.080	1535[c]	[b] 1830[c]	...	...	...
0.090	1710[c]	2090[c]	[b] ...	...	...
0.100	1880[c]	2330[c]	2970[c]	...	...
0.125	2200[c]	2825[c]	3805[c]	[b] 4490[c]	...
0.160	2340	3365	4760[c]	5850[c]	[b] 6960[c]
0.190	...	3450	5370[c]	6790[c]	8310[c] [b]
0.250	...	...	5900	8290[c]	10450[c]
0.312	...	...	...	8500	12200
0.375	...	...	...	...	12200
Fastener shear strength[d]	2340	3450	5900	8500	12200
	Yield Strength[e], lbs				
Sheet or plate thickness, in.:					
0.071	557	...	...	...	...
0.080	666	757	...	...	...
0.090	787	875	...	...	...
0.100	909	1025	1240	...	...
0.125	1215	1395	1640	1860	...
0.160	1640	1910	2315	2590	2850
0.190	...	2355	2895	3290	3675
0.250	...	...	4055	4680	5345
0.312	...	...	...	6125	7075
0.375	...	...	...	...	8830
Head height (ref.), in.	0.072	0.080	0.105	0.137	0.165

[a]Data supplied by Huck Manufacturing Company.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Yield value is less than 2/3 of indicated ultimate strength value.
[d]Fastener shear strength is documented in MIL-F-81177.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3) revised May 1, 1986, from the greater of 0.012 inch or 4% of nominal diameters.

TABLE 8.1.3.2.3(c). *Static Joint Strength of Blind 100° Flush Head Alloy Steel Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	FF-200[a]		FF-260[a]		FF-312[a]	
Sheet and Plate Material	Clad 2024-T42	Clad 7075-T6	Clad 2024-T42	Clad 7075-T6	Clad 2024-T42	Clad 7075-T6
Fastener Diameter, in. (Nominal Shank Diameter, in.)	3/16 (0.198)	3/16 (0.198)	1/4 (0.259)	1/4 (0.259)	5/16 (0.311)	5/16 (0.311)
	Ultimate Strength, lbs					
Sheet or plate thickness, in.:						
0.071	1220[b]	1360[b]	...	...	...	...
0.080	1380[b]	1500[b]	[c] ...	...	...	...
0.090	1520[b]	1620[b]	...	...	...	...
0.100	1650[b]	1740[b]	2250[b]	2700[b]	...	...
0.125	1890[b]	1960	2940[b]	3220[b]	[c] 2720	3080[b]
0.160	2160	2200	3390[b]	3570[b]	3600[b]	3940[b] [c]
0.190	2400	2420	3730[b]	2860[b]	4490[b]	4810[b]
0.250	2620	2620	4260[b]	4320	5550[b]	6000[b]
0.312	...	...	4500	4500	6000[b]	...
Fastener shear strength[d]	2620	2620	4500	4500	6000	6000
	Yield Strength[e], lbs					
Sheet or plate thickness, in.:						
0.071	685	850	...	...	...	...
0.080	770	930	...	...	...	...
0.090	870	1025	...	...	...	...
0.100	980	1130	1120	1280	...	...
0.125	1200	1350	1380	1600	1440	1540
0.160	1500	1640	1700	2050	1820	1980
0.190	1800	1960	2010	2470	2200	2520
0.250	2400	2550	2600	3190	2950	3710
0.312	...	...	3200	3880	3690	...
Head height (ref.), in.	0.077		0.102		0.134	

[a]Data supplied by Monogram Aerospace Fasteners.
[b]Yield value is less than 2/3 of indicated ultimate strength value.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Fastener shear strength is documented in NAS1675.
[e]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.3.2.3(d). *Static Joint Strength of Blind 100° Flush Head Alloy Steel Fasteners in Machine-Countersunk Aluminum Alloy Sheet*

Fastener Type	NS 100[a]		
Sheet Material	Clad 7075-T6		
Fastener Diameter, in. (Nominal Shank Diameter, in.)	5/32 (0.163)	3/16 (0.198)	1/4 (0.259)
	Ultimate Strength, lbs		
Sheet thickness, in.:			
0.063	1085[b]	...	...
0.071	1295[b]	1400[b]	...
0.080	1525[b]	1710[b]	...
0.090	1695[b]	2020[b]	...
0.100	1830[b]	2335[b]	2715[b]
0.125	2170[b]	2745[b]	3765[b]
0.160	2190	3325[b]	4615[b]
0.190	...	3325[b]	5280[b]
0.250	...	...	5690[b]
Fastener shear strength[d]	2190	3325	5690
	Yield Strength[e], lbs		
Sheet thickness, in.:			
0.063	516	...	...
0.071	602	690	...
0.080	698	805	...
0.090	804	936	...
0.100	911	1065	1300
0.125	1180	1390	1725
0.160	1500	1835	2320
0.190	...	2165	2830
0.250	...	...	3725
Head height (ref.), in.	0.069	0.077	0.102

[a]Data supplied by Monogram Aerospace Fasteners.
[b]Yield value is less than 2/3 of the indicated ultimate strength value.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Fastener shear strength values are A basis from analysis of test data.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3) (revised May 1, 1985, from the greater of 0.012 inch or 4% of nominal diameter).

TABLE 8.1.3.2.3(e). *Static Joint Strength of Blind 100° Flush Head Aluminum Alloy Fasteners in Machine-Countersunk Aluminum Alloy Sheet*

Fastener Type	SSHFA-200[a] (F_{su} = 50 ksi)		SSHFA-260[a] (F_{su} = 50 ksi)	
Sheet Material	Clad 2024-T42	Clad 7075-T6	Clad 2024-T42	Clad 7075-T6
Fastener Diameter, in. (Nominal Shank Diameter, in.)	3/16 (0.198)	3/16 (0.198)	1/4 (0.259)	1/4 (0.259)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.050	500	590	...	...
0.063	640	750	... [b]	...
0.071	790	880	...	...
0.080	1040	1060	1310	1480
0.090	1270	1270	1480	1650 [b]
0.100	1450	1450	1680	1850
0.125	1550	1550	2010	2250
0.160	...	...	2300	2650
0.190	...	...	2520	...
0.250	...	...	2650	...
Fastener shear strength[c]	1550	1550	2650	2650
	Yield Strength[d], lbs			
Sheet thickness, in.:				
0.050	500	520	...	...
0.063	630	700	...	...
0.071	740	800	...	...
0.080	860	915	940	1160
0.090	990	1040	1080	1300
0.100	1130	1180	1230	1460
0.125	1340	1420	1550	1790
0.160	...	...	1980	2240
0.190	...	...	2420	...
0.250	...	...	2650	...
Head height (ref.), in.	0.061	0.061	0.088	0.088

[a]Data supplied by Monogram Aerospace Fasteners.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Fastener shear strength is documented in NAS1675.
[d]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.3.2.3(f). *Static Joint Strength of Blind 100° Flush Head Alloy Steel Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	PLT-150[a] (F_{su} = 112 ksi) (H-11 Nut and screw, Inconel X-750 or A-286 Sleeve)			
Sheet or Plate Material	Clad 7075-T6 and T651			
Fastener Diameter, in.	5/32	3/16	1/4	3/8
(Nominal Shank Diameter, in.)	(0.163)	(0.198)	(0.259)	(0.373)
	Ultimate Strength, lbs			
Sheet or plate thickness, in.:				
0.063	1120[b]	...	...	...
0.071	1320[b]	[c] 1470[b]	...	...
0.080	1550[b]	1755[b]	[c] ...	...
0.090	1730[b]	2060[b]	...	...
0.100	1885[b]	2350[b]	2820[b]	...
0.125	2300[b]	2850[b]	3825[b]	[c] ...
0.160	2340[b]	3450[b]	4790[b]	6695[b]
0.190	...	...	5570[b]	8440[b] [c]
0.250	...	...	5900[b]	10700[b]
0.312	...	...	...	12250[b]
Fastener shear strength[d]	2340	3450	5900	12250
	Yield Strength[e], lbs			
Sheet or plate thickness, in.:				
0.063	534	...	...	...
0.071	615	730	...	...
0.080	705	830	...	...
0.090	805	953	...	...
0.100	906	1075	1345	...
0.125	1235	1390	1750	...
0.160	1545	1910	2310	3160
0.190	...	...	2965	3850
0.250	...	...	3840	5395
0.312	...	...	...	6985
Head height (ref.), in.	0.069	0.077	0.102	0.160

[a]Data supplied by Voi-Shan Industries (Inconel X-750 Sleeve) and Monogram Aerospace Fasteners (A-286 Sleeve).
[b]Yield value is less than 2/3 of the indicated ultimate strength value.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Fastener shear strength based on area computed from nominal shank diameter in Table 9.4.1.2(a) and F_{su} = 112 ksi.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3) (revised May 1, 1985, from the greater of 0.012 inch or 4% or nominal diameter).

TABLE 8.1.3.2.3(g). *Static Joint Strength of Blind 100° Flush Head Alloy Steel Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	NAS1670-L[a]				
Sheet and Plate Material	Clad 7075-T6 and T651				
Fastener Diameter, in.[b] (Nominal Shank Diameter, in.)	5/32 (0.163)	3/16 (0.198)	1/4 (0.259)	5/16 (0.311)	3/8 (0.373)
	Ultimate Strength, lbs				
Sheet or plate thickness, in.:					
0.063	1110[c]	...	...	...	...
0.071	1230[c]	[d] 1530[c]	...	...	...
0.080	1365[c]	1700[c]	[d] ...	...	...
0.090	1525[c]	1885[c]	...	...	...
0.100	1678[c]	2065[c]	2800[c]	...	...
0.125	1678	2530[c]	3400[c]	[d] 4165[c]	...
0.160	1678	2620[c]	4255[c]	5190[c]	6350[c]
0.190	...	2620	4500[c]	6000[c]	7395[c] [d]
0.250	...	...	4500	6000	9625[c]
0.312	...	...	...	...	9750
0.375	...	...	...	...	9750
Fastener shear strength[e]	1678	2620	4500	6000	9750
	Yield Strength[f], lbs				
Sheet or plate thickness, in.:					
0.063	500	...	...	...	...
0.071	601	647	...	...	...
0.080	711	788	...	...	...
0.090	802	941	...	...	...
0.100	887	1085	1255	...	...
0.125	1105	1340	1770	1930	...
0.160	1405	1700	2250	2720	3055
0.190	...	2020	2655	3200	3890
0.250	...	...	3480	4185	5020
0.312	...	...	...	...	6280
0.375	...	...	...	...	7520
Head height (ref.), in.	0.069	0.077	0.102	0.134	0.160

[a]Data supplied by Monogram Aerospace Fasteners.
[b]Fasteners installed in 0.165/0.166, 0.200/0.201, 0.261/0.262, 0.312/0.313, 0.375/0.376 inch holes.
[c]Yield value is less than 2/3 of the indicated ultimate strength value.
[d]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[e]Fastener shear strength is documented in NAS1675.
[f]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.3.2.3(h). *Static Joint Strength of Blind 100° Flush Head Aluminum Alloy Fasteners in Machine-Countersunk Aluminum Alloy Sheet*

Fastener Type	NAS1674-L[a]		
Sheet Material	Clad 7075-T6		
Fastener Diameter, in. (Nominal Shank Diameter, in.)[b]	5/32 (0.163)	3/16 (0.198)	1/4 (0.259)
	Ultimate Strength, lbs		
Sheet thickness, in.:			
0.050	548[c]	...	...
0.063	756[c]	853	...
0.071	882[c]	1010	...
0.080	960	1185	...
0.090	...	1375	1645
0.100	...	1550	1900
0.125	...	...	2535
0.160	...	...	2650
Fastener shear strength[d]	960	1550	2650
	Yield Strength[e], lbs		
Sheet thickness, in.:			
0.050	356	...	...
0.063	481	666	...
0.071	561	774	...
0.080	650	892	...
0.090	...	1025	1275
0.100	...	1155	1450
0.125	...	...	1880
0.160	...	...	2480
Head height (ref.), in.	0.049	0.061	0.088

[a]Data supplied by Monogram Aerospace Fasteners.
[b]Fasteners installed in 0.165/0.166, 0.199/0.200, 0.260/0.261 inch holes.
[c]Yield value is less than 2/3 of the indicated ultimate strength value.
[d]Fastener shear strength is documented in NAS1675.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

8.1.4 SWAGED COLLAR/UPSET-PIN FASTENERS.—The strengths shown in the following tables are applicable only when grip lengths and hole tolerances are as recommended by respective fastener manufacturers. For some fastener systems, permanent set at yield load may be increased if hole sizes greater than those listed in the applicable table are used. This condition may exist even though the test hole size lies within the manufacturer's recommended hole size range (refer to Secion 9.4.1.3.3).

The ultimate allowable shear load for lockbolts and lockbolt stumps may be obtained from Table 8.1.4 for the appropriate shear stress level. Tensile strengths of lockbolts and lockbolt stumps also are contained in Table 8.1.4.

For lockbolts under combined loading of shear and tension installed in material having a thickness large enough to make the shear cutoff strength critical for shear loading, the following interaction equations are applicable:

$$\text{Steel lockbolts, } R_t + R_s^{10} = 1.0$$
$$\text{7075-T6 lockbolts, } R_t + R_s^{5} = 1.0$$

where R_t and R_s are the ratios of applied load to allowable load in tension and shear, respectively.

Unless otherwise specified, yield load is defined in Section 9.4.1.3.3 as the load which results in a joint permanent set equal to 0.4D, where D is the decimal equivalent of the fastener shank diameter, as defined in 9.4.1.2(a).

8.1.4.1 *Protruding-Head Swaged Collar Fastener Joints.*—Tables 8.1.4.1(a) and (b) contain joint allowables for various protruding-head swaged collar fastener/sheet material combinations. It has been shown that protruding shear head (representative configurations are NAS2406 to NAS2412 and M43859/1) fastener joints may not develop the full bearing strength of joint material. Therefore, static allowable loads for protruding shear head fasteners must be established from test data using the criteria specified in Section 9.4.1. For shear joints with protruding tension head fasteners, the load per fastener at which shear or bearing type of failure occurs is calculated separately and the lower of the two governs the design. Allowable shear loads are obtained from Table 8.1.4.

The design bearing stresses for various materials at room and other temperatures are given in strength properties stated for each alloy or group of alloys, and are applicable to joints with pins in cylindrical holes and where $t/D \geq 0.18$. Where $t/D < 0.18$, tests to substantiate yield and ultimate bearing strengths must be performed. These bearing stresses are applicable only for design of rigid joints where there is no possibility of relative motion of the parts joined without deformation of such parts.

For convenience, "unit" sheet bearing strengths for pins, based on bearing stress of 100 ksi and nominal fastener diameters, are given in Table 8.1.5.1. The strength for a specific combination of fastener, sheet thickness, and sheet material is obtained by multiplying the proper "unit" strength by the ratio of material allowable bearing stress (ksi) to 100.

8.1.4.2 *Flush-Head Swaged Collar Fastener Joints.*—Tables 8.1.4.2(a) through (j) contain joint allowables for various flush-head swaged collar fastener/sheet material combinations. The allowable loads for flush-head swaged collar fasteners were established from test data using the following criteria, unless otherwise noted in the footnotes of individual tables.

Ultimate Load.—Average ultimate test load divided by a factor of 1.14, as defined in Section 9.4. This factor is not applicable to shear strength cutoff values which may be either the procurement specification shear strength (S value) of the fastener or, if no specification exists, a statistical value determined from test results as described in Section 9.4.

The allowable loads shown for flush-head swaged collar fasteners are applicable to joints having e/D equal to or greater than 2.0.

For machine countersunk joints, the sheet gage specified in the tables is that of countersunk sheet. When the noncountersunk sheet is thinner than the countersunk sheet, the bearing allowable for the noncountersunk sheet-fastener combination should be computed, compared to the table value, and the lower of the two values selected.

TABLE 8.1.4. *Ultimate Single-Shear and Tensile Strengths of Lockbolts and Lockbolt Stumps*[a]

Nominal Diameter (inches)	Heat Treated Alloy Steel[b](160 ksi)			7075-T6[c]	
	Single-Shear Strength, lbs.	Tensile Strength, lbs.		Single-Shear Strength, lbs.	Tensile Strength, lbs.
		Tensile Type[d]	Shear Type[e]	Tensile type[d]	
		NAS 1456 thru 1462 NAS 1465 thru 1472 NAS 1475 thru 1482 NAS 1486 thru 1492 NAS 1496 thru 1502	NAS 1414 thru 1422 NAS 1424 thru 1432 NAS 1436 thru 1442 NAS 1446 thru 1452	NAS 1516 thru 1522 NAS 1525 thru 1532 NAS 1535 thru 1542 NAS 1546 thru 1552 NAS 1556 thru 1562	
5/32	2007[f]/ 1822[g]	1100[f]	705[g]	960[f]	740[f]
3/16	2623	2210	1105	1260	1195
1/4	4660	4080	2040	2185	2200
5/16	7290	6500[d]	3250	3450	3500
3/8	10490	10100[h]	5050	4970	5455

[a]Lockbolts are pull-gun driven; lockbolt stumps are hammer or squeeze driven.
[b]Used with 2024-T4 aluminum alloy collar, NAS 1080.
[c]Used with 6061-T6 aluminum alloy collar.
[d]Tensile type have a higher head and more grooves than the shear type and can be either protruding or 100° flush head. Strength value listed refers to lowest strength fastener configuration within this type.
[e]Shear type have shorter head and less grooves than the tensile type and can be either protruding or 100° flush head. Strength values listed refer to lowest strength fastener configuration within this type.
[f]Available as lockbolt only.(0.164 dia. for #8 lockbolts.)
[g]Available as lockbolt stump only. (0.156 dia. for 5/32 stumps.)
[h]Five groove design on lockbolts.

TABLE 8.1.4.1(a). *Static Joint Strength of Protruding Shear Head Ti-6Al-4V Cherrybuck Fasteners in Aluminum Alloy Sheet*

Fastener Type	CSR 925[a] (F_{su}=95 ksi)		
Sheet Material	Clad 7075-T6		
Fastener Diameter, in.	5/32	3/16	1/4
(Nominal Shank Diameter, in.)[b]	(0.164)	(0.190)	(0.250)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.050	995	...	...
0.063	1227	1442	...
0.071	1371	1607	...
0.080	1532	1792	2415
0.090	1711	2001	2688
0.100	1890	2205	2960
0.125	2007	2694	3641
0.160	...	...	4595
0.190	...	...	4660
Fastener shear strength[c]	2007	2694	4660
	Yield Strength[d], lbs.		
Sheet thickness, in.:			
0.050	861	...	...
0.063	1013	1225	...
0.071	1107	1334	..
0.080	1213	1455	2067
0.090	1331	1592	2246
0.100	1448	1727	2425
0.125	1741	2068	2873
0.160	...	...	3499
0.190	...	...	4036

[a] Data supplied by Cherry Fasteners.
[b] Fasteners installed in clearance holes (0.0005"-0.002") (Ref. Section 8.1.4).
[c] Fastener shear strength based on area computed from nominal shank diameters in Table 9.4.1.2(a) and F_{su} = 95 ksi.
[d] Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.4.1(b). *Static Joint Strength of Protruding Shear Head Ti-6Al-4V Cherrybuck Fasteners in Aluminum Alloy Sheet*

Fastener Type	CSR 925 [a] (F_{su} = 95 ksi)		
Sheet Material	Clad 2024-T3		
Fastener Diameter, in.	5/32	3/16	1/4
(Nominal Shank Diameter, in.)[b]	(0.164)	(0.190)	(0.250)
Sheet thickness, in.:	**Ultimate Strength, lbs.**		
0.050	807	...	...
0.063	1020	1180	...
0.071	1150	1335	...
0.080	1300	1505	1970
0.090	1465	1695	2220
0.100	1630	1885	2470
0.125	2007	2360	3095
0.160	...	2694	3975
0.190	...	...	4660
Fastener shear strength[c]	2007	2694	4660
Sheet thickness, in.:	**Yield Strength[d], lbs.**		
0.050	619	...	...
0.063	747	889	...
0.071	827	981	...
0.080	916	1085	1495
0.090	1015	1200	1645
0.100	1115	1315	1795
0.125	1360	1600	2175
0.160	...	2000	2705
0.190	...	...	3155

[a] Data supplied by Cherry Fasteners.
[b] Fasteners installed in clearance holes (0.005"-0.002") (Ref. Section 8.1.4).
[c] Fastener shear strength based on area computed from nominal shank diameters in Table 9.4.1.2(a) and F_{su} = 95 ksi.
[d] Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.4.2(a). *Static Joint Strength of 100° Flush Shear Head Alloy Steel Lockbolt Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	NAS1436-1442[a] (F_{su} = 95 ksi)			
Sheet and Plate Material	Clad 7075-T6 and T651			
Fastener Diameter, in. (Nominal Shank Diameter, in.)	3/16 (0.190)	1/4 (0.250)	5/16 (0.312)	3/8 (0.375)
	Ultimate Strength, lbs			
Sheet or plate thickness, in.:				
0.071	1684	...	...	...
0.080	1875	...	...	...
0.090	2077	...	...	...
0.100	2286	3075	...	...
0.125	2620	3750	4811	...
0.160	...	4625	5994[b]	7350
0.190	...	4650	6993	8554
0.250	...	...	7300	10435
0.312	...	...	...	10500
Fastener shear strength[c]	2620	4650	7300	10500
	Yield Strength[d], lbs			
Sheet or plate thickness, in.:				
0.071	1405	...	...	...
0.080	1598	...	...	...
0.090	1717	...	...	...
0.100	1850	2395	...	...
0.125	2232	2790	3327	...
0.160	...	3415	3851	5656
0.190	...	3765	4666	6342
0.250	...	...	5248	7910
0.312	...	...	...	8946
Head height (max.), in.	0.049	0.063	0.071	0.081

[a]Data supplied by Huck Manufacturing Company.
[b]Yield value is less than 2/3 of the indicated ultimate strength value.
[c]Fastener shear strength is documented in NAS1413.
[d]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.4.2(b). *Static Joint Strength of 100° Flush Shear/Tension Head Alloy Steel Lockbolt Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	NAS7024-7032[a,b] (F_{su} = 108 ksi)					
Sheet and Plate Material	Clad 7075-T6 and T651					
Fastener Diameter, in. (Nominal Shank Diameter, in.)	1/8 (0.125)	5/32 (0.156)	3/16 (0.190)	1/4 (0.250)	5/16 (0.312)	3/8 (0.375)
	Ultimate Strength, lbs					
Sheet or plate thickness, in.:						
0.040	563	...	...	...	...	...
0.050	846[d]	[c] 881	1071	...	...	...
0.063	1040[d]	1341[d]	1398	[c] ...	...	...
0.071	1147	1494[d]	1743[d]	2001	...	...
0.080	1231	1645[d]	2083[d]	2256	[c] ...	...
0.090	1289	1813	2288[d]	2823	3071	...
0.100	1325	1921	2493[d]	3390[d]	3425	[c] 4225
0.125	...	2070	2878	4140[d]	5200[d]	5500 [c]
0.160	...	...	3060	4930	6490	8080[d]
0.190	...	...	...	5280	7530	8725[d]
0.250	...	...	...	5300	7870	10010
0.312	...	...	...	...	8220	11270
0.324	...	...	...	...	8280	11340
0.375	...	...	...	...	...	11620
0.433	...	...	...	...	...	11930
Fastener shear strength[e]	1325	2070	3060	5300	8280	11930
	Yield Strength[f], lbs					
Sheet or plate thickness, in.:						
0.040	426	...	...	...	...	...
0.050	537	666	804	...	...	...
0.063	682	846	1024	...	...	...
0.071	770	957	1159	1508	...	...
0.080	870	1082	1311	1708	...	...
0.090	981	1221	1430	1931	2392	...
0.100	1092	1360	1649	2152	2669	3177
0.125	...	1705	2071	2709	3363	4010
0.160	...	...	2595	3486	4340	4975
0.190	...	...	...	4050	5170	5760
0.250	...	...	...	4140	6210	7340
0.312	...	...	...	...	7040	8730
0.324	...	...	...	...	7200	8810
0.375	...	...	...	...	...	9160
0.433	...	...	...	...	...	9560
Head height (ref.), in.	0.042	0.050	0.060	0.077	0.094	0.111

[a]Data supplied by Huck Manufacturing Company.
[b]Used with NAS1080K aluminum alloy collar.
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Yield value is less than 2/3 of indicated ultimate strength value.
[e]Fastener shear strength is documented in NAS1413.
[f]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.4.2(c). *Static Joint Strength of 100° Flush Shear Head Ti-6Al-4V Cherrybuck Fasteners in Machine-Countersunk Aluminum Alloy Sheet*

Fastener Type	CSR 924[a] (F_{su}=95 ksi)		
Sheet Material	Clad 7075-T6		
Nominal Diameter, in.	5/32	3/16	1/4
(Nominal Shank Diameter, in.)	(0.164)	(0.190)	(0.250)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.050	941	...	...
0.063	1207	1383	...
0.071	1385	1588	...
0.080	1557	1779	2281
0.090	1775	2050	2594
0.100	1876	2263	2919
0.125	1950	2542	3765
0.160	2007	2660	4387
0.190	...	2694	4525
0.250	...	...	4660
Fastener shear strength[b]	2007	2694	4660
	Yield Strength[c], lbs.		
Sheet thickness, in.:			
0.050	659	...	...
0.063	887	985	...
0.071	1022	1148	...
0.080	1116	1325	1625
0.090	1189	1480	1894
0.100	1257	1545	2162
0.125	1393	1733	2619
0.160	1608	1978	2950
0.190	...	2191	3231
0.250	...	...	3794
Head height (ref.), in.	0.034	0.046	0.060

[a] Data supplied by Cherry Fasteners.
[b] Fastener shear strength based on area computed from nominal shank diameter in Table 9.4.1.2(a) and F_{su} = 95 ksi.
[c] Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.4.2(d). *Static Joint Strength of 100° Flush Shear Head Ti-6Al-4V Cherrybuck Fasteners in Machine-Countersunk Aluminum Alloy Sheet*

Fastener Type	CSR 924[a] (F_{su}=95 ksi)		
Sheet Material	Clad 2024-T3		
Fastener Diameter, in. (Nominal Shank Diameter, in.)[b]	5/32 (0.164)	3/16 (0.190)	1/4 (0.250)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.050	737	...	...
0.063	1019	1118	...
0.071	1152	1319	...
0.080	1279[c]	1509	1837
0.090	1419[c]	1673[c]	2168
0.100	1560[c]	1834[c]	2500
0.125	1898[c]	2242[c]	3036[c]
0.160	2007[c]	2680[c]	3786[c]
0.190	...	2694	4404[c]
0.250	...	...	4660
Fastener shear strength[d]	2007	2694	4660
	Yield Strength[e], lbs.		
Sheet thickness, in.:			
0.050	511	...	...
0.063	712	778	...
0.071	786	922	...
0.080	840	1039	1276
0.090	900	1109	1513
0.100	960	1178	1750
0.125	1110	1352	1979
0.160	1321	1596	2300
0.190	...	1805	2575
0.250	...	...	3125
Head height (ref.), in.	0.034	0.046	0.060

[a] Data supplied by Cherry Fasteners.
[b] Fasteners installed in clearance holes (0.0005-0.002) (Ref. Section 8.1.4).
[c] Yield load is less than 2/3 of indicated ultimate.
[d] Fastener shear strength based on area computed from nominal shank diameter in Table 9.4.1.2(a) and F_{su} = 95 ksi.
[e] Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.4.2(e). *Static Joint Strength of 100° Flush Shear Head A-286 Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	HSR201 [a] (F_{su} = 95 ksi)		
Sheet Material	7075-T6		
Rivet Diameter, in.	5/32	3/16	1/4
(Nominal Shank Diameter, in.) [b]	(0.164)	(0.190)	(0.250)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.050	1055	1095	...
0.063	1330	1545	2030
0.071	1500	1740	2285
0.080	1690	1955	2575
0.090	1900	2200	2895
0.100	2007	2445	3220
0.125	...	2694	4025
0.160	...	...	4660
Rivet shear strength [c]	2007	2694	4660
	Yield Strength [d], lbs.		
Sheet thickness, in.:			
0.050	835	870	...
0.063	1055	1225	1605
0.071	1185	1380	1810
0.080	1340	1550	2040
0.090	1505	1745	2295
0.100	1675	1940	2550
0.125	...	2420	3190
0.160	...	...	4180
Head height (nom.), in.	0.040	0.046	0.060

[a] Data supplied by Hi-Shear Corporation.
[b] Hole Size: Fastener installed in 0.000 interference to 0.005 clearance (Ref. Section 8.1.4).
[c] Fastener shear strength based on areas computed from the nominal shank diameter in Table 9.4.1.2(a) and F_{su} = 95 ksi.
[d] Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.4.2(f). *Static Joint Strength of 100° Flush Shear Head Ti-8Mo-8V-2Fe-3Al Rivets in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	HSR101[a] (F_{su} = 95 ksi)		
Sheet Material	7075-T6		
Rivet Diameter, in.	5/32	3/16	1/4
(Nominal Shank Diameter, in.)[b]	(0.164)	(0.190)	(0.250)
	Ultimate Strength, lbs.		
Sheet thickness, in.:			
0.050	1040	1205	...
0.063	1310	1520	2000
0.071	1480	1715	2255
0.080	1665	1930	2540
0.090	1875	2170	2855
0.100	2007	2410	3175
0.125	...	2694	3965
0.160	...	...	4660
Rivet shear strength[c]	2007	2694	4660
	Yield Strength[d], lbs.		
Sheet thickness, in.:			
0.050	797	921	...
0.063	1005	1165	1530
0.071	1130	1310	1725
0.080	1275	1475	1945
0.090	1435	1660	2185
0.100	1595	1845	2430
0.125	...	2310	3035
0.160	...	...	3885
Head height (nom.), in.	0.040	0.046	0.060

[a]Data supplied by Hi-Shear Corporation.

[b]Hole Size: Fastener installed in 0.000 interference to 0.005 clearance (Ref. Section 8.1.4).

[c]Fastener shear strength based on areas computed from the nominal shank diameter in Table 9.4.1.2(a) and 1/4 = 0.250 and F_{su} = 95 ksi.

[d]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.4.2(g). *Static Joint Strength of 100° Flush Shear Head Ti-6Al-4V Lockbolt Fasteners in Machine-Countersunk Aluminum Alloy Sheet*

Rivet Type	GPL3SC-V Pin[a,b] (F_{su} = 95 ksi), 2SC-3C Collar			
Sheet Material	Clad 7075-T6			
Rivet Diameter, in.	3/16	1/4	5/16	3/8
(Nominal Shank Diameter, in.)[c]	(0.190)	(0.250)	(0.312)	(0.375)
	Ultimate Strength, lbs.			
Sheet thickness, in.:				
0.050	1105	...	...	...
0.063	1500	1800	[e] ...	...
0.071	1740	2125	2430	...
0.080	2020	2485	2865	3170 [e]
0.090	2200	2885	3365	3780
0.100	2355	3310	3865	4390
0.125	2694	3945	5135	5880
0.160	...	4660	6245	8005
0.190	...	...	7010	8955
0.250	...	...	7290	10490
Fastener shear strength[d]	2694	4660	7290	10490
	Yield Strength[f], lbs.			
Sheet thickness, in.:				
0.050	948	...	...	...
0.063	1160	1585	...	...
0.071	1290	1755	2265	...
0.080	1435	1945	2500	3090
0.090	1600	2160	2765	3415
0.100	1760	2375	3030	3740
0.125	2095	2910	3705	4535
0.160	...	3585	4640	5670
0.190	...	...	5440	6635
0.250	...	...	6270	8230
Head height (ref.), in.	0.048	0.063	0.070	0.081

[a]Data supplied by Huck Manufacturing Company and Voi-Shan Industries.

[b]Aluminum coated per NAS 4006.

[c]Hole size: Fasteners installed in 0.005" interference to 0.0005" clearance (Ref. Section 8.1.4).

[d]Fastener shear strength based on area computed from nominal shank diameter in Table 9.4.1.2(a) and F_{su} = 95 ksi.

[e]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.

[f]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.4.2(h). *Static Joint Strength of 100° Flush Shear Head Ti-6Al-4V Lockbolt Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Rivet Type	GPL3SC-V Pin[a,b] (F_{su} = 95 ksi), 2SC-3C Collar			
Sheet Material	Clad 2024-T3			
Rivet Diameter, in. (Nominal Shank Diameter, in.)[c]	3/16 (0.190)	1/4 (0.250)	5/16 (0.312)	3/8 (0.375)
	Ultimate Strength, lbs.			
Sheet thickness, in.:				
0.050	938	...	...	...
0.063	1255	1535	[f] ...	...
0.071	1455	1795	2085	...
0.080	1680	2085	2440	2740 [f]
0.090	1920[e]	2410	2845	3230
0.100	2080[e]	2735	3245	3725
0.125	2460[e]	3470[e]	4270	4930
0.160	2694	4175[e]	5505[e]	6645
0.190	...	4590[e]	6260[e]	7885[e]
0.250	...	4660	7230	9705[e]
0.312	...	...	7290	10490
0.375	...	...	...	...
Fastener shear strength[d]	2694	4660	7290	10490
	Yield Strength[g], lbs.			
Sheet thickness, in.:				
0.050	777	...	...	...
0.063	945	1285	...	...
0.071	1050	1435	1810	...
0.080	1140	1590	2030	2440
0.090	1230	1760	2260	2750
0.100	1320	1910	2475	3065
0.125	1545	2205	2975	3705
0.160	1860	2620	3495	4475
0.190	...	2975	3935	5010
0.250	...	3685	4820	6075
0.312	...	...	5740	7175
Head height (ref.), in.	0.048	0.063	0.070	0.081

[a]Data supplied by Huck Manufacturing Company and Voi-Shan Industries.

[b]Aluminum coated per NAS 4006.

[c]Hole size: fasteners installed in 0.005" interference to 0.0005" clearance (Ref. Section 8.1.4).

[d]Fastener shear strength based on area computed from nominal shank diameter in Table 9.4.1.2(a) and F_{su} = 95 ksi.

[e]Yield load is less than 2/3 of indicated ultimate.

[f]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.

[g]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.4.2(i). *Static Joint Strength of 100° Flush Shear Head Ti-6Al-4V Lockbolt Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Rivet Type	LGPL2SC-V Pin[a,b] (F_{su} = 95 ksi), 3SLC-C Collar			
Sheet Material	Clad 7075-T6			
Rivet Diameter, in. (Nominal Shank Diameter, in.)[c]	3/16 (0.190)	1/4 (0.250)	5/16 (0.312)	3/8 (0.375)
	Ultimate Strength, lbs.			
Sheet thickness, in.:				
0.050	1040	...	...	...
0.063	1370	1710	[e] ...	...
0.071	1575	1980	2345	...
0.080	1805	2280	2715	3105 [e]
0.090	2060	2615	3130	3620
0.100	2315	2950	3550	4130
0.125	2590	3790	4605	5375
0.160	2694	4430	6070	7150
0.190	...	4660	6750	8660
0.250	...	...	7290	10154
0.312	...	...	...	10490
Fastener shear strength[d]	2694	4660	7290	10490
	Yield Strength[f], lbs.			
Sheet thickness, in.:				
0.050	948	...	...	...
0.063	1160	1585	...	...
0.071	1290	1755	2265	...
0.080	1435	1945	2500	3090
0.090	1600	2160	2765	3415
0.100	1760	2375	3030	3740
0.125	2095	2910	3705	4535
0.160	2395	3585	4640	5670
0.190	...	3900	5440	6635
0.250	...	...	6270	8230
0.312	...	...	...	9255
Head height (ref.), in.	0.048	0.063	0.070	0.081

[a]Data supplied by Huck Manufacturing Company and Voi-Shan Industries.

[b]Aluminum coated per NAS 4006.

[c]Hole size: fasteners installed in 0.005" interference to 0.0005" clearance (Ref. Section 8.1.4).

[d]Fastener shear strength based on area computed from nominal shank diameter in Table 9.4.1.2(a) and F_{su} = 95 ksi.

[e]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.

[f]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.4.2(j). *Static Joint Strength of 100° Flush Shear Head Ti-6Al-4V Lockbolt Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Rivet Type	LGPL2SC-V Pin[a,b] (F_{su} = 95 ksi), 3SLC-C Collar			
Sheet Material	Clad 2024-T3			
Rivet Diameter, in.	3/16	1/4	5/16	3/8
(Nominal Shank Diameter, in.)[c]	(0.190)	(0.250)	(0.312)	(0.375)
	Ultimate Strength, lbs.			
Sheet thickness, in.:				
0.050	836	...	...	...
0.063	1180	1350	[f] ...	...
0.071	1395	1630	1775	...
0.080	1640	1950	2155	2270 [f]
0.090	1900[e]	2300	2595	2800
0.100	2115[e]	2650	3035	3335
0.125	2340	3530[e]	4140	4640
0.160	2655	4000	5645[e]	6500
0.190	2694	4355	6085	8080[e]
0.250	...	4660	6965	9180
0.312	...	...	7290	10270
0.375	...	...	...	10490
Fastener shear strength[d]	2694	4660	7290	10490
	Yield Strength[g], lbs.			
Sheet thickness, in.:				
0.050	733	...	...	...
0.063	901	1220	...	...
0.071	1005	1360	1745	...
0.080	1125	1515	1930	2270
0.090	1250	1685	2140	2635
0.100	1380	1855	2355	2895
0.125	1640	2280	2895	3530
0.160	1910	2795	3640	4430
0.190	2140	3100	4230	5200
0.250	...	3700	4985	6440
0.312	...	...	5760	7375
0.375	...	...	...	8325
Head height (ref.), in.	0.048	0.063	0.070	0.081

[a]Data supplied by Huck Manufacturing Company and Voi-Shan Industries.

[b]Aluminum coated per NAS 4006.

[c]Hole size: Fasteners installed in 0.0005" interference to 0.0005" clearance (Ref. Section 8.1.4).

[d]Fastener shear strength based on area computed from nominal shank diameter in Table 9.4.1.2(a) and F_{su} = 95 ksi.

[e]Yield load is less than 2/3 of indicated ultimate.

[f]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.

[g]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

8.1.5 THREADED FASTENERS.—The strengths shown in the following tables are applicable only when grip lengths and hole tolerances are as recommended by the respective fastener manufacturers. For some fastener systems, permanent set at yield load may be increased if hole sizes greater than those listed in the applicable table are used. This condition may exist even though the test hole size lies within the manufacturer's recommended hole size range (refer to Section 9.4.1.3.3).

The ultimate single shear strength of threaded fasteners at full diameter is shown in Table 8.1.5(a). The ultimate tensile strength of threaded fasteners is shown in Tables 8.1.5(b_1) and (b_2). In both tables values shown are a product of the indicated strength and area, with the area based on the following:

Shear.—Based on basic shank diameter.

Tension.—Based on the nominal minor diameter of the thread as published in Table 2.21 of Handbook H-28.

For any given threaded fastener the allowable load shall be chosen using an appropriate category corresponding to minimum tensile strength, shear strength, or other requirements of the pertinent procurement specification.

It is recognized that some procurement specifications may provide higher tensile strengths than those reported in Tables 8.1.5(b_1) and (b_2), since they may be based on a larger effective area than shown in the table. The values listed herein have been judged acceptable for design, acknowledging that they may be slightly conservative since they are based on the nominal minor diameter area.

Unless otherwise specified, the yield load is defined in Section 9.4.1.3.3 for threaded fasteners as the load at which the joint permanent is set equal to 0.04D, where D is the decimal equivalent of the fastener shank diameter as defined in Table 9.4.1.2(a).

8.1.5.1 *Protruding-Head Threaded Fastener Joints.*—It has been shown that protruding shear head (representative configuration is NAS1982) fastener joints may not develop the full bearing strength of the joint material. Therefore, static allowable loads for protruding shear head fasteners must be established from test data using the criteria specified in Section 9.4.1. For shear joints with protruding tension head fasteners, the load per fastener at which shear or bearing type of failure occurs is separately calculated, and the lower of the two values so determined governs the design. Allowable shear loads may be obtained from Table 8.1.5(a).

The design bearing stresses for various materials at room and other temperatures are given in the h properties for each alloy or group of alloys, and are applicable to joints with fasteners in cylindrical holes and where $t/D \geq 0.18$. Where $t/D < 0.18$, tests to substantiate yield and ultimate bearing strengths must be performed. These bearing stresses are applicable only for design of rigid joints where there is no possibility of relative motion of the parts joined without deformation of such parts.

For convenience, "unit" sheet bearing strengths for threaded fasteners, based on a strength of 100 ksi and nominal fastener diameters, are given in Table 8.1.5.1. The strength for a specific combination of fasteners, sheet thickness, and sheet material is obtained by multiplying the proper "unit" strength by the ratio of material allowable bearing stress (ksi) to 100.

The following interaction formula is applicable to AN3 series bolts under combined shear and tension loading: $R_s^3 + R_t^2 = 1.0$, where R_s and R_t are ratios of applied load to allowable load in shear and tension, respectively.

8.1.5.2 *Flush-head Threaded Fastener Joints.*—Tables 8.1.5.2(a) through (o) contain joint allowables for various flush-head threaded fastener/sheet material combinations. Unless otherwise noted, the allowable loads for flush-head threaded fasteners were established from test data using the following criteria:

Ultimate Load.—Average ultimate test load divided by a factor of 1.15, as defined in Chapter 9. This factor is not applicable to shear strength cutoff values which may be either procurement specification shear strength (S value) of the

fastener or, if no specification exists, a statistical value determined from test results. It should coincide with shear values from Table 8.1.5(a).

The allowables shown for flush-head threaded fasteners are applicable to joints having e/D equal to or greater than 2.0.

For machine countersunk joints, the sheet gage specified in the tables is that the countersunk sheet. When the noncountersunk sheet is thinner than the countersunk sheet, the bearing allowable for the noncountersunk sheet-fastener combination should be computed, compared to the table value, and the lower of the two values selected.

TABLE 8.1.5(a). *Ultimate Single Shear Strength of Threaded Steel Fasteners*

Shear strength of fastener, ksi			Ultimate single shear strength, lbs.[a]									
			35	38	75	91	95	108	125	132	156	180
Fastener diameter		Basic shank area										
In.	b											
0.112	# 4	0.0098520	345	374	739	897	936	1 064	1 232	1 300	1 537	1 773
0.125	1/8	0.012272	430	466	920	1 117	1 166	1 325	1 534	1 620	1 914	2 209
0.138	# 6	0.014957	523	568	1 122	1 361	1 421	1 615	1 870	1 974	2 333	2 692
0.156	5/32	0.019175	671	729	1 438	1 745	1 822	2 071	2 397	2 531	2 991	3 452
0.164	# 8	0.021124	739	803	1 584	1 922	2 007	2 281	2 640	2 788	3 295	3 802
0.188	3/16	0.027612	966	1 049	2 071	2 513	2 623	2 982	3 452	3 645	4 310	4 970
0.190	#10	0.028353	992	1 077	2 126	2 580	2 694	3 062	3 544	3 743	4 420	5 100
0.216	#12	0.036644	1 283	1 392	2 748	3 335	3 481	3 958	4 580	4 840	5 720	6 600
0.219	7/32	0.037582	1 315	1 428	2 819	3 420	3 570	4 060	4 700	4 960	5 860	6 760
0.250	1/4	0.049087	1 718	1 865	3 682	4 470	4 660	5 300	6 140	6 480	7 660	8 840
0.312	5/16	0.076699	2 684	2 915	5 750	6 980	7 290	8 280	9 590	10 120	11 970	13 810
0.375	3/8	0.11045	3 866	4 200	8 280	10 050	10 490	11 930	13 810	14 580	17 230	19 880
0.438	7/16	0.15033	5 260	5 710	11 270	13 680	14 280	16 240	18 790	19 840	23 450	27 060
0.500	1/2	0.19635	6 870	7 460	14 730	17 870	18 650	21 210	24 540	25 920	30 630	35 340
0.562	9/16	0.24850	8 700	9 440	18 640	22 610	23 610	26 840	31 060	32 800	38 770	44 700
0.625	5/8	0.30680	10 740	11 660	23 010	27 920	29 150	33 130	38 350	40 500	47 900	55 200
0.750	3/4	0.44179	15 460	16 790	33 130	40 200	42 000	47 700	55 200	58 300	68 900	79 500
0.875	7/8	0.60132	21 050	22 850	45 100	54 700	57 100	64 900	75 200	79 400	93 800	108 200
1.000	1	0.78540	27 490	29 850	58 900	71 500	74 600	84 800	98 200	103 700	122 500	141 400
1.125	1-1/8	0.99402	34 790	37 770	74 600	90 500	94 400	107 400	124 300	131 200	155 100	178 900
1.250	1-1/4	1.2272	43 000	46 600	92 000	111 700	116 600	132 500	153 400	162 000	191 400	220 900
1.375	1-3/8	1.4849	52 000	56 400	111 400	135 100	141 100	160 400	185 600	196 000	231 600	267 300
1.500	1-1/2	1.7671	61 800	67 100	132 500	160 800	167 900	190 800	220 900	233 300	275 700	318 100

[a]Values with the first digit <4 are shown to 4 significant figures, all other are shown to 3 significant figures.

[b]Fractional equivalent or screw number.

TABLE 8.1.5(b_1). *Ultimate Tensile Strength of Threaded Steel Fasteners*

Tensile strength of fastener, ksi			Ultimate tensile strength, lbs. [a,b,c]						
			55	62	62.5	125	140	160	180
Fastener diameter		Nominal minor area[e]	MIL-S-7742						
In.	d								
0.112	4-40	0.0050896	280	316	318	636	713	814	916
0.138	6-32	0.0076821	423	476	480	960	1 075	1 229	1 383
0.164	8-32	0.012233	673	758	765	1 529	1 713	1 957	2 202
0.190	10-32	0.018074	994	1,121	1 130	2 259	2 530	2 892	3 253
0.250	1/4-28	0.033394	1 837	2 070	2 087	4 170	4 680	5 340	6 010
0.312	5/16-24	0.053666	2 952	3 327	3 354	6 710	7 510	8 590	9 660
0.375	3/8-24	0.082397	4 530	5 110	5 150	10 300	11 540	13 180	14 830
0.438	7/16-20	0.11115	6 110	6 890	6 950	13 890	15 560	17 780	20 010
0.500	1/2-20	0.15116	8 310	9 370	9 450	18 900	21 160	24 190	27 210
0.562	9/16-18	0.19190	10 550	11 900	11 990	23 990	26 870	30 700	34 540
0.625	5/8-18	0.24349	13 390	15 100	15 220	30 440	34 090	38 960	43 800
0.750	3/4-16	0.35605	19 580	22 080	22 250	44 500	49 800	57 000	64 100
0.875	7/8-14	0.48695	26 780	30 190	30 430	60 900	68 200	77 900	87 700
1.000	1-12	0.63307	34 820	39 250	39 570	79 100	88 600	101 300	114 000
1.125	1-1/8-12	0.82162	45 200	50 900	51 400	102 700	115 000	131 500	147 900
1.250	1-1/4-12	1.0347	56 900	64 200	64 700	129 300	144 900	165 600	186 200
1.375	1-3/8-12	1.2724	70 000	78 900	79 500	159 000	178 100	203 600	229 000
1.500	1-1/2-12	1.5345	84 400	95 100	95 900	191 800	214 800	245 500	276 200

[a]Values shown above heavy line are for 2A threads; all other values are for 3A threads.

[b]Nuts designed to develop the ultimate tensile strength of the fastener are required to develop the tabulated tension loads.

[c]Values with the first digit <4 are shown to 4 significant figures; all others are shown to 3 significant figures.

[d]Fractional equivalent or number and threads per inch.

[e]Area computed using nominal minor diameter as published in Table 2.2.1 of Handbook H-28.

TABLE 8.1.5(b_2). *Ultimate Tensile Strength of Threaded Steel Fasteners (Continued)*

Tensile strength of fastener, ksi			Ultimate tensile strength, lbs [a,b,c]				
			160	180	220	260	300
Fastener diameter		Maximum minor area[e]	MIL-S-8879				
In.	d						
0.112	4-40	0.0054367	869	979	1,196	1,414	1,631
0.138	6-32	0.0081553	1,305	1,468	1,794	2,120	2,447
0.164	8-32	0.012848	2,055	2,313	2,827	3,340	3,854
0.190	10-32	0.018602	2,976	3,348	4,090	4,840	5,580
0.250	1/4-28	0.034241	5,480	6,160	7,530	8,900	10,270
0.312	5/16-24	0.054905	8,780	9,880	12,080	14,280	16,470
0.375	3/8-24	0.083879	13,420	15,100	18,450	21,810	25,160
0.438	7/16-20	0.11323	18,120	20,380	24,910	29,440	33,970
0.500	1/2-20	0.15358	24,570	27,640	33,790	39,930	46,100
0.562	9/16-18	0.19502	31,200	35,100	42,900	50,700	58,500
0.625	5/8-18	0.24700	39,520	44,500	54,300	64,200	74,100
0.750	3/4-16	0.36082	57,700	64,900	79,400	93,800	108,200
0.875	7/8-14	0.49327	78,900	88,800	108,500	128,300	148,000
1.000	1-12	0.64156	102,600	115,500	141,100	166,800	192,500
1.125	1-1/8-12	0.83129	133,000	149,600	182,900	216,100	249,400
1.250	1-1/4-12	1.0456	167,300	188,200	230,000	271,900	313,700
1.375	1-3/8-12	1.2844	205,500	231,200	282,600	333,900	385,300
1.500	1-1/2-12	1.5477	247,600	278,600	340,500	402,400	464,300

[a]All values are for 3A threads.

[b]Nuts designed to develop the ultimate tensile strength of the fastener are required to develop the tabulated tension loads.

[c]Values with the first digit <4 are shown to 4 significant figures; all others are shown to 3 significant figures.

[d]Fractional equivalent or number and threads per inch.

[e]Area computed using maximum minor diameter as published in Tables II and III of MIL-S-8879.

TABLE 8.1.5.1. *Unit Bearing Strength of Sheet and Plate in Joints With Threaded Fasteners or Pins;* F_{br}=100 ksi

Fastener, Diameter,in.	Unit bearing strength of sheet for fastener diameter indicated, lbs.[a]													
	0.156	0.164	0.188	0.190	0.250	0.312	0.375	0.438	0.500	0.562	0.625	0.750	0.875	1.000
Thickness, in.														
0.032	500	525	...	...	...	...	...	...	...	...	...	...	...	...
0.036	563	590	675	684	...	...	...	...	...	...	...	...	...	...
0.040	625	656	750	760	...	...	...	...	...	...	...	...	...	...
0.045	704	738	845	855	...	...	...	...	...	...	...	...	...	...
0.050	781	820	940	950	1 250	...	...	...	...	...	...	...	...	...
0.063	985	1 033	1 180	1 197	1 575	1 969	...	...	...	...	...	...	...	...
0.071	1 110	1 164	1 330	1 349	1 775	2 219	2 662	...	...	...	...	...	...	...
0.080	1 250	1 312	1 500	1 520	2 000	2 500	3 000	3 500	...	...	...	...	...	...
0.090	1 407	1 476	1 690	1 710	2 250	2 812	3 375	3 938	4 500	...	...	...	...	...
0.100	1 562	1 640	1 875	1 900	2 500	3 125	3 750	4 375	5 000	...	...	...	...	...
0.125	1 953	2 050	2 340	2 375	3 125	3 906	4 688	5 469	6 250	7 030	7 812	...	...	...
0.160	2 500	2 624	3 000	3 040	4 000	5 000	6 000	7 000	8 000	9 000	10 000	12 000	...	...
0.200	3 125	3 280	3 750	3 800	5 000	6 250	7 500	8 750	10 000	11 250	12 500	15 000	17 500	20 000
0.250	3 916	4 100	4 688	4 750	6 250	7 812	9 375	10 940	12 500	14 060	15 625	18 750	21 875	25 000
0.312	4 867	5 117	5 866	5 928	7 800	9 734	11 700	13 670	15 600	17 530	19 500	23 400	27 300	31 200
0.375	5 850	6 150	7 050	7 125	9 375	11 700	14 063	16 425	18 750	21 075	23 400	28 125	32 810	37 500
0.500	7 800	8 200	9 400	9 500	12 500	15 600	18 750	21 900	25 000	28 100	31 250	37 500	43 750	50 000
0.625	9 750	10 250	11 750	11 875	15 625	19 500	23 440	27 375	31 250	35 125	39 062	46 875	54 690	62 500
0.750	11 700	12 300	14 100	14 250	18 750	23 400	28 125	32 850	37 500	42 150	46 875	56 250	65 625	75 000
0.875	13 650	14 350	16 450	16 625	21 875	27 300	32 810	38 325	43 750	49 175	56 690	65 625	76 560	87 500
1.000	15 600	16 400	18 800	19 000	25 000	31 200	37 600	43 800	50 000	56 200	62 500	75 000	87 500	100 000

[a]Bearing strengths shown are based on nominal fastener diameter.

TABLE 8.1.5.2(a_1). *Static Joint Strength of 100° Flush Head Alloy Steel Screws in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	AN509[b] steel screw (F_{su} = 75 ksi) w/MS20365 or equiv. steel nut				
Sheet and Plate Material	Clad 2024-T3 and T351				
Fastener Diameter, in. (Nominal Shank Diameter, in.)	3/16 (0.190)	1/4 (0.250)	5/16 (0.312)	3/8 (0.375)	1/2 (0.500)
	Ultimate Strength[a], lbs				
Sheet or plate thickness, in.:					
0.080	1576[c]	...	...	...	...
0.090	1726[c]	...	...	...	...
0.100	1877[c]	2567[c]	...	...	...
0.125	2126[c]	3054[c]	3922[c]	4579[c]	...
0.160	...	3536[c]	4722[c]	5878[c]	...
0.190	...	3682	5405[c]	6872[c]	9408[c]
0.250	...	...	5750	8280[c]	12201[c]
0.312	...	...	...	8280[c]	14141[c]
0.375	...	...	...	...	14730
Fastener shear strength[e]	2126	3682	5750	8280	14730
	Yield Strength[a,f], lbs				
Sheet or plate thickness, in.:					
0.080	903	...	...	...	...
0.090	989	...	...	...	...
0.100	1084	1490	...	...	...
0.125	1296	1748	2001	2559	...
0.160	1615	2116	2334	2939	...
0.190	...	2484	2702	3361	6012
0.250	...	...	3404	4197	7306
0.312	...	...	...	5092	8452
0.375	...	...	...	...	9996
Head height (ref.), in.	0.080	0.106	0.133	0.159	0.213

[a]Test data from which the yield and ultimate strengths were derived can be found in Reference 8.1.5.2.
[b]This fastener is no longer manufactured; do not specify for new designs.
[c]Yield value is less than 2/3 of the indicated ultimate strength value.
[d]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[e]Fastener shear strength based on area computed from nominal shank diameters in Table 9.4.1.2(a) and F_{su} = 75 ksi.
[f]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.5.2(a_2). *Static Joint Strength of 100° Flush Head Alloy Steel Screws in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	AN509[b] steel screw (F_{su} = 75 ksi) w/MS20365 or equiv. steel nut				
Sheet and Plate Material	Clad 7075-T6 and T651				
Fastener Diameter, in. (Nominal Shank Diameter, in.)	3/16 (0.190)	1/4 (0.250)	5/16 (0.312)	3/8 (0.375)	1/2 (0.500)
	Ultimate Strength[a], lbs				
Sheet or plate thickness, in.:					
0.080	1632[c]	...	...	...	...
0.090	1762[c] [d]	...	...	...	...
0.100	1892	2723[c]	...	...	...
0.125	2126	3109[c] [d]	4180[c]	5216[c]	...
0.160	...	3551[c]	4858[c]	6193[c] [d]	...
0.190	...	3682	5433[c]	6996[c]	...
0.250	...	...	5750	8280[c]	12421[c]
0.312	...	...	...	8280	14185[c] [d]
0.375	...	...	...	...	14730
Fastener shear strength[e]	2126	3682	5750	8280	14730
	Yield Strength[a,f], lbs				
Sheet or plate thickness, in.:					
0.080	965	...	...	...	...
0.090	1063	...	...	...	...
0.100	1179	1600	...	...	...
0.125	1462	1895	2098	2699	...
0.160		2363	2501	3088	...
0.190	...	2926	3018	3601	...
0.250	...	...	4312	4868	8041
0.312	...	...	...	6624	9437
0.375	...	...	...	...	11686
Head height (ref.), in.	0.080	0.106	0.133	0.159	0.213

[a]Test data from which the yield and ultimate strengths were derived can be found in Reference 8.1.5.2.
[b]This fastener is no longer manufactured; do not specify for new designs.
[c]Yield value is less than 2/3 of the indicated ultimate strength value.
[d]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[e]Fastener shear strength based on area computed from nominal shank diameters in Table 9.4.1.2(a) and F_{su} = 75 ksi.
[f]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.5.2(b). *Static Joint Strength of 100° Flush Head Stainless Steel (PH13-8Mo-H1000) Fasteners in Machine-Countersunk Titanium Alloy Sheet and Plate*

Fastener Type	PBF 11[a] (F_{su} = 125 ksi)			
Sheet and Plate Material	Annealed Ti-6Al-4V			
Rivet Diameter, in. (Nominal Shank Diameter, in.)[b]	5/32 (0.164)	1/4 (0.250)	3/8 (0.375)	1/2 (0.500)
	Ultimate Strength, lbs			
Sheet or plate thickness, in.:				
0.040	1535	...	...	...
0.050	1963	...	...	...
0.063	2528	3656	...	...
0.071	2640	4213	...	...
0.080	...	4813	6820	...
0.090	...	5438	7818	...
0.100	...	6140	8775	11250
0.125	...	...	11264	14575
0.160	...	...	13810	19250
0.190	...	...	...	23200
0.200	...	...	...	24540
Fastener shear strength[d]	2640	6140	13810	24540
	Yield Strength[e], lbs			
Sheet or plate thickness, in.:				
0.040	1237	...	...	...
0.050	1543	...	...	...
0.063	1947	2969	...	...
0.071	2049	3350	...	...
0.080	...	3756	5667	...
0.090	...	4219	6370	...
0.100	...	4600	7101	9500
0.125	...	...	8789	11825
0.160	...	...	10645	15025
0.190	...	...	...	17825
0.200	...	...	...	18400
Head height (nom.), in.	0.040	0.060	0.077	0.101

[c] Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable.

[a]Data supplied by Huck Manufacturing Company and PB Fasteners.
[b]Fasteners installed in clearance holes (0.0025-0.0030) (Ref. Section 8.1.5).
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Fastener shear strength based on areas computed from indicated nominal shank diameter F_{su} = 125 ksi.
[e]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.5.2(c). *Static Joint Strength of 100° Flush Head Tapered Alloy Steel Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	TL 100[a] (F_{su} = 108 ksi)					
Sheet and Plate Material	Clad 7075-T6 and T651					
Fastener Diameter, in. (Nominal Shank Diameter, in.)	3/16 (0.1969)	1/4 (0.2585)	5/16 (0.3214)	3/8 (0.3860)	7/16 (0.4490)	1/2 (0.5122)
	Ultimate Strength, lbs					
Sheet or plate thickness, in.:						
0.100	2435	...	...	...	...	...
0.125	2913	3745	4443	...	...	...
0.160	3290	4831	6017	7016	7993	...
0.190	...	5269	7017	8511	9737	10900
0.250	...	5670	8148	11120	13220	14890
0.285	...	...	8760	11360	15000	17240
0.312	...	...	...	11570	15280	19000
0.344	...	...	...	11800	15560	19800
0.375	...	...	...	12030	15820	20110
0.500	...	...	...	12640	16870	21320
Fastener shear strength[b]	3290	5670	8760	12640	17100	22250
	Yield Strength[c], lbs					
Sheet or plate thickness, in.:						
0.100	1960	...	...	...	...	...
0.125	2350	2990	3818	...	...	...
0.160	2840	3550	4650	5650	6703	...
0.190	...	3970	5308	6596	7806	9045
0.250	...	4830	6450	8209	9903	11560
0.285	...	...	7060	9090	10930	12840
0.312	...	...	...	9680	11780	13930
0.344	...	...	...	10010	12710	14930
0.375	...	...	...	10430	13200	16000
0.500	...	...	...	...	15160	18490
Head height (max.), in.	0.048	0.063	0.070	0.081	0.100	0.110

[a]Data supplied by Briles Manufacturing Company.
[b]Fastener shear strength based on areas computed from indicated nominal shank diameter and F_{su} = 108 ksi.
[c]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.5.2(d). *Static Joint Strength of 100° Flush Head Tapered STA Ti-6Al-4V Fasteners in Machine-Countersunk Aluminum Alloy Sheet*

Fastener Type	TLV 10[a] (F_{su} = 95 ksi)			
Sheet Material	Clad 7075-T6			
Fastener Diameter, in. (Nominal Shank Diameter, in.)	1/8 (0.1437)	5/32 (0.1688)	3/16 (0.1965)	1/4 (0.2583)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.032	488	...	...	...
0.040	610	[b] 713	826	...
0.050	768	896	1050	[b] ...
0.063	967	1145	1312	1730
0.071	1120	1290	1491	1960 [b]
0.080	1260	1470	1690	2223
0.090	1377	1670	1910	2505
0.100	1441	1845	2130	2800
0.125	1530	2010	2580	3540
0.160	1540	2125	2800	4410
0.190	...	...	2880	4750
0.250	...	...	...	4980
Fastener shear strength[c]	1540	2125	2880	4980
	Yield Strength[d], lbs			
Sheet thickness, in.:				
0.032	488	...	...	...
0.040	610	713	826	...
0.050	753	890	1050	...
0.063	925	1118	1301	1730
0.071	1035	1240	1467	1960
0.080	1138	1377	1637	2192
0.090	1238	1522	1806	2455
0.100	1321	1639	1976	2711
0.125	1480	1880	2331	3304
0.160	1540	2111	2683	3986
0.190	...	...	2880	4437
0.250	...	...	...	4980
Head height (max.), in.	0.033	0.041	0.048	0.063

[a]Data supplied by Lockheed Georgia Company.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Fastener shear strength based on areas computed from indicated nominal shank diameter F_{su} = 95 ksi.
[d]Permanent set at yield load: the greater of 0.012 inch or 4% of fractional diameter.

TABLE 8.1.5.2(e). *Static Joint Strength of 70° Flush Head Tapered Ti-6Al-4V Fasteners in Non-Matching Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	HPB-V[a] (F_{su} = 95 ksi)			
Sheet and Plate Material	Clad 7075-T6 and T651			
Fastener Diameter (Nominal Shank Diameter, in.)[b]	3/16 (0.1976)	1/4 (0.2587)	5/16 (0.3211)	3/8 (0.3850)
Sheet Countersink Angle	82°	82°	82°	75°
	Ultimate Strength, lbs			
Sheet or plate thickness, in.:				
0.063	1355	...	...	...
0.071	1554	2041	...	...
0.080	1710	2296	...	...
0.090	1847	2583	3207	...
0.100	1984	2864	3567	4269
0.125	2319	3293	4454	5336
0.160	2792	3908	5176	6611
0.190	2913	4444	5836	7396
0.250	...	4993	7155	8968
0.312	...	...	7692	10613
0.375	...	...	...	11058
0.500	...	...	...	11058
Fastener shear strength[c]	2913	4993	7692	11058
	Yield Strength[d], lbs			
Sheet or plate thickness, in.:				
0.063	1269	...	...	...
0.071	1429	1874	...	...
0.080	1613	2108	...	...
0.090	1812	2376	2949	...
0.100	1995	2637	3279	3928
0.125	2366	3299	4093	4906
0.160	2718	3975	5217	6285
0.190	2913	4397	5949	7441
0.250	...	4993	6980	9042
0.312	...	...	7692	10257
0.375	...	...	...	11058
0.500	...	...	...	11058
Head height (max.), in.	0.057	0.067	0.076	0.086

[a]Data supplied by PB Fasteners.
[b]Fasteners installed in interference holes (0.0015-0.0048) (Ref. Section 8.1.5).
[c]Fastener shear strength based on areas computed from the indicated nominal shank diameter and F_{su} = 95 ksi.
[d]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.5.2(f). *Static Joint Strength of 100° Flush Shear Head Ti-6Al-4V Fasteners in Machine-Countersunk Aluminum Alloy Sheet*

Fastener Type	KLBHV Pin (F_{su} = 95 ksi), KFN 600 Nut[a]				
Sheet Material	Clad 7075-T6				
Fastener Diameter, in. (Nominal Shank Diameter, in.)[b]	5/32 (0.164)	3/16 (0.190)	1/4 (0.250)	5/16 (0.3125)	3/8 (0.375)
	Ultimate Strength, lbs				
Sheet thickness, in.:					
0.040	748	...	...	...	...
0.050	987	[c] 1112	...	...	...
0.063	1291	1462	1813	...	...
0.071	1428	1679	2100	[c] ...	...
0.080	1571	1888	2438	2902	...
0.090	1722	2058	2794	3322	3867
0.100	1883	2231	3150	3810	4402
0.125	2007	2694	3725	4924	5724
0.160	...	...	4531	4901	7397
0.190	...	...	4660	6790	8452
0.200	...	...	...	7083	8789
0.250	...	...	...	7290	10490
Fastener shear strength[d]	2007	2694	4660	7290	10490
	Yield Strength[e], lbs				
Sheet thickness, in.:					
0.040	594	...	...	...	...
0.050	740	859	...	...	...
0.063	931	1079	1419	...	...
0.071	1049	1213	1600	...	...
0.080	1176	1368	1806	2267	...
0.090	1283	1534	2031	2540	3052
0.100	1375	1675	2250	2824	3375
0.125	1606	1942	2813	3517	4219
0.160	...	...	3306	4455	5386
0.190	...	...	3725	4983	6385
0.200	...	...	...	5168	6581
0.250	...	...	...	6038	7636
Head height (ref.), in.	0.043	0.048	0.063	0.070	0.081

[a]Data supplied by Kaynar Manufacturing Co., Inc.
[b]Fasteners installed in interference holes (0.003-0.055) (Ref. 8.1.5).
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Fastener shear strength based on areas computed from indicated nominal shank diameter and F_{su} = 95 ksi.
[e]Permanent set at yield load: 4% of the nominal diameter (Ref. 9.4.1.3.3).

TABLE 8.1.5.2(g). *Static Joint Strength of 100° Flush Shear AISI 431[a] Hi-Lok Fasteners in Aluminum Alloy Sheet and Plate*

Rivet Type	HL 61 Pin (F_{su} = 125 ksi), HL 70 Collar[b]			
Sheet and Plate Material	Clad 7075-T6 and T651			
Rivet Diameter (Nominal Shank Diameter, in.)	3/16 (0.190)	1/4 (0.250)	5/16 (0.312)	3/8 (0.375)
	Ultimate Strength, lbs			
Sheet or plate thickness, in.:				
0.090	2327	...	...	...
0.100	2430	3740	...	...
0.125	2695	4080	...	...
0.160	3070	4560	6500[c]	...
0.190	3390	4970	7160	9100
0.250	3544	5800	8320	10230
0.312	...	6140	9590	11390
0.375	...	...	...	12580
0.500	...	...	...	13810
Fastener shear strength[d]	3544	6140	9590	13810
	Yield Strength[e], lbs			
Sheet or plate thickness, in.:				
0.090	1840	...	...	...
0.100	1943	2900	...	...
0.125	2195	3240	...	...
0.160	2540	3700	4030	...
0.190	2840	4020	5430	7120
0.250	3110	4870	6590	8500
0.312	...	5350	7580	9700
0.375	...	...	7890	10410
0.500	...	...	...	12070
Head height (max.), in.	0.049	0.063	0.077	0.051

[a]AISI 431 is prohibited from use in Air Force and Navy structure by MIL-STD-1568 and SD-24, respectively, because of its sensitivity to heat treatment. Use of fasteners made of this material in design of military aerospace structures requires the specific approval of the procuring activity.
[b]Data supplied by Hi-Shear Corporation.
[c]Yield value is less than 2/3 of the indicated ultimate strength value.
[d]Fastener shear strength based on areas computed from the indicated nominal shank diameter and F_{su} = 125 ksi.
[e]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.5.2(h). *Static Joint Strength of 100° Flush Shear Head Alloy Steel Hi-Lok Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	HL 719 Pin (F_{su} = 108 ksi), HL 79 Collar[a]				
Sheet and Plate Material	7075-T6 and T651				
Fastener Diameter, in. (Nominal Shank Diameter, in.)[b]	5/32 (0.164)	3/16 (0.190)	1/4 (0.250)	5/16 (0.312)	3/8 (0.375)
	Ultimate Strength, lbs				
Sheet or plate thickness, in.:					
0.040	734	...	...	...	...
0.050	1044	[c] 1131	...	...	...
0.063	1384	1565	1813	...	...
0.071	1518	1820	2216	...	...
0.080	1668	1998	2594	2916	...
0.090	1764	2193	3015	3532	3724
0.100	1825	2345	3338	4059	4516
0.125	1979	2524	3980	5229	6167
0.160	2195	2774	4350	6347	7928
0.190	...	2989	4634	6702	9087
0.250	...	3062	5200	7512	9985
0.312	...	...	5300	8146	10870
0.375	...	...	...	8280	11760
Fastener shear strength[d]	2281	3062	5300	8280	11930
	Yield Strength[e], lbs				
Sheet or plate thickness, in.:					
0.040	690	...	...	...	...
0.050	861	1000	...	...	...
0.063	1086	1261	1664	...	...
0.071	1224	1421	1876	...	...
0.080	1346	1601	2114	2647	...
0.090	1478	1771	2378	2978	3578
0.100	1610	1924	2642	3309	3976
0.125	1845	2308	3210	4136	4970
0.160	2022	2583	3920	5124	6362
0.190	...	2750	4344	5886	7330
0.250	...	3062	4785	6925	9160
0.312	...	...	...	7496	10130
0.375	...	...	...	8158	10820
Head height (nom.), in.	0.040	0.046	0.060	0.067	0.077

[a]Data supplied by Hi-Shear Corporation.
[b]Fasteners installed in interference holes (0.001-0.002) (Ref. Section 8.1.5).
[c]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[d]Fastener shear strength based on areas computed from indicated nominal shank diameter and F_{su} = 108 ksi.
[e]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.5.2(i). *Static Joint Strength of 100° Flush Shear Head Ti-6Al-4V Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	HL 11 Pin (F_{su} = 95 ksi), HL 70 Collar[a]			
Sheet and Plate Material	Clad 7075-T6 and T651			
Fastener Diameter, in. (Nominal Shank Diameter, in.)	5/32 (0.164)	3/16 (0.190)	1/4 (0.250)	5/16 (0.312)
	Ultimate Strength, lbs			
Sheet or plate thickness, in.:				
0.040	734	837	...	...
0.050	941	1083	[b] 1343	...
0.063	1207	1393	1762	[b] 2170
0.071	1385	1588	2012	2463 [b]
0.080	1557	1779	2281	2823
0.090	1775	2050	2594	3193
0.100	1876	2263	2919	3631
0.125	1950	2542	3765	4594
0.160	2007	2660	3970	5890
0.190	...	2694	4165	6105
0.250	...	...	4530	6580
0.312	...	...	4660	7050
0.375	...	...	...	7290
Fastener shear strength[c]	2007	2694	4660	7290
	Yield Strength[d], lbs			
Sheet or plate thickness, in.:				
0.040	674	794	...	...
0.050	835	982	1325	...
0.063	1038	1230	1655	2141
0.071	1130	1355	1813	2338
0.080	1230	1480	2062	2620
0.090	1342	1625	2250	2880
0.100	1440	1750	2470	3420
0.125	1670	2020	2930	3860
0.160	1891	2360	3480	4620
0.190	...	2560	3840	5150
0.250	...	...	4440	6170
0.312	...	...	4660	6900
0.375	...	...	...	7290
Head height (nom.), in.	0.040	0.046	0.060	0.067

[a]Data supplied by Hi-Shear Corporation.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Fastener shear strength based on areas computed from indicated nominal shank diameter F_{su} = 95 ksi.
[d]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.5.2(j). *Static Joint Strength of 100° Flush Shear Head Ti-6Al-6V-2Sn Fasteners in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	HL 911 Pin (F_{su} = 108 ksi), HL 70 Collar[a]				
Sheet and Plate Material	Clad 7075-T6 and T651				
Fastener Diameter, in. (Nominal Shank Diameter, in.)	5/32 (0.164)	3/16 (0.190)	1/4 (0.250)	5/16 (0.312)	3/8 (0.375)
	Ultimate Strength, lbs				
Sheet or plate thickness, in.:					
0.040	780	...	...	...	...
0.050	982	[b] 1137	1456	...	...
0.063	1264	1458	1863	[b] 2287	...
0.071	1426	1642	2094	2570	[b] 3096
0.080	1622	1866	2425	2920	3473 [b]
0.090	1740	2105	2750	3339	3965
0.100	1794	2310	3063	3777	4415
0.125	1915	2455	3875	4770	5666
0.160	2098	2660	4219	6181	7339
0.190	2252	2840	4450	6483	8788
0.250	2281	3062	4925	7067	9589
0.312	...	...	5300	7670	10362
0.375	...	...	...	8280	11079
0.500	...	...	...	...	11930
Fastener shear strength[c]	2281	3062	5300	8280	11930
	Yield Strength[d], lbs				
Sheet or plate thickness, in.:					
0.040	734	...	...	...	...
0.050	882	1044	1394	...	...
0.063	1076	1300	1750	2190	...
0.071	1184	1406	1938	2472	2995
0.080	1320	1540	2188	2774	3332
0.090	1392	1680	2375	3066	3768
0.100	1480	1810	2569	3358	4120
0.125	1700	2085	3031	4010	5019
0.160	1870	2380	3563	4818	6074
0.190	1978	2530	3937	5354	6749
0.250	2178	2740	4375	6269	8183
0.312	...	...	4687	6883	9209
0.375	...	...	...	7418	9870
0.500	...	...	...	...	11039
Head height (nom.), in.	0.040	0.046	0.060	0.067	0.077

[a]Data supplied by Hi-Shear Corporation.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Fastener shear strength based on areas computed from indicated nominal shank diameter and F_{su} = 108 ksi.
[d]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.5.2(k). *Static Joint Strength of 100° Flush Head Ti-6Al-6V-2Sn or Alloy Steel, Shear Type Fasteners in Machine-Countersunk Aluminum Alloy Sheet*

Fastener Type	NAS4452S and KS 100-FV Pins[a] (F_{su} = 108 ksi), NAS4445DD Nut			
Sheet Material	7075-T6			
Fastener Diameter, in. (Nominal Shank Diameter, in.)	1/8 (0.138)	5/32 (0.164)	3/16 (0.190)	1/4 (0.250)
	Ultimate Strength, lbs			
Sheet thickness, in.:				
0.040	644	...	...	...
0.050	857	976	1065	...
0.063	1131	1305	1458	1750
0.071	1268	1512	1697	2062[b]
0.080	1428	1703	1964	2406
0.090	1499	1910	2227	2794
0.100	1539	2084	2458	3181
0.125	1615	2200	2848	4063
0.160	...	2281	3036	4900
0.190	...	...	3062	5113
0.250	...	...	...	5300
Fastener shear strength[c]	1615	2281	3062	5300
	Yield Strength[d], lbs			
Sheet thickness, in.:				
0.040	609	...	...	...
0.050	766	906	1029	...
0.063	946	1157	1325	1706
0.071	1044	1278	1505	1956
0.080	1152	1412	1668	2219
0.090	1261	1555	1848	2500
0.100	1320	1694	2014	2762
0.125	1444	1904	2397	3350
0.160	...	2106	2661	4100
0.190	...	...	2845	4419
0.250	...	...	...	4925
Head height (max.), in.	0.037	0.040	0.049	0.063

[a]Data supplied by Huck Manufacturing Company.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Fastener shear strength is documented in NAS4444.
[d]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.5.2(l). *Static Joint Strength of 70° Flush Head Straight Shank Ti-6Al-4V Fasteners in Non-Matching Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	HPT-V[a] (F_{su} = 95 ksi)			
Sheet and Plate Material	Clad 7075-T6 and T651			
Fastener Diameter (Nominal Shank Diameter, in.)[b]	3/16 (0.193)	1/4 (0.255)	5/16 (0.3175)	3/8 (0.380)
Sheet Countersink angle	82°	82°	82°	75°
	Ultimate Strength, lbs			
Sheet or plate thickness, in.:				
0.063	1348	...	...	...
0.071	1546	1970	...	...
0.080	1704	2275	...	...
0.090	1814	2580	3125	...
0.100	1948	2873	3528	4100
0.125	2265	3282	4465	5270
0.160	2700	3868	5171	6642
0.190	2779	4361	5826	7393
0.250	...	4851	7056	8880
0.312	...	...	7521	10396
0.375	...	...	...	10774
Fastener shear strength[c]	2779	4851	7521	10774
	Yield Strength[d], lbs			
Sheet or plate thickness, in.:				
0.063	1180	...	...	...
0.071	1378	1651	...	...
0.080	1590	1944	...	...
0.090	1702	2321	2631	...
0.100	1818	2620	3024	3350
0.125	2112	3055	4133	4664
0.160	2496	3601	4848	6209
0.190	2734	4062	5413	6902
0.250	...	4745	6552	8288
0.312	...	7378	9631	
0.375	...	...	...	10584
Head height (max.), in.	0.060	0.070	0.080	0.090

[a]Data supplied by PB Fasteners.
[b]Fasteners installed in interference holes (0.0045-0.0055) (Ref. 8.1.5).
[c]Fastener shear strength based on areas computed from the indicated nominal shank diameter and F_{su} = 95 ksi.
[d]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.5.2(m). *Static Joint Strength of 100° Flush Shear Head STA Ti-6Al-4V Fasteners in Machine-Countersunk Aluminum Alloy Sheet*

Fastener Type	NAS4452V Pin (F_{su} = 95 ksi), NAS4445D Nut[a]				
Sheet Material	Clad 7075-T6				
Fastener Diameter, in. (Nominal Shank Diameter, in.)	5/32 (0.164)	3/16 (0.190)	1/4 (0.250)	5/16 (0.312)	3/8 (0.375)
	Ultimate Strength, lbs				
Sheet or plate thickness, in.:					
0.040	766	...	...	...	...
0.050	1092	[b] 1173	...	...	...
0.063	1450	1639	1886	...	...
0.071	1633	1889	2290	[b] ...	...
0.080	1805	2136	2710	3028	...
0.090	1955	2368	3135	3651	...
0.100	2007	2557	3515	4230	4669
0.125	...	2694	4273	5485	6428
0.160	...	...	4660	6776	8426
0.190	...	...	...	7290	9708
0.250	...	...	...	...	10490
Fastener shear strength[c]	2007	2694	4660	7290	10490
	Yield Strength[d], lbs				
Sheet thickness, in.:					
0.040	712	...	...	...	...
0.050	891	1034	...	...	...
0.063	1103	1295	1712	...	...
0.071	1223	1445	1932	...	...
0.080	1349	1604	2169	2715	...
0.090	1475	1768	2420	3056	...
0.100	1489	1920	2658	3383	4082
0.125		2241	3196	4145	5072
0.160	...	...	3812	5076	6321
0.190	...	...	...	5746	7265
0.250	...	...	...	...	8802
Head height (max.), in.	0.040	0.049	0.063	0.077	0.091

[a]Data supplied by Huck Manufacturing Company.
[b]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[c]Fastener shear strength is documented in NAS4444.
[d]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.5.2(n). *Static Joint Strength of Protruding Shear Head Alloy Steel Hi-Lok Fasteners in Aluminum Alloy Sheet*

Fastener Type	HL 18 Pin (F_{su} = 95 ksi), HL 70 Collar[a]			
Sheet Material	Clad 7075-T6			
Fastener Diameter, in.	5/32	3/16	1/4	5/16
(Nominal Shank Diameter, in.)[b]	(0.164)	(0.190)	(0.250)	(0.312)
	Ultimate Strength, lbs.			
Sheet thickness, in.:				
0.050	1078	...	...	...
0.063	1353	1559	...	...
0.071	1520	1776	...	...
0.080	1718	1957	2593	...
0.090	1890	2224	2937	...
0.100	1930	2473	3250	4050
0.125	2007	2580	4063	5075
0.160	...	2694	4450	6509
0.190	...	...	4620	6880
0.250	...	...	4660	7290
Fastener shear strength[c]	2007	2694	4660	7290
	Yield Strength[d], lbs.			
Sheet thickness, in.:				
0.050	976	...	...	...
0.063	1251	1426	...	...
0.071	1430	1624	...	...
0.080	1589	1848	2344	...
0.090	1746	2065	2687	...
0.100	1875	2242	3031	3660
0.125	...	2563	3750	4734
0.160	...	...	4406	6051
0.190	...	...	...	6686

[a]Data supplied by Hi-Shear Corporation.

[b]Fasteners installed in clearance holes (0.0005-0.0025) (Ref. Section 8.1.5).

[c]Fastener shear strength based on areas computed from indicated nominal shank diameter and F_{su} = 95 ksi.

[d]Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

TABLE 8.1.5.2(o). *Static Joint Strength of 100° Flush Shear Head Alloy Steel Hi-Lok Fasteners in Machine-Countersunk Aluminum Alloy Sheet*

Fastener Type	HL 19 Pin (F_{su} = 95 ksi), HL 70 Collar[a]			
Sheet Material	Clad 7075-T6			
Fastener Diameter, in. (Nominal Shank Diameter, in.)[b]	5/32 (0.164)	3/16 (0.190)	1/4 (0.250)	5/16 (0.312)
	Ultimate Strength, lbs.			
Sheet thickness, in.:				
0.050	968	...	...	...
0.063	1251	1408	...	...
0.071	1400	1606	...	...
0.080	1595	1823	2344	...
0.090	1815	2050	2675	...
0.100	1903	2300	3000	3660
0.125	2005	2570	3781	4685
0.160	...	2694	4420	6051
0.190	...	...	4625	6832
0.250	...	...	4660	7290
Fastener shear strength[c]	2007	2694	4660	7290
	Yield Strength[d], lbs.			
Sheet thickness, in.:				
0.050	839	...	...	...
0.063	1031	1191	...	...
0.071	1141	1336	...	...
0.080	1279	1480	2013	...
0.090	1416	1632	2219	...
0.100	1540	1805	2420	3143
0.125	1807	2173	3000	3777
0.160	...	2545	3670	4800
0.190	...	...	4144	5514
0.250	...	...	...	6686
Head height (nom.), in.	0.040	0.046	0.060	0.067

[a] Data supplied by Hi-Shear Corporation.
[b] Fasteners installed in clearance holes (0.0005-0.0025) (Ref. Section 8.1.5).
[c] Fastener shear strength based on areas computed from indicated nominal shank diameter and F_{su} = 95 ksi.
[d] Permanent set at yield load: the greater of 0.012 inch or 4% of nominal diameter.

8.1.6 SPECIAL FASTENERS.—Due to the special nature of this classification of fastener, care must be exercised in their application. Consideration should be given to the proposed fastener application and its compatibility with data presented in this section. In particular, test and analysis methods used for fasteners in this section may necessarily be different than those used in preceding sections.

8.1.6.1 *Fastener Sleeves.*—Fastener sleeves are precision-formed, tubular elements designed to replace oversize fasteners used in the repair of damaged or enlarged holes.

8.1.6.1.1 *A-286 ACRES Sleeves in 7075-T6 Aluminum Alloy Sheet and Plate.*—Analysis of static lap joint data indicates that a single 100° low profile head, A-286 [ACRES Sleeve (part number JK5512C)] installed with titanium or steel Hi-Loks and alloy steel lockbolts (up to 108 ksi F_{su}) provided static joint allowable shear loads equivalent to those developed by the above-noted fasteners when tested without sleeves. Fasteners and sleeves were installed to the same comparable hole tolerance and fit condition as fasteners when tested alone. The analysis was restricted to static lap joint data (in accordance with MIL-STD-1312 Test 4) and equivalency to fastener systems other than those listed above is not implied. Other properties such as tensile strength, preload, fatigue strength, and corrosion characteristics should be verified by test data. When using sleeves, knife-edge conditions should be avoided.

8.1.6.2 *Sleeve Bolts.*—Tables 8.1.6.2(a) and (b) contain joint allowables for various sleeve bolt/sheet material combinations. Sleeve bolts are made of precision-formed aluminum alloy sleeve elements assembled on standard taper shank bolts. When the assembly is placed in a cylindrical hole and the bolt is drawn into the sleeve, the sleeve expands, thus filling the hole and causing an interference-fit condition.

The allowable loads were established from test data using the following criteria:

Ultimate Load.—Average ultimate test load divided by a factor of 1.15, as defined in Section 9.4. This factor is not applicable to shear strength cutoff values which are defined by the procurement specification.

Yield Load.—Average yield test load as defined in Section 9.4.1.3.3 and the load which results in a joint permanent set equal to 0.04D, where D is the hole size.

The allowable loads shown for flush-head fasteners are applicable to joints have e/D equal to or greater than 2.0.

For machine countersunk joints, the sheet gage specified in the tables herein is that of the countersunk sheet. When the noncountersunk sheet is thinner than the countersunk sheet, the bearing allowable for the noncountersunk sheet-fastener combination should be computed, compared to the table value, and the lower of the two values selected.

TABLE 8.1.6.2(a). *Static Joint Strength of 100° Reduced Flush Head, Alloy Steel Pin, Aluminum Alloy Sleeve, Fastener in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	MIL-B-8831/4[a] (F_{su} = 108 ksi)					
Sheet Material	Clad 7075-T6					
Fastener Diameter, in. (Nominal Hole Diameter, in.)[b,c]	3/16 (0.2390)	1/4 (0.3032)	5/16 (0.3695)	3/8 (0.4350)	7/16 (0.5022)	1/2 (0.5735)
	Ultimate Strength, lbs.					
Sheet thickness, in.:						
0.100	2585	...	...	...	...	...
0.125	3205	4100	5035	...	...	...
0.160	3290	5205	6385	7560	8790	...
0.190	...	5670	7535	8925	10360	11900
0.250	...	...	8760	11640	13495	15480
0.312	...	...	...	12395	16195	19180
0.375	...	...	...	12640	16625	21265
0.500	...	...	...	...	17100	22250
Fastener shear strength[d]	3290	5670	8760	12640	17100	22250
	Yield Strength[e], lbs.					
Sheet thickness, in.:						
0.100	2080	...	...	...	...	...
0.125	2570	3300	4075	...	...	...
0.160	3255	4170	5135	6105	7125	...
0.190	...	4915	6040	7175	8360	9635
0.250	...	...	7855	9310	10825	12450
0.312	...	...	...	11520	13375	15360
0.375	...	...	...	12355	15620	18320
0.500	...	...	...	...	...	21570
Sleeve head height (ref.) in.	0.062	0.075	0.082	0.093	0.115	0.120

[a]Data supplied by P.B. Fasteners.

[b]Nominal hole diameter based on $\left(\frac{\text{max. expanded sleeve} - \text{min. hole}}{2}\right)$ + min. hole using larger expanded diameter from MIL-B-8831/4 dated 23 August 1982.

[c]Fasteners installed to interference levels of 0.0025-0.008 in.

[d]Fastener shear strength is documented in NAS 1724 as 108 ksi.

[e]Permanent set at yield load: 4% of nominal hole diameter (Ref. 9.4.1.3.3).

TABLE 8.1.6.2(b). *Static Joint Strength of 100° Reduced Flush Head, Alloy Steel Pin, Aluminum Alloy Sleeve, Fastener in Machine-Countersunk Aluminum Alloy Sheet and Plate*

Fastener Type	MIL-B-8831/4[a] (F_{su} = 108 ksi)					
Sheet Material	Clad 2024-T3					
Fastener Diameter, in. (Nominal Hole Diameter, in.)[b,c]	3/16 (0.2390)	1/4 (0.3032)	5/16 (0.3695)	3/8 (0.4350)	7/16 (0.5022)	1/2 (0.5735)
	Ultimate Strength, lbs.					
Sheet thickness, in.:						
0.100	2175	...	...	...	...	...
0.125	2720	3450	4205	...	...	...
0.160	3290	4415	5380	6335	7315	...
0.190	...	5240	6390	7525	8685	9920
0.250	...	5480	7945	9895	11425	13050
0.312	...	5655	8165	11085	14260	16285
0.375	...	5670	8385	11345	14845	19070
0.500	...	...	8760	11865	15445	19755
0.625	...	...	...	12385	16045	20440
0.750	...	...	...	12640	16645	21225
0.875	...	...	...	....	17100	21805
1.000	...	...	...	...	...	22250
Fastener shear strength[d]	3290	5670	8760	12640	17100	22250
	Yield Strength[e], lbs.					
Sheet thickness, in.:						
0.100	1575	...	...	...	...	...
0.125	1880	2505	3200	...	...	...
0.160	2310	3050	3865	4720	5655	...
0.190	...	3515	4435	5395	6430	7595
0.250	...	4450	5570	6735	7980	9360
0.312	...	5055	6745	8115	9580	11185
0.375	...	5560	7460	9525	11205	13040
0.500	...	...	8680	11010	13655	16720
0.625	...	...	...	12385	15315	18625
0.750	...	...	...	12640	16645	20520
0.875	...	...	...	...	17100	21805
1.000	...	...	...	...	...	22250
Sleeve head height (ref.) in.	0.062	0.075	0.082	0.093	0.115	0.120

[a]Data supplied by P.B. Fasteners.

[b]Nominal hole diameter based on $\left(\frac{\text{max. expanded sleeve} - \text{min. hole}}{2}\right)$ + min. hole using larger expanded diameter from MIL-B-8831/4 dated 23 August 1982.

[c]Fasteners installed to interference levels of 0.002-0.008 in.

[d]Fastener shear strength is documented in NAS 1724 as 108 ksi.

[e]Permanent set at yield load: 4% of nominal hole diameter (Ref. 9.4.1.3.3).

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8.2 Metallurgical Joints

In the design of metallurgical joints, the strength of the joining material (for example, weld metal) and the adjacent parent material must be considered. The joint should be analyzed on the basis of its loading, the specified allowable strengths, dimensions and geometry.

8.2.1 INTRODUCTION AND DEFINITIONS.—The allowable strength for both the adjacent parent metal and the weld metal is given below in the particular section dealing with the method of foining used, and the material being joined. The following subparagraphs define certain joing processes.

Welding.—Welding consists of joining two or more pieces of metal by applying heat, pressure or both, with or without filler material, to produce a localized union through fusion or recrystallization across the joint interface. Examples of common welding processes include: fusion [inert-gas, shielded-arc welding with tungsten electrode (TIG) and inert-gas shielded metal-arc welding using covered electrodes (MIG)], resistance (spot and seam), and flash. Several terms used in describing various sections of a welded joint are illustrated in Figure 8.2.1.

Brazing.—Brazing consists of joining metals by the application of heat causing the flow of a thin layer, capillary thickness, of nonferrous filler metal into the space between the pieces. Bonding results from the intimate conatact produced by the dissolution of a small amount of base metal in the molten filler metal, without fusion of the base metal.

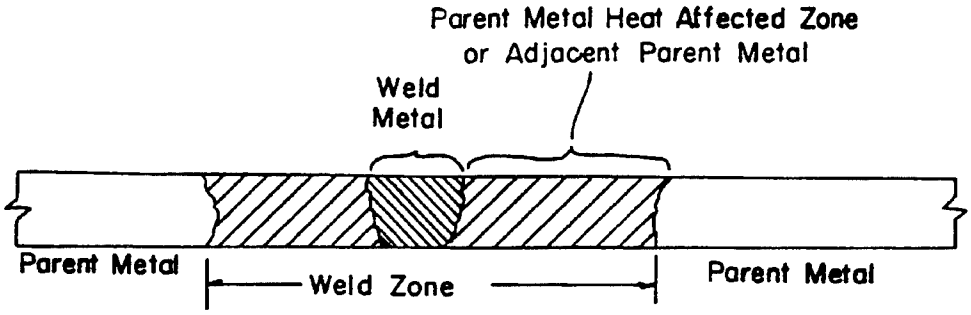


FIGURE 8.2.1. *Schematic diagram of weld and parent metal.*

8.2.2 WELDED JOINTS.—The weld metal section of a joint should be analyzed on the basis of its loading, specified allowable strength, dimensions and geometry. The effects of the parent metal are to be accounted for as specified herein.

8.2.2.1 *Fusion Welding—Arc and Gas.*— Section 9.4.2 contains a detailed discussion of one acceptable method of establishing fusion welding allowables. As stated in that section, other methods can be employed as approved by certificating agencies. The following subsections contain specific information for a number of materials.

8.2.2.1.1 *Strength of Fusion Welded Joints of Steel Alloys.*—Allowable fusion weld-metal strengths of steel alloys are shown in Table 8.2.2.1.1(a). Design allowable stresses for the weld metal are based on 85 percent of the respective minimum tensile ultimate test values.

For steel joints welded after heat treatment, the allowable strengths near the weld are given in Tables 8.2.2.1.1(b) and (c).

TABLE 8.2.2.1.1(a). *Strength of Fusion Welded Joints of Steel Alloys*

Material	Heat treatment subsequent to welding	Welding rod or electrode	F_{su}, ksi	F_{tu}, ksi
Carbon and alloy steels . .	None.....	AMS 6457	32	51
		AWSA5.1 classes E6010 and E6013	32	51
Alloy steels	None.....	AMS 6452	43	72
Alloy steels	Stress relieved.....	AWSA5.5 class E10013 . . . . . MIL-E-22200/10, classes MIL-10018-M1	50	85

TABLE 8.2.2.1.1(b). *Allowable Ultimate Tensile Stresses Near Fusion Welds in 4130, 4140, or 8630 Steels*[a]

Section thickness ¼ inch or less	
Type of joint	Ultimate tensile stress, ksi
Tapered joints of 30° or less[b]	90
All others	80

[a]Welded after heat treatment or normalized after weld.
[b]Gussets or plate inserts considered 0° taper with centerline.

TABLE 8.2.2.1.1(c). *Allowable Bending Modulus of Rupture Near Fusion Weld in 4130, 4140, 4340, or 8630 Steels*[a]

Type of joint	Bending modulus of rupture, ksi
Tapered joints of 30° or less[b]	F_b from Figure 2.8.1.1 for F_{tu} = 90 ksi
All others.....	0.9 of the values of F_b from Figure 2.8.1.1 for F_{tu} = 90 ksi

[a]Welded after heat treatment or normalized after weld.
[b]Gussets or plate inserts considered 0° taper with centerline.

For materials heat treated after welding, the allowable strength in the parent metal near a welded joint may equal the allowable strength for the material in the heat treated condition as given in the tables of design mechanical properties of the specific alloys; however, it should be noted that the weld metal allowables are based on 85 percent of these values.

8.2.2.2 *Flash and Pressure Welding.*--The ultimate tensile allowable strength and bending allowable modulus of rupture for flash and pressure welds are given in Tables 8.2.2.2(a) and (b). A higher efficiency may be permitted in special cases by the applicable procuring or certificating agency upon approval of the manufacturer's process specification.

8.2.2.3 *Spot and Seam Welding.*--Permission to use spot and seam welding on structural parts is governed by the requirements of the procuring or certificating agency. Table 8.2.2.3 gives the recommended allowable edge distance for spot and seam welds.

TABLE 8.2.2.2(a). *Allowable Ultimate Tensile Stress for Flash Welds in Steel Tubing*

Tubing	Allowable ultimate tensile stress of welds
Normalized tubing--not heat treated (including normalizing after welding	1.0 F_{tu} (based on F_{tu} of normalized tubing)
Heat-treated tubing welded after heat treatment	1.0 F_{tu} (based on F_{tu} of normalized tubing)
Tubing heat treated (including normalizing) after welding. F_{tu} of unwelded material in heat-treated condition:	
<100 ksi	0.9 F_{tu}
100 to 150 ksi	0.6 F_{tu} + 30
>150 ksi	0.8 F_{tu}

TABLE 8.2.2.2(b). *Allowable Bending Modulus of Rupture for Flash Welds in Steel Tubing*

Tubing	Allowable bending modulus of rupture of welds (F_b from Figure 2.8.1.1 using values of F_{tu} listed)
Normalized tubing--not heat treated (including normalizing after welding	1.0 F_{tu} for normalized tubing
Heat-treated tubing welded after heat treatment	1.0 F_{tu} for normalized tubing
Tubing heat treated (including normalizing) after welding. F_{tu} of welded material in heat-treated condition:	
<100 ksi	0.9 F_{tu}
100 to 150 ksi	0.6 F_{tu} + 30
>150 ksi	0.8 F_{tu}

TABLE 8.2.2.3. *Recommended Minimum Edge Distances for Spot-Welded Joints*

Nominal thickness of thinner sheet[a], in.	Edge distance[b], e, in.
0.016	3/16
0.020	3/16
0.025	7/32
0.032	1/4
0.036	1/4
0.040	9/32
0.045	5/16
0.050	5/16
0.063	3/8
0.071	3/8
0.080	13/32
0.090	7/16
0.100	7/16
0.125	9/16
0.160	5/8

[a]Intermediate gages will conform to the requirement for the next thinner gage shown.

[b]Edge distances less than those specified above may be used provided there is no explusion of weld material or bulging of the edge of the sheet or damage to bend radii by the electrode.

8.2.2.3.1 *Design Shear Strengths for Spot and Seam Welds in Uncoated Steels and Nickel and Cobalt Alloys.*--The design shear strength for spot welds for these materials are given in Tables 8.2.2.3.1(a) and (b). The thickness ratio of the thickest sheet to the thinnest outer sheet in the combination should not exceed 4:1.

8.2.2.3.1.1 *Effects of Spot-Welds on the Parent Metal Strength of 300 Series Stainless Steel.*--In applications of spot welding where ribs, intercostals, or doublers are attached to sheet, either at splices or at other joints on the sheet panels, the allowable ultimate strength of the spot-welded stainless steel sheet shall be determined by multiplying the ultimate tensile strength of the sheet (A or S-value) by the appropriate efficiency factors shown in Figures 8.2.2.3.1.1(a) through (c). Efficiencies for gages under 0.012 shall be determined by test.

8.2.2.3.2 *Design Shear Strengths for Spot and Seam Weldings in Aluminum Alloys.*--The acceptable aluminum and aluminum alloy combinations for spot and seam welding are given in Table 8.2.2.3.2(a).

Design shear-strength for spot welds in aluminum alloys are given in Tables 8.2.2.3.2(b) and (c). The thickness ratio of the thickest to the thinnest outer sheet in the combination should not exceed 4:1.

Design shear-strength for spot-welded joints, based on tearing of the sheet, is given in Table 8.2.2.3.2(d) for some aluminum alloys, together with the "maximum" pitches that permit attainment of these strengths. Joints having larger pitches fail in the spot welds rather than by tearing of the sheet, and are governed by Tables 8.2.2.3.2(b) and (c). The design shear strengths listed are also applicable to seam welds.

8.2.2.3.2.1 *Effects of Spot Welds on Parent Metal Strength of Aluminum Alloys.*--In applications of spot welding other than splices, where ribs, intercostals, or doublers are attached to sheet, the allowable ultimate strength of the spot-welded sheet may be determined by multiplying the ultimate tensile strength of the sheet (A or S values) by the appropriate efficiency factor shown on Figure 8.2.2.3.2.1. Efficiencies for gages under 0.020 shall be determined by test.

8.2.2.3.2.2 *Fatigue Strength of Spot-Welded Joints in Aluminum Alloys.*--The fatigue strength of spot-welded joints in aluminum alloy are given in Figures 8.2.2.3.2.2(a) through 8.2.2.3.2.2(e).

8.2.2.3.3 *Design Shear Strengths for Spot and Seam Welds in Magnesium Alloys.*--Design shear-strength for spot welds in magnesium alloys are given in Table 8.2.2.3.3. The thickness ratio of the thickest sheet to the thinnest outer sheet in the combination should not exceed 4:1.

8.2.2.3.4. *Design Shear Strengths for Spot and Seam Welds in Titanium and Titanium Alloys.*--Design shear strength for spot welds in titanium and titanium alloys are given in Tables 8.2.2.3.4(a) and (b). The thickness ratio of the thickest sheet to the thinnest outer sheet in the combination should not exceed 4:1.

TABLE 8.2.2.3.1(a). *Spot-Weld Design Shear Stregnth[a,b] in Thin Sheet and Foil for Uncoated Steels[c] and Nickel and Cobalt Alloys (Welding Specification MIL-W-6858)*

Thickness of Thinnest Outer Sheet, in.	Spots/inch		Material Ultimate Tensile Strength, ksi			
	Standard (Ns)[d]	Range[e,f]	Above 185	150 to 185	90 to 149	Below 90
			Design Shear Strength, pounds per linear inch (Xm)			
0.001	40	1-50	72	64	52	36
0.002	20	1-30	144	128	104	72
0.003	12	1-17	240	208	164	120
0.004	10	1-14	324	280	228	152
0.005	9	1-13	392	340	272	188
0.006	7	1-10	432	380	304	220
0.007	6	1-8	504	440	352	256
0.008	5	1-7	552	488	392	284

[a]Strength based on 80 percent of minimum values specified in Specification MIL-W-6858.

[b]The allowable tensile strength of spot-welds is 25 percent of the design shear strength. Higher values may be used, however, if these are substantiated by tests acceptable to the procuring or certifying agency.

[c]Refers to plain carbon steels containing not more than 0.15 percent carbon, austenitic heat and corrosion resistant, and precipitation hardening steels. The reduction in strength of spot-welds due to the cumulative effects of time-temperature-stress factors is not greater than the reduction in strength of the parent metal.

[d]When the number of spots per inch is within 15 percent of the standard spot per inch requirement, the design shear strengths tabulated above shall apply.

[e]When the number of spots differs from the standard spots per inch by 15 percent or greater, but does not exceed the noted range of spots per inch, applicable design strength shall be determined as noted below:

$$\frac{XM}{Ns}(K)Nr = Xr$$

where

Xm = design shear strength in accordance with the above table
Ns = standard spots per inch in accordance with the above table
Nr = required spots per inch (production part)
Xr = actual design shear strength requirement
K = 1.15 when number of spots per inch is reduced more than 15 percent of the standard spacing of the above table
K = 0.90 when number of spots is increased more than 15 percent of the standard spacing but within range of the tabular spacing.

[f]When the number of spots per inch is above the range indicated in the table, the design shear strength shall remain constant at the value obtained at the top of the range.

TABLE 8.2.2.3.1(b). *Spot-Weld Design Shear Strength[a,b] in Panels for Uncoated Steels[c] and Nickel and Cobalt Alloys (Welding Specification MIL-W-6858)*

Material Ultimate Tensile Strength, ksi	Design Shear Strength, pounds per spot			
	Above 185	150 to 185	90 to 149	Below 90
Nominal Thickness of Thinner Sheet, in.:				
0.009	160	140	104	80
0.010	196	164	128	92
0.012	280	220	160	120
0.016	384	320	236	172
0.018	472	392	272	200
0.020	508	424	312	224
0.022	584	488	360	264
0.025	696	580	424	320
0.028	820	684	508	372
0.032	1000	836	620	452
0.036	1200	1004	736	552
0.040	1400	1168	852	652
0.045	1680	1436	1028	804
0.050	1960	1700	1204	956
0.056	2304	2040	1416	1168
0.063	2840	2472	1688	1408
0.071	3360	2984	2028	1664
0.080	3880	3528	2404	1964
0.090	4480	4072	2812	2308
0.100	5040	4576	3200	2640
0.112	5600	5092	3636	3036
0.125	6228	5664	4052	3440

[a]Strength based on 80 percent of minimum values specified in Specification MIL-W-6858.

[b]The allowable tensile strength of spot-welds is 25 percent of the design shear strength. Higher values may be used, however, if these are substantiated by tests acceptable to the procuring or certifying agency.

[c]Refers to plain carbon steels containing not more than 0.15 percent carbon and to austenitic heat and corrosion resistant, precipitation hardening steels. The reduction in strength of spot-welds due to the cumulative effects of time-temperature-stress factors is not greater than the reduction in strength of the parent metal.

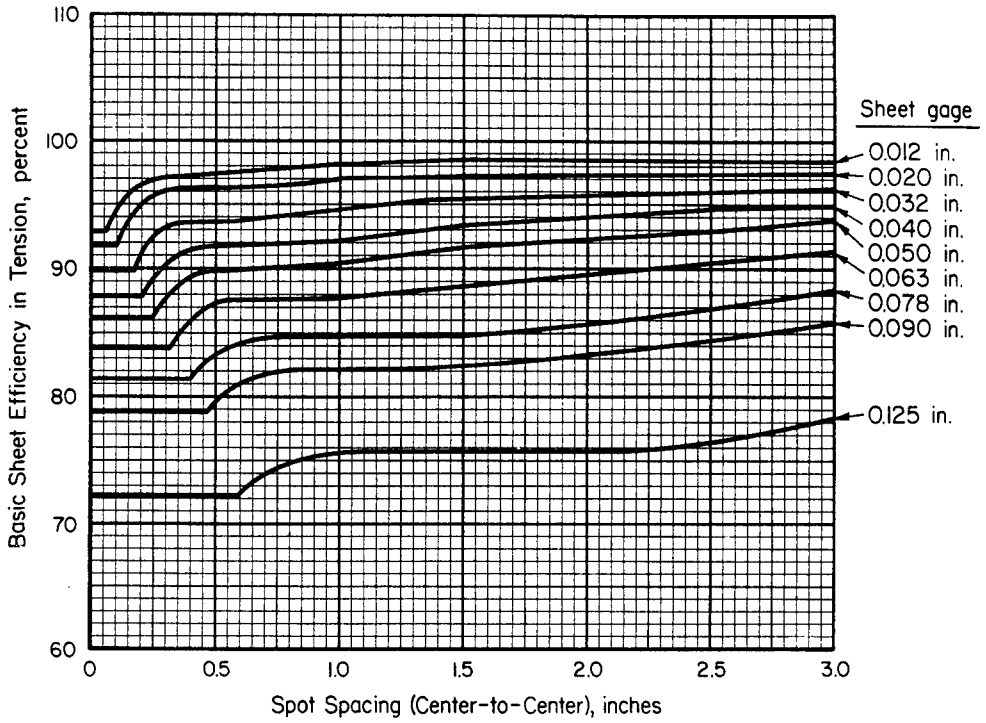


FIGURE 8.2.2.3.1.1(a). *Efficiency of the parent metal in tension for spot-welded AISI 301-A, AISI 347-A, and AISI 301-1/4 stainless steel.*

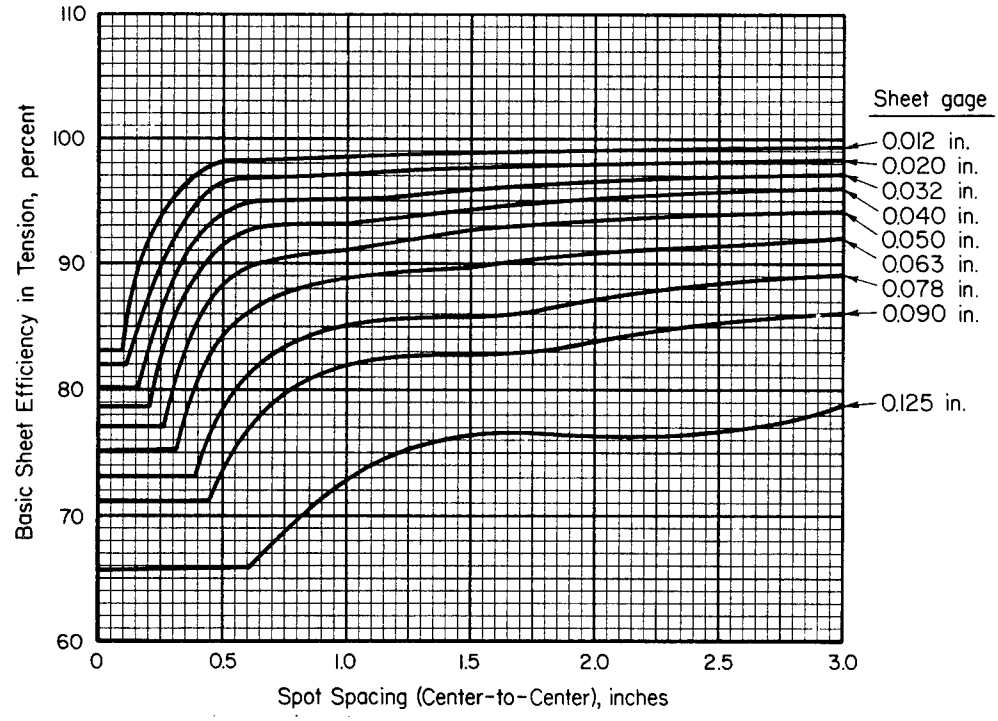


FIGURE 8.2.2.3.1.1(b). *Efficiency of the parent metal in tension for spot-welding AISI 301-1/2H stainless steel.*

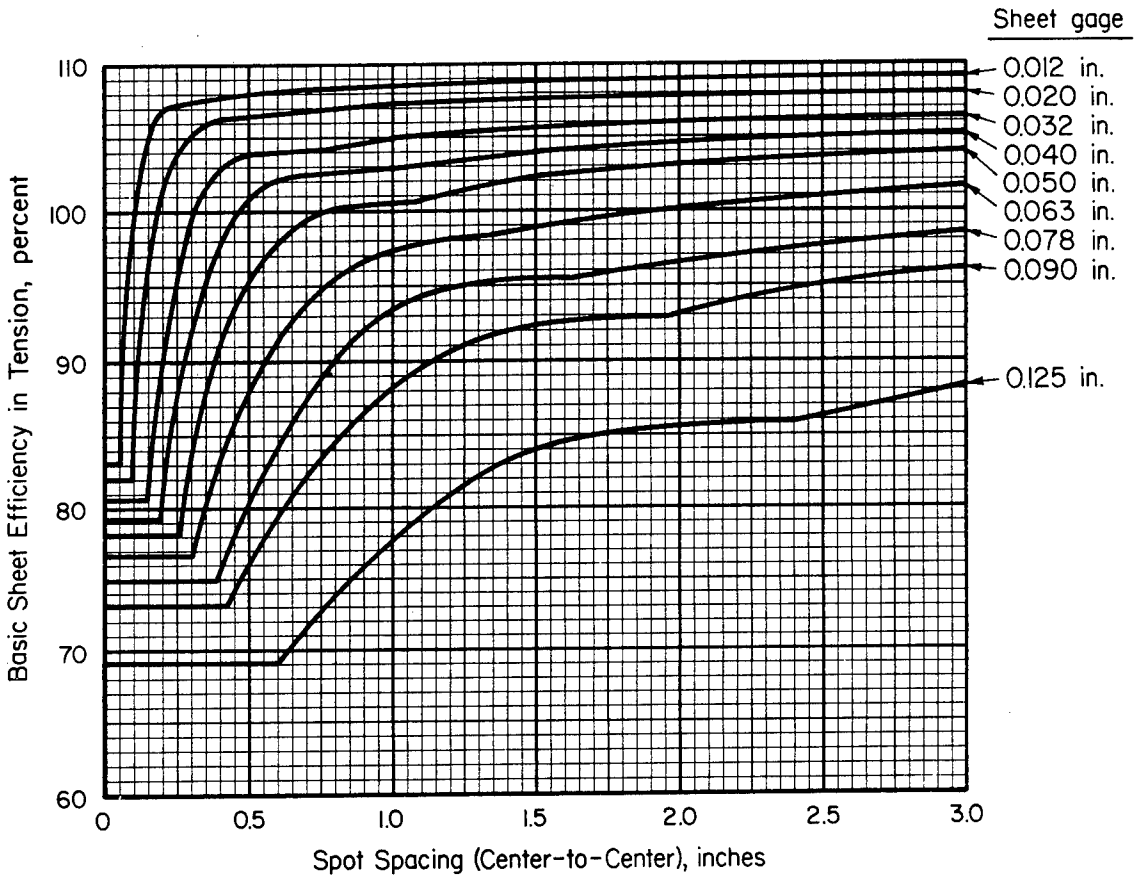


FIGURE 8.2.2.3.1.1(c). *Efficiency of the parent metal in tension for spot-welded AISI 301-H stainless steel.*

TABLE 8.2.2.3.2(a). *Acceptable Aluminum and Aluminum Alloy Combinations[a] for Spot and Seam Welding*

Specification		QQ-A-250/1	AMS-4029[b]	QQ-A-250/3	QQ-A-250/4[b]	QQ-A-250/5	QQ-A-250/2	QQ-A-250/8	QQ-A-250/11	QQ-A-250/12[b]	QQ-A-250/13[c]
Material		1100	Bare 2014	Clad 2014	Bare 2024	Clad 2024	3003	5052	6061	Bare 7075	Clad 7075
Specification	Material										
QQ-A-250/1	1100	...	...	...	...	...	...	...	...	...	...
AMS-4029	Bare 2014[b]	...	*	*	*	...	...	...	...	*	...
QQ-A-250/3	Clad 2014	...	*	...	*	...	...	...	...	*	...
QQ-A-250/4	Bare 2024[b]	...	*	*	*	...	...	...	...	*	...
QQ-A-250/5	Clad 2024	...	...	...	...	...	...	...	...	...	...
QQ-A-250/2	3003	...	...	...	...	...	...	...	...	...	...
QQ-A-250/8	5052	...	...	...	...	...	...	...	...	...	...
QQ-A-250/11	6061	...	...	...	...	...	...	...	...	...	...
QQ-A-250/12	Bare 7075[b]	...	*	*	*	...	...	...	...	*	...
QQ-A-250/13	Clad 7075[b]	...	...	...	...	...	...	...	...	...	...

[a]The various aluminum and aluminum-alloy materials referred to in this table may be spot-welded in any combinations except the combinations indicated by the asterisk (*) in the table. The combinations indicated by the asterisk (*) may be spot-welded only with the specific approval of the procuring or certifying agency.

[b]This table applies to construction of land- and carrier-based aircraft only. The welding of bare, high-strength alloys in construction of seaplanes and amphibians is prohibited unless specifically authorized by the procuring or certifying agency.

[c]Clad heat-treated and aged 7075 material in thicknesses less than 0.020 inch shall not be welded without specific approval of the procuring or certifying agency.

TABLE 8.2.2.3.2(b). *Spot-Weld Design Shear Strength in Thin Sheet and Foil for Bare and Clad Aluminum Alloys[a,b,c] (Welding Specification MIL-W-6858)*

Thickness of Thinnest Outer Sheet, in.	Spots/inch		Material Ultimate Tensile Strength, ksi	
			56 and above	Below 56
	Standard (Ns)[d]	Range[e,f]	Design Shear Strength, pounds per linear inch (Xm)	
0.001	40	1-50	24	16
0.002	20	1-30	48	32
0.003	12	1-17	80	52
0.004	10	1-14	108	72
0.005	9	1-13	132	92
0.006	7	1-10	148	100
0.007	6	1-8	168	112
0.008	5	1-7	188	128

[a]The reduction in strength of spot-welds due to the cumulative effects of time-temperature-stress factors is not greater than the reduction in strength of the parent metal.

[b]Strength based on 80 percent of minimum values specified in Specification MIL-W-6858.

[c]The allowable tensile strength of spot-welds is 25 percent of the design shear strength. Higher values may be used, however, if these are substantiated by tests acceptable to the procuring or certifying agency.

[d]When the number of spots per inch is within 15 percent of the standard spot per inch requirement, the design shear stregnths tabulated above shall apply.

[e]When the number of spots differs from the standard spots per inch by 15 percent or greater, but does not exceed the noted range of spots per inch, applicable design strength shall be determined as noted below:

$$XM/Ns\,(K)Nr = Xr$$

where

Xm = design shear strength in accordance with the above table
Ns = standard spots per inch in accordance with the above table
Nr = required spots per inch (production part)
Xr = actual dsign shear strength requirement
K = 1.15 when number of spots is reduced more than 15 percent of the standard spacing of the above table
K = 0.90 when number of spots is increased more than 15 percent of the standard spacing but within range of the tabular spacing.

[f]When the number of spots per inch is above the range indicated in the table, the design shear strength shall remain constant at the value obtained at the top of the range

TABLE 8.2.2.3.2(c). *Spot-Weld Design Shear Strength in Panels for Bare and Clad Aluminum Alloys[a,b,c] (Welding Specification MIL-W-6858)*

	Design Shear Strength, pounds per spot			
Material Ultimate Tensile Strength, ksi ...	56 and above	35 to 56	19.5 to 34.9	Below 19.5
Nominal Thickness of Thinner Sheet, in.:				
0.010	48	40	...	...
0.012	60	52	24	16
0.016	88	80	56	40
0.018	100	92	68	52
0.020	112	108	80	64
0.022	128	124	96	76
0.025	148	140	116	88
0.028	172	164	140	108
0.032	208	188	168	132
0.036	244	220	204	156
0.040	276	248	240	180
0.045	324	296	280	208
0.050	372	344	320	236
0.056	444	412	380	272
0.063	536	488	456	316
0.071	660	576	516	360
0.080	820	684	612	420
0.090	1004	800	696	476
0.100	1192	936	752	540
0.112	1424	1072	800	588
0.125	1696	1300	840	628
0.140	2020	1538	...	...
0.160	2496	1952	...	...
0.180	2980	2400	...	...
0.190	3228	2592	...	...
0.250	5880	5120	...	...

[a]The reduction in strength of spot-welds due to the cumulative effects of time-temperature-stress factors is not greater than the reduction in strength of the parent metal.

[b]Strength based on 80 percent of minimum values specified in Specification MIL-W-6858.

[c]The allowable tensile strength of spot-welds is 25 percent of the design shear strength. Higher values may be used, however, if these are substantiated by tests acceptable to the procuring or certifying agency.

TABLE 8.2.2.3.2(d). *Maximum Static Strength of Spot-Welded Joints in Aluminum Alloys and Corresponding Maximum Design Spot-Weld Pitch*[a,b]

Material	Single row joints						Multiple row joints					
	7075-T6 clad		2024-T3 clad		6061-T6		7075-T6 clad		2024-T3 clad		6061-T6	
Thickness of thinnest sheet, in.	Strength, lbs/in.	Pitch, in.	Strength, lbs/in.	Pitch, in.	Strength, lbs/in.	Pitch, in.	Strength, lbs/in.	Pitch÷No. of rows,in.	Strength, lbs/in.	Pitch÷No. of rows,in.	Strength, lbs/in.	Pitch÷no of rows,in
0.010	288	0.167	250	0.192	210	0.190	438	0.110	384	0.125	329	0.122
0.012	346	0.173	300	0.200	252	0.206	526	0.114	461	0.130	395	0.132
0.016	461	0.191	400	0.220	336	0.238	701	0.126	614	0.143	526	0.152
0.020	577	0.194	500	0.224	420	0.257	876	0.128	768	0.146	658	0.164
0.025	721	0.205	625	0.237	525	0.267	1095	0.135	960	0.154	822	0.170
0.032	923	0.225	800	0.260	672	0.280	1402	0.148	1229	0.169	1053	0.179
0.040	1059	0.261	918	0.301	778	0.319	1752	0.158	1536	0.180	1316	0.188
0.050	1230	0.302	1067	0.349	910	0.378	2190	0.170	1920	0.194	1645	0.209
0.063	1452	0.369	1259	0.426	1082	0.451	2759	0.194	2419	0.222	2073	0.235
0.071	1589	0.415	1378	0.479	1187	0.485	3110	0.212	2726	0.242	2336	0.247
0.080	1742	0.471	1511	0.543	1306	0.524	3504	0.234	3072	0.267	2632	0.260
0.090	1913	0.525	1660	0.605	1438	0.556	3942	0.255	3456	0.290	2061	0.270
0.100	2084	0.572	1808	0.659	1580	0.596	4380	0.272	3840	0.310	3290	0.284
0.112	2289	0.622	1986	0.717	1728	0.620	4906	0.290	4301	0.331	3685	0.291
0.125	2511	0.675	2179	0.788	1900	0.684	5475	0.310	4800	0.353	4112	0.316

[a] For multiple row joints row spacing is at minimum and same pitch in all rows.

[b] For pitches greater than those shown, strength is governed by Tables 8.2.2.3.2(b) and (c).

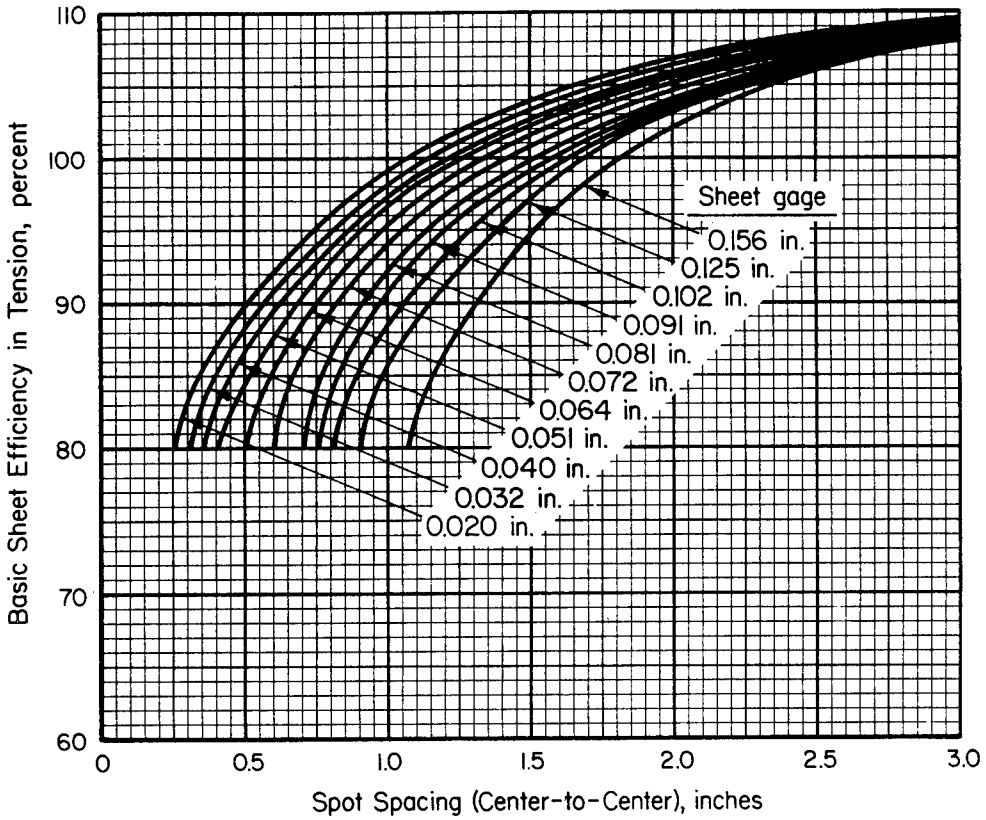


FIGURE 8.2.2.3.2.1. *Efficiency of the parent metal in tension for spot-welded aluminum alloys.*

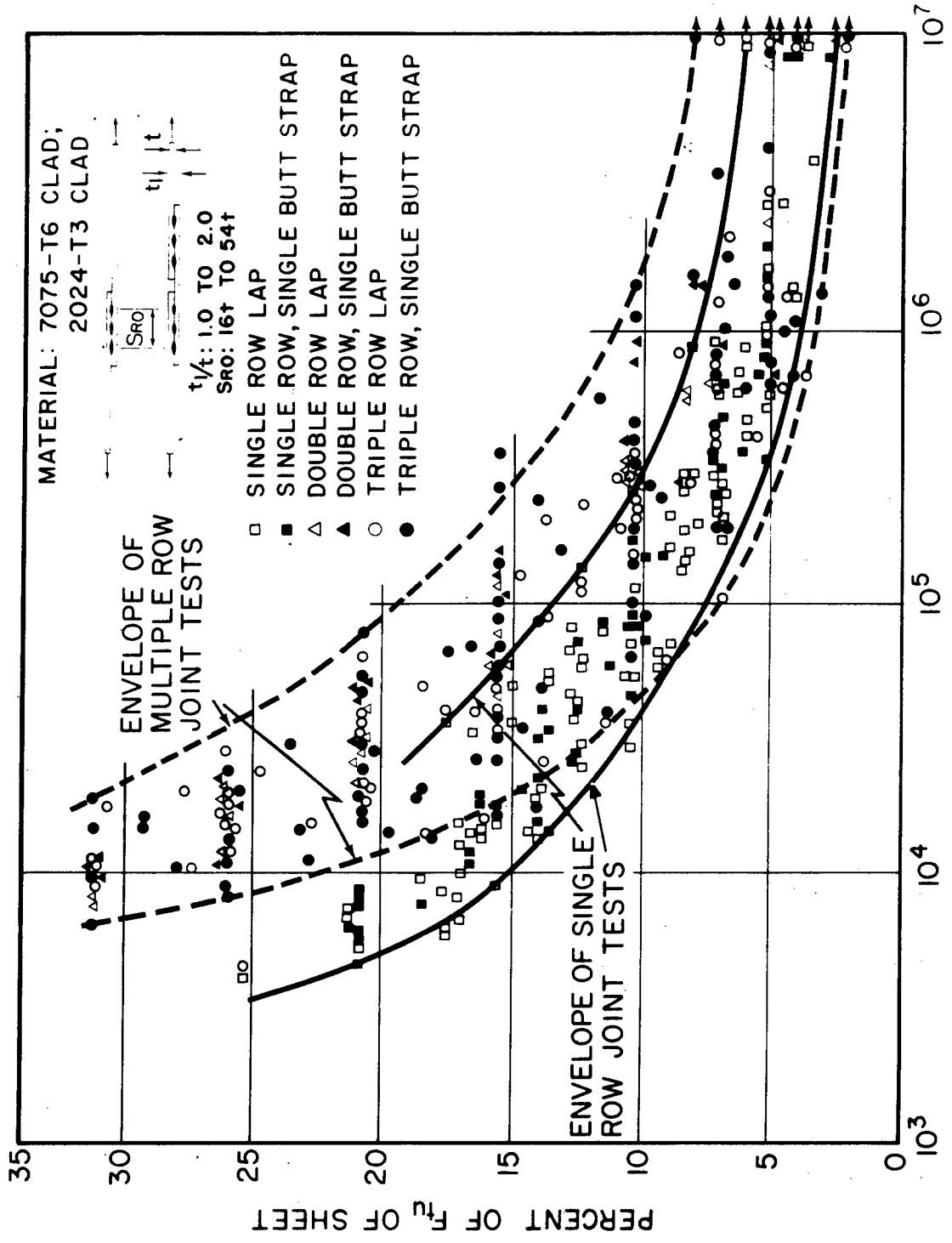


FIGURE 8.2.2.3.2.2(a). *Fatigue strength of spot-welded joints in aluminum alloy sheet. Load Ratio = 0.05 (static failure by tearing sheet).*

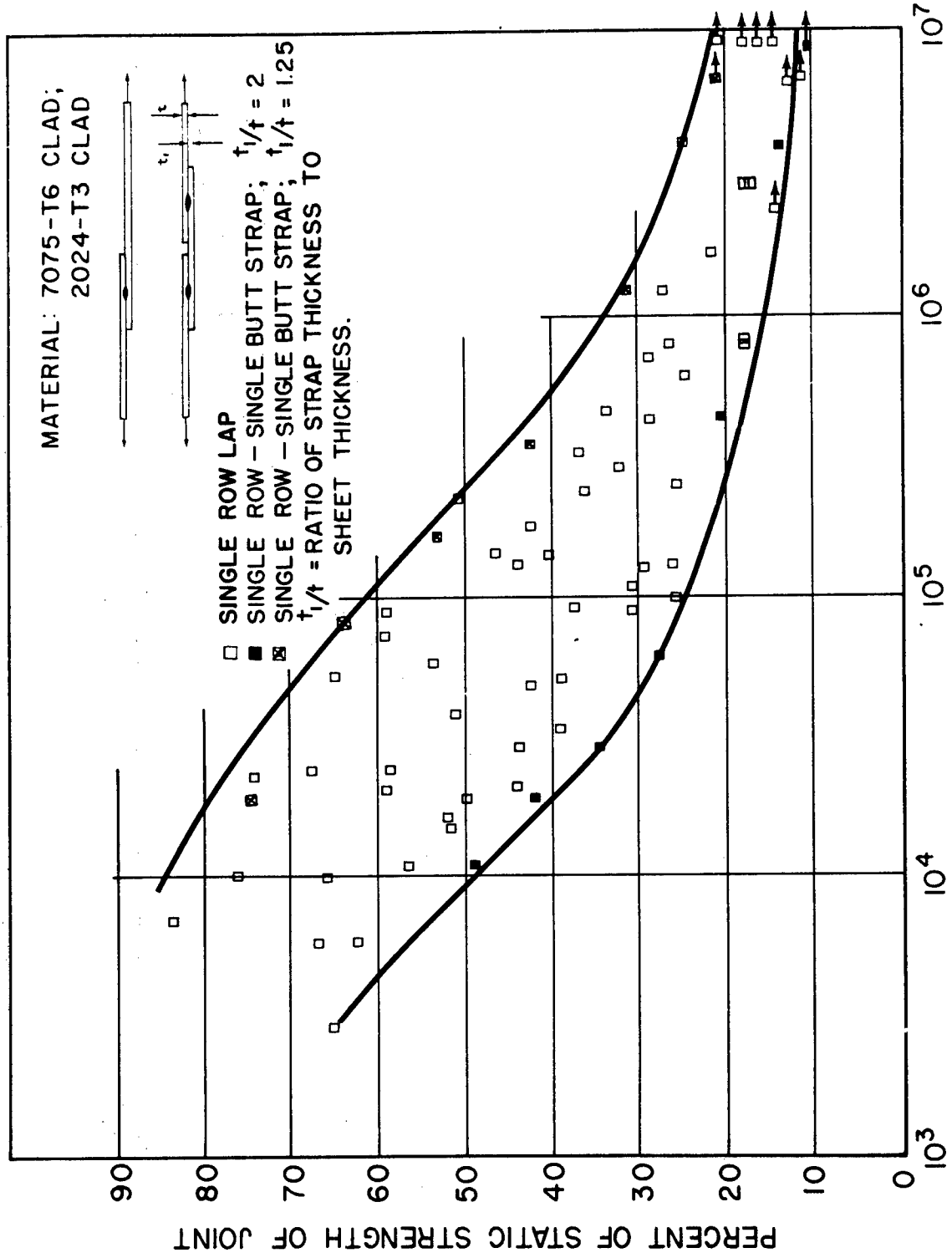


FIGURE 8.2.2.3.2.2(b). *Fatigue strength of spot-welded joints in aluminum alloy sheet. Load Ratio = 0.05 (static failure by shear in spot welds).*

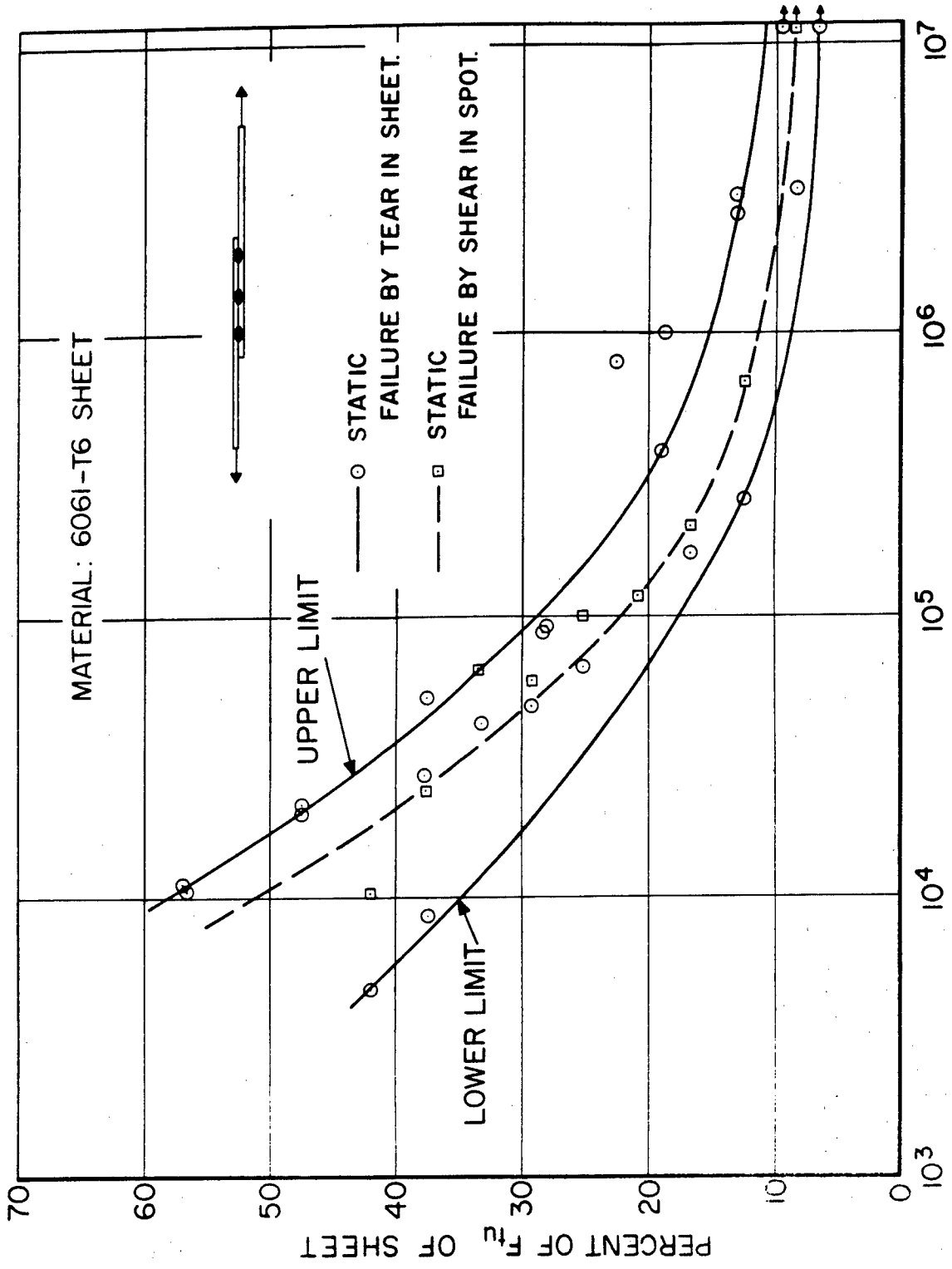


FIGURE 8.2.2.3.2.2(c). *Fatigue strength of triple row spot-welded lap joints in 6061-T6 aluminum alloy sheet. Load Ratio = 0.05.*

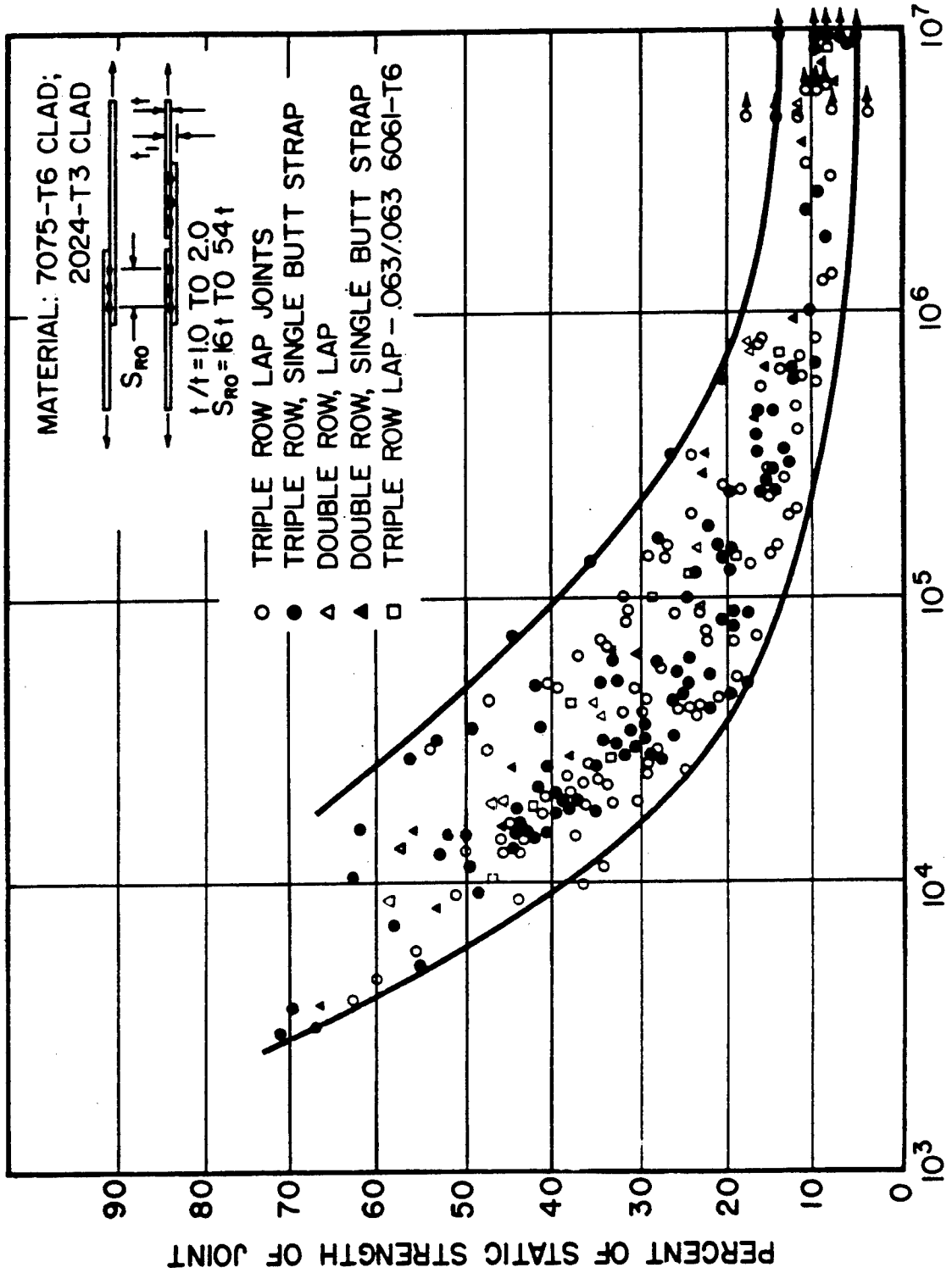


FIGURE 8.2.2.3.2.2(d). *Fatigue strength of spot-welded multiple row joints in aluminum alloy sheet. Load Ratio = 0.05 (static failure by shear in the spot welds).*

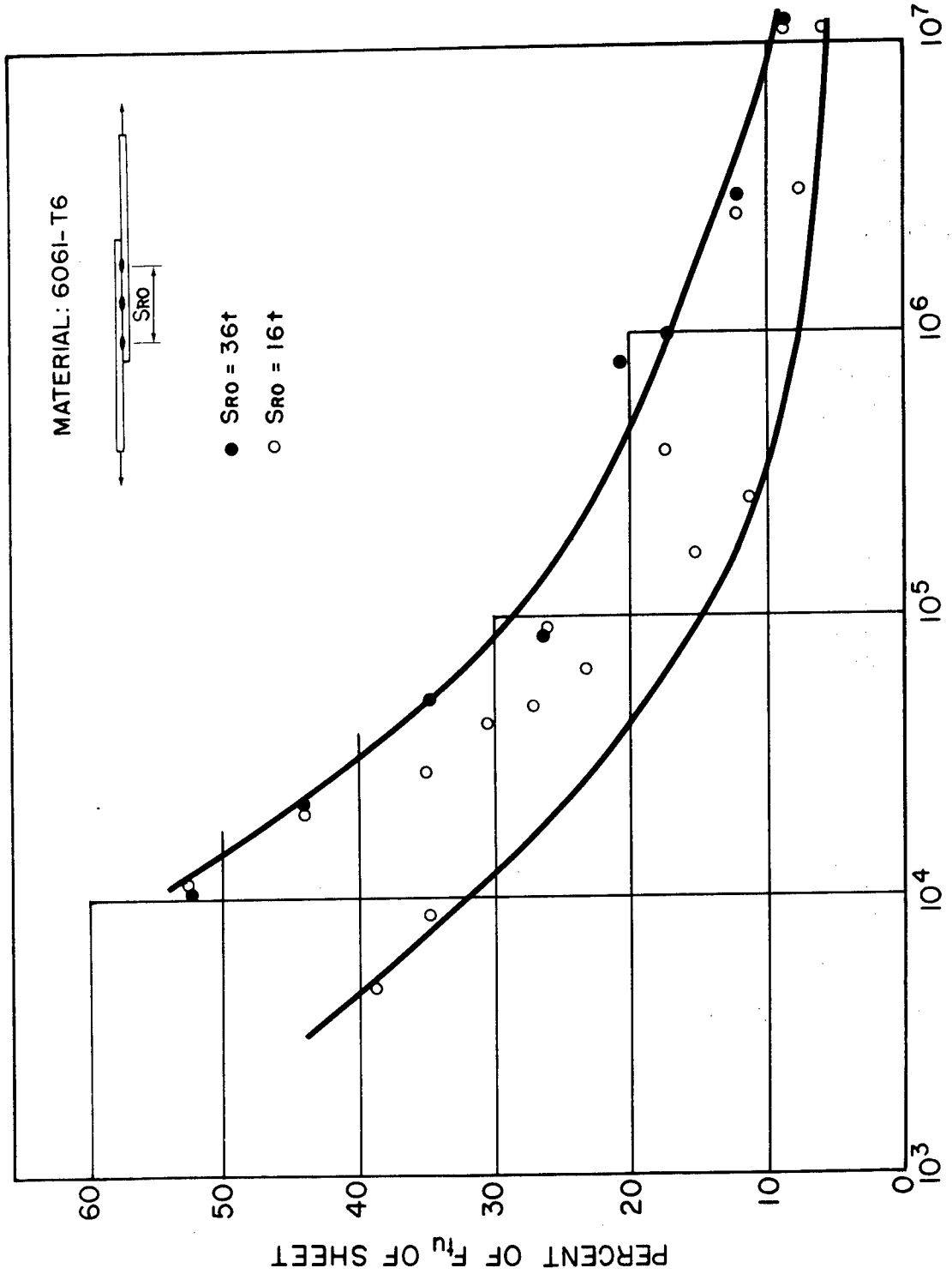


FIGURE 8.2.2.3.2.2(e). *Fatigue strength of triple row spot-welded lap joints in 6061-T6 aluminum alloy sheet. Load Ratio = 0.05 (static failure by tear in sheets).*

TABLE 8.2.2.3.3. *Spot-Weld Design Shear Strength in Panels for Magnesium Alloys*[a,b,c] *(Welding Specification MIL-W-6858)*

Material Ultimare Tensile Strength, ksi...	Design Shear Strength, pounds per spot	
	Greater than 19.5	Less than 19.5
Nominal Thickness of Thinner Sheet, in.:		
0.012	24	16
0.016	56	40
0.018	68	52
0.020	80	64
0.022	96	76
0.025	116	88
0.028	140	108
0.032	168	132
0.036	204	156
0.040	240	180
0.045	280	208
0.050	320	236
0.056	380	272
0.063	456	316
0.071	516	360
0.080	612	420
0.090	696	476
0.100	752	540
0.112	800	588
0.125	840	628

[a]Strength based on 80 percent of minimum values specified in Specification MIL-W-6858.
[b]The allowable tensile strength of spot-welds is 25 percent of the design shear strength. Higher values may be used, however, if these are substantiated by tests acceptable to the procuring or certifying agency.
[c]Magnesium alloys AZ31B and HK31A may be spot-welded in any combination.

TABLE 8.2.2.3.4(a). *Spot-Weld Design Shear Strength in Thin Sheet and Foils for Titanium and Titanium Alloys[a,b,c] (Welding Specification MIL-W-6858)*

Thickness of Thinnest Outer Sheet, in.	Spots/inch		Materials Ultimate Tensile Strength, ksi			
	Standard (Ns)[d]	Range[e,f]	Above 185	150 to 185	90 to 149	Below 90
			Design Shear Strength, pounds per linear inch (Xm)			
0.001	40	1-50	72	64	52	36
0.002	20	1-30	144	128	104	72
0.003	12	1-17	240	208	164	120
0.004	10	1-14	324	280	228	152
0.005	9	1-13	392	340	272	188
0.006	7	1-10	432	380	304	220
0.007	6	1-8	504	440	352	256
0.008	5	1-7	552	488	392	284

[a] The reduction in strength of spot-welds due to the cumulative effects of time-temperature-stress factors is not greater than the reduction in strength of the parent metal.

[b] Strength based on 80 percent of minimum values specified in Specification MIL-W-6858.

[c] The allowable tensile strength of spot-welds is 25 percent of the design shear strength. Higher values may be used, however, if these are substantiated by tests acceptable tot he procuring or certifying agency.

[d] When the number of spots per inch is within 15 percent of the standard spot per inch requirement, the design shear strengths tabulated above shall apply.

[e] When the number of spots differs from the standard spots per inch by 15 percent or greater, but does not exceed the notedrange of spots per inch, applicable design strength shall be determined as noted below:

$$XM/Ns(K)Nr = Xr$$

where

Xm = design shear strength in accordance with the above table
Ns = standard spots per inch in accordance with the above table
Nr = required spots per inch (production part)
Xr = actual design shear strength requirement
K = 1.15 when number of spots is reduced more than 15 percent of the standard spacing of the above table
K = 0.90 when number of spots is increased more than 15 percent of the standard spacing but within range of the tabular spacing

[f] When the number of spots per inch is above the range indicated in the table, the design shear strength shall remain constant at the value obtained at the top of the range.

TABLE 8.2.2.3.4(b). *Spot-Weld Design Shear Strength in Panels for Titanium and Titanium Alloy[a,b,c] (Welding Specification MIL-W-6858)*

	Design Shear Strength, pounds per spot	
Material Ultimate Tensile Strength, ksi ...	Above 100	100 and Below
Nominal Thickness of Thinner Sheet, in.:		
0.010	164	128
0.012	220	160
0.016	320	236
0.018	392	272
0.020	424	312
0.022	488	360
0.025	580	424
0.028	684	508
0.032	836	620
0.036	1004	736
0.040	1168	852
0.045	1438	1028
0.050	1702	1204
0.056	2040	1416
0.063	2400	1688
0.071	2702	1914
0.080	3048	2160
0.090	3430	2435
0.100	3810	2702
0.112	4260	3030
0.125	4760	3380

[a]The reduction in strength of spot-welds due to the cumulative effects of time-temperature-stress factors is not greater than the reduction in strength of the parent metal.

[b]Strength based on 80 percent of minimum value specified in Specification MIL-W-6858.

[c]The allowable tensile strength of spot-welds is 25 percent of the design shear strength. Higher values may be used, however, if these are substantiated by tests acceptable to the procuring or certifying agency.

8.2.3 BRAZING

8.2.3.1 *Copper Brazing.*--The allowable shear strength for copper brazing of steel alloys shall be 15 ksi, for all conditions of heat treatment. Higher values may be allowed upon approval of the procuring certificating agency.

The effect of the brazing process on the strength of the parent or base metal of steel alloys shall be considered in the structural design. Where copper furnace brazing is employed, the calculated allowable strength of the base metal which is subjected to the temperatures of the brazing process shall be in accordance with the following:

Material	Allowable strength
Heat-treated material (including normalized) used in "as-brazed" condition	Mechanical properties of normalized material
Heat-treated material (including normalized) reheat-treated during or after brazing	Mechanical properties corresponding to heat treatment performed

8.2.3.2 Silver Brazing.--Silver-brazed areas should not be subjected to temperatures exceeding 900F. Silver brazing alloys are listed in specification QQ-B-654. Deviation from this specification may be allowed upon approval of the procuring or certificating agency.

The allowable shear strength for silver brazing of steel alloys shall be 15 ksi, provided that clearances or gaps between parts to be brazed do not exceed 0.010 in. Deviation from this specified allowable value may be allowed upon approval of the procuring or certificating agency.

The effect of silver brazing on the strength of the parent or base metal is the same as shown for copper brazing in Section 8.2.3.1.

8.3 Bearings, Pulleys, and Wire Rope

Bearings.--Design, strengths, selection criteria, and other data for plain and antifriction bearings are found in AFSC Design Handbook AFSC DH-2-1, Chapters 3 and 6.

Pulleys.--Pulley strengths and design data are to be utilized in accordance with Specification MIL-P-7034.

Wire Rope.--Strengths and design data for wire rope are to be selected from the following specifications, whichever is appropriate: MIL-W-83420 or MIL-W-87161.

REFERENCES

8.1.2.1 Fugazzi, G. R., "Results of Test Evaluation Program to Develop Design Joint Strength Load Allowable Values for A-286 Solid Rivets Under Room and Elevated Temperature Conditions", Almay Research and Testing Corporation Report No. G8058, 63 pp. (November 1964).

8.1.2.2 "Report on Flush Riveted Joint Strength", Airworthiness Requirements Committee, A/C Industries Association of America, Inc., Airworthiness Project 12 (Revised May 25, 1948).

8.1.5.2 "Report on Flush Screw Joint Strength", Airworthiness Requirements Committee, A/C Industries Association of American, Inc., Airworthiness Project 20 (Revised April 6, 1953).

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Chapter 9

GUIDELINES FOR THE PRESENTATION OF DATA

This chapter contains Guidelines for judging adequacy of data, procedures for analyzing data in determining property values for inclusion in previous chapters, and formats for submitting results of analyses to the MIL-HDBK-5 Coordination Group for approval.

The following subindex should be helpful in locating sections of these Guidelines applicable to various properties:

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9.0	Summary	9-1a
9.1	General	9-2
9.1.1	Introduction	9-2
9.1.2	Applicability	9-2
9.1.3	Approval Procedures	9-2
9.1.4	Documentation Requirements	9-2
9.1.5	Symbols and Definitions	9-3
9.1.6	Data Requirements for Incorporation of a New Product into MIL-HDBK-5	9-3a
9.1.7	Procedure for the Submission of Mechanical Property Data	9-8
9.2	Room-Temperature Design Properties	9-9
9.2.1	Introduction	9-9
9.2.2	Definitions	9-9
9.2.3	Computational Procedures, General	9-12
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References		9-237

9.0 Summary

The objective of this summary is to provide a global overview of Chapter 9 without defining specific statistical details. This overview will be most helpful to those unfamiliar with the statistical procedures used in MIL-HDBK-5 and to those who would like to learn more about the philosophy behind the MIL-HDBK-5 guidelines.

Chapter 9 is the "rule book" for MIL-HDBK-5. Since 1966, these guidelines have described statistical procedures used to calculate mechanical properties for alloys included in the Handbook. Recommended changes in the guidelines are reviewed first by the Guidelines and Emerging Materials Task Group (GEMTG) and later approved by the entire coordination committee. Recommended changes in statistical procedures within the guidelines are evaluated first by the Statistics Working Group (SWG), which supports the GEMTG. Similarly, recommended changes in fastener analysis procedures are examined by the Fastener Task Group (FTG) before approval by the coordination committee.

Chapter 9 is divided into 6 subchapters which cover the analysis methods used to define room and elevated temperature properties. The room temperature mechanical properties are tensile, compression, bearing, shear, fatigue, fracture toughness, elongation and elastic modulus. The elevated temperature properties are the same, except that creep and stress rupture properties are added to the list. Analysis procedures for fatigue, fatigue crack growth and mechanically fastened joints are also covered since these data are commonly used in aircraft design. The presentation of these data varies depending upon the data type. For instance, the room temperature mechanical properties (tensile, compression, bearing, shear, elongation and elastic modulus) are provided in a tabular format, while the fatigue, elevated temperature properties, and typical stress strain curves are presented in graphical format.

Before an alloy can be considered for inclusion in MIL-HDBK-5, it must be covered by a commercial or government specification. There are two main reasons for this: 1) the alloy, and its method of manufacture, must be "reduced to standard practice" to increase confidence that the material, if obtained from different suppliers, will still demonstrate similar mechanical properties, and 2) specification minimum properties are included in MIL-HDBK-5 tables as design properties in situations where there are insufficient data to determine statistically-based material design values.

The majority, by far, of the data in MIL-HDBK-5 are room temperature design properties: including tensile (F_{tu}, F_{ty}), shear (F_{su}), compression (F_{cy}), bearing strengths (F_{bru}, and F_{bry}), elongation and elastic modulus. Room temperature design properties are the primary focus in the Handbook because most aircraft, commercial and military, typically operate at near-ambient temperatures and because most material specifications include only room temperature property requirements.

Design minimum mechanical properties tabulated in MIL-HDBK-5 are calculated either by "direct" or "indirect" statistical procedures. The minimum sample size required for the direct computation of T_{99} and T_{90} values (from which A and B-basis design properties are established) is 100. These 100 observations must include data from at least 10 heats and lots (as defined in the next paragraph). A T_{99} value is a statistically computed, one-sided lower tolerance limit, representing a 95 percent confidence lower limit on the first percentile of the distribution. Similarly, a T_{90} value is a statistically computed, one-sided lower tolerance limit, representing a 95 percent lower confidence limit on the tenth percentile of the distribution. If the sample cannot be described by a normal or Weibull distribution, the T_{99} and T_{90} values must be computed by nonparametric (distribution free) means, which can only be done if there are at least 299 observations. In most cases, only minimum tensile ultimate and yield strength values are determined by the direct method. T_{90} values are not computed if there are insufficient data to compute T_{99} values, even though a much smaller sample size is required to compute nonparametric T_{90} values.

This is because the general consensus within the MIL-HDBK-5 committee has been that a large number of observations (in the realm of 100) are needed from a large number of heats and lots (e.g. 10) for a particular material to properly characterize the variability in strength of that product.

A lot represents all of the material of a specific chemical composition, heat treat condition or temper, and product form that has passed through all processing operations at the same time. Multiple lots can be obtained from a single heat. A heat of material, in the case of batch melting, is all of the material that is cast at the same time from the same furnace and is identified with the same heat number. In the case of continuous melting, a single heat of material is generally poured without interruption. The exception is for ingot metallurgy wrought aluminum products, where a single heat is commonly cast in sequential aluminum ingots, which are melted from a single furnace change and poured in one or more drops without changes in the processing parameters (see Table 9.1.6.2).

Minimum compression, bearing, and shear strengths are typically determined through the indirect method. This is done to reduce cost, because as few as 10 data points (from 2 heats and 10 lots) can be used, in combination with "paired" direct properties to compute a design minimum value. In this indirect method, the compression, bearing, and shear strengths are paired with tensile values determined in the same region of the product to produce a ratio. Statistical analyses of these ratios are conducted to obtain lower bound estimates of the relationship between the primary property and the ratioed property. These ratios are then multiplied with the appropriate F_{tu} or F_{ty} in the Handbook to obtain the F_{su}, F_{cy}, F_{bru}, F_{bry} values for shear, compression, and bearing (ultimate and yield), respectively.

Many mechancial property tables in the Handbook include data for specific grain directions and thickness ranges. This is done to better represent anisotropic materials, such as wrought products, that often display variations in mechanical properties as a function of grain direction and/or product thickness. Therefore, it is common practice to test for variability in mechanical properties as a function of product thickness. This is done through the use of regression analysis for both direct and indirect properties. If a regression is found to be significant, properties may be computed separately (without regression) for reduced thickness ranges.

To compliment the mechanical property tables, the Handbook also contains typical stress-strain curves. These curves are included to illustrate each material's yield behavior and to graphically display differences in yield behavior for different grain directions, tempers, etc. These curves are identified as typical because they are based upon only a few test points. Typical curves are shown for both tension and compression and are extended to just beyond the 0.2 percent yield stress. Each typical curve also contains a shape factor called the Ramberg-Osgood number (n). These numbers can be used in conjunction with a material's elastic modulus to empirically develop a stress strain curve. Typical tensile full-range stress-strain curves are also provided that illustrate deformation behavior from the proportional limit to fracture. In addition, compression tangent modulus curves are provided to describe compression instability.

Effect of temperature and thermal exposure curves are included throughout the Handbook. For tensile properties, the curves are presented as a percentage of the room temperature design value. For these curves, there is a minimum data requirement and statistical procedures have been established to construct the curves. The creep rupture plots are shown as typical isothermal curves of stress versus time. The physical properties are shown as a function of temperature for each property i.e. specific heat, thermal conductivity etc. Physical properties are reported as average actual values, not a percentage of a room temperature value.

In addition to the mechanical properties, statistically based S/N fatigue curves are provided in the Handbook, since many airframe structures experience dynamic loading conditions. The statistical procedures are fairly rigorous. For example, the procedure describes how to treat outliers and run-outs (discontinued tests), and which models to use to best-fit a specific set of data. Each fatigue figure includes relevant information such as K_t, R value, material properties, sample size and equivalent stress equation. Each figure should be closely examined by the user to properly identify the fatigue curves required for a particular design.

Design properties for mechanical fasteners and mechanically fastened elements are also included in MIL-HDBK-5. A unique analysis procedure has been developed for mechanical fasteners because fasteners generally do not develop the full bearing strength of materials in which they are installed. Realistic joint allowables are determined from test data using the statistical analysis procedures described in Chapter 9. There are four different types of fasteners for which design allowables must be determined, as described in Section 5.

The last section in the Handbook (Section 6) provides a detailed description of statistical procedures used in Chapter 9 for the analysis of data. Most of these procedures are backed up with examples and appropriate statistical tables.

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9.1 General

This section of the Guidelines covers general information. Information specific to individual properties can be found in pertinent sections.

9.1.1 INTRODUCTION.—Design properties in MIL-HDBK-5 are used in the design of aerospace structures and elements. Thus, it is exceedingly important that the values presented in MIL-HDBK-5 reflect as accurately as possible the actual properties of the products covered.

Throughout the Guidelines, many types of statistical computations are referenced. Since these may not be familiar to all who may be analyzing data in the preparation of MIL-HDBK-5 proposals, a detailed description of each operation is required. To present the detailed description in the individual sections, however, would unnecessarily complicate the orderly presentation of the overall computational procedures. Therefore, the detailed description of the statistical techniques have been covered in Section 9.6.

9.1.2 APPLICABILITY.—Minimum data requirements and analytical procedures defined in these Guidelines for establishment of MIL-HDBK-5 design properties and elevated temperature curves for these properties should be used to obtain approval of such values or curves when proposed to the MIL-HDBK-5 Coordination Group or a certificating agency. However, the minimum data requirements and analytical procedures are not mandatory; to the extent of precluding use of other analytical procedures which can be substantiated. Any exceptions or deviations must be reported when requesting approval of these values or curves by the Coordination Group or certificating agency.

9.1.3 APPROVAL PROCEDURES.—The MIL-HDBK-5 Coordination Group (a voluntary, joint Government-Industry activity) meets twice yearly. At each meeting, this group acts upon proposed changes or additions to the document submitted in writing in advance of the meeting. The agenda is normally mailed to attendees four weeks prior to the meeting date, and the minutes four weeks following the meeting. Attachments for either the agenda or the minutes should be delivered to the Secretariat well in advance of the mailing date.

Attachments containing proposed changes or additions to the document shall include specific notations of changes or additions to be made; adequate documentation of supporting data; analytical procedures used (see Section 9.1.4); discussion of analysis of data; and a listing of exceptions or deviations from the requirements of these Guidelines.

Approval procedures for establishment of MIL-HDBK-5 equivalent design values are defined by the individual certificating agency.

9.1.4 DOCUMENTATION REQUIREMENTS.—The purpose of adequate documentation of proposals submitted to the MIL-HDBK-5 Coordination Group is to permit an independent evaluation of proposals by each interested attendee and to provide a historical record of actions of the Coordination Group. For this reason, both supporting data and a description of analytical procedures employed must be made available to attendees, either as an integral portion of an attachment to the agenda or minutes, or by reference to other documents that may reasonably be expected to be in the possession of MIL-HDBK-5 Meeting attendees. A specific example of the latter would be certain reports of Government-sponsored research or material evaluations for which distribution included the MIL-HDBK-5 attendance list. In some cases involving large quantities of supporting data, it may suffice (at the discretion of the Coordination Group) to furnish a single copy of these data to the Secretariat, from whom they would be available to interested attendees.

9.1.5 SYMBOLS AND DEFINITIONS (also see Sections 9.2.2, 9.3.4.2, 9.3.6.2, 9.4.1.2, 9.5.1.2, and 9.6).

α — Significance level; probability (risk) of erroneously rejecting the null hypothesis (see Section 9.6.2).

$\alpha_{99,90}$ — Shape parameter estimates for a T_{99} or T_{90} tolerance bound based on an assumed three-parameter Weibull distribution.

α_{50} — Shape parameter estimate for the Anderson-Darling goodness-of-fit test based on an assumed three-parameter Weibull distribution.

A — A-basis for mechanical property (see Section 9.2.2.1).

AD — Anderson-Darling test statistic, computed in goodness-of-fit tests for normality or Weibullness.

$\beta_{99,90}$ — Scale parameter estimate for a T_{99} or T_{90} tolerance bound based on an assumed three-parameter Weibull distribution.

β_{50} — Scale parameter estimate for the Anderson-Darling goodness-of-fit test based on an assumed three-parameter Weibull distribution.

B — B-basis for mechanical property (see Section 9.2.2.1).

df — Degrees of freedom.

F — The ratio of two sample variances.

heat — All material identifiable to a single molten metal source. (All material from a heat is considered to have the same composition. A heat may yield one or more ingots. A heat may be divided into several lots by subsequent processing.)

$k_{99,90}$ — The T_{99} or T_{90} tolerance limit factor for the normal distribution, based on 9 percent confidence and a sample of size n.

log — Base 10 logarithm.

lot — All material from a heat or single molten metal source of the same product type having the same thickness or configuration, and fabricated as a unit under the same conditions. If the material is heat treated, a lot is the above material processed through the required heat-treating operations as a unit.

ln — Natural (base e) logarithm.

n — Number of individual measurements or pairs of measurements; Ramberg-Osgood parameter.

r — Ratio of two paired measurements; rank of test point within a sample.

$\bar{r}$ — Average ratio of paired measurements.

S — S-basis for mechanical property values (see Section 9.2.2.1).

s — Estimated population standard deviation.

$\tau_{99,90}$ — Threshold estimates for a T_{99} or T_{90} tolerance bound based on an assumed three-parameter Weibull distribution.

τ_{50} — Threshold estimate for the Anderson-Darling goodness-of-fit test based on an assumed three-parameter Weibull distribution.

t — Tolerance factor for the "t" distribution with the specified "confidence" and appropriate degrees of freedom.

T_{90} — Statistically based lower tolerance bound for a mechanical property such that at least 90 percent of the population is expected to exceed T_{90} with 95 percent confidence.

T_{99} — Statistically based lower tolerance bound for a mechanical property such that at least 99 percent of the population is expected to exceed T_{99} with 95 percent confidence.

$V_{99,90}$ — The T_{99} or T_{90} tolerance limit factor for the three-parameter Weibull distribution, based on 95 percent confidence, a sample of size n, and a specified degree of upper tail censoring.

X_i — Value of an individual measurement.

$\bar{X}$ — Average value of individual measurements.

Σ — The sum of.

$'$ — Value determined by regression analysis.

9.1.6 DATA REQUIREMENTS FOR INCORPORATION OF A NEW PRODUCT INTO MIL-HDBK-5.—This section specifies requirements for the incorporation of a new product into MIL-HDBK-5 on an S-basis (see Section 9.2.2.1 for definition). These requirements are applicable to each alloy, product form, and heat treat condition or temper. Sections 9.1.6.2 through 9.1.6.7 delineate requirements for a test program for the determination of mechanical property data suitable for computation of derived properties (see Section 9.2.10). A test matrix, based on these requirements, is shown in Table 9.1.6.

9.1.6.1 *Material Specification.*—To be considered for inclusion in MIL-HDBK-5, a product must be covered by an industry specification (AMS specification issued by SAE Aerospace Materials Division or an ASTM standard published by the American Society for Testing and Materials), or a government specification (Military or Federal). If a public specification for the product is not available, action should be initiated to prepare a draft specification. Standard manufacturing procedures shall have been established for the fabrication and processing of production material before a draft specification is prepared. The draft specification shall describe a product which is commercially available on a production basis. An AMS draft specification should be submitted to the SAE Aerospace Materials Division and an ASTM standard should be transmitted to the American Society for Testing and Materials for publication. See Section 9.1.6.8 for requirements to substantiate the S-basis properties.

9.1.6.2 *Material.*—The product used for the determination of mechanical properties suitable for use in the determination of minimum design (derived) values for incorporation into MIL-HDBK-5 shall be production material. The material shall have been produced using production facilities and standard fabrication and processing procedures. If a test program to determine requisite mechanical properties is initiated before a public specification describing this product is available, precautionary measures shall be taken to ensure that the product supplied for the test program conforms to the specification, when published, and represents production material.

Ten lots of material from at least two production heats, casts or melts for each product form and heat treat condition shall be tested to determine required mechanical properties. See Table 9.1.6.2 for definitions of heat, cast, and melt. A lot is defined as all material of a specific chemical composition, heat treat condition or temper, and product form which has been processed at the same time through all processing operations. Different sizes and configurations from a heat cast or melt shall be considered different lots. For a single lot of material, only one heat treat lot may be used to meet the ten-lot requirement. Thicknesses of the 10 lots to be tested shall span the thickness range of the product form covered by the material specification (or for the thickness range for which design values are to be established).

Dimensionally discrepant castings or special test configurations may be used for the development of derived properties with prior approval by the MIL-HDBK-5 Coordination Group, providing these castings meet the requirements of the applicable material specification. Design values for separately cast test specimens shall not be presented in MIL-HDBK-5.

9.1.6.3 *Test Specimens.*—Mechanical property ratios are utilized in the analysis of data to determine minimum design values. Tensile yield in other than primary test direction, compressive yield, and bearing yield strengths are paired with the tensile yield strength in the primary test direction for each lot. Tensile ultimate in other than the primary test direction, shear ultimate, and bearing ultimate strengths are paired with the tensile ultimate strength in the primary test direction. See Table 9.2.10 for the primary testing direction for various products. Therefore, it is imperative that these test specimens be taken from the same sheet, plate, bar, extrusion, forging, or casting. Test specimens shall be located in close proximity. If coupons or specimens are machined prior to heat treatment, all specimens representing a lot shall be heat treated simultaneously in the same heat treat load through all heat treating operations. This procedure is necessary to provide precise mechanical property relationships (ratios).

Test specimens shall be located within the cross section of the product in accordance with the applicable material specification, or applicable sampling specification, such as AMS 2355, AMS 2370, and AMS 2371. Subsize tensile and compressive test specimens may be used when appropriate.

TABLE 9.1.6. *Test Matrix to Provide Required Mechanical Property Data for Determination of Design Values for Derived Properties (on S-Basis)*

Lot Number[a,b,c]	Test Specimen Requirements												
	TUS & TYS[d,e,f,g]			CYS[d,e,g]			SUS[k]			BUS & BYS[j], e/D = 1.5		BUS & BYS[j], e/D = 2.0	
	L	LT	ST[h]	L	LT	ST[h]	L	LT	ST[h]	L	LT[h]	L	LT[h]
A	2[i]	2	2	2	2	2	2	2	2	2	2	2	2
B	2	2	2	2	2	2	2	2	2	2	2	2	2
C	2	2	2	2	2	2	2	2	2	2	2	2	2
D	2	2	2	2	2	2	2	2	2	2	2	2	2
E	2	2	2	2	2	2	2	2	2	2	2	2	2
F	2	2	2	2	2	2	2	2	2	2	2	2	2
G	2	2	2	2	2	2	2	2	2	2	2	2	2
H	2	2	2	2	2	2	2	2	2	2	2	2	2
I	2	2	2	2	2	2	2	2	2	2	2	2	2
J	2	2	2	2	2	2	2	2	2	2	2	2	2

[a] Ten lots, representing at least two production heats, or casts or melts, are required.
[b] Thicknesses of ten lots shall span thickness range of product form covered by material specification.
[c] For a single lot, multiple heat treat lots shall not be used to meet 10-lot requirement.
[d] If precision modulus values for E and E_c are not available, precision modulus tests should be conducted on three lots.
[e] Stress-strain data from at least three lots shall be submitted.
[f] Full-range tensile stress-strain data from at least one lot shall be submitted, but data from three or more lots are preferred.
[g] Products should also be tested in the 45° grain direction that are anticipated to have significantly different properties in this direction than the standard grain directions; these include materials such as aluminum-lithium alloys and Aramid fiber reinforced sheet laminate.
[h] As applicable, depending on product form and size.
[i] At least two specimens are recommended; however, a single test is acceptable if retesting can be accomplished to replace invalid tests.
[j] It is recommended that minimum sheet and strip selected for bearing tests comply with the t/D ratio (0.25-0.50) specified in ASTM E238. For failure modes, see Figure 9.4.1.7.2.
[k] It is recommended that sheet and strip ≥0.050 inch in thickness be selected for shear tests conducted according to ASTM B831. Shear testing of sheet <0.050 inch in thickness may result in invalid results due to buckling around the pin hole areas during testing.

TABLE 9.1.6.2. *Definitions of Heat, Melt, and Cast*

Material	Heat, Melt, or Cast
Ingot Metallurgy Wrought Products Excluding Aluminum Alloys	A heat is material which, in the case of batch melting, is cast at the same time from the same furnace and is identified with the same heat number; or, in the case of continuous melting, is poured without interruption.
Ingot Metallurgy Wrought Aluminum Alloy Products	A cast consists of the sequential aluminum ingots which are melted from a single furnace change and poured in one or more drops without changes in the processing parameters. (The cast number is for internal identification and is not reported.)
Powder Metallurgy Wrought Products Including Metal-Matrix Composites	A heat is a consolidated (vacuum hot pressed) billet having a distinct chemical composition.
Cast Alloy Products Including Metal-Matrix Composites	A melt is a single homogeneous batch of molten metal for which all processing has been completed and the temperature has been adjusted and made ready to pour castings. (For metal-matrix composites, the molten metal includes unmelted reinforcements such as particles, fibers, or whiskers.)

Test specimens shall be excised in longitudinal, long transverse, and short transverse (when applicable) grain directions. Mechanical properties shall also be obtained in the 45° grain direction for materials that are anticipated to have significantly different properties in this direction than the standard grain directions. For some product configurations, it may be impractical to obtain transverse bearing specimens. For aluminum die forging, the transverse grain direction by definition includes all orientations not within 15 degrees of parallel to grain flow; consequently, only longitudinal and short transverse, as applicable, tests shall be conducted.

Triplicate test specimens are preferred. Single test specimens may be acceptable for some products providing retesting can be performed when needed. Duplicate specimens are recommended as an economical compromise. Some variation in strength within a product is expected. The use of replicate specimens provides multiple mechanical property observations so that lot averages can be used to form paired mechanical property ratios. Mechanical property ratios formed from lot averages are more reliable than those formed from individual observations.

9.1.6.4 *Test Procedures.*—All tests shall be performed in accordance with applicable ASTM specifications. The pin shear testing of aluminum alloys is covered by ASTM B 769. Grain orientations and loading directions for shear specimens are also specified in ASTM B 769. Published shear testing standards are not available for aluminum alloy sheet, strip, or thin extrusions or for products from other alloy systems. Bearing tests for products from all alloy systems shall be conducted in accordance with ASTM E 238 using "clean pin" test procedures. For aluminum alloy plate, bearing specimens are oriented flatwise and for aluminum alloy die and hand forgings, bearing specimens are oriented edgewise, as described in Section 3.1.2.1.1.

9.1.6.5 *Mechanical Properties.*—Tensile, compression, shear, and bearing tests shall be conducted at room temperature to determine tensile yield and ultimate strengths, compressive yield strength, shear ultimate strength, and bearing yield and ultimate strengths for e/D = 1.5 and e/D = 2.0 for each grain direction and each lot of material. All data shall be identified by lot, or heat, or melt. For materials used exclusively in high temperature applications, such as gas turbine or rocket engines, the determination of design values for compression, shear, and bearing strengths may be waived by the MIL-HDBK-5 Coordination Group. In lieu of data for these properties, sufficient elevated temperature data for tensile yield and ultimate strengths, as well as modulus of elasticity, shall be submitted so that elevated temperature curves can be constructed. Data should be submitted for the useful temperature range of the product. See Section 9.3.1.1.1 for data requirements for elevated temperature curves.

9.1.6.6 *Modulus of Elasticity Data.*—Tensile and compressive modulus of elasticity values shall be determined for at least three lots material. Elastic modulus values are those obtained using a Class B-1 or better extensometer. The method of determining or verifying the classification of extensometers is identified in ASTM E 83. ASTM E 111 is the standard test method for the determination of Young's Modulus, tangent modulus, and chord modulus of structural materials. A modulus value shall also be obtained for the 45 degree grain orientation for materials that are anticipated to have significantly different properties in this direction than the standard grain directions.

9.1.6.7 *Other Data.*—Room temperature, tensile, and compressive load-deformation curves or stress-strain data for each grain direction from at least three lots shall be provided. Room temperature, full-range, tensile load deformation curves or stress-strain data for each grain direction shall also be provided. Full-range stress-strain data shall be provided for at least one lot, but data for three lots are preferable. For heat resistant materials for which elevated temperature data for tensile yield and ultimate strengths are required, room and elevated temperature stress-strain data shall be provided. A precise density value in pounds per cubic inch shall be provided. Although not required, physical property data for coefficient of expansion, thermal conductivity, and specific heat should be submitted, when available. Also, information regarding manufacturing (fabrication and processing), environmental effects (corrosion resistance),

heat treat condition and applicable specification shall be provided so that a comments and properties section can be prepared. Also, data, if available, for creep, stress rupture, fatigue crack propagation, fatigue, and fracture toughness properties should be submitted.

9.1.6.8 *Guideline Requirements For Specification Minimum Design Mechanical Properties* (S-basis) — A product must be covered by an industry specification prior to being considered for inclusion into MIL-HDBK-5 as indicated in 9.1.6.1. Within a specification, one of the basic requirements is to provide minimum properties (S-basis) which includes tension yield, tension ultimate, elongation and compression yield (when specified). As indicated in Section 9.2.2, the statistical significance to the S-basis properties is typically not known. However, it is known that minimum mechanical properties in the SAE/AMS specifications have been statistically justified in recent years (since ~ 1975) with a procedure contained in their documents. With that in mind, a procedure has been established to provide some level of statistical significance to these S-basis properties contained within the handbook.

A material being submitted for inclusion into MIL-HDBK-5 shall include as part of the substantiation package the basis of the specification properties. This substantiation package should include the number of test samples, the number of lots, and the method of determining any property covered in the specification even if it is not to be reported in MIL-HDBK-5. This could include the development of minimum as well as maximum properties. Consideration must be made for the specified sizes, product forms, heat treatments and other variables affecting the physical and mechanical properties. It is also expected that the test material chemistry be in the nominal specification range and not tailored to the chemistry extremes.

It is recommended that the substantiation be based on a procedure similar to SAE/AMS in which the analysis of data or other appropriate documentation supports a statistical S-basis value where at least 99 percent of the population of values is expected to equal or exceed the minimum value with a confidence of 95 percent. Since only limited quantities of data are generally available for the basic mechanical properties (tension yield, tension ultimate, compression yield), it is recommended that at least 30 test samples from at least one heat or lot of material are provided for each thickness range or product form. The S-basis value may be computed by assuming the distribution of the sample population to be normal and using the following equation

$$\text{Minimum S} = \bar{X} - s \cdot k_A$$

where

$\bar{X}$ = sample mean
s = standard deviation
k_A = one-sided tolerance-limit factor corresponding to a proportion at least 0.99 of a normal distribution and a confidence coefficient of 0.95 based on the number of specimens (See Table 9.6.4.1).

When the tensile and compressive properties vary significantly with thickness, regression analysis should be used.

Although the establishment of an S-basis value should be based upon the statistically computed value, the S-basis value may be slightly lower, based on experience and judgement, to insure conservative values.

9.1.7 PROCEDURE FOR THE SUBMISSION OF MECHANICAL PROPERTY DATA.—This section specifies the procedure for submission of mechanical property data for statistical analysis; specifically data supplied for the determination of A and B-basis values for F_{tu} and F_{ty} and for data supplied to obtain derived property values for F_{cy}, F_{su}, F_{bru} and F_{bry}. The amount of data to be supplied for both of

these are indicated in other sections of Chapter 9, such as Table 9.1.6 for derived property values. This section covers the format to submit the data in electronic form.

9.1.7.1 *Computer Software.*—The data can be supplied on 3.5 or 5.25 inch disks for PC format or on 3.5 inch disks for Macintosh format. It is recommended that the software applications in Table 9.1.7.1 be used to construct the data files. Along with the floppy disk, provide a hard (paper) copy of the data contained on the disk and any other supporting documentation such as specimen dimensions, gage length etc. This information will be stored in the MIL-HDBK-5 archives for future reference.

TABLE 9.1.7.1. *Software Applications for Data Submission*

ASCII text editor
Current Spreadsheet or Database Applications
- The Chairman or Secretary of MIL-HDBK-5 can be contacted concerning software compatibility questions.

The data supplied on these disks are to be supplied in English units. For example, physical dimensions should be reported in units of inches to the nearest thousandth of an inch (X.XXX), stress should be reported in units of ksi to the nearest one hundredth of a ksi (X.XX), strain is to be reported in percent to the nearest tenth of a percent (X.X) and modulus is to be reported in units of msi to the nearest tenth of a msi (X.X). If necessary, refer to Table 1.2.2 to convert to English units of measure.

9.1.7.2 *General Data Format.*— Tables 9.1.7.2(a) and (b), for wrought and cast products respectively, show the information that should be supplied in electronic form along with the mechanical test results. The columns (or data fields), in order, will contain alloy type, specification number, temper/heat treatment, lot and/or heat number, product form, product thickness, specimen location, grain direction, and specimen number. Columns will be added towards the right of the specimen number and will contain the individual test results as discussed in Sections 9.1.7.3 and 9.1.7.4.

When specifying grain direction for wrought products, use the conventions identified in Table 9.1.6: L for longitudinal, LT for long transverse, and ST for short transverse. Products that are anticipated to have significantly different properties in directions other than those stated above should be tested in the appropriate directions and the results reported.

There are several types of product forms identified in the Handbook; therefore, the term product form should be properly defined and reported in this column. Examples for wrought products are sheet, plate, bar, and forging. Examples for cast products are sand casting, investment casting, and permanent mold casting. For cast products it is important to identify if it is from a designated or nondesignated area of the casting.

9.1.7.3 *Data Format for the Determination of A and B-Basis Values of F_{tu} and F_{ty}.*—The tensile test results that are to be reported for determination of A and B-basis properties are tensile ultimate strength (TUS), tensile yield strength (TYS) elongation (e) reduction of area (RA) and modulus. The results of these tests are to be reported as shown in Table 9.1.7.3 along with alloy designation, specification, lot and/or heat number, product thickness, grain direction, etc. as previously shown in Table 9.1.7.2. The number of tests required for determining A and B-basis properties are identified in Section 9.2.

9.1.7.4 *Data Format for Derived Property Values.*—For the derived property values, several types of tests may be conducted such as tensile, compression, shear and bearing, as shown in Table 9.1.6. The results of these tests are to be reported as shown in Table 9.1.7.4 along with alloy designation, specification, lot and/or heat number, product thickness, grain direction, etc. as previously shown in Table 9.1.7.2.

The ultimate strength properties are to be contained in one file as shown in Table 9.1.7.4(a) while the yield strength properties are to be contained in another file as shown in Table 9.1.7.4(b).

Generally, two tests are preferred (one required) for a given test type and product thickness. The results of these tests are to be reported in columns adjacent to each other. For example, TUS Test #1 and TUS Test #2 are on the same row for a given thickness and heat. An additional column should be created to report the specimen number for the second test. This column should be just to the left of the test result. The same procedure is to be used for the other properties. The abbreviations (see Section 1.2.2) for the other test types are CYS for compressive yield, SUS for ultimate shear, and BUS and BYS for ultimate and yield bearing strengths, respectively. For the bearing properties, also identify the e/D ratio of either 1.5 or 2.0.

9.1.7.5 *Data Format for the Construction of Typical Stress-Strain Curves.*—The tensile and compression stress-strain data should also be submitted in electronic form, if possible, so that typical tensile and compression stress strain curves, compression tangent modulus and typical tensile (full-range) curves can be constructed. In order to construct a typical stress-strain curve, the individual specimen curves must be documented up to slightly beyond the 0.2 percent offset yield strength. To construct a typical (full range) stress-strain curve, the individual curves must be documented through to failure.

The data for the stress-strain curves must be supplied on a separate floppy disk from the mechanical property data. The data should be stored in a file which contains the load (or stress) in the first column and the displacement (or strain) in the second column. Each stress-strain pair should be identified with its corresponding specimen identification number.

For the load-displacement curves, the load should be reported in pounds (X.) and the displacement should be reported in units of inches (X.XXX). For stress-strain curves, the stress should be reported to the nearest hundredth of a ksi (X.XX) and strain should be reported to the nearest X.XX $x10^{-6}$ units.

A hard copy of the load displacement curve should also be submitted for each curve.

TABLE 9.1.7.2(a) *General Data Format for Wrought Products*

Alloy Trade Name	Industry/-Government Specification Number	Temper/Heat Treatment	Lot and/or Heat No.	Product Form	Product Thickness (in), or Area (in^2)	Specimen Location	Grain Direction	Specimen Number

TABLE 9.1.7.2(b) *General Data Format for Cast Products*

Alloy Trade Name	Industry/-Government Specification No.	Temper/-Heat Treatment	Lot and/or Heat No.	Product Form	Product Thickness	Specimen Location (Designated, Nondesignated)	Specimen Number

TABLE 9.1.7.3 *Data Format for Determination of A and B-Basis Values of F_{tu} and F_{ty}*

Alloy Trade Name		Specimen No.	TUS ksi	TYS ksi	% E	% R	Elastic Modulus, msi
	The information to be entered between these two columns						
	columns depends upon the product form, see Table 9.1.7.2(a) or (b).						

TABLE 9.1.7.4(a) *Derived Ultimate Properties.*

Alloy Trade Name		Specimen No.	TUS Test 1	TUS Test 2*	SUS Test 1	SUS Test 2*	BUS e/D=1.5 Test 1	BUS e/D=1.5 Test 2*	BUS e/D-2.0 Test 1	BUS e/D=2.0 Test 2*
	The information to be entered between these two									
	columns depends upon the product form, see Table 9.1.7.2(a) or (b).									

* Two tests are preferred, only one is required.

TABLE 9.1.7.4(b) *Derived Yield Properties.*

Alloy Trade Name		Specimen No.	TYS Test 1	TYS Test 2*	CYS Test 1	CYS Test 2*	BYS e/D=1.5 Test 1	BYS e/D=1.5 Test 2*	BYS e/D-2.0 Test 1	BYS e/D=2.0 Test 2*
	The information to be entered between these two									
	columns depends upon the product form, see Table 9.1.7.2(a) or (b).									

* Two tests are preferred, only one is required.

9.2 Room-Temperature Design Properties

9.2.1 INTRODUCTION.—This section contains detailed procedures for the determination of room-temperature design properties.

9.2.2 DESIGNATIONS AND SYMBOLS.—Designations and Symbols presented in this section are applicable throughout the MIL-HDBK-5, but are particularly pertinent to computation and presentation of room-temperature mechanical properties.

9.2.2.1 *Data Basis.*—There are four types of room-temperature mechanical properties included in MIL-HDBK-5. They are listed here, in order, from the least statistical confidence to the highest statistical confidence, as follows:

Typical Basis.—A typical property value is an average value and has no statistical assurance associated with it.

S-Basis.—This designation represents the specification minimum value specified by the governing industry specification (as issued by standardization groups such as SAE Aerospace Materials Division, ASTM, etc.) or federal or military standards for the material. (See MIL-STD-970 for order of preference of specifications.) For certain products heat treated by the user (for example, steels hardened and tempered to a designated F_{tu}), the S-value may reflect a specified quality-control requirement. Statistical assurance associated with this value is not known.

B-Basis.—This designation indicates that at least 90 percent of the population of values is expected to equal or exceed the statistically calculated mechanical property value, with a confidence of 95 percent. This statistically calculated number is computed using the procedures specified in Section 9.2.

A-Basis.—The lower value of either a statistically calculated number, or the specification minimum (S-basis). The statistically calculated number indicates that at least 99 percent of the population is expected to equal or exceed the statistically calculated mechanical property value with a confidence of 95 percent. This statistically calculated number is computed using the procedures specified in Section 9.2.

Sections 9.2.5, 9.2.7.1, 9.2.8.1, and 9.2.9.1 contain discussions of data requirements for direct computation of design properties based on current process capability of the majority of suppliers of a given material and product form. To assure that the A- and B-values, defined above, represent true current process capability of a material, all available original test data for current material that is produced and supplied to the appropriate government, industry, or equivalent company specifications are included in calculating these values. (However, to be considered for inclusion in MIL-HDBK-5, a material must be covered by an industry, Federal, or Military specification per Section 9.1.6.) Only positive proof of improper processing or testing is cause for exclusion of original test data, except that the number of tests per lot shall not exceed the usual frequency of testing for the product. It is recognized, however, that extensive acceptance testing resulting in elimination of low-strength material from the population may justify establishment of higher mechanical-property values for the remaining material. Since this is a function of both the type of product and the nature and frequency of the acceptance tests practiced by each company, it is impractical to attempt to include these considerations in this document.

Usually, only tensile ultimate and yield strengths in a specified testing direction are determined in such a manner that they can be termed A- and B-values, in accordance with definitions given above. Only tensile ultimate strength, tensile yield strength, elongation, and reduction of area (for some alloys) are normally specified in the governing specifications and can be termed S-values. However, ratioing proce-

dures (described in Section 9.2.10) have been established, by which other property values such as compression, shear, and bearing are computed to have approximately the same assurance levels as A-, B-, or S-values for tensile ultimate and yield strength. Property values determined in this manner are presented as having the same data basis as tensile ultimate and yield strengths in the same column of the table.

Current practice regarding the use of the above data bases in the presentation of room-temperature design properties is as follows:

(1) Room-temperature design properties for tensile ultimate and yield strengths are presented on an A- and B- or S-basis. A-values that are higher than corresponding S-values are presented as footnotes in MIL-HDBK-5 property tables, and these A-values are not qualified for general use in design pending revision of specification requirements. However, A-values that are equal to or lower than corresponding S-values replace S-values in the document.

(2) The S-basis is used for elongation and reduction of area.

(3) If an A-value is presented for a strength property, the corresponding B-value is also presented.

(4) A- and B-values, when available, replace S-value entries, based upon item (1) conditions.

(5) A- and B-values, based upon data representing samples of material supplied in the annealed, solution treated, or as-fabricated conditions, which were heat treated to demonstrate response to heat treatment by suppliers, are incorporated into MIL-HDBK-5 with an explanatory footnote. It is recognized that structural fabrication and processing can alter mechanical properties. The use of A- and B-values for structural design requires consideration of such effects. These design values are derived from the statistically computed T_{99} and T_{90} values defined earlier.

(6) Strength at room temperature after thermal exposure is presented graphically as a percentage of the tabulated design property.

(7) Design data for all other properties, such as elastic modulus, Poisson's ratio, creep, fatigue, and physical properties, are presented on a typical basis unless indicated otherwise.

9.2.2.2 *Mechanical-Property Terms.*—Mechanical properties that are presented as room-temperature design properties are listed in Table 9.2.2.2. It is important that use of a subscripted, capital letter *"F"* should be limited to designation of minimum values. Its use to designate an individual test value can lead to confusion and should be avoided in MIL-HDBK-5 data proposals.

TABLE 9.2.2.2. *Mechanical Property Terms*

Property	Units	Symbol: Room-Temperature Minimum Value	Symbol: Individual or Typical Value
Tensile Ultimate Strength	ksi	F_{tu}	TUS
Tensile Yield Strength	ksi	F_{ty}	TYS
Compressive Yield Strength	ksi	F_{cy}	CYS
Shear Ultimate Strength	ksi	F_{su}	SUS
Shear Yield Strength*	ksi	F_{sy}	SYS
Bearing Ultimate Strength	ksi	F_{bru}	BUS
Bearing Yield Strength	ksi	F_{bry}	BYS
Elongation	percent	e	elong.
Total Strain at Failure*	percent	e_t	strain at failure
Reduction of Area	percent	RA	red. of area

*As applicable.

The absence of a directionality symbol implies that the property value is applicable to each of the grain directions when the product dimensions exceed approximately 2.5 inches.

The listed mechanical property symbols should be followed by one of the following additional symbols for wrought alloys, not castings.

L — Longitudinal direction; parallel to the principal direction of flow in a worked metal.

T — Transverse direction; perpendicular to the principal direction of flow in a worked metal; may be further defined as LT or ST.

LT — Long-transverse direction; the transverse direction having the largest dimension, often called the "width" direction.

ST — Short-transverse direction; the transverse direction having the smallest dimension, often called the "thickness" direction.

Values of F_{bru} and F_{bry} should indicate the appropriate edge distance/hole diameter (e/D) ratio. Design properties are presented for two such ratios: e/D = 1.5 and e/D = 2.0.

Data for use in establishing these properties should be based on ASTM standard testing practices. The test practice and any deviations therefrom should be reported when submitting proposals to the MIL-HDBK-5 Coordination Group for consideration.

9.2.2.3 *Statistical Terms.*—Proper use of the following statistical terms and equations will alleviate misunderstanding in the presentation of data analyses:

Population.—All potential measurements having certain independent characteristics in common, i.e., "all possible TUS(L) measurements for 17-7PH stainless steel sheet in TH1050 condition."

Sample.—A finite number of observations drawn from the population.

Sample mean.—Average of all observed values in the sample. It is an estimate of population mean. A mean is indicated by a bar over the symbol for the value observed. Thus, the mean of n observations of TUS would be expressed as:

$$\overline{TUS} = \frac{TUS_1 + TUS_2 + \ldots + TUS_n}{n} = \frac{\sum_{i=1}^{n} (TUS_i)}{n}$$

Sample variance.—The sum of the squared deviations, divided by n - 1, and, based on n observations of TUS, expressed as

$$s^2_{TUS} = \frac{\sum_{i=1}^{n} (TUS_i - \overline{TUS})^2}{n - 1} = \frac{n\sum_{i=1}^{n} (TUS_i)^2 - \left(\sum_{i=1}^{n} TUS_i\right)^2}{n(n - 1)}$$

Sample standard deviation.—An estimate of the population standard deviation; the square root of the sample variance, or

$$s_{TUS} = \sqrt{s^2_{TUS}}$$

Degrees of Freedom.—Number of degrees of freedom for n sample values is defined as that number minus the number of constraints. For example, the standard deviation calculation contains one fixed value (the mean); therefore, it has n - 1 degrees of freedom.

T_{99}.—At least 99 percent of the population of values is expected to equal or exceed this tolerance bound with a confidence of 95 percent.

T_{90}.—At least 90 percent of the population of values is expected to equal or exceed this tolerance bound with a confidence of 95 percent.

Probability.—Ratio of possible number of favorable events to total possible number of equally likely events. Probability, as related to design properties means that chances of a material-property measurement equaling or exceeding a certain value (the one-sided lower tolerance limit) is 99 percent in the case of a T_{99} value and 90 percent in the case of a T_{90} value.

Confidence.—A specified degree of certainty that at least a given proportion of all future measurements can be expected to equal or exceed the lower tolerance limit. Degree of certainty is referred to as the confidence coefficient. For MIL-HDBK-5, the confidence coefficient is 95 percent which, as related to tolerance bounds for design properties means that, in the long run over many future samples, 95 percent of conclusions regarding exceedance of T_{99} and T_{90} values would be true.

A and B-Values.—See Section 9.2.2.1.

9.2.3 COMPUTATIONAL PROCEDURES, GENERAL.—Procedures used to determine tolerance bounds for mechanical properties vary somewhat from one sample to another. All involve a number of steps that are best illustrated by the flowchart in Figure 9.2.3. These steps are summarized as follows:

(1) Specify the population to which the property applies
(2) Decide on the procedure for computing the property
(3) Compute the property.

These steps are described in greater detail in Sections 9.2.4 through 9.2.11, and a number of examples of the several procedures are presented in Section 9.2.12.

9.2.4 SPECIFYING THE POPULATION.—For computational purposes, definition of a population must be sufficiently restrictive to ensure that computed tolerance bounds for design properties are realistic and useful. This is done by establishing a range of products and test conditions for which a mechanical property can be characterized by a single statistical distribution. In most cases a homogeneous population of data for a measured test parameter should not include more than one alloy, heat-treated condition, or test temperature.

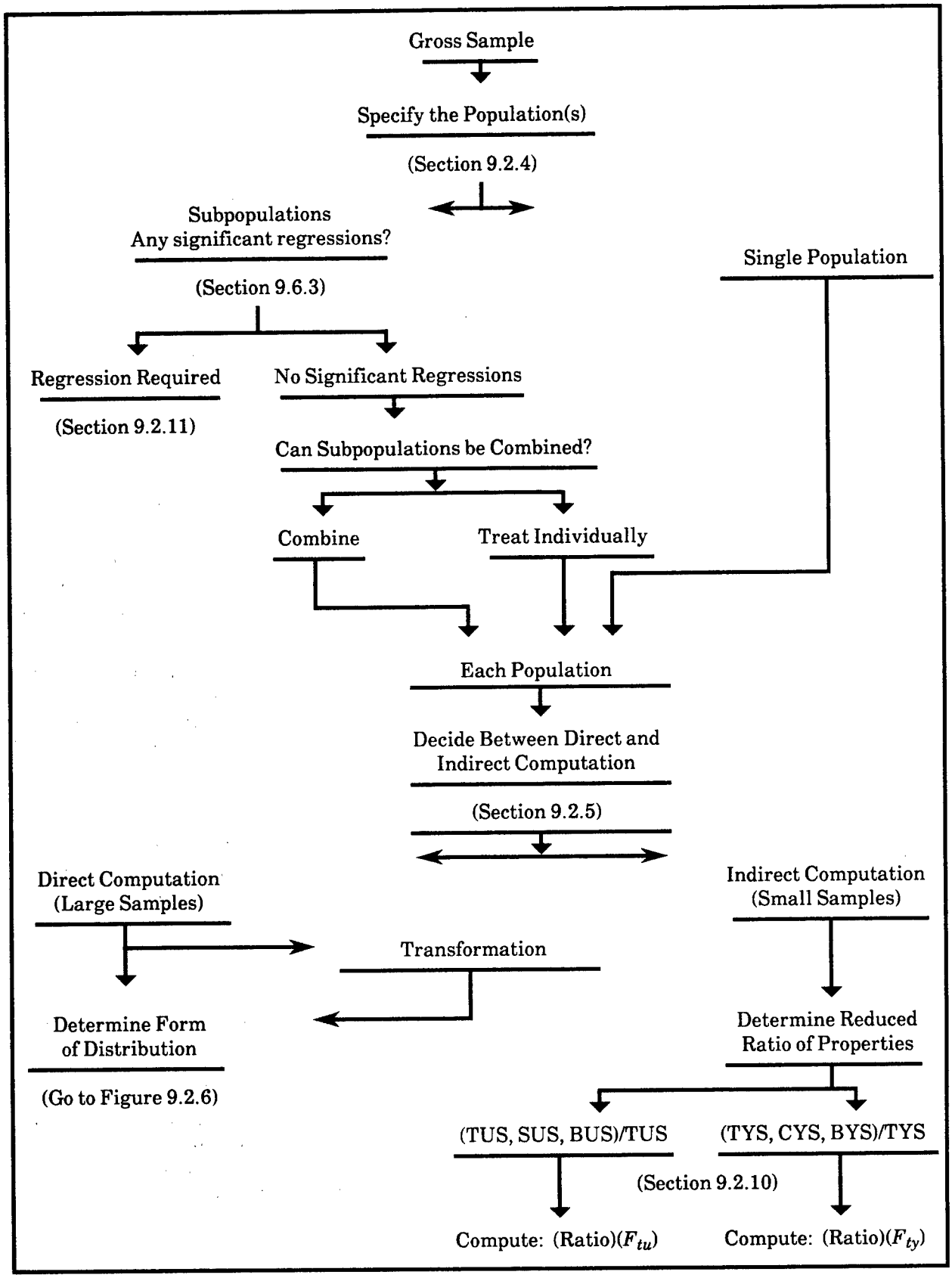


FIGURE 9.2.3. *General procedures for determining design allowables.*

It is not necessarily obvious whether such a population may include more than one product form or size, grain direction or processing history. Strip, plate, bars, and forgings of one alloy may have essentially the same TYS, while for another material the TYS may differ greatly among those product forms. To resolve these questions, appropriate statistical tests of significance should be applied to the respective groups of data. These tests are described in detail in Section 9.6, and Section 9.2.12 presents examples of their use in MIL-HDBK-5 data analyses.

The step-by-step procedure for specifying the population is illustrated in Figure 9.2.4 and described in Section 9.2.4.1. This procedure is used to determine whether several available data sets may be combined for the purpose of computing design allowables. The procedure is applicable to data collections for which regression analysis is required as well as those for which regression is not required. In the latter case, an acceptability test is employed to eliminate unacceptable data sets. This procedure is described in Section 9.2.4.2. A corresponding acceptability test would be desirable for the regression setting; however, such a procedure has not yet been developed.

9.2.4.1 *Specification Procedure.*—In most cases, these tests will provide a fairly clear-cut division between one population and another. For example, L and T properties either are or are not nearly identical. However, properties may sometimes vary continuously with some dimensional characteristic, such as thickness. It is necessary, therefore, to first test the data for the relationship between the property and the material dimension. Regression analysis procedures, which should be applied to each set of producer's data to determine if there is an effect due to a particular material dimension, are described in Section 9.6.3.

If any one of a group of data sets analyzed by regression shows a significant effect on properties due to selected material dimension, all regressions should be tested for equality to determine whether data sets may be combined and considered a homogeneous population. The procedure described in Section 9.6.3.3 should be used to perform this test.

If the regressions are accepted as equal, then A and B-allowables can be calculated one of two ways: (1) by regression; or (2) by dividing data into thickness ranges and calculating A and B-values for each range. If the regressions are not equal, A and B-allowables should be calculated separately for each data set and minimum A and B-values determined for all data sets should be reported.

If none of a group of data sets analyzed by regression show a significant effect due to the chosen material dimension, data from different data sets (e.g. different producers) should be tested for homogeneity using a k-sample Anderson-Darling test as described in Section 9.6.2.5. If data sets are found to be homogeneous, data should be pooled and A and B allowables should be calculated using the single combined data set. If data from the various producers constitute more than one population, the following procedure should be used.

(1) Data sets which do not comply with data requirements in Sections 9.2.6, 9.2.7, 9.2.8, or 9.2.9 should be excluded.

(2) Each remaining data set should be tested for acceptability using the three-parameter Weibull acceptability test described in Section 9.2.4.2. Any data sets which are found to be unacceptable should be excluded.

(3) All remaining data sets should be tested for homogeneity using the k-sample Anderson-Darling test. If data sets are found to be homogeneous, A and B-allowables can be calculated using a single combined data set. If populations are not homogeneous, allowables must be determined by calculating A and B-values for each data set.

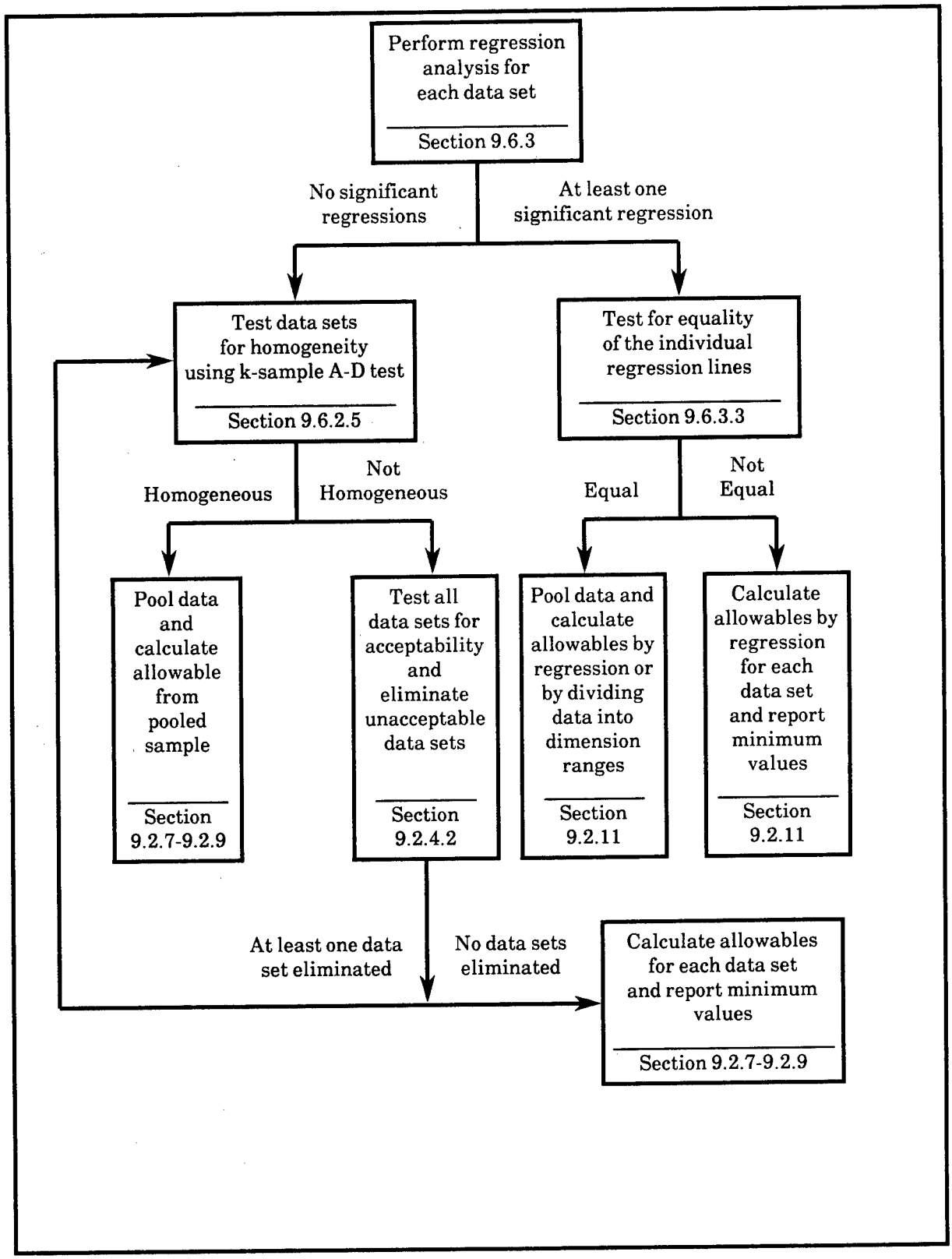


FIGURE 9.2.4. *General procedures for specifying the population and calculating design allowables.*

9.2.4.2 *Three-Parameter Weibull Acceptability Test.*—The three-parameter Weibull acceptability test is designed to determine whether an acceptable proportion of a producer's population is likely to exceed the specification limit for corresponding material property. To carry out this test, an upper confidence bound (UCB) is calculated for the first percentile of the producer's population assuming that the population is distributed according to a three-parameter Weibull distribution. This UCB value is calculated in the same manner as a T_{99} value is calculated (in Section 9.2.8) with the following modifications:

(1) In solving for the threshold $\tau(\theta)$ (Section 9.6.5.1), θ should be set equal to 0.90.

(2) The value of V_{99} should be taken from Table 9.6.4.7 rather than Table 9.6.4.8 when using the formula for T_{99} (equation [9.2.8.2,(e)]) to calculate the UCB value.

If UCB is greater than or equal to the specification limit, it is concluded that the producer's data is acceptable. If UCB is less than the specification limit, it is concluded (with a 5 percent risk of error) that the producer's data is unacceptable and should be excluded from the determination of properties.

In statistical terms, this method tests (at 5 percent significance level) the hypothesis that at least 99 percent of the producer's population is greater than the specification limit. If the hypothesis is not rejected (UCB greater than or equal to specification limit), then it is concluded that the producer's data is acceptable. If the hypothesis is rejected (UCB less than the specification limit), it is concluded that the producer's data is unacceptable.

This technique is applicable only when data have not been censored from the sample. It also assumes that the data are distributed according to a three-parameter Weibull distribution (although normally distributed data are also accommodated by this test). If the data sample is highly skewed, background data should be reviewed to determine whether the skewness is caused by a mixed population. If it is not, the Weibull test procedure can be applied. This test should be applied to both tensile yield and ultimate strengths (in appropriate grain directions), and if a producer's data is unacceptable for either property, that producer's data for both properties should be excluded for the purpose of computing T_{99} and T_{90} values.

9.2.5 DECIDING BETWEEN DIRECT AND INDIRECT COMPUTATION.—The only room-temperature design properties that are regularly determined by direct computation are F_{tu} and F_{ty}. This procedure is usually limited to a specified or usual testing direction because there are seldom enough data available to determine properties in other test directions. Two rules govern the choice between direct and indirect computation:

(1) F_{tu}, and F_{ty} in the specified or usual testing direction may be determined by direct computation only.

(2) F_{tu} and F_{ty} in other testing directions (as well as F_{cy}, F_{su}, F_{bru}, and F_{bry} in all directions) may be determined by direct computation only if (a) the data are adequate to determine the distribution form and reliable estimates of population parameters, or (b) the sample includes 300 or more individual, representative observations of the property to be determined.

For example, assume that available data for a relatively new alloy comprise 50 observations of TUS in the specified testing direction. This sample is not considered large enough to determine the distribution form and reliable estimates of population mean and standard deviation. Since only direct computation is permitted in this instance, determination of T_{99} and T_{90} values must be postponed until a larger sample is available. However, these properties may be considered for presentation on the S basis at the discretion of the MIL-HDBK-5 Coordination Group, contingent on availability of an acceptable procurement specification for the material.

If the number of observations increases to 100, this quantity may be adequate to allow determination of T_{99} and T_{90}-values, provided data can be described by a normal or Weibull distribution. If the distribution cannot be described parametrically, at least 299 observations are required so that computation can proceed without knowledge of the distributional form.

If the above example involved observations of SUS instead of TUS, the same criteria would apply for direct computation. However, F_{su} could be determined by indirect computation with as few as ten paired observations of SUS and TUS (representing at least ten lots and two heats), provided F_{tu} has been established.

9.2.6 DETERMINING THE APPROPRIATE COMPUTATION PROCEDURE.

9.2.6.1 *Background.*—Prior to 1984, lower tolerance bound mechanical properties (T_{99}, T_{90}) were established by one of two methods. If the sample population was found to be normally distributed by a chi-square test, then standard normal distribution computation procedures were used. Otherwise, nonparametric procedures were used.

In 1984, use of the normal distribution was replaced by use of the three-parameter Weibull distribution to accommodate skewness in many of the materials' properties. In addition, the chi-square test was replaced by the more sensitive Anderson-Darling goodness-of-fit test. Because the Anderson-Darling test is especially sensitive to departures in the tails from the candidate distribution (the very high and very low observations) in many situations, the Weibull distribution is often rejected, even when the model fit (by a probability plot) appears adequate in the lower values.

To permit computation of lower tolerance bound in more of these cases, the Weibull approach was expanded to incorporate two different levels of upper-tail censoring and a last-resort conservative "back-off" option. Also, a modified version of the A-D test was developed which places more emphasis on the lower tail than the upper tail. In addition, because methods based on the normal distribution have intuitive appeal and are less computationally burdensome, a normal-based approach is now permitted. This method is an adjusted version of the previously used normal method which was developed to protect against anticonservatism due to undetected skewness. These methods were incorporated into the guidelines in 1995.

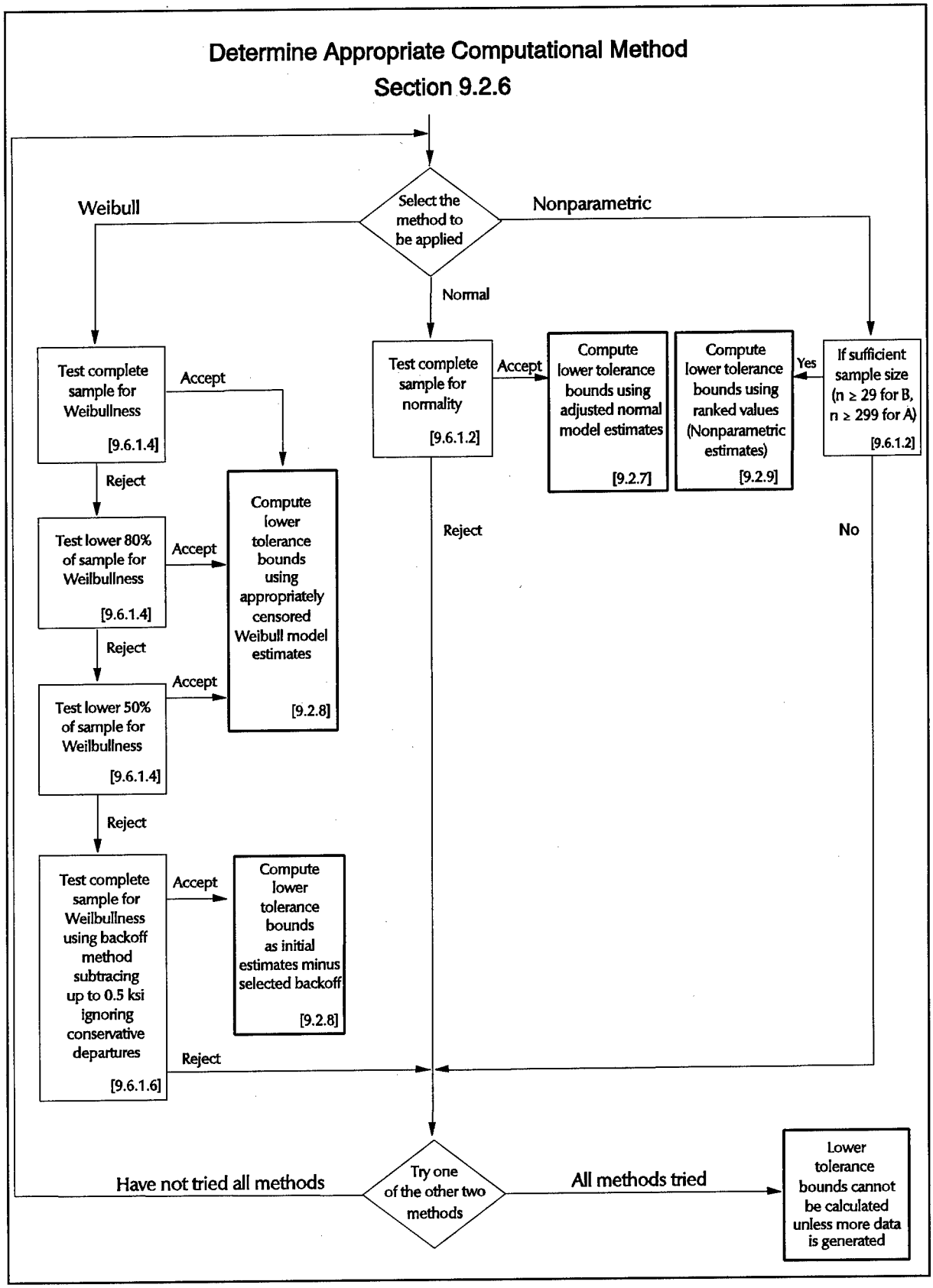
9.2.6.2 *Computation Procedures.*—Current analysis procedures are defined in Figure 9.2.6. Three methods are permitted for the computation of the lower tolerance bounds (T_{99}, T_{90}) sequential Weibull procedure, adjusted normal procedure, and nonparametric procedure. The sequential Weibull procedure is preferred, and will be applicable much more frequently than the adjusted normal procedure. In addition, if more than one method can be applied, the sequential Weibull procedure will in most cases provide a higher lower tolerance bound.

In what follows, certain procedures require artificial censoring of the measured data. That is, because the real engineering interest for design lies in lower percentiles of the distribution of a material's properties, some of the following procedures ignore a portion of the observations in the upper tail. Specifically, we use the notation $X_{(1)} \leq X_{(2)} \leq \ldots \leq X_{(n)}$ to denote the ordered sample, and will frequently refer to the censored sample:

$$X_{(1)} \leq X_{(2)} \leq \ldots \leq X_{(r)},$$

where r/n represents the proportion of the sample which is uncensored. Alternatively, (1-r/n) represents the proportion of the sample which is censored. The terms r and n will be used throughout subsequent sections without redefinition. In the case of uncensored data, r=n.

When the sequential Weibull procedure is applied, the first step is to perform a modified Anderson-Darling goodness-of-fit-test as described in 9.6.1.4 for the uncensored sample. If the assumption of Weibullness is not rejected, the lower tolerance bound should be computed using methods described in Section 9.2.8 for complete samples. (The risk that one may conclude erroneously that a true Weibull


Determine Appropriate Computational Method
Section 9.2.6
Select the method to be applied
Weibull
Nonparametric
Normal
Test complete sample for Weibullness [9.6.1.4]
Accept
Reject
Test lower 80% of sample for Weilbullness [9.6.1.4]
Accept
Reject
Test lower 50% of sample for Weilbullness [9.6.1.4]
Accept
Reject
Test complete sample for Weilbullness using backoff method subtracing up to 0.5 ksi ignoring conservative departures [9.6.1.6]
Accept
Reject
Compute lower tolerance bounds using appropriately censored Weibull model estimates [9.2.8]
Compute lower tolerance bounds as initial estimates minus selected backoff [9.2.8]
Test complete sample for normality [9.6.1.2]
Accept
Reject
Compute lower tolerance bounds using adjusted normal model estimates [9.2.7]
Compute lower tolerance bounds using ranked values (Nonparametric estimates) [9.2.9]
Yes
If sufficient sample size (n ≥ 29 for B, n ≥ 299 for A) [9.6.1.2]
No
Try one of the other two methods
Have not tried all methods
All methods tried
Lower tolerance bounds cannot be calculated unless more data is generated

distribution is non-Weibull is set at 5 percent.) If the assumption of Weibullness is rejected for the complete sample, then the next step is to test the lower 80 percent of the data for Weibullness by trimming the top 20 percent of the measurements and applying a censored version of the Anderson-Darling test. Use the version of the test described in Section 9.6.1.4 for 20 percent censoring is used. If this test is not rejected, then the lower tolerance bounds should be computed using the methods described in 9.2.8 for 20 percent censoring. If the assumption of Weibullness is rejected here, then 50 percent censoring should be attempted, in the same manner as described for 20 percent censoring.

If the Weibull model is still rejected with 50 percent censoring, then a last resort conservative method should be attempted. This method decreases the initial Weibull threshold estimate while holding the shape and scale parameters constant, until the percentiles of the resulting model are sufficiently less than the sample percentiles. To avoid accepting an extremely inadequate fit, the decrease is limited to 0.5 ksi.

Section 9.6.1.6 describes the method for identifying a proper backoff (the decrease from the initial Weibull threshold estimate), denoted by $\tau_{backoff}$, for this method. If the appropriate backoff is less than or equal to 0.5 ksi, the lower tolerance bounds should be calculated by first computing bounds based on the complete sample as specified in Section 9.2.8, and then subtracting the $\tau_{backoff}$ value. If an appropriate backoff less than or equal to 0.5 ksi is not identified, then the nonparametric procedures described in 9.2.9, or the adjusted normal procedure described in Section 9.2.7 should be considered.

If the adjusted normal analysis procedure is applied, the first step is to perform an Anderson-Darling goodness-of-fit test for normality as described in Section 9.6.1.2. If the assumption of normality is not rejected, the lower tolerance bounds may be computed using the methods described in Section 9.2.7. If the assumption of normality is rejected, the sequential Weibull procedures described in Section 9.2.8 or the nonparametric procedure described in Section 9.2.9 should be considered.

In those cases where sufficient data is available, one may choose to calculate the lower tolerance bounds by the nonparametric procedure. A T_{99} bound requires 299 data values and a T_{90} bound requires 29 data values. The nonparametric procedure is described in Section 9.2.9. If the sample size is too small for the nonparametric method, the sequential Weibull procedures described in Section 9.2.8 or the adjusted normal procedures described in Section 9.2.7 should be considered.

In those cases where sample sizes are insufficient to apply the nonparametric method, and the goodness-of-fit tests will not allow application of the sequential Weibull or adjusted normal procedures, the lower tolerance bounds cannot be calculated.

9.2.7 DIRECT COMPUTATION FOR THE NORMAL DISTRIBUTION.—This procedure should be used when a lower tolerance bound (T_{99}, T_{90}) is to be computed directly (not paired with another property for computational purposes) and the population may be interpreted to signify either the property measured (TUS, etc.) or some transformation of the measured value that is normally distributed. This procedure is applicable to F_{tu} and F_{ty}. It may also be used for F_{cy}, F_{su}, F_{bru}, and F_{bry} if sufficient quantity of data is available.

9.2.7.1 *Data Requirements.*—Direct calculation of T_{99} and T_{90} values requires adequate data to determine (1) the form of distribution and (2) reliable estimates of the population mean and standard deviation. Prior experience with the material under consideration will help in determining sample size requirements. For a material, each population should be represented by a sample containing at least 100 observations. The sample should include multiple lots, representing at least ten production heats, casts, or melts, from a majority of important producers. See Section 9.1.6.2 for definitions of lot, heat, cast, and melt. The sample should be distributed somewhat evenly over the size range applicable to the tolerance bound for the mecahnical property. In order to avoid an undesirable biasing of the sample in favor of lots represented by more observations than other lots, the number of observations from each lot must be nearly equal.

Grouped data may be "ungrouped" and analyzed as described below, if grouped data are reported in intervals of 1 ksi or less. The uniform smoothing method for ungrouping grouped data should be used. For the uniform smoothing method, observations in an interval are spread uniformly over that interval. The ith observation in an interval is set equal to

$$a_i = L + \frac{i}{n+1}(U - L) \qquad i = 1,2,\ldots,n$$

where

n = the number of observations in the interval
L = the lower end point of the interval
U = the upper end point of the interval.

9.2.7.2 *Computational Procedure.*—To compute the lower tolerance bounds for a normally distributed population, it is necessary to have (1) estimates of the mean and standard deviation of this population and (2) tables of one-sided* tolerance-limit factors for the normal distribution. Means and standard deviations are computed from samples drawn from the population by a random process. Equations for computing the mean and standard deviation are presented in Section 9.2.2.3. One-sided tolerance-limit factors for the normal distribution are tabulated as functions of sample size, population proportion covered by the tolerance interval, and confidence coefficients. Tolerance-limit factors are presented in Table 9.6.4.1.

With a suitable sample of size, n, computation of the lower tolerance bounds is carried out by the use of the following formulas:

$$T_{99} = \overline{X} - (k_A - 0.0855 - 1.203q_{LB} + 2.858/n^{1/2})\, s, \qquad [9.2.7.2(a)]$$

$$T_{90} = \overline{X} - (k_B + 0.0338 - 0.202q_{LB})\, s, \qquad [9.2.7.2(b)]$$

where

$\overline{X}$ = sample mean based on n observations
s = sample standard deviation
k_A = one-sided tolerance-limit factor corresponding to a proportion at least 0.99 of a normal distribution and a confidence coefficient of 0.95
k_B = one-sided tolerance-limit factor corresponding to a proportion at least 0.90 of a normal distribution and a confidence coefficient of 0.95

*At this point it is appropriate to distinguish between "one-sided" and "two-sided" tolerance factors, both of which are used in various stages of MIL-HDBK-5 analyses. A one-sided factor is used to establish a limit, above or below which it is predicted that at least some percentage of the values lie. A two-sided factor is used to establish an interval or range within which it is predicted that at least some percentage of the values lie. In both instances, a confidence is specified for the prediction. Thus, in determining an T_{99} value, one predicts, with 0.95 confidence, that at least 0.99 of the values in the population lie above the T_{99} value, and a one-sided tolerance factor is used in the prediction. See References 9.2.7.2(a) through (d).

q_{LB} = lower bound on skewness defined as

$$q_{LB} = \frac{q - \left[\frac{6n(n-1)}{(n-2)(n+1)(n+3)}\right]^{1/2}}{\left[\frac{n-2}{(n(n-1))^{1/2}}\right]}$$

q = sample skewness, defined as

$$q = \frac{n^2}{(n-1)^3}\frac{\sum_{i=1}^{n}(x_i-\bar{x})^3}{s^3}.$$

The quantities added to the tolerance-limit factors k_A and k_B, represent adjustments which were determined empirically to protect against anticonservatism even in the case of moderate negative skewness. Skewness is not easy to detect, and negative skewness in the underlying distribution can cause severely anticonservative estimates when using the normal model, even when the Anderson-Darling goodness-of-fit-test is used to filter samples. These adjustments help to ensure that the lower tolerance bounds computed maintain a confidence level near 95 percent for underlying skewness as low as -1.0. For higher skewness, the procedure will produce significantly greater coverage.

If the variable that is normally distributed represents a transformation of the mechanical property, the lower tolerance bounds (T_{99}, T_{90}) computed by the above formulas must be transformed back to the original units in which the mechanical property is conventionally reported. When the computed T_{99} or T_{90} value results in a fractional number, the mechanical property value used in the room temperature tables is determined by rounding. Fractions greater than 0.75 usually are raised to the next larger integer while lesser decimal fractions are disregarded. However, the rounded T_{99} value is replaced in the mechanical properties tables with the S value if the S value is known. In that case the rounded T_{99} value is included in a footnote.

9.2.8 DIRECT COMPUTATION FOR THE WEIBULL DISTRIBUTION.—This procedure should be used when a mechanical property value is to be computed directly (not paired with another property for computational purposes) and the population may be interpreted to signify either the property measured (TUS, etc.) or some transformation of the measured value that follows a three-parameter Weibull distribution. This procedure is applicable to F_{tu} and F_{ty}. It may also be used for F_{cy}, F_{su}, F_{bru}, and F_{bry} if a sufficient quantity of data is available.

9.2.8.1 *Data Requirements.*—Direct calculation of the lower tolerance bounds (T_{99}, T_{90}) requires adequate data to determine (1) form of the distribution and (2) reliable estimates of population threshold, shape, and scale parameters. Prior experience with the material under consideration will help determining sample size requirements. For a material, each population should be represented by a sample containing at least 100 observations that are distributed (parametrically) according to a three-parameter Weibull distribution. The sample should include multiple lots, representing at least ten production heats, from a majority of important producers. The sample should be distributed somewhat evenly over the size range applicable to the property. In order to avoid an undesirable biasing of the sample in favor of lots represented by more observations than other lots, the number of observations from each lot must be nearly equal.

Grouped data may be "ungrouped" and analyzed as described below, if grouped data are reported in intervals of 1 ksi or less. The uniform smoothing method for ungrouping grouped data should be used.

For the uniform smoothing method, observations in an interval are spread uniformly over that interval. The ith observation in an interval is set equal to

$$a_i = L + \frac{i}{n+1}(U - L) \qquad i = 1,2,\ldots,n$$

where n = the number of observations in the interval
L = the lower end point of the interval
U = the upper end point of the interval.

9.2.8.2. *Computational Procedures.*—In order to compute the lower tolerance bounds for a three-parameter Weibull population, it is necessary to have (1) an estimate of population threshold, (2) estimates of population shape and scale parameters, and (3) tables of one-sided tolerance limit factors for the three-parameter Weibull distribution. The method for estimating the population threshold based on complete or censored data (20 or 50 percent censoring) is presented in Section 9.6.5.1, and Section 9.6.5.2 contains the method for estimating population shape and scale parameters. A tabulation of tolerance limit factors by sample size, censoring level, and population proportion covered by the tolerance interval is presented in Table 9.6.4.8. For further information on these procedures and tabled values, see References 9.2.8(a) and 9.2.8(b).

The first step in calculating the lower tolerance bounds for a three-parameter Weibull population is to obtain an estimate of population threshold for each mechanical property. These threshold estimates will be denoted by τ_A and τ_B. The population threshold is theoretically the minimum achievable value for the property being measured. However, the real population is being empirically modeled by some Weibull population with a threshold. Since this empirical model is not perfect, there may be a small percentage of observations in the population that fall below the model threshold.

With a suitable sample of size n, population threshold estimates are obtained as follows. Let $X_1,\ldots,X_n$ denote sample observations in any order and let $X_{(1)},\ldots,X_{(n)}$ denote sample observations ordered from smallest to largest. In computing tolerance bounds, a lower confidence bound estimate of the threshold is used. The appropriate confidence level to use for the threshold depends on the censoring level and the tolerance bound being computed (A or B). In what follows, p represents the proportion of the sample that is censored. The appropriate confidence levels for threshold in computing the lower tolerance bounds are given by θ_A and θ_B, defined as

$$\theta_A = 1/[1 + \exp(M_A)]$$

and

$$\theta_B = 1/[1 + \exp(M_B)]$$

where

$$EfuncM_A = 1.778 + 2.748/\sqrt{n} + p\,(7.051/\sqrt{n} - 1.253)$$

and

$$M_B = 0.425 + 8.127/\sqrt{n} - 0.741\ p.$$

Using the computation procedure outlined in Section 9.6.5.1, calculate $\tau_A = \tau(\theta_A)$ and $\tau_B = \tau(\theta_B)$.

The second step in calculating mechanical properties for a three-parameter Weibull population is to obtain estimates of population shape and scale parameters for each property. Shape parameter estimates will be denoted by β_A and β_B and scale parameter estimates will be denoted by α_A and α_B. Estimation of shape and scale parameters is performed using a maximum likelihood procedure for the two-parameter

Weibull distribution, after subtracting off the estimated threshold. (The two-parameter Weibull is equivalent to the three-parameter Weibull with threshold zero.)

Using the method outlined in Section 9.6.5.2, compute the maximum likelihood estimates of the shape and scale parameters for the censored or uncensored sample $\{X_{(i)} - \tau_A : i=1,\ldots,r\}$. Denote these estimates by β_A and α_A, respectively. Using the same procedure, compute estimates β_B and α_B based on the sample $\{X_{(i)} - \tau_B : i=1,\ldots,r\}$.

With population parameter estimates discussed above at hand, the computation of the lower tolerance bounds is carried out by use of the formulas:

$$T_{99} = \tau_A + Q_A \exp\left[- V_A/\left(\beta_A\sqrt{n}\right)\right],$$
$$T_{90} = \tau_B + Q_B \exp\left[- V_B/\left(\beta_B\sqrt{n}\right)\right],$$

where

$Q_A = \alpha_A (0.01005)^{1/\beta_A}$,
$Q_B = \alpha_B (0.10536)^{1/\beta_B}$,
V_A = the value in the V_A column of Table 9.6.4.8 corresponding to a sample of size n, and
V_B = the value in the V_B column of Table 9.6.4.8 corresponding to a sample of size n.

If the variable that follows a three-parameter Weibull distribution represents a transformation of the mechanical property, the lower tolerance bounds (T_{99}, T_{90}) computed by the above formulas must be transformed back to the original units in which the mechanical property is conventionally reported. When the computed T_{99} or T_{90} value results in a fractional number, the mechanical property used in the room temperature tables is determined by rounding. Fractions greater than 0.75 usually are raised to the next larger integer while lesser decimal fractions are disregarded. However, the rounded T_{99} value is replaced in the mechanical property tables with the S value if the S value is known. In that case the rounded T_{99} value is included in a footnote.

9.2.9 DIRECT COMPUTATION FOR AN UNKNOWN DISTRIBUTION.—This procedure should be used when a mechanical-property value is to be computed directly (not paired with another property for computational purposes) and the form of the distribution of population is unknown (not normal or three-parameter Weibull). Distribution should not be considered unknown (1) if tests show it to be nearly normal or three-parameter Weibull, (2) if it can be transformed to a nearly normal or three-parameter Weibull distribution, or (3) if it can be separated into nearly normal or three-parameter Weibull subpopulations. This procedure is applicable to F_{tu}, and F_{ty}. It may also be used for F_{cy}, F_{su}, F_{bru}, and F_{bry} if sufficient quantity of data is available.

9.2.9.1 *Data Requirements.*—Data must be adequate to assure that the sample is representative of the population. Although censoring is highly undesirable, parametric techniques will "tolerate" a limiteddegree of censoring. In contrast, nonparametric techniques will not "tolerate" censoring. Determination of a T_{99} value requires at least 299 individual observations, but additional data is very desirable. The selection of the number 299 is not arbitrary. Rather, 299 represents the smallest sample for which the lowest observation is a tolerance bound, T_{99}. For smaller samples, T_{99} is below the lowest observation and thus cannot be determined without knowledge of the form of population distribution. The lowest of 29 observations is a tolerance bound, T_{90}; in practice, however, 100 observations is the smallest sample normally employed to compute a T_{90} value for inclusion in the document. For 100 observations, T_{90} is the 5th ranked value from the lowest observation according to Table 9.6.4.2. The requirement for number of heats or lots for the sample is comparable to that required for a parametric analysis.

9.2.9.2 *Computational Procedure.*—Nonparametric (or distribution-free) data analysis assumes a random selection of test points and uses only the ranks of individual test points and the total number of

test points. If test points have been deleted from a sample, the random basis is violated; consequently, this procedure must not be used when there is reason to suspect that the sample may have been censored**.

As an example, assume that a sample consists of 299 test points selected in a random manner. The test point having the lowest value has rank 1, the test point having the next lowest value has rank 2, etc. Thus, an array of ranked test points might appear as follows:

Rank of Test Point	Value of Test Point, ksi
1	73.3
2	74.1
3	75.2
4	75.3
5	75.6
299	85.7

For each rank from a sample of size, n, it is possible to predict, with 0.95 confidence, the least fraction of population that exceeds the value of the test point having rank r. Since only two fractions, or probabilities, are of interest in determination of T_{99} and T_{90} values, only the ranks of test points having the probability and confidence of T_{99} and T_{90} values are presented in Table 9.6.4.2. To use this table with a sample size of 299, for example, one would designate the value of the lowest (r=1) test measurement as T_{99} and the 22nd lowest (r=22) test measurement as T_{90}. For sample sizes between tabulated values, interpolation is permissible. For sample sizes smaller than 299, T_{99} is smaller than the value of the lowest point and cannot be determined in this manner.

When the lower tolerance bound (T_{99} or T_{90}) results in a fractional number, the actual mechanical property value used in the room temperature tables is determined by rounding. Fractions greater than 0.75 usually are raised to the next larger integer while less decimal fractions are disregarded. However, the rounded T_{99} value is replaced in the mechanical property tables with the S value if the S value is lower. In that case the rounded T_{99} value is included in a footnote.

9.2.10 COMPUTATION OF DERIVED PROPERTIES.—Ideally, it is desirable to determine F_{cy}, F_{su}, F_{bru}, F_{bry}, as well as F_{tu} and F_{ty} in other than specified test direction by direct computation as described in Sections 9.2.7 through 9.2.9, and, if sufficient quantity of data is available, direct computation procedures shall be used. Unfortunately, the cost of generating required data for these properties is usually prohibitive. Consequently, this section describes an indirect method of computation to determine the mechanical property values.

*It should be pointed out that parametric techniques will "tolerate" a limited degree of censoring, although censoring is highly undesirable. Nonparametric techniques tolerate no censoring whatsoever.

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A derived property is a mechanical property value determined by its relationship to an established tensile property (F_{tu} or F_{ty}, A, B, or S-basis). This indirect method of computation is applicable to F_{tu} and F_{ty} in grain directions other than the specified testing direction, as delineated in the applicable material specification, and for all grain directions for F_{cy}, F_{su}, F_{bru}, and F_{bry}.

The procedure involves pairing of TUS, SUS, or BUS measurements with TUS measurements for which F_{tu} has been established or the pairing of TYS, CYS, and BYS measurements with TYS measurements for which F_{ty} has been established. Average values for each lot shall be used when more than one measurement per lot is available.

This technique is based on the premise that the mean ratio of paired observations representing related properties provides an estimate of the ratio of corresponding population means. The ratio consists of measurements of the property to be derived as the numerator and measurement of the established tensile property as the denominator. Thus, TUS or TYS in the specified testing direction always appears in the denominator of the ratio of observed values.

Grain direction to be used for the denominator is the specified test direction as delineated in the applicable material specification. For most materials, routine quality control (certification) tests are usually conducted only in one grain direction even though the specification may contain mechanical property requirements for two or three grain directions. For guidance, specified or primary test direction for different product forms of each alloy system is shown in Table 9.2.10.

TABLE 9.2.10. *Primary[a] Testing Direction for Various Alloy Systems*

Product Form	Carbon and Low Alloy Steels	Non-Heat Treatable Alum. Alloys	Heat Treatable Alum. Alloys	Magnesium Alloys	Titanium Alloys	Corrosion and Heat Resistant Alloys	Other Alloys
Sheet and Plate	LT	L	LT	L	[d]	LT	[b]
Bar	L	L	L	L	[d]	L	[b]
Tubing	L	L	L	L	L	L	[b]
Extrusion	L	L	L	L	[d]	L	[b]
Die Forging	[b]	L	L[c]	L	[d]	[b]	[b]
Hand Forging	[b]	LT	LT	LT	[d]	[b]	[b]

[a]Although material specifications may contain mechanical-property requirements for two or three grain directions, the primary test direction indicates the grain direction which is tested regularly.

[b]See applicable material specification.

[c]Although material specifications require testing in both L and T directions, the T direction by definition includes all orientations not within ±15° of parallel to grain flow. Hence, the L direction is preferred for analytical purposes.

[d]Since there is no primary test direction for titanium alloys, mechanical property ratios shall be formed using strength values which represent the same grain directions in the numerator and denominator. The design allowable is computed as the product of the reduced ratio and the F_{ty} or F_{tu} value for the grain direction represented by the reduced ratio.

9.2.10.1 *Data Requirements.*—Computation of a derived value for each significant test direction requires at least ten paired measurements from ten lots* of material obtained from at least two production heats, casts, or melts for each product form and heat-treat condition or temper. See Section 9.1.6.2 for definitions of lot, heat, cast, and melt. Thicknesses of the ten lots shall span the thickness range of product form covered by the material specification. Test specimens for paired ratios shall be located in close proximity and shall be taken from the same sheet, plate, bar, extrusion, forging, or casting. If

*For a single form and thickness, data from no more than one heat treat lot per heat may be used to meet the ten-lot requirement.

coupons or specimens are machined prior to heat treatment, all coupons or specimens from the same lot shall be heat treated simultaneously in the same heat-treat load through all heat-treating operations.

In the cases where multiple observations are available from a single lot, the average of those observations shall be treated as an individual observation. Since some variation in strength may be expected from one specimen location to another, use of lot averages minimizes the effect of this variable.

Dimensionally discrepant castings or special test configurations, as approved by the MIL-HDBK-5 Coordination Activity, may be used for a test program to obtain mechanical properties for determination of derived values, providing these castings meet the requirements of the applicable material specification. Separately cast bars are not acceptable for use in obtaining mechanical properties.

9.2.10.2 *Procedure.*—Four basic steps are involved in determining design allowable properties by indirect computation:

(1) Determine the ratios of paired observations for each lot of material.

(2) Compute the statistics, $\bar{r}$ and s, for the ratios of paired observations.

(3) Determine the lower confidence interval estimate (reduced ratio) for the mean ratio.

(4) Use the reduced ratio as the ratio of the derived to the established design allowable.

The ratio of two paired observations is obtained by dividing the measurement of the property to be derived [for example, CYS (LT) for heat-treatable aluminum sheet] by the measurement for established tensile property [for example, TYS (LT)] in the specified testing direction. Equations for computing average and standard deviation of the ratios are the same as those in Section 9.2.2.3.

The ratio of the two population means [for CYS (LT) and TYS (LT), respectively] is expected to exceed the lower confidence limit defined as

$$\bar{r} - t_{1-\alpha} s/\sqrt{n} \qquad [9.2.10.2(a)]$$

where n is the number of ratios

$\bar{r}$ is the average of n ratios

s is the standard deviation of the ratios

$t_{1-\alpha}$ is the $1-\alpha$ fractile of the t distribution for n - 1 degrees of freedom. At the risk level of $\alpha = 0.05$, the appropriate t value is $t_{0.95}$.

Since the lower confidence interval estimate is used as the ratio between the design allowable properties, the reduced ratio, R, may be defined as

$$R = \bar{r} - t_{0.95}\, s/\sqrt{n} \quad . \qquad [9.2.10.2(b)]$$

Values of $t_{0.95}$ for various degrees of freedom, n - 1, are tabulated in Table 9.6.4.5.

The reduced ratio may now be used to establish the design allowable for the property to be derived using the example of aluminum sheet,

$$R = \frac{F_{cy}(LT)}{F_{ty}(LT)} = \frac{\text{allowable to be derived}}{\text{established allowable in specified test direction}}$$

The derived allowable property is computed by cross multiplying:

$$F_{cy}\,(LT) = R\,F_{ty}\,(LT)\ .$$

The basis (A, B, or S) for computed or derived allowable is assumed to be the same as the basis for the F_{ty} or F_{tu} tensile allowable in the right-hand side of the equation.

In a sample of ratios for a given product, effect of thickness on the ratio should be examined. If there is no effect of thickness, ratios for the various thicknesses can be pooled to compute the average and reduced ratio. If there is an effect of thickness, then a regression with thickness should be computed and the average and reduced ratios determined from the regression. See Section 9.2.11.2 for procedure.

When the computed design allowable results in a fractional number, actual design allowable value used in room temperature tables is determined in the following manner. Fractions greater than 0.75 usually are raised to the next larger integer while lesser decimal fractions are disregarded.

9.2.10.3 *Treatment of Grain Direction.*—Tensile allowables are usually listed according to grain direction in material specifications although some specifications do not indicate a grain direction, which implies isotropy. For MIL-HDBK-5, it is recommended that tension allowables be shown for each grain direction. When the material is shown to be isotropic, then the same properties should be shown for each direction.

Compression allowables are shown by grain direction similar to tension allowables. An example of computing compression allowables for heat treatable plate is shown below. The reduced ratio, R, for longitudinal grain direction, is determined from ratios, r, formed from paired observations for each lot of material, CYS(L)/TYS(LT). Although a longitudinal ratio is being obtained, the divisor is long transverse because this is the specified testing direction (refer to Table 9.2.10). The reduced ratio, R, for long transverse grain direction, is determined from ratios, r, formed from paired observations for each lot of material, CYS(LT)/TYS(LT). Similarly the reduced ratios, R, for short transverse grain direction, are determined from ratios, r, formed from paired observations for each lot of material, CYS(ST)/TYS(LT). The ratios, r, determined in the above manner are used in conjunction with Equation 9.2.10.2(b) to obtain a reduced ratio, R, for each grain direction. Equating the reduced ratios, design allowable values are determined from the resulting relationships,

$$R = \frac{F_{cy}(L)}{F_{ty}(LT)}$$

or $\quad F_{cy}(L) = RF_{ty}(LT)\ ,$

similarly $\quad F_{cy}(LT) = RF_{ty}(LT)\ ,$

and $\quad F_{cy}(ST) = RF_{ty}(LT)\ .$

Shear and bearing allowables are usually shown without reference to grain direction. These properties shall be analyzed according to grain direction, and design allowables shall be based on the lowest

reduced ratio obtained for longitudinal, long transverse and short transverse (when applicable) directions. An exception is aluminum hand forgings for which shear values shall be presented according to grain direction.

In computing the derived properties, paired ratios representing different grain directions shall not be combined in the determination of a reduced ratio. This is based on the premise that, if the ratio for two paired measurements is to provide an estimate of population mean ratio, then paired measurements must represent the same grain direction as that of the corresponding population means.

For aluminum die forgings, the transverse, T, grain direction by definition includes all orientations not within ±15° of parallel to grain flow; consequently, only longitudinal tensile data shall be used as the bases to establish compression, shear, and bearing allowables for aluminum die forgings.

9.2.10.4 *Treatment of Test Specimen Location.*—Testing specifications require a change in test specimen location from T/2 for ≤1.500- to T/4 for >1.500-inch thickness for certain products. Although this change in specimen location may result in T/4 mechanical property ratios which are significantly different from T/2 ratios (different populations), as for aluminum plate, the T/2 and T/4 mechanical property ratios should be treated together for analysis to determine derived properties.

9.2.10.5 *Treatment of Clad Aluminum Alloy Plate.*—For clad aluminum alloy plate, 0.500 inch and greater in thickness, tensile properties are determined using round tensile specimens; consequently, tensile properties represent core material. To present design values which represent the average tensile properties across the thickness of the clad plate, an adjustment must be made in the tensile yield and ultimate strength values (S- or A- and B-basis), representing core strength, in the primary test direction(s). These strengths shall be reduced by a factor equal to twice the percentage of the nominal cladding thickness per side. These adjustments in the tensile yield and ultimate strengths shall be made prior to the computation of derived properties, except for short transverse properties. The following footnote, flagged to the appropriate thickness ranges, shall be incorporated into the design allowable table: "These values, except in the ST direction, have been adjusted to represent the average properties across the whole section, including X percent per side nominal cladding thickness."

9.2.10.6 *Proposals.*—Proposals presented to the MIL-HDBK-5 Coordination Group should include (1) proposed new or revised table of room-temperature allowables, (2) raw data used in the analysis, and (3) analysis for the proposed design values.

9.2.11 DETERMINING DESIGN ALLOWABLES BY REGRESSION ANALYSIS.—Procedures used to determine design allowables by regression analysis vary from sample to sample and all involve a number of decisions. These decisions are illustrated by a flowchart in Figure 9.2.11. Before employing regression analysis in the determination of material properties, one must ascertain that the average of property to be regressed varies continuously and linearly or quadratically with some dimensional parameter x (such as x = t, 1/t, etc., where t is thickness). If the variation of average is attributable to other causes, regression should not be used.

Regression analysis, as described herein, also assumes that residuals are normally distributed about the regression line. Residuals are the differences between observed data values and the values which are predicted by the fitted regression equation. Validity of this normality assumption should be evaluated by performing the Anderson-Darling test presented in Section 9.6.1.2.

The procedure for fitting a regression equation of the form,

$$TUS = a + bx,$$

or

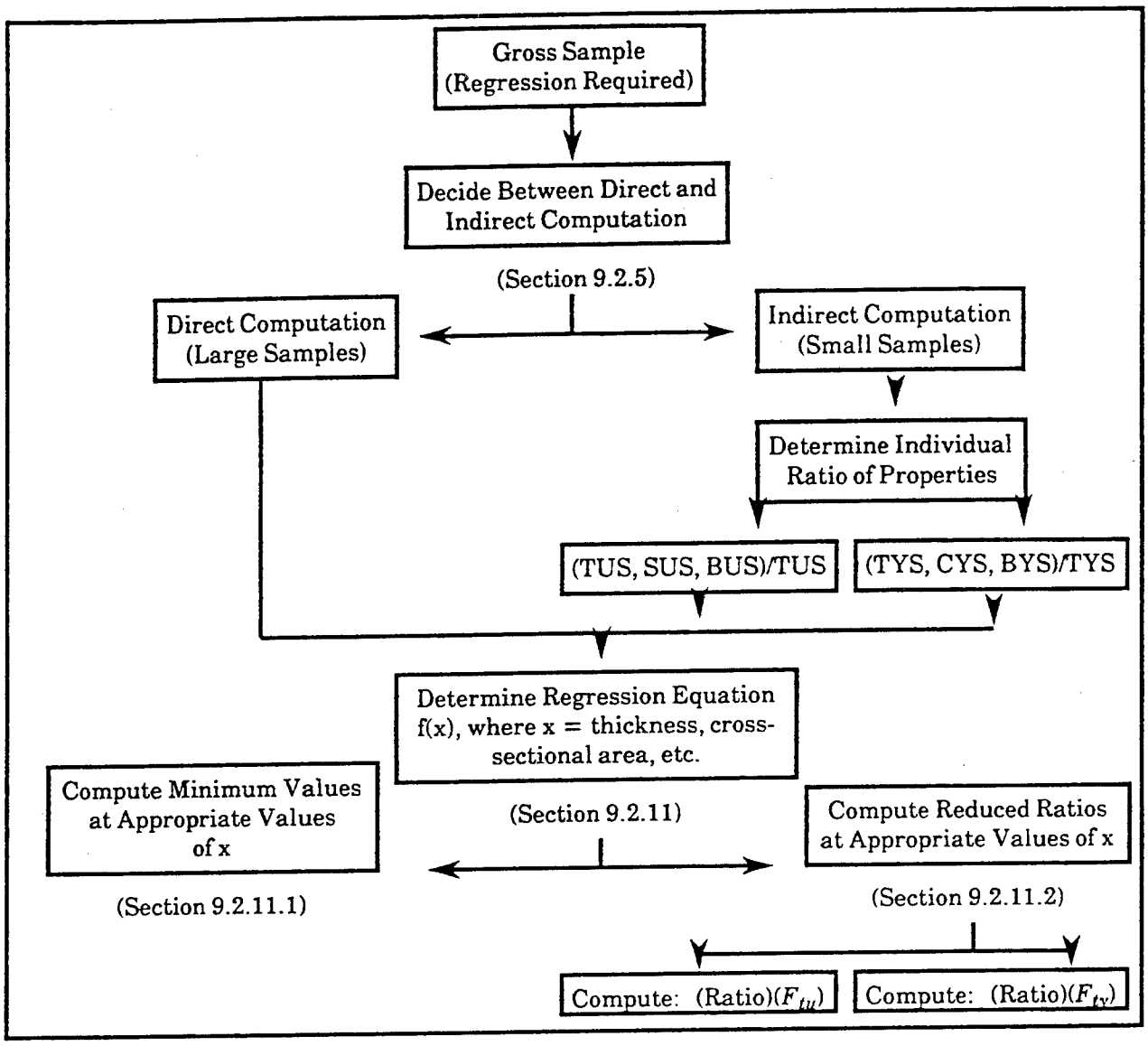


FIGURE 9.2.11. *General procedures for determining design allowables when regression is required.*

$$(SUS/TUS) = a + bx,$$

to n data points is described in Section 9.6.3. In addition to estimates for a and b, this procedure produces two F statistics. One statistic (F_1) tests the significance of regression. The other statistic (F_2) tests the adequacy of a linear model for describing the relationship between the material property and the dimensional parameter. If F_2 indicates a lack of fit of the model to the data, a transformation of the data may account for the nonlinearity. If F_1 indicates an insignificant regression, one of the other appropriate analysis techniques, as described in Sections 9.2.7, 9.2.8, 9.2.9, or 9.2.10, should be used.

The steps involved in determining design allowables by regression analysis are as follows:

(1) Express the property as a simple linear function of the dimensional parameter and obtain estimates of slope and intercept using the least squares regression procedure in Section 9.6.3.1 as follows:

(1) Express the property as a simple linear (or quadratic) function of the dimensional parameter and obtain estimates of the coefficient using the least squares regression procedure in Section 9.6.3.1 (or Section 9.6.3.2); for example

$$TUS = a + bx$$

or

$$(SUS/TUS) = a + bx + cx^2$$

where x is thickness or area and a, b, and c are constants from the least squares equation.

(2) Determine the root mean square error of regression (s_y). A convenient equation for computing the root mean square error from large quantities of data is shown in Section 9.6.3.1.

(3) At selected values of x, determine the allowable for the property by the procedures described in Sections 9.2.11.1 or 9.2.11.2.

The procedures described in this section permit the determination of design allowables only for specific values of x. When it is desired to present a single allowable covering a range of product thickness (for example, 1.001- to 2.000-inch plate), the lowest allowable for the range should be used. Thus, if TUS(LT) decreases continuously with increasing thickness, the TUS(LT) corresponding to x = 2.000 inches would be presented in MIL-HDBK-5. If the decrease is large, a decrease in product thickness interval can be made: for example, by splitting the 1.001- to 2.000-inch interval into two intervals of 1.001 to 1.500 and 1.501 to 2.000 inches.

When the computed design allowable results in a fractional number, actual design allowable value used in room temperature tables is determined in the following manner. Fractions greater than 0.75 usually are raised to the next larger integer while lesser decimal fractions are disregarded.

9.2.11.1 *Direct Computational Procedure.*—The direct computational procedure takes into account errors in the model estimates. If a linear relationship has been determined, compute an A-value for F_{tu} at $x = x_o$, use Equation [9.2.11.1(a)]

$$A = a + bx_0 - K'_A s_y \qquad [9.2.11.1(a)]$$

where a, b, and s_y are computed in the regression of TUS data, K'_A is $\sqrt{(1+\Delta)/n}$ times the 95th percentile of the noncentral t distribution with noncentrality parameter $2.326/\sqrt{(1+\Delta)/n}$ and n - 2 degrees of freedom, and

$$\Delta = \frac{(x_o - \Sigma\, x/n)^2}{\Sigma(x - \Sigma\, x/n)^2/n} \qquad [9.2.11.1(b)]$$

The equation for computing a B-value is similar with K'_B being used in place of K'_A. K'_B is $\sqrt{(1+\Delta)/n}$ times the 95th percentile of the noncentral t distribution with noncentrality parameter $1.282/\sqrt{(1+\Delta)/n}$ and n - 2 degrees of freedom, where Δ is defined above. If calculation of the appropriate noncentral t percentile is not possible, the following approximations to K'_A and K'_B may be used:

$$K'_A = 2.326 + \exp\{0.659 - 0.514\ln(n) + (0.481-1.42/n)\ln(3.71 + \Delta) + 6.58/n\} \qquad [9.2.11.1(c)]$$

$$K'_B = 1.282 + \exp\{0.595 - 0.508\ln(n) + (0.486 - 0.986/n)\ln(1.82 + \Delta) + 4.62/n\}. \qquad [9.2.11.1(d)]$$

These approximations are accurate to within 1.0 percent for $n \geq 10$ and $\Delta \leq 10$. The square root of Δ is the number of standard deviations between x_o and the arithmetic mean of the x-values. Thus, a Δ value of 10 would represent an extreme x_o value, which is more than three standard deviations from the mean x-value.

If a quadratic relationship has been determined, calculate an A-value for F_{tu} at $x = x_o$ using Equation [9.2.11.1(e)]

$$A = a+bx_o+cx_o^2-t_{0.95,\ n-3,\ \frac{2.326}{\sqrt{Q}}}\sqrt{Q}\ s_y \qquad [9.2.11.1(e)]$$

where a, b, c, s_y, and Q are computed by quadratic regression, and the factor $t_{0.95,n-3,\frac{2.326}{\sqrt{Q}}}$ is the 95th percentile of the noncentral t distribution with noncentrality parameter $2.326/\sqrt{Q}$ and n-3 degrees of freedom.

To calculate a B-value in the presence of a quadratic relationship, use 9.2.11.1(f).

$$B = a+bx_o+cx_o^2-t_{0.95,\ n-3,\ \frac{1.282}{\sqrt{Q}}}\sqrt{Q}\ s_y \qquad [9.2.11.1(f)]$$

where a, b, c, s_y, and Q are computed by quadratic regression, and the factor $t_{0.95,n-3,\frac{1.282}{\sqrt{Q}}}$ is the 95th percentile of the noncentral t distribution with noncentrality parameter $1.282/\sqrt{Q}$ and n-3 degrees of freedom.

9.2.11.2 *Reduced Ratio Computational Procedure.*—Regression may also be used to determine reduced ratios when an allowable for a property, such as SUS, is computed indirectly from an already established allowable for TUS. The following assumptions are inherent to the reduced ratio procedure:

(1) The two properties must be distributed according to a bivariate normal distribution.

(2) The coefficient of variation must be the same for the two properties within particular bounds.

(3) The average of the ratio of the two properties must be well described by a linear function of the independent variable.

It is also important that paired data be available over the entire range of the dimensional parameter for which there is data for the direct property (TUS). Note that the confidence level associated with allowables computed using the reduced ratio technique may be somewhat below 95 percent.

To compute the reduced ratio at $x = x_o$, use Equation [9.2.11.2(a)],

$$\text{Reduced Ratio} = a + bx_o - t_{0.95}\ s_y \sqrt{\frac{1+\Delta}{n}} \qquad [9.2.11.2(a)]$$

where Δ is defined in Equation [9.2.11.1(b)], a, b, and s_y, are computed in the regression of SUS/TUS data, and $t_{0.95}$ is selected from Table 9.6.4.5 corresponding to n-2 degrees of freedom. The allowable for F_{su}, at x_o is then computed as the product of the reduced ratio and the established allowable for F_{tu}:

$$F_{su} = (\text{Reduced Ratio})(F_{tu}) .$$

To compute the reduced ratio at $x = x_o$, in the case of linear regression, use Equation [9.2.11.2(a)],

$$\text{Reduced Ratio} = a + bx_0 - t_{0.95,n-2}\ s_y \sqrt{\frac{1+\Delta}{n}} \qquad [9.2.11.2(a)]$$

where Δ is defined in Equation 9.2.11.1(b), a, b, and s_y are computed in the regression of SUS/TUS data, and $t_{.95,n-2}$ is selected from Table 9.6.4.5 corresponding to n-2 degrees of freedom. The allowable for F_{su} at x_o is then computed as the product of the reduced ratio and the established allowable for F_{tu}:

$$F_{su} = (\text{Reduced Ratio})(F_{tu}) .$$

To compute the reduced ratio at $x = x_o$, in the case of quadratic regression, use Equation [9.2.11.2(b)],

$$\text{Reduced Ratio} = a + bx_o + cx_o^2 - t_{0.95,n-3}\, s_y \sqrt{Q} \qquad [9.2.11.2(b)]$$

where a,b,c, s_y, and Q are computed in the quadratic regression of SUS/TUS data, and $t_{.95,n-3}$ is selected from Table 9.6.4.5 corresponding to n-3 degrees of freedom.

The allowable for F_{su} at x_o is then computed as the product of the reduced ratio and the established allowable for F_{tu}:

$$F_{su} = (\text{Reduced Ratio})(F_{tu}) .$$

9.2.12 EXAMPLES OF COMPUTATIONAL PROCEDURES.—It is appropriate to review computational procedures described in Sections 9.2.4 through 9.2.11. To do so, a hypothetical set of input data has been invented. In progressing through this example, flow charts of Figures 9.2.3, 9.2.4, 9.2.6, and 9.2.11 have been followed, and appropriate references to specific sections of the guidelines have been made.

It is assumed for this example that a quantity of quality assurance test data has been amassed, representing one long transverse tensile test per lot, plus other tests from a portion of the lots, at a frequency of one test per lot.

The example problems presented fall into two major categories. Problems I through VII illustrate techniques based on an assumed underlying normal distribution. Problems VIII through XII provide illustrations of techniques based on an assumed underlying three-parameter Weibull distribution.

The input data for these example problems are described below. Because entire data sets (as opposed to means and standard deviations) are required for Problems VIII through XII, the data points for groups (1) through (4) and group (6) have been reported in Tables 9.2.12(a) through (c).

TABLE 9.2.12(a). *Group (1) Data Set for Example Problems in Section 9.2.12*

Group (1)				
139.608	146.534	147.442	151.229	153.792
140.638	146.651	147.489	151.234	153.844
140.711	146.667	147.497	151.283	153.846
140.988	146.699	147.653	151.323	153.855
141.873	146.710	147.752	151.388	153.914
141.940	146.714	147.765	151.425	153.992
142.105	146.766	147.785	151.428	154.021
142.478	146.825	147.803	151.433	154.064
142.597	146.857	147.911	151.471	154.068
142.694	146.876	147.942	151.557	154.077
143.309	146.941	147.952	151.599	154.110
143.502	146.944	147.961	151.609	154.128
143.620	146.970	147.980	151.628	154.149
143.644	147.087	148.001	151.641	154.219
143.674	147.198	148.012	151.670	154.242
143.720	147.284	148.029	151.785	154.297
143.844	147.291	148.038	151.837	154.359
143.865	147.326	148.048	151.876	154.382
143.867	147.334	148.049	151.962	154.508
143.997	147.353	148.051	151.992	154.541
144.221	148.686	148.059	152.015	154.571
144.320	148.691	148.074	152.037	154.781
144.463	148.695	148.091	152.081	154.858
144.508	148.701	148.118	152.101	155.012
144.612	148.714	148.122	152.143	155.077
144.651	148.724	148.197	152.150	155.102
144.837	148.854	148.201	152.151	155.116
144.864	148.868	148.236	152.157	155.231
144.890	148.884	148.267	152.199	155.267
144.973	148.891	148.292	152.207	155.311
145.076	148.919	148.304	152.270	155.336
145.110	148.952	148.334	152.332	155.359
145.122	148.957	148.339	152.352	155.386
145.165	148.982	148.355	152.448	155.422
145.214	149.016	148.368	152.656	155.469
145.229	149.045	148.567	152.736	155.604
145.270	149.103	148.584	152.802	155.627
145.277	149.107	148.620	152.840	155.641
145.325	149.158	148.678	152.882	155.785
145.399	149.180	148.684	152.907	155.823
145.416	149.183	150.194	152.920	155.863
145.577	149.187	150.310	152.929	155.904
145.600	149.321	150.315	153.007	156.078
145.693	149.416	150.340	153.029	156.088
145.709	149.473	150.377	153.049	156.379
145.721	149.571	150.415	153.102	156.616
145.741	149.581	150.423	153.118	156.716
145.872	149.605	150.427	153.206	156.740
145.921	149.605	150.459	153.279	156.924
145.925	149.606	150.579	153.286	157.053
145.966	149.653	150.722	153.296	157.341
145.978	149.707	150.731	153.298	157.357
146.069	149.731	150.739	153.478	157.614
146.136	149.755	150.773	153.504	157.763
146.220	149.798	150.830	153.543	157.980
146.285	149.810	151.019	153.576	158.021
146.301	149.812	151.042	153.648	158.154
146.367	149.894	151.075	153.695	158.518
146.479	149.996	151.111	153.707	159.377
146.500	150.124	151.211	153.715	162.717

TABLE 9.2.12(b). *Group (3) Data Set for Example Problems in Section 9.2.12*

Group (3)				
121.438	126.276	128.823	131.254	133.841
121.614	126.342	128.846	131.325	133.843
121.757	126.388	128.868	131.388	133.893
122.077	126.430	128.966	131.439	133.898
122.109	126.449	128.983	131.444	133.912
122.494	126.535	128.989	131.469	133.922
122.503	126.606	129.029	131.477	133.934
122.543	126.665	129.035	131.677	133.948
122.632	126.668	129.052	131.690	134.089
123.082	126.673	129.083	131.731	134.134
123.101	126.696	129.117	131.754	134.179
123.193	126.727	129.136	131.786	134.194
123.238	126.822	129.148	131.808	134.249
123.296	126.863	129.321	131.816	134.339
123.474	126.877	129.413	131.906	134.351
123.527	126.907	129.434	131.975	134.361
123.616	126.919	129.546	131.977	134.689
123.694	126.972	129.560	132.138	134.747
123.755	126.999	129.596	132.189	134.776
123.770	127.114	129.654	132.223	134.779
123.825	127.140	129.709	132.282	134.873
124.025	127.203	129.715	132.286	134.874
124.055	127.300	129.784	132.296	134.883
124.083	127.322	129.788	132.380	134.890
124.105	127.337	129.891	132.393	134.969
124.121	127.383	129.899	132.436	135.027
124.171	127.387	129.938	132.470	135.064
124.176	127.420	129.940	132.482	135.191
124.223	127.474	130.007	132.511	135.499
124.373	127.579	130.020	132.514	135.513
124.681	127.607	130.070	132.558	135.518
124.691	127.677	130.206	132.564	135.532
124.718	127.695	130.225	132.595	135.545
124.778	127.710	130.237	132.703	135.661
124.793	127.741	130.351	132.718	135.754
124.920	127.761	130.427	132.762	135.836
124.934	127.811	130.457	132.805	135.920
125.000	127.841	130.499	132.849	135.921
125.018	127.859	130.526	132.851	135.944
125.070	127.859	130.528	132.869	136.027
125.070	127.889	130.586	132.952	136.030
125.150	127.946	130.599	133.024	136.032
125.152	128.010	130.624	133.031	136.050
125.247	128.016	130.684	133.049	136.112
125.279	128.153	130.710	133.096	136.149
125.295	128.203	130.765	133.159	136.154
125.350	128.288	130.772	133.166	136.160
125.370	128.309	130.797	133.224	136.204
125.433	128.323	130.895	133.438	136.217
125.531	128.332	131.003	133.441	136.348
125.535	128.341	131.008	133.508	136.855
125.714	128.452	131.040	133.581	136.883
125.717	128.640	131.103	133.592	137.087
125.801	128.672	131.104	133.595	137.115
125.915	128.699	131.125	133.622	137.163
126.083	128.719	131.158	133.683	137.484
126.128	128.723	131.175	133.749	137.618
126.129	128.752	131.176	133.763	137.653
126.194	128.795	131.192	133.768	138.335
126.276	128.819	131.195	133.774	139.141

TABLE 9.2.12(c). *Group (2), (4), and (6) Data Sets for Example Problems in Section 9.2.12*

Group (2)	Group (4)	Group (6)	
141.914	120.487	135.373	145.061
143.980	122.271	135.500	145.072
145.110	124.167	135.775	145.082
145.681	124.622	136.450	145.082
145.829	124.672	137.114	145.331
145.919	125.280	137.241	145.460
145.981	125.862	137.900	145.606
148.412	126.332	138.916	145.626
148.694	128.860	139.158	145.754
148.772	129.158	139.307	145.785
148.831	129.179	139.626	145.802
148.965	130.238	139.827	145.876
149.197	130.782	139.839	146.091
149.761	130.985	140.022	146.096
150.150	131.612	140.461	146.159
151.472	131.642	140.957	146.302
151.746	132.129	141.083	146.303
152.089	132.147	141.149	146.447
152.564	132.812	141.435	146.797
152.737	133.388	141.473	146.937
152.798	133.716	141.518	146.967
153.857	134.127	141.582	147.149
153.930	135.787	141.592	147.224
154.012	135.836	141.731	147.305
154.024	136.235	141.937	147.500
154.153	136.770	142.125	147.657
155.637	137.068	142.138	147.675
157.118	137.901	142.298	147.833
162.241	137.919	142.441	148.084
164.426	138.017	142.785	148.556
		142.838	148.708
		142.859	148.954
		143.141	148.988
		143.180	149.082
		143.397	149.123
		143.426	149.590
		143.444	149.831
		143.558	149.974
		143.722	150.325
		143.886	151.484
		144.200	151.523
		144.276	151.605
		144.313	152.086
		144.418	152.467
		144.465	152.646
		144.650	152.852
		144.672	153.164
		144.847	153.675
		144.901	155.492
		144.924	157.944

INFORMATION FOR EXAMPLE PROBLEMS

Material Identification: Alloy X sheet, annealed.
Specified Testing Direction: Long Transverse (LT)
Specified Properties:
≤ 0.125 inch —
F_{tu} (LT) = 140 ksi, F_{ty} (LT) = 115 ksi;
0.126-0.249 inch —
F_{tu} (LT) = 135 ksi, F_{ty} (LT) = 110 ksi.
Available Test Results:

Group (1). 300 observations of TUS(LT) for thickness range 0.020-0.125 inch from Supplier A; no variation with thickness. Go to Problems I, III, VIII, and X.

Group (2). 30 observations of TUS(LT) for thickness range 0.020-0.125 inch from Supplier B; no variation with thickness. Go to Problems I and VIII.

Group (3). 300 observations of TYS(LT) for thickness range 0.020-0.125 inch from Supplier A; no variation with thickness. Go to Problems II and IX.

Group (4). 30 observations of TYS(LT) for thickness range 0.020-0.125 inch from Supplier B; no variation with thickness. Go to Problems II and IX.

Group (5). 30 observations of SUS(LT) for thickness range 0.020-0.249 inch; apparent decrease in SUS(LT) on increasing thickness; observations may be paired with TUS(LT) if desired. Go to problem VII.

Group (6). 100 observations of TUS(LT) for thickness range 0.126-0.249 inch; no variation with thickness. Go to Problems III and X.

EXAMPLE PROBLEMS BASED ON AN ASSUMED UNDERLYING NORMAL DISTRIBUTION

PROBLEM I

Should the data in Groups (1) and (2) be combined?

Other information: Neither property varies with thickness. Sample statistics are:

Subpopulation	n	$\overline{X}$, ksi	s, ksi
Group (1) TUS (LT), 0.020 to 0.125	300	150.0	4.00
Group (2) TUS (LT), 0.020 to 0.125	30	151.0	5.00

(Refer to Sections 9.2.4 and 9.6.2)

*The statistical tests described in Problems I through III apply specifically to the case where normality can be assumed. The more general Anderson-Darling procedure described in Problem IV can be applied to normal as well a nonnormal distributions.

Prob. I—Step 1. Test to determine whether the variances differ significantly:

$F = (s_1)^2/(s_2)^2 = (4.00)^2/(5.00)^2 = 0.64$

Degrees of freedom, numerator = $n_1 - 1 = 300 - 1 = 299$.

Degrees of freedom, denominator = $n_2 - 1 = 30 - 1 = 29$.

$F_{0.975}$(299,29df) from Table 9.6.4.4 = 1.87 (approximately)

$1/F_{0.975}$ (29,299df) = 1/1.69 = 0.59

Since the computed value of F(0.64) lies within the 0.95 confidence interval (0.59 to 1.87), conclude the variances do not differ significantly.

Prob. I—Step 2. Test to determine whether the averages differ significantly:

Difference between averages $D_{\overline{X}}$ = 150.0 − 151.0 = 1.0 ksi

$$u = t_{0.975}\, S_p \sqrt{\frac{n_1 + n_2}{n_1\, n_2}}$$

Degrees of freedom = $n_1 + n_2 - 2 = 300 + 30 - 2 = 328$

$t_{0.975}$ (328 df) from Table 9.6.4.5 = 1.969

$$S_p = \sqrt{\frac{(n_1 - 2)\, s_1^2 + (n_2 - 1)\, s_2^2}{n_1 + n_2 - 2}} = \sqrt{\frac{(300 - 1)(4.00)^2 + (30 - 1)(5.00)^2}{300 + 30 - 2}} = 4.10 \text{ ksi}$$

$$u = 1.969 \times 4.10 \times \sqrt{\frac{n_1 + n_2}{n_1\, n_2}} = 1.969 \times 4.10 \times \sqrt{\frac{300 + 30}{300 \times 30}} = 1.54 \text{ ksi}$$

Since the observed difference between the averages, $\overline{X}$ (1.0 ksi), is less than u (1.54 ksi), conclude the averages do not differ significantly.

Prob. I—Step 3. Since there is no reason to conclude that the subpopulations represented by Groups (1) and (2) do not belong to the same population, combine these groups.

Subpopulation	n	$\overline{X}$, ksi	s, ksi
Group (1&2) TUS (LT), 0.020-0.125, Suppliers A and B	330	150.1	4.10

Go to Problem IV.

PROBLEM II

Should the data in Groups (3) and (4) be combined?

Other information: Neither property varies with thickness. Sample statistics are:

Subpopulation	n	$\overline{X}$, ksi	s, ksi
Group (3) TYS (LT), 0.020-0.125, Supplier A	300	130.0	4.00
Group (4) TYS (LT), 0.020-0.125, Supplier B	30	131.0	5.00

The steps involved in this problem are identical to those in Problem I and similar conclusions were obtained from the input, namely, that Groups (3) and (4) should be combined. The sample statistics for the combined groups are:

Subpopulation	n	$\overline{X}$, ksi	s, ksi
Group (3&4) TYS (LT), 0.020-0.125, Suppliers A and B	330	130.1	4.10

Go to problem V.

PROBLEM III

Should the data in Groups (1) and (6) be combined?

Other information: Neither property varies with thickness. Sample statistics are:

Subpopulation	n	$\overline{X}$, ksi	s, ksi
Group (1) TUS (LT), 0.020-0.125	300	150.0	4.00
Group (6) TUS (LT), 0.126-0.249	100	145.0	4.47

Prob. III—Step 1. Test to determine whether the variances differ significantly.

$F = (s_1)^2/(s_2)^2 = (4.00)^2/(4.47)^2 = 0.80$

Degrees of freedom, numerator = $n_1 - 1 = 300 - 1 = 299$.

Degrees of freedom, denominator = $n_6 - 1 = 100 - 1 = 99$.

$F_{0.975}$ (299,99df) from Table 9.6.4.4 = 1.46 (approximately)

$1/F_{0.975}(99,299df) = 1/1.43 = 0.700$.

Since the computed value of F (0.80) lies within the 0.95 confidence interval (0.700 to 1.46), conclude that the variances do not differ significantly.

Prob. III—Step 2. Test to determine whether the averages differ significantly.

Difference between averages, $D_{\overline{X}} = (150.0 - 145.0) = 5.0$ ksi

$$u = t_{0.975} S_p \sqrt{\frac{n_1 + n_6}{n_1 n_6}}$$

Degrees of freedom = $n_1 + n_6 - 2 = 300 + 100 - 2 = 398$.

$t_{0.975}$ (398 df) from Table 9.6.4.5 = 1.968.

$$S_p = \sqrt{\frac{(n_1 - 1)s_1^2 + (n_6 - 1)s_6^2}{n_1 + n_6 - 2}} = \sqrt{\frac{(300 - 1)(4.00)^2 + (100 - 1)(4.47)^2}{300 + 100 - 2}} = 4.20 \text{ ksi}$$

$$u = (1.968)(4.20)\sqrt{\frac{n_1 + n_6}{n_1 n_6}} = (1.968)(4.20)\sqrt{\frac{300 + 100}{(300)(100)}} = 0.95 \text{ ksi}$$

Since the observed difference between the averages $D_{\overline{X}}$ (5.0 ksi) is greater than u (0.95 ksi), conclude that the averages differ significantly and that the subpopulations represented by Groups (1) and (6) do not belong to the same population.

Prob. III—Step 3. Do not combine the sample statistics for these groups.

Go to Problem VI.

PROBLEM IV

What computational method should be used for the combined observations of Groups (1) and (2)?

Other Information: This property does not vary with thickness. Sample statistics for the combined observations are:

Population	n	$\overline{X}$, ksi	s, ksi
Group (1&2) TUS (LT), 0.020-0.125	330	150.1	4.10

Form of the distribution has not been determined. (Refer to Sections 9.2.5, 9.2.6, 9.2.7, and 9.6.1.)

The sample is large enough to permit direct computation of A and B values. Consequently, the computational method will be determined by whether or not the observations are normally distributed.

Prob. IV—Step 1. Test to determine whether the distribution is normal. The Anderson-Darling test for normality will be employed in this example (see 9.6.1.2). Use the formula:

$$Z_{(i)} = (X_{(i)} - 150.1)/4.10,$$

the values of $Z_{(1)}, \ldots, Z_{(330)}$ must be calculated. The first three values are $Z_{(1)} = -2.56$, $Z_{(2)} = -2.31$, and $Z_{(3)} = -2.29$. Now $F_0(Z_{(1)}), \ldots, F_0(Z_{(330)})$ must be calculated by finding the area under the standard

normal curve to the left of each Z value. The first three values are $F_o(Z_{(1)}) = 0.0052$, $F_o(Z_{(2)}) = 0.0104$, and $F_o(Z_{(3)}) = 0.0110$.

The Anderson-Darling test statistic is then calculated as

$$AD = \left[\sum_{i=1}^{330} \frac{1 - 2i}{330} [\ln(F_o(Z_{(i)})) + \ln(1 - F_o(Z_{(331-i)}))]\right] - 330 = 0.693.$$

The computed value of the test statistic is then compared to the critical value

$0.750 = 0.752/[1 + 0.75/330 + 2.25/(330)^2]$

Since the computed value of 0.693 is less than the critical value of 0.750, the hypothesis of normality is not rejected.

Prob. I-V—Step 2. Compute F_{tu} (LT), 0.020 to 0.125, for Alloy X, using procedures for the normal distribution.

Population	n	$\overline{X}$, ksi	s, ksi
Group (1&2) TUS (LT), 0.020 to 0.125	330	150.1	4.10

$k_A = 2.512$
$k_B = 1.410$
F_{tu}(LT), A basis = X - k_As = 150.1 - 2.512 x 4.10 = 139.8 or 140 ksi (rounded per Section 9.2.10.2)
F_{tu}(LT), B basis = X - k_Bs = 150.1 - 1.410 x 4.10 = 144.3 or 144 ksi (rounded per Section 9.2.10.2)

PROBLEM V

What computational method should be used for the combined observations of Groups (3) and (4)?

Other Information: This property does not vary with thickness. Sample statistics for the combined observations are:

Population	n	$\overline{X}$, ksi	s, ksi
Group (3&4) TYS(LT), 0.20 to 0.125	330	130.1	4.10

Form of the distribution has not been determined. (Refer to Sections 9.2.5, 9.2.6, 9.2.9, and 9.6.1.)

The sample is large enough to permit direct computation of A and B-values. Consequently, the computational method to be used will be determined by whether or not the observations are normally distributed.

Prob. V—Step 1. Test to determine whether or not the distribution is normal. The value of the Anderson-Darling test statistic for normality is 1.315 for Group (3&4). Since 1.315 is greater than the critical value of 0.750, the underlying distribution cannot be assumed to be normal. Thus, the underlying distribution will be treated as a three-parameter Weibull or an unknown distributional form.

Prob. V—Step 2. Compute F_{ty}(LT), 0.020-0.125, using procedures for the unknown distribution. This procedure requires the ranking of observations from lowest to highest. Referring to Table 9.6.4.2, it is found that for a sample size of 330, the lowest observation (rank = 1) is an A-value and the 24th lowest (rank = 24) is a B-value. The 24 lowest observations are shown below:

Rank	TYS, ksi	Rank	TYS, ksi	Rank	TYS, ksi
1	120.5	9	122.5	17	123.5
2	121.4	10	122.5	18	123.5
3	121.6	11	122.6	19	123.6
4	121.8	12	123.1	20	123.7
5	122.1	13	123.1	21	123.8
6	122.1	14	123.2	22	123.8
7	122.3	15	123.2	23	123.8
8	122.5	16	123.3	24	124.0

Consequently, from these data the following allowables have been computed for Alloy X:

F_{ty}(LT), A-basis = 120.5 ksi.
F_{ty}(LT), B-basis = 124.0 ksi.

PROBLEM VI

What computational procedure should be used for the observations in Group (6)? The data in Group (6) represent a borderline situation. They cannot be combined with data for lesser thicknesses because there is significant difference between the TUS(LT) averages for the two thickness ranges, as shown in Problem III. The sample size is just barely adequate for direct computation if the distribution is found to be normal. If the distribution is not normal, the properties for this product would be presented on an S-basis, pending the accumulation of more data. The test for normality would be conducted as described in Problem IV, and will not be illustrated here.

PROBLEM VII

What computational procedure should be used for the observations in Group (5)?

Other Information: SUS(LT) decreases with increasing thickness, while TUS(LT) does not vary with thickness. Sample statistics are:

Population	n	$\overline{X}$, ksi	s, ksi
Group (5) SUS(LT), 0.020 to 0.249	30	not determined	

The sample size for these data is too small to permit direct computation. Thus, the procedure that should be used is indirect computation by pairing observations of SUS(LT) with observations of TUS(LT). Also, since a thickness effect was suspected in the original data, a regression against thickness should be made and checked for significance. (Refer to Sections 9.2.10, 9.2.1 1, and 9.6.3.)

Prob. VII—Step 1. Pair SUS(LT) with TUS(LT).

Ratios of SUS(LT)/TUS(LT) are as follows:

SUS(LT)/TUS(LT)	Thickness, inch	SUS(LT)/TUS(LT)	Thickness, inch
0.700	0.020	0.640	0.090
0.680	0.020	0.650	0.090
0.660	0.020	0.660	0.090
0.660	0.030	0.630	0.100
0.670	0.030	0.650	0.100
0.680	0.030	0.670	0.100
0.650	0.040	0.640	0.150
0.670	0.040	0.630	0.150
0.690	0.040	0.620	0.150
0.650	0.060	0.610	0.180
0.660	0.060	0.630	0.180
0.670	0.060	0.650	0.180
0.640	0.070	0.600	0.240
0.660	0.070	0.610	0.240
0.680	0.070	0.620	0.240

Prob. VII—Step 2. Determine regression equation in the form [SUS(LT)TUS(LT)]′=r′=a + bx, where x = thickness, using least-squares techniques. (Note—in this example, the letter r, rather than y, is used to denote the dependent variable and the prime (′) is used to indicate that the ratio is determined by regression.) The following sums were obtained from analysis of the ratios plotted in Figure 9.2.12.

Number of ratios, n = 30

$\Sigma(x) = 2.94$
$\Sigma(x^2) = 0.4260$
$\Sigma(r) = 19.53$
$\Sigma(r^2) = 12.7319$
$\Sigma(xr) = 1.8723$
$(\Sigma x)^2 = 8.6436$
$(\Sigma r)^2 = 381.4209$
$(\Sigma x)(\Sigma r) = 57.4182$
$S_{xx} = 0.1379$
$S_{xr} = 0.0416$
$S_{rr} = 0.0179$

Referring to the equations presented in Section 9.6.3:

$$\text{Slope, } b = \frac{S_{xr}}{S_{xx}} = \frac{-0.0416}{0.1379} = -0.302$$

$$\text{Intercept, } a = \frac{\Sigma r - b\,(\Sigma x)}{n} = \frac{19.53 - (-0.302)(2.94)}{30} = 0.6806$$

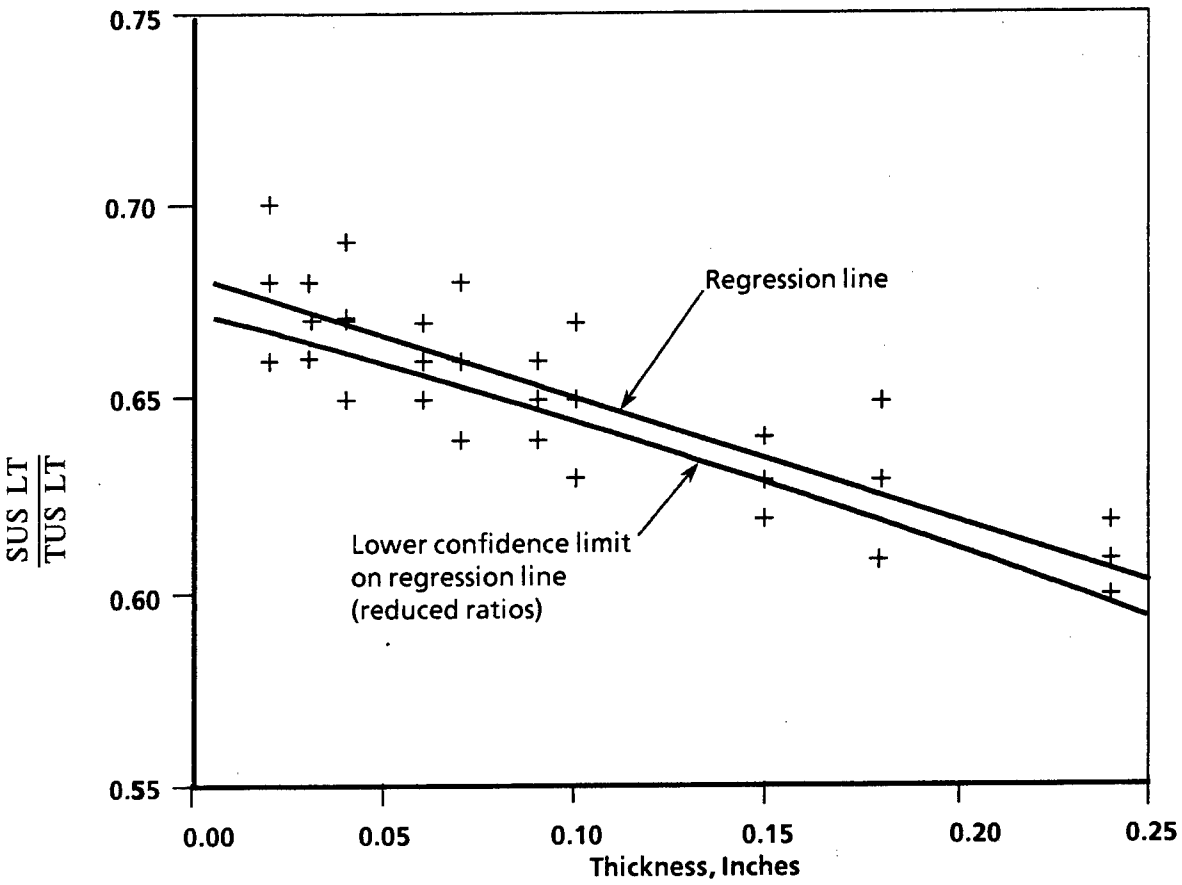


FIGURE 9.2.12. *Ratios of input data for Problem VII.*

Standard Error of Estimate,

$$s_r' = \sqrt{\frac{S_{rr} - b^2 S_{xx}}{(n - 2)}}$$

$$= \sqrt{\frac{0.0179 - (-0.302)^2(0.1379}{(30 - 2)}}$$

$$E = 0.014$$

The equation of the regression line is $r' = 0.6806 - 0.302x$.

The regression line is shown in Figure 9.2.12.

Prob. VII—Step 3. Perform an analysis of variance to check the significance and linearity of the regression.

Since there are 30 ratios, the analysis of variance approach rather than the method involving the computation of confidence limits on the slope term can be used to evaluate linearity.

The only information missing from Step 2 required for the analysis of variance is the values of T, or the summed values of r for each x. They are as follows:

x_1	T_1	x_1	T_1
0.02	2.04	0.09	1.95
0.03	2.01	0.10	1.95
0.04	2.01	0.15	1.89
0.06	1.98	0.18	1.89
0.07	1.98	0.24	1.83

Using these values, the analysis of variance, which is illustrated in Section 9.6.3.2, can be completed as follows:

Source of Variation	Sum of Squares	Degrees of Freedom	Mean Squares	F_{calc}
Regression	0.0126	1	0.0126	63.0
Error	0.0053	28	0.0002	
Lack of Fit	0.0004	8	0.00005	0.208
Pure Error	0.0049	20	0.00024	
Total	0.0179	29		

The second calculated F statistic of 0.208 with k - 2 = 8 and n - k = 20 degrees of freedom is less than the value of 2.45 from Table 9.6.4.9 corresponding to 8 numerator and 20 denominator degrees of freedom. Thus, the deviation from linearity is not significant. The first F statistic of 63.0 with 1 and 28 degrees of freedom is greater than the value of 4.20 from Table 9.6.4.9 corresponding to 1 numerator and 28 denominator degrees of freedom, so the slope of the regression is found to be significantly different from zero.

Prob. VII—Step 4. Compute the reduced ratio for SUS(LT)/TUS(LT). In performing this step, the reduced ratio will be computed at each of four thicknesses (0.020, 0.062, 0.125, and 0.249 inch). This is done by determining the lower confidence limit for the regression line at the desired thicknesses, using the equation from Section 9.2.11. The computation will be worked in detail for x_0 = 0.020 inch:

$$\text{Reduced ratio} = [\text{SUS(LT)/TUS(LT)}]' - t_{0.95}s'_r \sqrt{\frac{1}{n} + \frac{(x_0 - \Sigma x/n)^2}{(\Sigma x^2) - (\Sigma x)^2/n}}$$

$[\text{SUS(LT)/TUS(LT)}]' = r' = 0.681 - 0.302x_0$ (from Step 2, Problem VII)
$= 0.681 - 0.302 \times 0.020 = 0.6746.$

$t_{0.95}$ (for n - 2 = 30 - 2 = 28 degrees of freedom) = 1.701 (from Table 9.6.4.5)

s'_r = 0.014 (from Step 2)

$$\sqrt{\frac{1}{n} + \frac{(x_0 - \Sigma x/n)^2}{(\Sigma x^2) - (\Sigma x)^2/n}} = \sqrt{\frac{1}{30} + \frac{(0.020 - 2.94/30)^2}{0.4260 - 8.6436/30}} = 0.2783$$

Reduced ratio = 0.6746 - 1.701 x 0.014 x 0.2783 = 0.668.

The corresponding ratios for the other thicknesses are tabulated in Step 5. See Figure 9.2.12 for lower confidence limit curve.

Prob. VII—Step 5. Compute F_{su}. This computation will be illustrated for a thickness of 0.020 inch, using the reduced ratio from Step 4.

From Problem IV, F_{tu}(LT) = 140 ksi (A-basis)
F_{tu}(LT) = 144 ksi (B-basis)
F_{su}(LT) = Reduced Ratio x F_{tu}(LT)
F_{su}(LT)(A-Basis) = 0.668 x 140 = 93.5 ksi
F_{su}(LT)(B-Basis) = 0.668 x 144 = 96.2 ksi.

For the four thicknesses listed,

		F_{su}(LT), ksi		
t, inch	Reduced Ratio	A-basis	B-basis	S-basis
0.020	0.668	93.5	96.2	...
0.062	0.657	92.0	94.6	...
0.125	0.638	89.3	91.9	...
0.249	0.595	...	...	80.3

Since F_{su} is shown to decrease with increasing thickness, only the lowest value applicable to the range should be presented in MIL-HDBK-5. By dividing the 0.020 to 0.125 thickness range into two ranges, a somewhat higher F_{su}(LT) value may be presented for thinner material as shown below.

The results of the computations in Problems I through VII have produced the following results (fractions greater than 0.75 are raised to the next higher ksi, while less fractions are dropped):

	Thickness, inch					
	<0.020	0.020-0.062		0.063-0.125		0.126-0.249
Basis	S	A	B	A	B	S
F_{tu}(LT), ksi	140	140	144	140	144	135
F_{ty}(LT), ksi	115	120	124	120	124	110
F_{su}, ksi	...	92	94	89	92	80

Since SUS(LT) data were not available for thickness <0.020 inch, a design value is not presented for this range.

EXAMPLE PROBLEMS BASED ON AN ASSUMED UNDERLYING THREE-PARAMETER WEIBULL DISTRIBUTION

PROBLEM VIII

Should the data in Groups (1) and (2) be combined?

Other information. Neither property varies with thickness. (Refer to Sections 9.2.4 and 9.6.2.)

The k-sample Anderson-Darling test will be employed in this example (see Section 9.6.2.5) to determine whether or not the data in Groups (1) and (2) should be combined. There are 328 distinct values in the combined data from both groups and these are ordered from least to greatest to obtain $Z_{(1)},\ldots,Z_{(328)}$. All values of h_j are equal to 1 except for $h_{34} = 2$ and $h_{160} = 2$. Taking Group (2) to be the first (A_1)-sample and Group (1) to be the second (A_2)-sample, the first 24 Z-values are listed in the table below with the corresponding H- and F-values.

Z_j	H_j	F_{ij}	Z_j	H_j	F_{ij}	Z_j	H_j	F_{ij}
139.61	0.5	0	142.48	8.5	1	143.72	16.5	1
140.64	1.5	0	142.60	9.5	1	143.84	17.5	1
140.71	2.5	0	142.69	10.5	1	143.86	18.5	1
140.99	3.5	0	143.31	11.5	1	143.87	19.5	1
141.87	4.5	0	143.50	12.5	1	143.98	20.5	1.5
141.91	5.5	0.5	143.62	13.5	1	144.00	21.5	2
141.94	6.5	1	143.64	14.5	1	144.22	22.5	2
142.10	7.5	1	143.67	15.5	1	144.32	23.5	2

The k-sample Anderson-Darling test statistics is calculated as

$$ADK = \frac{1}{330(1)}\left[\frac{1}{300}\sum_{j=1}^{328} h_j \frac{(330F_{1j} - 300H_j)^2}{H_j(330 - H_j) - 330h_j/4} + \frac{1}{30}\sum_{j=1}^{328} h_j \frac{(330\,F_{2j} - 30H_j)^2}{H_j(330 - H_j) - 330h_j/4}\right] = 0.821$$

The computed value of the test statistic is compared to the critical value of

$$2.488 = 1 + 0.759\left(1.645 + \frac{0.678}{\sqrt{1}} - \frac{0.362}{1}\right) .$$

Since the computed value of 0.821 is less than the critical value of 2.488, the hypothesis that the populations from which these groups were drawn are identical is not rejected. Thus Groups (1) and (2) will be combined for the computation of allowables.

Go to Problem XI.

PROBLEM IX

Should the data in Groups (3) and (4) be combined?

Other information: Neither property varies with thickness. (Refer to Sections 9.2.4 and 9.6.2)

The value of the k-sample Anderson-Darling test statistic for Groups (3) and (4) is 2.147. Since 2.147 is less than the critical value of 2.488, the hypothesis that the populations from which these groups were drawn are identical is not rejected. Thus, Groups (3) and (4) will be combined for the computation of allowables.

Go to Problem XII.

PROBLEM X

Should the data in Groups (1) and (6) be combined?

Other information: Neither property varies with thickness. (Refer to Sections 9.2.4 and 9.6.2.)

The k-sample Anderson-Darling test will be employed in this example (see Section 9.6.2.5). Taking Group (6) to be the first sample (A_1) and Group (1) to be the second sample (A_2), the k-sample Anderson-Darling test statistic is calculated as:

$$ADK = \frac{1}{400(1)}\left[\frac{1}{100}\sum_{j=1}^{398} h_j \frac{(400\, f_{1j} - 100\, H_j)^2}{H_j(400 - H_j)\, 400\, h_j/4} + \frac{1}{300}\sum_{j=1}^{398} h_j \frac{(400\, F_{2j} - 300\, H_j)^2}{H_j\,(400 - H_j) - 400\, h_j/4}\right] = 44.195$$

Since the computed value of 44.195 is greater than the critical value of

$$2.486 = 1 + 0.758\left(1.645 + \frac{0.678}{\sqrt{1}} - \frac{0.362}{1}\right),$$

the hypothesis that the populations from which these groups are drawn are identical is rejected. Thus Groups (1) and (6) will not be combined for the calculation allowables.

PROBLEM XI

What computational method should be used for the combined observations of Groups (1) and (2)?

Other information: This property does not vary with thickness.

Form of the distribution has not been determined. (Refer to Sections 9.2.5, 9.2.6, 9.2.8, and 9.6.1.4.)

The sample is large enough to permit direct computation of A and B-values. Consequently, the computational method will be determined by whether or not the observations may be assumed to follow a three-parameter Weibull distribution.

Prob. XI—Step 1. Test to determine whether the distribution is a three-parameter Weibull distribution. The Anderson-Darling test for three-parameter Weibullness will be employed in this example (see Section 9.6.1.4). Preliminary calculations give

$K = 88$ $\quad W_{50} = 0.665$

$\overline{X} = 150.1$ $\quad S = 4.10$

$X_{(1)} = 139.608$ $\quad H = 139.6079$

$L = -259.9$

$$R(\tau) = \sum_{i=89}^{262} L_i(\tau) \Big/ \sum_{i=1}^{262} L_i(\tau)$$

It can be verified that $R(-259.9) > 0.665$ and $R(139.6079) < 0.665$. Solving the equation $R(\tau) = 0.665$ with the initial interval $(-259.9, 139.6079)$ gives $\tau_{50} = 138.70$. The function $G_{50}(\beta_{50})$ then becomes

$$G_{50}(\beta_{50}) = \frac{1}{330} \sum_{i=1}^{330} \ln (X_i - 138.70) \left[\left(\frac{X_i - 138.70}{\alpha_{50}} \right)^{\beta_{50}} - 1 \right] - \frac{1}{\beta_{50}}$$

where

$$\alpha_{50} = 10.53 \left[\frac{1}{330} \sum_{i=1}^{330} \left(\frac{X_i - 138.70}{10.53} \right)^{\beta_{50}} \right]^{1/\beta_{50}}$$

Solving the equation $G_{50}(\beta_{50}) = 0$ gives $\beta_{50} = 3.02$ which in turn gives $\alpha_{50} = 12.75$.

The values of $Z_{(1)}, \ldots, Z_{(330)}$ are obtained using the formula

$$Z_i = \left(\frac{X_{(i)} - 138.70}{12.75} \right)^{3.02}$$

The first three Z-values are $Z_{(1)} = 0.000345$, $Z_{(2)} = 0.00339$, and $Z_{(3)} = 0.00378$. The Anderson-Darling test statistic is calculated as

$$AD = \sum_{i=1}^{330} \frac{1 - 2i}{330} \left[\ln \left(1 - \exp(-Z_{(i)})\right) + \ln\left(\exp(-Z_{(331-i)})\right) \right] - 330 = 0.491$$

The computed value of the test statistic is compared to the critical value

$$0.749 = 0.757/(1 + 1/5\sqrt{330})$$

Since the computed value of 0.491 is less than the critical value of 0.749, the hypothesis that the observations follow a three-parameter Weibull distribution is not rejected.

Prob. XI—Step 2. Compute F_{tu} (LT), 0.020-0.125, for Alloy X, using procedures for the three-parameter Weibull distribution. Preliminary calculations give

$K = 88$ $\quad W_A = 0.698$
$W_\beta = 0.678$ $\quad \overline{X} = 150.1$
$S = 4.10$ $\quad X_{(1)} = 139.608$
$H = 139.6079$ $\quad L = -259.9$

$$R(\tau) = \sum_{i=89}^{262} L_i(\tau) \Big/ \sum_{i=1}^{262} L_i(\tau)$$

Solving the equation $R(\tau) = 0.698$ with the interval (-259.9, 139.6079) give $\tau_A = 136.43$. Solving $R(\tau) = 0.678$ gives $\tau_B = 137.98$.

Solving the equation $G_A(\beta_A) = 0$ gives $\beta_A = 3.63$ which in turn given $\alpha_A = 15.14$. Solving the equation $G_B(\beta_B) = 0$ gives $\beta_B = 3.22$ which in turn gives $\alpha_B = 13.52$.

Using the formulas from 9.2.8.4 the allowables are calculated as follows:

$$Q_A = 15.14\ (0.01005)^{1/3.63} = 4.263$$
$$Q_B = 13.52\ (0.10536)^{1/3.22} = 6.719$$
$$A = 136.43 + 4.263 \exp\left(-7.259/3.63\ \sqrt{330}\ \right) = 140.2$$
$$B = 137.98 + 6.716 \exp\left(-4.103/3.22\ \sqrt{330}\ \right) = 144.2$$

PROBLEM XII

What computational method should be used for the combined observations of Groups (3) and (4)?

Other Information: This property does not vary with thickness.

Form of the distribution has not been determined. (Refer to Sections 9.2.5, 9.2.6, 9.2.8, and 9.6.1.4.)

The sample is large enough to permit direct computation of A and B values. Consequently, the computational method will be determined by whether or not the observations may be assumed to follow a three-parameter Weibull distribution.

Prob. XII—Step 1. Test to determine whether the distribution is a three-parameter Weibull distribution. The Anderson-Darling test for three-parameter Weibullness will be employed in this example (see Section 9.6.1.4). Preliminary calculations give

$K = 88$
$\overline{X} = 130.1$ $\quad W_{50} = 0.665$
$X_{(1)} = 120.487$ $\quad S = 4.10$
$L = -279.9$ $\quad H = 120.4869$

$$R(\tau) = \sum_{i=89}^{262} L_i(\tau) \Big/ \sum_{i=1}^{262} L_i(\tau)$$

Solving the equation $R(\tau) = 0.665$ with initial interval (-279.9, 120.4869) gives $\tau_{50} = 119.58$. Solving the equation $G_{50}(\beta_{50}) = 0$ gives $\beta_{50} = 2.84$ which in turn gives $\alpha_{50} = 11.81$.

The values $Z_{(1)},...,Z_{(330)}$ are obtained using these estimates. The value of the Anderson-Darling test statistic is 1.392. Since the computed value of 1.392 is greater than the critical value of 0.749, the hypothesis that the observations follow a three-parameter Weibull distribution is rejected.

Prob. XII—Step 2. Compute $F_{ty}(LT)$, 0.020 to 0.125, using procedures for an unknown distribution. This computation has been carried out in Problem V, Step 2.

9.2.13 MODULUS OF ELASTICITY AND POISSON'S RATIO.—The following room-temperature elasticity values are presented in the room-temperature property tables as typical values:

Property	Units	Symbol	Recommended ASTM Test Procedures
Modulus of Elasticity			
In tension	1000 ksi	E	E 111
In compression	1000 ksi	E_c	E 111
In shear	1000 ksi	G	E 143
Poisson's Ratio	(Dimensionless)	μ	E 132

If the material is not isotropic, the applicable test direction must be specified. Deviations from isotropy must be suspected if the experimentally determined Poisson's ratio differs from the value computed by the formula

$$\mu = \frac{E}{2G} - 1 \qquad [9.2.13(a)]$$

where E is the average of E and E_c.

Given E, E_c, and G, μ may be computed by this equation. Likewise, given E, E_c, and μ, G may be computed from the equation:

$$G = \frac{E}{2(\mu + 1)} \qquad [9.2.13(b)]$$

In the event E_c is not available, E may be substituted for E in the above equations to provide an estimate of either μ or G.

9.2.14 PHYSICAL PROPERTIES.—Density, specific heat, thermal conductivity, and mean coefficient of thermal expansion are physical properties normally included in MIL-HDBK-5. Physical properties are presented in the room-temperature property table is they are not presented in effect-of-temperature curves (see Section 9.3.1.4). The basis for physical properties is "typical". Table 9.2.14 displays units and symbols used in MIL-HDBK-5, and also recommended ASTM test procedures for measuring these properties. Since modifications of procedures are employed in measuring physical properties, methods used for values proposed for inclusion in MIL-HDBK-5 should be reported in the supporting data proposal. For specific heat and thermal conductivity values reported in the room temperature property table, the reference temperature of measurement is also shown (for example) for 2017 aluminum the specific heat is 0.23 (at 212 F). For tabulated values of mean thermal expansion, temperature range of the coefficient is shown (for example 12.5 (70 to 212 F)). The reference temperature of 70 F is established as standard for mean coefficient of thermal expansion curves.

TABLE 9.2.14. *Units and Symbols Used to Present Physical Property Data and ASTM Test Procedures*

Property	Unit	Symbol	Recommended ASTM Test Procedures
Density	$lb/in.^3$	ω	C 693
Specific heat	Btu/lb-F	C	D 2766
Thermal conductivity	$Btu(hr\text{-}ft^2\text{-}F/ft)$	K	C 714[a]
Mean coefficient of thermal expansion	$10^6(in./in./F)$	α	E 228

[a]ASTM C 714 is a test for thermal diffusivity from which thermal conductivity can be computed.

9.2.15 PRESENTATION OF ROOM-TEMPERATURE DESIGN VALUES.—The proposal for the incorporation of design allowables into MIL-HDBK-5 shall contain supporting data and computations for all design properties. Depending on quantity and availability, data may be tabulated, plotted, or referenced (to readily available technical reports, specifications, etc.). Computations should indicate adequately the manner in which design values were computed and shall be presented in an orderly manner. Data sources shall be identified.

The table of room-temperature design values shall be presented in the format indicated in Figure 9.2.15(a) for conventional metallic materials. This format has been designed to accommodate most of these materials; however, some modifications may be required. For example, the format shown in Figure 9.2.15(b) shall be used for aluminum alloy sheet laminates which are generally anisotropic and have limited ductility. Design values for these hybrid materials are presented for several mechanical properties which differ from those shown for conventional metallic materials. Unused lines (for example, ST properties for sheet) are deleted. Guidance in the use of these formats may be obtained by examining tables throughout this document and by referral to the applicable procurement specification. The following instructions should be followed for the items located in Figure 9.2.15(a):

(1) Table number: If this is a revision of an existing table, use the same table number; otherwise, use a new table number in the proper sequence.

(2) Material designation: Use a numeric designation where available (for example, 7075 aluminum alloy). Avoid the use of trade names. Include products following the material designation, except products may be omitted from the title if there are many products covered by the table.

(3) Specification: Refer to a public specification (industry, Military, or Federal), followed by a type or class designation, if appropriate. Do not refer to proprietary specifications.

(4) Condition: Use a standard temper designation where applicable. Otherwise, use an easily recognized description, including pertinent details if these are not available in the reference specification. Examples: T651, TH1050, Aged (1400 F), Mill Annealed.

(5) Cross-sectional area: Use only when applicable.

(6) Location within casting: Applicable only to castings. Specify "Non-designated area," or "Designated area," as applicable.

(7) Design values shall be presented only for the thicknesses covered in the material specification.

(8) Basis: For each product and size, use two columns covering A- and B-basis properties or one column covering S-basis properties. A-values that are higher than the corresponding S-values are

TABLE ①. *Design Mechanical and Physical Properties of (material designation) ② (products)*

Specification			③	
Form				
Condition (or Temper)			④	
Cross-sectional area, in.^{2}			⑤	
Location within casting			⑥	
Thickness or diameter, in.			⑦	
Basis	S	A	B ⑧	S
Mechanical Properties:				
F_{tu}, ksi:				
L	120	120	124	
LT (or T) ⑨	...	... ⑩	...	
ST				
F_{ty}, ksi:				
L				
LT (or T)				
ST				
F_{cy}, ksi:				
L				
LT (or T)				
ST				
F_{su}, ksi				
F_{bru}, ksi:				
(e/D = 1.5) ⑪				
(e/D = 2.0)				
F_{bry}, ksi:				
(e/D = 1.5)				
(e/D = 2.0)				
e, percent (S-basis):				
L				
LT (or T)				
ST				
RA, percent (S-basis):				
L				
LT (or T)				
ST				
E, 10^3 ksi				
E_c, 10^3 ksi				
G, 10^3 ksi				
μ				
Physical Properties:				
ω, lb/in.^{3} ksi		⑫		
C, Btu/(lb)/(F)				
K, Btu/[(hr)(ft^2)(F)/ft]				
α, 10^{-6} in./in./F				

⑬ (footnotes)

FIGURE 9.2.15(a). *Format for room temperature property table.*

TABLE 7.5.X.X(b). *Design Mechanical and Physical Properties of (sheet material designation) Aluminum Alloy, Aramid Fiber Reinforced, Sheet Laminate*

Specification				
Form	Aramid fiber reinforced sheet laminate			
Laminate lay-up	2/1	3/2	4/3	5/4
Nominal thickness, in.	0.032	0.053	0.074	0.094
Basis	S	S	S	S
Mechanical Properties[a]:				
F_{tu}, ksi:				
L				
LT				
F_{ty}, ksi:				
L				
LT				
F_{cy}, ksi:				
L				
LT				
F_{su}, ksi				
F_{sy}, ksi				
F_{bru}, ksi:				
L (e/D = 1.5)				
LT (e/D = 1.5)				
L (e/D = 2.0)				
LT (e/D = 2.0)				
F_{bry}, ksi:				
L (e/D = 1.5)				
LT (e/D = 1.5)				
L (e/D = 2.0)				
LT (e/D = 2.0)				
ε_t, percent:				
L				
LT				
E, 10^3 ksi:				
L				
LT				
E_c, 10^3, ksi:				
L				
LT				
G, 10^3, ksi:				
L				
LT				
μ:				
L				
LT				
Physical Properties:				
ω, lb/in.^{3}				
C, K, and α				

[a]Design values were computed using nominal thickness of sheet laminate.

FIGURE 9.2.15(b). *Format for room temperature property table for aluminum alloy fiber reinforced sheet laminate.*

presented only in footnotes to the table. In such instances, A-values are replaced by S-values in the body of the table. When A-values are presented for some properties and S-values are presented for other properties for the same product, values shall be shown in a column labeled A-basis, and individual S-values shall be identified by appropriate footnotes. Elongation, total strain at failure, and reduction of area values are presented on an S-basis only. When other properties are presented on an A- and B-basis, add "(S-basis)" after "*e*, percent," or "ε_t percent" and "*RA*, percent." For aluminum alloy die forgings, F_{tu}, F_{ty}, and *e* shall be shown on an S-basis only for transverse, T, grain direction. To explain, add the following footnote to these values, "Specification value. T tensile properties are presented on an S-basis only." Design values for low alloy, quenched and tempered steels shall be presented on an S-basis only.

(9) Grain direction: Show design values for grain directions "L, LT, and ST" or for grain directions "L and T" for the properties F_{tu}, F_{ty}, F_{cy}, *e*, and *RA*. For aluminum-lithium sheet and plate, present design values for grain directions "L, 45°, and LT" for F_{tu}, F_{ty}, and F_{cy}. For aluminum alloy sheet laminates, show design values for L and LT grain directions of aluminum alloy sheet for all mechanical properties.

(10) Missing values: For table entries that are missing or not applicable, show a series of three dots aligned with the numbers in that column.

(11) Bearing values: Add footnote "Bearing values are dry pin values per Section 1.4.7.1" when bearing allowables are based on data from clean pin tests. Supporting information supplied with the proposal should describe the bearing test cleaning procedures used in testing.

(12) Physical properties: Include a section for physical properties even if properties are not available. If physical property data are presented in an effect-of-temperature curve, use table entry, "See Figure X.X.X.0" to refer to the illustration.

(13) Footnotes: Use footnotes to indicate anything unusual or restrictive concerning the property description, properties, or individual values; to present supplementary values; or to reference other tables or sections of text. When A-values have been replaced by S-values, the following wording is suggested: "S-basis. The A-values are as follows: (list values)."

In addition, the proposal shall contain supporting data and computations for all design properties. Depending on quantity and availability, data may be tabulated, plotted (by cumulative-probability curves or histograms), or referenced (to readily available technical reports, specifications, etc.). Computations should indicate adequately the manner in which design values were computed and shall be presented in an orderly manner. Data sources shall be identified.

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9.3 Graphical Mechanical Property Data

9.3.1 ELEVATED TEMPERATURE CURVES.—Effects of temperature and of thermal exposure on strength and certain other properties are presented graphically. Methods for determining these curves differ and are described below.

9.3.1.1 *Strength Properties.*—Tensile ultimate and yield strengths, compressive yield strength, shear ultimate strength, and bearing ultimate and yield strengths at temperatures other than room temperature (80 F) are shown as percentages of room-temperature value for that property. Use of percentage curves allows a single curve to be used in place of multiple curves when more than one room-temperature value is presented for a property, as for example, differing A- and B-design values for each of several thickness ranges. In instances where related properties differ in their response to temperature, additional curves are provided and are labeled to indicate specific properties and forms to which they apply.

No significance level is attached to these curves. For practical purposes, however, the product of a room-temperature A or B design value and an appropriate percentage value from the curve may be regarded as an A or B design value at the indicated temperature.

9.3.1.1.1 *Data Requirements.*—An idealistic approach to the establishment of elevated temperature curves would be to have A-basis design values at a sufficient number of temperatures to define corresponding temperature curves on an A-basis. If such data were available, finished curves would be constructed by plotting A-values on a percentage scale and fairing in a smooth curve, and the procedures described in Section 9.3.1.1.2 would not be considered applicable. Unfortunately, the cost of generating the required data is prohibitive, and idealism must be tempered with practicality. For this reason, data requirements and the procedures described in Sections 9.3.1.1.2 and 9.3.1.1.3 allow some latitude to make fullest use of whatever data may be available.

These procedures, as described in the following sections, are intended both to establish the general shape of curves, and to adjust their scaling in such manner that the resulting product of a percentage value from the curve and a corresponding value from the room-temperature property table will yield a design value, at some designated temperature, that will be a good approximation of a directly computed design value at that temperature.

To establish the shape of an elevated-temperature curve, sample shall include observations from at least five lots* of material composed of at least two heats at each of several temperatures. Choice of temperatures shall be guided by probable range of service temperatures anticipated for the material, as well as by its metallurgical characteristics. For materials used at cryogenic temperatures, testing is normally conducted at -110, -320, and -423 F; however, no attempt shall be made to extrapolate the curve below the lowest temperature for which adequate data are available. For elevated temperature applications, data should normally be available at temperature intervals from 200 to 300 F except in regions of time-temperature-dependent metallurgical change, where temperature intervals of perhaps 100 to 150 F are appropriate. Extrapolation beyond the range of temperatures covered by adequate data is not allowed.

For a number of alloys, most specifically heat-resisting alloys, procurement specifications may designate minimum property values at temperatures other than room temperature, and either A- or S-basis values may be available at both room temperature and secondary testing temperatures. When this is the case, the elevated temperature curve may be scaled by means of these values.

*For single form and thickness, data from no more than one heat treat lot per heat may be used to meet the five lot requirement.

9.3.1.1.2 *Determination of Working Curves.*—Working curves for each product form, heat treat condition, property, and grain direction should be constructed. Separate curves should be examined to determine if certain data can be combined. For example, it may be possible to combine data for sheet and plate, T73 and T7351 tempers, tensile and compressive yield strengths, or longitudinal and long transverse grain directions.

The dimensional units of these working curves shall be in terms of percentages of corresponding room-temperature value for the property. A percentage may be determined for each lot by dividing the average value of individual measurements (other than at room temperature) by the room-temperature average value for the same lot of material in the same testing direction (for isotropic materials, testing direction may be ignored), then multiplying by 100 to convert from a fraction to a percentage.

At each working temperature, the lower 95 percent confidence interval estimate (reduced ratio) of mean percentage shall be determined from percentage values for each lot at that temperature. Letting r equal percentage values, $\bar{r}$ the average of these values, and n the number of such percentages, estimated standard deviation(s), and reduced ratio (R) shall be determined from the equation:

$$s^2 = \Sigma(r - \bar{r})^2/(n - 1) \qquad [9.3.1.1.2(a)]$$

or

$$s^2 = [\Sigma(r^2) - (\Sigma r)^2/n]/(n - 1) \quad , \qquad [9.3.1.1.2(b)]$$

and

$$R = \bar{r} - t\, s/\sqrt{n} \qquad [9.3.1.1.2(c)]$$

where t is 0.95 fractile of the t distribution corresponding to n-1 degrees of freedom (see Table 9.6.4.5).

The working curve shall be a smooth curve drawn through 100 percent at room temperature and not higher than the computed values of R at each working temperature. When only room-temperature minima are applicable, no further adjustment of the working curve is required. However, when a secondary testing temperature is specified for the property, the working curve shall be lowered, if required, so that the product of percentage from this curve and a room-temperature S-value shall not exceed the S-value at the secondary testing temperature. In addition, if A-basis values have been established for this temperature, the working curve shall be lowered, if required, so that the product of the percentage from this curve and room temperature A-value shall not exceed the A-value at the secondary testing temperature.

Each working curve shall be labeled appropriately, designating product, property, and testing direction(s) covered by it. In addition, individual percentages, including R values and (if applicable) secondary A or S-values reduced to percentages, shall be plotted with the working curve. An example of a working curve is shown in Figure 9.3.1.1.2.

9.3.1.1.3 *Preparation of Finished Curves.*—When two or more working curves are to be combined into a single curve, percentages shown in the finished curve shall represent the separate bound of all individual working curves used in its preparation. When corresponding working curves differ substantially in shape or scaling, it may be appropriate to prepare more than one finished curve (for example, separate curves for longitudinal and transverse testing directions). Finished curves shall not exhibit

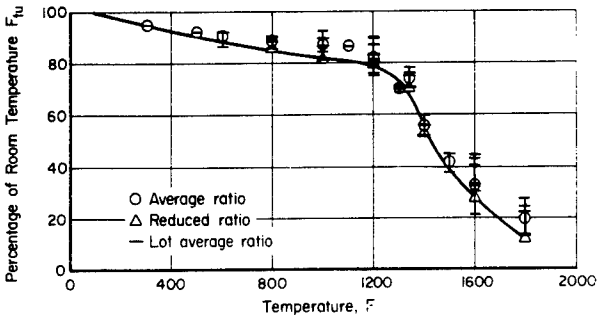


FIGURE 9.3.1.1.2. *Working curve drawn through reduced ratios converted to percentages.*

"humps", such as might appear with a temperature range where aging takes place. Where such humps appear in working curves, these shall be leveled by means of horizontal line segments.

Finished curves shall be drawn in reproducible form on grids of 10 lines to the inch, with each tenth line accented. The ordinate shall normally be scaled in units of 20 percent per inch and shall be labeled "Percentage of Room Temperature Strength". Abscissa shall be scaled in units of 100, 200, or 400 F per inch, as appropriate, and shall be labeled "Temperature, F". Both axes shall be annotated at intervals of 1 inch. Not more than two curves shall be drawn in a single figure, and these should be labeled clearly to distinguish between them. In addition, each figure shall carry a legend containing the words "strength at temperature", together with exposure limits and other information that would limit the applicability of the curve.

An example of the finished percentage curve is shown in Figure 9.3.1.1.3(a). When practical, single percentage curves, representing F_{tu} and F_{ty} may be located on a single illustration as shown in Figure 9.3.1.1.3(b). Likewise, single curves representative of F_{cy} and F_{su} may be located on one illustration and curves for F_{bru} and F_{bry} may also be placed on a single illustration.

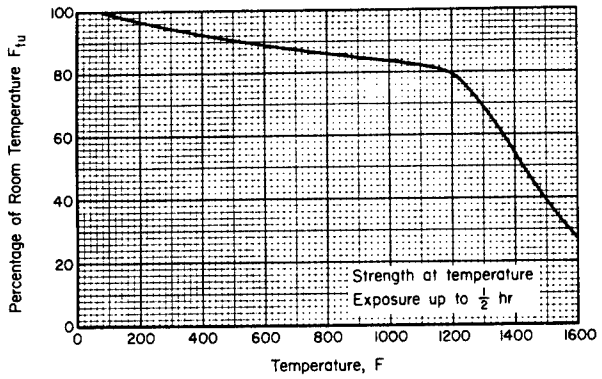


FIGURE 9.3.1.1.3(a). *Working curve from Figure 9.3.1.1.2 redrawn as finished curve.*

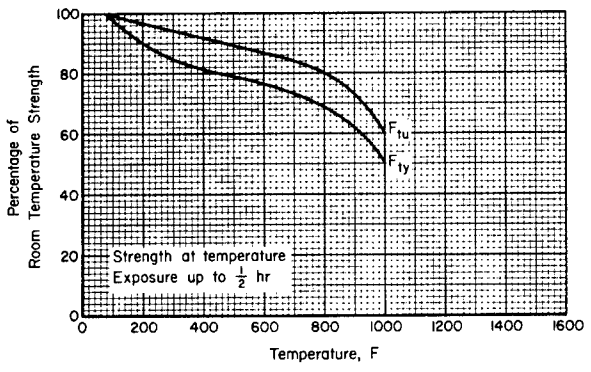


FIGURE 9.3.1.1.3(b). *Multiple percentage curves located on a single illustration.*

9.3.1.2 *Elongation and Reduction of Area.*—Elongation and reduction of area are presented as "typical" values at each temperature. If ductility values follow a log-normal distribution, they should be converted to logarithms before averaging. In most cases, the median (middle-most value) will be nearly identical to the average determined in this manner. Ductility values are not converted to percentages of

the room-temperature value. Hence, a best smooth curve drawn through the typical values at each temperature is merely redrawn without data points for presentation in the document, as shown in Figure 9.3.1.2. Separate curves may be required for products differing in ductility.

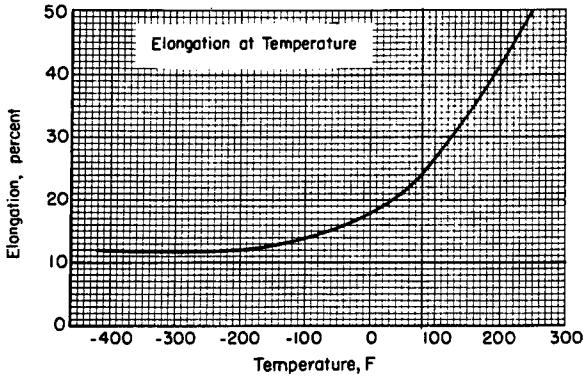


FIGURE 9.3.1.2. *Typical curve for elongation.*

As with strength data, care must be taken to avoid biasing the curve by the inclusion of large quantities of data from some lots and small quantities from others. Use of lot-average values in place of individual measurements is highly recommended.

9.3.1.3 *Modulus of Elasticity.*—The elastic modulus may vary with test direction and product form. Data should be examined before plotting, and if differences are observed, separate working curves should be prepared for each variable. The percentage curve for modulus of elasticity is a best-fit smooth curve drawn through the average of all percentages at each temperature, where individual percentage values are obtained as described in Section 9.3.1.1.2. As with strength data, temperatures should be so selected that the shape of the curve is defined adequately. Figure 9.3.1.3 illustrates a finished percentage curve representing two moduli, E and E_c, for which working curves were similar enough to permit their combination into a single curve.

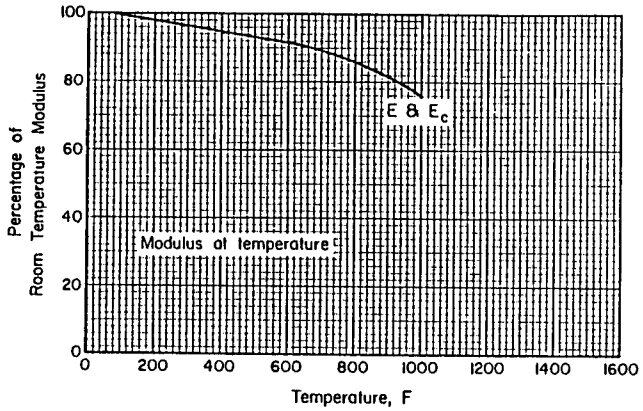


FIGURE 9.3.1.3. *Percentage curve representing two elastic moduli.*

9.3.1.4 *Physical Properties.*—When data are adequate to present curves showing specific heat, thermal conductivity, and mean coefficient of thermal expansion over a range of temperatures, graphical presentation is used in place of tabular presentation described in Section 9.2.1.3. Working curves are first prepared for each property with the actual data plotted over the range of test temperatures.

Figure 9.3.1.4(a) shows a typical working curve. A best-fit smooth curve is drawn through the plotted points to depict the overall trend of data. The smooth curves from the specific heat, thermal conductivity, and thermal expansion working curves are then shown in a single figure as illustrated in Figure 9.3.1.4(b). The reference temperature for thermal expansion should be shown on the figure. In

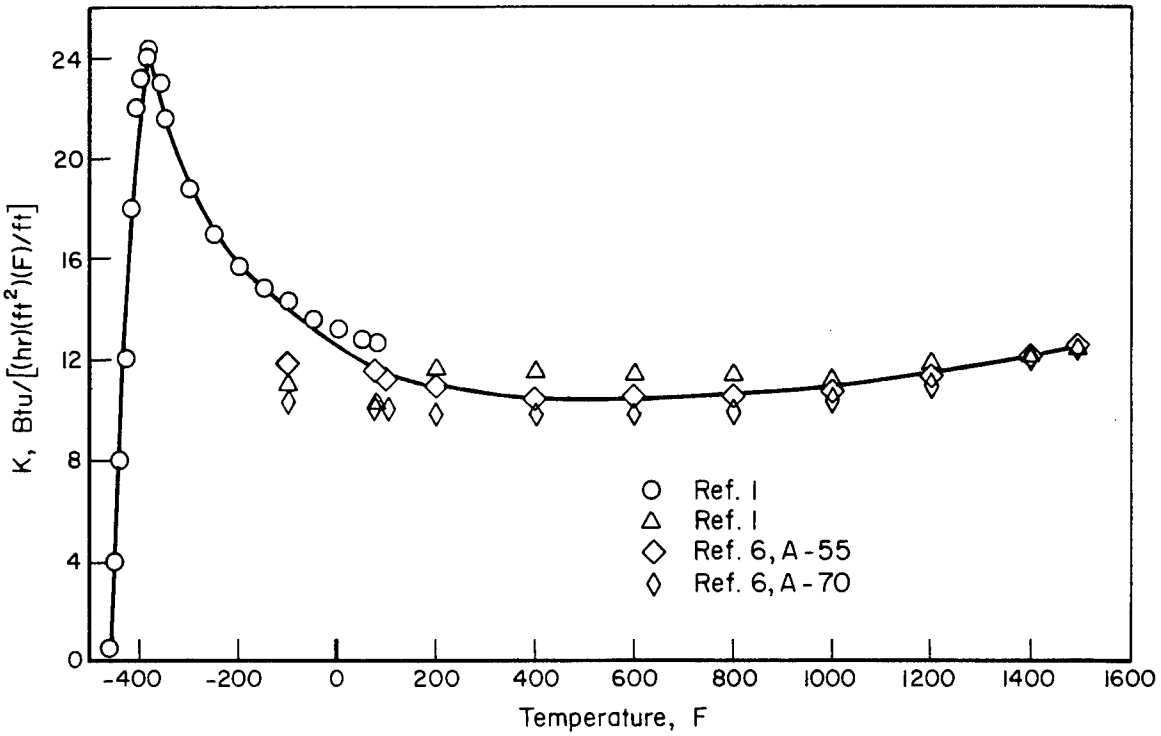


FIGURE 9.3.1.4(a). *Typical working curve for thermal conductivity.*

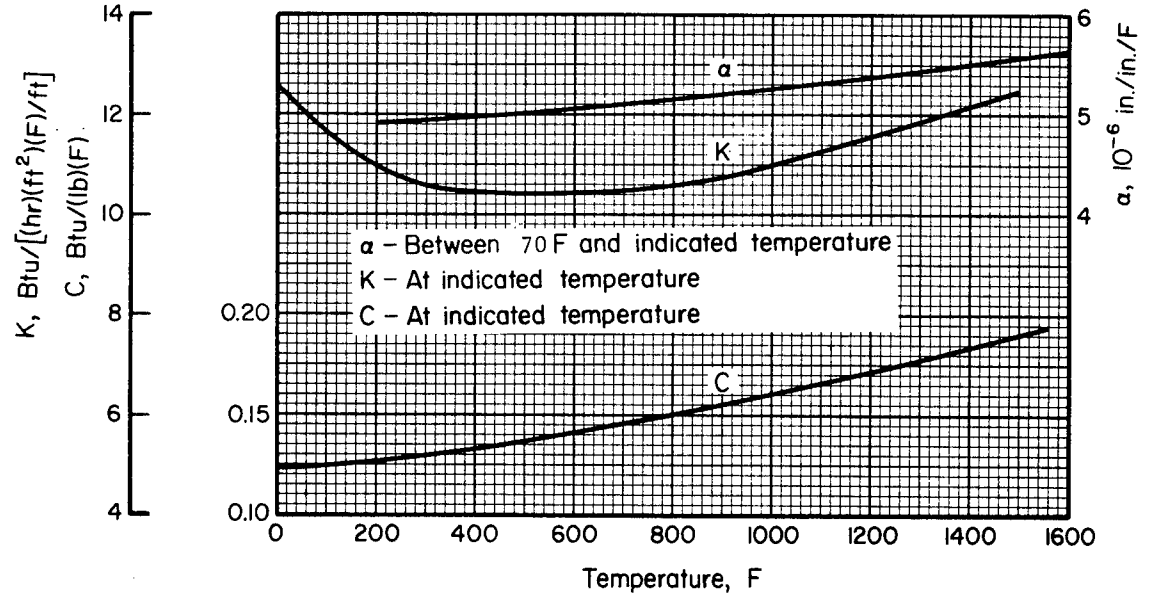


FIGURE 9.3.1.4(b). *Typical curves for physical properties.*

Figure 9.3.1.4(b) the reference temperature of 70 F indicates that the mean coefficient of expansion between 70 F and the indicated temperature is plotted.

9.3.1.5 *Effect of Thermal Exposure on Room-Temperature Strength.*—Curves described in this section are presented (1) when the material exhibits a decrease in room-temperature strength as a result of unstressed exposure to elevated temperatures, and (2) when data are not presented in the form of parametric curves (see "Complex-Exposure" in Section 9.3.1.6.2). Supporting data expressed as percentages of the "no-exposure" strength are plotted with percent of room-temperature strength as the ordinate and exposure temperature as the abscissa. Separate plots are required for each exposure time. Typical exposure times are 1/2, 10, 100, and 1000 hours. Design curves are drawn in the same manner as for effect of temperature on strength; humps that may appear in the design curve should be leveled off in drawing the final curve.

The following restrictions are placed on effect-of-exposure curves for strength properties at room temperature:

(1) Percentage curves for a designated exposure temperature may not show increasing percentage values with increasing exposure time.

(2) Percentage curves for a designated exposure time may not show increasing percentage values with increasing exposure temperature.

A typical effect-of-exposure curve is illustrated in Figure 9.3.1.5.

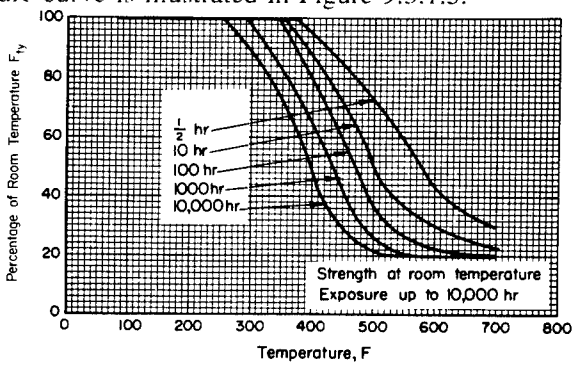


FIGURE 9.3.1.5. *Effect of exposure at elevated temperatures on room-temperature properties.*

9.3.1.6 *Effect of Thermal Exposure on Elevated Temperature Strength.*—The effect of thermal exposure on elevated-temperature strength is presented in one of two manners, depending upon whether or not the exposure temperature equals the test temperature. In the case of simple exposure, exposure temperature and test temperature are assumed to be identical. For complex exposure, exposure temperature and test temperature need not be the same. When either of these curves is presented in MIL-HDBK-5, it includes all information normally presented in elevated temperature curves described in Section 9.3.1.1; thus, these curves replace the elevated temperature curves.

9.3.1.6.1 *Simple Exposure.*—The curves are prepared in the same manner as basic elevated temperature curves described in Section 9.3.1.1. Separate design curves are prepared for each exposure time, and presented in a single figure. Typical exposure times for the curves are 1/2, 10, 100, and 1000 hours.

The following additional restrictions are placed on effect-of-exposure curves for strength properties at elevated temperatures:

(1) Percentage curves for a designated exposure (test) temperature may not show increasing percentage values with increasing exposure time.

(2) Percentage curves for a designated exposure time may not show increasing percentage values with increasing exposure (test) temperature.

A typical set of curves for exposure at test temperature is illustrated in Figure 9.3.1.6.1.

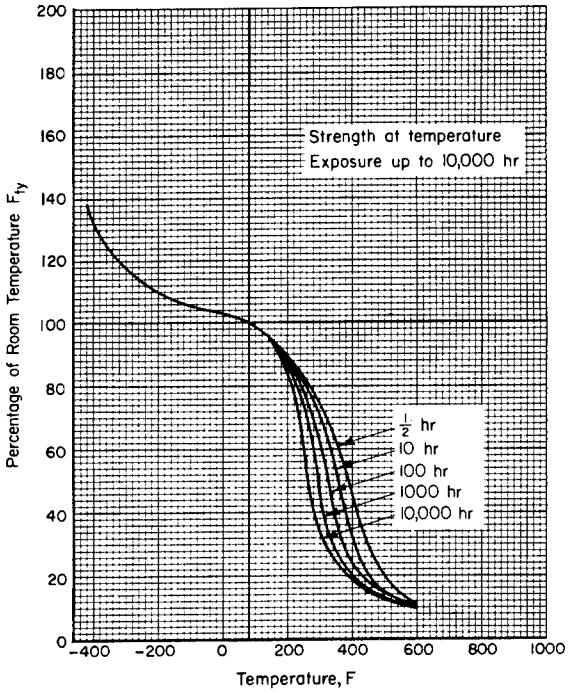


FIGURE 9.3.1.6.1. *Simple-exposure curves.*

9.3.1.6.2 *Complex Exposure.*—In these curves, thermal-exposure variables, time, and temperature are combined into an exposure parameter, which is plotted as the abscissa. The ordinate is expressed in the same manner as in effect-of-temperature curves. Separate percentage curves are presented for each test temperature. In addition, each figure contains a nomograph for use in converting exposure time and temperature to the exposure parameter.

The exposure parameter may be of the form $P = (T_F + 460)(C + \log t)$, where T_F is exposure temperature in degrees F, C is a constant, and t is exposure time in hours. There are a number of ways to determine the values of C. The simplest method is to select (by interpolation of test data) two exposure conditions that produce the same strength at some designated test temperature, set two parameters equal to each other, and solve for C. For example, assume that the following data are obtained:

Exposure		
Time, hr	Temp, F	TUS at 400 F, ksi
1000	400	80.0
1	500	83.0
10	500	78.0

Plot 500 F data as stress versus log time; a straight line between (83, log 1) and (78, log 10) crosses 80 ksi at log 4 (hours). Thus, 4 hours' exposure at 500 F is equal to 1000 hours' exposure at 400 F:

$$(400 + 460)\,(C + 3) = (500 + 450)\,(C + 0.602)$$
$$C = 20.$$

This exercise should be repeated for several pairs of exposure conditions to obtain an average value for C.

Alternatively, several equivalent exposure conditions may be plotted as log exposure time (ordinate) versus $1/(T_F + 460)$ (abscissa). A best-fit straight line is drawn through the plotted points and its slope determined. C is then found from the relationship

$$C = m/(T_F + 460) - \log t,$$

where m is slope and $(1/T_F + 460)$ and log t are coordinates of any point on the line. This method is amenable to data-regression procedures described in Section 9.6.4.3, from which a least-squares estimate of C is obtained.

Separate data plots are prepared for each test temperature, using percent of "no-exposure" room-temperature strength as the ordinate, and $P = (T_F + 460)\,(C + \text{lot t})$ as the abscissa. Design curves are then drawn as described in Section 9.3.1.1.2.

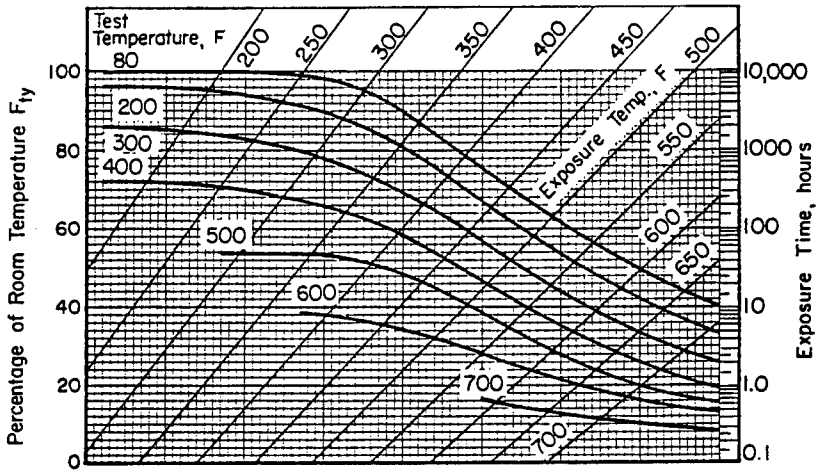


FIGURE 9.3.1.6.2. *Complex-exposure curves.*

A typical complex-exposure curve is illustrated in Figure 9.3.1.6.2. It should be noted that the abscissa scale is not shown in the figure since the time-temperature nomograph is used directly to locate the position on the abscissa.

9.3.2 TYPICAL STRESS-STRAIN, COMPRESSION-TANGENT-MODULUS, AND FULL-RANGE STRESS-STRAIN CURVES

9.3.2.1 *Introduction.*—The stress-strain and tangent-modulus data appearing in MIL-HDBK-5 are described as "typical" stress-strain and compression-tangent-modulus curves. The term typical indicates that representative stress-strain data for products covered have been adjusted to reflect precision typical values of the elastic modulus, and product average values of the 0.2 percent offset yield strength in tension or compression. Curves extend to strain somewhat beyond the 0.2 percent offset yield strength. Curves described as "full-range" stress-strain curves, are also included in MIL-HDBK-5. These curves extend through maximum load and beyond to rupture.

All curves will be prominently marked "typical". With regard to tension data, only stress-strain curves are shown; however, compression data should include stress-strain curves and tangent-modulus curves. The Ramberg-Osgood n exponent should appear on all stress-strain curves if n is shown to apply in the approximate range from proportional limit to yield strength. The procedures and methods to be used are described in the following paragraphs.

Two alternative procedures are described for determining typical stress-strain curves.

(1) The "strain-departure" method, which assumes no parametric relationship between stress and plastic strain, utilizes the full stress-strain curve.

(2) The Ramberg-Osgood method, which assumes an exponential relationship between stress and plastic strain. Its use requires as few as two points from the original stress-strain curve, once the exponential relationship has been found to be applicable.

Generally, the two methods yield nearly identical results for those portions of the curve lying between proportional limit and yield stress. For plastic strains greater than about 0.002 in./in. and for bimetallic or clad products, only the strain-departure method is applicable.

Stress-tangent modulus curves may be derived graphically from compressive stress-strain curves, or computed, if the Ramberg-Osgood method is used.

9.3.2.2 *Data Requirements.*—Preparation of each typical stress-strain curve requires (1) several representative original stress-strain curves, (2) average values for yield strength from original stress-strain curves, or, when available, product average values for yield strength, and (3) typical precision elastic-modulus values at test temperature.

Original stress-strain curves are utilized to obtain a representative curve shape which may be characterized by the Ramberg-Osgood parameter. The minimum number of original stress-strain curves required is dependent on the degree of variation from one curve to another. If curves are found to be similar in shape, and the range of products (thickness, etc.) is small, one curve from each of three plots should be adequate. Otherwise, the number of original curves should be increased as necessary to insure an adequate sampling.

Original stress-strain curves determined using an ASTM E 83 Class A extensometer (TUCKERMAN, Martens, etc.) are preferred for preparation of typical stress-strain curves up to 0.005-in./in. plastic strain or higher. When curves having this precision and accuracy are not available (particularly for full-range and elevated-temperature curves), curves determined using Class B-1 extensometers may be used as indicated in ASTM E 83.

Product average values for yield strength, ultimate strength, and elongation are average values rounded to the nearest whole number determined from production lots of product form. Product average values represent current production capabilities; hence, these are supplied by producers.

Elastic modulus values are considered to be those obtained with Class B-1 or better extensometers as indicated in ASTM E 83. Typical values for elastic moduli at room temperature are tabulated in MIL-HDBK-5 room-temperature property tables. Values for these properties at other temperatures may be approximated by multiplying the room-temperature value by appropriate percentages from effect-of-temperature curves in MIL-HDBK-5. The modulus value used in constructing a stress-strain curve must agree with the value obtained from the room-temperature table value multiplied by the appropriate percentage from the elevated temperature curve.

For some materials, the shape of the stress-strain curve, yield strength, and elastic modulus vary with test direction. When this is the case, individual curves should be prepared for each test direction, and each curve should be labeled accordingly. Likewise, tensile and compressive stress-strain curves usually differ, and individual curves should be prepared for each type of loading. If two or more finished curves are found to be identical, they may be combined in presenting the finished curves.

The selection of test temperatures to be represented by typical stress-strain curves should be guided by the temperatures at which the product is typically used. In the absence of other information, these temperatures should include room temperature, other temperatures at which tensile properties are determined in conformance with the requirement of applicable procurement specifications, and appropriate temperatures within the useful application range for the product.

9.3.2.3 *Strain-Departure Method.*—These steps, as illustrated in Table 9.3.2.3, should be followed to establish a typical tensile or compressive stress-strain curve using the strain-departure method:

(1) The straight-line (modulus) portion of each curve should be extended as in Figure 9.3.2.3(a), and the 0.002 (0.2%) offset yield strength should be indicated.

(2) At appropriate departures or offsets from the modulus line, load should be determined accurately, converted to stress, and recorded. Sufficient departure measurements should be made to accurately describe the curve to just beyond yield load for each load-strain curve.

(3) At each strain departure, the stresses should be averaged.

(4) When a product average yield strength value is available, the average stresses at each departure should be converted to product average stresses.

(5) Elastic strains should be computed for each departure. (Elastic Strain equals Total Stress/Elastic Modulus.)

(6) Elastic strains (computed) and plastic strains (departure) should be added to obtain total strain for each departure.

The following guidelines should be used to plot a typical stress-strain curve. The graph axis should be laid out such that there are 10 minor divisions for every major division with every tenth (major) division accented. The ordinate (Y-axis) is used for stress and should be scaled in units of 5, 10, 20, or 50 ksi to the major division, as appropriate, to produce a total scale length of approximately 5 major divisions. The abscissa (X-axis) is used for total strain and should be scaled in units of 0.001 or 0.002 in./in. to the major division, as appropriate, to produce a total scale length of approximately 6 major divisions.

TABLE 9.3.2.3. *Example of Use of Strain Departures to Establish Typical Stress-Strain Curve as Described in Section 9.3.2.3.*

	Stress, ksi					Strain, μ in./in.	
Departure (D) μ in./in.	Test #1	Test #2	Test #3	Average[a] (σ_A)	Product average[b] (σ_T)	Elastic[c] (ε_E)	Total[d] (ε_T)
0	43.81	42.75	41.20	42.59	42.63	4022	4022
20	49.77	48.81	45.14	47.91	47.95	4524	4544
40	51.41	50.98	47.82	50.17	50.12	4728	4768
100	54.31	53.96	51.24	53.17	53.22	5021	5121
500	60.16	60.37	57.10	59.21	59.27	5592	6092
1000	62.67	62.85	59.45	61.66	61.72	5823	6823
2000	64.95	65.06	61.80	63.94[f]	64.00[e]	6038	8038
2200	65.26	65.38	62.12	64.25	64.31	6067	8267

[a]Average of Tests 1, 2, and 3.
[b]σ_T = (Product average yield strength ÷ average yield strength) x σ_A.
[c]$\varepsilon_E = \sigma_T/E$.
[d]$\varepsilon_T = \varepsilon_E + D$.
[e]Product average yield strength.
[f]Average yield strength.

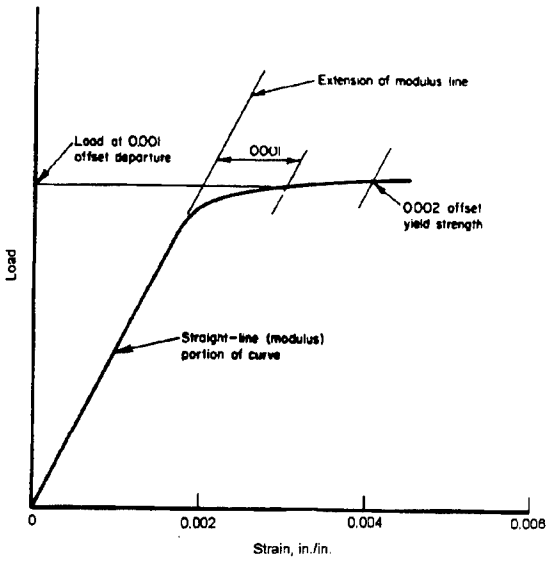


FIGURE 9.3.2.3(a). *Measuring loads by strain departure method.*

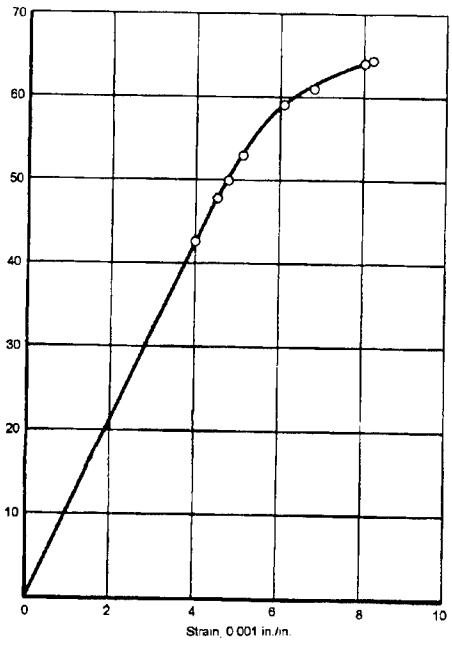


FIGURE 9.3.2.3(b). *Plotted data from Table 9.3.2.3.*

The final step is plotting the values in Table 9.3.2.3 to produce the typical stress-strain curve as shown in Figure 9.3.2.3(b). In addition to plotting the graphs by hand, they may be plotted with computer software programs. In the latter case, input the stress-strain pairs (σ_T and ε_T) from Table 9.3.2.3 into the computer and then curve fit the data. In all cases, the elastic section must be linear up to the proportional limit. It is recommended that the Ramberg-Osgood equation be used to fit the data from the proportional limit to just beyond the 0.2% yield stress. If not, a power-law polynomial second order may be used to fit the data points. The stress-strain curve should extend slightly beyond the 0.2% yield strength.

To complete the figure, the Ramberg-Osgood number from Section 9.3.2.4 and the typical yields strength (TYS) product average must be contained in a table within the figure. If more than one curve is contained in the figure, information such as the grain direction (L, LT, and ST), and/or temperature for each curve must be indicated in the figure. Figure 9.3.2.3(c) shows the proper format of a figure for presentation in Chapters 2 through 7.3.

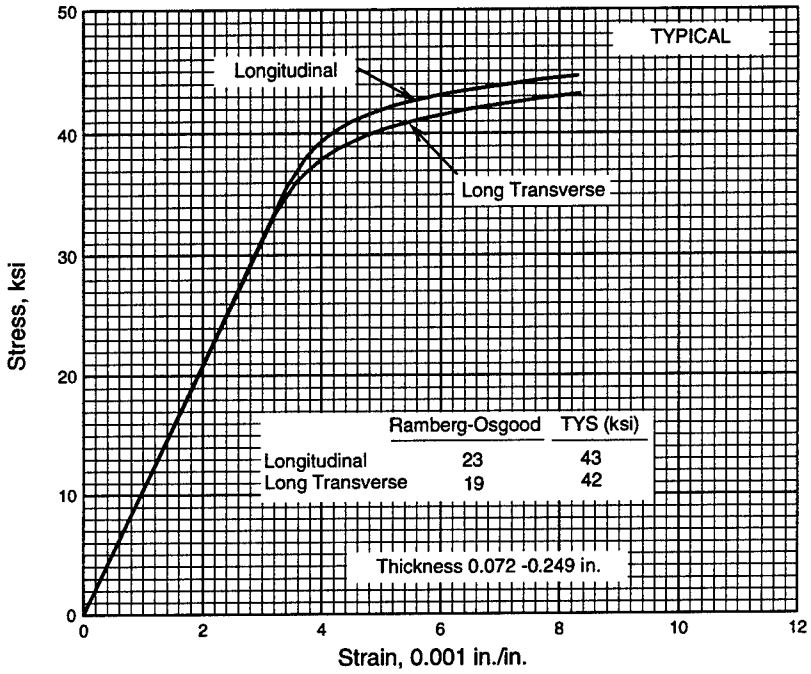


FIGURE 9.3.2.3(c). *Typical stress-strain curves showing the proper presentation format.*

9.3.2.4 *Ramberg-Osgood Method.*—This method, which is based on the work of Ramberg and Osgood [Reference 9.3.2.4(a)], and Hill [Reference 9.3.2.4(b)], assumes that an exponential relationship exists between stress and plastic strain, as expressed by

$$e_p = 0.002 \left(\frac{f}{f_{.2ys}} \right)^n \qquad [9.3.2.4(a)]$$

where

f is stress,

$f_{0.2ys}$ is the 0.2 percent yield stress,

e_p is plastic strain,
n is the Ramberg-Osgood parameter*.

While this relationship may not be exact, it is sufficiently accurate for use up to the yield strength for many materials, but cannot be employed to compute full-range stress-strain curves.

Since total strain equals elastic strain plus plastic strain,

$$e_{total} = f/E + 0.002\left(\frac{f}{f_{.2ys}}\right)^n \qquad [9.3.2.4(b)]$$

where E is the typical value of modulus of elasticity from the room-temperature property tables.

Equation 9.3.2.4(b) can be programmed for determination and plotting by a computer, given only values for E, n, and $f_{0.2ys}$. To obtain typical curves, TYS or CYS is used for $f_{0.2ys}$. TYS and CYS values are based on product averages when available; in other cases, average values from original stress-strain curves are used. The Ramberg-Osgood parameter, n, shall be determined analytically in development of typical stress-strain curves for MIL-HDBK-5.

As the first step in the analytical determination of n, a series of values of stress and strain departure (plastic strain) must be obtained from each original stress-strain curve. These may be determined by the method of strain-departure described in Section 9.3.2.3 or the alternate method outlined below:

(1) Determine the indicated modulus of elasticity for the individual stress-strain curves.

(2) For each curve, construct two lines parallel to the modulus line and intersecting the stress-strain curve at plastic strains ofapproximately 0.020 and 0.20 percent. The lines will bound the zone where stress-plastic strain pairs are determined. This zone also eliminates the small plastic strain region where nonlinearities in stress versus plastic strain sometimes exist.

(3) Digitize each stress-strain curve over the range bounded in Step 2. A series of approximately ten to 12 pairs of stress-total pairs should be taken at nearly equal intervals within this range. A resolution of 0.25 ksi stress and 0.01 percent strain is desirable here.

(4) Compute plastic strains from each collection of total strains, using the individual curve's modulus to subtract out elastic strains.

Once the stress and plastic strain values are tabulated for available stress-strain curves, it is possible to proceed with determination of the Ramberg-Osgood parameter. To determine n analytically, Equation 9.3.2.4(a) is rearranged to solve for stress, f, the dependent variable.

$$f = Ae_p^{1/n} \qquad [9.3.2.4(c)]$$

where

$$A = \frac{f_{.2ys}}{(0.002)^{1/n}} \qquad [9.3.2.4(d)]$$

* The Ramberg-Osgood parameter, n, should not be confused with the strain hardening coefficient, which is also denoted by the letter n. The one is the reciprocal of the other. Values of the Ramberg-Osgood parameter usually lie within the range of 2 to 40. It should be noted that an occasional practice in the aircraft industry, but not followed in MIL-HDBK-5, is to subtract a small increment of strain from Equation 9.3.2.4(a) in order to compensate for the existence of a proportional limit.

Taking the natural logarithm of Equation 9.3.2.4(c), a transformed equation is obtained which can be analyzed by the method of linear least squares.

$$\ln f = \ln A + 1/n \ln e_p \qquad [9.3.2.4(e)]$$

The solution for n is the same as that for a linear regression least-squares estimate of the slope, b, as shown in Section 9.6.3.1, Equation 9.6.3.1(d) where b = 1/n, therefore,

$$n = \frac{\Sigma x^2 - \frac{(\Sigma x)^2}{N}}{\Sigma xy - \frac{\Sigma x \, \Sigma y}{N}} \qquad [9.3.2.4(f)]$$

where $x = \ln e_p$
$y = \ln f$
N = number of data points.

Correspondingly, A can be obtained from Equation 9.6.3.2(d) as

$$\ln A = \frac{\Sigma y - \frac{1}{n} \Sigma x}{N} \qquad [9.3.2.4(g)]$$

Values for stress and strain departure may be input for solution of Equation 9.6.3.2(f) by either of two methods. In one method, $x = \ln e_p$ and $y = \ln f$ are input for each value of stress and strain departure for each stress-strain curve used in the analysis. N is the total number of points obtained from stress-departure analysis of all specimens from all heats that are analyzed. Care should be taken to ensure that the same number of data points are collected from each curve. In the other method, average stress (f) is determined for all available curves at designated values of strain departure (e_p). In this case, x and y in Equation 9.6.3.2(f) are $\ln e_p$ and $\ln f$, respectively, and N is the number of strain departure points. Again, the same number of data points should be computed for each stress-strain curve.

Some investigators may analyze the results of each individual specimen by the method outlined by Equations 9.3.2.4(c) through (g) and record individual values of the parameter n. In these cases, an alternate approach must be used to combine results and establish n. This technique is called the method of computed strain-departure.

In the method of computed strain-departure, results from individual specimen analyses are used to compute stress levels [from Equation 9.3.2.4(c)] at specific strain-departure levels for all specimens. In so doing, the original data are used to analytically perform the method of strain-departure of Section 9.3.2.3 which should be used as a guideline for doing this analysis. Once these computed stress values are obtained, they can be used to calculate the exponent, n, by Equation 9.3.2.4(f) using either of the two methods that are described above for the case when data are recorded by the method of strain-departure.

An approximate value of the Ramberg-Osgood parameter can be found graphically, although this approach shall not be used to construct stress-strain curves for MIL-HDBK-5. Graphically determined stress-strain curves must be verified by computer analysis according to previously described techniques before inclusion in MIL-HDBK-5. A graphical procedure is described in the following paragraphs and is illustrated in Figure 9.3.2.4.

(1) Plot at least three pairs of stress-plastic strain points from each original stress-strain curve on log-log graph paper. As illustrated in Figure 9.3.2.4(a), the ordinate is conventionally used for log stress, the abscissa is log plastic strain (strain departure method is described in Section 9.3.2-.3), and the slope is 1/n.

(2) A straight line then is drawn through the plotted points and the slope (1/n) is computed as shown in the figure.

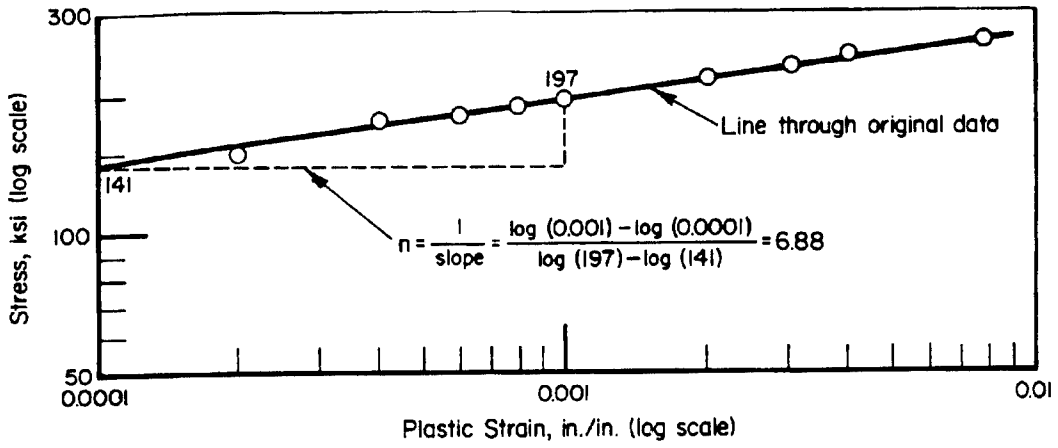


FIGURE 9.3.2.4. *Graphical approximation of Ramberg-Osgood Parameter, n.*

When using the above-described approaches, it is recommended that a check be made to determine how well the value of n reproduces the stress-strain curve in the approximate range from the proportional limit (defined as 0.02% ys) to $f_{0.2ys}$. This can be done by constructing the stress-strain curve using Equation 9.3.2.4(b), and comparing an original stress-strain curve through the yield strength with the computed curve. In checking an original stress-strain curve with the computed curve, some judgment must be exercised in the vicinity of the proportional limit since the Ramberg-Osgood relationship may not precisely represent original stress-strain curves in this area. Stress deviations greater than about 5 percent between the two curves suggest that the Ramberg-Osgood relation is not applicable.

9.3.2.5 *Compression-Tangent-Modulus Curves.*—In deriving tangent-modulus curves graphically from typical compressive stress-strain curves, a number of points are marked off on the latter curves, particularly where the curve departs from linearity and in regions of greatest curvature. At each point on the curve, a line is drawn tangent to the curve as shown in Figure 9.3.2.5(a). The slope of each line is the tangent modulus corresponding to the stress coordinate of the point of tangency. The Ramberg-Osgood relationship, Equation 9.3.2.4(b),

$$e_{total} = f/E + 0.002\left(\frac{f}{f_{0.2ys}}\right)^n$$

also may be employed to determine the compression-tangent-modulus curve.

Tangent modulus is the first derivative of stress with respect to strain, df/de, or

$$E_t = \frac{1}{\frac{1}{E} + \frac{0.002n}{f_{0.2ys}}\left(\frac{f}{f_{0.2ys}}\right)^{n-1}} \qquad [9.3.2.5(a)]$$

This equation can be programmed for determination and plotting by a computer, given only values for E, n, and $f_{0.2\%ys}$. To obtain typical curves, average CYS is used for $f_{0.2\%ys}$.

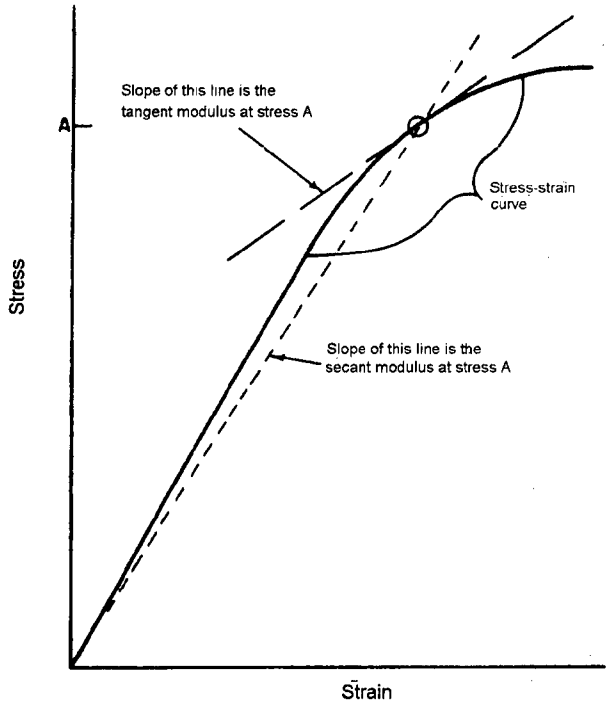


FIGURE 9.3.2.5(a). *Determining tangent modulus and secant modulus.*

The following guidelines should be used to plot a compression tangent-modulus curve. The graph axis should be laid out such that there are 10 minor divisions for every major division with every tenth (major) division accented. The ordinate (Y-axis) scale is plotted in the same manner as that used for the stress-strain curves in Section 9.3.2.3. The abscissa (X-axis) scale is usually made equal to 2, 4, or 5 x 10^3 ksi per major division, depending on material, to produce a total scale length of approximately 6 major divisions.

The compression tangent-modulus curve is illustrated in Figure 9.3.2.5(b) where stress is plotted (on the ordinate) versus tangent modulus (on the abscissa). In addition to plotting the graphs by hand, they may be plotted with computer software programs. In the latter case, input the stress-modulus pairs (σ_T and E_t) from equation 9.3.2.5(a) into the computer or program the computer with the equation and then curve fit the data. If it will not lead to confusion, stress-tangent modulus curves may be superimposed on the corresponding stress-strain figures as illustrated in Figure 9.3.2.5(c). If, however, several stress-strain curves appear in one figure, it is advisable to present stress-tangent modulus curves in a separate figure, as illustrated in Figure 9.3.2.5(b).

The compression tangent modulus curves for clad material should show a primary and secondary modulus as indicated in Figure 9.3.2.5(d). The stress-strain curves of clad material may indicate two modulus lines due to the cladding. The primary modulus is due to the combined modulus of both clad and base materials. However, the clad material is typically weaker than the base material and will yield at a low stress; therefore not contributing to the modulus at higher stresses. At this point, the secondary modulus becomes predominate. The compression tangent-modulus curves should show the primary and secondary modulus and indicated in Figure 9.3.2.5(d).

To complete the figure, the Ramberg-Osgood number from Section 9.3.2.4 must be contained in a table within the figure. If more than one tangent modulus curve is contained in the figure, information

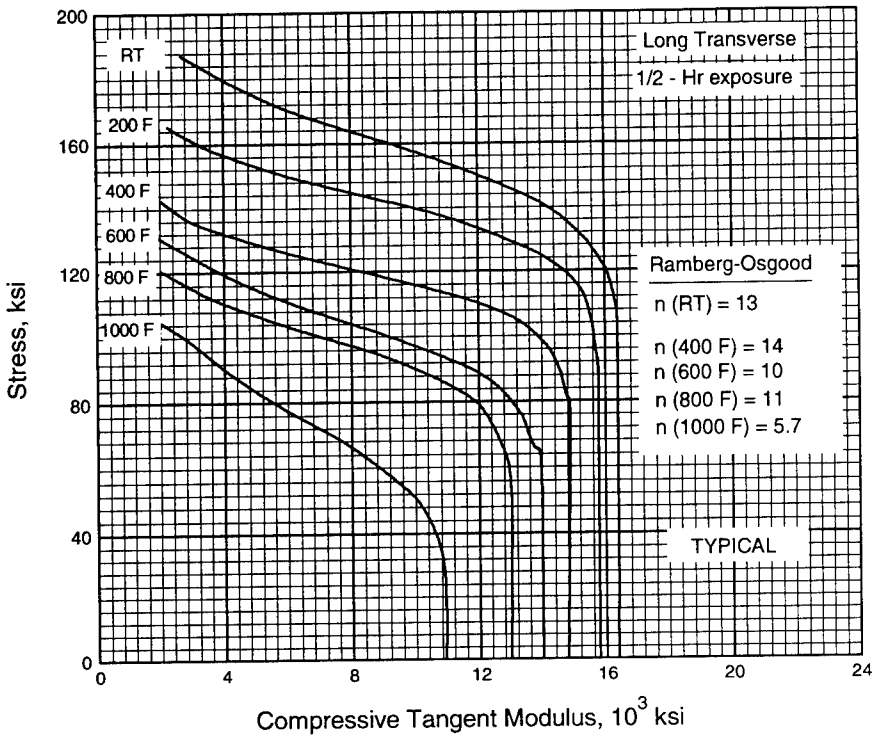


FIGURE 9.3.2.5(b). *Typical stress-tangent modulus curves.*

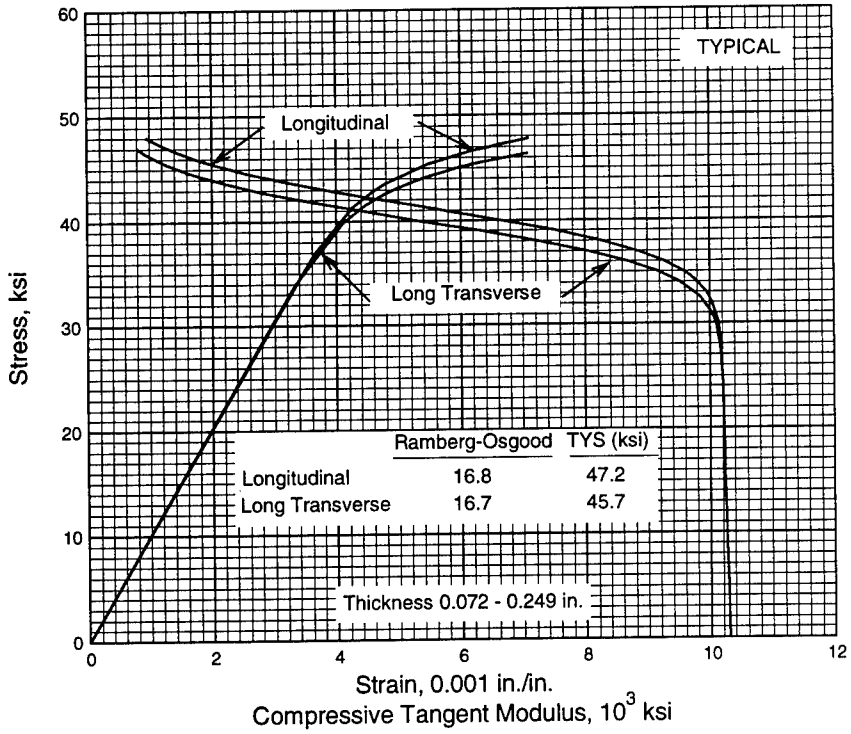


FIGURE 9.3.2.5(c). *Typical compressive stress-strain and compressive tangent-modulus within the same figure.*

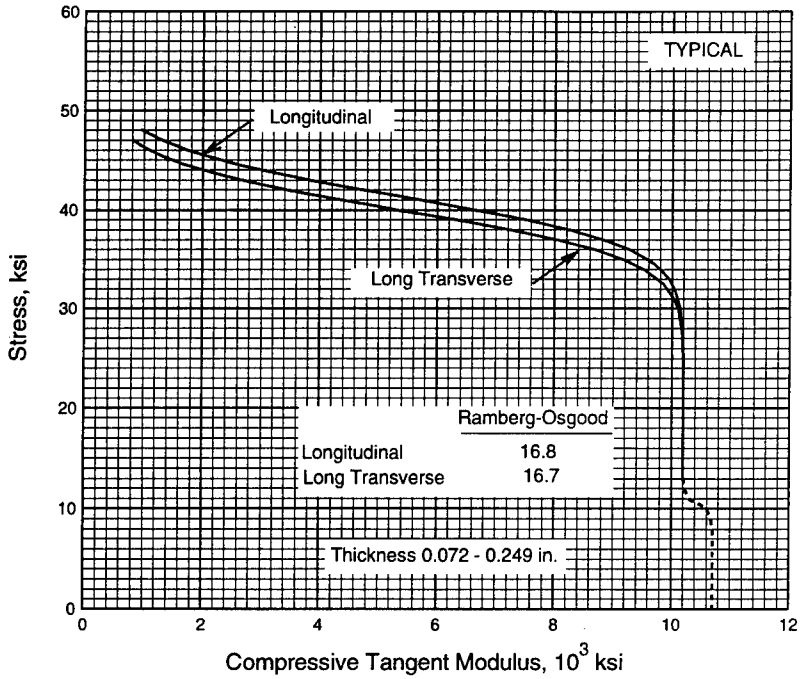


FIGURE 9.3.2.5(d). *Typical compressive-tangent-modulus curves for clad aluminum alloy sheet showing the primary and secondary modulus.*

such as the grain direction (L, LT, and ST), and/or temperature for each curve must be indicated in the figure. Figures 9.3.2.5(b), (c), and (d) show the proper format for presentation in Chapters 2 through 7.

Stress-secant modulus curves are not presently used in MIL-HDBK-5. Secant or "chord" modulus is determined as illustrated in Figure 9.3.2.5(a) and is plotted in the same manner as the tangent modulus. The equation for secant modulus is:

$$E_s = \frac{f}{e} = \frac{f}{\frac{f}{E} + 0.002\left(\frac{f}{f_g}\right)^n} \qquad [9.3.2.5\ (b)]$$

at the point of stress.

9.3.2.6 *Minimum Stress-Strain and Stress-Tangent Modulus Curves.*—Minimum stress strain and stress-tangent modulus curves are not presented in MIL-HDBK-5, but these are sometimes required by the designer. Procedures for preparing minimum curves are identical to those for preparing typical curves, except for choice of yield-strength values. Product average, or average values of yield strength, are used to determine typical curves; minimum values (F_{ty} or F_{cy} A- or B-basis) are used to determine minimum curves. Average values of precision elastic modulus (E or E_c) are used.

9.3.2.7 *Full-Range Tensile Stress-Strain Curves.*—Preparation of each typical full-range tensile stress-strain curve requires (1) representative original full-range stress-strain curves, (2) product average values for ultimate strength, yield strength, and elongation, and (3) typical precision elastic-modulus values at test temperature. (See 9.3.2.2 for source and definition of product average values for ultimate strength, yield strength, and elongation as well as typical elastic-modulus values.) Full-range tensile stress-strain data for at least one lot of material shall be provided, but data from three lots are preferred. If data for less than three lots are submitted, the full-range stress-strain curve shall be labeled "BASED

ON ONE LOT" or "BASED ON TWO LOTS", as appropriate.

The procedure for developing typical full-range tensile stress-strain curves is based upon strain departures obtained from several original test curves, and the product average tensile strength, yield strength, and elongation established from production data. Properties of material tested for determining strain departures should be in reasonable agreement with the product average properties.

These steps, as illustrated in Table 9.3.2.7 and Figures 9.3.2.7(a) and (b), should be followed in developing typical full-range tensile stress-strain curves.

(1) From each stress-strain test curve, measure strain departures (D) between the extension of the modulus line and the curve at stresses determined by taking appropriate percentages of the differences between ultimate stress and yield stress added to the yield stress.

$$\sigma_{(1,n)} = TYS + \% \ (TUS - TYS)$$

where TUS and TYS are values for each test. Also identify the proportional limit for each test. The proportional limit is defined as the stress level below which the stress-strain curve is linear; as determined by $\sigma=E\varepsilon$ where is the σ stress, E is Young's Modulus and ε is the strain.

(2) For departures beyond ultimate stress, the stresses are determined by taking the percentage of the difference between the fracture stress and ultimate stress and subtracting it from the ultimate stress.

$$\sigma_{(1,n)} = TUS - (1 - \%) \cdot (TUS - FS)$$

or

$$\sigma_{(1,n)} = FS + \% \ (TUS - FS)$$

where TUS and FS are values for each specimen.

(3) For each percentage, average the stresses and strain departures, σ_A and D_A, respectively.

(4) Compute typical stresses between TYS and TUS using product average yield strengths.

$$\sigma_T = TYS_{Prod.Avg.} + \% \ \left(TUS_{Prod.Avg.} - TYS_{Prod.Avg.}\right)$$

(5) Compute typical fracture stress, $\sigma_T(FS)$, as follows:

$$\sigma_T(FS) = \frac{TUS_{Prod.\ Avg.}}{TUS_{Avg.}} \sigma_{Avg.}(FS) \quad .$$

(6) Compute typical stresses between TUS and FS using product average ultimate strength and typical fracture stress.

$$\sigma_T = TUS_{Prod.Avg.} - (1 - \%) \cdot \left(TUS_{Prod.Avg.} - \sigma_T(FS)\right)$$

or

(7) Adjust the average departures, D_A, to typical departures, D_T, as follows:

$$\sigma_T = \sigma_T(FS) + \% \left(TUS_{Prod.\,Avg.} - \sigma_T(FS)\right)$$

$$D_T = \frac{(D_A - 0.002)(\text{Prod. Avg. Elong.} - 0.002)}{(D_A \text{ at Fracture Stress} - 0.002)} + 0.002 \quad .$$

(8) Compute elastic strains, ε_E, by dividing typical stresses by typical modulus.

$$\varepsilon_T = \frac{\sigma_T}{E}$$

(9) Obtain total strain, ε_T, by adding D_T and ε_E.

(10) Calculate the average proportional limit from the stress strain curves and compute the typical proportional limit.

$$\sigma_T(PL) = \left(TYS_{Prod.\,Avg.}/TYS_{Avg.}\right) \cdot \sigma_{Avg.}(PL)$$

The final step is plotting the full-range stress-strain curves. The following guidelines should be followed to plot the stress-strain curve. There should be 10 minor divisions for every major division with every tenth (major) division accented. The ordinate (Y-axis) is used for stress and should be in units of 5, 10, 20, or 50 ksi to the major division. The abscissa (X-axis) is used for strain and should be in units of 0.01, 0.02, 0.05, or 0.1 in./in. to the major division.

In addition to plotting the graphs by hand, they may be plotted with computer software programs. In the latter case, input the stress-strain pairs (σ_T and ε_T) from Table 9.3.2.7 into the computer and then curve fit the data. The elastic section must be linear up to the proportional limit. It is recommended that a power-law polynomial second order be used to fit the data from the proportional limit to fracture stress. The full-range stress-strain curve should be solid up to maximum stress and dashed from maximum stress to rupture. The fracture point should be indicated with an X. Only one typical full-range stress-strain figure should be plotted per page and should fill as much of the page as possible as illustrated in Figure 9.3.2.7(c). If more than one curve is contained in the figure, information such as the direction (ST, LT, and L), and/or temperature for each curve must be indicated.

9.3.3 BIAXIAL STRESS-STRAIN BEHAVIOR.—Procedures for analyzing and presenting biaxial stress-strain properties may be added to the guidelines at a later date. In the interim, procedures described in Reference 9.3.3 may be used as a general guide.

TABLE 9.3.2.7. *Example of Strain-Departure Method to Establish Typical Full-Range Stress-Strain Curves.*

Percent	Test 1		Test 2		Average		Typical			
	Stress, ksi σ_1	Strain Departure[c] in./in. (D_1)	Stress, ksi σ_2	Strain Departure[c] in./in. (D_2)	Stress,[d] ksi σ_A	Strain Departure[d] in./in. (D_A)	Stress, ksi σ_T	Strain Departure[i] in./in. (D_T)	Elastic Strain[j] in/in. (ε_E)	Total Strain[k] in./in. (ε_T)
				Yield Stress to Ultimate Stress						
Proportional Limit (PL)	56.5		58.5		57.5[h]		59.6[l]	0.0000	0.0058	0.0058
0(TYS)	58.8[a]	0.0020	60.9[a]	0.0020	59.8	0.0020	62.0[e]	0.0020	0.0061	0.0081
20	61.0[a]	0.0106	63.0[a]	0.0094	62.0	0.0100	64.0[e]	0.0100	0.0063	0.0163
40	63.2[a]	0.0204	65.2[a]	0.0194	64.2	0.0199	66.0[e]	0.0200	0.0065	0.0265
60	65.4[a]	0.0302	67.4[a]	0.0302	66.4	0.0302	68.0[e]	0.0303	0.0067	0.0370
80	67.7[a]	0.0452	69.5[a]	0.0436	68.6	0.0444	70.0[e]	0.0446	0.0069	0.0515
95	69.3[a]	0.0640	71.1[a]	0.0626	70.2	0.0633	71.5[e]	0.0636	0.0070	0.0706
100(TUS)	69.9[a]	0.0848	71.7[a]	0.0838	70.8	0.0843	72.0[e]	0.0847	0.0071	0.0918
				Ultimate Stress to Fracture Stress (FS)						
100(TUS)	69.9[b]	0.0848	71.7[b]	0.0838	70.8	0.0843	72.0[g]	0.0847	0.0071	0.0918
90	69.0[b]	0.0962	70.9[b]	0.1014	70.0	0.0988	71.1[g]	0.0992	0.0070	0.1062
60	66.3[b]	0.1058	68.5[b]	0.1156	67.4	0.1107	68.5[g]	0.1112	0.0067	0.1179
0(FS)	60.9[b]	0.1210	63.7[b]	0.1378	62.3	0.1294	63.4[f]	0.1300 (Elong.)	0.0062	0.1362

[a] $\sigma_{1,n}$ = TYS + % (TUS-TYS) where TUS and TYS are values for each test.
[b] $\sigma_{1,n}$ = TUS - (1 - %) · (TUS-FS) or $\sigma_{(1,n)}$ = FS + % (TUS-FS) where TUS and FS are values for each test.
[c] D = Departure (plastic strain) from modulus line at corresponding stresses.
[d] Averages (σ and D) of Tests 1 and 2.
[e] $\sigma_T = TYS_{Prod.\ Avg.}$ + % ($TUS_{Prod.\ Avg.}$ - $TYS_{Prod.\ Avg.}$).
[f] $\sigma_T(FS) = (TUS_{Prod.\ Avg.}/TUS_{Avg.}) \cdot \sigma_{Avg.}(FS)$.
[g] $\sigma_T = TUS_{Prod.\ Avg.}$ - (1 - %) · ($TUS_{Prod.\ Avg.}$ - $\sigma_T(FS)$) or $\sigma_T = \sigma_T(FS)$+% ($TUS_{Prod.Avg.}$ - $\sigma_T(FS)$).
[h] Average proportional limit.
[i] D_T = [((D_A - 0.002) x (Product Average Elongation -0.002)) ÷ (D_A at FS - 0.002)] + 0.002.
[j] $\varepsilon_E = \sigma_T \div E$ (E = 10.2 x 10^3 ksi in this example).
[k] $\varepsilon_T = D_T + \varepsilon_E$.
[l] σ_T (PL) = ($TYS_{Prod.\ Avg.}/TYS_{Avg.}$) · $\sigma_{Avg.}$(PL).

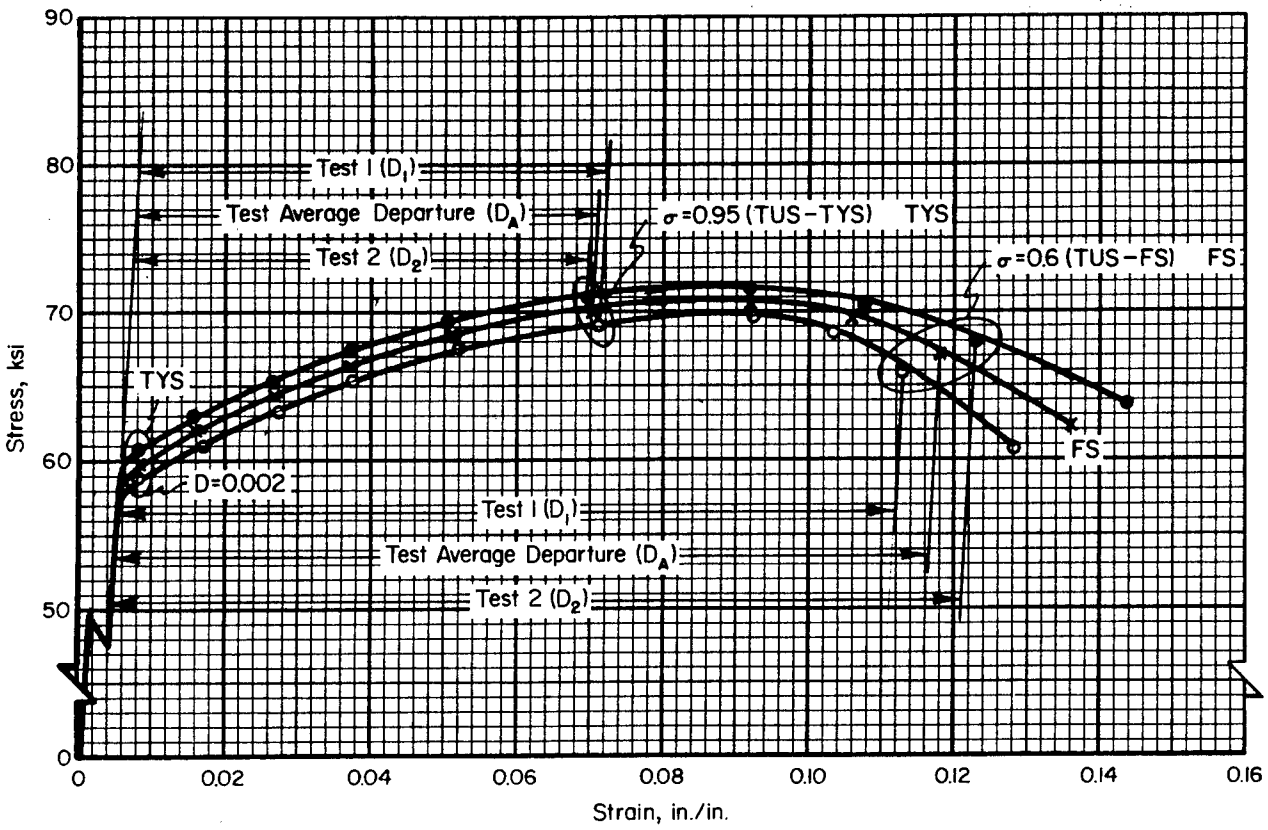


FIGURE 9.3.2.7(a). *Strain departure method for determining average full-range stress-strain curve.*

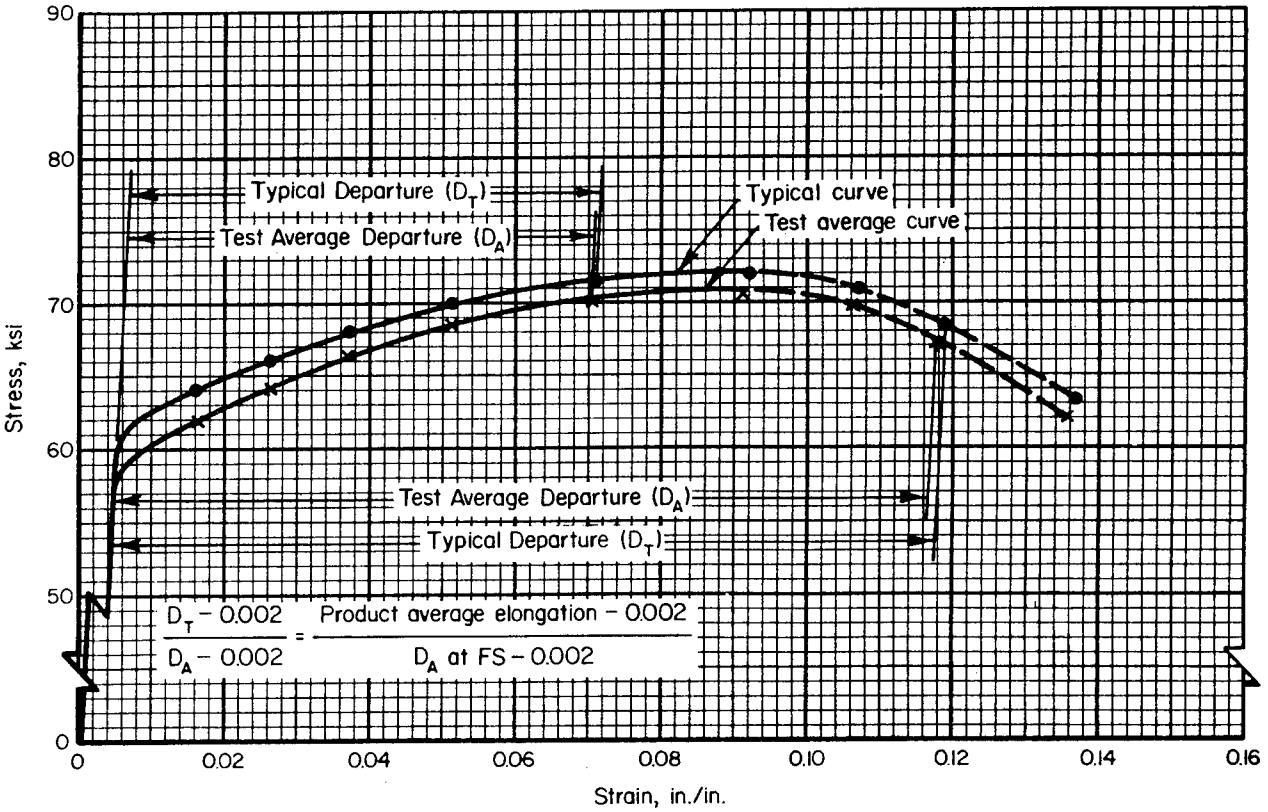


FIGURE 9.3.2.7(b). *Method of adjusting average to typical full-range stress-strain curve.*

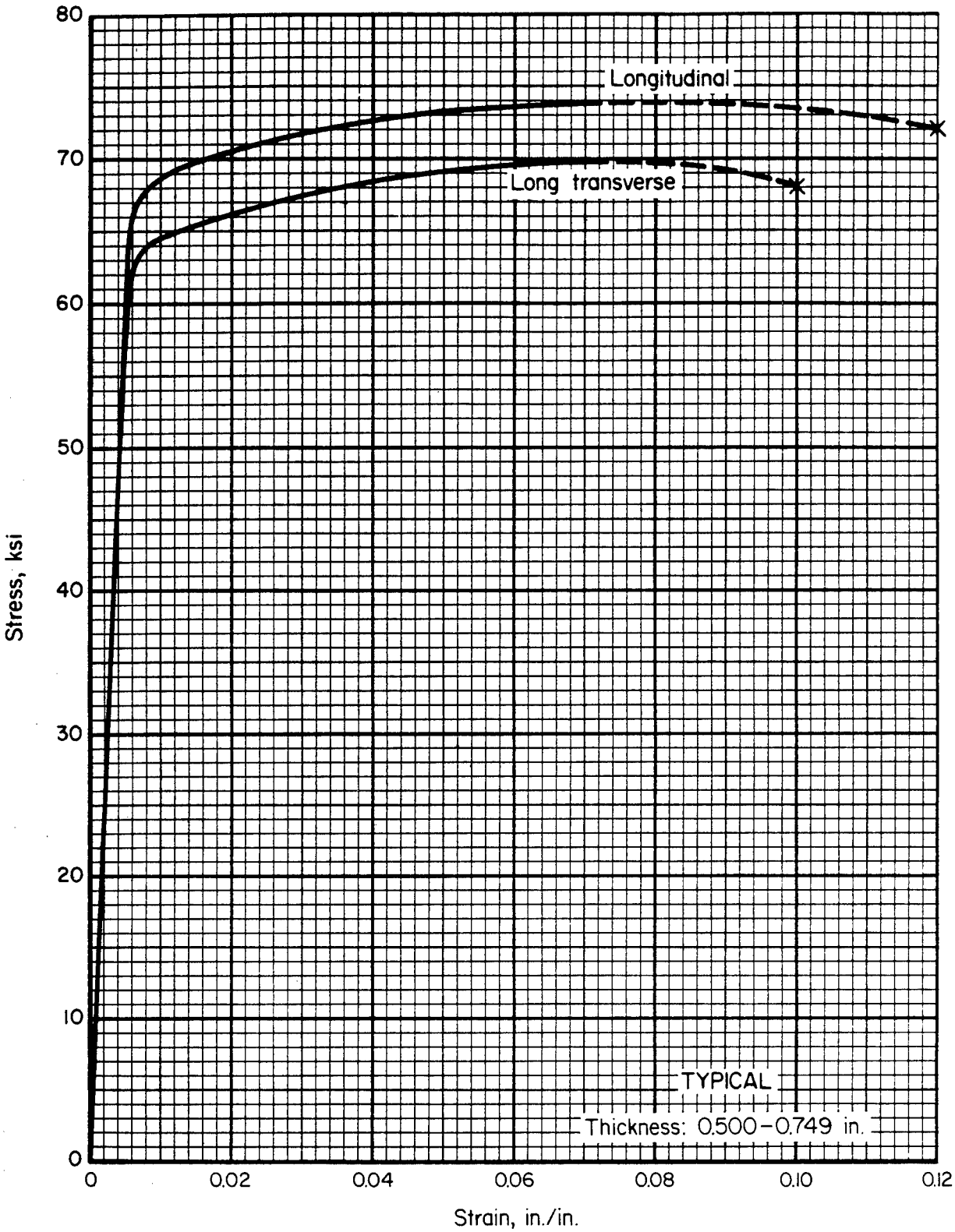


FIGURE 9.3.2.7(c). *Typical full-range curves drawn by the strain-departure method.*

9.3.4 FATIGUE DATA ANALYSIS

9.3.4.1 *Introduction.*—Fatigue has been defined as "the process of progressive localized permanent structural change occurring in a material subjected to conditions that produce fluctuating stresses and strains at some point or points, and which may culminate in cracks or complete fracture after a sufficient number of fluctuations."

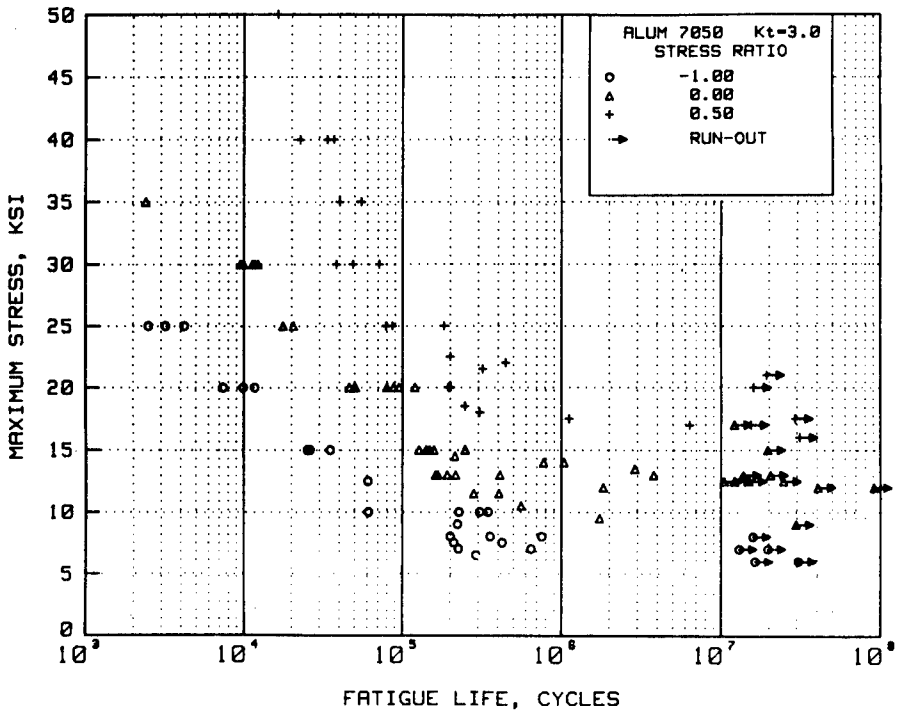
For many years, tests have been performed on specimens having simple geometries in attempts to characterize the fatigue properties of particular materials. Fatigue tests have been conducted for many reasons. Basic fatigue-life information may be desired for design purposes, or to evaluate the differences between materials. The effects of heat treatments, mechanical working, or material orientation may also be studied through comparative fatigue testing.

Many types of machines and specimen designs have been used to develop fatigue data. Machine types include mechanical, electromechanical, hydraulic, and ultrasonic. Specimens have been designed for testing in cyclic tension and/or compression, bending, and torsion. Cyclic loading conditions have been produced by rotating bending, axial loading and cantilever bending. In- and out-of-phase biaxial and multiaxial fatigue conditions have also been examined using specially designed specimens. Tests have been conducted in a variety of simulated environments including temperatures ranging from cryogenic to near melting point levels. The fatigue data included in MIL-HDBK-5 are limited to constant-amplitude axial fatigue data on simple laboratory specimens tested according to ASTM E606 [Reference 9.3.4.1(a)]. Data obtained under both strain control and load (stress) control are included. Figure 9.3.4.1(a) shows examples of trends for stress-life and strain-life fatigue data. Generally, stress-life data for unnotched specimens are limited to stress levels that produce intermediate-to-long fatigue lives because of unstable cyclic creep and tensile failure that can occur at high stress ratios in load-control testing. This phenomenon is shown in Figure 9.3.4.1(b). Strain-life curves are often focused on strain ranges that produce short-to-intermediate fatigue lives because of strain rate and frequency limitations which require long testing times to generate long-life fatigue data under strain control. However, there is no inherent limit to the life range that can be evaluated in strain-control testing.

For fatigue to occur, a material must undergo cyclic plasticity, at least on a localized level. The relationship between total strain, plastic strain, and elastic strain is shown in Figure 9.3.4.1(c). Low-cycle fatigue tests involve relatively high levels of cyclic plasticity. Intermediate-life fatigue tests usually involve plastic strains of the same order as the elastic strains. Long-life fatigue tests normally involve very low levels of cyclic plasticity. These trends are shown in Figure 9.3.4.1(d). In the MIL-HDBK-5 fatigue analysis guidelines, engineering strain is denoted as e and true or local strain is denoted as ε. These symbols are used interchangeably within MIL-HDBK-5 for small strain values.

The limited plasticity involved in intermediate and long-life fatigue tests often results in a similar stress-strain response for both fully reversed strain-control and fully reversed load-control tests. A fatigue test, under strain control that produces a stable maximum stress of X, should produce (on the average) a fatigue life that is comparable to that obtained for a sample tested under load control at a maximum stress of X. Strictly speaking, the results are likely to be most comparable in terms of crack initiation life and not total life. If the comparison is made in terms of total life, the load-control results will tend to be more conservative than those generated by strain-control testing. When a specimen cracks in a test under strain control, it will usually display a decrease in maximum tensile load. Under load control, the maximum tensile load will remain constant but stress will increase as the crack grows, resulting in a shorter period of crack growth before the specimen fails.

A number of factors can significantly influence fatigue properties for a particular material—whether the data are developed under load or under strain control. The surface condition (such as surface roughness) of the test specimens is an important factor. The methods used for fabricating the specimens are also important—principally because such methods influence the state of surface residual stresses and residual stress profiles. Other factors such as mean stress or strain, specimen geometry (including notch type), heat treatment, environment, frequency and temperature can also be significant variables. In MIL-HDBK-5, fatigue data are always presented in separate displays for different theoretical stress con-



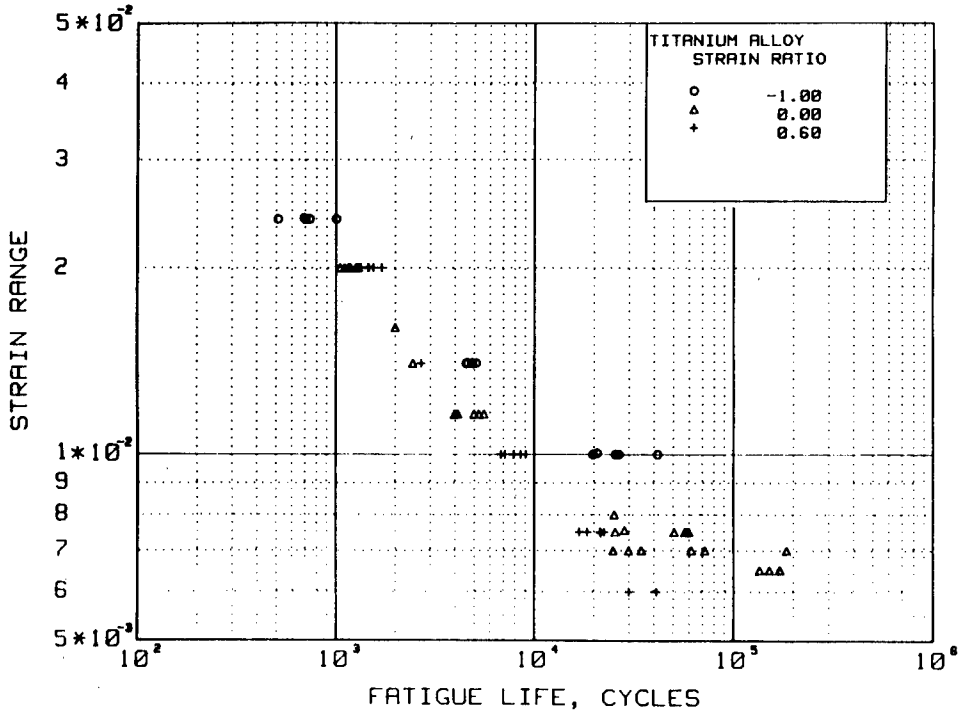


FIGURE 9.3.4.1(a). *Examples of stress-life and strain-life fatigue trends.*

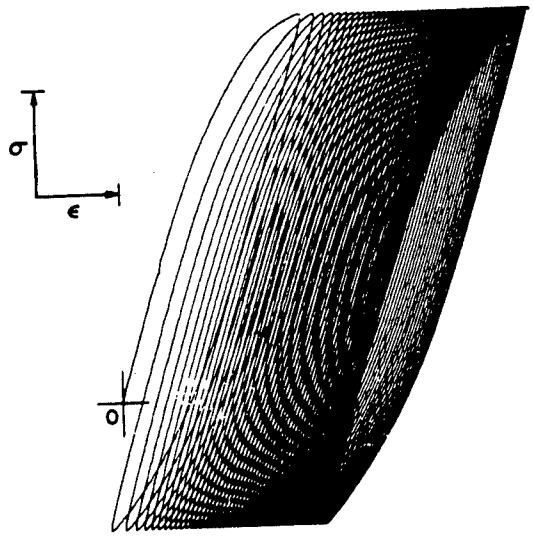


FIGURE 9.3.4.1(b). *Example of cyclic creep phenomenon that can occur in a load control test with a high tensile mean stress [Reference 9.3.4.1(b)].*

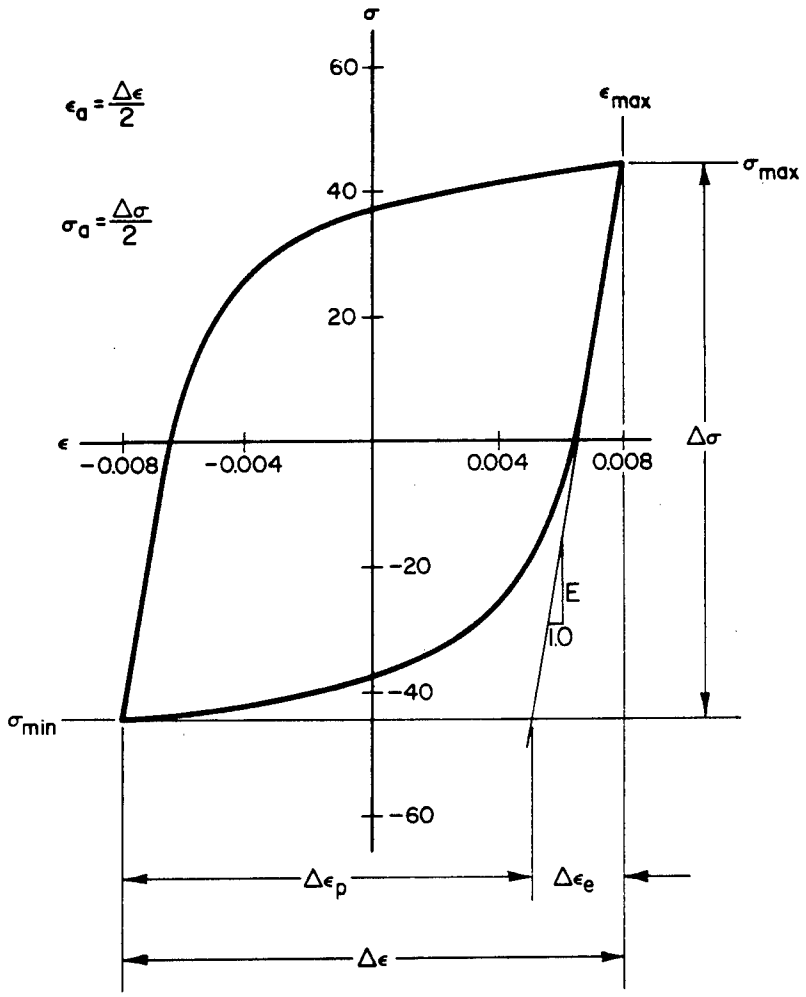


FIGURE 9.3.4.1(c). *A typical hysteresis loop for a material tested in fatigue under strain control illustrating the relationship between stress and strain parameters.*

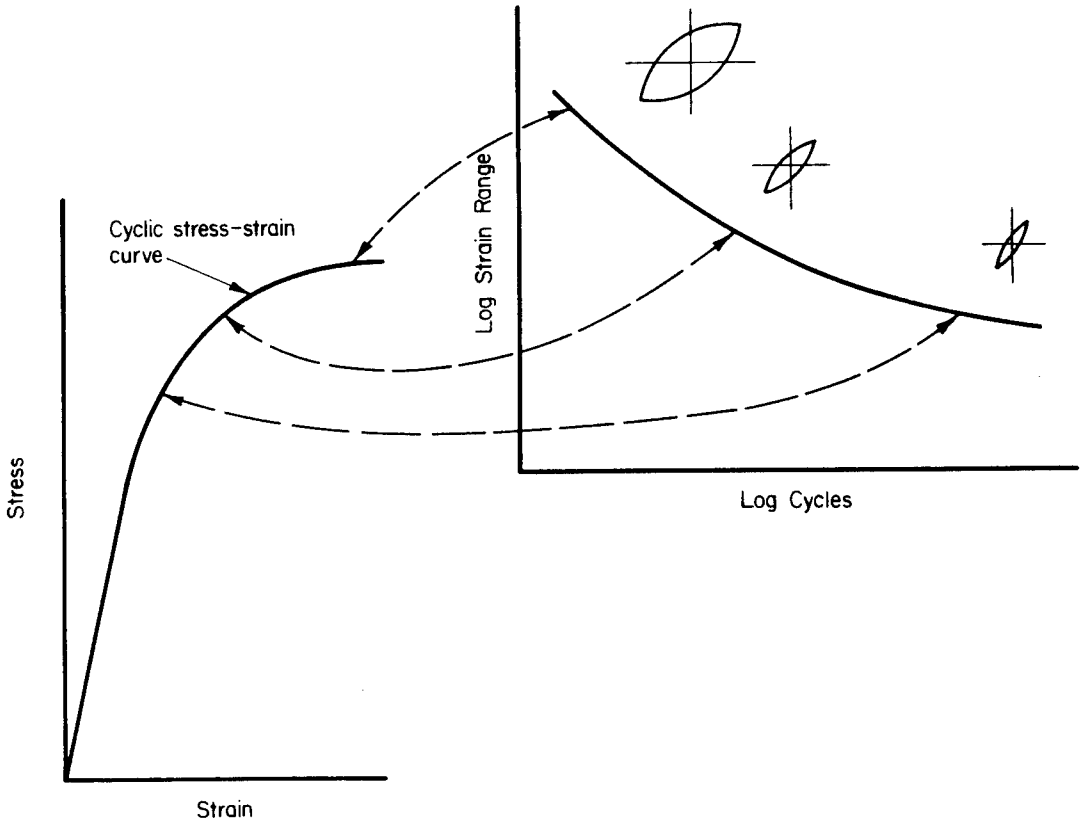


FIGURE 9.3.4.1(d). *An example of a strain-life fatigue curve and the stress-strain response at short, intermediate, and long fatigue lives.*

centration factors. However, data sets may be presented for various combinations of variables if preliminary analyses indicate that the data sets are compatible. In any case, it is very important to fully document both the input data and their resulting illustrations in MIL-HDBK-5 with regard to variables that can influence fatigue.

9.3.4.2 *Disclaimer.*—The selection of the specific procedures and methods that are outlined in this guideline for fatigue data presentation should not be construed as an endorsement of these procedures and methods for life prediction of components. The selection was made for consistency in data presentation only. For the purpose of life prediction, other methods and models are also commonly employed. Depending on the material, component and loading history, other models may be more appropriate for the particular situation. It is beyond the scope of these guidelines to make recommendations with respect to a specific life prediction methodology (e.g., the construction of design allowable fatigue curves).

9.3.4.3 *Terminology.*—The symbols and definitions used in analyzing and reporting fatigue data have been standardized by the American Society for Testing and Materials (ASTM). Most definitions of terms are consistent with those defined by the ASTM. However, some of the symbols and definitions differ and are noted with an asterisk (*). The terms are listed in alphabetical order. In the definitions listed below, the term for load (P) is taken to represent stress (S), strain (ε or e), or any other expression or function of loading. The most common terms relating to fatigue loading are illustrated in Figure 9.3.4.3.

Alternating Load.—See Loading Amplitude.

Confidence Interval.—An interval estimate of a population parameter computed so that the statement "the population parameter lies in this interval" will be true, on the average, in a stated proportion of the times such statements are made.

Confidence Level (or Coefficient).—The stated portion of the time that the confidence interval is expected to include the population parameter.

Confidence Limits*.—The two numeric values that define a confidence interval.

Constant-Amplitude Loading.—A loading in which all of the peak loads are equal and all of the valley loads are equal.

Constant-Life Fatigue Diagram.—A plot (usually on Cartesian coordinates) of a family of curves, each of which is for a single fatigue life, N—relating S, S_{max}, and/or S_{min} to the mean stress, S_m. Generally, the constant life fatigue diagram is derived from a family of S-N curves, each of which represents a different stress ratio (A or R) for a 50 percent probability of survival. NOTE—MIL-HDBK-5 no longer presents fatigue data in the form of constant-life diagrams.

Cycle.—Under constant-amplitude loading, the load varies from the minimum to the maximum and then to the minimum load (see Figure 9.3.4.3). The symbol n or N (see definition of fatigue life) is used to indicate the number of cycles.

Discontinued Test.—See Runout.

Fatigue.—The process of progressive localized permanent structural change occurring in a material subjected to conditions that produce fluctuating stresses and strains at some point or points, and which may culminate in cracks or complete fracture after a sufficient number of fluctuations. NOTE—fluctuations in stress and in time (frequency), as in the case of "random vibration".

Fatigue Life.—N—the number of cycles of stress or strain of a specified character that a given specimen sustains before failure of a specified nature occurs.

Fatigue Limit.—S_f—the limiting value of the median fatigue strength as N becomes very large. NOTE—Certain materials and environments preclude the attainment of a fatigue limit. Values tabulated as "fatigue limits" in the literature are frequently (but not always) values of S_N for 50 percent survival at N cycles of stress in which $S_m = 0$.

Fatigue Loading.—Periodic or non-periodic fluctuating loading applied to a test specimen or experienced by a structure in service (also known as cyclic loading).

Fatigue Notch Factor*.—The fatigue notch factor, K_f (also called fatigue strength reduction factor) is the ratio of the fatigue strength of a specimen with no stress concentration to the fatigue strength of a specimen with a stress concentration at the same number of cycles for the same conditions. NOTE—In specifying K_f, it is necessary to specify the geometry, mode of loading, and the values of S_{max} S_m, and N for which it is computed.

Fatigue Notch Sensitivity.—The fatigue notch sensitivity, q, is a measure of the degree of agreement between K_f and K_t. NOTE—the definition of fatigue notch sensitivity is $q = (K_f - 1)/(K_t - 1)$.

Hysteresis Diagram.—The stress-strain path during a fatigue cycle.

Interrupted Test*.—Tests which have been stopped before failure because of some mechanical problem, e.g., power failure, load or temperature spikes.

*Different from ASTM.

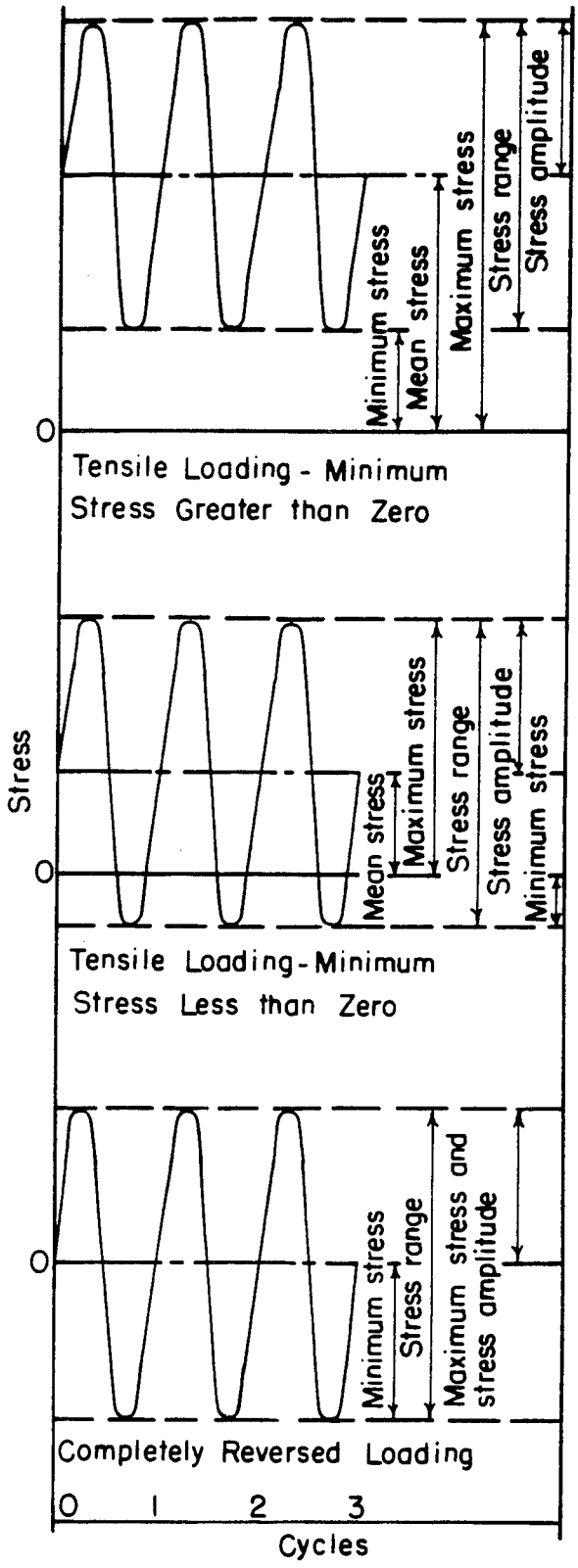


FIGURE 9.3.4.3. *Typical fatigue loadings.*

Loading Amplitude.—The loading amplitude, P_a, S_a, or ε_a represents one-half of the range of a cycle (see Figure 9.3.4.3). (Also known as alternating load, alternating stress, or alternating strain.)

Loading (Unloading) Rate.—The time rate of change in the monotonically increasing (decreasing) portion of the load-time function.

Load Ratio.—The load ratio, R, A, or R_ε, A_ε, or R_σ, A_σ, is the algebraic ratio of the two loading parameters of a cycle; the two most widely used ratios are

$$R = \frac{\text{minimum load}}{\text{maximum load}} = \frac{P_{min}}{P_{max}}$$

or

$$R_\sigma = \frac{S_{min}}{S_{max}}$$

or

$$R_\varepsilon = \varepsilon_{min}/\varepsilon_{max}$$

and

$$A = \frac{\text{loading amplitude}}{\text{mean load}} = \frac{P_a}{P_m} \text{ or } \frac{S_a}{S_M}$$

$$A_\varepsilon = \frac{\text{strain amplitude}}{\text{mean strain}} = \frac{\varepsilon_a}{\varepsilon_M} \text{ or } (\varepsilon_{max} - \varepsilon_{min})/(\varepsilon_{max} + \varepsilon_{min})$$

NOTE—load ratios R or R_ε are generally used in MIL-HDBK-5.

Maximum Load.—The maximum load, P_{max}, S_{max}, ε_{max} is the load having the greatest algebraic value.

Mean Load.—The mean load, P_m, is the algebraic average of the maximum and minimum loads in constant-amplitude loading:

$$P_m = \frac{P_{max} + P_{min}}{2}, \text{ or}$$

$$S_m = \frac{S_{max} + S_{min}}{2}, \text{ or}$$

$$\varepsilon_m = \frac{\varepsilon_{max} + \varepsilon_{min}}{2},$$

or the integral average of the instantaneous load values.

Median Fatigue Life.—The middlemost of the observed fatigue life values (arranged in order of magnitude) of the individual specimens in a group tested under identical conditions. In the case where an even number of specimens are tested, it is the average of the two middlemost values (based on log lives in MIL-HDBK-5). NOTE 1—The use of the sample median instead of the arithmetic mean (that is, the average) is usually preferred. NOTE 2—In the literature, the abbreviated term "fatigue life" usually has meant the median fatigue life of the group. However, when applied to a collection of data without further qualification, the term "fatigue life" is ambiguous.

Median Fatigue Strength at N Cycles.—An estimate of the stress level at which 50 percent of the population would survive N cycles. NOTE—The estimate of the median fatigue strength is derived from a particular point of the fatigue-life distribution, since there is no test procedure by which a frequency distribution of fatigue strengths at N cycles can be directly observed. That is, one can not perform constant-life tests.

Minimum Load.—The minimum load, P_{min}, S_{min}, or ε_{min}, is the load having the least algebraic value.

Outlier*—An experimental observation which deviates markedly from other observations in the sample. An outlier is often either an extreme value of the variability in the data, or the result of gross deviation in the material or experimental procedure.

Peak—The point at which the first derivative of the load-time history changes from a positive to a negative sign; the point of maximum load in constant-amplitude loading (see Figure 9.3.4.3).

Precision*—The degree of mutual agreement among individual measurements. Relative to a method of test, precision is the degree of mutual agreement among individual measurements made under prescribed like conditions. The lack of precision in a measurement may be characterized as the standard deviation of the errors in measurement.

Range—Range, ΔP, S_r, $\Delta\varepsilon$, ε_r, $\Delta\sigma$ is the algebraic difference between successive valley and peak loads (positive range or increasing load range) or between successive peak and valley loads (negative range or decreasing load range), see Figure 9.3.4.3. In constant-amplitude loading, for example, the range is given by $\Delta P = P_{max} - P_{min}$.

Residual*—The difference between the observed fatigue (log) life and the fatigue (log) life estimated from the fatigue model at a particular stress/strain level.

Runout*—A test that has been terminated prior to failure. Runout tests are usually stopped at an arbitrary life value because of time and economic considerations. NOTE—Runout tests are useful for estimating a pseudo-fatigue-limit for a fatigue data sample.

*Different from ASTM.

Sample—The number of specimens selected from a population for test purposes. NOTE—The method of selecting the sample determines the population about which statistical inferences or generalization can be made.

Sample Average (Arithmetic Mean)—The sum of all the observed values in a sample divided by the sample size (number). It is a point estimate of the population mean.

Sample Median—The middle value when all observed values in a sample are arranged in order of magnitude if an odd number of samples are tested. If the sample size is even, it is the average of the two middlemost values. It is a point estimate of the population median, or 50 percentile point.

Sample Standard Deviation*—The standard deviation of the sample, s, is the square root of the sample variance. It is a point estimate of the standard deviation of a population, a measure of the "spread" of the frequency distribution of a population. NOTE—this value of s provides a statistic that is used in computing interval estimates and several test statistics.

Sample Variance*—Sample variance, s^2, is the sum of the squares of the differences between each observed value and the sample average divided by the sample size minus one. It is a point estimate of the population variance. NOTE—This value of s^2 provides both an unbiased point estimate of the population variance and a statistic that is used on computing the interval estimates and several test statistics. Some texts define s^2 as "the sum of the squared differences between each observed value and the sample average divided by the sample size", however; this statistic underestimates the population variance, particularly for small sample sizes.

Significant (Statistically significant)—An effect or difference between populations is said to be present if the value of a test statistic is significant, that is, lies outside of predetermined limits. NOTE—An effect that is statistically significant may not have engineering importance.

Significance Level—The stated probability (risk) that a given test of significance will reject the hypothesis that a specified effect is absent when the hypothesis is true.

S-N Curve for 50 Percent Survival*—A curve fitted to the median values of fatigue life at each of several stress levels. It is an estimate of the relationship between applied stress and the number of cycles-to-failure that 50 percent of the population would survive. NOTE 1—This is a special case of the more general definition of S-N curve for P percent survival. NOTE 2—In the literature, the abbreviated term "S-N Curve" usually has meant either the S-N curve drawn through the mean (averages) or through the medians (50 percent values) for the fatigue life values. Since the term "S-N Curve" is ambiguous, it should be used only when described appropriately. NOTE 3—Mean S-N curves (based on log lives) are shown in MIL-HDBK-5.

S-N Diagram—A plot of stress against the number of cycles to failure. The stress can be S_{max}, S_{min}, or S_a. The diagram indicates the S-N relationship for a specified value of S_m, A, or R and a specified probability of survival. Typically, for N, a log scale (base 10) is used. Generally, for S, a linear scale is used, but a log scale is used occasionally. NOTE—S_{max}-versus-log N diagrams are used commonly in MIL-HDBK-5.

Theoretical Stress Concentration Factor (or Stress Concentration Factor)—This factor, K_t, is the ratio of the nominal stress to the greatest stress in the region of a notch (or other stress concentrator) as determined by the theory of elasticity (or by experimental procedures that give equivalent values). NOTE—The theory of plasticity should not be used to determine K_t.

Tolerance Interval—An interval computed so that it will include at least a stated percentage of the population with a stated probability.

*Different from ASTM.

Tolerance Level—The stated probability that the tolerance interval includes at least the stated percentage of the population. It is not the same as a confidence level, but the term confidence level is frequently associated with tolerance intervals.

Tolerance Limits—The two statistics that define a tolerance interval. (One value may be "minus infinity" or "plus infinity".)

Transition Fatigue Life*—The point on a strain-life diagram where the elastic and plastic strains are equal.

Waveform—The shape of the peak-to-peak variation of a controlled mechanical test variable (for example, load, strain, displacement) as a function of time.

The following symbols are used frequently for the term covered by the preceding definitions. For stress, the use of S with appropriate lower case subscripts is preferred for general purposes; for mathematical analysis, the use of Greek symbols is generally preferred.

Symbol	Term
A	"A" ratio, loading amplitude/mean load; or area
A_ε	Strain "A" ratio, strain amplitude/mean strain
A_i	Model parameter
D or d	diameter, or Durbin Watson statistic
E	modulus of elasticity in tension or compression
e	engineering strain
ε	true or local strain
ε_{eq}^*	equivalent strain
ε_m	mean strain, $(\varepsilon_{max} + \varepsilon min)/2$
ε_{max}	maximum strain
ε_{min}	minimum strain
$\Delta\varepsilon$ or ε_r*	strain range, $\varepsilon_{max} - \varepsilon_{min}$
$\Delta\varepsilon_e$	elastic strain range
$\Delta\varepsilon_p$	plastic strain range
K_f	fatigue notch factor, or fatigue strength reduction factor
K_t	theoretical stress concentration factor
μ	Poisson's ratio
N	fatigue life, number of cycles

*Different from ASTM.

Symbol	Term
N_f	fatigue life, cycles to failure
N_i*	fatigue life, cycles to initiation
N_t*	transition fatigue life where plastic and elastic strains are equal
P	load
P_a	load amplitude
P_m	mean load
P_{max}	maximum load
P_{min}	minimum load
q	fatigue notch sensitivity
R	load (stress) ratio, or residual (observed minus predicted value)
R_ε	strain ratio, $\varepsilon_{min}/\varepsilon_{max}$
S	nominal or engineering stress
s	sample standard deviation
s^2	sample variance
S_a	stress amplitude
S_{eq}*	equivalent stress
S_f	fatigue limit
S_m	mean stress
S_{max}	maximum stress
S_{min}	minimum stress
SR	studentized residual
ΔS (S_r)*	stress range
TUS (S_u)*	tensile ultimate strength
σ	true or local stress; or population standard deviation
σ_x	population standard deviation of x
σ_x^2	population variance of x
$\Delta\sigma$	true or local stress range.

*Different from ASTM.

9.3.4.4 *Data Requirements*—Both strain-controlled and load-controlled axial fatigue data can be considered for inclusion in MIL-HDBK-5. Constant amplitude test data are the primary focus. Well documented, initial and/or periodic overstrain data may also be included. Data obtained under strain control are considered only for unnotched, uniform-gage-length specimens, while both notched and unnotched specimens are considered for load-control conditions.

Fatigue data generated under load control over a wide range of stress ranges and ratios can be acceptable. However, load-control experiments on unnotched samples can produce ratcheting failures rather than true fatigue failures. This can be a problem with materials that cyclically soften. In the absence of cyclic stress-strain data, the acceptability of short-life data obtained under load control on unnotched specimens can be difficult to evaluate. Therefore, results from specimens tested at a maximum stress level greater than the average tensile ultimate strength of the material should not be used. In addition, test results obtained under load control that have produced average fatigue lives on unnotched specimens of less than 10^3 cycles should be excluded. Short-life, load-control data generated on notched samples tested at high stress levels may be considered.

Fatigue data generated under strain control over a wide range of strain ratios and ranges can be acceptable also. High-strain-range tests producing low fatigue lives can be considered assuming that documented bending strains were held within ASTM E606 limits and buckling failures were not produced. Documenting the stress response associated with each test result is important. The stress data that are reported should reflect the material's stable response, including effects of cyclic hardening or softening and of mean stress relaxation provided such data were obtained at other than $R_\varepsilon = -1$. The normal convention is to report the stress values associated with one-half the material's fatigue life to crack initiation. Several criteria are commonly used to define crack initiation in a test under strain control. The primary requirements for inclusion in MIL-HDBK-5 are that the criteria be specific and applied consistently. If multiple sources of data are being considered, the potential problem of inconsistent crack initiation criteria must be addressed before that data are merged.

If strain-control data only are reported with fatigue test results obtained under strain control, these data must be supported by well-documented cyclic stress-strain curves and mean stress relaxation data for that specific material.

For fatigue experiments under load control, data are normally generated at specific stress ratios or mean stress levels. If the stress ratio is held constant, a fatigue curve is generated by performing a series of experiments at prescribed maximum stress levels such that the desired range of fatigue lives is achieved. If means stress levels are held constant, a range of maximum stress levels is also used, but the stress ratio for each maximum stress level is different. Presentation of the latter type of data in a traditional S_{max}-versus-log N_f display, with individual stress ratio curves, can be cumbersome because of the large number of stress ratios involved. For this reason, constant mean-stress fatigue data should be identified by mean stress level, even though they are plotted on a standard S_{max}-versus-log N_f display. The illustrations should be clearly labeled to properly identify the mean-stress or stress-ratio levels.

To evaluate analytically the effects of stress or strain ratio on the fatigue performance of a particular material, it is recommended that data be available for at least three stress or strain ratios, or alternatively, three mean-stress or strain levels. Similarly, at least three stress or strain levels are recommended to evaluate the effects of mean stress on fatigue performance. In the case of data under strain control, a specific strain ratio or mean strain may not define a mean-stress level uniquely. For $R_\varepsilon = -1.0$ (mean strain = 0), the stress ratio is usually very close to R = -1.0 (mean stress = 0)—if it is not, the data should be examined carefully for validity. For strain ratios greater than $R_\varepsilon = -1.0$, the stress ratio is usually less than the strain ratio, and the difference is generally greater at the greatest strain ranges. For very large strain ranges in ductile materials, the stable stress ratio will approach R = -1.0 (mean stress = 0), regardless of the strain ratio, R_ε. Mean stress relaxation behavior is shown in Figure 9.3.4.4.

There should be at least six non-runout fatigue test results for each condition, and these data should be distributed over at least two orders of magnitude in fatigue life. These requirements are the minimum sample sizes normally required to consider developing a fatigue data display. Meeting the minimum data requirements does not ensure an acceptable set of fatigue curves. In cases involving highly scattered data, substantially larger sample sizes may be required to achieve a meaningful description of mean fatigue trends. The statistical procedures used to evaluate the significance of a fatigue data collection are described in Section 9.3.4.12.

9.3.4.5 *Fatigue Test Planning and Data Development*—In view of the above data requirements, fatigue data generated for inclusion in MIL-HDBK-5 should be the result of a well planned test program. The following general discussion of fatigue test planning is based in large part on the concepts presented in References 9.3.4.5(a), (b), and (c). Those interested in the detailed aspects of fatigue test planning should refer to these and other sources. The discussion that follows pertains to fatigue testing under either load control or strain control.

Traditionally, fatigue testing under load control has been performed to evaluate the fatigue performance of engineering materials and components subjected to numerous load fluctuations. Notched specimens are often used to evaluate the effect of stress concentrations upon fatigue life in load-control testing. The nominal stresses during load-control testing are generally below the materials yield strength and the resulting fatigue lives are usually greater than 10^4 cycles. Load-control tests with high mean-stress levels may develop unconstrained cyclic plasticity which may lead to racheting failures (see Figure 9.3.4.1(b)]. Unless cyclic strains are monitored in load-control tests, it is not possible to know exactly when unconstrained cyclic plasticity will develop. In general, however, there are test conditions that should be avoided when operating under load control, as follows:

(1) Unnotched-specimen fatigue tests in which fatigue lives less than 10^3 cycles to failure are expected.

(2) Fatigue tests involving net-section maximum stresses greater than the yield strength or over 95 percent of the typical monotonic ultimate strength of the material.

Strain-controlled fatigue testing has emerged since the mid-1950s because the fatigue damage process was found to be highly dependent upon cumulative plastic deformation. Cycling a material between two strain limits can alter the material's stress-strain response (cyclic hardening or softening) compared to the monotonic response. Fatigue testing under strain control should be considered in cases where constrained inelastic cyclic strains may occur in the actual component. Strain control should also be used for any conditions where unconstrained cyclic plasticity may lead to racheting failures in load-control testing.

Fatigue data obtained under load control for use in MIL-HDBK-5 should be generated for at least three stress ratios. Fatigue lives ranging from approximately 10^3 to 10^6 cycles are most commonly of interest while the stress ratios chosen should normally span the range from about R = -1.0 to 0.50 or greater.

Fatigue data obtained under strain control are commonly generated at R_ε = -1.0. These data will be considered for MIL-HDBK-5, but generating data for at least two other strain ratios is also desirable.

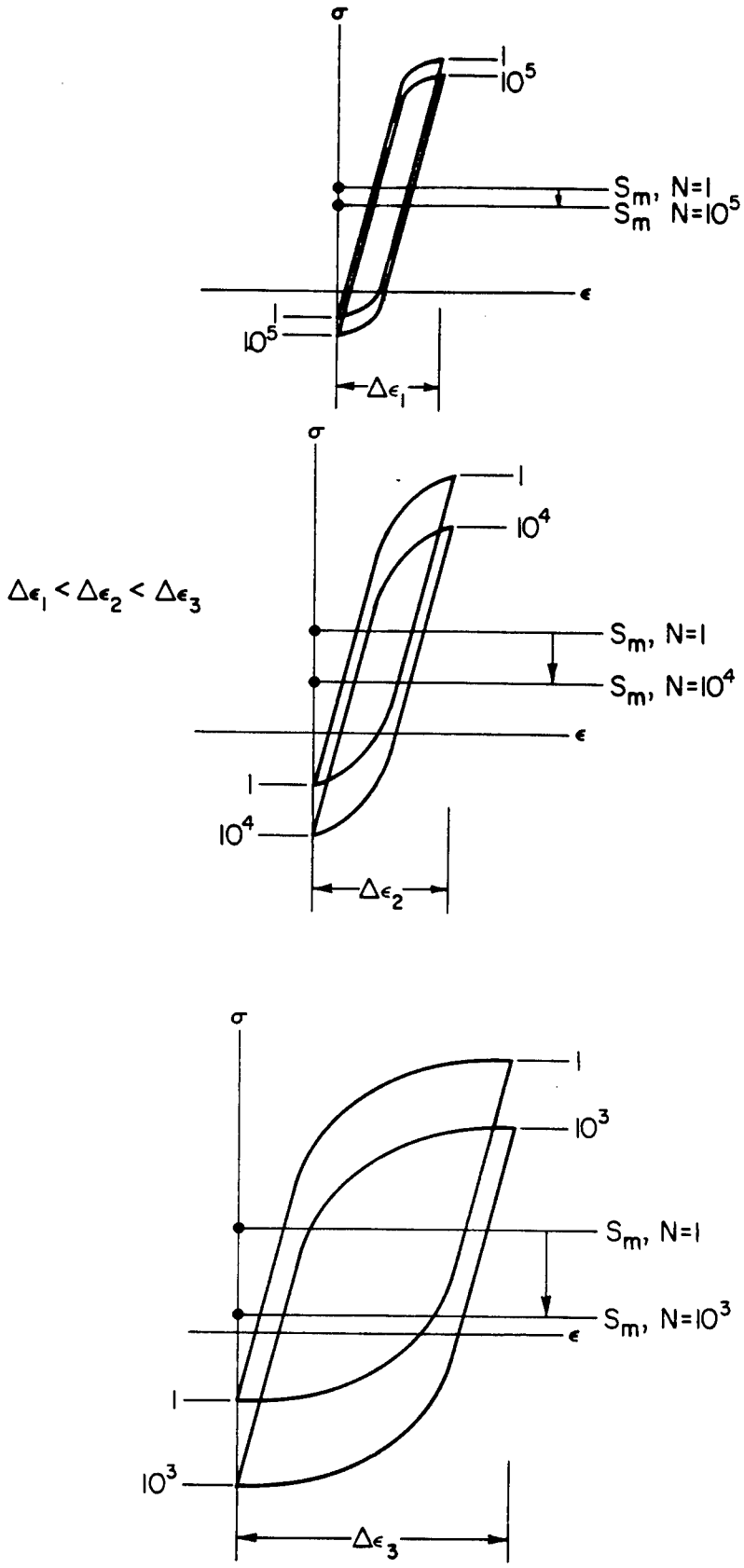


FIGURE 9.3.4.4. *Schematic of stabilized mean stress relaxation for different strain ranges at* $R_\epsilon = 0$.

The stabilized value of mean stress attained in a strain-control test at R_ε greater than -1.0 will be different from that observed at the beginning of the test for materials that undergo cyclic mean stress relaxation. The degree of stress relaxation will depend on strain range and strain ratio, the magnitude being greater at larger strain ranges or larger strain ratios. Complete relaxation to a zero mean stress is the limiting case. When testing at strain ratios greater than -1.0, it is appropriate to limit the strain ranges to values below those at which total cyclic mean-stress relaxation occurs.

The amount of cyclic stress relaxation also varies with the anticipated fatigue life. Large-strain-range, low-cycle tests usually exhibit the greatest mean stress relaxation. Because of this behavior, it is usually appropriate to run the positive mean strain experiments at strain ranges less than or equal to the level that produces complete mean stress relaxation.

A given series of fatigue tests conducted under strain control should be targeted to describe the useful life range for the material. The life range explored need only be limited on the low side by the maximum strain ranges that can be performed without specimen buckling problems, and on the high side by the maximum strain rates that are allowable, in combination with the permissible duration of individual tests. Life ranges of 10 to 10^6 cycles are reasonable to explore in strain-control tests with many materials and specimen geometries. Strain-control tests performed for inclusion in MIL-HDBK-5 should normally be conducted with symmetric waveforms, with no hold times at frequencies ranging from 0.10 to 5 Hz—depending on the response of extensometry and recording equipment. It is important to document the strain rates and conformance of the testing techniques with ASTM E606 [Reference 9.3.4.1(a)].

Long-life fatigue tests are a special situation in strain-control testing because of the extended test periods that may be required, especially if maximum test frequencies must be kept at or below 1 Hz. For example, a test run at 1 Hz involving one million cycles requires about 11-1/2 days. Decreasing the duration of long-life, strain-control fatigue tests are desirable whenever possible; otherwise, a few tests in the 10^6 to 10^7 cycle range can take as much time as the rest of the life curve.

Switching from strain-control testing to load-control testing at a greater frequency at some point in the life of the specimen is becoming a common practice. This switch is typically done when the cyclic response is nominally elastic. Usually the frequency can be increased by a factor of 10 or more but even a factor of 2 or 3 is certainly worthwhile.

When the control mode and/or frequency are changed, certain criteria should be observed. When generating a strain-control fatigue curve, ranging from the short-life regime (10 to 10^3 cycles) to the long-life regime (10^6 to 10^8 cycles), the fatigue tests can be placed in three groups for consideration.

At the short-life end of the curve, the material response will typically vary throughout the test. In this regime, a significant amount of inelastic strain may be present, cyclic hardening or softening may occur as well as mean stress shifts. In short, no consistent relationships exist between stress and strain and, therefore, no control mode change is recommended in this life regime.

For intermediate life tests, some inelastic strain may be present and, for a period of time, the stress-strain relationship may vary. Generally, however, a stabilized, consistent relationship is eventually achieved. Under these conditions, it may be possible to switch the test mode to load control at a higher frequency.

In the long-life regime, very little inelastic strain will normally be present, and stress-strain stabilization is achieved very rapidly. Here, switching from the strain-control mode to the load-control mode can be accomplished.

The material behavior cited above can only be evaluated by starting all of the tests in the strain-control mode and then switching the mode and frequency when stabilized stress-strain behavior is achieved. An evaluation of the strain rate behavior of the material in the strain-control mode (within the normal response capabilities of the equipment) may be desirable to determine if the stress-strain relationship is likely to change when the frequency is changed.

In summary, do not switch control modes in the low life regime of the fatigue curve. When some inelastic strain is present, switching may be employed if stable stress-strain response can be obtained and a negligible strain rate effect at the test temperature and strain range of interest can be demonstrated (i.e., it can be shown that fatigue life and stress range are not influenced by loading rate). One very good check is to produce overlapping data points in this regime where some tests are run to failure in the strain-control mode while others are switched to high-frequency load-control mode after stabilization is obtained. This is necessary to provide assurance that the switching procedure is not influencing results.

At the very long-life end of the curve, the essentially elastic behavior of the material is most conducive to switching of control modes. The greatest benefit of the increased frequency can also be obtained here. If results have shown that switching is successful at the intermediate strain range level, then the probability of the long-life tests being at least as successful is high. If, however, the material exhibits a measurable inelastic strain and is slow to stabilize even after many cycles, caution should be exercised in making the decision for a control mode change.

When the determination that a test should be switched from strain control to load control has been made, the following sequence is recommended:

(1) Note the maximum and minimum stabilized load levels.

(2) Gradually reduce the strain range to zero. This process should take several cycles (at least 10). If a measurable inelastic strain is present, the strain range reduction should take sufficient cycles so the magnitudes of the maximum and minimum loads are reduced symmetrically.

(3) At this point (strain range at zero) the load may or may not be at zero, depending on the conditions of strain ratio and strain range to which the specimen was exposed. If a residual load is present, the load should be adjusted to zero by carefully changing the strain level.

(4) Next, the test system should be switched to the load-control mode and the test restarted. The strain-control cycling may have been performed using a triangular waveform. The higher frequency testing under load control generally employs a sine wave. The waveshape difference is only of secondary importance, and most machines can easily control a high frequency sine wave. The actual frequency used should be well within the capability of the test equipment so that the load can be accurately measured and controlled. Furthermore, care must be taken to avoid frequency effects, e.g., self-heating, and strain-rate effects. This is commonly a problem with tests involving a significant amount of inelastic strain.

When reproducing the maximum and minimum stresses that existed under strain-control testing, first introducing the mean load on the specimen and then gradually increasing the load range symmetrically from this point is generally preferred. Whatever procedures are used should be clearly defined and well documented.

The tendency of the load-control results to be slightly more conservative than those generated in strain-control testing is worth repeating. When a specimen develops a fatigue crack, a test that is being conducted under strain-control mode will generally exhibit a reduced tensile load as the crack propagates. Under load-control testing, the load remains constant and the crack will grow faster, resulting in a lesser

life. For this reason, all data generated by this technique should be so noted and identified on data tables and graphs.

Essentially two steps are involved in the generation of a fatigue curve for a specific stress or strain ratio. First, the general shape of the curve should be determined. Nonreplicated fatigue tests completed at not more than four to six maximum stress levels are usually sufficient to define the basic shape of the curve above the fatigue limit. After the shape of the curve is found from test results, or estimated from fatigue data on similar materials, then the mean curve should be verified through carefully planned replicate fatigue tests.

If the lower maximum stress levels or strain ranges chosen result in nonfailures or runouts*, do not repeat these stress levels while defining the general shape of the fatigue curve. Simply focus on relatively evenly spaced stress or strain levels that generally provide fatigue failures.

In performing these exploratory fatigue tests, obtaining the test specimens from a random sample that adequately represents the material is important. In that context, specimens should be taken from several different lots if possible. Particular care should also be given to minimizing nuisance variables such as test machine effects, frequency effects, surface finish irregularities, residual stress effects, or environmental variations. Unfortunately, variables such as specimen fabrication can influence fatigue results to such an extent that the effect being studied is eclipsed. Composition, thermal-mechanical processing and the origin of the material should be well documented. The same type documentation should apply to the fabrication of the specimens. ASTM E606 provides an example of a machining procedure in Appendix X3 [Reference 9.3.4.1(a)]. It is frequently referenced in machining specifications.

In addition, fabricating fatigue specimens also involves many special considerations. For example, simulating a component fabrication process for making the specimens may be desired, e.g., heat treating before or after machining. The specimens may be ground or lathe turned. A mechanical polish or electro-polish may be employed. Special processing such as shot peening, stress relieving, plating or coating may be used. All of these procedures (including their sequence) must be documented.

The formation of surface residual stresses should be recognized as one of the most influential effects of machining, although it is frequently overlooked. Any mechanical removal of material from the specimen can produce residual stresses on the surface. Even when special care is taken to remove material very gradually, residual stresses (either surface or profile) may approach the yield point of the material. Under certain conditions these stresses can have a dramatic effect on the fatigue life of the specimen. Whenever the test environment and strain range are such that these stresses are not dissipated, they can alter the stress on the surface of the specimen. Crack initiation and propagation life will therefore be affected. Machining processes for producing fatigue specimens, therefore, should be evaluated not only on the basis of machining tolerances and surface finish, but also on the magnitude, consistency, and profile of these residual stresses.

Fatigue tests that exhibit little inelastic strain are especially influenced by the procedures employed in specimen preparation. Test results in these intermediate- and long-life regimes can be very confusing and misleading if the residual stresses are not considered. These stresses should at least be measured and documented and, in some cases, it may be desirable to stress relieve or electro-polish the specimens.

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*A specific fatigue cycle limit should be chosen as a runout point, and that limit should be used for all further tests on that material, regardless of the stress or strain ratio. For materials that typically display constant amplitude fatigue limits (many steels do), a runout limit as low as 3×10^6 cycles may be satisfactory. Normally, however, a runout limits of 10^7 cycles is preferred, especially for materials that typically do not show a definite fatigue limit (many aluminums do not) and for experiments conducted at reasonably high cyclic frequencies (10^7 cycles is accumulated in less than 4 days of continuous cycling at 30 Hz). Fatigue tests for cast metals are traditionally continued to 2×10^7 cycles as a fatigue limit.

After the general shape of the fatigue curve has been identified (as shown in Figure 9.3.4.5 for three different stress and strain ratios), replicate tests at specific stress or strain levels may be performed to improve the statistical definition of the fatigue curve. Normally, replications at three levels are sufficient, if no fatigue limit is anticipated (or no attempt is to be made to define one).

The replicated stress or strain levels should be selected to represent initial estimates (based on the exploratory experiments) that would be expected to provide average fatigue lives at the extremes of the life interval of interest and at an intermediate fatigue life. For example, if load-control tests are to be performed and the fatigue performance between 10^4 and 10^6 cycles to failure is of concern, select three maximum stress levels for each stress ratio that appear likely to provide average fatigue lives of about 10^4, 10^5, and 10^6 cycles to failure, respectively.

Figure 9.3.4.5 illustrates this maximum stress and strain level selection process. As this figure suggests, specifying the levels with great precision is not necessary (or justified). The use of levels that have been established from exploratory testing may be appropriate. Use the same levels as those used on one of the exploratory tests if it results in a fatigue life near one of the life ranges of interest. The order of fatigue testing at these stress levels should be randomized for each series of replicates.

If further definition of the fatigue curve is desired in the long-life regime, replication at a fourth maximum stress level may be helpful*. To select this stress level, examine the number of runouts obtained at the lowest of the three replicated stress levels. If the number of runouts is less than 50 percent at the lowest stress level, select another, somewhat lower stress level for replication (5 to 10 percent is suggested). Alternatively, if the number of runouts at the lowest of the three replicated stress levels is above 50 percent, select a fourth replicated stress level that is somewhat higher (again, 5 to 10 percent is suggested). Using such an approach, defining a fatigue limit stress at the selected runout level in clearly defined statistical terms will, in many cases, be possible.

The amount of replication required at each maximum stress level or strain range is the key remaining issue. Reference 9.3.4.5(a) recommends a minimum of 50 to 75 percent replication for design allowables data. This translates into two to four specimens at each stress or strain level. If the data displays minor variability, two specimens per level may be sufficient. If the data are highly variable, even four specimens per level may still not clearly define a statistically significant mean fatigue curve (see Section 9.3.4.12).

Adding the number of specimens recommended for curve shape definition and the number recommended for replication, the normal minimum number of fatigue tests per curve ranges from 8 to 16. Therefore, the development of fatigue curves for three stress or strain ratios for a fatigue data display in MIL-HDBK-5 might be based on 24 to 48 specimens. If additional stress or strain ratios are to be considered, the number of recommended tests would expand further, although fewer tests may be employed at these R-ratios.

More fatigue specimens are recommended for test in developing a fatigue data display for use in MIL-HDBK-5 than are actually required by current minimum data standards (see Section 9.3.4.4). This discrepancy exists primarily because the satisfaction of current minimum data standards does not ensure a statistically significant set of fatigue curves. The chance of producing a significant set of fatigue curves is much greater if the recommended fatigue test planning procedure is used and the designed test matrix is carefully completed.

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*It is assumed here that long-life fatigue tests will be run in load control or started in strain control and switched to load control as discussed earlier.

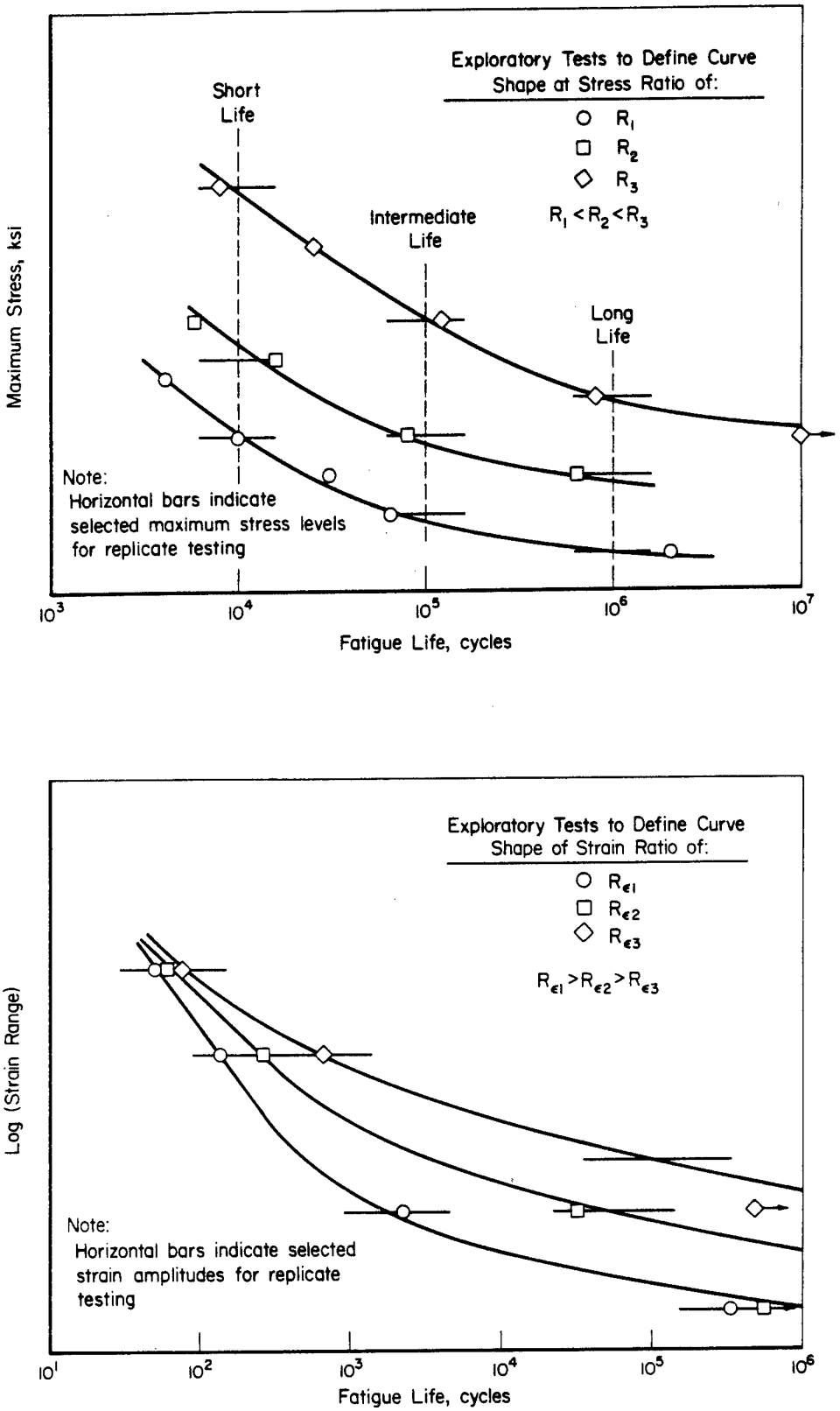


FIGURE 9.3.4.5. *Schematic fatigue data displays (showing the initial exploratory tests as symbols and the strain levels subsequently chosen for replicate fatigue testing as bars; the length of the bars denoting observed data variability).*

Strain control fatigue data for a particular material must be accompanied by sufficient information to allow the construction of a cyclic stress-strain curve. Normally, such a curve can be constructed from stress-strain pairs recorded from stable hysteresis loops. Pairs obtained from a number of different tests covering a wide range of plastic strain ranges will allow construction of a complete cyclic stress-strain curve. Results from replicated incremental step tests may also be used to construct cyclic stress-strain tests [Reference 9.3.4.5(d)].

9.3.4.6 *Data Collection*—If a set of strain- or load-control data for a material of interest meet the minimum requirements, the data should be processed for analysis. Load-control data reports should clearly specify the net section stresses, stress ratios, and associated cycles to failure. Strain-control data reports should clearly specify the strain levels used, the stable stress response values, and the associated cycles to initiation and/or failure, along with a clear and concise definition of the failure criterion. Acceptable definitions of failure in a strain-control fatigue test report include:

(1) Total specimen separation

(2) Decrease of 50 percent in the maximum or stabilized tensile load value.

Acceptable definitions of crack initiation in a strain-control fatigue test report include:

(1) First significant deviation from the stabilized load range or a stabilized rate-of-change of the load range. Detection reliability is dependent upon the sensitivity of the monitoring equipment and consequently values as small as 1 to 5 percent are used in some cases, while values as great as 10 to 20 percent are used in other cases.

(2) Verifiable results from a calibrated nondestructive inspection device, such as an electrical potential drop system.

The definition of crack initiation or failure used in a particular study must be clearly and quantitatively documented. Correlative information that is important for load or strain-control test data includes detailed specimen dimensions, fabrication procedures (and their sequence), surface finish, product form, environment, frequency, waveform, surface residual stresses, and temperature. Other useful information includes average material tensile properties, product dimensions, and manufacturer.

All fatigue data that are not listed as invalid by the author of the test report will be prepared for analysis, except for specimens tested at a maximum stress level greater than the average tensile ultimate strength of the material. The identity of different sources should be retained to determine whether combinations of data are appropriate. If all conditions from the different sources are virtually identical, the data should be analyzed together. Data should be identified as invalid if efforts in specimen preparation or testing efforts are discovered.

Runouts should be designated differently from failure data, since runouts are given special consideration in the regression analysis used to define mean fatigue curves. Runouts are generally defined as tests that have accumulated some predetermined number of cycles and have been subsequently stopped to reduce test time. Tests which have been stopped due to distinct problems encountered during testing are termed interrupted tests. Typical problems include power failures, temperature deviations, and load spikes. Interrupted tests are generally valid up until time at which the problem occurred. In this context, interrupted tests are treated the same as runouts in determining the mean fatigue-life trends of a data collection. However, if the interruption occurs long before expected failure of the specimen, the information contributed by the interrupted test is minimal, and the data point should be discarded.

Data from specimens which exhibit failures outside of the gage section may, in certain circumstances, be included in the analysis and treated as interrupted tests. Failures occurring just outside the gage

section are essentially normal failures and should be included for analysis. In strain-control tests, however, the crack initiation is not sensed by the extensometer. Failures at threads, shoulders, or button heads may be indicative of a problem with the specimen design or test procedure.

Strain-control fatigue data must be accompanied by sufficient information to construct a cyclic stress-strain curve. The cyclic stress-strain curve may be established based on incremental stress-strain results or multiple specimen data for which stable stress amplitudes are defined for the complete range of strain ranges. The method used to define the cyclic stress-strain curve must be recorded so that it can be included in the correlative information along with the strain-life fatigue data displays.

9.3.4.7 *Analysis Procedures*—Once a collection of data is reviewed (see Section 9.3.4.6) and compiled for the material of interest, analysis of that data may begin. An outline of the analysis procedure that is normally followed is given in Figure 9.3.4.7. Each of the elements in the flow chart are discussed in the following sections.

The same basic analysis procedure is used for strain- and load-control data except these data types are normally analyzed separately even if they represent the same material and product form. The only case where load- and strain-control data can be combined is the situation where some specimens have been switched from strain- to load-control testing. In this case, the load- and strain-control data may be analyzed on an equivalent strain basis. In all other cases, load-control data should be analyzed on an equivalent stress basis. Load-control data generated at different stress concentrations should always be analyzed separately.

9.3.4.8 *Fatigue Life Models*—To clarify the fatigue data trends for a specific stress or strain ratio, a linear regression model can be applied as follows:

$$\log(N_i \text{ or } N_f) = A_1 + A_2 \log(S_{max} \text{ or } \Delta\varepsilon). \qquad [9.3.4.8(a)]$$

Note that fatigue life is specified as the dependent variable. The alternative approach, using stress or strain as the dependent variable, is sometimes used, but this procedure will not be employed in developing mean fatigue curves in MIL-HDBK-5. The use of fatigue life or, more specifically, logarithm (base 10) of fatigue life as the dependent variable will be used since stress or strain is the controlled parameter in a fatigue experiment, and the resultant fatigue life is a random variable.

If Equation 9.3.4.8(a) does not adequately describe long-life data trends, a nonlinear model (or a more complicated linear model) may be warranted. For example, long-life, load-control data might be modeled by the non-linear expression

$$\log N_j = A_1 + A_2(S_{max} - A_3) \qquad [9.3.4.8(a)]$$

or by the more complicated equation [Reference 9.3.4.8]

$$\log N_f = A_1 + A_2 \log S_{max} + A_3 \sqrt{\log S_{max} + A_4} \qquad [9.3.4.8(c)]$$

These more complex forms should only be employed in instances where they are warranted based on a distinct fatigue limit at long lives and when the simpler linear model was inadequate.

Standard least squares regression analysis and the procedure for detecting outliers in Section 9.3.4.11 require that the variance be relatively constant at all fatigue life values. Traditionally, the logarithm of fatigue life is approximated by a normal distribution. However, the variability or scatter of fatigue life is generally not constant, but increases with increasing fatigue life. To ensure the reliable use of the outlier

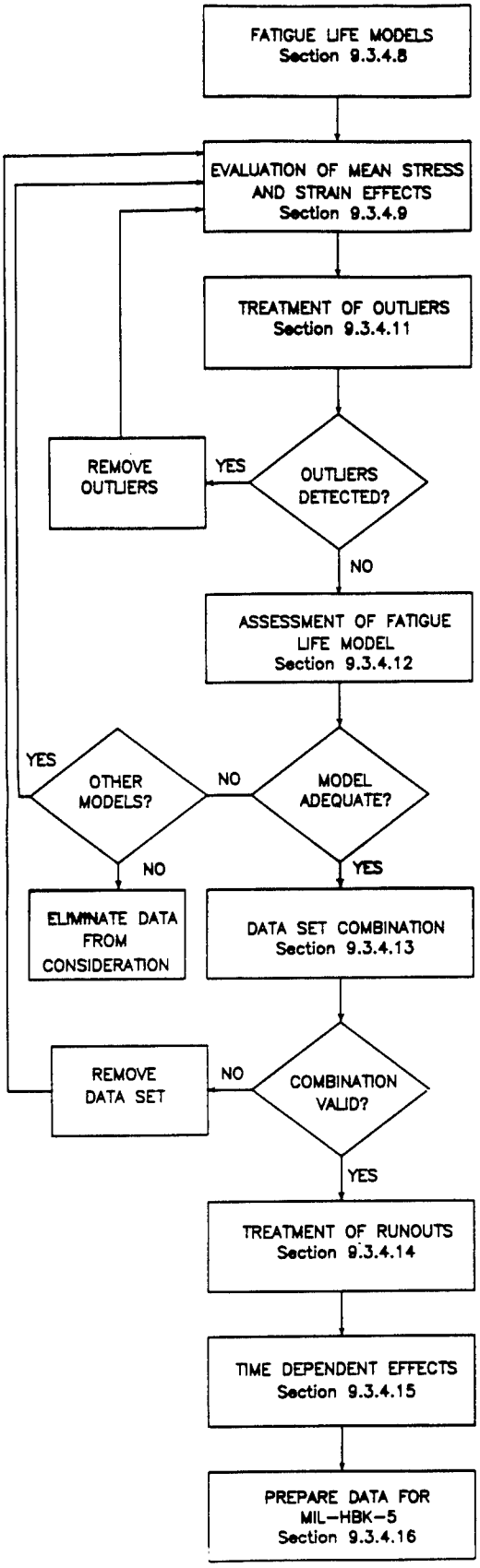


FIGURE 9.3.4.7. *Flow chart of general fatigue analysis procedure.*

detection procedure, a weighting scheme designed to produce a more uniform distribution of residuals is suggested in Section 9.3.4.10.

9.3.4.9 *Evaluation of Mean Stress and Strain Effects*—Commonly, load-controlled fatigue data generated over a range of stress ratios can be represented by the following equivalent stress-fatigue life formulation:

$$\log N_f = A_1 + A_2 \log (S_{eq} - A_4) \qquad [9.3.4.9(a)]$$

where

$$S_{eq} = (\Delta S)^{A_3}(S_{max})^{1-A_3}$$

$$S_{eq} = S_{max}(1 - R)^{A_3}$$

The equivalent stress model (and the related equivalent strain model) are derived from Reference 9.3.4.9(a).

Equation 9.3.4.9(a) is nonlinear in its general form and must, therefore, normally be optimized through use of a nonlinear regression package. However, the above equation can be solved through a linear analysis, if A_3 and A_4 are optimized through an iterative solution. The parameter A_3 normally lies in the range of 0.30 to 0.70, while A_4 represents, in essence, the fatigue limit stress. In cases where the optimum value of A_4 is negative or insignificant, it should be omitted. Unnotched data, especially aluminum alloy data, can frequently be represented without using the nonlinear A_4 term. Parameter optimization is discussed more thoroughly in Section 9.3.4.10.

If A_4 is zero or set equal to zero, Equation 9.3.4.9(a) becomes linear in log S_{max} and log (1-R), and it can be written as follows:

$$\log N_f = A_1 + A_2 \log S_{max} + B \log (1-R) \qquad [9.3.4.9(b)]$$

where $B = A_2A_3$. Thus, if A_4 is zero, then

$$A_3 = B/A_2$$

Strain-controlled fatigue data generated over a range of strain ratios often can be consolidated by the following equivalent strain formulation:

$$\log N_f = A_1 + A_2 \log (\varepsilon_{eq} - A_4) \qquad [9.3.4.9(c)]$$

where

$$\varepsilon_{eq} = (\Delta\varepsilon)^{A_3}(S_{max}/E)^{1-A_3} \quad .$$

Note that Equation 9.3.4.9(c) is very similar in form to Equation 9.3.4.9(a). It is important to note, however, that the maximum stress value used in Equation 9.3.4.9(c) is not a controlled quantity. It is a measured quantity and its magnitude depends primarily on the amount of cyclic softening or hardening that occurs in combination with mean stress relaxation. Although S_{max} can be predicted with reasonable

accuracy if the cyclic response of the material is well established, using the stable measured values of S_{max}, when analyzing strain-control data for presentation in MIL-HDBK-5, is preferred.

The equivalent stress and strain approaches are very useful for computing mean fatigue life estimates for conditions intermediate to those for which the test data have been generated. Caution should be used, however, in making life predictions for stress/strain conditions beyond the range of those represented in the data base. Also, when only two stress/strain ratios are used in the equivalence formulation, fatigue life estimates at conditions other than those two ratios (either intermediate or beyond) may be unreliable.

If the basic formulations just described do not realistically represent the data, alternative equivalent stress or strain formulations should be considered. Two formulations [References 9.3.4.9(a) and (b)], in particular, may apply in these specific instances where equivalent stress is defined as:

$$S_{eq} = S_a + A_3 S_m \qquad [9.3.4.9(d)]$$

or

$$S_{eq} = S_a + S_m^{A_3} \qquad [9.3.4.9(e)]$$

and equivalent strain is defined as:

$$\varepsilon_{eq} = \varepsilon_a + A_3 S_m/E \qquad [9.3.4.9(f)]$$

or

$$\varepsilon_{eq} = \varepsilon_a + (S_m/E)^{A_3} \qquad [9.3.4.9(g)]$$

where

S_{eq} = equivalent stress
ε_{eq} = equivalent strain
S_a = alternating stress
S_m = mean stress
ε_a = alternating strain
E = elastic modulus (from each test result).

Other data consolidation parameters may also be used provided they do not violate other guideline requirements, and they can be proven adequate. Adequacy may be assessed by employing the procedures described in Section 9.3.4.12.

To evaluate the adequacy of one equivalent stress or strain formulation compared to another, it is also useful to construct a plot of residuals versus stress or strain identifying individual stress or strain ratios. In this way the usefulness of a given formulation for modeling stress or strain ratio effects is visually apparent.

9.3.4.10 *Estimation of Fatigue-Life Model Parameters*—The fatigue-life model parameters are estimated to obtain the best-fit S/N or ε/N curve for the data. The procedure used to determine the parameters includes a statistical method for adjusting the fatigue model for the nonconstant variance commonly observed in long-life fatigue data. The motivation for this adjustment is the fact that constant variance is an inherent assumption in least squares regression analysis. To estimate the parameters in

Equation 9.3.4.9(a) or Equation 9.3.4.9(c) and adjust the model to incorporate nonuniform variance, the following six-step procedure is performed.

Step 1 - Initial Parameter Estimates. If A_4 is assumed to be zero, then a linear least squares regression analysis is performed to obtain the initial parameter estimates for A_1, A_2, and A_3. If A_4 is to be estimated from the data, a nonlinear least squares regression analysis is performed to obtain the initial parameter estimates for A_1, A_2, A_3, and A_4. Runout observations above the minimum equivalent stress (strain) at which a failure occurred should be included in the calculation of the initial parameter estimates and residuals.

To facilitate convergence of the nonlinear least squares fit when A_4 is to be estimated from the data, the following procedure may be used to obtain starting values. Set A_3 equal to 0.5 and calculate equivalent stress (strain) values for each observation. Set A_4 equal to one-half the smallest equivalent stress (strain) not associated with a runout. Using these values of A_3 and A_4 as constants, obtain least squares estimates of A_1 and A_2 usng a linear regression routine.

Step 2 - Fitting the Varibility Model. The magnitude of the residuals from these fatigue-life models typicaly increases with decreasing stress or strain as illustrated in Figure 9.3.4.10(a). The residuals plotted are the observed log(life) values minus the predicted log(life) values.

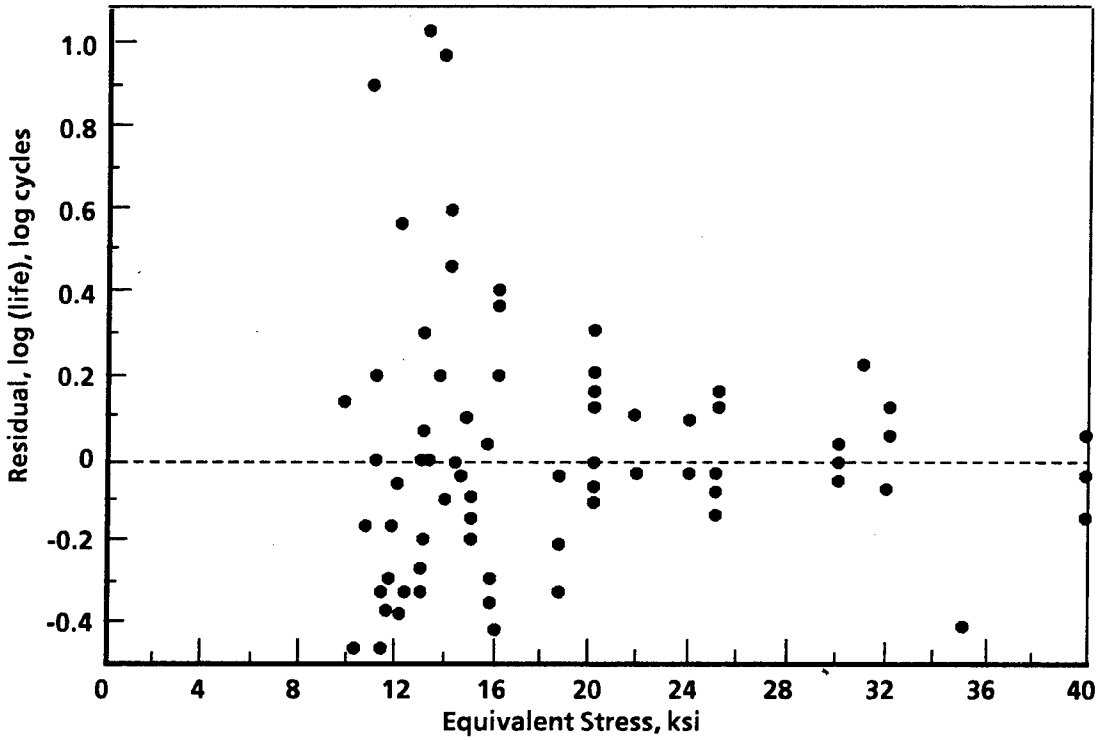


FIGURE 9.3.4.10(a). *Example plot showing increasing magnitude of residuals with decreasing stress/strain levels.*

To evaluate the fatigue-life model for nonuniform variance, it is useful to construct a model to estimate the standard deviation of log(life) as a function of equivalent stress (strain). If there is nonuniform variance, such a model can then be used to perform a weighted regression to estimate the fatigue life model parameters where the weight for each observations inversely proportional to its estimated variance.

The suggested standard deviation model is

$$\frac{|R|}{\sqrt{2/\pi}} = \sigma_o + \sigma_1 \left[\frac{1}{S_{eq}}\right] = g(S_{eq}) \qquad [9.3.4.10(a)]$$

$$\frac{|R|}{\sqrt{2/\pi}} = \sigma_o + \sigma_1 \left[\frac{1}{\varepsilon_{eq}}\right] = h(\varepsilon_{eq})$$

where R (observed log(life) minus predicted log(life)) represents the residuals from the fatigue life model fitted in Step 1. This model assumes that the standard deviation of log(life) is a linear function of the reciprocal of equivalent stress (strain). The absolute values of the residuals are divided by $\sqrt{2/\pi}$ so that $g(S_{eq})$ or $h(\varepsilon_{eq})$ is an estimate of the standard deviation of log(life).

The intercept, σ_o, and the slope, σ_1, are first estimated by ordinary least squares. If the least squares estimate of σ_o is negative, σ_o should be set to zero and σ_1 should be estimated by performing a least squares regression through the origin (no intercept term). A 90 percent confidence interval for σ_1 should also be obtained. If the lower bound of the confidence interval for σ_1 is positive, there is evidence of nonuniform variance and one should proceed to Step 3A. If the confidence interval for σ_1 contains zero, there is no evidence of nonuniform variance and one should proceed to Step 3B. If the upper bound of the confidence interval for σ_1 is negative, this indicates abnormal behavior requiring further examination of the data set before proceeding with the analysis.

Figure 9.3.4.10(b) is a plot of the absolute values of the residuals from Figure 9.3.4.10(a) versus the reciprocal of equivalent stress. The slope and vertical intercept of the least squares line displayed in this plot are the estimated parameters σ_1 and σ_o.

Step 3A - Fitting the Weighted Fatigue Model. Adjust the fatigue model for nonconstant variance by dividing each term in the model by $g(S_{eq})$ or $h(\varepsilon_{eq})$, the estimated standard deviation of the dependent regression variable. If the four-parameter fatigue model is being used, the adjusted model becomes

$$\left[\frac{\log(N)}{g(S_{eq})}\right] = A_1 \left[\frac{1}{g(S_{eq})}\right] A_2 \left[\frac{\log(S_{eq} - A_4)}{g(S_{eq})}\right]$$

or [9.3.4.10(b)]

$$\left[\frac{\log(N)}{g(\varepsilon_{eq})}\right] = A_1 \left[\frac{1}{g(\varepsilon_{eq})}\right] + A_2 \left[\frac{\log(\varepsilon_{eq} - A_4)}{g(\varepsilon_{eq})}\right]$$

where S_{eq} and ε_{eq} are defined in Equations 9.3.4.9(a) and 9.3.4.9(c). Perform a nonlinear least squares regression analysis (no intercept) using the adjusted model to obtain new estimates of A_1, A_2, A_3, and A_4. When performing this regression, all runouts above the minimum S_{eq} or ε_{eq} at which a failure occurred should be included in the analysis and treated as failures. The inclusion of runouts in this step should be determined based on equivalent stress (strain) values using the value of A_3 estimated in Step 1.

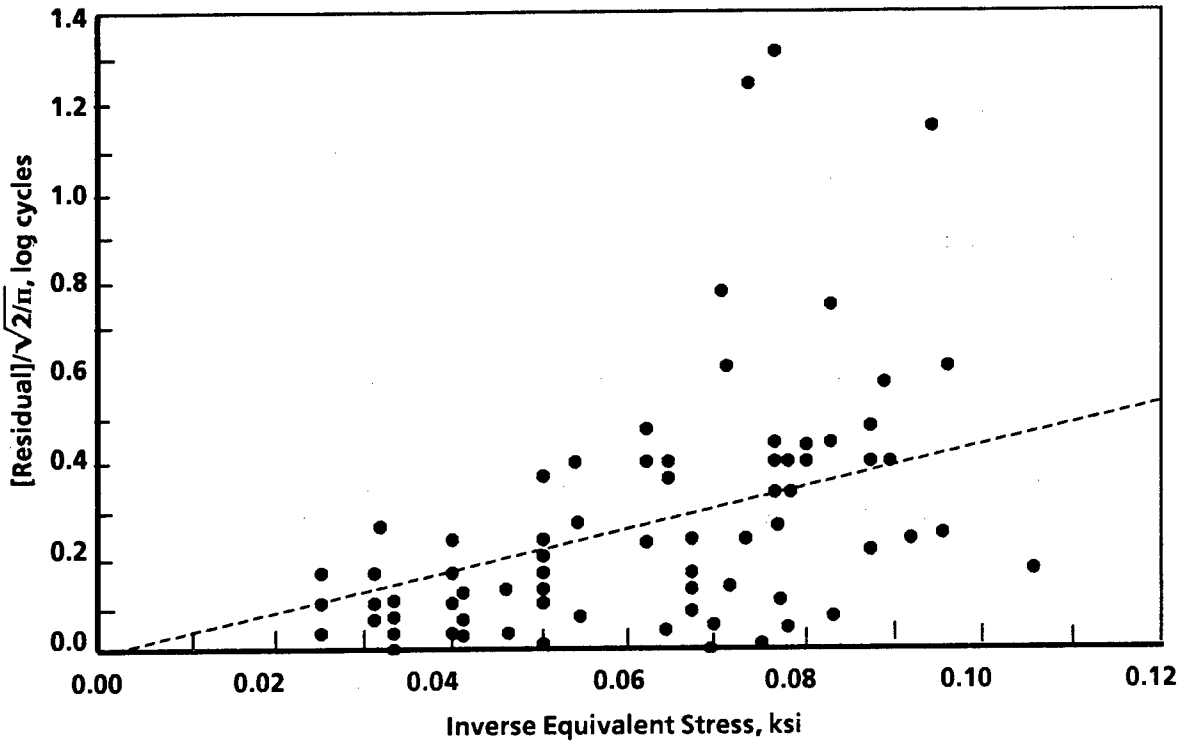


FIGURE 9.3.4.10(b). *Example plot showing the magnitude of the residuals versus the inverse of equivalent stress/strain levels.*

Assuming that the equivalent stress/strain model is valid, this qualifying stress/strain level allows the use of all runouts above stresses or strains at which failures have been observed. Below this level, there is no statistical evidence that discontinued tests would have failed. Therefore, runouts below the minimum S_{eq} or ε_{eq} value at which a failure occurred are not assigned finite life values in estimating the parameters.

It should be noted that the regression analysis performed using the adjusted model [Equation 9.3.4.10(b)] is equivalent to performing a weighted least squares regression analysis using the original fatigue life model [Equation 9.3.4.9(c)] and weights equal to $1/g^2(S_{eq})$ or $1/g^2(\varepsilon_{eq})$. Also, it may be desirable in certain situations to fit alternative standard deviation models to the residuals from Step 1. In this case, simply redefine $g(S_{eq})$ or $g(\varepsilon_{eq})$ to be equal to the desired model and follow Steps 1 through 3 above. Upon completion of Step 3A, proceed to Step 4.

Step 3B - Fitting the Unweighted Fatigue Model. Using the initial estimate of A_3 obtained in Step 1, calculate equivalent stress (strain) values for all observations including runouts. All runouts above the minimum equivalent stress (strain) at which a failure occurred should be included in the analysis and treated as failures. (See Step 3A for an explanation of this rationale.) Using the same regression techniques employed in Step 1, obtain least squares estimates of the parameters A_1, A_2, A_3, and A_4.

Step 4 - Testing the Significance of Model Parameters. Obtain a 90 percent confidence interval for A_4. If the lower bound of the confidence interval is negative, there is no evidence that A_4 is different from zero. In this case, assume A_4 is equal to zero and repeat Step 3A or 3B, eliminating A_4 from the model.

Next, obtain a 90 percent confidence interval for A_2. If the upper bound of the confidence interval is negative, this indicates that the relationship between log(life) and equivalent stress (strain) is significant. If the upper bound of the confidence interval is positive, there is no evidence of a significant

relationship between log(life) and equivalent stress (strain) and the data set should be examined further before proceeding with the analysis.

Step 5 - Re-estimating A_1 and A_2. If a weighted least squares analysis was performed in Step 3A, A_1 and A_2 should be re-estimated to include the effect of the new value of A_3 on the calculation of weights and the inclusion of runouts. First, recompute the weights $g(S_{eq})$ or $g(\varepsilon_{eq})$ using the value of A_3 obtained in Step 3A. Then perform a linear regression (no intercept) to obtain updated estimates of A_1 and A_2 in Equation 9.3.4.10(b) treating A_3 as a constant. The inclusion of runouts in this linear regression should be determined based on equivalent stress (strain) values using the value of A_3 obtained in Step 3A.

Step 6 - Estimating the Standard Deviation and Calculating Standardized Residuals. The method for estimating the "standard deviation of log(life)" (SD) depends on whether there is evidence of nonuniform variance in the fatigue life data. If an unweighted regression was performed in Step 3B to obtain the model parameters, SD should be set equal to the root mean square error (RMSE) associated with the fitted and unweighted fatigue life model. In this case, SD may be calculated as

$$SD = RMSE = \sqrt{\sum_{i=1}^{n} R_i^2/(n-k)} \qquad [9.3.4.10(c)]$$

where k is the number of parameters estimated in Step 3, and

$$R_i = \log N_i - \widehat{\log N_i} \qquad [9.3.4.10(d)]$$

where R_i is the residual, $\log N_i$ is the logarithm of observed number of cycles, and $\widehat{\log N_i}$ is the logarithm of predicted number of cycles associated with the ith observation.

If a weighted regression was performed in Step 3A to obtain the model parameters, SD should be reported as linear function of the reciprocal of equivalent stress (strain). This function should be obtained by multiplying the fitted standard deviation model $g(S_{eq})$ or $g(\varepsilon_{eq})$ from Step 2 by the root mean square error (RMSE) associated with the fitted and weighted fatigue life model to obtain an updated standard deviation model. In this case, SD may be calculated as

$$SD = RMSE * (\sigma_0 + \sigma_1/S_{eq})$$

or [9.3.4.19(e)]

$$SD = RMSE * (\sigma_0 + \sigma_1/\varepsilon_{eq})$$

where

$$RMSE = \sum_{i-1}^{n} WR_i^2/(n-k) \quad , \qquad [9.3.4.10(f)]$$

k is the number of parameters estimated in Step 3, and

$$WR_i = \frac{\log N_i - \log \hat{N}_i}{g(S_{eq,i} \text{ or } \varepsilon_{eq,i})} \qquad [9.3.4.10(g)]$$

with WR_i denoting the weighted residual and $S_{eq,i}(\varepsilon_{eq,i})$ the equivalent stress (strain) associated with the ith observation.

As a final step associated with the estimation of fatigue life model parameters, standardized residuals should be calculated for use in the judging the appropriateness of the fitted model. Standardized residuals are calculated as

$$SR_i = R_i/SD \qquad [9.3.4.10(h)]$$

where the form of the residual R_i is given in Equation 9.3.4.10(d) and the estimated standard deviation SD is given by either Equation 9.3.4.10(c) or Equation 9.3.4.10(e).

Figure 9.3.4.10(c) is a plot of the standardized residuals for the same data plotted in Figure 9.3.4.10(b) but based on a standard deviation model to correct the nonuniform variance. Note that the pattern of nonconstant variance has been eliminated.

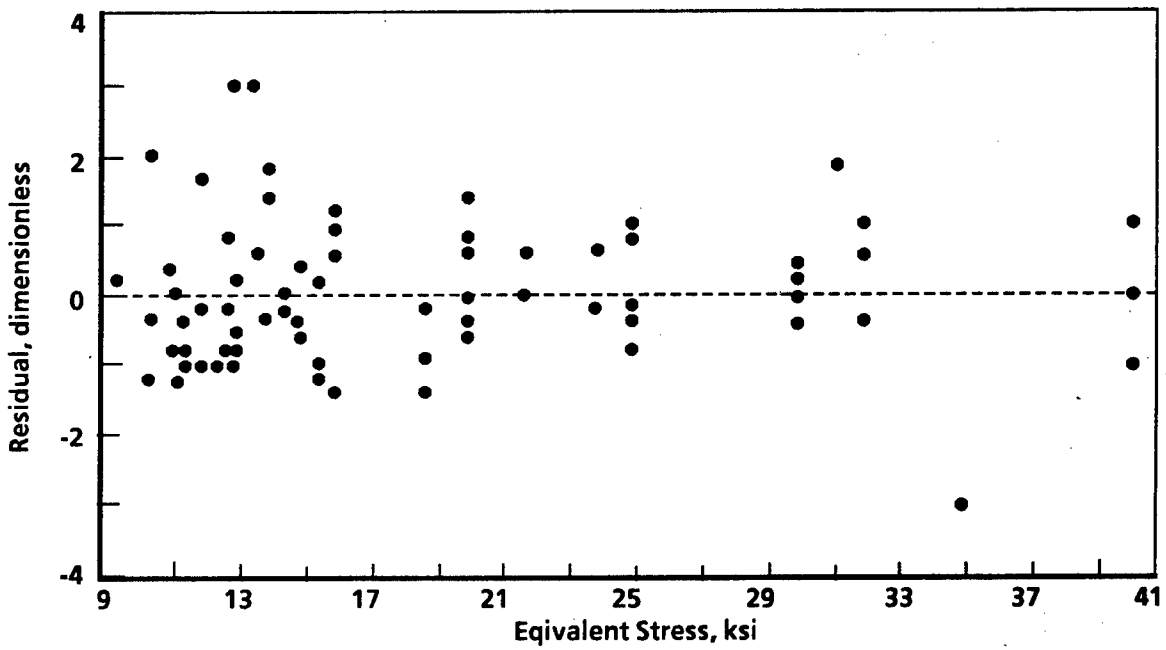


FIGURE 9.3.4.10(c). *Example plot showing constant variance of standardized residuals.*

Note - When performing any of the regression analyses described above to estimate the parameters A_1, A_2, A_3, and A_4, the estimate of A_4 should be restricted to be greater than or equal to zero. Some regression programs allow such restrictions as an option. If such an option is not available and if the estimate of A_4 is negative, set A_4 equal to zero and refit the model treating A_4 as a constant. Also note that the parameter estimates obtained from the regression analysis of Step 3A or 3B need not necessarily be reported as the final parameter estimates. If the data set includes runout observations, final estimates of the A_1 and A_2 parameters may be calculated using the maximum likelihood techniques presented in Section 9.3.4.14, provided that software for performing this procedure is available.

9.3.4.11 *Treatment of Outliers*—An outlying observation (or outlier) is one that appears to deviate markedly from other observations in the sample in which it occurs. Outliers may essentially be classified into two groups:

(1) An extreme value of the random variable inherent in the data (in this case fatigue life). If this is true, the value should be retained in future analyses.

(2) An unusual result caused by a gross deviation in material or prescribed experimental procedure or an error in calculating or recording any experimental data.

An outlier of the second type is sometimes correctable by a review of the test sample and/or test records, which may provide sufficient evidence for rejection of the observation. An outlying value from a failure that occurred in the fillet of an unnotched fatigue test sample is an example of a potentially rejectable result based on physical evidence alone. The more difficult case is one where an observation is an obvious outlier and no physical reasons can be identified to justify its exclusion.

Assuming uniform variance in the standardized residuals over the complete range in equivalent stress or strain, the problem of identifying certain observations as potential outliers should be addressed as follows. Calculate the studentized residuals,

$$T_i = \frac{SR_i}{(1 - h_i)^{1/2}} \left[\frac{RMSE}{RMSE(i)} \right]$$

for i = 1, ..., n where SR_i is the standardized residual from Equation 9.3.4.10(h), RMSE is the root mean square error based on the entire sample as calculated in either Equation 9.3.4.10(c) or Equation 9.3.4.10(f), and RMSE(i) is the root mean square error based on the sample which excludes the ith observation as calculated by either Equation 9.3.4.10(c) or Equation 9.3.4.10(f).

The value h_i is calculated using the formula

$$h_i = \frac{X_{1i}^2 \left(\Sigma X_{2j}^2\right) - 2 X_{1i}X_{2i} \left(\Sigma X_{1j}X_{2j}\right) + X_{2j}^2\left(\Sigma X_{1j}^2\right)}{\left(\Sigma X_{1j}^2\right)\left(\Sigma X_{2j}^2\right) - \left(\Sigma X_{1j}X_{2j}^2\right)}$$

where X_{1i} is the value of 1/SD for the ith specimen, S_{2i} is the value of $\log(S_{eq}\text{-}A_4)/SD$ for the ith specimen and all summations are over j = 1, ..., n. Note that

$$RMSE^2(i) = \frac{(n - k)RMSE^2 - SR_1^2/(1 - h_i)}{(n - k - 1)}$$

where RMSE is the root mean square error based on the entire sample as calculated in either Equation 9.3.4.10(c) or Equation 9.3.4.10(f) and k is the number of parameters estimated in Step 3 of Section 9.3.4.10.

It can be shown that each T_i has a central t distribution with n-k-1 degrees of freedom. Applying the Bonferroni inequality [Reference 9.3.4.11] to obtain a conservative critical value leads to the following outlier test. Calculate the maximum absolute studentized residual

$$G = \max [T_i]$$

and declare the data value corresponding to G to be an outlier if

$$G > t(\alpha/2n, n - k - 1)$$

where $t(\alpha/2n,n-k-1)$ is the upper $\alpha/2n$ percentile point of the central t distribution with n-k-1 degrees of freedom and α represents the significance level of the outlier test. Under the hypothesis that no outliers are present in the data, the probability is less than α that the data value corresponding to G will be falsely declared an outlier.

In applying this test to fatigue life data, a significance level of $\alpha = 0.05$ is used and the test is first applied to the entire sample. If an outlier is detected, the outlying observation is removed from the sample and the entire analysis is repeated on the smaller sample of n-1 observations starting with Step 1 of Section 9.3.4.10. (When a nonlinear least squares fit is performed in Step 1, use the current estimates for A_1, A_2, A_3, and A_4 as starting values rather than following the starting value algorithm.) This process of removing outliers and repeating the analysis continues until no outliers are detected in the remaining sample. For strain-control data, apply the procedure described above replacing S_{eq} with ε_{eq} throughout.

The data analyst may also wish to carry out the outlier test procedure using a significance level of $\alpha = 0.20$ in order to identify additional observations that may warrant investigation. To identify even more suspect observations, a larger significance level may be used. Any data values identified by this procedure should be examined but retained in the data set unless physical evidence justifies their exclusion.

9.3.4.12 *Assessment of the Fatigue Life Model*—The fit of the fatigue model S/N curve to the data may be assessed in two ways—the adequacy of the equivalent stress/strain model and the adequacy of the fatigue life model. The equivalent stress model lack of fit test and the overall lack of fit test described below provide a reasonable assessment of the fatigue life model.

When three or more stress (strain) ratios are used, the fit of the equivalent stress (strain) model may be tested by determining the relationship between the standardized residuals from Equation 9.3.4.10(h) and stress (strain) ratio. A difference in the means of the standardized residuals at each stress (strain) ratio indicates that the equivalent stress (strain) model is inadequate. To determine whether or not there is a statistically significant difference in the means of the standardized residuals at each stress (strain)

ratio, an analysis of variance should be performed on the standardized residuals using stress (strain) ratio as the treatment variable. A statistical F-test should be used to determine if the effect of stress ratio is significant at the 5 percent level [Reference 9.3.4.12]. The equivalent stress (strain) model should be considered inadequate when the effect of stress (strain) ratio is significant according to the statistical F-test.

The plot of the standardized residuals versus stress ratio shown in Figure 9.3.4.12(a) illustrates such a relationship between the standardized residuals and stress ratio. Since there would be no such

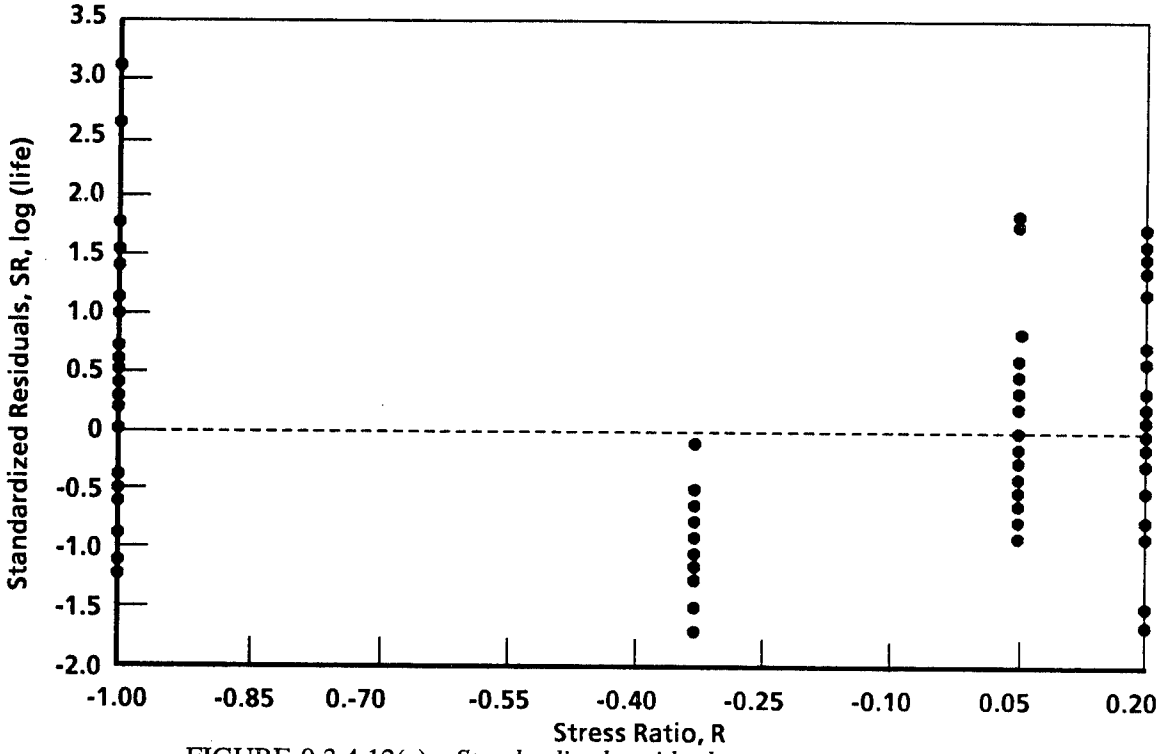


FIGURE 9.3.4.12(a). *Standardized residuals versus stress ratio.*

relationship if the equivalent stress model were adequate, the plot indicates that the equivalent stress model must have been misspecified in this case. In addition to the lack of fit shown by differences in standardized residual means, other types of lack of fit could exist. Therefore, it would be prudent to examine stress-life plots in addition to performing the statistical test for lack of fit of the equivalent stress model.

If the equivalent stress (strain) model is inappropriate, then a new equivalent stress (strain) model should be selected. When a suitable stress (strain) model is not available, an alternative strategy is to present the data with best fit regression lines for each stress (strain) ratio. To be acceptable, each curve must meet minimum data requirements and satisfy significance checks as discussed in Section 9.3.4.10. This approach is less desirable than the equivalent stress (strain) modeling approach because it requires the estimation of fatigue trends using a graphical technique for intermediate conditions where no data exist. It should, therefore, be used only in cases where significant fatigue data collections cannot be handled by standard procedures.

Once an equivalent stress (strain) model has been found that describes the general fatigue data trends for all stress (strain) ratios, an overall test of the fit of the fatigue model should be performed. The stress-life plot shown in Figure 9.3.4.12(b) is characteristic of an overall lack of fit. To identify such a lack of fit, the Durbin-Watson test may be used [Reference 9.3.4.12]. The statistic D should be computed according to the formula

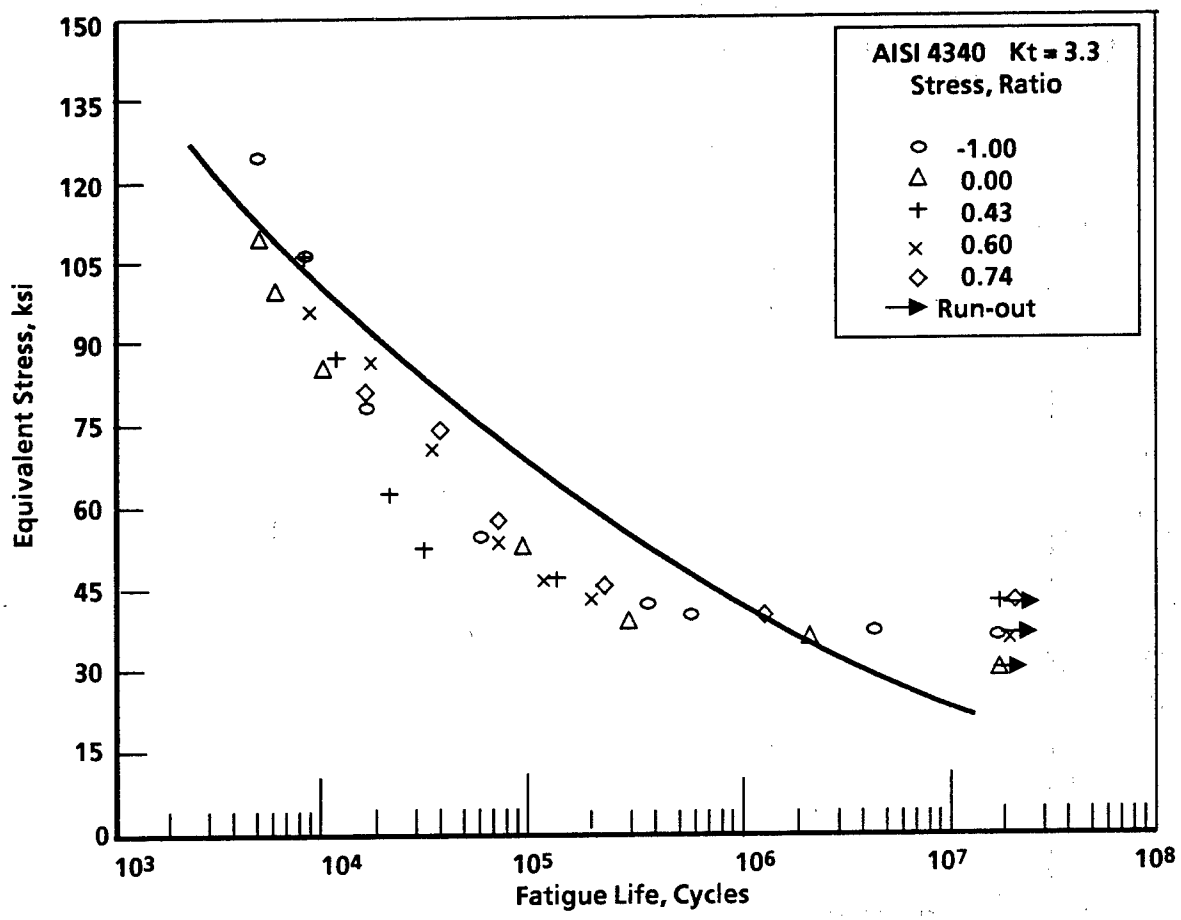


FIGURE 9.3.4.12(b). *Stress-life plot showing lack of fit.*

$$D_i = \frac{\sum_{i=2}^{n} (SR_i - SR_{i-1})^2}{\sum_{i=1}^{n} SR_i^2} \qquad [9.3.4.12(a)]$$

where SR_i is the ith standardized residual [Equation 9.3.4.10(h)] ordered by increasing values of equivalent stress(strain). If

$$D < 2 - 4.73/n^{0.555} \qquad [9.3.4.12(b)]$$

conclude that there is a significant lack of fit at the 5 percent significance level. This equation was derived from the conservative critical value (d_L) reported in Table A.6 of Montgomery and Peck [Reference 9.3.4.12]. When an overall lack of fit is determined from this test, the modeling procedure should be repeated with a more appropriate fatigue model.

9.3.4.13 Data Set Combination—In many cases, data from different sources, orientations, etc., may need to be combined for analysis. When data set combinations of this sort are performed, the validity of the combination should be tested with the method described below. The test is similar to that used to determine the adequacy of the equivalent stress (strain) model in the previous section.

If there is a relationship between the standardized residuals from Equation 9.3.4.10(h) and the data set from which they were obtained, such as that shown in Figure 9.3.4.13, then the data sets should normally

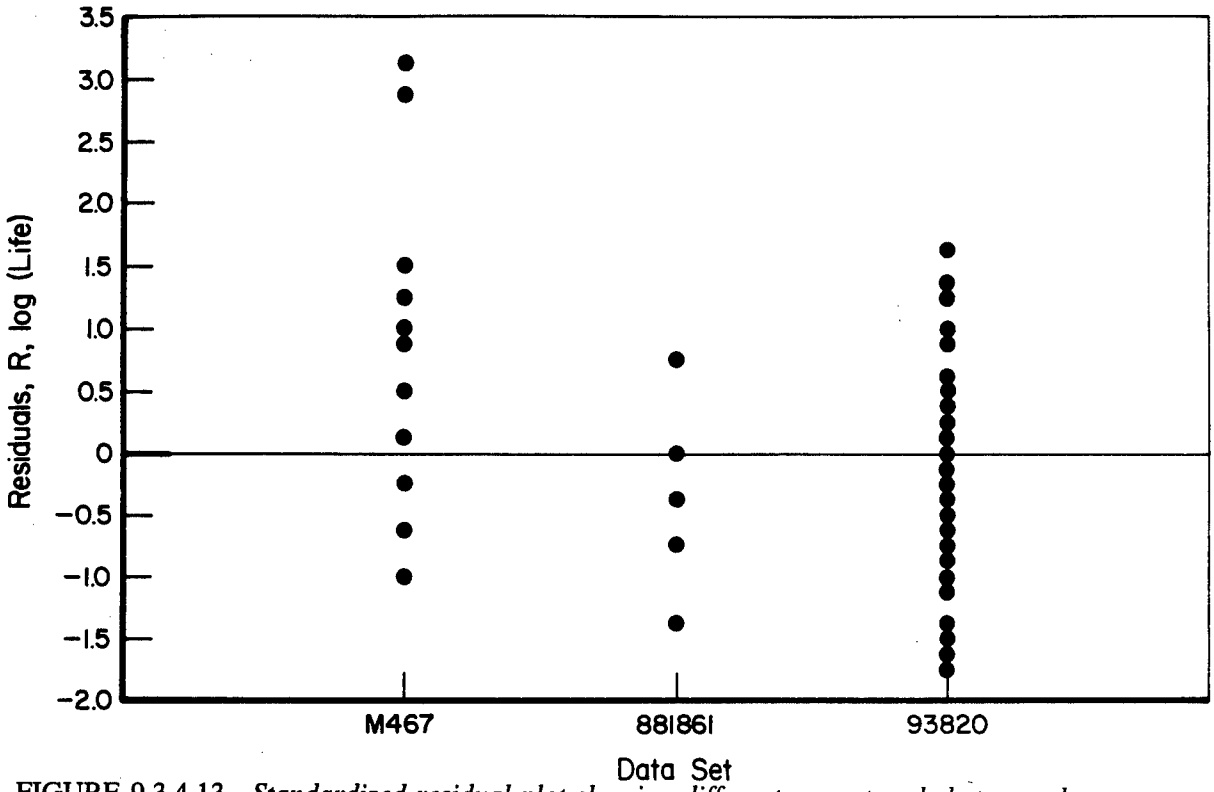


FIGURE 9.3.4.13. *Standardized residual plot showing different mean trends between data sets.*

not be combined. To determine whether or not the mean of the standardized residuals is significantly different for any of the data sets, an analysis of variance should be performed on the standardized residuals using data set as the treatment variable. The analysis of variance F-test should be used to determine if the combined data sets are significantly different at the 5 percent level.

When the data sets are found to be significantly different, at least one of the data sets should normally be removed from the data set combination. In this situation, the data analyst may wish to apply a standard multiple comparison procedure to the standardized residual data to determine which standardized residual means are significantly different from the others. For a discussion of standard multiple comparison procedures, see pages 185-201 of Winer [Reference 9.3.4.13].

There may be situations where differences between data sets are found to be statistically significant, yet these differences are so small as to be unimportant from an engineering standpoint. If a particular analysis reveals such a case, exceptions may be taken, if clearly noted and explained in the fatigue data proposal.

9.3.4.14 Treatment of Runouts—It is difficult to incorporate information from runouts (or interrupted tests) when using the least squares criterion to fit fatigue life models to data since the failure times for these observations are not known. The runouts must be either ignored or treated as failures and neither of

these alternatives adequately incorporates the information contained in the runout observations. Both of these approaches tend to produce smaller predicted lives at a given equivalent stress (strain) value than is appropriate. The treatment of runouts presented below is more appropriate but requires that two of the fatigue life model parameters be estimated by maximum likelihood techniques rather than by least squares procedures.

The maximum likelihood procedure is employed to obtain new estimates for the parameters A_1 and A_2 in Equation 9.3.4.9(a) or 9.3.4.9(c). For the purpose of this analysis, fatigue life (cycles to failure) is assumed to be log normally distributed and the parameters A_3 and A_4 are considered to be constants which are equal to the values obtained using the procedures of Section 9.3.4.10.

The estimated values of A_1 and A_2 obtained previously are used as initial values. The maximum likelihood procedure then determines the values of A_1 and A_2 which maximize the log-likelihood function

$$L(A_1,A_2,\sigma) = \sum_{i=1}^{n} (1 - d_i) \left[\log\left(f(w_i)/\sigma\right)\right] + d_i \log S(w_i)$$

where

$$f(w) = \frac{1}{\sqrt{2\pi}} \exp\left[-\frac{w^2}{2}\right]$$

is the standard normal density function,

$$S(w) = \int_{w}^{\infty} f(t)\, dt$$

is the survival function for the standard normal distribution, d_i is equal to 1 if the ith observation is a runout and zero otherwise, σ is a scale parameter to be estimated, and

$$w_i = \left[\frac{\log(N)}{SD}\right] - A_1\left[\frac{1}{SD}\right] - A_2\left[\frac{\log(S_{eq} - A_4)}{SD}\right]$$

where N is the cycles to failure and SD is the standard deviation for the ith observation as calculated from Equation 9.3.4.10(c) or Equation 9.3.4.10(e).

For more information on the maximum likelihood procedure, see Reference 9.3.4.14(a). For use in standard data analysis, the maximum likelihood procedure is conveniently implemented in some statistical software packages such as SAS [see Reference 9.3.4.14(b)].

When runouts are present, the fitted curve produced by maximum likelihood will generally predict longer average cycles to failure at given equivalent stress (strain) values than the fitted curve produced by least squares. Although it would be desirable to update all of the parameters in the fatigue model with maximum likelihood, algorithms to perform maximum likelihood on nonlinear models are not readily available. For this reason, the least squares estimates of the parameters A_3 and A_4 must be used.

9.3.4.15 Recognition of Time Dependent Effects.—All prior discussion has been based on the assumption that time dependent effects in the fatigue data sample of interest are negligible. When dealing with elevated temperature fatigue properties of materials (or room temperature fatigue properties in a corrosive environment, for example), this assumption may not be realistic. Analysis methods that are approved for use in MIL-HDBK-5 do not account for time-dependent effects. Therefore, every effort must be made to identify data that embody significant time-dependent effects.

There are no absolute methods presently available for sensing time-dependent effects in fatigue data; however, there are some useful approximation techniques. One of the more useful approaches applied to "suspect" data is to include time-dependent terms in the regression model. If the terms are significant, there is reason to believe that the population contains time dependent data. Subdividing the data into subsets that do not show time dependent effect may be possible. If this is not possible, the data set should either be rejected or included with a disclaimer restricting usage of the data to predict performance at other frequencies or temperatures.

One other possible indicator of time dependent effects is an abnormal equivalent stress (strain) model. If data for different stress or strain ratios do not fit the customary models (as described in Section 9.3.4.9), or abnormal optimum parameters are defined the problem may be caused by time dependent effects. In the case of the primary equivalent stress (strain) formulation equation the exponent normally is between zero and one. If the A_3 exponent approaches or exceeds one, the influence of maximum stress on fatigue life is negligible. This is a very unusual result that usually indicates problems with the data sample. The problem may result from mixed sources, where the data from each source were generated at different stress (strain) ratios. Rejection of such data sets is discussed in Section 9.3.4.13. In the case of the primary equivalent stress model [Equation 9.3.4.9(a)], if the exponent (A_3) approaches or is less than zero, it indicates the influence of maximum stress on fatigue life is "too strong". This result implies that creep is affecting the data.

If data are available for a material at a range of different temperatures it may be possible to analyze these sets separately and make comparisons between best-fit mean trend lines for increasing temperatures. If the different mean trend lines are not consistent with the higher-temperature curves converging or diverging from the lower-temperature curves, there is probably a significant time-dependent effect in the data. The suspect data should either be excluded or included with a disclaimer as previously cited. If data are excluded for time-dependent effects, the preliminary analyses of those data should be included in the data proposal and reasons for their exclusion should be given.

9.3.4.16 Presentation of Fatigue Analysis Results.—Separate data presentations are made for strain-controlled and load-controlled data. The only case where load-controlled data can be presented with strain-controlled data is when long-life tests have been switched from strain to load control in accordance with recommended procedures (see Section 9.3.4.5). Separate plots should be constructed for each material, notch concentration (in the case of load-controlled data), temperature, or other documented parameters that have been demonstrated to cause significant variations in fatigue behavior.

Load-controlled data presentations should consist of a family of at least three stress ratio or mean stress curves, with at least six data points per curve covering two orders of magnitude in life. (See exceptions noted in Section 9.3.4.4). The basic data should be included on each plot, with separate symbols used for each stress ratio or mean stress. Runouts should be identified with an arrow (→). The analytically defined mean S-N curves for each stress ratio or mean stress should also be included on each plot. These curves should not be extrapolated beyond existing data.

The fatigue curve for each stress ratio should be constructed based on the following criteria:

(1) The curve should start at the greatest maximum stress for that specific stress ratio. Unnotched fatigue curves should not extend above the average tensile ultimate strength of the material.

(2) The curve shall terminate at the lowest maximum stress or longest life value, whichever is most limiting for that specific stress ratio.

In addition to the stress-life plot [such as shown in Figure 9.3.4.17(h)], a tabulation of test and material conditions should also be included. At a minimum the following information should be included with an S-N plot:

(1) Material
(2) Product Form, Grain Direction, Thickness, Processing History, Fabrication Sequence
(3) Test Parameters
- Loading
- Test Frequency
- Temperature
- Environment

(4) Average Tensile Properties
(5) Specimen Details
- Notch Description
- Specimen Dimensions

(6) Surface Condition/Surface Residual Stresses/Finish
- Finish
- Residual Stress Data

(7) Equivalent Stress Equation
- Life Equation With Parameter Estimates
- Standard Deviation of log(Life)
- Adjusted R-squared Statistic
- Sample Size

(8) Reference Numbers
(9) No. of Heats/Lots

The following cautionary note should be included with each equivalent stress equation: [Caution: The equivalent stress model may provide unrealistic life predictions for maximum stresses and stress ratios beyond those represented above.] In calculating the "standard deviation of log(life)" and the djusted R-squared statistic, all quantities should be computed using the final estimates of the fatigue model parameters and excluding runout observations.

The method for reporting the "standard deviation of log(life)" (SD) depends on whether there is evidence of nonuniform variance in the fatigue life data. If an unweighted fatigue model was fitted to the data, the single SD value from Equation 9.3.4.10(c) should be reported. If a weighted fatigue model was fitted to the data, SD should be reported as the linear function of the reciprocal of equivalent stress (strain) as calculated from Equation 9.3.4.10(e).

If an unweighted fatigue life model was fitted to the data, the adjusted R-squared statistic may be calculated as

$$R^2 = 1 - (RMSE)^2/(RTE)^2 \qquad [9.3.4.16(a)]$$

where

$$RTE = \sqrt{\sum_{i=1}^{n} D_i^2/(n-1)}$$

$$D_i = \log(N_i) - \overline{\log(N)}$$

$$\overline{\log(N)} = \frac{1}{n}\sum_{i=1}^{n} \log(N_i)$$

and RMSE is calculated in Equation 9.3.4.10(c). If a weighted fatigue life model was fitted to the data, the adjusted R-squared statistic may be calculated as

$$R^2 = 1 - (RMSE)^2 / (RTE)^2 \qquad [9.3.4.16(b)]$$

where

$$RTE = \sqrt{\sum_{i=1}^{n} WD_i^2 / (n-1)}$$

$$WD_i = \frac{\log(N_i) - \overline{\log(N)}}{g(S_{eq,i} \text{ or } \varepsilon_{eq,i})}$$

$$\overline{\log(N)} = \frac{\sum_{i=1}^{n} \log(N_i) / g(S_{eq,i} \text{ or } \varepsilon_{eq,i})}{\sum_{i=1}^{n} \left(1/g(S_{eq,i} \text{ or } \varepsilon_{eq,i})\right)}$$

and RMSE is as calculated in Equation 9.3.4.10(f).

Strain-controlled data presentations should consist of a plot of log(strain range) versus log(life) and a separate graph displaying the monotonic and cyclic stress-strain response for the material. Normally the fatigue curves should be based on at least six data points for each of three or more strain ratios, and the data should cover at least two orders of magnitude in life. As with the load-controlled data, the individual data points should be included on each plot, with separate symbols used for each strain ratio. If runouts are included in the data, they should be identified with an arrow (→). Data points that are based on tests that were switched from strain to load control should be identified clearly. The mean curves should extend from slightly above the greatest strain value to slightly below the least strain value.

Plotting the strain-life curves for different strain ratios is not as straightforward as plotting stress-life curves. The equivalent strain models cannot be written explicitly in terms of R_ε. Therefore, other information must be used to model the data trends for the various strain ratios. The mean-stress relaxation behavior for each strain ratio must be identified and mathematically defined. In general, the onset of mean stress relaxation occurs at smaller strain amplitudes for larger strain ratios. This behavior is shown

in the mean stress relaxation plot of Figure 9.3.4.16(a). The elastic response (dashed lines) predicts much higher mean stresses than those actually observed, suggesting that mean stress relaxation has occurred. The regression line correlating the relaxed mean stresses with strain amplitude intersects the elastic response lines at larger strain amplitudes for smaller strain ratios. The elastic response line for the higher strain ratio ($R_\varepsilon = 0.6$) intersects the mean stress relaxation line at approximately $\Delta\varepsilon/2 = 0.0007$. The elastic response line for the lower strain ratio ($R_\varepsilon = 0.0$) intersects the mean stress relaxation at approximately $\Delta\varepsilon/2 = 0.002$. This information can be used to construct reasonable mean curves for each strain ratio for which fatigue data are available.

Considering the primary equivalent strain relation [Equation 9.3.4.9(c)]

$$\varepsilon_{eq} = (\Delta\varepsilon)^{A_3} (S_{max}/E)^{1 - A_3} \quad ,$$

S_{max} can be written as

$$S_{max} = S_m + S_a$$

where S_m is the relaxed mean stress and S_a is the stress amplitude found from the cyclic stress-strain curve. Given the mean stress relaxation data, both S_m and S_a can be estimated for a particular strain amplitude and strain ratio. Once S_{max} is defined, based on S_a and S_m, ε_{eq} can be calculated and a fatigue-life can be determined. Through this procedure an approximate mean curve can be constructed for each strain ratio as shown in Figure 9.3.4.16.

If the stress amplitude (S_a) and the mean stress relaxation pattern can reasonably be assumed to be independent of strain ratio, the following procedure may be used to construct mean curves for each strain ratio by expressing S_a as a function of the strain range and S_m as a function of strain range and strain ratio. Using the data corresponding to a strain ratio of $R_\varepsilon = -1$ only, fit the regression equation

$$\log(s_{max}) = \alpha_1 + \beta_1 \log (\Delta\varepsilon/2 - S_{max}/E)$$

In some cases it may be necessary to exclude small plastic strain observations from the regression, because of the scatter (and likely unreliability) in these values. In other words, it is recommended that the cyclic stress-strain curve be defined, through at least squares regression treating stress as the dependent variable, with consideration given to a cutoff in cyclic plastic strain. A cutoff of approximately 0.0001 in plastic strain amplitude is often useful.

Assuming that stress amplitude is independent of strain ratio and provided that the estimate of the parameter β_1 is greater than zero, a mean value for stress amplitude can be determined as a function of strain range by solving the formula

$$S_a / E + (S_a/k)^{\frac{1}{n}} = \Delta\varepsilon/2 \qquad [9.3.4.16(c)]$$

for S_a where E is the average elastic modulus for all specimens tested and

$$n = \beta_1 \text{ and } k = \text{Alog } (\alpha_1) \quad .$$

If the estimate of the parameter β_1 is less than or equal to zero, the data set should be examined further before proceeding with the analysis.

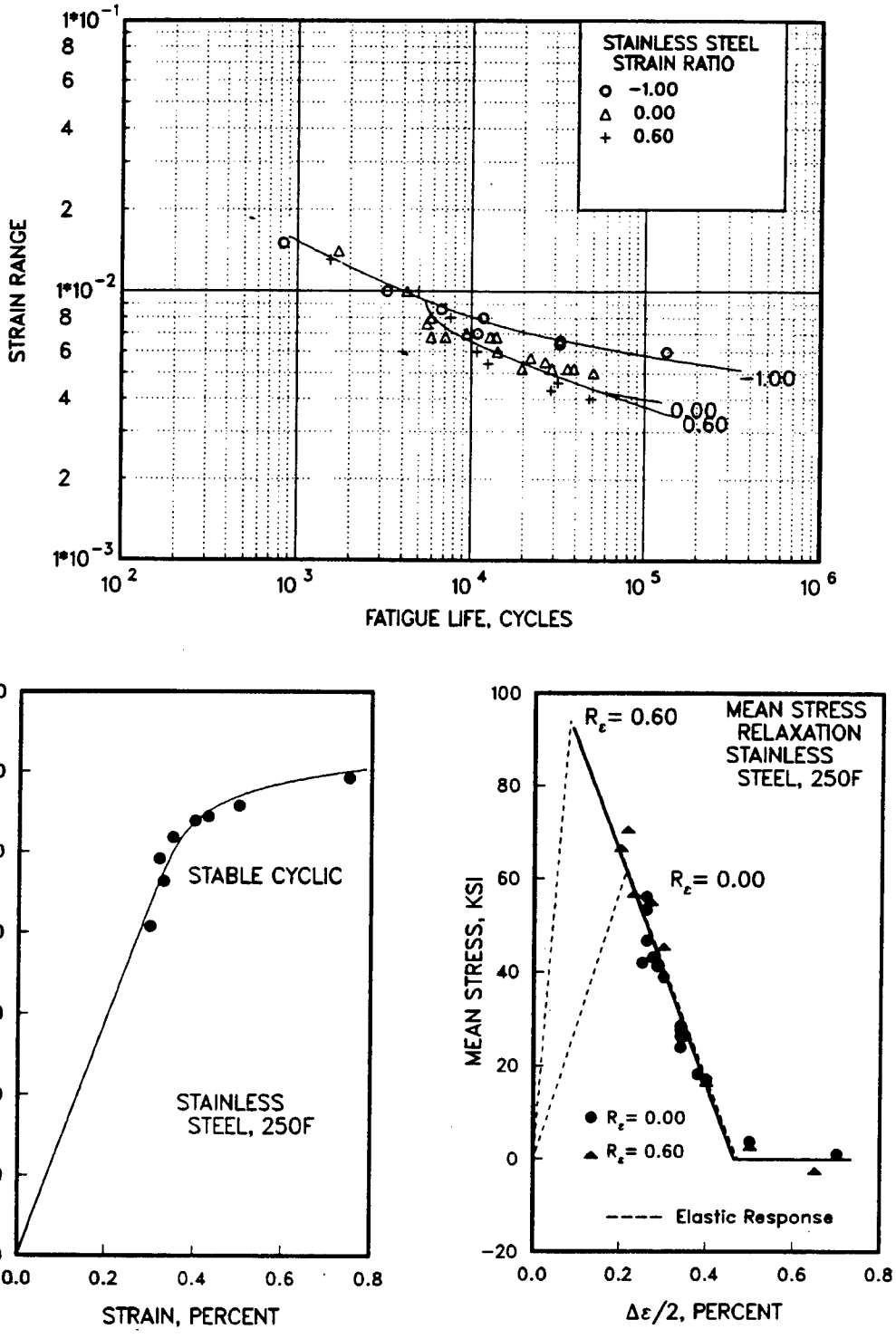


FIGURE 9.3.4.16(a). *Example strain-life, cycle stress-strain, and mean stress relaxation curves.*

Using the data corresponding to all strain ratios other than $R_\varepsilon = -1$, fit the regression equation

$$S_m = \alpha_2 + \beta_2 (\Delta\varepsilon/2)$$

using weighed least squares to give higher weight to the observations which exhibit partial mean stress relaxation. If there is not way to directly calculate S_m from the data reported in the data set, an S_m value for use in fitting the above regression equation may be calculated by solving Equation 9.3.4.16(c) for S_a and subtracting this value from the reported S_{max} value. The weighting function

$$w = \left(|S_m|/S^*\right)\left(1 - S_m/S^*\right)^2$$

where

$$S^* = \left[(1 + R_\varepsilon) / (1 - R_\varepsilon)\right] E (\Delta\varepsilon/2)$$

appears to work well in general. Assuming that the mean stress relaxation pattern is independent of strain ratio and provided that the estimate of the parameter β_2 is less than zero, a mean value for S_m can be determined as a function of strain range and strain ratio according to the formula

$$S_m = \begin{cases} \beta_3(\Delta\varepsilon/2) & (\Delta\varepsilon/2) \leq \alpha_2/(\beta_3 - \beta_2) \\ \alpha_2 + \beta_2(\Delta\varepsilon/2) & \alpha_2/(\beta_3 - \beta_2) \leq \Delta\varepsilon/2 \leq -\alpha_2/\beta_2 \\ 0 & -\alpha_2/\beta_2 \leq (\Delta\varepsilon/2) \end{cases}$$

where

$$\beta_3 = \left[(1 + R_\varepsilon)/(1 - R_\varepsilon)\right] E$$

If the estimate of parameter β_2 is greater than or equal to zero, the data set should be examined further before proceeding with the analysis.

Mean curves determined according to the above procedures exhibit the following characteristics:

(1) At large strain ranges, enough plastic strain is available to relax at the mean stress to zero, regardless of the strain ratio. Therefore, all strain ratios result in equivalent predicted fatigue lives.

(2) At strain ranges corresponding to mean stresses represented by the relaxation regression line, strain ratios other than $R_\varepsilon = -1$ (zero mean stress) result in equivalent predicted fatigue lives.

(3) At low strain ranges, the individual strain ratios assume their elastic mean stress response and diverge from each other.

The above procedure is used for plotting the strain-life curves in MIL-HDBK-5 when multiple strain ratios are involved.* The curves generally represent the mean data trends closely.

*In the general case, data generated at different strain ratios will not necessarily follow the same mean stress relaxation pattern. If different patterns for each strain ratio are evident in a particular case, it is suggested that a family of mean stress relaxation curves be constructed.

In addition to the strain-life plot, stress-strain curves and mean stress relaxation curves should be presented as shown in Figure 9.3.4.16(a). A tabulation of test and material conditions should also be included as shown in Figure 9.3.4.16(b). This information should include:

(1) Material
(2) Product Form, Grain Direction, Thickness, Processing History, Fabrication Sequence
(3) Test Parameters
- Strain Rate and/or Frequency
- Wave Form
- Temperature
- Environment
(4) Average Tensile Properties
(5) Stress-Strain Equation
- Monotonic (if available and appropriate) - Cyclic
(6) Specimen Details
- Specimen Type
- Specimen Dimensions
- Fabrication Sequence
(7) Surface Condition/Surface Residual Stresses/Finish
- Finish
- Residual Stress Data

Correlative Information for Figure 9.3.4.16(a)

Product Form: Die forging, 2-inch thick

Thermal Mechanical Processing History:
Annealed at 1800 F, water quench

Properties:

TUS, ksi	TYS, ksi	E, ksi	Temp., F
155-160	135-140	29,000	250

Stress-Strain Equations:
Monotonic
Proportional Limit = 111 ksi
$\sigma = 289\ (\epsilon_p)^{0.138}$
Cyclic (Companion Specimens)
Proportional Limit = 92 ksi
$(\Delta\epsilon/2) = 156\ (\Delta\epsilon_p/2)^{0.046}$
Mean Stress Relaxation
$\sigma_m = 114.0\text{-}24562(\Delta\epsilon/2)$

Specimen Details:
Uniform gage test section
0.250-inch diameter
Polished with increasingly finer grits of emery paper to surface roughness of 10 RMS with polishing marks longitudinal.

Test Parameters:
Strain Rate/Frequency - 180 cpm
Wave Form - Sinusoidal
Temperature - 250 F
Atmosphere - Air

No. of Heats/Lots: 2

Equivalent Strain Equation:
$\log N_f = -6.56 - 4.20 \log (\epsilon_{eq} - 0.0022)$

$\epsilon_{eq} = (\Delta\epsilon)^{0.46}\ (S_{max}/E)^{0.54}$

Standard Deviation of log(Life): 0.123
Adjusted R^2 Statistic: 93%

Sample Size: 33

[Caution: The equivalent strain model may provide unrealistic life predictions for strain ratios and ranges beyond those represented above.]

References: 3.4.5.6.8(a)

FIGURE 9.3.4.16(b). *Example of correlative information and analysis results for a strain control fatigue data presentation.*

(8) Equivalent Strain Equation
- Life Equation with Parameter Estimates
- Standard Deviation of log(life)
- Adjusted R-squared Statistic
- Sample Size

(9) Reference Numbers

(10) No. of Heats/Lots.

The following cautionary note should be included with each equivalent strain equation: Caution: The equivalent strain model may provide unrealistic life predictions for strain ratios and ranges beyond those represented above.]

9.3.4.17 Example Problems.—

EXAMPLE 1. STRAIN CONTROL

A collection of iron alloy bar strain-controlled fatigue data at 70 F is given in Table 9.3.4.17.

The required steps for the analysis of the data set are presented below. The guideline sections relating to each step in the analysis are noted.

Data Requirements (See Section 9.3.4.4).—The data set includes three strain ratios (R_ε = -1.0, 0.0, 0.6) each consisting of at least eight nonrunout data points. This satisfies the minimum recommended sample size for analysis. Two runouts ($N_f = 10^5$ and 10^6_ at R_ε = -1 are included in the data set.

Data Collection (See Section 9.3.4.6)—The specimen design for the test program is reported as uniform-gage section with a diameter of 0.20 inches. Failure is defined as complete separation. The tensile properties are presented in the correlative information. No information is available regarding the fabrication sequence for the specimens. Fabrication information is important, although in this case it is not considered sufficient cause to reject the data set for analysis. The test data at the R_ε = -1.0 strain ratio provide information regarding this material's cyclic stress-strain response. The cyclic stress-strain curve constructed from the data is shown in Figure 9.3.4.17(a). The monotonic curve (dashed) is estimated from the reported yield and ultimate strengths.

Evaluation of Mean Stress and Strain Effects (See Section 9.3.4.9)—The data set consists of three strain ratios and therefore an equivalent-strain formulation is used to consolidate the data on the basis of equivalent strain. Equation 9.3.4.9(c),

$$\log N_f = A_1 + A_2 \log (\varepsilon_{eq} - A_4)$$

where

$$\varepsilon_{eq} = (\Delta\varepsilon)^{A_3} (S_{max}/E)^{1 - A_3} \quad ,$$

is the initial model attempted for fitting the data and proves to be adequate thoroughout the analysis.

Estimation of Fatigue Life Model Parameters - Least Squares (See Section 9.3.4.10)—The initial least-squares regression results in the following fatigue-life equation parameters:

$$A_1 = -4.62$$

TABLE 9.3.4.17. *Iron Alloy Strain-Controlled Fatigue Data at 70 F.*

Specimen Number	Δ_ε	S_{max} (ksi)	Cycles to Failure	Strain Ratio
1	0.600	71.1	10223	-1.00
2	0.600	77.8	10396	-1.00
3	0.600	79.2	8180	-1.00
4	0.970	117.2	605	-1.00
5	1.000	110.7	672	-1.00
6	1.000	112.8	642	-1.00
7	1.500	126.9	209	-1.00
8	1.500	127.1	340	-1.00
9	0.600	116.6	3958	0.0
10	0.600	124.2	3895	0.0
11	0.597	118.2	3919	0.0
12	0.600	128.3	4050	0.0
13	0.600	122.6	2470	0.0
14	0.400	106.4	16388	0.0
15	0.393	101.9	22896	0.0
16	0.400	102.1	15388	0.0
17	0.400	93.7	38648	0.0
18	0.400	101.2	11960	0.0
19	0.750	139.4	1099	0.60
20	0.750	137.3	1544	0.60
21	0.750	113.0	966	0.60
22	0.500	124.5	4665	0.60
23	0.500	140.6	4342	0.60
24	0.500	138.4	4240	0.60
25	0.400	158.0	7460	0.60
26	0.400	146.1	11134	0.60
27	0.400	119.1	10876	0.60
28	0.440	65.8	100000*	-1.00
29	0.330	50.0	1000000*	-1.00

*Did not fail.

$$A_2 = -3.28$$

$$A_3 = 0.610$$

$$A_4 = 0.00198.$$

A plot of the residuals for the fatigue model using these parameters is shown in Figure 9.3.4.17(b). These residuals do not exhibit the characteristic pattern of increasing residual magnitudes with decreasing equivalent strain levels shown in Figure 9.3.4.10(a). Rather, the variance appears to be relatively uniform. During Step 2 of the parameter estimation procedure, a negative, but insignificant, estimate of the

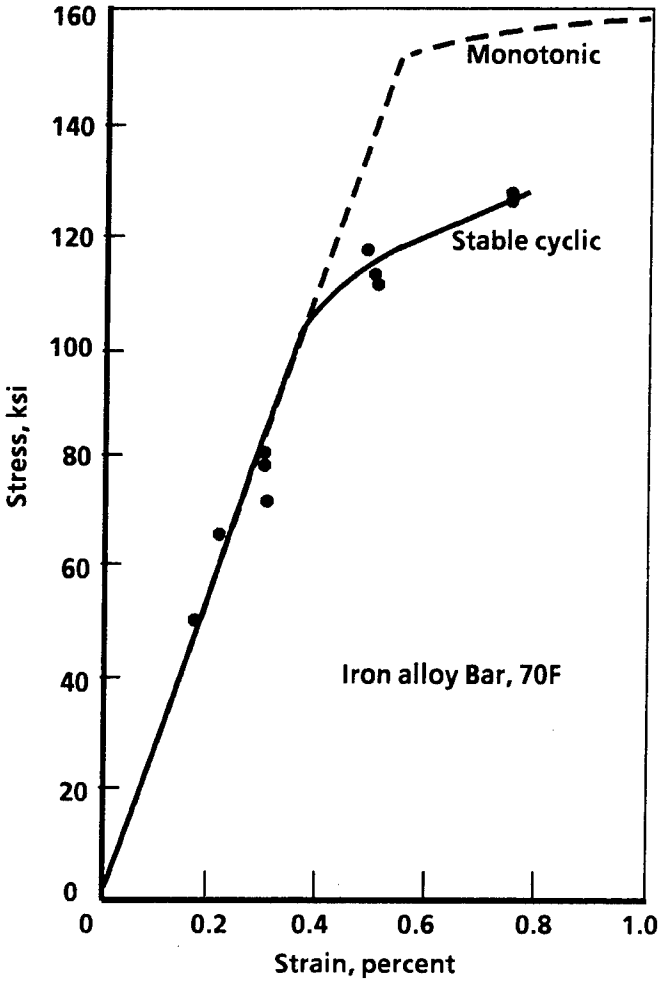


FIGURE 9.3.4.17(a). *Stable cyclic and monotonic stress-strain curves for iron alloy at 70 F.*

residual model slope, $\sigma 1$ was obtained. This result indicates the residuals are already uniformly distributed and a constant variance model can be used. The constant variance model, in effect, does not weight the fatigue life model, so the initial parameter estimates are retained.

Treatment of Outliers (See Section 9.3.4.11)—After the data have been checked for uniformity of variance, they can be screened to determine if any outliers are present. The critical studentized residual at the 5 percent significance level for this sample of 27 observations is found to be 3.53. Any of the observations with the absolute value of the studentized residuals being greater than 3.53 would be considered outliers. The largest studentized residual from the data was 2.09, therefore, none of the observations are identified as statistically significant outliers.

Assessment of the Fatigue Life Model (See Section 9.3.4.12)—The equivalent strain formulation is marginally acceptable at the 5 percent level. The lack of fit test for the fatigue-life model results in a Durbin-Watson D statistic of 1.042. The critical value of D for a sample size of 27 is 1.241 [Equation 9.3.4.12(b)].

Since the Durbin-Watson statistic is less than the critical value, the equivalent strain model must be considered questionable in terms of its compensation for effects of strain ratio. However, no other model

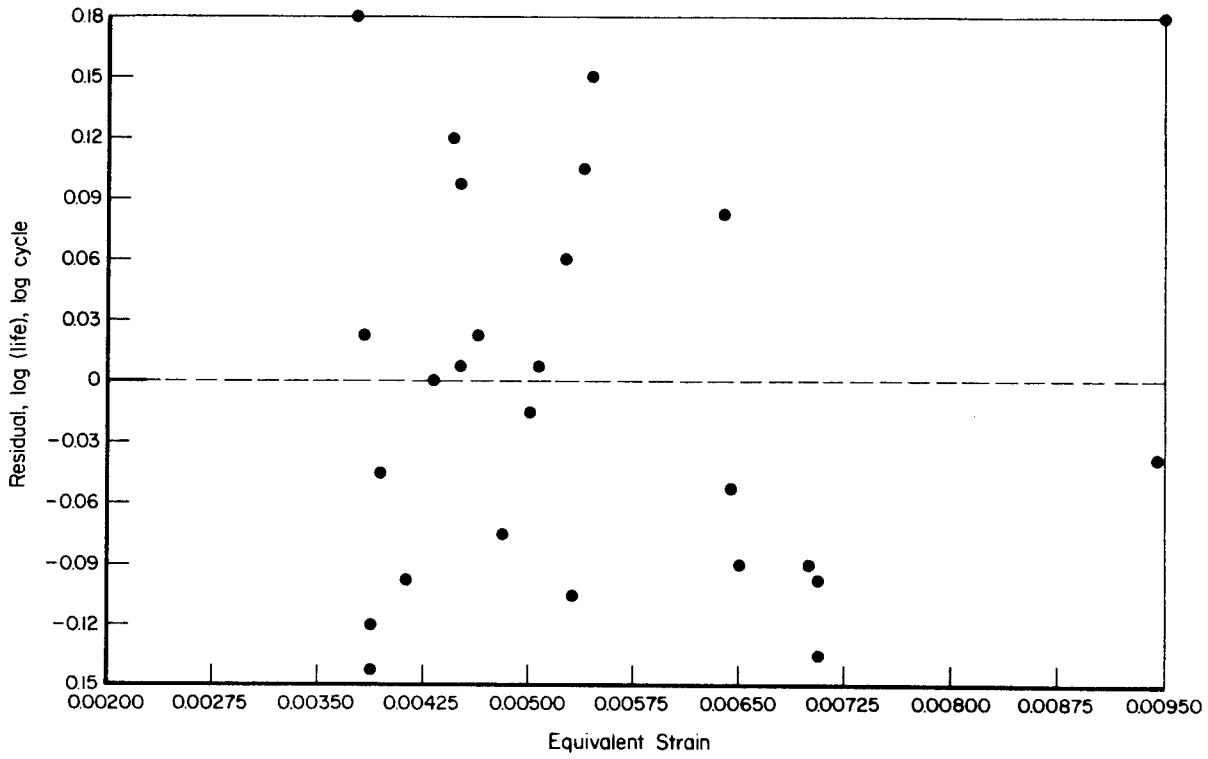


FIGURE 9.3.4.17(b). *Residual plot of fatigue-life model for initial parameter estimates.*

was found to perform better and a review of the plotted data revealed very low scatter compared to the predicted trends. Therefore, engineering judgement was used, and the proposed model was accepted.

Data Set Combination (See Section 9.3.4.13)—All of the data for this analysis came from a single source; therefore, this test is not applicable.

Treatment of Runouts (See Section 9.3.4.14)—The data set being considered includes two runout observations. The parameters A_1 and A_2 are therefore reestimated using the maximum likelihood regression to account for censored life values. The maximum likelihood estimates are:

$$A_1 = -5.07$$

$$A_2 = -3.47$$

$$A_3 = 0.610$$

$$A_4 = 0.00198.$$

The change in parameters A_1 and A_2 shift the predicted lives to greater values than the least squares parameter estimates.

Presentation of Fatigue Analysis Results (See Section 9.3.4.16)—The presentation of the strain-life curve and correlative information shown in Figure 9.3.4.17(c) is typical of a MIL-HDBK-5 strain-control fatigue data proposal. Regarding the mean stress relaxation plot, note that a single regression has been performed to represent both the $R_\varepsilon = 0.6$ and $R_\varepsilon = 0.0$ strain ratios. Although it would be expected that higher strain ratios would result in higher stabilized mean stresses, the limited amount of data precludes performing separate regressions for each strain ratio. It can be seen from the strain-life plot that using the single regression does represent the mean fatigue trends fairly well.

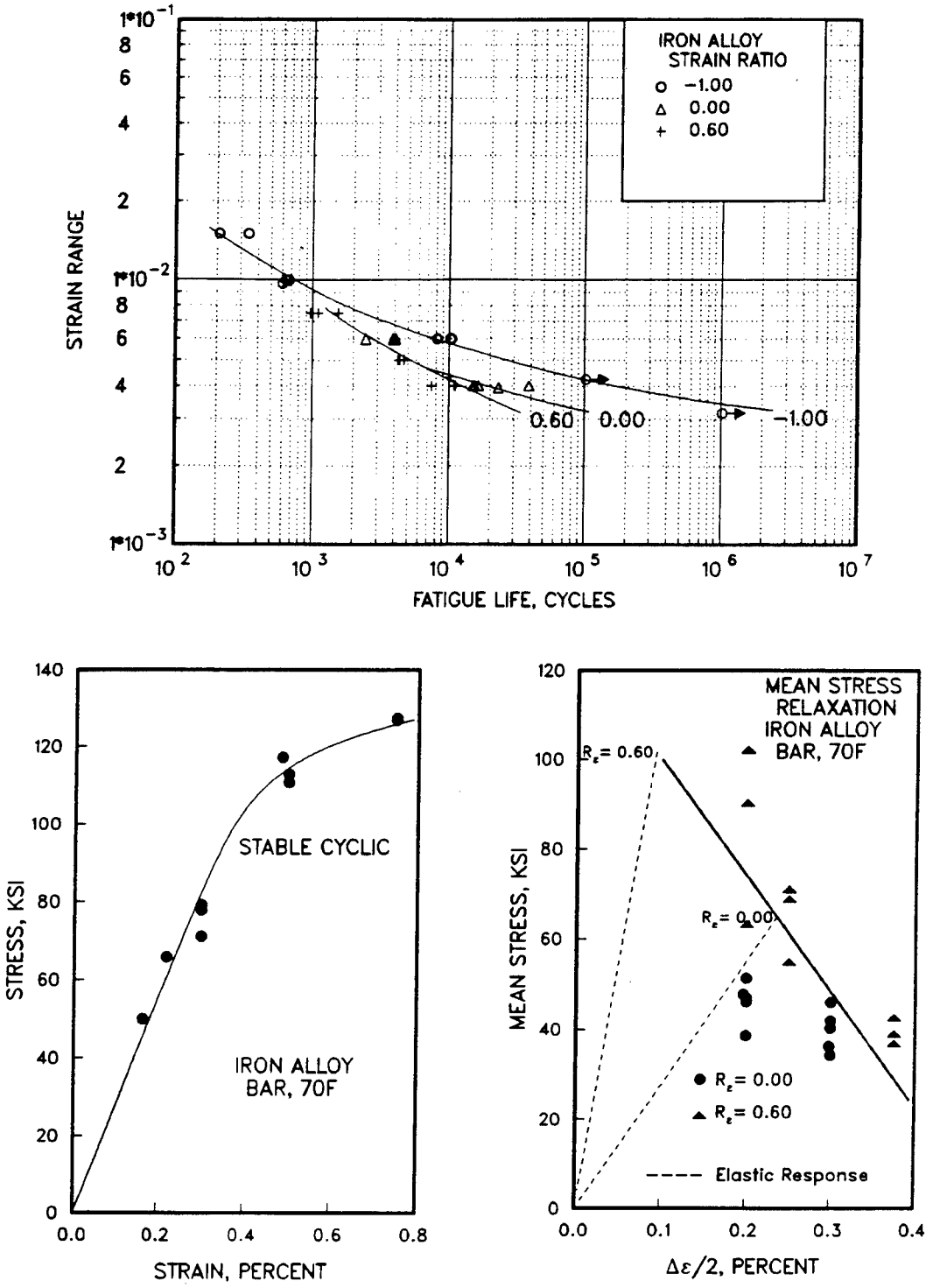


FIGURE 9.3.4.17(c). *ε/N curve and correlative information for iron alloy at 700 F.*

Correlative Information for Figure 9.3.4.17(c)

Product Form: Bar, 1 inch thick

Thermal Mechanical Processing History:
Not available

Properties:

TUS, ksi	TYS, ksi	E, ksi	Temp., F
175-180	150-155	27,500	70

Stress-Strain Equations:
Monotonic
Proportional Limit = 150 ksi
$\sigma = 280\ (\varepsilon_p)^{0.12}$
Cyclic (Companion Specimens)
Proportional Limit = 105 ksi (est.)
$(\Delta\sigma/2) = 196\ (\Delta\varepsilon_p/2)^{0.076}$
Mean Stress Relaxation
$\sigma_m = 125.4\text{-}25666(\Delta\varepsilon/2)$

Specimen Details:
Uniform gage test section
0.200-inch diameter

References: 3.4.5.6.8(a)

Test Parameters:
Strain Rate/Frequency - 180 cpm
Wave Form - Sinusoidal
Temperature - 70 F

No. of Heats/Lots: 4

Equivalent Strain Equation:
$\log N = -5.07 - 3.47 \log (\varepsilon_{eq} - 0.00198)$

$\varepsilon_{eq} = (\Delta\varepsilon)^{0.61}\ (S_{max}/E)^{0.39}$

Standard Deviation of log(Life): 0.111

Adjusted R^2 Statistic: 96%

Sample Size: 29

[Caution: The equivalent strain model may provide unrealistic life predictions for strain ratios and ranges beyond those represented above.]

FIGURE 9.3.4.17(c). *ε/N curve and correlative information for iron alloy at 700 F.—Continued*

EXAMPLE 2. LOAD CONTROL

A large collection of 300M alloy die forging fatigue data is presented in Figure 9.3.4.17(d). The required steps for the analysis of the data set are presented below.

Data Requirements (See Section 9.3.4.4)—The data set consists of four stress ratios (R = -1.0, -0.33, 0.05, 0.2). Each stress ratio includes at least twenty-three nonrunout observations, easily satisfying the minimum sample size requirement of six tests per stress ratio.

Data Collection (See Section 9.3.4.6).—The data shown in Figure 9.3.4.17(d) were compiled from four sources. Each source reports the results of fatigue testing programs conducted within two years of each other (1968-1970).

The failure criteria for all tests is reported as complete separation of the specimen. Those tests which did not fail are identified on the S/N plot with an arrow (→). These runout observations are treated differently in the regression analysis which define the mean fatigue curves (see Section 9.3.4.14).

Evaluation of Mean Stress and Strain Effects (See Section 9.3.4.9)—The collection of data consists of four stress ratios, and therefore, an equivalent-stress formation was used to consolidate the data. Equation 9.3.4.9(a),

$$\log N_f = A_1 + A_2 \log (S_{eq} - A_4)$$

where

$$S_{eq} = S_{max}(1 - R)^{A_3} \quad ,$$

is the initial model attempted for fitting the data, and it proved adequate throughout the analysis.

Estimation of Fatigue Life Model Parameters.—Least Squares (See Section 9.3.4.10).—The initial least-squares regression (runouts excluded) results in the following fatigue-life equation parameters:

$$A_1 = 23.7$$

$$A_2 = -8.41$$

$$A_3 = 0.366$$

$$A_4 = 0.0.$$

The fatigue-limit parameter (A_4) of zero seems somewhat inconsistent with the data shown in Figure 9.3.4.17(d). A visual examination of the S/N plot reveals a tendency for the data to asymptotically approach some limiting value. The zero fatigue limit term suggests that some problem may exist within the data collection. A plot of the residuals for the fatigue model using these parameters is shown in Figure 9.3.4.17(e).

The parameters obtained after the model is adjusted for nonconstant variance are:

$$A_1 = 23.4$$

$$A_2 = -8.38$$

$$A_3 = 0.40$$

$$A_4 = 13.5.$$

Note that a fatigue limit term of 13 ksi has now been estimated. However, a check on the significance of the A_4 term revealed that it was clearly insignificant. All of the runouts in the data collection were above this equivalent stress level and, therefore, all runouts were used in the regression procedure. A plot of the residuals after the fatigue life model has been adjusted is shown in Figure 9.3.4.17(f). Note the relative shift in the magnitude of the residuals at the higher and lower S_{eq} values compared to Figure 9.3.4.17(e).

Treatment of Outliers (See Section 9.3.4.11)—None of the observations were identified as outliers. The critical studentized residual at the 5 percent significance level for this data set of 114 observations is 3.63. The largest standardized residual was 3.23, resulting from a runout observation.

Assessment of the Fatigue Life Model (See Section 9.3.4.12).—The equivalent stress model is not able to consolidate the R = -0.33 stress ratio with the other stress ratios. The F-test performed on the residuals of the stress ratios proves significant at the 5 percent level for R = -0.33. This indicates that the mean of the residuals for R = -0.33 differs significantly from the mean of the residuals from the other ratios. The plot of stress ratios versus residuals, as shown in Figure 9.3.4.17(g) illustrates that the mean of the residuals for R = -0.33 is significantly different than those for the other stress ratios. A close examina

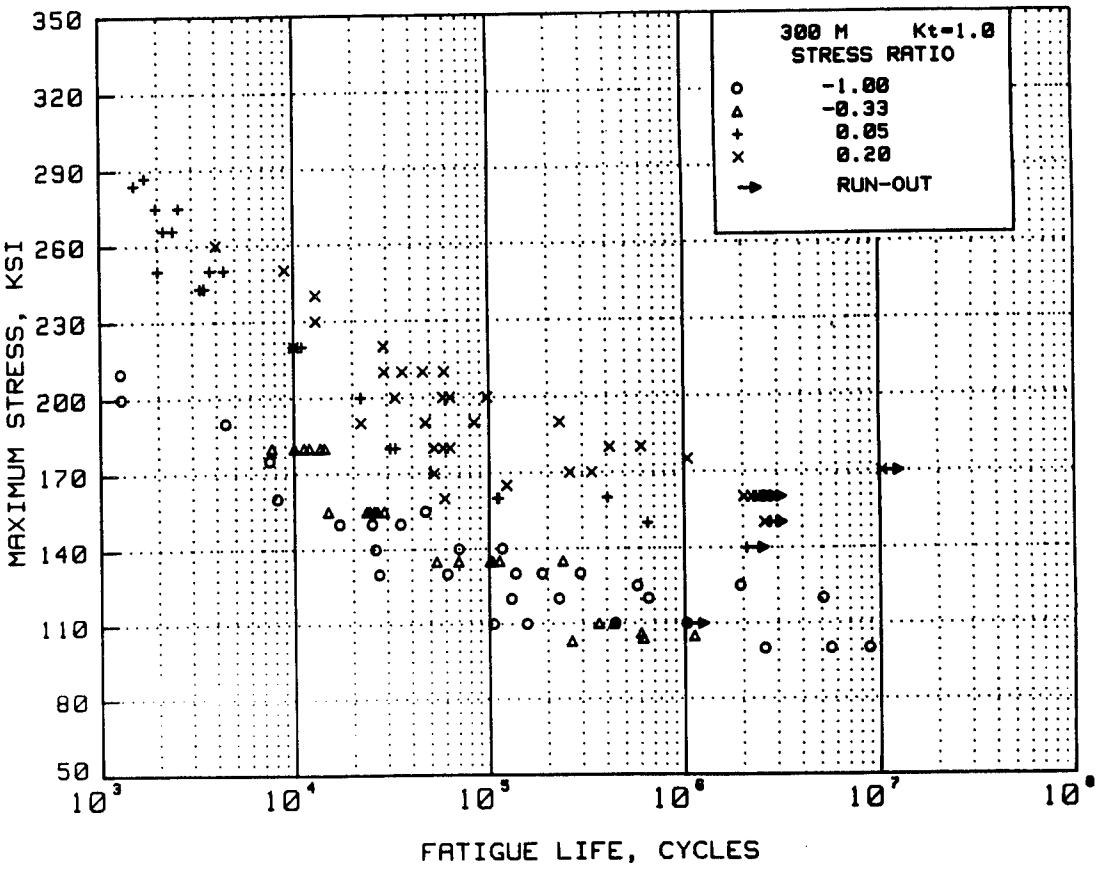


FIGURE 9.3.4.17(d). *S/N plot of unnotched 300M die forging fatigue data, transverse orientation.*

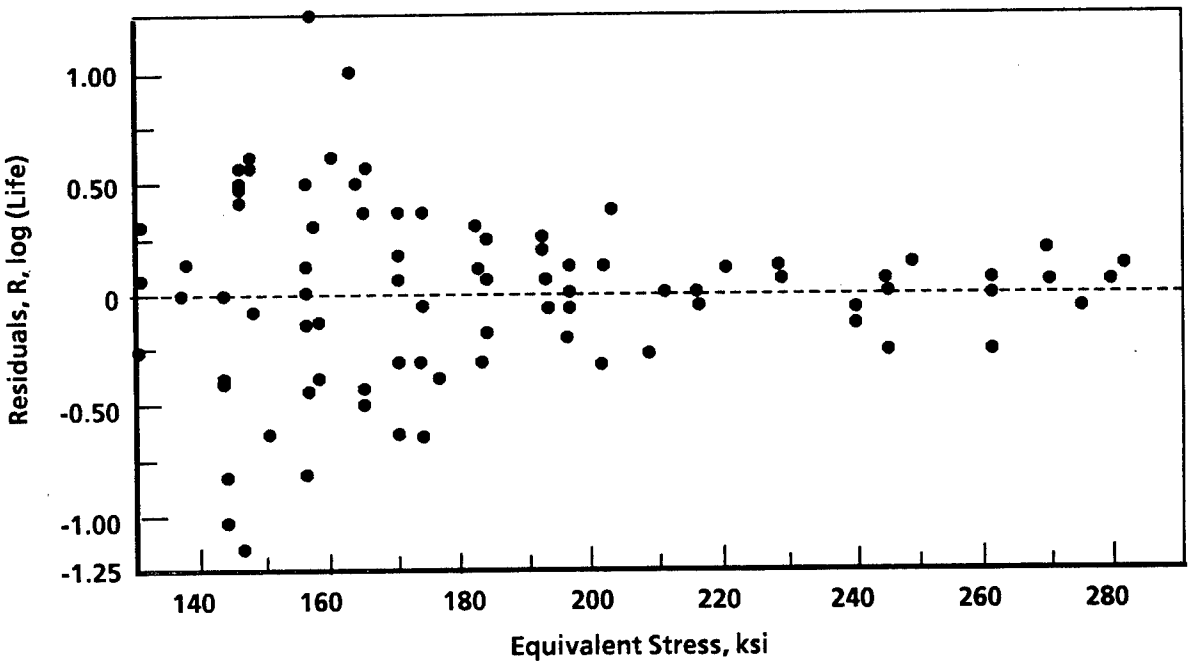


FIGURE 9.3.4.17(e). *Residual plot before model has been adjusted for nonconstant variance.*

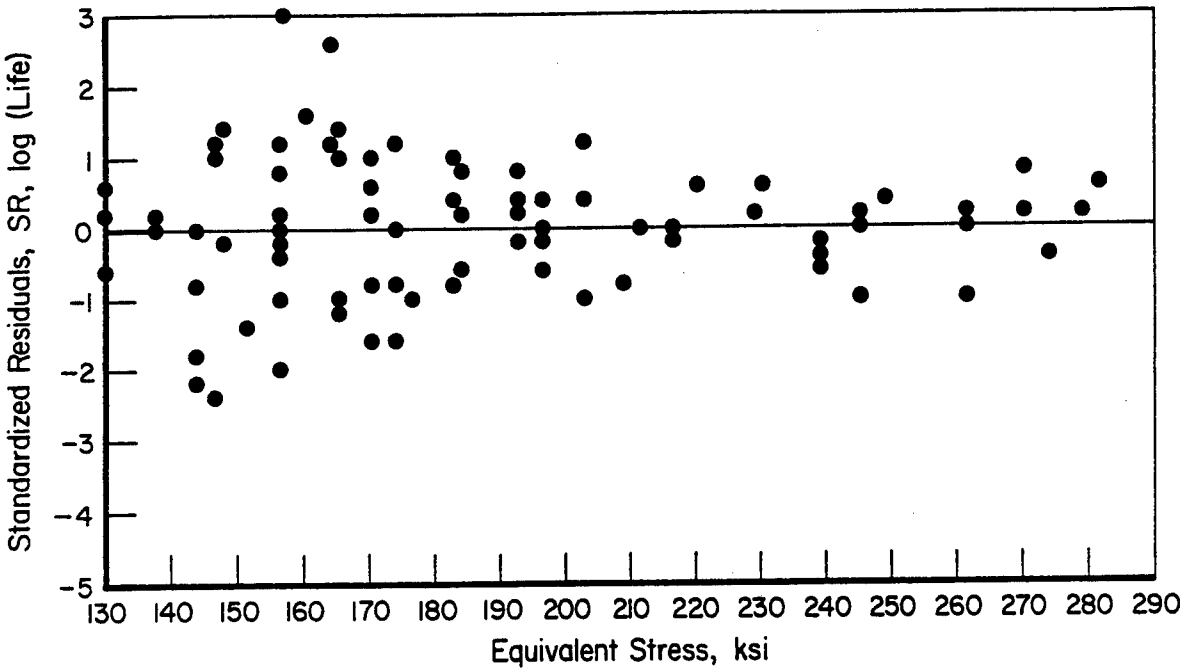


FIGURE 9.3.4.17(f). *Standardized residual plot after model has adjusted for nonconstant variance.*

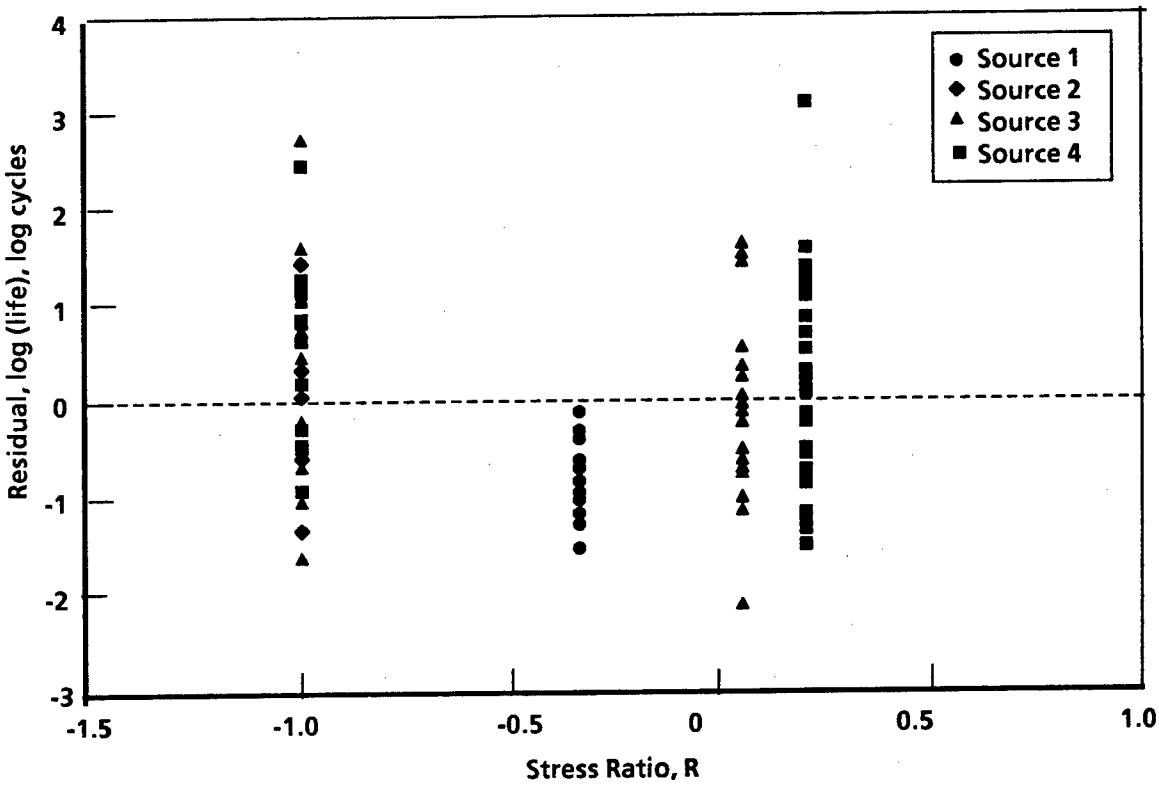


FIGURE 9.3.4.17(g). *Residual plot of stress ratios. Note the low mean value of R = -0.33.*

tion of the original S/N plot shown in Figure 9.3.4.17(d) reveals that the R = -0.33 data tend to overlap the R = -1.0 data: at the lower maximum stress levels (about 100 ksi), the R = -1.00 data actually show longer average fatigue lives than do the R = -0.33 data, when the reverse would be expected. The Durbin-Watson D statistic for determining lack of fit is 1.61, indicating a poor fit of the model to the data. The critical value of D for a sample of 114 observations [Equation 9.4.3.12(b)] is 1.66.

This incompatibility among stress ratios indicates that either a problem exists with the data or with the assumed equivalent stress model. The data sources were re-examined to possibly determine if some difference in specimen preparation or testing procedure among the sources may have caused the inconsistencies. Unfortunately, no significant differences were discovered that would provide sufficient reason to exclude the suspect R = -0.33 data due to testing methods alone. The problem is confounded because all of the R = -0.33 data comes from a single source which does not include other stress ratios. This precludes examining source to source variability.

In situations such as this where a data set for a single source is determined to statistically deviate from the fatigue trends exhibited by the bulk of the data, it should be evaluated for exclusion. Engineering judgement suggests that the R = -0.33 data be excluded from the data collection based on the following:

(1) unrealistic fatigue limit

(2) lack of fit for fatigue life model based upon Durbin-Watson statistic

(3) stress ratio incompatibility.

The modified data collection is now reanalyzed. For the sake of brevity, the details of the analysis procedure for Sections 9.3.4.4 (Data Requirements) through 9.3.4.11 (Treatment of Runouts) will be omitted. It is interesting to note, however, that the fatigue limit term (A_4) resulting from the least squares regression with the R = -0.33 data excluded is 94.2 ksi. This result more realistically represents the longer life fatigue trends compared to the previous (insignificant) estimate of 13.5 ksi. With the suspect data removed, the equivalent stress model is determined to be acceptable at the 5 percent level. The Durbin-Watson D statistic also is increased to 2.18 indicating that the model now provides an adequate fit to the data.

Dataset Combination (See Section 9.3.4.13)—With the exclusion of the source containing the R = -0.33 data, the remaining data set combination is determined acceptable at the 5 percent level.

Treatment of Runouts (See Section 9.3.4.14)—The data collection includes seven runout observations. The maximum likelihood procedure has the effect of essentially shifting these runouts to the fatigue lives at which they most likely would have failed. The resulting fatigue life model parameters should reflect the slight increase in estimated fatigue life over the least squares parameters, particularly in the long life region. In general, the maximum likelihood regression will result in a higher intercept term (A_1) and a steeper (more negative) slope (A_2). The A_3 and A_4 terms are taken as constants to reduce the problem to a linear analysis.

The parameters resulting from the least squares regression are:

$$A_1 = 14.54$$

$$A_2 = -5.04$$

$$A_3 = 0.385$$

$$A_4 = 94.2.$$

The maximum likelihood parameters conform to the expected trends for A_1 and A_2:

$$A_1 = 14.79$$

$$A_2 = -5.16$$

$$A_3 = 0.385$$

$$A_4 = 94.2.$$

Note the increase in A_1 and the decrease (more negative slope) in A_2.

Presentation of Fatigue Analysis Results (See Section 9.3.4.16)—The stress-life curve and correlative information shown in Figure 9.3.4.17(h) is typical of a MIL-HDBK-5 load-control fatigue data proposal.

9.3.5 FATIGUE-CRACK-PROPAGATION DATA

9.3.5.1 *General*—Fatigue-crack-propagation data, recorded in the form of crack-length measurements and cycle counts (a_i, N_i) can be presented as crack-growth curve drawn through the data points as shown in Figure 9.3.5.1(a).

Although data presented in this form indicate general trends, they are not generally useful for design purposes since a variety of stress levels, stress ratios, initial crack conditions, and environmental conditions are encountered.

It has been found convenient to model fatigue-crack-propagation damage behavior as rate process and formulate a dependent variable based on the slope of this growth curve, or an approximation to it, namely,

$$\frac{da}{dN} \simeq \frac{\Delta A}{\Delta N} \qquad [9.3.5.1(a)]$$

Results obtained from the theory of linear elastic fracture mechanics have suggested that rate process at the crack tip might be represented as a function of a stress-intensity factor, K, which, in general form, may be written as

$$K = S\sqrt{a}\ g(a,w) \quad , \qquad [9.3.5.1(b)]$$

where g(a,w) is a geometric scaling function dependent on crack and specimen geometry, and S is nominal stress. As a result, the independent variable is usually considered as some function of K. At present, in MIL-HDBK-5 the independent variable is considered to be simply the range of the stress intensity factor, ΔK, and data are considered to be parametric on the stress ratio, R, such that Equation 1.4.13.3(b) becomes

$$da/dN \approx \Delta a/\Delta N = g(\Delta K,R) \quad , \qquad [9.3.5.1(c)]$$

where $\Delta K = K_{max} - K_{min}$. Values of maximum and minimum stress intensity factors, K_{max} and K_{min}, respectively, are computed with Equation 9.3.5.1(b) using respective maximum and minimum cyclic stresses.

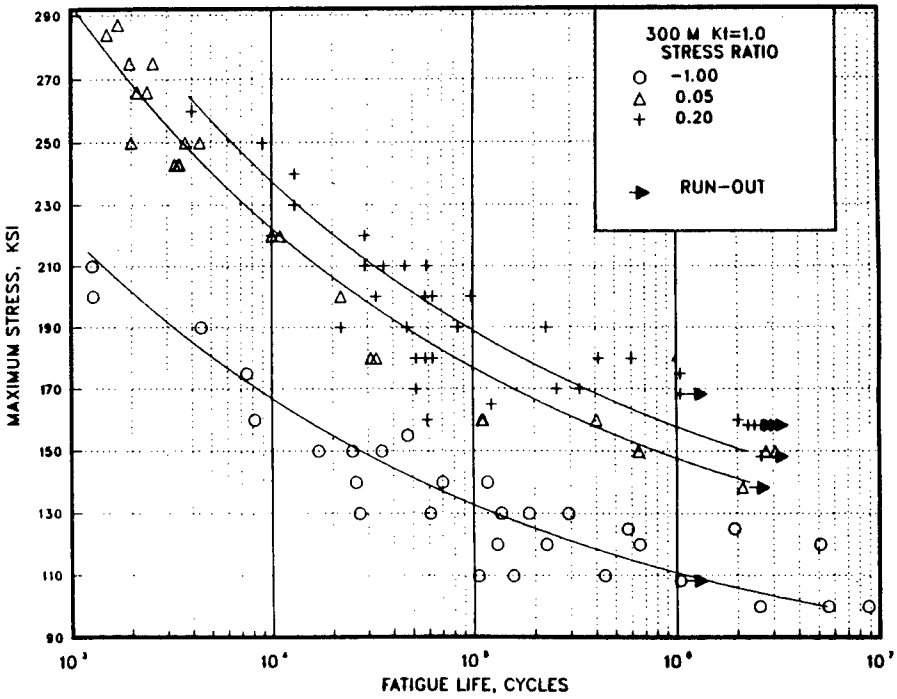


FIGURE X.X.X.X.X. *Best fit S/N curves for unnotched 300M alloy forging F_{tu} = 280 ksi, transverse orientation.*

Correlative Information for Figure X.X.X.X.X.

Product Forms: Forged billet, uncertain size
Die forging, 6-1/2 x 20 inches
6-inch RCS billet
1-1/4 x 8-inch forged bar
all CEVM

Properties:

TUS, ksi	TYS, ksi	Temp., F
272-294	226-243	RT

Specimen Details: Unnotched

0.200-0.250-inch diameter

Surface Condition: Heat treat and finish grind to a finish of 63 RMS or better with light grinding parallel to specimen length, stress relieve.

References: 2.3.1.2.8(c), (d), (e)

Test Parameters:

Loading - Axial
Frequency - 1800-2000 cpm
Temperature - RT
Environment - Air

No. of Heats/Lots: 5

Equivalent Stress Equation:

$\text{Log } N_f = 14.8 - 5.2 \log (S_{eq} - 94.2)$

$S_{eq} = S_{max}(1-R)^{0.38}$

Standard Deviation of log(Life) = 65.8 $1/(S_{eq})$

Adjusted R^2 Statistic = 87%

Sample Size = 90

(Caution: The equivalent stress model may provide unrealistic life predictions for stress ratios and maximum stress beyond those represented above.)

FIGURE 9.3.4.17(h). *Example S/N curve and correlative information.*

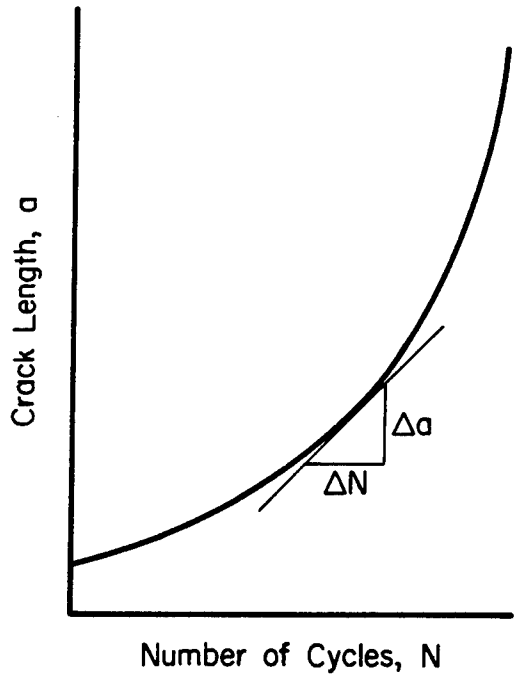


FIGURE 9.3.5.1(a). *Crack-growth curve.*

A crack growth rate curve, as shown in Figure 9.3.5.1(b), is obtained by plotting the locus of points (da/dN, ΔK) derived from the crack-growth curve [see Figure 9.3.5.1(a)] at selected values of crack length, a. Crack-growth-rate curves are generally plotted on log-log coordinates.

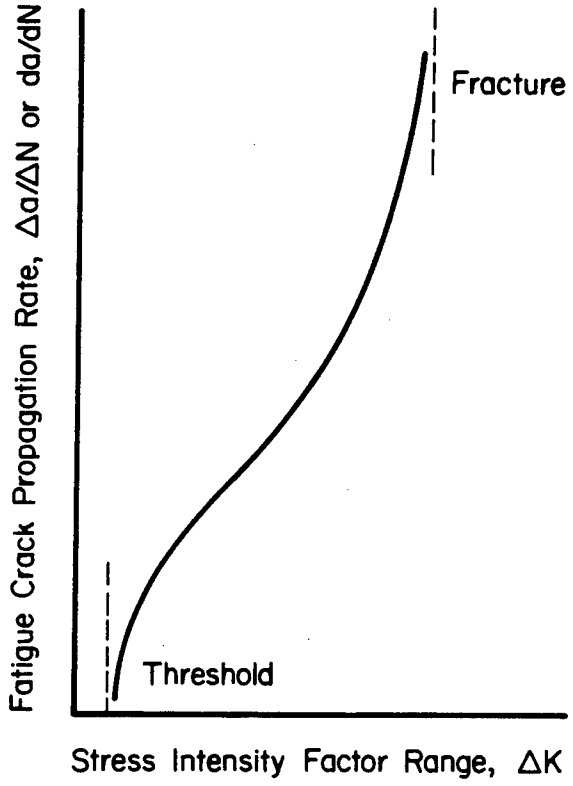


FIGURE 9.3.5.1(b). *Crack-growth-rate curve.*

Within the general curve shape described above, systematic variations in data point locations are observed. When data from tests conducted at several different stress ratios are present, the plot of crack-growth rate versus stress-intensity-factor range will be layered into distinct bands. Layering of data points may also occur as a result of variation in such parameters as test frequency, environment, temperature, and specimen grain direction.

9.3.5.2 *Data Generation and Interpretation*—Fatigue-crack-propagation data may be generated by several types of fracture mechanics test specimens. The principal criteria for acceptance of data are twofold. One is that a valid stress-intensity-factor formulation be available for the specimen; the other is that nominal net-section stresses, as calculated by concepts of elementary strength of materials, be less than eighty percent (80%) of the tensile yield strength of the material.

Basic data are generated as crack lengths, a, and associated cycle counts, N. These data are interpreted as crack-growth rates determined as slopes, or average slopes, of sequential subsets of data. For MIL-HDBK-5, da/dN is calculated as the weighted average incremental slope approximation.

$$\left(\frac{da}{dn}\right) \approx \left(\frac{\Delta a}{\Delta N}\right) i-1 + \frac{N_i - N_{i-1}}{(N_{i+1} - N_{i-1})} \left[\left(\frac{\Delta A}{\Delta N}\right) i - \left(\frac{\Delta A}{\Delta N}\right) i-1\right] \quad i=2,\ldots,n-1 \qquad [(9.3.5.2)]$$

from the measured crack-growth data as illustrated in Figure 9.3.5.2. However, alternative methods, such as polynomial fitting of the a versus N curve, are acceptable for computation of da/dN values. By this indexing and calculating procedure "n" measurements provide "n-2" slope or rate values at all but first and last measurement points. The directly associated stress-intensity factor for each slope computation is computed in accordance with Expression 9.3.5.1(b).

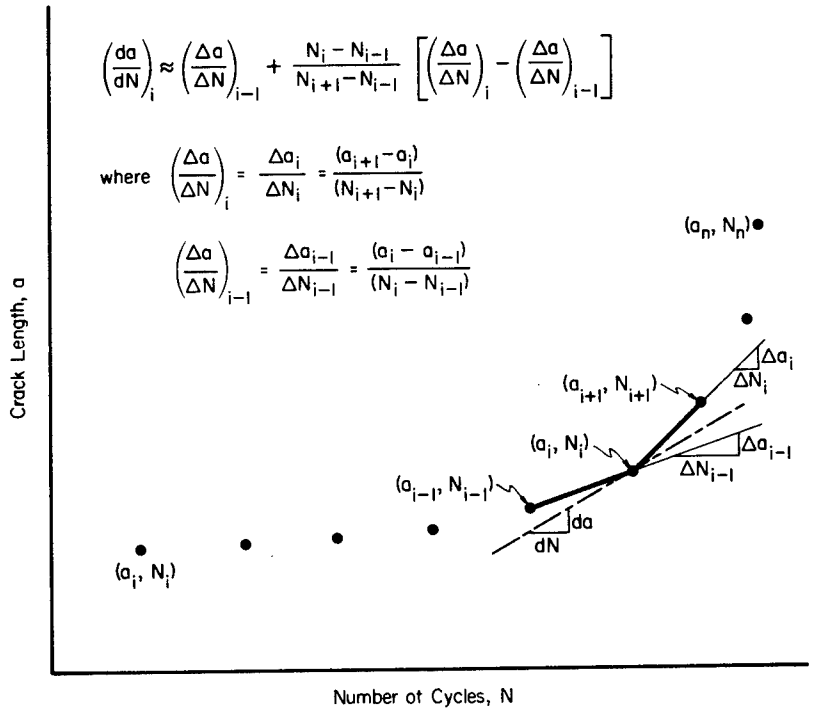


FIGURE 9.3.5.2. *Analytical definition of crack-growth rate calculation.*

9.3.5.3 *Data Requirements*—In order to establish a positive trend in rate behavior, it is recommended that rate data be generated over a range of at least two orders of magnitude. In general, this will be associated with a domain of stress-intensity-factor range from one half to a full order of magnitude. Good experimental techniques coupled with this data-range criterion should provide a concise and consistent data display for linear or other analysis.

When planning experimental programs to achieve the best, most complete derivation of fatigue-crack-propagation data, the range of ΔK over which tests are conducted should include those which will provide crack-growth rates as low as 10^{-8} inches/cycle. Furthermore, if possible, multiple heats of material should be included. Ideally, to properly document the effects of stress ratio, FCP data should also be generated over a range of R ratios (0.1, 0.4, and 0.7 are typically good values). If data representing negative R ratios are available, they should also be included.

9.3.5.4 *Reporting*—Reporting of basic crack-growth data shall be as complete as possible. In addition to reporting cyclic loading conditions, such as maximum cyclic load and/or stress levels, stress ratio, test frequency, and specimen dimensions, it is particularly important to identify environmental conditions associated with the tests. The number of specimens and number of respective heats should also be identified. Table 9.3.5.4 serves as an example of the type of information which should be available (or at least is desirable) for each collection of FCP data.

9.3.5.5 *Preparation of FCP Data Proposals*—When preparing FCP data proposals for submittal to MIL-HDBK-5 Coordination Group, several steps must be taken. First, various factors potentially influencing crack-propagation rates should be documented in a FCP Data Proposal as shown in Table 9.3.5.4. Second, data for individual test conditions should be plotted and compared so that a determination can be made as to whether combinations of test conditions are appropriate. If data are available for a range of specimen thicknesses, it may be desirable to treat such data in separate plots, if FCP rate behavior is influenced by thickness. Similarly, potential effects of environment, buckling restraints, specimen width, specimen type, crack orientation, temperature, and frequency should be evaluated; and, where visible differences in FCP rate trends exist, separate plots must be developed. In some cases, it may be necessary (or helpful) to include working figures of trial combinations of FCP data so that reviewers of the data proposal can more easily see reasons for particular data combinations. If a collection of FCP data (involving one or more figures) is approved, working curves and background data sheet will be retained in MIL-HDBK-5 files and only the final data plot will be incorporated in the Handbook.

9.3.5.6 *Data Presentations*—Fatigue crack-propagation data are presented in the Handbook on double logarithmic graphical displays of crack-growth rate, da/dN, μ-in./cycle, versus stress-intensity factor range, ΔK. Data points are presented along with a visually best-fit line judged to be most representative of the median behavior of those data. A sample display is presented in Figure 9.3.5.6.

Since data are not necessarily generated at predesignated stress ratio levels, stress ratio increments which are used on a given display are selected to present the most complete portrayal of available data. Data are summarized in graphical displays in the appropriate chapters of MIL-HDBK-5.

9.3.6 CREEP AND CREEP-RUPTURE DATA

9.3.6.1 *Introduction*—Creep is defined as time-dependent deformation of a material under an applied load. It is usually regarded as an elevated temperature phenomenon, although some materials creep at room temperature. If permitted to continue indefinitely, creep terminates in rupture. (First stage or logarithmic creep exhibited by many materials at lower temperatures is not the subject of this section.) Creep in service usually occurs under varying conditions of temperature and complex (multiaxial) stress, leading to an infinite number of stress-temperature-time combinations. Creep data for use in general design are usually obtained under conditions of constant uniform temperature and uniaxial stress. This

Table 9.3.5.4. *Sample Listing of Fatigue-Crack-Propagation Background Data*

Materials:	Ti-6Al-4V Titanium
Alloy Designation or Specification:	MIL-T-9046, Type III, Composition C
Product Form:	Plate
Heat Treatment:	Mill Annealed
Heat Number(s):	Ingot 295338

Chemistry (% by weight):

C	0.02
N	0.010
Fe	0.18
Al	6.4
V	4.2
0	0.127
H	81 (PPM)

Data Source(s): Feddersen, C. E., and Hyler, W. S., "Fracture and Fatigue-Crack Propagation Characteristics of 1/4 Inch Mill Annealed Ti-6Al-4V Titanium Alloy Plate", Report No. G9706, Battelle (1971).

Specimen Description

Type:	Center Cracked Panel
Thickness:	0.250 inch
Width:	9, 16, 32 inches
Crack Orientation:	L-T
Location w-r-t Product Thickness:	Through-thickness specimen
Surface Finish:	Not Indicated

Test Conditions:

No. of Specimens:	9	7	6
Maximum Stress or Load:	5, 10, 30 ksi	5, 10, 30, 50 ksi	10, 30, 50 ksi
Stress Ratio:	0.10	0.40	0.70
Cyclic Frequency:	1-25 Hz		
Environment:	50% relative humidity		
Temperature:	68 ± 2 F		
Buckling Restraints?:	Yes		
Crack Monitoring Technique:	Optical		

Additional Comments:

1. Frequency was varied from 1 to 25 Hz according to the magnitude of stress range, no frequency effects were noted in this environment.

2. From 20 to 70 crack readings were made on each specimen.

3. No panel width effects on FCP rates were evident.

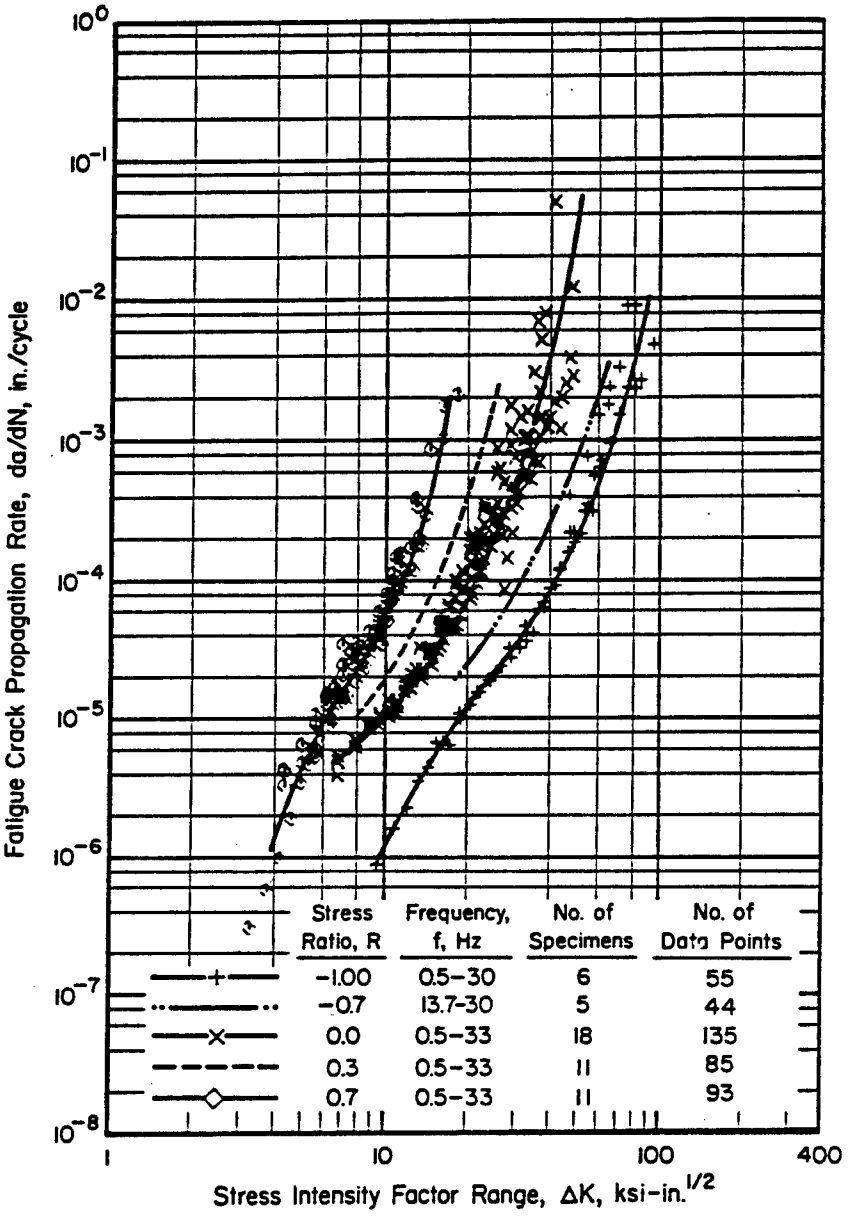


FIGURE X.X.X.X.X. *Typical-crack-propagation data for 0.090 inch thick, 7075-T6 aluminum alloy sheet with buckling restraint. [References 3.7.4.1.9(a) through (e)].*

Specimen Thickness: 0.090 inch
Specimen Width: 1½-12 inches
Specimen Type: CC
Environment: Lab Air
Temperature: RT
Orientation: L-T

FIGURE 9.3.5.6. *Sample display of fatigue-crack-propagation-rate data.*

type of data is the subject of this section.

9.3.6.2 *Terminology*—The definitions presented below will be helpful in preparing creep-rupture data for inclusion in MIL-HDBK-5.

Creep—The time-dependent deformation of a solid resulting from force.

Note 1—Creep tests are usually made at constant load and temperature. For tests on metals, initial loading strain, however defined, is not included.

Note 2—This change in strain is sometimes referred to as creep strain.

Primary Creep—Creep occurring at a diminishing rate, sometimes called initial stage of creep.

Secondary Creep—Creep occurring at a constant rate, sometimes called second stage creep.

Tertiary Creep—Creep occurring at an accelerating rate, sometimes called third stage creep.

Creep Test—A creep test has the objective of measuring deformation and deformation rates at stresses usually well below those which would result in fracture during the time of testing.

Creep-Rupture Test—A creep-rupture test is one in which progressive specimen deformation and time for rupture are measured. In general, deformation is much larger than that developed during a creep test.

Stress-Rupture Test—A stress-rupture test is one in which time for rupture is measured, no deformation measurement being made during the test.

Total Strain—Total strain at any given time, including initial loading strain (which may include plastic strain in addition to elastic strain) and creep strain, but not including thermal expansion.

Loading Strain—Loading strain is the change in strain during the time interval from the start of loading to the instant of full-load application, sometimes called initial strain.

Plastic Strain During Loading—Plastic strain during loading is the portion of the strain during loading determined as the offset from the linear portion to the end of a stress-strain curve made during load application.

Creep-Strain—The time-dependent part of the strain resulting from stress, excluding initial loading strain and thermal expansion.

Total Plastic Strain—Total plastic strain at a specified time is equal to the sum of plastic strain during loading plus creep.

Creep Stress—The constant load divided by the original cross-sectional area of the specimen.

Elapsed Time—The time interval from application of the creep stress to a specified observation.

Creep-Rupture Strength—Stress that will cause fracture in a creep test at a given time, in a specified constant environment. Note: This is sometimes referred to as the stress-rupture strength.

Creep Strength—Stress that causes a given creep in a creep test at a given time in a specified constant environment.

Rate of Creep—The slope of the creep-time curve at a given time determined from a Cartesian plot.

Creep-Rupture Curve—Results of material tests under constant load and temperature; usually plotted as strain versus time to rupture. A typical plot of creep-rupture data is shown in Figure 9.3.6.2. The strain indicated in this curve includes both initial deformation due to loading and plastic strain due to creep.

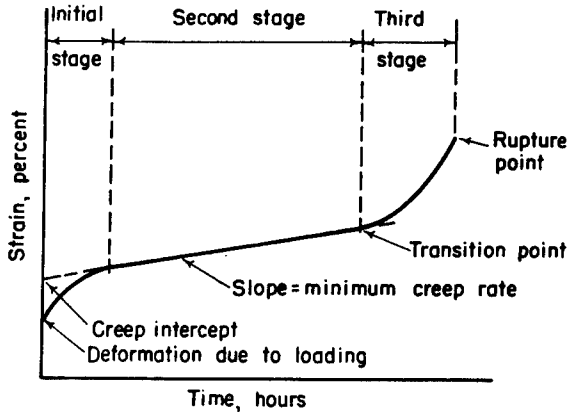


FIGURE 9.3.6.2. *Typical creep-rupture curve.*

Master Creep Equation—An equation expressing combinations of stress, temperature, time and creep, or a set of equations expressing combinations of stress, temperature and time for given levels of creep.

Master Rupture Equation—An equation expressing combinations of stress, temperature, and time that cause complete separation (fracture or rupture) of the specimen.

Isothermal Lines—Lines of uniform temperature on a creep or stress-rupture curve.

Isostrain Lines—Lines representing constant levels of creep.

9.3.6.3 *Data Generation*—The following paragraphs provide guidelines on testing methods and designing an experimental matrix for developing creep and creep-rupture data.

Test Methods—Test methods must conform to ASTM E-139. However, it is recognized that this standard allows considerable latitude in procedures such that both level and scatter results can be significantly affected.

In case of significant difference in results from different testing sources, the following should be evaluated:

Material Condition (see Section 9.3.6.4)

Specimen Dimensions and Configuration (geometry effect)

Specimen Surface Preparation (residual stresses)

Specimen Alignment (concentricity, fixturing, load train, and loading method)

Temperature Control (number, type, and location of sensors, reference junction temperature control, monitoring and recording)

Extensometers (type, fixturing, and recording)

Strain Recording (records inelastic strain on loading and creates a record to be evaluated for test stability)

Documentation (testing procedures)

General Laboratory Conditions, Personnel Qualifications, Calibration Intervals.

The submittor of a proposal should be prepared to provide documentation sufficient to permit a comparative evaluation of data. Inability to do so may cause rejection of some associated data, or the entire proposal.

Design of Experiments—A design of experiments approach to creep data development is highly recommended because it provides the maximum amount of useful data for the least expenditure of time and testing funds. If such an approach is not used, it is likely that several times as many test data will not serve as well in developing desired mathematical models of creep behavior as data developed through design of experiments. This section is devoted to a description of design of experiments approach which can be used to develop regression models to mathematically portray creep rupture life and creep as a function of temperature and stress.

One method for planning testing is to develop a test layout in matrix form, with temperatures in rows and expected creep lives in columns. Then, through testing, simply fill out blocks within the matrix. There should be a minimum of eight observations per isothermal line, or twenty observations per Larson-Miller or other regression model. This insures coverage of all conditions of interest. Further explanation of this method, by way of an example, is provided in Section 9.3.6.8.

Choosing the Number of Temperatures and Life Intervals—Before the test matrix can be formed, interval sizes must be considered, first for temperature and then life.

(a) Temperature—A range of temperatures is usually required. For example, if experiments must range from 1000 F through 1500 F, a choice must be made whether to perform tests at six levels (1000 F, 1100 F, 1200 F, 1300 F, 1400 F, 1500 F), or maybe at three levels (1000 F, 1300 F, 1500 F). The decision can be quite complicated and based on such phenomena as:

(1) The relative closeness of the isothermal lines

(2) Parallel or divergent isothermal lines

(3) The precipitation of secondary phases within the life ranges of interest.

However, this selection can be greatly simplified with very little user risk. Start with the lowest temperature, and then choose the next temperature line such that at least one level of testing stress, on log stress-log life plot, will be common to both temperatures. Then, proceed to the next temperature line, etc., ensuring like stress values on adjacent temperature levels.

(b) Life—Divide a log-life cycle into four equidistant segments. For example, between 100 hours and 1000 hours, the divisions would be approximately 180 hours, 320 hours, and 560 hours on the log-life scale. These divisions are far enough apart to insure a well-defined curve and a minimum overlap of data. To convert from temperature and life desired to temperature and test stress requires that there be some prior knowledge of this relationship. If there is no prior knowledge, a series of "probe" tests must be made to locate the isothermal lines on a log-log plot.

Choosing the Number of Heats—Batch variations in chemistry, heat treating, etc., can cause considerable variations in the mechanical properties of an alloy. This difference is referred to as heat-to-heat

components, as opposed to within-heat components of variance.* Heat-to-heat standard deviation is usually 50 to 70 percent of within-heat standard deviation. The root sum square of the two components of variance produces a measure of scatter about the regression that, when added to curve fitting error, gives the regression parameter called SEE (Standard Error of Estimate). SEE is a product of regression analysis; it is rarely determined as defined above. It is this parameter which fixes design minimums about the regression estimates of the typical or mean values.

To make a mathematically sound decision on the minimum number of heats that should be used in a given analysis, it is necessary that an estimate of heat-to-heat and within-heat variance be known. This can usually be estimated from like alloys, or calculated from development data. Simulation has shown the following minimum number of heats to be satisfactory:

(1) When the heat-to-heat component of variance is less than 25 percent of within-heat variance, use two heats equally.

(2) When the heat-to-heat component of variance is between 25-65 percent of within-heat variance, use three heats equally.

(3) When the heat-to-heat component of variance is greater than 65 percent of within-heat variance, use five heats equally.

Heats should be distributed randomly and essentially equally throughout the test matrix to insure an unbiased heat distribution.

When regression models are developed from data that were not taken from an experimental model, heats are rarely chosen randomly. Therefore, unless there are large samples of data in all areas of the regression matrix, this imbalance of heat sample sizes must be accounted for as described in Section 9.3.6.5. Order of testing must also be randomized so that any time-, operator-, or machine-oriented effects are randomly distributed within the test matrix as described in Reference 9.3.6.3.

9.3.6.4 *Data Collection and Interpretation*—After a desired group of creep and/or creep-rupture data have been experimentally developed or isolated in preproduction files, it is necessary to carefully collect and interpret these data in accordance with the following guidelines:

Data collection—For isostrain creep, collected data will include stress, temperature, modulus and plastic strain on initial loading, and strain-time pairs sufficient to define a curve. While strain-time pairs will be only those for the isostrain of interest, after inelastic strain on loading has been included in the reported strain, it may be that reported data may not correspond to isostrain levels. Consequently, isostrain-time pairs may be read from a smooth curve drawn through the values recorded during the test.

For rupture, collected data will include stress, temperature, time-to-rupture, percent elongation, and reduction of area. Percent elongation and reduction of area can then be used to define rupture ductility curves or equations.

Data Interpretation—State-of-the-art for interpreting these types of creep and rupture data requires that a certain amount of judgment be allowed. The general approach will be to optimize one of several empirical equations that best follows the trend of data, using life (or time) as the dependent variable. Independent variables will include stress and temperature for rupture and isostrain creep curves, and will also include strain for isostrain creep curves.

Rupture ductility can be an exception to the above because of complex behavior and data scatter. At least a cautionary note should be given in the introductory material on times and temperatures included in

*The within heat variance is the pooled variability of data from all heats, where the variability for each heat is calculated about its own average regression line. The heat-to-heat variance is calculated from the variability of each heat's average regression line about the overall average regression line of all heats. All heat average curves are assumed to be parallel in log life.

rupture data. Some materials exhibit such low elongation in certain time-temperature regions that normal, reasonable values of design creep strain cannot be achieved without risk of fracture.

Interpretation of creep and rupture data should also include variables that are reflected in background data reporting requirements (discussed in the next subsection). Depending on the information content of the data, and the type of variable, it may be desirable to develop a series of equations, or to include additional physical variables in the regression analysis. The proposal should demonstrate that these additional variables have been evaluated and appropriately treated in the analysis.

The individual interpreting the data should also take note of the following special types of data, and consider the following recommendations on their use:

Specification Data—Virtually all alloys used for high-temperature applications are controlled and purchased by a process control variable generally called "spec point". Therefore, there will often be large quantities of data available from quality control data records at the specification condition. Data will contain many heats, and serve as an excellent measurement source of scatter. Therefore, in regression modeling, specification data are often the major source of scatter measurements. Slope measurements must come from the experimental design matrix.

Specification data can also be used to (1) determine, through analysis-of-variance techniques, fractions of scatter due to heat-to-heat variations, etc., (2) determine, through distribution analysis, if data are normal, log normal, etc., and (3) find out, if data are not normal, what transformation is required.

Outliers—These can be excluded only if tests are demonstrably invalid, or if the effect on the equation and statistical parameters is unreasonable. Since exclusion of outliers normally involves a certain degree of judgment, it should only be done by a knowledgeable, experienced individual.

Discontinued Tests—These can be included if longer lived, or excluded if shorter lived, than average life of the data subset (lot, section thickness, etc.) to which they belong. (Also, see censored distributions in Section 9.3.6.5 on Data Analysis Procedures.)

Stepped-Tests—If load on the specimen had been increased or decreased after initial loading, this test result shall be excluded.

Truncating Data—Certain equations, notably parametrics, often do not properly represent a mix of shorter and longer time data. These equations can severely overpredict creep and rupture lives less than ten to thirty hours. Similarly a preponderance of short time data can cause long lives to be overpredicted. Eliminating such data requires truncating the data (or subset). This is done by removing all data above (or below) a fixed stress level, even though normally acceptable data are excluded.

Background Data Reporting—The significance and reliability of creep data generated at elevated temperatures for heat-resistant alloys are, to a major extent, a function of detailed factors which relate to the material, its processing, and its testing. Hence, it is necessary to evaluate not only the property data, but also correlative information concerning these factors.

It is not possible to specify individual items of correlative information, or the minimum thereof, which must be provided with elevated temperature property data to make those data properly meaningful. Individual alloy systems, product forms, and testing practices can all be quite unique with regard to associated information which should be provided with the data. A certain minimum amount of information is required for all data, including:

(1) Identity of alloy

(2) Chemical composition of the specific material tested

(3) Form of product (sheet, forging, etc.)

(4) Heat-treatment condition

(5) Producer(s)

(6) Specification to which product was produced (AMS specifications are normally considered standard*)

(7) Date when part was made.

Lack of such information is sufficient basis for rejection of a particular data set.

In addition, it is vital that the individual submitting data consider those factors which contribute to uniqueness of the alloy, processing, and/or testing, and give thought to information which is pertinent to that uniqueness. Thus, grain size can be a significant variable, not only between cast turbine blades, but within a single blade. Thermomechanical working processes may result in significantly different properties (not only higher, but lower as well); and test specimen design can affect resultant data. It is mandatory that knowledgeable personnel be involved when data are submitted for evaluation and potential use. Any correlative data that can be provided will aid the analyst in identifying valid reasons for rejection of data which may not fit the trends of other data (outliers). Such apparent outliers may be indicated through analysis of between-heat variance as described in Section 9.3.6.5.

These examples illustrate the need for adequate information:

(1) Creep-rupture specimens are being machined from cast high-strength, nickel-base alloy turbine blades. At center span location, specimens are 0.070- to 0.090-inch diameter, while at the trailing edge, specimens are flat and 0.020-inch thick. Flat specimens are typically about one Larson-Miller parameter weaker than round specimens, which is attributable both to thickness effects of the thin specimens and to finer grain size at the trailing edge. In addition, trailing edge specimens exhibit more scatter. Hence, availability of associated information is vital when considering data from specimens machined from cast turbine blades.

(2) Comparison of creep-rupture properties of Waspaloy and Superwaspaloy shows that the latter is much weaker at temperatures approaching the upper bounds of utility of the alloy. The significantly lower properties at higher temperatures are attributed to a finer grain size of Super waspaloy and also to a recovery process that may well be occurring at these temperatures. This alloy is subjected to extensive thermomechanical working, and some strengthening gained by the associated warm working is lost at higher testing temperatures. This effect clearly indicates that processing history significantly affects levels of mechanical properties and, hence, must be adequately documented when property data are submitted.

9.3.6.5 *Data Analysis Procedures*—After an acceptable data collection has been obtained and interpreted, it is possible to proceed in analyzing those data and developing mathematical models of creep and creep-rupture behavior. The objective of the procedures described in the following paragraphs is to calculate creep and rupture life as a function of test conditions and other significant variables. This calculation is done to provide an average curve and a measure of expected variability about the average. The approach that is discussed involves regression analysis to optimize the fit of an equation to the data set. Linear regression analysis is described in Section 9.6.3. The following information provides guidelines in the application of regression analysis to creep and rupture data and recommends approaches to specific problems that are frequently encountered.

General—It is assumed that life or time is the dependent variable for rupture or isostrain creep equation analysis, respectively, and logarithmic transformation of the dependent variable is normally distributed.

*Company specification data may be included with federal, military, and industry specification data if it is properly documented and can be shown to compare favorably in creep or stress-rupture behavior.

The data set will nearly always contain a variety of stresses and temperatures. If the data set is the product of a very well-balanced test design (see Section 9.3.6.3), good results may be obtained by independently fitting each temperature. Since this type of data set is often not available, and the approach sacrifices the opportunity for interpolation, the discussion will assume that at least temperature and stress are used as independent variables.

In order to achieve good results, it may be necessary to consider other variables. Some variables are continuous physical variables that are incorporated into regression variables, e.g., section size. Other variables may occur as discrete subsets that require modifying the regression analysis (this is discussed under Subsets of Data). In such cases, it may be necessary to group data per subset for data reporting if regression analysis cannot easily accommodate the observed subsets.

Selection of Equations—For isostrain and rupture time, as a function of stress and temperature, a number of relationships have been proposed. Some useful ones are:

(1) $\log t = c + b_1/T + b_2X/T + b_3X^2/T + b_4X^3/T$
(2) $\log t = c + b_1/T + b_2X + b_3X^2 + b_4X^3$
(3) $\log t = c + b_1 T + b_2X + b_3X^2 + b_4X^3$
(4) $\log t = c + (T-T_a)(b_1 + b_2X + b_3X^2 + b_4X^3)$.

These are the Larson-Miller, Dorn, Manson-Succop, and Manson-Haferd, respectively, where

c = the regression constant
b_1 = coefficients (b_1 through b_4)
t = time
T = absolute temperature (T_a is the temperature of convergence of the isostress lines)
X = log S (stress).

While all forms may be used to model a data set with varying degrees of goodness of fit, experience and practice indicate the Larson-Miller relationship adequately models most materials, and is usually the preferred equation form.

If data for a given material is available at a variety of creep strain levels as well as the stress rupture point, only one model should be used to describe data trends for each strain level. The decision as to which of the four customary models is chosen should be based on a comparative analysis of data for the most comprehensive data collection, whether that collection be for a specific creep strain level or stress rupture point. In addition, the constant term found in the optimum analysis should be held the same for all creep strain levels. If this is done, it will be possible to construct a composite plot of stress versus parameter for all creep strain levels and the stress-rupture level.

If none of these standard forms satisfactorily follows data trends, various combinations of stress and temperature may be tried. For example, terms can be selected from a matrix obtained using cross products of T^{-1}, T^o, T^1 with S^{-1}, S^o and S^1. Methods for generalizing and applying these equations are discussed in Reference 9.3.6.5.

The exact form of the functions should reflect data and reasonable boundary conditions. Quadratic, quartic, etc., can be expected to give poor boundary conditions, e.g., zero life at zero stress, and should be avoided. Extrapolation by users of the equation is inevitable (though it is not recommended), so other general equations must be checked for unusual behavior beyond the data—this can be done, in many cases, by differentiating to obtain maxima and minima. In general, short times should give strengths approximately corresponding to tensile yield and ultimate strength; zero stress should predict infinite life.

Metallurgical instabilities and transition regions may present difficulties in some analyses. Methods for handling such problems have been discussed in Reference 9.3.6.5.

Optimum Fit-Guidelines for an optimum fit are:

(1) Minimum number of terms. With two independent variables, σ and T, six regression variables are reasonable, each additional physical variable allowing two additional regression variables.

(2) Reasonable curve characteristics for material behavior, including extrapolation.

(3) Minimum standard error and maximum correlation coefficient (as long as 1 and 2 are not violated). Standard errors are typically between 0.1 and 0.2.

(4) Uniform deviations (see a later paragraph on Weights for a brief discussion of nonuniform deviations and their analytical treatment).

Subsets of Data—A non-normal or multimodal population, or an excessive standard error may indicate the presence of subsets. However, an apparently typical data set may contain subsets that should receive special consideration.

One type can be treated by adding physical variables to the regression analysis. For example, different thicknesses of sheet material may give different average lives. Including sheet thickness in the regression should not only improve fit but also avoid the risk of misrepresenting behavior of the material. Section thickness, distance from surface, and grain size are other examples of subsets that can be treated as regression variables. Section thickness and distance from surface refer to location of the specimen in terms of geometry of the original material, e.g., finish work thickness, final heat thickness, etc.

A second type is not typically subject to use as a regression variable. Examples of these are orientation (L, LT, and ST), or different heats (chemistry). A decision must be made whether to treat these as unique subsets to be analyzed separately (if properties are different) or as randomly distributed subsets. Orientation will usually be analyzed separately, while heats will usually be randomly distributed subsets. Other methods (e.g., fixed intercept, centered above mean values for each creep level) may be more suited for a given data set and may be tried. The specific procedure used must be indicated in the data package.

The theory of treatment of randomly distributed subsets has been developed in Reference 9.3.6.3, while application to lots of material (actually "heats" in chemistry) is considered in Reference 9.3.6.5. Treating subsets as random affects calculation of both average curve and standard error. While effect on standard error may become insignificant as the number of subsets exceeds ten (depending on the relative contribution to total standard error), effect on the trend of the calculated average remains. Lots whose average lives are uniformly displaced (parallel) in logarithm of life, or are not significantly non-parallel, are discussed in Reference 9.3.6.5. There is no known published reference for treating non-parallel lots. Data permitting, individual lots can be fitted, within-lot variances pooled, and average and variance of lot averages calculated for selected stress-temperature combinations. After calculating total variance and desired lower level tolerance limit* (X-ks) at each stress level, curves can be drawn and, if desired, equations be fit to X's and (X-ks)'s. It should be noted that the equation for (X-ks) is not likely to properly reflect uncertainty in coefficients obtained by normal fitting procedures. Alternately, all data for non-parallel lots can be pooled and variance weighted, providing sufficient lots are represented and average curve is reasonably similar to the first approach.

*Tolerance limits used here are one-sided and are normally developed for tolerance levels of 90 or 99 percent at a confidence level of 95 percent.

Consistency in Creep and Stress Rupture Trends—When creep data are somewhat limited, an independent analysis of each creep strain level may produce inconsistent trends between different creep strain levels and stress rupture mean curve. There may be cases where very minor extrapolations will produce creep curves that cross over each other or the stress rupture curve. In some instances, this problem can be eliminated, without a significant loss in quality of fit at each creep strain level, by forcing a prescribed relationship to exist between creep curves and stress rupture curve. Parallelism in log(time) is the simplest relationship that can be assumed, but it is also a relationship that is often supported by data trends. A linearly increasing or decreasing separation of creep curves and stress rupture curve in log(time) as a function of stress is also a possibility, but it takes a large quantity of data to verify such trends. If large quantities of data are available, then it is generally preferable to analyze each creep strain level individually. Therefore, about the only practical relationship to assume between individual creep curves and the stress rupture curve is parallelism in log(time).

Parallelism in log(time) can be achieved through the addition of a dummy variable to the stress rupture equation for each creep strain level being added to the regression analysis. For example, in the case of the Larson-Miller equation, which (in its third order form) is normally written as

$$\log t = c + b_1/T + b_2X/T + b_3 X^2/T + b_4 X^3/T,$$

where

t = is time

T = is absolute temperature

X = is log (stress),

the equation can be modified to include additional terms for each creep level, as follows

$$\log t = c + b_1/T + b_2X/T + b_3X^2/T + b_4X^3/T + b_5 Y_1 + b_6 Y_2 + ...b_4 + i Y_i$$

where the value of Y_i new terms are either 0 or 1. If a creep strain level 1 data point is considered, Y_1 = 1 and all other Y's are 0. Similarly, if a creep strain level 2 data point is considered, Y_2 = 1 and all other Y's are 0. If a stress rupture data point is considered, all the Y's are 0. In this way, the optimized values of additional b's represent average A in log(time) that each creep curve falls below the stress rupture curve.

The usefulness of such an approach must be verified through an examination of quality of fit for each creep strain level compared to raw data trends.

Weights—Rupture and isostrain creep curves will not normally require weights to obtain uniform variables. Analysis, including strain as a variable, frequently will. Variables other than strain, temperature, and stress will require evaluation for uniform variance. Reference 9.3.6.5 provides further discussion of weighting.

Rejection of Analyses—Regression analyses of specific creep or stress-rupture data sets should normally be rejected if the R^2 statistic for analysis is <75 percent, or there are fewer data than five times the number of temperature levels, or there are <20 data points total available for regression.

If data for several different creep strain levels are analyzed in combination with stress rupture data, R^2 levels below 75 percent for one or two creep strain levels may be acceptable, if the overall R^2 exceeds 75 percent. Separate analyses of low creep strain data may show relatively high variation with R^2 values

below 75 percent. In these cases, if there are sufficient data to produce significant regression coefficients at a 95 percent confidence level, the result may still be acceptable for inclusion in MIL-HDBK-5.

9.3.6.6 *Preparation of Creep-Rupture Data Proposals*—Creep-rupture proposals developed for review and possible inclusion in MIL-HDBK-5 should contain the following information and meet associated criteria.

Data Reporting—The background information shall meet the requirements of Section 9.3.6.4. Test results shall be listed in a manner such that all data are identifiable in terms of material and test background information as well as test conditions used in generating data (see Section 9.3.6.7 for an example).

Analysis Reporting—The analysis report will display the following (see Section 9.3.6.5 for details);

(a) Trials—Equations tried and reason for ejecting.

(b) Data rejected—Reason.

(c) Best-fit details—Listing of data, calculated values, and deviations. All data are to be clearly traceable in terms of data reporting requirements.

(d) Standard error or total variance and correlation coefficient.

(e) Subset variance—If random subsets are used, report both the pooled within-subset variance and the between-subset variances as well as the total variances.

(f) Constants—Report the average regression constant and regression constants for any subsets.

(g) Coefficients—Report the numerical value of the coefficient of each regression variable and its standard error.

(h) Equation—Exhibit the equation used; with the coefficients, b_1, traceable to the numerical listing in above item (g).

(i) Deviation—Exhibit plots of deviations in life versus calculated life for each temperature and, as far as possible, identify according to subsets. It is also possible to provide a summary table of deviations. As an example of isostrain creep or rupture, divide the life range of data in five equal logarithmic increments and, for each temperature, give the algebraic sum of deviation with that increment. If random subsets are used, deviations summed are to be those from within the respective subsets.

(j) Data and Curve Comparison—Display data against the calculated average curve. Encode data with symbols as the deviation plots. Scale coordinates such that the curves have an apparent slope of about -1.0. Use scales appropriate for the most significant from of the regression variable, usually log(stress) versus log(life), with life (dependent variable) on the abscissa and stress on the ordinate.

(k) Curve Extrapolation Tests—Exhibit the average curve from one to 105 hours for corresponding temperature levels. Representative curves may be used including extreme values of independent variables represented in data. Further, calculation of desired tolerance limit (e.g., probability level) should be performed to assist in determining validity of the extrapolation.

The above recommendations apply to incorporation of new creep and/or stress-rupture curves in MIL-HDBK-5. The use of creep nomographs has been discontinued. Creep nomographs in MIL-HDBK-5 will be replaced as data are reanalyzed and new analytically defined creep and stress rupture curves are developed.

9.3.6.7 *Data Presentation*—The presentation for MIL-HDBK-5 will include one or more pages of correlative information, equations, and curves as needed. Requirements on each will vary with the problem and should be reasonably obvious from data, background information, and analytical results.

An example of a typical data presentation is shown in Figure 9.3.6.7. Note that raw data are displayed along with mean trend lines, on a semi-logarithmic plot of stress versus time. Supportive data describing alloy, specimen details, and analysis results are also presented. Table 9.3.6.7 provides even more detailed, but necessary, information on such factors as heat treatment details and inverse matrix (which can be used in conjunction with other analysis results to compute lower level tolerance limits for the data).

Some creep data are still presented in creep nomographs. For these cases, the analysis and presentation were based primarily on Reference 1.4.8.2(b). The presentation of creep data in the form of a nomograph is not in compliance with the above guidelines. Therefore, these creep nomographs will be replaced in the near future.

9.3.6.8 *An Example of the Use of Experimental Design for the Purpose of Developing Regression Models*—By a slight chemical change and modification of heat, the former Alloy 325 is now believed to have an increased stress-rupture life of 20 percent to 30 percent. It is desired to fully characterize these properties over the 1600 to 1900 F range. Average creep life is to be from 10 hours to 1000 hours.

Nineteen stress rupture tests from two heats of new alloy averaged 37.4 hours at 30 ksi/1800 F, s(log 10) = 0.150. Figure 9.3.6.8(a) is a log-log mean life plot of predicted stress rupture properties of modified Alloy 325 based on a predicted value. A 1750 F line has been added to the original plot. From this log-log plot, it can be seen that only three temperatures need to be tested because there are stress levels in common with the 1600 F line, and the same is true for the 1750 F and 1900 F lines.

Next, three temperature lines are bracketed with the 10-hours to 1000-hours life range. See Figure 9.3.6.8(b). Stress levels are then chosen to give the desired life. There are 25 tests required with this procedure. All 25 could be run, or 3 tests could be randomly eliminated from the center cells of the matrix (see circled cells). If 3 are deleted this would leave 22 tests, which are near the minimum of 20. These tests could be conducted and these data added to the 19 specific data points at 30 ksi/1800 F. This quantity would constitute the data set. Table 9.3.6.8 shows the results of a simulated sampling.

A Larson-Miller analysis of data produced the curves in Figures 9.3.6.8(c) and (d). Data plotted with the temperature lines of Figure 9.3.6.8(d) confirm a good fit over the range of data. The approach described in this example can be used for any creep or rupture experimental design.

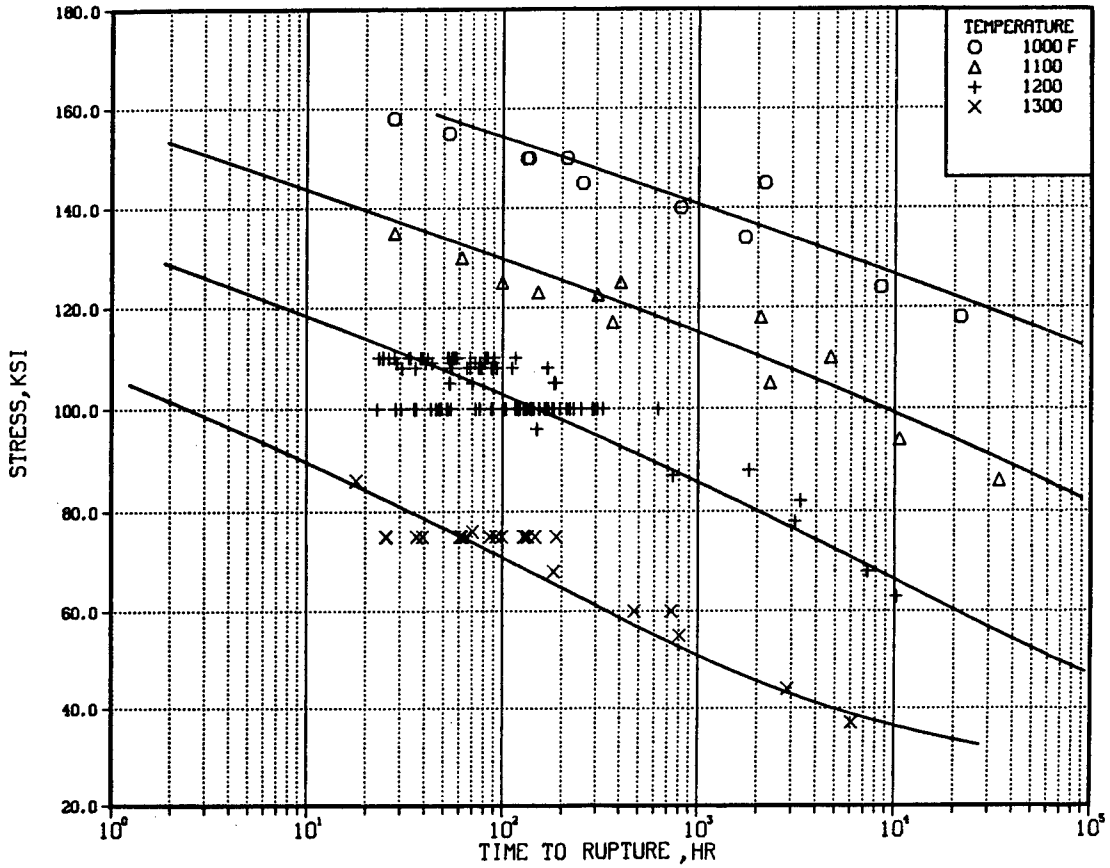


FIGURE 9.3.6.7. *Average isothermal stress rupture curves for alloy XYZ forging.*

Correlative Information for Figure 9.3.6.7(a)

Makeup of Data Collection:

Public Specifications—AMS 5663
Heat Treatment—2, 21 [See Table 9.3.6.7(a)]
Number of Vendors—Not specified
Number of Heats—7
Number of Test Laboratories = 3
Number of Tests = 347

Specimen Description:

Type—Unnotched round bar
Gage Length—N.A.
Gage Thickness—1/4"—3/8"

Stress Rupture Equation:

$\log t = c + b_1 T + b_2 X + b_3 X^2 + b_4 X^3$
T = °R, X = log (stress, ksi)
c = 186.27
b_1 = -0.01778
b_2 = -255.25
b_3 = 146.28
b_4 = -28.65

Analysis Details:

Inverse Matrix—See Table 9.3.6.7(a)
Standard Deviation = 0.63
Standard Error of Estimate = 0.29
Within Heat Variance = 0.071
Ratio of Between to Within Heat Variance = (at spec pt.) < 0.10

TABLE 9.3.6.7. *Supplemental Data Pertaining to the Stress Rupture Behavior of Alloy XYZ Forging*

Heat Treatment Details

Heat Treatment Number	Cycle Number	Temperature, °F	Time, Hours	Cool
2	1	1800	1	AC, WQ
	2	1325	8	FC (100 F/hr)
	3	1150	8	AC
21	1	1700–1850	1	AC
	2	1325	8	FC (100 F/hr)
	3	1150	8	AC

Stress Rupture Equation and Inverse Matrix for the Creep Stress = 0.10, 0.20, 0.50, and 5.00% and Stress Rupture Conditions

$$\log t = c + b_1T + b_2X + b_3X^2 + b_4X^3 + b_5Y_1 + b_6Y_2 + b_7Y_3 + b_8Y_4 + b_9Y_5$$

where $Y_1 = 1$; Y_2, Y_3, Y_4, $Y_5 = 0$ for Creep Strain = 0.10% Data
$Y_2 = 1$; Y_1, Y_3, Y_4, $Y_5 = 0$ for Creep Strain = 0.20% Data
$Y_3 = 1$; Y_1, Y_2, Y_4, $Y_5 = 0$ for Creep Strain = 0.50% Data
$Y_4 = 1$; Y_1, Y_2, Y_3, $Y_5 = 0$ for Creep Strain = 5.00% Data
Y_1, Y_2, Y_3, Y_4 $Y_5 = 0$ for Stress Rupture Data

Column / Row	1	2	3	4	5	6	7	8	9
1	1.809E+00	-1.108E-03	-1.978E+00	6.499E-01	-5.748E-02	-1.606E+00	-1.444E+00	-1.015E+00	-9.777E-01
2	-1.108E-03	6.834E-07	1.212E-03	-3.979E-04	3.517E-05	9.843E-04	8.852E-04	6.219E-04	5.993E-04
3	-1.978E+00	1.212E-03	3.482E+00	-1.657E+00	2.032E-01	1.634E+00	1.359E+00	6.886E-01	5.921E-01
4	6.499E-01	-3.979E-04	-1.657E+00	9.145E-01	-1.220E-01	-4.892E-01	-3.610E-01	-6.305E-02	3.594E-03
5	-5.748E-02	3.517E-05	2.032E-01	-1.220E-01	1.697E-02	3.801E-02	2.248E-02	-1.245E-02	-2.618E-02
6	-1.606E+00	9.843E-04	1.634E+00	-4.892E-01	3.801E-02	1.471E+00	1.303E+00	9.401E-01	9.124E-01
7	-1.444E+00	8.852E-04	1.359E+00	-3.610E-01	2.248E-02	1.303E+00	1.222E+00	8.806E-01	8.600E-01
8	-1.015E+00	6.219E-04	6.886E-01	-6.305E-02	-1.245E-02	9.401E-01	8.806E-01	7.491E-01	6.987E-01
9	-9.777E-01	5.993E-04	5.921E-01	3.594E-03	-2.618E-02	9.124E-01	8.600E-01	6.987E-01	1.195E+00

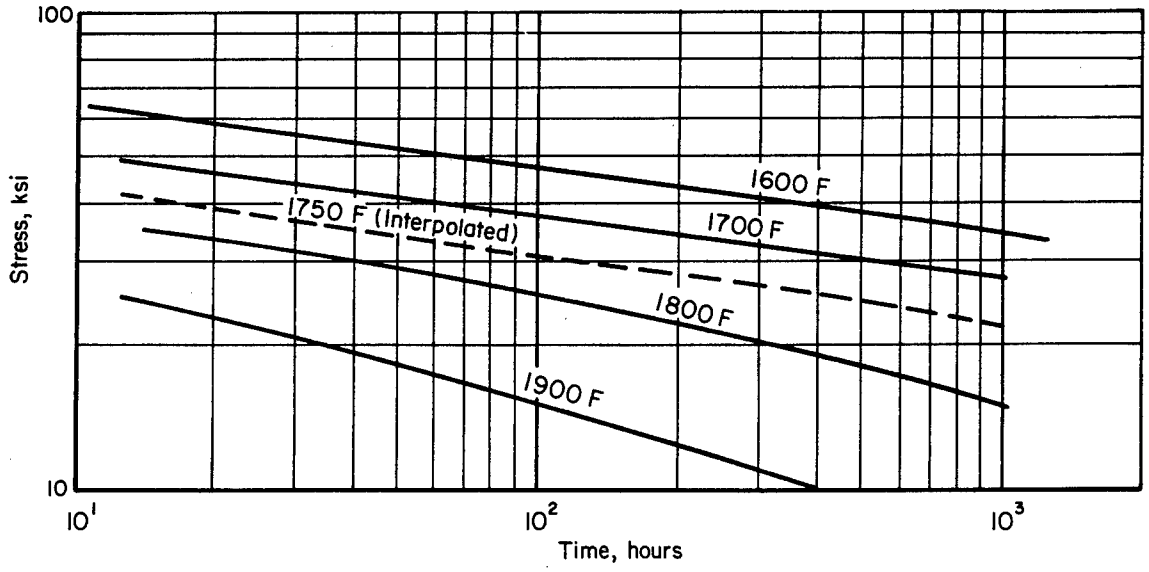


FIGURE 9.3.6.8(a). *Estimated stress rupture curves for Alloy 325 (MOD).*

TEMP	3	6	10	18	32	HOURS 56	100	180	320	560	1000	3000	5600	°F
T1			63	59	54	52	(48)	46	42	39	36			1600
T2			42	39	36	32	29	27	(25)	22	20			1750
T3			25	22	(20)	17	15	12	10					1900
T4														
T5														
T6														
T7														
T8														

FIGURE 9.3.6.8(b). *Experimental design matrix for creep rupture.*

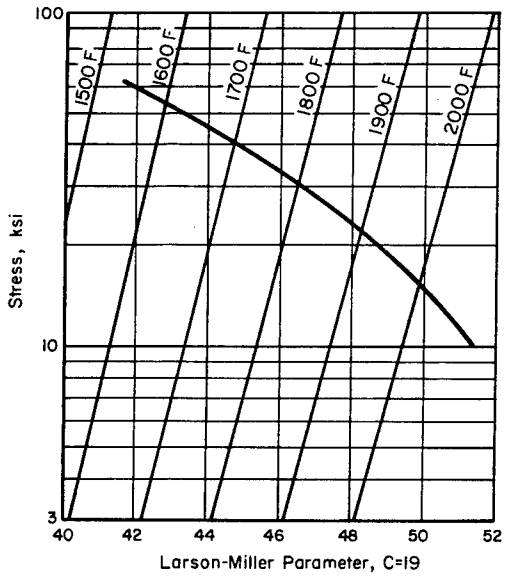


FIGURE 9.3.6.8(c). *Alloy 325 (MOD) stress rupture typical life.*

TABLE 9.3.6.8. *Results of simulated sampling of creep-rupture data*

ksi	1600 F	ksi	1750 F	ksi	1900 F
63	19.0 hrs.	42	8.8 hrs.	25	27.6 hrs.
59	11.1 hrs.	39	35.5 hrs.	22	23.9 hrs.
54	36.3 hrs.	36	52.3 hrs.	17	65.4 hrs.
52	170.7 hrs.	32	71.8 hrs.	15	140.3 hrs.
45	148.0 hrs.	29	121.9 hrs.	12	257.5 hrs.
42	376.0 hrs.	27	355.9 hrs.	10	623.5 hrs.
39	806.9 hrs.	22	389.0 hrs.	*	
36	878.0 hrs.	20	2912.4 hrs.	*	

*No interest.

SPECIFICATION DATA
@ 30 KSI 1800 F

Hours

41.4	33.1	70.5	36.1
16.5	27.4	37.5	34.9
35.0	33.4	48.6	74.2
33.6	51.3	29.0	47.5
32.6	42.7	26.4	

(n = 19, $\overline{X}$ = 37.4, s(log 10) = 0.150)

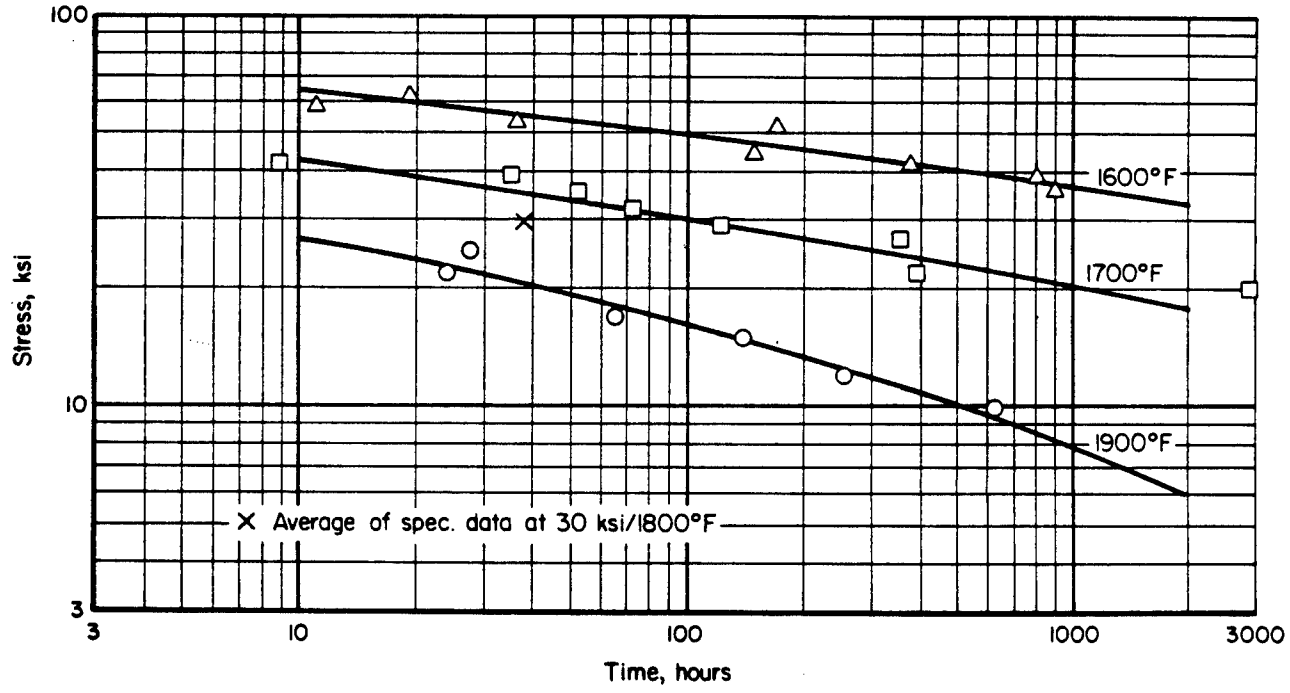


FIGURE 9.3.6.8(d). *Alloy 325 (MOD) stress rupture typical life.*

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9.4 Properties of Joints and Structures

9.4.1 MECHANICALLY FASTENED JOINTS

9.4.1.1 *Introduction*—Some mechanical fasteners will not develop full bearing strengths of materials in which they are installed. Joint allowables for these fasteners must therefore be determined from test data. Fasteners for which allowable loads must be determined are: (1) flush-head fasteners in dimpled or countersunk sheet, (2) fasteners with hollow or multiple-piece shanks, (3) protruding-head fasteners with shear-type heads*, and (4) protruding-head bolts and rivets when thickness-to-diameter ratio (t/D) is less than 0.18.

These guidelines define data generation (quality/quantity), analysis methods, and presentation format applicable to mechanically fastened joint allowables. They reflect a need to (1) ensure that the aerospace industry is interested in new fastener systems which are incorporated in MIL-HDBK-5, and (2) ensure that confirmatory data to substantiate allowable loads meet certain stated requirements that simplify the process of acceptance through coordination. To accomplish these needs, fastener systems proposed for inclusion in MIL-HDBK-5 may be introduced (sponsored) by airlines, airframe or engine prime contractors, and Government agencies (DoD, FAA, or NASA); i.e., one of the users. When introducing a new fastener, the sponsoring organization shall supply information specified in Section 9.4.1.7.1. The sponsoring organization is also expected to review the test program plan, actual testing, and data analysis. At least 25 percent of the specimen fabrication and testing shall be performed at a second facility. It also is expected that fasteners and fastener materials will be obtained from three production runs per diameter as documented in the report. The sponsoring organization shall submit a report documenting design allowables to MIL-HDBK-5 Coordination Group for evaluation. (See Section 9.4.1.7.2.)

Proposals not meeting the requirements described herein will be rejected or require more time-consuming evaluation, inevitably delaying approval and release of proposed allowables. Therefore, use of these guidelines in preparing proposals for MIL-HDBK-5 is essential.

In case of conflict, provisions of this document take precedence over reference documents for any tests or analyses made to provide, substantiate, or revise MIL-HDBK-5 fastener allowables.

9.4.1.2 *Definitions*—Terms used in Section 9.4.1 vary among users of this Handbook. To provide consistency, these terms are defined herein in accordance with the intent of MIL-HDBK-5.

(a) Deformable Shank Fasteners—A fastener whose shank is deformed in the grip area during normal installation processes.

(b) Nominal Hole Diameters—Nominal hole diameters for deformable shank fasteners shall be according to Table 9.4.1.2(a). When tests are made with hole diameters other than those tabulated, hole sizes used shall be noted in the report and on the proposed joint allowables table.

(c) Nondeformable Shank Fasteners—A fastener whose shank does not deform in the grip area during normal installation processes.

(d) Nominal Shank Diameter—Nominal shank diameter of fasteners with shank diameters equal to those used for standard size bolts and screws (NAS 618 sizes) shall be the decimal equivalents of

*For example, protruding-head fasteners with reduced head heights similar to those shown for NAS 529 rivets.

TABLE 9.4.1.2. *Nominal Hole and Shank Diameters, Inches*

Fastener Size, Fractional or Numbered	Deformable Shank Fasteners Nominal Hold Diameter		Nondeformable Shank Fasteners Nominal Shank Diameter[a]	
	Solid Rivets	Blind Fasteners	Solid Shank Fasteners	Blind Fasteners
1/16	0.067	...	...	...
3/32	0.096	0.098		
#4	...	...	0.112	...
1/8	0.1285	0.130	0.125	...
		0.144		
#6	...	...	0.138	...
5/32	0.159	0.162	0.156	0.163
		0.178		
#8	...	...	0.164	...
3/16	0.191	0.194	0.188	0.198
		0.207		
#10	...	...	0.190	...
#12	...	...	0.216	...
7/32	...	...	0.219	...
1/4	0.257	0.258	0.250	0.259
		0.273		
5/16	0.323		0.312	0.311
3/8	0.386	...	0.375	0.373
7/16	...	...	0.438	0.436
1/2	...	...	0.500	0.497
9/16	...	...	0.562	...
5/8	...	...	0.625	...
3/4	...	...	0.750	...
7/8	...	...	0.875	...
1	...	...	1.000	...
1-1/8	...	...	1.125	...
1-1/4	...	...	1.250	...
1-3/8	...	...	1.375	...
1-1/2	...	...	1.500	...

[a]In order to standardize test and analysis procedures, nondeformable shank fasteners shall be installed in net fit ± 0.0005 inch holes.

stated fractional or numbered sizes. These diameters are those listed in the fourth column of Table 9.4.1.2. Nominal shank diameters for nondeformable shank blind fasteners are listed in the fifth column of Table 9.4.1.2. Nominal shank diameters for other fasteners shall be the average of required maximum and minimum shank diameters.

There are many generically named fasteners for which joint allowables are provided. These fasteners are listed below, followed by the letter H or S. H signifies that, in the analysis, nominal hole diameter (as described above) is used. S signifies that, in the analysis, nominal shank diameter is used.

(a) Solid rivets and blind fasteners whose shanks deform during installation. (H)

(b) Solid rivets and blind fasteners whose shanks do not deform during installation. (S)

(c) Threaded and swaged-collar fasteners whose shanks do not deform during installation. (S)

(d) AR interference-fit and close-tolerance fasteners. (S)

9.4.1.3 *Data Generation*—Development of mechanically fastened joint allowables from test data usually is accomplished with the aid of graphic analysis. Coordinates of the graph are P/D^2 and t/D, where P is subscripted P_u for ultimate load and P_y for yield load. The analysis assumes that design of a line of fasteners (a given configuration, material, and range of diameters) is proportional so that, when data from tests are plotted with the above coordinates, all data for all diameters can be represented by a single design curve. A schematic diagram of such a design curve for ultimate load is shown in Figure 9.4.1.3.

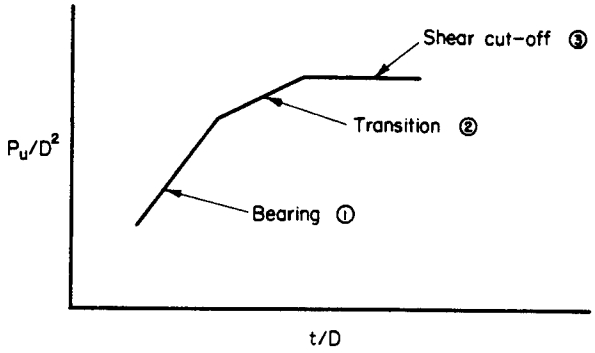


FIGURE 9.4.1.3. *Schematic diagram of P_u/D^2 versus t/D.*

Note there are three regions to the curve as follows:

Region 1, in which the joint failure mode is by sheet bearing.

Region 2, which is a transition failure zone in which failure may be by other means, such as head pulling through sheet, tension or shear of the fastener head, etc.

Region 3, in which the joint failure mode is by fastener shear.

The design curve shall be constructed so that all data fall to the left and above.

Data required for determining mechanically fastened joint allowables are based on results of single-shear lap-joint tests over the three regions described above, and fastener shear tests (usually, double shear tests in hardened steel test plates or fixtures). For driven rivets and blind fasteners, the single-shear lap-joint test in hardened steel test plates may be used to obtain shear strength or cutoff (Region 3). It is preferred, however, that shear strength be obtained from double shear tests of the fastener. Fastener system tensile strength data are required for all fasteners except solid and blind rivets (see Section 9.4.1.4.2). Sheet tensile test data also are necessary (see Section 9.4.1.4.5).

9.4.1.3.1 *Testing Equipment and Procedures*—Room-temperature testing equipment and procedures should comply with the provisions of MIL-STD-1312, Tests 4, 13, and 20 [References 9.4.1.3.1(a) through (c) for both single- and double-shear tests.

9.4.1.3.2 *Specimen Design Configuration*—Specimen design should be as provided in MIL-STD-13-12, Test 4, Figure 1, Reference 9.4.1.3.1(a).

9.4.1.3.3 *Yield Load Definition*—Joint yield loads for all fasteners are defined as loads which result in 0.04D permanent set in the joint when the fastener is tested in nominal hole size as defined in Table 9.4.1.2. For some fastening systems, tests in larger hole sizes, although within manufacturer's recommended hole size limits, may result in joint permanent sets greater than 0.04D* at yield load.

9.4.1.3.4 *Yield Load Determination*—The preferred method of determining yield load is by the secondary modulus method.** To obtain secondary modulus line, during the test the joint is unloaded from a load close to, and preferably above, estimated yield load to a load value in the range of about 10 to 20 percent of estimated yield load. The joint then is reloaded and secondary modulus is the slope of this second loading line. This procedure is described in Reference 9.4.1.3.1(a) and is illustrated in Figures 9.4.1.3.4(a) through (e).

If curves similar to Curves A and B in Figure 9.4.1.3.4(b) are obtained early in the test program, strain hardening will be presumed. In that case, unloading should be delayed in subsequent tests until after anticipated yield load. Curves showing strain hardening may be extrapolated a reasonable amount to determine yield load by the secondary modulus method as shown.

The initial loading line is used to establish the intersection with the abscissa from which to measure yield offset. At times, minor irregularities occur on initial loading which necessitates redrawing of the lower part of the curve as a continuation of the normal curve, as shown in Curves C and D of Figure 9.4.1.3.4(c).

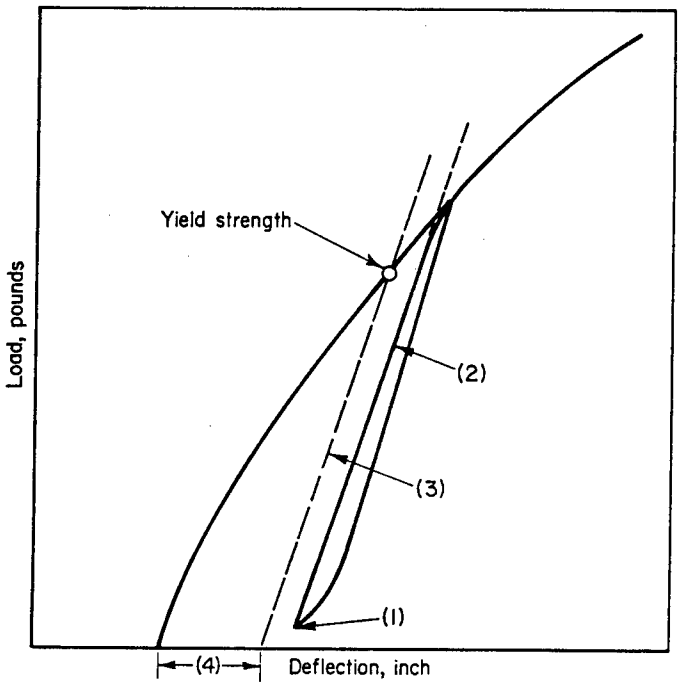


FIGURE 9.4.1.3.4(a). *Illustration of secondary-modulus method of yield strength determination.*

(1) Reduce load to 10-20 percent of yield load.
(2) Secondary-modulus line. The straight part of the loading side of the secondary-modulus loop indicating elastic behavior.
(3) Offset line. A line parallel to the secondary-modulus line.
(4) Offset. Equal to permanent set value specified in 9.4.1.3.3.

*Or previous yield load criteria used prior to 1973. Applicable yield criteria are noted in footnote for design allowable table.
**The primary modulus line has been used in the past, on occasion. It is the slope of the initial loading line and frequently is observed to have greater variability than the secondary modulus line.

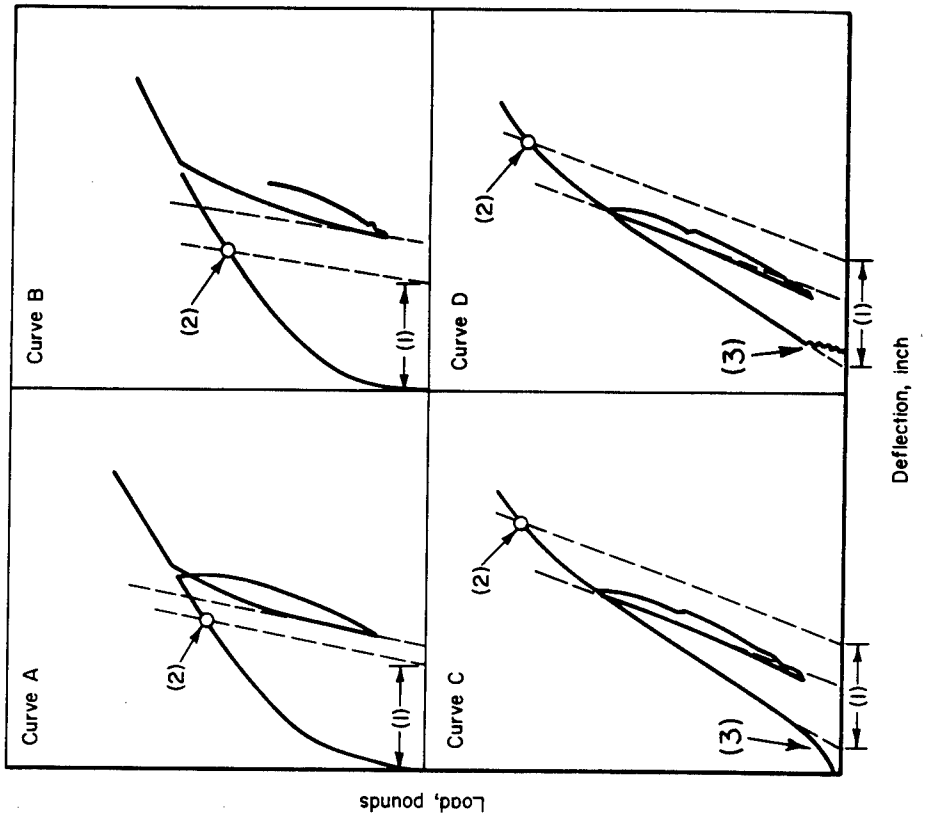


FIGURE 9.4.1.3.4(c). *Sample secondary-modulus load-deflection curves.*

(1) Offset per 9.4.1.3.3.
(2) Joint yield strength.
(3) Disregarded irregularities, per 9.4.1.3.

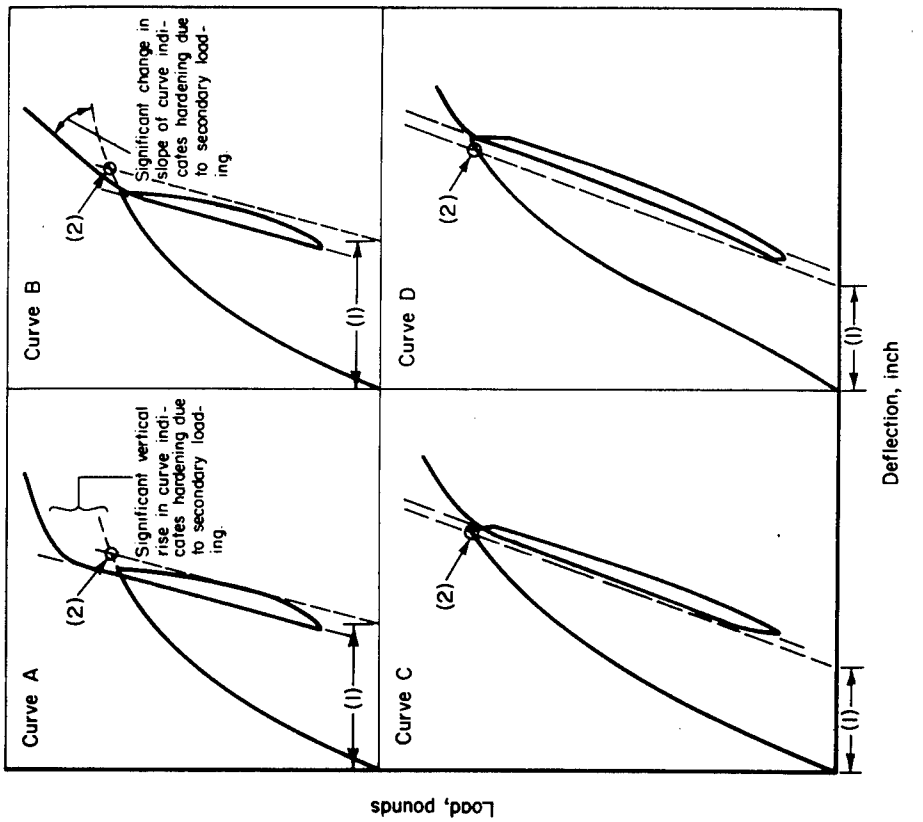


FIGURE 9.4.1.3.4(b). *Sample secondary modulus load-deflection curves.*

(1) Offset per 9.4.1.3.3.
(2) Joint yield strength.

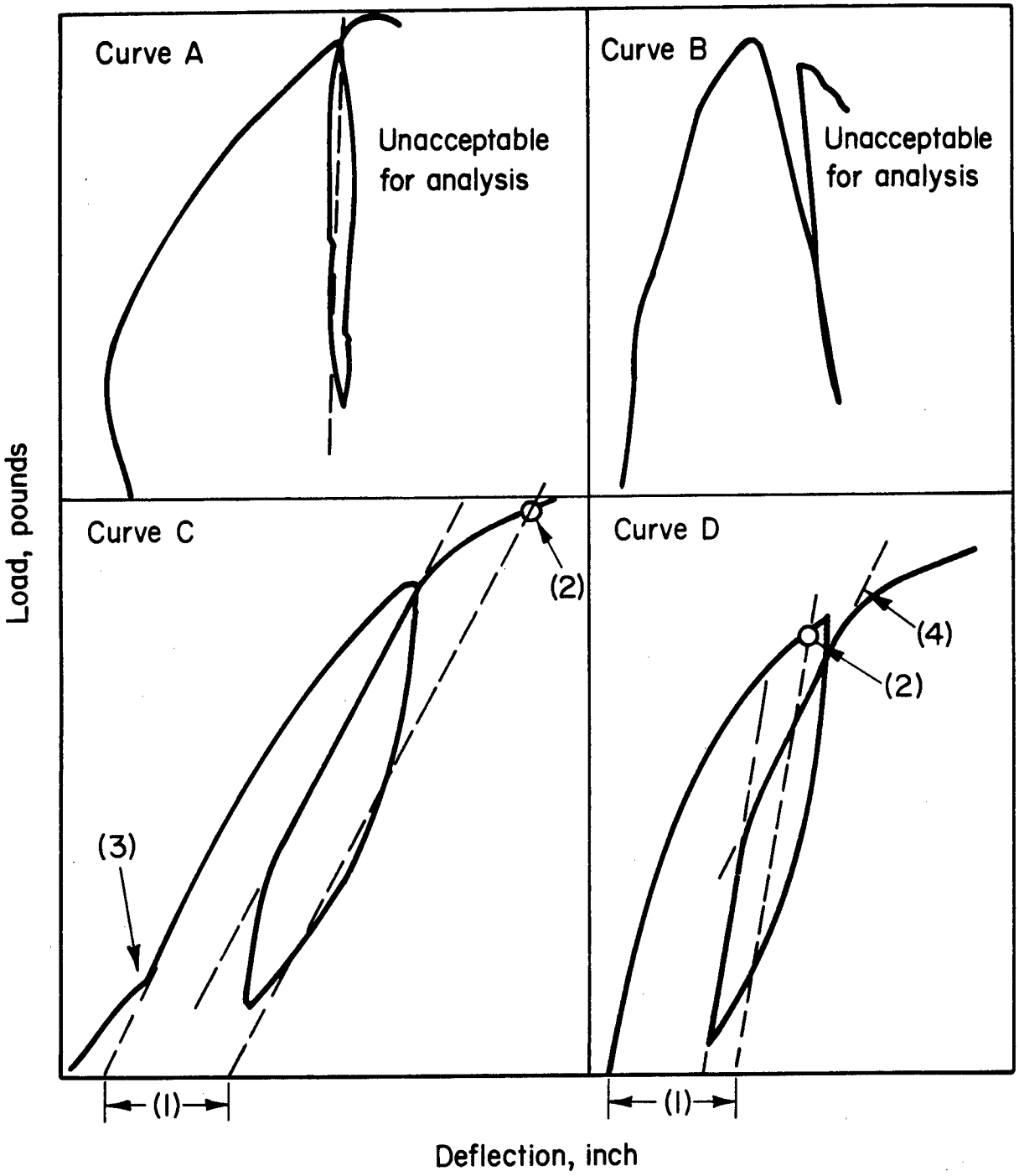


FIGURE 9.4.1.3.4(d). *Sample secondary-modulus load-deflection curves.*

(1) Offset, per 9.4.1.3.3.
(2) Joint yield strength.
(3) Disregarded irregularities, per 9.4.1.3.4.
(4) Disregarded second slope in secondary-modulus curve.

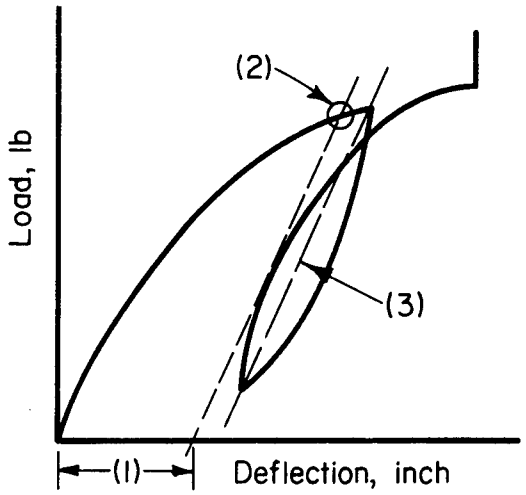


FIGURE 9.4.1.3.4(e). *Sample alternative second-load-ary modulus deflection curve.*

(1) Offset, per Section 9.4.1.3.3.
(2) Joint yield strength.
(3) Alternative secondary-modulus line.

Unusually shaped curves are sometimes obtained. Typical of these are the illustrations in Figure 9.4.1.3.4(d). Data which are typified by Curves A or B are unacceptable for analysis. When the secondary modulus has a straight-line portion of recognizable length, do as shown in Curve C. When the secondary curve has two straight parts, but is more in question (as in Curve D), and there are satisfactory curves available from similar group test specimens, use the slope which approximates other curves. Otherwise, the more conservative (steepest) shall be used. An acceptable alternate is to draw a straight line between end points of the off-loading-reloading loop and consider this as the secondary modulus line, as shown in Figure 9.4.1.3.4(e). The primary modulus method may be used as a last resort, if there is no straight-line portion or usable loop in the secondary modulus curve.

9.4.1.4 *Quantity and Distribution of Test Data*—This section delineates required data to develop the design curve shown schematically in Figure 9.4.1.3. There are three facets to consider, which are described in following subsections: (1) shear strength of the fastener, Region 3; (2) shear critical strength, bearing and transition regions, Regions 1 and 2; and (3) tensile properties of sheet and plate material used in the joint.

A fourth subsection is concerned with the case when data are required for certification purposes (not for use in MIL-HDBK-5) for a specific thickness and fastener diameter.

9.4.1.4.1 *Shear Strength of Fastener*—Although many fasteners for which joint allowables are given in MIL-HDBK-5 are covered by MIL and NAS specifications (which provide for minimum shear strength values), many proprietary fasteners are listed wherein minimum shear strength values are established by the manufacturer. In either case, sufficient testing is necessary to establish minimum values. The intent of this subsection is to provide minimum test requirements to document shear strength of fasteners appearing in MIL-HDBK-5, regardless of specification source.

Shear strengths shall be determined from shear-critical single-shear test results or double-shear test results. Double-shear test results performed in accordance with MIL-STD-1312, Test 13, are preferred over single-shear results, except for blind fasteners and driven rivets. For these latter fasteners, shear-critical tests shall be conducted with all components in the installed condition in hardened steel test plates. MIL-STD-1312, Test 20, is the preferred test method. Furthermore, when fasteners of a given configuration and material are identical in every respect except for head size and shape, fastener shear test data are necessary only on one head style.

The minimum quantity of shear tests required for each fastener diameter for which allowables are to be established is 15. Fasteners for each diameter shall be selected from at least three production lots that represent at least two heats of the fastener component materials.

Fasteners developed from materials not previously used for fastener applications will require additional testing in order to determine statistically reliable minimum shear strengths. Test values should be developed in accordance with the test methods noted above using hole sizes specified in those methods or Table 9.4.1.2, as appropriate. Test values shall represent a minimum of 10 tests from each of 10 production lots made of at least 3 heats of material (100 tests). Fasteners tested should be evenly distributed over the diameter range under consideration with grip ranging from 2 to 3 diameters for solid and blind rivets and any appropriate length for solid shank fasteners. Shear strength (F_{su}) should be computed based on hole size for solid and blind rivets and measured shank diameter for non-hole filling blind fasteners and pins. Data shall be checked for normality and if distribution is found to be normal:

(a) For solid driven rivets, compute the B-value and select the next lower shear strength from Table 8.1.1.1, if it is within 2 ksi of the computed value. If the computed B value is more than 2 ksi above the next lower value in Table 8.1.1.1, a new value may be proposed.

(b) For other fasteners, compute the A-value and select the next lower shear strength from Table 8.1.1.1. If the computed A-value is more than 5 ksi above the next lower value in Table 8.1.1.1, a new value may be proposed.

If analysis of data shows a non-normal distribution, obtain additional observations (as required) and employ the nonparametric procedure described in Section 9.2.8.2. Minimum shear strength shall then be selected as described in (a) and (b) above.

9.4.1.4.2 *Tensile Strength of Fastener*—Tensile strength shall be determined for all fastener systems except solid and blind rivets from tests performed in accordance with MIL-STD-1312, Test 8. Tensile test requirements and analytical methods shall be the same as for shear strength determination (see Section 9.4.1.4.1).

9.4.1.4.3 *Assembled Joint Strength*—The requirement for data from two fabricating and testing sources applies to assembled joint strength. Approximately 75 percent of required data shall come from one source; the remainder from a second source. Data shall cover the t/D range that results in bearing, transitional and shear-type failures as shown in Figure 9.4.1.3(a). It is suggested that the second source concentrate testing in the bearing and transition regions. Selection of sheet thickness shall be made in such a way that, for each fastener diameter, an even distribution of data is achieved over the t/D (thickness/diameter) range with about 20 percent of the data taken at t/D values for which joint failure will be by fastener shear (not applicable to dimpled joints). Sheet thickness/fastener grip combinations shall be selected to include a uniform distribution of minimum and maximum grip conditions throughout the t/D range tested. Specimen fabrication and testing shall be allocated to provide data from each source, distributed across the sheet critical and transition ranges.

9.4.1.4.4 *Sheet Critical Strength*—The requirement for data from two fabricating and testing sources applies to sheet critical strength. Approximately 75 percent of required data shall come from one source; the remainder from a second source. The data will cover the t/D range that results in bearing, transitional and shear-type failures as shown in Figure 9.4.1.3. It is suggested that the second source concentrate testing in the bearing and transition regions. Selection of sheet thickness shall be made in such a way that an even distribution of data is achieved over the t/D (thickness/diameter) range with about 20 percent of the data taken at t/D values for which joint failures will be by fastener shear (not applicable to dimpled joints).

All diameters of a given fastener for which joint allowable loads are established shall be included in the test plan. Since a fastener line usually comprises 2 to 5 more diameters, quantity of joint specimens to be tested will be expected to vary, depending upon number of fastener diameters. Quantity of data shall include results from at least the following valid tests: two diameters, 40 tests; three diameters, 55 tests; four diameters, 70 tests; five diameters, 85 tests. In allocating test joint specimens among fastener diameters, for a three- or four-diameter fastener line a larger quantity of specimens shall be used for the largest and smallest diameters with somewhat less testing for intermediate diameter(s). In the case of a five-diameter fastener line, larger quantities of specimens should be allocated to the largest, middlemost, and smallest diameters with somewhat less testing for the two remaining intermediate diameters. For each diameter and t/D combination tested, a minimum of three specimens should be used.

In the sheet critical range, fasteners with different head shapes, head sizes (NAS 1097, MS 29694, or MS 20426), material, or heat treatment will be considered different fasteners and shall require separate tests. Sheet materials with different heat treatments or compositions will be considered different materials and also shall require separate tests. In the case of aluminum alloys, data obtained with clad sheet may be used to determine allowables for clad and bare sheet; however, allowables, obtained from tests on bare sheet can be used only to determine allowables for bare sheet. In the case of all sheet materials, data from tests using sheet at one heat-treat level may be used to determine allowables for sheet having higher strength heat treatments. However, the reverse is not permissible.

9.4.1.4.5 *Tensile Properties of Joint Materials*—At least three sheet tension test results as required by MIL-STD-1312, Test 4, shall be provided for each sheet or plate used to make single-shear test specimens described in the previous subsection. Tensile ultimate and yield strengths and percent elongation shall be reported in accordance with ASTM E8. Grain direction shall be that applicable to the procurement specification tensile test requirements. Tabulated data shall identify single-shear specimens made from sheet to which each group of sheet-tension specimens apply by appropriate coding.

9.4.1.4.6 *Joint Allowable Loads for Limited Thickness Material*—In the event that joint allowable loads for a limited range of thickness or diameter required for procuring or regulatory agency (one such case would be where t/D is less than 0.18 for protruding head fasteners), a much smaller quantity of data is required than described in Section 9.4.1.4.2. As a minimum, this could require development of allowables for one thickness and one diameter of a given fastener. In this case, data shall consist of the results from 15 lap-joint tests and if practical shall represent at least three production lots of fasteners.

9.4.1.4.7 *Fastener Systems With Limited Grip Lengths*—Should a static joint strength table be desired for a fastener system produced in a limited range of grip lengths, the following procedure shall be followed:

(1) Sponsorship (see Section 9.4.1.7.1), including a specification and standards page, shall be required.

(2) Test all diameters (at least 2) through the full grip range (a minimum of 3 grip lengths above knife-edge) shown on the standards page.

(3) Test a minimum of 5 specimens per t/D ratio (3 from the prime source and 2 from the second source).

(4) To the extent possible, the distribution of minimum/maximum grip combinations and fabrication testing allocation specified in Section 9.4.1.4.2 shall be observed.

(5) Analyze the data using a conservative application of the standard approach (possibly requiring all test data points to be above the average ultimate -5 percent or average yield -10 percent lines in cases of extreme data scatter).

(6) Use the standard design allowables presentation except:

(a) Don't show fastener shear strength unless shear failures are obtained in the test program.

(b) In a box, located prominently within the table, place the following information.

THIS FASTENER IS ONLY MANUFACTURED IN LIMITED GRIP LENGTHS. IT HAS ONLY BEEN TESTED IN THE SHEET GAGES SHOWN IN THIS TABLE. DESIGN DATA FOR SHEET GAGES OR DIAMETERS OTHER THAN THOSE SHOWN HERE CANNOT BE EXTRAPOLATED.

(7) Additional test data and a new part number may be required if available diameters and/or grip lengths are extended in the future.

9.4.1.4.8 *Confirmatory Data.*—If a manufacturer wishes the company name to be added to the footnote of an existing table as a supplier of confirmatory data, the following procedure shall be used:

(1) Repeat, in total (quantities and conditions), the original test program from which the table was developed.

(2) Utilizing the test report from the original supplier of the test data, plot the average ultimate strength +10 percent and -5 percent, ultimate load design lines, and average yield strength ±10 percent lines.

(3) Utilizing these plots, plot the average data points and the lowest ultimate data point from each t/D combination tested by the supplier of confirmatory data.

(4) If all plotted average points fall within or above the plotted bands, and all lowest ultimate values fall above the design ultimate line, then the new product has the same allowable load values as the original fastener tested and can be included in the table.

(5) The existing design allowable table shall be modified in accordance with Item 17(c) of Section 9.4.1.6.

If a manufacturer wishes the company name to be added to the footnote of an existing design allowable table with four or more diameters as a supplier of confirmatory data but does not produce or market

the fastener in all diameters contained in the design allowable table, the following procedure shall be used:

(1) Test at least three successive diameters including the smallest diameter in the design allowable table, or test at least three successive diameters including the largest diameter in the design allowable table. Quantities shall be the same as for the original test program.

(2) Utilizing the test report from the original supplier of the test data, plot the average ultimate strength +10 percent and -5 percent, ultimate load design lines, and average yield strength ±10 percent lines.

(3) Utilizing these plots, plot the average data points and the lowest ultimate data point from each t/D combination tested by the supplier of confirmatory data.

(4) If all plotted average points fall within or above the plotted bands, and all lowest ultimate values fall above the design ultimate line, then the new product has the same allowable load values for the fastener diameters tested as the original fastener tested and can be included in the table.

(5) Add the following footnote to the design allowable table: "Confirmatory data provided by XYZ Company." Flag this footnote to supplier's part number and applicable fastener diameters.

9.4.1.5 Analysis of Test Data

9.4.1.5.1 *Shear Strength of Fastener*—Each group of double-shear or single-shear results for a specific fastener type, size, and material shall be analyzed to determine an A-value, except driven rivets which shall be analyzed to obtain a B-value. The lower limit shall be calculated using one of the following formulas:

$$L = \bar{x} - k\sqrt{\frac{\Sigma(x - \bar{x})^2}{n - 1}} \qquad [9.4.1.5.1(a)]$$

$$L = \bar{x} - k\sqrt{\frac{\Sigma x^2 - (\Sigma\bar{x})^2/n}{n - 1}} \qquad [9.4.1.5.1(b)]$$

$$L = \bar{x} - k\sqrt{\frac{n\Sigma x^2 - (\Sigma\bar{x})^2}{n(n - 1)}} \qquad [9.4.1.5.1(c)]$$

where

x = individual observed test result in terms of load

n = number of observed test results

L = lower tolerance limit corresponding to either the A- or B-basis

$\bar{x}$ = average of test results = $(\Sigma x)/n$

Σ = summation of all values of the indicated quantity

k = factor from Table 9.6.4.1 applicable to either the A- or B-basis.

The calculated L values shall be equal to or greater than the values in Table 8.1.5(a) (for the appropriate stress level) and the specification value. (That is, the computed L value for a 0.190 diameter, 95 ksi fastener shall be greater than, or equal to, the allowable load value of 2,694 pounds.) The allowable load shall be the lower of the appropriate Table 8.1.5(a) value or the specification value.

If Table 8.1.5(a) is not applicable (i.e., driven rivets, blind fasteners, and fasteners without shear-load requirements in the specification), the L values shall be converted to stresses for each diameter using nominal shank areas for S fasteners and nominal hole areas for H fasteners.

The allowable stress for the fastener system shall be established as the lowest of the above calculated stresses, or the specification stress value, whichever is lower. Allowable fastener shear strength shall be the product of this stress and the appropriate (H or S) areas used above.

The shear strengths so calculated shall be clearly identified as either 90 percent (B-value) or 99 percent (A-value) allowables.

9.4.1.5.2 *Sheet Critical and Transition Critical Strengths*—The analysis of data in the bearing and transitional regions provides design allowable curves for yield and ultimate strength where sheet or plate material of the joint is generally critical. To accomplish the analysis, tables and graphs are required as detailed in this subsection. The use of computer programs to analyze data and to prepare tables of calculations and figures, as next described, is acceptable. However, all tables and figures subsequently described should be illustrated in the report. When using a computer for analysis, some engineering judgements may be necessary for certain data sets in the transition thickness range.

(a) Presentation and Analysis of Basic Test Data—The values of the functions t/D, P_u/D^2, and P_y/D^2 shall be calculated from the basic t, D, P_u, and P_y test data obtained on each specimen tested, using the values defined below:

t = measured sheet thickness, inch, for thinnest sheet gage of combination

D = measured hole diameter, inch, for H-type fasteners, nominal shank diameter for S-type fasteners as defined in Section 9.4.1.2

P_u = test ultimate load, pounds per fastener

P_y = test yield load, determined per Section 9.4.1.3.4, pounds per transfer.

A suggested format for reporting the basic data and the computed values of t/D, P_u/D^2, and P_y/D^2 is shown in Figure 9.4.1.5.2(a). The average P_u/D^2 and P_y/D^2 for each fastener diameter at each t/D shall be indicated in the table.

Computation of P/D^2 and t/D from Basic Data

Test Specimen No.	D Diameter	D^2	t Gage	t/D	Yield Load, P_y	$\frac{P_y}{10^4 D^2}$	Ultimate Load, P_u	$\frac{P_u}{10^4 D^2}$	Type of Failure

t, D, P_u, and P_y, per Section 9.4.1.5.2.

FIGURE 9.4.1.5.2(a). *Suggested tabular layout for basic data and computer P/D^2 and t/D data.*

(b) Graphical Analysis to Determine Average Ultimate and Yield Load Curves—The general assumption inherent in a P/D^2 versus t/D analysis procedures is that the dimensions of a fastener system are proportional to the fastener diameter. Therefore, a graph of the average P_u/D^2 and P_y/D^2 values for each t/D tested is expected to yield a compact band of data points through which single ultimate and yield load curves can be drawn. This portion of the graphical analysis is to establish the all-diameters average curves; or if the data requires, establish more than one average curve for yield and ultimate loads for groups of fastener diameters. The suggested format for these graphical presentations is shown in Figure 9.4.1.5.2(b).

Using different symbols (suitably identified on the graphs) for each fastener diameter, the average P_u/D^2 values for all diameters tested shall be plotted as a function of t/D on a single graph. Sheet critical and transitional regional failures are to be plotted using symbols with an open form (i.e., ○, △, etc.). Fastener shear failures are plotted with the same symbols, but in closed form (i.e., •, ▲, etc.). Similarly, the average P_y/D^2 values shall be plotted as a function of t/D on a single graph. When applicable the data from the two sources shall be identified. In both cases, the resultant collection of data will be analyzed to establish average ultimate-load and yield-load curves. In the case of ultimate-load curve, consideration will be given to all test data for which joint failure was by failure modes other than fastener shear. The resultant average curves may be straight lines, a series of straight lines, or a smooth curve.

In constructing average ultimate- and yield-load curves in the low t/D region, which may include some data taken where the countersink extends into the second sheet, curves will be projected linearly downward, generally toward the 0-0 coordinate point. Such construction may ignore certain data that suggests the possibility of higher allowables. It is done in this manner to insure conservative design allowables in the near knife-edge condition.

The average curve (yield or ultimate load) represents the average of all plotted results and also represents reasonably the average curve for each diameter tested. The suggested test for reasonableness is that all of the plotted average ultimate load points shall fall in a band +10 percent, -5 percent of average curve for all diameters, and plotted average yield load points shall fall in a band ±10 percent of all average curve for all diameters. These lines should appear on the graphs. See Figures 9.4.1.5.2(c) and (d).

Individual graphs for each diameter will be provided that show average yield and ultimate load points at each t/D tested and lines representing the ±10 percent band for yield and +10, -5 percent band for ultimate. See Figure 9.4.1.5.2(e). In the event that any of individual diameter average values fall outside the band, the following apply: (1) for fastener diameters whose individual averages lie all or partly above the band, use the average curve obtained for all fasteners, (2) for fastener diameters whose individual averages lie all or partly below the band, use the lowest portions of the individual diameter average curve and the all-diameter average curve.

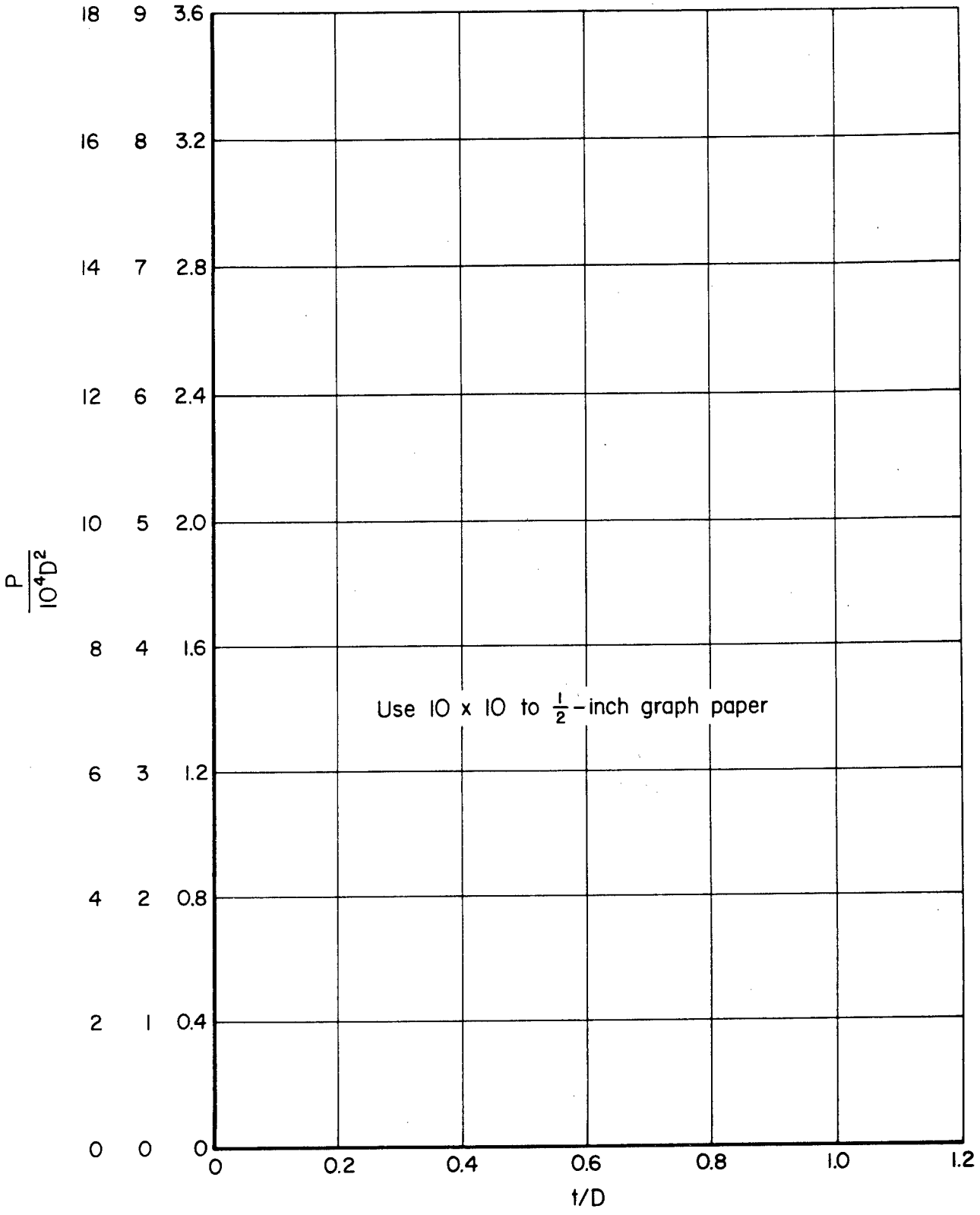


FIGURE 9.4.1.5.2(b). *Suggested coordinates for graphical presentation of joint allowables data.*

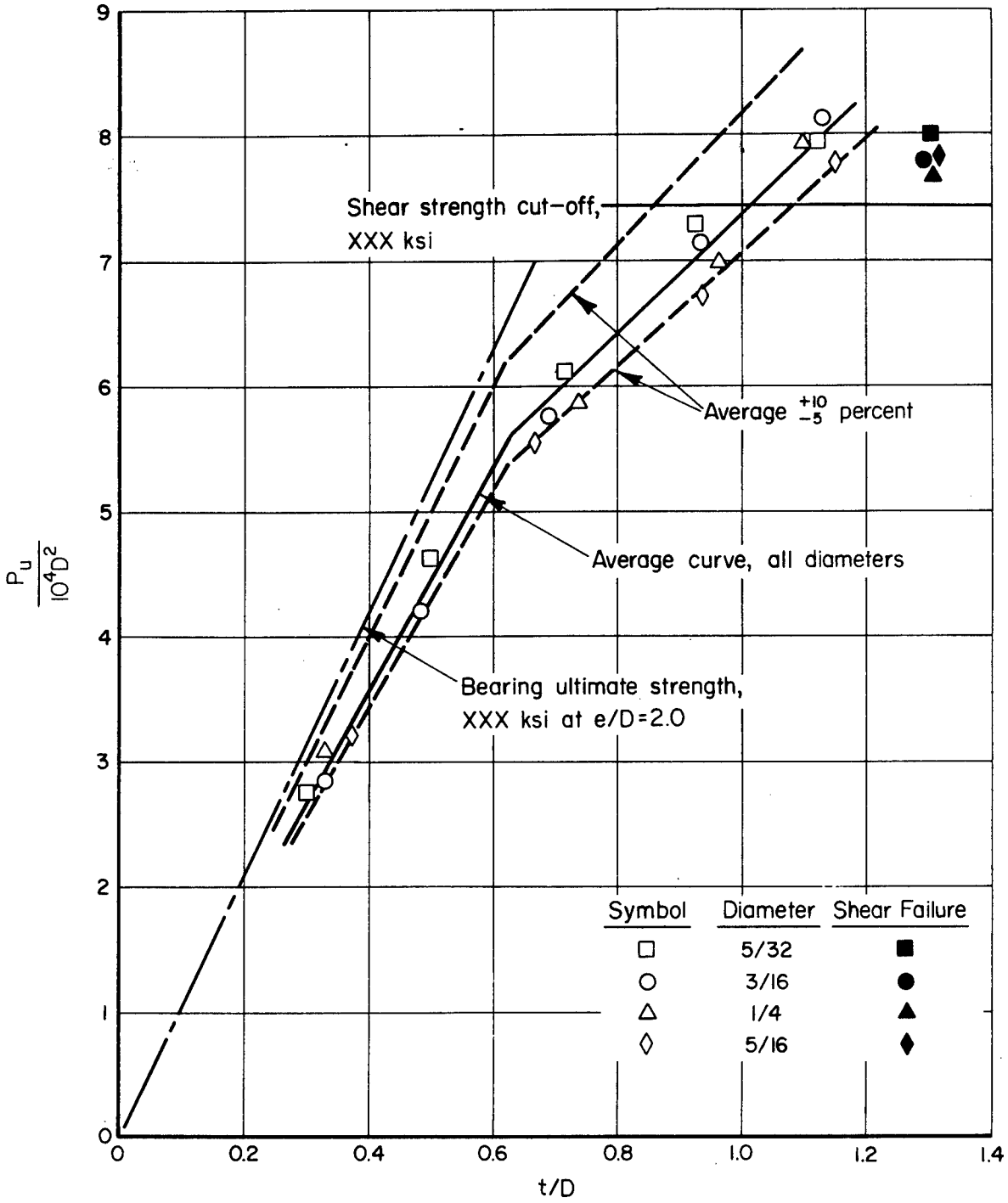


FIGURE 9.4.1.5.2(c). *Average ultimate-load analysis.*

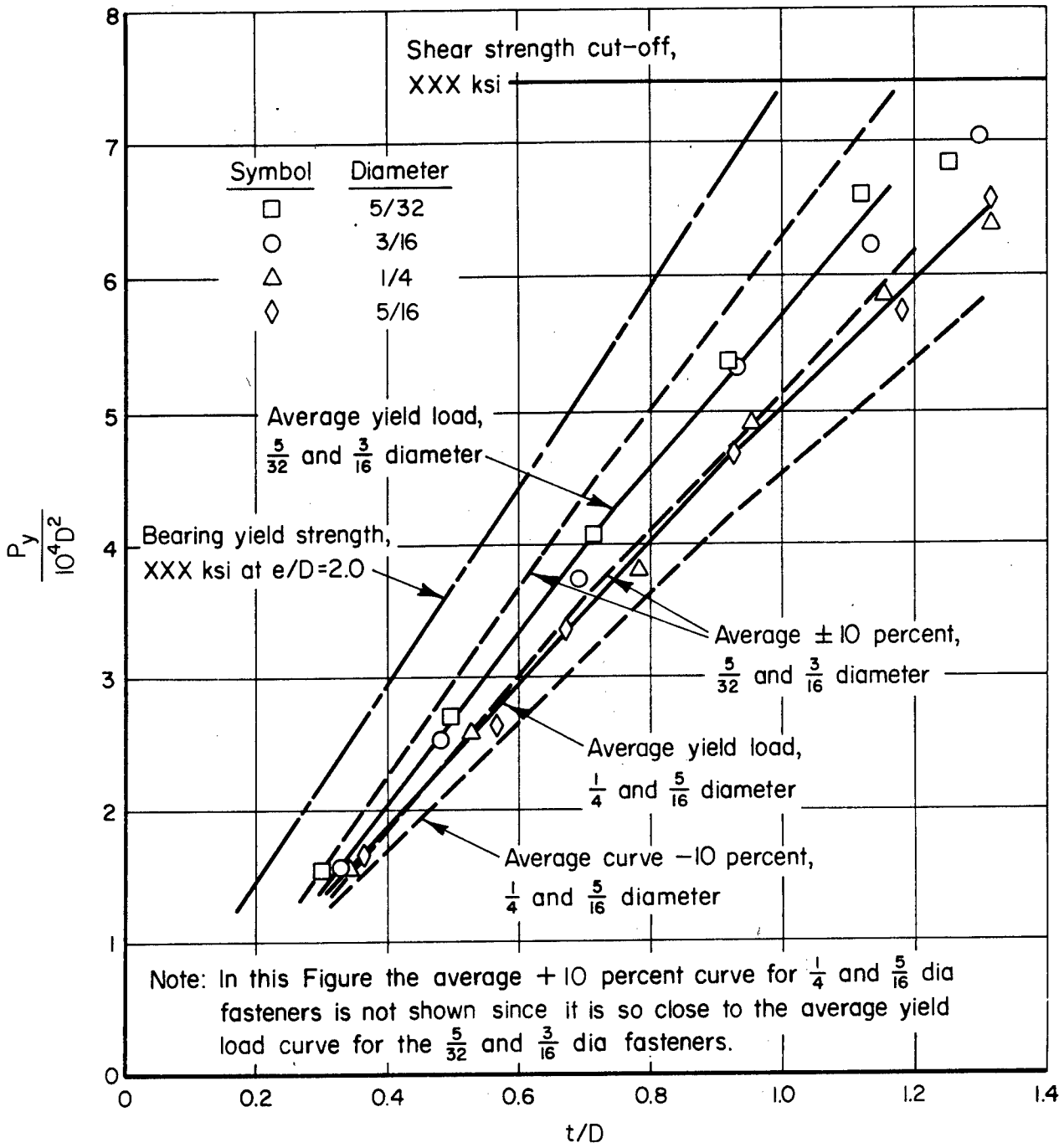


FIGURE 9.4.1.5.2(d). *Average yield-load analysis.*

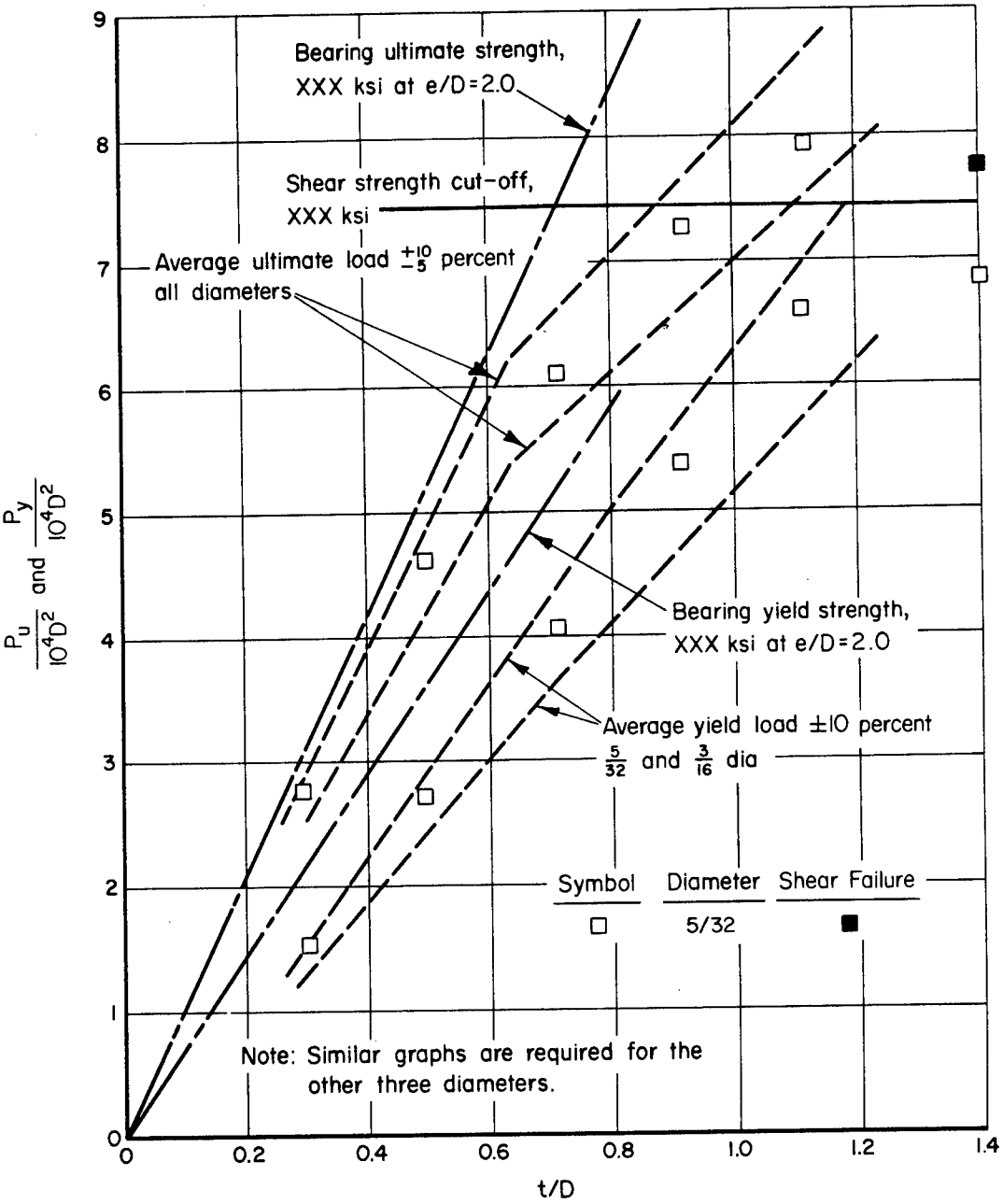


FIGURE 9.4.1.5.2(e). *Average test data for 5/32-diameter fastener.*

In the event that the dispersion pattern of average P_u/D^2 versus t/D (or P_y/D^2 versus t/D) graphs suggest that two adjacent fastener diameters can be grouped to form one average curve and the remaining average curve, this can be done; however, appropriate percentage bands should be indicated on the various graphs.

On graphs containing all of the average P_u/D^2 versus t/D data (or P_y/D^2 versus t/D data), each line should be clearly labeled as to its significance. Also to be shown on these graphs are one or more horizontal lines representing fastener shear strength (more than one line occurs when shear strength in pounds is not proportional to shank area) and allowable sheet or plate ultimate bearing strength and bearing yield strength lines. For materials where bearing properties vary with thickness, bearing strengths plotted shall include the lowest value in the applicable thickness range and the values used shall be the S or A values.

The nonshear-critical test data indicated above will include all data below the fastener shear strength line and all data for joints that failed in sheet bearing, pullout, head failure, combinations of shear, or any other mode of failure, other than shear of fastener shanks, even though same data may lie above the fastener shear strength line. All shear-critical data must be above the fastener shear strength line. The curves shall not extend beyond the tested t/D range.

(c) Graphical Analysis to Determine Ultimate and Yield Load Design Allowable Curves—Three graphs are to be provided for this analysis. The first two graphs contain test data and analysis; the third graph contains final design allowable curves as described below.

On a single graph, plot all P_u/D^2 individual test data for all diameters as a function of t/D, using the same symbols for each diameter as used on the previous graphs. Data from the two sources shall be suitably identified. Draw on the graph the average ultimate load curve, or curves, obtained as described above. Also show the shear cutoff line(s). Construct the tentative design allowable line(s), which is the average curve/1.15. In this construction, the shear cutoff line is not divided by 1.15 since it is the design-allowable curve.

The tentative ultimate-load design-allowable curve(s) is compared with the test data. If the data all lie above the curve(s), the tentative curve is the design allowable curve. If some data lie below the tentative curve(s), they shall be reduced as necessary so that none of the plotted test data points are below the applicable curve. This reduced curve(s) is the ultimate-load design allowable curve, subject to one further possible limitation discussed below. Label all curves with the applicable fastener diameters. See Figure 9.4.1.5.2(f).

On a single graph, plot all of the P_y/D^2 individual test data for all diameters as a function of t/D, using the same symbols for each diameter as used on previous graphs, identifying both test sources. Show on the graph the average yield-load curve(s) obtained as described in Section 9.4.1.5.2(b). This curve(s) is the yield-load allowable design curve(s) and should be with the applicable fastener diameters. See Figure 9.4.1.5.2(g).

The calculations that lead to tabular presentations in MIL-HDBK-5 are based on design allowable curves described above, subject to one further check. That check is provided in a final graph, included in the analysis. The graph, a sample of which is shown in Figure 9.4.1.5.2(h), contains the design-allowable curves for ultimate and yield load, obtained as described above, without the inclusion of plotted data. Also shown on the graph are sheet-bearing ultimate and sheet-bearing yield lines, which are minimum strengths for the thickness range encompassing the data. If these sheet-bearing lines fall partly below the design curves in the sheet-critical t/D range, they become the design curve in those regions.

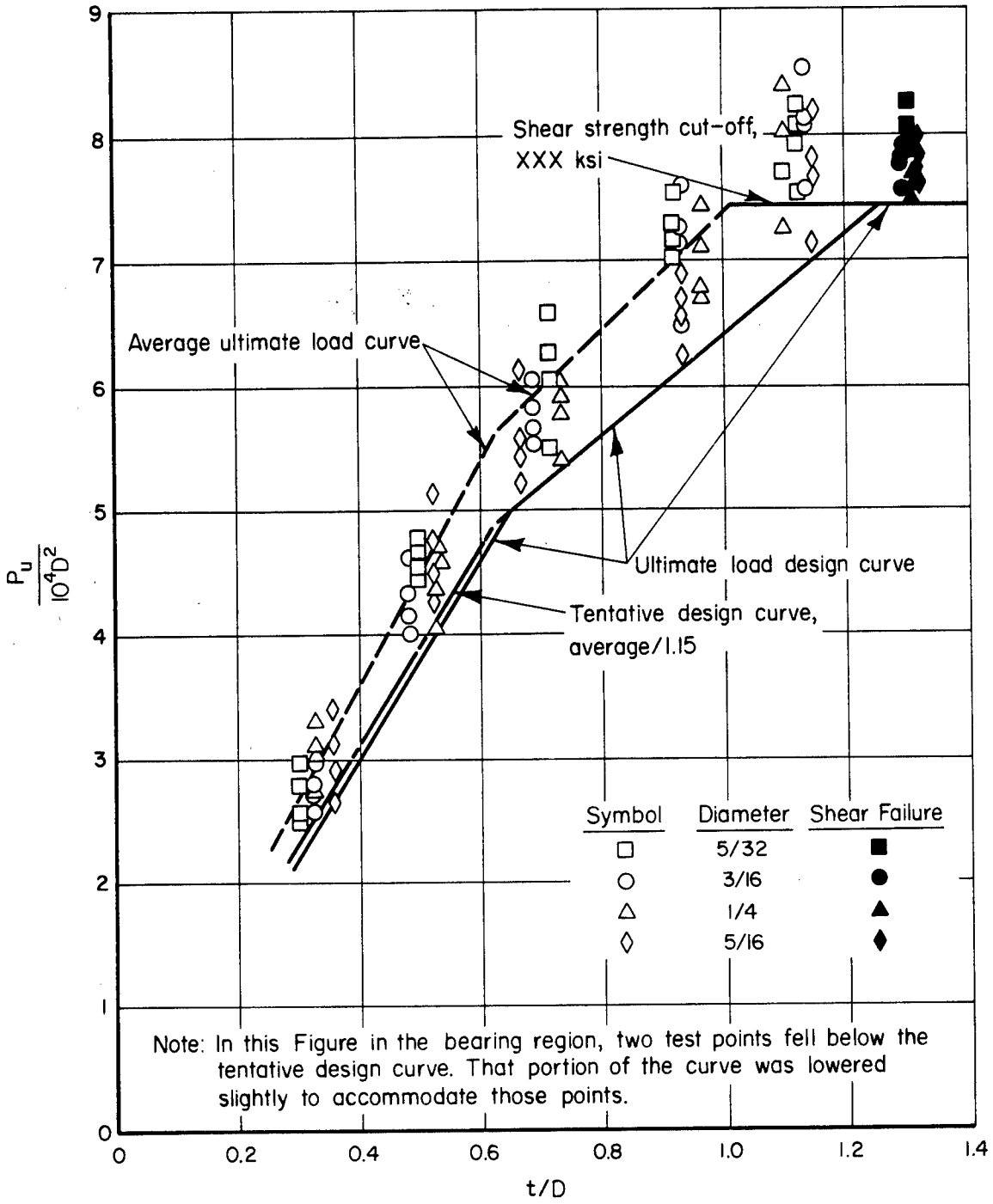


FIGURE 9.4.1.5.2(f). *Establishment of design curve for ultimate load.*

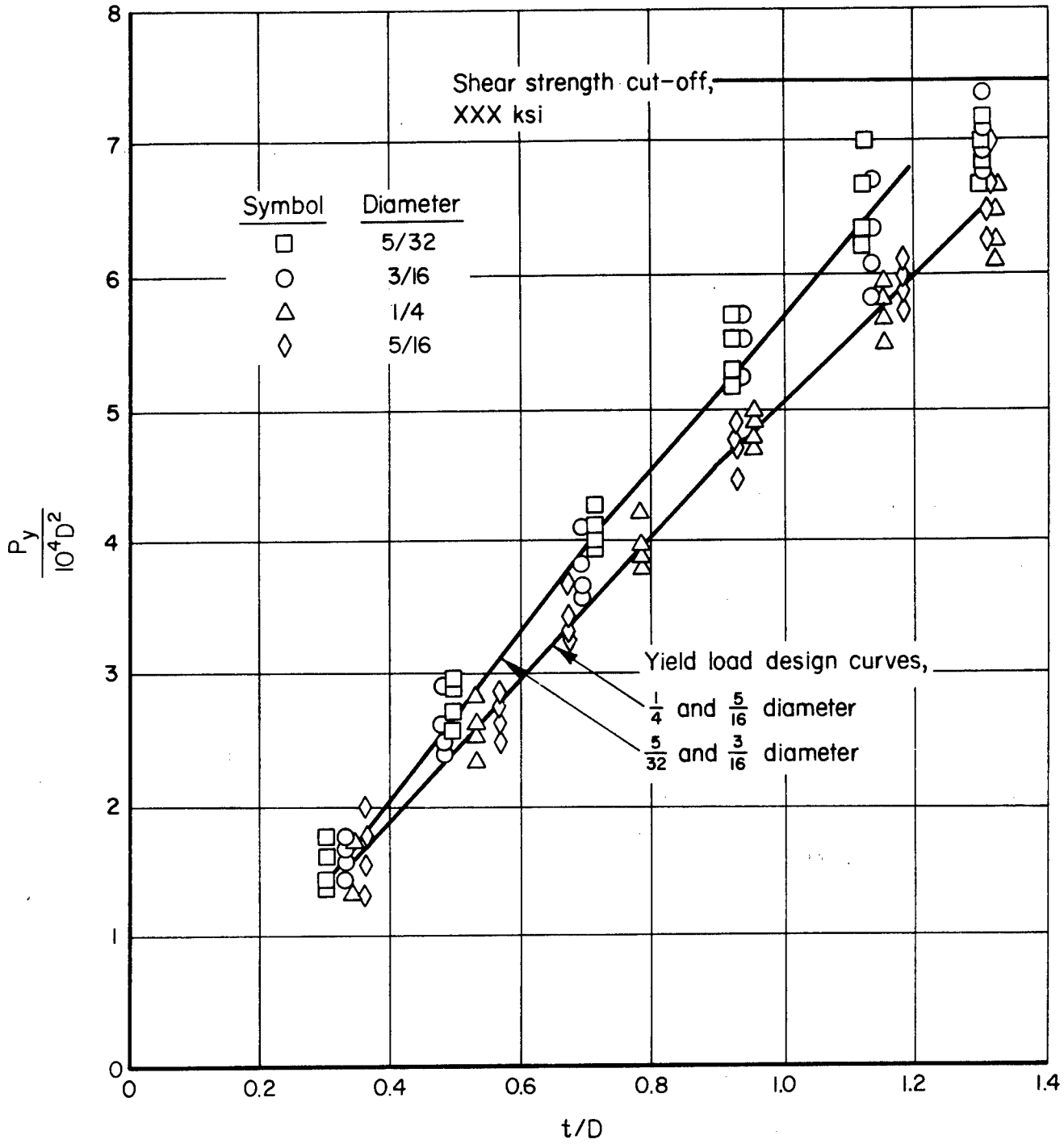


FIGURE 9.4.1.5.2(g). *Establishment of design curve for yield load.*

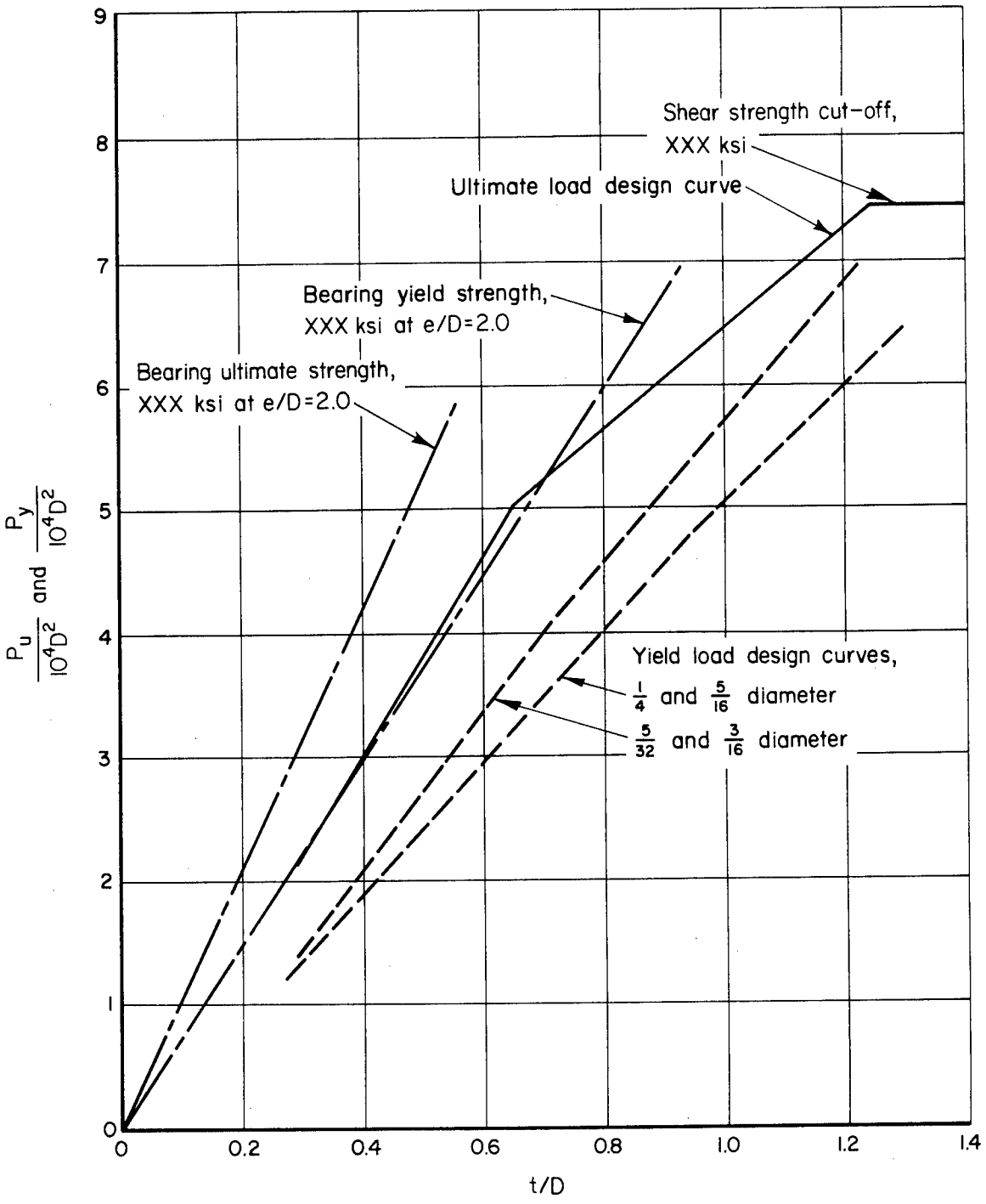


FIGURE 9.4.1.5.2(h). *Relationship bearing strengths of sheet to design curves.*

All curves on this graph are to be clearly labeled. Those segments of the bearing ultimate line, average ultimate load/1.15 curve(s), and shear cutoff that provide the lower bound and, thus, the design-allowable curve, shall be indicated. Similarly, those segments of the bearing yield line and average yield load curve(s) that provide the lower bound and, thus, the design-allowable curve for the yield load shall be indicated.

9.4.1.5.3 *Calculation of Allowable Loads*—On the basis of lower bound curves described above, the allowable ultimate loads and allowable yield loads shall be calculated for each thickness and diameter combination for which allowable yield loads are required. Allowable loads shall not be calculated for thickness/diameter combinations below the t/D range tested, or for diameters not tested.

In these calculations, thickness (per Section 9.4.1.6, Note 11), and diameters to be used shall be the nominal shank diameter (per Section 9.4.1.2) for S-Type fasteners and recommended nominal hole diameters (per Section 9.4.1.2) for H-type fasteners. Figure 9.4.1.5.3 shows a suggested format for this set of calculations.

Computation of Allowables from Design Curves

D	D^2	t	t/D		$P_y/10^4D^2$	P_y	$P_u/10^4D^2$		P_u

D, t, P_u, and P_y, as described in 9.4.1.5.2.

FIGURE 9.4.1.5.3. *Suggested tabular layout for computing allowables from design curves.*

The analysis of joint allowable load data for the case where data are required for procuring or regulatory agency (not for use in MIL-HDBK-5) for a limited range of sheet thickness and fastener diameter is as follows. An analysis similar to that described in Section 9.4.1.5.2 is required for data over the limited t/D range evaluated. In the special case where one sheet thickness and one fastener diameter have been tested in accordance with the requirements of Section 9.4.1.4.4, data shall be analyzed as follows: the ultimate-load calculations shall be made utilizing statistical formulas listed in Section 9.4.1.5.1, where the k value is obtained from Table 9.6.4.1 for the appropriate number of test values (n) and 99 percent probability (A) value at a 95 percent confidence. These ultimate-load values shall be compared with values computed from bearing ultimate strengths of joint material. In each comparison, the lower of either (1) statistical value computed from joint test data, (2) average ultimate load divided by 1.15, (3) computed bearing strength, or (4) fastener shear strength, shall be the ultimate-load design allowable. The yield-load design allowable shall be selected as the lesser of the average yield load or the value computed from the bearing yield strength of the joint material.

The load values so calculated will be rounded to three or four significant figures as follows:

(1) Load values less than 1000 will be rounded to 3 figures (load values less than 100, 2 figures).

(2) Load values greater than 1000 will be rounded to 4 figures. The fourth figure will be a 0 or 5.

9.4.1.6 *Presentation Format*—The final table of allowable loads will be presented in a format suitable for use in MIL-HDBK-5, as illustrated in Figure 9.4.1.6. The following notes apply to the circled numbers in Figure 9.4.1.6.

(1) Omit table number. (Secretariat will assign table number.)

TABLE XXXX(b). *Static Joint Strength of Flush Head 6061-T8 Aluminum Alloy Rivets in Machine-Countersunk Clad Aluminum Alloy Sheet*

Rivet Type	NASXXXX[a] (F_{su} = AAA ksi)				
Sheet Material	Clad 7075-T6				
Rivet Diameter, in.	3/32	1/8	5/32	3/16	1/4
(Nominal Hole Diameter, in.)[b]	(0.096)	(0.1285)	(0.159)	(0.191)	(0.257)
	Ultimate Strength, lbs				
Sheet thickness:					
0.032	182[c]	...	...	...	...
0.040	227	[d] 304	...	...	...
0.050	246	381	[d] 471	...	...
0.063	...	441	594	[d] 714	...
0.071	...	...	670	805	[d] ...
0.080	...	...	675	907	...
0.090	...	...	...	974	1375
0.100	...	...	...	...	1525 [d]
0.125	...	...	...	...	1765
Fastener shear strength[c]	246	441	675	974	1765
	Yield Strength[f], lbs				
Sheet thickness, in.:					
0.032	119	...	...	...	...
0.040	188	224	...	...	...
0.050	246	307	349	...	...
0.063	...	414	481	539	...
0.071	...	...	563	637	...
0.080	...	...	655	748	...
0.090	...	...	...	870	1060
0.100	...	...	...	...	1230
0.125	...	...	...	...	1640
Fastener tensile strength[g], lbs	275	495	755	1090	1975
Head height (ref.), in.	0.039	0.049	0.059	0.070	0.091

[a]Data supplied by ABC Corporation and DEF Company, Confirmatory data provided by XYZ Company.
[b]Fasteners installed in clearance holes (.00XX-.00YY) (Ref. 8.1.X).
[c]Yield value is less than 2/3 of indicated ultimate strength value.
[d]Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity.
[e]Rivet shear strength is documented in NAS XXZZ as AAA ksi.
[f]Permanent set at yield load: 4% of nominal diameter (Ref. 9.4.1.3.3).
[g]System maximum tensile strength as tested in steel fixture.

NOTE: See Section 9.4.1.6 for format recommendations indicated by circled numbers.

FIGURE 9.4.1.6. *Sample format for MIL-HDBK-5 allowable joint strength at 70 F.*

(2) Head type: 100° Flush Head, 100° Flush Shear Head, Protruding Head, Protruding Shear Head, etc. The shear designation is applied to 100° or protruding head fasteners with heads similar in size to those on Hi-Shear rivets, shear-type lock-bolts, shear-head Hi-Lok, Taper-Lok, or similar fasteners.

(3) Fastener material: steel, aluminum alloy, Monel, A286, nickel alloy, etc.

(4) Type of fastener: blind rivet, rivet, bolt, blind bolt, screw, tapered fastener, etc.

(5) Type of hole: machine countersunk or dimpled. (Omit for protruding head fasteners.)

(6) Sheet material: consistent with other MIL-HDBK-5 tables.

(7) "Rivet" for blind or conventional rivets, "Fastener" for other type fasteners.

(8) Add footnote indicator to part numbers and indicate in a footnote the vendor(s) whose part number is shown if the fastener is not covered by an MS or NAS part number. Include fastener shear strength, material temper, and nut or collar identification.

(9) Sheet or plate material and heat treatment or condition.

(10) Nominal fastener diameter. For H-category fasteners, show nominal fractional hole size and, in parentheses, show actual nominal hole size in decimal equivalent. For S-category fasteners, show nominal fractional shank diameter and, in parentheses, show actual fastener shank diameter in decimals [i.e., a 1/8-inch-diameter NAS1740 rivet would be listed as 1/8 (0.144)].

(11) Select standard sheet and plate thickness from the following:

0.008	0.016	0.032	0.063	0.090	0.160	0.312	0.625
0.010	0.020	0.040	0.071	0.100	0.190	0.375	0.750
0.012	0.025	0.050	0.080	0.125	0.250	0.500	0.875

(12) Present design allowable values starting at first sheet thickness below knife-edge condition and continuing through the first value equal to or greater than shear strength value. Allowable loads shall not exceed shear strength. Add footnote indicator to ultimate strength values when yield is less than two-thirds of ultimate loads as indicated in Item (17).

(13) Use the words: "Rivet shear strength" or "Fastener shear strength" conforming to Item (7) nomenclature.

(14) Fastener single-shear allowable loads in pounds.

(15) Present yield strength values for the same thickness and diameters for which ultimate strength values are provided.

(16) For those countersunk head fasteners for which design values are applicable to thin sheet thicknesses, such that the countersink extends into the bottom sheet, a horizontal line shall be drawn in each column of the joint allowables table above the first ultimate strength design value for which the countersink still is contained within the top sheet. For these cases, footnote (f) will be used, as indicated in Item (17).

(17) Add all applicable footnotes from the list of standard notes shown below. All footnotes shall be designated by lower case letters.

(a) "Yield value is less than two-thirds of the indicated ultimate strength value." (Place footnote indicator next to applicable ultimate strength value.)

(b) "These allowables apply to double-dimpled sheets and to the upper sheet dimpled into a machine-countersunk sheet. The thickness of the machine-countersunk sheet must be at least one tabulated gage thicker than the upper dimpled sheet." (Place footnote indicator next to the words "Ultimate Strength, lbs" at the top of the table.)

(c) "Data supplied by ABC Corporation." When applicable add: "Confirmatory data provided by XYZ Company." (Place footnote indicator next to part number.)

(d) "Shear strength based on areas computed from nominal hole diameters or nominal shank diameters, as applicable (indicate Table 8.1.2(a), or list hole diameters), and F_{su} = (indicate shear strength)." Indicate the source of the shear strength (MIL or NAS specifications or data analysis). The footnote indicator is placed next to the words "Fastener shear strength" indicated by Item 13 above. The shear strength shall not be greater than the strength required in the controlling specification or standard.

(e) "Allowables based on nominal hole diameters of (list hole diameters)." This footnote is used when shear strength is controlled by MIL or NAS specifications, and Table 8.1.2(a) hole diameters are not used.

(f) "Values above line are for knife-edge condition and the use of fasteners in this condition is undesirable. The use of knife-edge condition in design of military aircraft requires specific approval of the procuring activity."

(g) "Permanent set at yield load: 4% of nominal diameter (see Section 9.4.1.3.3)."

(h) "Fasteners installed in clearance (or interference) holes." Indicate actual range of fastener-hole fits (interference-clearance) from test program.

(i) "System maximum tensile strength as tested in steel fixture." This footnote is used when table contains fastener tensile strength values. (Place footnote indicator next to the words "Fastener tensile strength, lbs".)

(18) When applicable, add line below yield strength section to present "Fastener tensile strength, lbs". List the appropriate value for each fastener diameter.

(19) For flush head fasteners, add line below yield strength section to present "Head height (ref.), in." List appropriate value for each fastener diameter.

9.4.1.7 *Required Information*

9.4.1.7.1 *Introduction to New Fastener*—When introducing a new fastener for possible inclusion in MIL-HDBK-5, sponsor shall submit a written request (on company letterhead) to Chairman, MIL-HDBK-5 Coordination Activity, providing the following information:

(1) A description of the fastener such as: (a) type of fastener (driven rivet, blind fastener, swaged collar, etc.), (b) fastener material (alloy and temper), (c) unique or new features, (d) nominal sizes and actual diameters, and (e) part drawings and functional description.

(2) Reason for fastener usage or intended usage such as: (a) higher strength, (b) higher or lower temperature capability, (c) improved fatigue performance, and (d) lower installed cost.

(3) Development and use status. (It is not required that the fastener system actually be in use on production airframe structure, but there should be a high level of interest and an intent to use the fastener.) (a) What are current or planned airframe applications? (b) How long has the fastener been produced on a production (nonexperimental) basis? Include preliminary lap joint test data that demonstrates that sufficient diameters and grips are available to conduct a design allowable test program (i.e., data for at least one test for each diameter/grip combination contained in the proposed test plan).

(4) Specification status. Under what type of specification is the fastener covered (MS, NAS, airframe or fastener company standard)?

(5) In what sheet or plate material will the fastener be installed? (The proposed allowables should be for the same or similar sheet or plate material that the sponsor is using or plans to use.)

(6) Shank deformation. Does shank deform during installation? Verification is desirable. (a) If a blind fastener, is it hole filling or nonhole filling? Verification of hole fill is desirable. (b) If a solid shank fastener, are design values to be presented for clearance or interference holes?

(7) Has the sponsor conducted any testing on the fastener system (especially joint allowables) and will the sponsor provide data to the MIL-HDBK-5 Coordination Group?

(8) Has the sponsor reviewed (or will the sponsor review) test program plan, actual testing, analysis of data, and specifications?

9.4.1.7.2 *Final Report*—A report will be submitted to MIL-HDBK-5 Coordination Group summarizing the test program, results, analysis, and suggested table of joint allowables for MIL-HDBK-5. The following information will be provided in the report:

(1) A description of sheet and plate material with heat-treatment details and mechanical property test data for each sheet thickness used in the program in accordance with the requirements of Section 9.4.1.4.5.

(2) A description of fastener, including drawings and specifications. If the fastener is not covered by a government or industry specification, a copy of an appropriate draft specification will be attached to the report.

(3) A statement of compliance with MIL-STD-1312, including a detailed statement of any differences from this standard.

(4) Basic test data [see Figure 9.4.1.5.2(a)], including that required in References 9.4.1.3(a), (b), (c), and representative load deflection curves.

(5) Values for fastener shear calculation: L, x, k, n, and either $\Sigma(x - \bar{x})^2$ or both $[\Sigma\bar{x}^2]$ and $[\Sigma(\bar{x})^2]$ defined in Section 9.4.1.5.1 and fastener shear stress curves, if applicable.

(6) Designation of allowable shear strength reliability (90 or 99 percent value).

(7) Calculated t/D, P_u/D^2, and P_y/D^2 values [see Figure 9.4.1.5.2(a) for sample format].

(8) Seven or more graphs, as required, of P/D^2 versus t/D, as described in detail in Section 9.4.1.5.2, including the proposed design allowable curves for yield and ultimate load.

(9) Calculations of allowable loads (see Figure 9.4.1.5.3 for sample format).

(10) The suggested allowable load tables in the format shown in Section 9.4.1.6.

(11) Failure identification code for failure of each fastener and/or joint is required, as shown in Figure 9.4.1.7.2. If failure is unique or not covered in the figure, so indicate.

(12) Off-set used to obtain yield data.

(13) Draft, in NAS or MA format, of specification for applicable fastener system.

9.4.1.7.3 *Sample Fasteners*—At time of approval of a fastener static joint strength proposal, fastener manufacturer shall submit, to the Chairman, MIL-HDBK-5 Coordination Activity, 10 fasteners each from maximum and minimum diameter and grip size tested in the allowables program. These 40 samples shall be from the same production lots as those used in the test program. Samples shall be packaged suitable for storage with full identification of contents on the container. The information may also include any storage time limitation due to coating or lubricant life.

9.4.2 FUSION-WELDED JOINTS

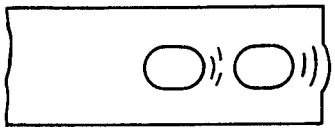
9.4.2.1 *Introduction.*—The purpose of this section of the guidelines is to provide a uniform procedure by which reliable design data on welded joints can be developed for use within the aerospace industry. Unlike most other guidelines procedures, for which reasonably complete concurrence has been found among the users of MIL-HDBK-5, those relating to fusion-welding allowables are still subject to interpretation by users in view of their own welding processes. An additional consideration is that fusion-welding allowables are highly process-dependent. Design values will not be presented in MIL-HDBK-5 since their application will be limited to the process represented by data from which the allowables were derived. Consequently, it is the purpose of these guidelines to describe one of possibly many valid procedures, without excluding other procedures that may be authorized for determination of fusion-welding allowables. Basis for this discussion is presented in Reference 9.4.2.1.

These guidelines generally reflect procedures currently used within the aerospace industry. They are applicable to all types of weldable materials and welding processes. However, recommended test coupon configurations and testing methods described herein have been limited to those used in evaluation of butt-type joints.

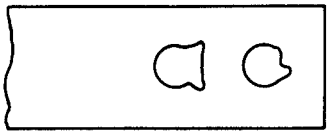
A distinction is made in properties of weldments between those applicable to design and those used for welding development and process control. These guidelines are concerned with those properties applicable to design.

The approach followed establishes coupon-derived design properties for weldments produced under known and defined conditions. Appropriate analysis must be conducted to adapt coupon-derived data to design of the structure being considered. This is accomplished by determining the state of stress for the component joint, and/or by relating structural hardware test results to coupon-derived design properties. This approach is consistent with techniques used to obtain design data for MIL-HDBK-5, as defined in other sections of these guidelines.

1. SHEET FAILURE



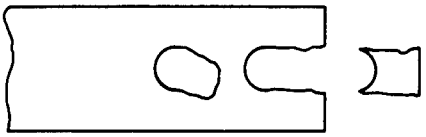
(a) Bearing Deformation of Hole



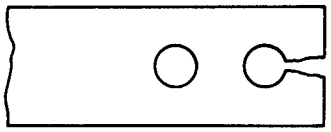
(b) Tearing of Sheet Allowing Fastener Pull-Through, Head Pull-Through or Nut Collar of Formed Head Pull-Through



(c) Tearing of Sheet at Edge Margin

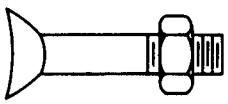


(d) Shear Out of Sheet Through Edge Margin

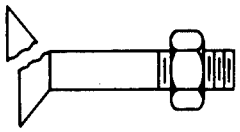


(e) Hoop Tension Failure of Sheet

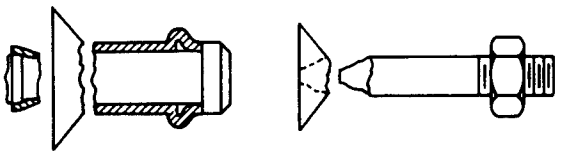
2. FASTENER HEAD FAILURE



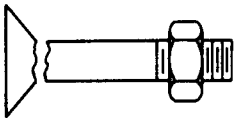
(a) Head Dished in Tension



(b) Partial Shear Failure of Head



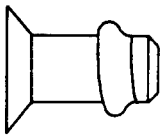
(c) Shear Failure of Head



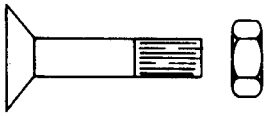
(d) Tensile Failure at Head to Shank Junction

FIGURE 9.4.1.7.2. *Failure identification code.*

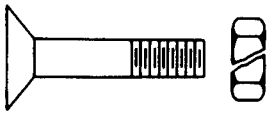
3. FASTENER NUT OR FORMED HEAD FAILURE



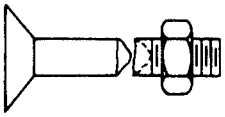
(a) Blind Head Deformed in Tension



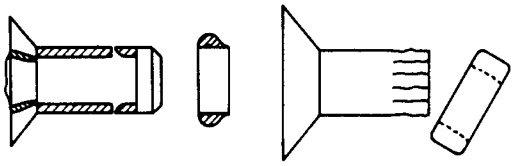
(b) Nut Stripped



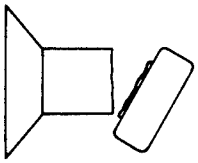
(c) Nut Cracked



(d) Tensile Failure in Threads

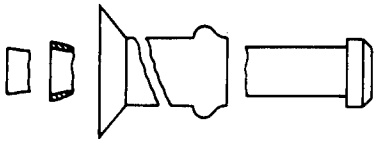


(e) Shear Failure of Blind or Formed Head

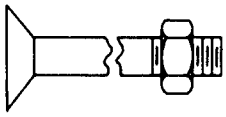


(f) Tension Failure of Formed Head

4. FASTENER SHANK FAILURE

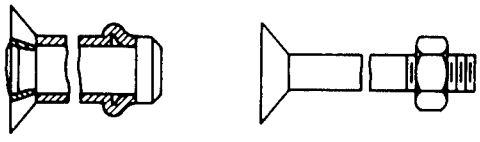


(a) Sleeve or Stem Tensile Failure



(b) Tensile Failure in Shank

5. FASTENER SHANK SHEAR FAILURE



Shear at Midgrip

FIGURE 9.4.1.7.2. *Failure identification code—Continued.*

Current military welding specifications do not contain adequate requirements for defining a meaningful population of weldments. Due to this lack of applicable industry-wide specifications, the necessary specification information must be presented with coupon-derived weldment design data.

Throughout the guidelines and in preparation of data, definitions of the American Welding Society will be used for terms relating to welding. The definitions utilized in MIL-HDBK-5 and in other sections of these guidelines will be used for other terms relating to material properties and statistical treatment of data.

9.4.2.2 *Population Definition*—Determination and presentation of properties of weldments requires adequate definition of pertinent welding parameters, including a description of base materials, welding process variables, and weld character. The most significant variables considered are divided into three basic categories: base materials, welding process variables, and weld character (see Figure 9.4.2.2). Variables listed are the minimum that must be identified and required by the specification.

BASE MATERIAL

Alloy, Composition, Form, Pre- and Post-Weld Heat Treat Condition, Material Thickness, Filler Material

WELDING PROCESS VARIABLES

Joint Preparation	Tooling	Welding Conditions	Weld Repair
Joint Type	Alignment	Welding Process	Number of Repairs
Edge Preparation	Restraint	Welding Method	Type of Repair
Cleaning	Thermal Control	Welding Position	
		Heat Input (Weld Setting)	
		Preheat	
		Interpress Temperature	
		Shielding Gas	

WELD CHARACTER

Inspection Methods	Acceptance Levels
NDT	External
Visual	Underfill and Undercut
Radiographic	Cracks
Magnetic Particle	Pores
Ultrasonic	Reinforcements
DT	Internal
Transverse Tensile Test	Pores
	Inclusions
	Cracks
	Tensile Properties
	Minimum and Minimum Average

FIGURE 9.4.2.2. *Summary of population definition considerations.*

In summary, the primary concern of population definition for weldments is to describe welding conditions in a manner that will assure reproducibility of this same population and will be sufficiently detailed to allow proper data analysis.

9.4.2.2.1 *Base Materials*—Base material variables include appropriate stipulation of alloy, composition form, preweld and postweld heat treat conditions, filler material, and material thickness.

9.4.2.2.2 *Welding Process Variables*—The most difficult aspect is establishing welding variables. The variables must be sufficiently detailed to represent the population of weldments produced, as well as to assure reproducibility of welds within this population. Appropriate selection of variables to be stipulated must be based on an interpretation of their effect on weldment properties and desirability of control. Using the variable of thermal control tooling as an example, it may be found that various types of tooling influence tensile properties of a weld joint by their effect on cooling rate. However, the difficulty in adequately describing thermal-control tooling for more than a single application makes it desirable to treat tooling as a random and uncontrolled variable. This same judgment of effect on properties and desirability of control must be made for each welding process variable.

9.4.2.2.3 *Weld Character*—Appropriate levels of weld character must be prescribed in order to define a population of weldments. This includes a description of internal and external quality levels, as well as minimum joint strength requirements. In most specifications there are several weld classes which identify in detail the quality level requirements. In addition, means of determining weldment characteristics are established by stipulation of both nondestructive and destructive test methods.

9.4.2.3 *Data Generation*—Data generation involves developing a testing program based on considerations of design data requirements, population definition, subpopulation definition, welding procedures, testing procedures, and minimum test data requirements. Data generation is in two parts:

(1) Determination of the properties of weld coupons cut from simple panels welded in accordance with a welding process specification.

(2) Determination of the strength of welded structural components and the relation between the structural component strength and the coupon strength determined in (1).

9.4.2.3.1 *Design Data Requirements (Coupons)*—The type of data required (i.e., tension, shear, fatigue, etc.) and general welding conditions of interest must be established first.

9.4.2.3.2 *Basic Population Definition*—A basic population definition is selected, satisfying the general welding conditions previously established. The procedure for population definition requires a detailed review of applicable welding conditions to select a single population which will provide data consistent with requirements of the specification. The example shown in Figure 9.4.2.3.2 for 6061 aluminum weldments is typical of a basic population definition. In this example, tooling and heat input have not been specified.

9.4.2.3.3 *Subpopulation Definition*—Appropriate subpopulations must be selected. Obvious subpopulations or associated populations in Figure 9.4.2.3.2 would be alternative weld/heat treating sequences, filler materials, welding processes, weld repair, joint thickness, and weld classes (quality level). Selection of these preplanned subpopulations is dependent upon previous knowledge of their potential effect on weldment properties. However, those mentioned are most frequently encountered subpopulations required.

9.4.2.3.4 *Welding Procedure*—The variables defining the selected basic and subpopulations must be controlled within (but no better than) their prescribed ranges during test program welding. This requires

BASE MATERIAL

Alloy: 6061 Aluminum per QQ-A-250/11
Form: Sheet
Preweld Heat Treat Condition: T4 or T6
Postweld Heat Treat Condition: As-Welded
Material Thickness: 0.09 inch
Filler Material: 4043 per QQ-B-655

WELDING VARIABLES

Joint Preparation
- Joint Type: Butt
- Edge Preparation: Square Groove
- Cleaning: Deoxidize, solvent wipe and hand scrape

Tooling: None Specified
Welding Conditions
- Process: Mechanized GTA

Sequence: Single Pass
Position: Flat
Heat Input: Not Specified
Weld Repair: None

WELDMENT QUALITY

Inspection Methods
- Visual
- Radiographic, Mil-Std-453
- Penetrant, Mil-I-6866

Acceptance Levels
- External
  - Weld Beads: Removed Flush
  - Underfill and Undercut: None Allowed
  - Cracks: None Allowed
  - Pores: *Maximum size 0.02-inch, one per inch
  - Mismatch: 10% of Thickness Maximum
- Internal
  - Pores and Inclusions: *Maximum Size 50% T or 0.12 inch whichever is lesser. Maximum accumulated amount less than 2% of cross section area.

*Sharp-tailed or crack-like indications not allowed, appropriate acceptance levels will be added.

FIGURE 9.4.2.3.2. *Example population definition.*

welding in accordance with a referenced specification and any additional requirements which may limit the population. The generation of data requires that welding be conducted under production conditions rather than closely controlled laboratory conditions. Data for development of design properties must realistically represent the variation allowed in referenced specification and/or supplemental requirements for each variable.

Weldments from which data are generated should represent the product of several welders, welding machines, and weld setups. It is advisable to select test samples from weldments produced at different times by different operators guided only by specified requirements.

9.4.2.3.5 *Coupon Preparation*—Two types of transverse-weld tensile coupon configurations are recommended. Use flat coupons for materials up to 0.5-inch thickness. For weld joint thicknesses greater than 0.5-inch, round coupons are recommended. These two configurations are shown in Figure 9.4.2.3.5(a) and (b), respectively. Exact specimen dimensions are dependent on thickness of the weldment being evaluated, but geometric similitude is maintained within each type of specimen. Appropriate dimensions are given for the reduced test section of each coupon. The dimensions of gripping areas at each end are optional and may be modified to accommodate standard test fixtures.

Remove the weld heads from all flat coupons unless standards have been established regarding weld reinforcement configuration. When data are required for welds with reinforcements intact, their configurations must be specified. When round coupons are used in thick weldments, location within the weldment becomes an additional variable which must be described and associated with data.

At present, coupon configuration requirements for evaluation of properties other than transverse tensile have not been sufficiently defined to be utilized on an industry-wide basis. Due to the nature of fatigue testing, no specific test configurations are recommended. Configurations selected according to standard base metal practices have been used and may be satisfactory. Weld reinforcements are of particular significance in fatigue testing, and should be removed or specified in detail, together with a description of the coupon used.

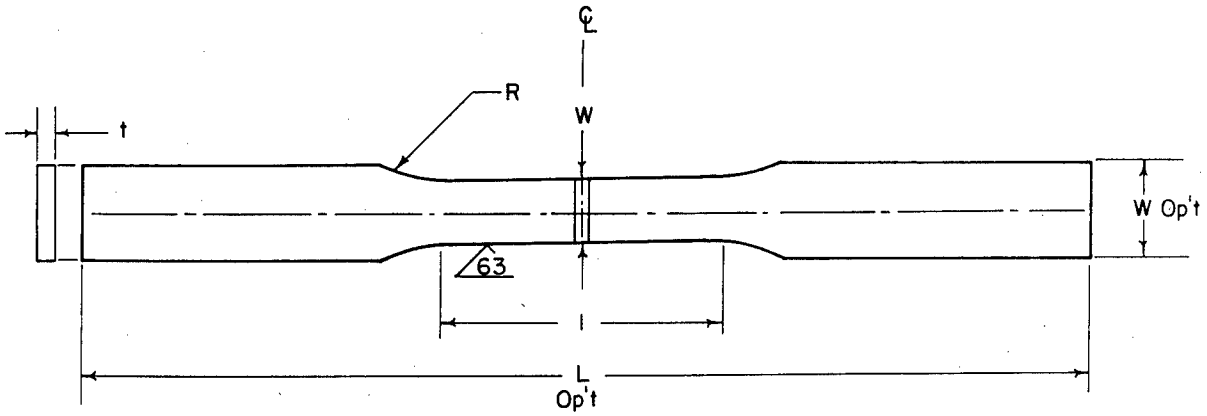
Fracture toughness coupons should conform to the latest requirements defined by ASTM E399, Reference 9.5.1.4.1. Crack location with respect to weldment is of particular importance, and the criteria for validity of specimen must be met. Coupons used for evaluation of other weldment properties, such as fillet-weld shear strength and creep or stress rupture, also require definition in order to be used for design strengths.

9.4.2.3.6 *Testing Procedures*—Availability of accepted test methods for base metal evaluation, as evidence by federal and ASTM standards, has resulted in their general application to testing of weldments. These standards control test equipment, data accuracy, and loading rates. Reference to existing base metal test methods are generally considered satisfactory for mechanical property testing of weldments except for configuration definition. The testing practice and any deviations should be reported when data samples are generated. In no case may a test result be discarded on the basis of a defect found after final inspection—for example, during post-test examination of fractured surfaces.

9.4.2.3.7 *Minimum Data Requirements*—The data sample must be adequate to determine form and distribution of the population from which it was drawn. If the weldment population definition is broad and allows considerable latitude in the range of parameters defined, it is obvious that larger sample sizes will be required. Certain minimum requirements can be stated, however, based on statistical considerations.

For data to be directly analyzed on a statistical basis, a typical weldment population exhibiting nearly normal distribution characteristics should be represented by a sample containing a minimum of 50 random observations. These observations should include at least 10 subsamples representing random variables such as base material lots, filler material lots, weld processing variables, and weld machine operators and setups.

Direct analysis of a data sample not normally distributed requires at least 300 observations to established a minimum value on an A-basis. A B-value may be established from the smaller sample defined above. As in the previous case, the observations should be representative of the total population.

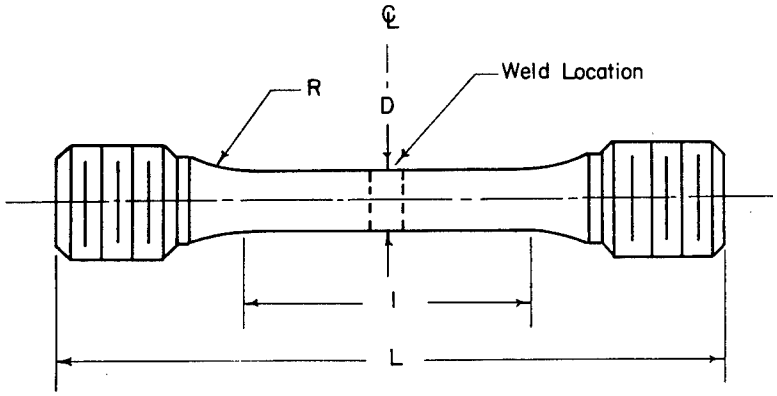


t	w	l	R
< .188	0.5	2.25	1 min.
0.188 to 0.25	0.75	3.0	1.5 min.
0.25 to 0.5	1.0	4.0	2 min.

NOTES:

1. Dimension "W" and "L" optional.
2. Weld bead on or off optional
3. Fillet radii must fair smoothly into reduced section.
4. Material and grain direction per test requirements.
5. Specimens warped from welding or heat treatment shall not be straightened.
6. Reduced section machined surfaces 63
7. The reduced section and grip ends must be symmetrical about the longitudinal ℄ within ± 0.01.
8. Tolerances except otherwise noted: Linear ± 0.03, Angular ± 1°.

FIGURE 9.4.2.3.5(a). *Flat transverse-weld tensile coupon.*



D	l	R
0.250	1.25	0.250
0.505	2.0	0.50

Notes:

1. Dimension "L" and thread size optional.
2. Fillet radii must fair smoothly into reduced section
3. Reduced section machined surface 32
4. Heat treatment to be performed prior to finish machining.
5. The reduced section and grip ends must be symmetrical about the longitudinal ℄ within ±0.01.
6. Tolerances except otherwise noted: Linear ± 0.03, Angular ±1°

FIGURE 9.4.2.3.5(b). *Round transverse-weld tensile coupon.*

At least 10 pairs of measurements should be used for indirect analysis based on derived ratios. These paired observations should represent a range of variables in the specified population. If broad ranges in parameters are involved, additional observations may be required.

9.4.2.3.8 *Sample Requirements*—Due to the number of variables inherent in a welding process, it is advisable to make as broad a sampling as practicable within the population definition. The range of material and processing parameters included in the sample will obviously influence sample size. The total number of observations should be sufficient to identify factors that may be significant within the population, such as joint thickness, weld repair, filler material, and heat-treat condition.

9.4.2.4 *Data Analysis*—Certain concepts have been used for base-metal analyses which lend themselves to analysis techniques for weldments. The procedures described in other sections of the guidelines are used as a basis for analysis of mechanical property data for weldments in order to obtain A-and B-values. The procedures involve either direct statistical analysis of weldment data when sufficient data exist, or an indirect statistical analysis of ratios of paired properties.

The data samples required for direct statistical analysis will usually limit its use to tensile ultimate strength of weldment coupons. The indirect analysis may be used to derive other properties of interest using smaller samples. One example is to derive the minimum shear strength for the cases where only tensile distribution is known; one would operate on the ratio SUS/TUS in this case.

The indirect computation method also provides a tool for rational development of weld factors to be used in translating coupon-derived minimum properties to hardware design. In this case, ratio of hardware failure stress to control coupon failure stress is used.

9.4.2.5 *Data Presentation*—A minimum number of welding conditions should be shown in the data presentation for each basic population of weldments considered. These would include conditions of major significance to potential users of the data. In the population definition discussion, many potential welding variables were discussed. Among these variables, the following variables are the minimum that should always be specified where applicable:

(1) Alloys

(2) Weld-heat-treat conditions

(3) Filler materials

(4) Welding processes

(5) Weld repairs

(6) Joint thicknesses

(7) Joint types

(8) Weld quality levels

(9) Welding methods, i.e., manual or mechanized.

Since data presented are based on coupon-derived results, it is also necessary to provide comments on use of data in structural design.

9.4.2.5.1 *Additional Information*—When weldment data are presented, they should include comments to aid designers in selecting appropriate welding processes or conditions. In addition, comments alerting a designer to possible fabrication problems or environmental effects should be included. These may include:

(1) Potential weld heat-treating sequences for the alloy

(2) Applicable welding methods

(3) Comments on weldment properties

(4) Discussion of pertinent welding process variables, such as heat input sensitivity or restrictions, preheat requirements, atmospheric contamination, and significant metallurgical phenomena.

9.4.2.5.2 *Room-Temperature Properties*—Data on room-temperature properties of weldments are presented in tabular form illustrated in Figure 9.4.2.5.2. The figure describes base material, welding variables, and weld character conditions that the data represent, as well as properties of interest. Precautionary notes for use of data in design are presented in footnotes and are discussed in Section 9.4.2.5.4.

9.4.2.5.3 *Data on Effect of Temperature*—A typical effect-of-temperature curve of weldment properties is shown in Figure 9.4.2.5.3. This type of curve should be presented in conjunction with room-temperature properties, referencing welding conditions and precautionary notes of the room-temperature case.

9.4.2.5.4 *Use of Design Data*—In footnotes to coupon-derived design data, it is necessary to present precautionary notes on the use of data in structural design. It is recognized that structures may not fail under load in the same manner as a coupon. This lack of one-to-one correlation may be due to differences either in weldment character resulting from potentially higher variability of production welding, or state of stress. Coupon-structure ratios are used to account for these differences.

The coupon-derived basic weld allowable accounts for a sizeable portion of the variability in welded joints; coupon-structure ratio accounts for the remainder. Since the state of stress (and to some extent, distribution of stress) is accounted for in the coupon-structure ratio, it is probable that each general structural configuration will have a unique coupon-structure ratio. For example, the coupon-structure ratio for a tank which must resist internal pressure would be different from the ratio for a welded joint in a sandwich panel.

Material	Material Thickness	Weld Joint Type	Filler Wire Alloy	Heat Treat After Welding	Properties [1] F_{tu} [2] A	F_{tu} [2] B	F_{tu} [3] A	F_{tu} [3] B	Other Properties or → → Welding Conditions
6061-T4	Up to 0.30 Above 0.30	Sq. Butt Groove	4043 4043	Aged to T6					
6061-T4 6061-T6	Up to 0.30 Above 0.30	Sq. Butt Groove	4043 4043	As-Welded					
6061-F	Up to 0.30 Above 0.30	Sq. Butt Groove	4043 4043	Sol. Ht and Age to T6					

[1] These coupon-derived properties are subject to the usage limitations discussed under "Use of Design Data."

[2] For the following welding conditions ----------

[3] For the following welding conditions ---------

FIGURE 9.4.2.5.2. *Typical format for presentation of room-temperature properties of weldments.*

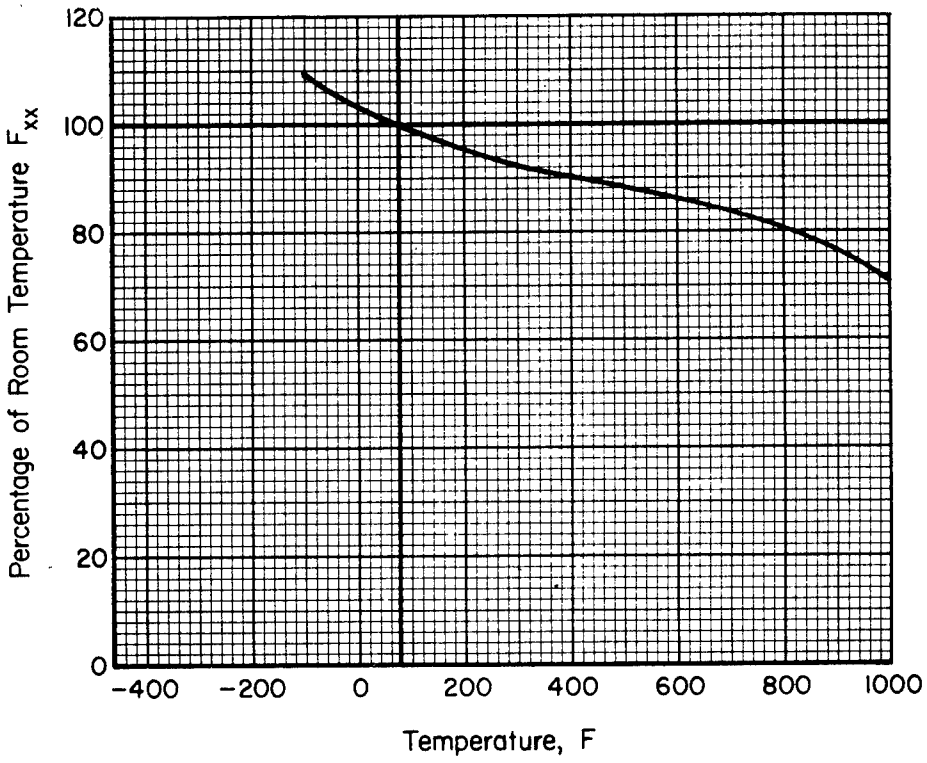


FIGURE 9.4.2.5.3. *Typical effect of temperature presentation.*

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9.5 Miscellaneous Properties

9.5.1 FRACTURE TOUGHNESS

9.5.1.1 *Introduction.*—Fracture toughness of a material is its ability to resist flaw propagation and fracture. This characteristic is a generic quality, somewhat elusive to assess quantitatively. Of several measures of fracture toughness which have evolved for appraising the sensitivity of metals to the presence of small flaws, those based on crack stress or strain analysis appear to be more meaningful for use in design applications. Significant quantification of fracture and flaw propagation behavior of high-strength metals has been achieved through the concept of stress intensity factors. Typical room-temperature values and effect-of-temperature curves for critical stress intensity factors are presented in MIL-HDBK-5 for "information only" where data are available. Basic concepts, testing considerations, and interpretations of fracture toughness are briefly described in the following subsections.

9.5.1.2 *Nomenclature*—The following definitions are provided for discussion of fracture toughness:

Plane Strain—The stress state in which all strains occur only in the principal loading plane. No strains occur out of the plane, i.e., $\varepsilon_z = 0$, and $\sigma_z \neq 0$.

Plane Stress—The stress state in which all stresses occur only in the principal loading plane. No stresses occur out of the plane, i.e., $\sigma_z = 0$, and $\varepsilon_z \neq 0$.

Stress Intensity Factor—A physical quantity describing the severity of a flaw in the stress field of a loaded structural element. The gross stress in the material and flaw size are characterized parametrically by the stress intensity factor,

$$K = f\sqrt{a}\ Y,\ \text{ksi} - \text{in.}^{1/2} \qquad [9.5.1.2]$$

where

f = stress applied to the gross section including the flaw, ksi

a = measure of flaw size, inches

Y = factor relating component geometry and flaw size, non-dimensional. See Reference 1.4.12.2.1(a) for values.

Roman numeral subscripts I, II, and III on K are utilized to denote opening, sliding, and tearing modes, respectively, of flaw enlargement. Mode I has been evaluated almost exclusively in current data generation programs.

Critical Stress Intensity Factor—A limiting value of the stress intensity factor beyond which continued flaw propagation and/or fracture may be expected. This value is dependent on material and may vary with type of loading and conditions of use.

Plane-Strain Fracture Toughness—A generic term now generally adopted for the critical plane-strain stress intensity factor characteristic of plane-strain fracture, symbolically denoted K_{Ic}. This is because in current fracture testing practices, specification of the slowly increasing load test of specimen materials in the plane-strain stress state and in opening mode (I) has been dominant.

Plane-Stress and Transitional Fracture Toughness—A generic term denoting the critical stress intensity factor associated with fracture behavior under nonplane-strain conditions. Because of plasticity effects

and stable crack growth which can be encountered prior to fracture under these conditions, designation of a specific value is dependent on the stage of crack growth detected during testing. Residual strength or apparent fracture toughness is a special case of plane-stress and transitional fracture toughness wherein the reference crack length is the initial pre-existing crack length and subsequent crack growth during the test is neglected.

9.5.1.3 *Significance of Stress State*—A primary factor in fracture behavior of a material is stress state, i.e., plane-stress or plane-strain. In accord with previous definitions, these stress states may be interpreted mechanically as a size or thickness effect within the material. The ideal plane-stress condition occurs in the two-dimensional ($\sigma_z = 0$) case, in which all stresses are restricted to one plane. Material can accommodate extensive plastic deformation adjacent to the flaw prior to fracture, and at fracture exhibit a relatively high K value, as computed by a relationship such as Equation 9.5.1.2. At the opposite extreme is the ideal plane-strain case, in which the third dimension is of infinite extent so that bulk restraint of the material permits no out-of-plane strains. As a result, plastic deformation is restricted and the material fractures in a nearly elastic manner at a relatively low K value. In real materials, these ideal extremes can be closely approximated by "quasi" conditions of "thin" and "thick" bodies. Variation in stress intensity at fracture over these extremes, and the transition stage between, may be represented as in Figure 9.5.1.3.

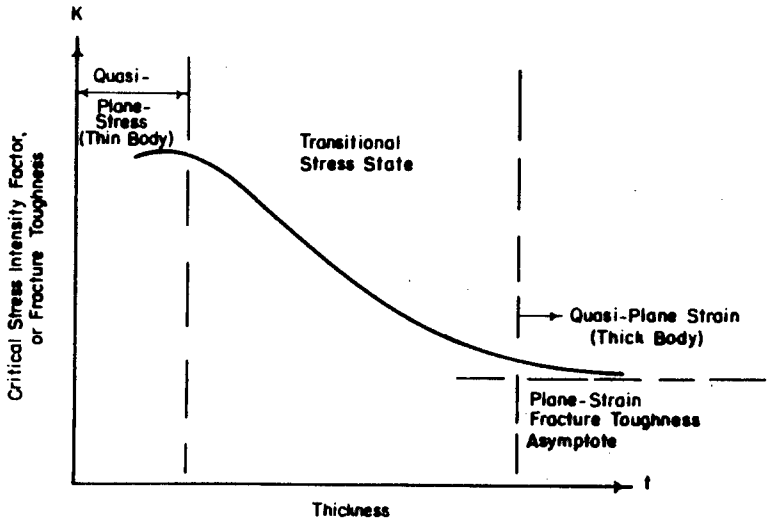


FIGURE 9.5.1.3. *Variation of fracture toughness with thickness or stress state (size effect).*

9.5.1.4 *Plane-Strain Fracture Toughness*—For materials which are inherently brittle, or for structure and flaw configurations which are in triaxial tension due to their thickness or bulk restraint, quasi-plane-strain-stress conditions can be obtained in a finite-sized structural element. Triaxial stress state implicit to plane strain effectively embrittles the material by providing maximum restraint against plastic deformation. In this condition, component behavior is essentially elastic until fracture stress is reached and is

readily amenable to analysis in terms of elastic fracture mechanics. This mode of fracture is frequently characteristic of the very high strength metals.

9.5.1.4.1 *Data Generation and Interpretation*—While a wide variety of fracture specimens are available for specified testing objectives, the notch-bend specimen and compact specimen generally offer the greatest convenience and material economics for testing. Details of recommended testing practice are presented in Reference 9.5.1.4.1.

9.5.1.4.2 *Data Presentation*—Room temperature values of K_{Ic} are tabulated in the introductory comments for each chapter. This table shall include the range (minimum, average, and maximum) in K_{Ic} values, alloy, product form, heat treat condition, TYS range, product thickness, number of test specimens, number of lots, test specimen thickness range, and grain direction represented by data. Where data are available, effect of temperature on K_{Ic} is presented graphically in the appropriate alloy section. It is preferable that data incorporated in MIL-HDBK-5 represent a minimum of three specimens each from a minimum of five lots of material for each test direction.

9.5.1.5 *Plane-Stress and Transitional-Fracture Toughness*—In ductile materials and relatively thin structural elements, stress state may approach plane-stress conditions. As a result, cracktip plasticity and stable-crack growth may be expected in cracked structural components under load prior to reaching a critical stress-intensity factor value. Furthermore, due to the interaction of plasticity and geometry, characteristic fracture toughness of a material may vary with the stress state, as illustrated in Figure 9.5.1.3.

It is convenient to consider critical stress-intensity factor values, varying with thickness or stress state, as indices of crack-damage resistance. The stress-intensity factor can be used as a consistent measure of crack damage, not only for fracture instability, but also for other levels of crack damage severity, provided the damage is consistently specified and detected. This concept implies that plane-stress and transitional-fracture toughness of metallic materials, while not necessarily a fixed value for the material, is a characteristic value for a given product form, thickness, grain direction, temperature, and strain rate.

9.5.1.5.1 *Data Generation and Interpretation*—Because of the complexity of crack behavior in plane-stress and transitional-stress states, test methods for evaluating material toughness have not been completely standardized; however, several useful methods do exist. Although each configuration generates nearly consistent results when data are properly evaluated, it is recommended that each general flaw configuration be interpreted and applied within its own design context.

Center-Through-Cracked Tension Panels—Because it simulates typical crack conditions in thin-sheet structures, the center-through cracked tension panel is a popular testing configuration for evaluating crack behavior. This specimen is illustrated in Figure 9.5.1.5.1(a).

The crack-tip plasticity and slow-stable growth of the crack which are attendant to plane-stress or transitional stress state conditions may cause a deviation from abrupt fracture which is normally associated with crack extension under ideal plane conditions, as illustrated in Figure 9.5.1.5.1(b).

Two limiting damage levels are noted in this figure. Point O is the threshold or onset of slow, stable tear where the crack slowly extends after reaching a threshold stress level. Point C is fracture instability. Both levels of crack damage can be associated with a different stress intensity factor, or damage index, for product forms and thicknesses of interest. These damage levels can be identified either directly with the K value as determined from instantaneous stress-crack length coordinate dimensions at these points, or approximately by the coordinates of Point A, which is residual strength, or apparent toughness concept of relating initial crack length to final fracture stress.

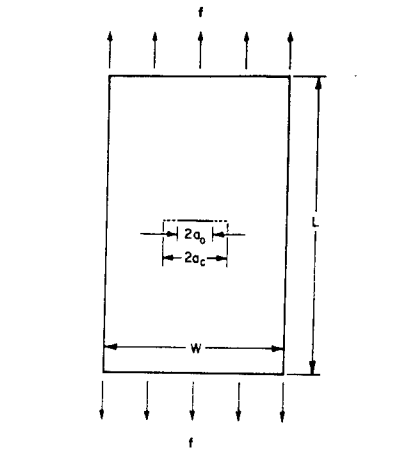


FIGURE 9.5.1.5.1(a). *Center through-cracked tension panel.*

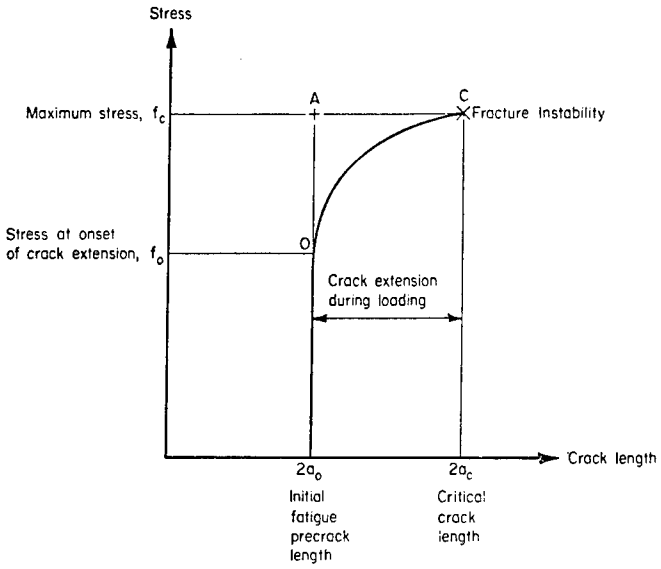


FIGURE 9.5.1.5.1(b). *Crack growth curve.*

The stress intensity factor, K, associated with any of these damage levels is determined from Expression 9.5.1.2 where, for this configuration,

a = half-length of center-through crack

$Y = (\pi \sec \pi a/W)^{1/2}$.

The locus of data points can be represented by a parametric stress-intensity factor curve, as shown in Figure 9.5.1.5.1(c), where each curve represents a different stress-intensity factor formulation. The slow growth curve is superimposed on this figure to illustrate the general relationship between the threshold of stable crack extension, apparent instability, and fracture instability for a typical crack.

Because of experimental difficulties associated with precise detection of threshold and instability points, points O and C, apparent toughness, or residual strength concept of crack damage is used in this presentation. This is the locus of data points "A", noted in Figure 9.5.1.5.1(b), which determine apparent fracture toughness.

$$K_{app} = f_c(\pi a_o \sec \pi a_o/W)^{\frac{1}{2}} \qquad [9.5.1.5.1]$$

See Reference 9.5.1.5.2 for additional information.

9.5.1.5.2 *Criteria for Calculating Apparent Toughness*—Since precise definitions of damage mechanisms and their associated instability conditions have not been devised for crack behavior in plane-stress and transitional stress states, only general constraints can be suggested for screening data. To assure that crack damage or fracture instability occurs under predominantly linear elastic conditions the basic criterion is that net section stress must be less than 80 percent of tensile yield strength, TYS, actually represen-

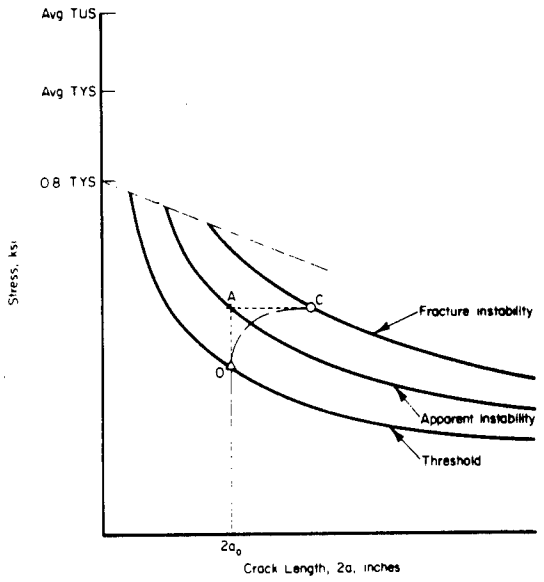


FIGURE 9.5.1.5.1(c). *Stress intensity factor curves as parametric indices of crack damage.*

tative of that material. Additional criteria may be imposed by stress and boundary constraints characteristic to specific specimen configurations.

Center-Through-Cracked Tension Panels—To maintain consistency with the Damage Tolerant Design Handbook, a related strength of materials document for Air Force contractors, a singular criterion,

$$f_c \leq 0.8\ (TYS)\ (1 - 2a/W) \qquad [9.5.1.5.2]$$

corresponding to the above net section stress requirement, is imposed on fracture data from center-cracked tension panels. Data which satisfy this criterion are used with Expression 9.5.1.5.1 to define apparent fracture toughness.

The validity of elastic fracture in a given set of data may also be substantiated by additional tests conducted to demonstrate that elastic fracture conditions have been achieved and that the associated K value is nearly constant. For example, once a tentative value of K_{app} has been determined, it can be confirmed by testing additional panels of larger width (at least 50 percent larger) with the same initial crack length, or by testing the same panel width containing a smaller initial crack length (approximately two-thirds of the previous). These additional K_{app} values must confirm to the original tentative value. In any case, it is recommended that tests can be conducted at a variety of crack lengths and panel widths whenever practical to obtain a more complete characterization of panel behavior.

9.5.1.5.3 *Data Presentation*—Plane stress and transitional fracture toughness data and other crack damage information are presented in each alloy chapter. Data are categorized by product form, grain direction, thickness (or thickness range), temperature, and strain rate. The presentation format is dependent upon the flaw and structural configuration as described in the following paragraphs.

Center-Through-Cracked Tension Panel Data—Apparent fracture instability data for center-through-cracked tension panels are presented on the graphical format of maximum gross stress

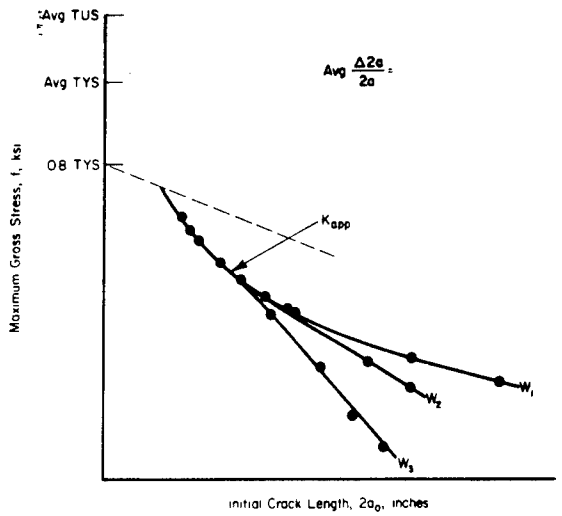


FIGURE 9.5.1.5.3. *Format for the presentation of center-cracked tension panel data.*

versus initial crack length as illustrated in Figure 9.5.1.5.3. These data plots are presented as information and not as design allowables; hence, additional testing is necessary to substantiate design allowables over the range of crack lengths of interest.

The data in such graphical display satisfy the screening criterion of Expression 9.5.1.5.2.

The apparent stability fracture toughness value K_{app} associated with each curve is a simple average of test values determined according to Expression 9.5.1.5.1.

The average apparent toughness curve is presented over a range extending from the short crack length associated with a net section stress of 80 percent of tensile yield strength to either the largest crack length contained in the data, or one-third the panel width, whichever is greater.

Since slow, stable tear may occur during the loading of a cracked panel, an approximate measure of crack extension possible prior to fracture is useful to assess conditions of fracture instability. Where data are available, the average ratio, Δ (2a)/($2a_o$,) of crack extension prior to fracture to initial crack length is indicated in the field of the graphical display. This ratio is determined through

$$\frac{\Delta 2a}{2a_o} = \frac{2a_c - 2a_o}{2a_o} = \frac{a_c}{a_o} - 1 = \left(\frac{K_c^2}{K_{app}}\right) - 1 \quad ,$$

where

$$K_c = f_c\left(\pi a_c \sec \pi a_c / W\right)^{1/2}$$

is the average stress intensity factor associated with critical fracture instaiblity as determined by the reporting investigator.

Where data for a material include a thickness range from essentially plane stress to plane strain fracture toughness data will be summarized also as a display of thickness effect similar to Figure 9.5.1.3. From this figure, K values for the appropriate thickness, t, can be selected and residual strength curve similar to Figure 9.5.1.5.3 can be constructed.

At present, since these are not design allowable data, requirements on the quantity of information necessary will not be specified. Data displays will be prepared for those materials, product forms and thicknesses where a sufficient number of tests at various crack and specimen sizes are available to establish a distinct trend. Correlative information will be appended below such graphical displays to indicate range of test panel sizes, crack lengths, and number of heats or lots of the material from which determination of K_{app} was determined.

9.5.1.5.4 *Required Reporting and Documentation*—To assure proper evaluation of plane stress and traditional fracture toughness data, adequate documentation of test results must be included with any data submittals for MIL-HDBK-5. The minimum quantity of experimental information considered appropriate for data proposals on the subject is described in the following subsections.

Center-Through-Cracked Tension Panels—To identify the material tested, it is necessary to report alloy temper, product form, and grain directions being tested. Reference tensile properties, actually representative of specimen or material lot (i.e., not specification or MIL-HDBK-5 A and B values), are also necessary information. These shall include yield strength, ultimate strength, and elongation.

The specimen configuration is described by measured thickness, panel width, and free length between grips. The minimum flaw details to be reported are fatigue stress levels used in generating the fatigue crack and length of the fatigue crack existent prior to the rising load fracture test.

The test procedure shall be described briefly, identifying environment (temperature, humidity, salinity, etc.), loading rate, and the mode of buckling restraint.

The report of test results shall include maximum load and stress, and estimated critical crack length (indicate method of detection, such as visual observation, film record, or compliance calibration). It is recommended that whenever practical, a record of load versus crack length be obtained to assess slow stable crack extension prior to fracture.

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9.6 Statistical Procedures and Tables

This section includes a number of statistical aids for use in preparation of data for MIL-HDBK-5. These aids are intended to supplement, not to replace, the basic procedure described elsewhere in these Guidelines.

Many different statistical techniques may be useful in analysis of mechanical-property data. This section presents brief descriptions of procedures that will be used most frequently in this application. More detailed descriptions of these and other statistical techniques and tables in their various forms can be found in a number of workbooks and texts; Reference 9.6 is a particularly useful one.

When procedures other than those described below are employed in preparation of data proposals, they should be described adequately in the proposal.

9.6.1 GOODNESS-OF-FIT TESTS

9.6.1.1 *Introduction*—The computational procedure selected to establish design-allowable values by statistical techniques is dependent upon distribution of strength measurements in the available sample. The most frequently used parametric procedures involve the use of normal distribution or three-parameter Weibull distribution. As noted previously, references to normal or Weibull distributions shall be interpreted as applying either to original measurements or to an appropriate transformation of them. This section contains a discussion and illustration of methods used to establish whether or not a population follows a normal or Weibull distribution.

Two goodness-of-fit test procedures are described below. The purpose of each is to indicate whether an initial distribution assumption should be rejected. The methods presented are based on the "Anderson-Darling" goodness-of-fit test statistic for testing normality (in Section 9.6.1.2) or three-parameter Weibullness (in Section 9.6.1.4). These tests are objective and indicate (at 5 percent risk of error) whether the sample is drawn from the tested distribution. Unfortunately, these tests may reject the hypothesis of normality or Weibullness even though the distribution may provide a reasonable approximation within the lower tail. Consequently, some subjective reasoning is employed after using a goodness-of-fit test.

After a goodness-of-fit test has been performed (especially if the distributional assumption has been rejected), it is often useful to form a cumulative probability plot of data to graphically illustrate the degree to which the assumed distribution fits the data. Methods for development of both normal probability plots (in Section 9.6.1.3) and Weibull probability plots (in Section 9.6.1.5) are presented.

In what follows, sample size is denoted by n, sample observations by X_1, ..., X_n, and sample observations ordered from least to greatest by $X_{(1)}$, ..., $X_{(n)}$. Obviously, the assumption is made that the data are ungrouped.

9.6.1.2 *"Anderson-Darling" Test for Normality.*—The "Anderson-Darling" test for normality is used to determine whether the curve which fits a given set of data can be approximated by a normal curve. The essence of the test is a numerical comparison of the cumulative distribution function for observed data with that for fitted normal curve over the entire range of the property being measured. Let

$$Z_{(i)} = \left(X_{(i)} - \overline{X}\right)/s \quad i = 1,...,n$$

where $X_{(i)}$ is the i^{th} smallest sample observation, $\overline{X}$ is the sample average, and s is the sample standard deviation. Equations for computing sample statistics are presented in Section 9.2.2.3.

The "Anderson-Darling" test statistic is

$$AD = \left[\sum_{i=1}^{n} \frac{1 - 2i}{n} \left[\ln\left(F_o(Z_{(i)})\right) + \ln\left(1 - F_o(Z_{n+1-i})\right)\right]\right] - n$$

where F_o is the standard normal distribution function*. If

$$AD > 0.752/\left(1 + 0.75/n + 2.25/n^2\right)$$

one may conclude (at 5 percent risk of error) that the population from which the sample was drawn is not normally distributed. Otherwise, the hypothesis that the population is normally distributed is not rejected. For further information on this test procedure, see References 9.6.1.2(a) and (b).

The same procedure can be used to test the normality of the residuals

$$e_i = y_i - \left(a + bx_i\right) \quad i = 1,...,n$$

from a regression (see Section 9.6.3) assuming uniformity of variance of the residuals over the range of the independent variable. When calculating the test statistic AD, define

$$Z_{(i)} = e_{(i)}/s_y \quad i = 1,...,n$$

where $e_{(i)}$, i = 1,...,n are the ordered residuals from smallest to largest and s_y is the root mean square error of the regression defined in Section 9.6.3.1. The justification for this procedure may be found in Reference 9.6.1.2(c).

9.6.1.3 *Normal Probability Plot.*—To graphically illustrate the degree to which a normal distribution fits a set of data, the use of arithmetic probability paper is recommended. Logarithmic probability paper may be used to determine whether the distribution of data could be made normal by logarithmic transformation. One axis is scaled in units of the property measured, and the other is a non-linear scale of probability.

If there are relatively few data points, all of them may be plotted individually on the chart. With larger samples, it is only necessary to plot enough points to define the curve.

*The standard normal distribution function F_o is that function such that $F_o(x)$ is equal to the area under the standard normal curve to the left of the value x.

The rank of each point selected for plotting is equal to the number of lower test points plus plotted point plus one half the number of other points equal to plotted point. Cumulative probability (P), in percent, is equal to the rank times 100, divided by one more than the total number of test points:

$$P\ (\text{in percent}) = \frac{(\text{rank})(100)}{n + 1} \qquad [9.6.1.3]$$

The measured value of each test point is plotted versus its cumulative probability and a straight line is drawn to represent the normal distribution. This line may be established by plotting any two points from the normal distribution curve for $\overline{X}$ and s (for example, $\overline{X}$ - 3s at 0.13 percent probability, and $\overline{X}$ at 99.87 percent probability) and connecting these two points.

The plotted points should finally be compared with the line to determine whether there appears to be a reasonably good fit. With sample sizes on the order of 100 test points, only those points lying between about 10 and 90 percent probability should be considered in making this evaluation. With sample sizes of 1000 test points, these limits can be extended to about 1 and 99 percent.

If normal probability paper is unavailable, a normal probability plot may be formed by plotting the measured value of each test point versus $\overline{X}$ + s F_o^{-1} (P/100) where F_o^{-1} is the inverse standard normal cumulative distribution function.*** The line representing fitted normal distribution is the line passing through the points with equal horizontal and vertical coordinates. If the horizontal axis is labeled with cumulative probabilities (P values) rather than F_o^{-1} (P/100) values, the plot will be identical to a plot formed on normal probability paper.

9.6.1.4 *Modified "Anderson-Darling" Test for Weibullness*—The "Anderson-Darling" test for three-parameter Weibullness is used to determine whether the curve which fits a given set of data can be approximated by a three-parameter Weibull curve. The essence of the test is a numerical comparison of the cumulative distribution function for observed data with that for a fitted Weibull curve over the entire range of property being measured. This test differs from the original version of the Anderson-Darling test in that it emphasizes the lower tail. This method can be applied with complete or censored data.

The first two steps produce estimates of the parameters of a three-parameter Weibull distribution. Be sure to acknowledge the appropriate degree of censoring in computing the threshold, shape, and scale parameters as described in sections 9.6.5.1 and 9.6.5.2. Using the procedure outlined in 9.6.5.1 compute a lower 50 percent confidence bound on the threshold, $\tau(0.50)$ or $\tau_{.50}$. Then, using the method described in 9.6.5.2, compute the maximum likelihood estimates of the shape and scale parameters for $\{X_{(i)} - \tau_{.50} : i=1,...,r\}$. Denote these estimates by $\beta_{.50}$ and $\alpha_{.50}$, respectively. Calculate the (censored or uncensored) A-D statistic by the following steps. For i=1,...,r, let

$$\xi_i = \left(\frac{X_{(i)} - \tau_{.50}}{\alpha_{.50}} \right)^{\beta_{.50}},$$

and

$$C_i = \frac{2i-1}{n}.$$

*The point F_o^{-1} (P/100) is that value such that the area under the standard normal curve to the left of F_o^{-1} (P/100) is P/100.

Define the A-D statistic as

$$AD = -\sum_{i=1}^{r}\left(C_i \ln\left(1-e^{-\xi_{(i)}}\right) + (2-C_i)\xi_{(i)}\right) + \frac{r^2}{n}\ln(1-e^{-\xi_{(r)}}) + \frac{(n-r)^2}{n}\xi_{(r)} - n(1-e^{-\xi_{(r)}}).$$

If

$$AD \geq \begin{cases} 0.3951 + 4.186 \times 10^{-6}\, n & (\textit{Uncensored}) \\ 0.2603 + 4.182 \times 10^{-6}\, n & (20\ \textit{percent censored}) \\ 0.1761 + 1.842 \times 10^{-6}\, n & (50\ \textit{percent censored}) \end{cases} \qquad [9.6.1.4]$$

one may conclude (at 5 percent risk of error) that the population from which the sample was drawn is not a three-parameter Weibull population. Otherwise, the hypothesis that the population is a three-parameter Weibull population is not rejected. Equation 9.6.1.4 was derived under the assumption that the threshold parameter is estimated, not known. For further information on this test procedure, see Reference 9.6.1.2-(a).

9.6.1.5 *Weibull Probability Plot*—To graphically illustrate the degree to which a three-parameter Weibull distribution fits a set of data, the following procedure for creation of a Weibull probability plot is recommended. If there are relatively few data points, all of them may be plotted individually. With larger samples, it is only necessary to plot enough points to define the curve.

The rank of each point selected for plotting is the number of lower test points plus the plotted point plus one-half the number of other test points equal to the plotted point. Its cumulative probability, P (in percent), is equal to the rank multiplied by 100, divided by one more than the total number of test points:

$$\text{P (in percent)} = \frac{(\text{rank})(100)}{n + 1}$$

The measured value of each test point is plotted versus F^{-1} (P/100) where

$$F^{-1}(P/100) = \tau_{50} + \alpha_{50}\left[-\ln\left(1 - (P/100)\right)\right]^{\frac{1}{\beta_{50}}}$$

and τ_{50}, α_{50}, and β_{50} are population parameter estimates obtained according to the procedures outlined in Section 9.6.5. A straight line is drawn to represent the fitted Weibull distribution. This line may be established by plotting any two points with equal vertical and horizontal coordinates and drawing a line through these two points. If the horizontal axis is labeled with cumulative probabilities rather than F^{-1} values, the plot will take the same form as the normal probability plot of Section 9.6.1.3.

The plotted points should finally be compared with the line to determine whether there appears to be a reasonably good fit. With sample sizes on the order of 100 test points, only those points lying between about 10 and 90 percent probability should be considered in making this evaluation. With sample sizes of 1000 test points, these limits can be extended to about 1 and 99 percent.

9.6.1.6 *Identifying Proper Backoff for Weibull Method.*—Begin with the estimates $\tau_{.50}$, $\alpha_{.50}$, and $\beta_{.50}$ obtained according to the procedures outlined in Section 9.6.5. Let $F_\tau(x)$ represent the cumulative distribution function of the three-parameter Weibull distribution with threshold parameter τ, and scale and shape parameters, $\alpha_{.50}$ and $\beta_{.50}$, respectively:

$$F_\tau(x) = 1 - \exp\left(-\left(\frac{x-\tau}{\alpha_{.50}}\right)^{\beta_{.50}}\right)$$

Define the special "backoff" Anderson Darling statistic by

$$ADB(\tau) = \sum_{i=1}^{r}\left[\left(\frac{i}{n}\right)^2(\ln b_i - \ln a_i) - \frac{2i}{n}(b_i - a_i) + \frac{1}{2}(b_i^2 - a_i^2)\right]$$

where $a_i = \min\{F_\tau(x_{(i)}), i/n\}$, and $b_i = \min\{F_\tau(x_{(i+1)}), i/n\}$. Let $\tau_{backoff}$ be the smallest value among 0.1, 0.2, 0.3, 0.4, and 0.5 such that

$$ADB(\tau_{.50} - \tau_{backoff}) < 0.0359 + 1.2 \times 10^{-5} n . \qquad [9.6.1.5]$$

If none of the five values satisfies Equation 9.6.1.5, the backoff procedure cannot be used to compute allowables. Otherwise, $\tau_{backoff}$ is subtracted from the allowable calculated from the complete sample.

9.6.2 TESTS OF SIGNIFICANCE

9.6.2.1 *Introduction*—A test of significance is employed to make a decision on a statistical basis. In this section, three tests ("F" test, "t" test, and k-sample Anderson-Darling test) are described for use in determining whether the populations from which two or more samples are drawn are identical.

Assuming an underlying normal distribution, "F" and "t" tests may be used in the case of two samples. The "F" test is used first to determine whether the two sample variances differ significantly or not (with a 5 percent risk of error). If the two sample variances do not differ significantly, the "t" test is used to determine whether the two sample means differ significantly. If either the two sample variances of the two sample means differ significantly (with a 5 percent risk of error), one may conclude (with a 9.75 percent joint risk error) that the populations from which the two samples were drawn are not identical. Otherwise, the hypothesis that the two populations are identical is not rejected. The tests given are exact when:

(1) The observations within each sample are taken randomly from a single population of possible observations, and

(2) The characteristic measured is normally distributed within this population.

To carry out a similar procedure without requiring the assumption of an underlying normal distribution, or if three or more samples are to be compared, the k-sample Anderson-Darling test should be employed. This test is a nonparametric procedure and simply tests the hypothesis that populations from which the samples are drawn are identical.

9.6.2.2 *Definitions*—Location and dispersion parameters are defined in Section 9.2.2.3, and these terms are used in various parts of the Guidelines. The following definitions apply specifically to tests in this section:

Significance Level (As Used Here)—Risk of concluding that two samples were drawn from different populations when, in fact, they were drawn from the same population. A significance level of $\alpha = 0.05$ is employed through these Guidelines.*

Confidence Interval Estimate—Range of values, computed with the sample that is expected to include the population variance or mean.

Degrees of Freedom—Number of independent comparisons afforded by a sample.

9.6.2.3 *The F Test*—The F test is used to determine whether the strength of two products differs with regard to variability.

Consider two products, A and B. These might represent two different processes, thickness ranges, or test directions. The statistics for the samples drawn from these products are:

	Product A	Product B
Sample size	n_A	n_B
Sample standard deviation	s_A	s_B
Sample mean	$\overline{X}_A$	$\overline{X}_B$

F is the ratio of the two sample variances, thus,

$$F = s_A^2/s_B^2 \qquad [9.6.2.3]$$

If the true variances of Products A and B are identical at a significance level of $\alpha = 0.05$, F should lie within the interval defined by

$F_{0.975}$ (for n_A - 1 and n_B - 1 degrees of freedom),

and

$1/F_{0.975}$ (for n_B - 1 and n_A - 1 degrees for freedom).**

If F does not lie within this interval, it can be concluded that the two products differ with regard to their variability. Values of $F_{0.975}$ are presented in Table 9.6.4.4.

9.6.2.3.1 *Example of Test Computation*—The following sample statistics are reported:

	Product A	Product B
Sample size	20	30
Sample standard deviation, ksi	4.0	5.0
Sample mean, ksi	100	102.0

*This is appropriate, since a confidence level $1 - \alpha = 0.95$ is used in establishing A and B-values.

**Since a two-sided interval is being defined for the population variance, the fractile of the F distribution corresponding to $1 - \alpha/2$ should be used, i.e., $F_{0.975}$.

Perform an F test as follows:

$F = s_A^2/s_B^2 = 4^2/5^2 = 0.64$

$df = n_A - 1 = 19$

$n_B - 1 = 29$

$F_{0.975\ (19,29)} = 2.23$

$1/F_{0.975\ (29,19)} = 1/2.40 = 0.42$

} From Table 9.6.4.4

Since 0.64 lies within the interval of 0.42 to 2.23 one can conclude that there is no reason to believe that Products A and B differ with regard to their variability.

9.6.2.4 *The t Test*—The t test is used to determine whether two products differ with regard to average strength. If they do, one may conclude that the two products do not belong to the same population.

In making the t test, it is assumed that the variances of two products are nearly equal, as first determined from the F test. If the F test shows that the variances are significantly different, there is no need to conduct the t test.

Consider the same products, A and B. The statistics for samples drawn from these products are:

	Product A	Product B
Sample size	n_A	n_B
Sample standard deviation	s_A	s_B
Sample mean	$\overline{X}_A$	$\overline{X}_B$

$D_{\bar{x}}$ is the absolute difference between the two sample means.

$$D_{\bar{X}} = | \bar{X}_A - \bar{X}_B | \qquad [9.6.2.4(a)]$$

If the true means of products A and B are identical, $D_{\bar{x}}$ should not exceed u, which is determined as indicated by the following equation for a significance level of $\alpha = 0.05$.

$$u = t_{0.975} s_p \sqrt{\frac{n_A + n_B}{n_A n_B}} \qquad [9.6.2.4(b)]$$

where

$t_{0.975}$ has $n_A + n_B - 2$ degrees of freedom*

*Since a two-sided interval is being defined from the population means, the fractile of the t distribution corresponding to $1-\alpha/2$ should be used, i.e., $t_{0.975}$.

and

$$s_p = \sqrt{\frac{(n_A - 1)s_A^2 + (n_B - 1)s_B^2}{n_A + n_B - 2}} \qquad [9.6.2.4(c)]$$

Values of $t_{0.975}$ are found in Table 9.6.4.5.

9.6.2.4.1 *Example of Test Computation.*—The following sample statistics are the same as those in Section 9.6.2.3.1:

	Product A	Product B
Sample size	20.0	30.0
Sample standard deviation	4.0	5.0
Sample mean	100.0	102.0

It was determined in Section 9.6.2.3.1 that the variances of Products A and B do not differ significantly. The t test computations to test the sample means are:

$$df = n_A + n_B - 2 = 48$$

$t_{0.975}$ (for 48 df) = 2.011 (from Table 9.6.4.5)

$$s_p = \sqrt{\frac{(n_A - 1)s_A^2 + (n_B - 1)s_B^2}{n_A + n_B - 2}} = \sqrt{\frac{(19)(4)^2 + (29)(5)^2}{48}} = 4.63 \text{ ksi}$$

$$\sqrt{\frac{n_A + n_B}{n_A n_B}} = \sqrt{\frac{20 + 30}{(20)(30)}} = 0.2887$$

$$u = t_{0.975}s_p \sqrt{\frac{n_A + n_B}{n_A n_B}} = (2.011)(4.63)(0.2887) = 2.7 \text{ ksi}$$

$$D_{\bar{x}} = |\bar{X}_A - \bar{X}_B| = 2.0 \text{ ksi}$$

Since $D_{\bar{x}}$ (2.0) is not greater than u (2.7), it may be concluded that there is no reason to believe that Products A and B differ with regard to their average strength. On the basis of both tests in this example, the conclusion would be that the two products were drawn from the same population.

9.6.2.5 *The k-Sample Anderson-Darling Test.*—The k-sample Anderson-Darling test is designed to test the hypothesis that populations from which two or more independent random samples were drawn are

identical. The test is appropriately applied to determine whether two or more products differ with regard to strength distributions. The test is a nonparametric statistical procedure and, thus, requires no assumptions other than the samples are true independent random samples from their respective populations.

Consider the products $A_1, A_2, ..., A_k$. Let $X_{11}, X_{12}, ..., X_{1n_1}$, denote a sample of n_1 data points from product A_1, let $X_{21}, X_{22}, ..., X_{2n_2}$ denote a sample of the n_2 data points from product A_2, and so forth. Furthermore, let $N = n_1 + n_2 + ... + n_k$ represent the total number of data points in the combined samples.

Let L denote the total number of distinct data points in the combined samples $Z_{(1)}, Z_{(2)}, ..., Z_{(L)}$ denote the distinct values in the combined data set ordered from least to greatest. The k-sample Anderson-Darling statistic is defined by

$$ADK = \frac{1}{N(k-1)} \sum_{i=1}^{k} \left[\frac{1}{n_i} \sum_{j=1}^{L} h_j \frac{(NF_{ij} - n_i H_j)^2}{H_j(N - H_j) - Nh_j/4} \right]$$

where

h_j = the number of values in the combined samples equal to $Z_{(j)}$

H_j = the number of values in the combined samples less than $Z_{(j)}$ plus one-half the number of values in the combined samples equal to $Z_{(j)}$

and

F_{ij} = the number of values in sample corresponding to product A_i which are less than $Z_{(j)}$ plus one-half the number of values in the sample corresponding to product A_i which are equal to $Z_{(j)}$.

Under the hypothesis of no differences in the sampled populations, the mean of ADK is approximately one and the variance is approximately

$$\sigma_N^2 = Var(ADK) = \frac{aN^3 + bN^2 + cN + d}{(k-1)^2 (N-1) (N-2) (N-3)}$$

with

$a = (4g - 6) (k - 1) + (10 - 6g)S$

$b = (2g - 4)k^2 + 8Tk + (2g - 14T - 4)S - 8T + 4g - 6$

$c = (6T + 2g - 2)k^2 + (4T - 4g + 6)k + (2T - 6)S + 4T$

$d = (2T + 6)k^2 - 4Tk$

where

$$S = \sum_{i=1}^{k} \frac{1}{n_i}$$

$$T = \sum_{i=1}^{N-1} \frac{1}{i}$$

and

$$g = \sum_{i=1}^{N-2} \sum_{j=i+1}^{N-1} \frac{1}{(N-i)j}$$

If

$$ADK \geq 1 + \sigma_N \left[1.645 + \frac{0.678}{\sqrt{k-1}} - \frac{0.362}{k-1} \right]$$

one may conclude (with a 5 percent risk error) that samples were drawn from different populations. Otherwise, the hypothesis that samples were selected from identical populations is not rejected. For more information on the k-sample Anderson-Darling test, see Reference 9.6.2.5.

9.6.3 DATA-REGRESSION TECHNIQUES.—When it is suspected that the average of one measured value varies linearly or curvilinearly with some other measured value, a regression is often employed to investigate and describe the relationship between the two quantities. Examples are effect of thickness on TUS, effect temperature on TUS, and effect of stress on cycles or time to rupture. Mathematical techniques for performing a simple linear regression analysis are contained in Section 9.6.3.1. Mathematical techniques for performing a quadratic regression analysis are contained in 9.6.3.2. Statistical tests to determine whether or not a straight line adequately describes the data are described in Section 9.6.3.3 and a test for equality of several regression lines is presented in Section 9.6.3.4. An example is presented in Section 9.6.3.5 using hypothetical data to illustrate many of the regression calculations. Figure 9.6.3 provides guidance in choosing an appropriate regression analysis to use for calculating design allowables.

Since least-squares regression is a general analytical tool used for multiple purposes, further instructions for use of the computed best-fit equation and standard deviation are given elsewhere in the Guidelines. It should be pointed out, however, that this technique is sometimes employed with transformed variables; that is, it may be necessary to work with log(TUS), t^2, or 1/(T + 460), for example. When this is the case, the analyst must remember to transform variables back to the original engineering units after final computations.

9.6.3.1 *Least-Squares Linear Regressions.*—Linear regression is appropriate when there is an approximate linear relationship between two measurable characteristics. Such a relationship is expressed algebraically by an equation that, in the case of two measurable characteristics x and y has the form

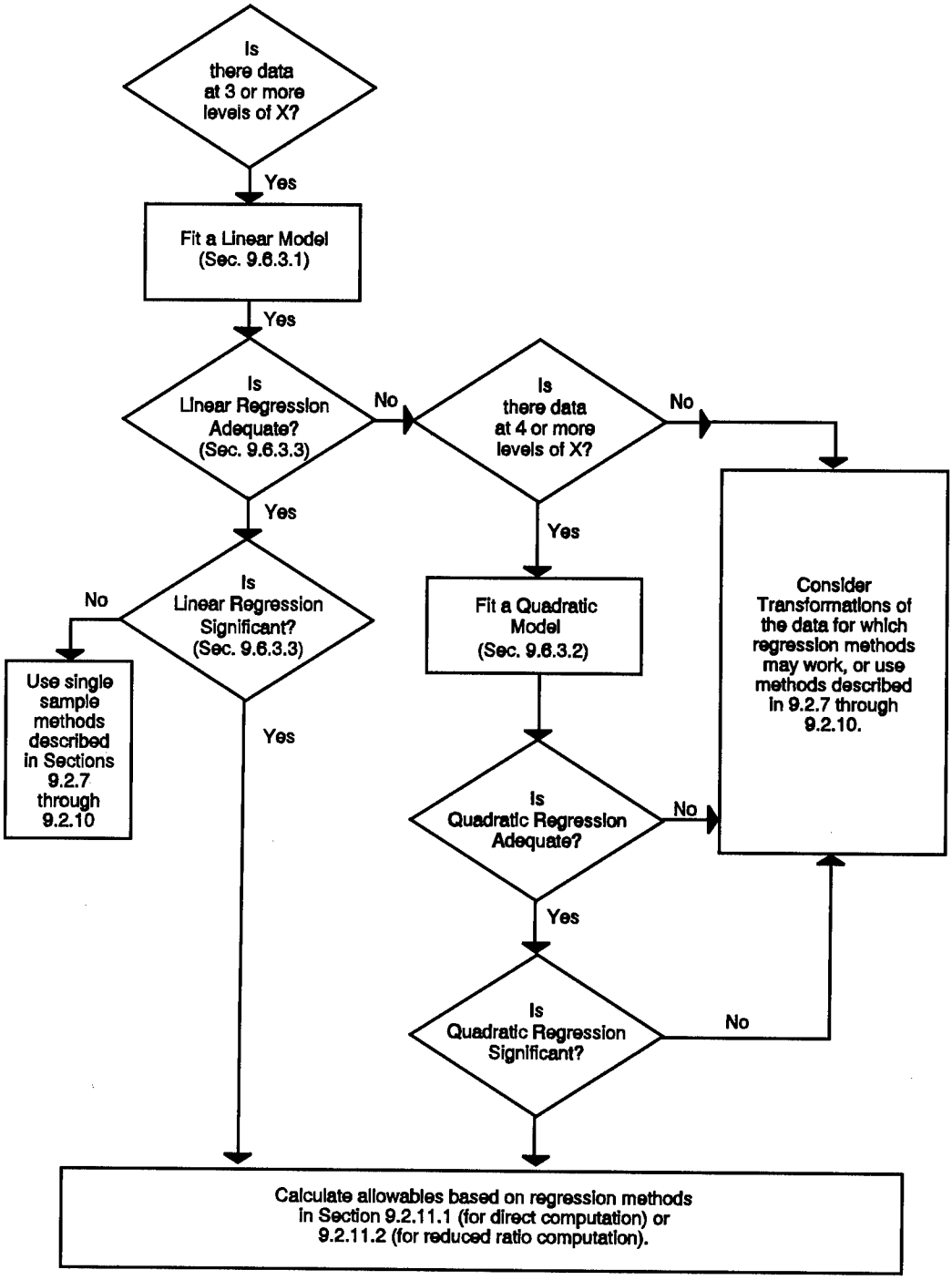


FIGURE 9.6.3. *General procedures for performing a regression analysis in order to calculate design allowables.*

$$y = \alpha + \beta x + \varepsilon \qquad [9.6.3.1(a)]$$

where

x = independent variable
y = dependent variable
α = true intercept of the regression equation
β = true slope of the regression equation
ε = measurement or experimental error by which y differs from the ideal linear relationship.

Aside from the error term, ε, this is the equation of a straight line. The parameter α determines the point where this line intersects the y-axis, and the β represents its slope. The variable x and y may represent either direct measurements or some transformation measurements of the characteristics under consideration.

Knowing or assuming such an approximate linear relationship, the problem becomes one of estimating the parameters α and β of the regression equations. It is necessary to have a random sample consisting of n pairs of observations, which is denoted by $(x_1, y_1),(x_2, y_2),..., (x_n, y_n)$. Such a sample can be represented graphically by n points plotted on a coordinate system, in which x is plotted horizontally and y vertically. A subjective solution can be obtained by drawing a line that, by visual inspection, appears to fit the points satisfactorily. An objective solution is given by the method of least squares.

The method of least squares is a numerical procedure for obtaining a line having the property that the sum of squares of vertical deviations of the sample points from this line is less than that for any other line. In this analysis, the least-squares line is represented by the equation

$$\hat{y} = a + bx \quad , \qquad [9.6.3.1(b)]$$

in which

$\hat{y}$ = predicted value of y for any value of x

a and b = estimates of the parameters α and β in the true regression equation obtained by the least squares method presented below.

It can be shown with the aid of calculus that the values of a and b that minimize the sum of squares of the vertical deviations are given by the formulas:

$$a = \frac{\Sigma y - b\Sigma x}{n} \qquad [9.6.3.1(c)]$$

$$b = \frac{S_{xy}}{S_{xx}} \qquad [9.6.3.1(d)]$$

where

$$S_{xy} = \Sigma xy - \frac{\Sigma x \, \Sigma y}{n} \quad , \qquad [9.6.3.1(e)]$$

and

$$S_{xx} = \Sigma x^2 - \frac{(\Sigma x)^2}{n} \qquad [9.6.3.1(f)]$$

The root mean square error of y is expressed as

$$S_y = \sqrt{\frac{\Sigma(y - \hat{y})^2}{n - 2}} \qquad [9.6.3.1(g)]$$

where $\hat{y}$ is the predicted value of y defined above. This quantity is an estimate of the standard deviation of the distribution of y about the regression line. A convenient computational formula for s_y is

$$s_y = \sqrt{\frac{S_{yy} - b^2 S_{xx}}{n - 2}} \qquad [9.6.3.1(h)]$$

where

$$S_{yy} = \Sigma y^2 - \frac{(\Sigma y)^2}{n} \qquad [9.6.3.1(i)]$$

The quantity $R^2 = (b^2 S_{xx})/S_{yy}$ measures the proportion of total variation in the y data, about its average, that is explained by the regression. An R^2 equal to 1 indicates that the regression model describes data perfectly, which is rare in practice. R^2 provides a rough idea of how well data is described by a linear regression. A more precise determination of the adequacy of a linear regression is discussed in the next section.

9.6.3.2 *Least-Squares Quadratic Regression.*—Quadratic regression is appropriate when there is an approximate quadratic relationship between two measurable characteristics. Such a relationship is expressed algebraically by an equation that, in the case of two measurable characteristics x and y, has the form

$$y = \alpha + \beta x + \gamma x^2 + \varepsilon \ ,$$

where

x = independent variable
y = dependent variable
α = true intercept of the regression equation
β = true coefficient of the linear term in the regression equation
γ = true coefficient of the quadratic term in the regression equation
ε = measurement or experimental error by which y differs from the ideal linear relationship.

Aside from the error term, ε, this is the equation of a parabola. The parameter α determines the point where this curve intersects the y-axis. The variable x and y may represent either direct measurements or some transformation measurements of the characteristics under consideration.

Knowing or assuming such an approximately quadratic relationship, the problem becomes one of estimating the parameters α, β, and γ of the regression equation. It is necessary to have a random sample consisting of n pairs of observations, which is denoted by (x_1,y_1), (x_2,y_2), ..., (x_n,y_n). Such a sample can be represented graphically by n points plotted on a coordinate system, in which x is plotted horizontally, y vertically. A subjective solution can be obtained by drawing a curve that, by visual inspection, appears to fit the points satisfactorily. An objective solution is given by the method of least squares.

The model of least squares is a numerical procedure for obtaining a second-degree polynomial having the property that the sum of squares of vertical deviations of the sample points from this curve is less than that for any other second-degree polynomial. In this analysis, the least squares curve is represented by the equation

$$\hat{y} = a + bx + cx^2 \qquad [9.6.3.2(a)]$$

in which

$\hat{y}$ = predicted value of y for any value of x

a, b, and c = estimates of the parameters α, β and γ in the true regression equation obtained by the least squares method presented below.

It can be shown with the aid of calculus that the values of a, b, and c that minimize the sum of squares of the vertical deviations are given by the formulas:

$$c = \frac{\left(\sum X_2Y\right)\left(\sum X_1^2\right) - \left(\sum X_1Y\right)\left(\sum X_1X_2\right)}{D} \qquad [9.6.3.2(b)]$$

$$b = \frac{\left(\sum X_1Y\right)\left(\sum X_2^2\right) - \left(\sum X_2Y\right)\left(\sum X_1X_2\right)}{D}$$

$$a = \bar{y} - b\left(\sum \frac{x}{n}\right) - c\left(\sum \frac{x^2}{n}\right)$$

where

$$D = \left(\sum X_1^2\right)\left(\sum X_2^2\right) - \left(\sum X_1 X_2\right)^2 \qquad [9.6.3.2(c)]$$

and where $X_1 = x - \Sigma x/n$, $X_2 = x^2 - \Sigma x^2/n$, $Y = y - \Sigma y/n$, all symbols being summed are subscripted by i, and all summations are over i=1 to n.

The root mean square error of y is expressed as

$$s_y = \sqrt{\frac{\sum (y-\hat{y})^2}{n-3}} \qquad [9.6.3.2(d)]$$

where $\hat{y}$ is the predicted value of y defined above. This quantity is an estimate of the standard deviation of the distribution of y about the regression curve. A convenient computational formula for s_y is

$$s_y = \sqrt{\left(\sum Y^2 - b\sum X_1 Y - c\sum X_2 Y\right) / (n-3)} \qquad [9.6.3.2(e)]$$

The quantity $R^2 = 1-(n-3)\, s_y^2 / \Sigma Y^2$ measures the proportion of total variation in the y data, about its average, that is explained by the regression. An R^2 equal to 1 indicates that the regression model describes data perfectly, which is rare in practice. R^2 provides a rough idea of how well the data are described by a quadratic regression.

Another quantity, Q, is required to compute allowables by quadratic regression analysis. Q is defined as

$$Q = q_1 + 2q_2 x_o + (2q_3 + q_4)\, x_o^2 + 2q_5\, x_o^3 + q_6\, x_o^4 \qquad [9.6.3.2(f)]$$

where x_0 is the value of the independent variable for which the allowable is being calculated and q_1, q_2, q_3, q_4, q_5 and q_6 are defined to be elements of the inverse of the matrix X′X as follows:

$$(X'X)^{-1} = \begin{bmatrix} q_1 & q_2 & q_3 \\ q_2 & q_4 & q_5 \\ q_3 & q_5 & q_6 \end{bmatrix} \qquad [9.6.3.2(g)]$$

with

$$X'X = \begin{bmatrix} n & \sum x_i & \sum x_i^2 \\ \sum x_i & \sum x_i^2 & \sum x_i^3 \\ \sum x_i^2 & \sum x_i^3 & \sum x_i^4 \end{bmatrix} \qquad [9.6.3.2(h)]$$

9.6.3.3 *Tests for Adequacy of a Regression*—It is possible that the relationship between dependent variable y and independent variable x may not be approximately linear. In that case, a straight line would not "fit" the data very well. It is also possible that the relationships between x and y, although, approximately linear, may not be very strong. In such a case, estimated slope parameter b would not be significantly different from zero. Both the lack of fit and the significance of a linear regression equation can be evaluated through an analysis of variance as described in this section.

The analysis of variance for testing lack of fit and significance of regression is based on the assumption that measurement errors, ε_i, in the approximate linear relationship between y_i and x_i, i.e.,

$$\varepsilon_i = y_i - (\alpha + \beta x_i) \quad i = 1,..., n$$

are independent and normally distributed with an overall mean of zero and a constant variance of σ^2. Assuming uniformity of variance of measurement errors over the range of the independent variable, the normality assumption concerning unobservable ε_i can be checked by performing the Anderson-Darling test for normality on the observable residuals

$$e_i = y_i - (a + bx_i) \quad i = 1,..., n$$

where a and b are the least squares estimates of α and β. See Section 9.6.1.2 for more details. By plotting the residuals e_i against the respective x_i, an informal check on the assumption of constant variance σ^2 is possible as well. In such a plot residuals should vary approximately equally over the range of x_i values.

The analysis of variance table for testing the lack of fit and significance of a linear regression is shown below. The sums of squares for the three primary lines of the analysis of variance table (Regression, Error, and Total) are calculated using quantities defined in Section 9.6.3.1:

Source of Variation	Degrees of Freedom, (Linear)	Sum of Square, SS	Mean Squares, MS	F_{calc}
Regression	1	SSR	MSR	F_1
Error	n-2	SSE	MSE	
Lack of Fit	k-2	SSLF	MSLF	F_2
Pure Error	n-k	SSPE	MSPE	
Total	n-1	SST		

$$SSR = b^2 S_{xx}$$

$$SST = S_{yy}$$

$$SSE = SST - SSR.$$

If the multiple observations at one or more values of the independent variable x are available, and observations are made at three or more distinct x values, then it is possible to evaluate the adequacy of a line in describing the relationship between x and y. The notation in testing for this lack of fit is summarized in the analysis of variance table above. Let Y_{ij} denote the j^{th} data value at the i^{th} x level, k represent the number of distinct x levels for which there is data, and n_i represent the number of data values at the i^{th} x level. Denote the total of the observations at the i^{th} x level by

$$T_i = \sum_{j=1}^{n_i} Y_{ij} \text{ for } i = 1, \ldots, k$$

and note that

$$n = \sum_{i=1}^{k} n_i$$

is used to denote the total number of observations. The lack of fit and pure error sums of squares are computed as

$$SSLF = \sum_{i=1}^{k} \left(T_i^2/n_i\right) - \left(\Sigma y\right)^2/n - SSR$$

and

$$SSPE = SSE - SSLF$$

The sums of squares are divided by the corresponding degrees of freedom to compute mean squares as shown below:

$$MSR = SSR$$
$$MSE = SSE/(n - 2)$$
$$MSLF = SSLF/(k - 2)$$
$$MSPE = SSPE/(n - k)$$

These mean squares are used to compute two F statistics which test for lack of fit and significance of regression. (Note: If there is only one data value for each x level, i.e., $n_i = 1$ for $i = 1, 2, \ldots, k$, or if $k \leq 2$, then it is not possible to test for lack of fit.)

The two F statistics, F_1 and F_2, are defined as ratios of the mean squares as specified below:

$$F_1 = MSR/MSE$$
$$F_2 = MSLF/MSPE.$$

F_2 and Table 9.6.4.9 are used to test for lack of fit. If F_2 is greater than the 95th percentile of F distribution with k - 2 numerator degrees of freedom and n - k denominator degrees of freedom (from Table 9.6.4.9), then there is significant lack of fit. In this case it may be concluded (with a 5 percent risk of error) that linear regression does not adequately describe the relationship between x and y. Otherwise, lack of fit can be considered insignificant and a linear regression model can be assumed.

If lack of fit is not significant, the significance of regression may be tested using F_1 and Table 9.6.4.9. If F_1 is greater than the 95th percentile of F distribution with 1 numerator degree of freedom and n - 2 denominator degrees of freedom (from Table 9.6.4.9), then regression is significant. Otherwise, regression is not significant and x is considered to have little or no predictive value for y.

9.6.3.4 *Testing for Equality of Several Regressions.*—The procedure presented in this section is designed to test the hypothesis that the true regression equations corresponding to two or more independent data sets are equal (linear or quadratic). It is appropriately applied to test the equality of several regressions in determining whether corresponding data sets should be combined for the purpose of calculating design allowables. To test k regressions for equality, the following procedure should be performed.

Perform separate regression analyses for each data set. The same model form should be used in all regressions (all linear or all quadratic). Add error sum of squares (SSE) values from each of the separate regressions to obtain SSE(F), error sum of squares for the full model which allows separate slope and intercept parameters for each data set. Then fit a single regression to the combined data from all data sets to obtain SSE(R), error sum of squares for the reduced model which contains a single set of coefficients a and b (and c for quadratic models) which apply to all data sets. The F statistic for testing the equality of the k regressions is

$$F = \frac{SSE(R) - SSE(F)}{2(k - 1)} \div \frac{SSE(F)}{n - 2k}$$

for simple linear models, and

$$F = \frac{SSE(R) - SSE(F)}{3(k - 1)} \div \frac{SSE(F)}{n - 3k}$$

for quadratic models, where n denotes total number of observations in all k data sets combined. In the linear case, if F is greater than the 95th percentile of the F distribution with 2(k - 1) numerator degrees of freedom and n - 2k denominator degrees of freedom (from Table 9.6.4.9), the hypothesis that the regressions are equal is rejected. In the quadratic case, if F is greater than the 95th percentile of the F distribution with 3(k - 1) numerator degrees of freedom, and n - 3k denominator degrees of freedom, the hypothesis that the regressions are equal is rejected. See Reference 9.6.3.3 for more detail.

9.6.3.5 *Example of Computations.*—In this example, x represents thickness and y, the TYS values determined from a group of tensile tests. Values of x and y are as follows:

X	Y
0.100	121
0.100	119
0.200	114
0.200	108
0.300	112
0.300	108
0.400	112
0.400	106
0.500	101
0.500	99

From these data, the following quantities may be calculated:

$n = 10$	$(\Sigma x)^2 = 9$
$\Sigma x = 3$	$(\Sigma y)^2 = 121000$
$\Sigma y = 1100.0$	$(\Sigma x)(\Sigma y) = 3300$
$\Sigma x^2 = 1.1$	$S_{xx} = 0.20$
$\Sigma y^2 = 121452$	$S_{xy} = -8.4$
$\Sigma xy = 321.6$	$S_{yy} = 452.$

The slope of the regression line is:

$$b = \frac{S_{xy}}{S_{xx}} = \frac{-8.4}{0.20} = -42$$

The y-intercept of the regression line is:

$$a = \frac{\Sigma y - b\Sigma x}{n} = \frac{1100}{10} - \frac{(-42)(3)}{10} = 110 + 12.6 = 122.6$$

Thus the final equation of the least squares regression line is:

$$\hat{y} = a + b\,x = 122.6 - 42x$$

The total of the y data at each x level is needed to calculate lack of fit and pure error sums of squares. These totals are as follows:

x_i	T_i
0.1	240
0.2	222
0.3	220
0.4	218
0.5	200

There are data values at k = 5 different x levels, with $n_i = 2$ values at each level and

$$\sum_{i=1}^{k} (T_i^2/n_i) = \frac{(240)^2}{2} + \ldots + \frac{(200)^2}{2} = 121404$$

Thus,

$$SSLF = 121404 - (1100)^2/10 - 352.8 = 51.2$$

and

$$SSPE = 99.2 - 51.2 = 48.$$

The mean square values are computed by dividing corresponding sums of squares by their degrees of freedom. The F1 and F2 statistics are then calculated as ratios of mean squares. The analysis of variance table is shown below.

Source of Variation	Degree of Freedom, DF	Sum of Square, SS	Mean Squares, MS	F_{calc}
Regression	1	352.8	352.8	$F_1 = 28.5$
Error	8	99.2	12.4	
Lack of Fit	3	51.2	17.07	$F_2 = 1.78$
Pure Error	5	48.0	9.6	
Total	9	452.0		

Using this equation, the following values of $\hat{y}$ may be computed for the values of x listed previously.

x	$\hat{y}$
0.100	118.4
0.200	114.2
0.300	110.0
0.400	105.8
0.500	101.6

The root mean square error is computed as follows:

$$S_y = \sqrt{\frac{\Sigma(y - \hat{y})^2}{n - 2}} = \sqrt{\frac{99.2}{8}}$$

or

$$s_y = \sqrt{\frac{S_{yy} - b^2 S_{xx}}{n-2}} = \sqrt{\frac{452 - (-42)^2(0.2)}{8}} = 3.52.$$

R^2 is computed as follows:

$$R^2 = \frac{b^2 S_{xx}}{S_{yy}} = \frac{(-42)^2(0.2)}{452} = 0.78.$$

The sum of squares for the regression, total and error lines are computed as follows:

$$SSR = (-42)^2\ (0.20) = 352.8$$
$$SST = 452$$
$$SSE = 452 - 352.8 = 99.2.$$

The F_2 value of 1.78 with k - 2 = 3 and n - k = 5 degrees of freedom is less than the value of 5.41 from Table 9.6.4.9 corresponding to 3 numerator and 5 denominator degrees of freedom. This indicates that lack of fit can be considered insignificant. Thus, it is reasonable to assume that a linear regression adequately describes the data. The F_1 value of 28.5 with 1 and n - 2 = 8 degrees of freedom is greater than the value of 5.32 from Table 9.6.4.9 corresponding to 1 numerator and 8 denominator degrees of freedom, so the slope of the regression is found to be significantly different from zero.

9.6.4 TABLES.—In this section a number of tables of statistical values that are required for analyses described in the Guidelines are presented. For tables containing various fractiles or confidence levels, only applicable portions are reproduced herein. Table 9.6.4.1 was reproduced by permission from Reference 9.6.4.1. Tables 9.6.4.2, 9.6.4.7, and 9.6.4.8 were computed specifically for MIL-HDBK-5. Tables 9.6.4.3 through 9.6.4.6, and 9.6.4.9 were reproduced or adapted from tables in Reference 9.6, with the addition of a few individual values from various sources.

Table 9.6.4.1 One-Sided Tolerance Limit Factors[a], k, for the Normal Distribution, 0.95 Confidence, and n-1 Degrees of Freedom (continued)

Note: use values for P = 0.99 to determine A allowables
use values for P = 0.90 to determine B allowables

n	P = 0.90	P = 0.99
2	20.581	37.094
3	6.155	10.553
4	4.162	7.042
5	3.407	5.741
6	3.006	5.062
7	2.755	4.642
8	2.582	4.354
9	2.454	4.143
10	2.355	3.981
11	2.275	3.852
12	2.210	3.747
13	2.155	3.659
14	2.109	3.585
15	2.068	3.520
16	2.033	3.464
17	2.002	3.414
18	1.974	3.370
19	1.949	3.331
20	1.926	3.295
21	1.905	3.263
22	1.886	3.233
23	1.869	3.206
24	1.853	3.181
25	1.838	3.158
26	1.824	3.136
27	1.811	3.116
28	1.799	3.098
29	1.788	3.080
30	1.777	3.064
31	1.767	3.048
32	1.758	3.034
33	1.749	3.020
34	1.740	3.007
35	1.732	2.995
36	1.725	2.983
37	1.717	2.972
38	1.710	2.961
39	1.704	2.951
40	1.697	2.941
41	1.691	2.932
42	1.685	2.923
43	1.680	2.914
44	1.674	2.906
45	1.669	2.898
46	1.664	2.890
47	1.659	2.883
48	1.654	2.876
49	1.650	2.869
50	1.646	2.862
51	1.641	2.856
52	1.637	2.850
53	1.633	2.844
54	1.630	2.838
55	1.626	2.833
56	1.622	2.827
57	1.619	2.822
58	1.615	2.817
59	1.612	2.812
60	1.609	2.807

Table 9.6.4.1 One-Sided Tolerance Limit Factors[a], k, for the Normal Distribution, 0.95 Confidence, and n-1 Degrees of Freedom (continued)

n	P = 0.90	P = 0.99
61	1.606	2.802
62	1.603	2.798
63	1.600	2.793
64	1.597	2.789
65	1.594	2.785
66	1.591	2.781
67	1.589	2.777
68	1.586	2.773
69	1.584	2.769
70	1.581	2.765
71	1.579	2.762
72	1.576	2.758
73	1.574	2.755
74	1.572	2.751
75	1.570	2.748
76	1.568	2.745
77	1.565	2.742
78	1.563	2.739
79	1.561	2.736
80	1.559	2.733
81	1.557	2.730
82	1.556	2.727
83	1.554	2.724
84	1.552	2.721
85	1.550	2.719
86	1.548	2.716
87	1.547	2.714
88	1.545	2.711
89	1.543	2.709
90	1.542	2.706
91	1.540	2.704
92	1.538	2.701
93	1.537	2.699
94	1.535	2.697
95	1.534	2.695
96	1.532	2.692
97	1.531	2.690
98	1.530	2.688
99	1.528	2.686
100	1.527	2.684
101	1.525	2.682
102	1.524	2.680
103	1.523	2.678
104	1.521	2.676
105	1.520	2.674
106	1.519	2.672
107	1.518	2.671
108	1.517	2.669
109	1.515	2.667
110	1.514	2.665
111	1.513	2.663
112	1.512	2.662
113	1.511	2.660
114	1.510	2.658
115	1.508	2.657
116	1.507	2.655
117	1.506	2.654
118	1.505	2.652
119	1.504	2.651
120	1.503	2.649

Table 9.6.4.1 One-Sided Tolerance Limit Factors[a], k, for the Normal Distribution, 0.95 Confidence, and n-1 Degrees of Freedom (continued)

n	P = 0.90	P = 0.99	n	P = 0.90	P = 0.99
121	1.502	2.648	151	1.477	2.610
122	1.501	2.646	152	1.476	2.609
123	1.500	2.645	153	1.476	2.608
124	1.499	2.643	154	1.475	2.607
125	1.498	2.642	155	1.474	2.606
126	1.497	2.640	156	1.474	2.605
127	1.496	2.639	157	1.473	2.604
128	1.496	2.638	158	1.472	2.603
129	1.495	2.636	159	1.472	2.602
130	1.494	2.635	160	1.471	2.601
131	1.493	2.634	161	1.470	2.600
132	1.492	2.632	162	1.470	2.600
133	1.491	2.631	163	1.469	2.599
134	1.490	2.630	164	1.469	2.598
135	1.489	2.628	165	1.468	2.597
136	1.489	2.627	166	1.467	2.596
137	1.488	2.626	167	1.467	2.595
138	1.487	2.625	168	1.466	2.594
139	1.486	2.624	169	1.466	2.593
140	1.485	2.622	170	1.465	2.592
141	1.485	2.621	171	1.464	2.592
142	1.484	2.620	172	1.464	2.591
143	1.483	2.619	173	1.463	2.590
144	1.482	2.618	174	1.463	2.589
145	1.481	2.617	175	1.462	2.588
146	1.481	2.616	176	1.462	2.587
147	1.480	2.615	177	1.461	2.587
148	1.479	2.613	178	1.460	2.586
149	1.479	2.612	179	1.460	2.585
150	1.478	2.611	180	1.459	2.584

Table 9.6.4.1 One-Sided Tolerance Limit Factors[a], k, for the Normal Distribution, 0.95 Confidence, and n-1 Degrees of Freedom (continued)

n	P = 0.90	P = 0.99	n	P = 0.90	P = 0.99
181	1.459	2.583	255	1.429	2.540
182	1.458	2.583	260	1.428	2.537
183	1.458	2.583	265	1.426	2.535
184	1.457	2.581	270	1.425	2.533
185	1.457	2.580	275	1.423	2.531
186	1.456	2.580	280	1.422	2.529
187	1.456	2.579	285	1.421	2.527
188	1.455	2.578	290	1.419	2.525
189	1.455	2.577	295	1.418	2.524
190	1.454	2.577	300	1.417	2.522
191	1.454	2.576	305	1.416	2.520
192	1.453	2.575	310	1.415	2.518
193	1.453	2.575	315	1.413	2.517
194	1.452	2.574	320	1.412	2.515
195	1.452	2.573	325	1.411	2.514
196	1.451	2.572	330	1.410	2.512
197	1.451	2.572	335	1.409	2.511
198	1.450	2.571	340	1.408	2.509
199	1.450	2.570	345	1.407	2.508
200	1.450	2.570	350	1.406	2.506
205	1.447	2.566	355	1.405	2.505
210	1.445	2.563	360	1.404	2.504
215	1.443	2.560	365	1.404	2.502
220	1.441	2.557	370	1.403	2.501
225	1.439	2.555	375	1.402	2.500
230	1.437	2.552	380	1.401	2.499
235	1.436	2.549	385	1.400	2.498
240	1.434	2.547	390	1.399	2.496
245	1.432	2.544	395	1.399	2.495
250	1.431	2.542	400	1.398	2.494

Table 9.6.4.1 One-Sided Tolerance Limit Factors[a], k, for the Normal Distribution, 0.95 Confidence, and n-1 Degrees of Freedom (continued)

n	P = 0.90	P = 0.99	n	P = 0.90	P = 0.99
425	1.394	2.489	800	1.363	2.443
450	1.391	2.484	825	1.361	2.441
475	1.388	2.480	850	1.360	2.439
500	1.385	2.475	875	1.359	2.438
525	1.382	2.472	900	1.358	2.436
550	1.380	2.468	925	1.357	2.434
575	1.378	2.465	950	1.356	2.433
600	1.376	2.462	975	1.355	2.432
625	1.374	2.459	1000	1.354	2.430
650	1.372	2.456	1500	1.340	2.411
675	1.370	2.454	2000	1.332	2.399
700	1.368	2.451	3000	1.323	2.385
725	1.367	2.449	5000	1.313	2.372
750	1.365	2.447	10000	1.304	2.358
775	1.364	2.445	∞	1.282	2.326

[a] The following equations may be used to compute k factors in lieu of using table values:

$$K_A = 2.326 + \exp [1.34 - 0.522 \ln(n) + 3.87/n]$$

$$K_B = 1.282 + \exp [0.958 - 0.520 \ln(n) + 3.19/n]$$

These approximations are accurate to within 0.2% of the table values for n greater than or equal to 16.

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TABLE 9.6.4.2. *Ranks, r, of Observations, n, for an Unknown Distribution Having the Probability and Confidence of T_{99} and T_{90} Values*

T_{99} Value						T_{90} Value					
n	r_{99}	n	r_{99}	n	r_{99}	n	r_{90}	n	r_{90}	n	r_{90}
≤298	a	4635	36	8643	72	≤28	b	638	52	2693	340
299	1	4749	37	8753	73	29	1	660	54	3797	350
473	2	4862	38	8862	74	46	2	682	56	3901	360
628	3	4975	39	8972	75	61	3	704	58	4005	370
773	4	5088	40	9081	76	76	4	726	60	4109	380
913	5	5201	41	9190	77	89	5	781	65	4213	390
1049	6	5314	42	9300	78	103	6	836	70	4317	400
1182	7	5427	43	9409	79	116	7	890	75	4421	410
1312	8	5539	44	9518	80	129	8	945	80	4525	420
1441	9	5651	45	9627	81	142	9	999	85	4629	430
1568	10	5764	46	9736	82	154	10	1053	90	4733	440
1693	11	5876	47	9845	83	167	11	1107	95	4836	450
1818	12	5988	48	9954	84	179	12	1161	100	4940	460
1941	13	6099	49	10063	85	191	13	1269	110	5044	470
2064	14	6211	50	10172	86	203	14	1376	120	5147	480
2185	15	6323	51	10281	87	215	15	1483	130	5251	490
2305	15	6434	52	10390	88	227	16	1590	140	5354	500
2425	16	6545	53	10498	89	239	17	1696	150	5613	525
2546	18	6657	54	10607	90	251	18	1803	160	5871	550
2665	19	6768	55	10716	91	263	19	1909	170	6130	575
2784	20	6879	56	10824	92	275	20	2015	180	6388	600
2902	21	6990	57	10933	93	298	22	2120	190	6645	625
3020	22	7100	58	11041	94	321	24	2226	200	6903	650
3137	23	7211	59	11150	95	345	26	2331	210	7161	675
3254	24	7322	60	11258	96	368	28	2437	220	7418	700
3371	25	7432	61	11366	97	391	30	2542	230	7727	730
3487	26	7543	62	11475	98	413	32	2647	240	8036	760
3603	27	7653	63	11583	99	436	34	2752	250	8344	790
3719	28	7763	64	11691	100	459	36	2857	260	8652	820
3834	29	7874	65			481	38	2962	270	8960	850
3949	30	7984	66			504	40	3066	280	9268	880
4064	31	8094	67			526	42	3171	290	9576	910
4179	32	8204	68			549	44	3276	300	9884	940
4293	33	8314	69			571	46	3380	310	10191	970
4407	34	8423	70			593	48	3484	320	10499	1000
4521	35	8533	71			615	50	3589	330		

[a] T_{99} value is lower than value of lowest observation.
[b] T_{90} value is lower than value of lowest observation.

The following equations may be used to compute ranks in lieu of using table values or for n values greater than these presented in the table:

$$r_{99} = n/100 - 1.645\sqrt{99n/10000} + 0.29 + 19.1/n \text{ , for } n \geq 299$$

rounded to the nearest integer. For n less than 299, the T_{99} value does not exist. This approximation is

exact for all but 23 values of n in the range of the table ($299 \leq n \leq 11691$), which is an error rate of about 0.2%. For this small percentage of n values, the approximation gives an r value 1 below the actual r, resulting in a conservative T_{99} value. For T_{90} values, the approximation is

$$r_{90} = n/10 - 1.645\sqrt{99n/100} + 0.23 \text{ , for } n \geq 29$$

rounded to the nearest integer. For n less than 29, the T_{90} value does not exist. The approximation is exact for all but 12 values of n in the range of the table ($29 \leq n \leq 10499$), and errs conservatively by one rank for this small percentage (0.1%).

Table 9.6.4.3. *0.95 Fractiles[a] of the Chi-Squared Distribution Associated with df Degrees of Freedom*

df	$x^2_{0.95}$	df	$x^2_{0.95}$
1	3.84	16	26.30
2	5.99	17	27.59
3	7.81	18	28.87
4	9.49	19	30.14
5	11.07	20	31.41
6	12.59	21	32.67
7	14.07	22	33.92
8	15.51	23	35.17
9	16.92	24	36.42
10	18.31	25	37.65
11	19.68	26	38.88
12	21.03	27	40.11
13	22.36	28	41.34
14	23.68	29	42.56
15	25.00	30	43.77

[a] The following equation may be used to compute 0.95 fractiles of the Chi-Squared distribution in lieu of using table values:

$$x^2_{0.95} = \gamma\left(1 - \frac{2}{9\gamma} + 1.645\sqrt{\frac{2}{9\gamma}}\right)^3 + \frac{9}{100\gamma}$$

where γ is the degrees of freedom (df). This approximation is accurate to within 0.2% of the table values. See Reference 9.6.4.3.

TABLE 9.6.4.4. *0.975 Fractiles[a] of the F Distribution Associated with n_1 and n_2 Degrees of Freedom $F_{.975}(n_1, n_2)$*

n_1 = degrees of freedom for numerator

n_1 / n_2[b]	1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40	60	120	∞
1	647.8	799.5	864.2	899.6	921.8	937.1	948.2	956.7	963.3	968.6	976.7	984.9	993.1	997.2	1001	1006	1010	1014	1018
2	38.51	39.00	39.17	39.25	39.30	39.33	39.36	39.37	39.39	39.40	39.41	39.43	39.45	39.46	39.45	39.47	39.48	39.49	39.50
3	17.44	16.04	15.44	15.10	14.88	14.73	14.62	14.54	14.47	14.42	14.34	14.25	14.17	14.12	14.08	14.04	13.99	13.95	13.90
4	12.22	10.65	9.98	9.60	9.36	9.20	9.07	8.98	8.90	8.84	8.75	8.66	8.56	8.51	8.46	8.41	8.36	8.31	8.26
5	10.01	8.43	7.76	7.39	7.15	6.98	6.85	6.76	6.68	6.62	6.52	6.43	6.33	6.28	6.23	6.18	6.12	6.07	6.02
6	8.81	7.26	6.60	6.23	5.99	5.82	5.70	5.60	5.52	5.46	5.37	5.27	5.17	5.12	5.07	5.01	4.96	4.90	4.85
7	8.07	6.54	5.89	5.52	5.29	5.12	4.99	4.90	4.82	4.76	4.67	4.57	4.47	4.42	4.36	4.31	4.25	4.20	4.14
8	7.57	6.06	5.42	5.05	4.82	4.65	4.53	4.43	4.36	4.30	4.20	4.10	4.00	3.95	3.89	3.84	3.78	3.73	3.67
9	7.21	5.71	5.08	4.72	4.48	4.32	4.20	4.10	4.03	3.96	3.87	3.77	3.67	3.61	3.56	3.51	3.45	3.39	3.33
10	6.94	5.46	4.83	4.47	4.24	4.07	3.95	3.85	3.78	3.72	3.62	3.52	3.42	3.37	3.31	3.26	3.20	3.14	3.08
11	6.72	5.26	4.63	4.28	4.04	3.88	3.76	3.66	3.59	3.53	3.43	3.33	3.23	3.17	3.12	3.06	3.00	2.94	2.88
12	6.55	5.10	4.47	4.12	3.89	3.73	3.61	3.51	3.44	3.37	3.28	3.18	3.07	3.02	2.96	2.91	2.85	2.79	2.72
13	6.41	4.97	4.35	4.00	3.77	3.60	3.48	3.39	3.31	3.25	3.15	3.05	2.95	2.89	2.84	2.78	2.72	2.66	2.60
14	6.30	4.86	4.24	3.89	3.66	3.50	3.38	3.29	3.21	3.15	3.05	2.95	2.84	2.79	2.73	2.67	2.61	2.55	2.49
15	6.20	4.77	4.15	3.80	3.58	3.41	3.29	3.20	3.12	3.06	2.96	2.86	2.76	2.70	2.64	2.59	2.52	2.46	2.40
16	6.12	4.69	4.08	3.73	3.50	3.34	3.22	3.12	3.05	2.99	2.89	2.79	2.68	2.63	2.57	2.51	2.45	2.38	2.32
17	6.04	4.62	4.01	3.66	3.44	3.28	3.16	3.06	2.98	2.92	2.82	2.72	2.62	2.56	2.50	2.44	2.38	2.32	2.25
18	5.98	4.56	3.95	3.61	3.38	3.22	3.10	3.01	2.93	2.87	2.77	2.67	2.56	2.50	2.44	2.38	2.32	2.26	2.19
19	5.92	4.51	3.90	3.56	3.33	3.17	3.05	2.96	2.88	2.82	2.72	2.62	2.51	2.45	2.39	2.33	2.27	2.20	2.13
20	5.87	4.46	3.86	3.51	3.29	3.13	3.01	2.91	2.84	2.77	2.68	2.57	2.46	2.41	2.35	2.29	2.22	2.16	2.09
21	5.83	4.42	3.82	3.48	3.25	3.09	2.97	2.87	2.80	2.73	2.64	2.53	2.42	2.37	2.31	2.25	2.18	2.11	2.04
22	5.79	4.38	3.78	3.44	3.22	3.05	2.93	2.84	2.76	2.70	2.60	2.50	2.39	2.33	2.27	2.21	2.14	2.08	2.00
23	5.75	4.25	3.75	3.41	3.18	3.02	2.90	2.81	2.73	2.67	2.57	2.47	2.36	2.30	2.24	2.18	2.11	2.04	1.97
24	5.72	4.32	3.72	3.38	3.15	2.99	2.87	2.78	2.70	2.64	2.54	2.44	2.33	2.27	2.21	2.15	2.08	2.01	1.94
25	5.69	4.29	3.69	3.35	3.13	2.97	2.85	2.75	2.68	2.61	2.51	2.41	2.30	2.24	2.18	2.12	2.05	1.98	1.91
26	5.66	4.27	3.67	3.33	3.10	2.94	2.82	2.73	2.65	2.59	2.49	2.39	2.28	2.22	2.16	2.09	2.03	1.95	1.88
27	5.63	4.24	3.65	3.31	3.08	2.92	2.80	2.71	2.63	2.57	2.47	2.36	2.25	2.19	2.13	2.07	2.00	1.93	1.85
28	5.61	4.22	3.63	3.29	3.06	2.90	2.78	2.69	2.61	2.55	2.45	2.34	2.23	2.17	2.11	2.05	1.98	1.91	1.83
29	5.59	4.20	3.61	3.27	3.04	2.88	2.76	2.67	2.59	2.53	2.43	2.32	2.21	2.15	2.09	2.03	1.96	1.89	1.81
30	5.57	4.18	3.59	3.25	3.03	2.87	2.75	2.65	2.57	2.51	2.41	2.31	2.20	2.14	2.07	2.01	1.94	1.87	1.79
40	5.42	4.05	3.46	3.13	2.90	2.74	2.62	2.53	2.45	2.39	2.29	2.18	2.07	2.01	1.94	1.88	1.80	1.72	1.64
60	5.29	3.93	3.34	3.01	2.79	2.63	2.51	2.41	2.33	2.27	2.17	2.06	1.94	1.88	1.82	1.74	1.67	1.58	1.48
120	5.15	3.80	3.23	2.89	2.67	2.52	2.39	2.30	2.22	2.16	2.05	1.94	1.82	1.76	1.69	1.61	1.53	1.43	1.31
∞	5.02	3.69	3.12	2.79	2.57	2.41	2.29	2.19	2.11	2.05	1.94	1.83	1.71	1.64	1.57	1.48	1.39	1.27	1.00

[a]See following page for footnote.
[b]n_2 = degrees of freedom for denominator.

TABLE 9.6.4.4. *0.975 fractiles[a] of the F distribution associated with n_1 and n_2 degrees of freedom $F_{.975}(n_1,n_2)$*

[a]The following equation may be used to compute 0.975 fractiles of the F distribution in lieu of using table values:

$$F_{.975} \approx \exp\left[2\delta\left(1 + \frac{z^2 - 1}{3} - \frac{4\sigma^2}{3}\right) + 2\sigma z\left(1 + \frac{\sigma^2(z^2 - 3)}{6}\right)^{1/2}\right]$$

where

$z = 1.96$
$\delta = 0.5\,(1/(\gamma_2 - 1) - 1/(\gamma_1 - 1))$
$\sigma^2 = 0.5\,(1/(\gamma_2 - 1) + 1/(\gamma_1 - 1))$
γ_1 = degrees of freedom for numerator
γ_2 = degrees of freedom for denominator.

This approximation is accurate to within 0.4% for $\gamma_1 \geq 10$ and $\gamma_2 \geq 16$. See reference 9.6.4.4.

TABLE 9.6.4.5. *0.95 and 0.975 fractiles[a] of the t distribution association with df degrees of freedom*

df	$t_{.95}$	$t_{.975}$	df	$t_{.95}$	$t_{.975}$
1	6.314	12.706	21	1.721	2.080
2	2.920	4.303	22	1.717	2.074
3	2.353	3.182	23	1.714	2.069
4	2.132	2.776	24	1.711	2.064
5	2.015	2.571	25	1.708	2.060
6	1.943	2.447	26	1.706	2.056
7	1.895	2.365	27	1.703	2.052
8	1.860	2.306	28	1.701	2.048
9	1.833	2.262	29	1.699	2.045
10	1.812	2.228	30	1.697	2.042
11	1.796	2.201	40	1.684	2.021
12	1.782	2.179	50	1.676	2.009
13	1.771	2.160	60	1.671	2.000
14	1.761	2.145	80	1.664	1.990
15	1.753	2.131	100	1.660	1.984
16	1.746	2.120	120	1.658	1.980
17	1.740	2.110	200	1.653	1.972
18	1.734	2.101	500	1.648	1.965
19	1.729	2.093	∞	1.645	1.960
20	1.725	2.086			

[a]The following equations may be used to compute 0.95 and 0.975 fractiles of the t distribution in lieu of using table values:

$$t_{.95} \approx 1.645 + \exp\,[0.377 - 0.990\,\ln(\gamma) + 1.15/\gamma]$$

$$t_{.975} \approx 1.96 + \exp\,[0.779 - 0.980\,\ln(\gamma) + 1.57/\gamma]$$

where γ is the degrees of freedom (df). These approximations are accurate to within 0.5% for $\gamma \geq 4$.

TABLE 9.6.4.6. *Area Under the Normal Curve from - ∞ to Mean + Z Standard Deviations*[ab]

z_p	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8820
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319
1.5	.9332	.9345	.9257	.9270	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998

[a]For negative values of Z, subtract the tabular value of area from unity.
[b]The following equation may be used to compute the probabilities in lieu of using table values:

$$p \approx 0.5\ \{1-[1 + (A+Bz_p)^C]^D + [1 + (A-Bz_p)^C]^D\}$$

where

$A = 0.644693$
$B = 0.161984$
$C = 4.874$
$D = -6.158$

This approximation is accurate to within 0.07% of the true probabilities. See reference 9.6.4.3.

TABLE 9.6.4.7. *One-Sided Tolerance-Limit Factors for the Three-Parameter Weibull Distribution with 5 Percent Confidence*

Sample Size	V_A
10	-4.46
15	-4.77
20	-4.93
25	-5.12
30	-5.23
35	-5.32
40	-5.40
50	-5.51
75	-5.71
100	-5.82
150	-5.97
200	-6.05
300	-6.17
400	-6.23
500	-6.27
750	-6.29
1,000	-6.34
2,000	-6.39
5,000	-6.51
10,000	-6.55
∞	-6.65

Table 9.6.4.8. One-Sided Tolerance Factors for the Three-Parameter Weibull Distribution with 95 Percent Confidence

N	V_{99} for T_{99}			V_{90} for T_{90}		
	Uncensored	20% Censored	50% Censored	Uncensored	20% Censored	50% Censored
10	12.330	16.508	29.921	6.763	8.466	13.182
11	11.885	15.700	27.134	6.529	8.067	12.004
12	11.520	15.053	25.086	6.337	7.747	11.138
13	11.214	14.522	23.514	6.177	7.485	10.474
14	10.955	14.078	22.266	6.040	7.266	9.946
15	10.730	13.700	21.251	5.922	7.079	9.516
16	10.535	13.374	20.406	5.820	6.918	9.159
17	10.362	13.090	19.692	5.729	6.778	8.857
18	10.208	12.840	19.080	5.649	6.655	8.597
19	10.071	12.617	18.548	5.577	6.545	8.372
20	9.946	12.417	18.082	5.512	6.447	8.174
21	9.834	12.238	17.669	5.453	6.358	8.000
22	9.731	12.074	17.300	5.399	6.278	7.843
23	9.636	11.926	16.969	5.349	6.204	7.703
24	9.549	11.789	16.670	5.304	6.137	7.577
25	9.469	11.664	16.398	5.262	6.075	7.461
26	9.394	11.548	16.150	5.223	6.018	7.356
27	9.325	11.441	15.922	5.187	5.966	7.260
28	9.260	11.341	15.712	5.153	5.916	7.171
29	9.199	11.248	15.518	5.121	5.870	7.088
30	9.142	11.160	15.338	5.091	5.828	7.012
31	9.089	11.078	15.170	5.063	5.787	6.941
32	9.038	11.002	15.014	5.037	5.750	6.875
33	8.990	10.929	14.868	5.012	5.714	6.813
34	8.945	10.861	14.730	4.989	5.680	6.754
35	8.902	10.796	14.601	4.966	5.648	6.700
36	8.862	10.735	14.479	4.945	5.618	6.648
37	8.823	10.676	14.364	4.925	5.590	6.599
38	8.786	10.621	14.256	4.906	5.562	6.553
39	8.751	10.568	14.153	4.887	5.537	6.510
40	8.717	10.518	14.055	4.870	5.512	6.468
41	8.685	10.470	13.962	4.853	5.488	6.429
42	8.654	10.424	13.873	4.837	5.466	6.391
43	8.624	10.380	13.789	4.822	5.444	6.356
44	8.596	10.338	13.708	4.807	5.423	6.321
45	8.569	10.298	13.631	4.793	5.404	6.289
46	8.543	10.259	13.558	4.779	5.385	6.258
47	8.517	10.221	13.487	4.766	5.366	6.228
48	8.493	10.186	13.419	4.753	5.349	6.199

Table 9.6.4.8. One-Sided Tolerance Factors for the Three-Parameter Weibull Distribution with 95 Percent Confidence (Continued)

N	V_A for T_{99}			V_B for T_{90}		
	Uncensored	20% Censored	50% Censored	Uncensored	20% Censored	50% Censored
49	8.469	10.151	13.354	4.741	5.332	6.171
50	8.447	10.118	13.292	4.729	5.315	6.145
51	8.425	10.086	13.232	4.718	5.300	6.119
52	8.404	10.055	13.174	4.707	5.284	6.095
53	8.383	10.025	13.118	4.696	5.270	6.071
54	8.364	9.996	13.064	4.686	5.255	6.048
55	8.344	9.968	13.012	4.676	5.242	6.026
56	8.326	9.940	12.962	4.666	5.228	6.005
57	8.308	9.914	12.914	4.657	5.216	5.985
58	8.290	9.889	12.867	4.648	5.203	5.965
59	8.273	9.864	12.822	4.639	5.191	5.946
60	8.257	9.840	12.778	4.631	5.179	5.927
61	8.241	9.817	12.735	4.622	5.168	5.909
62	8.225	9.794	12.694	4.614	5.157	5.892
63	8.210	9.772	12.654	4.606	5.146	5.875
64	8.195	9.751	12.615	4.599	5.135	5.858
65	8.181	9.730	12.577	4.591	5.125	5.842
66	8.167	9.709	12.541	4.584	5.115	5.827
67	8.153	9.690	12.505	4.577	5.106	5.811
68	8.140	9.671	12.470	4.570	5.096	5.797
69	8.127	9.652	12.436	4.563	5.087	5.782
70	8.114	9.634	12.404	4.557	5.078	5.769
71	8.102	9.616	12.372	4.550	5.069	5.755
72	8.090	9.598	12.340	4.544	5.061	5.742
73	8.078	9.581	12.310	4.538	5.053	5.729
74	8.067	9.565	12.280	4.532	5.044	5.716
75	8.055	9.549	12.252	4.526	5.036	5.704
76	8.044	9.533	12.223	4.520	5.029	5.692
77	8.034	9.517	12.196	4.515	5.021	5.681
78	8.023	9.502	12.169	4.509	5.014	5.669
79	8.013	9.487	12.143	4.504	5.006	5.658
80	8.003	9.473	12.117	4.499	4.999	5.647
81	7.993	9.459	12.092	4.494	4.992	5.637
82	7.983	9.445	12.067	4.489	4.986	5.626
83	7.974	9.431	12.043	4.484	4.979	5.616
84	7.964	9.418	12.020	4.479	4.973	5.606
85	7.955	9.405	11.997	4.474	4.966	5.596
86	7.946	9.392	11.975	4.470	4.960	5.587
87	7.938	9.380	11.952	4.465	4.954	5.578
88	7.929	9.367	11.931	4.461	4.948	5.568
89	7.921	9.355	11.910	4.456	4.942	5.559

Table 9.6.4.8. One-Sided Tolerance Factors for the Three-Parameter Weibull Distribution with 95 Percent Confidence (Continued)

N	V_A for T_{99}			V_B for T_{90}		
	Uncensored	20% Censored	50% Censored	Uncensored	20% Censored	50% Censored
90	7.912	9.344	11.889	4.452	4.936	5.551
91	7.904	9.332	11.869	4.448	4.930	5.542
92	7.896	9.321	11.849	4.444	4.925	5.534
93	7.888	9.309	11.829	4.440	4.919	5.525
94	7.881	9.298	11.810	4.436	4.914	5.517
95	7.873	9.288	11.791	4.432	4.909	5.509
96	7.866	9.277	11.773	4.428	4.904	5.502
97	7.859	9.267	11.755	4.424	4.899	5.494
98	7.851	9.257	11.737	4.420	4.894	5.486
99	7.844	9.247	11.720	4.417	4.889	5.479
100	7.837	9.237	11.703	4.413	4.884	5.472
102	7.824	9.217	11.669	4.406	4.874	5.458
104	7.811	9.199	11.637	4.399	4.865	5.444
106	7.798	9.181	11.606	4.393	4.857	5.431
108	7.786	9.163	11.576	4.387	4.848	5.418
110	7.774	9.146	11.546	4.380	4.840	5.406
112	7.762	9.130	11.518	4.374	4.832	5.394
114	7.751	9.114	11.491	4.369	4.824	5.382
116	7.740	9.099	11.464	4.363	4.816	5.371
118	7.729	9.084	11.439	4.357	4.809	5.360
120	7.719	9.069	11.414	4.352	4.802	5.349
122	7.709	9.055	11.389	4.347	4.795	5.339
124	7.699	9.041	11.366	4.342	4.788	5.329
126	7.690	9.028	11.343	4.337	4.782	5.319
128	7.680	9.015	11.320	4.332	4.775	5.310
130	7.671	9.002	11.299	4.327	4.769	5.301
132	7.663	8.989	11.278	4.323	4.763	5.292
134	7.654	8.977	11.257	4.318	4.757	5.283
136	7.646	8.965	11.237	4.314	4.751	5.275
138	7.637	8.954	11.217	4.310	4.746	5.266
140	7.629	8.943	11.198	4.306	4.740	5.258
142	7.622	8.932	11.180	4.302	4.735	5.250
144	7.614	8.921	11.161	4.298	4.730	5.243
146	7.606	8.910	11.144	4.294	4.724	5.235
148	7.599	8.900	11.126	4.290	4.719	5.228
150	7.592	8.890	11.109	4.286	4.715	5.221
152	7.585	8.880	11.093	4.283	4.710	5.214
154	7.578	8.871	11.077	4.279	4.705	5.207
156	7.571	8.861	11.061	4.276	4.700	5.200
158	7.565	8.852	11.045	4.272	4.696	5.194
160	7.558	8.843	11.030	4.269	4.692	5.187

Table 9.6.4.8. One-Sided Tolerance Factors for the Three-Parameter Weibull Distribution with 95 Percent Confidence (Continued)

N	V_A for T_{99}			V_B for T_{90}		
	Uncensored	20% Censored	50% Censored	Uncensored	20% Censored	50% Censored
162	7.552	8.834	11.015	4.266	4.687	5.181
164	7.546	8.826	11.001	4.263	4.683	5.175
166	7.540	8.817	10.987	4.260	4.679	5.169
168	7.534	8.809	10.973	4.257	4.675	5.163
170	7.528	8.801	10.959	4.254	4.671	5.157
172	7.522	8.793	10.946	4.251	4.667	5.151
174	7.517	8.785	10.932	4.248	4.663	5.146
176	7.511	8.777	10.920	4.245	4.659	5.140
178	7.506	8.770	10.907	4.242	4.656	5.135
180	7.501	8.762	10.894	4.239	4.652	5.130
182	7.495	8.755	10.882	4.237	4.649	5.125
184	7.490	8.748	10.870	4.234	4.645	5.120
186	7.485	8.741	10.859	4.231	4.642	5.115
188	7.480	8.734	10.847	4.229	4.638	5.110
190	7.475	8.727	10.836	4.226	4.635	5.105
192	7.471	8.720	10.825	4.224	4.632	5.100
194	7.466	8.714	10.814	4.221	4.629	5.096
196	7.461	8.707	10.803	4.219	4.625	5.091
198	7.457	8.701	10.793	4.217	4.622	5.087
200	7.452	8.695	10.782	4.214	4.619	5.082
204	7.443	8.683	10.762	4.210	4.613	5.074
208	7.435	8.671	10.742	4.206	4.608	5.066
212	7.427	8.659	10.724	4.201	4.602	5.058
216	7.419	8.648	10.705	4.197	4.597	5.050
220	7.411	8.638	10.687	4.193	4.591	5.042
224	7.404	8.627	10.670	4.189	4.586	5.035
228	7.396	8.617	10.653	4.186	4.581	5.028
232	7.389	8.607	10.637	4.182	4.576	5.021
236	7.382	8.597	10.621	4.178	4.572	5.014
240	7.375	8.588	10.606	4.175	4.567	5.008
244	7.369	8.579	10.591	4.171	4.563	5.002
248	7.363	8.570	10.576	4.168	4.559	4.995
252	7.356	8.562	10.562	4.165	4.554	4.990
256	7.350	8.553	10.548	4.162	4.550	4.984
260	7.344	8.545	10.535	4.159	4.546	4.978
264	7.339	8.537	10.522	4.156	4.542	4.972
268	7.333	8.529	10.509	4.153	4.539	4.967
272	7.327	8.522	10.497	4.150	4.535	4.962
276	7.322	8.514	10.485	4.147	4.531	4.957
280	7.317	8.507	10.473	4.145	4.528	4.952
284	7.312	8.500	10.461	4.142	4.524	4.947

Table 9.6.4.8. One-Sided Tolerance Factors for the Three-Parameter Weibull Distribution with 95 Percent Confidence (Continued)

N	V_A for T_{99}			V_B for T_{90}		
	Uncensored	20% Censored	50% Censored	Uncensored	20% Censored	50% Censored
288	7.307	8.493	10.450	4.139	4.521	4.942
292	7.302	8.486	10.439	4.137	4.518	4.937
296	7.297	8.479	10.428	4.134	4.514	4.933
300	7.292	8.473	10.417	4.132	4.511	4.928
310	7.281	8.457	10.392	4.126	4.504	4.917
320	7.270	8.442	10.368	4.121	4.496	4.907
330	7.260	8.428	10.345	4.115	4.489	4.898
340	7.250	8.415	10.323	4.110	4.483	4.888
350	7.241	8.402	10.302	4.106	4.477	4.880
360	7.232	8.390	10.282	4.101	4.471	4.871
370	7.223	8.378	10.263	4.097	4.465	4.863
380	7.215	8.367	10.245	4.092	4.459	4.855
390	7.207	8.356	10.227	4.088	4.454	4.848
400	7.200	8.346	10.211	4.084	4.449	4.841
425	7.182	8.321	10.172	4.075	4.437	4.825
450	7.166	8.299	10.136	4.067	4.427	4.810
475	7.151	8.279	10.104	4.060	4.417	4.796
500	7.138	8.261	10.074	4.053	4.408	4.783
525	7.125	8.244	10.047	4.046	4.400	4.772
550	7.114	8.228	10.021	4.040	4.392	4.761
575	7.103	8.213	9.997	4.035	4.385	4.751
600	7.093	8.199	9.975	4.030	4.378	4.742
625	7.083	8.186	9.955	4.025	4.372	4.733
650	7.074	8.174	9.935	4.020	4.366	4.725
675	7.066	8.162	9.917	4.016	4.360	4.717
700	7.058	8.152	9.900	4.012	4.355	4.710
725	7.050	8.141	9.884	4.008	4.350	4.703
750	7.043	8.132	9.868	4.004	4.345	4.697
775	7.037	8.123	9.854	4.001	4.341	4.690
800	7.030	8.114	9.840	3.998	4.337	4.685
825	7.024	8.106	9.827	3.994	4.332	4.679
850	7.018	8.098	9.814	3.991	4.329	4.674
875	7.013	8.090	9.802	3.989	4.325	4.669
900	7.007	8.083	9.791	3.986	4.321	4.664
925	7.002	8.076	9.780	3.983	4.318	4.659
950	6.997	8.069	9.769	3.981	4.315	4.655
975	6.993	8.063	9.759	3.978	4.312	4.651
1000	6.988	8.057	9.750	3.976	4.309	4.646
1100	6.972	8.034	9.714	3.968	4.298	4.632
1200	6.957	8.015	9.684	3.960	4.288	4.619
1300	6.945	7.998	9.657	3.954	4.280	4.608

Table 9.6.4.8. One-Sided Tolerance Factors for the Three-Parameter Weibull Distribution with 95 Percent Confidence (Continued)

N	V_A for T_{99}			V_B for T_{90}		
	Uncensored	20% Censored	50% Censored	Uncensored	20% Censored	50% Censored
1400	6.934	7.983	9.633	3.948	4.273	4.597
1500	6.924	7.969	9.612	3.943	4.266	4.589
1600	6.914	7.957	9.593	3.938	4.260	4.580
1700	6.906	7.946	9.575	3.934	4.255	4.573
1800	6.899	7.936	9.560	3.930	4.250	4.567
1900	6.892	7.926	9.545	3.927	4.246	4.560
2000	6.886	7.918	9.532	3.923	4.241	4.555
3000	6.841	7.858	9.438	3.901	4.212	4.515
4000	6.815	7.822	9.383	3.887	4.195	4.492
5000	6.797	7.798	9.346	3.878	4.183	4.477
6000	6.784	7.781	9.319	3.871	4.175	4.465
7000	6.773	7.767	9.298	3.866	4.168	4.456
8000	6.765	7.756	9.281	3.862	4.163	4.449
9000	6.758	7.747	9.267	3.859	4.159	4.443
10000	6.753	7.739	9.255	3.856	4.155	4.438
15000	6.733	7.713	9.215	3.846	4.142	4.422
20000	6.722	7.698	9.192	3.840	4.135	4.412
25000	6.714	7.688	9.176	3.836	4.130	4.405
30000	6.708	7.680	9.164	3.833	4.126	4.400

The values provided in Table 9.6.4.8 are calculated by the following formula:

$$d^{-1}\left\{ ck_n\frac{\left(a_{11}+2a_{01}g(p)+a_{00}g(p)^2+c^2(a_{01}^2-a_{00}a_{11})/n\right)^{1/2}}{1-c^2a_{00}/n} + n^{1/2}\left[g(p)-k_n\frac{g(p)+c^2a_{01}/n}{1-c^2a_{00}/n}\right]\right\}$$

where d=.7796968, c=1.645, $k_n=(n/(n-1))^{1/2}$, p is the percentile being estimated (T_{99}: p=.01, T_{90}: p=.10), and g(p)=0.45 + 0.7797 ln(-ln(1-p)). The constants a_{00} a_{01}, and a_{11} depend on the level of censoring, and are given below. The statistical methodology employed here is discussed in detail in Reference [9.6.4.8].

	Uncensored	20% Censored	50% Censored
a_{00}	-0.6079	0.9282	1.7162
a_{01}	-0.4740	-0.4562	-0.0428
a_{11}	0.9775	0.9841	1.2169

TABLE 9.6.4.8. *One-Sided Tolerance-Limit Factors*[ab] *for the Three-Parameter Weibull Distribution With 95 Percent Confidence (Continued)*

N	V_A	V_B	N	V_A	V_B
4000	6.815	3.887	9000	6.759	3.859
5000	6.797	3.878	10000	6.753	3.856
6000	6.784	3.872	15000	6.734	3.846
7000	6.774	3.866	20000	6.722	3.840
8000	6.766	3.862	∞	6.649	3.803

[a] Values for sample sizes less than or equal to 400 are exact. Values for sample sizes greater than 400 are based on a large sample approximation. The entries in this table were reproduced with the permission of the Boeing Computer Services Company, see Reference 9.6.4.8.

[b] The following equations may be used to compute the V_A and V_B values in lieu of using table values:

$$V_A = 6.649 + \exp[2.55 - 0.526 \ln(n) + 4.76/n]$$

$$V_B = 3.803 + \exp[1.79 - 0.516 \ln(n) + 5.1/n]$$

These approximations are accurate to within 0.5% of the table values for n greater than or equal to 16.

TABLE 9.6.4.9 *Quantities of the F Distribution Associated with Degrees of Freedom*

n_1 - degrees of freedom for numerator

n_1 / n_2	1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40	60	120	∞
1	161.45	199.50	215.71	224.58	230.16	233.99	236.77	238.88	240.54	241.88	243.91	245.95	248.01	249.05	250.10	251.14	252.20	253.25	254.31
2	18.51	19.00	19.16	19.25	19.30	19.33	19.35	19.37	19.38	19.40	19.41	19.43	19.45	19.45	19.46	19.47	19.48	19.49	19.51
3	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81	8.79	8.74	8.70	8.66	8.64	8.62	8.59	8.57	8.55	8.53
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96	5.91	5.86	5.80	5.77	5.75	5.72	5.69	5.66	5.63
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77	4.74	4.68	4.62	4.56	4.53	4.50	4.46	4.43	4.40	4.37
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06	4.00	3.94	3.87	3.84	3.81	3.77	3.74	3.70	3.67
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.64	3.57	3.51	3.44	3.41	3.38	3.34	3.30	3.27	3.23
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.35	3.28	3.22	2.15	3.12	3.08	3.04	3.01	2.97	2.93
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.14	3.07	3.01	2.94	2.90	2.86	2.83	2.79	2.75	2.71
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.98	2.91	2.85	2.77	2.74	2.70	2.66	2.62	2.58	2.54
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.85	2.79	2.72	2.65	2.61	2.57	2.53	2.49	2.45	2.40
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80	2.75	2.69	2.62	2.54	2.51	2.47	2.43	2.38	2.34	2.30
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71	2.67	2.60	2.53	2.46	2.42	2.38	2.34	2.30	2.25	2.21
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65	2.60	2.53	2.46	2.39	2.35	2.31	2.27	2.22	2.18	2.13
15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59	2.54	2.48	2.40	2.33	2.29	2.25	2.20	2.16	2.11	2.07
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	2.49	2.42	2.35	2.28	2.24	2.19	2.15	2.11	2.06	2.01
17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49	2.45	2.38	2.31	2.23	2.19	2.15	2.10	2.06	2.01	1.96
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46	2.41	2.34	2.27	2.19	2.15	2.11	2.06	2.02	1.97	1.92
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42	2.38	2.31	2.23	2.16	2.11	2.07	2.03	1.98	1.93	1.88
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39	2.35	2.28	2.20	2.12	2.08	2.04	1.99	1.95	1.90	1.84
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37	2.32	2.25	2.18	2.10	2.05	2.01	1.96	1.92	1.87	1.81
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34	2.30	2.23	2.15	2.07	2.03	1.98	1.94	1.89	1.84	1.78
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32	2.27	2.20	2.13	2.05	2.01	1.96	1.91	1.86	1.81	1.76
24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	2.25	2.18	2.11	2.03	1.98	1.94	1.89	1.84	1.79	1.73
25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28	2.24	2.16	2.09	2.01	1.96	1.92	1.87	1.82	1.77	1.71
26	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27	2.22	2.15	2.07	1.99	1.95	1.90	1.85	1.80	1.75	1.69
27	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25	2.20	2.13	2.06	1.97	1.93	1.88	1.84	1.79	1.73	1.67
28	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24	2.19	2.12	2.04	1.96	1.91	1.87	1.82	1.77	1.71	1.65
29	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.22	2.18	2.10	2.03	1.94	1.90	1.85	1.81	1.75	1.70	1.64
30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21	2.16	2.09	2.01	1.93	1.89	1.84	1.79	1.74	1.68	1.62
40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12	2.08	2.00	1.92	1.84	1.79	1.74	1.69	1.64	1.58	1.51
60	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04	1.99	1.92	1.84	1.75	1.70	1.65	1.59	1.53	1.47	1.39
12	3.92	3.07	2.68	2.45	2.29	2.18	2.09	2.02	1.96	1.91	1.83	1.75	1.66	1.61	1.55	1.50	1.43	1.35	1.25
0	3.84	3.00	2.61	2.37	2.21	2.10	2.01	1.94	1.88	1.83	1.75	1.67	1.57	1.52	1.46	1.39	1.32	1.22	1.00
∞																			

9.6.5 ESTIMATION PROCEDURES FOR THE WEIBULL DISTRIBUTION.—This section describes procedures required for modeling data with the three-parameter Weibull distribution. Section 9.6.5.1 describes methods for estimating the threshold parameter, τ. Section 9.6.5.2 describes methods for estimating the shape and scale parameters, β and α, respectively. Both procedures permit estimation with upper tail censored data. For a good exposition of such methods, see Reference 9.6.1.2(a).

9.6.5.1 *Estimating the Lower Confidence Bound on Weibull Population Threshold Based on Censored or Uncensored Data.*—This section describes a method for obtaining a lower confidence bound $\tau(\theta)$ on the threshold parameter for a three-parameter Weibull distribution, where θ $(0 < \theta < 1)$ is the confidence coefficient. For further details, see References 9.2.8(a) and 9.2.8(b). This procedure can be applied with upper tail censoring. In what follows, p represents the proportion of the upper tail which is censored.

Let K equal the greatest integer less than or equal to min{4n/15, (1-p)n/3}. Define the function $R(\tau)$ by

$$R(\tau)=\sum_{i=K+1}^{3K-2} L_i(\tau)/\sum_{i=1}^{3K-2} L_i(\tau)$$

where

$$L_i(\tau)=\frac{1}{D_i}\left[\ln\left(X_{(i+1)}-\tau\right) - \ln\left(X_{(i)}-\tau\right)\right]$$

with

$$D_1 = n \ln\left(1 + \frac{1}{n-1}\right)$$

$$D_2 = \binom{n}{2} \ln\left(1+\frac{1}{n(n-2)}\right),$$

$$D_3 = \binom{n}{3} \ln\left(1+\frac{2n - 3}{(n-1)^3\ (n-3)}\right),$$

$$D_4 = \binom{n}{4} \ln\left(1+\frac{6n^4 - 48n^3 + 140n^2 - 176n + 81}{n(n-4)\ (n-2)^6}\right),$$

$$D_i = \ln\left[-\ln\left(1 - \frac{i + 0.05}{n + 0.25}\right)\right] - \ln\left[-\ln\left(1 - \frac{i - 0.05}{n - 0.25}\right)\right]$$

for i=5,6,...,3K-2. Finally, let $H=0.999999X_{(1)}$ and L=0.

Let Beta(a,b,p) denote the pth percentile of the beta distribution with parameters a and b. (A computational formula for Beta(a,b,p) is provided in Section 9.6.5.3.) If $R(L) \leq$ Beta(2k-2, k, θ), then let $\tau(\theta)$ = L. If $R(H) \geq$ Beta(2k-2, k, θ), then let $\tau_{20}(\theta)$ = H. Otherwise, $\tau(\theta)$ is taken to be the solution to the equation $R(\tau)$ = Beta(2k-2, k, θ). The following describes a method for solving this equation by a binary search. The function $R(\tau)$ is a monotonically decreasing continuous function of τ. If the solution of the equation $R(\tau)$ = b is necessary, then R(L) > b and R(H) <b. Thus, the only solution to $R(\tau)$ = b falls in the interval (L,H). A simple method for finding the solution is as follows: Calculate R(M) where M = (L+H)/2. If R(M) = b, then the solution is τ = M. If R(M) > b, then let L = M. If R(M) < b, then let H = M. The new interval (L,H) still contains the solution to $R(\tau)$ = b but is only half as long as the old interval. Calculate a new M-value and begin the process of interval halving again. The process is repeated until $H - L \leq 2X/10^6$. The solution to $R(\tau)$ = b is then taken to be M = (L + H)/2 and the solution is in error by at most $X/10^6$.

9.6.5.2 *Estimating the Shape and Scale Parameters for the Weibull Distribution.*—This section describes methods for estimation of the shape and scale parameters of the two-parameter Weibull distribution based on data which may be censored in the upper tail. The assumption is made here that if the data are censored, then only the r smallest observations in the sample are observed ($1 \leq r \leq n$), where r is some pre-specified number (often based on a percentage); this is called Type II censoring. Thus, the input to this procedure is a total sample size, n, a censored sample size, r, and the censored sample observations $X_{(1)}, \ldots, X_{(r)}$. We use the notation:

$$\sum_{i=1}^{r} * w_i = \sum_{i=1}^{r} w_i + (n-r)\, w_r$$

for any sequence $w_1, \ldots, w_r$. Define

$$g(\beta) = \sum_{i=1}^{r} * X_{(i)}^{\beta} \ln X_{(i)} \Big/ \sum_{i=1}^{r} * X_{(i)}^{\beta} - \frac{1}{\beta} - \frac{1}{r} \sum_{i=1}^{r} \log X_{(i)}$$

The shape parameter estimate, β, is the solution to the equation $g(\beta) = 0$. The function $G(\beta)$ is a monotonically increasing continuous function of β. A simple method for finding the solution is as follows. Let S_y denote the standard deviation of $Y_1, \ldots, Y_r$ where $Y_i = \ln(X_i - \tau)$ for i=1, ..., r. Calculate $I = 1.28/S_y$ as an initial guess at the solution and calculate G(I). If G(I) > 0, then find the smallest positive integer k such that $G(I/2^k) < 0$ and let $L = I/2^k$ and $H = 2^k/I$. In either case, the interval (L, H) contains the solution to $G(\beta) = 0$. Now calculate G(M) where M = L + H)/2. If G(M) = 0, then the solution is β = M. If G(M) > 0, then let H = M. If G(M) < 0, then let L = M. The new interval (L, H) still contains the solution to $G(\beta) = 0$ but is only half as long as the old interval. Calculate a new M-value and begin the process of interval halving again. The process is repeated until $H - L < 2I/10^6$. The solution to $G(\beta) = 0$ is then taken to be M = (L + H)/2. The solution is in error by the most $I/10^6$.

Once β has been determined, the scale parameter estimate is defined by

$$\alpha = \left(\frac{1}{r} \sum_{i=1}^{r} * X_{(i)}^{\beta}\right)^{\frac{1}{\beta}} .$$

9.6.5.3 *Beta Distribution Percentile Algorithm.*—The following algorithm can be used to calculate the Beta(a,b,p), the pth percentile of a beta distribution with parameters a and b ($0 < p < 1$, $0 < a$, $0 < b$). The cumulative beta distribution function I(a,b,x) has the form

$$I(a,b,x) = \frac{1}{Beta(a,b)} \int_0^x t^{a-b} (1-t)^{b-1} \, dt$$

where

$$Beta(a,b) = \int_0^1 t^{a-b} (1-t)^{b-1} \, dt.$$

The percentile, Beta(a,b,p), is the value of x for which I(a,b,x) = p. That is, I(a,b,Beta(a,b,p)) = p. This value is found by a simple binary search of I(a,b,x) over the range $0 \le x \le 1$. Calculating I(a,b,x) calls upon a formula for ln $\Gamma(\alpha)$, provided below, and a subroutine which is provided in the form of pseudocode. The subroutine calculates the cumulative beta distribution function, I(a,b,x), using Lentz's method for continued fractions (see reference 9.6.5.1).

In what follows, use this formula to compute ln $\Gamma(x)$ (Lanczos expansion for $\Gamma(x)$)

$$\ln \Gamma(x) = \left(x+\frac{1}{2}\right)\ln\left(x+\frac{11}{2}\right) - \left(x+\frac{11}{2}\right) + \ln\left[\sqrt{2\pi}\left(76.18 - \frac{86.50}{x} + \frac{24.01}{x+1} - \frac{1.231}{x+2} + \frac{0.1209}{x+3} - \frac{0.5364e^{-5}}{x+4}\right)\right]$$

Let $x_{low} = 0$, $x_{high} = 1$.

while $((x_{high} - x_{low}) > 10^{-6})$ do { (Binary search for solution of I(a,b,x) = p)

$x = (x_{high} + x_{low})/2$

$C = \exp[\ln \Gamma(a+b) - \ln \Gamma(a) - \ln \Gamma(b) + a \ln x + b \ln(1-x)]$

if $x < \frac{a+1}{a+b+2}$ then $I = \frac{C}{a} \cdot L(a,b,x)$ (See algorithm below to compute L(a,b,x))

else $I = 1 - \frac{C}{b} \cdot L(b,a,1-x)$

if $I > p$ then $x_{high} = x$

else $x_{low} = x$

} (end while loop)

When the loop is completed, the solution is

$$Beta(a,b,p) = (x_{high}+x_{low})/2.$$

To compute L(a,b,x) use the following algorithm:

Let MAX = 100, let $C_1 = 1$, let and let

$$d_1 = \frac{a + b}{a + 1} x$$

Let $\Delta_{old} = C_1 D_1$.

$$D_1 = \frac{1}{1 + d_1}$$

For m = 1 to MAX {

$$d_{2m} = \frac{m(b-m)x}{(a+2m-1)(a+2m)}$$

$$\frac{1}{D_{2m}} = \frac{1}{1+d_{2m}/D_{2m-1}}$$

$$C_{2m} = 1 + d_{2m}/C_{2m-1}$$

$$d_{2m+1} = -\frac{(a+m)(a+b+m)x}{(a+2m)(a+2m+1)}$$

$$\frac{1}{D_{2m+1}} = \frac{1}{1 + d_{2m+1}/D_{2m}}$$

$$C_{2m+1} = 1 + d_{2m+1}/C_{2m}$$

Let $\Delta_{new} = C_{2m} D_{2m} C_{2m+1} D_{2m+1} \Delta_{old}$

If $(|\Delta_{new} - \Delta_{old}| < 10^{-6})$
then m = Δ_{new}

else $\Delta_{old} = \Delta_{new}$

} (end For loop)

Let L (a,b,x) = Δ_{new}.

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A.0 Glossary

A.1 ABBREVIATIONS (also see Sections 1.2.1, 9.2.2, 9.3.4.3, 9.3.6.2, 9.4.1.2, 9.5.1.2, and 9.6).

a — Amplitude; crack or flaw dimension; measure of flaw size, inches.
a_c — Critical half crack length.
a_o — Initial half crack length.
A — Area of cross section, square inches; ratio of alternating stress to mean stress; subscript "axial"; A basis for mechanical-property values (see Section 1.4.1.1 or Section 9.2.2.1); "A" ratio, loading amplitude/mean load; or area.
A_ε — Strain "A" ratio, strain amplitude/mean strain.
A_i — Model parameter.
AD — Anderson-Darling test statistic, computed in goodness-of-fit tests for normality or Weibullness.
AISI — American Iron and Steel Institute.
AMS — Aerospace Materials Specification (published by Society of Automotive Engineers, Inc.).
Ann — Annealed.
AN — Air Force-Navy Aeronautical Standard.
ASTM — American Society for Testing and Materials.
b — Width of sections; subscript "bending".
br — Subscript "bearing".
B — Biaxial ratio (see Equation 1.3.2.8); B-basis for mechanical-property values (see Section 1.4.1.1 oe Section 9.2.2.1).
Btu — British thermal unit(s).
BUS — Individual or typical bearing ultimate strength.
BYS — Individual or typical bearing yield strength.
c — Fixity coefficient for columns; subscript "compression".
cpm — Cycles per minute.
C — Specific heat; Celsius; Constant.
CC — Center cracked.
CEM — Consumable electrode melted.
CRES — Corrosion resistant steel (stainless steel).
CT — Compact tension.
CYS — Individual or typical compressive yield strength.
d — Mathematical operator denoting differential.
D or d — Diameter, or Durbin Watson statistic; hole or fastener diameter; dimpled hole.
df — Degrees of freedom.
e — Elongation in percent, a measure of the ductility of a material based on a tension test; unit deformation or strain; subscript "fatigue or endurance"; the minimum distance from a hole. center to the edge of the sheet; Engineering strain.
e_e — Elastic strain.
e_p — Plastic strain.
e/D — Ratio of edge distance to hole diameter (bearing strength).
E — Modulus of elasticity in tension; average ratio of stress to strain for stress below proportional limit.
E_c — Modulus of elasticity in compression; average ratio of stress to strain below proportional limit.
E_s — Secant modulus of elasticity.
E_t — Tangent modulus of elasticity.
ELI — Extra low interstitial (grade of titanium alloy).

ER — Equivalent round.
ESR — Electro-slag remelted.
f — Internal (or calculated) stress; stress applied to the gross flawed section; creep stress.
f_b — Internal (or calculated) primary bending stress.
f_c — Internal (or calculated) compressive stress; maximum stress at fracture: gross stress limit (for screening elastic fracture data).
f_{pl} — Proportional limit.
f_s — Internal (or calculated) shear stress.
f_t — Internal (or calculated) tensile stress.
ft — Foot: feet.
F — Allowable stress; Fahrenheit; Ratio of two sample variances.
F_A — Axial stress.
F_b — Allowable bending stress; modulus of rupture in bending.
F_{bru} — Allowable ultimate bearing stress.
F_{bry} — Allowable bearing yield stress.
F_c — Allowable column stress.
F_{cc} — Allowable crushing or crippling stress (upper limit of column stress for local failure).
F_{cu} — Ultimate compressive stress.
F_{cy} — Allowable compressive yield stress at which permanent strain equals 0.002.
F_H — Hoop stress.
F_s — Allowable shear stress.
F_{sp} — Proportional limit in shear.
F_{st} — Modulus of rupture in torsion.
F_{su} — Allowable ultimate stress in pure shear (this value represents the average shear stress over the cross section).
F_{tp} — Proportional limit in tension.
F_{tu} — Allowable tensile ultimate stress.
F_{ty} — Allowable tensile yield stress at which permanent strain equals 0.002.
g — Gram(s).
G — Modulus of rigidity (shear modulus).
Gpa — Gigapascal(s).
hr — Hour(s).
H — Subscript "hoop".
i — Slope (due to bending) of neutral plane of a beam, in radians (1 radian = 57.3 degrees).
in. — Inch(es).
I — Moment of inertia.
J — Torsion constant (= Ip for round tubes); Joule.
k — Tolerance limit factor for the normal distribution and the specified probability, confidence, and degrees of freedom; Strain at unit stress.
$k_{99,90}$ — K to A basis or B basis, respectively (see Section 9.2.7.2).
ksi — Kips (1,000 pounds) per square inch.
K — A constant, generally empirical; thermal conductivity; stress intensity; Kelvin; correction factor.
K_{app} — Apparent plane stress fracture toughness or residual strength.
K_c — Critical plane stress fracture toughness, a measure of fracture toughness at point of crack growth instability.
K_f — Fatigue notch factor, or fatigue strength reduction factor.
K_{Ic} — Plane strain fracture toughness.
K_N — Empirically calculated fatigue notch factor.
K_t — Theoretical stress concentration factor.

lb — Pound.
ln — Natural (base e) logarithm.
log — Base 10 logarithm.
L — Length; subscript "lateral"; longitudinal (grain direction).
LT — Long transverse (grain direction).
m — Subscript "mean"; metre; slope.
mm — Millimeter(s).
M — Applied moment or couple, usually a bending moment.
Mc — Machine countersunk.
Mg — Megagram(s).
MIG — Metal-inert-gas (welding).
MPa — Megapascal(s).
MS — Military Standard.
M.S. — Margin of safety.
M(T) — Middle tension cracked.
n — Number of individual measurements or pairs of measurements; subscript "normal"; cycles applied to failure; shape parameter for the standard stress-strain surve (Ramberg-Osgood parameter); number of fatigue cycles endured.
N — Fatigue life, number of cycles to failure; Newton; normalized.
N_f — Fatigue life, cycles to failure.
N_i* — Fatigue life, cycles to initiation.
N_t* — Transition fatigue life where plastic and elastic strains are equal.
NAS — National Aerospace Standard.
p — Subscript "polar"; subscript "proportional limit".
psi — Pounds per square inch.
P — Load; applied load (total, not unit, load); exposure parameter; probability
P_a — Load amplitude.
P_m — Mean load.
P_{max} — Maximum load.
P_{min} — Minimum load.
Pu — Test ultimate load, pounds per fastener.
Py — Test yield load, pounds per fastener.
q — Fatigue notch sensitivity.
Q — Static moment of a cross section.
Q&T — Quenched and tempered.
r — Radius; root radius; reduced ratio (regression analysis); ratio of two pair measurements; rank of test point within a sample; average ratio of paired measurements.
R — Load (stress) ratio, or residual (observed minus predicted value); stress ratio, ratio of minimum stress to maximum stress in a fatigue cycle; reduced ratio.
R_b — Stress ratio in bending.
R_c — Stress ratio in compression; Rockwell hardness - C scale.
R_ε — Strain ratio, $\varepsilon_{min}/\varepsilon_{max}$.
R_s — Stress ratio in shear or torsion; ratio of applied load to allowable shear load.
R_t — Ratio of applied load to allowable tension load.
RA — Reduction of area.
R.H. — Relative humidity.
RMS — Root-mean-square (surface finish).

*Different from ASTM.

RT — Room temperature.

s — Estimated population standard deviation; sample standard deviation; subscript "shear".
s^2 — Sample variance.
S — Shear force; nominal engineering stress, fatigue; S-basis for mechanical-property values (see Section 1.4.1.1).
S_a — Stress amplitude, fatigue.
S_e — Fatigue limit.
S_{eq}* — Equivalent stress.
S_f — Fatigue limit.
s_m — Mean stress, fatigue.
S_{max} — Highest algebraic value of stress in the stress cycle.
S_{min} — Lowest algebraic value of stress in the stress cycle.
S_r — Algebraic difference between the maximum and minimum stresses in one cycle.
SAE — Society of Automotive Engineers.
SCC — Stress-corrosion cracking.
SEE — Estimate population standard error of estimate.
SR — Studentized residual.
ST — Short transverse (grain direction).
STA — Solution treated and aged.
SUS — Individual or typical shear ultimate strength.
SYS — Individual or typical shear yield strength.
t — Thickness; subscript "tension"; exposure time; elapsed time; tolerance factor for the "t" distribution with the specified probability and appropriate degrees of freedom.
T — Transverse direction; applied torsional moment; transverse (grain direction); subscript "transverse".
T_F — Exposure temperature.
T_{90} — Statistically based lower tolerance bound for a mechanical property such that at least 90 percent of the population is expected to exceed T_{90} with 95 percent confidence.
T_{99} — Statistically based lower tolerance bound for a mechanical property such that at least 99 percent of the population is expected to exceed T_{99} with 95 percent confidence.
TIG — Tungsten-inert-gas (welding).
TUS — Individual or typical tensile ultimate strength.
TUS (S_u)* — Tensile ultimate strength.
TYS — Individual or typical tensile yield strength.
u — Subscript "ultimate".
U — Factor of utilization.
$V_{99,90}$ — The T_{99} or T_{90} tolerance limit factor for the three-parameter Weibull distribution, based on a 95 percent confidence level and a sample of size n.
W — Width of center-through-cracked tension panel; Watt.
$\bar{x}$ — Distance along a coordinate axis.
x — Sample mean based upon n observations.
X — Value of an individual measurement; average value of individual measurements.
y — Deflection (due to bending) of elastic curve of a beam; distance from neutral axis to given fiber; subscript "yield"; distance along a coordinate axis.
Y — Nondimensional factor relating component geometry and flaw size. See Reference 1.4.12.2.1(a) for values.
z — Distance along a coordinate axis.
Z — Section modulus, I/y.

A.2 SYMBOLS (also see Sections 1.2.1, 9.2.2, 9.3.4.3, 9.3.6.2, 9.4.1.2, 9.5.1.2, and 9.6).

α — 1) Coefficient of thermal expansion, mean; constant. 2) Significance level; probability (risk of erroneously rejecting the null hypothesis (see Section 9.6.2).

$\alpha_{A,B}$ — Shape parameter estimates for an A or B allowable based on an assumed three-parameter Weibull distribution.

α_{50} — Shape parameter estimate for the Anderson-Darling goodness-of-fit test based on an assumed three-parameter Weibull distribution.

β — Constant.

$\beta_{A,B}$ — Scale parameter estimate for an A or B allowable based on an assumed three-parameter Weibull distribution.

β_{50} — Scale parameter estimate for the Anderson-Darling goodness-of-fit test based on an assumed three-parameter Weibull distribution.

$\Delta\varepsilon$ or ε_r^* — strain range, $\varepsilon_{max} - \varepsilon_{min}$.

$\Delta\varepsilon_e$ — Elastic strain range.

$\Delta\varepsilon_p$ — Plastic strain range.

ΔS $(S_r)^*$ — Stress range.

$\Delta\sigma$ — True or local stress range.

ε — True or local strain.

ε_{eq}^* — Equivalent strain.

ε_m — Mean strain, $(\varepsilon_{max} + \varepsilon min)/2$.

ε_{max} — Maximum strain.

ε_{min} — Minimum strain.

ε_t — Total (elastic plus plastic) strain at failure determined from tensile stress-strain curve

δ — Deflection.

Φ — Angular deflection.

ρ — Radius of gyration; Neubur constant (block length).

μ — Poisson's ratio.

σ — True or local stress; or population standard deviation

σ_x — Population standard deviation of x.

σ_x^2 — Population variance of x.

$\tau_{A,B}$ — Threshold estimates for an A or B allowable based on an assumed three-parameter Weibull distribution.

τ_{50} — Threshold estimate for an A or B allowable based on an assumed three-parameter Weibull distribution.

ω — Density; flank angle.

∞ — Infinity.

Σ — The sum of.

$'$ — Value determined by regression analysis.

*Different from ASTM.

A.3 Definitions (also see Sections 1.2.1, 9.2.2, 9.3.6.2, 9.4.1.2, 9.5.1.2 and 9.6).

A-Basis.—The lower of either a statistically caluculated number, or the specification minimum (S-basis). The statistically calculated number indicates that at least 99 percent of the population of values is expected to equal or exceed the A-basis mechanical property allowable, with a confidence of 95 percent.

Alternating Load.—See Loading Amplitude.

B-Basis.—At least 90 percent of the population of values is expected to equal or exceed the B-basis mechanical property allowable, with a confidence of 95 percent.

Cast.—Cast consists of the sequential aluminum ingots which are melted from a single furnace change and poured in one or more drops without changes in the processing parameters. (The cast number is for internal identification and is not reported.) (See Table 9.1.6.1).

Confidence.—A specified degree of certainty that at least a given proportion of all future measurements can be expected to equal or exceed the lower tolerance limit. Degree of certainty is referred to as the confidence coefficient. For MIL-HDBK-5, the confidence coefficient is 95 percent which, as related to design allowables, means that, in the long run over many future samples, 95 percent of conclusions regarding exceedance of A and B-values would be true.

Confidence Interval.—An interval estimate of a population parameter computed so that the statement "the population parameter lies in this interval" will be true, on the average, in a stated proportion of the times such statements are made.

Confidence Interval Estimate.—Range of values, computed with the sample that is expected to include the population variance or mean.

Confidence Level (or Coefficient).—The stated portion of the time that the confidence interval is expected to include the population parameter.

Confidence Limits.*—The two numeric values that define a confidence interval.

Constant-Amplitude Loading.—A loading in which all of the peak loads are equal and all of the valley loads are equal.

Constant-Life Fatigue Diagram.—A plot (usually on Cartesian coordinates) of a family of curves, each of which is for a single fatigue life, N—relating S, S_{max}, and/or S_{min} to the mean stress, S_m. Generally, the constant life fatigue diagram is derived from a family of S-N curves, each of which represents a different stress ratio (A or R) for a 50 percent probability of survival. NOTE—MIL-HDBK-5 no longer presents fatigue data in the form of constant-life diagrams.

Creep.—The time-dependent deformation of a solid resulting from force.

Note 1—Creep tests are usually made at constant load and temperature. For tests on metals, initial loading strain, however defined, is not included.

Note 2—This change in strain is sometimes referred to as creep strain.

*Different from ASTM.

Note 2—This change in strain is sometimes referred to as creep strain.

Creep-Rupture Curve.—Results of material tests under constant load and temperature; usually plotted as strain versus time to rupture. A typical plot of creep-rupture data is shown in Figure 9.3.6.2. The strain indicated in this curve includes both initial deformation due to loading and plastic strain due to creep.

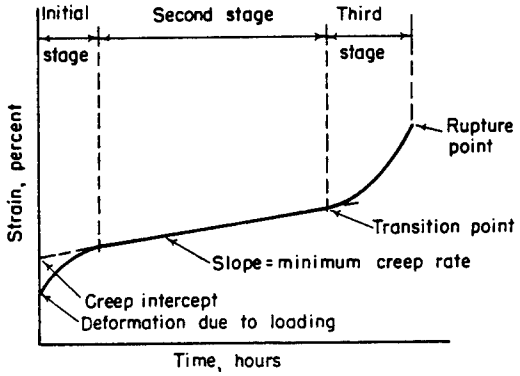


FIGURE A.1. *Typical creep-rupture curve.*

Creep-Rupture Strength.—Stress that will cause fracture in a creep test at a given time, in a specified constant environment. Note: This is sometimes referred to as the stress-rupture strength.

Creep-Rupture Test.—A creep-rupture test is one in which progressive specimen deformation and time for rupture are measured. In general, deformation is much larger than that developed during a creep test.

Creep-Strain.—The time-dependent part of the strain resulting from stress, excluding initial loading strain and thermal expansion.

Creep Strength.—Stress that causes a given creep in a creep test at a given time in a specified constant environment.

Creep Stress.—The constant load divided by the original cross-sectional area of the specimen.

Creep Test.—A creep test has the objective of measuring deformation and deformation rates at stresses usually well below those which would result in fracture during the time of testing.

Critical Stress Intensity Factor.—A limiting value of the stress intensity factor beyond which continued flaw propagation and/or fracture may be expected. This value is dependent on material and may vary with type of loading and conditions of use.

Cycle.—Under constant-amplitude loading, the load varies from the minimum to the maximum and then to the minimum load (see Figure 9.3.4.3). The symbol n or N (see definition of fatigue life) is used to indicate the number of cycles.

Deformable Shank Fasteners.—A fastener whose shank is deformed in the grip area during normal installation processes.

Degree of Freedom.—Number of degrees of freedom for n variables may be defined as number of variables minus number of constraints between them. Since the standard deviation calculation contains one fixed value (the mean) it has n - 1 degrees of freedom.

Degrees of Freedom.—Number of independent comparisons afforded by a sample.

Discontinued Test.—See Runout.

Elapsed Time.—The time interval from application of the creep stress to a specified observation.

Fatigue.—The process of progressive localized permanent structural change occurring in a material subjected to conditions that produce fluctuating stresses and strains at some point or points, and which may culminate in cracks or complete fracture after a sufficient number of fluctuations. NOTE—fluctuations in stress and in time (frequency), as in the case of "random vibration".

Fatigue Life.—N—the number of cycles of stress or strain of a specified character that a given specimen sustains before failure of a specified nature occurs.

Fatigue Limit.—S_f—the limiting value of the median fatigue strength as N becomes very large. NOTE—Certain materials and environments preclude the attainment of a fatigue limit. Values tabulated as "fatigue limits" in the literature are frequently (but not always) values of S_N for 50 percent survival at N cycles of stress in which $S_m = 0$.

Fatigue Loading.—Periodic or non-periodic fluctuating loading applied to a test specimen or experienced by a structure in service (also known as cyclic loading).

*Fatigue Notch Factor**.—The fatigue notch factor, K_f (also called fatigue strength reduction factor) is the ratio of the fatigue strength of a specimen with no stress concentration to the fatigue strength of a specimen with a stress concentration at the same number of cycles for the same conditions. NOTE—In specifying K_f, it is necessary to specify the geometry, mode of loading, and the values of S_{max} S_m, and N for which it is computed.

Fatigue Notch Sensitivity.—The fatigue notch sensitivity, q, is a measure of the degree of agreement between K_f and K_t. NOTE—the definition of fatigue notch sensitivity is $q = (K_f - 1)/(K_t - 1)$.

Heat.—All material identifiable to a single molten metal source. (All material from a heat is considered to have the same composition. A heat may yield one or more ingots. A heat may be divided into several lots by subsequent processing.)

Heat.—Heat is material which, in the case of batch melting, is cast at the same time from the same furnace and is identified with the same heat number; or, in the case of continuous melting, is poured without interruption. (See Table 9.1.6.2)

Heat—.Heat is a consolidated (vacuum hot pressed) billet having a distinct chemical composition. (See Table 9.1.6.2)

Hysteresis Diagram.—The stress-strain path during a fatigue cycle.

Isostrain Lines.—Lines representing constant levels of creep.

Isothermal Lines.—Lines of uniform temperature on a creep or stress-rupture curve.

*Interrupted Test**.—Tests which have been stopped before failure because of some mechanical problem, e.g., power failure, load or temperature spikes.

Loading Amplitude.—The loading amplitude, P_a, S_a, or ε_a represents one-half of the range of a cycle (see Figure 9.3.4.3). (Also known as alternating load, alternating stress, or alternating strain.)

Loading Strain.—Loading strain is the change in strain during the time interval from the start of loading to the instant of full-load application, sometimes called initial strain.

Loading (Unloading) Rate.—The time rate of change in the monotonically increasing (decreasing) portion of the load-time function.

Load Ratio.—The load ratio, R, A, or R_ε, A_ε, or R_σ, A_σ, is the algebraic ratio of the two loading parameters of a cycle; the two most widely used ratios are

$$R = \frac{\text{minimum load}}{\text{maximum load}} = \frac{P_{min}}{P_{max}}$$

or

$$R_\sigma = \frac{S_{min}}{S_{max}}$$

or

$$R_\varepsilon = \varepsilon_{min}/\varepsilon_{max}$$

and

$$A = \frac{\text{loading amplitude}}{\text{mean load}} = \frac{P_a}{P_m} \text{ or } \frac{S_a}{S_M}$$

$$A_\varepsilon = \frac{\text{strain amplitude}}{\text{mean strain}} = \frac{\varepsilon_a}{\varepsilon_M} \text{ or } (\varepsilon_{max} - \varepsilon_{min})/(\varepsilon_{max} + \varepsilon_{min})$$

NOTE—load ratios R or R_ε are generally used in MIL-HDBK-5.

Longitudinal Direction.—Parallel to the principal direction of flow in a worked metal.

Long-transverse Direction.—The transverse direction having the largest dimension, often called the "width" direction.

Lot.—All material from a heat or single molten metal source of the same product type having the same thickness or configuration, and fabricated as a unit under the same conditions. If the material is heat treated, a lot is the above material processed through the required heat-treating operations as a unit.

Master Creep Equation.—An equation expressing combinations of stress, temperature, time and creep, or a set of equations expressing combinations of stress, temperature and time for given levels of creep.

Master Rupture Equation.—An equation expressing combinations of stress, temperature, and time that cause complete separation (fracture or rupture) of the specimen.

Maximum Load.—The maximum load, P_{max}, maximum stress S_{max}, maximum strain ε_{max} is the load having the greatest algebraic value.

Mean Load.—The mean load, P_m, is the algebraic average of the maximum and minimum loads in constant-amplitude loading:

$$\text{Load} \quad P_m = \frac{P_{max} + P_{min}}{2}, \text{ or}$$

$$\text{Stress} \quad S_m = \frac{S_{max} + S_{min}}{2}, \text{ or}$$

$$\text{Strain} \quad \varepsilon_m = \frac{\varepsilon_{max} + \varepsilon_{min}}{2},$$

or the integral average of the instantaneous load values.

Median Fatigue Life.—The middlemost of the observed fatigue life values (arranged in order of magnitude) of the individual specimens in a group tested under identical conditions. In the case where an even number of specimens are tested, it is the average of the two middlemost values (based on log lives in MIL-HDBK-5). NOTE 1—The use of the sample median instead of the arithmetic mean (that is, the average) is usually preferred. NOTE 2—In the literature, the abbreviated term "fatigue life" usually has meant the median fatigue life of the group. However, when applied to a collection of data without further qualification, the term "fatigue life" is ambiguous.

Median Fatigue Strength at N Cycles.—An estimate of the stress level at which 50 percent of the population would survive N cycles. NOTE—The estimate of the median fatigue strength is derived from a particular point of the fatigue-life distribution, since there is no test procedure by which a frequency distribution of fatigue strengths at N cycles can be directly observed. That is, one can not perform constant-life tests.

Melt.—Melt is a single homogeneous batch of molten metal for which all processing has been completed and the temperature has been adjusted and made ready to pour castings. (For metal-matrix composites, the molten metal includes unmelted reinforcements such as particles, fibers, or whiskers.) (See Table 9.1.6.2)

Minimum Load.—The minimum load, P_{min}, S_{min}, or ε_{min}, is the load having the least algebraic value.

Nominal Hole Diameters.—Nominal hole diameters for deformable shank fasteners shall be according to Table 9.4.1.2(a). When tests are made with hole diameters other than those tabulated, hole sizes used shall be noted in the report and on the proposed joint allowables table.

Nominal Shank Diameter.—Nominal shank diameter of fasteners with shank diameters equal to those used for standard size bolts and screws (NAS 618 sizes) shall be the decimal equivalents of stated fractional or numbered sizes. These diameters are those listed in the fourth column of Table 9.4.1.2. Nominal shank diameters for nondeformable shank blind fasteners are listed in the fifth column of Table 9.4.1.2. Nominal shank diameters for other fasteners shall be the average of required maximum and minimum shank diameters.

Nondeformable Shank Fasteners.—A fastener whose shank does not deform in the grip area during normal installation processes.

*Outlier**—An experimental observation which deviates markedly from other observations in the sample. An outlier is often either an extreme value of the variability in the data, or the result of gross deviation in the material or experimental procedure.

Peak.—The point at which the first derivative of the load-time history changes from a positive to a negative sign; the point of maximum load in constant-amplitude loading (see Figure 9.3.4.3).

Plane Strain.—The stress state in which all strains occur only in the principal loading plane. No strains occur out of the plane, i.e., $\varepsilon_z = 0$, and $\sigma_z \neq 0$.

Plane Stress.—The stress state in which all stresses occur only in the principal loading plane. No stresses occur out of the plane, i.e., $\sigma_z = 0$, and $\varepsilon_z \neq 0$.

Plastic Strain During Loading.—Plastic strain during loading is the portion of the strain during loading determined as the offset from the linear portion to the end of a stress-strain curve made during load application.

Plane-Strain Fracture Toughness.—A generic term now generally adopted for the critical plane-strain stress intensity factor characteristic of plane-strain fracture, symbolically denoted K_{Ic}. This is because in current fracture testing practices, specification of the slowly increasing load test of specimen materials in the plane-strain stress state and in opening mode (I) has been dominant.

Plane-Stress and Transitional Fracture Toughness.—A generic term denoting the critical stress intensity factor associated with fracture behavior under nonplane-strain conditions. Because of plasticity effects and stable crack growth which can be encountered prior to fracture under these conditions, designation of a specific value is dependent on the stage of crack growth detected during testing. Residual strength or apparent fracture toughness is a special case of plane-stress and transitional fracture toughness wherein the reference crack length is the initial pre-existing crack length and subsequent crack growth during the test is neglected.

Population.—All potential measurements having certain independent characteristics in common; i.e., "all possible TUS(L) measurements for 17-7PH stainless steel sheet in TH1050 condition".

*Precision.**—The degree of mutual agreement among individual measurements. Relative to a method of test, precision is the degree of mutual agreement among individual measurements made under prescribed like conditions. The lack of precision in a measurement may be characterized as the standard deviation of the errors in measurement.

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*Different from ASTM.

Primary Creep.—Creep occurring at a diminishing rate, sometimes called initial stage of creep.

Probability.—Ratio of possible number of favorable events to total possible number of equally likely events. For example, if a coin is tossed, the probability of heads is one-half (or 50 percent) because heads can occur one way and the total possible events are two, either heads or tails. Similarly, the probability of throwing a three or greater on a die is 4/6 or 66.7 percent. Probability, as related to design allowables, means that chances of a material-property measurement equaling or exceeding a certain value (the one-sided lower tolerance limit) is 99 percent in the case of a A-value and 90 percent in the case of a B-value.

Range.—Range, ΔP, S_r, $\Delta\varepsilon$, ε_r, $\Delta\sigma$ is the algebraic difference between successive valley and peak loads (positive range or increasing load range) or between successive peak and valley loads (negative range or decreasing load range), see Figure 9.3.4.3. In constant-amplitude loading, for example, the range is given by $\Delta P = P_{max} - P_{min}$.

Rate of Creep.—The slope of the creep-time curve at a given time determined from a Cartesian plot.

*Residual.**—The difference between the observed fatigue (log) life and the fatigue (log) life estimated from the fatigue model at a particular stress/strain level.

*Runout.**—A test that has been terminated prior to failure. Runout tests are usually stopped at an arbitrary life value because of time and economic considerations. NOTE—Runout tests are useful for estimating a pseudo-fatigue-limit for a fatigue data sample.

Sample.—A finite number of observations drawn from the population.

Sample.—The number of specimens selected from a population for test purposes. NOTE—The method of selecting the sample determines the population about which statistical inferences or generalization can be made.

Sample Average (Arithmetic Mean).—The sum of all the observed values in a sample divided by the sample size (number). It is a point estimate of the population mean.

Sample Mean.—Average of all observed values in the sample. It is an estimate of population mean. A mean is indicated by a bar over the symbol for the value observed. Thus, the mean of n observations of TUS would be expressed as:

$$\overline{TUS} = \frac{TUS_1 + TUS_2 + \ldots + TUS_n}{n} = \frac{\sum_{i=1}^{n} (TUS_i)}{n}$$

Sample Median.—Value of the middle-most observation. If the sample is nearly normally distributed, the sample median is also an estimate of the population mean.

Sample Median.—The middle value when all observed values in a sample are arranged in order of magnitude if an odd number of samples are tested. If the sample size is even, it is the average of the two middlemost values. It is a point estimate of the population median, or 50 percentile point.

Sample Point Deviation.—The difference between an observed value and the sample mean.

*Sample Standard Deviation.**—The standard deviation of the sample, s, is the square root of the sample variance. It is a point estimate of the standard deviation of a population, a measure of the "spread" of the

*Different from ASTM.

frequency distribution of a population. NOTE—this value of s provides a statistic that is used in computing interval estimates and several test statistics.

*Sample Variance.**—Sample variance, s^2, is the sum of the squares of the differences between each observed value and the sample average divided by the sample size minus one. It is a point estimate of the population variance. NOTE—This value of s^2 provides both an unbiased point estimate of the population variance and a statistic that is used on computing the interval estimates and several test statistics. Some texts define s^2 as "the sum of the squared differences between each observed value and the sample average divided by the sample size", however; this statistic underestimates the population variance, particularly for small sample sizes.

Sample Variance.—The sum of the squared deviations, divided by n - 1, and, based on n observations of TUS, expressed as

$$S^2_{TUS} = \frac{\sum_{i=1}^{n} (TUS_i - \overline{TUS})^2}{n - 1} = \frac{n\sum_{i=1}^{n} (TUS_i)^2 - \left(\sum_{i=1}^{n} TUS_i\right)^2}{n(n - 1)}$$

S-Basis.—The S-value is the minimum property value specified by the governing industry specification (as issued by standardization groups such as SAE Aerospace Materials Division, ASTM, etc.) or federal or military standards for the material. (See MIL-STD-970 for order of preference for specifications.) For certain products heat treated by the user (for example, steels hardened and tempered to a designated F_{tu}), the S-value may reflect a specified quality-control requirement. Statistical assurance associated with this value is not known.

Secondary Creep.—Creep occurring at a constant rate, sometimes called second stage creep.

Short-transverse Direction.—The transverse direction having the smallest dimension, often called the "thickness" direction.

Significance Level (As Used Here).—Risk of concluding that two samples were drawn from different populations when, in fact, they were drawn from the same population. A significance level of $\alpha = 0.05$ is employed through these Guidelines.*

Significance Level.—The stated probability (risk) that a given test of significance will reject the hypothesis that a specified effect is absent when the hypothesis is true.

Significant (Statistically Significant).—An effect or difference between populations is said to be present if the value of a test statistic is significant, that is, lies outside of predetermined limits. NOTE—An effect that is statistically significant may not have engineering importance.

*S-N Curve for 50 Percent Survival***.—A curve fitted to the median values of fatigue life at each of several stress levels. It is an estimate of the relationship between applied stress and the number of cycles-to-failure that 50 percent of the population would survive. NOTE 1—This is a special case of the more general definition of S-N curve for P percent survival. NOTE 2—In the literature, the abbreviated term "S-N Curve" usually has meant either the S-N curve drawn through the mean (averages) or through the medians (50 percent values) for the fatigue life values. Since the term "S-N Curve" is ambiguous, it

* This is appropriate, since a confidence level $1 - \alpha = 0.95$ is used in establishing A and B-values.
** Different from ASTM.

should be used only when described appropriately. NOTE 3—Mean S-N curves (based on log lives) are shown in MIL-HDBK-5.

S-N Diagram.—A plot of stress against the number of cycles to failure. The stress can be S_{max}, S_{min}, or S_a. The diagram indicates the S-N relationship for a specified value of S_m, A, or R and a specified probability of survival. Typically, for N, a log scale (base 10) is used. Generally, for S, a linear scale is used, but a log scale is used occasionally. NOTE—S_{max}-versus-log N diagrams are used commonly in MIL-HDBK-5.

Standard Deviation.—An estimate of the population standard deviation; the square root of the variance, or

$$S_{TUS} = \sqrt{\frac{\sum_{i=1}^{n} (TUS_i - \overline{TUS})^2}{n - 1}} = \frac{\sqrt{n\sum_{i=1}^{n} (TUS_i)^2 - \sum_{i=1}^{n} (TUS_i)^2}}{n(n - 1)}$$

Stress Intensity Factor.—A physical quantity describing the severity of a flaw in the stress field of a loaded structural element. The gross stress in the material and flaw size are characterized parametrically by the stress intensity factor,

$$K = f\sqrt{a}\ Y,\ \text{ksi} - \text{in.}^{1/2} \qquad [9.5.1.2]$$

Stress-Rupture Test—A stress-rupture test is one in which time for rupture is measured, no deformation measurement being made during the test.

Tertiary Creep.—Creep occurring at an accelerating rate, sometimes called third stage creep.

Theoretical Stress Concentration Factor (or Stress Concentration Factor).—This factor, K_t, is the ratio of the nominal stress to the greatest stress in the region of a notch (or other stress concentrator) as determined by the theory of elasticity (or by experimental procedures that give equivalent values). NOTE—The theory of plasticity should not be used to determine K_t.

Tolerance Interval.—An interval computed so that it will include at least a stated percentage of the population with a stated probability.

Tolerance Level.—The stated probability that the tolerance interval includes at least the stated percentage of the population. It is not the same as a confidence level, but the term confidence level is frequently associated with tolerance intervals.

Tolerance Limits.—The two statistics that define a tolerance interval. (One value may be "minus infinity" or "plus infinity".)

Total Plastic Strain.—Total plastic strain at a specified time is equal to the sum of plastic strain during loading plus creep.

Total Strain.—Total strain at any given time, including initial loading strain (which may include plastic strain in addition to elastic strain) and creep strain, but not including thermal expansion.

*Transition Fatigue Life.**—The point on a strain-life diagram where the elastic and plastic strains are equal.

Transverse Direction.—Perpendicular to the principal direction of flow in a worked metal; may be defined as T, LT, or ST.

Typical Basis.—A typical property value is an average value and has no statistical assurance associated with it.

Waveform.—The shape of the peak-to-peak variation of a controlled mechanical test variable (for example, load, strain, displacement) as a function of time.

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B.0 Alloy Index

Alloy Name	Form	Specification	Section
250	Bar	AMS 6512	2.5.1
250	Sheet and Plate	AMS 6520	2.5.1
354.0	Casting	MIL-A-21180	3.9.1
355.0	Permanent Mold Casting	AMS 4281	3.9.2
356.0	Sand Casting	AMS 4217	3.9.4
356.0	Investment Casting	AMS 4260	3.9.4
356.0	Permanent Mold Casting	AMS 4282	3.9.4
359.0	Casting	MIL-A-21180	3.9.8
2014	Bare Sheet and Plate	AMS 4028	3.2.1
2014	Bare Sheet and Plate	AMS 4029	3.2.1
2014	Bar and Rod, Rolled or Cold Finished	AMS 4121	3.2.1
2014	Forging	AMS 4133	3.2.1
2014	Extrusion	AMS 4153	3.2.1
2014	Forging	MIL-A-22771	3.2.1
2014	Extruded Bar, Rod and Shapes	QQ-A-200/2	3.2.1
2014	Rolled or Drawn Bar, Rod and Shapes	QQ-A-225/4	3.2.1
2014	Clad Sheet and Plate	QQ-A-250/3	3.2.1
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2017	Rolled Bar and Rod	QQ-A-225/5	3.2.2
2024	Bare Sheet and Plate	AMS 4035	3.2.3
2024	Bare Sheet and Plate	AMS 4037	3.2.3
2024	Tubing, Hydraulic, Seamless, Drawn	AMS 4086	3.2.3
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2024	Extrusion	AMS 4152	3.2.3
2024	Extrusion	AMS 4164	3.2.3
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2024	Extruded Bar, Rod and Shapes	QQ-A-200/3	3.2.3
2024	Rolled or Drawn Bar, Rod and Wire	QQ-A-225/6	3.2.3
2024	Clad Sheet and Plate	QQ-A-250/5	3.2.3
2024	Tubing	WW-T-700/3	3.2.3
2025	Die Forging	AMS 4130	3.2.4
2090	Sheet	AMS 4251	3.2.5
2124	Plate	AMS 4101	3.2.6
2124	Plate	QQ-A-250/9	3.2.6
2219	Sheet and Plate	AMS 4031	3.2.7
2219	Hand Forging	AMS 4144	3.2.7
2219	Extrusion	AMS 4162	3.2.7
2219	Extrusion	AMS 4163	3.2.7
2219	Sheet and Plate	QQ-A-250/30	3.2.7
2519	Plate	MIL-A-46192	3.2.8
2618	Die and Hand Forgings	AMS 4132	3.2.9
2618	Die Forging	MIL-A-22771	3.2.9
2618	Forging	QQ-A-367	3.2.9
4130	Bar and Forging	AMS 6348	2.3.1
4130	Sheet, Strip and Plate	AMS 6350	2.3.1
4130	Sheet, Strip and Plate	AMS 6351	2.3.1

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4130	Tubing	AMS 6362	2.3.1
4130	Bar and Forging	AMS 6370	2.3.1
4130	Tubing	AMS 6370	2.3.1
4130	Tubing	AMS 6371	2.3.1
4130	Tubing	AMS 6373	2.3.1
4130	Sheet, Strip and Plate	MIL-S-18729	2.3.1
4130	Bar and Forging	MIL-S-6758	2.3.1
4130	Tubing	MIL-T-6736	2.3.1
4135	Sheet, Strip and Plate	AMS 6352	2.3.1
4135	Tubing	AMS 6365	2.3.1
4135	Tubing	AMS 6372	2.3.1
4135	Tubing	MIL-T-6735	2.3.1
4140	Bar and Forging	AMS 6349	2.3.1
4140	Tubing	AMS 6381	2.3.1
4140	Bar and Forging	AMS 6382	2.3.1
4140	Tubing	AMS 6390	2.3.1
4140	Sheet, Strip and Plate	AMS 6395	2.3.1
4140	Bar and Forging	MIL-S-5626	2.3.1
4340	Sheet, Strip and Plate	AMS 6359	2.3.1
4340	Bar and Forging	AMS 6414	2.3.1
4340	Tubing	AMS 6414	2.3.1
4340	Bar and Forging	AMS 6415	2.3.1
4340	Tubing	AMS 6415	2.3.1
4340	Sheet, Strip and Plate	AMS 6454	2.3.1
4340	Bar and Forging	MIL-S-5000	2.3.1
4340	Bar and Forging	MIL-S-8844	2.3.1
4340	Tubing	MIL-S-8844	2.3.1
5052	Sheet and Plate	AMS 4015	3.5.1
5052	Sheet and Plate	AMS 4016	3.5.1
5052	Sheet and Plate	AMS 4017	3.5.1
5052	Sheet and Plate	QQ-A-250/8	3.5.1
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5083	Bare Sheet and Plate	QQ-A-250/6	3.5.2
5086	Extruded Bar, Rod and Shapes	QQ-A-200/5	3.5.3
5086	Sheet and Plate	QQ-A-250/7	3.5.3
5454	Extruded Bar, Rod and Shapes	QQ-A-200/6	3.5.4
5454	Sheet and Plate	QQ-A-250/10	3.5.4
5456	Extruded Bar, Rod and Shapes	QQ-A-200/7	3.5.5
5456	Sheet and Plate	QQ-A-250/9	3.5.5
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6013	Sheet (T6)	AMS 4347	3.6.1
6061	Sheet and Plate	AMS 4025	3.6.2
6061	Sheet and Plate	AMS 4026	3.6.2
6061	Sheet and Plate	AMS 4027	3.6.2
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6061	Tubing Seamless, Drawn	AMS 4082	3.6.2
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6061	Extrusion	AMS 4160	3.6.2
6061	Extrusion	AMS 4161	3.6.2
6061	Extrusion	AMS 4172	3.6.2
6061	Hand Forging	AMS 4248	3.6.2
6061	Forging	MIL-A-22771	3.6.2
6061	Pipe	MIL-P-25995	3.6.2
6061	Extruded Rod, Bar Shapes and Tubing	QQ-A-200/8	3.6.2
6061	Rolled Bar, Rod and Shapes	QQ-A-225/8	3.6.2
6061	Sheet and Plate	QQ-A-250/11	3.6.2
6061	Forging	QQ-A-367	3.6.2
6061	Tubing Seamless, Drawn	WW-T-700/6	3.6.2
6151	Die Forging	AMS 4125	3.6.3
6151	Forging	MIL-A-22771	3.6.3
7010	Plate	AMS 4204	3.7.1
7010	Plate	AMS 4205	3.7.1
7050	Bare Plate	AMS 4050	3.7.3
7050	Die Forging	AMS 4107	3.7.3
7050	Hand Forging	AMS 4108	3.7.3
7050	Bare Plate	AMS 4201	3.7.3
7050	Die Forging	AMS 4333	3.7.3
7050	Extruded Shape	AMS 4340	3.7.3
7050	Extruded Shape	AMS 4341	3.7.3
7050	Extruded Shape	AMS 4342	3.7.3
7050	Forging	MIL-A-22771	3.7.3
7075	Bare Sheet and Plate	AMS 4044	3.7.4
7075	Bare Sheet and Plate	AMS 4045	3.7.4
7075	Clad Sheet and Plate	AMS 4049	3.7.4
7075	Bare Plate	AMS 4078	3.7.4
7075	Bar and Rod, Rolled or Cold Finished	AMS 4122	3.7.4
7075	Bar and Rod, Rolled or Cold Finished	AMS 4123	3.7.4
7075	Bar and Rod, Rolled or Cold Finished	AMS 4124	3.7.4
7075	Forging	AMS 4126	3.7.4
7075	Die Forging	AMS 4141	3.7.4
7075	Forging	AMS 4147	3.7.4
7075	Bar and Rod, Rolled or Cold Finished	AMS 4186	3.7.4
7075	Bar and Rod, Rolled or Cold Finished	AMS 4187	3.7.4
7075	Forging	MIL-A-22771	3.7.4
7075	Extruded Bar, Rod and Shapes	QQ-A-200/11, 15	3.7.4
7075	Rolled or Drawn Bar and Rod	QQ-A-225/9	3.7.4
7075	Bare Sheet and Plate	QQ-A-250/12, 24	3.7.4
7075	Clad Sheet and Plate	QQ-A-250/13, 25	3.7.4
7075	Forging	QQ-A-367	3.7.4
7150	Bare Plate	AMS 4252 (T7751)	3.7.5
7150	Bare Plate	AMS 4306 (T6151)	3.7.5
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7150	Extrusion	AMS 4345 (T77511)	3.7.5
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7175	Forging	MIL-A-22771	3.7.6
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7475	Bare Sheet	AMS 4090 (T651)	3.7.7
7475	Clad Sheet	AMS 4100 (T761)	3.7.7
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8630	Tubing	AMS 6281	2.3.1
8630	Sheet, Strip and Plate	AMS 6355	2.3.1
8630	Sheet, Strip and Plate	MIL-S-18728	2.3.1
8630	Bar and Forging	MIL-S-6050	2.3.1
8735	Tubing	AMS 6282	2.3.1
8735	Bar and Forging	AMS 6320	2.3.1
8735	Sheet, Strip and Plate	AMS 6357	2.3.1
8740	Bar and Forging	AMS 6322	2.3.1
8740	Tubing	AMS 6323	2.3.1
8740	Bar and Forging	AMS 6327	2.3.1
8740	Sheet, Strip and Plate	AMS 6358	2.3.1
8740	Bar and Forging	MIL-S-6049	2.3.1
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15-5PH	Bar, Forging, Ring and Extrusion (CEVM)	AMS 5659	2.6.6
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17-4PH	Investment Casting (H1000)	AMS 5343	2.6.8
17-4PH	Investment Casting (H900)	AMS 5344	2.6.8
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300M (0.42C)	Tubing	AMS 6419	2.3.1
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4330V	Tubing	AMS 6427	2.3.1
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4335V	Sheet, Strip and Plate	AMS 6435	2.3.1
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5Cr-Mo-V	Bar and Forging	AMS 6485	2.4.1
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A-286	Bar, Forging, Tubing and Ring	AMS 5732	6.2.1
A-286	Bar, Forging and Tubing	AMS 5734	6.2.1
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A356.0	Casting	MIL-A-21180	3.9.5
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AISI 1025	Sheet and Strip	MIL-S-7952	2.2.1
AISI 1025	Tubing	MIL-T-5066	2.2.1
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AM-350	Sheet and Strip	AMS 5548	2.6.1
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AZ31B	Sheet and Plate	AMS 4377	4.2.1
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D6AC	Tubing	AMS 6431	2.3.1
D6AC	Bar and Forging	MIL-S-8949	2.3.1
D6AC	Sheet, Strip and Plate	MIL-S-8949	2.3.1
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Inconel Alloy 706	Bar, Forging and Ring	AMS 5702	6.3.4
Inconel Alloy 706	Bar, Forging and Ring	AMS 5703	6.3.4
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Inconel Alloy X-750	Bar and Forging; Equalized	AMS 5667	6.3.6
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L-605	Bar and Forging	AMS 5759	6.4.1
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QE22A Magnesium	Sand Casting	MIL-M46062	4.3.5
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Ti-10V-2Fe-3Al (Ti-10-2-3)	Forging	AMS 4986	5.5.3
Ti-13V-11Cr-3Al	Sheet, Strip and Plate	MIL-T-9046	5.5.1
Ti-13V-11Cr-3Al	Bar	MIL-T-9047	5.5.1
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Ti-5Al-2.5Sn	Bar	AMS 4926	5.3.1
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Ti-5Al-2.5Sn	Sheet, Strip and Plate	MIL-T-9046	5.3.1
Ti-5Al-2.5Sn	Bar	MIL-T-9047	5.3.1
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Ti-6Al-4V	Extrusion	AMS 4934	5.4.1
Ti-6Al-4V	Extrusion	AMS 4935	5.4.1
Ti-6Al-4V	Bar	AMS 4967	5.4.1
Ti-6Al-4V	Sheet, Strip and Plate	MIL-T-9046	5.4.1
Ti-6Al-4V	Bar	MIL-T-9047	5.4.1
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Ti-8Al-1Mo-1V	Sheet, Strip and Plate	MIL-T-9046	5.3.2
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