

A Computational Model for Visual Selection

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Abstract

We propose a computational model for detecting and localizing instances from an object class in static grey level images. We divide detection into *visual selection* and *final classification*, concentrating on the former: Drastically reducing the number of candidate regions which require further, usually more intensive, processing, but with a minimum of computation and missed detections. Bottom-up processing is based on local groupings of edge fragments constrained by loose geometrical relationships. They have no *a priori* semantic or geometric interpretation. The role of training is to select special groupings which are moderately likely at certain places on the object but rare in the background. We show that the statistics in both populations are stable. The candidate regions are those which contain *global* arrangements of several local groupings. Whereas our model was not conceived to explain brain functions, it does cohere with evidence about the functions of neurons in V1 and V2, such as responses to coarse or incomplete patterns (e.g., “illusory contours”) and to scale and translation invariance in IT. Finally, the algorithm is applied to face and symbol detection.

1 Introduction

Approximately 150 milliseconds after visual input is presented, or within several tens of milliseconds after local processing in V1, cells in IT signal that an object has been detected and a location has been selected in a field of view larger than the fovea. Assuming a specific detection task is required, the decision is rapid but might be wrong. Additional processing might reveal that the desired object is not in the vicinity of the first location and a sequence of locations may need to be inspected. Therefore, in a very short period of time, local information is processed in a region somewhat larger than the fovea in order to identify “hot spots” which are likely, though not certain, to contain a desired object or class of objects. Final determination of whether

these candidate locations correspond to objects of interest requires intensive high resolution processing after foveation. This scenario - *visual selection* (or *selective attention*) and sequential processing - is widely accepted in the literature; see Thorpe, Fize & Marlot (1996), Desimone, Miller, Chelazzi & Lueschow (1995), Lueschow, Miller & Desimone (1994), Van Essen & Deyoe (1995), Ullman (1996).

In artificial vision, the problem of detecting and localizing all instances from a generic object class, such as faces or cars, is referred to as *object detection*. Our goal is an efficient algorithm for object detection in static grey level scenes, emphasizing the role of visual selection. By this we mean quickly identifying a relatively small set of poses (position, scale, etc.) which account for nearly all instances of the object class in a grey level image. Experiments are presented illustrating visual selection in complex scenes, as well as the final classification of each candidate as “object” or “background.” We also explore connections between our computational model and evidence for neuronal responses to “illusory” contours or otherwise incomplete image structures in which fragmentary data is sufficient for activation. We argue that it is more efficient and robust to exploit spatial regularity by not filling in missing fragments.

Here is a synopsis of the approach: Bottom-up processing is based on local features defined as flexible groupings of nearby edge fragments. The object class is represented by a union of global spatial arrangements, this time among several of the local features and at the scale of the objects. Photometric (i.e., grayscale) invariance is built into the definition of an edge fragment. Geometric invariance results from explicit disjunction (ORing): The local groupings are disjunctions of conjunctions of nearby edge fragments and the global arrangements are disjunctions of conjunctions of the local ones. In principle we entertain *all* possible local features, a virtually infinite family. The role of training is to select dedicated local groupings which are each rare in the “background population” but moderately likely to appear in certain places on the object. We will provide evidence that a very small amount of training data may

suffice to identify such groupings.

Visual selection is based on an image-wide search for each global arrangement in the union over a range of scales and other deformations of a reference arrangement. Each instance signals a candidate pose. Accurate visual selection is then feasible due to the favorable marginal statistics and to weak dependence among spatially distant groupings. It is fast because the search is coarse-to-fine and the indexing in pose space is driven by rare events, namely the global arrangements; in addition, there is no search for “parts” (or other sub-classification task) and no segmentation per se. The result of an experiment in face detection is shown in Figure 1. The lefthand panel shows the regions containing final detections. The righthand panel is a grayscale rendering of the *logarithm* of the number of times each pixel in the image is accessed for some form of calculation during visual selection; the corresponding image for many other approaches, e.g., those based on artificial neural networks, would be constant.

Part of this program is familiar. The emphasis on groupings and spatial relationships, the use of edges to achieve illumination invariance, the general manner of indexing and the utility of statistical modeling have all been explored in object recognition; some points of contact will be mentioned shortly. Moreover, the general strategy for visual selection goes back at least to Lowe (1985) and others who emphasized the role of selecting groupings based on their statistical or “non-accidental” properties.

What seems to be new is that our approach is *purely* algorithmic and statistical. The groupings have no a priori semantical or geometrical content. They are chosen within a very large family based solely on their statistical properties in the object and background populations. They are also more primitive and *less* individually informative than the model-based features generally found in computer vision algorithms. For example, we use the term “edge fragment” even though the marked transitions have no precise orientation. Moreover, the groupings do not necessarily correspond to smooth object contours and other regular structures (such as corners and lines) that

are often the target of bottom-up processing. In other words, there is no geometrical or topological analysis of contours and object boundaries. (See Figure 3.) Nor is there an abstract concept of a “good grouping” as in Gestalt psychology.

In addition, we argue that visual selection, if not final classification, can be accomplished with object representations which are very coarse and sparse compared with most others, for example 3D geometric models, structural descriptions based on “parts” (Winston (1970), Biederman (1985)) and “pictorial representations” (Ullman (1996)). The “face graphs” in Maurer & von der Malsburg (1996) are closer in spirit, although the “jets” (outputs from multiple Gabor filters) at the graph vertices are more discriminating than our local groupings; also, the representation there is much denser, perhaps because the application, namely face *recognition*, is more challenging.

Our representation of pose space (a three point “basis” or local coordinate system) is the same as in geometric hashing (Lamdan, Schwartz & Wolfson (1988)), wherein the local features are affine invariants (e.g., sharp inflections and concavities) and objects are represented by hash tables indexed by feature locations. But again our framework is inherently nondeterministic: Features may or may not be visible on the objects, regardless of occlusion or other degrading factors, and are characterized by probability distributions. In addition, the global arrangements are more than a list; it is the geometrical constraints which render them “rare” in the background population. The statistical framework in Rojer & Schwartz (1992) is similar, although there is no systematic exploration of features. Also pose indexing based on global information is more efficient than the Hough transform. Finally, there are shared properties with artificial neural networks (Rowley, Baluja & Takeo (1998), Sung & Poggio (1998)), for example the emphasis on learning and the absence of formal models. However, our algorithm is not purely “bottom-up” and our treatment of invariance is explicit; we do not expect the system to “learn” about it, or about weak dependence or coarse-to-fine processing. These properties are “hard-wired.”

In the following section the object detection and visual selection problems are



Figure 1: Left: Regions containing final detections. Right: A grayscale rendering of the *logarithm* of the number of times each pixel in the image is accessed for some form of calculation during visual selection.

formulated more carefully. In Section 3 we delineate the statistical and invariance properties we require of our local and global features. The edge groupings are defined in Section 4, together with an analysis of their “statistics” in natural images. Training and object representations are discussed in Section 5, as well as error rates and parameter selection. In Section 6 we briefly comment on how final classification is performed and present some experiments on face and symbol detection. Section 7 is devoted to connections with brain modeling, especially evidence for similar types of coarse processing in the visual cortex, and to neural network-type architectures for efficient parallel implementation of the proposed algorithm. We conclude with a summary of the main strengths and weaknesses of the proposed model.

2 Problem Formulation

The problem is to detect objects of a specific class, e.g., faces, cars, a handwritten “5”, any digit, etc. In order to narrow the scope we assume static gray level images, and hence do not utilize color, depth or motion cues. However, since our initial processing

is edge-based, one way to incorporate such information would be to replace intensity edges by those resulting from discontinuities in color, depth or motion. Moreover, we do not use *context*. Thus, the detection is primarily shape-based.

We assume that the object appears at a limited range of scales, say $\pm 25\%$ of some mean scale, and at a limited range of rotations about a reference orientation (e.g., an upright face). Other poses are accommodated by applying the algorithm to pre-processed data; for example we detect faces at scales larger than the reference one by simple downsampling.

We want to be more precise about the manner in which a detected object is localized within the image. Since the given range of scales is still rather wide and since we also desire invariance to other transformations, for instance local linear and nonlinear image deformations, it is hardly meaningful to identify the pose of an object with a single degree of freedom. Instead we assign each detection a *basis* - three points (six degrees of freedom) which define a local coordinate system. Consequently, in addition to translation, there is an adjustment for scale and other small deformations. Of course this extended notion of localization increases the number of poses by several orders of magnitude; within the class of transformations mentioned above, the number of bases in a 100×100 image is on the order of ten million.

Assume that each image in a training set of examples of the object is registered to a fixed reference grid in such a way that three distinguished points on the object are always at the same fixed coordinates, denoted z_1, z_2, z_3 . As an example of three distinguished points on a face, consider the “centers” of the two eyes and the mouth. Typically we use a reference grid of about 30×30 pixels and expect the smallest detection to be at a scale of around 25×25 . Each possible image basis (b_1, b_2, b_3) then determines a unique affine map which carries z_i to b_i for $i = 1, 2, 3$. In addition, the reference grid itself is carried to a subimage, or “region-of-interest” (ROI), around the basis.

The ROI plays the role of a segmented region. In particular, there is no effort to

determine a silhouette or a subregion consisting more or less exactly of object pixels. Note also that we do *not* search directly for the distinguished points; they merely define localization. We find that a search for either a silhouette or for special points during a chain of processing leading up to recognition is highly unreliable; in fact, it may only be when the object as a whole is detected that such things can actually be identified.

Visual selection means identifying a set of candidate ROIs; the ultimate problem is to classify each one as “object” or “background,” which may not be easy with high accuracy. However, given the drastic reduction of candidates, presumably the final classification of each candidate could be allotted considerable computational resources. Moreover, this final classification can be greatly facilitated by *registering* the image data in the ROI to the reference grid using the affine map mentioned above. For example, in our previous work, the final classification was based on training decision trees using registered and normalized gray level values, and the computer vision literature is replete with other methods, such as those based on neural networks. However, this is not the main focus of this paper. *The theme here is the reduction of the number of ROI’s which require further and intensive processing from several millions to several tens or hundreds, and with a minimum of computation and missed detections.*

3 Feature Attributes

Our local features are binary, point-based image functionals which are defined modulo translation. Moreover, the set of all occurrences on an image-wide basis is regarded as the realization of a *point process*, assumed to be stationary in the background population in a statistical sense. Instances of this process have no a priori semantic interpretation and hence there is no sub-recognition problem implicit in their computation. *In particular there is no such thing as a “missed detection” at the feature*

level. Their utility for visual selection depends on the following attributes:

- **LI: Stability:** A significant degree of invariance to geometric deformations and to gray level transformations representing changes in illumination.
- **LII: Localization:** Appearance in a specified small region on a significant fraction (e.g., one-half) of the registered training images of the object.
- **LIII: Low Background Density:** Realizations of the point process should be relatively sparse in generic background images.

The first two properties are linked. Suppose, for example, that all images of the object corresponded to smooth deformations of a template. Then stability would imply that a local feature which was well-localized on the template should be present near that characteristic location on a sizeable fraction of the examples. In the next section we will exhibit an enormous family of local features with properties LI and LIII and explain how to select a small subset of these based on training data which also satisfy LII.

Global information is essential. Complex objects are difficult to detect (and distinguish from one another) even when coherent “parts” are individually recognized, and doing this independently of the whole object is itself extremely problematic. For example, although faces can be detected at low resolution, it might be very difficult to identify say a left eye based only on the intensity data in its immediate vicinity, i.e., outside the context of the entire face; see the example and discussion in Ullman (1996). Furthermore, local features do not provide information about the pose, except for translation.

A *global arrangement* in a registered training image is the conjunction, i.e., simultaneous occurrence, of a small number of local features subject to the constraint that their locations in the reference grid are confined to specified regions. An instance of a global arrangement in a test image occurs in the ROI of a basis if the locations of the local features fall in their distinguished regions *in the local coordinate system*

determined by the basis. This will be made more precise later on. The properties we need are these:

- **GI: Coverage:** A small collection (union) of such arrangements “covers” the object class in the range of scales and rotations in which the object is expected to appear in the scene.
- **GII: Rare Events:** The arrangements are very rare events in a generic scene, i.e., in general background images.

The precise meaning of GI is that a very high percentage of images of the object exhibit *at least one* global arrangement after registration to the reference grid. In other words, the union of the arrangements is nearly an invariant for the object class. During selection, the object instances which are detected are those which are “covered” by at least one global arrangement. Hence this “coverage probability” is lower bound on the false negative rate of the entire detection process. The coverage probability is directly determined by the joint statistics of the local features on registered images of the object class, together with the degree of invariance introduced in the definition of the arrangements, i.e., the amount of “slack” in the relative coordinates of the local features; see Section 5.

Property GII - limiting the number of “hot spots” - is of course related to false positive error, as will be explained more fully in Section 5.2. Statistical characteristics of the global arrangements in “natural scenes” are determined by the density and higher order moments of the point processes corresponding to the local features.

4 Local Groupings and Their Statistics

All the features described here are constructed from intensity transitions. A great many edge detectors have been proposed and some of these with enough greyscale invariance would suffice for our purposes. The one we use is based on comparisons of

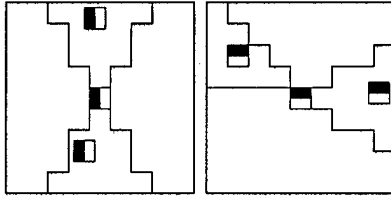


Figure 2: Two examples of edge arrangements with $N_{edges} = 2$ edges in addition to the center one, each allowed to lie anywhere in a subregion of size $N_{pixels} \approx 10$.

intensity differences and is consequently invariant to linear transformations of the grey scale, insuring the photometric part of LI. There are four edge types, corresponding roughly to vertical and horizontal orientation and two polarities; the details are in Amit, Geman & Jedynak (1998) and are not important for the discussion here, except to note that the orientation is not very precise. For example, the “vertical” edge responds to any linear boundary over a ninety degree range of orientations.

4.1 Edge Groupings

The local features are flexible spatial arrangements of several edge fragments, organized as disjunctions of local conjunctions of edges. Each feature has a “central edge” of some type, and a number N_{edges} of other edge types which are constrained to lie in specific subregions within a square neighborhood of the location of the center edge. The sizes of the subregions are all the same and denoted by N_{pixels} . Typically the subregions are wedge-shaped as indicated in Figure 2. Disjunction - allowing the N_{edges} edges to float in their respective subregions - is how geometric invariance (LI) is explicitly introduced at this level; there is also disjunction at the global level as indicated earlier.

The frequency of occurrence of these groupings depends on N_{edges} , N_{pixels} and the particular spatial arrangement. Among the set of all possible edge groupings - the generic feature class - most are simultaneously rare in both object and background images. When specific groupings are selected according to their frequency in training



Figure 3: Examples of 9×9 subimages centered at instances of local features (edge groupings) identified for faces. Left: Samples of one local feature from an image without faces. Right: The same thing for another local feature.

examples of a particular object, they appear to be loosely correlated with evidence for contour segments, or even relationships among several segments. In Figure 3 we show subimages of size 9×9 which contain two particular groupings common in faces. The one on the left is typically located at the region of the eyebrows; the grouping involves some horizontal edges of one polarity above some others of the opposite polarity. These instances were chosen randomly from among all instances in a complex scene with no faces.

The point process determined by any local feature, as localized by the central edge, is a *thinning* of the point process determined by instances of the central edge type. Each additional edge type in the grouping, and corresponding subregion thins it even further. Figure 4 illustrates the thinning by showing all instances of horizontal edges of one polarity alongside all instances of a local feature centered at the horizontal edge with $N_{edges} = 3$ and $N_{pixels} = 10$.

We present some statistics of local features in 70 images randomly downloaded from the web. The local features were chosen by varying the number of edges N_{edges} (from 2 – 7) and the size of the subregions N_{pixels} (from 7 – 40) and using different shapes for the subregions. For each local feature we calculated the *density per pixel* in each of the 70 images and took the average over images. The regression of the log



Figure 4: Left: All instances of horizontal edges. Right: All instances of a local feature dedicated to faces.

density on N_{edges} and N_{pixels} yields an $R^2 > .95$. The scatter plot of the log density versus the estimated linear regression is presented in Figure 5. Although at such relatively close distances, the individual edges are *not* independent, the dependence is sufficiently weak that if N_{pixels} is held fixed there is a consistent multiplicative reduction in density of approximately $e^{-.6} = .5$. In particular, property LIII (low background density) is clearly satisfied in the ranges of parameters presented here.

Despite the high correlation, which is due to the averaging over images, there is substantial variation in the density from image to image. On the natural log-scale this variation is of order of ± 1 . In Table 1 we display the mean and standard deviation of the log-density for $N_{pixels} = 10$ pixels for various values of N_{edges} . The value $N_{edges} = 0$ corresponds to the density of each of the four edges. It is clear that the order-of-magnitude of the feature densities in generic images can be predicted based on the number of edges and the size of the regions. These general statistical properties are useful for constructing detection algorithms, for example in estimating false positive rates and computational demands.

4.2 Higher-Order Moments

We are also interested in higher-order moments of the point processes corresponding to the local features. These determine the statistics of the global arrangements. They

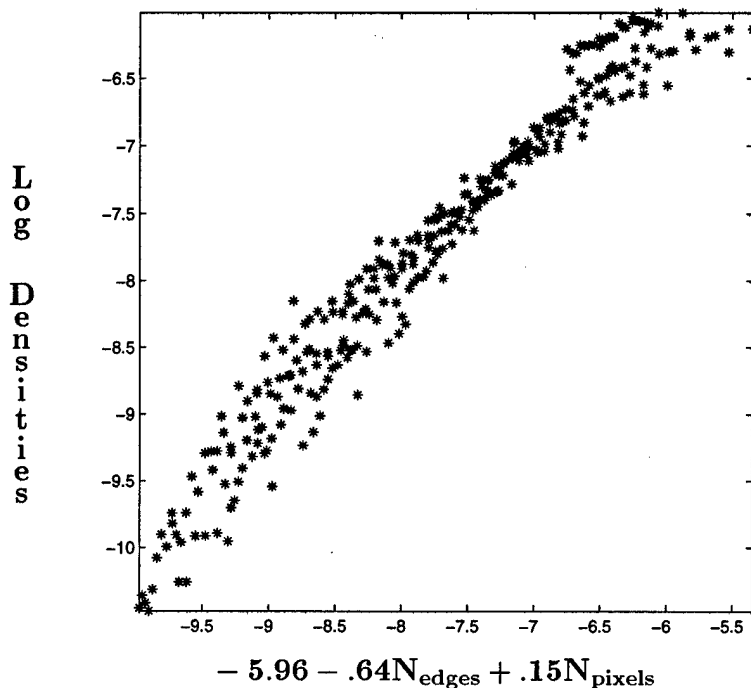


Figure 5: Scatter plot of log densities of local features vs. fitted regression to N_{edges} (the number of edges in a grouping) and N_{pixels} (the size of the subregions).

are defined in the same manner as a local grouping, except with edges replaced by entire local groupings. The degree of geometric invariance is again determined by the degree of disjunction, which in turn depends on the (common) size of the subregions in which the local groupings are constrained to lie.

We will concentrate on global arrangements of exactly three local features, referred to as “triangles.” (This is the minimum number necessary to uniquely determine a basis.) Let us be more specific about what it means for a particular triangle - triple of local features - to be present “at pixel x ”. Denote the “central” local feature by α_0 and the two others by α_1 and α_2 . Of course α_0, α_1 and α_2 are each local groupings of edges. Let $\mathcal{B}_1$ and $\mathcal{B}_2$ be two boxes centered at the origin; these determine the degree of disjunction for α_1 and α_2 . Also, let v_1 and v_2 be two vectors; these determine the

N_{edges}	0	1	2	3	4	5	6
mean	-3.8	-4.7	-5.2	-5.7	-6.3	-6.9	-7.5
std	.65	.83	.87	.97	.95	.93	.92

Table 1: Mean and standard deviation of local feature log-density over 70 random images for various values of N_{edges} , with $N_{pixels} = 10$

locations of the boxes relative the location of α_0 . Then there is an instance of the triangle at x if feature α_0 is present at $x^0 = x$, feature α_1 is present at some point $x^1 \in x^0 + v_1 + \mathcal{B}_1$ and feature α_2 is present at some point $x^2 \in x^0 + v_2 + \mathcal{B}_2$.

We used the 70 images to determine typical triangle densities in real images over a wide range of sizes for $\mathcal{B}_1, \mathcal{B}_2$ and offsets v_1, v_2 (triangle shapes). We searched for all instances of each triangle in each image. For comparison, for each triangle and each image, we generated realizations of three mutually independent Poisson processes using the average densities of the local features in the image and searched for instances of these “ideal” triangles. In the lefthand panel of Figure 6 we show a typical scatter plot of the log densities of a global arrangement as a function of the log of the average density of the local features. Each point represents one of the seventy images, with $\circ$ indicating actual local features and $*$ indicating the Poisson simulation. It appears that the density of the global arrangements can be rather well predicted from the density of the local features.

If the point processes defined by $\alpha_0, \alpha_1, \alpha_2$ were indeed Poisson and mutually independent, and if each local feature had the same density, say λ_{local} , then the density of the corresponding triangle would be

$$\lambda_{global} = \lambda_{local}^3 \cdot |\mathcal{B}_1| \cdot |\mathcal{B}_2|, \quad (1)$$

assuming we ignore small clustering effects. Indeed this is the explanation for the particular slope, which is close to 3, observed in the Poisson log-log scatter plot in Figure 6. The overall shape of the scatter plot for the real features is similar, although

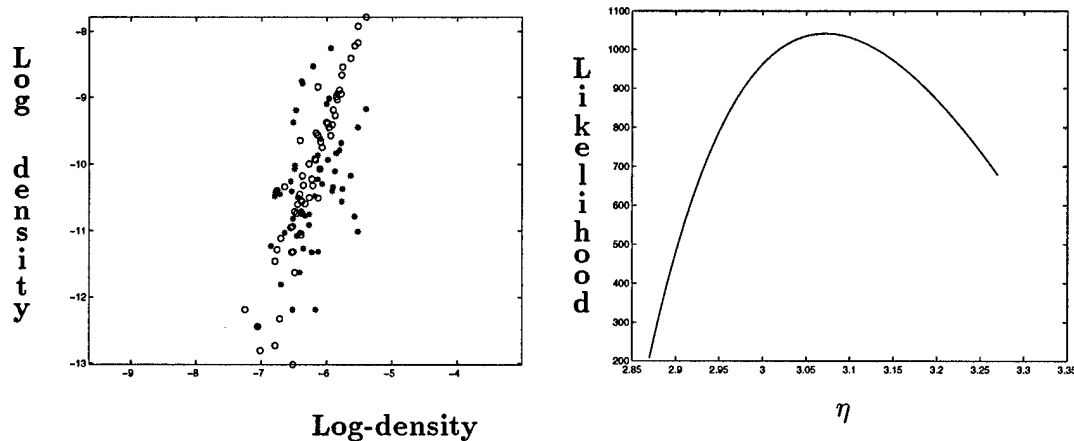


Figure 6: Left: Log-density of triples of local features versus log-density of individual local features, for both real local features ($\circ$) and Poisson data ($*$). Right: The log-likelihood curve for η .

there is naturally more variation. We replaced the exponent 3 in the expression for λ_{global} by a parameter η and estimated η by maximum likelihood based on the *counts* of the global arrangements. In the righthand panel of Figure 6 we show the log-likelihood curve for the seventy images; the maximum is nearly at $\eta = 3$ with negligible variance. For Poisson data the maximum is also at $\eta = 3$.

We hasten to add that there are important exceptions to this seemingly straightforward Poisson analogy. For example, if α_0 and α_1 are both horizontal groupings of horizontal edges, and if v_1 respects this orientation, then *long range correlations* become significant and affect the estimates given above. For example, with such local features, if $v_1 = (20, 0)$ and $v_2 = (10, -20)$, we obtained $\eta = 2.2$ and the number of detected triangles was extremely large.

5 Representing Objects

How well do the global arrangements represent classes of objects? The training data are registered to a fixed size reference grid in such a way that linear variability is essentially factored out. Given parameters N_{edges} and N_{pixels} , we first identify a collection of local features $\alpha_i, i = 1, \dots, N_{types}$, which are each “common” in a certain region of the object. This means it appears in a significant fraction of the training data within a fixed small neighborhood. Assume these neighborhoods are centered at points $y_i, i = 1 \dots, N_{types}$. We also insist that the neighborhoods be spread out over the entire object. In Amit et al. (1998) we describe a simple algorithm for finding such feature/neighborhood pairs which are common in registered training images and thereby verifying the “localization property” LII. This is the *only* training which takes place for visual selection. The computation time required for this training stage is on the order of *minutes* for several hundred training images.

Each triple $(i, j, k), 1 \leq i < j < k \leq N_{types}$, of selected local features determines a “model” triangle (y_i, y_j, y_k) . *The set of these triangles is the object representation.* The triangles provide a straightforward mechanism for incorporating invariance into the search for candidate bases. Given an image and a model triangle $\Delta = (y_i, y_j, y_k)$ for three local features $\alpha_i, \alpha_j, \alpha_k$, we search for all instances of these local features which form a triangle *similar* to the model triangle Δ up to small perturbations and a scaling of $\pm 25\%$. The image-wide search for similar triangles is equivalent to a search for a global arrangement with $v_1 = (y_j - y_i), v_2 = (y_k - y_i)$, and the size of $\mathcal{B}_1$ and $\mathcal{B}_2$ on the order of a hundred pixels. We shall make this somewhat more precise in the following section.

In Figure 7 we show 16 randomly deformed $\mathcal{Z}$ ’s, obtained from a prototype by applying a random low frequency non-linear deformation and then a random rotation and skew. We also show a smoothed version of the prototype with seven local features identified for this class of objects, and the first three deformed $\mathcal{Z}$ ’s with an instance of one of features. The images are *not* registered and the feature was detected on the

unregistered images. In a data set of 100 perturbed symbols all but one of these local features was found in over 35% of the symbols in the correct location.

5.1 False Negative Probabilities

In order to estimate false negative error rates we estimate the probability that a registered object does not have any of the triangles (with the vertices in their distinguished neighborhoods). This is equivalent to having less than three of the local features at the specified locations. First, for each $i = 1, \dots, N_{types}$, we compute the fraction of registered training images which have local feature α_i in a small neighborhood of y_i . Then, *assuming independence of these features on registered data*, and assuming the different fractions are approximately equal, we determine the false negative probability by a simple calculation using the binomial distribution. We can then choose N_{types} , the number of local features, in order to acquire the “coverage property” GI mentioned in Section 3 and maintain an acceptable level of error. We note that these estimates only require a small amount of training data since only the frequencies of local features are compiled and a degree of invariance is built in.

In Figure 8 we show frequencies of local features identified for faces in a training set of 300 faces as a function of N_{edges} and N_{pixels} . (The ranges for N_{edges} and N_{pixels} are the same as before.) The frequencies show a strong linear relation to the number N_{edges} of edges and the size of the regions, N_{pixels} . The R^2 after regression on these two variables was 93%. Similar numbers are observed for randomly deformed latex symbols.

The data suggest a rather consistent relationship among N_{edges} , N_{pixels} and the frequencies of the most common local features. Frequencies on the order of 50% lead to very low false negative rates with only order $N_{types} = 10$ local features. Clearly the local variability of the object class is crucial in determining these frequencies. However, it is not unrealistic to assume that, after factoring out linear variability, there are a good number of local groupings which appear in approximately 50% of

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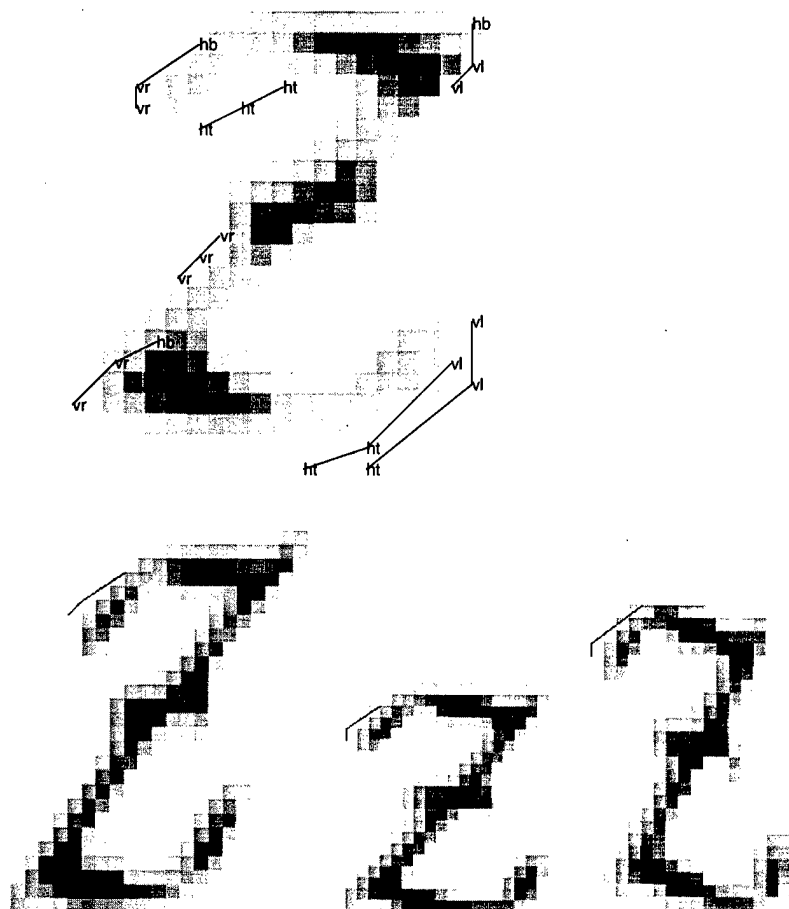


Figure 7: Top: Sixteen randomly deformed Z 's. Middle: Seven local features found on a prototype Z . The abbreviations "ht,hb,vr,vl" mean, respectively, horizontal edge brighter on top, horizontal edge brighter below, vertical edge brighter on the left, vertical edge brighter on the right. Bottom: Instances of the the top left local feature on 3 random Z 's.

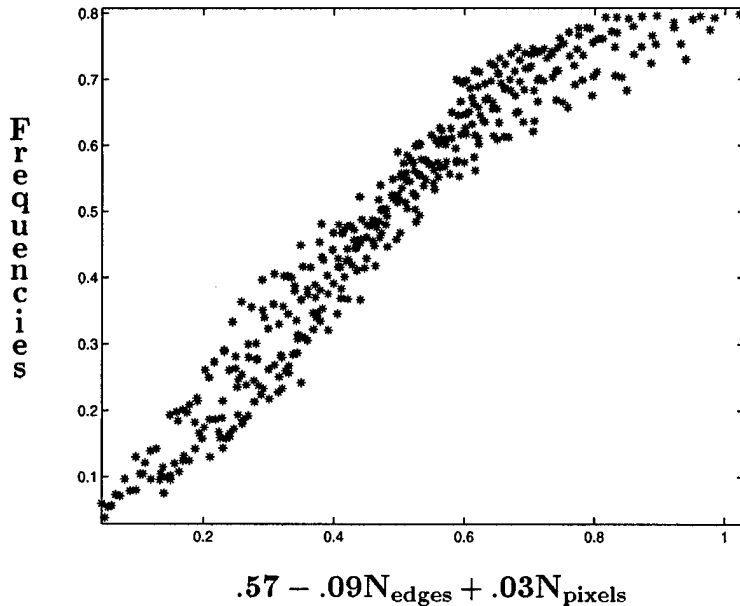


Figure 8: Frequencies of common local features on 300 faces as a function of the fitted regression on N_{edges} and N_{pixels}

the object images.

In the special case in which the object class is created from smooth deformations of a single prototype, as in the LaTeX experiments presented here, the stability of the features is directly related to N_{pixels} , the degree of disjunction. This is demonstrated in Figure 7, in which local features identified on a single smoothed version of the prototype are then found on various deformations of that prototype at the correct location.

5.2 False Positive Rates

False positive rates are expressed by the density of the global arrangements in generic images. Given the local densities and the near-Poisson nature of the corresponding point processes, one can obtain reasonable upper bounds on the densities of the global arrangements in generic scenes (see Section 4). The important constraint is that the size of the regions $\mathcal{B}_1, \mathcal{B}_2$ used in the image-wide search for the global arrangements be sufficiently large to guarantee the following property: If the registered ROI of a basis has at least three local features $\alpha_i, \alpha_j, \alpha_k$ somewhere in their distinguished

neighborhoods in the reference grid, then this ROI will in fact be “hit” in the sense of finding an instance of the corresponding global arrangement in the original image coordinates. As mentioned above this implies the size of the regions must be on the order of one hundred pixels.

5.3 Choosing the Parameters

In our experiments we used $N_{edges} = 3$ and $N_{pixels} = 10$. The density λ_{local} of the local features is then order 10^{-3} , and it follows from equation 1 that the density λ_{global} of the global arrangements is order 10^{-5} . In the experiments reported here and in Amit et al. (1998), we used $N_{types} = 9$ local features, which yields 84 model triangles. Hence, the density of detected candidate bases is order $84 \times 10^{-5} \sim 10^{-3}$, or approximately several tens per 100^2 pixels. Thus we see that, indeed, the conjunctions are very rare events in the background population, which is property GII in Section 3. In addition, as explained in Section 5.1, false negative rates can also be predicted from the model parameters $(N_{edges}, N_{pixels}, N_{types})$. Therefore, it is possible to choose these parameters in order to achieve specific constraints on false alarms, missed detections and computation time. Of course there are the usual tradeoffs. For example, if N_{edges} and N_{pixels} are held fixed, then increasing N_{types} increases the number of false alarms but decreases the false negative rate, and similarly for N_{pixels} .

5.4 Coarse-to-Fine Processing

Visual selection - the search for the global arrangements - is highly coarse-to-fine. The reason is that organization of each step is tree-structured. For example, the edge fragments are defined as conjunctions of comparisons of intensity differences, organized as a vine; the search is terminated as soon as one comparison fails. Similarly, the point process determined by a local grouping is a thinning of the point process corresponding to the central edge; if the second edge is not found in the sub-region determined by the central one (see Figure 2), the search is abandoned, and

so forth. Finally, the global arrangements are strictly scarcer than the constituent local groupings and this search also has an underlying tree structure. This explains why the spatial distribution of processing illustrated in Figure 1 is so asymmetric. In contrast, if a neural network is trained to detect faces at a reference scale and then applied to every (or many) subregions of the image, the corresponding distribution would be more or less flat.

6 Experiments

The selection of candidate bases is determined by an image-wide search for the particular global arrangements which represent the object class, as discussed above. Given a triple of local features $\alpha_i, \alpha_j, \alpha_k$ at locations y_i, y_j, y_k on the reference grid, the steps are the following

1. Precompute the locations of all local features in the image.
2. Assume N instances of local feature α_i in the image: $x_{i,1}, \dots, x_{i,N}$.
3. For $n = 1, \dots, N$, find all instances of α_j in $x_{i,n} + \mathcal{B}_1$; call these $x_{j,1}, \dots, x_{j,M}$ (M may be 0).
 - For $m = 1, \dots, M$, define $R_{x_{j,m}-x_{i,n}}$ to be the rotation determined by the vector $x_{j,m} - x_{i,n}$. For each instance of α_k at $x_k \in x_{i,n} + R_{x_{j,m}-x_{i,n}}\mathcal{B}_2$, determine the affine map T taking y_i, y_j, y_k into $x_{i,n}, x_{j,m}, x_k$.
 - Add (Tz_1, Tz_2, Tz_3) to the list of candidate bases.

The requirements for the regions $\mathcal{B}_1$ and $\mathcal{B}_2$ were described in Section 5.2. In our applications it was sufficient to take $\mathcal{B}_1$ at most 11×11 (to accommodate the required range of scales) and $\mathcal{B}_2$ at most 7×7 .

Final classification means assigning the label “object” or “background” to each candidate basis. This final disambiguation might be more computationally intensive

than selection; this was our experience with detecting faces. One reason is that final classification generally requires both geometric and grey level *image normalization* whereas visual selection does not, at least not in our scheme. In our experiments, geometric normalization means registering the ROI around the basis to the reference grid and greyscale normalization means standardizing the registered intensity data. Similar techniques have been used elsewhere. After normalization, one typically computes a fixed-length feature vector and classifies the candidates based on standard inductive methods (e.g., neural networks). The training set contains both “positive” examples from the object class and “negative” examples, which might be false positives from the selection stage. In our case we use regions-of-interest which are flagged by the triangle search in the types of generic images mentioned earlier.

We use classification trees for the final step. For detecting faces, we recursively partition registered and standardized data by comparing the normalized grey levels to thresholds. For detecting deformed LaTeX symbols, the splitting rules are based on the *registered* locations of the local features rather than on individual pixels. When a candidate basis is detected, the associated affine transformation maps the locations of the local features in the ROI of the candidate basis into the reference grid, yielding a binary feature vector with one component for each of the N_{types} types of local features and each pixel in the reference grid.

In Figure 9 we show detection experiments including both visual selection and final classification, for the LaTeX symbols $\&$ and $\mathcal{Z}$ and for faces. The two symbol detectors are trained with 32 samples. The test images are 250x250 artificial scenes which contain 100 randomly chosen and randomly placed symbols in addition to the target one which is not occluded. The negative training examples were extracted from real scenes not the artificial scenes illustrated in Figure 9; consequently, the detection algorithm is independent of the particular statistics or other properties of these synthetic backgrounds. The lefthand panels of Figure 9 show all bases detected in the selection phase. Observe that a basis represents a precise hypothesis regarding

the pose of the object. Processing time is approximately 20 seconds on a 166Mhz laptop pentium and 3 seconds on a Sparc 20.

For faces we trained on 300 pictures of 30 people (10 images per person) taken from the Olivetti database. The algorithm was tested on images from Rowley et al. (1998) (for example Figure 1), and images captured on the Sun Videocam (for example Figure 9). Processing time on a Sparc 20 is approximately .5 seconds per 100×100 subimage. All computation times reported include six applications of the algorithm at different resolutions obtained by downsampling the original image by factors ranging from 1 (original resolution) to $1/4$. About half of the processing time is spent in detecting the edges and the local groupings. Both operations are highly parallelizable.

In hundreds of experiments using pictures obtained from a videocam, a Sony digital camera and Rowley's (Rowley et al. (1998)) database the false negative rate of the visual selection stage is close to zero. However, faces are lost during final classification. The main reason seems to be that all 300 faces in the Olivetti training set have more or less uniform lighting. When faces appear with significantly different illumination, for example when the two halves of the face have very different mean intensities, the final classifier is likely to fail. Numerous results can be found at '<http://galton.uchicago.edu/~amit/faces>'.

7 Biological Vision

Our model was not conceived to explain how real brains function, although we have borrowed terms like "visual selection" and "foveation" from physiological and psychological studies in which these aspects of visual processing are well-established. In particular, there is evidence that object detection occurs in two phases - first searching for distinguished locations in a rather large field of view and then "focusing" the processing at these places. In this section we investigate some compelling links be-

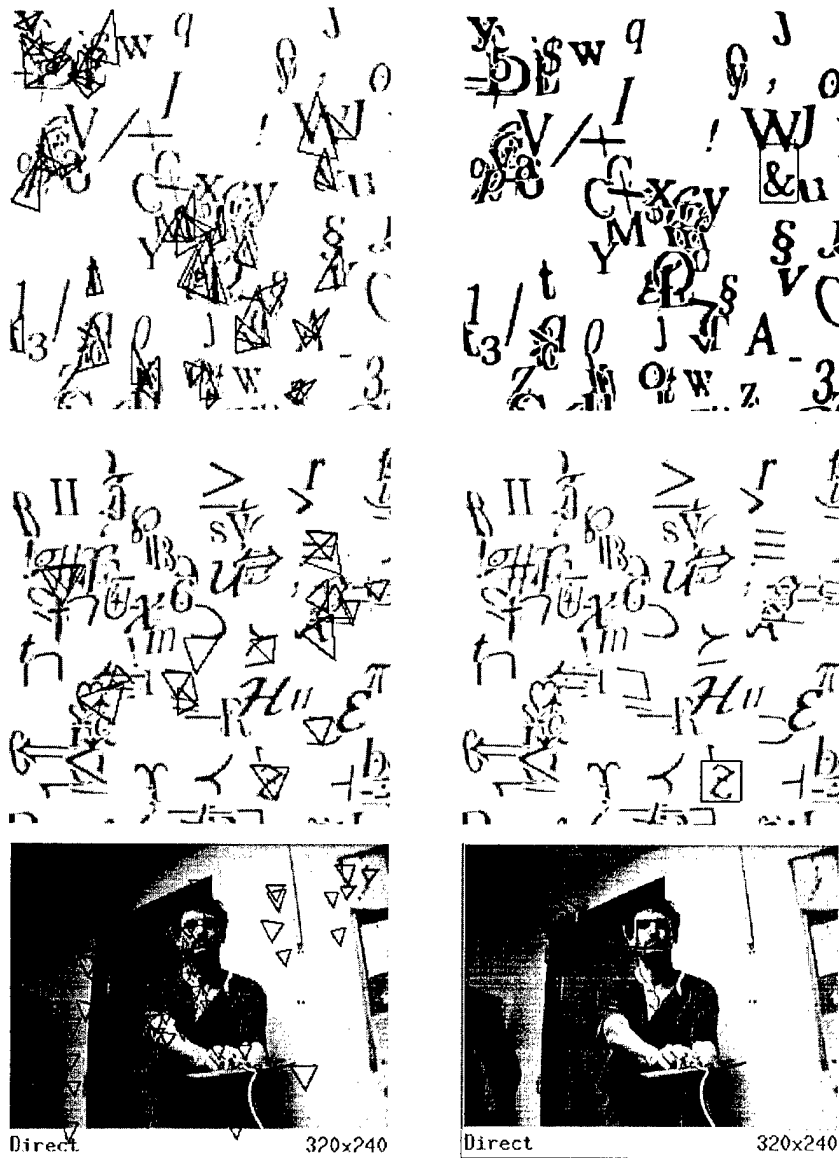


Figure 9: Top Left: All bases flagged by the &-detector. Top Right: Final decision. Middle - same thing for a Z detector. Bottom - same thing for the face detector.

tween our computational model and work on biological vision. We also consider an implementation using the architecture of artificial neural networks.

We have assumed that the only source of information for visual selection is grey level values from a single image; there is no color, motion or depth data. In other words, the procedure is entirely shape-based. It is obvious on empirical grounds that human beings analyze scenes without these additional cues. In addition, there are experiments in neuropsychology (e.g., Bulthoff & Edelman (1992)) which indicate that 3D information is not crucial.

Our selection model has three clearly distinct levels of computation:

- Level I - edge fragments;
- Level II - local groupings of fragments;
- Level III - global arrangements of local groupings.

Level I roughly corresponds to the basic type of processing believed to be performed in certain layers of V1 (Hubel (1988)). Level II involves more complex operations which might relate to processing occurring in V2; and Level III could relate to functions of neurons in IT. These connections are elaborated in the next two subsections.

7.1 Flexible Groupings and Illusory Contours

How regular are the grey level patterns which activate cells in the brain? There is evidence of cells in various areas which respond to rather general stimuli. For example, in V1 there are responses to edge-like patterns which are orientation-dependent but contrast-independent (Schiller, Finlay & Volman (1976)). And in von der Heydt (1995) there is a review of the neurophysiological evidence for V2 cells responsive to “illusory” or “anomalous” contours; even in V1 according to Grosz, Shapley & Hawken (1993). These cells respond equally well to an oriented line and to an occluded or interrupted line. They also respond to gradings which form the preferred orientation. Finally, cells in IT also respond to loose patterns and even to configurations

which are difficult to name (Fujita, Tanaka, Ito & Cheng (1992)). One interpretation of these experiments is that these cells respond to a *flexible* local configuration of edges constrained by loose geometrical relationships. Activation does not require a complete, continuous contour at a certain orientation; sufficient evidence for the presence of such a contour is enough.

This approach seems to be more robust and efficient than a finely-tuned search. Consider image contours arising from object boundaries and discontinuities in depth, lighting or shape. Such contours are often partially occluded or degraded by noise and therefore continuous contours may not be sufficiently stable for visual selection. Moreover, given that one observes a several nearby edge fragments of a certain orientation, it appears wasteful to attempt to “fill in” missing fragments and form a more complete entity. Since objects and “clutter” are locally indistinguishable, the additional information gain might be small compared, say, to inspecting another region. More specifically, detecting three approximately colinear horizontal edges in close proximity might be a rather unlikely event at a random image location, and hence might sharply increase the likelihood of some non-accidental structure, such as an object of interest. However, conditioned on the presence of these three edge fragments, and on the presence of *either* an object *or* clutter, the remaining fragments needed to complete the contour might be very likely to be detected (or very unlikely due to occlusion) and hence of little use in discrimination. The fact that the visual system at the very low levels of LGN responds to contrast and not to homogeneous regions of lighting is another manifestation of the same phenomenon. Finally, the computation of these flexible groupings is local and it is not difficult to imagine a simple feed-forward architecture for detecting them from edge fragment data.

7.2 Global Arrangements and Invariance

There is clear evidence for translation and scale invariance within certain ranges in the responses of some neurons in IT, (Lueschow et al. (1994), Ito, Tamura, Fujita &

Tanaka (1995)). Most of these neurons do not select highly specific shapes. This is demonstrated in the experiments in Kobatake & Tanaka (1994) and in Ito et al. (1995) where successive simplifications of the selective stimuli, and various deformations or degradations, still evoke a strong response. Moreover the time between the local processing in V1 and the responses in IT, which involve integrating information in a rather large field of view and at a large range of scales, is a few tens of milliseconds.

Suppose a neuron in IT responds to stimuli similar to the types of global arrangements discussed here, and anywhere in the receptive field and over a range of scales. Then the speed of the calculation is at least partially explained by the simplicity of the structure it is detecting, which is not really an object but rather a more general structure, perhaps dedicated to many shapes simultaneously. However, conditioned on the presence of this structure, the likelihood of finding an object of interest in its immediate vicinity is considerably higher than at a random location.

Put another way, the neurons in IT seem to have already overcome the problem of “moding out” scale, translation and other types of deformations and degradations. This would appear to be very difficult based on complex object representations. It is more efficient to use sparse representations for which it is easy to define those *disjunctions* needed for invariance. Scale and deformation invariance are achieved by taking disjunctions over the angles and distances between the local features; occlusion and degradation invariance are achieved by taking a disjunction over several spatial arrangements (the different triangles).

7.3 Segmentation

There is no segmentation in the sense of a processing stage which precedes recognition and extracts a rough approximation of the bounding contours of the object. The classical “bottom-up” model of visual processing assumes that edge information leads to the segmentation of objects. This is partly motivated by the widespread assumption that local processing carried out in V1 involves the detection, and possibly organi-

zation, of oriented edge segments (Hubel & Wiesel (1977), Hubel (1988)). However, edge detectors do not directly determine smooth, connected curves which delineate well-defined regions and it is now clear to many researchers in both computer and biological vision that purely edge-based segmentation is not feasible in most real scenes (von der Heydt (1995), Ullman (1996)), at least not without a tentative interpretation of the visual input.

7.4 Architecture

Our actual implementation of the visual selection algorithm is of course entirely serial. However, suppose we consider the type of multi-layer arrays of processors which are common in neural models and suppose a large degree of connectivity. Then what sort of architecture might be efficient for the detection of the types of global arrangements we have described? In particular, how would one achieve invariance to scale, translation and other transformations with a reasonable number of units and connections?

The required complexity seems considerable, particularly if we consider detecting many types of objects. Even for a single object class, a large number of arrangements might be needed to “cover” the class and accommodate a wide range of poses. Consider just “triangle” arrangements. Of course only a small fraction of all *possible* triangles of all *possible* local groupings provides information about an object class, i.e., has markedly different statistics in the object and background populations. Still, due to natural in-class variation and object positioning, there must be considerable flexibility in the shape of a triangle corresponding to a useful global arrangement.

One significant reduction in the degree of connectivity required to detect all the arrangements at all allowable variations can be achieved by “spreading the information” collected by the local feature detectors. Consider an auxiliary array of units arranged the same as the array of features detectors and with local connections between the two arrays. Suppose that when a unit in the detector array is activated

(by detecting a local feature) so does every unit in some neighborhood in the auxiliary array. If these neighborhoods are sufficiently large then for each instance of a global arrangement of three features α, β, γ found in the original detector arrays (as described in Section 6), there will be an instance of the *exact* model triangle, with the instance of the first feature coming from the detector array for α , and the other two from the auxiliary arrays for β and γ . The original search for all “similar” triangles can be replaced by a search for the single “model” triangle. This search will flag essentially the same arrangements as the original search in terms of the *first* local feature α in the triple. However, the other two are always in exactly the same relative location and hence information regarding scale or rotation is lost.

The number of connections needed for this coarser search is only on the order of thousands. The “master” unit dedicated to the arrangement needs to be connected to each unit u in the local detector array for say feature α and, for each such u , to exactly two other units in the auxiliary arrays for features β, γ , namely those which correspond to the other two vertices of the model triangle when it is translated to u . Moreover, the lost information about scale, rotation, etc. can be retrieved. The information about the true locations of the local features is preserved in the original detector arrays. Suppose $x_\alpha, x_\beta, x_\gamma$ are the three vertices of a detected model triangle in the auxiliary arrays. Then there must be an instance of local feature β in the detector array in the neighborhood of the unit situated at x_β , and similarly for γ . Since x_α is fixed, the search to recover the true triangle is local. The final output of visual selection - namely the set of candidate bases - is the same as before.

The detection of the local features themselves could be achieved by the same mechanism (spreading information). The only pose parameter in this case is the location of the edge fragment at the center of the local grouping. Some complex neurons in V1 are a simple example of such information spreading, where the original local features are highly localized oriented edges detected by the simple neurons in V1. The question is whether this phenomenon occurs at higher levels as well, with

more complex local features, and whether this is indeed the means by which the brain achieves scale invariance.

7.5 Multiple Object Classes

Remarkably, real brains manage to parse full scenes and perform rapid visual selection when *no specific detection task is specified*, i.e., no prior information is provided about objects of interest. Clearly at least thousands of possible object classes are then simultaneously considered. Perhaps context plays a significant role; see Biederman (1981) and Palmer (1975).

More modestly, how might a computer algorithm be designed to conduct an efficient search for say tens or hundreds of object classes? Ideally, this would be done in some coarse-to-fine manner, in which many object classes are *simultaneously* investigated, leading eventually to finely-tuned distinctions. Clearly, efficient indexing is crucial (Lowe (1985)).

Although we have concentrated here on a single object class, it is evident that the representations obtained during training could be informative about many objects. Some evidence for this was discussed in Amit & Geman (1997) in the context of “shape quantization”; decision trees induced from training data about one object class were found to be useful for classifying shapes never seen during training.

We are currently trying to represent multiple object classes by arrangements of local groupings in much the same manner as discussed in this paper for a single object class. The world of spatial relationships is exceptionally rich and our previous experience with symbol detection is promising. We expect the number of arrangements needed to identify multiple classes, or separate them from each other, will grow logarithmically with the number of classes. The natural progression is to first separate all objects of interest from “background” and then begin to separate object classes from one another, eventually arriving at very precise hypotheses. The organization of the computation is motivated by the “twenty questions paradigm”; the processing

is tree-structured and computational efficiency is measured by mean path length.

8 Conclusion

The main strengths of the proposed model are stability, computational efficiency, and the relatively small amount of training data. For example, in regard to face detection, we have tested the algorithm under many imaging conditions, including "on-line" experiments involving a digital camera in which viewing angles and illumination vary considerably. It is likely that the algorithm could be accelerated to nearly real-time. One source of these properties is the use of crude, image-based features rather than refined, model-based features; any "sub-classification" problems are eliminated. Another source is the explicit treatment of photometric and geometric invariance. And finally there is the surprising uniformity of the "statistics" of these features in both object and background populations, which can be learned from a modest number of examples, and which determine error rates and total computation.

The main limitations involve accuracy and generality. First, there is a non-negligible false negative rate (e.g., five percent for faces) if the number of regions selected for final classification is of order 10-100. This is clearly well below human performance, although comparable to other detection algorithms. Second, we have not dealt with general poses or 3D aspects; whereas scale and location are arbitrary, we have by no means considered all possible viewing angles, nor the effects of occlusion. Finally, our model is dedicated to a specific object class and does not account for general *scene parsing*. How is visual selection guided when no specific detection task is required and a great many objects of interest, perhaps thousands, are simultaneously spotted?

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