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EFFECTS OF ARTIFICIAL CRACKS
AND POISSON'S RATIO UPON PHOTOELASTIC
STRESS INTENSITY DETERMINATION

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| 16. Abstract
<p>/ A series of stress freezing photoelastic experiments were performed with multiple replications upon edge cracked strips for three types of "cracks" in current use: i) Rectangular slots 0.152 mm wide, ii) 1.59 mm wide slots terminating in a 30° vee notch of approximately 0.025 mm root radius, and iii) Natural cracks (approximately 0.0025 mm root radius). Stress intensity results were compared with the Gross-Srawley Analysis; in addition (i) was compared with Savin's solution. It was concluded that (ii) and (iii) yield the same results but (i) was slightly higher. Both (ii) and (iii) were about 12% higher than the Gross-Srawley results. This is conjectured to be related to a Poisson's Ratio Effect.</p> | | |
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LIST OF SYMBOLS

r, θ	Polar coordinates as defined in Figure 1 (mm, rad)
x, y	Cartesian coordinates as defined in Figure 1 (mm)
σ_{ij}	Stress Components $i, j = 1, 2$ (KPa)
ϵ_{ij}	Strain Components $i, j = 1, 2$ (mm/mm)
u_i	Displacement Components $i = 1, 2$ (mm)
$\tau_{\max}$	Maximum in plane shearing stress (KPa)
K_I	Mode I Stress Intensity Factor (KPa-m ^{1/2})
K_{AP}	Apparent Mode I Stress Intensity Factor (KPa-m ^{1/2})
	$K_{AP} = \tau_{\max}(8\pi r)^{1/2}$
K_{TSCM}	Estimated K_I by TSCM (KPa-m ^{1/2})
s	Length along curved path (mm)
g_I	Mode I strain energy release rate (J/m ²)
E	Modulus of Elasticity (GPa)
ν	Poisson's Ratio

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Introduction

The idea of obtaining stress intensity factors (SIF) from photoelastic results was suggested by G. R. Irwin [1] in the early 1950's. Since that time, a number of investigators have contributed to efforts to obtain SIF values from photoelastic data. The early work of Post and Wells and Post [2], [3] studies by Fessler and Mansell [4], by Marloff et al [5], by Liebowitz, Vanderveldt, and Sanford [6], by Kobayashi and his associates [7], [8], [9] and recently by the senior author and his associates [10]-[25] has led to both a clarification and means for overcoming difficulties associated with application of the method. The most important current difficulties appear to be:

- i) Accuracy with which the SIF may be extracted from photoelastic data.
- ii) A means for constructing "artificial" cracks of known geometry and their susceptibility to finite deformation effects in stress freezing.
- iii) The influence upon local constraint of the high Poisson's Ratio ($\nu \approx 0.5$) encountered in stress freezing work.

Over a period of five years, the senior author and his associates have evolved a technique for extracting the stress intensity factor directly from photoelastic data, without resorting to stress separation methods. This approach met with success in dealing with three dimensional Mode I problems. The technique employs a representation of the maximum in-plane shearing stress as a singular term plus a Taylor series to account for effects of the regular stress field in the data zone. Referred to as a Taylor Series Correction Method (TSCM), it is described elsewhere [16], [17], [19], [20] and is believed to be useful in overcoming the difficulty noted in Item i).

An extensive photoelastic investigation of crack-like notches was conducted by Dixon and Strannigan [26] some years ago. However, the thrust

of this work was not directed towards direct SIF determination. Recently, Gross and Mendelson [27] found analytically that vee notches of 30° or less would simulate notch tip stress fields which lead to agreement to within 2% of SIF values for natural cracks. This led the senior author to examine various vee notch angles photoelastically for compact tension specimens [18]. His results confirmed the findings of Gross and Mendelson but the confirmation was done primarily at room temperature.

The writers have had occasion to employ "artificial" cracks in several instances in order to achieve uniform and repeatable crack geometries. In so doing, they have found two types of notches convenient to use:

a) A 0.152 mm wide rectangular tipped slot

b) 1.59 mm wide slots terminating in a vee notch of approximately 0.025 mm root radius. A primary goal of this study is to assess how well these notches simulate natural cracks in stress freezing work.

When one conducts stress freezing experiments, care must be taken to avoid gross field finite deformations. Moreover, for a cracked plate of finite thickness, a state of nearly plane strain exists near the crack tip. However, remote from the crack tip the states of stress and deformation are well characterized by generalized plane stress. Since a zone of transition must lie between these extremes, the problem becomes three dimensional and thus dependent upon Poisson's Ratio. Since all stress freezing materials exhibit a value of Poisson's Ratio of ≈ 0.5 , and since $\nu \approx 0.3$ for most structural materials, the influence of the "artificially" elevated value of Poisson's Ratio needs to be examined. A secondary goal of this paper is to examine this effect.

Analytical Considerations

Although these topics are treated elsewhere in the open literature, a brief discussion of concepts applied to the present study is included here

for convenience.

The TSCM [16][17][19][20] - As is well known, the elastic stress field surrounding the crack tip can be expressed, for the Mode I case as:

$$\sigma_{ij} = \frac{K_I}{(2\pi r)^{1/2}} f_{ij}(\theta) \quad \dots i, j = x, y \dots \quad (1)$$

with the notation given in Figure 1. By substituting Equation 1 into Equation 2

$$\tau_{\max} = 1/2 \left[(\sigma_x - \sigma_y)^2 + 4\tau_{xy}^2 \right]^{1/2} \quad (2)$$

one obtains

$$\tau_{\max} = f(r, \theta, K_I) \quad (3)$$

and since, for Mode I loadings, the fringe loops tend to spread in a direction approximately normal to the crack surfaces (Figure 2), we may evaluate $\tau_{\max}$ along $\theta = \pi/2$, yielding

$$\tau_{\max} = \frac{K_I}{(8\pi r)^{1/2}} \quad (4)$$

Moreover, since the stress-optic law prescribes

$$\tau_{\max} = \frac{nf}{2t} \quad (5)$$

a relationship of the fringe order to K_I is established. In obtaining data along $\theta = \pi/2$ some of the points may be far enough away from the crack tip to be influenced by the regular stress field. In order account for this, we use a Taylor series to represent the regular part of the stress field. Thus,

$$\tau_{\max} = \frac{K_I}{(8\pi r)^{1/2}} + \sum_{N=0}^M B_N r^{N/2} \quad (6)$$

becomes the equation to which values of K_I are fitted by a least squares process in TSCM. This result corresponds to the Williams Stress Function

for two dimensional problems and reduces to the Irwin two parameter method. to within truncation error for a three term expression for $\tau_{\max}$.

Poisson's Ratio Effect [28][29][30]

The experimentally determined SIF for a plate containing a through crack is known [28][29] to yield a higher result than the corresponding two dimensional solution. This difference in SIF values is due to the fact that a constraint develops near the crack tip in the experiment since the plate thickness is much greater than the crack root radius and a state of nearly plane strain results local to the crack tip. At distances which are substantially larger than the thickness from the crack tip, a state of nearly generalized plane stress will result. As noted earlier, a zone of transition will exist between these extremes, resulting in a three dimensional problem. Brown and Srawley [29], and Irwin [30], have pointed out that the two dimensional result can be converted to the three dimensional SIF by multiplying the SIF by $(1 - \nu^2)^{-1/2}$. A rationale for this conversion can be constructed as follows:

Consider the Mode I traction loaded cracked plate of Figure 3. Rice [31] has identified an integral:

$$J = \int [U dy - \sigma_i \frac{\partial u_i}{\partial x} ds] \quad (7)$$

where $U = \frac{1}{2} \sigma_{ij} \epsilon_{ij}$, the strain energy density,

u_i = displacement components

σ_i = stress vector components

which is independent of path for two dimensional problems. Moreover, if the strain energy density is a quadratic function of the strains, the J integral is identical to the strain energy release rate g.

If we compute J_I for Path A, which is located at distances substantially larger than the plate thickness from the crack tip, the result will be approximately the strain energy release rate for plane stress as computed by Paris and Sih [32]. Thus

$$J_I = g_I \approx \frac{K_{IA}^2}{E} \quad (8)$$

On the other hand, locating the path B within the constrained region, we would expect our result to be approximately the plane strain g value, or

$$J_I = g_I = \frac{(1 - \nu^2)K_{IB}^2}{E} \quad (9)$$

For J_I to be path independent, it follows that $K_{IB} = (1 - \nu^2)^{-1/2} K_{IA}$.

In real plate problems the thickness is finite, and the preceding conversion becomes a maximum conversion factor. If the thickness is large relative to the lateral dimensions of the body, no conversion would be required. It is only where the thickness is substantially less than the lateral dimensions of the body that the two dimensional solution will agree with the plane stress result.

Alternatively, if we multiply the SIF measured photoelastically at the crack tip by $(1 - \nu)^{1/2}$, we get the SIF which corresponds to the two dimensional solution for a thin plate. In stress freezing work, $\nu = 0.5$ and if we wish to obtain the test result which would correspond to Poisson's ratio ≈ 0.3 , we can convert the two dimensional result back to the test result form using the inverse of the above conversion. Our complete conversion factor is then:

$$\frac{[1 - (0.5)^2]^{1/2}}{[1 - (0.3)^2]^{1/2}} = 0.91$$

for correcting the "plane strain" test result for the fact that Poisson's Ratio was different for the test material than for the prototype structural material. This effect is further verified in [33].

The Experiments

A series of stress freezing photoelastic experiments were designed using an edge cracked strip as the test model. This model was selected because, due to bending effects and lack of gross constraint, it was very sensitive to small load changes and also because accurate analytical solutions such as that of reference [34] were available. The basic specimen geometry and loading is pictured in Figure 4 together with the three types of cracks studied. Beginning with stress free strips of PSM-8 (Photolastic, Inc.) natural cracks were tapped into the plate edge, while the "artificial" cracks were inserted with circular saws. Specimens were then placed in the stress freezing oven in a string loaded tensile load rig as indicated in Figure 4. After heating to critical temperature and soaking to achieve uniform temperature, loads were applied and the specimens were cooled under load. Two load levels were employed. One load level corresponded essentially to about 80% of the threshold value for slow crack growth of the natural crack, and, twice this load was also used for the artificial cracks. For natural cracks, half of this load or 40% of the threshold value was also employed. A summary of the tests run together with average data values are found in the upper part of Table I.

The frozen slices were then coated with an oil of the same index of refraction as the model material and inserted into the field of Photolastic Model 051 Slice Analyzer for fringe order determination along a line normal to the crack surfaces and passing through the crack tip.

In addition to the stress freezing tests, tests were conducted on Vee-notched and naturally cracked specimens at room temperature at which the material's Poisson's Ratio was 0.36.

Results and Discussion

A set of test data from one of the V-H tests (Table I) are plotted in Figure 5 which may be regarded as typical for all tests. This plot of normalized apparent SIF, $K_{Ap}/\sigma(\pi a)^{1/2}$ vs $(r/a)^{1/2}$ is used to interpret the data and to extrapolate the portion of the data in the appropriate zone to obtain the SIF. In his discussion [1] Irwin pointed out that at least two parameters were necessary to obtain the SIF in a two dimensional problem. This leads to an equation for τ_{max} which corresponds to Equation 6 with $M = 0$. Moreover, it implies that a plot of the data such as given by Figure 5 should yield a straight line in the zone dominated by the singular stresses. Thus, in the present study, M was set equal to zero in the computer program and only the data in Zone II of Figure 5 were used in obtaining K_{TSCM} .

In Zone I, effects of the regular stress field are significant; and in Zone III, recent studies [25] indicate that the stress relaxation here is due to material non-linearity near the crack or notch tip. Zone II occurred in the same r/a range for all crack geometries.

From a study of the average values of $\left[\frac{K_{TSCM}}{K_{Th}} \right]$ in Table I, it is concluded that all experimental results were higher than predicted by the two dimensional theory with the rectangular cracks exhibiting SIF values of over 20% above analytical results. The vee notches and the natural cracks yielded essentially the same results which averaged 12% above the two dimensional solution. Since the SIF reproducibility of the "artificial" cracks was to within $\pm 2.5\%$ and for the natural cracks $\pm 4\%$, the above results clearly represent a definite data trend.

Upon applying the conversion factor of 0.91 noted earlier to the test results, the natural and vee-notch cracks agree with the two dimensional solution to within $\pm 3\%$ for the stress freezing tests and within 1% for the room temperature tests. The rectangular slots, however, still average 10% above the two dimensional solution.

The rectangular slot was studied by Schroedl and Smith [24]. Using their computer program for Savin's solution, the authors constructed Figure 6. From this graph it is clear that, if data in the $(r/a)^{1/2}$ range of 0.2 to 0.4 are linearly extrapolated to the origin for the rectangular slot, $(b/a = 0.006)$ a normalized SIF results which is about 6% greater than for the line crack. The balance of the difference (Table I) is attributed to finite deformation effects at the higher load.

By comparing Figures 5 and 6, it is clear that the singularity introduced by the presence of the square corner in Figure 6 is absent from Figure 5. This is believed to be due to the fact that material nonlinearities develop in the zone of high K_{AP}/K_{Th} values. However, in any case, one can still obtain valid values of the SIF with rectangular slots at lower loads by taking data outside of $(r/a)^{1/2} \approx 0.3$ to 0.4 provided the data are linear there.

The rather significant Poisson's Ratio effect noted here in stress freezing work on two dimensional problems naturally raises the question as to the extent of this effect in three dimensional problems where generalized plane stress does not exist away from the crack tip. By studying existing approximate solutions to such problems such as [35] one can conjecture that the effect will generally be less than the usual experimental error of 5%. More exact information, however, will require further study.

It is noted that only one plate thickness was studied here and the authors hope to extend their results to other thicknesses in future work.

Summary and Conclusions

A stress freezing photoelastic study was carried out on a series of edge cracked strips containing three types of cracks. It was concluded that:

- i) 1.59 mm wide slots terminating in a 30° vee notch of approximately 0.025 mm root radius yield essentially the same SIF values as natural cracks.
- ii) Test results can be replicated to within $\pm 4\%$.
- iii) The effect of Poisson's Ratio in a stress freezing plate test is significant and should be accounted for when comparing results with two dimensional solutions. An approximate means for doing this is described.
- iv) Rectangular slots 0.152 mm wide tend to give SIF values which are some 10 percent higher than vee notch or natural crack results. This effect can be alleviated by utilizing data further from the crack tip provided the data are still linear in Fig. 5 and by keeping loads quite small.

The present studies were quite restrictive in terms of both test and crack geometries. However, it is hoped that useful quantitative information on photoelastic stress intensity determination has resulted. Studies directed to improve the accuracy of the method are continuing.

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TABLE 1
Test Results for Edge Cracks

	Stress Freezing Tests							Room Temperature Tests	
	R-H	R-L	V-H	V-L	N-H	N-L	V	N	
Type of Notch									
Number of Replications	5	1	5	2	2	1	2	1	
Remote Stress kPa	70.3	42.2	76.4	43.04	34.6	21.1	3053	2352	
$\left[\frac{K_{TSCM}}{K_{Th} a} \right]_{avg}$	1.25	1.18	1.12	1.14	1.08	1.13	1.02	1.03	
$\left[\frac{K_{TSCM}}{K_{Th} a} \right]_{Range}$	1.23 to 1.29		1.08 to 1.15	1.11 to 1.17	1.04 to 1.12		1.00 to 1.04		
$\left[\frac{K_{TSCM}}{K_{Th} a} \right] \frac{(1-\nu^2)^{1/2}}{0.955^+}$	1.13	1.07	1.02	1.03	0.97	1.02	0.99	1.00	

a - Theoretical SIF Gross-Srawley Solution
Average Material fringe value 254 N/m/order

R-H Rectangular-High Load
R-L Rectangular-Low Load
V-H Vee-High Load
V-L Vee-Low Load
N-H Natural-High Load
N-L Natural-Low Load

$$+0.955 = \{1 - [0.3]^2\}^{1/2}$$

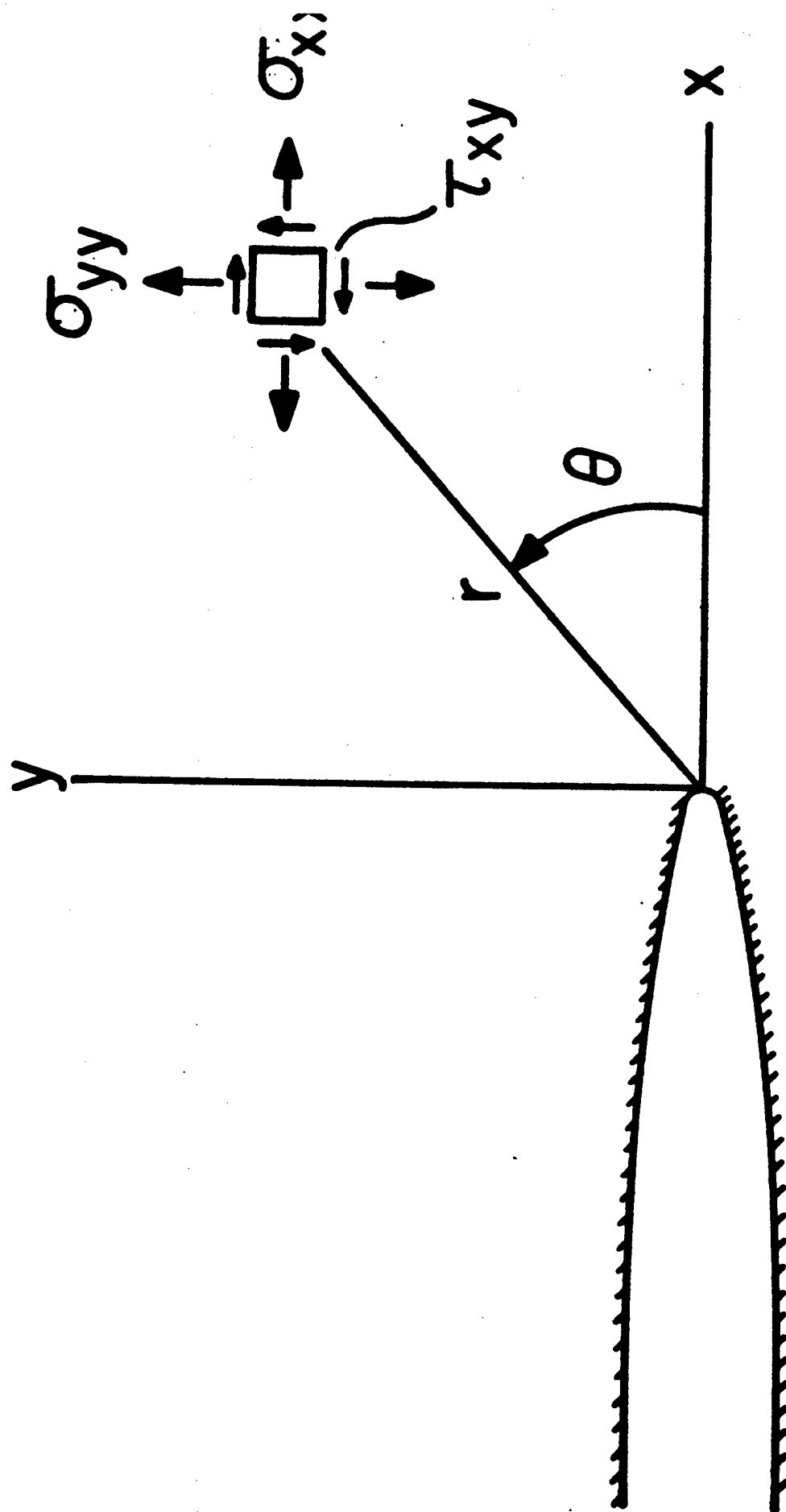


Figure 1. Notation

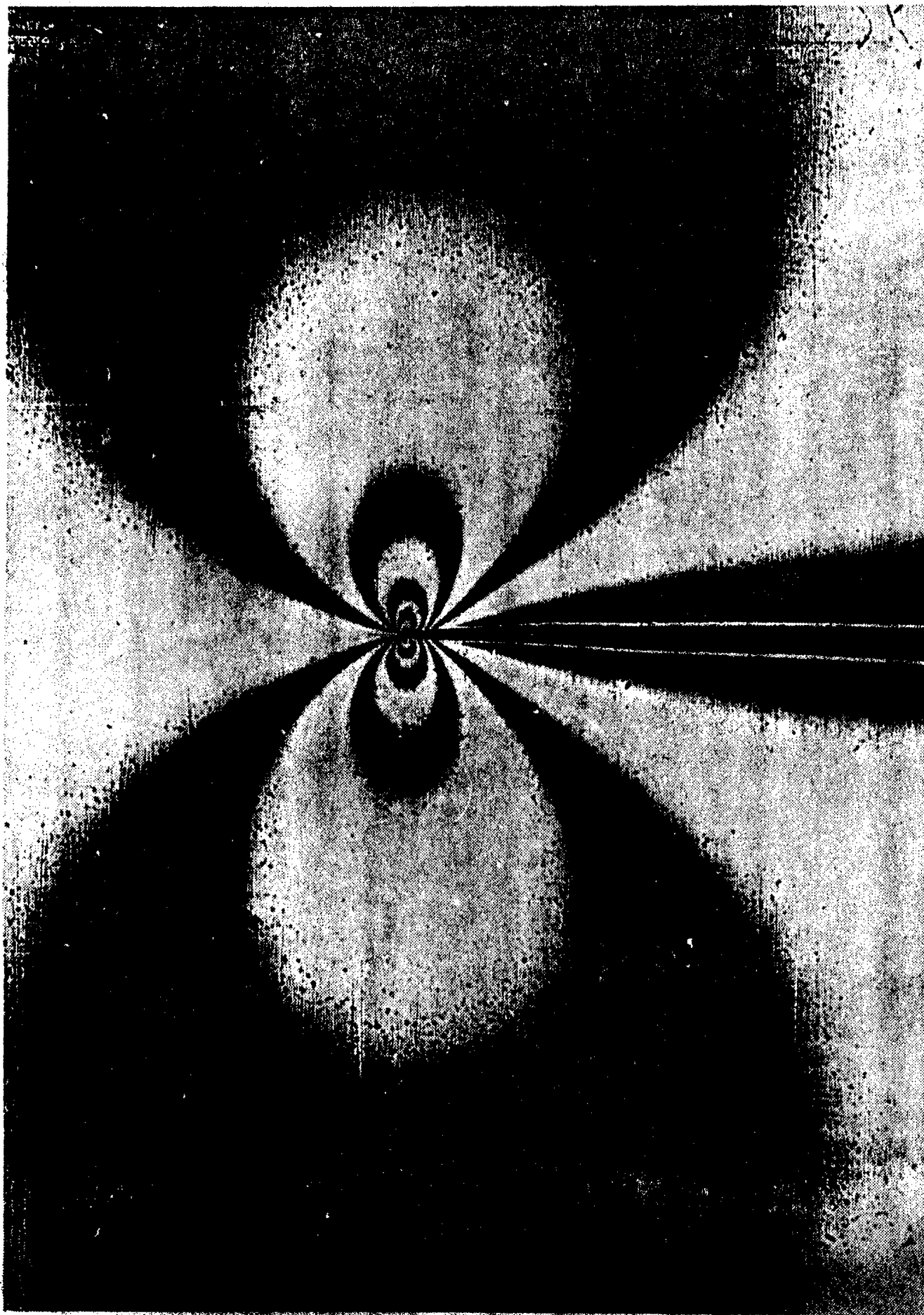


Figure 2. Spreading of Fringes Normal to Crack Plane (Mode I)

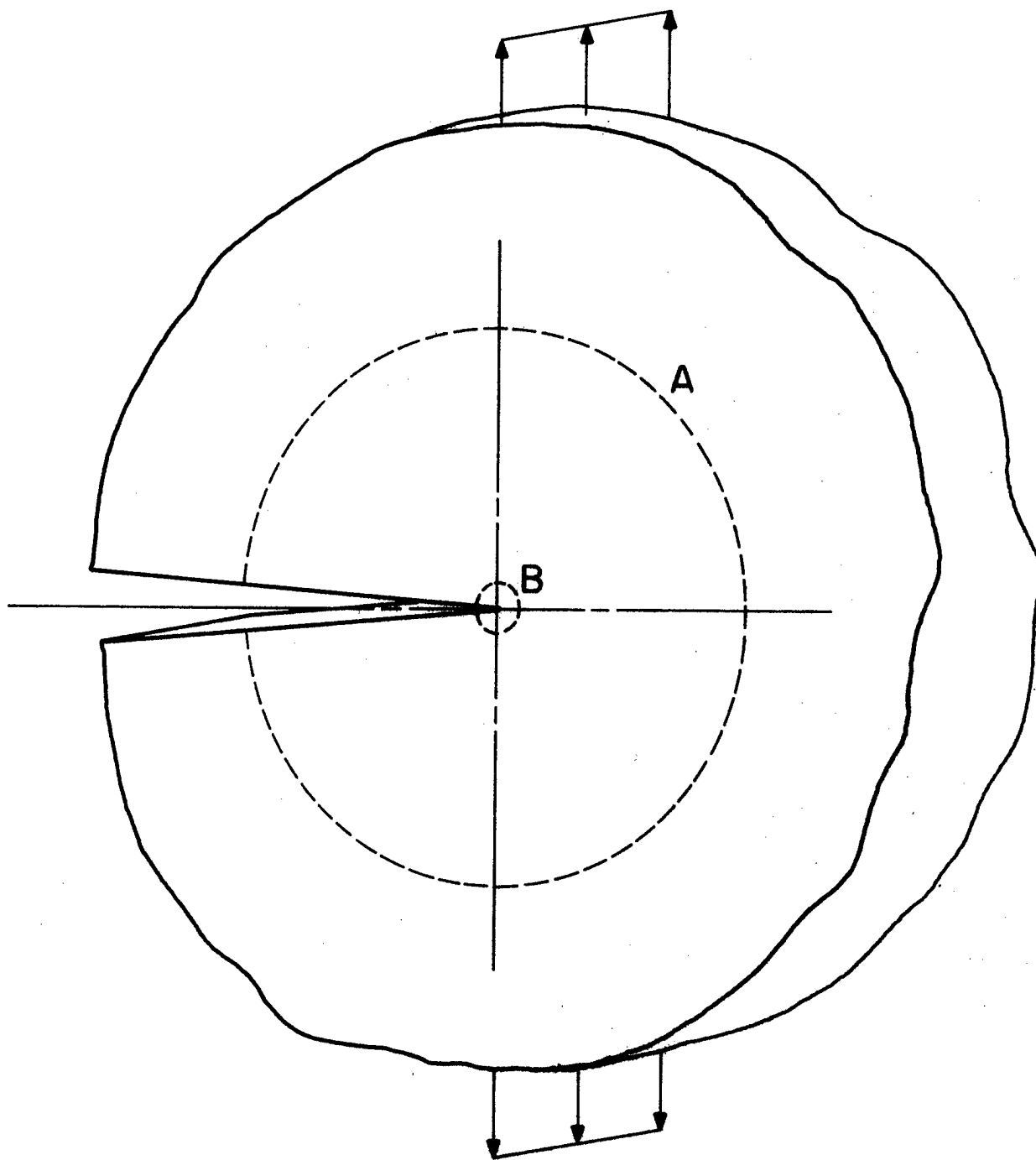
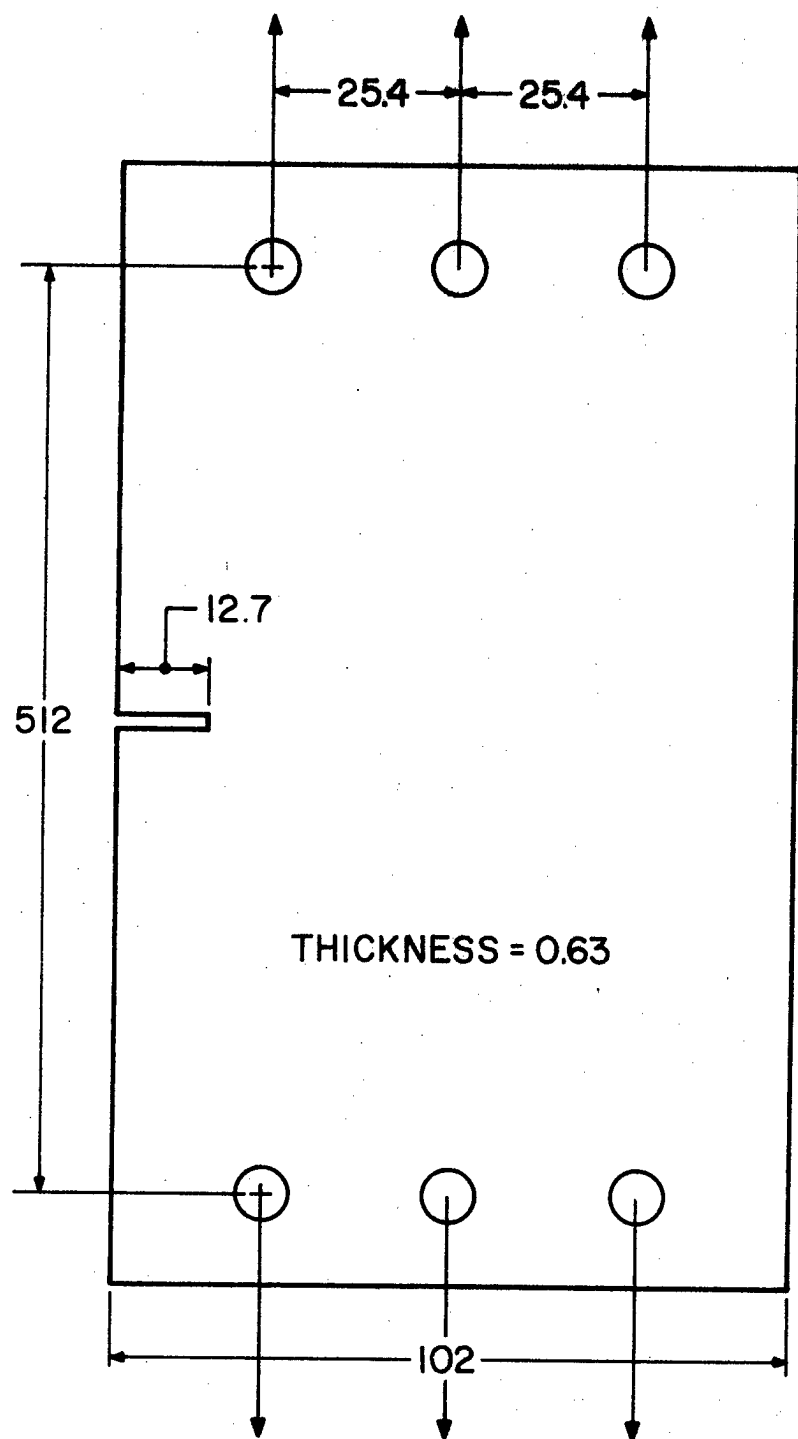
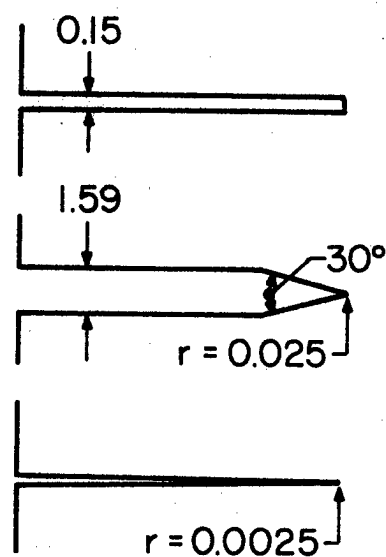


Figure 3. Generalized Plate Specimen



CRACK GEOMETRIES



ALL DIMENSIONS
IN MILLIMETERS

PLATE DIMENSIONS ARE
NOMINAL DIMENSIONS

Figure 4. Specimen Geometry and Loading.

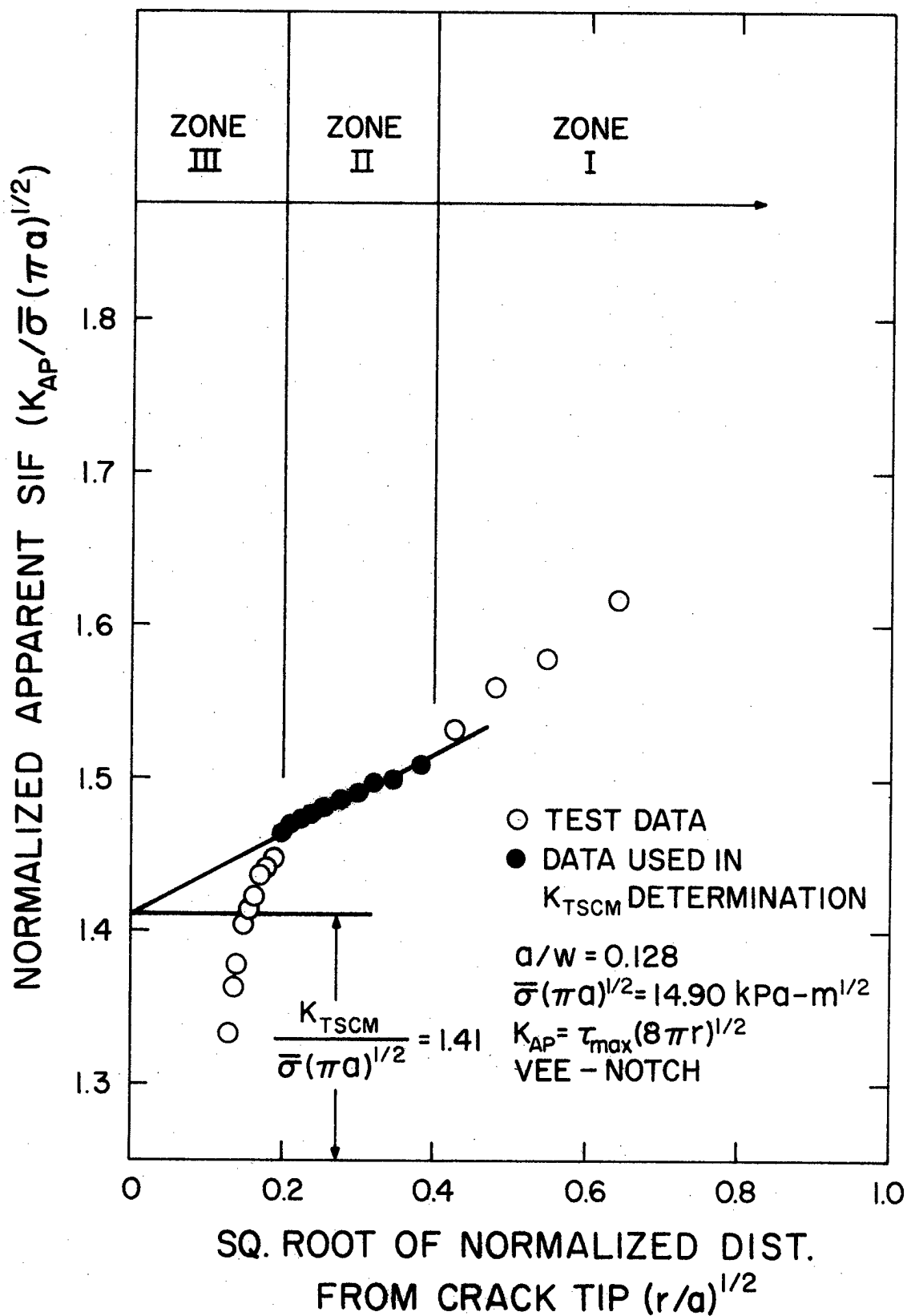


Figure 5. Normalized K_{AP} vs $r^{1/2}$ A Typical Result

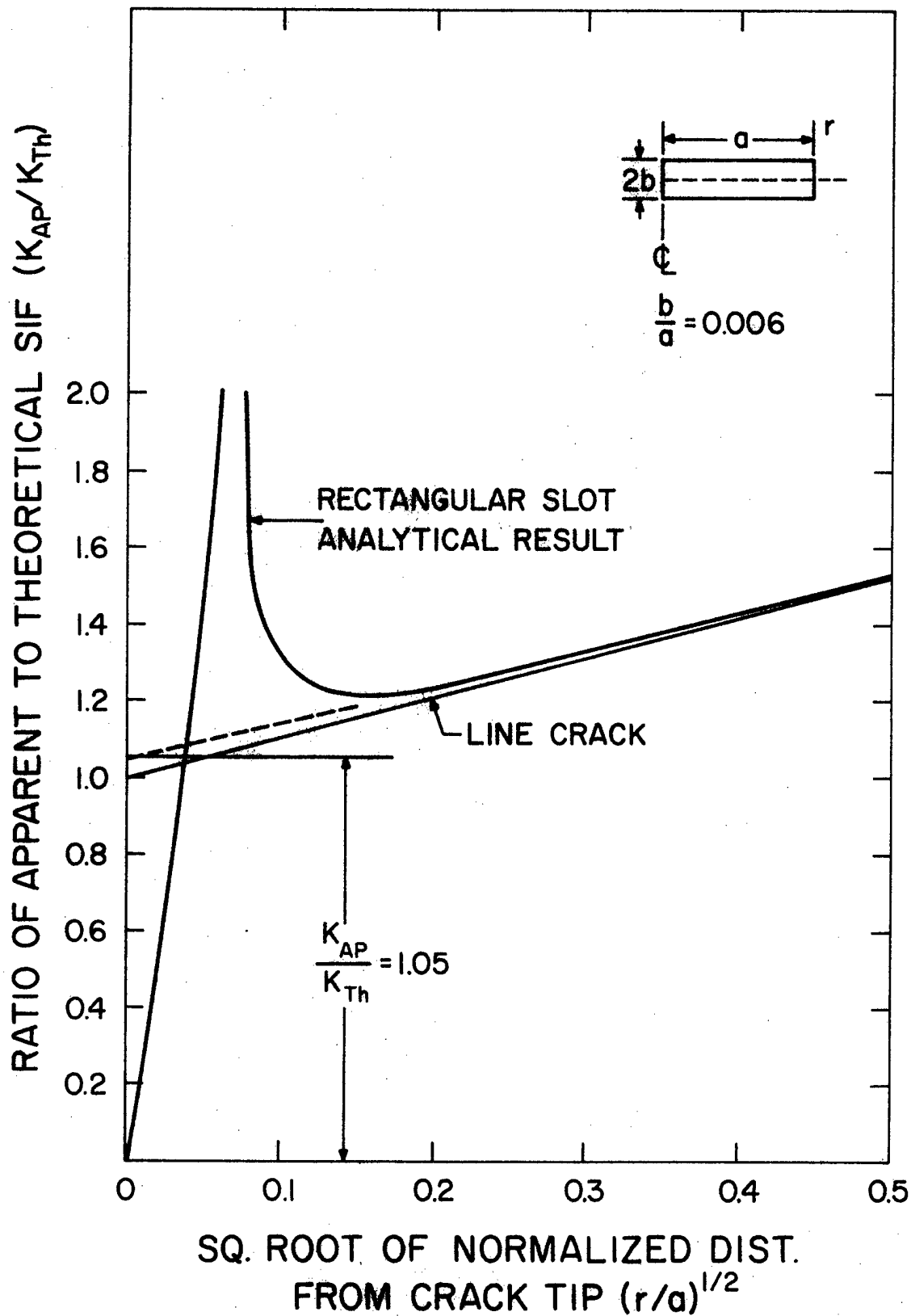


Figure 6. Normalized K_{Ap} vs $r^{1/2}$ Rectangular Slot

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